

# The Scraps of Imagination : A Catalog of Spatio Angular Aberations and Anomalies

0-9

$$\text{Solve}\left[\left(\left(\left(\sqrt{\left(-1.1294090667581471\theta^{18} + 8.987551787368176\theta^{16} + 3.5481432270250993\theta^{18}\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2\right)}\right)\right)\right)/\right. \\ \left.\left(\sqrt{\left(-12.566370614359172\theta + \theta^2 + 39.47841760435743\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2\right)}\right)\right)\right]^{\wedge}x + \\ \left(\frac{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - 2\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta}{2\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}\right)^{\wedge}y == \\ \left(\frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]}{\theta}\right)^{\wedge} \\ z, x] \\ \{\{\}\}$$



$$\begin{aligned}
 & \text{Solve} \left[ \left( \left( \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3.5481432270250993 \cdot \theta^{18} \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right]^2 \right) \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \right. \right. \right. \\
 & \quad \left. \left. \left. \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right]^2 \right) \right) \right) \right)^{\wedge} x + \\
 & \quad \left( \frac{4\pi \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 - 2 \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta}{2 \sqrt{4\pi \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}} \right)^{\wedge} y == \\
 & \quad \left( \frac{2\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right]}{\theta} \right)^{\wedge} z, z] \\
 & \left\{ \left\{ z \rightarrow - \left( 1. \log \left[ 2.^{-1. y} \left( \frac{-\frac{78.9568}{12.5664 - 1. \theta} + \frac{496.1}{(12.5664 - 1. \theta) \theta}}{\sqrt{\frac{496.1}{12.5664 - 1. \theta} - \frac{39.4784 \theta}{12.5664 - 1. \theta}}} \right)^y + \right. \right. \right. \\
 & \quad \left. \left( \left( \sqrt{(-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} (12.5664 - 1. \theta) \theta + 8.98755 \times 10^{16} \theta^2)} \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{-12.5664 \theta + 1. (12.5664 - 1. \theta) \theta + \theta^2} \right)^x \right] \right) / \left( -1.83788 - 1. \log \left[ \frac{1}{\theta} \right] \right) \right\}
 \end{aligned}$$

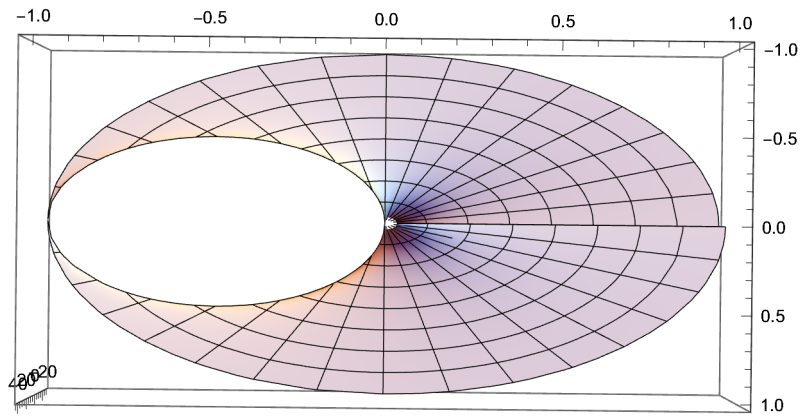
$$\text{Solve} \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} == \frac{2\pi \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}}, r \right]$$

$$\left\{ \left\{ r \rightarrow -\frac{4\pi^2 \sin[\beta]}{(4\pi - \theta)\theta} \right\}, \left\{ r \rightarrow \frac{4\pi^2 \sin[\beta]}{(4\pi - \theta)\theta} \right\} \right\}$$

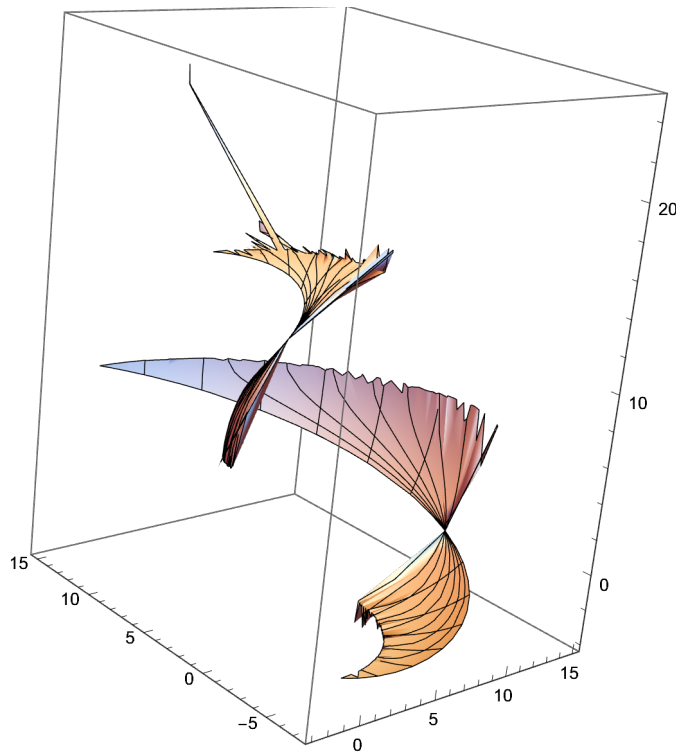
$$\text{Solve} \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} == \frac{2\pi \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}}, \theta \right]$$

$$\begin{aligned}
 & \left\{ \left\{ \theta \rightarrow \frac{2 \left( \pi r - \sqrt{\pi^2 r^2 - \pi^2 r \sin[\beta]} \right)}{r} \right\}, \left\{ \theta \rightarrow \frac{2 \left( \pi r + \sqrt{\pi^2 r^2 - \pi^2 r \sin[\beta]} \right)}{r} \right\}, \right. \\
 & \left. \left\{ \theta \rightarrow \frac{2 \left( \pi r - \sqrt{\pi^2 r^2 + \pi^2 r \sin[\beta]} \right)}{r} \right\}, \left\{ \theta \rightarrow \frac{2 \left( \pi r + \sqrt{\pi^2 r^2 + \pi^2 r \sin[\beta]} \right)}{r} \right\} \right\}
 \end{aligned}$$

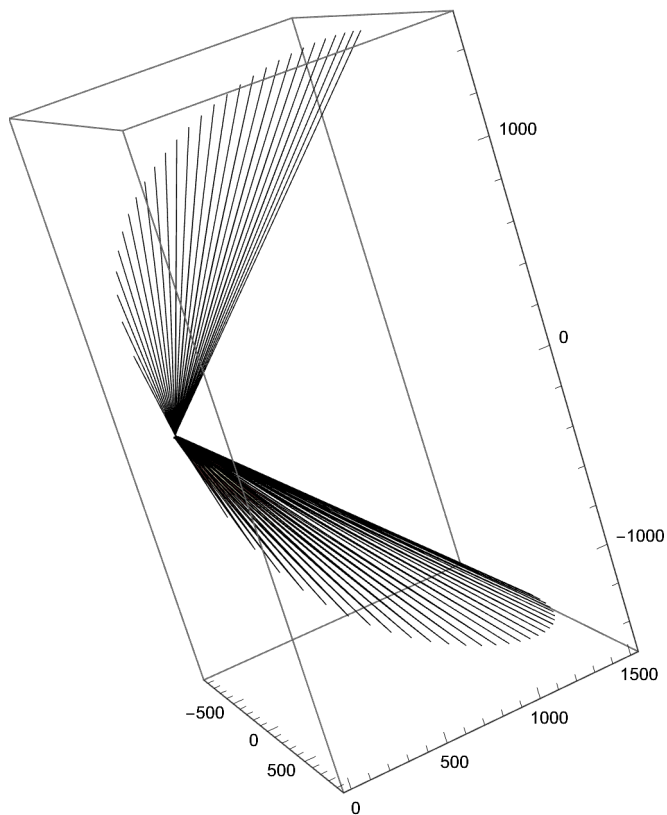
$\text{RevolutionPlot3D}\left[\frac{2\left(\pi r + \sqrt{\pi^2 r^2 + \pi^2 r \sin[\beta]}\right)}{r}, \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}\right]$



$\text{RevolutionPlot3D}\left[\left\{\frac{2\left(\pi r - \sqrt{\pi^2 r^2 - \pi^2 r \sin[\beta]}\right)}{r}, \frac{2\left(\pi r + \sqrt{\pi^2 r^2 + \pi^2 r \sin[\beta]}\right)}{r}\right\}, \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}\right]$



$\text{RevolutionPlot3D}\left[\left\{\frac{2\left(\pi r + \sqrt{\pi^2 r^2 + \pi^2 r \sin[\beta]}\right)}{r}, \frac{2\left(\pi r - \sqrt{\pi^2 r^2 + \pi^2 r \sin[\beta]}\right)}{r}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}\right]$



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ContourPlot3D[ -  $\left( 1. \cdot \text{Log}\left[ 2. \cdot^{-1.} y \left( \frac{-\frac{78.95683520871486}{12.566370614359172} - 1. \cdot \theta}{(12.566370614359172 - 1. \cdot \theta) \theta} + \frac{496.1004268847971}{(12.566370614359172 - 1. \cdot \theta) \theta} \right)^y \right. \right. +$ 

$$\left( \left( \sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16}} \right. \right.$$

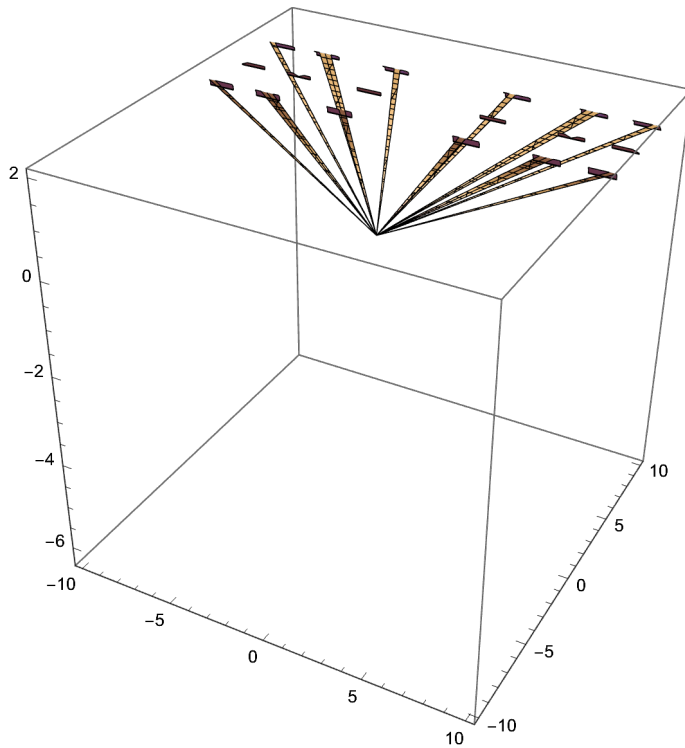

$$\left. \left. (12.566370614359172 - 1. \cdot \theta) \theta + 8.987551787368176 \cdot \theta^{16} \theta^2 \right) \right) /$$


$$\left( \sqrt{(-12.566370614359172 \cdot \theta + 1. \cdot (12.566370614359172 - 1. \cdot \theta) \theta + \theta^2))} \right)^x \Bigg] /$$


$$\left( -1.8378770664093456 - 1. \cdot \text{Log}\left[ \frac{1}{\theta} \right] \right), \{y,$$

-10,
10},
{x,
-10,
10}, {\theta,
-2
 $\pi, 2$ }]

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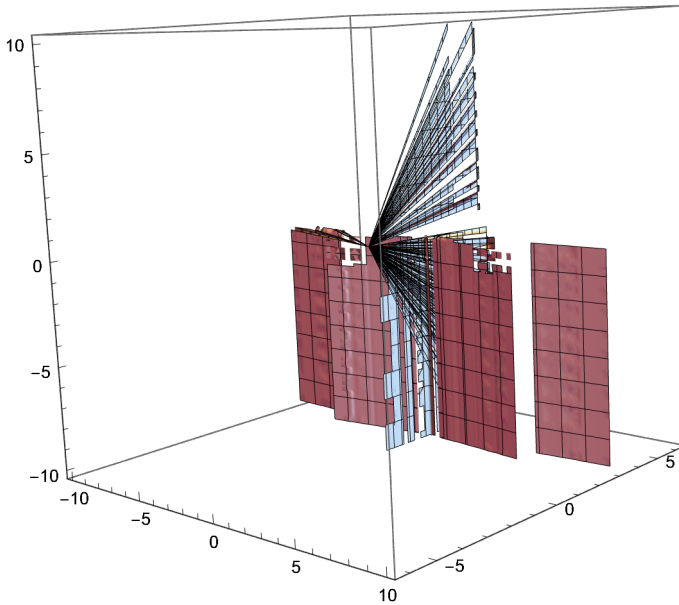


$$\begin{aligned}
 & \text{Solve} \left[ \left( \left( \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3.5481432270250993 \cdot \theta^{18} \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right]^2 \right) \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \right. \right. \right. \\
 & \quad \left. \left. \left. \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right]^2 \right) \right) \right) \right) \right]^{\wedge} x + \\
 & \quad \left( \frac{4\pi \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 - 2 \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta}{2 \sqrt{4\pi \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}} \right)^{\wedge} y == \\
 & \quad \left( \frac{2\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right]}{\theta} \right)^{\wedge} \\
 & \quad z, y] \\
 & \left\{ \left\{ y \rightarrow - \left( 1. \log \left[ 6.28319^z \left( \frac{1}{\theta} \right)^z - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1. \left( \left( \sqrt{\left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} (12.5664 - 1. \theta) \theta + 8.98755 \times 10^{16} \theta^2 \right) \right) \right) / \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left( \sqrt{-12.5664 \theta + 1. (12.5664 - 1. \theta) \theta + \theta^2} \right)^x \right) \right] \right) \right) / \\
 & \quad \left( 0.693147 - 1. \log \left[ \frac{-\frac{78.9568}{12.5664 - 1. \theta} + \frac{496.1}{(12.5664 - 1. \theta) \theta}}{\sqrt{\frac{496.1}{12.5664 - 1. \theta} - \frac{39.4784 \theta}{12.5664 - 1. \theta}}} \right] \right) \right\} \}
 \end{aligned}$$

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ContourPlot3D[
- (1.` Log[6.283185307179586`^z (1/θ)^z - 1.` ((√(-1.1294090667581471`*^18 θ +
      8.987551787368176`*^16 (12.566370614359172` - 1.` θ) θ +
      8.987551787368176`*^16 θ^2)) / (√(-12.566370614359172` θ +
      1.` (12.566370614359172` - 1.` θ) θ + θ^2)))^x] ) /
(
0.6931471805599453` - 1.` Log[
- 78.95683520871486` / (12.566370614359172` - 1.` θ) + 496.1004268847971` / (12.566370614359172` - 1.` θ) θ
/ (
496.1004268847971` / (12.566370614359172` - 1.` θ) - 39.47841760435743` θ / (12.566370614359172` - 1.` θ)
)
],
{z,
-10,
10},
{θ,
-2
π, 2
π}, {x, -10, 10}]

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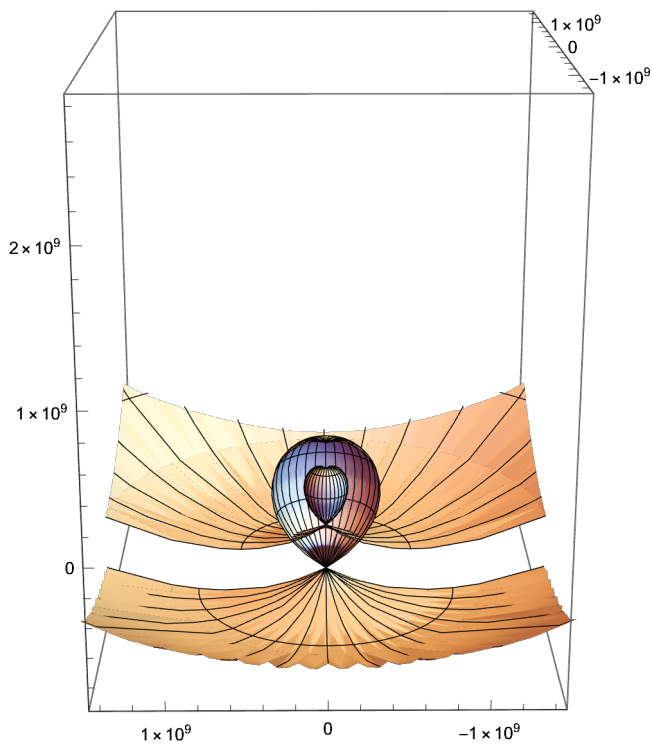
$$v^3 = \left( \left( \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta])} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]} \right) \right) \left( \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} \right) \frac{\sqrt{\frac{16\pi^3}{4\pi - \theta} - \frac{4\pi^2 \theta}{4\pi - \theta}}}{\theta}$$

$$\begin{aligned}
& \left( \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right.} \right. \\
& \quad \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)} \right) / \\
& \quad \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \Bigg) \\
& \quad \left( \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \frac{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}{\theta} \\
& \quad \left( \left( -\frac{8 \pi^2}{4 \pi - \theta} + \frac{16 \pi^3}{(4 \pi - \theta) \theta} \right) \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \quad \left( 2 \theta \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \right)
\end{aligned}$$

SphericalPlot3D[  

$$\left( \left( -\frac{8\pi^2}{4\pi-\theta} + \frac{16\pi^3}{(4\pi-\theta)\theta} \right) \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) /$$
  

$$\left( 2\theta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right),$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]



$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} / (\theta / (2\pi))$$

$$\frac{\sqrt{\frac{16\pi^3}{4\pi-\theta} - \frac{4\pi^2\theta}{4\pi-\theta}}}{\theta}$$

$$a^{\wedge}x + b^{\wedge}y = c^{\wedge}z$$



$$\text{Solve}\left[a^{\frac{2\pi r - r\theta}{2\pi}} + b^{\frac{2\pi \frac{2\pi r - r\theta}{2\pi} - \frac{2\pi r - r\theta}{2\pi} \theta}{2\pi}} == c^{\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}, c\right]$$

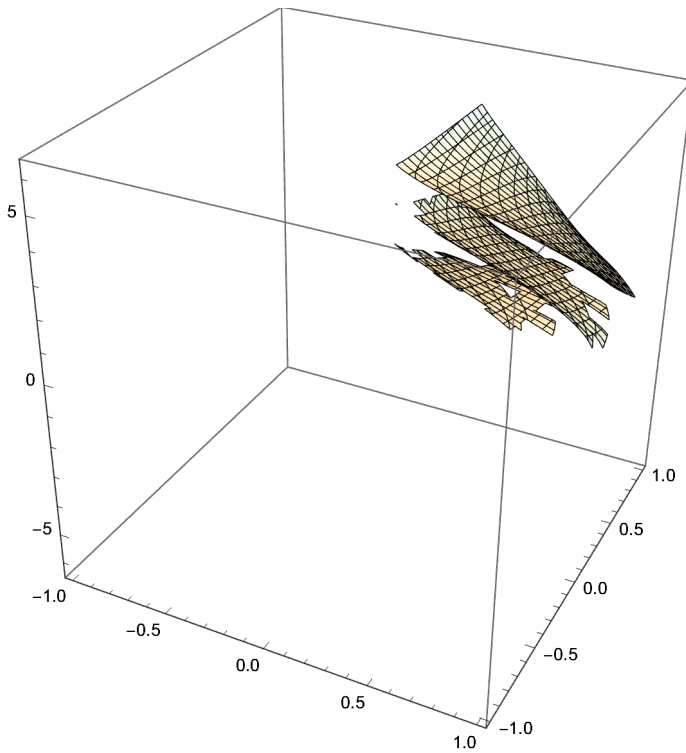
$$\left\{ \left\{ c \rightarrow a^{-\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta}} b^{-\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} - \frac{\theta \left( -\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{4\pi^2 \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)}{4\pi^2}} \right. \right.$$

$$\left. \left. \left( a^{\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta}} b^{\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}} + a^{\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}} b^{\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{\theta \left( -\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{4\pi^2 \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)}{4\pi^2}} \right) \right\} \right\}$$

$$\text{ContourPlot3D}\left[a^{-\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta}} b^{-\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} - \frac{\theta \left( -\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{4\pi^2 \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)}{4\pi^2}} \right.$$

$$\left. \left. \left( a^{\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta}} b^{\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}} + a^{\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}} b^{\frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{\theta \left( -\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{4\pi^2 \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)}{4\pi^2}} \right) \right\} \right\},$$

$$\{a, -1, 1\}, \{b, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$

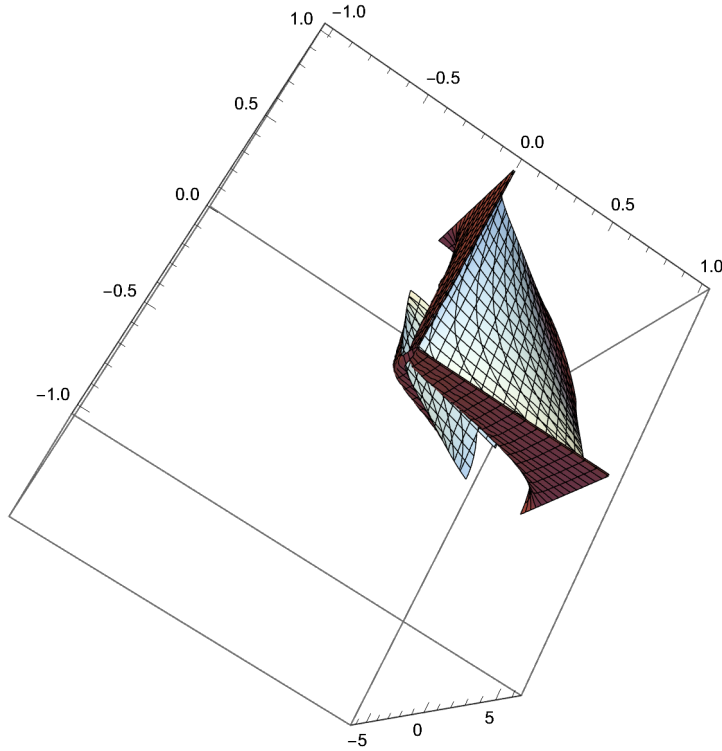


$$\text{Solve}\left[a^{\frac{2\pi r - r\theta}{2\pi}} + b^{\frac{2\pi \frac{2\pi r - r\theta}{2\pi} - \frac{2\pi r - r\theta}{2\pi} \theta}{2\pi}} == c^{\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}, c\right]$$

$$\left\{ \left\{ c \rightarrow \left( a^{r^{-\frac{r\theta}{2\pi}}} + b^{r^{-\frac{r\theta}{2\pi}}} \right)^{\frac{2\pi}{\sqrt{r^2 (4\pi - \theta)\theta}}} \right\} \right\}$$

$$r := \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

$$\text{ContourPlot3D}\left[\left(a^{r-\frac{r\theta}{2\pi}} + b^{r-\frac{r\theta}{2\pi}}\right)^{\frac{2\pi}{\sqrt{r^2(4\pi-\theta)\theta}}}, \{a, -1, 1\}, \{b, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



## The Base Ten Numbers - 0,1,2,3,4,5,6,7,8,9

### The Number 0

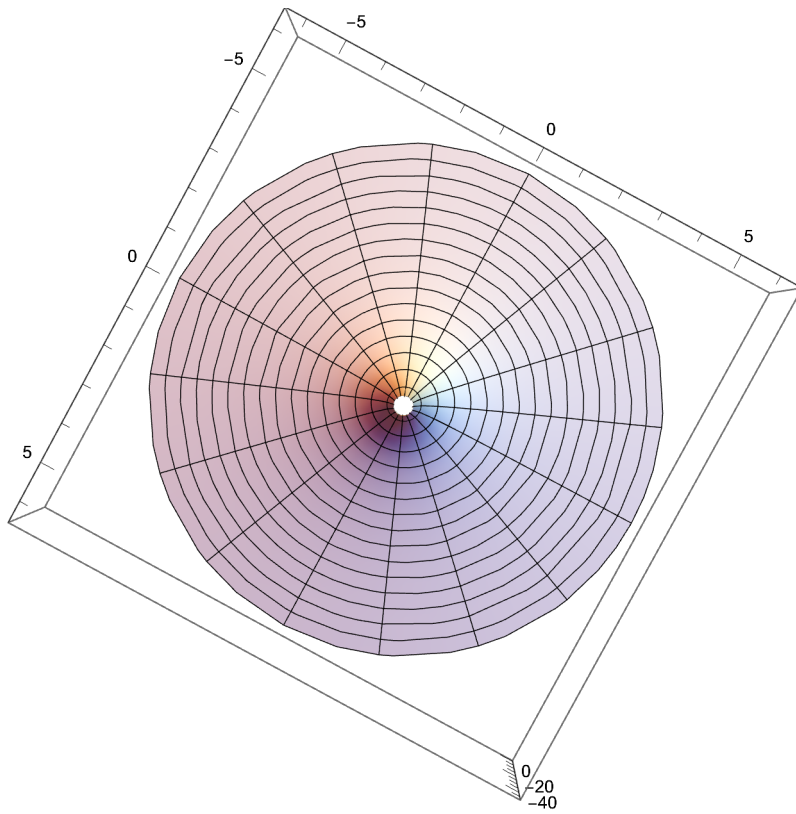
$$\theta r - 2\pi r - 2\pi r_1 = 0$$

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

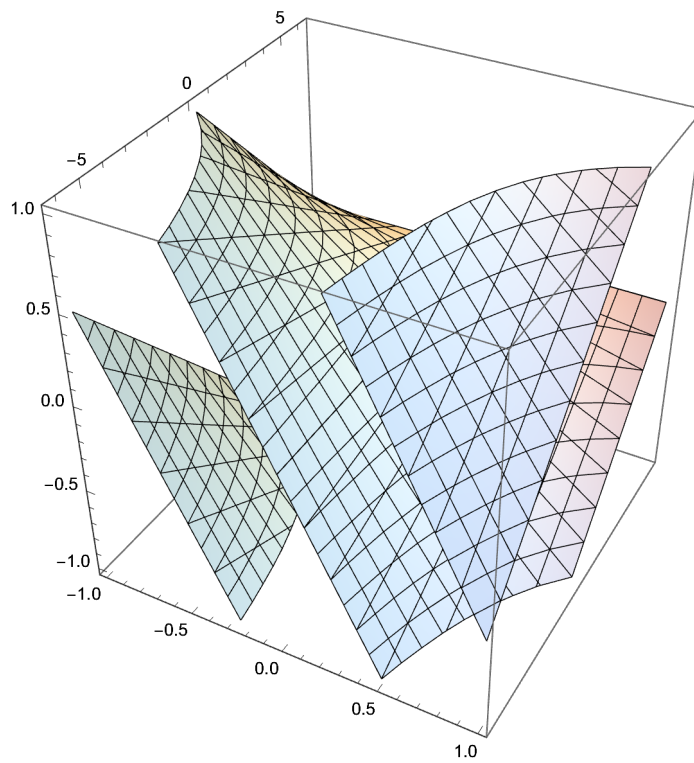
$$r := \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

$$\frac{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} \left( \theta r - 2\pi r - 2\pi \frac{2\pi r - r\theta}{2\pi} \right)}{\frac{\sqrt{(4\pi - \theta)\theta} \left( \frac{4\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} - \frac{8\pi^2 \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)}{\sqrt{4\pi\theta - \theta^2}}}$$

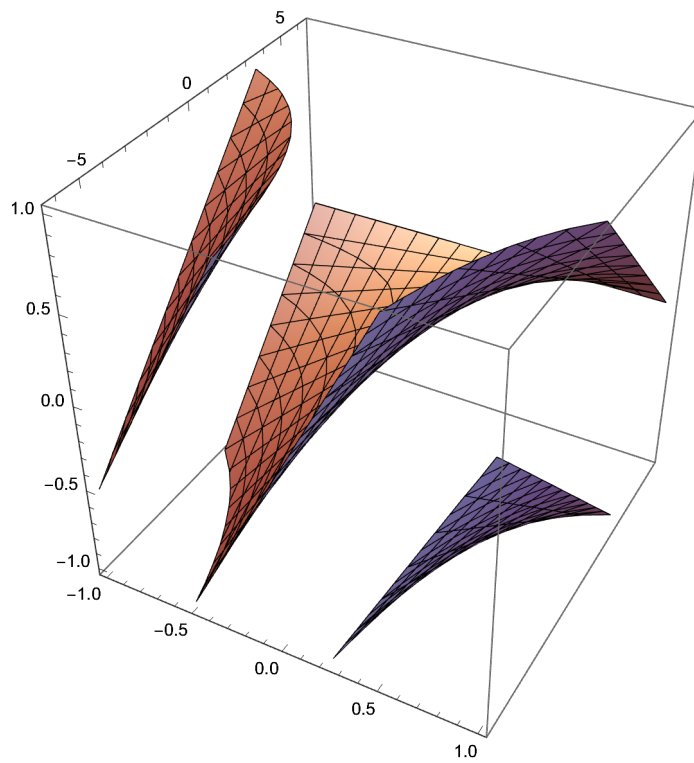
`RevolutionPlot3D` $\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \left(\theta r - 2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right), \{\theta, -2 \pi, 2 \pi\}\right]$



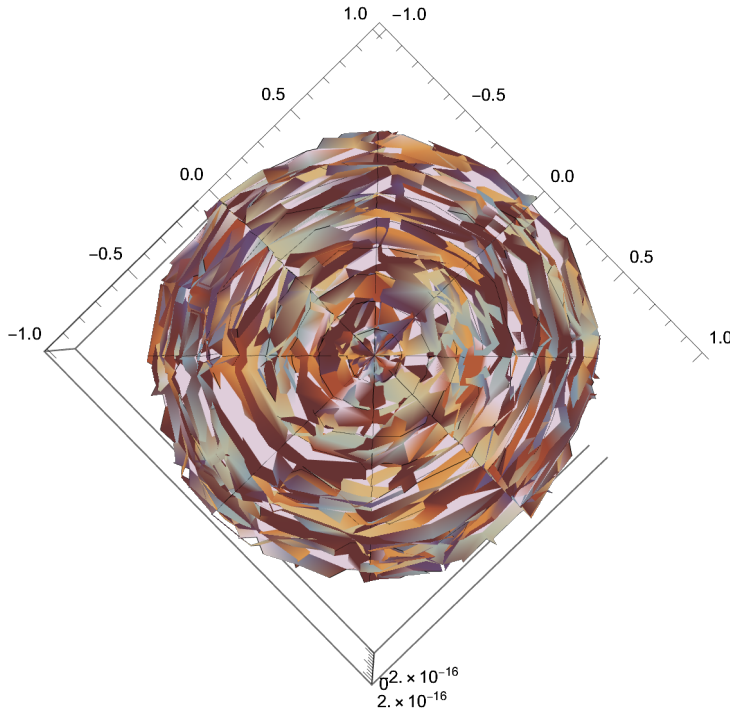
`ContourPlot3D[ $\theta r - 2 \pi r - 2 \pi r_1$ , {r, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }, {r1, -1, 1}]`



`ContourPlot3D[ $2 \pi r - 2 \pi r_1 - \theta r$ , {r, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }, {r1, -1, 1}]`



RevolutionPlot3D $\left[2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} - \theta r, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



## The Number 1

**Lemma 5**     *The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\theta$  is a function of  $\beta$  alone.*

Proof. Since we have shown that  $\theta r = 2 \pi r - 2 \pi r_1$  and  $x = r_1 \rightarrow \sqrt{r^2 - \eta^2}$ , we can substitute the expression for  $r_1$ , calculated from the Pythagorean theorem in terms of the height of the cone and the initial radius of the circle, into the expression for  $\theta r$  in terms of the change in circumference of the initial circle to the circle that is the base of the cone into which the circle was transformed.

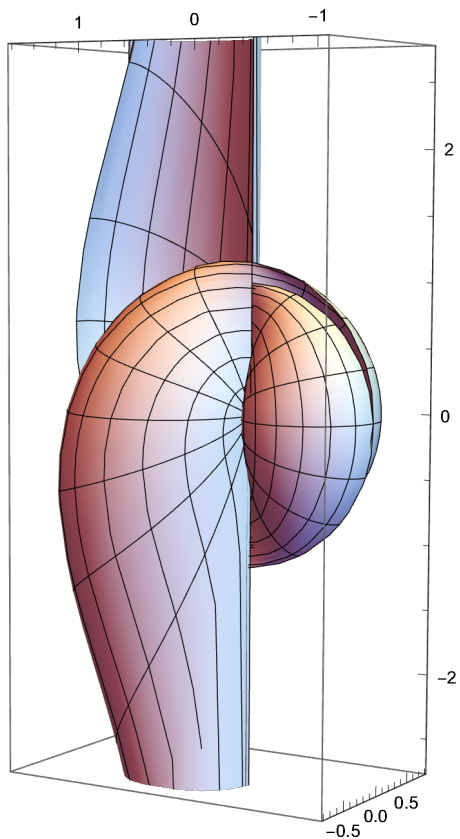
$\theta r = 2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}$ , thus,  $\eta = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} = (r \sin[\beta])$ . From  $\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} = r$ , we note that:  $r = \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$ . So we solve the equation,

$$\text{Solve}\left[r == \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta\right]$$

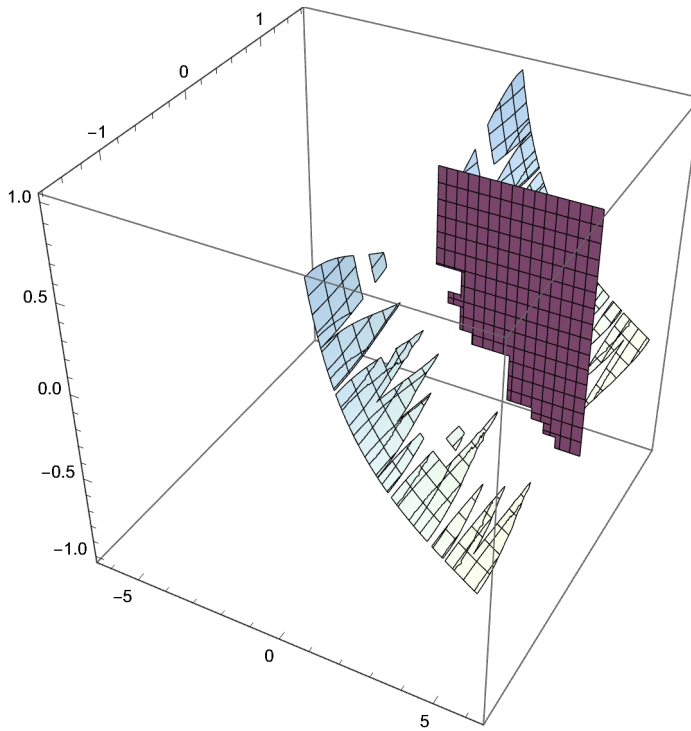
$$\left\{\left\{\theta \rightarrow 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$$

$$1 = \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

`SphericalPlot3D` $\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



ContourPlot3D $\left[\frac{\frac{r \theta}{\pi (r-x)} \pi \sin[\beta]}{\sqrt{\left(\frac{r \theta}{\pi (r-x)}\right) \left(\frac{r \theta}{\pi (r-x)}\right) \pi \theta - \theta^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}, \{x, -1, 1\}\right]$



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

## The Number 2

**Theorem 1** When a sector of angle  $\theta$  is removed from a circle of radius  $r$  and the resulting shape is folded into a cone, then the base of the cone has radius  $r_1$  given by  $r_1 = r - \frac{(r \theta)}{2 \pi}$ ; and height  $\eta$ , given by  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$

Proof. The circumference of the initial circle is  $2 \pi r$  and the wedge removed has an arc length  $r \theta$ . Therefore, the remaining circumference is of length  $r (2 \pi - \theta)$ , and after the fold, this is the circumference of the base of the cone.

Establishing the circumference of the base of the cone, from the equation,  $\theta r = 2 \pi r - 2 \pi r_1$ , we calculate that its radius  $r_1$  is  $\frac{2 \pi r - r \theta}{2 \pi}$ , which simplifies to  $r - \frac{r \theta}{2 \pi}$ . Thus, we have proved the first part of the theorem.

To find the height of the cone,  $\eta$ , we apply the Pythagorean theorem to a right triangle formed between the apex of the cone, the center of the base, and a point on the circumference of the base. This gives  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$ , where  $\beta$  is the angle formed by the slant of the cone and the base of the cone. The initial radius is always equal to the slant of the cone, and the height of the cone is always orthogonal to the center of the base of the cone.

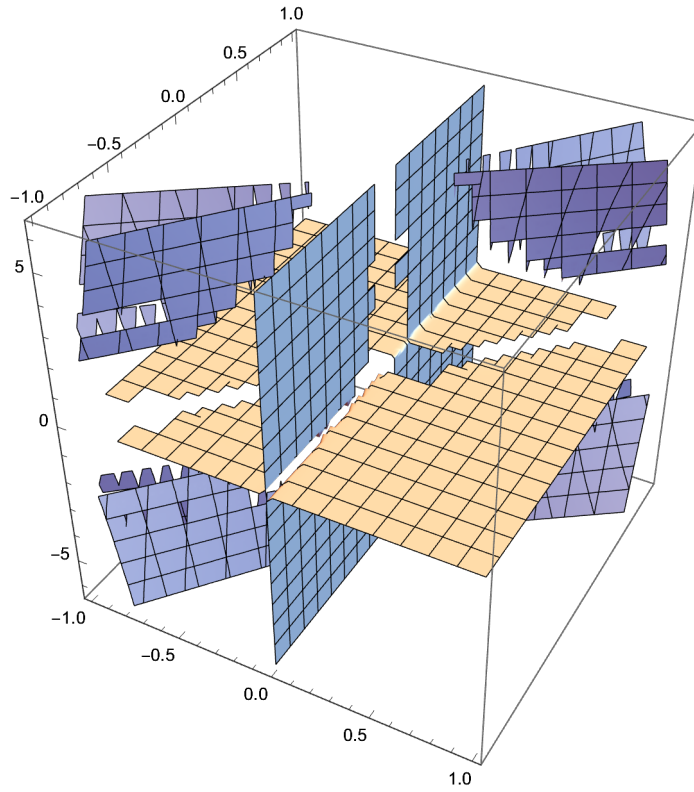
$$\theta r = 2 \pi r - 2 \pi r_1$$

Solve[ $\theta r == \text{two } \pi r - \text{two } \pi r_1, \text{two}$ ]

$$\left\{ \left\{ \text{two} \rightarrow \frac{r \theta}{\pi (r - r_1)} \right\} \right\}$$

$$\frac{r \theta}{\pi (r - r_1)} = \frac{r \theta}{\pi (r - x)}$$

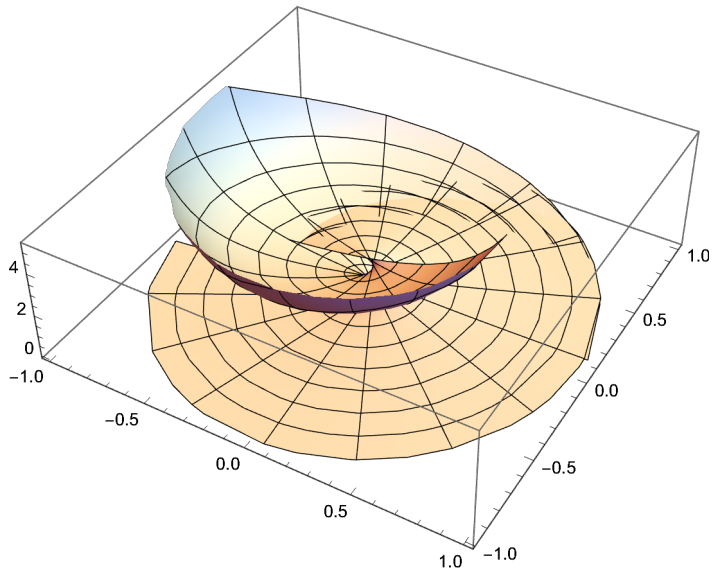
ContourPlot3D $\left[\frac{r \theta}{\pi (r - r_1)}, \{r, -1, 1\}, \{r_1, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$



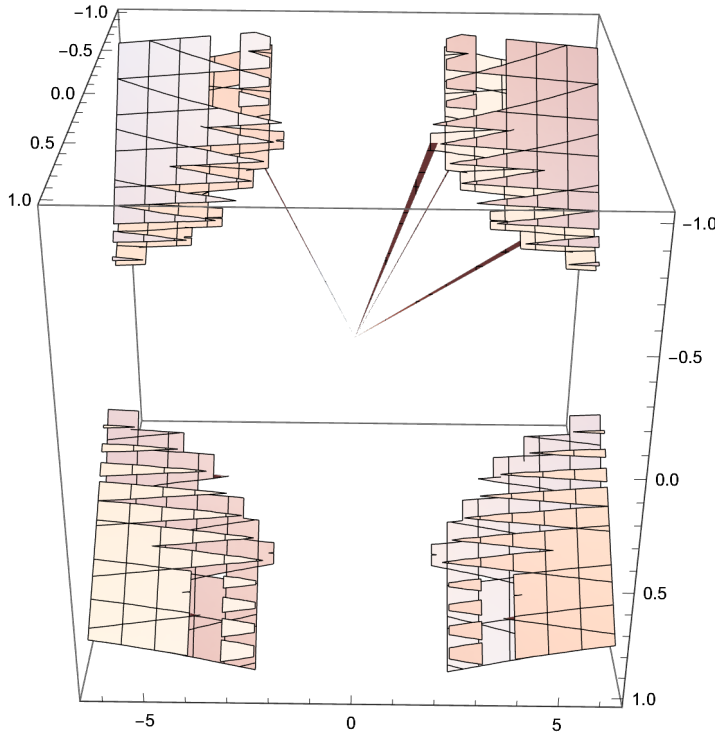
`RevolutionPlot3D` $\left[\frac{r \theta}{\pi (r - x)}, \{x, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



### The Number 3

$$3 = \frac{r \theta}{\pi (r - x)} + \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} = \frac{r \theta}{\pi (r - x)} + \frac{\frac{r \theta}{\pi (r - x)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - x)}\right) \left(\frac{r \theta}{\pi (r - x)}\right) \pi \theta - \theta^2}}$$

$$\text{ContourPlot3D}\left[\frac{r \theta}{\pi (r-x)} + \frac{\frac{r \theta}{\pi (r-x)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{\left(\frac{r \theta}{\pi (r-x)}\right) \left(\frac{r \theta}{\pi (r-x)}\right) \pi - \theta} \theta}{\left(\frac{r \theta}{\pi (r-x)}\right) \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r-x)}\right) \left(\frac{r \theta}{\pi (r-x)}\right) \pi \theta - \theta^2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{x, -1, 1\}\right]$$



## The Number 4

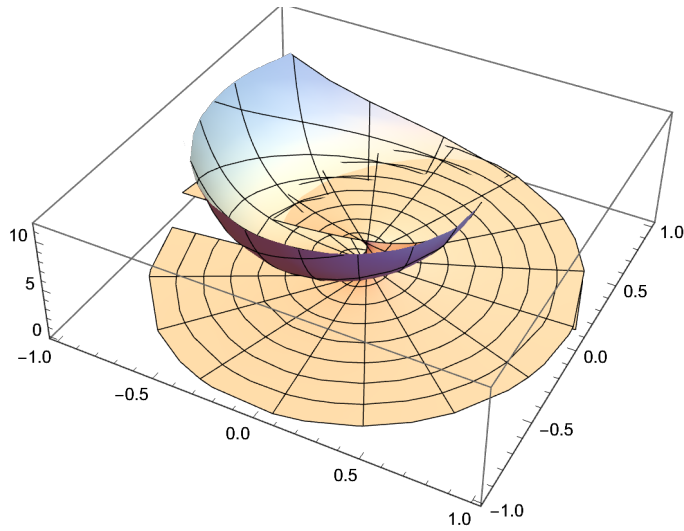
$$r = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$r == \frac{\frac{r \theta}{\pi (r-x)} \pi \sqrt{(\text{four } \pi - \theta) \theta}}{(\text{four } \pi - \theta) \theta}$$

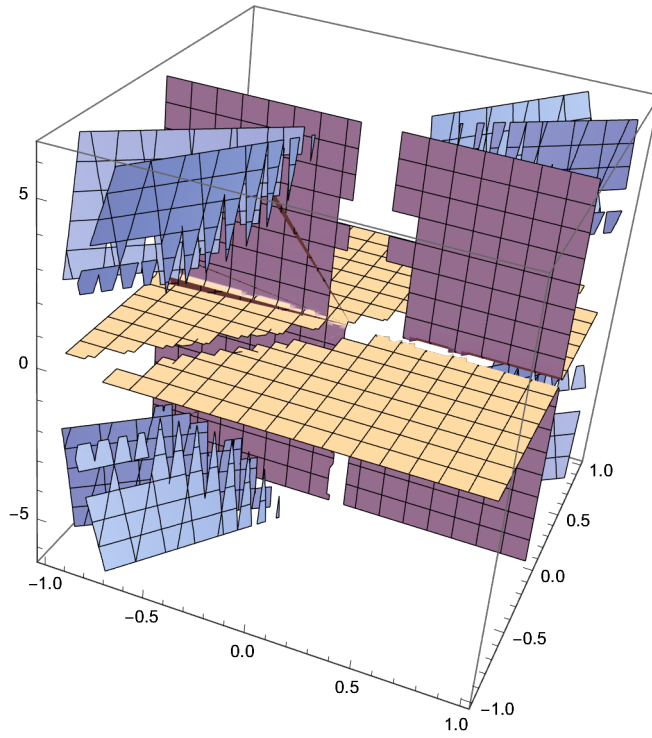
$$\text{Solve}\left[r == \frac{\frac{r \theta}{\pi (r-x)} \pi \sqrt{(\text{four } \pi - \theta) \theta}}{(\text{four } \pi - \theta) \theta}, \text{four}\right]$$

$$\left\{\left\{\text{four} \rightarrow \frac{1}{\pi} \left( \theta + \frac{16 \pi^2 \theta^3}{(4 \pi x \theta - x \theta^2 - 2 \pi \sqrt{(4 \pi - \theta) \theta})^2} - \frac{8 \pi \theta^4}{(4 \pi x \theta - x \theta^2 - 2 \pi \sqrt{(4 \pi - \theta) \theta})^2} + \frac{\theta^5}{(4 \pi x \theta - x \theta^2 - 2 \pi \sqrt{(4 \pi - \theta) \theta})^2} \right) \right\}\right\}$$

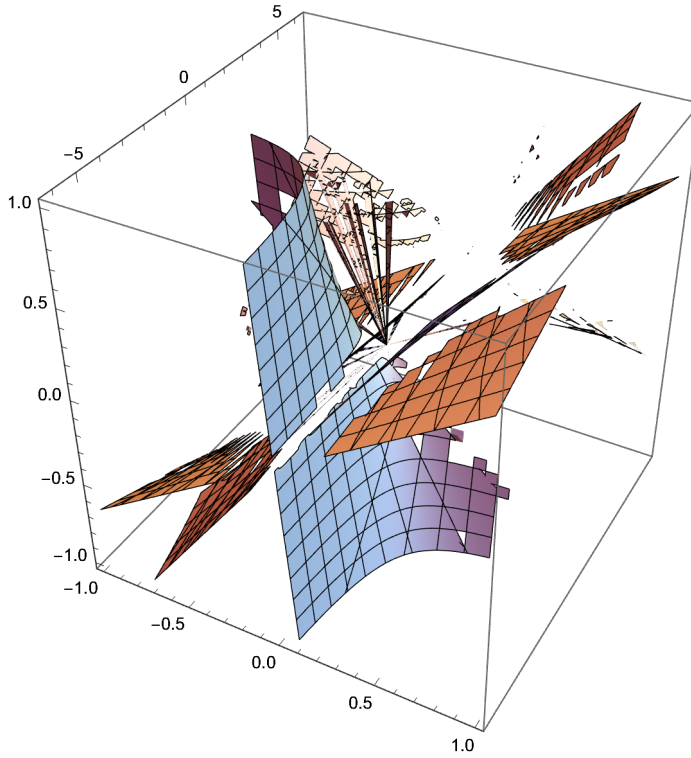
$\text{RevolutionPlot3D}\left[\frac{1}{\pi}\right.$   
 $\left(\theta + \frac{16 \pi^2 \theta^3}{\left(4 \pi x \theta - x \theta^2 - 2 \pi \sqrt{(4 \pi - \theta) \theta}\right)^2} - \frac{8 \pi \theta^4}{\left(4 \pi x \theta - x \theta^2 - 2 \pi \sqrt{(4 \pi - \theta) \theta}\right)^2} + \right.$   
 $\left.\frac{\theta^5}{\left(4 \pi x \theta - x \theta^2 - 2 \pi \sqrt{(4 \pi - \theta) \theta}\right)^2}\right), \{x, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$



`ContourPlot3D` $\left[\frac{r \theta}{\pi (r - r_1)} + \frac{r \theta}{\pi (r - r_1)}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{r_1, -1, 1\}\right]$



$$\text{ContourPlot3D}\left[\frac{r \theta}{\pi (r - r_1)} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi \theta - \theta^2}} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi \theta - \theta^2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{r_1, -1, 1\}\right]$$



## The Number 5

$$\theta = \theta r - 2 \pi r - 2 \pi r_1, 1 = \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, 2 = \frac{r \theta}{\pi (r - r_1)}, \text{ therefore } 1 = \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} =$$

$$\frac{r \theta}{\pi (r - r_1)} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{\left(\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta\right) \theta}}{\left(\frac{r \theta}{\pi (r - r_1)}\right) \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\frac{r \theta}{\pi (r - r_1)} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta} \theta}{\left(\frac{r \theta}{\pi (r - r_1)}\right) \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta^2}} + \frac{r \theta}{\pi (r - r_1)} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta} \theta}{\left(\frac{r \theta}{\pi (r - r_1)}\right) \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta^2}} == 2, r\right]$$

{{r → 0}}

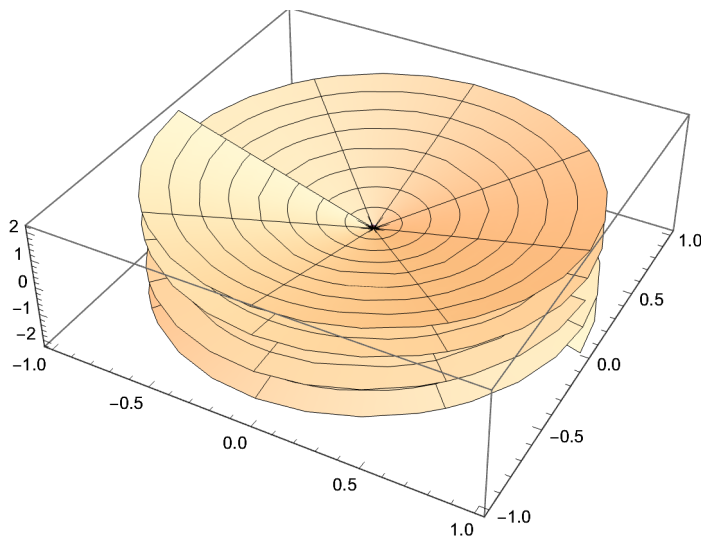
$$\text{Solve}\left[\frac{r \theta}{\pi (r - r_1)} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta} \theta}{\left(\frac{r \theta}{\pi (r - r_1)}\right) \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta^2}} + \frac{r \theta}{\pi (r - r_1)} + \frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta} \theta}{\left(\frac{r \theta}{\pi (r - r_1)}\right) \pi}\right]\right]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)}\right) \left(\frac{r \theta}{\pi (r - r_1)}\right) \pi - \theta^2}} == 2, r\right]$$

{{}}

Solve[θ r - 2 π r - 2 π r<sub>1</sub> == r, r, r<sub>1</sub>]

{{r<sub>1</sub> →  $\frac{-r - 2 \pi r + r \theta}{2 \pi}$ }}

RevolutionPlot3D[ $\frac{-r - 2 \pi r + r \theta}{2 \pi}$ , {r, -1, 1}, {θ, -2 π, 2 π}]



$$\text{ContourPlot3D}\left[\frac{\frac{r\theta}{\pi(r-r_1)}\pi\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]}{\sqrt{\left(\frac{r\theta}{\pi(r-r_1)}\right)\left(\frac{r\theta}{\pi(r-r_1)}\right)\pi\theta-\theta^2}}+\frac{\frac{r\theta}{\pi(r-r_1)}\pi\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]}{\sqrt{\left(\frac{r\theta}{\pi(r-r_1)}\right)\left(\frac{r\theta}{\pi(r-r_1)}\right)\pi\theta-\theta^2}}+\frac{\frac{r\theta}{\pi(r-r_1)}\pi\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]}{\sqrt{\left(\frac{r\theta}{\pi(r-r_1)}\right)\left(\frac{r\theta}{\pi(r-r_1)}\right)\pi\theta-\theta^2}}+\frac{\frac{r\theta}{\pi(r-r_1)}\pi\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]}{\sqrt{\left(\frac{r\theta}{\pi(r-r_1)}\right)\left(\frac{r\theta}{\pi(r-r_1)}\right)\pi\theta-\theta^2}},\{r,-1,1\},\{\theta,-2\pi,2\pi\},\{r_1,-1,1\}\right]$$

## Inside V-Curvature

$$\text{Solve}\left[\frac{\sqrt{r}\sqrt{1-\frac{(v)^2}{c^2}}\sqrt{\frac{\theta}{1-\frac{(v)^2}{c^2}}}\sqrt{4\pi r-r\theta}}{2\pi}=\sqrt{\left(\frac{\sqrt{r}\left(2\pi r-2\pi\frac{2\pi r-r\theta}{2\pi}-\theta r\right)\sqrt{\frac{\theta}{\left(2\pi r-2\pi\frac{2\pi r-r\theta}{2\pi}-\theta r\right)}}\sqrt{4\pi r-r\theta}}{2\pi}r\sin[\beta]\right)},v\right]$$

{{}}

$$\text{Solve}\left[\frac{\sqrt{r}\sqrt{1-\frac{(v)^2}{c^2}}\sqrt{\frac{\theta}{1-\frac{(v)^2}{c^2}}}\sqrt{4\pi r-r\theta}}{2\pi}=\frac{\sqrt{r}\left(2\pi r-2\pi\frac{2\pi r-r\theta}{2\pi}-\theta r\right)\sqrt{\frac{\theta}{\left(2\pi r-2\pi\frac{2\pi r-r\theta}{2\pi}-\theta r\right)}}\sqrt{4\pi r-r\theta}}{2\pi},v\right]$$

{{}}

$$c := 2.99792458 (10^8)$$

$$r := \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}$$

$$r := \frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}}$$

$$\frac{\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}{\left(2\pi r-2\pi\frac{2\pi r-r\theta}{2\pi}-\theta r\right)}==$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}-1} \sqrt{\frac{\theta}{\sqrt{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}-1}} \sqrt{4\pi r-r\theta}}{2\pi} = r \sin[\beta], \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}-1} \sqrt{\frac{\theta}{\sqrt{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}-1}} \sqrt{4\pi r-r\theta}}{2\pi} = \frac{\sqrt{r} \sqrt{1-\frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}} \sqrt{4\pi r-r\theta}}{2\pi}, v\right]$$

{}

$$\text{Solve}\left[\frac{1}{2\pi} \sqrt{\left(r \sqrt{\left(1 - \frac{1}{c^2} \left((\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)) / (\sqrt{(-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2))})^2\right)}\right)}\right]$$

$$\sqrt{\left(\theta / \left(\sqrt{\left(1 - \frac{1}{c^2} \left((\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)) / (\sqrt{(-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2))})^2\right)}\right)}\right)} \sqrt{4\pi r-r\theta} = r \sin[\beta], r\right]$$

{{}}

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1-\frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}} \sqrt{4\pi r-r\theta}}{2\pi} = r \sin[\beta], \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{1}{-8.98755 \times 10^{16} + v^2} \left(0.5 \left(-1.12941 \times 10^{18} + 12.5664 v^2 - 1. \sqrt{\left(\left(1.12941 \times 10^{18} - 12.5664 v^2\right)^2 - 4. \left(-8.98755 \times 10^{16} + v^2\right) \left(-3.54814 \times 10^{18} + 39.4784 v^2\right) \sin[\beta]^2\right)}\right)\right), \left\{\theta \rightarrow \frac{1}{-8.98755 \times 10^{16} + v^2} \left(0.5 \left(-1.12941 \times 10^{18} + 12.5664 v^2 + \sqrt{\left(\left(1.12941 \times 10^{18} - 12.5664 v^2\right)^2 - 4. \left(-8.98755 \times 10^{16} + v^2\right) \left(-3.54814 \times 10^{18} + 39.4784 v^2\right) \sin[\beta]^2\right)}\right)\right)\right\}\right\}$$

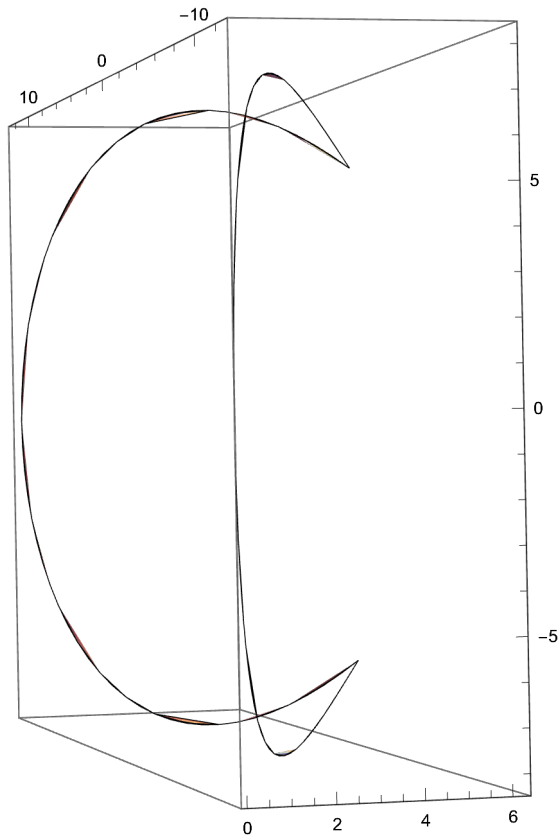


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RevolutionPlot3D[
{
  
$$\frac{1}{-8.987551787368176 v^{16} + v^2} 0.5 \left( -1.1294090667581471 v^{18} + 12.566370614359172 v^2 - 1. \sqrt{\left( (1.1294090667581471 v^{18} - 12.566370614359172 v^2)^2 - 4. (-8.987551787368176 v^{16} + v^2) (-3.5481432270250993 v^{18} + 39.47841760435743 v^2) \sin^2[\beta] \right)} \right),$$

  
$$\frac{1}{-8.987551787368176 v^{16} + v^2} 0.5 \left( -1.1294090667581471 v^{18} + 12.566370614359172 v^2 + \sqrt{\left( (1.1294090667581471 v^{18} - 12.566370614359172 v^2)^2 - 4. (-8.987551787368176 v^{16} + v^2) (-3.5481432270250993 v^{18} + 39.47841760435743 v^2) \sin^2[\beta] \right)} \right), \{v, -.5 c, .5 c\}, \{\beta, -\pi, \pi\}]$$


```



$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(c)^2}{v^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(c)^2}{v^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == r \sin[\beta], v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}}\right\}\right\}$$

$$\text{Solve}\left[\left(\sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)}\right) / \right.$$

$$\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) ==$$

$$\left(\sqrt{(-1.1294090667581471 \cdot \theta^{18} \theta + 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)}\right) /$$

$$\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \beta]$$

$$\{\{\}\}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == r \sin[\beta], v\right]$$

$$\left\{\left\{v \rightarrow -\left(\sqrt{2} \sqrt{(-4c^2\pi^2\theta \sqrt{(4\pi - \theta)\theta} \sin[\beta] + c^2\pi\theta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 8c^2\pi^4 \sin[\beta]^4)}\right) / \right.$$

$$\left(\sqrt{-16\pi^2\theta^2 + 8\pi\theta^3 - \theta^4 + 16\pi^4 \sin[\beta]^4}\right)\right\},$$

$$\left\{v \rightarrow \left(\sqrt{2} \sqrt{(-4c^2\pi^2\theta \sqrt{(4\pi - \theta)\theta} \sin[\beta] + c^2\pi\theta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 8c^2\pi^4 \sin[\beta]^4)}\right) / \right.$$

$$\left(\sqrt{-16\pi^2\theta^2 + 8\pi\theta^3 - \theta^4 + 16\pi^4 \sin[\beta]^4}\right)\right\}\}$$

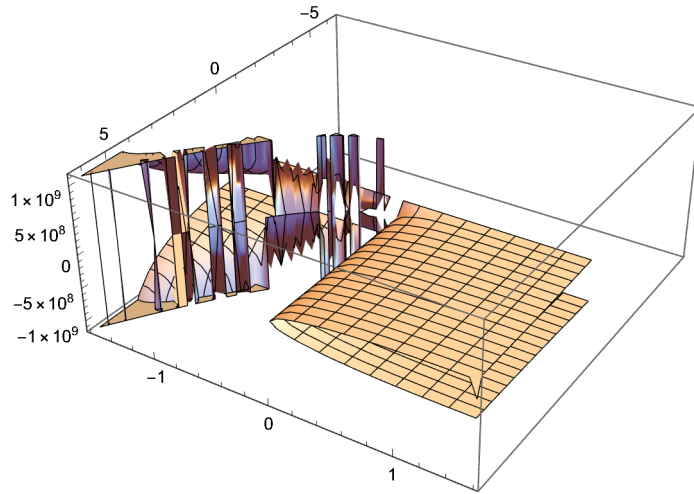
Plot3D[  

$$\left\{ - \left( \sqrt{2} \sqrt{-4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 c^2 \pi^4 \sin[\beta]^4} \right) / \right.$$
  

$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right),$$
  

$$\left( \sqrt{2} \sqrt{-4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 c^2 \pi^4 \sin[\beta]^4} \right) /$$
  

$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right) \}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



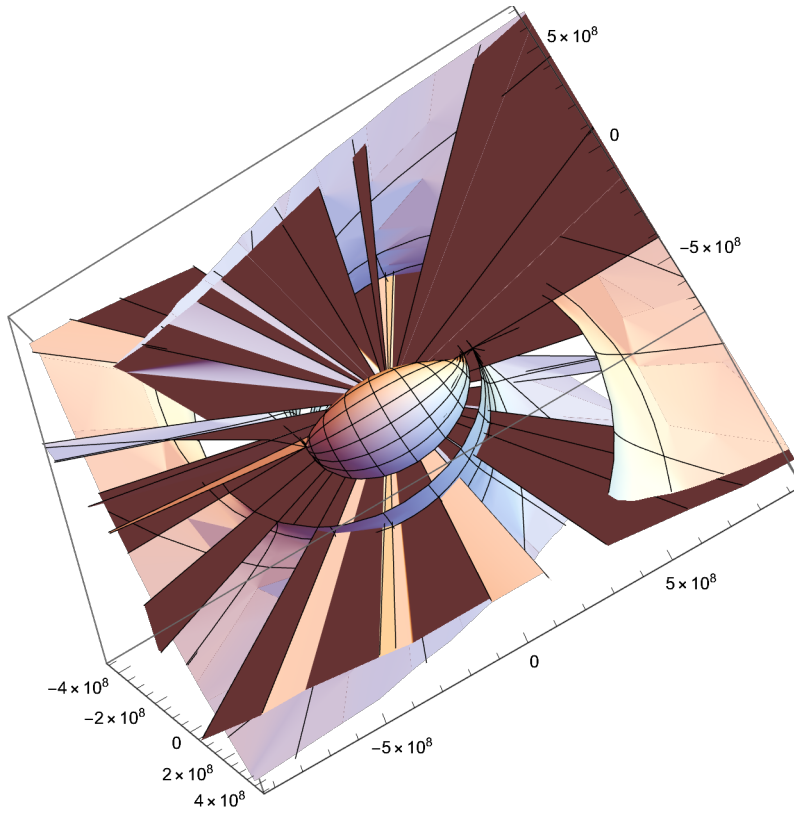
SphericalPlot3D[  

$$\left\{ -\left( \sqrt{2} \sqrt{-4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 c^2 \pi^4 \sin[\beta]^4} \right) / \right.$$
  

$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right),$$
  

$$\left( \sqrt{2} \sqrt{-4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 c^2 \pi^4 \sin[\beta]^4} \right) /$$
  

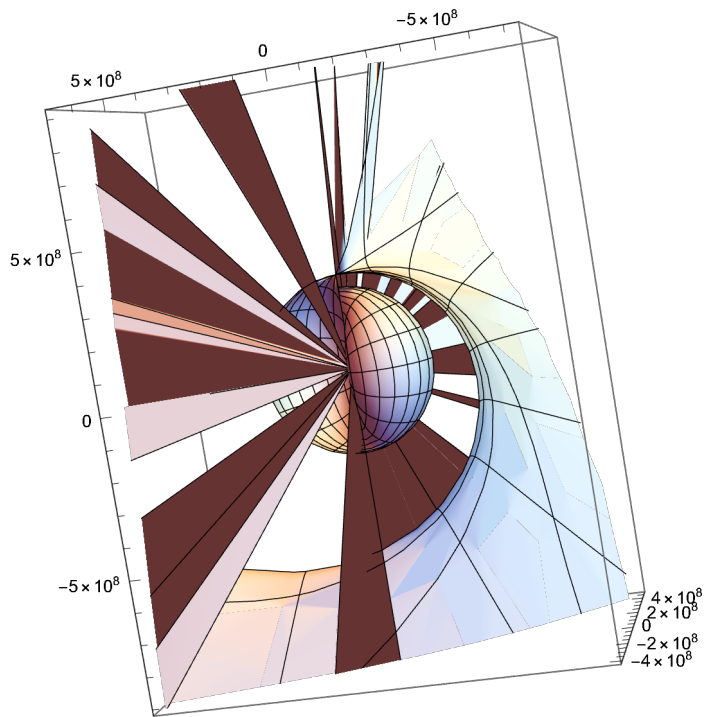
$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right) \}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



SphericalPlot3D[  

$$\left( \sqrt{2} \sqrt{\left( -4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + 8 c^2 \pi^4 \sin[\beta]^4 \right)} \right) /$$
  

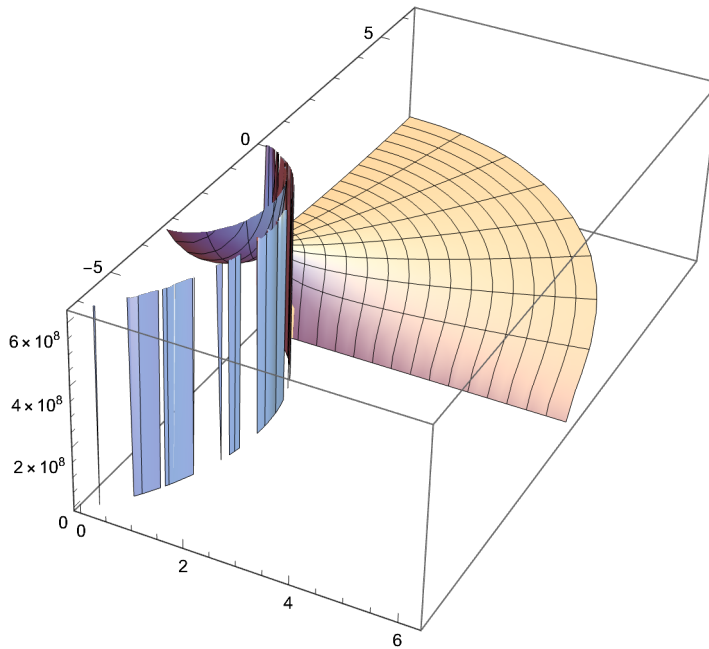
$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



RevolutionPlot3D[  

$$\left( \sqrt{2} \sqrt{\left( -4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + 8 c^2 \pi^4 \sin[\beta]^4 \right)} \right) /$$
  

$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



Solve[
$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], v]$$

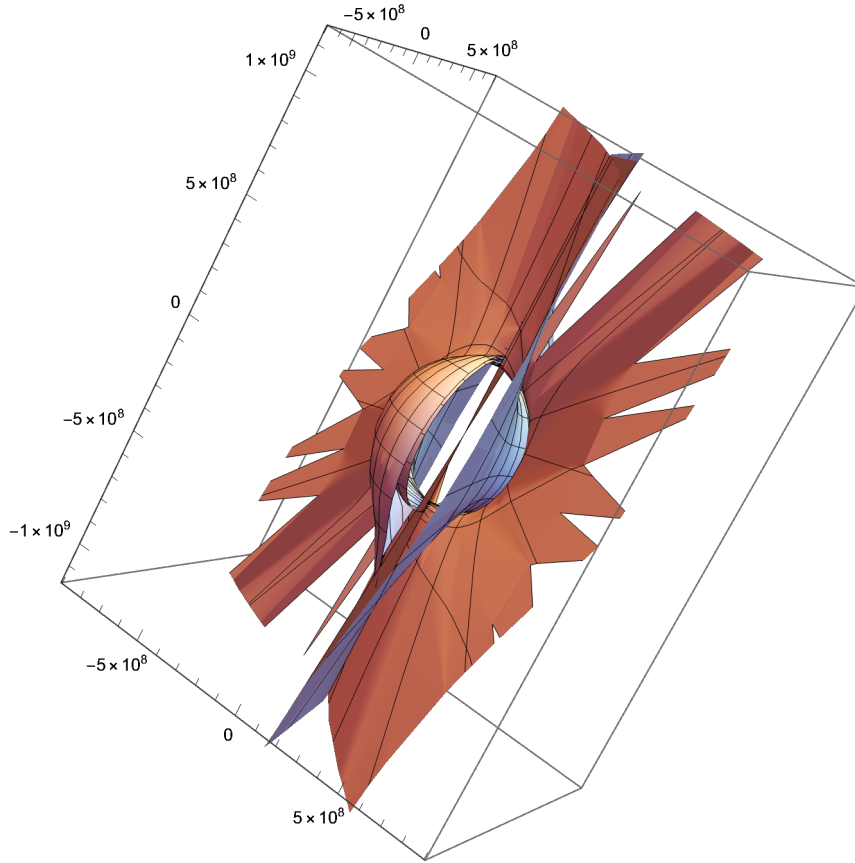
$$\left\{ \left\{ v \rightarrow - \frac{\sqrt{-16 c^2 \pi^2 \theta^2 + 8 c^2 \pi \theta^3 - c^2 \theta^4 + \frac{32 c^2 \pi^5 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^5}}{(4 \pi - \theta) \theta}}}{\sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-16 c^2 \pi^2 \theta^2 + 8 c^2 \pi \theta^3 - c^2 \theta^4 + \frac{32 c^2 \pi^5 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^5}}{(4 \pi - \theta) \theta}}}{\sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4}} \right\} \right\}$$

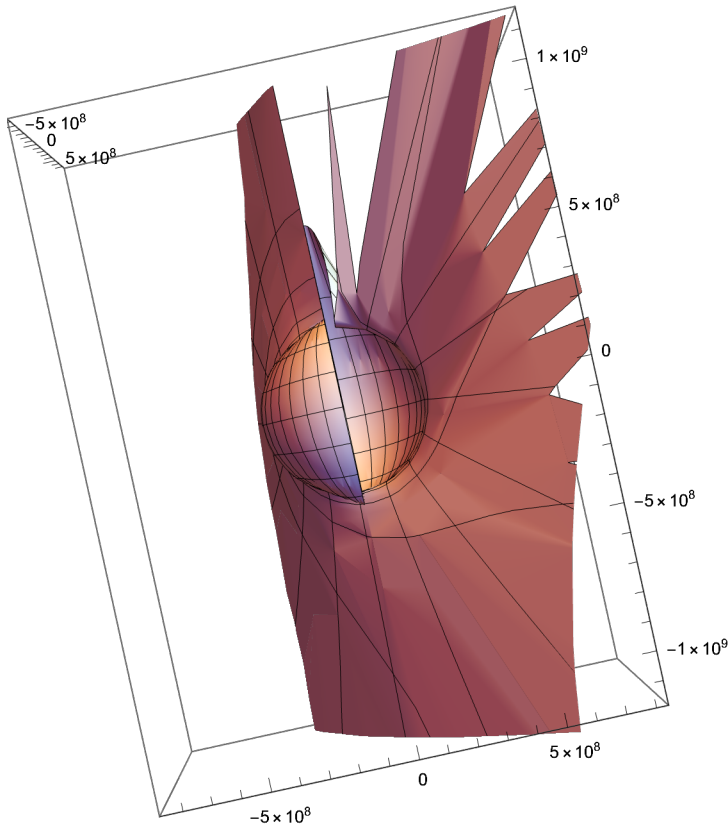
$c := 2.99792458 (10^8)$

SphericalPlot3D[
$$- \frac{\sqrt{-16 c^2 \pi^2 \theta^2 + 8 c^2 \pi \theta^3 - c^2 \theta^4 + \frac{32 c^2 \pi^5 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^5}}{(4 \pi - \theta) \theta}}}{\sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4}},$$
  
 $\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$

$$\text{SphericalPlot3D}\left[\left\{\frac{\sqrt{-16 c^2 \pi^2 \theta^2 + 8 c^2 \pi \theta^3 - c^2 \theta^4 + \frac{32 c^2 \pi^5 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{(4 \pi - \theta) \theta}}}{\sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \text{Sin}[\beta]^4}},\right.\right. \\ \left.\left.-\frac{\sqrt{-16 c^2 \pi^2 \theta^2 + 8 c^2 \pi \theta^3 - c^2 \theta^4 + \frac{32 c^2 \pi^5 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{(4 \pi - \theta) \theta}}}{\sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \text{Sin}[\beta]^4}}\right\},\right. \\ \left.\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{\sqrt{-16 c^2 \pi^2 \theta^2 + 8 c^2 \pi \theta^3 - c^2 \theta^4 + \frac{32 c^2 \pi^5 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{(4 \pi - \theta) \theta}}}{\sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4 + 16 \pi^4 \text{Sin}[\beta]^4}},\right. \\
\left. \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$





SphericalPlot3D[  

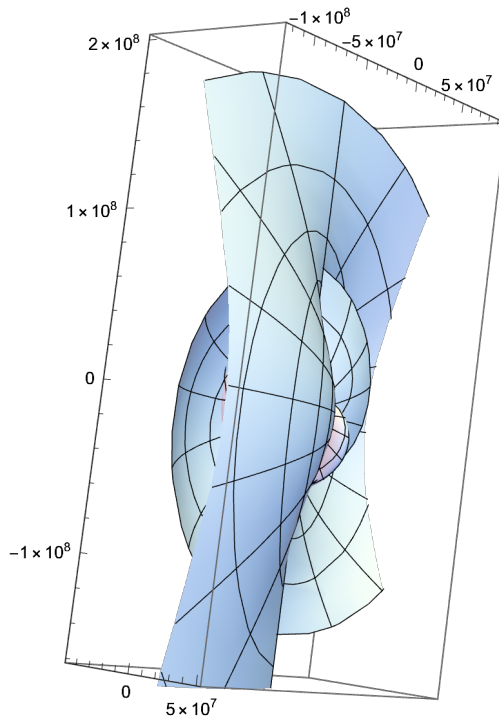
$$\left\{ - \left( \sqrt{2} \sqrt{(-4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 c^2 \pi^4 \sin[\beta]^4)} \right) / \right.$$
  

$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^3 - \theta^4 + 16 \pi^4 \sin[\beta]^4} \right),$$
  

$$\left( \sqrt{2} \sqrt{(-4 c^2 \pi^2 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + c^2 \pi \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 c^2 \pi^4 \sin[\beta]^4)} \right) /$$
  

$$\left( \sqrt{-16 \pi^2 \theta^2 + 8 \pi \theta^3 - \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 + 16 \pi^4 \sin[\beta]^4} \right) \right\},$$
  

$$\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}$$



## 3 D plots of $f(r_1)=f(r)=\theta$

Plot[ $\left\{ \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \right.$   

$$\frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + (2^{1/3} (16 \pi^4 - 512 \pi^8 + \right.$$
  

$$4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2))$$

$$\begin{aligned}
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 \right. \\
& \quad r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \\
& \quad r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \Big)^{1/3} \Big) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \\
& \quad \quad \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \Big)^{1/3} \Big) \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Big) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \Big/ \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 \right. \right. \\
& \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 \\
& \quad r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \\
& \quad \quad \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \Big)^{1/3} \Big) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \Big)^{1/3} \Big) \Big/ \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Big/ \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \\
& \quad \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \right) \Big/
\end{aligned}$$

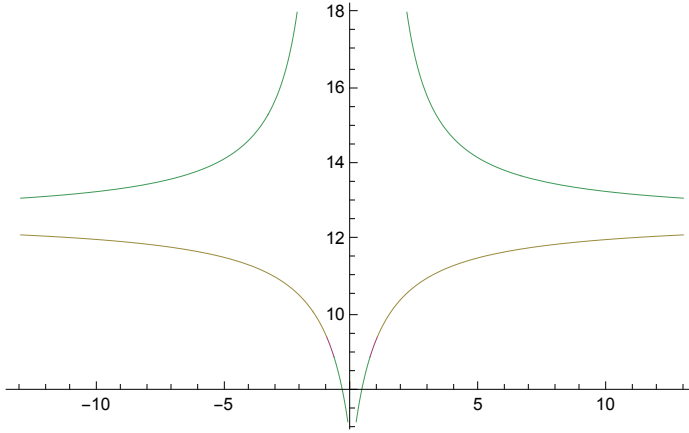
$$\begin{aligned}
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\
& \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\
& \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right.} \\
& \quad \quad 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\
& \quad \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\
& \quad \quad \left. \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \right. \\
& \quad \quad \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg\} , \\
& \left\{ \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right. \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \Bigg/ \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\
& \quad \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} \\
& \quad \quad r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad \quad \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \\
& \quad \quad \quad \left. \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \quad \quad \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg\} + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \Bigg/ \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\
& \quad \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18}
\end{aligned}$$

$$\begin{aligned} & r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + \\ & 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + \\ & 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \\ & \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8))^{1/3}} - \\ & (128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \\ & 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\ & \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - \\ & 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \\ & 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \\ & 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8))^{1/3}} / \\ & (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\ & \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) / \\ & \left( 4 \sqrt[4]{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\ & \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4) \right) / \right. \\ & \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + \right. \right. \\ & 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - \\ & 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - \\ & 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \\ & \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \\ & 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \\ & 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8))^{1/3}} \Bigg) + \\ & (128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \\ & \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + \\ & 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + \\ & 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \\ & \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + \\ & 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + \\ & 474\,989\,023\,199\,232 \pi^{32} r_1^8))^{1/3}} / (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2))) \Bigg) \Bigg] \Bigg\}, \\ & \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt[4]{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\ & \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4) \right) / \right. \end{aligned}$$

$$\begin{aligned}
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 \right. \\
& \quad \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \quad \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right. \\
& \quad \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \right. \\
& \quad \left. \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 \right. \\
& \quad \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \quad \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) / \\
& \quad \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Bigg) / \\
& \quad \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\
& \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\
& \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right.} \\
& \quad \quad 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\
& \quad \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \left. + \right. \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\
& \quad \quad \left. \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \right. \\
& \quad \quad \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right. \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} \right. \\
& \quad \quad r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} \\
& \quad \quad r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \left. + \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \\
& \quad \quad \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg) \Bigg\} + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) /
\end{aligned}$$





$$\text{Plot}\left[\left\{\left\{\pi - \frac{1}{2} \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3} + \frac{\left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3}}{12\pi^2 r^2}\right)}\right\} - \right.$$

$$\left. \frac{1}{2} \sqrt{\left(8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3} - \frac{\left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3}}{12\pi^2 r^2} - \left(64\pi^3 + \frac{4}{\pi r^2}\right)\right)}\right]$$

$$\left. \left(4 \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3} + \frac{\left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3}}{12\pi^2 r^2}\right)}\right)\right\},$$

$$\left\{\pi - \frac{1}{2} \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3} + \frac{\left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3}}{12\pi^2 r^2}\right)} + \right.$$

$$\left. \frac{1}{2} \sqrt{\left(8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3} - \frac{\left(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8}\right)^{1/3}}{12\pi^2 r^2} - \left(64\pi^3 + \frac{4}{\pi r^2}\right)\right)}\right]$$



$$\begin{aligned}
& \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} - \left(64\,\pi^3 + \frac{4}{\pi\,r^2}\right) / \\
& \left(4\,\sqrt{\left(4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2}\right)\right)\right\}, \\
& \left\{\pi + \frac{1}{2}\,\sqrt{\left(4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2}\right)\right) - \\
& \frac{1}{2}\,\sqrt{\left(8\,\pi^2 - \frac{1}{3\,\pi^2\,r^2} - \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} - \right. \\
& \quad \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} + \left(64\,\pi^3 + \frac{4}{\pi\,r^2}\right) / \right. \\
& \quad \left. \left(4\,\sqrt{\left(4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2}\right)\right)\right)\right\}, \\
& \left\{\pi + \frac{1}{2}\,\sqrt{\left(4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2}\right)\right) + \\
& \frac{1}{2}\,\sqrt{\left(8\,\pi^2 - \frac{1}{3\,\pi^2\,r^2} - \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} - \right.}
\end{aligned}$$

$$\frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} + \left(64 \pi^3 + \frac{4}{\pi r^2}\right) /$$

$$\left(4 \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2}\right)}\right)\right\}, \{r, -6, 6\}]$$

Plot3D[

$$\left\{\left\{\frac{\pi \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left(\frac{4 \pi^2 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)^2}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^2} - \frac{8 \pi^2 \left(13 - 16 \pi^4 + 64 \pi^4 r_1^2\right)}{3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)} + \left(2^{1/3} \left(16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4\right)\right) / \left(3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right) \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)}\right)^{1/3}}\right) + \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)}\right)^{1/3}} / \left(3 \times 2^{1/3} \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)\right)\right\} - \frac{1}{2} \sqrt{\left(\frac{8 \pi^2 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)^2}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^2} - \frac{16 \pi^2 \left(13 - 16 \pi^4 + 64 \pi^4 r_1^2\right)}{3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)} - \left(2^{1/3} \left(16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4\right)\right) / \left(3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right) \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)}\right)^{1/3}}\right) - \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right.$$

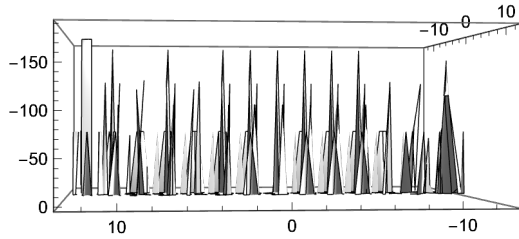
$$\frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right.}$$

$$\frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} -$$

$$\left(64 \pi^3 + \frac{4}{\pi r^2}\right) /$$

$$\left(4 \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2}\right)}\right) \Bigg\},$$

$$\{r_1, -13, 13\}, \{r, -13, 13\}]$$



Plot3D[

$$\left\{ \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right.} \right. \right.$$

$$\left. \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \right. \right.$$

$$\left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \right.$$

$$1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \Big)^{1/3} +$$

$$\left. \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \right.$$

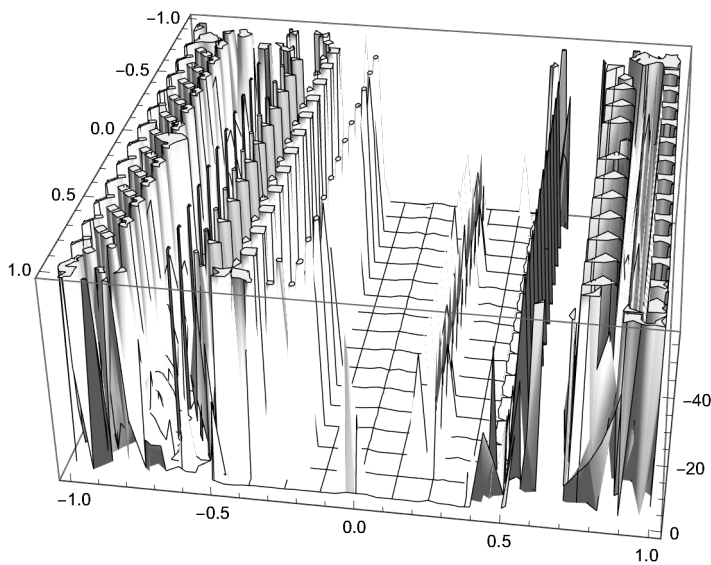
$$\left. \left. \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right.$$

$$\left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \right\} -$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right.} \\
& \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4)) \right) / \\
& \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} \right. \\
& \quad r_1^2 + 6 291 456 \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} \\
& \quad r_1^4 + 33 554 432 \pi^{18} r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + \\
& \quad 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + \\
& \quad 38 963 943 309 312 \pi^{28} r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \\
& \quad \pi^{28} r_1^6 - 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3} \right) - \\
& (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \\
& \quad 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
& \quad \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \\
& \quad 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& \quad 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
& \quad 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3} / \\
& (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right.} \right. \\
& \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4)) \right) / \\
& \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + \right. \\
& \quad 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - \\
& \quad 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - \\
& \quad 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \\
& \quad \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& \quad 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
& \quad 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3} \right) + \\
& (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \\
& \quad \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + \\
& \quad 33 554 432 \pi^{18} r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + \\
& \quad 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \\
& \quad \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + \\
& \quad 22 265 110 462 464 \pi^{28} r_1^6 - 356 241 767 399 424 \pi^{32} r_1^6 +
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. 474\,989\,023\,199\,232\,\pi^{32} r_1^8 \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16\pi^4 + 16\pi^4 r_1^2 \right) \right) \right) \right) \right) \Bigg\}, \\
& \left\{ \frac{1}{2} \sqrt[4]{ \left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13\,824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3} + \right.} \right.} \\
& \quad \left. \left. \frac{\left( 1 + 13\,824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right.} \\
& \quad \left. \frac{1}{2} \sqrt[4]{ \left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13\,824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3} - \right.} \right.} \\
& \quad \left. \left. \frac{\left( 1 + 13\,824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right.} \\
& \quad \left. \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right.} \\
& \quad \left. \left( 4 \sqrt[4]{ \left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13\,824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3} + \right.} \right. \right.} \\
& \quad \left. \left. \left. \frac{\left( 1 + 13\,824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right) \Bigg\},
\end{aligned}$$

$\{r_1, -1, 1\}, \{r, -1, 1\}]$



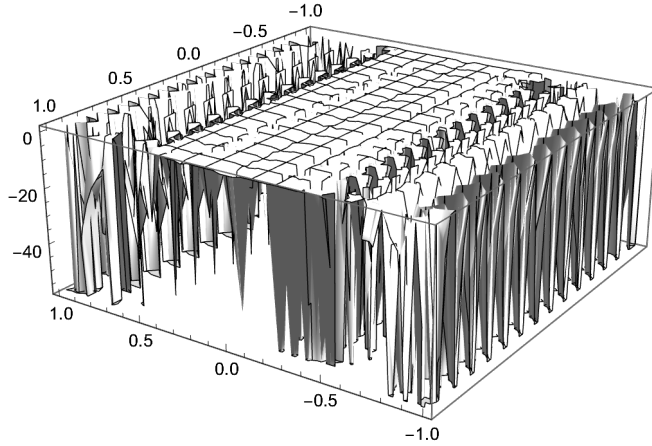
Plot3D[

$$\left\{ \left\{ \frac{\pi \left( 3 - 16\pi^4 + 32\pi^4 r_1^2 \right)}{1 - 16\pi^4 + 32\pi^4 r_1^2} - \frac{1}{2\pi^2} \sqrt[4]{ \left( 4\pi^2 \left( 3 - 16\pi^4 + 32\pi^4 r_1^2 \right)^2 - \frac{8\pi^2 \left( 13 - 16\pi^4 + 64\pi^4 r_1^2 \right)}{1 - 16\pi^4 + 32\pi^4 r_1^2} + \right.} \right.} \right.$$

$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right.
\end{aligned}$$

$$\{r_1, -1, 1\}, \{r, -1, 1\}]$$





Plot3D[

$$\left\{ \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right.} \right. \right.$$

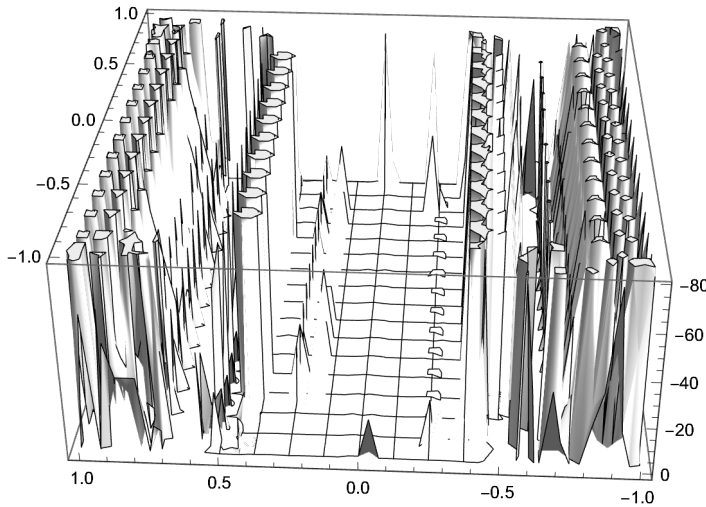
$$\left. \left. \begin{aligned} & (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4)) / \\ & (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)})^{1/3} + \\ & (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)})^{1/3} / (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) \right\} \right\} - \end{aligned}$$

$$\frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right.}$$

$$\left. \begin{aligned} & (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4)) / \\ & (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)})^{1/3} - \end{aligned} \right.$$

$$\begin{aligned}
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \Big/ \\
& \quad \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt[4]{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) \Big/ \right. \\
& \quad \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\
& \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\
& \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 - 7421703487488 \\
& \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \Big) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \\
& \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\
& \quad 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \\
& \quad \left. 474989023199232 \pi^{32} r_1^8) \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Big) \Big) \Big) \Big\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt[4]{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 (1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}}{12 \pi^2 r^2} \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \right. \\
& \quad \left. \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\}, \\
& \{r_1, -1, 1\}, \{r, -1, 1\}
\end{aligned}$$



r1 theta 2 s

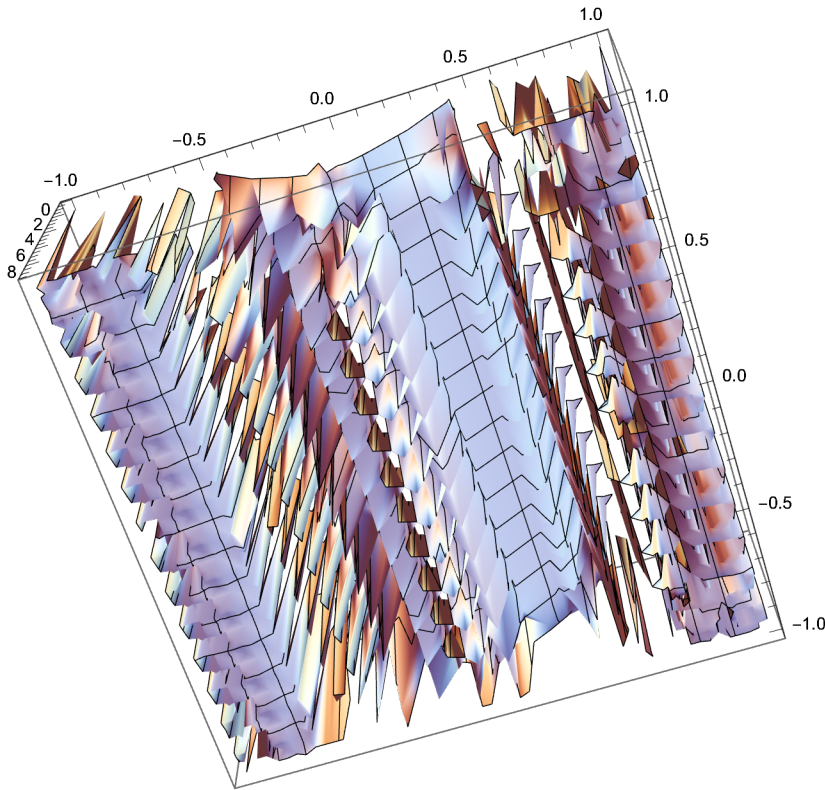
Plot3D[

$$\begin{aligned}
& \left\{ \left\{ \frac{\pi (3 - 16\pi^4 + 32\pi^4 r_1^2)}{1 - 16\pi^4 + 16\pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4 r_1^2)^2} - \frac{8\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2)}{3(1 - 16\pi^4 + 16\pi^4 r_1^2)} + \right. \right. \right. \\
& \quad \left. \left. \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8 r_1^2 - 32768\pi^{12} r_1^2 + 65536\pi^{12} r_1^4) \right) / \right. \right. \\
& \quad \left. \left( 3(1 - 16\pi^4 + 16\pi^4 r_1^2) (128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10} \right. \right. \\
& \quad \left. \left. r_1^2 + 6291456\pi^{14} r_1^2 + 6291456\pi^{18} r_1^2 + 1572864\pi^{14} r_1^4 - 25165824\pi^{18} \right. \right. \\
& \quad \left. \left. r_1^4 + 33554432\pi^{18} r_1^6 + \sqrt{(1811939328\pi^{20} r_1^2 - 86973087744\pi^{24} r_1^2 + \right. \right. \\
& \quad \left. \left. 1391569403904\pi^{28} r_1^2 - 7421703487488\pi^{32} r_1^2 + 347892350976\pi^{24} r_1^4 + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\right. \\
& \quad \left. \pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right)^{1/3} + \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \\
& \quad 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \\
& \quad \sqrt{\left( 1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - \right.} \\
& \quad \left. 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \right. \\
& \quad \left. 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\right. \\
& \quad \left. \pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \right) \Big) + \\
& \frac{1}{2} \sqrt[3]{\left( \frac{8\,\pi^2\,(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2)^2}{(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2)^2} - \frac{16\,\pi^2\,(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2)}{3\,(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + \right. \right. \\
& \quad \left. \left. r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \right. \right. \\
& \quad \left. \left. r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + \right. \right. \right. \\
& \quad \left. \left. 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + \right. \right. \\
& \quad \left. \left. 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\right. \right. \\
& \quad \left. \left. \pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right) \right)^{1/3} - \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \\
& \quad 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \\
& \quad \sqrt{\left( 1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - \right.} \\
& \quad \left. 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \right. \\
& \quad \left. 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \right. \\
& \quad \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right)^{1/3} \Big/ \\
& \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \right) - \left( \frac{768\,\pi^3}{1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2} + \frac{64\,\pi^3\,(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2)^3}{(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2)^3} - \right. \\
& \quad \left. \frac{64\,\pi^3\,(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2)\,(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2)}{(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2)^2} \right) \Big/ \\
& \left( 4 \sqrt[3]{\left( \frac{4\,\pi^2\,(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2)^2}{(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2)^2} - \frac{8\,\pi^2\,(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2)}{3\,(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2)} + \right.} \right. \\
& \quad \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + \right. \right. \\
& \quad \left. \left. 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - \right. \right. \\
& \quad \left. \left. 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}\,r_1^2 - \right. \right. \right. \\
& \quad \left. \left. 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\right. \right. \\
& \quad \left. \left. \pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} - \right.} \\
& \quad \left. \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right.} \\
& \quad \left. \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right. \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \Bigg\} \Bigg\}, \\
& \{r_1, -1, 1\}, \{r, -1, 1\}
\end{aligned}$$



$$\text{Plot3D}\left[ \left\{ \left\{ \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right. \right.
\right.$$

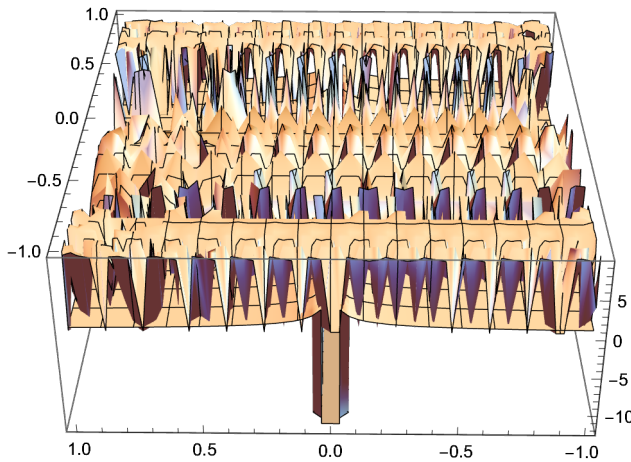
$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right.
\end{aligned}$$

$$\left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) / \right. \\ \left. \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \right. \\ \left. \left. \left. 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \right. \right. \right. \\ \left. \left. \left. 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right. \right. \right. \right. \\ \left. \left. \left. 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \right. \right. \right. \\ \left. \left. \left. \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \right. \\ \left. \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \right. \\ \left. \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \right) + \\ \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\ \left. \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \right. \\ \left. 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \right. \\ \left. \left. 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \right. \right. \\ \left. \left. \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \right. \right. \\ \left. \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \right. \\ \left. \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg] \Bigg\},$$
$$\left\{ \pi - \frac{1}{2} \sqrt[3]{ \left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right. \right. \\ \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) } - \right. \\ \left. \frac{1}{2} \sqrt[3]{ \left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right. \right. \\ \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) } - \right. \\ \left. \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right. \\ \left. \left( 4 \sqrt[3]{ \left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right. \right. \right. \\ \left. \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \Bigg\},$$



$$\begin{aligned}
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \right.} \\
& \quad \left. \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\},
\end{aligned}$$

{r<sub>1</sub>, -1, 1}, {r, -1, 1}]



Plot3D[  

$$\left\{ \left\{ \frac{\pi (3 - 16\pi^4 + 32\pi^4 r_1^2)}{1 - 16\pi^4 + 16\pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4 r_1^2)^2} - \frac{8\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2)}{3(1 - 16\pi^4 + 16\pi^4 r_1^2)} + \right.} \right. \right.$$

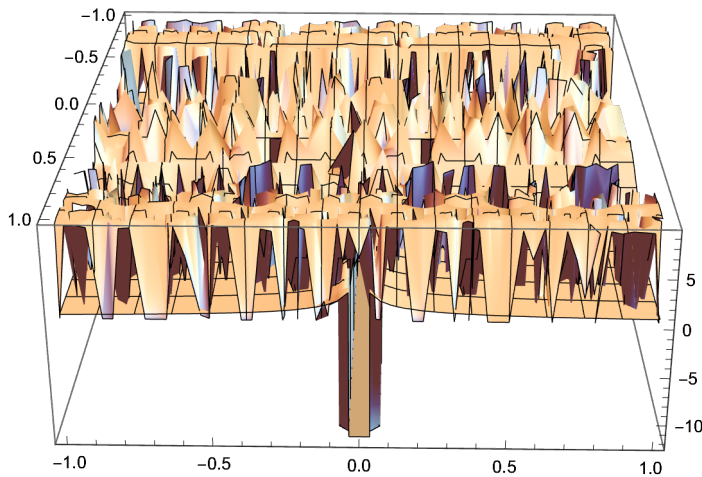
$$\left. \left. \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8 r_1^2 - 32768\pi^{12} r_1^2 + 65536\pi^{12} r_1^4) \right) \right) \right\} /$$

$$\begin{aligned}
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\
& \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} \\
& \quad r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \\
& \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \\
& \quad \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \left. \right)^{1/3} \Bigg) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \\
& \quad \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \left. \right)^{1/3} \Bigg) / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) + \\
& \frac{1}{2} \sqrt[3]{ \left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right. \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\
& \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} \\
& \quad r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \\
& \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \\
& \quad \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \left. \right)^{1/3} \Bigg) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \left. \right)^{1/3} \Bigg) / \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Bigg) / \\
& \left( 4 \sqrt[3]{ \left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right. \right. \\
& \left. \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \right) / \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) - \\
& \frac{1}{2} \sqrt{\left(8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} - \right.} \\
& \left. \frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} + \right. \\
& \left. \left(64 \pi^3 + \frac{4}{\pi r^2}\right) / \right. \\
& \left. \left(4 \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \right. \right. \right. \\
& \left. \left. \left. \frac{\left(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \right\},
\end{aligned}$$

$\{r_1, -1, 1\}, \{r, -1, 1\}]$



Plot3D[

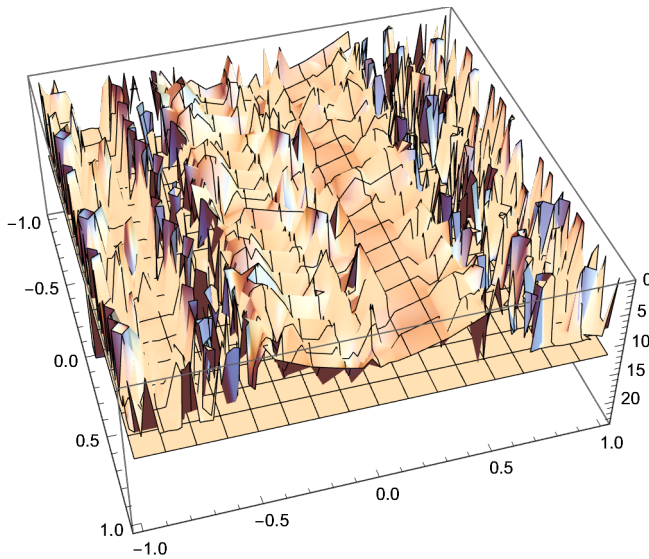
$$\begin{aligned}
& \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \left. \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4)) / \right. \right. \\
& \left. \left. (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\
& \left. \left. r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} \right. \right. \\
& \left. \left. r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1391569403904\pi^{28}r_1^2 - 7421703487488\pi^{32}r_1^2 + 347892350976\pi^{24}r_1^4 + \right. \\
& 38963943309312\pi^{28}r_1^4 + 89060441849856\pi^{32}r_1^4 + 22265110462464 \\
& \left. \pi^{28}r_1^6 - 356241767399424\pi^{32}r_1^6 + 474989023199232\pi^{32}r_1^8 \right)^{1/3} + \\
& \left( 128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10}r_1^2 + 6291456\pi^{14}r_1^2 + \right. \\
& 6291456\pi^{18}r_1^2 + 1572864\pi^{14}r_1^4 - 25165824\pi^{18}r_1^4 + 33554432\pi^{18}r_1^6 + \\
& \sqrt{(1811939328\pi^{20}r_1^2 - 86973087744\pi^{24}r_1^2 + 1391569403904\pi^{28}r_1^2 - \\
& 7421703487488\pi^{32}r_1^2 + 347892350976\pi^{24}r_1^4 + 38963943309312\pi^{28}r_1^4 + \\
& 89060441849856\pi^{32}r_1^4 + 22265110462464\pi^{28}r_1^6 - 356241767399424 \\
& \left. \pi^{32}r_1^6 + 474989023199232\pi^{32}r_1^8) \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4r_1^2) \right) \Big) + \\
& \frac{1}{2} \sqrt[3]{ \left( \frac{8\pi^2(3 - 16\pi^4 + 32\pi^4r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4r_1^2)^2} - \frac{16\pi^2(13 - 16\pi^4 + 64\pi^4r_1^2)}{3(1 - 16\pi^4 + 16\pi^4r_1^2)} - \right. \\
& \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8r_1^2 - 32768\pi^{12}r_1^2 + 65536\pi^{12}r_1^4) \right) \Big/ \\
& \left( 3(1 - 16\pi^4 + 16\pi^4r_1^2) (128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10}r_1^2 + \right. \\
& 6291456\pi^{14}r_1^2 + 6291456\pi^{18}r_1^2 + 1572864\pi^{14}r_1^4 - 25165824\pi^{18}r_1^4 + \\
& 33554432\pi^{18}r_1^6 + \sqrt{(1811939328\pi^{20}r_1^2 - 86973087744\pi^{24}r_1^2 + \\
& 1391569403904\pi^{28}r_1^2 - 7421703487488\pi^{32}r_1^2 + 347892350976\pi^{24}r_1^4 + \\
& 38963943309312\pi^{28}r_1^4 + 89060441849856\pi^{32}r_1^4 + 22265110462464 \\
& \left. \pi^{28}r_1^6 - 356241767399424\pi^{32}r_1^6 + 474989023199232\pi^{32}r_1^8) \right)^{1/3} - \\
& (128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10}r_1^2 + 6291456\pi^{14}r_1^2 + \\
& 6291456\pi^{18}r_1^2 + 1572864\pi^{14}r_1^4 - 25165824\pi^{18}r_1^4 + 33554432\pi^{18}r_1^6 + \\
& \sqrt{(1811939328\pi^{20}r_1^2 - 86973087744\pi^{24}r_1^2 + 1391569403904\pi^{28}r_1^2 - \\
& 7421703487488\pi^{32}r_1^2 + 347892350976\pi^{24}r_1^4 + 38963943309312\pi^{28}r_1^4 + \\
& 89060441849856\pi^{32}r_1^4 + 22265110462464\pi^{28}r_1^6 - \\
& \left. 356241767399424\pi^{32}r_1^6 + 474989023199232\pi^{32}r_1^8) \right)^{1/3} \Big/ \\
& \left( 3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4r_1^2) \right) - \left( \frac{768\pi^3}{1 - 16\pi^4 + 16\pi^4r_1^2} + \frac{64\pi^3(3 - 16\pi^4 + 32\pi^4r_1^2)^3}{(1 - 16\pi^4 + 16\pi^4r_1^2)^3} - \right. \\
& \left. \frac{64\pi^3(3 - 16\pi^4 + 32\pi^4r_1^2)(13 - 16\pi^4 + 64\pi^4r_1^2)}{(1 - 16\pi^4 + 16\pi^4r_1^2)^2} \right) \Big/ \\
& \left( 4 \sqrt[3]{ \left( \frac{4\pi^2(3 - 16\pi^4 + 32\pi^4r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4r_1^2)^2} - \frac{8\pi^2(13 - 16\pi^4 + 64\pi^4r_1^2)}{3(1 - 16\pi^4 + 16\pi^4r_1^2)} + \right. \right. \\
& \left. \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8r_1^2 - 32768\pi^{12}r_1^2 + 65536\pi^{12}r_1^4) \right) \Big/ \right. \\
& \left. \left( 3(1 - 16\pi^4 + 16\pi^4r_1^2) (128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + \right. \right. \\
& 24576\pi^{10}r_1^2 + 6291456\pi^{14}r_1^2 + 6291456\pi^{18}r_1^2 + 1572864\pi^{14}r_1^4 - \\
& 25165824\pi^{18}r_1^4 + 33554432\pi^{18}r_1^6 + \sqrt{(1811939328\pi^{20}r_1^2 - \\
& 86973087744\pi^{24}r_1^2 + 1391569403904\pi^{28}r_1^2 - 7421703487488
\end{aligned}$$

$$\begin{aligned} & \left( \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^6 + \right. \\ & 89\,060\,441\,849\,856 \pi^{32} r_1^8 + 22\,265\,110\,462\,464 \pi^{28} r_1^{10} - \\ & \left. 356\,241\,767\,399\,424 \pi^{32} r_1^{12} + 474\,989\,023\,199\,232 \pi^{32} r_1^{14} \right)^{1/3} + \\ & \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{22} r_1^2 + 6\,291\,456 \right. \\ & \pi^{26} r_1^4 + 6\,291\,456 \pi^{20} r_1^6 + 1\,572\,864 \pi^{24} r_1^8 - 25\,165\,824 \pi^{28} r_1^{10} + \\ & 33\,554\,432 \pi^{32} r_1^{12} + \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^4 + \right. \\ & 1\,391\,569\,403\,904 \pi^{28} r_1^6 - 7\,421\,703\,487\,488 \pi^{32} r_1^8 + 347\,892\,350\,976 \\ & \pi^{24} r_1^{10} + 38\,963\,943\,309\,312 \pi^{28} r_1^{12} + 89\,060\,441\,849\,856 \pi^{32} r_1^{14} + \\ & 22\,265\,110\,462\,464 \pi^{28} r_1^{16} - 356\,241\,767\,399\,424 \pi^{32} r_1^{18} + \\ & \left. \left. \left. 474\,989\,023\,199\,232 \pi^{32} r_1^{20} \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \right) \right) \Bigg\}, \\ & \left\{ \pi - \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} + \right.} \right. \\ & \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) - \right. \\ & \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} - \right.} \\ & \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} - \right. \\ & \left. \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right. \\ & \left. \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} + \right.} \right. \right. \\ & \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \Bigg\}, \\ & \left\{ \pi + \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} + \right.} \right. \\ & \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) + \right. \end{aligned}$$

$$\frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} + \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right)} \right)} \right)} \right\},$$

$$\{r_1, -1, 1\}, \{r, -1, 1\}]$$



Plot3D[

$$\left\{ \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464} \right)} \right)} \right\} \right\},$$

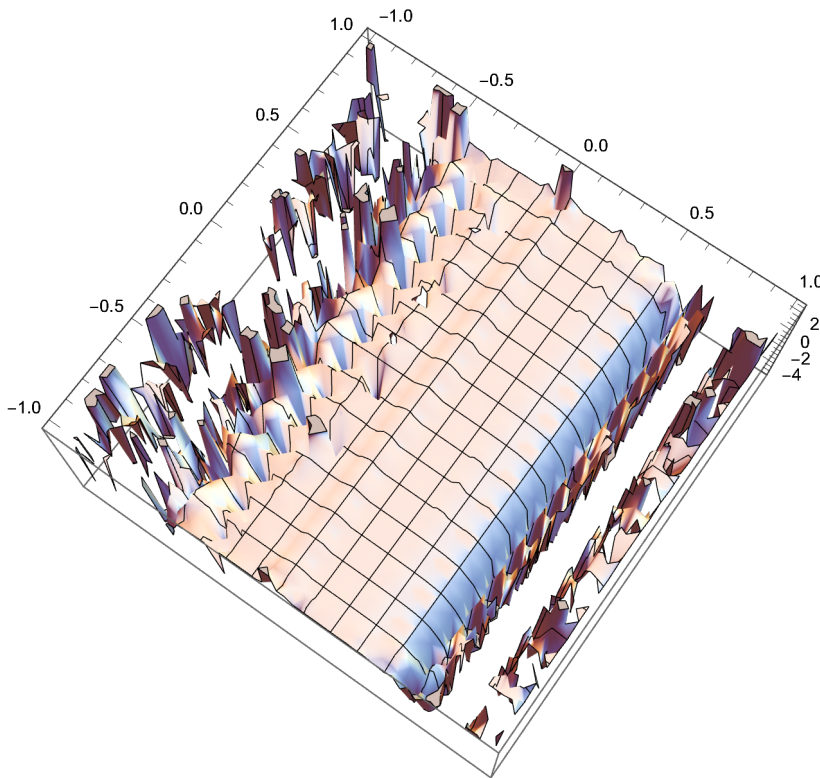
$$\begin{aligned}
& \left( \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \right. \\
& \quad 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \\
& \quad \quad \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \right. \\
& \quad \quad \left. \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Big) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + \right. \right. \\
& \quad \quad 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + \right.} \\
& \quad \quad \quad 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \\
& \quad \quad \quad \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \Big) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \right. \\
& \quad \quad 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + \right.} \\
& \quad \quad \quad 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \\
& \quad \quad \quad \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \Big/ \\
& \quad \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \\
& \quad \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + \right. \right. \\
& \quad \quad \quad 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - \\
& \quad \quad \quad 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - \right.} \\
& \quad \quad \quad \quad 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \\
& \quad \quad \quad \quad \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \\
& \quad \quad \quad \quad \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \left( 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} + \right. \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 \right. \\
& \left. + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + \right. \\
& \left. 33\,554\,432\,\pi^{18}r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + \right. \right. \\
& \left. \left. 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 \right. \right. \\
& \left. \left. + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + \right. \right. \\
& \left. \left. 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + \right. \right. \\
& \left. \left. 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right) \right) \Bigg\}, \\
& \left\{ \pi - \frac{1}{2} \sqrt{ \left( 4\,\pi^2 - \frac{1}{6\,\pi^2r^2} + \frac{1}{12\,\pi^2r^2 \left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3} + \right. \right. } \right. \\
& \left. \left. \frac{\left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3}}{12\,\pi^2r^2} \right) - \right. \\
& \frac{1}{2} \sqrt{ \left( 8\,\pi^2 - \frac{1}{3\,\pi^2r^2} - \frac{1}{12\,\pi^2r^2 \left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3} - \right. } \\
& \left. \left. \frac{\left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3}}{12\,\pi^2r^2} - \right. \right. \\
& \left. \left( 64\,\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \left. \left( 4 \sqrt{ \left( 4\,\pi^2 - \frac{1}{6\,\pi^2r^2} + \frac{1}{12\,\pi^2r^2 \left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3} + \right. \right. } \right. \\
& \left. \left. \frac{\left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3}}{12\,\pi^2r^2} \right) \right) \Bigg\}, \\
& \left\{ \pi - \frac{1}{2} \sqrt{ \left( 4\,\pi^2 - \frac{1}{6\,\pi^2r^2} + \frac{1}{12\,\pi^2r^2 \left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3} + \right. \right. } \right. \\
& \left. \left. \frac{\left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3}}{12\,\pi^2r^2} \right) - \right. \\
& \left. \left. \frac{\left( 1 + 13\,824\,\pi^8r^4 + 96\,\sqrt{3}\,\pi^4\sqrt{r^4 + 6912\,\pi^8r^8} \right)^{1/3}}{12\,\pi^2r^2} \right) \right\}
\end{aligned}$$

$$\frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} - \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right)} \right) \right) \right) \right\},$$

$$\{r_1, -1, 1\}, \{r, -1, 1\}]$$



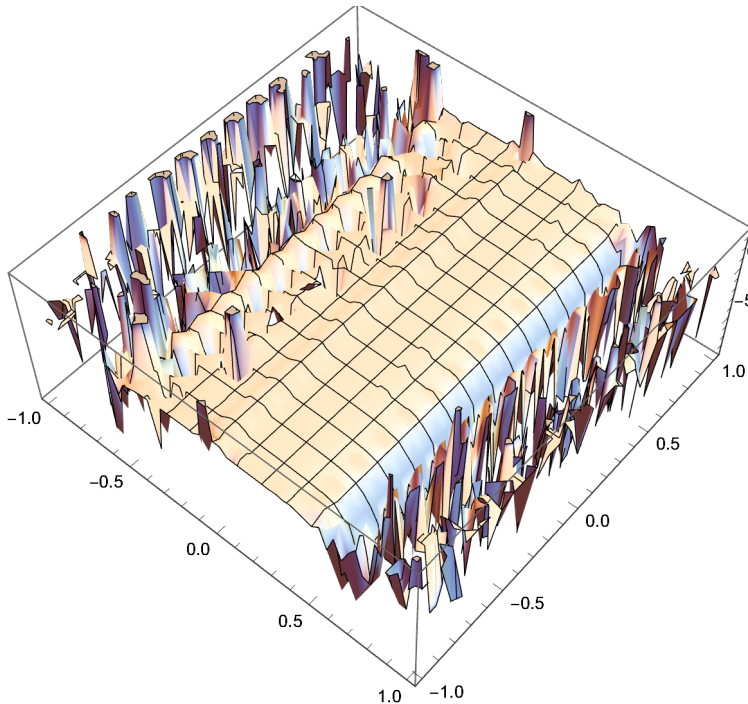
$$\text{Plot3D}\left[\left\{\left\{\frac{\pi \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left(\frac{4 \pi^2 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)^2}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^2} - \frac{8 \pi^2 \left(13 - 16 \pi^4 + 64 \pi^4 r_1^2\right)}{3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)} + \right.}\right.\right.$$

$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right.
\end{aligned}$$

$$\begin{aligned} & \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) / \right. \\ & \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\ & \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\ & \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right.} \\ & \quad 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\ & \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\ & \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\ & \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\ & \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\ & \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\ & \quad 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\ & \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\ & \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\ & \quad \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \\ & \quad \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg] \Bigg\}, \\ & \left\{ \pi - \frac{1}{2} \sqrt[3]{ \left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right. \right. \\ & \quad \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) } - \right. \\ & \quad \left. \frac{1}{2} \sqrt[3]{ \left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right. \right. \\ & \quad \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) } - \right. \\ & \quad \left. \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right. \\ & \quad \left. \left( 4 \sqrt[3]{ \left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right. \right. \right. \\ & \quad \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \Bigg] \Bigg\}, \end{aligned}$$

$$\begin{aligned}
& \left\{ \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \right.} \\
& \quad \left. \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\},
\end{aligned}$$

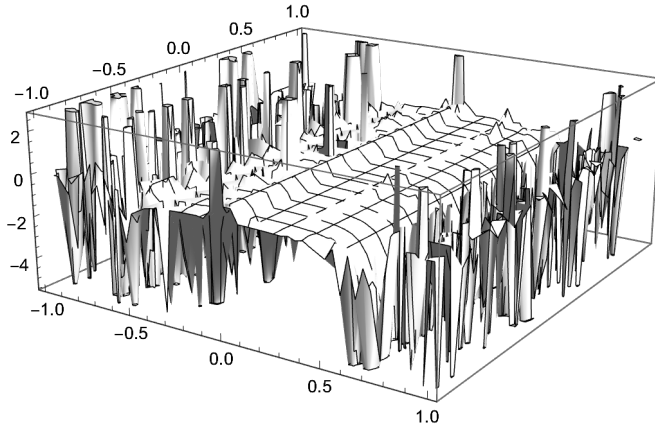
$\{r_1, -1, 1\}, \{r, -1, 1\}]$



Plot3D[  
 $r, r, \pi (3 - 16\pi^4 + 32\pi^4 r_1^2) - 1 \mid (4\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2 - 8\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2))$

$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} \right) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right)} \right)^{1/3} / \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.}
\end{aligned}$$





Plot3D[

$$\begin{aligned}
 & \left\{ \frac{\pi (3 - 16\pi^4 + 32\pi^4 r_1^2)}{1 - 16\pi^4 + 16\pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4 r_1^2)^2} - \frac{8\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2)}{3(1 - 16\pi^4 + 16\pi^4 r_1^2)} \right.} \right. \\
 & \quad \left. \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8 r_1^2 - 32768\pi^{12} r_1^2 + 65536\pi^{12} r_1^4) \right) / \right. \\
 & \quad \left( 3(1 - 16\pi^4 + 16\pi^4 r_1^2) (128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10} \right. \\
 & \quad \left. r_1^2 + 6291456\pi^{14} r_1^2 + 6291456\pi^{18} r_1^2 + 1572864\pi^{14} r_1^4 - 25165824\pi^{18} \right. \\
 & \quad \left. r_1^4 + 33554432\pi^{18} r_1^6 + \sqrt{(1811939328\pi^{20} r_1^2 - 86973087744\pi^{24} r_1^2 + \right. \\
 & \quad \left. 1391569403904\pi^{28} r_1^2 - 7421703487488\pi^{32} r_1^2 + 347892350976\pi^{24} r_1^4 + \right. \\
 & \quad \left. 38963943309312\pi^{28} r_1^4 + 89060441849856\pi^{32} r_1^4 + 22265110462464 \right. \\
 & \quad \left. \pi^{28} r_1^6 - 356241767399424\pi^{32} r_1^6 + 474989023199232\pi^{32} r_1^8) \right)^{1/3} \Big) + \\
 & \quad \left( 128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10} r_1^2 + 6291456\pi^{14} r_1^2 + \right. \\
 & \quad \left. 6291456\pi^{18} r_1^2 + 1572864\pi^{14} r_1^4 - 25165824\pi^{18} r_1^4 + 33554432\pi^{18} r_1^6 + \right. \\
 & \quad \left. \sqrt{(1811939328\pi^{20} r_1^2 - 86973087744\pi^{24} r_1^2 + 1391569403904\pi^{28} r_1^2 - \right. \\
 & \quad \left. 7421703487488\pi^{32} r_1^2 + 347892350976\pi^{24} r_1^4 + 38963943309312\pi^{28} r_1^4 + \right. \\
 & \quad \left. 89060441849856\pi^{32} r_1^4 + 22265110462464\pi^{28} r_1^6 - 356241767399424 \right. \\
 & \quad \left. \pi^{32} r_1^6 + 474989023199232\pi^{32} r_1^8) \right)^{1/3} / (3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4 r_1^2)) \Big) - \\
 & \quad \frac{1}{2} \sqrt{\left( \frac{8\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4 r_1^2)^2} - \frac{16\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2)}{3(1 - 16\pi^4 + 16\pi^4 r_1^2)} \right.} \\
 & \quad \left. \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8 r_1^2 - 32768\pi^{12} r_1^2 + 65536\pi^{12} r_1^4) \right) / \right. \\
 & \quad \left( 3(1 - 16\pi^4 + 16\pi^4 r_1^2) (128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10} \right. \\
 & \quad \left. r_1^2 + 6291456\pi^{14} r_1^2 + 6291456\pi^{18} r_1^2 + 1572864\pi^{14} r_1^4 - 25165824\pi^{18} \right. \\
 & \quad \left. r_1^4 + 33554432\pi^{18} r_1^6 + \sqrt{(1811939328\pi^{20} r_1^2 - 86973087744\pi^{24} r_1^2 + \right. \\
 & \quad \left. 1391569403904\pi^{28} r_1^2 - 7421703487488\pi^{32} r_1^2 + 347892350976\pi^{24} r_1^4 + \right. \\
 & \quad \left. 38963943309312\pi^{28} r_1^4 + 89060441849856\pi^{32} r_1^4 + 22265110462464 \right. \\
 & \quad \left. \pi^{28} r_1^6 - 356241767399424\pi^{32} r_1^6 + 474989023199232\pi^{32} r_1^8) \right)^{1/3} \Big) -
 \end{aligned}$$



$$\begin{aligned}
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \Big/ \\
& \quad \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt[4]{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) \Big/ \right. \\
& \quad \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\
& \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\
& \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 - 7421703487488 \\
& \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \Big) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\
& \quad 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \\
& \quad 474989023199232 \pi^{32} r_1^8)}^{1/3} \Big/ (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) \Big) \Big) \Big) \Big) \Big\}, \\
& \quad \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt[4]{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) \Big/ \right. \\
& \quad \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + \right. \right. \\
& \quad 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \Big) \Big) \Big) \Big) \Big\},
\end{aligned}$$

$$\begin{aligned}
& \left( \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \right. \\
& \quad 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \\
& \quad \quad \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \right. \\
& \quad \quad \left. \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Big) + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + \right. \right. \\
& \quad \quad 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + \right.} \\
& \quad \quad \quad 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \\
& \quad \quad \quad \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \Big) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \right. \\
& \quad \quad 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + \right.} \\
& \quad \quad \quad 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \\
& \quad \quad \quad \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \Big/ \\
& \quad \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \\
& \quad \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + \right. \right. \\
& \quad \quad \quad 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - \\
& \quad \quad \quad 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - \right.} \\
& \quad \quad \quad \quad 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \\
& \quad \quad \quad \quad \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \\
& \quad \quad \quad \quad \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} + \right. \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 \right. \\
& \quad \left. + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + \right. \\
& \quad \left. 33\,554\,432\,\pi^{18}r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + \right. \right. \\
& \quad \left. \left. 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 \right. \right. \\
& \quad \left. \left. + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + \right. \right. \\
& \quad \left. \left. 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + \right. \right. \\
& \quad \left. \left. 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right) \right) \Bigg\}, \\
& \left\{ \frac{\pi \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right)}{1 - 16\,\pi^4 + 16\,\pi^4r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)^2} - \frac{8\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8r_1^2 - 32\,768\,\pi^{12}r_1^2 + 65\,536\,\pi^{12}r_1^4 \right) \right) / \right. \\
& \quad \left. \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right. \right. \\
& \quad \left. \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 \right. \right. \\
& \quad \left. \left. + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 \right. \right. \\
& \quad \left. \left. + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right. \right. \right. \\
& \quad \left. \left. 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \right. \right. \\
& \quad \left. \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - \right. \right. \\
& \quad \left. \left. 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \right) + \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad \left. 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 + \right. \\
& \quad \left. \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right. \right. \\
& \quad \left. \left. 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \right. \right. \\
& \quad \left. \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}r_1^6 \right. \right. \\
& \quad \left. \left. + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right) \right) \Bigg\} - \\
& \frac{1}{2} \sqrt{\left( \frac{8\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)^2} - \frac{16\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)} - \right. \\
& \quad \left. \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8r_1^2 - 32\,768\,\pi^{12}r_1^2 + 65\,536\,\pi^{12}r_1^4 \right) \right) / \right. \\
& \quad \left. \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 \right. \right. \right. \\
& \quad \left. \left. + 6\,291\,456\,\pi^{14}r_1^2 + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 \right. \right. \\
& \quad \left. \left. + 33\,554\,432\,\pi^{18}r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + \right. \right. \right. \\
& \quad \left. \left. 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + \right. \right. \\
& \quad \left. \left. 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 \right. \right. \\
& \quad \left. \left. + 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \right) - \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right.
\end{aligned}$$

[illegible]

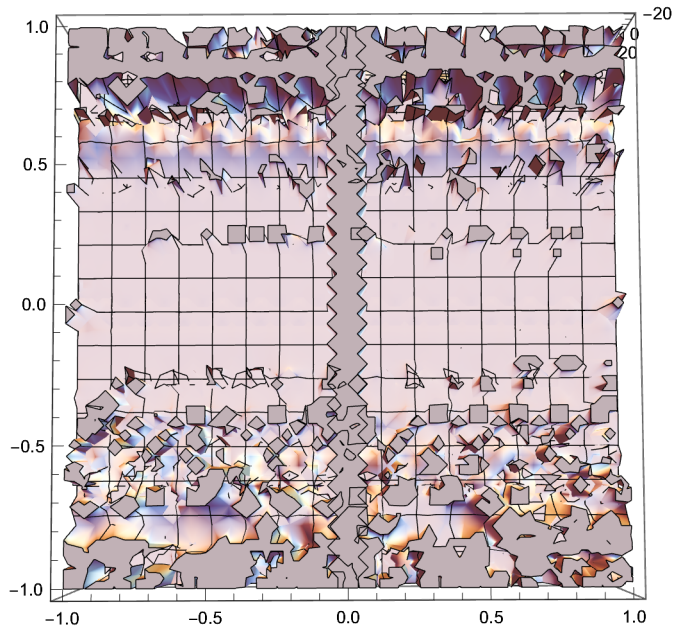
$$\begin{aligned}
& \left( 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} + \\
& \left( 128\pi^6 - 6144\pi^{10} + 98\,304\pi^{14} - 524\,288\pi^{18} + 24\,576\pi^{10}r_1^2 + 6\,291\,456\pi^{14}r_1^2 + \right. \\
& \quad 6\,291\,456\pi^{18}r_1^2 + 1\,572\,864\pi^{14}r_1^4 - 25\,165\,824\pi^{18}r_1^4 + 33\,554\,432\pi^{18}r_1^6 + \\
& \quad \sqrt{(1\,811\,939\,328\pi^{20}r_1^2 - 86\,973\,087\,744\pi^{24}r_1^2 + 1\,391\,569\,403\,904\pi^{28}r_1^2 - \\
& \quad 7\,421\,703\,487\,488\pi^{32}r_1^2 + 347\,892\,350\,976\pi^{24}r_1^4 + 38\,963\,943\,309\,312\pi^{28}r_1^4 + \\
& \quad 89\,060\,441\,849\,856\pi^{32}r_1^4 + 22\,265\,110\,462\,464\pi^{28}r_1^6 - 356\,241\,767\,399\,424} \\
& \quad \left. \pi^{32}r_1^6 + 474\,989\,023\,199\,232\pi^{32}r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4r_1^2) \right) \Big) + \\
& \frac{1}{2} \sqrt[4]{ \left( \frac{8\pi^2(3 - 16\pi^4 + 32\pi^4r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4r_1^2)^2} - \frac{16\pi^2(13 - 16\pi^4 + 64\pi^4r_1^2)}{3(1 - 16\pi^4 + 16\pi^4r_1^2)} - \right. \\
& \quad \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8r_1^2 - 32\,768\pi^{12}r_1^2 + 65\,536\pi^{12}r_1^4) \right) \Big/ \\
& \quad \left( 3(1 - 16\pi^4 + 16\pi^4r_1^2) \right) \\
& \quad \left( 128\pi^6 - 6144\pi^{10} + 98\,304\pi^{14} - 524\,288\pi^{18} + 24\,576\pi^{10}r_1^2 + 6\,291\,456\pi^{14}r_1^2 + \right. \\
& \quad \quad r_1^2 + 6\,291\,456\pi^{18}r_1^2 + 1\,572\,864\pi^{14}r_1^4 - 25\,165\,824\pi^{18}r_1^4 + 33\,554\,432\pi^{18}r_1^6 \\
& \quad \quad r_1^6 + \sqrt{(1\,811\,939\,328\pi^{20}r_1^2 - 86\,973\,087\,744\pi^{24}r_1^2 + 1\,391\,569\,403\,904\pi^{28}r_1^2 - \\
& \quad \quad 7\,421\,703\,487\,488\pi^{32}r_1^2 + 347\,892\,350\,976\pi^{24}r_1^4 + 38\,963\,943\,309\,312\pi^{28}r_1^4 + \\
& \quad \quad 89\,060\,441\,849\,856\pi^{32}r_1^4 + 22\,265\,110\,462\,464\pi^{28}r_1^6 - \\
& \quad \quad \left. 356\,241\,767\,399\,424\pi^{32}r_1^6 + 474\,989\,023\,199\,232\pi^{32}r_1^8 \right)^{1/3} \Big) - \\
& \quad \left( 128\pi^6 - 6144\pi^{10} + 98\,304\pi^{14} - 524\,288\pi^{18} + 24\,576\pi^{10}r_1^2 + 6\,291\,456\pi^{14}r_1^2 + \right. \\
& \quad 6\,291\,456\pi^{18}r_1^2 + 1\,572\,864\pi^{14}r_1^4 - 25\,165\,824\pi^{18}r_1^4 + 33\,554\,432\pi^{18}r_1^6 + \\
& \quad \sqrt{(1\,811\,939\,328\pi^{20}r_1^2 - 86\,973\,087\,744\pi^{24}r_1^2 + 1\,391\,569\,403\,904\pi^{28}r_1^2 - \\
& \quad 7\,421\,703\,487\,488\pi^{32}r_1^2 + 347\,892\,350\,976\pi^{24}r_1^4 + 38\,963\,943\,309\,312\pi^{28}r_1^4 + \\
& \quad 89\,060\,441\,849\,856\pi^{32}r_1^4 + 22\,265\,110\,462\,464\pi^{28}r_1^6 - \\
& \quad \left. 356\,241\,767\,399\,424\pi^{32}r_1^6 + 474\,989\,023\,199\,232\pi^{32}r_1^8 \right)^{1/3} \Big/ \\
& \quad \left( 3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4r_1^2) \right) + \left( \frac{768\pi^3}{1 - 16\pi^4 + 16\pi^4r_1^2} + \frac{64\pi^3(3 - 16\pi^4 + 32\pi^4r_1^2)^3}{(1 - 16\pi^4 + 16\pi^4r_1^2)^3} - \right. \\
& \quad \left. \frac{64\pi^3(3 - 16\pi^4 + 32\pi^4r_1^2)(13 - 16\pi^4 + 64\pi^4r_1^2)}{(1 - 16\pi^4 + 16\pi^4r_1^2)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt[4]{ \left( \frac{4\pi^2(3 - 16\pi^4 + 32\pi^4r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4r_1^2)^2} - \frac{8\pi^2(13 - 16\pi^4 + 64\pi^4r_1^2)}{3(1 - 16\pi^4 + 16\pi^4r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8r_1^2 - 32\,768\pi^{12}r_1^2 + 65\,536\pi^{12}r_1^4) \right) \Big/ \right. \\
& \quad \left. \left( 3(1 - 16\pi^4 + 16\pi^4r_1^2) \right) (128\pi^6 - 6144\pi^{10} + 98\,304\pi^{14} - 524\,288\pi^{18} + \right. \\
& \quad 24\,576\pi^{10}r_1^2 + 6\,291\,456\pi^{14}r_1^2 + 6\,291\,456\pi^{18}r_1^2 + 1\,572\,864\pi^{14}r_1^4 - \\
& \quad 25\,165\,824\pi^{18}r_1^4 + 33\,554\,432\pi^{18}r_1^6 + \sqrt{(1\,811\,939\,328\pi^{20}r_1^2 - \\
& \quad 86\,973\,087\,744\pi^{24}r_1^2 + 1\,391\,569\,403\,904\pi^{28}r_1^2 - 7\,421\,703\,487\,488}
\end{aligned}$$

$$\begin{aligned} & \left( \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^6 + \right. \\ & 89\,060\,441\,849\,856 \pi^{32} r_1^8 + 22\,265\,110\,462\,464 \pi^{28} r_1^{10} - \\ & \left. 356\,241\,767\,399\,424 \pi^{32} r_1^{12} + 474\,989\,023\,199\,232 \pi^{32} r_1^{14} \right)^{1/3} + \\ & \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{22} r_1^2 + 6\,291\,456 \right. \\ & \pi^{26} r_1^4 + 6\,291\,456 \pi^{20} r_1^6 + 1\,572\,864 \pi^{24} r_1^8 - 25\,165\,824 \pi^{28} r_1^{10} + \\ & 33\,554\,432 \pi^{32} r_1^{12} + \sqrt{\left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^4 + \right. \\ & 1\,391\,569\,403\,904 \pi^{28} r_1^6 - 7\,421\,703\,487\,488 \pi^{32} r_1^8 + 347\,892\,350\,976 \\ & \pi^{24} r_1^{10} + 38\,963\,943\,309\,312 \pi^{28} r_1^{12} + 89\,060\,441\,849\,856 \pi^{32} r_1^{14} + \\ & 22\,265\,110\,462\,464 \pi^{28} r_1^{16} - 356\,241\,767\,399\,424 \pi^{32} r_1^{18} + \\ & \left. \left. \left. 474\,989\,023\,199\,232 \pi^{32} r_1^{20} \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \right) \right) \right) \Bigg\}, \\ & \left\{ \pi - \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} + \right.} \right. \\ & \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) - \right. \\ & \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} - \right.} \\ & \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} - \right. \right. \\ & \left. \left. \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right. \right. \\ & \left. \left. \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} + \right.} \right. \right. \right. \\ & \left. \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \right) \Bigg\}, \\ & \left\{ \pi - \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3} + \right.} \right. \\ & \left. \left. \frac{\left( 1 + 13\,824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) + \right. \end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \right. \\
& \quad \left. \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \right. \\
& \quad \left. \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) + \\
& \frac{1}{2} \sqrt{\left(8\,\pi^2 - \frac{1}{3\,\pi^2\,r^2} - \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} + \right. \\
& \quad \left. \left(64\,\pi^3 + \frac{4}{\pi\,r^2}\right) / \right. \\
& \quad \left. \left(4 \sqrt{\left(4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 + 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) \right) \right) \right) \Bigg\} \Bigg\},
\end{aligned}$$

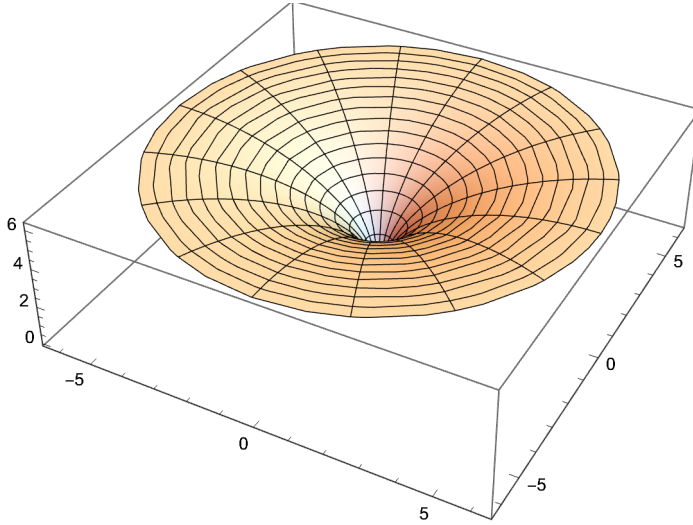
$\{r_1, -1, 1\}, \{r, -1, 1\}]$





## 5 Torus

RevolutionPlot3D[ $\sqrt{4\pi\theta - \theta^2}$ , { $\theta$ ,  $-2\pi$ ,  $2\pi$ }]



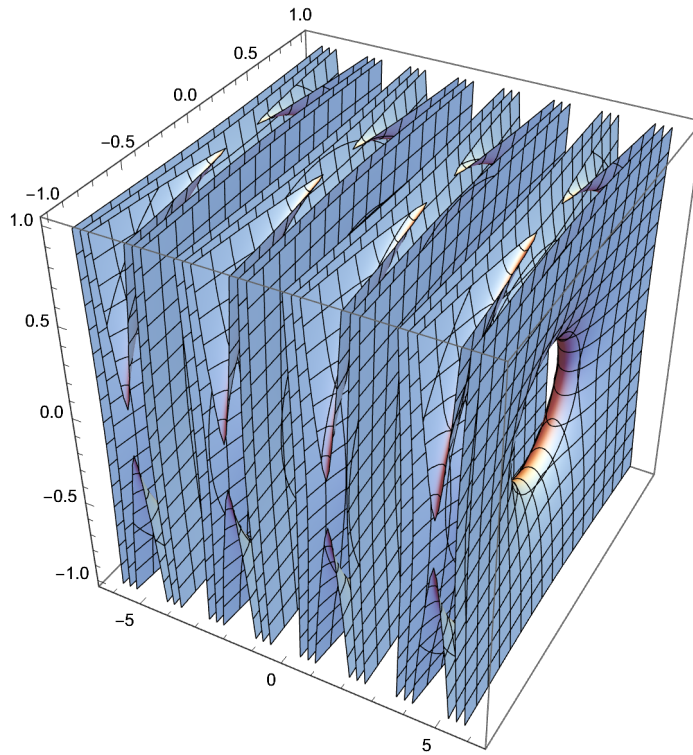
$\text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right]$

$\text{Solve}\left[\frac{\sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) \text{Abs}[x + \text{I} y]}}{2\pi} = \text{Abs}[x + \text{I} y] \sin[\beta], \beta\right]$

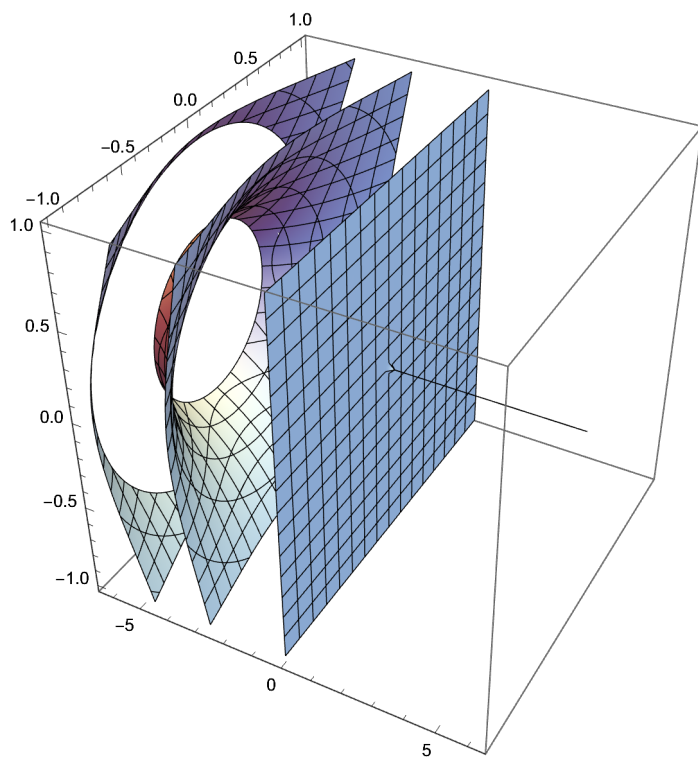
$\text{Solve}\left[\frac{\sqrt{4\pi - \theta} \sqrt{\theta}}{2\pi} = \sin[\beta], \beta\right]$

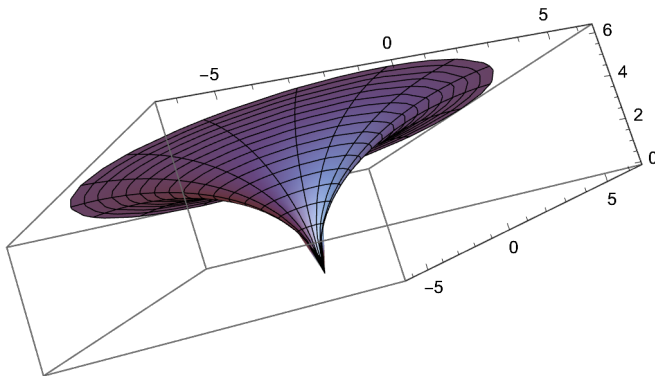
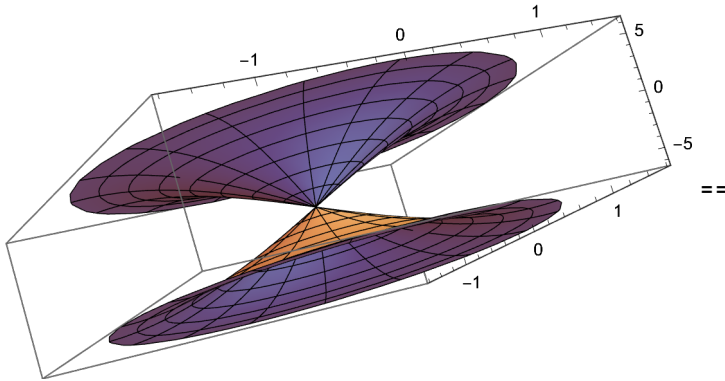
$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{4\pi - \theta} \sqrt{\theta}}{2\pi}\right]\right\}\right\}$

`ContourPlot3D` $\left[ \frac{2 \pi \sin \left[ \operatorname{ArcSin} \left[ \frac{4 \pi \operatorname{Abs}[x + \mathbf{i} y] 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \operatorname{Abs}[x + \mathbf{i} y] \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}{4 \pi^2} \right) \right]}{\{ \beta, -2 \pi, 2 \pi \}, \{ x, -1, 1 \}, \{ y, -1, 1 \}} \right]$



```
ContourPlot3D[2 π Sin[ArcSin[ $\frac{4 \pi \text{Abs}[x + \text{i} y] \theta - \text{Abs}[x + \text{i} y] \theta^2}{4 \pi^2}$ ]]],  
{θ, -2 π, 2 π}, {x, -1, 1}, {y, -1, 1}]
```





## 8-Fold

$$c := (2.99792458 * 10^8)$$

$$r' * \theta' = r \theta = 2 \pi r - 2 \pi r_1 = 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2} \quad (1)$$

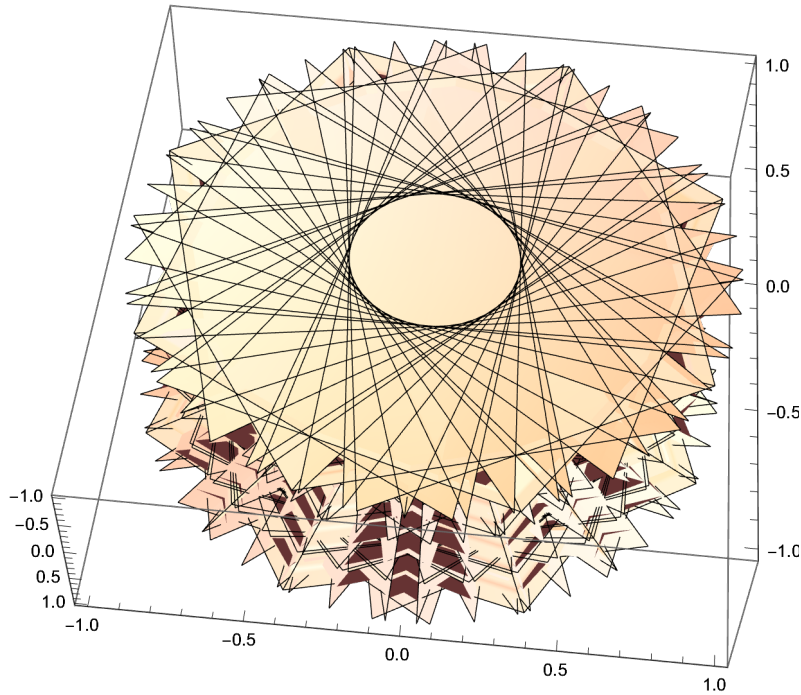
$$r' * \theta' = r \theta == 2 \pi r' - 2 \pi r_1' == 2 \pi r' - 2 \pi \sqrt{r'^2 - \eta'^2}$$

$$\eta' = \eta \sqrt{1 - ((v^2) / (c^2))} = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - ((v^2) / (c^2))}$$

$$r' * \theta' = r \theta == 2 \pi r' - 2 \pi r_1' ==$$

$$2 \pi r' - 2 \pi \sqrt{r'^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - ((v^2) / (c^2))} \right)^2}$$

RevolutionPlot3D $\left[\eta \sqrt{1 - ((v^2) / (c^2))}, \{\eta, -1, 1\}, \{v, -100\,000, 100\,000\}\right]$



$$\eta \sqrt{1 - ((v^2) / (c^2))}$$

$$r' * \theta' = r \theta == 2 \pi r' - 2 \pi r_1' == 2 \pi r' - 2 \pi \sqrt{r'^2 - \eta'^2}$$

$$r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \theta \sqrt{1 - ((v^2) / (c^2))} = 2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - 2 \pi \sqrt{2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - \left( \eta \sqrt{1 - ((v^2) / (c^2))} \right)^2}$$

$$\text{Solve}\left[\left(r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right) \left( \theta \sqrt{1 - ((v^2) / (c^2))} \right) == 2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - 2 \pi \sqrt{2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - \left( \eta \sqrt{1 - ((v^2) / (c^2))} \right)^2}, v\right]$$

$$\text{RevolutionPlot3D}\left[\left\{(-c), (c), \left(-\sqrt{c^2 - \frac{8 c^2 \pi^2}{3 \theta^2} + \frac{8 c^2 \pi^2 \eta^2}{3 r^2 \theta^2}} + \frac{(16 \times 2^{1/3} c^4 \pi^4 r^4)}{\left(3 \left(128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \sqrt{4 \left(-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5\right)^3 + \left(128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8\right)^2}\right)^{1/3}}\right\}\right]$$

[illegible]

[illegible]

[illegible]





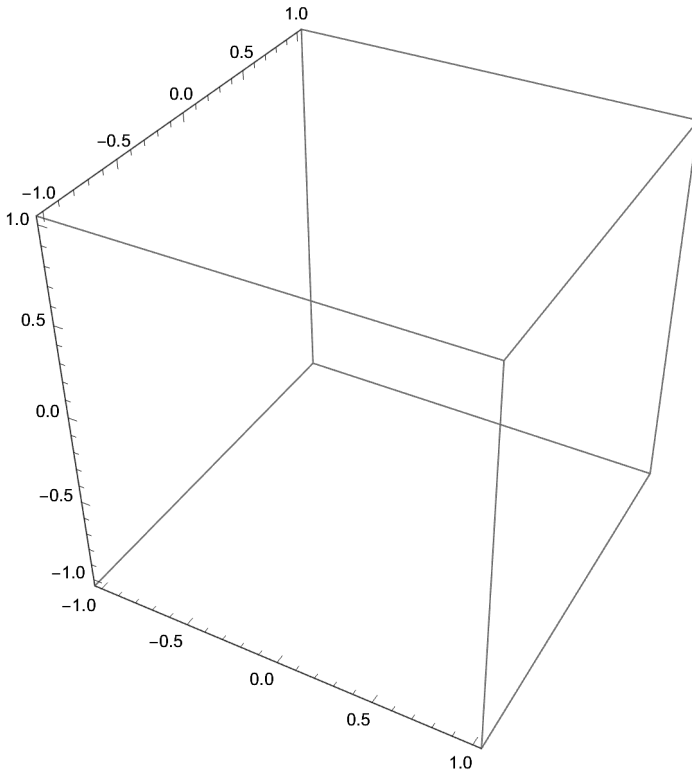
$$\begin{aligned}
& \left( \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 \right)^2 \Big)^{1/3} \Big) + \\
& (8 \pm 2^{1/3} c^4 \pi^4 \eta^4) \Big/ \left( \sqrt{3} \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \right. \\
& \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\
& \quad \sqrt{4 \left( -16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5 \right)^3 +} \\
& \quad \left. \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \right. \\
& \quad \left. \left. \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 \right)^2 \right) \Big)^{1/3} \Big) - \\
& (32 \times 2^{1/3} c^4 \pi^4 r^3 \theta) \Big/ \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\
& \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\
& \quad \sqrt{4 \left( -16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5 \right)^3 +} \\
& \quad \left. \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \right. \\
& \quad \left. \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 \right)^2 \right) \Big)^{1/3} + \\
& (32 \pm 2^{1/3} \sqrt{3} c^4 \pi^4 r^3 \theta) \Big/ \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - \right. \\
& \quad 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \\
& \quad 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\
& \quad \sqrt{4 \left( -16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5 \right)^3 +} \\
& \quad \left. \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \right. \\
& \quad \left. \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 \right)^2 \right) \Big)^{1/3} - \\
& \frac{1}{6 \times 2^{1/3} r^4 \theta^4} \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\
& \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\
& \quad \sqrt{4 \left( -16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5 \right)^3 +} \\
& \quad \left. \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \right. \\
& \quad \left. \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 \right)^2 \right) \Big)^{1/3} - \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} r^4 \theta^4} \pm \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\
& \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\
& \quad \sqrt{4 \left( -16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5 \right)^3 +} \\
& \quad \left. \left( 128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \right. \\
& \quad \left. \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 \right)^2 \right) \Big)^{1/3} \Big) \Big), \\
& \left( -\sqrt{\left( c^2 - \frac{8 c^2 \pi^2}{3 \theta^2} + \frac{8 c^2 \pi^2 \eta^2}{3 r^2 \theta^2} - (8 \times 2^{1/3} c^4 \pi^4 r^4) \Big/ \left( 3 \left( 128 c^6 \pi^6 r^{12} \theta^6 + \right. \right. \right. \right. \\
& \quad 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \\
& \quad \left. \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \right. \right. \right.
\end{aligned}$$



$$\begin{aligned} & \left( (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\ & \quad \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8)^2 \right)^{1/3} - \\ & \left( 32 i 2^{1/3} \sqrt{3} c^4 \pi^4 r^3 \theta \right) / \left( (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - \right. \\ & \quad 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \\ & \quad 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\ & \quad \sqrt{4 (-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5)^3 +} \\ & \quad \left. (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\ & \quad \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8)^2 \right)^{1/3} - \\ & \frac{1}{6 \times 2^{1/3} r^4 \theta^4} \left( (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\ & \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\ & \quad \sqrt{4 (-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5)^3 +} \\ & \quad \left. (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\ & \quad \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8)^2 \right)^{1/3} + \\ & \frac{1}{2 \times 2^{1/3} \sqrt{3} r^4 \theta^4} i \left( (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\ & \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\ & \quad \sqrt{4 (-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5)^3 +} \\ & \quad \left. (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\ & \quad \left. 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8)^2 \right)^{1/3} \Bigg), \\ & \left( \sqrt{\left( c^2 - \frac{8 c^2 \pi^2}{3 \theta^2} + \frac{8 c^2 \pi^2 \eta^2}{3 r^2 \theta^2} - (8 \times 2^{1/3} c^4 \pi^4 r^4) \right) / \left( 3 \left( (128 c^6 \pi^6 r^{12} \theta^6 + \right. \right. \right. \\ & \quad 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \\ & \quad 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\ & \quad \sqrt{4 (-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5)^3 +} \\ & \quad \left. (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\ & \quad \left. \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8)^2 \right)^{1/3} \Bigg) - \\ & (8 i 2^{1/3} c^4 \pi^4 r^4) / \left( \sqrt{3} \left( (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \right. \\ & \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\ & \quad \sqrt{4 (-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5)^3 +} \\ & \quad \left. (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\ & \quad \left. \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8)^2 \right)^{1/3} \Bigg) + \\ & (112 \times 2^{1/3} c^4 \pi^4 r^2 \eta^2) / \left( 3 \left( (128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \right. \\ & \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \end{aligned}$$



$$\begin{aligned}
& \sqrt{\left(4 \left(-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5\right)^3 + \right. \\
& \quad \left.(128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - \right. \\
& \quad \left.4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8\right)^2\right)^{1/3} + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} r^4 \theta^4} \pm \left(128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\
& \quad 128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - 1728 c^6 \pi^6 r^{10} \theta^8 + \\
& \quad \sqrt{\left(4 \left(-16 c^4 \pi^4 r^8 \theta^4 + 224 c^4 \pi^4 r^6 \eta^2 \theta^4 - 16 c^4 \pi^4 r^4 \eta^4 \theta^4 - 192 c^4 \pi^4 r^7 \theta^5\right)^3 + \right. \\
& \quad \left.(128 c^6 \pi^6 r^{12} \theta^6 + 4224 c^6 \pi^6 r^{10} \eta^2 \theta^6 - 4224 c^6 \pi^6 r^8 \eta^4 \theta^6 - \right. \\
& \quad \left.128 c^6 \pi^6 r^6 \eta^6 \theta^6 - 4608 c^6 \pi^6 r^{11} \theta^7 + 4608 c^6 \pi^6 r^9 \eta^2 \theta^7 - \right. \\
& \quad \left.1728 c^6 \pi^6 r^{10} \theta^8\right)^2\right)^{1/3}\bigg)\bigg\}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]
\end{aligned}$$



$$\begin{aligned}
& \text{Solve}\left[\left(r \left(\sqrt{1 - ((v^2) / (c^2))}\right)\right) \left(\theta / \sqrt{1 - ((v^2) / (c^2))}\right) == \right. \\
& \quad \left.2 \pi r \left(\sqrt{1 - ((v^2) / (c^2))}\right) - 2 \pi \right.
\end{aligned}$$

$$\left. \sqrt{\left(2 \pi r \left(\sqrt{1 - ((v^2) / (c^2))}\right) - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right) \sqrt{1 - ((v^2) / (c^2))}\right)^2}, v\right]$$

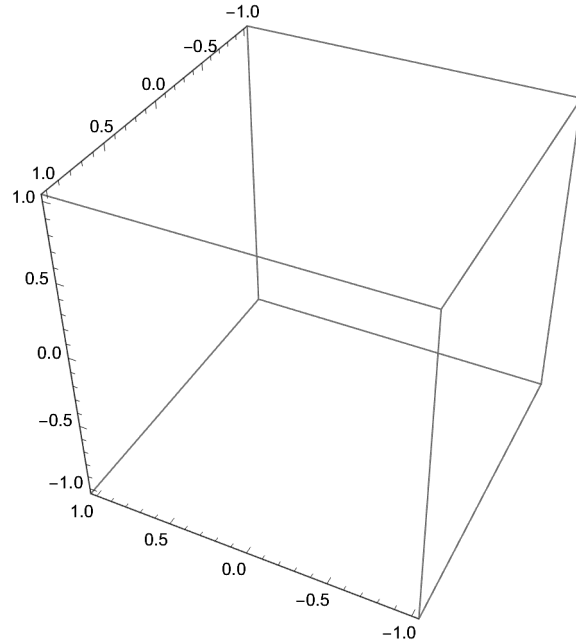
$$\left\{\left\{v \rightarrow -\sqrt{\left(-\frac{32 c^2 \pi^6}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \right.} \right.
\right.$$

$$\begin{aligned}
& \frac{16 c^2 \pi^4 r^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \frac{32 c^2 \pi^4 r \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \frac{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}{\left( 4 \pi \sqrt{\left( 64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + \right. \right.} \\
& \quad \left. \left. 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6 \right)} \right) / \\
& \quad \left. \left( 16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4 \right) \right] \Bigg\}, \\
& \left\{ v \rightarrow \sqrt{\left( - \frac{32 c^2 \pi^6}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \right. \right. \\
& \quad \frac{16 c^2 \pi^4 r^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \quad \frac{32 c^2 \pi^4 r \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \quad \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \quad \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \quad \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \quad \frac{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}{\left( 4 \pi \sqrt{\left( 64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + \right. \right.} \\
& \quad \left. \left. 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6 \right)} \right) / \\
& \quad \left. \left( 16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4 \right) \right] \Bigg\}, \\
& \left\{ v \rightarrow - \sqrt{\left( - \frac{32 c^2 \pi^6}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \right. \right. \\
& \quad \frac{16 c^2 \pi^4 r^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \quad \frac{32 c^2 \pi^4 r \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \quad \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \quad \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \quad \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \quad \frac{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}{\left( 4 \pi \sqrt{\left( 64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + \right. \right.} \\
& \quad \left. \left. 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6 \right)} \right) / \\
& \quad \left. \left( 16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4 \right) \right] \Bigg\},
\end{aligned}$$

$$\begin{aligned}
& \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \left( 4 \pi \sqrt{\left( 64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + \right. \right. \\
& \quad \left. \left. 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6 \right) \right) / \\
& \quad \left. \left( 16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4 \right) \right\}, \\
\{v \rightarrow & \sqrt{\left( - \frac{32 c^2 \pi^6}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \right. \\
& \frac{16 c^2 \pi^4 r^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \frac{32 c^2 \pi^4 r \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \\
& \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \\
& \left( 4 \pi \sqrt{\left( 64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + \right. \right. \\
& \quad \left. \left. 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6 \right) \right) / \\
& \quad \left. \left( 16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4 \right) \right\} \}
\end{aligned}$$



$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\left\{\sqrt{\left(-\frac{32 c^2 \pi^6}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{16 c^2 \pi^4 r^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \frac{32 c^2 \pi^4 r \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \frac{4 \pi \sqrt{\left(64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6\right)}}{\left(16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4\right)}\right\}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right] \\
& -\sqrt{\left(-\frac{32 c^2 \pi^6}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{16 c^2 \pi^4 r^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \frac{32 c^2 \pi^4 r \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{32 c^2 \pi^3 r^2 \theta}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{4 c^2 \pi^2 r^2 \theta^2}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} - \frac{4 c^2 \pi r^2 \theta^3}{16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4} + \frac{4 \pi \sqrt{\left(64 c^4 \pi^{10} + 128 c^4 \pi^8 r \theta + 80 c^4 \pi^6 r^2 \theta^2 - 16 c^4 \pi^5 r^2 \theta^3 + 16 c^4 \pi^4 r^3 \theta^3 + 4 c^4 \pi^4 r^2 \theta^4 - 16 c^4 \pi^3 r^3 \theta^4 + 4 c^4 \pi^2 r^3 \theta^5 - 4 c^4 \pi r^4 \theta^5 + c^4 r^4 \theta^6\right)}}{\left(16 \pi^4 r^2 + 32 \pi^3 r^2 \theta + 8 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4\right)}\right\}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]
\end{aligned}$$



Solve[

$$\left( r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right) \left( \theta \sqrt{1 - ((v^2) / (c^2))} \right) == 2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - 2 \pi \sqrt{2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - \left( \eta \sqrt{1 - ((v^2) / (c^2))} \right)^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{1}{2 \pi \sqrt{-c^2 + v^2}} \left( \sqrt{4 c^2 \pi^2 r^2 - 4 \pi^2 r^2 v^2 - 8 c^2 \pi^3 r \sqrt{\frac{c^2 - v^2}{c^2}} - 4 c^2 \pi r^2 \sqrt{\frac{c^2 - v^2}{c^2}} \theta + 4 \pi r^2 v^2 \sqrt{\frac{c^2 - v^2}{c^2}} \theta + c^2 r^2 \theta^2 - 2 r^2 v^2 \theta^2 + \frac{r^2 v^4 \theta^2}{c^2}} \right) \right\}, \right. \\ \left. \left\{ \eta \rightarrow \frac{1}{2 \pi \sqrt{-c^2 + v^2}} \left( \sqrt{4 c^2 \pi^2 r^2 - 4 \pi^2 r^2 v^2 - 8 c^2 \pi^3 r \sqrt{\frac{c^2 - v^2}{c^2}} - 4 c^2 \pi r^2 \sqrt{\frac{c^2 - v^2}{c^2}} \theta + 4 \pi r^2 v^2 \sqrt{\frac{c^2 - v^2}{c^2}} \theta + c^2 r^2 \theta^2 - 2 r^2 v^2 \theta^2 + \frac{r^2 v^4 \theta^2}{c^2}} \right) \right\} \right\}$$

$$c := (2.99792458 * 10^8)$$

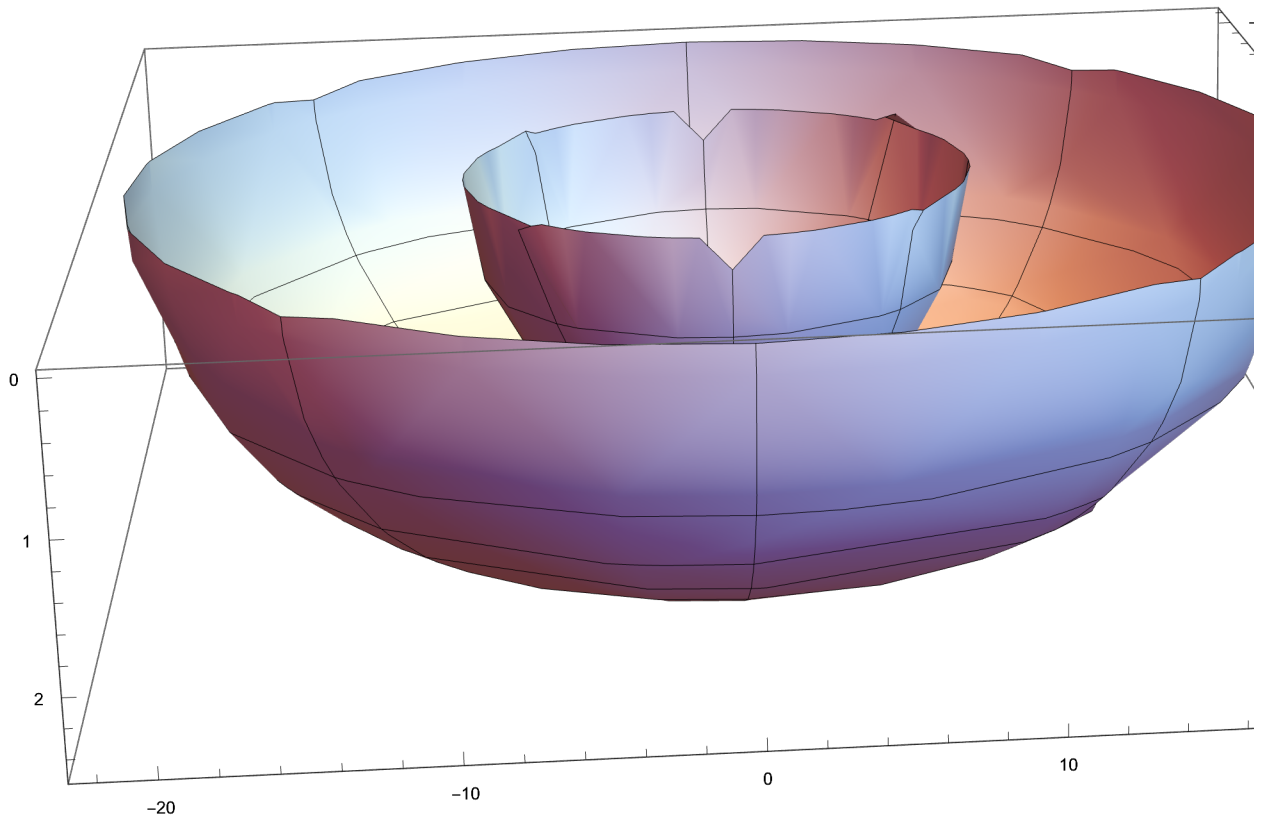
$$v := c$$

$$r := 1$$

```

RevolutionPlot3D[
  
$$\frac{1}{2 \pi \sqrt{-c^2 + v^2}} \left( \sqrt{4 c^2 \pi^2 r^2 - 4 \pi^2 r^2 v^2 - 8 c^2 \pi^3 r \sqrt{\frac{c^2 - v^2}{c^2}} - 4 c^2 \pi r^2 \sqrt{\frac{c^2 - v^2}{c^2}} \theta + 4 \pi r^2 v^2 \sqrt{\frac{c^2 - v^2}{c^2}} \theta + c^2 r^2 \theta^2 - 2 r^2 v^2 \theta^2 + \frac{r^2 v^4 \theta^2}{c^2}} \right), \{\theta, -41, 41\}, \{v, -2 \pi, 2 \pi\}]$$

```



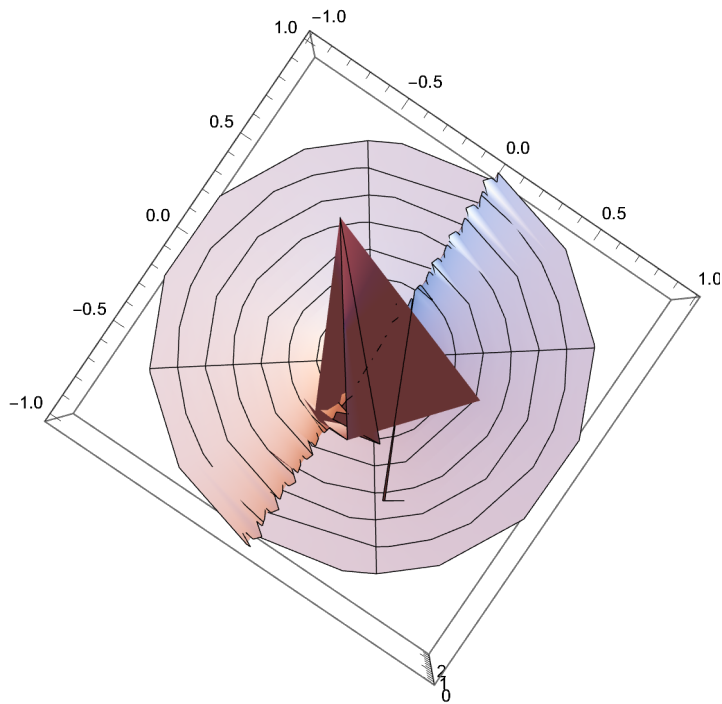
```
r := 1
```

```
v := c
```

```

RevolutionPlot3D[ $\left(\sqrt{\left(1.4006047365452214 \cdot r^{116} - 1.5583829386260045 \cdot r^2 v^2 - \right.}\right.$ 
 $\left.2.9354504648102485 \cdot r^{108} \sqrt{8.987551787368176 \cdot 16 - 1 \cdot v^2} - \right.$ 
 $1.487116578090125 \cdot r^{107} \sqrt{8.987551787368176 \cdot 16 - 1 \cdot v^2} \theta +$ 
 $1.6546403439702433 \cdot r^2 v^2 \sqrt{8.987551787368176 \cdot 16 - 1 \cdot v^2} \theta +$ 
 $3.5477732430456623 \cdot r^{114} r^2 \theta^2 - 7.894860195480569 \cdot r^2 v^2 \theta^2 +$ 
 $\left.4.3921083195184683 \cdot r^2 v^4 \theta^2\right)\right) /$ 
 $\left(\sqrt{-1.4006047365452214 \cdot r^{116} + 1.5583829386260045 \cdot r^2 v^2}\right), \{v,$ 
 $-1, 1\}, \{\theta,$ 
 $-4 \pi, 4 \pi\}]$ 

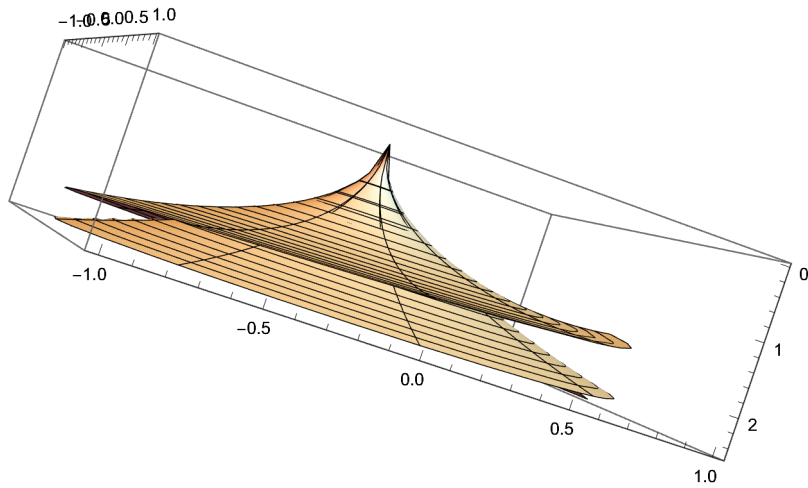
```



$r := 1$

RevolutionPlot3D[

$$\left( \sqrt{\left( 1.4006047365452214 \cdot r^{116} - 1.5583829386260045 \cdot r^2 \left( \frac{r}{2\pi\theta} \right)^2 - 2.9354504648102485 \cdot r \sqrt{8.987551787368176 \cdot 10^{-16} - 1. \cdot \left( \frac{r}{2\pi\theta} \right)^2} - 1.487116578090125 \cdot r^2 \sqrt{8.987551787368176 \cdot 10^{-16} - 1. \cdot \left( \frac{r}{2\pi\theta} \right)^2} \theta + 1.6546403439702433 \cdot r^2 \left( \frac{r}{2\pi\theta} \right)^2 \sqrt{8.987551787368176 \cdot 10^{-16} - 1. \cdot \left( \frac{r}{2\pi\theta} \right)^2} \theta + 3.5477732430456623 \cdot r^2 \theta^2 - 7.894860195480569 \cdot r^2 \left( \frac{r}{2\pi\theta} \right)^2 \theta^2 + 4.3921083195184683 \cdot r^2 \left( \frac{r}{2\pi\theta} \right)^4 \theta^2 \right) \right) / \left( \sqrt{-1.4006047365452214 \cdot r^{116} + 1.5583829386260045 \cdot r^2 \left( \frac{r}{2\pi\theta} \right)^2} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



$$v := \left( \frac{r}{2\pi\theta} \right)$$

$$\begin{aligned}
& \text{Solve}\left[ \left( r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right) \left( \theta / \sqrt{1 - ((v^2) / (c^2))} \right) == 2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - \right. \\
& \quad \left. 2 \pi \sqrt{2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) - \left( \eta \sqrt{1 - ((v^2) / (c^2))} \right)^2}, v \right] \\
& \left\{ \left\{ v \rightarrow - \sqrt{\left( - \frac{2 c^2 \pi^2 r^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 r^4}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{2 c^2 r^2 \eta^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 \eta^4}{r^4 + 2 r^2 \eta^2 + \eta^4} - \right. \right. \right. \\
& \quad \left. \frac{2 c^2 r^3 \theta}{r^4 + 2 r^2 \eta^2 + \eta^4} - \frac{c^2 r^4 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} + \frac{c^2 r^2 \eta^2 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} - \right. \\
& \quad \left. \left( \sqrt{(16 c^4 \pi^8 r^4 + 32 c^4 \pi^6 r^5 \theta + 20 c^4 \pi^4 r^6 \theta^2 - 4 c^4 \pi^4 r^4 \eta^2 \theta^2 + 4 c^4 \pi^2 r^7 \theta^3 - \right. \right. \\
& \quad \left. \left. 4 c^4 \pi^2 r^5 \eta^2 \theta^3 - c^4 r^6 \eta^2 \theta^4)} \right) / (2 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)) \right) \left. \right\}, \\
& \left\{ v \rightarrow \sqrt{\left( - \frac{2 c^2 \pi^2 r^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 r^4}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{2 c^2 r^2 \eta^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 \eta^4}{r^4 + 2 r^2 \eta^2 + \eta^4} - \right. \right. \\
& \quad \left. \frac{2 c^2 r^3 \theta}{r^4 + 2 r^2 \eta^2 + \eta^4} - \frac{c^2 r^4 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} + \frac{c^2 r^2 \eta^2 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} - \right. \\
& \quad \left. \left( \sqrt{(16 c^4 \pi^8 r^4 + 32 c^4 \pi^6 r^5 \theta + 20 c^4 \pi^4 r^6 \theta^2 - 4 c^4 \pi^4 r^4 \eta^2 \theta^2 + 4 c^4 \pi^2 r^7 \theta^3 - \right. \right. \\
& \quad \left. \left. 4 c^4 \pi^2 r^5 \eta^2 \theta^3 - c^4 r^6 \eta^2 \theta^4)} \right) / (2 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)) \right) \left. \right\}, \\
& \left\{ v \rightarrow - \sqrt{\left( - \frac{2 c^2 \pi^2 r^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 r^4}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{2 c^2 r^2 \eta^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 \eta^4}{r^4 + 2 r^2 \eta^2 + \eta^4} - \right. \right. \\
& \quad \left. \frac{2 c^2 r^3 \theta}{r^4 + 2 r^2 \eta^2 + \eta^4} - \frac{c^2 r^4 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} + \frac{c^2 r^2 \eta^2 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} + \right. \\
& \quad \left. \left( \sqrt{(16 c^4 \pi^8 r^4 + 32 c^4 \pi^6 r^5 \theta + 20 c^4 \pi^4 r^6 \theta^2 - 4 c^4 \pi^4 r^4 \eta^2 \theta^2 + 4 c^4 \pi^2 r^7 \theta^3 - \right. \right. \\
& \quad \left. \left. 4 c^4 \pi^2 r^5 \eta^2 \theta^3 - c^4 r^6 \eta^2 \theta^4)} \right) / (2 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)) \right) \left. \right\}, \\
& \left\{ v \rightarrow \sqrt{\left( - \frac{2 c^2 \pi^2 r^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 r^4}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{2 c^2 r^2 \eta^2}{r^4 + 2 r^2 \eta^2 + \eta^4} + \frac{c^2 \eta^4}{r^4 + 2 r^2 \eta^2 + \eta^4} - \right. \right. \\
& \quad \left. \frac{2 c^2 r^3 \theta}{r^4 + 2 r^2 \eta^2 + \eta^4} - \frac{c^2 r^4 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} + \frac{c^2 r^2 \eta^2 \theta^2}{4 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)} + \right. \\
& \quad \left. \left( \sqrt{(16 c^4 \pi^8 r^4 + 32 c^4 \pi^6 r^5 \theta + 20 c^4 \pi^4 r^6 \theta^2 - 4 c^4 \pi^4 r^4 \eta^2 \theta^2 + 4 c^4 \pi^2 r^7 \theta^3 - \right. \right. \\
& \quad \left. \left. 4 c^4 \pi^2 r^5 \eta^2 \theta^3 - c^4 r^6 \eta^2 \theta^4)} \right) / (2 \pi^2 (r^4 + 2 r^2 \eta^2 + \eta^4)) \right) \left. \right\} \left. \right\}
\end{aligned}$$

$$\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi}$$

$$\text{Solve}\left[\theta r = \left(2\pi r \left(\sqrt{1 - ((v^2) / (c^2))}\right)\right) - 2\pi \sqrt{\left(r \left(\sqrt{1 - ((v^2) / (c^2))}\right)\right)^2 -$$

$$\left(\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} \sqrt{1 - ((v^2) / (c^2))}\right)^2\right), v]$$

$$\left\{\{v \rightarrow 0\}, \left\{v \rightarrow -\frac{2\sqrt{2\pi}\sqrt{2c^2\pi - c^2\theta}}{\sqrt{16\pi^2 - 8\pi\theta + \theta^2}}\right\}, \left\{v \rightarrow \frac{2\sqrt{2\pi}\sqrt{2c^2\pi - c^2\theta}}{\sqrt{16\pi^2 - 8\pi\theta + \theta^2}}\right\}\right\}$$

$$\text{Solve}\left[\theta r = \left(2\pi r \left(\sqrt{1 - ((v^2) / (c^2))}\right)\right) - 2\pi$$

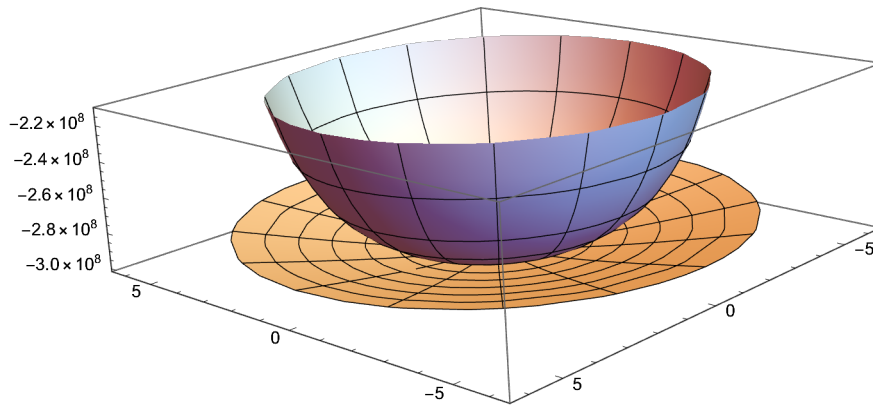
$$\sqrt{\left(r \left(\sqrt{1 - ((v^2) / (c^2))}\right)\right)^2 - \left(\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - ((v^2) / (c^2))}\right)^2}\right), v]$$

$$\left\{\{v \rightarrow 0\}, \left\{v \rightarrow -\frac{2\sqrt{2\pi}\sqrt{2c^2\pi - c^2\theta}}{\sqrt{16\pi^2 - 8\pi\theta + \theta^2}}\right\}, \left\{v \rightarrow \frac{2\sqrt{2\pi}\sqrt{2c^2\pi - c^2\theta}}{\sqrt{16\pi^2 - 8\pi\theta + \theta^2}}\right\}\right\}$$

$$\text{Solve}\left[\frac{2\sqrt{2\pi}\sqrt{2c^2\pi - c^2\theta}}{\sqrt{16\pi^2 - 8\pi\theta + \theta^2}} == c, \theta\right]$$

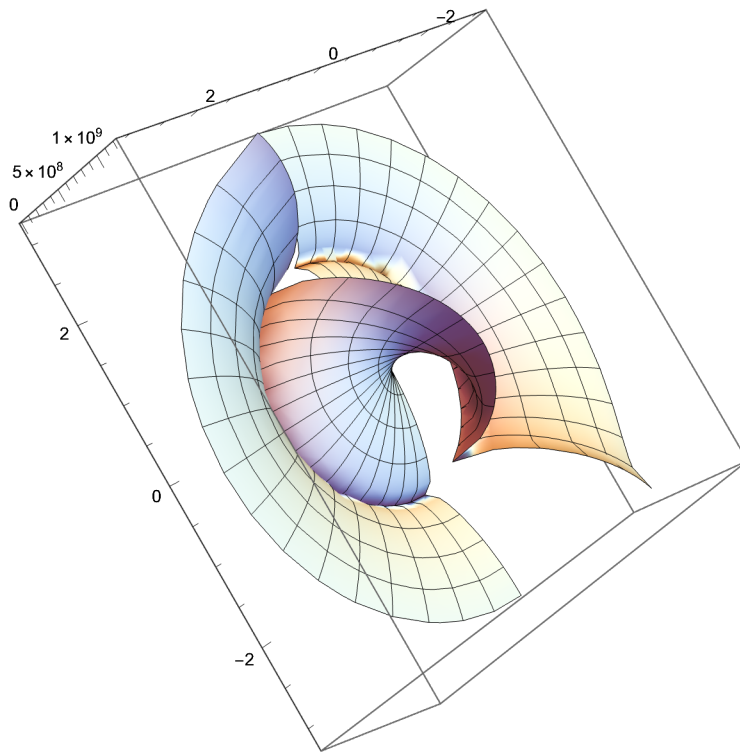
$$\{\{\theta \rightarrow 0\}\}$$

$$\text{RevolutionPlot3D}\left[-\frac{2\sqrt{2}\pi\sqrt{2c^2\pi-c^2\theta}}{\sqrt{16\pi^2-8\pi\theta+\theta^2}},\{\theta,-2\pi,2\pi\}\right]$$



$$2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)$$

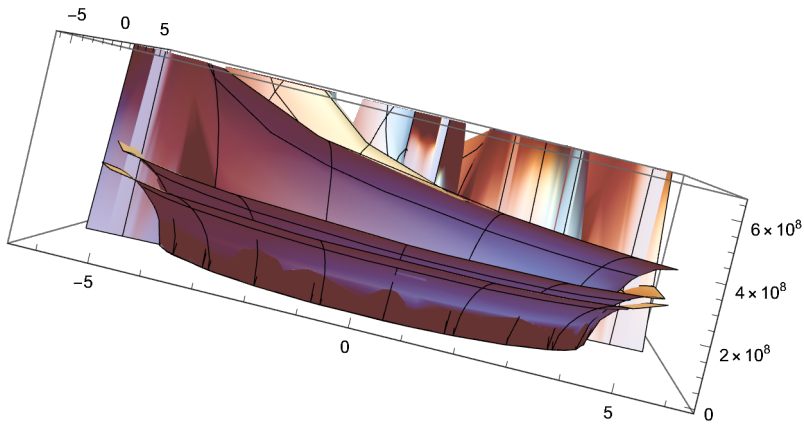
$$\text{RevolutionPlot3D}\left[\frac{2\sqrt{2}\pi\sqrt{2c^2\pi-c^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}}{\sqrt{16\pi^2-8\pi 2(\theta)+(\theta)^2}},\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$$





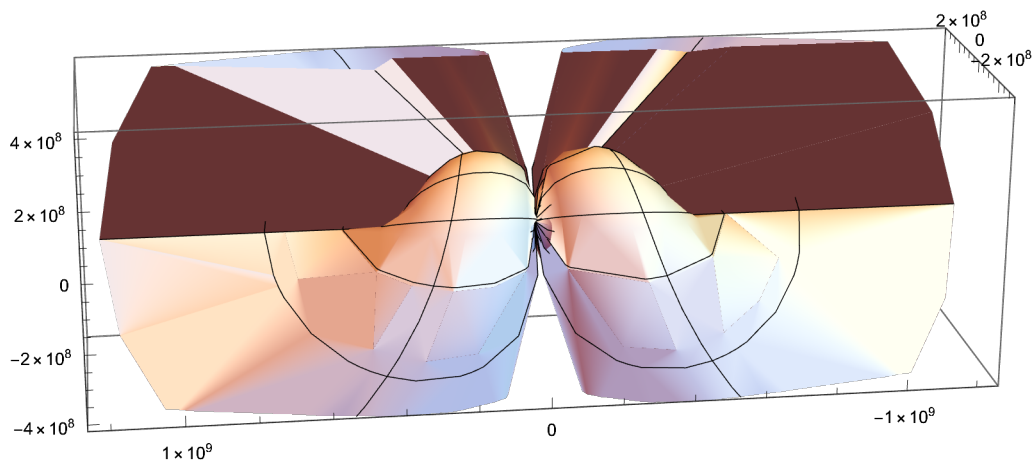
$$\text{RevolutionPlot3D}\left[\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}}{\sqrt{16 \pi^2 - 8 \pi^2 (\theta) + (\theta)^2}},\right.$$

$$\left.\{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$

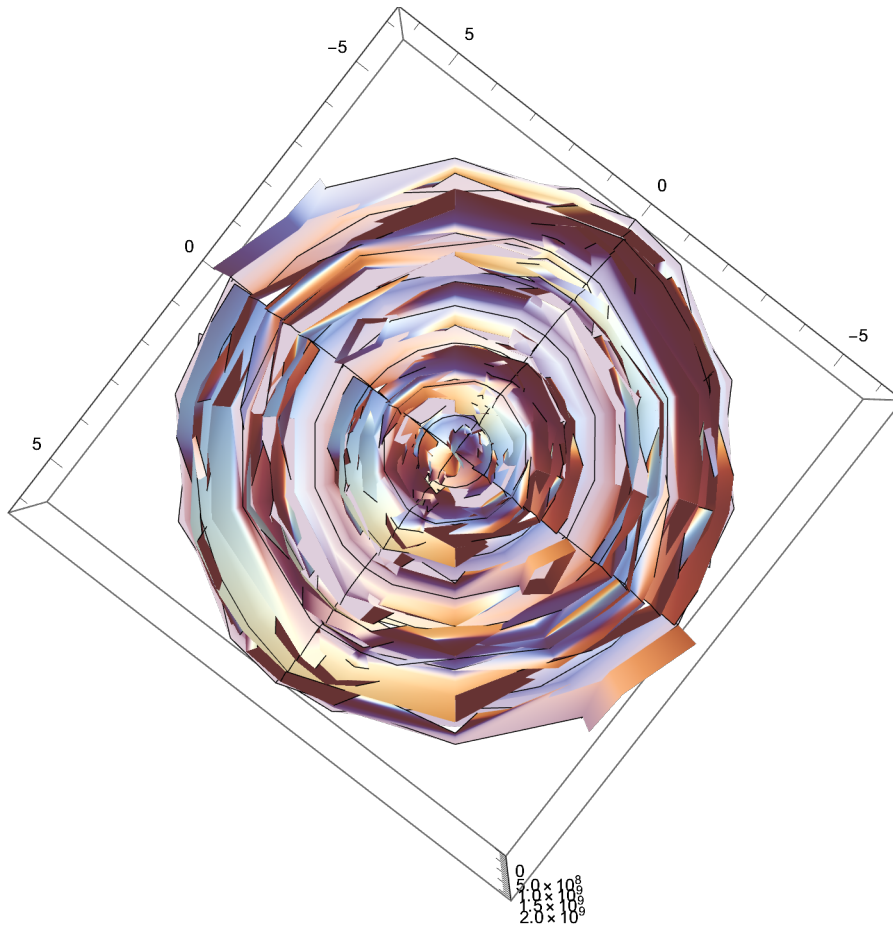


$$\text{SphericalPlot3D}\left[\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}}{\sqrt{16 \pi^2 - 8 \pi^2 (\theta) + (\theta)^2}},\right.$$

$$\left.\{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$

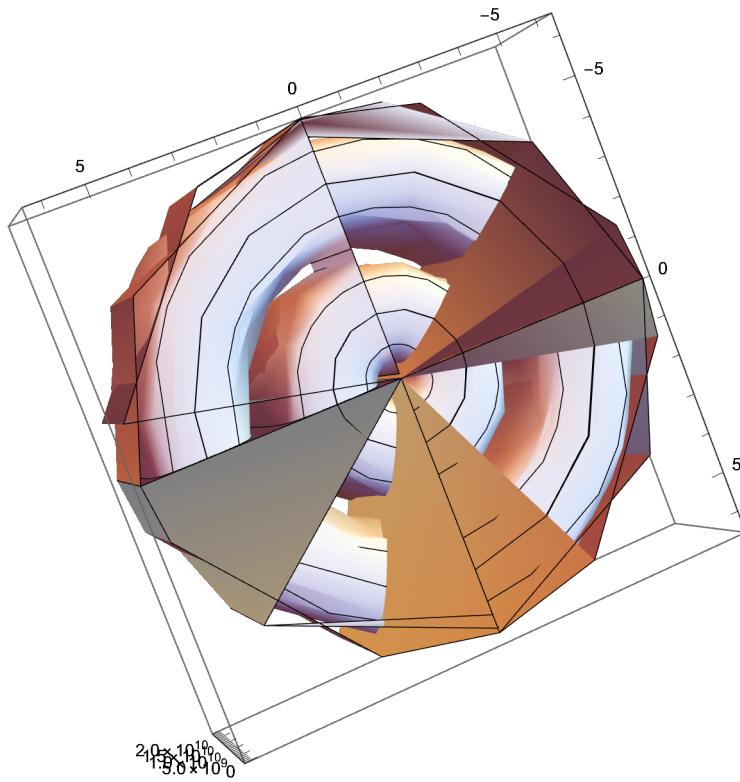


$$\text{RevolutionPlot3D}\left[\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 (\theta)}}{\sqrt{16 \pi^2 - 8 \pi^2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + (\theta)^2}},\right. \\
\left.\{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$

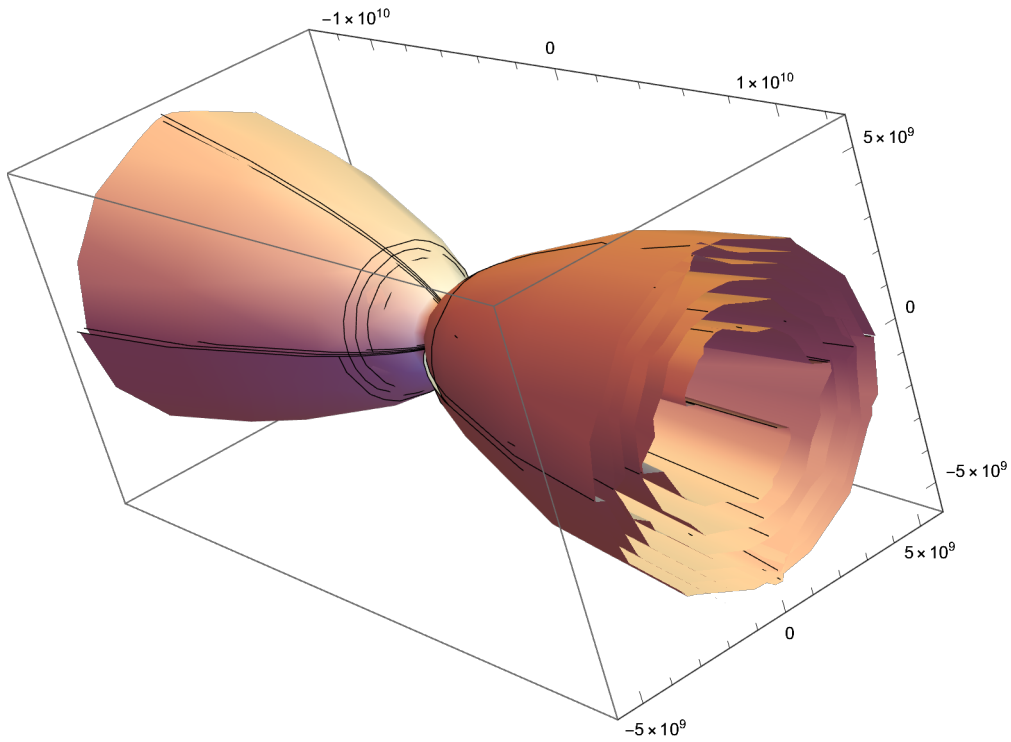


$$\text{RevolutionPlot3D}\left[\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 (\theta)}}{\sqrt{16 \pi^2 - 8 \pi 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)^2}},\right.$$

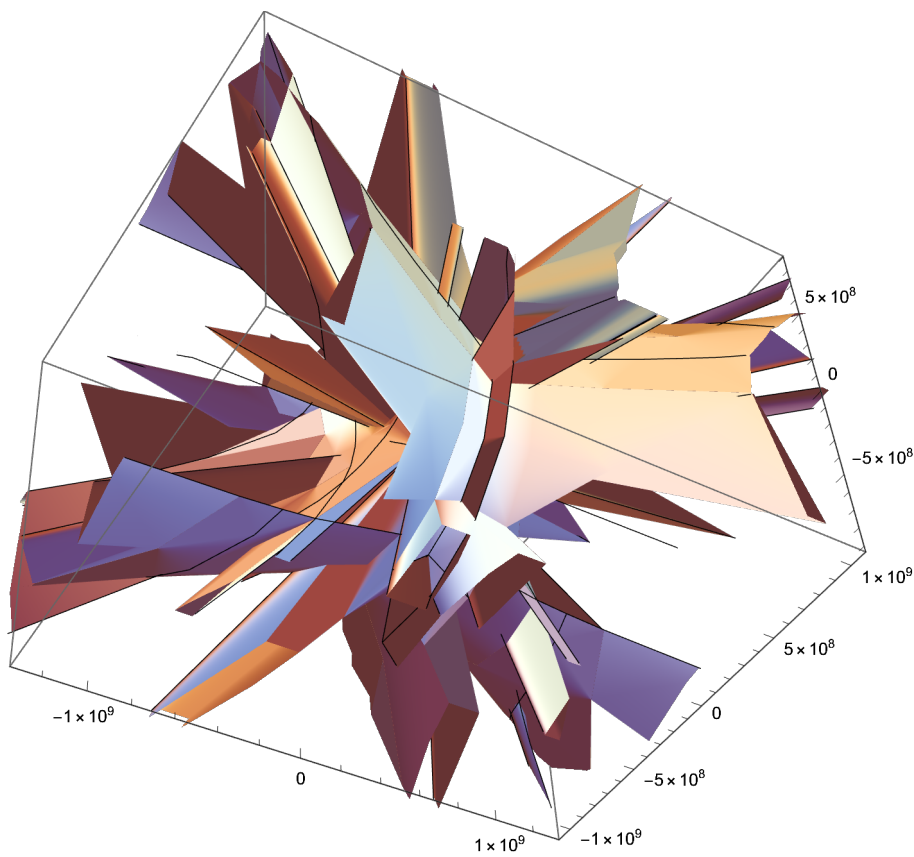
$$\{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}]$$



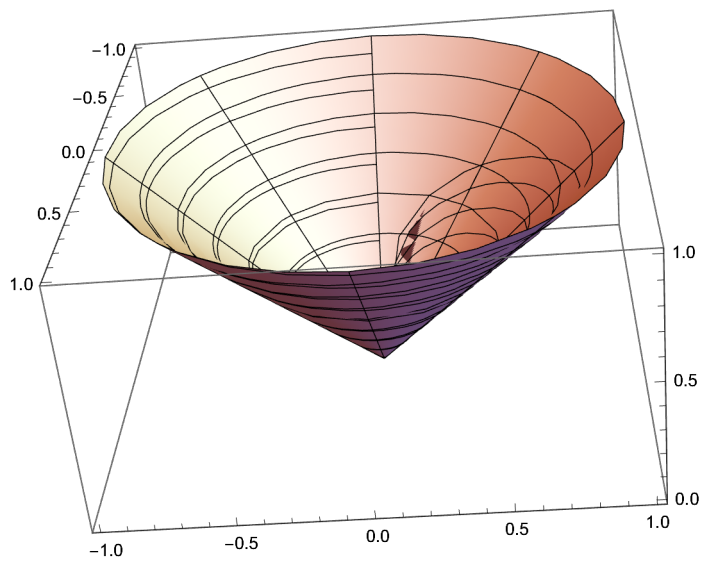
$$\text{SphericalPlot3D}\left[\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 (\theta)}}{\sqrt{16 \pi^2 - 8 \pi^2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}},\right. \\
\left.\{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



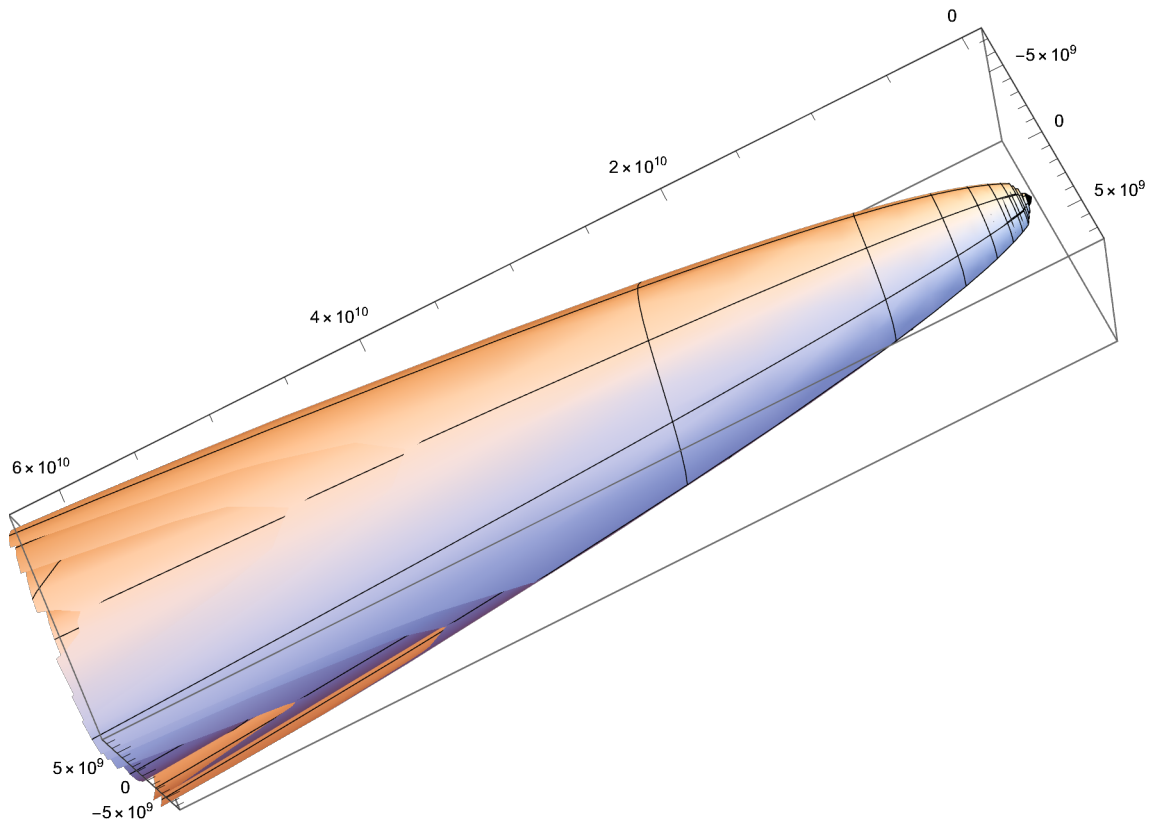
$$\text{SphericalPlot3D}\left[\frac{2 \sqrt{2 \pi} \sqrt{2 c^2 \pi - c^2 (\theta)}}{\sqrt{16 \pi^2 - 8 \pi^2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) + \theta^2}}, \{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\left\{-\frac{2 \sqrt{2 \pi} \sqrt{2 c^2 \pi - c^2 \theta}}{\sqrt{16 \pi^2 - 8 \pi \theta + \theta^2}}, \frac{2 \sqrt{2 \pi} \sqrt{2 c^2 \pi - c^2 \theta}}{\sqrt{16 \pi^2 - 8 \pi \theta + \theta^2}}\right\}, \{c, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$

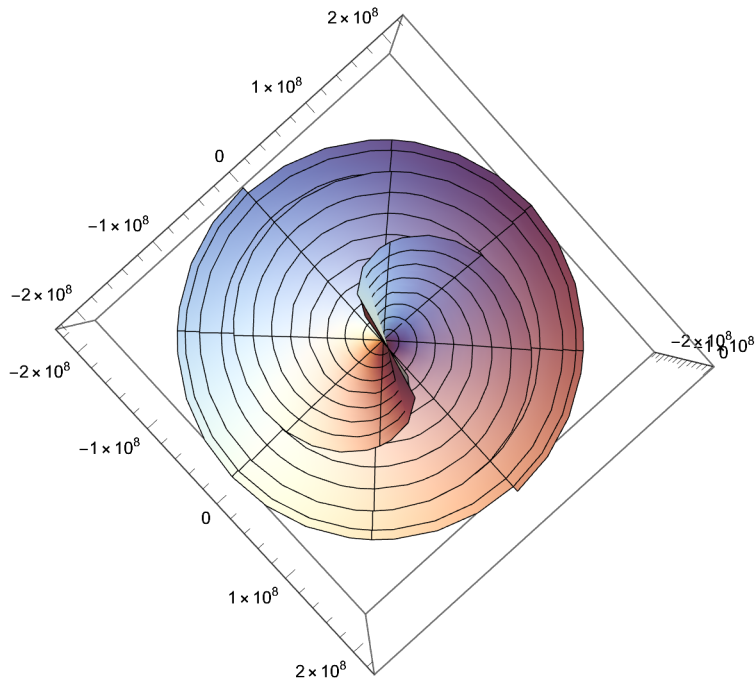


$$\text{SphericalPlot3D}\left[\left\{-\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}}{\sqrt{16 \pi^2 - 8 \pi \theta + \theta^2}}, \frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 (\theta)}}{\sqrt{16 \pi^2 - 8 \pi \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) + \left(\left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)\right)^2}}\right\}, \{\beta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



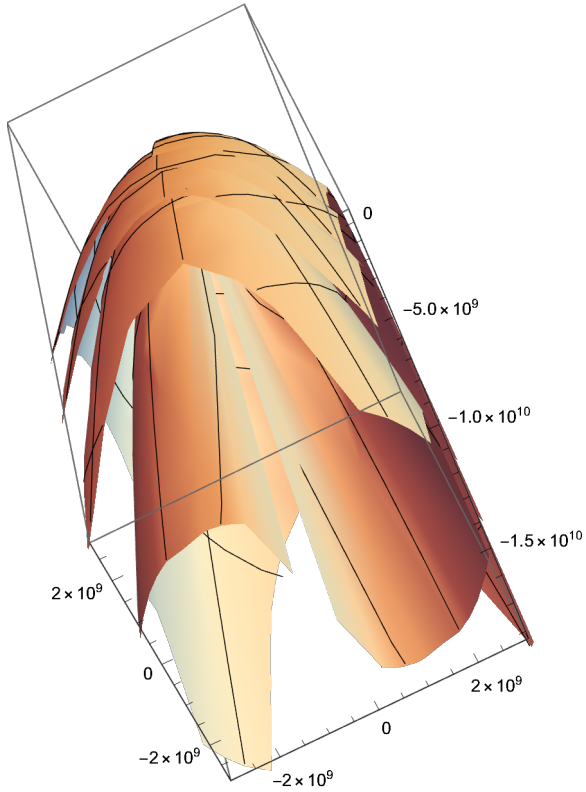
$$\text{SphericalPlot3D}\left[\left\{-\frac{2\sqrt{2}\pi\sqrt{2c^2\pi-c^2\theta}}{\sqrt{16\pi^2-8\pi\theta+\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2}},\right.\right.$$

$$\left.\frac{2\sqrt{2}\pi\sqrt{2c^2\pi-c^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)}}{\sqrt{16\pi^2-8\pi\theta+\theta^2}}\right\},\{\beta,-1,1\},\{\theta,-2\pi,2\pi\}\right]$$





$$\text{SphericalPlot3D}\left[\left\{-\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \theta}}{\sqrt{16 \pi^2 - 8 \pi \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}, \frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}}{\sqrt{16 \pi^2 - 8 \pi \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \theta^2}}\right\}, \{\beta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$

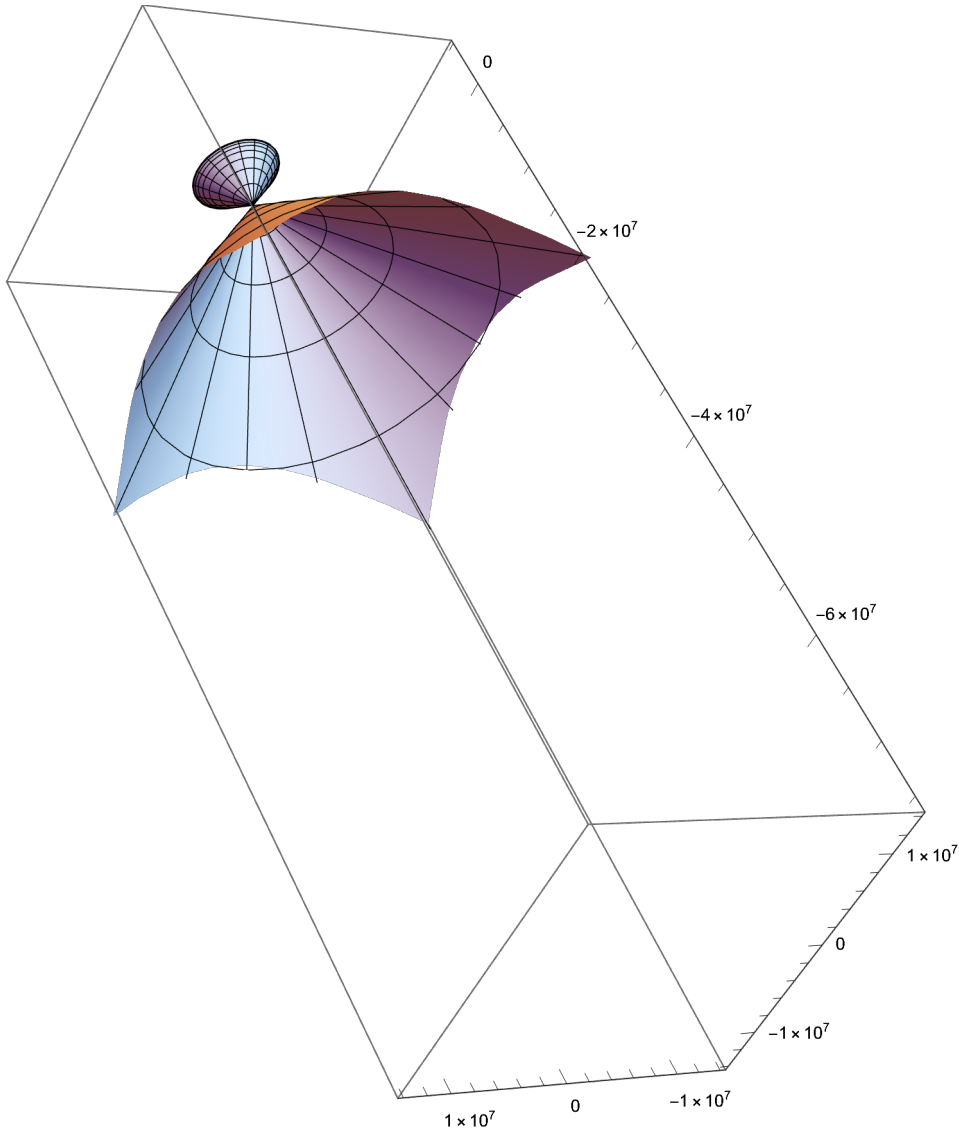


$$D\left[\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \theta}}{\sqrt{16 \pi^2 - 8 \pi \theta + \theta^2}}, \theta\right]$$

$$D\left[-\frac{2 \sqrt{2} \pi \sqrt{2 c^2 \pi - c^2 \theta}}{\sqrt{16 \pi^2 - 8 \pi \theta + \theta^2}}, \theta\right]$$

$$\frac{\sqrt{2} \pi \sqrt{5.64705 \times 10^{17} - 8.98755 \times 10^{16} \theta} (-8 \pi + 2 \theta)}{(16 \pi^2 - 8 \pi \theta + \theta^2)^{3/2}} + \frac{2.25285 \times 10^{17}}{\sqrt{5.64705 \times 10^{17} - 8.98755 \times 10^{16} \theta} \sqrt{16 \pi^2 - 8 \pi \theta + \theta^2}}$$

$\text{RevolutionPlot3D}\left[\right.$   
 $\left\{\left(\frac{\sqrt{2\pi} \sqrt{5.6470453337907354 \cdot 10^{17} - 8.987551787368176 \cdot 10^{16} \theta} (-8\pi + 2\theta)}{(16\pi^2 - 8\pi\theta + \theta^2)^{3/2}} + \right.\right.$   
 $\left.\left.\frac{2.2528451429927453 \cdot 10^{17}}{\sqrt{5.6470453337907354 \cdot 10^{17} - 8.987551787368176 \cdot 10^{16} \theta} \sqrt{16\pi^2 - 8\pi\theta + \theta^2}}\right), \right.$   
 $\left.\left(-\frac{\sqrt{2\pi} (-8\pi + 2\theta) \sqrt{2c^2\pi - c^2\theta}}{(16\pi^2 - 8\pi\theta + \theta^2)^{3/2}} - \frac{c^2 \sqrt{2\pi}}{\sqrt{2c^2\pi - c^2\theta} \sqrt{16\pi^2 - 8\pi\theta + \theta^2}}\right)\right\}, \{\theta, -2\pi, 2\pi\}]$



# 11 Dimensional

## Touching on the 11th dimension.

by Parker Emmerson © 2010

### We start by examining the wavelength with constant value

:

**Theorem 4 :** The derivative of the height of the cone with respect to time equals the average rate of the circumference of the initial circle divided by  $\theta$  when  $\theta = k t$  (the angle is a constant function of time like a clock).

velocity =

$$\begin{aligned}
 \text{wavelength of frequency} = v &= \lambda f = r f = r / \tau = r (1 / (\theta / (2 \pi))) = \frac{2 \pi r}{\theta} = \\
 \frac{(2 \pi r_1 + \theta r)}{\theta} &= \frac{2 \pi \theta r}{\theta^2} = \frac{2 \pi s}{\theta^2} = \frac{2 \pi \frac{(2 \pi r - 2 \pi r_1)}{\theta}}{\theta} = \frac{2 \pi \frac{(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2})}{\theta}}{\theta} = \\
 \frac{2 \pi (2 \pi r - 2 \pi \sqrt{r^2 - \eta^2})}{\theta^2} &= \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2} \right)}{\theta^2} = \\
 (1 / (1 / (2 \pi))) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] &= \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}
 \end{aligned} \tag{2}$$

**Theorem 5 :** The derivative of the height of the cone with respect to time equals the average rate of the circumference of the initial circle divided by  $\theta$  when  $\theta = k t$  (the angle is a constant function of time like a clock).

## We Solve for r

$$\text{Solve}\left[\frac{2\pi\left(2\pi r - 2\pi\sqrt{r^2 - (\eta)^2}\right)}{\theta^2} == \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}, r\right]$$

[illegible]

I construct the expression:  $\frac{r^2}{\frac{\theta}{2\pi}}$  (the ratio or rate of  $r^2$  to

theta) from the solutions from the previous section:

$$\begin{aligned}
 & \frac{r^2}{\frac{\theta}{2\pi}} = \\
 & \frac{1}{\frac{\theta}{2\pi}} \left( \sqrt{(- (256 \pi^7 \eta^2 \theta^3) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - \right. \\
 & \quad \left. 8 \pi \theta^9 + \theta^{10}) + (320 \pi^6 \eta^2 \theta^4) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - \right. \\
 & \quad \left. 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) - (128 \pi^5 \eta^2 \theta^5) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - \right. \\
 & \quad \left. 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + (16 \pi^4 \eta^2 \theta^6) / \right. \\
 & \quad \left. (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \right. \\
 & \quad \left. (128 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / \right. \\
 & \quad \left. (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10})) \right)^2 = \\
 & \frac{1}{\frac{\theta}{2\pi}} 2\pi \left( - (256 \pi^7 \eta^2 \theta^3) / \right. \\
 & \quad \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \right. \\
 & \quad \left( 320 \pi^6 \eta^2 \theta^4) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + \right. \\
 & \quad \left. 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) - (128 \pi^5 \eta^2 \theta^5) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - \right. \\
 & \quad \left. 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + (16 \pi^4 \eta^2 \theta^6) / \right. \\
 & \quad \left. (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \right. \\
 & \quad \left. (128 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / \right. \\
 & \quad \left. (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10})) \right) = \\
 & 2\pi \left( - \frac{1}{\theta} (256 \pi^7 \eta^2 \theta^3) / \right. \\
 & \quad \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \right. \\
 & \quad \frac{1}{\theta} (320 \pi^6 \eta^2 \theta^4) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + \\
 & \quad 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) - \frac{1}{\theta} (128 \pi^5 \eta^2 \theta^5) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - \\
 & \quad 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \frac{1}{\theta} (16 \pi^4 \eta^2 \theta^6) / \\
 & \quad \left. (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \right. \\
 & \quad \frac{1}{\theta} \left( (128 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / \right. \\
 & \quad \left. (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10})) \right) \Big) =
 \end{aligned}$$

$$2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \left( \theta \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right) \right) =$$

$$2 \pi \left( - \left( 256 \pi^7 \eta^2 \theta^2 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \left( \left( -1024 \pi^7 \theta \theta^3 + 1280 \pi^6 \theta \theta^4 - 512 \pi^5 \theta \theta^5 + 80 \pi^4 \theta \theta^6 - 32 \pi^3 \theta \theta^7 + 24 \pi^2 \theta \theta^8 - 8 \pi \theta \theta^9 + \theta \theta^{10} \right) \right) \right) =$$

$$2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \right)$$

$$\begin{aligned}
\frac{r^2}{\frac{\theta}{2\pi}} = & 2\pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \\
& \left. \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \right)
\end{aligned}$$



Solve[

$$\frac{r^2}{\frac{\theta}{2\pi}} == 2\pi \left( - \left( 256 \pi^7 \eta^2 \theta^2 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \right. \\ \left. \left( 320 \pi^6 \eta^2 \theta^3 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \right. \\ \left. \left( 128 \pi^5 \eta^2 \theta^4 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \right. \\ \left. \left( 16 \pi^4 \eta^2 \theta^5 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \right. \\ \left. \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} / \right. \right. \\ \left. \left. \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \right) \right), r]$$

$$\left\{ \left\{ r \rightarrow -\frac{1}{\sqrt{2}} \right. \right.$$

$$\left. \sqrt{\theta} \sqrt{\left( \left( 512 \pi^7 \eta^2 \theta^2 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) - \left( 640 \pi^6 \eta^2 \theta^3 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) + \left( 256 \pi^5 \eta^2 \theta^4 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) - \left( 32 \pi^4 \eta^2 \theta^5 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) - \left( 256 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} / \left( 1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \theta^{11} \right) \right) \right) \right\},$$

$$\left. \left\{ r \rightarrow \frac{1}{\sqrt{2}} \sqrt{\theta} \sqrt{\left( \frac{512 \pi^7 \eta^2 \theta^2}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} - \left( 640 \pi^6 \eta^2 \theta^3 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) + \left( 256 \pi^5 \eta^2 \theta^4 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) - \left( 32 \pi^4 \eta^2 \theta^5 \right) / \left( 1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10} \right) - \left( 256 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} / \left( 1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \theta^{11} \right) \right) \right) \right\} \right\}$$

RevolutionPlot3D[

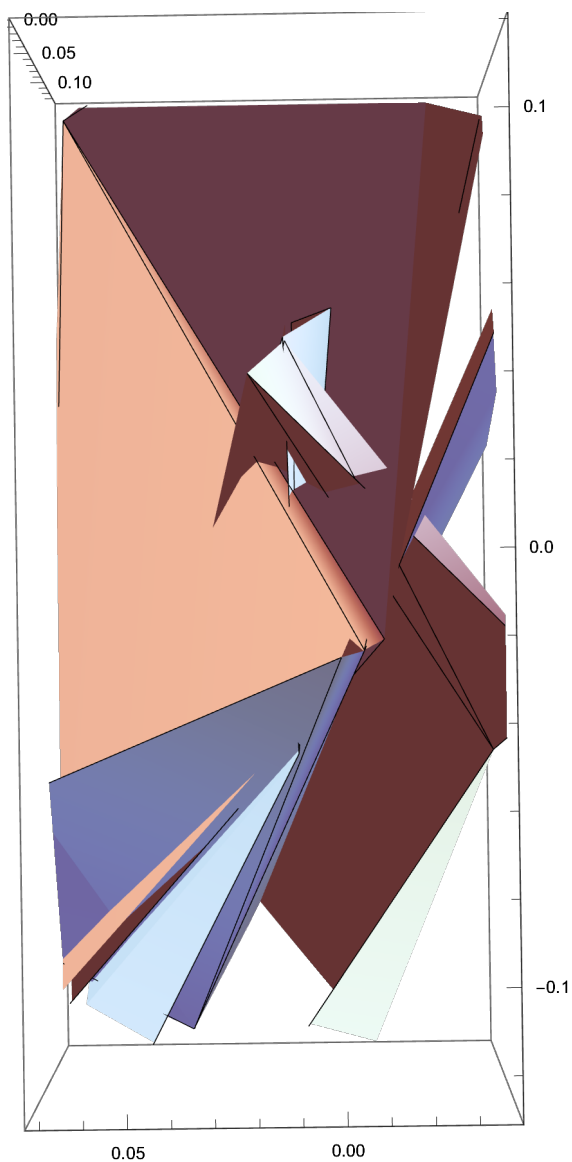
$$\left\{ -\frac{1}{\sqrt{2}} \sqrt{\theta} \sqrt{\left( (512 \pi^7 \eta^2 \theta^2) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (640 \pi^6 \eta^2 \theta^3) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + (256 \pi^5 \eta^2 \theta^4) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (32 \pi^4 \eta^2 \theta^5) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (256 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / (1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \theta^{11}) \right) }, \frac{1}{\sqrt{2}} \sqrt{\theta} \sqrt{\left( (512 \pi^7 \eta^2 \theta^2) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (640 \pi^6 \eta^2 \theta^3) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + (256 \pi^5 \eta^2 \theta^4) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (32 \pi^4 \eta^2 \theta^5) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (256 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / (1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \theta^{11}) \right) }, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\} \right]$$

ComputationalGeometry`Methods`SpatialSearch::spoutbounds : -- Message text not found --  
 ({-5.98759, -42.1091})

ComputationalGeometry`Methods`SpatialSearch::spoutbounds : -- Message text not found --  
 ({5.55128, -39.8165})

ComputationalGeometry`Methods`SpatialSearch::spoutbounds : -- Message text not found --  
 ({5.98759, -42.1091})

General::stop : Further output of ComputationalGeometry`Methods`SpatialSearch::spoutbounds will be suppressed during this calculation. >>



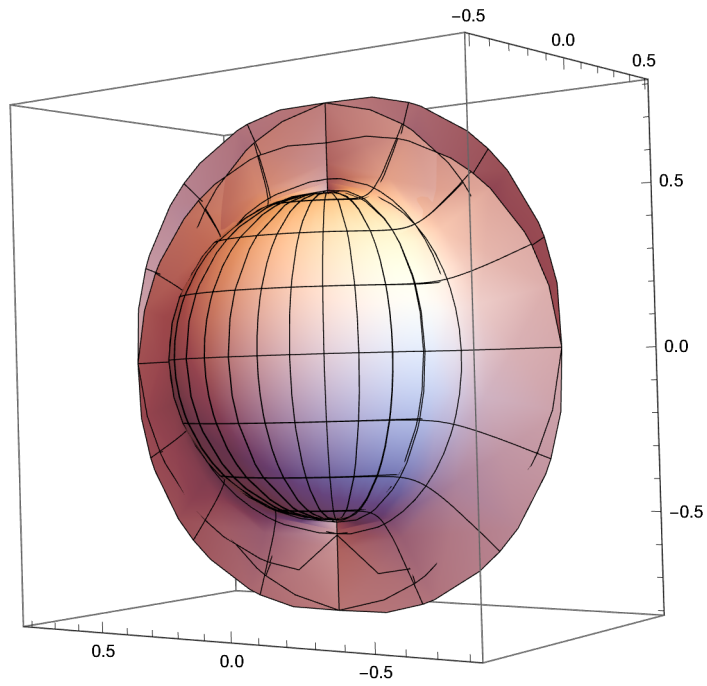
$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\theta :=$$

SphericalPlot3D[

$$\begin{aligned}
& \left\{ -\frac{1}{\sqrt{2}} \sqrt{\theta} \sqrt{\left( (512 \pi^7 \eta^2 \theta^2) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - \right. \right.} \\
& \quad \left. \left. 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (640 \pi^6 \eta^2 \theta^3) / \right. \right. \\
& \quad \left. \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + \right. \right. \\
& \quad \left. \left. (256 \pi^5 \eta^2 \theta^4) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + \right. \right. \\
& \quad \left. \left. 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (32 \pi^4 \eta^2 \theta^5) / \right. \right. \\
& \quad \left. \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - \right. \right. \\
& \quad \left. \left. (256 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / \right. \right. \\
& \quad \left. \left. (1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - \right. \right. \\
& \quad \left. \left. 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^{11} \right) \right) \right\}, \\
& \frac{1}{\sqrt{2}} \sqrt{\theta} \sqrt{\left( (512 \pi^7 \eta^2 \theta^2) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + \right.} \\
& \quad \left. 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (640 \pi^6 \eta^2 \theta^3) / \right.} \\
& \quad \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + \right.} \\
& \quad \left. (256 \pi^5 \eta^2 \theta^4) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + \right.} \\
& \quad \left. 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (32 \pi^4 \eta^2 \theta^5) / \right.} \\
& \quad \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - \right.} \\
& \quad \left. (256 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / \right.} \\
& \quad \left. (1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \right.} \\
& \quad \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^{11} \right) \right) \right\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} ]
\end{aligned}$$



Having composed the expression for  $\frac{r^2}{\frac{\theta}{2\pi}}$  in the 11th dimension, we solve for the 11th dimensional position of theta. This takes two "runs through."

First run-through.

Solve[

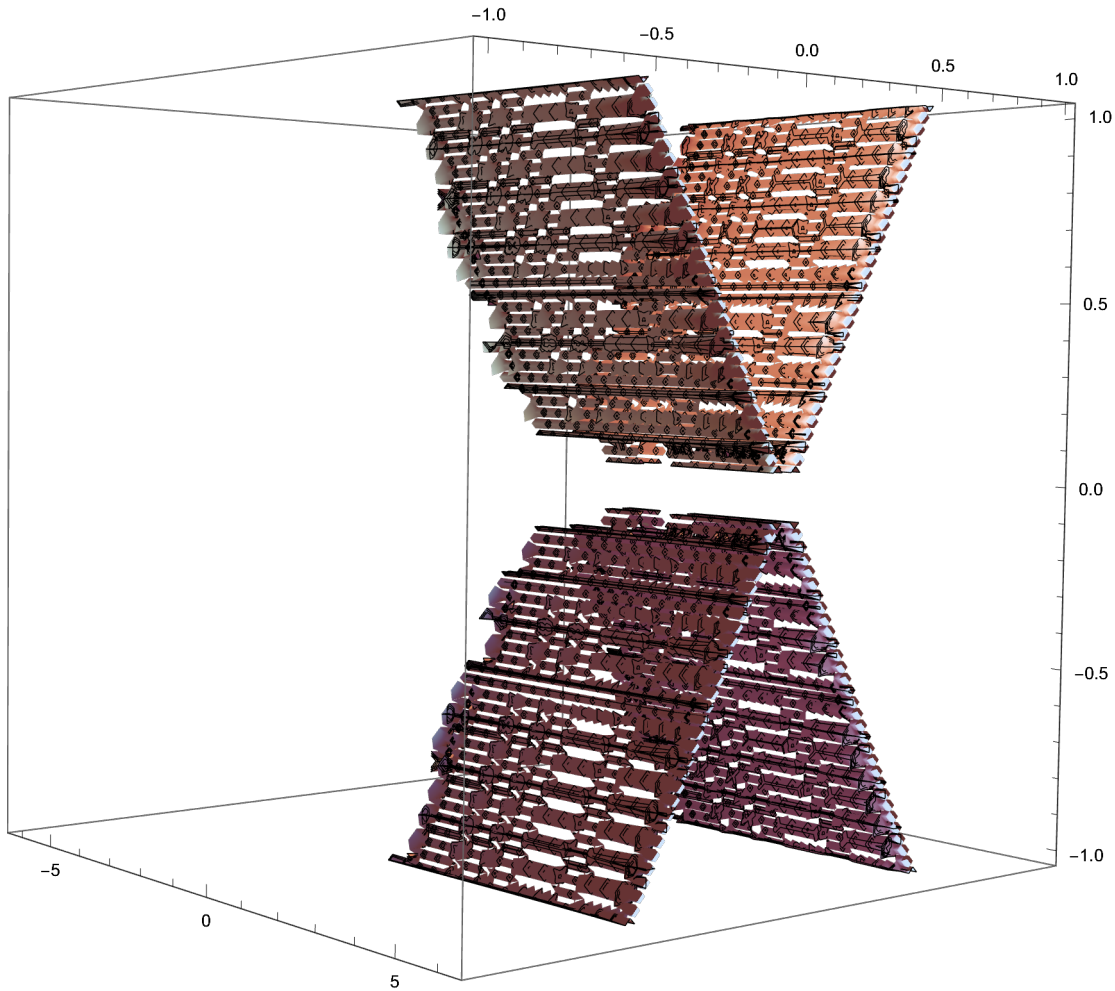
$$\frac{r^2}{\frac{\theta}{2\pi}} == 2\pi \left( - (256 \pi^7 \eta^2 \theta^2) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - \right.$$

$$\begin{aligned} & \left. 8 \pi \theta^9 + \theta^{10}) + (320 \pi^6 \eta^2 \theta^3) / \right. \\ & \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \\ & \left( 128 \pi^5 \eta^2 \theta^4 \right) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - \\ & 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + (16 \pi^4 \eta^2 \theta^5) / \\ & (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + \\ & \left( 128 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)} \right) / \\ & \left. (-1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + x) \right), x] \end{aligned}$$

$$\begin{aligned} & \left\{ \left\{ x \rightarrow \left( -262144 \pi^{12} r^2 \theta^4 + 65536 \pi^{12} \eta^2 \theta^4 + 393216 \pi^{11} r^2 \theta^5 - \right. \right. \right. \\ & 98304 \pi^{11} \eta^2 \theta^5 - 212992 \pi^{10} r^2 \theta^6 + 53248 \pi^{10} \eta^2 \theta^6 + 57344 \pi^9 r^2 \theta^7 - \\ & 13312 \pi^9 \eta^2 \theta^7 - 22528 \pi^8 r^2 \theta^8 + 3328 \pi^8 \eta^2 \theta^8 + 16384 \pi^7 r^2 \theta^9 - 2048 \pi^7 \eta^2 \theta^9 - \\ & 7232 \pi^6 r^2 \theta^{10} + 896 \pi^6 \eta^2 \theta^{10} + 1472 \pi^5 r^2 \theta^{11} - 128 \pi^5 \eta^2 \theta^{11} - 304 \pi^4 r^2 \theta^{12} + \\ & 160 \pi^3 r^2 \theta^{13} - 56 \pi^2 r^2 \theta^{14} + 8 \pi r^2 \theta^{15} - 32768 \pi^{11} \theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + \\ & 8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + 512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} - \\ & \left. \left. 512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + 128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} \right) / \right. \\ & \left. \left. (-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5) \right\} \right\} \end{aligned}$$

ContourPlot3D[

$$\begin{aligned} & \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - 98\,304\,\pi^{11}\,\eta^2\,\theta^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + \right. \\ & 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + \\ & 3328\,\pi^8\,\eta^2\,\theta^8 + 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + \\ & 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2\,\theta^{11} - 128\,\pi^5\,\eta^2\,\theta^{11} - 304\,\pi^4\,r^2\,\theta^{12} + 160\,\pi^3\,r^2\,\theta^{13} - \\ & 56\,\pi^2\,r^2\,\theta^{14} + 8\,\pi\,r^2\,\theta^{15} - 32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + \\ & 8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} - \\ & \left. 512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} \right) / \\ & (-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5), \\ & \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\} \end{aligned}$$



```

Animate[Plot3D[
  (
    -262 144  $\pi^{12} r^2 \theta^4 + 65 536 \pi^{12} \eta^2 \theta^4 + 393 216 \pi^{11} r^2 \theta^5 - 98 304 \pi^{11} \eta^2 \theta^5 - 212 992 \pi^{10} r^2 \theta^6 +$   

    53 248  $\pi^{10} \eta^2 \theta^6 + 57 344 \pi^9 r^2 \theta^7 - 13 312 \pi^9 \eta^2 \theta^7 - 22 528 \pi^8 r^2 \theta^8 +$   

    3328  $\pi^8 \eta^2 \theta^8 + 16 384 \pi^7 r^2 \theta^9 - 2048 \pi^7 \eta^2 \theta^9 - 7232 \pi^6 r^2 \theta^{10} +$   

    896  $\pi^6 \eta^2 \theta^{10} + 1472 \pi^5 r^2 \theta^{11} - 128 \pi^5 \eta^2 \theta^{11} - 304 \pi^4 r^2 \theta^{12} + 160 \pi^3 r^2 \theta^{13} -$   

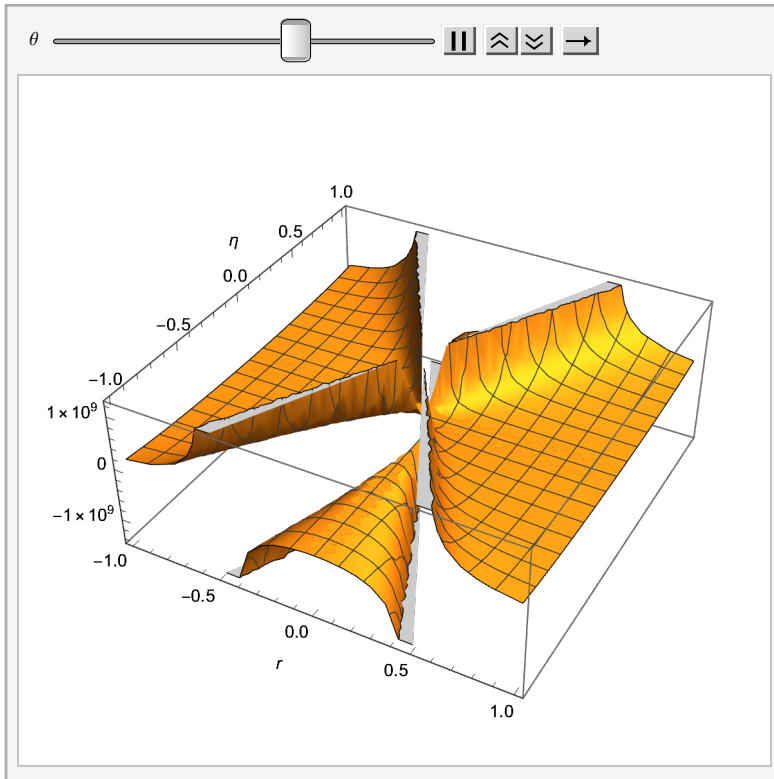
    56  $\pi^2 r^2 \theta^{14} + 8 \pi r^2 \theta^{15} - 32 768 \pi^{11} \theta \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} +$   

    8192  $\pi^{10} \theta^2 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} + 512 \pi^8 \theta^4 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} -$   

    512  $\pi^7 \theta^5 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} + 128 \pi^6 \theta^6 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} \Big) /$   

    (-256  $\pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5$ ),
  {r, -1, 1}, { $\eta$ , -1, 1}, AxesLabel -> Automatic], { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

```

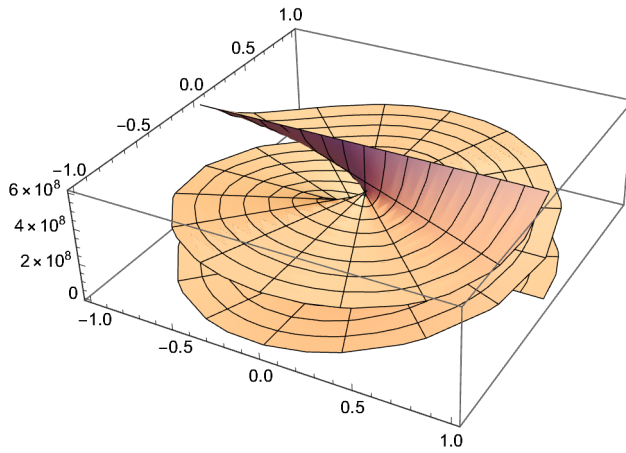


$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$



RevolutionPlot3D[

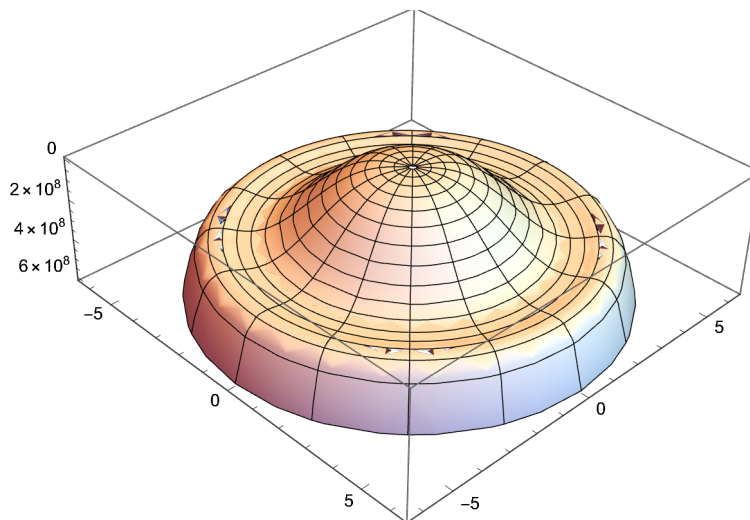
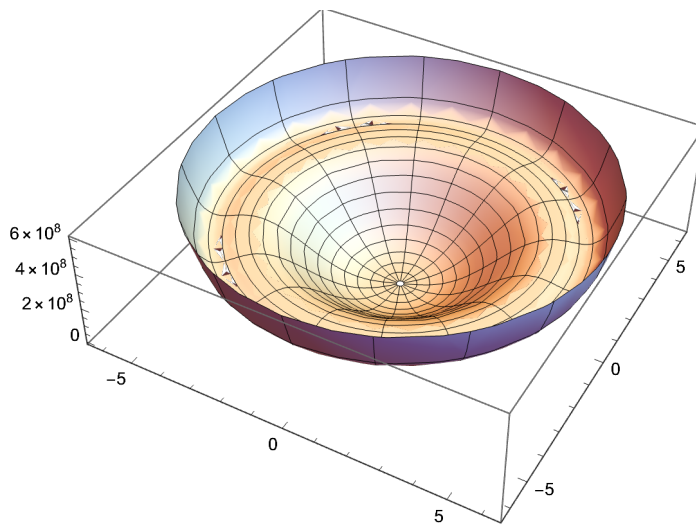
$$\begin{aligned} & \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - 98\,304\,\pi^{11}\,\eta^2\,\theta^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + \right. \\ & 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + \\ & 3328\,\pi^8\,\eta^2\,\theta^8 + 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + \\ & 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2\,\theta^{11} - 128\,\pi^5\,\eta^2\,\theta^{11} - 304\,\pi^4\,r^2\,\theta^{12} + 160\,\pi^3\,r^2\,\theta^{13} - \\ & 56\,\pi^2\,r^2\,\theta^{14} + 8\,\pi\,r^2\,\theta^{15} - 32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + \\ & 8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} - \\ & \left. 512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} \right) / \\ & \left( -256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5 \right), \\ & \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} \end{aligned}$$



$$r := \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}$$

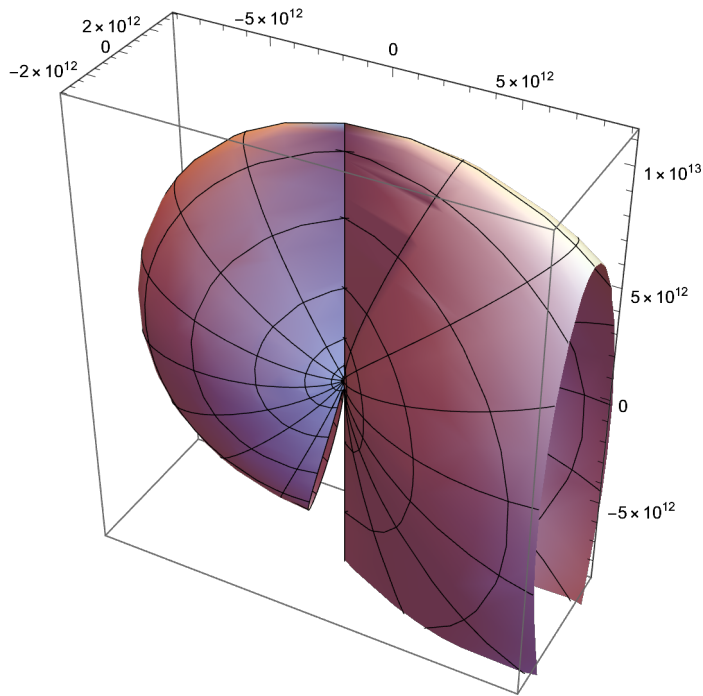
RevolutionPlot3D[

$$\begin{aligned} & \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - 98\,304\,\pi^{11}\,\eta^2\,\theta^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + \right. \\ & 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + \\ & 3328\,\pi^8\,\eta^2\,\theta^8 + 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + \\ & 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2\,\theta^{11} - 128\,\pi^5\,\eta^2\,\theta^{11} - 304\,\pi^4\,r^2\,\theta^{12} + 160\,\pi^3\,r^2\,\theta^{13} - \\ & 56\,\pi^2\,r^2\,\theta^{14} + 8\,\pi\,r^2\,\theta^{15} - 32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + \\ & 8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} - \\ & \left. 512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} \right) / \\ & (-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5), \{\theta, -2\pi, 2\pi\} \end{aligned}$$

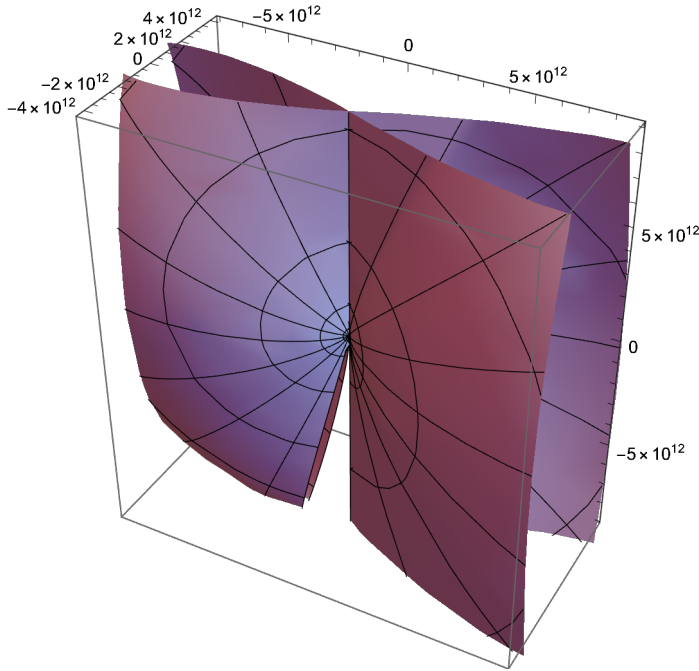


SphericalPlot3D[

$$\begin{aligned}
& \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - 98\,304\,\pi^{11}\,\eta^2\,\theta^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + \right. \\
& 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + 3328\,\pi^8\,\eta^2\,\theta^8 + \\
& 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2 \\
& \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{11} - 128\,\pi^5\,\eta^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{11} - 304\,\pi^4\,r^2\,\theta^{12} + \right. \\
& 160\,\pi^3\,r^2\,\theta^{13} - 56\,\pi^2\,r^2\,\theta^{14} + 8\,\pi\,r^2\,\theta^{15} - 32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + \\
& 8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} - \\
& 512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} \Big) / \\
& \left( -256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5 \right), \\
& \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} \Big]
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - \right. \right. \\
& \quad 98\,304\,\pi^{11}\,\eta^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + \\
& \quad 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + 3328\,\pi^8\,\eta^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^8 + \\
& \quad 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2\,(\theta)^{11} - \\
& \quad 128\,\pi^5\,\eta^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{11} - 304\,\pi^4\,r^2\,\theta^{12} + 160\,\pi^3\,r^2\,\theta^{13} - 56\,\pi^2\,r^2\,\theta^{14} + \\
& \quad 8\,\pi\,r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{15} - 32\,768\,\pi^{11}\,\theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + \\
& \quad 8192\,\pi^{10}\,\theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + 512\,\pi^8\,\theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} - \\
& \quad 512\,\pi^7\,\theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right))^3 \theta^3} + \\
& \quad \left. 128\,\pi^6\,\theta^6 \sqrt{\eta^4 (2\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right))^2 (4\pi - \theta)^3 \theta^3} \right) / \\
& \quad (-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5), \\
& \quad \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} \Big]
\end{aligned}$$



## Second run-through

Solve[

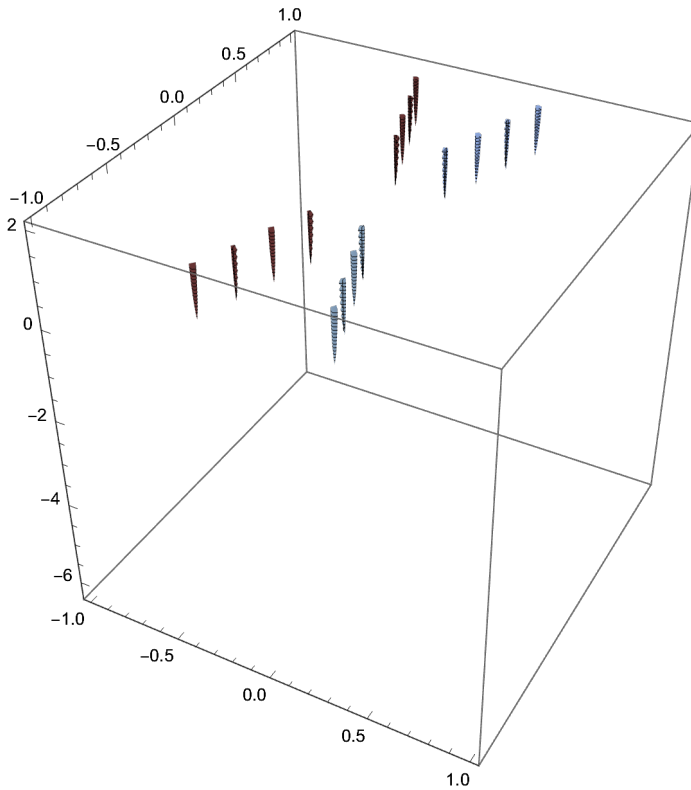
$$\begin{aligned}
 x == & \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - 98\,304\,\pi^{11}\,\eta^2\,\theta^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + \right. \\
 & 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + \\
 & 3328\,\pi^8\,\eta^2\,\theta^8 + 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + \\
 & 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2\,x - 128\,\pi^5\,\eta^2\,x - 304\,\pi^4\,r^2\,\theta^{12} + 160\,\pi^3\,r^2\,\theta^{13} - \\
 & 56\,\pi^2\,r^2\,\theta^{14} + 8\,\pi\,r^2\,\theta^{15} - 32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + \\
 & 8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} - \\
 & \left. 512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} \right) / \\
 & \left( -256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5 \right), x]
 \end{aligned}$$

$$\begin{aligned}
 \left\{ x \rightarrow \right. & -\frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \left. \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} \right\}
 \end{aligned}$$

$$\begin{aligned}
& \frac{2048 \pi^7 \eta^2 \theta^9}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{7232 \pi^6 r^2 \theta^{10}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{896 \pi^6 \eta^2 \theta^{10}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{304 \pi^4 r^2 \theta^{12}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{160 \pi^3 r^2 \theta^{13}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{56 \pi^2 r^2 \theta^{14}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8 \pi r^2 \theta^{15}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{32768 \pi^{11} \theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right) \Bigg\} \Bigg\} \\
& \text{ContourPlot3D} \left[ \left( - \frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \right. \\
& \frac{65536 \pi^{12} \eta^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \left. \frac{393216 \pi^{11} r^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} +
\end{aligned}$$

$$\begin{aligned}
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right), \\
& \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\}
\end{aligned}$$



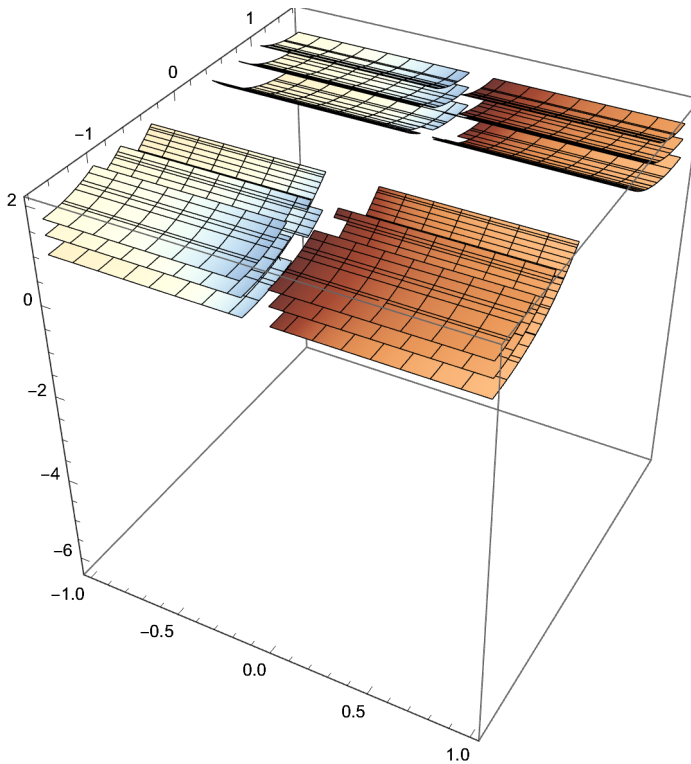
$$\eta := r \sin[\beta]$$

$$\begin{aligned}
& \text{ContourPlot3D} \left[ \left( - \frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \right. \\
& \left. \frac{65536 \pi^{12} \eta^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} +
\end{aligned}$$

$$\begin{aligned}
& \frac{8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right), \\
& \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\}
\end{aligned}$$



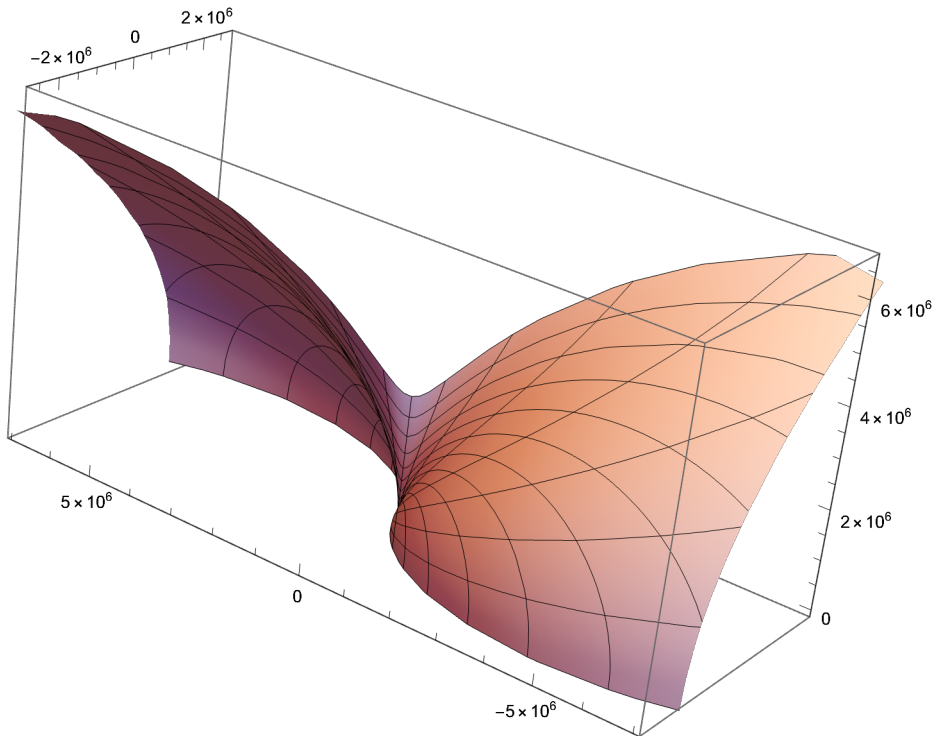
$$\eta := r \sin[\beta]$$

$$r := \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

$$\text{SphericalPlot3D} \left[ -\frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right.$$

$$\begin{array}{r}
\frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} -
\end{array}$$

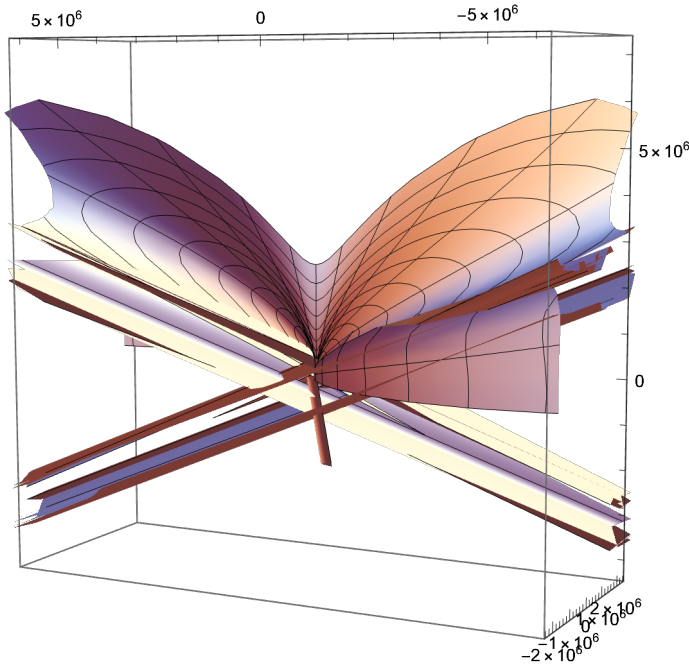
$$\begin{aligned}
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \\
& \frac{512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} - \\
& \frac{512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \\
& \frac{128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} \Bigg) / \\
& \left( 1 - \frac{1472\,\pi^5\,r^2}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \right. \\
& \left. \frac{128\,\pi^5\,\eta^2}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} \right), \\
& \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\}
\end{aligned}$$



$$\text{SphericalPlot3D} \left[ -\frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \right.$$

$$\begin{array}{r}
\frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} -
\end{array}$$

$$\begin{aligned}
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \\
& \frac{512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} - \\
& \frac{512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \\
& \frac{128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} \Bigg) / \\
& \left( 1 - \frac{1472\,\pi^5\,r^2}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5} + \right. \\
& \left. (128\,\pi^5\,\eta^2) / \left( -256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4 + \right. \right. \\
& \left. \left. r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^5\right)\right) \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\} \Bigg]
\end{aligned}$$



Composing 11th Dimensional Theta from A Geometric Pattern of Perception Theorems.

$$\theta^{11} == \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \left( 2 \sqrt{2\pi^2 - \pi^2 \sin[\beta]^2} + 2\pi^2 \sqrt{1 - \sin[\beta]^2} \right) \right)$$

$$\begin{aligned}
& \left( 2 \left( 2 \pi - \frac{\pi^2 \sin[\beta]^2}{\pi + \pi \sqrt{1 - \sin[\beta]^2}} \right) \right) \left( 2 \left( \pi + \frac{\sqrt{\pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^3} \sqrt{\sin[\beta]^2}}{\sqrt{\sin[\beta]^2}} \right) \right) \left( \left( 0.5 \right. \right. \\
& \left. \left. \left( 6.916640561054567 \cdot \pi^{33} + \frac{1.5190901312653737 \cdot \pi^{18}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} + \right. \right. \\
& \left. \left. 2.3071429505590057 \cdot \pi^{25} \sqrt{8.987551787368176 \cdot \pi^{16} + \right. \right. \\
& \left. \left. \frac{19.739208802178716}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \right) \left. \right) / \\
& \left( 5.504087674408674 \cdot \pi^{32} + \frac{1.2088535169650016 \cdot \pi^{17}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \\
& \left( -i \operatorname{ArcSinh} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( -i \operatorname{Log} \left[ -e^{-i \sqrt{e^{-2 i \beta} (1 + e^{2 i \beta})^2} \pi} \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right) \\
& \left( -i \operatorname{Log} \left[ \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] + i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right) == \\
& \left( - \frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \frac{65536 \pi^{12} \eta^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{393216 \pi^{11} r^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{98304 \pi^{11} \eta^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{212992 \pi^{10} r^2 \theta^6}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \left. \frac{53248 \pi^{10} \eta^2 \theta^6}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} \Bigg) /
\end{aligned}$$



$$\begin{aligned}
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \quad \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right) \\
& \text{SphericalPlot3D} \left[ \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right) \left( 2 \sqrt{2 \pi^2 - \pi^2 \text{Sin}[\beta]^2} + 2 \pi^2 \sqrt{1 - \text{Sin}[\beta]^2} \right) \right) \right. \\
& \quad \left( 2 \left( 2 \pi - \frac{\pi^2 \text{Sin}[\beta]^2}{\pi + \pi \sqrt{1 - \text{Sin}[\beta]^2}} \right) \right) \left( 2 \left( \pi + \frac{\sqrt{\pi^2 \text{Sin}[\beta]^2 - \pi^2 \text{Sin}[\beta]^3} \sqrt{\text{Sin}[\beta]^2}}{\sqrt{\text{Sin}[\beta]^2}} \right) \right) \left( \left( 0.5 \right. \right. \\
& \quad \left. \left. \left( 6.916640561054567 \cdot 10^{33} + \frac{1.5190901312653737 \cdot 10^{18}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)} + \right. \right. \right. \\
& \quad \left. \left. 2.3071429505590057 \cdot 10^{25} \sqrt{\left( 8.987551787368176 \cdot 10^{16} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{19.739208802178716}{\left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right) \right)} \right) \right) \right) / \\
& \quad \left( 5.504087674408674 \cdot 10^{32} + \frac{1.2088535169650016 \cdot 10^{17}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)} \right) \\
& \quad \left( -i \text{ArcSinh} \left[ e^{2 i \pi \sqrt{1 - \text{Sin}[\beta]^2}} - \text{Cos} \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right] \right] \right) \\
& \quad \left( -i \text{Log} \left[ -e^{-i \sqrt{e^{-2 i \beta} (1 + e^{2 i \beta})^2} \pi} \right] \right) \\
& \quad \left( \text{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \text{Sin}[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \text{Sin}[\beta]^2}} \right) \right] \right) \\
& \quad \left( -i \text{Log} \left[ \text{Cos} \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right] + i \text{Sin} \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right] \right] \right) \\
& \quad \left( \text{ArcCos} \left[ e^{2 i \pi \sqrt{1 - \text{Sin}[\beta]^2}} - i \text{Sin} \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right] \right] \right) \\
& \quad \left( \text{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \text{Sin}[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \text{Sin}[\beta]^2}} \right) \right] \right) - \\
& \quad \left( - \frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \quad \frac{65536 \pi^{12} \eta^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \quad \left. \frac{393216 \pi^{11} r^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} +
\end{aligned}$$

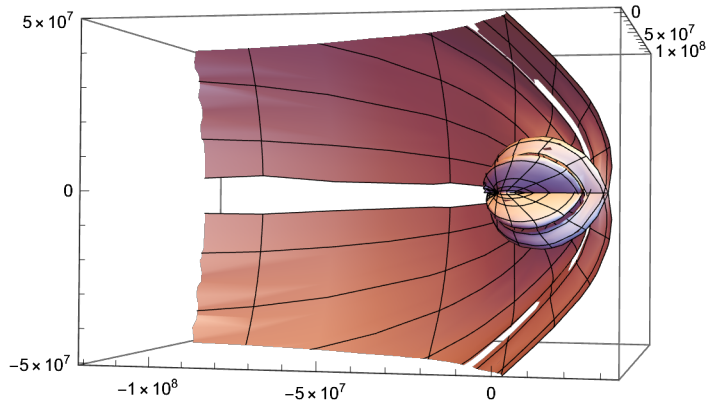
$$\begin{aligned}
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right), \\
& \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} \Big]
\end{aligned}$$

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>



## D-Brane Mechanics

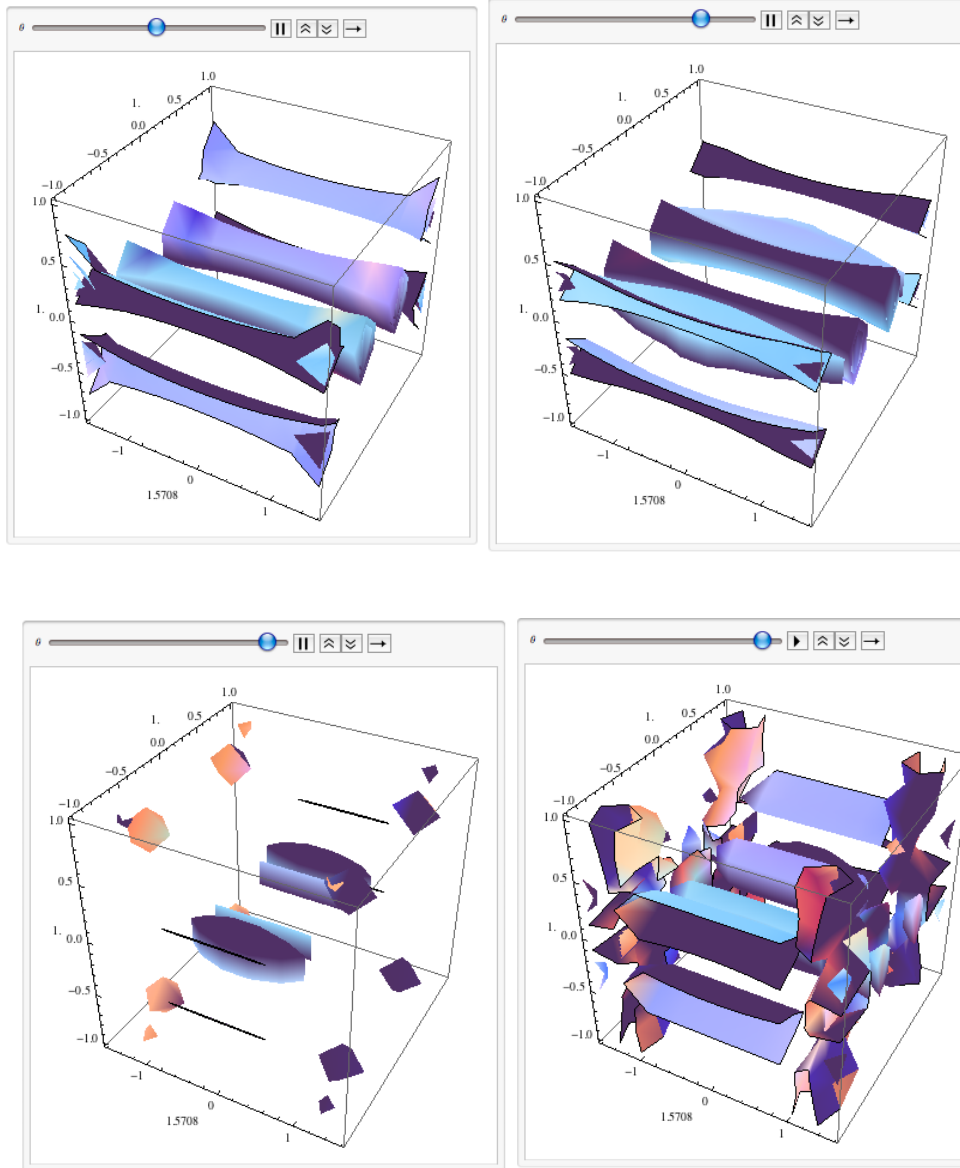
The D - Brane theta moves in the following manners :

Animate[

$$\text{ContourPlot3D} \left[ \left( - \frac{262\,144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \right.$$

$$\begin{array}{r}
\frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
\frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
\frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} -
\end{array}$$

$$\begin{aligned}
& \frac{32768 \pi^{11} \theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. (128 \pi^5 \eta^2) / \left( -256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + \right. \right. \\
& \left. \left. 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^5 \right) \right) \right), \\
& \{\beta, -\pi/2, \pi/2\}, \{\eta, -1, 1\}, \{r, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic}], \{\theta, \\
& -2\pi, 2\pi\}
\end{aligned}$$



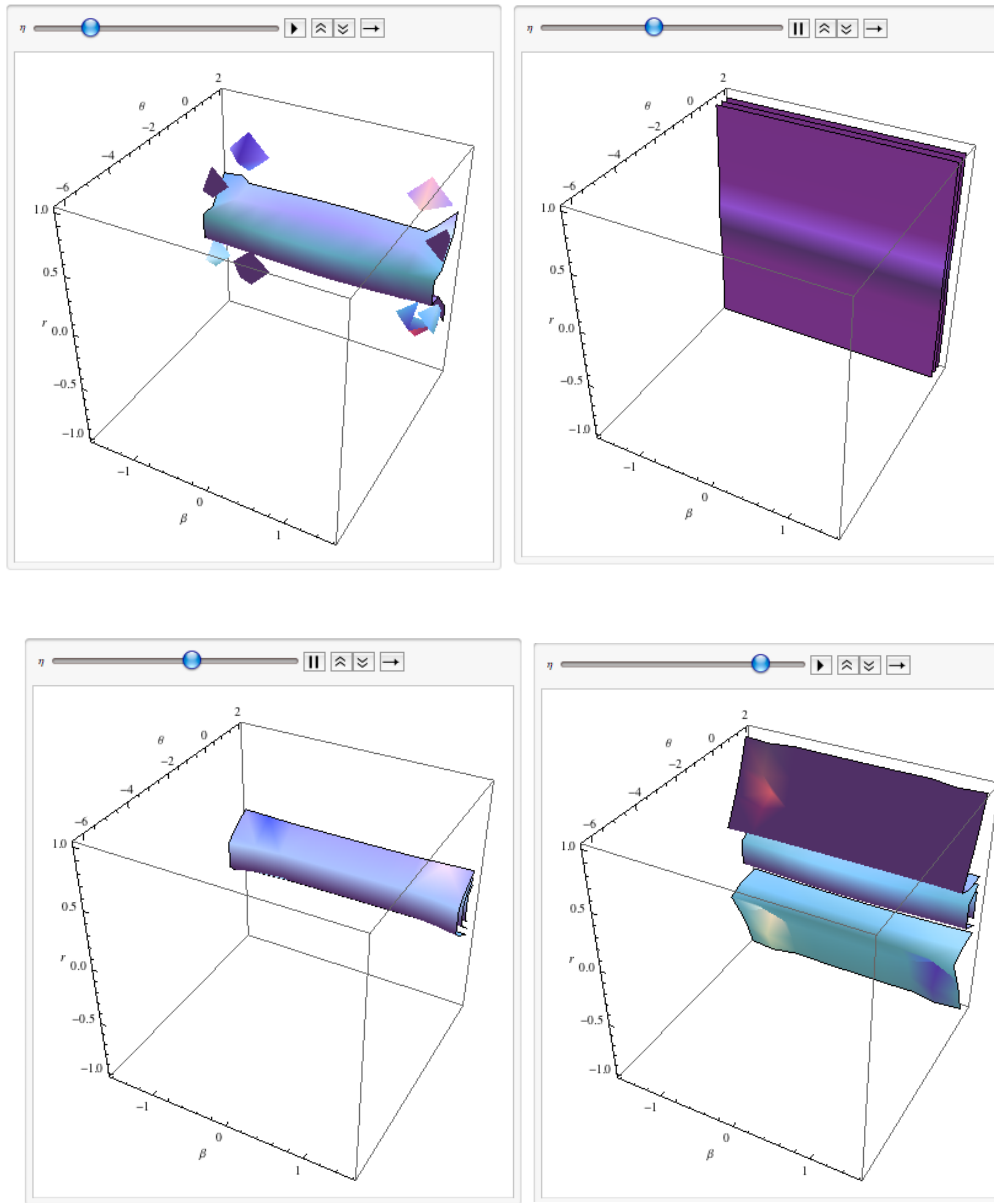
Animate[

$$\text{ContourPlot3D}\left[\left(-\frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}+\frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}+\frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}\right)\right]$$

$$\begin{aligned}
& \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} +
\end{aligned}$$

$$\begin{aligned}
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. (128 \pi^5 \eta^2) / \left( -256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + \right. \right. \\
& \left. \left. 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^5 \right) \right), \\
& \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\}, \{r, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic} \Big], \{\eta, \\
& -1, 1\} \Big]
\end{aligned}$$



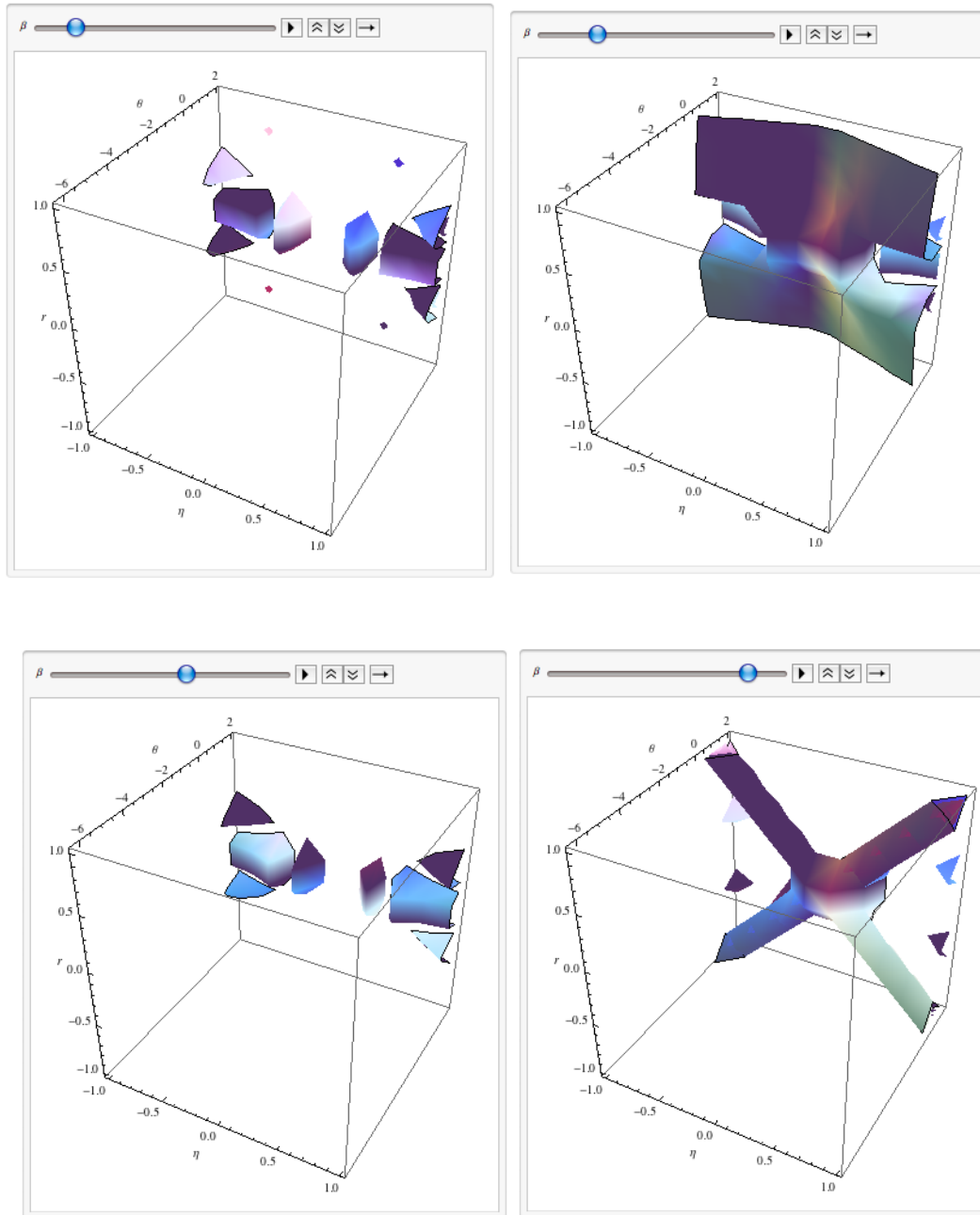


Animate[

$$\text{ContourPlot3D}\left[\left(-\frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}+\frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}+\frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}-\frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}\right]$$

$$\begin{aligned}
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} -
\end{aligned}$$

$$\begin{aligned}
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. (128 \pi^5 \eta^2) / \left( -256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + \right. \right. \\
& \left. \left. 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^5 \right) \right), \\
& \{\eta, -1, 1\}, \{\theta, -2\pi, 2\}, \{r, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic}], \{\beta, \\
& -\pi/2, \pi/2\} \Big]
\end{aligned}$$

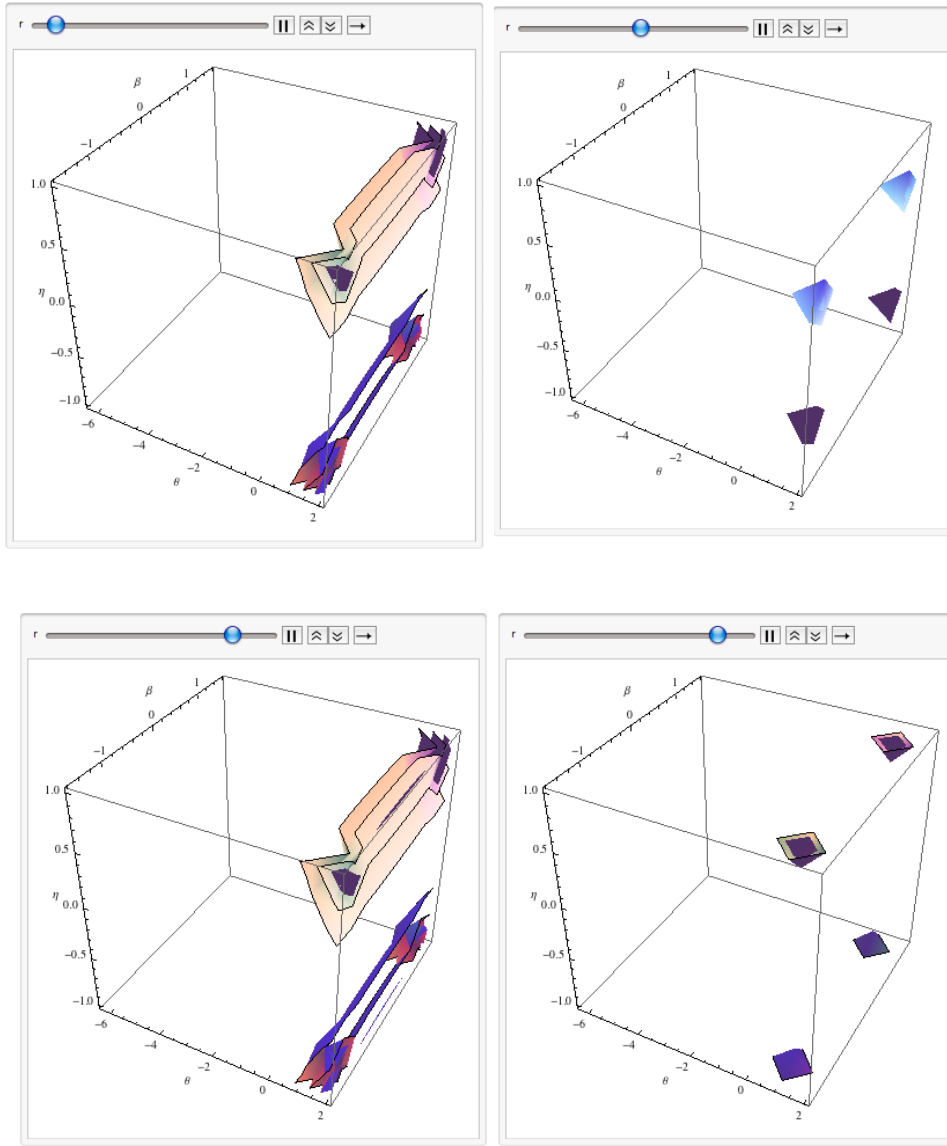


Animate[

$$\text{ContourPlot3D}\left[\left(-\frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}+\right.\right. \\ \left.\frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}+\right. \\ \left.\frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2+64\,\pi^5\,\eta^2+64\,\pi^4\,r^2\,\theta-16\,\pi^4\,\eta^2\,\theta+4\,\pi^2\,r^2\,\theta^3-4\,\pi\,r^2\,\theta^4+r^2\,\theta^5}-\right]$$

$$\begin{aligned}
& \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} +
\end{aligned}$$

$$\begin{aligned}
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. (128 \pi^5 \eta^2) / \left( -256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + \right. \right. \\
& \left. \left. 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^5 \right) \right), \\
& \{\theta, -2\pi, 2\}, \{\beta, -\pi/2, \pi/2\}, \{\eta, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic} \Big], \{r, \\
& -1, 1\} \Big]
\end{aligned}$$



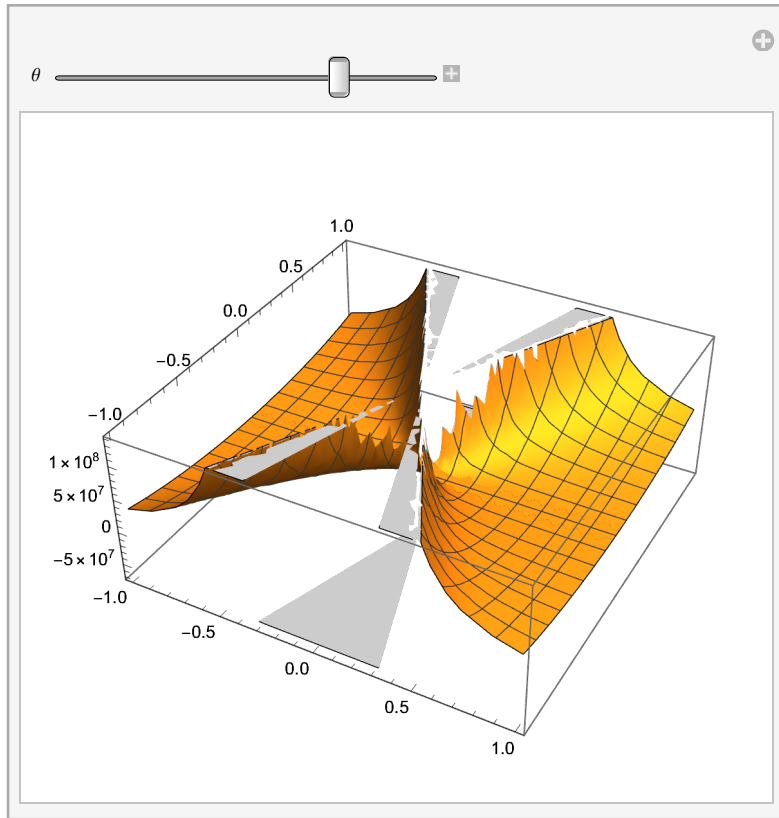
$$\begin{aligned} \theta^{11} = & \left( - \frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \right. \\ & \frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\ & \frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\ & \left. \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} \right) \end{aligned}$$

$$\begin{aligned}
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} -
\end{aligned}$$

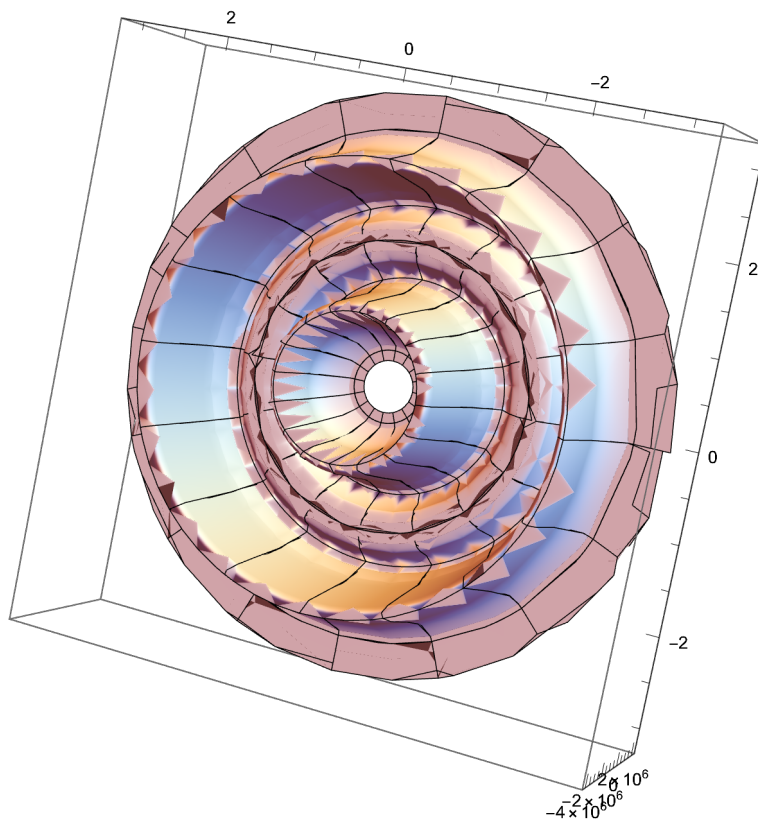
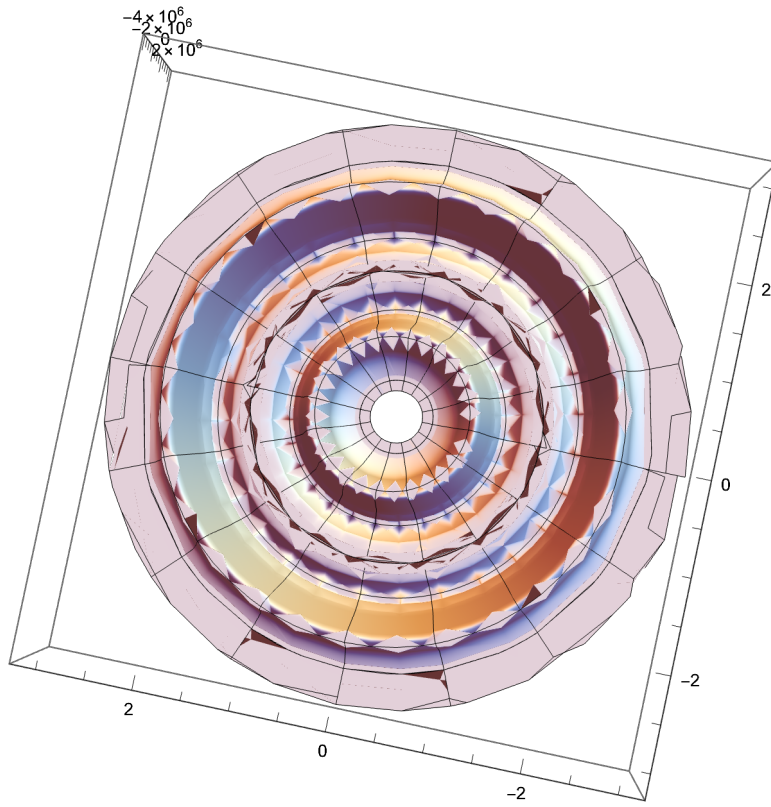


$$\begin{aligned}
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right) \\
& \text{Manipulate} \left[ \text{Plot3D} \left[ \left( - \frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \right. \right. \\
& \frac{65536 \pi^{12} \eta^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{393216 \pi^{11} r^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{98304 \pi^{11} \eta^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{212992 \pi^{10} r^2 \theta^6}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{53248 \pi^{10} \eta^2 \theta^6}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{57344 \pi^9 r^2 \theta^7}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{13312 \pi^9 \eta^2 \theta^7}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{22528 \pi^8 r^2 \theta^8}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{3328 \pi^8 \eta^2 \theta^8}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{16384 \pi^7 r^2 \theta^9}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{2048 \pi^7 \eta^2 \theta^9}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \left. \left. \frac{7232 \pi^6 r^2 \theta^{10}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \right.
\end{aligned}$$

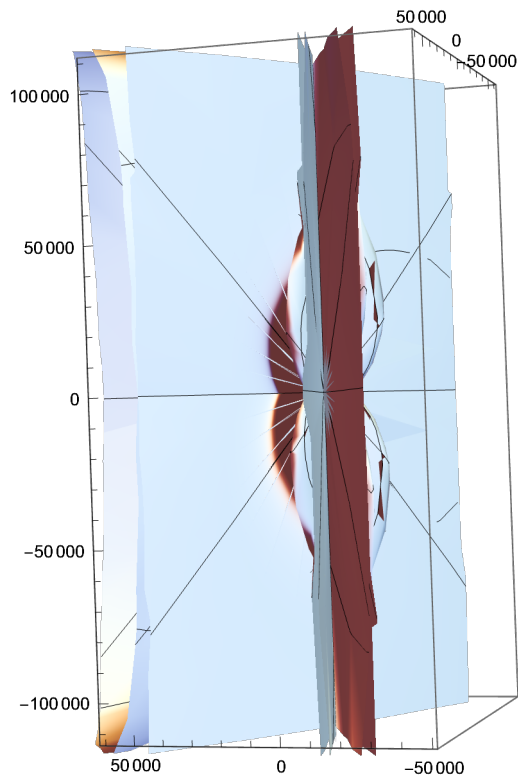
$$\begin{aligned}
& \frac{896 \pi^6 \eta^2 \theta^{10}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{304 \pi^4 r^2 \theta^{12}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{160 \pi^3 r^2 \theta^{13}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{56 \pi^2 r^2 \theta^{14}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8 \pi r^2 \theta^{15}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{32768 \pi^{11} \theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right), \\
& \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}
\end{aligned}$$



$$\begin{aligned}
\theta^{11} = & \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \left( 2 \sqrt{2 \pi^2 - \pi^2 \sin[\beta]^2 + 2 \pi^2 \sqrt{1 - \sin[\beta]^2}} \right) \right. \\
& \left( 2 \left( 2 \pi - \frac{\pi^2 \sin[\beta]^2}{\pi + \pi \sqrt{1 - \sin[\beta]^2}} \right) \right) \left( 2 \left( \pi + \frac{\sqrt{\pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^3} \sqrt{\sin[\beta]^2}}{\sqrt{\sin[\beta]^2}} \right) \right) \left( \left( 0.5 \right. \right. \\
& \left. \left( 6.916640561054567 \cdot 10^{33} + \frac{1.5190901312653737 \cdot 10^{18}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} + \right. \right. \\
& \left. \left. 2.3071429505590057 \cdot 10^{25} \sqrt{8.987551787368176 \cdot 10^{16} + \right. \right. \\
& \left. \left. \frac{19.739208802178716}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \right) \left. \right) / \\
& \left( 5.504087674408674 \cdot 10^{32} + \frac{1.2088535169650016 \cdot 10^{17}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \\
& \left( -i \operatorname{ArcSinh} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( -i \operatorname{Log} \left[ -e^{-i \sqrt{e^{-2 i \beta} (1 + e^{2 i \beta})^2} \pi} \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right) \\
& \left( -i \operatorname{Log} \left[ \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] + i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right)
\end{aligned}$$



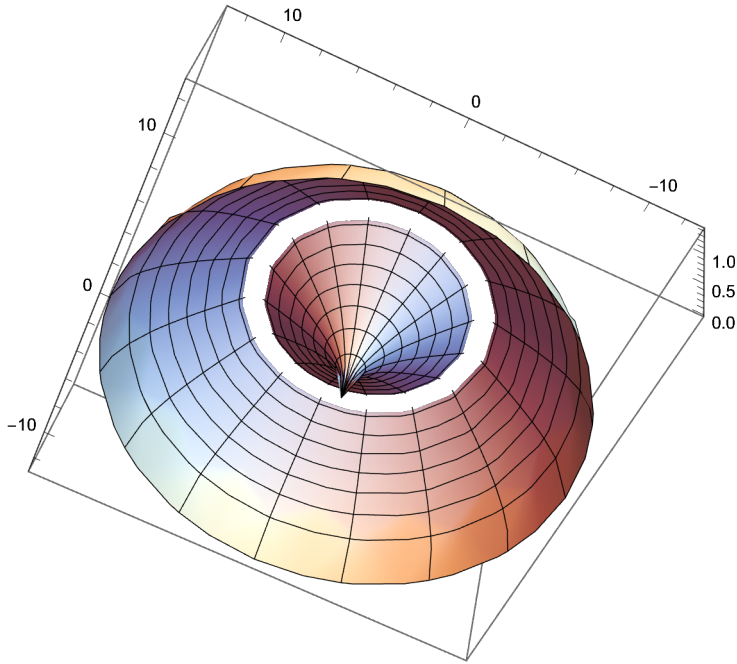
$$\begin{aligned}
& \text{SphericalPlot3D}\left[\theta(\theta)(\theta)\left(2\left(\pi+\frac{\sqrt{\pi^2\sin[\beta]^2-\pi^2\sin[\beta]^3}\sqrt{\sin[\beta]^2}}{\sqrt{\sin[\beta]^2}}\right)\right)\left(\left(0.5\right.\right.\right. \\
& \left.\left.\left(6.916640561054567\cdot^{*^33}+\frac{1.5190901312653737\cdot^{*^18}}{\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)}+\right.\right.\right. \\
& \left.\left.\left.2.3071429505590057\cdot^{*^25}\sqrt{\left(8.987551787368176\cdot^{*^16}+\right.\right.\right. \\
& \left.\left.\left.\frac{19.739208802178716\cdot^{*^18}}{\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\right)}\right)\right)\right)/ \\
& \left.\left.\left(5.504087674408674\cdot^{*^32}+\frac{1.2088535169650016\cdot^{*^17}}{\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\right)}\right)\right) \\
& \left(-\mathfrak{i}\text{ArcSinh}\left[\mathfrak{e}^{2\mathfrak{i}\pi\sqrt{1-\sin[\beta]^2}}-\text{Cos}\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]\right]\right) \\
& \left(-\mathfrak{i}\text{Log}\left[-\mathfrak{e}^{-\mathfrak{i}\sqrt{\mathfrak{e}^{-2\mathfrak{i}\beta}\left(1+\mathfrak{e}^{2\mathfrak{i}\beta}\right)^2}\pi}\right]\right) \\
& \left(\text{ArcCos}\left[\frac{1}{2}\mathfrak{e}^{-2\mathfrak{i}\pi\sqrt{1-\sin[\beta]^2}}\left(1+\mathfrak{e}^{4\mathfrak{i}\pi\sqrt{1-\sin[\beta]^2}}\right)\right]\right) \\
& \left(-\mathfrak{i}\text{Log}\left[\text{Cos}\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]+\mathfrak{i}\text{Sin}\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]\right]\right) \\
& \left(\text{ArcCos}\left[\mathfrak{e}^{2\mathfrak{i}\pi\sqrt{1-\sin[\beta]^2}}-\mathfrak{i}\text{Sin}\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]\right]\right) \\
& \left(\text{ArcCos}\left[\frac{1}{2}\mathfrak{e}^{-2\mathfrak{i}\pi\sqrt{1-\sin[\beta]^2}}\left(1+\mathfrak{e}^{4\mathfrak{i}\pi\sqrt{1-\sin[\beta]^2}}\right)\right]\right), \\
& \{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}
\end{aligned}$$



## Fire Diamond

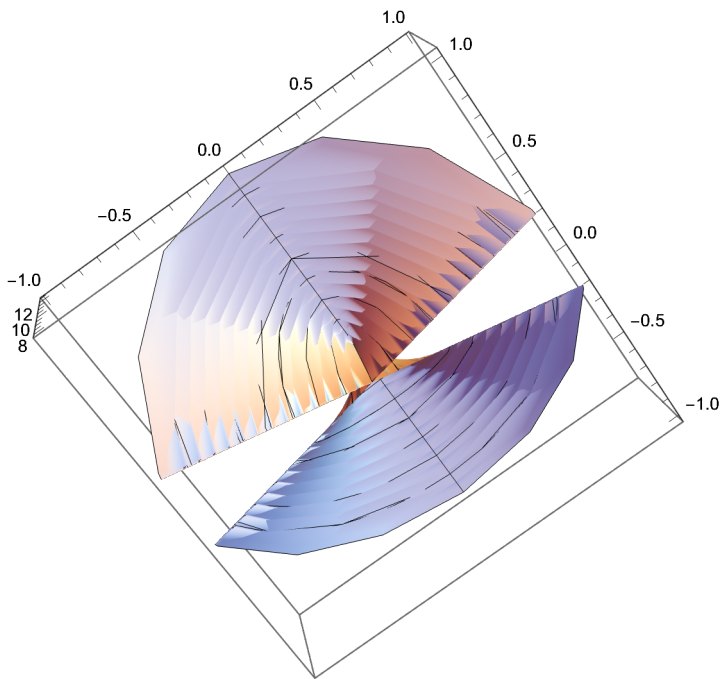
$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta) \theta}}{2\pi} \right] \right\} \right\}$$

`RevolutionPlot3D[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ], { $\theta$ ,  $-4\pi$ ,  $4\pi$ }]`



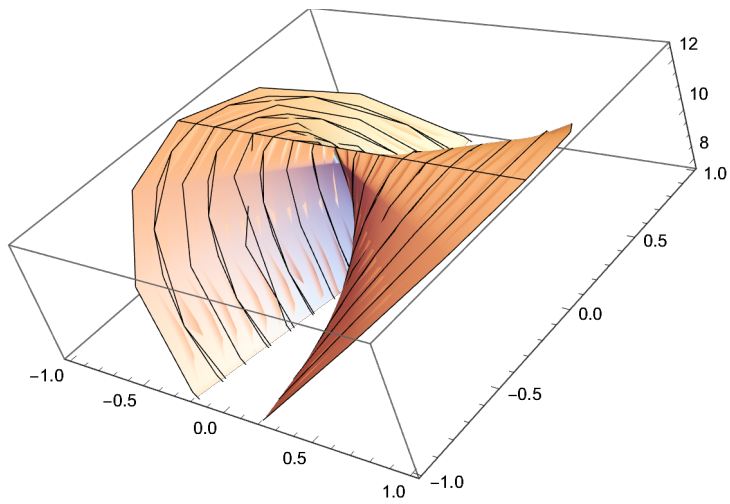
$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\} \right\} \quad (3)$$

`RevolutionPlot3D[ $2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$ , { $r$ ,  $-1$ ,  $1$ }, { $\beta$ ,  $-4\pi$ ,  $4\pi$ }]`

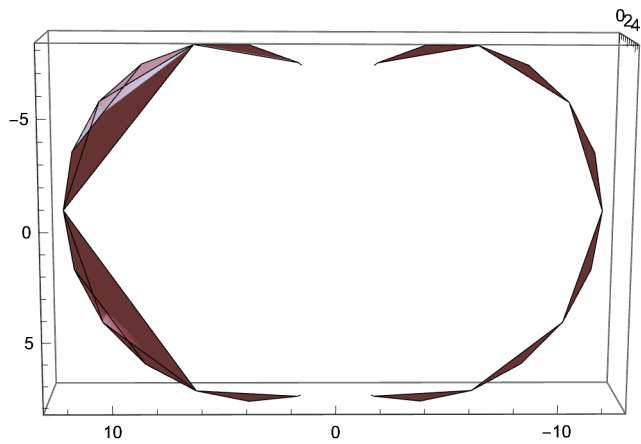




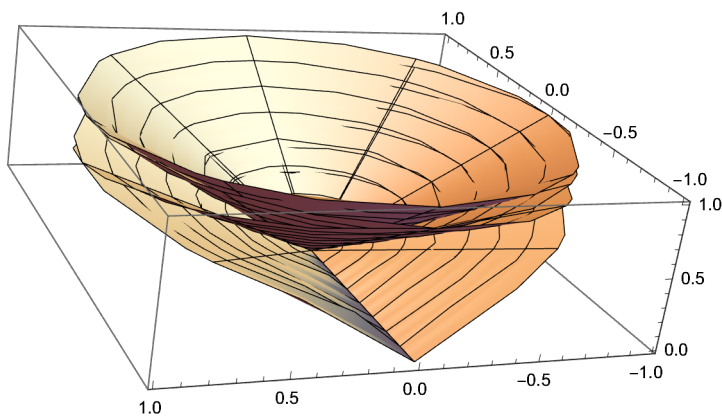
`RevolutionPlot3D` $\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right), \{r, -1, 1\}, \{\beta, -4 \pi, 4 \pi\}\right]$



`RevolutionPlot3D` $\left[\left\{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right), 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \{r, -1, 1\}, \{\beta, -4 \pi, 4 \pi\}\right]$

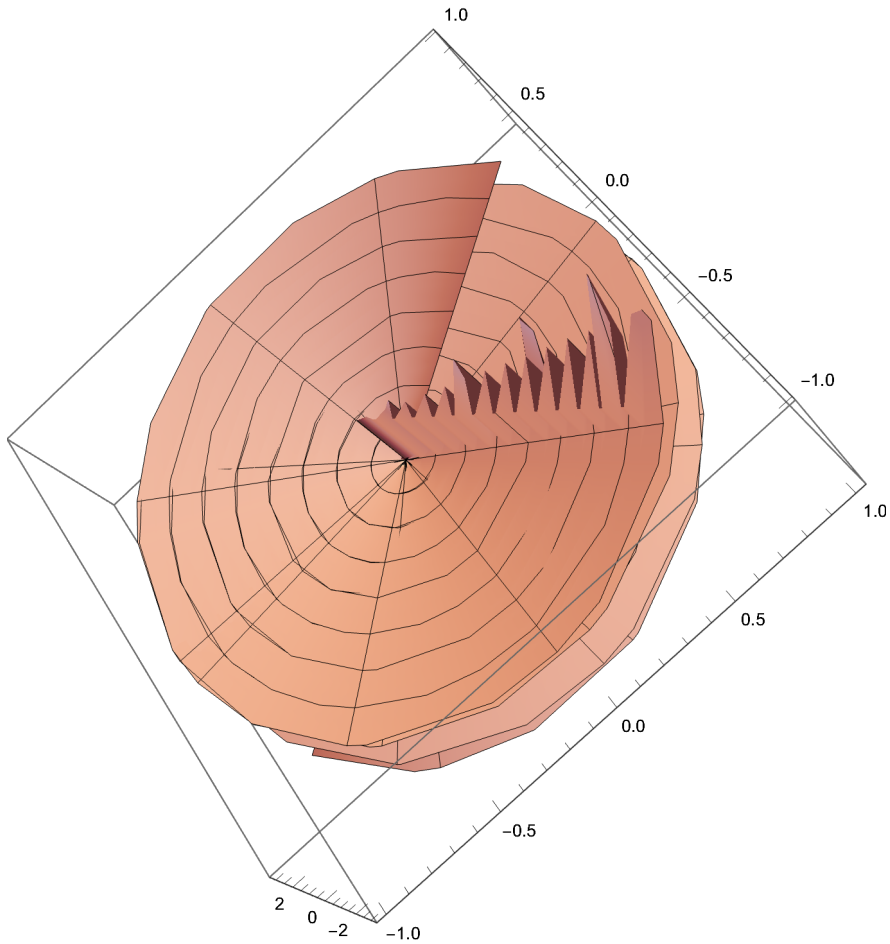


$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$



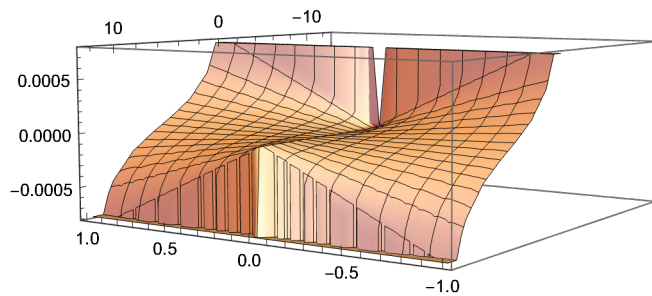
$$r = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{RevolutionPlot3D}\left[\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \{\eta, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\text{Velocity when } r \text{ is constant} = \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Plot3D}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



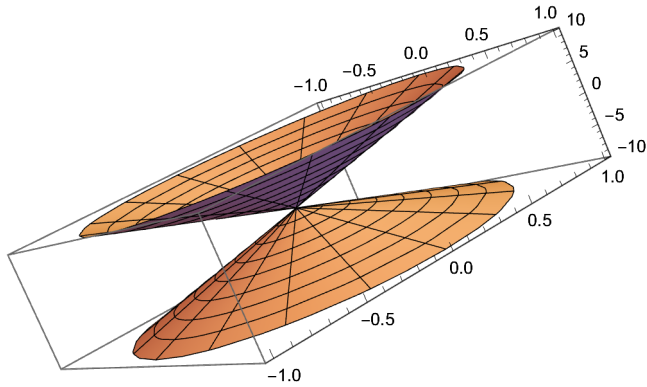
$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == r (1 / ((1080 / \pi) \theta)), \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2}{3} \left(2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi\right)\right\},\right.$$

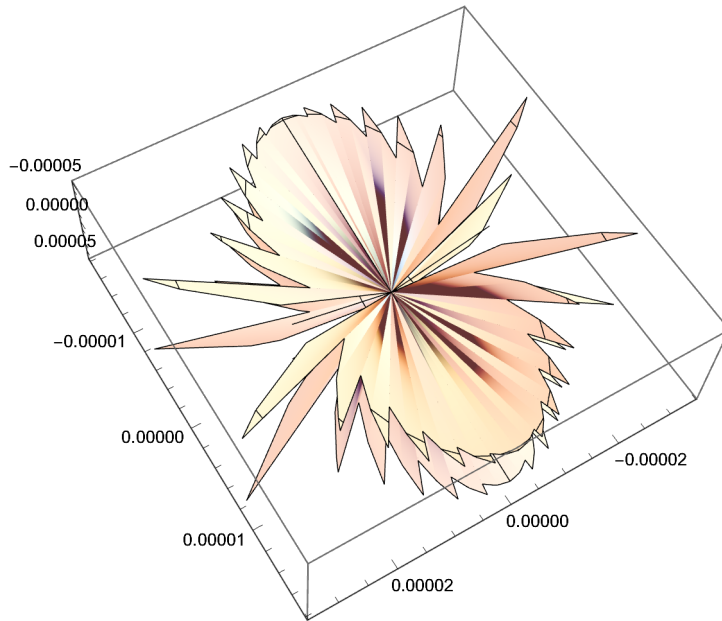
$$\left\{\theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi\right\},$$

$$\left\{\theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 - i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 + i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi\right\}\}$$

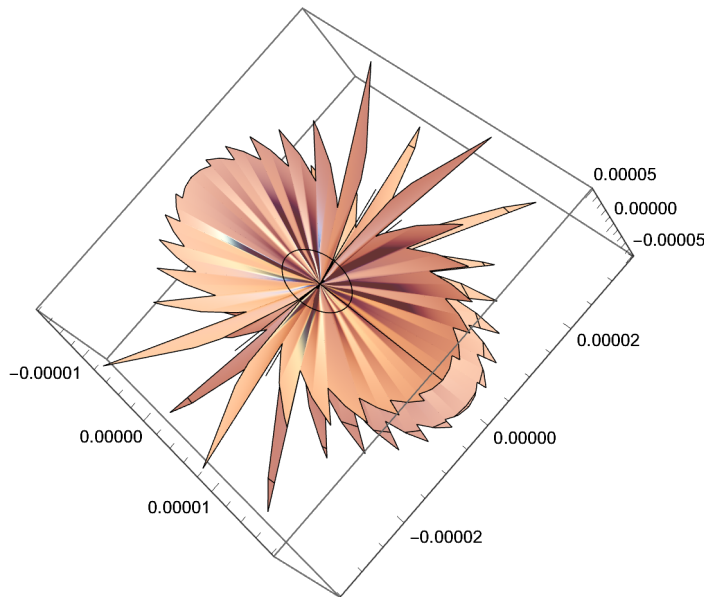
$$\text{RevolutionPlot3D}\left[r \frac{2}{3} \left(2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi\right), \{r, -1, 1\}\right]$$



`RevolutionPlot3D` $\left[r \left( \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \right), \{r, -1, 1\}\right]$

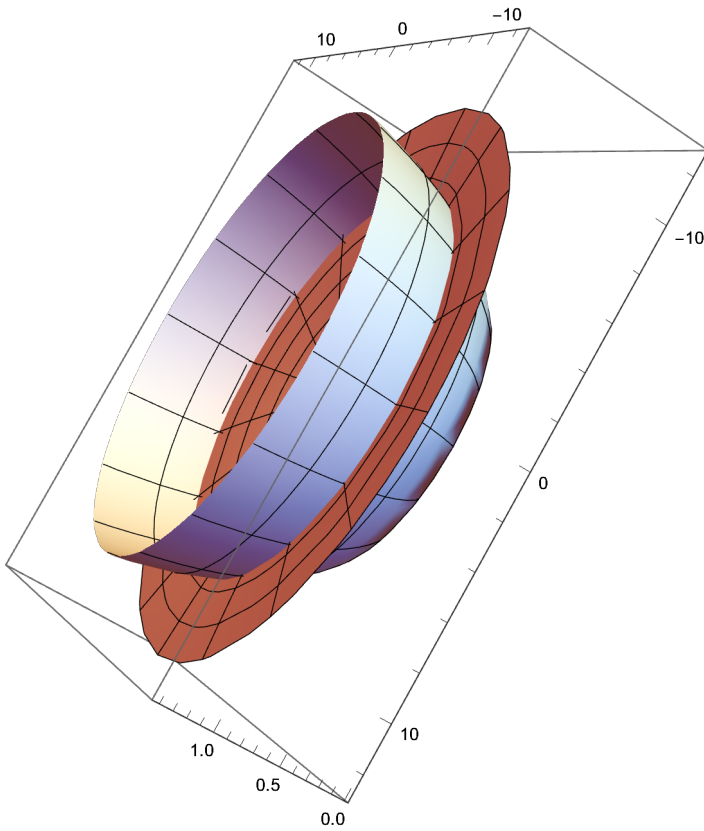


`RevolutionPlot3D` $\left[r \left( \frac{4 \pi}{3} + \frac{2 \left( 1 - \mathfrak{i} \sqrt{3} \right) \pi}{3 \left( 17 + 3 \sqrt{33} \right)^{1/3}} - \frac{1}{3} \left( 1 + \mathfrak{i} \sqrt{3} \right) \left( 17 + 3 \sqrt{33} \right)^{1/3} \pi \right), \{r, -1, 1\} \right]$

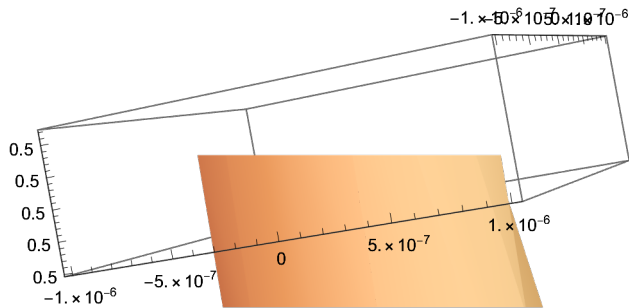


$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}, \{\theta, -4 \pi, 4 \pi\}\right]$$

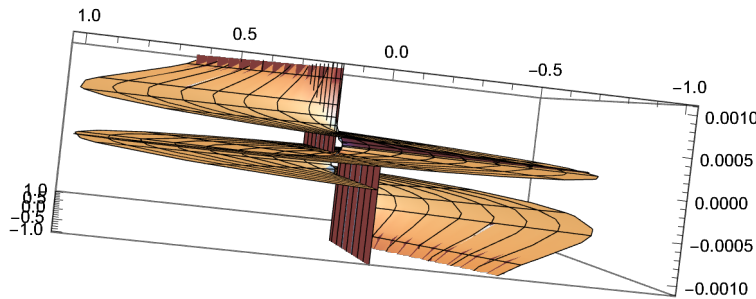


$$\text{RevolutionPlot3D}\left[\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}, \{\theta, -.000001, .000001\}\right]$$

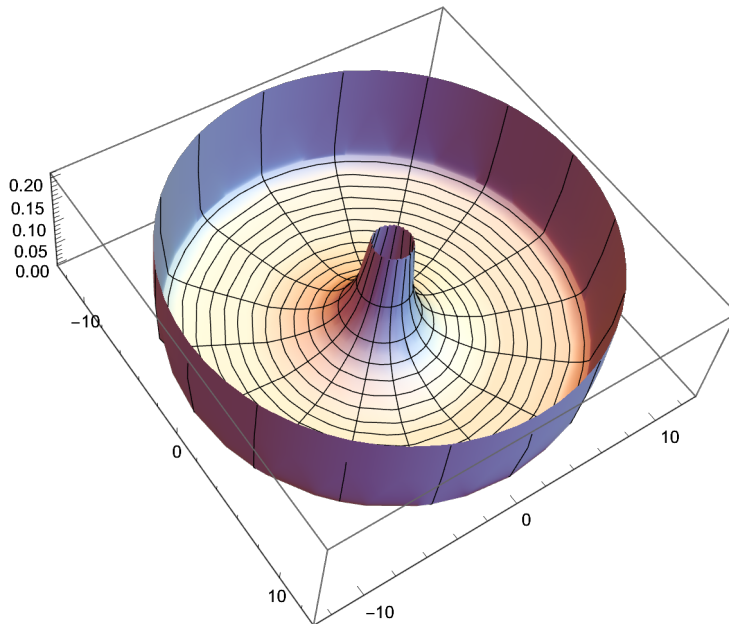


$$\text{velocity with changing wavelength} = \frac{\pi \left( -\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right)}{1080}$$

$$\text{RevolutionPlot3D}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080},\{r,-1,1\},\{\theta,-3\pi,3\pi\}\right]$$



$$\left\{\left\{r\rightarrow-\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\},\left\{r\rightarrow\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\}$$



$$\text{RevolutionPlot3D}\left[\left\{\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}},-\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\},\{\theta,-13,13\}\right]$$

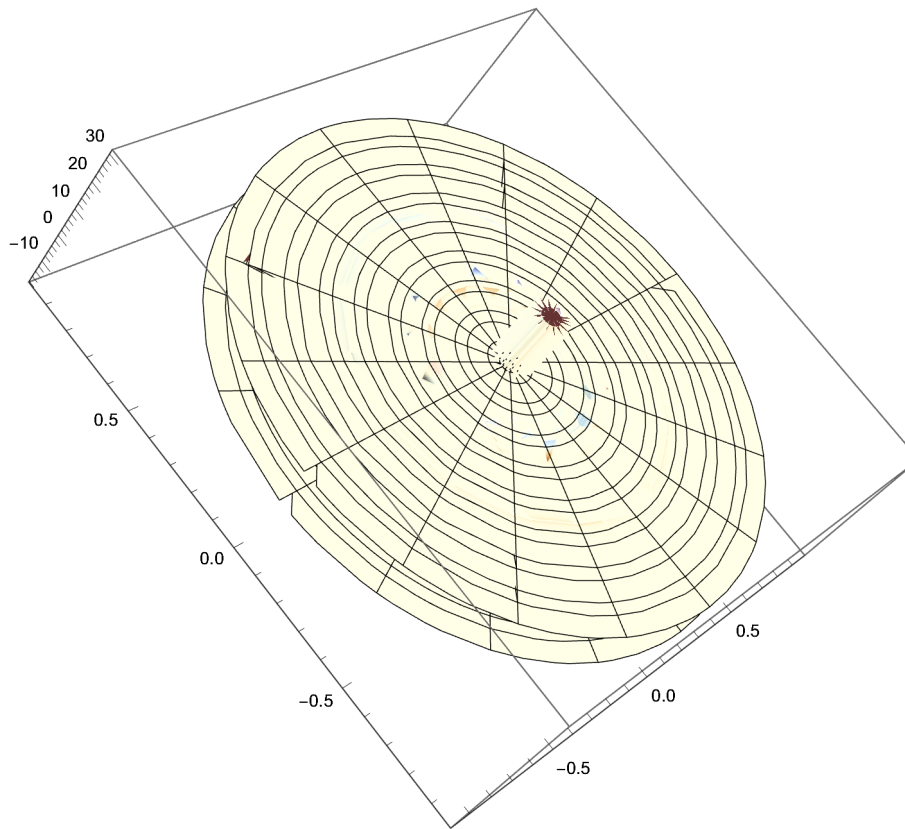
$$\text{Solve}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}==r(1/(1080/\pi)\theta),\theta\right]$$

$$\text{RevolutionPlot3D}\left[$$

$$\begin{aligned}
& \left\{ \left\{ \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) /} \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\}, \\
& \left\{ \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) /} \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\},
\end{aligned}$$

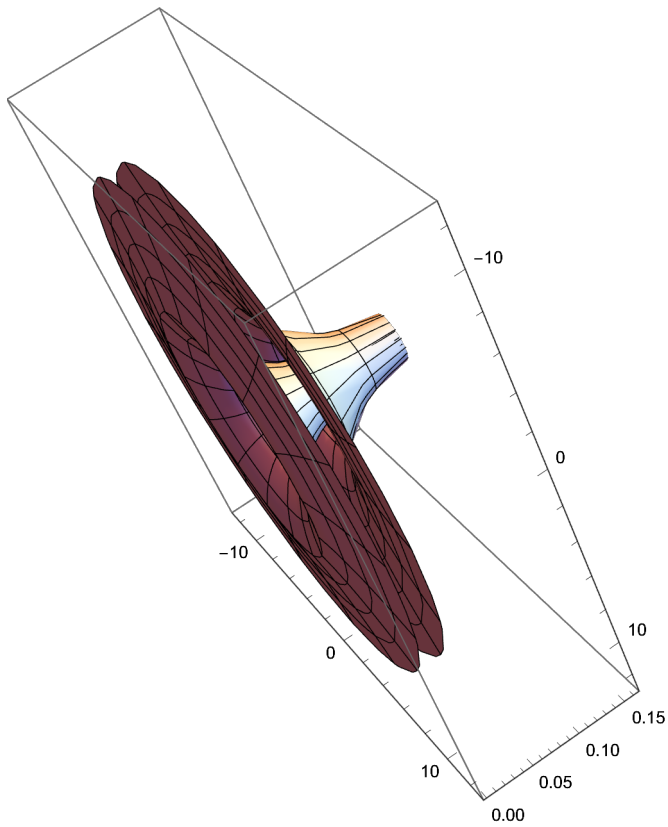


$$\begin{aligned}
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 - 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\}, \{r, -1, 1\}
\end{aligned}$$



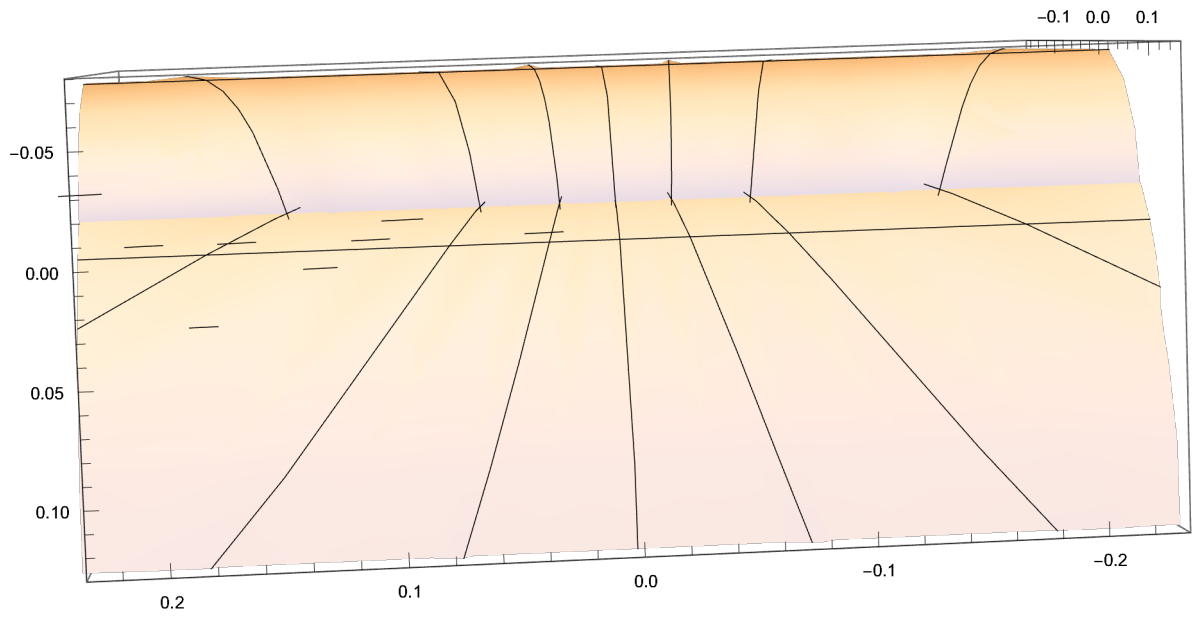
$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right\} \right\}$$

RevolutionPlot3D $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}, \{\theta, -4\pi, 4\pi\}\right]$



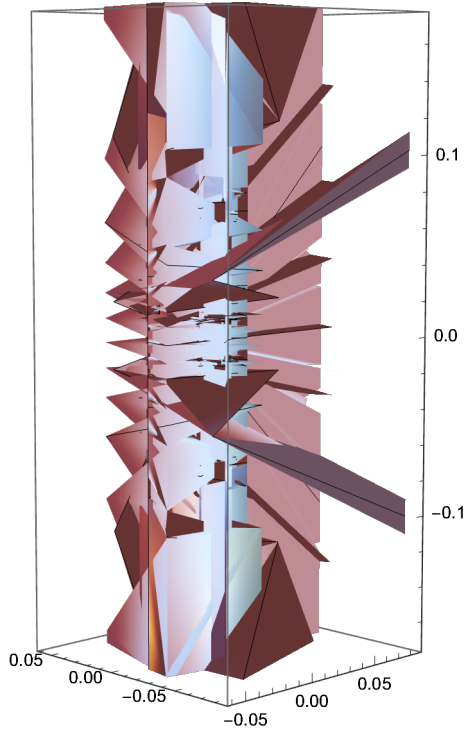
$$\left\{ \left\{ \mathbf{r} \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}} \right\} \right\}$$

SphericalPlot3D $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}}, \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\}\right]$

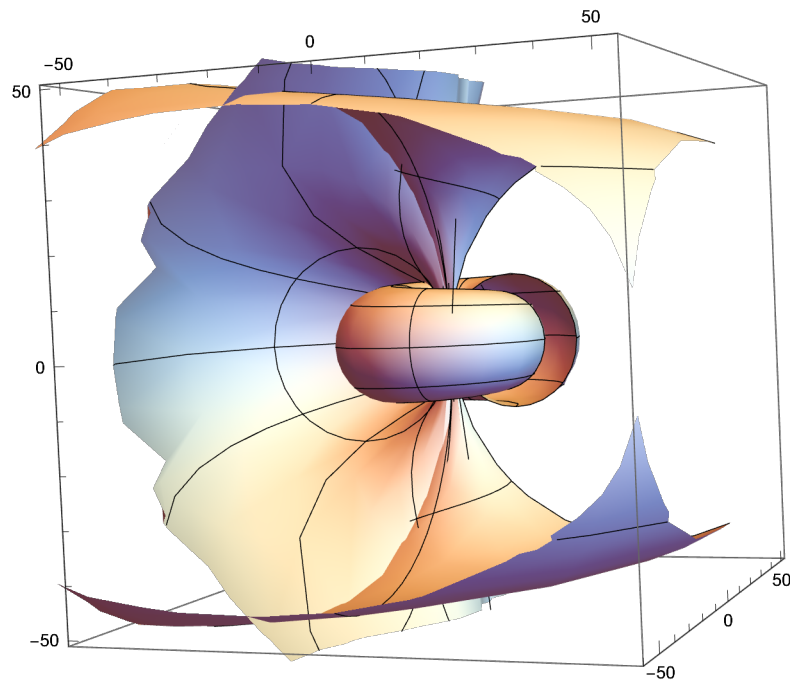


$8\pi^2 \sqrt{\theta}$

`SphericalPlot3D` $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}}, \{\beta, -\pi, \pi\}, \{\theta, -40\pi, 40\pi\}\right]$

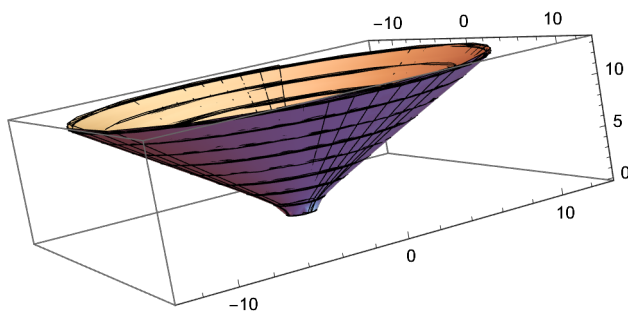


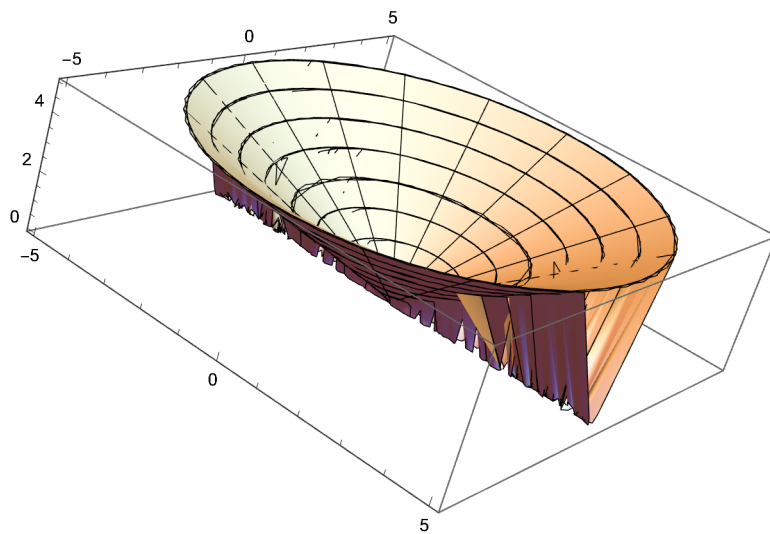
$$\text{SphericalPlot3D}\left[\frac{8 \pi^2 \sqrt{\theta}}{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2} \text{Csc}[\beta]}, \{\beta, -\pi, \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$

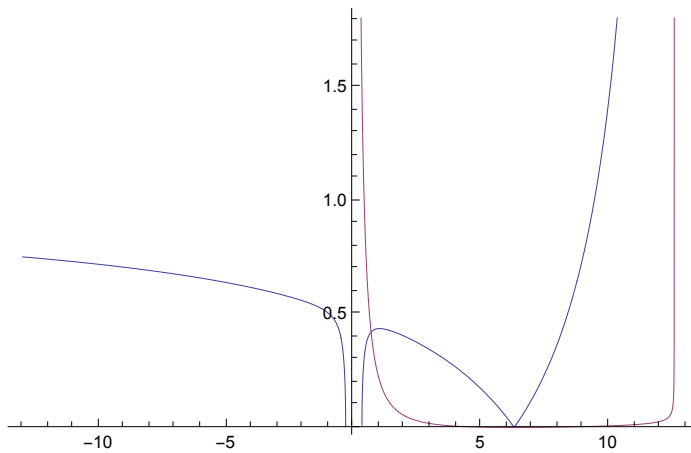


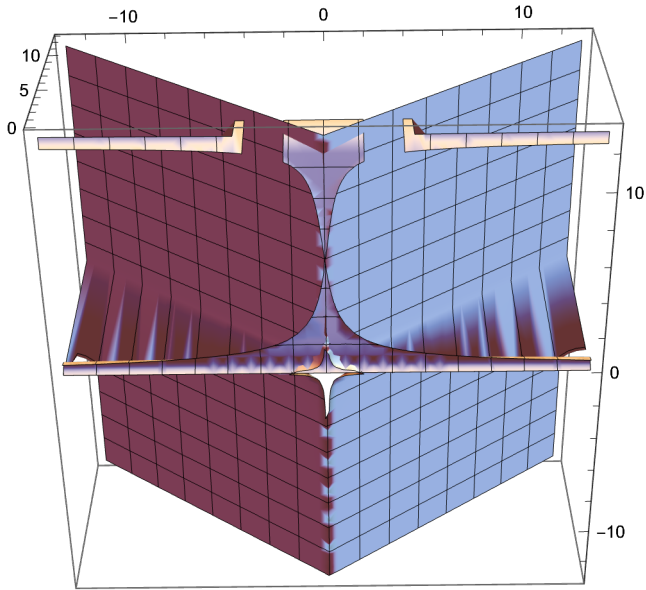
$$r_1 = \sqrt{r^2 - \eta^2}$$

$$\text{RevolutionPlot3D}\left[\sqrt{(r)^2 - \left(\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right)^2}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$$



$$\text{RevolutionPlot3D}\left[\sqrt{(r)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \{r, -5, 5\}, \{\theta, -3\pi, 3\pi\}\right]$$


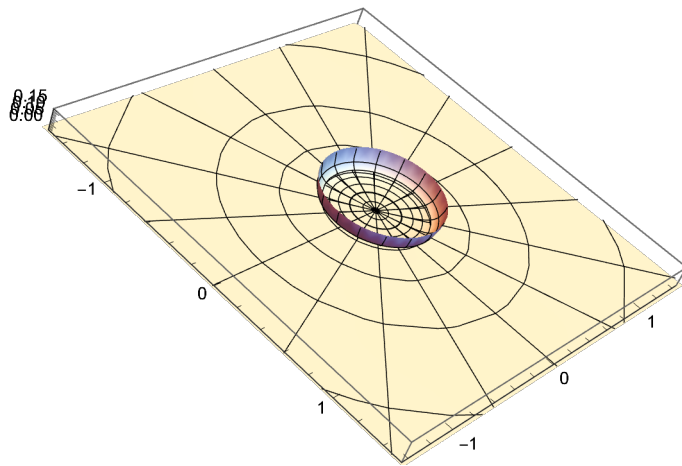
$$\text{Plot}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -13, 13\}\right]$$


$$\text{Plot3D}\left[\left\{\sqrt{r^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -13, 13\}, \{r, -13, 13\}\right]$$


$$\text{Plot3D}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}^2 - \left(\frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \sqrt{(r)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -13, 13\}, \{r, -1, 1\}\right]$$

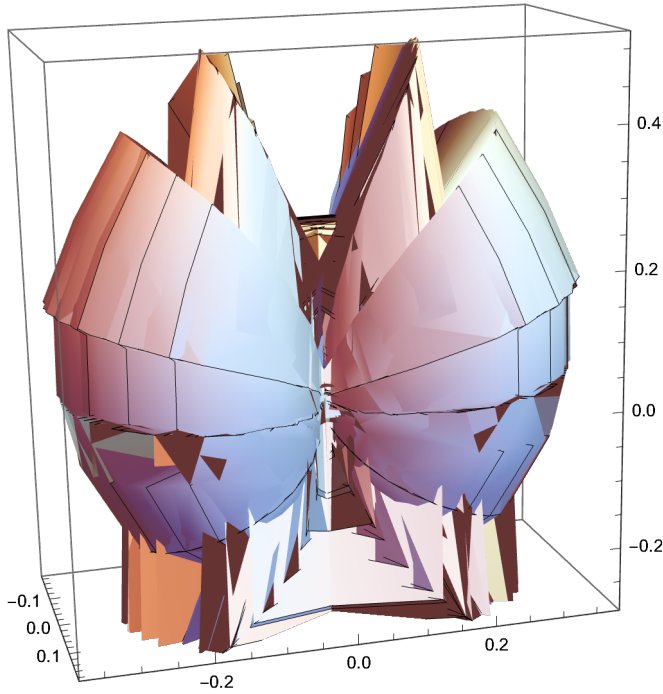


$$\text{RevolutionPlot3D}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \right. \right. \\ \left. \left. \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -4\pi, 4\pi\}\right]$$



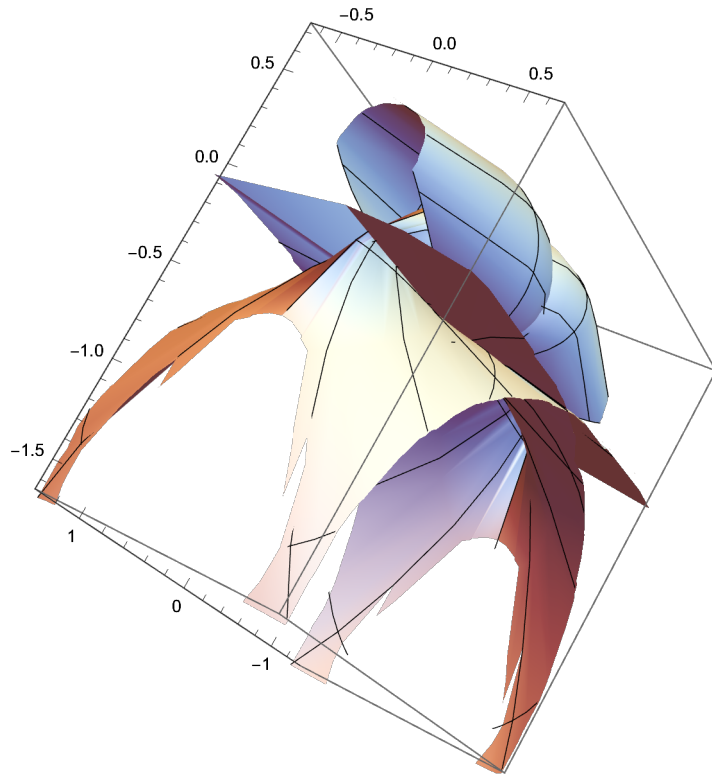
$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}}\right]^2}{2\pi},$$

$$\{\theta, -360, 360\}, \{\beta, -360, 360\}\right]$$



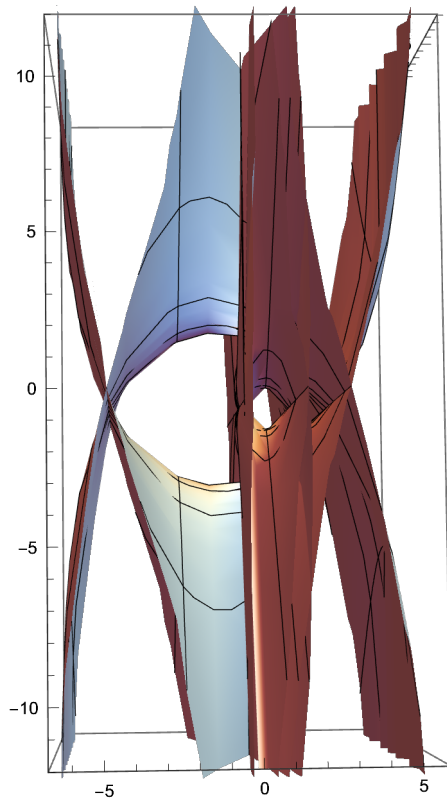
$$r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}} = \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta-\theta^2}} = \frac{2\pi\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}} = \frac{2\pi\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}$$

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$



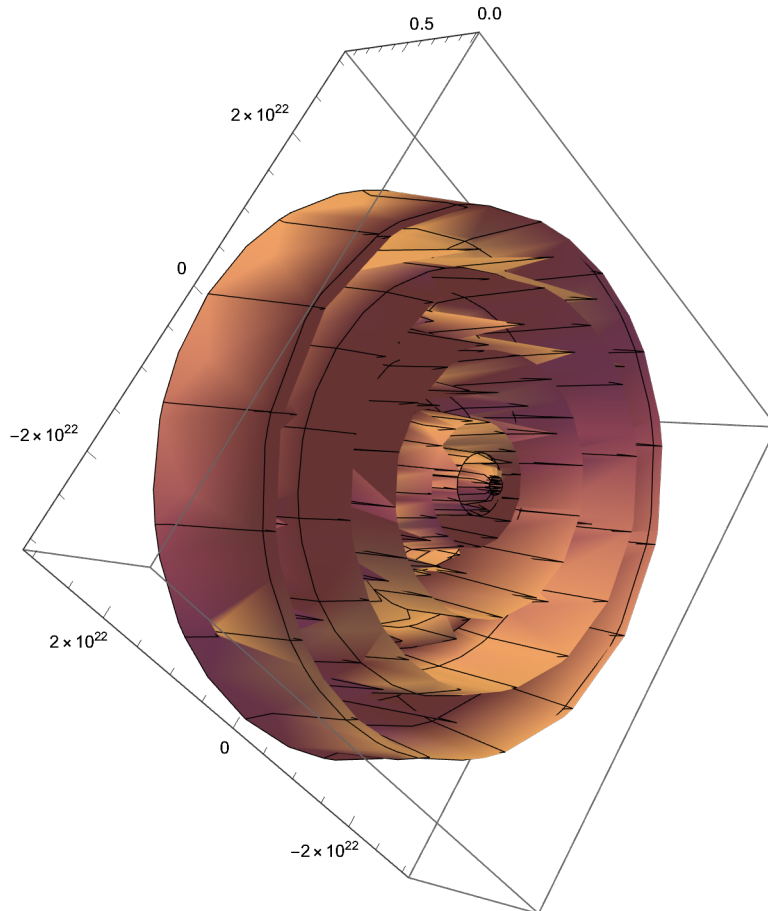
$$\sqrt{4 \pi \theta - \theta^2}$$

$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\theta - \theta^2}}{2\pi\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}}\sin[\beta], \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi, \pi\}\right]$

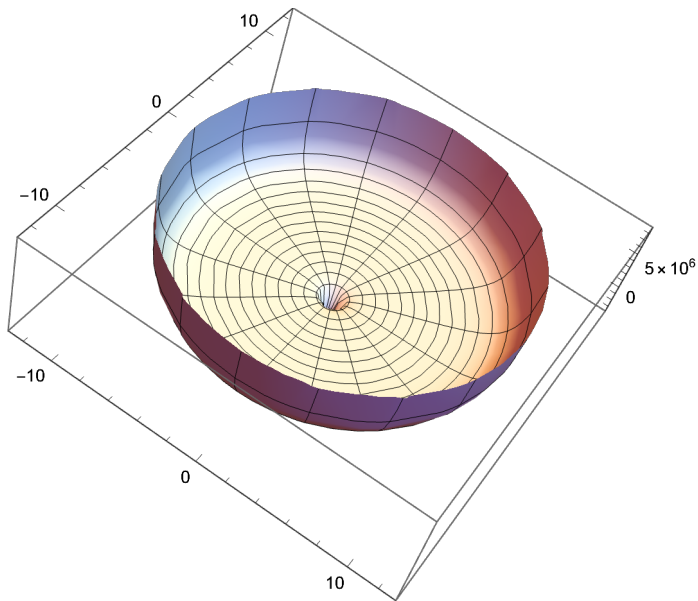


$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\right.$$

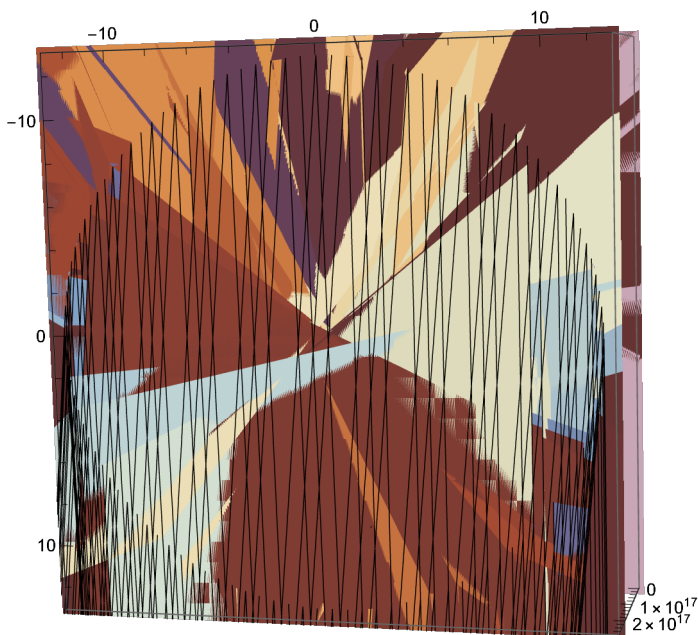
$$\left.\{\theta, -30000000000000000000000, 30000000000000000000000\}\right]$$



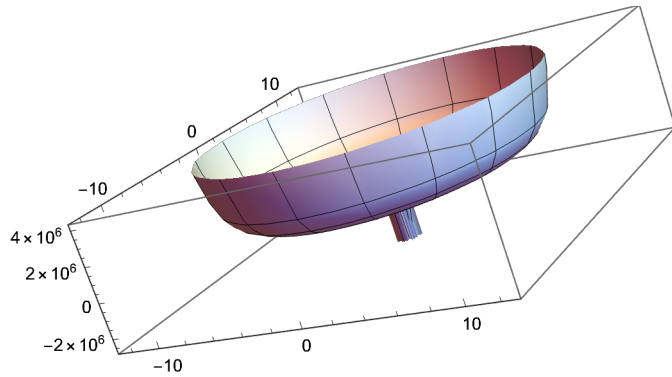
$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\{\theta,-4 \pi, 4 \pi\}\right]$



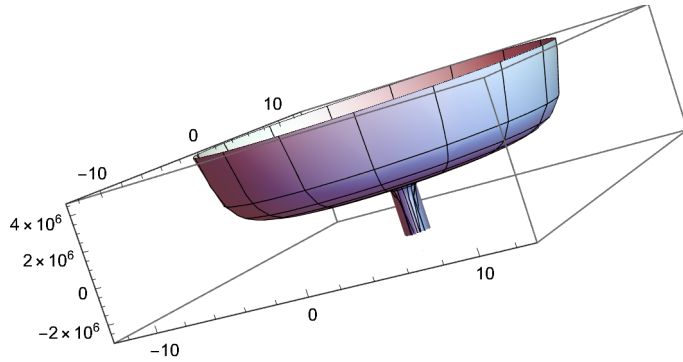
$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\{\theta,-12.8, 12.8\}\right]$



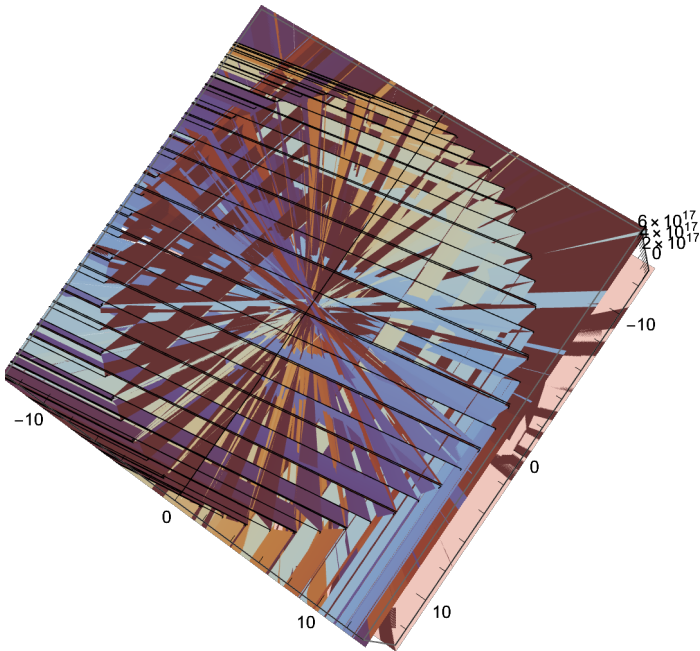
$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -12.9, 12.9\}\right]$$



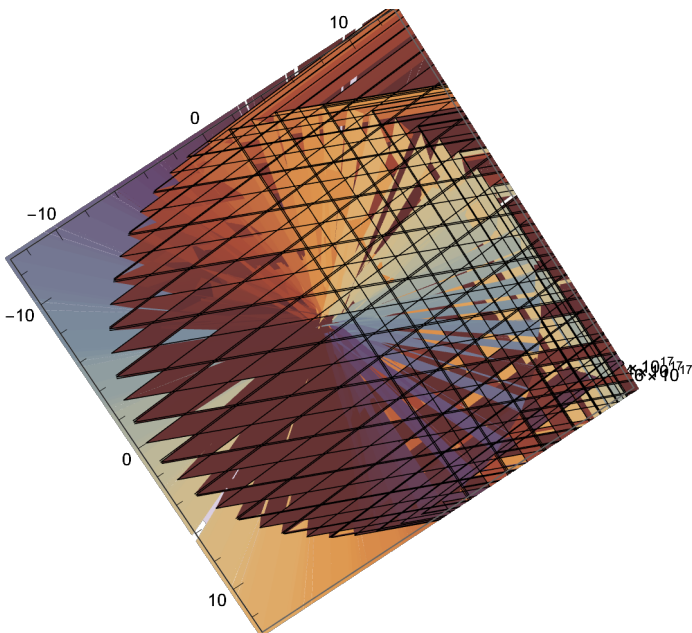
$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -12.99, 12.99\}\right]$$



$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\right. \\ \left.\{\theta,-12.999999999,12.999999999\}\right]$$

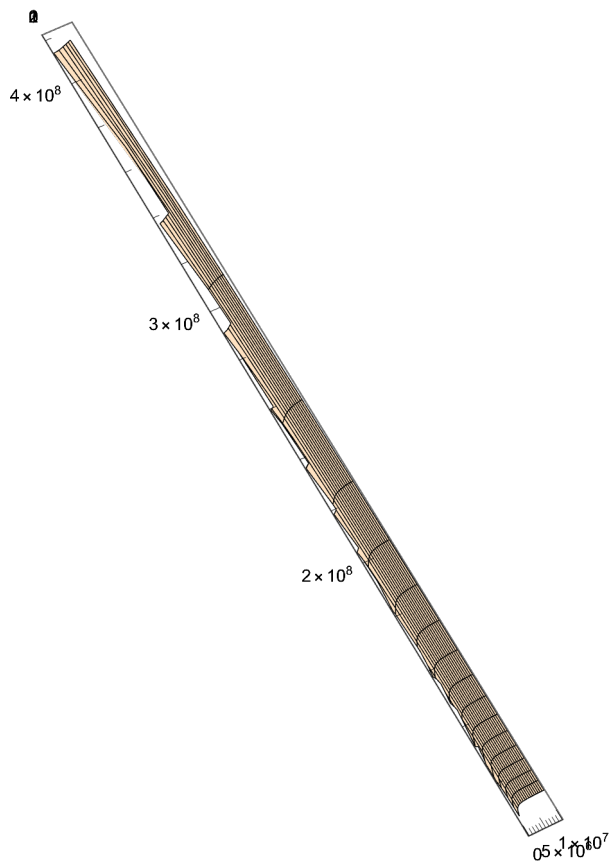


$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\{\theta,-13,13\}\right]$$

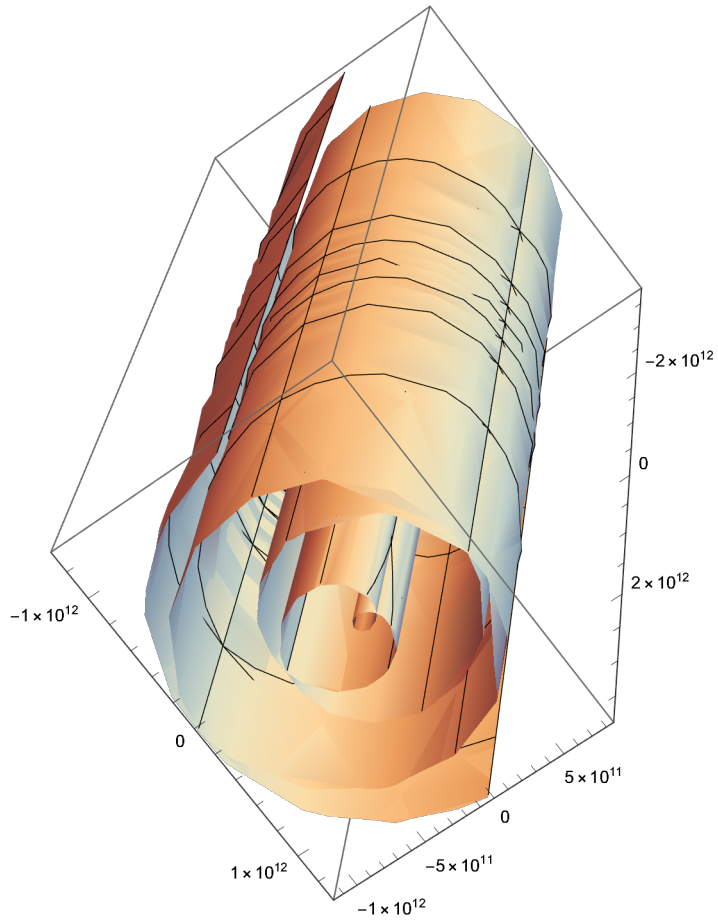




$$\text{RevolutionPlot3D}\left[\left\{\sqrt{(r)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \frac{\pi^2 \left(-\frac{540c}{\sqrt{4\pi-\theta}} (r\theta)^{3/2} + \frac{1080c}{(4\pi-\theta)^{3/2} \sqrt{\theta}} + \frac{1620c \sqrt{\theta}}{(4\pi-\theta)^{5/2}}\right)}{1166400}\right\}, \{r, -10000000, 10000000\}, \{\theta, -.0000003, .0000003\}\right]$$



`SphericalPlot3D` $\left[\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{4 \pi - \theta} \, \theta \, \text{Csc}[\beta]}{\pi \sqrt{4 \pi - \theta}}, \{\beta, -\pi, \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$



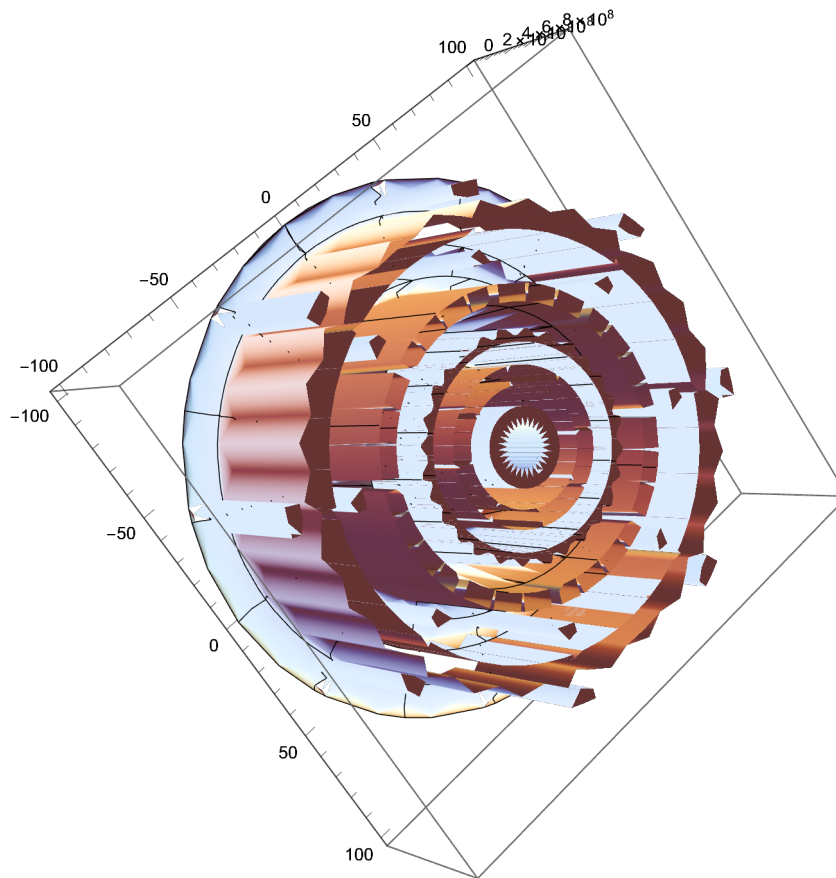
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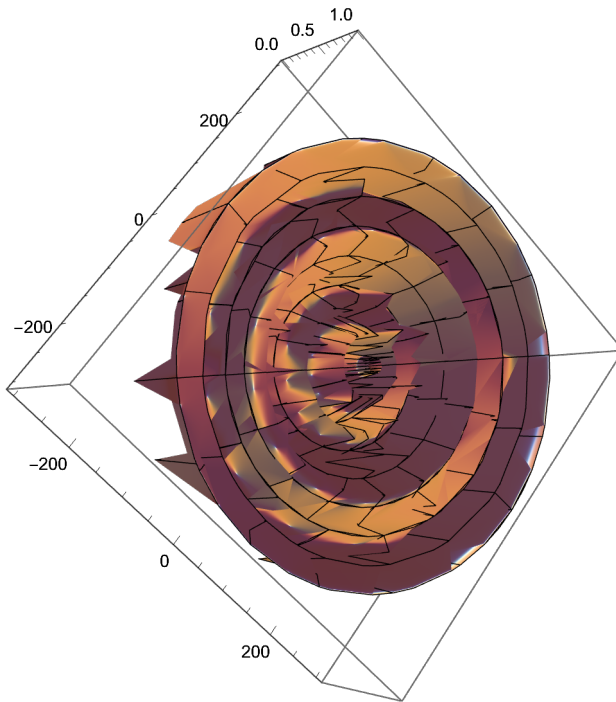
RevolutionPlot3D[
  
$$\frac{1}{1166400} \pi^2 \left( - \frac{540 c}{\sqrt{4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}} + \right.$$


$$\frac{1080 c}{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2} \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}} +$$


$$\left. \frac{1620 c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{5/2}} \right), \{\beta, -100, 100\}]$$

```



$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi}, \{\theta, -300, 300\}\right]$$


## Eulerian

A Paper on Leonard Euler's Formula in Natural Scientific Thought

To show that the ideas presented through the ontological cone  
(an analogy to the gestalt of perception through the sense of being),  
are applicable to the Euler equation is the purpose of this section.

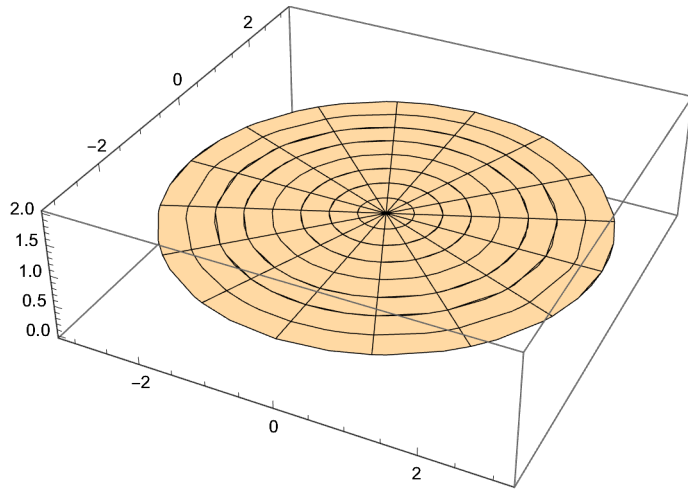
$$e^{i\beta} = \cos[\beta] + i\sin[\beta]$$

$$e^{i\theta} = \cos[\theta] + i\sin[\theta]$$

$$\text{RevolutionPlot3D}\left[e^{i\left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)}, \{\beta, -\pi, \pi\}\right]$$

RevolutionPlot3D[  

$$e^{\mathbf{i} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} e^{\mathbf{i} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)}, \{\beta, -\pi, \pi\}]$$

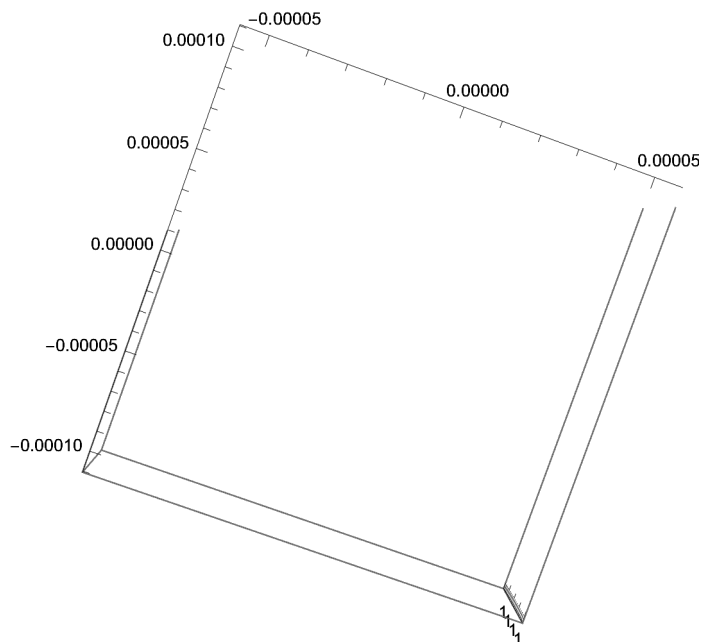


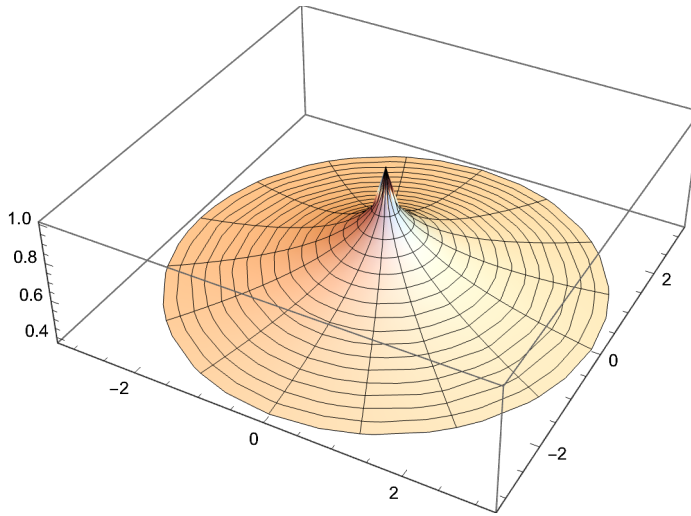
$$e^{\mathbf{i} \theta} = \cos[\theta] + \mathbf{i} \sin[\theta]$$

RevolutionPlot3D[Cos[θ] + i Sin[θ], {β, -π, π}]

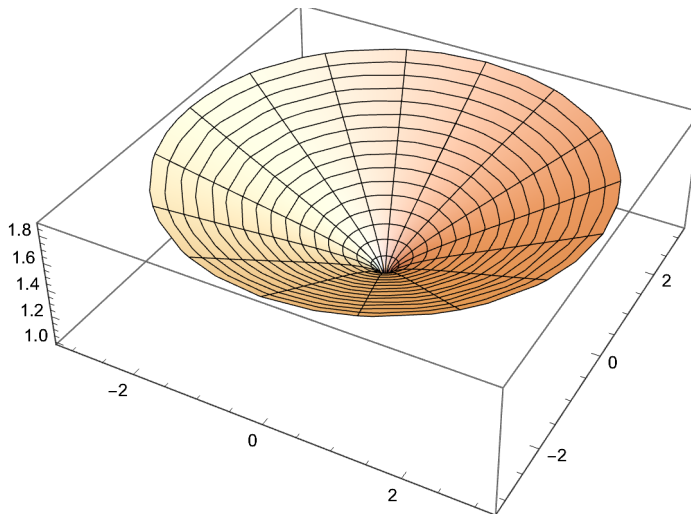
$$\beta = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

RevolutionPlot3D[Cos[β] + i Sin[β], {β, -π, π}]

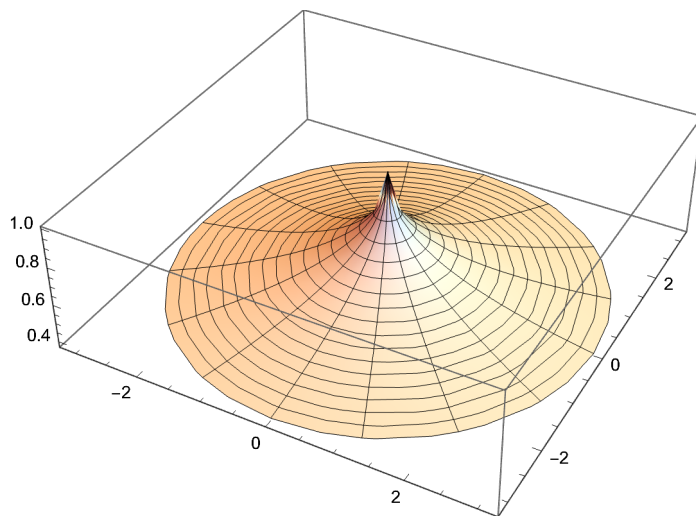


$$\text{RevolutionPlot3D}\left[\text{Cos}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] + i \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right], \{\theta, -\pi, \pi\}\right]$$


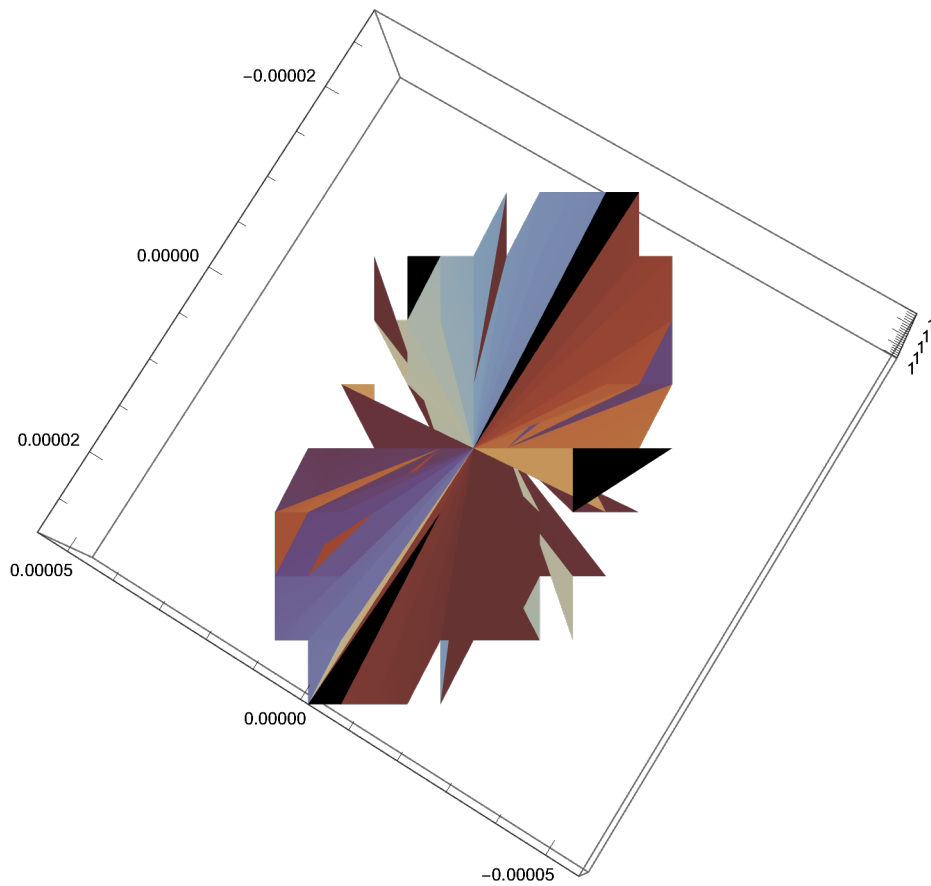
$$\text{SphericalPlot3D}\left[\text{Cos}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] + i \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right], \{\theta, -\pi, \pi\}\right]$$

$$\text{RevolutionPlot3D}\left[e^{i \left( \text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi\sqrt{-4\pi + \theta}}\right] \right)}, \{\theta, -\pi, \pi\}\right]$$


`RevolutionPlot3D` $\left[e^{\mathbf{i} \left(\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right)}, \{\theta, -\pi, \pi\}\right]$

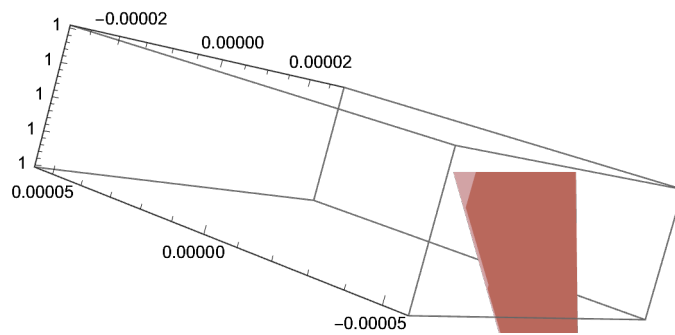


$\text{RevolutionPlot3D}\left[\text{e}^{\text{i} \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right)} \right. \\
\left. \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \right. \\
\left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right), \{\beta, -\pi, \pi\}]$

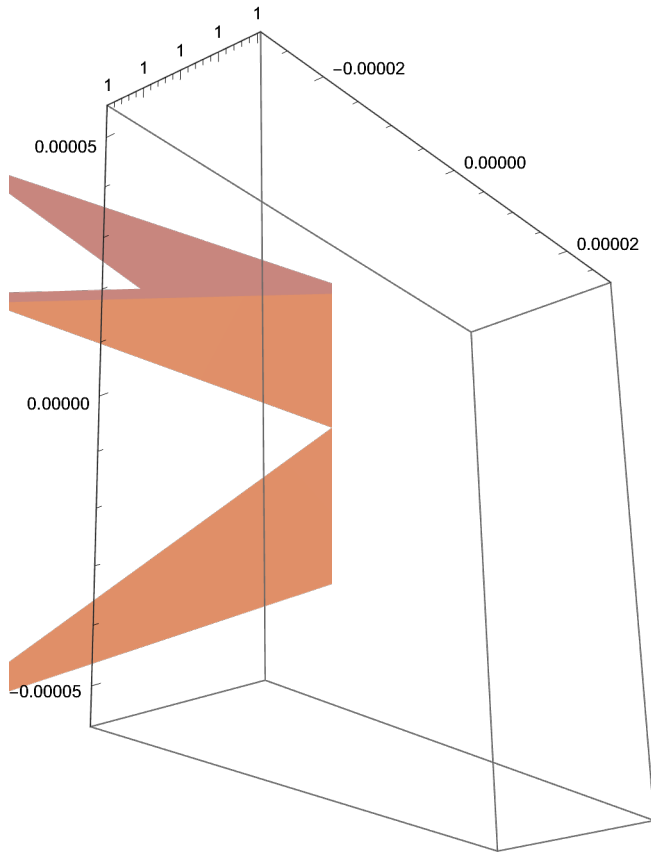




$\text{RevolutionPlot3D}\left[\text{e}^{\text{i} \left( \frac{4 \pi}{3} + \left( (1 - \text{i} \sqrt{3}) (-4 \pi^2 + 12 \pi^2 \text{Sin}[\beta]^2) \right) \right)} / \right.$   
 $\left. \left( 12 \left( -\pi^3 + 18 \pi^3 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) - \right.$   
 $\left. \frac{1}{3} \left( 1 + \text{i} \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \text{Sin}[\beta]^2 + \right. \right.$   
 $\left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right], \{\beta, -\pi, \pi\}]$



$\text{RevolutionPlot3D}\left[\text{e}^{\text{i} \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)}, \{\beta, -\pi, \pi\}]$



```

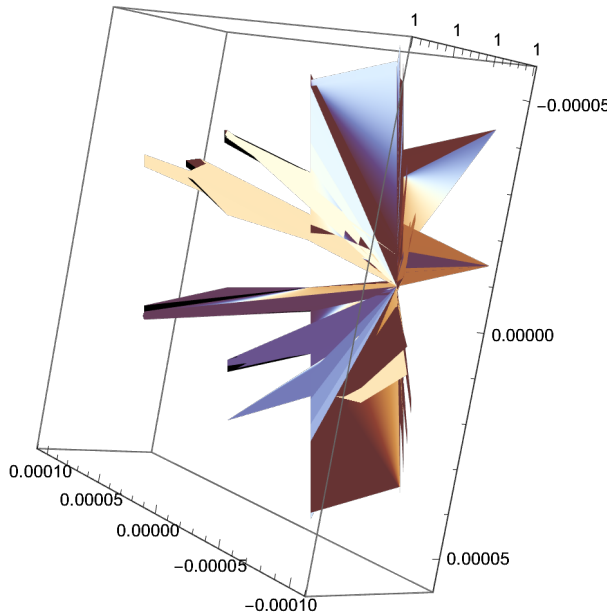
RevolutionPlot3D[
  (e^ (i ( (4 pi / 3) + ((1 - i sqrt(3)) (-4 pi^2 + 12 pi^2 Sin[beta]^2))) / (12 (-pi^3 + 18 pi^3 Sin[beta]^2 + 3 sqrt(3)
    sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3)) - 1/3 (1 + i sqrt(3))
    (-pi^3 + 18 pi^3 Sin[beta]^2 + 3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3))))
  (e^ (4 pi / 3 - (-4 pi^2 + 12 pi^2 Sin[beta]^2) / (6 (-pi^3 + 18 pi^3 Sin[beta]^2 +
    3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3)) + 2/3 (-pi^3 + 18 pi^3 Sin[beta]^2 +
    3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3)))) , {beta, -pi, pi}]

```

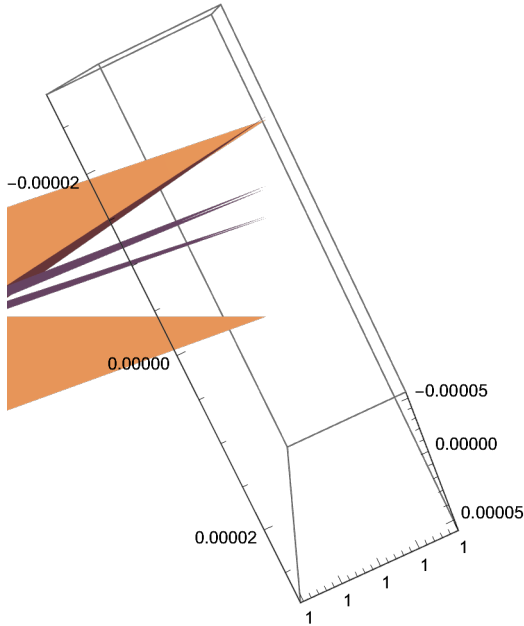
```

RevolutionPlot3D[
  e^ (i ( (4 pi / 3) + ((1 + i sqrt(3)) (-4 pi^2 + 12 pi^2 Sin[beta]^2)) / (12 (-pi^3 + 18 pi^3 Sin[beta]^2 +
    3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3)) - (1/3) (1 - i sqrt(3))
    (-pi^3 + 18 pi^3 Sin[beta]^2 + 3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3))
  e^ (i ( (4 pi / 3) + ((1 - i sqrt(3)) (-4 pi^2 + 12 pi^2 Sin[beta]^2)) /
    (12 (-pi^3 + 18 pi^3 Sin[beta]^2 + 3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3)) -
    (1/3) (1 + i sqrt(3)) (-pi^3 + 18 pi^3 Sin[beta]^2 +
    3 sqrt(3) sqrt(-pi^6 Sin[beta]^2 + 11 pi^6 Sin[beta]^4 + pi^6 Sin[beta]^6)^(1/3))
  ), {beta, -pi, pi}]

```



$$\text{RevolutionPlot3D}\left[e^{\imath}\left(\frac{4\pi}{3}-\left(-4\pi^2+12\pi^2\sin[\beta]^2\right)\right)\right. \\ \left.\left(6\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)+\frac{2}{3}\right. \\ \left.\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)\right],\{\beta,-\pi,\pi\}]$$



$$e^{\imath(\beta)} = (\cos[\beta] + \imath \sin[\beta])$$

$$e^{\imath\beta} = \cos[\beta] + \imath \sin[\beta]$$

If matter is composed of a geometric element in the shape of a cone,  
it may be purely geometrically stated that :

$$e^{\imath \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \left(\cos\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] + \imath \sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]\right)$$

$$e^{\imath \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \frac{\imath \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi-\theta)\theta}{4\pi^2}}$$

if it is within the region of  $\theta = \pi$ ,  $\beta = \frac{\pi}{2}$ .

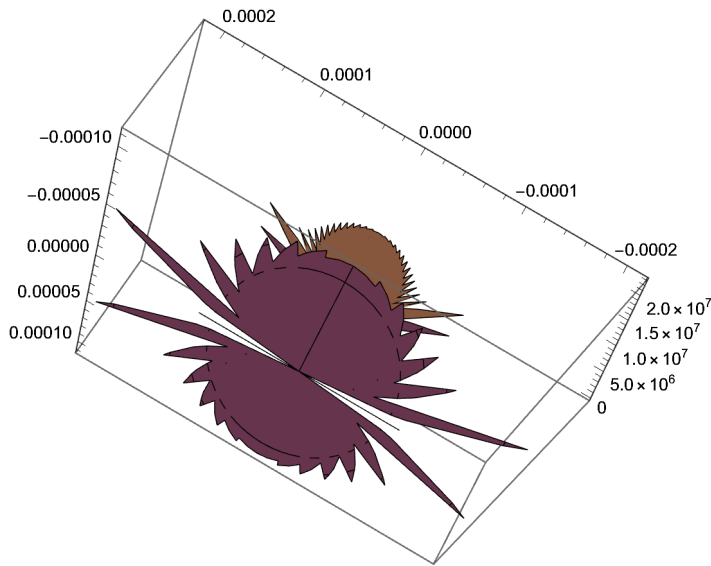
$$e^{\imath \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \frac{\imath \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi-\theta)\theta}{4\pi^2}} = \frac{\imath \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{u^2}{c^2}}$$

$$\text{Solve}\left[\sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}} == \frac{i\sqrt{(4\pi - \theta)\theta}}{2\pi} + \sqrt{1 - \frac{u^2}{c^2}}, u\right]$$

$$\left\{\left\{u \rightarrow -0.000494236 \sqrt{\left(2.34235 \times 10^{23} \theta - 1.86399 \times 10^{22} \theta^2 + \left(0. + 1.86399 \times 10^{22} i\right) \sqrt{12.5664 \theta - 1. \theta^2} \sqrt{39.4784 - 12.5664 \theta + 1. \theta^2}\right)}\right\},\right.$$

$$\left.\left\{u \rightarrow 0.000494236 \sqrt{\left(2.34235 \times 10^{23} \theta - 1.86399 \times 10^{22} \theta^2 + \left(0. + 1.86399 \times 10^{22} i\right) \sqrt{12.5664 \theta - 1. \theta^2} \sqrt{39.4784 - 12.5664 \theta + 1. \theta^2}\right)}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - 1.863986866980889 \theta^2 + \left(0. + 1.863986866980889 i\right) \sqrt{12.566370614359172 \theta - 1. \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)}, \{\theta, -2\pi, 2\pi\}\right]$$



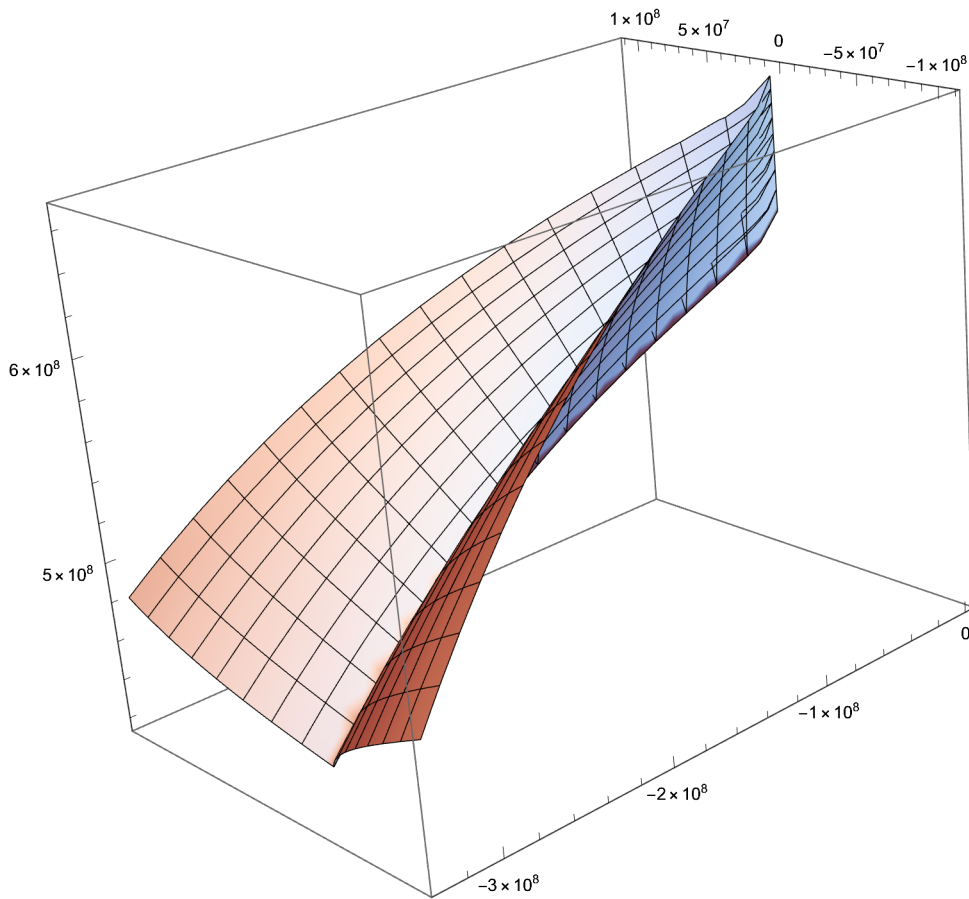
$$\theta = 2 \left( \pi \pm \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) == \frac{4\pi}{3} - \left( -4\pi^2 + 12\pi^2 \sin[\beta]^2 \right) /$$

$$\left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) +$$

$$\frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}$$

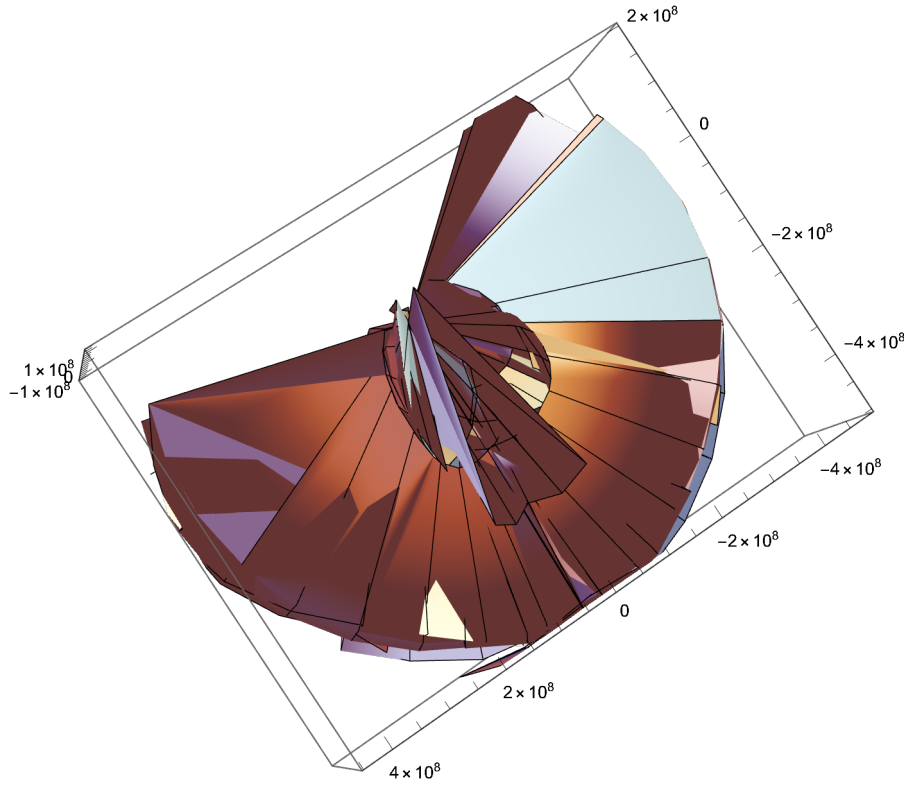
SphericalPlot3D[

$$\begin{aligned}
 &0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot 10^{23} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right.} \\
 &\quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
 &\quad \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) - \\
 &\quad 1.863986866980889 \cdot 10^{22} (\theta)^2 + (0. + 1.863986866980889 \cdot 10^{22} i) \\
 &\quad \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \\
 &\quad \left. \sqrt{39.47841760435743 \cdot \theta - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right), \\
 &\{\theta, -.2\pi, .2\pi\}, \{\beta, -.1\pi, .1\pi\}
 \end{aligned}$$



SphericalPlot3D[  

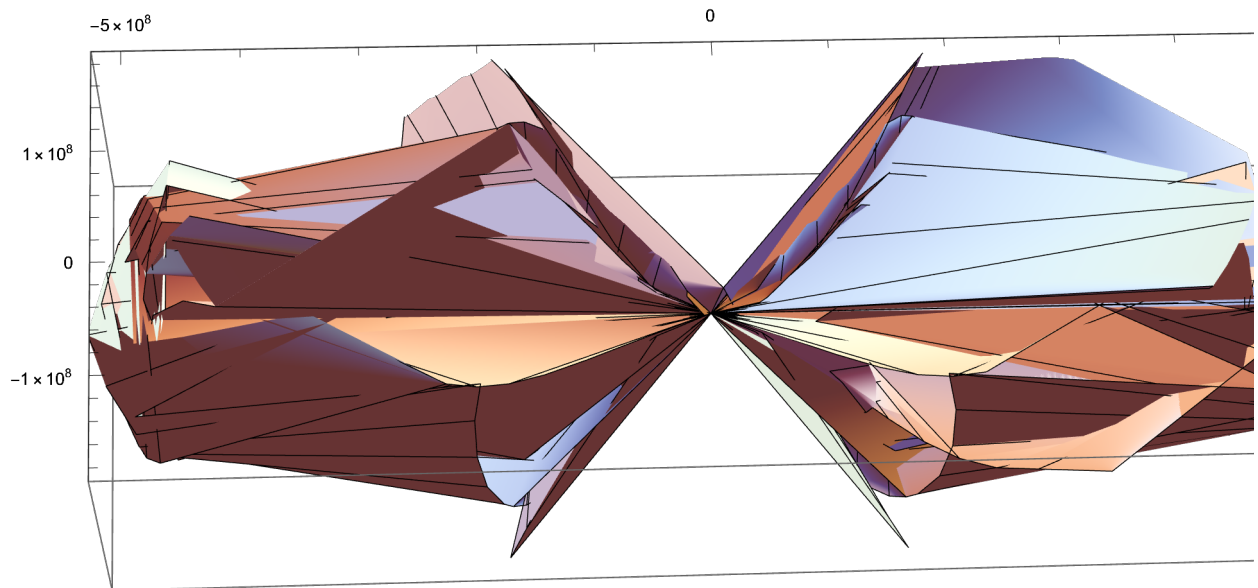
$$0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta^{23} - 1.863986866980889 \theta^{22} + (0. + 1.863986866980889 i) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right)} \sqrt{\left(39.47841760435743 - 12.566370614359172 \theta + 1. \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) / \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2\right)} \right),$$
  
 $\{\theta, -20 \pi, 20 \pi\}, \{\beta, -10 \pi, 10 \pi\}]$





SphericalPlot3D[

$$\begin{aligned}
 &0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta^{23} - 1.863986866980889 \theta^{22} + \right.} \\
 &\quad \left. (\theta + 1.863986866980889 \theta^{22} i) \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 &\quad \left. \sqrt{\left(39.47841760435743 - 12.566370614359172 \theta + \right.} \right. \\
 &\quad \left. 1. \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \\
 &\quad \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \right. \\
 &\quad \left. \left. \left. \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 \right) \right), \\
 &\{\beta, -10 \pi, 10 \pi\}, \{\theta, -20 \pi, 20 \pi\}
 \end{aligned}$$



$$\begin{aligned}
 &\text{Solve}\left[\sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}} == \frac{i \sqrt{(4 \pi - \theta) \theta}}{2 \pi} + \sqrt{1 - \frac{u^2}{c^2}}, \theta\right] \\
 &\left\{\left\{\theta \rightarrow \frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2}\right\},\right. \\
 &\quad \left.\left\{\theta \rightarrow \frac{\pi \left(2 c^4 - 2 c^2 u^2 + \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2}\right\}\right\}
 \end{aligned}$$

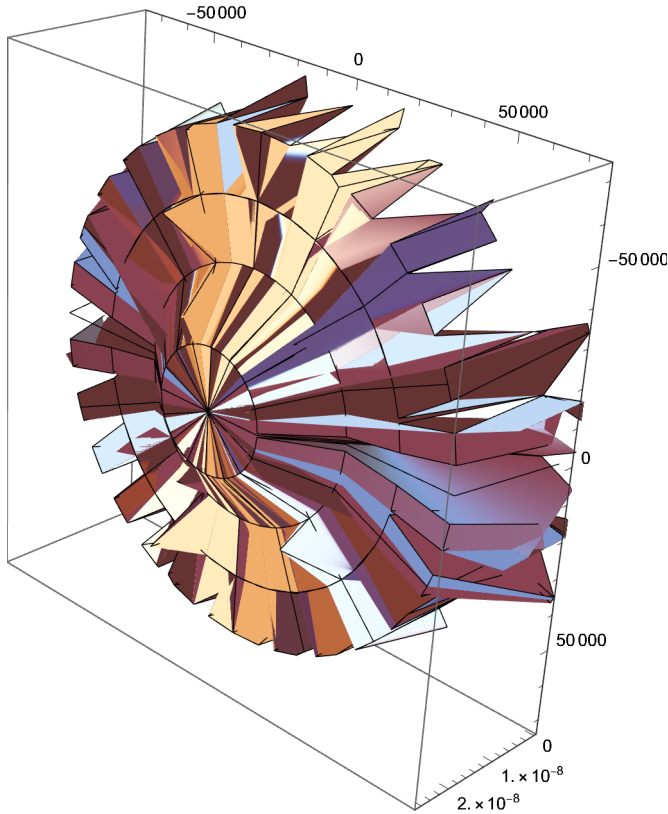
$$\text{Solve}\left[\frac{\pi\left(2c^4-2c^2u^2-\sqrt{4c^8-8c^6u^2+5c^4u^4-c^2u^6}\right)}{c^4-c^2u^2}==2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}[\beta]^2}\right),\beta\right]$$

$$\left\{\left\{\beta\rightarrow-1.\text{ArcSin}\left[0.31831\right.\right.\right.$$

$$\begin{aligned} & \sqrt{\left(-\frac{1.28794\times 10^{69}}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}+\frac{2.86605\times 10^{52}u^2}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}-\right. \\ & \frac{1.79376\times 10^{35}u^4}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}+\frac{2.21759\times 10^{17}u^6}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}+ \\ & \frac{1.59446\times 10^{35}}{8.07761\times 10^{33}-8.98755\times 10^{16}u^2}-\frac{1.77407\times 10^{18}u^2}{8.07761\times 10^{33}-8.98755\times 10^{16}u^2}+ \\ & \left(2.39003\times 10^{43}\sqrt{\left(2.90392\times 10^{51}+2.47588\times 10^{27}u-6.46209\times 10^{34}\right.}\right. \\ & \left.\left.u^2+1.71799\times 10^{10}u^3+4.49378\times 10^{17}u^4-1.u^6\right)\right)/ \\ & \left.\left.\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2-\left(2.65927\times 10^{26}u^2\right.\right. \right. \\ & \left.\left.\sqrt{\left(2.90392\times 10^{51}+2.47588\times 10^{27}u-6.46209\times 10^{34}u^2+1.71799\times 10^{10}\right.}\right. \right. \\ & \left.\left.\left.u^3+4.49378\times 10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2-\right. \\ & \left.\left.\left(2.95883\times 10^9\sqrt{\left(2.90392\times 10^{51}+2.47588\times 10^{27}u-6.46209\times 10^{34}\right.}\right. \right. \right. \\ & \left.\left.\left.u^2+1.71799\times 10^{10}u^3+4.49378\times 10^{17}u^4-1.u^6\right)\right)/\right. \\ & \left.\left.\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)\right)\right]\},\left\{\beta\rightarrow\text{ArcSin}\left[0.31831\right.\right. \end{aligned}$$

$$\begin{aligned} & \sqrt{\left(-\frac{1.28794\times 10^{69}}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}+\frac{2.86605\times 10^{52}u^2}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}-\right. \\ & \frac{1.79376\times 10^{35}u^4}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}+\frac{2.21759\times 10^{17}u^6}{\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2}+ \\ & \frac{1.59446\times 10^{35}}{8.07761\times 10^{33}-8.98755\times 10^{16}u^2}-\frac{1.77407\times 10^{18}u^2}{8.07761\times 10^{33}-8.98755\times 10^{16}u^2}+ \\ & \left(2.39003\times 10^{43}\sqrt{\left(2.90392\times 10^{51}+2.47588\times 10^{27}u-6.46209\times 10^{34}u^2+1.71799\times\right.}\right. \\ & \left.\left.10^{10}u^3+4.49378\times 10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2- \\ & \left(2.65927\times 10^{26}u^2\sqrt{\left(2.90392\times 10^{51}+2.47588\times 10^{27}u-6.46209\times 10^{34}u^2+1.71799\times\right.}\right. \\ & \left.\left.10^{10}u^3+4.49378\times 10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)^2- \\ & \left.\left.\left(2.95883\times 10^9\sqrt{\left(2.90392\times 10^{51}+2.47588\times 10^{27}u-6.46209\times 10^{34}u^2+1.71799\times 10^{10}\right.}\right. \right. \right. \\ & \left.\left.\left.u^3+4.49378\times 10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times 10^{33}-8.98755\times 10^{16}u^2\right)\right)\right]\}\} \end{aligned}$$

$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\text{ArcSin}\left[ \right. \right. \\
& 0.3183098861837907 \sqrt{\left( -\frac{1.2879392082837613 \cdot u^{69}}{(8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2} + \right.} \\
& \quad \frac{2.86605126458116 \cdot u^{52}}{(8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2} - \\
& \quad \frac{1.793763056356184 \cdot u^{43}}{(8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2} + \\
& \quad \frac{2.217589516890687 \cdot u^{17}}{(8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2} + \\
& \quad \frac{1.594456050094386 \cdot u^{35}}{8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2} - \\
& \quad \frac{1.7740716135125496 \cdot u^{18}}{8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2} + \\
& \quad (2.3900294921538355 \cdot u^{43} \sqrt{(2.903917065069822 \cdot u^{51} + \\
& \quad 2.4758800785707605 \cdot u^{27} u - 6.462086970449991 \cdot u^{34} u^2 + \\
& \quad 1.7179869184 \cdot u^{10} u^3 + 4.493775893684088 \cdot u^{17} u^4 - 1 \cdot u^6)}) / \\
& \quad (8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2 - \\
& \quad (2.6592664484147662 \cdot u^{26} u^2 \sqrt{(2.903917065069822 \cdot u^{51} + \\
& \quad 2.4758800785707605 \cdot u^{27} u - 6.462086970449991 \cdot u^{34} u^2 + \\
& \quad 1.7179869184 \cdot u^{10} u^3 + 4.493775893684088 \cdot u^{17} u^4 - 1 \cdot u^6)}) / \\
& \quad (8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2 - \\
& \quad (2.958832962890196 \cdot u^9 \sqrt{(2.903917065069822 \cdot u^{51} + \\
& \quad 2.4758800785707605 \cdot u^{27} u - 6.462086970449991 \cdot u^{34} u^2 + \\
& \quad 1.7179869184 \cdot u^{10} u^3 + 4.493775893684088 \cdot u^{17} u^4 - 1 \cdot u^6)}) / \\
& \quad (8.07760871306249 \cdot u^{33} - 8.987551787368176 \cdot u^{16} u^2)^2 \left. \right] \right], \{u, -c, c\}]
\end{aligned}$$



$$\text{Solve}\left[\frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2} == 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right), u\right]$$

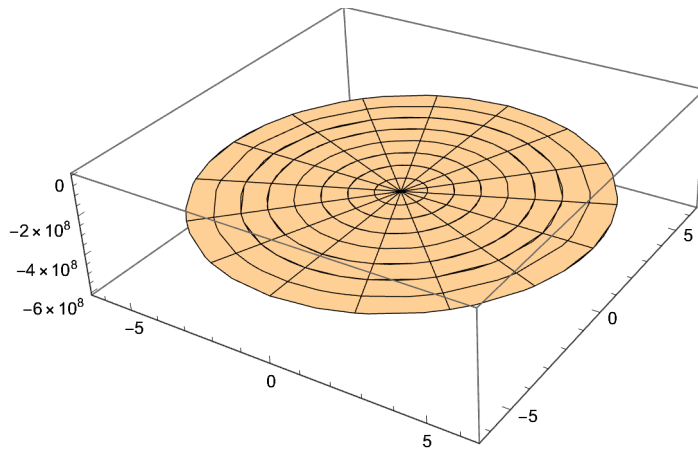
$$\begin{aligned} & \left\{ \left\{ u \rightarrow \text{Root}\left[4.0532258104836432542368746274352 \times 10^{67} - \right. \right. \right. \\ & \quad 1.7079612615978583669368862294392 \times 10^{83} \text{Sin}[\beta]^2 + \\ & \quad 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\ & \quad \left(-5.4111401881449464088210664670613 \times 10^{50} + \right. \\ & \quad \quad \left. 3.8007263869085317046852183304742 \times 10^{66} \text{Sin}[\beta]^2\right) \#1^2 - \\ & \quad 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\ & \quad \left(-5.2860980342978121431211906423698 \times 10^{48} - \right. \\ & \quad \quad \left. 2.1144392137191221020101719542600 \times 10^{49} \text{Sin}[\beta]^2\right) \#1^4 - \\ & \quad \left. 3.5056932414569705289890250000000 \times 10^{24} \#1^5 + \right. \\ & \quad \left. 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 1\right\}, \\ & \left\{ u \rightarrow \text{Root}\left[4.0532258104836432542368746274352 \times 10^{67} - \right. \right. \\ & \quad 1.7079612615978583669368862294392 \times 10^{83} \text{Sin}[\beta]^2 + \\ & \quad 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\ & \quad \left(-5.4111401881449464088210664670613 \times 10^{50} + \right. \\ & \quad \quad \left. 3.8007263869085317046852183304742 \times 10^{66} \text{Sin}[\beta]^2\right) \#1^2 - \\ & \quad 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\ & \quad \left(-5.2860980342978121431211906423698 \times 10^{48} - \right. \\ & \quad \quad \left. 2.1144392137191221020101719542600 \times 10^{49} \text{Sin}[\beta]^2\right) \#1^4 - \end{aligned}$$

\_\_\_\_\_ 31 6 2 1 1 1

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RevolutionPlot3D[Root[
  4.0532258104836432542368746274352049384829996549868873500941076135936`31.909179\
    540382016*^67 -
  1.7079612615978583669368862294391867719820309387352160756817670917`31.9091795\
    4038201*^83 Sin[ $\beta$ ]2 +
  1.456208000368304401804170610562654241243542338347007475712`31.90917954038201\
    *^59 #1 +
  (-5.41114018814494640882106646706128560033702885720064`31.90917954038201*^50 +
    3.800726386908531704685218330474210119415700395484123748732097265664`31.9\
    0917954038201*^66 Sin[ $\beta$ ]2) #12 -
  2.0208945633153124779637513510658550792192`31.909179540382*^42 #13 +
  (-5.286098034297812143121190642369759388314386825216`31.90917954038201*^48 -
    2.1144392137191221020101719542599757567807700598784`31.90917954038201*^49
    Sin[ $\beta$ ]2) #14 - 3.505693241456970528989025`31.90917954038201*^24 #15 +
  5.88157727416637492704831340544`31.90917954038201*^31 #16 &, 1], { $\beta$ , -2  $\pi$ , 2  $\pi$ }]

```



$$\begin{aligned}
& \frac{\pi \left( 2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6} \right)}{c^4 - c^2 u^2} = \\
& \left\{ \left\{ \theta \rightarrow \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \right. \right. \\
& \quad \left. \frac{2 \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} - \frac{\left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2 \right)}{12 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} + \right. \\
& \quad \left. \frac{\left( 1 - \mathfrak{i} \sqrt{3} \right) \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} - \frac{\left( 1 - \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2 \right)}{12 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} + \right. \\
& \quad \left. \frac{\left( 1 + \mathfrak{i} \sqrt{3} \right) \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right\} \} \\
& \left\{ \left\{ \theta \rightarrow \frac{4 \pi}{3} - \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} + \left( \left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) \right) / \left( 12 \right. \right. \\
& \quad \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \left. \right) - \frac{1}{3} \left( 1 - \right. \\
& \quad \left. \mathfrak{i} \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \left. \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} + \left( \left( 1 - \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) \right) / \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \left. \right\} \}
\end{aligned}$$

$\theta$  = Those other three long ones (1 real 2 imaginary)

$$\begin{aligned} \text{from Solve} \left[ \frac{1}{2\pi} \left( \sqrt{4\pi r^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right)} \right. \right. \\ \left. \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\ \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \\ \left. r^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right] \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \right. \\ \left. \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 \Bigg) \Bigg] = \\ r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{-4\pi^2 \theta + 4\pi \theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}} \right] \right], \theta \end{aligned}$$

$c := (2.99792458 * 10^8)$

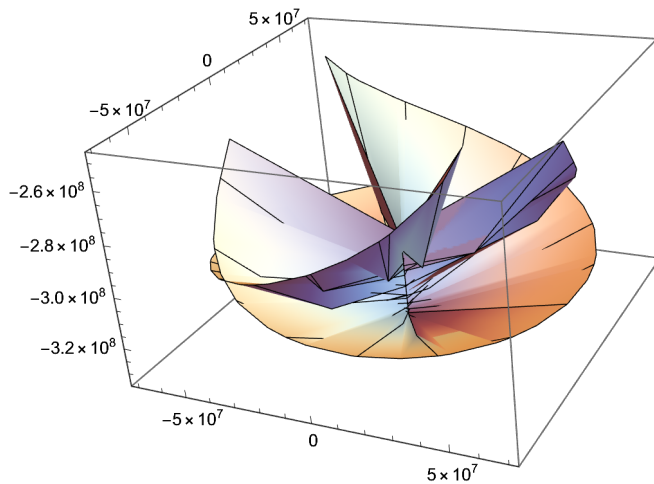
$\theta$  = A set of three potential threes of solutions solvable with ease.



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SphericalPlot3D[Root[
  4.0532258104836432542368746274352049384829996549868873500941076135936`31.909179\
  540382016*^67 -
  1.7079612615978583669368862294391867719820309387352160756817670917`31.9091795\
  4038201*^83 Sin[ArcSin[ $\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}$ ]]^2 +
  1.456208000368304401804170610562654241243542338347007475712`31.90917954038201\
  *^59 #1 +
  (-5.41114018814494640882106646706128560033702885720064`31.90917954038201*^50 +
  3.800726386908531704685218330474210119415700395484123748732097265664`31.9\
  0917954038201*^66 Sin[ $\beta$ ]^2) #1^2 -
  2.0208945633153124779637513510658550792192`31.909179540382*^42 #1^3 +
  (-5.286098034297812143121190642369759388314386825216`31.90917954038201*^48 -
  2.1144392137191221020101719542599757567807700598784`31.90917954038201*^49
  Sin[ $\beta$ ]^2) #1^4 - 3.505693241456970528989025`31.90917954038201*^24 #1^5 +
  5.88157727416637492704831340544`31.90917954038201*^31 #1^6 &,
  1], { $\beta$ , -2  $\pi$ , 2  $\pi$ }, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

```



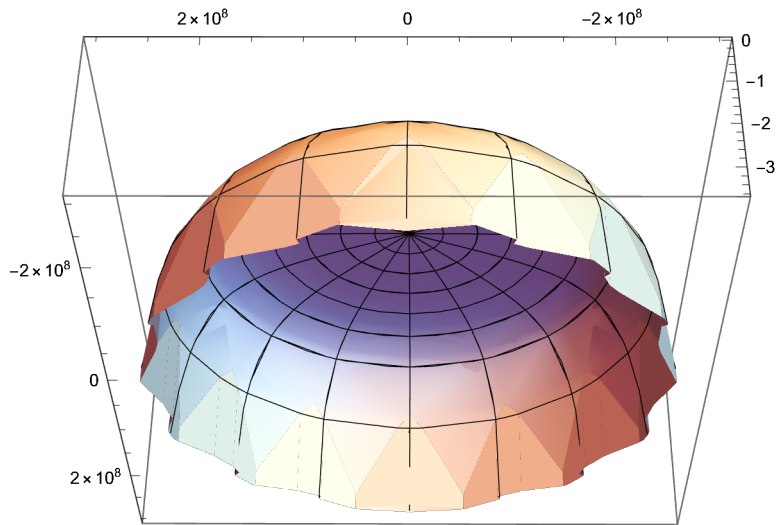
$$\beta = \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]$$

$v = u = \text{Relativistic sorts}$

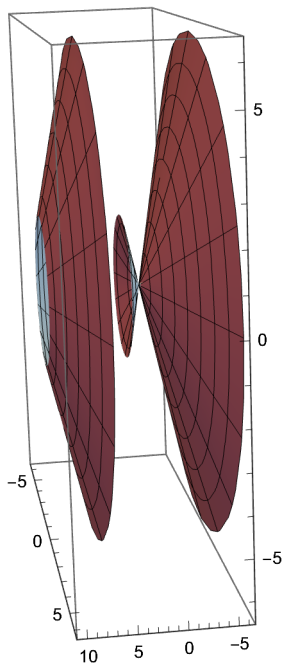
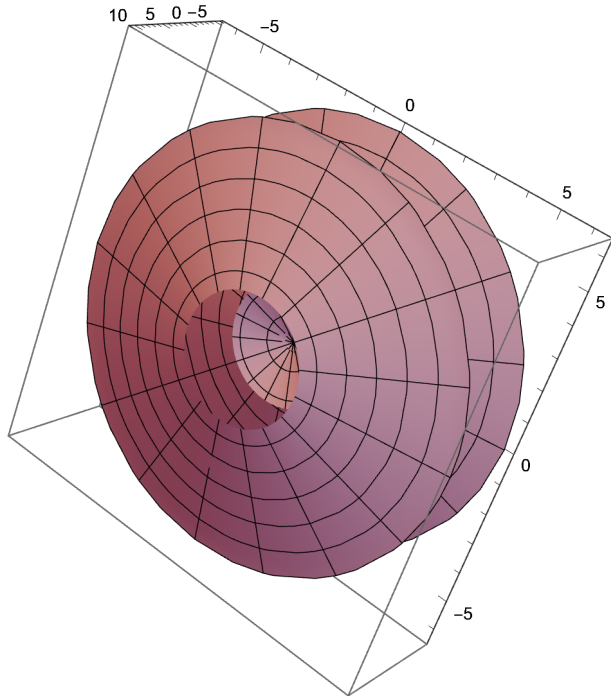
$$\begin{aligned}
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - \right. \right. \right. \\
& \quad \left. \left. \left. 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{ 39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 } \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - 1.1294090667581471 \cdot r^2 \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot r^2 \theta^2 \right) \right) \right\} / \\
& \quad \left( \sqrt{ 39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 } \right) \Big\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right) \right\} / \\
& \quad \left( \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \right) \Big\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \sqrt{ - \frac{ 4 c^2 \pi r^2 }{ -4 \pi r^2 + r^2 \theta } + \frac{ c^2 r^2 \theta }{ -4 \pi r^2 + r^2 \theta } - \frac{ \sqrt{ c^6 r^2 (4 \pi - \theta) \theta } }{ -4 \pi r^2 + r^2 \theta } } \right\}, \right. \\
& \left\{ v \rightarrow \sqrt{ - \frac{ 4 c^2 \pi r^2 }{ -4 \pi r^2 + r^2 \theta } + \frac{ c^2 r^2 \theta }{ -4 \pi r^2 + r^2 \theta } - \frac{ \sqrt{ c^6 r^2 (4 \pi - \theta) \theta } }{ -4 \pi r^2 + r^2 \theta } } \right\}, \\
& \left\{ v \rightarrow - \sqrt{ - \frac{ 4 c^2 \pi r^2 }{ -4 \pi r^2 + r^2 \theta } + \frac{ c^2 r^2 \theta }{ -4 \pi r^2 + r^2 \theta } + \frac{ \sqrt{ 4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2 } }{ -4 \pi r^2 + r^2 \theta } } \right\}, \\
& \left\{ v \rightarrow \sqrt{ - \frac{ 4 c^2 \pi r^2 }{ -4 \pi r^2 + r^2 \theta } + \frac{ c^2 r^2 \theta }{ -4 \pi r^2 + r^2 \theta } + \frac{ \sqrt{ 4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2 } }{ -4 \pi r^2 + r^2 \theta } } \right\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{ 39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot \theta + \theta^2 } \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - 1.1294090667581471 \cdot \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot \theta^2 \right) \right) \right\} / \\
& \quad \left( \sqrt{ 39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot \theta + \theta^2 } \right) \Big\} \Big\}
\end{aligned}$$

$$u = v = 0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot 10^{23} \theta - 1.863986866980889 \cdot 10^{22} \theta^2 + (0. \cdot 1.863986866980889 \cdot 10^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 \cdot \theta - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)}$$

$$\text{RevolutionPlot3D}\left[\frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2}, \{u, -2.99792458 \cdot 10^8, (2.99792458 \cdot 10^8)\}\right]$$



$$\begin{aligned}
& \text{RevolutionPlot3D}\left[1/\left(c^4 - c^2\right.\right. \\
& \quad \left.\left(-0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - 1.863986866980889 \theta^{22} \right.\right.\right. \\
& \quad \left.\left.\left.\theta^2 + (\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^2\right) \\
& \quad \pi \left(2 c^4 - 2 c^2 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right. \\
& \quad \left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right. \\
& \quad \left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^2 - \right. \\
& \quad \sqrt{\left(4 c^8 - 8 c^6 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right. \\
& \quad \left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right. \\
& \quad \left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^2 + \right. \\
& \quad \left.5 c^4 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right. \\
& \quad \left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right. \\
& \quad \left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^4 - \right. \\
& \quad \left.c^2 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right. \\
& \quad \left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right. \\
& \quad \left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^6\right)\right), \\
& \quad \{\theta, -2 \pi, 2 \pi\}]
\end{aligned}$$

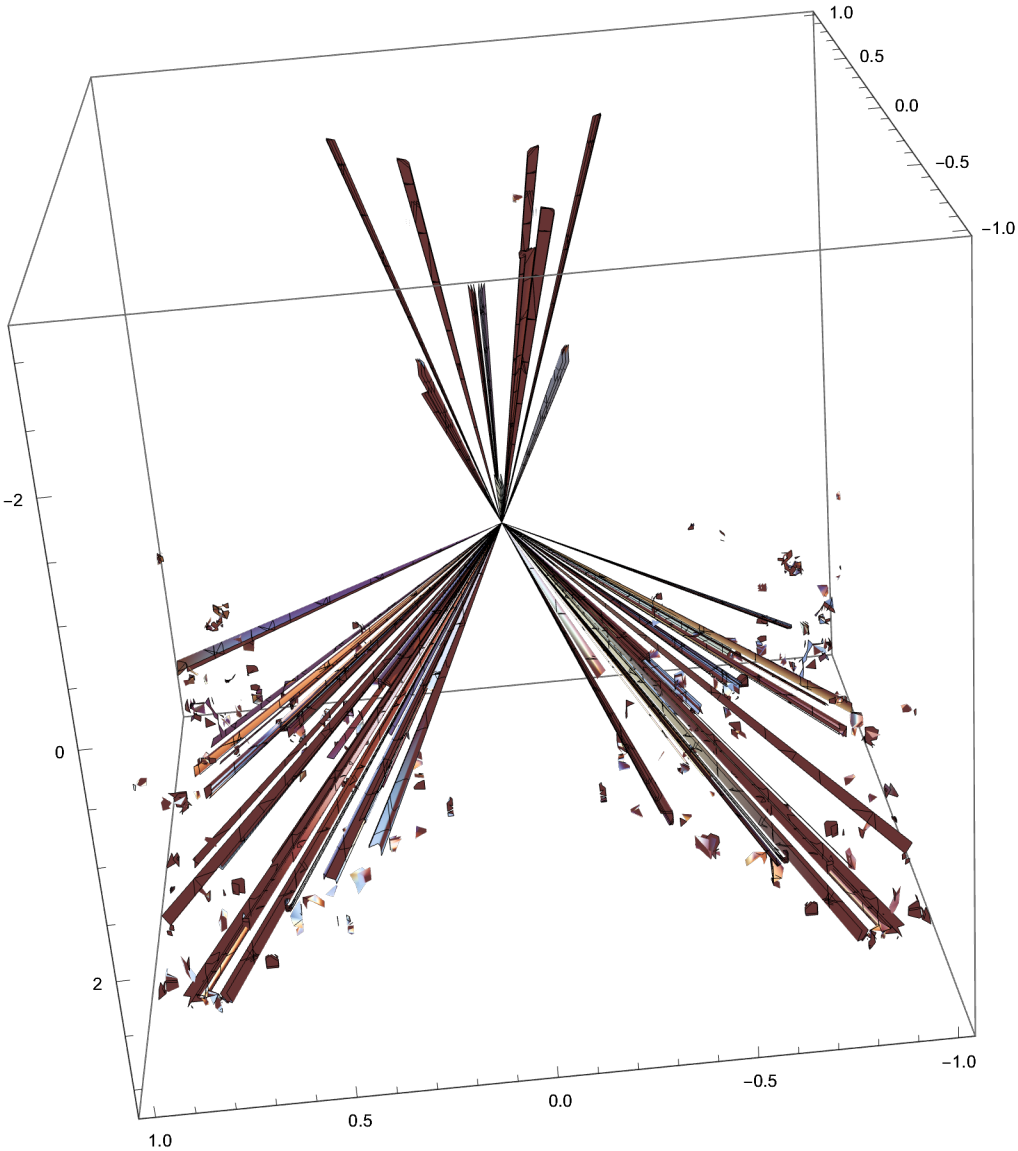


$\text{RevolutionPlot3D}\left[\frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2},\right.$   
 $\left.\{u, -2.99792458 * 10^8, (2.99792458 * 10^8)\}\right]$

```

ContourPlot3D[
  1 / (c^4 - c^2 (- (1. ` Sqrt (3.5481432270250993 ` ^18 η^2 - 1.1294090667581471 ` ^18 r^2 θ +
    8.987551787368176 ` ^16 r^2 θ^2))) /
    (Sqrt (39.47841760435743 ` η^2 - 12.566370614359172 ` r^2 θ + r^2 θ^2)))^2) π
  (2 c^4 - 2 c^2 (- (1. ` Sqrt (3.5481432270250993 ` ^18 η^2 - 1.1294090667581471 ` ^18
    r^2 θ + 8.987551787368176 ` ^16 r^2 θ^2))) /
    (Sqrt (39.47841760435743 ` η^2 - 12.566370614359172 ` r^2 θ + r^2 θ^2)))^2 -
  Sqrt (4 c^8 - 8 c^6 (- (1. ` Sqrt (3.5481432270250993 ` ^18 η^2 - 1.1294090667581471 ` ^18
    r^2 θ + 8.987551787368176 ` ^16 r^2 θ^2))) /
    (Sqrt (39.47841760435743 ` η^2 - 12.566370614359172 ` r^2 θ + r^2 θ^2)))^2 +
  5 c^4 (- (1. ` Sqrt (3.5481432270250993 ` ^18 η^2 - 1.1294090667581471 ` ^18
    r^2 θ + 8.987551787368176 ` ^16 r^2 θ^2))) /
    (Sqrt (39.47841760435743 ` η^2 - 12.566370614359172 ` r^2 θ + r^2 θ^2)))^4 -
  c^2 (- (1. ` Sqrt (3.5481432270250993 ` ^18 η^2 - 1.1294090667581471 ` ^18
    r^2 θ + 8.987551787368176 ` ^16 r^2 θ^2))) /
    (Sqrt (39.47841760435743 ` η^2 - 12.566370614359172 ` r^2 θ +
    r^2 θ^2)))^6) ), {r, -1, 1}, {η, -1, 1}, {θ, -π, π}]

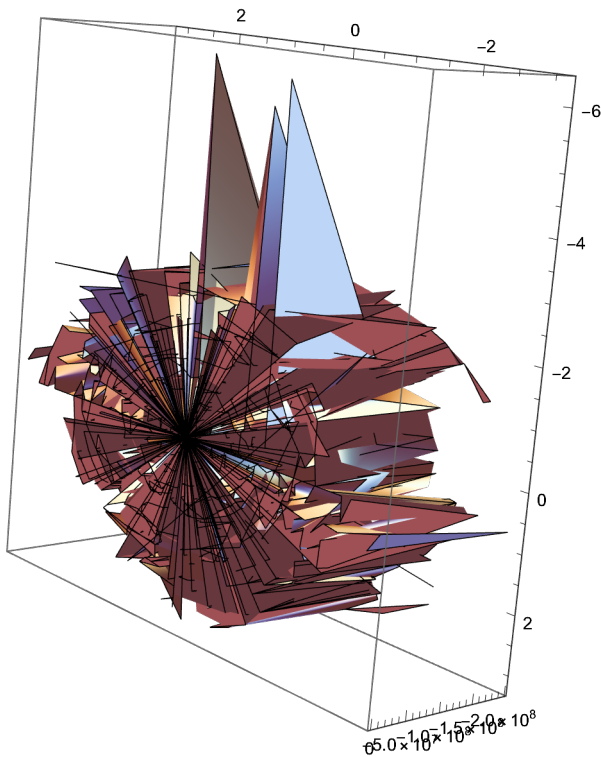
```



```

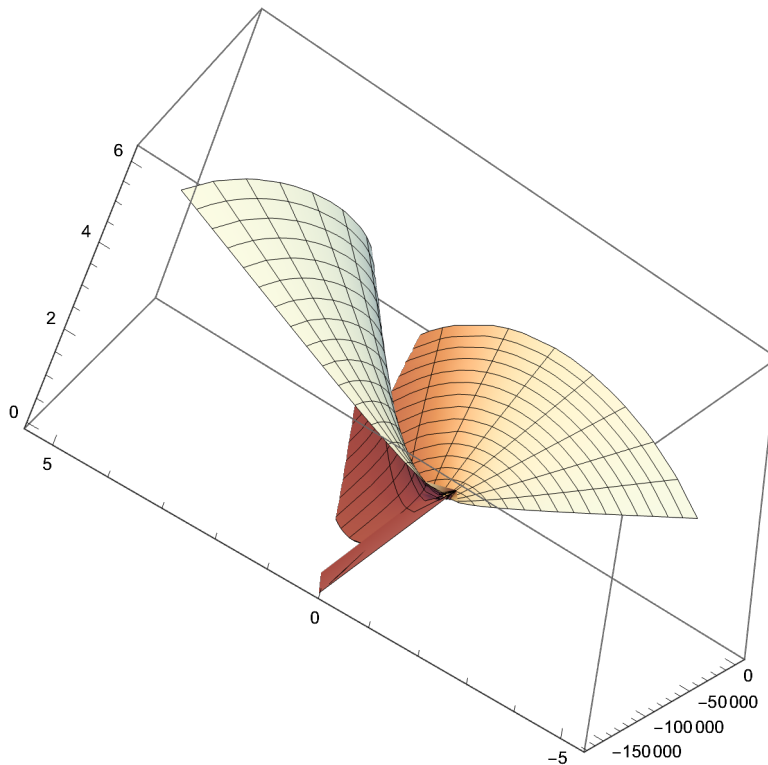
RevolutionPlot3D[
  1 / (c^4 - c^2 ((sqrt(-1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2))) /
    (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)))^2)
  pi (2 c^4 - 2 c^2 ((sqrt(-1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2))) /
    (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)))^2 -
    sqrt(4 c^8 - 8 c^6 ((sqrt(-1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2))) /
    (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)))^2 +
    5 c^4 ((sqrt(-1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2))) /
    (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)))^4 -
    c^2 ((sqrt(-1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2))) / (sqrt(-12.566370614359172` theta +
    theta^2 + 39.47841760435743` Sin[beta]^2)))^6), {beta, -pi, pi}, {theta, -2 pi, 2 pi}]

```





$$\text{RevolutionPlot3D}\left[\frac{1}{c^4 - c^2 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^2}, \right. \\ \pi \left( 2c^4 - 2c^2 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^2 - \right. \\ \left. \sqrt{\left( 4c^8 - 8c^6 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^2 + \right. \right. \\ \left. \left. 5c^4 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^4 - \right. \right. \\ \left. \left. c^2 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^6 \right) \right), \\ \{\theta, -2\pi, 2\pi\}, \{r, -1, 1\}]$$



$$\left\{ \left\{ u \rightarrow \right. \right. \\ \left. \left. -0.000494236036686326 \sqrt{2.3423549790780066 * ^{23} \theta - 1.863986866980889 * ^{22} \theta^2 +} \right. \right.$$

$$\begin{aligned}
& \left( (0. + 1.863986866980889 \cdot \eta^{22}) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \right. \\
& \quad \left. \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right) \Bigg\}, \\
& \left\{ u \rightarrow 0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \eta^{23} \theta - 1.863986866980889 \cdot \eta^{22} \right.} \right. \\
& \quad \left. \left. \theta^2 + (0. + 1.863986866980889 \cdot \eta^{22}) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \right. \right. \\
& \quad \left. \left. \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right) \right\} = \\
& \left\{ \left\{ v \rightarrow - \left( 1. \cdot \sqrt{\left( 3.5481432270250993 \cdot \eta^{18} \eta^2 - 1.1294090667581471 \cdot \eta^{18} r^2 \theta + \right.} \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot \eta^{16} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left. \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{\left( 3.5481432270250993 \cdot \eta^{18} \eta^2 - 1.1294090667581471 \cdot \eta^{18} r^2 \theta + \right.} \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot \eta^{16} r^2 \theta^2 \right) \right) / \\
& \quad \left. \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) \right\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \cdot \sqrt{\left( -1.1294090667581471 \cdot \eta^{18} \theta + 8.987551787368176 \cdot \eta^{16} \theta^2 + \right.} \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \eta^{18} \sin[\beta]^2 \right) \right) / \right. \\
& \quad \left. \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{\left( -1.1294090667581471 \cdot \eta^{18} \theta + 8.987551787368176 \cdot \eta^{16} \theta^2 + \right.} \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \eta^{18} \sin[\beta]^2 \right) \right) / \\
& \quad \left. \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \right\} \\
& \left\{ \left\{ v \rightarrow - \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} \right\}, \right. \\
& \left\{ v \rightarrow \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} \right\}, \\
& \left\{ v \rightarrow - \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta}} \right\}, \\
& \left\{ v \rightarrow \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta}} \right\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \cdot \sqrt{\left( 3.5481432270250993 \cdot \eta^{18} - \right.} \right. \right. \\
& \quad \left. \left. 1.1294090667581471 \cdot \eta^{18} \theta + 8.987551787368176 \cdot \eta^{16} \theta^2 \right) \right) / \right. \\
& \quad \left. \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) \right\},
\end{aligned}$$

$$\left\{v \rightarrow \left( \sqrt{\left( 3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \right)} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) \right\}$$

Solve $\left[0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. \cdot + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right)} = \right.$

$$\left. \left( \sqrt{\left( 3.5481432270250993 \cdot \eta^{18} - 1.1294090667581471 \cdot \eta^{18} r^2 + 8.987551787368176 \cdot \eta^{16} r^2 \right)} \right) / \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right), r \right]$$

{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. - 652931. i$ ],  
{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. + 652931. i$ ], {Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow 753946.$ ]}}

Solve $\left[0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. \cdot + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right)} = \right.$

$$\left. \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), \beta \right]$$

{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. - 652931. i$ ],  
{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. + 652931. i$ ], {Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow 753946.$ ]}}

Solve $\left[0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. \cdot + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right)} = \right.$

$$\left. \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), \theta \right]$$

{ $\{\theta \rightarrow -245215. - 424732. i\}$ ,  $\{\theta \rightarrow -245215. + 424732. i\}$ ,  $\{\theta \rightarrow 490443.\}$ }

$$\text{Solve}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)} = \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}, \theta\right]$$

$$\text{Solve}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)} = \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}, r\right]$$

$$\text{Solve}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)} = (\sqrt{(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2)}) / (\sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2}), \theta\right]$$

$$\{\{\theta \rightarrow -245215. - 424732. i\}\}$$

$$c := (2.99792458 \cdot 10^8)$$

$$e^{i \beta} = \cos[\beta] + i \sin[\beta]$$

$$\beta = \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]$$

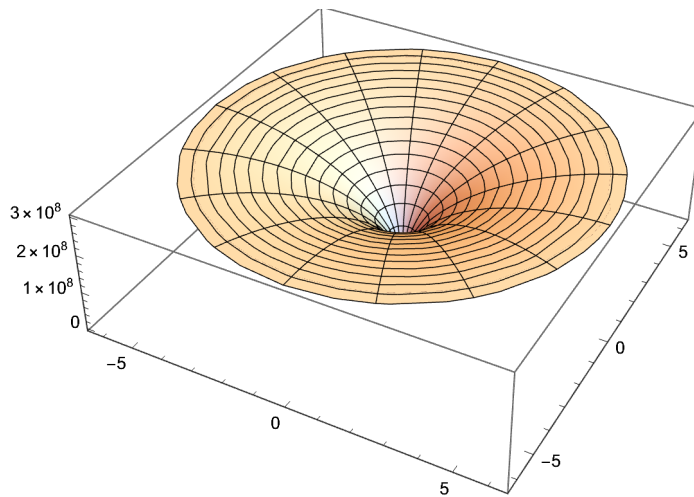
$$e^{i \left(\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right)} = \left(\cos\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right] + i \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]\right)$$

$$e^{i \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]} = \frac{i \sqrt{(4 \pi - \theta) \theta}}{2 \pi} + \sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}$$

$$\text{Solve}\left[\sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}} = \sqrt{1 - \frac{u^2}{c^2}}, u\right]$$

$$\left\{\left\{u \rightarrow -\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}, \left\{u \rightarrow \frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}\right\}$$

RevolutionPlot3D $\left[\frac{\sqrt{4 (2.99792458 * 10^8)^2 \pi \theta - (2.99792458 * 10^8)^2 \theta^2}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}\right]$



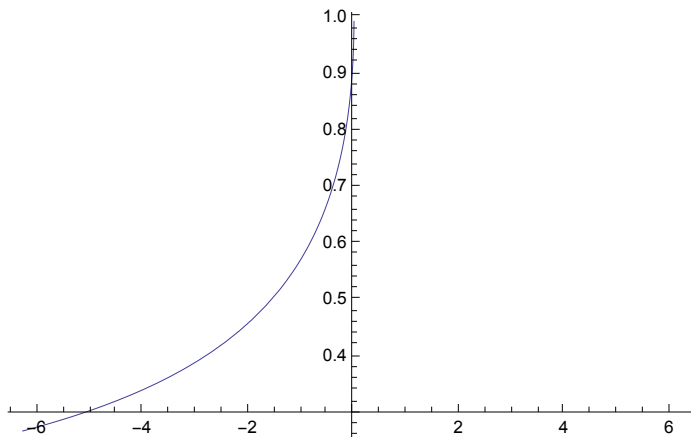
Solve $\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$

{{r -> -c}, {r -> c}}

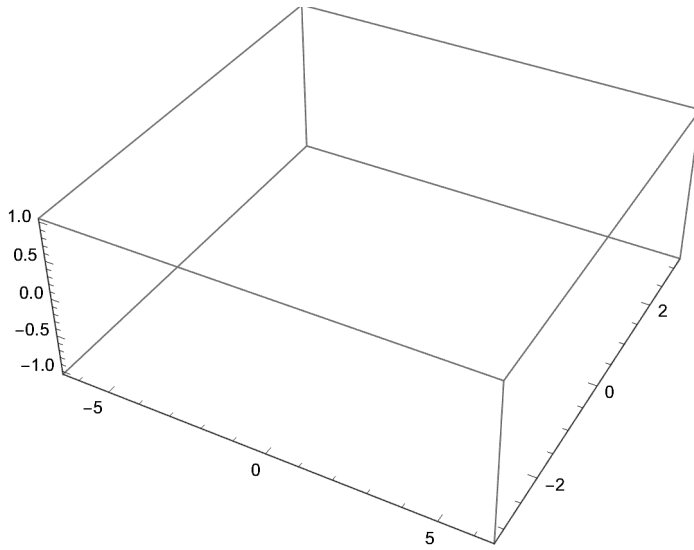
$$e^{\left(i \operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right)} = \left(\cos\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right] + i \sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]\right)$$

$$\theta = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)$$

Plot $\left[e^{i \operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]}, \{\theta, -2 \pi, 2 \pi\}\right]$

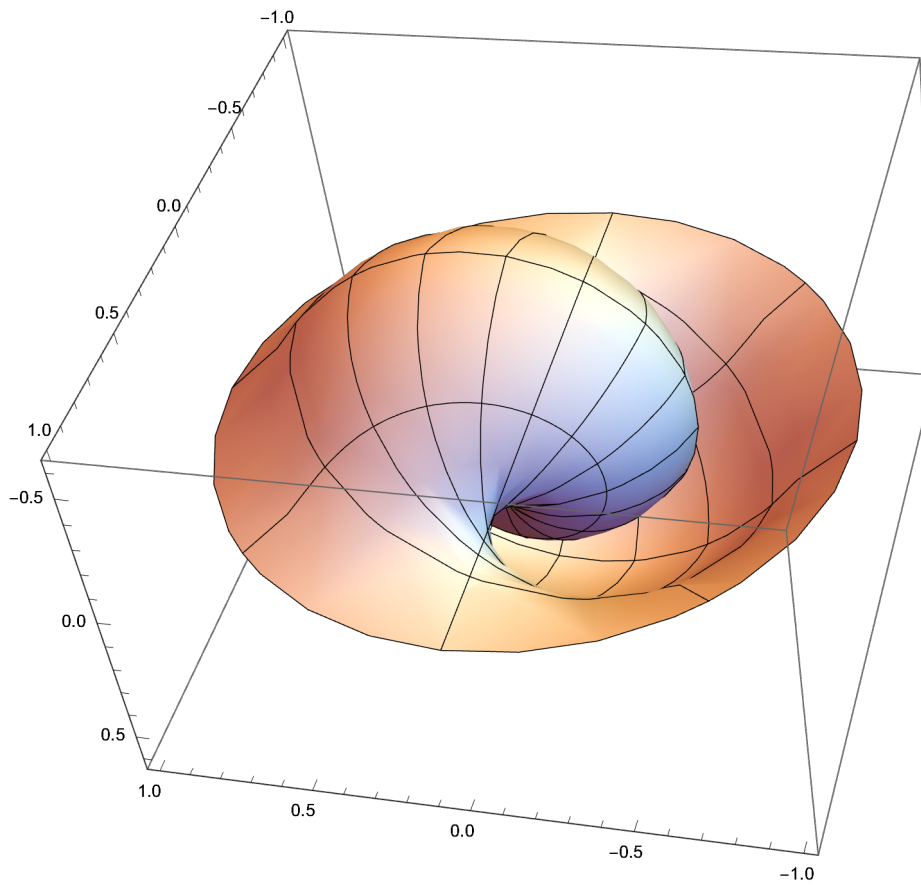


$\text{Plot3D}\left[e^{i \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \left(2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}}{2 \pi}\right]}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$

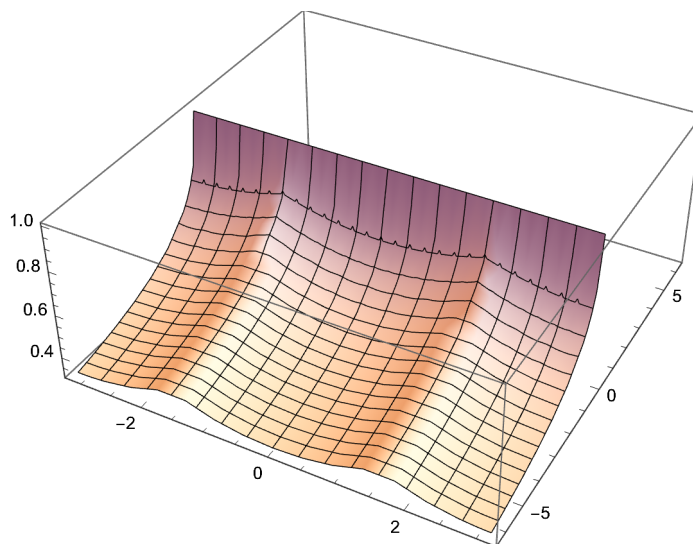


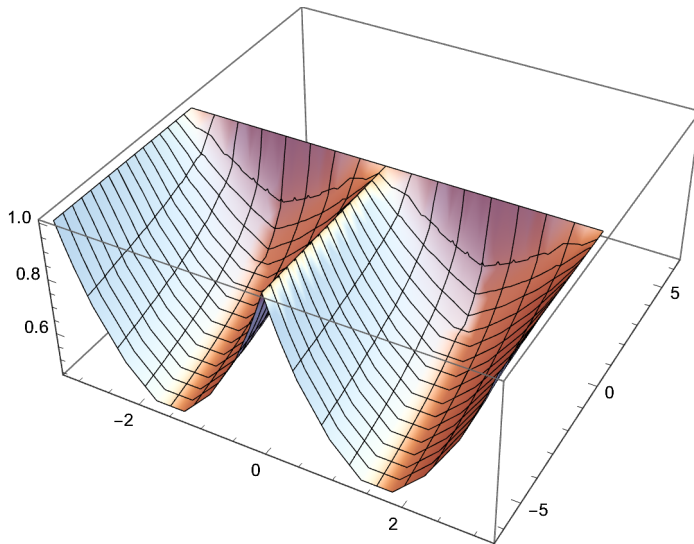
$$e^{i \text{ArcSin}\left[\frac{\sqrt{(4 \pi - 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) \theta}}{2 \pi}\right]} = e^{i \beta}$$

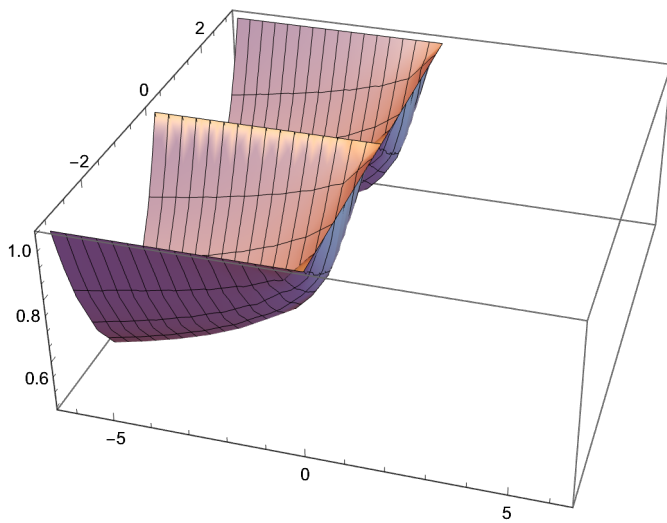
**SphericalPlot3D** $\left[e^{\frac{i \operatorname{ArcSin}\left[\frac{\sqrt{4 \pi-2\left(\pi-\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)}{2 \pi}\right]}{\theta}}\right],\{\beta,-(2) \pi,(2) \pi\},\{\theta,-(2) \pi,(2) \pi\}\right]$



**Plot3D** $\left[e^{\frac{i \operatorname{ArcSin}\left[\frac{\sqrt{4 \pi-2\left(\pi-\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)}{2 \pi}\right]}{\theta}}\right],\{\beta,-\pi,\pi\},\{\theta,-2 \pi,2 \pi\}\right]$

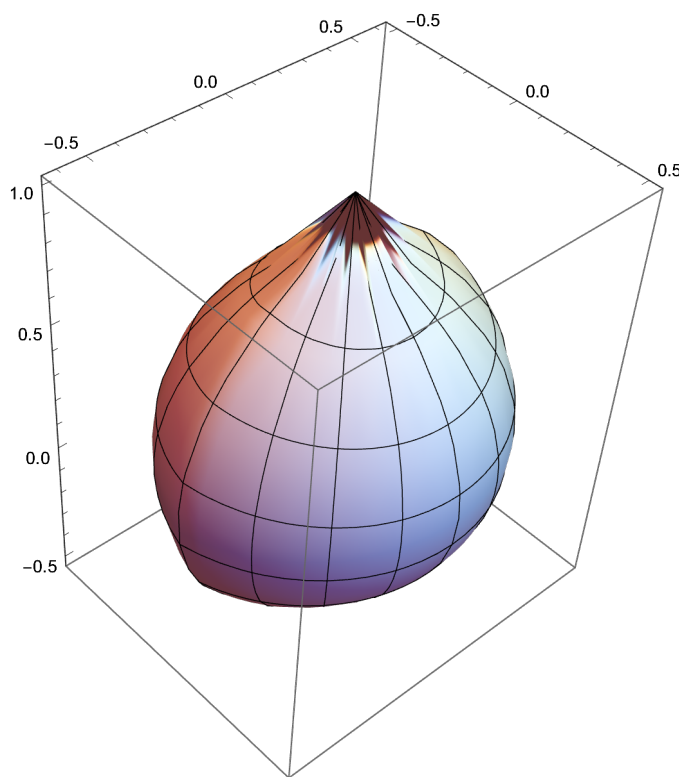


$$\text{Plot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)}{\theta}\right] \theta}{2\pi}}\right], \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$$


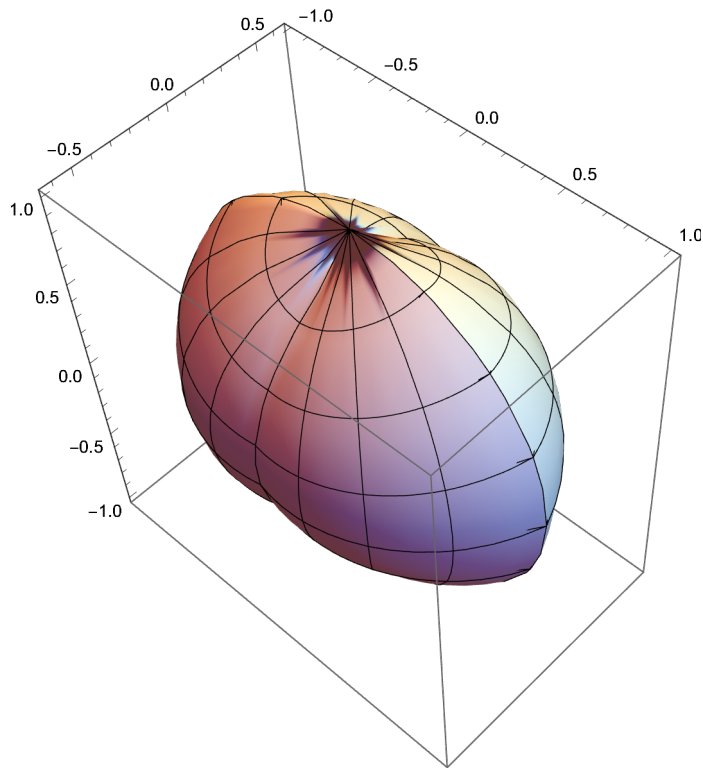
$$\text{Plot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)}{\theta}\right] \theta}{2\pi}}\right], \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}\right]$$




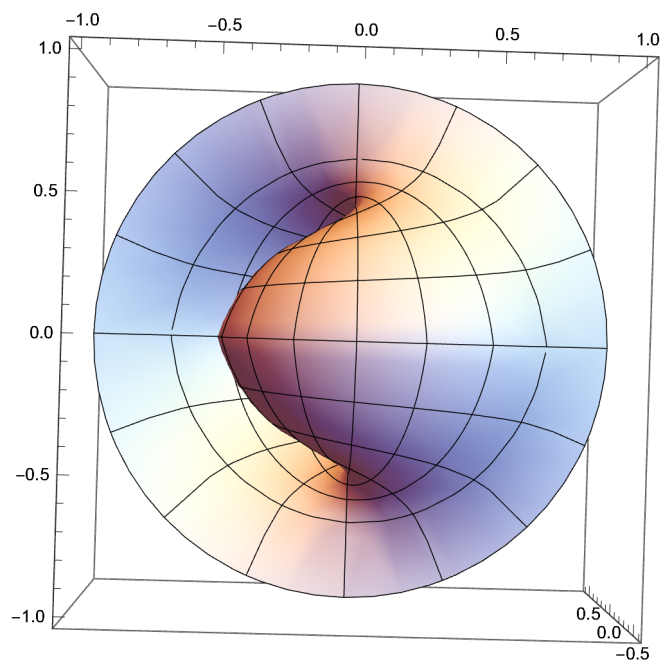
`SphericalPlot3D` $\left[e^{\frac{i \operatorname{ArcSin}\left[\frac{\sqrt{4 \pi-2\left(\pi-\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)}{2 \pi}\right]}{\theta}}\right],\left\{\theta,-2 \pi, 2 \pi\right\},\left\{\beta,-\pi, \pi\right\}\right]$



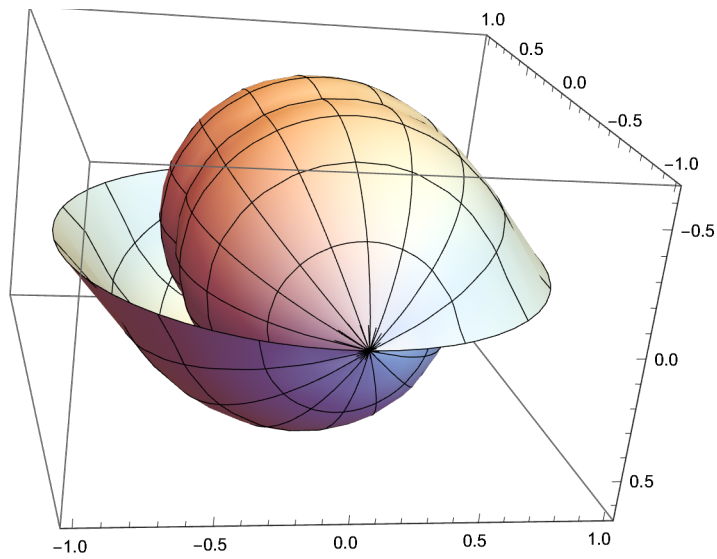
$\text{SphericalPlot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}{2\pi}\right]}{\theta}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}\right]$



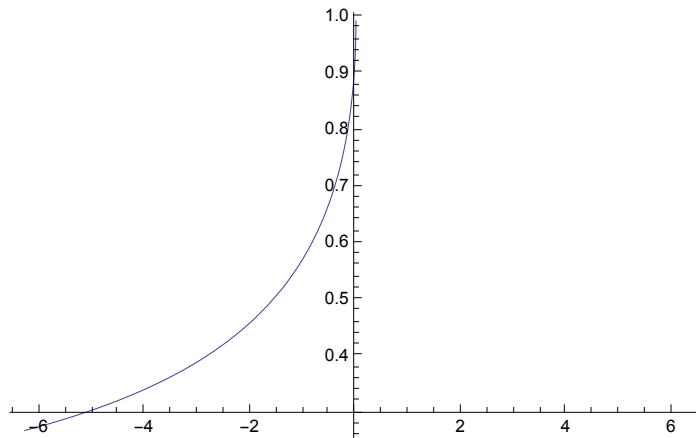
$\text{SphericalPlot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{4\pi-2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}{2\pi}\right]}{\theta}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$



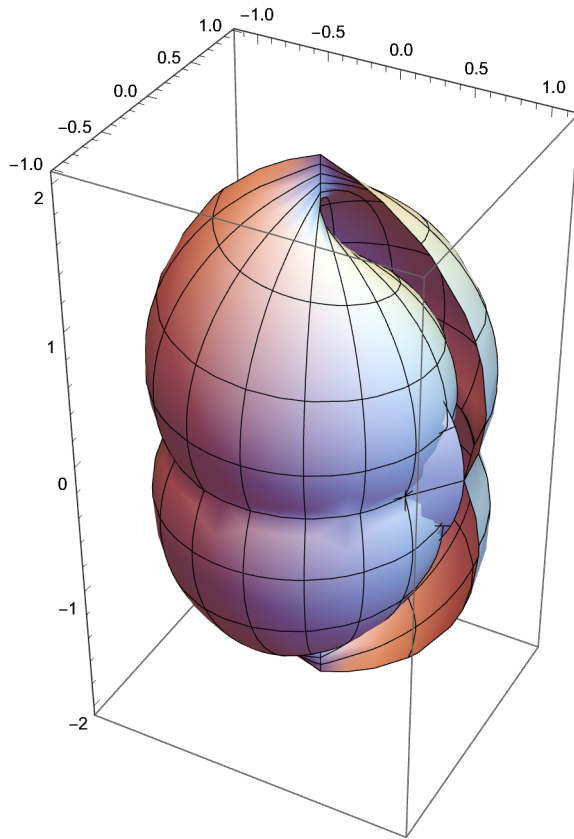
$\text{SphericalPlot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}{\theta}\right]}{2\pi}}\right], \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$



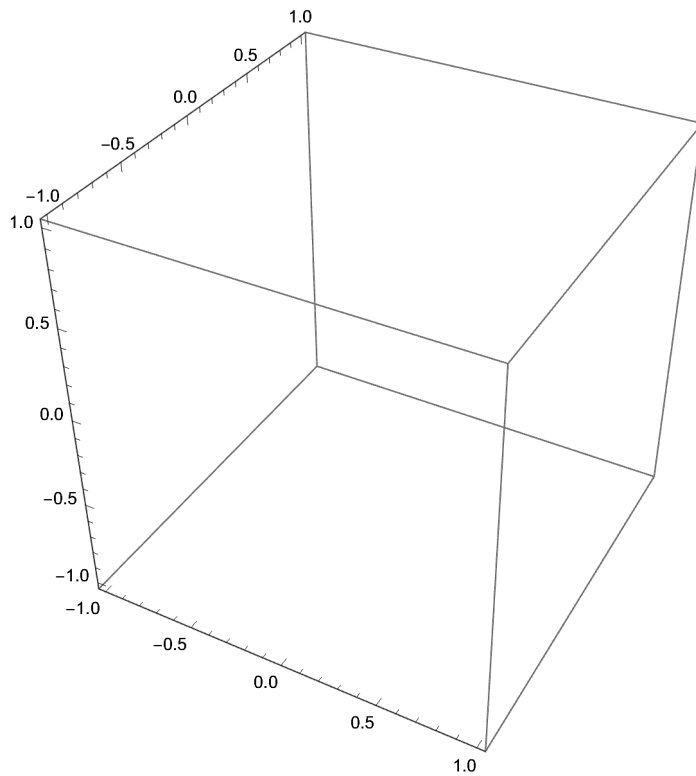
$\text{Plot}\left[\frac{i \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi-\theta)\theta}{4\pi^2}}, \{\theta, -2\pi, 2\pi\}\right]$



$\text{SphericalPlot3D}\left[\frac{i \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) \theta}}{2 \pi} + \sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}, \right.$   
 $\left. \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$

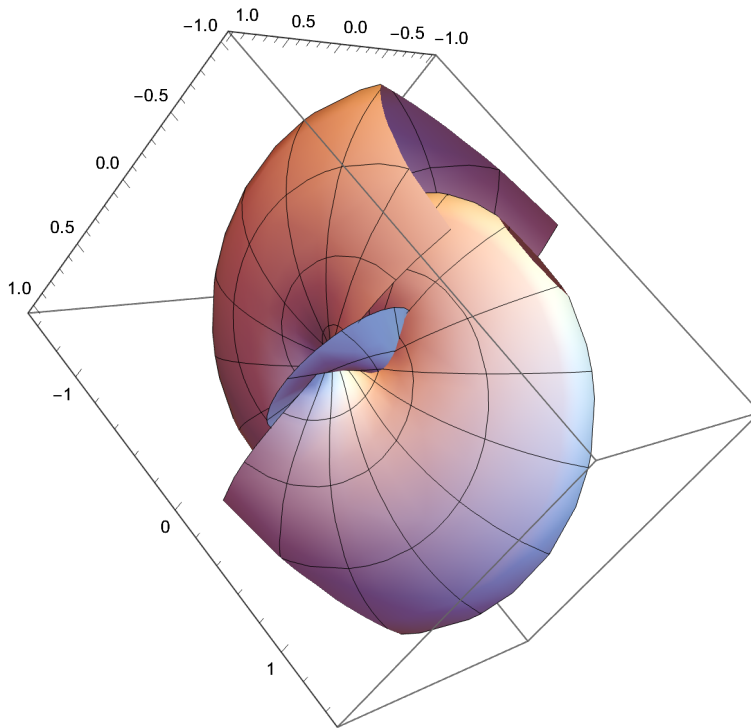


$$\text{SphericalPlot3D}\left[\frac{i \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}{2 \pi} + \sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



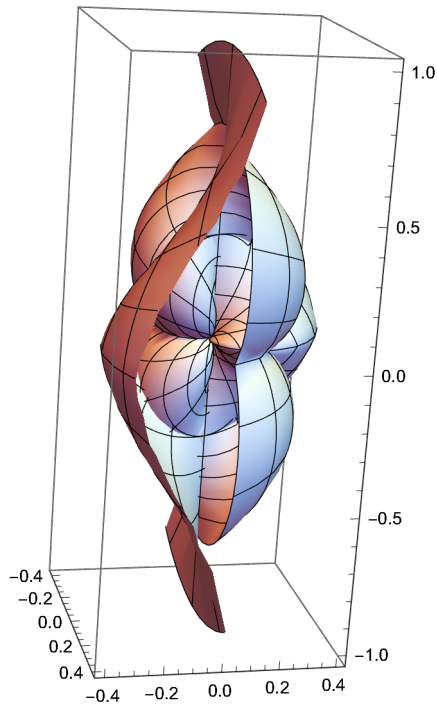
SphericalPlot3D[  

$$\frac{i \sqrt{(4\pi - \theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{4\pi^2}},$$
  
 $\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$

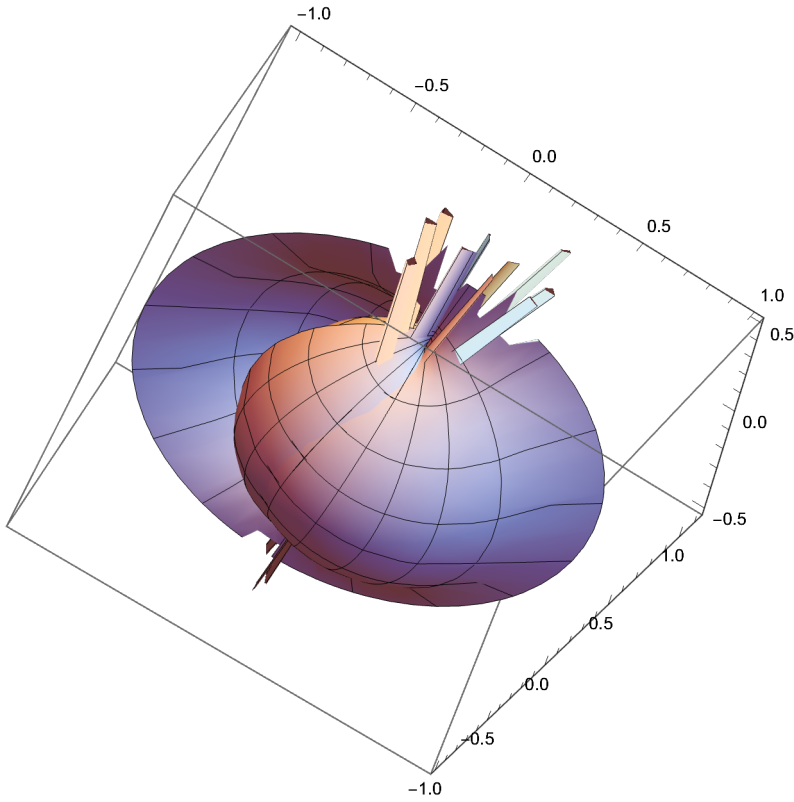


SphericalPlot3D[  

$$\frac{i \sqrt{(4\pi - \theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))\theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



$$\text{SphericalPlot3D}\left[\frac{1}{2\pi} \pm \sqrt{\left(\left(4\pi - \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right.}\right. \\
\left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
\left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) \theta) + \\
\left. \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, \right. \\
\left. 2\pi\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{1}{2\pi} \pm \sqrt{\left(\left(4\pi - \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right.}\right. \\
\left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
\left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) \theta) + \\
\left. \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, \right. \\
\left. 2\pi\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{i \sqrt{(4 \pi - \theta) \theta}}{2 \pi} + \sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$$

$$\beta = \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]$$

$$e^{\left(i \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right)} =$$

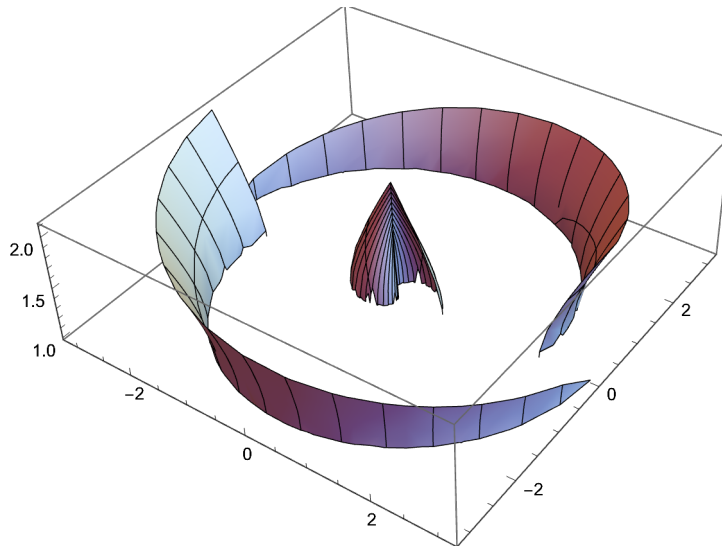
$$\left(\text{Cos}\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right] + i \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right]\right)$$

$$e^{i \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]} = \frac{i \sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} + \sqrt{1 - \frac{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}{4 \pi^2 (-4 \pi + \theta)}}$$

$$\text{RevolutionPlot3D}\left[$$

$$e^{i \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \left(\frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \text{Sin}[\beta]^2}{6 \left(-\pi^2 + 18 \pi^2 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)^3}}{2 \pi \sqrt{-4 \pi + \theta}}}\right]},$$

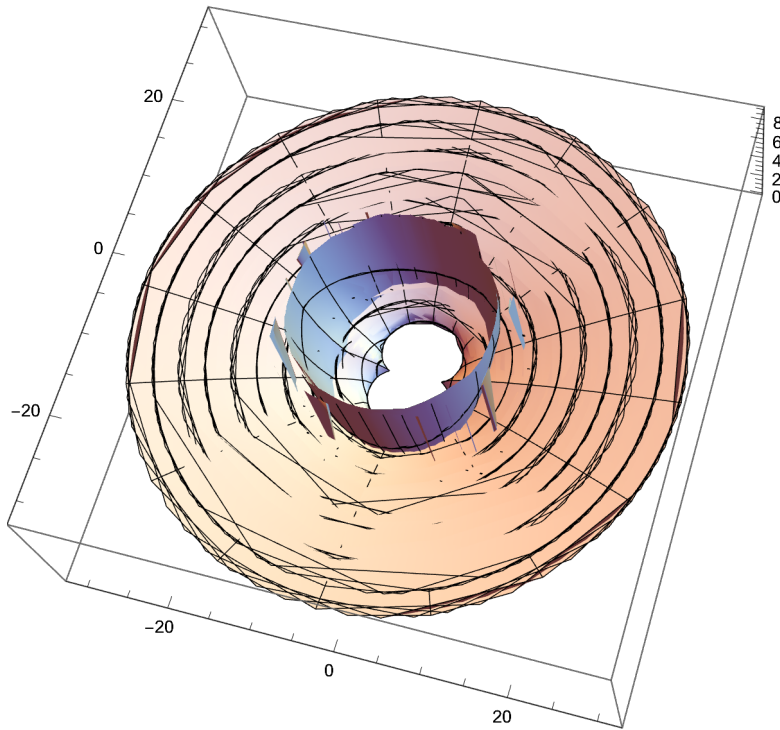
$$\{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}]$$



RevolutionPlot3D[

$$e^{i \operatorname{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \left(\frac{4 \pi}{3} \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)}}{2 \pi \sqrt{-4 \pi + 6}}}\right]},$$

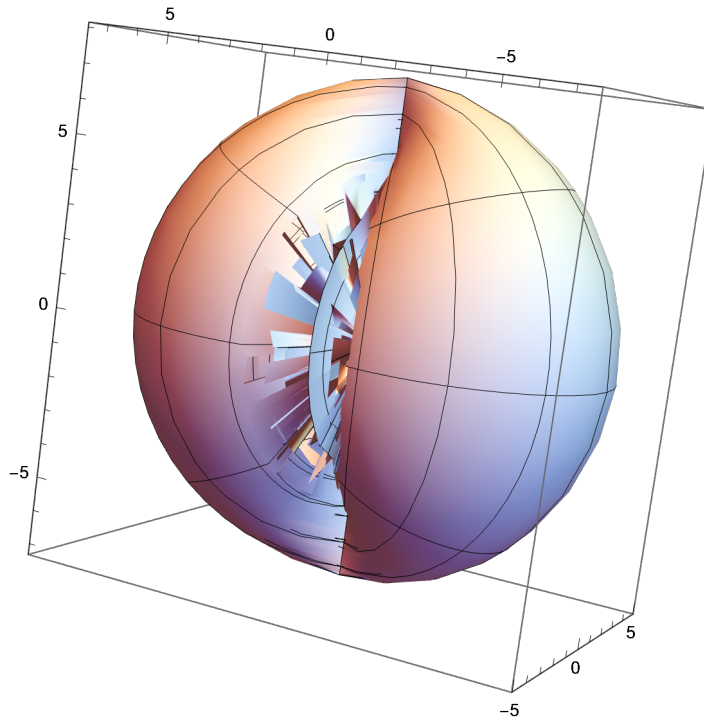
{ $\theta$ , -10  $\pi$ , 10  $\pi$ }, { $\beta$ , -5  $\pi$ , 5  $\pi$ }]



SphericalPlot3D[

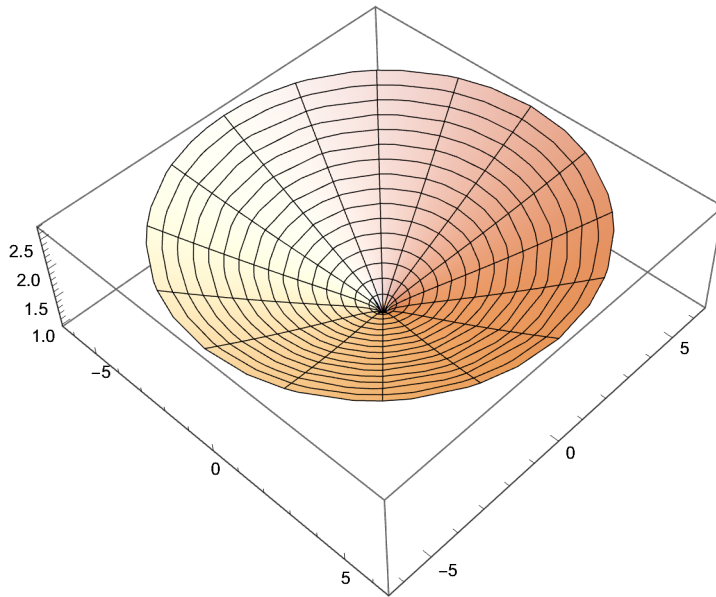
$$\frac{\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi}\left(\frac{4\pi}{3}-\frac{-4\pi^2+12\pi^2\sin[\beta]^2}{6(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6})^{1/3}}+\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2}{-2\pi\sqrt{-4\pi+\frac{4\pi}{3}\left(\frac{4\pi}{3}-\frac{-4\pi^2+12\pi^2\sin[\beta]^2}{6(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6})^{1/3}}+\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2}}\right]}{e},$$

{θ, -2 π, 2 π}, {β, -π, π}]

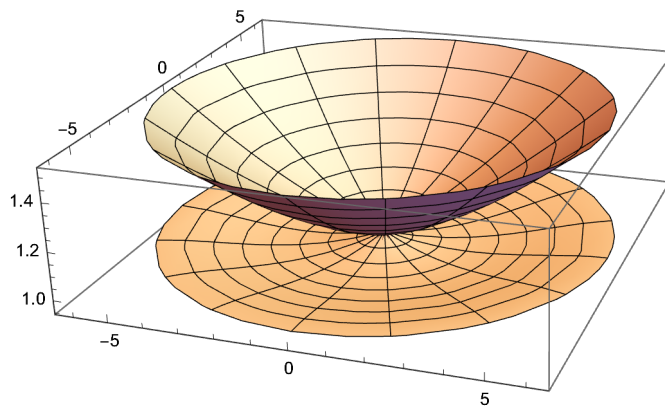


$$\text{RevolutionPlot3D}\left[\frac{\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi\theta^2-\theta^3}}{2\pi\sqrt{-4\pi+\theta}}\right]}{1-\frac{-4\pi^2\theta+4\pi\theta^2-\theta^3}{4\pi^2(-4\pi+\theta)}}, \{\theta, -2\pi, 2\pi\}\right]$$

$$\text{RevolutionPlot3D}\left[\frac{\mathbf{i} \sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} + \sqrt{1 - \frac{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}{4 \pi^2 (-4 \pi + \theta)}}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\sqrt{1 - \frac{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}{4 \pi^2 (-4 \pi + \theta)}}, \{\theta, -2 \pi, 2 \pi\}\right]$$

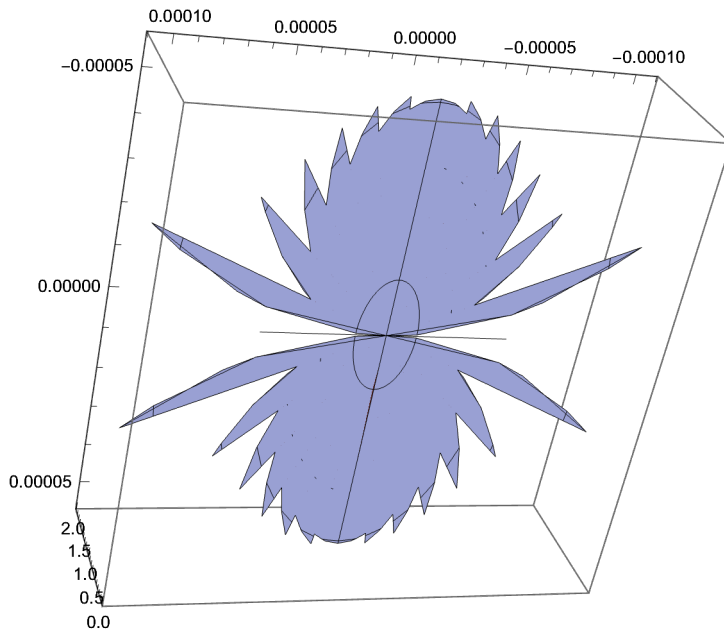


$$e^{\mathbf{i} \theta} = \cos[\theta] + \mathbf{i} \sin[\theta]$$

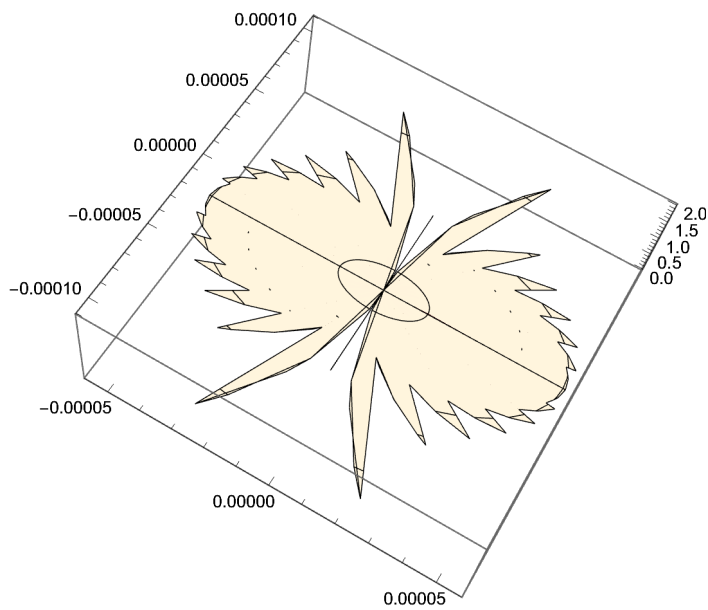
$$\theta \rightarrow \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}$$

$$\theta = 2 \left( \pi \pm \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

`RevolutionPlot3D[E^I (2 (π + √(π² - π² Sin[β]²))), {β, -π, π}]`



`RevolutionPlot3D[E^I (2 (π - √(π² - π² Sin[β]²))), {β, -π, π}]`



# A Unifying Theory

Parker Emmerson and Andrew Berisha

$$c = 3.0 \times 10^8 \text{ m / s}$$

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle,  
the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + h^2$$

This is the initial radius squared expressed as the slant of  
the cone in terms of the height of the cone,  $h$ , and the radius  
of the base of the cone,  $r_1$

$$r = \sqrt{(r_1^2 + h^2)} \quad (4)$$

$$t = \theta r$$

$$t / \theta = r$$

The arc length taken out of a circle at a given time is =

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \quad \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - h^2$$

$$r_1 = \sqrt{(r^2 - h^2)}$$

$$h \leq r$$

$$\tau = \text{time}$$

$$1 \text{ second} = 6 \text{ degrees}$$

$$\pi r^2 = \text{Area} = h^2$$

To construct a square of the same area as a given circle, we will begin with the postulates above regarding the geometry of a cone.

When, "relationship is added to non relational stimuli" (Perception, MacLeod and Pick for Gibson, 24), illusion is able to be understood through phenomenology. We can use mathematics like a language for discussing its structural elements.

The derivative of zero is equal to the derivative of an equation that is equal to 0.

$$\text{Solve}[r_1^2 + h^2 = r^2, h]$$

$$\left\{ \left\{ h \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ h \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\} \quad (5)$$

$$(t / \theta) = r$$

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = 2 \pi (t / \theta) - 2 \pi \sqrt{((t / \theta)^2 - h^2)}$$

$$t = 2 \pi (t / \theta) - 2 \pi \sqrt{((t / \theta)^2 - h^2)}$$

Add  $2\pi\sqrt{((r)^2 - h^2)}$  to both sides

$$t + 2\pi\sqrt{((t/\theta)^2 - h^2)} = 2\pi(t/\theta)$$

Subtract t from both sides and remember that  $(t/\theta) = r$

$$2\pi\sqrt{((t/\theta)^2 - (h^2))} = 2\pi(t/\theta) - t = 2\pi r - t$$

Divide by  $2\pi$  on both sides.

$$(t/\theta) - t/(2\pi) = (r) - t/(2\pi) = \sqrt{((t/\theta)^2 - (h^2))} = \sqrt{((r)^2 - (h^2))} = r_1$$

Square both sides. Substitute :  $(t/\theta) = r$

$$((t/\theta) - (t/(2\pi)))^2 = ((r) - (t/(2\pi)))^2 = ((t/\theta)^2 - (h^2)) = (r_1^2)$$

$$((r) - (t/(2\pi)))^2 = ((r)^2 - (h^2))$$

Add  $h^2$  to both sides.

$$((r) - (t/(2\pi)))^2 + (h^2) = (r)^2$$

Substitute :  $\theta r = t$

$$((t/\theta) - (t/(2\pi)))^2 = ((r) - (\theta * r/(2\pi)))^2$$

$$((r) - (\theta * r/(2\pi)))^2$$

$$\left(r - \frac{r\theta}{2\pi}\right)^2$$

$$\text{Expand}\left[\left(r - \frac{r\theta}{2\pi}\right)^2\right]$$

$$r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}$$

$$r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2} + h^2 = ((r) - (t/2\pi))^2 + (h^2) = r^2$$

$$(r^2) - \left(r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}\right) = h^2$$

$$\text{Simplify}\left[(r^2) - \left(r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}\right)\right]$$

$$\frac{r^2(4\pi - \theta)\theta}{4\pi^2} = h^2$$

(6)

$$\frac{2h\pi}{\sqrt{4\pi\theta - \theta^2}} = r$$

(7)

$$\frac{2(r/6\theta)(6\theta)\pi}{\sqrt{4\pi\theta - \theta^2}} = r = \frac{2r\pi}{\sqrt{4\pi\theta - \theta^2}}$$

(8)

$$1 = \frac{2\pi}{\sqrt{4\pi\theta - \theta^2}}$$

This is the equation for  $r_1$  in terms of the geometric parameters of the cone described above.

$$\pi (r^2 - h^2) = \pi r_1^2$$

Then, we substitute for the solved height in terms of purely theta and radius.

Done just with

$$\begin{aligned} & \text{Solve}\left[\pi \left(r^2 - \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)\right) = \pi \left(r^2 - \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)\right)^2, r\right] \\ & \left\{ \{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{ r \rightarrow -\frac{2\pi \sqrt{4\pi^2 - 4\pi\theta + \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\}, \right. \\ & \left. \left\{ r \rightarrow \frac{2\pi \sqrt{4\pi^2 - 4\pi\theta + \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \right\} \end{aligned} \quad (9)$$

Remember when we said that  $\pi (r^2 - h^2) = \pi r_1^2$ .

When is the area of  $h^2$  equal to the area of the circle of  $r_1$ ?

$$\text{Well, what if } h^2 = \pi r_1^2 = \pi \left(r^2 - \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)\right)$$

$$\pi r_1^2 = \pi \left(r^2 - \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)\right)^2 = \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)$$

$$\begin{aligned} & \text{Solve}\left[\pi \left(r^2 - \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)\right)^2 = \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right), r\right] \\ & \left\{ \{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{ r \rightarrow -\frac{2\sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\}, \right. \\ & \left. \left\{ r \rightarrow \frac{2\sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \right\} \end{aligned} \quad (10)$$

We will now elaborate on the nature of  $r_1$  in terms of constant rate, and then come back to the equations for  $r$  that we have found through the realization of its parameters and solve them for theta.

$$r_1^2 = \left(r^2 - \left(\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}\right)\right)^2 = r^2 - h^2$$

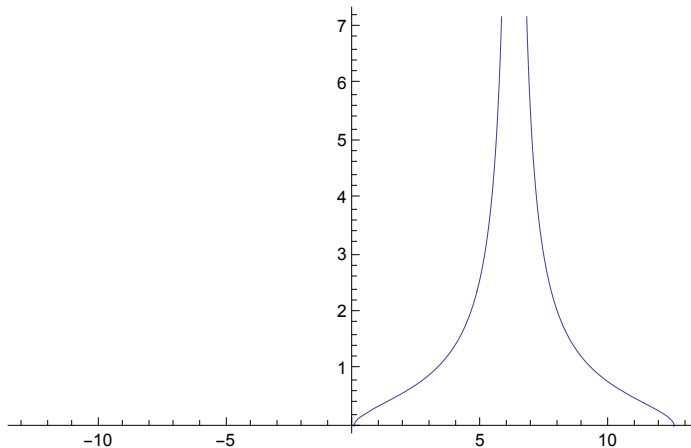


$$\begin{aligned}
 r_1 = \sqrt{(r^2 - h^2)} &= \sqrt{\left( \left( \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 - \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)} = \\
 &\sqrt{\left( \left( \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 - \right. \\
 &\quad \left. \left( \frac{\left( -\frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)} = \\
 &\sqrt{\left( \left( \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 - \right. \\
 &\quad \left. \left( \frac{\left( \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)}
 \end{aligned}$$

Plot[

$$\sqrt{\left( \left( \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 - \left( \frac{\left( -\frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)},$$

{θ, -13, 13}]



We will briefly show what the graph looks like when the speed of light is the constant rate at which  $h$  is traveling, not  $h = c\theta = (r / 6\theta) (6\theta)$ . In that case,  $r$  would equal  $h$ , but what about the fact that  $h$  changes through  $r_1$  (the base of the cone) ? We

will instead propose to say that  $h$  travels not at any rate, but at the speed of light. Of course, it's also possible to theorize and propose that the cone travels up into the third dimension,  $h$ , at a rate equal to the first derivative of the equation for  $r$  in terms of  $\theta$  with respect to  $\theta$ . However, we will now briefly discuss what happens to  $r_1$  when the cone travels

$$\frac{r^2 (4\pi - \theta) \theta}{4\pi^2} = h^2; \quad \frac{2h\pi}{\sqrt{4\pi\theta - \theta^2}} = r$$

$$\text{Simplify}\left[\sqrt{\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}}\right]$$

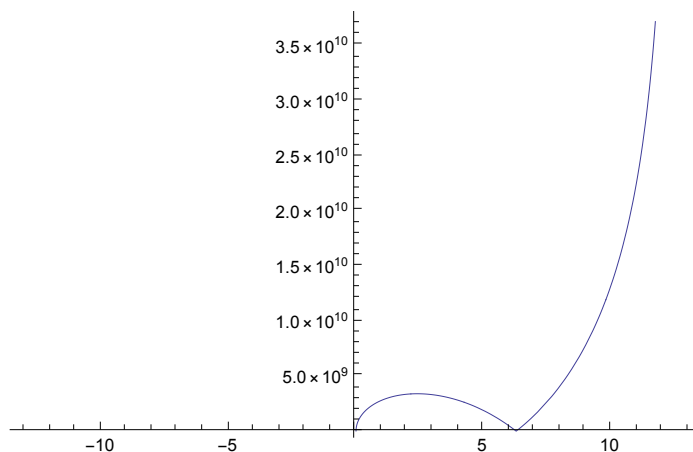
$$\frac{\sqrt{r^2 (4\pi - \theta) \theta}}{2\pi}$$

For light, the equation would read :

$$r_1 = \sqrt{\left(\left(\frac{2(2.99792 \times 10^8)(6)(\theta)\pi}{\sqrt{4\pi\theta - \theta^2}}\right)^2 - \left(\frac{\sqrt{\left(\frac{2(2.99792 \times 10^8)(6)(\theta)\pi}{\sqrt{4\pi\theta - \theta^2}}\right)^2 (4\pi - \theta) \theta}}{2\pi}\right)^2\right)}$$

$$\sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}}$$

$$\text{Plot}\left[\sqrt{\frac{1.2773276589129854 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}}, \{\theta, -13, 13\}\right]$$



This is something much different from the quality of matter whose energetic relation to velocity is defined within its own consistency.

Now we will return to the more general form of the equation. The case when  $h = (r/6\theta)(6\theta)$

Now, by doing the first and second derivatives of the functions for radius in terms of the square of h being equal to the are of the circle of  $r_1$  with respect to time will give us velocity.

$$\left\{ r \rightarrow -\frac{2\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}} \right\}, \left\{ r \rightarrow \frac{2\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}} \right\}$$

$$D\left[-\frac{2\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}, \theta\right] = D[r, \theta]$$

$$D\left[-\frac{2\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}, \theta\right]$$

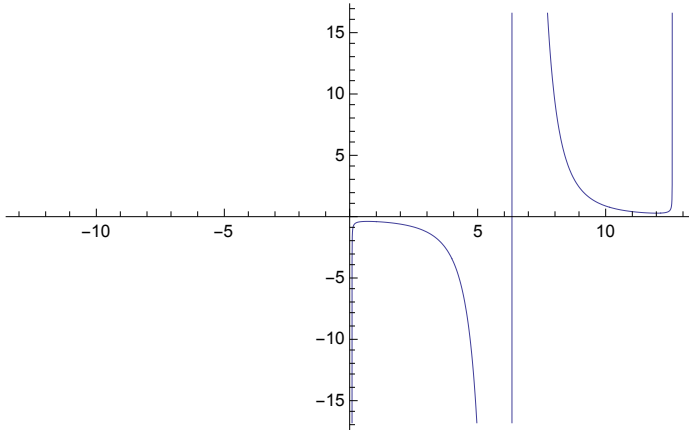
$$\frac{\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3)}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}} -$$

(11)

$$\frac{\sqrt{\pi}(4\pi-2\theta)}{\sqrt{4\pi\theta-\theta^2}\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}$$

$$\text{Plot}\left[\frac{\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3)}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}} -$$

$$\frac{\sqrt{\pi}(4\pi-2\theta)}{\sqrt{4\pi\theta-\theta^2}\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}, \{\theta, -13, 13\}\right]$$



$$D\left[\frac{2\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}, \theta\right] = D[r, \theta]$$

$$D\left[\frac{2\sqrt{\pi}\sqrt{4\pi\theta-\theta^2}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}, \theta\right]$$

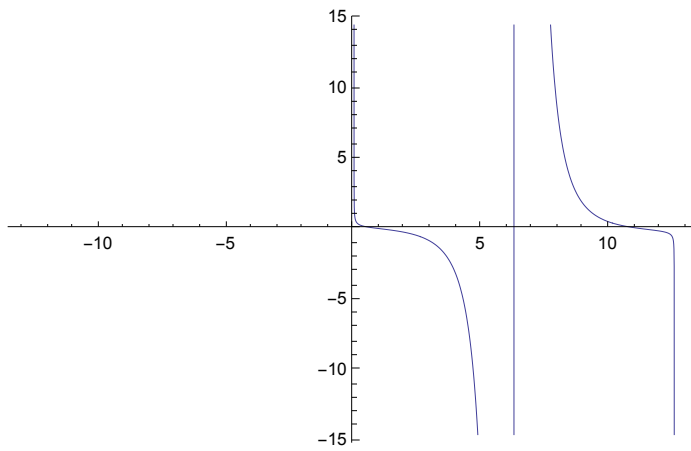
$$- \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} +$$

(11)

$$\frac{\sqrt{\pi} (4\pi - 2\theta)}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}$$

$$\text{Plot} \left[ \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \right.$$

$$\left. \frac{\sqrt{\pi} (4\pi - 2\theta)}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \{\theta, -13, 13\} \right]$$



$$D \left[ \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \right.$$

$$\left. \frac{\sqrt{\pi} (4\pi - 2\theta)}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta \right]$$

$$- \frac{3 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} +$$

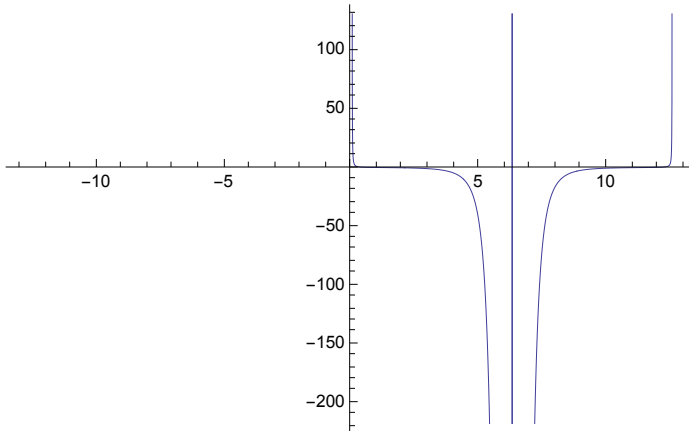
$$\frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} +$$

$$\frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} +$$

$$\frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} +$$

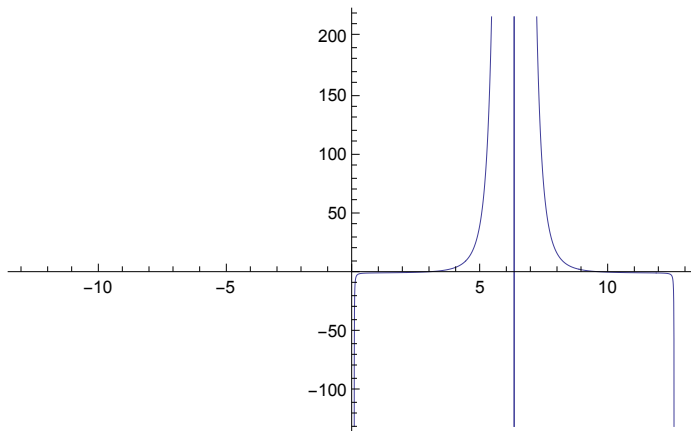
(12)

$$\begin{aligned}
& \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \\
\text{Plot} & \left[ -\frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} + \right. \\
& \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \left. \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} + \right. \\
& \left. \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \{\theta, -13, 13\} \right]
\end{aligned}$$

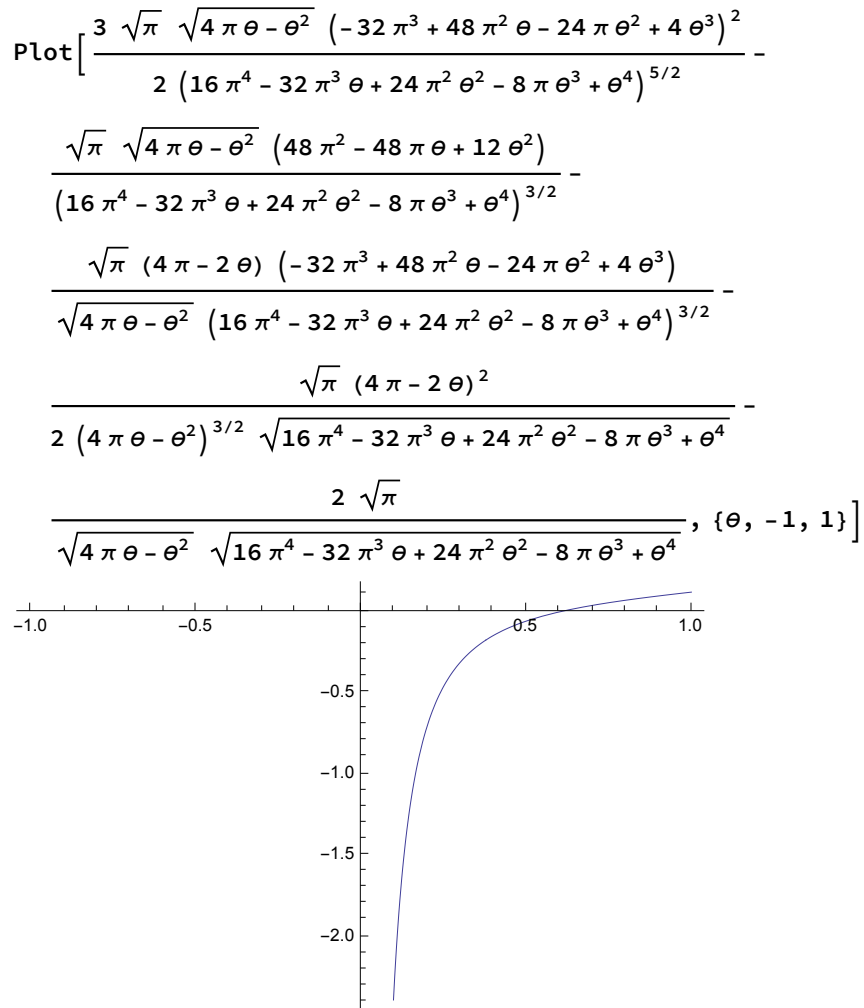


$$\begin{aligned}
& \text{D} \left[ -\frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \right. \\
& \left. \frac{\sqrt{\pi} (4 \pi - 2 \theta)}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \theta \right] \\
& 3 \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \\
& \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} -
\end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} - \\
& \frac{2\sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \\
\text{Plot} & \left[ \frac{3\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} - \right. \\
& \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} - \\
& \left. \frac{2\sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \{\theta, -13, 13\} \right]
\end{aligned}$$



In the following graph, we will zoom in to show that there is possibly a solution for theta, which is the Golden Ratio.



There is a gap at the Golden ratio, and we can show this by saying :

That, for instance, when considering the above equation and graph, we note that :

$$\text{when } a = 0 = \frac{3 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} -$$

$$\frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} -$$

$$\frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} -$$

$$\frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} -$$

$$\frac{2 \sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}$$

$$\text{Solve}\left[0 == \frac{3 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} -$$

$$\frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} -$$

$$\frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} -$$

$$\frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} -$$

$$\frac{2 \sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta]$$

$$\left\{ \left\{ \theta \rightarrow 2\pi - \sqrt{9 - \sqrt{33}} \pi \right\}, \left\{ \theta \rightarrow 2\pi + \sqrt{9 - \sqrt{33}} \pi \right\}, \right.$$

$$\left. \left\{ \theta \rightarrow 2\pi - \sqrt{9 + \sqrt{33}} \pi \right\}, \left\{ \theta \rightarrow 2\pi + \sqrt{9 + \sqrt{33}} \pi \right\} \right\}$$

The following solutions for theta come from :

$$\text{Solve}\left[\pi \left( r^2 - \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)^2 == \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right), \theta \right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{2\pi r^2 - \sqrt{2\pi} \sqrt{-r^2 - r^2} \sqrt{1 + 4\pi r^2}}{r^2} \right\}, \right.$$

$$\left. \left\{ \theta \rightarrow \frac{2\pi r^2 + \sqrt{2\pi} \sqrt{-r^2 - r^2} \sqrt{1 + 4\pi r^2}}{r^2} \right\}, \right.$$



$$\left\{ \theta \rightarrow \frac{2 \pi r^2 - \sqrt{2 \pi} \sqrt{-r^2 + r^2} \sqrt{1 + 4 \pi r^2}}{r^2} \right\},$$

$$\left\{ \theta \rightarrow \frac{2 \pi r^2 + \sqrt{2 \pi} \sqrt{-r^2 + r^2} \sqrt{1 + 4 \pi r^2}}{r^2} \right\}$$

This frequency comes from :

$$r = \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \lambda = \frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \quad (15)$$

$$r = \frac{2 h \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 (c) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 (r / t) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 (r / (6 \theta)) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} =$$

$$\frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}$$

Where c is the speed of light.

$$\text{Solve} \left[ \frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} == \frac{2 (r / (6 \theta)) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}}, \theta \right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{2 \left( -\pi + \pi^{3/2} r - \sqrt{\pi^2 - \pi^{5/2} r} \right)}{-1 + \sqrt{\pi} r} \right\}, \left\{ \theta \rightarrow \frac{2 \left( -\pi + \pi^{3/2} r + \sqrt{\pi^2 - \pi^{5/2} r} \right)}{-1 + \sqrt{\pi} r} \right\}, \right.$$

$$\left. \left\{ \theta \rightarrow \frac{2 \left( \pi + \pi^{3/2} r - \sqrt{\pi^2 + \pi^{5/2} r} \right)}{1 + \sqrt{\pi} r} \right\}, \left\{ \theta \rightarrow \frac{2 \left( \pi + \pi^{3/2} r + \sqrt{\pi^2 + \pi^{5/2} r} \right)}{1 + \sqrt{\pi} r} \right\} \right\}$$

$$\text{Solve} \left[ \frac{2 (r / (6 \theta)) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} == r, \theta \right]$$

$$\{ \{ \theta \rightarrow 2 \pi \} \}$$

The age of a negative mitichlorian.

(See the Geometric Patterns of Perception Series for more in depth solutions (explanations, system of variables and postulates))

$E = hnf = h\nu$ , where h is Planck' s constant, not the height of the cone.

$$r / t = r / (6 \theta) = c = \lambda f = r (1 / 6 \theta)$$

r/t is the rate of travel for the wave and is related to the speed of light. The speed of light is variable.

$$\text{Solve} \left[ (r / t) == \frac{(r / t) 6 (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} * \nu, \nu \right]$$

$$\left\{ \left\{ \nu \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta} \right\} \right\}$$

(16)

$$\text{Solve}\left[n \left(1 / 6 \theta\right) == \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta}, n\right]$$

$$\left\{\left\{n \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta^2}\right\}\right\} \quad (17)$$

Where  $h$  is Planck's Constant,  $n$  the number of moles, and  $f$  the frequency, we may say that the force of dark matter ( $F_{dm}$ ) is capable of being solved for in terms of time or purely space.

$$D[h n f, \theta] = (F_{dm})$$

$$D\left[(6.62606896 * 10^{-34}) \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta^2} \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta}, \theta\right] = (F_{dm}) = m a$$

$$D\left[(6.62606896 * 10^{-34}) \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta^2} \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta}, \theta\right] - \frac{2.2378704997431808 * 10^{-35} (4 \pi - \theta)}{\theta^3} - \frac{1.1189352498715904 * 10^{-35}}{\theta^2} =$$

$$(F_{dm}) = m a = m \left( \frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} - \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right)$$

$$\begin{aligned}
& \text{Solve} \left[ -\frac{2.2378704997431808 \cdot \pi^{-35} (4\pi - \theta)}{\theta^3} - \frac{1.1189352498715904 \cdot \pi^{-35}}{\theta^2} == \right. \\
& m \left( \frac{3 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} - \right. \\
& \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} - \\
& \left. \left. \frac{2 \sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right), m \right] \\
& \left\{ \left\{ m \rightarrow - \left( 1. \left( \frac{2.23787 \times 10^{-35} (12.5664 - 1. \theta)}{\theta^3} + \frac{1.11894 \times 10^{-35}}{\theta^2} \right) \right) / \right. \right. \\
& \left( 2.65868 \sqrt{12.5664\theta - 1. \theta^2} (-992.201 + 473.741\theta - 75.3982\theta^2 + 4. \theta^3)^2 \right) / \\
& (1558.55 - 992.201\theta + 236.871\theta^2 - 25.1327\theta^3 + \theta^4)^{5/2} - \\
& \frac{1.77245 \sqrt{12.5664\theta - 1. \theta^2} (473.741 - 150.796\theta + 12. \theta^2)}{(1558.55 - 992.201\theta + 236.871\theta^2 - 25.1327\theta^3 + \theta^4)^{3/2}} - \\
& (1.77245 (12.5664 - 2. \theta) (-992.201 + 473.741\theta - 75.3982\theta^2 + 4. \theta^3)) / \\
& \left( \sqrt{12.5664\theta - 1. \theta^2} (1558.55 - 992.201\theta + 236.871\theta^2 - 25.1327\theta^3 + \theta^4)^{3/2} \right) - \\
& (0.886227 (12.5664 - 2. \theta)^2) / \\
& \left( (12.5664\theta - 1. \theta^2)^{3/2} \sqrt{1558.55 - 992.201\theta + 236.871\theta^2 - 25.1327\theta^3 + \theta^4} \right) - \\
& \left. \left. 3.54491 / \left( \sqrt{12.5664\theta - 1. \theta^2} \sqrt{1558.55 - 992.201\theta + 236.871\theta^2 - 25.1327\theta^3 + \theta^4} \right) \right) \right\} \}
\end{aligned}$$

Remember that this solution is only for one of the possibilities for theta and r put together. There are other valid solutions that may work parametrically. Approximating these by their derivative functions relates to the uncertainty of their position to a more simplified structure for solutions. Now we'll find Planck's constant in terms of the S.I. units.

$$h = (m r^2) / (6 \theta)^2 \quad (6 \theta) = (m r^2) / (6 \theta)$$

$$E = h n f = h \nu$$

$$E = hnf = (m r^2) / (6 \theta) \quad v = (m r^2) / (6 \theta) \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta^2} \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta} = hnf$$

$$(m r^2) / (6 \theta) \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta^2} \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta} = hnf$$

This is the acceleration due to gravity of dark matter.

$$g = - (mG / d^2) \hat{r}$$

For  $\hat{r}$ , we will say that it is any distance with a max of  $r$ . Before, we defined  $h$  to be the height of a cone and then changed our definition of the variable  $h$  to be Planck's constant. We are now redefining again for  $h$  to say that it is the height of the cone once again.

$$\text{Solve}\left[\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2} == h^2, h\right]$$

$$\left\{ \left\{ \eta = h \rightarrow - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ \eta = h \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\} \right\}$$

Final redefinition :

$h := \text{Planck's Constant}$

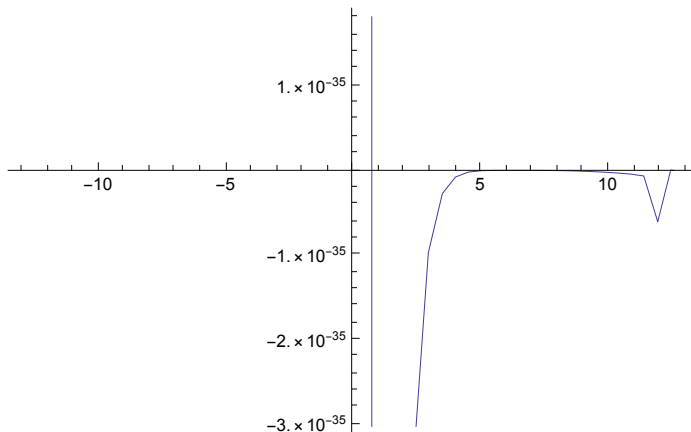
$$d = r$$

$$g = - (mG / r^2) \hat{r} = - (mG / \eta^2) = \quad (18)$$

The big  $G$  is the universal gravitational constant, which we will now take out the numerical constant part of it, and replace its units with variables.

The object is taken up by the sphere with radius  $r_1$ .  $\eta$  is the distance away from the center of the other gravitational object. This shows that the radius,  $r_1$  refers to an expanding object when gravity accelerates objects through spacetime. This is why the universe is expanding.

$$\begin{aligned}
& \text{Plot}\left[\left\{\left\{-\left(1.\cdot\left(\frac{2.2378704997431808\cdot10^{-35}(12.566370614359172\cdot10^{-1}\cdot\theta)}{\theta^3}+\right.\right.\right.\right. \\
& \quad \left.\left.\left.\frac{1.1189352498715904\cdot10^{-35}}{\theta^2}\right)\right)\right\}/ \\
& \quad \left(\left(2.658680776358274\cdot\sqrt{12.566370614359172\cdot\theta-1.\cdot\theta^2}(-992.2008537695941\cdot\right.\right. \\
& \quad \left.\left.473.7410112522892\cdot\theta-75.39822368615503\cdot\theta^2+4.\cdot\theta^3)^2\right)/\right. \\
& \quad \left.(1558.5454565440389\cdot-992.2008537695941\cdot\theta+236.8705056261446\cdot\theta^2-\right. \\
& \quad \left.25.132741228718345\cdot\theta^3+\theta^4)^{5/2}-\right. \\
& \quad \left.(1.7724538509055159\cdot\sqrt{12.566370614359172\cdot\theta-1.\cdot\theta^2}\right. \\
& \quad \left.(473.7410112522892\cdot-150.79644737231007\cdot\theta+12.\cdot\theta^2)\right)/ \\
& \quad \left.(1558.5454565440389\cdot-992.2008537695941\cdot\theta+236.8705056261446\cdot\theta^2-\right. \\
& \quad \left.25.132741228718345\cdot\theta^3+\theta^4)^{3/2}-\right. \\
& \quad \left.(1.7724538509055159\cdot(12.566370614359172\cdot-2.\cdot\theta)(-992.2008537695941\cdot\right. \\
& \quad \left.473.7410112522892\cdot\theta-75.39822368615503\cdot\theta^2+4.\cdot\theta^3)\right)/ \\
& \quad \left(\sqrt{12.566370614359172\cdot\theta-1.\cdot\theta^2}(1558.5454565440389\cdot-992.2008537695941\cdot\theta+\right. \\
& \quad \left.236.8705056261446\cdot\theta^2-25.132741228718345\cdot\theta^3+\theta^4)^{3/2}\right)- \\
& \quad \left.(0.8862269254527579\cdot(12.566370614359172\cdot-2.\cdot\theta)^2\right)/ \\
& \quad \left(\left((12.566370614359172\cdot\theta-1.\cdot\theta^2)^{3/2}\sqrt{(1558.5454565440389\cdot-992.2008537695941\cdot\right.\right. \\
& \quad \left.\left.\theta+236.8705056261446\cdot\theta^2-25.132741228718345\cdot\theta^3+\theta^4)\right)\right)- \\
& \quad \left.3.5449077018110318\cdot\left(\sqrt{12.566370614359172\cdot\theta-1.\cdot\theta^2}\right.\right. \\
& \quad \left.\left.\sqrt{(1558.5454565440389\cdot-992.2008537695941\cdot\theta+236.8705056261446\cdot\theta^2-\right.\right. \\
& \quad \left.\left.25.132741228718345\cdot\theta^3+\theta^4)\right)\right)\right\},\{\theta,-13,13\}]
\end{aligned}$$



$E = h\nu$ , where  $E$  is energy,  $h$  is Planck's Constant, and  $\nu$  is frequency.

(19)

$$E = \hbar \omega, \text{ where } E \text{ is energy, } \hbar \text{ is } h/2\pi, \text{ and } \omega \text{ is angular frequency.} \quad (20)$$

$$v = \lambda f, \text{ where } v \text{ is velocity, } \lambda \text{ is wavelength, and } f \text{ is frequency.} \quad (21)$$

$$E = mc^2, \text{ where } E \text{ is energy, } m \text{ is mass, and } c \text{ is the speed of light.} \quad (22)$$

---

The First  $r$  and  $\theta$  solutions will be discussed now.

$$v = \lambda f$$

$$\left( \frac{2\sqrt{\pi}\sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right) \left( 1 / \frac{2(-\pi + \pi^{3/2}r - \sqrt{\pi^2 - \pi^{5/2}r})}{-1 + \sqrt{\pi}r} \right)$$

$$v = \left( \frac{2\sqrt{\pi}\sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right) \left( 1 / \frac{1}{-1 + \sqrt{\pi} \left( \frac{2\sqrt{\pi}\sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)} \right)$$

$$2 \left( -\pi + \pi^{3/2} \left( \left( \frac{2\sqrt{\pi}\sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right) \right) - \right.$$

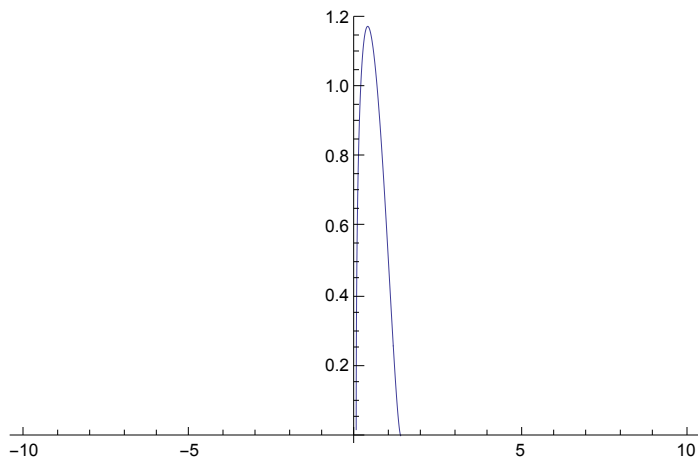
$$\left. \sqrt{\pi^2 - \pi^{5/2} \left( \frac{2\sqrt{\pi}\sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)} \right)$$

Simplify[

$$\begin{aligned}
& \left( \frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right) \left( \frac{1}{-1 + \sqrt{\pi} \left( \frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right)} \times 2 \right. \\
& \left. \left( -\pi + \pi^{3/2} \left( \left( \frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right) - \right. \right. \right. \\
& \left. \left. \left. \sqrt{\pi^2 - \pi^{5/2} \left( \frac{2 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right)} \right) \right) \right) \right] \\
& \frac{1}{((-2 \pi + \theta)^4)^{3/2}} \\
& 4 \pi^{3/2} \sqrt{(4 \pi - \theta) \theta} \left( -2 \pi \sqrt{(4 \pi - \theta) \theta} + \sqrt{(-2 \pi + \theta)^4} \right) \left( -2 \pi \sqrt{(4 \pi - \theta) \theta} + \sqrt{(-2 \pi + \theta)^4} + \right. \\
& \left. \sqrt{(-2 \pi + \theta)^4} \sqrt{\frac{(-2 \pi + \theta)^4 - 2 \pi \sqrt{(4 \pi - \theta) \theta} \sqrt{(-2 \pi + \theta)^4}}{(-2 \pi + \theta)^4}} \right)
\end{aligned}$$

$$\text{Plot} \left[ \frac{1}{((-2 \pi + \theta)^4)^{3/2}} 4 \pi^{3/2} \sqrt{(4 \pi - \theta) \theta} \right.$$

$$\begin{aligned}
& \left. \left( -2 \pi \sqrt{(4 \pi - \theta) \theta} + \sqrt{(-2 \pi + \theta)^4} \right) \left( -2 \pi \sqrt{(4 \pi - \theta) \theta} + \sqrt{(-2 \pi + \theta)^4} + \right. \right. \\
& \left. \left. \sqrt{(-2 \pi + \theta)^4} \sqrt{\frac{(-2 \pi + \theta)^4 - 2 \pi \sqrt{(4 \pi - \theta) \theta} \sqrt{(-2 \pi + \theta)^4}}{(-2 \pi + \theta)^4}} \right) \right], \{\theta, -10, 10\}
\end{aligned}$$



$$\frac{1}{((-2\pi + \theta)^4)^{3/2}} 4\pi^{3/2} \sqrt{(4\pi - \theta)\theta}$$

$$\left( -2\pi \sqrt{(4\pi - \theta)\theta} + \sqrt{(-2\pi + \theta)^4} \right) \left( -2\pi \sqrt{(4\pi - \theta)\theta} + \sqrt{(-2\pi + \theta)^4} + \sqrt{(-2\pi + \theta)^4} \sqrt{\frac{(-2\pi + \theta)^4 - 2\pi \sqrt{(4\pi - \theta)\theta} \sqrt{(-2\pi + \theta)^4}}{(-2\pi + \theta)^4}} \right) = r / 6\theta$$

$$E = h\nu$$

$$\nu = \lambda\nu = r / 6\theta$$

$$\theta \rightarrow \frac{2(\pi + \pi^{3/2}r - \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r}$$

$$\lambda\nu = r / 6\theta = r \left( 1 / 6 \left( \frac{2(\pi + \pi^{3/2}r - \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r} \right) \right)$$

$$r / 6 \left( 1 / 6 \left( \frac{2(\pi + \pi^{3/2}r - \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r} \right) \right) = r \left( 1 / 6 \left( \frac{2(\pi + \pi^{3/2}r - \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r} \right) \right)$$

$$\text{Solve}\left[r / 6 \left( 1 / 6 \left( \frac{2(\pi + \pi^{3/2}r - \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r} \right) \right) == r \left( 1 / 6 \left( \frac{2(\pi + \pi^{3/2}r - \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r} \right) \right), r\right]$$

$$\{\{r \rightarrow 0\}\}$$

$$E = h\nu$$

$$\nu = \lambda\nu = r / 6\theta$$

$$\theta = \frac{2(\pi + \pi^{3/2}r + \sqrt{\pi^2 + \pi^{5/2}r})}{1 + \sqrt{\pi}r}$$

## From a Basic Equation for Acceleration

From a basic equation for acceleration.

$$\text{Solve}\left[\frac{2\sqrt{\pi}}{\sqrt{4\pi(\theta) - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} = a, a\right]$$

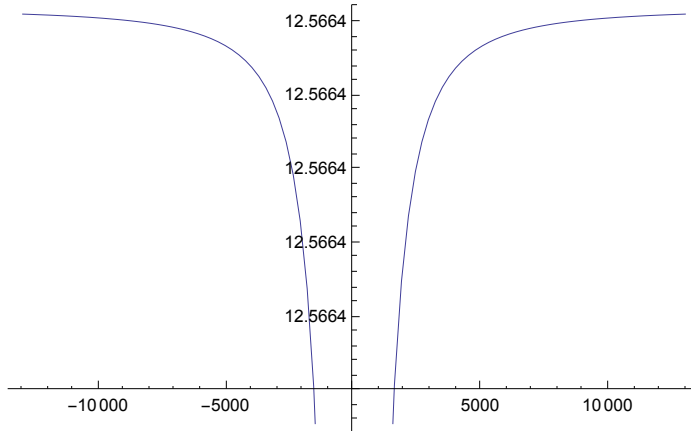
$$\left\{ \left\{ a \rightarrow \frac{2\sqrt{\pi}}{\sqrt{(2\pi - \theta)^4} \sqrt{(4\pi - \theta)\theta}} \right\} \right\}$$



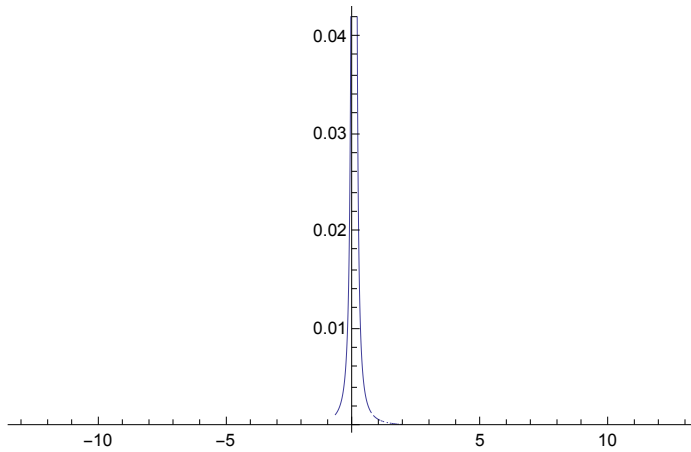
$$\text{Solve}\left[a == \frac{2 \sqrt{\pi}}{\sqrt{(2 \pi - \theta)^4} \sqrt{(4 \pi - \theta) \theta}}, \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow - \left( -12 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} - \right. \right. \\ & \quad \sqrt{\left( 384 \times 2^{1/3} a^8 \pi^{16/3} - 324 a^6 (2 \pi)^{1/3} + 36 \sqrt{3} a^2 (2 \pi)^{1/3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right) +} \\ & \quad 96 \times 2^{2/3} a^6 \pi^{11/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \\ & \quad \left. \left. 48 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \right\} / \\ & \quad \left( 6 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right) \Big\}, \\ & \left\{ \theta \rightarrow - \left( -12 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \right. \right. \\ & \quad \sqrt{\left( 384 \times 2^{1/3} a^8 \pi^{16/3} - 324 a^6 (2 \pi)^{1/3} + 36 \sqrt{3} a^2 (2 \pi)^{1/3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right) +} \\ & \quad 96 \times 2^{2/3} a^6 \pi^{11/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \\ & \quad \left. \left. 48 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \right\} / \\ & \quad \left( 6 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right) \Big\}, \\ & \left\{ \theta \rightarrow \left( 24 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} - \right. \right. \\ & \quad \sqrt{\left( 576 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} - \right.} \\ & \quad 24 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \left( 8 \times 2^{2/3} a^4 \pi^{11/3} + \right. \\ & \quad 8 i 2^{2/3} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \\ & \quad \left. \left. (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} - \right. \right. \\ & \quad \left. \left. i \sqrt{3} (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \right) \Big\} / \\ & \quad \left( 12 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right) \Big\}, \\ & \left\{ \theta \rightarrow \left( 24 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \right. \right. \\ & \quad \sqrt{\left( 576 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} - \right.} \\ & \quad 24 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \left( 8 \times 2^{2/3} a^4 \pi^{11/3} + \right. \\ & \quad 8 i 2^{2/3} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \\ & \quad \left. \left. (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} - \right. \right. \\ & \quad \left. \left. i \sqrt{3} (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \right) \Big\} / \\ & \quad \left( 12 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right) \Big\}, \end{aligned}$$

$$\begin{aligned}
& \left\{ \theta \rightarrow \left( 24 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} - \right. \right. \\
& \quad \sqrt{\left( 576 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} - \right.} \\
& \quad \left. 24 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \left( 8 \times 2^{2/3} a^4 \pi^{11/3} - \right. \right. \\
& \quad \left. 8 i 2^{2/3} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \right. \\
& \quad \left. (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} + \right. \\
& \quad \left. \left. i \sqrt{3} (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \Bigg) \Bigg) / \\
& \quad \left( 12 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right) \Bigg\}, \\
& \left\{ \theta \rightarrow \left( 24 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \right. \right. \\
& \quad \sqrt{\left( 576 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} - \right.} \\
& \quad \left. 24 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \left( 8 \times 2^{2/3} a^4 \pi^{11/3} - \right. \right. \\
& \quad \left. 8 i 2^{2/3} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \right. \\
& \quad \left. (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} + \right. \\
& \quad \left. \left. i \sqrt{3} (2 \pi)^{1/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \Bigg) \Bigg) / \\
& \quad \left( 12 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right) \Bigg\} \Bigg\} \\
& \text{Plot} \left[ - \left( -12 a^2 \pi \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} - \right. \right. \\
& \quad \sqrt{\left( 384 \times 2^{1/3} a^8 \pi^{16/3} - 324 a^6 (2 \pi)^{1/3} + 36 \sqrt{3} a^2 (2 \pi)^{1/3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} + \right.} \\
& \quad \left. 96 \times 2^{2/3} a^6 \pi^{11/3} \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} + \right. \\
& \quad \left. \left. 48 a^4 \pi^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{2/3} \right) \right) \Bigg) \Bigg) / \\
& \quad \left( 6 a^2 \left( -27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} \right)^{1/3} \right), \{a, \\
& \quad -13000, \\
& \quad 13000\} ]
\end{aligned}$$



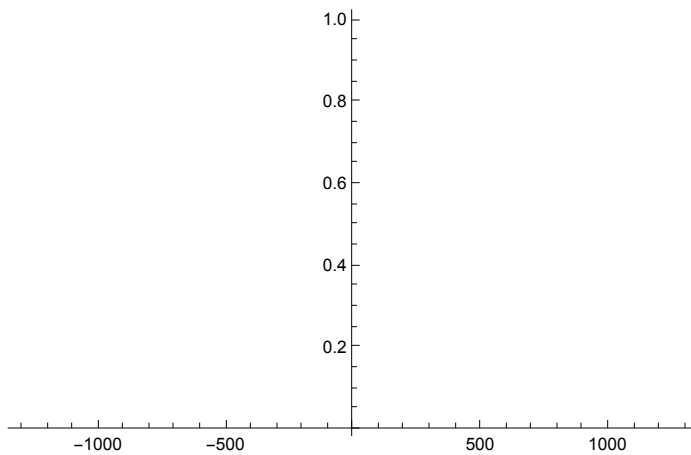
$\text{Plot}\left[-\left(-12 a^2 \pi \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + \right.\right.$   
 $\left.\sqrt{\left(384 \times 2^{1/3} a^8 \pi^{16/3} - 324 a^6 (2 \pi)^{1/3} + 36 \sqrt{3} a^2 (2 \pi)^{1/3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)} + \right.\right.$   
 $\left.96 \times 2^{2/3} a^6 \pi^{11/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + \right.$   
 $\left.48 a^4 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3}\right)^{1/3} \Bigg] /$   
 $\left(6 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3}\right), \{a,$   
 $-13,$   
 $13\}$



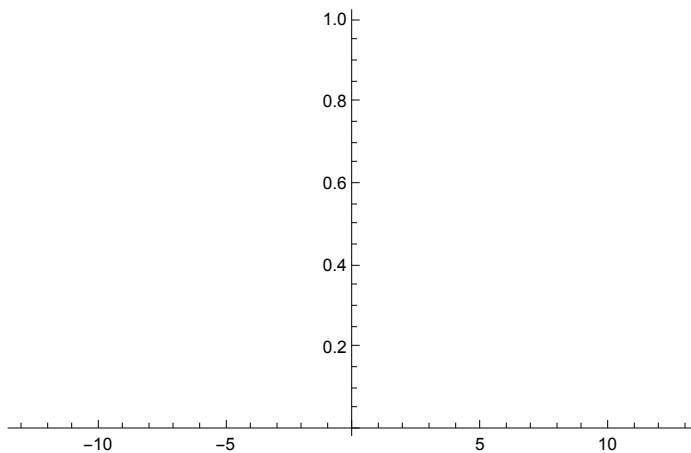
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Plot[ ( 24 a^2 π (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(1/3) -
√( (576 a^4 π^2 (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(2/3) -
24 a^2 (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(1/3) (8 × 2^(2/3) a^4 π^(11/3) +
8 i 2^(2/3) √3 a^4 π^(11/3) + 16 a^2 π^2 (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(1/3) +
(2 π)^(1/3) (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(2/3) -
i √3 (2 π)^(1/3) (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(2/3) ) ) ) /
( 12 a^2 (-27 a^4 + 32 a^6 π^5 + 3 √3 √(-a^8 (-27 + 64 a^2 π^5)))^(1/3) ), {a,
-1300,
1300} ]

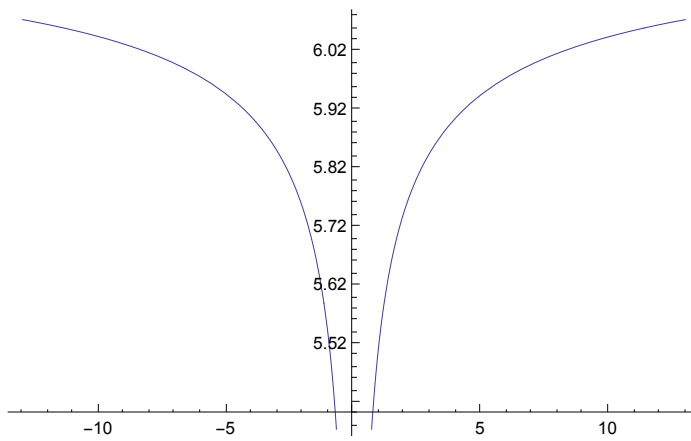
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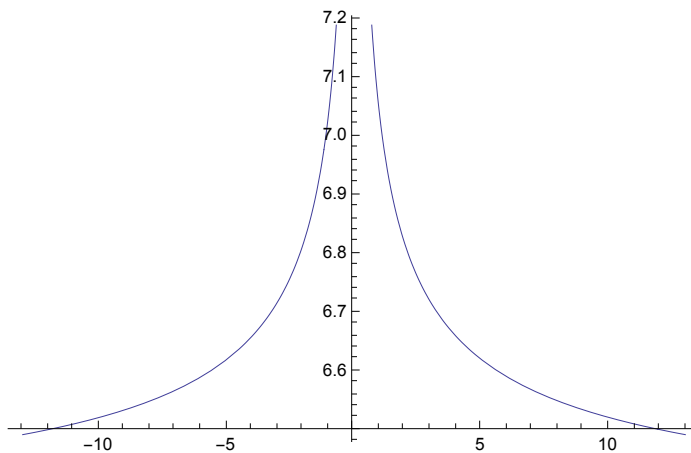
$$\begin{aligned}
 & \text{Plot}\left[\left(24 a^2 \pi \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + \right. \right. \\
 & \quad \sqrt{\left(576 a^4 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3} - \right.} \\
 & \quad \left. 24 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} \left(8 \times 2^{2/3} a^4 \pi^{11/3} + \right. \\
 & \quad \left. 8 i 2^{2/3} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + \right. \\
 & \quad \left. (2 \pi)^{1/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3} - \right. \\
 & \quad \left. i \sqrt{3} (2 \pi)^{1/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3}\right)\right) \Bigg] / \\
 & \quad \left(12 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3}\right), \{a, \\
 & \quad -13, \\
 & \quad 13\}]
 \end{aligned}$$



$\text{Plot}\left[\left(24 a^2 \pi \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} - \right.\right.$   
 $\left.\sqrt{\left(576 a^4 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3} - \right.\right.}\right.$   
 $\left.24 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} \left(8 \times 2^{2/3} a^4 \pi^{11/3} - \right.\right.$   
 $\left.8 i^{2^{2/3}} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + \right.$   
 $\left.(2 \pi)^{1/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3} + \right.$   
 $\left.\left.i \sqrt{3} (2 \pi)^{1/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3}\right)\right) \Bigg] /$   
 $\left(12 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3}\right), \{a,$   
 $-13,$   
 $13\}$



$$\text{Plot}\left[\left(24 a^2 \pi \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + \sqrt{\left(576 a^4 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3} - 24 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} \left(8 \times 2^{2/3} a^4 \pi^{11/3} - 8 \sqrt[3]{2} \sqrt{3} a^4 \pi^{11/3} + 16 a^2 \pi^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3} + (2 \pi)^{1/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3} + \sqrt{3} (2 \pi)^{1/3} \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{2/3}\right)\right)}\right] / \left(12 a^2 \left(-27 a^4 + 32 a^6 \pi^5 + 3 \sqrt{3} \sqrt{-a^8 (-27 + 64 a^2 \pi^5)}\right)^{1/3}\right), \{a, -13, 13\}]$$



## Accretion of Contour

$$t = \theta / k == (\theta r) / (r k) == (2 \pi r - 2 \pi x) / (r k)$$

Solve[ $\theta / k$

Solve[ $t == (2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}) / (r k), t]$

$$\left\{\left\{t \rightarrow -\frac{2 \left(-\pi r + \pi \sqrt{r^2 - \eta^2}\right)}{k r}\right\}\right\}$$

$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), k\right]$$

$$\left\{\left\{k \rightarrow \frac{2 \pi \left(r - \sqrt{r^2 - \eta^2}\right)}{r t}\right\}\right\}$$

$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 k \pi t - k^2 t^2}}\right\}, \left\{r \rightarrow \frac{2 \pi \eta}{\sqrt{4 k \pi t - k^2 t^2}}\right\}\right\}$$

$$\text{Solve}\left[\left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k) == \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) / k, k\right]$$

$$\{\{\}\}$$

$$\text{Solve}\left[\left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k) == \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) / k, r\right]$$

$$\text{Solve}\left[2 \pi \sqrt{r^2 - \eta^2} == 2 \pi r - (r k) t, \eta\right]$$

$$\text{Solve}\left[(2 \pi r - (r k) t) / (2 \pi) == \sqrt{r^2 - \eta^2}, \eta\right]$$

$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 k \pi r^2 t - k^2 r^2 t^2}}{2 \pi} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}, k\right]$$

$$\{\{\}\}$$

$$\text{Solve}\left[((2 \pi r - (r k) t) / (2 \pi))^2 == (r^2 - \eta^2), \eta\right]$$

$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{4 k \pi r^2 t - k^2 r^2 t^2}}{2 \pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{4 k \pi r^2 t - k^2 r^2 t^2}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[((2 \pi r - (r k) t) / (2 \pi))^2 == (r^2 - \eta^2), \eta\right]$$

$$\text{Solve}\left[((2 \pi r - (r k) t) / (2 \pi))^2 == \sqrt{r^2 - \eta^2}^2, \eta\right]$$

$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), \eta\right]$$

$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{4 \pi - \theta}{k}\right\}, \left\{t \rightarrow \frac{\theta}{k}\right\}\right\}$$



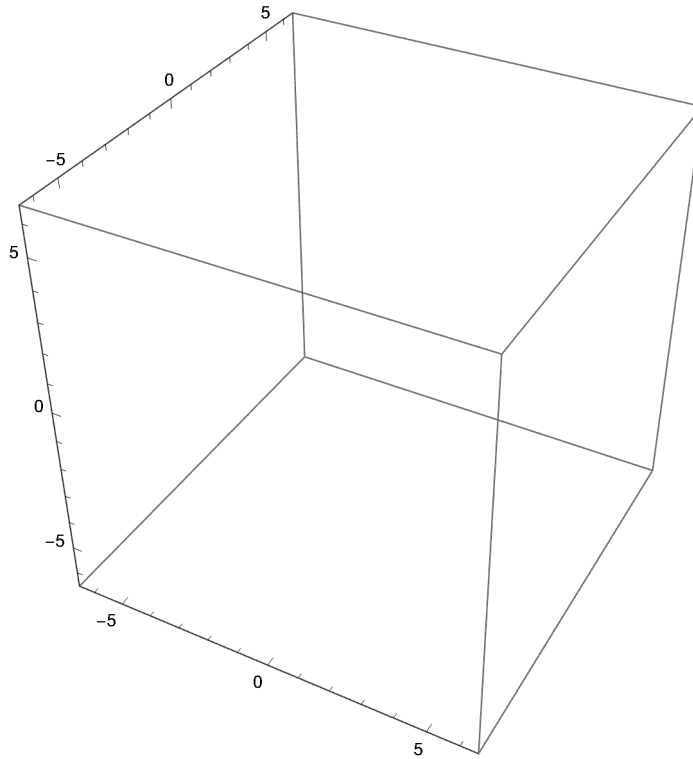
$$\text{Solve}\left[\eta == \frac{\sqrt{k} r \sqrt{t} \sqrt{4\pi - kt}}{2\pi}, k\right]$$

$$\left\{ \left\{ k \rightarrow \left( -\pi t \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right) - \right. \right. \right. \\ \left. \sqrt{\left( \pi^2 t^2 \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right)^2 + \right. \right. \\ \left. 4 \pi^2 t^2 \eta^2 \theta \left( -1024 \pi^4 \theta + 1536 \pi^3 \theta^2 - 832 \pi^2 \theta^3 + 192 \pi \theta^4 - 16 \theta^5 - \right. \right. \\ \left. 1024 \pi^4 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 1280 \pi^3 \theta \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 512 \pi^2 \theta^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 64 \pi \theta^3 \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 1024 \pi^5 \sin[\beta]^2 + 1280 \pi^4 \theta \sin[\beta]^2 - 512 \pi^3 \theta^2 \sin[\beta]^2 + 64 \pi^2 \theta^3 \sin[\beta]^2 \right) \\ \left. \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \right) \Bigg/ \\ \left. \left( 2 t^2 \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \right\}, \\ \left\{ k \rightarrow \left( -\pi t \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right) + \right. \right. \\ \left. \sqrt{\left( \pi^2 t^2 \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right)^2 + \right. \right. \\ \left. 4 \pi^2 t^2 \eta^2 \theta \left( -1024 \pi^4 \theta + 1536 \pi^3 \theta^2 - 832 \pi^2 \theta^3 + 192 \pi \theta^4 - 16 \theta^5 - \right. \right. \\ \left. 1024 \pi^4 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 1280 \pi^3 \theta \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 512 \pi^2 \theta^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 64 \pi \theta^3 \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 1024 \pi^5 \sin[\beta]^2 + 1280 \pi^4 \theta \sin[\beta]^2 - 512 \pi^3 \theta^2 \sin[\beta]^2 + 64 \pi^2 \theta^3 \sin[\beta]^2 \right) \\ \left. \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \right) \Bigg/ \\ \left. \left( 2 t^2 \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \right\} \right\}$$

```

ContourPlot3D[
  (
    -π t (-64 π² θ² + 32 π θ³ - 4 θ⁴ + 128 π³ θ Sin[β]² - 32 π² θ² Sin[β]² - 64 π⁴ Sin[β]⁴) +
    √(
      π² t² (-64 π² θ² + 32 π θ³ - 4 θ⁴ + 128 π³ θ Sin[β]² - 32 π² θ² Sin[β]² - 64 π⁴ Sin[β]⁴)² +
      4 π² t² (
        √(4 π r² θ - r² θ²)
        /
        2 π
      )² θ (-1024 π⁴ θ + 1536 π³ θ² - 832 π² θ³ + 192 π θ⁴ -
        16 θ⁵ - 1024 π⁴ √(4 π - θ) θ Sin[β] + 1280 π³ θ √(4 π - θ) θ Sin[β] -
        512 π² θ² √(4 π - θ) θ Sin[β] + 64 π θ³ √(4 π - θ) θ Sin[β] -
        1024 π⁵ Sin[β]² + 1280 π⁴ θ Sin[β]² - 512 π³ θ² Sin[β]² + 64 π² θ³ Sin[β]²)
      (16 π² θ² - 8 π θ³ + θ⁴ - 32 π³ θ Sin[β]² + 8 π² θ² Sin[β]² + 16 π⁴ Sin[β]⁴)
    )
  ) /
  (2 t² (16 π² θ² - 8 π θ³ + θ⁴ - 32 π³ θ Sin[β]² + 8 π² θ² Sin[β]² + 16 π⁴ Sin[β]⁴)), {θ,
-2 π,
2 π}, {t,
-2 π,
2 π}, {β,
-2 π,
2 π}
]

```



$$\text{Solve}\left[\frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, k\right]$$

$$\left\{\left\{k \rightarrow \frac{4 \pi - \theta}{t}\right\}, \left\{k \rightarrow \frac{\theta}{t}\right\}\right\}$$

$$t = \theta / k = \theta / \frac{4 \pi - \theta}{t}$$

$$\text{Solve}\left[\theta / \frac{4 \pi - \theta}{t} == t, t\right]$$

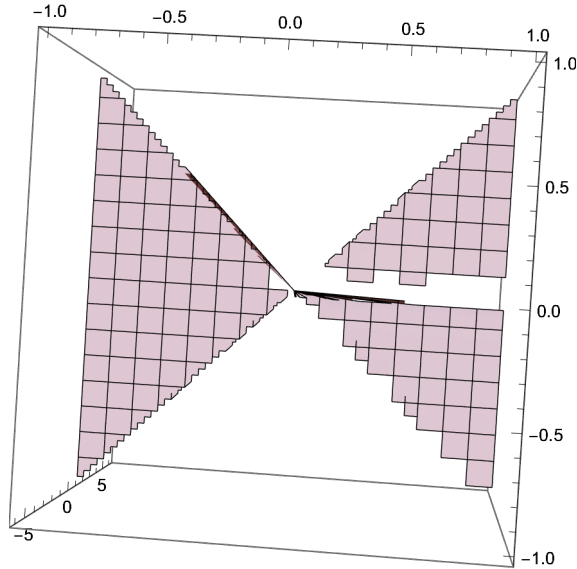
$$\{\{t \rightarrow 0\}\}$$

$$\text{Solve}\left[\theta / \frac{4 \pi - \theta}{t} == t, \theta\right]$$

$$\{\{\theta \rightarrow 2 \pi\}\}$$

$$\text{Solve}[\theta r == y r - y \sqrt{(r^2 - \eta^2)}, y]$$

$$\left\{ \left\{ y \rightarrow -\frac{r \theta}{-r + \sqrt{r^2 - \eta^2}} \right\} \right\}$$



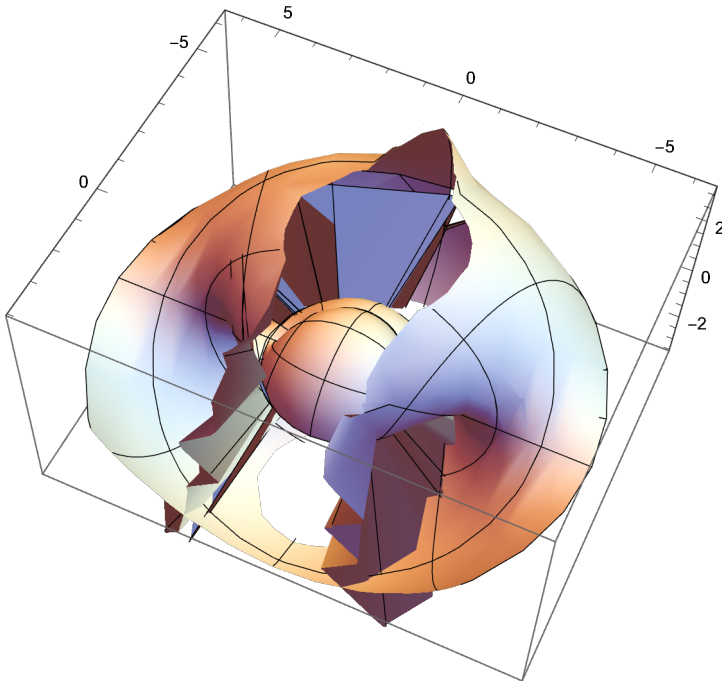
$$\frac{r \theta}{-r + \sqrt{r^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2}}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}, k\right]$$

$$\left\{ \left\{ k \rightarrow \frac{4 \pi - \theta}{t} \right\}, \left\{ k \rightarrow \frac{\theta}{t} \right\} \right\}$$

SphericalPlot3D $\left[\frac{r \theta}{-r + \sqrt{r^2 - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = h$$

$$\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = h$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \eta, \eta\right]$$

$$\left\{\left\{\eta \rightarrow \frac{\sqrt{r(-2 \pi + 2 \pi r + k t)}}{\sqrt{2 \pi}}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \eta, k\right]$$

$$\left\{\left\{k \rightarrow -\frac{2(-\pi r + \pi r^2 - \pi \eta^2)}{r t}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, k\right]$$

$$\left\{\left\{k \rightarrow \frac{4 \pi^2 - 4 \pi^2 r + 4 \pi r \theta - r \theta^2}{2 \pi t}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$$

$$\left\{\{r \rightarrow 0\}, \left\{r \rightarrow \frac{2 \pi(2 \pi - k t)}{(2 \pi - \theta)^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2\pi r - k r t) / (2\pi))} == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{4\pi^2 - 4\pi^2 r + 4\pi r \theta - r \theta^2}{2k\pi}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2\pi r - k r t) / (2\pi))} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4\pi - k t}}{2\pi}, r\right]$$

$$\left\{\{r \rightarrow 0\}, \left\{r \rightarrow \frac{2\pi}{2\pi - k t}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2\pi r - k r t) / (2\pi))} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4\pi - k t}}{2\pi}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{2\pi}{k}\right\}, \left\{t \rightarrow \frac{2\pi(-1+r)}{k r}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r \theta}}{2\pi} == r \sin[\beta], \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{1}{-8.98755 \times 10^{16} + v^2}\right\}\right\}$$

$$0.5 \left( -1.12941 \times 10^{18} + 12.5664 v^2 - 1. \sqrt{\left( (1.12941 \times 10^{18} - 12.5664 v^2)^2 - 4. (-8.98755 \times 10^{16} + v^2) (-3.54814 \times 10^{18} + 39.4784 v^2) \sin[\beta]^2 \right)} \right), \left\{\theta \rightarrow \right.$$

$$\left. \frac{1}{-8.98755 \times 10^{16} + v^2} 0.5 \left( -1.12941 \times 10^{18} + 12.5664 v^2 + \sqrt{\left( (1.12941 \times 10^{18} - 12.5664 v^2)^2 - 4. (-8.98755 \times 10^{16} + v^2) (-3.54814 \times 10^{18} + 39.4784 v^2) \sin[\beta]^2 \right)} \right) \right\}$$

$$v := \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + \right.$$

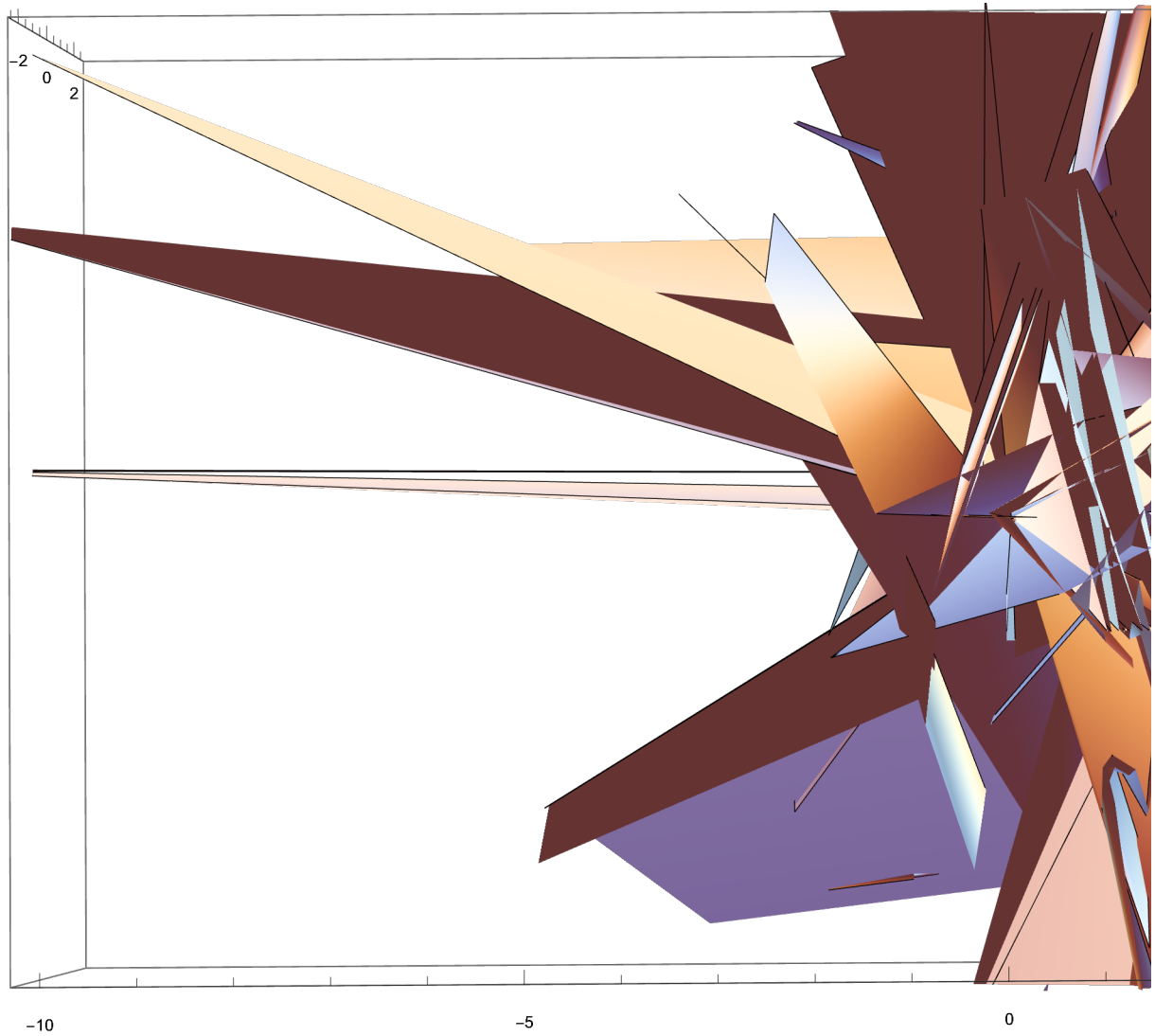
$$8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2) \Big/$$

$$\left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right)$$

```

SphericalPlot3D[ $\frac{1}{-8.987551787368176 \cdot v^{16} + v^2}$ ,
0.5` (-1.1294090667581471`*^18 + 12.566370614359172` v^2 +
 $\sqrt{\left((1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2)^2 -$ 
4.` (-8.987551787368176`*^16 + v^2) (-3.5481432270250993`*^18 +
39.47841760435743` v^2) Sin[ $\beta$ ]^2)}), { $\beta$ , - $\pi/2$ ,  $\pi/2$ }, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

```

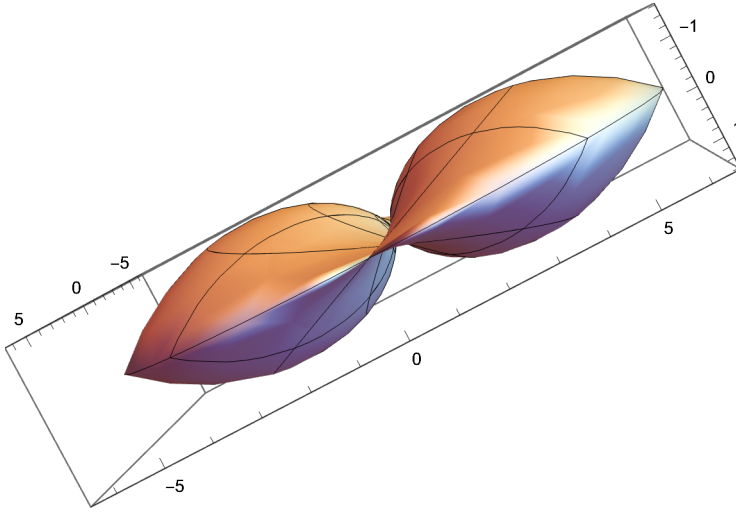


```
SphericalPlot3D[
$$\frac{1}{-8.987551787368176 \cdot 10^{16} + v^2}$$

0.5` (-1.1294090667581471`*^18 + 12.566370614359172` v^2 +

$$\sqrt{\left((1.1294090667581471 \cdot 10^{18} - 12.566370614359172 v^2)^2 -\right.}$$

4.` (-8.987551787368176`*^16 + v^2) (-3.5481432270250993`*^18 +
39.47841760435743` v^2) Sin[ $\beta$ ]^2)}, {v, -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi$ ,  $\pi$ }]
```



```
c := 2.99792458 (108)
```

```
 $\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$ 
```

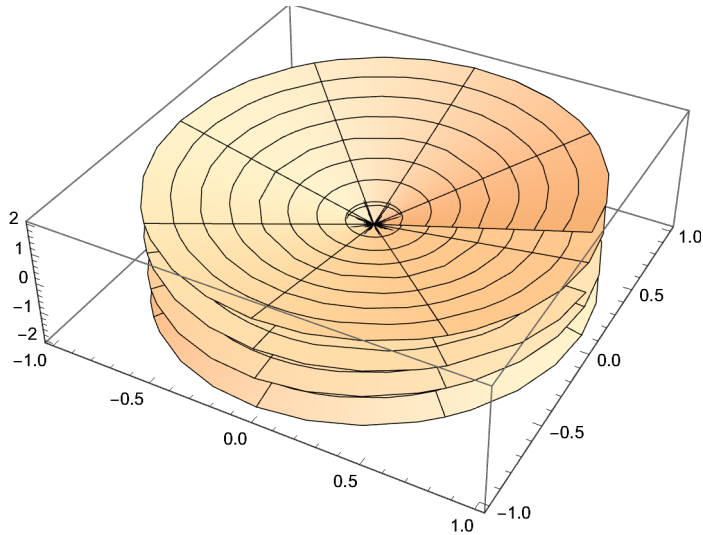
```
ArcCos[ $\eta$  / r] ==  $\beta$ 
```

```
Solve[ArcCos[ $\eta$  / r] == ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ],  $\eta$ ]
```

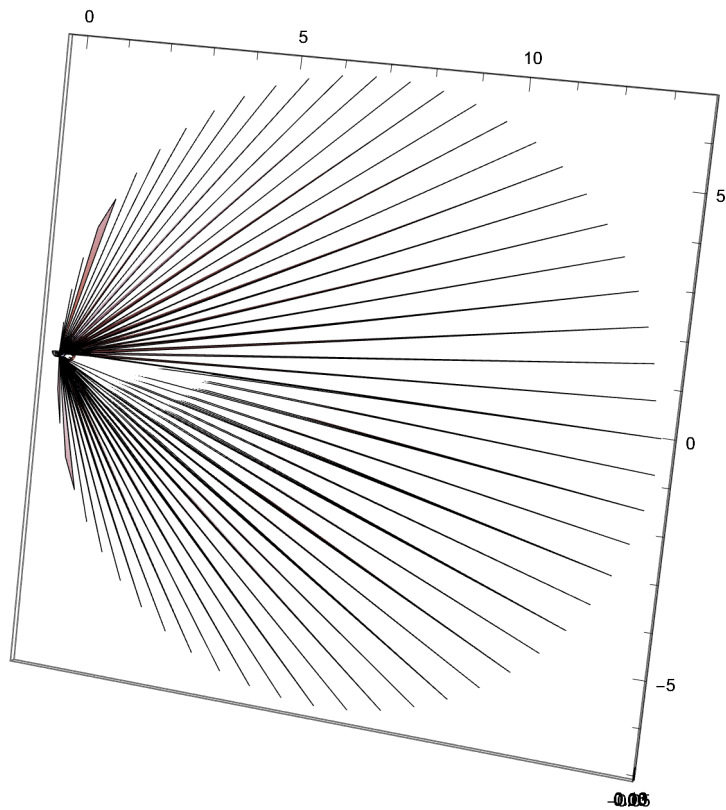
```
{ { $\eta \rightarrow r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}$  } }
```



RevolutionPlot3D $\left[r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



SphericalPlot3D $\left[r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



$$\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == r\sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow (2 - \sqrt{2})\pi\right\}, \left\{\theta \rightarrow (2 + \sqrt{2})\pi\right\}\right\}$$

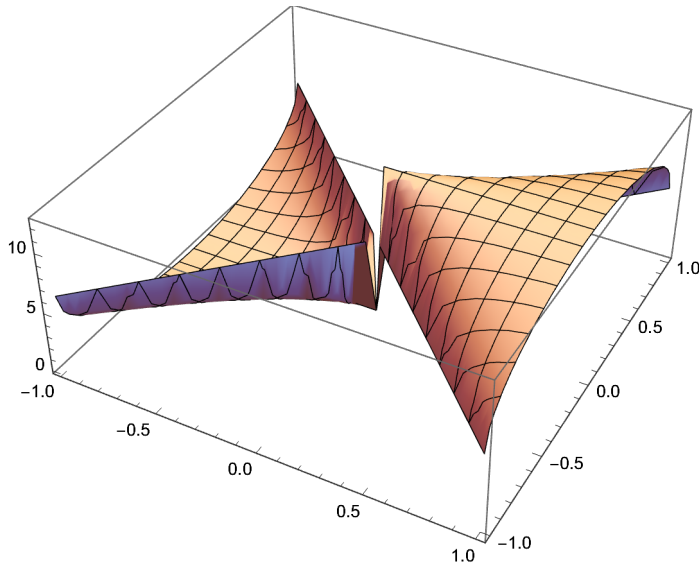
$$c := 2.99792458 * (10^8)$$

$$\text{Solve}\left[\frac{\sqrt{r\sqrt{1 - \frac{(4\pi - \theta)\theta}{c^2}}}\sqrt{\frac{\theta}{\sqrt{1 - \frac{(4\pi - \theta)\theta}{c^2}}}}\sqrt{4\pi r - r\theta}}{2\pi} == \eta, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{0.5\left(12.5664r^2 - 12.5664r\sqrt{1. r^2 - 1. \eta^2}\right)}{r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow \frac{0.5\left(12.5664r^2 + 12.5664r\sqrt{1. r^2 - 1. \eta^2}\right)}{r^2}\right\}\right\}$$

$$\text{Plot3D}\left[\frac{0.5\left(12.566370614359172r^2 + 12.566370614359172r\sqrt{1. r^2 - 1. \eta^2}\right)}{r^2},\right. \\ \left.\{r, -1, 1\}, \{\eta, -1, 1\}\right]$$

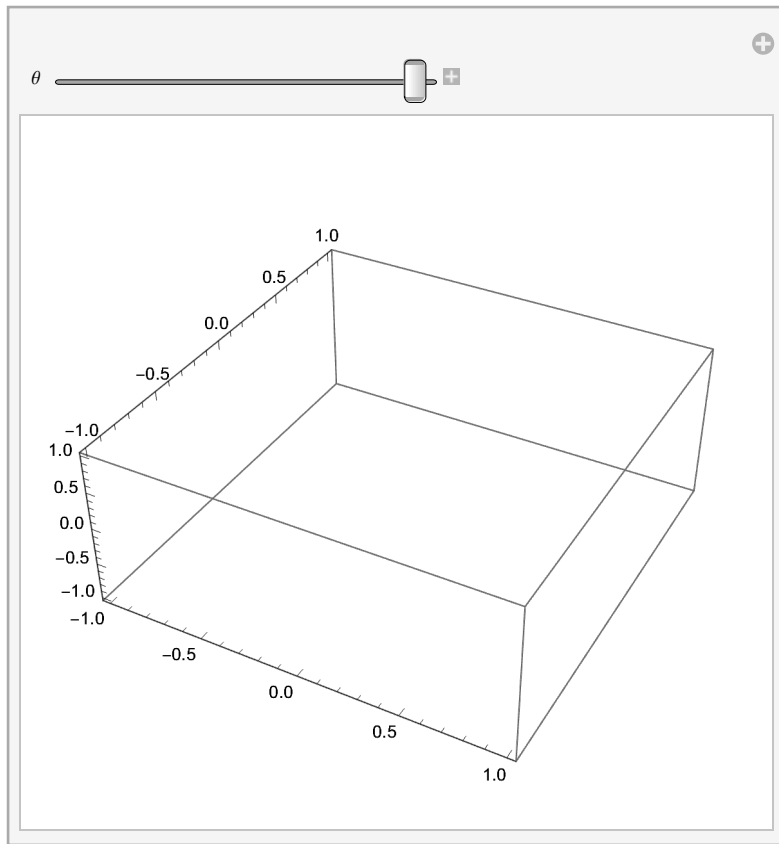


$$r = \sqrt{x^2 + y^2 + z^2} = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}^2}$$

$$\text{Solve}\left[r == \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2\pi\sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}\right\}, \left\{r \rightarrow \frac{2\pi\sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}\right\}\right\}$$

Manipulate[Plot3D[ $\frac{2 \pi \sqrt{x^2 + y^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}$ , {x, -1, 1}, {y, -1, 1}], {θ, -2 π, 2 π}]



Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

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Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

... Power: Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

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... **General:** Further output of Power::infy will be suppressed during this calculation.

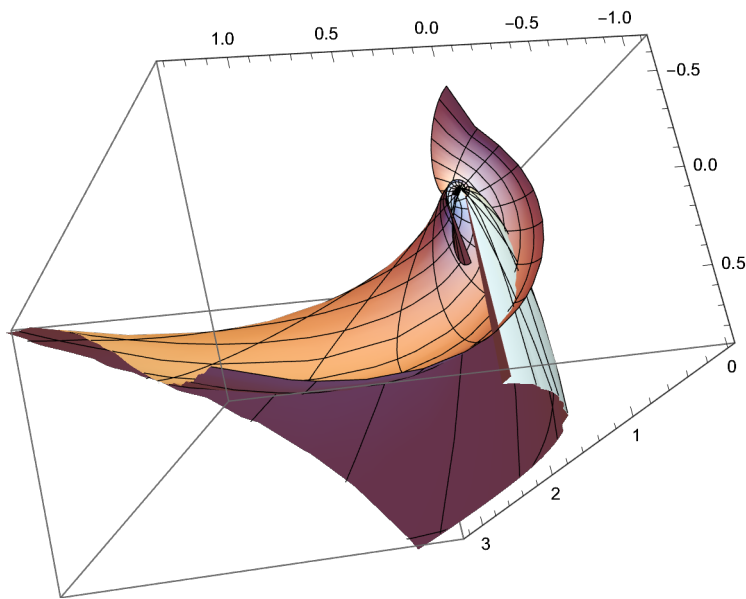
... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **General:** Further output of Power::infy will be suppressed during this calculation.

$$\text{SphericalPlot3D}\left[\frac{2\pi\sqrt{\left(\frac{2\pi r-r\theta}{2\pi}\right)^2+\left(\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\right)^2}}{\sqrt{4\pi^2-4\pi\theta+\theta^2}},\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$$



$$\text{Solve}\left[\frac{r\sqrt{\pi^2-\text{ArcCos}\left[\sqrt{\frac{1}{2}+\frac{1}{2}\sqrt{1-\text{Sin}[\theta]^2}}\right]}^2}{\pi}=r\text{Sin}[\beta],\beta\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta\rightarrow\text{ArcSin}\left[\frac{1}{\pi}\sqrt{\left(\left(\pi-\text{ArcCos}\left[\sqrt{\frac{1}{2}+\frac{1}{2}\sqrt{1-\text{Sin}[\theta]^2}}\right]\right)\left(\pi+\text{ArcCos}\left[\sqrt{\frac{1}{2}+\frac{1}{2}\sqrt{1-\text{Sin}[\theta]^2}}\right]\right)\right)}\right]\right\}\right\}$$

$$c:=2.99792458\left(10^8\right)$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == r, v\right]$$

$$\text{Solve}\left[\frac{r \sqrt{1 - \left(\frac{v^2}{c^2}\right)} \sqrt{\pi^2 - \text{ArcCos}\left[\sqrt{\frac{1}{2} + \frac{1}{2}} \sqrt{1 - \text{Sin}\left[\theta / \sqrt{1 - \left(\frac{v^2}{c^2}\right)}\right]^2}\right]^2}}{\pi} == r \text{Sin}[\beta], v\right]$$

Solve::tdep : The equations appear to involve the variables to be solved for in an essentially non-algebraic way. >>

$$\text{Solve}\left[\frac{1}{\pi} r \sqrt{1 - 1.11265 \times 10^{-17} v^2} \sqrt{\pi^2 - \text{ArcCos}\left[\sqrt{\frac{1}{2} + \frac{1}{2}} \sqrt{1 - \text{Sin}\left[\frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}}\right]^2}\right]^2} == r \text{Sin}[\beta], v\right]$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta] + 4\pi^2 \text{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \text{Sin}[\beta]^2 + 8\pi^2\theta \text{Sin}[\beta]^2)$$

$$\text{Solve}\left[\frac{\frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}}{2\pi r - r\theta - 2\pi \sqrt{r^2 - \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}}{2\pi}} == t, v\right]$$

Power::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == \eta, v\right]$$

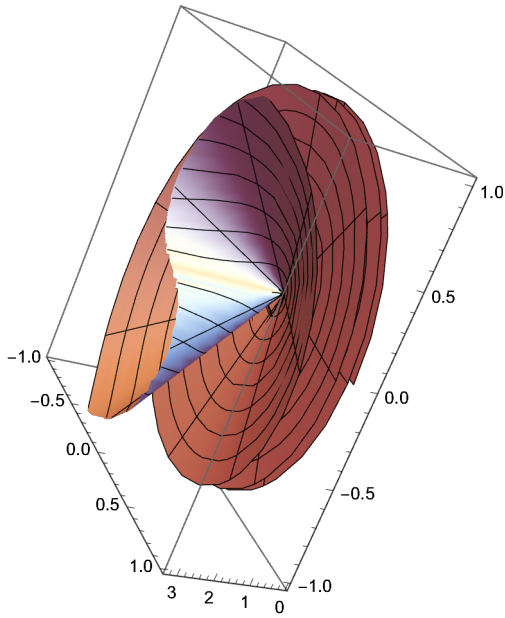
Set::write : Tag Times in  $\frac{\sqrt{\frac{\theta}{\sqrt{1 - \ll 24 \gg v^2}}} \sqrt{\frac{\ll 1 \gg}{\ll 1 \gg}} \sqrt{\frac{4\pi(\ll 1 \gg)}{\ll 1 \gg}} - \frac{\theta(\ll 1 \gg)}{\ll 1 \gg}}{2\pi}$  is Protected. >>

Solve::eqf :  $\eta$  is not a well-formed equation. >>

Solve[ $\eta, v$ ]

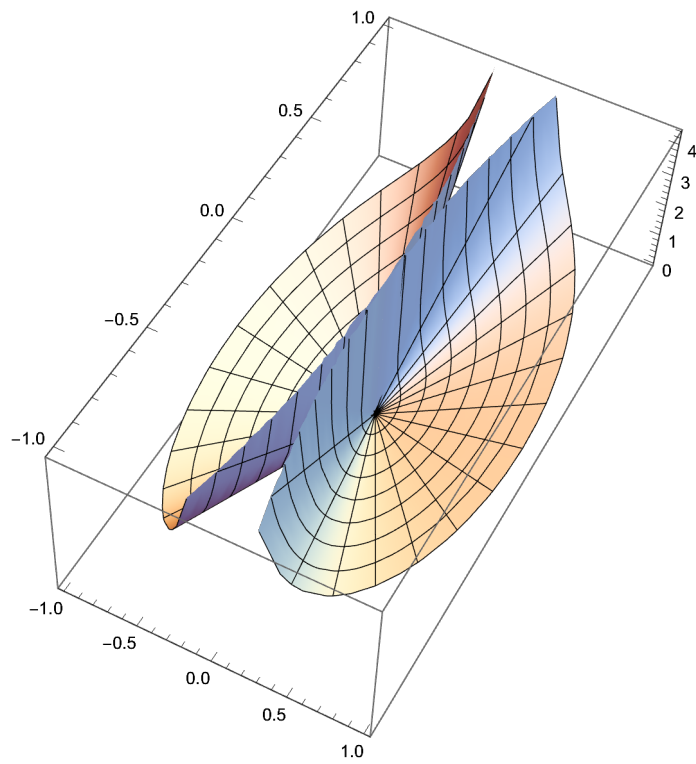
$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = r, v\right]$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi \sqrt{\left(\frac{2\pi r - r\theta}{2\pi}\right)^2 + \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

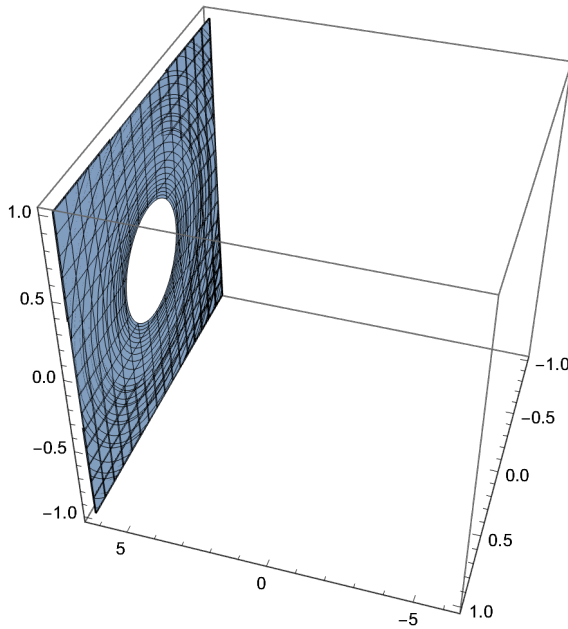


$$\text{RevolutionPlot3D}\left[\frac{2\pi \sqrt{\left(\frac{2\pi r - r\theta}{2\pi}\right)^2 + \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

$\text{RevolutionPlot3D}\left[\frac{1}{\sqrt{4\pi^2 - 4\pi^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right) + \left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}}\right.$   
 $2\pi\sqrt{\left(\left(\frac{2\pi r - r^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)}{2\pi}\right)^2 + \left(\frac{1}{2\pi}\left(\sqrt{4\pi r^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right) - r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}\right)\right)^2},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}\right]$



ContourPlot3D $\left[\frac{2 \pi \sqrt{x^2 + (y)^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{x, -1, 1\}, \{y, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$z == r \cos[\beta]$$

$$\text{Solve}\left[r == \frac{2 \pi \sqrt{\left(\frac{2 \pi r - r \theta}{2 \pi}\right)^2 + y^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, r\right]$$

{}

$$\text{Solve}\left[r == \sqrt{\frac{2 \pi r - r \theta}{2 \pi}^2 + y^2} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$$

{}

$$\beta == \text{ArcCos}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} / r\right]$$

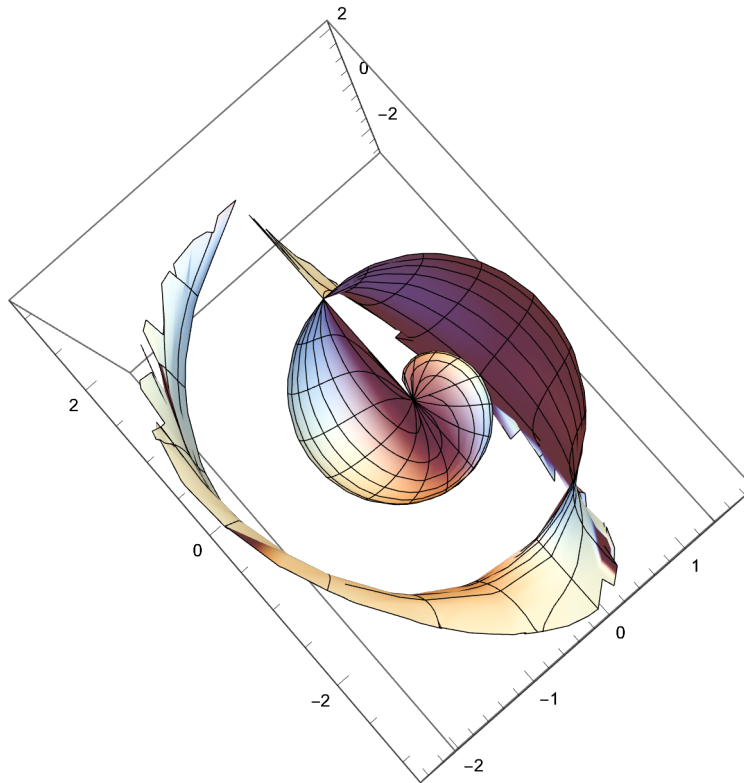
$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == r \sin[\beta] \cos[\phi], \phi\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\phi \rightarrow -\text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}, \left\{\phi \rightarrow \text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}\right\}$$



`SphericalPlot3D[ArcCos[ $\frac{(2\pi - \theta) \text{Csc}[\beta]}{2\pi}$ ], {\theta, -2\pi, 2\pi}, {\beta, -\pi/2, \pi/2}]`

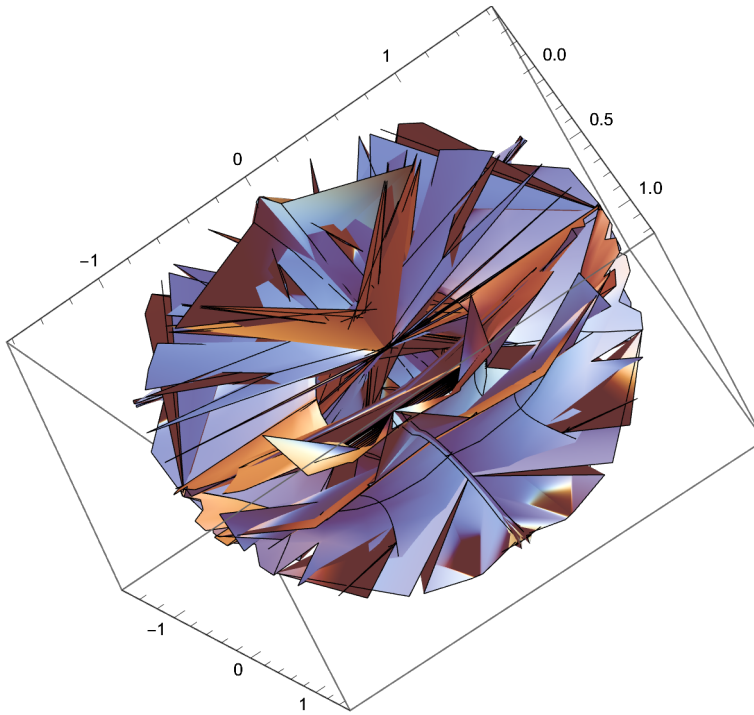


`Solve[ $\frac{2\pi r - r\theta}{2\pi} == r \text{Sin}[\beta] \text{Cos}[\phi], \beta]$`

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

`{ {  $\beta \rightarrow \text{ArcSin}\left[\frac{(2\pi - \theta) \text{Sec}[\phi]}{2\pi}\right]$  } }`

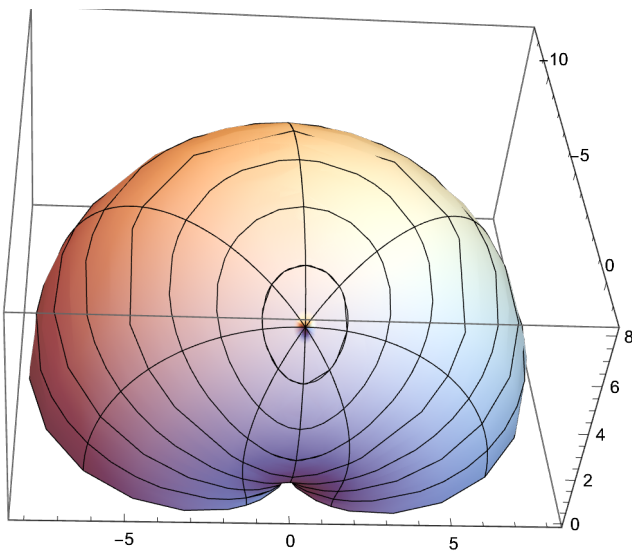
`SphericalPlot3D[ArcSin[ $\frac{(2\pi - \theta) \text{Sec}[\phi]}{2\pi}$ ], {\theta, -2\pi, 2\pi}, {\phi, -\pi, \pi}]`

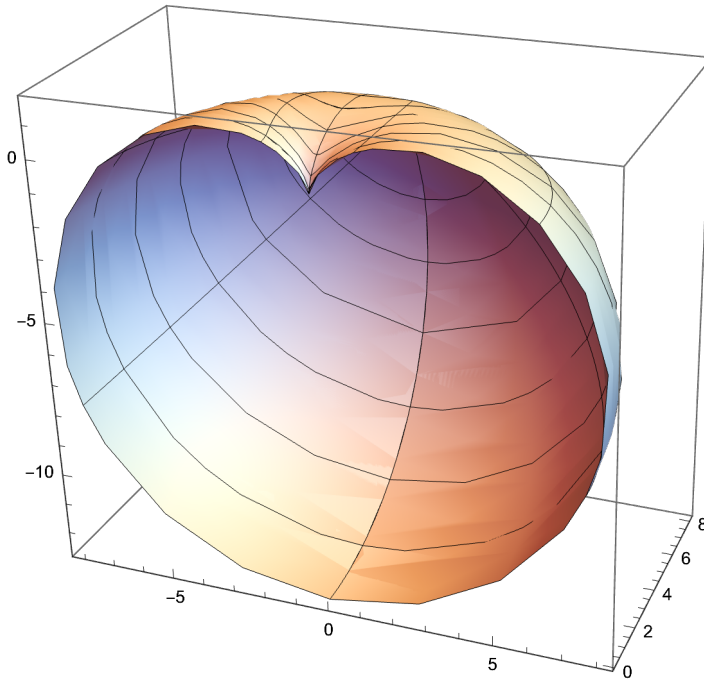


`Solve[ $\frac{2\pi r - r\theta}{2\pi} = r \sin[\beta] \cos[\phi], \theta]$`

`{{\theta \to -2\pi (-1 + \cos[\phi] \sin[\beta])}}`

`SphericalPlot3D[-2\pi (-1 + \cos[\phi] \sin[\beta]), {\beta, -\pi/2, \pi/2}, {\phi, -2\pi, 2\pi}]`





$$r := \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} = r \sin[\beta] \cos[\phi], \phi\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\phi \rightarrow -\text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}, \left\{\phi \rightarrow \text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}\right\}$$

$$\text{Solve}\left[\frac{2 \pi r - r 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2 \pi} = r \sin[\beta] \cos[\phi], \phi\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\phi \rightarrow -\text{ArcCos}\left[-\csc[\beta] \sqrt{1 - \sin[\beta]^2}\right]\right\}, \left\{\phi \rightarrow \text{ArcCos}\left[-\csc[\beta] \sqrt{1 - \sin[\beta]^2}\right]\right\}\right\}$$

$$\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

$$r = \sqrt{x^2 + y^2 + z^2} = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2} =$$

$$\sqrt{(r \sin[\theta] \cos[\phi])^2 + (r \sin[\theta] \sin[\phi])^2 + (r \cos[\theta])^2}$$

$$\sqrt{(r \sin[\theta] \cos[\phi])^2 + (r \sin[\theta] \sin[\phi])^2 + (r \cos[\theta])^2} = r$$

$$\text{Solve}[r == \sqrt{x^2 + y^2 + z^2}, z]$$

$$\left\{ \left\{ z \rightarrow -\frac{1}{2} \sqrt{\left( -4x^2 - 4y^2 + \frac{1}{(2\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)(4\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)^2(4\pi - \theta)} - \frac{4\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(4\pi - \theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi - \theta)^2} + \frac{\sin[\beta]^2}{(4\pi - \theta)\theta} \right)} \right\}, \right.$$

$$\left. \left\{ z \rightarrow \frac{1}{2} \sqrt{\left( -4x^2 - 4y^2 + \frac{1}{(2\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)(4\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)^2(4\pi - \theta)} - \frac{4\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(4\pi - \theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi - \theta)^2} + \frac{\sin[\beta]^2}{(4\pi - \theta)\theta} \right)} \right\} \right\}$$

$$\text{Solve}[r == \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, y]$$

{{}}

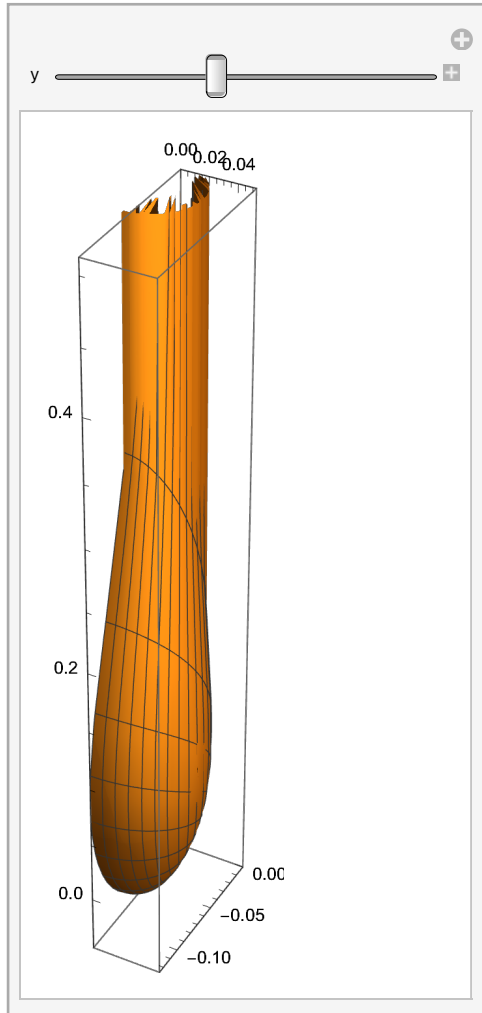
$$\text{Solve}[r == \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, x]$$

{{}}

$$\text{Solve}[r == \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, x]$$

$$\begin{aligned}
& \text{Solve} \left[ \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \right. \\
& \quad \left. \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}^2, x \right] \\
& \left\{ \left\{ x \rightarrow -\frac{\sqrt{1 - 16\pi^2 y^2 - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta}}}{4\pi} \right\}, \right. \\
& \quad \left. \left\{ x \rightarrow \frac{\sqrt{1 - 16\pi^2 y^2 - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta}}}{4\pi} \right\} \right\}
\end{aligned}$$

Manipulate[  
 SphericalPlot3D[ $\frac{\sqrt{1 - 16 \pi^2 y^2 - \frac{\sqrt{(4 \pi - \theta) \theta} \sin[\beta]}{4 \pi - \theta}} - \frac{\sqrt{(4 \pi - \theta) \theta} \sin[\beta]}{\theta} + \frac{\pi \sin[\beta]^2}{4 \pi - \theta} + \frac{\pi \sin[\beta]^2}{\theta}}{4 \pi}$ ,  
 { $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }, { $\beta$ ,  $-\pi / 2$ ,  $\pi / 2$ }, { $y$ ,  $-1$ ,  $1$ }]

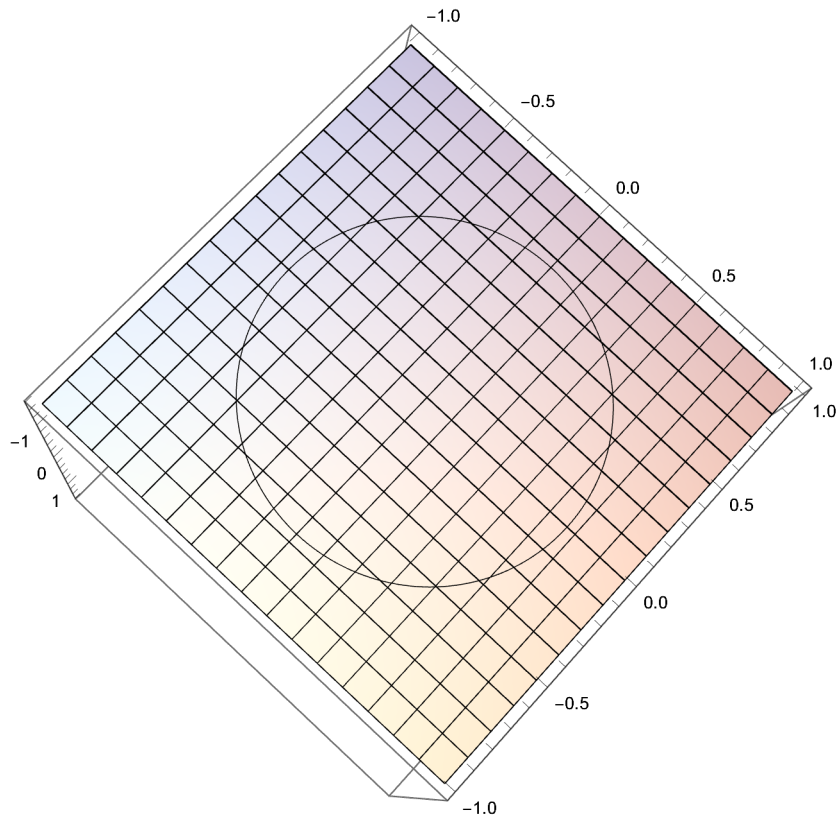


$$\begin{aligned}
& \text{Solve} \left[ \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \right. \\
& \quad \left. \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}^2, x \right] \\
& \left\{ \left\{ x \rightarrow -\frac{1}{4\pi} \left( \sqrt{-16\pi^2 y^2 + \frac{4\pi^2}{(2\pi-\theta)^2} - \right. \right. \right. \\
& \quad 16\pi r^2\theta + 4r^2\theta^2 - \frac{4\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)^2} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \\
& \quad \left. \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \frac{4\pi^2\sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta} \right) \right\}, \\
& \left\{ x \rightarrow \frac{1}{4\pi} \left( \sqrt{-16\pi^2 y^2 + \frac{4\pi^2}{(2\pi-\theta)^2} - 16\pi r^2\theta + 4r^2\theta^2 - \frac{4\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)^2} - \right. \right. \\
& \quad \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \\
& \quad \left. \left. \frac{4\pi^2\sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta} \right) \right\} \right\} \\
& \frac{1}{2} \sqrt{\left( -4x^2 - 4y^2 + \frac{1}{(2\pi-\theta)^2} - \frac{2\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)(4\pi-\theta)^2} - \right. \\
& \quad \left. \frac{2\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)^2(4\pi-\theta)} - \frac{4\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(4\pi-\theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\sin[\beta]^2}{(4\pi-\theta)\theta} \right)} \\
& \theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)
\end{aligned}$$

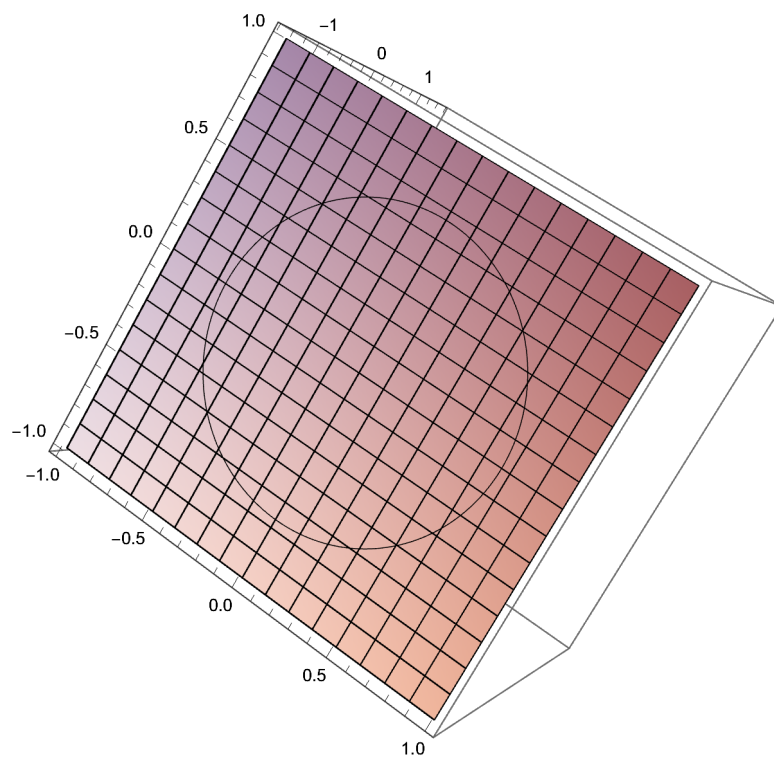
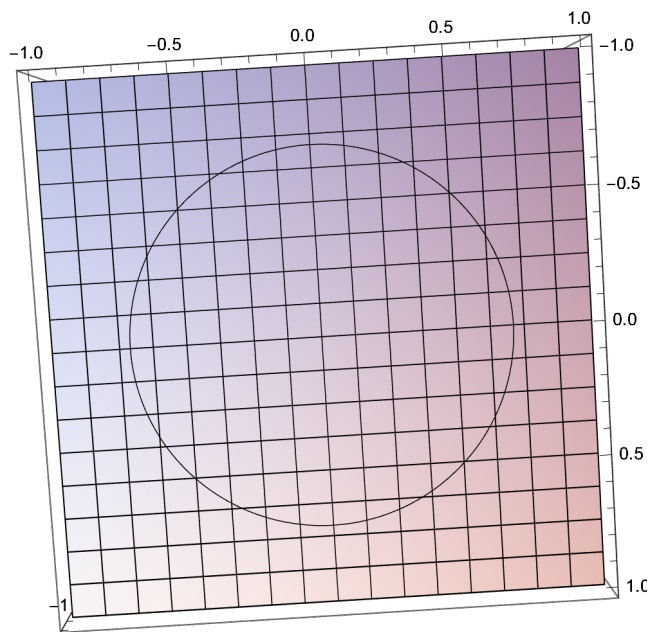
ContourPlot3D[

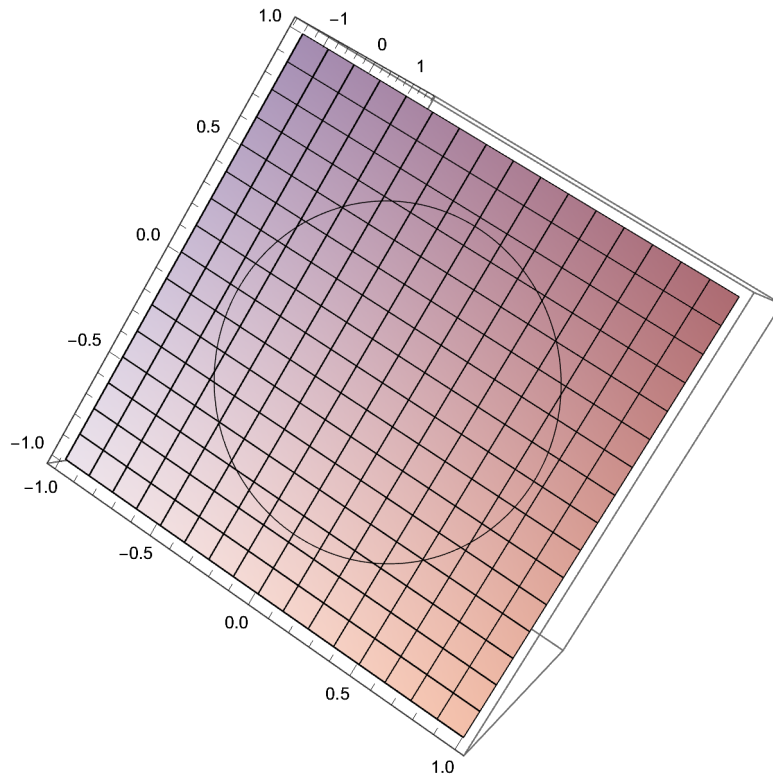
$$\frac{1}{2} \sqrt{\left( -4x^2 - 4y^2 + \frac{1}{(2\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta}\sin[\beta]}{(2\pi - \theta)(4\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta}\sin[\beta]}{(2\pi - \theta)^2(4\pi - \theta)} - \frac{4\sqrt{(4\pi - \theta)\theta}\sin[\beta]}{(4\pi - \theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi - \theta)^2} + \frac{\sin[\beta]^2}{(4\pi - \theta)\theta} \right)},$$

{x, -1, 1}, {y, -1, 1}, {\beta, -\pi/2, \pi/2}]

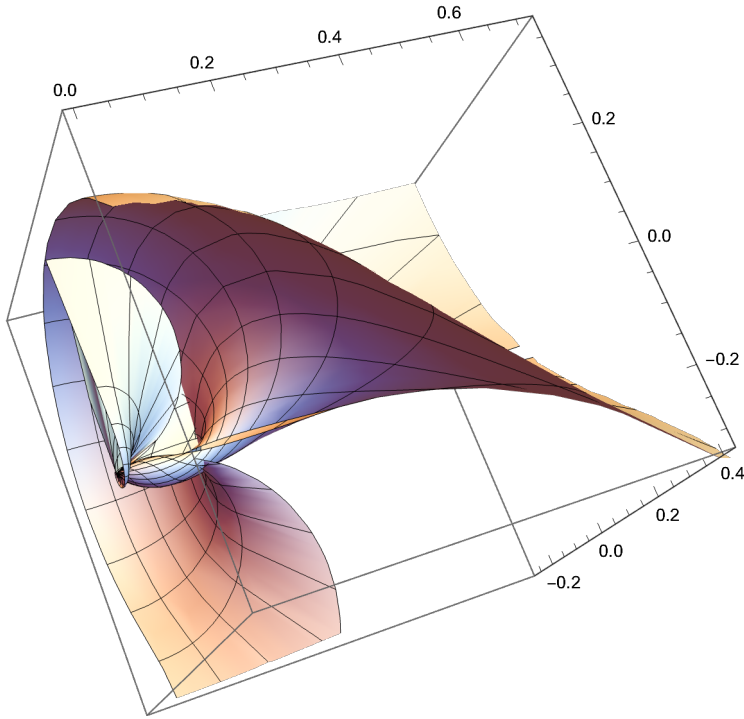






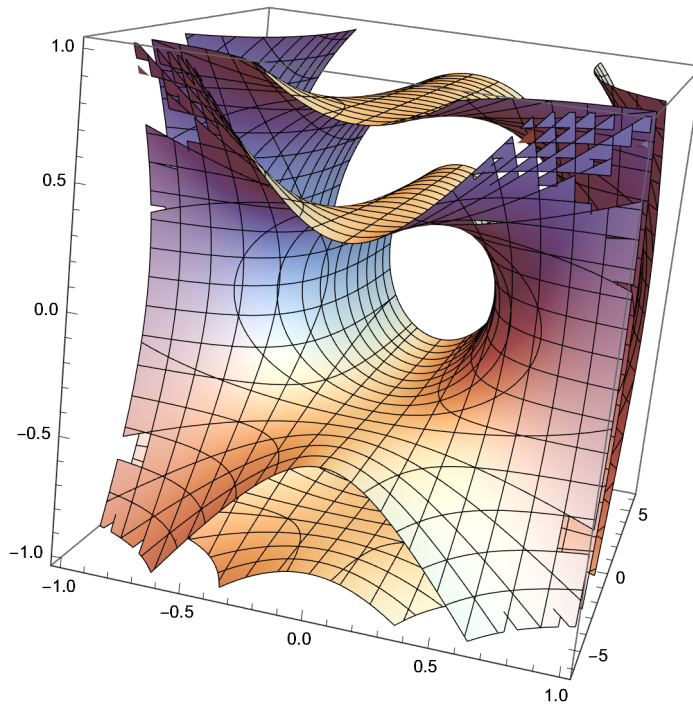


`SphericalPlot3D` $\left[\sqrt{\left(\left(r \sin[\beta] \cos\left[\text{ArcCos}\left[\frac{(2 \pi - \theta) \text{Csc}[\beta]}{2 \pi}\right]\right)\right)^2 + \left(r \sin[\beta] \sin\left[\text{ArcCos}\left[\frac{(2 \pi - \theta) \text{Csc}[\beta]}{2 \pi}\right]\right)\right)^2 + (r \cos[\beta])^2}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}\right]$



`ContourPlot3D` $\left[\sqrt{x^2 + y^2 + z^2}, \{x, -1, 1\}, \{y, -2 \pi, 2 \pi\}, \{z, -1, 1\}\right]$

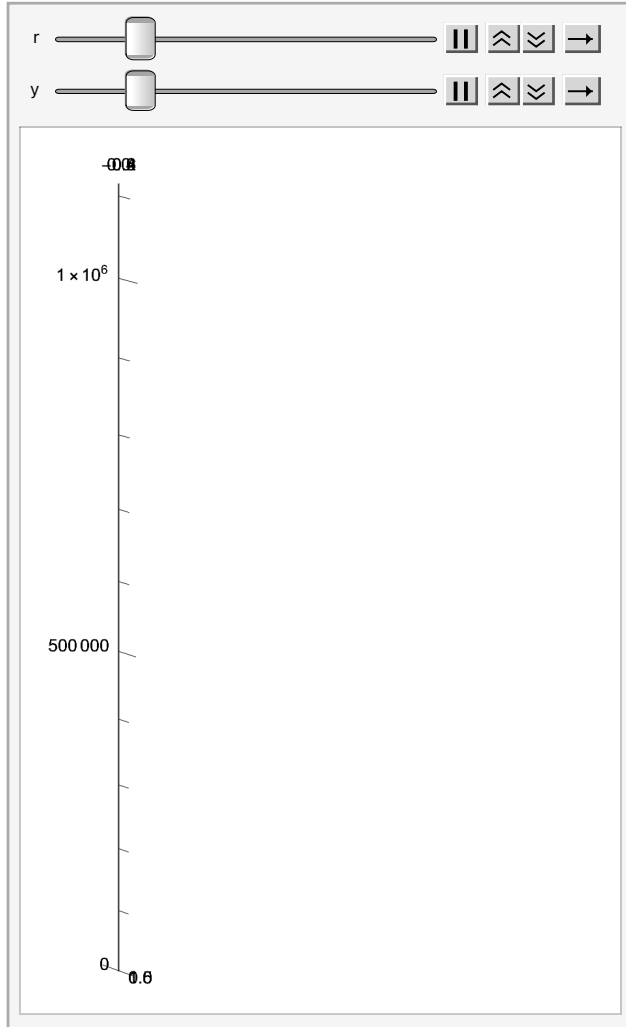
ContourPlot3D $\left[\sqrt{r^2 + x^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{x, -1, 1\}\right]$



ContourPlot3D $\left[\sqrt{r^2 + x^2 + z^2}, \{r, -1, 1\}, \{z, -1, 1\}, \{x, -1, 1\}\right]$

`Animate[SphericalPlot3D[`  

$$\frac{1}{4\pi} \left( \sqrt{-16\pi^2 y^2 + \frac{4\pi^2}{(2\pi-\theta)^2} - 16\pi r^2 \theta + 4r^2 \theta^2 - \frac{4\pi \sqrt{(4\pi-\theta)\theta} \sin[\beta]}{(2\pi-\theta)^2} - \frac{\sqrt{(4\pi-\theta)\theta} \sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta} \sin[\beta]}{\theta} + \frac{4\pi^2 \sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\pi \sin[\beta]^2}{4\pi-\theta} + \frac{\pi \sin[\beta]^2}{\theta}} \right),$$
  
`{θ, -2π, 2π}, {β, -π/2, π/2}], {r, -1, 1}, {y, -1, 1}]`



$$\text{Solve}\left[r == \sqrt{\left(x^2 + y^2 + \left(\frac{1}{4\pi^2} \left(\sqrt{\left(64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta}\right)}\right)^2\right)}, y\right]$$

$$\left\{\left\{y \rightarrow -\frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} + \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta}\right)}\right\},\right.$$

$$\left.\left\{y \rightarrow \frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} + \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta}\right)}\right\}\right\}$$

Export["lldradius.avi"]

Export["lldradius.avi",

$$\text{Animate}\left[\text{Plot3D}\left[\frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} + \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta}\right)}\right],\right.$$

$$\left.\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right], \{x, -1.3, 1.3\}\right]$$

lldradius.avi

Manipulate[

$$\text{Plot3D}\left[\frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} + \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta}\right)}\right),\right.$$

$$\left.\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right], \{x, -1, 1\}]$$

$$\sqrt{x^2 + y^2 + z^2}$$

$$\text{Solve}\left[\sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}^2 == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\sqrt{\frac{\pi}{2}} \sqrt{\frac{2\pi\eta^2}{(4\pi - \theta)^2} - \frac{2x^2}{4\pi - \theta} - \frac{2y^2}{4\pi - \theta} + \frac{\eta^2}{4\pi - \theta} + \frac{2\pi\eta^2}{\theta^2} - \frac{2x^2}{\theta} - \frac{2y^2}{\theta} + \frac{\eta^2}{\theta}}\right\},\right.$$

$$\left.\left\{r \rightarrow \sqrt{\frac{\pi}{2}} \sqrt{\frac{2\pi\eta^2}{(4\pi - \theta)^2} - \frac{2x^2}{4\pi - \theta} - \frac{2y^2}{4\pi - \theta} + \frac{\eta^2}{4\pi - \theta} + \frac{2\pi\eta^2}{\theta^2} - \frac{2x^2}{\theta} - \frac{2y^2}{\theta} + \frac{\eta^2}{\theta}}\right\}\right\}$$

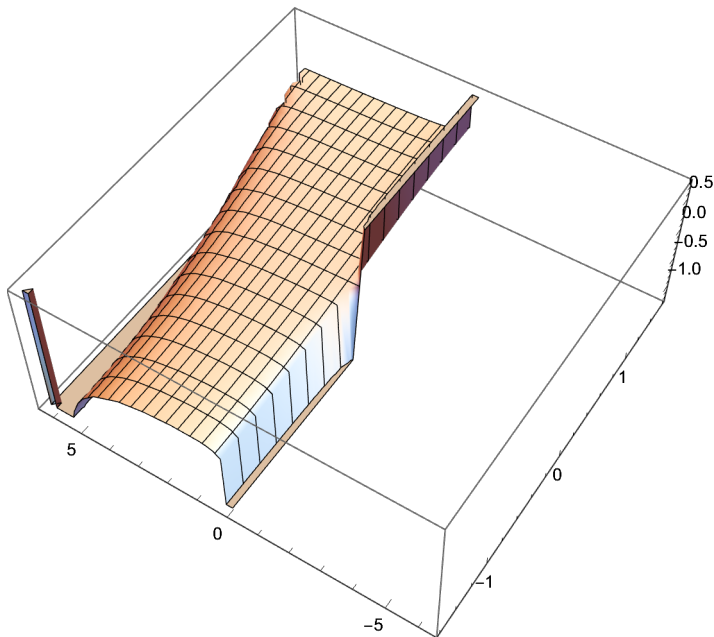
$$\sqrt{\frac{\pi}{2}} \sqrt{\frac{2\pi\eta^2}{(4\pi - \theta)^2} - \frac{2x^2}{4\pi - \theta} - \frac{2y^2}{4\pi - \theta} + \frac{\eta^2}{4\pi - \theta} + \frac{2\pi\eta^2}{\theta^2} - \frac{2x^2}{\theta} - \frac{2y^2}{\theta} + \frac{\eta^2}{\theta}}$$

$$\text{Solve}\left[\frac{2\pi\sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}} ==\right.$$

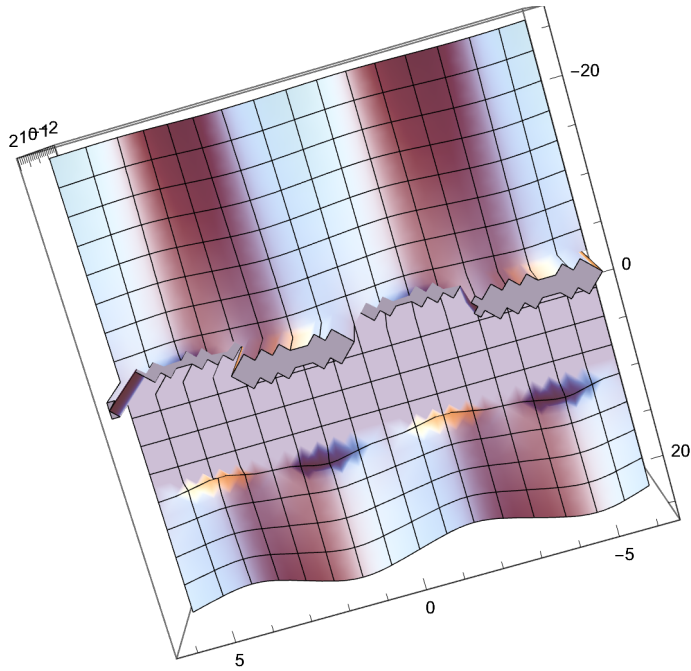
$$\text{Plot3D}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] +\right.\right.$$

$$\left.\left.4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right)\right/$$

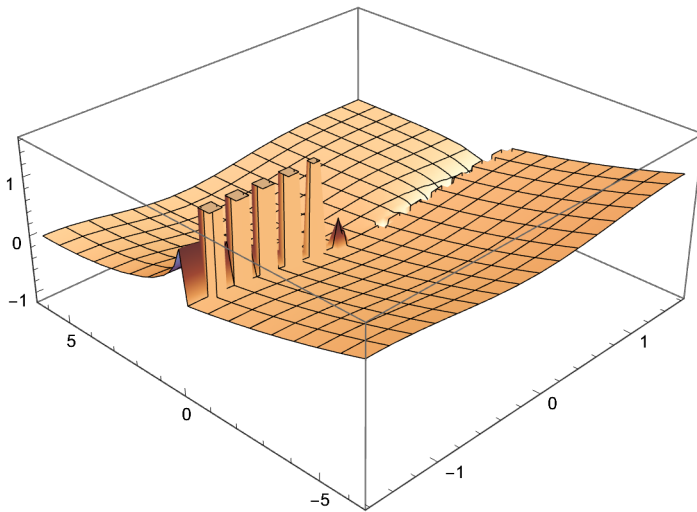
$$(16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



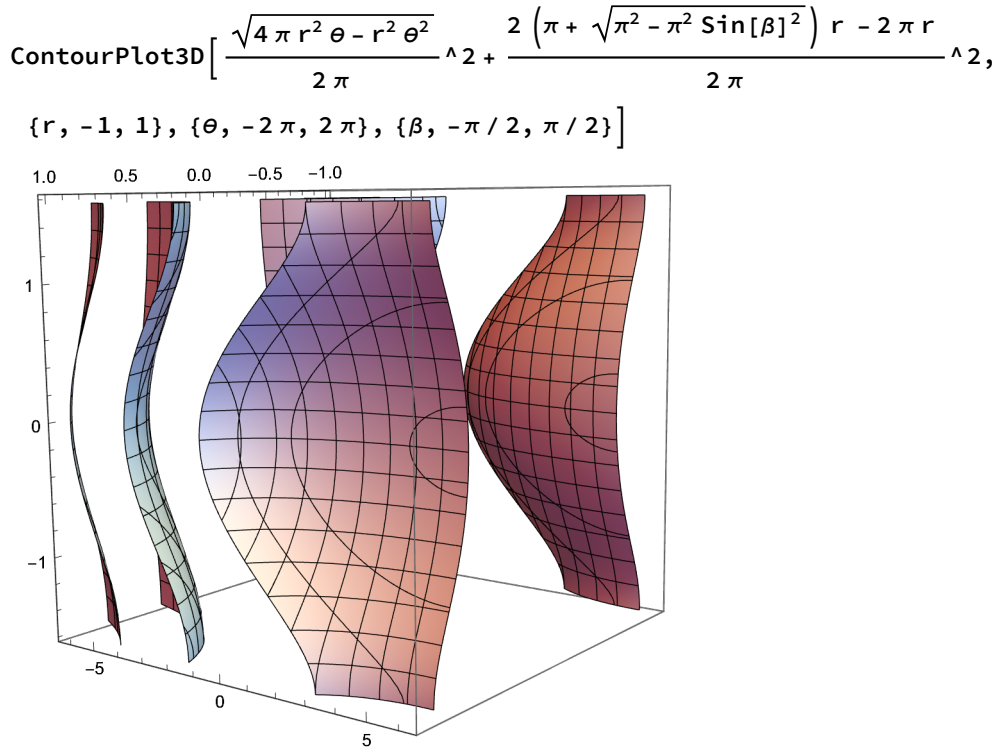
```
Plot3D[0.00633256 Im[-12.5664  $\theta$  +  $\theta^2$  + 6.28319 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ] +
39.4784 Sin[ $\beta$ ]^2 - (19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) / (12.5664 - 1.  $\theta$ ) -
(19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) /  $\theta$ ], { $\beta$ , -6.3, 6.3}, { $\theta$ , -26, 26}]
```



```
Plot3D[0.00633256 Re[-12.5664  $\theta$  +  $\theta^2$  + 6.28319 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ] +
39.4784 Sin[ $\beta$ ]^2 - (19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) / (12.5664 - 1.  $\theta$ ) -
(19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) /  $\theta$ ], { $\beta$ , - $\pi/2$ ,  $\pi/2$ }, { $\theta$ , -2 $\pi$ , 2 $\pi$ }]
```







## Addendum No. 1

# Addendum No. 1

Visualizing Multiple Possible Equations for Non-Relativistic Velocity with Constant Initial Radius through A Transition

All of these functions come from just a single expression. Think about how many different visualizations of a single function there are in terms of our system.

$$\left\{\left\{\theta \rightarrow 2\pi\left(1 - \sqrt{1 - \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\pi\left(1 + \sqrt{1 - \sin[\beta]^2}\right)\right\}\right\}$$

$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \frac{2 \pi r}{\theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2}{3} \left(2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi\right)\right\},\right.$$

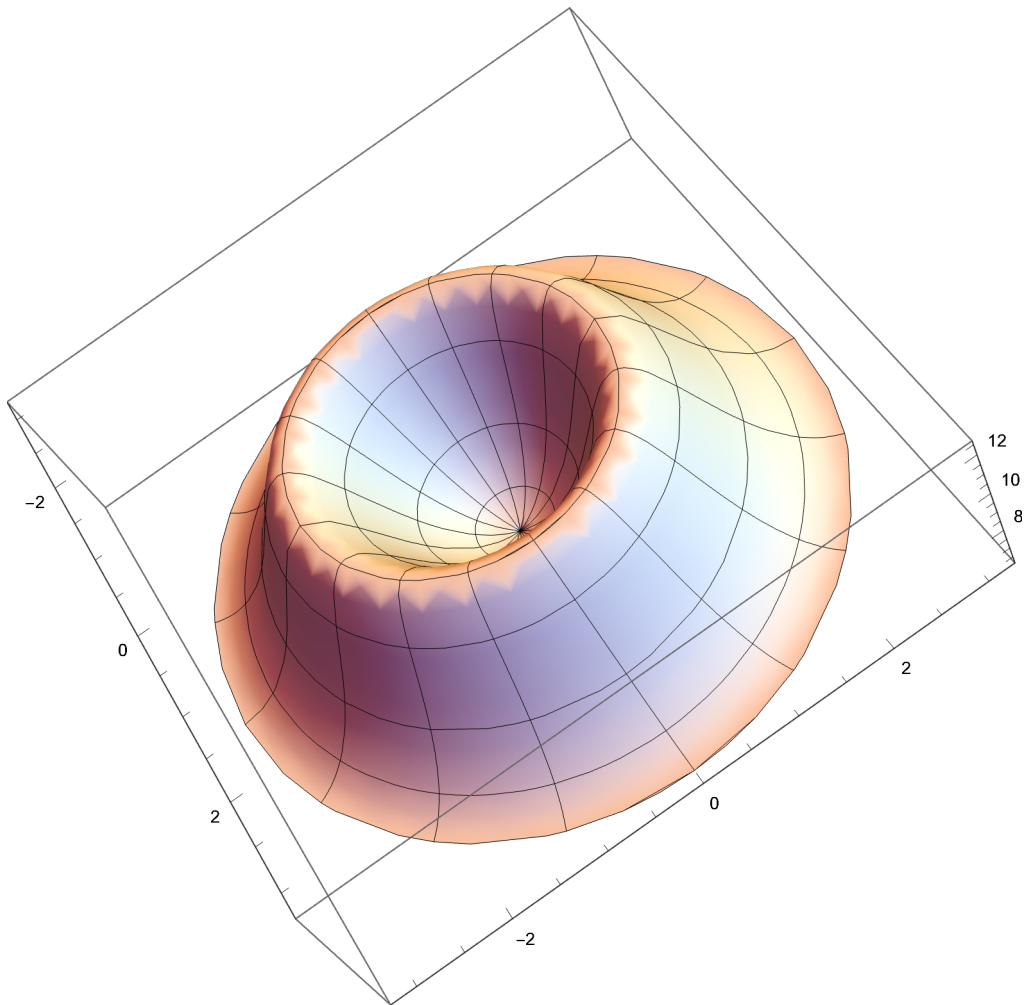
$$\left\{\theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi\right\},$$

$$\left\{\theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 - i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 + i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi\right\}\}$$

$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 2 \pi (1 + \sqrt{1 - \text{Sin}[\beta]^2})}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \frac{2 \pi r}{\theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{8 \pi}{3 + \text{Cos}[2 \beta]}\right\}\right\}$$

RevolutionPlot3D $\left[\frac{8 \pi}{3 + \text{Cos}[2 \beta]}, \{\beta, -\pi, \pi\}\right]$

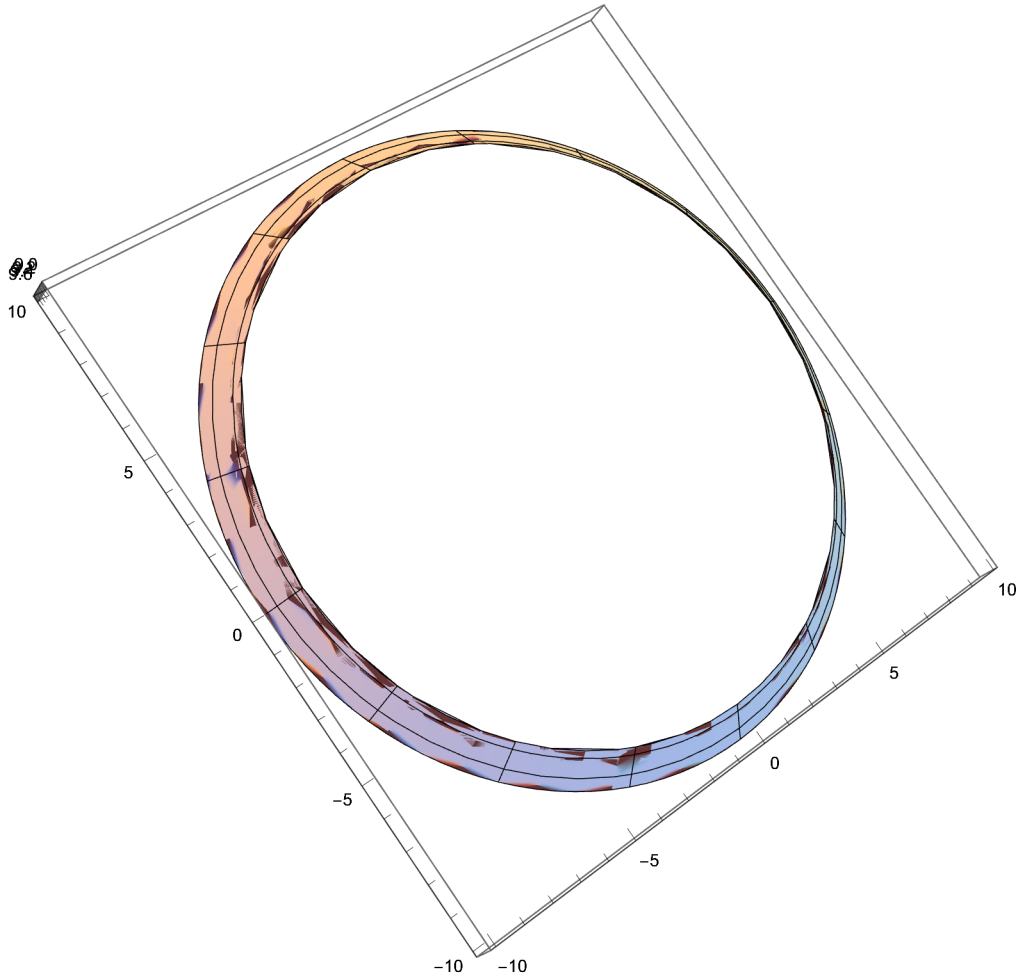


$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)}{2 \sqrt{4 \pi r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right) - r^2 \theta^2}} = \frac{2 \pi r}{\theta}, \theta\right]$$

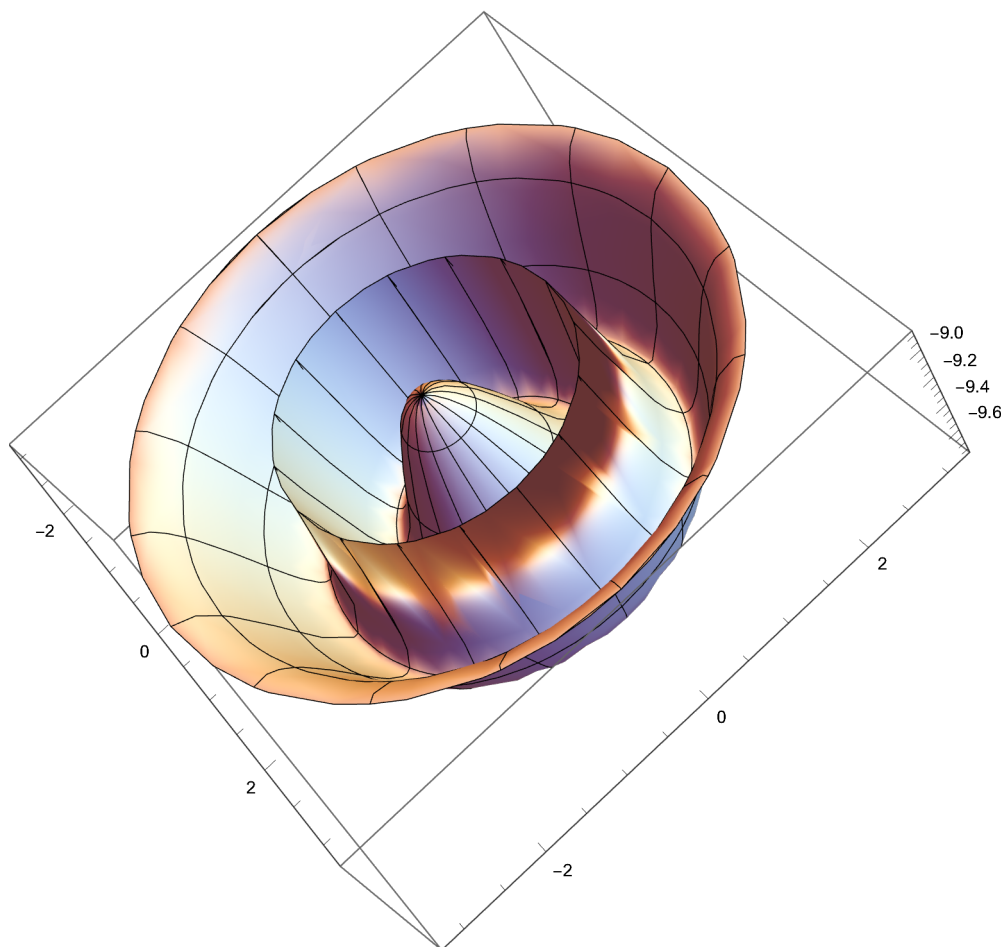
$$\left\{\left\{\theta \rightarrow -\frac{2 \sqrt{2} \sqrt{-\pi^2 - \pi^2 \sqrt{1 - \text{Sin}[\beta]^2}}}{\sqrt{-2 + \text{Sin}[\beta]^2}}\right\}, \left\{\theta \rightarrow \frac{2 \sqrt{2} \sqrt{-\pi^2 - \pi^2 \sqrt{1 - \text{Sin}[\beta]^2}}}{\sqrt{-2 + \text{Sin}[\beta]^2}}\right\}\right\}$$

`RevolutionPlot3D[`  

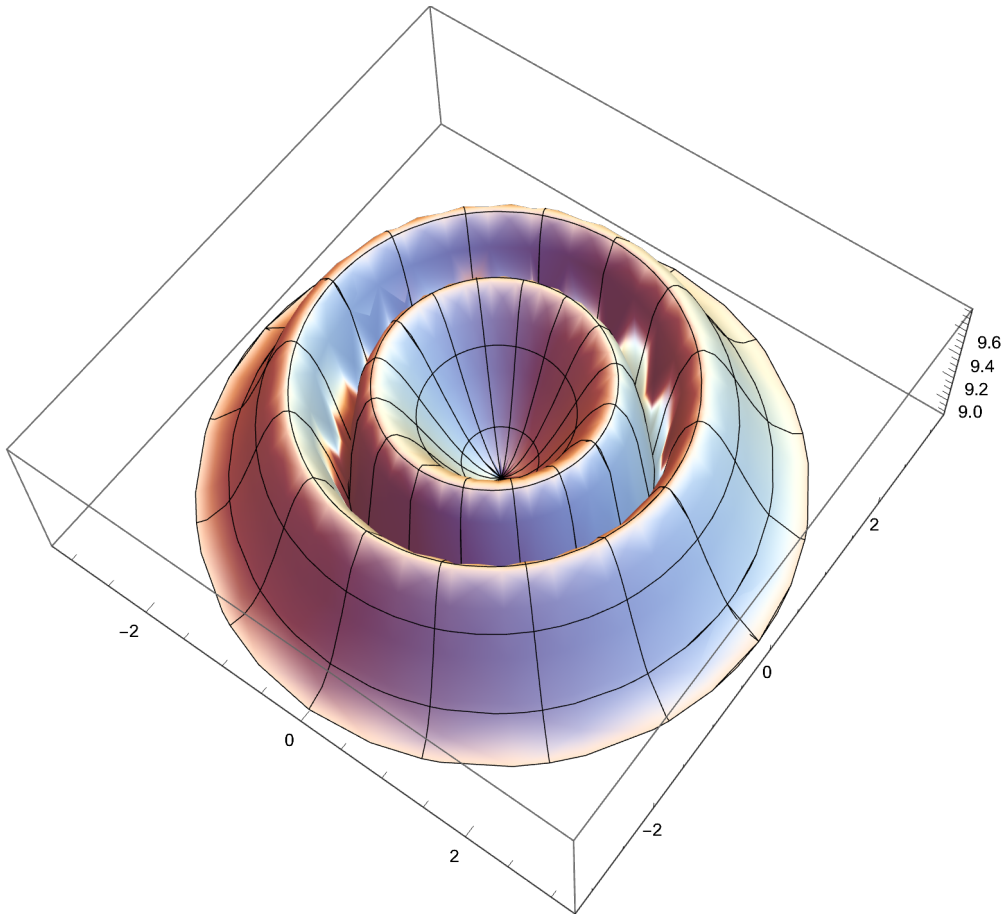
$$\left\{ -\frac{2\sqrt{2}\sqrt{-\pi^2-\pi^2}\sqrt{1-\sin[\beta]^2}}{\sqrt{-2+\sin[\beta]^2}}, \frac{2\sqrt{2}\sqrt{-\pi^2-\pi^2}\sqrt{1-\sin[\beta]^2}}{\sqrt{-2+\sin[\beta]^2}} \right\}, \{\beta, -\pi, \pi\}]$$



$\text{RevolutionPlot3D}\left[-\frac{2\sqrt{2}\sqrt{-\pi^2-\pi^2}\sqrt{1-\text{Sin}[\beta]^2}}{\sqrt{-2+\text{Sin}[\beta]^2}}, \{\beta, -\pi, \pi\}\right]$



RevolutionPlot3D $\left[\frac{2 \sqrt{2} \sqrt{-\pi^2 - \pi^2 \sqrt{1 - \text{Sin}[\beta]^2}}}{\sqrt{-2 + \text{Sin}[\beta]^2}}, \{\beta, -\pi, \pi\}\right]$



Solve $\left[\frac{4 \pi r^2 - 2 r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)}{2 \sqrt{4 \pi r^2 (\theta) - r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)^2}} = \frac{2 \pi r}{\theta}, \theta\right]$

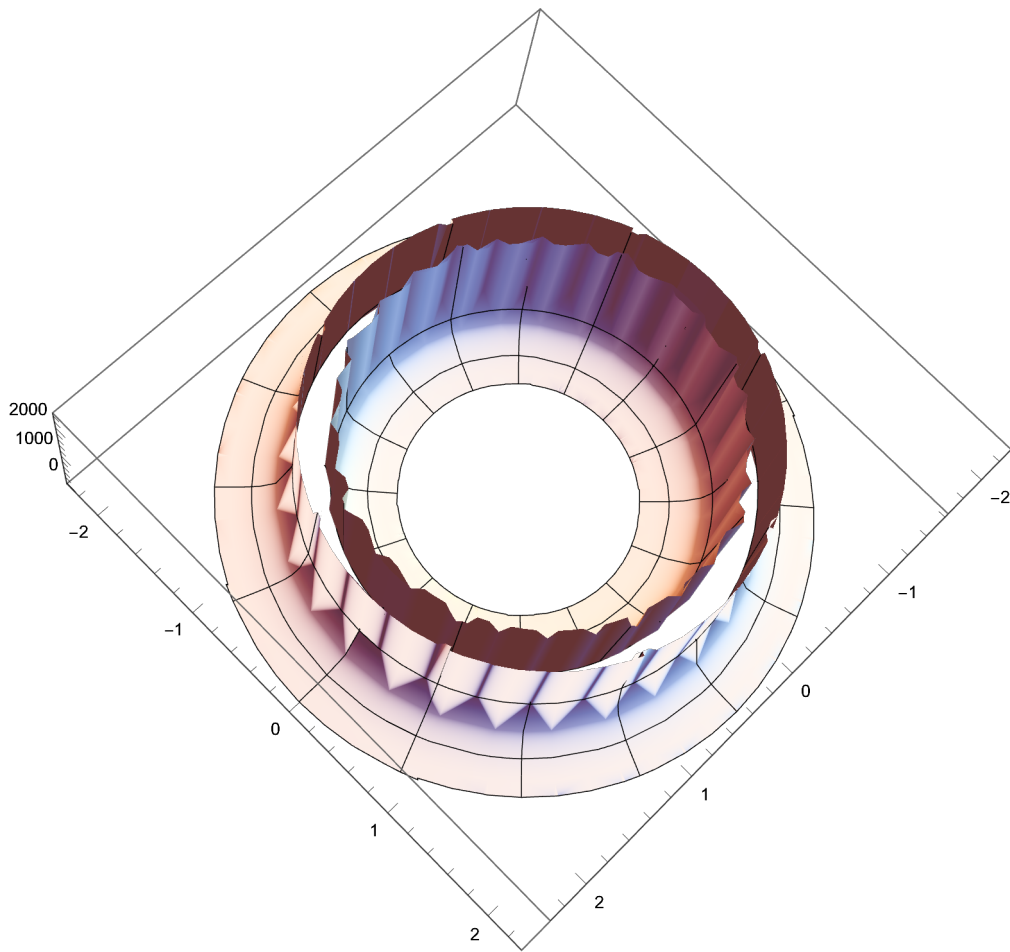
$\{\{\theta \rightarrow \text{ComplexInfinity}\},$

$\left\{\theta \rightarrow \frac{1}{2 (-1 + \text{Sin}[\beta]^2)} \left(-4 \pi - \sqrt{(16 \pi^2 - 4 (-1 + \text{Sin}[\beta]^2) (-8 \pi^2 + 4 \pi^2 \text{Sin}[\beta]^2 - 8 \pi^2 \sqrt{-(-1 + \text{Sin}[\beta]) (1 + \text{Sin}[\beta])})}\right)\right\},$

$\left\{\theta \rightarrow \frac{1}{2 (-1 + \text{Sin}[\beta]^2)} \left(-4 \pi + \sqrt{(16 \pi^2 - 4 (-1 + \text{Sin}[\beta]^2) (-8 \pi^2 + 4 \pi^2 \text{Sin}[\beta]^2 - 8 \pi^2 \sqrt{-(-1 + \text{Sin}[\beta]) (1 + \text{Sin}[\beta])})}\right)\right\}\right\}$

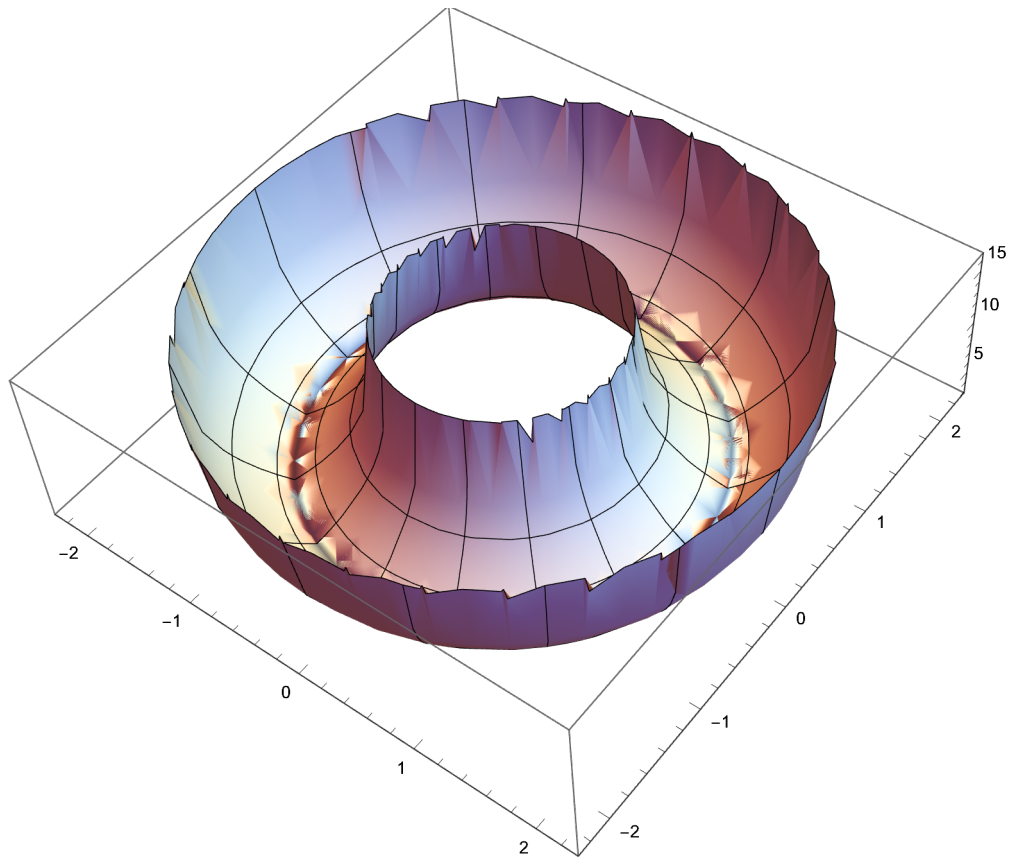
`RevolutionPlot3D[`  

$$\left( \frac{1}{2 (-1 + \sin[\beta]^2)} \left( -4 \pi - \sqrt{(16 \pi^2 - 4 (-1 + \sin[\beta]^2) (-8 \pi^2 + 4 \pi^2 \sin[\beta]^2 - 8 \pi^2 \sqrt{-(-1 + \sin[\beta]) (1 + \sin[\beta])})} \right) \right), \{\beta, -\pi, \pi\} \right]$$



`RevolutionPlot3D[`  

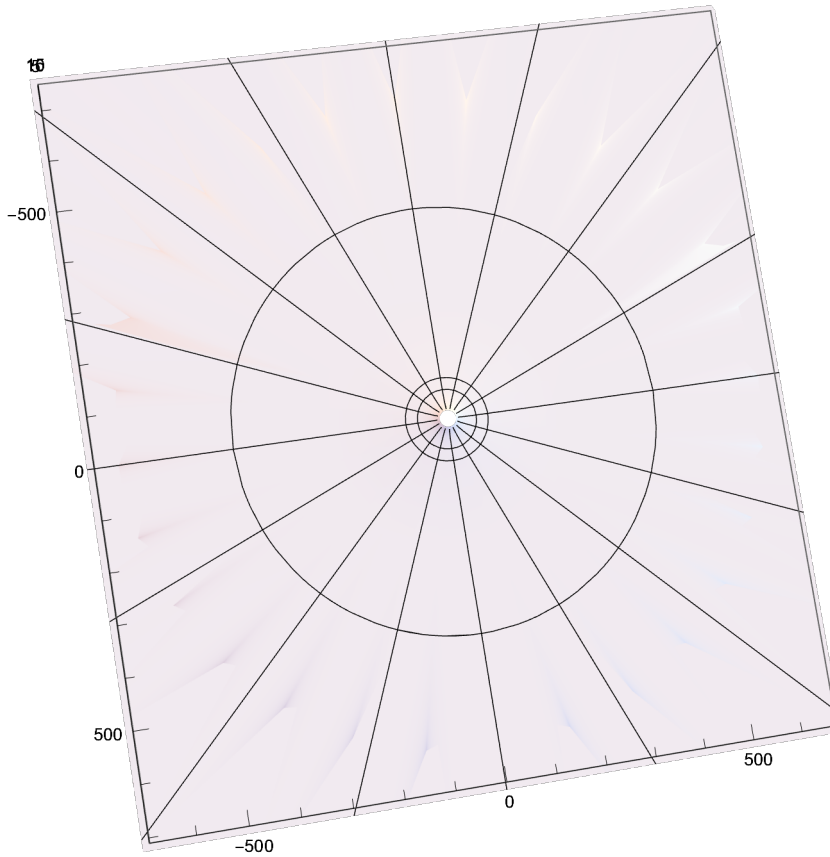
$$\left( \frac{1}{2 (-1 + \sin[\beta]^2)} \left( -4 \pi + \sqrt{(16 \pi^2 - 4 (-1 + \sin[\beta]^2) (-8 \pi^2 + 4 \pi^2 \sin[\beta]^2 - 8 \pi^2 \sqrt{-(-1 + \sin[\beta]) (1 + \sin[\beta])})} \right) \right), \{\beta, -\pi, \pi\} \right]$$





$$\text{RevolutionPlot3D}\left[\left\{\left(\frac{1}{2(-1+\sin[\beta]^2)}\left(-4\pi-\sqrt{\left(16\pi^2-4(-1+\sin[\beta]^2)\left(-8\pi^2+4\pi^2\sin[\beta]^2-8\pi^2\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])}\right)}\right)\right)\right),\right.\right.$$

$$\left.\left(\frac{1}{2(-1+\sin[\beta]^2)}\left(-4\pi+\sqrt{\left(16\pi^2-4(-1+\sin[\beta]^2)\left(-8\pi^2+4\pi^2\sin[\beta]^2-8\pi^2\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])}\right)}\right)\right)\right)\right\},\{\beta,-\pi,\pi\}]$$



$$\text{Solve}\left[\frac{4\pi r^2-2r^2\left(2\pi\left(1+\sqrt{1-\sin[\beta]^2}\right)\right)}{2\sqrt{4\pi r^2(\theta)-r^2(\theta)^2}}=\frac{2\pi r}{2\pi\left(1+\sqrt{1-\sin[\beta]^2}\right)},\theta\right]$$

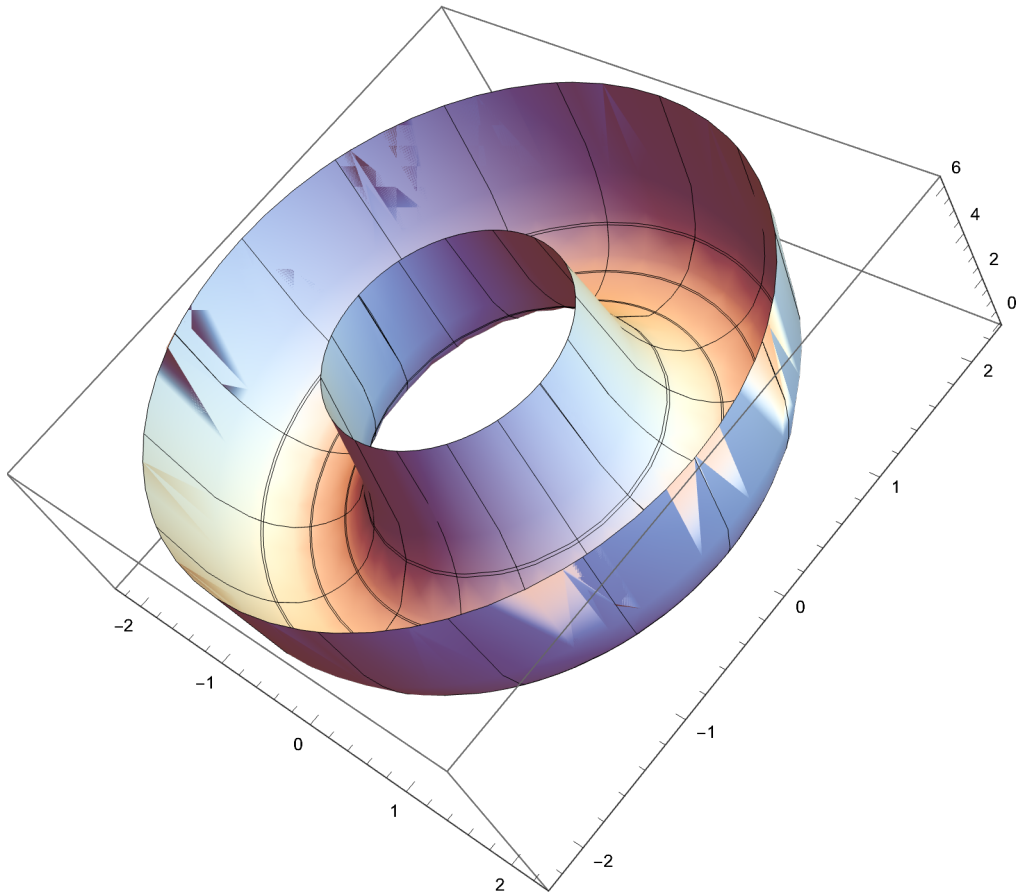
$$\left\{\left\{\theta\rightarrow\frac{1}{2}\left(4\pi-\sqrt{\left(16\pi^2+4\pi^2\left(-8+12\sin[\beta]^2-4\sin[\beta]^4-8\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])}+8\sin[\beta]^2\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])}\right)}\right)}\right)\right\},\right.$$

$$\left.\left\{\theta\rightarrow\frac{1}{2}\left(4\pi+\sqrt{\left(16\pi^2+4\pi^2\left(-8+12\sin[\beta]^2-4\sin[\beta]^4-8\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])}+8\sin[\beta]^2\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])}\right)}\right)}\right)\right\}\right\}$$

```

RevolutionPlot3D[
  
$$\frac{1}{2} \left( 4\pi - \sqrt{\left( 16\pi^2 + 4\pi^2 \left( -8 + 12\sin[\beta]^2 - 4\sin[\beta]^4 - 8\sqrt{-(-1+\sin[\beta]) (1+\sin[\beta])} + 8\sin[\beta]^2 \sqrt{-(-1+\sin[\beta]) (1+\sin[\beta])} \right) \right)} \right), \{\beta, -\pi, \pi\}$$

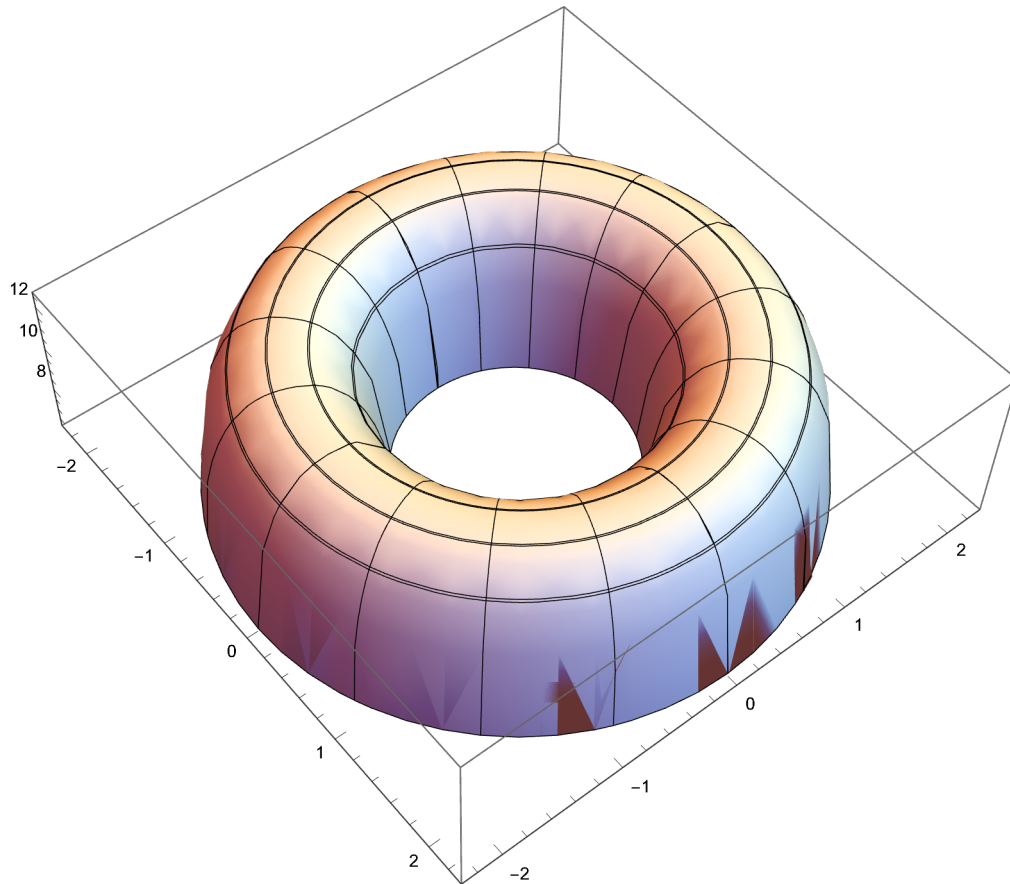
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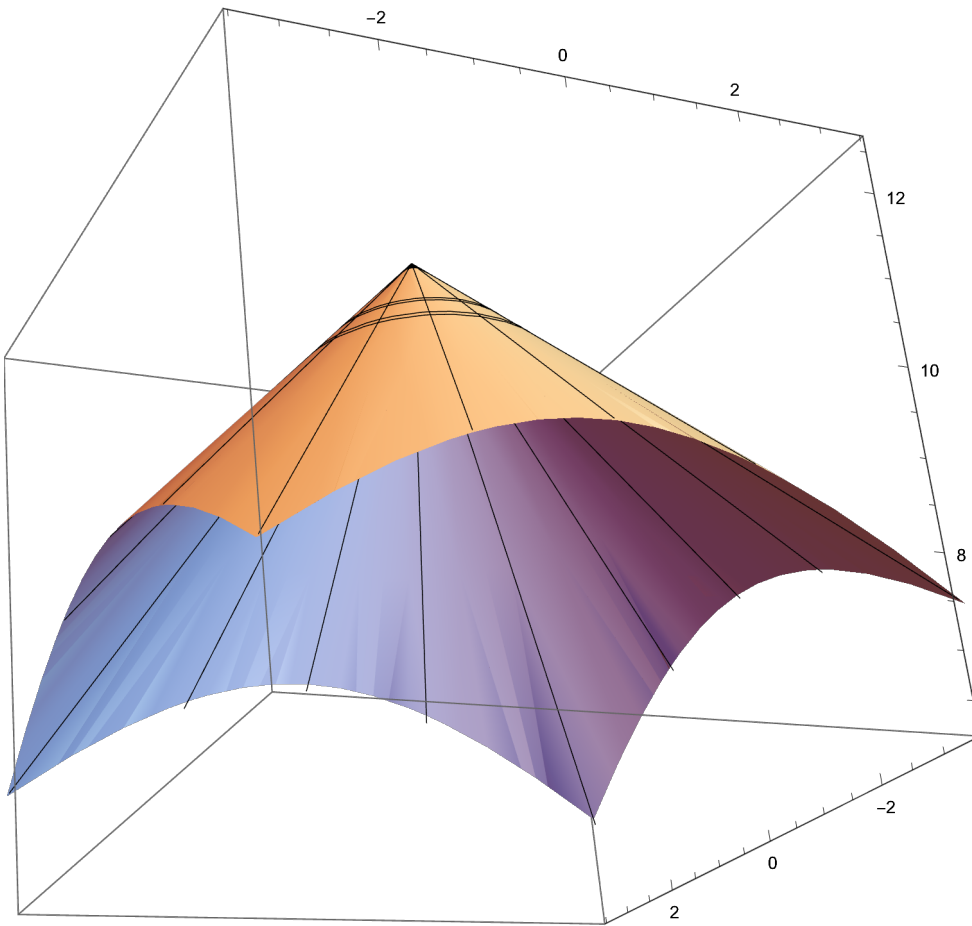
```

RevolutionPlot3D[
  
$$\frac{1}{2} \left( 4\pi + \sqrt{\left( 16\pi^2 + 4\pi^2 \left( -8 + 12\sin[\beta]^2 - 4\sin[\beta]^4 - 8\sqrt{-(-1+\sin[\beta])(1+\sin[\beta])} + 8\sin[\beta]^2 \sqrt{-(-1+\sin[\beta])(1+\sin[\beta])} \right) \right)} \right), \{\beta, -\pi, \pi\}$$

```

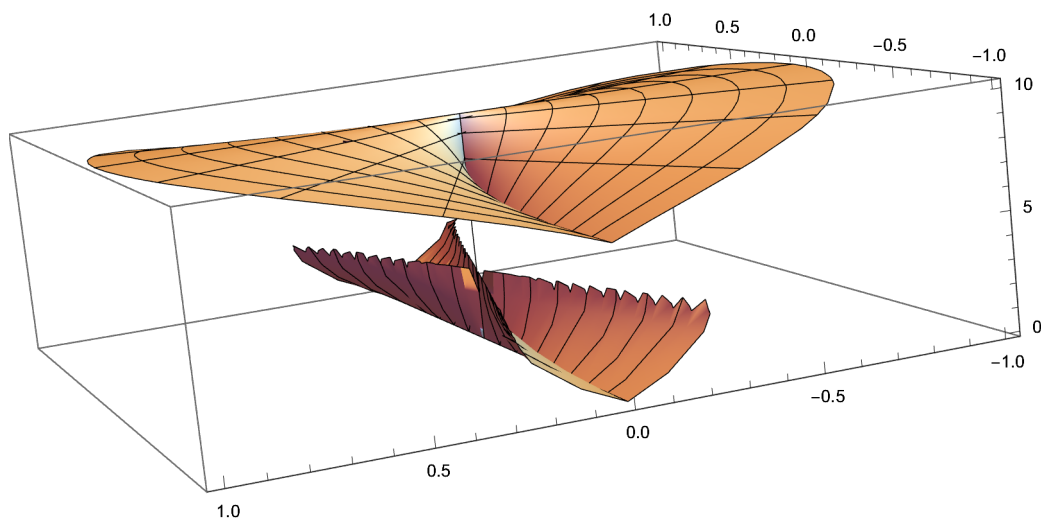


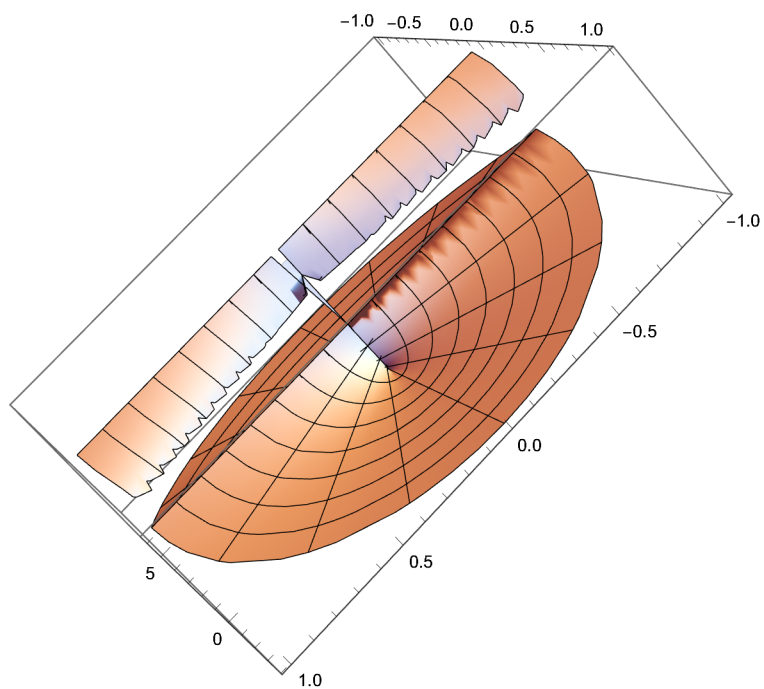
$\text{RevolutionPlot3D}\left[\right.$   
 $\left\{\left(\frac{1}{2}\left(4\pi - \sqrt{\left(16\pi^2 + 4\pi^2\left(-8 + 12\sin[\beta]^2 - 4\sin[\beta]^4 - 8\sqrt{-(-1 + \sin[\beta])\left(1 + \sin[\beta]\right)} + 8\sin[\beta]^2\sqrt{-(-1 + \sin[\beta])\left(1 + \sin[\beta]\right)}\right)}\right)\right),\right.$   
 $\left.\left(\frac{1}{2}\left(4\pi + \sqrt{\left(16\pi^2 + 4\pi^2\left(-8 + 12\sin[\beta]^2 - 4\sin[\beta]^4 - 8\sqrt{-(-1 + \sin[\beta])\left(1 + \sin[\beta]\right)} + 8\sin[\beta]^2\sqrt{-(-1 + \sin[\beta])\left(1 + \sin[\beta]\right)}\right)}\right)\right)\right\}, \{\beta, -\pi, \pi\}\right]$



$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2(\theta)}{2\sqrt{4\pi r^2\left(2\pi\left(1 + \sqrt{1 - \sin[\beta]^2}\right)\right) - r^2\left(2\pi\left(1 + \sqrt{1 - \sin[\beta]^2}\right)\right)^2}} = \frac{2\pi r}{(\theta)}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{\pi r - \sqrt{\pi^2 r^2 - 4\pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \left\{\theta \rightarrow \frac{\pi r + \sqrt{\pi^2 r^2 - 4\pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}\right\}$$

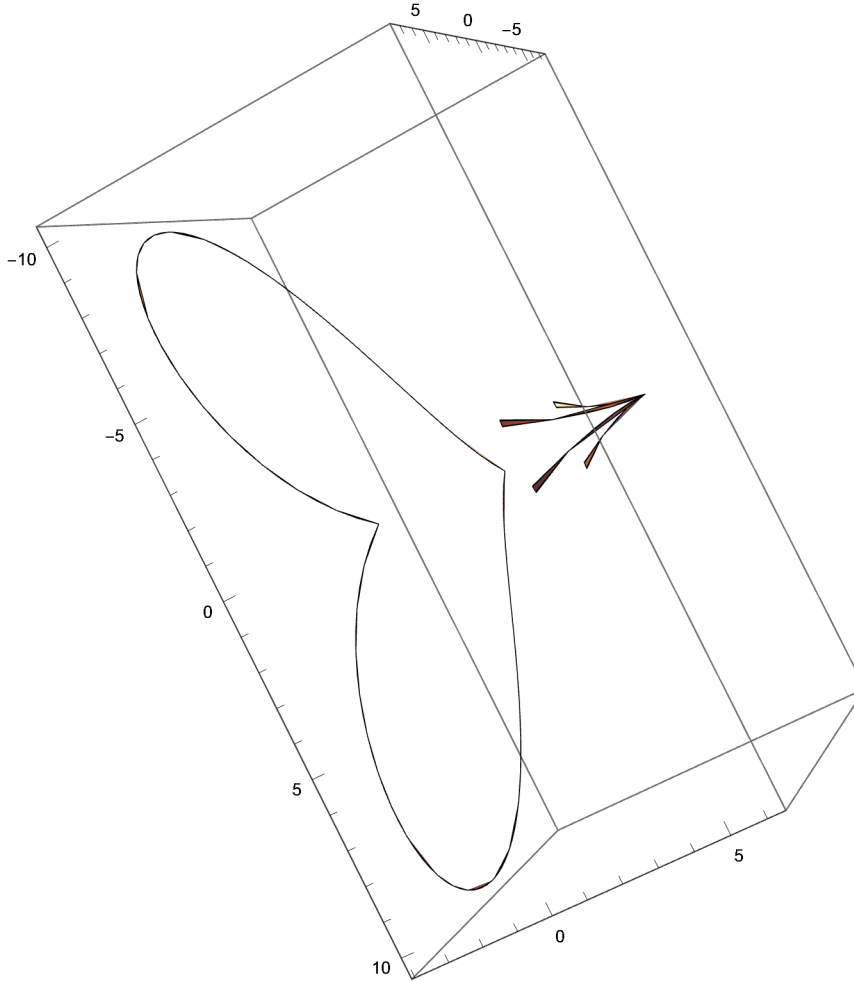
$$\text{RevolutionPlot3D}\left[\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$$


```

RevolutionPlot3D[{{
   $\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}$ ,  $\frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}$ 
},
{r, -1, 1}, {β, -π, π}]

```

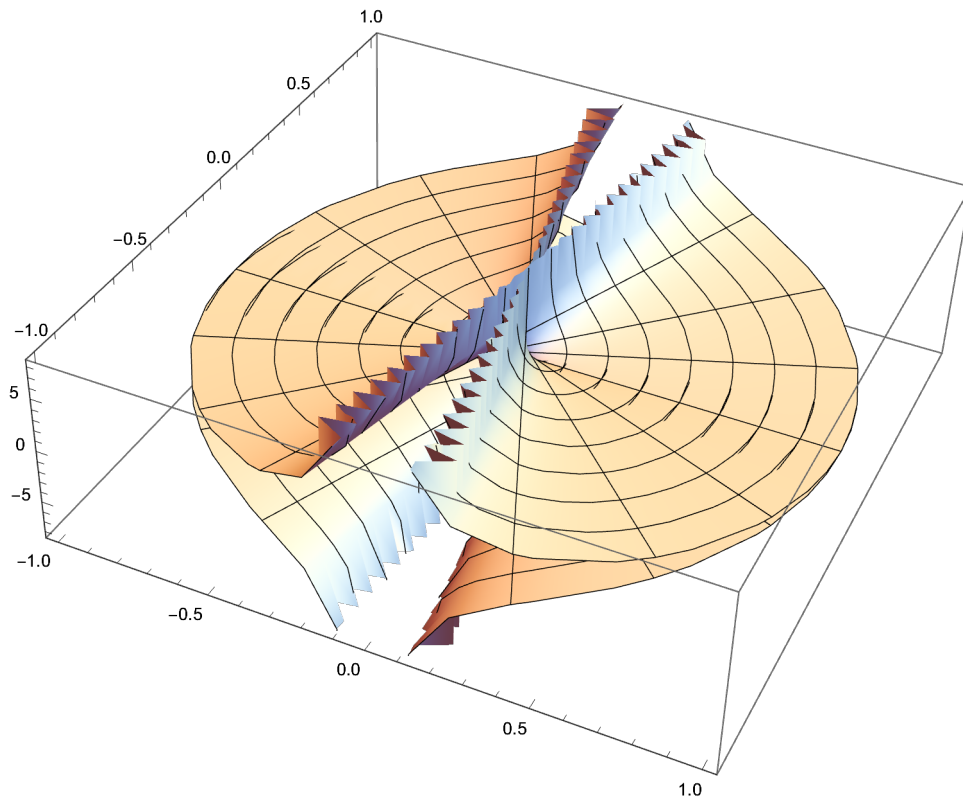


```

Solve[ $\frac{4 \pi r^2 - 2 r^2 (2 \pi (1 + \sqrt{1 - \sin[\beta]^2}))}{2 \sqrt{4 \pi r^2 (2 \pi (1 + \sqrt{1 - \sin[\beta]^2}))} - r^2 (2 \pi (1 + \sqrt{1 - \sin[\beta]^2}))^2} = \frac{2 \pi r}{2 \pi (\theta)}, \theta]$ 
{{θ → - $\frac{\sqrt{r^2 \sin[\beta]^2}}{r \sqrt{1 - \sin[\beta]^2}}$ }}

```

RevolutionPlot3D $\left[-\frac{\sqrt{r^2 \sin[\beta]^2}}{r \sqrt{1 - \sin[\beta]^2}}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$

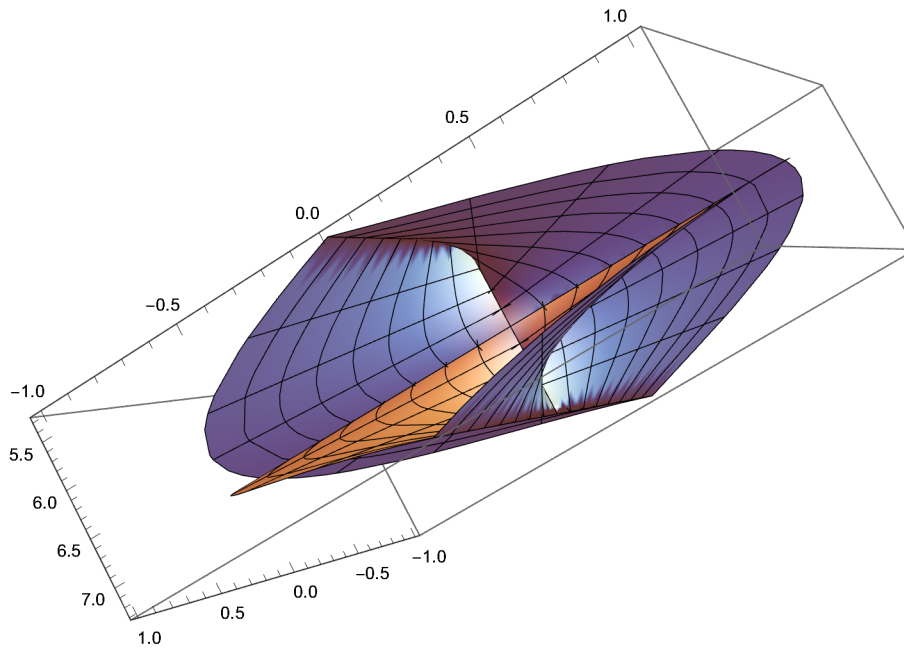


$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 (\theta)}{2 \sqrt{4 \pi r^2 (2 \pi (1 + \sqrt{1 - \sin[\beta]^2})) - r^2 (2 \pi (1 + \sqrt{1 - \sin[\beta]^2}))^2}} = \frac{2 \pi r}{2 \pi (2 \pi (1 + \sqrt{1 - \sin[\beta]^2}))}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -\frac{1}{r^2} \sqrt{8 \pi^2 r^2 (1 + \sqrt{1 - \sin[\beta]^2}) - 4 \pi^2 r^2 (1 + \sqrt{1 - \sin[\beta]^2})^2}\right.\right.$$

$$\left.\left.\left(\frac{r}{2 \pi (1 + \sqrt{1 - \sin[\beta]^2})} - \frac{2 \pi r^2}{\sqrt{8 \pi^2 r^2 (1 + \sqrt{1 - \sin[\beta]^2}) - 4 \pi^2 r^2 (1 + \sqrt{1 - \sin[\beta]^2})^2}}\right)\right\}\right\}$$

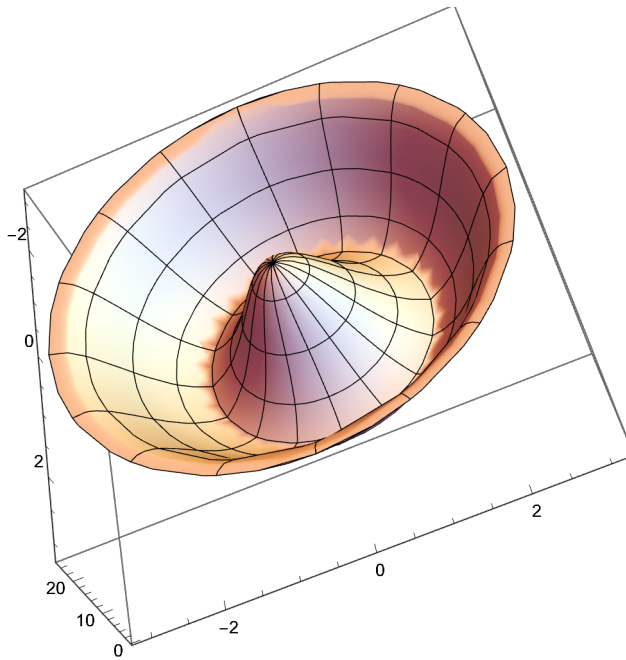
$\text{RevolutionPlot3D}\left[-\frac{1}{r^2} \sqrt{8 \pi^2 r^2 \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right) - 4 \pi^2 r^2 \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)^2}\right.$   
 $\left.\left(\frac{r}{2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)} - \frac{2 \pi r^2}{\sqrt{8 \pi^2 r^2 \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right) - 4 \pi^2 r^2 \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)^2}}\right),\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$



$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)}{2 \sqrt{4 \pi r^2 (\theta) - r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)^2}} = \frac{2 \pi r}{\left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)}, \theta\right]$   
 $\left\{\left\{\theta \rightarrow 4 \pi - 4 \pi \text{Sin}[\beta]^2 + \pi \text{Sin}[\beta]^4 + 4 \pi \sqrt{1 - \text{Sin}[\beta]^2} - 2 \pi \text{Sin}[\beta]^2 \sqrt{1 - \text{Sin}[\beta]^2}\right\}\right\}$



```
RevolutionPlot3D[
  4 π - 4 π Sin[β]2 + π Sin[β]4 + 4 π √{1 - Sin[β]2} - 2 π Sin[β]2 √{1 - Sin[β]2}, {β, -π, π}]
```

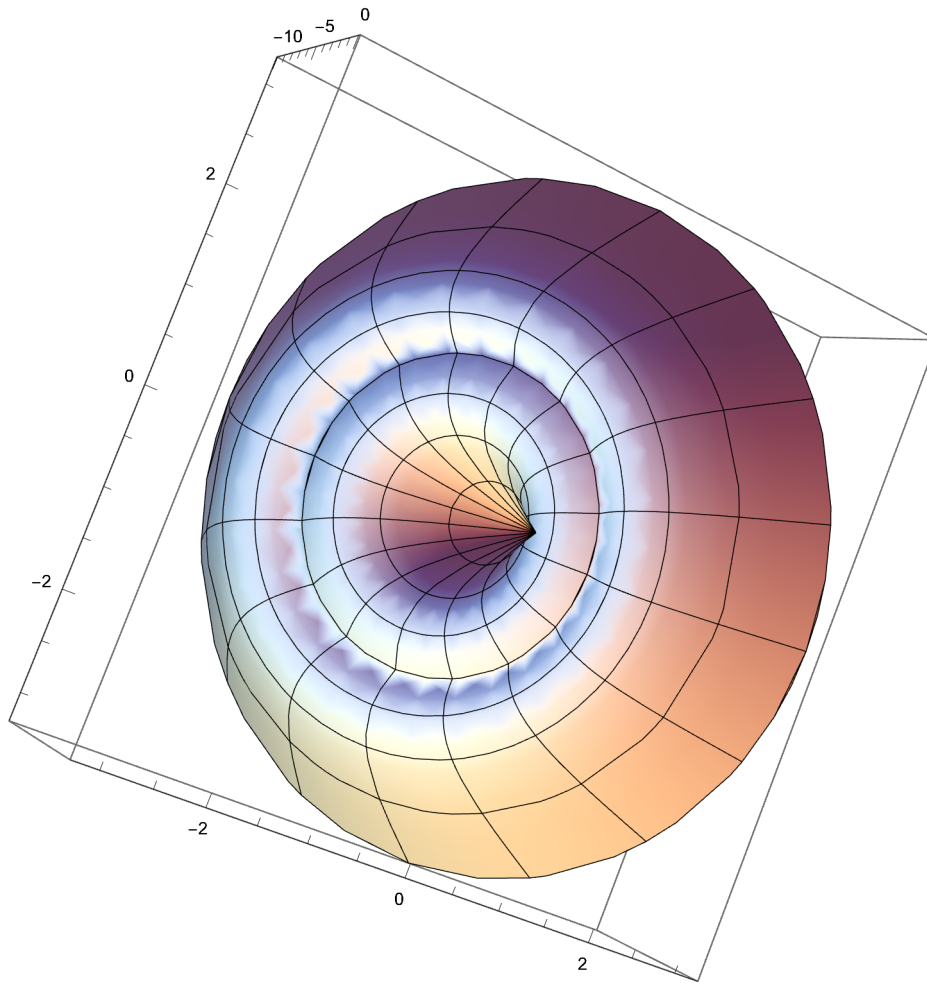


$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)}{2 \sqrt{4 \pi r^2 \left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right) - r^2 (\theta)^2}} = \frac{2 \pi r}{\left(2 \pi \left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right)}, \theta\right]$$

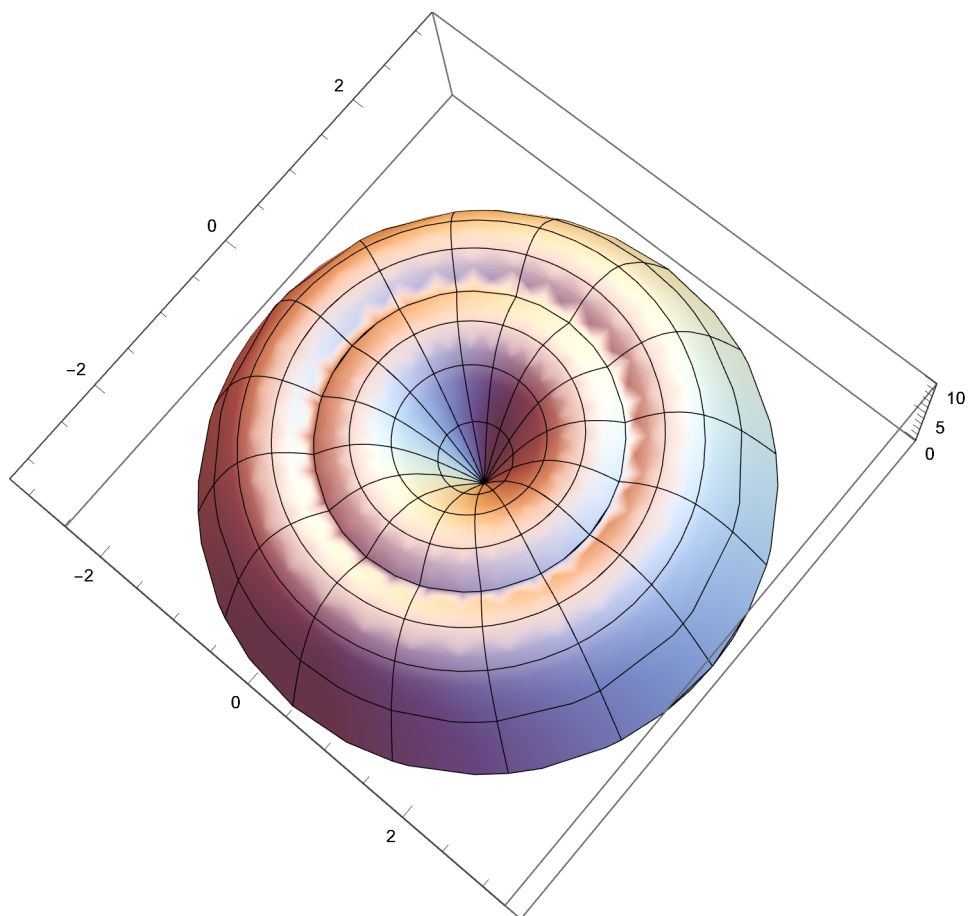
$$\left\{\left\{\theta \rightarrow -2 \sqrt{3 \pi^2 \text{Sin}[\beta]^2 - \pi^2 \text{Sin}[\beta]^4 + 2 \pi^2 \text{Sin}[\beta]^2 \sqrt{1 - \text{Sin}[\beta]^2}}\right\},\right.$$

$$\left.\left\{\theta \rightarrow 2 \sqrt{3 \pi^2 \text{Sin}[\beta]^2 - \pi^2 \text{Sin}[\beta]^4 + 2 \pi^2 \text{Sin}[\beta]^2 \sqrt{1 - \text{Sin}[\beta]^2}}\right\}\right\}$$

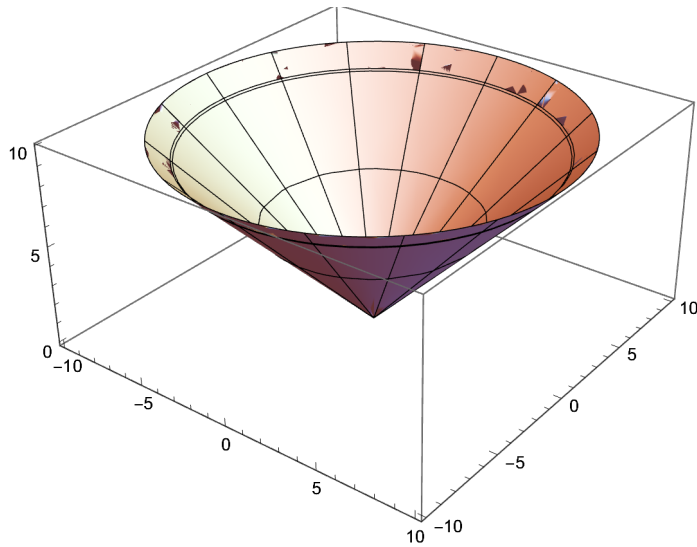
`RevolutionPlot3D` $\left[-2 \sqrt{3 \pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^4 + 2 \pi^2 \sin[\beta]^2 \sqrt{1 - \sin[\beta]^2}}, \{\beta, -\pi, \pi\}\right]$



`RevolutionPlot3D[ $2 \sqrt{3 \pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^4 + 2 \pi^2 \sin[\beta]^2 \sqrt{1 - \sin[\beta]^2}}$ , { $\beta$ ,  $-\pi$ ,  $\pi$ }]`

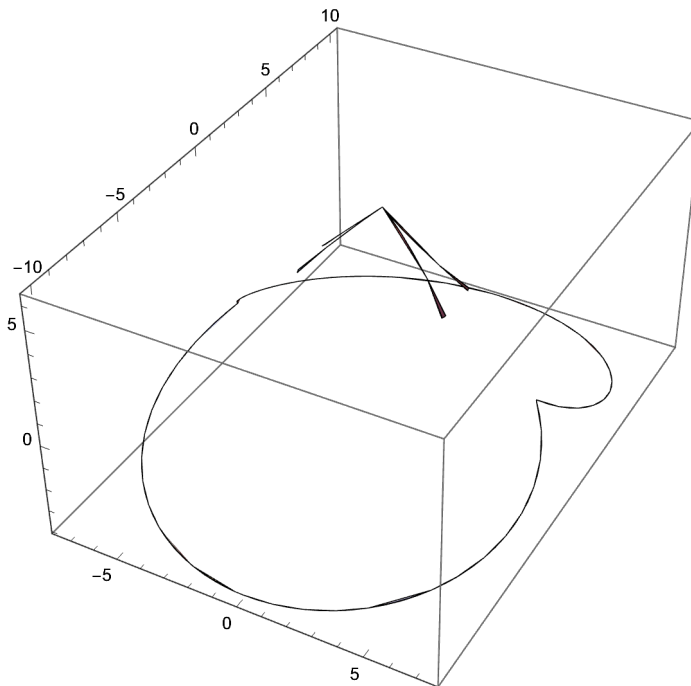


$\text{RevolutionPlot3D}\left[\left\{-2 \sqrt{3 \pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^4 + 2 \pi^2 \sin[\beta]^2 \sqrt{1 - \sin[\beta]^2}},\right.\right.$   
 $\left.2 \sqrt{3 \pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^4 + 2 \pi^2 \sin[\beta]^2 \sqrt{1 - \sin[\beta]^2}}\right\}, \{\beta, -\pi, \pi\}]$



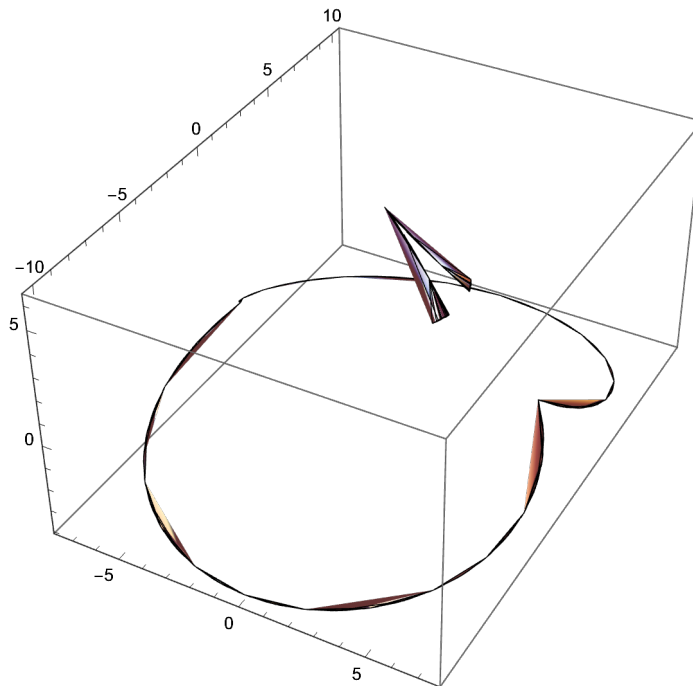
Of course, the above visualizations are all just a single potential scaling of the function. For instance, when we take the function :

$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$

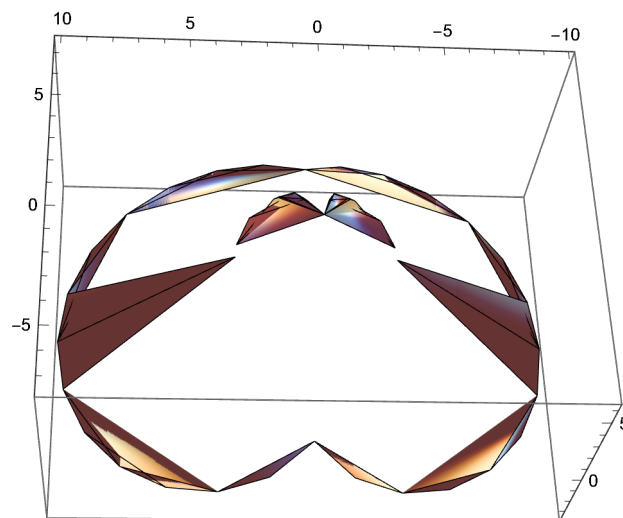


And scale it differently, we see a totally interconnected realm of designs.

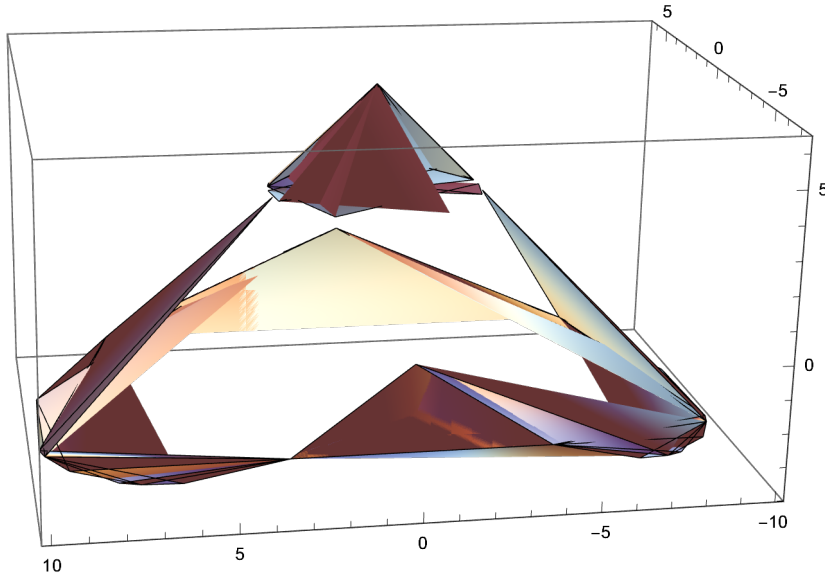
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -2 \pi, 2 \pi\}\right]$



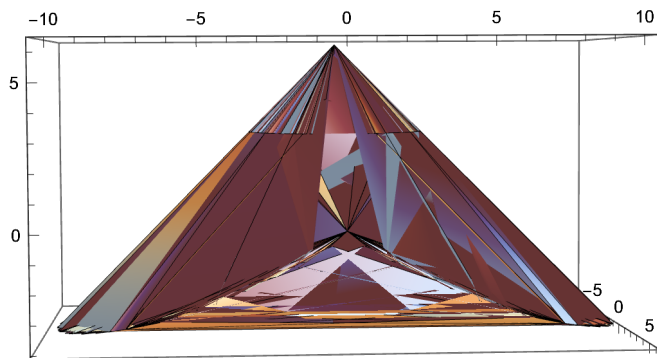
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -4 \pi, 4 \pi\}\right]$



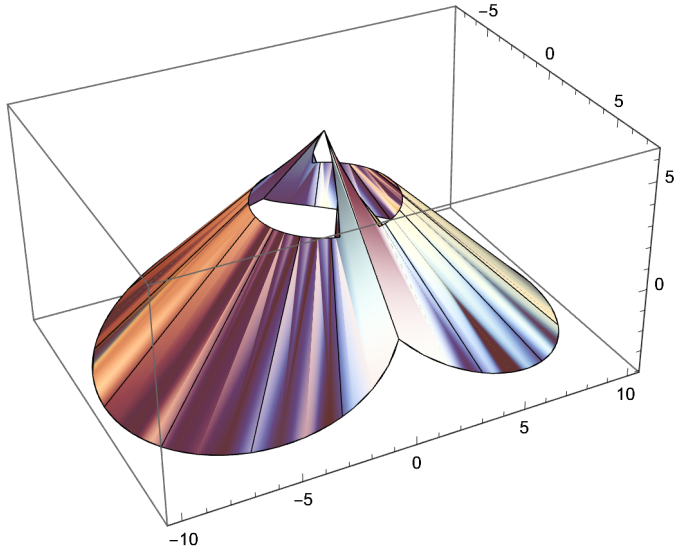
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -8 \pi, 8 \pi\}\right]$



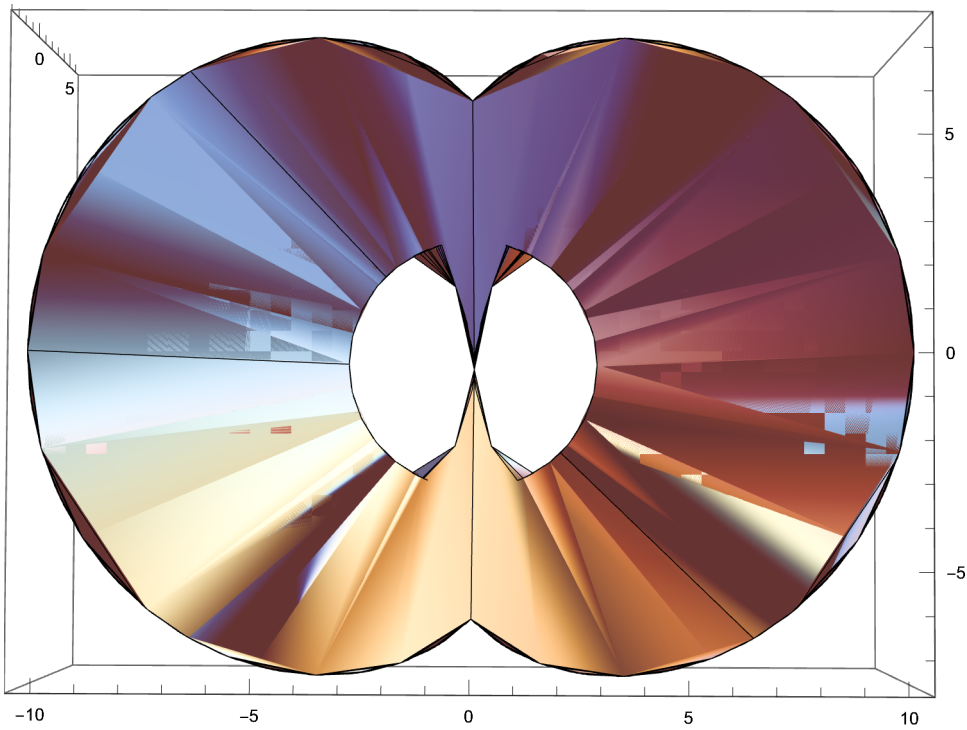
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -16 \pi, 16 \pi\}\right]$



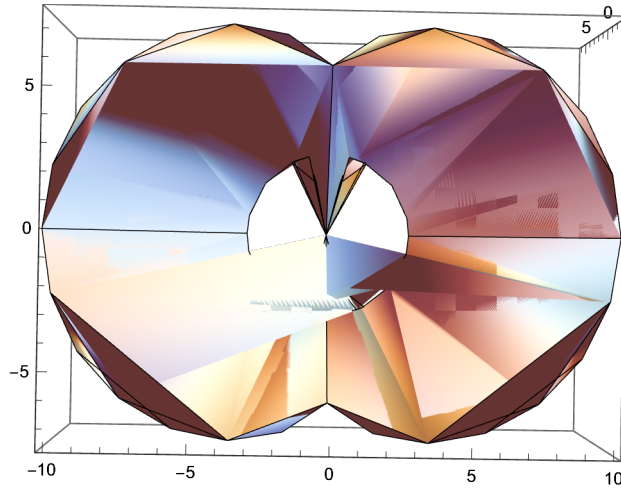
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -10, 10\}, \{\beta, -\pi, \pi\}\right]$



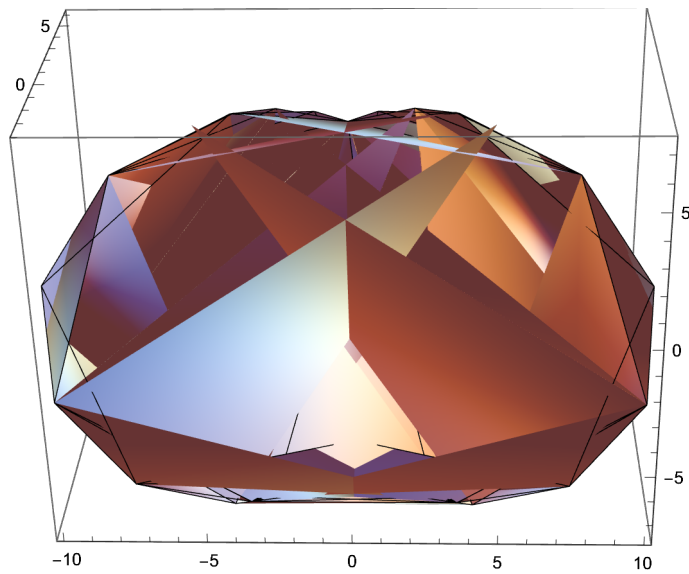
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -10, 10\}, \{\beta, -2\pi, 2\pi\}\right]$



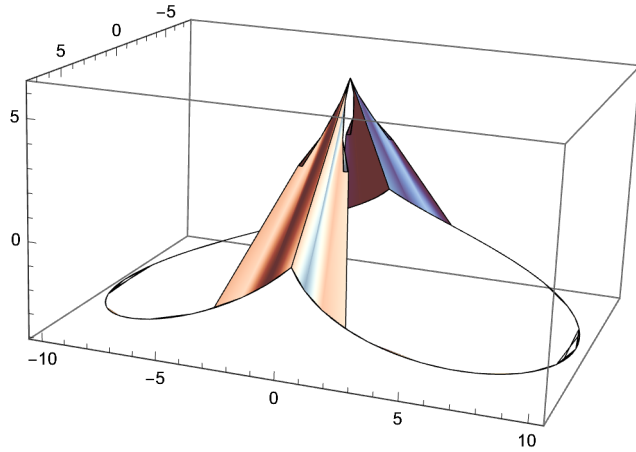
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -10, 10\}, \{\beta, -4 \pi, 4 \pi\}\right]$

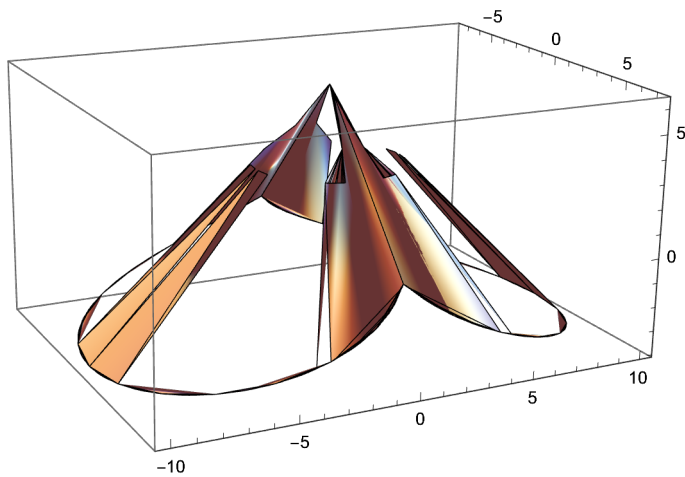


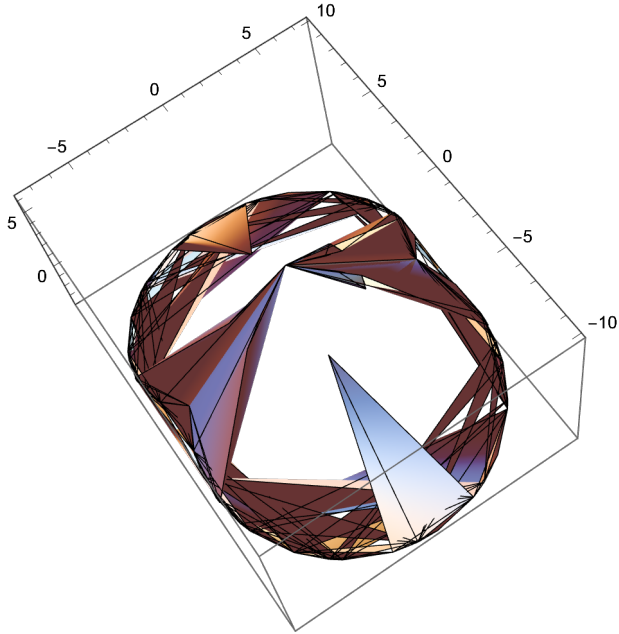
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -10, 10\}, \{\beta, -8 \pi, 8 \pi\}\right]$

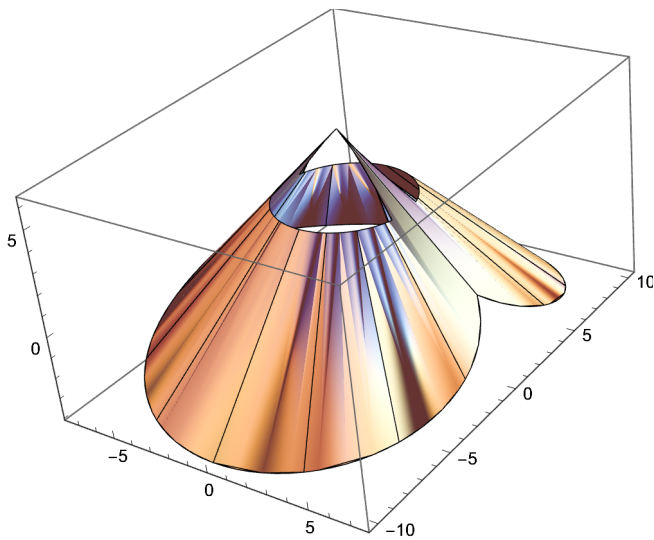




$$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -100, 100\}, \{\beta, -\pi, \pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -100, 100\}, \{\beta, -2\pi, 2\pi\}\right]$$


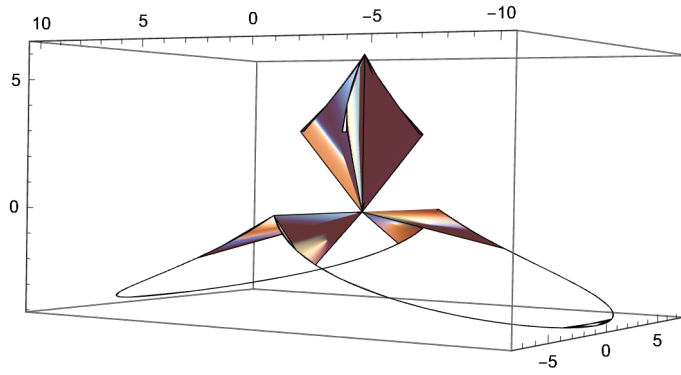
$$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -100, 100\}, \{\beta, -4 \pi, 4 \pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -1000, 1000\}, \{\beta, -\pi, \pi\}\right]$$


```

RevolutionPlot3D[ $\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},$ 
  {r, -10 000, 10 000}, {β, -π, π}]

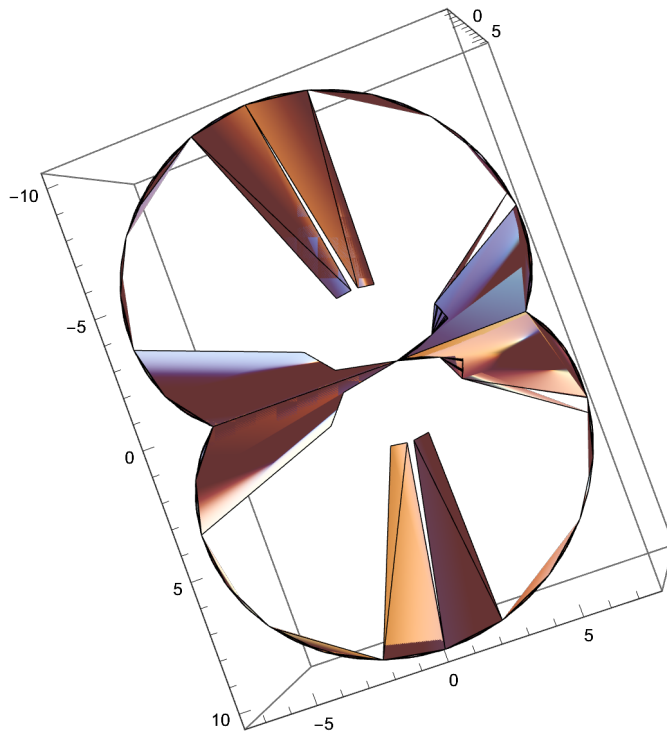
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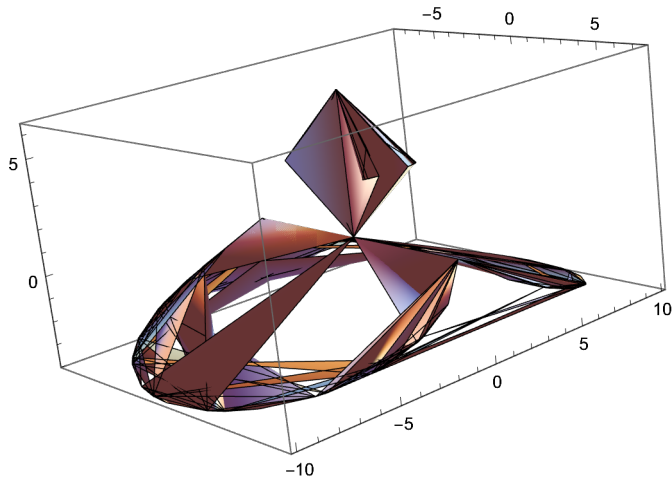
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RevolutionPlot3D[ $\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},$ 
  {r, -10 000, 10 000}, {β, -2 π, 2 π}]

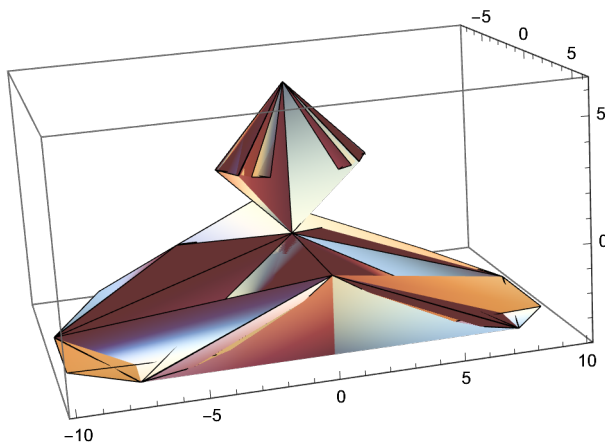
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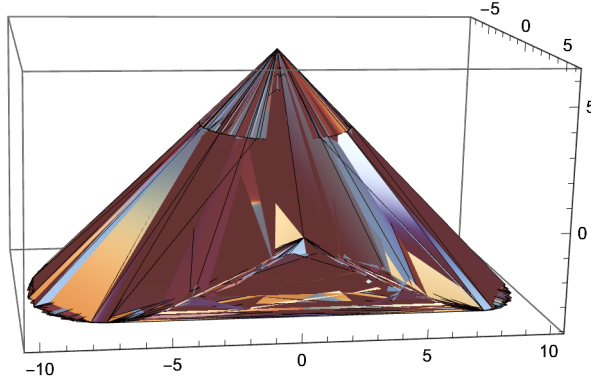
$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -10\,000, 10\,000\}, \{\beta, -4 \pi, 4 \pi\}\right]$



$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},\right.$   
 $\left.\{r, -10\,000, 10\,000\}, \{\beta, -8 \pi, 8 \pi\}\right]$



RevolutionPlot3D[ $\left\{\frac{\pi r - \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r + \sqrt{\pi^2 r^2 - 4 \pi^2 r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\},$   
 $\{r, -10000, 10000\}, \{\beta, -16\pi, 16\pi\}$ ]



$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \frac{2 \pi r}{\theta}, \theta\right]$$

$$\theta = \frac{2}{3} \left( 2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi \right) \quad (23)$$

$$\text{Solve}\left[\frac{2}{3} \left( 2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi \right) = 2 \pi \left( 1 + \sqrt{1 - \sin[\beta]^2} \right), \beta\right]$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin}\left[ \frac{1}{\sqrt{\frac{3 (17 + 3 \sqrt{33})}{68 + 12 \sqrt{33} + 10 (17 + 3 \sqrt{33})^{1/3} + 2 \sqrt{33} (17 + 3 \sqrt{33})^{1/3} - 7 (17 + 3 \sqrt{33})^{2/3} - \sqrt{33} (17 + 3 \sqrt{33})^{2/3}}}} \right]} \right\}, \right.$$

$$\left. \left\{ \beta \rightarrow \text{ArcSin}\left[ \frac{1}{\sqrt{\frac{3 (17 + 3 \sqrt{33})}{68 + 12 \sqrt{33} + 10 (17 + 3 \sqrt{33})^{1/3} + 2 \sqrt{33} (17 + 3 \sqrt{33})^{1/3} - 7 (17 + 3 \sqrt{33})^{2/3} - \sqrt{33} (17 + 3 \sqrt{33})^{2/3}}}} \right]} \right\} \right\}$$

$$\theta = \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \quad (24)$$

$$\text{Solve}\left[\frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi = 2 \pi \left( 1 + \sqrt{1 - \sin[\beta]^2} \right), \beta\right]$$

$$\{\}$$

$$\theta = \frac{4 \pi}{3} + \frac{2 (1 - i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 + i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \quad (25)$$

# Addendum No. 1

Visualizing Multiple Possible Equations for Non-Relativistic Velocity with Constant Initial Radius through a Transition.

$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\} \right\} \quad (26)$$

We will not apply these substitutions for every single possible variation of possible patterns, but please note that it is possible to do so. When you do this, you find many different possible visualizations of a given function.

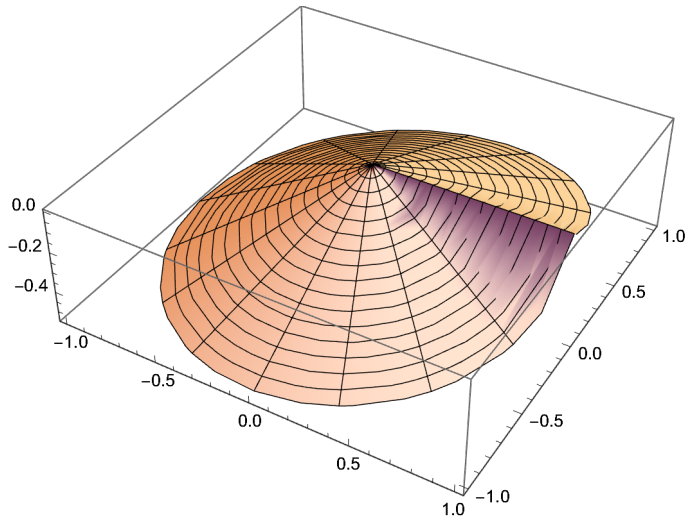
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$\eta$

$$\begin{aligned} \text{Solve} \left[ \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2} \right)}{\theta^2} == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \eta \right] \\ \left\{ \left\{ \eta \rightarrow -\frac{1}{4 \pi^2} \right. \right. \\ \left. \left( \sqrt{64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta}} \right) \right\}, \quad (27) \\ \left. \left\{ \eta \rightarrow \frac{1}{4 \pi^2} \left( \sqrt{64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta}} \right) \right\} \right\} \end{aligned}$$

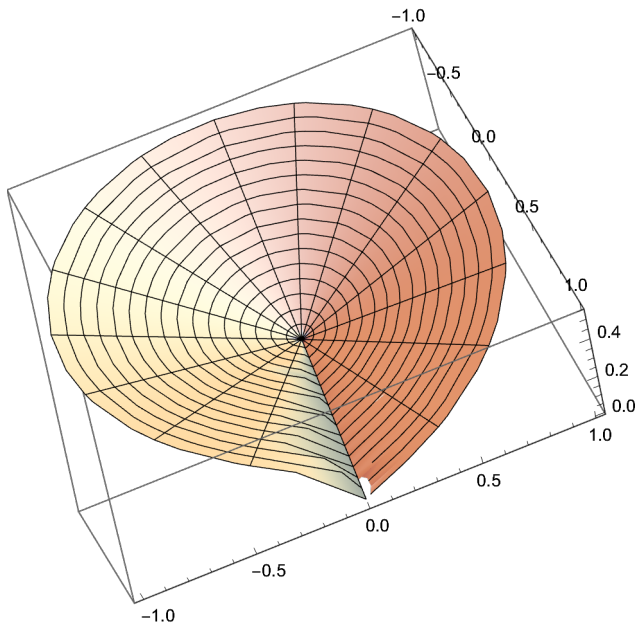
RevolutionPlot3D[  

$$-\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



RevolutionPlot3D[

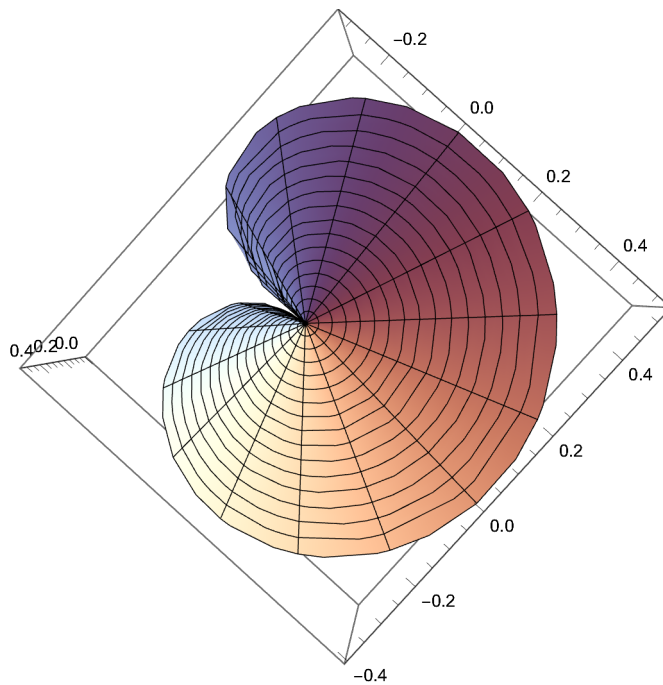
$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$





RevolutionPlot3D[

$$\left\{ -\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \right. \\ \left. \frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right) \right\}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



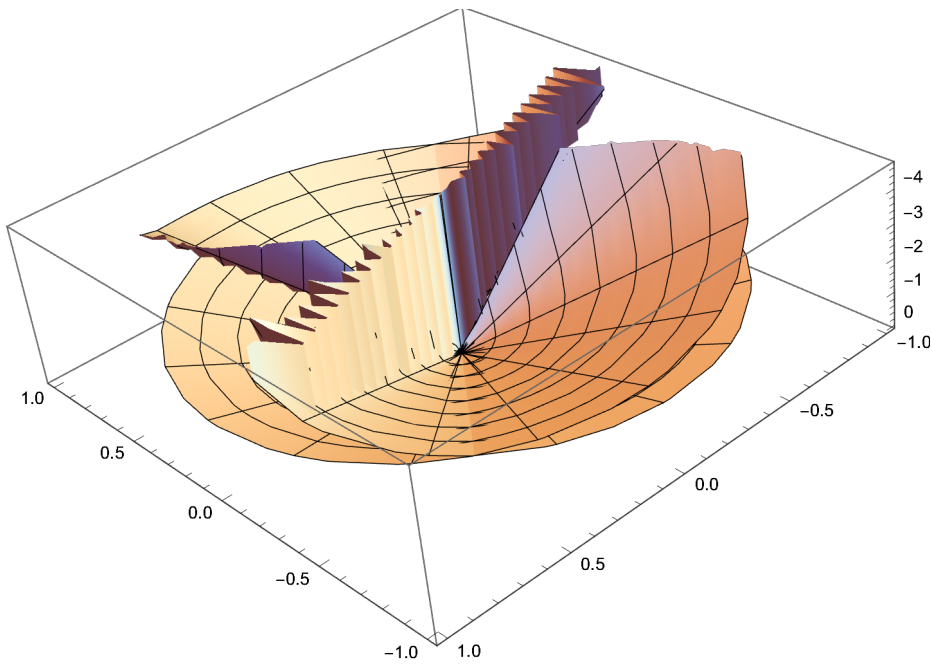
r

$$\text{Solve}\left[\frac{2\pi\left(2\pi r - 2\pi\sqrt{r^2 - (\eta)^2}\right)}{\theta^2} == \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}, r\right]$$



RevolutionPlot3D[

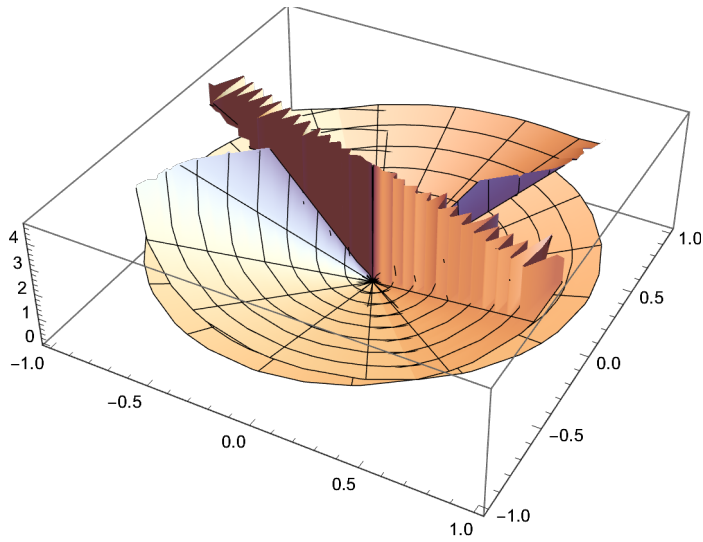
$$\left\{ -\sqrt{\left( -\left( 256 \pi^7 \eta^2 \theta^3 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \left( \theta \right)^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 320 \pi^6 \eta^2 \theta^4 \right) / \right.} \right. \\ \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \right. \\ \left. \left( 128 \pi^5 \eta^2 \theta^5 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 16 \pi^4 \eta^2 \theta^6 \right) / \right. \\ \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \right. \\ \left. \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} \right) / \right. \\ \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$



```

RevolutionPlot3D[
  Sqrt[(- (256 Pi^7 eta^2 theta^3) / (-1024 Pi^7 theta^3 + 1280 Pi^6 theta^4 - 512 Pi^5 theta^5 + 80 Pi^4 theta^6 - 32 Pi^3 theta^7 + 24 Pi^2 theta^8 - 8 Pi theta^9 + theta^10) + (320 Pi^6 eta^2 theta^4) /
    (-1024 Pi^7 theta^3 + 1280 Pi^6 theta^4 - 512 Pi^5 theta^5 + 80 Pi^4 theta^6 - 32 Pi^3 theta^7 + 24 Pi^2 theta^8 - 8 Pi theta^9 + theta^10) -
    (128 Pi^5 eta^2 theta^5) / (-1024 Pi^7 theta^3 + 1280 Pi^6 theta^4 - 512 Pi^5 theta^5 + 80 Pi^4 theta^6 - 32 Pi^3 theta^7 + 24 Pi^2 theta^8 - 8 Pi theta^9 + theta^10) + (16 Pi^4 eta^2 theta^6) /
    (-1024 Pi^7 theta^3 + 1280 Pi^6 theta^4 - 512 Pi^5 theta^5 + 80 Pi^4 theta^6 - 32 Pi^3 theta^7 + 24 Pi^2 theta^8 - 8 Pi theta^9 + theta^10) -
    (128 Pi^6 Sqrt[256 Pi^5 eta^4 theta^3 - 448 Pi^4 eta^4 theta^4 + 304 Pi^3 eta^4 theta^5 - 100 Pi^2 eta^4 theta^6 + 16 Pi eta^4 theta^7 - eta^4 theta^8]) /
    (-1024 Pi^7 theta^3 + 1280 Pi^6 theta^4 - 512 Pi^5 theta^5 + 80 Pi^4 theta^6 - 32 Pi^3 theta^7 + 24 Pi^2 theta^8 - 8 Pi theta^9 + theta^10))],
  {eta, -1, 1}, {theta, -2 Pi, 2 Pi}]

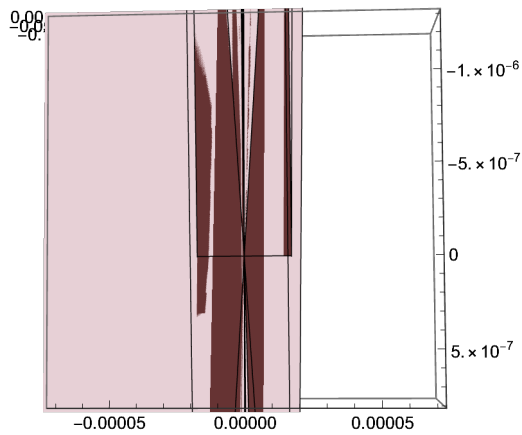
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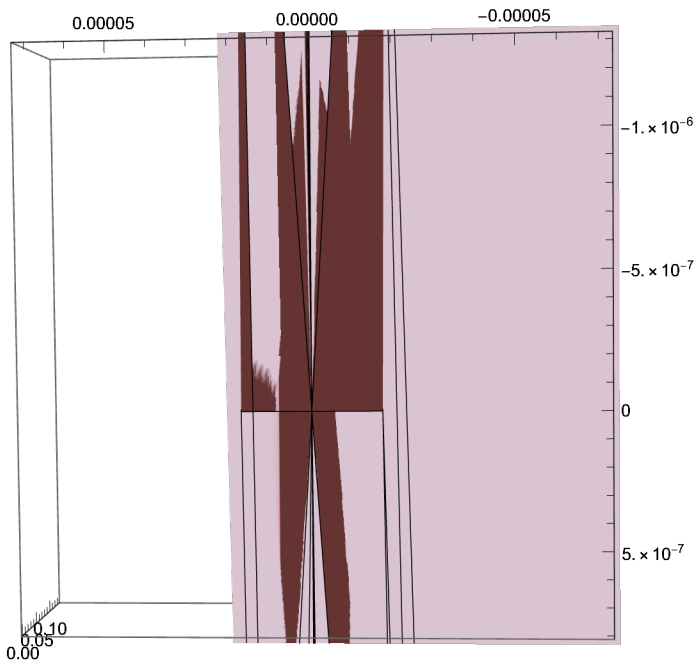
RevolutionPlot3D[
  - $\sqrt{\left(-\left(256 \pi^7 \eta^2 \theta^3\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+\right.\right.}$ 
     $\left.\left.24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(320 \pi^6 \eta^2 \theta^4\right) /\right.}$ 
     $\left.\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)-\right.}$ 
     $\left.\left(128 \pi^5 \eta^2 \theta^5\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-\right.\right.}$ 
     $\left.\left.32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(16 \pi^4 \eta^2 \theta^6\right) /\right.}$ 
     $\left.\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\right.}$ 
     $\left.\left(128 \pi^6 \sqrt{\left(256 \pi^5 \eta^4 \theta^3-448 \pi^4 \eta^4 \theta^4+304 \pi^3 \eta^4 \theta^5-100 \pi^2 \eta^4 \theta^6+16 \pi \eta^4 \theta^7-\eta^4 \theta^8\right)}\right) /\right.}$ 
     $\left.\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+\right.\right.}$ 
     $\left.\left.24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)\right),\{\eta,-1,1\},\{\theta,-2 \pi, 2 \pi\}]$ 

```



RevolutionPlot3D[

$$\begin{aligned} & \sqrt{\left(-\left(256 \pi^7 \eta^2 \theta^3\right) / \left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(320 \pi^6 \eta^2 \theta^4\right) /\right.} \\ & \quad \left.\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)-\right. \\ & \quad \left.\left(128 \pi^5 \eta^2 \theta^5\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(16 \pi^4 \eta^2 \theta^6\right) /\right.} \\ & \quad \left.\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\right. \\ & \quad \left.\left(128 \pi^6 \sqrt{\left(256 \pi^5 \eta^4 \theta^3-448 \pi^4 \eta^4 \theta^4+304 \pi^3 \eta^4 \theta^5-100 \pi^2 \eta^4 \theta^6+16 \pi \eta^4 \theta^7-\eta^4 \theta^8\right)} /\right.\right. \\ & \quad \left.\left.\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)\right), \right. \\ & \quad \left.\{\eta,-1,1\},\{\theta,-2 \pi, 2 \pi\}\right] \end{aligned}$$



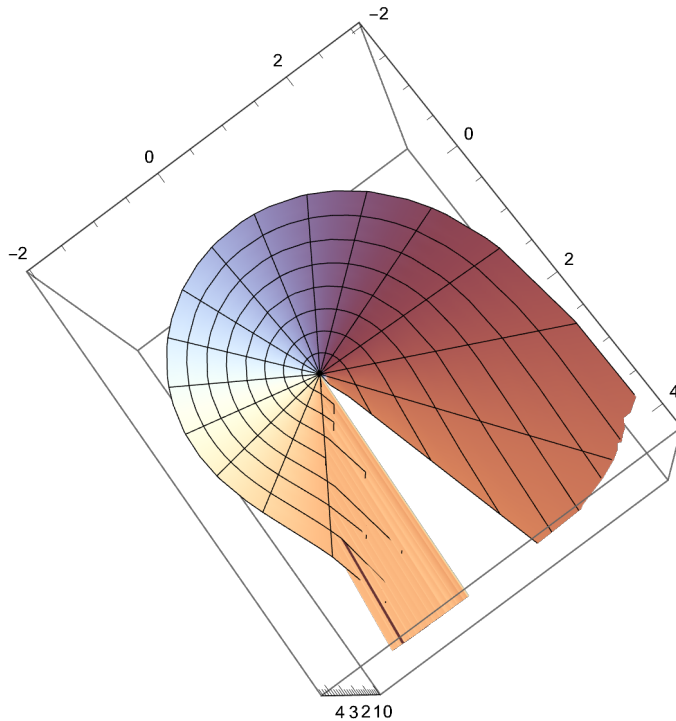
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RevolutionPlot3D[
{

$$\sqrt{\left(-\left(256 \pi^7 \eta^2 \theta^3\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(320 \pi^6 \eta^2 \theta^4\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)-\left(128 \pi^5 \eta^2 \theta^5\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(16 \pi^4 \eta^2 \theta^6\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)-\left(128 \pi^6 \sqrt{\left(256 \pi^5 \eta^4 \theta^3-448 \pi^4 \eta^4 \theta^4+304 \pi^3 \eta^4 \theta^5-100 \pi^2 \eta^4 \theta^6+16 \pi \eta^4 \theta^7-\eta^4 \theta^8\right)} /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)\right)},$$


$$\sqrt{\left(-\left(256 \pi^7 \eta^2 \theta^3\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(320 \pi^6 \eta^2 \theta^4\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)-\left(128 \pi^5 \eta^2 \theta^5\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)+\left(16 \pi^4 \eta^2 \theta^6\right) /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)-\left(128 \pi^6 \sqrt{\left(256 \pi^5 \eta^4 \theta^3-448 \pi^4 \eta^4 \theta^4+304 \pi^3 \eta^4 \theta^5-100 \pi^2 \eta^4 \theta^6+16 \pi \eta^4 \theta^7-\eta^4 \theta^8\right)} /\left(-1024 \pi^7 \theta^3+1280 \pi^6 \theta^4-512 \pi^5 \theta^5+80 \pi^4 \theta^6-32 \pi^3 \theta^7+24 \pi^2 \theta^8-8 \pi \theta^9+\theta^{10}\right)\right)},\left\{\eta,-1,1\right\},\left\{\theta,-2 \pi, 2 \pi\right\}]$$

```



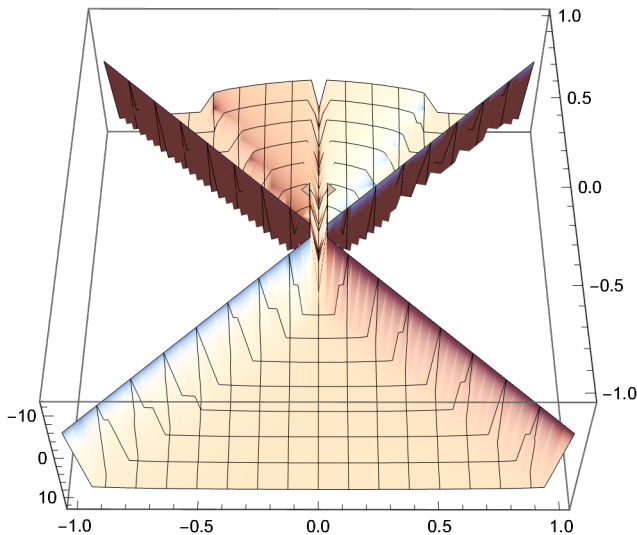


$\theta$ 

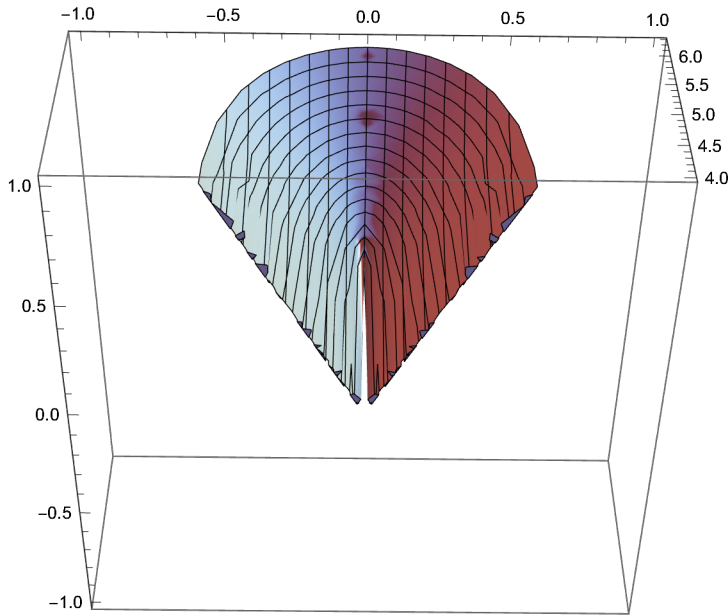
$$\text{Solve}\left[\frac{2\pi(2\pi r - 2\pi\sqrt{r^2 - (\eta)^2})}{\theta^2} == \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}, \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \text{Root}\left[-128\pi^5 r^2 + 64\pi^5 \eta^2 + 128\pi^5 r\sqrt{r^2 - \eta^2} + \right. \right. \\ & \quad \left. \left. (32\pi^4 r^2 - 16\pi^4 \eta^2 - 32\pi^4 r\sqrt{r^2 - \eta^2}) \mp 1 + 4\pi^2 r^2 \mp 1^3 - 4\pi r^2 \mp 1^4 + r^2 \mp 1^5 \&, 1\right], \right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[-128\pi^5 r^2 + 64\pi^5 \eta^2 + 128\pi^5 r\sqrt{r^2 - \eta^2} + (32\pi^4 r^2 - 16\pi^4 \eta^2 - 32\pi^4 r\sqrt{r^2 - \eta^2}) \mp 1 + \right. \right. \\ & \quad \left. \left. 4\pi^2 r^2 \mp 1^3 - 4\pi r^2 \mp 1^4 + r^2 \mp 1^5 \&, 2\right], \right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[-128\pi^5 r^2 + 64\pi^5 \eta^2 + 128\pi^5 r\sqrt{r^2 - \eta^2} + (32\pi^4 r^2 - 16\pi^4 \eta^2 - 32\pi^4 r\sqrt{r^2 - \eta^2}) \mp 1 + \right. \right. \\ & \quad \left. \left. 4\pi^2 r^2 \mp 1^3 - 4\pi r^2 \mp 1^4 + r^2 \mp 1^5 \&, 3\right], \right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[-128\pi^5 r^2 + 64\pi^5 \eta^2 + 128\pi^5 r\sqrt{r^2 - \eta^2} + (32\pi^4 r^2 - 16\pi^4 \eta^2 - 32\pi^4 r\sqrt{r^2 - \eta^2}) \mp 1 + \right. \right. \\ & \quad \left. \left. 4\pi^2 r^2 \mp 1^3 - 4\pi r^2 \mp 1^4 + r^2 \mp 1^5 \&, 4\right], \right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[-128\pi^5 r^2 + 64\pi^5 \eta^2 + 128\pi^5 r\sqrt{r^2 - \eta^2} + (32\pi^4 r^2 - 16\pi^4 \eta^2 - 32\pi^4 r\sqrt{r^2 - \eta^2}) \mp 1 + \right. \right. \\ & \quad \left. \left. 4\pi^2 r^2 \mp 1^3 - 4\pi r^2 \mp 1^4 + r^2 \mp 1^5 \&, 5\right], \right\} \end{aligned}$$

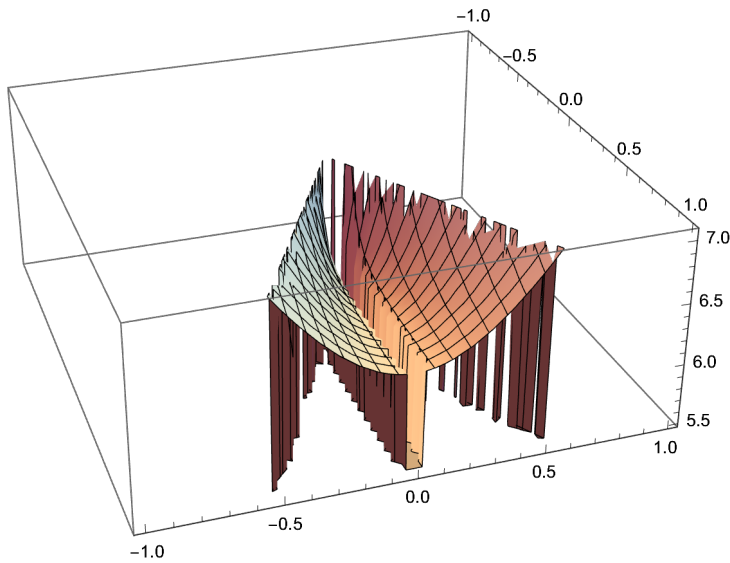
$$\begin{aligned} & \text{Plot3D}\left[ \right. \\ & \quad \left. \text{Root}\left[-128\pi^5 r^2 + 64\pi^5 \eta^2 + 128\pi^5 r\sqrt{r^2 - \eta^2} + (32\pi^4 r^2 - 16\pi^4 \eta^2 - 32\pi^4 r\sqrt{r^2 - \eta^2}) \mp 1 + \right. \right. \\ & \quad \left. \left. 4\pi^2 r^2 \mp 1^3 - 4\pi r^2 \mp 1^4 + r^2 \mp 1^5 \&, 1\right], \{r, -1, 1\}, \{\eta, -1, 1\} \right] \end{aligned}$$



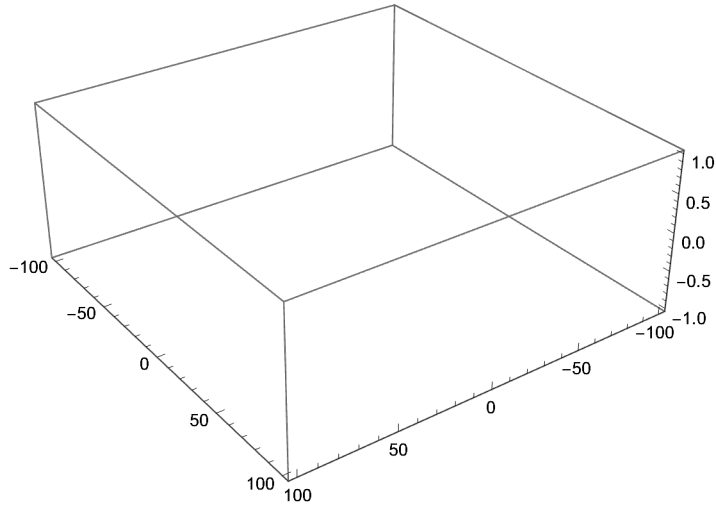
Plot3D[  
 Root[-128  $\pi^5 r^2 + 64 \pi^5 \eta^2 + 128 \pi^5 r \sqrt{r^2 - \eta^2} + (32 \pi^4 r^2 - 16 \pi^4 \eta^2 - 32 \pi^4 r \sqrt{r^2 - \eta^2}) \#1 +$   
 $4 \pi^2 r^2 \#1^3 - 4 \pi r^2 \#1^4 + r^2 \#1^5 \&, 2], \{r, -1, 1\}, \{\eta, -1, 1\}]$



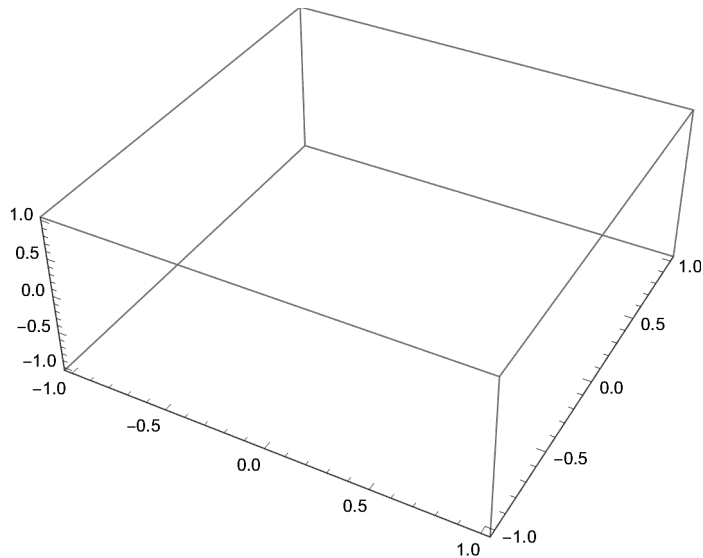
Plot3D[  
 Root[-128  $\pi^5 r^2 + 64 \pi^5 \eta^2 + 128 \pi^5 r \sqrt{r^2 - \eta^2} + (32 \pi^4 r^2 - 16 \pi^4 \eta^2 - 32 \pi^4 r \sqrt{r^2 - \eta^2}) \#1 +$   
 $4 \pi^2 r^2 \#1^3 - 4 \pi r^2 \#1^4 + r^2 \#1^5 \&, 3], \{r, -1, 1\}, \{\eta, -1, 1\}]$



```
Plot3D[
  Root[-128 π5 r2 + 64 π5 η2 + 128 π5 r √(r2 - η2) + (32 π4 r2 - 16 π4 η2 - 32 π4 r √(r2 - η2)) #1 +
    4 π2 r2 #13 - 4 π r2 #14 + r2 #15 &, 4], {r, -100, 100}, {η, -100, 100}]
```



```
Plot3D[
  Root[-128 π5 r2 + 64 π5 η2 + 128 π5 r √(r2 - η2) + (32 π4 r2 - 16 π4 η2 - 32 π4 r √(r2 - η2)) #1 +
    4 π2 r2 #13 - 4 π r2 #14 + r2 #15 &, 5], {r, -1, 1}, {η, -1, 1}]
```



$$\text{Solve}\left[\frac{2\pi\left(2\pi r - 2\pi\sqrt{r^2 - \left(\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right)^2}\right)}{\theta^2} == \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{4\pi}{3} + \frac{4\pi}{3(-17+3\sqrt{33})^{1/3}} - \frac{2}{3}(-17+3\sqrt{33})^{1/3}\pi\right\},\right.$$

$$\left\{\theta \rightarrow \frac{4\pi}{3} - \frac{2(1+i\sqrt{3})\pi}{3(-17+3\sqrt{33})^{1/3}} + \frac{1}{3}(1-i\sqrt{3})(-17+3\sqrt{33})^{1/3}\pi\right\},$$

$$\left\{\theta \rightarrow \frac{4\pi}{3} - \frac{2(1-i\sqrt{3})\pi}{3(-17+3\sqrt{33})^{1/3}} + \frac{1}{3}(1+i\sqrt{3})(-17+3\sqrt{33})^{1/3}\pi\right\},$$

$$\left\{\theta \rightarrow \pi \text{Root}\left[-256 + 192\#1 - 48\#1^2 + 8\#1^3 - 4\#1^4 + \#1^5 \&, 1\right]\right\},$$

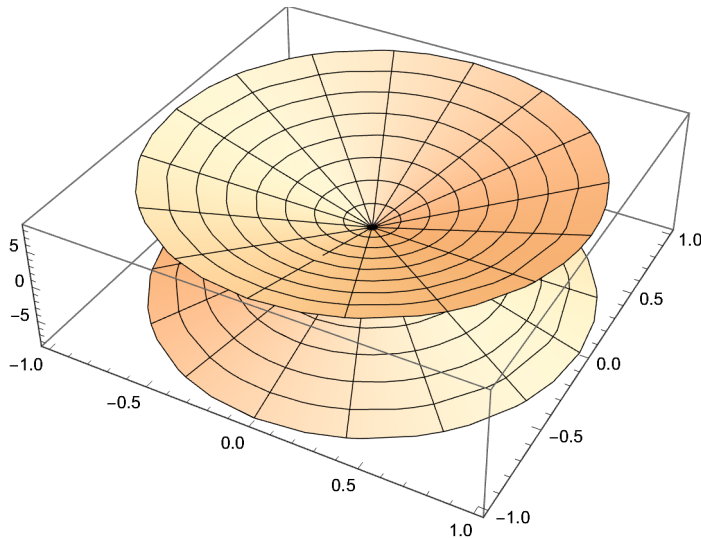
$$\left\{\theta \rightarrow \pi \text{Root}\left[-256 + 192\#1 - 48\#1^2 + 8\#1^3 - 4\#1^4 + \#1^5 \&, 2\right]\right\},$$

$$\left\{\theta \rightarrow \pi \text{Root}\left[-256 + 192\#1 - 48\#1^2 + 8\#1^3 - 4\#1^4 + \#1^5 \&, 3\right]\right\},$$

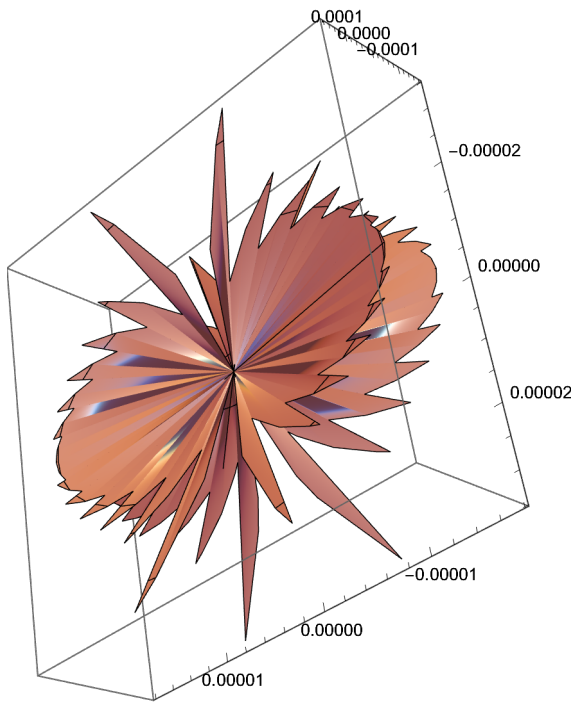
$$\left\{\theta \rightarrow \pi \text{Root}\left[-256 + 192\#1 - 48\#1^2 + 8\#1^3 - 4\#1^4 + \#1^5 \&, 4\right]\right\},$$

$$\left\{\theta \rightarrow \pi \text{Root}\left[-256 + 192\#1 - 48\#1^2 + 8\#1^3 - 4\#1^4 + \#1^5 \&, 5\right]\right\}\}$$

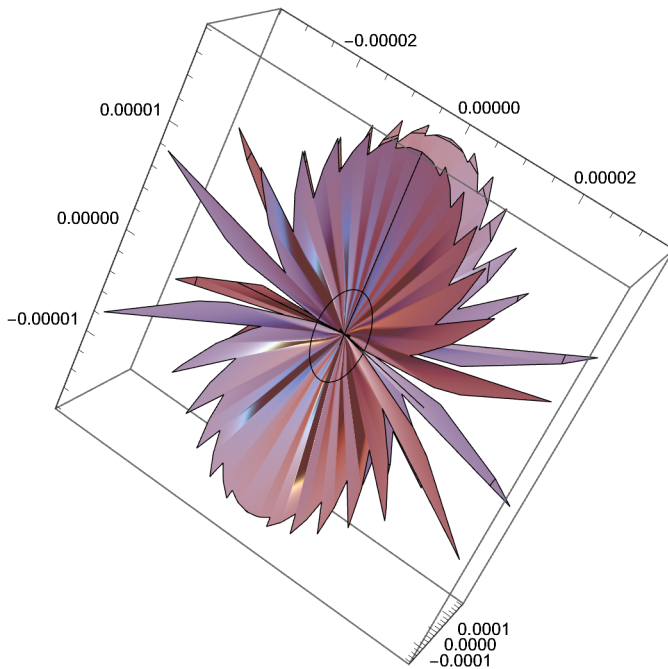
**RevolutionPlot3D** $\left[r \pi \text{Root}\left[-256 + 192\#1 - 48\#1^2 + 8\#1^3 - 4\#1^4 + \#1^5 \&, 1\right], \{r, -1, 1\}\right]$



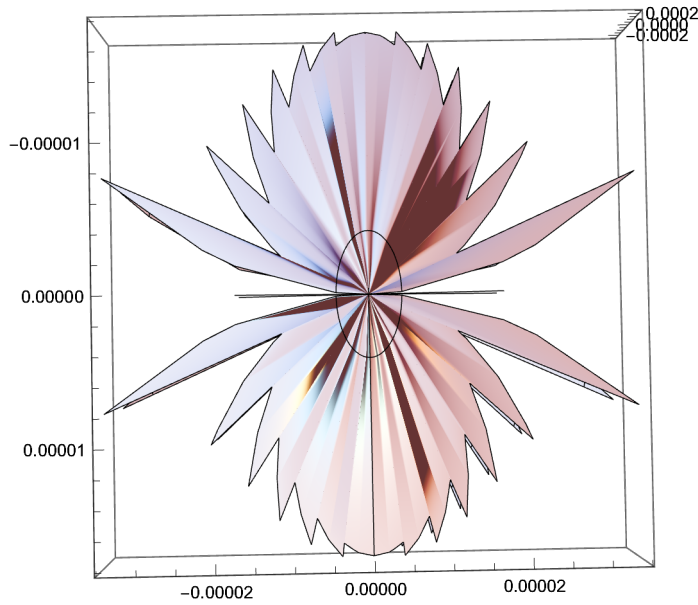
`RevolutionPlot3D[r π Root[-256 + 192 #1 - 48 #12 + 8 #13 - 4 #14 + #15 &, 2], {r, -1, 1}]`



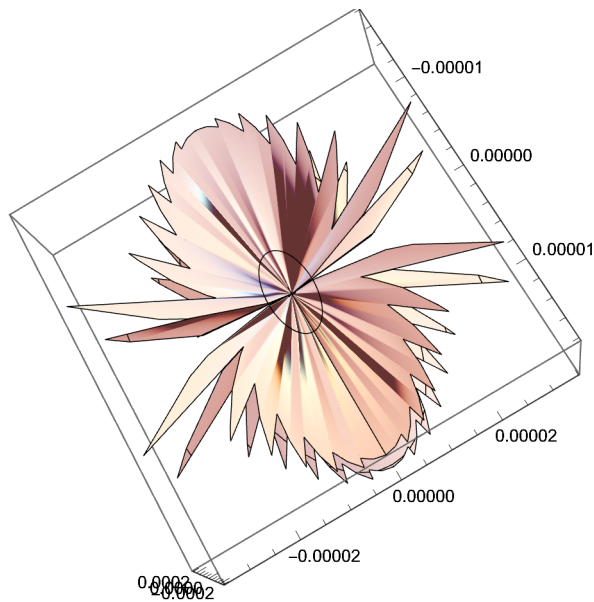
`RevolutionPlot3D[r π Root[-256 + 192 #1 - 48 #12 + 8 #13 - 4 #14 + #15 &, 3], {r, -1, 1}]`



```
RevolutionPlot3D[{r π Root[-256 + 192 #1 - 48 #1^2 + 8 #1^3 - 4 #1^4 + #1^5 &, 4]], {r, -1, 1}]
```



```
RevolutionPlot3D[{r π Root[-256 + 192 #1 - 48 #1^2 + 8 #1^3 - 4 #1^4 + #1^5 &, 5]], {r, -1, 1}]
```

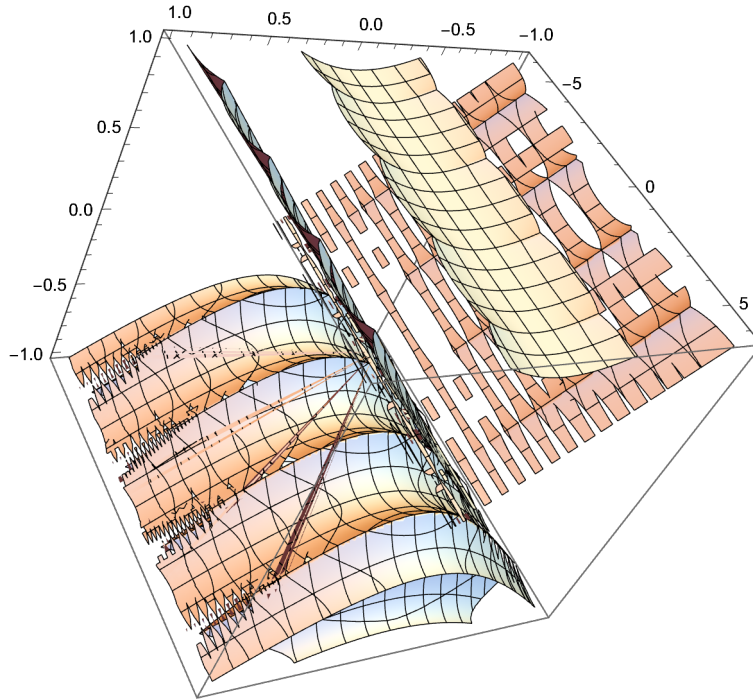


$$\text{Solve}\left[\frac{2 \pi s}{\theta^2} == \frac{2 \pi \frac{(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2})}{\theta}}{\theta}, s\right]$$

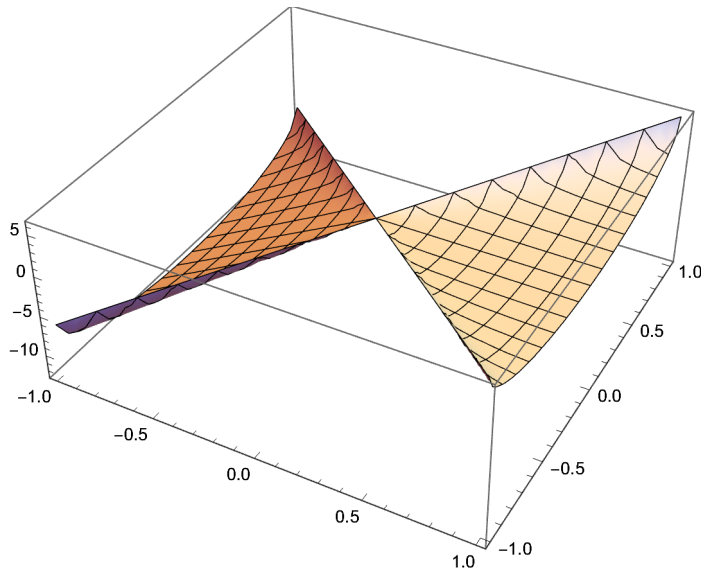
$$\left\{\left\{s \rightarrow -2 \left(-\pi r + \pi \sqrt{r^2 - \eta^2}\right)\right\}\right\}$$

$$\theta = \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)$$

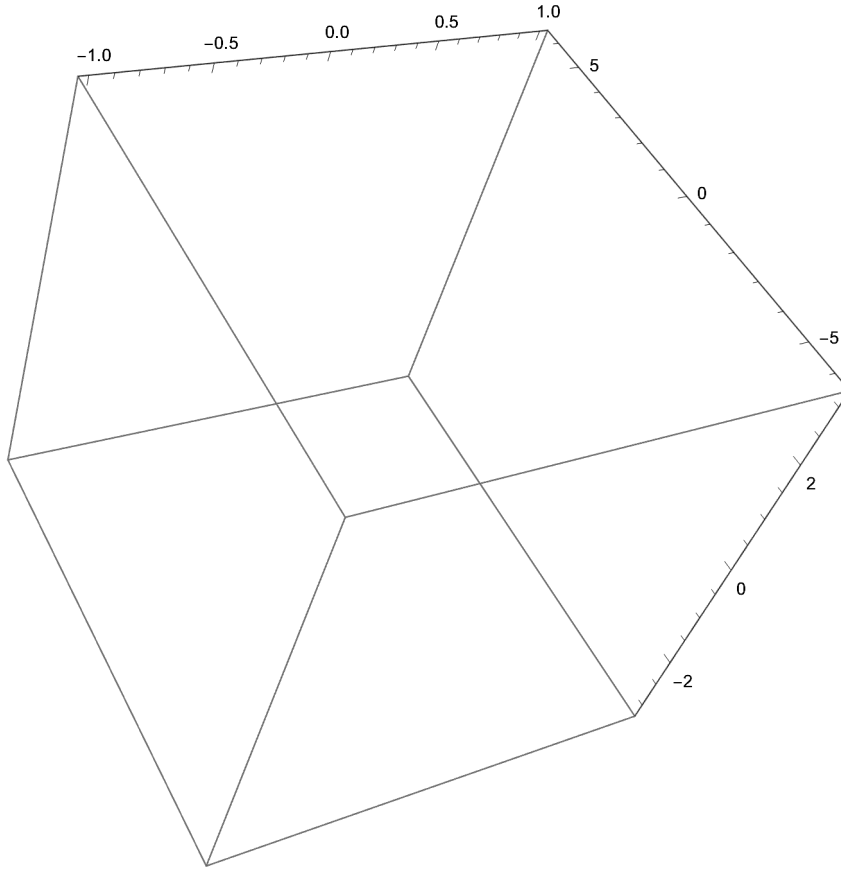
ContourPlot3D $\left[-2 \left(-\pi \left(\frac{2 \pi r-2 \pi \sqrt{r^2-\eta^2}}{2\left(\pi+\sqrt{\pi^2-\pi^2 \operatorname{Sin}[\beta]^2}\right)}+\pi \sqrt{r^2-\eta^2}\right)\right),\right.$   
 $\left.\{r,-1,1\},\{\eta,-1,1\},\{\beta,-2 \pi,2 \pi\}\right]$



Plot3D $\left[-2 \left(-\pi (r)+\pi \sqrt{r^2-\eta^2}\right),\{r,-1,1\},\{\eta,-1,1\}\right]$



$$\text{ContourPlot3D}\left[-2 \left(-\pi \left(\frac{(2 \pi r - 2 \pi \sqrt{r^2 - r^2})}{\theta}\right) + \pi \sqrt{\left(\frac{(2 \pi r - 2 \pi \sqrt{r^2 - r^2})}{(2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}\right)^2 - r^2}\right), \right. \\ \left. \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$$



$$\text{Plot3D}\left[-2 \left(-\pi r + \pi \sqrt{r^2 - \eta^2}\right), \{r, -1, 1\}, \{\eta, -1, 1\}\right]$$

## Addendum No. 2

$$\theta \rightarrow \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} \quad (28)$$

$$\text{Solve}\left[\theta == \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}\right\}$$



$$\theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \quad (29)$$

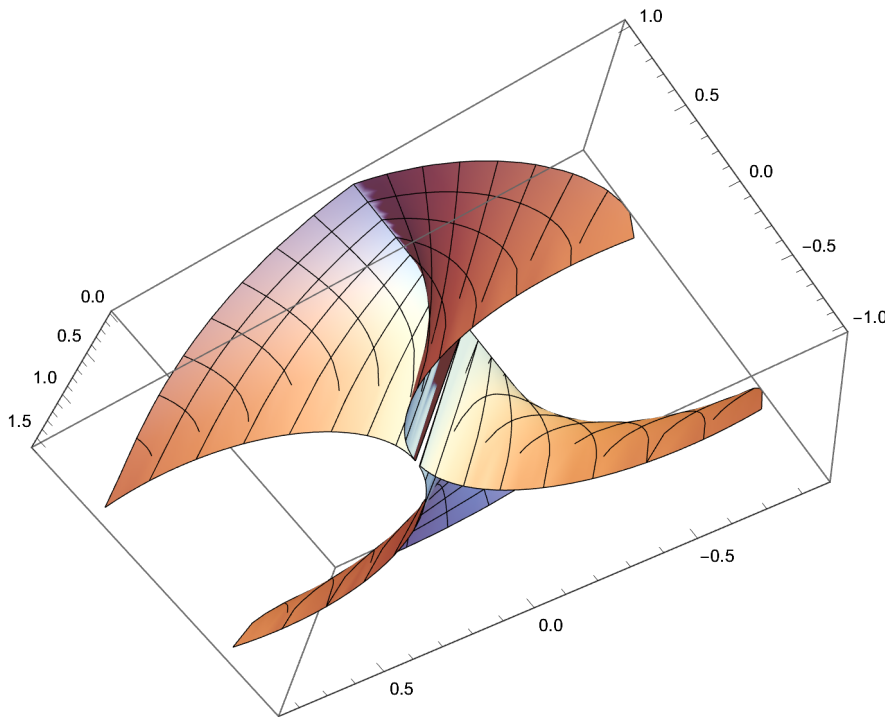
$$\frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \quad (30)$$

$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \quad (31)$$

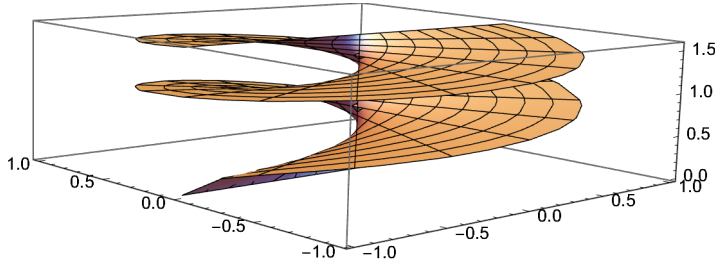
$$\text{Solve} \left[ \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right), \beta \right]$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right\}, \left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right\} \right\}$$

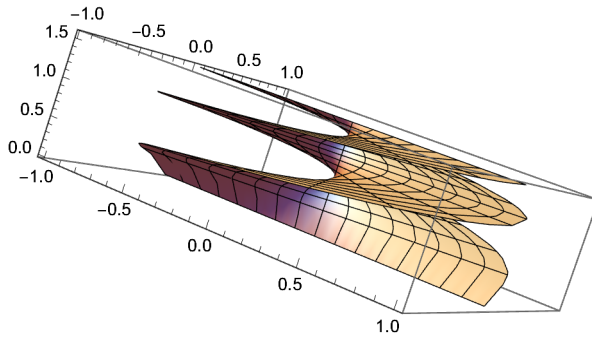
$$\text{RevolutionPlot3D} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right], \{r, -1, 1\}, \{\eta, -1, 1\} \right]$$



$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\sqrt{\frac{\left(\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\right)^2}{r^2}}\right], \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\sqrt{\frac{(\eta)^2}{\left(\frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}}\right)^2}}\right], \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



## Addendum No. 3

### Initial Values

$$\begin{aligned} &\left\{\left\{\theta_1 \rightarrow \frac{2}{3} \left(2\pi - \frac{2\pi}{(17+3\sqrt{33})^{1/3}} + (17+3\sqrt{33})^{1/3}\pi\right)\right\}, \right. \\ &\left\{\theta_2 \rightarrow \frac{4\pi}{3} + \frac{2(1+i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1-i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi\right\}, \\ &\left.\left\{\theta_3 \rightarrow \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi\right\}\right\} \end{aligned} \quad (32)$$

$$\theta_1 := \frac{2}{3} \left( 2\pi - \frac{2\pi}{\left(17 + 3\sqrt{33}\right)^{1/3}} + \left(17 + 3\sqrt{33}\right)^{1/3} \pi \right)$$

$$\theta_2 := \left( \frac{4\pi}{3} + \frac{2(1 + i\sqrt{3})\pi}{3\left(17 + 3\sqrt{33}\right)^{1/3}} - \frac{1}{3}(1 - i\sqrt{3})\left(17 + 3\sqrt{33}\right)^{1/3} \pi \right)$$

$$\theta_3 := \left( \frac{4\pi}{3} + \frac{2(1 - i\sqrt{3})\pi}{3\left(17 + 3\sqrt{33}\right)^{1/3}} - \frac{1}{3}(1 + i\sqrt{3})\left(17 + 3\sqrt{33}\right)^{1/3} \pi \right)$$

$$\eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

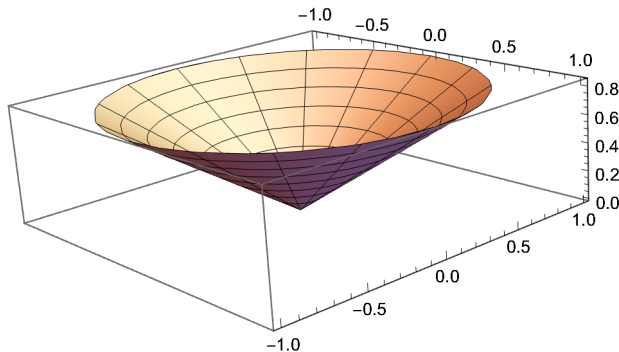
$$\text{Solve}\left[\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\}$$

$$r = \pm \frac{2\pi\eta}{\sqrt{4\pi\theta_1 - \theta_1^2}}, \pm \frac{2\pi\eta}{\sqrt{4\pi\theta_2 - \theta_2^2}}, \frac{2\pi\eta}{\sqrt{4\pi\theta_3 - \theta_3^2}}$$

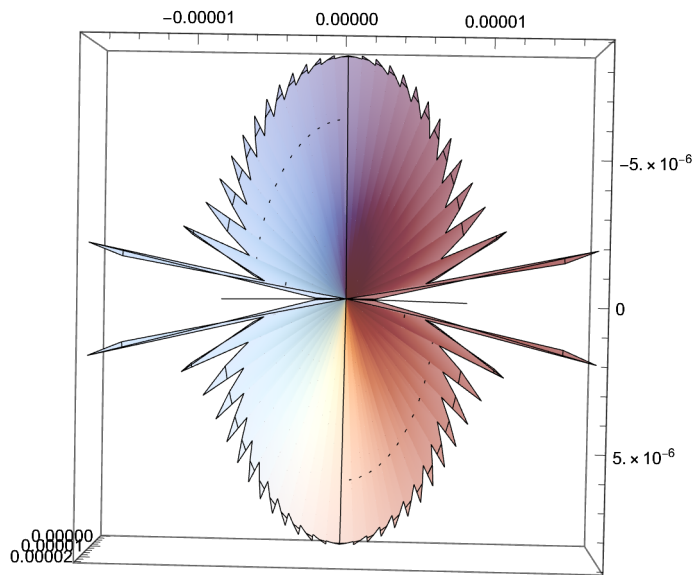
We will now see what the three theta values will show us for the height of the cone.

$$\text{RevolutionPlot3D}\left[\frac{1}{2\pi} \left( \sqrt{\left( 4\pi r^2 \left( \frac{2}{3} \left( 2\pi - \frac{2\pi}{\left(17 + 3\sqrt{33}\right)^{1/3}} + \left(17 + 3\sqrt{33}\right)^{1/3} \pi \right) \right)^2} \right)} \right), \{r, -1, 1\}]$$



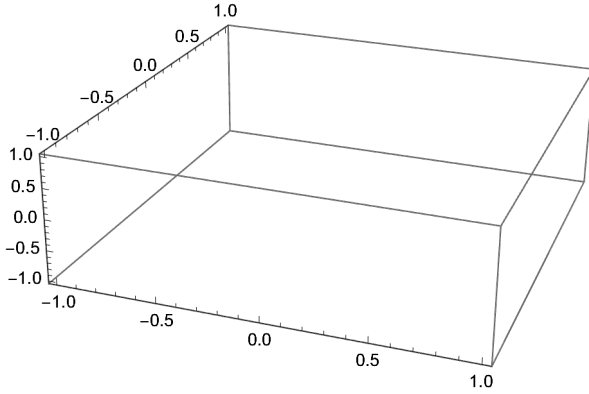
RevolutionPlot3D[

$$\frac{1}{2\pi} \left( \sqrt{\left( 4\pi r^2 \left( \frac{4\pi}{3} + \frac{2(1+i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1-i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right) - \right.} \right. \\ \left. \left. r^2 \left( \frac{4\pi}{3} + \frac{2(1+i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1-i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right)^2 \right)}, \{r, -1, 1\} \right]$$



RevolutionPlot3D[

$$\frac{1}{2\pi} \left( \sqrt{\left( 4\pi r^2 \left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right) - r^2 \left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right)^2} \right)}, \{r, -1, 1\}]$$



## Additional Substitutions of a Known Formula

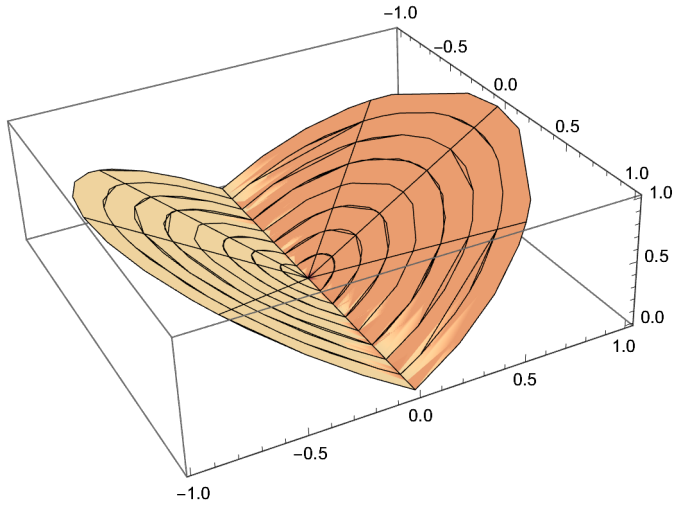
$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\} \right\} \quad (33)$$

$$\text{For this section, } r = 1 \quad (34)$$

$$\frac{2}{3} \left( 2\pi - \frac{2\pi}{(17+3\sqrt{33})^{1/3}} + (17+3\sqrt{33})^{1/3}\pi \right)$$

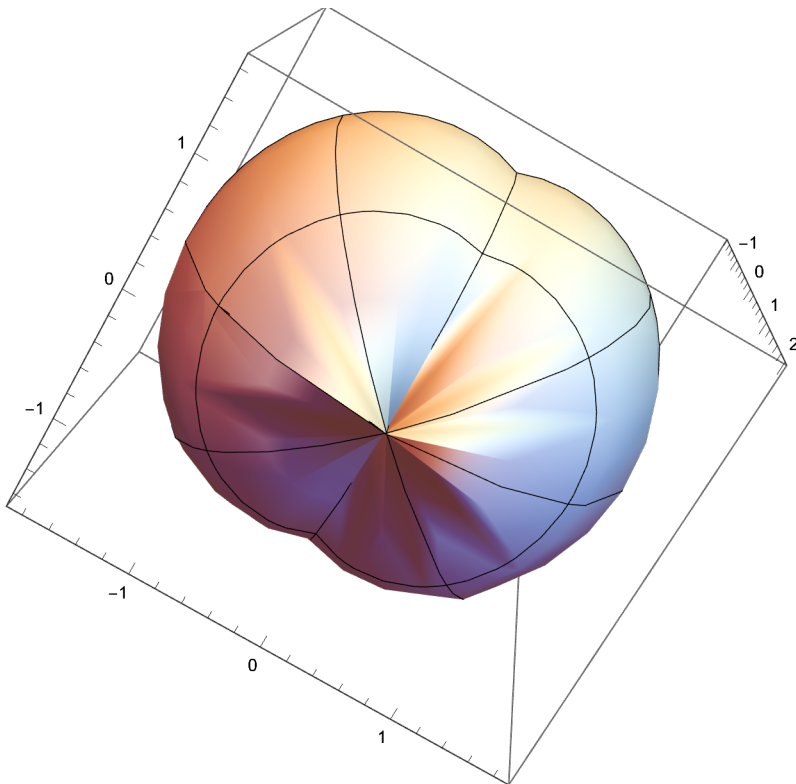
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi(r)^2\left(2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)-(r)^2\left(2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2}}{2\pi},\right.$$

$$\left.\{r,-1,1\},\{\beta,-2\pi,2\pi\}\right]$$



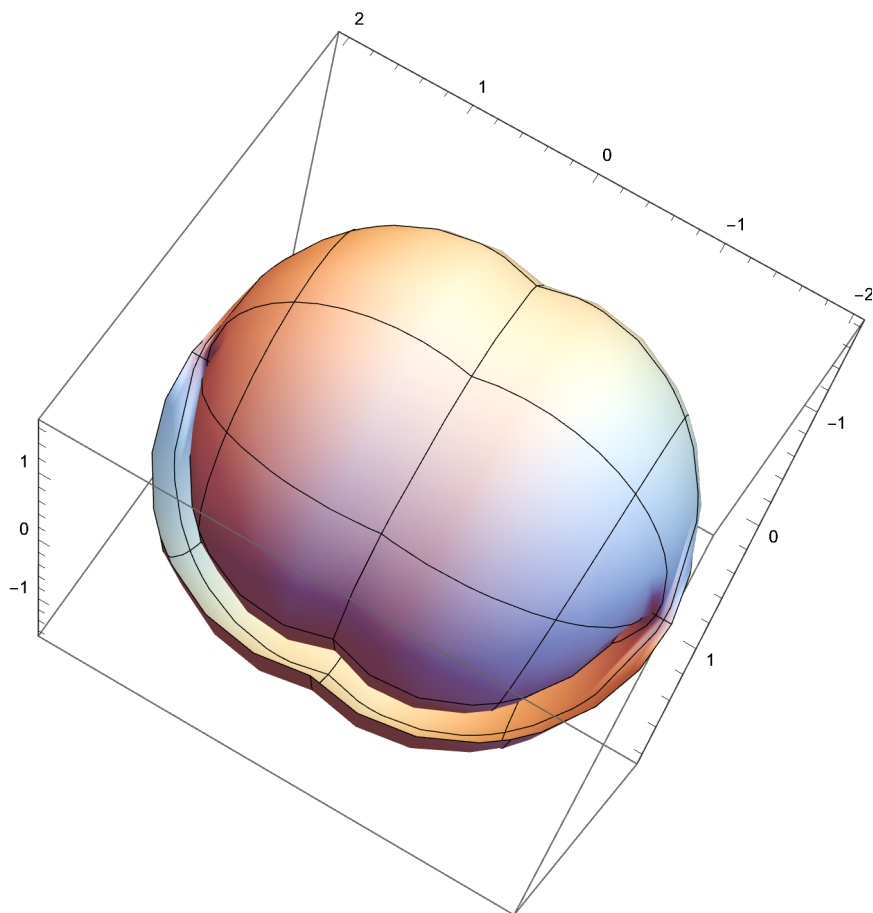
$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi(1)^2(\theta)-(1)^2\left(2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2}}{2\pi},\right.$$

$$\left.\{\theta,-4\pi,4\pi\},\{\beta,-2\pi,2\pi\}\right]$$



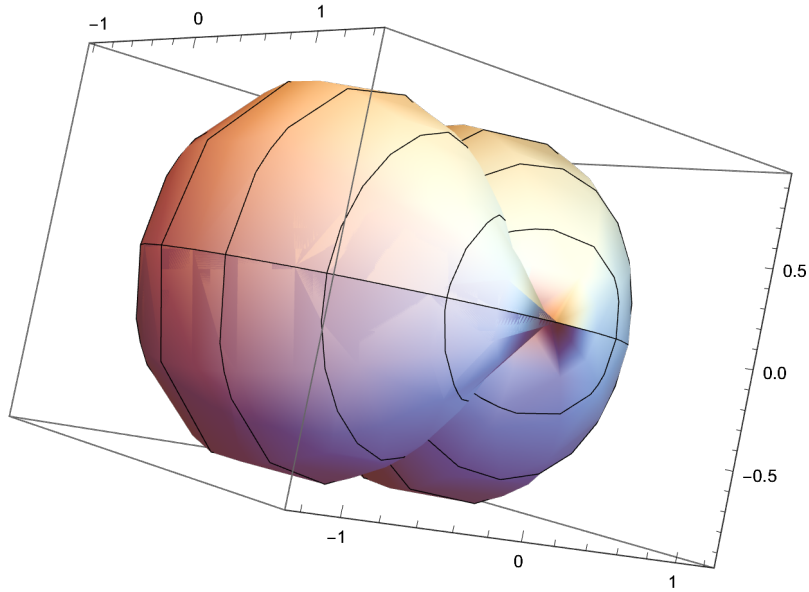
$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi(1)^2(\theta) - (1)^2\left(2\left(\pi - \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}}{2\pi},\right.$$

$$\left.\{\beta, -2\pi, 2\pi\}, \{\theta, -4\pi, 4\pi\}\right]$$

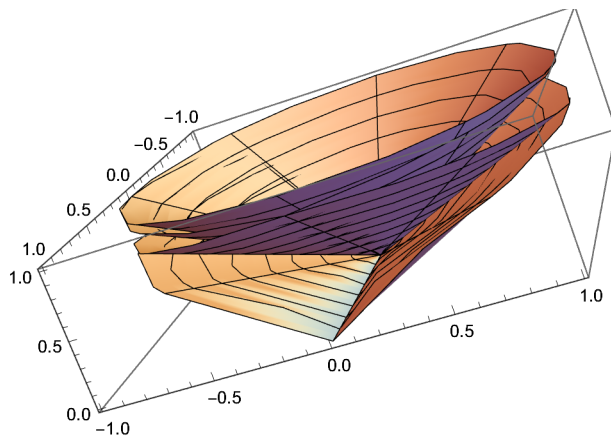


$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi(1)^2(\theta) - (1)^2\left(2\left(\pi - \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}}{2\pi},\right.$$

$$\left.\{\theta, -2\pi, 2\pi\}, \{\beta, -4\pi, 4\pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$$

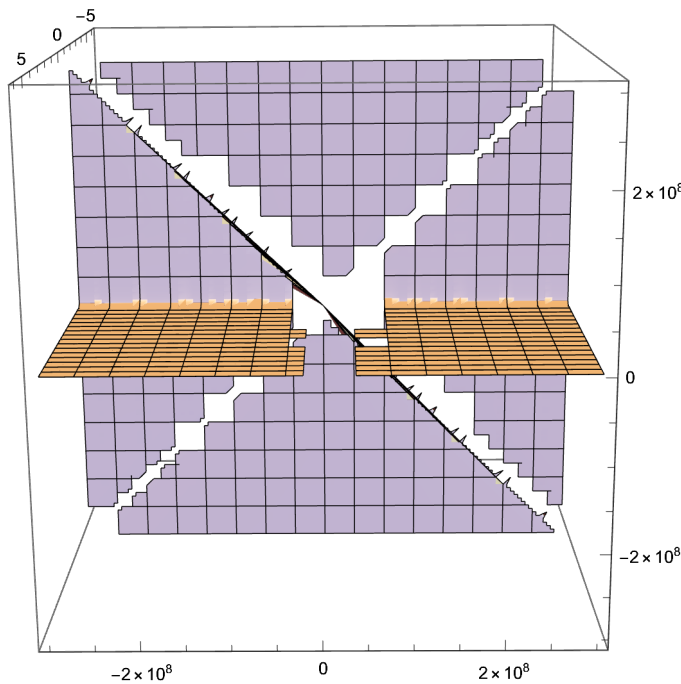




# Addendum No. 5

Substitutions for  $\theta$  in terms of  $\beta$  for the contour plot of radius in terms of the speed of light, angle, and velocity.

```
ContourPlot3D[{-  $\frac{\mathfrak{i} c^3 \sqrt{\theta}}{(c-v)(c+v)\sqrt{-4\pi+\theta}}$ ,  $\frac{\mathfrak{i} c^3 \sqrt{\theta}}{(c-v)(c+v)\sqrt{-4\pi+\theta}}$ },
{ $\theta$ , -2  $\pi$ , 2  $\pi$ }, {v, -((2.99792458 * 10^8)), ((2.99792458 * 10^8))},
{c, -(2.99792458 * 10^8), (2.99792458 * 10^8)}]
```

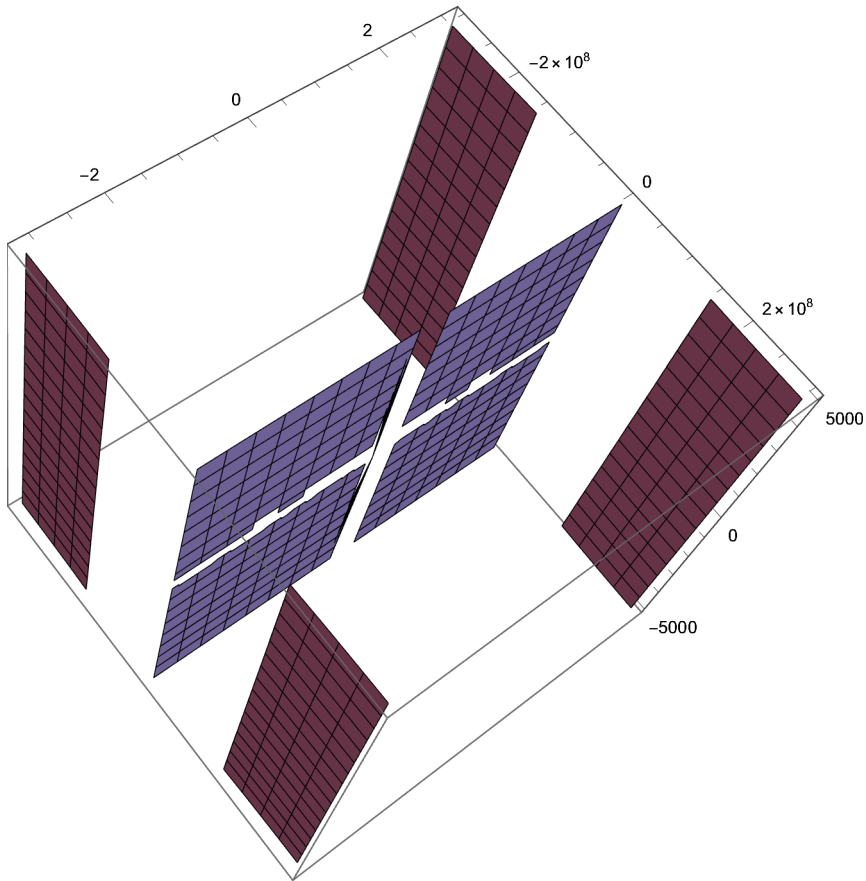


$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\} \right\}$$

$$c := (2.99792458 * 10^8)$$

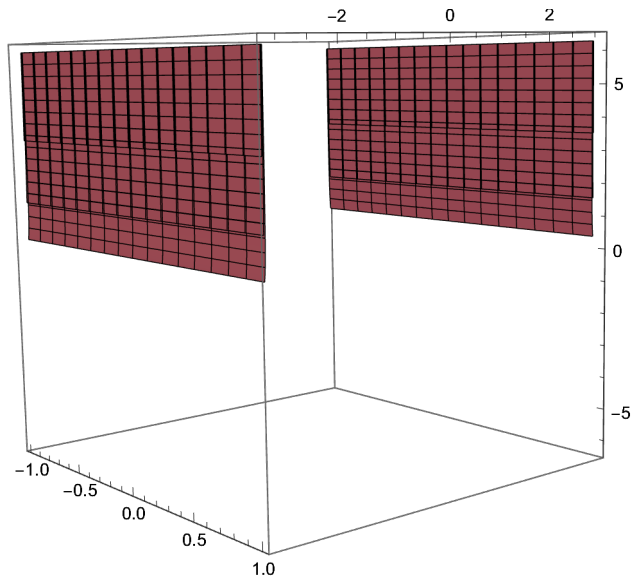
$$\text{ContourPlot3D}\left[\frac{i c^3 \sqrt{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{(c - v)(c + v) \sqrt{-4 \pi + 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}},\right.$$

$$\left.\{c, -(2.99792458 \times 10^8), (2.99792458 \times 10^8)\}, \{\beta, -\pi, \pi\}, \{v, -5000, 5000\}\right]$$



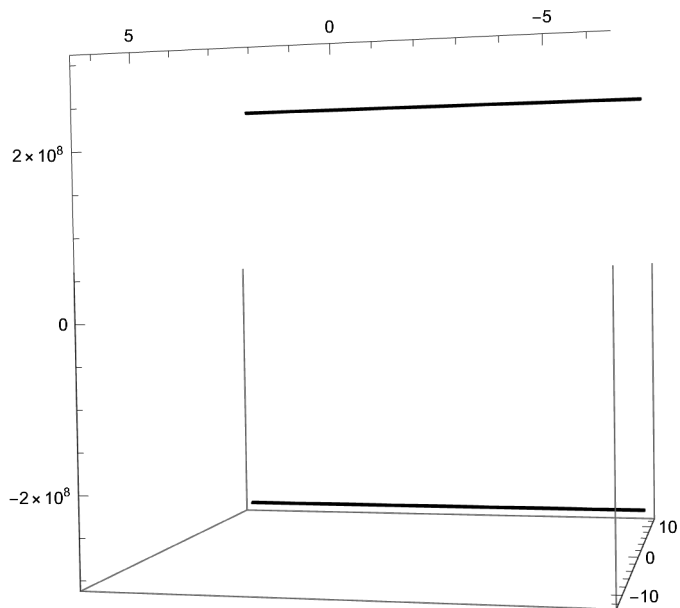
```
ContourPlot3D[
$$\frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4\pi + 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}},$$

{v, -1, 1}, {\beta, -\pi, \pi}, {\theta, -2\pi, 2\pi}]
```



```
ContourPlot3D[
$$\frac{i c^3 \sqrt{2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}}{(c-v)(c+v) \sqrt{-4\pi + \theta}},$$

{\theta, -4\pi, 4\pi},
{\beta, -2\pi, 2\pi}, {v, -(2.99792458 * 10^8), (2.99792458 * 10^8)}]
```



# Addendum No. 6

Application of cone theory to a change in volume of a sphere.

$$(4/3) \pi (r)^3 = \text{Volume of Sphere} \quad (35)$$

$$r \rightarrow \frac{4 \pi^2 \eta}{(2 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \quad (36)$$

$$D[(4/3) \pi r^3, r]$$

$$4 \pi (r)^2 - 4 \pi r_1^2 == (r^2) (\theta^2) = \text{change in surface area}$$

$$\text{Solve}\left[4 \pi \left(\frac{2 \pi r \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 - 4 \pi \left(\sqrt{r^2 - \eta^2}\right)^2 == (r^2) (\theta^2), \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{\frac{(4 \pi - \theta) \theta (4 \pi r^2 - 4 \pi \eta^2 + r^2 \theta^2)}{r^2}}}{4 \pi^{3/2}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{\frac{(4 \pi - \theta) \theta (4 \pi r^2 - 4 \pi \eta^2 + r^2 \theta^2)}{r^2}}}{4 \pi^{3/2}}\right]\right\}\right\}$$

$$\text{Solve}\left[4 \pi \left(\frac{2 \pi r \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 - 4 \pi \left(\sqrt{r^2 - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right)^2 == (r^2) (\theta^2), \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2 \pi + \pi^2}{1 + \pi} - \frac{1}{2} \sqrt{\left(-\frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \text{Sin}[\beta]^2 + 12 \pi^5 \text{Sin}[\beta]^2))\right)}\right\}\right\}$$

$$\left(3 (1 + \pi) \left(16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \text{Sin}[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \text{Sin}[\beta]^2 + \sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \text{Sin}[\beta]^2 + 192 \pi^5 \text{Sin}[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \text{Sin}[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \text{Sin}[\beta]^2)^2}\right)^{1/3}\right) + \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left(16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \text{Sin}[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \text{Sin}[\beta]^2 + \sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \text{Sin}[\beta]^2 + 192 \pi^5 \text{Sin}[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \text{Sin}[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \text{Sin}[\beta]^2)^2}\right)^{1/3}\right)$$

$$\begin{aligned}
& \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{2} \sqrt[4]{\left( -\frac{80\,\pi^2}{3\,(1+\pi)} + \frac{8\,(2\pi+\pi^2)^2}{(1+\pi)^2} - \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\sin[\beta]^2 + 12\,\pi^5\,\sin[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \right. \right. \\
& \left. \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \right. \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} - \\
& \left( \frac{128\,\pi^3}{1+\pi} - \frac{320\,\pi^2\,(2\pi+\pi^2)}{(1+\pi)^2} + \frac{64\,(2\pi+\pi^2)^3}{(1+\pi)^3} \right) \sqrt[4]{\left( -\frac{40\,\pi^2}{3\,(1+\pi)} + \right.} \\
& \left. \frac{4\,(2\pi+\pi^2)^2}{(1+\pi)^2} + \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\sin[\beta]^2 + 12\,\pi^5\,\sin[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) + \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) +
\end{aligned}$$

$$\left. \left( (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2\pi + \pi^2)^2 \sin[\beta]^2 \right)^{1/3} \right) \Bigg] \Bigg\},$$
$$\left\{ \theta \rightarrow \frac{2\pi + \pi^2}{1 + \pi} - \frac{1}{2} \sqrt{\left( -\frac{40\pi^2}{3(1 + \pi)} + \frac{4(2\pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12\pi^5 + 12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2)) \right) / \right.$$
$$\left( 3(1 + \pi) \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right. \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) +$$
$$\frac{1}{3 \times 2^{1/3}(1 + \pi)} \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) +$$
$$\frac{1}{2} \sqrt{\left( -\frac{80\pi^2}{3(1 + \pi)} + \frac{8(2\pi + \pi^2)^2}{(1 + \pi)^2} - (16 \times 2^{1/3} (\pi^4 - 12\pi^5 + 12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2)) / \right.$$
$$\left( 3(1 + \pi) \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right. \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) -$$
$$\frac{1}{3 \times 2^{1/3}(1 + \pi)} \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} -$$



$$\begin{aligned}
& \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{2} \sqrt[4]{\left( -\frac{80\,\pi^2}{3\,(1+\pi)} + \frac{8\,(2\pi+\pi^2)^2}{(1+\pi)^2} - \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\text{Sin}[\beta]^2 + 12\,\pi^5\,\text{Sin}[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + \right. \right. \\
& \quad \left. 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \right. \\
& \quad \left. \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2)^3 +} \right. \\
& \quad \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \quad \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^{1/3} \right) \Bigg) - \\
& \frac{1}{3 \times 2^{1/3} \,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \\
& \quad \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2)^3 +} \\
& \quad \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^{1/3} \Bigg) + \\
& \left( \frac{128\,\pi^3}{1+\pi} - \frac{320\,\pi^2\,(2\pi+\pi^2)}{(1+\pi)^2} + \frac{64\,(2\pi+\pi^2)^3}{(1+\pi)^3} \right) \sqrt[4]{\left( -\frac{40\,\pi^2}{3\,(1+\pi)} + \right.} \\
& \quad \left. \frac{4\,(2\pi+\pi^2)^2}{(1+\pi)^2} + \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\text{Sin}[\beta]^2 + 12\,\pi^5\,\text{Sin}[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \\
& \quad \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2)^3 +} \\
& \quad \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + \right. \\
& \quad \left. 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^{1/3} \Bigg) \Bigg) + \\
& \frac{1}{3 \times 2^{1/3} \,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \\
& \quad \sqrt[4]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2)^3 +} \\
& \quad \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + \right.
\end{aligned}$$





$$\left( \frac{128 \pi^3}{1 + \pi} - \frac{320 \pi^2 (2 \pi + \pi^2)}{(1 + \pi)^2} + \frac{64 (2 \pi + \pi^2)^3}{(1 + \pi)^3} \right) \Bigg/ \left( 4 \sqrt[3]{ - \frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2)) \right) \Bigg/$$

$$\left( 3 (1 + \pi) \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt[3]{ -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \right) +$$

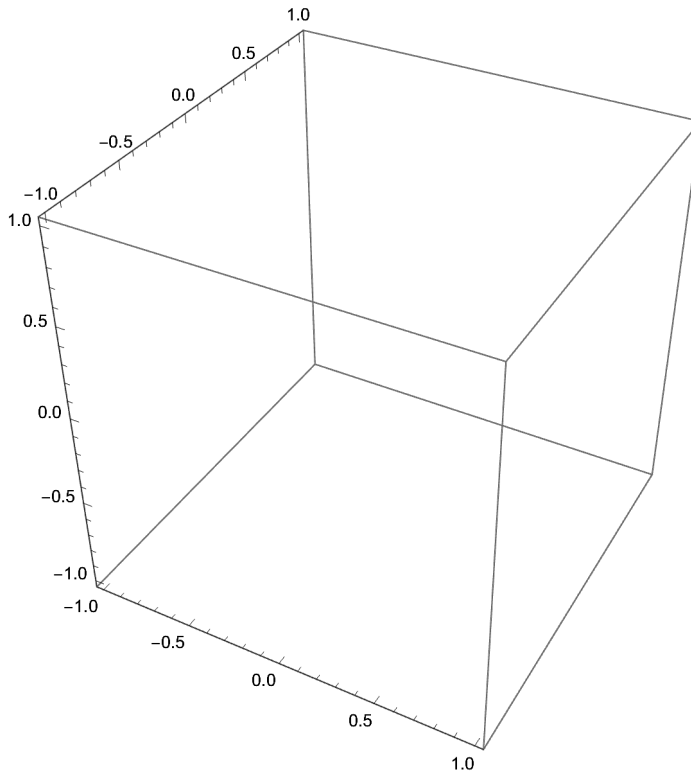
$$\frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt[3]{ -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) \Bigg) \Bigg) \Bigg\} \Bigg\}$$

$$\text{SphericalPlot3D} \left[ \frac{2 \pi + \pi^2}{1 + \pi} - \frac{1}{2} \sqrt[3]{ - \frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} \left( \pi^4 - 12 \pi^5 + 12 \pi^4 \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right]^2 + 12 \pi^5 \sin[\beta]^2 \right) \right) \Bigg/}$$

$$\left( 3 (1 + \pi) \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt[3]{ -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \right) +$$

$$\begin{aligned}
& \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - 23\,040 \pi^6 \right. \\
& \quad (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt{\left( -4 \left( 16 \pi^4 - 192 \pi^5 + \right. \right.} \\
& \quad \left. \left. 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right]^2 \right)^3 + \right.} \\
& \quad \left. \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - 23\,040 \pi^6 (1 + \pi) \right. \right. \\
& \quad \left. \left. \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{2} \sqrt{\left( -\frac{80 \pi^2}{3 (1 + \pi)} + \frac{8 (2 \pi + \pi^2)^2}{(1 + \pi)^2} - (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2)) \right) /} \\
& \quad \left( 3 (1 + \pi) \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - 23\,040 \pi^6 (1 + \pi) \right. \right. \\
& \quad \left. \left. \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \right. \right. \\
& \quad \left. \sqrt{\left( -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + \right. \right. \\
& \quad \left. \left. (16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - \right. \right. \\
& \quad \left. \left. 23\,040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - \right. \\
& \quad 23\,040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \\
& \quad \sqrt{\left( -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + \right.} \\
& \quad \left. \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - \right. \right. \\
& \quad \left. \left. 23\,040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 \right)^2 \right)^{1/3} - \\
& \left( \frac{128 \pi^3}{1 + \pi} - \frac{320 \pi^2 (2 \pi + \pi^2)}{(1 + \pi)^2} + \frac{64 (2 \pi + \pi^2)^3}{(1 + \pi)^3} \right) / \left( 4 \sqrt{\left( -\frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + \right. \right. \\
& \quad \left. \left. (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2)) \right) /} \right. \\
& \quad \left. \left( 3 (1 + \pi) \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \\
& \sqrt{\left(-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2)^3 + \right. \\
& \quad \left.(16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2\right)^2\right)^{1/3}} + \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \sqrt{\left(-4\right. \\
& \quad \left.(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2)^3 + (16\,000\,\pi^6 + 6912\right. \\
& \quad \left.\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\right. \\
& \quad \left.\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2\right)^2\right)^{1/3}} \Bigg) \Bigg] , \{\beta, -10, 10\}, \{\theta, -2\pi, 2\pi\} ]
\end{aligned}$$



$$\text{Solve}\left[4 \pi \left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 - 4 \pi \left(\sqrt{r^2 - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right)^2 == (r^2) (\theta^2), \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{-\theta (-4 \pi + \theta) (4 \pi^2 - 4 \pi \theta + \theta^2 + \pi \theta^2)}}{4 \pi^2}\right]\right\},\right.$$

$$\left.\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{-\theta (-4 \pi + \theta) (4 \pi^2 - 4 \pi \theta + \theta^2 + \pi \theta^2)}}{4 \pi^2}\right]\right\}\right\}$$

$$\text{Solve}\left[\text{ArcSin}\left[\frac{\sqrt{-\theta (-4 \pi + \theta) (4 \pi^2 - 4 \pi \theta + \theta^2 + \pi \theta^2)}}{4 \pi^2}\right] == \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right], \theta\right]$$

$$\{\{\theta \rightarrow 0\},$$

$$\left\{\theta \rightarrow \frac{3 \pi}{1 + \pi} + \frac{2 \pi^2}{1 + \pi} + \frac{1}{2} \sqrt{\left(-\frac{32 \pi^2}{1 + \pi} - \frac{32 \pi^3}{3 (1 + \pi)} + \frac{4 (3 \pi + 2 \pi^2)^2}{(1 + \pi)^2} + 1 \sqrt[3]{3 (1 + \pi) \left(2 \sqrt[3]{6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)}\right)}\right\} +$$

$$\frac{1}{3 (1 + \pi)} \left(192 \pi^5 + 256 \pi^6\right) \left(2 \sqrt[3]{6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}}\right)^{1/3} -$$

$$\frac{1}{2} \sqrt{\left(-\frac{64 \pi^2}{1 + \pi} - \frac{64 \pi^3}{3 (1 + \pi)} + \frac{8 (3 \pi + 2 \pi^2)^2}{(1 + \pi)^2} - 1 \sqrt[3]{3 (1 + \pi) \left(2 \sqrt[3]{6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)}\right)} -$$

$$\frac{1}{3 (1 + \pi)} \left(192 \pi^5 + 256 \pi^6\right) \left(2 \sqrt[3]{6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}}\right)^{1/3} +$$

$$\left(\frac{1728 \pi^3}{(1 + \pi)^3} + \frac{3456 \pi^4}{(1 + \pi)^3} + \frac{2304 \pi^5}{(1 + \pi)^3} + \frac{512 \pi^6}{(1 + \pi)^3} - \frac{2304 \pi^3}{(1 + \pi)^2} - \frac{2304 \pi^4}{(1 + \pi)^2} - \frac{512 \pi^5}{(1 + \pi)^2} + \frac{640 \pi^3}{1 + \pi}\right) \sqrt[3]{}$$

$$\left(4 \sqrt{\left(-\frac{32 \pi^2}{1 + \pi} - \frac{32 \pi^3}{3 (1 + \pi)} + \frac{4 (3 \pi + 2 \pi^2)^2}{(1 + \pi)^2} + 1 \sqrt[3]{3 (1 + \pi) \left(2 \sqrt[3]{6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)}\right)}\right)^{1/3} +$$

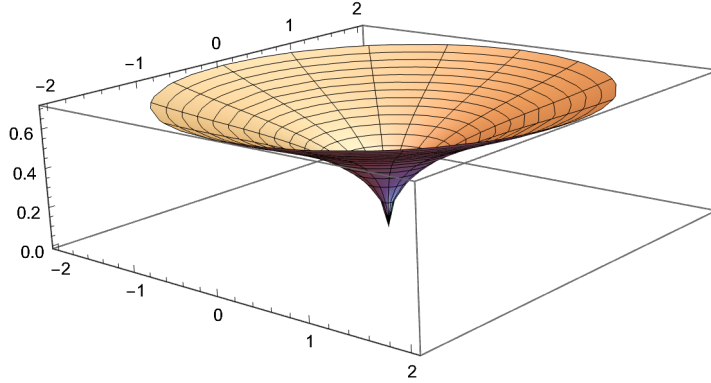
$$\frac{1}{3 (1 + \pi)} \left(192 \pi^5 + 256 \pi^6\right) \left(2 \sqrt[3]{6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}}\right)^{1/3} \sqrt[3]{}$$

$$\sqrt[3]{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)^{1/3} \sqrt[3]{}$$

$$\text{Solve}\left[\text{ArcSin}\left[\frac{\sqrt{-\theta(-4\pi+\theta)(4\pi^2-4\pi\theta+\theta^2+\pi\theta^2)}}{4\pi^2}\right]==\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right],\theta\right]$$

$$\left\{\{\theta\rightarrow 0\},\{\theta\rightarrow 4\pi\},\left\{\theta\rightarrow\frac{4\pi}{1+\pi}\right\}\right\}$$

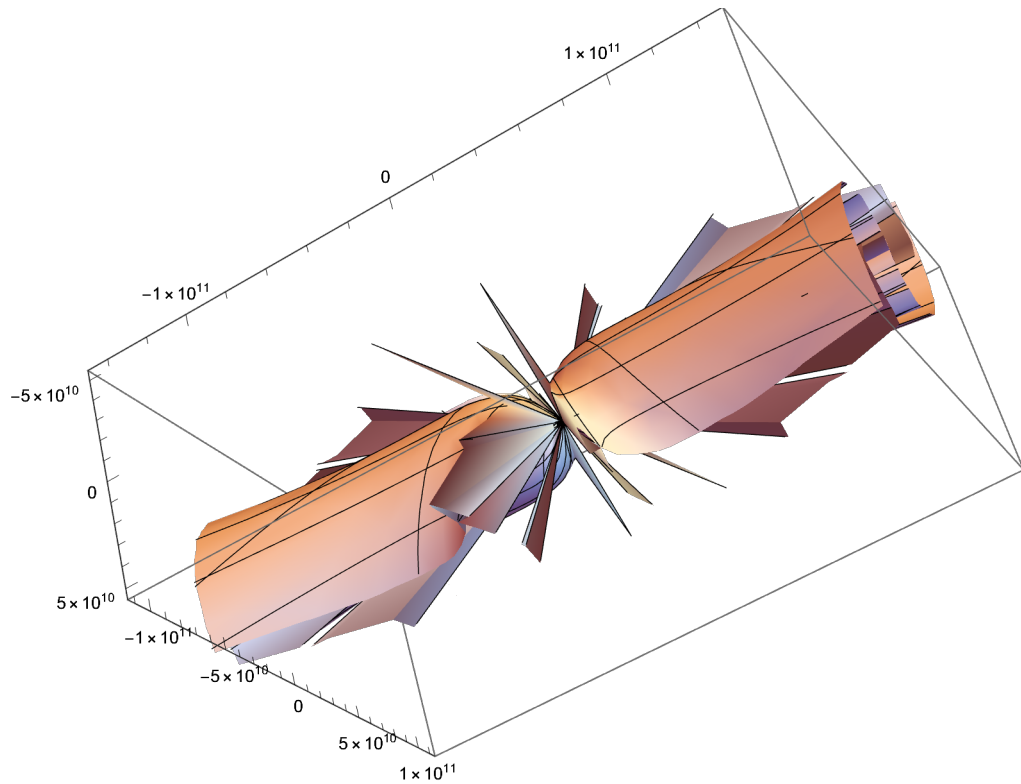
RevolutionPlot3D[ArcSin[ $\frac{\sqrt{-\theta(-4\pi + \theta)(4\pi^2 - 4\pi\theta + \theta^2 + \pi\theta^2)}}{4\pi^2}$ ], { $\theta, -2\pi, 2$ }]



SphericalPlot3D[ $\left(2\pi\theta\pi\left(\left(\sqrt{-1.1294090667581471\theta + 8.987551787368176\theta^2 + 3.5481432270250993\sin^2[\beta]}\right)\right)\right)/\left(\sqrt{\left(-12.566370614359172\theta + \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2\sin^2[\beta])\right)/\left(6(-\pi^3 + 18\pi^3\sin^2[\beta] + 3\sqrt{3}\sqrt{-\pi^6\sin^2[\beta] + 11\pi^6\sin^4[\beta] + \pi^6\sin^6[\beta]}\right)^{1/3}\right) + \frac{2}{3}(-\pi^3 + 18\pi^3\sin^2[\beta] + 3\sqrt{3}\sqrt{-\pi^6\sin^2[\beta] + 11\pi^6\sin^4[\beta] + \pi^6\sin^6[\beta]})^{1/3}\right)^2 + 39.47841760435743\sin^2[\beta]}\right)\right)/\left(\sqrt{4\pi\theta - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin^2[\beta]}\right)\right)^2}\right)\right)$

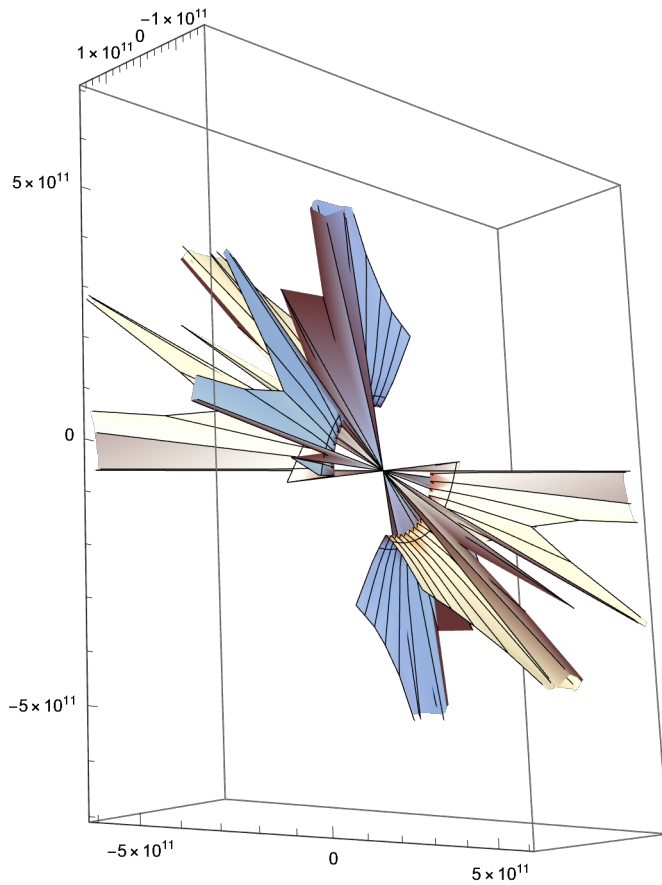
$\left(\frac{3\pi}{1+\pi} + \frac{2\pi^2}{1+\pi} + \frac{1}{2}\sqrt{\left(-\frac{32\pi^2}{1+\pi} - \frac{32\pi^3}{3(1+\pi)} + \frac{4(3\pi + 2\pi^2)^2}{(1+\pi)^2} + \frac{1}{3(1+\pi)}\left(192\pi^5 + 256\pi^6\right)\left(2\sqrt{6912\pi^7 + 9216\pi^8 + 8192\pi^9 + \sqrt{47775744\pi^{14} + 99090432\pi^{15} + 84934656\pi^{16}}}\right)^{1/3}\right)} - \frac{1}{3(1+\pi)}\left(192\pi^5 + 256\pi^6\right)\left(2\sqrt{6912\pi^7 + 9216\pi^8 + 8192\pi^9 + \sqrt{47775744\pi^{14} + 99090432\pi^{15} + 84934656\pi^{16}}}\right)^{1/3}\right)$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{64 \pi^2}{1+\pi} - \frac{64 \pi^3}{3(1+\pi)} + \frac{8(3\pi+2\pi^2)^2}{(1+\pi)^2} - 1 \right) / \left( 3(1+\pi) \left( 2 / \left( 6912 \pi^7 + 9216 \pi^8 + \right. \right. \right. \\
& \quad \left. \left. \left. 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}} \right) \right)^{1/3} \right) - \\
& \quad \frac{1}{3(1+\pi)} (192 \pi^5 + 256 \pi^6) \left( 2 / \left( 6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \right. \right. \\
& \quad \left. \left. \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}} \right) \right)^{1/3} + \\
& \quad \left( \frac{1728 \pi^3}{(1+\pi)^3} + \frac{3456 \pi^4}{(1+\pi)^3} + \frac{2304 \pi^5}{(1+\pi)^3} + \frac{512 \pi^6}{(1+\pi)^3} - \frac{2304 \pi^3}{(1+\pi)^2} - \frac{2304 \pi^4}{(1+\pi)^2} - \frac{512 \pi^5}{(1+\pi)^2} + \frac{640 \pi^3}{1+\pi} \right) / \\
& \quad \left( 4 \sqrt{\left( -\frac{32 \pi^2}{1+\pi} - \frac{32 \pi^3}{3(1+\pi)} + \frac{4(3\pi+2\pi^2)^2}{(1+\pi)^2} + 1 \right) / \left( 3(1+\pi) \left( 2 / \left( 6912 \pi^7 + 9216 \pi^8 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}} \right) \right)^{1/3} \right) + \\
& \quad \frac{1}{3(1+\pi)} (192 \pi^5 + 256 \pi^6) \left( 2 / \left( 6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \right. \right. \\
& \quad \left. \left. \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}} \right) \right)^{1/3} \Bigg) \Bigg) \Bigg) \Bigg) \Bigg), \\
& \left\{ \beta, -\pi, \pi \right\}, \left\{ \theta, -2\pi, 2\pi \right\} \Big]
\end{aligned}$$



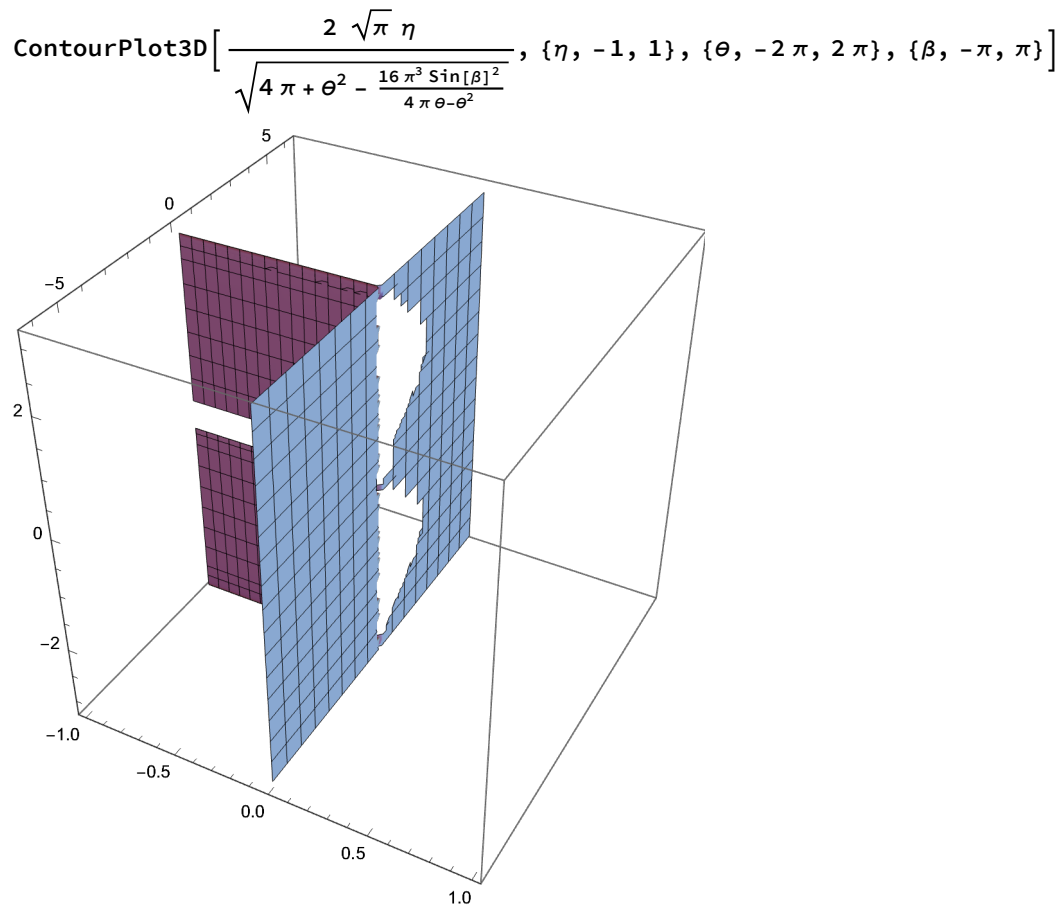


$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left(2 \pi \theta 2 \pi \left(\left(\sqrt{\left(-1.1294090667581471 \cdot \pi^{18} \theta + \right.\right.\right.\right.\right. \\
& \quad \left.\left.\left.8.987551787368176 \cdot \pi^{16} \theta^2 + 3.5481432270250993 \cdot \pi^{18} \sin[\beta]^2\right)\right)\right) / \\
& \quad \left.\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)\right)\right) / \\
& \quad \left(\sqrt{4 \pi \theta - \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}\right) \left(\frac{3 \pi}{1 + \pi} + \frac{2 \pi^2}{1 + \pi} + \right. \\
& \quad \frac{1}{2} \sqrt{\left(-\frac{32 \pi^2}{1 + \pi} - \frac{32 \pi^3}{3(1 + \pi)} + \frac{4(3 \pi + 2 \pi^2)^2}{(1 + \pi)^2} + 1 / \left(3(1 + \pi) \left(2 / \left(6912 \pi^7 + 9216 \pi^8 + \right.\right.\right.\right. \\
& \quad \left.\left.\left.8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)\right)^{1/3}\right) + } \\
& \quad \frac{1}{3(1 + \pi)} (192 \pi^5 + 256 \pi^6) \left(2 / \left(6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \right.\right. \\
& \quad \left.\left.\sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)\right)^{1/3}\bigg) - \\
& \quad \frac{1}{2} \sqrt{\left(-\frac{64 \pi^2}{1 + \pi} - \frac{64 \pi^3}{3(1 + \pi)} + \frac{8(3 \pi + 2 \pi^2)^2}{(1 + \pi)^2} - 1 / \left(3(1 + \pi) \left(2 / \left(6912 \pi^7 + 9216 \pi^8 + \right.\right.\right.\right. \\
& \quad \left.\left.\left.8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)\right)^{1/3}\right) - } \\
& \quad \frac{1}{3(1 + \pi)} (192 \pi^5 + 256 \pi^6) \left(2 / \left(6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \right.\right. \\
& \quad \left.\left.\sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)\right)^{1/3} + \\
& \quad \left(\frac{1728 \pi^3}{(1 + \pi)^3} + \frac{3456 \pi^4}{(1 + \pi)^3} + \frac{2304 \pi^5}{(1 + \pi)^3} + \frac{512 \pi^6}{(1 + \pi)^3} - \frac{2304 \pi^3}{(1 + \pi)^2} - \frac{2304 \pi^4}{(1 + \pi)^2} - \frac{512 \pi^5}{(1 + \pi)^2} + \frac{640 \pi^3}{1 + \pi}\right) / \\
& \quad \left(4 \sqrt{\left(-\frac{32 \pi^2}{1 + \pi} - \frac{32 \pi^3}{3(1 + \pi)} + \frac{4(3 \pi + 2 \pi^2)^2}{(1 + \pi)^2} + 1 / \left(3(1 + \pi) \left(2 / \left(6912 \pi^7 + 9216 \pi^8 + \right.\right.\right.\right. \right. \\
& \quad \left.\left.\left.8192 \pi^9 + \sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)\right)^{1/3}\right) + } \\
& \quad \frac{1}{3(1 + \pi)} (192 \pi^5 + 256 \pi^6) \left(2 / \left(6912 \pi^7 + 9216 \pi^8 + 8192 \pi^9 + \right.\right. \\
& \quad \left.\left.\sqrt{47775744 \pi^{14} + 99090432 \pi^{15} + 84934656 \pi^{16}}\right)\right)^{1/3}\bigg)\bigg)\bigg)\bigg), \\
& \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



$$\text{Solve}\left[4 \pi \left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 - 4 \pi \left(\sqrt{r^2 - \eta^2}\right)^2 == (r^2) (\theta^2), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \sqrt{\pi} \eta}{\sqrt{4 \pi + \theta^2 - \frac{16 \pi^3 \sin[\beta]^2}{4 \pi \theta - \theta^2}}}\right\}, \left\{r \rightarrow \frac{2 \sqrt{\pi} \eta}{\sqrt{4 \pi + \theta^2 - \frac{16 \pi^3 \sin[\beta]^2}{4 \pi \theta - \theta^2}}}\right\}\right\}$$



$$2 \pi r - 2 \pi r_1 = \theta r$$

$$(2 \pi r - 2 \pi r_1) (2 \pi r - 2 \pi r_1) = (\theta r) (\theta r)$$

$$(2 \pi r - 2 \pi r_1) (2 \pi r - 2 \pi r_1)$$

$$\text{Expand}\left[(2 \pi r - 2 \pi r_1)^2\right]$$

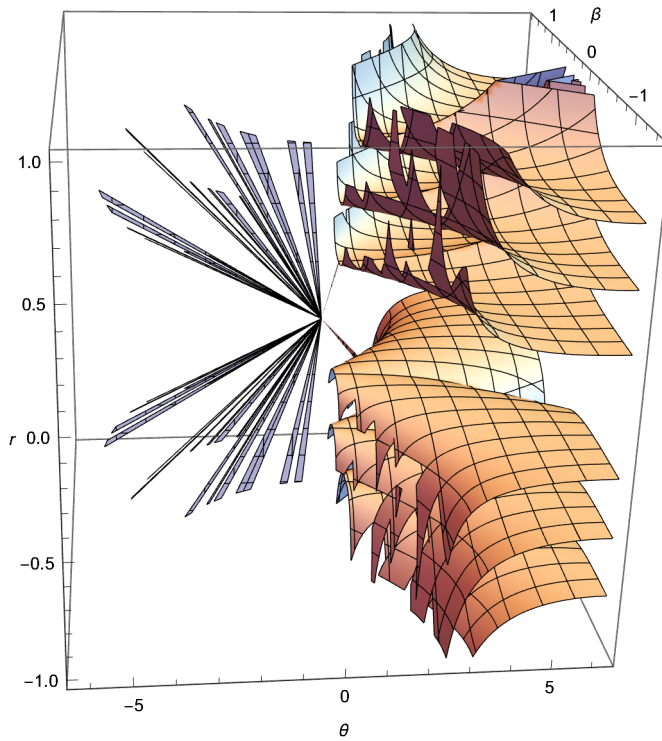
$$4 \pi^2 r^2 - 8 \pi^2 r r_1 + 4 \pi^2 r_1^2 == (\theta r) (\theta r)$$

$$\text{Solve}\left[4 \pi^2 \left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 -\right.$$

$$\left.8 \pi^2 \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{r^2 - \eta^2} + 4 \pi^2 \left(\left(\sqrt{r^2 - \eta^2}\right)^2\right) == (\theta r) (\theta r), \eta\right]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{\left( \frac{16 \pi^2 r^2 \theta^2}{16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \frac{8 \pi r^2 \theta^3}{16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \frac{3 r^2 \theta^4}{16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} + \frac{2 r^2 \theta^5}{\pi (16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \frac{r^2 \theta^6}{4 \pi^2 (16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \frac{16 \pi^3 r^2 \theta \sin[\beta]^2}{16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} + \frac{4 \pi^2 r^2 \theta^2 \sin[\beta]^2}{16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - (2 \sqrt{(64 \pi^{11} r^4 \theta^5 \sin[\beta]^2 - 48 \pi^{10} r^4 \theta^6 \sin[\beta]^2 + 12 \pi^9 r^4 \theta^7 \sin[\beta]^2 - \pi^8 r^4 \theta^8 \sin[\beta]^2)}) / (\pi^4 (16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4))) \right\} \right\},$$

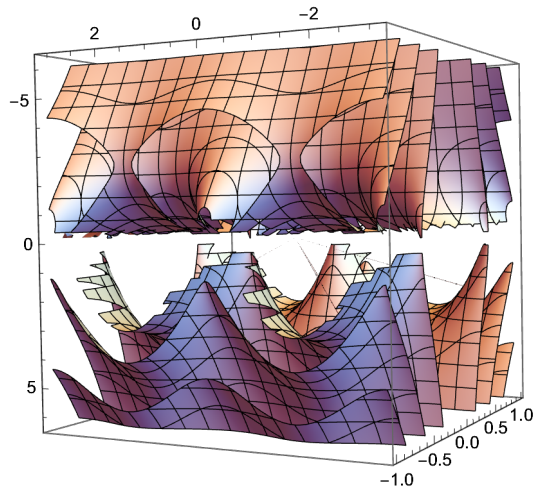
```
ContourPlot3D[
  Sqrt[
    (
      (16 π^2 r^2 θ^2) / (16 π^2 θ^2 - 8 π θ^3 + θ^4) -
      (8 π r^2 θ^3) / (16 π^2 θ^2 - 8 π θ^3 + θ^4) -
      (3 r^2 θ^4) / (16 π^2 θ^2 - 8 π θ^3 + θ^4) +
      (2 r^2 θ^5) / (π (16 π^2 θ^2 - 8 π θ^3 + θ^4)) -
      (r^2 θ^6) / (4 π^2 (16 π^2 θ^2 - 8 π θ^3 + θ^4)) -
      (16 π^3 r^2 θ Sin[β]^2) / (16 π^2 θ^2 - 8 π θ^3 + θ^4) +
      (4 π^2 r^2 θ^2 Sin[β]^2) / (16 π^2 θ^2 - 8 π θ^3 + θ^4) +
      (2 Sqrt[(64 π^11 r^4 θ^5 Sin[β]^2 - 48 π^10 r^4 θ^6 Sin[β]^2 + 12 π^9 r^4 θ^7 Sin[β]^2 - π^8 r^4 θ^8 Sin[β]^2)]) /
      (π^4 (16 π^2 θ^2 - 8 π θ^3 + θ^4))
    )
  ], {r, -1, 1},
  {θ, -2 π, 2 π}, {β, -π / 2, π / 2}, AxesLabel -> Automatic]
```



```
Solve[4 π (
  (2 π r Sin[β]) / (sqrt[4 π θ - θ^2])
)^2 - 4 π (sqrt[r^2 - η^2])^2 == (r^2) (θ^2), η]

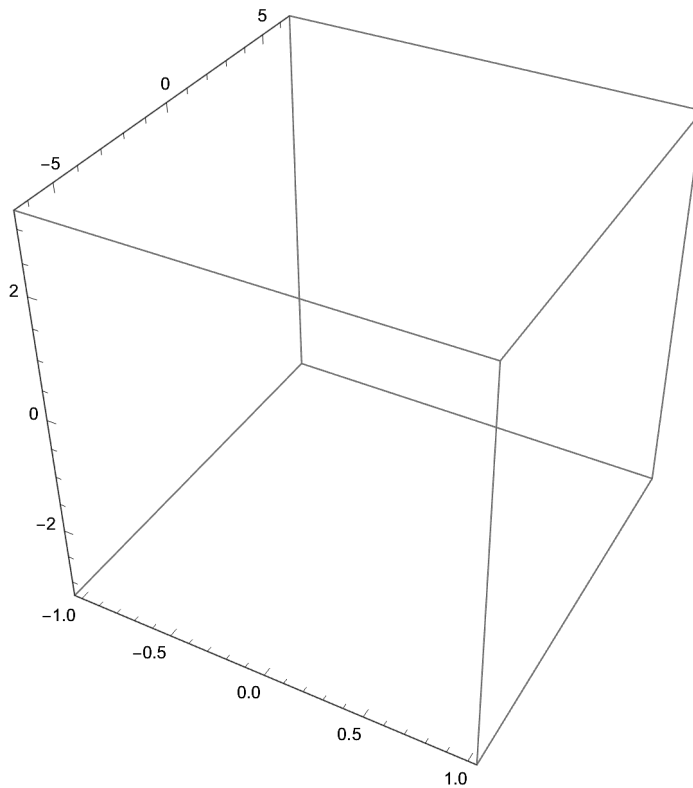
{{η -> -sqrt[4 π r^2 + r^2 θ^2 - (16 π^3 r^2 Sin[β]^2) / (4 π θ - θ^2)] / (2 sqrt[π])}, {η -> sqrt[4 π r^2 + r^2 θ^2 - (16 π^3 r^2 Sin[β]^2) / (4 π θ - θ^2)] / (2 sqrt[π])}}
```

ContourPlot3D $\left[\frac{\sqrt{4 \pi r^2 + r^2 \theta^2 - \frac{16 \pi^3 r^2 \sin[\beta]^2}{4 \pi \theta - \theta^2}}}{2 \sqrt{\pi}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$



== (r^2) (theta^2)

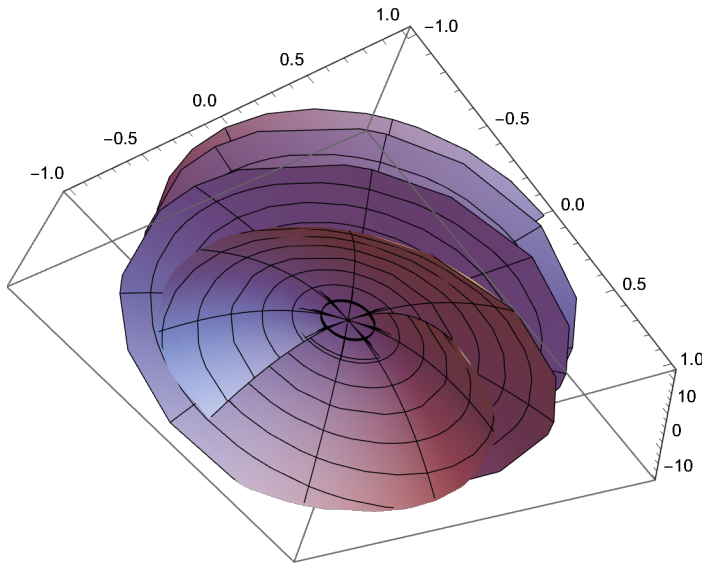
ContourPlot3D $\left[4 \pi (r)^2 - 4 \pi \left(\frac{\sqrt{4 \pi r^2 + r^2 \theta^2 - \frac{16 \pi^3 r^2 \sin[\beta]^2}{4 \pi \theta - \theta^2}}}{2 \sqrt{\pi}}\right)^2, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$



$$\text{Solve}\left[4 \pi \left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 - 4 \pi \left(\frac{2 \pi r - r \theta}{2 \pi}\right)^2 == (r^2) (\theta^2), r\right]$$

$$\{\{r \rightarrow 0\}, \{r \rightarrow 0\}\}$$

$$\text{RevolutionPlot3D}\left[4 \pi (r)^2 - 4 \pi \left(\frac{2 \pi r - r \theta}{2 \pi}\right)^2, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$\text{Solve}\left[4 \pi \left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 - 4 \pi \left(\frac{2 \pi r - r \theta}{2 \pi}\right)^2 == (r^2) (\theta^2), \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2 \pi + \pi^2}{1 + \pi} - \right.\right.$$

$$\left. \frac{1}{2} \sqrt{\left(-\frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2))\right)}\right\}$$

$$\left(3 (1 + \pi) \left(16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040\right.\right.$$

$$\left.\pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \right.$$

$$\left.\sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + \right.$$

$$\left.\left(16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - \right.\right.$$

$$\left.\left.23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2\right)^2\right)^{1/3}\right) +$$

$$\frac{1}{3 \times 2^{1/3} (1 + \pi)} \left(16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - \right.$$

$$\left.23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \right.$$

$$\left.\sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + \right.$$

$$\begin{aligned}
& \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{2} \sqrt{\left( -\frac{80\,\pi^2}{3\,(1+\pi)} + \frac{8\,(2\pi+\pi^2)^2}{(1+\pi)^2} - \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\text{Sin}[\beta]^2 + 12\,\pi^5\,\text{Sin}[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 \right. \right. \\
& \quad \left. \left. + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \sqrt{\left( -4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2) \right)^3 + \right. \right. \\
& \quad \left. \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^2 \right) \right)^{1/3} \Bigg) - \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \\
& \quad \sqrt{\left( -4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2) \right)^3 +} \\
& \quad \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^2 \Bigg)^{1/3} - \\
& \left( \frac{128\,\pi^3}{1+\pi} - \frac{320\,\pi^2\,(2\pi+\pi^2)}{(1+\pi)^2} + \frac{64\,(2\pi+\pi^2)^3}{(1+\pi)^3} \right) \Bigg/ \left( 4 \sqrt{\left( -\frac{40\,\pi^2}{3\,(1+\pi)} + \right. \right. \\
& \quad \left. \left. \frac{4\,(2\pi+\pi^2)^2}{(1+\pi)^2} + \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\text{Sin}[\beta]^2 + 12\,\pi^5\,\text{Sin}[\beta]^2 \right) \right) \right)} \right. \\
& \quad \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \quad \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \sqrt{\left( -4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2) \right)^3 + \right. \right. \\
& \quad \left. \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^2 \right) \right)^{1/3} \Bigg) + \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 + \\
& \quad \sqrt{\left( -4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\text{Sin}[\beta]^2 + 192\,\pi^5\,\text{Sin}[\beta]^2) \right)^3 +} \\
& \quad \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\text{Sin}[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\text{Sin}[\beta]^2 \right)^2 \Bigg)
\end{aligned}$$



$$\left. \left( (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2\pi + \pi^2)^2 \sin[\beta]^2 \right)^{1/3} \right) \Bigg] \Bigg\},$$
$$\left\{ \theta \rightarrow \frac{2\pi + \pi^2}{1 + \pi} - \frac{1}{2} \sqrt{\left( -\frac{40\pi^2}{3(1 + \pi)} + \frac{4(2\pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12\pi^5 + 12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2)) \right) / \right.$$
$$\left( 3(1 + \pi) \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right. \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) +$$
$$\frac{1}{3 \times 2^{1/3}(1 + \pi)} \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) +$$
$$\frac{1}{2} \sqrt{\left( -\frac{80\pi^2}{3(1 + \pi)} + \frac{8(2\pi + \pi^2)^2}{(1 + \pi)^2} - (16 \times 2^{1/3} (\pi^4 - 12\pi^5 + 12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2)) / \right.$$
$$\left( 3(1 + \pi) \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right. \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \Bigg) -$$
$$\frac{1}{3 \times 2^{1/3}(1 + \pi)} \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right.$$
$$\left. \sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 + (16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} -$$

$$\left( \frac{128 \pi^3}{1 + \pi} - \frac{320 \pi^2 (2 \pi + \pi^2)}{(1 + \pi)^2} + \frac{64 (2 \pi + \pi^2)^3}{(1 + \pi)^3} \right) / \left( 4 \sqrt{\left( -\frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2)) \right) / \left( 3 (1 + \pi) \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \right) \right) + \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \right) \right) \Bigg\},$$

$$\left\{ \Theta \rightarrow \frac{2 \pi + \pi^2}{1 + \pi} + \frac{1}{2} \sqrt{\left( -\frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2)) \right) / \left( 3 (1 + \pi) \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \right) \right) + \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt{-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2} \right)^{1/3} \right) \right\},$$

$$\begin{aligned}
& \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{2} \sqrt[3]{\left( -\frac{80\,\pi^2}{3\,(1+\pi)} + \frac{8\,(2\pi+\pi^2)^2}{(1+\pi)^2} - \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\sin[\beta]^2 + 12\,\pi^5\,\sin[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \right. \right. \\
& \left. \sqrt[3]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \right. \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \left. \sqrt[3]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \right. \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} + \\
& \left( \frac{128\,\pi^3}{1+\pi} - \frac{320\,\pi^2\,(2\pi+\pi^2)}{(1+\pi)^2} + \frac{64\,(2\pi+\pi^2)^3}{(1+\pi)^3} \right) \sqrt[3]{\left( -\frac{40\,\pi^2}{3\,(1+\pi)} + \right.} \\
& \left. \frac{4\,(2\pi+\pi^2)^2}{(1+\pi)^2} + \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\sin[\beta]^2 + 12\,\pi^5\,\sin[\beta]^2 \right) \right) \right)} \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \left. \sqrt[3]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \right. \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) + \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \left. \sqrt[3]{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 +} \right. \\
& \left. \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) +
\end{aligned}$$

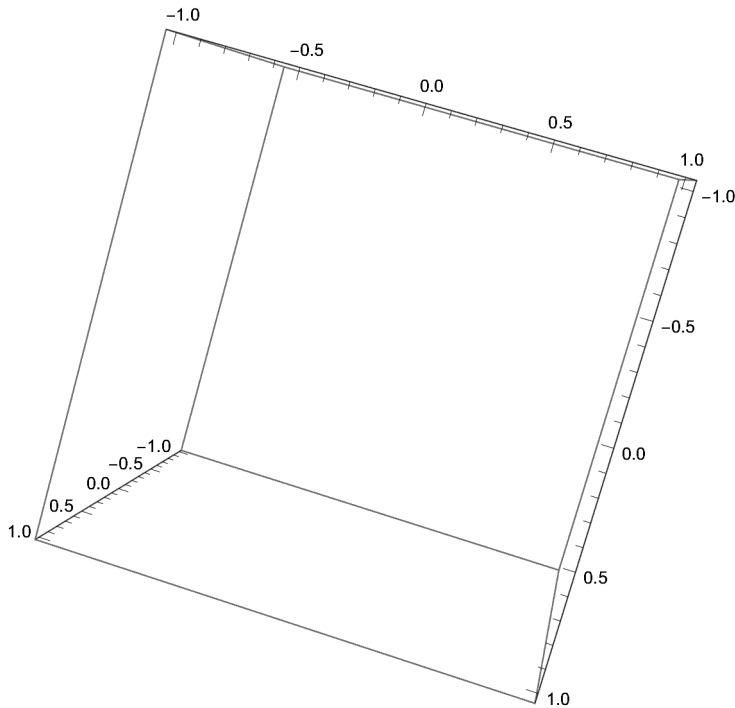
$$\left. \left( (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2\pi + \pi^2)^2 \sin[\beta]^2 \right)^{1/3} \right) \Bigg\},$$
$$\left\{ \theta \rightarrow \frac{2\pi + \pi^2}{1 + \pi} + \frac{1}{2} \sqrt{\left( -\frac{40\pi^2}{3(1 + \pi)} + \frac{4(2\pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12\pi^5 + 12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2)) \right)^{1/3}} \right.$$
$$12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2 \Bigg) /$$
$$\left( 3(1 + \pi) \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right. \right.$$
$$\sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 +}$$
$$(16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) -$$
$$23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 \Bigg)^{1/3} \Bigg) +$$
$$\frac{1}{3 \times 2^{1/3}(1 + \pi)} \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) -$$
$$23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right.$$
$$\sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 +}$$
$$(16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) -$$
$$23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 \Bigg)^{1/3} \Bigg) +$$
$$\frac{1}{2} \sqrt{\left( -\frac{80\pi^2}{3(1 + \pi)} + \frac{8(2\pi + \pi^2)^2}{(1 + \pi)^2} - (16 \times 2^{1/3} (\pi^4 - 12\pi^5 + 12\pi^4 \sin[\beta]^2 + 12\pi^5 \sin[\beta]^2)) \right)^{1/3}}$$
$$\left( 3(1 + \pi) \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) - 23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right. \right.$$
$$\sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 +}$$
$$(16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) -$$
$$23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 \Bigg)^{1/3} \Bigg) -$$
$$\frac{1}{3 \times 2^{1/3}(1 + \pi)} \left( 16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) -$$
$$23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 + \right.$$
$$\sqrt{-4(16\pi^4 - 192\pi^5 + 192\pi^4 \sin[\beta]^2 + 192\pi^5 \sin[\beta]^2)^3 +}$$
$$(16000\pi^6 + 6912\pi^6(1 + \pi) - 11520\pi^5(2\pi + \pi^2) -$$
$$23040\pi^6(1 + \pi) \sin[\beta]^2 + 6912\pi^4(2\pi + \pi^2)^2 \sin[\beta]^2 \Bigg)^{1/3} \Bigg) +$$

$$\left( \frac{128 \pi^3}{1 + \pi} - \frac{320 \pi^2 (2 \pi + \pi^2)}{(1 + \pi)^2} + \frac{64 (2 \pi + \pi^2)^3}{(1 + \pi)^3} \right) \Bigg/ \left( 4 \sqrt[3]{\left( -\frac{40 \pi^2}{3 (1 + \pi)} + \frac{4 (2 \pi + \pi^2)^2}{(1 + \pi)^2} + (16 \times 2^{1/3} (\pi^4 - 12 \pi^5 + 12 \pi^4 \sin[\beta]^2 + 12 \pi^5 \sin[\beta]^2)) \right)} \right. \\ \left. \left( 3 (1 + \pi) \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt[3]{\left( -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2 \right)} \right)^{1/3} \right) \right. \\ \left. \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 + \sqrt[3]{\left( -4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + 192 \pi^5 \sin[\beta]^2)^3 + (16000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11520 \pi^5 (2 \pi + \pi^2) - 23040 \pi^6 (1 + \pi) \sin[\beta]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2)^2 \right)} \right)^{1/3} \right) \right) \Bigg\} \Bigg\}$$

$$\text{SphericalPlot3D}\left[\frac{2\pi+\pi^2}{1+\pi}-\frac{1}{2}\sqrt{\left(-\frac{40\pi^2}{3(1+\pi)}+\frac{4(2\pi+\pi^2)^2}{(1+\pi)^2}+(16\times 2^{1/3}(\pi^4-12\pi^5+12\pi^4\sin[\beta]^2+12\pi^5\sin[\beta]^2))\right)/\left(3(1+\pi)\left(16000\pi^6+6912\pi^6(1+\pi)-11520\pi^5(2\pi+\pi^2)-23040\pi^6(1+\pi)\sin[\beta]^2+6912\pi^4(2\pi+\pi^2)^2\sin[\beta]^2+\sqrt{\left(-4(16\pi^4-192\pi^5+192\pi^4\sin[\beta]^2+192\pi^5\sin[\beta]^2)^3+(16000\pi^6+6912\pi^6(1+\pi)-11520\pi^5(2\pi+\pi^2)-23040\pi^6(1+\pi)\sin[\beta]^2+6912\pi^4(2\pi+\pi^2)^2\sin[\beta]^2)^2\right)}^{1/3}\right)}+\frac{1}{3\times 2^{1/3}(1+\pi)}\left(16000\pi^6+6912\pi^6(1+\pi)-11520\pi^5(2\pi+\pi^2)-23040\pi^6(1+\pi)\sin[\beta]^2+6912\pi^4(2\pi+\pi^2)^2\sin[\beta]^2+\sqrt{\left(-4(16\pi^4-192\pi^5+192\pi^4\sin[\beta]^2+192\pi^5\sin[\beta]^2)^3+(16000\pi^6+6912\pi^6(1+\pi)-11520\pi^5(2\pi+\pi^2)-\right.\right.}$$

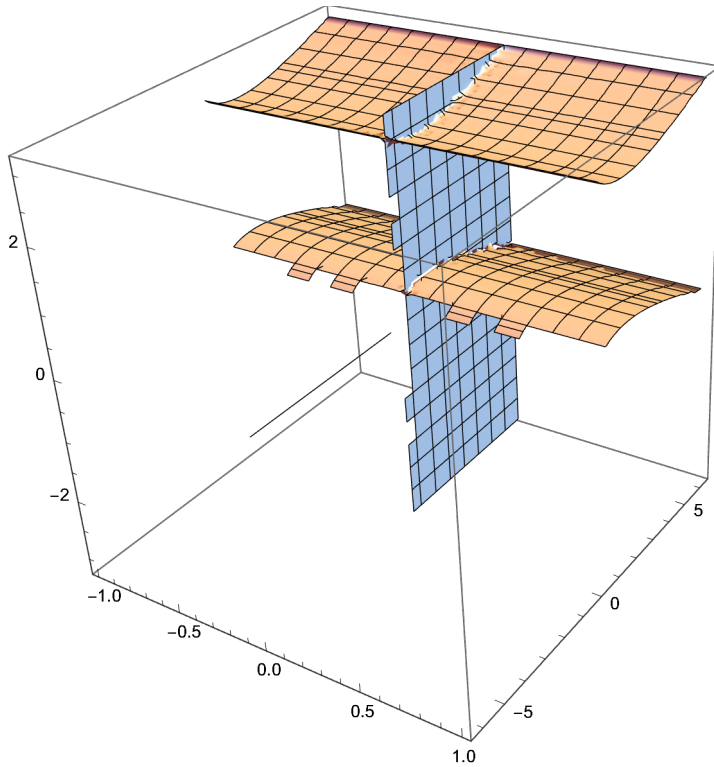
$$\begin{aligned}
& \left. \left( 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{2} \sqrt[3]{ \left( -\frac{80\,\pi^2}{3\,(1+\pi)} + \frac{8\,(2\pi+\pi^2)^2}{(1+\pi)^2} - \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\sin[\beta]^2 + 12\,\pi^5\,\sin[\beta]^2 \right) \right) \right) / } \\
& \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\,\theta}}{2\pi}\right]\right]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2 \\
& \quad \sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\,\theta}}{2\pi}\right]\right]^2 + \sqrt{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + } \\
& \quad \quad 192\,\pi^5\,\sin[\beta]^2)^3 + \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \quad \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} \Bigg) - \\
& \frac{1}{3 \times 2^{1/3}\,(1+\pi)} \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \quad \sqrt{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin[\beta]^2 + 192\,\pi^5\,\sin[\beta]^2)^3 + } \\
& \quad \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \quad \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 \right)^2 \right)^{1/3} - \\
& \left( \frac{128\,\pi^3}{1+\pi} - \frac{320\,\pi^2\,(2\pi+\pi^2)}{(1+\pi)^2} + \frac{64\,(2\pi+\pi^2)^3}{(1+\pi)^3} \right) / \left( 4 \sqrt[3]{ \left( -\frac{40\,\pi^2}{3\,(1+\pi)} + \frac{4\,(2\pi+\pi^2)^2}{(1+\pi)^2} + \right. \right. \\
& \quad \left. \left. \left( 16 \times 2^{1/3} \left( \pi^4 - 12\,\pi^5 + 12\,\pi^4\,\sin[\beta]^2 + 12\,\pi^5\,\sin[\beta]^2 \right) \right) \right) / } \right. \\
& \quad \left( 3\,(1+\pi) \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \right. \\
& \quad \quad 23\,040\,\pi^6\,(1+\pi)\,\sin[\beta]^2 + 6912\,\pi^4\,(2\pi+\pi^2)^2\,\sin[\beta]^2 + \\
& \quad \quad \sqrt{-4\,(16\,\pi^4 - 192\,\pi^5 + 192\,\pi^4\,\sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\,\theta}}{2\pi}\right]\right]^2 + } \\
& \quad \quad \quad 192\,\pi^5\,\sin[\beta]^2)^3 + \left( 16\,000\,\pi^6 + 6912\,\pi^6\,(1+\pi) - 11\,520\,\pi^5\,(2\pi+\pi^2) - \right. \\
& \quad \quad \quad \left. \left. 23\,040\,\pi^6\,(1+\pi)\,\sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\,\theta}}{2\pi}\right]\right]^2 + \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 6912 \pi^4 (2 \pi + \pi^2)^2 \sin[\beta]^2 \Big)^2 \Big)^{1/3} \Big) + \\
 & \frac{1}{3 \times 2^{1/3} (1 + \pi)} \left( 16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \pi^2) - \right. \\
 & 23\,040 \pi^6 (1 + \pi) \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2 + 6912 \pi^4 (2 \pi + \pi^2)^2 \\
 & \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2 + \sqrt{\left(-4 (16 \pi^4 - 192 \pi^5 + 192 \pi^4 \sin[\beta]^2 + \right. \\
 & 192 \pi^5 \sin[\beta]^2)^3 + \left(16\,000 \pi^6 + 6912 \pi^6 (1 + \pi) - 11\,520 \pi^5 (2 \pi + \right. \\
 & \pi^2) - 23\,040 \pi^6 (1 + \pi) \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2 + 6912 \pi^4 \\
 & \left. (2 \pi + \pi^2)^2 \sin[\beta]^2 \right)^2 \Big)^{1/3} \Big) \Big) \Big), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\} \Big]
 \end{aligned}$$



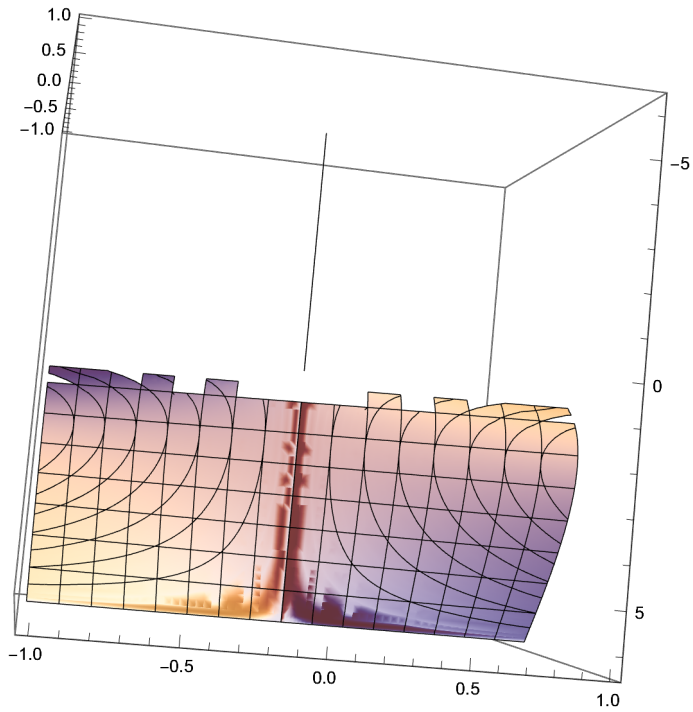
```
ContourPlot3D[ $\left( \left( \frac{4}{3} \right) \pi \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^3 - \left( \frac{4}{3} \right) \pi \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^3 \right) = 4 \pi r^2 \theta,$ 
  {r, -1, 1}, {θ, -2 π, 2 π}, {β, -π, π}]
```

```
ContourPlot3D[ $\left( \left( \frac{4}{3} \right) \pi \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^3 - \left( \frac{4}{3} \right) \pi \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^3 \right),$ 
  {r, -1, 1}, {θ, -2 π, 2 π}, {β, -π, π}]
```

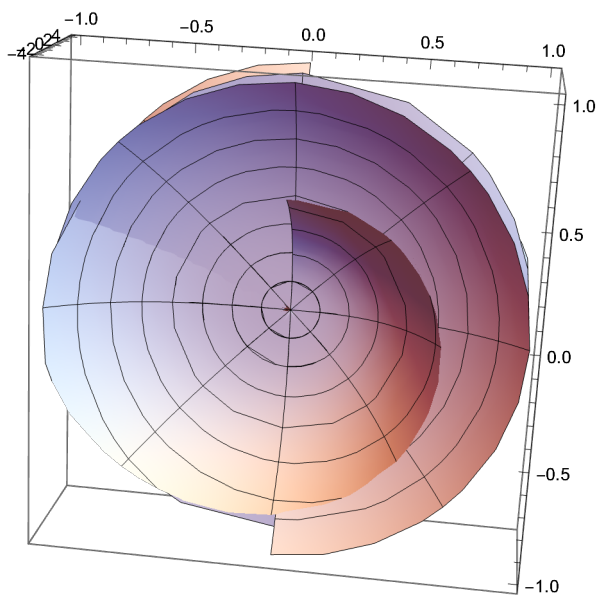




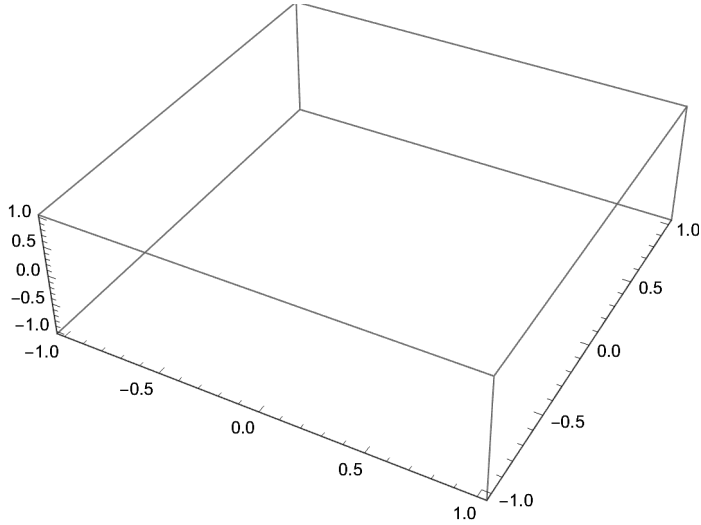
```
ContourPlot3D[ $\left( (4/3) \pi \left( \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right)^3 - (4/3) \pi \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^3 \right)$ ,  
{r, -1, 1}, {η, -1, 1}, {θ, -2 π, 2 π}]
```



```
RevolutionPlot3D[ $\left( (4/3) \pi (r)^3 - (4/3) \pi \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^3 \right)$ , {r, -1, 1}, {θ, -2 π, 2 π}]
```

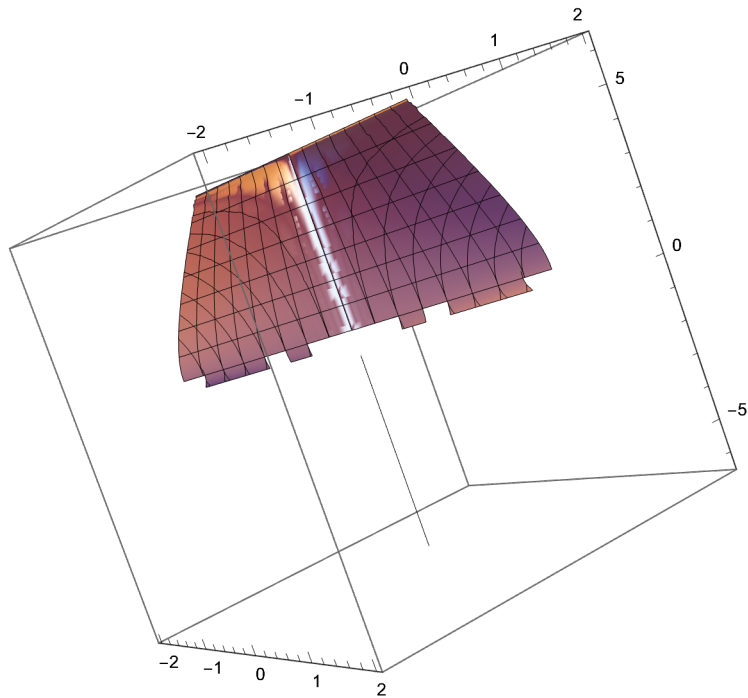


$$\text{RevolutionPlot3D}\left[\left((4/3)\pi(r)^3 - (4/3)\pi\left(\frac{2\pi r - r^2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{2\pi}\right)^3\right),\right. \\ \left.\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



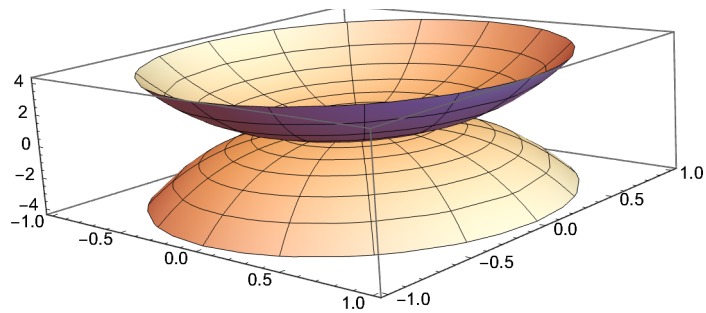
$$\int \left( (4/3)\pi \left( \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right)^3 - (4/3)\pi \left( \frac{2\pi r - r\theta}{2\pi} \right)^3 \right) d\theta \\ - \frac{\frac{16\pi^4\eta^3(-2\pi+\theta)}{\sqrt{(4\pi-\theta)\theta}} - \frac{1}{4}r^3(-2\pi+\theta)^4}{6\pi^2}$$

`ContourPlot3D` $\left[-\frac{-\frac{16 \pi^4 \eta^3 (-2 \pi + \theta)}{\sqrt{(4 \pi - \theta) \theta}} - \frac{1}{4} r^3 (-2 \pi + \theta)^4}{6 \pi^2}, \{r, -2, 2\}, \{\eta, -2, 2\}, \{\theta, -2 \pi, 2 \pi\}\right]$

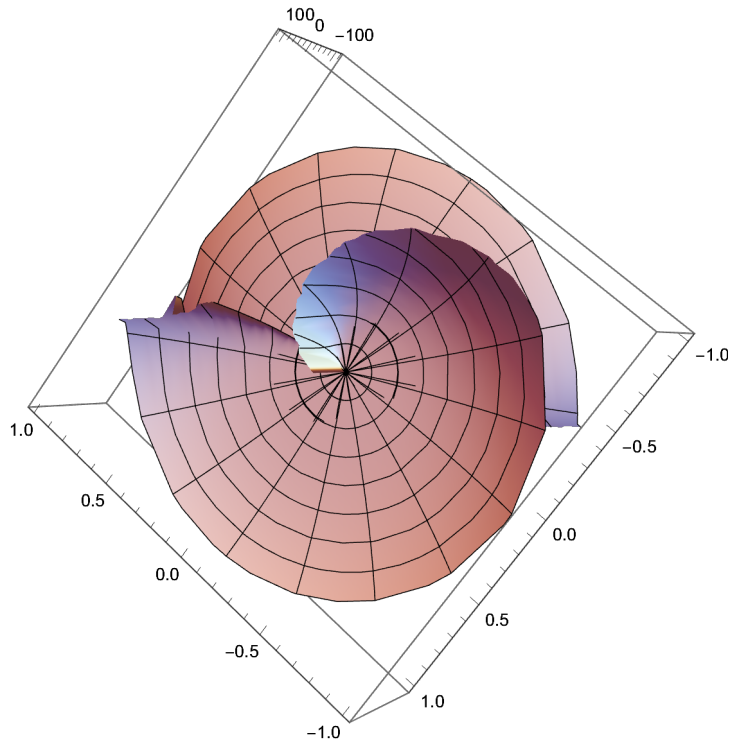


$$\left(\frac{4}{3}\right) \pi \left( \frac{4 \pi^2 \eta}{(2 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} \right)^3 = \left(\frac{4}{3}\right) \pi (r)^3 = \text{Volume of Sphere} \quad (37)$$

`RevolutionPlot3D` $[(4/3) \pi (r)^3, \{r, -1, 1\}]$

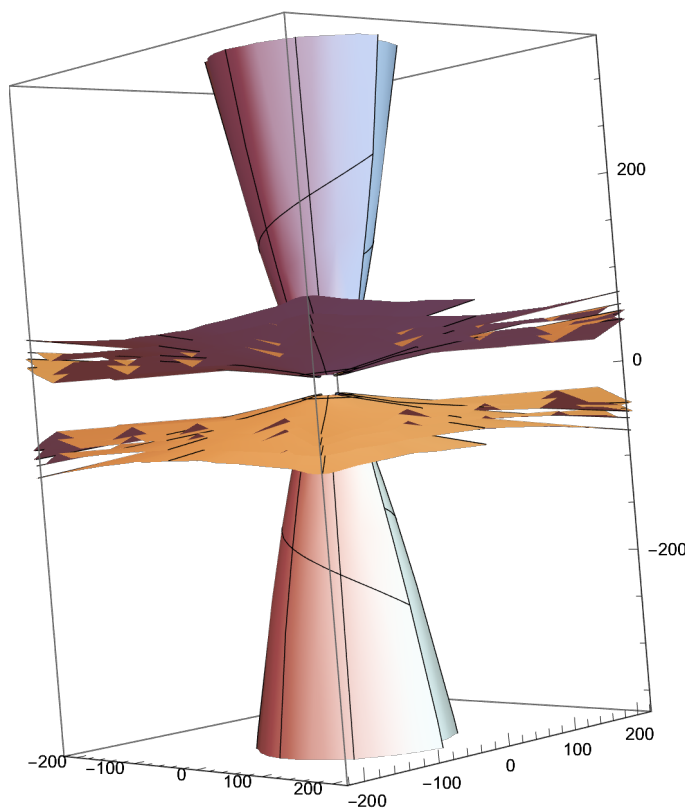


$\text{RevolutionPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{4\pi^2\eta}{(2\pi-\theta)\sqrt{(4\pi-\theta)\theta}}\right)^3, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$

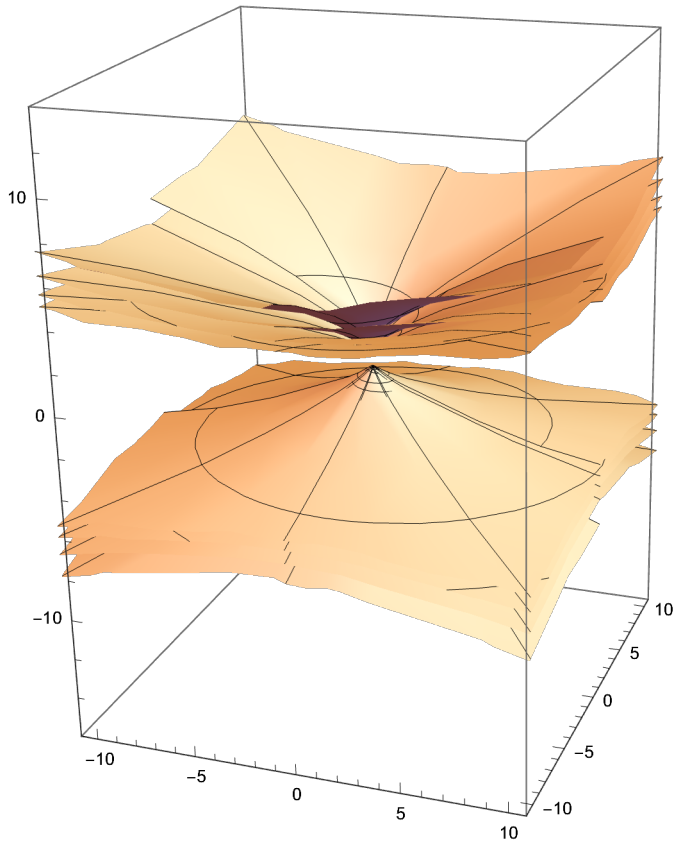
`SphericalPlot3D` $\left[\left(\frac{4}{3}\right)\pi\right.$   
 $\left.\left(\frac{(4\pi^2)}{\left(2\pi - 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right)}\sqrt{(4\pi - \theta)\left(2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right)}\right)^3,\right.$   
 $\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}$



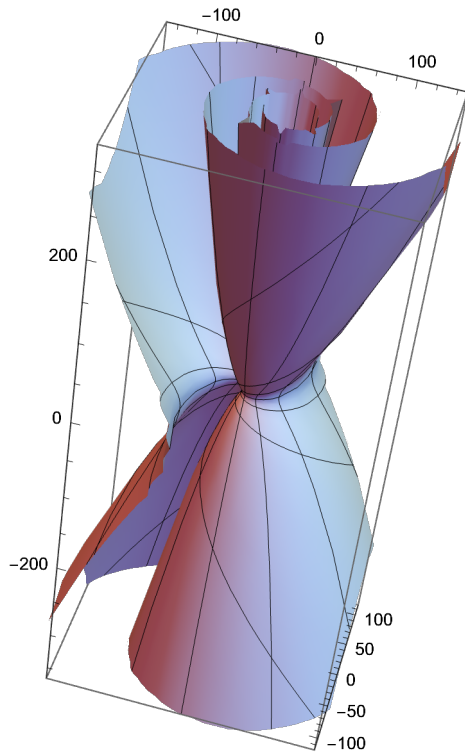
SphericalPlot3D[(4/3)  $\pi$

$$\left( \frac{(4\pi^2)}{\left( 2\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \sqrt{(4\pi - \theta) \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right)^3,$$

$\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$



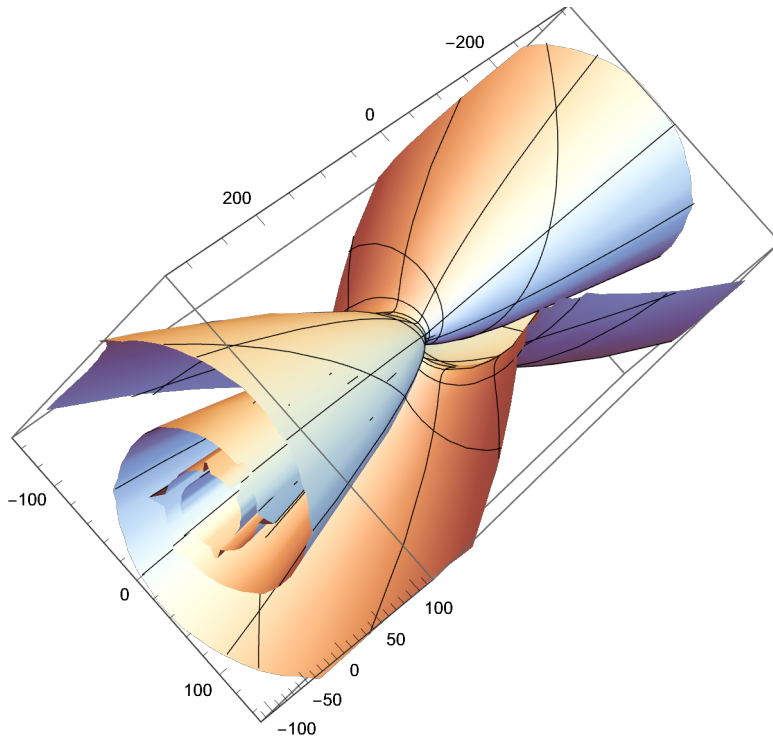
SphericalPlot3D $\left[\left(\frac{4}{3}\right)\pi\right.$   
 $\left.\left(\frac{\left(4\pi^2\right)}{\left(2\pi-\theta\right)\sqrt{\left(4\pi-2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\left(2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\right)}\right)^3,$   
 $\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$



SphericalPlot3D[(4/3) π

$$\left( \frac{(4\pi^2)}{\left( (2\pi - \theta) \sqrt{4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right) \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \right) \right)^3,$$

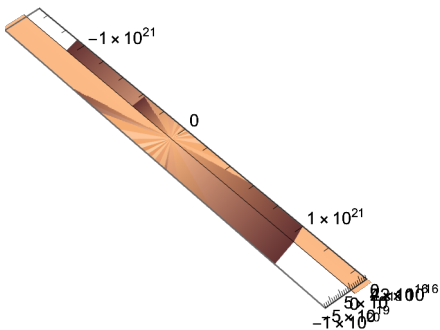
$$\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



SphericalPlot3D[(4/3) π

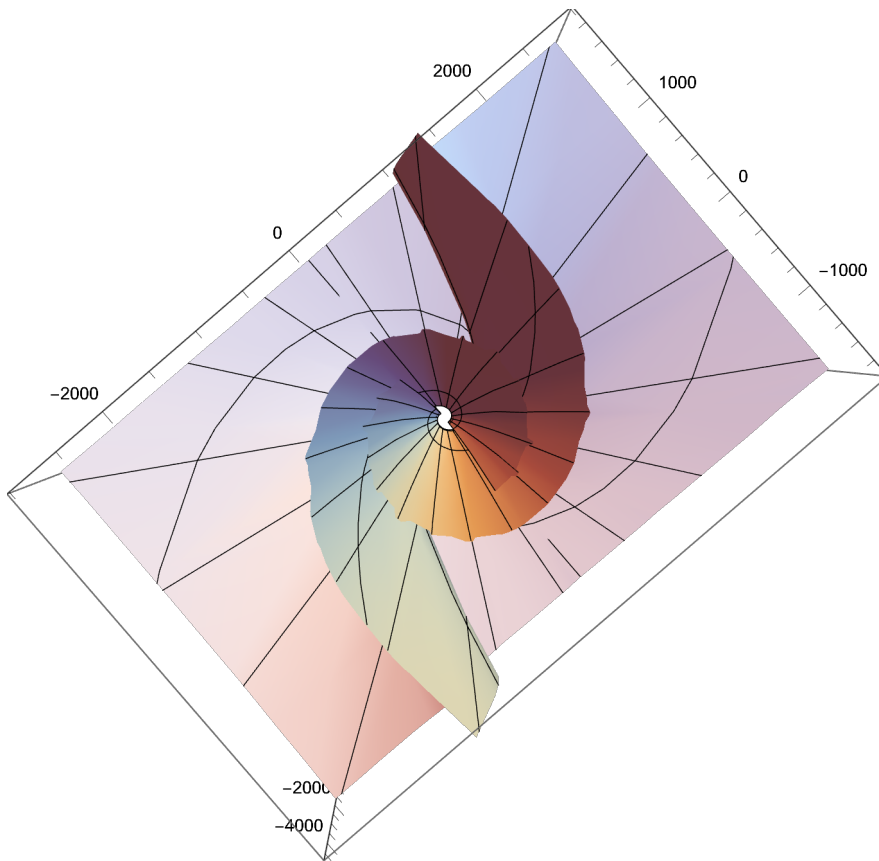
$$\left( \frac{(4\pi^2)}{\left( (2\pi - 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)) \sqrt{4\pi - 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right) (\theta) \right) \right)^3,$$

$$\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$

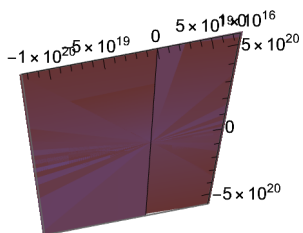




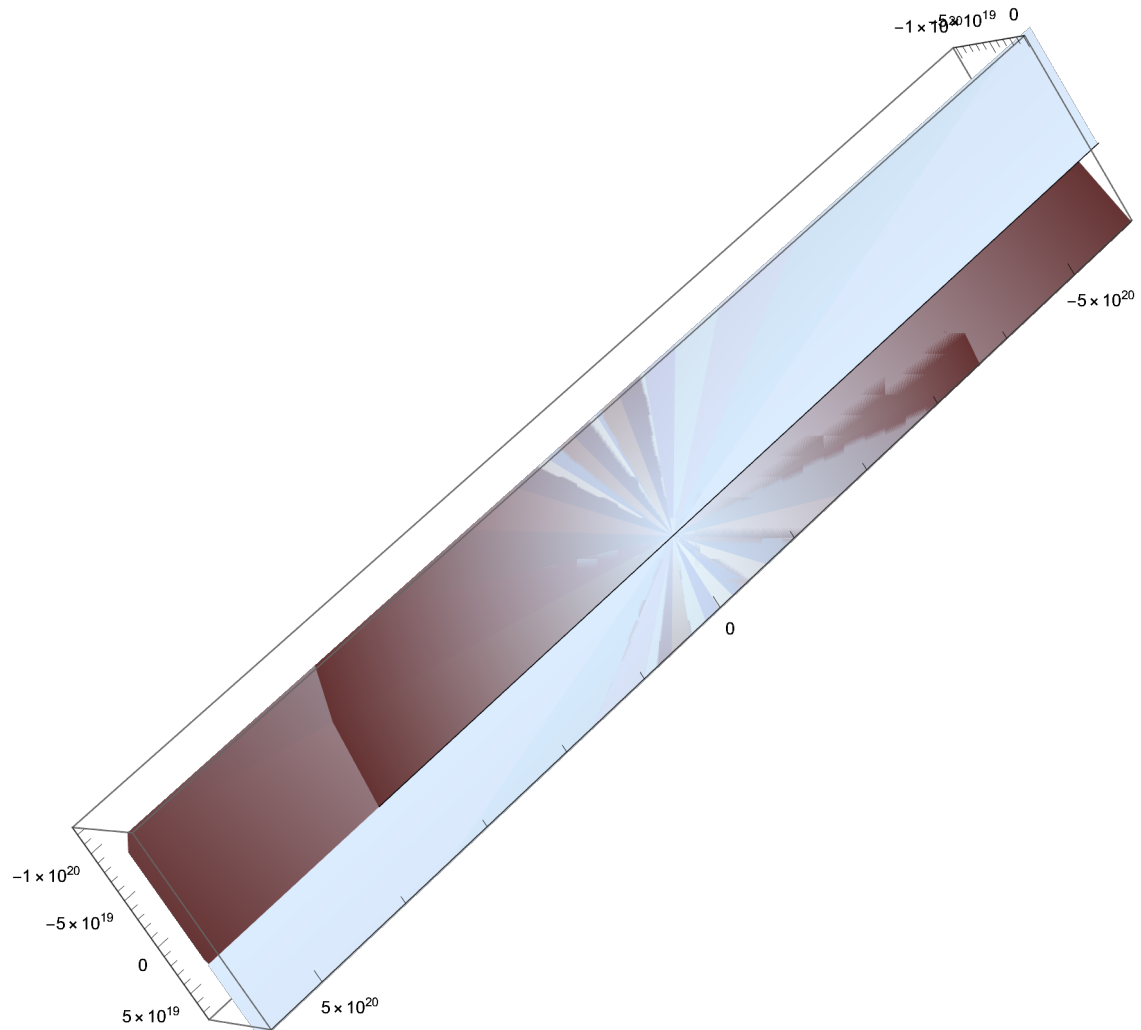
SphericalPlot3D $\left[\left(\frac{4}{3}\right) \pi \left( \frac{\left(4 \pi^2\right)}{\left(2 \pi-2\left(\pi+\sqrt{\pi^2-\pi^2 \operatorname{Sin}[\beta]^2}\right)\right)} \sqrt{\left(4 \pi-2\left(\pi+\sqrt{\pi^2-\pi^2 \operatorname{Sin}[\beta]^2}\right)\right)(\theta)}\right)^3,\right.$   
 $\left.\{\beta,-.849 \pi,.849 \pi\},\{\theta,-2 \pi, 2 \pi\}\right]$



SphericalPlot3D $\left[\left(\frac{4}{3}\right) \pi \left( \frac{4 \pi^2}{\left(2 \pi-2\left(\pi-\sqrt{\pi^2-\pi^2 \operatorname{Sin}[\beta]^2}\right)\right)} \sqrt{(4 \pi-\theta)(\theta)}\right)^3,\right.$   
 $\left.\{\beta,-\pi, \pi\},\{\theta,-2 \pi, 2 \pi\}\right]$

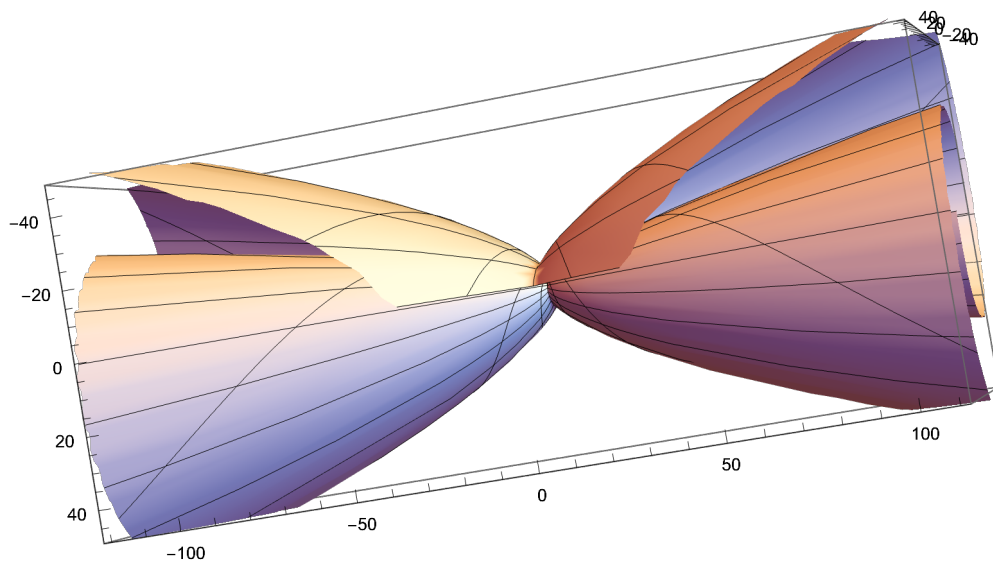


$\text{SphericalPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{4\pi^2}{\left(2\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)\sqrt{(4\pi - \theta)(\theta)}}\right)^3,\right.$   
 $\left.\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$

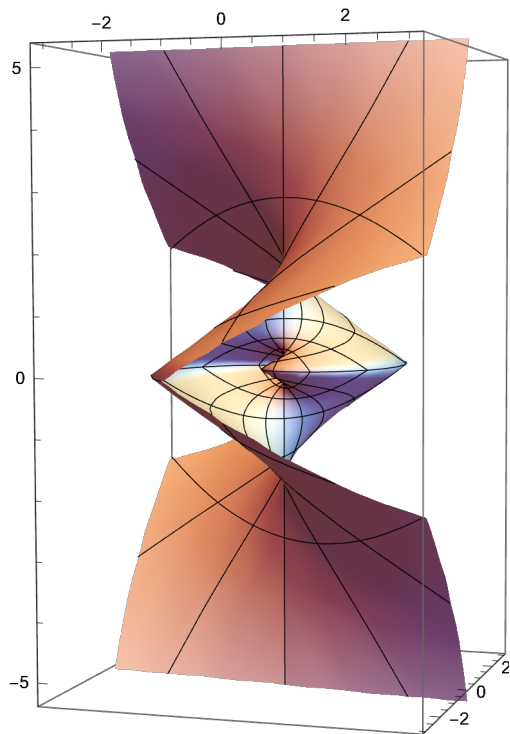


SphericalPlot3D[

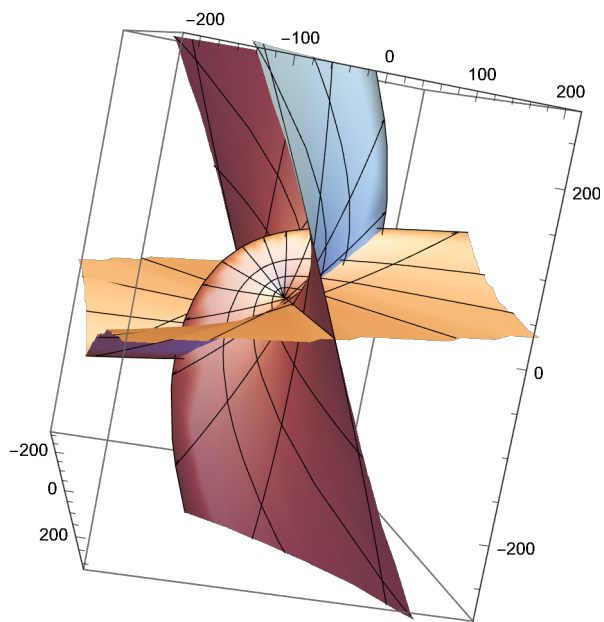
$$\left( \frac{4}{3} \pi \frac{4 \pi^2}{(2 \pi - \theta) \sqrt{(4 \pi - \theta) \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]^2} \right) \right)}} \right)^3, \{\beta, -\pi, \pi\}, \{\theta, -\pi, \pi\}]$$



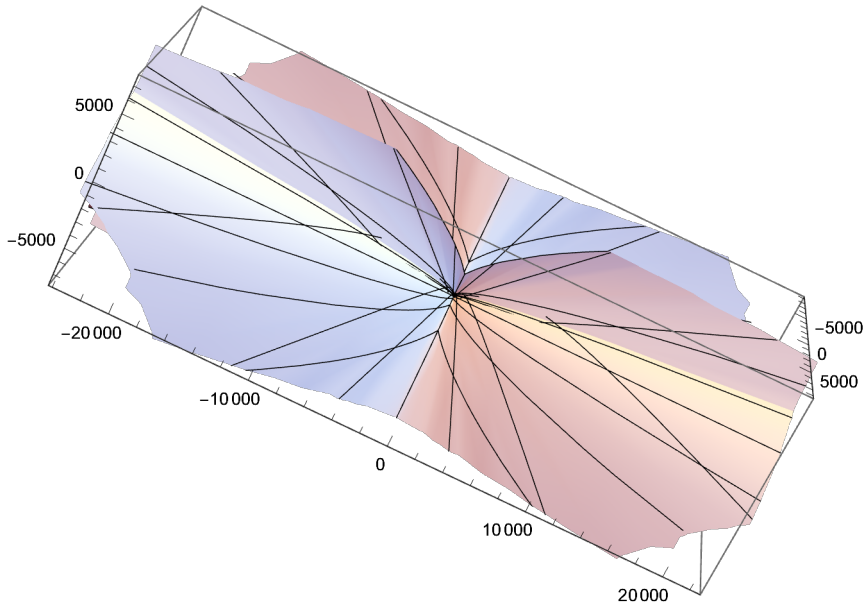
`SphericalPlot3D` $\left[\left(\frac{4}{3}\right)\pi\left(\frac{4\pi^2}{(2\pi-\theta)\sqrt{(4\pi-\theta)\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)}}\right)^3,\right.$   
 $\left.\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$



`SphericalPlot3D` $\left[ \left( \frac{4}{3} \right) \pi \left( \frac{4 \pi^2}{(2 \pi - \theta) \sqrt{\left( 4 \pi - 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \theta} \right)} \right)^3, \right.$   
 $\left. \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\} \right]$



$$\text{SphericalPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{4\pi^2}{(2\pi-\theta)\sqrt{(4\pi-2(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2})\theta)}\right)^3,\right. \\ \left.\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$$



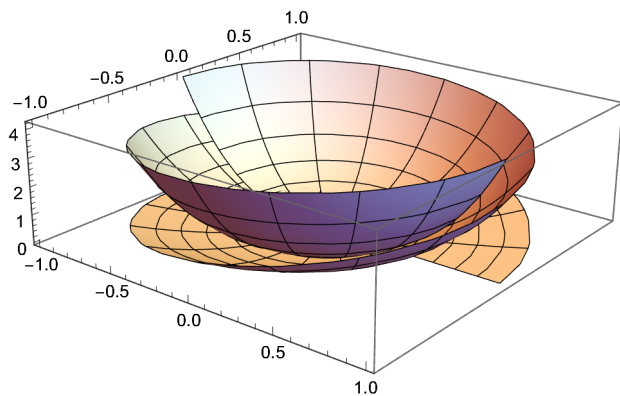
$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right\}\right\} \quad (38)$$

When  $\eta = r$ ,

$$\left(\frac{4}{3}\right)\pi(r)^3 = \left(\frac{4}{3}\right)\pi\left(\frac{4\pi^2\eta}{(2\pi-\theta)\sqrt{(4\pi-\theta)\theta}}\right)^3 = \quad (39)$$

$$\left(\frac{4}{3}\right)\pi(\eta)^3 = \left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right)^3 = \text{Volume of Sphere}$$

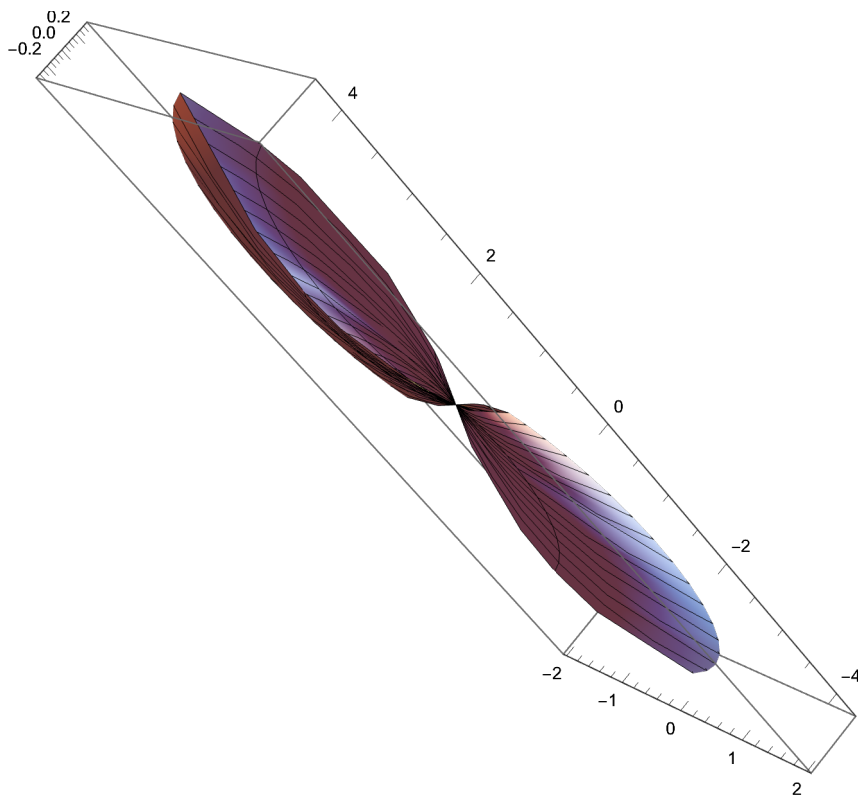
`RevolutionPlot3D` $\left[\left(\frac{4}{3}\right) \pi \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^3, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



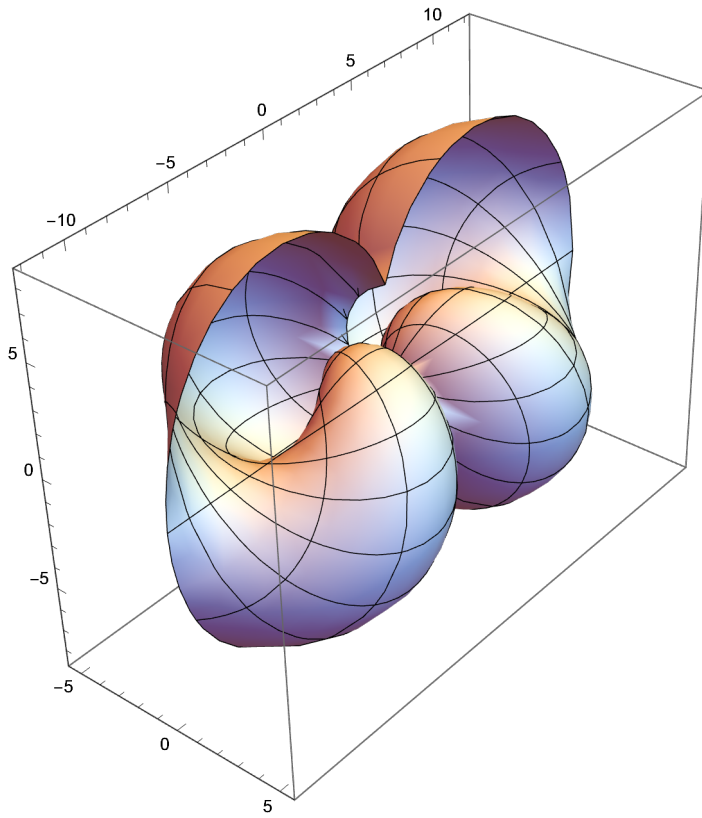
$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$

`SphericalPlot3D`

$\left(\frac{4}{3}\right) \pi \left(\frac{\sqrt{4 \pi 1^2 \theta - 1^2 \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2 \pi}\right)^3, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}$



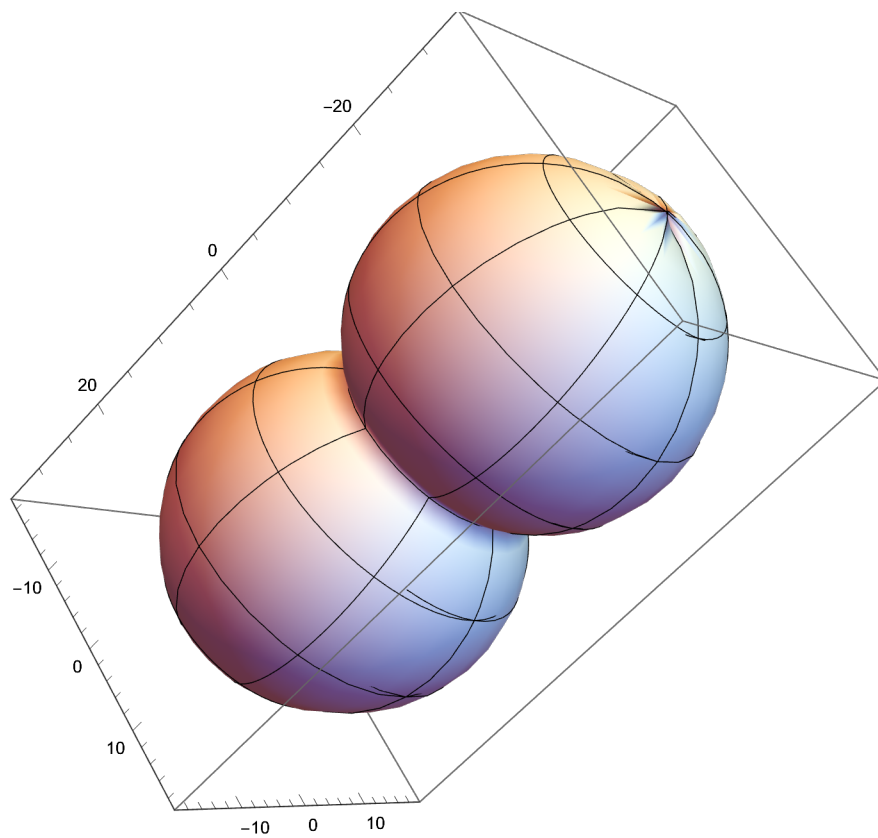
$$\text{SphericalPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi^2\theta - 1^2\left(2\left(\pi - \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}}{2\pi}\right)^3,\right. \\ \left.\{\beta, -1\pi, 1\pi\}, \{\theta, -2\pi, 2\pi\}\right]$$





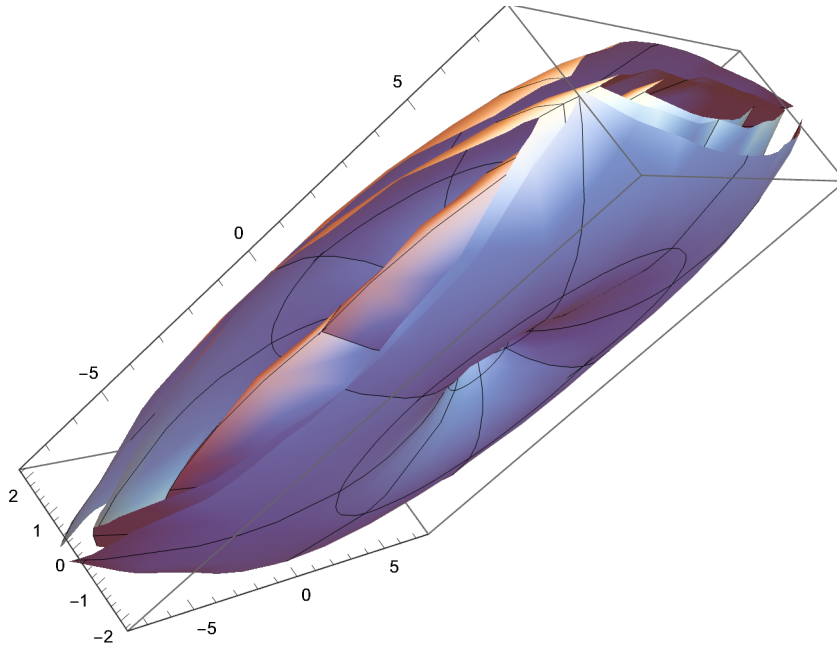
SphericalPlot3D[  

$$\left( \frac{(4/3)\pi \sqrt{4\pi^2 \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - 1^2 \theta^2}}{2\pi} \right)^3, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$

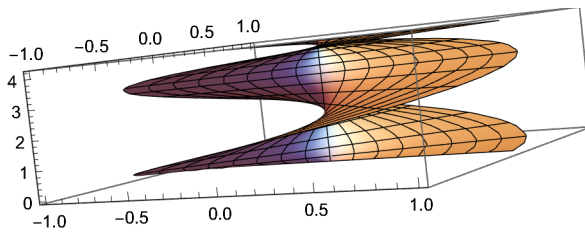


SphericalPlot3D[

$$\left( \frac{4}{3} \right) \pi \left( \frac{\sqrt{4 \pi 1^2 \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - 1^2 \theta^2}}{2 \pi} \right)^3, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}]$$

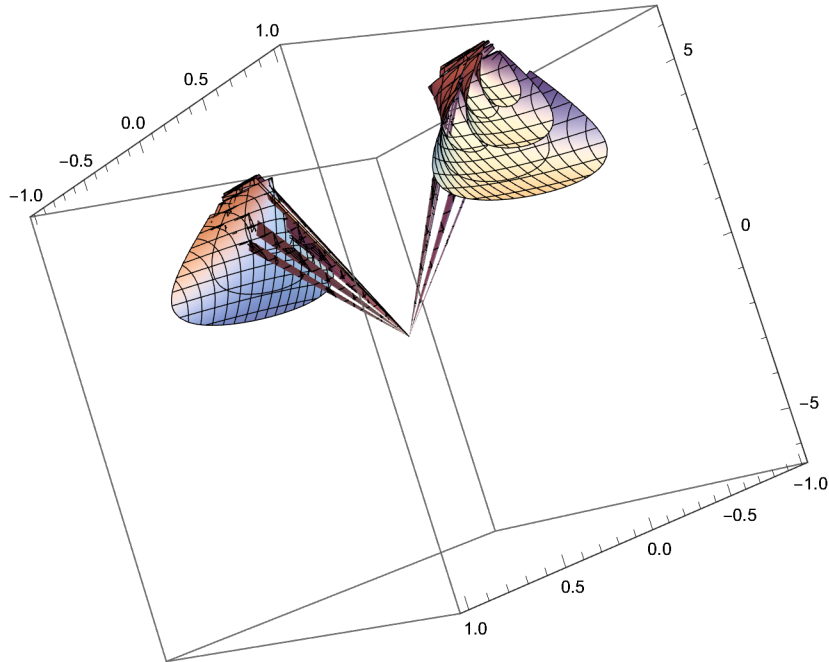


RevolutionPlot3D[ $\left( \frac{4}{3} \right) \pi \left( \frac{\sqrt{4 \pi 1^2 \theta - 1^2 \theta^2}}{2 \pi} \right)^3, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$

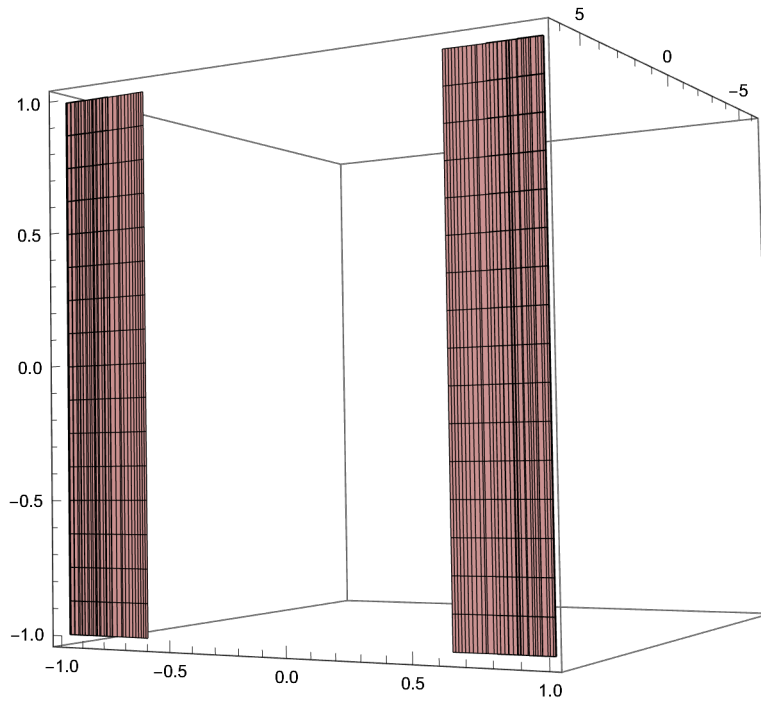


Or, more generally, we can construct the equation :

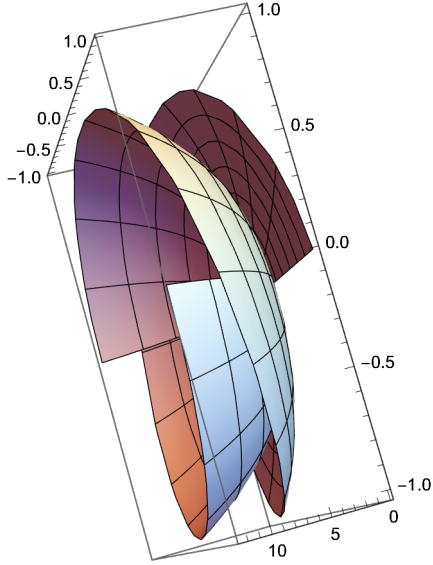
$\text{ContourPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi(r)^2\theta - \left(\frac{4\pi^2\eta}{(2\pi-\theta)\sqrt{(4\pi-\theta)\theta}}\right)^2\theta^2}}{2\pi}\right)^3,\right.$   
 $\left.\{\eta, -1, 1\}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



`ContourPlot3D`  $\left[ (4/3) \pi \frac{\sqrt{4 \pi \left( \frac{4 \pi^2 \eta}{(2 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} \right)^2 \theta - r^2 \theta^2}}{2 \pi} \right]^3,$   
 $\{\eta, -1, 1\}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}$



`RevolutionPlot3D` $\left[4 \pi \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^3, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

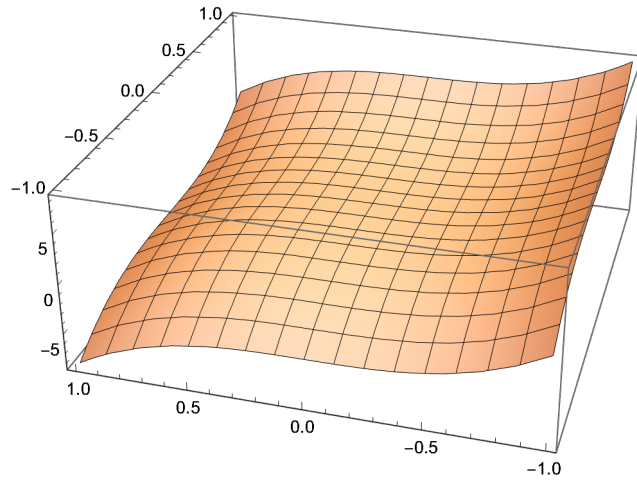


$$4 \pi \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^3 - 4 \pi (r_1)^3 = \Delta V \quad (40)$$

$$r_1 \rightarrow \frac{2 \pi r - r \theta}{2 \pi} \quad (41)$$

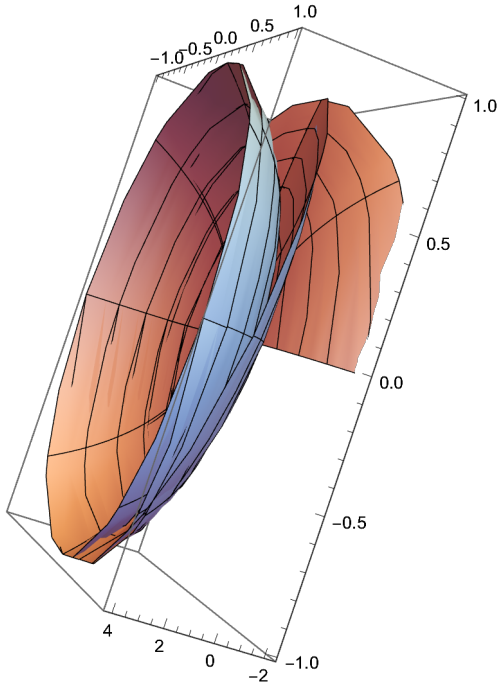
$$4 \pi \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^3 - 4 \pi \left(\frac{2 \pi r - r \theta}{2 \pi}\right)^3 = \Delta V \quad (42)$$

`Plot3D` $[(4/3) \pi (r)^3 - (4/3) \pi (\eta)^3], \{r, -1, 1\}, \{\eta, -1, 1\}]$



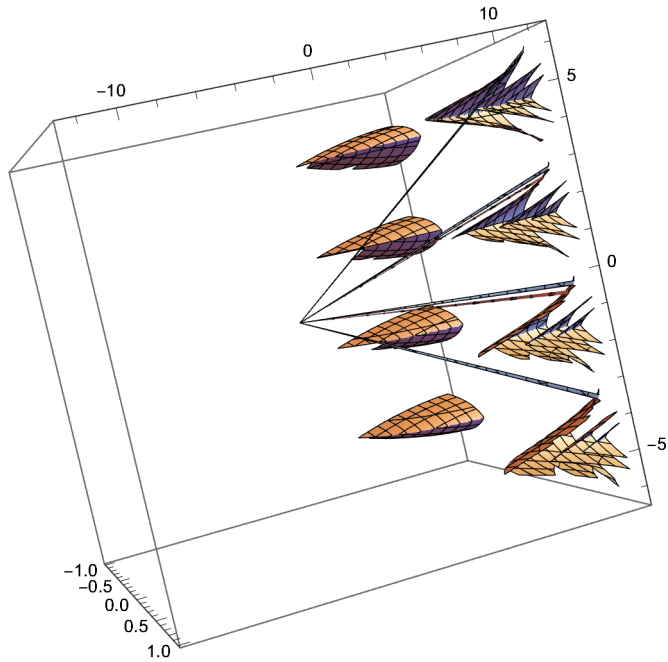
RevolutionPlot3D[  

$$(4/3)\pi \left( \frac{\sqrt{4\pi r^2(\theta) - r^2\theta^2}}{2\pi} \right)^3 - (4/3)\pi \left( \frac{2\pi r - r\theta}{2\pi} \right)^3, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$

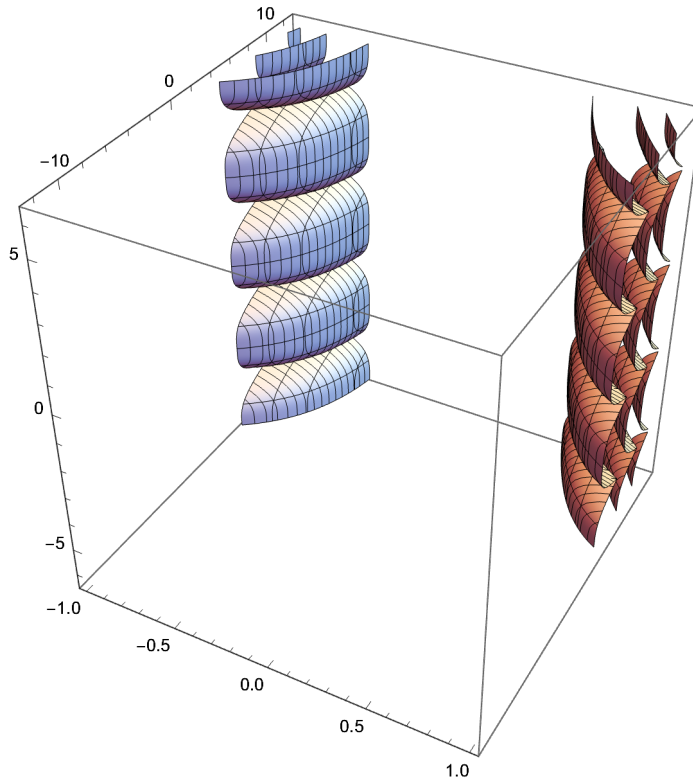


$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\} \right\}$$

$$\text{ContourPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2(\theta) - r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2\pi}\right)^3 - \left(\frac{4}{3}\right)\pi\left(\frac{2\pi r - r(\theta)}{2\pi}\right)^3, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -2\pi, 2\pi\}\right]$$



$\text{ContourPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2(\theta) - r^2\left(2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2\pi}\right)^3 - \right.$   
 $\left. \left(\frac{4}{3}\right)\pi\left(\frac{2\pi r - r(\theta)}{2\pi}\right)^3, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -2\pi, 2\pi\}\right]$

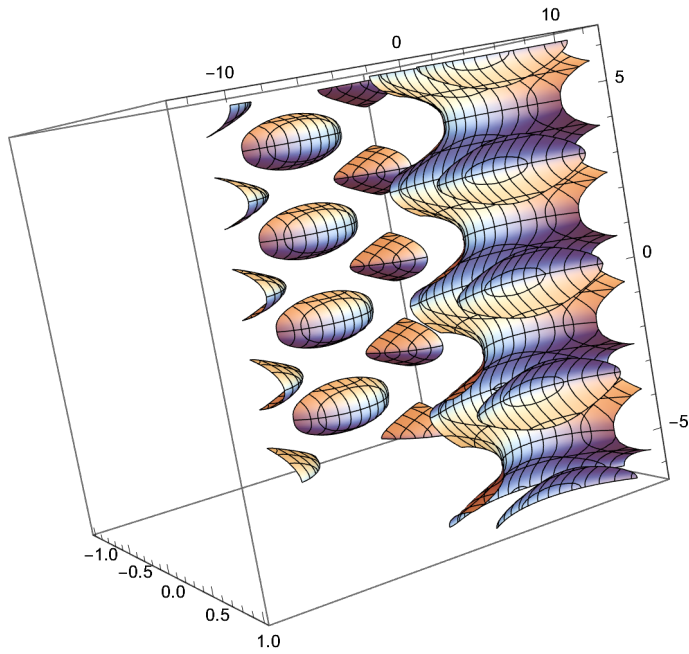




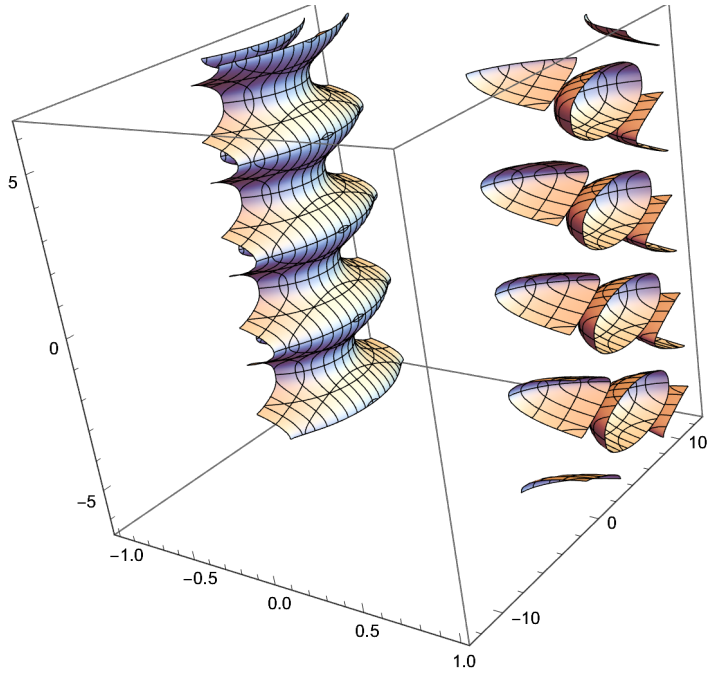
ContourPlot3D[

$$\left( \frac{4}{3} \pi \left( \frac{\sqrt{4 \pi r^2 (\theta) - r^2 (\theta)^2}}{2 \pi} \right)^3 - \left( \frac{4}{3} \pi \left( \frac{2 \pi r - r \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)}{2 \pi} \right)^3 \right) \right)^3,$$

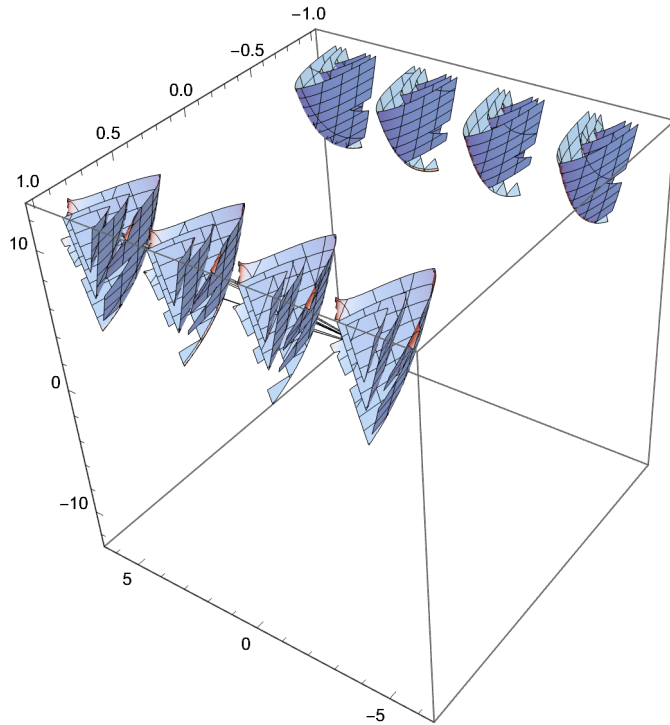
{r, -1, 1}, {\theta, -4 \pi, 4 \pi}, {\beta, -2 \pi, 2 \pi}]



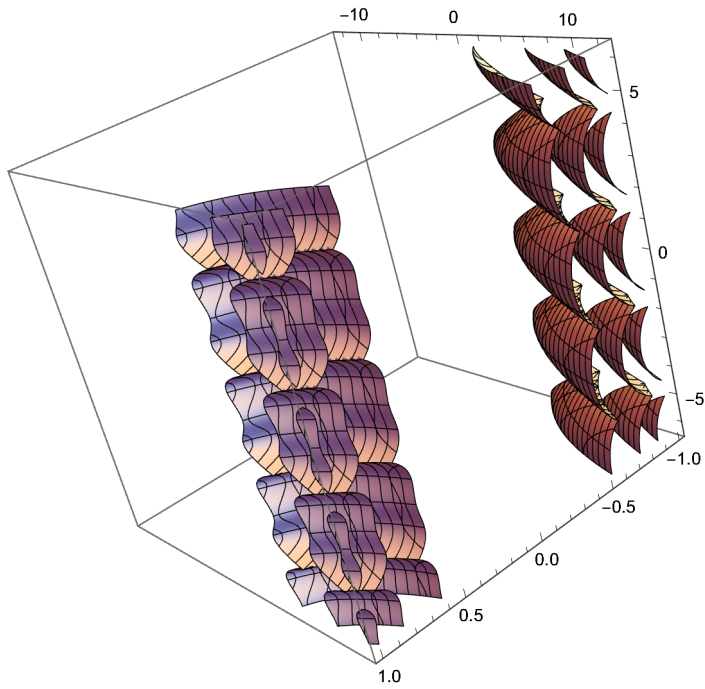
```
ContourPlot3D[
  (4 / 3)  $\pi$   $\left( \frac{\sqrt{4 \pi r^2 (\theta) - r^2 (\theta)^2}}{2 \pi} \right)^3 - (4 / 3) \pi \left( \frac{2 \pi r - r \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)}{2 \pi} \right)^3,$ 
  {r, -1, 1}, { $\theta$ , -4  $\pi$ , 4  $\pi$ }, { $\beta$ , -2  $\pi$ , 2  $\pi$ }]
```



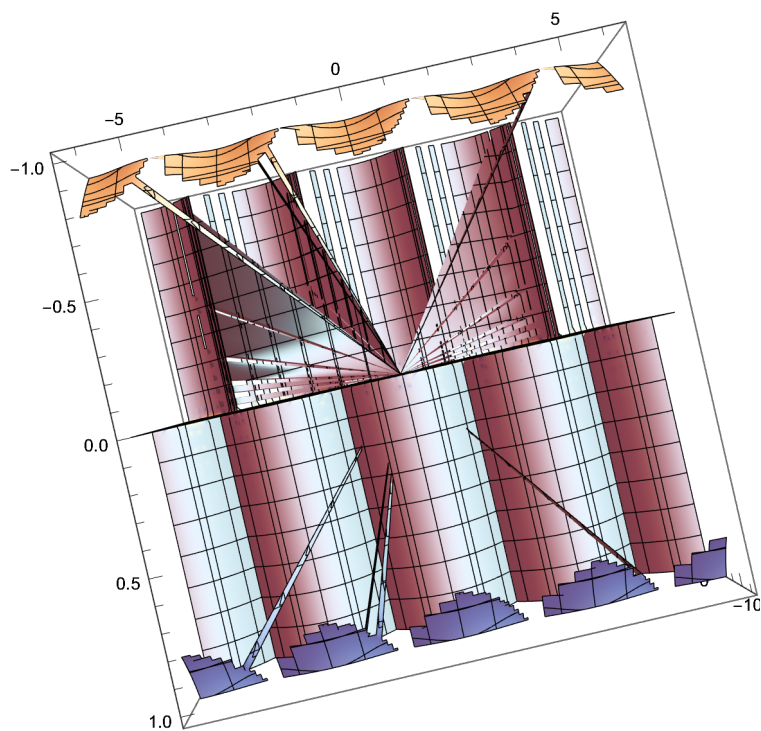
$\text{ContourPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2(\theta) - r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2\pi}\right)^3 - \right.$   
 $\left.\left(\frac{4}{3}\right)\pi\left(\frac{2\pi r - r\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}{2\pi}\right)^3, \right.$   
 $\left.\{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -2\pi, 2\pi\}\right]$



`ContourPlot3D`  $\left[ (4/3) \pi \left( \frac{\sqrt{4 \pi r^2 (\theta) - r^2 \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2}}{2 \pi} \right)^3 - \right. \right.$   
 $\left. (4/3) \pi \left( \frac{2 \pi r - r \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)}{2 \pi} \right)^3, \right.$   
 $\left. \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -2 \pi, 2 \pi\} \right]$

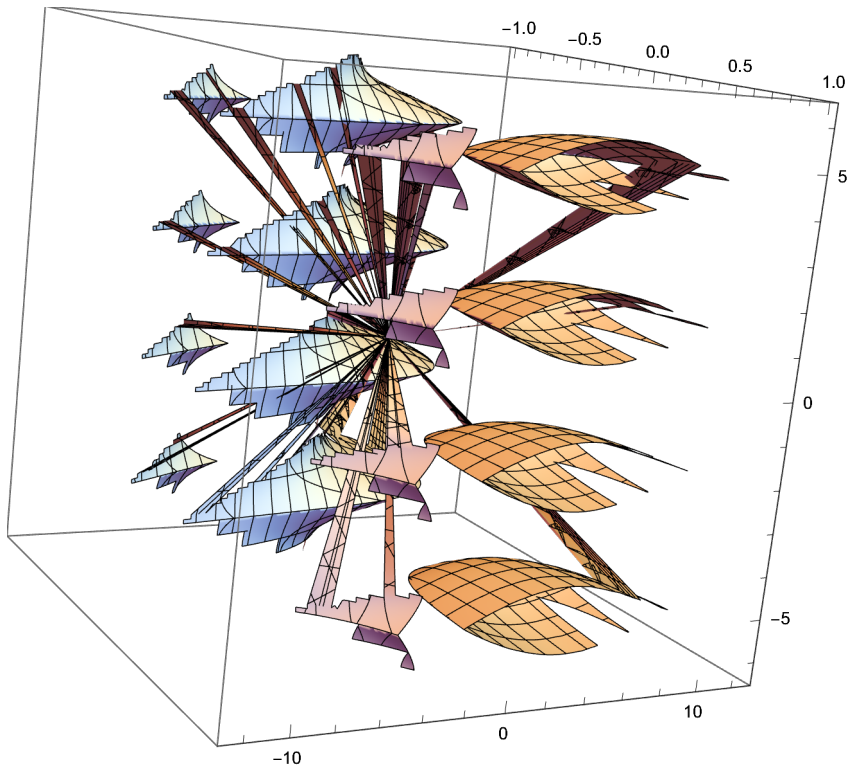


$\text{ContourPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)-r^2(\theta)^2}}{2\pi}\right)^3-\right.$   
 $\left.\left(\frac{4}{3}\right)\pi\left(\frac{2\pi r-r\theta}{2\pi}\right)^3,\{r,-1,1\},\{\theta,-4\pi,4\pi\},\{\beta,-2\pi,2\pi\}\right]$



$$\text{ContourPlot3D}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2\left(2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)-r^2(\theta)^2}}{2\pi}\right)^3-\right.$$

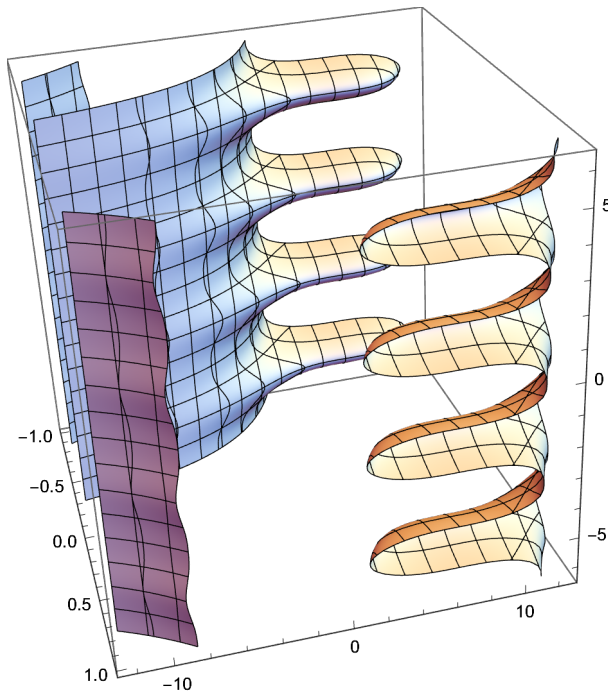
$$\left.\left(\frac{4}{3}\right)\pi\left(\frac{2\pi r-r\theta}{2\pi}\right)^3,\{r,-1,1\},\{\theta,-4\pi,4\pi\},\{\beta,-2\pi,2\pi\}\right]$$



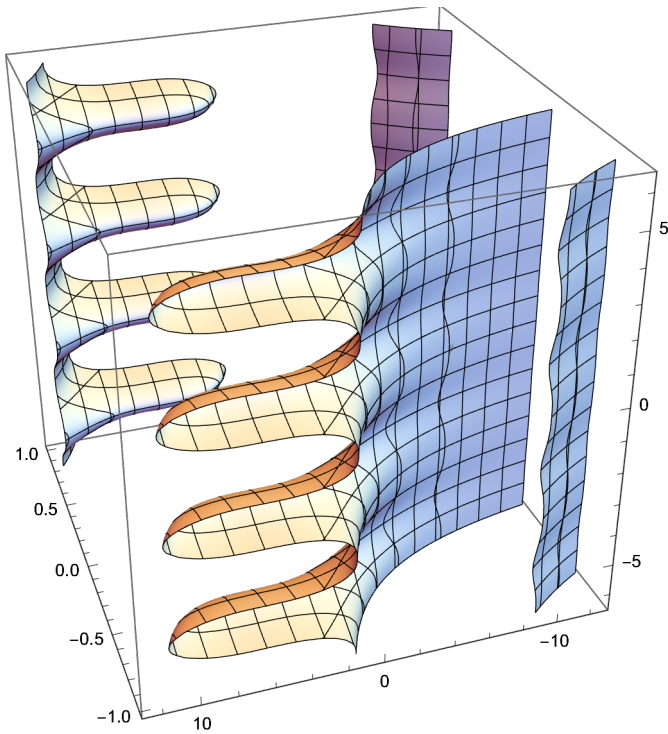
ContourPlot3D[  

$$(4/3)\pi \left( \frac{\sqrt{4\pi r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}}{2\pi} \right)^3 -$$
  

$$(4/3)\pi \left( \frac{2\pi r - r\theta}{2\pi} \right)^3, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -2\pi, 2\pi\}]$$



```
ContourPlot3D[
  (4 / 3)  $\pi \left( \frac{\sqrt{4 \pi r^2 \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}}{2 \pi} \right)^3 -$ 
  (4 / 3)  $\pi \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^3, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -2 \pi, 2 \pi\}]$ 
```



When more generally, we can understand that the function for the distance,  $\eta$ , and the function for the distance,  $r$  are different spheres. We can then discuss what the change in volume would be between these two spheres.

$$\text{Solve}\left[\theta == \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}, \beta \right]$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin}\left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\}, \left\{ \beta \rightarrow \text{ArcSin}\left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\} \right\}$$

## Solutions for the Speed of Light



# The Tearing of Space - Time?

In order to visualize these functions, we must set the internal velocity equal to something more specific.

Earlier, we showed

$$\text{that : } \left\{ \left\{ \mathbf{v} \rightarrow - \left( 1. \sqrt{ \left( 3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 \right) } \right) / \right. \right. \\ \left. \left( \sqrt{39.4784 - 12.5664 \theta + \theta^2} \right) \right\}, \quad (43) \\ \left\{ \mathbf{v} \rightarrow \left( \sqrt{ \left( 3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 \right) } \right) / \right. \\ \left. \left( \sqrt{39.4784 - 12.5664 \theta + \theta^2} \right) \right\} \left. \right\}$$

when the height of the cone equals the initial radius.

Thus, if we use the positive solutions for velocity, we can visualize these functions for the speed of light.

$$V :=$$

$$\sqrt{(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2)} / \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right)$$

$$\text{Solve} \left[ \frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} = c \left( (\theta / (2 \pi)) / \sqrt{1 - \frac{v^2}{c^2}} \right), c \right]$$

$$\left\{ \left\{ c \rightarrow -\sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} - (8 \times 2^{1/3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} + (2 \times 2^{1/3} r^4 \theta^3) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} + (16 \times 2^{1/3} \pi^2 r^4 \theta^3) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \right. \right.$$

$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} - \\
& (8 \times 2^{1/3} \pi r^4 \theta^4) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \Bigg) + \\
& (2^{1/3} r^4 \theta^5) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \Bigg) + \\
& \frac{1}{3 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \Bigg) \Bigg\}, \\
& \left\{ c \rightarrow \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} - (8 \times 2^{1/3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right. \right. \right. \\
& \quad 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& \quad 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} \right.} \\
& \quad \left. \left. \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} + \right. \\
& \quad \left. (2 \times 2^{1/3} r^4 \theta^3) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad \left. 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \right.
\end{aligned}$$

$$\begin{aligned}
& \left( (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} + \\
& \left( 16 \times 2^{1/3} \pi^2 r^4 \theta^3 \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} - \\
& \left( 8 \times 2^{1/3} \pi r^4 \theta^4 \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} + \\
& \left( 2^{1/3} r^4 \theta^5 \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} + \\
& \frac{1}{3 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} \Bigg\}, \\
& \left\{ c \rightarrow -\sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right. \right. \right. \\
& \quad 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& \quad 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \, i \, 2^{1/3} \sqrt{3} \, \pi \, r^4 \, \theta^2 \right) / \left( 108 \, \pi \, r^6 \, \theta^{10} - 27 \, r^6 \, \theta^{11} - 288 \, \pi^2 \, r^6 \, \theta^{11} + 144 \, \pi \, r^6 \, \theta^{12} + \right. \\
& \quad 128 \, \pi^3 \, r^6 \, \theta^{12} - 18 \, r^6 \, \theta^{13} - 96 \, \pi^2 \, r^6 \, \theta^{13} + 24 \, \pi \, r^6 \, \theta^{14} - 2 \, r^6 \, \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \, \pi^2 \, r^{12} \, \theta^{20} + \frac{1}{27} \left( -5832 \, \pi - 6912 \, \pi^3 \right) r^{12} \, \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \, \pi^2 \right) r^{12} \, \theta^{22} - 48 \, \pi \, r^{12} \, \theta^{23} + 4 \, r^{12} \, \theta^{24} \right) \right)^{1/3} - \\
& \left( 2^{1/3} \, r^4 \, \theta^3 \right) / \left( 108 \, \pi \, r^6 \, \theta^{10} - 27 \, r^6 \, \theta^{11} - 288 \, \pi^2 \, r^6 \, \theta^{11} + 144 \, \pi \, r^6 \, \theta^{12} + \right. \\
& \quad 128 \, \pi^3 \, r^6 \, \theta^{12} - 18 \, r^6 \, \theta^{13} - 96 \, \pi^2 \, r^6 \, \theta^{13} + 24 \, \pi \, r^6 \, \theta^{14} - 2 \, r^6 \, \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \, \pi^2 \, r^{12} \, \theta^{20} + \frac{1}{27} \left( -5832 \, \pi - 6912 \, \pi^3 \right) r^{12} \, \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \, \pi^2 \right) r^{12} \, \theta^{22} - 48 \, \pi \, r^{12} \, \theta^{23} + 4 \, r^{12} \, \theta^{24} \right) \right)^{1/3} + \\
& \left( i \, 2^{1/3} \sqrt{3} \, r^4 \, \theta^3 \right) / \left( 108 \, \pi \, r^6 \, \theta^{10} - 27 \, r^6 \, \theta^{11} - 288 \, \pi^2 \, r^6 \, \theta^{11} + 144 \, \pi \, r^6 \, \theta^{12} + \right. \\
& \quad 128 \, \pi^3 \, r^6 \, \theta^{12} - 18 \, r^6 \, \theta^{13} - 96 \, \pi^2 \, r^6 \, \theta^{13} + 24 \, \pi \, r^6 \, \theta^{14} - 2 \, r^6 \, \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \, \pi^2 \, r^{12} \, \theta^{20} + \frac{1}{27} \left( -5832 \, \pi - 6912 \, \pi^3 \right) r^{12} \, \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \, \pi^2 \right) r^{12} \, \theta^{22} - 48 \, \pi \, r^{12} \, \theta^{23} + 4 \, r^{12} \, \theta^{24} \right) \right)^{1/3} - \left( 8 \times 2^{1/3} \, \pi^2 \, r^4 \, \theta^3 \right) / \\
& \left( 3 \left( 108 \, \pi \, r^6 \, \theta^{10} - 27 \, r^6 \, \theta^{11} - 288 \, \pi^2 \, r^6 \, \theta^{11} + 144 \, \pi \, r^6 \, \theta^{12} + 128 \, \pi^3 \, r^6 \, \theta^{12} - 18 \, r^6 \, \theta^{13} - \right. \right. \\
& \quad \left. \left. 96 \, \pi^2 \, r^6 \, \theta^{13} + 24 \, \pi \, r^6 \, \theta^{14} - 2 \, r^6 \, \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \, \pi^2 \, r^{12} \, \theta^{20} + \frac{1}{27} \left( -5832 \, \pi - 6912 \right. \right. \right. \right. \\
& \quad \left. \left. \left. \pi^3 \right) r^{12} \, \theta^{21} + \frac{1}{27} \left( 729 + 5184 \, \pi^2 \right) r^{12} \, \theta^{22} - 48 \, \pi \, r^{12} \, \theta^{23} + 4 \, r^{12} \, \theta^{24} \right) \right)^{1/3} \right) + \\
& \left( 8 \, i \, 2^{1/3} \, \pi^2 \, r^4 \, \theta^3 \right) / \left( \sqrt{3} \left( 108 \, \pi \, r^6 \, \theta^{10} - 27 \, r^6 \, \theta^{11} - 288 \, \pi^2 \, r^6 \, \theta^{11} + 144 \, \pi \, r^6 \, \theta^{12} + \right. \right. \\
& \quad 128 \, \pi^3 \, r^6 \, \theta^{12} - 18 \, r^6 \, \theta^{13} - 96 \, \pi^2 \, r^6 \, \theta^{13} + 24 \, \pi \, r^6 \, \theta^{14} - 2 \, r^6 \, \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \, \pi^2 \, r^{12} \, \theta^{20} + \frac{1}{27} \left( -5832 \, \pi - 6912 \, \pi^3 \right) r^{12} \, \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \, \pi^2 \right) r^{12} \, \theta^{22} - 48 \, \pi \, r^{12} \, \theta^{23} + 4 \, r^{12} \, \theta^{24} \right) \right)^{1/3} \right) + \\
& \left( 4 \times 2^{1/3} \, \pi \, r^4 \, \theta^4 \right) / \left( 3 \left( 108 \, \pi \, r^6 \, \theta^{10} - 27 \, r^6 \, \theta^{11} - 288 \, \pi^2 \, r^6 \, \theta^{11} + 144 \, \pi \, r^6 \, \theta^{12} + \right. \right. \\
& \quad \left. \left. 128 \, \pi^3 \, r^6 \, \theta^{12} - 18 \, r^6 \, \theta^{13} - 96 \, \pi^2 \, r^6 \, \theta^{13} + 24 \, \pi \, r^6 \, \theta^{14} - 2 \, r^6 \, \theta^{15} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) - \\
& (4 \, \mathbf{i} \, 2^{1/3} \pi r^4 \theta^4) \Bigg/ \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) - \\
& (r^4 \theta^5) \Bigg/ \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) + \\
& (\mathbf{i} \, r^4 \theta^5) \Bigg/ \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \mathbf{i} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.}
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \Bigg\}, \\
\{c \rightarrow & \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right.} \\
& 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \right.} \\
& \left. \left. \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \right.} \\
& \left. (4 \pm 2^{1/3} \sqrt{3} \pi r^4 \theta^2) \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \right.} \\
& \left. (2^{1/3} r^4 \theta^3) \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \right.} \\
& \left. (\pm 2^{1/3} \sqrt{3} r^4 \theta^3) \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \right.} \\
& \left. (8 \times 2^{1/3} \pi^2 r^4 \theta^3) \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \right) \Bigg\} +
\end{aligned}$$

$$\begin{aligned}
& (8 \, \mathfrak{i} \, 2^{1/3} \pi^2 r^4 \theta^3) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) + \\
& (4 \times 2^{1/3} \pi r^4 \theta^4) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& (4 \, \mathfrak{i} \, 2^{1/3} \pi r^4 \theta^4) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& (r^4 \theta^5) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) + \\
& (\mathfrak{i} \, r^4 \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right.
\end{aligned}$$

$$\begin{aligned}
& 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \mathfrak{i} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg\}, \\
& \left\{ c \rightarrow -\sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right.} \right. \\
& \quad 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& \quad 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} + \\
& \quad \left. (4 \mathfrak{i} 2^{1/3} \sqrt{3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \quad \left. (2^{1/3} r^4 \theta^3) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \quad \left. (\mathfrak{i} 2^{1/3} \sqrt{3} r^4 \theta^3) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.}
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \Bigg)^{1/3} - \\
& (8 \times 2^{1/3} \pi^2 r^4 \theta^3) \Bigg/ \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& (8 \imath 2^{1/3} \pi^2 r^4 \theta^3) \Bigg/ \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) + \\
& (4 \times 2^{1/3} \pi r^4 \theta^4) \Bigg/ \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) + \\
& (4 \imath 2^{1/3} \pi r^4 \theta^4) \Bigg/ \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& (r^4 \theta^5) \Bigg/ \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) -
\end{aligned}$$

$$\begin{aligned}
& (\mathfrak{i} \, r^4 \, \theta^5) \Big/ \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Big) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \Big)^{1/3} + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \mathfrak{i} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \Big)^{1/3} \Big), \\
& \left\{ \mathfrak{c} \rightarrow \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) \Big/ \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right. \right. \right. \\
& \quad 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& \quad 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} + \\
& \quad (4 \mathfrak{i} \, 2^{1/3} \sqrt{3} \pi r^4 \theta^2) \Big/ \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} - \\
& \quad (2^{1/3} r^4 \theta^3) \Big/ \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} +
\end{aligned}$$

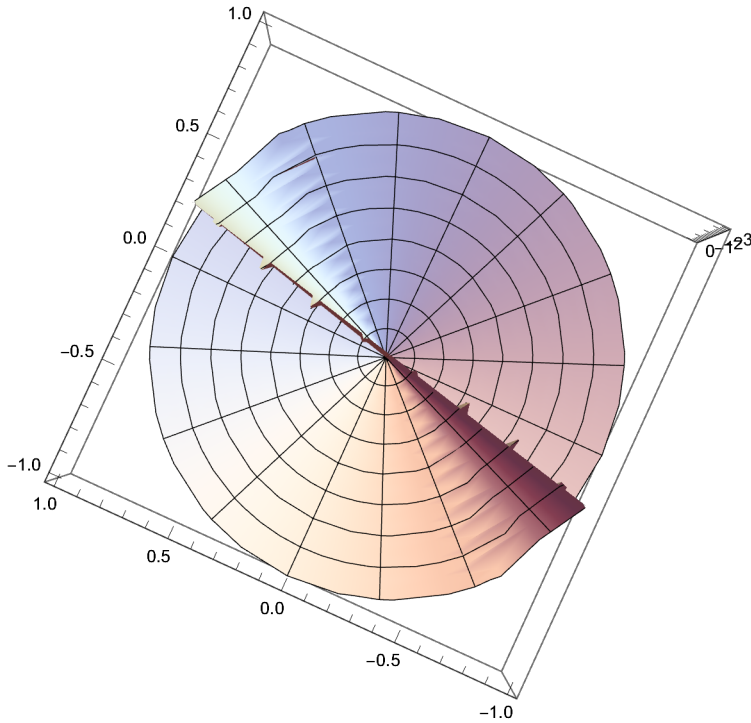
$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& (\mathfrak{i} 2^{1/3} \sqrt{3} r^4 \theta^3) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& (8 \times 2^{1/3} \pi^2 r^4 \theta^3) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) - \\
& (8 \mathfrak{i} 2^{1/3} \pi^2 r^4 \theta^3) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) + \\
& (4 \times 2^{1/3} \pi r^4 \theta^4) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) + \\
& (4 \mathfrak{i} 2^{1/3} \pi r^4 \theta^4) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.}
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3} \Bigg) - \\
& (r^4 \theta^5) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) - \\
& (i r^4 \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} i \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) \Bigg\}
\end{aligned}$$

RevolutionPlot3D[

$$\begin{aligned}
& -\sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} - (8 \times 2^{1/3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right. \right.} \\
& \quad 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& \quad \left. \left. 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \right.} \right. \right.
\end{aligned}$$

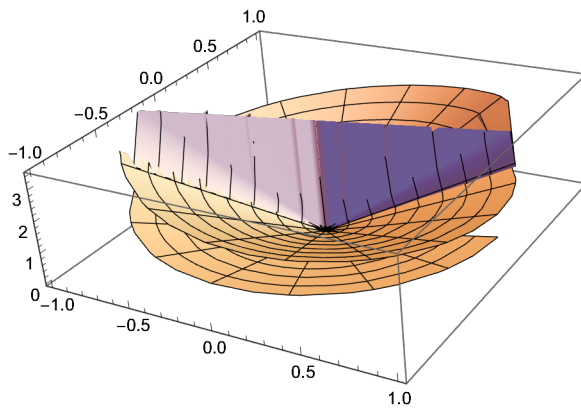
$$\begin{aligned}
& \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} + \\
& (2 \times 2^{1/3} r^4 \theta^3) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} + (16 \times 2^{1/3} \pi^2 r^4 \theta^3) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right. \right. \right. \\
& \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \right) - \\
& (8 \times 2^{1/3} \pi r^4 \theta^4) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) + \\
& (2^{1/3} r^4 \theta^5) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) + \\
& \frac{1}{3 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) \right.} \\
& \left. \left. r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} ]
\end{aligned}$$



RevolutionPlot3D[

$$\begin{aligned}
 & \sqrt{\left(-\frac{r^2}{3} + \frac{4\pi r^2}{3\theta} - (8 \times 2^{1/3} \pi r^4 \theta^2)\right) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
 & \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
 & \quad \left. 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - \right. \right. \\
 & \quad \left. \left. 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)\right)^{1/3} + (2 \times 2^{1/3} r^4 \theta^3) / \\
 & \quad \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + \right. \\
 & \quad \left. 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right. \right. \\
 & \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)\right)^{1/3} + (16 \times 2^{1/3} \pi^2 r^4 \theta^3) / \\
 & \quad \left(3 \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
 & \quad \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right. \right. \right. \\
 & \quad \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)\right)^{1/3} \right) -
 \end{aligned}$$

$$\begin{aligned}
& \left( 8 \times 2^{1/3} \pi r^4 \theta^4 \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) + (2^{1/3} r^4 \theta^5) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right. \right. \right. \\
& \quad \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \right) + \\
& \frac{1}{3 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - \right.} \\
& \quad \left. \left. 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}
\end{aligned}$$



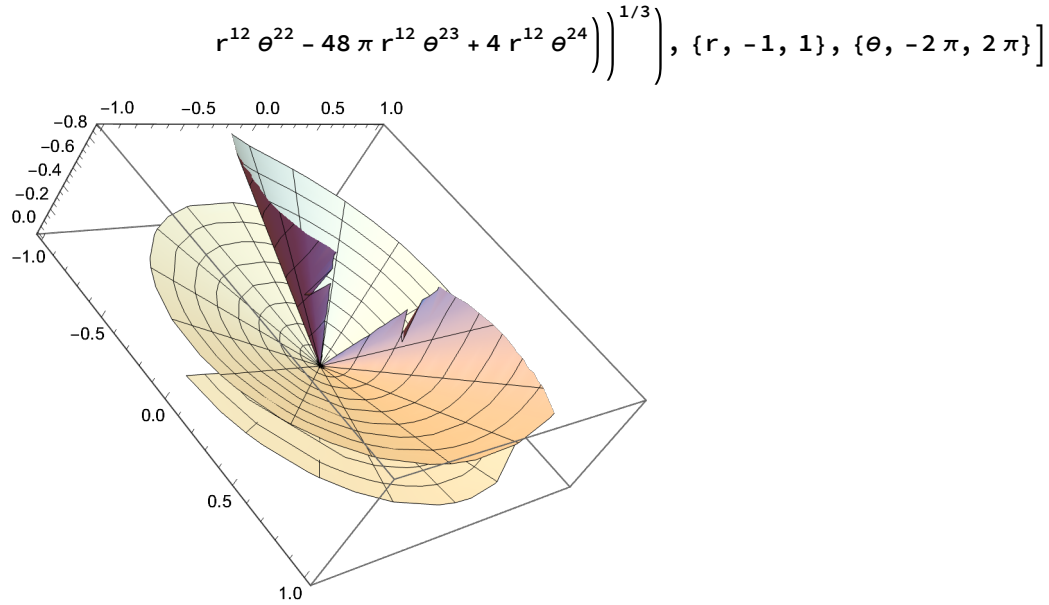
RevolutionPlot3D[

$$\begin{aligned}
& -\sqrt{\left( -\frac{r^2}{3} + \frac{4\pi r^2}{3\theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right. \right.} \\
& \quad 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \\
& \quad \left. \left. 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \left( 4 \, i^{1/3} \sqrt{3} \pi r^4 \theta^2 \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \left( 2^{1/3} r^4 \theta^3 \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - \right.} \\
& \quad \left. 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} + \\
& \left( i^{2/3} \sqrt{3} r^4 \theta^3 \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - (8 \times 2^{1/3} \pi^2 r^4 \theta^3) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right. \right. \right. \\
& \quad \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \right) + \\
& \left( 8 \, i^{2/3} \pi^2 r^4 \theta^3 \right) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} \Bigg) + \\
& \left( 4 \times 2^{1/3} \pi r^4 \theta^4 \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \right.
\end{aligned}$$



$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3}} - \\
& (4 \pm 2^{1/3} \pi r^4 \theta^4) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3}} - \\
& (r^4 \theta^5) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3}} + \\
& (\pm r^4 \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3}} - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3}} - \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \pm \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) \right.}
\end{aligned}$$

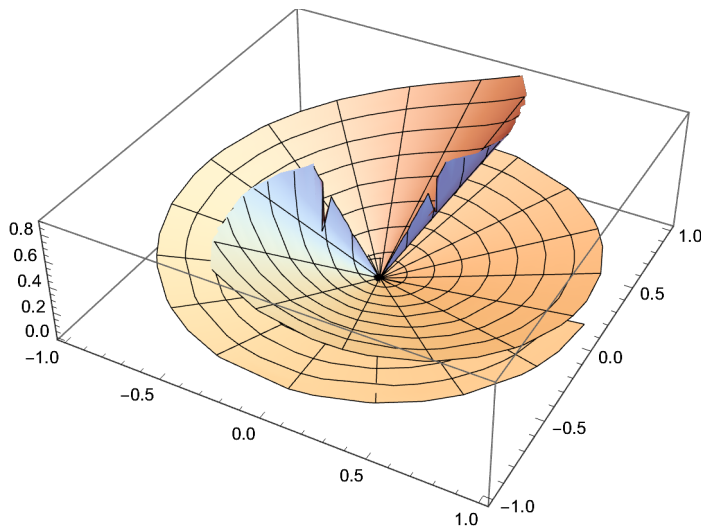


RevolutionPlot3D[

$$\begin{aligned}
 & \sqrt{\left(-\frac{r^2}{3} + \frac{4\pi r^2}{3\theta} + (4 \times 2^{1/3} \pi r^4 \theta^2)\right) / \left(108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + \right. \\
 & \quad 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + \\
 & \quad 3\sqrt{3} \sqrt{\left(432\pi^2 r^{12} \theta^{20} + \frac{1}{27}(-5832\pi - 6912\pi^3) r^{12} \theta^{21} + \frac{1}{27}(729 + 5184\pi^2) r^{12} \theta^{22} - \right. \\
 & \quad \left. 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24}\right)} \Big)^{1/3} - (4 \pm 2^{1/3} \sqrt{3} \pi r^4 \theta^2) / \\
 & \quad \left(108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - \right. \\
 & \quad 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + 3\sqrt{3} \sqrt{\left(432\pi^2 r^{12} \theta^{20} + \frac{1}{27}(-5832\pi - 6912\pi^3) \right. \\
 & \quad \left. r^{12} \theta^{21} + \frac{1}{27}(729 + 5184\pi^2) r^{12} \theta^{22} - 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24}\right)} \Big)^{1/3} - \\
 & \quad (2^{1/3} r^4 \theta^3) / \left(108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + 128\pi^3 r^6 \theta^{12} - \right. \\
 & \quad 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + 3\sqrt{3} \sqrt{\left(432\pi^2 r^{12} \theta^{20} + \frac{1}{27}(-5832\pi - \right. \\
 & \quad \left. 6912\pi^3) r^{12} \theta^{21} + \frac{1}{27}(729 + 5184\pi^2) r^{12} \theta^{22} - 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24}\right)} \Big)^{1/3} + \\
 & \quad (\pm 2^{1/3} \sqrt{3} r^4 \theta^3) / \left(108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + \right. \\
 & \quad \left. 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + \right.
 \end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} - (8 \times 2^{1/3} \pi^2 r^4 \theta^3) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right.} \right. \\
& \quad \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \right) + \\
& (8 \pm 2^{1/3} \pi^2 r^4 \theta^3) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) \right.} \right. \\
& \quad \left. \left. r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \right) + (4 \times 2^{1/3} \pi r^4 \theta^4) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right.} \right. \\
& \quad \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \right) - \\
& (4 \pm 2^{1/3} \pi r^4 \theta^4) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \right. \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \right) - \\
& (r^4 \theta^5) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \right. \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)^{1/3}} \right) +
\end{aligned}$$

$$\begin{aligned}
& (\mathbf{i} \, r^4 \, \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \mathbf{i} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - \right.} \\
& \quad \left. \left. 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg), \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



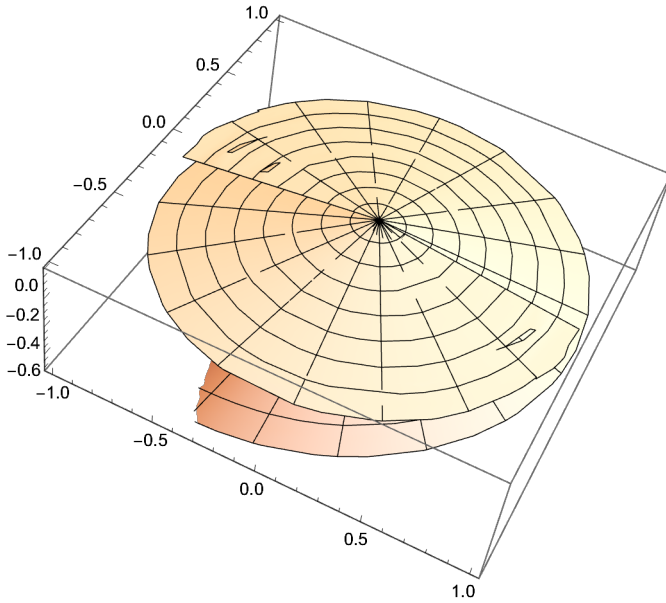
$$\begin{aligned}
& \text{RevolutionPlot3D} \Big[ \\
& \quad - \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + \right. \right.} \\
& \quad \left. \left. 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)}^{1/3} + \\
& \left(4 \pm 2^{1/3} \sqrt{3} \pi r^4 \theta^2\right) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)}^{1/3} - \\
& \left(2^{1/3} r^4 \theta^3\right) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - \right.} \\
& \quad \left. 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)}^{1/3} - \\
& \left(\pm 2^{1/3} \sqrt{3} r^4 \theta^3\right) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)}^{1/3} - (8 \times 2^{1/3} \pi^2 r^4 \theta^3) / \\
& \left(3 \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) \right. \right. \right. \\
& \quad \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)}^{1/3} \right) \right) - \\
& (8 \pm 2^{1/3} \pi^2 r^4 \theta^3) / \left(\sqrt{3} \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)}^{1/3} \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& (4 \times 2^{1/3} \pi r^4 \theta^4) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) + \\
& (4 \imath 2^{1/3} \pi r^4 \theta^4) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& (r^4 \theta^5) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& (\imath r^4 \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} \Bigg) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right)} \right)^{1/3} + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \imath \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right.
\end{aligned}$$

$$128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} +$$

$$3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)}^{1/3}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$



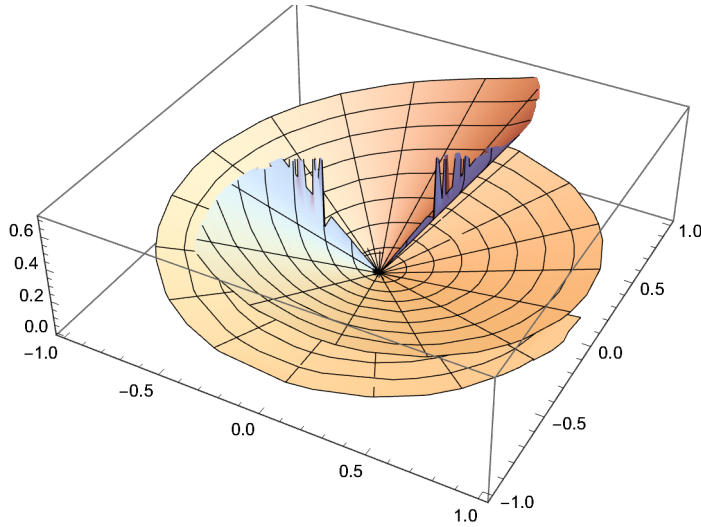
RevolutionPlot3D[

$$\sqrt{\left(-\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4 \theta^2)\right) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)}^{1/3} + (4 \pm 2^{1/3} \sqrt{3} \pi r^4 \theta^2) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)}^{1/3} - (2^{1/3} r^4 \theta^3) / \left(108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right)}^{1/3} - \right.$$

$$\begin{aligned}
& \left. \left( 6912 \pi^3 \right) r^{12} \theta^{21} + \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \\
& \left( i 2^{1/3} \sqrt{3} r^4 \theta^3 \right) / \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} - \left( 8 \times 2^{1/3} \pi^2 r^4 \theta^3 \right) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) \right. \right. \right. \\
& \quad \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \right) - \\
& \left( 8 i 2^{1/3} \pi^2 r^4 \theta^3 \right) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \frac{1}{27} \left( 729 + 5184 \pi^2 \right) \right.} \\
& \quad \left. \left. r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) + \left( 4 \times 2^{1/3} \pi r^4 \theta^4 \right) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \right. \right. \\
& \quad \left. \left. \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) \right. \right. \right. \\
& \quad \left. \left. \left. r^{12} \theta^{21} + \frac{1}{27} \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \right) + \\
& \left( 4 i 2^{1/3} \pi r^4 \theta^4 \right) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} \left( -5832 \pi - 6912 \pi^3 \right) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. \left( 729 + 5184 \pi^2 \right) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) - \\
& \left( r^4 \theta^5 \right) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right.
\end{aligned}$$



$$\begin{aligned}
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right) \Big)^{1/3} \Big) - \\
& (\mathfrak{i} r^4 \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right) \Big)^{1/3} \Big) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right) \Big)^{1/3} + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \mathfrak{i} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& 3 \sqrt{3} \sqrt{\left(432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - \right.} \\
& \left. 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24}\right) \Big)^{1/3} \Big), \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\} \Big]
\end{aligned}$$



RevolutionPlot3D[

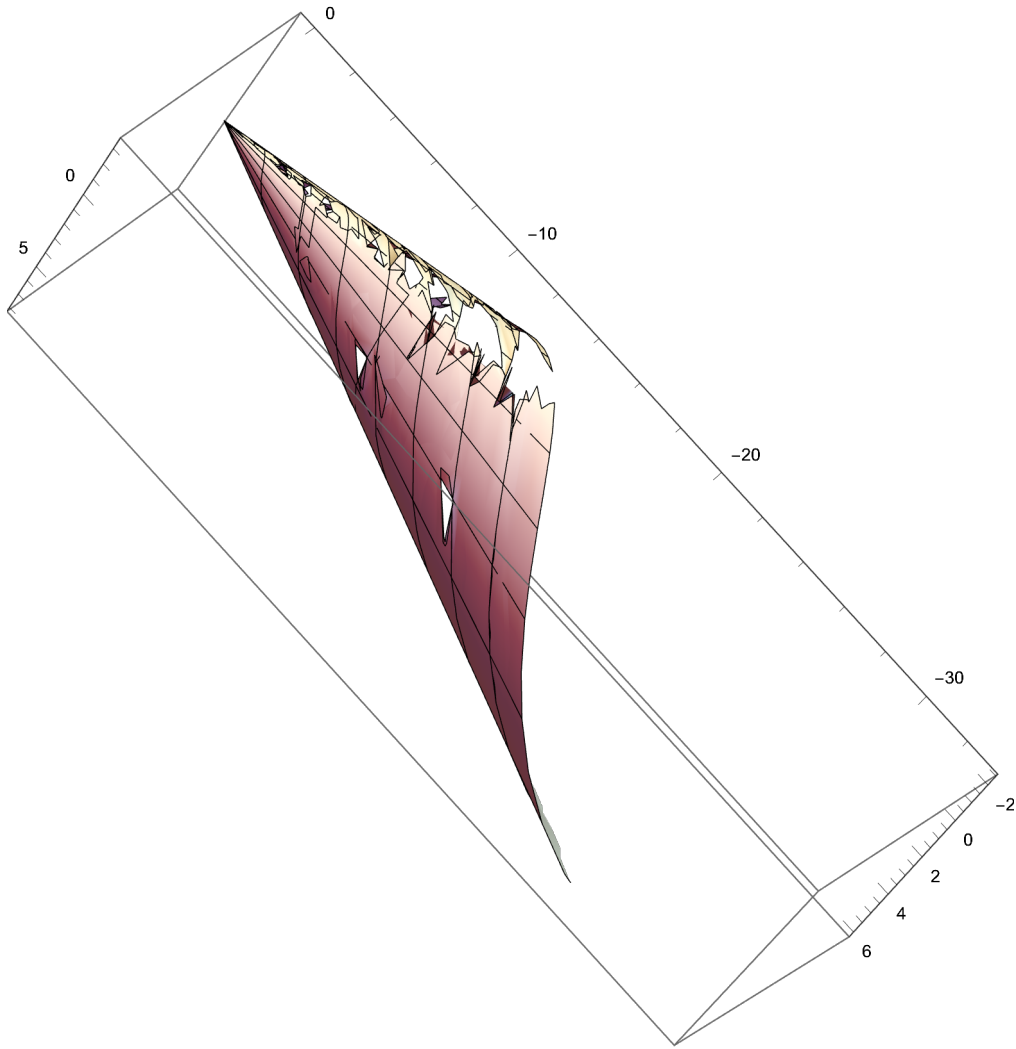
$$\left\{ \sqrt{\left( -\frac{r^2}{3} + \frac{4\pi r^2}{3\theta} + (4 \times 2^{1/3} \pi r^4 \theta^2) \right) / \left( 108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + 3\sqrt{3} \sqrt{\left( 432\pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832\pi - 6912\pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184\pi^2) r^{12} \theta^{22} - 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24} \right)} \right)^{1/3} + (4 \pm 2^{1/3} \sqrt{3} \pi r^4 \theta^2) / \left( 108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + 3\sqrt{3} \sqrt{\left( 432\pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832\pi - 6912\pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184\pi^2) r^{12} \theta^{22} - 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24} \right)} \right)^{1/3} - (2^{1/3} r^4 \theta^3) / \left( 108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + 3\sqrt{3} \sqrt{\left( 432\pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832\pi - 6912\pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184\pi^2) r^{12} \theta^{22} - 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24} \right)} \right)^{1/3} - (\pm 2^{1/3} \sqrt{3} r^4 \theta^3) / \left( 108\pi r^6 \theta^{10} - 27r^6 \theta^{11} - 288\pi^2 r^6 \theta^{11} + 144\pi r^6 \theta^{12} + 128\pi^3 r^6 \theta^{12} - 18r^6 \theta^{13} - 96\pi^2 r^6 \theta^{13} + 24\pi r^6 \theta^{14} - 2r^6 \theta^{15} + 3\sqrt{3} \sqrt{\left( 432\pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832\pi - 6912\pi^3) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184\pi^2) r^{12} \theta^{22} - 48\pi r^{12} \theta^{23} + 4r^{12} \theta^{24} \right)} \right)^{1/3} \right\}$$

$$\begin{aligned}
& \left. r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \Bigg)^{1/3} - \left( 8 \times 2^{1/3} \pi^2 r^4 \theta^3 \right) / \\
& \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - \right. \right. \\
& \quad \left. \left. 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \right. \right. \right. \\
& \quad \left. \left. \left. \pi^3 \right) r^{12} \theta^{21} + \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} \right) - \\
& \left( 8 \sqrt[3]{2^{1/3} \pi^2 r^4 \theta^3} \right) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} \right) + \\
& \left( 4 \sqrt[3]{2^{1/3} \pi r^4 \theta^4} \right) / \left( 3 \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} \right) + \\
& \left( 4 \sqrt[3]{2^{1/3} \pi r^4 \theta^4} \right) / \left( \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} \right) - \\
& \left( r^4 \theta^5 \right) / \left( 3 \times 2^{2/3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad \left. \left. 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right) \Bigg)^{1/3} \right) -
\end{aligned}$$

$$\begin{aligned}
& (\mathfrak{i} r^4 \theta^5) / \left( 2^{2/3} \sqrt{3} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \right.} \\
& \quad \left. \left. \frac{1}{27} (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) - \\
& \frac{1}{6 \times 2^{1/3} \theta^5} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + 128 \pi^3 r^6 \theta^{12} - \right. \\
& \quad 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg) + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta^5} \mathfrak{i} \left( 108 \pi r^6 \theta^{10} - 27 r^6 \theta^{11} - 288 \pi^2 r^6 \theta^{11} + 144 \pi r^6 \theta^{12} + \right. \\
& \quad 128 \pi^3 r^6 \theta^{12} - 18 r^6 \theta^{13} - 96 \pi^2 r^6 \theta^{13} + 24 \pi r^6 \theta^{14} - 2 r^6 \theta^{15} + \\
& \quad 3 \sqrt{3} \sqrt{\left( 432 \pi^2 r^{12} \theta^{20} + \frac{1}{27} (-5832 \pi - 6912 \pi^3) r^{12} \theta^{21} + \frac{1}{27} \right.} \\
& \quad \left. \left. (729 + 5184 \pi^2) r^{12} \theta^{22} - 48 \pi r^{12} \theta^{23} + 4 r^{12} \theta^{24} \right) \right)^{1/3} \Bigg), \\
& - \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4) / \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + \right. \right. \right. \\
& \quad 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& \quad \left. \left. 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6 \right) \right)^{1/3}} + (4 \mathfrak{i} 2^{1/3} \pi r^4) / \right. \\
& \quad \left( \sqrt{3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad \left. \left. 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right. \right. \\
& \quad \left. \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6 \right) \right)^{1/3} \Bigg) + \\
& (4 \times 2^{1/3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \\
& \quad \left. \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6 \right) \right)^{1/3} + \\
& (4 \mathfrak{i} 2^{1/3} \sqrt{3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \right.}
\end{aligned}$$

$$\begin{aligned}
& \left( \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6 \right)^{1/3} - \left( 8 \times 2^{1/3} \pi^2 r^4 \right) / \\
& \left( 3 \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad \left. \left. 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right. \right. \\
& \quad \left. \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) - \\
& \left( 8 i 2^{1/3} \pi^2 r^4 \right) / \left( \sqrt{3} \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) - \\
& (r^4 \theta) / \left( 3 \times 2^{2/3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) - \\
& (i r^4 \theta) / \left( 2^{2/3} \sqrt{3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) - \\
& (2^{1/3} r^2 v^2 \theta) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad \left. 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right. \\
& \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} - \\
& (i 2^{1/3} \sqrt{3} r^2 v^2 \theta) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right. \\
& \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} - \\
& \frac{1}{6 \times 2^{1/3} \theta} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad \left. 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right. \\
& \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} + \\
& \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta} i \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad \left. 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6 \right)^{1/3} \Bigg), \\
& - \sqrt[3]{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} - (8 \times 2^{1/3} \pi r^4) \right) / \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + \right. \right. \\
& \quad 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - \\
& \quad 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& \quad 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Bigg)^{1/3} - \\
& \quad (8 \times 2^{1/3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \\
& \quad \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Bigg)^{1/3} + \\
& \quad (16 \times 2^{1/3} \pi^2 r^4) / \left( 3 \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& \quad 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Bigg)^{1/3} \Bigg) + (2^{1/3} r^4 \theta) / \\
& \quad \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& \quad 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Bigg)^{1/3} \Bigg) + \\
& \quad (2 \times 2^{1/3} r^2 v^2 \theta) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \\
& \quad \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Bigg)^{1/3} + \\
& \quad \frac{1}{3 \times 2^{1/3} \theta} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi \\
& \quad \left. r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Bigg)^{1/3} \Bigg] \Bigg\}, \{r, -10, 10\}, \{\theta, -4 \pi, 4 \pi\} \Bigg]
\end{aligned}$$



$$1 == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \sqrt{\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}} ==\right.$$

$$\left. c \left( \frac{\theta}{2 \pi} \right) / \sqrt{\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}} \right), ]$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \sqrt{\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}} == \right. \\ \left. c \left( (\theta / (2 \pi)) / \sqrt{\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{v^2}{c^2}} \right), \beta \right] \\ \left\{ \left\{ \beta \rightarrow \text{ArcSin}\left[\frac{-c^5 r \theta + c^2 r^2 v^2 \sqrt{(4 \pi - \theta) \theta}}{2 c^4 \pi r^2}\right] \right\}, \left\{ \beta \rightarrow \text{ArcSin}\left[\frac{c^5 r \theta + c^2 r^2 v^2 \sqrt{(4 \pi - \theta) \theta}}{2 c^4 \pi r^2}\right] \right\} \right\}$$

```
c := (2.99792458 * 10 ^ 8)
```

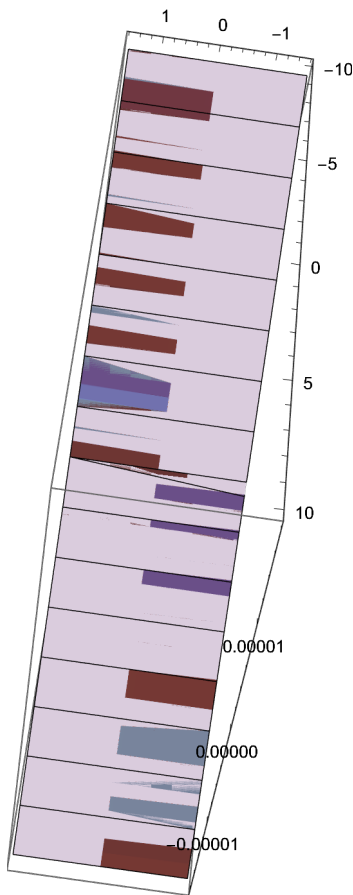
$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{-c^5 \theta + c^2 v^2 \sqrt{(4\pi - \theta)^2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}}{2 c^4 \pi}\right], \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi, \pi\}\right]$$

-0.0002900065



$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\frac{-c^5 r \theta + c^2 r^2 v^2 \sqrt{(4 \pi - \theta) \theta}}{2 c^4 \pi r^2}\right], \{r, -10, 10\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right\}\right\} \quad (44)$$

$$\text{Solve}\left[\text{ArcSin}\left[\frac{c^5 r \theta + c^2 r^2 v^2 \sqrt{(4 \pi - \theta) \theta}}{2 c^4 \pi r^2}\right] == \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right], \theta\right]$$

## Addendum No. 2

$$\theta \rightarrow \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} \quad (45)$$

$$\text{Solve}\left[\theta == \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}\right\}$$

$$\theta \rightarrow 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \quad (46)$$

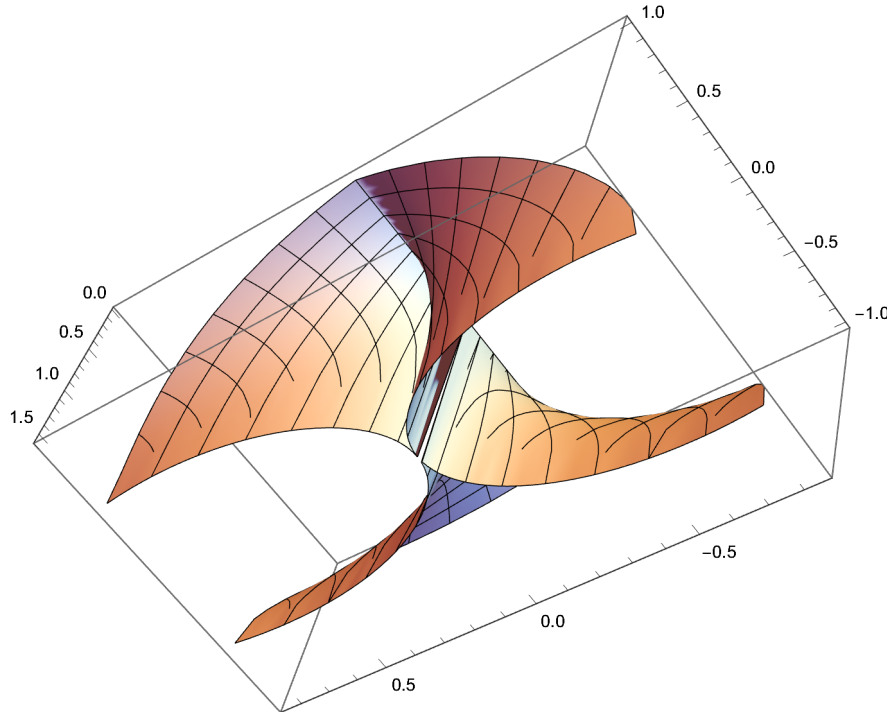
$$\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} == 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \quad (47)$$

$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \quad (48)$$

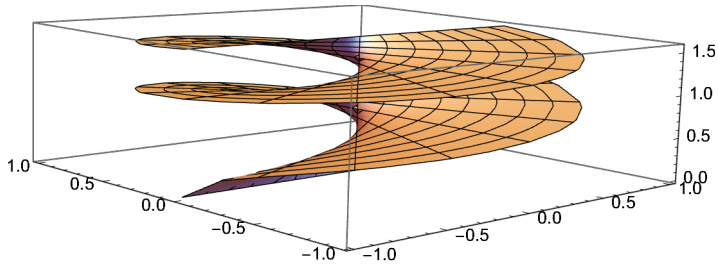
$$\text{Solve}\left[\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} == 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right), \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right\}\right\}$$

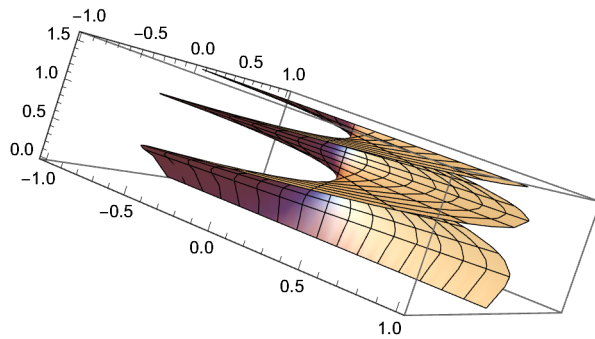
$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right], \{r, -1, 1\}, \{\eta, -1, 1\}\right]$$



$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\sqrt{\frac{\left(\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right)^2}{r^2}}\right], \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



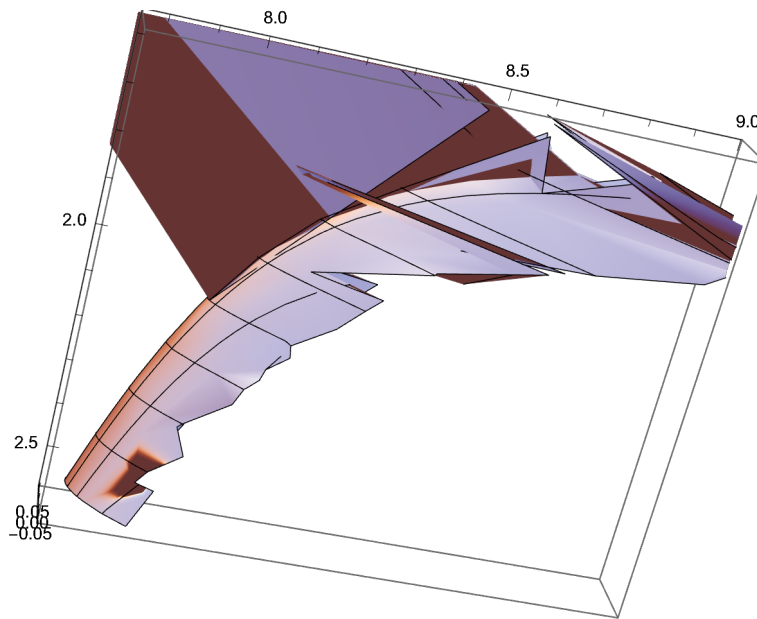
$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\sqrt{\frac{(\eta)^2}{\left(\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right)^2}}\right], \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



## Grasshopper Batman Helmet

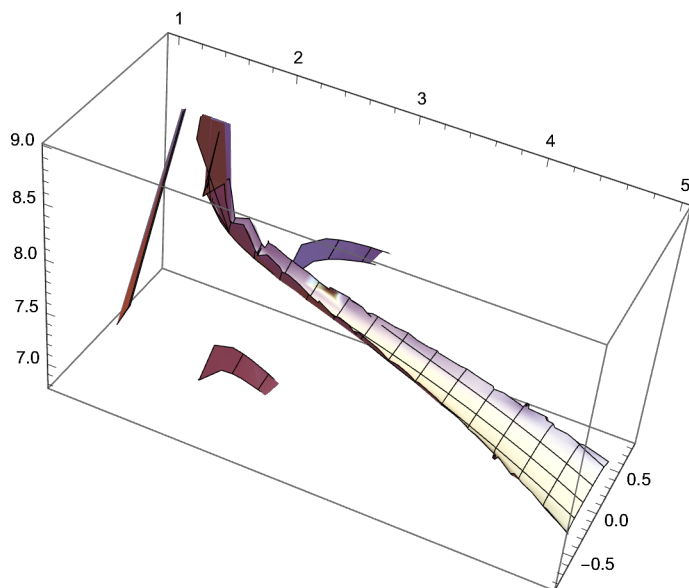
SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} + \right. \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right), \{\theta, -.1\pi, .1\pi\}, \{\beta, -.05\pi, .05\pi\}]$$



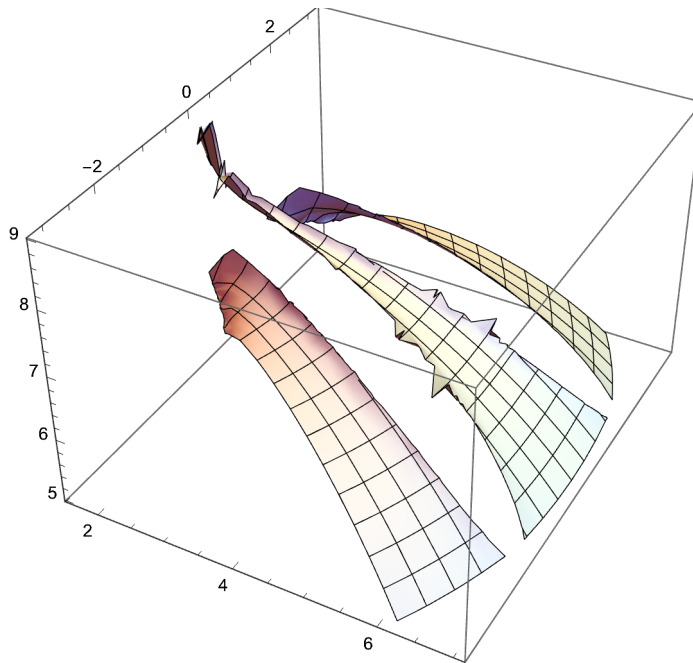
SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^4 + \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right], \{\theta, -.2\pi, .2\pi\}, \{\beta, -.1\pi, .1\pi\}]$$



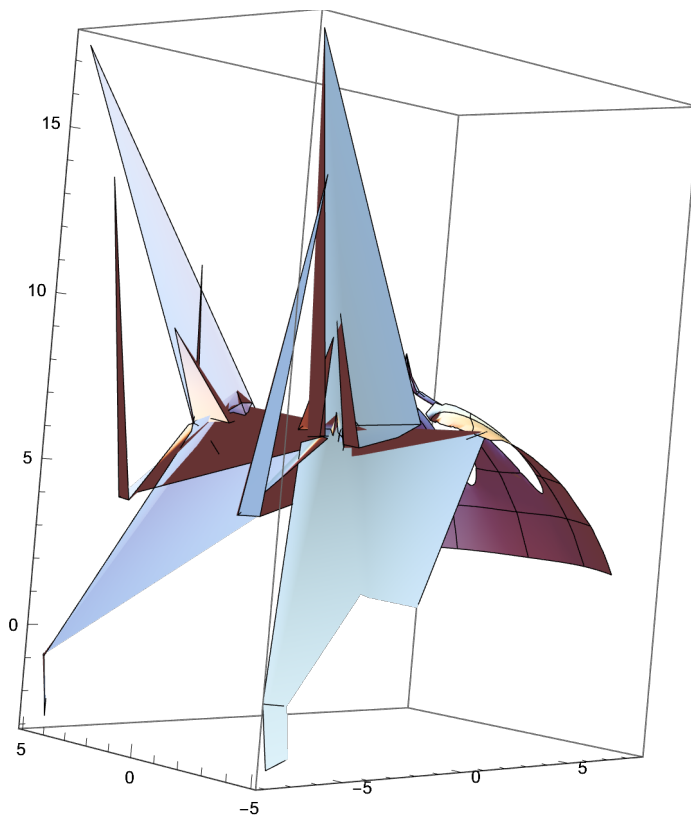
SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^4 + \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right], \{\theta, -.3\pi, .3\pi\}, \{\beta, -.15\pi, .15\pi\}]$$



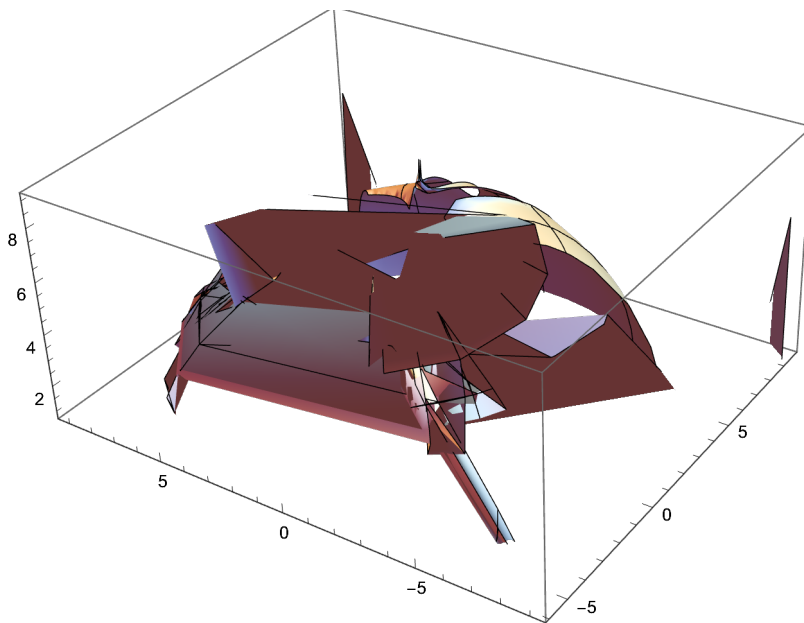
SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} + \right. \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3}, \{\theta, -.4\pi, .4\pi\}, \{\beta, -.2\pi, .2\pi\} \right]$$



SphericalPlot3D[

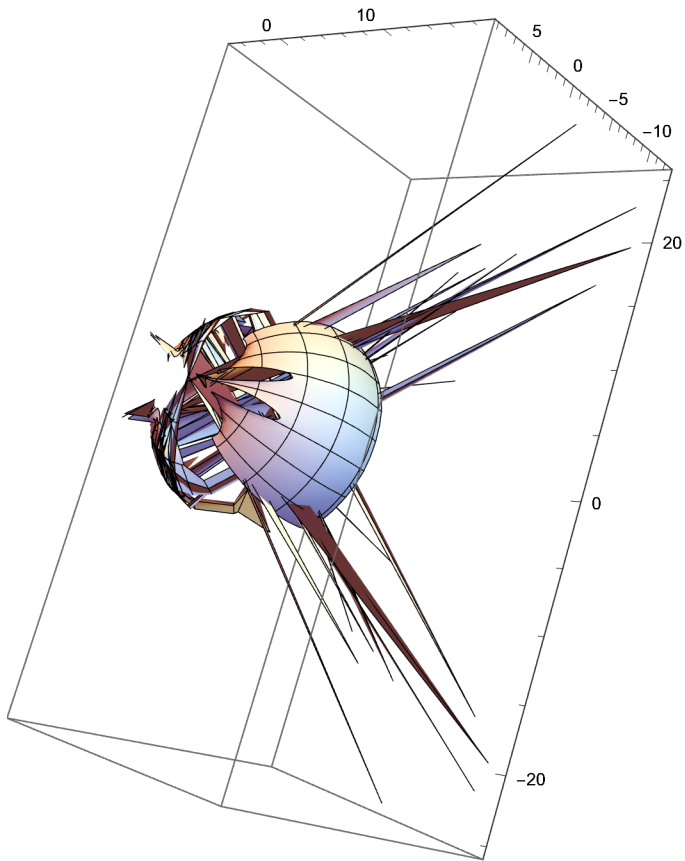
$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} + \right. \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right), \{\theta, -.5\pi, .5\pi\}, \{\beta, -.25\pi, .25\pi\}]$$





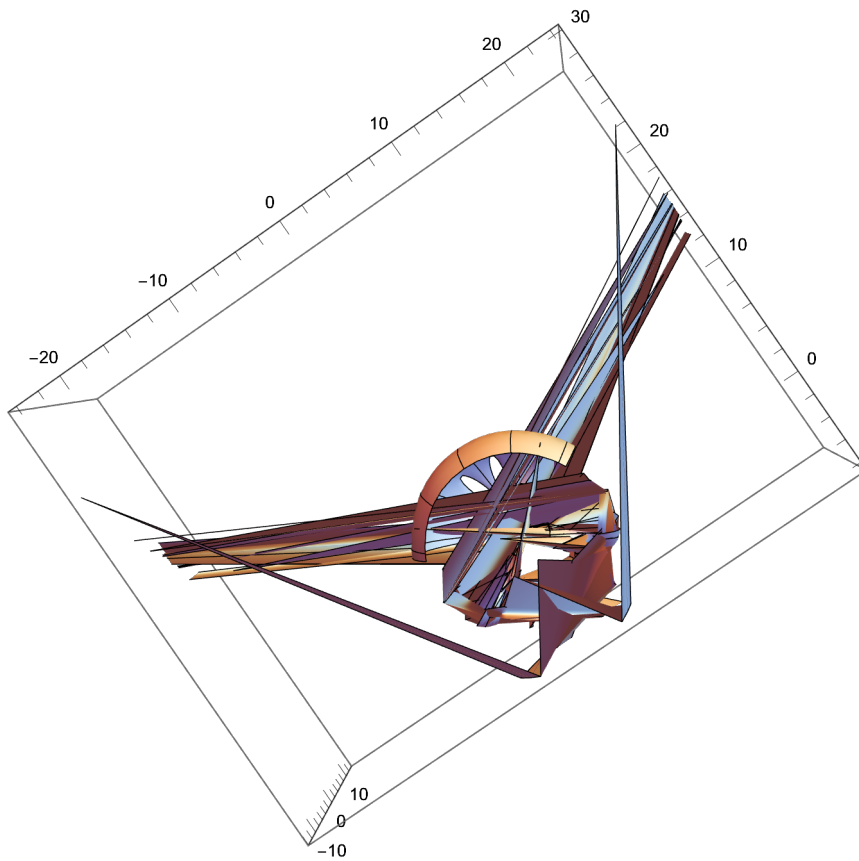
SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} + \right. \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right], \{\theta, -.6\pi, .6\pi\}, \{\beta, -.3\pi, .3\pi\}]$$



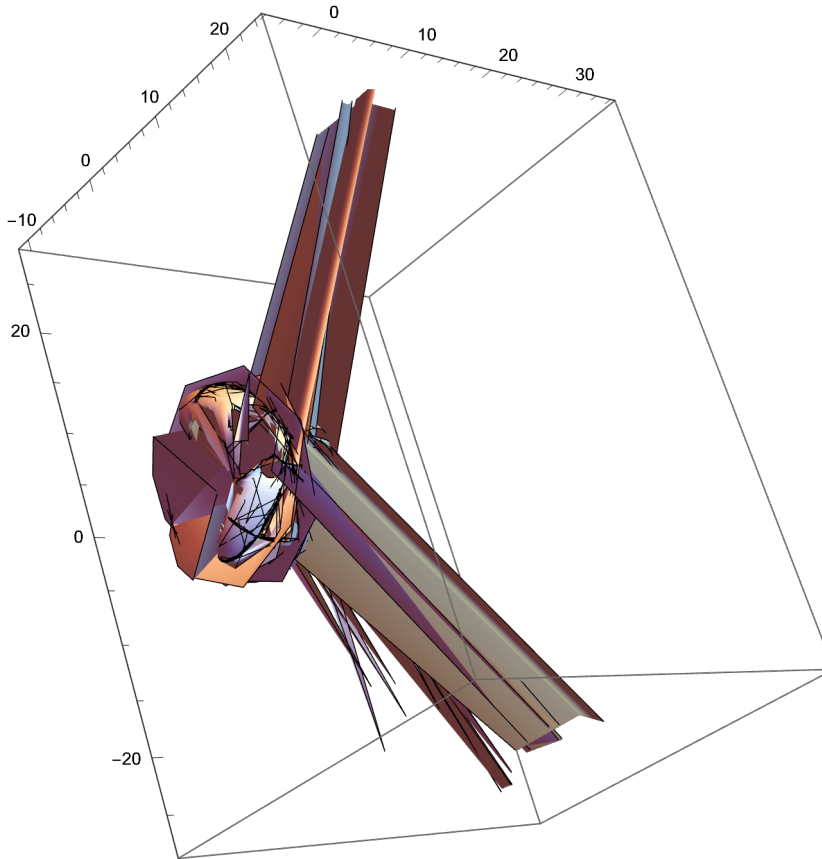
SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} + \right. \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right], \{\theta, -.7\pi, .7\pi\}, \{\beta, -.35\pi, .35\pi\}]$$



SphericalPlot3D[

$$\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + 3\sqrt{3} \right. \right. \\ \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} \right)^{1/3} \right) + \\ \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^6} + \right. \\ \left. \left. \pi^6 \sin[\beta]^6 \right)^{1/3} \right], \{\theta, -.8\pi, .8\pi\}, \{\beta, -.4\pi, .4\pi\}]$$

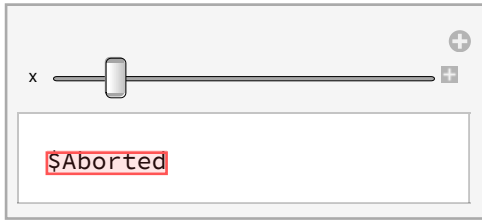


Solve[n π θ == m π r - m π x, n]

$$\left\{ \left\{ n \rightarrow \frac{m r - m x}{\theta} \right\} \right\}$$

Manipulate[

$$\text{ContourPlot3D}\left[\frac{m r - m x}{\theta}, \{m, -10, 10\}, \{r, -10, 10\}, \{\theta, -2\pi, 2\pi\}, \{x, -10, 10\}\right]$$



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

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... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

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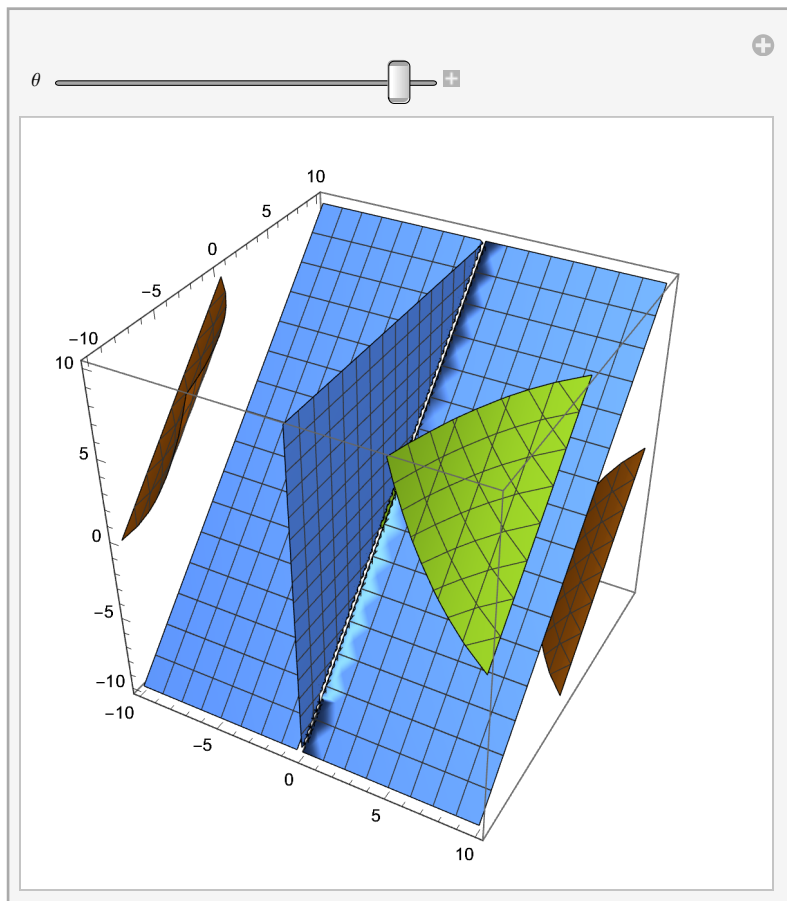
... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

Manipulate[  
 ContourPlot3D[ $\frac{m r - m x}{\theta}$ , {m, -10, 10}, {x, -10, 10}, {r, -10, 10}], { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

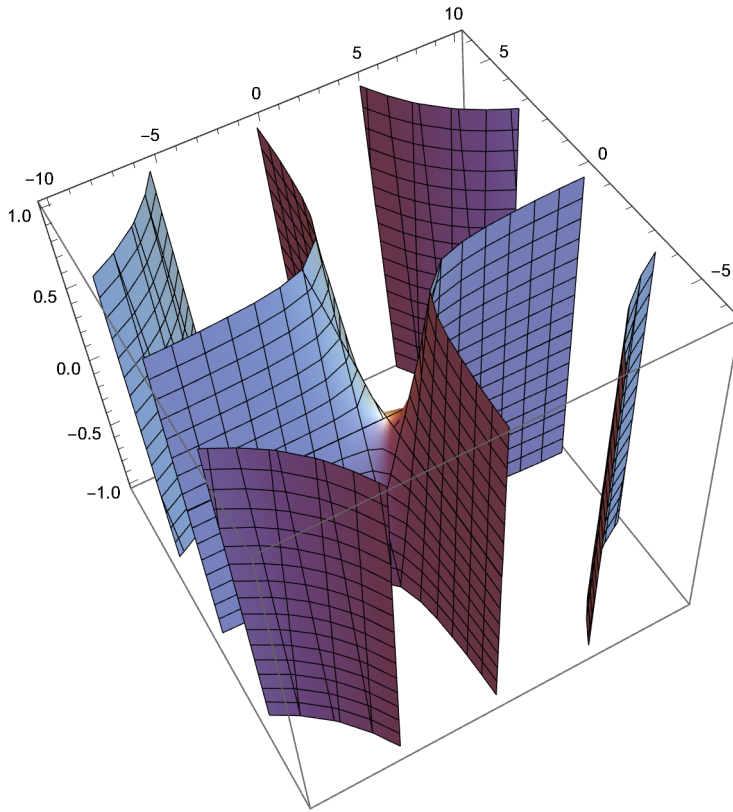


$$\frac{m r - m x}{\theta}$$

Solve[n  $\pi$   $\theta$  == 2  $\pi$  r - 2  $\pi$  x, r]

$$\left\{ \left\{ r \rightarrow \frac{1}{2} (2 x + n \theta) \right\} \right\}$$

ContourPlot3D $\left[\frac{1}{2} (2 x + n \theta), \{x, -1, 1\}, \{n, -10, 10\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\begin{aligned} & \text{Solve}\left[\left((8 \pi r \theta - 2 r \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right.\right. \\ & \quad \left.\left(2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right.\right. \\ & \quad \left.\left.\frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta}\right)\right. \\ & \quad \left.\left(-4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right.\right. \\ & \quad \left.\left.\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2}\right)\right) / \\ & \quad \left(2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right.\right. \\ & \quad \left.\left.\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right)^3\right) - \end{aligned}$$

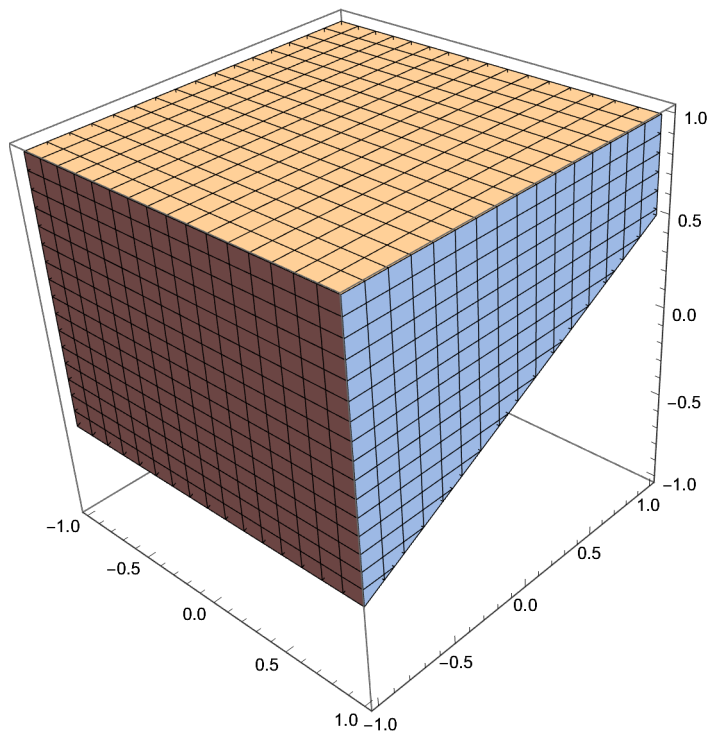
$$\begin{aligned}
& \left( (8\pi r\theta - 2r\theta^2) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right. \\
& \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \left. \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \right) / \\
& \left( 4\pi\sqrt{4\pi r^2\theta - r^2\theta^2} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) - \\
& \left( (8\pi r\theta - 2r\theta^2) (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2\sin[\beta]^2) \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta] \right. \right. \\
& \left. \left. \sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right) / \\
& \left( 4\pi\sqrt{4\pi r^2\theta - r^2\theta^2} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) + \\
& \left( (4\pi r^2 - 2r^2\theta) (8\pi r\theta - 2r\theta^2) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right. \\
& \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \right. \\
& \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right) / \\
& \left( 8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) - \\
& \left( (8\pi r - 4r\theta) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) / \\
& \left( 4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) - \\
& \left( (8 \pi r \theta - 2 r \theta^2) (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) / \\
& \left( 4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) + \\
& (4 \pi (8 \pi r \theta - 2 r \theta^2) \cos[\beta] \sin[\beta]) / \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \\
& \quad \left. \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) - \\
& ((4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2) (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta])) / \\
& \left( 8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) + \\
& ((8 \pi r - 4 r \theta) (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta])) / \\
& \left( 4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) =
\end{aligned}$$

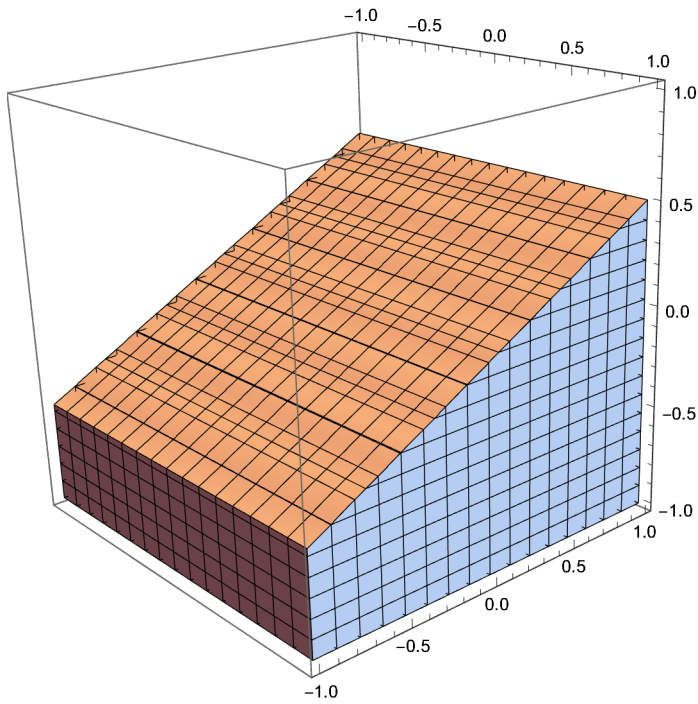


$$\left( r - \frac{r \theta}{2 \pi} \right) / \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right. \\ \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right), r]$$

RegionPlot3D[ $\overline{AC} < \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{AC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]



`RegionPlot3D[ $\overline{AC} \geq \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{AC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`



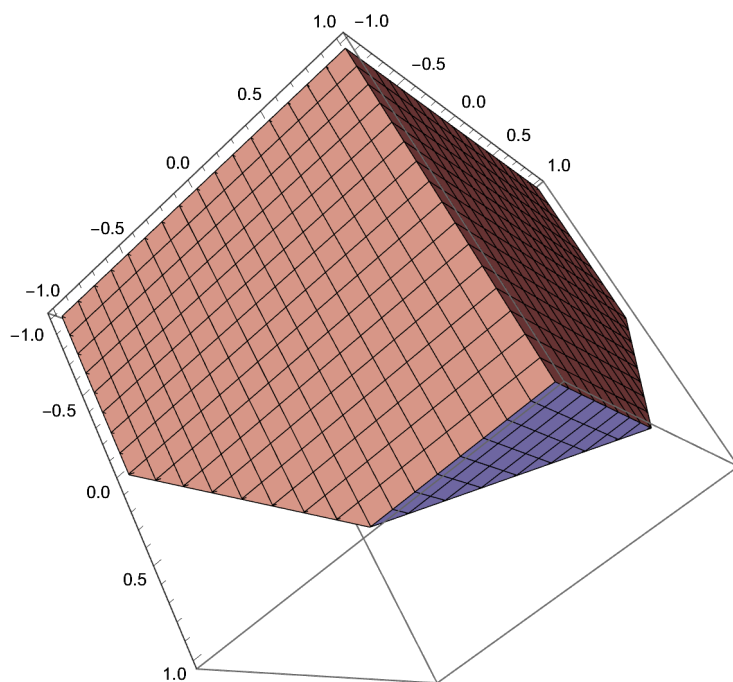
`RegionPlot3D[ $g > \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} + \frac{2\pi r - r\theta}{2\pi}$ , { $r$ , -1, 1}, { $g$ , -1, 1}, { $\theta$ , -1, 1}]`

Greater::nord: Invalid comparison with  $-1.15915 + 0.586208 i$  attempted. >>

RegionPlot3D::boolf:  $g > \frac{\sqrt{4\pi r^2 \theta - \text{Power}[\ll 2 \gg] \text{Power}[\ll 2 \gg]}}{2\pi} + \frac{2\pi r - r\theta}{2\pi}$  must be a Boolean function. >>

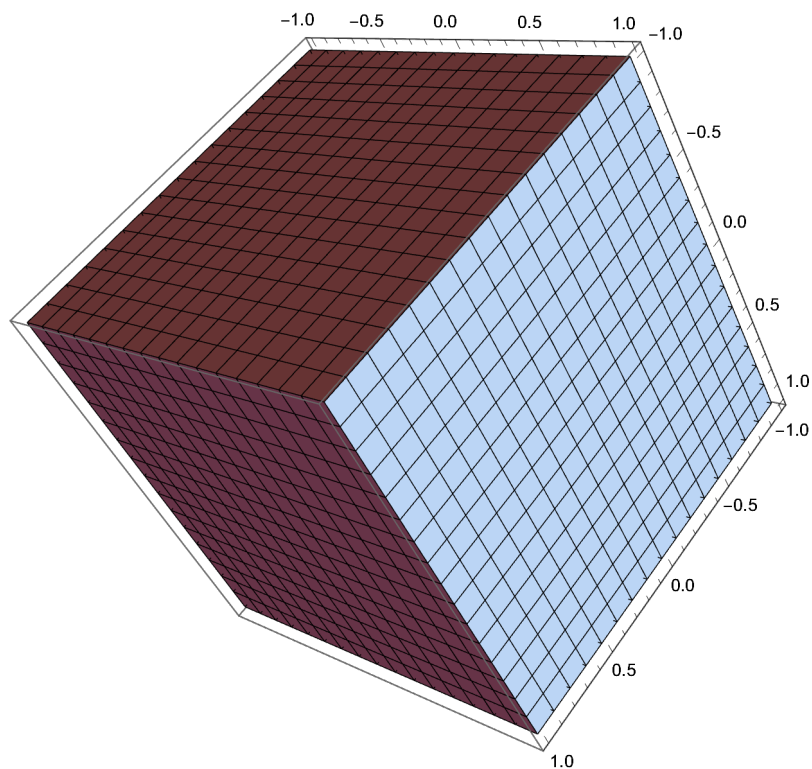
`RegionPlot3D[ $g > \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} + \frac{2\pi r - r\theta}{2\pi}$ , { $r$ , -1, 1}, { $g$ , -1, 1}, { $\theta$ , -1, 1}]`

`RegionPlot3D[AC ≥ AB + DE, {AB, -1, 1}, {AC, -1, 1}, {DE, -1, 1}]`

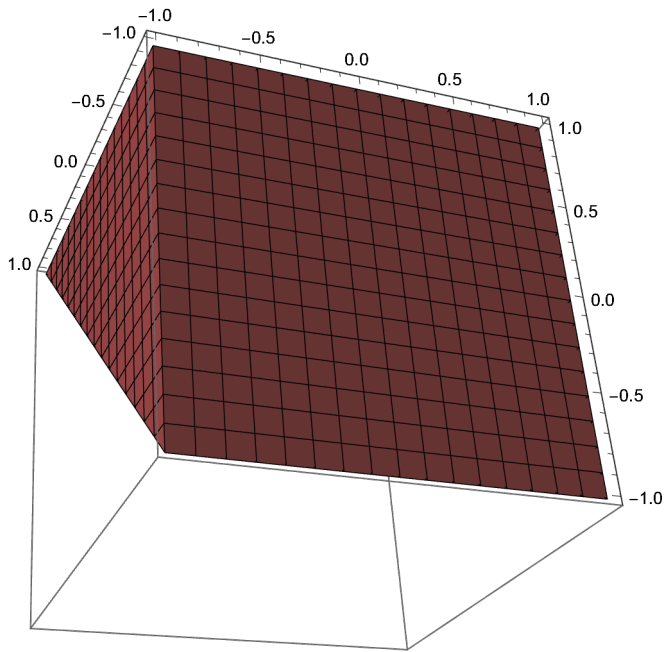


`RegionPlot3D[ $\overline{AC} \geq \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{AC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`

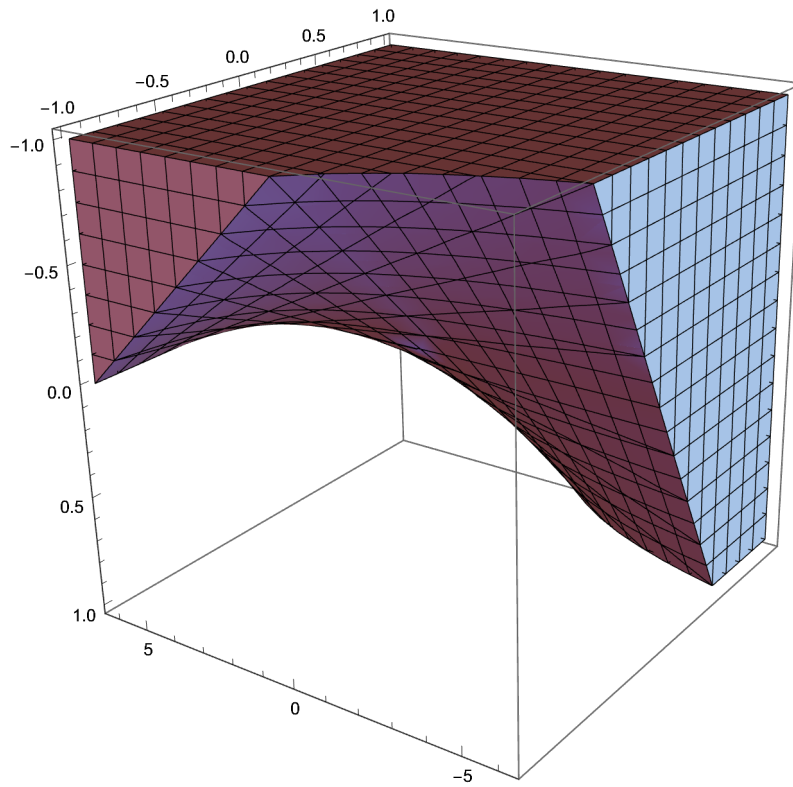
`RegionPlot3D[ $\overline{AB} + \overline{BC} \geq \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{BC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`



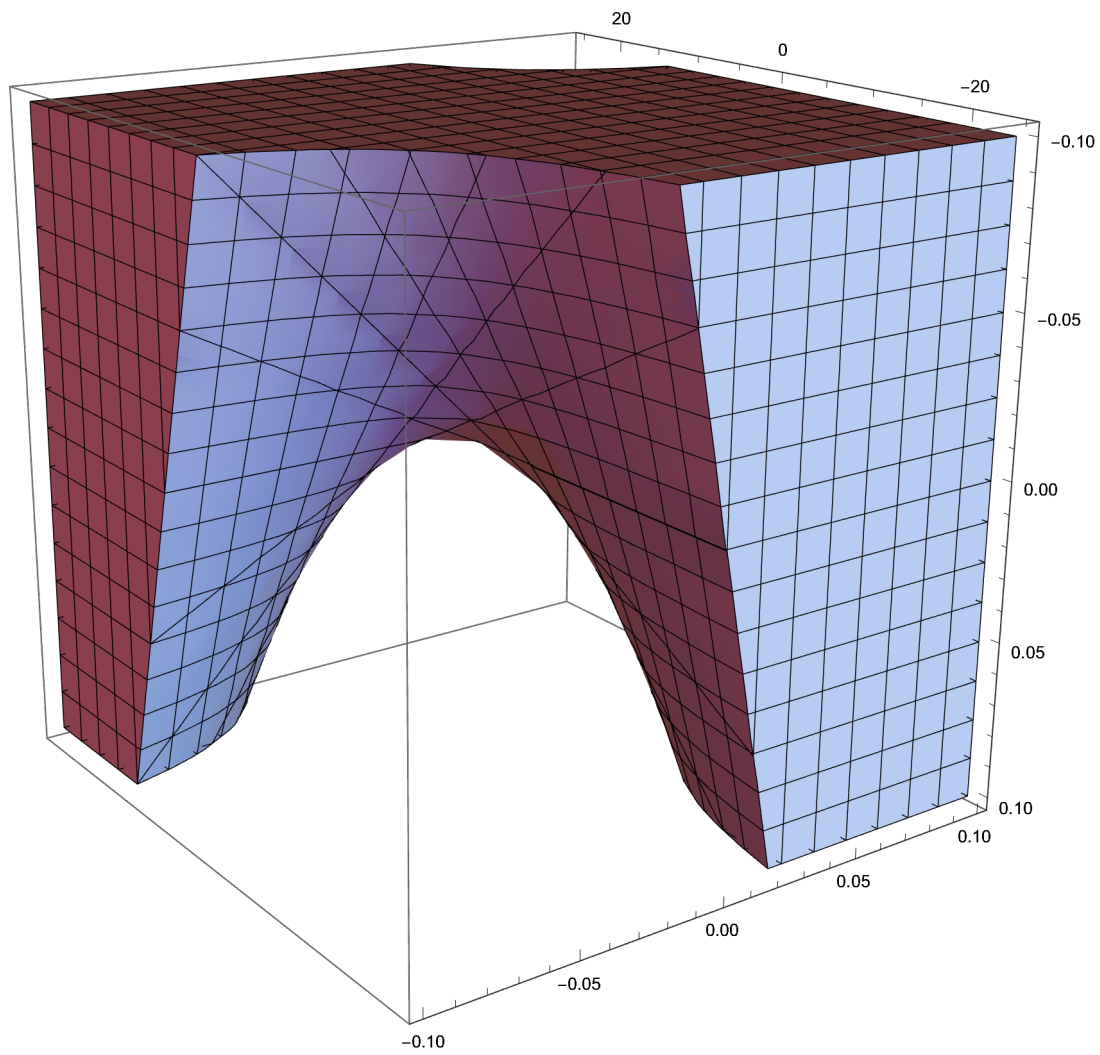
`RegionPlot3D[AB + BC < AB + DE, {AB, -1, 1}, {BC, -1, 1}, {DE, -1, 1}]`



`RegionPlot3D[2  $\pi$  r - 2  $\pi$  x >  $\theta$  r, {r, -1, 1}, {x, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]`



`RegionPlot3D[2  $\pi$  r - 2  $\pi$  x >  $\theta$  r, {r, -.1, .1}, {x, -.1, .1}, { $\theta$ , -8  $\pi$ , 8  $\pi$ }]`



```

RegionPlot3D[
  2 π ⎛⎛⎛ -4 π θ + θ² + 2 π √(4 π - θ) θ Sin[β] + 4 π² Sin[β]² -  $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta}$  -
 $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}$  ⎟⎟⎟ /
  (16 π² θ - 12 π θ² + 2 θ³ - 16 π³ Sin[β]² + 8 π² θ Sin[β]²) ⎟ - 2 π x <
  θ ⎛⎛⎛ -4 π θ + θ² + 2 π √(4 π - θ) θ Sin[β] + 4 π² Sin[β]² -  $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta}$  -
 $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}$  ⎟⎟⎟ / (16 π² θ - 12 π θ² + 2 θ³ - 16 π³ Sin[β]² + 8 π² θ Sin[β]²) ⎟,
  {β, -π, π}, {x, -1, 1}, {θ, -2 π, 2 π}]

```

Less::nord : Invalid comparison with  $6.03319 + 1.76763 \times 10^{-17} i$  attempted. >>

```

RegionPlot3D::boolf :  $\frac{2 \pi (-4 \pi \theta + \theta^2 + 2 \ll 3 \gg + \ll 1 \gg - \ll 1 \gg - 2 \ll 3 \gg \text{Power}[\ll 2 \gg])}{\ll 6 \gg + 8 \text{Power}[\ll 2 \gg] \theta \text{Power}[\ll 2 \gg]} - 2 \pi x < \frac{\theta(\ll 1 \gg)}{\ll 1 \gg}$  must be a
Boolean function. >>

```

```

RegionPlot3D[
  ⎛⎛⎛ 2 π ⎛⎛⎛ -4 π θ + θ² + 2 π √(4 π - θ) θ Sin[β] + 4 π² Sin[β]² -  $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta}$  -
 $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}$  ⎟⎟⎟ /
  (16 π² θ - 12 π θ² + 2 θ³ - 16 π³ Sin[β]² + 8 π² θ Sin[β]²) - 2 π x <
  ⎛⎛⎛ θ ⎛⎛⎛ -4 π θ + θ² + 2 π √(4 π - θ) θ Sin[β] + 4 π² Sin[β]² -
 $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta}$  -  $\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}$  ⎟⎟⎟ /
  (16 π² θ - 12 π θ² + 2 θ³ - 16 π³ Sin[β]² + 8 π² θ Sin[β]²) ⎟, {β,
  -π, π}, {x, -1, 1}, {θ, -2 π, 2 π} ⎟

```

```

RegionPlot3D[2 π r - 2 π  $\frac{2 \pi r - r^2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{2 \pi} < 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) r,$ 
  {r, -1, 1}, {β, -π/2, π/2}, {θ, -4 π, 4 π}]

```

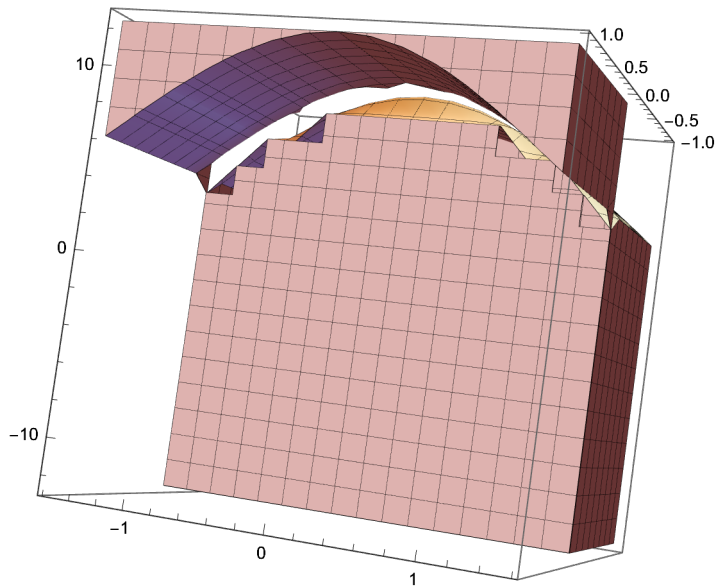
**RegionPlot3D** $\left[2 \pi \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} - 2 \pi x > \theta \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

Greater::nord : Invalid comparison with 6.28319 + 3.6276 i attempted. >>

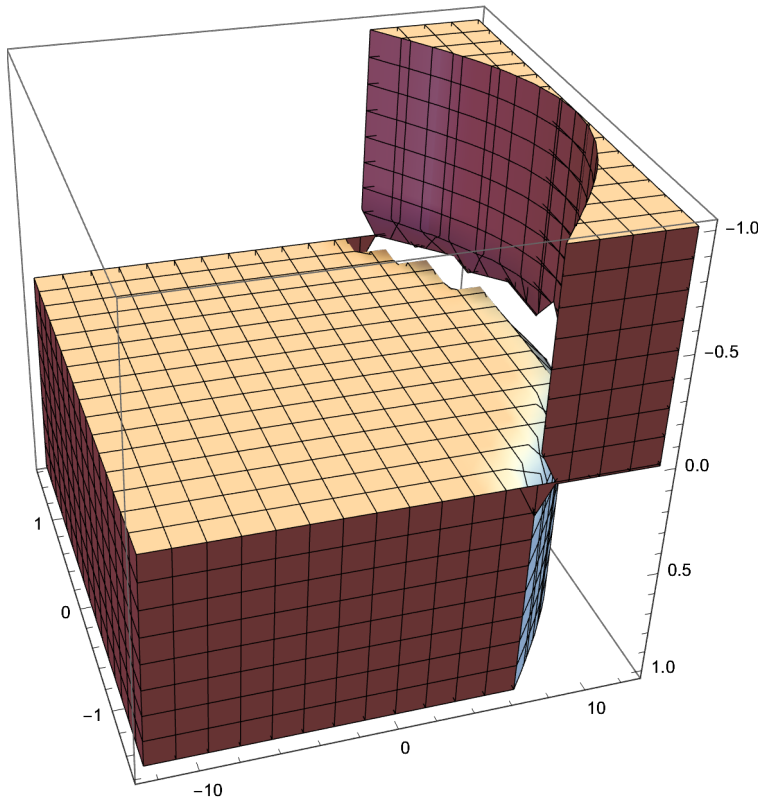
**RegionPlot3D::boolf** :  $\frac{2 \pi (2 \pi \eta)}{\sqrt{\text{Times}[\llbracket 3 \rrbracket] + \text{Times}[\llbracket 2 \rrbracket]}} - 2 \pi x > \frac{\theta (2 \pi \eta)}{\sqrt{4 \pi \theta - \text{Power}[\llbracket 2 \rrbracket]}}$  must be a Boolean function. >>

**RegionPlot3D** $\left[\frac{2 \pi (2 \pi \eta)}{\sqrt{4 \pi \theta - \theta^2}} - 2 \pi x > \frac{\theta (2 \pi \eta)}{\sqrt{4 \pi \theta - \theta^2}}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

**RegionPlot3D** $\left[2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} > 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) r, \{r, -1, 1\}, \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -4 \pi, 4 \pi\}\right]$

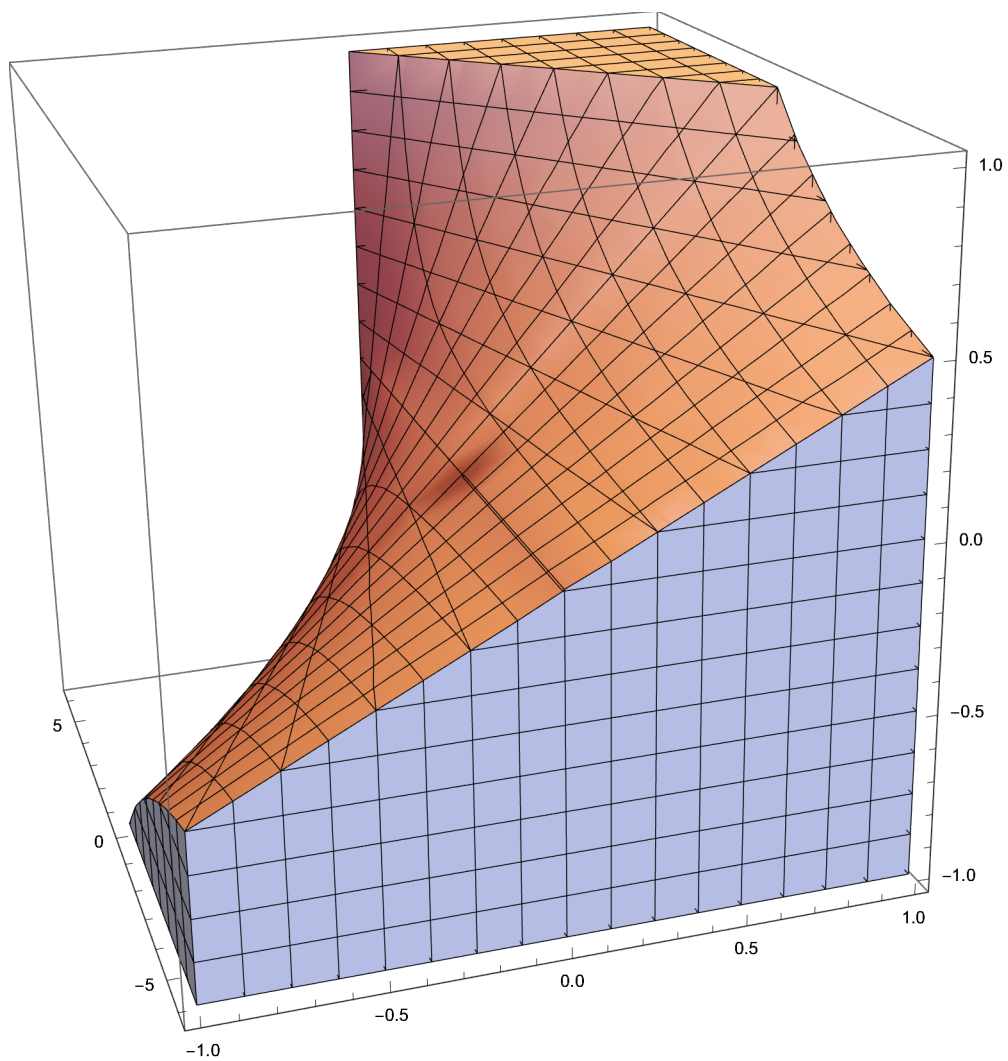


$\text{RegionPlot3D}\left[2\pi r - 2\pi \frac{2\pi r - r\theta}{2\pi} < 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)r,\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -4\pi, 4\pi\}\right]$

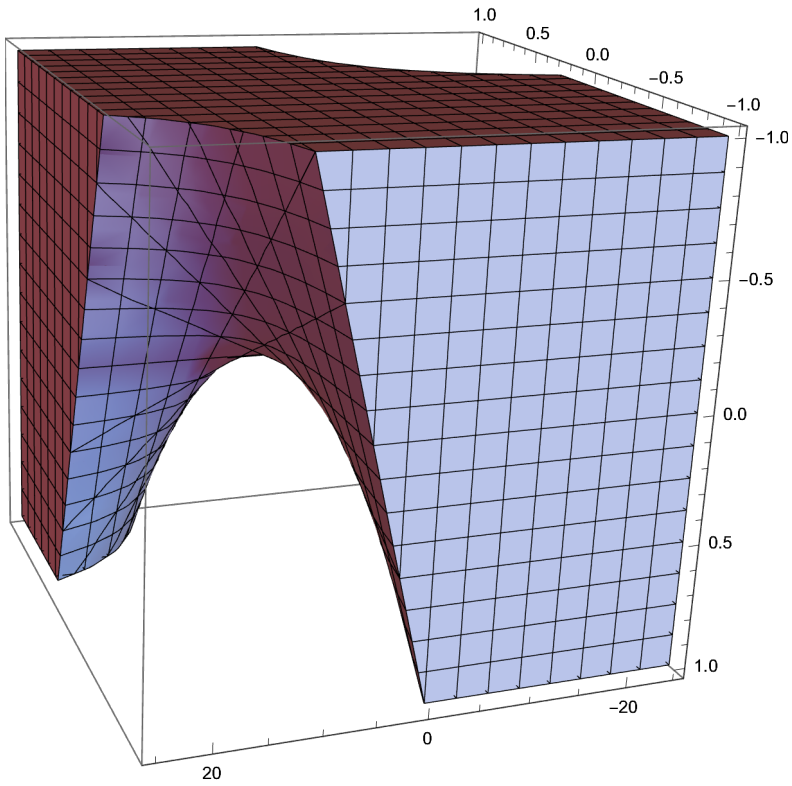


$\text{RegionPlot3D}[2\pi r - 2\pi x < \theta r, \{r, -1, 1\}, \{x, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$





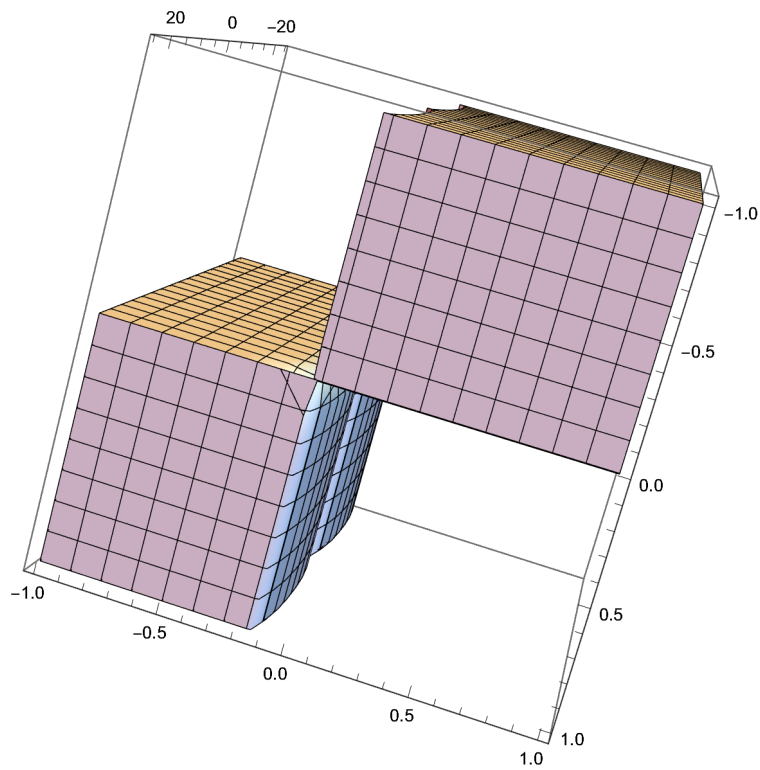
```
RegionPlot3D[ $2\pi r + 2\pi x < \theta r$ , {r, -1, 1}, {x, -1, 1}, { $\theta$ ,  $-8\pi$ ,  $8\pi$ }]
```



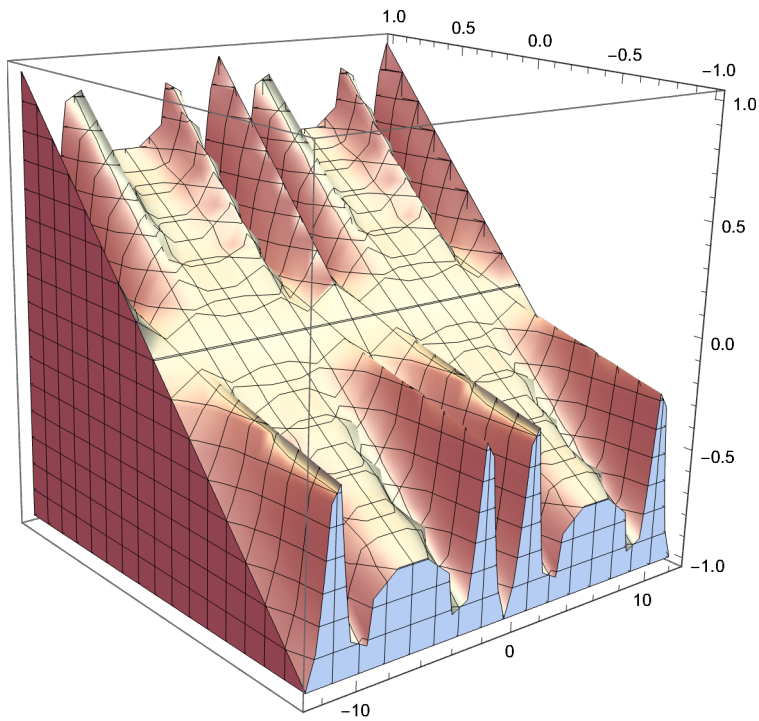
RegionPlot3D[ $2 \pi r +$

$$2 \pi x \left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right. \\ \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) r,$$

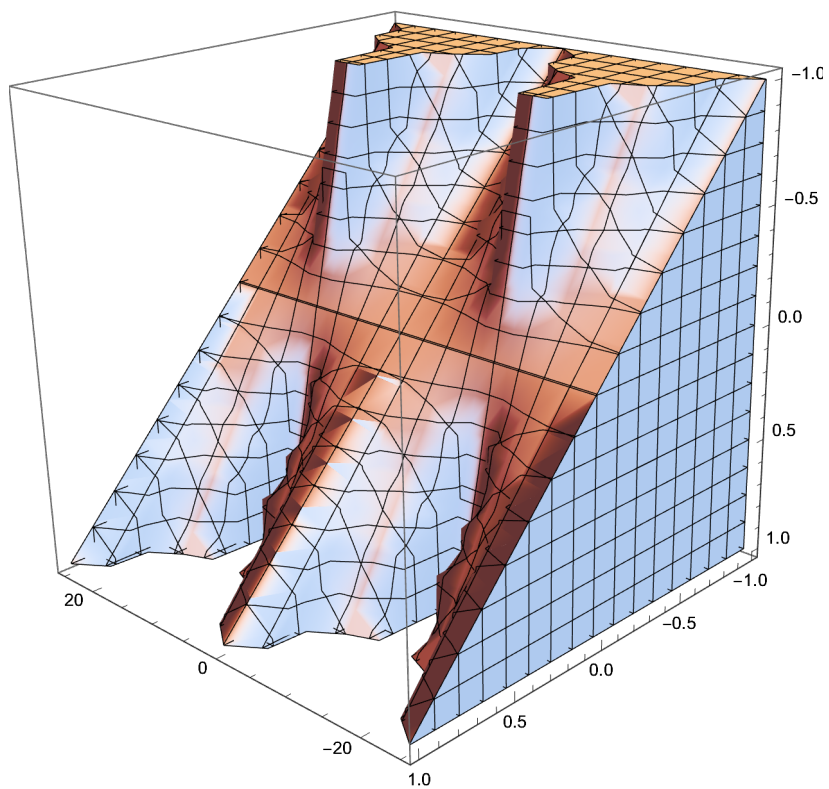
{r, -1, 1}, {x, -1, 1}, {\beta, -8 \pi, 8 \pi}]



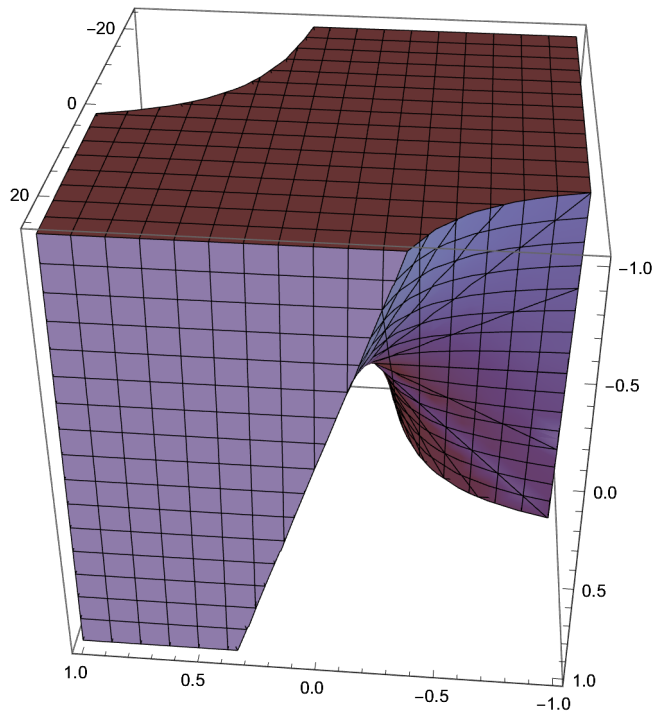
`RegionPlot3D` $\left[2 \pi r+2 \pi x \leq\left(2\left(\pi+\sqrt{\pi^2-\pi^2 \operatorname{Sin}[\beta]^2}\right)\right) r,\right.$   
 $\left.\{r,-1,1\},\{x,-1,1\},\{\beta,-4 \pi, 4 \pi\}\right]$



```
RegionPlot3D[2 π r + 2 π x ≤ (2 (π + √(π² - π² Sin[β]²))) r,
  {r, -1, 1}, {x, -1, 1}, {β, -8 π, 8 π}]
```



`RegionPlot3D[2 π r + 2 π x ≤ θ r, {r, -1, 1}, {x, -1, 1}, {θ, -8 π, 8 π}]`



$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2$$

$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2$$

$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2 = 2\pi \frac{\text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}$$

$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2 = \frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}$$

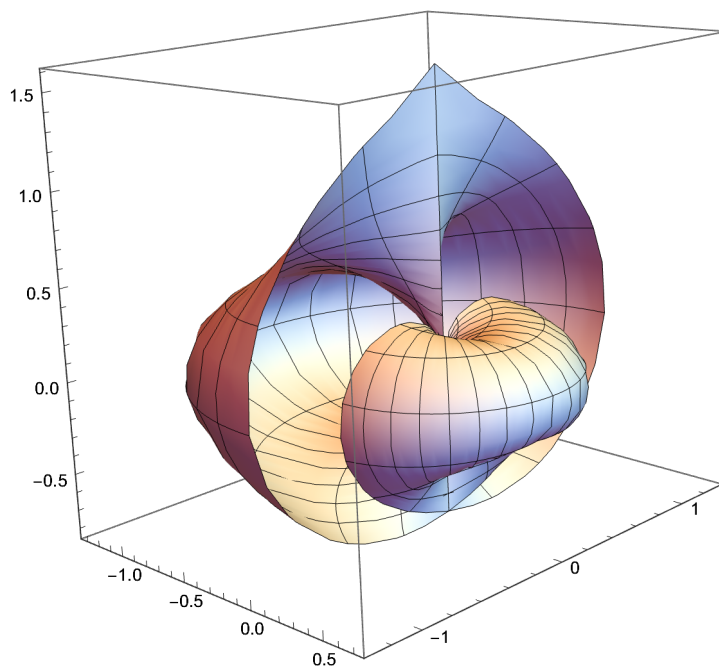
$$\text{Solve}\left[\text{Cos}[\theta]^2 + \text{Sin}[\theta]^2 = \frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \beta\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

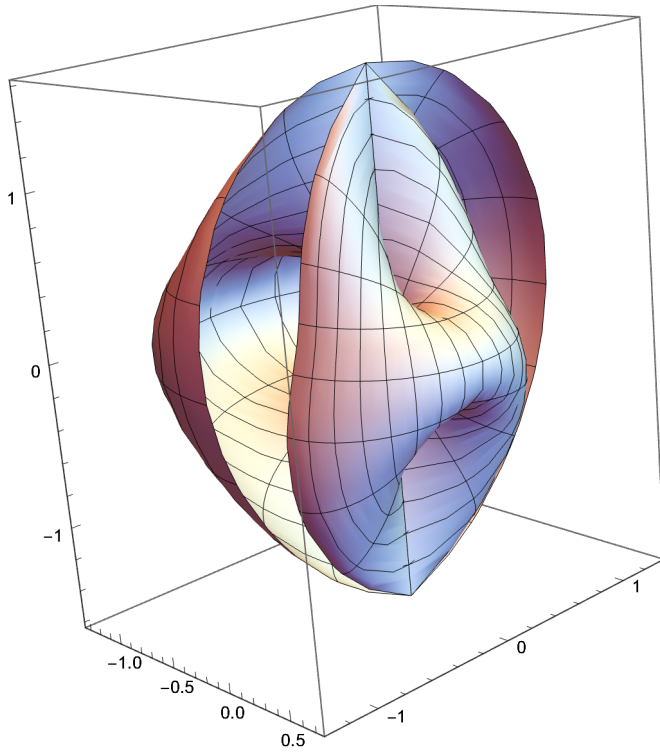
$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta} \text{Cos}[\theta]^2 + \sqrt{(4\pi - \theta)\theta} \text{Sin}[\theta]^2}{2\pi}\right]\right\}\right\}$$

SphericalPlot3D[  

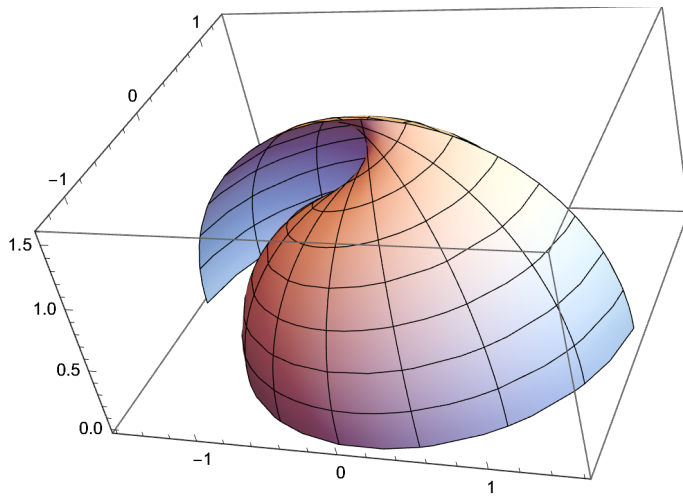
$$\text{ArcSin}\left[\frac{\sqrt{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)} \theta \cos[\theta]^2 + \sqrt{(4\pi - \theta) \theta} \sin[\theta]^2}{2\pi}\right],$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]



`SphericalPlot3D[`  
`ArcSin[ $\frac{1}{2\pi} \left( \sqrt{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))} 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \cos[\theta]^2 + \sqrt{(4\pi - \theta)\theta} \sin[\theta]^2 \right)$ ],  $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]`



`SphericalPlot3D[`  
`ArcSin[ $\frac{1}{2\pi} \left( \sqrt{(4\pi - \theta)\theta} \cos[2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})]^2 + \sqrt{(4\pi - \theta)\theta} \sin[2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})]^2 \right)$ ],  $\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}$ ]`





$$\text{Solve}\left[\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2 = \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \beta\right]$$

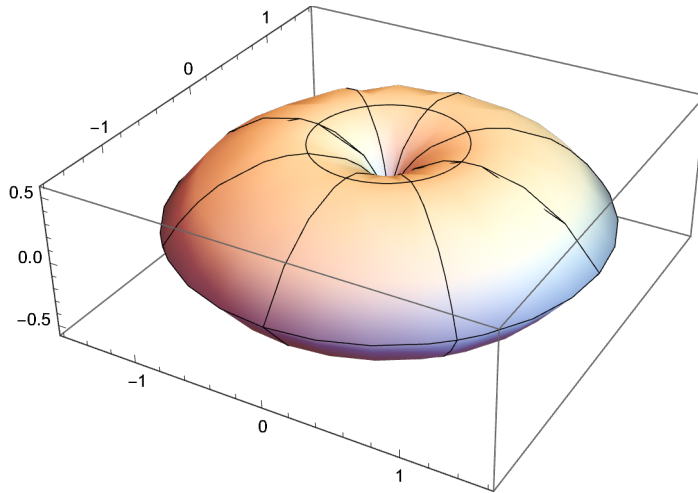
Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta} \text{Cos}[\alpha]^2 + \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\alpha]^2}{2 \pi}\right]\right\}\right\}$$

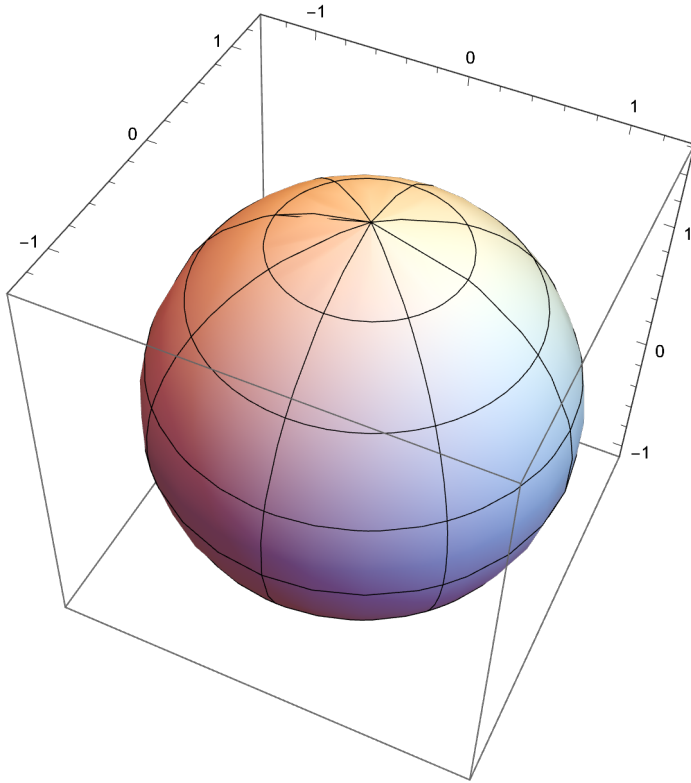
SphericalPlot3D[

$$\text{ArcSin}\left[\frac{1}{2 \pi} \left( \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \text{Cos}[\alpha]^2 + \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \text{Sin}[\alpha]^2}} \right)\right],$$

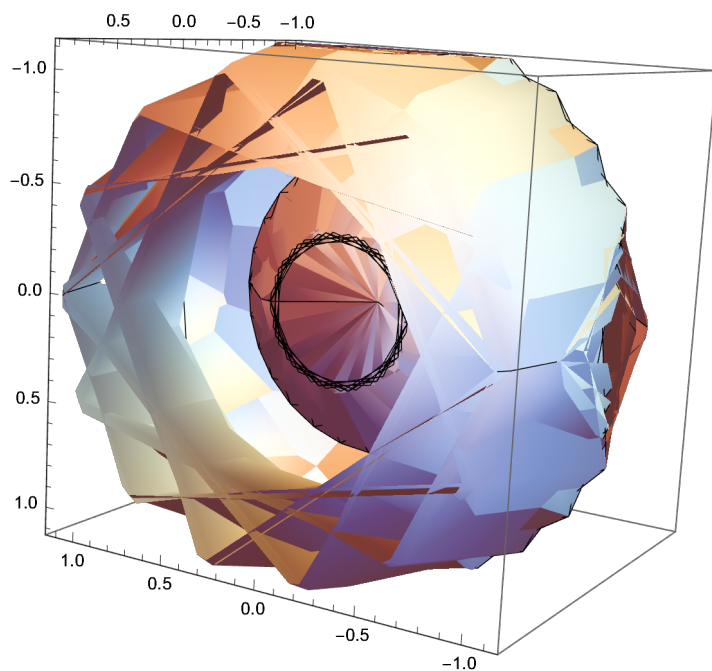
$$\{\beta, -2 \pi, 2 \pi\}, \{\alpha, -2 \pi, 2 \pi\}]$$



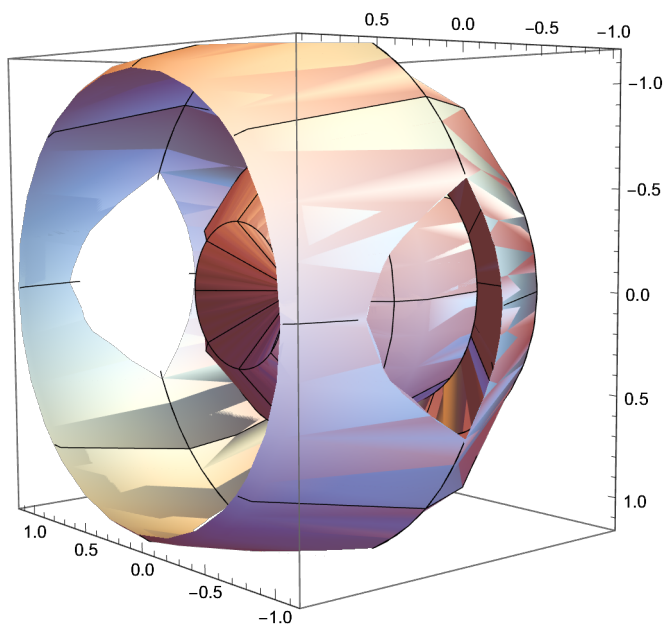
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{1}{2\pi}\left(\sqrt{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2}\right)}\right)}\right.\right.\right. \\ \left.\left.\left.2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2}\right)\right)\cos[\alpha]^2+\right.\right. \\ \left.\left.\sqrt{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2}\right)\right)}\right]^2\right.\right. \\ \left.\left.\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2}\right)\right)\right.\right. \\ \left.\left.\text{Sin}[\alpha]^2\right]\right],\{\theta,-2\pi,2\pi\},\{\alpha,-2\pi,2\pi\}]$$



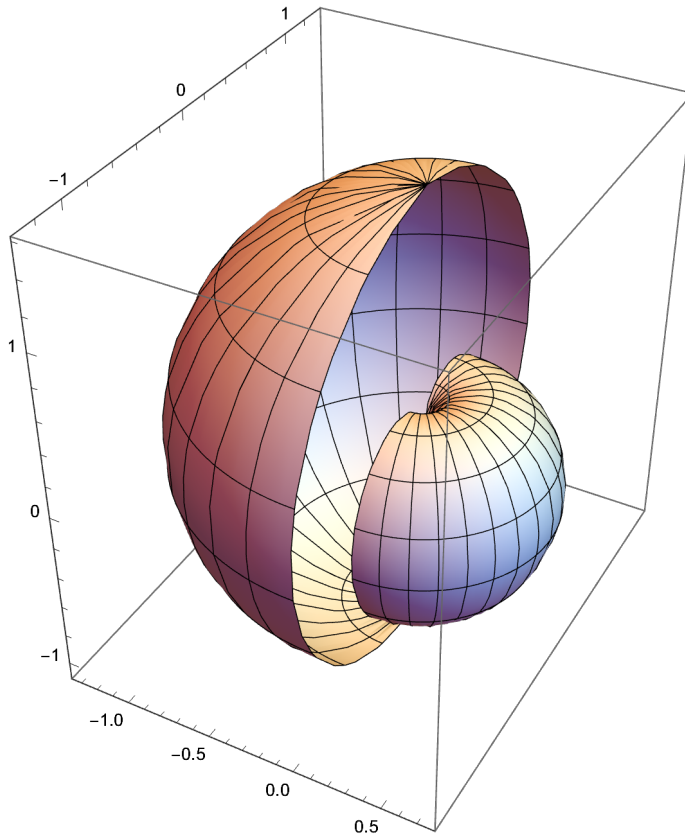
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}\cos[\alpha]^2+\sqrt{(4\pi-\theta)\theta}\sin[\alpha]^2}{2\pi}\right],\right. \\ \left.\{\theta,-16\pi,16\pi\},\{\alpha,-16\pi,16\pi\}\right]$$



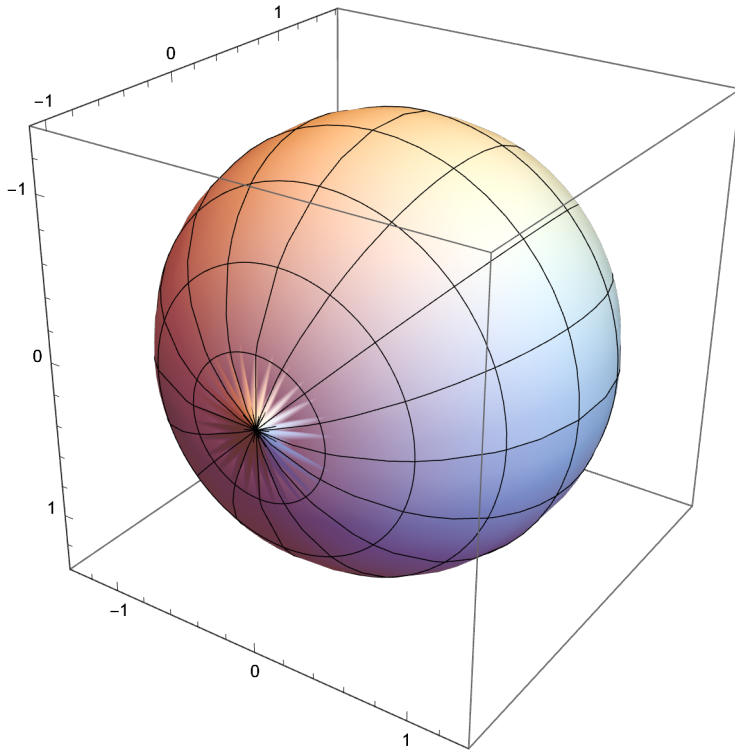
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}\cos[\alpha]^2+\sqrt{(4\pi-\theta)\theta}\sin[\alpha]^2}{2\pi}\right],\right. \\ \left.\{\theta,-16\pi,16\pi\},\{\alpha,-2\pi,2\pi\}\right]$$



`SphericalPlot3D` $\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}\cos[\alpha]^2 + \sqrt{(4\pi - \theta)\theta}\sin[\alpha]^2}{2\pi}\right],\right.$   
 $\left.\{\theta, -2\pi, 2\pi\}, \{\alpha, -\pi/2, \pi/2\}\right]$



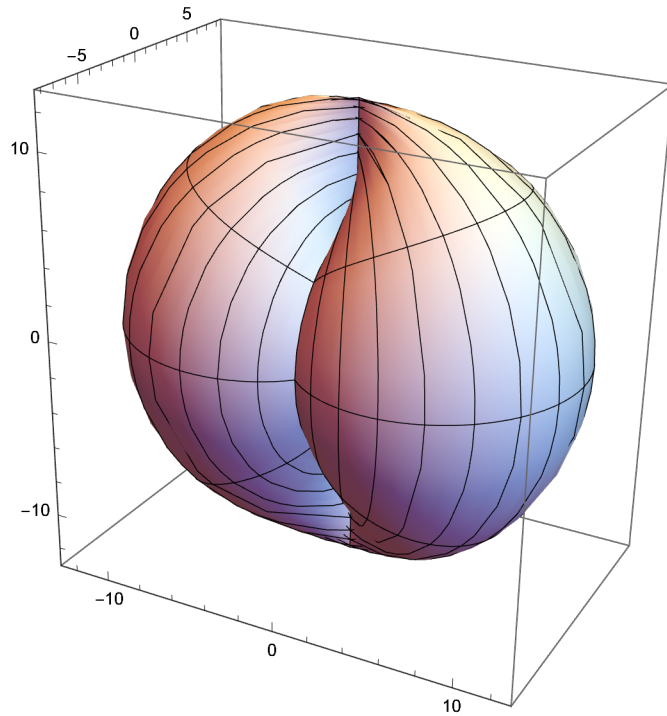
SphericalPlot3D[  
ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}\cos[\alpha]^2 + \sqrt{(4\pi - \theta)\theta}\sin[\alpha]^2}{2\pi}$ ], { $\theta, -2\pi, 2\pi$ }, { $\alpha, -\pi, \pi$ }]



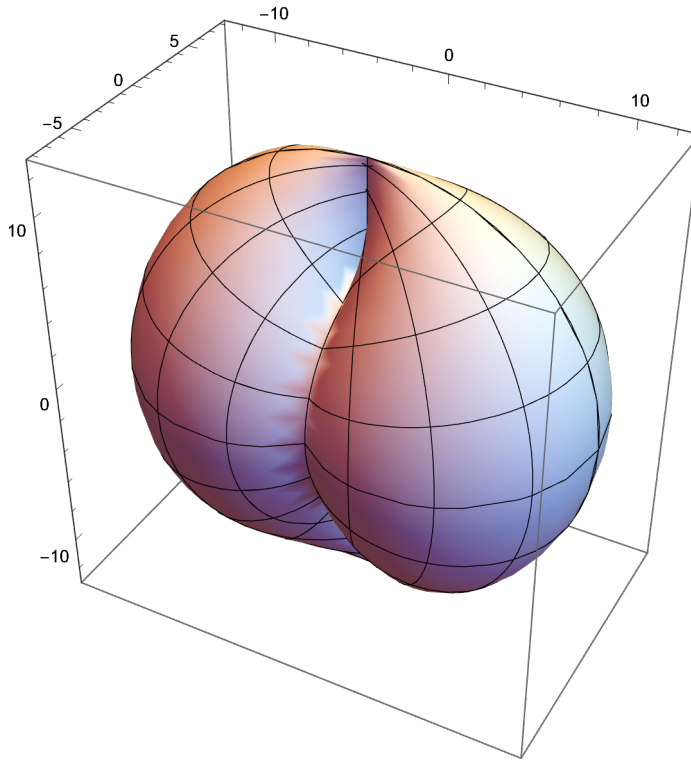
Solve[ $\cos[\alpha]^2 + \sin[\alpha]^2 = \frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}$ ,  $\theta$ ]

{ $\theta \rightarrow \left( 4\pi\cos[\alpha]^4 + 8\pi\cos[\alpha]^2\sin[\alpha]^2 + 4\pi\sin[\alpha]^4 - \sqrt{\left( (-4\pi\cos[\alpha]^4 - 8\pi\cos[\alpha]^2\sin[\alpha]^2 - 4\pi\sin[\alpha]^4)^2 - 16\pi^2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4)\sin[\beta]^2 \right)} \right) / (2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4)) \right)$ ,  
 $\theta \rightarrow \left( 4\pi\cos[\alpha]^4 + 8\pi\cos[\alpha]^2\sin[\alpha]^2 + 4\pi\sin[\alpha]^4 + \sqrt{\left( (-4\pi\cos[\alpha]^4 - 8\pi\cos[\alpha]^2\sin[\alpha]^2 - 4\pi\sin[\alpha]^4)^2 - 16\pi^2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4)\sin[\beta]^2 \right)} \right) / (2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4)) \right)$ }

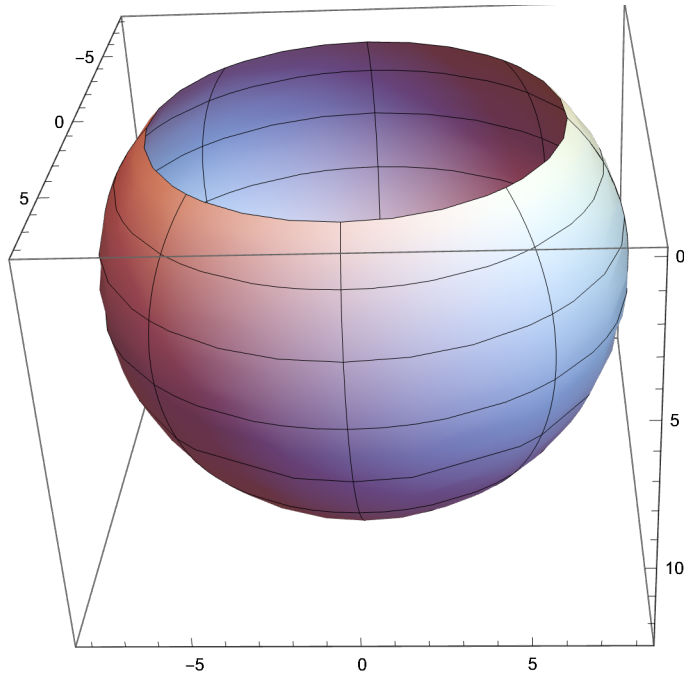
SphericalPlot3D[ $\left(4 \pi \cos[\alpha]^4 + 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 + 4 \pi \sin[\alpha]^4 + \sqrt{\left((-4 \pi \cos[\alpha]^4 - 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 - 4 \pi \sin[\alpha]^4)^2 - 16 \pi^2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4) \sin[\beta]^2\right)}\right) / (2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4))$ ,  $\{\alpha, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}$ ]



`SphericalPlot3D`  $\left[ \left( 4 \pi \cos[\alpha]^4 + 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 + \right. \right.$   
 $\left. \left. 4 \pi \sin[\alpha]^4 + \sqrt{\left( (-4 \pi \cos[\alpha]^4 - 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 - 4 \pi \sin[\alpha]^4)^2 - \right. \right. \right.$   
 $\left. \left. 16 \pi^2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4) \sin[\beta]^2 \right) \right) / \right.$   
 $\left. (2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4)) \right), \{\alpha, -\pi, \pi\}, \{\beta, -\pi, \pi\} \right]$



SphericalPlot3D[ $\left(4 \pi \cos[\alpha]^4 + 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 + 4 \pi \sin[\alpha]^4 + \sqrt{\left((-4 \pi \cos[\alpha]^4 - 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 - 4 \pi \sin[\alpha]^4)^2 - 16 \pi^2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4) \sin[\beta]^2\right)}\right) / (2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4))$ ,  $\{\beta, -\pi/2, \pi/2\}$ ,  $\{\alpha, -2\pi, 2\pi\}$ ]



$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

$$D\left[D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \beta\right]$$

$$- \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \right.$$



$$\begin{aligned}
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \quad \left( 8 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 2 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \Bigg) \\
& \quad \left( \left( 8 \pi \theta \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \\
& \quad \left. \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \quad \left( 2 \theta^2 \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\pi^2 (4\pi - 2\theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4\pi - \theta) \theta}} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \Bigg) \\
& \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 - \\
& \left( 8\pi\theta (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \operatorname{Sin}[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \operatorname{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^3 + \\
& \left( 2\theta^2 (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \operatorname{Sin}[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \operatorname{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^3 + \\
& \left( 4\pi \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 - \\
& \left( 2\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 \Bigg) \Bigg) / \\
& \left( 8\pi \left( \left( 4\pi\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( \theta^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^{3/2} \Bigg) + \\
& \left( \left( 8\pi\theta \left( 2\pi\sqrt{(4\pi-\theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi-\theta} - \right. \right. \right. \\
& \quad \left. \left. \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 - \\
& \left( 2\theta^2 \left( 2\pi\sqrt{(4\pi-\theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi-\theta} - \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 + \\
& \left( 8\pi\theta \left( \frac{\pi(4\pi-2\theta)\cos[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{3\pi^2(4\pi-2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi-2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi-\theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( \frac{\pi (4 \pi - 2 \theta) \operatorname{Cos}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{(4 \pi - \theta)^2} + \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \quad \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2) \right. \\
& \quad \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \quad \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \quad \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 24 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^4 - \\
& \left( 6 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^4 - \\
& \left( 128 \pi^3 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 32 \pi^2 \theta^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 - \\
& \left( 8 \pi \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 \Bigg/ \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) \Bigg)
\end{aligned}$$

SphericalPlot3D[

$$\begin{aligned}
& - \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 2\theta^2(-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 \right) \\
& \left( \left( 8\pi\theta \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \right. \\
& \quad \left. \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \left. \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 -
\end{aligned}$$



$$\begin{aligned}
& \left( 8 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \quad \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 2 \theta^2 \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \quad \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 4 \pi \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Big) \Big) / \\
& \left( 8 \pi \left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right) \Big) /
\end{aligned}$$

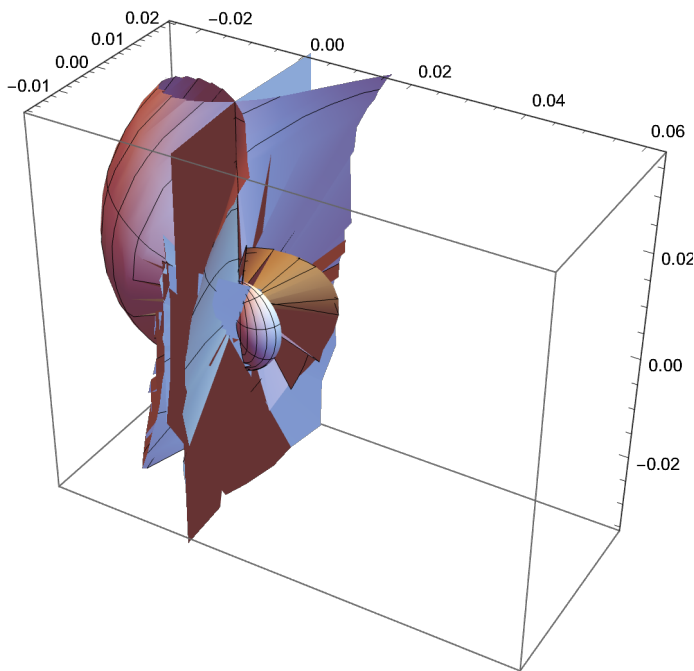
$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^{3/2} \Bigg) + \\
& \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& \left( 8 \pi \theta \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \\
& \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 16 \pi \theta (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 16 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 24 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 6 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 128 \pi^3 \theta \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 32 \pi^2 \theta^2 \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 - \\
& \left( 8 \pi (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left. \left. \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \right) \right) \right) / \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \right. \\
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left. \left. \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) \right) \right), \\
& \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \right. \\
& \left. - \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 2 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 \Bigg) \\
& \left( \left( 8 \pi \theta \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\pi^2 (4\pi - 2\theta) \sin[\beta]^3}{\theta \sqrt{(4\pi - \theta) \theta}} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{(4\pi - \theta)^2} + \\
& \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta) \sin[\beta]}{\sqrt{(4\pi - \theta) \theta}} - \frac{\pi^2 (4\pi - 2\theta) \sin[\beta]^3}{(4\pi - \theta) \sqrt{(4\pi - \theta) \theta}} - \right. \right. \\
& \left. \frac{\pi^2 (4\pi - 2\theta) \sin[\beta]^3}{\theta \sqrt{(4\pi - \theta) \theta}} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{(4\pi - \theta)^2} + \right. \\
& \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 8\pi\theta (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \left. \left. \pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 2\theta^2 (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \left. \left. \pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4\pi \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 -
\end{aligned}$$



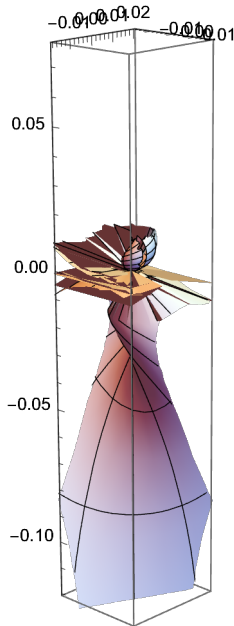
$$\begin{aligned}
& \left( 2 \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg) / \\
& \left( 8 \pi \left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg)^{3/2} \Bigg) + \\
& \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& \left( 8\pi\theta \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 16\pi\theta(16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2\sin[\beta]^2) \right. \\
& \quad \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \right. \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 +
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 16 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) /
\end{aligned}$$

$$\begin{aligned}
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 24 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 6 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 128 \pi^3 \theta \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 +
\end{aligned}$$

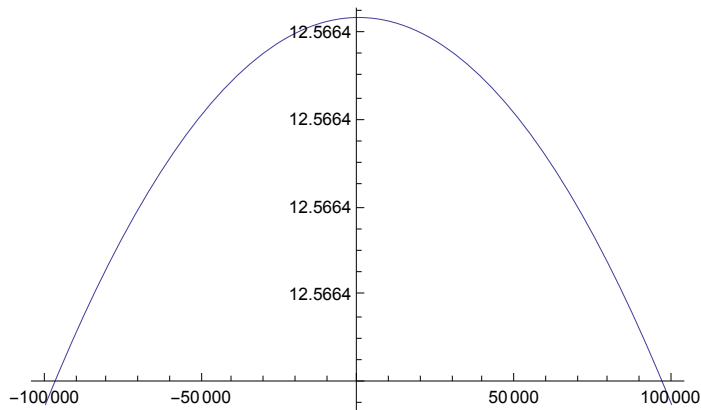
$$\begin{aligned}
& \left( 32 \pi^2 \theta^2 \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 - \\
& \left( 8 \pi (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \Big) / \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \right. \\
& \quad \left. \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left. \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) \right) \Big), \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 -
\end{aligned}$$

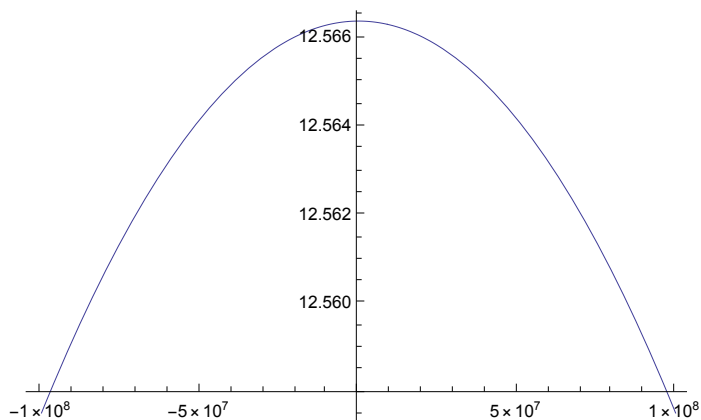


$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \theta\right]$$

$$\left\{\left\{\theta \rightarrow \left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 - 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1. \cdot 10^{18} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right)\right\}, \left\{\theta \rightarrow \left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 + 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1. \cdot 10^{18} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right)\right\}\right\}$$

$$\text{Plot}\left[\left(0.5 \cdot \left(2.697911582835683 \cdot r^{41} + 7.60372795068286 \cdot r^{22} + 1.4322774071693905 \cdot r^{32} \sqrt{3.548143227025099 \cdot r^{18} + 1 \cdot r^2}\right)\right) / \left(2.1469298221658919 \cdot r^{40} + 6.050854446385924 \cdot r^{21}\right), \{r, -1 \cdot 10^5, 1 \cdot 10^5\}\right]$$

$$\text{Plot}\left[\left(0.5 \cdot \left(2.697911582835683 \cdot r^{41} + 7.60372795068286 \cdot r^{22} + 1.4322774071693905 \cdot r^{32} \sqrt{3.548143227025099 \cdot r^{18} + 1 \cdot r^2}\right)\right) / \left(2.1469298221658919 \cdot r^{40} + 6.050854446385924 \cdot r^{21}\right), \{r, -1 \cdot 10^5, 1 \cdot 10^5\}\right]$$


$$\text{Plot}\left[\left(0.5 \cdot \left(2.697911582835683 \cdot r^{41} + 7.60372795068286 \cdot r^{22} + 1.4322774071693905 \cdot r^{32} \sqrt{3.548143227025099 \cdot r^{18} + 1 \cdot r^2}\right)\right) / \left(2.1469298221658919 \cdot r^{40} + 6.050854446385924 \cdot r^{21}\right), \{r, -1 \cdot 10^8, 1 \cdot 10^8\}\right]$$


Solve[

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), r]$$

$$\left\{ \left\{ r \rightarrow - \frac{1. \sqrt{2.69791 \times 10^{41} - 2.14693 \times 10^{40} \theta} \sqrt{\theta}}{\sqrt{2.38878 \times 10^{23} - 7.60373 \times 10^{22} \theta + 6.05085 \times 10^{21} \theta^2}} \right\}, \right.$$

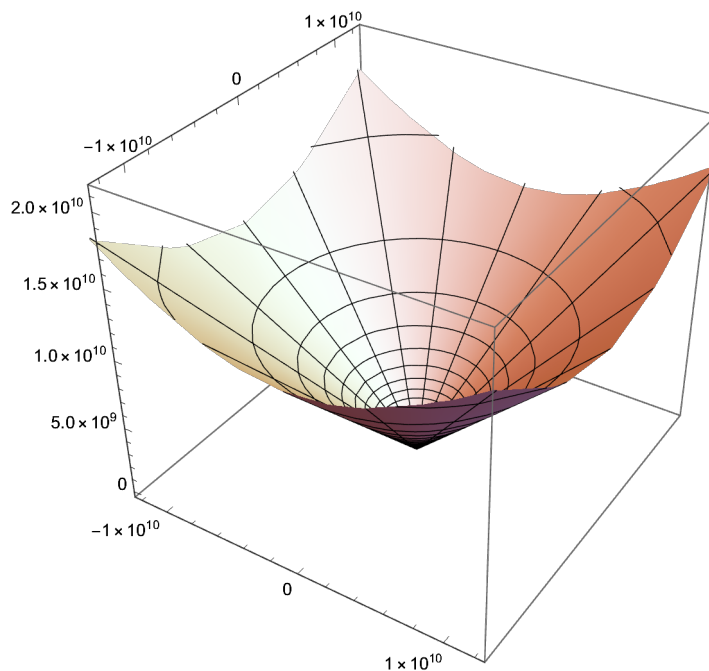
$$\left. \left\{ r \rightarrow \frac{\sqrt{2.69791 \times 10^{41} - 2.14693 \times 10^{40} \theta} \sqrt{\theta}}{\sqrt{2.38878 \times 10^{23} - 7.60373 \times 10^{22} \theta + 6.05085 \times 10^{21} \theta^2}} \right\} \right\}$$

$$\text{RevolutionPlot3D} \left[ \left\{ - \left( 1. \sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta} \right) / \right. \right.$$

$$\left. \left( \sqrt{2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2} \right) \right\},$$

$$\left( \sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta} \right) /$$

$$\left( \sqrt{2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2} \right) \right\}, \{\theta, -2 \pi, 2 \pi\}]$$

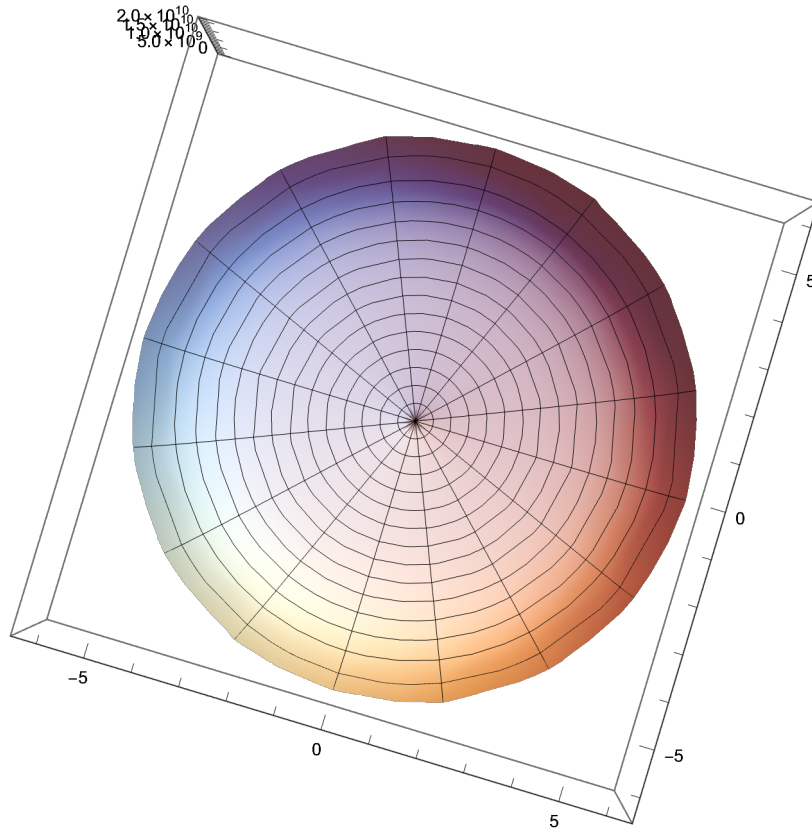




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RevolutionPlot3D[ (  $\sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta}$  ) /  

  (  $\sqrt{2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2}$  ) ),  

  { $\theta$ , -2  $\pi$ , 2  $\pi$ } ]
```



$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

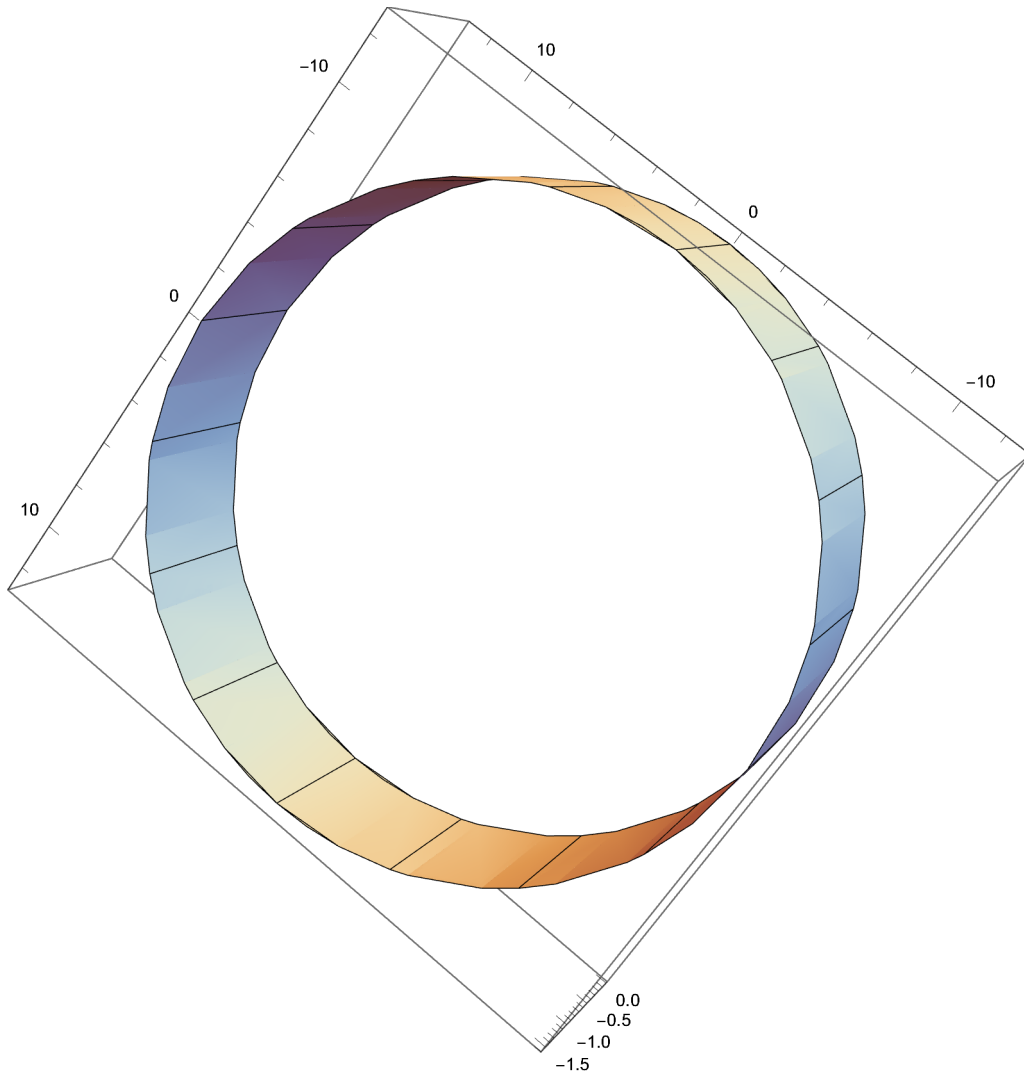
$$\frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Solve}\left[\left(\sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta}\right) / \left(\sqrt{\left(2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2\right)}\right) == \left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / \left(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right), \beta\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[2.05971 \times 10^{-25} \left(7.72706 \times 10^{23} \sqrt{12.5664 \theta - 1. \theta^2} - \frac{2.41639 \times 10^8 \sqrt{12.5664 \theta - 1. \theta^2}}{12.5664 - 1. \theta} - \frac{1.14922 \times 10^{35} \sqrt{\theta} \sqrt{12.5664 \theta - 1. \theta^2}}{\sqrt{12.5664 - 1. \theta} \sqrt{39.4784 - 12.5664 \theta + \theta^2}} + \frac{1.82905 \times 10^{34} \sqrt{12.5664 - 1. \theta} \sqrt{\theta} \sqrt{12.5664 \theta - 1. \theta^2}}{\sqrt{39.4784 - 12.5664 \theta + \theta^2}} + \frac{2.91102 \times 10^{33} \sqrt{\theta} \sqrt{12.5664 \theta - 1. \theta^2} \sqrt{39.4784 - 12.5664 \theta + \theta^2}}{\sqrt{12.5664 - 1. \theta}}\right)\right]\right\}}$$

$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[2.0597093504953005 \cdot 10^{-25} \left(7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 - 1. \theta} - \frac{\left(1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2}\right)}{\left(\sqrt{12.566370614359172 - 1. \theta} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2}\right)} + \frac{\left(1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 - 1. \theta} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2}\right)}{\left(\sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2}\right)} + \frac{\left(2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2}\right)}{\left(\sqrt{12.566370614359172 - 1. \theta}\right)}\right]\right], \{\beta, -4 \pi, 8 \pi / 2\}]$$



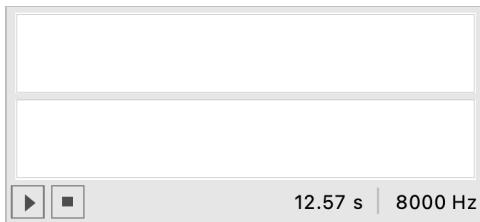
$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[1000 \beta]^2} \right)$$

$$\theta := \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}$$

Play[ArcSin[

$$\begin{aligned}
 & 2.0597093504953005 \cdot 10^{-25} \left( 7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \right. \\
 & \quad \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 \theta - 1. \theta} \\
 & \quad \left. \left( 1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \right. \\
 & \quad \left( \sqrt{12.566370614359172 \theta - 1. \theta} \sqrt{39.47841760435743 \theta - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \quad \left. \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{39.47841760435743 \theta - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 & \quad \quad \left. \sqrt{39.47841760435743 \theta - 12.56637061435917 \theta + \theta^2} \right) / \\
 & \quad \left. \left( \sqrt{12.566370614359172 \theta - 1. \theta} \right) \right] \Bigg], \{\beta, -2\pi, 2\pi\}
 \end{aligned}$$

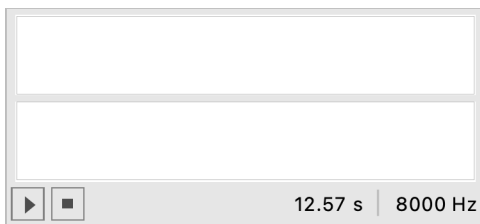
Sound::ssnm: A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>



Play[ArcSin[

$$\begin{aligned}
 & 2.0597093504953005 \cdot 10^{-25} \left( 7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \right. \\
 & \quad \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 \theta - 1. \theta} \\
 & \quad \left. \left( 1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \right. \\
 & \quad \left( \sqrt{12.566370614359172 \theta - 1. \theta} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \quad \left. \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 & \quad \quad \left. \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) / \\
 & \quad \left. \left( \sqrt{12.566370614359172 \theta - 1. \theta} \right) \right] \Bigg], \{\beta, -2\pi, 2\pi\}
 \end{aligned}$$

Sound::ssnm: A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>



"ribbit.wav"

Export["ribbit.wav",

Play[ $\sqrt{12.566370614359172 \sin[1000 \theta] - 1. \cos[1000 \theta]^2}$ , { $\beta$ ,  $-\pi$ ,  $\pi$ }]]

Sound::ssnm: A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>

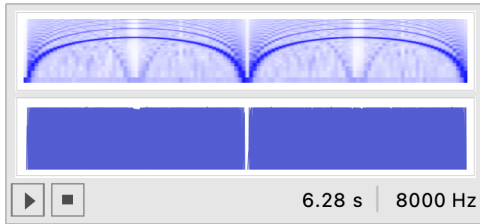
LinkObject::linkw: Unable to write data to closed link LinkObject[

/Applications/Mathematica.app/SystemFiles/Converters/Binaries/MacOSX-x86-64/Audio.exe, 25, 9]. >>

\$Failed

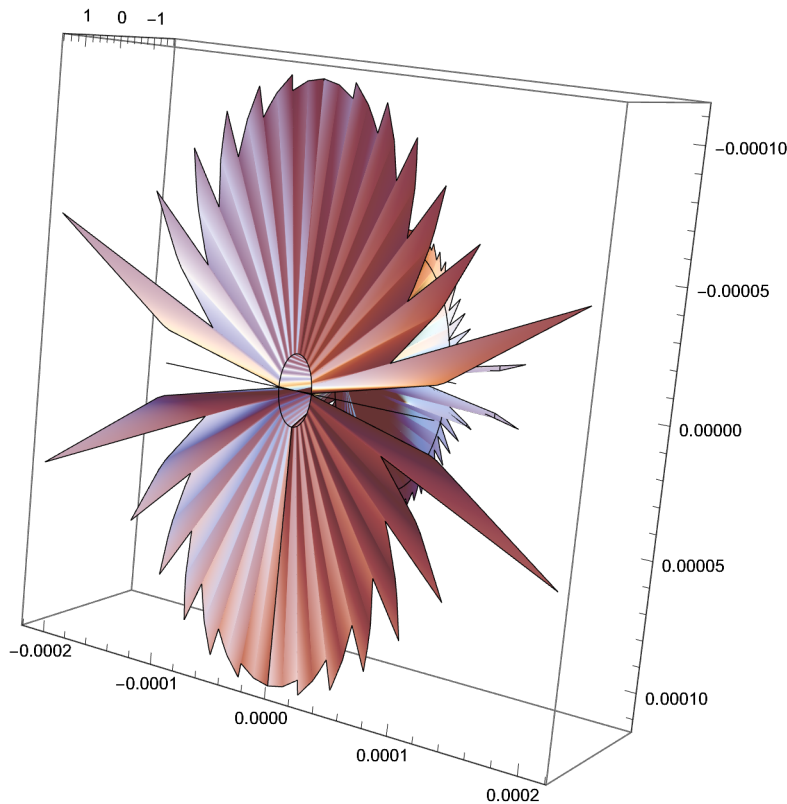
```
Play[ $\sqrt{12.566370614359172 \sin[1000 \theta] - 1. \cos[1000 \theta]^2}$ , { $\beta$ ,  $-\pi$ ,  $\pi$ }]
```

Sound::ssnm : A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>



RevolutionPlot3D[ArcSin[

$$\begin{aligned}
 & 2.0597093504953005 \cdot 10^{-25} \left( 7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \right. \\
 & \quad \left. \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \left( 1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{12.566370614359172 \theta - 1. \theta} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \left. \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 & \quad \left. \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) / \\
 & \quad \left. \left( \sqrt{12.566370614359172 \theta - 1. \theta} \right) \right], \{\theta, -2\pi, 2\pi\}
 \end{aligned}$$

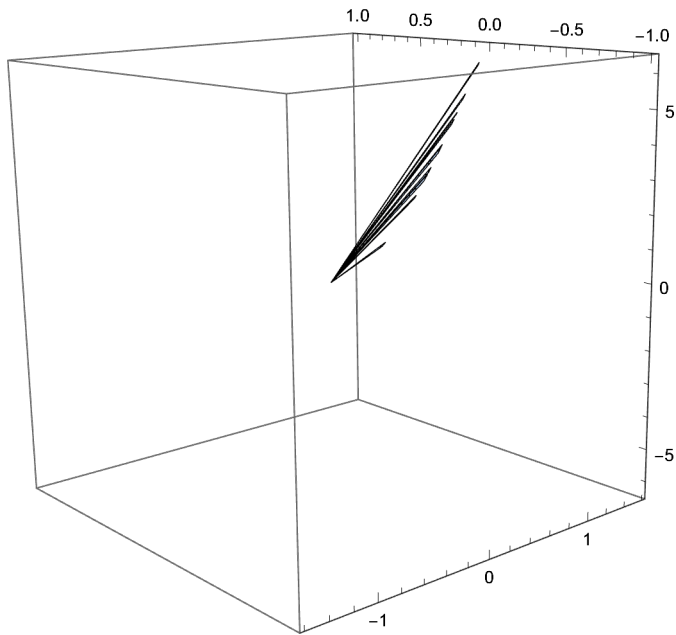


ContourPlot3D[

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) ==$$

$$\sqrt{(- (256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})) ,$$

{ $\theta$ ,  $-2\pi$ ,  $2\pi$ }, { $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }, { $\eta$ ,  $-1$ ,  $1$ }]





Export["r=r.3ds", ContourPlot3D[

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) ==$$

$$\sqrt{(- (256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})) ,$$

$$\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}, \{\eta, -1, 1\}]]$$

r=r.3ds

$$\text{Solve}\left[\frac{2\pi(2\pi r - 2\pi\sqrt{r^2 - (\eta)^2})}{\theta^2} == \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}, \eta\right]$$

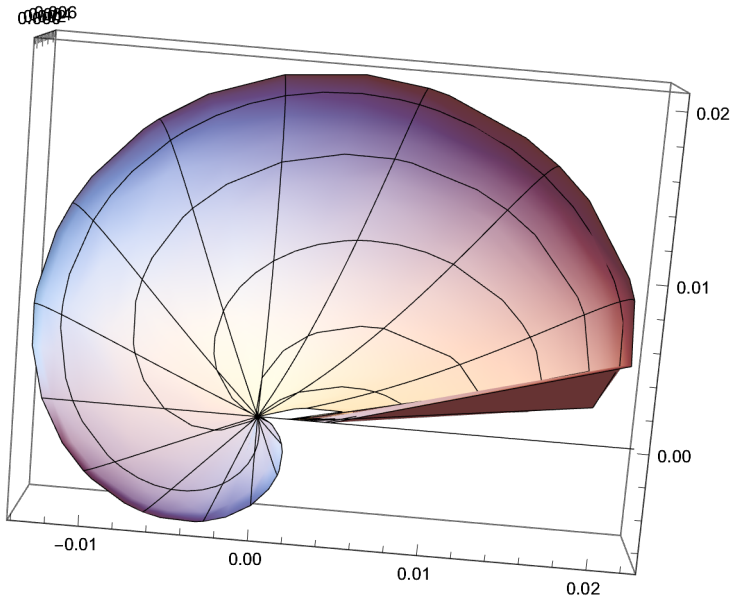
$$\left\{ \left\{ \eta \rightarrow -\frac{1}{4\pi^2} \left( \sqrt{64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi-\theta} + 16\pi^3 r^2\theta + 4\pi^2 r^2\theta^2 + r^2\theta^4 + 16\pi^3 r\sqrt{r^2(4\pi-\theta)\theta} - \frac{64\pi^4 r\sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta} + 8\pi^2 r\theta\sqrt{r^2(4\pi-\theta)\theta}} \right) \right\} \right\},$$

$$\left\{ \eta \rightarrow \frac{1}{4\pi^2} \left( \sqrt{64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi-\theta} + 16\pi^3 r^2\theta + 4\pi^2 r^2\theta^2 + r^2\theta^4 + 16\pi^3 r\sqrt{r^2(4\pi-\theta)\theta} - \frac{64\pi^4 r\sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta} + 8\pi^2 r\theta\sqrt{r^2(4\pi-\theta)\theta}} \right) \right\}$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

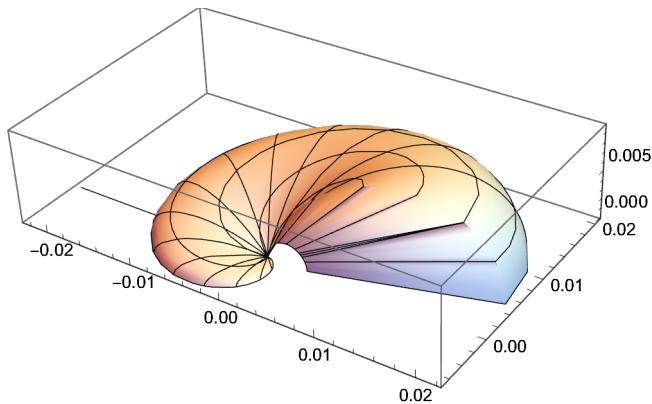
SphericalPlot3D[

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$



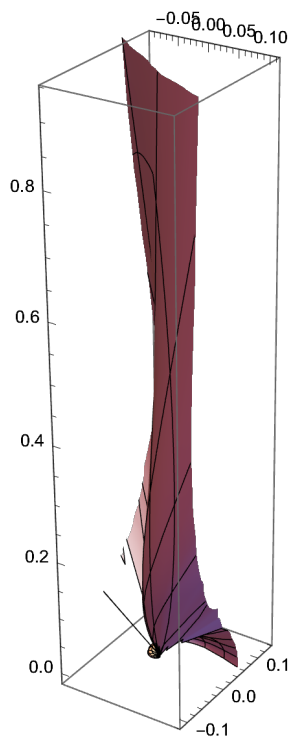
SphericalPlot3D[

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$

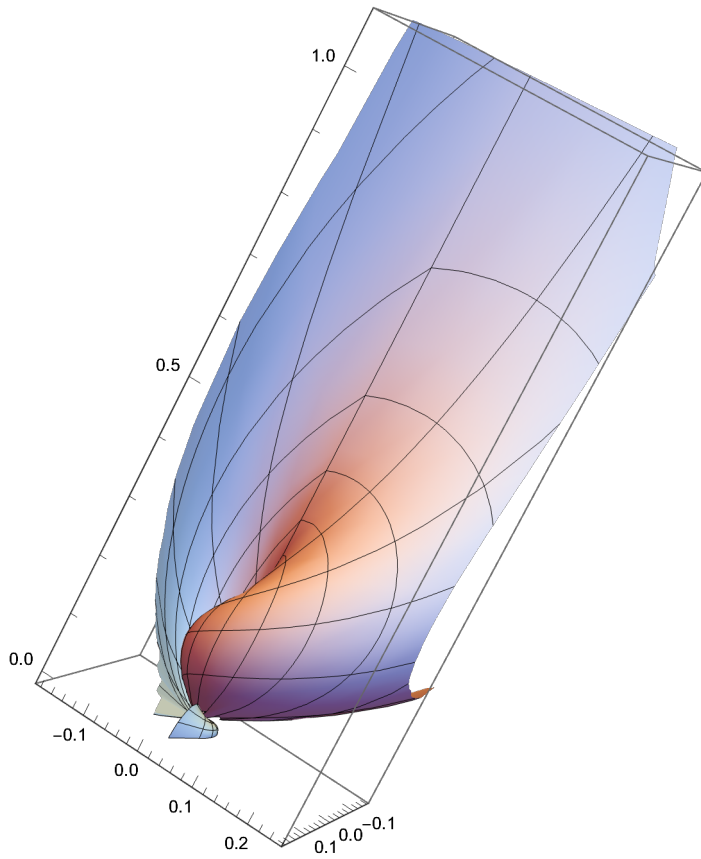


SphericalPlot3D[

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r^2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \sqrt{r^2 \left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \theta \right)} \right)} \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



$\text{SphericalPlot3D}\left[\frac{1}{4\pi^2}\left(\sqrt{\left(64\pi^4r^2-\frac{256\pi^5r^2}{4\pi-\theta}+16\pi^3r^2\theta+4\pi^2r^2\theta^2+r^2\theta^4+\right.}\right.\right.$   
 $\left.\left.16\pi^3r\sqrt{r^2\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\theta}-\frac{64\pi^4r\sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta}+\right.}\right.$   
 $\left.\left.8\pi^2r^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\sqrt{r^2\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\theta}\right)\right],$   
 $\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$



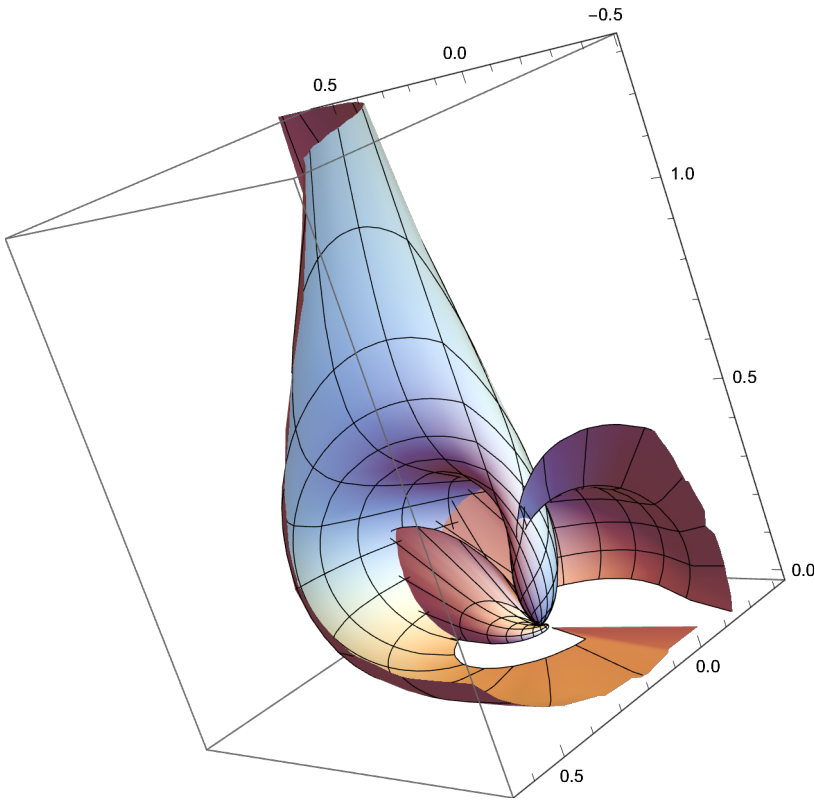
SphericalPlot3D[  

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + \right.} \right.$$

$$16\pi^3 r \sqrt{r^2 \left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} +$$

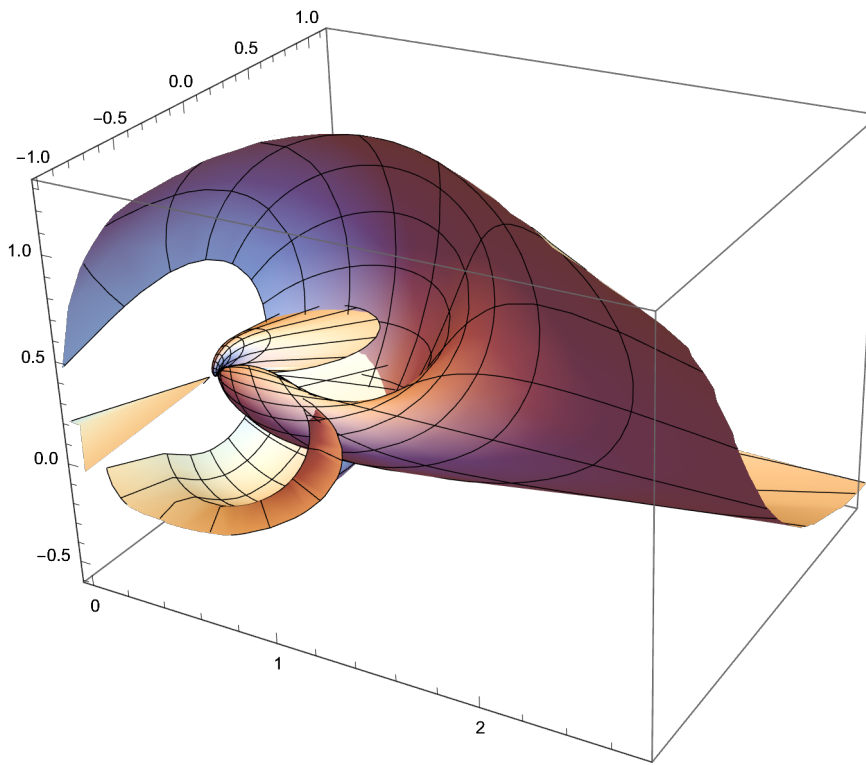
$$\left. \left. 8\pi^2 r 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \sqrt{r^2 \left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} \right) \right),$$

$$\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



SphericalPlot3D[

$$\frac{1}{4 \pi^2} \left( \sqrt{\left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 4 \pi^2 r^2 \theta^2 + r^2 \right.} \right. \\ \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 + 16 \pi^3 r \sqrt{r^2 \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} - \right. \\ \left. \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right. \\ \left. \left. \sqrt{r^2 \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} \right) \right], \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



q

$$\text{Solve}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right) / \right. \\ \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \sqrt{-(256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})} + \right. \\ \left. (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})\right), \eta]$$

General::ivar : 1 is not a valid variable. >>

General::ivar : 1 is not a valid variable. >>

$$\text{Solve}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right) / \right. \\ \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \sqrt{-(256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})} + \right. \\ \left. (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - \right. \\ \left. (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})\right), \{\eta, -1, 1\}]$$

ContourPlot3D[

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) ==$$

$$\sqrt{(- (256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})) , \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}, \{\eta, -1, 1\}]$$

$$\iint \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} d\theta d\beta == D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right], \beta]$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

$$D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right], \beta]$$

$$- \left( \left( \left( 8\pi\theta \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \left( 2\theta^2 \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right) \right)$$



$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \quad \left( 8\pi\theta (-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \quad \left( 2\theta^2 (-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 \Bigg) \\
& \quad \left( \left( 8\pi\theta \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \right. \\
& \quad \left. \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) \Bigg) \Bigg/ \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \quad \left( 2\theta^2 \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \left. \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 - \\
& \left( 8\pi\theta (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^3 + \\
& \left( 2\theta^2 (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^3 + \\
& \left( 4\pi \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 - \\
& \left( 2\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 \Big) / \\
& \left( 8\pi \left( \left( 4\pi\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 - \\
& \left. \left( \theta^2 \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^{3/2} \Bigg) + \\
& \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& \left( 8 \pi \theta \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} +
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2 \right)^2 - \\
& \left( 16\pi\theta \left( 16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2 \right) \right. \\
& \left( 2\pi \sqrt{(4\pi - \theta)\theta} \cos[\beta] + 8\pi^2 \cos[\beta] \sin[\beta] - \right. \\
& \left. \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \\
& \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \\
& \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2 \right)^3 + \\
& \left( 4\theta^2 \left( 16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2 \right) \left( 2\pi \sqrt{(4\pi - \theta)\theta} \cos[\beta] + 8\pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \\
& \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \\
& \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2 \right)^3 + \\
& \left( 8\pi \left( 2\pi \sqrt{(4\pi - \theta)\theta} \cos[\beta] + 8\pi^2 \cos[\beta] \sin[\beta] - \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{4\pi - \theta} - \right. \right. \\
& \left. \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2 \right)^2 - \\
& \left( 4\theta \left( 2\pi \sqrt{(4\pi - \theta)\theta} \cos[\beta] + 8\pi^2 \cos[\beta] \sin[\beta] - \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{4\pi - \theta} - \right. \right. \\
& \left. \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 24 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^4 - \\
& \left( 6 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 - \\
& \left( 128\pi^3\theta\cos[\beta]\sin[\beta] \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 32\pi^2\theta^2\cos[\beta]\sin[\beta] \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 - \\
& \left( 8\pi(-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 4\theta(-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 \Bigg/ \\
& \left( 4\pi\sqrt{\left( \left( 4\pi\theta \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) \Bigg)
\end{aligned}$$

SphericalPlot3D[

$$\begin{aligned}
& - \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 2 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 \Bigg) \\
& \left( \left( 8 \pi \theta \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 +
\end{aligned}$$



$$\begin{aligned}
& \left( 2 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \quad \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 4 \pi \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \quad \left( 2 \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big) / \\
& \quad \left( 8 \pi \left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \right. \\
& \quad \left. \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right)^{3/2} \Big) + \\
& \quad \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right) \right)
\end{aligned}$$

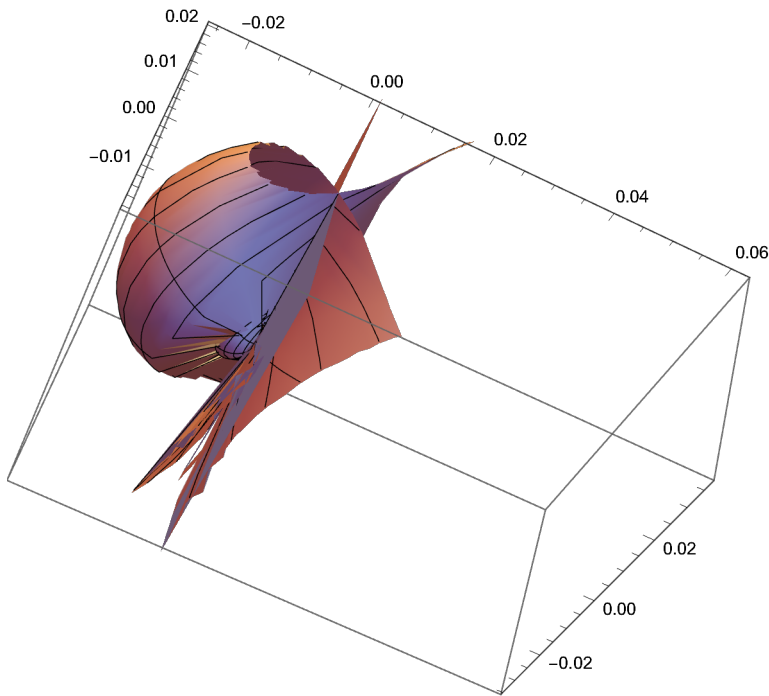
$$\begin{aligned}
& \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& \left( 8\pi\theta \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \right. \\
& \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 4 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 24 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \quad (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \quad \left( 6 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right.
\end{aligned}$$

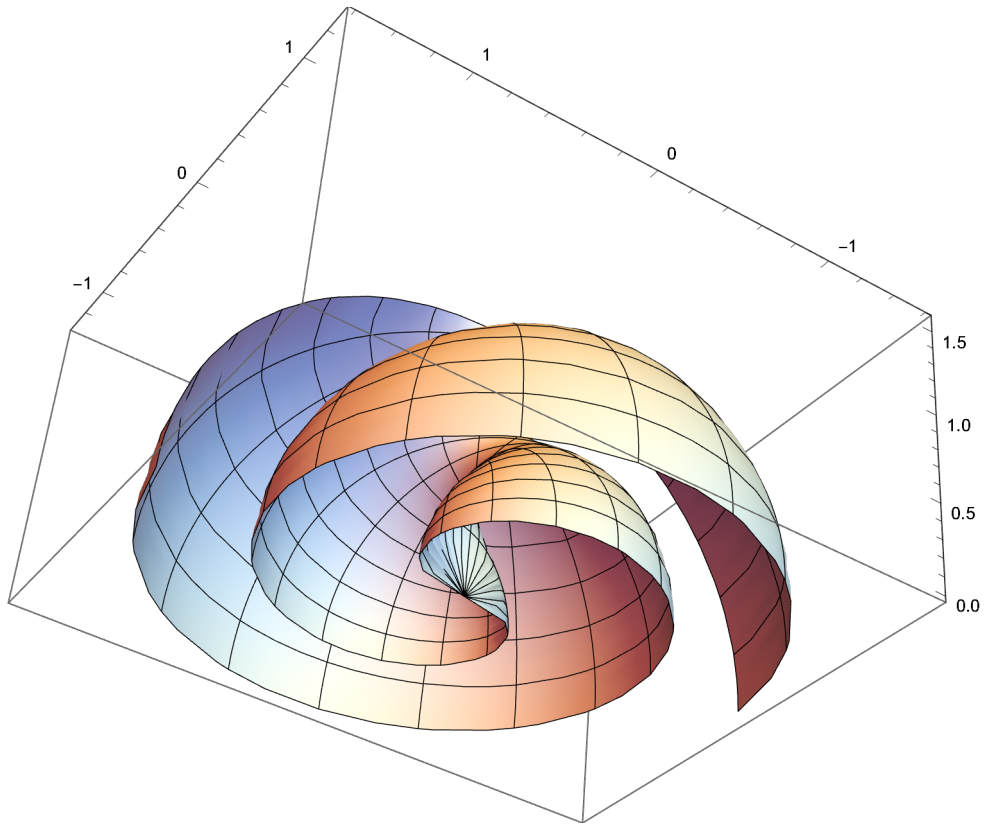
$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 128 \pi^3 \theta \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 32 \pi^2 \theta^2 \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 - \\
& \left( 8 \pi (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \Bigg/ \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
 & \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \right. \\
 & \left. \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
 & \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
 & \left. \left. \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) \right) \right), \\
 & \left\{ \theta, -2 \pi, 2 \pi \right\}, \left\{ \beta, -\pi / 2, \pi / 2 \right\} \Big]
 \end{aligned}$$

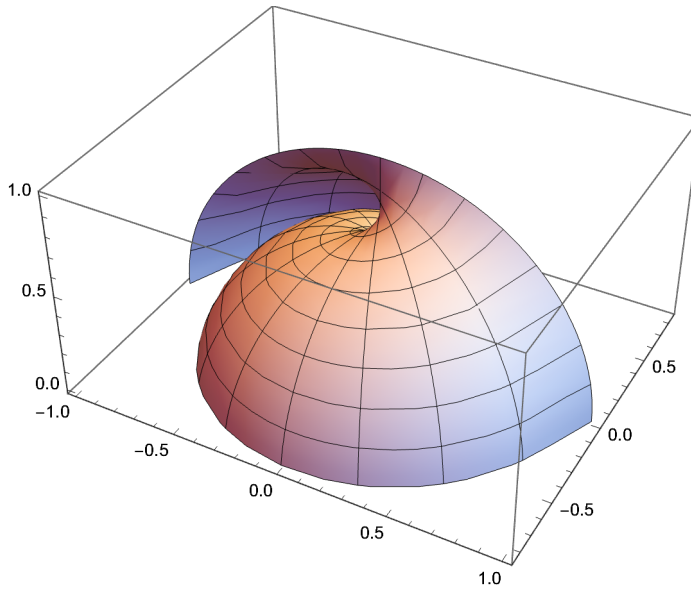


$$\left( \frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}} \right) \frac{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}{4 \pi}$$

$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{1}{2\pi}\left(\sqrt{(4\pi-\theta)\theta}\cos\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2+\sqrt{(4\pi-\theta)\theta}\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2\right)\right],\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$$



SphericalPlot3D $\left[\left(\frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}}\right)^{\frac{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4 \pi}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}\right]$

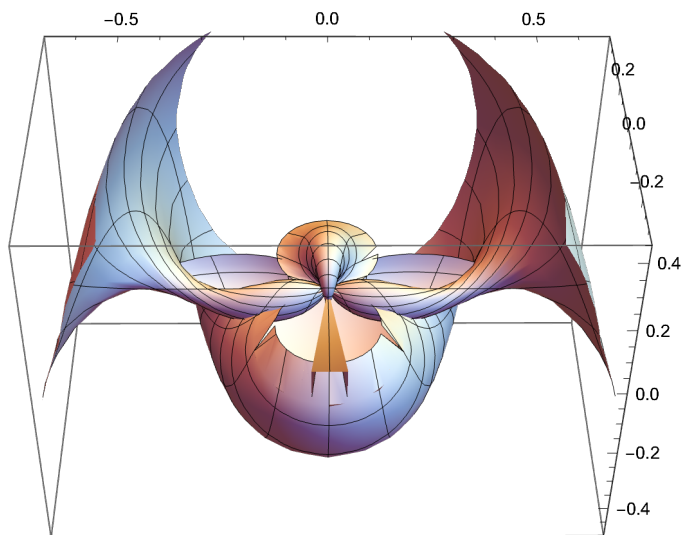


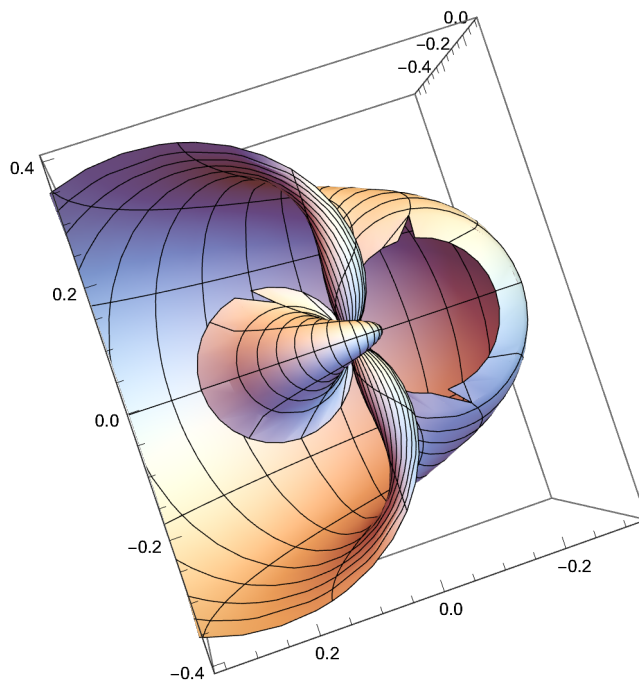
Solve $\left[\left(\frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}}\right)^{\frac{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4 \pi}} == \right.$   
 $\text{ArcSin}\left[\frac{1}{2 \pi} \left(\sqrt{(4 \pi - \theta) \theta} \cos\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 + \right.\right.$   
 $\left.\left.\sqrt{(4 \pi - \theta) \theta} \sin\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2\right)\right], \beta\right]$

Solve::tdep : The equations appear to involve the variables to be solved for in an essentially non-algebraic way. >>

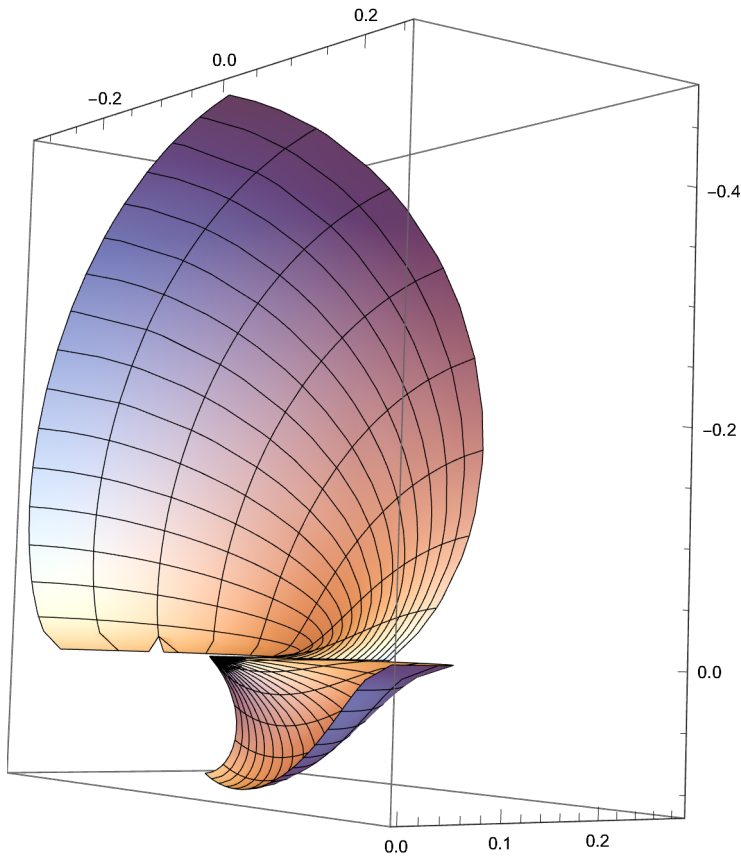
Solve $\left[\left(\frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}}\right)^{\frac{\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}}{2 \pi}} == \text{ArcSin}\left[\frac{1}{2 \pi} \left(\sqrt{(4 \pi - \theta) \theta} \cos\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 + \right.\right.\right.$   
 $\left.\left.\left.\sqrt{(4 \pi - \theta) \theta} \sin\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2\right)\right], \beta\right]$



$$\text{SphericalPlot3D}\left[\frac{\theta (2 \pi r^2 - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta)} \theta}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$$


$$\text{SphericalPlot3D}\left[\frac{\theta (2 \pi r^2 - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta)} \theta}, \{\beta, -\pi, \pi\}, \{\theta, -\pi, \pi\}\right]$$


SphericalPlot3D $\left[\frac{\theta (2 \pi r^2 - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -\pi/2, \pi/2\}\right]$



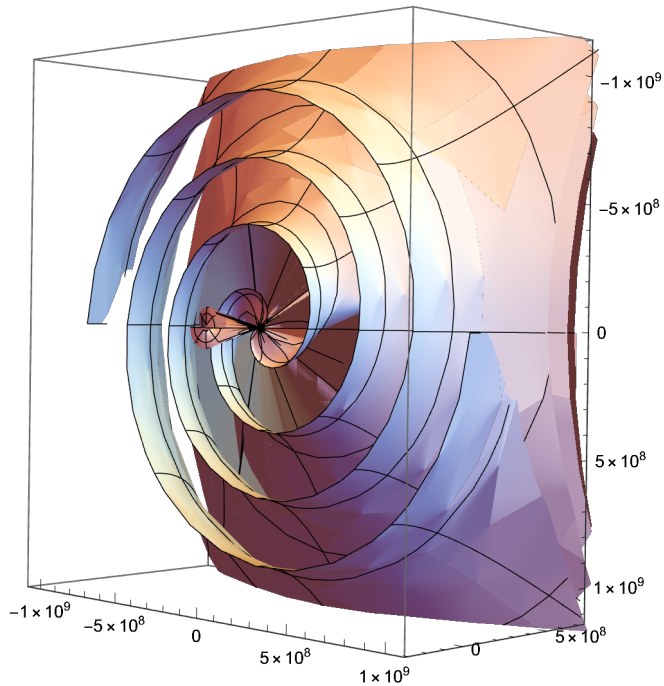
Solve[

$$1 - r \sin[\beta] / \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \theta r - \left(2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right), v]$$

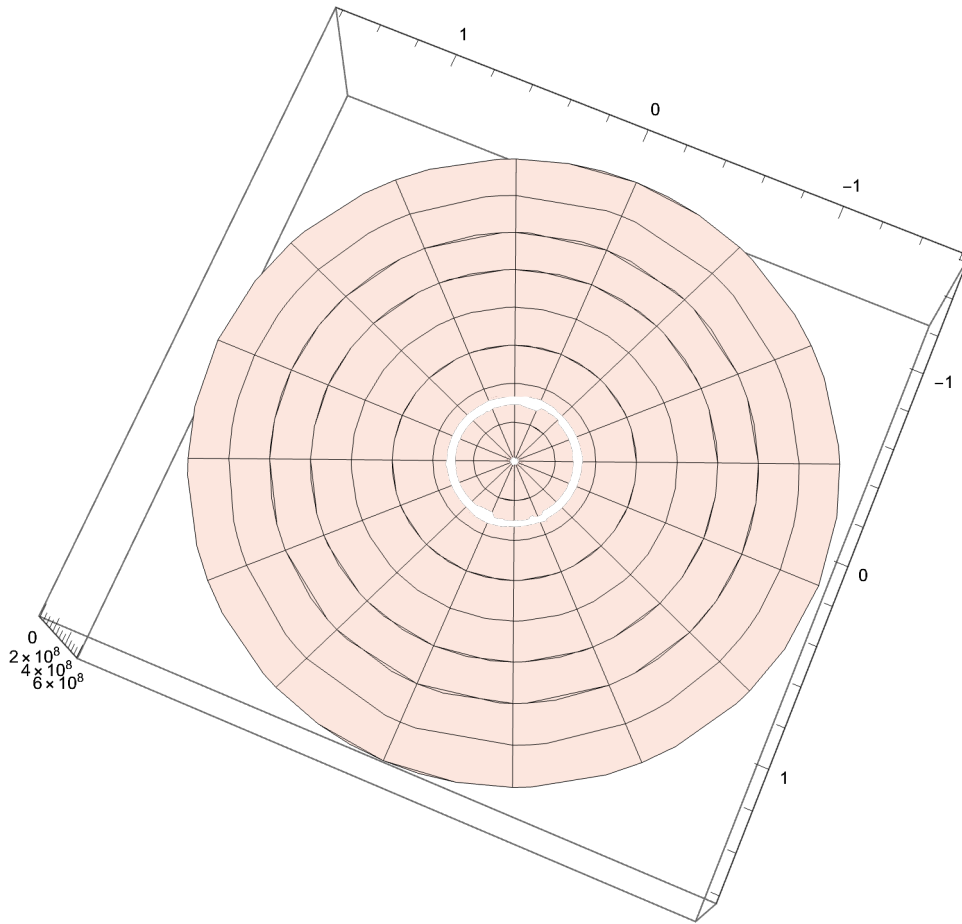
$$\left\{ \left\{ v \rightarrow -\frac{1. \sqrt{-6.91664 \times 10^{33} \theta + 5.50409 \times 10^{32} \theta^2 + 2.17293 \times 10^{34} \sin[\beta]^2}}{\sqrt{-7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-6.91664 \times 10^{33} \theta + 5.50409 \times 10^{32} \theta^2 + 2.17293 \times 10^{34} \sin[\beta]^2}}{\sqrt{-7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2}} \right\} \right\}$$

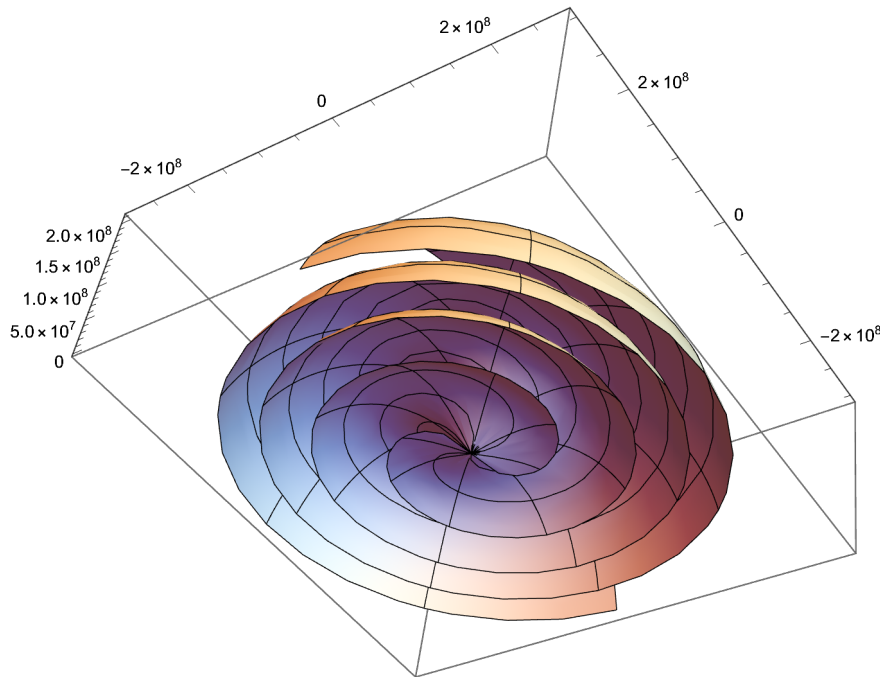
$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left(\sqrt{\left(-6.916640561054567 \cdot 10^{33} \theta + \right. \right. \right. \\
& \quad \left. \left. 5.504087674408673 \cdot 10^{32} \theta^2 + 2.1729267174130213 \cdot 10^{34} \sin[\beta]^2\right)\right)} \Bigg/ \\
& \left(\sqrt{\left(-7.695800507960096 \cdot 10^{16} \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) \Bigg/ \right. \right. \\
& \quad \left. \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
& \quad \left. 6.124123459454841 \cdot 10^{15} \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) \Bigg/ \right. \\
& \quad \left. \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2 + \right. \\
& \quad \left. \left. 2.4177070339300032 \cdot 10^{17} \sin[\beta]^2\right)\right)}, \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]
\end{aligned}$$



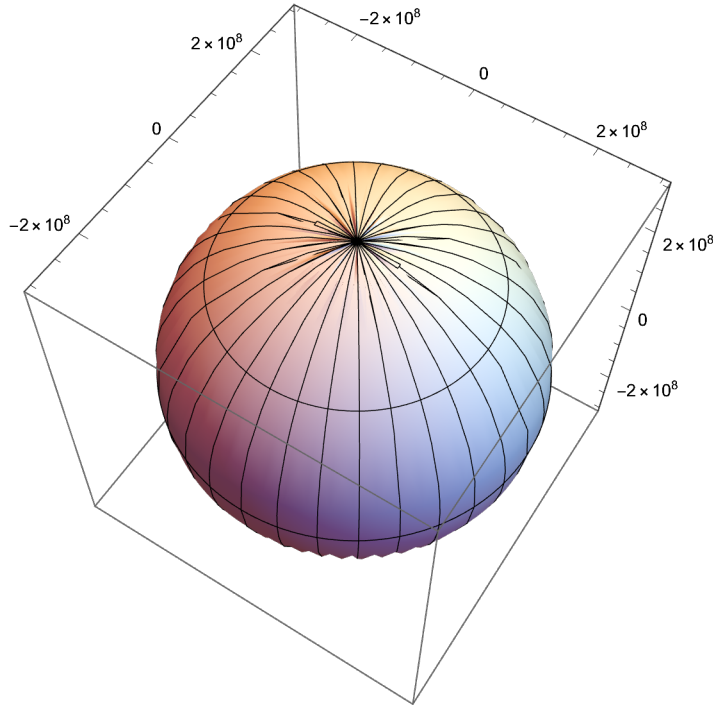
$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\sqrt{\left(-6.916640561054567 \cdot 10^{33} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \right. \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. 5.504087674408673 \cdot 10^{32} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. \left. 2.1729267174130213 \cdot 10^{34} \sin[\beta]^2\right)\right) / \\
& \left(\sqrt{\left(-7.695800507960096 \cdot 10^{16} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \right. \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. 6.124123459454841 \cdot 10^{15} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left. \left. 2.4177070339300032 \cdot 10^{17} \sin[\beta]^2\right)\right), \{\beta, -\pi/2, \pi/2\}]
\end{aligned}$$



`SphericalPlot3D` $\left[\left(\sqrt{\left(-6.916640561054567 \cdot 10^{33} \theta + 5.504087674408673 \cdot 10^{32} \theta^2 + 2.1729267174130213 \cdot 10^{34} \sin[\beta]^2\right)}\right) / \left(\sqrt{\left(-7.695800507960096 \cdot 10^{16} \theta + 6.124123459454841 \cdot 10^{15} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 2.4177070339300032 \cdot 10^{17} \sin[\beta]^2\right)}\right)\right], \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]$



```
SphericalPlot3D[( $\sqrt{(-6.916640561054567 \cdot \theta + 5.504087674408673 \cdot \theta^2 + 2.1729267174130213 \cdot \sin[\beta]^2)}$ )/
( $\sqrt{(-7.695800507960096 \cdot \theta + 6.124123459454841 \cdot \theta^2 + 2.4177070339300032 \cdot \sin[\beta]^2)}$ ), { $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi/2$ ,  $\pi/2$ }]
```



$$\text{Solve}\left[1 - r \sin[\beta] / \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \theta r - \left(2 \pi r - 2 \pi \sqrt{\left(r^2 - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right), r\right]$$

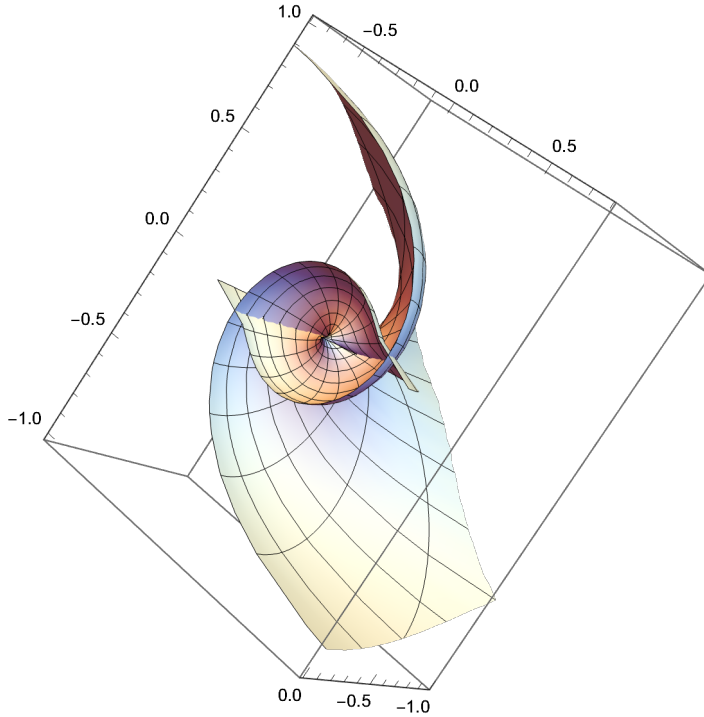
Solve::verif : Potential solution { $r \rightarrow 0$ } (possibly discarded by verifier) should be checked by hand. May require use of limits. >>

Solve::verif : Potential solution { $r \rightarrow \text{ComplexInfinity}$ } (possibly discarded by verifier) should be checked by hand. May require use of limits. >>

$$\left\{\left\{r \rightarrow \frac{\left(8 \pi^2 \theta - 6 \pi \theta^2 + \theta^3 - 2 \sqrt{16 \pi^5 \theta \sin[\beta]^2 - 20 \pi^4 \theta^2 \sin[\beta]^2 + 8 \pi^3 \theta^3 \sin[\beta]^2 - \pi^2 \theta^4 \sin[\beta]^2}\right)}{2 \left(-16 \pi^3 \theta + 20 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4\right)}\right\}, \left\{r \rightarrow \frac{\left(8 \pi^2 \theta - 6 \pi \theta^2 + \theta^3 + 2 \sqrt{16 \pi^5 \theta \sin[\beta]^2 - 20 \pi^4 \theta^2 \sin[\beta]^2 + 8 \pi^3 \theta^3 \sin[\beta]^2 - \pi^2 \theta^4 \sin[\beta]^2}\right)}{2 \left(-16 \pi^3 \theta + 20 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4\right)}\right\}\right\}$$

SphericalPlot3D[  

$$\left( \frac{8 \pi^2 \theta - 6 \pi \theta^2 + \theta^3 + 2 \sqrt{16 \pi^5 \theta \sin[\beta]^2 - 20 \pi^4 \theta^2 \sin[\beta]^2 + 8 \pi^3 \theta^3 \sin[\beta]^2 - \pi^2 \theta^4 \sin[\beta]^2}}{2 (-16 \pi^3 \theta + 20 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



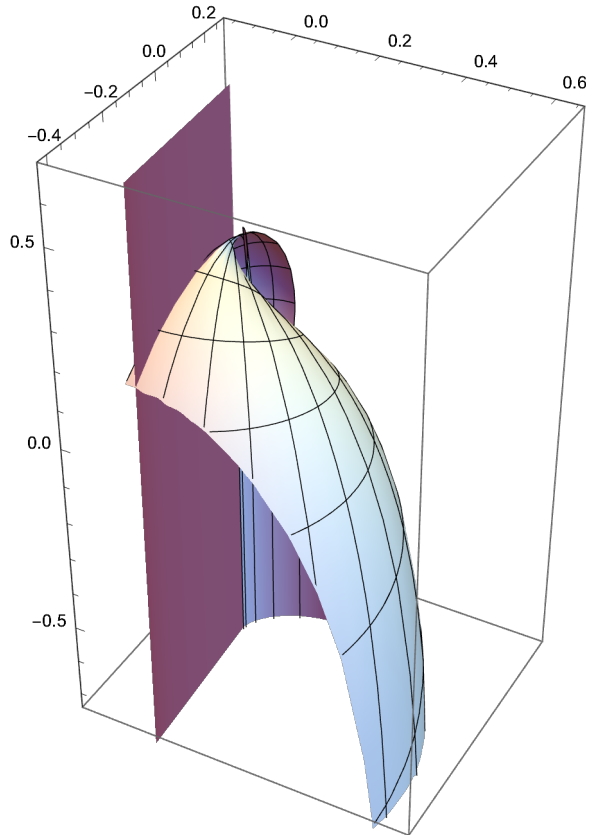
c := 2.99792458 \* (10^8)

Solve[ $1 - \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} == \theta r - \left( 2 \pi r - 2 \pi \sqrt{\left( r^2 - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2} \right), r]$

$\left\{ \left\{ r \rightarrow \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right\} \right\}$

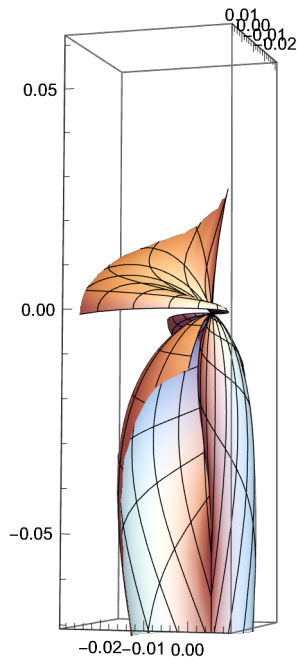


$$\text{SphericalPlot3D}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \frac{4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}}{(16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$

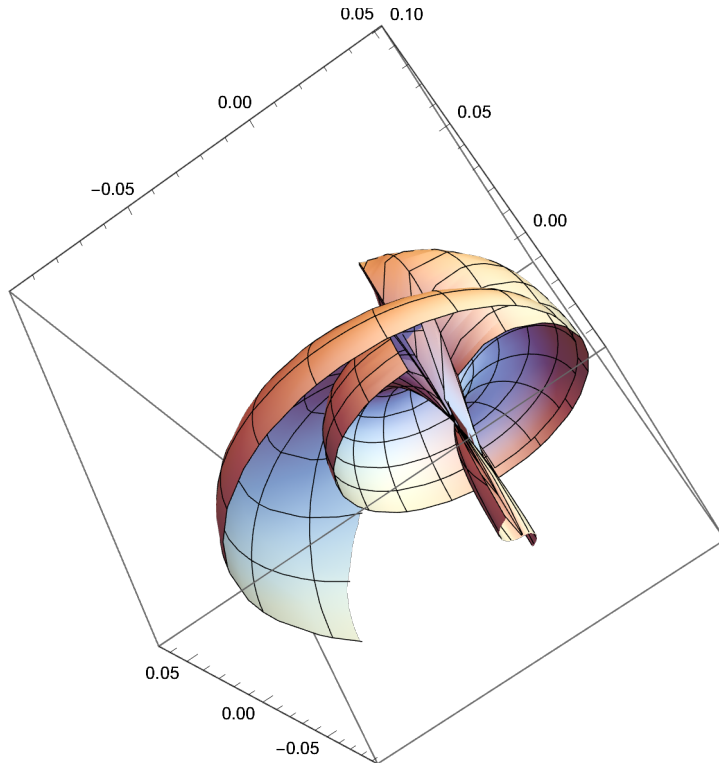


SphericalPlot3D[

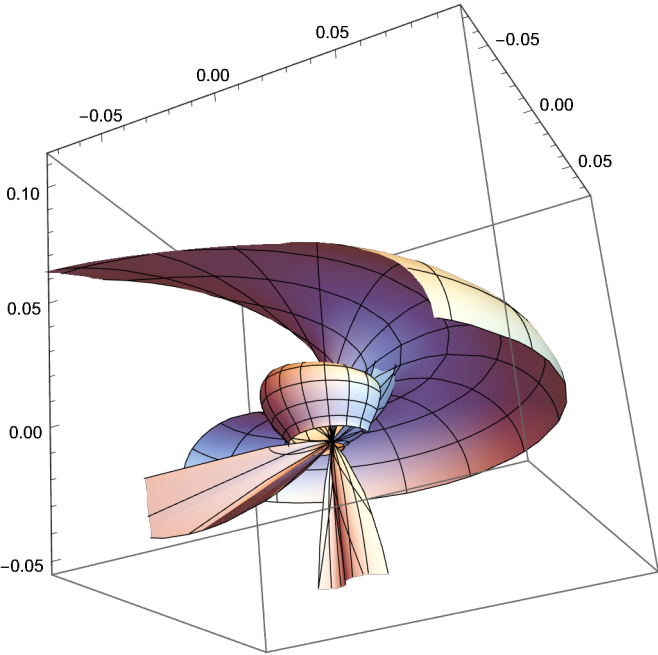
$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \left( 16\pi^2\theta - 12\pi\theta^2 + 2\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2\sin[\beta]^2)\right) / \left( 6\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3} \right) + \frac{2}{3}\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3} \right)^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



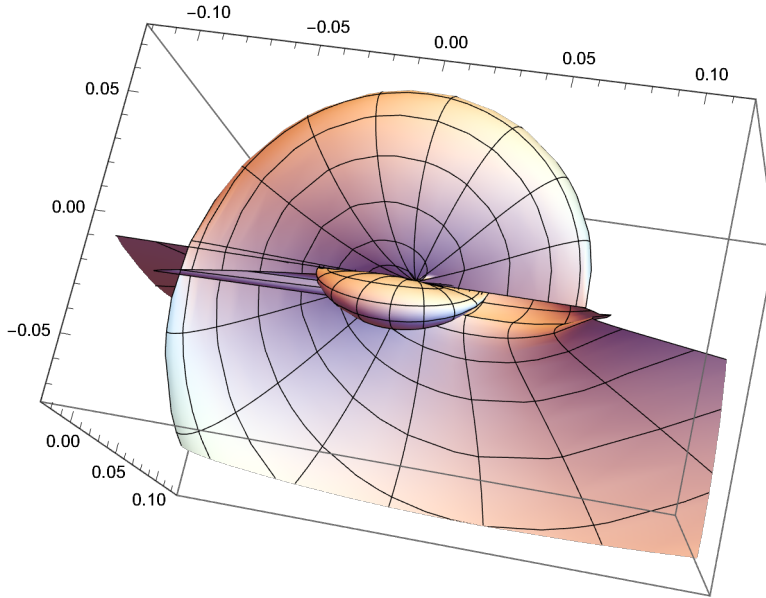
$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \left( -4 \pi \theta + \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^3 - \\
& \quad \left. 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \left( -4 \pi \theta + \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \left( 2 \pi^2 \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) \\
& \quad \left. \sin[\beta]^3 \right) / \left( 4 \pi - \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad 2 \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^3 - \\
& \quad \left. 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



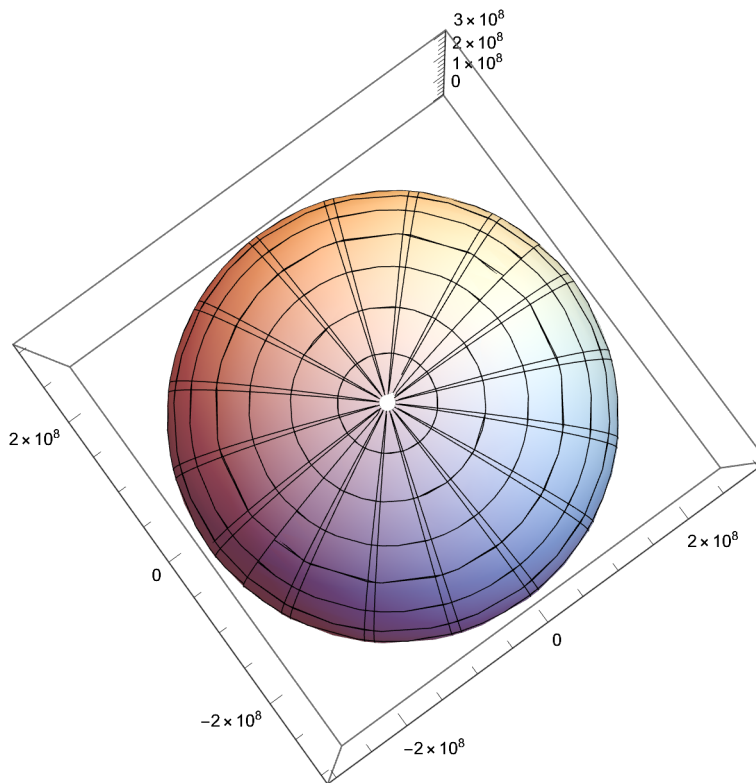
$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \left( -4 \pi \theta + \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \left( 2 \pi^2 \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) \\
& \quad \left. \sin[\beta]^3 \right) / \left( 4 \pi - \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad 2 \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^3 - \\
& \quad \left. 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}
\end{aligned}$$



SphericalPlot3D[

$$\begin{aligned}
 & \left( \sqrt{\left( -6.916640561054567 \cdot 10^{-33} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
 & \quad \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
 & \quad 5.504087674408673 \cdot 10^{-32} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + \right. \right. \right. \\
 & \quad \left. \left. \left. 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
 & \quad \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + \\
 & \quad \left. \left. \left. 2.1729267174130213 \cdot 10^{-34} \sin[\beta]^2 \right) \right) \right) / \\
 & \left( \sqrt{\left( -7.695800507960096 \cdot 10^{-16} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \right. \right. \\
 & \quad \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
 & \quad \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
 & \quad 6.124123459454841 \cdot 10^{-15} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + \right. \right. \right. \\
 & \quad \left. \left. \left. 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
 & \quad \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 +
 \end{aligned}$$

$$\begin{aligned}
 & 2.4177070339300032 \cdot \theta^{17} \sin[\beta]^2 \Big) + \\
 & \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
 & \quad \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
 & \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \\
 & (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2), \\
 & \{\beta, -\pi/2, \pi/2\}, \{\theta, \\
 & -2 \\
 & \pi, 2 \\
 & \pi\}
 \end{aligned}$$

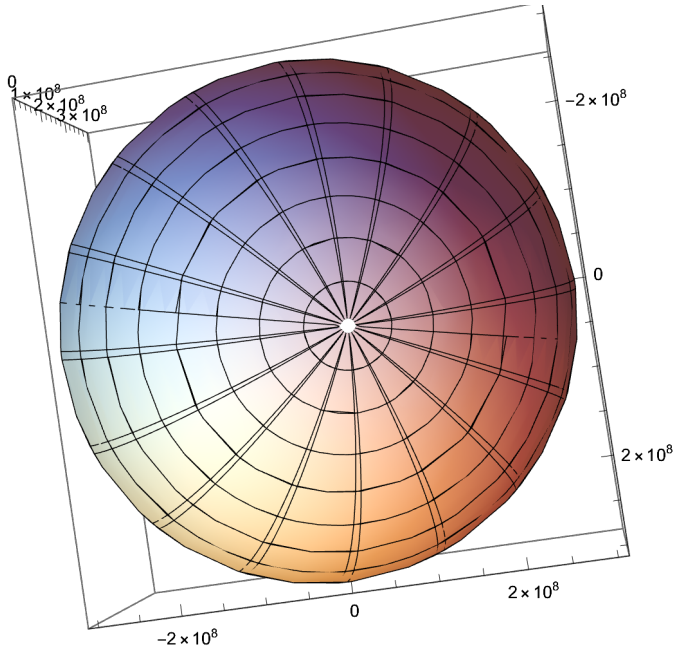




```

SphericalPlot3D[
  (
    Sqrt[
      (-6.916640561054567`*^33 (
        (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
          6 (-Pi^3 + 18 Pi^3 Sin[beta]^2 +
            3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    ) +
    5.504087674408673`*^32 (
      (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
        6 (-Pi^3 +
          18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    )^2 +
    2.1729267174130213`*^34 Sin[beta]^2
  ) /
  (
    Sqrt[
      (-7.695800507960096`*^16 (
        (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
          6 (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    ) +
    6.124123459454841`*^15 (
      (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
        6 (-Pi^3 +
          18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    )^2 +
    2.4177070339300032`*^17 Sin[beta]^2
  )
] +
  (
    (
      (-4 Pi theta + theta^2 + 2 Pi Sqrt[(4 Pi - theta) theta] Sin[beta] + 4 Pi^2 Sin[beta]^2 -
        (2 Pi^2 Sqrt[(4 Pi - theta) theta] Sin[beta]^3) / (4 Pi - theta) -
        (2 Pi^2 Sqrt[(4 Pi - theta) theta] Sin[beta]^3) / theta
    ) /
    (16 Pi^2 theta - 12 Pi theta^2 + 2 theta^3 - 16 Pi^3 Sin[beta]^2 + 8 Pi^2 theta Sin[beta]^2)
  ) /
  (
    (theta / (2 Pi)), {beta, -Pi/2, Pi/2}, {theta,
-2
  Pi,
  2
  Pi}
]

```



TotalVelocity = PhenomenalVelocity + InstantaneousVelocity + AverageVelocity

$$\begin{aligned}
 & \left( \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) / \\
 & \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) + \\
 & \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
 & \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right. \right. \\
 & \left. \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) / (\theta / (2 \pi)) \right) \right) \\
 & r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
 & \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)
 \end{aligned}$$

```

SphericalPlot3D[
  (

$$\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \bigg/ \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) +$$

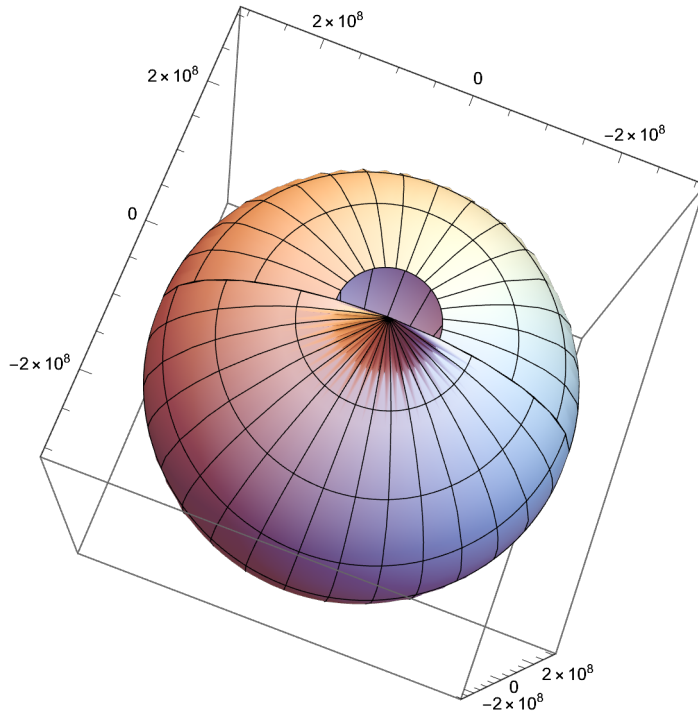

$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right.$$


$$\left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \bigg/ \right.$$


$$\left. \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) \bigg/ \right.$$

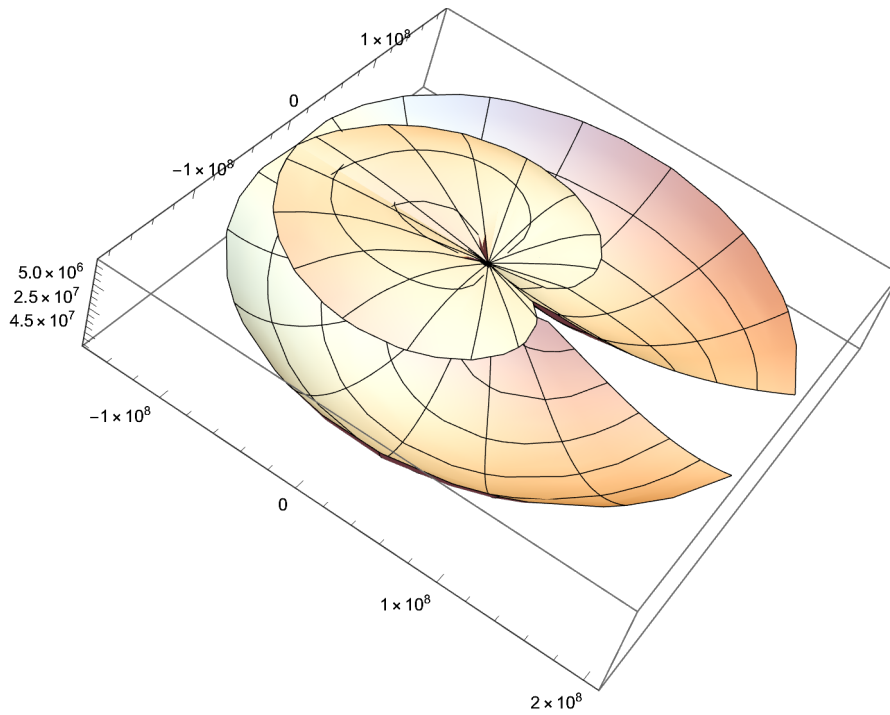

$$\left. \left. \left( \theta / (2 \pi) \right) \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

```



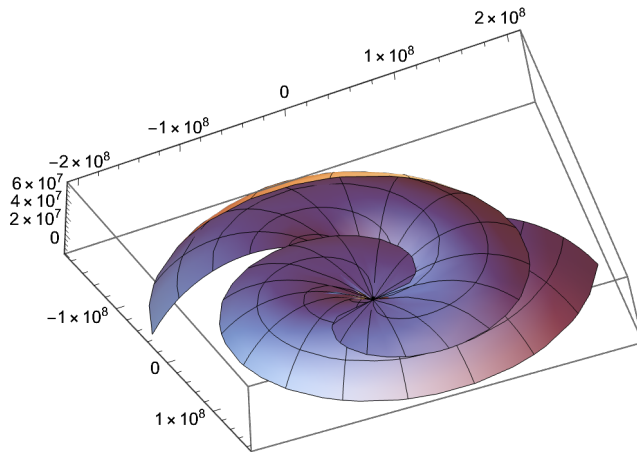
SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right)} \right) / \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)} \right) + \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) / (\theta / (2 \pi)) \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



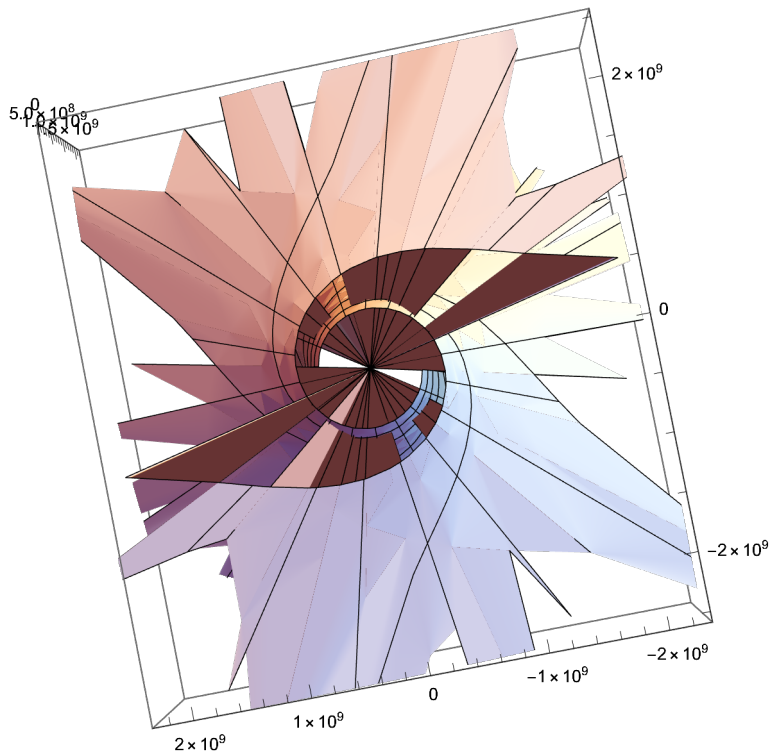
SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{14} \right.} \right. \\
\left. \left. \sin[\beta]^2 \right) \right) / \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \right.} \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) + \\
\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
\left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
\left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) / \\
\left. \left( \theta / (2 \pi) \right) \right], \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]$$

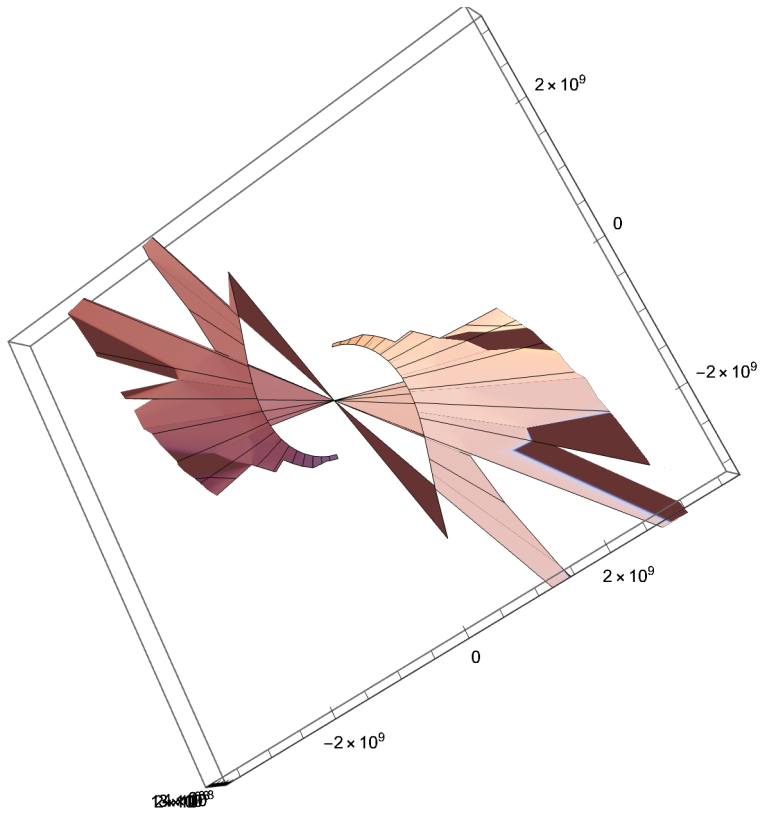


SphericalPlot3D[

$$\begin{aligned}
& \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right) \right) / \\
& \left( \sqrt{\left( -12.566370614359172 \cdot \theta + (\theta)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)} + \right. \\
& \quad \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \quad \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) / \\
& \quad \left. (\theta / (2 \pi)) \right), \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D}\left[ \right. \\
& \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \sin^{16}[\beta] \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin^{18}[\beta] \right) \right) / \\
& \left( \sqrt{-12.566370614359172 \cdot \theta + (\theta)^2} + 39.47841760435743 \cdot \sin^2[\beta] \right) + \\
& \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2}} + \\
& \left( \left( \left( -4 \pi \theta + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin^2[\beta] - \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin^3[\beta]}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right) \theta} \sin^3[\beta]}{\theta} \right) \right) / \\
& \quad \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^3 - 16 \pi^3 \sin^2[\beta] + 8 \pi^2 \theta \sin^2[\beta] \right) \right) / \\
& \left. (\theta / (2 \pi)) \right), \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\} \left. \right]
\end{aligned}$$





SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \theta^{18} \right.} \right.$$
  

$$\left. \sin[\beta]^2 \right) \Big/ \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \right.} \right.$$
  

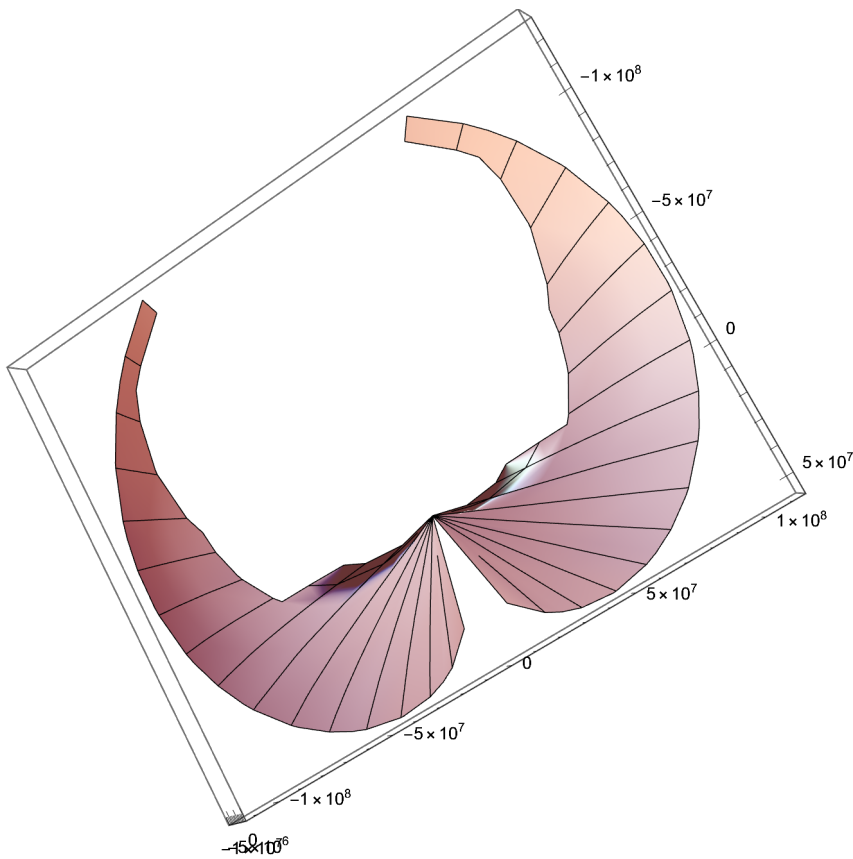
$$\left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \Bigg) +$$
  

$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right.$$
  

$$\left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Big/$$
  

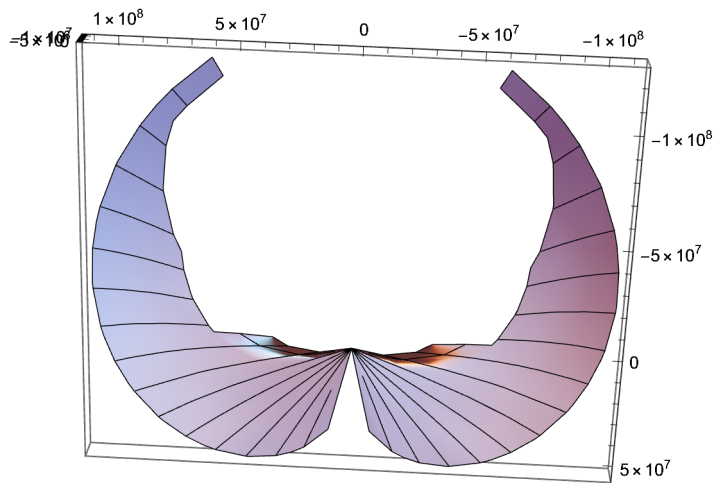
$$\left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \Bigg) \Big/$$
  

$$\left( \theta / (2 \pi) \right) \Bigg], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{14} \right.} \right. \\
\left. \left. \sin[\beta]^2 \right) \right) / \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \right.} \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) + \\
\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
\left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \right. \\
\left. \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) / \right. \\
\left. \left. \left( \theta / (2 \pi) \right) \right) \right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

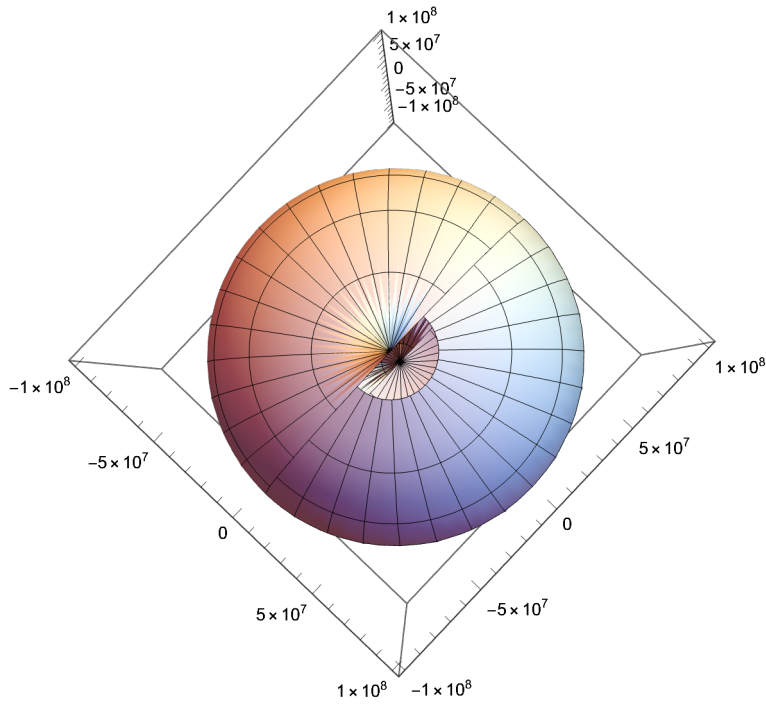


$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)$$

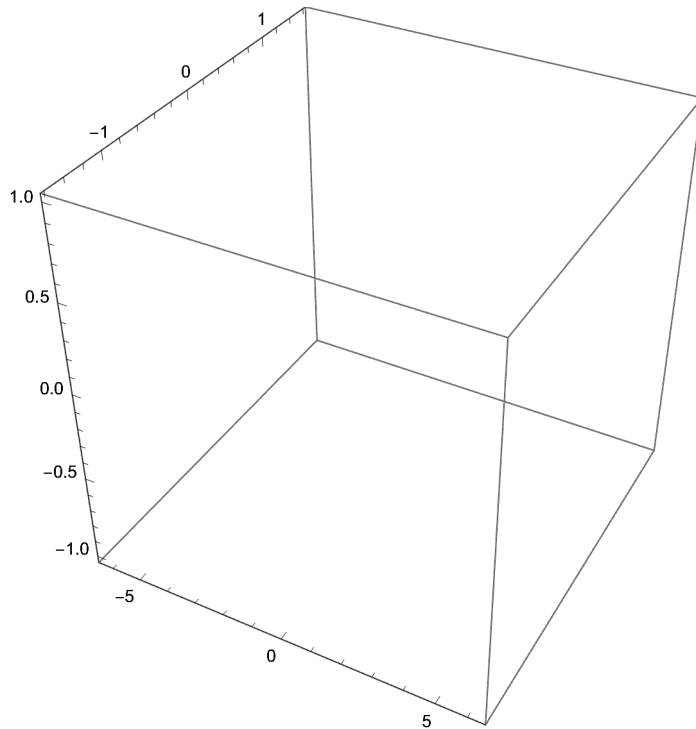
$$D\left[k \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{k (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{SphericalPlot3D}\left[\left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) + \frac{2 \pi (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + r / (\theta / (2 \pi))\right] / 3, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



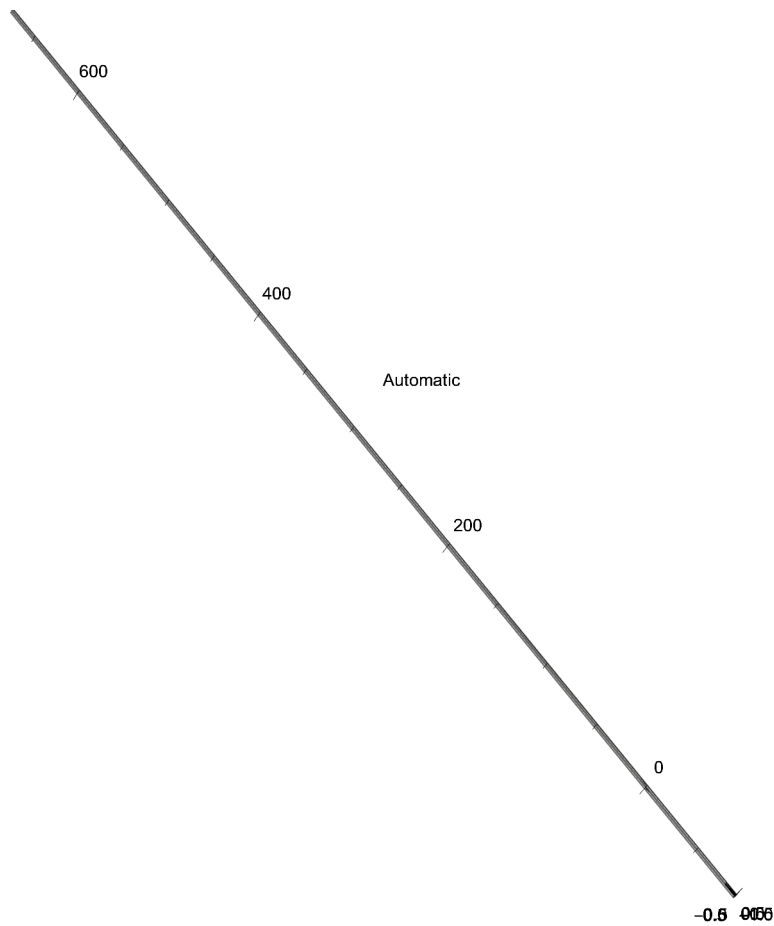
$\text{ContourPlot3D}\left[\left(\left(\sqrt{\left(-1.1294090667581471\right)^{18}\theta + 8.987551787368176\theta^{16} + 3.5481432270250993\sin^2[\beta]\right)}\right) / \left(\sqrt{-12.566370614359172\theta + \theta^2 + 39.47841760435743\sin^2[\beta]}\right) + \frac{k(4\pi r^2 - 2r^2\theta)}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} + r/(\theta/(k))\right) / 3,$   
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}, \{k, -2\pi, 2\pi\}]$



```

SphericalPlot3D[
  2 \pi \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
    \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.
    \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) -
  2 \pi \sqrt{\left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right.
    \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.
    \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right)^2 -
    \left( \frac{1}{2 \pi} \sqrt{4 \pi - \theta} \sqrt{\theta} \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right.
      \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.
      \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) \right)^2 \right),
  {\theta, -4 \pi, 4 \pi}, {\beta, -\pi, \pi}, AxesLabel \rightarrow Automatic]

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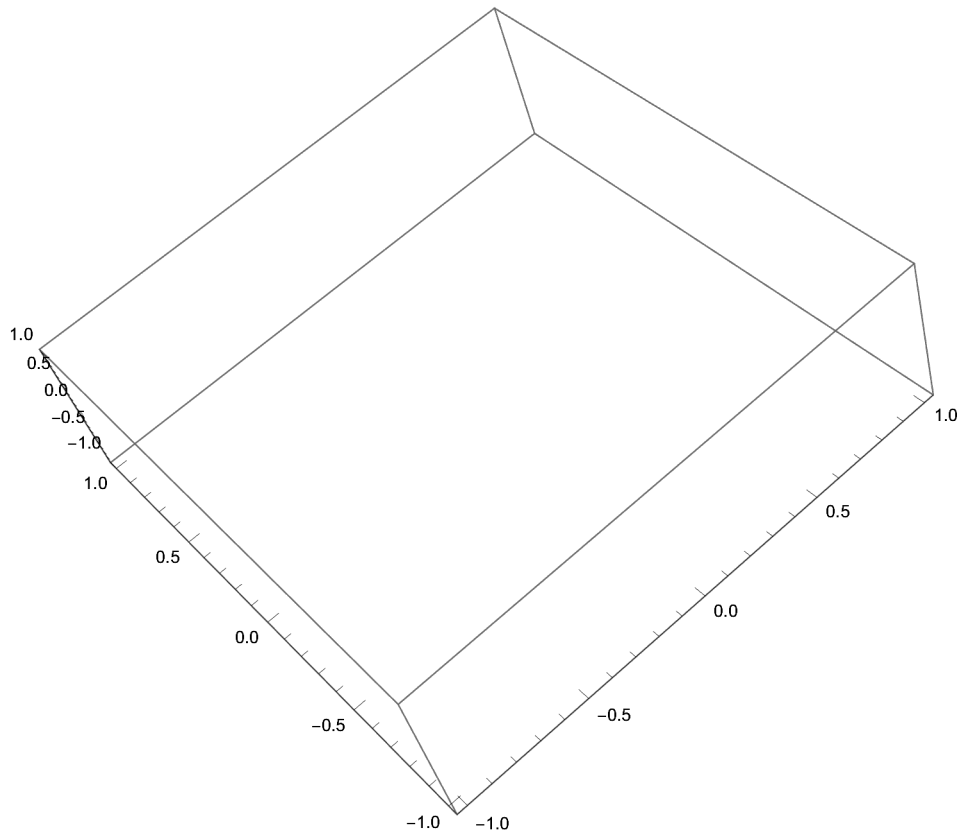


**Solve**[ $y == \text{Abs}[x + i y] \sin[\beta]$ ,  $x$ ]

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

{{ $x \rightarrow -i y - y \csc[\beta]$ }, { $x \rightarrow -i y + y \csc[\beta]$ }}

RevolutionPlot3D[-i y + y Csc[β], {y, -10, 10}, {β, -8 π, 8 π}]

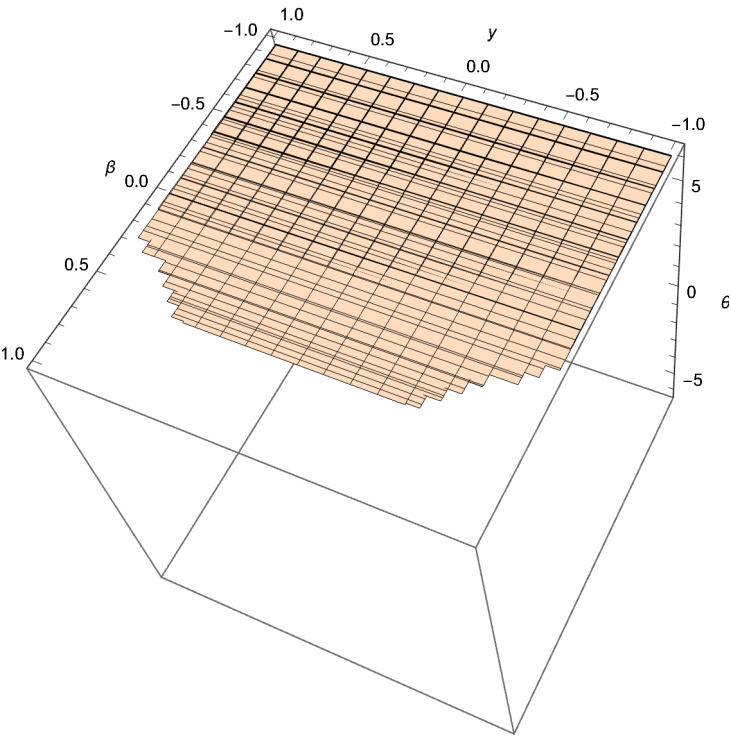


ContourPlot3D[ $\frac{1}{2\pi} \sqrt{4\pi - \theta}$

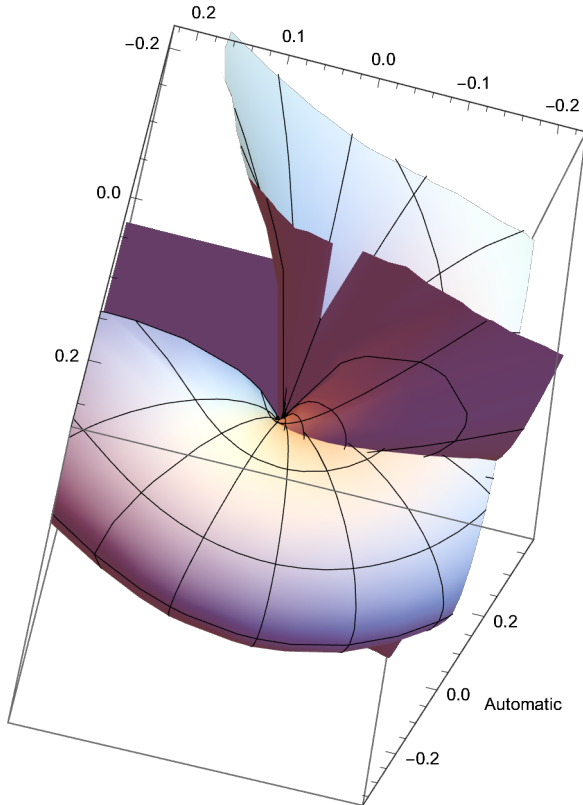
$$\sqrt{\left(1 / \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / \left(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right)\right)^2 \times 2 \pi \left(\left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / \left(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right)\right)^2 + \right.$$

$$\sqrt{\left(-y^2 \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right)^2 + \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right)^4\right)} \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right), \{\beta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{y, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic}]$$

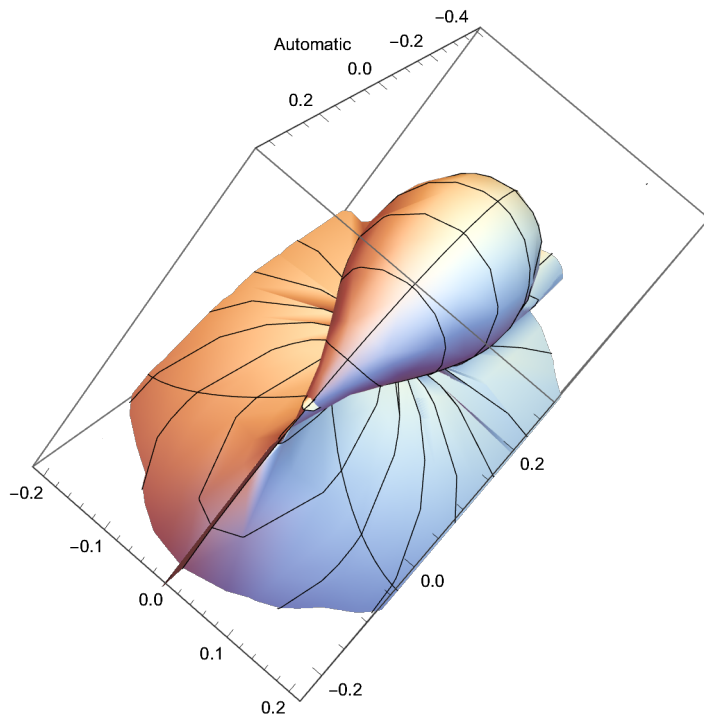




`SphericalPlot3D` $\left[\frac{1}{2\pi}\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\right.$   
 $\left.\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)/\left(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2\right)\right),\right.$   
 $\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\},\text{AxesLabel}\rightarrow\text{Automatic}\Big]$



```
SphericalPlot3D[ $\frac{1}{2\pi} \sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}$ 
 $\left(\left(-4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta}\right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)\right),$ 
{ $\theta, -2\pi, 2\pi$ }, { $\beta, -2\pi, 2\pi$ }, AxesLabel -> Automatic]
```



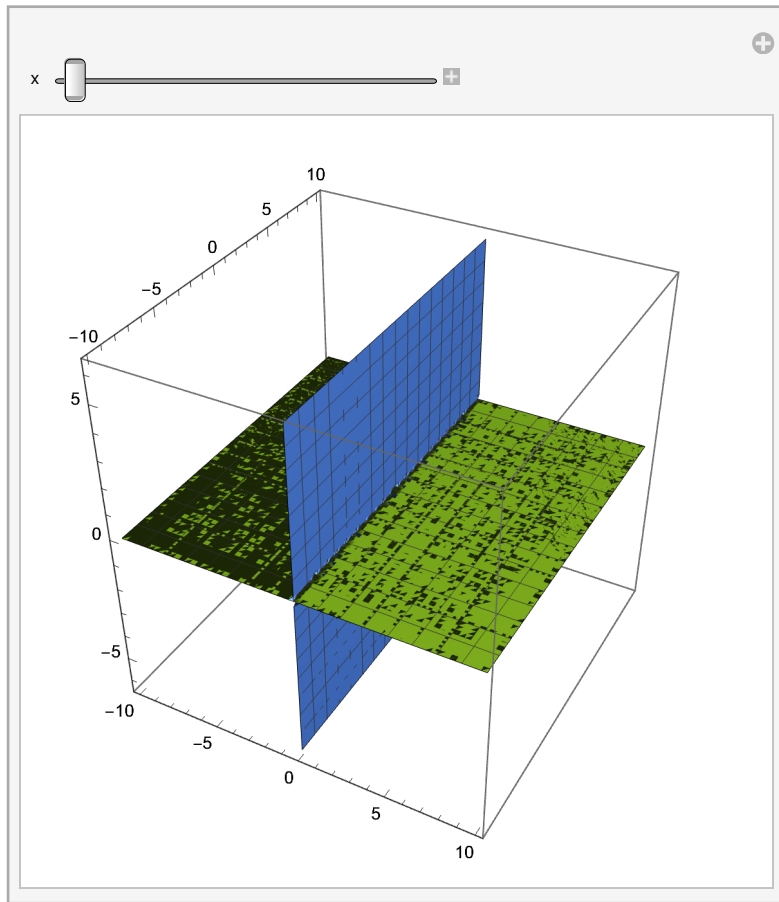
```
ContourPlot3D[ $\frac{1}{2\pi} \sqrt{4\pi - \theta} \sqrt{\frac{2\pi \left(\text{Abs}[x + \text{I} y]^2 + \sqrt{-y^2 \text{Abs}[x + \text{I} y]^2 + \text{Abs}[x + \text{I} y]^4}\right)}{\text{Abs}[x + \text{I} y]^2}} \text{Abs}[x + \text{I} y],$ 
{x, -1, 1}, {y, -1, 1}, { $\theta, -2\pi, 2\pi$ }, AxesLabel -> Automatic]
```

```
Solve[n  $\pi \theta == m \pi r - m \pi x$ , n]
```

```
{{n ->  $\frac{m r - m x}{\theta}$ }}
```

```
In[ ]:= Manipulate[
  ContourPlot3D[ $\frac{m r - m x}{\theta}$ , {m, -10, 10}, {r, -10, 10}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }, {x, -10, 10}]
```

Out[ ]:=



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

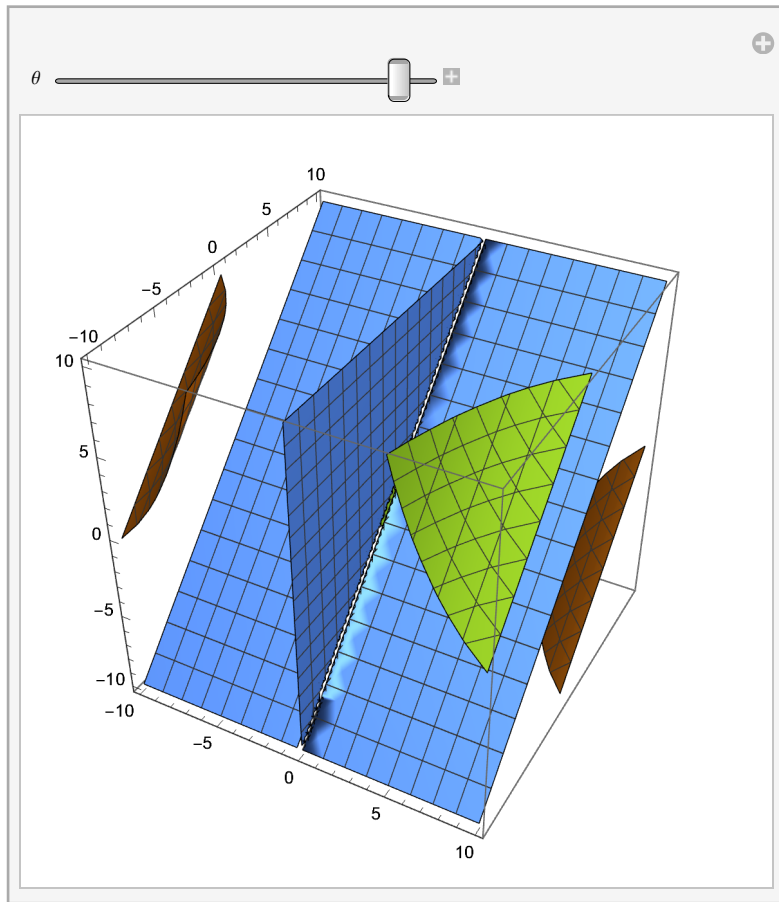
... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

Manipulate[  
 ContourPlot3D[ $\frac{m r - m x}{\theta}$ , {m, -10, 10}, {x, -10, 10}, {r, -10, 10}], { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

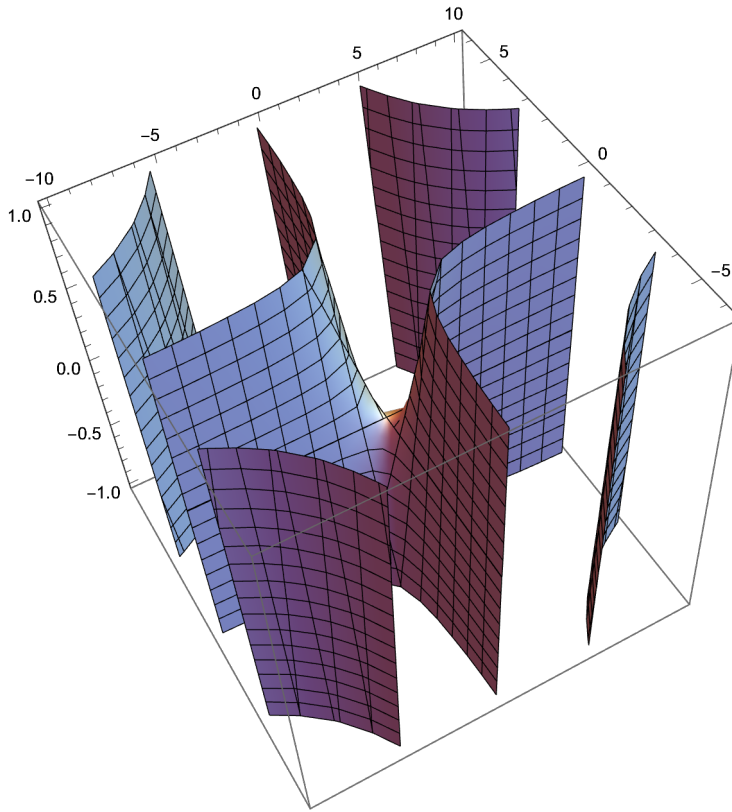


$$\frac{m r - m x}{\theta}$$

Solve[n  $\pi$   $\theta$  == 2  $\pi$  r - 2  $\pi$  x, r]

$$\left\{ \left\{ r \rightarrow \frac{1}{2} (2 x + n \theta) \right\} \right\}$$

ContourPlot3D $\left[\frac{1}{2} (2 x + n \theta), \{x, -1, 1\}, \{n, -10, 10\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\begin{aligned} & \text{Solve}\left[\left(8 \pi r \theta - 2 r \theta^2\right) \left(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right) \right. \\ & \quad \left(2 \pi \sqrt{4 \pi - \theta} \theta \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \\ & \quad \left. \frac{6 \pi^2 \sqrt{4 \pi - \theta} \theta \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{4 \pi - \theta} \theta \cos[\beta] \sin[\beta]^2}{\theta} \right) \\ & \quad \left(-4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{4 \pi - \theta} \theta} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{4 \pi - \theta} \theta} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{4 \pi - \theta} \theta} - \right. \\ & \quad \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta^2} \right) \Bigg] / \\ & \quad \left(2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\ & \quad \left. \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta} \right)^3 \right) - \end{aligned}$$

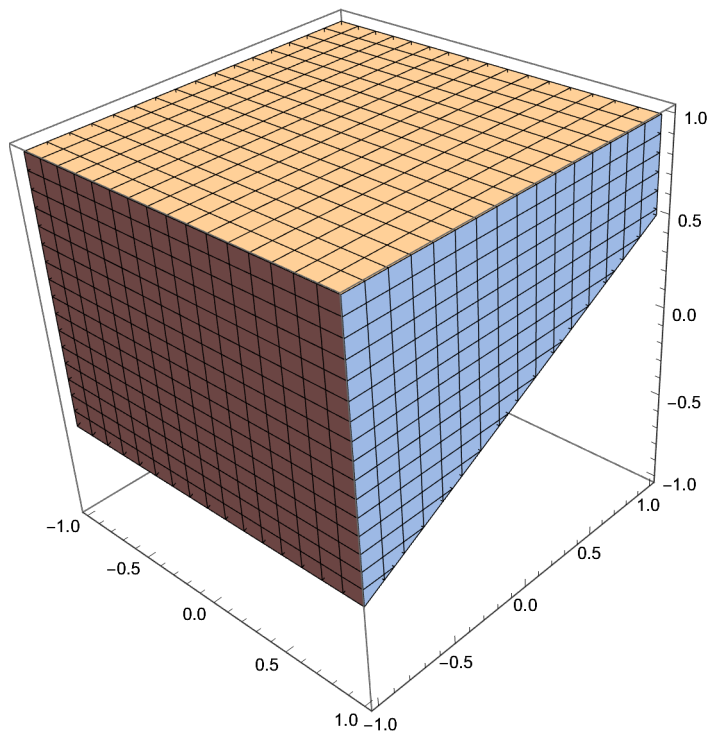
$$\begin{aligned}
& \left( (8\pi r\theta - 2r\theta^2) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right. \\
& \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \left. \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \right) / \\
& \left( 4\pi\sqrt{4\pi r^2\theta - r^2\theta^2} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) - \\
& \left( (8\pi r\theta - 2r\theta^2) (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2\sin[\beta]^2) \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta] \right. \right. \\
& \left. \left. \sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right) / \\
& \left( 4\pi\sqrt{4\pi r^2\theta - r^2\theta^2} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) + \\
& \left( (4\pi r^2 - 2r^2\theta) (8\pi r\theta - 2r\theta^2) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right. \\
& \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \right. \\
& \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right) / \\
& \left( 8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) - \\
& \left( (8\pi r - 4r\theta) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 2\pi \sqrt{(4\pi - \theta)\theta} \cos[\beta] + 8\pi^2 \cos[\beta] \sin[\beta] - \right. \\
& \quad \left. \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2 \sqrt{(4\pi - \theta)\theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) / \\
& \left( 4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2} \left( -4\pi \theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) - \\
& \left( (8\pi r \theta - 2r \theta^2) (-32\pi^3 \cos[\beta] \sin[\beta] + 16\pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta) \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta) \sin[\beta]^3}{(4\pi - \theta) \sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta) \sin[\beta]^3}{\theta \sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta^2} \right) / \\
& \left( 4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2} \left( -4\pi \theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) + \\
& (4\pi (8\pi r \theta - 2r \theta^2) \cos[\beta] \sin[\beta]) / \left( \sqrt{4\pi r^2 \theta - r^2 \theta^2} \left( -4\pi \theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \right. \right. \\
& \quad \left. \left. \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \right) - \\
& ((4\pi r^2 - 2r^2 \theta) (8\pi r \theta - 2r \theta^2) (-32\pi^3 \cos[\beta] \sin[\beta] + 16\pi^2 \theta \cos[\beta] \sin[\beta])) / \\
& \left( 8\pi (4\pi r^2 \theta - r^2 \theta^2)^{3/2} \left( -4\pi \theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \right) + \\
& ((8\pi r - 4r \theta) (-32\pi^3 \cos[\beta] \sin[\beta] + 16\pi^2 \theta \cos[\beta] \sin[\beta])) / \\
& \left( 4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2} \left( -4\pi \theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \right) =
\end{aligned}$$

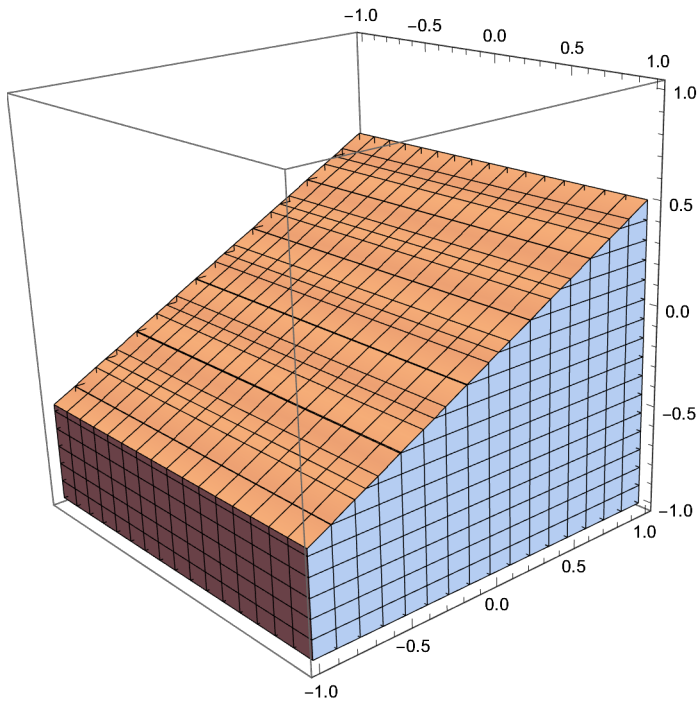


$$\left( r - \frac{r \theta}{2 \pi} \right) / \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right. \\ \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right), r]$$

`RegionPlot3D[ $\overline{AC} < \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{AC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`



`RegionPlot3D[ $\overline{AC} \geq \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{AC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`



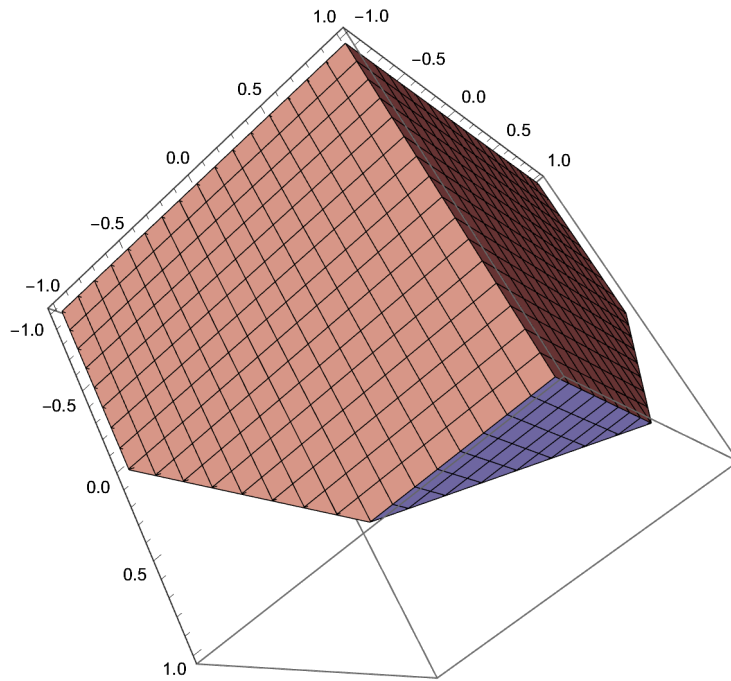
`RegionPlot3D[ $g > \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} + \frac{2\pi r - r\theta}{2\pi}$ , { $r$ , -1, 1}, { $g$ , -1, 1}, { $\theta$ , -1, 1}]`

Greater::nord: Invalid comparison with  $-1.15915 + 0.586208 i$  attempted. >>

RegionPlot3D::boolf:  $g > \frac{\sqrt{4\pi r^2 \theta - \text{Power}[\ll 2 \gg] \text{Power}[\ll 2 \gg]}}{2\pi} + \frac{2\pi r - r\theta}{2\pi}$  must be a Boolean function. >>

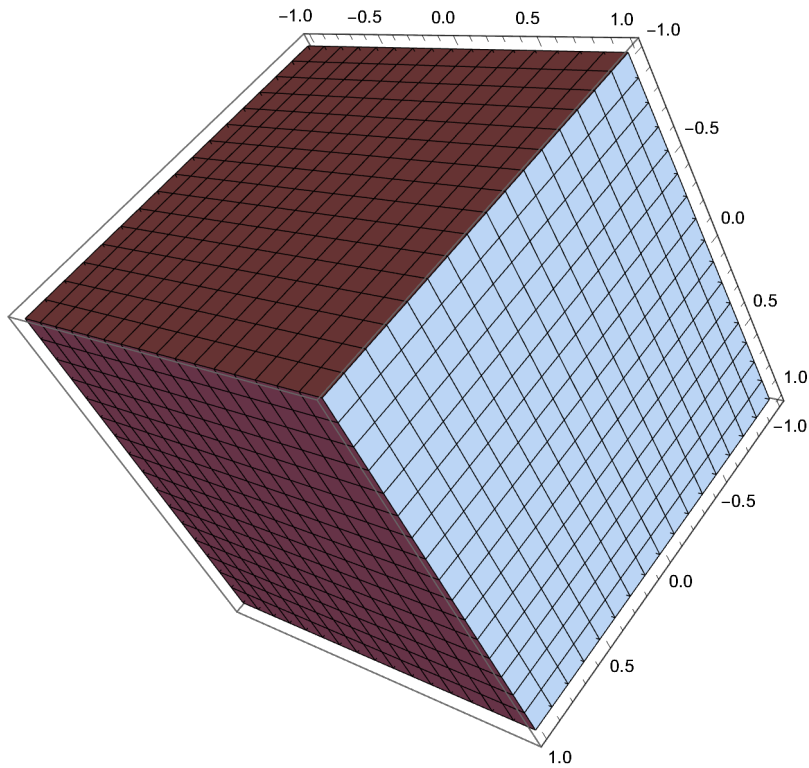
`RegionPlot3D[ $g > \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} + \frac{2\pi r - r\theta}{2\pi}$ , { $r$ , -1, 1}, { $g$ , -1, 1}, { $\theta$ , -1, 1}]`

`RegionPlot3D[AC ≥ AB + DE, {AB, -1, 1}, {AC, -1, 1}, {DE, -1, 1}]`

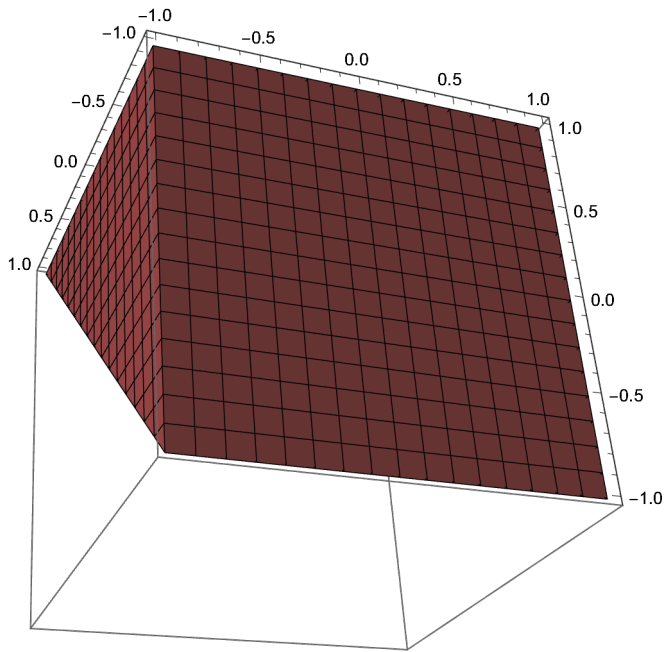


`RegionPlot3D[ $\overline{AC} \geq \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{AC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`

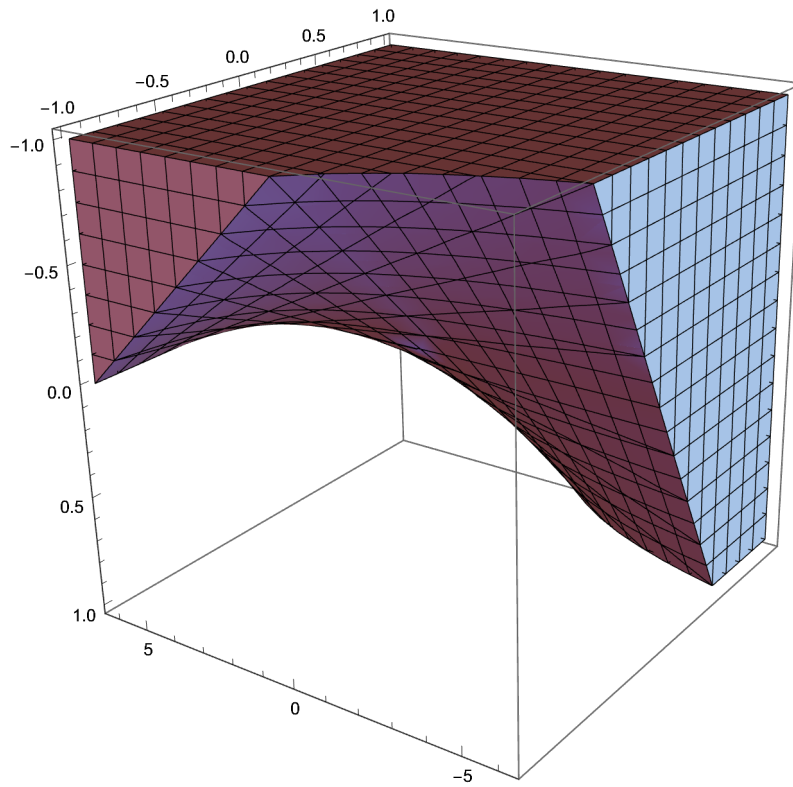
`RegionPlot3D[ $\overline{AB} + \overline{BC} \geq \overline{AB} + \overline{DE}$ , { $\overline{AB}$ , -1, 1}, { $\overline{BC}$ , -1, 1}, { $\overline{DE}$ , -1, 1}]`



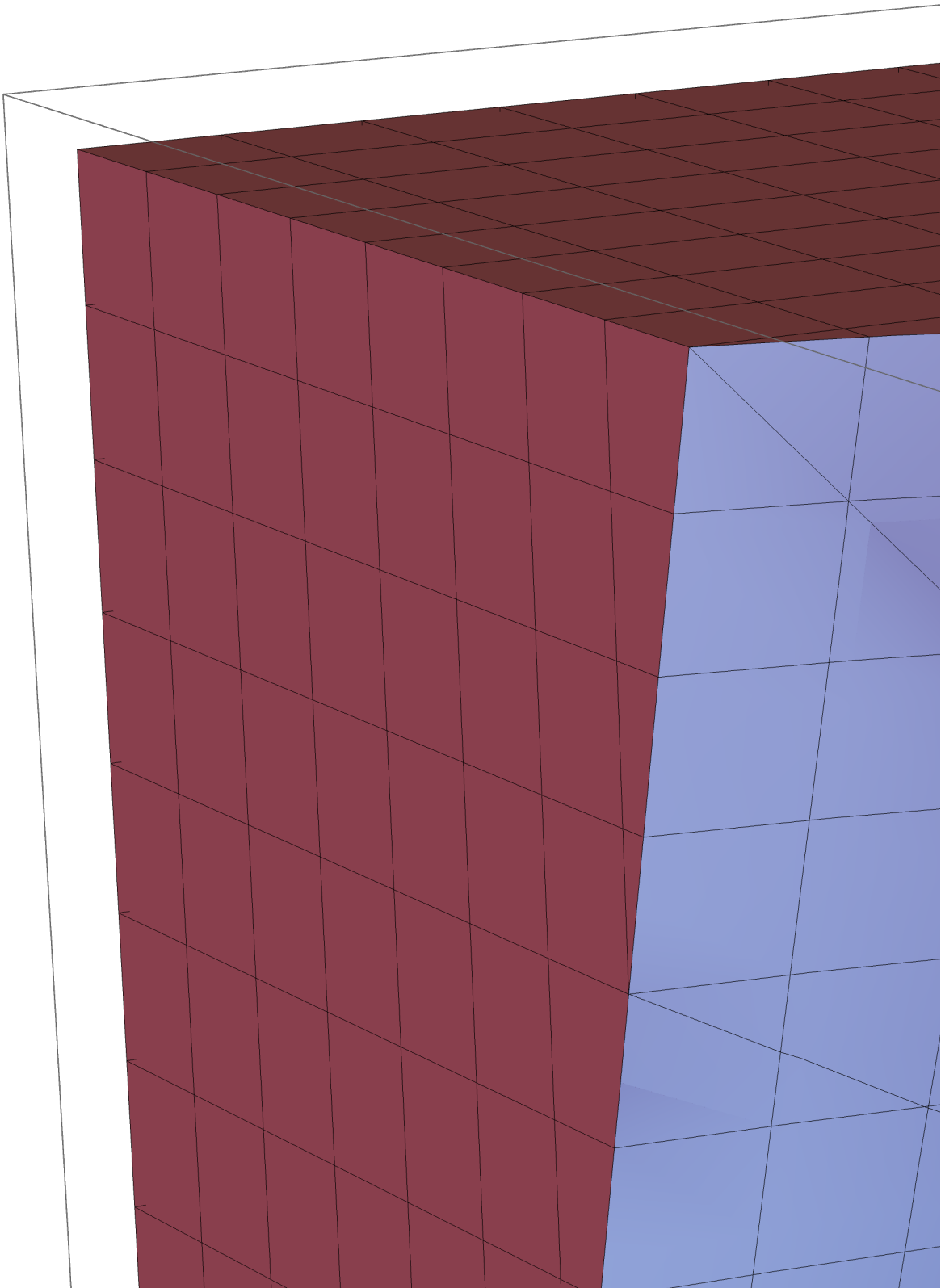
`RegionPlot3D[AB + BC < AB + DE, {AB, -1, 1}, {BC, -1, 1}, {DE, -1, 1}]`

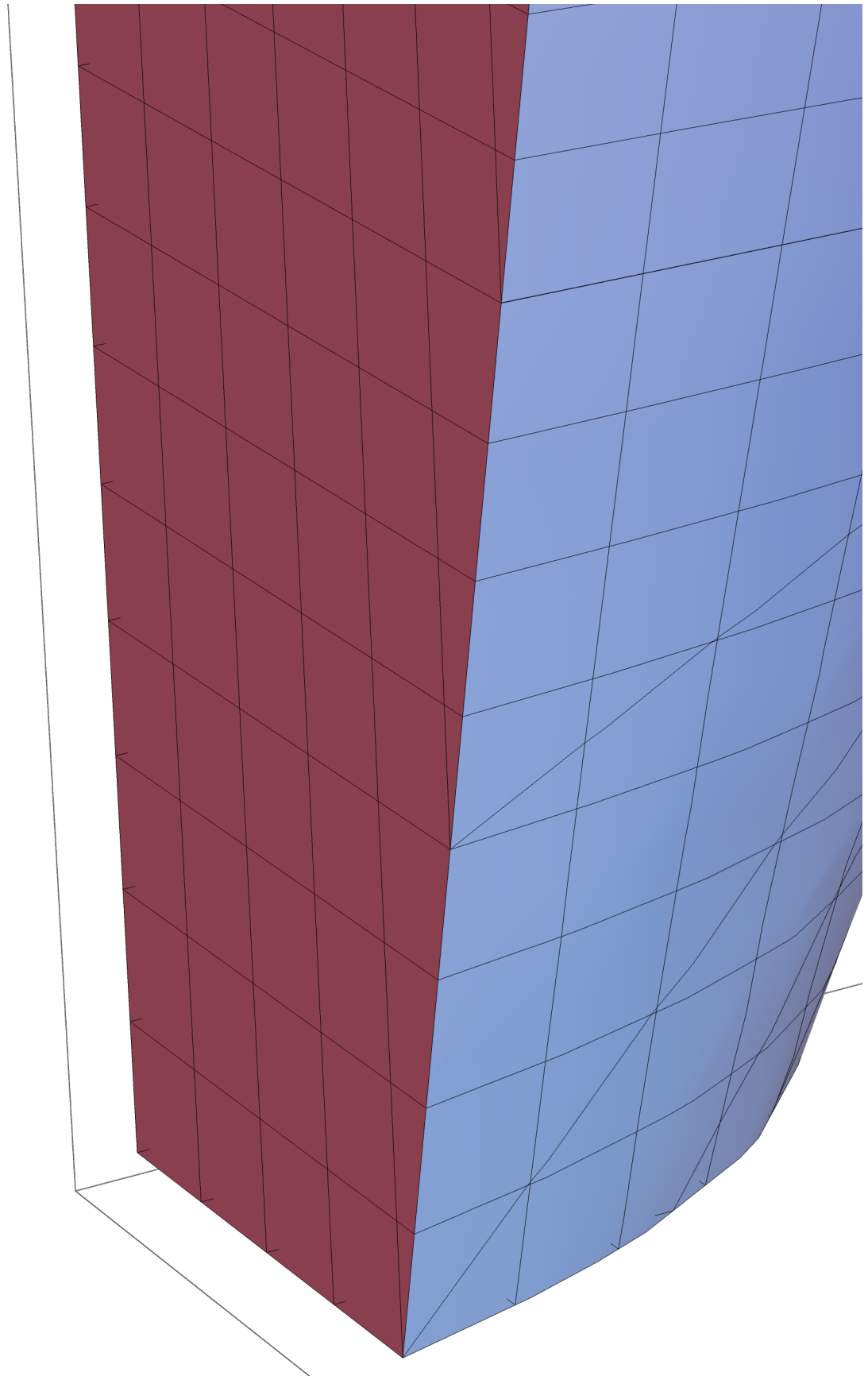


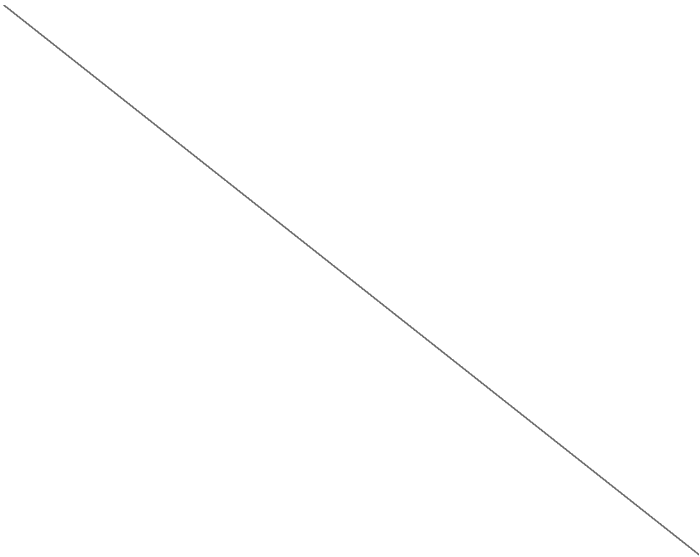
`RegionPlot3D[2  $\pi$  r - 2  $\pi$  x >  $\theta$  r, {r, -1, 1}, {x, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]`



`RegionPlot3D[2  $\pi$  r - 2  $\pi$  x >  $\theta$  r, {r, -.1, .1}, {x, -.1, .1}, { $\theta$ , -8  $\pi$ , 8  $\pi$ }]`







RegionPlot3D[  

$$2 \pi \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.$$

$$\left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) - 2 \pi x <$$

$$\theta \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.$$

$$\left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) \Bigg],$$

$$\{\beta, -\pi, \pi\}, \{x, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$

Less::nord : Invalid comparison with  $6.03319 + 1.76763 \times 10^{-17} i$  attempted. >>

RegionPlot3D::boolf :  $\frac{2 \pi (-4 \pi \theta + \theta^2 + 2 \ll 3 \gg + \ll 1 \gg - \ll 1 \gg - 2 \ll 3 \gg \text{Power}[\ll 2 \gg])}{\ll 6 \gg + 8 \text{Power}[\ll 2 \gg] \theta \text{Power}[\ll 2 \gg]} - 2 \pi x < \frac{\theta(\ll 1 \gg)}{\ll 1 \gg}$  must be a Boolean function. >>

RegionPlot3D[  

$$\left( 2 \pi \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.$$

$$\left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) - 2 \pi x < \right.$$

$$\left( \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.$$

$$\left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right), \{\beta,$$

$$-\pi, \pi\}, \{x, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$

RegionPlot3D[ $2 \pi r - 2 \pi \frac{2 \pi r - r^2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{2 \pi} < 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) r,$   
 $\{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -4 \pi, 4 \pi\}]$



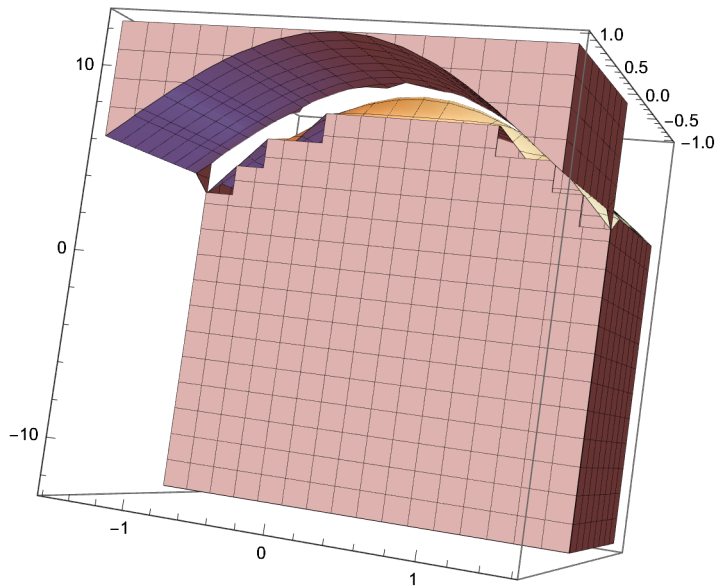
**RegionPlot3D** $\left[2 \pi \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} - 2 \pi x > \theta \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

Greater::nord : Invalid comparison with 6.28319 + 3.6276 i attempted. >>

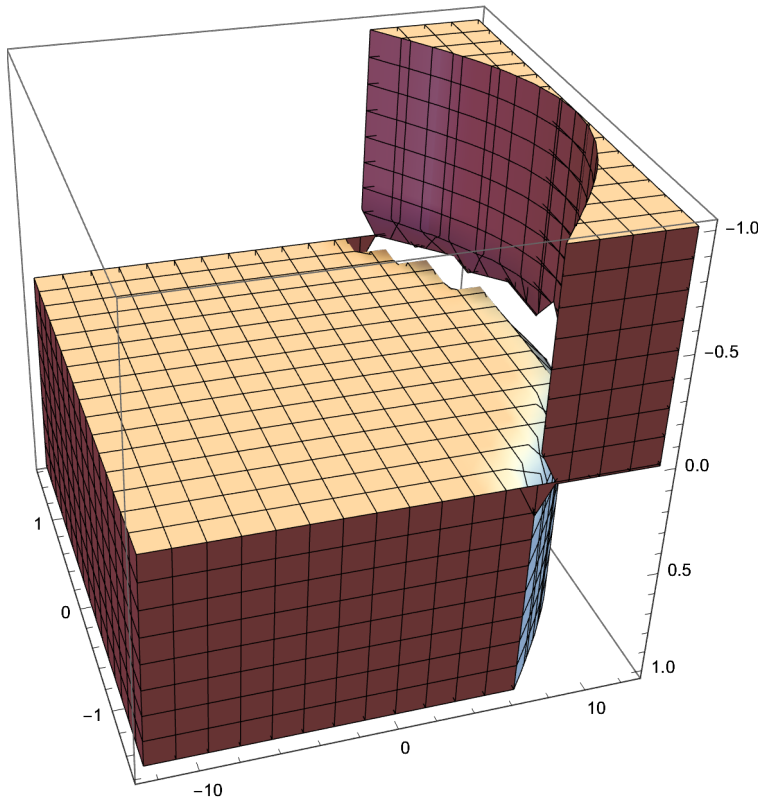
**RegionPlot3D::boolf** :  $\frac{2 \pi (2 \pi \eta)}{\sqrt{\text{Times}[\llbracket 3 \rrbracket] + \text{Times}[\llbracket 2 \rrbracket]}} - 2 \pi x > \frac{\theta (2 \pi \eta)}{\sqrt{4 \pi \theta - \text{Power}[\llbracket 2 \rrbracket]}}$  must be a Boolean function. >>

**RegionPlot3D** $\left[\frac{2 \pi (2 \pi \eta)}{\sqrt{4 \pi \theta - \theta^2}} - 2 \pi x > \frac{\theta (2 \pi \eta)}{\sqrt{4 \pi \theta - \theta^2}}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

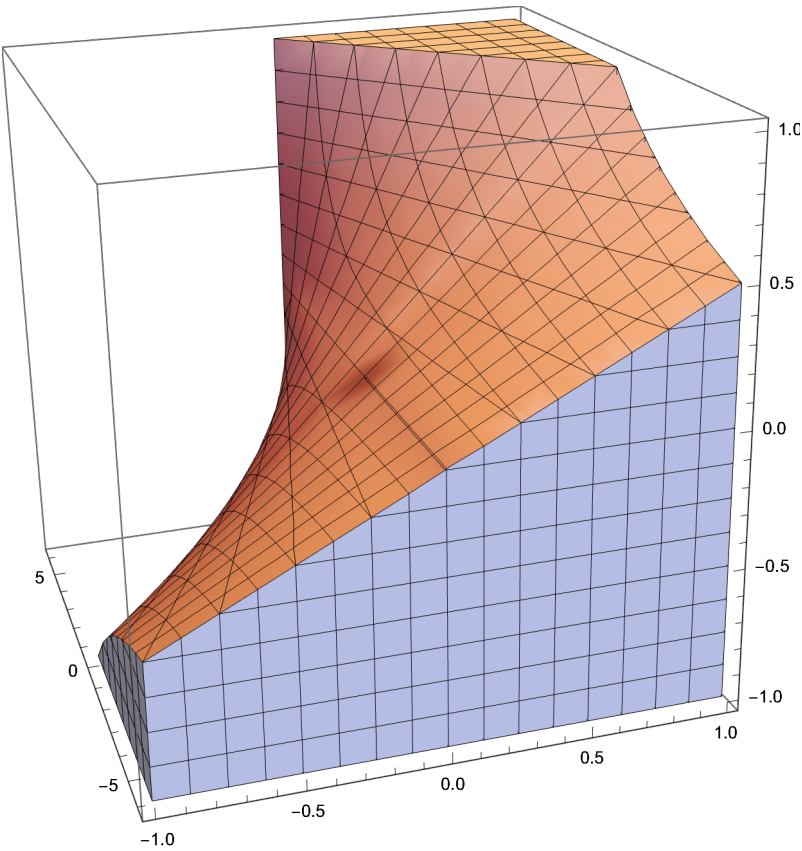
**RegionPlot3D** $\left[2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} > 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) r, \{r, -1, 1\}, \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -4 \pi, 4 \pi\}\right]$



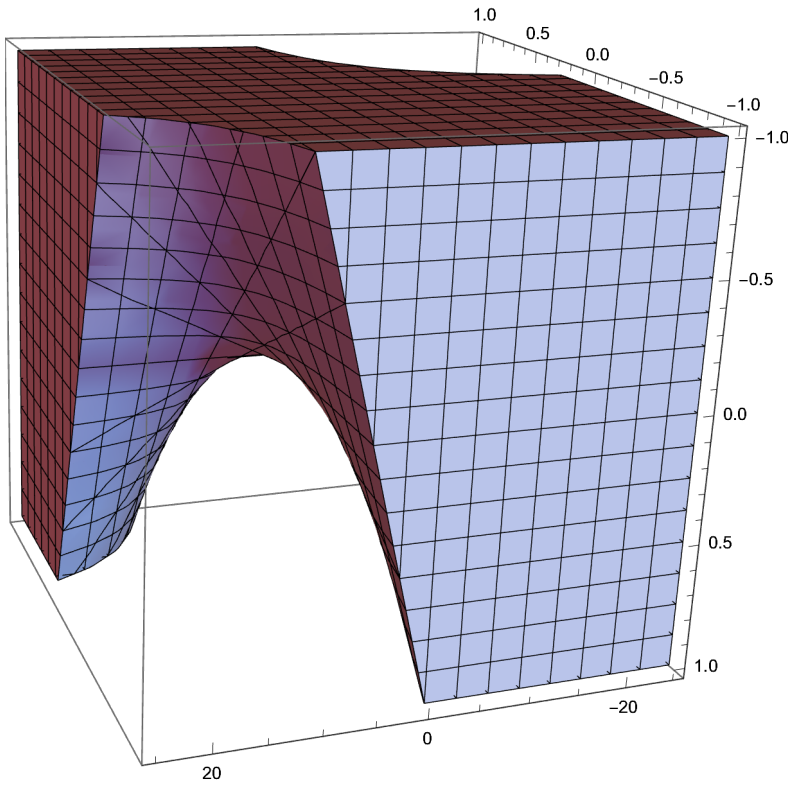
`RegionPlot3D` $\left[2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} < 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) r, \right.$   
 $\left. \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -4 \pi, 4 \pi\} \right]$



`RegionPlot3D` $[2 \pi r - 2 \pi x < \theta r, \{r, -1, 1\}, \{x, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$



```
RegionPlot3D[2 π r + 2 π x < θ r, {r, -1, 1}, {x, -1, 1}, {θ, -8 π, 8 π}]
```

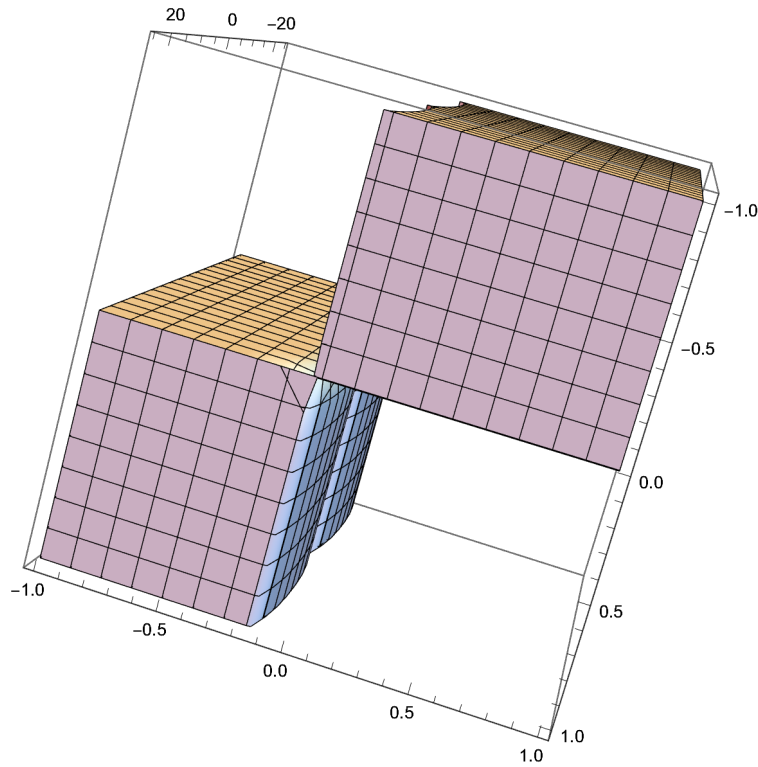


RegionPlot3D[ $2 \pi r +$

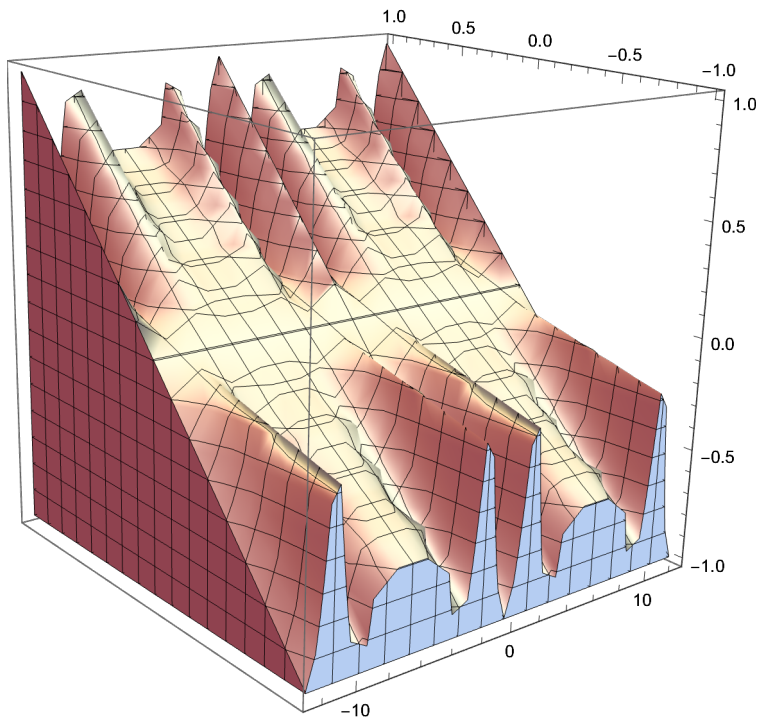
$$2 \pi x \left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right.$$

$$\left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) r,$$

{r, -1, 1}, {x, -1, 1}, {\beta, -8 \pi, 8 \pi}]

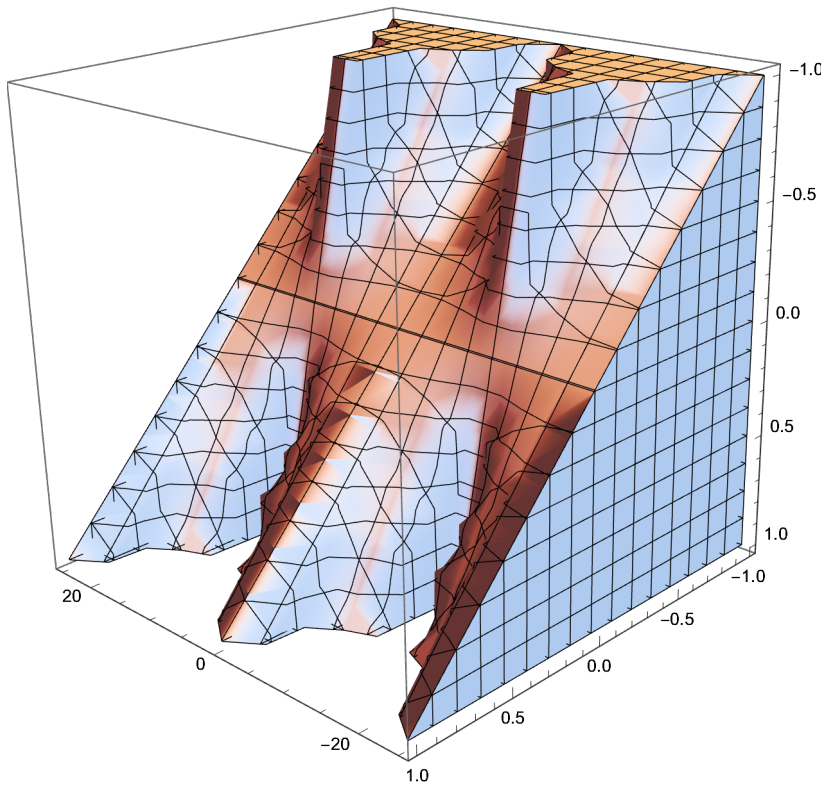


$\text{RegionPlot3D}\left[2 \pi r+2 \pi x \leq\left(2\left(\pi+\sqrt{\pi^2-\pi^2 \operatorname{Sin}[\beta]^2}\right)\right) r,\right.$   
 $\left.\{r,-1,1\},\{x,-1,1\},\{\beta,-4 \pi, 4 \pi\}\right]$

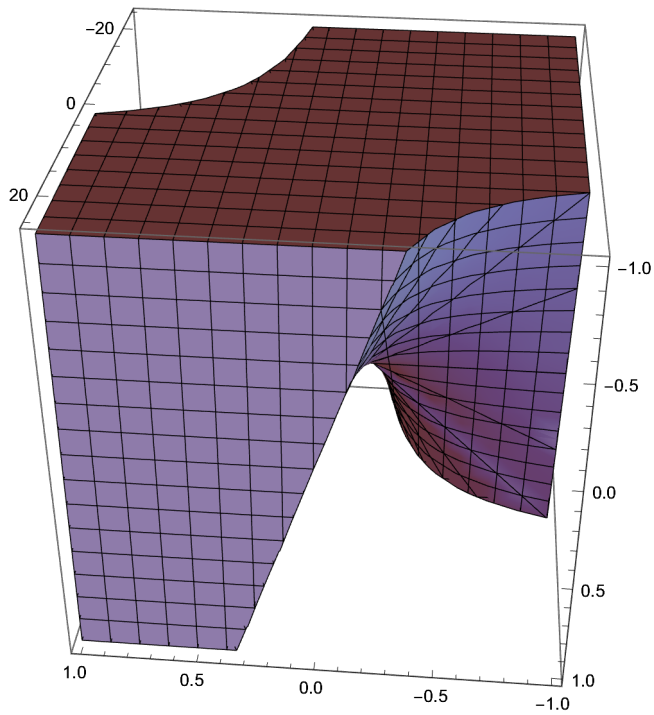


```
RegionPlot3D[ $2 \pi r + 2 \pi x \leq \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right) r,$   

{r, -1, 1}, {x, -1, 1}, { $\beta$ ,  $-8 \pi$ ,  $8 \pi$ }]
```



```
RegionPlot3D[2 π r + 2 π x ≤ θ r, {r, -1, 1}, {x, -1, 1}, {θ, -8 π, 8 π}]
```



$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2$$

$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2$$

$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2 == 2 \pi \frac{\text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2 == \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\text{Cos}[\theta]^2 + \text{Sin}[\theta]^2 == \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \beta\right]$$

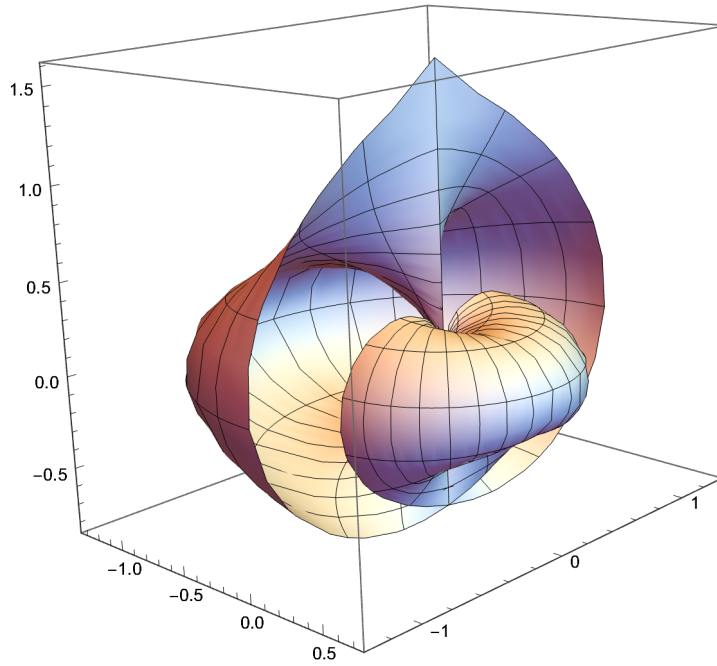
Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta} \text{Cos}[\theta]^2 + \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\theta]^2}{2 \pi}\right]\right\}\right\}$$

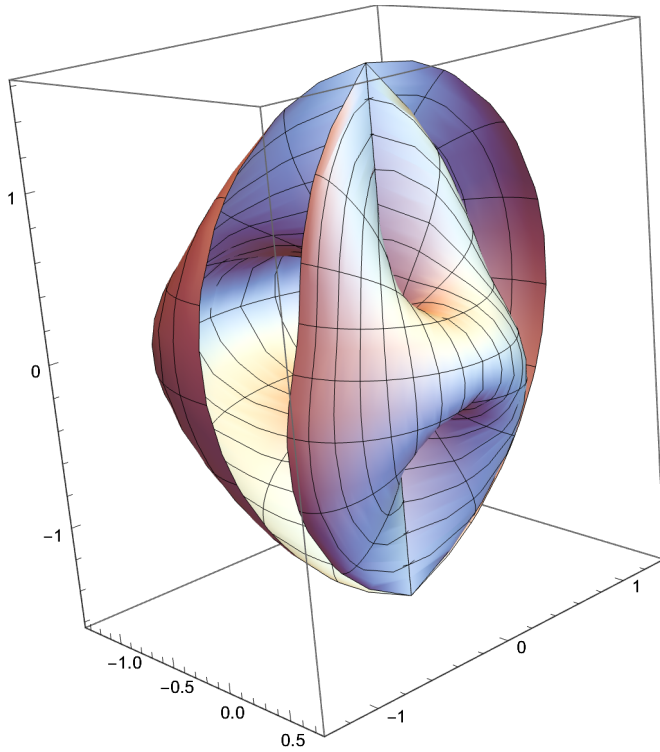


SphericalPlot3D[  

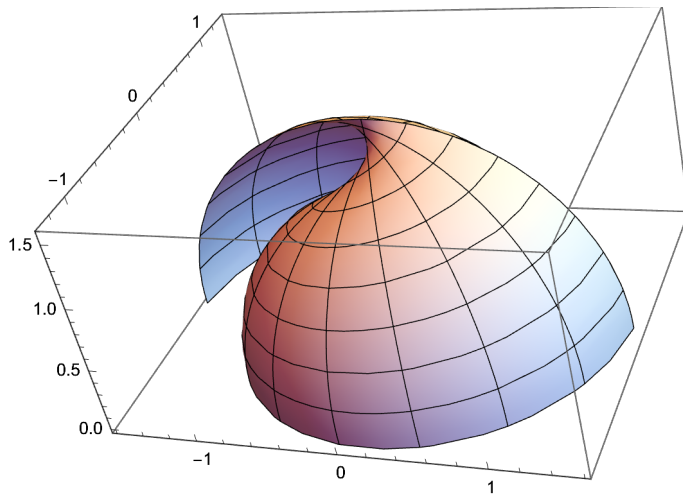
$$\text{ArcSin}\left[\frac{\sqrt{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)\theta \cos[\theta]^2 + \sqrt{(4\pi - \theta)\theta} \sin[\theta]^2}}{2\pi}\right],$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]



`SphericalPlot3D[`  
 $\text{ArcSin}\left[\frac{1}{2\pi} \left( \sqrt{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) \cos[\theta]^2 + \sqrt{(4\pi - \theta)\theta} \sin[\theta]^2} \right)\right], \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$   
`]`



`SphericalPlot3D[`  
 $\text{ArcSin}\left[\frac{1}{2\pi} \left( \sqrt{(4\pi - \theta)\theta} \cos\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 + \sqrt{(4\pi - \theta)\theta} \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 \right)\right], \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$   
`]`



$$\text{Solve}\left[\text{Cos}[\alpha]^2 + \text{Sin}[\alpha]^2 = \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \beta\right]$$

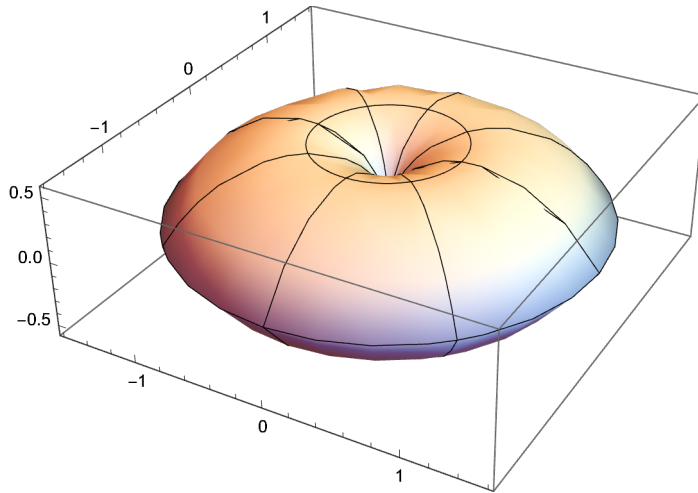
Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta} \text{Cos}[\alpha]^2 + \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\alpha]^2}{2 \pi}\right]\right\}\right\}$$

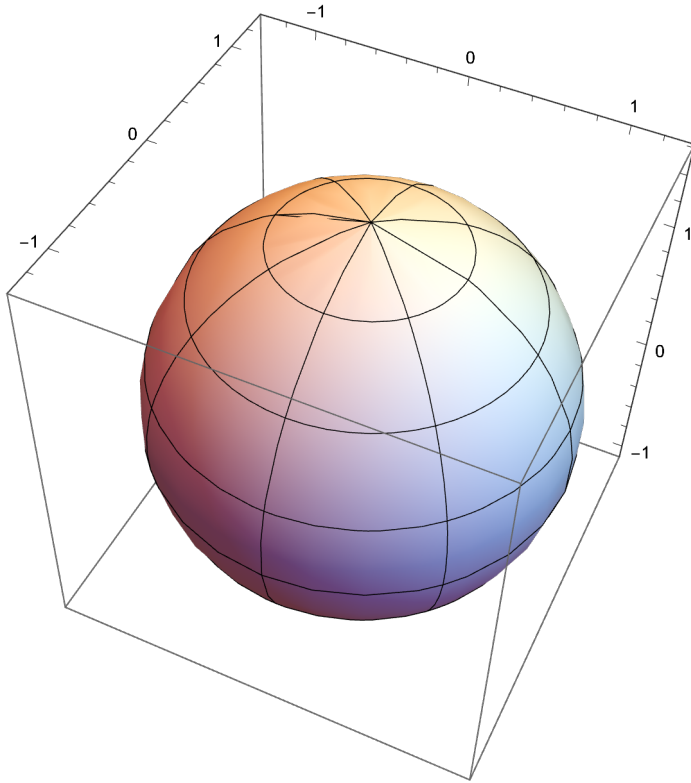
SphericalPlot3D[

$$\text{ArcSin}\left[\frac{1}{2 \pi} \left( \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \text{Cos}[\alpha]^2 + \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \text{Sin}[\alpha]^2}\right)}\right],$$

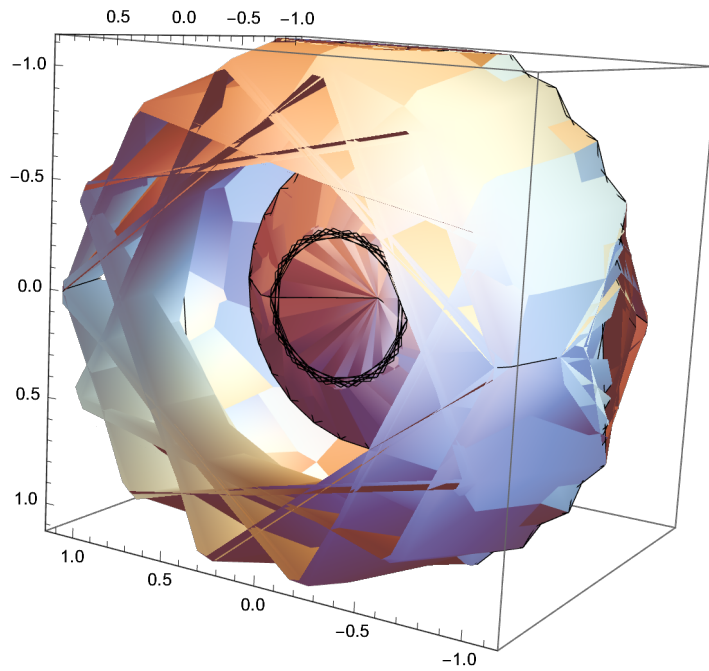
$$\{\beta, -2 \pi, 2 \pi\}, \{\alpha, -2 \pi, 2 \pi\}]$$



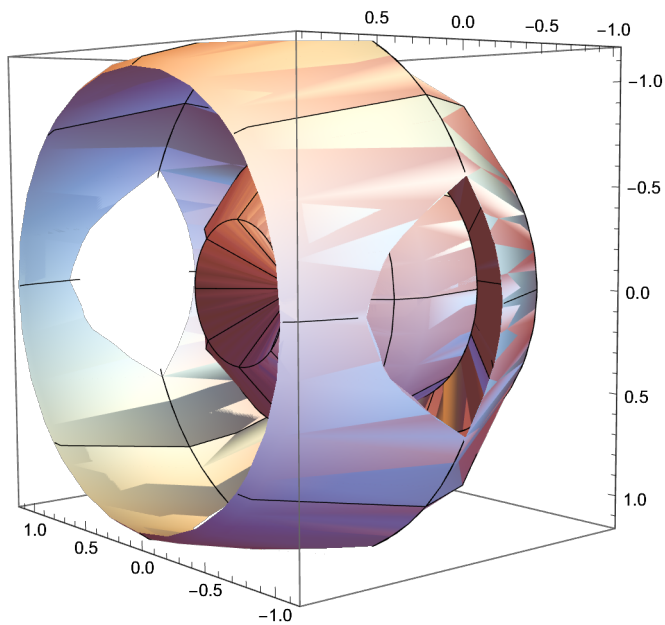
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{1}{2\pi}\sqrt{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]^2}\right)\right)^2}\right.\right.\right. \\ \left.\left.\left.2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]^2}\right)\right)\right)\cos[\alpha]^2+\right.\right. \\ \left.\left.\sqrt{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]^2}\right)\right)^2}\right)^2}\right.\right. \\ \left.\left.\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]^2}\right)\right)\right.\right. \\ \left.\left.\left.\text{Sin}[\alpha]^2\right)\right],\{\theta,-2\pi,2\pi\},\{\alpha,-2\pi,2\pi\}\right]$$



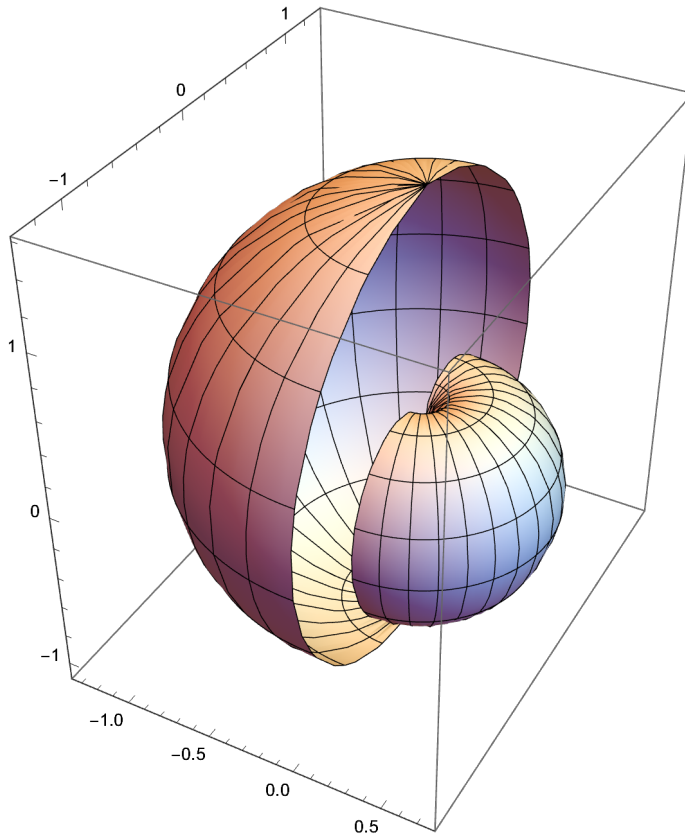
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}\cos[\alpha]^2+\sqrt{(4\pi-\theta)\theta}\sin[\alpha]^2}{2\pi}\right],\right. \\ \left.\{\theta,-16\pi,16\pi\},\{\alpha,-16\pi,16\pi\}\right]$$



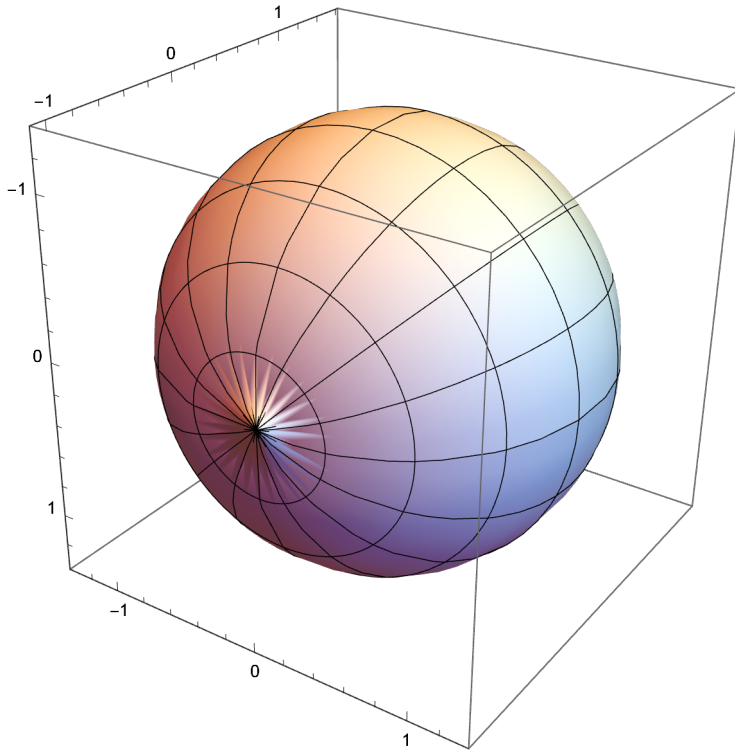
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}\cos[\alpha]^2+\sqrt{(4\pi-\theta)\theta}\sin[\alpha]^2}{2\pi}\right],\right. \\ \left.\{\theta,-16\pi,16\pi\},\{\alpha,-2\pi,2\pi\}\right]$$



`SphericalPlot3D` $\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}\cos[\alpha]^2 + \sqrt{(4\pi - \theta)\theta}\sin[\alpha]^2}{2\pi}\right],\right.$   
 $\left.\{\theta, -2\pi, 2\pi\}, \{\alpha, -\pi/2, \pi/2\}\right]$



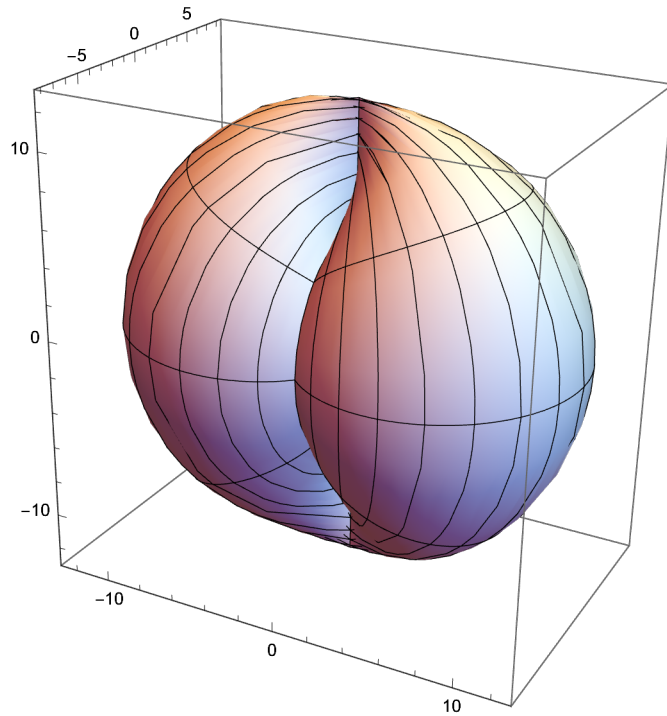
SphericalPlot3D[  
 $\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}\cos[\alpha]^2 + \sqrt{(4\pi - \theta)\theta}\sin[\alpha]^2}{2\pi}\right], \{\theta, -2\pi, 2\pi\}, \{\alpha, -\pi, \pi\}$



Solve[ $\cos[\alpha]^2 + \sin[\alpha]^2 = \frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \theta]$

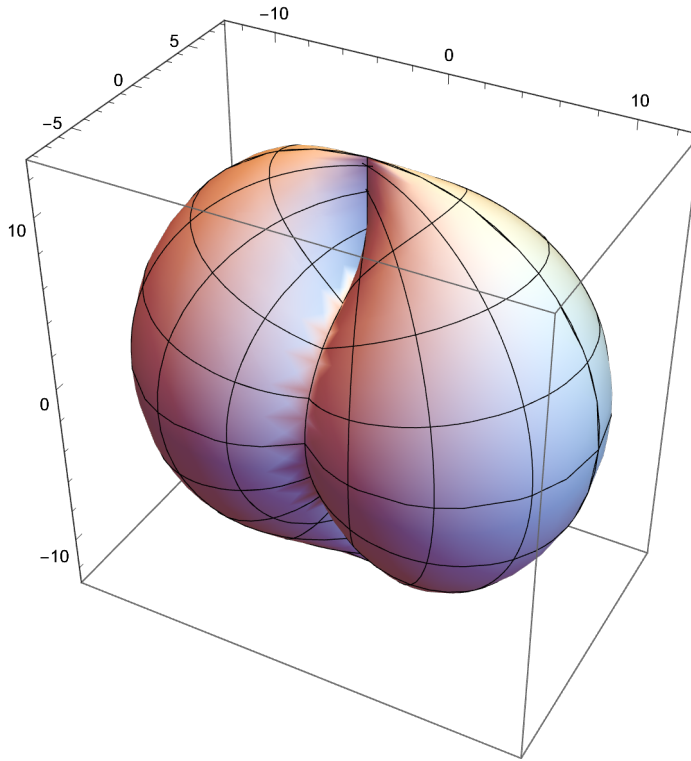
$\left\{ \left\{ \theta \rightarrow \left( 4\pi\cos[\alpha]^4 + 8\pi\cos[\alpha]^2\sin[\alpha]^2 + 4\pi\sin[\alpha]^4 - \sqrt{\left( (-4\pi\cos[\alpha]^4 - 8\pi\cos[\alpha]^2\sin[\alpha]^2 - 4\pi\sin[\alpha]^4)^2 - 16\pi^2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4)\sin[\beta]^2 \right)} \right) / \left( 2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4) \right) \right\}, \right.$   
 $\left. \left\{ \theta \rightarrow \left( 4\pi\cos[\alpha]^4 + 8\pi\cos[\alpha]^2\sin[\alpha]^2 + 4\pi\sin[\alpha]^4 + \sqrt{\left( (-4\pi\cos[\alpha]^4 - 8\pi\cos[\alpha]^2\sin[\alpha]^2 - 4\pi\sin[\alpha]^4)^2 - 16\pi^2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4)\sin[\beta]^2 \right)} \right) / \left( 2(\cos[\alpha]^4 + 2\cos[\alpha]^2\sin[\alpha]^2 + \sin[\alpha]^4) \right) \right\} \right\}$

SphericalPlot3D[ $\left(4 \pi \cos[\alpha]^4 + 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 + 4 \pi \sin[\alpha]^4 + \sqrt{\left((-4 \pi \cos[\alpha]^4 - 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 - 4 \pi \sin[\alpha]^4)^2 - 16 \pi^2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4) \sin[\beta]^2\right)}\right) / (2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4))$ ,  $\{\alpha, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}$ ]

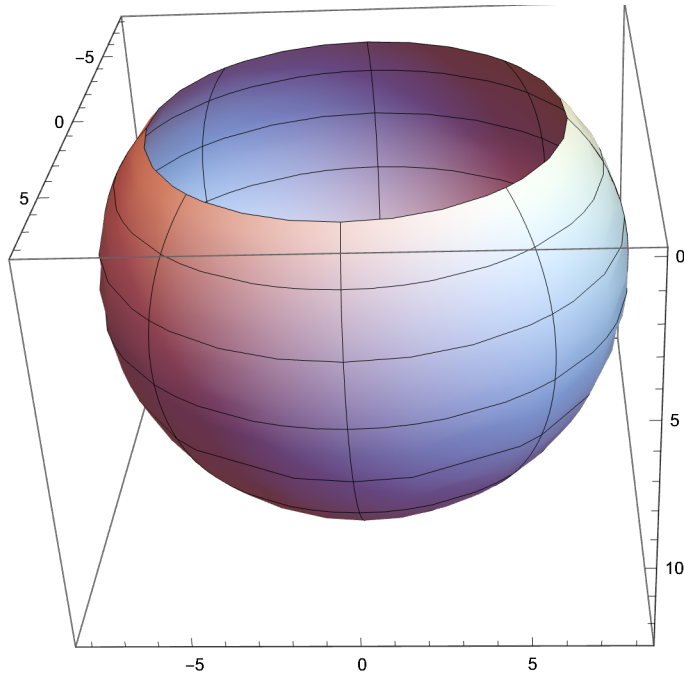




$\text{SphericalPlot3D}\left[\frac{\left(4\pi\cos^4[\alpha] + 8\pi\cos^2[\alpha]\sin^2[\alpha] + 4\pi\sin^4[\alpha] + \sqrt{\left((-4\pi\cos^4[\alpha] - 8\pi\cos^2[\alpha]\sin^2[\alpha] - 4\pi\sin^4[\alpha])^2 - 16\pi^2(\cos^4[\alpha] + 2\cos^2[\alpha]\sin^2[\alpha] + \sin^4[\alpha])\sin^2[\beta])}\right)}{2(\cos^4[\alpha] + 2\cos^2[\alpha]\sin^2[\alpha] + \sin^4[\alpha])}\right], \{\alpha, -\pi, \pi\}, \{\beta, -\pi, \pi\}]$



SphericalPlot3D[ $\left(4 \pi \cos[\alpha]^4 + 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 + 4 \pi \sin[\alpha]^4 + \sqrt{\left((-4 \pi \cos[\alpha]^4 - 8 \pi \cos[\alpha]^2 \sin[\alpha]^2 - 4 \pi \sin[\alpha]^4)^2 - 16 \pi^2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4) \sin[\beta]^2\right)}\right) / (2 (\cos[\alpha]^4 + 2 \cos[\alpha]^2 \sin[\alpha]^2 + \sin[\alpha]^4))$ ,  $\{\beta, -\pi/2, \pi/2\}$ ,  $\{\alpha, -2\pi, 2\pi\}$ ]



$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

$$D\left[D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \beta\right]$$

$$- \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \right.$$

$$\begin{aligned}
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \quad \left( 8 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 2 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \Bigg) \\
& \quad \left( \left( 8 \pi \theta \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \\
& \quad \left. \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \quad \left( 2 \theta^2 \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\pi^2 (4\pi - 2\theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4\pi - \theta) \theta}} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \Bigg) \\
& \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 - \\
& \left( 8\pi\theta (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \operatorname{Sin}[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \operatorname{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^3 + \\
& \left( 2\theta^2 (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \operatorname{Sin}[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \operatorname{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^3 + \\
& \left( 4\pi \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 - \\
& \left( 2\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 \Bigg) \Bigg) / \\
& \left( 8\pi \left( \left( 4\pi\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta] + 4\pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \operatorname{Sin}[\beta]^2 + 8\pi^2\theta \operatorname{Sin}[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( \theta^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^{3/2} \Bigg) + \\
& \left( \left( 8\pi\theta \left( 2\pi\sqrt{(4\pi-\theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi-\theta} - \right. \right. \right. \\
& \quad \left. \left. \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 - \\
& \left( 2\theta^2 \left( 2\pi\sqrt{(4\pi-\theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi-\theta} - \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 + \\
& \left( 8\pi\theta \left( \frac{\pi(4\pi-2\theta)\cos[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{3\pi^2(4\pi-2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi-2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi-\theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi-\theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( \frac{\pi (4 \pi - 2 \theta) \operatorname{Cos}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{(4 \pi - \theta)^2} + \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \quad \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2) \right. \\
& \quad \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \right. \right. \\
& \quad \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \Bigg) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \quad \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] + 8 \pi^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Cos}[\beta] \operatorname{Sin}[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \quad \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 24 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^4 - \\
& \left( 6 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^4 - \\
& \left( 128 \pi^3 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 32 \pi^2 \theta^2 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 - \\
& \left( 8 \pi \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/
\end{aligned}$$



$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 \Bigg/ \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg)
\end{aligned}$$

SphericalPlot3D[

$$\begin{aligned}
& - \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 2\theta^2(-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 \right) \\
& \left( \left( 8\pi\theta \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \right. \\
& \quad \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 8 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \quad \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 2 \theta^2 \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \quad \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 4 \pi \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Big) / \\
& \left( 8 \pi \left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) /
\end{aligned}$$

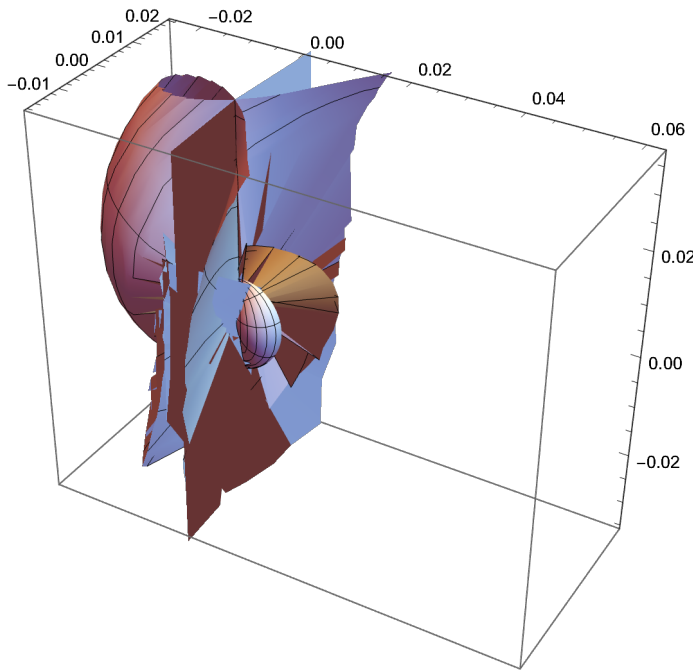
$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^{3/2} \Bigg) + \\
& \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& \left( 8 \pi \theta \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \\
& \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 16 \pi \theta (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 16 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 24 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 6 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 128 \pi^3 \theta \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 32 \pi^2 \theta^2 \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 - \\
& \left( 8 \pi (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left. \left. \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \right) \right) \right) / \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \right. \\
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left. \left. \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) \right) \right), \\
& \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \right. \\
& - \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left( \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 2 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 \Bigg) \\
& \left( \left( 8 \pi \theta \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\pi^2 (4\pi - 2\theta) \sin[\beta]^3}{\theta \sqrt{(4\pi - \theta) \theta}} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{(4\pi - \theta)^2} + \\
& \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta) \sin[\beta]}{\sqrt{(4\pi - \theta) \theta}} - \frac{\pi^2 (4\pi - 2\theta) \sin[\beta]^3}{(4\pi - \theta) \sqrt{(4\pi - \theta) \theta}} - \right. \right. \\
& \left. \frac{\pi^2 (4\pi - 2\theta) \sin[\beta]^3}{\theta \sqrt{(4\pi - \theta) \theta}} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{(4\pi - \theta)^2} + \right. \\
& \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 8\pi\theta (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \left. \left. \pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 2\theta^2 (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \left. \left. \pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4\pi \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 -
\end{aligned}$$

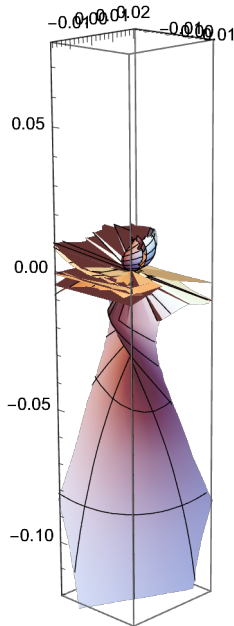
$$\begin{aligned}
& \left( 2 \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg) / \\
& \left( 8 \pi \left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg)^{3/2} \Bigg) + \\
& \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& \left( 8\pi\theta \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 16\pi\theta(16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2\sin[\beta]^2) \right. \\
& \quad \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \right. \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 +
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( 16 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) /
\end{aligned}$$

$$\begin{aligned}
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 24 \pi \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 6 \theta^2 (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 128 \pi^3 \theta \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 +
\end{aligned}$$

$$\begin{aligned}
& \left( 32 \pi^2 \theta^2 \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 - \\
& \left( 8 \pi (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \Bigg) / \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Bigg) \Bigg), \\
& (0 - 12 - 12) (0 - 2 - 2 - 1)
\end{aligned}$$

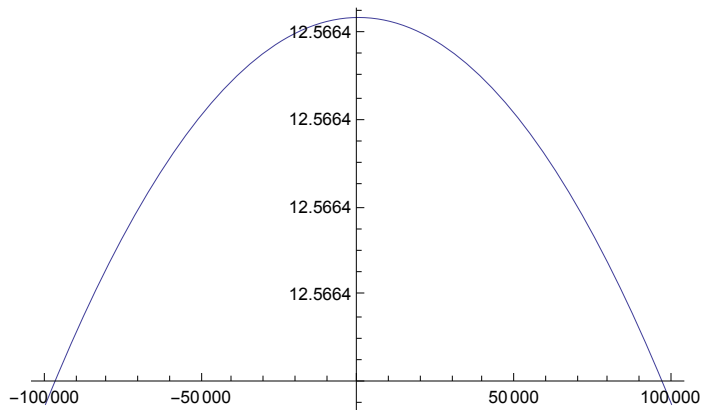


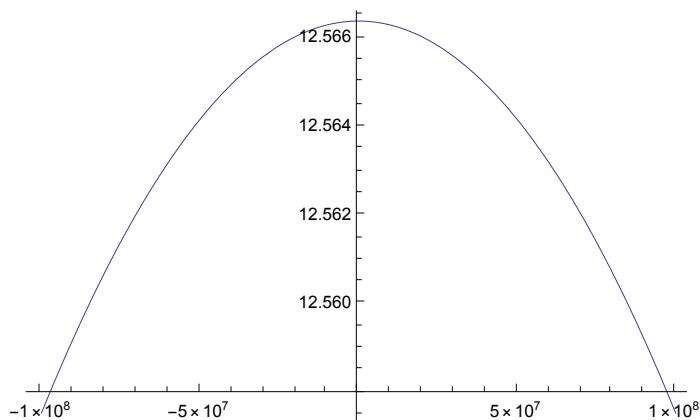
$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \theta\right]$$

$$\left\{\left\{\theta \rightarrow \left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 - 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1. \cdot 10^{18} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right)\right\}, \left\{\theta \rightarrow \left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 + 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1. \cdot 10^{18} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right)\right\}\right\}$$



$$\text{Plot}\left[\left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 + 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1 \cdot 10^{22} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right), \{r, -1 \cdot 10^5, 1 \cdot 10^5\}\right]$$

$$\text{Plot}\left[\left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 + 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1 \cdot 10^{22} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right), \{r, -1 \cdot 10^5, 1 \cdot 10^5\}\right]$$


$$\text{Plot}\left[\left(0.5 \cdot \left(2.697911582835683 \cdot 10^{41} + 7.60372795068286 \cdot 10^{22} r^2 + 1.4322774071693905 \cdot 10^{32} \sqrt{3.548143227025099 \cdot 10^{18} + 1 \cdot 10^{22} r^2}\right)\right) / \left(2.1469298221658919 \cdot 10^{40} + 6.050854446385924 \cdot 10^{21} r^2\right), \{r, -1 \cdot 10^8, 1 \cdot 10^8\}\right]$$


Solve[

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), r]$$

$$\left\{ \left\{ r \rightarrow - \frac{1. \sqrt{2.69791 \times 10^{41} - 2.14693 \times 10^{40} \theta} \sqrt{\theta}}{\sqrt{2.38878 \times 10^{23} - 7.60373 \times 10^{22} \theta + 6.05085 \times 10^{21} \theta^2}} \right\}, \right.$$

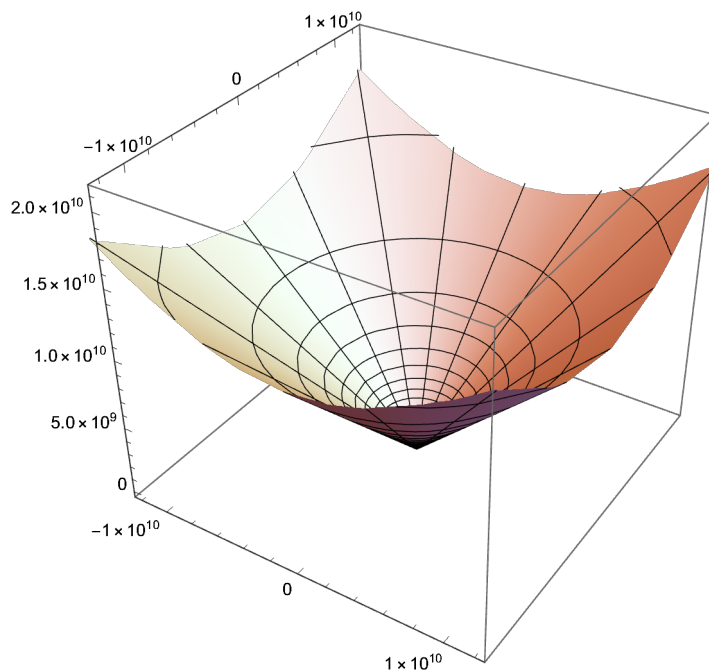
$$\left. \left\{ r \rightarrow \frac{\sqrt{2.69791 \times 10^{41} - 2.14693 \times 10^{40} \theta} \sqrt{\theta}}{\sqrt{2.38878 \times 10^{23} - 7.60373 \times 10^{22} \theta + 6.05085 \times 10^{21} \theta^2}} \right\} \right\}$$

$$\text{RevolutionPlot3D} \left[ \left\{ - \left( 1. \sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta} \right) / \right. \right.$$

$$\left. \left( \sqrt{2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2} \right) \right\},$$

$$\left( \sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta} \right) /$$

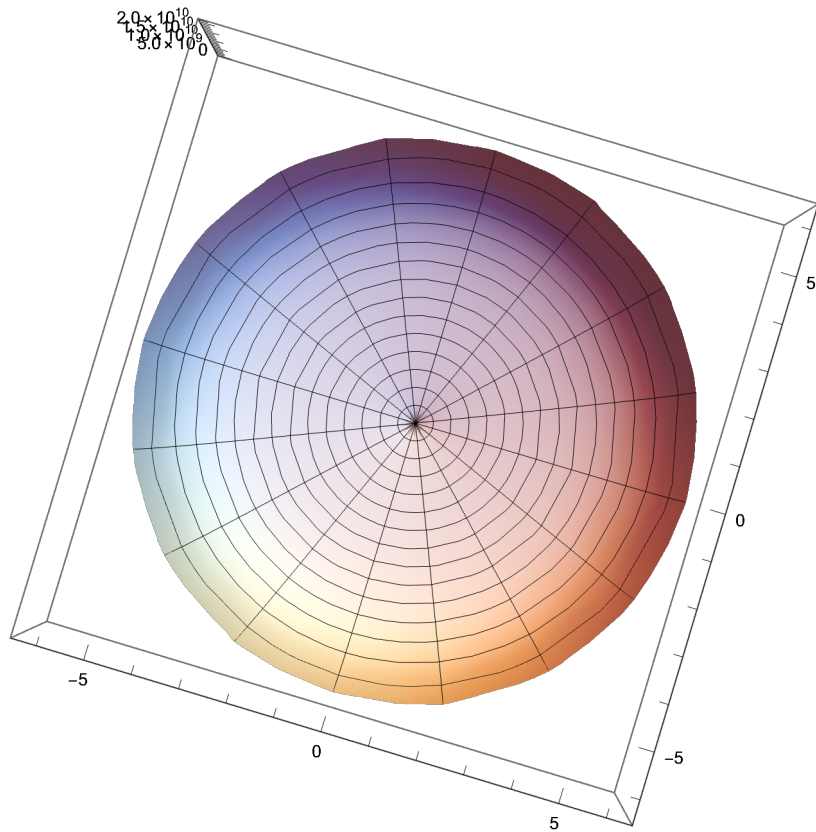
$$\left( \sqrt{2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2} \right) \right\}, \{\theta, -2 \pi, 2 \pi\}]$$



```
RevolutionPlot3D[ (  $\sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta}$  ) /  

  (  $\sqrt{2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2}$  ) ) ,  

  {  $\theta$  , -2  $\pi$  , 2  $\pi$  } ]
```



$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

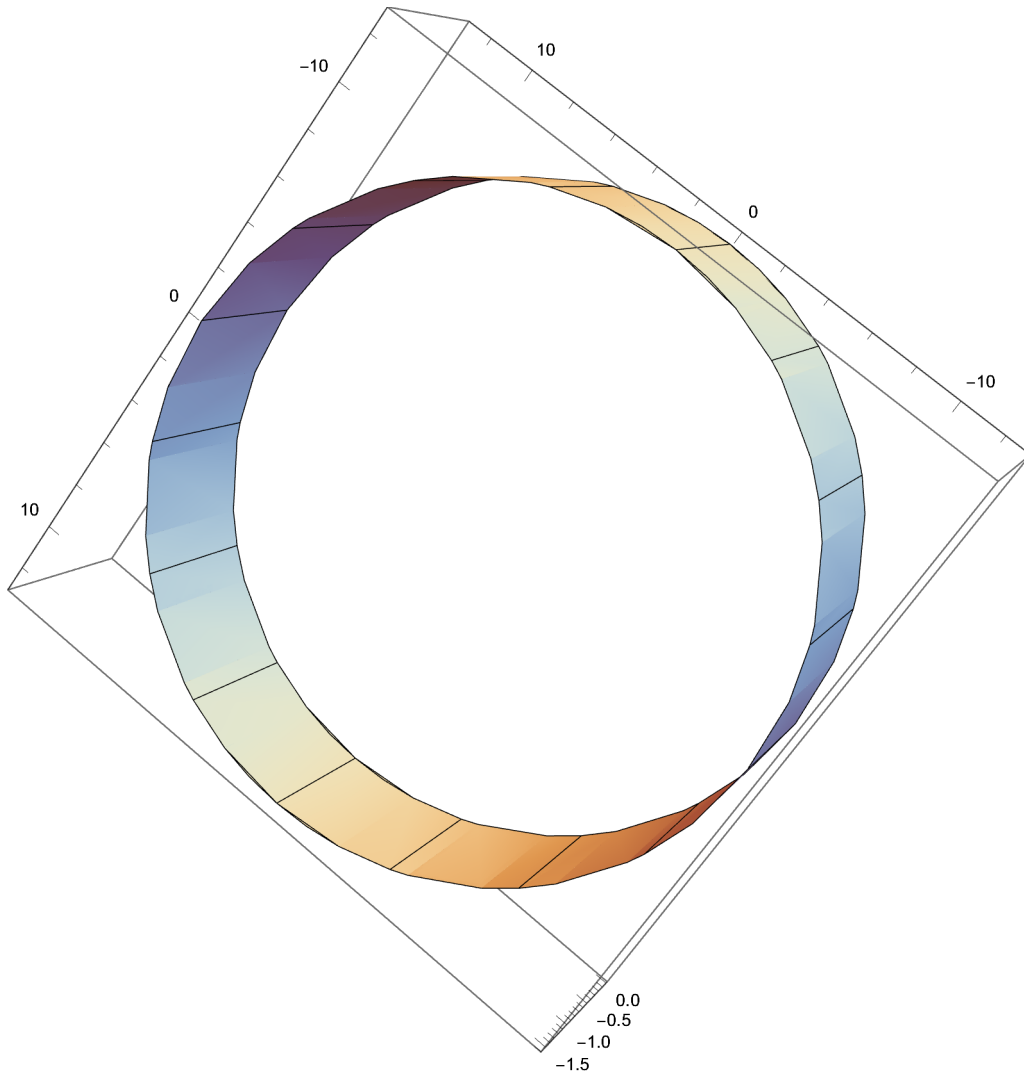
$$\frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Solve}\left[\left(\sqrt{2.697911582835683 \cdot 10^{41} - 2.1469298221658919 \cdot 10^{40} \theta} \sqrt{\theta}\right) / \left(\sqrt{\left(2.3887815869760647 \cdot 10^{23} - 7.60372795068286 \cdot 10^{22} \theta + 6.050854446385924 \cdot 10^{21} \theta^2\right)}\right) == \left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / \left(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right), \beta\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[2.05971 \times 10^{-25} \left(7.72706 \times 10^{23} \sqrt{12.5664 \theta - 1. \theta^2} - \frac{2.41639 \times 10^8 \sqrt{12.5664 \theta - 1. \theta^2}}{12.5664 - 1. \theta} - \frac{1.14922 \times 10^{35} \sqrt{\theta} \sqrt{12.5664 \theta - 1. \theta^2}}{\sqrt{12.5664 - 1. \theta} \sqrt{39.4784 - 12.5664 \theta + \theta^2}} + \frac{1.82905 \times 10^{34} \sqrt{12.5664 - 1. \theta} \sqrt{\theta} \sqrt{12.5664 \theta - 1. \theta^2}}{\sqrt{39.4784 - 12.5664 \theta + \theta^2}} + \frac{2.91102 \times 10^{33} \sqrt{\theta} \sqrt{12.5664 \theta - 1. \theta^2} \sqrt{39.4784 - 12.5664 \theta + \theta^2}}{\sqrt{12.5664 - 1. \theta}}\right)\right]\right\}}$$

$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[2.0597093504953005 \cdot 10^{-25} \left(7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 - 1. \theta} - \frac{\left(1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2}\right)}{\left(\sqrt{12.566370614359172 - 1. \theta} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2}\right)} + \frac{\left(1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 - 1. \theta} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2}\right)}{\left(\sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2}\right)} + \frac{\left(2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2}\right)}{\left(\sqrt{12.566370614359172 - 1. \theta}\right)}\right]\right], \{\beta, -4 \pi, 8 \pi / 2\}]$$



$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[1000 \beta]^2} \right)$$

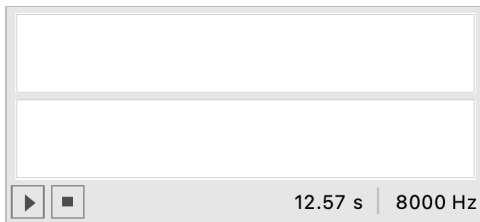
$$\theta := \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} +$$

$$\frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}$$

Play[ArcSin[

$$\begin{aligned}
 & 2.0597093504953005 \cdot 10^{-25} \left( 7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \right. \\
 & \quad \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 \theta - 1. \theta} \\
 & \quad \left. \left( 1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \right. \\
 & \quad \left( \sqrt{12.566370614359172 \theta - 1. \theta} \sqrt{39.47841760435743 \theta - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \quad \left. \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{39.47841760435743 \theta - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 & \quad \quad \left. \sqrt{39.47841760435743 \theta - 12.56637061435917 \theta + \theta^2} \right) / \\
 & \quad \left. \left( \sqrt{12.566370614359172 \theta - 1. \theta} \right) \right] \Bigg], \{\beta, -2\pi, 2\pi\}
 \end{aligned}$$

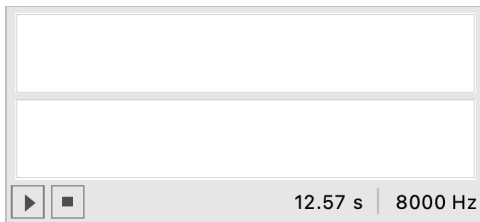
Sound::ssnm: A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>



Play[ArcSin[

$$\begin{aligned}
 & 2.0597093504953005 \cdot 10^{-25} \left( 7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \right. \\
 & \quad \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 \theta - 1. \theta} \\
 & \quad \left. \left( 1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \right. \\
 & \quad \left( \sqrt{12.566370614359172 \theta - 1. \theta} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \left. \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 & \quad \left. \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) / \\
 & \quad \left. \left( \sqrt{12.566370614359172 \theta - 1. \theta} \right) \right] \Bigg], \{\beta, -2\pi, 2\pi\}
 \end{aligned}$$

Sound::ssnm: A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>



"ribbit.wav"

Export["ribbit.wav",

Play[ $\sqrt{12.566370614359172 \sin[1000 \theta] - 1. \cos[1000 \theta]^2}$ , { $\beta$ ,  $-\pi$ ,  $\pi$ }]]

Sound::ssnm: A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>

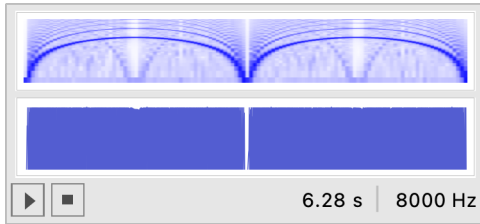
LinkObject::linkw: Unable to write data to closed link LinkObject[

/Applications/Mathematica.app/SystemFiles/Converters/Binaries/MacOSX-x86-64/Audio.exe, 25, 9]. >>

\$Failed

```
Play[ $\sqrt{12.566370614359172 \sin[1000 \theta] - 1. \cos[1000 \theta]^2}$ , { $\theta$ ,  $-\pi$ ,  $\pi$ }]
```

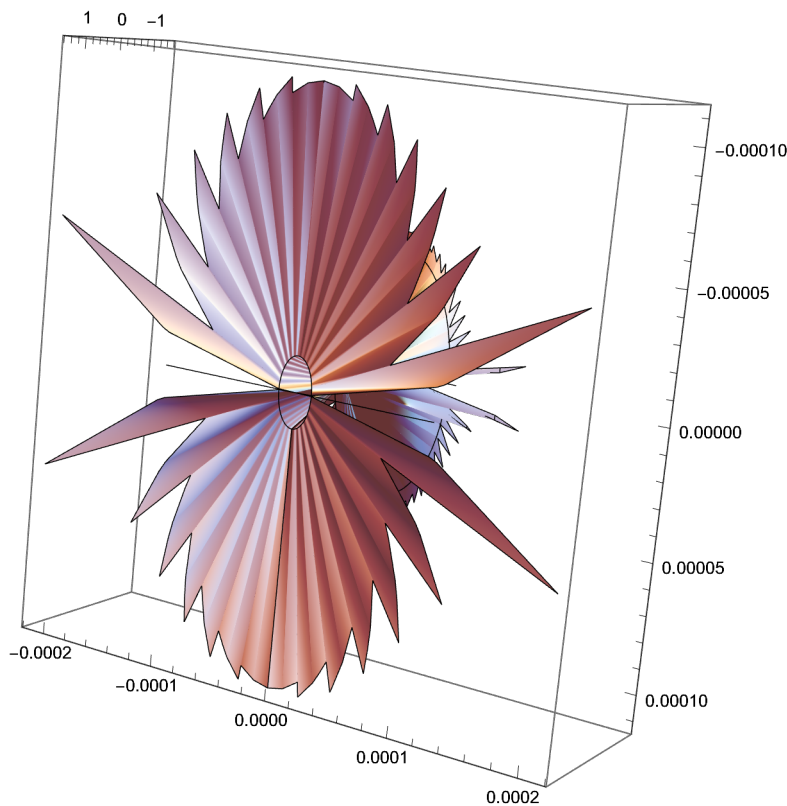
Sound::ssnm : A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>





RevolutionPlot3D[ArcSin[

$$\begin{aligned}
 & 2.0597093504953005 \cdot 10^{-25} \left( 7.727058337314591 \cdot 10^{23} \sqrt{12.566370614359172 \theta - 1. \theta^2} - \right. \\
 & \quad \frac{2.4163860935781455 \cdot 10^8 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{12.566370614359172 \theta - 1. \theta} \\
 & \quad \left. \left( 1.1492234910439907 \cdot 10^{35} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \right. \\
 & \quad \left( \sqrt{12.566370614359172 \theta - 1. \theta} \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 1.8290459931697553 \cdot 10^{34} \sqrt{12.566370614359172 \theta - 1. \theta} \right. \\
 & \quad \quad \left. \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right) / \\
 & \quad \left( \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) + \\
 & \quad \left( 2.911017109553914 \cdot 10^{33} \sqrt{\theta} \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
 & \quad \quad \left. \sqrt{39.47841760435743 - 12.56637061435917 \theta + \theta^2} \right) / \\
 & \quad \left. \left( \sqrt{12.566370614359172 \theta - 1. \theta} \right) \right], \{\theta, -2\pi, 2\pi\}
 \end{aligned}$$

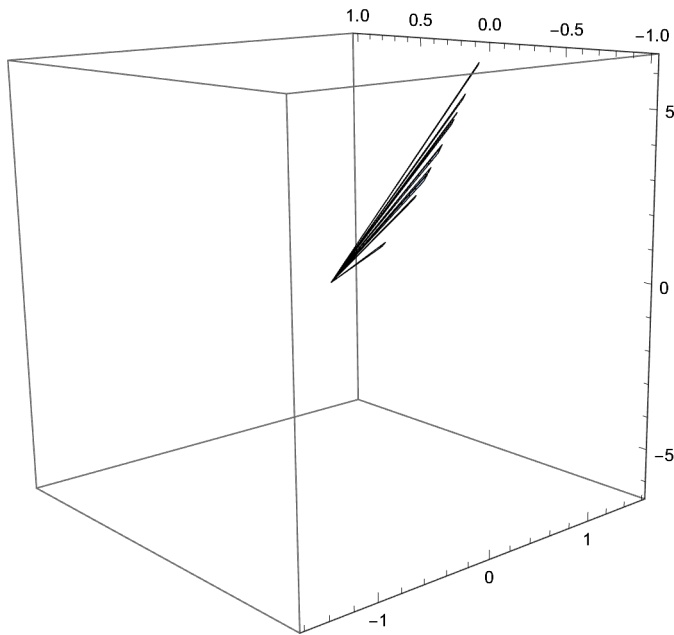


ContourPlot3D[

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) ==$$

$$\sqrt{(- (256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})) ,$$

{ $\theta$ ,  $-2\pi$ ,  $2\pi$ }, { $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }, { $\eta$ ,  $-1$ ,  $1$ }]



Export["r=r.3ds", ContourPlot3D[

$$\left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) ==$$

$$\sqrt{(- (256 \pi^7 \eta^2 \theta^3) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + (320 \pi^6 \eta^2 \theta^4) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) - (128 \pi^5 \eta^2 \theta^5) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + (16 \pi^4 \eta^2 \theta^6) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}) + (128 \pi^6 \sqrt{(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8)}) / (-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10})) ,$$

$$\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}, \{\eta, -1, 1\}]]$$

r=r.3ds

$$\text{Solve}\left[\frac{2 \pi (2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2})}{\theta^2} == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \eta\right]$$

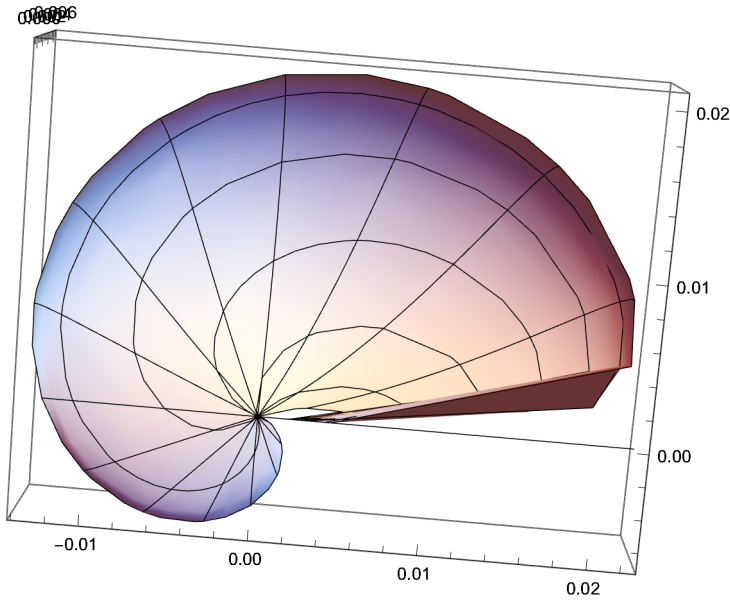
$$\left\{ \left\{ \eta \rightarrow -\frac{1}{4 \pi^2} \left( \sqrt{64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta}} \right) \right\} \right\},$$

$$\left\{ \eta \rightarrow \frac{1}{4 \pi^2} \left( \sqrt{64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta}} \right) \right\} \right\}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

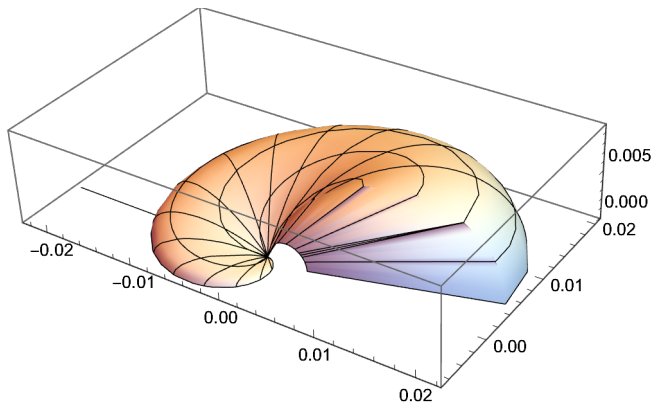
SphericalPlot3D[

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$



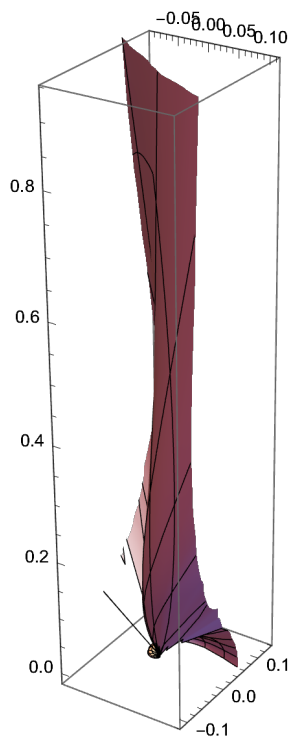
SphericalPlot3D[

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right)} \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$

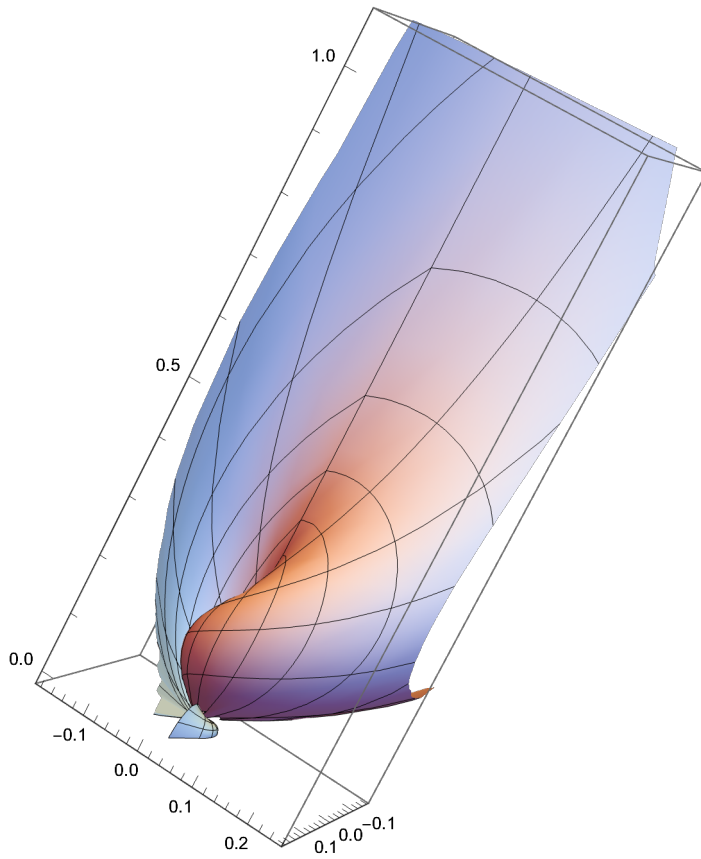


SphericalPlot3D[

$$\frac{1}{4 \pi^2} \left( \sqrt{\left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r^2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \sqrt{r^2 \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} \right)}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\} \right]$$



$\text{SphericalPlot3D}\left[\frac{1}{4\pi^2}\left(\sqrt{\left(64\pi^4r^2-\frac{256\pi^5r^2}{4\pi-\theta}+16\pi^3r^2\theta+4\pi^2r^2\theta^2+r^2\theta^4+\right.}\right.\right.$   
 $\left.\left.16\pi^3r\sqrt{r^2\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\theta}-\frac{64\pi^4r\sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta}+\right.\right.$   
 $\left.\left.8\pi^2r^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\sqrt{r^2\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)\theta}\right)\right],$   
 $\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$



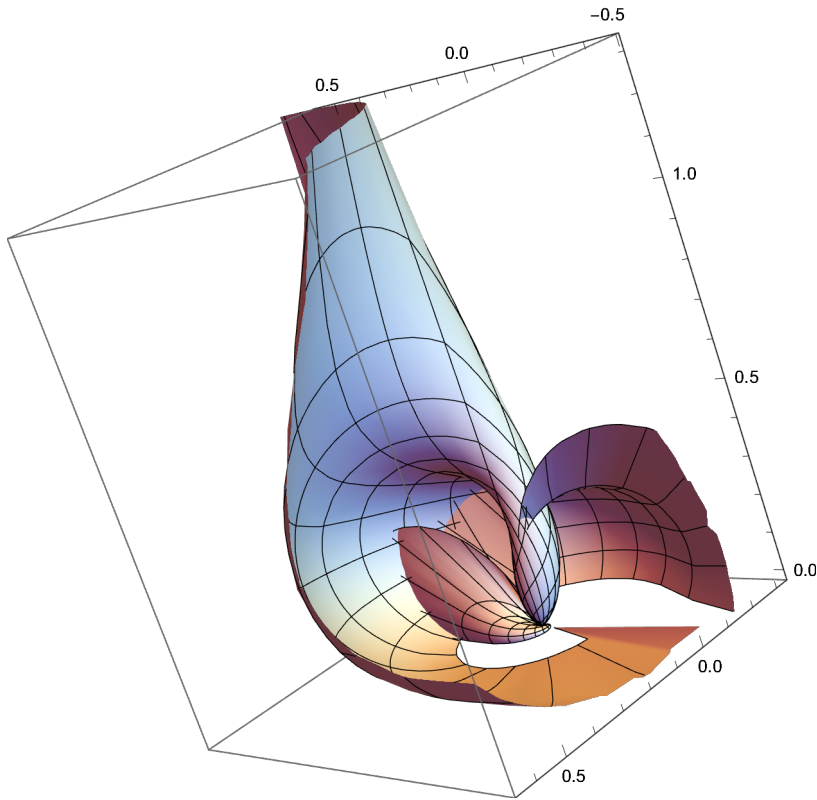
SphericalPlot3D[

$$\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + \right.} \right.$$

$$\left. 16\pi^3 r \sqrt{r^2 \left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + \right.$$

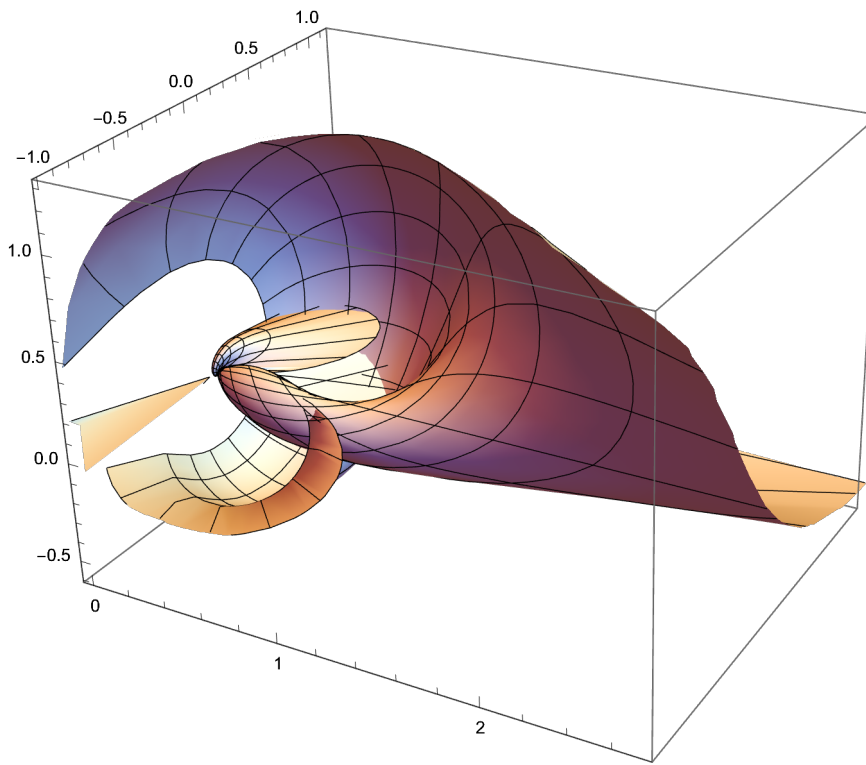
$$\left. 8\pi^2 r 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \sqrt{r^2 \left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} \right),$$

$$\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



SphericalPlot3D[

$$\frac{1}{4 \pi^2} \left( \sqrt{\left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 4 \pi^2 r^2 \theta^2 + r^2 \right.} \right. \\ \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 + 16 \pi^3 r \sqrt{r^2 \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} - \right. \\ \left. \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r^2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right. \\ \left. \left. \sqrt{r^2 \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} \right) \right], \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



q



$$\text{Solve}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right) / \right. \\ \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \sqrt{-(256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})} + \right. \\ \left. (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})\right), \eta]$$

General::ivar : 1 is not a valid variable. >>

General::ivar : 1 is not a valid variable. >>

$$\text{Solve}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right) / \right. \\ \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \sqrt{-(256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})} + \right. \\ \left. (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - \right. \\ \left. (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})\right), \{\eta, -1, 1\}]$$

ContourPlot3D[

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) ==$$

$$\sqrt{(- (256\pi^7\eta^2\theta^3) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})) , \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}, \{\eta, -1, 1\}]$$

$$\iint \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} d\theta d\beta == D\left[D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right], \beta\right]$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

$$D\left[D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right], \beta\right]$$

$$- \left( \left( \left( 8\pi\theta \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \left( 2\theta^2 \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right) \right)$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 8\pi\theta (-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 2\theta^2 (-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 \Big) \\
& \left( \left( 8\pi\theta \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \right. \\
& \quad \left. \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( -4\pi + 2\theta + \frac{\pi(4\pi-2\theta)\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}} - \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{(4\pi-\theta)\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \left. \frac{\pi^2(4\pi-2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{(4\pi-\theta)^2} + \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 - \\
& \left( 8\pi\theta (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^3 + \\
& \left( 2\theta^2 (16\pi^2 - 24\pi\theta + 6\theta^2 + 8\pi^2 \sin[\beta]^2) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^3 + \\
& \left( 4\pi \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 - \\
& \left( 2\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 \Big) / \\
& \left( 8\pi \left( \left( 4\pi\theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 - \\
& \left. \left( \theta^2 \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^{3/2} \Bigg) + \\
& \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& \left( 8 \pi \theta \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \\
& \quad \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( \frac{\pi (4 \pi - 2 \theta) \cos[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \left. \frac{3 \pi^2 (4 \pi - 2 \theta) \cos[\beta] \sin[\beta]^2}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{(4 \pi - \theta)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta^2} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \right. \\
& \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^2 - \\
& \left( 16 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \operatorname{Sin}[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \operatorname{Sin}[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta^2} \right) \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 4 \pi^2 \operatorname{Sin}[\beta]^2 - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^3 + \\
& \left( 24 \pi \theta \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \right. \\
& \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \right. \\
& \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right)^4 - \\
& \left( 6 \theta^2 \left( -32 \pi^3 \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] + 16 \pi^2 \theta \operatorname{Cos}[\beta] \operatorname{Sin}[\beta] \right) \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \operatorname{Sin}[\beta]^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 - \\
& \left( 128\pi^3\theta\cos[\beta]\sin[\beta] \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 32\pi^2\theta^2\cos[\beta]\sin[\beta] \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 - \\
& \left( 8\pi(-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 + \\
& \left( 4\theta(-32\pi^3\cos[\beta]\sin[\beta] + 16\pi^2\theta\cos[\beta]\sin[\beta]) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^3 \Bigg) \Bigg/ \\
& \left( 4\pi\sqrt{\left( \left( 4\pi\theta \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \left( \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) \Bigg)
\end{aligned}$$

SphericalPlot3D[

$$\begin{aligned}
& - \left( \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 2 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 \Bigg) \\
& \left( \left( 8 \pi \theta \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 2 \theta^2 \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \left. \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 8 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 +
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \theta^2 (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \right. \right. \\
& \quad \left. \left. \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 4 \pi \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
& \quad \left( 2 \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big) / \\
& \quad \left( 8 \pi \left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \right. \\
& \quad \left. \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right)^{3/2} \Big) + \\
& \quad \left( \left( 8 \pi \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right) \right)
\end{aligned}$$

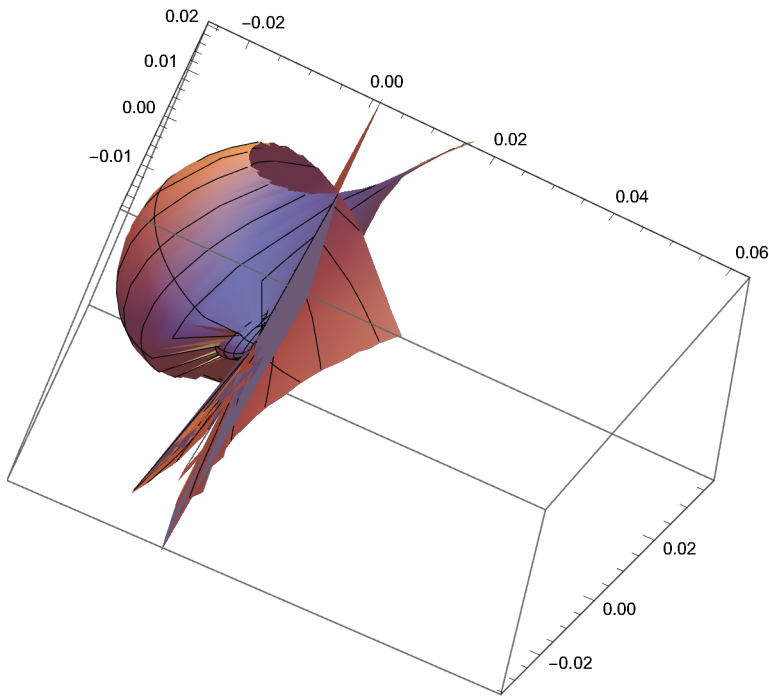
$$\begin{aligned}
& \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( 2\pi\sqrt{(4\pi - \theta)\theta}\cos[\beta] + 8\pi^2\cos[\beta]\sin[\beta] - \right. \right. \\
& \quad \left. \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{4\pi - \theta} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta} \right) \right. \\
& \quad \left( -4\pi + 2\theta + \frac{\pi(4\pi - 2\theta)\sin[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \frac{\pi^2(4\pi - 2\theta)\sin[\beta]^3}{\theta\sqrt{(4\pi - \theta)\theta}} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{(4\pi - \theta)^2} + \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta^2} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& \left( 8\pi\theta \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 - \\
& \left( 2\theta^2 \left( \frac{\pi(4\pi - 2\theta)\cos[\beta]}{\sqrt{(4\pi - \theta)\theta}} - \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \quad \frac{3\pi^2(4\pi - 2\theta)\cos[\beta]\sin[\beta]^2}{\theta\sqrt{(4\pi - \theta)\theta}} - \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{(4\pi - \theta)^2} + \\
& \quad \left. \frac{6\pi^2\sqrt{(4\pi - \theta)\theta}\cos[\beta]\sin[\beta]^2}{\theta^2} \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi \theta \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \right. \\
& \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \\
& \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 4 \theta^2 \left( 16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2 \right) \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^3 + \\
& \left( 8 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \left( 4 \theta \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \cos[\beta] + 8 \pi^2 \cos[\beta] \sin[\beta] - \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{6 \pi^2 \sqrt{(4 \pi - \theta) \theta} \cos[\beta] \sin[\beta]^2}{\theta} \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 4 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \quad \left( -4 \pi + 2 \theta + \frac{\pi (4 \pi - 2 \theta) \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{(4 \pi - \theta) \sqrt{(4 \pi - \theta) \theta}} - \frac{\pi^2 (4 \pi - 2 \theta) \sin[\beta]^3}{\theta \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(4 \pi - \theta)^2} + \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \quad \left( 24 \pi \theta \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) \right. \\
& \quad (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \quad \left( 6 \theta^2 \left( -32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta] \right) (16 \pi^2 - 24 \pi \theta + 6 \theta^2 + 8 \pi^2 \sin[\beta]^2) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 128 \pi^3 \theta \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 32 \pi^2 \theta^2 \cos[\beta] \sin[\beta] \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 - \\
& \left( 8 \pi (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 + \\
& \left( 4 \theta (-32 \pi^3 \cos[\beta] \sin[\beta] + 16 \pi^2 \theta \cos[\beta] \sin[\beta]) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^3 \Bigg/ \\
& \left( 4 \pi \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \right.
\end{aligned}$$

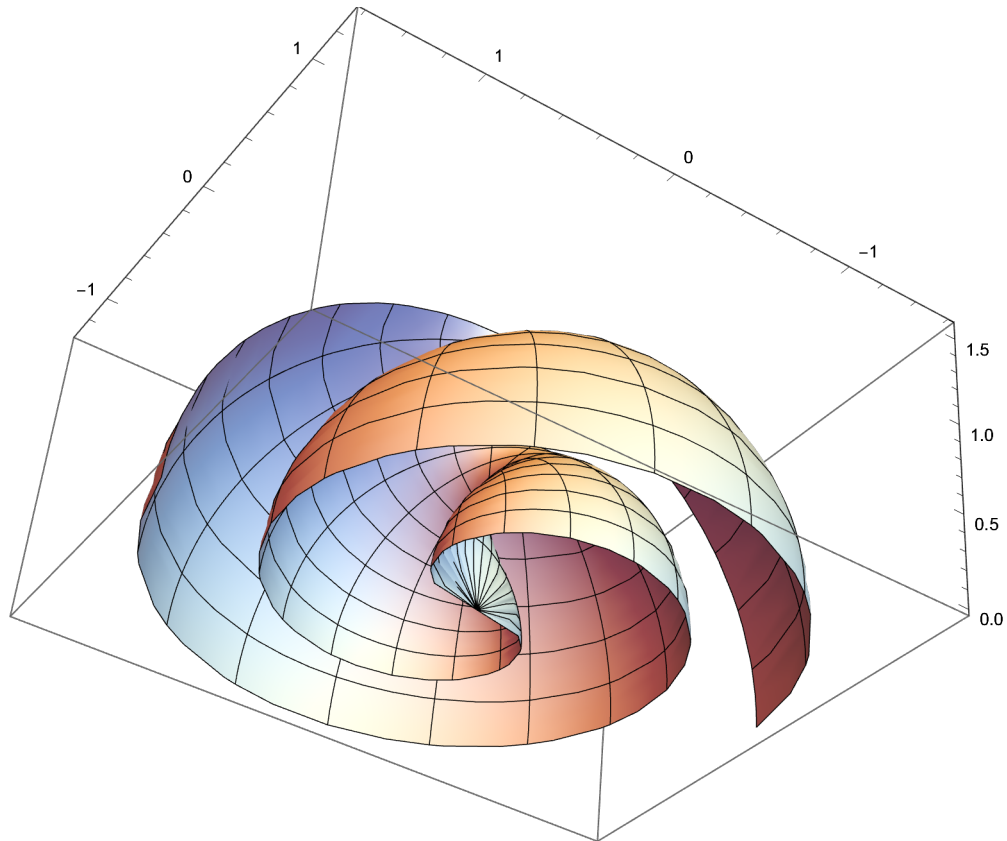
$$\begin{aligned}
 & \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 / \\
 & (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \\
 & \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
 & \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
 & (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Bigg), \\
 & \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}
 \end{aligned}$$



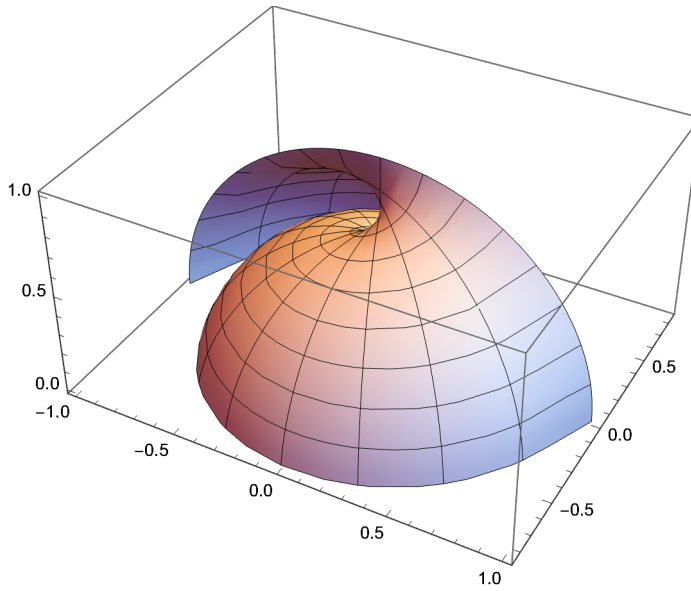
$$\left( \frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}} \right) \frac{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}{4 \pi}$$



$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{1}{2\pi}\left(\sqrt{(4\pi-\theta)\theta}\cos\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2+\sqrt{(4\pi-\theta)\theta}\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2\right)\right],\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$$



SphericalPlot3D $\left[\left(\frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}}\right)^{\frac{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4 \pi}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}\right]$

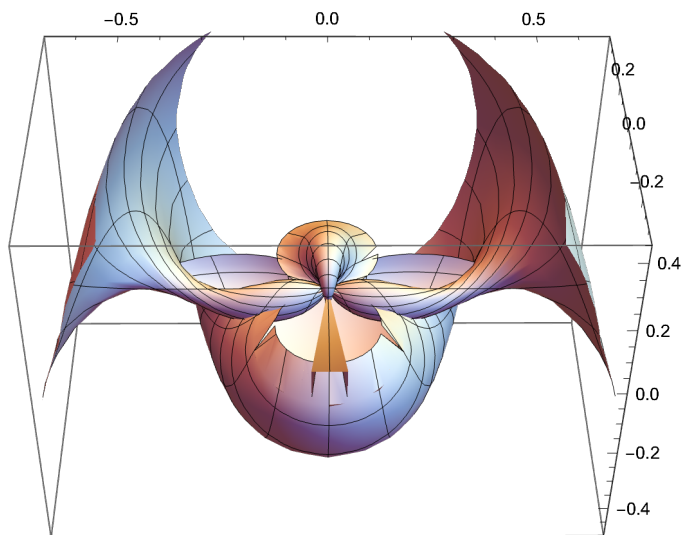


Solve $\left[\left(\frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}}\right)^{\frac{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4 \pi}} == \right.$   
 $\left. \text{ArcSin}\left[\frac{1}{2 \pi} \left(\sqrt{(4 \pi - \theta) \theta} \cos\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 + \right.\right.\right.$   
 $\left.\left.\sqrt{(4 \pi - \theta) \theta} \sin\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2\right)\right], \beta\right]$

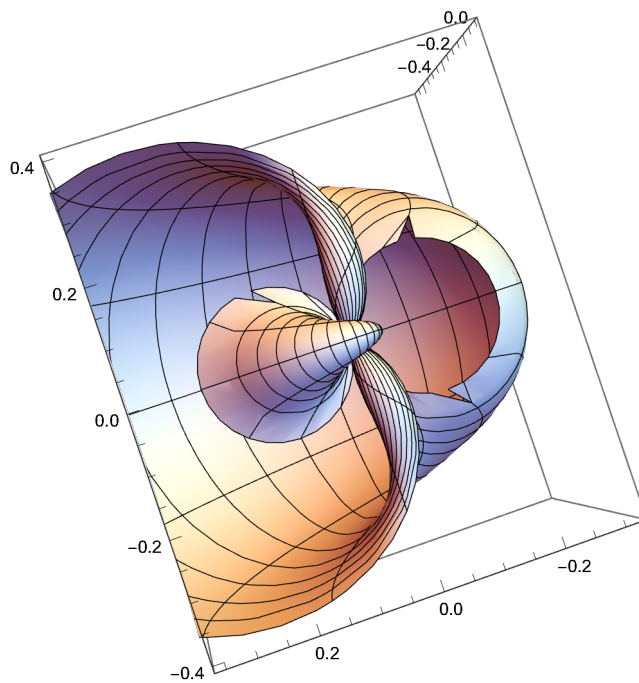
Solve::tdep : The equations appear to involve the variables to be solved for in an essentially non-algebraic way. >>

Solve $\left[\left(\frac{i \sqrt{\theta}}{2 \sqrt{\pi}} + \sqrt{1 - \frac{\theta}{4 \pi}}\right)^{\frac{\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}}{2 \pi}} == \text{ArcSin}\left[\frac{1}{2 \pi} \left(\sqrt{(4 \pi - \theta) \theta} \cos\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 + \right.\right.\right.$   
 $\left.\left.\sqrt{(4 \pi - \theta) \theta} \sin\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2\right)\right], \beta\right]$

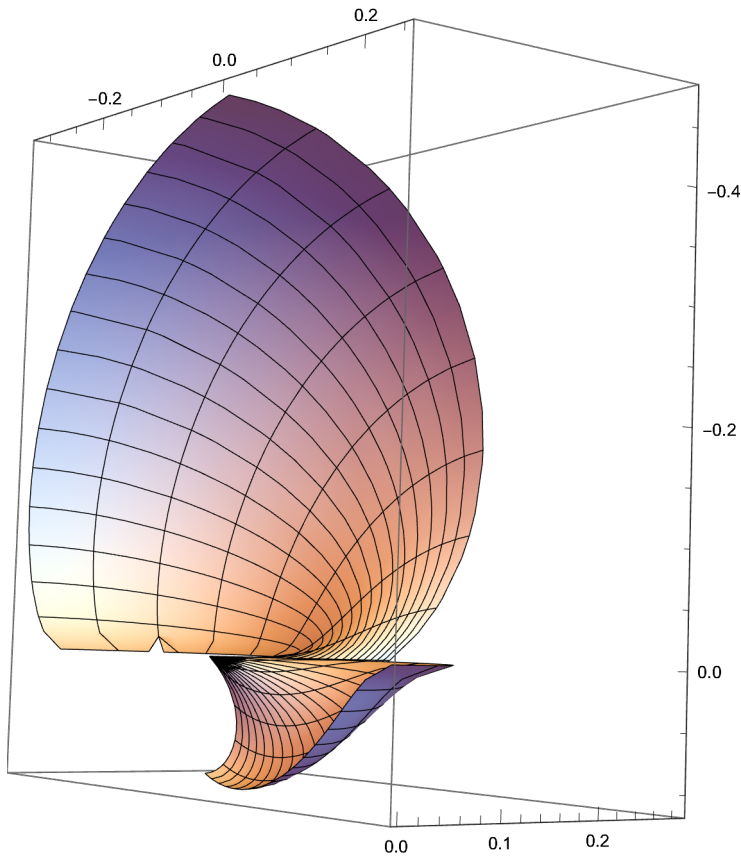
$\text{SphericalPlot3D}\left[\frac{\theta (2 \pi r^2 - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta)} \theta}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$\text{SphericalPlot3D}\left[\frac{\theta (2 \pi r^2 - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta)} \theta}, \{\beta, -\pi, \pi\}, \{\theta, -\pi, \pi\}\right]$



SphericalPlot3D $\left[\frac{\theta (2 \pi r^2 - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -\pi/2, \pi/2\}\right]$



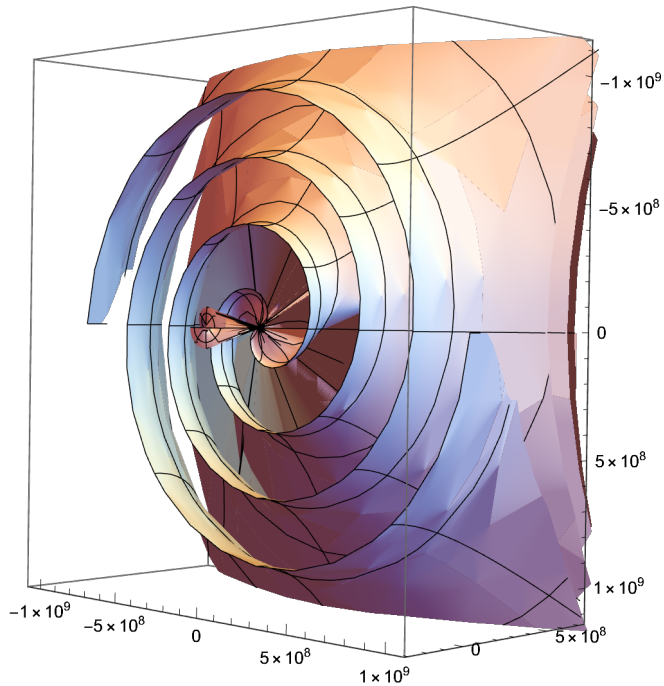
Solve[

$$1 - r \sin[\beta] / \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \theta r - \left(2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right), v]$$

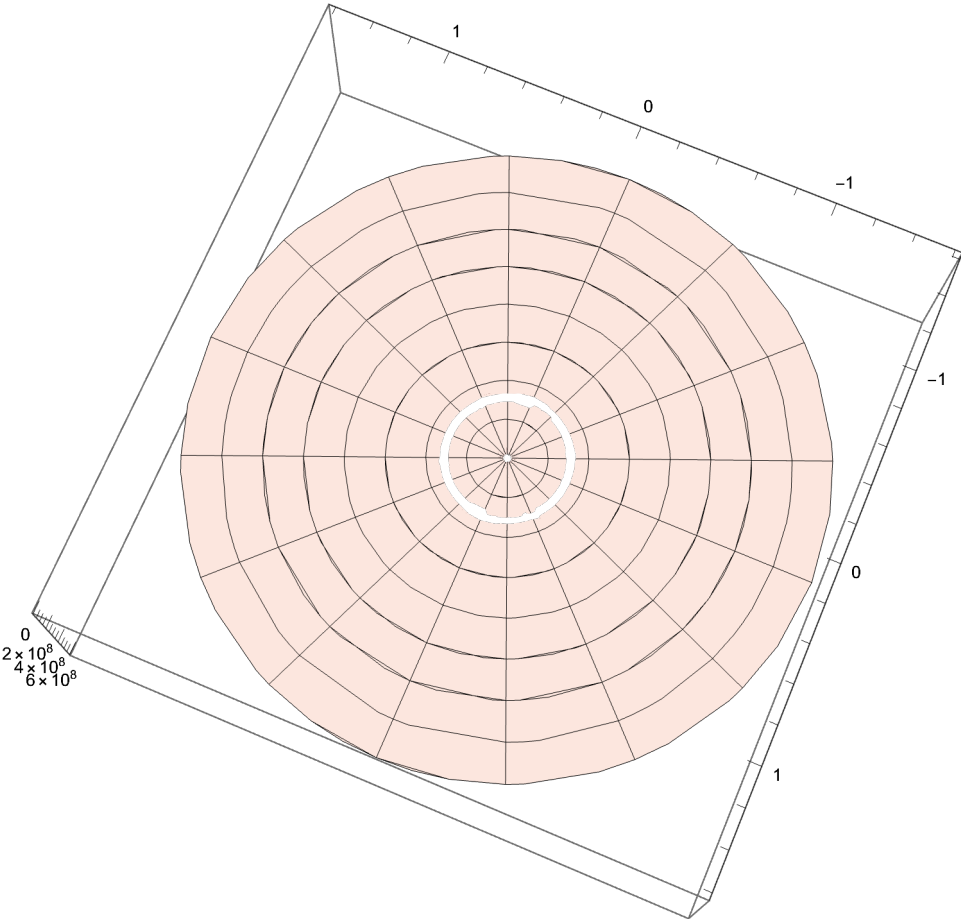
$$\left\{ \left\{ v \rightarrow -\frac{1. \sqrt{-6.91664 \times 10^{33} \theta + 5.50409 \times 10^{32} \theta^2 + 2.17293 \times 10^{34} \sin[\beta]^2}}{\sqrt{-7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-6.91664 \times 10^{33} \theta + 5.50409 \times 10^{32} \theta^2 + 2.17293 \times 10^{34} \sin[\beta]^2}}{\sqrt{-7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2}} \right\} \right\}$$

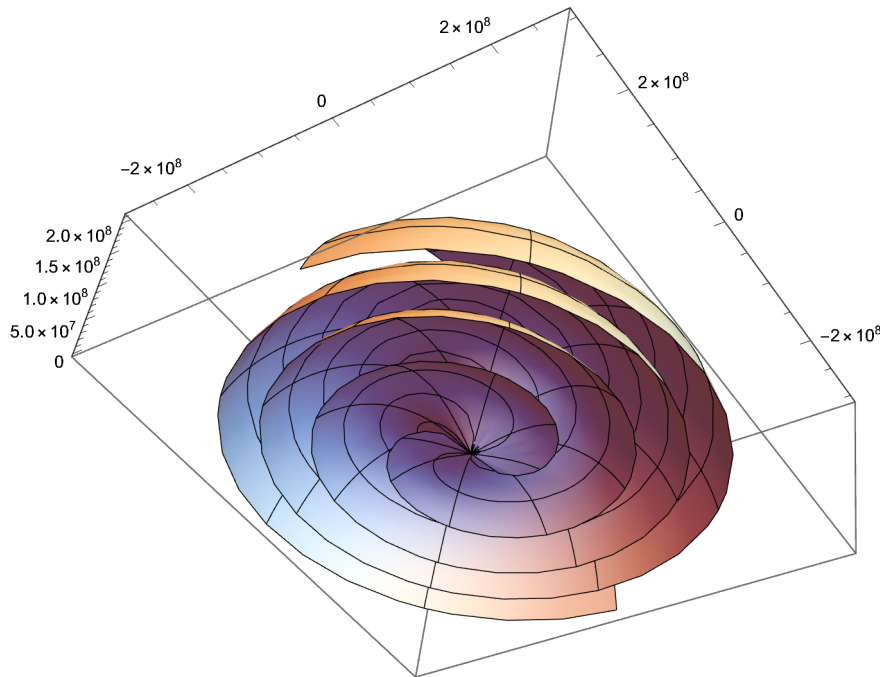
$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left(\sqrt{\left(-6.916640561054567 \cdot 10^{33} \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 5.504087674408673 \cdot 10^{32} \theta^2 + 2.1729267174130213 \cdot 10^{34} \sin[\beta]^2\right)\right)} \right. \\
& \quad \left. \left(\sqrt{\left(-7.695800507960096 \cdot 10^{16} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) \right. \right. \right. \\
& \quad \left. \left. \left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \right. \right. \\
& \quad \left. \left. \left. 6.124123459454841 \cdot 10^{15} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) \right. \right. \right. \\
& \quad \left. \left. \left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \right. \right. \\
& \quad \left. \left. \left. 2.4177070339300032 \cdot 10^{17} \sin[\beta]^2\right)\right)\right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}
\end{aligned}$$



$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\left(\sqrt{\left(-6.916640561054567 \cdot 10^{33} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \right. \right. \\
& \quad \left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad 5.504087674408673 \cdot 10^{32} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right)^2 + \\
& \quad \left. 2.1729267174130213 \cdot 10^{34} \sin[\beta]^2 \right)\Bigg] \Bigg] / \\
& \left(\sqrt{\left(-7.695800507960096 \cdot 10^{16} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \right. \right. \\
& \quad \left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \right. \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad 6.124123459454841 \cdot 10^{15} \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right)^2 + \\
& \quad \left. 2.4177070339300032 \cdot 10^{17} \sin[\beta]^2 \right)\Bigg] \Bigg], \{\beta, -\pi/2, \pi/2\}]
\end{aligned}$$

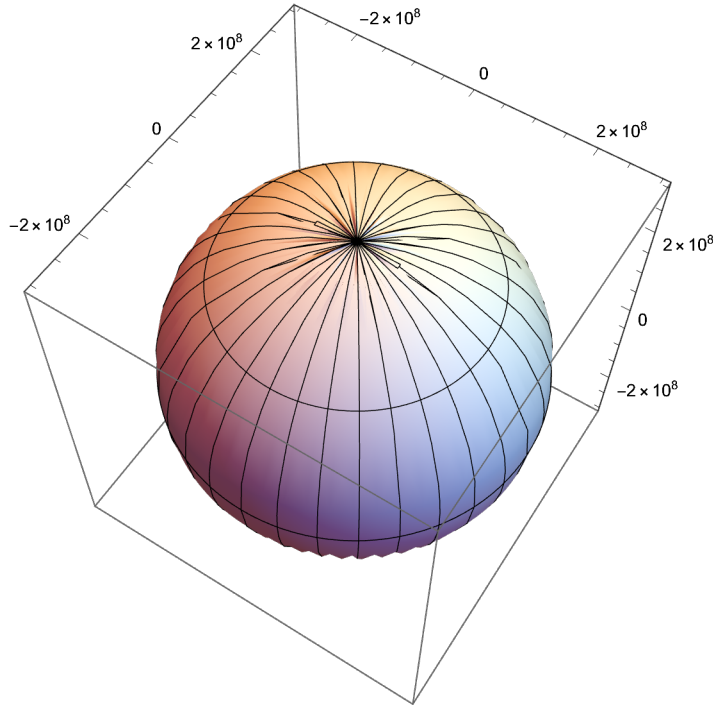


$\text{SphericalPlot3D}\left[\left(\sqrt{\left(-6.916640561054567 \cdot 10^{33} \theta + 5.504087674408673 \cdot 10^{32} \theta^2 + 2.1729267174130213 \cdot 10^{34} \sin^2[\beta]\right)}\right) / \right. \\
\left. \left(\sqrt{\left(-7.695800507960096 \cdot 10^{16} \theta + 6.124123459454841 \cdot 10^{15} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right)^2 + 2.4177070339300032 \cdot 10^{17} \sin^2[\beta]\right)}\right)\right], \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$





```
SphericalPlot3D[( $\sqrt{(-6.916640561054567 \cdot \theta^{33} + 5.504087674408673 \cdot \theta^{32} + 2.1729267174130213 \cdot \sin[\beta]^2)}$ )/
( $\sqrt{(-7.695800507960096 \cdot \theta^{16} + 6.124123459454841 \cdot \theta^{15} + 2.4177070339300032 \cdot \sin[\beta]^2)}$ ), { $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi/2$ ,  $\pi/2$ }]
```



$$\text{Solve}\left[1 - r \sin[\beta] / \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \theta r - \left(2 \pi r - 2 \pi \sqrt{\left(r^2 - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right), r\right]$$

Solve::verif : Potential solution { $r \rightarrow 0$ } (possibly discarded by verifier) should be checked by hand. May require use of limits. >>

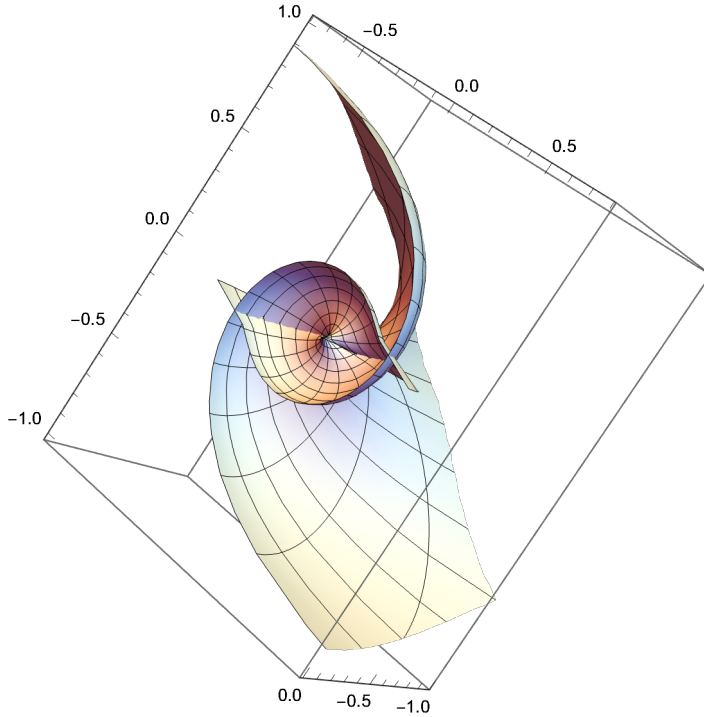
Solve::verif : Potential solution { $r \rightarrow \text{ComplexInfinity}$ } (possibly discarded by verifier) should be checked by hand. May require use of limits. >>

$$\left\{\left\{r \rightarrow \frac{\left(8 \pi^2 \theta - 6 \pi \theta^2 + \theta^3 - 2 \sqrt{16 \pi^5 \theta \sin[\beta]^2 - 20 \pi^4 \theta^2 \sin[\beta]^2 + 8 \pi^3 \theta^3 \sin[\beta]^2 - \pi^2 \theta^4 \sin[\beta]^2}\right)}{2 \left(-16 \pi^3 \theta + 20 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4\right)}\right\}, \left\{r \rightarrow \frac{\left(8 \pi^2 \theta - 6 \pi \theta^2 + \theta^3 + 2 \sqrt{16 \pi^5 \theta \sin[\beta]^2 - 20 \pi^4 \theta^2 \sin[\beta]^2 + 8 \pi^3 \theta^3 \sin[\beta]^2 - \pi^2 \theta^4 \sin[\beta]^2}\right)}{2 \left(-16 \pi^3 \theta + 20 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4\right)}\right\}\right\}$$

SphericalPlot3D[  

$$\left(8 \pi^2 \theta - 6 \pi \theta^2 + \theta^3 + 2 \sqrt{16 \pi^5 \theta \sin[\beta]^2 - 20 \pi^4 \theta^2 \sin[\beta]^2 + 8 \pi^3 \theta^3 \sin[\beta]^2 - \pi^2 \theta^4 \sin[\beta]^2}\right) /$$
  

$$\left(2 \left(-16 \pi^3 \theta + 20 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4\right)\right), \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]$$

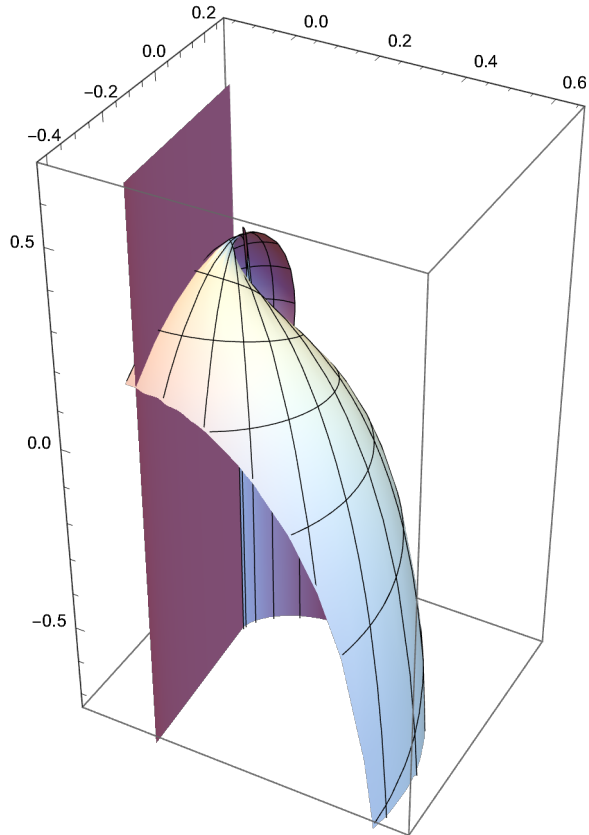


c := 2.99792458 \* (10^8)

Solve[ $1 - \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} == \theta r - \left(2 \pi r - 2 \pi \sqrt{\left(r^2 - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right), r]$   

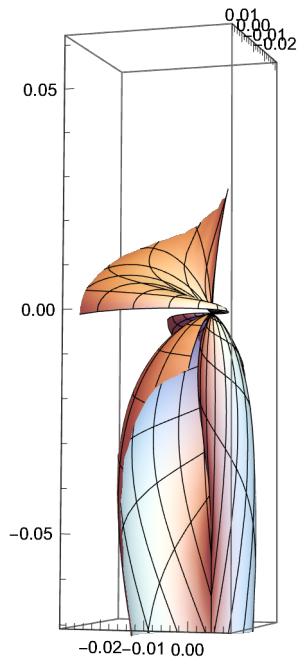
$$\left\{\left\{r \rightarrow \left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / \left(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right)\right\}\right\}$$

$\text{SphericalPlot3D}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right.\right.$   
 $\left.4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right)/$   
 $\left.(16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$

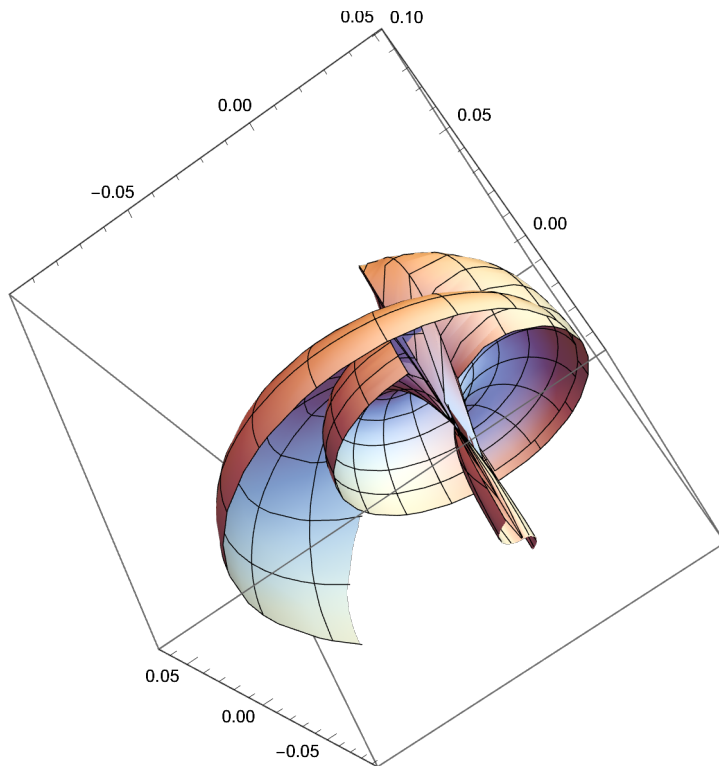


SphericalPlot3D[

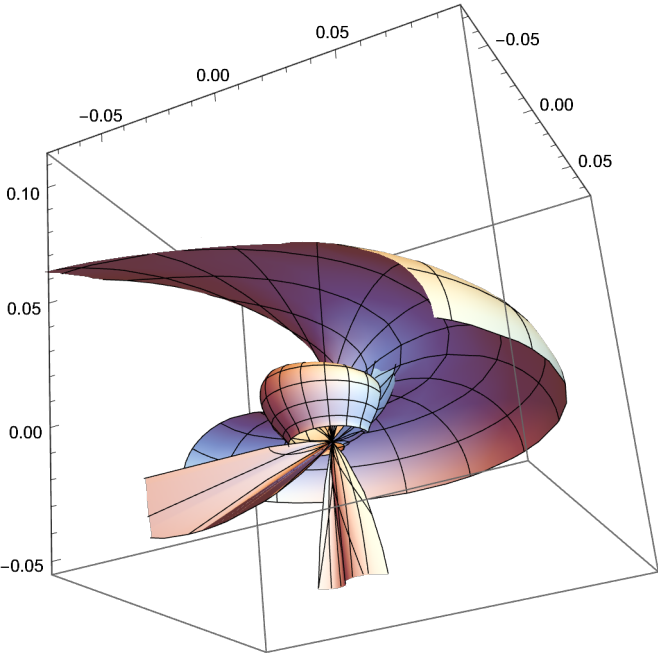
$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / \left( 16\pi^2\theta - 12\pi\theta^2 + 2\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2\sin[\beta]^2)\right) / \left( 6\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3} \right) + \frac{2}{3}\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3} \right)^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \left( -4 \pi \theta + \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^3 - \\
& \quad \left. 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$

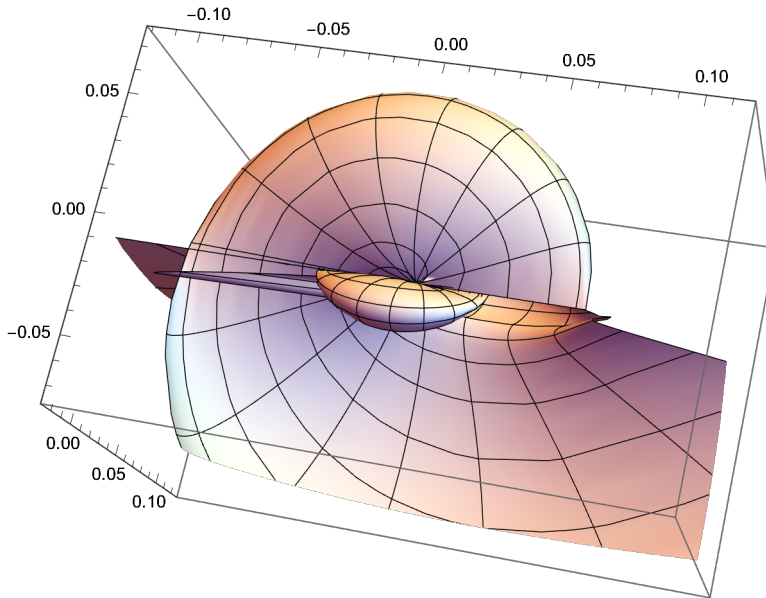


$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left(-4 \pi \theta + \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) / \right.\right. \\
& \quad \left.\left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
& \quad \left.\frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2 + \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \left(2 \pi^2 \sqrt{\left((4 \pi - \theta) \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) / \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right.\right.\right.\right. \\
& \quad \left.\left.\left.3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
& \quad \left.\left.\frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)\right)^{1/3}} \\
& \quad \left.\sin[\beta]^3\right) / \left(4 \pi - \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.\frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) - \\
& \quad \left.\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / \left(16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left.2 \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.\frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^3 - \\
& \quad \left.16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2\right), \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D} \left[ \left( -4 \pi \theta + \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \left( 2 \pi^2 \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) \\
& \quad \left. \sin[\beta]^3 \right) / \left( 4 \pi - \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad 2 \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^3 - \\
& \quad \left. 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}
\end{aligned}$$



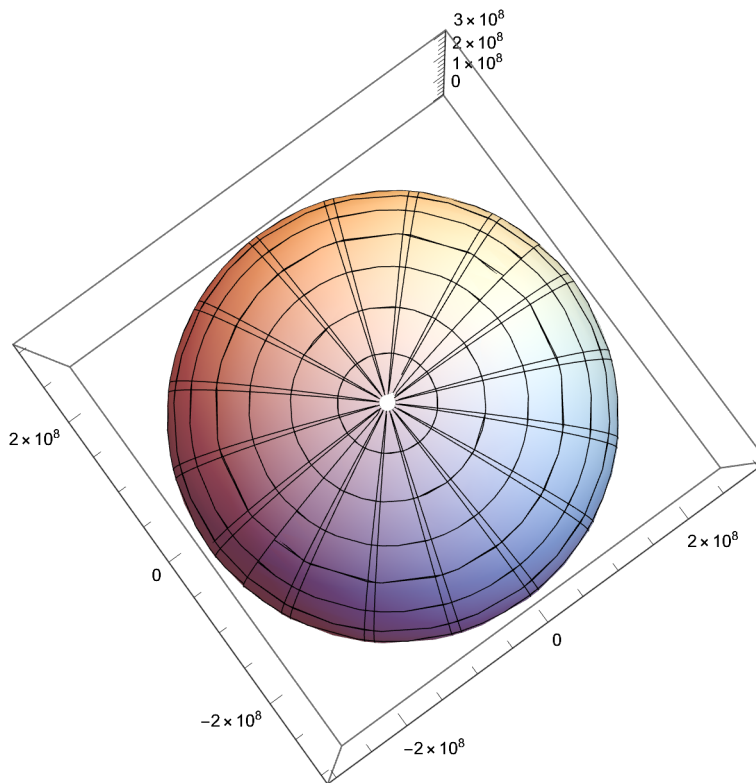


SphericalPlot3D[  

$$\left( \sqrt{\left( -6.916640561054567 \cdot 10^{33} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + 5.504087674408673 \cdot 10^{32} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 + 2.1729267174130213 \cdot 10^{34} \sin[\beta]^2 \right) \Bigg) /$$
  

$$\left( \sqrt{\left( -7.695800507960096 \cdot 10^{16} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + 6.124123459454841 \cdot 10^{15} \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 +$$

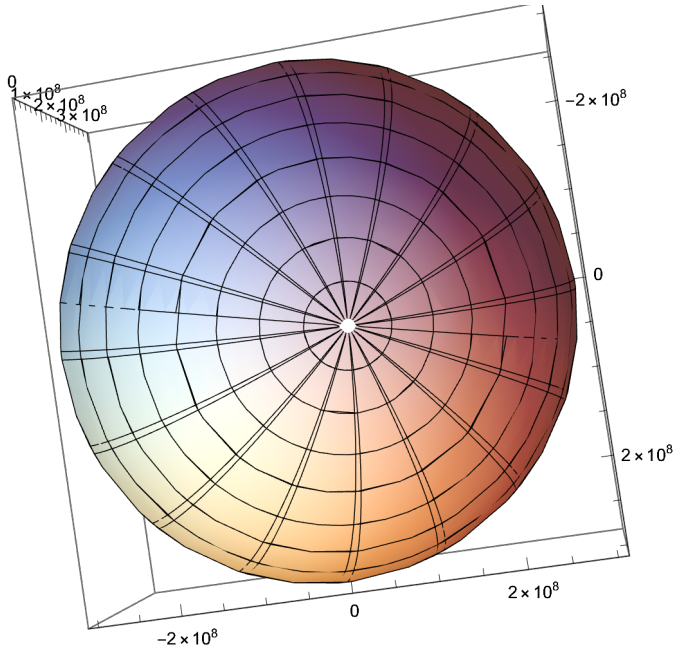
$$\begin{aligned}
 & \left. \left. \left. 2.4177070339300032 \cdot \theta^{17} \sin[\beta]^2 \right) \right) + \right. \\
 & \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
 & \quad \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
 & \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right. \\
 & \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), \\
 & \quad \left\{ \beta, -\pi / 2, \pi / \right. \\
 & \quad \quad \left. 2 \right\}, \left\{ \theta, \right. \\
 & \quad \quad -2 \\
 & \quad \quad \pi, 2 \\
 & \quad \quad \left. \pi \right\} \left. \right]
 \end{aligned}$$



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SphericalPlot3D[
  (
    Sqrt[
      (-6.916640561054567`*^33 (
        (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
          6 (-Pi^3 + 18 Pi^3 Sin[beta]^2 +
            3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    ) +
    5.504087674408673`*^32 (
      (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
        6 (-Pi^3 +
          18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    )^2 +
    2.1729267174130213`*^34 Sin[beta]^2
  ) /
  (
    Sqrt[
      (-7.695800507960096`*^16 (
        (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
          6 (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    ) +
    6.124123459454841`*^15 (
      (4 Pi)/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) / (
        6 (-Pi^3 +
          18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
      ) +
      (2/3) (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6]
        )^(1/3)
    )^2 +
    2.4177070339300032`*^17 Sin[beta]^2
  )
] +
  (
    (-4 Pi theta + theta^2 + 2 Pi Sqrt[(4 Pi - theta) theta] Sin[beta] + 4 Pi^2 Sin[beta]^2 -
      (2 Pi^2 Sqrt[(4 Pi - theta) theta] Sin[beta]^3) / theta -
      (16 Pi^2 theta - 12 Pi theta^2 + 2 theta^3 - 16 Pi^3 Sin[beta]^2 + 8 Pi^2 theta Sin[beta]^2)
    ) /
    (
      (theta / (2 Pi)), {beta, -Pi/2, Pi/2}, {theta,
        -2
        Pi,
        2
        Pi}
    )
  ]

```



TotalVelocity = PhenomenalVelocity + InstantaneousVelocity + AverageVelocity

$$\begin{aligned}
 & \left( \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) / \\
 & \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) + \\
 & \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
 & \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right. \right. \\
 & \left. \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) / (\theta / (2 \pi)) \right) \right) \\
 & r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
 & \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)
 \end{aligned}$$

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SphericalPlot3D[
  (

$$\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \Big/ \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) +$$

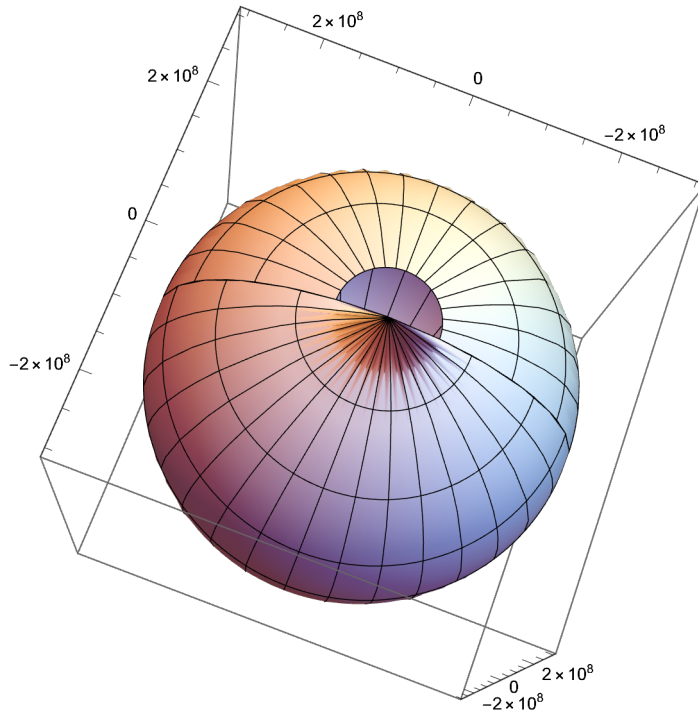

$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right.$$


$$\left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) \Big/$$


$$(16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \Big/$$


$$(\theta / (2 \pi)) \Big], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

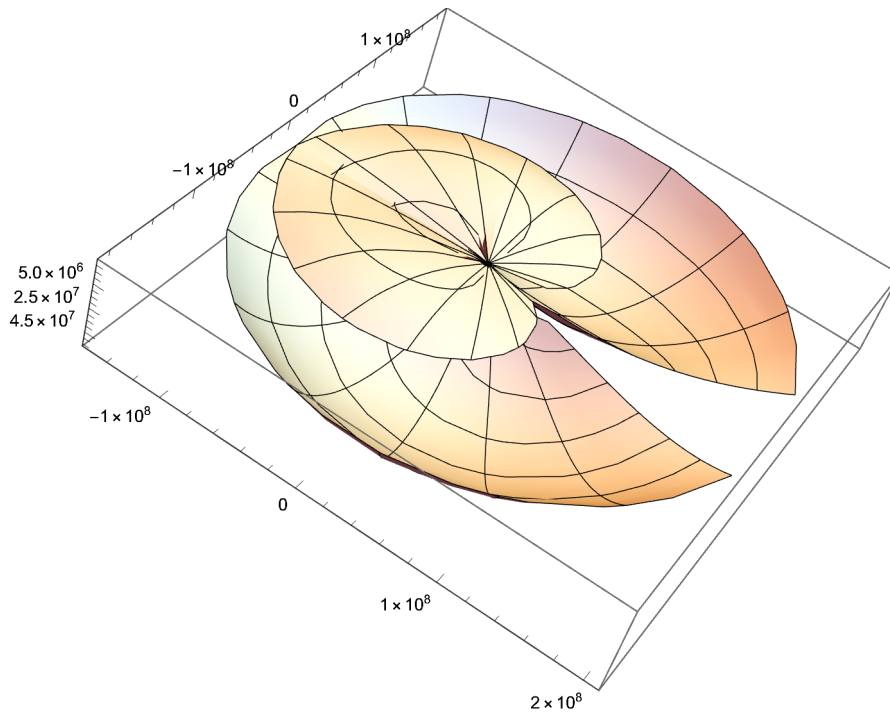
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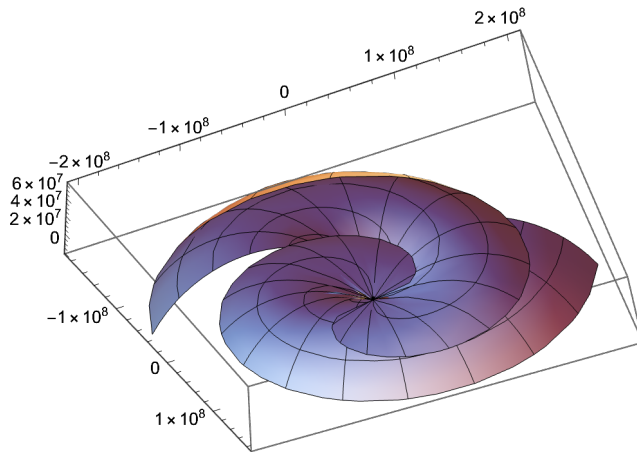
SphericalPlot3D[
  (√((-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 θ^2 + 3.5481432270250993`*^18
    Sin[β]^2)))/√(-12.566370614359172` θ +
    (2 (π + √(π^2 - π^2 Sin[β]^2))^2 + 39.47841760435743` Sin[β]^2)) +
    4 π r^2 - 2 r^2 θ
  2 √(4 π r^2 θ - r^2 θ^2) + (((-4 π θ + θ^2 + 2 π √(4 π - θ) θ Sin[β] + 4 π^2 Sin[β]^2 -
    2 π^2 √(4 π - θ) θ Sin[β]^3
    4 π - θ - 2 π^2 √(4 π - θ) θ Sin[β]^3
    θ
  )))/
  (16 π^2 θ - 12 π θ^2 + 2 θ^3 - 16 π^3 Sin[β]^2 + 8 π^2 θ Sin[β]^2)
  (θ / (2 π))
], {θ, -2 π, 2 π}, {β, -π / 2, π / 2}]

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SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{14} \right.} \right. \\
\left. \left. \sin[\beta]^2 \right) \right) / \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \right.} \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) + \\
\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
\left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \\
\left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) / \\
\left. \left( \theta / (2 \pi) \right) \right], \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]$$



SphericalPlot3D[

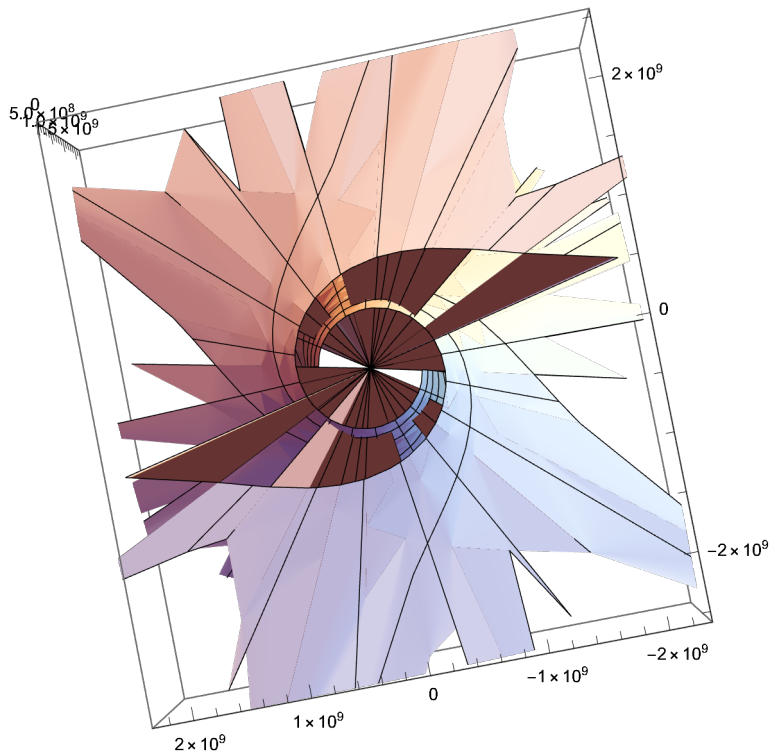
$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + (\theta)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)} \right) +$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \right.$$

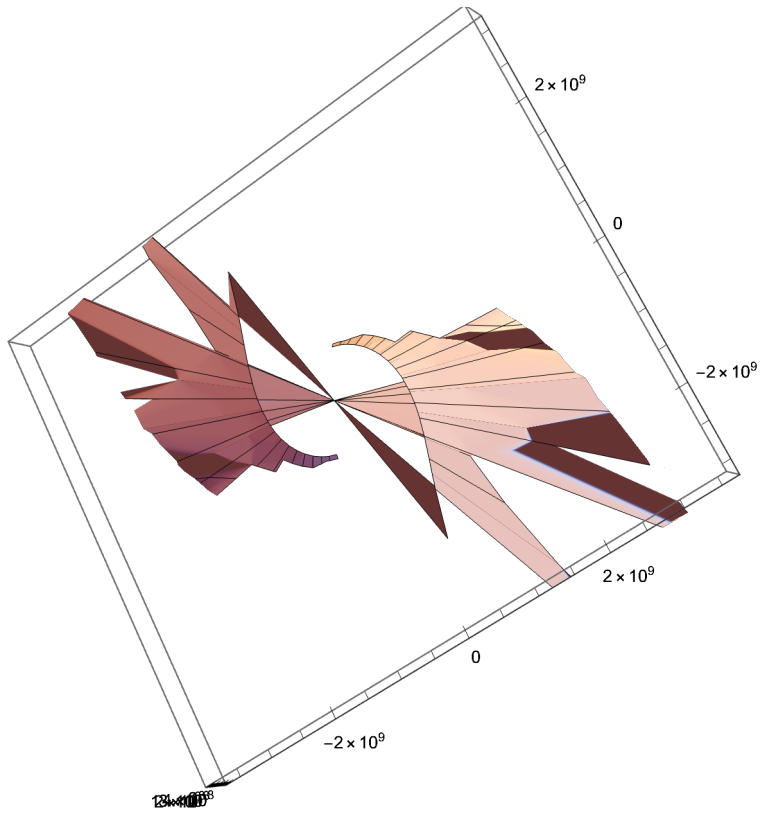
$$\left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) /$$

$$\left( \theta / (2 \pi) \right) \Bigg], \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}]$$



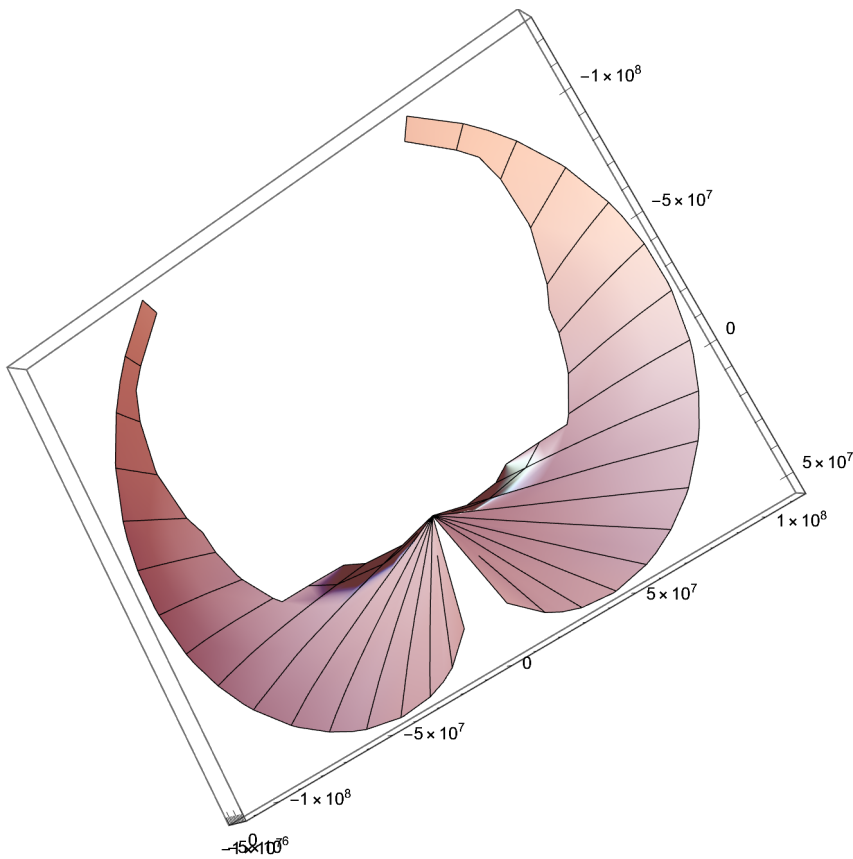


$$\begin{aligned}
& \text{SphericalPlot3D}\left[ \right. \\
& \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right)} \Bigg/ \\
& \left( \sqrt{-12.566370614359172 \cdot \theta + (\theta)^2} + 39.47841760435743 \cdot \sin[\beta]^2 \right) + \\
& \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}} + \\
& \left( \left( \left( -4 \pi \theta + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta} \sin[\beta]^3}{\theta} \right) \right) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \Bigg/ \\
& \left. \left( \theta / (2 \pi) \right) \right], \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{14} \right.} \right. \\
\left. \left. \sin[\beta]^2 \right) \right) / \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \right.} \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) + \\
\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}} + \left( \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
\left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \right. \\
\left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) / \\
\left. \left( \theta / (2 \pi) \right) \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



SphericalPlot3D[  

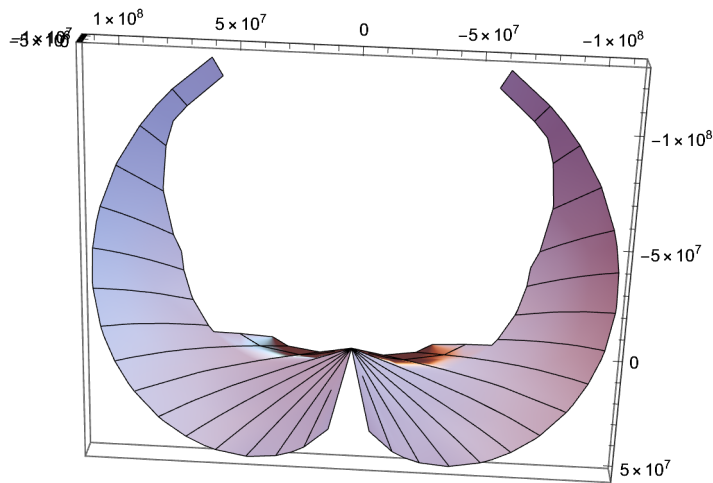
$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right)} \right) / \left( \sqrt{\left( -12.566370614359172 \cdot \theta + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)} \right) +$$
  

$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}} + \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right.$$
  

$$\left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.$$
  

$$\left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right) /$$
  

$$\left( \theta / (2 \pi) \right) \Big], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

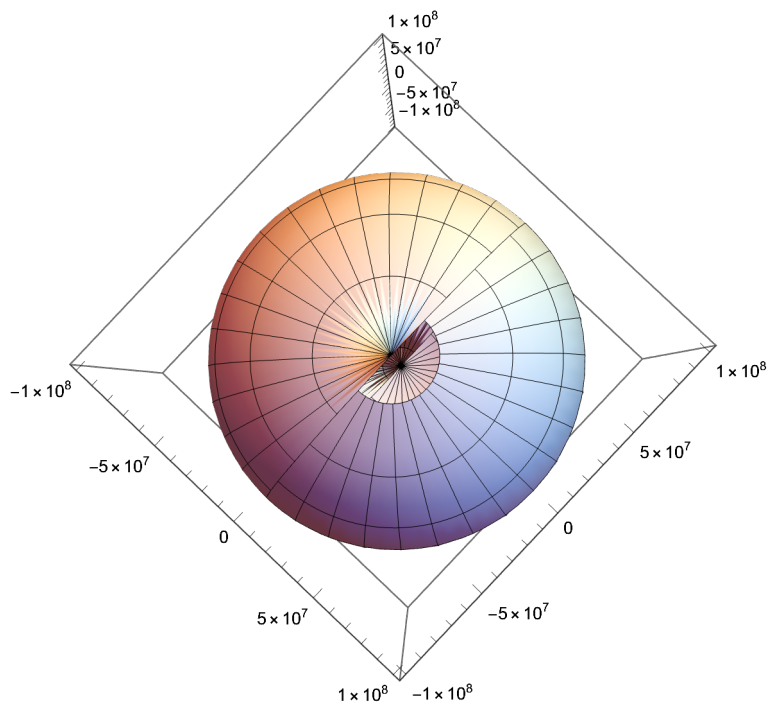


$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)$$

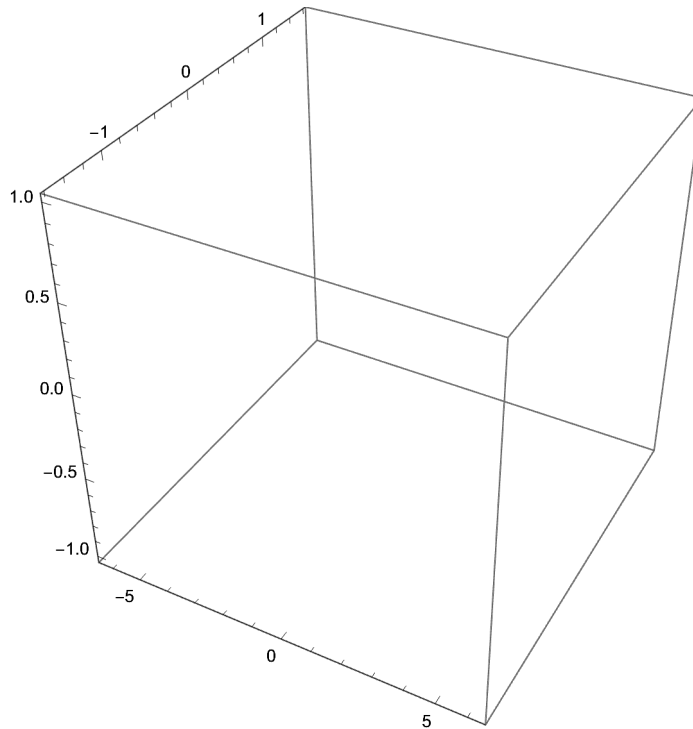
$$D\left[k \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{k (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{SphericalPlot3D}\left[\left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) + \frac{2 \pi (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + r / (\theta / (2 \pi))\right) / 3, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



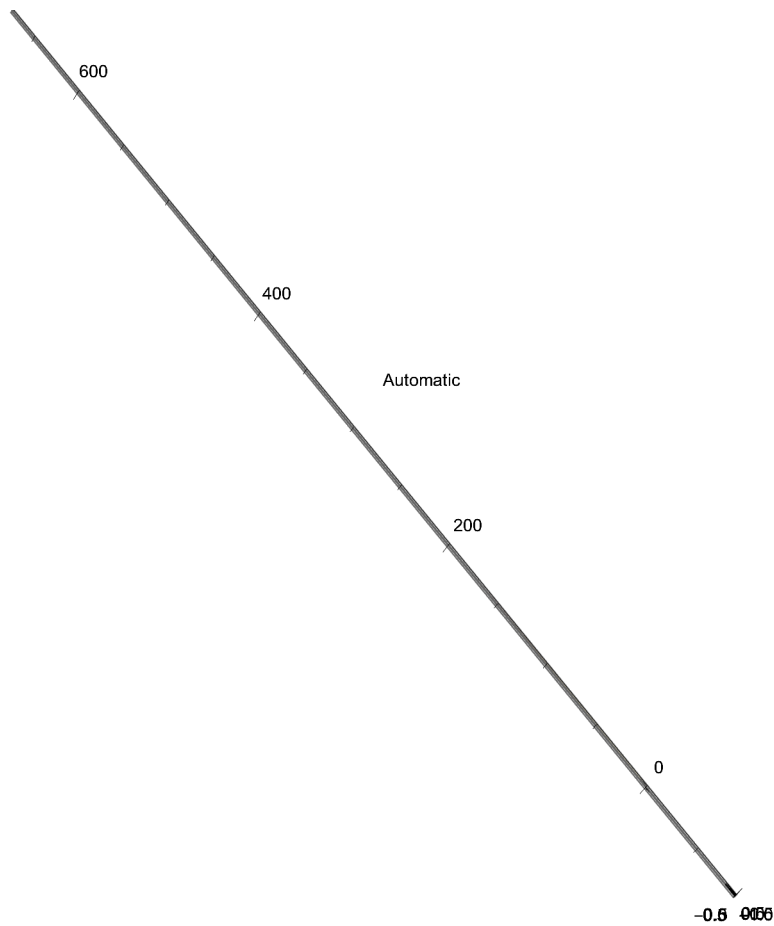
$\text{ContourPlot3D}\left[\left(\left(\sqrt{\left(-1.1294090667581471\right)^{18}\theta + 8.987551787368176\theta^{16} + 3.5481432270250993\sin^2[\beta]\right)}\right) / \left(\sqrt{-12.566370614359172\theta + \theta^2 + 39.47841760435743\sin^2[\beta]}\right) + \frac{k(4\pi r^2 - 2r^2\theta)}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} + r/(\theta/(k))\right) / 3,$   
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}, \{k, -2\pi, 2\pi\}]$



```

SphericalPlot3D[
  2 \pi \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
    \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.
    \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) -
  2 \pi \sqrt{\left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right.
    \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.
    \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right)^2 -
    \left( \frac{1}{2 \pi} \sqrt{4 \pi - \theta} \sqrt{\theta} \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right.
      \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \right.
      \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right) \right)^2 \right)^2,
  {\theta, -4 \pi, 4 \pi}, {\beta, -\pi, \pi}, AxesLabel \rightarrow Automatic]

```



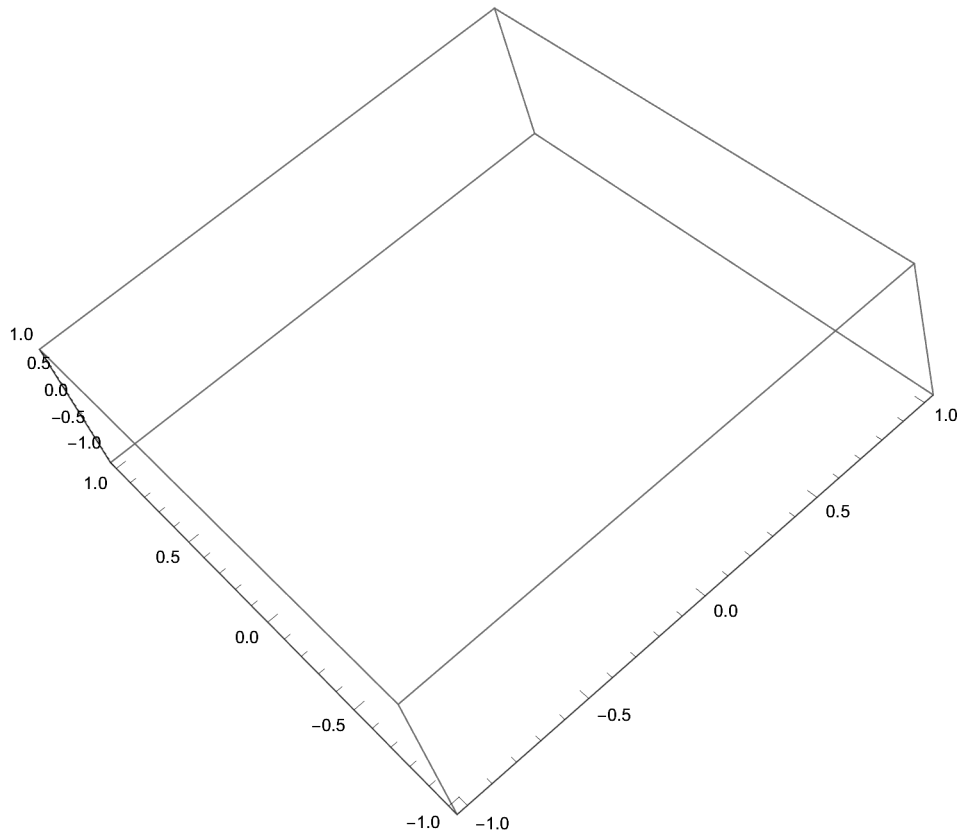
**Solve**[ $y == \text{Abs}[x + i y] \sin[\beta]$ ,  $x$ ]

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

{{ $x \rightarrow -i y - y \csc[\beta]$ }, { $x \rightarrow -i y + y \csc[\beta]$ }}



RevolutionPlot3D[-i y + y Csc[β], {y, -10, 10}, {β, -8 π, 8 π}]



ContourPlot3D[ $\frac{1}{2\pi} \sqrt{4\pi - \theta}$

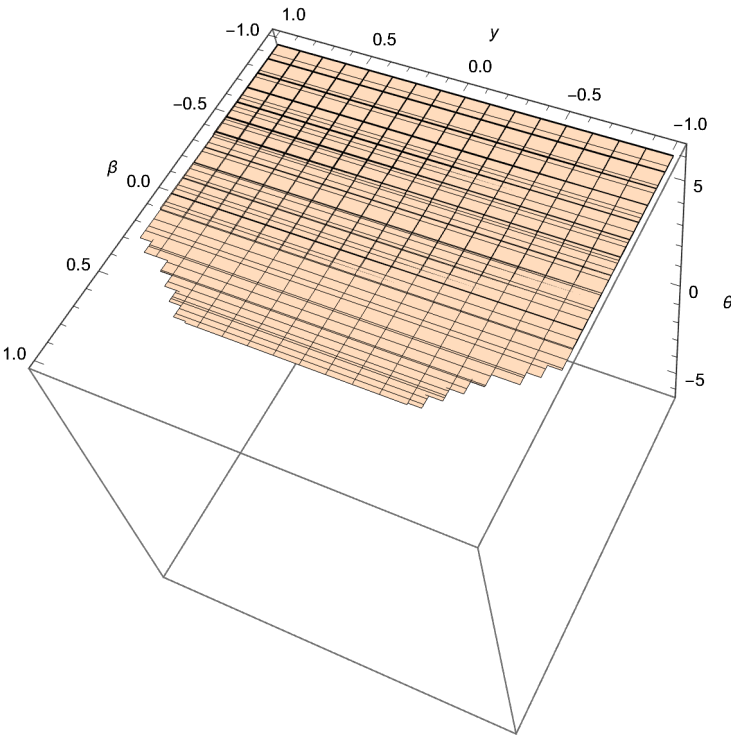
$$\sqrt{\left(1/\left(\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right)\right)\right) \times$$

$$\left(16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2\right)^2 \times$$

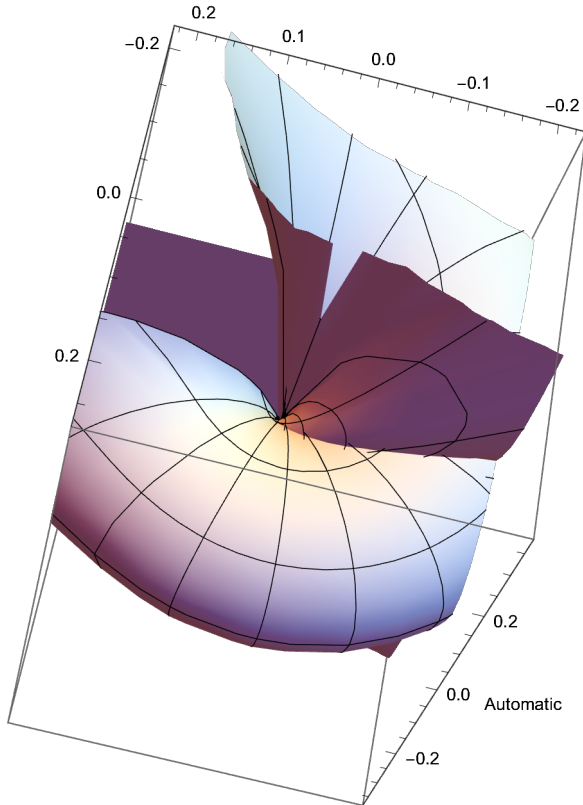
$$2\pi \left(\left(\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right)\right)\right)^2 +$$

$$\left(16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2\right)^2 \Bigg)$$

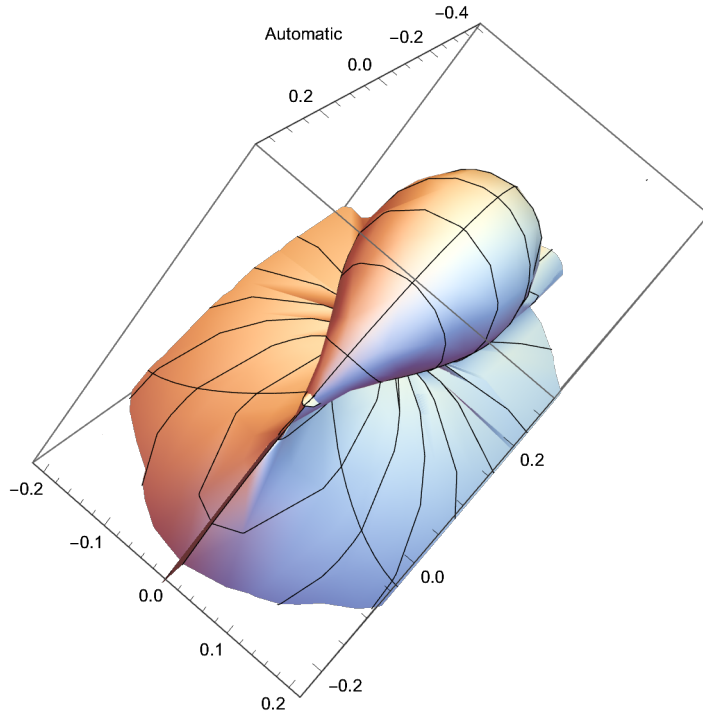
$$\sqrt{\left(-y^2 \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right)^2 + \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right)^4\right)} \left(\left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)\right)\right), \{\beta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{y, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic}]$$



`SphericalPlot3D` $\left[\frac{1}{2\pi}\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\right.$   
 $\left.\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)/\left(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2\right)\right),\right.$   
 $\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\},\text{AxesLabel}\rightarrow\text{Automatic}\Big]$



`SphericalPlot3D` $\left[\frac{1}{2\pi}\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\right.$   
 $\left.\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)/(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)\right)\right]$   
`{ $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , -2  $\pi$ , 2  $\pi$ }, AxesLabel  $\rightarrow$  Automatic]`

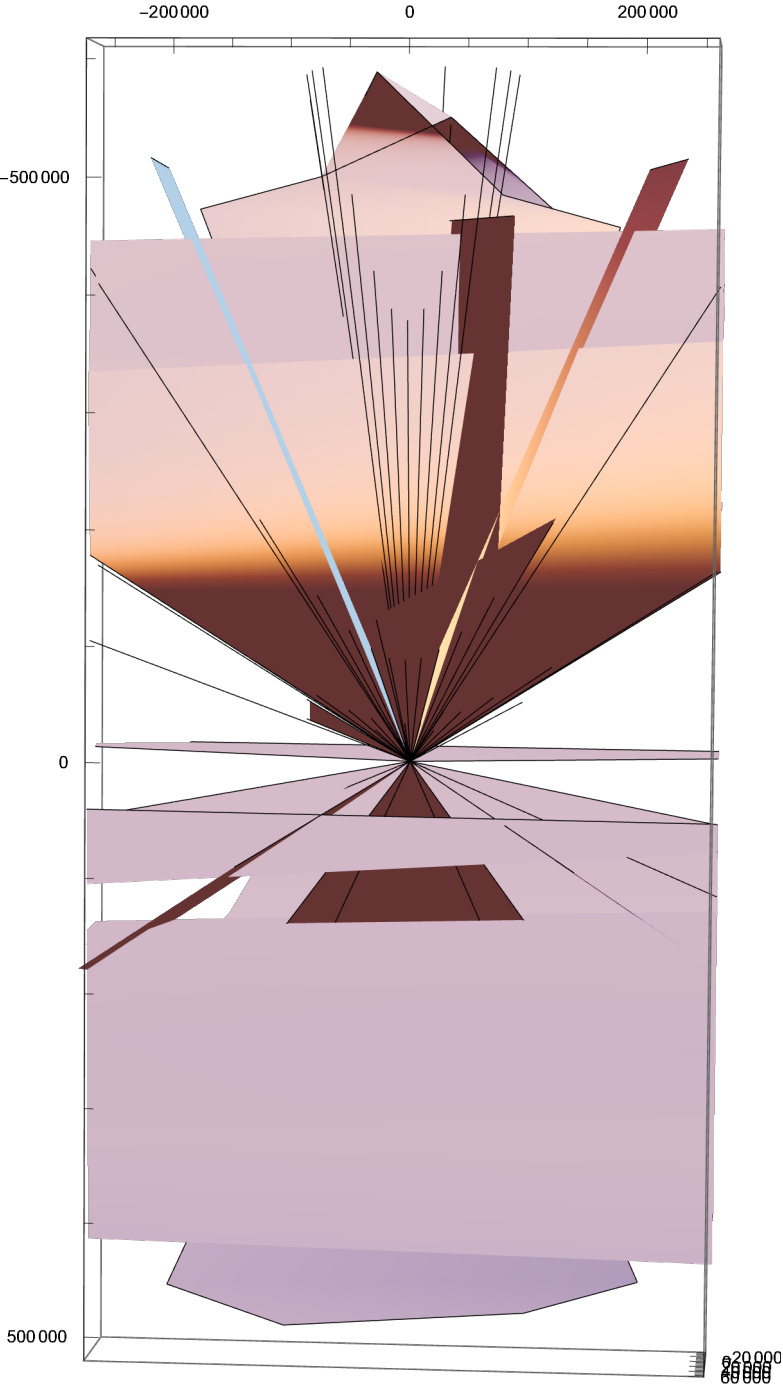


`ContourPlot3D` $\left[\frac{1}{2\pi}\sqrt{4\pi-\theta}\sqrt{\frac{2\pi\left(\text{Abs}[x+\text{I}y]^2+\sqrt{-y^2\text{Abs}[x+\text{I}y]^2+\text{Abs}[x+\text{I}y]^4}\right)}{\text{Abs}[x+\text{I}y]^2}}\text{Abs}[x+\text{I}y],\right.$   
 $\{x, -1, 1\}, \{y, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \text{AxesLabel} \rightarrow \text{Automatic}]$

```

SphericalPlot3D[(((6.283185307179586` θ Csc[β]
  √(-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 θ^2 +
    3.5481432270250993`*^18 Sin[ArcSin[√(4 π - θ) θ]
      2 π]^2))] /
  (√(-12.566370614359172` θ + θ^2 + 39.47841760435743`
    Sin[ArcSin[√(4 π - θ) θ]
      2 π]^2]))^(-13.16979643063896` /
    (-1.8378770664093453` - 1.` Log[(θ Csc[β] √(-1.1294090667581471`*^18 θ +
      8.987551787368176`*^16 θ^2 + 3.5481432270250993`*^18 Sin[β]^2)) /
      (√(-12.566370614359172` θ + θ^2 + 39.47841760435743` Sin[β]^2)))) -
1, {θ, -1.9 π, 1.9 π}, {β, -85 π, 85
  π}]

```



$$\text{Solve}\left[1 == \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -\left(\frac{2}{108 \pi^5 + \sqrt{108 \pi^6 + 11\,664 \pi^{10}}}\right)^{1/3} + \frac{\left(\frac{1}{2} \left(108 \pi^5 + \sqrt{108 \pi^6 + 11\,664 \pi^{10}}\right)\right)^{1/3}}{3 \pi^2}\right\}\right\}$$

$$\text{Solve}\left[2 == \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -\left(\frac{2}{1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}}\right)^{1/3} + \frac{\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{12\pi^2}\right\}\right\}$$

$$\text{Solve}\left[3 == \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -\left(\frac{2}{8748\pi^5 + \sqrt{78732\pi^6 + 76527504\pi^{10}}}\right)^{1/3} + \frac{\left(\frac{1}{2}\left(8748\pi^5 + \sqrt{78732\pi^6 + 76527504\pi^{10}}\right)\right)^{1/3}}{27\pi^2}\right\}\right\}$$

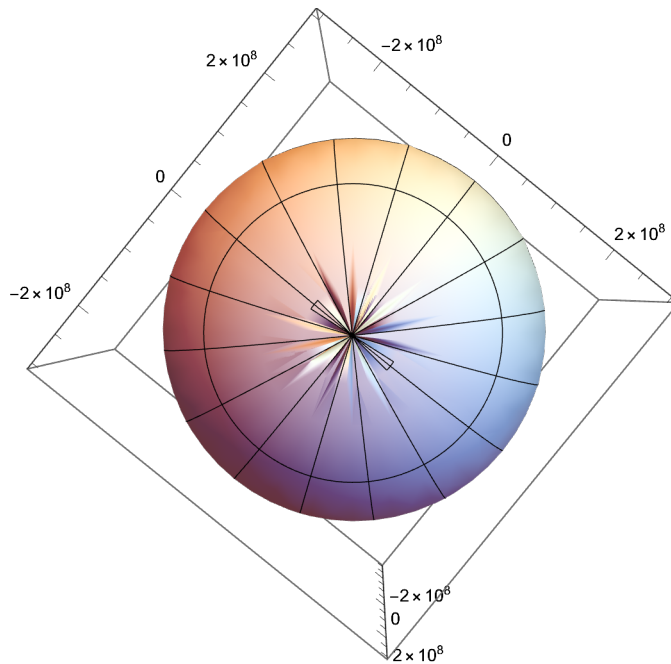
$$(\mathbf{F}_{dm}) = m \mathbf{a}$$



$$\begin{aligned}
& \frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right)^2}{2\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4} \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)^{3/2}} - \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2\theta((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \left. \left. \frac{4(4\pi-2\theta)}{\pi^2\theta^2\sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} \right) + \\
& \left( \pi^{3/2} (-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3) \right. \\
& \quad \left. \left( -\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} \right) - \\
& \frac{3\pi^{3/2} (-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{2(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{5/2}} + \\
& \frac{\pi^{3/2} (48\pi^2-48\pi\theta+12\theta^2) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}}
\end{aligned}$$

$$\begin{aligned}
& - \frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right)^2}{2\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4} \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)^{3/2}} + \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2\theta((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3\sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \left. \left. \frac{4(4\pi-2\theta)}{\pi^2\theta^2\sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} \right) - \\
& \left( \pi^{3/2} (-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3) \right. \\
& \quad \left. \left( -\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} \right) + \\
& \frac{3\pi^{3/2} (-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{2(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{5/2}} - \\
& \frac{\pi^{3/2} (48\pi^2-48\pi\theta+12\theta^2) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}}
\end{aligned}$$

SphericalPlot3D[ $\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{-12.566370614359172 \cdot 10^8 \theta + \theta^2 + 39.47841760435743 \cdot 10^8 \sin[\beta]^2}\right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$



Solve[ $1 == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$ ,  $\beta$ ]

$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right\}\right\}$

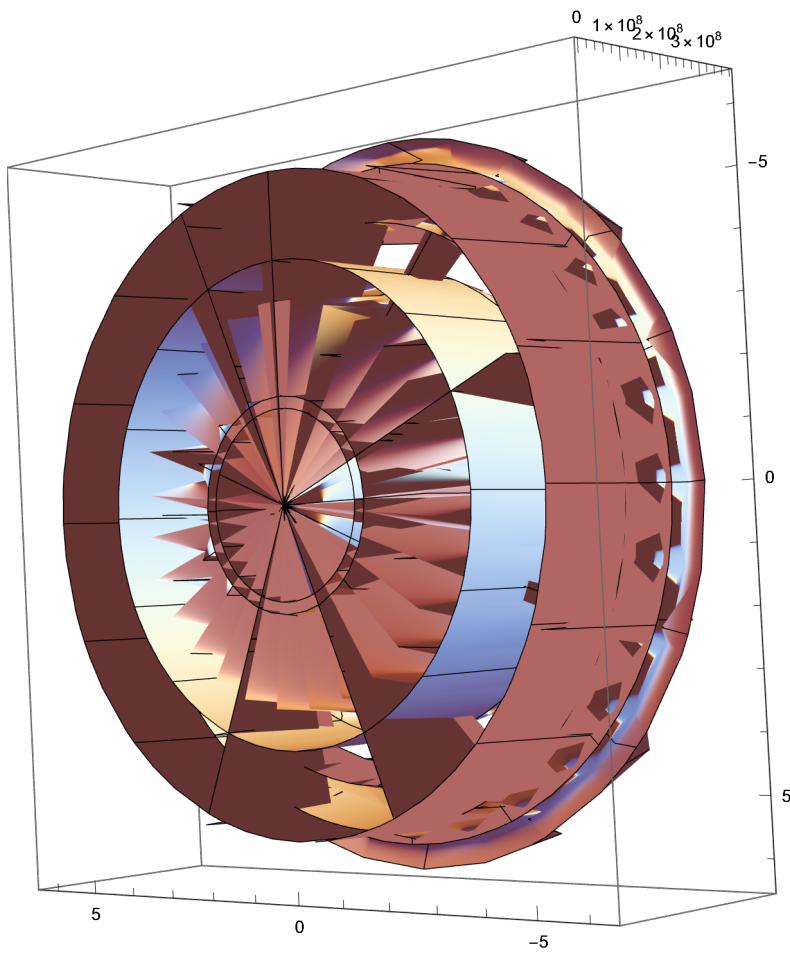
Solve[ $1 == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$ ,  $\theta$ ]

$\left\{\left\{\theta \rightarrow 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$

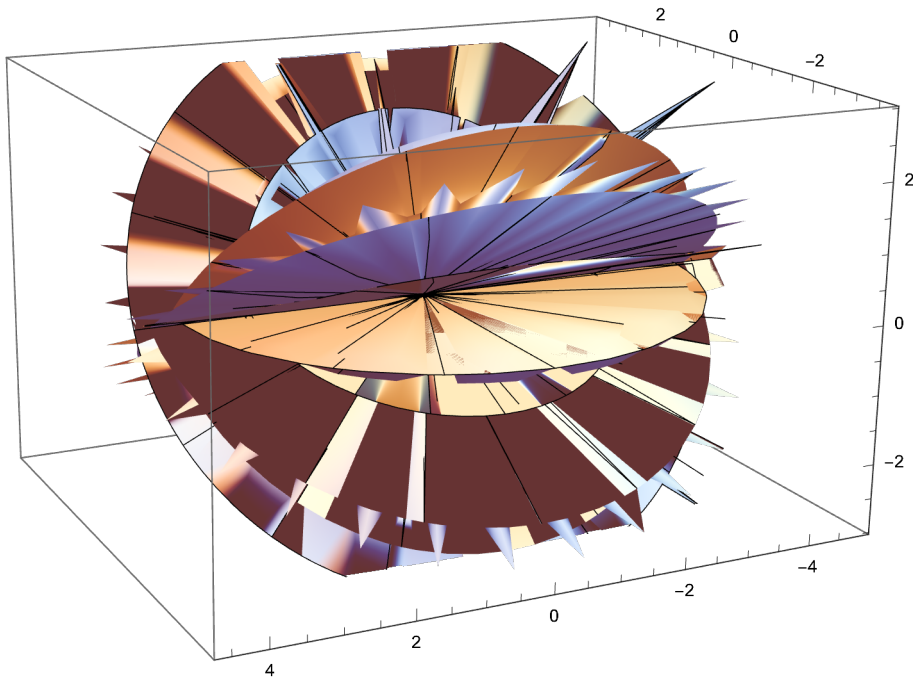
```

RevolutionPlot3D[ $\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} (\theta) + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin\left[\arcsin\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin\left[\arcsin\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2\right)}\right), \{\theta, -2\pi, 2\pi\}$ ]

```



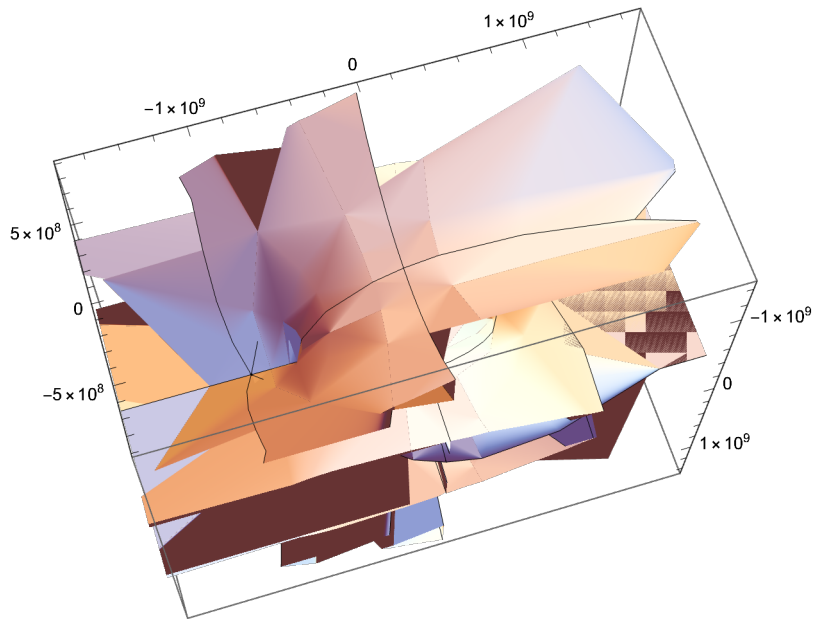
```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18 (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])) + 8.987551787368176`*^16
        (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2]))^2 + 3.5481432270250993`*^18 Sin[beta]^2)
    ] /
    (
      Sqrt[
        (-12.566370614359172` (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])) + theta^2 +
          39.47841760435743` Sin[beta]^2)
      ], {theta, -pi, pi}, {beta, -.5 pi, .5 pi}
  ]
```



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$
  

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right),$$
  
 $\{\theta, -4\pi, 4\pi\}, \{\beta, -2\pi, 2\pi\}]$



```

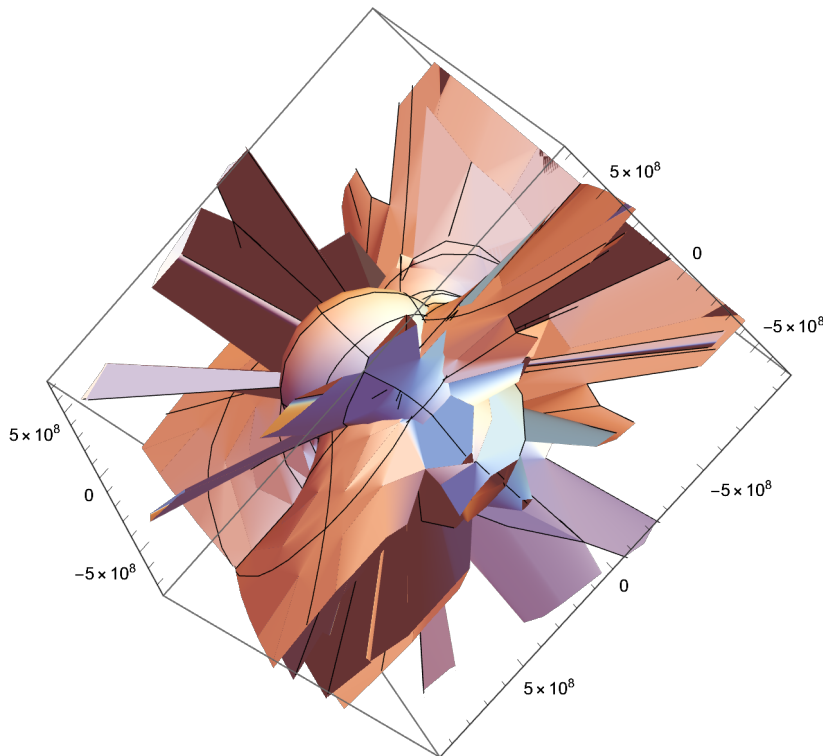
SphericalPlot3D[
  (

$$\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left(2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\theta]^2\right)} /$$


$$\left(\sqrt{-12.566370614359172 \cdot 10^{18} \theta + \theta^2 + 39.47841760435743 \cdot 10^{18} \sin[\beta]^2}\right), \{\theta,$$


$$-2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$$

```



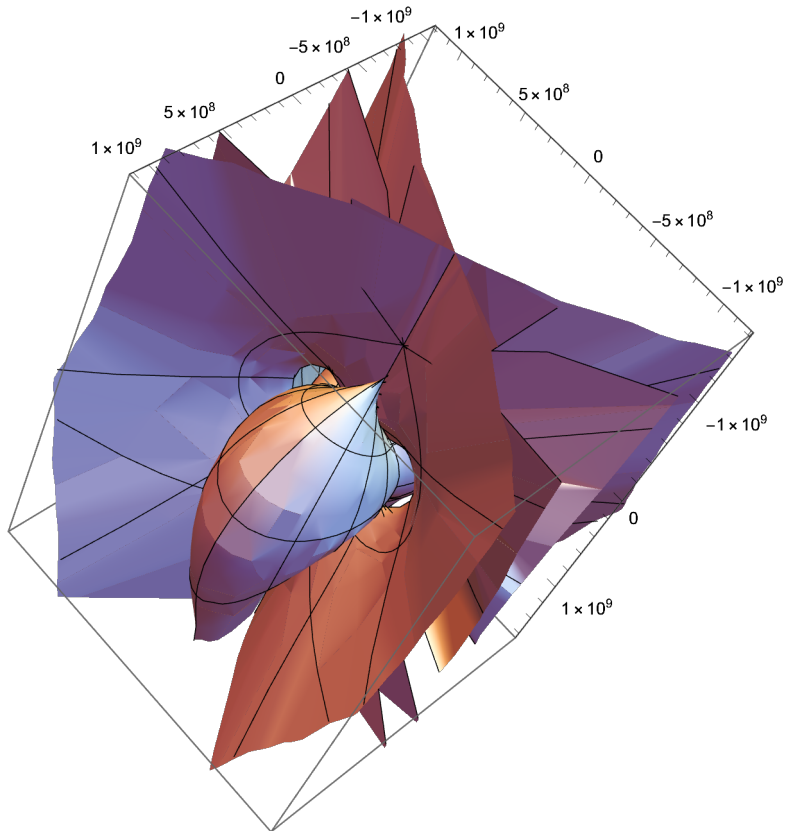
```
SphericalPlot3D[
  (

$$\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\theta]^2\right)} /$$


$$\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \{\theta,$$


$$-2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$$

```



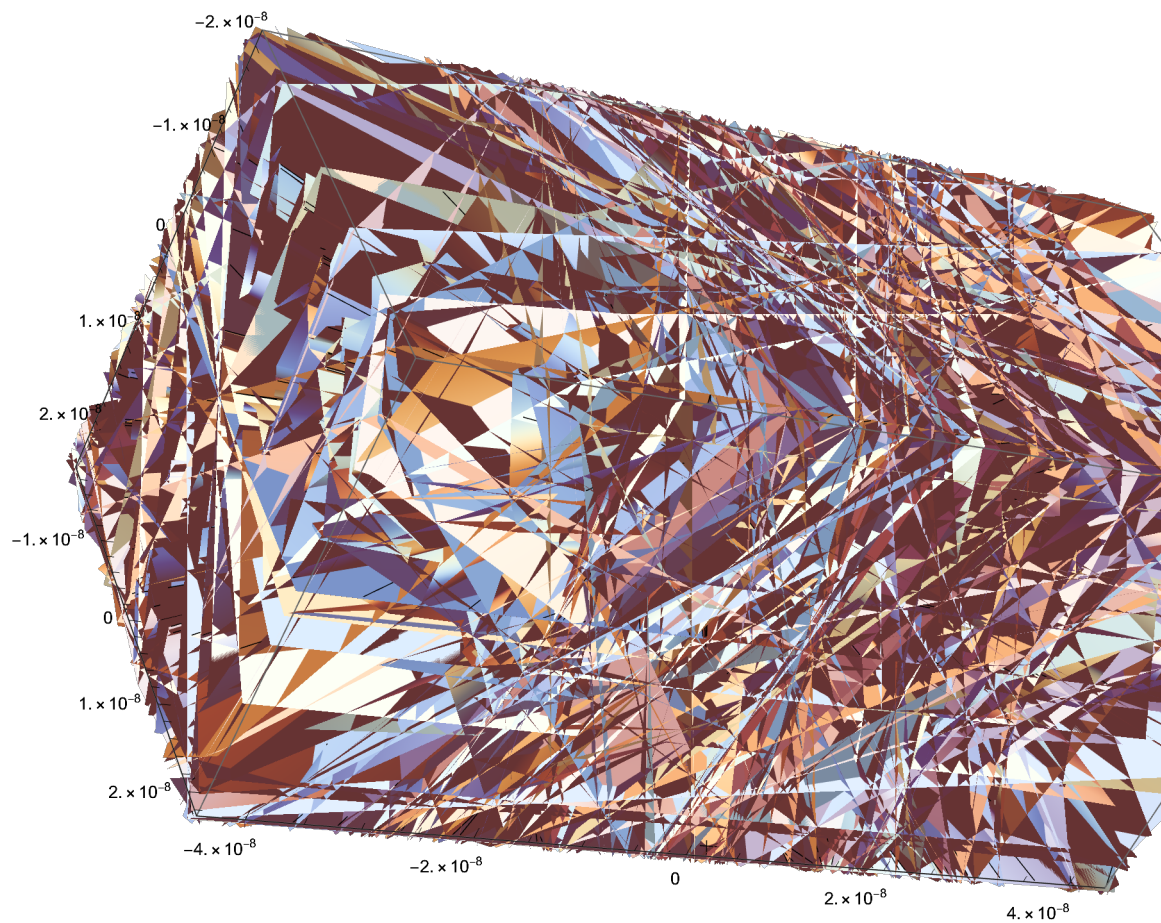


$$\begin{aligned}
& D \left[ \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2) \right) \right] / \\
& \left( \sqrt{-12.566370614359172 \cdot 10^0 \theta + \theta^2 + 39.47841760435743 \cdot 10^0 \sin[\beta]^2} \right), \theta, \beta \Big] \\
& - \left( 1.77407 \times 10^{18} (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta] \right) / \\
& \left( \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \right. \\
& \quad \left. (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)^{3/2} \right) - \\
& \left( 1.77407 \times 10^{18} (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] \right) / \left( (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^{3/2} \right. \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) - \\
& \left( 19.7392 (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta] \right) / \\
& \left( (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^{3/2} \right. \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) + \\
& \left( 59.2176 (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] \right. \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^{5/2}
\end{aligned}$$

```

SphericalPlot3D[
- (1.7740716135125496`^18 (-1.1294090667581471`^18 + 1.7975103574736352`^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( \sqrt{-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2} \right.$ 
   $\left. (-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 + \right.$ 
   $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2) ^{3/2} \right) -$ 
(1.7740716135125496`^18 (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]) /
 $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2) ^{3/2} \right.$ 
 $\left. \sqrt{(-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 + \right.$ 
 $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2) \right) -$ 
(19.739208802178716` (-1.1294090667581471`^18 + 1.7975103574736352`^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2) ^{3/2} \right.$ 
 $\left. \sqrt{(-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 + \right.$ 
 $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2) \right) +$ 
(59.21762640653615` (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]
 $\sqrt{(-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 + \right.$ 
 $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2) \right) /$ 
 $\left( -12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2 \right)^{5/2},$ 
 $\{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\} ]$ 

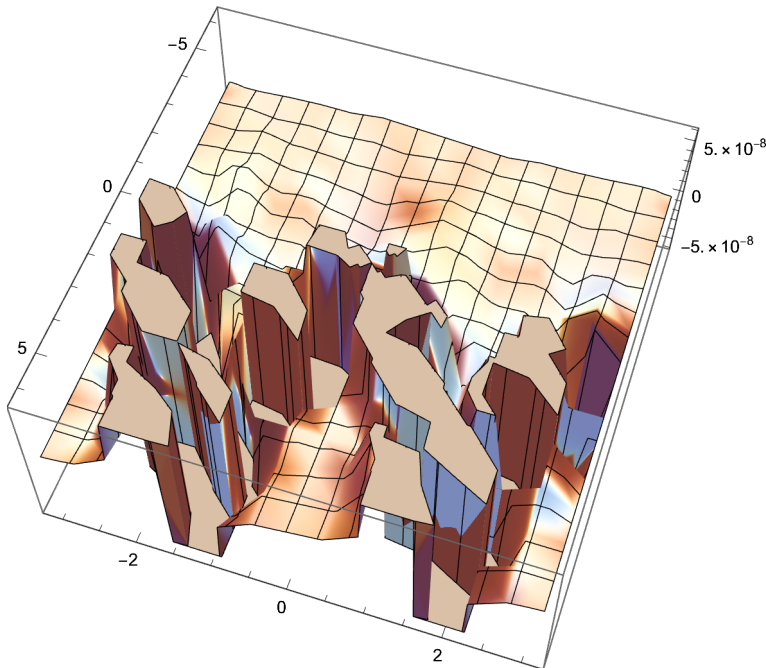
```



```

Plot3D[
- (1.7740716135125496`^18 (-1.1294090667581471`^18 + 1.7975103574736352`^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( \sqrt{-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2} \right.$ 
   $\left( -1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 + \right.$ 
   $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2 \right)^{3/2} -$ 
(1.7740716135125496`^18 (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]) /
 $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)^{3/2} \right.$ 
 $\sqrt{(-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 +$ 
 $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2 \right)}$  -
(19.739208802178716` (-1.1294090667581471`^18 + 1.7975103574736352`^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)^{3/2} \right.$ 
 $\sqrt{(-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 +$ 
 $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2 \right)}$  +
(59.21762640653615` (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]
 $\sqrt{(-1.1294090667581471`^18 \theta + 8.987551787368176`^16 \theta^2 +$ 
 $\left. 3.5481432270250993`^18 \text{Sin}[\beta]^2 \right)}) /$ 
 $\left( -12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2 \right)^{5/2}, \{\theta, -2$ 
 $\pi, 2\pi\}, \{\beta, -\pi, \pi\}$ 

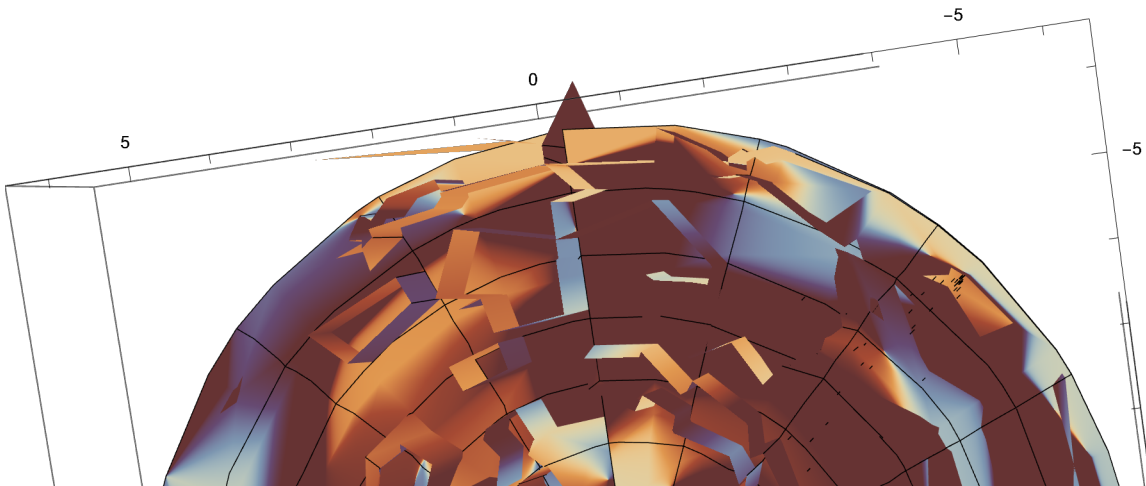
```

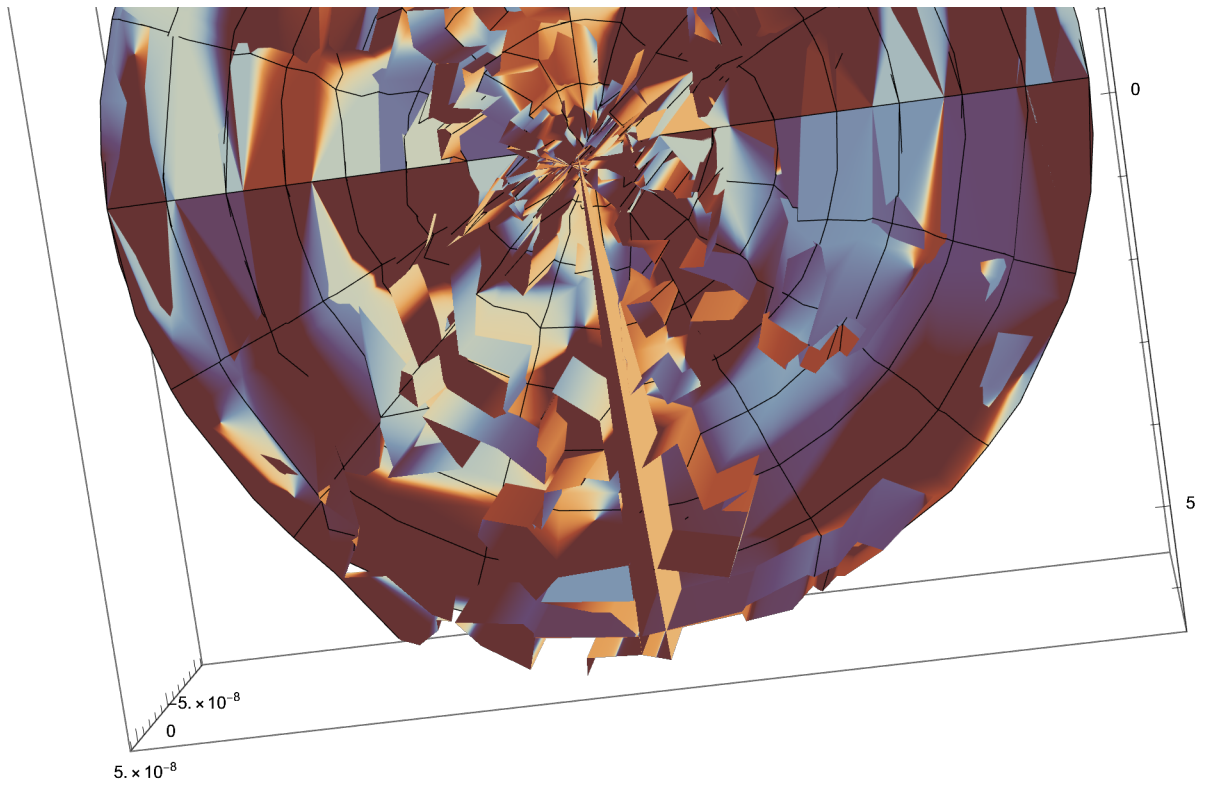


```

RevolutionPlot3D[
- (1.7740716135125496`*^18 (-1.1294090667581471`*^18 + 1.7975103574736352`*^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( \sqrt{-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2} \right.$ 
   $\left( -1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 + \right.$ 
   $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2 \right)^{3/2}$ ) -
(1.7740716135125496`*^18 (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]) /
 $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)^{3/2} \right.$ 
 $\sqrt{(-1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 +$ 
 $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2 \right)}$  -
(19.739208802178716` (-1.1294090667581471`*^18 + 1.7975103574736352`*^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)^{3/2} \right.$ 
 $\sqrt{(-1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 +$ 
 $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2 \right)}$  +
(59.21762640653615` (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]
 $\sqrt{(-1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 +$ 
 $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2 \right)}) /$ 
 $\left( -12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2 \right)^{5/2}, \{\theta, -2$ 
 $\pi, 2\pi\}, \{\beta, -\pi, \pi\}$ 

```





Force =

$$\begin{aligned}
 & m \left( - (1.7740716135125496 \cdot 10^{18} (-1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \theta) \right. \\
 & \quad \left. \cos[\beta] \sin[\beta]) \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right. \\
 & \quad \left. (-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \\
 & \quad \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)^{3/2} \right) - \\
 & (1.7740716135125496 \cdot 10^{18} (-12.566370614359172 \cdot \theta + 2 \theta) \cos[\beta] \sin[\beta]) / \\
 & \left( (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^{3/2} \right. \\
 & \quad \left. \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \\
 & \quad \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) - \\
 & (19.739208802178716 \cdot (-1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \theta) \\
 & \quad \cos[\beta] \sin[\beta]) / \left( (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^{3/2} \right. \\
 & \quad \left. \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \\
 & \quad \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) + \\
 & (59.21762640653615 \cdot (-12.566370614359172 \cdot \theta + 2 \theta) \cos[\beta] \sin[\beta] \\
 & \quad \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \\
 & \quad \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}) / \\
 & \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)^{5/2} \Big)
 \end{aligned}$$

```

ContourPlot3D[
  m \[LeftBracketingBar] - (1.7740716135125496`*^18 (-1.1294090667581471`*^18 + 1.7975103574736352`*^17 \[Theta])
    Cos[\[Beta] Sin[\[Beta]]) / \[LeftBracketingBar] \[Sqrt] - 12.566370614359172` \[Theta] + \[Theta]^2 + 39.47841760435743` Sin[\[Beta]]^2
    (-1.1294090667581471`*^18 \[Theta] + 8.987551787368176`*^16 \[Theta]^2 +
      3.5481432270250993`*^18 Sin[\[Beta]]^2)^(3/2) \[RightBracketingBar] -
    (1.7740716135125496`*^18 (-12.566370614359172` + 2 \[Theta]) Cos[\[Beta] Sin[\[Beta]]) /
      \[LeftBracketingBar] (-12.566370614359172` \[Theta] + \[Theta]^2 + 39.47841760435743` Sin[\[Beta]]^2)^(3/2)
      \[Sqrt] (-1.1294090667581471`*^18 \[Theta] + 8.987551787368176`*^16 \[Theta]^2 +
        3.5481432270250993`*^18 Sin[\[Beta]]^2) \[RightBracketingBar] -
    (19.739208802178716` (-1.1294090667581471`*^18 + 1.7975103574736352`*^17 \[Theta])
      Cos[\[Beta] Sin[\[Beta]]) / \[LeftBracketingBar] (-12.566370614359172` \[Theta] + \[Theta]^2 + 39.47841760435743` Sin[\[Beta]]^2)^(3/2)
      \[Sqrt] (-1.1294090667581471`*^18 \[Theta] + 8.987551787368176`*^16 \[Theta]^2 +
        3.5481432270250993`*^18 Sin[\[Beta]]^2) \[RightBracketingBar] +
    (59.21762640653615` (-12.566370614359172` + 2 \[Theta]) Cos[\[Beta] Sin[\[Beta]])
      \[Sqrt] (-1.1294090667581471`*^18 \[Theta] + 8.987551787368176`*^16 \[Theta]^2 +
        3.5481432270250993`*^18 Sin[\[Beta]]^2) \[RightBracketingBar] \[LeftBracketingBar]
      (-12.566370614359172` \[Theta] + \[Theta]^2 + 39.47841760435743` Sin[\[Beta]]^2)^(5/2) \[RightBracketingBar],
  {m, -5, 5}, {\[Beta], -\[Pi], \[Pi]},
  {\[Theta],
    -2
    \[Pi], 2
    \[Pi]}]
Solve[\[LeftBracketingBar] (\[Sqrt] (3.5481432270250993`*^18 \[eta]^2 -
  1.1294090667581471`*^18 r^2 \[Theta] + 8.987551787368176`*^16 r^2 \[Theta]^2) \[RightBracketingBar] /
  (\[Sqrt] (39.47841760435743` \[eta]^2 - 12.566370614359172` r^2 \[Theta] + r^2 \[Theta]^2) = c, \[eta]]
{{}}

```

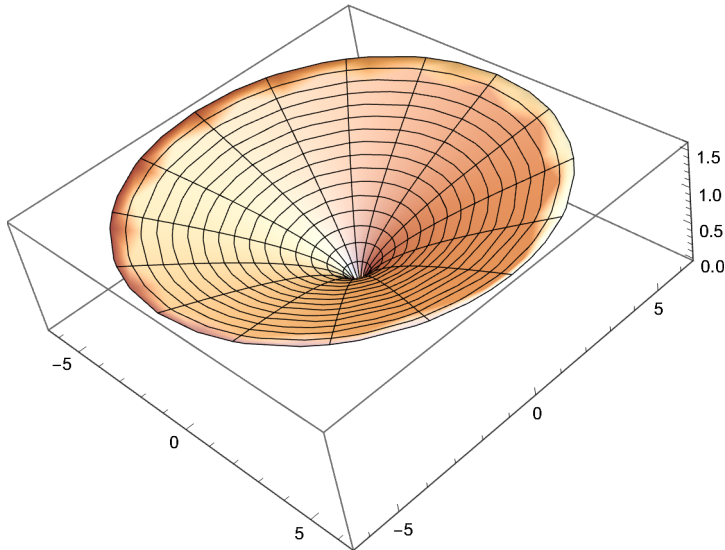


```
Solve[c == (sqrt(-1.1294090667581471`*^18 theta +
8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2)) /
(sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)), beta]
{{beta -> -1.
ArcSin[(sqrt(theta) sqrt(-1.34523 * 10^24 + 4.48719 * 10^15 c + 1.0705 * 10^23 theta - 3.57079 * 10^14 c theta)) /
(sqrt(-4.22615 * 10^24 + 1.40969 * 10^16 c))]}, {beta ->
ArcSin[(sqrt(theta) sqrt(-1.34523 * 10^24 + 4.48719 * 10^15 c + 1.0705 * 10^23 theta - 3.57079 * 10^14 c theta)) /
(sqrt(-4.22615 * 10^24 + 1.40969 * 10^16 c))]}]}
```

```
Solve[c == (sqrt(-1.1294090667581471`*^18 theta +
8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2)) /
(sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)), theta]
{}
```

```
c := (2.99 * 10^8)
```

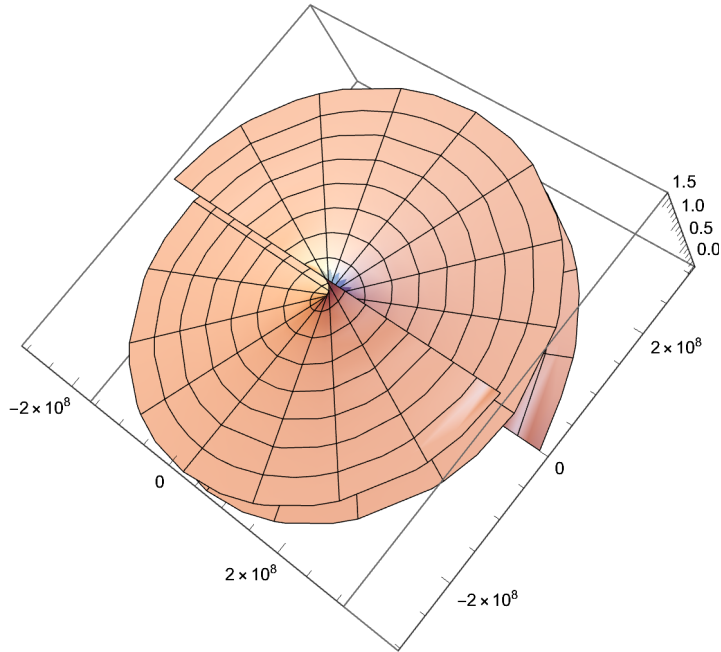
```
RevolutionPlot3D[ArcSin[(sqrt(theta) sqrt(-1.3452259606784795`*^24 + 4.487190804107819`*^15 c +
1.0704968060876181`*^23 theta - 3.57079298535128`*^14 c theta)) /
(sqrt(-4.226151995485783`*^24 + 1.40969256654408`*^16 c))], {theta, -2 pi, 2 pi}]
```



```

RevolutionPlot3D[ArcSin[ $\left(\sqrt{\theta} \sqrt{(-1.3452259606784795 \cdot 10^{24} + 4.487190804107819 \cdot 10^{15} c + 1.0704968060876181 \cdot 10^{23} \theta - 3.57079298535128 \cdot 10^{14} c \theta)}\right) / \left(\sqrt{-4.226151995485783 \cdot 10^{24} + 1.40969256654408 \cdot 10^{16} c}\right)$ ],
{c, -(2.99 \cdot 10^8), (2.99 \cdot 10^8)}, {\theta, -2 \pi, 2 \pi}]

```



```

Solve[ $\theta \text{ Energy} == 2 \pi \text{ Energy} - 2 \pi \sqrt{(\text{Energy}^2 - (m c^2)^2)}$ , Energy]

```

```

{{Energy ->  $-\frac{2 c^2 m \pi}{\sqrt{4 \pi \theta - \theta^2}}$ }, {Energy ->  $\frac{2 c^2 m \pi}{\sqrt{4 \pi \theta - \theta^2}}$ }}

```

```

Solve[ $\text{Energy}^2 == (p v)^2 + (m c^2)^2$ , m]

```

```

{{m ->  $-\frac{i \sqrt{-\text{Energy}^2 + p^2 v^2}}{c^2}$ }, {m ->  $\frac{i \sqrt{-\text{Energy}^2 + p^2 v^2}}{c^2}$ }}

```

```

Solve[ $\text{Energy}^2 == (p v)^2 + (m c^2)^2$ , Energy]

```

```

{{Energy ->  $-\sqrt{c^4 m^2 + p^2 v^2}$ }, {Energy ->  $\sqrt{c^4 m^2 + p^2 v^2}$ }}

```

$$\text{Solve}\left[\frac{2 \pi m c^2}{\sqrt{4 \pi \theta - \theta^2}} = \sqrt{c^4 m^2 + (m v)^2 v^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 1.52668 \times 10^{-8} \left(4.11558 \times 10^8 + \frac{8.8193 \times 10^{25}}{8.07761 \times 10^{33} + v^4} - \right.\right.\right. \\ \left.\left.\left.1. \sqrt{1.6938 \times 10^{17} + \frac{7.77801 \times 10^{51}}{(8.07761 \times 10^{33} + v^4)^2} - \frac{1.36819 \times 10^{51}}{8.07761 \times 10^{33} + v^4}}\right)\right\}, \right. \\ \left.\left\{\theta \rightarrow 1.52668 \times 10^{-8} \left(4.11558 \times 10^8 + \frac{8.8193 \times 10^{25}}{8.07761 \times 10^{33} + v^4} + \right.\right.\right. \\ \left.\left.\left.\sqrt{1.6938 \times 10^{17} + \frac{7.77801 \times 10^{51}}{(8.07761 \times 10^{33} + v^4)^2} - \frac{1.36819 \times 10^{51}}{8.07761 \times 10^{33} + v^4}}\right)\right\}\right\}$$

$$\theta := 1.526682874746296 \cdot 10^{-8}$$

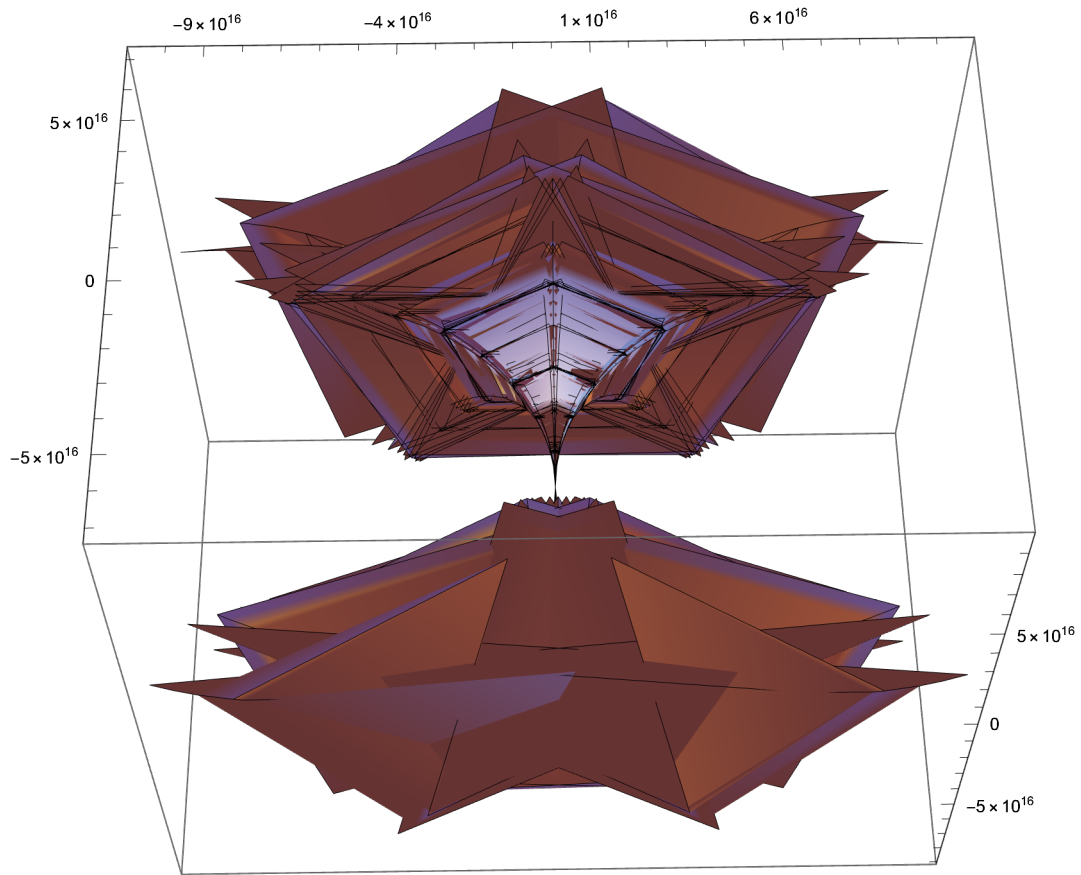
$$\left(4.11557987 \cdot 10^8 + \frac{8.819302218404142 \cdot 10^{25}}{8.07760871306249 \cdot 10^{33} + v^4} + \sqrt{1.6937997666349216 \cdot 10^{17} + \right. \\ \left.\frac{7.778009161954823 \cdot 10^{51}}{(8.07760871306249 \cdot 10^{33} + v^4)^2} - \frac{1.3681851753153453 \cdot 10^{51}}{8.07760871306249 \cdot 10^{33} + v^4}}\right) \\ \left(m \sqrt{2.86605126458116 \cdot 10^{52} - 3.1889121001887717 \cdot 10^{35} v^2}\right) / \\ \left(\sqrt{\theta} \sqrt{1.1294090667581471 \cdot 10^{18} - \right. \\ \left.12.566370614359172 \cdot v^2 - 8.987551787368176 \cdot 10^{16} \theta + v^2 \theta}\right)$$

Energy ==

$$\begin{aligned}
& \left( 8093.298956544235 \text{ m } \sqrt{2.86605126458116 \cdot v^{52} - 3.1889121001887717 \cdot v^{35}} \right) / \\
& \left( \sqrt{\left( 4.11557987 \cdot v^8 + \frac{8.819302218404142 \cdot v^{25}}{8.07760871306249 \cdot v^{33} + v^4} + \sqrt{\left( 1.6937997666349216 \cdot v^{17} + \right.} \right. \right. \\
& \quad \left. \left. \frac{7.778009161954823 \cdot v^{51}}{(8.07760871306249 \cdot v^{33} + v^4)^2} - \frac{1.3681851753153453 \cdot v^{51}}{8.07760871306249 \cdot v^{33} + v^4} \right) \right) \\
& \sqrt{\left( 1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2 - 1.3721141399670458 \cdot v^9 \right.} \\
& \quad \left. \left( 4.11557987 \cdot v^8 + \frac{8.819302218404142 \cdot v^{25}}{8.07760871306249 \cdot v^{33} + v^4} + \sqrt{\left( 1.6937997666349216 \cdot v^{17} + \right.} \right. \right. \\
& \quad \left. \left. \frac{7.778009161954823 \cdot v^{51}}{(8.07760871306249 \cdot v^{33} + v^4)^2} - \frac{1.3681851753153453 \cdot v^{51}}{8.07760871306249 \cdot v^{33} + v^4} \right) \right) + \\
& 1.526682874746296 \cdot v^{-8} v^2 \left( 4.11557987 \cdot v^8 + \frac{8.819302218404142 \cdot v^{25}}{8.07760871306249 \cdot v^{33} + v^4} + \right. \\
& \quad \left. \sqrt{\left( 1.6937997666349216 \cdot v^{17} + \frac{7.778009161954823 \cdot v^{51}}{(8.07760871306249 \cdot v^{33} + v^4)^2} - \right.} \right. \\
& \quad \left. \left. \frac{1.3681851753153453 \cdot v^{51}}{8.07760871306249 \cdot v^{33} + v^4} \right) \right) \right)
\end{aligned}$$

```

SphericalPlot3D[
  (8093.298956544235` m  $\sqrt{2.86605126458116` * ^{52} - 3.1889121001887717` * ^{35} v^2}$ ) /
  (
 $\sqrt{\left(4.11557987` * ^8 + \frac{8.819302218404142` * ^{25}}{8.07760871306249` * ^{33} + v^4} + \sqrt{\left(1.6937997666349216` * ^{17} + \frac{7.778009161954823` * ^{51}}{(8.07760871306249` * ^{33} + v^4)^2} - \frac{1.3681851753153453` * ^{51}}{8.07760871306249` * ^{33} + v^4}\right)}\right)}$ 
 $\sqrt{\left(1.1294090667581471` * ^{18} - 12.566370614359172` v^2 - 1.3721141399670458` * ^9\right)}$ 
 $\left(4.11557987` * ^8 + \frac{8.819302218404142` * ^{25}}{8.07760871306249` * ^{33} + v^4} + \sqrt{\left(1.6937997666349216` * ^{17} + \frac{7.778009161954823` * ^{51}}{(8.07760871306249` * ^{33} + v^4)^2} - \frac{1.3681851753153453` * ^{51}}{8.07760871306249` * ^{33} + v^4}\right)}\right) +$ 
 $1.526682874746296` * ^{-8} v^2 \left(4.11557987` * ^8 + \frac{8.819302218404142` * ^{25}}{8.07760871306249` * ^{33} + v^4} + \sqrt{\left(1.6937997666349216` * ^{17} + \frac{7.778009161954823` * ^{51}}{(8.07760871306249` * ^{33} + v^4)^2} - \frac{1.3681851753153453` * ^{51}}{8.07760871306249` * ^{33} + v^4}\right)}\right) \right) \right) \right), \{m, -1, 1\}, \{v, -c, c\}]$ 
```



$$\begin{aligned}
& \text{SphericalPlot3D}\left[ \right. \\
& \left( 8093.298956544235 \, m \sqrt{2.86605126458116 \, v^{52} - 3.1889121001887717 \, v^{35}} \right) / \\
& \left( \sqrt{\left( 4.11557987 \, v^8 + \frac{8.819302218404142 \, v^{25}}{8.07760871306249 \, v^{33} + v^4} + \sqrt{\left( 1.6937997666349216 \, v^{17} + \right.} \right. \right. \\
& \left. \left. \frac{7.778009161954823 \, v^{51}}{(8.07760871306249 \, v^{33} + v^4)^2} - \frac{1.3681851753153453 \, v^{51}}{8.07760871306249 \, v^{33} + v^4} \right) \right) \\
& \sqrt{\left( 1.1294090667581471 \, v^{18} - 12.566370614359172 \, v^2 - 1.3721141399670458 \, v^9 \right.} \\
& \left. \left( 4.11557987 \, v^8 + \frac{8.819302218404142 \, v^{25}}{8.07760871306249 \, v^{33} + v^4} + \sqrt{\left( 1.6937997666349216 \, v^{17} + \right.} \right. \right. \\
& \left. \left. \frac{7.778009161954823 \, v^{51}}{(8.07760871306249 \, v^{33} + v^4)^2} - \frac{1.3681851753153453 \, v^{51}}{8.07760871306249 \, v^{33} + v^4} \right) \right) + \\
& 1.526682874746296 \, v^{-8} v^2 \left( 4.11557987 \, v^8 + \frac{8.819302218404142 \, v^{25}}{8.07760871306249 \, v^{33} + v^4} + \right. \\
& \sqrt{\left( 1.6937997666349216 \, v^{17} + \frac{7.778009161954823 \, v^{51}}{(8.07760871306249 \, v^{33} + v^4)^2} - \right.} \\
& \left. \left. \frac{1.3681851753153453 \, v^{51}}{8.07760871306249 \, v^{33} + v^4} \right) \right) \left. \right], \{m, -10^{-41}, 10^{-41}\}, \{v, -4 \, c, 4 \, c\}
\end{aligned}$$

$$1. \times 10^{-23}$$

$$0$$

$$-1. \times 10^{-23}$$

$$-2. \times 10^{-65}$$

$$-2. \times 10^{-65}$$

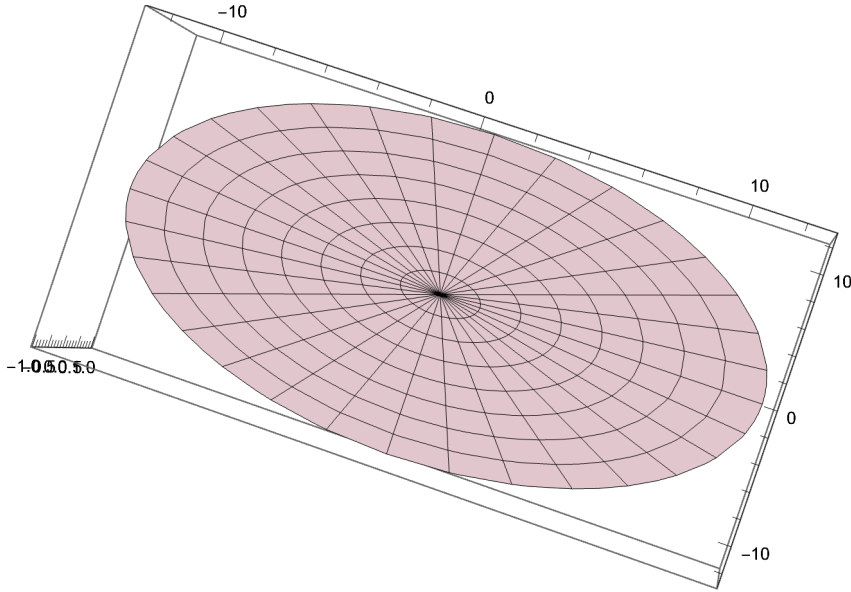
$$\text{Solve}\left[\frac{2 \pi m c^2}{\sqrt{4 \pi \theta - \theta^2}} == \left(m \sqrt{2.86605126458116 \cdot^{*52} - 3.1889121001887717 \cdot^{*35} v^2}\right) / \right. \\ \left. \left(\sqrt{\theta} \sqrt{\left(1.1294090667581471 \cdot^{*18} - \right. \right. \right. \\ \left. \left. \left. 12.566370614359172 \cdot v^2 - 8.987551787368176 \cdot^{*16} \theta + v^2 \theta\right)\right)}, v\right] \\ \left\{\left\{v \rightarrow -\left(\left(1. \sqrt{\left(1.55683 \times 10^{74} - 1.92734 \times 10^{40} c^4 - 1.23889 \times 10^{73} \theta + 1.53373 \times 10^{39} c^4 \theta\right)}\right) / \right. \right. \right. \\ \left. \left. \left. \left(\sqrt{\left(1.73221 \times 10^{57} - 2.14445 \times 10^{23} c^4 - 1.37845 \times 10^{56} \theta + 1.7065 \times 10^{22} c^4 \theta\right)}\right)\right)\right\}, \right. \\ \left. \left\{v \rightarrow \frac{\sqrt{1.55683 \times 10^{74} - 1.92734 \times 10^{40} c^4 - 1.23889 \times 10^{73} \theta + 1.53373 \times 10^{39} c^4 \theta}}{\sqrt{1.73221 \times 10^{57} - 2.14445 \times 10^{23} c^4 - 1.37845 \times 10^{56} \theta + 1.7065 \times 10^{22} c^4 \theta}}\right\}\right\}$$



```

RevolutionPlot3D[
  (√(1.5568291164930838`^74 - 1.9273391071487519`^40 c^4 - 1.2388852471963122`^73 θ +
    1.5337277295852198`^39 c^4 θ)) /
  (√(1.732206003731935`^57 - 2.14445396560339`^23 c^4 - 1.3784457397369778`^56 θ +
    1.706502244293984`^22 c^4 (2 (π + √(π^2 - π^2 Sin[β]^2)))))),
  {θ, -4 π, 4 π}, {β, -π / 2, π / 2}]

```



```

Energy → (m √(2.86605126458116`^52 - 3.1889121001887717`^35 v^2)) /
  (√θ √(1.1294090667581471`^18 -
    12.566370614359172` v^2 - 8.987551787368176`^16 θ + v^2 θ))

```

```

Solve[Energy == (2 π m c^2) / √(4 π θ - θ^2), θ]

```

$$\left\{ \left\{ \theta \rightarrow \frac{2 \left( \text{Energy}^2 - \sqrt{\text{Energy}^4 - c^4 \text{Energy}^2 m^2} \right) \pi}{\text{Energy}^2} \right\}, \right.$$

$$\left. \left\{ \theta \rightarrow \frac{2 \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - c^4 \text{Energy}^2 m^2} \right) \pi}{\text{Energy}^2} \right\} \right\}$$

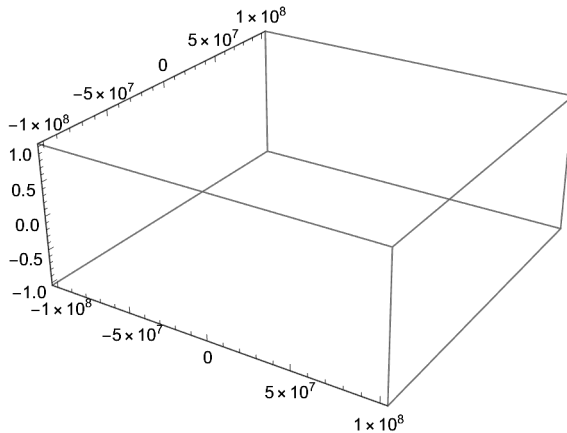
$$\sqrt{c^4 m^2 + p^2 v^2}$$

$$\frac{2 c^2 m \pi}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\theta \text{ Energy} == 2 \pi \text{ Energy} - 2 \pi \sqrt{(\text{Energy}^2 - (m c^2)^2)} , \theta\right]$$

$$\left\{\left\{\theta \rightarrow -\frac{2 \left(-\text{Energy} \pi + \sqrt{\text{Energy}^2 - c^4 m^2} \pi\right)}{\text{Energy}}\right\}\right\}$$

$$\text{Plot3D}\left[-\frac{2 \left(-\text{Energy} \pi + \sqrt{\text{Energy}^2 - c^4 m^2} \pi\right)}{\text{Energy}}, \{m, -10^8, 10^8\}, \{\text{Energy}, -10^8, 10^8\}\right]$$



$$c := 2.99792458 (10^8)$$

$$\text{Solve}\left[\theta \text{ Energy} == 2 \pi \text{ Energy} - 2 \pi \sqrt{(\text{Energy}^2 - (m c^2)^2)} , m\right]$$

$$\left\{\left\{m \rightarrow -3.09434 \times 10^{-22} \text{ Energy} \sqrt{4.11558 \times 10^8 - 3.27507 \times 10^7 \theta} \sqrt{\theta}\right\},\right. \\ \left.\left\{m \rightarrow 3.09434 \times 10^{-22} \text{ Energy} \sqrt{4.11558 \times 10^8 - 3.27507 \times 10^7 \theta} \sqrt{\theta}\right\}\right\}$$

$$\text{Solve}\left[\theta \text{ Energy} == 2 \pi \text{ Energy} - 2 \pi \sqrt{(\text{Energy}^2 - (h)^2)} , h\right]$$

$$\left\{\left\{h \rightarrow -\frac{\sqrt{4 \text{ Energy}^2 \pi \theta - \text{Energy}^2 \theta^2}}{2 \pi}\right\}, \left\{h \rightarrow \frac{\sqrt{4 \text{ Energy}^2 \pi \theta - \text{Energy}^2 \theta^2}}{2 \pi}\right\}\right\}$$

$$\frac{\sqrt{4 \text{ Energy}^2 \pi \theta - \text{Energy}^2 \theta^2}}{2 \pi}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \frac{\sqrt{4 \text{ Energy}^2 \pi \theta - \text{Energy}^2 \theta^2}}{2 \pi}, \text{Energy}\right]$$

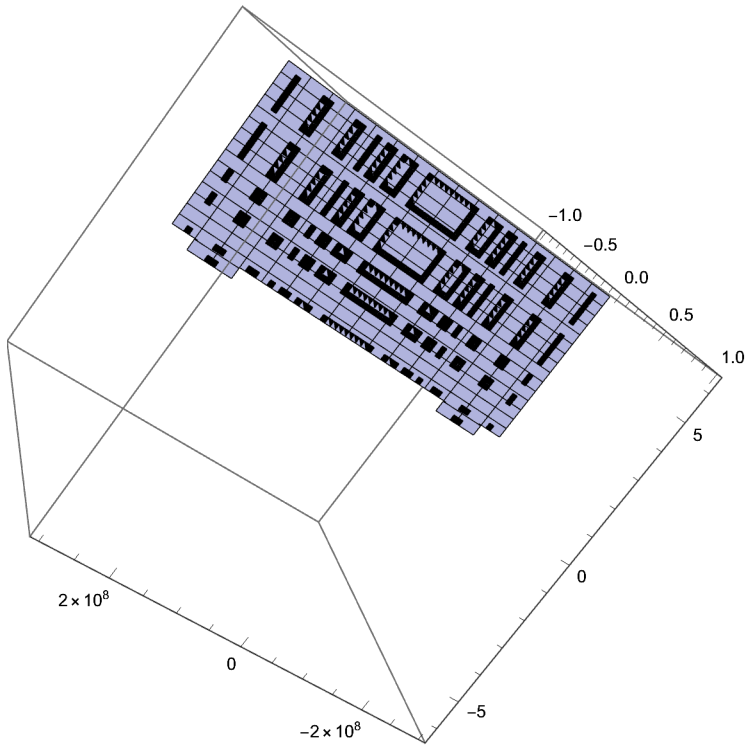
$$\{\{\text{Energy} \rightarrow -1. r\}, \{\text{Energy} \rightarrow r\}\}$$

$$\text{Solve}\left[\frac{\sqrt{\text{Energy}} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi \text{Energy} - \text{Energy} \theta}}{2 \pi} = m c^2, \text{Energy}\right]$$

$$\left\{\left\{\text{Energy} \rightarrow -\frac{1. m \sqrt{2.86605 \times 10^{52} - 3.18891 \times 10^{35} v^2}}{\sqrt{\theta} \sqrt{1.12941 \times 10^{18} - 12.5664 v^2 - 8.98755 \times 10^{16} \theta + v^2 \theta}}\right\},\right.$$

$$\left.\left\{\text{Energy} \rightarrow \frac{m \sqrt{2.86605 \times 10^{52} - 3.18891 \times 10^{35} v^2}}{\sqrt{\theta} \sqrt{1.12941 \times 10^{18} - 12.5664 v^2 - 8.98755 \times 10^{16} \theta + v^2 \theta}}\right\}\right\}$$

$$\text{ContourPlot3D}\left[\left(m \sqrt{2.86605126458116 \cdot 10^{52} - 3.1889121001887717 \cdot 10^{35} v^2}\right) / \left(\sqrt{\theta} \sqrt{(1.1294090667581471 \cdot 10^{18} - 12.566370614359172 \cdot v^2 - 8.987551787368176 \cdot 10^{16} \theta + v^2 \theta)}\right)\right], \{m, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{v, -c, c\}]$$



$$\left(m \sqrt{2.86605126458116 \cdot 10^{52} - 3.1889121001887717 \cdot 10^{35} v^2}\right) / \left(\sqrt{\theta} \sqrt{(1.1294090667581471 \cdot 10^{18} - 12.566370614359172 \cdot v^2 - 8.987551787368176 \cdot 10^{16} \theta + v^2 \theta)}\right)$$

$$\text{Solve}\left[\frac{\sqrt{\text{Energy}} \sqrt{1 - \frac{(v)^2}{c^2}}}{2 \pi} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi \text{Energy} - \text{Energy} \theta} = m c^2, v\right]$$

$$\left\{ \left\{ v \rightarrow - \left( \left( 1. \sqrt{2.86605 \times 10^{52} \text{ m}^2 - 1.12941 \times 10^{18} \text{ Energy}^2 \theta + 8.98755 \times 10^{16} \text{ Energy}^2 \theta^2} \right) / \left( \sqrt{3.18891 \times 10^{35} \text{ m}^2 - 12.5664 \text{ Energy}^2 \theta + \text{Energy}^2 \theta^2} \right) \right) \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{2.86605 \times 10^{52} \text{ m}^2 - 1.12941 \times 10^{18} \text{ Energy}^2 \theta + 8.98755 \times 10^{16} \text{ Energy}^2 \theta^2}}{\sqrt{3.18891 \times 10^{35} \text{ m}^2 - 12.5664 \text{ Energy}^2 \theta + \text{Energy}^2 \theta^2}} \right\} \right\}$$

$$\text{Solve}\left[\frac{\sqrt{\text{Energy}} \sqrt{1 - \frac{(v)^2}{c^2}}}{2 \pi} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi \text{Energy} - \text{Energy} \theta} = \text{Energy Sin}[\beta], v\right]$$

$$\left\{ \left\{ v \rightarrow - \frac{1. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \text{ Sin}[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \text{ Sin}[\beta]^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \text{ Sin}[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \text{ Sin}[\beta]^2}} \right\} \right\}$$

$$\text{Solve}\left[\frac{\sqrt{\text{Energy}} \sqrt{1 - \frac{(v)^2}{c^2}}}{2 \pi} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi \text{Energy} - \text{Energy} \theta} = m c^2, v\right]$$

$$\left\{ \left\{ v \rightarrow - \left( \left( 1. \sqrt{2.86605 \times 10^{52} \text{ m}^2 - 1.12941 \times 10^{18} \text{ Energy}^2 \theta + 8.98755 \times 10^{16} \text{ Energy}^2 \theta^2} \right) / \left( \sqrt{3.18891 \times 10^{35} \text{ m}^2 - 12.5664 \text{ Energy}^2 \theta + \text{Energy}^2 \theta^2} \right) \right) \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{2.86605 \times 10^{52} \text{ m}^2 - 1.12941 \times 10^{18} \text{ Energy}^2 \theta + 8.98755 \times 10^{16} \text{ Energy}^2 \theta^2}}{\sqrt{3.18891 \times 10^{35} \text{ m}^2 - 12.5664 \text{ Energy}^2 \theta + \text{Energy}^2 \theta^2}} \right\} \right\}$$

$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \left( \sqrt{2.86605126458116 \times 10^{52} \text{ m}^2 - 1.1294090667581471 \times 10^{18} r^2 \theta + 8.987551787368176 \times 10^{16} r^2 \theta^2} \right) / \left( \sqrt{3.1889121001887717 \times 10^{35} \text{ m}^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2} \right), m \right]$$

{ }

$$p c = \frac{2 \pi \text{Energy} - \text{Energy} \theta}{2 \pi} =$$

$$m \left( \left( \sqrt{2.86605126458116 \times 10^{52} \text{ m}^2 - 1.1294090667581471 \times 10^{18} \text{ Energy}^2 \theta + 8.987551787368176 \times 10^{16} \text{ Energy}^2 \theta^2} \right) / \left( \sqrt{3.1889121001887717 \times 10^{35} \text{ m}^2 - 12.566370614359172 \text{ Energy}^2 \theta + \text{Energy}^2 \theta^2} \right) \right)$$

$$\text{Solve}\left[\frac{2 \pi \text{Energy} - \text{Energy} \theta}{2 \pi} == \right.$$

$$\left. m \left( \left( \sqrt{\left( 2.86605126458116 \cdot 10^{52} \text{m}^2 - 1.1294090667581471 \cdot 10^{18} \text{Energy}^2 \theta + \right.} \right. \right.$$

$$\left. \left. 8.987551787368176 \cdot 10^{16} \text{Energy}^2 \theta^2 \right) \right) / \left( \sqrt{\left( 3.1889121001887717 \cdot 10^{35} \text{m}^2 - \right.} \right.$$

$$\left. \left. 12.566370614359172 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \theta^2 \right) \right) \right), \text{Energy}]$$

$$\left\{ \left\{ \text{Energy} \rightarrow - \frac{2.07755 \times 10^{24} \text{m}}{-6.92997 \times 10^{15} + 1.10294 \times 10^{15} \theta} \right\} \right\}$$

$$\text{Energy} == - \frac{2.077551912824036 \cdot 10^{24} \text{m}}{-6.929967240283397 \cdot 10^{15} + 1.102938541756003 \cdot 10^{15} \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}}$$

$$\text{Solve}\left[\text{Energy} == - \frac{2.077551912824036 \cdot 10^{24} \text{m}}{-6.929967240283397 \cdot 10^{15} + 1.102938541756003 \cdot 10^{15} \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}}, m\right]$$

$$\left\{ \left\{ m \rightarrow -4.81336 \times 10^{-25} \text{Energy} \left( -6.92997 \times 10^{15} + \frac{6.92997 \times 10^{15} \left( r^2 + \sqrt{r^4 - 1. r^2 \eta^2} \right)}{r^2} \right) \right\} \right\}$$

$$\frac{2 \pi \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - \text{Energy}^2 (m c^2)^2} \right)}{\text{Energy}^2}$$

$$\frac{2 \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - 8.07761 \times 10^{33} \text{Energy}^2 \text{m}^2} \right) \pi}{\text{Energy}^2}$$

$$x == \frac{2 \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - 8.07760871306249 \cdot 10^{33} \text{Energy}^2 \text{m}^2} \right) \pi}{\text{Energy}^2}$$

$$\text{Energy} == \frac{2 \pi m c^2}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Energy} == \frac{2 \pi m c^2}{\sqrt{4 \pi \theta - \theta^2}} == \frac{2 \pi r \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\frac{2 \pi m c^2}{\sqrt{4 \pi \theta - \theta^2}} == \frac{2 \pi \text{Energy} \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \text{Energy}\right]$$

$$\left\{ \left\{ \text{Energy} \rightarrow 8.98755 \times 10^{16} \text{m Csc}[\beta] \right\} \right\}$$

$$8.987551787368176 \cdot 10^{16} \text{m Csc}[\beta]$$

$$\text{Solve}\left[\frac{2 \pi m c^2}{\sqrt{4 \pi \theta - \theta^2}} == \frac{2 \pi \text{Energy} \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, m\right]$$

$$\left\{ \left\{ m \rightarrow 1.11265 \times 10^{-17} \text{Energy Sin}[\beta] \right\} \right\}$$

$$m == 1.1126500560536183 \cdot 10^{-17} \text{ Energy (m c}^2) / \text{Energy}$$

$$m == 1. m$$

$$\left\{ \left\{ r \rightarrow \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right\} \right\}$$

$$\beta := \text{ArcSin}[(m c^2) / r]$$

$$\theta := \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 (m c^2)^2} \right)}{r^2}$$

$$\text{Solve} \left[ r == \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right), m \right]$$

{}

$$\text{Solve} \left[ m == -4.813357460900654 \cdot 10^{-25} r \right.$$

$$\left. \left( -6.929967240283397 \cdot 10^{15} + \frac{6.929967240283397 \cdot 10^{15} \left( r^2 + \sqrt{r^4 - 1. \cdot r^2 \eta^2} \right)}{r^2} \right), \eta \right]$$

{}

$$\frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}$$

$$- (2.077551912824036 \cdot 10^{24} m) / \left( -6.929967240283397 \cdot 10^{15} + \right.$$

$$\left. \frac{1.102938541756003 \cdot 10^{15} \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - \text{Energy}^2 (m c^2)^2} \right)}{r^2} \right)$$

$$- \frac{2.07755 \times 10^{24} m}{-6.92997 \times 10^{15} + \frac{6.92997 \times 10^{15} \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - 8.07761 \times 10^{33} \text{Energy}^2 m^2} \right)}{r^2}}$$

$$- \frac{2.07755 \times 10^{24} m}{-6.92997 \times 10^{15} + \frac{6.92997 \times 10^{15} \left( \text{Energy}^2 + \sqrt{\text{Energy}^4 - 8.07761 \times 10^{33} \text{Energy}^2 m^2} \right)}{r^2}}$$

```
Solve[ $\left(\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \vartheta^2 + 3.5481432270250993 \cdot \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) == \left(\sqrt{(2.86605126458116 \cdot m^2 - 1.1294090667581471 \cdot \text{Energy}^2 \theta + 8.987551787368176 \cdot \text{Energy}^2 \vartheta^2)}\right) / \left(\sqrt{(3.1889121001887717 \cdot m^2 - 12.566370614359172 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \vartheta^2)}\right), m]$ 
{{}}
```

```
 $\left(\sqrt{(2.86605126458116 \cdot m^2 - 1.1294090667581471 \cdot \text{Energy}^2 \theta + 8.987551787368176 \cdot \text{Energy}^2 \vartheta^2)}\right) / \left(\sqrt{(3.1889121001887717 \cdot m^2 - 12.566370614359172 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \vartheta^2)}\right)$ 
```

```
Solve[ $\left(\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \vartheta^2 + 3.5481432270250993 \cdot \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) == \left(\sqrt{(2.86605126458116 \cdot m^2 - 1.1294090667581471 \cdot \text{Energy}^2 \theta + 8.987551787368176 \cdot \text{Energy}^2 \vartheta^2)}\right) / \left(\sqrt{(3.1889121001887717 \cdot m^2 - 12.566370614359172 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \vartheta^2)}\right), \text{Energy}]$ 
{{}}
```

```
Solve[ $\left(\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \vartheta^2 + 3.5481432270250993 \cdot \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) == \left(\sqrt{(2.86605126458116 \cdot m^2 - 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \vartheta^2)}\right) / \left(\sqrt{(3.1889121001887717 \cdot m^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \vartheta^2)}\right), \text{Energy}]$ 
{{}}
```

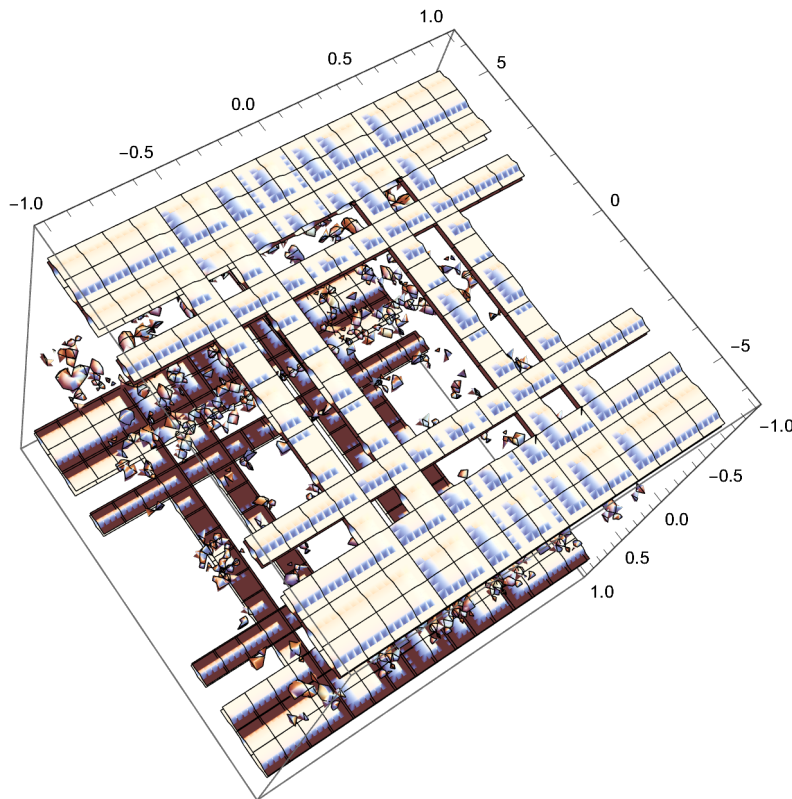
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Export["davincisprize.dae",
ContourPlot3D[ $\left(\sqrt{(2.86605126458116 \cdot \text{Energy}^2 \theta + 8.987551787368176 \cdot \text{Energy}^2 \vartheta^2)}\right) / \left(\sqrt{(3.1889121001887717 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \vartheta^2)}\right), \{m, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\text{Energy}, -1, 1\}]$ 

```

```
$Failed
```

```
Export["davincisprize.obj",
  ContourPlot3D[( $\sqrt{(2.86605126458116 \cdot 10^{52} \text{ m}^2 - 1.1294090667581471 \cdot 10^{18} \text{ Energy}^2 \theta + 8.987551787368176 \cdot 10^{16} \text{ Energy}^2 \theta^2)}$ )/
    ( $\sqrt{(3.1889121001887717 \cdot 10^{35} \text{ m}^2 - 12.566370614359172 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \theta^2)}$ )],
  {m, -1, 1}, {θ, -2 π, 2 π}, {Energy, -1, 1}]
davincisprize.obj
```

```
ContourPlot3D[( $\sqrt{(2.86605126458116 \cdot 10^{52} \text{ m}^2 - 1.1294090667581471 \cdot 10^{18} \text{ Energy}^2 \theta + 8.987551787368176 \cdot 10^{16} \text{ Energy}^2 \theta^2)}$ )/
  ( $\sqrt{(3.1889121001887717 \cdot 10^{35} \text{ m}^2 - 12.566370614359172 \cdot \text{Energy}^2 \theta + \text{Energy}^2 \theta^2)}$ )],
  {m, -1, 1}, {θ, -2 π, 2 π}, {Energy, -1, 1}]
```



```
v := ( $\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}$ )/
  ( $\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}$ )
```



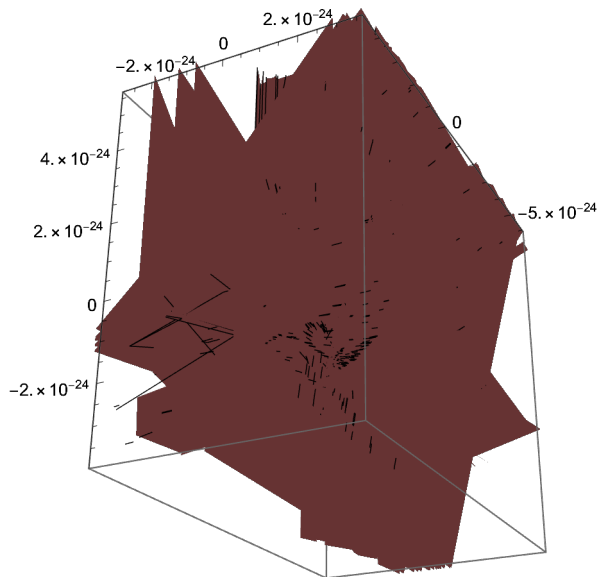
SphericalPlot3D[  

$$\left( \left( 7.372495999759142 \cdot 10^{-51} \left( 1.6880179234807384 \cdot 10^{10} \theta \sqrt{-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin^2[\beta]} \right) - 4.029845948245144 \cdot 10^9 \theta^2 \sqrt{-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin^2[\beta]} \right) + 2.1378996752068695 \cdot 10^8 \theta^3 \sqrt{-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin^2[\beta]} \right) \Bigg) /$$
  

$$\left( -12.566370614359172 \cdot \theta \sqrt{-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin^2[\beta]} \right) + 1. \cdot \theta^2 \sqrt{-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin^2[\beta]} \Bigg) + 6.283185307179586 \cdot \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2 \sin^2[\beta]} \sqrt{-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin^2[\beta]} \Bigg) \Bigg) /$$
  

$$\sqrt{2.86605126458116 \cdot 10^{52} - 3.1889121001887717 \cdot 10^{35} v^2} \Bigg) /$$
  

$$\left( \sqrt{\theta} \sqrt{1.1294090667581471 \cdot 10^{18} - 12.566370614359172 \cdot v^2 - 8.987551787368176 \cdot 10^{16} \theta + v^2 \theta} \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} ]$$



$$r == m c^2$$

$$\text{Solve}\left[e^{\pm 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \frac{r^2}{c^2 m}} \right)} == \right.$$

$$\left. \pm \sin\left[-\frac{2 \left( -r \pi + \sqrt{r^2 - c^4 m^2} \pi \right)}{r} \right] + \cos\left[-\frac{2 \left( -r \pi + \sqrt{r^2 - c^4 m^2} \pi \right)}{r} \right], c \right]$$

$$\text{Solve}\left[e^{2 \pm \left( \pi + \sqrt{\pi^2 - \frac{\pi^2 r^2}{c^4 m^2}} \right)} == \cos\left[\frac{2 \left( -\pi r + \pi \sqrt{-c^4 m^2 + r^2} \right)}{r} \right] - \pm \sin\left[\frac{2 \left( -\pi r + \pi \sqrt{-c^4 m^2 + r^2} \right)}{r} \right], c \right]$$

$$\text{Solve}\left[\frac{r \sqrt{\pi^2 - \text{ArcCos}\left[\sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{1 - \sin\left[-\frac{2 \left( -r \pi + \sqrt{r^2 - c^4 m^2} \pi \right)}{r} \right]^2}}\right]^2}}{\pi} == m c^2, r \right]$$

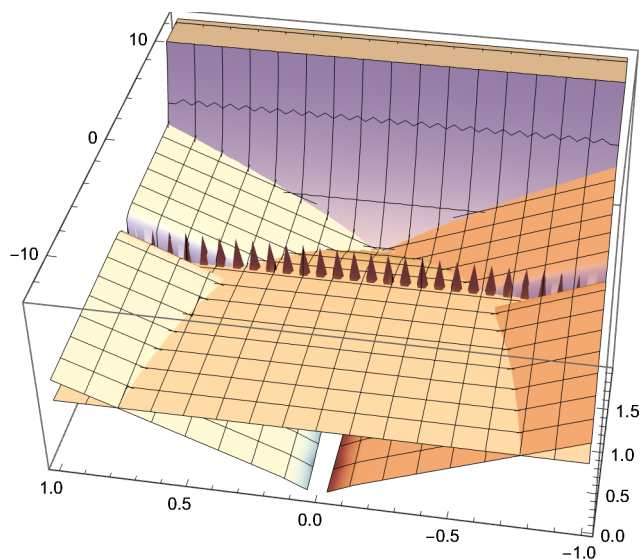
$$\text{Solve}\left[\frac{r \sqrt{\pi^2 - \text{ArcCos}\left[\sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{1 - \sin\left[\frac{2 \left( -\pi r + \pi \sqrt{-c^4 m^2 + r^2} \right)}{r} \right]^2}}\right]^2}}{\pi} == c^2 m, r \right]$$

$$\text{Plot3D}\left[\left\{\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{r\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right.\right.$$

$$\sqrt{(r)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\sqrt{r^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},$$

$$\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2-\left(\frac{r\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\sqrt{(r)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},$$

$$\left.\frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\pi-\theta)}\,\theta\,\text{Csc}[\beta]}{\pi\sqrt{4\pi-\theta}}\right\},\{\theta,-13,13\},\{r,-1,1\}]$$



Plot3D[

$$\left\{ \sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}^2 - \left( \frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}, \sqrt{(r)^2 - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}, \right.$$

$$\left( \frac{\sqrt{1 + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}}}{\pi \sqrt{16\pi^2 - 16\pi\theta + 4\theta^2}} - \sqrt{(r)^2 - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} \right),$$

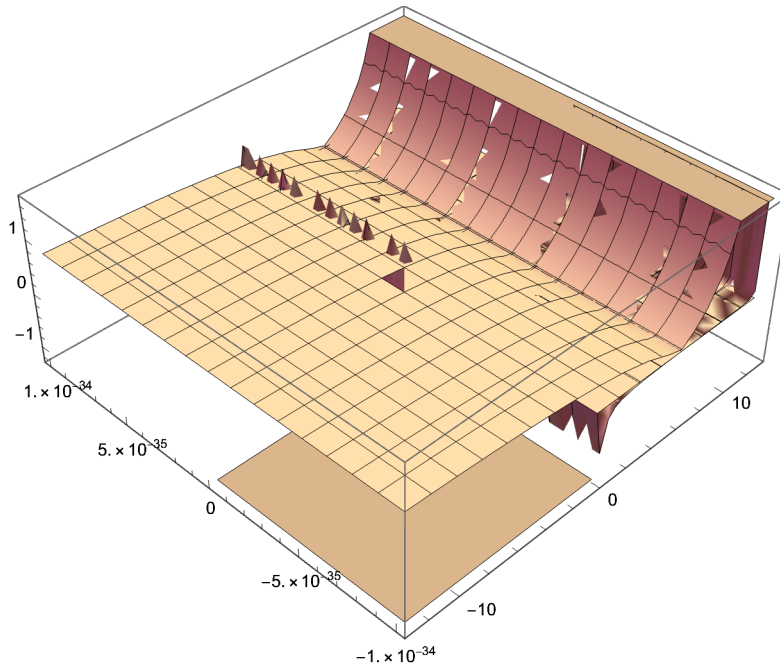
$$2.144571844054625 \cdot 10^{-53} \theta \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}}, \frac{4\pi r^2 - 2r^2\theta}{4320 \sqrt{4\pi r^2\theta - r^2\theta^2}},$$

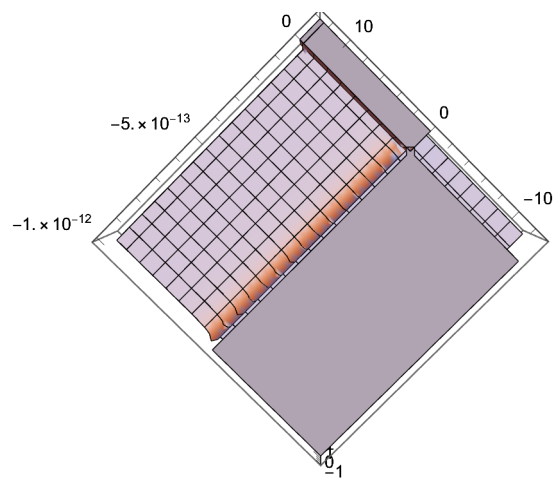
$$\frac{\pi^2 \left( -\frac{540c}{\sqrt{4\pi - (r\theta)} (r\theta)^{3/2}} + \frac{1080c}{(4\pi - (r\theta))^{3/2} \sqrt{(r\theta)}} + \frac{1620c \sqrt{r\theta}}{(4\pi - (r\theta))^{5/2}} \right)}{1166400},$$

$$r \left( \frac{4 \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]}{3} + \frac{2(1 - i\sqrt{3}) \left( \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] \right)}{3(17 + 3\sqrt{33})^{1/3}} - \right.$$

$$\left. \frac{1}{3}(1 + i\sqrt{3})(17 + 3\sqrt{33})^{1/3} \left( \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] \right) \right),$$

$$\left. \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}} \right\}, \{\theta, -13, 13\}, \{r, -10^{34}, 10^{34}\}]$$





$$\text{Solve}\left[\theta == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right), \beta\right]$$

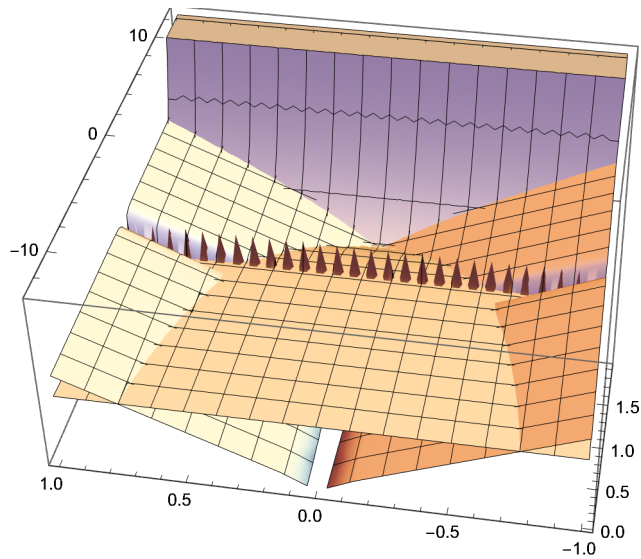
$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin}\left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right\}, \left\{ \beta \rightarrow \text{ArcSin}\left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right\} \right\}$$

$$\text{Plot3D}\left[\left\{\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{r\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right.\right.$$

$$\sqrt{(r)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\sqrt{r^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},$$

$$\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2-\left(\frac{r\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\sqrt{(r)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},$$

$$\left.\frac{1080\text{c}\sqrt{\theta}\sqrt{(4\pi-\theta)}\theta\text{Csc}[\beta]}{\pi\sqrt{4\pi-\theta}}\right\},\{\theta,-13,13\},\{r,-1,1\}]$$



Plot3D[

$$\left\{ \sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}^2 - \left( \frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}, \sqrt{(r)^2 - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}, \right.$$

$$\left( \frac{\sqrt{1 + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}}}{\pi \sqrt{16\pi^2 - 16\pi\theta + 4\theta^2}} - \sqrt{(r)^2 - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} \right),$$

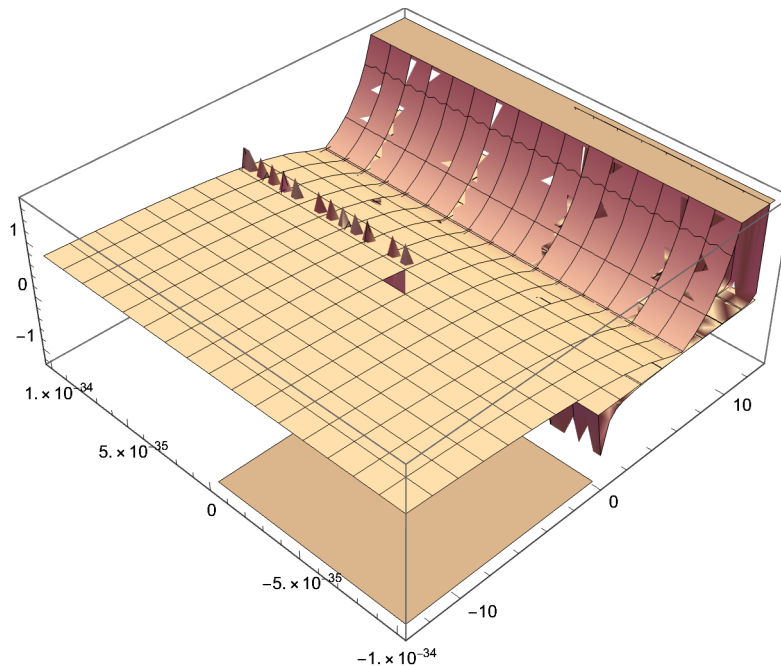
$$2.144571844054625 \cdot 10^{-53} \theta \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}}, \frac{4\pi r^2 - 2r^2\theta}{4320 \sqrt{4\pi r^2\theta - r^2\theta^2}},$$

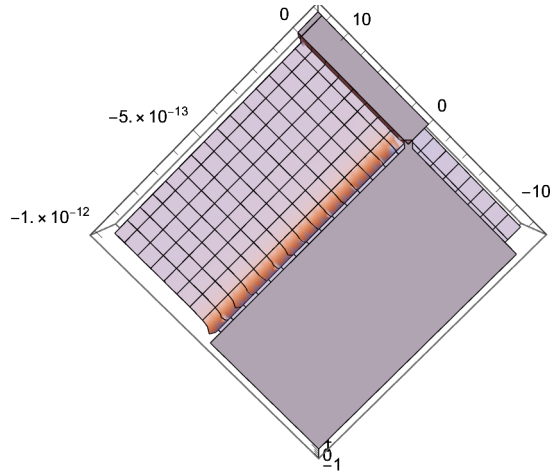
$$\frac{\pi^2 \left( -\frac{540c}{\sqrt{4\pi - (r\theta)} (r\theta)^{3/2}} + \frac{1080c}{(4\pi - (r\theta))^{3/2} \sqrt{(r\theta)}} + \frac{1620c \sqrt{r\theta}}{(4\pi - (r\theta))^{5/2}} \right)}{1166400},$$

$$r \left( \frac{4 \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]}{3} + \frac{2(1 - i\sqrt{3}) \left( \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] \right)}{3(17 + 3\sqrt{33})^{1/3}} - \right.$$

$$\left. \frac{1}{3}(1 + i\sqrt{3})(17 + 3\sqrt{33})^{1/3} \left( \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] \right) \right),$$

$$\left. \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}} \right\}, \{\theta, -13, 13\}, \{r, -10^{-34}, 10^{-34}\}]$$





$$\text{Solve}\left[\theta == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right), \beta\right]$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin}\left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right\}, \left\{ \beta \rightarrow \text{ArcSin}\left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right\} \right\}$$

$$\text{Solve}\left[\left(r/t\right) == \frac{(r/t) 6 (\theta) \pi}{\sqrt{4\pi\theta - \theta^2}} * v, v\right]$$

$$\left\{ \left\{ v \rightarrow \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta} \right\} \right\} \quad (49)$$

$$\text{Solve}\left[n (1/6\theta) == \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}, n\right]$$

$$\left\{ \left\{ n \rightarrow \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \right\} \right\} \quad (50)$$

$$D[\text{hnf}, \theta] = (F_{dm}) = ma$$

$$D\left[h \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} (1/6\theta), \theta\right]$$

$$\frac{h (4\pi - 2\theta)}{12\pi\theta \sqrt{(4\pi - \theta)\theta}} - \frac{h \sqrt{(4\pi - \theta)\theta}}{6\pi\theta^2}$$



$$\text{Solve}\left[\frac{h(4\pi - 2\theta)}{12\pi\theta\sqrt{(4\pi - \theta)\theta}} - \frac{h\sqrt{(4\pi - \theta)\theta}}{6\pi\theta^2} == \right. \\ \left. m \frac{\sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (-80\pi^4 + 224\pi^3\theta - 448\pi^2\theta^2 + 160\pi\theta^3 - 15\theta^4)}{2\theta^2\sqrt{(-2\pi + \theta)^4}(8\pi^2 - 6\pi\theta + \theta^2)^2}, h\right] \\ \left\{\left\{h \rightarrow \frac{m\sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (-80\pi^4 + 224\pi^3\theta - 448\pi^2\theta^2 + 160\pi\theta^3 - 15\theta^4)}{2\theta^2\sqrt{(-2\pi + \theta)^4}(8\pi^2 - 6\pi\theta + \theta^2)^2} \left(\frac{4\pi - 2\theta}{12\pi\theta\sqrt{(4\pi - \theta)\theta}} - \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta^2}\right)\right\}\right\}$$

$$\text{Solve}\left[\frac{h(4\pi - 2\theta)}{12\pi\theta\sqrt{(4\pi - \theta)\theta}} - \frac{h\sqrt{(4\pi - \theta)\theta}}{6\pi\theta^2} == \right. \\ \left. m \frac{\sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (-80\pi^4 + 224\pi^3\theta - 448\pi^2\theta^2 + 160\pi\theta^3 - 15\theta^4)}{2\theta^2\sqrt{(-2\pi + \theta)^4}(8\pi^2 - 6\pi\theta + \theta^2)^2}, \theta\right]$$

$$\text{Solve}[2m == \text{Root}[3317760000m^4\pi^{16} - 37158912000m^4\pi^{15}\#1 + \\ 230385254400m^4\pi^{14}\#1^2 + (-942137671680m^4\pi^{13} - 67108864h^4\pi^{19})\#1^3 + \\ (2801594843136m^4\pi^{12} + 587202560h^4\pi^{18})\#1^4 + \\ (-6218413867008m^4\pi^{11} - 2428502016h^4\pi^{17})\#1^5 + \\ (10484567506944m^4\pi^{10} + 6309281792h^4\pi^{16})\#1^6 + \\ (-13268250427392m^4\pi^9 - 11542724608h^4\pi^{15})\#1^7 + \\ (12416904377856m^4\pi^8 + 15797846016h^4\pi^{14})\#1^8 + \\ (-8208129116160m^4\pi^7 - 16771973120h^4\pi^{13})\#1^9 + \\ (3742726072320m^4\pi^6 + 14132445184h^4\pi^{12})\#1^{10} + \\ (-1171098777600m^4\pi^5 - 9589751808h^4\pi^{11})\#1^{11} + \\ (250171934400m^4\pi^4 + 5285609472h^4\pi^{10})\#1^{12} + \\ (-35827920000m^4\pi^3 - 2375712768h^4\pi^9)\#1^{13} + \\ (3289248000m^4\pi^2 + 870604800h^4\pi^8)\#1^{14} + (-174960000m^4\pi - 258998272h^4\pi^7)\#1^{15} + \\ (4100625m^4 + 61988864h^4\pi^6)\#1^{16} - 11759616h^4\pi^5\#1^{17} + 1727488h^4\pi^4\#1^{18} - \\ 189440h^4\pi^3\#1^{19} + 14592h^4\pi^2\#1^{20} - 704h^4\pi\#1^{21} + 16h^4\#1^{22} \&, 1], m]$$

$$\{\{m \rightarrow 0\}, \{m \rightarrow 0\}, \{m \rightarrow 0\},$$

$$\{m \rightarrow \text{Root}[-8192h^4\pi^{19} + (50625\pi^{16} + 143360h^4\pi^{18})\#1 + (-1134000\pi^{15} - 1185792h^4\pi^{17}) \\ \#1^2 + (14061600\pi^{14} + 6161408h^4\pi^{16})\#1^3 + (-115007040\pi^{13} - 22544384h^4\pi^{15})\#1^4 + \\ (683983116\pi^{12} + 61710336h^4\pi^{14})\#1^5 + (-3036334896\pi^{11} - 131031040h^4\pi^{13})\#1^6 + \\ (10238835456\pi^{10} + 220819456h^4\pi^{12})\#1^7 + \\ (-25914551616\pi^9 - 299679744h^4\pi^{11})\#1^8 + \\ (48503532726\pi^8 + 330350592h^4\pi^{10})\#1^9 + (-64126008720\pi^7 - 296964096h^4\pi^9)\#1^{10} + \\ (58480094880\pi^6 + 217651200h^4\pi^8)\#1^{11} + (-36596836800\pi^5 - 129499136h^4\pi^7)\#1^{12} +$$

$$\begin{aligned}
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 1 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 2 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 3 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 4 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} +
\end{aligned}$$

$$\begin{aligned}
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 5 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 6 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 7 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 8 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 +
\end{aligned}$$

$$\begin{aligned}
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 9 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 10 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 11 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11}) \#1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10}) \#1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9) \#1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8) \#1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7) \#1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6) \#1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5) \#1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4) \#1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3) \#1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2) \#1^{17} - 22\,528\,h^4\,\pi \#1^{18} + 1024\,h^4\,\#1^{19} \&, 12 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18}) \#1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
& \#1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16}) \#1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15}) \#1^4 + \\
& (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14}) \#1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13}) \#1^6 + \\
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12}) \#1^7 +
\end{aligned}$$

$$\begin{aligned}
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 13 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18})\,\#\!1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
\quad \#\!1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16})\,\#\!1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15})\,\#\!1^4 + \\
\quad (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14})\,\#\!1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13})\,\#\!1^6 + \\
\quad (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12})\,\#\!1^7 + \\
\quad (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
\quad (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
\quad (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
\quad (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
\quad (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
\quad (4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 14 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18})\,\#\!1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
\quad \#\!1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16})\,\#\!1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15})\,\#\!1^4 + \\
\quad (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14})\,\#\!1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13})\,\#\!1^6 + \\
\quad (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12})\,\#\!1^7 + \\
\quad (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
\quad (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
\quad (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
\quad (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
\quad (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
\quad (4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 15 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18})\,\#\!1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
\quad \#\!1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16})\,\#\!1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15})\,\#\!1^4 + \\
\quad (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14})\,\#\!1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13})\,\#\!1^6 + \\
\quad (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12})\,\#\!1^7 + \\
\quad (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
\quad (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
\quad (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
\quad (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
\quad (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
\quad (4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 16 \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18})\,\#\!1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
\quad \#\!1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16})\,\#\!1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15})\,\#\!1^4 + \\
\quad (683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14})\,\#\!1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13})\,\#\!1^6 +
\end{aligned}$$

$$\begin{aligned}
& (10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12})\,\#\!1^7 + \\
& (-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
& (-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
& (58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
& (15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
& (822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
& (4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 17] \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18})\,\#\!1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
\,\#\!1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16})\,\#\!1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15})\,\#\!1^4 + \\
(683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14})\,\#\!1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13})\,\#\!1^6 + \\
(10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12})\,\#\!1^7 + \\
(-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
(-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
(58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
(15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
(822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
(4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 18] \}, \\
\{m \rightarrow \text{Root}[-8192\,h^4\,\pi^{19} + (50\,625\,\pi^{16} + 143\,360\,h^4\,\pi^{18})\,\#\!1 + (-1\,134\,000\,\pi^{15} - 1\,185\,792\,h^4\,\pi^{17}) \\
\,\#\!1^2 + (14\,061\,600\,\pi^{14} + 6\,161\,408\,h^4\,\pi^{16})\,\#\!1^3 + (-115\,007\,040\,\pi^{13} - 22\,544\,384\,h^4\,\pi^{15})\,\#\!1^4 + \\
(683\,983\,116\,\pi^{12} + 61\,710\,336\,h^4\,\pi^{14})\,\#\!1^5 + (-3\,036\,334\,896\,\pi^{11} - 131\,031\,040\,h^4\,\pi^{13})\,\#\!1^6 + \\
(10\,238\,835\,456\,\pi^{10} + 220\,819\,456\,h^4\,\pi^{12})\,\#\!1^7 + \\
(-25\,914\,551\,616\,\pi^9 - 299\,679\,744\,h^4\,\pi^{11})\,\#\!1^8 + (48\,503\,532\,726\,\pi^8 + 330\,350\,592\,h^4\,\pi^{10})\,\#\!1^9 + \\
(-64\,126\,008\,720\,\pi^7 - 296\,964\,096\,h^4\,\pi^9)\,\#\!1^{10} + \\
(58\,480\,094\,880\,\pi^6 + 217\,651\,200\,h^4\,\pi^8)\,\#\!1^{11} + (-36\,596\,836\,800\,\pi^5 - 129\,499\,136\,h^4\,\pi^7)\,\#\!1^{12} + \\
(15\,635\,745\,900\,\pi^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{13} + (-4\,478\,490\,000\,\pi^3 - 23\,519\,232\,h^4\,\pi^5)\,\#\!1^{14} + \\
(822\,312\,000\,\pi^2 + 6\,909\,952\,h^4\,\pi^4)\,\#\!1^{15} + (-87\,480\,000\,\pi - 1\,515\,520\,h^4\,\pi^3)\,\#\!1^{16} + \\
(4\,100\,625 + 233\,472\,h^4\,\pi^2)\,\#\!1^{17} - 22\,528\,h^4\,\pi\,\#\!1^{18} + 1024\,h^4\,\#\!1^{19} \&, 19] \}
\end{aligned}$$

$$h := 6.626 * 10^{\wedge} - 34$$

$$\text{Solve}\left[m == - \frac{2\,\theta^2\,\sqrt{(-2\,\pi + \theta)^4}\,(8\,\pi^2 - 6\,\pi\,\theta + \theta^2)^2\left(-\frac{h\,(4\,\pi - 2\,\theta)}{12\,\pi\,\theta\,\sqrt{(4\,\pi - \theta)\,\theta}} + \frac{h\,\sqrt{(4\,\pi - \theta)\,\theta}}{6\,\pi\,\theta^2}\right)}{\sqrt{\frac{((4\,\pi - \theta)\,\theta)^{3/2}}{\theta^2}}\,(-80\,\pi^4 + 224\,\pi^3\,\theta - 448\,\pi^2\,\theta^2 + 160\,\pi\,\theta^3 - 15\,\theta^4)}}, \theta\right]$$

$$\begin{aligned}
\{ \{ \theta \rightarrow \text{Root}[3\,317\,760\,000\,m^4\,\pi^{16} - 37\,158\,912\,000\,m^4\,\pi^{15}\,\#\!1 + \\
230\,385\,254\,400\,m^4\,\pi^{14}\,\#\!1^2 + (-942\,137\,671\,680\,m^4\,\pi^{13} - 67\,108\,864\,h^4\,\pi^{19})\,\#\!1^3 + \\
(2\,801\,594\,843\,136\,m^4\,\pi^{12} + 587\,202\,560\,h^4\,\pi^{18})\,\#\!1^4 + \\
(-6\,218\,413\,867\,008\,m^4\,\pi^{11} - 2\,428\,502\,016\,h^4\,\pi^{17})\,\#\!1^5 + \\
(10\,484\,567\,506\,944\,m^4\,\pi^{10} + 6\,309\,281\,792\,h^4\,\pi^{16})\,\#\!1^6 + \\
(-13\,268\,250\,427\,392\,m^4\,\pi^9 - 11\,542\,724\,608\,h^4\,\pi^{15})\,\#\!1^7 + \\
(12\,416\,904\,377\,856\,m^4\,\pi^8 + 15\,797\,846\,016\,h^4\,\pi^{14})\,\#\!1^8 +
\end{aligned}$$

$$\begin{aligned}
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\, \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\, \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\, \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\, \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\, \#1^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8)\, \#1^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\, \#1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\, \#1^{16} - \\
& 11\,759\,616\,h^4\pi^5\, \#1^{17} + 1\,727\,488\,h^4\pi^4\, \#1^{18} - 189\,440\,h^4\pi^3\, \#1^{19} + \\
& 14\,592\,h^4\pi^2\, \#1^{20} - 704\,h^4\pi\, \#1^{21} + 16\,h^4\, \#1^{22} \&, 1] \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\, \#1 + 230\,385\,254\,400\,m^4\pi^{14}\, \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\, \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\, \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\, \#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\, \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\, \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\, \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\, \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\, \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\, \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\, \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\, \#1^{13} + (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \\
& \#1^{14} + (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\, \#1^{15} + \\
& (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\, \#1^{16} - 11\,759\,616\,h^4\pi^5\, \#1^{17} + 1\,727\,488\,h^4\pi^4\, \#1^{18} - \\
& 189\,440\,h^4\pi^3\, \#1^{19} + 14\,592\,h^4\pi^2\, \#1^{20} - 704\,h^4\pi\, \#1^{21} + 16\,h^4\, \#1^{22} \&, 2] \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\, \#1 + 230\,385\,254\,400\,m^4\pi^{14}\, \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\, \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\, \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\, \#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\, \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\, \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\, \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\, \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\, \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\, \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\, \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\, \#1^{13} + (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \\
& \#1^{14} + (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\, \#1^{15} + \\
& (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\, \#1^{16} - 11\,759\,616\,h^4\pi^5\, \#1^{17} + 1\,727\,488\,h^4\pi^4\, \#1^{18} - \\
& 189\,440\,h^4\pi^3\, \#1^{19} + 14\,592\,h^4\pi^2\, \#1^{20} - 704\,h^4\pi\, \#1^{21} + 16\,h^4\, \#1^{22} \&, 3] \},
\end{aligned}$$

$$\begin{aligned}
& \{ \theta \rightarrow \text{Root} [ 3\,317\,760\,000\, m^4 \pi^{16} - 37\,158\,912\,000\, m^4 \pi^{15} \#1 + 230\,385\,254\,400\, m^4 \pi^{14} \#1^2 + \\
& \quad (-942\,137\,671\,680\, m^4 \pi^{13} - 67\,108\,864\, h^4 \pi^{19}) \#1^3 + \\
& \quad (2\,801\,594\,843\,136\, m^4 \pi^{12} + 587\,202\,560\, h^4 \pi^{18}) \#1^4 + \\
& \quad (-6\,218\,413\,867\,008\, m^4 \pi^{11} - 2\,428\,502\,016\, h^4 \pi^{17}) \#1^5 + \\
& \quad (10\,484\,567\,506\,944\, m^4 \pi^{10} + 6\,309\,281\,792\, h^4 \pi^{16}) \#1^6 + \\
& \quad (-13\,268\,250\,427\,392\, m^4 \pi^9 - 11\,542\,724\,608\, h^4 \pi^{15}) \#1^7 + \\
& \quad (12\,416\,904\,377\,856\, m^4 \pi^8 + 15\,797\,846\,016\, h^4 \pi^{14}) \#1^8 + \\
& \quad (-8\,208\,129\,116\,160\, m^4 \pi^7 - 16\,771\,973\,120\, h^4 \pi^{13}) \#1^9 + \\
& \quad (3\,742\,726\,072\,320\, m^4 \pi^6 + 14\,132\,445\,184\, h^4 \pi^{12}) \#1^{10} + \\
& \quad (-1\,171\,098\,777\,600\, m^4 \pi^5 - 9\,589\,751\,808\, h^4 \pi^{11}) \#1^{11} + \\
& \quad (250\,171\,934\,400\, m^4 \pi^4 + 5\,285\,609\,472\, h^4 \pi^{10}) \#1^{12} + \\
& \quad (-35\,827\,920\,000\, m^4 \pi^3 - 2\,375\,712\,768\, h^4 \pi^9) \#1^{13} + (3\,289\,248\,000\, m^4 \pi^2 + 870\,604\,800\, h^4 \pi^8) \\
& \quad \#1^{14} + (-174\,960\,000\, m^4 \pi - 258\,998\,272\, h^4 \pi^7) \#1^{15} + \\
& \quad (4\,100\,625\, m^4 + 61\,988\,864\, h^4 \pi^6) \#1^{16} - 11\,759\,616\, h^4 \pi^5 \#1^{17} + 1\,727\,488\, h^4 \pi^4 \#1^{18} - \\
& \quad 189\,440\, h^4 \pi^3 \#1^{19} + 14\,592\, h^4 \pi^2 \#1^{20} - 704\, h^4 \pi \#1^{21} + 16\, h^4 \#1^{22} \&, 4 \} \}, \\
& \{ \theta \rightarrow \text{Root} [ 3\,317\,760\,000\, m^4 \pi^{16} - 37\,158\,912\,000\, m^4 \pi^{15} \#1 + 230\,385\,254\,400\, m^4 \pi^{14} \#1^2 + \\
& \quad (-942\,137\,671\,680\, m^4 \pi^{13} - 67\,108\,864\, h^4 \pi^{19}) \#1^3 + \\
& \quad (2\,801\,594\,843\,136\, m^4 \pi^{12} + 587\,202\,560\, h^4 \pi^{18}) \#1^4 + \\
& \quad (-6\,218\,413\,867\,008\, m^4 \pi^{11} - 2\,428\,502\,016\, h^4 \pi^{17}) \#1^5 + \\
& \quad (10\,484\,567\,506\,944\, m^4 \pi^{10} + 6\,309\,281\,792\, h^4 \pi^{16}) \#1^6 + \\
& \quad (-13\,268\,250\,427\,392\, m^4 \pi^9 - 11\,542\,724\,608\, h^4 \pi^{15}) \#1^7 + \\
& \quad (12\,416\,904\,377\,856\, m^4 \pi^8 + 15\,797\,846\,016\, h^4 \pi^{14}) \#1^8 + \\
& \quad (-8\,208\,129\,116\,160\, m^4 \pi^7 - 16\,771\,973\,120\, h^4 \pi^{13}) \#1^9 + \\
& \quad (3\,742\,726\,072\,320\, m^4 \pi^6 + 14\,132\,445\,184\, h^4 \pi^{12}) \#1^{10} + \\
& \quad (-1\,171\,098\,777\,600\, m^4 \pi^5 - 9\,589\,751\,808\, h^4 \pi^{11}) \#1^{11} + \\
& \quad (250\,171\,934\,400\, m^4 \pi^4 + 5\,285\,609\,472\, h^4 \pi^{10}) \#1^{12} + \\
& \quad (-35\,827\,920\,000\, m^4 \pi^3 - 2\,375\,712\,768\, h^4 \pi^9) \#1^{13} + (3\,289\,248\,000\, m^4 \pi^2 + 870\,604\,800\, h^4 \pi^8) \\
& \quad \#1^{14} + (-174\,960\,000\, m^4 \pi - 258\,998\,272\, h^4 \pi^7) \#1^{15} + \\
& \quad (4\,100\,625\, m^4 + 61\,988\,864\, h^4 \pi^6) \#1^{16} - 11\,759\,616\, h^4 \pi^5 \#1^{17} + 1\,727\,488\, h^4 \pi^4 \#1^{18} - \\
& \quad 189\,440\, h^4 \pi^3 \#1^{19} + 14\,592\, h^4 \pi^2 \#1^{20} - 704\, h^4 \pi \#1^{21} + 16\, h^4 \#1^{22} \&, 5 \} \}, \\
& \{ \theta \rightarrow \text{Root} [ 3\,317\,760\,000\, m^4 \pi^{16} - 37\,158\,912\,000\, m^4 \pi^{15} \#1 + 230\,385\,254\,400\, m^4 \pi^{14} \#1^2 + \\
& \quad (-942\,137\,671\,680\, m^4 \pi^{13} - 67\,108\,864\, h^4 \pi^{19}) \#1^3 + \\
& \quad (2\,801\,594\,843\,136\, m^4 \pi^{12} + 587\,202\,560\, h^4 \pi^{18}) \#1^4 + \\
& \quad (-6\,218\,413\,867\,008\, m^4 \pi^{11} - 2\,428\,502\,016\, h^4 \pi^{17}) \#1^5 + \\
& \quad (10\,484\,567\,506\,944\, m^4 \pi^{10} + 6\,309\,281\,792\, h^4 \pi^{16}) \#1^6 + \\
& \quad (-13\,268\,250\,427\,392\, m^4 \pi^9 - 11\,542\,724\,608\, h^4 \pi^{15}) \#1^7 + \\
& \quad (12\,416\,904\,377\,856\, m^4 \pi^8 + 15\,797\,846\,016\, h^4 \pi^{14}) \#1^8 + \\
& \quad (-8\,208\,129\,116\,160\, m^4 \pi^7 - 16\,771\,973\,120\, h^4 \pi^{13}) \#1^9 + \\
& \quad (3\,742\,726\,072\,320\, m^4 \pi^6 + 14\,132\,445\,184\, h^4 \pi^{12}) \#1^{10} +
\end{aligned}$$



$$\begin{aligned}
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\#1^{13} + (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \\
& \#1^{14} + (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\#1^{15} + \\
& (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\#1^{16} - 11\,759\,616\,h^4\pi^5\#1^{17} + 1\,727\,488\,h^4\pi^4\#1^{18} - \\
& 189\,440\,h^4\pi^3\#1^{19} + 14\,592\,h^4\pi^2\#1^{20} - 704\,h^4\pi\#1^{21} + 16\,h^4\#1^{22} \&, 6] \}, \\
\{\theta \rightarrow \text{Root}[3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\#1 + 230\,385\,254\,400\,m^4\pi^{14}\#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\#1^{13} + (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \\
& \#1^{14} + (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\#1^{15} + \\
& (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\#1^{16} - 11\,759\,616\,h^4\pi^5\#1^{17} + 1\,727\,488\,h^4\pi^4\#1^{18} - \\
& 189\,440\,h^4\pi^3\#1^{19} + 14\,592\,h^4\pi^2\#1^{20} - 704\,h^4\pi\#1^{21} + 16\,h^4\#1^{22} \&, 7] \}, \\
\{\theta \rightarrow \text{Root}[3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\#1 + 230\,385\,254\,400\,m^4\pi^{14}\#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\#1^{13} + (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \\
& \#1^{14} + (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\#1^{15} + \\
& (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\#1^{16} - 11\,759\,616\,h^4\pi^5\#1^{17} + 1\,727\,488\,h^4\pi^4\#1^{18} - \\
& 189\,440\,h^4\pi^3\#1^{19} + 14\,592\,h^4\pi^2\#1^{20} - 704\,h^4\pi\#1^{21} + 16\,h^4\#1^{22} \&, 8] \}, \\
\{\theta \rightarrow \text{Root}[3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\#1 + 230\,385\,254\,400\,m^4\pi^{14}\#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\#1^4 +
\end{aligned}$$

$$\begin{aligned}
& (-6218413867008 m^4 \pi^{11} - 2428502016 h^4 \pi^{17}) \#1^5 + \\
& (10484567506944 m^4 \pi^{10} + 6309281792 h^4 \pi^{16}) \#1^6 + \\
& (-13268250427392 m^4 \pi^9 - 11542724608 h^4 \pi^{15}) \#1^7 + \\
& (12416904377856 m^4 \pi^8 + 15797846016 h^4 \pi^{14}) \#1^8 + \\
& (-8208129116160 m^4 \pi^7 - 16771973120 h^4 \pi^{13}) \#1^9 + \\
& (3742726072320 m^4 \pi^6 + 14132445184 h^4 \pi^{12}) \#1^{10} + \\
& (-1171098777600 m^4 \pi^5 - 9589751808 h^4 \pi^{11}) \#1^{11} + \\
& (250171934400 m^4 \pi^4 + 5285609472 h^4 \pi^{10}) \#1^{12} + \\
& (-35827920000 m^4 \pi^3 - 2375712768 h^4 \pi^9) \#1^{13} + (3289248000 m^4 \pi^2 + 870604800 h^4 \pi^8) \\
& \#1^{14} + (-174960000 m^4 \pi - 258998272 h^4 \pi^7) \#1^{15} + \\
& (4100625 m^4 + 61988864 h^4 \pi^6) \#1^{16} - 11759616 h^4 \pi^5 \#1^{17} + 1727488 h^4 \pi^4 \#1^{18} - \\
& 189440 h^4 \pi^3 \#1^{19} + 14592 h^4 \pi^2 \#1^{20} - 704 h^4 \pi \#1^{21} + 16 h^4 \#1^{22} \&, 9 \}, \\
\{ \theta \rightarrow \text{Root}[ & 3317760000 m^4 \pi^{16} - 37158912000 m^4 \pi^{15} \#1 + 230385254400 m^4 \pi^{14} \#1^2 + \\
& (-942137671680 m^4 \pi^{13} - 67108864 h^4 \pi^{19}) \#1^3 + \\
& (2801594843136 m^4 \pi^{12} + 587202560 h^4 \pi^{18}) \#1^4 + \\
& (-6218413867008 m^4 \pi^{11} - 2428502016 h^4 \pi^{17}) \#1^5 + \\
& (10484567506944 m^4 \pi^{10} + 6309281792 h^4 \pi^{16}) \#1^6 + \\
& (-13268250427392 m^4 \pi^9 - 11542724608 h^4 \pi^{15}) \#1^7 + \\
& (12416904377856 m^4 \pi^8 + 15797846016 h^4 \pi^{14}) \#1^8 + \\
& (-8208129116160 m^4 \pi^7 - 16771973120 h^4 \pi^{13}) \#1^9 + \\
& (3742726072320 m^4 \pi^6 + 14132445184 h^4 \pi^{12}) \#1^{10} + \\
& (-1171098777600 m^4 \pi^5 - 9589751808 h^4 \pi^{11}) \#1^{11} + \\
& (250171934400 m^4 \pi^4 + 5285609472 h^4 \pi^{10}) \#1^{12} + \\
& (-35827920000 m^4 \pi^3 - 2375712768 h^4 \pi^9) \#1^{13} + (3289248000 m^4 \pi^2 + 870604800 h^4 \pi^8) \\
& \#1^{14} + (-174960000 m^4 \pi - 258998272 h^4 \pi^7) \#1^{15} + \\
& (4100625 m^4 + 61988864 h^4 \pi^6) \#1^{16} - 11759616 h^4 \pi^5 \#1^{17} + 1727488 h^4 \pi^4 \#1^{18} - \\
& 189440 h^4 \pi^3 \#1^{19} + 14592 h^4 \pi^2 \#1^{20} - 704 h^4 \pi \#1^{21} + 16 h^4 \#1^{22} \&, 10 \}, \\
\{ \theta \rightarrow \text{Root}[ & 3317760000 m^4 \pi^{16} - 37158912000 m^4 \pi^{15} \#1 + 230385254400 m^4 \pi^{14} \#1^2 + \\
& (-942137671680 m^4 \pi^{13} - 67108864 h^4 \pi^{19}) \#1^3 + \\
& (2801594843136 m^4 \pi^{12} + 587202560 h^4 \pi^{18}) \#1^4 + \\
& (-6218413867008 m^4 \pi^{11} - 2428502016 h^4 \pi^{17}) \#1^5 + \\
& (10484567506944 m^4 \pi^{10} + 6309281792 h^4 \pi^{16}) \#1^6 + \\
& (-13268250427392 m^4 \pi^9 - 11542724608 h^4 \pi^{15}) \#1^7 + \\
& (12416904377856 m^4 \pi^8 + 15797846016 h^4 \pi^{14}) \#1^8 + \\
& (-8208129116160 m^4 \pi^7 - 16771973120 h^4 \pi^{13}) \#1^9 + \\
& (3742726072320 m^4 \pi^6 + 14132445184 h^4 \pi^{12}) \#1^{10} + \\
& (-1171098777600 m^4 \pi^5 - 9589751808 h^4 \pi^{11}) \#1^{11} + \\
& (250171934400 m^4 \pi^4 + 5285609472 h^4 \pi^{10}) \#1^{12} + \\
& (-35827920000 m^4 \pi^3 - 2375712768 h^4 \pi^9) \#1^{13} + (3289248000 m^4 \pi^2 + 870604800 h^4 \pi^8)
\end{aligned}$$

$$\begin{aligned}
& \#1^{14} + (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7) \#1^{15} + \\
& (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6) \#1^{16} - 11\,759\,616\,h^4\pi^5 \#1^{17} + 1\,727\,488\,h^4\pi^4 \#1^{18} - \\
& 189\,440\,h^4\pi^3 \#1^{19} + 14\,592\,h^4\pi^2 \#1^{20} - 704\,h^4\pi \#1^{21} + 16\,h^4 \#1^{22} \&, 11 \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15} \#1 + 230\,385\,254\,400\,m^4\pi^{14} \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19}) \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18}) \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17}) \#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16}) \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15}) \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14}) \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13}) \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12}) \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11}) \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10}) \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9) \#1^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \#1^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7) \#1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6) \#1^{16} - \\
& 11\,759\,616\,h^4\pi^5 \#1^{17} + 1\,727\,488\,h^4\pi^4 \#1^{18} - 189\,440\,h^4\pi^3 \#1^{19} + \\
& 14\,592\,h^4\pi^2 \#1^{20} - 704\,h^4\pi \#1^{21} + 16\,h^4 \#1^{22} \&, 12 \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15} \#1 + 230\,385\,254\,400\,m^4\pi^{14} \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19}) \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18}) \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17}) \#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16}) \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15}) \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14}) \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13}) \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12}) \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11}) \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10}) \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9) \#1^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8) \#1^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7) \#1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6) \#1^{16} - \\
& 11\,759\,616\,h^4\pi^5 \#1^{17} + 1\,727\,488\,h^4\pi^4 \#1^{18} - 189\,440\,h^4\pi^3 \#1^{19} + \\
& 14\,592\,h^4\pi^2 \#1^{20} - 704\,h^4\pi \#1^{21} + 16\,h^4 \#1^{22} \&, 13 \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15} \#1 + 230\,385\,254\,400\,m^4\pi^{14} \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19}) \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18}) \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17}) \#1^5 +
\end{aligned}$$

$$\begin{aligned}
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\, \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\, \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\, \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\, \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\, \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\, \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\, \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\, \#1^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8)\, \#1^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\, \#1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\, \#1^{16} - \\
& 11\,759\,616\,h^4\pi^5\, \#1^{17} + 1\,727\,488\,h^4\pi^4\, \#1^{18} - 189\,440\,h^4\pi^3\, \#1^{19} + \\
& 14\,592\,h^4\pi^2\, \#1^{20} - 704\,h^4\pi\, \#1^{21} + 16\,h^4\, \#1^{22} \&, 14] \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\, \#1 + 230\,385\,254\,400\,m^4\pi^{14}\, \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\, \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\, \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\, \#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\, \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\, \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\, \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\, \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\, \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\, \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\, \#1^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\, \#1^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8)\, \#1^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\, \#1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\, \#1^{16} - \\
& 11\,759\,616\,h^4\pi^5\, \#1^{17} + 1\,727\,488\,h^4\pi^4\, \#1^{18} - 189\,440\,h^4\pi^3\, \#1^{19} + \\
& 14\,592\,h^4\pi^2\, \#1^{20} - 704\,h^4\pi\, \#1^{21} + 16\,h^4\, \#1^{22} \&, 15] \}, \\
\{ \theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\, \#1 + 230\,385\,254\,400\,m^4\pi^{14}\, \#1^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\, \#1^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\, \#1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\, \#1^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\, \#1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\, \#1^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\, \#1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\, \#1^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\, \#1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\, \#1^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\, \#1^{12} +
\end{aligned}$$

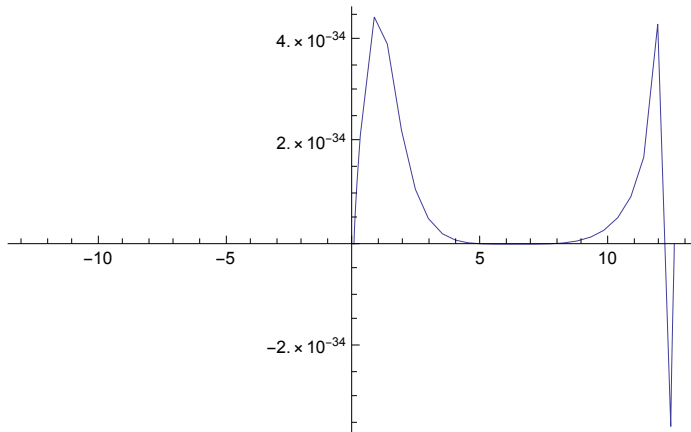
$$\begin{aligned}
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\pi^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8)\pi^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\pi^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\pi^{16} - \\
& 11\,759\,616\,h^4\pi^5\pi^{17} + 1\,727\,488\,h^4\pi^4\pi^{18} - 189\,440\,h^4\pi^3\pi^{19} + \\
& 14\,592\,h^4\pi^2\pi^{20} - 704\,h^4\pi\pi^{21} + 16\,h^4\pi^{22} \&, 16] \}, \\
\{\theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\pi + 230\,385\,254\,400\,m^4\pi^{14}\pi^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\pi^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\pi^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\pi^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\pi^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\pi^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\pi^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\pi^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\pi^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\pi^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\pi^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\pi^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8)\pi^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\pi^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\pi^{16} - \\
& 11\,759\,616\,h^4\pi^5\pi^{17} + 1\,727\,488\,h^4\pi^4\pi^{18} - 189\,440\,h^4\pi^3\pi^{19} + \\
& 14\,592\,h^4\pi^2\pi^{20} - 704\,h^4\pi\pi^{21} + 16\,h^4\pi^{22} \&, 17] \}, \\
\{\theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\pi + 230\,385\,254\,400\,m^4\pi^{14}\pi^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\pi^3 + \\
& (2\,801\,594\,843\,136\,m^4\pi^{12} + 587\,202\,560\,h^4\pi^{18})\pi^4 + \\
& (-6\,218\,413\,867\,008\,m^4\pi^{11} - 2\,428\,502\,016\,h^4\pi^{17})\pi^5 + \\
& (10\,484\,567\,506\,944\,m^4\pi^{10} + 6\,309\,281\,792\,h^4\pi^{16})\pi^6 + \\
& (-13\,268\,250\,427\,392\,m^4\pi^9 - 11\,542\,724\,608\,h^4\pi^{15})\pi^7 + \\
& (12\,416\,904\,377\,856\,m^4\pi^8 + 15\,797\,846\,016\,h^4\pi^{14})\pi^8 + \\
& (-8\,208\,129\,116\,160\,m^4\pi^7 - 16\,771\,973\,120\,h^4\pi^{13})\pi^9 + \\
& (3\,742\,726\,072\,320\,m^4\pi^6 + 14\,132\,445\,184\,h^4\pi^{12})\pi^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\pi^5 - 9\,589\,751\,808\,h^4\pi^{11})\pi^{11} + \\
& (250\,171\,934\,400\,m^4\pi^4 + 5\,285\,609\,472\,h^4\pi^{10})\pi^{12} + \\
& (-35\,827\,920\,000\,m^4\pi^3 - 2\,375\,712\,768\,h^4\pi^9)\pi^{13} + \\
& (3\,289\,248\,000\,m^4\pi^2 + 870\,604\,800\,h^4\pi^8)\pi^{14} + \\
& (-174\,960\,000\,m^4\pi - 258\,998\,272\,h^4\pi^7)\pi^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\pi^6)\pi^{16} - \\
& 11\,759\,616\,h^4\pi^5\pi^{17} + 1\,727\,488\,h^4\pi^4\pi^{18} - 189\,440\,h^4\pi^3\pi^{19} + \\
& 14\,592\,h^4\pi^2\pi^{20} - 704\,h^4\pi\pi^{21} + 16\,h^4\pi^{22} \&, 18] \}, \\
\{\theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\pi^{16} - 37\,158\,912\,000\,m^4\pi^{15}\pi + 230\,385\,254\,400\,m^4\pi^{14}\pi^2 + \\
& (-942\,137\,671\,680\,m^4\pi^{13} - 67\,108\,864\,h^4\pi^{19})\pi^3 +
\end{aligned}$$

$$\begin{aligned}
& (2\,801\,594\,843\,136\,m^4\,\pi^{12} + 587\,202\,560\,h^4\,\pi^{18})\,\#\!1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\,\pi^{11} - 2\,428\,502\,016\,h^4\,\pi^{17})\,\#\!1^5 + \\
& (10\,484\,567\,506\,944\,m^4\,\pi^{10} + 6\,309\,281\,792\,h^4\,\pi^{16})\,\#\!1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\,\pi^9 - 11\,542\,724\,608\,h^4\,\pi^{15})\,\#\!1^7 + \\
& (12\,416\,904\,377\,856\,m^4\,\pi^8 + 15\,797\,846\,016\,h^4\,\pi^{14})\,\#\!1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\,\pi^7 - 16\,771\,973\,120\,h^4\,\pi^{13})\,\#\!1^9 + \\
& (3\,742\,726\,072\,320\,m^4\,\pi^6 + 14\,132\,445\,184\,h^4\,\pi^{12})\,\#\!1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\,\pi^5 - 9\,589\,751\,808\,h^4\,\pi^{11})\,\#\!1^{11} + \\
& (250\,171\,934\,400\,m^4\,\pi^4 + 5\,285\,609\,472\,h^4\,\pi^{10})\,\#\!1^{12} + \\
& (-35\,827\,920\,000\,m^4\,\pi^3 - 2\,375\,712\,768\,h^4\,\pi^9)\,\#\!1^{13} + \\
& (3\,289\,248\,000\,m^4\,\pi^2 + 870\,604\,800\,h^4\,\pi^8)\,\#\!1^{14} + \\
& (-174\,960\,000\,m^4\,\pi - 258\,998\,272\,h^4\,\pi^7)\,\#\!1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{16} - \\
& 11\,759\,616\,h^4\,\pi^5\,\#\!1^{17} + 1\,727\,488\,h^4\,\pi^4\,\#\!1^{18} - 189\,440\,h^4\,\pi^3\,\#\!1^{19} + \\
& 14\,592\,h^4\,\pi^2\,\#\!1^{20} - 704\,h^4\,\pi\,\#\!1^{21} + 16\,h^4\,\#\!1^{22} \&, 19 \}, \\
\{\theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\,\pi^{16} - 37\,158\,912\,000\,m^4\,\pi^{15}\,\#\!1 + 230\,385\,254\,400\,m^4\,\pi^{14}\,\#\!1^2 + \\
& (-942\,137\,671\,680\,m^4\,\pi^{13} - 67\,108\,864\,h^4\,\pi^{19})\,\#\!1^3 + \\
& (2\,801\,594\,843\,136\,m^4\,\pi^{12} + 587\,202\,560\,h^4\,\pi^{18})\,\#\!1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\,\pi^{11} - 2\,428\,502\,016\,h^4\,\pi^{17})\,\#\!1^5 + \\
& (10\,484\,567\,506\,944\,m^4\,\pi^{10} + 6\,309\,281\,792\,h^4\,\pi^{16})\,\#\!1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\,\pi^9 - 11\,542\,724\,608\,h^4\,\pi^{15})\,\#\!1^7 + \\
& (12\,416\,904\,377\,856\,m^4\,\pi^8 + 15\,797\,846\,016\,h^4\,\pi^{14})\,\#\!1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\,\pi^7 - 16\,771\,973\,120\,h^4\,\pi^{13})\,\#\!1^9 + \\
& (3\,742\,726\,072\,320\,m^4\,\pi^6 + 14\,132\,445\,184\,h^4\,\pi^{12})\,\#\!1^{10} + \\
& (-1\,171\,098\,777\,600\,m^4\,\pi^5 - 9\,589\,751\,808\,h^4\,\pi^{11})\,\#\!1^{11} + \\
& (250\,171\,934\,400\,m^4\,\pi^4 + 5\,285\,609\,472\,h^4\,\pi^{10})\,\#\!1^{12} + \\
& (-35\,827\,920\,000\,m^4\,\pi^3 - 2\,375\,712\,768\,h^4\,\pi^9)\,\#\!1^{13} + \\
& (3\,289\,248\,000\,m^4\,\pi^2 + 870\,604\,800\,h^4\,\pi^8)\,\#\!1^{14} + \\
& (-174\,960\,000\,m^4\,\pi - 258\,998\,272\,h^4\,\pi^7)\,\#\!1^{15} + (4\,100\,625\,m^4 + 61\,988\,864\,h^4\,\pi^6)\,\#\!1^{16} - \\
& 11\,759\,616\,h^4\,\pi^5\,\#\!1^{17} + 1\,727\,488\,h^4\,\pi^4\,\#\!1^{18} - 189\,440\,h^4\,\pi^3\,\#\!1^{19} + \\
& 14\,592\,h^4\,\pi^2\,\#\!1^{20} - 704\,h^4\,\pi\,\#\!1^{21} + 16\,h^4\,\#\!1^{22} \&, 20 \}, \\
\{\theta \rightarrow \text{Root}[ & 3\,317\,760\,000\,m^4\,\pi^{16} - 37\,158\,912\,000\,m^4\,\pi^{15}\,\#\!1 + 230\,385\,254\,400\,m^4\,\pi^{14}\,\#\!1^2 + \\
& (-942\,137\,671\,680\,m^4\,\pi^{13} - 67\,108\,864\,h^4\,\pi^{19})\,\#\!1^3 + \\
& (2\,801\,594\,843\,136\,m^4\,\pi^{12} + 587\,202\,560\,h^4\,\pi^{18})\,\#\!1^4 + \\
& (-6\,218\,413\,867\,008\,m^4\,\pi^{11} - 2\,428\,502\,016\,h^4\,\pi^{17})\,\#\!1^5 + \\
& (10\,484\,567\,506\,944\,m^4\,\pi^{10} + 6\,309\,281\,792\,h^4\,\pi^{16})\,\#\!1^6 + \\
& (-13\,268\,250\,427\,392\,m^4\,\pi^9 - 11\,542\,724\,608\,h^4\,\pi^{15})\,\#\!1^7 + \\
& (12\,416\,904\,377\,856\,m^4\,\pi^8 + 15\,797\,846\,016\,h^4\,\pi^{14})\,\#\!1^8 + \\
& (-8\,208\,129\,116\,160\,m^4\,\pi^7 - 16\,771\,973\,120\,h^4\,\pi^{13})\,\#\!1^9 + \\
& (3\,742\,726\,072\,320\,m^4\,\pi^6 + 14\,132\,445\,184\,h^4\,\pi^{12})\,\#\!1^{10} +
\end{aligned}$$

$$\begin{aligned}
& (-1171098777600 m^4 \pi^5 - 9589751808 h^4 \pi^{11}) \#1^{11} + \\
& (250171934400 m^4 \pi^4 + 5285609472 h^4 \pi^{10}) \#1^{12} + \\
& (-35827920000 m^4 \pi^3 - 2375712768 h^4 \pi^9) \#1^{13} + \\
& (3289248000 m^4 \pi^2 + 870604800 h^4 \pi^8) \#1^{14} + \\
& (-174960000 m^4 \pi - 258998272 h^4 \pi^7) \#1^{15} + (4100625 m^4 + 61988864 h^4 \pi^6) \#1^{16} - \\
& 11759616 h^4 \pi^5 \#1^{17} + 1727488 h^4 \pi^4 \#1^{18} - 189440 h^4 \pi^3 \#1^{19} + \\
& 14592 h^4 \pi^2 \#1^{20} - 704 h^4 \pi \#1^{21} + 16 h^4 \#1^{22} \&, 21 \Big] \Big\}, \\
\{ \theta \rightarrow \text{Root} [ & 3317760000 m^4 \pi^{16} - 37158912000 m^4 \pi^{15} \#1 + 230385254400 m^4 \pi^{14} \#1^2 + \\
& (-942137671680 m^4 \pi^{13} - 67108864 h^4 \pi^{19}) \#1^3 + \\
& (2801594843136 m^4 \pi^{12} + 587202560 h^4 \pi^{18}) \#1^4 + \\
& (-6218413867008 m^4 \pi^{11} - 2428502016 h^4 \pi^{17}) \#1^5 + \\
& (10484567506944 m^4 \pi^{10} + 6309281792 h^4 \pi^{16}) \#1^6 + \\
& (-13268250427392 m^4 \pi^9 - 11542724608 h^4 \pi^{15}) \#1^7 + \\
& (12416904377856 m^4 \pi^8 + 15797846016 h^4 \pi^{14}) \#1^8 + \\
& (-8208129116160 m^4 \pi^7 - 16771973120 h^4 \pi^{13}) \#1^9 + \\
& (3742726072320 m^4 \pi^6 + 14132445184 h^4 \pi^{12}) \#1^{10} + \\
& (-1171098777600 m^4 \pi^5 - 9589751808 h^4 \pi^{11}) \#1^{11} + \\
& (250171934400 m^4 \pi^4 + 5285609472 h^4 \pi^{10}) \#1^{12} + \\
& (-35827920000 m^4 \pi^3 - 2375712768 h^4 \pi^9) \#1^{13} + \\
& (3289248000 m^4 \pi^2 + 870604800 h^4 \pi^8) \#1^{14} + \\
& (-174960000 m^4 \pi - 258998272 h^4 \pi^7) \#1^{15} + (4100625 m^4 + 61988864 h^4 \pi^6) \#1^{16} - \\
& 11759616 h^4 \pi^5 \#1^{17} + 1727488 h^4 \pi^4 \#1^{18} - 189440 h^4 \pi^3 \#1^{19} + \\
& 14592 h^4 \pi^2 \#1^{20} - 704 h^4 \pi \#1^{21} + 16 h^4 \#1^{22} \&, 22 \Big] \Big\} \Big\}
\end{aligned}$$

Numbers have specific meanings based on their discrete sets of solutions relating to the structure of light through time. For instance, the reduced time traveled by a single wavelength of light has 22 solutions in terms of the mass of that light.

$$\text{Plot}\left[-\frac{2 \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2 \left(-\frac{h (4 \pi - 2 \theta)}{12 \pi \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{h \sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta^2}\right)}{\sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}, \{\theta, -13, 13\}\right]$$



$$\text{Solve}\left[m == -\frac{2 \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2 \left(-\frac{h (4 \pi - 2 \theta)}{12 \pi \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{h \sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta^2}\right)}{\sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)},\right]$$

$$\text{Solve}\left[-\frac{h (4 \pi - \theta)}{3 \pi^2 \theta^3} - \frac{h}{6 \pi^2 \theta^2} == m \frac{\sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}{2 \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}, \theta\right]$$

$$\left\{\left\{h \rightarrow \frac{m \sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}{2 \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}\right\}\right\}$$

$$\text{Solve}\left[h == \frac{m \sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}{2 \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}, m\right]$$

$$\left\{\left\{m \rightarrow \frac{2 h \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}{\sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}\right\}\right\}$$



$$\text{Solve}\left[h == \frac{\left(2 h \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2\right)}{\sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}\right]$$

$$\left(2 \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2\right), \theta]$$

{{}}

$$\text{Solve}\left[h == \frac{m \sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}{2 \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}, m\right]$$

$$\left\{\left\{m \rightarrow \frac{7 h}{53 \times 3^{3/4} \sqrt{\pi}}\right\}\right\}$$

$$\text{Solve}\left[h == \frac{\frac{7 h}{53 \times 3^{3/4} \sqrt{\pi}} \sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}{2 \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}, \theta\right]$$

Solve[True,  $\pi$ ]

$$\text{Simplify}\left[\frac{\frac{7 h}{53 \times 3^{3/4} \sqrt{\pi}} \sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (-80 \pi^4 + 224 \pi^3 \theta - 448 \pi^2 \theta^2 + 160 \pi \theta^3 - 15 \theta^4)}{2 \left(-\frac{4 \pi - \theta}{3 \pi^2 \theta^3} - \frac{1}{6 \pi^2 \theta^2}\right) \theta^2 \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2} / h\right]$$

$$\frac{7 \times 3^{1/4} \pi^{3/2} \theta \sqrt{\frac{((4 \pi - \theta) \theta)^{3/2}}{\theta^2}} (80 \pi^4 - 224 \pi^3 \theta + 448 \pi^2 \theta^2 - 160 \pi \theta^3 + 15 \theta^4)}{53 (8 \pi - \theta) \sqrt{(-2 \pi + \theta)^4} (8 \pi^2 - 6 \pi \theta + \theta^2)^2}$$

$$\text{Solve}\left[7 \times 3^{1/4} \pi^{3/2} \theta \sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (80\pi^4 - 224\pi^3\theta + 448\pi^2\theta^2 - 160\pi\theta^3 + 15\theta^4) ==\right.$$

$$\left.53(8\pi - \theta) \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)^2, \theta\right]$$

$$\{\{\theta \rightarrow \pi\}, \{\theta \rightarrow 4\pi\}, \{\theta \rightarrow$$

$$\pi \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right],$$

$$\{\theta \rightarrow \pi \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 13\right],$$

$$\{\theta \rightarrow \pi \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 14\right]\}\}$$

$$\text{Solve}\left[\frac{7 \times 3^{1/4} \pi^{3/2} \theta \sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (80\pi^4 - 224\pi^3\theta + 448\pi^2\theta^2 - 160\pi\theta^3 + 15\theta^4)}{53(8\pi - \theta) \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)^2} == 1, \theta\right]$$

$$\text{Solve}\left[h == \frac{\frac{7h}{53 \times 3^{3/4} \sqrt{\pi}} \sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (-80\pi^4 + 224\pi^3\theta - 448\pi^2\theta^2 + 160\pi\theta^3 - 15\theta^4)}{2 \left(-\frac{4\pi - \theta}{3\pi^2\theta^3} - \frac{1}{6\pi^2\theta^2}\right) \theta^2 \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)^2}, h\right]$$

$\{\{h \rightarrow 0\}\}$

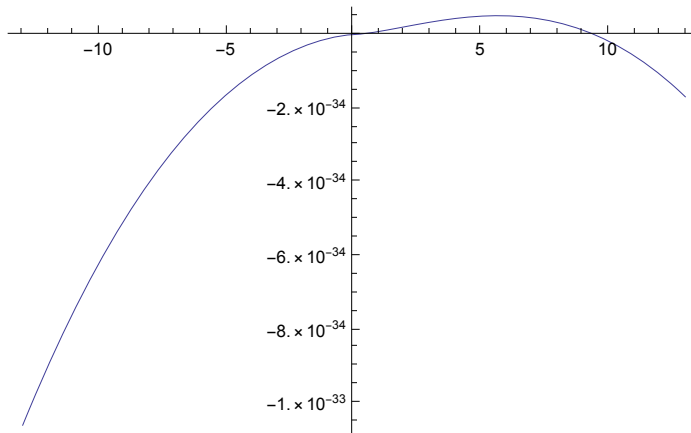
ParametricPlot[

$$\left\{ \frac{m \sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}} (-80\pi^4 + 224\pi^3\theta - 448\pi^2\theta^2 + 160\pi\theta^3 - 15\theta^4)}{2 \left(-\frac{4\pi - \theta}{3\pi^2\theta^3} - \frac{1}{6\pi^2\theta^2}\right) \theta^2 \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)^2}, \text{y function} \right\}, \{\text{var}, \text{min}, \text{max}\}]$$

$$\text{Solve}\left[h == \frac{m \sqrt{\frac{((4\theta - \theta)\theta)^{3/2}}{\theta^2}} (-80\theta^4 + 224\theta^3\theta - 448\theta^2\theta^2 + 160\theta\theta^3 - 15\theta^4)}{2\theta^2 \sqrt{(-2\theta + \theta)^4} (8\theta^2 - 6\theta\theta + \theta^2)^2 \left(\frac{4\theta - 2\theta}{12\pi\theta \sqrt{(4\theta - \theta)\theta}} - \frac{\sqrt{(4\theta - \theta)\theta}}{6\theta\theta^2}\right)}, m\right]$$

$$\left\{ \left\{ m \rightarrow -\frac{(6.626 \times 10^{-34}) \theta \sqrt{\theta^4} (-3\pi + \theta)}{159 \times 3^{1/4} \pi (\theta^2)^{3/4}} \right\} \right\}$$

$$\text{Plot}\left[-\frac{(6.626 \times 10^{-34}) \theta \sqrt{\theta^4} (-3\pi + \theta)}{159 \times 3^{1/4} \pi (\theta^2)^{3/4}}, \{\theta, -13, 13\}\right]$$



$\theta := \pi$

$$\text{Solve}\left[h == \left( \frac{(6.626 \times 10^{-34}) \theta \sqrt{\theta^4} (-3\pi + \theta)}{159 \times 3^{1/4} \pi (\theta^2)^{3/4}} \right) \sqrt{\frac{((4\theta - \theta) \theta)^{3/2}}{\theta^2}} (-80\theta^4 + 224\theta^3\theta - 448\theta^2\theta^2 + 160\theta\theta^3 - 15\theta^4) / \left( 2\theta^2 \sqrt{(-2\theta + \theta)^4} (8\theta^2 - 6\theta\theta + \theta^2)^2 \left( \frac{4\theta - 2\theta}{12\pi\theta \sqrt{(4\theta - \theta)\theta}} - \frac{\sqrt{(4\theta - \theta)\theta}}{6\theta\theta^2} \right) \right), \theta \right]$$

$$\text{Solve}[h == -6.626 \times 10^{-34}, \pi]$$

Solve[

$$\pi \text{Root}\left[2168918902061400064 - 18978040393037250560 \#1 + 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + 188564508611188480 \#1^{14} - 414645442256220736 \#1^{15} + 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + 10847052121181 \#1^{20} - 627853463651 \#1^{21} + 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1] ==$$

$$\text{Root}\left[3317760000 \text{m}^4 \pi^{16} - 37158912000 \text{m}^4 \pi^{15} \#1 + 230385254400 \text{m}^4 \pi^{14} \#1^2 + (-942137671680 \text{m}^4 \pi^{13} - 67108864 \text{h}^4 \pi^{19}) \#1^3 + (2801594843136 \text{m}^4 \pi^{12} + 587202560 \text{h}^4 \pi^{18}) \#1^4 + (-6218413867008 \text{m}^4 \pi^{11} - 2428502016 \text{h}^4 \pi^{17}) \#1^5 + (10484567506944 \text{m}^4 \pi^{10} + 6309281792 \text{h}^4 \pi^{16}) \#1^6 + (-13268250427392 \text{m}^4 \pi^9 - 11542724608 \text{h}^4 \pi^{15}) \#1^7 + (12416904377856 \text{m}^4 \pi^8 + 15797846016 \text{h}^4 \pi^{14}) \#1^8 + (-8208129116160 \text{m}^4 \pi^7 - 16771973120 \text{h}^4 \pi^{13}) \#1^9 + (3742726072320 \text{m}^4 \pi^6 + 14132445184 \text{h}^4 \pi^{12}) \#1^{10} + (-1171098777600 \text{m}^4 \pi^5 - 9589751808 \text{h}^4 \pi^{11}) \#1^{11} + (250171934400 \text{m}^4 \pi^4 + 5285609472 \text{h}^4 \pi^{10}) \#1^{12} + (-35827920000 \text{m}^4 \pi^3 - 2375712768 \text{h}^4 \pi^9) \#1^{13} + (3289248000 \text{m}^4 \pi^2 + 870604800 \text{h}^4 \pi^8) \#1^{14} + (-174960000 \text{m}^4 \pi - 258998272 \text{h}^4 \pi^7) \#1^{15} + (4100625 \text{m}^4 + 61988864 \text{h}^4 \pi^6) \#1^{16} - 11759616 \text{h}^4 \pi^5 \#1^{17} + 1727488 \text{h}^4 \pi^4 \#1^{18} - 189440 \text{h}^4 \pi^3 \#1^{19} + 14592 \text{h}^4 \pi^2 \#1^{20} - 704 \text{h}^4 \pi \#1^{21} + 16 \text{h}^4 \#1^{22} \&, 1], \text{m}]$$

$$\left\{ \left\{ \text{m} \rightarrow - \left( 2 \left( 4194304 \text{h}^4 \pi^6 \text{Root}\left[2168918902061400064 - 18978040393037250560 \#1 + 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + 648682023351408197632 \#1^6 - \right. \right. \right. \right.$$

$$\begin{aligned}
& 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - \\
& 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - \\
& 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - \\
& 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - \\
& 414\,645\,442\,256\,220\,736 \, \#1^{15} + 76\,017\,374\,115\,971\,904 \, \#1^{16} - \\
& 11\,512\,748\,778\,227\,136 \, \#1^{17} + 1\,421\,817\,926\,789\,824 \, \#1^{18} - \\
& 140\,603\,723\,926\,691 \, \#1^{19} + 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^3 - \\
& 36\,700\,160 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^4 + \\
& 151\,781\,376 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^5 - \\
& 394\,330\,112 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} +
\end{aligned}$$

$$\begin{aligned}
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^6 + \\
& 721\,420\,288 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^7 - \\
& 987\,365\,376 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& \quad 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^8 + 1\,048\,248\,320 \, h^4 \\
& \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^9 - \\
& 883\,277\,824 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 +
\end{aligned}$$

$$\begin{aligned}
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{10} + \\
& 599\,359\,488 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{11} - \\
& 330\,350\,592 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{12} + \\
& 148\,482\,048 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{13} -
\end{aligned}$$

$$\begin{aligned}
& 54\,412\,800\,h^4\,\pi^6\,\text{Root}\big[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& \quad 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& \quad 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1\big]^{14} + \\
& 16\,187\,392\,h^4\,\pi^6\,\text{Root}\big[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& \quad 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& \quad 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1\big]^{15} - \\
& 3\,874\,304\,h^4\,\pi^6\,\text{Root}\big[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& \quad 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& \quad 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1\big]^{16} + \\
& 734\,976\,h^4\,\pi^6\,\text{Root}\big[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} +
\end{aligned}$$



$$\begin{aligned}
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{17} - \\
& 107\,968 \, h^4 \pi^6 \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1\right]^{18} + \\
& 11\,840 \, h^4 \pi^6 \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1\right]^{19} - \\
& 912 \, h^4 \pi^6 \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1\right]^{20} + \\
& 44 \, h^4 \pi^6 \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right.
\end{aligned}$$

$$\begin{aligned}
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1]^{21} - \\
& h^4 \pi^6 \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1]^{22})^{1/4}) / \\
& \left( 3 \left( 40\,960\,000 - 458\,752\,000 \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \right. \right. \\
& \quad \#1 + 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \\
& \quad \#1^3 + 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \\
& \quad \#1^5 + 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \\
& \quad \#1^7 + 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \\
& \quad \#1^9 + 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \\
& \quad \#1^{11} + 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \\
& \quad \#1^{13} + 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \\
& \quad \#1^{15} + 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \\
& \quad \#1^{17} + 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \\
& \quad \#1^{19} + 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1\right] + \\
& \quad 2\,844\,262\,400 \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad \left. 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \right.
\end{aligned}$$

$$\begin{aligned}
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^2 - \\
11\,631\,329\,280 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^3 + \\
34\,587\,590\,656 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^4 - \\
76\,770\,541\,568 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^5 + \\
129\,439\,105\,024 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 +
\end{aligned}$$

$$\begin{aligned}
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^6 - \\
163\,805\,560\,832 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^7 + \\
153\,295\,115\,776 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^8 - \\
101\,334\,927\,360 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} +
\end{aligned}$$

$$\begin{aligned}
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^9 + \\
46\,206\,494\,720 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{10} - \\
14\,458\,009\,600 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{11} + \\
3\,088\,542\,400 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{12} - \\
442\,320\,000 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 +
\end{aligned}$$

$$\begin{aligned}
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{13} + \\
40\,608\,000 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{14} - \\
2\,160\,000 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{15} + \\
50\,625 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} +
\end{aligned}$$

$$\begin{aligned}
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + 25604610845 \#1^{22} - \\
& 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{16})^{1/4})\}, \\
\left\{ m \rightarrow - \left( 2 \, i \, \left( 4194304 h^4 \pi^6 \operatorname{Root}\left[ 2168918902061400064 - 18978040393037250560 \#1 + \right. \right. \right. \right. \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{3} - \\
& 36700160 h^4 \pi^6 \operatorname{Root}\left[ 2168918902061400064 - 18978040393037250560 \#1 + \right. \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{4} + \\
& 151781376 h^4 \pi^6 \operatorname{Root}\left[ 2168918902061400064 - 18978040393037250560 \#1 + \right. \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{5} - \\
& 394330112 h^4 \pi^6 \operatorname{Root}\left[ 2168918902061400064 - 18978040393037250560 \#1 + \right. \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 +
\end{aligned}$$

$$\begin{aligned}
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^6 + \\
& 721\,420\,288 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^7 - \\
& 987\,365\,376 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^8 + 1\,048\,248\,320 \, h^4 \\
& \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} +
\end{aligned}$$



$$\begin{aligned}
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1] ^9 - \\
& 883277824 h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1] ^{10} + \\
& 599359488 h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1] ^{11} - \\
& 330350592 h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1] ^{12} + \\
& 148482048 h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 +
\end{aligned}$$

$$\begin{aligned}
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{13} - \\
& 54\,412\,800 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{14} + \\
& 16\,187\,392 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{15} - \\
& 3\,874\,304 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} +
\end{aligned}$$

$$\begin{aligned}
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{16} + \\
734\,976 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{17} - \\
107\,968 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{18} + \\
11\,840 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{19} - \\
912 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 +
\end{aligned}$$

$$\begin{aligned}
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{20} + \\
& 44 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{21} - \\
& h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \, \Big]^{22} \Big)^{1/4} \Big) / \\
& \Big( 3 \Big( 40\,960\,000 - 458\,752\,000 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \\
& \, \#1 + 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \\
& \, \#1^3 + 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \\
& \, \#1^5 + 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \\
& \, \#1^7 + 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \\
& \, \#1^9 + 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \\
& \, \#1^{11} + 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \\
& \, \#1^{13} + 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \\
& \, \#1^{15} + 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \\
& \, \#1^{17} + 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691
\end{aligned}$$

$$\begin{aligned}
& \#1^{19} + 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1] + \\
& 2\,844\,262\,400\,\text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1]^2 - \\
& 11\,631\,329\,280\,\text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1]^3 + \\
& 34\,587\,590\,656\,\text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1]^4 - \\
& 76\,770\,541\,568\,\text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \\
& 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 +
\end{aligned}$$

$$\begin{aligned}
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big] ^5 + \\
129\,439\,105\,024 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big] ^6 - \\
163\,805\,560\,832 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big] ^7 + \\
153\,295\,115\,776 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big] ^8 -
\end{aligned}$$

$$\begin{aligned}
& 101\,334\,927\,360 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right]^9 + \\
& 46\,206\,494\,720 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right]^{10} - \\
& 14\,458\,009\,600 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right]^{11} + \\
& 3\,088\,542\,400 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad \left. 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \right.
\end{aligned}$$

$$\begin{aligned}
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{12} - \\
442\,320\,000 \, \text{Root} [ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{13} + \\
40\,608\,000 \, \text{Root} [ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{14} - \\
2\,160\,000 \, \text{Root} [ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{15} + \\
50\,625 \, \text{Root} [ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 +
\end{aligned}$$



$$\left\{ m \rightarrow \left( 2 \pm \left( 4 \cdot 194 \cdot 304 \cdot h^4 \cdot \pi^6 \cdot \text{Root} \left[ 2 \cdot 168 \cdot 918 \cdot 902 \cdot 061 \cdot 400 \cdot 064 - 18 \cdot 978 \cdot 040 \cdot 393 \cdot 037 \cdot 250 \cdot 560 \cdot \#1 + \right. \right. \right. \\ 79 \cdot 368 \cdot 876 \cdot 072 \cdot 309 \cdot 358 \cdot 592 \cdot \#1^2 - 210 \cdot 927 \cdot 363 \cdot 520 \cdot 506 \cdot 036 \cdot 224 \cdot \#1^3 + \\ 399 \cdot 577 \cdot 242 \cdot 368 \cdot 348 \cdot 585 \cdot 984 \cdot \#1^4 - 573 \cdot 829 \cdot 583 \cdot 478 \cdot 846 \cdot 586 \cdot 880 \cdot \#1^5 + \\ 648 \cdot 682 \cdot 023 \cdot 351 \cdot 408 \cdot 197 \cdot 632 \cdot \#1^6 - 591 \cdot 701 \cdot 371 \cdot 191 \cdot 864 \cdot 410 \cdot 112 \cdot \#1^7 + \\ 442 \cdot 936 \cdot 140 \cdot 843 \cdot 213 \cdot 864 \cdot 960 \cdot \#1^8 - 275 \cdot 308 \cdot 180 \cdot 674 \cdot 442 \cdot 018 \cdot 816 \cdot \#1^9 + \\ 143 \cdot 208 \cdot 928 \cdot 923 \cdot 654 \cdot 668 \cdot 288 \cdot \#1^{10} - 62 \cdot 655 \cdot 701 \cdot 239 \cdot 304 \cdot 847 \cdot 872 \cdot \#1^{11} + \\ 23 \cdot 115 \cdot 614 \cdot 063 \cdot 608 \cdot 354 \cdot 304 \cdot \#1^{12} - 7 \cdot 194 \cdot 172 \cdot 796 \cdot 107 \cdot 088 \cdot 384 \cdot \#1^{13} + \\ 1 \cdot 885 \cdot 645 \cdot 086 \cdot 111 \cdot 188 \cdot 480 \cdot \#1^{14} - 414 \cdot 645 \cdot 442 \cdot 256 \cdot 220 \cdot 736 \cdot \#1^{15} + \\ 76 \cdot 017 \cdot 374 \cdot 115 \cdot 971 \cdot 904 \cdot \#1^{16} - 11 \cdot 512 \cdot 748 \cdot 778 \cdot 227 \cdot 136 \cdot \#1^{17} + \\ 1 \cdot 421 \cdot 817 \cdot 926 \cdot 789 \cdot 824 \cdot \#1^{18} - 140 \cdot 603 \cdot 723 \cdot 926 \cdot 691 \cdot \#1^{19} + \\ 10 \cdot 847 \cdot 052 \cdot 121 \cdot 181 \cdot \#1^{20} - 627 \cdot 853 \cdot 463 \cdot 651 \cdot \#1^{21} + 25 \cdot 604 \cdot 610 \cdot 845 \cdot \#1^{22} - \\ \left. \left. \left. 654 \cdot 909 \cdot 923 \cdot \#1^{23} + 7 \cdot 890 \cdot 481 \cdot \#1^{24} \&, 1 \right]^{16} \right)^{1/4} \right\}, \\ \\ \left\{ m \rightarrow \left( 2 \pm \left( 4 \cdot 194 \cdot 304 \cdot h^4 \cdot \pi^6 \cdot \text{Root} \left[ 2 \cdot 168 \cdot 918 \cdot 902 \cdot 061 \cdot 400 \cdot 064 - 18 \cdot 978 \cdot 040 \cdot 393 \cdot 037 \cdot 250 \cdot 560 \cdot \#1 + \right. \right. \right. \\ 79 \cdot 368 \cdot 876 \cdot 072 \cdot 309 \cdot 358 \cdot 592 \cdot \#1^2 - 210 \cdot 927 \cdot 363 \cdot 520 \cdot 506 \cdot 036 \cdot 224 \cdot \#1^3 + \\ 399 \cdot 577 \cdot 242 \cdot 368 \cdot 348 \cdot 585 \cdot 984 \cdot \#1^4 - 573 \cdot 829 \cdot 583 \cdot 478 \cdot 846 \cdot 586 \cdot 880 \cdot \#1^5 + \\ 648 \cdot 682 \cdot 023 \cdot 351 \cdot 408 \cdot 197 \cdot 632 \cdot \#1^6 - 591 \cdot 701 \cdot 371 \cdot 191 \cdot 864 \cdot 410 \cdot 112 \cdot \#1^7 + \\ 442 \cdot 936 \cdot 140 \cdot 843 \cdot 213 \cdot 864 \cdot 960 \cdot \#1^8 - 275 \cdot 308 \cdot 180 \cdot 674 \cdot 442 \cdot 018 \cdot 816 \cdot \#1^9 + \\ 143 \cdot 208 \cdot 928 \cdot 923 \cdot 654 \cdot 668 \cdot 288 \cdot \#1^{10} - 62 \cdot 655 \cdot 701 \cdot 239 \cdot 304 \cdot 847 \cdot 872 \cdot \#1^{11} + \\ 23 \cdot 115 \cdot 614 \cdot 063 \cdot 608 \cdot 354 \cdot 304 \cdot \#1^{12} - 7 \cdot 194 \cdot 172 \cdot 796 \cdot 107 \cdot 088 \cdot 384 \cdot \#1^{13} + \\ 1 \cdot 885 \cdot 645 \cdot 086 \cdot 111 \cdot 188 \cdot 480 \cdot \#1^{14} - 414 \cdot 645 \cdot 442 \cdot 256 \cdot 220 \cdot 736 \cdot \#1^{15} + \\ 76 \cdot 017 \cdot 374 \cdot 115 \cdot 971 \cdot 904 \cdot \#1^{16} - 11 \cdot 512 \cdot 748 \cdot 778 \cdot 227 \cdot 136 \cdot \#1^{17} + \\ 1 \cdot 421 \cdot 817 \cdot 926 \cdot 789 \cdot 824 \cdot \#1^{18} - 140 \cdot 603 \cdot 723 \cdot 926 \cdot 691 \cdot \#1^{19} + \\ 10 \cdot 847 \cdot 052 \cdot 121 \cdot 181 \cdot \#1^{20} - 627 \cdot 853 \cdot 463 \cdot 651 \cdot \#1^{21} + \\ 25 \cdot 604 \cdot 610 \cdot 845 \cdot \#1^{22} - 654 \cdot 909 \cdot 923 \cdot \#1^{23} + 7 \cdot 890 \cdot 481 \cdot \#1^{24} \&, 1 \right]^{16} \right)^{1/4} \right\} - \\ 36 \cdot 700 \cdot 160 \cdot h^4 \cdot \pi^6 \cdot \text{Root} \left[ 2 \cdot 168 \cdot 918 \cdot 902 \cdot 061 \cdot 400 \cdot 064 - 18 \cdot 978 \cdot 040 \cdot 393 \cdot 037 \cdot 250 \cdot 560 \cdot \#1 + \right. \\ 79 \cdot 368 \cdot 876 \cdot 072 \cdot 309 \cdot 358 \cdot 592 \cdot \#1^2 - 210 \cdot 927 \cdot 363 \cdot 520 \cdot 506 \cdot 036 \cdot 224 \cdot \#1^3 + \\ 399 \cdot 577 \cdot 242 \cdot 368 \cdot 348 \cdot 585 \cdot 984 \cdot \#1^4 - 573 \cdot 829 \cdot 583 \cdot 478 \cdot 846 \cdot 586 \cdot 880 \cdot \#1^5 + \\ 648 \cdot 682 \cdot 023 \cdot 351 \cdot 408 \cdot 197 \cdot 632 \cdot \#1^6 - 591 \cdot 701 \cdot 371 \cdot 191 \cdot 864 \cdot 410 \cdot 112 \cdot \#1^7 + \\ 442 \cdot 936 \cdot 140 \cdot 843 \cdot 213 \cdot 864 \cdot 960 \cdot \#1^8 - 275 \cdot 308 \cdot 180 \cdot 674 \cdot 442 \cdot 018 \cdot 816 \cdot \#1^9 + \\ 143 \cdot 208 \cdot 928 \cdot 923 \cdot 654 \cdot 668 \cdot 288 \cdot \#1^{10} - 62 \cdot 655 \cdot 701 \cdot 239 \cdot 304 \cdot 847 \cdot 872 \cdot \#1^{11} + \\ 23 \cdot 115 \cdot 614 \cdot 063 \cdot 608 \cdot 354 \cdot 304 \cdot \#1^{12} - 7 \cdot 194 \cdot 172 \cdot 796 \cdot 107 \cdot 088 \cdot 384 \cdot \#1^{13} + \\ 1 \cdot 885 \cdot 645 \cdot 086 \cdot 111 \cdot 188 \cdot 480 \cdot \#1^{14} - 414 \cdot 645 \cdot 442 \cdot 256 \cdot 220 \cdot 736 \cdot \#1^{15} + \\ 76 \cdot 017 \cdot 374 \cdot 115 \cdot 971 \cdot 904 \cdot \#1^{16} - 11 \cdot 512 \cdot 748 \cdot 778 \cdot 227 \cdot 136 \cdot \#1^{17} + \\ 1 \cdot 421 \cdot 817 \cdot 926 \cdot 789 \cdot 824 \cdot \#1^{18} - 140 \cdot 603 \cdot 723 \cdot 926 \cdot 691 \cdot \#1^{19} + \\ 10 \cdot 847 \cdot 052 \cdot 121 \cdot 181 \cdot \#1^{20} - 627 \cdot 853 \cdot 463 \cdot 651 \cdot \#1^{21} + \\ 25 \cdot 604 \cdot 610 \cdot 845 \cdot \#1^{22} - 654 \cdot 909 \cdot 923 \cdot \#1^{23} + 7 \cdot 890 \cdot 481 \cdot \#1^{24} \&, 1 \right]^{16} \right)^{1/4} + \\ 151 \cdot 781 \cdot 376 \cdot h^4 \cdot \pi^6 \cdot \text{Root} \left[ 2 \cdot 168 \cdot 918 \cdot 902 \cdot 061 \cdot 400 \cdot 064 - 18 \cdot 978 \cdot 040 \cdot 393 \cdot 037 \cdot 250 \cdot 560 \cdot \#1 + \right. \\ 79 \cdot 368 \cdot 876 \cdot 072 \cdot 309 \cdot 358 \cdot 592 \cdot \#1^2 - 210 \cdot 927 \cdot 363 \cdot 520 \cdot 506 \cdot 036 \cdot 224 \cdot \#1^3 + \\ 399 \cdot 577 \cdot 242 \cdot 368 \cdot 348 \cdot 585 \cdot 984 \cdot \#1^4 - 573 \cdot 829 \cdot 583 \cdot 478 \cdot 846 \cdot 586 \cdot 880 \cdot \#1^5 + \\ 648 \cdot 682 \cdot 023 \cdot 351 \cdot 408 \cdot 197 \cdot 632 \cdot \#1^6 - 591 \cdot 701 \cdot 371 \cdot 191 \cdot 864 \cdot 410 \cdot 112 \cdot \#1^7 + \\ 442 \cdot 936 \cdot 140 \cdot 843 \cdot 213 \cdot 864 \cdot 960 \cdot \#1^8 - 275 \cdot 308 \cdot 180 \cdot 674 \cdot 442 \cdot 018 \cdot 816 \cdot \#1^9 + \\ 143 \cdot 208 \cdot 928 \cdot 923 \cdot 654 \cdot 668 \cdot 288 \cdot \#1^{10} - 62 \cdot 655 \cdot 701 \cdot 239 \cdot 304 \cdot 847 \cdot 872$$

$$\begin{aligned}
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^5 - \\
394\,330\,112 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^6 + \\
721\,420\,288 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^7 - \\
987\,365\,376 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^8 + \\
1\,048\,248\,320 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 +
\end{aligned}$$

$$\begin{aligned}
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^9 - \\
& 883\,277\,824 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{10} + \\
& 599\,359\,488 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{11} - \\
& 330\,350\,592 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} +
\end{aligned}$$

$$\begin{aligned}
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{12} + \\
148\,482\,048 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{13} - \\
54\,412\,800 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{14} + \\
16\,187\,392 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{15} - \\
3\,874\,304 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 +
\end{aligned}$$

$$\begin{aligned}
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{16} + \\
734\,976 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{17} - \\
107\,968 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{18} + \\
11\,840 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} +
\end{aligned}$$

$$\begin{aligned}
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{19} - \\
912 h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{20} + \\
44 h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + \\
& 25604610845 \#1^{22} - 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{21} - \\
h^4 \pi^6 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \\
& 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \\
& 399577242368348585984 \#1^4 - 573829583478846586880 \#1^5 + \\
& 648682023351408197632 \#1^6 - 591701371191864410112 \#1^7 + \\
& 442936140843213864960 \#1^8 - 275308180674442018816 \#1^9 + \\
& 143208928923654668288 \#1^{10} - 62655701239304847872 \#1^{11} + \\
& 23115614063608354304 \#1^{12} - 7194172796107088384 \#1^{13} + \\
& 1885645086111188480 \#1^{14} - 414645442256220736 \#1^{15} + \\
& 76017374115971904 \#1^{16} - 11512748778227136 \#1^{17} + \\
& 1421817926789824 \#1^{18} - 140603723926691 \#1^{19} + \\
& 10847052121181 \#1^{20} - 627853463651 \#1^{21} + 25604610845 \#1^{22} - \\
& 654909923 \#1^{23} + 7890481 \#1^{24} \&, 1]^{22})^{1/4}) / \\
3 \left( 40960000 - 458752000 \text{Root}[2168918902061400064 - 18978040393037250560 \#1 + \right. \\
& \left. 79368876072309358592 \#1^2 - 210927363520506036224 \#1^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1] + \\
& 2\,844\,262\,400 \, \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1\right]^2 - \\
& 11\,631\,329\,280 \, \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1\right]^3 + \\
& 34\,587\,590\,656 \, \text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad \left. 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \right.
\end{aligned}$$

$$\begin{aligned}
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^4 - \\
76\,770\,541\,568 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^5 + \\
129\,439\,105\,024 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^6 - \\
163\,805\,560\,832 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^7 + \\
153\,295\,115\,776 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 +
\end{aligned}$$



$$\begin{aligned}
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^8 - \\
101\,334\,927\,360 \operatorname{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^9 + \\
46\,206\,494\,720 \operatorname{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^{10} - \\
14\,458\,009\,600 \operatorname{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} +
\end{aligned}$$

$$\begin{aligned}
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1]^{11} + \\
3\,088\,542\,400 \text{ Root} \big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1]^{12} - \\
442\,320\,000 \text{ Root} \big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1]^{13} + \\
40\,608\,000 \text{ Root} \big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1]^{14} - \\
2\,160\,000 \text{ Root} \big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 +
\end{aligned}$$

$$\begin{aligned}
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{15} + \\
& 50\,625 \operatorname{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{16} \Big)^{1/4} \Big\}, \\
& \left\{ m \rightarrow \left( 2 \left( 4\,194\,304 \, h^4 \, \pi^6 \operatorname{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \right. \right. \right. \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{16} \Big)^{1/4} \Big)^3 - \\
& 36\,700\,160 \, h^4 \, \pi^6 \operatorname{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} +
\end{aligned}$$

$$\begin{aligned}
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^4 + \\
151\,781\,376 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^5 - \\
394\,330\,112 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^6 + \\
721\,420\,288 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^7 - \\
987\,365\,376 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 +
\end{aligned}$$

$$\begin{aligned}
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \Big]^8 + \\
1\,048\,248\,320 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \Big]^9 - \\
883\,277\,824 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, \, 1 \Big]^{10} + \\
599\,359\,488 \, h^4 \, \pi^6 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} +
\end{aligned}$$

$$\begin{aligned}
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{11} - \\
& 330\,350\,592 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{12} + \\
& 148\,482\,048 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{13} - \\
& 54\,412\,800 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& \quad 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1]^{14} + \\
& 16\,187\,392 \, h^4 \, \pi^6 \, \text{Root}[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& \quad 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 +
\end{aligned}$$

$$\begin{aligned}
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{15} - \\
& 3\,874\,304 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{16} + \\
& 734\,976 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{17} - \\
& 107\,968 \, h^4 \, \pi^6 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^{18} +
\end{aligned}$$

$$\begin{aligned}
& 11\,840\,h^4\pi^6\text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& \quad 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& \quad \left. 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1\right]^{19} - \\
& 912\,h^4\pi^6\text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& \quad 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& \quad \left. 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1\right]^{20} + \\
& 44\,h^4\pi^6\text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480\,\#1^{14} - 414\,645\,442\,256\,220\,736\,\#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904\,\#1^{16} - 11\,512\,748\,778\,227\,136\,\#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824\,\#1^{18} - 140\,603\,723\,926\,691\,\#1^{19} + \\
& \quad 10\,847\,052\,121\,181\,\#1^{20} - 627\,853\,463\,651\,\#1^{21} + \\
& \quad \left. 25\,604\,610\,845\,\#1^{22} - 654\,909\,923\,\#1^{23} + 7\,890\,481\,\#1^{24} \&, 1\right]^{21} - \\
& h^4\pi^6\text{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560\,\#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592\,\#1^2 - 210\,927\,363\,520\,506\,036\,224\,\#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984\,\#1^4 - 573\,829\,583\,478\,846\,586\,880\,\#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632\,\#1^6 - 591\,701\,371\,191\,864\,410\,112\,\#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960\,\#1^8 - 275\,308\,180\,674\,442\,018\,816\,\#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288\,\#1^{10} - 62\,655\,701\,239\,304\,847\,872\,\#1^{11} + \\
& \quad \left. 23\,115\,614\,063\,608\,354\,304\,\#1^{12} - 7\,194\,172\,796\,107\,088\,384\,\#1^{13} + \right.
\end{aligned}$$



$$\begin{aligned}
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big)^{22} \Big)^{1/4} \Big) / \\
& \Big( 3 \Big( 40\,960\,000 - 458\,752\,000 \operatorname{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big] + \\
& 2\,844\,262\,400 \operatorname{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^2 - \\
& 11\,631\,329\,280 \operatorname{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \Big]^3 +
\end{aligned}$$

$$\begin{aligned}
& 34\,587\,590\,656 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right]^4 - \\
& 76\,770\,541\,568 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right]^5 + \\
& 129\,439\,105\,024 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& \quad 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& \quad 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& \quad 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& \quad 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& \quad \left. 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1\right]^6 - \\
& 163\,805\,560\,832 \operatorname{Root}\left[2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \right. \\
& \quad 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& \quad 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& \quad 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& \quad 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& \quad 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& \quad \left. 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \right.
\end{aligned}$$

$$\begin{aligned}
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^7 + \\
153\,295\,115\,776 \text{ Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^8 - \\
101\,334\,927\,360 \text{ Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^9 + \\
46\,206\,494\,720 \text{ Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \#1^2 - 210\,927\,363\,520\,506\,036\,224 \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \#1^4 - 573\,829\,583\,478\,846\,586\,880 \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \#1^6 - 591\,701\,371\,191\,864\,410\,112 \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \#1^8 - 275\,308\,180\,674\,442\,018\,816 \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \#1^{14} - 414\,645\,442\,256\,220\,736 \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \#1^{16} - 11\,512\,748\,778\,227\,136 \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \#1^{18} - 140\,603\,723\,926\,691 \#1^{19} + \\
& 10\,847\,052\,121\,181 \#1^{20} - 627\,853\,463\,651 \#1^{21} + \\
& 25\,604\,610\,845 \#1^{22} - 654\,909\,923 \#1^{23} + 7\,890\,481 \#1^{24} \&, 1 \Big]^{10} - \\
14\,458\,009\,600 \text{ Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \#1 +
\end{aligned}$$

$$\begin{aligned}
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{11} + \\
3\,088\,542\,400 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{12} - \\
442\,320\,000 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{13} + \\
40\,608\,000 \, \text{Root} \Big[ & 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} +
\end{aligned}$$

$$\begin{aligned}
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{14} - \\
& 2\,160\,000 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + \\
& 25\,604\,610\,845 \, \#1^{22} - 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{15} + \\
& 50\,625 \, \text{Root} \Big[ 2\,168\,918\,902\,061\,400\,064 - 18\,978\,040\,393\,037\,250\,560 \, \#1 + \\
& 79\,368\,876\,072\,309\,358\,592 \, \#1^2 - 210\,927\,363\,520\,506\,036\,224 \, \#1^3 + \\
& 399\,577\,242\,368\,348\,585\,984 \, \#1^4 - 573\,829\,583\,478\,846\,586\,880 \, \#1^5 + \\
& 648\,682\,023\,351\,408\,197\,632 \, \#1^6 - 591\,701\,371\,191\,864\,410\,112 \, \#1^7 + \\
& 442\,936\,140\,843\,213\,864\,960 \, \#1^8 - 275\,308\,180\,674\,442\,018\,816 \, \#1^9 + \\
& 143\,208\,928\,923\,654\,668\,288 \, \#1^{10} - 62\,655\,701\,239\,304\,847\,872 \, \#1^{11} + \\
& 23\,115\,614\,063\,608\,354\,304 \, \#1^{12} - 7\,194\,172\,796\,107\,088\,384 \, \#1^{13} + \\
& 1\,885\,645\,086\,111\,188\,480 \, \#1^{14} - 414\,645\,442\,256\,220\,736 \, \#1^{15} + \\
& 76\,017\,374\,115\,971\,904 \, \#1^{16} - 11\,512\,748\,778\,227\,136 \, \#1^{17} + \\
& 1\,421\,817\,926\,789\,824 \, \#1^{18} - 140\,603\,723\,926\,691 \, \#1^{19} + \\
& 10\,847\,052\,121\,181 \, \#1^{20} - 627\,853\,463\,651 \, \#1^{21} + 25\,604\,610\,845 \, \#1^{22} - \\
& 654\,909\,923 \, \#1^{23} + 7\,890\,481 \, \#1^{24} \, \&, 1 \, \Big]^{16} \Big)^{1/4} \Big) \Big\} \Big\}
\end{aligned}$$

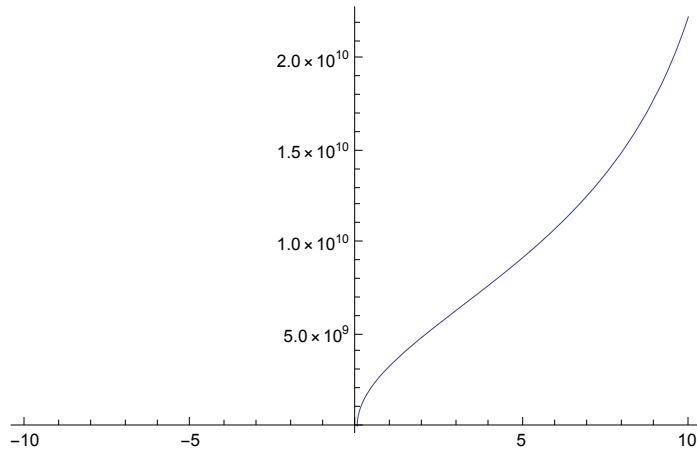
Previously, it was shown that the radius of our initial circle can be expressed in terms of the height of a cone and a given angle through which the initial circle is folded, pulling a cone into the third dimension.

$$\left\{ r \rightarrow \frac{2 h \pi}{\sqrt{4 \pi \theta - \theta^2}} \right\} \quad (51)$$

$$h = c * 6 * \theta; \text{ where } c \simeq (3.0 * 10^8) \quad (52)$$

In our space-time model, the cone extends through its height at the speed of light. Although, for every distance  $r$  traveled by the light, through a certain amount of time, into the dimension represented by the distance  $h$ , the circumference of the initial circle declines at a rate such that the distance that theta covers in arc lengths relating to the circumference of the base of the cone and the radial distance covered, does not exceed  $r$ . For, if it did exceed  $r$ , light would have a specific geometric element that goes faster than light, which is a paradox of the highest order.

$$\text{Plot}\left[\frac{2 (3.0 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}}, \{\theta, -10, 10\}\right]$$



$$r = \frac{2 (3.0 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\frac{4 \pi^2 h^2}{4 \pi \theta - \theta^2} = r^2$$

We are now going to redefine the variable h to distinguish it from Planck' s constant.

From this point forth, what was previously known as the variable h, height, will now be termed y, and it is the height of the cone.

$$\frac{4 \pi^2 y^2}{4 \pi \theta - \theta^2} = r^2$$

h is Planck' s Constant and is expressible by :

$$h = 6.62606896 \times 10^{-34}$$

$$6.62607 \times 10^{-34}$$

$$E = h \nu, \text{ where } E \text{ is energy, } h \text{ is Planck' s Constant, and } \nu \text{ is frequency.} \quad (53)$$

$$E = \hbar \omega, \text{ where } E \text{ is energy, } \hbar \text{ is } h/2\pi, \text{ and } \omega \text{ is angular frequency.} \quad (54)$$

$$\nu = \lambda \nu, \text{ where } \nu \text{ is velocity, } \lambda \text{ is wavelength, and } f \text{ is frequency.} \quad (55)$$

$$E = m c^2, \text{ where } E \text{ is energy, } m \text{ is mass, and } c \text{ is the speed of light.} \quad (56)$$

We will now say that the wavelength,  $\lambda$ , has the quality of the geometric system that takes a circle and folds it into a cone. That wavelength can be described by the function of height and angle, and reduced to being purely in terms of theta.

$$r = \frac{2 (3.0 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \lambda$$

$$\text{Solve}\left[(3.0 * 10^8) == \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} * v, v\right]$$

$$\left\{\left\{v \rightarrow \frac{0.0265258 \sqrt{12.5664 \theta - 1. \theta^2}}{\theta}\right\}\right\}$$

$$E = m c^2 = h v$$

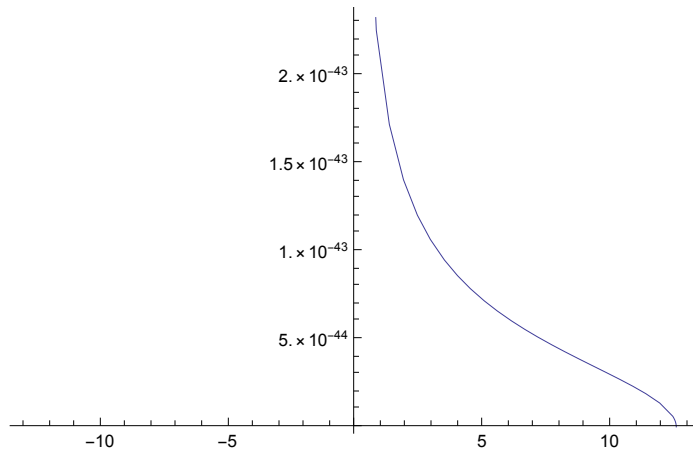
$$m c^2 = h v = (6.62606896 * 10^{-34}) v$$

$$\text{Solve}\left[(6.62606896 * 10^{-34})\right]$$

$$\left(\frac{0.02652582384864922 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{\theta}\right) == m (3.0 * 10^8), m\right]$$

$$\left\{\left\{m \rightarrow \frac{5.85873 \times 10^{-44} \sqrt{12.5664 \theta - 1. \theta^2}}{\theta}\right\}\right\}$$

$$\text{Plot}\left[\frac{5.858731268065412 * 10^{-44} \sqrt{12.566370614359172 \theta - 1. \theta^2}}{\theta}, \{\theta, -13, 13\}\right]$$



$$\text{Solve}\left[0 == \frac{5.858731268065412 * 10^{-44} \sqrt{12.566370614359172 \theta - 1. \theta^2}}{\theta}, \theta\right]$$

$$\{\{\theta \rightarrow 12.5664\}\}$$

$$4 \pi - 12.566370614359172$$

$$0.$$

$$\text{Solve}\left[\frac{4 \pi^2 y^2}{4 \pi (4 \pi) - (4 \pi)^2} == r^2, y\right]$$

$$\{\{\}\}$$

$$m \rightarrow \frac{5.858731268065412 * 10^{-44} \sqrt{12.566370614359172 \theta - 1. \theta^2}}{\theta}$$

$$\frac{5.858731268065412 \cdot 10^{-44} \sqrt{12.566370614359172 (360) - 1. (360)^2}}{360}$$

$$0. + 5.75557 \times 10^{-44} i$$

$$\frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}}$$

$$2 \pi = \text{ArcTan}[r_1 / h]$$

$$r_1 = \sqrt{(r^2 - h^2)}$$

$$\frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi} = h = c \tau = (18.0 \cdot 10^8) \theta$$

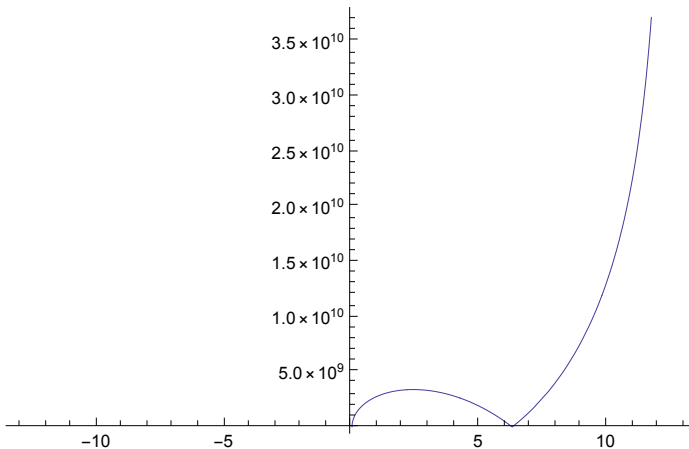
$$r = \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \lambda$$

$$\frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} = h$$

$$r_1 = \sqrt{\left( \left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \left( \frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2 \right)}$$

Plot[

$$\sqrt{\left( \left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \left( \frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2 \right)}, \{\theta, -13, 13\}]$$





$$r_1 = \sqrt{\left( \left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2}$$

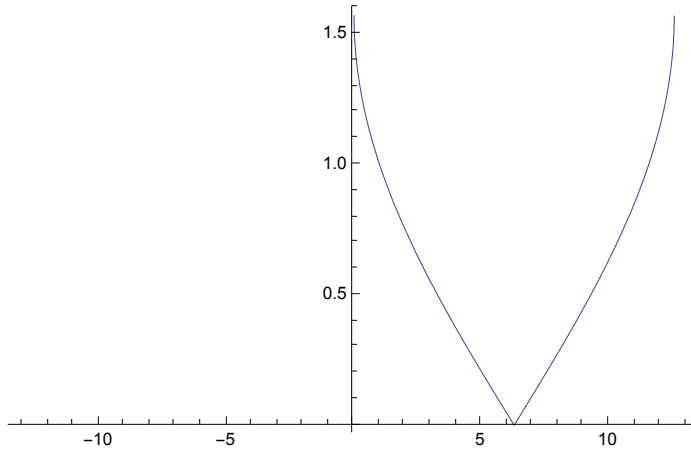
$$2 \pi = \text{ArcTan}[r_1 / h] :=$$

$$\text{ArcTan} \left[ \sqrt{\left( \left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2} \right] /$$

$$\frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi}, \{\theta, -13, 13\}]$$

$$\text{Plot} \left[ \text{ArcTan} \left[ \sqrt{\left( \left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2} \right] / \right.$$

$$\left. \frac{\sqrt{\left( \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right], \{\theta, -13, 13\}]$$



Solve[

$$2 \pi == \text{ArcTan} \left[ \sqrt{\left( \left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2} \right] /$$

$$\frac{\sqrt{\left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi}, \theta]$$

{ }

Tan[2 π]

0

$$\text{Solve}[0 == \sqrt{\left( \left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2} /$$

$$\frac{\sqrt{\left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi}, \theta]$$

{ {θ → 6.28319} , {θ → 6.28319} }

$$\sqrt{\left( \left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2} /$$

$$\frac{\sqrt{\left( \frac{2 (3.0 * 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi}, \theta]$$

We know that only radiant energy is available to the eye for stimuli. I will now show that this radiant energy can be expressed in terms of the parameters of the cone. The wavelength of light is the height of the cone, and the velocity of the light is equal to the speed of light in a vacuum. Therefore, we can place the energy of the light in terms of the speed of light, the initial radius of the circle, and the velocity of light. We can then show that information available in this energy comes in the idea of illusory contour. This mean that everything we see is an illusion.

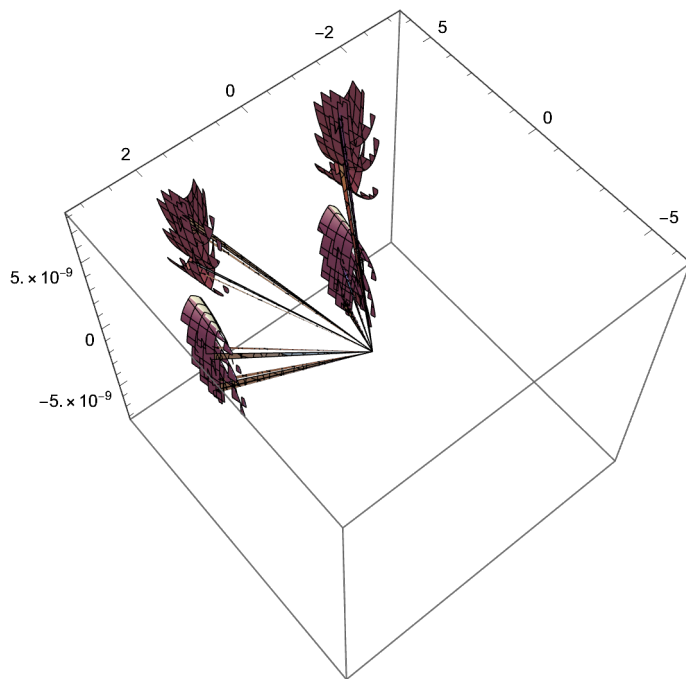
$$\text{velocity} = \lambda \nu = \eta \nu = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \nu = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left( \frac{1}{\left( \frac{\theta}{k} \right)} \right) = c$$

$$\text{Solve}\left[\frac{4 \pi r^2}{c^2 + r^2} == 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right), r\right]$$

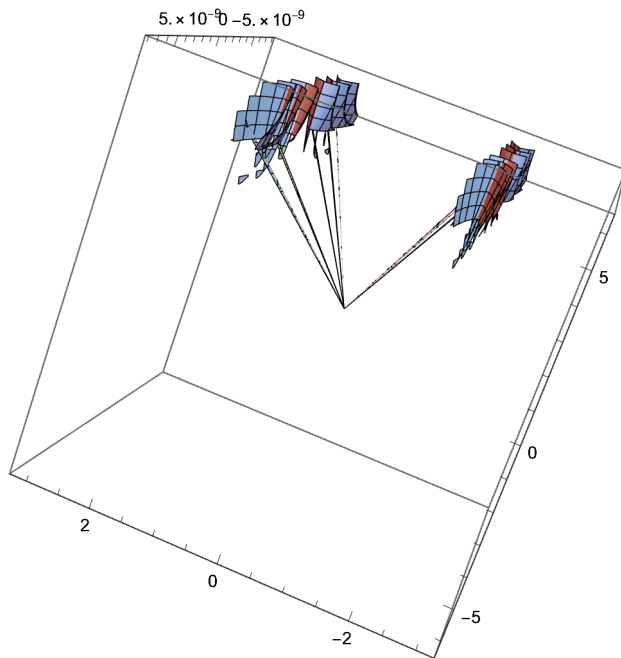
$$\left\{\left\{r \rightarrow -\frac{\sqrt{-c^2 - c^2 \sqrt{1 - \text{Sin}[\beta]^2}}}{\sqrt{-1 + \sqrt{1 - \text{Sin}[\beta]^2}}}\right\}, \left\{r \rightarrow \frac{\sqrt{-c^2 - c^2 \sqrt{1 - \text{Sin}[\beta]^2}}}{\sqrt{-1 + \sqrt{1 - \text{Sin}[\beta]^2}}}\right\}\right\}$$

$$\text{ContourPlot3D}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)^2}}{2 \pi} \left(\frac{1}{\left(\frac{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}{2 \pi}\right)}\right), \right.$$

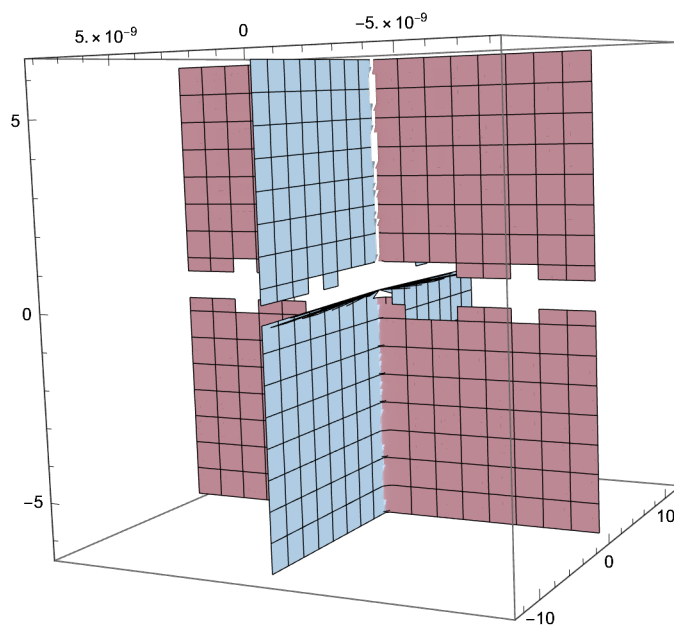
$$\left.\{r, -(8 * (10^9)), (8 * (10^9))\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$$



$\text{ContourPlot3D}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2\pi} \left(\frac{1}{\left(\frac{\theta}{2\pi}\right)}\right), \{r, -(8 \times 10^{-9}), (8 \times 10^{-9})\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}\right]$



$\text{ContourPlot3D}\left[\lambda \left(\frac{1}{\left(\frac{\theta}{k}\right)}\right), \{\lambda, -(8 \times 10^{-9}), (8 \times 10^{-9})\}, \{\theta, -2\pi, 2\pi\}, \{k, -4\pi, 4\pi\}\right]$



$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left(\frac{1}{\left(\frac{\theta}{k}\right)}\right) == c, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{4 k^2 \pi r^2}{4 c^2 \pi^2 + k^2 r^2}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left(\frac{1}{\left(\frac{\theta}{(2 \pi)}\right)}\right) == c, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{4 \pi r^2}{c^2 + r^2}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left(\frac{1}{\left(\frac{\theta}{k}\right)}\right) == c, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right\}, \left\{r \rightarrow \frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left(\frac{1}{\left(\frac{\theta}{(2 \pi)}\right)}\right) == c, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}, \left\{r \rightarrow \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} == \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -1.88365 \times 10^9\right\}, \left\{\theta \rightarrow 0.\right\}\right\}$$

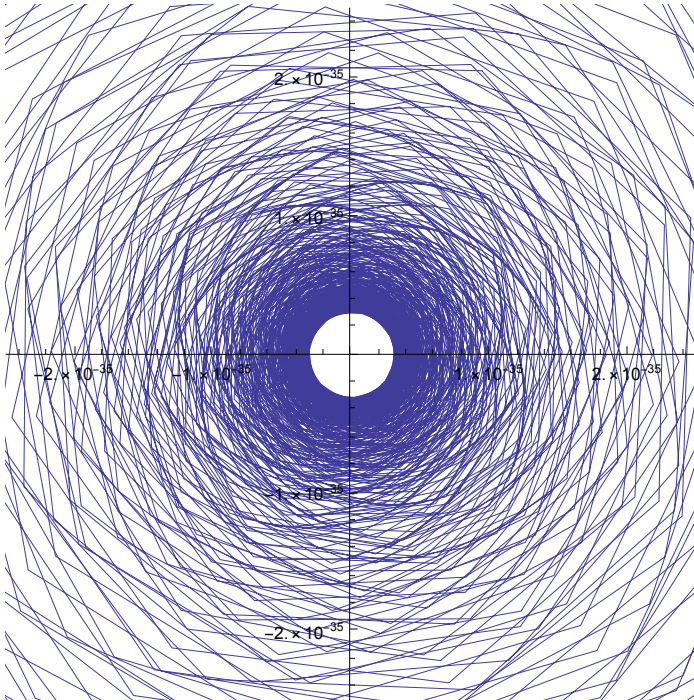
$$9.28 * 180 / \pi$$

$$531.705$$

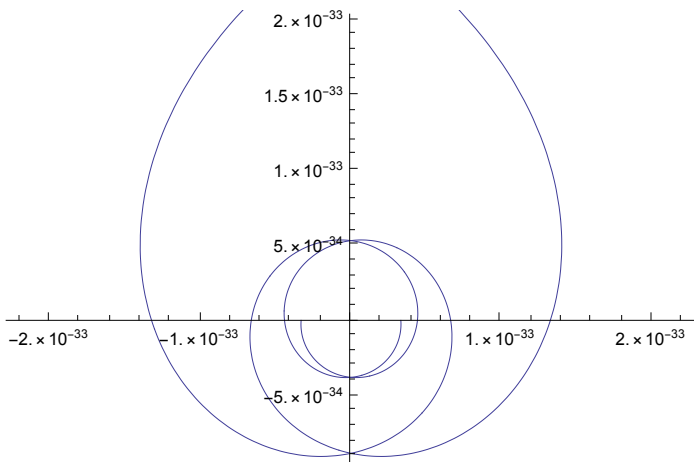
$$E = h \nu = h \frac{1}{\frac{4 k^2 \pi r^2}{4 c^2 \pi^2 + k^2 r^2}} = \frac{h (4 c^2 \pi^2 + k^2 r^2)}{4 k^2 \pi r^2} = \frac{h (4 k^2 \pi - k^2 \theta) \left(4 c^2 \pi^2 + \frac{4 c^2 k^2 \pi^2 \theta}{4 k^2 \pi - k^2 \theta}\right)}{16 c^2 k^2 \pi^3 \theta},$$

$$\text{and when } k = 2 \pi, E = \frac{h}{\frac{\left(\frac{4 \pi r^2}{c^2 + r^2}\right)}{2 \pi}} = \frac{h (c^2 + r^2)}{2 r^2} = \frac{h \left(c^2 + \left(\frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2\right)}{2 \left(\frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2} = \frac{h (4 \pi - \theta) \left(c^2 + \frac{c^2 \theta}{4 \pi - \theta}\right)}{2 c^2 \theta}$$

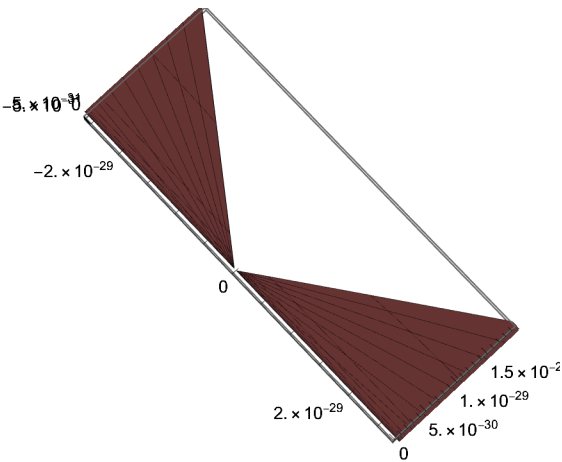
$$\text{PolarPlot}\left[\frac{h\left(c^2 + \left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2}, \{\theta, -400\pi, 400\pi\}\right]$$



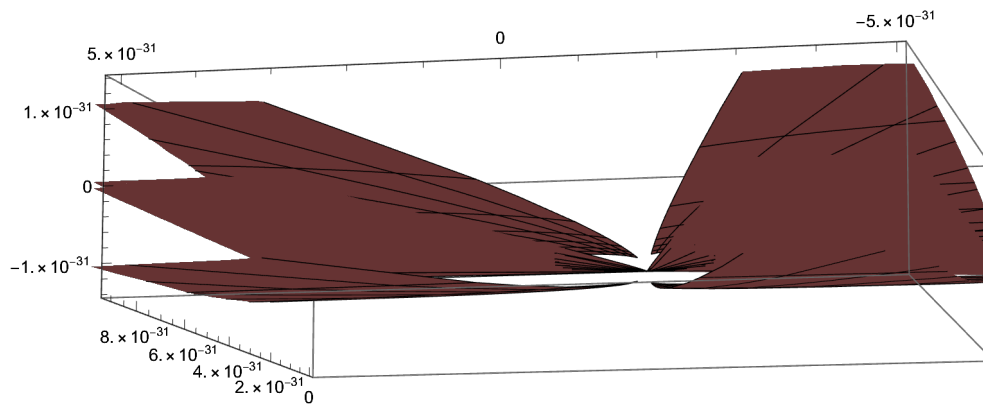
$$\text{PolarPlot}\left[\frac{h(4\pi - \theta)\left(c^2 + \frac{c^2\theta}{4\pi - \theta}\right)}{2c^2\theta}, \{\theta, -4\pi, 4\pi\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{h\left(c^2+\left(\frac{\sqrt{-c^2-c^2}\sqrt{1-\text{Sin}[\beta]^2}}{\sqrt{-1+\sqrt{1-\text{Sin}[\beta]^2}}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2},\{\theta,-.2\pi,.2\pi\},\{\beta,-.1\pi,.1\pi\}\right]$$

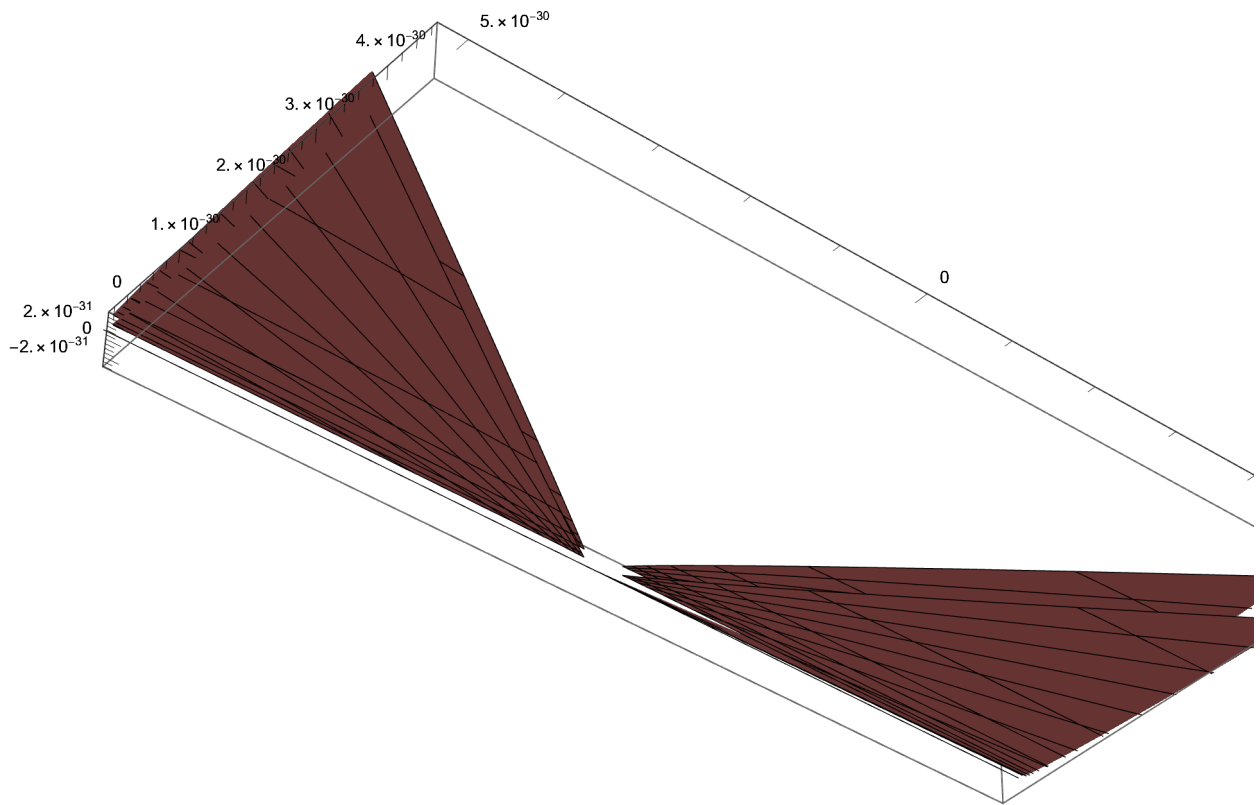


$$\text{SphericalPlot3D}\left[\left\{\frac{h\left(c^2+\left(\frac{\sqrt{-c^2-c^2}\sqrt{1-\text{Sin}[\beta]^2}}{\sqrt{-1+\sqrt{1-\text{Sin}[\beta]^2}}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2},\frac{h\left(c^2+\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2}\text{Sin}[\beta]^2\right)}}\right)^2\right)}{2\left(\frac{c\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2}\text{Sin}[\beta]^2\right)}}{\sqrt{4\pi-\theta}}\right)^2}\right\},\right. \\ \left.\{\theta,-.4\pi,.4\pi\},\{\beta,-.2\pi,.2\pi\}\right]$$

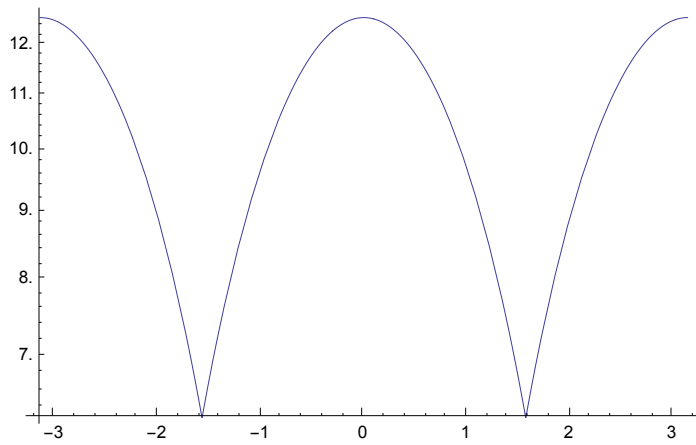




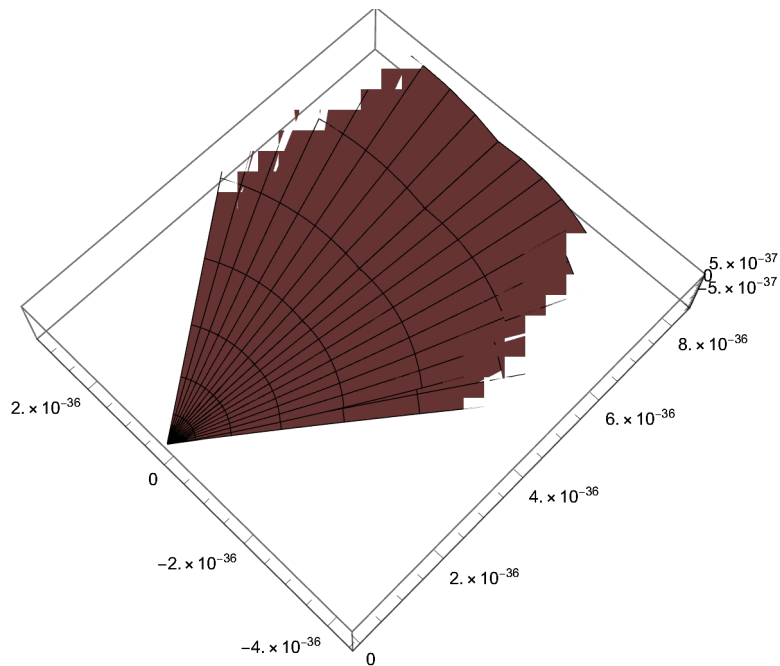
$$\text{SphericalPlot3D}\left[\left\{\frac{h\left(c^2+\left(\frac{\sqrt{-c^2-c^2}\sqrt{1-\text{Sin}[\beta]^2}}{\sqrt{-1+\sqrt{1-\text{Sin}[\beta]^2}}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2},\frac{h\left(c^2+\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}[\beta]^2}\right)}}\right)^2}\right\},\right. \\ \left.\{\theta,-.2\pi,.2\pi\},\{\beta,-.1\pi,.1\pi\}\right]$$



`LogPlot` $\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right), \{\beta, -\pi, \pi\}\right]$



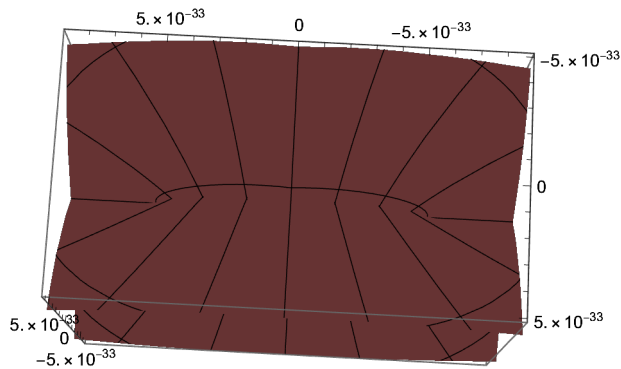
`SphericalPlot3D` $\left[\frac{h \left(c^2 + \left(\frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2\right)}{2 \left(\frac{\sqrt{-c^2 - c^2 \sqrt{1 - \text{Sin}[\beta]^2}}}{\sqrt{-1 + \sqrt{1 - \text{Sin}[\beta]^2}}}\right)^2}, \{\theta, -.2 \pi, .2 \pi\}, \{\beta, -.1 \pi, .1 \pi\}\right]$



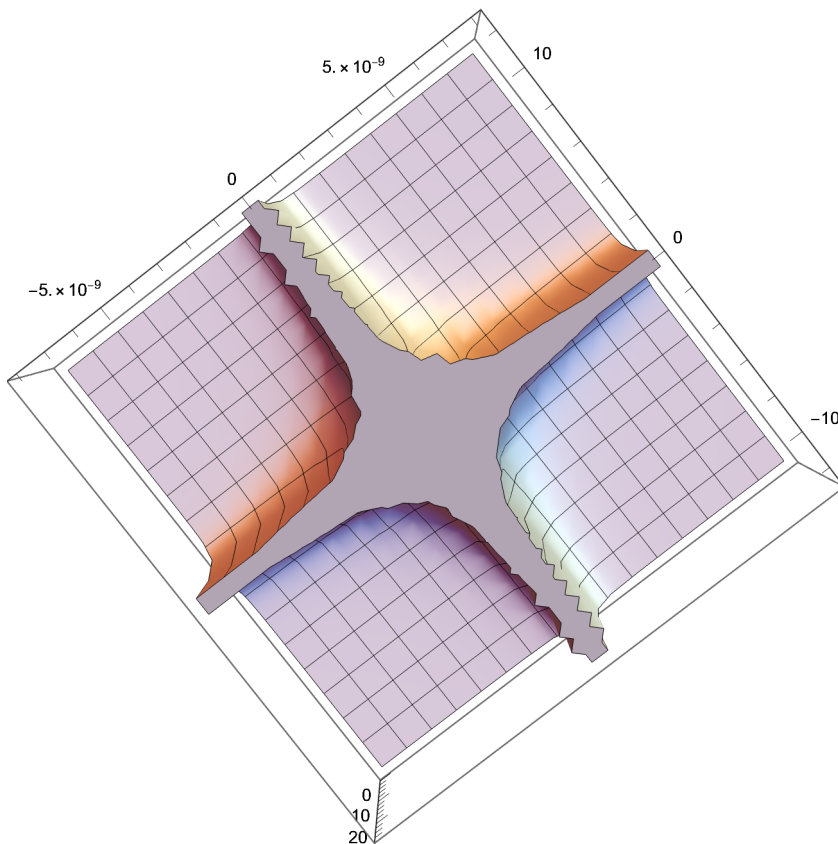
`c := (2.99792458 * 10^8)`

`h := (6.62606896 * (10^-34))`

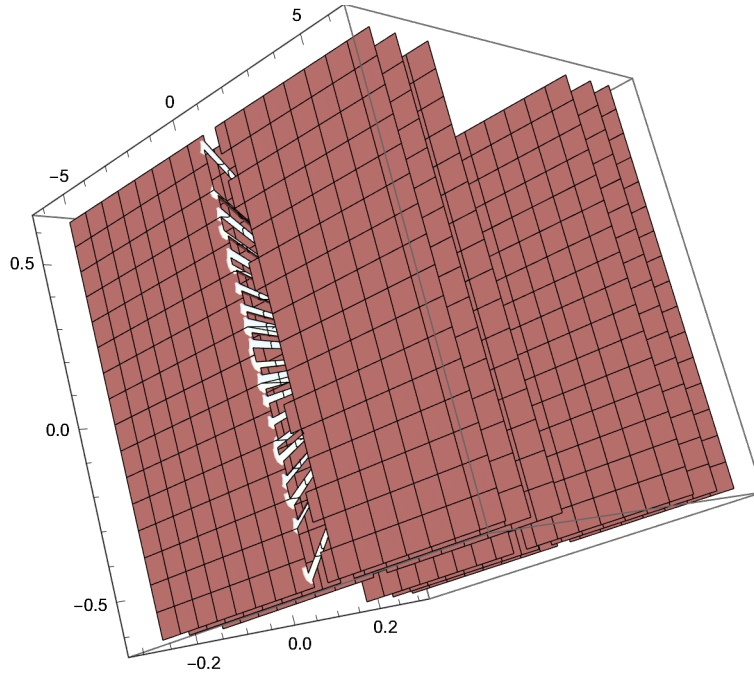
$$\text{SphericalPlot3D}\left[\frac{h(4\pi - \theta)\left(c^2 + \frac{c^2 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{4\pi - \theta}\right)}{2c^2\theta}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$$



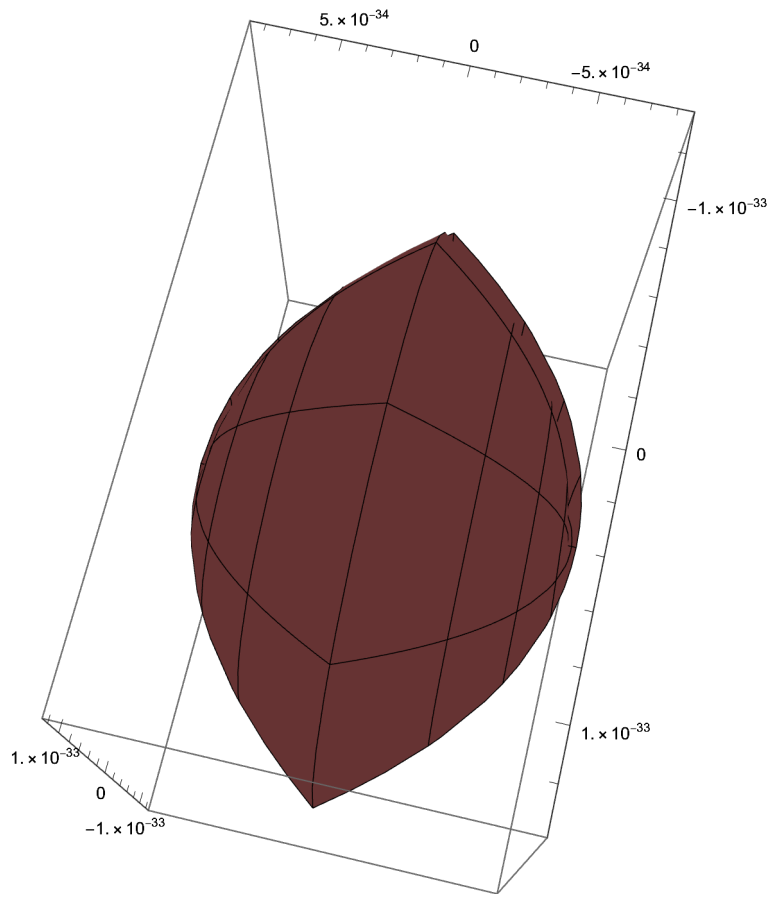
$$\text{Plot3D}\left[\frac{h(4c^2\pi^2 + k^2r^2)}{4k^2\pi r^2}, \{r, -(8 \times 10^{-9}), (8 \times 10^{-9})\}, \{k, -4\pi, 4\pi\}\right]$$



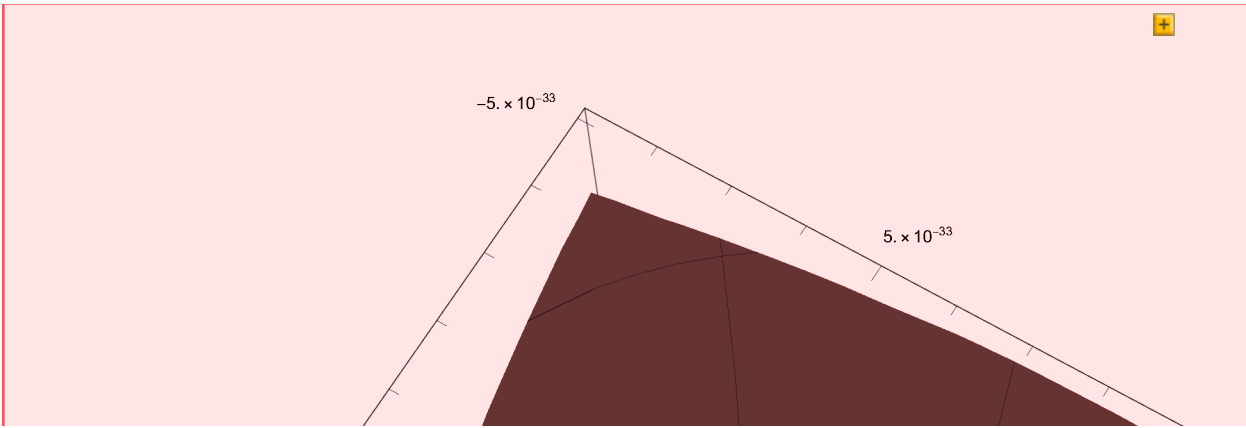
`ContourPlot3D`  $\left[ \frac{h \left( 4 k^2 \pi - k^2 \theta \right) \left( 4 c^2 \pi^2 + \frac{4 c^2 k^2 \pi^2 \theta}{4 k^2 \pi - k^2 \theta} \right)}{16 c^2 k^2 \pi^3 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)}, \right.$   
 $\left. \{\beta, -.1 \pi, .1 \pi\}, \{\theta, -.2 \pi, .2 \pi\}, \{k, -2 \pi, 2 \pi\} \right]$

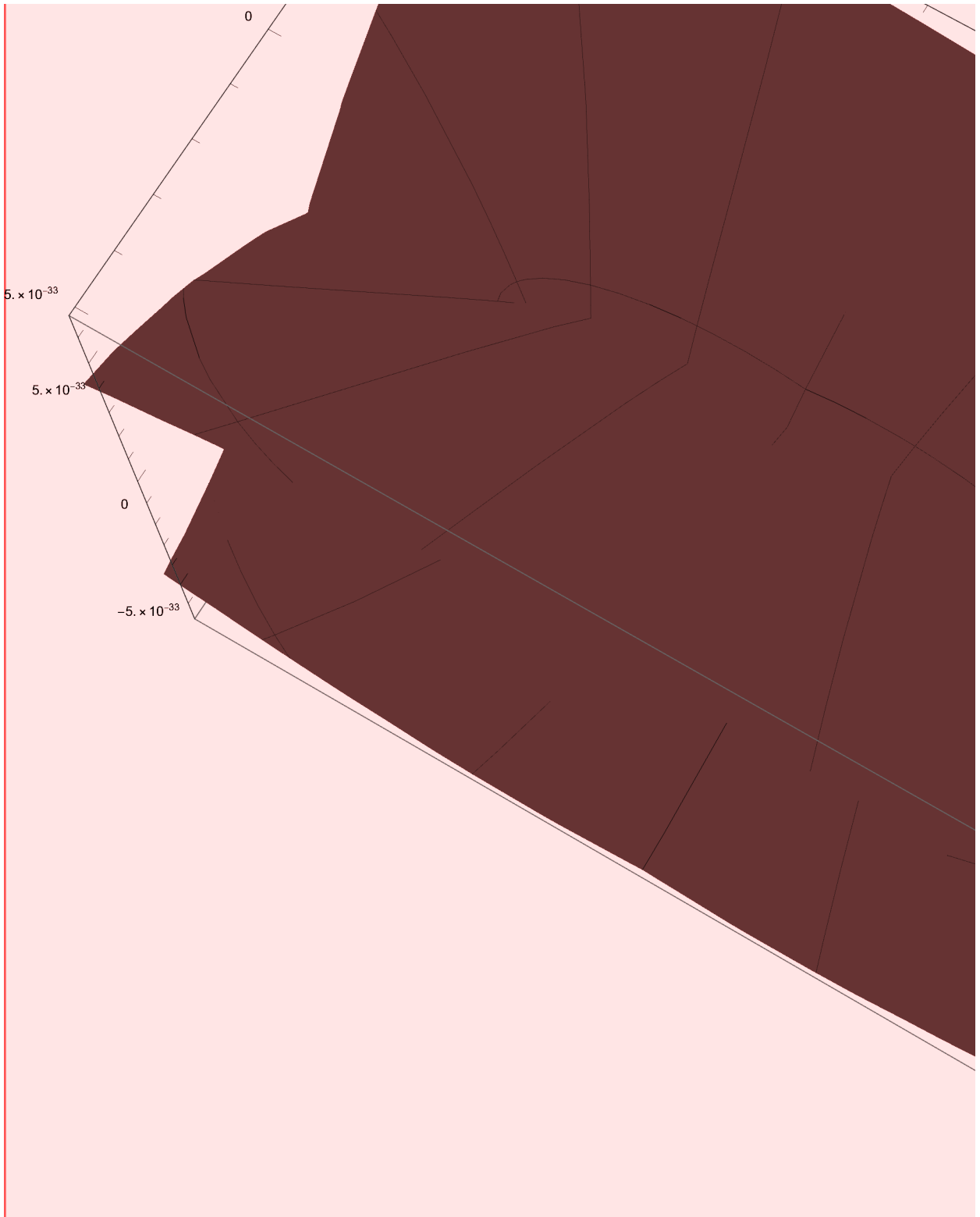


$$\text{SphericalPlot3D}\left[\frac{h\left(c^2+\left(\frac{c\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{\sqrt{4\pi-\theta}}\right)^2\right)}{2\left(\frac{c\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{\sqrt{4\pi-\theta}}\right)^2},\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$$

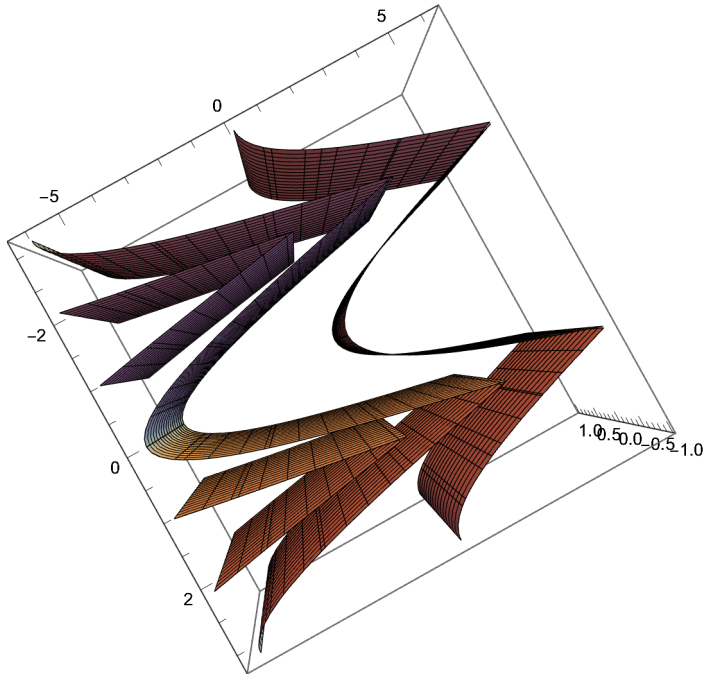


$$\text{SphericalPlot3D}\left[\frac{h\left(c^2+\left(\frac{c\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{\sqrt{4\pi-\theta}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2},\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$$

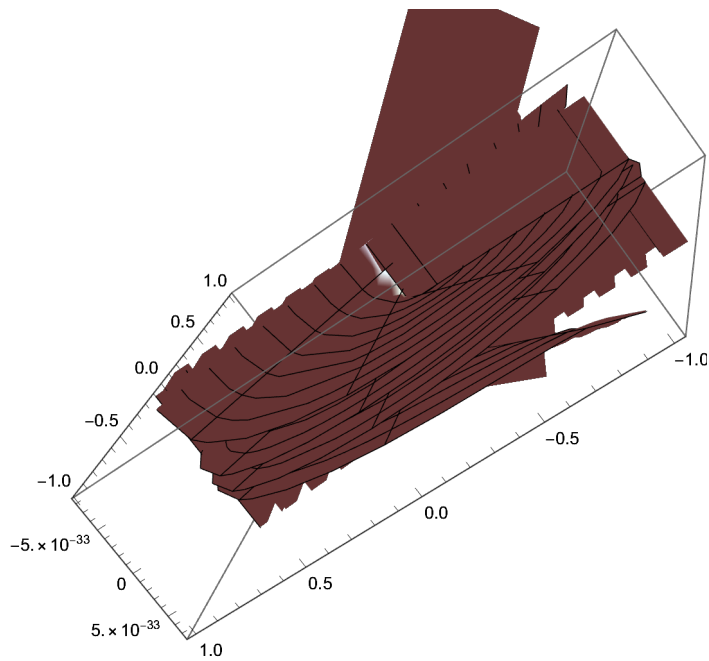




ContourPlot3D $\left[\frac{h\left(c^2+r^2\right)}{2\left(\frac{c\sqrt{2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{\sqrt{4\pi-\theta}}\right)^2},\{r,-1,1\},\{\theta,-2\pi,2\pi\},\{\beta,-\pi,\pi\}\right]$

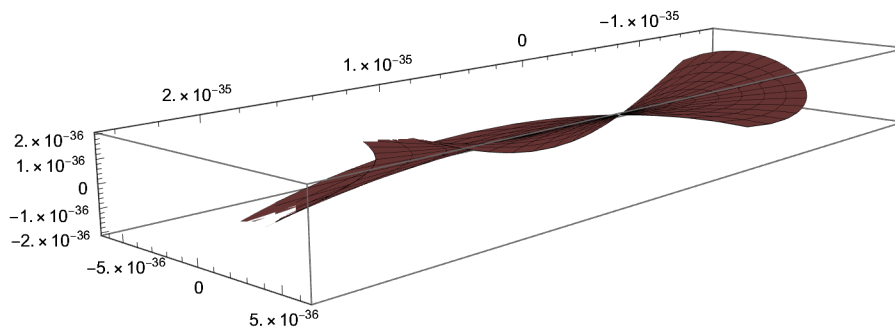


RevolutionPlot3D $\left[\frac{h\left(c^2+r^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2},\{r,-1,1\},\{\theta,-2\pi,2\pi\}\right]$



$$\text{SphericalPlot3D}\left[\frac{h\left(4\pi - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)\right)\left(c^2 + \frac{c^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}{4\pi - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}\right)}{2c^2(\theta)}, \{\beta, -.1\pi, .1\pi\}, \{\theta, -.2\pi, .2\pi\}\right]$$

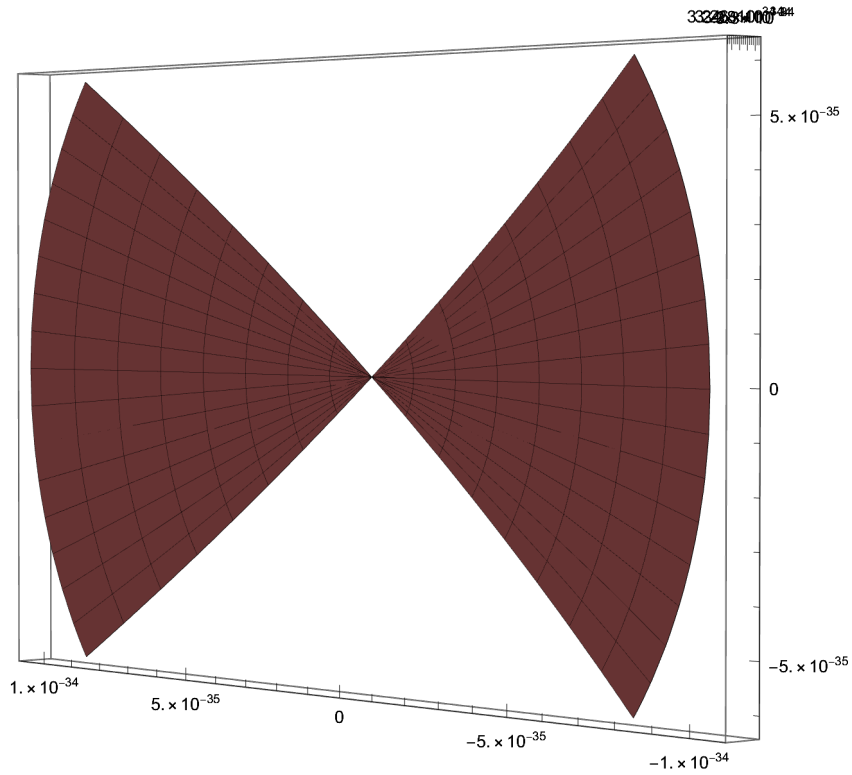
$$\text{SphericalPlot3D}\left[\frac{h\left(4\pi - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)\right)\left(c^2 + \frac{c^2\theta}{4\pi - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}\right)}{2c^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}, \{\beta, -.1\pi, .1\pi\}, \{\theta, -.2\pi, .2\pi\}\right]$$



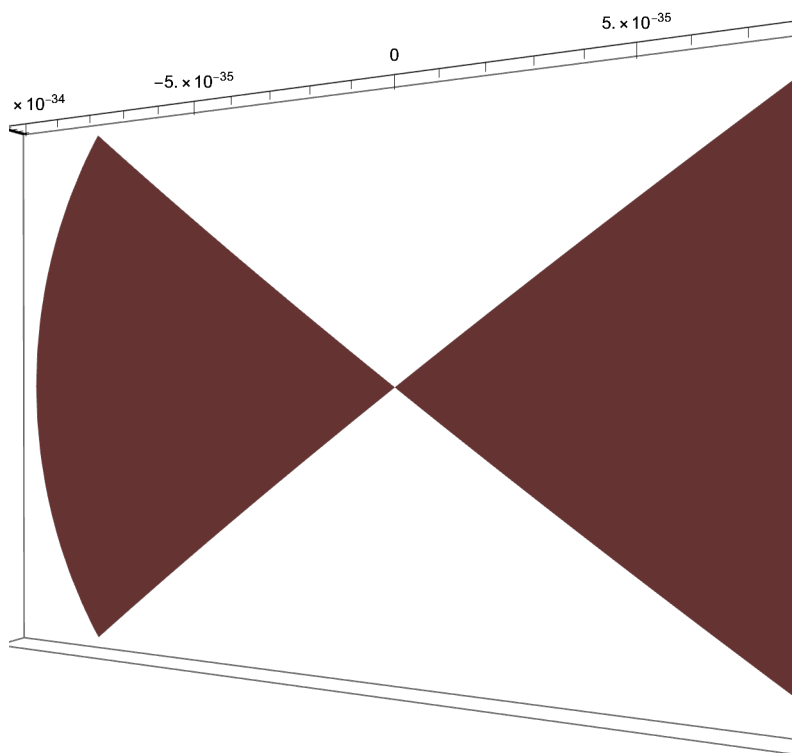


This piece is made entirely of lines,  
 as are all the pieces of this section. We experience both actual and virtual contour in  
 this diagram. This comes from the meshing of individual lines and the foreshortening  
 of their contextual meaning to the space through being placed at different depths  
 and different angles. Because of the individual foreshortening of each line,  
 we are capable of detecting the non-rigid gradient when the object rotates,  
 or when we rotate with regard to the object. The object of perception in  
 this situation is a graphing of a single wavelength of external stimulus  
 energy (radiant energy, i.e. light). The idea of compression allows us  
 to understand the meaning of the perceived creases created from darker,  
 denser areas of the gradient. The relationship between the external stimulus energy and  
 the perceived non-rigid motion through visualizing this stimulus energy existing  
 objectively in space through the angular transition of  $\beta$  and  $\theta$  elucidates how  
 actual contour is perceived through the combination of individual stimuli on the  
 retina. In relation to the more straightforward example of perceiving rigid motion,  
 Gibson has said that, "In general, the greater the slant of a physical surface  
 the steeper will be all of these retinal gradients, and the steeper  
 they are, we may postulate, the greater will be the impression of slant"  
 (The Visual World, 174). It could also be noted that gradients of shading  
 yield the illusion of depth on two dimensional depictions. We can  
 also tell that there is three dimensional information of depth  
 within a single external stimuli (wavelength of light). With  
 actual three dimensional visualizations of radiant energy,  
 we find that the idea of illusory contour is extremely important,  
 and that the idea of a projective plane can be defined by the inherent  
 structure of light stimulus. That in essence, the absence of line is  
 the positive presence of depth perception. Gibson has also noted that,  
 "The illumination of a given surface, then, is a function of the  
 orientation of the surface toward or away from the source of light"  
 (The Visual World, 94). This suggests that an object has a real contour,  
 but if all the information received by the visual system  
 alone is delivered through virtual contour,  
 we cannot say that anything but virtual contour is actually perceived.

$$\text{SphericalPlot3D}\left[\frac{h(4\pi - \theta)\left(c^2 + \frac{c^2\theta}{4\pi - \theta}\right)}{2c^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)}, \{\beta, -.1\pi, .1\pi\}, \{\theta, -.2\pi, .2\pi\}\right]$$

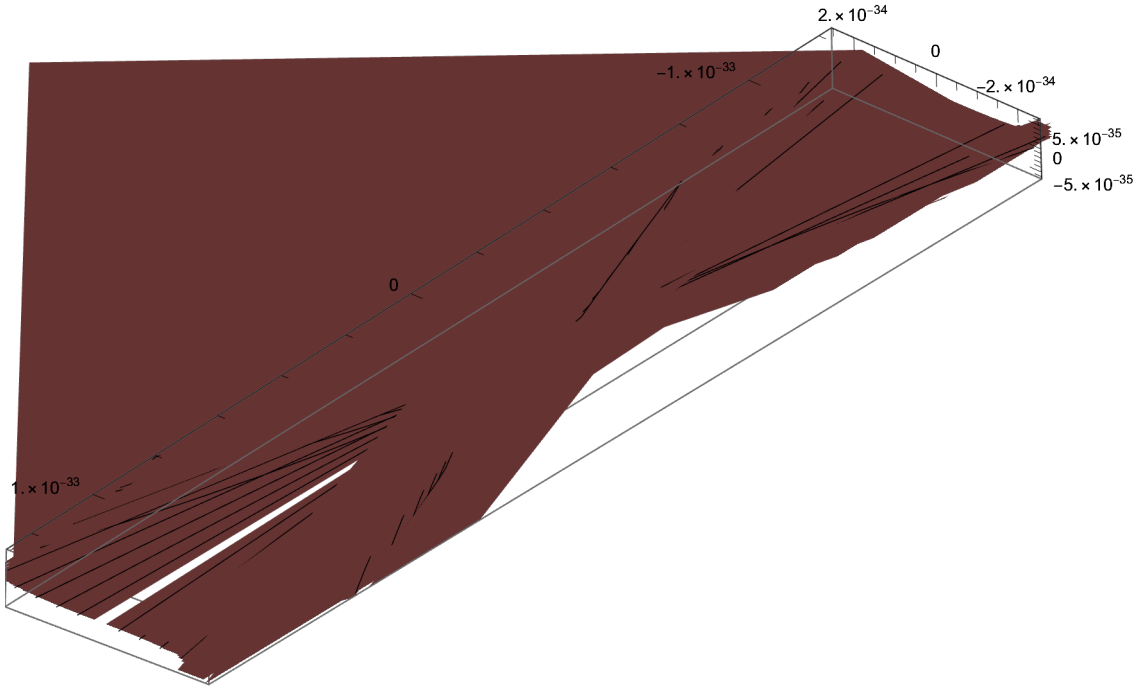


`SphericalPlot3D` $\left[\frac{h(4\pi - \theta)\left(c^2 + \frac{c^2\theta}{4\pi - \theta}\right)}{2c^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)}, \{\beta, -.1\pi, .1\pi\}, \{\theta, -.2\pi, .2\pi\}\right]$



SphericalPlot3D $\left[\frac{h \left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) \left(c^2 + \frac{c^2 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4 \pi - \theta}\right)}{2 c^2 \theta}, \right.$

$\{\beta, -.1 \pi, .1 \pi\}, \{\theta, -.2 \pi, .2 \pi\}]$



Solve $\left[\frac{h \left(4 \pi - \theta\right) \left(c^2 + \frac{c^2 \theta}{4 \pi - \theta}\right)}{2 c^2 \theta} == m c^2, m\right]$

$\left\{\left\{m \rightarrow \frac{2 h \pi}{c^2 \theta}\right\}\right\}$

Solve $\left[\frac{h \left(c^2 + r^2\right)}{2 r^2} == m c^2, m\right]$

$\left\{\left\{m \rightarrow \frac{h \left(c^2 + r^2\right)}{2 c^2 r^2}\right\}\right\}$

Solve $\left[\frac{h \left(4 c^2 \pi^2 + k^2 r^2\right)}{4 k^2 \pi r^2} == m c^2, m\right]$

$\left\{\left\{m \rightarrow \frac{h \left(4 c^2 \pi^2 + k^2 r^2\right)}{4 c^2 k^2 \pi r^2}\right\}\right\}$

$$\text{Solve}\left[\frac{h(c^2 + r^2)}{2c^2 r^2} == \frac{2h\pi}{c^2 \theta}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{c\sqrt{\theta}}{\sqrt{4\pi - \theta}}\right\}, \left\{r \rightarrow \frac{c\sqrt{\theta}}{\sqrt{4\pi - \theta}}\right\}\right\}$$

$$r = \frac{\sqrt{-c^2 - c^2 \sqrt{1 - \sin[\beta]^2}}}{\sqrt{-1 + \sqrt{1 - \sin[\beta]^2}}} = \frac{2c\pi\sqrt{\theta}}{\sqrt{4k^2\pi - k^2\theta}}$$

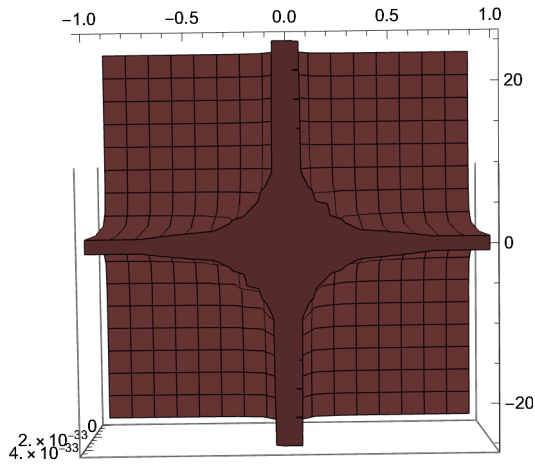
$$\text{Solve}\left[\frac{h\left(4c^2\pi^2 + k^2\left(\frac{2c\pi\sqrt{\theta}}{\sqrt{4k^2\pi - k^2\theta}}\right)^2\right)}{4k^2\pi\left(\frac{2c\pi\sqrt{\theta}}{\sqrt{4k^2\pi - k^2\theta}}\right)^2} == mc^2, m\right]$$

$$\left\{\left\{m \rightarrow \frac{h}{c^2\theta}\right\}\right\}$$

$$\text{Solve}\left[\frac{h(4c^2\pi^2 + k^2r^2)}{4c^2k^2\pi r^2} c^2 == mc^2, m\right]$$

$$\left\{\left\{m \rightarrow \frac{h(4c^2\pi^2 + k^2r^2)}{4c^2k^2\pi r^2}\right\}\right\}$$

$$\text{Plot3D}\left[\frac{h(4c^2\pi^2 + k^2r^2)}{4c^2k^2\pi r^2}, \{r, -1, 1\}, \{k, -8\pi, 8\pi\}\right]$$



**c := 2.99792458 \* 10^8**

**h := (6.62606896 \* (10^-34))**

$$\text{Solve}\left[\frac{h(c^2 + r^2)}{2c^2 r^2} c^2 == mc^2, m\right]$$

$$\left\{\left\{m \rightarrow \frac{h(c^2 + r^2)}{2c^2 r^2}\right\}\right\}$$

$$\text{Solve}\left[\frac{2h\pi}{c^2 \theta} == mc^2, m\right]$$

$$\left\{\left\{m \rightarrow \frac{2h\pi}{c^4 \theta}\right\}\right\}$$

$$h\nu = h(1/(\theta/k)) = mc^2 = \frac{h}{c^2 \theta} c^2 = \frac{h(4c^2 \pi^2 + k^2 r^2)}{4c^2 k^2 \pi r^2} c^2 = \frac{h(c^2 + r^2)}{2c^2 r^2} c^2 = \frac{2h\pi}{c^2 \theta}$$

$$\text{Solve}\left[\frac{2h\pi}{c^2 \theta} == h(1/(\theta/k)), r\right]$$

$$\{\{\}\}$$

$$\text{Solve}\left[\frac{2h\pi}{c^2 \theta} == h(1/(\theta/k)), \theta\right]$$

$$\{\{\}\}$$

$$\text{Solve}\left[\frac{2h\pi}{c^2 \theta} == h(1/(\theta/k)), k\right]$$

$$\left\{\left\{k \rightarrow \frac{2\pi}{c^2}\right\}\right\}$$

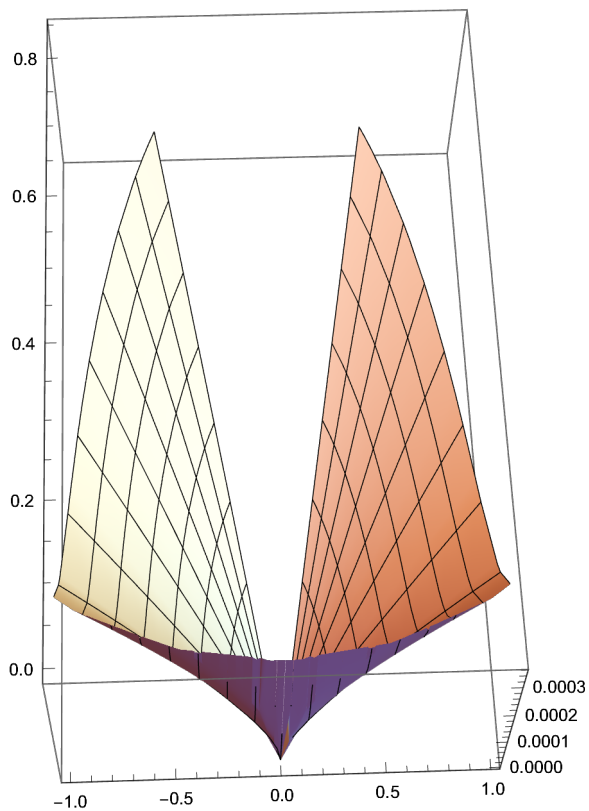
$$\eta == c \left( \frac{\theta}{\frac{2\pi}{c^2}} \right) =$$

$$c \left( \frac{\frac{2kr^2}{c^2 + r^2}}{\frac{2\pi}{c^2}} \right) = c \left( \frac{\frac{4k^3 \pi r^2}{4c^2 \pi^2 + k^2 r^2}}{\frac{2\pi}{c^2}} \right) = c \left( \frac{\frac{2kr^2}{c^2(c^2 + r^2)}}{\frac{2\pi}{c^2}} \right) = c \left( \frac{2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{\frac{2\pi}{c^2}} \right) = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$\text{Solve}\left[\eta == c \left( \frac{2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{\frac{2\pi}{c^2}} \right), \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\sqrt{\frac{(2c^3 - \eta)\eta}{c^6}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\sqrt{\frac{(2c^3 - \eta)\eta}{c^6}}\right]\right\}\right\}$$

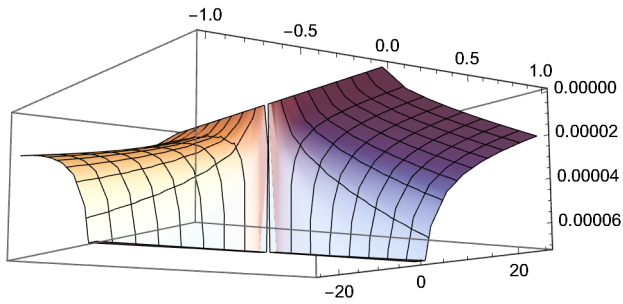
$\text{RevolutionPlot3D}\left[\frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c^3 k - \pi \eta}}, \{\eta, -1, 1\}, \{k, -1, 1\}\right]$



$\text{Solve}\left[\eta == c \left( \frac{2 k r^2}{c^2 + r^2} \right), r\right]$

$\left\{ \left\{ r \rightarrow -\frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c^3 k - \pi \eta}} \right\}, \left\{ r \rightarrow \frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c^3 k - \pi \eta}} \right\} \right\}$

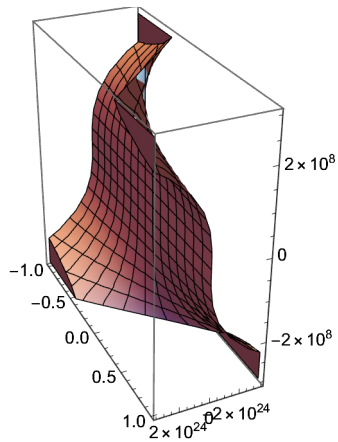
$\text{Plot3D}\left[\frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c^3 k - \pi \eta}}, \{\eta, -1, 1\}, \{k, -8 \pi, 8 \pi\}\right]$



$\text{Solve}\left[\frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c^3 k - \pi \eta}} == \frac{2 c \pi \sqrt{\eta}}{\sqrt{2 c^3 k^3 - k^2 \eta}}, \eta\right]$

$\left\{\left\{\eta \rightarrow 0\right\}, \left\{\eta \rightarrow \frac{2\left(c^3 k^3 - 2 c^3 k \pi\right)}{k^2 - 4 \pi^2}\right\}\right\}$

$\text{Plot3D}\left[\frac{2\left(c^3 k^3 - 2 c^3 k \pi\right)}{k^2 - 4 \pi^2}, \{k, -1, 1\}, \{c, -2.99792458 * 10^8, 2.99792458 * 10^8\}\right]$

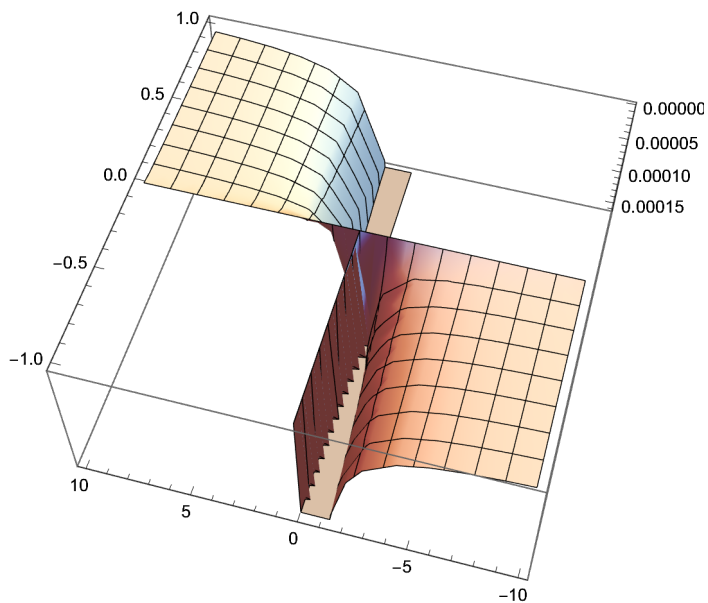


$\text{Solve}\left[\eta == c \left(\frac{\frac{4 k^3 \pi r^2}{4 c^2 \pi^2 + k^2 r^2}}{\frac{2 \pi}{c^2}}\right), r\right]$

$\left\{\left\{r \rightarrow -\frac{2 c \pi \sqrt{\eta}}{\sqrt{2 c^3 k^3 - k^2 \eta}}\right\}, \left\{r \rightarrow \frac{2 c \pi \sqrt{\eta}}{\sqrt{2 c^3 k^3 - k^2 \eta}}\right\}\right\}$



`Plot3D` $\left[\frac{2 c \pi \sqrt{\eta}}{\sqrt{2 c^3 k^3 - k^2 \eta}}, \{k, -10, 10\}, \{\eta, -1, 1\}\right]$



`Solve` $\left[\eta == c \left( \frac{\frac{2 k r^2}{c^2 (c^2 + r^2)}}{\frac{2 \pi}{c^2}} \right), r\right]$

$\left\{ \left\{ r \rightarrow -\frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c k - \pi \eta}} \right\}, \left\{ r \rightarrow \frac{c \sqrt{\pi} \sqrt{\eta}}{\sqrt{c k - \pi \eta}} \right\} \right\}$

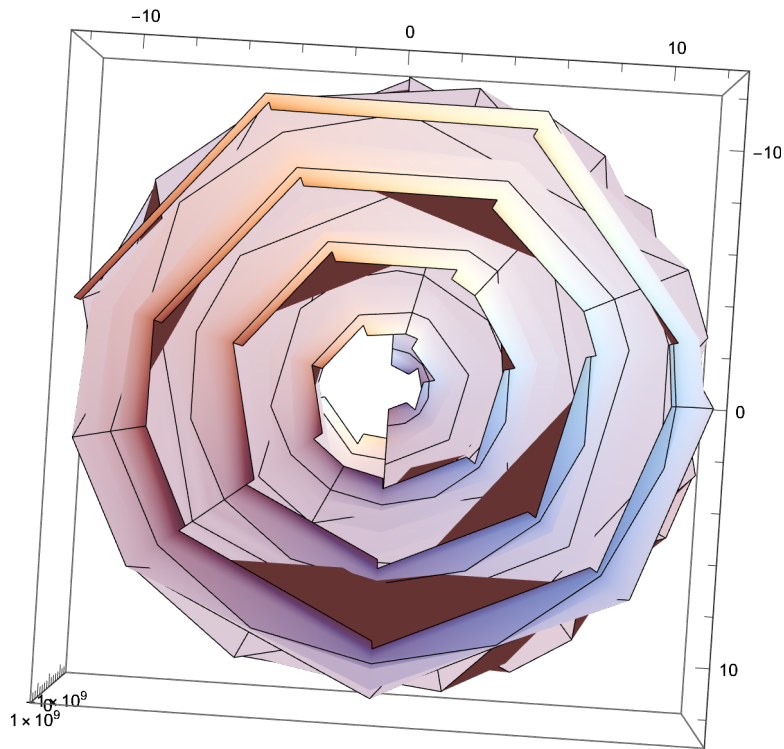
`Solve` $\left[\eta == c \left( \frac{\theta}{\frac{2 \pi}{c^2}} \right), \theta\right]$

$\left\{ \left\{ \theta \rightarrow \frac{2 \pi \eta}{c^3} \right\} \right\}$

`Solve` $\left[\frac{h (c^2 + r^2)}{2 c^2 r^2} c^{\wedge} 2 == h (1 / (\theta / k)), r\right]$

$\left\{ \left\{ r \rightarrow -\frac{i c \sqrt{\theta}}{\sqrt{-2 k + \theta}} \right\}, \left\{ r \rightarrow \frac{i c \sqrt{\theta}}{\sqrt{-2 k + \theta}} \right\} \right\}$

RevolutionPlot3D $\left[\frac{i c \sqrt{\theta}}{\sqrt{-2 k+\theta}},\{k,-4 \pi, 4 \pi\},\{\theta,-8 \pi, 8 \pi\}\right]$



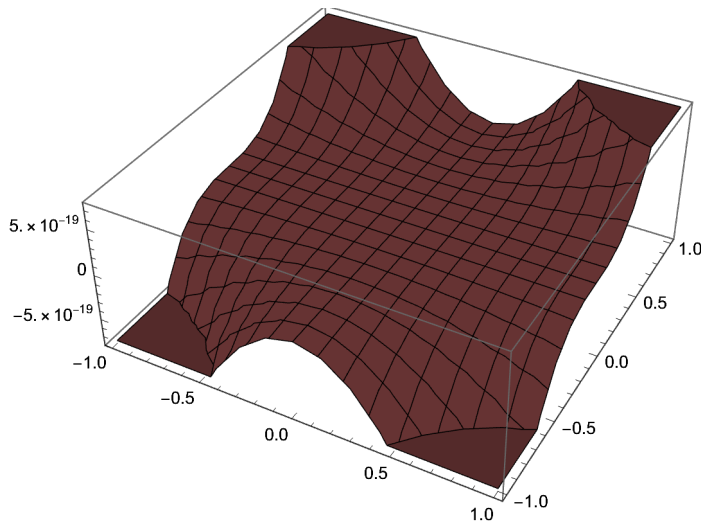
Solve $\left[\frac{h\left(c^2+r^2\right)}{2 c^2 r^2} c^{\wedge} 2==h\left(1 /\left(\theta / k\right)\right), \theta\right]$

$\left\{\left\{\theta \rightarrow \frac{2 k r^2}{c^2+r^2}\right\}\right\}$

Solve $\left[h\left(1 /\left(\theta / k\right)\right)==\frac{h\left(4 c^2 \pi^2+k^2 r^2\right)}{4 c^2 k^2 \pi r^2} c^{\wedge} 2, \theta\right]$

$\left\{\left\{\theta \rightarrow \frac{4 k^3 \pi r^2}{4 c^2 \pi^2+k^2 r^2}\right\}\right\}$

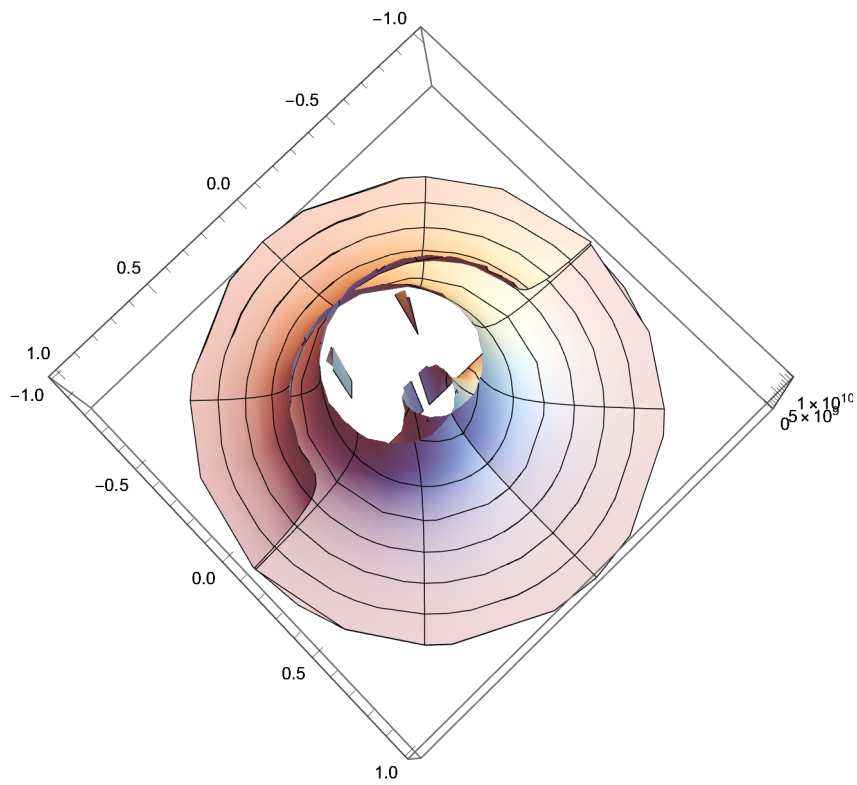
`Plot3D` $\left[\frac{4 k^3 \pi r^2}{4 c^2 \pi^2 + k^2 r^2}, \{r, -1, 1\}, \{k, -1, 1\}\right]$



`Solve` $\left[h(1/(\theta/k)) == \frac{h(4 c^2 \pi^2 + k^2 r^2)}{4 c^2 k^2 \pi r^2} c^2, r\right]$

$\left\{\left\{r \rightarrow -\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^3 \pi - k^2 \theta}}\right\}, \left\{r \rightarrow \frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^3 \pi - k^2 \theta}}\right\}\right\}$

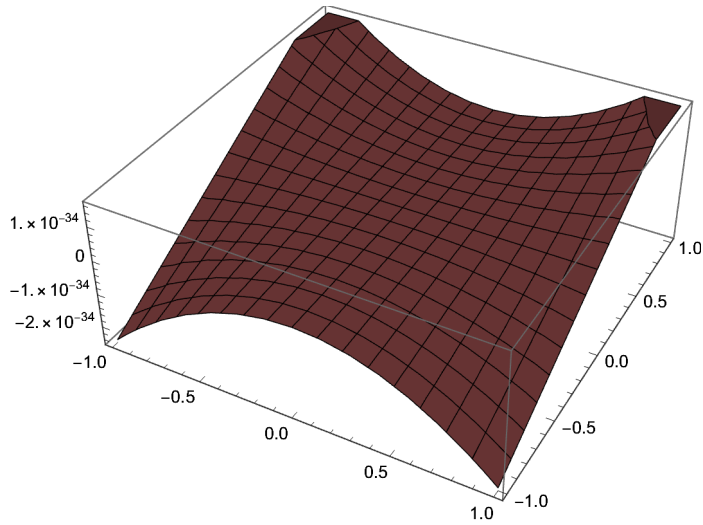
RevolutionPlot3D $\left[\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^3 \pi-k^2 \theta}},\{k,-1,1\},\{\theta,-2 \pi, 2 \pi\}\right]$



Solve $\left[h\left(1 /\left(\theta / k\right)\right)=\frac{h\left(c^2+r^2\right)}{2 c^2 r^2} c^{\wedge} 2 c^{\wedge} 2, \theta\right]$

$\left\{\left\{\theta \rightarrow \frac{2 k r^2}{c^2\left(c^2+r^2\right)}\right\}\right\}$

Plot3D $\left[\frac{2 k r^2}{c^2 (c^2 + r^2)}, \{r, -1, 1\}, \{k, -1, 1\}\right]$



$$\theta = \frac{4 k^2 \pi r^2}{4 c^2 \pi^2 + k^2 r^2} = \frac{4 k^3 \pi r^2}{4 c^2 \pi^2 + k^2 r^2} = \frac{2 k r^2}{c^2 (c^2 + r^2)}$$

Solve $\left[\frac{2 k r^2}{c^2 (c^2 + r^2)} == \frac{4 k^2 \pi r^2}{4 c^2 \pi^2 + k^2 r^2}, r\right]$

$$\left\{\{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{r \rightarrow -\frac{\sqrt{2} \pi \sqrt{-c^4 k + 2 c^2 \pi}}{\sqrt{-k^2 + 2 c^2 k \pi}}\right\}, \left\{r \rightarrow \frac{\sqrt{2} \pi \sqrt{-c^4 k + 2 c^2 \pi}}{\sqrt{-k^2 + 2 c^2 k \pi}}\right\}\right\}$$

r =

Solve $\left[\frac{1}{\theta} == (1 / (\theta / k)), k\right]$

{{k → 1}}

Solve $\left[\frac{\square}{c^2 \theta} c^2 == (1 / (\theta / k)), c\right]$

{{}}

Solve $\left[\frac{h}{c^2 \theta} c^2 == h (1 / (\theta / 2 \pi)), h\right]$

{{h → 0}}

$$\text{Solve}\left[\frac{h \left(4 c^2 \pi^2 + k^2 (r)^2\right)}{4 k^2 \pi \left(\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right)^2} == m c^2, m\right]$$

$$\left\{\left\{m \rightarrow \frac{h \left(4 c^2 \pi^2 + k^2 r^2\right) (4 \pi - \theta)}{16 c^4 \pi^3 \theta}\right\}\right\}$$

$$\text{Solve}\left[\frac{h \left(4 c^2 \pi^2 + k^2 \left(\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right)^2\right)}{4 k^2 \pi r^2} == m c^2, m\right]$$

$$\left\{\left\{m \rightarrow \frac{4 h \pi^2}{k^2 r^2 (4 \pi - \theta)}\right\}\right\}$$

$$\frac{h \left(4 c^2 \pi^2 + k^2 r^2\right)}{4 k^2 \pi r^2} = E$$

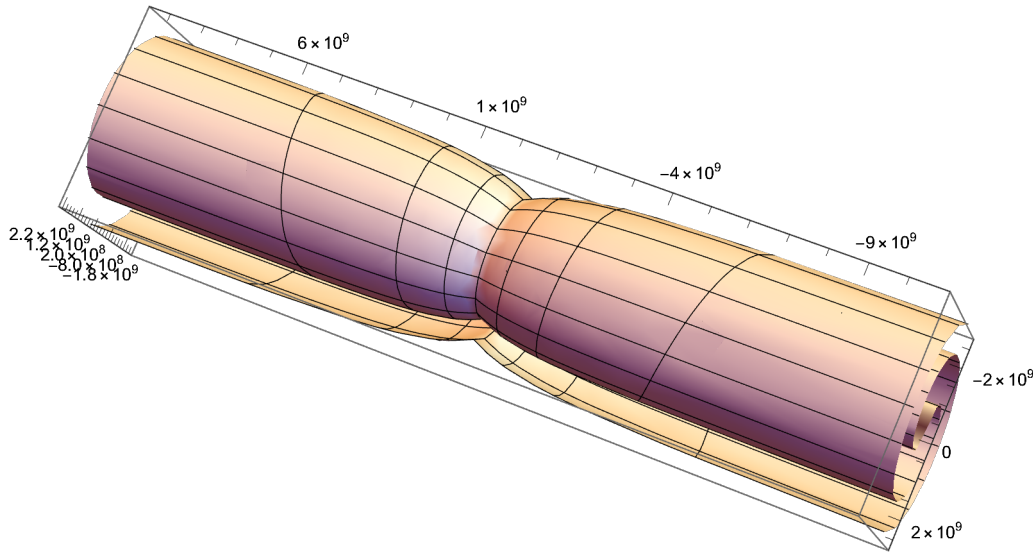
$$\frac{h \left(c^2 + r^2\right)}{2 r^2}$$

$$2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == c (\theta / (k)), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right\}, \left\{r \rightarrow \frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 \times 1^2 \pi - 1^2 \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$\left\{\left\{\theta \rightarrow 0\right\},\left\{\theta \rightarrow \frac{4 \pi r^2}{c^2+r^2}\right\}\right\}$$

$$\text{Solve}\left[\frac{4 \pi r^2}{c^2+r^2}==2\left(\pi+\sqrt{\pi^2-\pi^2 \text{Sin}[\beta]^2}\right), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{-c^2-c^2 \sqrt{1-\text{Sin}[\beta]^2}}}{\sqrt{-1+\sqrt{1-\text{Sin}[\beta]^2}}}\right\},\left\{r \rightarrow \frac{\sqrt{-c^2-c^2 \sqrt{1-\text{Sin}[\beta]^2}}}{\sqrt{-1+\sqrt{1-\text{Sin}[\beta]^2}}}\right\}\right\}$$

## "Conic" Relativity: Expositions of Relativity through Difference in Circumferences of Two Circles

In this paper,

I will perform a "limited" exposition of the general principle,  $\theta r =$

$$2 \pi r - 2 \pi x = 2 \pi r - 2 \pi r' = 2 \pi r - 2 \pi r \sqrt{1 - \frac{(v)^2}{c^2}} = 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2},$$

from the algebraicized geometry of a cone combined with the

relativistic length contraction first suggested by Einstein's application of the Lorentz transformation in his theory of relativity. The exposition is limited. I will only solve equations for expressions of velocity and expressions of angle measure. I will not make substitutions. The system is multi-variant in the sense that there are so many different possible combinations of algebraic forms that one would have to take a very long extended exposition in order to visualize all of them.

"The language of matter expresses the same quality of motion as the meaning of the creative thought/idea field. In order to perceive motion, one must set aside certain quantifiable characteristics of the existence of transformation. This leads to insight into a relationship and mutual interpenetration of mathematics and ethics." - Emerson

For more information about how Einstein applied the Lorentz transformation to describe length contraction, see :

**Einstein, Albert. Relativity : The Special and the General Theory (Classic Reprint). Forgotten Books, 2010. Print.**

This is an original interpretation of the notion of a length contraction as it would relate to the difference in circumferences of two circles.

## Table of Contents :

### 1. Conic Relativity: "General Relativity" Circumferential Cone-Difference Functions

Height of the cone equals

the length contracted initial radius :

$$\eta = r' = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} =$$

$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$2\pi\eta - 2\pi r' = \phi\eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different.

$$2\pi\eta - 2\pi r' = \theta\eta$$

$2\pi r' - 2\pi\eta = \phi\eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but



different. - This section is not visualized in this paper, but implied.

$2 \pi r - 2 \pi \eta = \theta \eta$  - This section will not be visualized in this paper, but is implied.

Changed radius equals the

length contracted initial radius :

$$x = r' = \frac{2 \pi r - r \theta}{2 \pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} =$$

$$\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$2 \pi x - 2 \pi r' = \phi \eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different.

$$2 \pi x - 2 \pi r' = \theta \eta$$

$2 \pi r' - 2 \pi x = \phi \eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different is implied but not visualized in this paper.

$2 \pi r' - 2 \pi x = \phi \eta$  is implied but not visualized in this paper.

Height of the cone equals the

length contracted "changed radius" :  $\eta =$

$$x' = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$2 \pi \eta - 2 \pi x' = \omega \eta$ , where  $\omega$  is an angle of a similar dimensional kind to theta, but different.

Synchronized angles:  $2 \pi \eta - 2 \pi x' = \theta \eta$

Changed radius equals the

length contracted height of the cone :

$$x = \eta' = \frac{2 \pi r - r \theta}{2 \pi} = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$2 \pi x - 2 \pi \eta' = \rho \eta$ , where  $\rho$  is an angle of a similar dimensional kind to theta, but different.

$$2 \pi x - 2 \pi \eta' = \theta \eta$$

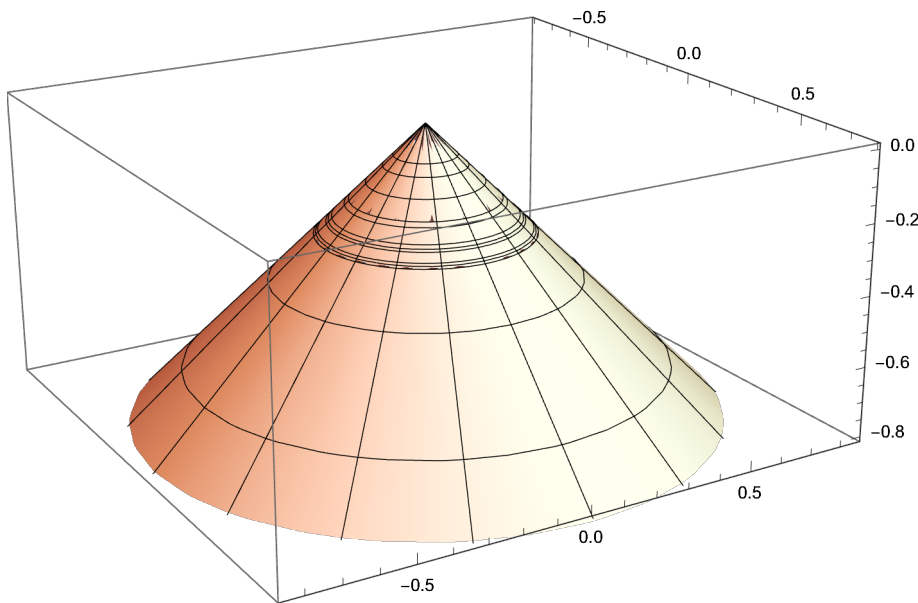
There are also the implied forms :  $\eta' = r$  and  $x' = r$  with their respective

## Commentary on the Forms

One commentary on the forms is their semblance to the position at which the instantaneous rate of change of the height of the cone equals the average rate of change of the height of the cone with respect to theta. Please see A Geometric Pattern of Perception (Emmerson, 2009), for more background information regarding the system of the univocal cone transformation. The six potential equalities of the system wind up miming the 30 - 60 - 90 position at which the instantaneous velocity of the height of the cone equals the average velocity of the height of the cone. When plotted, the 45 - 45 - 90 cone is evident within process of solving for this position.

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\}, \left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\} \right\} \quad (57)$$

RevolutionPlot3D[  
 $\left\{ \text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right], -\text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\}, \{\theta, -4 \pi, 4 \pi\}$



## "General Relativity" Circumferential Cone - Difference Functions

$$\eta = r' = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} =$$

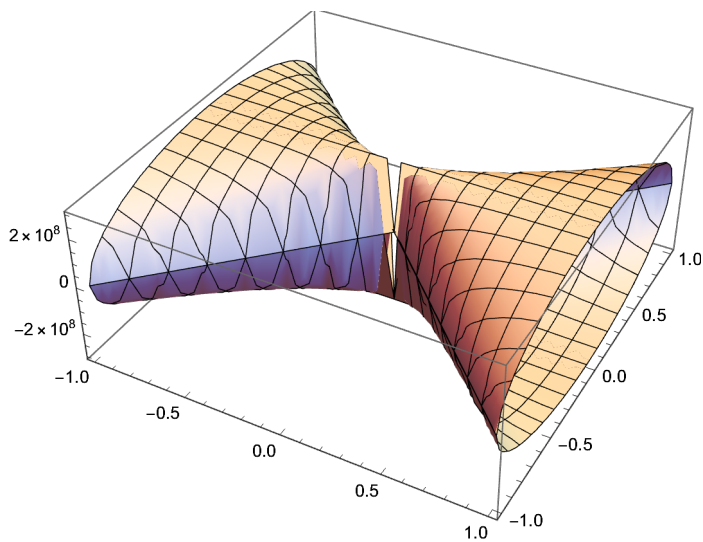
$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$$\text{Solve}\left[\eta == r \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -1. \sqrt{8.98755 \times 10^{16} - \frac{8.98755 \times 10^{16} \eta^2}{r^2}} \right\}, \left\{ v \rightarrow \sqrt{8.98755 \times 10^{16} - \frac{8.98755 \times 10^{16} \eta^2}{r^2}} \right\} \right\}$$

$$\text{Plot3D}\left[\left\{ -1. \sqrt{8.987551787368176 \times 10^{16} - \frac{8.987551787368176 \times 10^{16} \eta^2}{r^2}}, \right. \right.$$

$$\left. \sqrt{8.987551787368176 \times 10^{16} - \frac{8.987551787368176 \times 10^{16} \eta^2}{r^2}} \right\}, \{r, -1, 1\}, \{\eta, -1, 1\}]$$

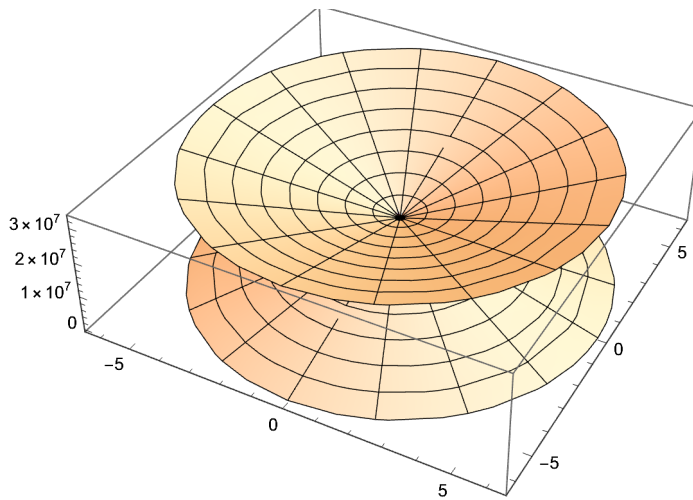


$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == r\sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -1.05839 \times 10^{-7} \sqrt{8.02317 \times 10^{30} - 2.55385 \times 10^{30} \theta + 2.03229 \times 10^{29} \theta^2}\right\},\right. \\ \left.\left\{v \rightarrow 1.05839 \times 10^{-7} \sqrt{8.02317 \times 10^{30} - 2.55385 \times 10^{30} \theta + 2.03229 \times 10^{29} \theta^2}\right\}\right\}$$

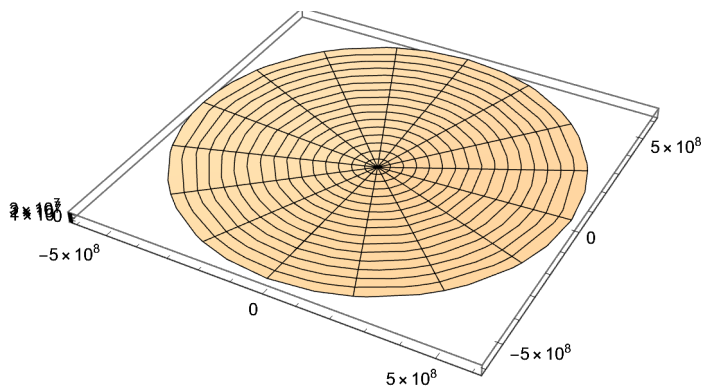
RevolutionPlot3D[.0583947067478751`\*^-7

$\sqrt{(8.02317171945391 \times 10^{30} - 2.5538548768523825 \times 10^{30} \theta + 2.0322931379520014 \times 10^{29} \theta^2)}$ ,  
 $\{\theta, -2\pi, 2\pi\}$ ]



RevolutionPlot3D[{-1.0583947067478751`\*^-7

$\sqrt{(8.02317171945391 \times 10^{30} - 2.5538548768523825 \times 10^{30} \theta + 2.0322931379520014 \times 10^{29} \theta^2)}$ ,  
 $.0583947067478751 \times 10^{-7} \sqrt{(8.02317171945391 \times 10^{30} -$   
 $2.5538548768523825 \times 10^{30} \theta + 2.0322931379520014 \times 10^{29} \theta^2)}$ },  $\{\theta, -2\pi, 2\pi\}$ ]



$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

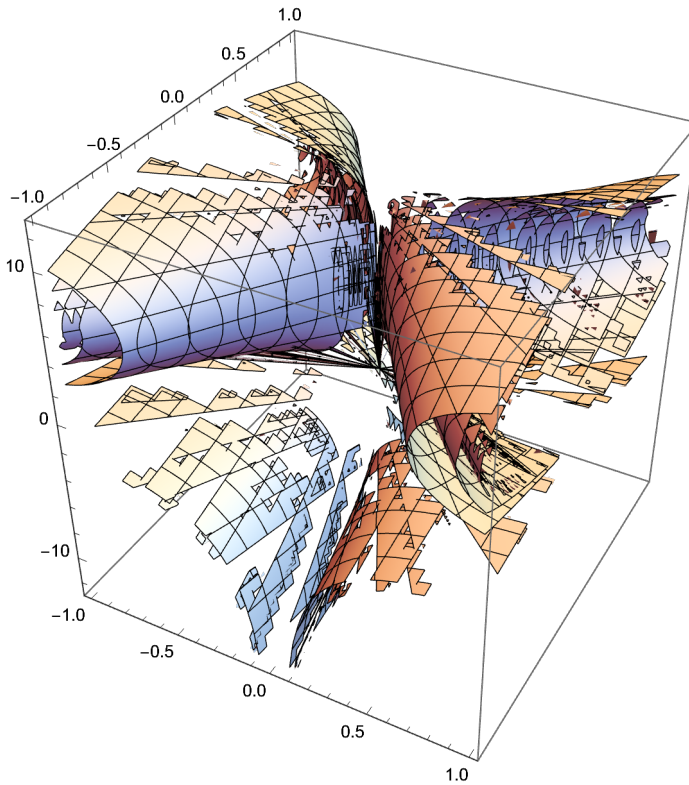
$$\left\{\left\{v \rightarrow -1.54328 \times 10^{-11} \sqrt{\left(3.77356 \times 10^{38} - \frac{3.82342 \times 10^{37} r^2 \theta^2}{\eta^2} + \frac{6.08516 \times 10^{36} r^2 \theta^3}{\eta^2} - \frac{2.42121 \times 10^{35} r^2 \theta^4}{\eta^2}\right)}\right\},\right.$$

$$\left.\left\{v \rightarrow 1.54328 \times 10^{-11} \sqrt{\left(3.77356 \times 10^{38} - \frac{3.82342 \times 10^{37} r^2 \theta^2}{\eta^2} + \frac{6.08516 \times 10^{36} r^2 \theta^3}{\eta^2} - \frac{2.42121 \times 10^{35} r^2 \theta^4}{\eta^2}\right)}\right\}\right\}$$

ContourPlot3D[-1.5432808288459432`\*^-11

$$\sqrt{\left(3.7735619429356124`*^{38} - \frac{3.8234176260591615`*^{37} r^2 \theta^2}{\eta^2} + \frac{6.085158146919955`*^{36} r^2 \theta^3}{\eta^2} - \frac{2.4212074964455716`*^{35} r^2 \theta^4}{\eta^2}\right)},$$

$$\{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$



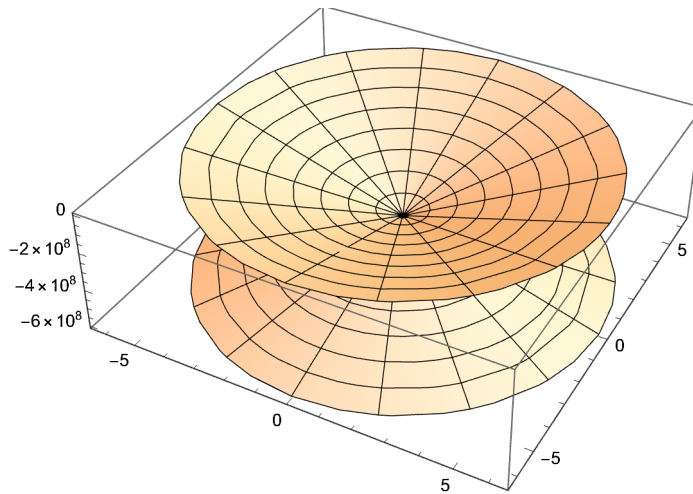
c := 2.99792458 (10^8)

$$r := \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == r\sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow \frac{2c\pi - c\theta}{2\pi} \right\}, \left\{ v \rightarrow \frac{-2c\pi + c\theta}{2\pi} \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\frac{-2c\pi + c\theta}{2\pi}, \{\theta, -2\pi, 2\pi\}\right]$$



$2\pi\eta - 2\pi r' = \phi\eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different.

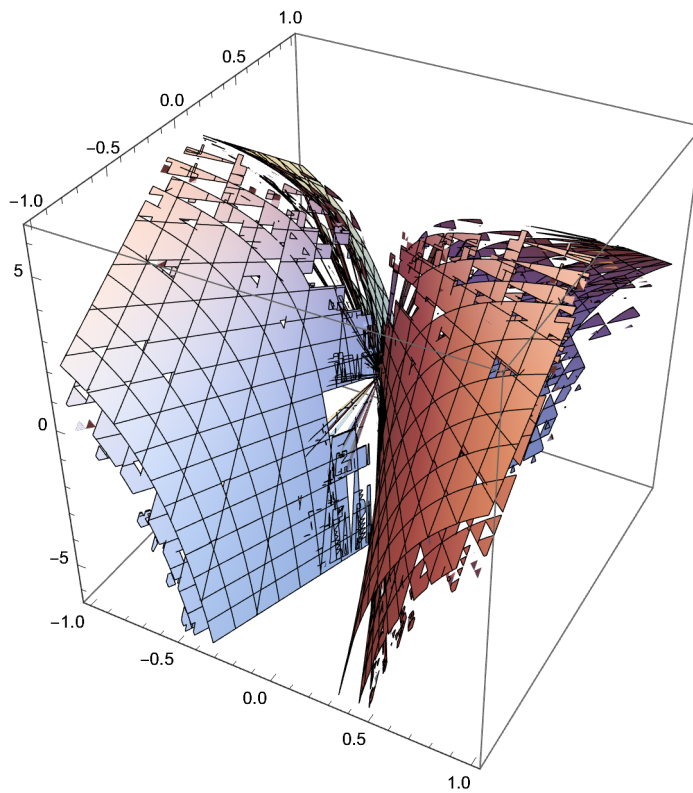
$$\text{Solve}[2\pi\eta - 2\pi r' == \phi\eta, \phi]$$

$$\left\{ \left\{ \phi \rightarrow \frac{2(\pi\eta - \pi r')}{\eta} \right\} \right\}$$

$$\text{Solve}\left[\phi == \frac{2 \left( \pi \eta - \pi r \sqrt{1 - \frac{(v)^2}{c^2}} \right)}{\eta}, v\right]$$

$$\left\{ \left\{ v \rightarrow -1.05839 \times 10^{-7} \sqrt{\left( 8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \phi}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \phi^2}{r^2} \right)} \right\}, \right. \\ \left. \left\{ v \rightarrow 1.05839 \times 10^{-7} \sqrt{\left( 8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \phi}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \phi^2}{r^2} \right)} \right\} \right\}$$

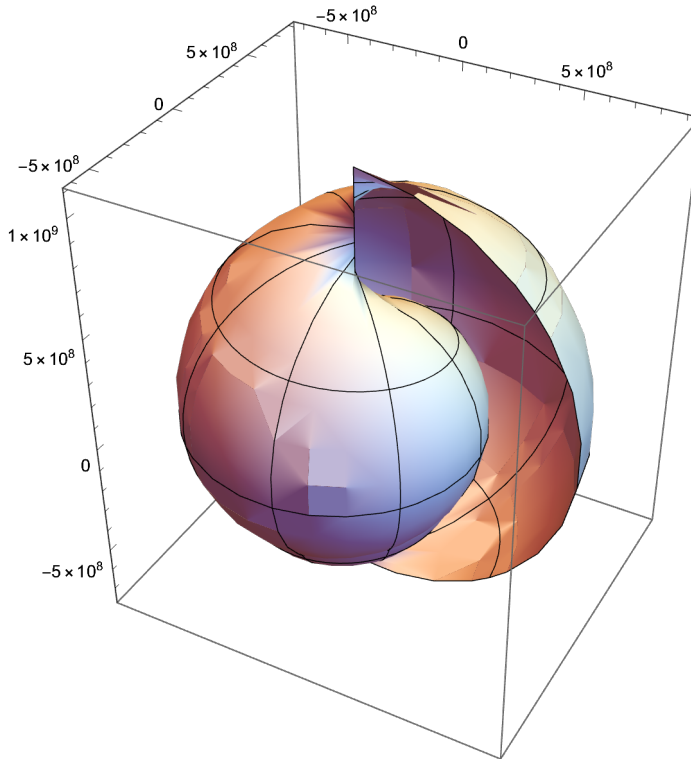
$$\text{ContourPlot3D}\left[1.0583947067478751 \cdot 10^{-7} \sqrt{\left( 8.02317171945391 \cdot 10^{30} - \frac{8.02317171945391 \cdot 10^{30} \eta^2}{r^2} + \frac{2.5538548768523825 \cdot 10^{30} \eta^2 \phi}{r^2} - \frac{2.0322931379520014 \cdot 10^{29} \eta^2 \phi^2}{r^2} \right)}, \{\eta, -1, 1\}, \{r, -1, 1\}, \{\phi, -2 \pi, 2 \pi\}\right]$$



$$\text{Solve}\left[\phi == \frac{2 \left( \pi \frac{\sqrt{4 \pi (r)^2 \theta - (r)^2 \theta^2}}{2 \pi} - \pi r \sqrt{1 - \frac{(v)^2}{c^2}} \right)}{\frac{\sqrt{4 \pi r^2 \theta - (r)^2 \theta^2}}{2 \pi}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{c \sqrt{16 \pi^4 - 16 \pi^3 \theta + 4 \pi^2 \theta^2 + 16 \pi^2 \theta \phi - 4 \pi \theta^2 \phi - 4 \pi \theta \phi^2 + \theta^2 \phi^2}}{4 \pi^2} \right\}, \right. \\ \left. \left\{ v \rightarrow \frac{c \sqrt{16 \pi^4 - 16 \pi^3 \theta + 4 \pi^2 \theta^2 + 16 \pi^2 \theta \phi - 4 \pi \theta^2 \phi - 4 \pi \theta \phi^2 + \theta^2 \phi^2}}{4 \pi^2} \right\} \right\}$$

$$\text{SphericalPlot3D}\left[\frac{c \sqrt{16 \pi^4 - 16 \pi^3 \theta + 4 \pi^2 \theta^2 + 16 \pi^2 \theta \phi - 4 \pi \theta^2 \phi - 4 \pi \theta \phi^2 + \theta^2 \phi^2}}{4 \pi^2}, \right. \\ \left. \{\theta, -2 \pi, 2 \pi\}, \{\phi, -2 \pi, 2 \pi\}\right]$$



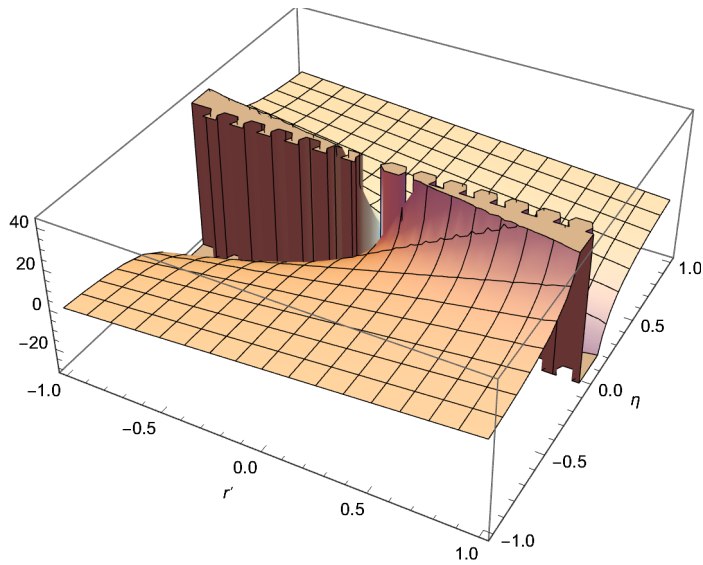
$$2 \pi \eta - 2 \pi r' = \theta \eta$$

$$\text{Solve}[2 \pi \eta - 2 \pi r' == \theta \eta, \theta]$$

$$\left\{ \left\{ \theta \rightarrow \frac{2 (\pi \eta - \pi r')}{\eta} \right\} \right\}$$



Plot3D $\left[\frac{2 (\pi \eta - \pi r')}{\eta}, \{r', -1, 1\}, \{\eta, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic}\right]$



$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

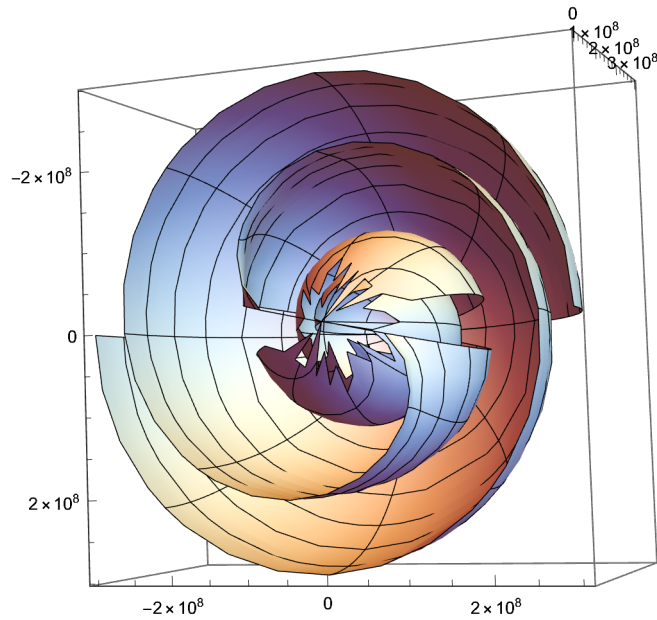
$$c := 2.99792458 (10^8)$$

$$\text{Solve}\left[\theta == \frac{2 \left( \pi \eta - \pi r \sqrt{1 - \frac{(v)^2}{c^2}} \right)}{\eta}, v\right]$$

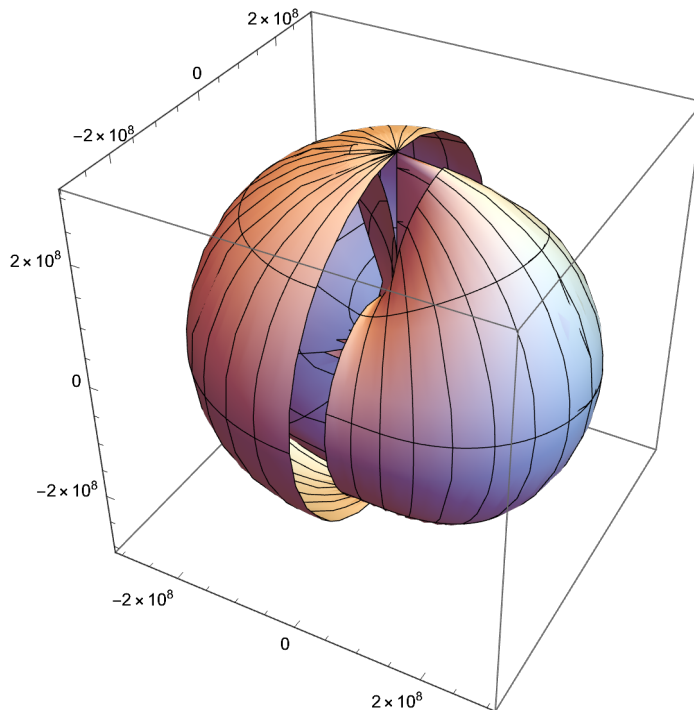
$$\left\{ \left\{ v \rightarrow - \frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 \eta^2}{r^2} + \frac{4 \pi \eta^2 \theta}{r^2} - \frac{\eta^2 \theta^2}{r^2}}}{2 \pi} \right\}, \left\{ v \rightarrow \frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 \eta^2}{r^2} + \frac{4 \pi \eta^2 \theta}{r^2} - \frac{\eta^2 \theta^2}{r^2}}}{2 \pi} \right\} \right\}$$

$$\eta := r \sin[\beta]$$

$$\text{SphericalPlot3D}\left[\frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 \eta^2}{r^2} + \frac{4 \pi \eta^2 \theta}{r^2} - \frac{\eta^2 \theta^2}{r^2}}}{2 \pi}, \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}\right]$$

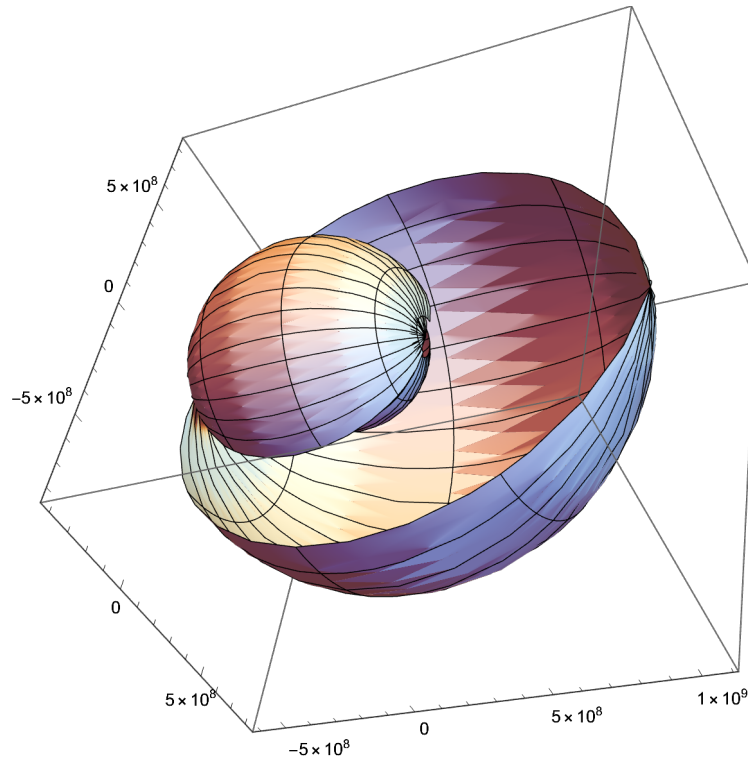


$$\text{SphericalPlot3D}\left[\frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 \eta^2}{r^2} + \frac{4 \pi \eta^2 \theta}{r^2} - \frac{\eta^2 \theta^2}{r^2}}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$

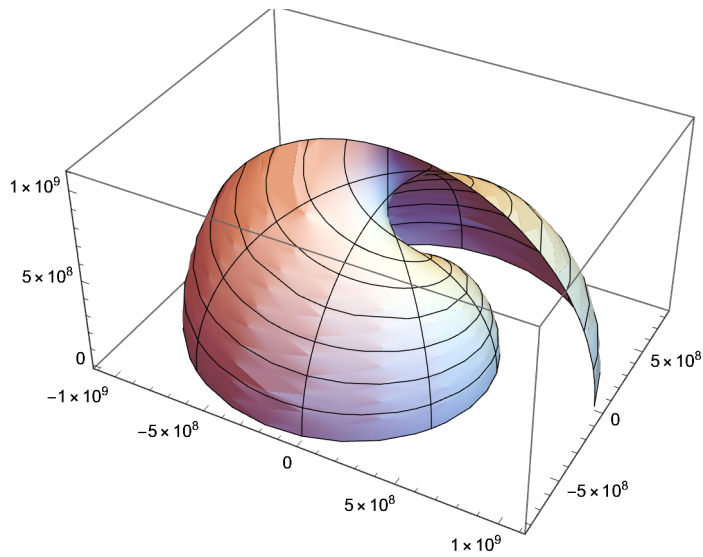


$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

SphericalPlot3D $\left[\frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 \eta^2}{r^2} + \frac{4 \pi \eta^2 \theta}{r^2} - \frac{\eta^2 \theta^2}{r^2}}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



SphericalPlot3D $\left[\frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 \eta^2}{r^2} + \frac{4 \pi \eta^2 \theta}{r^2} - \frac{\eta^2 \theta^2}{r^2}}}{2 \pi}, \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}\right]$



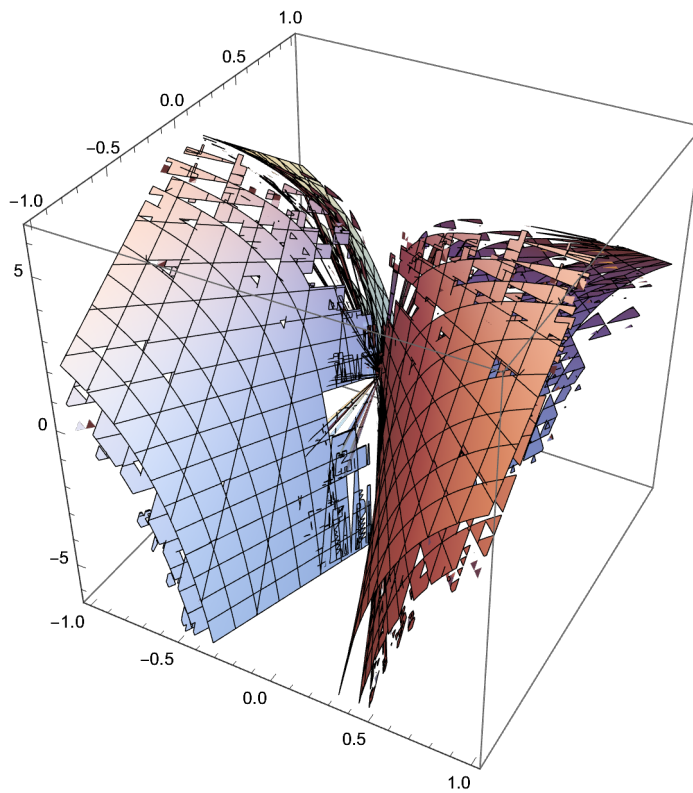
$$\text{Solve}\left[\theta == \frac{2 \left( \pi \eta - \pi r \sqrt{1 - \frac{(v)^2}{c^2}} \right)}{\eta}, v\right]$$

$$\left\{ \left\{ v \rightarrow -1.05839 \times 10^{-7} \right. \right.$$

$$\left. \sqrt{\left( 8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \theta}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \theta^2}{r^2} \right)} \right\},$$

$$\left. \left\{ v \rightarrow 1.05839 \times 10^{-7} \sqrt{\left( 8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \theta}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \theta^2}{r^2} \right)} \right\} \right\}$$

$$\text{ContourPlot3D}\left[1.0583947067478751 \cdot 10^{-7} \sqrt{\left( 8.02317171945391 \cdot 10^{30} - \frac{8.02317171945391 \cdot 10^{30} \eta^2}{r^2} + \frac{2.5538548768523825 \cdot 10^{30} \eta^2 \theta}{r^2} - \frac{2.0322931379520014 \cdot 10^{29} \eta^2 \theta^2}{r^2} \right)}, \{\eta, -1, 1\}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$x = r' = \frac{2\pi r - r\theta}{2\pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} =$$

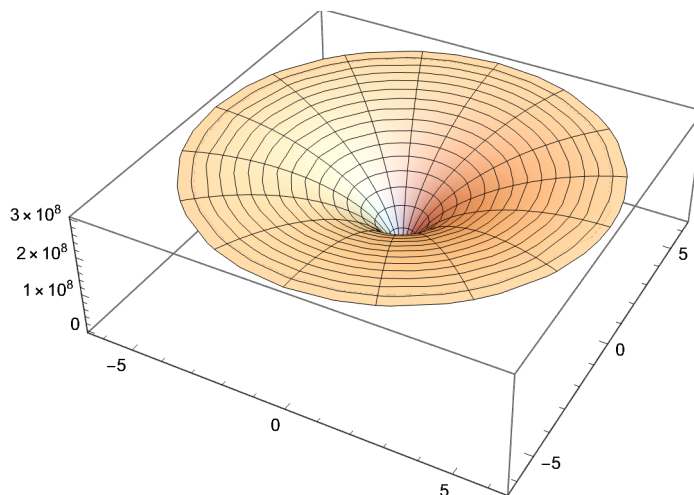
$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$$\text{Solve}\left[\frac{2\pi r - r\theta}{2\pi} == r \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

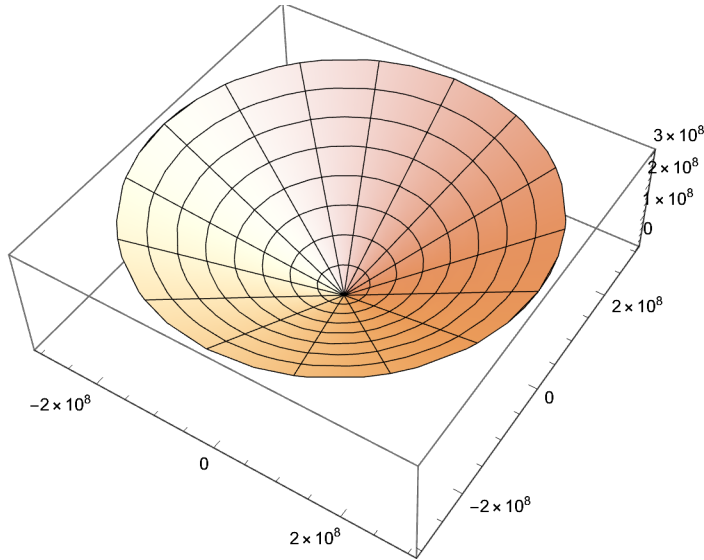
$$\left\{\left\{v \rightarrow -\frac{\sqrt{4c^2\pi\theta - c^2\theta^2}}{2\pi}\right\}, \left\{v \rightarrow \frac{\sqrt{4c^2\pi\theta - c^2\theta^2}}{2\pi}\right\}\right\}$$

$$c := 2.99792458 (10^8)$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4c^2\pi\theta - c^2\theta^2}}{2\pi}, \{\theta, -2\pi, 2\pi\}\right]$$



$\text{RevolutionPlot3D}\left[\frac{\sqrt{4 c^2 \pi^2 - c^2 (2 \pi)^2}}{2 \pi}, \{c, -3.0 \times 10^8, 3.0 \times 10^8\}\right]$



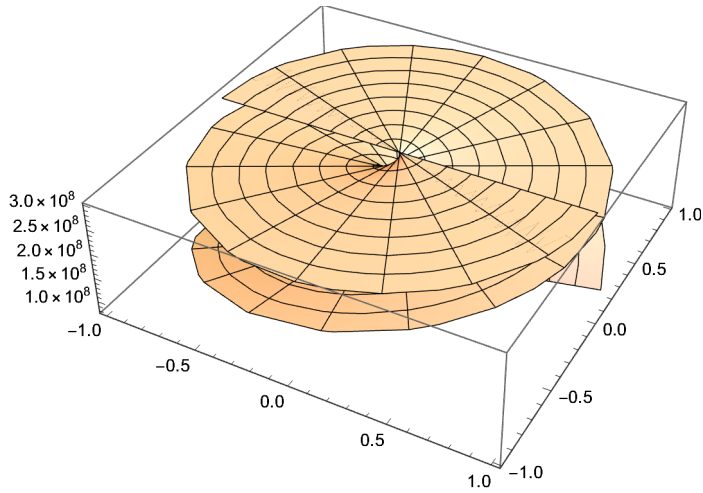
$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{c \sqrt{16 \pi^4 - \frac{16 \pi^3 r^2 \theta}{\eta^2} + \frac{20 \pi^2 r^2 \theta^2}{\eta^2} - \frac{8 \pi r^2 \theta^3}{\eta^2} + \frac{r^2 \theta^4}{\eta^2}}}{4 \pi^2}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{c \sqrt{16 \pi^4 - \frac{16 \pi^3 r^2 \theta}{\eta^2} + \frac{20 \pi^2 r^2 \theta^2}{\eta^2} - \frac{8 \pi r^2 \theta^3}{\eta^2} + \frac{r^2 \theta^4}{\eta^2}}}{4 \pi^2}\right\}\right\}$$

$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

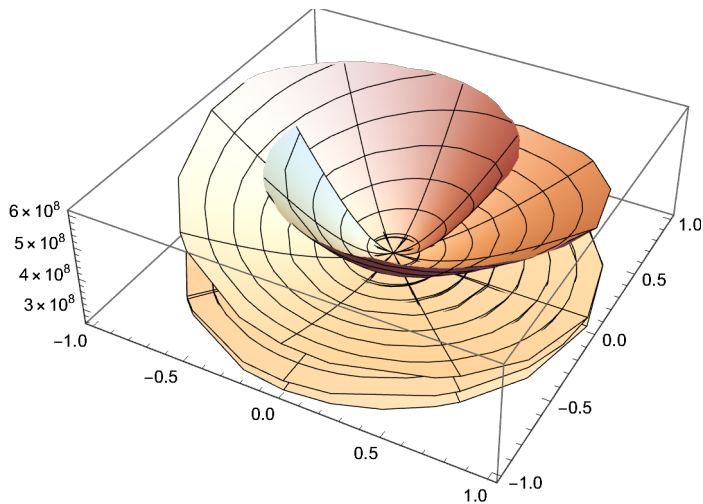
RevolutionPlot3D $\left[\frac{c \sqrt{16 \pi^4 - \frac{16 \pi^3 r^2 \theta}{\eta^2} + \frac{20 \pi^2 r^2 \theta^2}{\eta^2} - \frac{8 \pi r^2 \theta^3}{\eta^2} + \frac{r^2 \theta^4}{\eta^2}}}{4 \pi^2}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



Solve $\left[\frac{2 \pi r - r \theta}{2 \pi} = r \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$

$\left\{\left\{v \rightarrow -\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}, \left\{v \rightarrow \frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}\right\}$

RevolutionPlot3D $\left[\frac{c \sqrt{16 \pi^4 - 16 \pi^3 r^2 \theta + 20 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}}{4 \pi^2}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



Solve $\left[\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$

$\{\{v \rightarrow -c\}, \{v \rightarrow c\}\}$

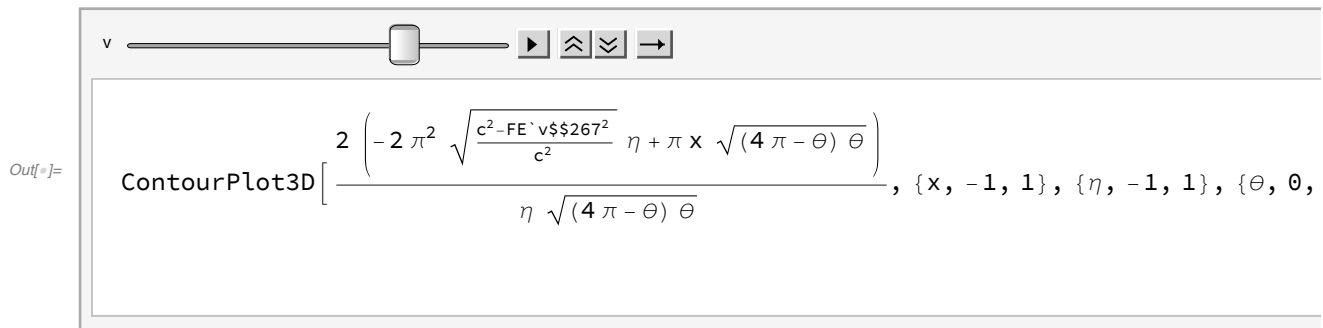
$2 \pi x - 2 \pi r' = \vartheta \eta$ , where  $\vartheta$  is an angle of a similar dimensional kind to theta, but different.

In[ ]:=  $c := 2.99792458 (10^8)$

$$\text{Solve}\left[2 \pi x - 2 \pi \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} == \vartheta \eta, \vartheta\right]$$

$$\left\{\left\{\vartheta \rightarrow \frac{2 \left(-2 \pi^2 \sqrt{\frac{c^2 - v^2}{c^2}} \eta + \pi x \sqrt{(4 \pi - \theta) \theta}\right)}{\eta \sqrt{(4 \pi - \theta) \theta}}\right\}\right\}$$

In[ ]:=  $\text{Animate}\left[\text{ContourPlot3D}\left[\frac{2 \left(-2 \pi^2 \sqrt{\frac{c^2 - v^2}{c^2}} \eta + \pi x \sqrt{(4 \pi - \theta) \theta}\right)}{\eta \sqrt{(4 \pi - \theta) \theta}}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, 0, 4 \pi\}\right], \{v, -c, c\}\right]$



$$\text{Solve}\left[2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \frac{2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} == \vartheta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \vartheta\right]$$

$$\left\{\left\{\vartheta \rightarrow -\frac{2 \pi \left(-2 \pi r + r \theta + \frac{2 \pi \sqrt{1 - \frac{v^2}{c^2}} \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{\sqrt{4 \pi \theta - \theta^2}}\right)}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right\}\right\}$$

$$\theta := 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)$$

$$r := \left(-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta] + 4 \pi^2 \text{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3}{\theta}\right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \text{Sin}[\beta]^2 + 8 \pi^2 \theta \text{Sin}[\beta]^2)$$



$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi\left(-2\pi r + r\theta + \frac{2\pi\sqrt{1-\frac{v^2}{c^2}}\sqrt{4\pi r^2\theta - r^2\theta^2}}{\sqrt{4\pi\theta - \theta^2}}\right)}{\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{v, -c, c\}, \{\theta, -2\pi, 2\pi\}\right]$$

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

∞::indet : Indeterminate expression  $(0. + 0. i)\pi$  ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

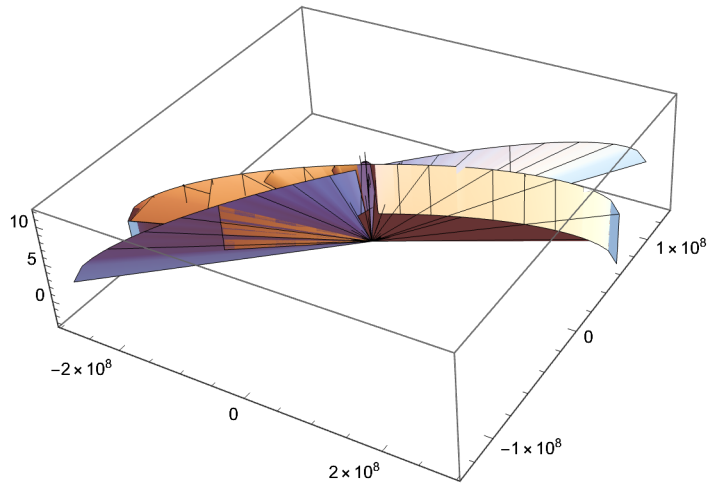
∞::indet : Indeterminate expression  $(0. + 0. i)\pi$  ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

∞::indet : Indeterminate expression  $(0. + 0. i)\pi$  ComplexInfinity encountered. >>

General::stop : Further output of ∞::indet will be suppressed during this calculation. >>



$$\text{RevolutionPlot3D}\left[\frac{2\pi\left(-2\pi r + r\theta + \frac{2\pi\sqrt{1-\frac{v^2}{c^2}}\sqrt{4\pi r^2\theta - r^2\theta^2}}{\sqrt{4\pi\theta - \theta^2}}\right)}{\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{v, -c, c\}, \{\beta, -\pi/2, \pi/2\}\right]$$

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

∞::indet : Indeterminate expression 0. π ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

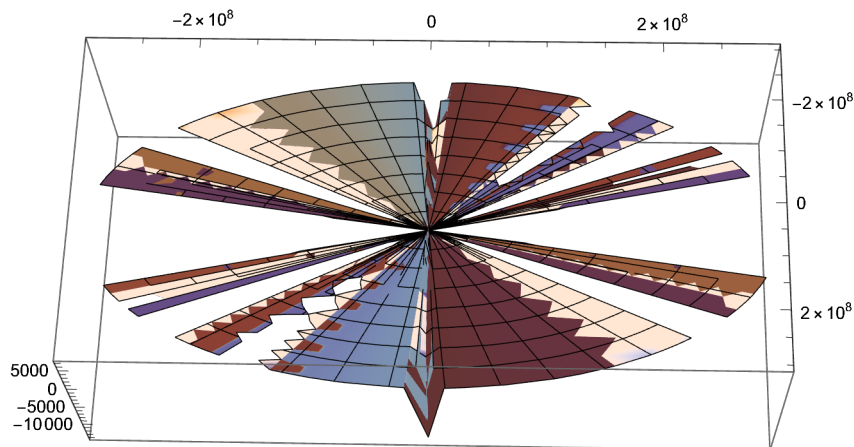
∞::indet : Indeterminate expression 0. π ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

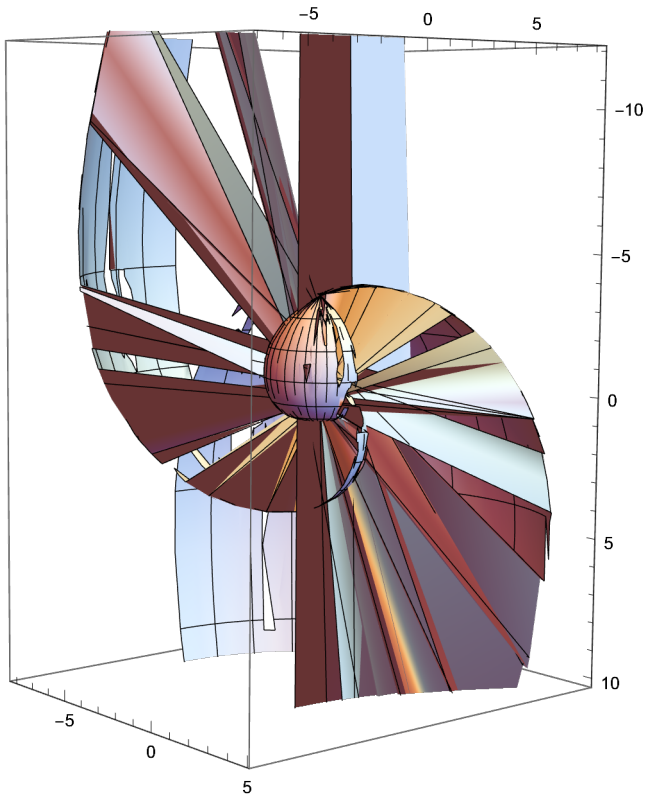
∞::indet : Indeterminate expression 0. π ComplexInfinity encountered. >>

General::stop : Further output of ∞::indet will be suppressed during this calculation. >>



$$v := \left( \sqrt{(-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right)$$

$$\text{SphericalPlot3D}\left[\frac{2\pi\left(-2\pi r + r\theta + \frac{2\pi\sqrt{1-\frac{v^2}{c^2}}\sqrt{4\pi r^2\theta - r^2\theta^2}}{\sqrt{4\pi\theta - \theta^2}}\right)}{\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$

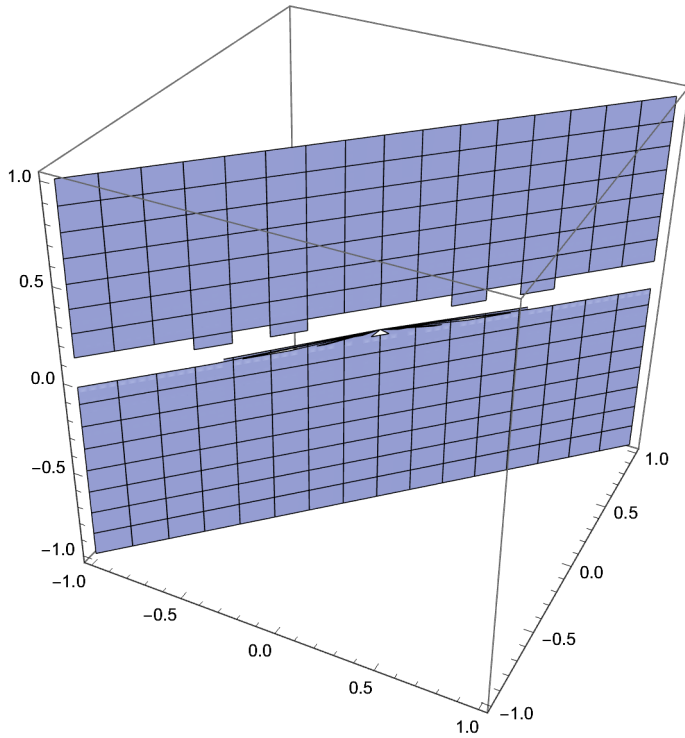


$$2\pi x - 2\pi r' = \theta \eta$$

$$\text{Solve}[2\pi x - 2\pi r' == \theta \eta, \theta]$$

$$\left\{\left\{\theta \rightarrow \frac{2(\pi x - \pi r')}{\eta}\right\}\right\}$$

ContourPlot3D $\left[\frac{2 (\pi x - \pi r')}{\eta}, \{x, -1, 1\}, \{r', -1, 1\}, \{\eta, -1, 1\}\right]$



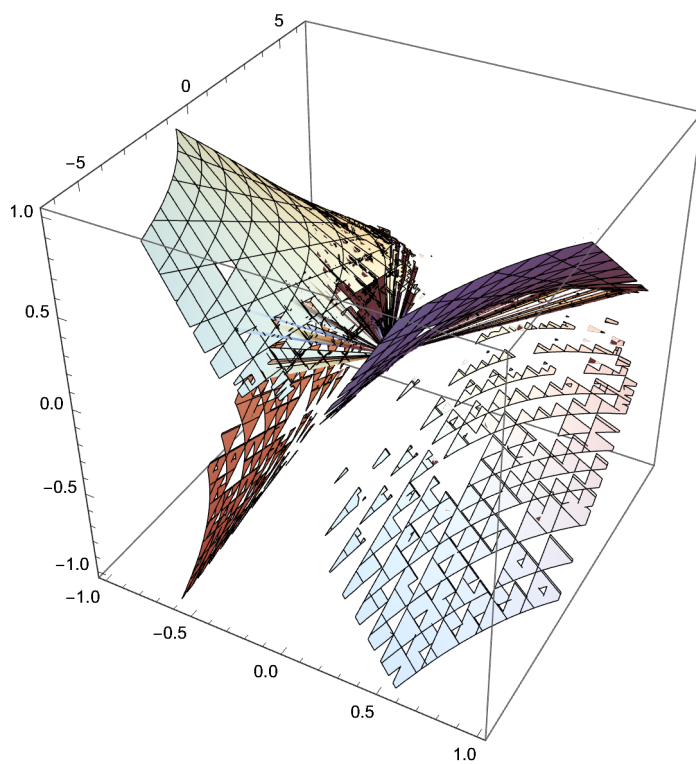
$$\eta = x' = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$c := 2.99792458 (10^8)$

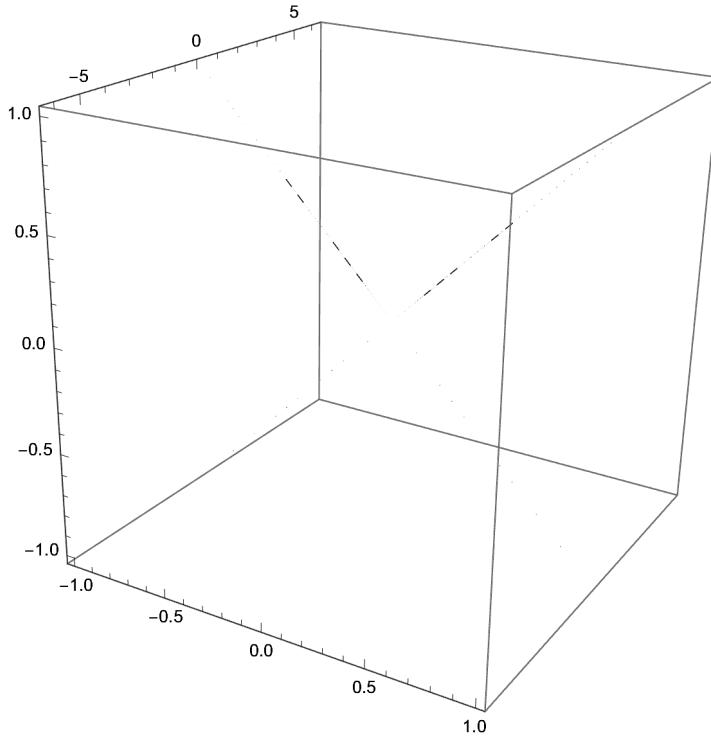
Solve $\left[\eta == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$

$$\left\{ \left\{ v \rightarrow -\frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\}, \left\{ v \rightarrow \frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\} \right\}$$

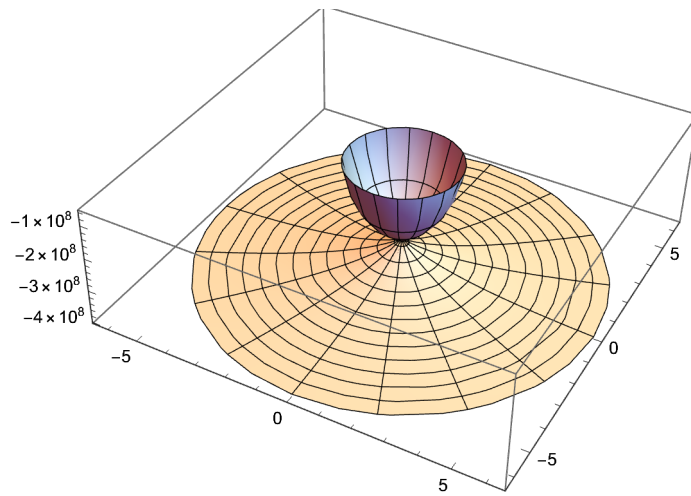
ContourPlot3D $\left[-\frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}\right]$

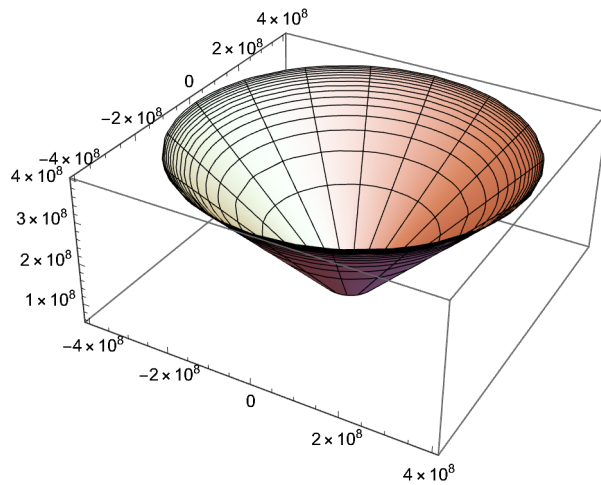


ContourPlot3D $\left[\left\{-\frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\},\right.$   
 $\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}\mathbf{]}$



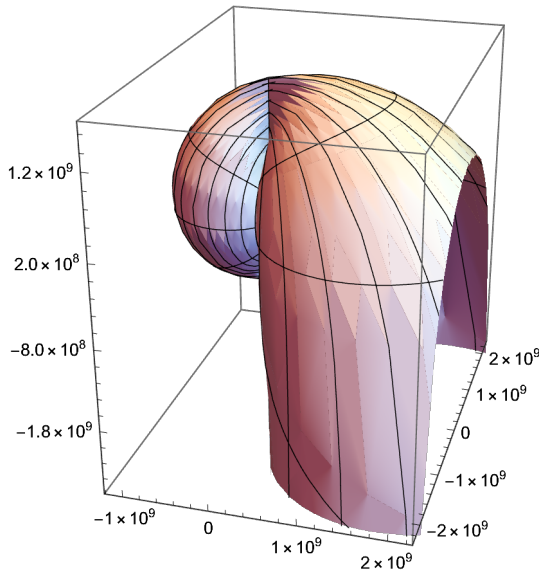
Solve $\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$   
 $\left\{\left\{v \rightarrow -\frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}, \left\{v \rightarrow \frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}\right\}$

$$\text{RevolutionPlot3D}\left[-\frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{\theta, -2 \pi, 2 \pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\left\{-\frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}, \{\theta, -2 \pi, 2 \pi\}\right]$$


A brief substitution :

`SphericalPlot3D` $\left[-\left(\sqrt{2} \sqrt{\left(2 c^2 \pi^2-4 c^2 \pi \theta+c^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)\right)^2\right)}\right) / \right.$   
 $\left.\left(\sqrt{4 \pi^2-4 \pi \theta+(\theta)^2}\right),\{\theta,-2 \pi, 2 \pi\},\{\beta,-\pi / 2, \pi / 2\}\right]$



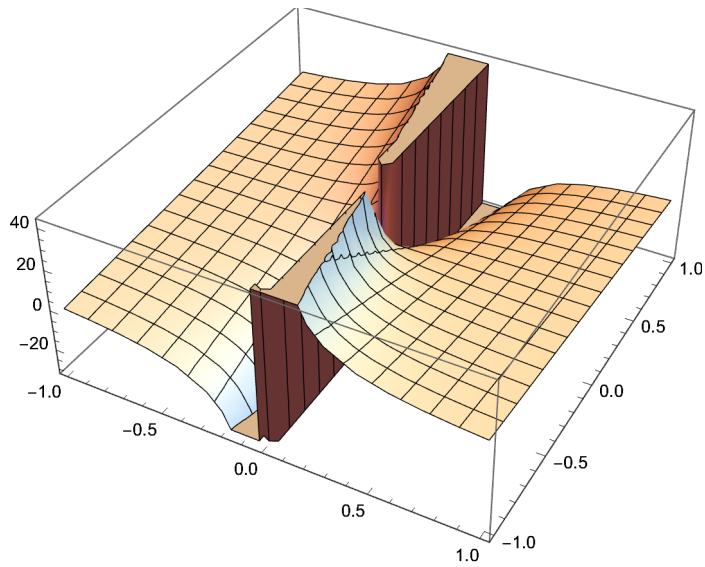
$2 \pi \eta-2 \pi x^{\prime}=\omega \eta$ , where  $\omega$  is an angle of a similar dimensional kind to theta, but different.

`Solve` $[2 \pi \eta-2 \pi x^{\prime}==\omega \eta, \omega]$

$\left\{\left\{\omega \rightarrow \frac{2\left(\pi \eta-\pi x^{\prime}\right)}{\eta}\right\}\right\}$



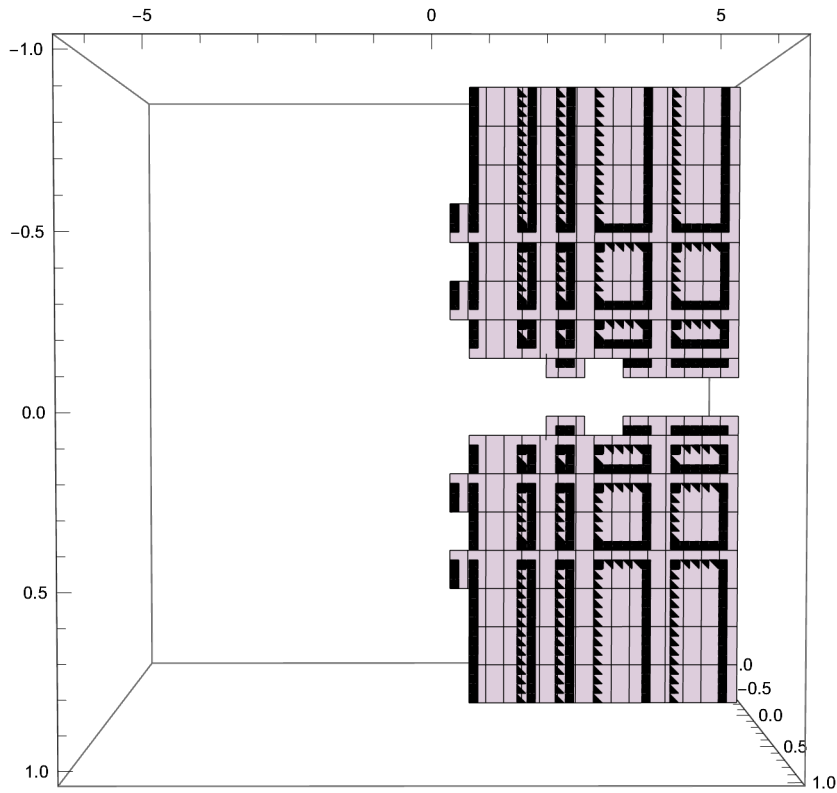
Plot3D $\left[\frac{2 (\pi \eta - \pi x')}{\eta}, \{\eta, -1, 1\}, \{x', -1, 1\}\right]$



Solve $\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi x' == \omega \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \omega\right]$

$\left\{\left\{\omega \rightarrow \frac{2 \pi \left(\sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi x'\right)}{\sqrt{r^2 (4 \pi - \theta) \theta}}\right\}\right\}$

ContourPlot3D $\left[\frac{2 \pi \left(\sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi x'\right)}{\sqrt{r^2 (4 \pi - \theta) \theta}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{x', -1, 1\}\right]$



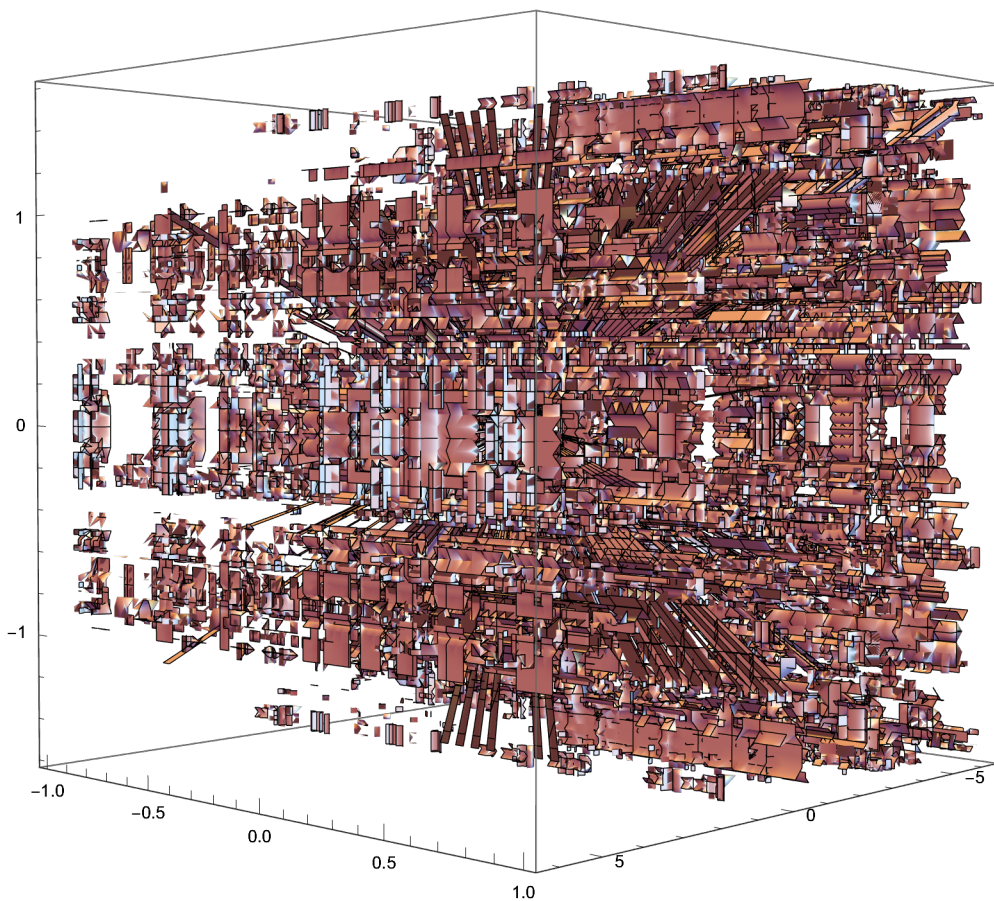
Solve $\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} == \omega \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \omega\right]$

$\left\{\left\{\omega \rightarrow -\left(6.28319 \left(1. \sqrt{1. - 1.11265 \times 10^{-17} v^2} (6.28319 r - 1. r \theta) - 1. \sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}\right)\right) / \left(\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}\right)\right\}\right\}$

```

ContourPlot3D[-(6.283185307179586`
  (1.`√(1.`-1.1126500560536185`*^-17((√(-1.1294090667581471`*^18θ+
    8.987551787368176`*^16θ²+3.5481432270250993`*^18Sin[β]²)))/
    (√(-12.566370614359172`θ+θ²+39.47841760435743`Sin[β]²))))²)
  (6.283185307179586`r-1.`rθ)-1.`√(12.566370614359172`r²θ-1.`r²θ²)))/
  (√(12.566370614359172`r²θ-1.`r²θ²)),
{β,
 -π/
  2, π/
  2}, {θ, -2
  π, 2
  π}, {r, -1, 1}]

```



$$r := \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}$$

```

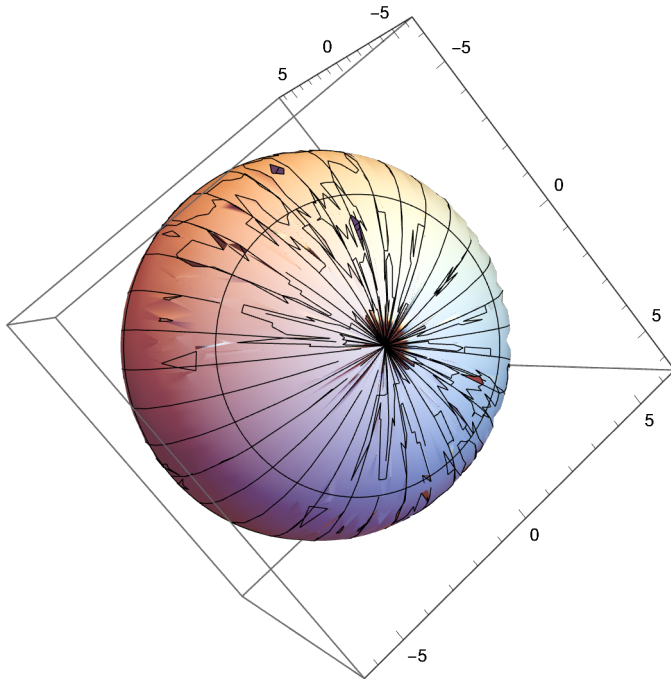
SphericalPlot3D[ - ( 6.283185307179586`
  ( 1.`  $\sqrt{(1.` - 1.1126500560536185` *^{-17} ((\sqrt{(-1.1294090667581471` *^{18} \theta +$ 
    8.987551787368176` *^{16} \theta^2 + 3.5481432270250993` *^{18} \text{Sin}[\beta]^2)) /
```

$$\left( \sqrt{(-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)} \right)^2$$

```

    (6.283185307179586` r - 1.` r \theta) - 1.`  $\sqrt{12.566370614359172` r^2 \theta - 1.` r^2 \theta^2}$  ) ) /
    (  $\sqrt{12.566370614359172` r^2 \theta - 1.` r^2 \theta^2}$  ),
  { \theta,
    -2
    \pi, 2
    \pi}, {\beta, -\pi /
    2, \pi /
    2} ]

```



$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{c^2}} == \omega \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, v\right]$$

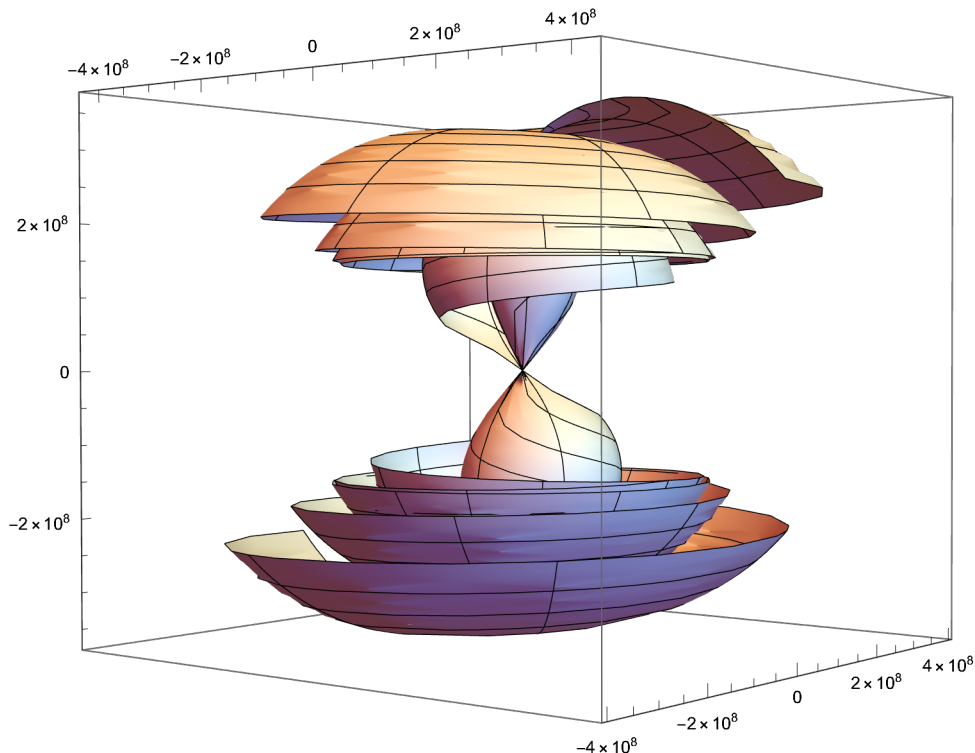
$$\left\{\left\{v \rightarrow -\left(1. \sqrt{\left(1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 7.57575 \times 10^{46} \theta^2 + 1.51515 \times 10^{47} \theta \omega - 1.20572 \times 10^{46} \theta^2 \omega - 1.20572 \times 10^{46} \theta \omega^2 + 9.59481 \times 10^{44} \theta^2 \omega^2\right)}\right) / \left(\sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2}\right)\right\}, \right.$$

$$\left.\left\{v \rightarrow \left(\sqrt{\left(1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 7.57575 \times 10^{46} \theta^2 + 1.51515 \times 10^{47} \theta \omega - 1.20572 \times 10^{46} \theta^2 \omega - 1.20572 \times 10^{46} \theta \omega^2 + 9.59481 \times 10^{44} \theta^2 \omega^2\right)}\right) / \left(\sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2}\right)\right\}\right\}$$

SphericalPlot3D[

$$\left\{-\left(1. \sqrt{\left(1.495394089917615 \times 10^{48} - 9.519974451231788 \times 10^{47} \theta + 7.575754960110463 \times 10^{46} \theta^2 + 1.5151509920220929 \times 10^{47} \theta \omega - 1.2057188495545248 \times 10^{46} \theta^2 \omega - 1.2057188495545248 \times 10^{46} \theta \omega^2 + 9.594805744283795 \times 10^{44} \theta^2 \omega^2\right)}\right) / \left(\sqrt{\left(1.663850317969084 \times 10^{31} - 5.296200053396031 \times 10^{30} \theta + 4.2145820905076925 \times 10^{29} \theta^2\right)}\right), \right.$$

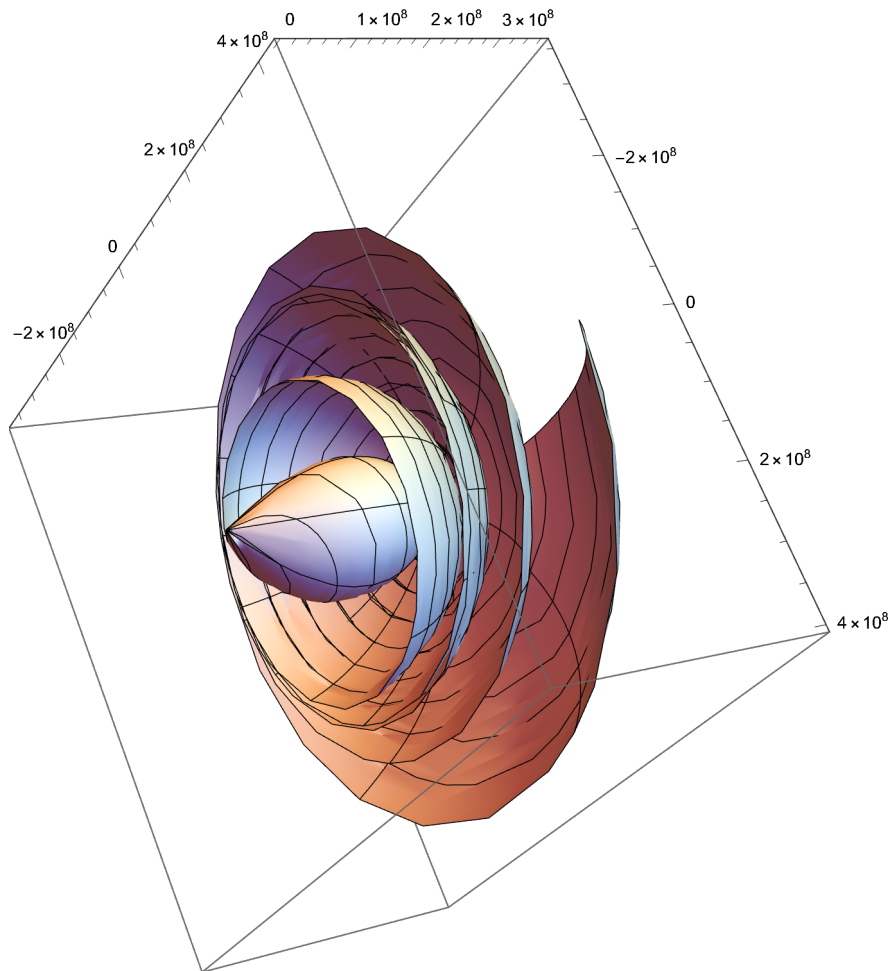
$$\left(\sqrt{\left(1.495394089917615 \times 10^{48} - 9.519974451231788 \times 10^{47} \theta + 7.575754960110463 \times 10^{46} \theta^2 + 1.5151509920220929 \times 10^{47} \theta \omega - 1.2057188495545248 \times 10^{46} \theta^2 \omega - 1.2057188495545248 \times 10^{46} \theta \omega^2 + 9.594805744283795 \times 10^{44} \theta^2 \omega^2\right)}\right) / \left(\sqrt{\left(1.663850317969084 \times 10^{31} - 5.296200053396031 \times 10^{30} \theta + 4.2145820905076925 \times 10^{29} \theta^2\right)}\right)\right\}, \{\theta, -\pi/3, \pi/3\}, \{\omega, -3\pi, 3\pi\}]$$



SphericalPlot3D[

$$\left( \sqrt{\left( 1.495394089917615 \cdot 10^{48} - 9.519974451231788 \cdot 10^{47} \theta + 7.575754960110463 \cdot 10^{46} \theta^2 + 1.5151509920220929 \cdot 10^{47} \theta \omega - 1.2057188495545248 \cdot 10^{46} \theta^2 \omega - 1.2057188495545248 \cdot 10^{46} \theta \omega^2 + 9.594805744283795 \cdot 10^{44} \theta^2 \omega^2 \right)} \right) /$$

$$\left( \sqrt{\left( 1.663850317969084 \cdot 10^{31} - 5.296200053396031 \cdot 10^{30} \theta + 4.2145820905076925 \cdot 10^{29} \theta^2 \right)} \right), \{\theta, -\pi/3, \pi/3\}, \{\omega, -3\pi, 3\pi\}]$$



Synchronized angles:  $2\pi\eta - 2\pi x' = \theta\eta$

Solve[ $2\pi\eta - 2\pi x' == \theta\eta, \theta$ ]

$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} - 2\pi x' == \theta \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi r^2 - \sqrt{2}\pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2}\right\},\right.$$

$$\left\{\theta \rightarrow \frac{2\pi r^2 + \sqrt{2}\pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2}\right\},$$

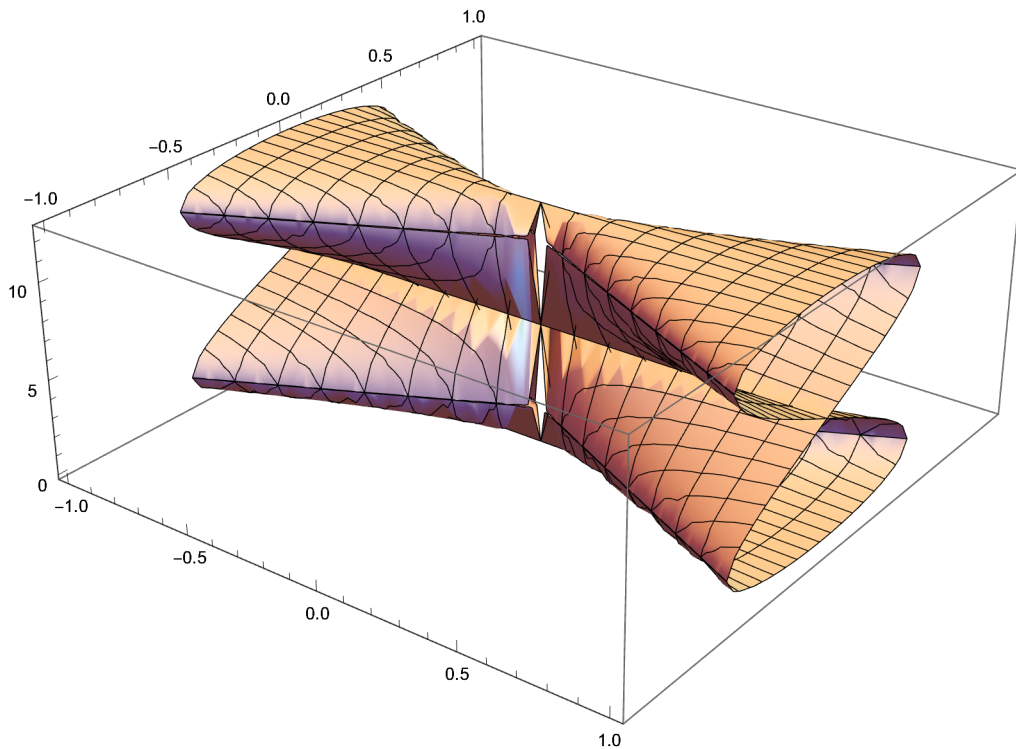
$$\left\{\theta \rightarrow \frac{2\pi r^2 - \sqrt{2}\pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2}\right\},$$

$$\left\{\theta \rightarrow \frac{2\pi r^2 + \sqrt{2}\pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2}\right\}\}$$

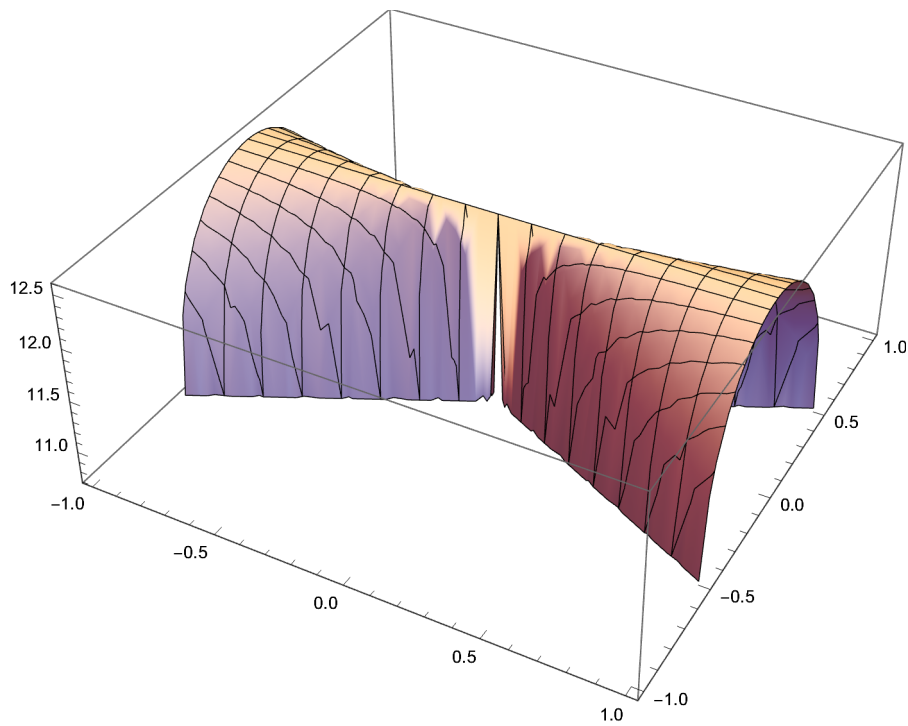
$$\text{Plot3D}\left[\left\{\frac{2\pi r^2 - \sqrt{2}\pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2},\right.\right.$$

$$\frac{2\pi r^2 - \sqrt{2}\pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2}, \frac{2\pi r^2 + \sqrt{2}\pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2},$$

$$\left.\frac{2\pi r^2 + \sqrt{2}\pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4(x')^2)}}{r^2}\right\}, \{r, -1, 1\}, \{x', -1, 1\}]$$



Plot3D $\left[\frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}, \{r, -1, 1\}, \{x', -1, 1\}\right]$



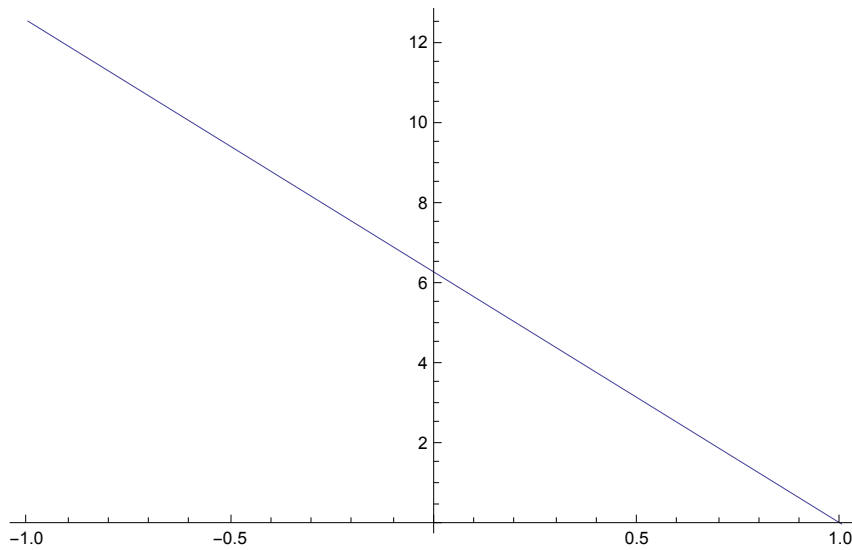
$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi x' == \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\{\{\theta \rightarrow -2 \pi (-1 + x')\}\}$$



Plot[-2 π (-1 + x'), {x', -1, 1}]



$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{c^2}} == \theta \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2\pi\right\}, \left\{\theta \rightarrow \frac{2(c\pi - \pi v)}{c}\right\}, \left\{\theta \rightarrow \frac{2(c\pi + \pi v)}{c}\right\}\right\}$$

Manipulate[SphericalPlot3D[

$$\left\{\frac{1}{c} 2(c\pi + \pi) \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{(-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2)}\right)\right\},$$

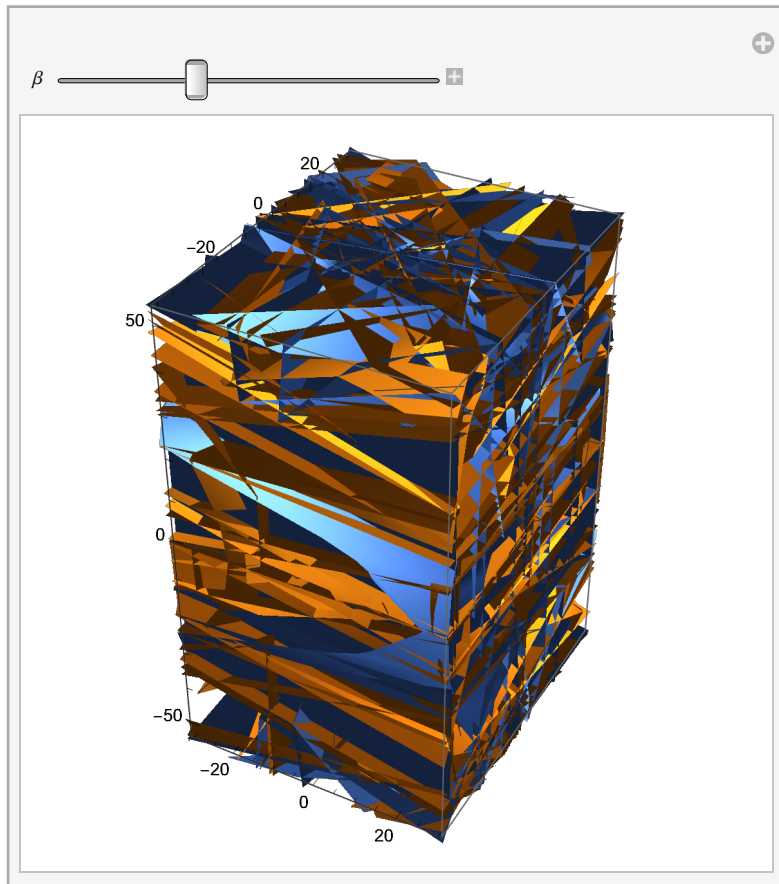
$$\frac{1}{c} 2(c\pi - \pi) \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{(-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2)}\right)\right\},$$

$$\{\theta, -2\pi, 2\pi\}, \{c, -3 \cdot 10^8, 3 \cdot 10^8\}], \{\beta,$$

$$-4$$

$$\pi, 4$$

$$\pi\}$$



General::ivar : 2.99792458`\*^8 is not a valid variable. >>

General::ivar : 2.99792458`\*^8 is not a valid variable. >>

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General::stop : Further output of General::ivar will be suppressed during this calculation. >>

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General::stop : Further output of General::ivar will be suppressed during this calculation. >>

... General: 2.99792458`\*^8 is not a valid variable.

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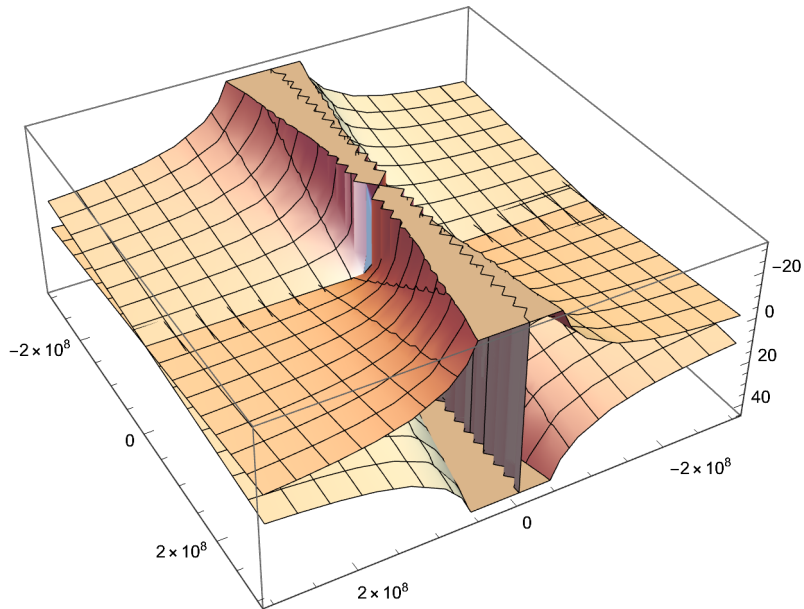
... General: 2.99792458`\*^8 is not a valid variable.

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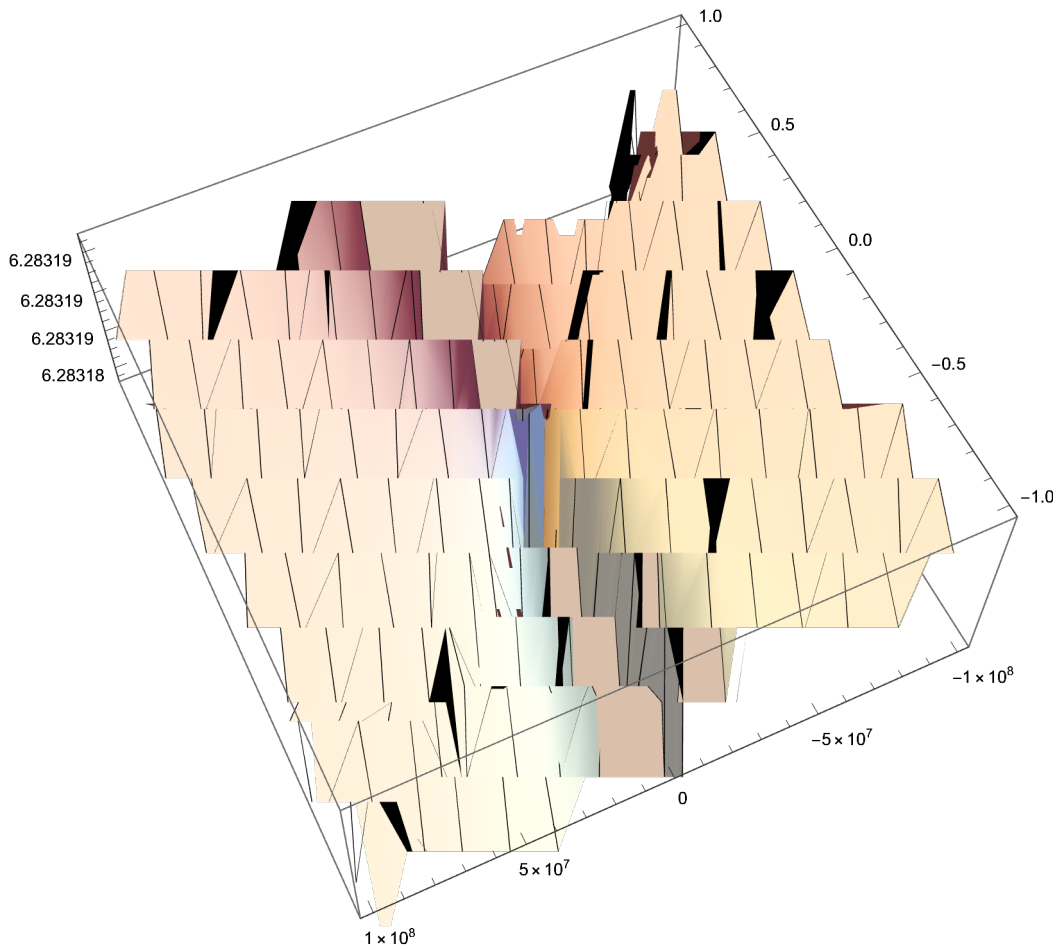
... General: 2.99792458`\*^8 is not a valid variable.

... General: Further output of General::ivar will be suppressed during this calculation.

`Plot3D`[[ $\left\{\frac{2(c\pi + \pi v)}{c}, \frac{2(c\pi - \pi v)}{c}\right\}$ , {v, -3 \* 10^8, 3 \* 10^8}, {c, -3 \* 10^8, 3 \* 10^8}]



Plot3D $\left[\frac{2 (c \pi + \pi v)}{c}, \{v, -1, 1\}, \{c, -10^8, 10^8\}\right]$



$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} == \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, v\right]$$

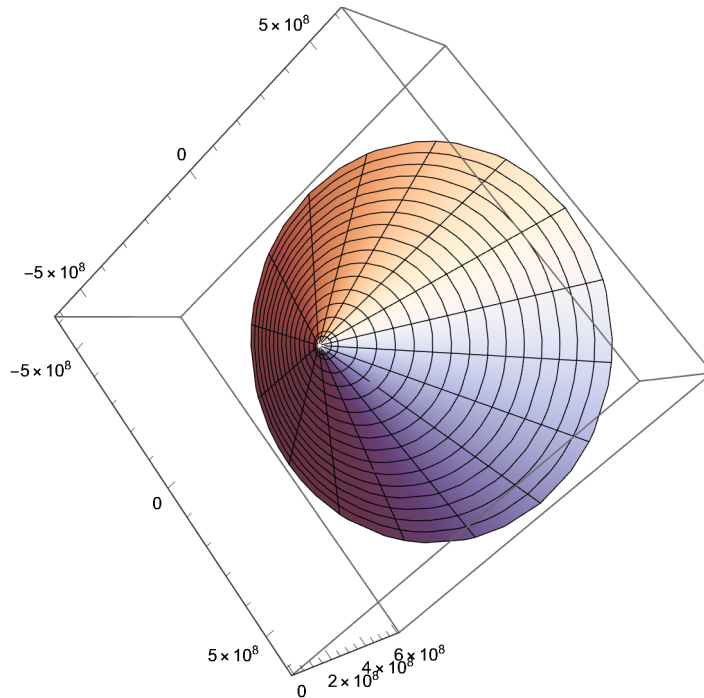
$$\left\{\left\{v \rightarrow -\left(1. \sqrt{\left(9.41587 \times 10^{45} - 5.99433 \times 10^{45} \theta + 1.43104 \times 10^{45} \theta^2 - 1.51838 \times 10^{44} \theta^3 + 6.04145 \times 10^{42} \theta^4\right)}\right) / \left(\sqrt{1.04766 \times 10^{29} - 3.33479 \times 10^{28} \theta + 2.65375 \times 10^{27} \theta^2}\right)\right\},\right.$$

$$\left.\left\{v \rightarrow \left(\sqrt{\left(9.41587 \times 10^{45} - 5.99433 \times 10^{45} \theta + 1.43104 \times 10^{45} \theta^2 - 1.51838 \times 10^{44} \theta^3 + 6.04145 \times 10^{42} \theta^4\right)}\right) / \left(\sqrt{1.04766 \times 10^{29} - 3.33479 \times 10^{28} \theta + 2.65375 \times 10^{27} \theta^2}\right)\right\}\right\}$$

```

RevolutionPlot3D[
  {-(1.√(9.415867378162551`^45 - 5.99432734692918`^45 θ + 1.431040241662059`^45
    θ^2 - 1.5183808548262475`^44 θ^3 + 6.04144546354237`^42 θ^4)) /
    (√(1.0476565366106001`^29 - 3.3347943292822445`^28 θ +
      2.653745008500455`^27 θ^2))),
  (√(9.415867378162551`^45 - 5.99432734692918`^45 θ + 1.431040241662059`^45 θ^2 -
    1.5183808548262475`^44 θ^3 + 6.04144546354237`^42 θ^4)) /
    (√(1.0476565366106001`^29 - 3.3347943292822445`^28 θ +
      2.653745008500455`^27 θ^2))), {θ, -2 π, 2 π}]

```



$$x = \eta' = \frac{2\pi r - r\theta}{2\pi} = \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}}$$

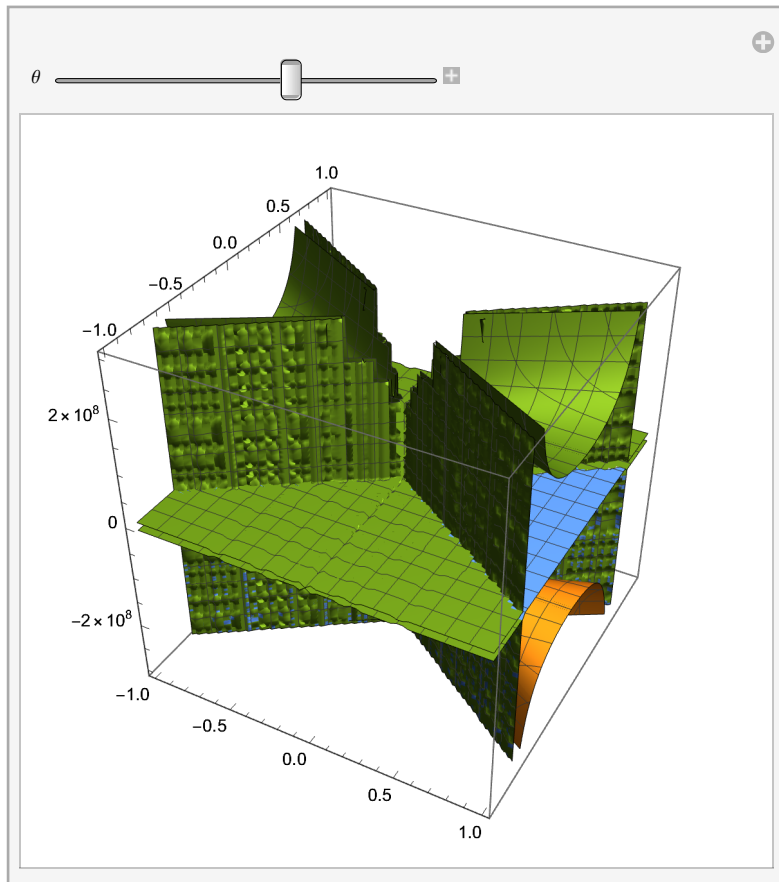
$$\text{Solve}\left[x == \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -c \sqrt{1 - \frac{\pi x^2}{r^2(4\pi - \theta)} - \frac{\pi x^2}{r^2\theta}}\right\}, \left\{v \rightarrow c \sqrt{1 - \frac{\pi x^2}{r^2(4\pi - \theta)} - \frac{\pi x^2}{r^2\theta}}\right\}\right\}$$

```

Manipulate[ContourPlot3D[c √(1 - (π x^2)/(r^2 (4 π - θ)) - (π x^2)/(r^2 θ)),
  {r, -1, 1}, {x, -1, 1}, {c, -3 * 10^8, 3 * 10^8}], {θ, -2 π, 2 π}]

```



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression  $1 + \text{ComplexInfinity} + \text{ComplexInfinity}$  encountered.

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... **General:** Further output of Power::infy will be suppressed during this calculation.

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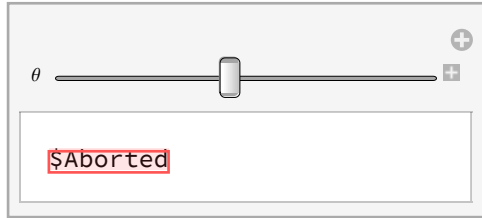
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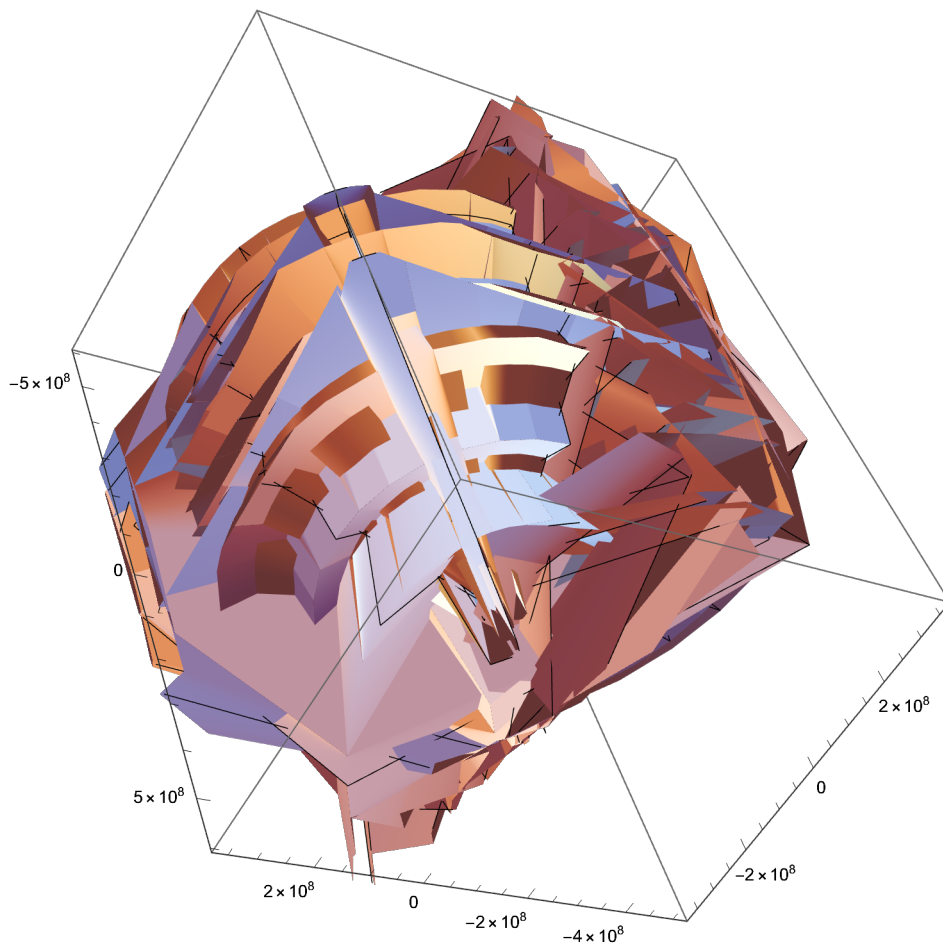
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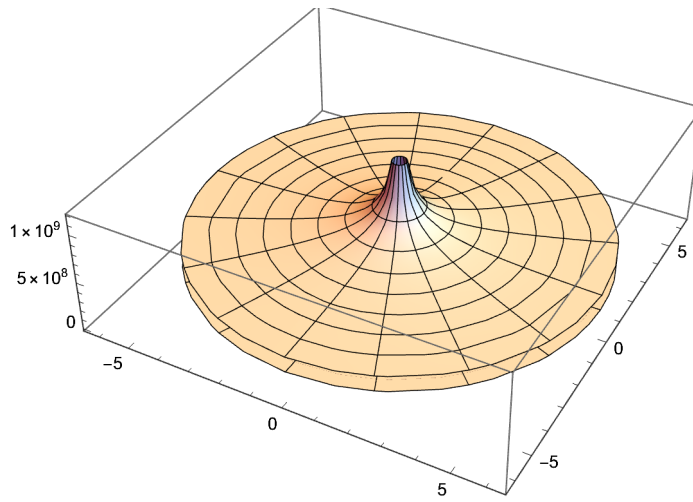
$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

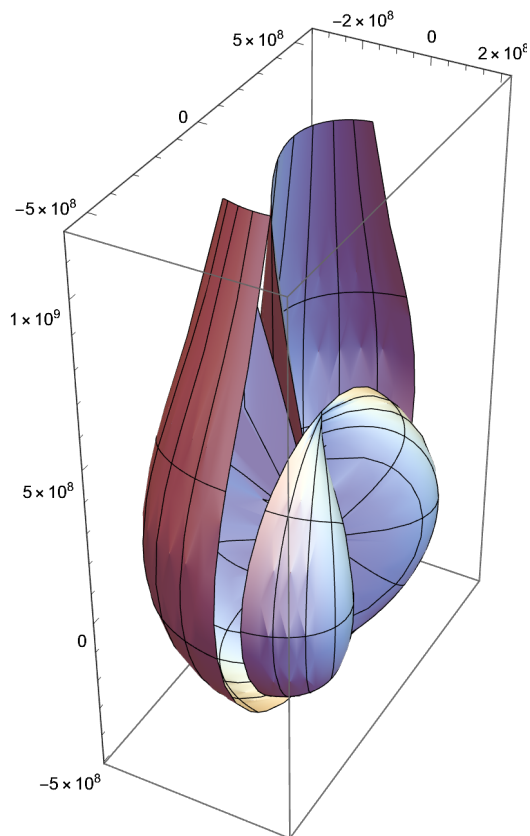
$$\left\{\left\{v \rightarrow -c \sqrt{2 - \frac{\pi}{4 \pi - \theta} - \frac{\pi}{\theta}}\right\}, \left\{v \rightarrow c \sqrt{2 - \frac{\pi}{4 \pi - \theta} - \frac{\pi}{\theta}}\right\}\right\}$$

$$\text{SphericalPlot3D}\left[c \sqrt{2 - \frac{\pi}{4 \pi - \theta} - \frac{\pi}{\theta}}, \{c, -2.99792458 (10^8), 2.99792458 (10^8)\}, \{\theta, -2 \pi, 2 \pi\}\right]$$

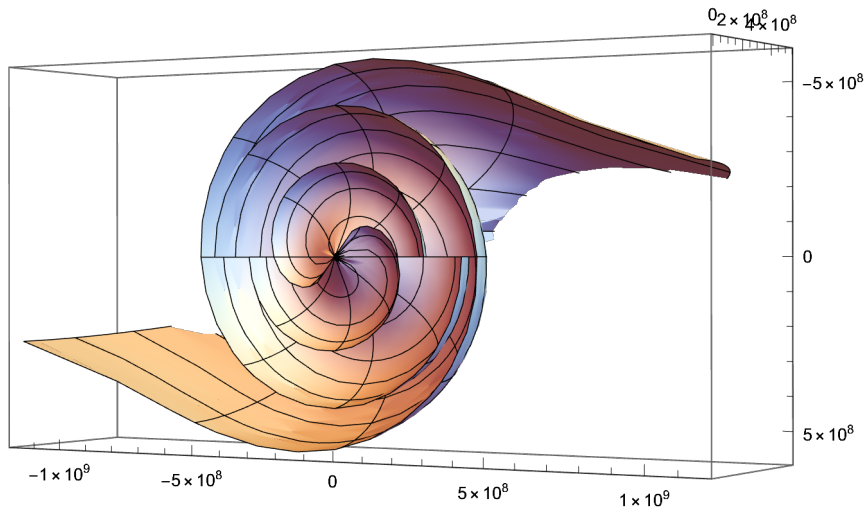


$c := 2.99792458 (10^8)$

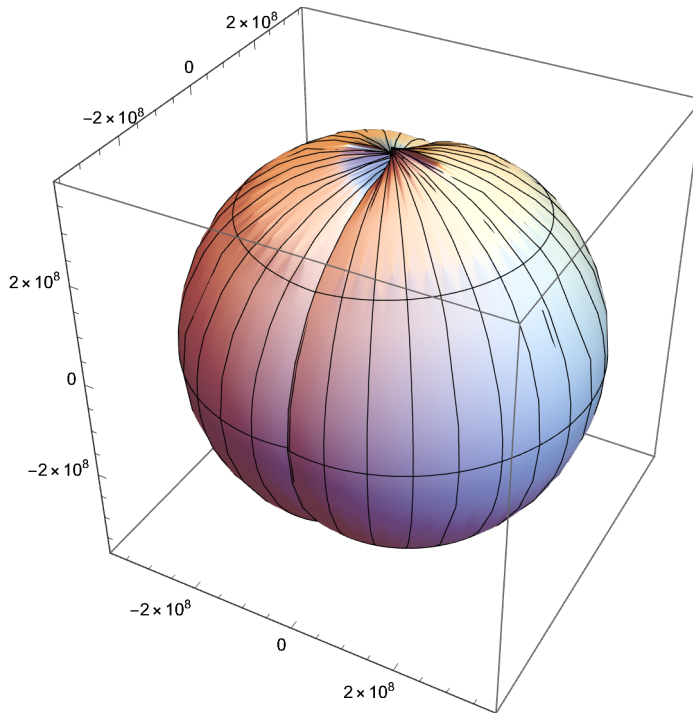
$$\text{RevolutionPlot3D}\left[c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{\theta}}, \{\theta, -2\pi, 2\pi\}\right]$$


$$\text{SphericalPlot3D}\left[c \sqrt{2 - \frac{\pi}{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} - \frac{\pi}{\theta}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$


SphericalPlot3D $\left[c \sqrt{2 - \frac{\pi}{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} - \frac{\pi}{\theta}}, \right.$   
 $\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}$

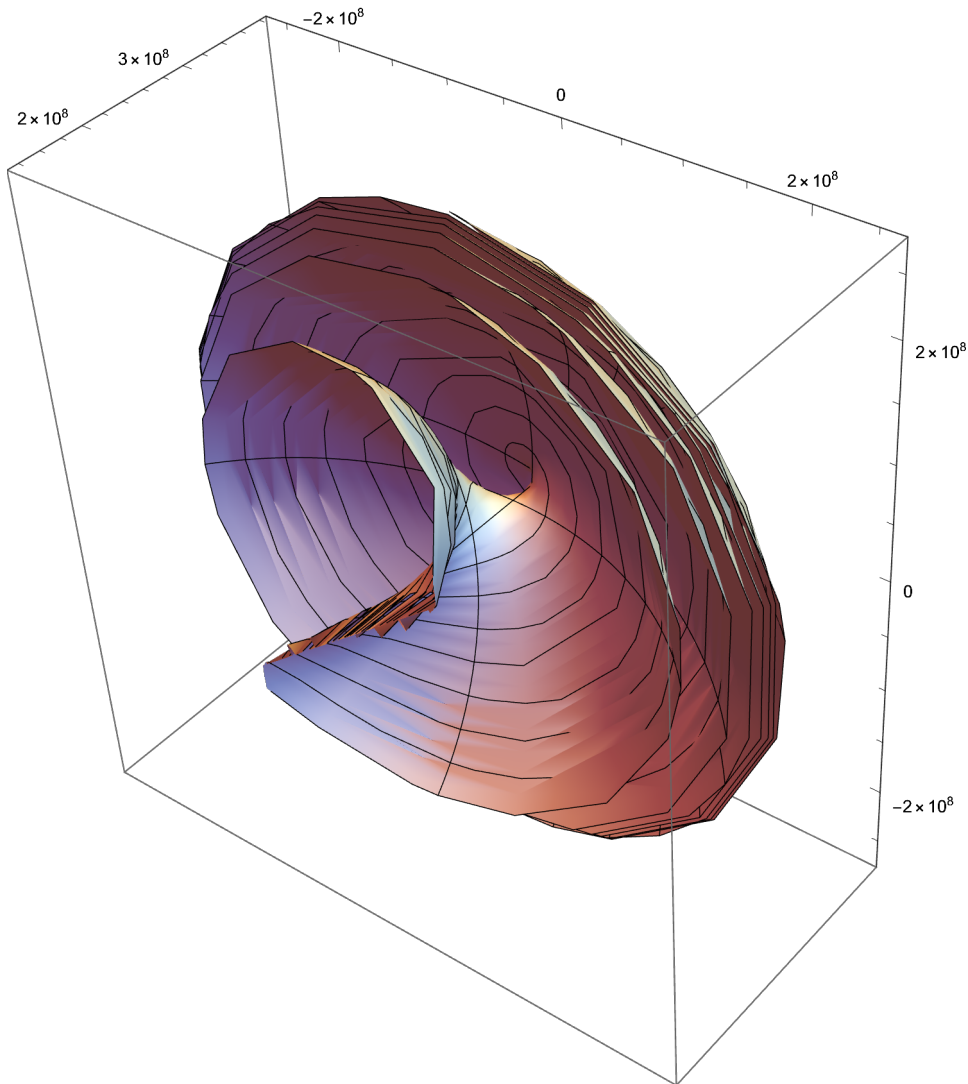


SphericalPlot3D $\left[c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}, \right.$   
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$



$$\text{SphericalPlot3D}\left[c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}}, \right.$$

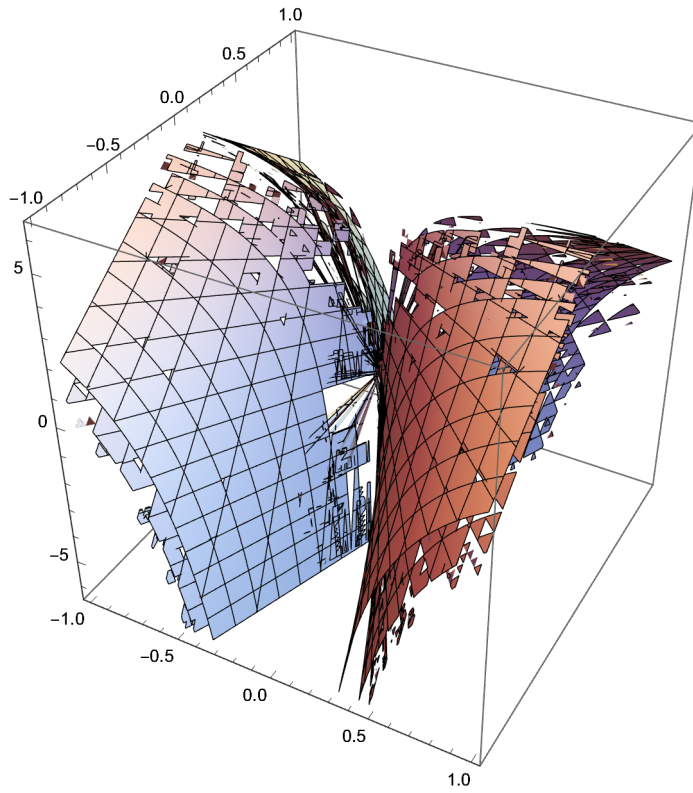
$$\left. \{\beta, -\pi/4, \pi/4\}, \{\theta, -4\pi, 4\pi\} \right]$$



$$\text{Solve}\left[\frac{2\pi r - r\theta}{2\pi} = \eta \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{c \sqrt{4\pi^2 - \frac{4\pi^2 r^2}{\eta^2} + \frac{4\pi r^2 \theta}{\eta^2} - \frac{r^2 \theta^2}{\eta^2}}}{2\pi} \right\}, \left\{ v \rightarrow \frac{c \sqrt{4\pi^2 - \frac{4\pi^2 r^2}{\eta^2} + \frac{4\pi r^2 \theta}{\eta^2} - \frac{r^2 \theta^2}{\eta^2}}}{2\pi} \right\} \right\}$$

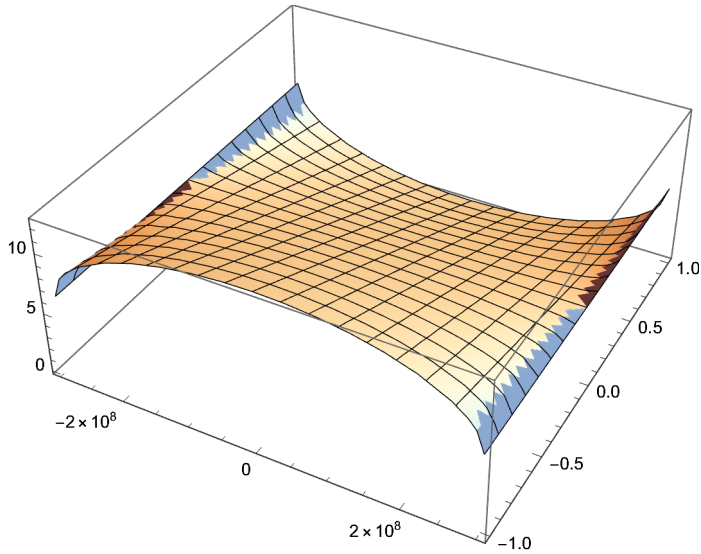
ContourPlot3D $\left[\frac{c \sqrt{4 \pi^2 - \frac{4 \pi^2 r^2}{\eta^2} + \frac{4 \pi r^2 \theta}{\eta^2} - \frac{r^2 \theta^2}{\eta^2}}}{2 \pi}, \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



Solve $\left[\frac{2 \pi r - r \theta}{2 \pi} = \eta \sqrt{1 - \frac{(v)^2}{c^2}}, \theta\right]$

$\left\{\left\{\theta \rightarrow -6.28319 \left(-1. + 1. \sqrt{1. - 1.11265 \times 10^{-17} v^2} \eta\right)\right\}\right\}$

```
Plot3D[-6.283186703443298`
  (-0.9999997777777779` + 1.`  $\sqrt{1.` - 1.1126500560536185` *^{-17} v^2 \eta}$ ), {v,
    -c, c}, {\eta, -1, 1}]
```



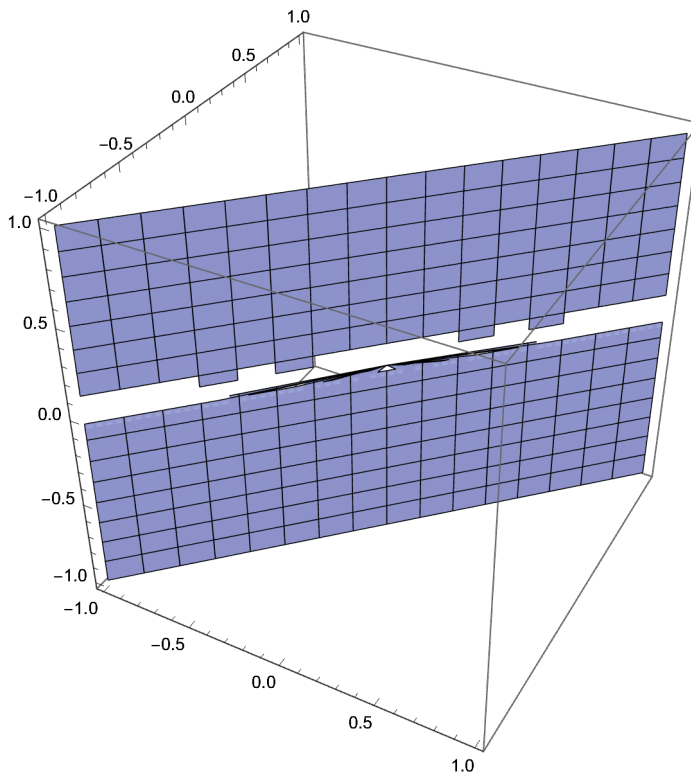
$2 \pi x - 2 \pi \eta' = \rho \eta$ , where  $\rho$  is an angle of a similar dimensional kind to theta, but different.

```
Solve[2  $\pi$  x - 2  $\pi$   $\eta'$  ==  $\rho \eta$ ,  $\rho$ ]
```

```
{ {  $\rho \rightarrow \frac{2 (\pi x - \pi \eta')}{\eta}$  } }
```

$\eta' = p$

ContourPlot3D $\left[\frac{2 (\pi x - \pi p)}{\eta}, \{x, -1, 1\}, \{p, -1, 1\}, \{\eta, -1, 1\}\right]$



Solve $\left[2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \eta' == \rho \eta, \rho\right]$

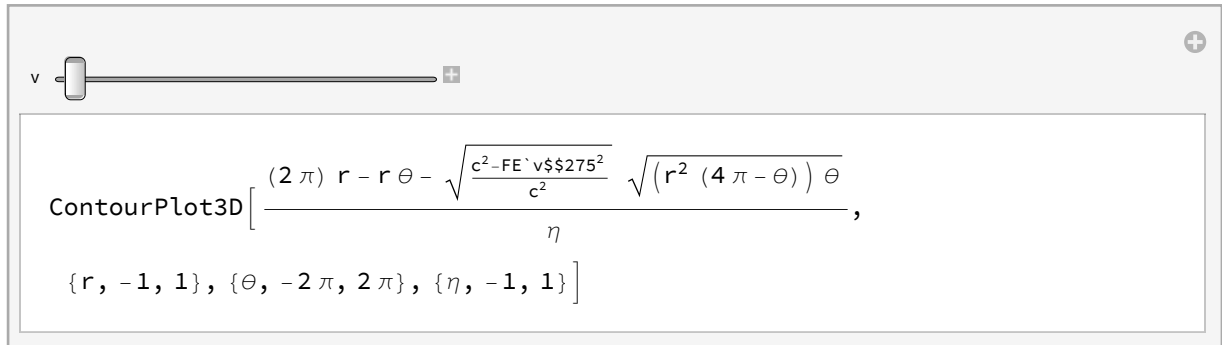
$\left\{\left\{\rho \rightarrow \frac{2 \pi r - r \theta - 2 \pi \eta'}{\eta}\right\}\right\}$

Solve $\left[2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \rho \eta, \rho\right]$

$\left\{\left\{\rho \rightarrow \frac{2 \pi r - r \theta - \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta}}{\eta}\right\}\right\}$

c := 2.99792458 (10<sup>8</sup>)

Manipulate[ContourPlot3D[ $\frac{2 \pi r - r \theta - \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta}}{\eta}$ ,  
 $\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}], \{v, -c, c\}]$



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

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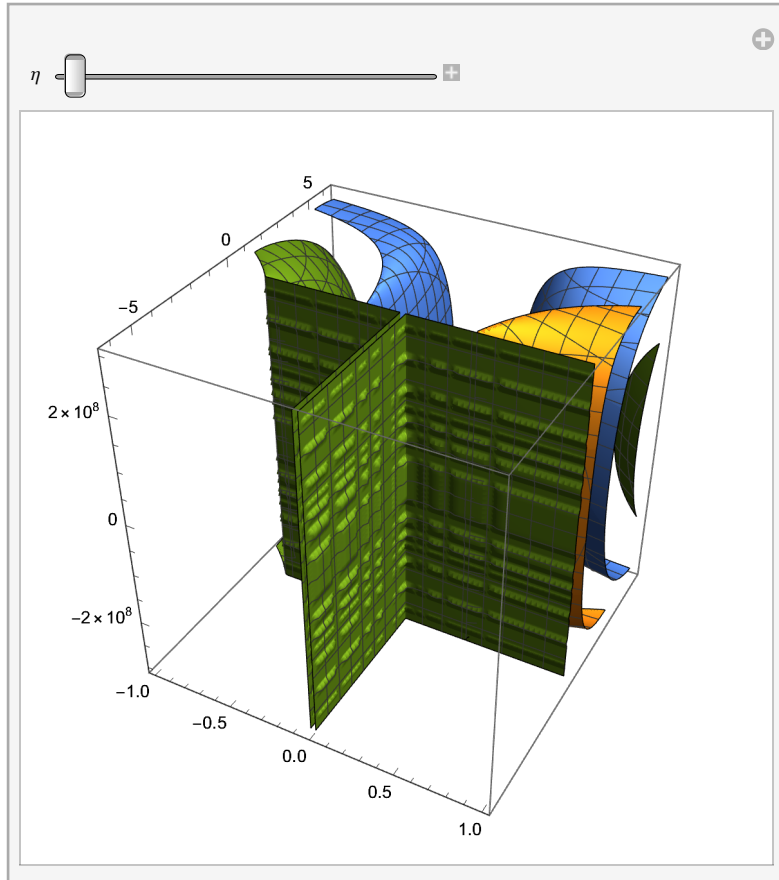
... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

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Manipulate[ContourPlot3D[ $\frac{2 \pi r - r \theta - \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta}}{\eta}$ ,  
 $\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{v, -c, c\}, \{\eta, -1, 1\}$ ]



ContourPlot3D::valuef :  $\frac{(2 \pi) r - r \theta - \sqrt{\frac{\text{Power}[\langle\langle 2 \rangle\rangle] + \langle\langle 1 \rangle\rangle}{\text{Power}[\langle\langle 2 \rangle\rangle]}} \sqrt{(\langle\langle 1 \rangle\rangle) \theta}}{\text{FE} \backslash \eta \$\$12}$  must be a numerical function. >>

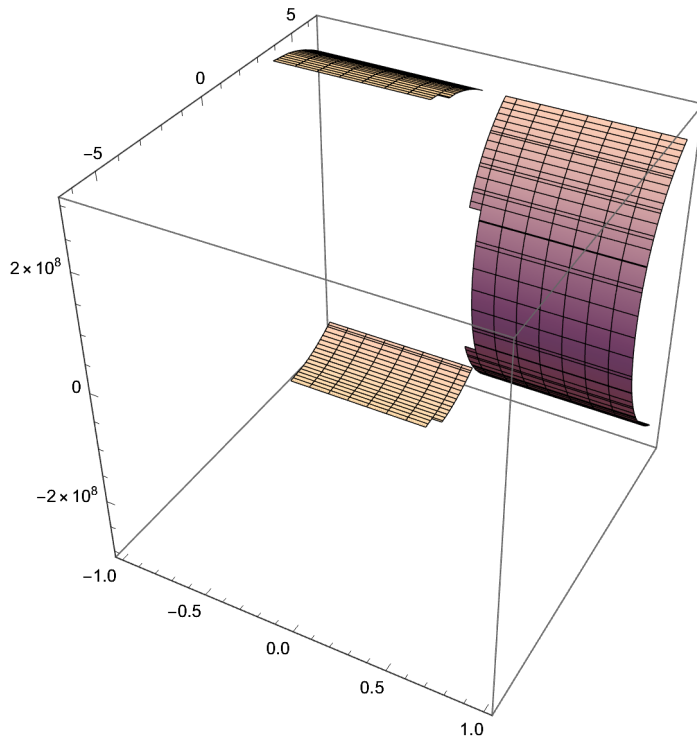
ContourPlot3D::valuef :  $\frac{(2 \pi) r - r \theta - \sqrt{\frac{\text{Power}[\langle\langle 2 \rangle\rangle] + \langle\langle 1 \rangle\rangle}{\text{Power}[\langle\langle 2 \rangle\rangle]}} \sqrt{(\langle\langle 1 \rangle\rangle) \theta}}{\text{FE} \backslash \eta \$\$12}$  must be a numerical function. >>

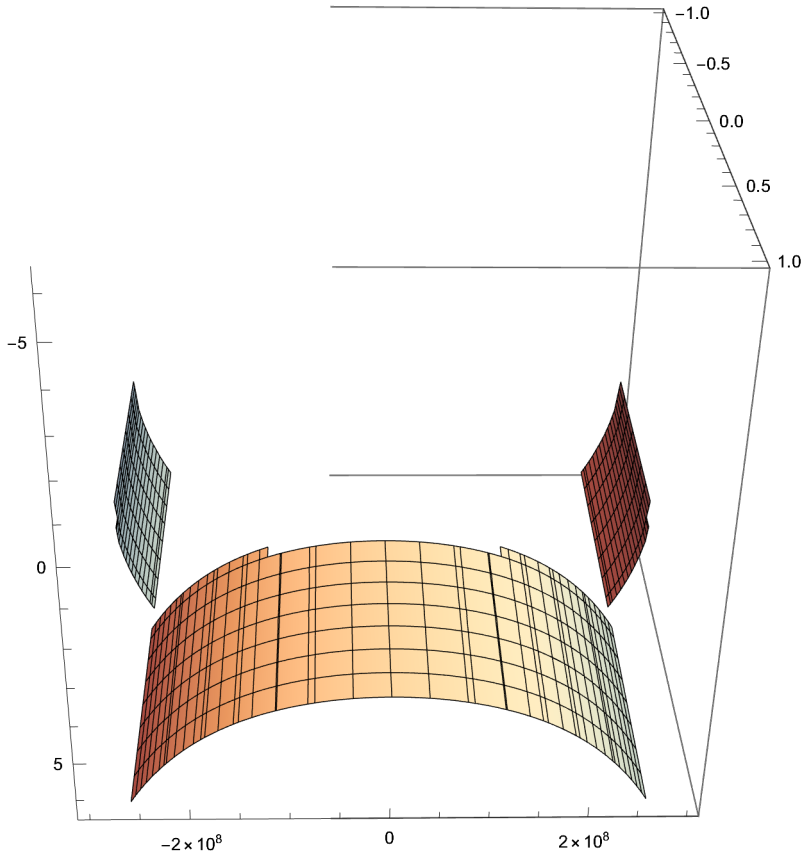
Solve[ $2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \rho \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \rho]$

$\left\{ \left\{ \rho \rightarrow - \frac{2 \pi \left( -2 \pi r + r \theta + \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta} \right)}{\sqrt{r^2 (4 \pi - \theta) \theta}} \right\} \right\}$

$$\text{ContourPlot3D}\left[-\frac{2\pi\left(-2\pi r+r\theta+\sqrt{\frac{c^2-v^2}{c^2}}\sqrt{r^2(4\pi-\theta)\theta}\right)}{\sqrt{r^2(4\pi-\theta)\theta}},\right.$$

$$\left.\{r,-1,1\},\{\theta,-2\pi,2\pi\},\{v,-c,c\}\right]$$



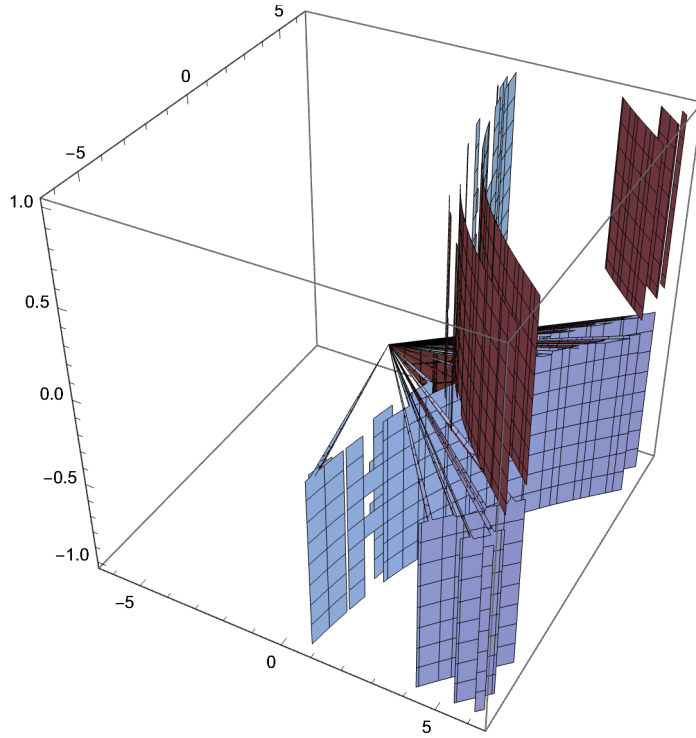


$$\text{Solve}\left[2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \rho \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1}{2 \pi} \left(\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta}} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r \theta} - c^2 \rho^2\right)\right\}, \left\{v \rightarrow \frac{1}{2 \pi} \left(\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta}} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r \theta} - c^2 \rho^2\right)\right\}\right\}$$

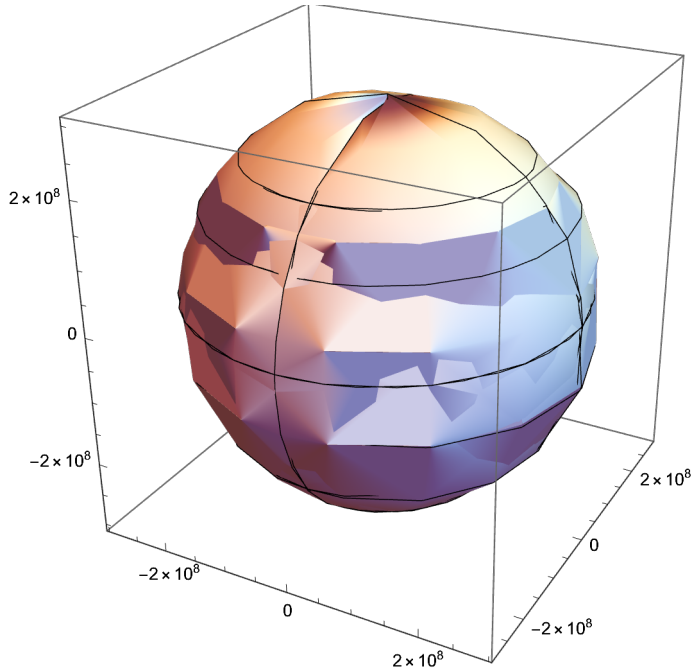
$$\left\{\left\{v \rightarrow -\frac{1}{2 \pi} \left(\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta}} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r \theta} - c^2 \rho^2\right)\right\}, \left\{v \rightarrow \frac{1}{2 \pi} \left(\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta}} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta \rho}}{r \theta} - c^2 \rho^2\right)\right\}\right\}$$

$\text{ContourPlot3D}\left[\frac{\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta} \rho}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta} \rho}{r \theta} - c^2 \rho^2}}{2 \pi},\right.$   
 $\left.\{\theta, -2 \pi, 2 \pi\}, \{\rho, -2 \pi, 2 \pi\}, \{r, -1, 1\}\right]$



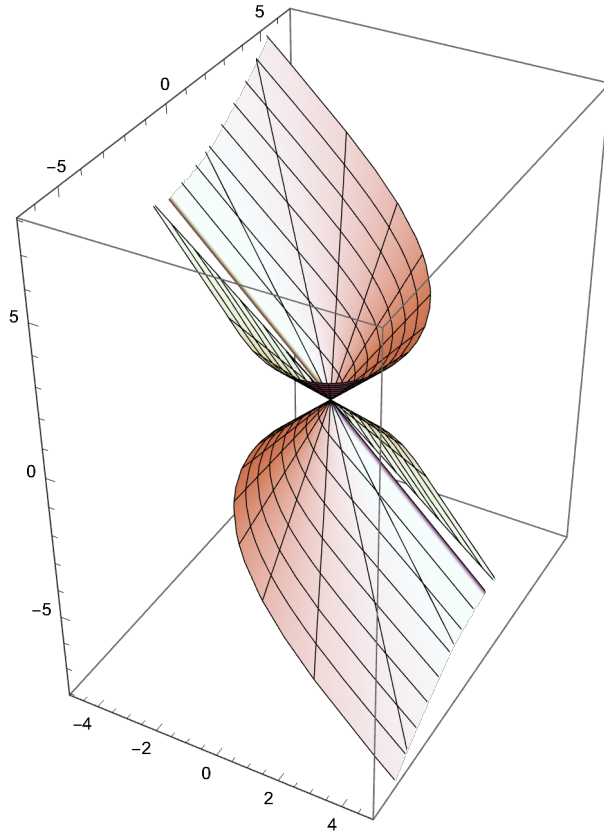
$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

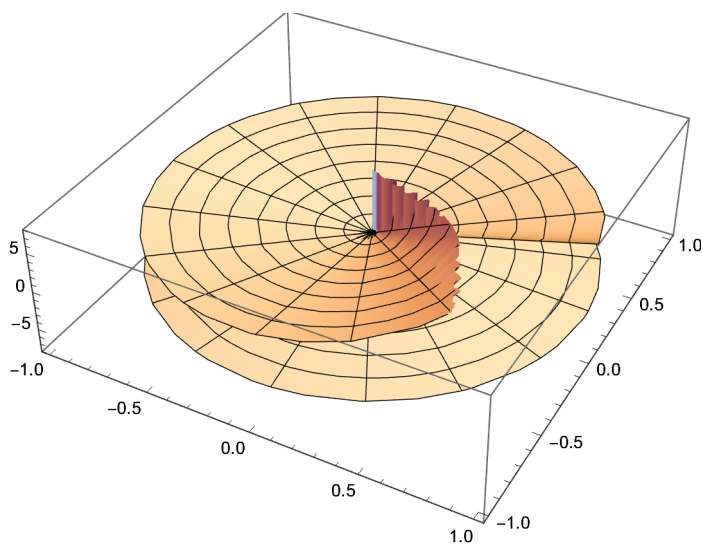
$$\text{SphericalPlot3D}\left[\frac{\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta} \rho}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta) \theta} \rho}{r \theta} - c^2 \rho^2}}{2 \pi},\right. \\ \left.\{\theta, -4 \pi, 4 \pi\}, \{\rho, -4 \pi, 4 \pi\}\right]$$



$$2 \pi \eta - 2 \pi x' = \theta \eta$$

$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi x' = \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right] \\ \left\{\left\{r \rightarrow -\frac{4 \pi^2 x'}{\sqrt{16 \pi^3 \theta - 20 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4}}\right\}, \left\{r \rightarrow \frac{4 \pi^2 x'}{\sqrt{16 \pi^3 \theta - 20 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\left\{-\frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}, \frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}\right\}, \{x', -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}, \{x', -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$


$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \theta \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 6.28319 -\right.\right.$$

$$\begin{aligned} & 0.5 \sqrt{\left(-78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \left(2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2\right) + \right.} \\ & \left. \left(4.37709 \times 10^{-46} \left(3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4\right)\right) \right\} / \\ & \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\ & \left. \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right)^{1/3} + \\ & 2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \\ & \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right)^{1/3} \Bigg) - \end{aligned}$$

$$\begin{aligned} & 0.5 \sqrt{\left(78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} \left(2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2\right) - \right.} \\ & \left. \left(4.37709 \times 10^{-46} \left(3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4\right)\right) \right\} / \\ & \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\ & \left. \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right)^{1/3} - \\ & 2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \\ & \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right)^{1/3} \Bigg) - \end{aligned}$$

$$\left(0.25 \left(15875.2 - 100.531 \left(236.871 - 4.39257 \times 10^{-16} v^2\right) - \right.\right.$$

$$\left. 8. \left(-992.201 + 5.51986 \times 10^{-15} v^2\right)\right) \Bigg) / \left(\sqrt{\left(-78.9568 + \right.\right.$$

$$\left. 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \left(2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2\right) + \right.$$

$$\left. \left(4.37709 \times 10^{-46} \left(3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4\right)\right) \right\} /$$

$$\left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right.$$

$$\left. \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right.$$

$$\left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right)^{1/3} +$$

$$2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times \right.$$

$$10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right.$$

$$\left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right)^{1/3} \Bigg) \Bigg\},$$

$$\left\{\theta \rightarrow 6.28319 - 0.5 \sqrt{\left(-78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \right.\right.$$

$$\begin{aligned}
& (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} + \\
& 2.7574 \times 10^{-46} (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \\
& 1.49725 \times 10^{89} v^6 + \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3}) + \\
& 0.5 \sqrt{(78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) - \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} - \\
& 2.7574 \times 10^{-46} (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \\
& 1.49725 \times 10^{89} v^6 + \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} - \\
& (0.25 (15875.2 - 100.531 (236.871 - 4.39257 \times 10^{-16} v^2) - \\
& 8. (-992.201 + 5.51986 \times 10^{-15} v^2))) / (\sqrt{(-78.9568 + \\
& 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} + \\
& 2.7574 \times 10^{-46} (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times \\
& 10^{89} v^6 + \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3})}) \}, \\
& \left\{ \theta \rightarrow 6.28319 + 0.5 \sqrt{(-78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \right. \\
& (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 -
\end{aligned}$$



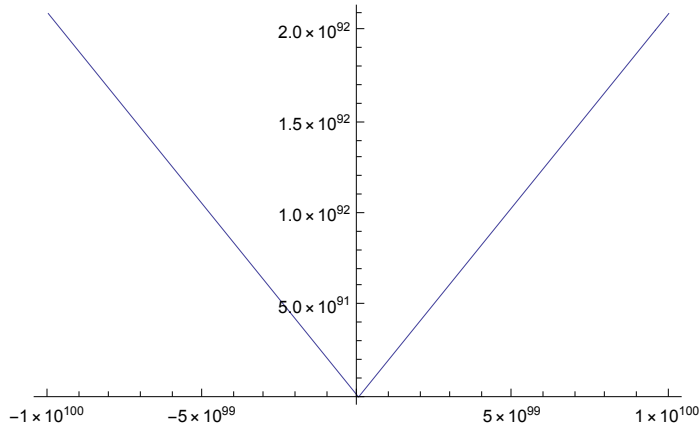
$$\begin{aligned}
& \left. \left( 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \\
& 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \\
& \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\
& \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} \Big) - \\
& 0.5 \sqrt{\left( 78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) - \right. \\
& \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) \Big/ \\
& \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\
& \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\
& \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} - \\
& 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \\
& \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\
& \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \\
& \left. \left( 0.25 \left( 15875.2 - 100.531 \left( 236.871 - 4.39257 \times 10^{-16} v^2 \right) - \right. \right. \right. \\
& \left. \left. 8. \left( -992.201 + 5.51986 \times 10^{-15} v^2 \right) \right) \right) \Big/ \left( \sqrt{\left( -78.9568 + \right. \right. \\
& \left. \left. 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) + \right. \right. \\
& \left. \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) \Big/ \right. \\
& \left. \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \right. \\
& \left. \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \right. \\
& \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times \right. \right. \\
& \left. \left. 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} \right) \Big) \Big) \Big\}, \\
& \left\{ \theta \rightarrow 6.28319 + 0.5 \sqrt{\left( -78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \right. \right. \\
& \left. \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) + \right. \\
& \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) \Big/ \\
& \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\
& \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\
& \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \right. \\
& \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \right. \\
& \left. \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right)^{1/3} + \\
& 0.5 \sqrt{\left( 78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) - \right. \\
& \left. \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) / \right. \\
& \left. \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \right. \\
& \left. \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} - \right. \\
& \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \right. \\
& \left. \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \right. \\
& \left. \left( 0.25 \left( 15875.2 - 100.531 \left( 236.871 - 4.39257 \times 10^{-16} v^2 \right) - \right. \right. \\
& \left. \left. 8. \left( -992.201 + 5.51986 \times 10^{-15} v^2 \right) \right) \right) / \left( \sqrt{\left( -78.9568 + \right. \right. \\
& \left. \left. 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) + \right. \right. \\
& \left. \left. \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) / \right. \right. \\
& \left. \left. \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \right. \right. \\
& \left. \left. \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \right. \\
& \left. \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \right. \right. \\
& \left. \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times \right. \right. \right. \\
& \left. \left. \left. 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \right. \\
& \left. \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} \right) \right) \} \} \}
\end{aligned}$$

Plot[6.283185307179586` +

$$\begin{aligned}
& 0.5 \sqrt{\left( -78.95683520871486 + 4.392566356039645 \times 10^{-16} v^2 + 3.474101948670718 \times 10^{-46} \right. \\
& \left. \left( 2.2727264880331392 \times 10^{47} - 4.2145820905076925 \times 10^{29} v^2 \right) + \right. \\
& \left. \left( 4.377094174611036 \times 10^{-46} \left( 3.0319879916202416 \times 10^{62} + \right. \right. \right. \\
& \left. \left. \left. 6.555025201979783 \times 10^{60} v^2 + 1.776270219762819 \times 10^{59} v^4 \right) \right) / \right. \\
& \left. \left( 8.274653940104402 \times 10^{109} - 1.3805000153057876 \times 10^{93} v^2 - \right. \right. \\
& \left. \left. 8.288007545727168 \times 10^{90} v^4 - 1.497247331222908 \times 10^{89} v^6 + \right. \right. \\
& \left. \left. \sqrt{\left( 6.846989782848531 \times 10^{219} - 2.2846319781928445 \times 10^{203} v^2 - \right. \right. \right. \\
& \left. \left. \left. 1.371607885877325 \times 10^{201} v^4 - 2.477840705722886 \times 10^{199} v^6 + \right. \right. \right. \\
& \left. \left. \left. 2.7569696001145084 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \right)^{1/3} + \right. \\
& \left. 2.7573965439823348 \times 10^{-46} \left( 8.274653940104402 \times 10^{109} - 1.3805000153057876 \times 10^{93} \right. \right. \\
& \left. \left. v^2 - 8.288007545727168 \times 10^{90} v^4 - 1.497247331222908 \times 10^{89} v^6 + \right. \right. \\
& \left. \left. \sqrt{\left( 6.846989782848531 \times 10^{219} - 2.2846319781928445 \times 10^{203} v^2 - \right. \right. \right. \\
& \left. \left. \left. 1.371607885877325 \times 10^{201} v^4 - 2.477840705722886 \times 10^{199} v^6 + \right. \right. \right.
\end{aligned}$$

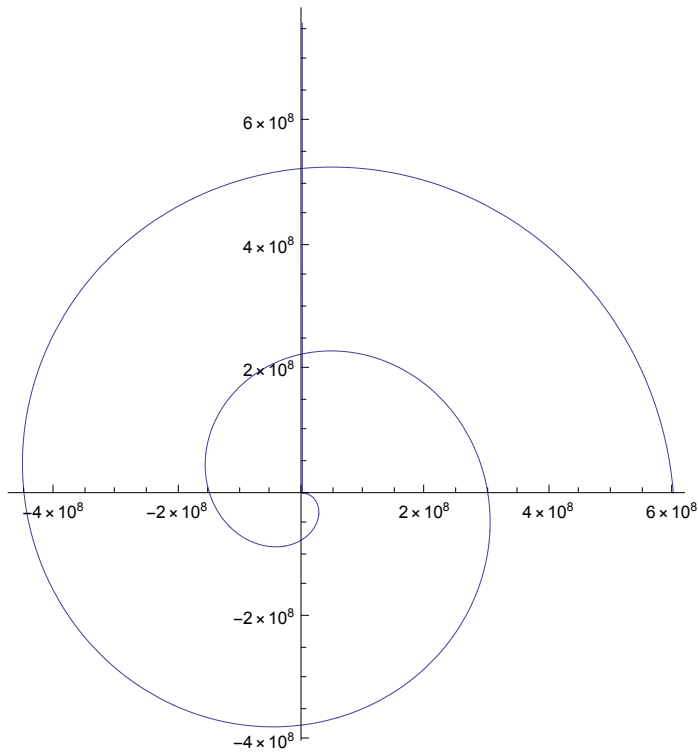
$$\begin{aligned}
& 2.7569696001145084 \cdot v^{182} + 0 \cdot v^{10} + 0 \cdot v^{12} \Big)^{1/3} \Big) + \\
& 0.5 \cdot \sqrt{\Big( 78.95683520871488 + 4.392566356039645 \cdot v^{-16} v^2 - \\
& 3.474101948670718 \cdot v^{-46} \\
& \quad \big( 2.2727264880331392 \cdot v^{47} - 4.2145820905076925 \cdot v^{29} v^2 \big) - \\
& \quad \big( 4.377094174611036 \cdot v^{-46} \big( 3.0319879916202416 \cdot v^{62} + \\
& \quad \quad 6.555025201979783 \cdot v^{60} v^2 + 1.776270219762819 \cdot v^{59} v^4 \big) \Big) \Big) / \\
& \quad \big( 8.274653940104402 \cdot v^{109} - 1.3805000153057876 \cdot v^{93} v^2 - \\
& \quad 8.288007545727168 \cdot v^{90} v^4 - 1.497247331222908 \cdot v^{89} v^6 + \\
& \quad \sqrt{\big( 6.846989782848531 \cdot v^{219} - 2.2846319781928445 \cdot v^{203} v^2 - \\
& \quad 1.371607885877325 \cdot v^{201} v^4 - 2.477840705722886 \cdot v^{199} v^6 + \\
& \quad 2.7569696001145084 \cdot v^{182} v^8 + 0 \cdot v^{10} + 0 \cdot v^{12} \big) \Big)^{1/3} - \\
& 2.7573965439823348 \cdot v^{-46} \big( 8.274653940104402 \cdot v^{109} - 1.3805000153057876 \cdot v^{93} \\
& \quad v^2 - 8.288007545727168 \cdot v^{90} v^4 - 1.497247331222908 \cdot v^{89} v^6 + \\
& \quad \sqrt{\big( 6.846989782848531 \cdot v^{219} - 2.2846319781928445 \cdot v^{203} v^2 - \\
& \quad 1.371607885877325 \cdot v^{201} v^4 - 2.477840705722886 \cdot v^{199} v^6 + \\
& \quad 2.7569696001145084 \cdot v^{182} v^8 + 0 \cdot v^{10} + 0 \cdot v^{12} \big) \Big)^{1/3} + \\
& \big( 0.25 \cdot \big( 15875.213660313508 - 100.53096491487338 \cdot \\
& \quad \big( 236.8705056261446 - 4.392566356039645 \cdot v^{-16} v^2 \big) - \\
& \quad 8 \cdot \big( -992.2008537695941 + 5.519861677815934 \cdot v^{-15} v^2 \big) \big) \Big) \Big) / \\
& \quad \Big( \sqrt{\big( -78.95683520871486 + 4.392566356039645 \cdot v^{-16} v^2 + \\
& \quad 3.474101948670718 \cdot v^{-46} \\
& \quad \big( 2.2727264880331392 \cdot v^{47} - 4.2145820905076925 \cdot v^{29} v^2 \big) + \\
& \quad \big( 4.377094174611036 \cdot v^{-46} \big( 3.0319879916202416 \cdot v^{62} + \\
& \quad \quad 6.555025201979783 \cdot v^{60} v^2 + 1.776270219762819 \cdot v^{59} v^4 \big) \Big) \Big) / \\
& \quad \big( 8.274653940104402 \cdot v^{109} - 1.3805000153057876 \cdot v^{93} v^2 - \\
& \quad 8.288007545727168 \cdot v^{90} v^4 - 1.497247331222908 \cdot v^{89} v^6 + \\
& \quad \sqrt{\big( 6.846989782848531 \cdot v^{219} - 2.2846319781928445 \cdot v^{203} v^2 - \\
& \quad 1.371607885877325 \cdot v^{201} v^4 - 2.477840705722886 \cdot v^{199} v^6 + \\
& \quad 2.7569696001145084 \cdot v^{182} v^8 + 0 \cdot v^{10} + 0 \cdot v^{12} \big) \Big)^{1/3} + \\
& 2.7573965439823348 \cdot v^{-46} \big( 8.274653940104402 \cdot v^{109} - \\
& \quad 1.3805000153057876 \cdot v^{93} v^2 - 8.288007545727168 \cdot v^{90} v^4 - \\
& \quad 1.497247331222908 \cdot v^{89} v^6 + \sqrt{\big( 6.846989782848531 \cdot v^{219} - \\
& \quad 2.2846319781928445 \cdot v^{203} v^2 - 1.371607885877325 \cdot v^{201} v^4 - \\
& \quad 2.477840705722886 \cdot v^{199} v^6 + 2.7569696001145084 \cdot v^{182} v^8 + \\
& \quad 0 \cdot v^{10} + 0 \cdot v^{12} \big) \Big)^{1/3} \Big) \Big) \Big), \{v, -10^{100}, 10^{100}\} \Big]
\end{aligned}$$



$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{(c)^2}} = \theta \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, v\right]$$

$$\left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( 1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 2.27273 \times 10^{47} \theta^2 - 2.41144 \times 10^{46} \theta^3 + 9.59481 \times 10^{44} \theta^4 \right) } \right) / \left( \sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2} \right) \right\}, \right. \\ \left. \left\{ v \rightarrow \left( \sqrt{ \left( 1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 2.27273 \times 10^{47} \theta^2 - 2.41144 \times 10^{46} \theta^3 + 9.59481 \times 10^{44} \theta^4 \right) } \right) / \left( \sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2} \right) \right\} \right\}$$

```
PolarPlot[
  (√(1.495394089917615`*^48 - 9.519974451231788`*^47 θ + 2.2727264880331392`*^47 θ² -
    2.4114376991090496`*^46 θ³ + 9.594805744283795`*^44 θ⁴)) /
  (√(1.663850317969084`*^31 - 5.296200053396031`*^30 θ +
    4.2145820905076925`*^29 θ²)), {θ, -2 π, 2 π}]
```



## Light

$$2 \pi r - 2 \pi x = \theta r$$

$$\text{Solve}\left[2 \pi r - 2 \pi r \sqrt{1 - \frac{(v)^2}{c^2}} = \theta r, v\right]$$

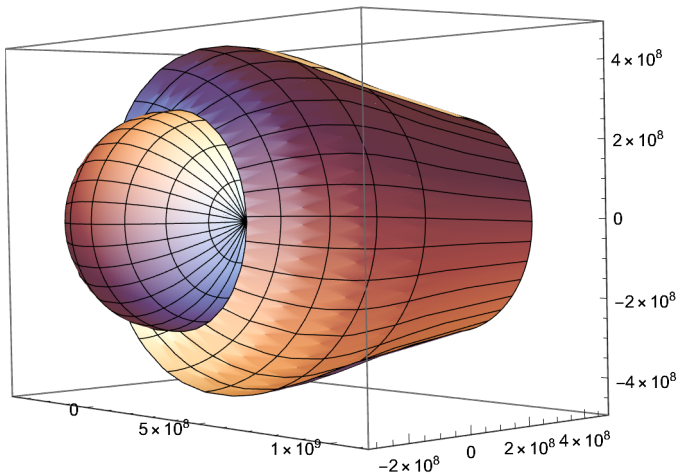
$$\left\{\left\{v \rightarrow -\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}, \left\{v \rightarrow \frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi} == \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), c\right]$$

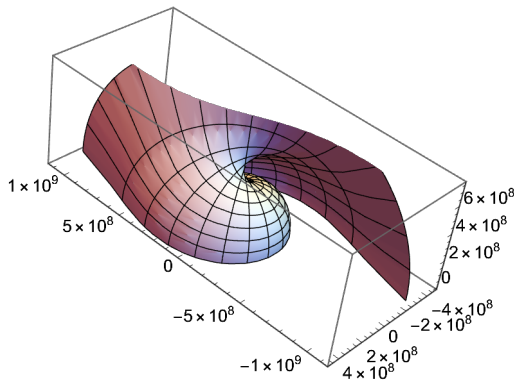
$$\left\{\left\{c \rightarrow -\left(1. \sqrt{2.02015 \times 10^{40} \theta - 1.60758 \times 10^{39} \theta^2 - 6.34649 \times 10^{40} \sin[\beta]^2}\right) / \left(\sqrt{\theta} \sqrt{(7.15472 \times 10^{22} \theta - 1.13871 \times 10^{22} \theta^2 + 4.53078 \times 10^{20} \theta^3 - 2.24772 \times 10^{23} \sin[\beta]^2 + 1.78868 \times 10^{22} \theta \sin[\beta]^2)}\right)\right\}, \right.$$

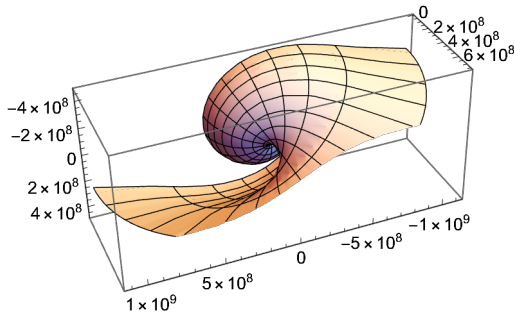
$$\left.\left\{c \rightarrow \left(\sqrt{2.02015 \times 10^{40} \theta - 1.60758 \times 10^{39} \theta^2 - 6.34649 \times 10^{40} \sin[\beta]^2}\right) / \left(\sqrt{\theta} \sqrt{(7.15472 \times 10^{22} \theta - 1.13871 \times 10^{22} \theta^2 + 4.53078 \times 10^{20} \theta^3 - 2.24772 \times 10^{23} \sin[\beta]^2 + 1.78868 \times 10^{22} \theta \sin[\beta]^2)}\right)\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\left(\sqrt{(2.0201505625374124 \cdot 10^{40} \theta - 1.607584739088511 \cdot 10^{39} \theta^2 - 6.346490166412822 \cdot 10^{40} \sin[\beta]^2)}\right) / \left(\sqrt{\theta} \sqrt{(7.154717000231094 \cdot 10^{22} \theta - 1.138708577010396 \cdot 10^{22} \theta^2 + 4.530777469308567 \cdot 10^{20} \theta^3 - 2.2477206366440006 \cdot 10^{23} \sin[\beta]^2 + 1.7886792500577734 \cdot 10^{22} \theta \sin[\beta]^2)}\right)\right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



SphericalPlot3D $\left[\left(\sqrt{\left(2.0201505625374124 \cdot 10^{40} \theta - 1.607584739088511 \cdot 10^{39} \theta^2 - 6.346490166412822 \cdot 10^{40} \sin^2[\beta]\right)}\right) / \left(\sqrt{\theta} \sqrt{\left(7.154717000231094 \cdot 10^{22} \theta - 1.138708577010396 \cdot 10^{22} \theta^2 + 4.530777469308567 \cdot 10^{20} \theta^3 - 2.2477206366440006 \cdot 10^{23} \sin^2[\beta] + 1.7886792500577734 \cdot 10^{22} \theta \sin^2[\beta]\right)}\right)\right], \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]$





$c := 2.99792458 (10^8)$

$$\text{Solve}\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi} == \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \beta\right]$$

$$\left\{\left\{\beta \rightarrow -1.\right.\right.$$

$$\text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{\left(6.43991 \times 10^{46} - 2.56236 \times 10^{46} \theta + 3.2625 \times 10^{45} \theta^2 - 1.29811 \times 10^{44} \theta^3\right)}\right) / \left(\sqrt{2.02316 \times 10^{47} - 6.43991 \times 10^{46} \theta + 5.12472 \times 10^{45} \theta^2}\right)\right]\right\},$$

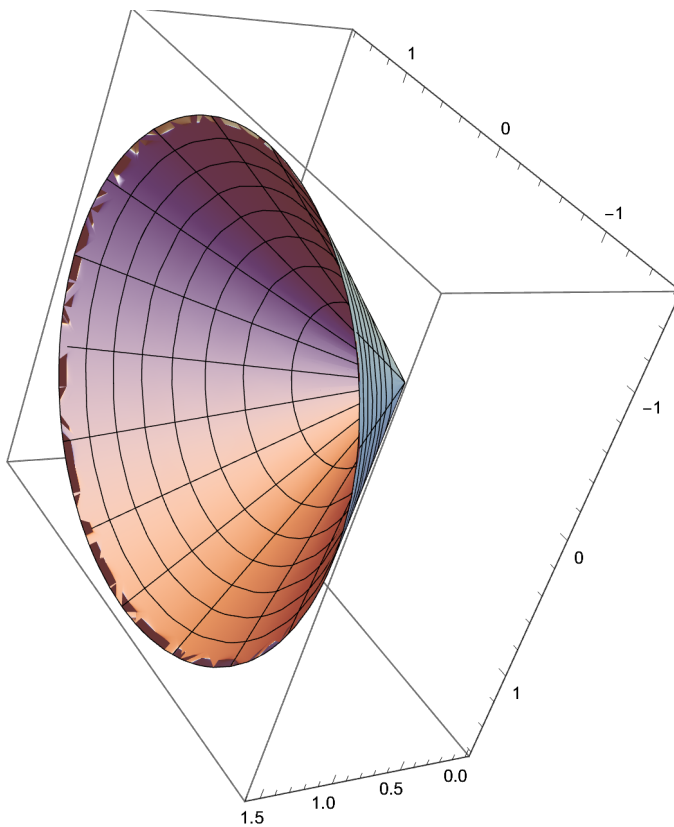
$$\left\{\beta \rightarrow \text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{\left(6.43991 \times 10^{46} - 2.56236 \times 10^{46} \theta + 3.2625 \times 10^{45} \theta^2 - 1.29811 \times 10^{44} \theta^3\right)}\right) / \left(\sqrt{2.02316 \times 10^{47} - 6.43991 \times 10^{46} \theta + 5.12472 \times 10^{45} \theta^2}\right)\right]\right\}\right\}$$



```

RevolutionPlot3D[
  { -1. ` ArcSin[ (  $\sqrt{\theta} \sqrt{(6.439907533884034 \cdot 10^{-46} - 2.562357792680954 \cdot 10^{-46} \theta +$ 
     $3.2624952694016945 \cdot 10^{-45} \theta^2 - 1.298105622348011 \cdot 10^{-44} \theta^3)}$  ) ) /
    (  $\sqrt{(2.0231566198247644 \cdot 10^{-47} - 6.439907533884035 \cdot 10^{-46} \theta +$ 
     $5.124715585361908 \cdot 10^{-45} \theta^2)}$  ) ) ],
  ArcSin[ (  $\sqrt{\theta} \sqrt{(6.439907533884034 \cdot 10^{-46} - 2.562357792680954 \cdot 10^{-46} \theta +$ 
     $3.2624952694016945 \cdot 10^{-45} \theta^2 - 1.298105622348011 \cdot 10^{-44} \theta^3)}$  ) ) /
    (  $\sqrt{(2.0231566198247644 \cdot 10^{-47} - 6.439907533884035 \cdot 10^{-46} \theta +$ 
     $5.124715585361908 \cdot 10^{-45} \theta^2)}$  ) ) ] ], { $\theta$ , -4  $\pi$ , 4  $\pi$ ] ]

```

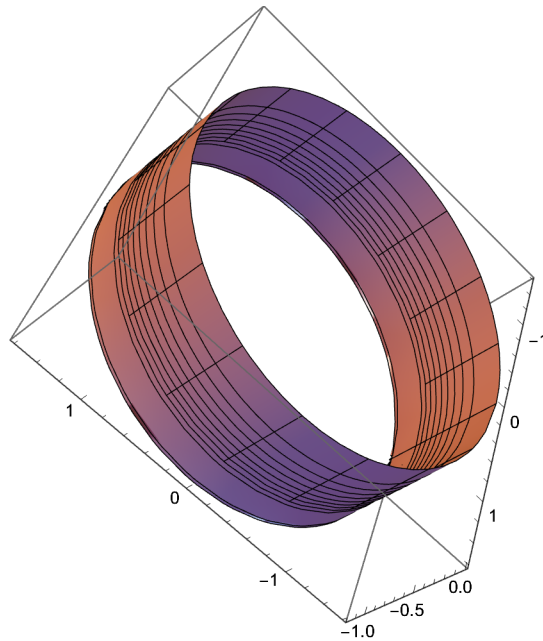


$$\begin{aligned}
& \text{Solve}\left[\frac{\sqrt{4 c^2 \pi^2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) - c^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2 \pi} == \right. \\
& \quad \left. \left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + \right. \right. \right. \\
& \quad \quad \left. \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right)} \right/ \\
& \quad \left. \left(\sqrt{-12.566370614359172 \cdot 10^0 \theta + \theta^2 + 39.47841760435743 \cdot 10^0 \sin[\beta]^2}\right), \beta\right] \\
& \left\{\left\{\beta \rightarrow -1. \right. \right. \\
& \quad \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) - 2. \sqrt{\left(-8.09397 \times 10^{-41} \left(1.57307 \times \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}, \\
& \left\{\beta \rightarrow \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) - 2. \sqrt{\left(-8.09397 \times 10^{-41} \right. \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. \left(1.57307 \times 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}, \\
& \left\{\beta \rightarrow -1. \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) + 2. \sqrt{\left(-8.09397 \times 10^{-41} \right. \right. \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. \left(1.57307 \times 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}, \\
& \left\{\beta \rightarrow \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) + 2. \sqrt{\left(-8.09397 \times 10^{-41} \right. \right. \right. \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. \left(1.57307 \times 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}
\end{aligned}$$

```

RevolutionPlot3D[
  {
    -1. `ArcSin[0.5 `Sqrt[(-2. `(-0.9999999999999999 - 0.3183098861837907 `theta +
      0.025330295910584444 `theta^2) +
      2. `Sqrt[(-8.093971489670607 `*^-41 (1.573071447508865 `*^40 -
        1.2518104835387941 `*^39 theta) theta + (-0.9999999999999999 -
        0.3183098861837907 `theta + 0.025330295910584444 `theta^2)^2)]]],
    -1. `ArcSin[0.5 `Sqrt[(-2. `(-0.9999999999999999 - 0.3183098861837907 `theta +
      0.025330295910584444 `theta^2) - 2. `Sqrt[(-8.093971489670607 `*^-41
        (1.573071447508865 `*^40 - 1.2518104835387941 `*^39 theta) theta +
        (-0.9999999999999999 - 0.3183098861837907 `theta +
        0.025330295910584444 `theta^2)^2)]]], {theta, -8 pi, 8 pi}]

```



# "Conic" Relativity: Expositions of Relativity through Difference in Circumferences of Two Circles

In this paper,

I will perform a "limited" exposition of the general principle,  $\theta r =$

$$2 \pi r - 2 \pi x = 2 \pi r - 2 \pi r' = 2 \pi r - 2 \pi r \sqrt{1 - \frac{(v)^2}{c^2}} = 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2},$$

from the algebraicized geometry of a cone combined with the relativistic length contraction first suggested by Einstein's application of the Lorentz transformation in his theory of relativity. The exposition is limited. I will only solve equations for expressions of velocity and expressions of angle measure. I will not make substitutions. The system is multi-variant in the sense that there are so many different possible combinations of algebraic forms that one would have to take a very long extended exposition in order to visualize all of them.

"The language of matter expresses the same quality of motion as the meaning of the creative thought/idea field. In order to perceive motion, one must set aside certain quantifiable characteristics of the existence of transformation. This leads to insight into a relationship and mutual interpenetration of mathematics and ethics." - Emerson

For more information about how Einstein applied the Lorentz transformation to describe length contraction, see :

**Einstein, Albert. Relativity : The Special and the General Theory (Classic Reprint). Forgotten Books, 2010. Print.**

This is an original interpretation of the notion of a length contraction as it would relate to the difference in circumferences of two circles.

## Table of Contents :

### 1. Conic Relativity: "General Relativity" Circumferential Cone-Difference Functions

Height of the cone equals

the length contracted initial radius :

$$\eta = r' = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} =$$

$$r \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} =$$

$$\left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right.$$

$$\begin{aligned}
& \left( \frac{4 \pi^2 \operatorname{Sin}[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{\theta}}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right) \sqrt{1 - \frac{(\mathbf{v})^2}{\mathbf{c}^2}} = \\
& \left( \left( -8 \pi^3 + 4 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\beta] + 8 \pi^2 \theta \operatorname{Csc}[\beta]^2 - \right. \right. \\
& \left. \left. 2 \pi \theta^2 \operatorname{Csc}[\beta]^2 - 4 \pi \theta \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\beta]^3 + \right. \right. \\
& \left. \left. \theta^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\beta]^3 \right) / \right. \\
& \left. \left( 4 \left( 8 \pi^4 - 4 \pi^3 \theta - 8 \pi^3 \theta \operatorname{Csc}[\beta]^2 + 6 \pi^2 \theta^2 \operatorname{Csc}[\beta]^2 - \right. \right. \right. \\
& \left. \left. \left. \pi \theta^3 \operatorname{Csc}[\beta]^2 \right) \right) \right) \sqrt{1 - \frac{(\mathbf{v})^2}{\mathbf{c}^2}} = \\
& \left( \left( -4 \pi^2 - 4 \pi \gamma - \gamma^2 + \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Csc}[\beta] + \right. \right. \\
& \left. \left. 4 \pi \gamma \operatorname{Csc}[\beta]^2 + \gamma^2 \operatorname{Csc}[\beta]^2 - \right. \right. \\
& \left. \left. \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Csc}[\beta]^3 + \right. \right. \\
& \left. \left. \frac{4 \pi^2 \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Csc}[\beta]^3}{(2 \pi + \gamma)^2} \right) / \right. \\
& \left. \left( \pi \left( -16 \pi^2 - 16 \pi \gamma - 4 \gamma^2 + 16 \pi \gamma \operatorname{Csc}[\beta]^2 + 4 \right. \right. \right. \\
& \left. \left. \left. \gamma^2 \operatorname{Csc}[\beta]^2 \right) \right) \right) \sqrt{1 - \frac{(\mathbf{v})^2}{\mathbf{c}^2}} = \\
& \left( \left( 4 \pi \gamma + \gamma^2 - \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Sin}[\beta] - \right. \right. \\
& \left. \left. 4 \pi^2 \operatorname{Sin}[\beta]^2 - 4 \pi \gamma \operatorname{Sin}[\beta]^2 - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \gamma^2 \text{Sin}[\beta]^2 - \frac{\pi \sqrt{\gamma} \sqrt{(2\pi + \gamma)^2} \text{Sin}[\beta]^3}{\sqrt{4\pi + \gamma}} + \\
& \frac{\pi \sqrt{(2\pi + \gamma)^2} \sqrt{4\pi + \gamma} \text{Sin}[\beta]^3}{\sqrt{\gamma}} + \\
& \left. \sqrt{\gamma} \sqrt{(2\pi + \gamma)^2} \sqrt{4\pi + \gamma} \text{Sin}[\beta]^3 \right) / \\
& \left( \pi \left( -16\pi\gamma - 4\gamma^2 + 16\pi^2 \text{Sin}[\beta]^2 + 16\pi\gamma \right. \right. \\
& \left. \left. \text{Sin}[\beta]^2 + 4\gamma^2 \text{Sin}[\beta]^2 \right) \right) \sqrt{1 - \frac{(v)^2}{c^2}}
\end{aligned}$$

$2\pi\eta - 2\pi r' = \phi\eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different.

$$2\pi\eta - 2\pi r' = \theta\eta$$

$2\pi r' - 2\pi\eta = \phi\eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different. - This section is not visualized in this paper, but implied.

$2\pi r - 2\pi\eta = \theta\eta$  - This section will not be visualized in this paper, but is implied.

Changed radius equals the

length contracted initial radius :

$$\begin{aligned}
x = r' &= \frac{2\pi r - r\theta}{2\pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \\
& \left( \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta] + \right. \right. \\
& \left. \left. 4\pi^2 \text{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]^3}{4\pi - \theta} - \right. \right. \\
& \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]^3}{\theta} \right) \right) / \left( 16\pi^2\theta - 12\pi\theta^2 + \right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \left( 2 \theta^3 - 16 \pi^3 \operatorname{Sin}[\beta]^2 + 8 \pi^2 \theta \operatorname{Sin}[\beta]^2 \right) \right) \sqrt{1 - \frac{(\mathbf{v})^2}{\mathbf{c}^2}} = \\
 & \left( \left( -8 \pi^3 + 4 \pi^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\beta] + 8 \pi^2 \theta \operatorname{Csc}[\beta]^2 - \right. \right. \\
 & \quad 2 \pi \theta^2 \operatorname{Csc}[\beta]^2 - 4 \pi \theta \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\beta]^3 + \\
 & \quad \left. \left. \theta^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\beta]^3 \right) / \right. \\
 & \quad \left( 4 \left( 8 \pi^4 - 4 \pi^3 \theta - 8 \pi^3 \theta \operatorname{Csc}[\beta]^2 + 6 \pi^2 \theta^2 \operatorname{Csc}[\beta]^2 - \right. \right. \\
 & \quad \left. \left. \pi \theta^3 \operatorname{Csc}[\beta]^2 \right) \right) \sqrt{1 - \frac{(\mathbf{v})^2}{\mathbf{c}^2}} = \\
 & \left( \left( -4 \pi^2 - 4 \pi \gamma - \gamma^2 + \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Csc}[\beta] + \right. \right. \\
 & \quad 4 \pi \gamma \operatorname{Csc}[\beta]^2 + \gamma^2 \operatorname{Csc}[\beta]^2 - \\
 & \quad \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Csc}[\beta]^3 + \\
 & \quad \left. \left. \frac{4 \pi^2 \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Csc}[\beta]^3}{(2 \pi + \gamma)^2} \right) / \right. \\
 & \quad \left( \pi \left( -16 \pi^2 - 16 \pi \gamma - 4 \gamma^2 + 16 \pi \gamma \operatorname{Csc}[\beta]^2 + 4 \right. \right. \\
 & \quad \left. \left. \gamma^2 \operatorname{Csc}[\beta]^2 \right) \right) \sqrt{1 - \frac{(\mathbf{v})^2}{\mathbf{c}^2}} = \\
 & \left( \left( 4 \pi \gamma + \gamma^2 - \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Sin}[\beta] - \right. \right. \\
 & \quad 4 \pi^2 \operatorname{Sin}[\beta]^2 - 4 \pi \gamma \operatorname{Sin}[\beta]^2 - \\
 & \quad \gamma^2 \operatorname{Sin}[\beta]^2 - \frac{\pi \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \operatorname{Sin}[\beta]^3}{\sqrt{4 \pi + \gamma}} + \\
 & \quad \left. \left. \frac{\pi \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \operatorname{Sin}[\beta]^3}{\sqrt{\gamma}} + \right. \right.
 \end{aligned}$$

$$\left. \sqrt{\gamma} \sqrt{(2\pi + \gamma)^2} \sqrt{4\pi + \gamma} \sin[\beta]^3 \right) /$$

$$\left( \pi \left( -16\pi\gamma - 4\gamma^2 + 16\pi^2 \sin[\beta]^2 + 16\pi\gamma \right. \right.$$

$$\left. \left. \sin[\beta]^2 + 4\gamma^2 \sin[\beta]^2 \right) \right) \sqrt{1 - \frac{(v)^2}{c^2}}$$

$2\pi x - 2\pi r' = \vartheta \eta$ , where  $\vartheta$  is an angle of a similar dimensional kind to theta, but different.

$$2\pi x - 2\pi r' = \theta \eta$$

$2\pi r' - 2\pi x = \vartheta \eta$ , where  $\vartheta$  is an angle of a similar dimensional kind to theta, but different is implied but not visualized in this paper.

$2\pi r' - 2\pi x = \vartheta \eta$  is implied but not visualized in this paper.

Height of the cone equals the

$$\text{length contracted "changed radius" : } \eta = x' =$$

$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} == \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2\pi r}{2\pi + \gamma} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$2\pi \eta - 2\pi x' = \omega \eta$ , where  $\omega$  is an angle of a similar dimensional kind to theta, but different.

$$\text{Synchronized angles: } 2\pi \eta - 2\pi x' = \theta \eta$$

Changed radius equals the

length contracted height of the cone :

$$x = \eta' = \frac{2\pi r - r\theta}{2\pi} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}} =$$

$$\frac{x \sqrt{\gamma} \sqrt{4\pi + \gamma}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{r \sqrt{\gamma} \sqrt{4\pi + \gamma}}{\sqrt{4\pi^2 + 4\pi\gamma + \gamma^2}} \sqrt{1 - \frac{(v)^2}{c^2}}$$



$2 \pi x - 2 \pi \eta' = \rho \eta$ , where  $\rho$  is an angle of a similar dimensional kind to theta, but different.

$$2 \pi x - 2 \pi \eta' = \theta \eta$$

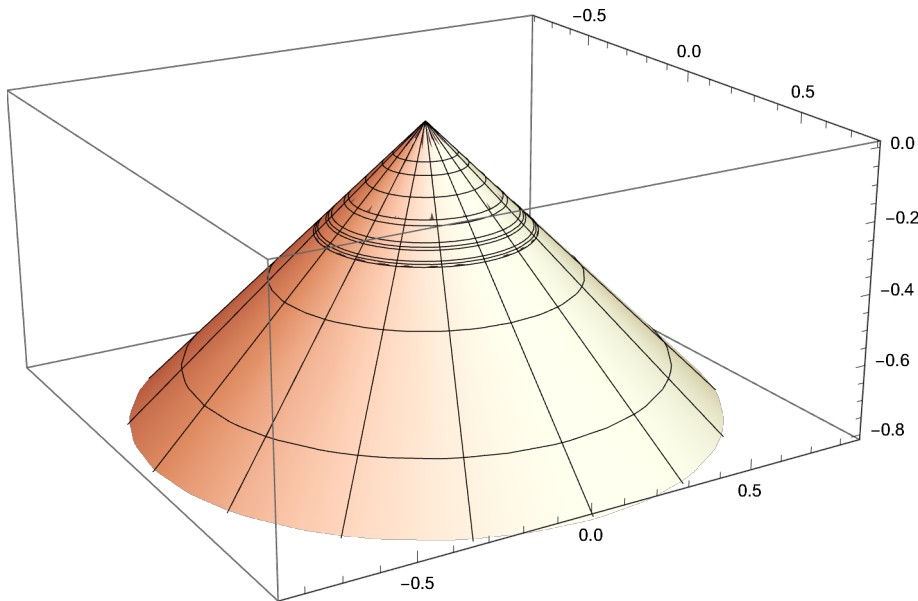
There are also the implied forms :  $\eta' = r$  and  $x' = r$  with their respective

## Commentary on the Forms

One commentary on the forms is their semblance to the position at which the instantaneous rate of change of the height of the cone equals the average rate of change of the height of the cone with respect to theta. Please see A Geometric Pattern of Perception (Emmerson, 2009), for more background information regarding the system of the univocal cone transformation. The six potential equalities of the system wind up miming the 30 - 60 - 90 position at which the instantaneous velocity of the height of the cone equals the average velocity of the height of the cone. When plotted, the 45 - 45 - 90 cone is evident within process of solving for this position.

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\}, \left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\} \right\} \quad (58)$$

RevolutionPlot3D[  
 $\left\{ \text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right], -\text{ArcSin} \left[ \frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} \right] \right\}, \{\theta, -4 \pi, 4 \pi\}$



## "General Relativity" Circumferential Cone - Difference Functions

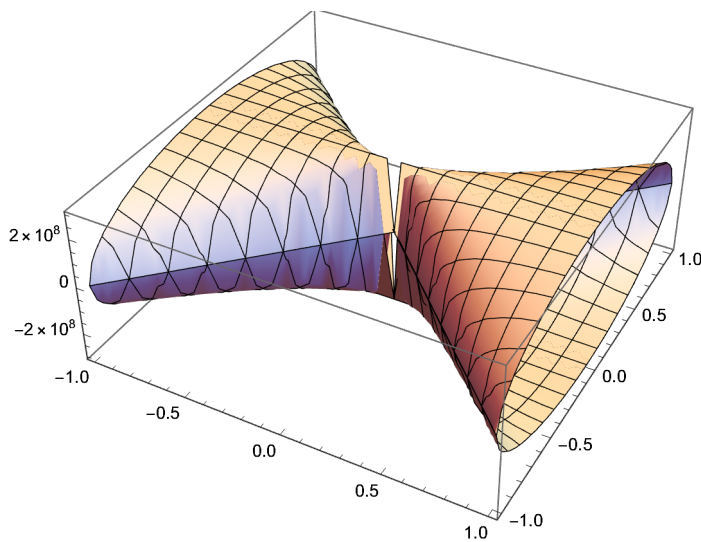
$$\eta = r' = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} =$$

$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$$\text{Solve}\left[\eta == r \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -1. \sqrt{8.98755 \times 10^{16} - \frac{8.98755 \times 10^{16} \eta^2}{r^2}} \right\}, \left\{ v \rightarrow \sqrt{8.98755 \times 10^{16} - \frac{8.98755 \times 10^{16} \eta^2}{r^2}} \right\} \right\}$$

$$\text{Plot3D}\left[\left\{-1. \sqrt{8.987551787368176 \times 10^{16} - \frac{8.987551787368176 \times 10^{16} \eta^2}{r^2}}, \sqrt{8.987551787368176 \times 10^{16} - \frac{8.987551787368176 \times 10^{16} \eta^2}{r^2}}\right\}, \{r, -1, 1\}, \{\eta, -1, 1\}\right]$$

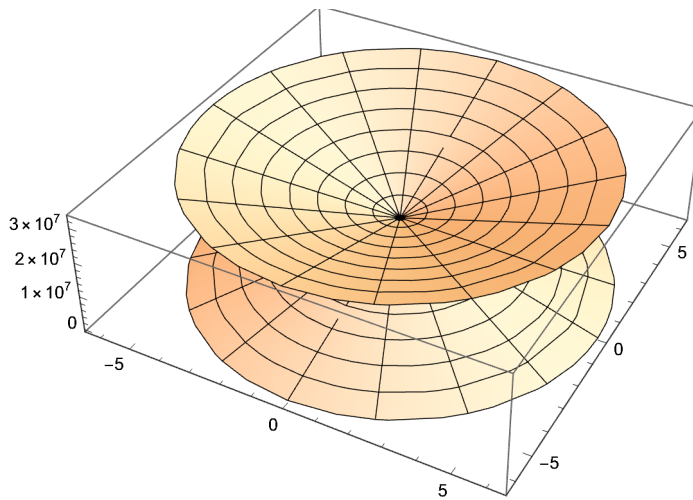


$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == r\sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -1.05839 \times 10^{-7} \sqrt{8.02317 \times 10^{30} - 2.55385 \times 10^{30} \theta + 2.03229 \times 10^{29} \theta^2}\right\},\right. \\ \left.\left\{v \rightarrow 1.05839 \times 10^{-7} \sqrt{8.02317 \times 10^{30} - 2.55385 \times 10^{30} \theta + 2.03229 \times 10^{29} \theta^2}\right\}\right\}$$

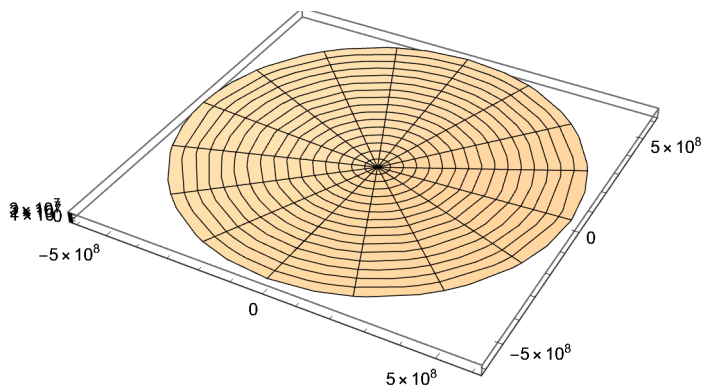
RevolutionPlot3D[.0583947067478751`\*^-7

$\sqrt{(8.02317171945391 \times 10^{30} - 2.5538548768523825 \times 10^{30} \theta + 2.0322931379520014 \times 10^{29} \theta^2)}$ ,  
{θ, -2π, 2π}]



RevolutionPlot3D[{-1.0583947067478751`\*^-7

$\sqrt{(8.02317171945391 \times 10^{30} - 2.5538548768523825 \times 10^{30} \theta + 2.0322931379520014 \times 10^{29} \theta^2)}$ ,  
.0583947067478751`\*^-7  $\sqrt{(8.02317171945391 \times 10^{30} -$   
 $2.5538548768523825 \times 10^{30} \theta + 2.0322931379520014 \times 10^{29} \theta^2)}$ }, {θ, -2π, 2π}]



$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

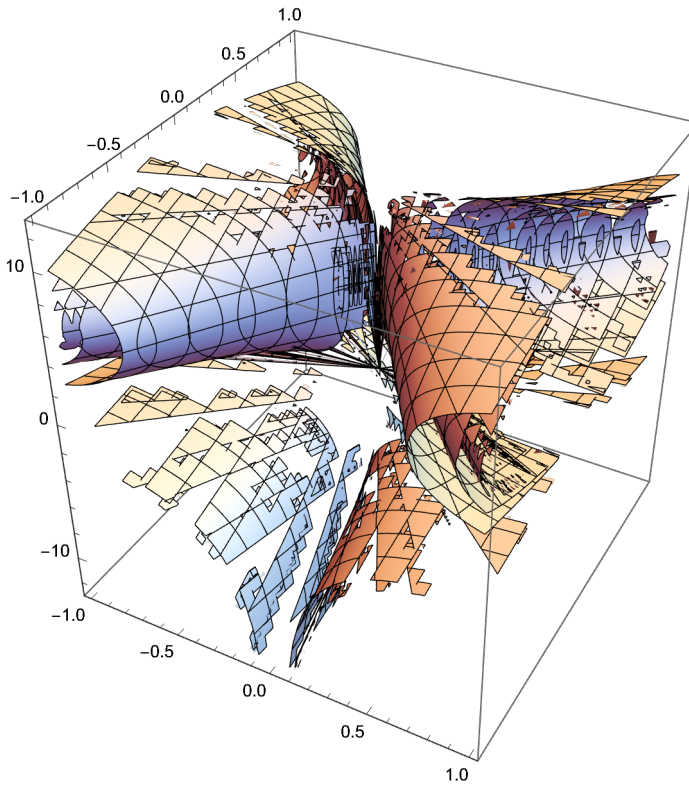
$$\left\{\left\{v \rightarrow -1.54328 \times 10^{-11} \sqrt{\left(3.77356 \times 10^{38} - \frac{3.82342 \times 10^{37} r^2 \theta^2}{\eta^2} + \frac{6.08516 \times 10^{36} r^2 \theta^3}{\eta^2} - \frac{2.42121 \times 10^{35} r^2 \theta^4}{\eta^2}\right)}\right\}, \right.$$

$$\left.\left\{v \rightarrow 1.54328 \times 10^{-11} \sqrt{\left(3.77356 \times 10^{38} - \frac{3.82342 \times 10^{37} r^2 \theta^2}{\eta^2} + \frac{6.08516 \times 10^{36} r^2 \theta^3}{\eta^2} - \frac{2.42121 \times 10^{35} r^2 \theta^4}{\eta^2}\right)}\right\}\right\}$$

ContourPlot3D[ $-1.5432808288459432 \times 10^{-11}$

$$\sqrt{\left(3.7735619429356124 \times 10^{38} - \frac{3.8234176260591615 \times 10^{37} r^2 \theta^2}{\eta^2} + \frac{6.085158146919955 \times 10^{36} r^2 \theta^3}{\eta^2} - \frac{2.4212074964455716 \times 10^{35} r^2 \theta^4}{\eta^2}\right)},$$

$$\{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$



From XXI.A Proof for Non -

Comprehensiveness of Euclidean Geometry (Due to its Consistency) :

$$r = \left( \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) \right)$$

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]$$

$$r = \frac{-4\pi\theta + 2(4\pi-\theta)\theta - \frac{(4\pi-\theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi-\theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi-\theta)\theta - 12\pi\theta^2 + 2(4\pi-\theta)\theta^2 + 2\theta^3}$$

Solve[

$$\frac{\sqrt{4\pi\left(\frac{-4\pi\theta + 2(4\pi-\theta)\theta - \frac{(4\pi-\theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi-\theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi-\theta)\theta - 12\pi\theta^2 + 2(4\pi-\theta)\theta^2 + 2\theta^3}\right)^2\theta - \left(\frac{-4\pi\theta + 2(4\pi-\theta)\theta - \frac{(4\pi-\theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi-\theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi-\theta)\theta - 12\pi\theta^2 + 2(4\pi-\theta)\theta^2 + 2\theta^3}\right)^2\theta^2}}{2\pi} == \frac{-4\pi\theta + 2(4\pi-\theta)\theta - \frac{(4\pi-\theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi-\theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi-\theta)\theta - 12\pi\theta^2 + 2(4\pi-\theta)\theta^2 + 2\theta^3} \sqrt{1 - \frac{(v)^2}{c^2}}, v]$$

{{}}

Pure Cancellation Indicating validity.

$2\pi\eta - 2\pi r' = \phi\eta$ , where  $\phi$  is an angle of a similar dimensional kind to theta, but different.

Solve[ $2\pi\eta - 2\pi r' == \phi\eta, \phi]$

$$\left\{\left\{\phi \rightarrow \frac{2(\pi\eta - \pi r')}{\eta}\right\}\right\}$$

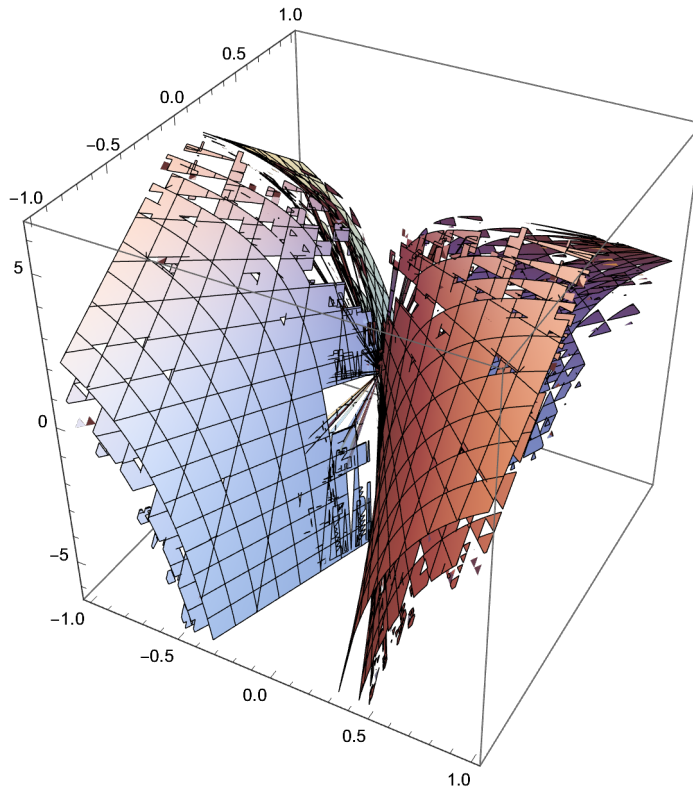
$$\text{Solve}\left[\phi == \frac{2\left(\pi\eta - \pi r\sqrt{1 - \frac{(v)^2}{c^2}}\right)}{\eta}, v\right]$$

$$\left\{\left\{v \rightarrow -1.05839 \times 10^{-7}\right\}\right\}$$

$$\sqrt{8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \phi}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \phi^2}{r^2}}\}, \{v \rightarrow 1.05839 \times 10^{-7} \sqrt{8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \phi}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \phi^2}{r^2}}\}}$$

ContourPlot3D[1.0583947067478751`\*^-7

$$\sqrt{\left(8.02317171945391`*^30 - \frac{8.02317171945391`*^30 \eta^2}{r^2} + \frac{2.5538548768523825`*^30 \eta^2 \phi}{r^2} - \frac{2.0322931379520014`*^29 \eta^2 \phi^2}{r^2}\right)}, \{\eta, -1, 1\}, \{r, -1, 1\}, \{\phi, -2 \pi, 2 \pi\}]$$

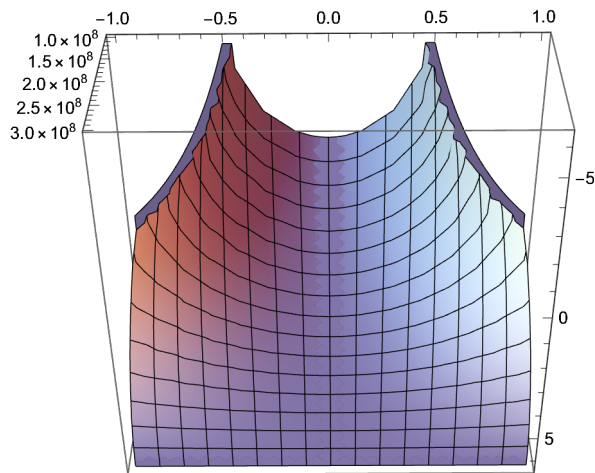


$$\text{Solve}\left[\phi == \frac{2 \left( \pi \eta - \pi \frac{-4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi}}{16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3} \sqrt{1 - \frac{(v)^2}{c^2}} \right)}{\eta}, \phi\right]$$

$$\left\{ \left\{ \phi \rightarrow \frac{1}{\eta} 2. \left( 3.14159 \eta - \left( 3.14159 \sqrt{1. - 1.11265 \times 10^{-17} v^2} \left( -12.5664 \theta + 2. (12.5664 - 1. \theta) \theta - 0.0795775 (12.5664 - 1. \theta)^2 \theta + \theta^2 - 0.0795775 (12.5664 - 1. \theta) \theta^2 \right) \right) / \left( 157.914 \theta - 12.5664 (12.5664 - 1. \theta) \theta - 37.6991 \theta^2 + 2. (12.5664 - 1. \theta) \theta^2 + 2. \theta^3 \right) \right) \right\} \right\}$$

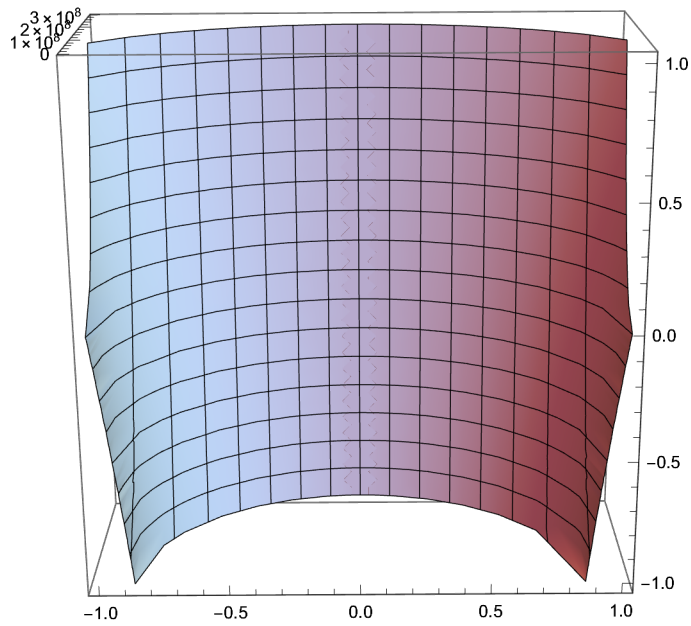
$$\text{Solve}\left[\phi == \frac{1}{\eta} 2. \sqrt{\left(3.141592653589793 \eta - \left(3.141592653589793 \sqrt{1. - 1.1126500560536185 \eta^{-17} v^2} - 12.566370614359172 \theta + 2. (12.566370614359172 - 1. \theta) \theta - 0.07957747154594767 (12.566370614359172 - 1. \theta)^2 \theta + \theta^2 - 0.07957747154594767 (12.566370614359172 - 1. \theta) \theta^2\right) / (157.91367041742973 \theta - 12.566370614359172 (12.566370614359172 - 1. \theta) \theta - 37.69911184307752 \theta^2 + 2. (12.566370614359172 - 1. \theta) \theta^2 + 2. \theta^3)\right)}, v]\right. \\ \left.\left\{\left\{v \rightarrow -3.27644 \times 10^{-13} \sqrt{8.37215 \times 10^{41} - 8.37215 \times 10^{41} \eta^2 + 2.66494 \times 10^{41} \eta^2 \phi - 2.12069 \times 10^{40} \eta^2 \phi^2}\right\}, \left\{v \rightarrow 3.27644 \times 10^{-13} \sqrt{8.37215 \times 10^{41} - 8.37215 \times 10^{41} \eta^2 + 2.66494 \times 10^{41} \eta^2 \phi - 2.12069 \times 10^{40} \eta^2 \phi^2}\right\}\right\}$$

$$\text{Plot3D}\left[3.2764405235343625 \eta^{-13} \sqrt{\left(8.372146677118284 \eta^{41} - 8.372146677118285 \eta^{41} \eta^2 + 2.6649370559075226 \eta^{41} \eta^2 \phi - 2.1206895273822245 \eta^{40} \eta^2 \phi^2\right)}, \{\phi, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}\right]$$



Plot3D[3.2764405235343625`\*^-13

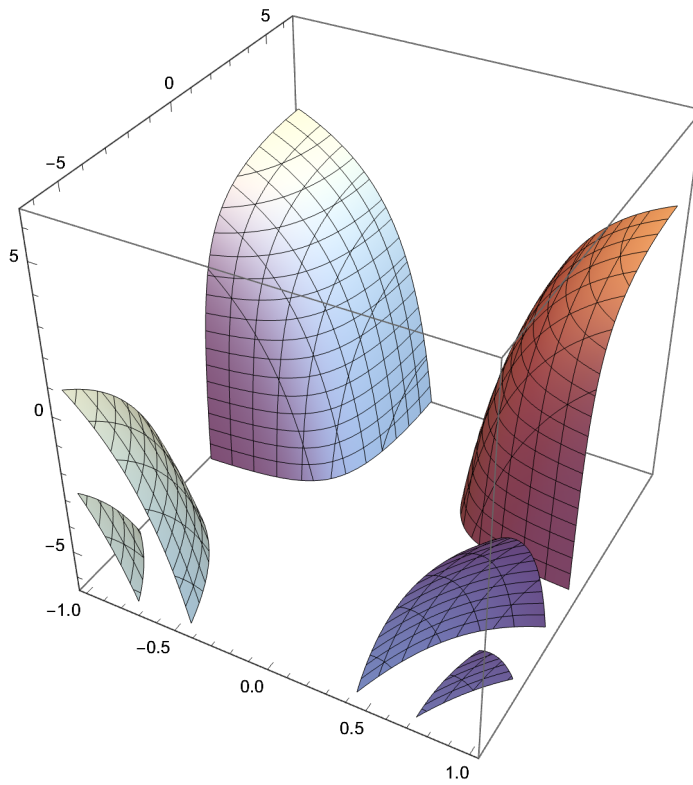
$$\sqrt{(8.372146677118284`*^41 - 8.372146677118285`*^41 \eta^2 + 2.6649370559075226`*^41 \eta^2 \phi - 2.1206895273822245`*^40 \eta^2 \phi^2)}, \{\phi, -1, 1\}, \{\eta, -1, 1\}]$$





ContourPlot3D[6.850321210799518`\*^-15

$\sqrt{(1.9152238172564892`^{45} - 6.096346752873982`^{44} \eta^2 \theta + 4.851318602610598`^{43} \eta^2 \theta^2 + 1.9405274410442392`^{44} \eta^2 \theta \phi - 1.544222672238286`^{43} \eta^2 \theta^2 \phi - 1.544222672238286`^{43} \eta^2 \theta \phi^2 + 1.2288533576064947`^{42} \eta^2 \theta^2 \phi^2)},$   
 $\{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\phi, -2\pi, 2\pi\}]$

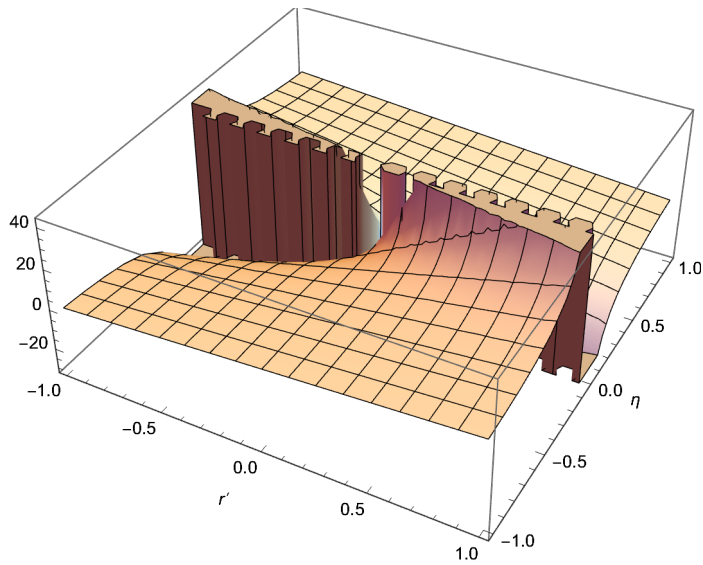


$$2\pi\eta - 2\pi r' = \theta\eta$$

Solve[2πη - 2πr' == θη, θ]

$$\left\{ \left\{ \theta \rightarrow \frac{2(\pi\eta - \pi r')}{\eta} \right\} \right\}$$

`Plot3D` $\left[\frac{2 (\pi \eta - \pi r')}{\eta}, \{r', -1, 1\}, \{\eta, -1, 1\}, \text{AxesLabel} \rightarrow \text{Automatic}\right]$

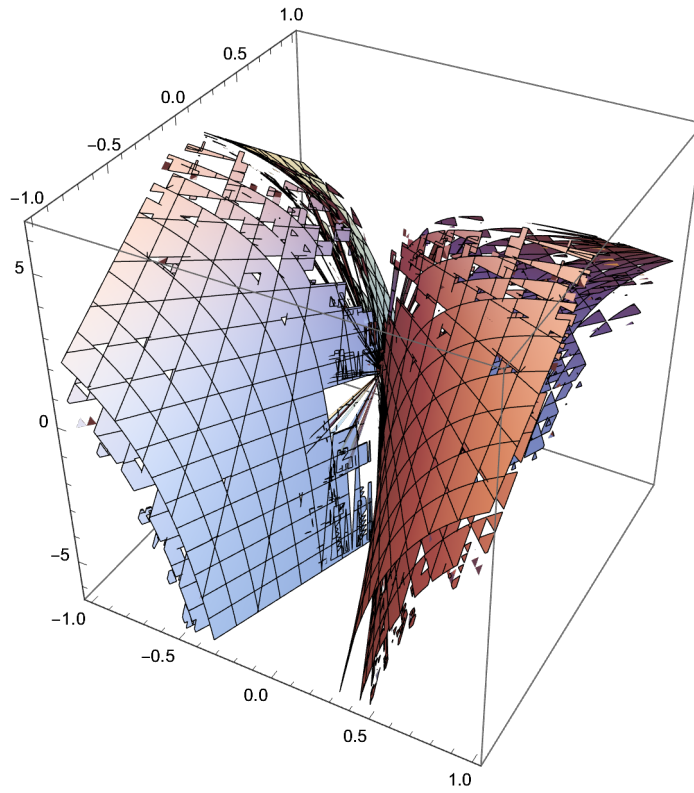


`Solve` $\left[\theta == \frac{2 \left( \pi \eta - \pi r' \sqrt{1 - \frac{(v)^2}{c^2}} \right)}{\eta}, v\right]$

$$\left\{ \left\{ v \rightarrow -1.05839 \times 10^{-7} \sqrt{\left( 8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \theta}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \theta^2}{r^2} \right)} \right\}, \right. \\ \left. \left\{ v \rightarrow 1.05839 \times 10^{-7} \sqrt{\left( 8.02317 \times 10^{30} - \frac{8.02317 \times 10^{30} \eta^2}{r^2} + \frac{2.55385 \times 10^{30} \eta^2 \theta}{r^2} - \frac{2.03229 \times 10^{29} \eta^2 \theta^2}{r^2} \right)} \right\} \right\}$$

ContourPlot3D[1.0583947067478751`\*^-7

$$\sqrt{\left(8.02317171945391`*^30 - \frac{8.02317171945391`*^30 \eta^2}{r^2} + \frac{2.5538548768523825`*^30 \eta^2 \theta}{r^2} - \frac{2.0322931379520014`*^29 \eta^2 \theta^2}{r^2}\right)}, \{\eta, -1, 1\}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$



c := 2.99792458 (10^8)

$$\text{Solve}\left[\theta == \frac{1}{\eta} 2\right.$$

$$\left( \pi \eta - \pi \left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right) / \right.$$

$$\left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \right)$$

$$\sqrt{1 - \frac{\left( \frac{\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}}{\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}} \right)^2}{c^2}}, \eta \right]$$

$$\left\{ \left\{ \eta \rightarrow \left( 8.36884 \times 10^9 \theta \sqrt{\left( - \frac{3.72447 \times 10^{14} \theta}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} + \right. \right. \right.$$

$$\frac{3.57079 \times 10^{14} \theta^2}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} +$$

$$\left. \frac{6.58448 \times 10^{16} \sin[\beta]^2}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} \right) -$$

$$6.65971 \times 10^8 \theta^2 \sqrt{\left( - \frac{3.72447 \times 10^{14} \theta}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} + \right.}$$

$$\frac{3.57079 \times 10^{14} \theta^2}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} +$$

$$\left. \frac{6.58448 \times 10^{16} \sin[\beta]^2}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} \right) -$$

$$4.18442 \times 10^9 \sqrt{12.5664 \theta - 1. \theta^2} \sin[\beta]$$

$$\sqrt{\left( - \frac{3.72447 \times 10^{14} \theta}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} + \right.}$$

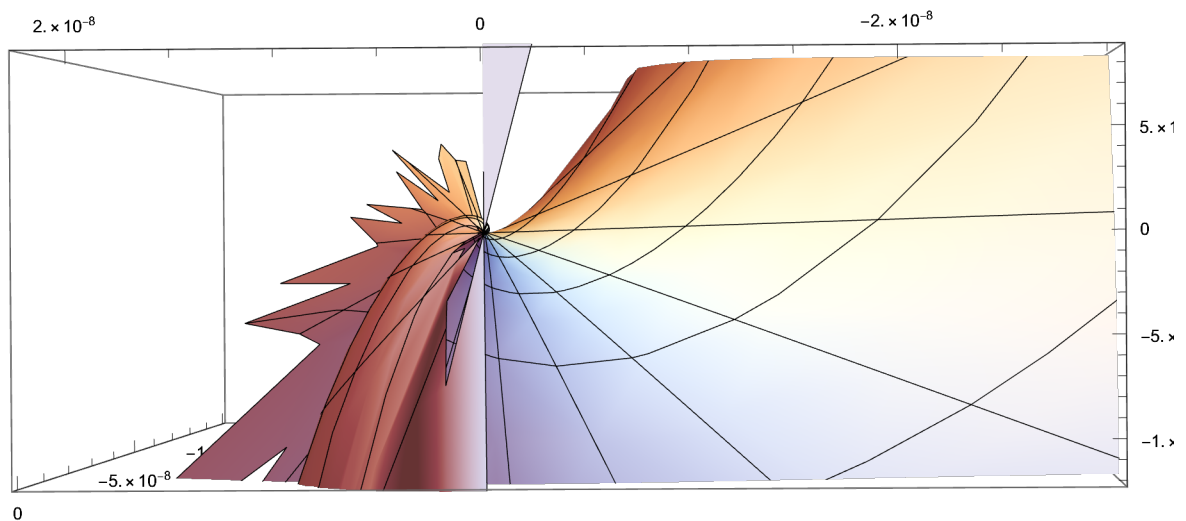
$$\frac{3.57079 \times 10^{14} \theta^2}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} +$$

$$\left. \frac{6.58448 \times 10^{16} \sin[\beta]^2}{4.48719 \times 10^{15} \theta - 3.57079 \times 10^{14} \theta^2 - 1.40969 \times 10^{16} \sin[\beta]^2} \right) \Bigg) /$$

$$\left( \theta \left( -2.22936 \times 10^{19} + 8.87036 \times 10^{18} \theta - 1.12941 \times 10^{18} \theta^2 + 4.49378 \times 10^{16} \theta^3 \right) \right) \Bigg\}$$

SphericalPlot3D[  

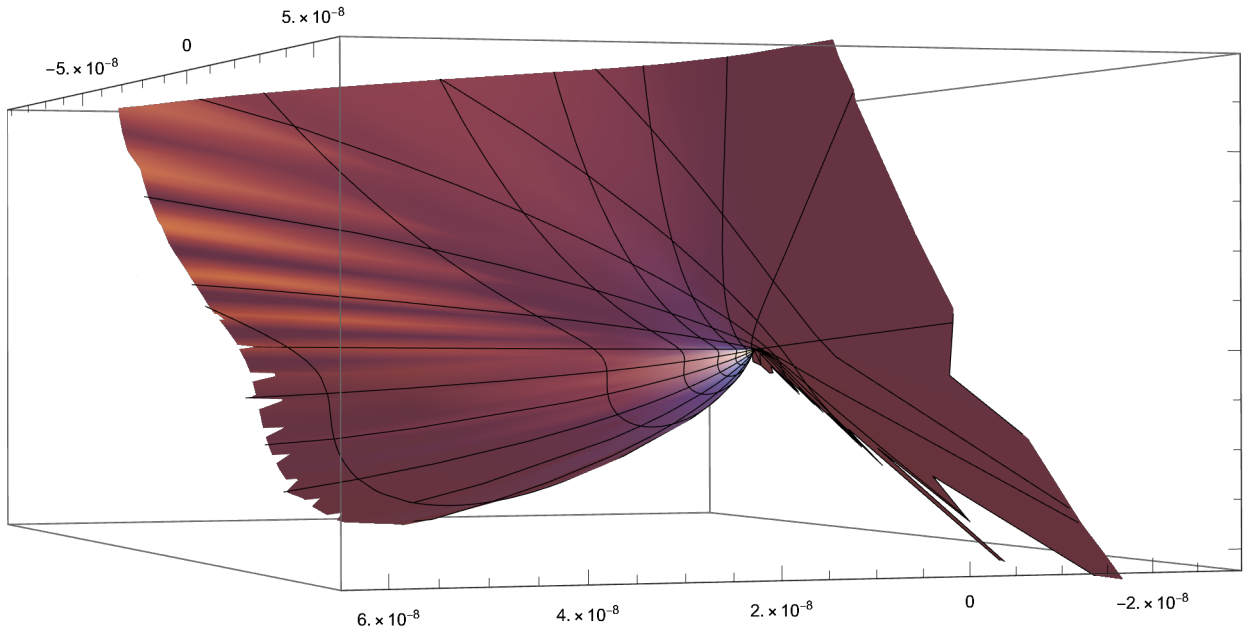
$$\left( \frac{8.368843409831769 \theta^9 \sqrt{-\left( \frac{(3.72446628439707 \theta^{14})}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} + \frac{(3.57079298535128 \theta^{14})}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} + \frac{(6.58448430010097 \sin^2[\beta])}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} \right) - 6.659713983183793 \theta^8 \sqrt{-\left( \frac{(3.72446628439707 \theta^{14})}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} + \frac{(3.57079298535128 \theta^{14})}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} + \frac{(6.58448430010097 \sin^2[\beta])}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} \right) - 4.1844217049158845 \theta^9 \sqrt{12.566370614359172 \theta - 1. \theta^2 \sin^2[\beta]}}}{\sqrt{-\left( \frac{(3.72446628439707 \theta^{14})}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} + \frac{(3.57079298535128 \theta^{14})}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} + \frac{(6.58448430010097 \sin^2[\beta])}{(4.487190804107819 \theta^{15} - 3.57079298535128 \theta^2 - 1.40969256654408 \sin^2[\beta])} \right) - 4.1844217049158845 \theta^9 \sqrt{12.566370614359172 \theta - 1. \theta^2 \sin^2[\beta]}}} \right) \theta \left( -2.2293641391812866 \theta^{19} + 8.870358067562748 \theta^{18} - 1.1294090667581471 \theta^{18} + 4.493775893684088 \theta^{16} \right),$$
  
 $\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$



```

SphericalPlot3D[
  (8.368843409831769`*^9  $\theta$   $\sqrt{-((3.72446628439707`*^14 \theta) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2)) +$ 
    (3.57079298535128`*^14  $\theta^2) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2) +$ 
    (6.58448430010097`*^16  $\sin[\beta]^2) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2)) -$ 
    6.659713983183793`*^8  $\theta^2 \sqrt{-((3.72446628439707`*^14 \theta) /$ 
    (4.487190804107819`*^15  $\theta - 3.57079298535128`*^14 \theta^2 -$ 
    1.40969256654408`*^16  $\sin[\beta]^2)) +$ 
    (3.57079298535128`*^14  $\theta^2) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2) +$ 
    (6.58448430010097`*^16  $\sin[\beta]^2) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2)) -$ 
    4.1844217049158845`*^9  $\sqrt{12.566370614359172` \theta - 1.` \theta^2 \sin[\beta]}$ 
     $\sqrt{-((3.72446628439707`*^14 \theta) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2)) +$ 
    (3.57079298535128`*^14  $\theta^2) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2) +$ 
    (6.58448430010097`*^16  $\sin[\beta]^2) / (4.487190804107819`*^15 \theta -$ 
    3.57079298535128`*^14  $\theta^2 - 1.40969256654408`*^16 \sin[\beta]^2))} /$ 
    ( $\theta (-2.2293641391812866`*^19 + 8.870358067562748`*^18 \theta -$ 
    1.1294090667581471`*^18  $\theta^2 + 4.493775893684088`*^16 \theta^3))$ ),
  { $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi / 2$ ,  $\pi / 2$ }]

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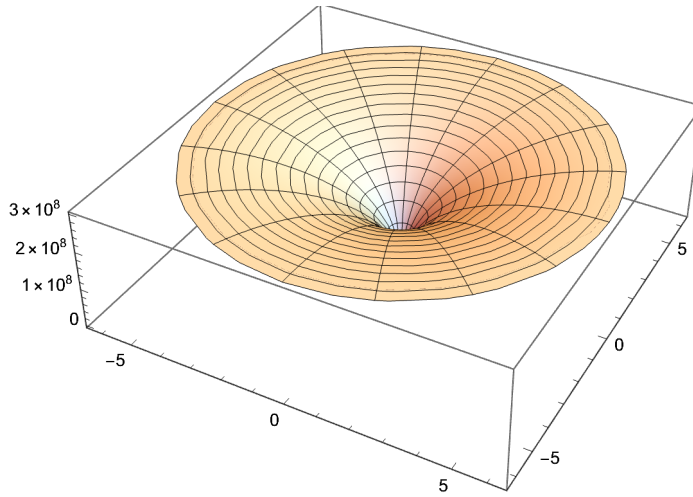
$$x = r' = \frac{2 \pi r - r \theta}{2 \pi} = r \sqrt{1 - \frac{(v)^2}{c^2}} =$$

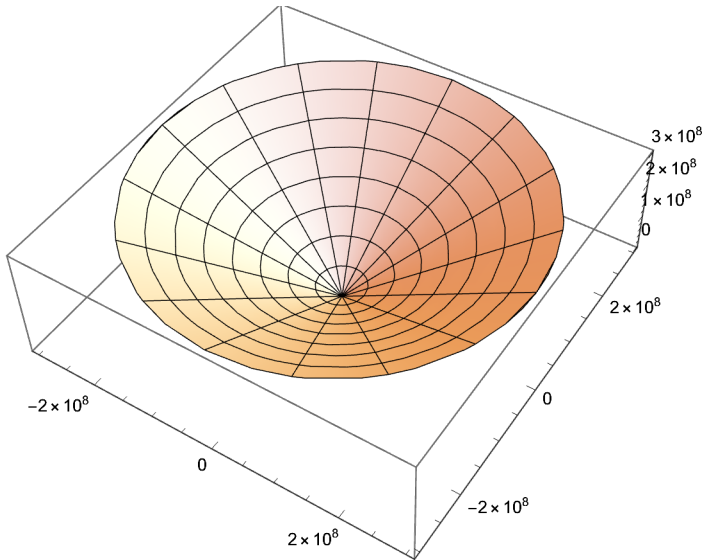
$$\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \sqrt{1 - \frac{(v)^2}{c^2}}$$

$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == r \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}, \left\{v \rightarrow \frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}\right\}$$

$$c := 2.99792458 (10^8)$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4 c^2 \pi 2 \pi - c^2 (2 \pi)^2}}{2 \pi}, \{c, -3.0 * 10^8, 3.0 * 10^8\}\right]$$


$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

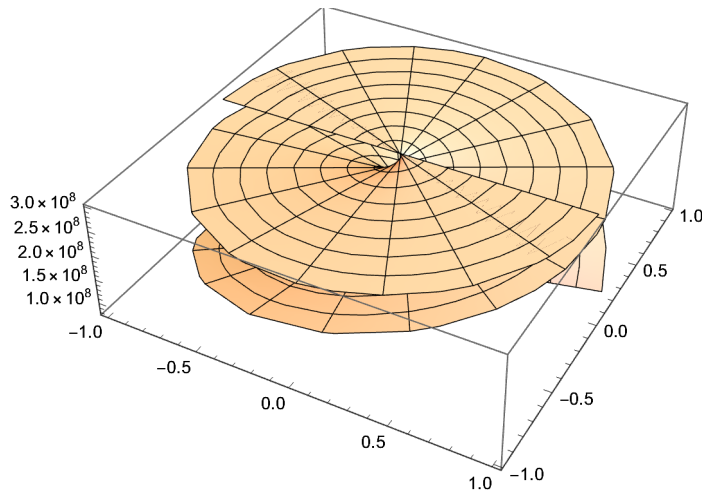
$$\left\{\left\{v \rightarrow -\frac{c \sqrt{16 \pi^4 - \frac{16 \pi^3 r^2 \theta}{\eta^2} + \frac{20 \pi^2 r^2 \theta^2}{\eta^2} - \frac{8 \pi r^2 \theta^3}{\eta^2} + \frac{r^2 \theta^4}{\eta^2}}}{4 \pi^2}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{c \sqrt{16 \pi^4 - \frac{16 \pi^3 r^2 \theta}{\eta^2} + \frac{20 \pi^2 r^2 \theta^2}{\eta^2} - \frac{8 \pi r^2 \theta^3}{\eta^2} + \frac{r^2 \theta^4}{\eta^2}}}{4 \pi^2}\right\}\right\}$$



$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\text{RevolutionPlot3D}\left[\frac{c \sqrt{16 \pi^4 - \frac{16 \pi^3 r^2 \theta}{\eta^2} + \frac{20 \pi^2 r^2 \theta^2}{\eta^2} - \frac{8 \pi r^2 \theta^3}{\eta^2} + \frac{r^2 \theta^4}{\eta^2}}}{4 \pi^2}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



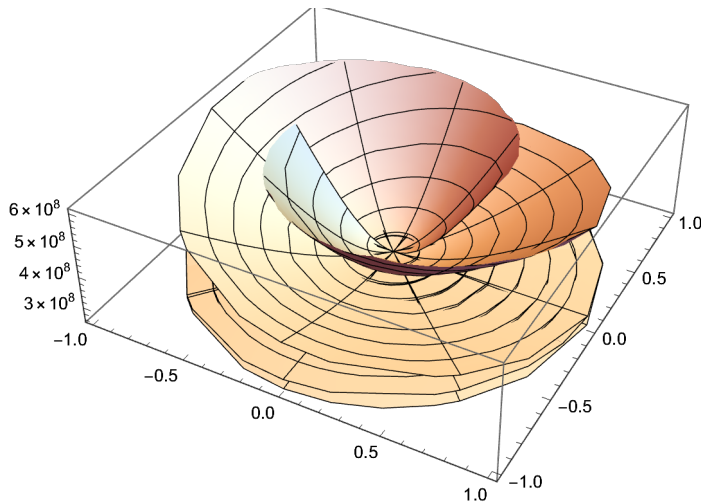
$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{c \sqrt{16 \pi^4 - 16 \pi^3 r^2 \theta + 20 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}}{4 \pi^2}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{c \sqrt{16 \pi^4 - 16 \pi^3 r^2 \theta + 20 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}}{4 \pi^2}\right\}\right\}$$

RevolutionPlot3D[  

$$\frac{c \sqrt{16 \pi^4 - 16 \pi^3 r^2 \theta + 20 \pi^2 r^2 \theta^2 - 8 \pi r^2 \theta^3 + r^2 \theta^4}}{4 \pi^2}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$



Solve[ $\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} == \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \sqrt{1 - \frac{(v)^2}{c^2}}, v]$

{ {v → -c}, {v → c} }

$2 \pi x - 2 \pi r' = \vartheta \eta$ , where  $\vartheta$  is an angle of a similar dimensional kind to theta, but different.

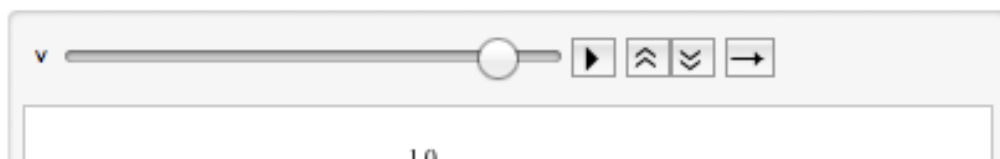
$c := 2.99792458 (10^8)$

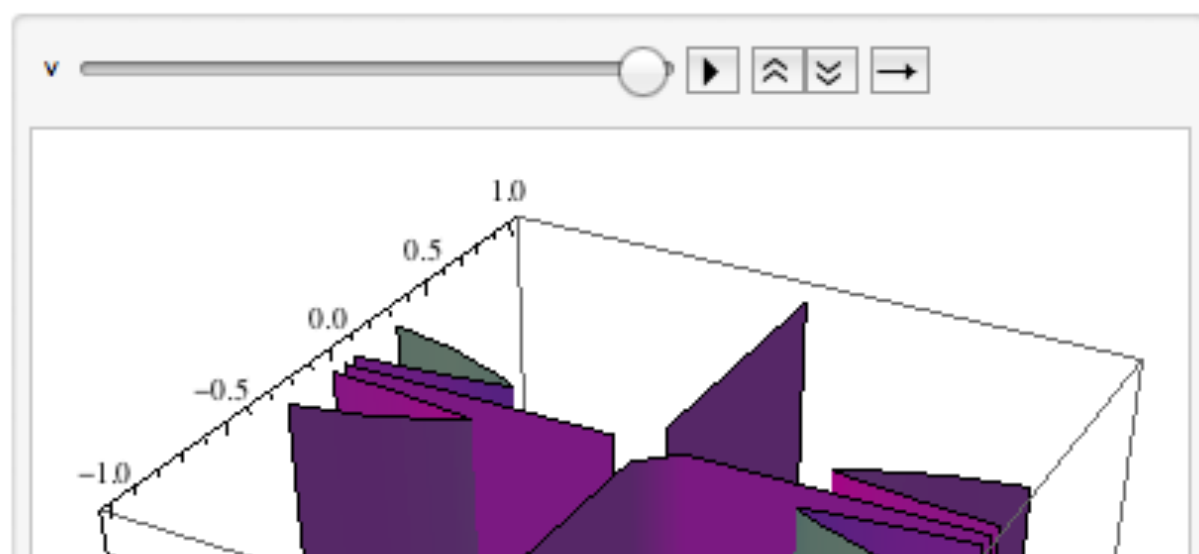
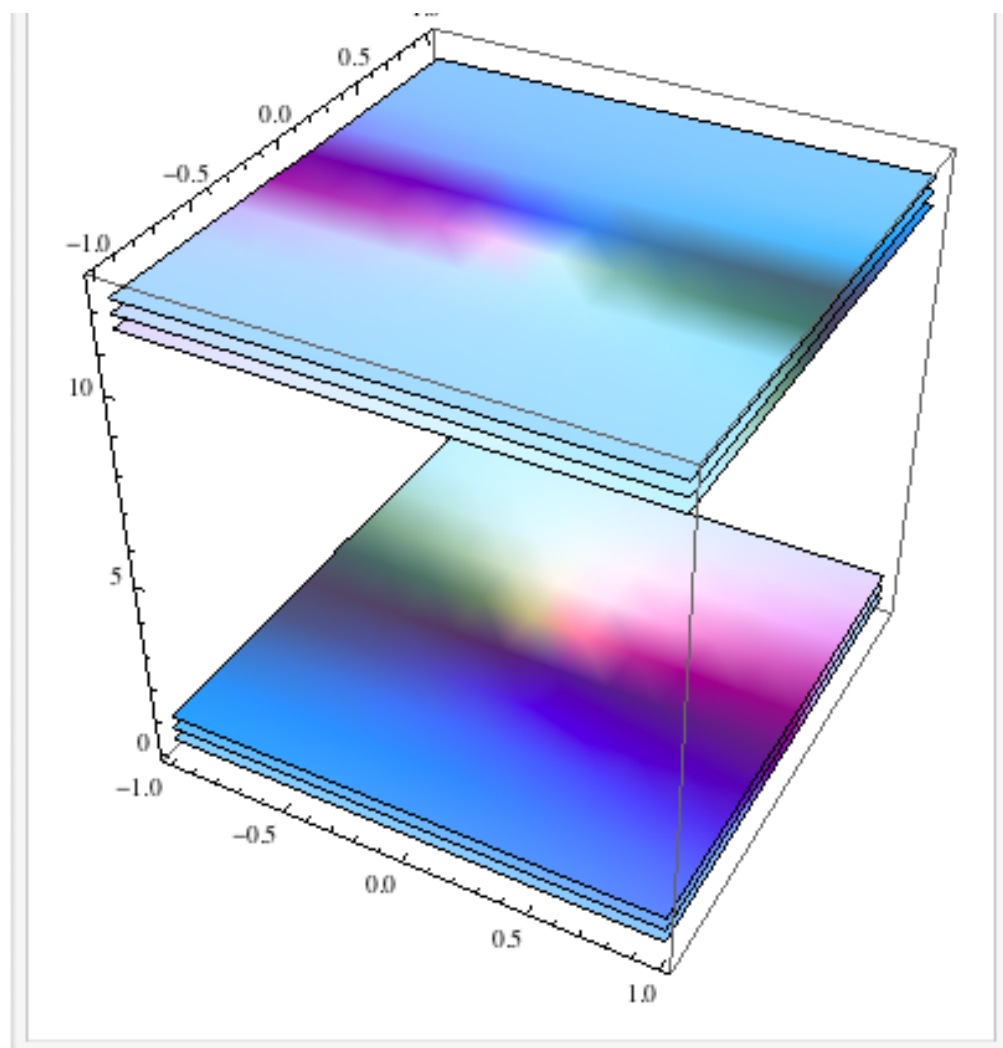
Solve[ $2 \pi x - 2 \pi \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} == \vartheta \eta, \vartheta]$

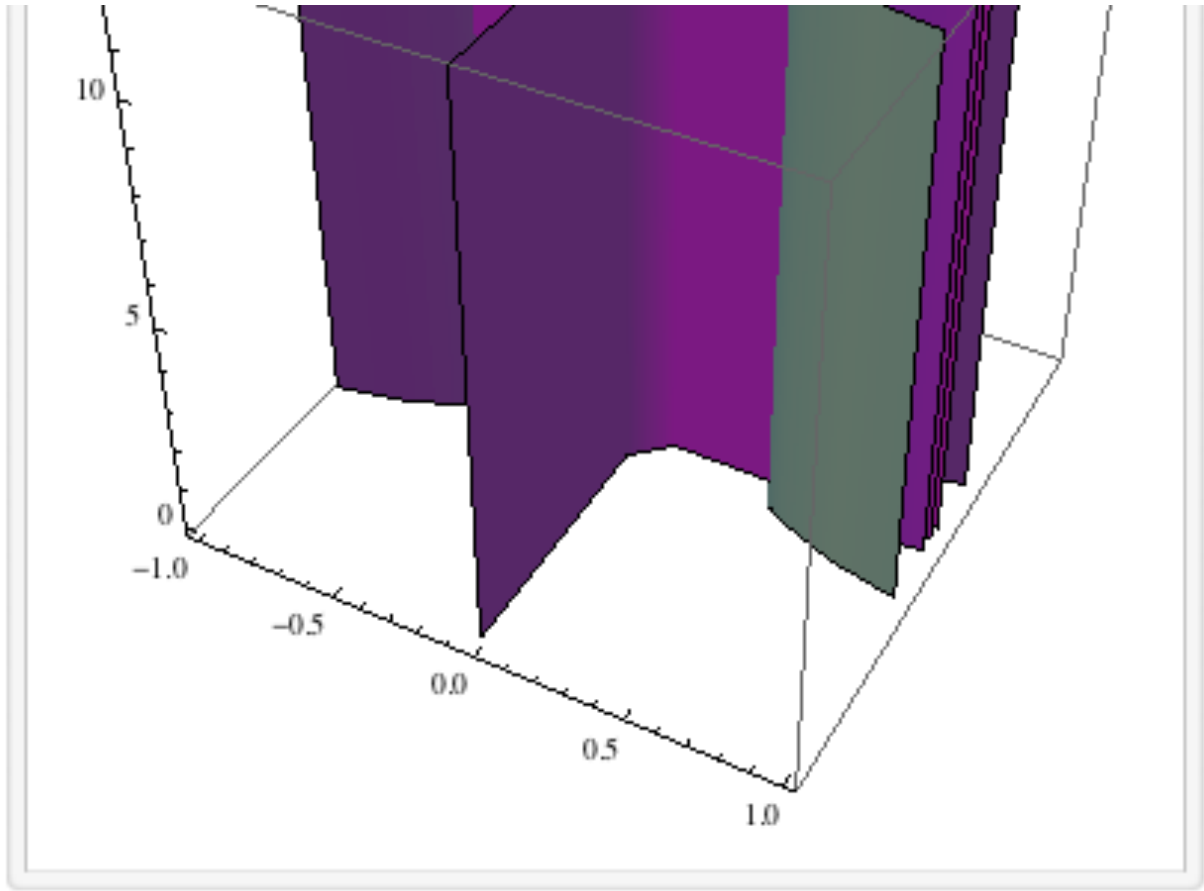
{ { $\vartheta \rightarrow \frac{2 \left( -2 \pi^2 \sqrt{\frac{c^2 - v^2}{c^2}} \eta + \pi x \sqrt{(4 \pi - \theta) \theta} \right)}{\eta \sqrt{(4 \pi - \theta) \theta}} \}$ }

Animate[ContourPlot3D[ $\frac{2 \left( -2 \pi^2 \sqrt{\frac{c^2 - v^2}{c^2}} \eta + \pi x \sqrt{(4 \pi - \theta) \theta} \right)}{\eta \sqrt{(4 \pi - \theta) \theta}},$

{x, -1, 1}, {η, -1, 1}, {θ, 0, 4 π}], {v, -c, c}]





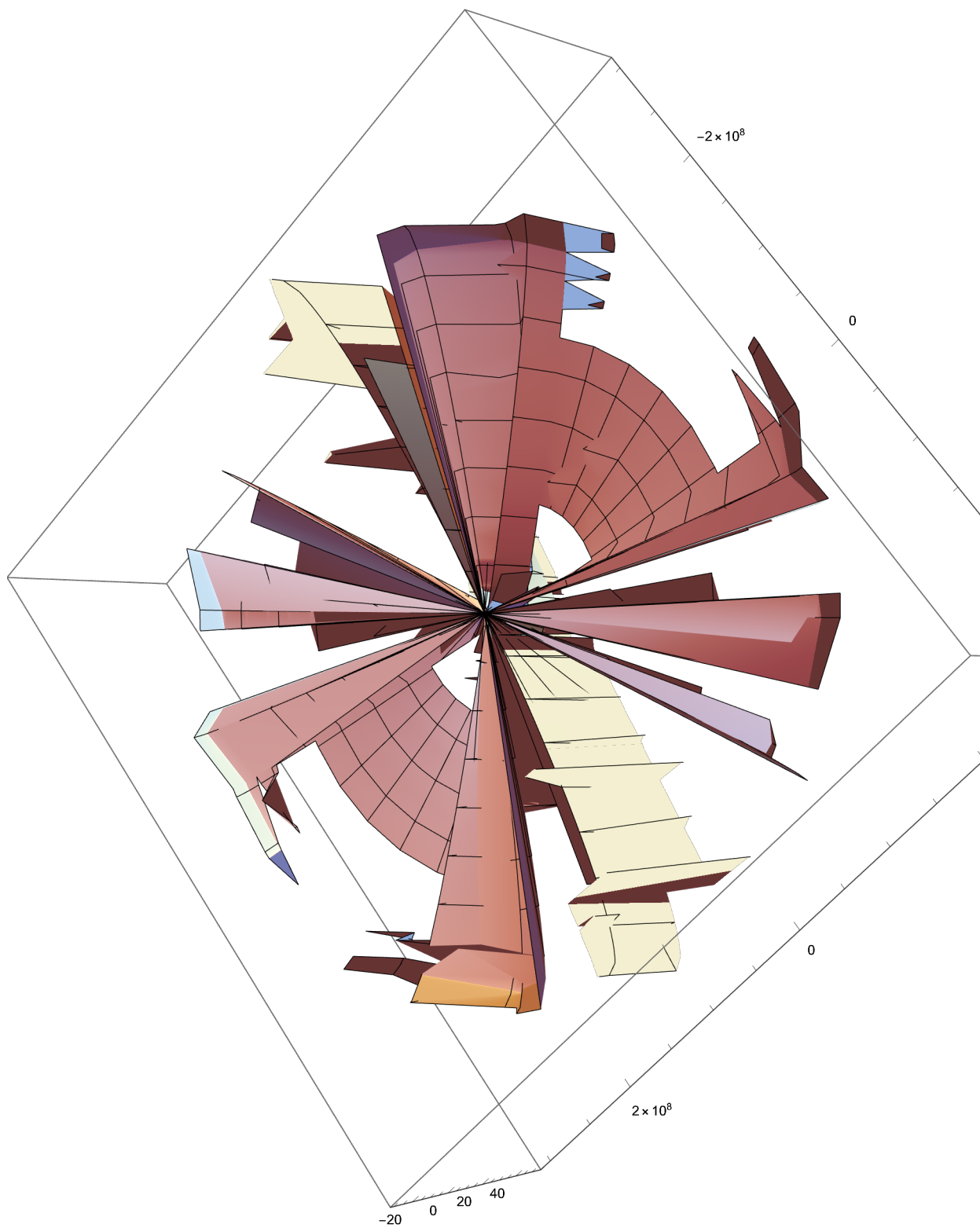


$$\text{Solve}\left[2\pi \frac{2\pi r - r\theta}{2\pi} - 2\pi \frac{2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}{\sqrt{4\pi\theta - \theta^2}} \sqrt{1 - \frac{(v)^2}{c^2}} == \theta \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right]$$

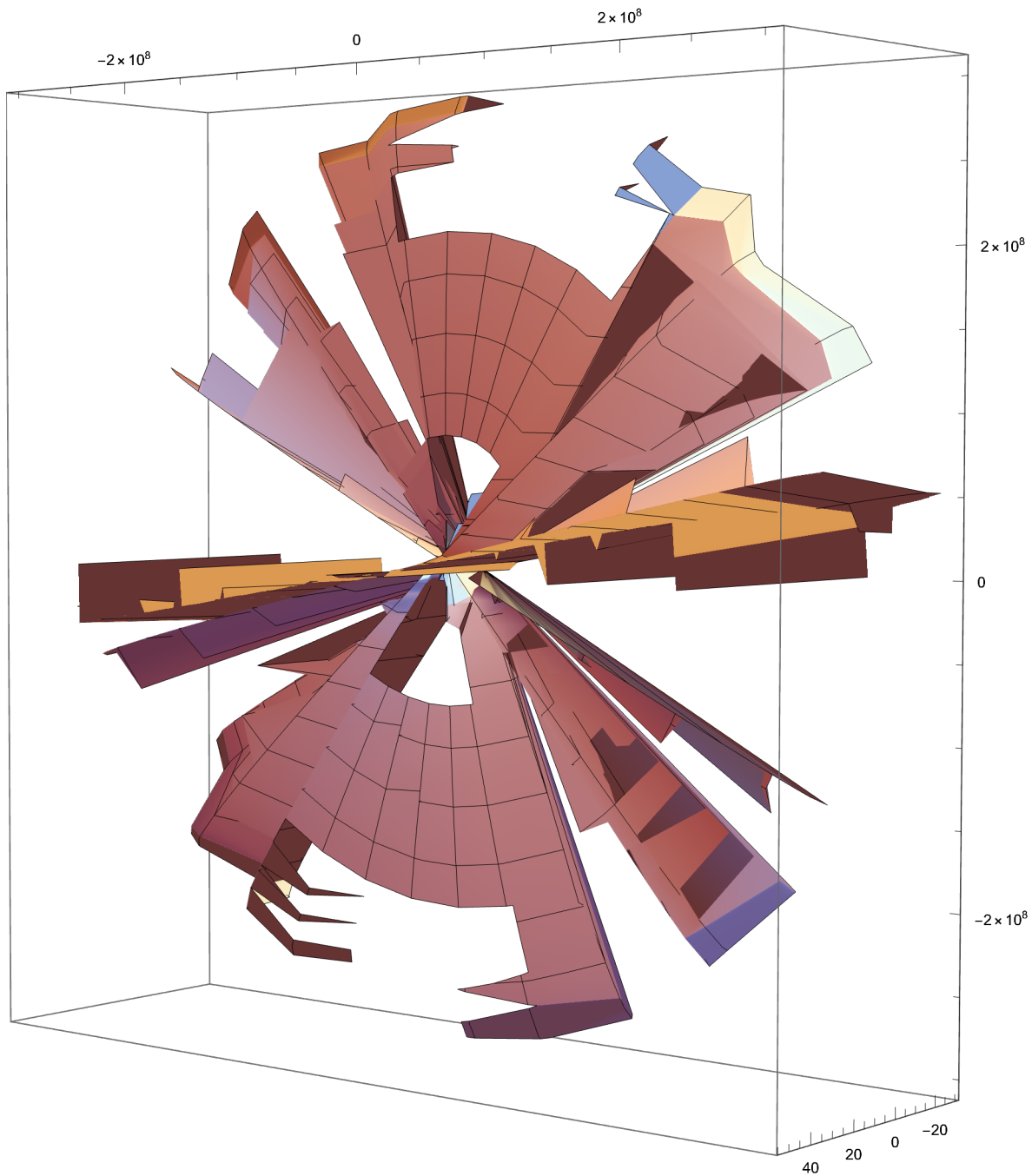
$$\left\{\left\{\theta \rightarrow -\frac{2\pi \left(-2\pi r + r\theta + \frac{2\pi \sqrt{1 - \frac{v^2}{c^2}} \sqrt{4\pi r^2\theta - r^2\theta^2}}{\sqrt{4\pi\theta - \theta^2}}\right)}{\sqrt{4\pi r^2\theta - r^2\theta^2}}\right\}\right\}$$

$$r := \frac{-4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3}$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi \left(-2\pi r + r\theta + \frac{2\pi \sqrt{1 - \frac{v^2}{c^2}} \sqrt{4\pi r^2\theta - r^2\theta^2}}{\sqrt{4\pi\theta - \theta^2}}\right)}{\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{v, -c, c\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$v := \left( \sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right)$$

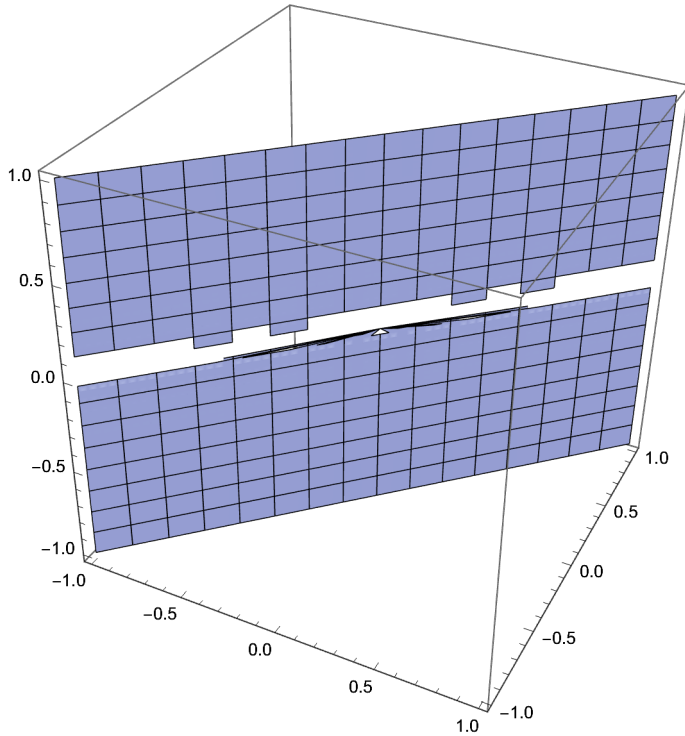
$$\text{RevolutionPlot3D}\left[\frac{2\pi\left(-2\pi r + r\theta + \frac{2\pi\sqrt{1-\frac{v^2}{c^2}}\sqrt{4\pi r^2\theta - r^2\theta^2}}{\sqrt{4\pi\theta - \theta^2}}\right)}{\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{v, -c, c\}, \{\theta, -2\pi, 2\pi\}\right]$$


$$2 \pi x - 2 \pi r' = \theta \eta$$

`Solve[2 π x - 2 π r' == θ η, θ]`

$$\left\{ \left\{ \theta \rightarrow \frac{2 (\pi x - \pi r')}{\eta} \right\} \right\}$$

`ContourPlot3D[ $\frac{2 (\pi x - \pi r')}{\eta}$ , {x, -1, 1}, {r', -1, 1}, {η, -1, 1}]`



$$\eta = x' = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}$$

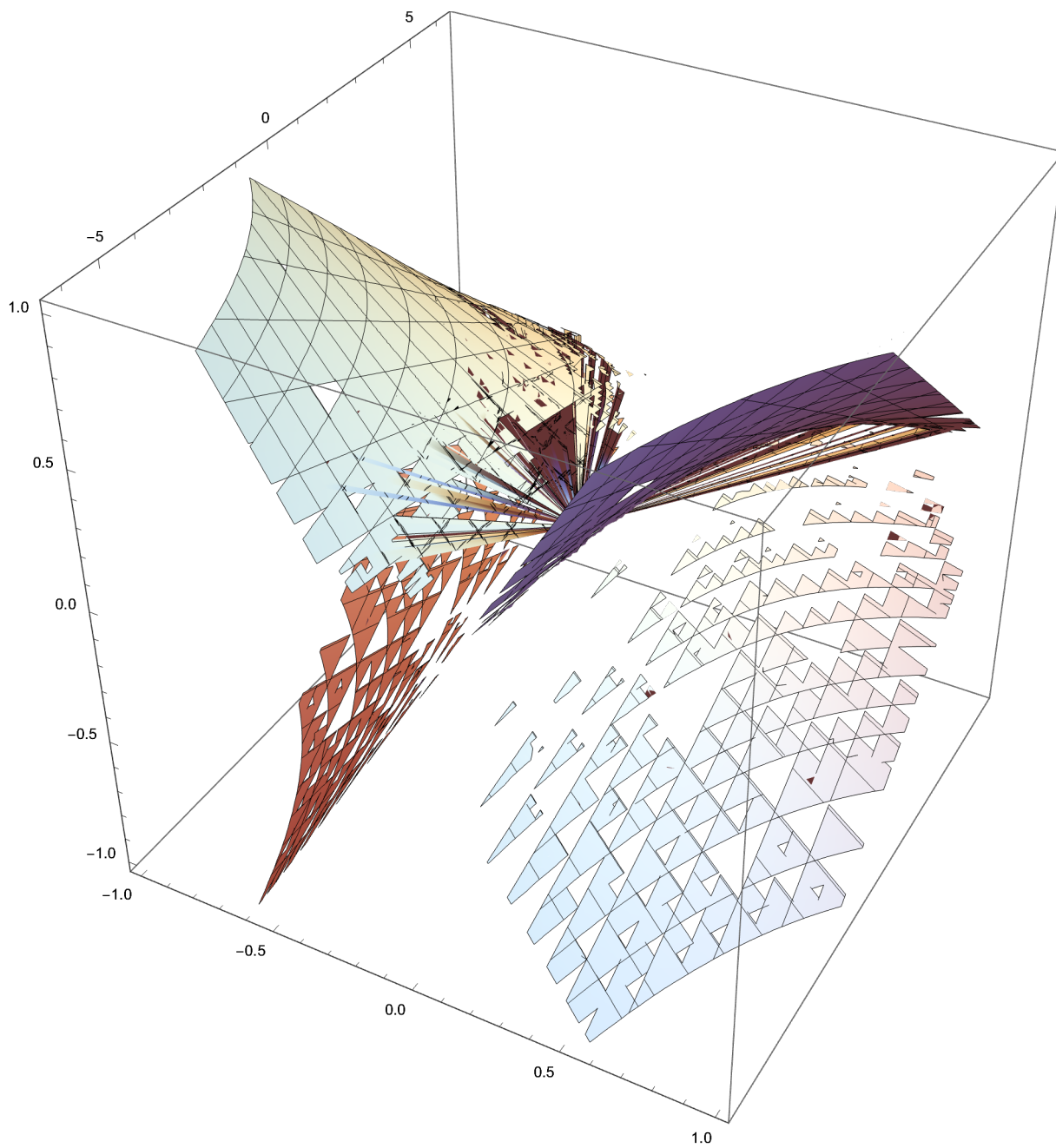
`c := 2.99792458 (10^8)`

`Solve[ $\eta == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}$ , v]`

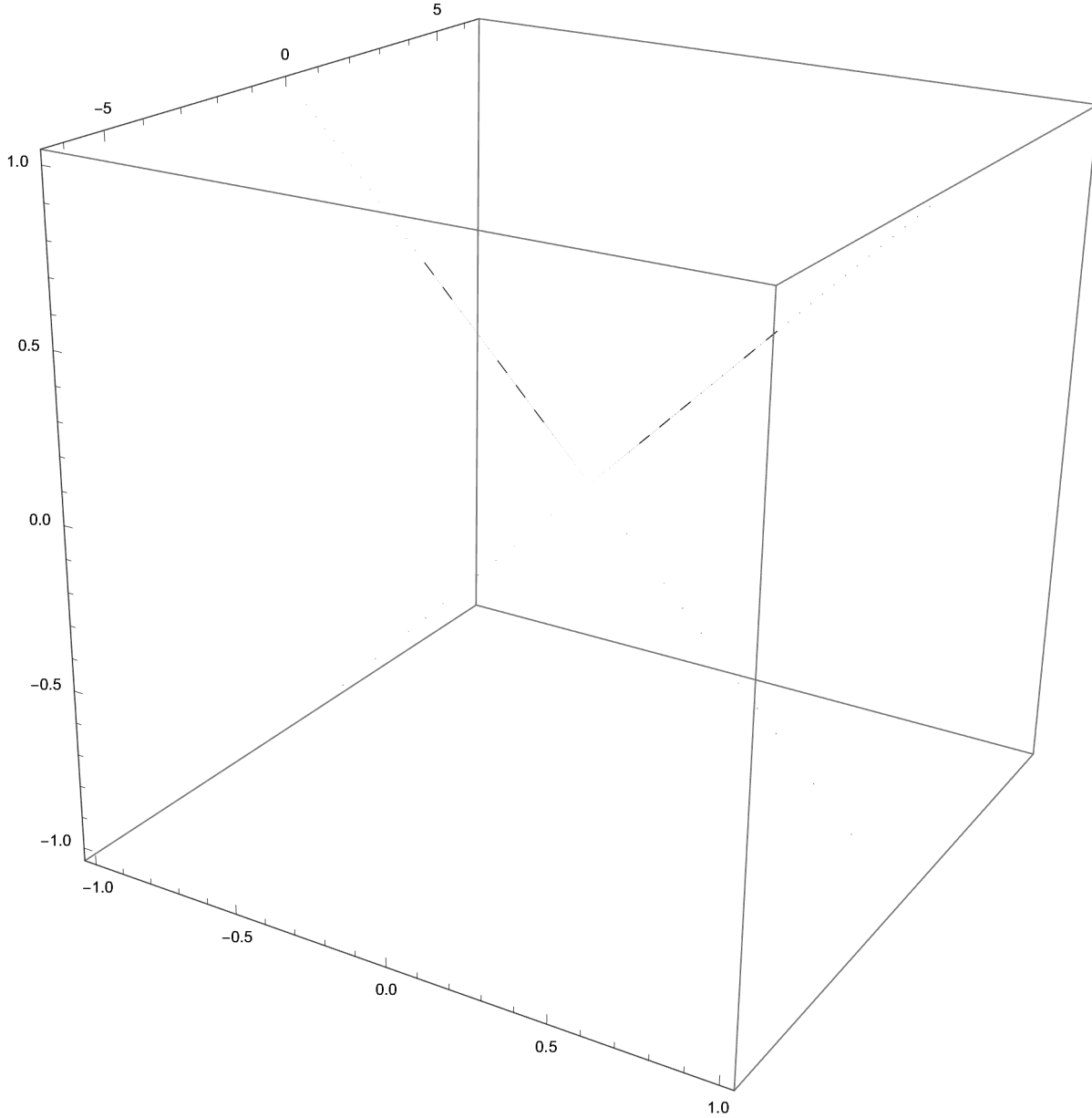
$$\left\{ \left\{ v \rightarrow -\frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\}, \left\{ v \rightarrow \frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\} \right\}$$



$\text{ContourPlot3D}\left[-\frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}\right]$

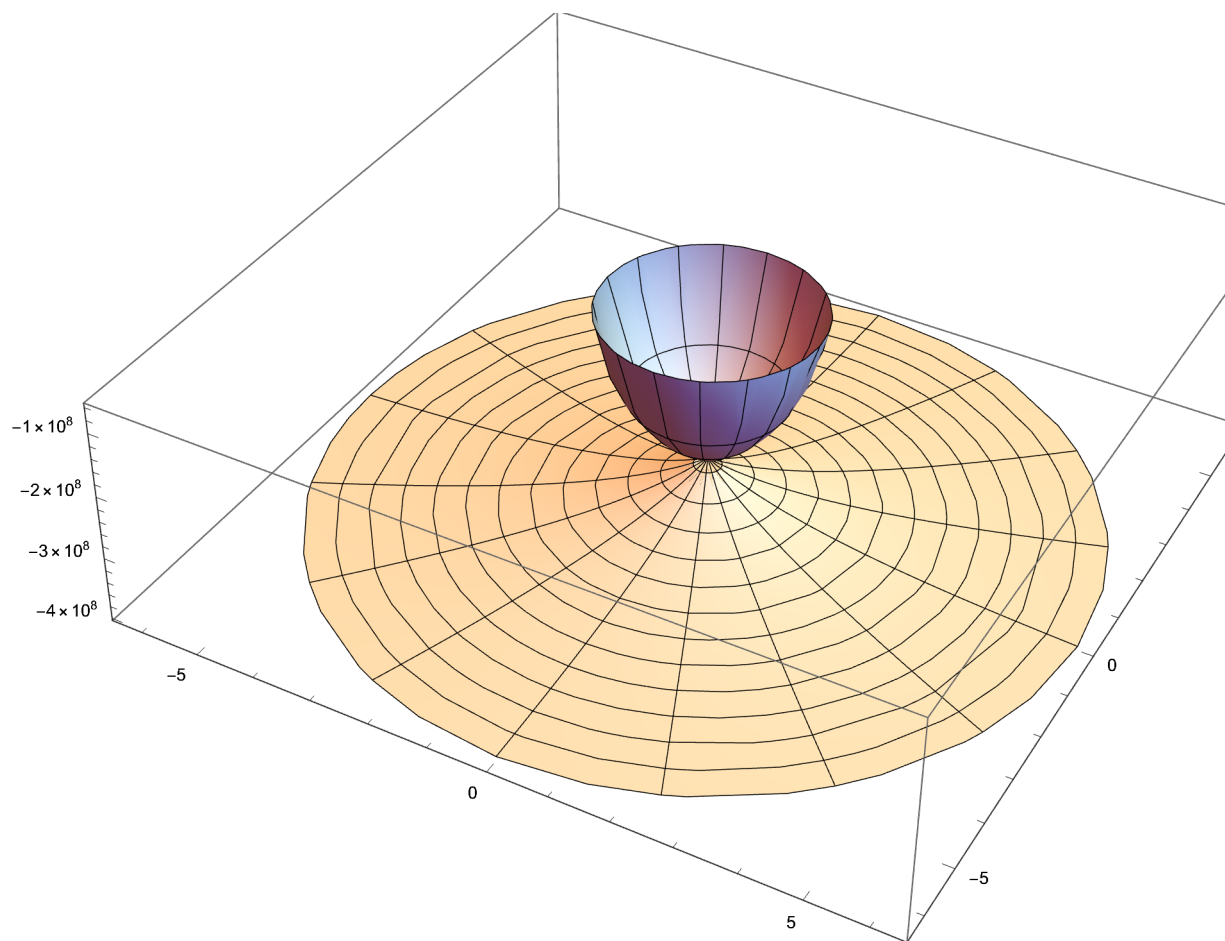


ContourPlot3D $\left[\left\{-\frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \frac{c \sqrt{4 \pi^2 r^2 - 4 \pi^2 \eta^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{r \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}\right]$

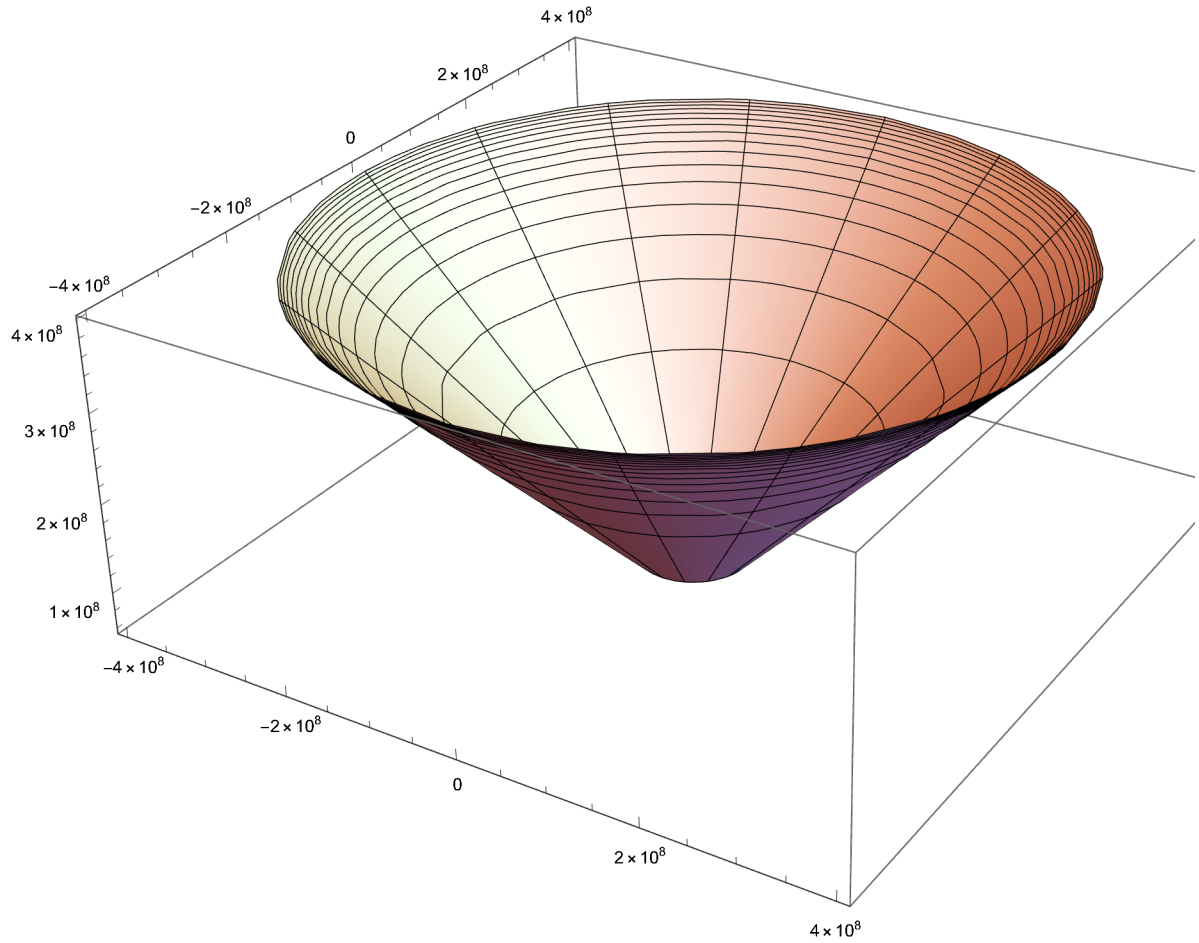


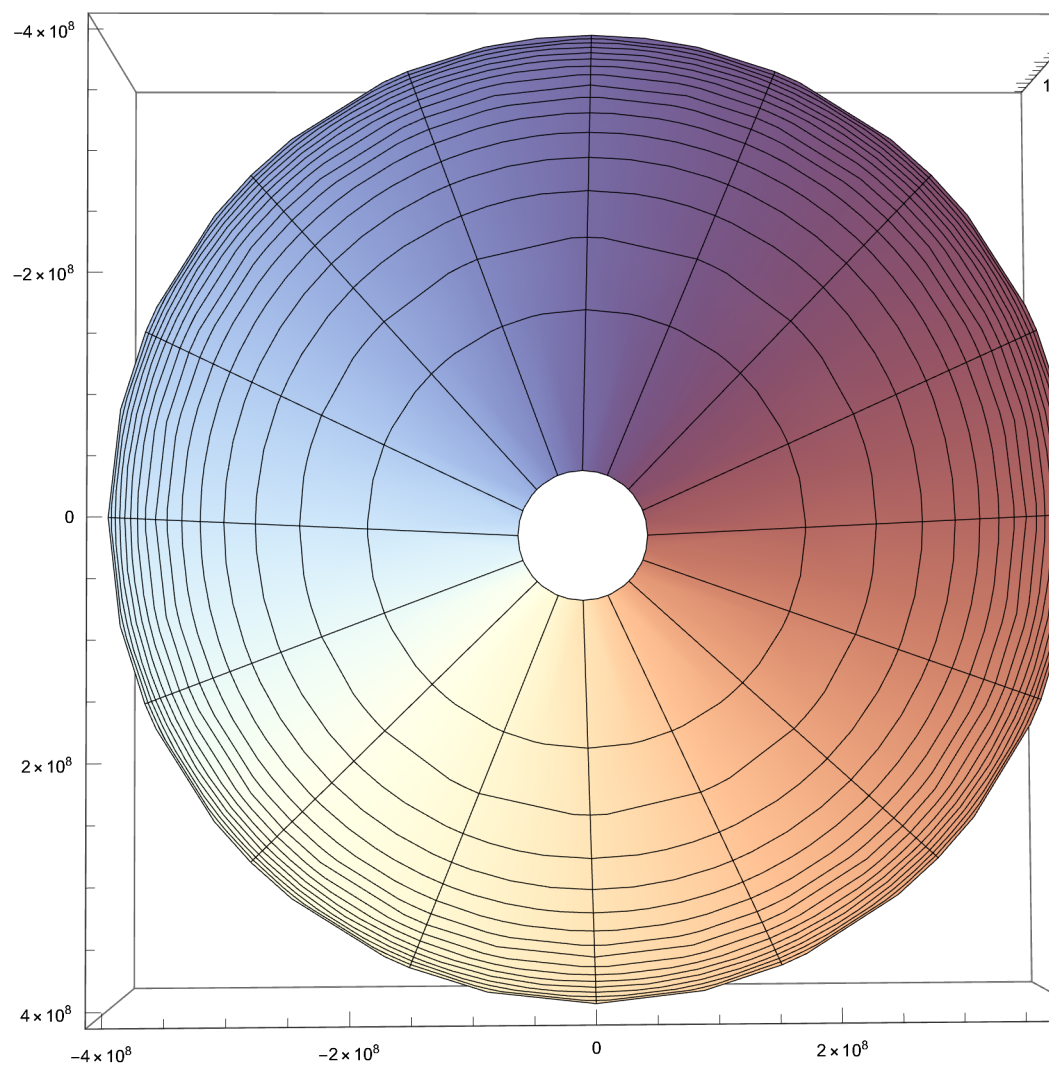
Solve $\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$   
 $\left\{\left\{v \rightarrow -\frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}, \left\{v \rightarrow \frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}\right\}$

$\text{RevolutionPlot3D}\left[-\frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{\theta, -2 \pi, 2 \pi\}\right]$



RevolutionPlot3D[  
 $\left\{ -\frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \frac{\sqrt{2} \sqrt{2 c^2 \pi^2 - 4 c^2 \pi \theta + c^2 \theta^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\}, \{\theta, -2 \pi, 2 \pi\}$   
 ]

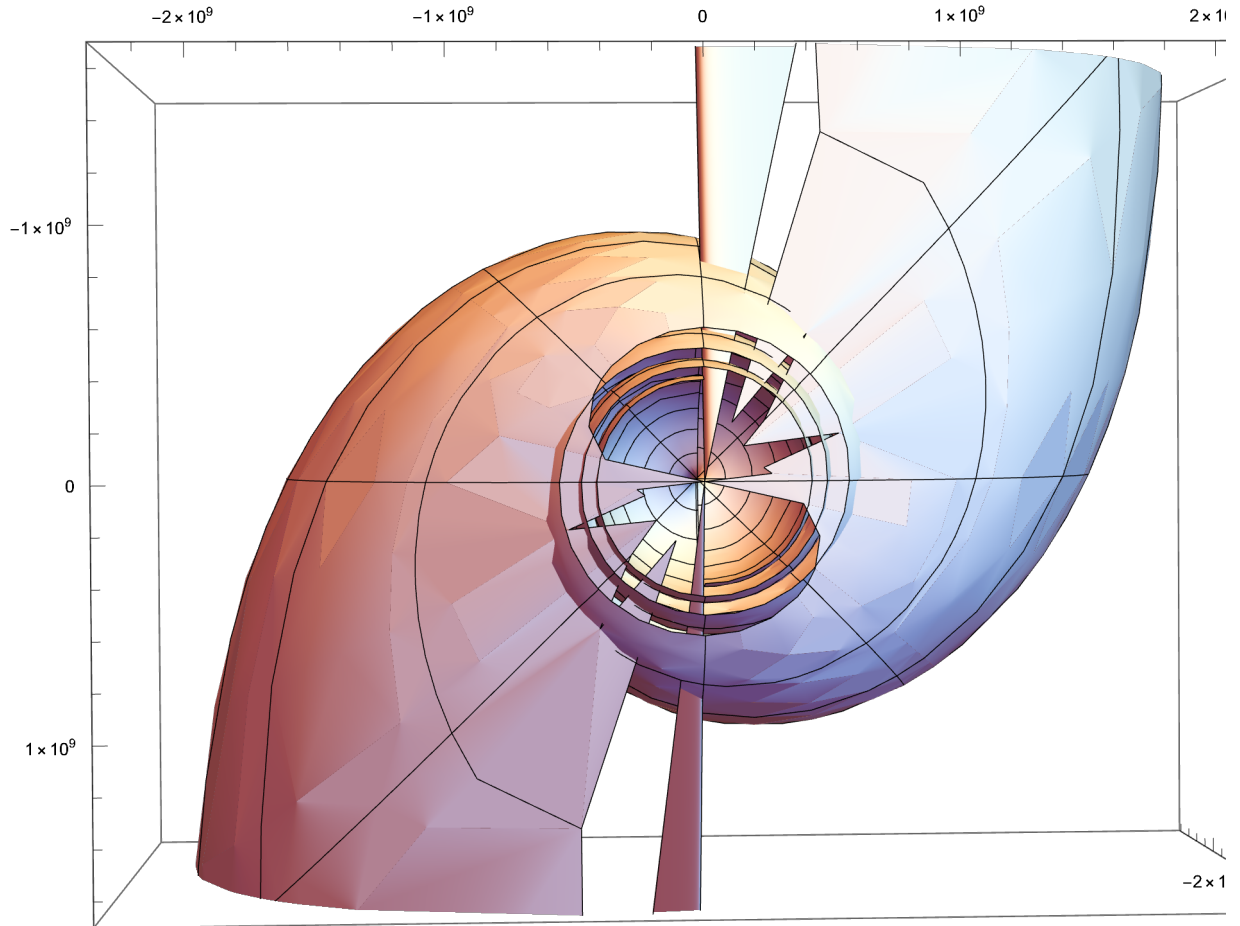




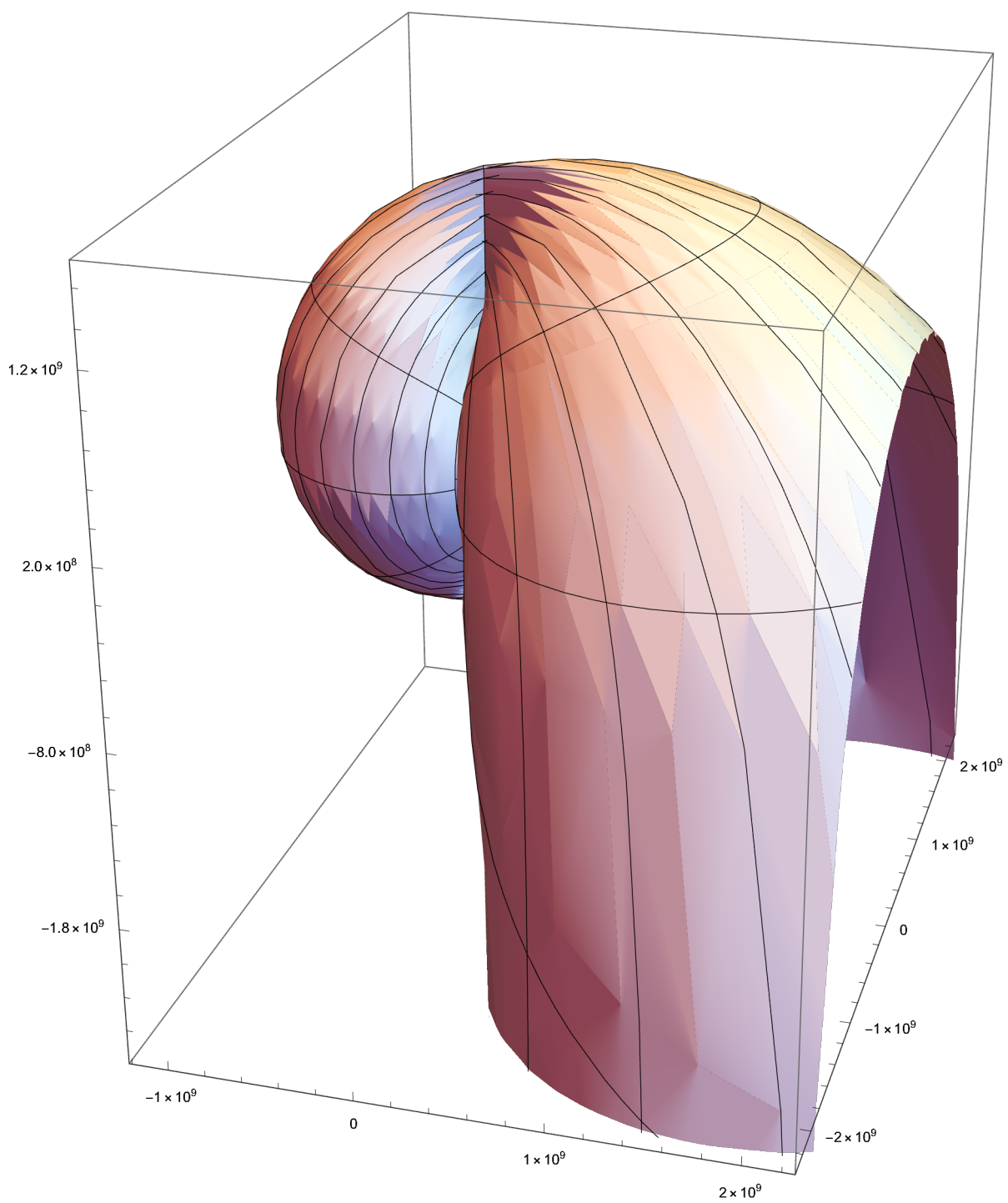
A brief substitution :

$c := 2.99792458 (10^8)$

$$\text{SphericalPlot3D}\left[-\left(\sqrt{2}\sqrt{\left(2c^2\pi^2-4c^2\pi\theta+c^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2\right)}\right)/\right. \\ \left.\left(\sqrt{4\pi^2-4\pi\theta+(\theta)^2}\right),\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$$



$$\text{SphericalPlot3D}\left[-\left(\sqrt{2}\sqrt{\left(2c^2\pi^2-4c^2\pi\theta+c^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2\right)}\right)/\right. \\ \left.\left(\sqrt{4\pi^2-4\pi\theta+(\theta)^2}\right),\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$$

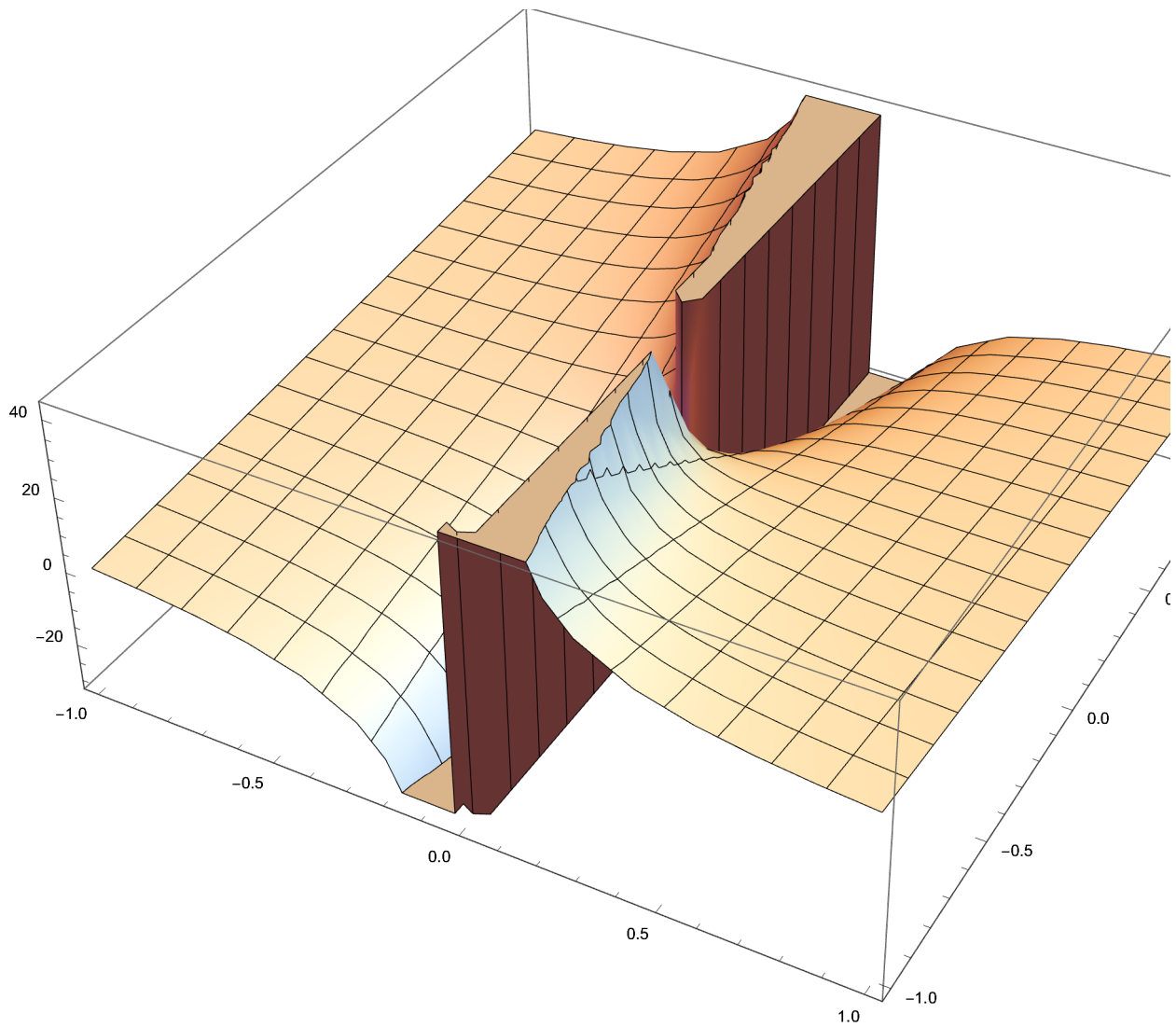


$2\pi\eta - 2\pi x' = \omega\eta$ , where  $\omega$  is an angle of a similar dimensional kind to theta, but different.

`Solve[ $2\pi\eta - 2\pi x' == \omega\eta$ ,  $\omega$ ]`

$$\left\{ \left\{ \omega \rightarrow \frac{2(\pi\eta - \pi x')}{\eta} \right\} \right\}$$

`Plot3D[ $\frac{2(\pi\eta - \pi x')}{\eta}$ , { $\eta$ , -1, 1}, { $x'$ , -1, 1}]`

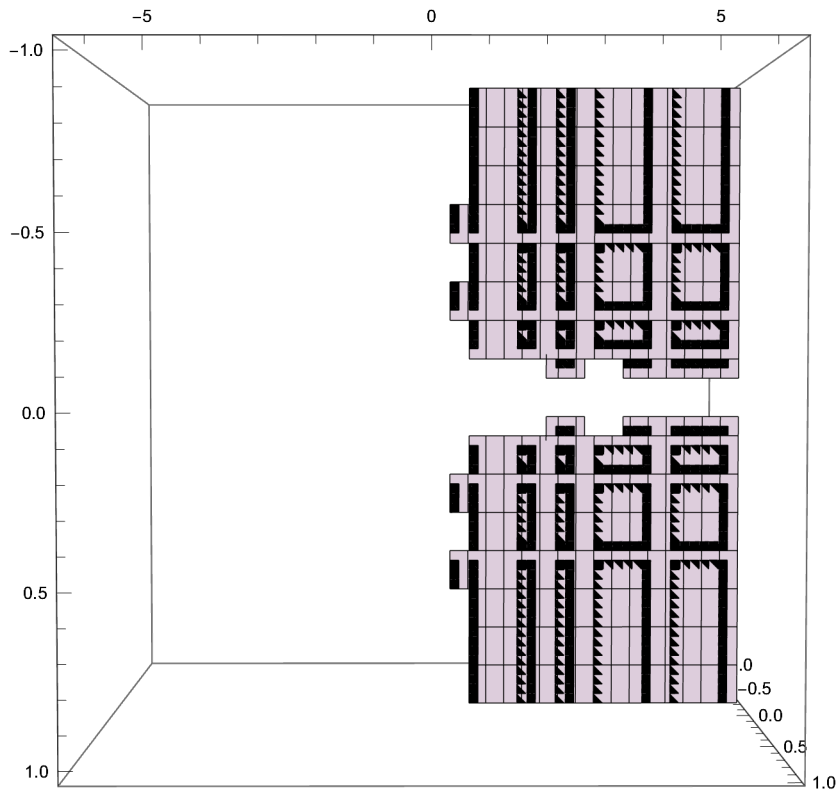




$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi x' == \omega \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \omega\right]$$

$$\left\{\left\{\omega \rightarrow \frac{2 \pi \left(\sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi x'\right)}{\sqrt{r^2 (4 \pi - \theta) \theta}}\right\}\right\}$$

$$\text{ContourPlot3D}\left[\frac{2 \pi \left(\sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi x'\right)}{\sqrt{r^2 (4 \pi - \theta) \theta}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{x', -1, 1\}\right]$$



$$v := \left( \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right)$$

$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{c^2}} == \omega \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \omega\right]$$

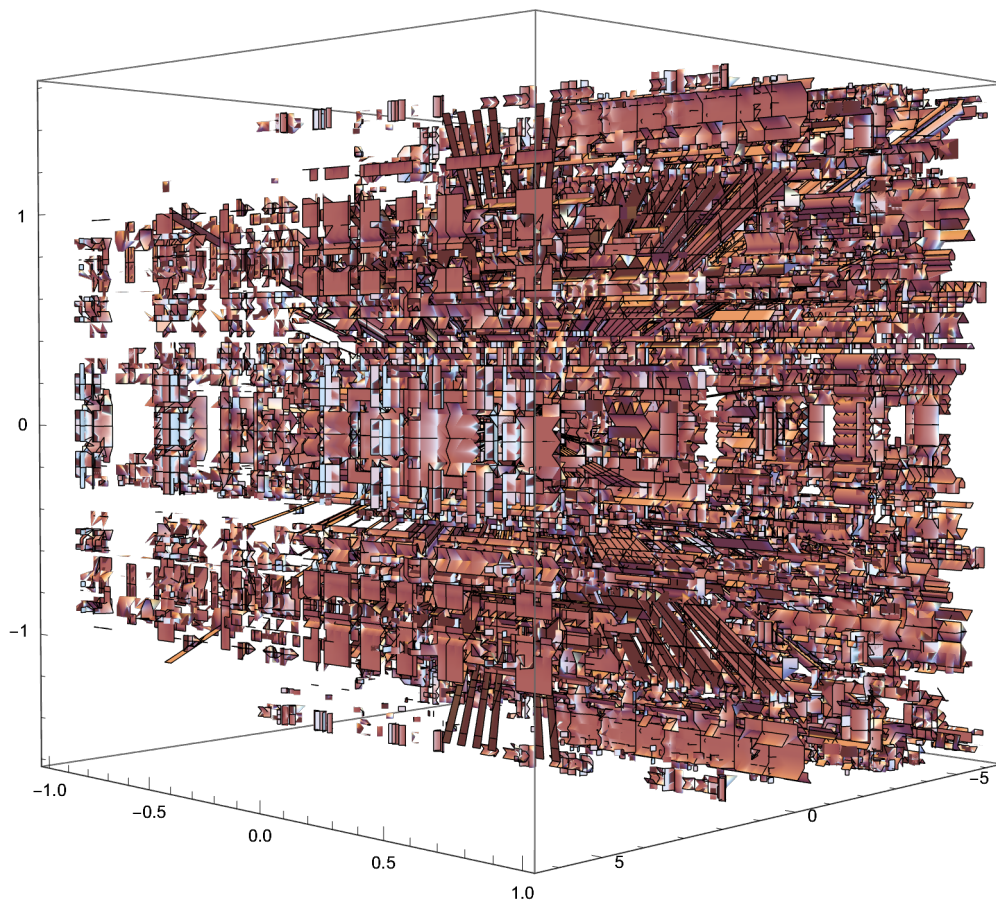
$$\left\{\left\{\omega \rightarrow\right.\right.$$

$$-\frac{1}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}} 6.28319 \left(-1. \sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2} + 1. (6.28319 r - 1. r \theta)\right.$$

$$\left.\sqrt{1.-\frac{1.11265 \times 10^{-17} \left(-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2\right)}{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}}\right.$$

$$\left.\right\}\left.\right\}$$

```
ContourPlot3D[-(6.283185307179586`
  (1.`√(1.`-1.1126500560536185`*^-17((√(-1.1294090667581471`*^18θ+
    8.987551787368176`*^16θ²+3.5481432270250993`*^18Sin[β]²)))/
    (√(-12.566370614359172`θ+θ²+39.47841760435743`Sin[β]²))))²)
  (6.283185307179586`r-1.`rθ)-1.`√12.566370614359172`r²θ-1.`r²θ²)))/
  (√12.566370614359172`r²θ-1.`r²θ²),
{β,
 -π/
  2, π/
  2}, {θ, -2
  π, 2
  π}, {r, -1, 1}]
```

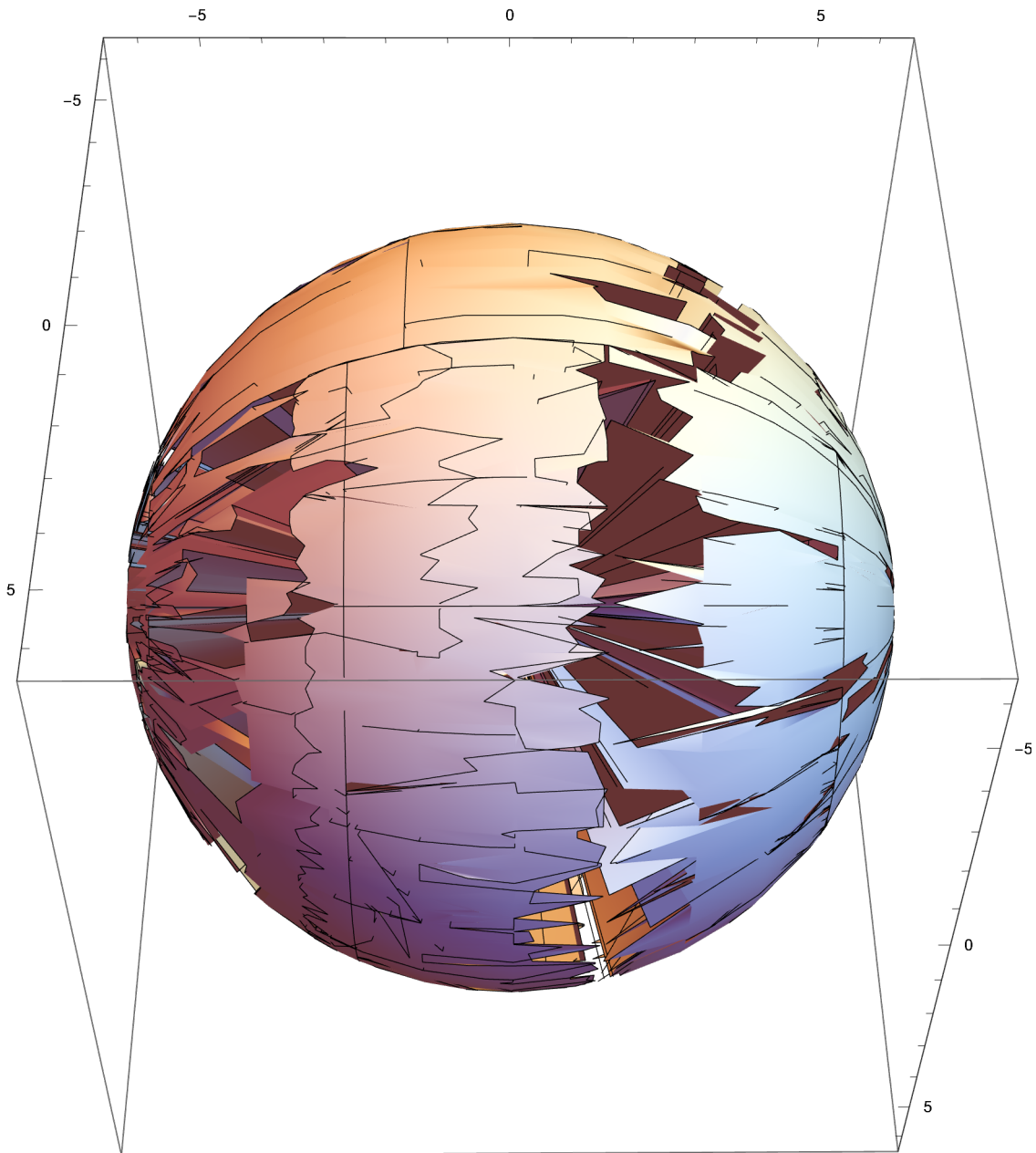


$$r := \frac{-4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3}$$

```

SphericalPlot3D[ - (6.283185307179586`
  (1.` Sqrt[ (1.` - 1.1126500560536185` *^-17 ( (Sqrt[ (-1.1294090667581471` *^18 ̸ +
    8.987551787368176` *^16 ̸^2 + 3.5481432270250993` *^18 Sin[̢]^2) ) ) /
    (Sqrt[ (-12.566370614359172` ̸ + ̸^2 + 39.47841760435743` Sin[̢]^2) ) ) )^2 )
    (6.283185307179586` r - 1.` r ̸) - 1.` Sqrt[12.566370614359172` r^2 ̸ - 1.` r^2 ̸^2] ) ) /
  ( Sqrt[12.566370614359172` r^2 ̸ - 1.` r^2 ̸^2] ),
{̸,
-2
  π, 2
  π}, {̢, -π /
  2, π /
  2} ]

```



$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} == \omega \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, v\right]$$

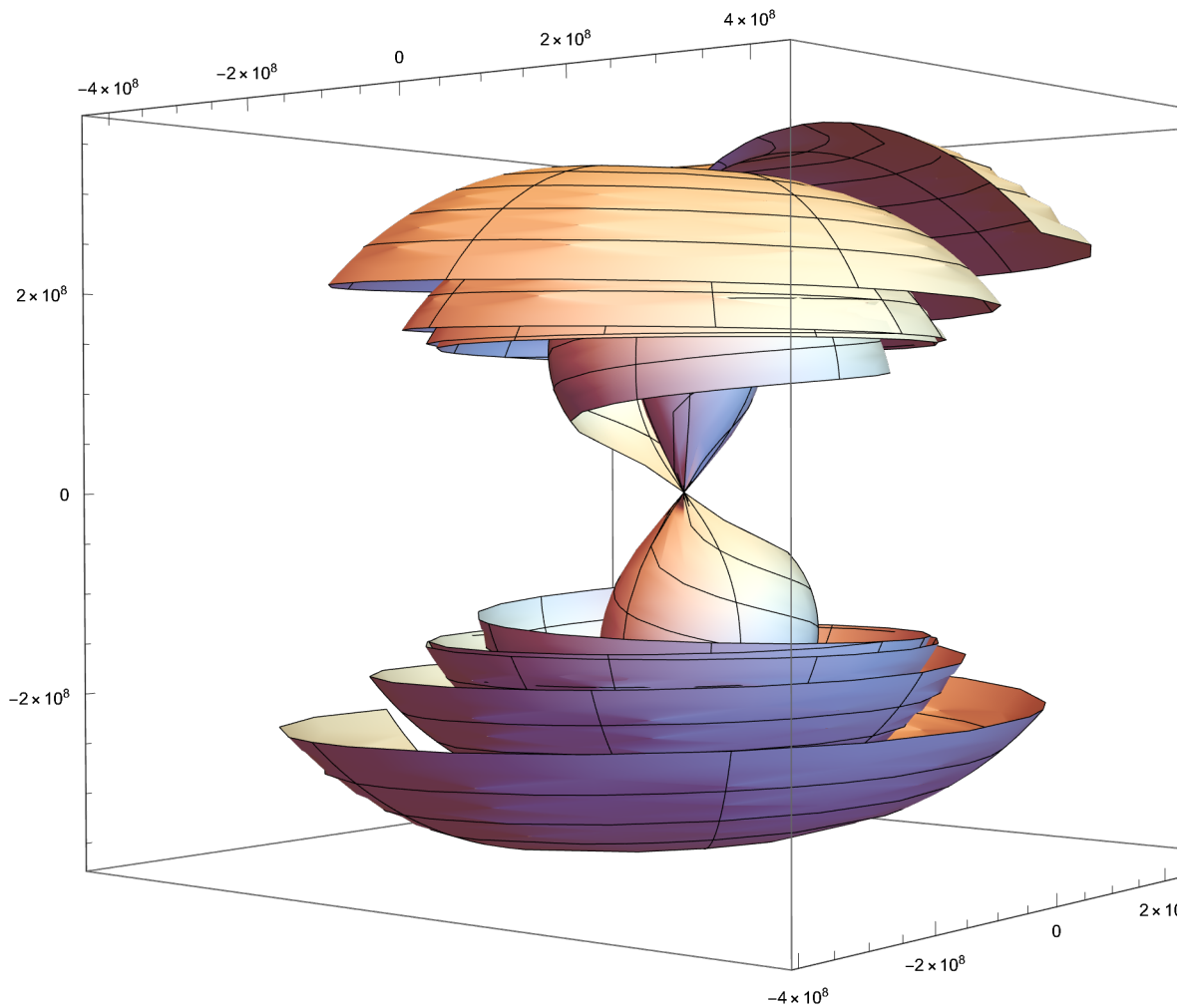
$$\left\{\left\{v \rightarrow -\frac{\sqrt{16 c^2 \pi^4 - 32 c^2 \pi^3 \theta + 8 c^2 \pi^2 \theta^2 + 16 c^2 \pi^2 \theta \omega - 4 c^2 \pi \theta^2 \omega - 4 c^2 \pi \theta \omega^2 + c^2 \theta^2 \omega^2}}{\sqrt{16 \pi^4 - 16 \pi^3 \theta + 4 \pi^2 \theta^2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{16 c^2 \pi^4 - 32 c^2 \pi^3 \theta + 8 c^2 \pi^2 \theta^2 + 16 c^2 \pi^2 \theta \omega - 4 c^2 \pi \theta^2 \omega - 4 c^2 \pi \theta \omega^2 + c^2 \theta^2 \omega^2}}{\sqrt{16 \pi^4 - 16 \pi^3 \theta + 4 \pi^2 \theta^2}}\right\}\right\}$$

$$\begin{aligned}
& \text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{c^2}} == \omega \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, v\right] \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( 1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 7.57575 \times 10^{46} \theta^2 + 1.51515 \times 10^{47} \theta \omega - \right. \right. \right. \\
& \quad \left. \left. \left. 1.20572 \times 10^{46} \theta^2 \omega - 1.20572 \times 10^{46} \theta \omega^2 + 9.59481 \times 10^{44} \theta^2 \omega^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2} \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( 1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 7.57575 \times 10^{46} \theta^2 + 1.51515 \times 10^{47} \theta \omega - \right. \right. \right. \\
& \quad \left. \left. \left. 1.20572 \times 10^{46} \theta^2 \omega - 1.20572 \times 10^{46} \theta \omega^2 + 9.59481 \times 10^{44} \theta^2 \omega^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2} \right) \right\} \}
\end{aligned}$$

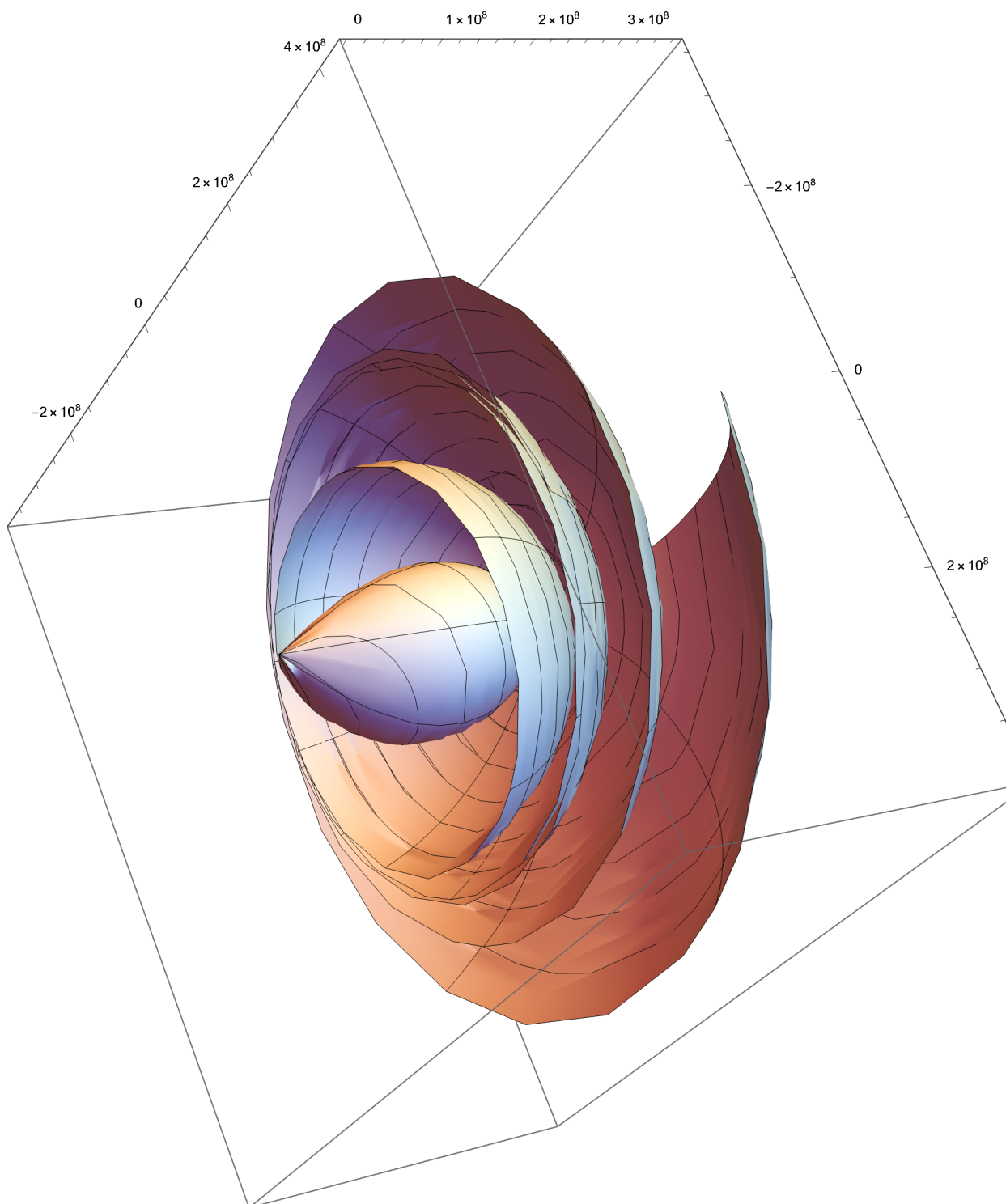
SphericalPlot3D[

$$\left\{ - \left( 1. \sqrt{ \left( 1.495394089917615 \cdot \theta^{48} - 9.519974451231788 \cdot \theta^{47} \omega + 7.575754960110463 \cdot \theta^{46} \omega^2 + 1.5151509920220929 \cdot \theta^{47} \omega - 1.2057188495545248 \cdot \theta^{46} \omega^2 - 1.2057188495545248 \cdot \theta^{46} \omega^2 + 9.594805744283795 \cdot \theta^{44} \omega^2 \right) } \right. \\ \left. \left( \sqrt{ \left( 1.663850317969084 \cdot \theta^{31} - 5.296200053396031 \cdot \theta^{30} \omega + 4.2145820905076925 \cdot \theta^{29} \omega^2 \right) } \right), \right. \\ \left. \left( \sqrt{ \left( 1.495394089917615 \cdot \theta^{48} - 9.519974451231788 \cdot \theta^{47} \omega + 7.575754960110463 \cdot \theta^{46} \omega^2 + 1.5151509920220929 \cdot \theta^{47} \omega - 1.2057188495545248 \cdot \theta^{46} \omega^2 - 1.2057188495545248 \cdot \theta^{46} \omega^2 + 9.594805744283795 \cdot \theta^{44} \omega^2 \right) } \right) / \right. \\ \left. \left( \sqrt{ \left( 1.663850317969084 \cdot \theta^{31} - 5.296200053396031 \cdot \theta^{30} \omega + 4.2145820905076925 \cdot \theta^{29} \omega^2 \right) } \right) \right\}, \{\theta, -\pi/3, \pi/3\}, \{\omega, -3\pi, 3\pi\}]$$



```
SphericalPlot3D[
  (√(1.495394089917615`*^48 - 9.519974451231788`*^47 θ + 7.575754960110463`*^46 θ² +
    1.5151509920220929`*^47 θ ω - 1.2057188495545248`*^46 θ² ω -
    1.2057188495545248`*^46 θ ω² + 9.594805744283795`*^44 θ² ω²)) /
  (√(1.663850317969084`*^31 - 5.296200053396031`*^30 θ +
    4.2145820905076925`*^29 θ²)), {θ, -π / 3, π / 3}, {ω, -3 π, 3 π}]
```





Synchronized angles:  $2 \pi \eta - 2 \pi x' = \theta \eta$

Solve[ $2 \pi \eta - 2 \pi x' == \theta \eta, \theta$ ]

Solve[ $2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi x' == \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta$ ]

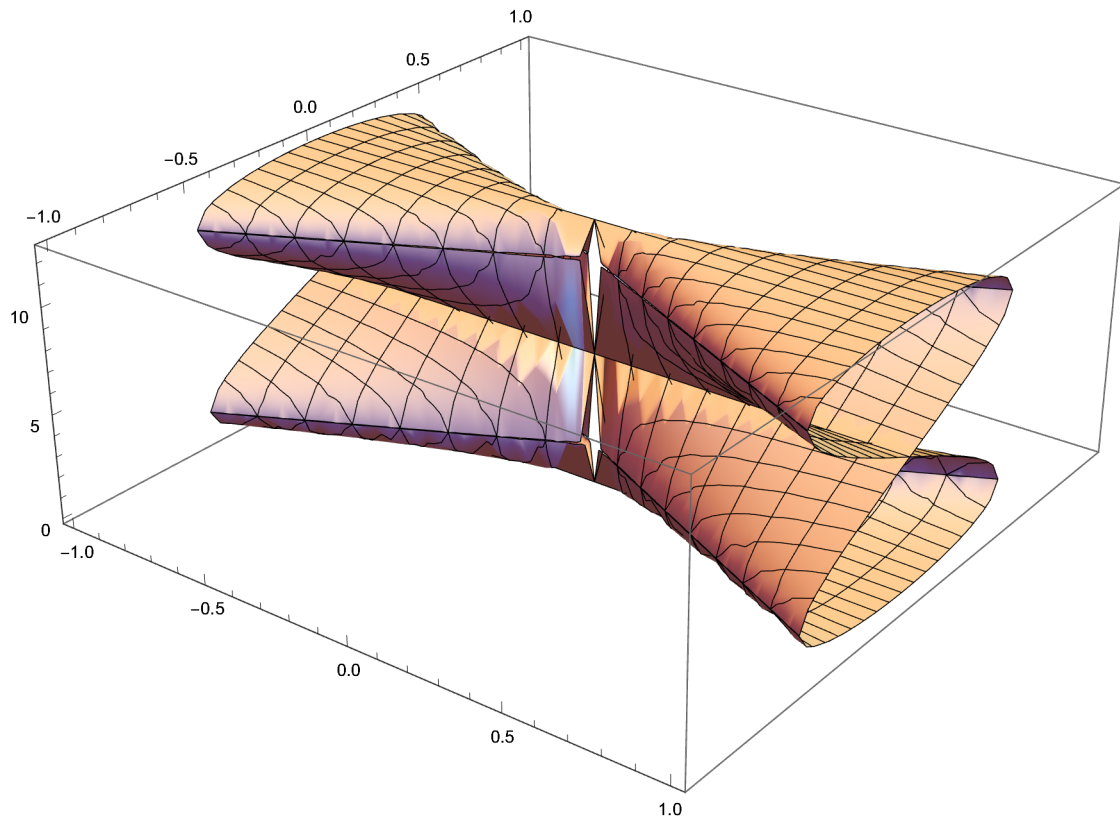
$$\left\{ \left\{ \theta \rightarrow \frac{2 \pi r^2 - \sqrt{2} \pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2} \right\} \right\},$$

$$\left\{ \theta \rightarrow \frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2} \right\},$$

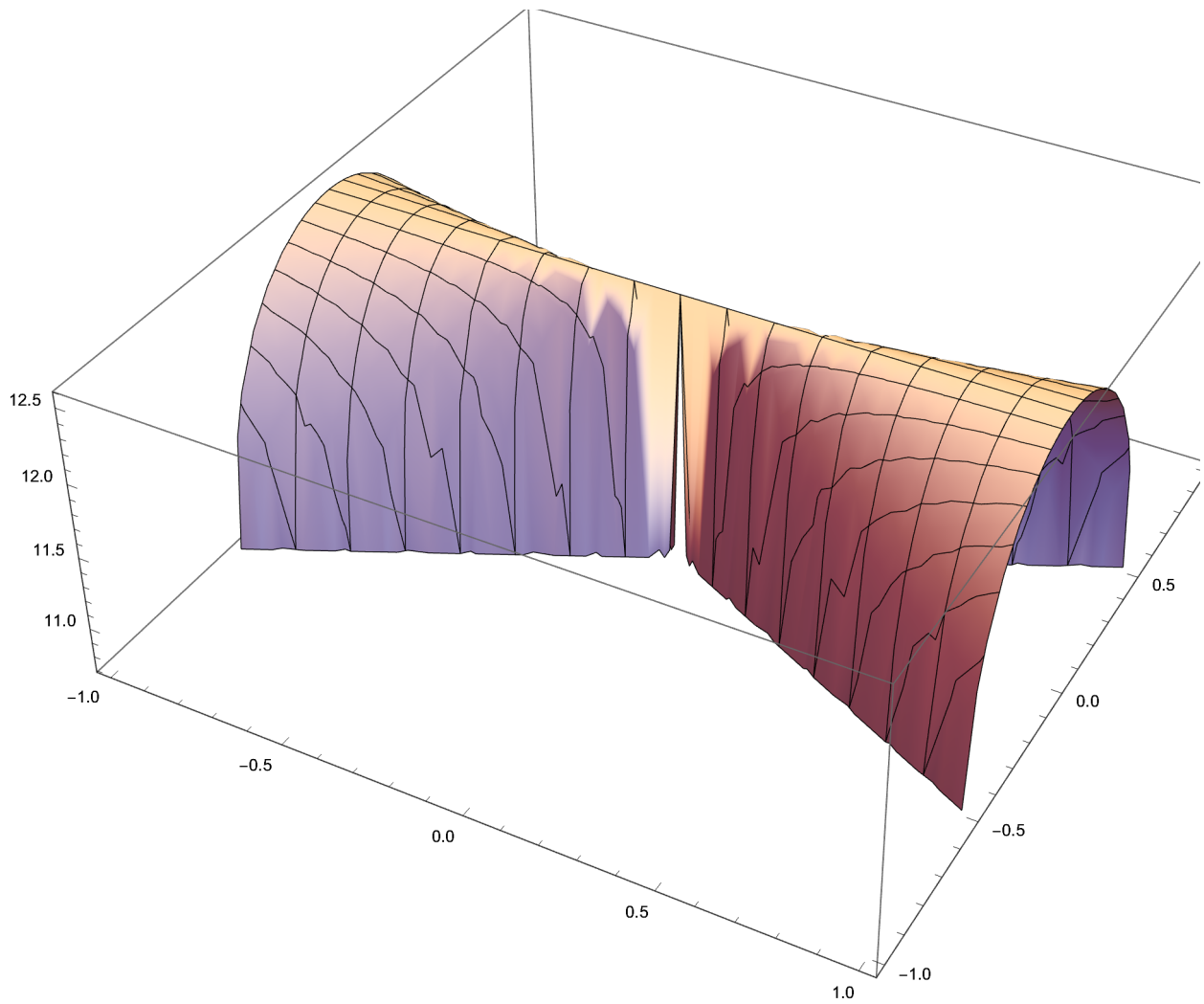
$$\left\{ \theta \rightarrow \frac{2 \pi r^2 - \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2} \right\},$$

$$\left\{ \theta \rightarrow \frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2} \right\}$$

$$\text{Plot3D}\left[\left\{\frac{2 \pi r^2 - \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}, \frac{2 \pi r^2 - \sqrt{2} \pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}, \frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}, \frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}\right\}, \{r, -1, 1\}, \{x', -1, 1\}\right]$$



Plot3D $\left[\frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}, \{r, -1, 1\}, \{x', -1, 1\}\right]$



$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi x' == \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

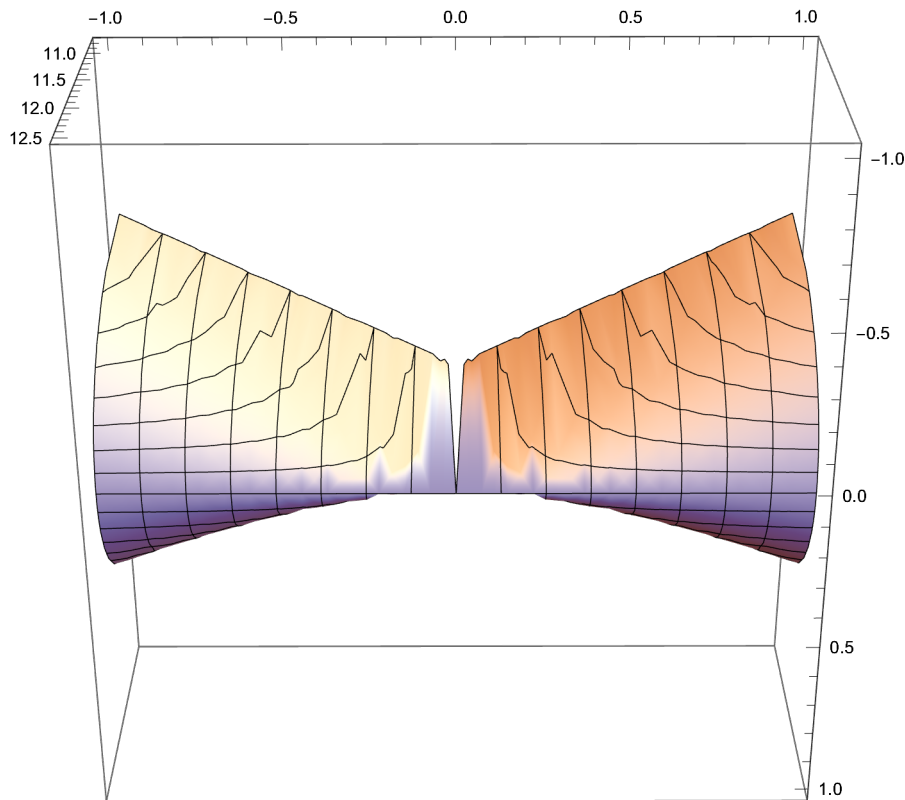
$$\left\{\left\{\theta \rightarrow \frac{2 \pi r^2 - \sqrt{2} \pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}\right\},\right.$$

$$\left\{\theta \rightarrow \frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 - r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}\right\},$$

$$\left\{\theta \rightarrow \frac{2 \pi r^2 - \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}\right\},$$

$$\left\{\theta \rightarrow \frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}\right\}\}$$

$$\text{Plot3D}\left[\frac{2 \pi r^2 + \sqrt{2} \pi \sqrt{r^4 + r^2} \sqrt{r^2 (r^2 - 4 (x')^2)}}{r^2}, \{x', -1, 1\}, \{r, -1, 1\}\right]$$



$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} == \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2 \pi\right\}, \left\{\theta \rightarrow \frac{2 (c \pi - \pi v)}{c}\right\}, \left\{\theta \rightarrow \frac{2 (c \pi + \pi v)}{c}\right\}\right\}$$

```

Manipulate[SphericalPlot3D[
  {

$$\frac{1}{c} 2 \left( c \pi + \pi \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) \right) /$$

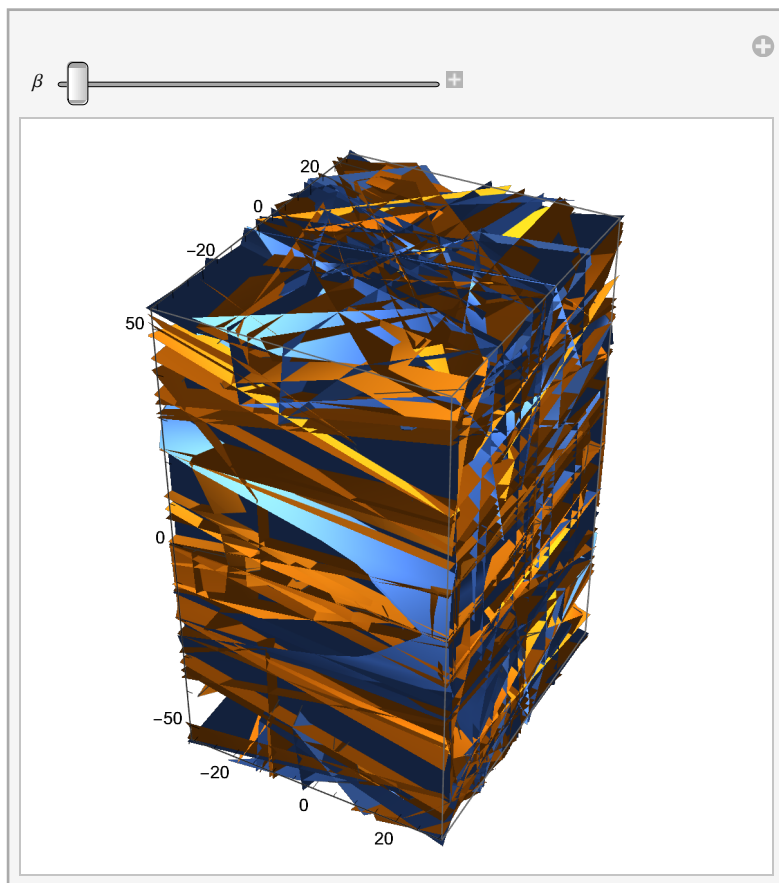

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right),$$


$$\frac{1}{c} 2 \left( c \pi - \pi \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) \right) /$$


$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \},$$

  {
 $\theta, -2\pi, 2\pi$ 
}, {
 $c, -3 \cdot 10^8, 3 \cdot 10^8$ 
}, {
 $\beta,$ 
 $-4$ 
 $\pi, 4$ 
 $\pi$ 
}
]

```



General::ivar : 2.99792458`\*^8 is not a valid variable. >>

General::ivar : 2.99792458`\*^8 is not a valid variable. >>

General::ivar : 2.99792458`\*^8 is not a valid variable. >>

General::stop : Further output of General::ivar will be suppressed during this calculation. >>

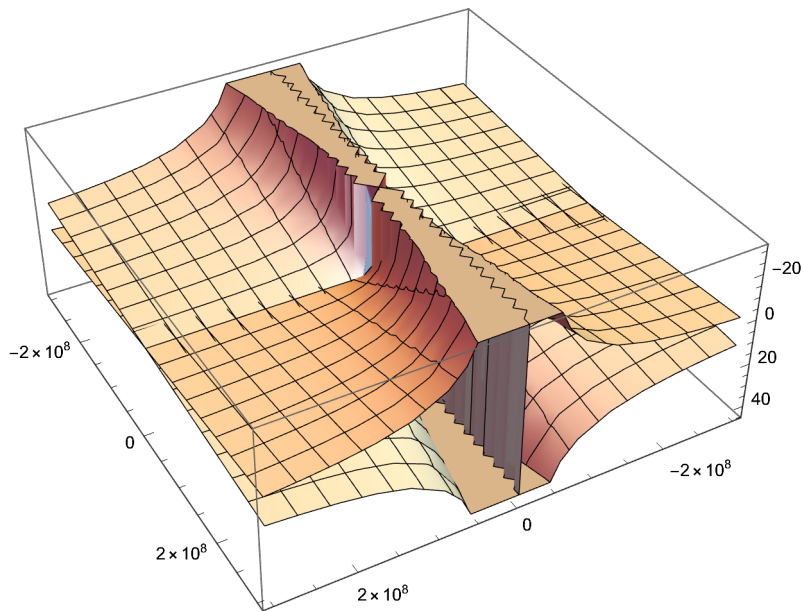
... General: 2.99792458`\*^8 is not a valid variable.

... General: 2.99792458`\*^8 is not a valid variable.

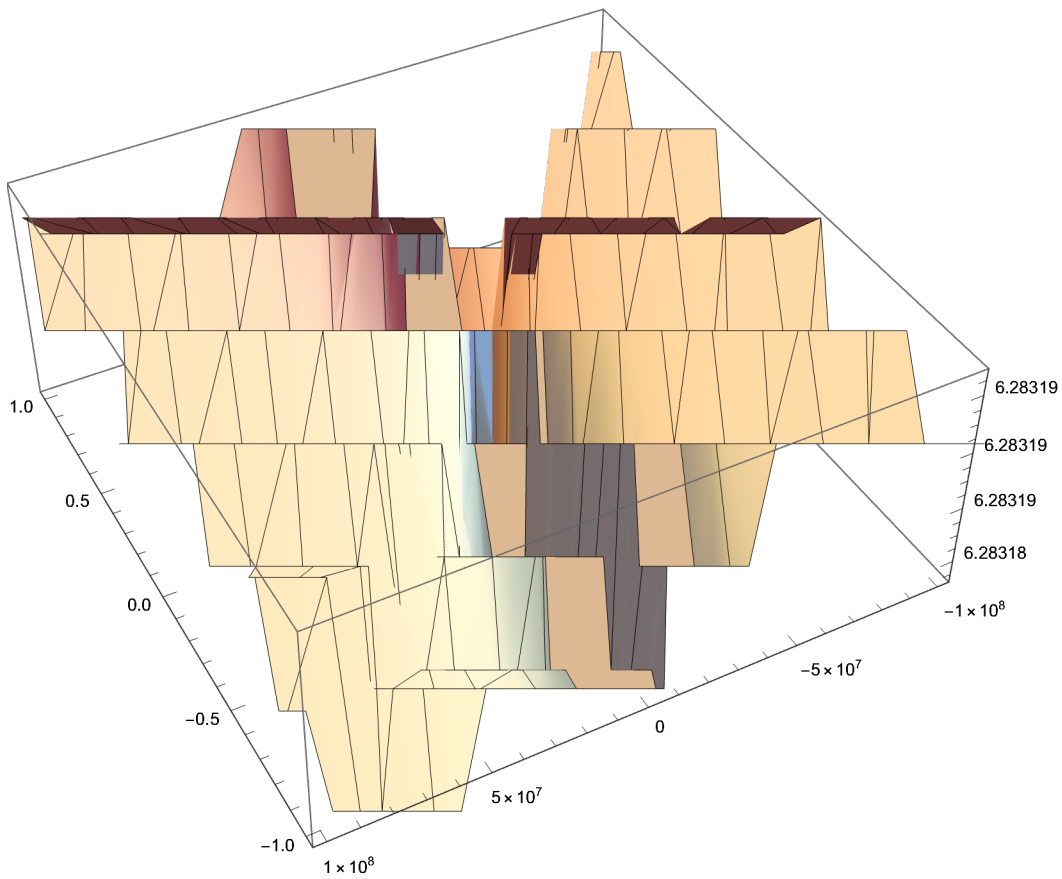
... General: 2.99792458`\*^8 is not a valid variable.

... General: Further output of General::ivar will be suppressed during this calculation.

$\text{Plot3D}\left[\left\{\frac{2(c\pi + \pi v)}{c}, \frac{2(c\pi - \pi v)}{c}\right\}, \{v, -3 \times 10^8, 3 \times 10^8\}, \{c, -3 \times 10^8, 3 \times 10^8\}\right]$



Plot3D $\left[\frac{2 (c \pi + \pi v)}{c}, \{v, -1, 1\}, \{c, -10^8, 10^8\}\right]$



$$r := \frac{-4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi}}{16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3}$$



$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \frac{2\pi r - r\theta}{2\pi} \sqrt{1 - \frac{v^2}{c^2}} == \theta \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, v\right]$$

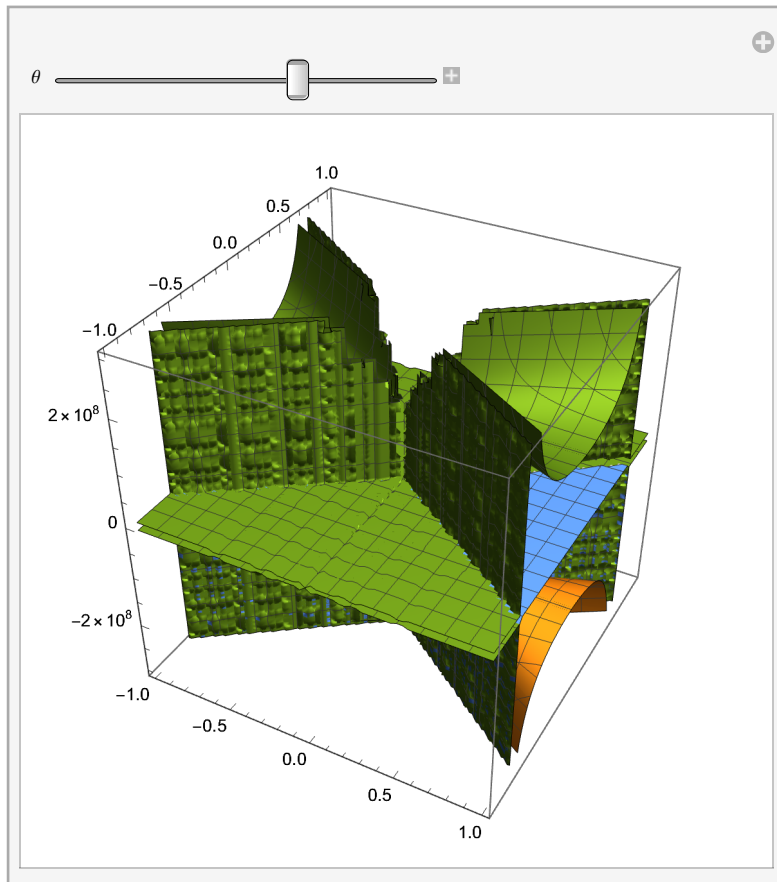
$$\left\{\left\{v \rightarrow -\frac{1}{2}c \sqrt{4 - \frac{4\theta}{\pi} + \frac{\theta^2}{\pi^2}}\right\}, \left\{v \rightarrow \frac{1}{2}c \sqrt{4 - \frac{4\theta}{\pi} + \frac{\theta^2}{\pi^2}}\right\}\right\}$$

$$x = \eta' = \frac{2\pi r - r\theta}{2\pi} = \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}}$$

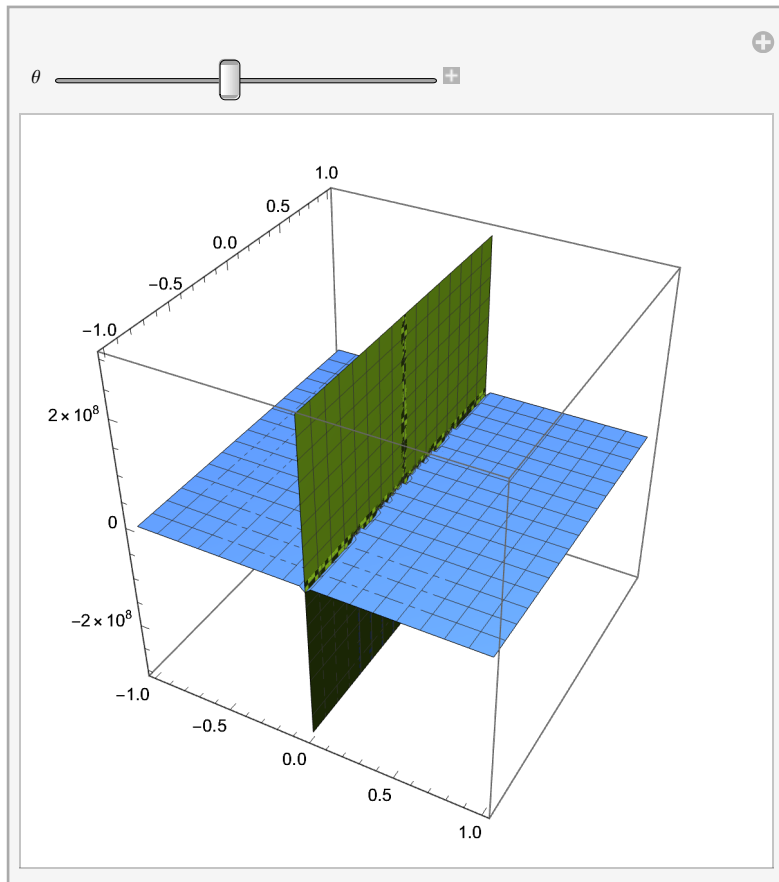
$$\text{Solve}\left[x == \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -c \sqrt{1 - \frac{\pi x^2}{r^2(4\pi - \theta)} - \frac{\pi x^2}{r^2\theta}}\right\}, \left\{v \rightarrow c \sqrt{1 - \frac{\pi x^2}{r^2(4\pi - \theta)} - \frac{\pi x^2}{r^2\theta}}\right\}\right\}$$

$$\text{Manipulate}\left[\text{ContourPlot3D}\left[c \sqrt{1 - \frac{\pi x^2}{r^2(4\pi - \theta)} - \frac{\pi x^2}{r^2\theta}}, \{r, -1, 1\}, \{x, -1, 1\}, \{c, -3 \cdot 10^8, 3 \cdot 10^8\}\right], \{\theta, -2\pi, 2\pi\}\right]$$



- ... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.
- ... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.
- ... **Infinity:** Indeterminate expression  $1 + \text{ComplexInfinity} + \text{ComplexInfinity}$  encountered.
- ... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.
- ... **General:** Further output of Power::infy will be suppressed during this calculation.
- ... **Infinity:** Indeterminate expression  $0. \text{ComplexInfinity}$  encountered.
- ... **Infinity:** Indeterminate expression  $0. \text{ComplexInfinity}$  encountered.
- ... **General:** Further output of Infinity::indet will be suppressed during this calculation.



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression  $1 + \text{ComplexInfinity} + \text{ComplexInfinity}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression  $0. \text{ComplexInfinity}$  encountered.

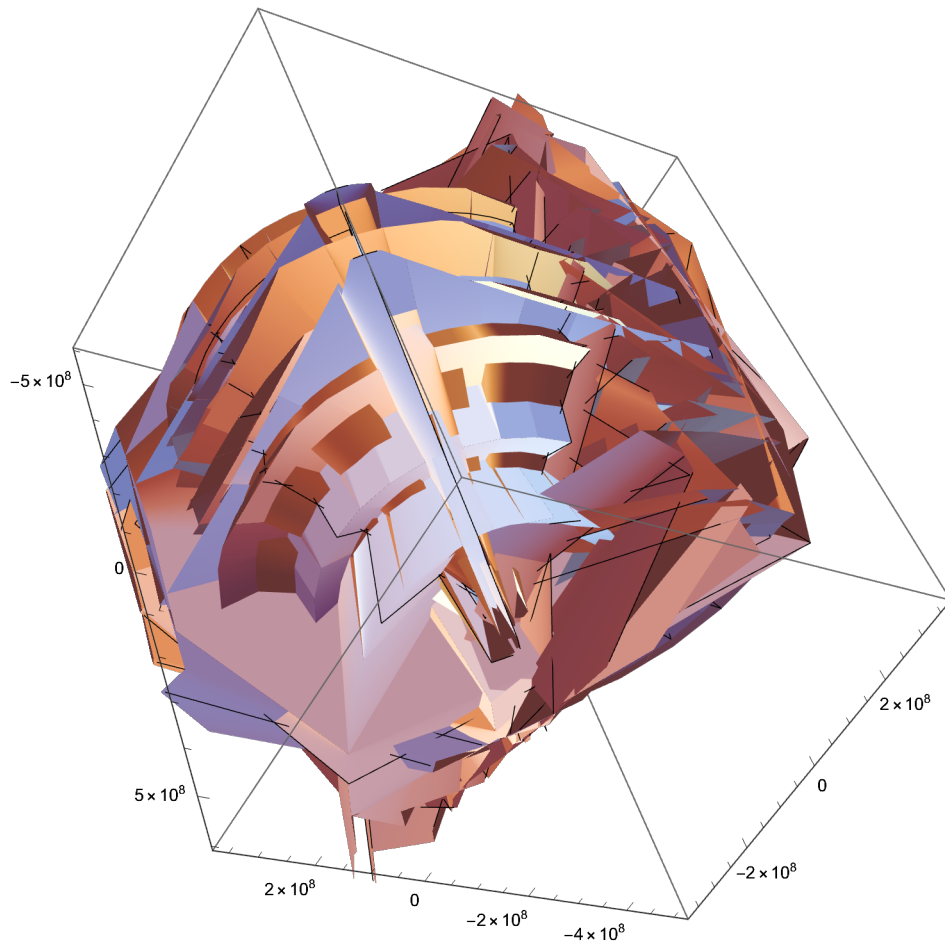
... **Infinity:** Indeterminate expression  $0. \text{ComplexInfinity}$  encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

$$\text{Solve}\left[\frac{2\pi r - r\theta}{2\pi} == \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

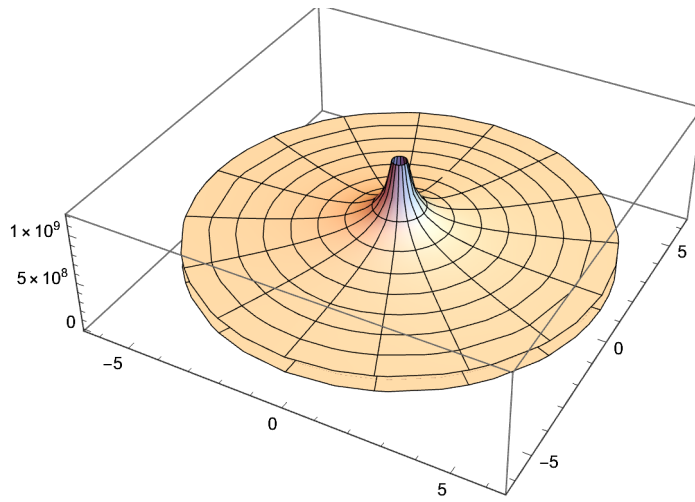
$$\left\{\left\{v \rightarrow -c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{\theta}}\right\}, \left\{v \rightarrow c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{\theta}}\right\}\right\}$$

```
SphericalPlot3D[c  $\sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{\theta}}$ ,
{c, -2.99792458 (10^8), 2.99792458 (10^8)}, {θ, -2 π, 2 π}]
```

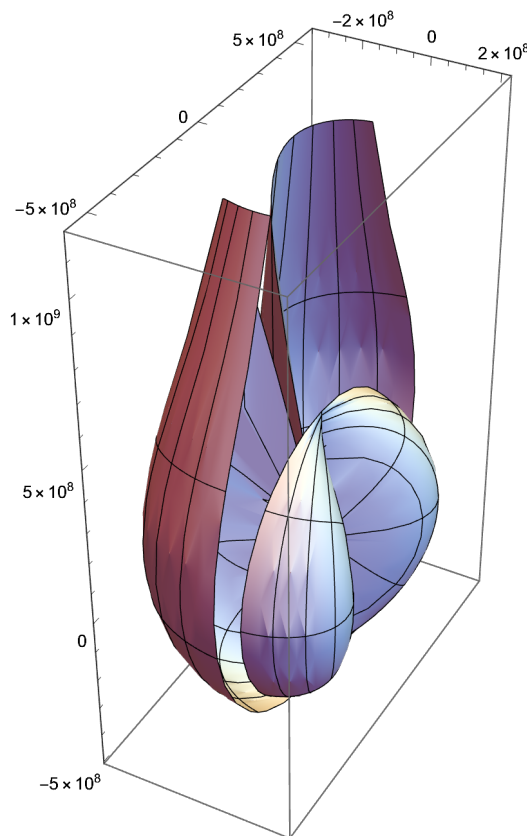


```
c := 2.99792458 (10^8)
```

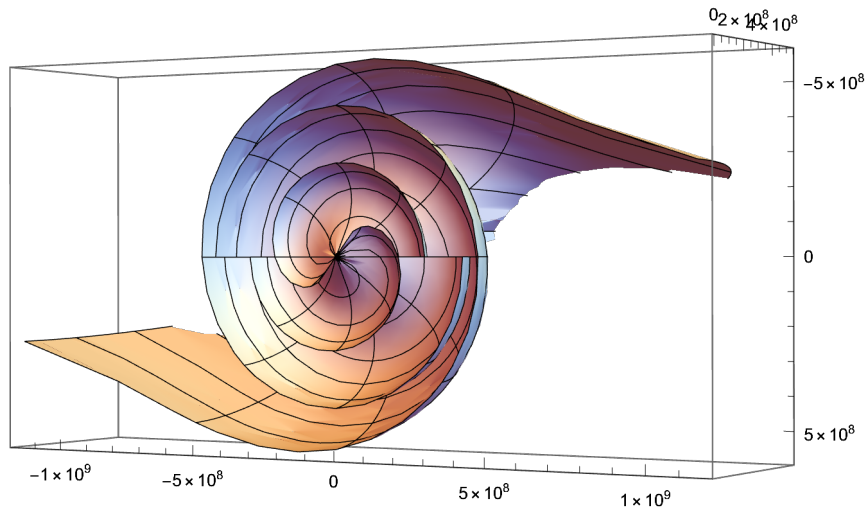
`RevolutionPlot3D` $\left[c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{\theta}}, \{\theta, -2\pi, 2\pi\}\right]$



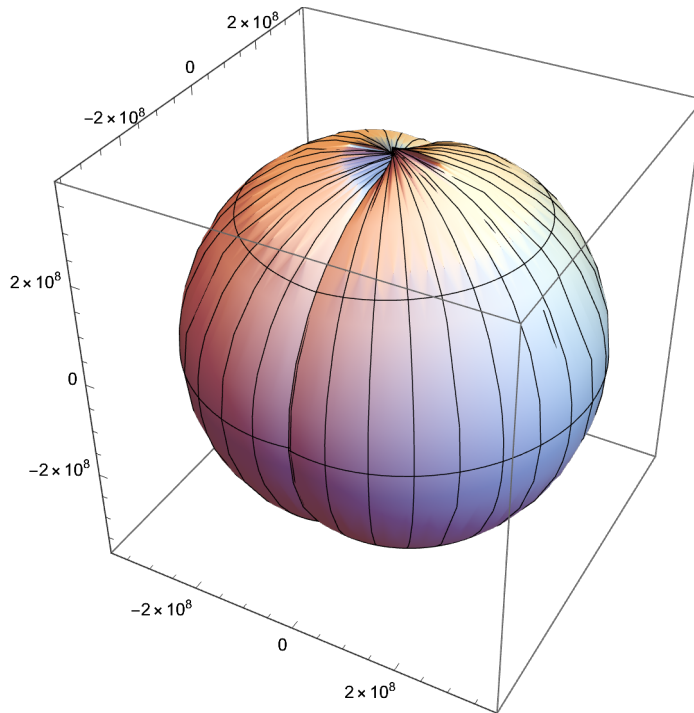
`SphericalPlot3D` $\left[c \sqrt{2 - \frac{\pi}{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} - \frac{\pi}{\theta}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



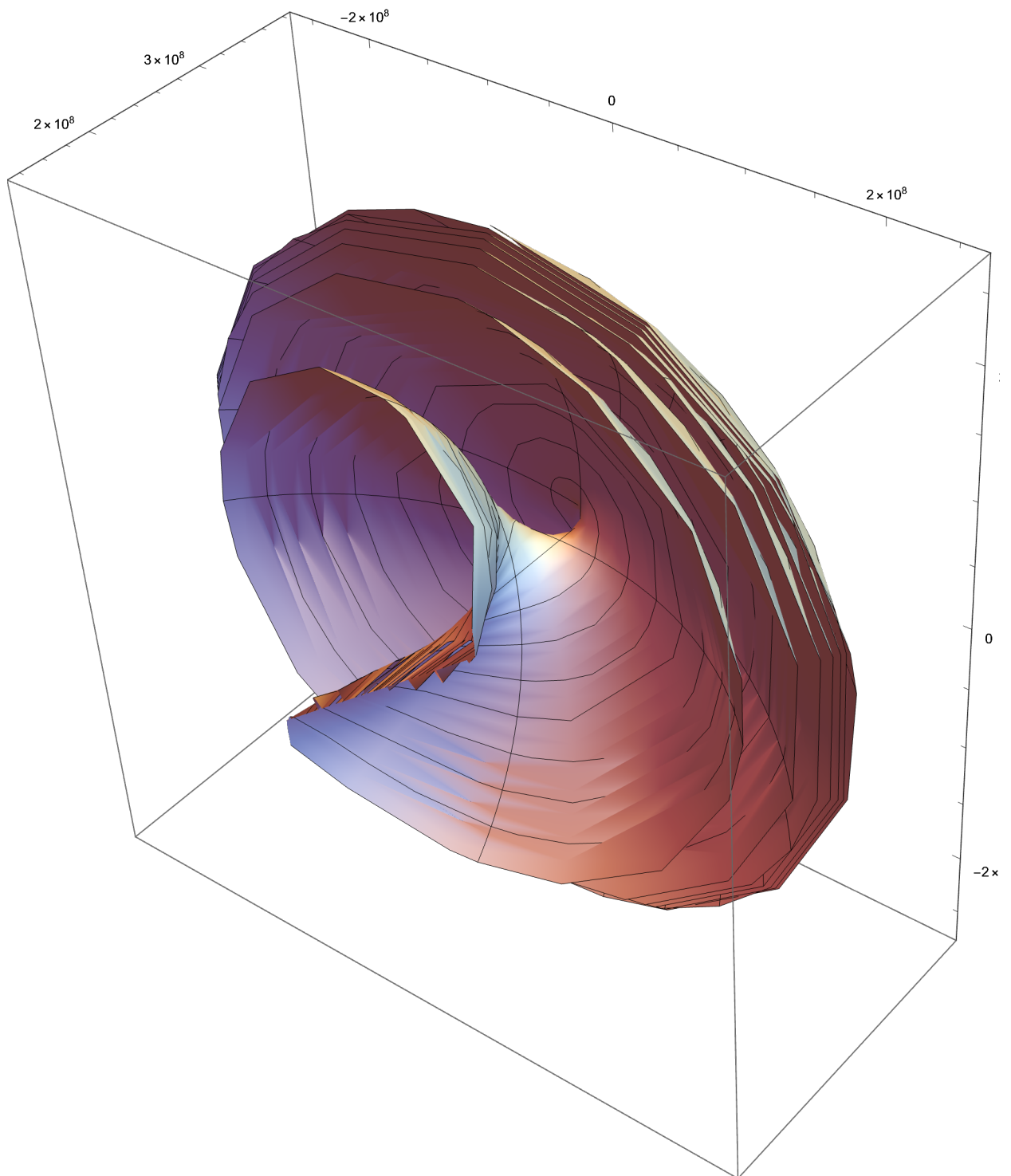
$\text{SphericalPlot3D}\left[c \sqrt{2 - \frac{\pi}{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} - \frac{\pi}{\theta}}, \right.$   
 $\left.\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



$\text{SphericalPlot3D}\left[c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}, \right.$   
 $\left.\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



$$\text{SphericalPlot3D}\left[c \sqrt{2 - \frac{\pi}{4\pi - \theta} - \frac{\pi}{2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}, \right. \\ \left. \{\beta, -\pi/4, \pi/4\}, \{\theta, -4\pi, 4\pi\}\right]$$

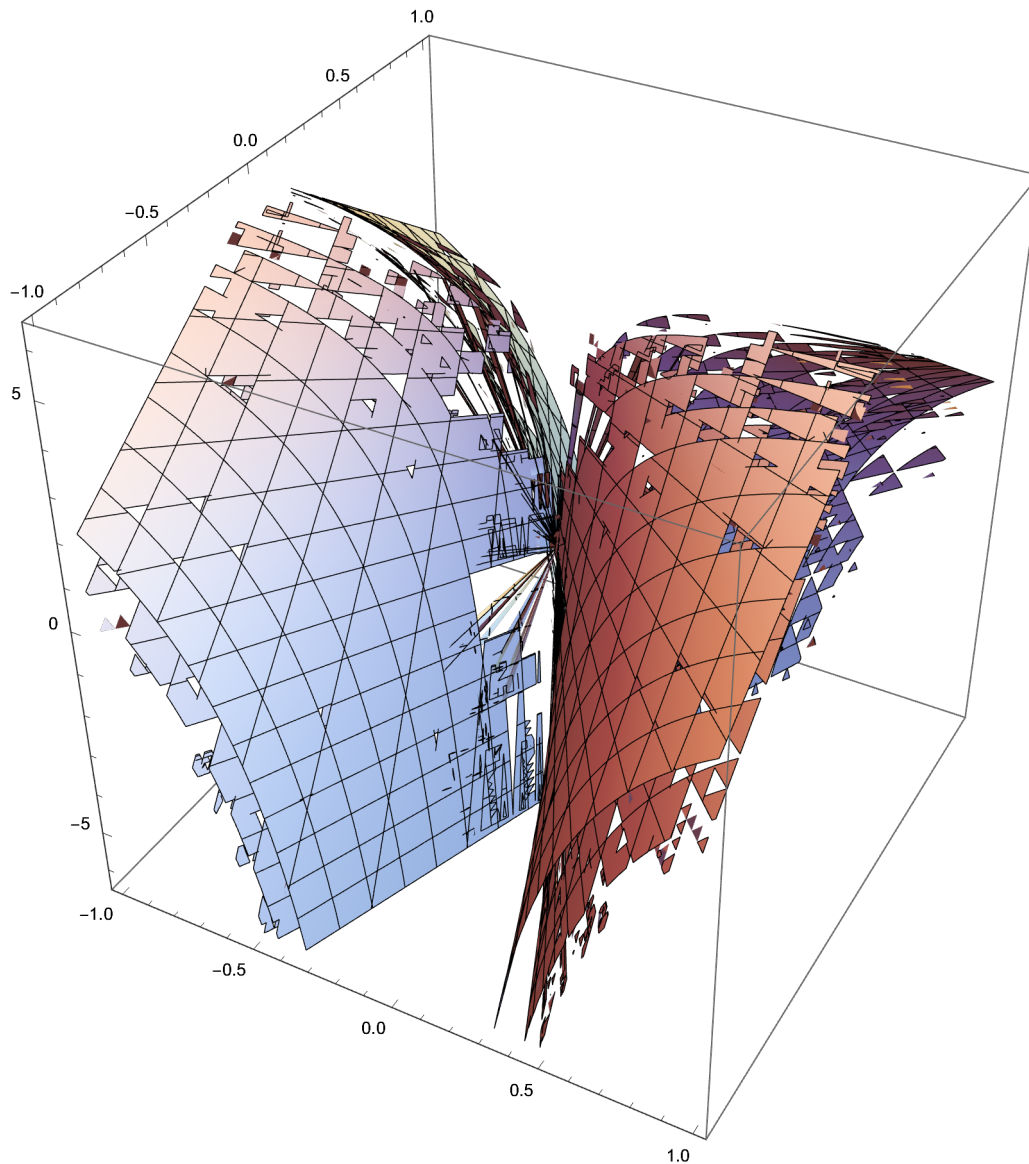




$$\text{Solve}\left[\frac{2\pi r - r\theta}{2\pi} = \eta \sqrt{1 - \frac{(v)^2}{c^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{c \sqrt{4\pi^2 - \frac{4\pi^2 r^2}{\eta^2} + \frac{4\pi r^2 \theta}{\eta^2} - \frac{r^2 \theta^2}{\eta^2}}}{2\pi}\right\}, \left\{v \rightarrow \frac{c \sqrt{4\pi^2 - \frac{4\pi^2 r^2}{\eta^2} + \frac{4\pi r^2 \theta}{\eta^2} - \frac{r^2 \theta^2}{\eta^2}}}{2\pi}\right\}\right\}$$

$$\text{ContourPlot3D}\left[\frac{c \sqrt{4\pi^2 - \frac{4\pi^2 r^2}{\eta^2} + \frac{4\pi r^2 \theta}{\eta^2} - \frac{r^2 \theta^2}{\eta^2}}}{2\pi}, \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

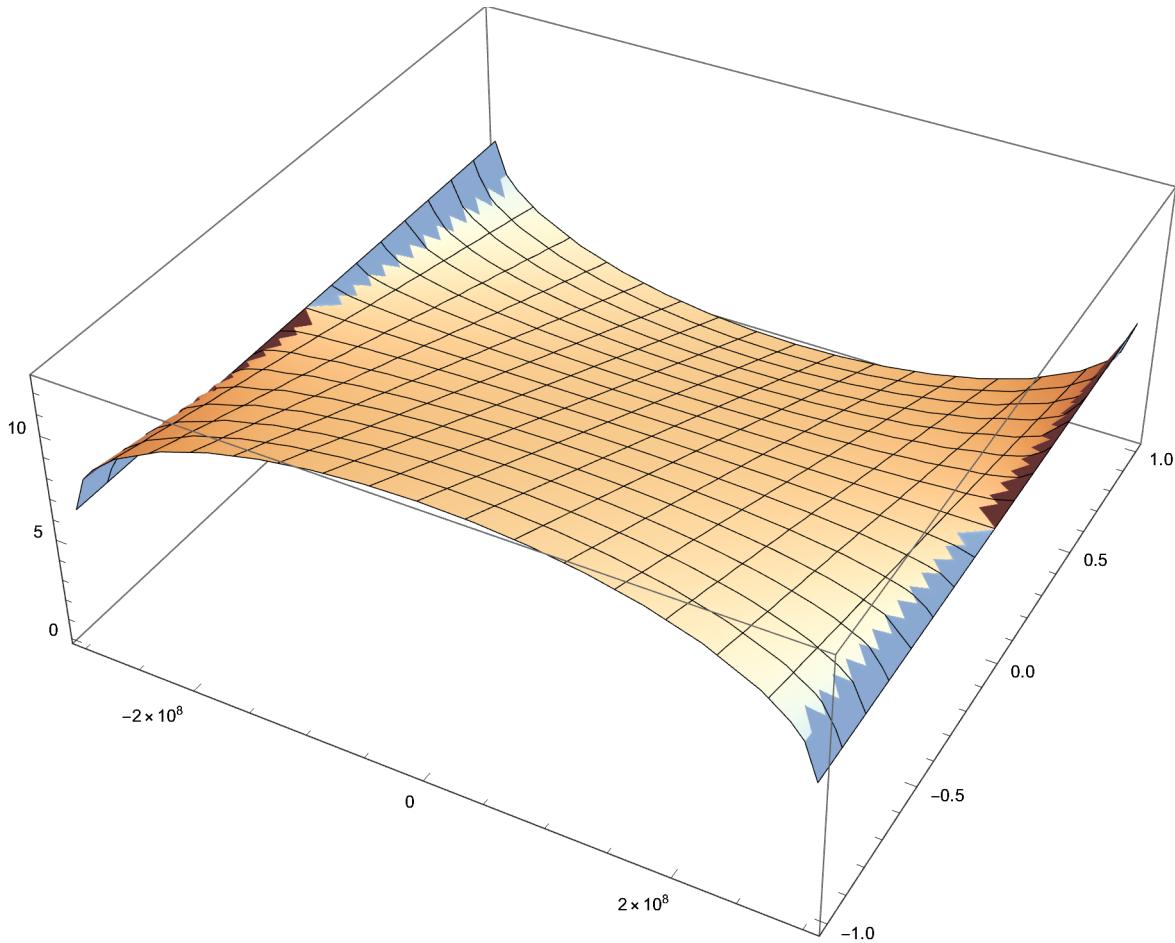


$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == \eta \sqrt{1 - \frac{(v)^2}{c^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -6.28319 \left(-1. + 1. \sqrt{1. - 1.11265 \times 10^{-17} v^2} \eta\right)\right\}\right\}$$

$$\text{Plot3D}\left[-6.283186703443298\right.$$

$$\left. \left(-0.9999997777777779 + 1. \sqrt{1. - 1.1126500560536185 \times 10^{-17} v^2} \eta\right), \{v, -c, c\}, \{\eta, -1, 1\}\right]$$



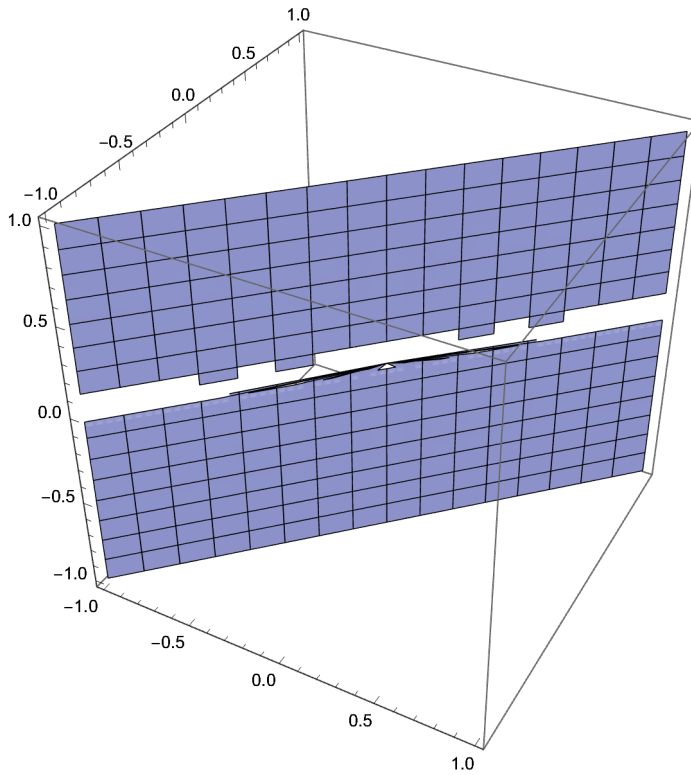
$2 \pi x - 2 \pi \eta' = \rho \eta$ , where  $\rho$  is an angle of a similar dimensional kind to theta, but different.

$$\text{Solve}[2 \pi x - 2 \pi \eta' == \rho \eta, \rho]$$

$$\left\{\left\{\rho \rightarrow \frac{2 (\pi x - \pi \eta')}{\eta}\right\}\right\}$$

$$\eta' = p$$

ContourPlot3D $\left[\frac{2 (\pi x - \pi p)}{\eta}, \{x, -1, 1\}, \{p, -1, 1\}, \{\eta, -1, 1\}\right]$



Solve $\left[2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \eta' == \rho \eta, \rho\right]$

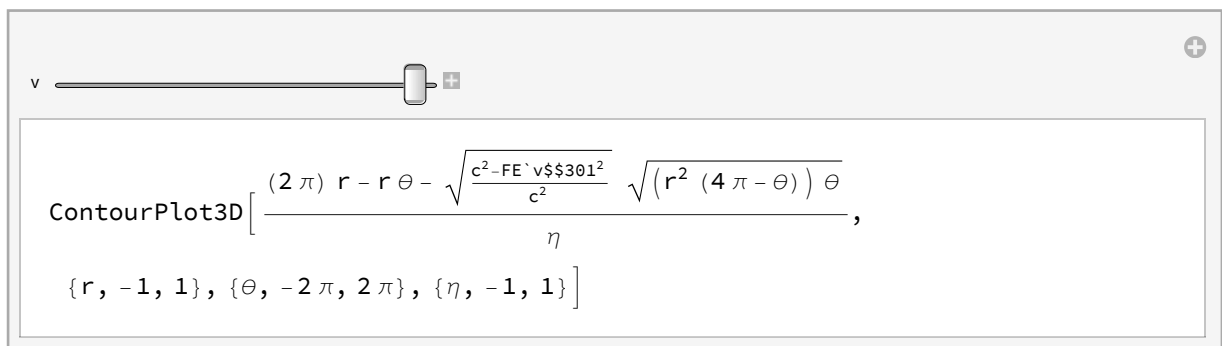
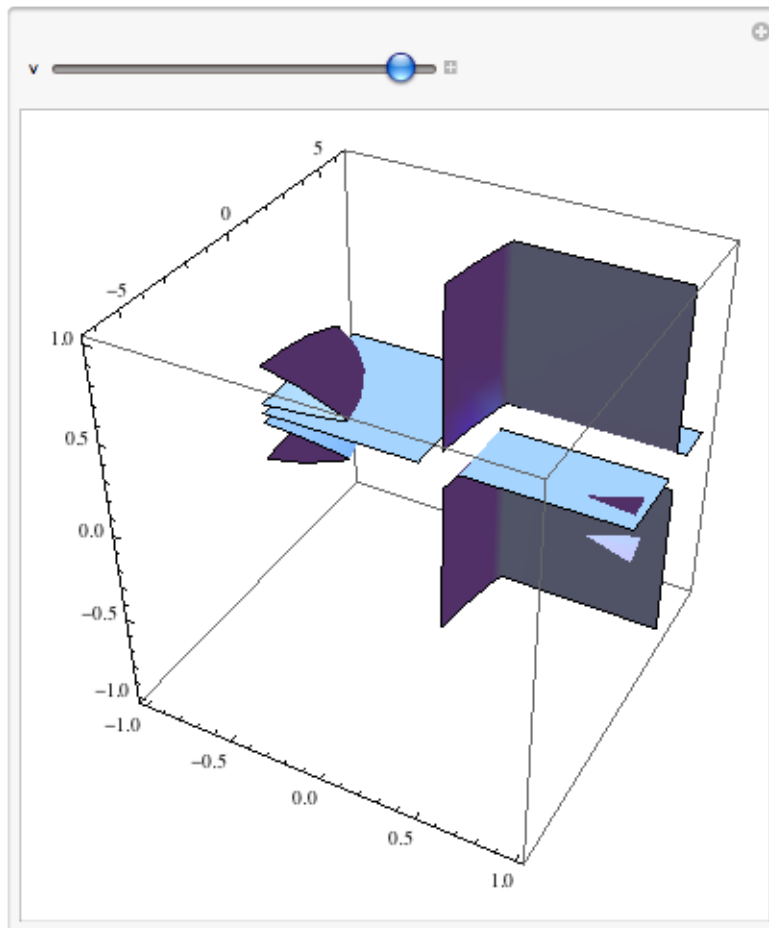
$\left\{\left\{\rho \rightarrow \frac{2 \pi r - r \theta - 2 \pi \eta'}{\eta}\right\}\right\}$

Solve $\left[2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \rho \eta, \rho\right]$

$\left\{\left\{\rho \rightarrow \frac{2 \pi r - r \theta - \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta}}{\eta}\right\}\right\}$

$c := 2.99792458 (10^8)$

Manipulate $\left[\text{ContourPlot3D}\left[\frac{2 \pi r - r \theta - \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta}}{\eta}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}\right], \{v, -c, c\}\right]$



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

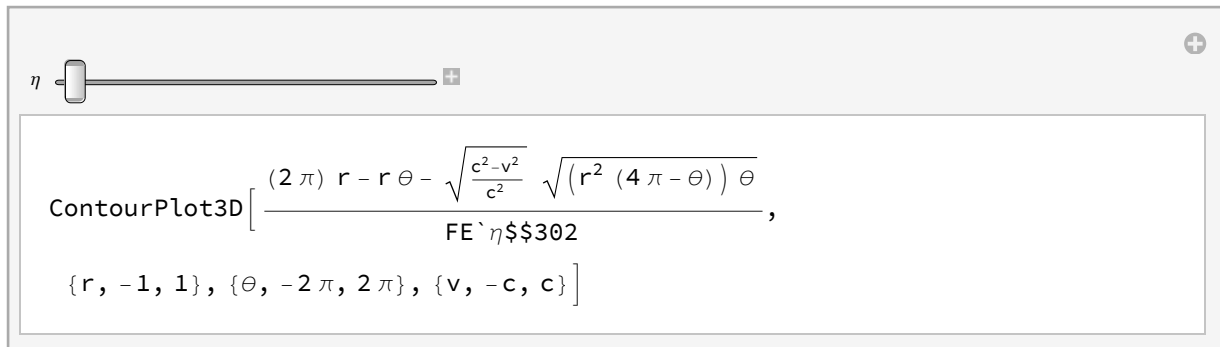
... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

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... **General**: Further output of Infinity::indet will be suppressed during this calculation.

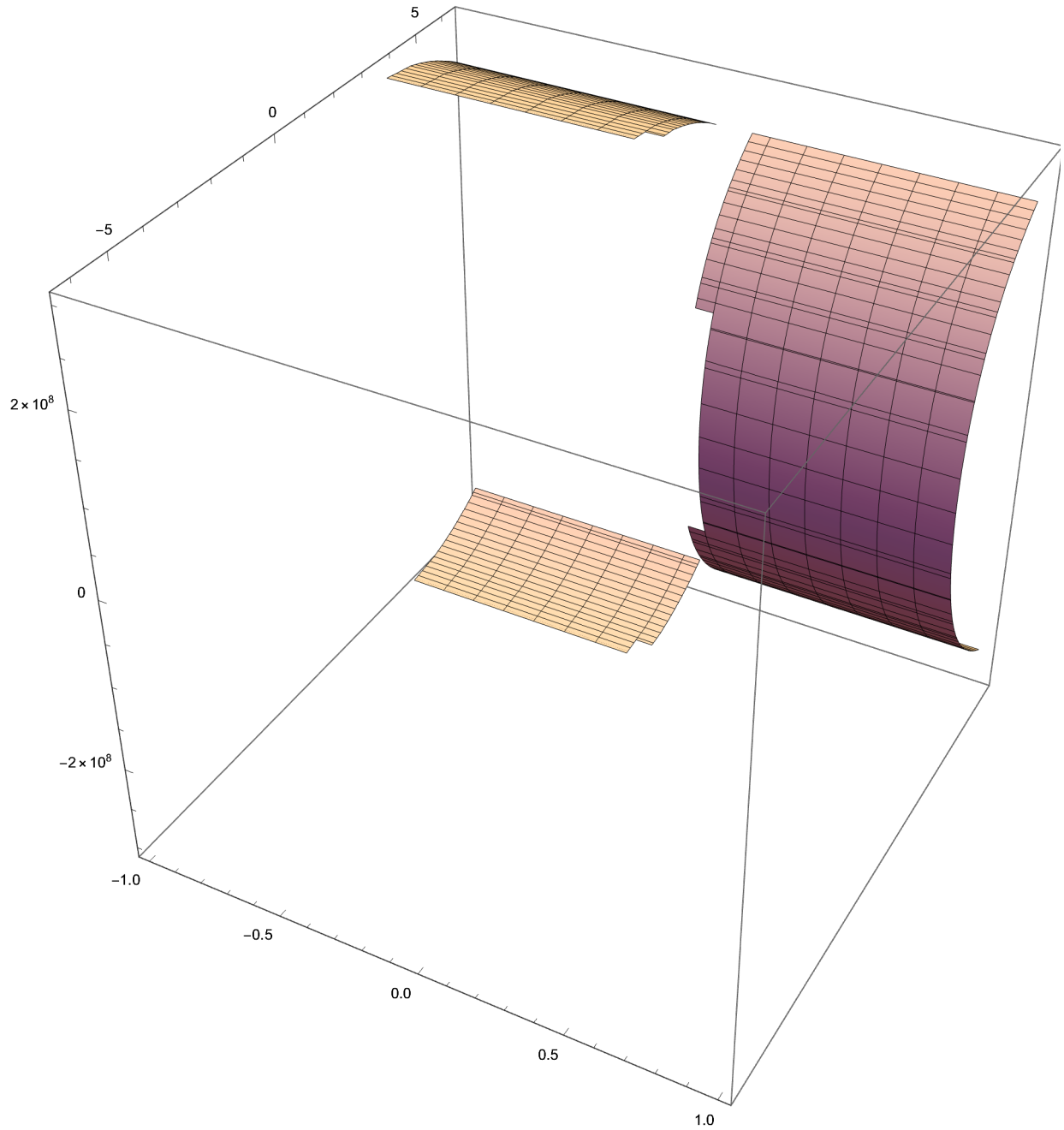
Manipulate[ContourPlot3D[ $\frac{2 \pi r - r \theta - \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta}}{\eta}$ ,  
 $\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{v, -c, c\}], \{\eta, -1, 1\}]$

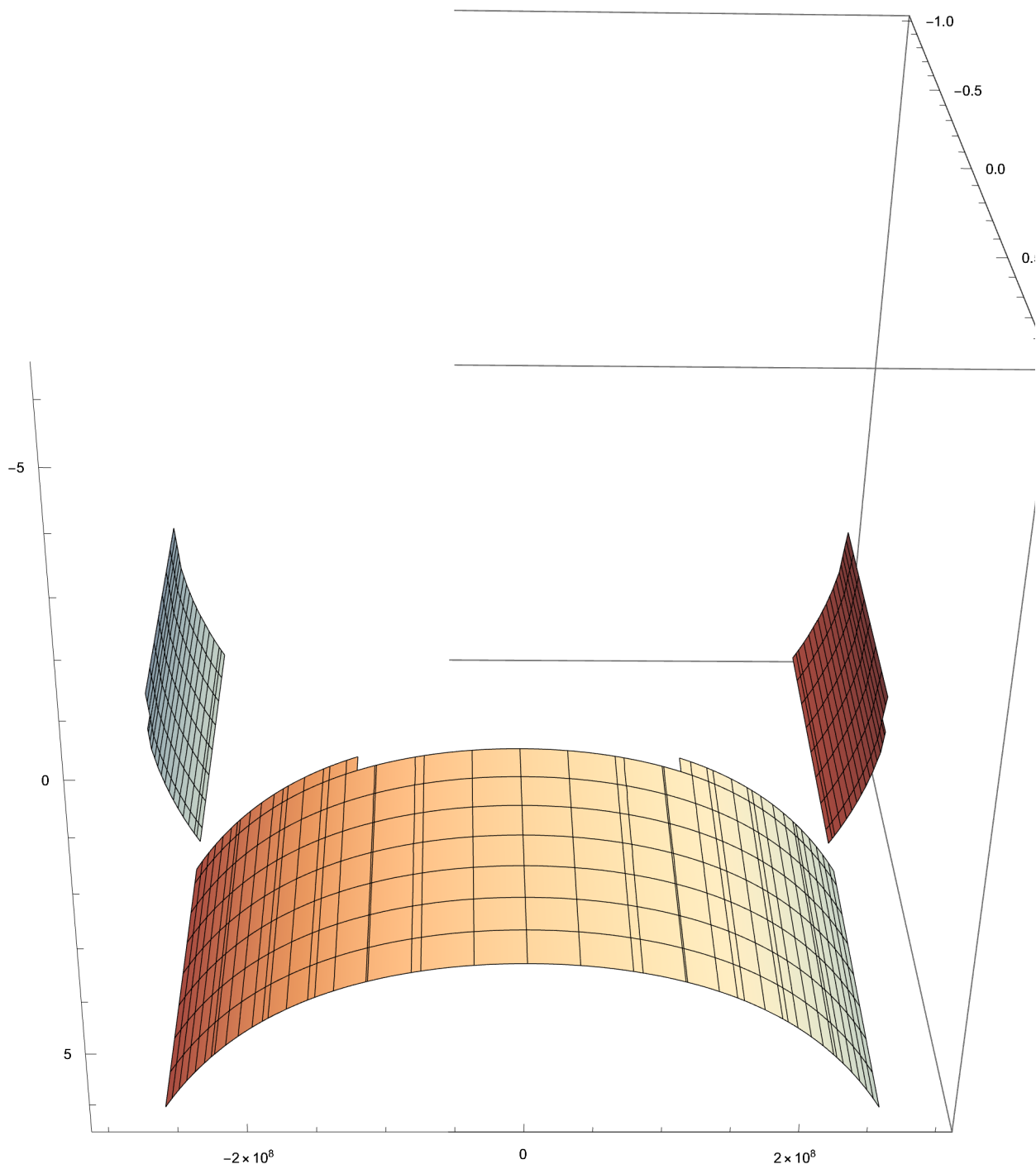


Solve[ $2 \pi \frac{2 \pi r - r \theta}{2 \pi} - 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \rho \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \rho]$

$\left\{ \left\{ \rho \rightarrow - \frac{2 \pi \left( -2 \pi r + r \theta + \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 (4 \pi - \theta) \theta} \right)}{\sqrt{r^2 (4 \pi - \theta) \theta}} \right\} \right\}$

$$\text{ContourPlot3D}\left[-\frac{2\pi\left(-2\pi r+r\theta+\sqrt{\frac{c^2-v^2}{c^2}}\sqrt{r^2(4\pi-\theta)\theta}\right)}{\sqrt{r^2(4\pi-\theta)\theta}},\right. \\
 \left.\{r,-1,1\},\{\theta,-2\pi,2\pi\},\{v,-c,c\}\right]$$





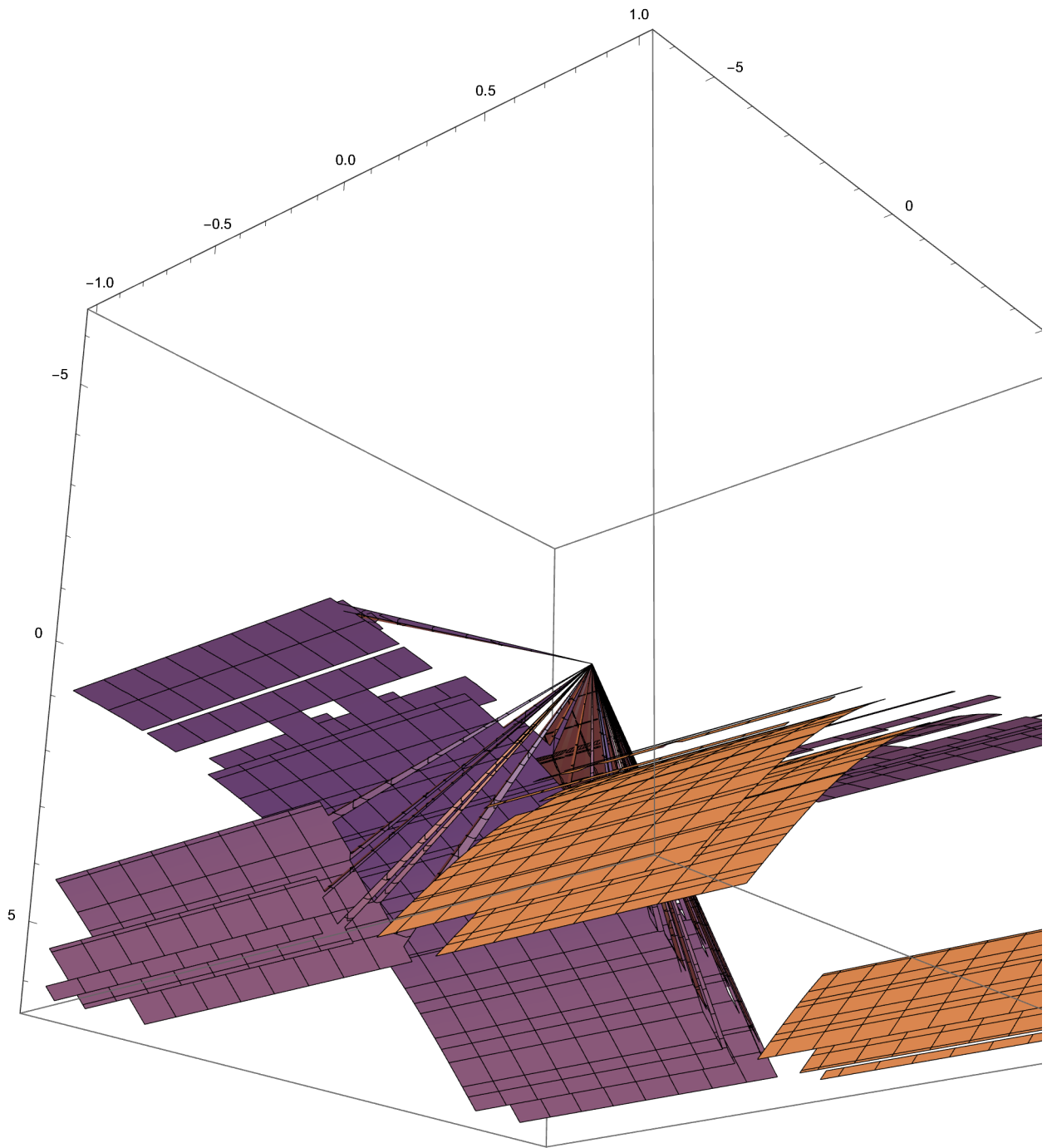
$$\text{Solve}\left[2\pi \frac{2\pi r - r\theta}{2\pi} - 2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \frac{v^2}{(c)^2}} == \rho \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{\sqrt{8c^2\pi^2 - \frac{4c^2\pi^3}{4\pi-\theta} - \frac{4c^2\pi^3}{\theta} - \frac{2c^2\pi\sqrt{r^2(4\pi-\theta)\theta}\rho}{r(4\pi-\theta)} + \frac{2c^2\pi\sqrt{r^2(4\pi-\theta)\theta}\rho}{r\theta} - c^2\rho^2}}{2\pi}\right\}\right\},$$

$$\left\{v \rightarrow \frac{\sqrt{8c^2\pi^2 - \frac{4c^2\pi^3}{4\pi-\theta} - \frac{4c^2\pi^3}{\theta} - \frac{2c^2\pi\sqrt{r^2(4\pi-\theta)\theta}\rho}{r(4\pi-\theta)} + \frac{2c^2\pi\sqrt{r^2(4\pi-\theta)\theta}\rho}{r\theta} - c^2\rho^2}}{2\pi}\right\}\right\}$$



ContourPlot3D $\left[\frac{\sqrt{8 c^2 \pi^2 - \frac{4 c^2 \pi^3}{4 \pi - \theta} - \frac{4 c^2 \pi^3}{\theta} - \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta)} \theta \rho}{r (4 \pi - \theta)} + \frac{2 c^2 \pi \sqrt{r^2 (4 \pi - \theta)} \theta \rho}{r \theta} - c^2 \rho^2}}{2 \pi},\right.$   
 $\{\theta, -2 \pi, 2 \pi\}, \{\rho, -2 \pi, 2 \pi\}, \{r, -1, 1\}\mathbf{]}$

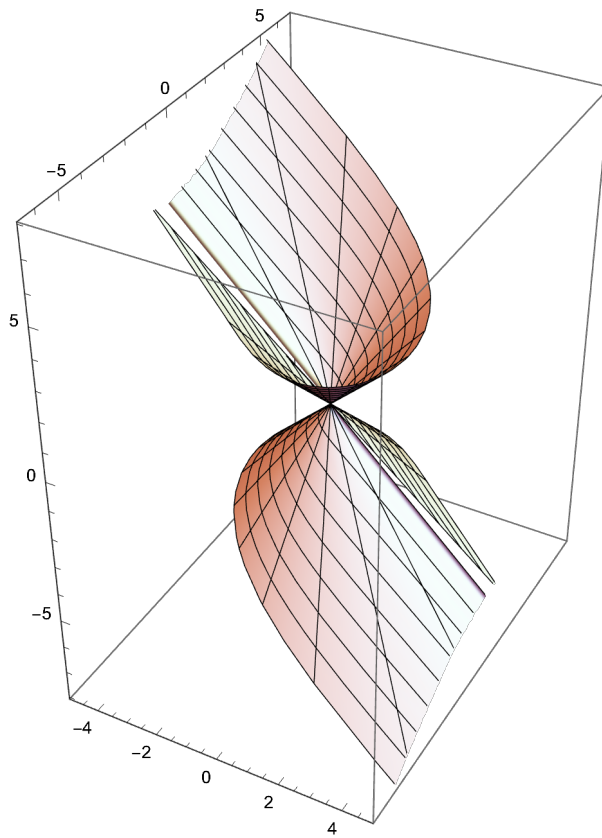


$$2\pi\eta - 2\pi x' = \theta\eta$$

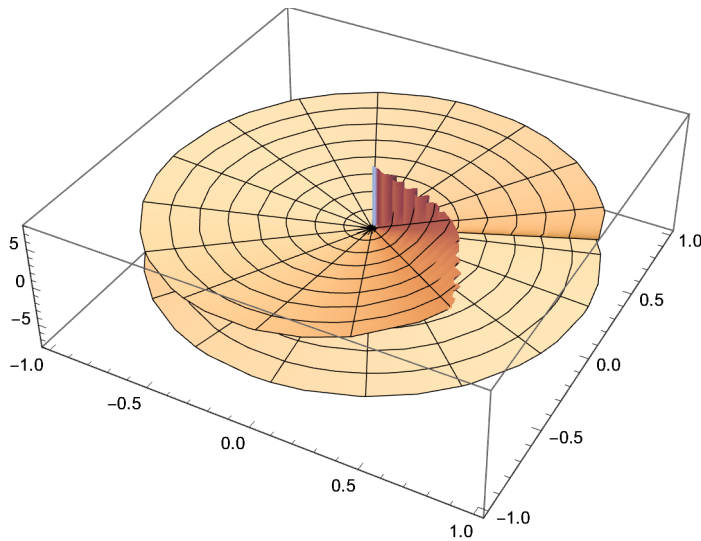
$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi x' = \theta \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}\right\}, \left\{r \rightarrow \frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\left\{-\frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}, \frac{4\pi^2 x'}{\sqrt{16\pi^3\theta - 20\pi^2\theta^2 + 8\pi\theta^3 - \theta^4}}\right\}, \{x', -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



RevolutionPlot3D $\left[\frac{4 \pi^2 x'}{\sqrt{16 \pi^3 \theta - 20 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4}}, \{x', -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$c := 2.99792458 (10^8)$

Solve $\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} = \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$

$\left\{\left\{\theta \rightarrow 6.28319 -\right.\right.$

$0.5 \sqrt{\left(-78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \left(2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2\right) +\right.$

$\left.\left(4.37709 \times 10^{-46} \left(3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4\right)\right)\right\} /$

$\left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 +\right.$

$\left.\sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 -\right.\right.$

$\left.\left.2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right\}^{1/3} +$

$2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 -\right.$

$\left.1.49725 \times 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 -\right.\right.$

$\left.\left.2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right\}^{1/3}\right) -$

$0.5 \sqrt{\left(78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} \left(2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2\right) -\right.$

$\left.\left(4.37709 \times 10^{-46} \left(3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4\right)\right)\right\} /$

$\left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 +\right.$

$\left.\sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 -\right.\right.$

$\left.\left.2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)\right\}^{1/3} -$

$2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 -\right.$

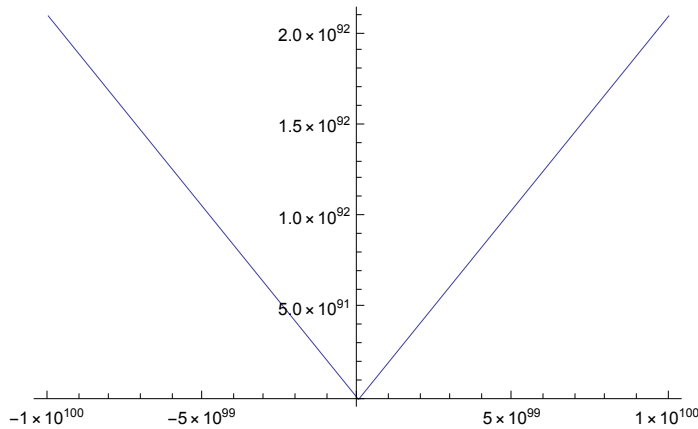
$$\begin{aligned}
& 1.49725 \times 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \\
& \quad \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3} - \\
& (0.25 (15875.2 - 100.531 (236.871 - 4.39257 \times 10^{-16} v^2) - \\
& \quad 8. (-992.201 + 5.51986 \times 10^{-15} v^2))) / \left(\sqrt{\left(-78.9568 + \right. \right. \\
& \quad \left. 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \right. \\
& \quad \left. (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4))\right)} / \\
& \quad \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\
& \quad \left. \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\
& \quad \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3} + \right. \\
& \quad \left. 2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times \right. \right. \\
& \quad \left. \left. 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \quad \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3}\right)\right)\right\}, \\
& \left\{\theta \rightarrow 6.28319 - 0.5 \sqrt{\left(-78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \right. \right. \\
& \quad \left. \left. (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \right. \right. \\
& \quad \left. \left. (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4))\right)} / \right. \\
& \quad \left. \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \right. \\
& \quad \left. \left. \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \quad \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3} + \right. \right. \\
& \quad \left. \left. 2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \right. \right. \\
& \quad \left. \left. \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3}\right)\right)\right) + \\
& 0.5 \sqrt{\left(78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) - \right. \\
& \quad \left. (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4))\right)} / \\
& \quad \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\
& \quad \left. \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\
& \quad \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3} - \right. \\
& \quad \left. 2.7574 \times 10^{-46} \left(8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \right. \\
& \quad \left. \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\
& \quad \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12}\right)}^{1/3}\right)\right) - \\
& (0.25 (15875.2 - 100.531 (236.871 - 4.39257 \times 10^{-16} v^2) - \\
& \quad 8. (-992.201 + 5.51986 \times 10^{-15} v^2))) / \left(\sqrt{\left(-78.9568 + \right. \right.}
\end{aligned}$$

$$\begin{aligned}
& 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} + \\
& 2.7574 \times 10^{-46} (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times \\
& 10^{89} v^6 + \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3})) \Bigg\}, \\
& \left\{ \theta \rightarrow 6.28319 + 0.5 \sqrt{(-78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \right. \\
& (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} + \\
& 2.7574 \times 10^{-46} (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \\
& 1.49725 \times 10^{89} v^6 + \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3}) - \\
& 0.5 \sqrt{(78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) - \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} - \\
& 2.7574 \times 10^{-46} (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \\
& 1.49725 \times 10^{89} v^6 + \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \\
& 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12})})^{1/3} + \\
& (0.25 (15875.2 - 100.531 (236.871 - 4.39257 \times 10^{-16} v^2) - \\
& 8. (-992.201 + 5.51986 \times 10^{-15} v^2))) / \left( \sqrt{(-78.9568 + \right. \\
& 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} (2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2) + \\
& (4.37709 \times 10^{-46} (3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4)) / \\
& (8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \\
& \sqrt{(6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 -
\end{aligned}$$

$$\begin{aligned} & \left( 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3} + \\ & 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \quad \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3}} \right) \Big) \Big\}, \\ & \left\{ \theta \rightarrow 6.28319 + 0.5 \sqrt{\left( -78.9568 + 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \right. \right. \\ & \quad \left. \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) + \right. \\ & \quad \left. \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) / \right. \\ & \quad \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\ & \quad \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \quad \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3}} + \right. \\ & \quad \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \right. \\ & \quad \left. \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\ & \quad \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3}} \right) \Big) + \right. \\ & \quad \left. 0.5 \sqrt{\left( 78.9568 + 4.39257 \times 10^{-16} v^2 - 3.4741 \times 10^{-46} \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) - \right. \right. \\ & \quad \left. \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) / \right. \\ & \quad \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\ & \quad \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \quad \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3}} - \right. \\ & \quad \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - \right. \right. \\ & \quad \left. \left. 1.49725 \times 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \\ & \quad \left. \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3}} + \right. \\ & \quad \left. \left( 0.25 \left( 15\,875.2 - 100.531 \left( 236.871 - 4.39257 \times 10^{-16} v^2 \right) - \right. \right. \\ & \quad \left. \left. 8. \left( -992.201 + 5.51986 \times 10^{-15} v^2 \right) \right) \right) / \left( \sqrt{\left( -78.9568 + \right. \right. \\ & \quad \left. \left. 4.39257 \times 10^{-16} v^2 + 3.4741 \times 10^{-46} \left( 2.27273 \times 10^{47} - 4.21458 \times 10^{29} v^2 \right) + \right. \right. \\ & \quad \left. \left( 4.37709 \times 10^{-46} \left( 3.03199 \times 10^{62} + 6.55503 \times 10^{60} v^2 + 1.77627 \times 10^{59} v^4 \right) \right) / \right. \\ & \quad \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \\ & \quad \left. \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \\ & \quad \left. \left. 2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \right) \Big)^{1/3}} + \right. \\ & \quad \left. 2.7574 \times 10^{-46} \left( 8.27465 \times 10^{109} - 1.3805 \times 10^{93} v^2 - 8.28801 \times 10^{90} v^4 - 1.49725 \times 10^{89} v^6 + \right. \right. \\ & \quad \left. \left. 10^{89} v^6 + \sqrt{\left( 6.84699 \times 10^{219} - 2.28463 \times 10^{203} v^2 - 1.37161 \times 10^{201} v^4 - \right. \right. \right. \end{aligned}$$

$$2.47784 \times 10^{199} v^6 + 2.75697 \times 10^{182} v^8 + 0. v^{10} + 0. v^{12} \Big)^{1/3} \Big) \Big) \Big) \Big) \Big\}$$

$$\begin{aligned}
& \left( 4.377094174611036 \cdot 10^{-46} \left( 3.0319879916202416 \cdot 10^{62} + \right. \right. \\
& \quad \left. \left. 6.555025201979783 \cdot 10^{60} v^2 + 1.776270219762819 \cdot 10^{59} v^4 \right) \right) / \\
& \left( 8.274653940104402 \cdot 10^{109} - 1.3805000153057876 \cdot 10^{93} v^2 - \right. \\
& \quad \left. 8.288007545727168 \cdot 10^{90} v^4 - 1.497247331222908 \cdot 10^{89} v^6 + \right. \\
& \quad \sqrt{\left( 6.846989782848531 \cdot 10^{219} - 2.2846319781928445 \cdot 10^{203} v^2 - \right. \\
& \quad \left. 1.371607885877325 \cdot 10^{201} v^4 - 2.477840705722886 \cdot 10^{199} v^6 + \right. \\
& \quad \left. 2.7569696001145084 \cdot 10^{182} v^8 + 0 \cdot v^{10} + 0 \cdot v^{12} \right)^{1/3}} + \\
& \quad 2.7573965439823348 \cdot 10^{-46} \left( 8.274653940104402 \cdot 10^{109} - \right. \\
& \quad \left. 1.3805000153057876 \cdot 10^{93} v^2 - 8.288007545727168 \cdot 10^{90} v^4 - \right. \\
& \quad \left. 1.497247331222908 \cdot 10^{89} v^6 + \sqrt{\left( 6.846989782848531 \cdot 10^{219} - \right. \right. \\
& \quad \left. \left. 2.2846319781928445 \cdot 10^{203} v^2 - 1.371607885877325 \cdot 10^{201} v^4 - \right. \right. \\
& \quad \left. \left. 2.477840705722886 \cdot 10^{199} v^6 + 2.7569696001145084 \cdot 10^{182} v^8 + \right. \right. \\
& \quad \left. \left. 0 \cdot v^{10} + 0 \cdot v^{12} \right)^{1/3}} \right) \Bigg], \{v, -10^{100}, 10^{100}\} \Bigg]
\end{aligned}$$

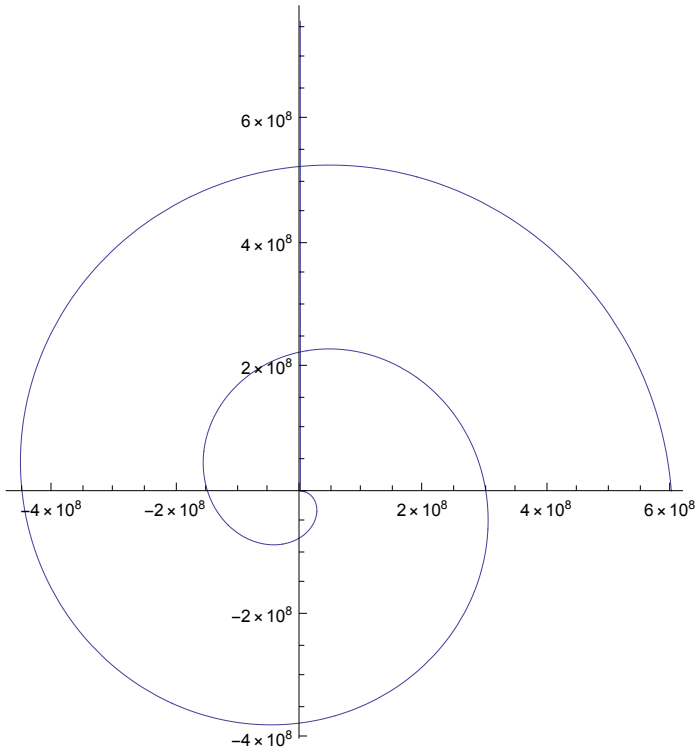


$$\text{Solve} \left[ 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \frac{2 \pi r - r \theta}{2 \pi} \sqrt{1 - \frac{v^2}{(c)^2}} = \theta \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, v \right]$$

$$\begin{aligned}
& \left\{ \left\{ v \rightarrow \right. \right. \\
& \quad - \left( \left( 1. \sqrt{\left( 1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 2.27273 \times 10^{47} \theta^2 - 2.41144 \times 10^{46} \theta^3 + 9.59481 \times \right. \right. \right. \\
& \quad \left. \left. \left. 10^{44} \theta^4 \right) \right) / \left( \sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2} \right) \right) \right\}, \left\{ v \rightarrow \right. \\
& \quad \left. \frac{\sqrt{1.49539 \times 10^{48} - 9.51997 \times 10^{47} \theta + 2.27273 \times 10^{47} \theta^2 - 2.41144 \times 10^{46} \theta^3 + 9.59481 \times 10^{44} \theta^4}}{\sqrt{1.66385 \times 10^{31} - 5.2962 \times 10^{30} \theta + 4.21458 \times 10^{29} \theta^2}} \right. \\
& \quad \left. \right\} \Bigg\}
\end{aligned}$$



```
PolarPlot[
  (√(1.495394089917615`*^48 - 9.519974451231788`*^47 θ + 2.2727264880331392`*^47 θ² -
    2.4114376991090496`*^46 θ³ + 9.594805744283795`*^44 θ⁴)) /
  (√(1.663850317969084`*^31 - 5.296200053396031`*^30 θ +
    4.2145820905076925`*^29 θ²)), {θ, -2 π, 2 π}]
```



## Light

$$2 \pi r - 2 \pi x = \theta r$$

$$\text{Solve}\left[2 \pi r - 2 \pi r \sqrt{1 - \frac{(v)^2}{c^2}} = \theta r, v\right]$$

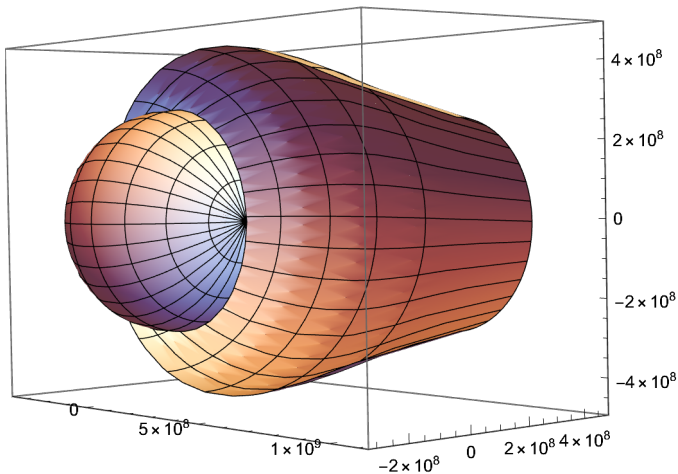
$$\left\{\left\{v \rightarrow -\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}, \left\{v \rightarrow \frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi} == \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), c\right]$$

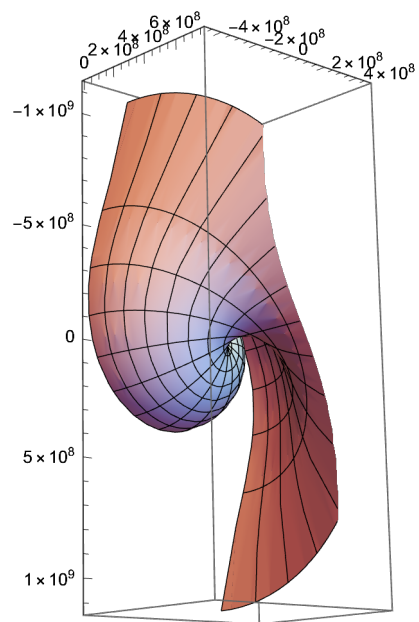
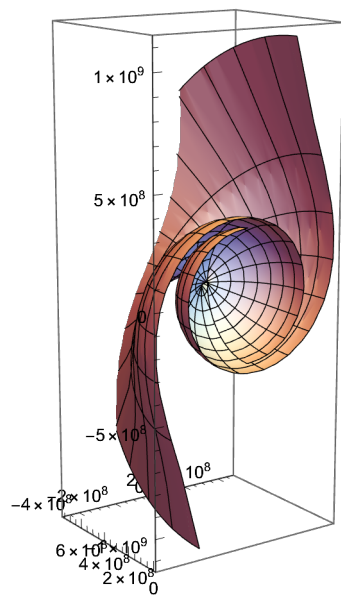
$$\left\{\left\{c \rightarrow -\left(1. \sqrt{2.02015 \times 10^{40} \theta - 1.60758 \times 10^{39} \theta^2 - 6.34649 \times 10^{40} \sin[\beta]^2}\right) / \left(\sqrt{\theta} \sqrt{(7.15472 \times 10^{22} \theta - 1.13871 \times 10^{22} \theta^2 + 4.53078 \times 10^{20} \theta^3 - 2.24772 \times 10^{23} \sin[\beta]^2 + 1.78868 \times 10^{22} \theta \sin[\beta]^2)}\right)\right\}, \right.$$

$$\left.\left\{c \rightarrow \left(\sqrt{2.02015 \times 10^{40} \theta - 1.60758 \times 10^{39} \theta^2 - 6.34649 \times 10^{40} \sin[\beta]^2}\right) / \left(\sqrt{\theta} \sqrt{(7.15472 \times 10^{22} \theta - 1.13871 \times 10^{22} \theta^2 + 4.53078 \times 10^{20} \theta^3 - 2.24772 \times 10^{23} \sin[\beta]^2 + 1.78868 \times 10^{22} \theta \sin[\beta]^2)}\right)\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\left(\sqrt{(2.0201505625374124 \cdot 10^{40} \theta - 1.607584739088511 \cdot 10^{39} \theta^2 - 6.346490166412822 \cdot 10^{40} \sin[\beta]^2)}\right) / \left(\sqrt{\theta} \sqrt{(7.154717000231094 \cdot 10^{22} \theta - 1.138708577010396 \cdot 10^{22} \theta^2 + 4.530777469308567 \cdot 10^{20} \theta^3 - 2.2477206366440006 \cdot 10^{23} \sin[\beta]^2 + 1.7886792500577734 \cdot 10^{22} \theta \sin[\beta]^2)}\right)\right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



$$\text{SphericalPlot3D}\left[\left(\sqrt{(2.0201505625374124 \cdot 10^{40} \theta - 1.607584739088511 \cdot 10^{39} \theta^2 - 6.346490166412822 \cdot 10^{40} \sin[\beta]^2)}\right) / \left(\sqrt{\theta} \sqrt{(7.154717000231094 \cdot 10^{22} \theta - 1.138708577010396 \cdot 10^{22} \theta^2 + 4.530777469308567 \cdot 10^{20} \theta^3 - 2.2477206366440006 \cdot 10^{23} \sin[\beta]^2 + 1.7886792500577734 \cdot 10^{22} \theta \sin[\beta]^2)}\right)\right], \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \pi\}]$$



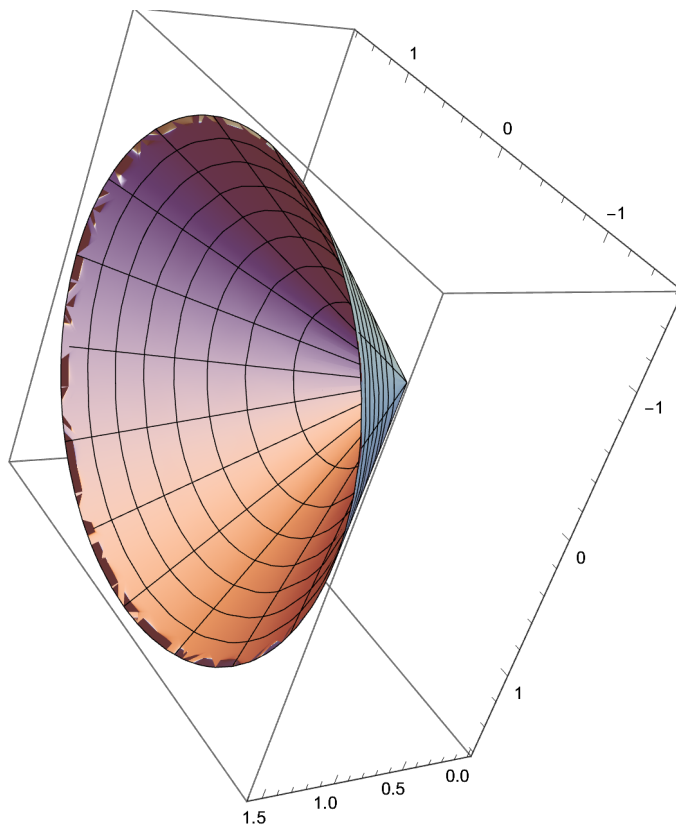
$c := 2.99792458 (10^8)$

$$\begin{aligned}
& \text{Solve}\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi} == \left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + \right.}\right.\right. \\
& \quad \left.\left.8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right) / \\
& \quad \left.\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \beta\right] \\
& \left\{\left\{\beta \rightarrow \right.\right. \\
& \quad \left.-1. \operatorname{ArcSin}\left[\frac{\sqrt{\theta} \sqrt{6.43991 \times 10^{46} - 2.56236 \times 10^{46} \theta + 3.2625 \times 10^{45} \theta^2 - 1.29811 \times 10^{44} \theta^3}}{\sqrt{2.02316 \times 10^{47} - 6.43991 \times 10^{46} \theta + 5.12472 \times 10^{45} \theta^2}}\right]\right\}, \\
& \quad \left.\left\{\beta \rightarrow \operatorname{ArcSin}\left[\frac{\sqrt{\theta} \sqrt{6.43991 \times 10^{46} - 2.56236 \times 10^{46} \theta + 3.2625 \times 10^{45} \theta^2 - 1.29811 \times 10^{44} \theta^3}}{\sqrt{2.02316 \times 10^{47} - 6.43991 \times 10^{46} \theta + 5.12472 \times 10^{45} \theta^2}}\right]\right\}\right\}
\end{aligned}$$

```

RevolutionPlot3D[
  { -1. ` ArcSin[ (  $\sqrt{\theta} \sqrt{(6.439907533884034 \cdot 10^{-46} - 2.562357792680954 \cdot 10^{-46} \theta +$ 
     $3.2624952694016945 \cdot 10^{-45} \theta^2 - 1.298105622348011 \cdot 10^{-44} \theta^3)}$  ) ) /
    (  $\sqrt{(2.0231566198247644 \cdot 10^{-47} - 6.439907533884035 \cdot 10^{-46} \theta +$ 
     $5.124715585361908 \cdot 10^{-45} \theta^2)}$  ) ) ],
  ArcSin[ (  $\sqrt{\theta} \sqrt{(6.439907533884034 \cdot 10^{-46} - 2.562357792680954 \cdot 10^{-46} \theta +$ 
     $3.2624952694016945 \cdot 10^{-45} \theta^2 - 1.298105622348011 \cdot 10^{-44} \theta^3)}$  ) ) /
    (  $\sqrt{(2.0231566198247644 \cdot 10^{-47} - 6.439907533884035 \cdot 10^{-46} \theta +$ 
     $5.124715585361908 \cdot 10^{-45} \theta^2)}$  ) ) ] ], { $\theta$ , -4  $\pi$ , 4  $\pi$ ] ]

```

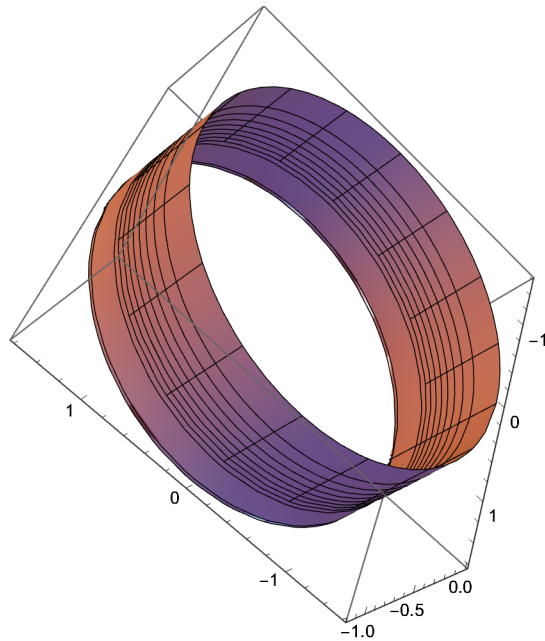


$$\begin{aligned}
& \text{Solve}\left[\frac{\sqrt{4 c^2 \pi^2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) - c^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2 \pi} == \right. \\
& \quad \left. \left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right)} \right. \\
& \quad \left. \left(\sqrt{-12.566370614359172 \cdot 10^0 \theta + \theta^2 + 39.47841760435743 \cdot 10^0 \sin[\beta]^2}\right), \beta\right] \\
& \left\{\left\{\beta \rightarrow -1. \right. \right. \\
& \quad \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) - 2. \sqrt{\left(-8.09397 \times 10^{-41} \left(1.57307 \times \right. \right. \right. \right. \\
& \quad \left. \left. \left. 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}, \\
& \left\{\beta \rightarrow \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) - 2. \sqrt{\left(-8.09397 \times 10^{-41} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left(1.57307 \times 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}, \\
& \left\{\beta \rightarrow -1. \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) + 2. \sqrt{\left(-8.09397 \times 10^{-41} \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left(1.57307 \times 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}, \\
& \left\{\beta \rightarrow \text{ArcSin}\left[0.5 \sqrt{\left(-2. \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right) + 2. \sqrt{\left(-8.09397 \times 10^{-41} \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left(1.57307 \times 10^{40} - 1.25181 \times 10^{39} \theta\right) \theta + \left(-1. - 0.31831 \theta + 0.0253303 \theta^2\right)^2\right)\right)}\right]\right\}
\end{aligned}$$

```

RevolutionPlot3D[
  { -1. ` ArcSin[0.5 `  $\sqrt{(-2. ` (-0.9999999999999999 - 0.3183098861837907 ` \theta + 0.025330295910584444 ` \theta^2) + 2. ` \sqrt{(-8.093971489670607 ` *^-41 (1.573071447508865 ` *^40 - 1.2518104835387941 ` *^39 \theta) \theta + (-0.9999999999999999 - 0.3183098861837907 ` \theta + 0.025330295910584444 ` \theta^2)^2)}}]$ ,
  -1. ` ArcSin[0.5 `  $\sqrt{(-2. ` (-0.9999999999999999 - 0.3183098861837907 ` \theta + 0.025330295910584444 ` \theta^2) - 2. ` \sqrt{(-8.093971489670607 ` *^-41 (1.573071447508865 ` *^40 - 1.2518104835387941 ` *^39 \theta) \theta + (-0.9999999999999999 - 0.3183098861837907 ` \theta + 0.025330295910584444 ` \theta^2)^2)}}]$  ]}, {\theta, -8 \pi, 8 \pi} ]

```



$$\begin{aligned}
 D[hnf, \theta] &= D\left[(6.62606896 * 10^{-34}) \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}, \theta\right] = \\
 D\left[h \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}, \theta\right] &= h D\left[\frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}, \theta\right] = ma = \text{Force} \\
 h D\left[\frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}, \theta\right] &= \\
 h \left(-\frac{4\pi - \theta}{3\pi^2\theta^3} - \frac{1}{6\pi^2\theta^2}\right) &
 \end{aligned}$$

$$\text{Solve}\left[\pi\left(r^2 - \frac{r^2(4\pi - \theta)\theta}{4\pi^2}\right)\right]^2 = \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \left(\frac{r^2(4\pi - \theta)\theta}{4\pi^2}\right), r]$$

$$\left\{\{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{r \rightarrow -\frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}\right\}\right\},$$

$$\left\{r \rightarrow \frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}\right\}\right\}$$

$$D\left[\frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta\right]$$

$$\text{Velocity} = \frac{\pi^{3/2} \left(-\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}} -$$

$$\frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}$$

$$D\left[\frac{\pi^{3/2} \left(-\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}} - \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}\right], \theta]$$



$$\begin{aligned}
a := & - \frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)^2}{2 \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta} \right)^{3/2}} + \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3 ((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2 \theta ((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \quad \left. \left. \frac{4(4\pi-2\theta)}{\pi^2 \theta^2 \sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}} \right) - \\
& \left( \pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \quad \left. \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right) \right) / \\
& \left( (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}} \right) + \\
& \frac{3\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} - \\
& \frac{\pi^{3/2} (48\pi^2 - 48\pi\theta + 12\theta^2) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} \\
D[hnf, \theta] = & D \left[ (6.62606896 * 10^{-34}) \frac{\sqrt{(4\pi-\theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi-\theta)\theta}}{6\pi\theta}, \theta \right] = \\
D[h \frac{\sqrt{(4\pi-\theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi-\theta)\theta}}{6\pi\theta}, \theta] = & h D \left[ \frac{\sqrt{(4\pi-\theta)\theta}}{\pi\theta^2} \frac{\sqrt{(4\pi-\theta)\theta}}{6\pi\theta}, \theta \right] = ma = \text{Force}
\end{aligned}$$

$$\text{Solve}\left[h\left(-\frac{4\pi-\theta}{3\pi^2\theta^3}-\frac{1}{6\pi^2\theta^2}\right)=ma, m\right]$$

$$\left\{\left\{m\rightarrow-\left(h\left(-\frac{4\pi-\theta}{3\pi^2\theta^3}-\frac{1}{6\pi^2\theta^2}\right)\right)\right\}\right. \\ \left(\frac{\pi^{3/2}\left(-\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}}+\frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}-\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)^2}{2\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}\left(-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}\right)^{3/2}}-\right. \\ \left.\left(\pi^{3/2}\left(\frac{(4\pi-2\theta)^2}{4\pi^3((4\pi-\theta)\theta)^{3/2}}-\frac{(4\pi-2\theta)^2}{\pi^2\theta((4\pi-\theta)\theta)^{3/2}}+\frac{1}{\pi^3\sqrt{(4\pi-\theta)\theta}}-\right.\right.\right. \\ \left.\left.\frac{4(4\pi-2\theta)}{\pi^2\theta^2\sqrt{(4\pi-\theta)\theta}}-\frac{4}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}+\frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^3}\right)\right)\right\} \\ \left(\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}\right)+ \\ \left(\pi^{3/2}(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3)\right. \\ \left.\left(-\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}}+\frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}-\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)\right)\left\{ \right. \\ \left.\left(\left(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4\right)^{3/2}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}\right)- \right. \\ \left.\frac{3\pi^{3/2}(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3)^2\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{2\left(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4\right)^{5/2}}+ \right. \\ \left.\frac{\pi^{3/2}(48\pi^2-48\pi\theta+12\theta^2)\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{\left(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4\right)^{3/2}}\right)\left.\right\}$$

$$\begin{aligned}
& \text{Simplify} \left[ - \left( h \left( - \frac{4\pi - \theta}{3\pi^2\theta^3} - \frac{1}{6\pi^2\theta^2} \right) \right) / \right. \\
& \left( \frac{\pi^{3/2} \left( - \frac{4\pi - 2\theta}{2\pi^3\sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta\sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right)^2}{2\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \left( - \frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta} \right)^{3/2}} - \right. \\
& \left( \pi^{3/2} \left( \frac{(4\pi - 2\theta)^2}{4\pi^3((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2\theta((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3\sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \left. \left. \frac{4(4\pi - 2\theta)}{\pi^2\theta^2\sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2\theta\sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}} \right) + \\
& \left( \pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \left. \left( - \frac{4\pi - 2\theta}{2\pi^3\sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta\sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}} \right) - \\
& \frac{3\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}}{2(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} + \\
& \left. \frac{\pi^{3/2} (48\pi^2 - 48\pi\theta + 12\theta^2) \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} \right] \\
& \text{Solve} \left[ - \frac{(6.26 \times 10^{\wedge} - 34) (8\pi - \theta) (-4\pi + \theta)^2 (-2\pi + \theta)^2 \sqrt{(-2\pi + \theta)^4}}{3\pi^2\theta \sqrt{\frac{((4\pi - \theta)\theta)^{3/2}}{\theta^2}}} (80\pi^4 - 224\pi^3\theta + 448\pi^2\theta^2 - 160\pi\theta^3 + 15\theta^4) \right] == F, \theta
\end{aligned}$$

# Perceptual Space Applied to the Uncertainty Model of Physics

by Parker Emmerson with assistance from Andrew Berisha

A bit of Philosophy of Perception. Also, see the Geometric Pattern of Perception of the Moon from beneath the Legs by Parker Emmerson.

$$c = 3.0 * 10^8 \text{ m / s}$$

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle,

the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + \eta^2$$

This is the initial radius squared expressed as the slant of

the cone in terms of the height of the cone,  $\eta$ , and the radius

of the base of the cone,  $r_1$

$$r = \sqrt{(r_1^2 + \eta^2)} \quad (59)$$

$$t = \theta r$$

$$t / \theta = r$$

The arc length taken out of a circle at a given time is =

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - \eta^2$$

$$r_1 = \sqrt{(r^2 - \eta^2)}$$

$$h \leq r$$

$$\tau = \text{time}$$

$$1 \text{ second} = 6 \text{ degrees}$$

$$\pi r_1^2 = \text{Area} = n \eta^2$$

To construct a square of the same area as a given circle, we will begin with the postulates above regarding the geometry of a cone.

When, "relationship is added to non relational stimuli" (Perception, MacLeod and Pick for Gibson, 24), illusion is able to be understood through phenomenology. We can use mathematics like a language for disussing its structural elements.

The derivative of zero is equal to the derivative of an equation that is equal to 0.

$$\text{Solve}[r_1^2 + \eta^2 = r^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\}$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\} \quad (60)$$

$$(t / \theta) = r$$

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = 2 \pi (t / \theta) - 2 \pi \sqrt{(t / \theta)^2 - \eta^2}$$

$$t = 2 \pi (t / \theta) - 2 \pi \sqrt{(t / \theta)^2 - \eta^2}$$

Add  $2\pi\sqrt{((r)^2 - \eta^2)}$  to both sides

$$t + 2\pi\sqrt{((t/\theta)^2 - \eta^2)} = 2\pi(t/\theta)$$

Subtract  $t$  from both sides and remember that  $(t/\theta) = r$

$$2\pi\sqrt{((t/\theta)^2 - (\eta^2))} = 2\pi(t/\theta) - t = 2\pi r - t$$

Divide by  $2\pi$  on both sides.

$$(t/\theta) - t/(2\pi) = (r) - t/(2\pi) = \sqrt{((t/\theta)^2 - (\eta^2))} = \sqrt{((r)^2 - (\eta^2))} = r_1$$

Square both sides. Substitute :  $(t/\theta) = r$

$$((t/\theta) - (t/(2\pi)))^2 = ((r) - (t/(2\pi)))^2 = ((t/\theta)^2 - (\eta^2)) = (r_1^2)$$

$$((r) - (t/(2\pi)))^2 = ((r)^2 - (\eta^2))$$

Add  $\eta^2$  to both sides.

$$((r) - (t/(2\pi)))^2 + (\eta^2) = (r)^2$$

Substitute :  $\theta r = t$

$$((t/\theta) - (t/(2\pi)))^2 = ((r) - (\theta * r/(2\pi)))^2$$

$$((r) - (\theta * r/(2\pi)))^2$$

$$\left(r - \frac{r\theta}{2\pi}\right)^2$$

$$\text{Expand} \left[ \left(r - \frac{r\theta}{2\pi}\right)^2 \right]$$

$$r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}$$

$$r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2} + \eta^2 = ((r) - (t/2\pi))^2 + (\eta^2) = r^2$$

$$(r^2) - \left(r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}\right) = \eta^2$$

$$\text{Simplify} \left[ (r^2) - \left(r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}\right) \right]$$

$$\frac{r^2(4\pi - \theta)\theta}{4\pi^2} = \eta^2$$

(61)

$$\text{Solve} \left[ \frac{r^2(4\pi - \theta)\theta}{4\pi^2} == \eta^2, \eta \right]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \right\} \right\}$$

$$\frac{2\eta\pi}{\sqrt{4\pi\theta - \theta^2}} = r$$

(62)

$$\frac{2 (r / 6 \theta) (6 \theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = r = \frac{2 r \pi}{\sqrt{4 \pi \theta - \theta^2}} \quad (63)$$

$$\text{Solve}\left[1 == \frac{2 \pi}{\sqrt{4 \pi \theta - \theta^2}}, \theta\right]$$

$$\{\{\theta \rightarrow 2 \pi\}\}$$

This is the equation for  $r_1$  in terms of the geometric parameters of the cone described above.

$$\pi (r^2 - \eta^2) = \pi r_1^2$$

Then, we substitute for the solved height in terms of purely theta and radius.

$$\begin{aligned} \text{Solve}\left[\pi \left(r^2 - \left(\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2}\right)\right) = \pi \left(r^2 - \left(\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2}\right)\right)^2, r\right] \\ \left\{\{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{r \rightarrow -\frac{2 \pi \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}\right\}, \right. \\ \left. \left\{r \rightarrow \frac{2 \pi \sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}\right\}\right\} \end{aligned} \quad (64)$$

Remember when we said that  $\pi (r^2 - \eta^2) = \pi r_1^2$ .

When is the area of  $h^2$  equal to the area of the circle of  $r_1$ ?

$$\text{Well, what if } n * \eta^2 = \pi r_1^2 = \pi \left(r^2 - \left(\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2}\right)\right)$$

If  $r_1 = \eta$ , then  $n = \pi$

Where  $n$  is just a given number of  $h^2$  that is related to  $E = h n f$ , where  $n$  is the number of frequencies,  $f$  is the frequency, and  $h$  is Planck's constant.

$$E = h n f = h \nu = m c^2 \quad (65)$$

$$r / t = r / (6 \theta) = c = \lambda f = r (1 / 6 \theta) \quad (66)$$

$$\nu = \text{velocity} = \lambda \nu, \text{ where } \lambda = r \text{ and is the wavelength, and } \nu \text{ is the frequency.} \quad (67)$$

$$\eta = \nu * \text{time} = (r / t) 6 (\theta) = (r / (6 \theta)) 6 (\theta)$$

$$\frac{2 \eta \pi}{\sqrt{4 \pi \theta - \theta^2}} = r = \frac{(r / t) 6 (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{(r / (6 \theta)) 6 (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[(r / t) == \frac{(r / t) 6 (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} * \nu, \nu\right]$$

$$\left\{\left\{\nu \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{6 \pi \theta}\right\}\right\} \quad (68)$$

$$v := \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}$$

$$nf = v$$

$$\text{Solve}\left[n(1/6\theta) == \frac{\sqrt{(4\pi - \theta)\theta}}{6\pi\theta}, n\right]$$

$$\left\{\left\{n \rightarrow \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2}\right\}\right\}$$

(69)

$$n := \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2}$$

Where  $h$  is Planck's Constant,  $n$  the number of moles,  
and  $f$  the frequency, we may say that the force of dark matter ( $F_{dm}$ )  
is capable of being solved for in terms of time or purely space.

$$\pi r_1^2 = (r^2 - \eta^2)^2 = \pi \left( r^2 - \left( \frac{r^2 (4\pi - \theta)\theta}{4\pi^2} \right) \right)^2 = n \left( \frac{r^2 (4\pi - \theta)\theta}{4\pi^2} \right)$$

The amount  $n(\eta^2)$  is correlated to the area of  $r_1$ ,  
because  $n$  is in terms of theta.

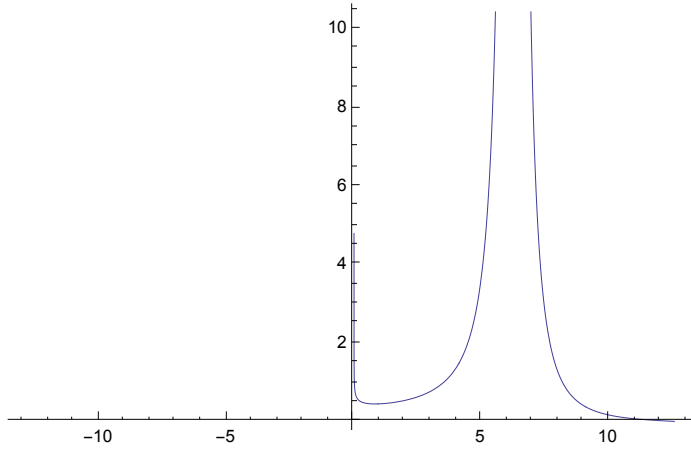
$$\text{Solve}\left[\pi \left( r^2 - \left( \frac{r^2 (4\pi - \theta)\theta}{4\pi^2} \right) \right)^2 == \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2} \left( \frac{r^2 (4\pi - \theta)\theta}{4\pi^2} \right), r\right]$$

$$\left\{\{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{r \rightarrow -\frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}\right\}\right\},$$

(70)

$$\left\{r \rightarrow \frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta}}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}\right\}\right\}$$

$$\text{Plot}\left[\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \{\theta, -13, 13\}\right]$$



We will now elaborate on the nature of  $r_1$  in terms of constant rate, and then come back to the equations for  $r$  that we have found through the realization of its parameters and solve them for theta.

$$r_1^2 = \left( r^2 - \left( \frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2} \right)^2 \right) = r^2 - \eta^2 \quad (71)$$

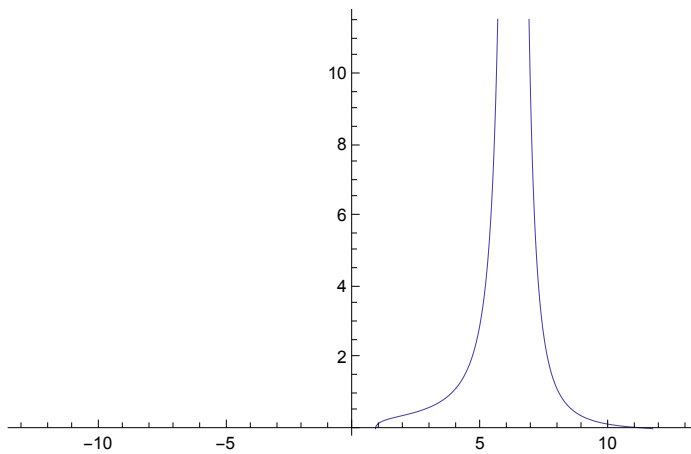
$$r_1 = \sqrt{r^2 - \eta^2} = \sqrt{\left( \left( \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right)^2 - \eta^2 \right)} =$$

$$\sqrt{\left( \left( \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right)^2 - \right)}$$

$$\left( \frac{\left( \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right) / (6 \theta) \cdot 6 (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2$$



$$\text{Plot}\left[\sqrt{\left(\frac{2\pi^{3/2}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}\right)^2-\frac{\left(\frac{2\pi^{3/2}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}\right)^2/(6\theta)}{6(\theta)\pi}}{\sqrt{4\pi\theta-\theta^2}}}\right)^2},\{\theta,-13,13\}]$$



We will briefly show what the graph looks like when the speed of light is the constant rate at which something along the line of  $\eta$  is traveling, not  $\eta = c6\theta = (r/6\theta)(6\theta)$ . In that case,  $r$  would equal  $\eta$ , but what about the fact that  $h$  changes through  $r_1$  (the base of the cone)? We will instead propose to say that  $\eta$  travels not at any rate, but at the speed of light. Of course, it's also possible to theorize and propose that the cone travels up into the third dimension,  $\eta$ , at a rate equal to the first derivative of the equation for  $r$  in terms of  $\theta$  with respect to  $\theta$ . However, we will now briefly discuss what happens to  $r_1$  when the cone travels

$$\eta^2 = \frac{4\eta^2\pi^2}{4\pi\theta - \theta^2}$$

$$r_1^2 = \left(r^2 - \left(\frac{r^2(4\pi - \theta)\theta}{4\pi^2}\right)^2\right)$$

$$D[r, \theta] = r - r_1 = \frac{2 h \pi}{\sqrt{4 \pi \theta - \theta^2}} - \left( r^2 - \left( \frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2} \right)^2 \right)$$

$$\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2} = \eta^2; \frac{2 h \pi}{\sqrt{4 \pi \theta - \theta^2}} = r$$

$$\eta = r / (6 \theta) = r / t$$

$$\frac{4 \eta^2 \pi^2}{4 \pi \theta - \theta^2} = r^2$$

$$\text{Solve}\left[\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2} = r^2, \theta\right]$$

$$\{\{\theta \rightarrow 2 \pi\}, \{\theta \rightarrow 2 \pi\}\}$$

$$\text{Solve}\left[\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2} = (r / 6 \theta)^2, r\right]$$

$$\{\{r \rightarrow 0\}, \{r \rightarrow 0\}\}$$

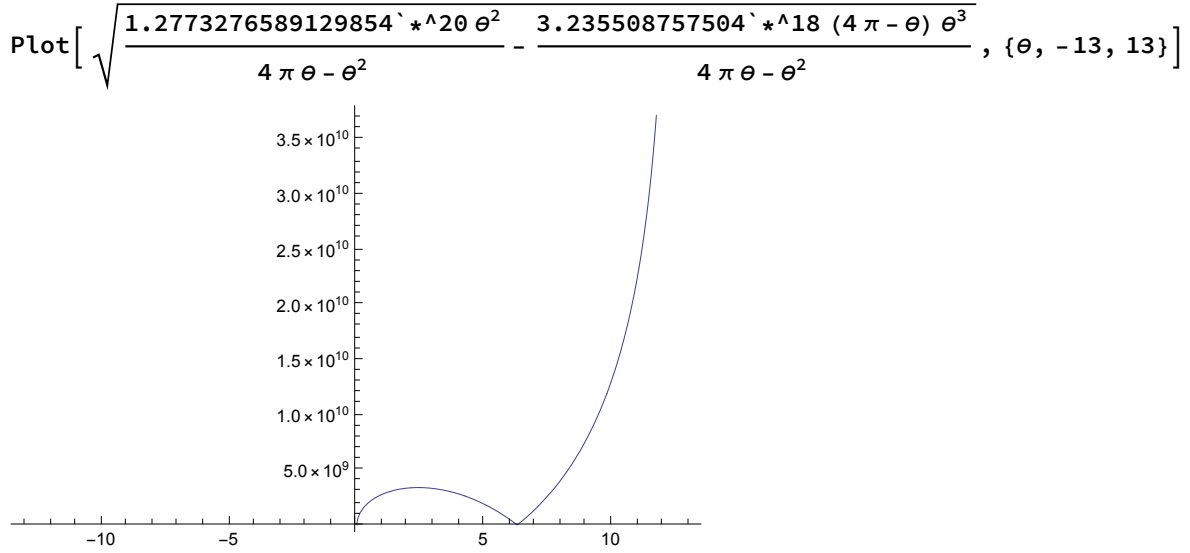
$$\text{Simplify}\left[\sqrt{\frac{r^2 (4 \pi - \theta) \theta}{4 \pi^2}}\right]$$

$$\frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi}$$

For light, the equation would read :

$$r_1 = \sqrt{\left( \left( \frac{2 (2.99792 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \left( \frac{\sqrt{\left( \frac{2 (2.99792 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2 \right)}$$

$$\sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2}}$$



This is something much different from the quality of matter whose energetic relation to velocity is defined within its own consistency.

Now we will return to the more general form of the equation. The case when  $h = (r/6\theta)$  ( $6\theta$ )

Now, by doing the first and second derivatives of the functions for radius in terms of the square of  $h$  being equal to the area of the circle of  $r_1$  with respect to time will give us velocity.

$$\left\{ \{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{ r \rightarrow -\frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \right\}, \quad (72)$$

$$\left\{ r \rightarrow \frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\}$$

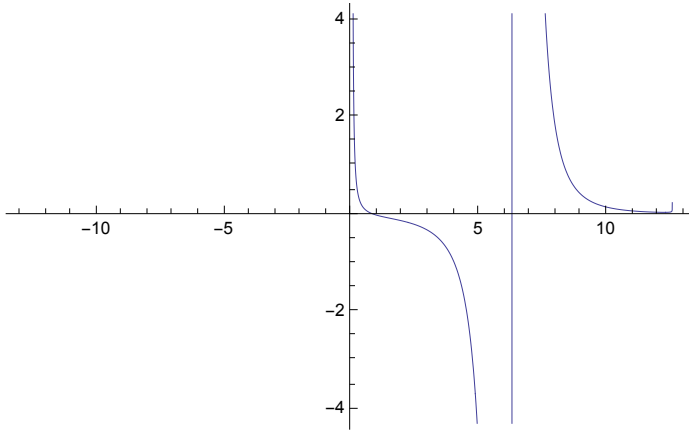
$$D\left[-\frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta\right] = D[r, \theta]$$

$$D\left[-\frac{2\pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta\right]$$

$$-\frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right)}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} +$$

$$\frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}$$

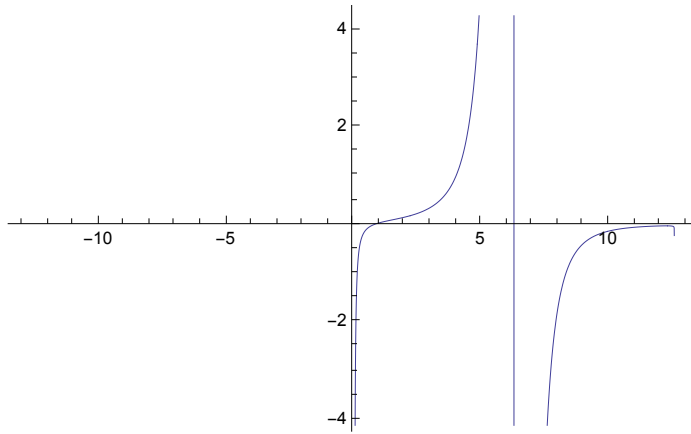
$$\text{Plot}\left[-\frac{\pi^{3/2}\left(-\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}}+\frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}-\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}+\frac{\pi^{3/2}\left(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3\right)\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}},\{\theta,-13,13\}\right]$$



$$\text{D}\left[\frac{2\pi^{3/2}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}},\theta\right]$$

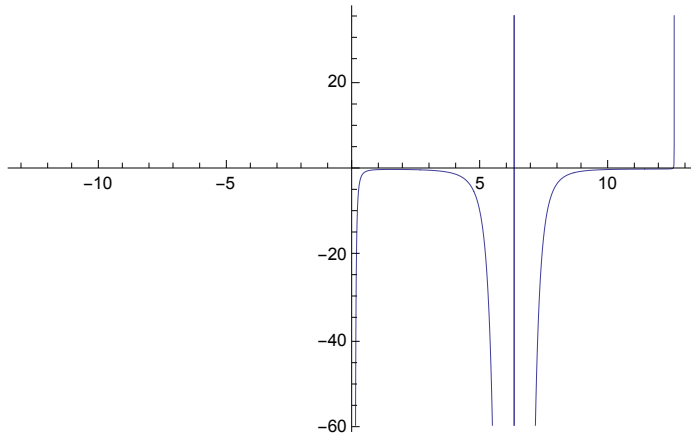
$$\frac{\pi^{3/2}\left(-\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}}+\frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}-\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}-\frac{\pi^{3/2}\left(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3\right)\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}}$$

$$\text{Plot}\left[\frac{\pi^{3/2}\left(-\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}}+\frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}-\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}-\frac{\pi^{3/2}\left(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3\right)\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{\left(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4\right)^{3/2}},\{\theta,-13,13\}\right]$$



$$\begin{aligned}
& D \left[ - \frac{\pi^{3/2} \left( - \frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}} + \right. \\
& \left. \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}, \theta \right] \\
& \frac{\pi^{3/2} \left( - \frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)^2}{2 \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \left( - \frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)^{3/2}} - \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3 ((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2\theta ((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \left. \left. \frac{4(4\pi-2\theta)}{\pi^2\theta^2 \sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2\theta \sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} \right) + \\
& \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( - \frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}} - \\
& \frac{3\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{2(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} + \\
& \frac{\pi^{3/2} (48\pi^2 - 48\pi\theta + 12\theta^2) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}
\end{aligned}$$

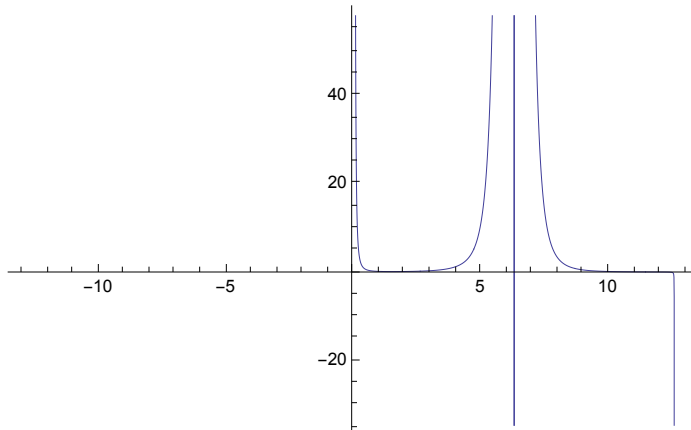
$$\begin{aligned}
& \text{Plot} \left[ \frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)^2}{2 \sqrt{16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4} \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta} \right)^{3/2}} - \right. \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3 ((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2 \theta ((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \left. \left. \frac{4(4\pi-2\theta)}{\pi^2 \theta^2 \sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}} \right) + \\
& \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2 \theta - 24\pi \theta^2 + 4\theta^3) \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)}{(16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}} - \\
& \frac{3\pi^{3/2} (-32\pi^3 + 48\pi^2 \theta - 24\pi \theta^2 + 4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}}{2(16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4)^{5/2}} + \\
& \frac{\pi^{3/2} (48\pi^2 - 48\pi \theta + 12\theta^2) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}}{(16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4)^{3/2}}, \{\theta, -13, 13\} \Big]
\end{aligned}$$



$$\begin{aligned}
& D \left[ \frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}} - \right. \\
& \left. \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}, \theta \right] \\
& - \frac{\pi^{3/2} \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)^2}{2 \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)^{3/2} +} \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3 ((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2\theta ((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \left. \left. \frac{4(4\pi-2\theta)}{\pi^2\theta^2 \sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2\theta \sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} \right) - \\
& \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( -\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}} + \\
& \frac{3\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{2(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} - \\
& \frac{\pi^{3/2} (48\pi^2 - 48\pi\theta + 12\theta^2) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}
\end{aligned}$$



$$\begin{aligned}
& \text{Plot} \left[ - \frac{\pi^{3/2} \left( - \frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)^2}{2 \sqrt{16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4} \left( - \frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta} \right)^{3/2}} + \right. \\
& \left( \pi^{3/2} \left( \frac{(4\pi-2\theta)^2}{4\pi^3 ((4\pi-\theta)\theta)^{3/2}} - \frac{(4\pi-2\theta)^2}{\pi^2 \theta ((4\pi-\theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi-\theta)\theta}} - \right. \right. \\
& \left. \left. \frac{4(4\pi-2\theta)}{\pi^2 \theta^2 \sqrt{(4\pi-\theta)\theta}} - \frac{4}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} + \frac{8\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^3} \right) \right) / \\
& \left( \sqrt{16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4} \sqrt{- \frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}} \right) - \\
& \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2 \theta - 24\pi \theta^2 + 4\theta^3) \left( - \frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2 \theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta^2} \right)}{(16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4)^{3/2} \sqrt{- \frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}} + \\
& \frac{3\pi^{3/2} (-32\pi^3 + 48\pi^2 \theta - 24\pi \theta^2 + 4\theta^3)^2 \sqrt{- \frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}}{2(16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4)^{5/2}} - \\
& \frac{\pi^{3/2} (48\pi^2 - 48\pi \theta + 12\theta^2) \sqrt{- \frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2 \theta}}}{(16\pi^4 - 32\pi^3 \theta + 24\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4)^{3/2}}, \{\theta, -13, 13\} \Big]
\end{aligned}$$



For more explanation on this section of the topic, please see the paper : No Time, Only True, available at : <http://www.scribd.com/doc/20041709/No-Time-Only-True>

If we take these solutions, or any of the solutions from the roots

The following solutions for theta come from :

$$n = \frac{\sqrt{(4\pi - \theta)\theta}}{\pi \theta^2}$$

$$\pi r_1^2 =$$

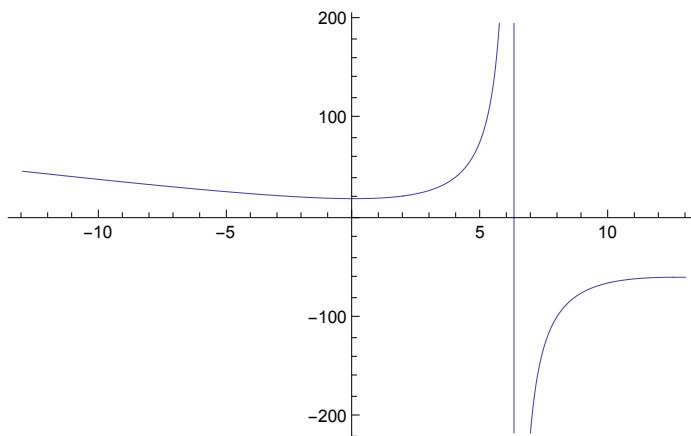
$$\pi (r^2 - \eta^2)^2 = \pi \left( r^2 - \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)^2 = n (\eta^2) = \frac{\sqrt{(4\pi - \theta) \theta}}{\pi \theta^2} \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right)$$

$$\pi r^2 - \pi \left( r^2 - \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)^2 = \Delta A$$

$$\int \left( \pi \left( \frac{2\pi \sqrt{4\pi^2 - 4\pi\theta + \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 - \pi \left( \left( \frac{2\pi \sqrt{4\pi^2 - 4\pi\theta + \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 - \frac{\left( \left( \frac{2\pi \sqrt{4\pi^2 - 4\pi\theta + \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)^2 (4\pi - \theta) \theta \right)}{4\pi^2} \right)^2 \right) d\theta$$

$$\pi \left( -\theta - \frac{4\pi^2}{-2\pi + \theta} \right)$$

$$\text{Plot} \left[ \pi \left( -\theta - \frac{4\pi^2}{-2\pi + \theta} \right), \{\theta, -13, 13\} \right]$$



$$\left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}$$

$$\frac{2\pi \sqrt{4\pi^2 - 4\pi\theta + \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} = r$$

Alden Daniels :

"geometric interpretation where you see higher dimensions being generated through implicit tensions that somehow cause dimensions stretching to infinity, but in the process of having that in a limiting case, they are actually creating expansion of higher dimensions."

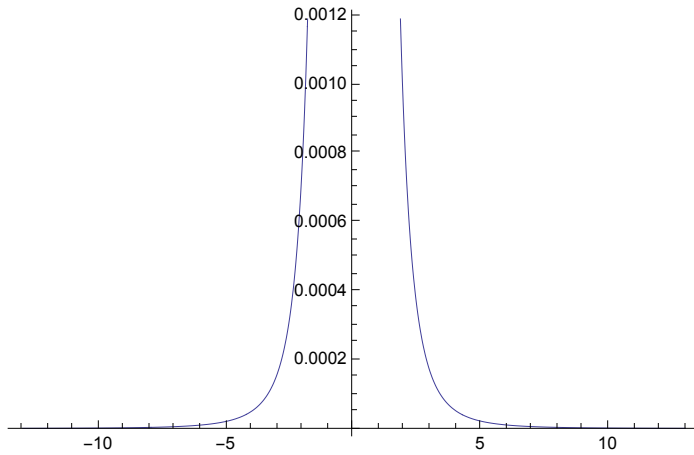
Implicit shape of consciousness relates to the genetic structure. Spin inherently generates motion.

Drawing

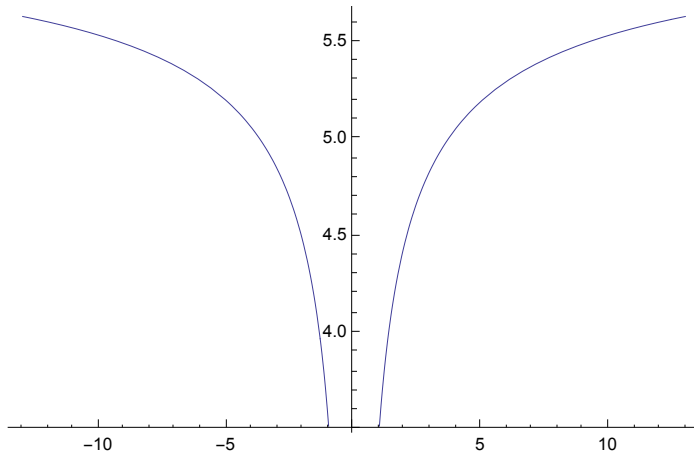
$$\text{Solve}\left[\pi\left(r^2 - \left(\frac{r^2(4\pi - \theta)\theta}{4\pi^2}\right)\right)^2 = \frac{\sqrt{(4\pi - \theta)\theta}}{\pi\theta^2}\left(\frac{r^2(4\pi - \theta)\theta}{4\pi^2}\right), \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 1\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 2\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 3\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 4\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 5\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 6\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 7\right\}, \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \\ & \quad \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 8\right\}, \right. \\ & \left. \left. \left\{ \theta \rightarrow \text{Root}\left[-1024\pi^3 + (768\pi^2 + 256\pi^8 r^4)\pi + (-192\pi - 1024\pi^7 r^4)\pi^2 + (16 + 1792\pi^6 r^4)\pi^3 - \right. \right. \right. \\ & \quad \left. \left. \left. 1792\pi^5 r^4 \pi^4 + 1120\pi^4 r^4 \pi^5 - 448\pi^3 r^4 \pi^6 + 112\pi^2 r^4 \pi^7 - 16\pi r^4 \pi^8 + r^4 \pi^9 \&, 9\right\} \right\} \right\} \end{aligned}$$

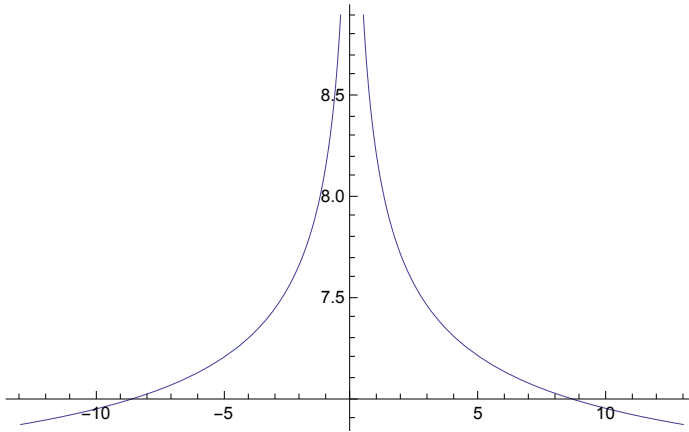
```
Plot[Root[-1024  $\pi^3$  + (768  $\pi^2$  + 256  $\pi^8 r^4$ ) #1 +
  (-192  $\pi$  - 1024  $\pi^7 r^4$ ) #12 + (16 + 1792  $\pi^6 r^4$ ) #13 - 1792  $\pi^5 r^4$  #14 + 1120  $\pi^4 r^4$  #15 -
  448  $\pi^3 r^4$  #16 + 112  $\pi^2 r^4$  #17 - 16  $\pi r^4$  #18 +  $r^4$  #19 &, 1], {r, -13, 13}]
```



```
Plot[Root[-1024  $\pi^3$  + (768  $\pi^2$  + 256  $\pi^8 r^4$ ) #1 +
  (-192  $\pi$  - 1024  $\pi^7 r^4$ ) #12 + (16 + 1792  $\pi^6 r^4$ ) #13 - 1792  $\pi^5 r^4$  #14 + 1120  $\pi^4 r^4$  #15 -
  448  $\pi^3 r^4$  #16 + 112  $\pi^2 r^4$  #17 - 16  $\pi r^4$  #18 +  $r^4$  #19 &, 2], {r, -13, 13}]
```



Plot[Root[-1024  $\pi^3$  + (768  $\pi^2$  + 256  $\pi^8 r^4$ ) #1 +  
 (-192  $\pi$  - 1024  $\pi^7 r^4$ ) #1<sup>2</sup> + (16 + 1792  $\pi^6 r^4$ ) #1<sup>3</sup> - 1792  $\pi^5 r^4$  #1<sup>4</sup> + 1120  $\pi^4 r^4$  #1<sup>5</sup> -  
 448  $\pi^3 r^4$  #1<sup>6</sup> + 112  $\pi^2 r^4$  #1<sup>7</sup> - 16  $\pi r^4$  #1<sup>8</sup> +  $r^4$  #1<sup>9</sup> &, 3], {r, -13, 13}]



The last six solutions (the last six roots for  $\theta$ ) plotted to empty, and no graph was able to be made.

$$\left\{ \{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{ r \rightarrow -\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right\}, \right. \\ \left. \left\{ r \rightarrow \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right\} \right\} \quad (73)$$

$$r = \frac{2 (2.99792 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \lambda = \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \quad (74)$$

$$r = \frac{2 h \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 (c) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 (r / t) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 (r / (6 \theta)) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \\ \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}$$

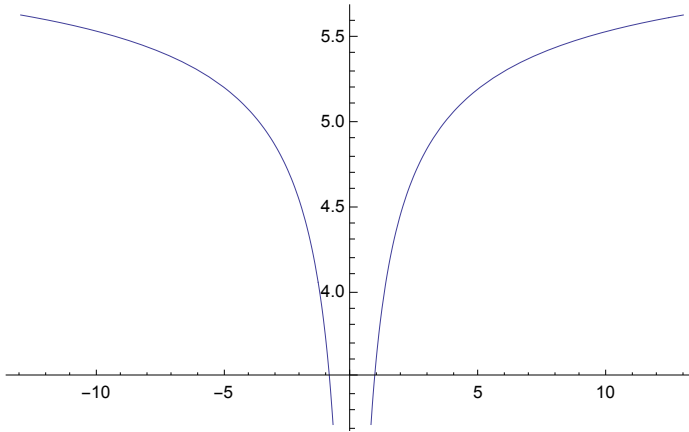
Where c is the speed of light.

$$\text{Solve}\left[\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} = \frac{2 (r / (6 \theta)) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}}, r\right] \\ \left\{ \left\{ r \rightarrow \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right\} \right\}$$

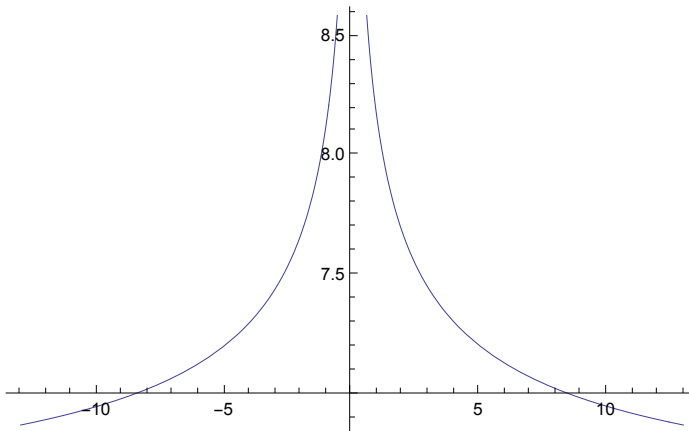
$$\text{Solve}\left[r == \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + \right. \right. \\ & \quad \left. \left. (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 1\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 2\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 3\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 4\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 5\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 6\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 7\right], \right. \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^{12}r^4 + (-1024\pi^5 - 1024\pi^{11}r^4)\pi + (1280\pi^4 + 1792\pi^{10}r^4)\pi^2 + \right. \right. \\ & \quad \left. \left. (-640\pi^3 - 1792\pi^9r^4)\pi^3 + (160\pi^2 + 1120\pi^8r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (-20\pi - 448\pi^7r^4)\pi^5 + (1 + 112\pi^6r^4)\pi^6 - 16\pi^5r^4\pi^7 + \pi^4r^4\pi^8 \&, 8\right] \right\} \end{aligned}$$

```
Plot[Root[256 π12 r4 + (-1024 π5 - 1024 π11 r4) #1 + (1280 π4 + 1792 π10 r4) #12 +
  (-640 π3 - 1792 π9 r4) #13 + (160 π2 + 1120 π8 r4) #14 + (-20 π - 448 π7 r4) #15 +
  (1 + 112 π6 r4) #16 - 16 π5 r4 #17 + π4 r4 #18 &, 1], {r, -13, 13}]
```



```
Plot[Root[256 π12 r4 + (-1024 π5 - 1024 π11 r4) #1 + (1280 π4 + 1792 π10 r4) #12 +
  (-640 π3 - 1792 π9 r4) #13 + (160 π2 + 1120 π8 r4) #14 + (-20 π - 448 π7 r4) #15 +
  (1 + 112 π6 r4) #16 - 16 π5 r4 #17 + π4 r4 #18 &, 2], {r, -13, 13}]
```



The last 6 roots yielded no graph, and we are uncertain of the x intercept.

```
Solve[ $\frac{2 (r / (6 \theta)) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} == r, \theta]$ 
```

```
{ {θ → 2 π} }
```

From  $\pi r_1^2 = (r^2 - \eta^2)^2 = \pi \left( r^2 - \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right) \right)^2 = n \left( \frac{r^2 (4\pi - \theta) \theta}{4\pi^2} \right)$

For,  $n = \frac{\sqrt{(4\pi - \theta) \theta}}{\pi \theta^2}$

We say the general statement that :

$$\left\{ \{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{ r \rightarrow - \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \right\},$$

$$\left\{ r \rightarrow \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \}$$

For  $n = 1$ , we say specifically that :

$$\text{Solve}\left[\pi \left(r^2 - \left(\frac{r^2 (4\pi - \theta)\theta}{4\pi^2}\right)\right)^2 = \left(\frac{r^2 (4\pi - \theta)\theta}{4\pi^2}\right), r\right]$$

$$\left\{ \{r \rightarrow 0\}, \{r \rightarrow 0\}, \left\{ r \rightarrow - \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \right\},$$

$$\left\{ r \rightarrow \frac{2 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right\} \}$$

So, we will now look at the velocity of our equations by taking their first derivative with respect to time.

$$D\left[-\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta\right]$$

$$\text{Simplify}\left[-\frac{\pi^{3/2} \left(-\frac{4\pi-2\theta}{2\pi^3 \sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta \sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}} + \frac{\pi^{3/2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}}\right]$$

$$\frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}} (4\pi^2 - 16\pi\theta + 3\theta^2)}{\theta \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)}$$

$$\theta \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)$$

$$m \frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}} (4\pi^2 - 16\pi\theta + 3\theta^2)}{\theta \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)} = \text{momentum} = p$$

$$\Delta p \Delta x = h / 2 \pi$$

$$x = r$$

$$\Delta m \frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}} (4\pi^2 - 16\pi\theta + 3\theta^2)}{\theta \sqrt{(-2\pi + \theta)^4} (8\pi^2 - 6\pi\theta + \theta^2)} \left( -\Delta \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}{\sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right)$$



$$\text{Solve}\left[\left(6.62606896 \times 10^{-34}\right) / 2 \pi == m D\left[\frac{\sqrt{\frac{((4 \pi-\theta) \theta)^{3/2}}{\theta^2}}\left(4 \pi^2-16 \pi \theta+3 \theta^2\right)}{\theta \sqrt{(-2 \pi+\theta)^4}\left(8 \pi^2-6 \pi \theta+\theta^2\right)}, \theta\right]\right.$$

$$\left.\left(D\left[-\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi-\theta) \theta}}{\pi^3}}+\frac{4 \sqrt{(4 \pi-\theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4-32 \pi^3 \theta+24 \pi^2 \theta^2-8 \pi \theta^3+\theta^4}}, \theta\right], m\right]\right.$$

$$\left.\left\{\left\{m \rightarrow\right.\right.\right.$$

$$1.04082 \times 10^{-33} / \left(\left(-\left(5.56833\left(-\frac{0.0161258(12.5664-2. \theta)}{\sqrt{(12.5664-1. \theta) \theta}}+\frac{0.202642(12.5664-2. \theta)}{\theta \sqrt{(12.5664-1. \theta) \theta}}-\frac{0.405285 \sqrt{(12.5664-1. \theta) \theta}}{\theta^2}\right)\right) / \right.$$

$$\left.\left(\sqrt{1558.55-992.201 \theta+236.871 \theta^2-25.1327 \theta^3+\theta^4}\right.\right.$$

$$\left.\sqrt{-0.0322515 \sqrt{(12.5664-1. \theta) \theta}+\frac{0.405285 \sqrt{(12.5664-1. \theta) \theta}}{\theta}}\right)+$$

$$\left(5.56833(-992.201+473.741 \theta-75.3982 \theta^2+4. \theta^3)\right.$$

$$\left.\sqrt{-0.0322515 \sqrt{(12.5664-1. \theta) \theta}+\frac{0.405285 \sqrt{(12.5664-1. \theta) \theta}}{\theta}}\right) /$$

$$\left.\left(1558.55-992.201 \theta+236.871 \theta^2-25.1327 \theta^3+\theta^4\right)^{3/2}\right)$$

$$\left(\frac{\sqrt{\frac{((12.5664-1. \theta) \theta)^{3/2}}{\theta^2}}(-50.2655+6. \theta)}{\sqrt{(-6.28319+\theta)^4 \theta(78.9568-18.8496 \theta+\theta^2)}}-\right.$$

$$1. \frac{\sqrt{\frac{((12.5664-1. \theta) \theta)^{3/2}}{\theta^2}}(-18.8496+2. \theta)(39.4784-50.2655 \theta+3. \theta^2)}{\sqrt{(-6.28319+\theta)^4 \theta(78.9568-18.8496 \theta+\theta^2)}^2}-$$

$$1. \frac{\sqrt{\frac{((12.5664-1. \theta) \theta)^{3/2}}{\theta^2}}(39.4784-50.2655 \theta+3. \theta^2)}{\sqrt{(-6.28319+\theta)^4 \theta^2(78.9568-18.8496 \theta+\theta^2)}}-$$

$$\begin{aligned}
& \frac{2. (-6.28319 + \theta)^3 \sqrt{\frac{((12.5664 - 1. \theta) \theta)^{3/2}}{\theta^2}} (39.4784 - 50.2655 \theta + 3. \theta^2)}{((-6.28319 + \theta)^4)^{3/2} \theta (78.9568 - 18.8496 \theta + \theta^2)} + \\
& \left( 0.5 (39.4784 - 50.2655 \theta + 3. \theta^2) \right. \\
& \quad \left. \left( \frac{1.5 (12.5664 - 2. \theta) \sqrt{(12.5664 - 1. \theta) \theta}}{\theta^2} - \frac{2. ((12.5664 - 1. \theta) \theta)^{3/2}}{\theta^3} \right) \right) / \\
& \quad \left( \sqrt{(-6.28319 + \theta)^4} \theta \sqrt{\frac{((12.5664 - 1. \theta) \theta)^{3/2}}{\theta^2}} (78.9568 - 18.8496 \theta + \theta^2) \right) \Bigg) \Bigg\}
\end{aligned}$$

Plot[1.0408204783457682`\*^-33/

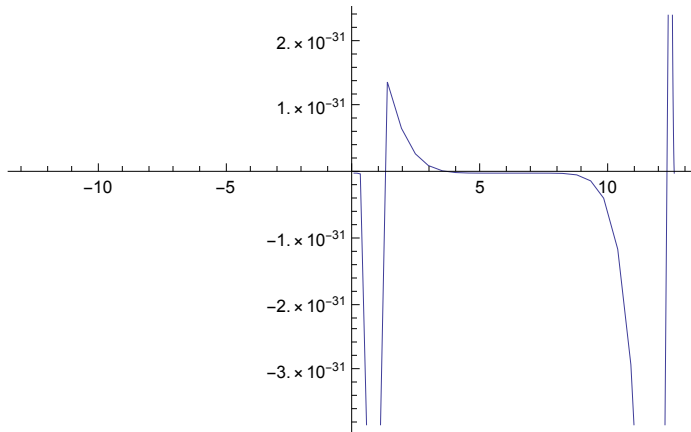
$$\begin{aligned}
& \left( \left( -5.568327996831707 \cdot \left( -\frac{0.016125767216599748 (12.566370614359172 - 2. \theta)}{\sqrt{(12.566370614359172 - 1. \theta) \theta}} + \right. \right. \right. \\
& \quad \frac{0.20264236728467555 (12.566370614359172 - 2. \theta)}{\theta \sqrt{(12.566370614359172 - 1. \theta) \theta}} - \\
& \quad \left. \left. \frac{0.4052847345693511 \sqrt{(12.566370614359172 - 1. \theta) \theta}}{\theta^2} \right) \right) / \\
& \quad \left( \sqrt{(1558.5454565440389 - 992.2008537695941 \theta + 236.8705056261446 \theta^2 - \right. \\
& \quad \left. 25.132741228718345 \theta^3 + \theta^4)} \right. \\
& \quad \left. \sqrt{\left( -0.032251534433199495 \sqrt{(12.566370614359172 - 1. \theta) \theta} + \right. \right. \\
& \quad \left. \left. \frac{0.4052847345693511 \sqrt{(12.566370614359172 - 1. \theta) \theta}}{\theta} \right) \right) + \\
& \quad \left( 5.568327996831707 (-992.2008537695941 + 473.7410112522892 \theta - \right. \\
& \quad \left. 75.39822368615503 \theta^2 + 4. \theta^3) \right. \\
& \quad \left. \sqrt{\left( -0.032251534433199495 \sqrt{(12.566370614359172 - 1. \theta) \theta} + \right. \right. \\
& \quad \left. \left. \frac{0.4052847345693511 \sqrt{(12.566370614359172 - 1. \theta) \theta}}{\theta} \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( 1558.5454565440389 - 992.2008537695941 \theta + 236.8705056261446 \theta^2 - \right. \\
& \quad \left. 25.132741228718345 \theta^3 + \theta^4 \right)^{3/2} \Bigg) \\
& \left( \left( \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} (-50.26548245743669 + 6. \theta) \right) \right. \\
& \quad \left( \sqrt{(-6.283185307179586 + \theta)^4} \theta \right. \\
& \quad \left. (78.95683520871486 - 18.84955592153876 \theta + \theta^2) \right) - \\
& \left( 1. \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} (-18.84955592153876 + 2. \theta) \right. \\
& \quad \left. (39.47841760435743 - 50.26548245743669 \theta + 3. \theta^2) \right) \Bigg) / \\
& \left( \sqrt{(-6.283185307179586 + \theta)^4} \theta \right. \\
& \quad \left. (78.95683520871486 - 18.84955592153876 \theta + \theta^2)^2 \right) - \\
& \left( 1. \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} (39.47841760435743 - \right. \\
& \quad \left. 50.26548245743669 \theta + 3. \theta^2) \right) \Bigg) / \left( \sqrt{(-6.283185307179586 + \theta)^4} \right. \\
& \quad \left. \theta^2 (78.95683520871486 - 18.84955592153876 \theta + \theta^2) \right) - \\
& \left( 2. (-6.283185307179586 + \theta)^3 \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} \right. \\
& \quad \left. (39.47841760435743 - 50.26548245743669 \theta + 3. \theta^2) \right) \Bigg) / \\
& \left( ((-6.283185307179586 + \theta)^4)^{3/2} \theta \right. \\
& \quad \left. (78.95683520871486 - 18.84955592153876 \theta + \theta^2) \right) + \\
& \left( 0.5 (39.47841760435743 - 50.26548245743669 \theta + 3. \theta^2) \right. \\
& \quad \left. \left( \frac{1}{\theta^2} 1.5 (12.566370614359172 - 2. \theta) \sqrt{(12.566370614359172 - 1. \theta) \theta} - \right. \right.
\end{aligned}$$

$$\left( \frac{2. \cdot ((12.566370614359172 \cdot -1. \cdot \theta) \theta)^{3/2}}{\theta^3} \right) /$$

$$\left( \sqrt{(-6.283185307179586 \cdot + \theta)^4 \theta} \sqrt{\frac{((12.566370614359172 \cdot -1. \cdot \theta) \theta)^{3/2}}{\theta^2}} \right.$$

$$\left. \left. \left. (78.95683520871486 \cdot -18.84955592153876 \cdot \theta + \theta^2) \right) \right) \right), \{\theta, -13, 13\}]$$



Now we will take the first derivative of our second r value for another solution to where the mass is in terms of angle.

$$D \left[ \frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \theta \right]$$

$$\frac{\pi^{3/2} \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{\sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}} -$$

$$\frac{\pi^{3/2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \sqrt{-\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3}} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta}}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}}$$

$$\text{Simplify}\left[\frac{\pi^{3/2}\left(-\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}}+\frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}}-\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2}\right)}{\sqrt{16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4}\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}\right. \\ \left.-\frac{\pi^{3/2}\left(-32\pi^3+48\pi^2\theta-24\pi\theta^2+4\theta^3\right)\sqrt{-\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3}+\frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta}}}{(16\pi^4-32\pi^3\theta+24\pi^2\theta^2-8\pi\theta^3+\theta^4)^{3/2}}\right] \\ \frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-4\pi^2+16\pi\theta-3\theta^2)}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}$$

$$\Delta p \Delta r = \hbar / 2 \pi$$

$$\text{Solve}\left[(6.62606896 * 10^{\wedge}-34) / 2 \pi ==\right.$$

$$\left.\text{m D}\left[\frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-4\pi^2+16\pi\theta-3\theta^2)}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}\right], \theta\right] \frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-4\pi^2+16\pi\theta-3\theta^2)}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}, \text{m}]$$

$$\text{Solve}\left[(\hbar) / 2 \pi ==\right.$$

$$\left.\text{m D}\left[\frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-4\pi^2+16\pi\theta-3\theta^2)}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}\right], \theta\right] \frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-4\pi^2+16\pi\theta-3\theta^2)}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}, \text{m}]$$

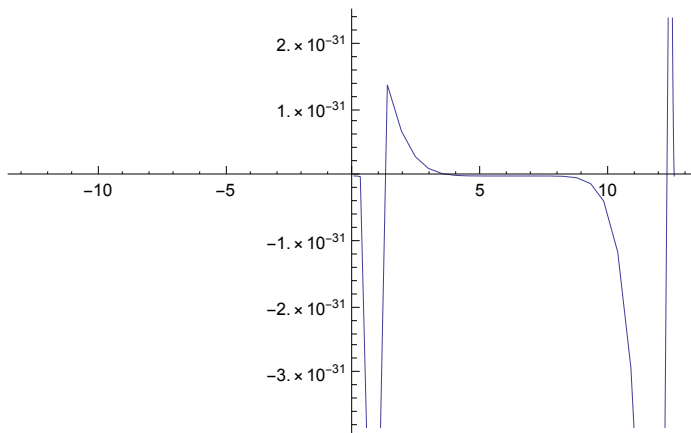
$$\left\{\left\{\text{m} \rightarrow \left(\hbar \pi \theta \sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)\right)\right\} / \left(2 \sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}\right.\right.$$

$$\left.(-4\pi^2+16\pi\theta-3\theta^2)\left(-\frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-6\pi+2\theta)(-4\pi^2+16\pi\theta-3\theta^2)}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)^2}+\right.\right. \\ \left.\left.\frac{(16\pi-6\theta)\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}}{\theta\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}-\frac{2\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-2\pi+\theta)^3(-4\pi^2+16\pi\theta-3\theta^2)}{\theta((-2\pi+\theta)^4)^{3/2}(8\pi^2-6\pi\theta+\theta^2)}\right.\right. \\ \left.\left.\frac{\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}(-4\pi^2+16\pi\theta-3\theta^2)}{\theta^2\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}+\right.\right. \\ \left.\left.\frac{(-4\pi^2+16\pi\theta-3\theta^2)\left(\frac{3(4\pi-2\theta)\sqrt{(4\pi-\theta)\theta}}{2\theta^2}-\frac{2((4\pi-\theta)\theta)^{3/2}}{\theta^3}\right)}{2\theta\sqrt{\frac{((4\pi-\theta)\theta)^{3/2}}{\theta^2}}\sqrt{(-2\pi+\theta)^4}(8\pi^2-6\pi\theta+\theta^2)}\right)\right\}\right\}$$

$$\text{Plot}\left[\left(1.0408204783457682^{\wedge}-33\sqrt{(-6.283185307179586^{\wedge}+\theta)^4}\right.\right.$$

$$\begin{aligned}
& \theta \left( 78.95683520871486 - 18.84955592153876 \theta + \theta^2 \right) \Bigg/ \\
& \left( \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} \right. \\
& \quad \left. (-39.47841760435743 + 50.26548245743669 \theta - 3. \theta^2) \right. \\
& \quad \left. \left( -1. \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} (-18.84955592153876 + 2. \theta) \right. \right. \\
& \quad \quad \left. \left. (-39.47841760435743 + 50.26548245743669 \theta - 3. \theta^2) \right) \right) \Bigg/ \\
& \quad \left( \sqrt{(-6.283185307179586 + \theta)^4} \theta \right. \\
& \quad \quad \left. (78.95683520871486 - 18.84955592153876 \theta + \theta^2)^2 \right) + \\
& \quad \left( (50.26548245743669 - 6. \theta) \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} \right) \Bigg/ \\
& \quad \left( \sqrt{(-6.283185307179586 + \theta)^4} \theta \right. \\
& \quad \quad \left. (78.95683520871486 - 18.84955592153876 \theta + \theta^2) \right) - \\
& \quad \left( 1. \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} (-39.47841760435743 + \right. \\
& \quad \quad \left. 50.26548245743669 \theta - 3. \theta^2) \right) \Bigg/ \left( \sqrt{(-6.283185307179586 + \theta)^4} \right. \\
& \quad \quad \left. \theta^2 (78.95683520871486 - 18.84955592153876 \theta + \theta^2) \right) - \\
& \quad \left( 2. (-6.283185307179586 + \theta)^3 \sqrt{\frac{((12.566370614359172 - 1. \theta) \theta)^{3/2}}{\theta^2}} \right. \\
& \quad \quad \left. (-39.47841760435743 + 50.26548245743669 \theta - 3. \theta^2) \right) \Bigg/ \\
& \quad \left( ((-6.283185307179586 + \theta)^4)^{3/2} \theta \right. \\
& \quad \quad \left. (78.95683520871486 - 18.84955592153876 \theta + \theta^2) \right) + \\
& \quad \left( 0.5 (-39.47841760435743 + 50.26548245743669 \theta - 3. \theta^2) \right.
\end{aligned}$$

$$\left( \frac{1}{\theta^2} 1.5 \cdot (12.566370614359172 - 2 \cdot \theta) \sqrt{(12.566370614359172 - 1 \cdot \theta) \theta} - \frac{2 \cdot ((12.566370614359172 - 1 \cdot \theta) \theta)^{3/2}}{\theta^3} \right) / \left( \sqrt{(-6.283185307179586 + \theta)^4 \theta} \sqrt{\frac{((12.566370614359172 - 1 \cdot \theta) \theta)^{3/2}}{\theta^2}} (78.95683520871486 - 18.84955592153876 \cdot \theta + \theta^2) \right), \{\theta, -13, 13\}]$$



We experience the mass of an object through its meaning and function. The shape of the cone and the equalities within the syntax of our system.

Perceptual Philosophy with William Edelglass

Parker Emmerson

Wednesday, September 16

I.From on the Soul by Aristotle

Aristotle is defining a perceivable difference for the relationship of ideas through systems of perception (the senses). To me, this project makes great sense, because when I think of the difference between sound and music, I feel like the sound is less permanent to my perception, whereas music is more structured and permanent. A sound leaves an impression, but can we really attempt to categorize something so infinitely dense like this impression by calling it a form? Within each sense, we can categorize qualities of the sense, however, the categories are a mixture of each other, and parameters may work better to discuss the elements of sense. I think of the object of sense, for example, sound, being like a well in time, just like a cup creates a well of space to hold a substance. When we perceive, we are giving something new to the system of the well, i.e. we are putting a "spoon" into the cup, and withdrawing meaning, by some sentient understanding of the material held within the well, be it waves created

by the spoon's maker interacting with water or tasting rice and thinking of snow, because, "The senses perceive each other's special objects incidentally; not because the percipient sense is this or that special sense, but because all form a unity." Aristotle, however, did lack an awareness of intuitive sensing, or sixth sense, i.e. the noticing of something uneasy or invisible. What is the difference between sense and vision for Aristotle, aside from pure sight due to physical stimuli? The difference between two ideas is indeed related to a mathematical description, although this allegory can be made loosely when it pertains to the perception of the properties of the meaning of ideas (structured by idea or inherent property).

## II. From an Essay toward a New Theory of Vision by George Berkeley

Berkeley is refining his semantic differences between seeing and vision. Vision, to me, implies an entire accessible realm of being visionary, whereas seeing is more related to sight in particular. I think that light is necessary for sight, but vision is related to both the visual and auditory systems. Light creates a chemical reaction in the brain, but the mind can access the same neurological and chemical structures to bring about a vision without direct light stimulus to the eye. Berkeley provides an overview of perceptual theory, and provides an account of the connection between meaning of senses and development of structure for the interpretation of any sense. When Berkeley says, "Moreover it is evident that no idea which is not itself perceived can be the means of perceiving any other idea" I sincerely disagree. There is the idea of 0/1 and it is not perceived. Yet, it can be the means of perceiving 10, in the base 10 system. If Berkeley's argument held, then 1 would be the same as 10. For the system to be consistent, we must be talking about numbering the same kind of things, not different placement values. Also, I could think of the frying ice cube, and this idea is not perceived when the true ice cube is not something that can change at all, for it is a perfect cube, and when frying, would immediately melt, however it could be the means of perceiving boiling water. I think that the mind can generate new ideas through invention. When invention occurs, an idea arises that previously went unseen. This arising may indeed come from the collection and contributions of other ideas. However, if the new idea is truly new, it is thus greater than the illusion in which the idea rests and the sum of all its component ideas. Thus, it can only relate to the phenomenon, through a direct make-believe correlation.

## III. Thomas Reid, Powers of Man

One might have a notion and conception of an object and not be able to see it, because of its context. There is a difference between perceiving an object and a system. How does language influence perception? Can one only see visible structure? What does it mean to give the name of a word? Is the mathematical validity of measuring things to have a self-evident axiom that depends on what we see, and can it be said to be true only insofar as it is true for what we see? When we discuss the God's eye perspective, we mean that it is possible, or hypothetically plausible that we, the perceivers are actually being perceived by some other being, and thus the observer is being affected by the perception of the other. This, however, would mean that God sees humanity from outside, and creates paradox, and that the origin of all paradox would be greater than we can conceive. However, I disagree. For, God knows the liars from the truth tellers without having to ask them, without having to inquire into by observation their own statements.



#### IV.From The Philosophy of the Enlightenment

Cassirer first asks touches on the problem of whether a man, born blind, would be able to acquire the sense of sight. He notes that this problem allows us to ponder into whether or not perception produces the physical world. He raises issues of the mind's being somehow involved in the perceivable world, and inquires what functions of the mind engage the relation of things to perceptions. A blind person may still have some idea or vision of geometry and mathematics without actually seeing the geometric structure. What perception of geometry would a blind person see? This idea relates loosely to Plato's thought experiment in the cave. "The idea of space is not, therefore, strictly speaking an element of sense consciousness but an expression of a process, which goes on in consciousness. Only the speed and regularity of this process cause us to overlook the intermediate stages in ordinary introspection and to anticipate the end of the process at the very start (Perception Edited by Robert Schwartz Page 33). Cassirer goes on to elaborate on other philosophers with ideas on spatiality. Spatiality is the only integration of the mass that is perceived, the time that is perceived, and the energy that is imprinted in the visual system. This is done by the giving act of inclusion through empathy and the informationally dense, expressively simple, being of truth. Can we then tie this to the perception of beauty existentially, or would that break down into objectivism?

#### V.Elements of Physiology by Johannes Muller

For Muller, each nerve has a particular quality of energy. He then denotes the energies of each nerve to relate to Aristotle's categorical descriptions of sense. For me, Aristotle's idea of category would need to be closer to the idea of enclosing quality of something in areas of parameters for phenomenal description. When I sense a strawberry, I taste it, feel it and see it. When I really experience a strawberry, all of these individual senses are combined. Thus, experience is a combination of "timbres" that have their workspace existent relationships accessible to the mind. Discussing the function of nerves in the delivery of sensation is helpful, because it allows us to differentiate ideas through the cognition of relationships. He outlines the physiological correlations between different kinds of sensations. How can this help us see the difference between sense and experience?

#### VI.Treatis on Physiological Optics by Helmholtz

Helmholtz proposes that phenomena regarding the visual system can be described by the use of analogy when things begin to look paradoxical. He takes into consideration the psychic faculties and suggests that the processing of the environment and its perceptual phenomena may occur through an unconscious working of analogy in the mind. I find this to be interesting and agreeable. It provides a humanist account through the recognition of biological factors regarding perceptual systems. VII.Principles of Gestalt Psychology

The facts of direct perception can be related intimately to observing and experiment. Koffka says that, "as a rule, things are what they look like" (BRP, 51). Why not just say, "things look like what

they are”? For, how can a table be seen when there is no table? Koffka introduces notions of proximal and distant, which he uses to conclude that one of two objects will only look larger than the other only if it is in the same vertical plane as the other when its retinal image is larger. The proximal stimulus allows us to see size. How does framing of the legs relatively decrease the efficacy of the retinal image in producing a depth perception? How does contour effect the perception of size when relating two objects in different perceivable planes of verticality? Recognition of an orthogonal plane of relational verticality that does not relate directly to the retinal image may be the method used for the visual system to make discernments of distance on the horizon. Is consciousness a concept and how does intentionality play into this? To observe creates an intention through cognition. Aristotle begins to try to categorize the meaning of sensation for perceptual systems of all types, “The term object of sense covers three kinds of objects, two kinds of which we call perceptible in themselves, while the remaining one is only incidentally perceptible. Of the first two kinds one consists of what is special to a single sense, the other of what is common to any and all of the senses” (De Anima, Bk II, 418 a 1 - 13). I. From The Senses Considered as Perceptual Systems, and The Ecological Approach to Visual Perception by James J. Gibson

Objects are given the ability to be able to be conceived in some terms, but not other terms. - For Gibson, information given during sensation is the information delivered to the receptor. Gibson suggests that information exists in the world already, similar to Husserl’s idea of meaning. Experience is a relation of the information given in the world and the imaginary adulated mind synnaptically relating to the realness of the idea of mind through the existence of a complex perceptual system. Gibson believes that the phenomena can be perceptually understood in terms of the parameters by which they are measured. Can residual images effect the perception of depth or change it within the processing of information through being, imbuing a perception of one’s own character of being? When Gibson says, “in the case of a perceptual system, the input - output loop can be supposed to obtain information, actively” (BRP, 78), he relates perception to the information that is learned. How will the idea of a narrative relate to this assertion? “That province of the senses which is to “furnish us with a variety of sensations” is by no means the same as that which is to ‘make us perceive’” (BRP 72). By this, Reid and Gibson believe that there is another element to perception other than the information being detected by a sensing organism. If a perception is to have being, it must be loved, thus there must be an element of persona to endow it with meaning and structure. A perception exists in terms of true and only true, for when the senses go from relative rest to motion, the processes include acceleration, which is also in terms of only true, and exists only more complexly in terms of variable time. Each of these informational points of perceptual space, for Gibson, is containing a means by which the information contained within it can be understood purely in terms of actuality of the presence of a perceptual object or object of sense. The measurability of a threshold presents an interesting semantic conundrum. Threshold could mean many things. “Stimulus energy varies along simple dimensions like intensity and frequency, but stimulus information varies along innumerable complex dimensions, not all amenable to physical measurement.” With this idea, Gibson differentiates between the more objective elements of stimulus and the more subjective ones. However, isn’t all of the information readily available to me? The variants of energy flux at a particular receptor can be described by a grid of Boolean operators

that relate our perception of the true in our world and the actual space through which it delivers the awareness. From the *Evolving Brain* by R. Grant Steen, we can notice that, “the memory of a particular place is encoded in just one place cell.” It may be possible that when measuring objects in our environment, that the determination of their location through perceptual systems hinges on a single variable. The true stimuli of the world and receptor are not dependent on the actuality of anything’s presence until a perception is founded from corroborating perceptions within definitions of concrete being. It can be shown that the easily measured variables of stimulus energy, the intensity of light, sound, odor, and touch, for example, vary from place to place and from time to time as the individual goes about his business in the environment” (BRP 73). I disagree strongly, and in fact, there is no variation in time past the first derivative of distance. II. From *In and Out of the Black Box* by David W. Hamlyn

What kind of a sensation is he talking about? Hamlyn is questioning the actual occurrence of perceptions. He says that sensuous elements of perception like touch allow for a vocabulary of sensation. I think sensations happen through response, but can be really expressed and introspected upon through logical statements of propositions and equalities. Hamlyn also touches on the issue of whether or not visual experience is required for perception, taking the position that sight is not required for perception, but vision is. He tries to limit the meaning of the word vision to the realm of seeing with the eyes by referring to the term seeing when discussing the lack of consciousness when there is no sensory aspect to the experience of light on the eyes. There is a sense and inference of space due to cognitive processing of complex perceptual systems. “To the extent that we are aware thereby of texture of the surface, the less are we likely to be aware of the sensations” (BPR 81). This sounds somewhat like the probability of finding a cat dead inside a box with a uranium death trigger. Perceptual space differs from physical space in that in physical space, there is never an occasion for infinity of weight, but with perceptual space, a single object of perception can take utmost, infinite priority during a given situation. Coming to awareness of an actual texture through physical sensation of touch requires that we abandon awareness of the sensations. When we are able to describe our sensational awareness’s being true, we are less likely to be aware of these as exact specific sensations. The forms of spatial perception proper are dependent on the information in light that is more easily specified to an exact location with relation to the environment than when the form itself is more general without any qualities of light able to fixed to their structure. III. From *Perception and Cognition* by John Heil

Heil begins proposing his theory by giving the layout of a theory he wishes to denounce in part, if not entirely. This account, which he rejects, is the account of sensory modalities by Grice. He says that theories that are based in the use of modalities for pinpointing the characteristics of sensation are, “burdened with two major, and a host of minor liabilities” (BRP 89). These theories are ones that he argues are based on an inner evidence, or, an “internal feature” (BPR 89). One of these is that they are hard pressed to find a series of components to perceptual experiences that designate a perception. I think that neuroscience has made progress doing this by analyzing the brain, but I’m sure that the same areas of the brain can be involved in multiple perceptual experiences. The other major “pitfall” is that all individuals do not perceive the world exactly the same. I do think that modes are relevant to discussing the perceptual system, but I think that they are general categories of linguistic expression

for stimuli, and do not capture the entire essence of the perceptual symphony. For instance, analogously, modalities of the physical stimuli of sound do not encompass all of the possible tonality. Heil acknowledges a character to senses and goes on to say that sensory modalities are the physical characteristic of the stimuli, not some inner - workings of the mind to interpret information provided like, “features we become aware of by means of them” (BRP 88). Perception, I am presently convinced, can be afforded by a mind interpreting its physical surroundings. Heil is expanding the act of seeing to include any detection of the physical environment by an individual by the perceptual system due to the sense of light. How would a T - perceiver respond to visual illusions? IV. From *The Will* by Brian O’Shaughnessy

O’Shaughnessy presents an account of sense that comes from awareness. Are we made aware of depth by inference? Awareness is a cognitive process, but also a potentially inferential one. When we are aware of space, we are also aware of material, time, and energy. Is there a sense that exists through the awareness of one of these in terms of any of the other three that can be said to infer an absence and a presence? The author’s project is to examine the will of the body and its relation to perceptual sensation. O’Shaughnessy would like to allow for the recognition that sensation occurs during the aftereffect of light or physical stimuli, not just during their immediate presence. Does O’Shaughnessy think that motions of the perceptual system are psychological? He talks about depth perception of a monocular system. A depth perception for a monocular visual experience requires multiple, sequential observations in which physical stimulus to the eye gives information to bring about awareness of the characteristics of the environment’s actuality. When the author talks about hallucination, I cannot follow his logic entirely, for when he says, “For a mental image is a seeming seeing, but not in the sense of being the same experience as seeing” (BPR 107), isn’t it that a hallucination is the belief in an actual presence, and a belief related to the perception of the world insofar as we can rely on the visual system? The afterimage is a reality in so far as it takes up space in the mind and this space is translated into a characteristic informative experience through embodied mind’s culminating vision of mind by anthropomorphic tendencies and the relinquishing of them into pure information. This resembles Gibson’s input - output loop. V. From *The Analysis of Sensation* by Ernst Mach

Mach begins by verifying a belief in the space - sense, an area of parameterized space relating the sense of an individual to the stimulus in the world. The space - sense provides a workspace for the individual senses like sense of sight and touch to enable a perceptual experience. “The perception of Depth depends on extra - ocular experiences” (BRP 118) is an idea that makes a great deal of sense to me, because when we experience or perceive truth, we use multiple faculties to make sense of a phenomenon. VI. From *Molyneux’s Question* by Michael J. Morgan

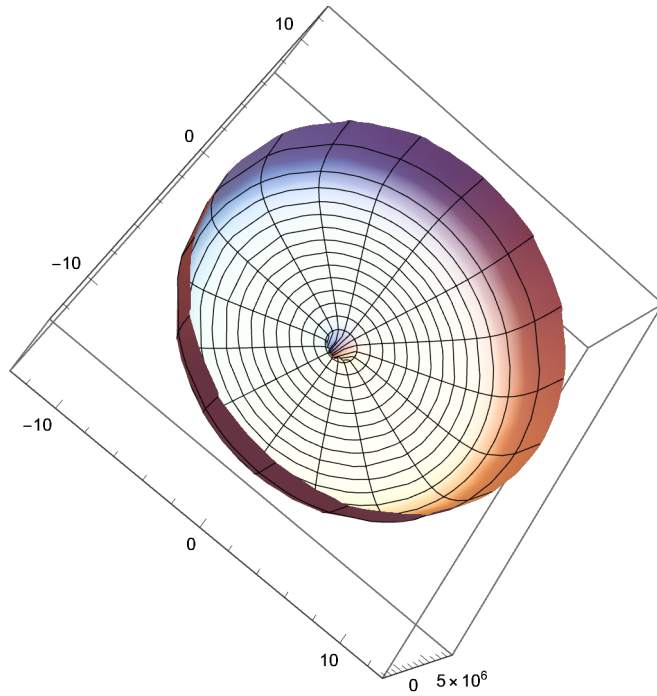
Morgan introduces the discussion with a discussion of Berkeley’s theory, which, from the interpretation of it by G.M. Stratton, suggested that inverted perception created by wearing a set of prismatic glasses would eventually go back to normal for the perceiver. Merleau - Ponty provides a description of what the experience is like. Merleau - Ponty reports that the vision changed gradually, but sounds were

still hard to place unless the object was identified. Morgan suggests that the experiment concludes that, “perceptual space is not at all like the space of the physicist, an indifferent, isomorphic three - dimensional manifold, in which objects are situated sensible to feeling as to sight, and in which things are the same no matter how oriented” (BRP 121). When we experience the world, the laws of physics are evident and consequential. The theories and propositions that pertain to the delivery of the meaning and stimulus in and due to the physical reality are equally valid when finding analogies to decipher meaning from the world for the pursuit of happiness, eternity, and knowledge. VII. Molyneux’s Question by Gareth Evans

If the man can eventually come to perceive relationships mathematically and gain enough knowledge through time, accustoming to the new perception of angles through sight, the answer is yes. It would be painful and hard, but plausible. A blind person can hear an amp and feel it at the same time. I think that Berkeley would be mistaken when thinking that touch could not have the same textural sense as sound. For Berkeley, sound and touch must occupy different areas of space - sense. If the blind man sees four dots, he can recognize the idea of four corners, which is in his database of prior experience. Vision with the eyes is a more immediate experience than perception with touch (feeling takes time), but that does not mean that the concept of the space taken up by a square cannot be conceived by a blind person and translated into mathematical language, then reapplied in a new method of perceiving the environment. Evans thinks that the notion of similarity will not apply. I agree, but I do think that the notion of realization could happen through a recognition of the parameters of the object with the newly acquired sensation. The conclusion would lead to the idea of language’s being a super - structure to the mind. We can tell a lot about something just by seeing it.

$$r = \frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}} = \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} = \frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \csc[\theta]}{\pi \sqrt{4 \pi - \theta}}$$

RevolutionPlot3D $\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}}\right)}{1166400}, \{\theta, -4 \pi, 4 \pi\}\right]$



$$\theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\text{Solve}\left[\theta == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), \beta\right]$$

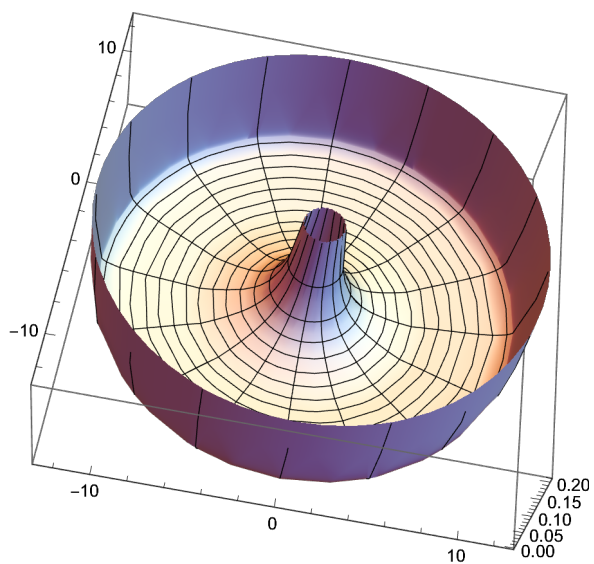
$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right] \right\}, \left\{ \beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right] \right\} \right\}$$

$$r = \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2} \text{Csc}\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{8 \pi^2 \sqrt{\theta}}$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\} \right\}$$

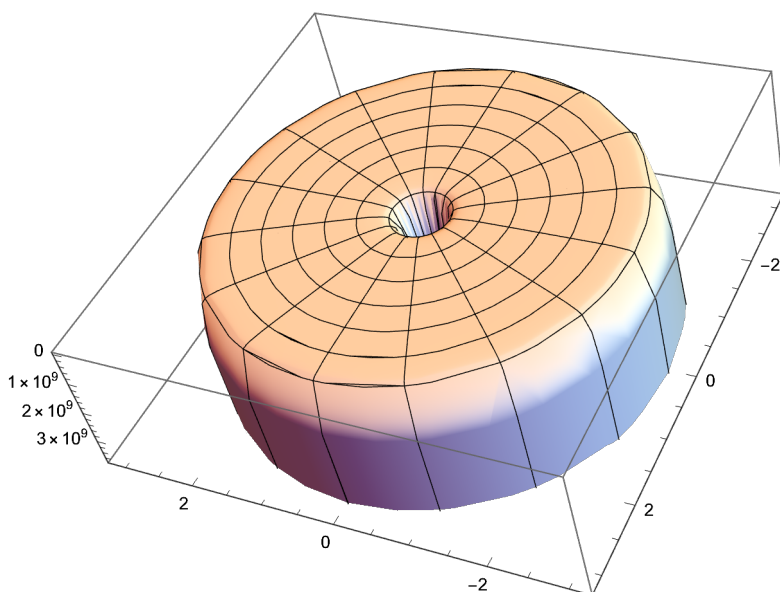
$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]}{8\pi^2\sqrt{\theta}}, \{\theta, -13, 13\}\right]$$



RevolutionPlot3D[

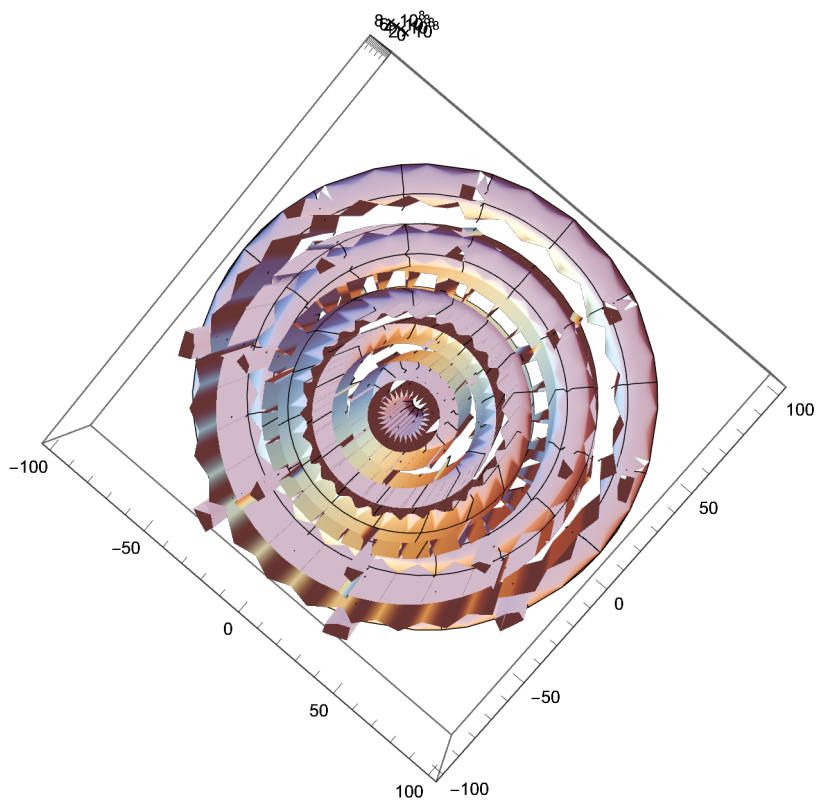
$$\frac{1}{1166400} \pi^2 \left( - \frac{540 c}{\sqrt{4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}} + \frac{1080 c}{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2} \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}} + \frac{1620 c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{5/2}} \right), \{\beta, -\pi, \pi\}]$$





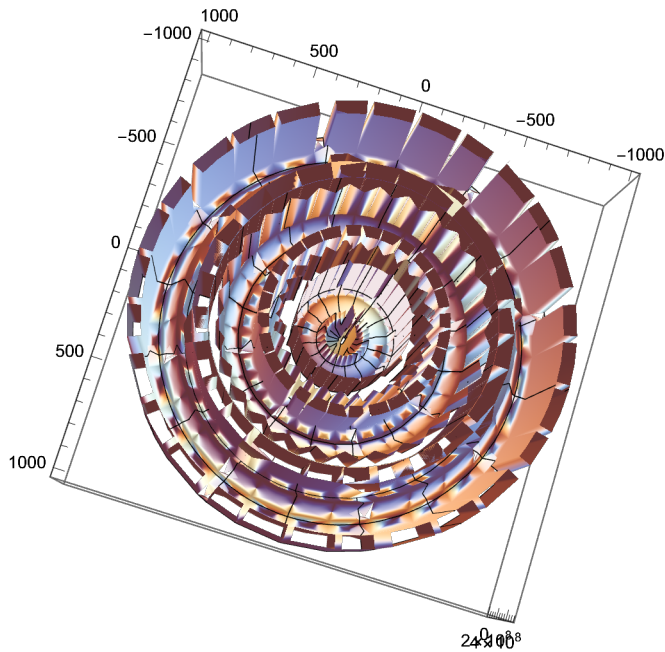
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$$\frac{1}{1166400} \pi^2 \left( - \frac{540 c}{\sqrt{4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}} + \frac{1080 c}{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2} \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}} + \frac{1620 c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{5/2}} \right), \{\beta, -100, 100\}]$$



RevolutionPlot3D[

$$\frac{1}{1166400} \pi^2 \left( -\frac{540 c}{\sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{3/2}} + \frac{1080 c}{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{3/2} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}} + \frac{1620 c \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{5/2}} \right), \{\beta, -1000, 1000\}]$$



$$\text{SphericalPlot3D}\left[\frac{1}{1166400} \pi^2 \left( -\frac{540 c}{\sqrt{4\pi - \theta} \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{3/2}} + \frac{1080 c}{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{3/2} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}} + \frac{1620 c \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{5/2}} \right), \{\theta, -13, 13\} \{\beta, -13, 13\}\right]$$

$$\text{From } \eta == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi},$$

$$\frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\text{Solve} \left[ \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), r \right]$$

$$\{\{r \rightarrow -\eta \csc[\beta]\}, \{r \rightarrow \eta \csc[\beta]\}\}$$

$$\text{Solve} \left[ \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), \eta \right]$$

$$\{\{\eta \rightarrow -r \sin[\beta]\}, \{\eta \rightarrow r \sin[\beta]\}\}$$

$$\text{Solve} \left[ \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), \beta \right]$$

$$\{\{\beta \rightarrow -\text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right]\}, \{\beta \rightarrow \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right]\}\}$$

$$\text{From D} \left[ 2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] = \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \frac{2 \pi \eta}{\theta},$$

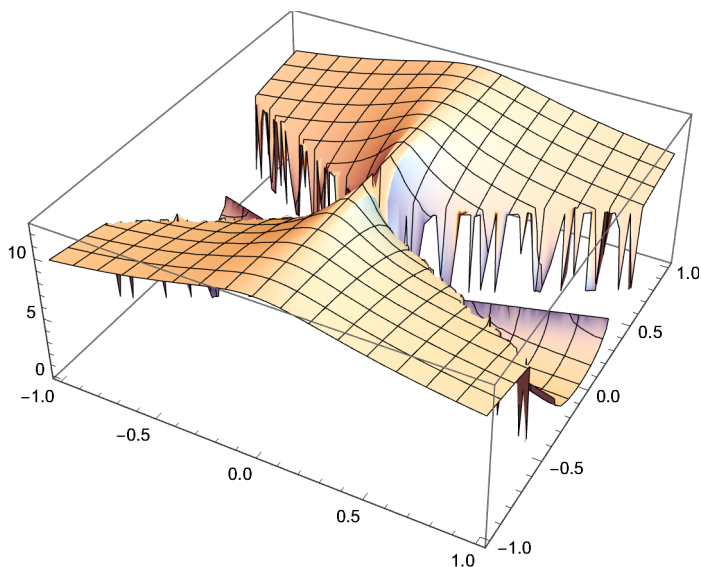
$$\theta = \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} -$$

$$\frac{2 \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} ==$$

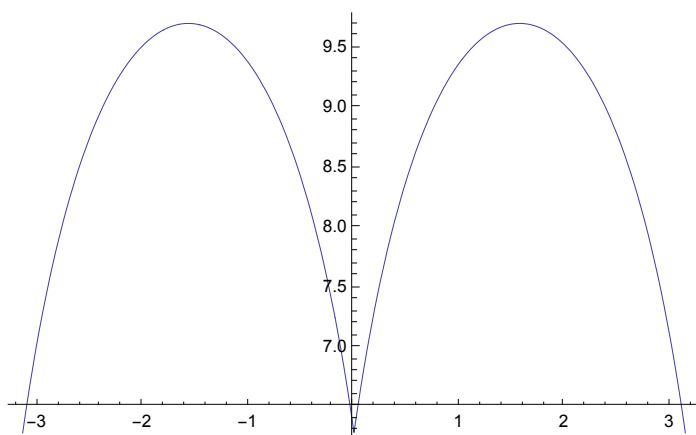
$$\frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} +$$

$$\frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}$$

$$\text{Plot3D}\left[\frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} - \frac{2\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}, \{r, -1, 1\}, \{\eta, -1, 1\}\right]$$

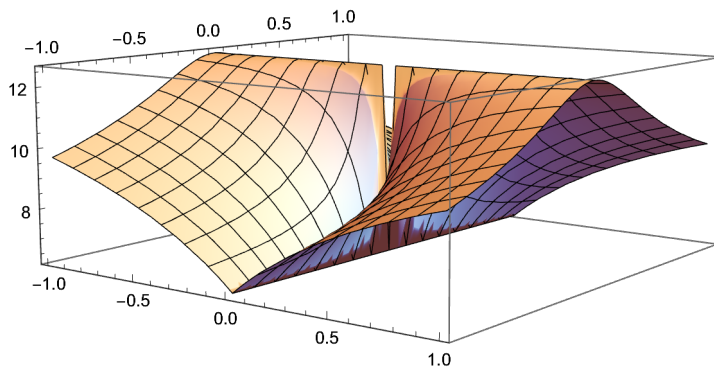


$$\text{Plot}\left[\frac{4\pi}{3} - \frac{-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2}{6 \left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}} + \frac{2}{3} \left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}, \{\beta, -\pi, \pi\}\right]$$



$$\begin{aligned}
\theta &= \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \\
&\quad \frac{2\pi \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3r^2} == \\
&\quad \frac{4\pi}{3} - \left( -4\pi^2 + 12\pi^2 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 \right) / \\
&\quad \left( 6 \left( -\pi^3 + 18\pi^3 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + 3\sqrt{3} \sqrt{\left( -\pi^6 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + \right.} \right. \right. \\
&\quad \left. \left. \left. 11\pi^6 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^4 + \pi^6 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^6 \right) \right)^{1/3} \right) + \\
&\quad \frac{2}{3} \left( -\pi^3 + 18\pi^3 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + 3\sqrt{3} \sqrt{\left( -\pi^6 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + \right.} \right. \\
&\quad \left. \left. \left. 11\pi^6 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^4 + \pi^6 \operatorname{Sin}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^6 \right) \right)^{1/3} \right)
\end{aligned}$$

$$\begin{aligned}
 & \text{Plot3D}\left[\frac{4\pi}{3} - \left(-4\pi^2 + 12\pi^2 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2\right) / \right. \\
 & \left. \left(6 \left(-\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + 3\sqrt{3} \sqrt{\left(-\pi^6 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 11\pi^6 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^6\right)\right)^{1/3} + \right. \\
 & \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + 3\sqrt{3} \sqrt{\left(-\pi^6 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^2 + 11\pi^6 \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^4 + \pi^6 \sin\left[\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right]\right]^6\right)\right)^{1/3}, \{\eta, -1, 1\}, \{r, -1, 1\}\right]
 \end{aligned}$$



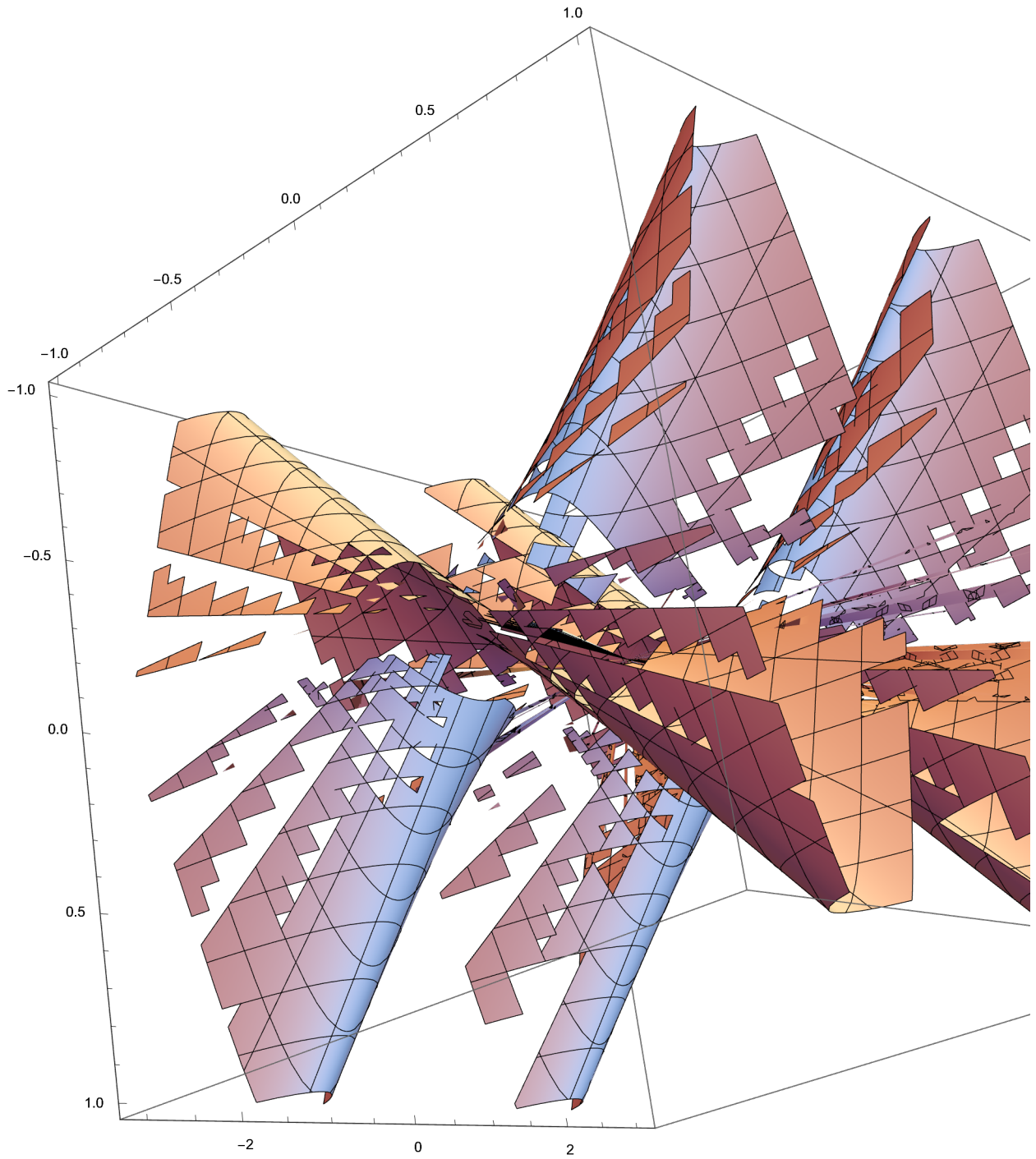
$$\begin{aligned}
& \text{Solve} \left[ \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \right. \\
& \quad \left. \frac{2 \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} == \right. \\
& \quad \frac{4 \pi}{3} - \left( -4 \pi^2 + 12 \pi^2 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 \right) / \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + 3 \sqrt{3} \sqrt{\left( -\pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 11 \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^4 + \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^6 \right) \right)^{1/3}} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + 3 \sqrt{3} \sqrt{\left( -\pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 11 \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^4 + \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^6 \right) \right)^{1/3}, r \right] \\
& \{\{\}\}
\end{aligned}$$

$$\begin{aligned}
& \text{Solve} \left[ \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \right. \\
& \quad \left. \frac{2 \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} == \right. \\
& \quad \frac{4 \pi}{3} - \left( -4 \pi^2 + 12 \pi^2 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 \right) / \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + 3 \sqrt{3} \sqrt{\left( -\pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 11 \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^4 + \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^6 \right) \right)^{1/3}} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + 3 \sqrt{3} \sqrt{\left( -\pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 11 \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^4 + \pi^6 \text{Sin} \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^6 \right) \right)^{1/3}, \eta]
\end{aligned}$$

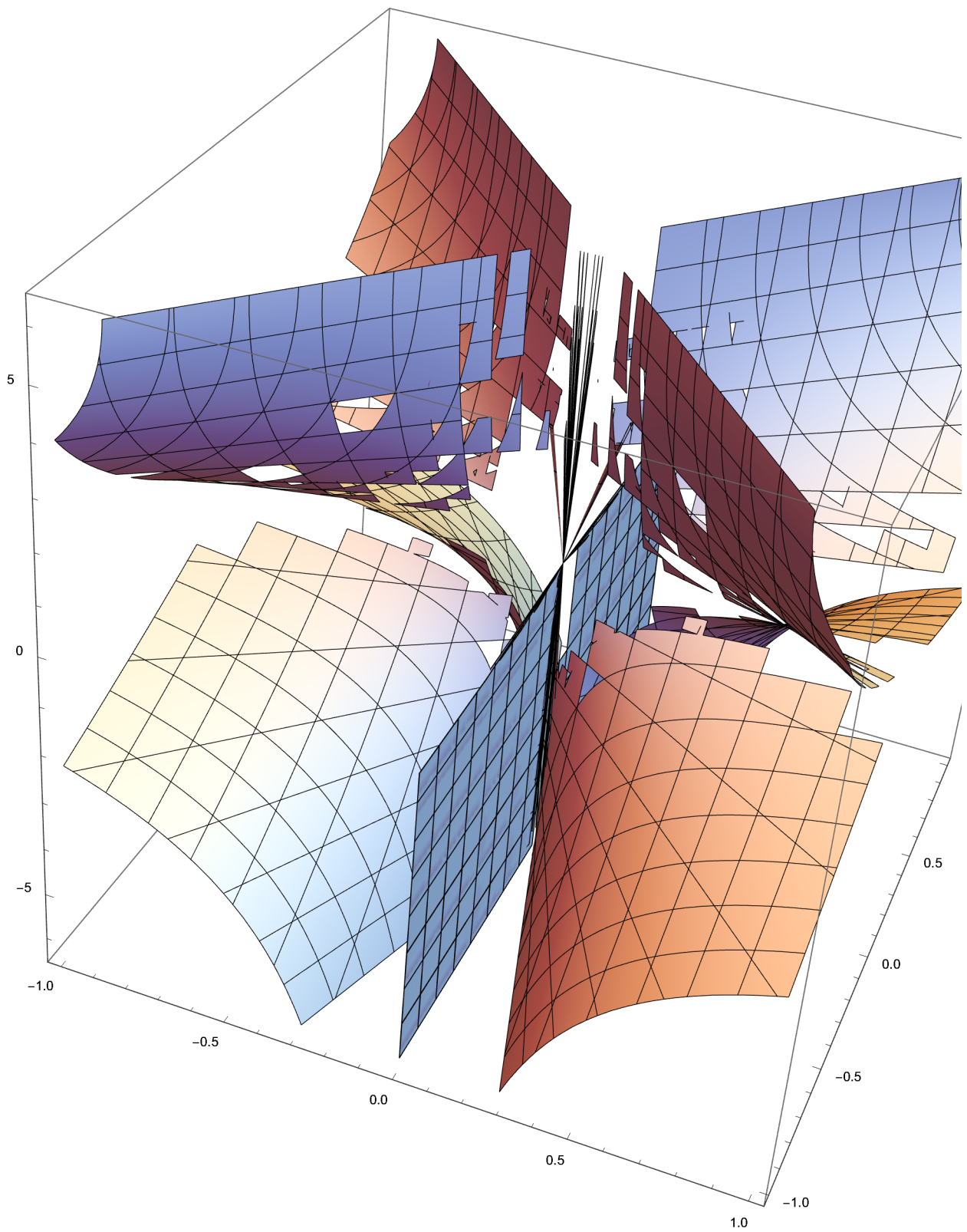
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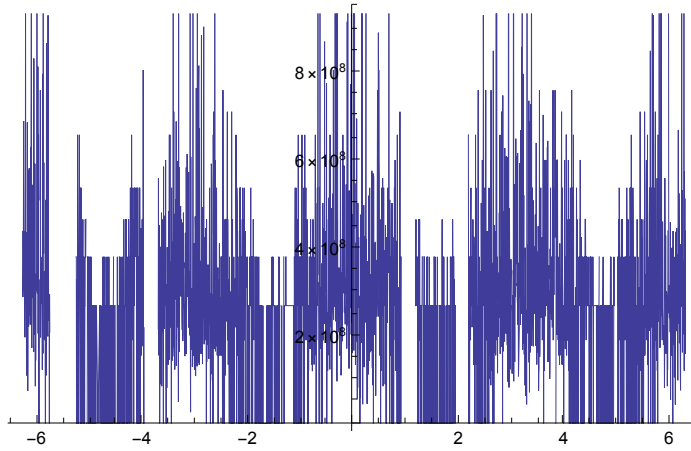
$$\begin{aligned}
& \text{Solve} \left[ \frac{4\pi}{3} + (-4\pi^2 (\eta \csc[\beta])^4 + 12\pi^2 (\eta \csc[\beta])^2 (r \sin[\beta])^2) / \right. \\
& \quad \left( 6\pi (\eta \csc[\beta])^2 \left( (\eta \csc[\beta])^6 - 18 (\eta \csc[\beta])^4 (r \sin[\beta])^2 + 3\sqrt{3} \sqrt{-(\eta \csc[\beta])^{10}} \right. \right. \\
& \quad \left. \left. (r \sin[\beta])^2 + 11 (\eta \csc[\beta])^8 (r \sin[\beta])^4 + (\eta \csc[\beta])^6 (r \sin[\beta])^6 \right) \right)^{1/3} \Bigg] - \\
& \quad \frac{1}{3 (\eta \csc[\beta])^2} 2\pi \left( (\eta \csc[\beta])^6 - 18 (\eta \csc[\beta])^4 (r \sin[\beta])^2 + 3\sqrt{3} \sqrt{-(\eta \csc[\beta])^{10}} \right. \\
& \quad \left. (r \sin[\beta])^2 + 11 (\eta \csc[\beta])^8 (r \sin[\beta])^4 + (\eta \csc[\beta])^6 (r \sin[\beta])^6 \right)^{1/3} == \\
& \quad \frac{4\pi}{3} - \left( -4\pi^2 + 12\pi^2 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \\
& \quad \left. \left. 3\sqrt{3} \sqrt{\left( -\pi^6 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 11\pi^6 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^4 + \pi^6 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^6 \right) \right)^{1/3} \right) + \\
& \quad \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + 3\sqrt{3} \sqrt{\left( -\pi^6 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 11\pi^6 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^4 + \pi^6 \sin \left[ \text{ArcSin} \left[ \sqrt{\frac{\eta^2}{r^2}} \right] \right]^6 \right) \right)^{1/3}, \eta \Bigg] \\
& \text{ContourPlot3D} \left[ \frac{4\pi}{3} + (-4\pi^2 (\eta \csc[\beta])^4 + 12\pi^2 (\eta \csc[\beta])^2 (r \sin[\beta])^2) / \right. \\
& \quad \left( 6\pi (\eta \csc[\beta])^2 \left( (\eta \csc[\beta])^6 - 18 (\eta \csc[\beta])^4 (r \sin[\beta])^2 + 3\sqrt{3} \sqrt{-(\eta \csc[\beta])^{10}} \right. \right. \\
& \quad \left. \left. (r \sin[\beta])^2 + 11 (\eta \csc[\beta])^8 (r \sin[\beta])^4 + (\eta \csc[\beta])^6 (r \sin[\beta])^6 \right) \right)^{1/3} \Bigg] - \\
& \quad \frac{1}{3 (\eta \csc[\beta])^2} 2\pi \left( (\eta \csc[\beta])^6 - 18 (\eta \csc[\beta])^4 (r \sin[\beta])^2 + \right. \\
& \quad \left. 3\sqrt{3} \sqrt{-(\eta \csc[\beta])^{10}} (r \sin[\beta])^2 + 11 (\eta \csc[\beta])^8 (r \sin[\beta])^4 + \right. \\
& \quad \left. (\eta \csc[\beta])^6 (r \sin[\beta])^6 \right)^{1/3}, \{r, -1, 1\}, \{\eta, -1, 1\}, \{\beta, -\pi, \pi\} \Bigg]
\end{aligned}$$



$$\begin{aligned}
& \text{ContourPlot3D} \left[ \frac{4\pi}{3} + \left( -4\pi^2 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^4 + \right. \right. \\
& \quad \left. \left. 12\pi^2 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 \right) / \right. \\
& \quad \left( 6\pi \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 \left( \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^6 - \right. \right. \\
& \quad \left. \left. 18 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^4 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 + \right. \\
& \quad \left. 3\sqrt{3} \sqrt{\left( - \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^{10} \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 + \right.} \\
& \quad \left. 11 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^8 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^4 + \right. \\
& \quad \left. \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^6 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^6 \right)^{1/3}} \right) - \\
& \quad \frac{1}{3 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2} 2\pi \left( \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^6 - \right. \\
& \quad \left. 18 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^4 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 + \right. \\
& \quad \left. 3\sqrt{3} \sqrt{\left( - \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^{10} \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^2 + \right.} \\
& \quad \left. 11 \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^8 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^4 + \right. \\
& \quad \left. \left( \eta \operatorname{Csc} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^6 \left( r \operatorname{Sin} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right)^6 \right)^{1/3}}, \\
& \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}
\end{aligned}$$

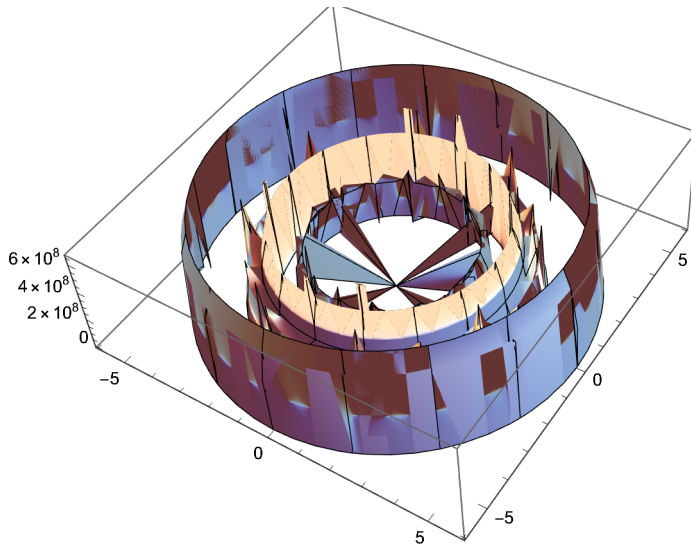


$$\text{Plot}\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.987551787368176 \cdot 10^{16}\right.\right.\right. \\ \left.\left.\left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right) / \\ \left(\sqrt{\left(-12.566370614359172 \cdot \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 +\right.\right. \\ \left.\left.39.47841760435743 \cdot \sin[\beta]^2\right)\right)}, \{\beta, -2\pi, 2\pi\} \right]$$



RevolutionPlot3D[

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right.} \right. \\ \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) / \\ \left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\ \left. \left. 39.47841760435743 \cdot \sin[\beta]^2 \right) \right), \{\beta, -2\pi, 2\pi\}]$$



$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

RevolutionPlot3D[ $\left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) / 2\pi$

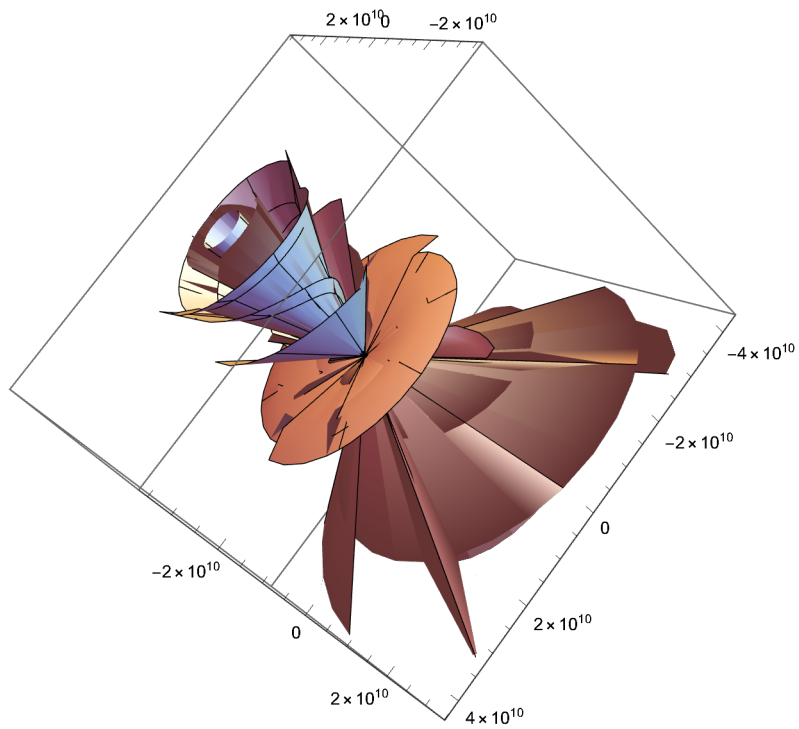
$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right.} \right. \\ \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) / \\ \left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\ \left. \left. 39.47841760435743 \cdot \sin[\beta]^2 \right) \right), \{\beta, -2\pi, 2\pi\}]$$

$$\begin{aligned}
\text{if } r = vt &= \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) / 2\pi \right) \\
&\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) / \\
&\left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) \\
\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} &= \frac{1}{2\pi} \\
&\left( \sqrt{\left( 4\pi \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) / 2\pi \right) \left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times \right. \right. \right. \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right. \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) \right) / \\
&\left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) \right)^2 \theta - \\
&\left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) / 2\pi \right) \left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \right. \right. \right. \\
&\quad \left. \left. \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) \right) / \\
&\left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \\
&\quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) \right)^2 \theta^2 \right)
\end{aligned}$$

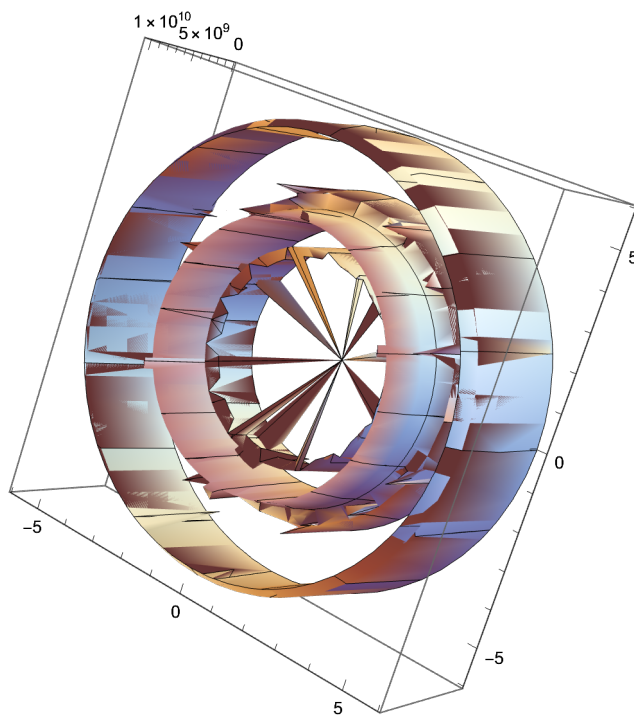
SphericalPlot3D[  

$$\left( \sqrt{4 \pi \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) / 2 \pi \right) \left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \right. \right.} \right. \right. \right. \\
\left. \left. \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right. \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) / \\
\left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \right) \right)^2 \theta - \\
\left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) / 2 \pi \right) \left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \right. \right. \right. \\
\left. \left. \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right. \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) \right) / \\
\left( \sqrt{\left( -12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \\
\left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot \right. \right. \\
\left. \left. \sin[\beta]^2 \right) \right) \right)^2 \theta^2 \right), \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}]$$



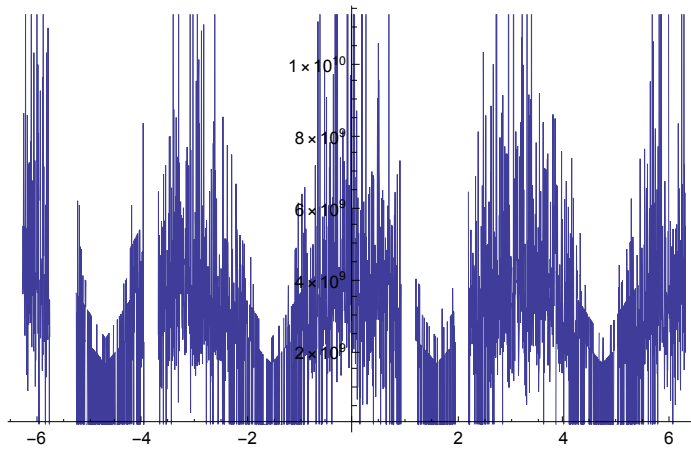


$\text{RevolutionPlot3D}\left[\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right.$   
 $\left.\left(\sqrt{\left(-1.1294090667581471 \times 10^{18} \times 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.987551787368176 \times 10^{16}\right.\right.\right.$   
 $\left.\left.\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2\right)\right) /$   
 $\left.\left(\sqrt{\left(-12.566370614359172 \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 +\right.\right.\right.$   
 $\left.\left.\left.39.47841760435743 \sin[\beta]^2\right)\right)\right), \{\beta, -2\pi, 2\pi\}]$

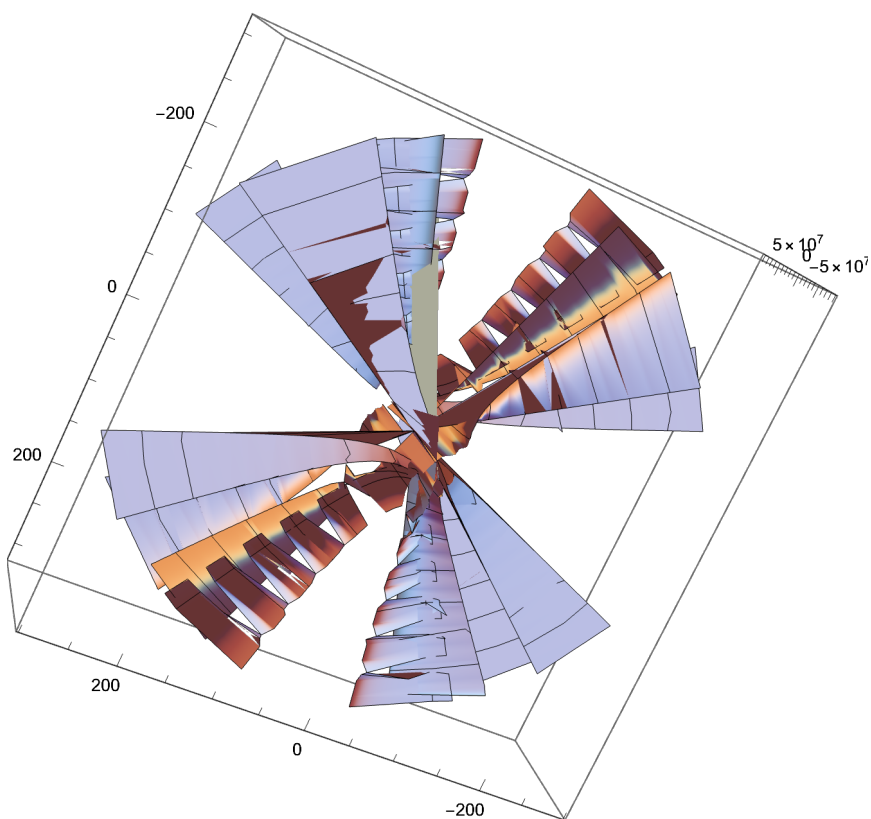


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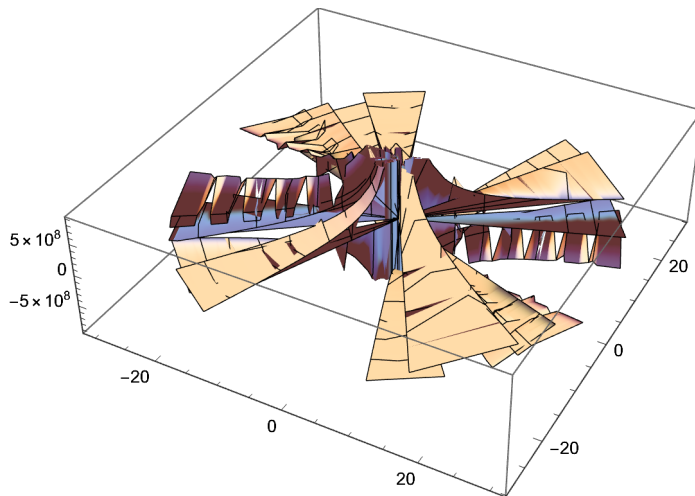
RevolutionPlot[ $\left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2 \pi\right)$ 
 $\left(\sqrt{\left(-1.1294090667581471 \times 10^{18} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.987551787368176 \times 10^{16}\right.\right.$ 
 $\left.\left.2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2}\right) /$ 
 $\left(\sqrt{\left(-12.566370614359172 \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 +\right.$ 
 $\left.\left.39.47841760435743 \sin[\beta]^2\right)\right), \{\beta, -2 \pi, 2 \pi\}]$ 
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$\text{RevolutionPlot3D}\left[\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / k\right)\right.$   
 $\left.\left(\sqrt{\left(-1.1294090667581471 \times 10^{18} \times 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.987551787368176 \times 10^{16}\right.\right.\right.$   
 $\left.\left.\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2\right)\right) / \right.$   
 $\left.\left(\sqrt{\left(-12.566370614359172 \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 +\right.\right.\right.$   
 $\left.\left.\left.39.47841760435743 \sin[\beta]^2\right)\right)\right], \{k, -100 \pi, 100 \pi\}, \{\beta, -2 \pi, 2 \pi\}]$



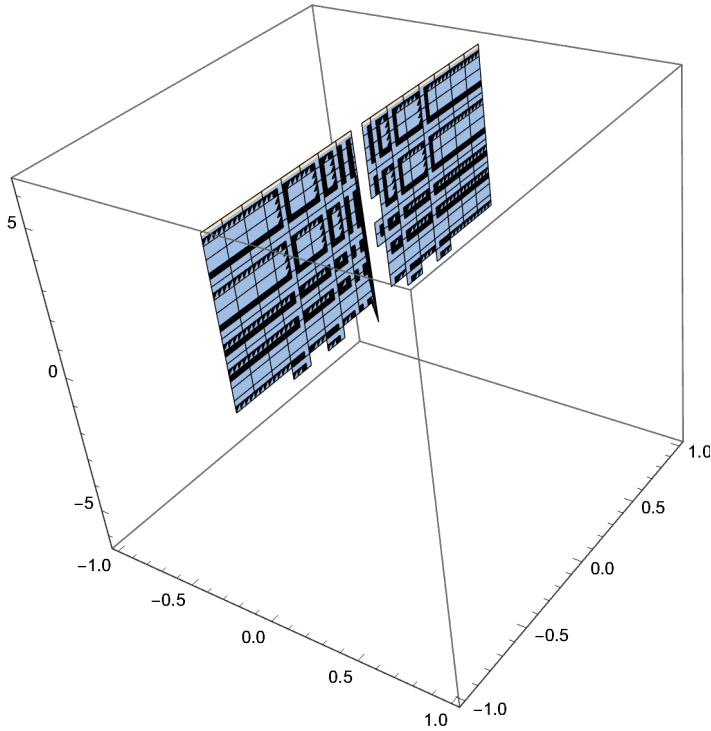
$$\text{RevolutionPlot3D}\left[\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / k\right)\right. \\ \left.\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \times 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.987551787368176 \cdot 10^{16}\right.\right.\right. \\ \left.\left.\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right) / \right. \\ \left.\left(\sqrt{\left(-12.566370614359172 \cdot \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 +\right.\right.\right. \\ \left.\left.\left.39.47841760435743 \cdot \sin[\beta]^2\right)\right)\right), \{k, -10 \pi, 10 \pi\}, \{\beta, -2 \pi, 2 \pi\}\right]$$



$$D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right] \\ \frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \\ D\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta\right] \\ - \frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \\ \int \left( - \frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) d\theta \\ - m \frac{r^2 (-2 \pi + \theta)}{2 \pi \sqrt{r^2 (4 \pi - \theta) \theta}}$$

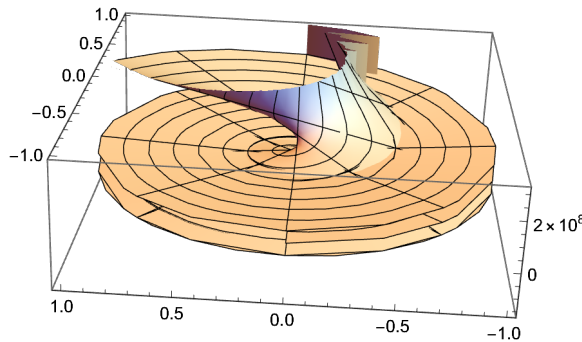
$$m \int F \, d\mathbf{t} = -m \frac{r^2 (-2\pi + \theta)}{2\pi \sqrt{r^2 (4\pi - \theta) \theta}} = W$$

$$\text{ContourPlot3D}\left[-m \frac{r^2 (-2\pi + \theta)}{2\pi \sqrt{r^2 (4\pi - \theta) \theta}}, \{m, -1, 1\}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$\begin{aligned} & D\left[\left(\sqrt{\left(3.5481432270250993 \times 10^{18} - \right. \right. \right. \\ & \quad \left. \left. \left. 1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2\right)\right)}\right) / \\ & \quad \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right), \theta] \\ & \left(-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta\right) / \\ & \quad \left(2 \sqrt{39.4784 - 12.5664 \theta + \theta^2} \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}\right) - \\ & \quad \frac{(-12.5664 + 2 \theta) \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{2 \left(39.4784 - 12.5664 \theta + \theta^2\right)^{3/2}} \end{aligned}$$

$$\text{RevolutionPlot3D}\left[\frac{\left(2 \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \sqrt{(3.5481432270250993 \theta^{18} - 1.1294090667581471 \theta^{18} \theta + 8.987551787368176 \theta^{16} \theta^2)}\right) - ((-12.566370614359172 + 2 \theta) \sqrt{(3.5481432270250993 \theta^{18} - 1.1294090667581471 \theta^{18} \theta + 8.987551787368176 \theta^{16} \theta^2)})}{\left(2 (39.47841760435743 - 12.566370614359172 \theta + \theta^2)^{3/2}\right)}, \{\theta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$



$$\begin{aligned} & \text{Solve} \left[ m \left( -1.1294090667581471 \cdot \theta^{18} + 1.7975103574736352 \cdot \theta^{17} \right) / \right. \\ & \quad \left( 2 \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \sqrt{(3.5481432270250993 \cdot \theta^{18} - \right. \\ & \quad \left. 1.1294090667581471 \cdot \theta^{18} \theta + 8.987551787368176 \cdot \theta^{16} \theta^2) \right) - \\ & \quad \left( (-12.566370614359172 + 2 \theta) \sqrt{(3.5481432270250993 \cdot \theta^{18} - \right. \\ & \quad \left. 1.1294090667581471 \cdot \theta^{18} \theta + 8.987551787368176 \cdot \theta^{16} \theta^2) \right) / \\ & \quad \left. \left( 2 (39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2)^{3/2} \right) = F, \theta \right] \\ & \left\{ \theta \rightarrow -\frac{0.25 (2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m)}{F} - \right. \\ & \quad 0.5 \sqrt{\left( \frac{0.25 (2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m)^2}{F^2} - \right. \\ & \quad \frac{1. (-5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m)}{F} + \frac{1}{F} \\ & \quad 2.45695 \times 10^{-29} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) + \\ & \quad (0.547258 (-2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + \\ & \quad 5.33882 \times 10^{31} m - 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2)) \Big) / \\ & \quad \left( F \left( 3.66307 \times 10^{29} F (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m)^2 - \right. \right. \\ & \quad 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m) (4.06727 \times 10^{36} - \\ & \quad \left. \left. 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m) (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \right. \end{aligned}$$

$$\begin{aligned}
& 7.66662 \times 10^{37} \text{ m}) + 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times \right. \\
& \quad \left. 10^{37} \text{ m})^3 + 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \right. \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - \right. \right. \\
& 9.7682 \times 10^{29} \text{ F} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) + \right. \right. \\
& \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} \text{ F} + 1.76788 \times 10^{28} \text{ F}^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} \text{ m} - 4.30581 \times 10^{52} \text{ F m} - 4.71919 \times 10^{59} \text{ m}^2 \right)^3 + \right. \\
& \quad \left. \left( 3.66307 \times 10^{29} \text{ F} \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m})^2 - \right. \right. \\
& \quad \left. \left. 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m}) \right. \right. \\
& \quad \left. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \right. \right. \\
& \quad \left. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \right. \right. \\
& \quad \left. \left. 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \right. \right. \\
& \quad \left. \left. 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \right. \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - 9.7682 \times \right. \right. \\
& \quad \left. \left. 10^{29} \text{ F} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \right. \right. \\
& \quad \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) \right)^2 \right)^{1/3} \right) + \\
& \frac{1}{\text{F}} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} \text{ F} \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - \right. \right. \\
& \quad \left. \left. 4.81708 \times 10^{38} \text{ m})^2 - 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - \right. \right. \right. \\
& \quad \left. \left. 4.81708 \times 10^{38} \text{ m}) \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \right. \right. \\
& \quad \left. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \right. \right. \\
& \quad \left. \left. 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \right. \right. \\
& \quad \left. \left. 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \right. \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - \right. \right. \\
& \quad \left. \left. 9.7682 \times 10^{29} \text{ F} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \right. \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) + \right. \right. \\
& \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} \text{ F} + 1.76788 \times 10^{28} \text{ F}^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} \text{ m} - 4.30581 \times 10^{52} \text{ F m} - 4.71919 \times 10^{59} \text{ m}^2 \right)^3 + \right. \\
& \quad \left. \left( 3.66307 \times 10^{29} \text{ F} \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m})^2 - \right. \right. \\
& \quad \left. \left. 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m}) \right. \right. \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \right. \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \right. \\
& \quad \left. \left. 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \right. \right. \\
& \quad \left. \left. 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \right. \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - 9.7682 \times \right. \right. \\
& \quad \left. \left. 10^{29} \text{ F} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right)^2 \Big)^{1/3} \Big) - \\
& 0.5 \sqrt{\left( \frac{0.5 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right.} \\
& \quad \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} - \\
& \quad \frac{1}{F} \\
& \quad 2.45695 \times 10^{-29} \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) - \\
& \quad \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + \right. \right. \\
& \quad \quad \left. \left. 5.33882 \times 10^{31} m - 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) \Big) / \\
& \quad \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right. \\
& \quad \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + 2. \\
& \quad \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + 27. \\
& \quad \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times 10^{29} \\
& \quad \quad F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \quad \quad \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \quad \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\
& \quad \quad \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& \quad \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& \quad \quad 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \quad \left. \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \right)^2 \right) \right)^{1/3} \Big) - \\
& \quad \frac{1}{F} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \quad \left. \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 4.81708 \times 10^{38} \text{ m}) (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \\
& 2. (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \\
& 27. (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - \\
& 9.7682 \times 10^{29} \text{ F} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) + \\
& \sqrt{\left( -4. (-4.71919 \times 10^{59} + 4.30581 \times 10^{52} \text{ F} + 1.76788 \times 10^{28} \text{ F}^2 + \right. \\
& \quad 9.43837 \times 10^{59} \text{ m} - 4.30581 \times 10^{52} \text{ F m} - 4.71919 \times 10^{59} \text{ m}^2) \left. \right)^3 + \\
& \quad (3.66307 \times 10^{29} \text{ F} (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m})^2 - \\
& \quad 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m}) \\
& \quad (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \\
& \quad (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \\
& \quad 2. (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \\
& \quad 27. (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \\
& \quad (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - 9.7682 \times \\
& \quad 10^{29} \text{ F} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \\
& \quad (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) \left. \right)^2 \Big)^{1/3} - \\
& \left( 0.25 \left( - \frac{8. (3.5506 \times 10^{10} - 992.201 \text{ F} - 3.5506 \times 10^{10} \text{ m})}{\text{F}} - \right. \right. \\
& \quad \frac{1. (2.99792 \times 10^8 - 25.1327 \text{ F} - 2.99792 \times 10^8 \text{ m})^3}{\text{F}^3} + \\
& \quad \frac{1}{\text{F}^2} 4. (2.99792 \times 10^8 - 25.1327 \text{ F} - 2.99792 \times 10^8 \text{ m}) \\
& \quad \left. \left. (-5.65095 \times 10^9 + 236.871 \text{ F} + 5.65095 \times 10^9 \text{ m}) \right) \right) \Big) \Big) / \\
& \left( \sqrt{\left( \frac{0.25 (2.99792 \times 10^8 - 25.1327 \text{ F} - 2.99792 \times 10^8 \text{ m})^2}{\text{F}^2} - \right. \right. \\
& \quad \frac{1. (-5.65095 \times 10^9 + 236.871 \text{ F} + 5.65095 \times 10^9 \text{ m})}{\text{F}} + \\
& \quad \frac{1}{\text{F}} 2.45695 \times 10^{-29} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \\
& \quad (0.547258 (-2.66941 \times 10^{31} + 2.43558 \times 10^{24} \text{ F} + 1. \text{ F}^2 + \\
& \quad \left. 5.33882 \times 10^{31} \text{ m} - 2.43558 \times 10^{24} \text{ F m} - 2.66941 \times 10^{31} \text{ m}^2) \right) \Big) \Big) / \\
& \left( \text{F} \left( 3.66307 \times 10^{29} \text{ F} (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m})^2 - \right. \right.
\end{aligned}$$





$$\begin{aligned}
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right)^2 \Big)^{1/3} \Big) + \\
& \frac{1}{F} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \\
& \left. 4.81708 \times 10^{38} m \right) \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \\
& \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right)^2 \right) \right)^{1/3} \Big) + \\
& 0.5 \sqrt{\left( \frac{0.5 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right.} \\
& \left. \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} - \right. \\
& \frac{1}{F} \\
& 2.45695 \times
\end{aligned}$$

$$\begin{aligned}
& 10^{-29} \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \\
& 7.66662 \times 10^{37} m) - \\
& (0.547258 (-2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + 5.33882 \times 10^{31} m - \\
& 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2)) / \\
& \left( F \left( 3.66307 \times 10^{29} F (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m)^2 - \right. \right. \\
& 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m) \\
& (4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m) \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) + 2. \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m)^3 + 27. \\
& (4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m)^2 \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m) - 9.7682 \times 10^{29} \\
& F (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m) + \\
& \sqrt{(-4. (-4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \\
& 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2))^3 + \\
& (3.66307 \times 10^{29} F (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m)^2 - \\
& 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m) \\
& (4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m) \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) + \\
& 2. (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m)^3 + \\
& 27. (4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m)^2 \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m) - 9.7682 \times \\
& 10^{29} F (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m))^2 \Big)^{1/3} \Big) - \\
& \frac{1}{F} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} F (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \\
& 4.81708 \times 10^{38} m)^2 - 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \\
& 4.81708 \times 10^{38} m) (4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m) \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) + \\
& 2. (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m)^3 + \\
& 27. (4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m)^2 \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m) - \\
& 9.7682 \times 10^{29} F (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m) \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m) + \\
& \left. \sqrt{(-4. (-4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& 9.43837 \times 10^{59} \text{ m} - 4.30581 \times 10^{52} \text{ F m} - 4.71919 \times 10^{59} \text{ m}^2)^3 + \\
& (3.66307 \times 10^{29} \text{ F} (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m})^2 - \\
& 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m}) \\
& (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \\
& 2. (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \\
& 27. (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - 9.7682 \times \\
& 10^{29} \text{ F} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m})^2)^{1/3} - \\
& \left( 0.25 \left( - \frac{8. (3.5506 \times 10^{10} - 992.201 \text{ F} - 3.5506 \times 10^{10} \text{ m})}{\text{F}} - \right. \right. \\
& \frac{1. (2.99792 \times 10^8 - 25.1327 \text{ F} - 2.99792 \times 10^8 \text{ m})^3}{\text{F}^3} + \\
& \frac{1}{\text{F}^2} 4. (2.99792 \times 10^8 - 25.1327 \text{ F} - 2.99792 \times 10^8 \text{ m}) \\
& \left. \left. (-5.65095 \times 10^9 + 236.871 \text{ F} + 5.65095 \times 10^9 \text{ m}) \right) \right) \Bigg/ \\
& \left( \sqrt[3]{\left( \frac{0.25 (2.99792 \times 10^8 - 25.1327 \text{ F} - 2.99792 \times 10^8 \text{ m})^2}{\text{F}^2} - \right. \right. \\
& \frac{1. (-5.65095 \times 10^9 + 236.871 \text{ F} + 5.65095 \times 10^9 \text{ m})}{\text{F}} + \\
& \frac{1}{\text{F}} 2.45695 \times 10^{-29} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \\
& (0.547258 (-2.66941 \times 10^{31} + 2.43558 \times 10^{24} \text{ F} + 1. \text{ F}^2 + \\
& 5.33882 \times 10^{31} \text{ m} - 2.43558 \times 10^{24} \text{ F m} - 2.66941 \times 10^{31} \text{ m}^2)) \Bigg/ \\
& \left( \text{F} \left( 3.66307 \times 10^{29} \text{ F} (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m})^2 - \right. \right. \\
& 9. (4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m}) \\
& (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m}) \\
& (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) + \\
& 2. (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m})^3 + \\
& 27. (4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m})^2 \\
& (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) - \\
& 9.7682 \times 10^{29} \text{ F} (-7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m}) \\
& \left. \left. (-1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m}) + \right. \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(-4. \left(-4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right.\right. \\
& \quad \left.9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2\right)^3 + \\
& \quad \left(3.66307 \times 10^{29} F \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right.\right. \\
& \quad \left.4.81708 \times 10^{38} m\right)^2 - 9. \left(4.81708 \times 10^{38} - \right. \\
& \quad \left.1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right) \\
& \quad \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right) \\
& \quad \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) + \\
& \quad 2. \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right)^3 + \\
& \quad 27. \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right)^2 \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) - \\
& \quad 9.7682 \times 10^{29} F \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \\
& \quad \left.7.66662 \times 10^{37} m\right) \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + \right. \\
& \quad \left.1.00889 \times 10^{39} m\right)^2 \Big)^{1/3} \Big) + \frac{1}{F} 1.95008 \times 10^{-29} \\
& \left(3.66307 \times 10^{29} F \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right)^2 - \right. \\
& \quad 9. \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right) \\
& \quad \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right) \\
& \quad \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) + \\
& \quad 2. \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right)^3 + \\
& \quad 27. \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right)^2 \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) - \\
& \quad 9.7682 \times 10^{29} F \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) + \\
& \quad \sqrt{\left(-4. \left(-4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right.\right. \\
& \quad \left.9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2\right)^3 + \\
& \quad \left(3.66307 \times 10^{29} F \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right.\right. \\
& \quad \left.4.81708 \times 10^{38} m\right)^2 - 9. \\
& \quad \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right) \\
& \quad \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right) \\
& \quad \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) + \\
& \quad 2. \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right)^3 + \\
& \quad 27. \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right)^2 \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) - \\
& \quad 9.7682 \times 10^{29} F \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \\
& \quad \left.7.66662 \times 10^{37} m\right) \left(-1.00889 \times 10^{39} + \right.
\end{aligned}$$



$$2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m) )^2))^{1/3})\Bigg)\Bigg),$$

$$\begin{aligned} & \left\{ \theta \rightarrow - \frac{0.25 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)}{F} + \right. \\ & 0.5 \\ & \sqrt{\left( \frac{0.25 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right.} \\ & \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} + \\ & \frac{1}{F} \\ & 2.45695 \times 10^{-29} \\ & \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \\ & \left. 7.66662 \times 10^{37} m \right) + \\ & \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + 5.33882 \times 10^{31} m - \right. \right. \\ & \left. \left. 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) \Big/ \\ & \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right. \\ & 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\ & \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\ & \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + 2. \\ & \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + 27. \\ & \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\ & \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times 10^{29} \\ & F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\ & \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\ & \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\ & \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\ & \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\ & 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\ & \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\ & \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\ & 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\ & 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\ & \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\ & \left. \left. 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \Big)^2 \Big)^{1/3} \Big) + \\
& \frac{1}{F} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \\
& \quad \left. 4.81708 \times 10^{38} m \right) \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& \quad 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \quad \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\
& \quad \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& \quad \left. 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \right. \\
& \quad \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \Big)^2 \Big)^{1/3} \Big) - \\
& 0.5 \sqrt{\left( \frac{0.5 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right.} \\
& \quad \left. \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} - \right. \\
& \quad \frac{1}{F} \\
& \quad 2.45695 \times \\
& \quad \quad 10^{-29} \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \\
& \quad \quad \left. 7.66662 \times 10^{37} m \right) - \\
& \quad \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + 5.33882 \times 10^{31} m - \right. \right. \\
& \quad \quad \left. \left. 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) / \\
& \quad \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + 2. \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + 27. \\
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times 10^{29} \\
& F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\
& \quad \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& \quad 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left. \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \right)^2 \right) \right)^{1/3} \right) - \\
& \frac{1}{F} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \left. \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \left. \left. 4.81708 \times 10^{38} m \right) \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \right. \\
& \quad \left. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \right. \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& \quad 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \right. \right. \\
& \quad \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\
& \quad \left. \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 +
\end{aligned}$$

$$\begin{aligned}
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \right)^{1/3} + \\
& \left( 0.25 \left( - \frac{8. \left( 3.5506 \times 10^{10} - 992.201 F - 3.5506 \times 10^{10} m \right)}{F} - \right. \right. \\
& \frac{1. \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^3}{F^3} + \\
& \frac{1}{F^2} 4. \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right) \\
& \left. \left. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right) \right) \right) \Bigg/ \\
& \left( \sqrt[3]{\left( \frac{0.25 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right. \right. \\
& \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} + \\
& \frac{1}{F} 2.45695 \times 10^{-29} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + \right. \right. \\
& \left. \left. 5.33882 \times 10^{31} m - 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) \Bigg/ \\
& \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right. \\
& 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \sqrt[3]{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right) \right)^3 + \\
& \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \left. \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - \right. \right. \\
& \left. \left. 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \right. \\
& \left. \left. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \right) \right)
\end{aligned}$$



$$\begin{aligned}
& \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} + \\
& \frac{1}{F} \\
& 2.45695 \times 10^{-29} \times \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + 5.33882 \times 10^{31} m - \right. \right. \\
& \quad \left. \left. 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) / \\
& \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + 2. \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + 27. \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times 10^{29} \\
& \quad F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \quad \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\
& \quad \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& \quad 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \right)^2 \right)^{1/3} \right) + \\
& \frac{1}{F} 1.95008 \times 10^{-29} \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \left. \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \left. \left. 4.81708 \times 10^{38} m \right) \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \right. \\
& \quad \left. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \right. \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad \left. \left. 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right)^3 + \right. \\
& \quad \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& \quad 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& \quad 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times \\
& \quad 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left. \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) \right)^2 \right) \right)^{1/3} \Bigg) + \\
& 0.5 \sqrt{\left( \frac{0.5 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right. \\
& \quad \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} - \\
& \quad \frac{1}{F} \\
& \quad 2.45695 \times \\
& \quad 10^{-29} \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \\
& \quad \quad \left. 7.66662 \times 10^{37} m \right) - \\
& \quad \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + 5.33882 \times 10^{31} m - \right. \right. \\
& \quad \quad \left. \left. 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) \Bigg) / \\
& \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right. \\
& \quad 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + 2. \\
& \quad \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + 27. \\
& \quad \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \quad \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - 9.7682 \times 10^{29} \\
& \quad F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \quad \left. \left. \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(-4. \left(-4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \quad \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2\right)^3 + \\
& \quad \left(3.66307 \times 10^{29} F \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right)^2 - \right. \\
& \quad 9. \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right) \\
& \quad \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right) \\
& \quad \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) + \\
& \quad 2. \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right)^3 + \\
& \quad 27. \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right)^2 \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) - 9.7682 \times \\
& \quad 10^{29} F \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) \\
& \quad \left. \left. \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right)\right)^2\right)^{1/3}} - \\
& \frac{1}{F} 1.95008 \times 10^{-29} \left(3.66307 \times 10^{29} F \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \quad \left. 4.81708 \times 10^{38} m\right)^2 - 9. \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \\
& \quad \left. 4.81708 \times 10^{38} m\right) \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right) \\
& \quad \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) + \\
& \quad 2. \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right)^3 + \\
& \quad 27. \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right)^2 \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) - \\
& \quad 9.7682 \times 10^{29} F \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) \\
& \quad \left. \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) + \right. \\
& \quad \left. \sqrt{\left(-4. \left(-4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \right. \\
& \quad \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2\right)^3 + \\
& \quad \left(3.66307 \times 10^{29} F \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right)^2 - \right. \\
& \quad 9. \left(4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m\right) \\
& \quad \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right) \\
& \quad \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) + \\
& \quad 2. \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right)^3 + \\
& \quad 27. \left(4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m\right)^2 \\
& \quad \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right) - 9.7682 \times \\
& \quad 10^{29} F \left(-7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m\right) \\
& \quad \left. \left. \left(-1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m\right)\right)^2\right)^{1/3}} + \\
& \left(0.25 \left(-\frac{8. \left(3.5506 \times 10^{10} - 992.201 F - 3.5506 \times 10^{10} m\right)}{F} - \right.\right.
\end{aligned}$$



$$\begin{aligned}
& \frac{1. \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^3}{F^3} + \\
& \frac{1}{F^2} 4. \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right) \\
& \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right) \Bigg) \Bigg) / \\
& \left( \sqrt{\left( \frac{0.25 \left( 2.99792 \times 10^8 - 25.1327 F - 2.99792 \times 10^8 m \right)^2}{F^2} - \right.} \right. \\
& \left. \frac{1. \left( -5.65095 \times 10^9 + 236.871 F + 5.65095 \times 10^9 m \right)}{F} + \right. \\
& \left. \frac{1}{F} 2.45695 \times 10^{-29} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \right. \\
& \left. \left( 0.547258 \left( -2.66941 \times 10^{31} + 2.43558 \times 10^{24} F + 1. F^2 + \right. \right. \right. \\
& \left. \left. \left. 5.33882 \times 10^{31} m - 2.43558 \times 10^{24} F m - 2.66941 \times 10^{31} m^2 \right) \right) \right) / \\
& \left( F \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right)^2 - \right. \right. \\
& 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \\
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) + \\
& \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} F + 1.76788 \times 10^{28} F^2 + \right. \right. \\
& \left. \left. 9.43837 \times 10^{59} m - 4.30581 \times 10^{52} F m - 4.71919 \times 10^{59} m^2 \right) \right)^3 + \\
& \left( 3.66307 \times 10^{29} F \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} F - \right. \right. \\
& \left. \left. 4.81708 \times 10^{38} m \right)^2 - 9. \left( 4.81708 \times 10^{38} - \right. \right. \\
& \left. \left. 1.34611 \times 10^{31} F - 4.81708 \times 10^{38} m \right) \right. \\
& \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right) \\
& \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right) + \\
& 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + 7.66662 \times 10^{37} m \right)^3 + \\
& 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} F - 4.06727 \times 10^{36} m \right)^2 \\
& \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + 1.00889 \times 10^{39} m \right) - \\
& 9.7682 \times 10^{29} F \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} F + \right. \\
& \left. 7.66662 \times 10^{37} m \right) \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} F + \right.
\end{aligned}$$

$$\begin{aligned} & \left( 3.66307 \times 10^{29} \text{ F} \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m} \right)^2 - \right. \\ & 9. \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m} \right) \\ & \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m} \right) \\ & \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m} \right) + \\ & 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m} \right)^3 + \\ & 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m} \right)^2 \\ & \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m} \right) - \\ & 9.7682 \times 10^{29} \text{ F} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m} \right) \\ & \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m} \right) + \\ & \sqrt{\left( -4. \left( -4.71919 \times 10^{59} + 4.30581 \times 10^{52} \text{ F} + 1.76788 \times 10^{28} \text{ F}^2 + \right. \right. \\ & \left. \left. 9.43837 \times 10^{59} \text{ m} - 4.30581 \times 10^{52} \text{ F m} - 4.71919 \times 10^{59} \text{ m}^2 \right)^3 + \right. \\ & \left. \left( 3.66307 \times 10^{29} \text{ F} \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - \right. \right. \right. \\ & \left. \left. 4.81708 \times 10^{38} \text{ m} \right)^2 - 9. \right. \\ & \left( 4.81708 \times 10^{38} - 1.34611 \times 10^{31} \text{ F} - 4.81708 \times 10^{38} \text{ m} \right) \\ & \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m} \right) \\ & \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m} \right) + \\ & 2. \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + 7.66662 \times 10^{37} \text{ m} \right)^3 + \\ & 27. \left( 4.06727 \times 10^{36} - 3.40974 \times 10^{29} \text{ F} - 4.06727 \times 10^{36} \text{ m} \right)^2 \\ & \left( -1.00889 \times 10^{39} + 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m} \right) - \\ & 9.7682 \times 10^{29} \text{ F} \left( -7.66662 \times 10^{37} + 3.21361 \times 10^{30} \text{ F} + \right. \\ & \left. 7.66662 \times 10^{37} \text{ m} \right) \left( -1.00889 \times 10^{39} + \right. \\ & \left. \left. 2.11447 \times 10^{31} \text{ F} + 1.00889 \times 10^{39} \text{ m} \right)^2 \right)^{1/3} \Bigg) \Bigg) \Bigg) \Bigg\} \Bigg\} \Bigg\} \\ \text{Plot3D} \Bigg[ & - \frac{0.25 \left( (2.99792458 \times 10^8 - 25.132741228718345 \text{ F} - 2.99792458 \times 10^8 \text{ m}) \right)}{\text{F}} + \\ & 0.5 \sqrt{\left( \frac{1}{\text{F}^2} 0.25 \left( (2.99792458 \times 10^8 - 25.132741228718345 \text{ F} - 2.99792458 \times 10^8 \text{ m})^2 - \frac{1}{\text{F}} \right. \right. \\ & 1. \left( -5.650954701926559 \times 10^9 + 236.8705056261446 \text{ F} + 5.650954701926559 \times 10^9 \text{ m} \right) + \\ & \frac{1}{\text{F}} 2.4569527253904567 \times 10^{-29} \left( -7.666617057149543 \times 10^{37} + \right. \\ & 3.2136082388873443 \times 10^{30} \text{ F} + 7.666617057149543 \times 10^{37} \text{ m} \right) + \\ & \left( 0.5472575866507531 \left( -2.6694115421499734 \times 10^{31} + \right. \right. \\ & 2.4355817514735585 \times 10^{24} \text{ F} + 1. \text{ F}^2 + 5.338823084299947 \times 10^{31} \text{ m} - \\ & \left. \left. 2.4355817514735585 \times 10^{24} \text{ F m} - 2.6694115421499734 \times 10^{31} \text{ m}^2 \right) \right) \Bigg) \Bigg] \Bigg] \end{aligned}$$

$$\begin{aligned}
& \left( F \left( 3.663074143426886 \cdot F^{29} (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} \right. \right. \\
& \quad \left. \left. F - 4.817077564925441 \cdot F^{38} m)^2 - 9 \cdot (4.817077564925441 \cdot F^{38} - \right. \right. \\
& \quad \left. \left. 1.346113071307215 \cdot F^{31} F - 4.817077564925441 \cdot F^{38} m) \right. \right. \\
& \quad (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} F - \\
& \quad \left. 4.0672666714599653 \cdot F^{36} m) (-7.666617057149543 \cdot F^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot F^{30} F + 7.666617057149543 \cdot F^{37} m) + \right. \\
& \quad 2 \cdot (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} F + \\
& \quad \left. 7.666617057149543 \cdot F^{37} m)^3 + 27 \cdot (4.0672666714599653 \cdot F^{36} - \right. \\
& \quad \left. 3.409744242531742 \cdot F^{29} F - 4.0672666714599653 \cdot F^{36} m)^2 \right. \\
& \quad \left. (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} F + \right. \\
& \quad \left. 1.0088863659827983 \cdot F^{39} m) - 9.768197715805029 \cdot F^{29} \right. \\
& \quad \left. F (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} F + \right. \\
& \quad \left. 7.666617057149543 \cdot F^{37} m) (-1.0088863659827983 \cdot F^{39} + \right. \\
& \quad \left. 2.11446946785997 \cdot F^{31} F + 1.0088863659827983 \cdot F^{39} m) + \right. \\
& \quad \left. \sqrt{-4 \cdot (-4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} F + \right. \right. \\
& \quad \left. \left. 1.7678754250530559 \cdot F^{28} F^2 + 9.438374129439836 \cdot F^{59} m - \right. \right. \\
& \quad \left. \left. 4.3058051241377837 \cdot F^{52} F m - 4.719187064719918 \cdot F^{59} m^2) \right)^3 + \right. \\
& \quad \left. (3.663074143426886 \cdot F^{29} F (4.817077564925441 \cdot F^{38} - \right. \right. \\
& \quad \left. \left. 1.346113071307215 \cdot F^{31} F - 4.817077564925441 \cdot F^{38} m)^2 - \right. \right. \\
& \quad \left. \left. 9 \cdot (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} F - \right. \right. \\
& \quad \left. \left. 4.817077564925441 \cdot F^{38} m) (4.0672666714599653 \cdot F^{36} - \right. \right. \\
& \quad \left. \left. 3.409744242531742 \cdot F^{29} F - 4.0672666714599653 \cdot F^{36} m) \right. \right. \\
& \quad \left. \left. (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} F + \right. \right. \\
& \quad \left. \left. 7.666617057149543 \cdot F^{37} m) + 2 \cdot (-7.666617057149543 \cdot F^{37} + \right. \right. \\
& \quad \left. \left. 3.2136082388873443 \cdot F^{30} F + 7.666617057149543 \cdot F^{37} m)^3 + \right. \right. \\
& \quad \left. \left. 27 \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} F - \right. \right. \\
& \quad \left. \left. 4.0672666714599653 \cdot F^{36} m)^2 (-1.0088863659827983 \cdot F^{39} + \right. \right. \\
& \quad \left. \left. 2.11446946785997 \cdot F^{31} F + 1.0088863659827983 \cdot F^{39} m) - \right. \right. \\
& \quad \left. \left. 9.768197715805029 \cdot F^{29} F (-7.666617057149543 \cdot F^{37} + \right. \right. \\
& \quad \left. \left. 3.2136082388873443 \cdot F^{30} F + 7.666617057149543 \cdot F^{37} m) \right. \right. \\
& \quad \left. \left. (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} F + \right. \right. \\
& \quad \left. \left. 1.0088863659827983 \cdot F^{39} m) \right)^2 \right)^{1/3} \Bigg) + \\
& \frac{1}{F} 1.9500846704604729 \cdot F^{-29} \left( 3.663074143426886 \cdot F^{29} F (4.817077564925441 \cdot F^{38} - \right. \\
& \quad \left. 1.346113071307215 \cdot F^{31} F - 4.817077564925441 \cdot F^{38} m)^2 - \right. \\
& \quad \left. 9 \cdot (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} F - \right. \\
& \quad \left. 4.817077564925441 \cdot F^{38} m) (4.0672666714599653 \cdot F^{36} - \right. \\
& \quad \left. 3.409744242531742 \cdot F^{29} F - 4.0672666714599653 \cdot F^{36} m) \right. \\
& \quad \left. (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} F + \right. \\
& \quad \left. 7.666617057149543 \cdot F^{37} m) + 2 \cdot (-7.666617057149543 \cdot F^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot F^{30} F + 7.666617057149543 \cdot F^{37} m)^3 + \right. \\
& \quad \left. 27 \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} F - \right.
\end{aligned}$$

$$\begin{aligned}
& 4.0672666714599653 \cdot m^{36} (-1.0088863659827983 \cdot F^{39} + \\
& 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot m^{39}) - \\
& 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37}) \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& 1.0088863659827983 \cdot m^{39}) + \\
& \sqrt{(-4 \cdot (-4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} + \\
& 1.7678754250530559 \cdot F^{28} + 9.438374129439836 \cdot m^{59} - \\
& 4.3058051241377837 \cdot F^{52} m - 4.719187064719918 \cdot m^{59})^3 + \\
& (3.663074143426886 \cdot F^{29} (4.817077564925441 \cdot F^{38} - \\
& 1.346113071307215 \cdot F^{31} - 4.817077564925441 \cdot m^{38})^2 - \\
& 9 \cdot (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& 4.817077564925441 \cdot m^{38}) (4.0672666714599653 \cdot F^{36} - \\
& 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot m^{36}) \\
& (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} + \\
& 7.666617057149543 \cdot m^{37}) + 2 \cdot (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37})^3 + \\
& 27 \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \\
& 4.0672666714599653 \cdot m^{36})^2 (-1.0088863659827983 \cdot F^{39} + \\
& 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot m^{39}) - \\
& 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37}) \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& 1.0088863659827983 \cdot m^{39})^2)^{1/3}} - \\
& 0.5 \cdot \sqrt{\left( \frac{0.5 \cdot (2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot m^8)^2}{F^2} - \right.} \\
& \left. \frac{1}{F} \right. \\
& 1 \cdot \\
& (-5.650954701926559 \cdot F^9 + 236.8705056261446 \cdot F + \\
& 5.650954701926559 \cdot m^9) - \\
& \left. \frac{1}{F} \right. 2.4569527253904567 \cdot F^{-29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + \\
& 7.666617057149543 \cdot m^{37}) - \\
& (0.5472575866507531 \cdot (-2.6694115421499734 \cdot F^{31} + 2.4355817514735585 \cdot F^{24} + \\
& 1 \cdot F^2 + 5.338823084299947 \cdot F^{31} m - \\
& 2.4355817514735585 \cdot F^{24} m - 2.6694115421499734 \cdot F^{31} m^2)) \Big/ \\
& \left( F \left( 3.663074143426886 \cdot F^{29} (4.817077564925441 \cdot F^{38} - \right. \right. \\
& \left. \left. 1.346113071307215 \cdot F^{31} - 4.817077564925441 \cdot m^{38})^2 - \right. \right.
\end{aligned}$$

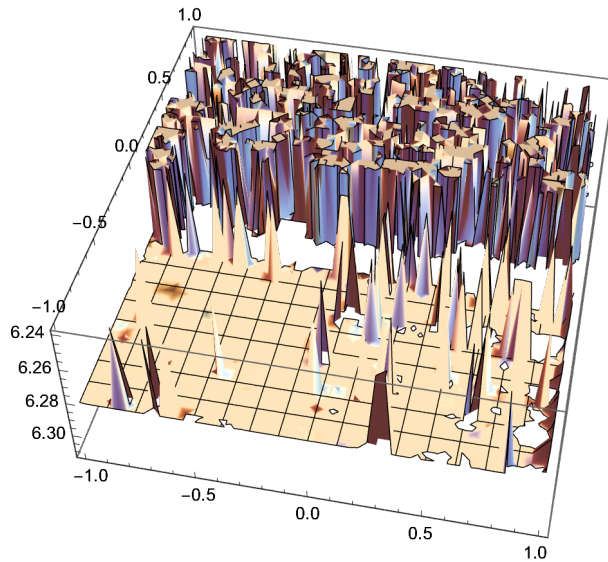
$$\begin{aligned}
& 9. \cdot (4.817077564925441 \cdot ^{\wedge}38 - 1.346113071307215 \cdot ^{\wedge}31 F - \\
& \quad 4.817077564925441 \cdot ^{\wedge}38 m) (4.0672666714599653 \cdot ^{\wedge}36 - \\
& \quad 3.409744242531742 \cdot ^{\wedge}29 F - 4.0672666714599653 \cdot ^{\wedge}36 m) \\
& \quad (-7.666617057149543 \cdot ^{\wedge}37 + 3.2136082388873443 \cdot ^{\wedge}30 F + \\
& \quad 7.666617057149543 \cdot ^{\wedge}37 m) + 2. \cdot (-7.666617057149543 \cdot ^{\wedge}37 + \\
& \quad 3.2136082388873443 \cdot ^{\wedge}30 F + 7.666617057149543 \cdot ^{\wedge}37 m)^3 + \\
& 27. \cdot (4.0672666714599653 \cdot ^{\wedge}36 - 3.409744242531742 \cdot ^{\wedge}29 F - \\
& \quad 4.0672666714599653 \cdot ^{\wedge}36 m)^2 (-1.0088863659827983 \cdot ^{\wedge}39 + \\
& \quad 2.11446946785997 \cdot ^{\wedge}31 F + 1.0088863659827983 \cdot ^{\wedge}39 m) - \\
& 9.768197715805029 \cdot ^{\wedge}29 F (-7.666617057149543 \cdot ^{\wedge}37 + \\
& \quad 3.2136082388873443 \cdot ^{\wedge}30 F + 7.666617057149543 \cdot ^{\wedge}37 m) \\
& \quad (-1.0088863659827983 \cdot ^{\wedge}39 + 2.11446946785997 \cdot ^{\wedge}31 F + \\
& \quad 1.0088863659827983 \cdot ^{\wedge}39 m) + \\
& \sqrt{(-4. \cdot (-4.719187064719918 \cdot ^{\wedge}59 + 4.3058051241377837 \cdot ^{\wedge}52 F + \\
& \quad 1.7678754250530559 \cdot ^{\wedge}28 F^2 + 9.438374129439836 \cdot ^{\wedge}59 m - \\
& \quad 4.3058051241377837 \cdot ^{\wedge}52 F m - 4.719187064719918 \cdot ^{\wedge}59 m^2)^3 + \\
& \quad (3.663074143426886 \cdot ^{\wedge}29 F (4.817077564925441 \cdot ^{\wedge}38 - \\
& \quad 1.346113071307215 \cdot ^{\wedge}31 F - 4.817077564925441 \cdot ^{\wedge}38 m)^2 - \\
& \quad 9. \cdot (4.817077564925441 \cdot ^{\wedge}38 - 1.346113071307215 \cdot ^{\wedge}31 F - \\
& \quad 4.817077564925441 \cdot ^{\wedge}38 m) (4.0672666714599653 \cdot ^{\wedge}36 - \\
& \quad 3.409744242531742 \cdot ^{\wedge}29 F - 4.0672666714599653 \cdot ^{\wedge}36 m) \\
& \quad (-7.666617057149543 \cdot ^{\wedge}37 + 3.2136082388873443 \cdot ^{\wedge}30 F + \\
& \quad 7.666617057149543 \cdot ^{\wedge}37 m) + 2. \cdot (-7.666617057149543 \cdot ^{\wedge}37 + \\
& \quad 3.2136082388873443 \cdot ^{\wedge}30 F + 7.666617057149543 \cdot ^{\wedge}37 m)^3 + \\
& \quad 27. \cdot (4.0672666714599653 \cdot ^{\wedge}36 - 3.409744242531742 \cdot ^{\wedge}29 F - \\
& \quad 4.0672666714599653 \cdot ^{\wedge}36 m)^2 (-1.0088863659827983 \cdot ^{\wedge}39 + \\
& \quad 2.11446946785997 \cdot ^{\wedge}31 F + 1.0088863659827983 \cdot ^{\wedge}39 m) - \\
& \quad 9.768197715805029 \cdot ^{\wedge}29 F (-7.666617057149543 \cdot ^{\wedge}37 + \\
& \quad 3.2136082388873443 \cdot ^{\wedge}30 F + 7.666617057149543 \cdot ^{\wedge}37 m) \\
& \quad (-1.0088863659827983 \cdot ^{\wedge}39 + 2.11446946785997 \cdot ^{\wedge}31 F + \\
& \quad 1.0088863659827983 \cdot ^{\wedge}39 m))^2)^{1/3}} - \\
& \frac{1}{F} 1.9500846704604729 \cdot ^{\wedge}-29 (3.663074143426886 \cdot ^{\wedge}29 F \\
& \quad (4.817077564925441 \cdot ^{\wedge}38 - 1.346113071307215 \cdot ^{\wedge}31 F - \\
& \quad 4.817077564925441 \cdot ^{\wedge}38 m)^2 - 9. \cdot (4.817077564925441 \cdot ^{\wedge}38 - \\
& \quad 1.346113071307215 \cdot ^{\wedge}31 F - 4.817077564925441 \cdot ^{\wedge}38 m) \\
& \quad (4.0672666714599653 \cdot ^{\wedge}36 - 3.409744242531742 \cdot ^{\wedge}29 F - \\
& \quad 4.0672666714599653 \cdot ^{\wedge}36 m) (-7.666617057149543 \cdot ^{\wedge}37 + \\
& \quad 3.2136082388873443 \cdot ^{\wedge}30 F + 7.666617057149543 \cdot ^{\wedge}37 m) + \\
& \quad 2. \cdot (-7.666617057149543 \cdot ^{\wedge}37 + 3.2136082388873443 \cdot ^{\wedge}30 F + \\
& \quad 7.666617057149543 \cdot ^{\wedge}37 m)^3 + \\
& \quad 27. \cdot (4.0672666714599653 \cdot ^{\wedge}36 - 3.409744242531742 \cdot ^{\wedge}29 F -
\end{aligned}$$

$$\begin{aligned}
& 4.0672666714599653 \cdot m^{36} \cdot (-1.0088863659827983 \cdot F^{39} + \\
& 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot m^{39}) - \\
& 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37}) \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& 1.0088863659827983 \cdot m^{39}) + \\
& \sqrt{\left( -4. \cdot (-4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} + \right. \\
& 1.7678754250530559 \cdot F^{28} + 9.438374129439836 \cdot m^{59} - \\
& 4.3058051241377837 \cdot F^{52} \cdot m - 4.719187064719918 \cdot m^{59})^3 + \\
& (3.663074143426886 \cdot F^{29} (4.817077564925441 \cdot F^{38} - \\
& 1.346113071307215 \cdot F^{31} - 4.817077564925441 \cdot m^{38})^2 - \\
& 9. \cdot (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& 4.817077564925441 \cdot m^{38}) (4.0672666714599653 \cdot F^{36} - \\
& 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot m^{36}) \\
& (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} + \\
& 7.666617057149543 \cdot m^{37}) + 2. \cdot (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37})^3 + \\
& 27. \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \\
& 4.0672666714599653 \cdot m^{36})^2 \cdot (-1.0088863659827983 \cdot F^{39} + \\
& 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot m^{39}) - \\
& 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37}) \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& 1.0088863659827983 \cdot m^{39}) \left. \right)^2 \Big)^{1/3} + \\
& \left( 0.25 \cdot \left( -\frac{1}{F} 8. \cdot (3.550599555468236 \cdot F^{10} - 992.2008537695941 \cdot F - \right. \right. \\
& \left. \left. 3.550599555468236 \cdot m^{10}) - \frac{1}{F^3} \right. \right. \\
& \left. \left. 1. \cdot (2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot m^8)^3 + \right. \right. \\
& \left. \left. \frac{1}{F^2} 4. \cdot (2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot m^8) \right. \right. \\
& \left. \left. (-5.650954701926559 \cdot F^9 + 236.8705056261446 \cdot F + \right. \right. \\
& \left. \left. 5.650954701926559 \cdot m^9) \right) \right) \Big) / \\
& \left( \sqrt{\left( \frac{1}{F^2} 0.25 \cdot (2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot m^8)^2 - \right. \right. \\
& \left. \left. \frac{1}{F} 1. \cdot (-5.650954701926559 \cdot F^9 + 236.8705056261446 \cdot \right. \right. \\
& \left. \left. F + 5.650954701926559 \cdot m^9) + \right. \right. \\
& \left. \left. \frac{1}{F} 2.4569527253904567 \cdot F^{-29} (-7.666617057149543 \cdot F^{37} + \right. \right. \\
& \left. \left. 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m^{37}) + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 0.5472575866507531 \cdot (-2.6694115421499734 \cdot F^{31} + \right. \\
& \quad 2.4355817514735585 \cdot F^{24} + 1 \cdot F^2 + 5.338823084299947 \cdot F^{31} m - \\
& \quad \left. 2.4355817514735585 \cdot F m - 2.6694115421499734 \cdot F^{31} m^2) \right) / \\
& \left( F \left( 3.663074143426886 \cdot F^{29} (4.817077564925441 \cdot F^{38} - \right. \right. \\
& \quad 1.346113071307215 \cdot F^{31} - 4.817077564925441 \cdot m)^2 - \\
& \quad 9 \cdot (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& \quad 4.817077564925441 \cdot m) (4.0672666714599653 \cdot F^{36} - \\
& \quad 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot m) \\
& \quad (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} + \\
& \quad 7.666617057149543 \cdot m) + 2 \cdot (-7.666617057149543 \cdot F^{37} + \\
& \quad 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m)^3 + \\
& \quad 27 \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \\
& \quad 4.0672666714599653 \cdot m)^2 (-1.0088863659827983 \cdot F^{39} + \\
& \quad 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot m) - \\
& \quad 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& \quad 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m) \\
& \quad (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& \quad 1.0088863659827983 \cdot m) + \\
& \quad \left. \sqrt{(-4 \cdot (-4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} + \right. \\
& \quad 1.7678754250530559 \cdot F^{28} + 9.438374129439836 \cdot m - \\
& \quad 4.3058051241377837 \cdot F m - 4.719187064719918 \cdot F^{59} \\
& \quad m^2)^3 + (3.663074143426886 \cdot F^{29} \\
& \quad (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& \quad 4.817077564925441 \cdot m)^2 - 9 \cdot \\
& \quad (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& \quad 4.817077564925441 \cdot m) (4.0672666714599653 \cdot F^{36} - \\
& \quad 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot m) \\
& \quad (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} \\
& \quad F + 7.666617057149543 \cdot m) + 2 \cdot \\
& \quad (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} \\
& \quad F + 7.666617057149543 \cdot m)^3 + 27 \cdot \\
& \quad (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} \\
& \quad F - 4.0672666714599653 \cdot m)^2 \\
& \quad (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} \\
& \quad F + 1.0088863659827983 \cdot m) - \\
& \quad 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& \quad 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot m) \\
& \quad (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} \\
& \quad F + 1.0088863659827983 \cdot m)^2 \Big)^{1/3} \Big) + \\
& \quad \frac{1}{F} 1.9500846704604729 \cdot F^{-29} (3.663074143426886 \cdot F^{29} F
\end{aligned}$$

$$\begin{aligned}
& (4.817077564925441 \cdot *^{38} - 1.346113071307215 \cdot *^{31} F - \\
& \quad 4.817077564925441 \cdot *^{38} m)^2 - 9 \cdot (4.817077564925441 \cdot *^{38} - \\
& \quad 1.346113071307215 \cdot *^{31} F - 4.817077564925441 \cdot *^{38} m) \\
& (4.0672666714599653 \cdot *^{36} - 3.409744242531742 \cdot *^{29} F - \\
& \quad 4.0672666714599653 \cdot *^{36} m) (-7.666617057149543 \cdot *^{37} + \\
& \quad 3.2136082388873443 \cdot *^{30} F + 7.666617057149543 \cdot *^{37} m) + \\
& 2 \cdot (-7.666617057149543 \cdot *^{37} + 3.2136082388873443 \cdot *^{30} F + \\
& \quad 7.666617057149543 \cdot *^{37} m)^3 + 27 \cdot (4.0672666714599653 \cdot *^{36} - \\
& \quad 3.409744242531742 \cdot *^{29} F - 4.0672666714599653 \cdot *^{36} m)^2 \\
& (-1.0088863659827983 \cdot *^{39} + 2.11446946785997 \cdot *^{31} F + \\
& \quad 1.0088863659827983 \cdot *^{39} m) - 9.768197715805029 \cdot *^{29} F \\
& (-7.666617057149543 \cdot *^{37} + 3.2136082388873443 \cdot *^{30} F + \\
& \quad 7.666617057149543 \cdot *^{37} m) (-1.0088863659827983 \cdot *^{39} + \\
& \quad 2.11446946785997 \cdot *^{31} F + 1.0088863659827983 \cdot *^{39} m) + \\
& \sqrt{\left( -4 \cdot (-4.719187064719918 \cdot *^{59} + 4.3058051241377837 \cdot *^{52} F + \right. \\
& \quad 1.7678754250530559 \cdot *^{28} F^2 + 9.438374129439836 \cdot *^{59} m - \\
& \quad \left. 4.3058051241377837 \cdot *^{52} F m - 4.719187064719918 \cdot *^{59} m^2 \right)^3 + \\
& \quad \left( 3.663074143426886 \cdot *^{29} F (4.817077564925441 \cdot *^{38} - \right. \\
& \quad \quad 1.346113071307215 \cdot *^{31} F - 4.817077564925441 \cdot *^{38} m)^2 - \\
& \quad 9 \cdot (4.817077564925441 \cdot *^{38} - 1.346113071307215 \cdot *^{31} \\
& \quad \quad F - 4.817077564925441 \cdot *^{38} m) \\
& \quad (4.0672666714599653 \cdot *^{36} - 3.409744242531742 \cdot *^{29} F - \\
& \quad \quad 4.0672666714599653 \cdot *^{36} m) (-7.666617057149543 \cdot *^{37} + \\
& \quad \quad 3.2136082388873443 \cdot *^{30} F + 7.666617057149543 \cdot *^{37} m) + \\
& \quad 2 \cdot (-7.666617057149543 \cdot *^{37} + 3.2136082388873443 \cdot *^{30} \\
& \quad \quad F + 7.666617057149543 \cdot *^{37} m)^3 + 27 \cdot \\
& \quad (4.0672666714599653 \cdot *^{36} - 3.409744242531742 \cdot *^{29} \\
& \quad \quad F - 4.0672666714599653 \cdot *^{36} m)^2 \\
& \quad (-1.0088863659827983 \cdot *^{39} + 2.11446946785997 \cdot *^{31} F + \\
& \quad \quad 1.0088863659827983 \cdot *^{39} m) - 9.768197715805029 \cdot *^{29} F \\
& \quad (-7.666617057149543 \cdot *^{37} + 3.2136082388873443 \cdot *^{30} F + \\
& \quad \quad 7.666617057149543 \cdot *^{37} m) (-1.0088863659827983 \cdot *^{39} + \\
& \quad \quad 2.11446946785997 \cdot *^{31} F + 1.0088863659827983 \cdot *^{39} \\
& \quad \quad m)^2 \Big)^{1/3} \Big) \Big) \Big) \Big) \Big), \{F, -1, 1\}, \{m, -1, 1\} \Big]
\end{aligned}$$





$$\begin{aligned}
 & \text{Plot3D}\left[-\frac{0.25 \cdot (2.99792458 \cdot 10^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot 10^8 \text{ m})}{F} + \right. \\
 & 0.5 \cdot \sqrt{\left(\frac{1}{F^2} 0.25 \cdot (2.99792458 \cdot 10^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot 10^8 \text{ m})^2 - \frac{1}{F} \right.} \\
 & 1. \cdot (-5.650954701926559 \cdot 10^9 + 236.8705056261446 \cdot F + 5.650954701926559 \cdot 10^9 \text{ m}) + \\
 & \frac{1}{F} 2.4569527253904567 \cdot 10^{-29} (-7.666617057149543 \cdot 10^{37} + \\
 & 3.2136082388873443 \cdot 10^{30} F + 7.666617057149543 \cdot 10^{37} \text{ m}) + \\
 & (0.5472575866507531 \cdot (-2.6694115421499734 \cdot 10^{31} + \\
 & 2.4355817514735585 \cdot 10^{24} F + 1. \cdot F^2 + 5.338823084299947 \cdot 10^{31} \text{ m} - \\
 & 2.4355817514735585 \cdot 10^{24} F \text{ m} - 2.6694115421499734 \cdot 10^{31} \text{ m}^2)) \Bigg) / \\
 & \left( F \left( 3.663074143426886 \cdot 10^{29} F (4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} \right. \right. \\
 & \quad F - 4.817077564925441 \cdot 10^{38} \text{ m})^2 - 9. \cdot (4.817077564925441 \cdot 10^{38} - \\
 & \quad 1.346113071307215 \cdot 10^{31} F - 4.817077564925441 \cdot 10^{38} \text{ m}) \\
 & \quad (4.0672666714599653 \cdot 10^{36} - 3.409744242531742 \cdot 10^{29} F - \\
 & \quad 4.0672666714599653 \cdot 10^{36} \text{ m}) (-7.666617057149543 \cdot 10^{37} + \\
 & \quad 3.2136082388873443 \cdot 10^{30} F + 7.666617057149543 \cdot 10^{37} \text{ m}) + \\
 & \quad 2. \cdot (-7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} F + \\
 & \quad 7.666617057149543 \cdot 10^{37} \text{ m})^3 + 27. \cdot (4.0672666714599653 \cdot 10^{36} - \\
 & \quad 3.409744242531742 \cdot 10^{29} F - 4.0672666714599653 \cdot 10^{36} \text{ m})^2 \\
 & \quad (-1.0088863659827983 \cdot 10^{39} + 2.11446946785997 \cdot 10^{31} F + \\
 & \quad 1.0088863659827983 \cdot 10^{39} \text{ m}) - 9.768197715805029 \cdot 10^{29} \\
 & \quad F (-7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} F + \\
 & \quad 7.666617057149543 \cdot 10^{37} \text{ m}) (-1.0088863659827983 \cdot 10^{39} + \\
 & \quad 2.11446946785997 \cdot 10^{31} F + 1.0088863659827983 \cdot 10^{39} \text{ m}) + \\
 & \quad \sqrt{(-4. \cdot (-4.719187064719918 \cdot 10^{59} + 4.3058051241377837 \cdot 10^{52} F + \\
 & \quad 1.7678754250530559 \cdot 10^{28} F^2 + 9.438374129439836 \cdot 10^{59} \text{ m} -
 \end{aligned}$$

$$\begin{aligned}
& 4.3058051241377837 \cdot 10^{52} \text{ F m} - 4.719187064719918 \cdot 10^{59} \text{ m}^2)^3 + \\
& (3.663074143426886 \cdot 10^{29} \text{ F} (4.817077564925441 \cdot 10^{38} - \\
& \quad 1.346113071307215 \cdot 10^{31} \text{ F} - 4.817077564925441 \cdot 10^{38} \text{ m})^2 - \\
& 9 \cdot (4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} \text{ F} - \\
& \quad 4.817077564925441 \cdot 10^{38} \text{ m}) (4.0672666714599653 \cdot 10^{36} - \\
& \quad 3.409744242531742 \cdot 10^{29} \text{ F} - 4.0672666714599653 \cdot 10^{36} \text{ m}) \\
& (-7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} \text{ F} + \\
& \quad 7.666617057149543 \cdot 10^{37} \text{ m}) + 2 \cdot (-7.666617057149543 \cdot 10^{37} + \\
& \quad 3.2136082388873443 \cdot 10^{30} \text{ F} + 7.666617057149543 \cdot 10^{37} \text{ m})^3 + \\
& 27 \cdot (4.0672666714599653 \cdot 10^{36} - 3.409744242531742 \cdot 10^{29} \text{ F} - \\
& \quad 4.0672666714599653 \cdot 10^{36} \text{ m})^2 (-1.0088863659827983 \cdot 10^{39} + \\
& \quad 2.11446946785997 \cdot 10^{31} \text{ F} + 1.0088863659827983 \cdot 10^{39} \text{ m}) - \\
& 9.768197715805029 \cdot 10^{29} \text{ F} (-7.666617057149543 \cdot 10^{37} + \\
& \quad 3.2136082388873443 \cdot 10^{30} \text{ F} + 7.666617057149543 \cdot 10^{37} \text{ m}) \\
& (-1.0088863659827983 \cdot 10^{39} + 2.11446946785997 \cdot 10^{31} \text{ F} + \\
& \quad 1.0088863659827983 \cdot 10^{39} \text{ m})^2)^{1/3} + \\
& \frac{1}{F} 1.9500846704604729 \cdot 10^{-29} (3.663074143426886 \cdot 10^{29} \text{ F} (4.817077564925441 \cdot 10^{38} - \\
& \quad 1.346113071307215 \cdot 10^{31} \text{ F} - 4.817077564925441 \cdot 10^{38} \text{ m})^2 - \\
& 9 \cdot (4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} \text{ F} - \\
& \quad 4.817077564925441 \cdot 10^{38} \text{ m}) (4.0672666714599653 \cdot 10^{36} - \\
& \quad 3.409744242531742 \cdot 10^{29} \text{ F} - 4.0672666714599653 \cdot 10^{36} \text{ m}) \\
& (-7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} \text{ F} + \\
& \quad 7.666617057149543 \cdot 10^{37} \text{ m}) + 2 \cdot (-7.666617057149543 \cdot 10^{37} + \\
& \quad 3.2136082388873443 \cdot 10^{30} \text{ F} + 7.666617057149543 \cdot 10^{37} \text{ m})^3 + \\
& 27 \cdot (4.0672666714599653 \cdot 10^{36} - 3.409744242531742 \cdot 10^{29} \text{ F} - \\
& \quad 4.0672666714599653 \cdot 10^{36} \text{ m})^2 (-1.0088863659827983 \cdot 10^{39} + \\
& \quad 2.11446946785997 \cdot 10^{31} \text{ F} + 1.0088863659827983 \cdot 10^{39} \text{ m}) - \\
& 9.768197715805029 \cdot 10^{29} \text{ F} (-7.666617057149543 \cdot 10^{37} + \\
& \quad 3.2136082388873443 \cdot 10^{30} \text{ F} + 7.666617057149543 \cdot 10^{37} \text{ m}) \\
& (-1.0088863659827983 \cdot 10^{39} + 2.11446946785997 \cdot 10^{31} \text{ F} + \\
& \quad 1.0088863659827983 \cdot 10^{39} \text{ m}) + \\
& \sqrt{(-4 \cdot (-4.719187064719918 \cdot 10^{59} + 4.3058051241377837 \cdot 10^{52} \text{ F} + \\
& \quad 1.7678754250530559 \cdot 10^{28} \text{ F}^2 + 9.438374129439836 \cdot 10^{59} \text{ m} - \\
& \quad 4.3058051241377837 \cdot 10^{52} \text{ F m} - 4.719187064719918 \cdot 10^{59} \text{ m}^2)^3 + \\
& (3.663074143426886 \cdot 10^{29} \text{ F} (4.817077564925441 \cdot 10^{38} - \\
& \quad 1.346113071307215 \cdot 10^{31} \text{ F} - 4.817077564925441 \cdot 10^{38} \text{ m})^2 - \\
& 9 \cdot (4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} \text{ F} - \\
& \quad 4.817077564925441 \cdot 10^{38} \text{ m}) (4.0672666714599653 \cdot 10^{36} - \\
& \quad 3.409744242531742 \cdot 10^{29} \text{ F} - 4.0672666714599653 \cdot 10^{36} \text{ m}) \\
& (-7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} \text{ F} + \\
& \quad 7.666617057149543 \cdot 10^{37} \text{ m}) + 2 \cdot (-7.666617057149543 \cdot 10^{37} +
\end{aligned}$$

$$\begin{aligned}
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \text{ m}^3 + \\
& 27 \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \\
& 4.0672666714599653 \cdot \text{m}^{36})^2 (-1.0088863659827983 \cdot F^{39} + \\
& 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot \text{m}^{39}) - \\
& 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \text{ m}) \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& 1.0088863659827983 \cdot \text{m}^{39})^2)^{1/3} + \\
& 0.5 \cdot \sqrt{\left( \frac{0.5 \cdot (2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot \text{m}^8)^2}{F^2} - \right.} \\
& \quad \frac{1}{F} \\
& \quad 1 \cdot \\
& \quad (-5.650954701926559 \cdot F^9 + 236.8705056261446 \cdot F + \\
& \quad 5.650954701926559 \cdot \text{m}^9) - \\
& \quad \frac{1}{F} 2.4569527253904567 \cdot F^{-29} (-7.666617057149543 \cdot F^{37} + \\
& \quad 3.2136082388873443 \cdot F^{30} + \\
& \quad 7.666617057149543 \cdot F^{37} \text{ m}) - \\
& \quad (0.5472575866507531 \cdot (-2.6694115421499734 \cdot F^{31} + 2.4355817514735585 \cdot F^{24} + \\
& \quad 1 \cdot F^2 + 5.338823084299947 \cdot \text{m}^{31} - \\
& \quad 2.4355817514735585 \cdot F \text{ m} - 2.6694115421499734 \cdot \text{m}^{31})^2) \Big/ \\
& \quad \left( F \left( 3.663074143426886 \cdot F^{29} (4.817077564925441 \cdot F^{38} - \right. \right. \\
& \quad 1.346113071307215 \cdot F^{31} - 4.817077564925441 \cdot F^{38} \text{ m})^2 - \\
& \quad 9 \cdot (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& \quad 4.817077564925441 \cdot \text{m}^{38}) (4.0672666714599653 \cdot F^{36} - \\
& \quad 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot \text{m}^{36}) \\
& \quad (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} + \\
& \quad 7.666617057149543 \cdot F^{37} \text{ m}) + 2 \cdot (-7.666617057149543 \cdot F^{37} + \\
& \quad 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \text{ m})^3 + \\
& \quad 27 \cdot (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \\
& \quad 4.0672666714599653 \cdot \text{m}^{36})^2 (-1.0088863659827983 \cdot F^{39} + \\
& \quad 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot \text{m}^{39}) - \\
& \quad 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& \quad 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \text{ m}) \\
& \quad (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& \quad 1.0088863659827983 \cdot \text{m}^{39}) + \\
& \quad \left. \sqrt{(-4 \cdot (-4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} + \right.} \\
& \quad 1.7678754250530559 \cdot F^{28} + 9.438374129439836 \cdot \text{m}^{59} - \\
& \quad 4.3058051241377837 \cdot F \text{ m} - 4.719187064719918 \cdot \text{m}^{59})^3 +
\end{aligned}$$

$$\begin{aligned}
& \left( 3.663074143426886 \cdot 10^{29} F \left( 4.817077564925441 \cdot 10^{38} - \right. \right. \\
& \quad 1.346113071307215 \cdot 10^{31} F - 4.817077564925441 \cdot 10^{38} m \Big)^2 - \\
& \quad 9. \cdot \left( 4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} F - \right. \\
& \quad \left. 4.817077564925441 \cdot 10^{38} m \right) \left( 4.0672666714599653 \cdot 10^{36} - \right. \\
& \quad \left. 3.409744242531742 \cdot 10^{29} F - 4.0672666714599653 \cdot 10^{36} m \right) \\
& \quad \left( -7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} F + \right. \\
& \quad \left. 7.666617057149543 \cdot 10^{37} m \right) + 2. \cdot \left( -7.666617057149543 \cdot 10^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot 10^{30} F + 7.666617057149543 \cdot 10^{37} m \right)^3 + \\
& \quad 27. \cdot \left( 4.0672666714599653 \cdot 10^{36} - 3.409744242531742 \cdot 10^{29} F - \right. \\
& \quad \left. 4.0672666714599653 \cdot 10^{36} m \right)^2 \left( -1.0088863659827983 \cdot 10^{39} + \right. \\
& \quad \left. 2.11446946785997 \cdot 10^{31} F + 1.0088863659827983 \cdot 10^{39} m \right) - \\
& \quad 9.768197715805029 \cdot 10^{29} F \left( -7.666617057149543 \cdot 10^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot 10^{30} F + 7.666617057149543 \cdot 10^{37} m \right) \\
& \quad \left( -1.0088863659827983 \cdot 10^{39} + 2.11446946785997 \cdot 10^{31} F + \right. \\
& \quad \left. 1.0088863659827983 \cdot 10^{39} m \right)^2 \Big)^{1/3} \Big) - \\
& \frac{1}{F} 1.9500846704604729 \cdot 10^{-29} \left( 3.663074143426886 \cdot 10^{29} F \right. \\
& \quad \left( 4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} F - \right. \\
& \quad \left. 4.817077564925441 \cdot 10^{38} m \right)^2 - 9. \cdot \left( 4.817077564925441 \cdot 10^{38} - \right. \\
& \quad \left. 1.346113071307215 \cdot 10^{31} F - 4.817077564925441 \cdot 10^{38} m \right) \\
& \quad \left( 4.0672666714599653 \cdot 10^{36} - 3.409744242531742 \cdot 10^{29} F - \right. \\
& \quad \left. 4.0672666714599653 \cdot 10^{36} m \right) \left( -7.666617057149543 \cdot 10^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot 10^{30} F + 7.666617057149543 \cdot 10^{37} m \right) + \\
& \quad 2. \cdot \left( -7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} F + \right. \\
& \quad \left. 7.666617057149543 \cdot 10^{37} m \right)^3 + \\
& \quad 27. \cdot \left( 4.0672666714599653 \cdot 10^{36} - 3.409744242531742 \cdot 10^{29} F - \right. \\
& \quad \left. 4.0672666714599653 \cdot 10^{36} m \right)^2 \left( -1.0088863659827983 \cdot 10^{39} + \right. \\
& \quad \left. 2.11446946785997 \cdot 10^{31} F + 1.0088863659827983 \cdot 10^{39} m \right) - \\
& \quad 9.768197715805029 \cdot 10^{29} F \left( -7.666617057149543 \cdot 10^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot 10^{30} F + 7.666617057149543 \cdot 10^{37} m \right) \\
& \quad \left( -1.0088863659827983 \cdot 10^{39} + 2.11446946785997 \cdot 10^{31} F + \right. \\
& \quad \left. 1.0088863659827983 \cdot 10^{39} m \right) + \\
& \quad \sqrt{\left( -4. \cdot \left( -4.719187064719918 \cdot 10^{59} + 4.3058051241377837 \cdot 10^{52} F + \right. \right. \\
& \quad \left. \left. 1.7678754250530559 \cdot 10^{28} F^2 + 9.438374129439836 \cdot 10^{59} m - \right. \right. \\
& \quad \left. \left. 4.3058051241377837 \cdot 10^{52} F m - 4.719187064719918 \cdot 10^{59} m^2 \right)^3 + \right. \\
& \quad \left. \left( 3.663074143426886 \cdot 10^{29} F \left( 4.817077564925441 \cdot 10^{38} - \right. \right. \right. \\
& \quad \left. \left. \left. 1.346113071307215 \cdot 10^{31} F - 4.817077564925441 \cdot 10^{38} m \right)^2 - \right. \right. \\
& \quad \left. \left. 9. \cdot \left( 4.817077564925441 \cdot 10^{38} - 1.346113071307215 \cdot 10^{31} F - \right. \right. \right. \\
& \quad \left. \left. \left. 4.817077564925441 \cdot 10^{38} m \right) \left( 4.0672666714599653 \cdot 10^{36} - \right. \right. \right. \\
& \quad \left. \left. \left. 3.409744242531742 \cdot 10^{29} F - 4.0672666714599653 \cdot 10^{36} m \right) \right. \right. \\
& \quad \left. \left. \left( -7.666617057149543 \cdot 10^{37} + 3.2136082388873443 \cdot 10^{30} F + \right. \right. \right. \\
& \quad \left. \left. \left. 7.666617057149543 \cdot 10^{37} m \right) + 2. \cdot \left( -7.666617057149543 \cdot 10^{37} + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \right)^3 + \\
& 27 \cdot \left( 4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \right. \\
& \quad \left. 4.0672666714599653 \cdot F^{36} \right)^2 \left( -1.0088863659827983 \cdot F^{39} + \right. \\
& \quad \left. 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot F^{39} \right) - \\
& 9.768197715805029 \cdot F^{29} \left( -7.666617057149543 \cdot F^{37} + \right. \\
& \quad \left. 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \right) \\
& \left. \left( -1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \right. \right. \\
& \quad \left. \left. 1.0088863659827983 \cdot F^{39} \right) \right)^{1/3} + \\
& \left( 0.25 \cdot \left( -\frac{1}{F} 8 \cdot \left( 3.550599555468236 \cdot F^{10} - 992.2008537695941 \cdot F - \right. \right. \right. \\
& \quad \left. \left. 3.550599555468236 \cdot F^{10} \right) - \frac{1}{F^3} \right. \\
& \quad \left. 1 \cdot \left( 2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot F^8 \right)^3 + \right. \\
& \quad \left. \frac{1}{F^2} 4 \cdot \left( 2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot F^8 \right) \right. \\
& \quad \left. \left( -5.650954701926559 \cdot F^9 + 236.8705056261446 \cdot F + \right. \right. \\
& \quad \left. \left. 5.650954701926559 \cdot F^9 \right) \right) \Bigg/ \\
& \left( \sqrt{\left( \frac{1}{F^2} 0.25 \cdot \left( 2.99792458 \cdot F^8 - 25.132741228718345 \cdot F - 2.99792458 \cdot F^8 \right)^2 - \right. \right. \\
& \quad \left. \frac{1}{F} 1 \cdot \left( -5.650954701926559 \cdot F^9 + 236.8705056261446 \cdot \right. \right. \\
& \quad \left. \left. F + 5.650954701926559 \cdot F^9 \right) + \right. \\
& \quad \left. \frac{1}{F} 2.4569527253904567 \cdot F^{-29} \left( -7.666617057149543 \cdot F^{37} + \right. \right. \\
& \quad \left. \left. 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \right) + \right. \\
& \quad \left. \left( 0.5472575866507531 \cdot \left( -2.6694115421499734 \cdot F^{31} + \right. \right. \right. \\
& \quad \left. \left. 2.4355817514735585 \cdot F^{24} + 1 \cdot F^2 + 5.338823084299947 \cdot F^{31} \right) - \right. \\
& \quad \left. \left. 2.4355817514735585 \cdot F^{24} - 2.6694115421499734 \cdot F^{31} \right) \right) \Bigg/ \\
& \left( F \left( 3.663074143426886 \cdot F^{29} \left( 4.817077564925441 \cdot F^{38} - \right. \right. \right. \\
& \quad \left. \left. 1.346113071307215 \cdot F^{31} - 4.817077564925441 \cdot F^{38} \right)^2 - \right. \\
& \quad \left. 9 \cdot \left( 4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \right. \right. \\
& \quad \left. \left. 4.817077564925441 \cdot F^{38} \right) \left( 4.0672666714599653 \cdot F^{36} - \right. \right. \\
& \quad \left. \left. 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot F^{36} \right) \right. \\
& \quad \left. \left( -7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} + \right. \right. \\
& \quad \left. \left. 7.666617057149543 \cdot F^{37} \right) + 2 \cdot \left( -7.666617057149543 \cdot F^{37} + \right. \right. \\
& \quad \left. \left. 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \right)^3 + \right. \\
& \quad \left. 27 \cdot \left( 4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} - \right. \right. \\
& \quad \left. \left. 4.0672666714599653 \cdot F^{36} \right)^2 \left( -1.0088863659827983 \cdot F^{39} + \right. \right. \\
& \quad \left. \left. 2.11446946785997 \cdot F^{31} + 1.0088863659827983 \cdot F^{39} \right) - \right. \\
& \quad \left. 9.768197715805029 \cdot F^{29} \left( -7.666617057149543 \cdot F^{37} + \right. \right. \\
& \quad \left. \left. 3.2136082388873443 \cdot F^{30} + 7.666617057149543 \cdot F^{37} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} + \\
& 1.0088863659827983 \cdot m^{39}) + \\
& \sqrt{\left( -4. \cdot \left( -4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} + \right. \right. \\
& 1.7678754250530559 \cdot F^{28} + 9.438374129439836 \cdot m^{59} - \\
& 4.3058051241377837 \cdot F^{52} m - 4.719187064719918 \cdot m^{59} \\
& \left. \left. m^2 \right)^3 + \left( 3.663074143426886 \cdot F^{29} + \right. \right. \\
& (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& 4.817077564925441 \cdot m^{38})^2 - 9. \cdot \\
& (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} - \\
& 4.817077564925441 \cdot m^{38}) (4.0672666714599653 \cdot F^{36} - \\
& 3.409744242531742 \cdot F^{29} - 4.0672666714599653 \cdot m^{36} - \\
& (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} \\
& F + 7.666617057149543 \cdot m^{37}) + 2. \cdot \\
& (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} \\
& F + 7.666617057149543 \cdot m^{37})^3 + 27. \cdot \\
& (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} \\
& F - 4.0672666714599653 \cdot m^{36})^2 \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} \\
& F + 1.0088863659827983 \cdot m^{39}) - \\
& 9.768197715805029 \cdot F^{29} (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} F + 7.666617057149543 \cdot m^{37}) \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} \\
& F + 1.0088863659827983 \cdot m^{39}) \Big)^{1/3} \Big) + \\
& \frac{1}{F} 1.9500846704604729 \cdot F^{-29} \left( 3.663074143426886 \cdot F^{29} + \right. \\
& (4.817077564925441 \cdot F^{38} - 1.346113071307215 \cdot F^{31} F - \\
& 4.817077564925441 \cdot m^{38})^2 - 9. \cdot (4.817077564925441 \cdot F^{38} - \\
& 1.346113071307215 \cdot F^{31} F - 4.817077564925441 \cdot m^{38}) \\
& (4.0672666714599653 \cdot F^{36} - 3.409744242531742 \cdot F^{29} F - \\
& 4.0672666714599653 \cdot m^{36}) (-7.666617057149543 \cdot F^{37} + \\
& 3.2136082388873443 \cdot F^{30} F + 7.666617057149543 \cdot m^{37}) + \\
& 2. \cdot (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} F + \\
& 7.666617057149543 \cdot m^{37})^3 + 27. \cdot (4.0672666714599653 \cdot F^{36} - \\
& 3.409744242531742 \cdot F^{29} F - 4.0672666714599653 \cdot m^{36})^2 \\
& (-1.0088863659827983 \cdot F^{39} + 2.11446946785997 \cdot F^{31} F + \\
& 1.0088863659827983 \cdot m^{39}) - 9.768197715805029 \cdot F^{29} F \\
& (-7.666617057149543 \cdot F^{37} + 3.2136082388873443 \cdot F^{30} F + \\
& 7.666617057149543 \cdot m^{37}) (-1.0088863659827983 \cdot F^{39} + \\
& 2.11446946785997 \cdot F^{31} F + 1.0088863659827983 \cdot m^{39}) + \\
& \sqrt{\left( -4. \cdot \left( -4.719187064719918 \cdot F^{59} + 4.3058051241377837 \cdot F^{52} + \right. \right. \\
& 1.7678754250530559 \cdot F^{28} + 9.438374129439836 \cdot m^{59} - \\
& 4.3058051241377837 \cdot F^{52} m - 4.719187064719918 \cdot m^{59} m^2 \Big)^3 +
\end{aligned}$$



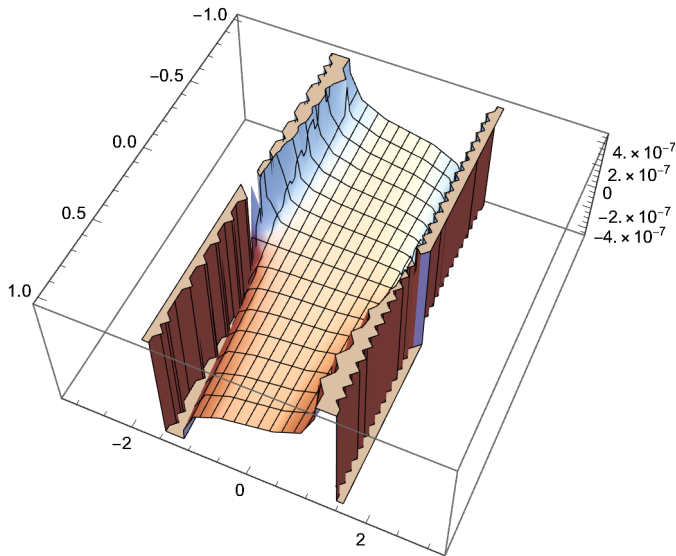
$$\begin{aligned}
& \int (2 \pi) \\
& \left( m \left( \left( -1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \right) \right) / \right. \\
& \quad \left( 2 \sqrt{\left( 39.47841760435743 - 12.566370614359172 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \\
& \quad \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - \right.} \\
& \quad \left. 1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \right. \\
& \quad \left. 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \left. \right) - \\
& \quad \left( \left( -12.566370614359172 + 2 \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \right) \\
& \quad \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - \right.} \\
& \quad \left. 1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \right. \\
& \quad \left. 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \left. \right) / \\
& \quad \left( 2 \left( 39.47841760435743 - 12.566370614359172 \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \right. \right. \\
& \quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right)^{3/2} \right) \left. \right) \right) d\beta \\
& m \left( -2.16301 \times 10^{-8} \sqrt{\cos[\beta]^2} \left( \log[1. - 1. \tan[0.5 \beta]] - 1. \log[1. + \tan[0.5 \beta]] \right) \sec[\beta] + \right. \\
& \quad 0.125 \sqrt{1. + \cos[2. \beta]} \sec[\beta]^5 \left( (0. + 0. i) \cos[\beta] + 5.16921 \times 10^{-18} \sin[\beta] \right) \\
& \quad \frac{\sqrt{39.4784 + 39.4784 \cos[2. \beta] + (0. + 0. i) \sin[2. \beta]}}{\sqrt{3.54814 \times 10^{18} + 3.54814 \times 10^{18} \cos[2. \beta] + (0. + 0. i) \sin[2. \beta]}} + \\
& \quad \frac{\sqrt{39.4784 + 39.4784 \cos[2. \beta] + (0. + 0. i) \sin[2. \beta]}}{\sqrt{3.54814 \times 10^{18} + 3.54814 \times 10^{18} \cos[2. \beta] + (0. + 0. i) \sin[2. \beta]}} \\
& \quad \left( \sec[\beta]^4 \left( (0. + 0. i) + 6.09197 \times 10^{-19} \tan[\beta] \right) + \right. \\
& \quad \left. \sec[\beta]^2 \left( (0. + 0. i) + 1.21839 \times 10^{-18} \tan[\beta] \right) \right) \left. \right)
\end{aligned}$$



```

Plot3D[m (-2.1630149725479812`*^-8 Sqrt[Cos[beta]^2]
(Log[1.`-1.`Tan[0.5`beta]]-1.`Log[1.`+Tan[0.5`beta]]) Sec[beta]+0.125`
Sqrt[1.`+Cos[2.`beta]] Sec[beta]^5 ((0.`+0.`I) Cos[beta]+5.169208853894573`*^-18 Sin[beta])
Sqrt[(39.47841760435743`+39.47841760435743`Cos[2.`beta]+(0.`+0.`I) Sin[2.`beta])
Sqrt[(3.5481432270250993`*^18+
3.5481432270250993`*^18 Cos[2.`beta]+(0.`+0.`I) Sin[2.`beta])+
Sqrt[(39.47841760435743`+39.47841760435743`Cos[2.`beta]+(0.`+0.`I) Sin[2.`beta])
Sqrt[(3.5481432270250993`*^18+
3.5481432270250993`*^18 Cos[2.`beta]+(0.`+0.`I) Sin[2.`beta])
(Sec[beta]^4 ((0.`+0.`I)+6.091971056597322`*^-19 Tan[beta])+Sec[beta]^2
((0.`+0.`I)+1.2183942113194644`*^-18 Tan[beta]))), {m, -1, 1}, {beta, -pi, pi}]

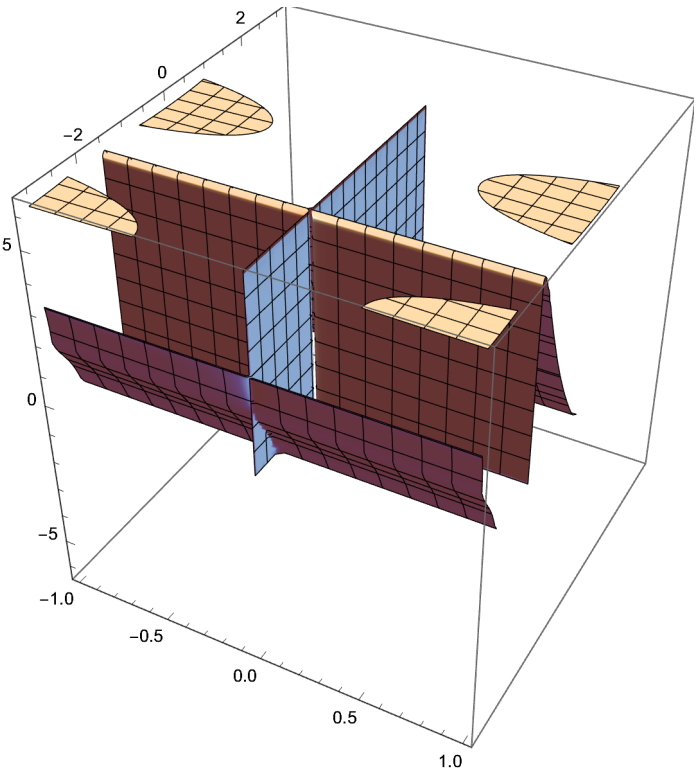
```



$$\theta = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

ContourPlot3D[

$$\begin{aligned}
 & m \left( -2.1630149725479812 \cdot 10^{-8} \sqrt{\cos\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2} \left( \log[1. - 1. \tan[0.5 \beta]] - \right. \right. \\
 & \quad \left. \left. 1. \log\left[1. + \tan\left[0.5 \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]\right] \right) \sec\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] + \right. \\
 & \quad 0.125 \sqrt{1. + \cos\left[2. \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]} \sec\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^5 \\
 & \quad \left( (0. + 0. i) \cos\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] + \right. \\
 & \quad \left. 5.169208853894573 \cdot 10^{-18} \sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] \right) \\
 & \quad \sqrt{(39.47841760435743 + 39.47841760435743 \cos[2. \beta] + (0. + 0. i) \sin[2. \beta])} \\
 & \quad \sqrt{(3.5481432270250993 \cdot 10^{18} + } \\
 & \quad 3.5481432270250993 \cdot 10^{18} \cos[2. \beta] + (0. + 0. i) \sin[2. \beta]) + \\
 & \quad \sqrt{(39.47841760435743 + 39.47841760435743 \cos[2. \beta] + (0. + 0. i) \sin[2. \beta])} \\
 & \quad \sqrt{(3.5481432270250993 \cdot 10^{18} + 3.5481432270250993 \cdot 10^{18} \cos[2. \beta] + (0. + 0. i) \sin[2. \beta])} \\
 & \quad \left( \sec[\beta]^4 ((0. + 0. i) + 6.091971056597322 \cdot 10^{-19} \tan[\beta]) + \right. \\
 & \quad \left. \sec[\beta]^2 ((0. + 0. i) + 1.2183942113194644 \cdot 10^{-18} \tan[\beta]) \right) \Bigg), \\
 & \{m, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}
 \end{aligned}$$



$$\text{Solve}\left[-m\left(\frac{(4\pi r^2 - 2r^2\theta)^2}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{r^2}{2\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right) == m\left(-2.1630149725479812 \cdot 10^{-8} \sqrt{\cos[\beta]^2} (\log[1. - 1. \tan[0.5 \beta]] - 1. \log[1. + \tan[0.5 \beta]]) \sec[\beta] + 0.125 \sqrt{1. + \cos[2. \beta]} \sec[\beta]^5 ((\theta. + \theta. i) \cos[\beta] + 5.169208853894573 \cdot 10^{-18} \sin[\beta]) \sqrt{(39.47841760435743 + 39.47841760435743 \cos[2. \beta] + (\theta. + \theta. i) \sin[2. \beta]) \sqrt{(3.5481432270250993 \cdot 10^{18} + 3.5481432270250993 \cdot 10^{18} \cos[2. \beta] + (\theta. + \theta. i) \sin[2. \beta]) + \sqrt{(39.47841760435743 + 39.47841760435743 \cos[2. \beta] + (\theta. + \theta. i) \sin[2. \beta]) \sqrt{(3.5481432270250993 \cdot 10^{18} + 3.5481432270250993 \cdot 10^{18} \cos[2. \beta] + (\theta. + \theta. i) \sin[2. \beta]) (\sec[\beta]^4 ((\theta. + \theta. i) + 6.091971056597322 \cdot 10^{-19} \tan[\beta]) + \sec[\beta]^2 ((\theta. + \theta. i) + 1.2183942113194644 \cdot 10^{-18} \tan[\beta]))}, m]\right.\right.$$

$$\text{ContourPlot3D}\left[0.\` / \left(-1.\` \left(\frac{0.039788735772973836\` (12.566370614359172\` r^2 - 2.\` r^2 \theta)^2}{(12.566370614359172\` r^2 \theta - 1.\` r^2 \theta^2)^{3/2}} - \frac{0.15915494309189535\` r^2}{\sqrt{12.566370614359172\` r^2 \theta - 1.\` r^2 \theta^2}}\right) - \right.$$

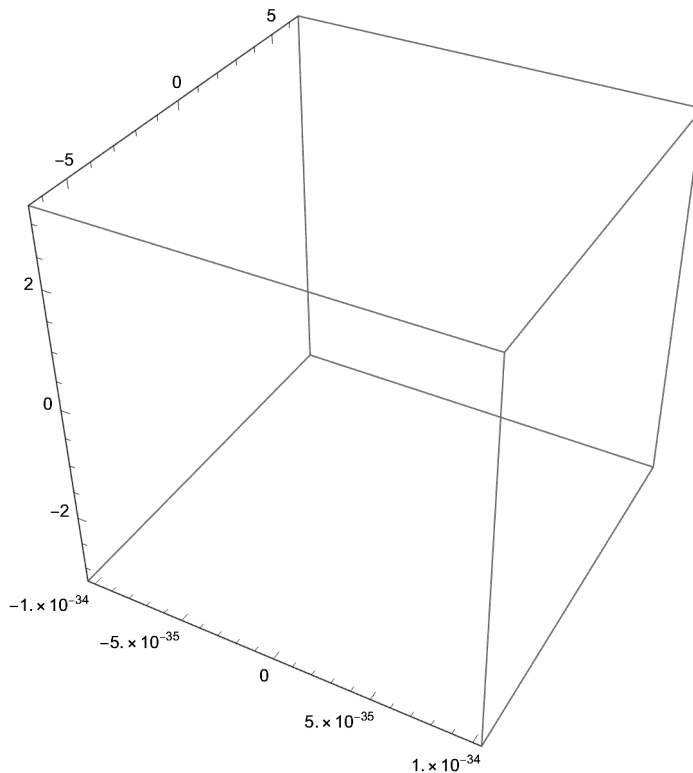
$$1.\` \left(-2.1630149725479812\` \cdot 10^{-8} \sqrt{\cos[\beta]^2} (\log[1.\` - 1.\` \tan[0.5\` \beta]] - \right.$$

$$1.\` \log[1.\` + \tan[0.5\` \beta]]) \sec[\beta] + 0.125\` \sqrt{1.\` + \cos[2.\` \beta]} \sec[\beta]^5 ((0.\` + 0.\` \imath) \cos[\beta] + 5.169208853894573\` \cdot 10^{-18} \sin[\beta])$$

$$\sqrt{(39.47841760435743\` + 39.47841760435743\` \cos[2.\` \beta] + (0.\` + 0.\` \imath) \sin[2.\` \beta])} \sqrt{(3.5481432270250993\` \cdot 10^{18} + 3.5481432270250993\` \cdot 10^{18} \cos[2.\` \beta] + (0.\` + 0.\` \imath) \sin[2.\` \beta])} +$$

$$\sqrt{(39.47841760435743\` + 39.47841760435743\` \cos[2.\` \beta] + (0.\` + 0.\` \imath) \sin[2.\` \beta])} \sqrt{(3.5481432270250993\` \cdot 10^{18} + 3.5481432270250993\` \cdot 10^{18} \cos[2.\` \beta] + (0.\` + 0.\` \imath) \sin[2.\` \beta])} \sin[2.\` \beta] (\sec[\beta]^4 ((0.\` + 0.\` \imath) + 6.091971056597322\` \cdot 10^{-19} \tan[\beta]) + \sec[\beta]^2 ((0.\` + 0.\` \imath) + 1.2183942113194644\` \cdot 10^{-18} \tan[\beta])) \right),$$

$$\{r, -1 \cdot 10^{-34}, 1 \cdot 10^{-34}\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$$



$$\text{Solve}\left[-m\left(\frac{(4\pi r^2 - 2r^2\theta)^2}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{r^2}{2\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right) ==\right. \\ \left.m\left(-2.1630149725479812 \cdot 10^{-8} \sqrt{\cos[\beta]^2}\right.\right. \\ \left.\left.(\log[1. - 1. \tan[0.5 \beta]] - 1. \log[1. + \tan[0.5 \beta]]) \sec[\beta] + 0.125 \sqrt{1. + \cos[2. \beta]} \sec[\beta]^5 ((0. + 0. \text{I}) \cos[\beta] + 5.169208853894573 \cdot 10^{-18} \sin[\beta])\right.\right. \\ \left.\left.\sqrt{(39.47841760435743 + 39.47841760435743 \cos[2. \beta] + (0. + 0. \text{I}) \sin[2. \beta])}\right.\right. \\ \left.\left.\sqrt{(3.5481432270250993 \cdot 10^{18} + 3.5481432270250993 \cdot 10^{18} \cos[2. \beta] + (0. + 0. \text{I}) \sin[2. \beta]) +}\right.\right. \\ \left.\left.\sqrt{(39.47841760435743 + 39.47841760435743 \cos[2. \beta] + (0. + 0. \text{I}) \sin[2. \beta])}\right.\right. \\ \left.\left.\sqrt{(3.5481432270250993 \cdot 10^{18} + 3.5481432270250993 \cdot 10^{18} \cos[2. \beta] + (0. + 0. \text{I}) \sin[2. \beta])}\right.\right. \\ \left.\left.\left(\sec[\beta]^4 ((0. + 0. \text{I}) + 6.091971056597322 \cdot 10^{-19} \tan[\beta]) + \sec[\beta]^2 ((0. + 0. \text{I}) + 1.2183942113194644 \cdot 10^{-18} \tan[\beta])\right)\right), \theta\right]$$

$$\text{Solve}\left[2.53303 \times 10^{-36} m == (-3.88304 \times 10^{-14} + 6.79531 \times 10^{-8} \text{I}) m, 6.28318\right]$$

$$\frac{\sqrt{r} \sqrt{\theta} \sqrt{4\pi r - r\theta}}{2\pi}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\theta} \sqrt{4\pi r - r\theta}}{2\pi} == \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right]$$

{{}}

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == r \sin[\beta], v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}}\right\}\right\}$$

$$c := 2.99792458 (10^8)$$

$$\begin{aligned}
& \text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = h, v\right] \\
& \left\{ \left\{ v \rightarrow - \frac{1. \sqrt{3.54814 \times 10^{18} h^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 h^2 - 12.5664 r^2 \theta + r^2 \theta^2}} \right\}, \right. \\
& \left. \left\{ v \rightarrow \frac{\sqrt{3.54814 \times 10^{18} h^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 h^2 - 12.5664 r^2 \theta + r^2 \theta^2}} \right\} \right\} \\
& \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} h^2 - \right. \right. \\
& \quad \left. \left. 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2 \right) \right) / \\
& \left( \sqrt{39.47841760435743 \cdot h^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) \\
& 3.5481432270250993 \cdot 10^{18} / c^2 \\
& 39.47841760435743 \cdot / \pi \\
& 12.5664 \\
& 4 \pi^2 c^2 \\
& \frac{\sqrt{4 \pi^2 c^2 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 - 4 \pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 - 4 \pi r^2 \theta + r^2 \theta^2}} \\
& \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \\
& \frac{\sqrt{4 \pi^2 c^2 h^2 - 4 \pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4 \pi r^2 \theta + r^2 \theta^2}} \\
& \frac{\sqrt{4 \pi^2 c^2 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 - 4 \pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 - 4 \pi r^2 \theta + r^2 \theta^2}} \\
& \frac{\sqrt{-4 c^2 \pi r^2 \theta + c^2 r^2 \theta^2 + c^2 (4 \pi r^2 \theta - r^2 \theta^2)}}{\sqrt{-4 \pi r^2 \theta + r^2 \theta^2 + \frac{1}{4} (4 \pi r^2 \theta - r^2 \theta^2)}} = v
\end{aligned}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi^2 c^2 h^2 - 4 \pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4 \pi r^2 \theta + r^2 \theta^2}} == v, c\right]$$

$$\left\{\left\{c \rightarrow -\frac{v \sqrt{h^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{\sqrt{4 h^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}}\right\}, \left\{c \rightarrow \frac{v \sqrt{h^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{\sqrt{4 h^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}}\right\}\right\}$$

$$\text{Solve}\left[c == \frac{c \sqrt{(r \text{Sin}[\theta])^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}}{\sqrt{4 (r \text{Sin}[\theta])^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}}, \theta\right]$$

{{}}

$$v == c \sqrt{4 h^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2} / \sqrt{h^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}$$

$$\blacksquare c \sqrt{4 \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2} / \sqrt{\left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2 \pi^2 - 4 \pi r^2 \theta + r^2 \theta^2}$$



```
ContourPlot3D[C Sqrt[4 (h)^2 π^2 - 4 π r^2 θ + r^2 θ^2] / Sqrt[(h)^2 π^2 - 4 π r^2 θ + r^2 θ^2],
  {h, -1, 1}, {r, -1, 1}, {θ, -2, 2}, PlotTheme -> {"Classic", "ClassicLights"}]
```

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

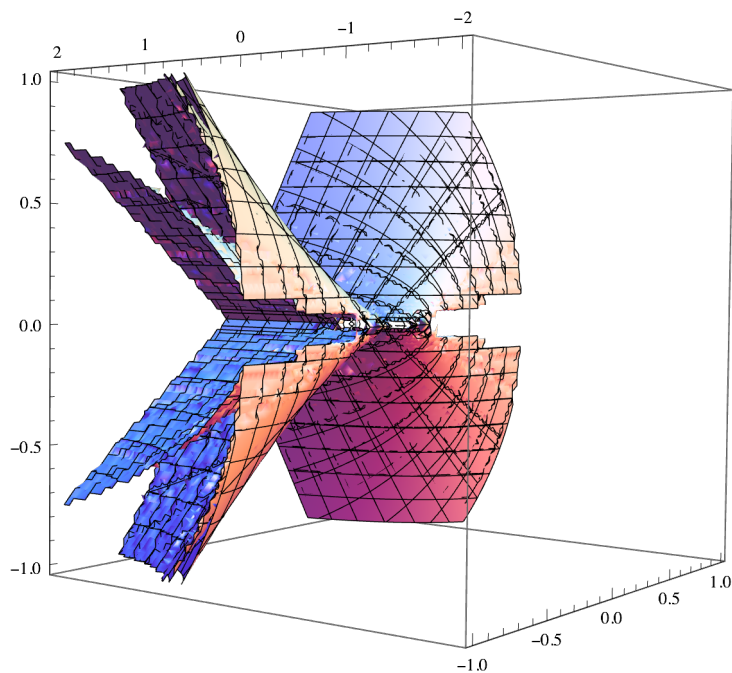
... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

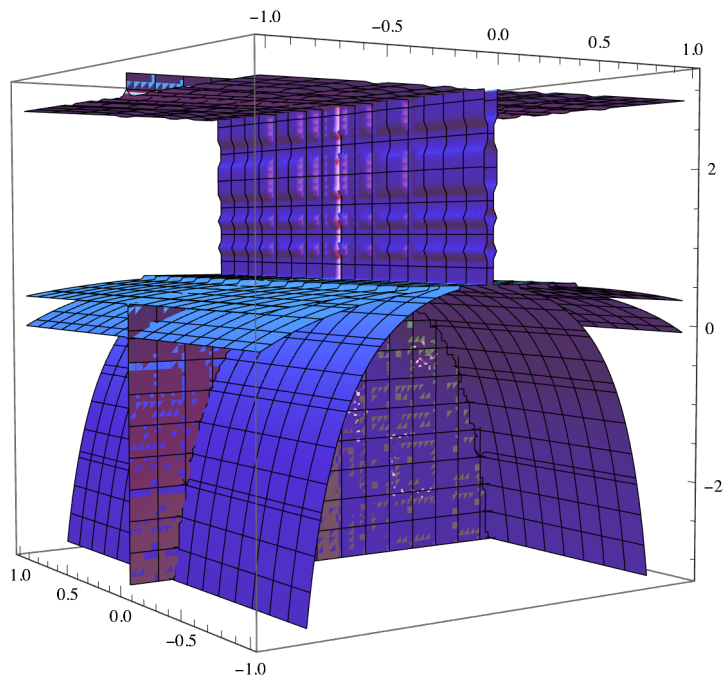
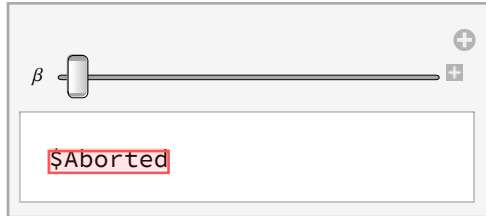
... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.



Manipulate[ContourPlot3D[ $\frac{\sqrt{4\pi^2 c^2 (r \sin[\beta])^2 - 4\pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 (r \sin[\beta])^2 - 4\pi r^2 \theta + r^2 \theta^2}}$ , {c, -1, 1}, {r, -1, 1}, {θ, -π, π}, PlotTheme → {"Classic", "ClassicLights"}], {β, -1, 1}]



... **Power:** Infinite expression  $\frac{1}{0}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0}$  encountered.

... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

... **Power:** Infinite expression  $\frac{1}{0}$  encountered.

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... **General**: Further output of Power::infy will be suppressed during this calculation.

... **Infinity**: Indeterminate expression 0. ComplexInfinity encountered.

... **General**: Further output of Infinity::indet will be suppressed during this calculation.

... **Power**: Infinite expression  $\frac{1}{0}$  encountered.

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... **Power**: Infinite expression  $\frac{1}{0}$  encountered.

... **General**: Further output of Power::infy will be suppressed during this calculation.

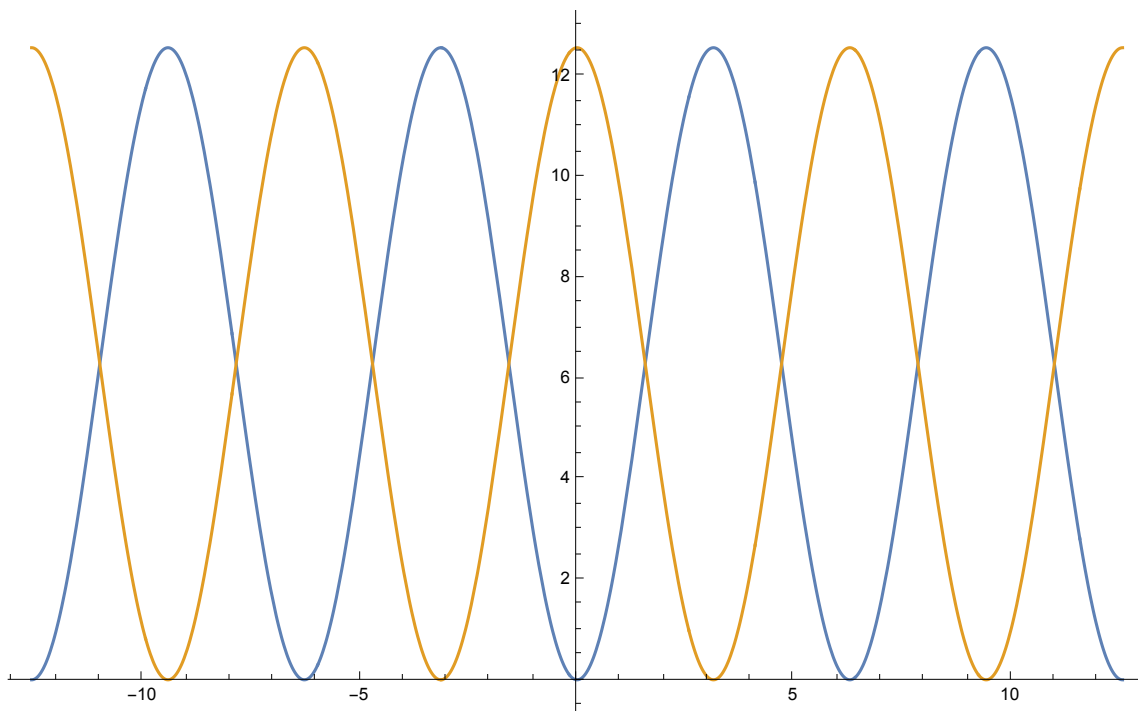
... **Infinity**: Indeterminate expression 0. ComplexInfinity encountered.

... **General**: Further output of Infinity::indet will be suppressed during this calculation.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{\left(\frac{\sqrt{4\pi^2 c^2 h^2 - 4\pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4\pi r^2 \theta + r^2 \theta^2}}\right)^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{\left(\frac{\sqrt{4\pi^2 c^2 h^2 - 4\pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4\pi r^2 \theta + r^2 \theta^2}}\right)^2}{c^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = r \sin[\beta], \theta\right]$$

$\{\{\theta \rightarrow -2(-\pi + \pi \cos[\beta])\}, \{\theta \rightarrow 2(\pi + \pi \cos[\beta])\}\}$

Plot[{-2 (-π + π Cos[β]), 2 (π + π Cos[β])}, {β, -4 π, 4 π}]



1.1294090667581471`\*^18 / c^2

$\pi^2$

8.987551787368176`\*^16 / c^2

1.

$4 \pi c^2$

$1.12941 \times 10^{18}$

3.7673031346177063`\*^9 /

c := 2.99792458 (10^8)

$$\int \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} d\theta$$

$$\frac{1}{2 \pi \sqrt{(4 \pi - \theta) \theta}} \sqrt{r \sqrt{1 - 1.11265 \times 10^{-17} v^2}} \sqrt{r (4 \pi - \theta)} \sqrt{\frac{\sqrt{1 - 1.11265 \times 10^{-17} v^2} \theta}{1. - 1.11265 \times 10^{-17} v^2}} \\ (0.5 \sqrt{12.5664 - 1. \theta} \theta^{3/2} - 3.14159 \sqrt{(12.5664 - 1. \theta) \theta} + 39.4784 \text{ArcSin}[0.282095 \sqrt{\theta}])$$

$$\begin{aligned}
 & \text{Solve}\left[\frac{1}{2 \pi \sqrt{(4 \pi - \theta) \theta}} \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot v^2}} \sqrt{r (4 \pi - \theta)} \right. \\
 & \quad \sqrt{\frac{\sqrt{1 - 1.1126500560536185 \cdot v^2} \theta}{1. - 1.1126500560536185 \cdot v^2}} \left(0.5 \sqrt{12.566370614359172 \cdot \theta} \theta^{3/2} - \right. \\
 & \quad 3.141592653589793 \sqrt{(12.566370614359172 \cdot \theta) \theta} + \\
 & \quad \left. 39.47841760435743 \text{ArcSin}\left[0.28209479177387814 \sqrt{\theta}\right]\right) == \\
 & \quad \left(\sqrt{(3.5481432270250993 \cdot h^2 - 1.1294090667581471 \cdot r^2 \theta + \right. \\
 & \quad \left. 8.987551787368176 \cdot r^2 \theta^2)}\right) / \\
 & \quad \left(\sqrt{39.47841760435743 \cdot h^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right), v] \\
 & \text{Solve}\left[\frac{1}{2 \pi} \right. \\
 & \quad \sqrt{(9.102860909133264 \cdot \sin^2[\beta] + 8.679267028916372 \cdot \sin[\beta] + 2.0633200682788 \cdot \sin^3[\beta] + \\
 & \quad \left. \sqrt{1.9463574830253733 \cdot \sin^2[\beta] - 1.9463574830253735 \cdot \sin^3[\beta]})} \right. \\
 & \quad \sqrt{1 - \frac{\left(\frac{\sqrt{4 \pi^2 c^2 h^2 - 4 \pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4 \pi r^2 \theta + r^2 \theta^2}}\right)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{\left(\frac{\sqrt{4 \pi^2 c^2 h^2 - 4 \pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4 \pi r^2 \theta + r^2 \theta^2}}\right)^2}{c^2}}}} \\
 & \quad \sqrt{(4 \pi (9.102860909133264 \cdot \sin^2[\beta] + 8.679267028916372 \cdot \sin[\beta] + 2.0633200682788 \cdot \sin^3[\beta] + \\
 & \quad \sqrt{1.9463574830253733 \cdot \sin^2[\beta] - 1.9463574830253735 \cdot \sin^3[\beta]}) - \\
 & \quad (9.102860909133264 \cdot \sin^2[\beta] + 8.679267028916372 \cdot \sin[\beta] + 2.0633200682788 \cdot \sin^3[\beta] + \\
 & \quad \sqrt{1.9463574830253733 \cdot \sin^2[\beta] - 1.9463574830253735 \cdot \sin^3[\beta]}) \theta) == \\
 & \quad (9.102860909133264 \cdot \sin^2[\beta] + 8.679267028916372 \cdot \sin[\beta] + 2.0633200682788 \cdot \sin^3[\beta] + \\
 & \quad \sqrt{1.9463574830253733 \cdot \sin^2[\beta] - 1.9463574830253735 \cdot \sin^3[\beta]}) \sin[\beta], r]
 \end{aligned}$$

{{}}

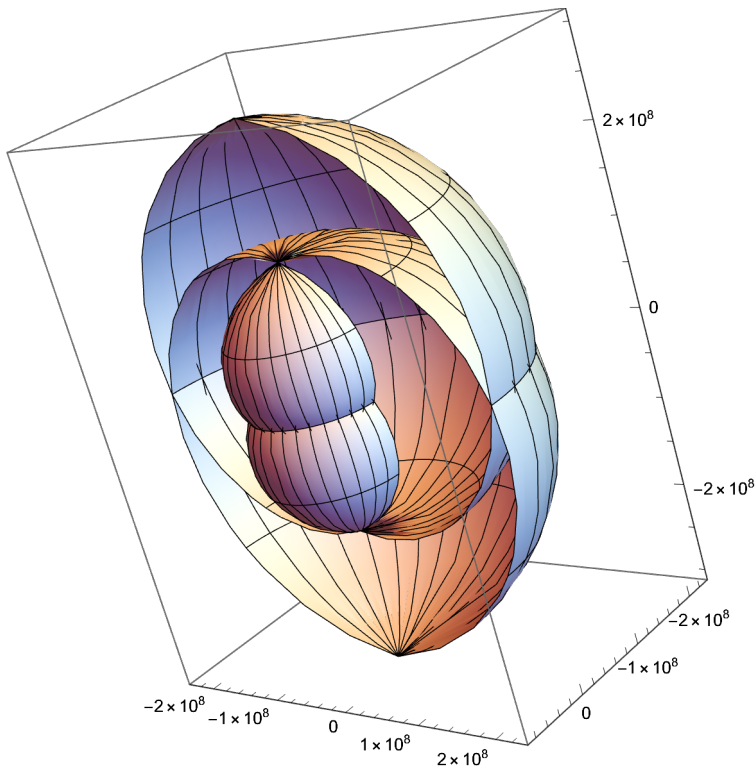
$$\text{Solve}[r == 2 \pi r - 2 \pi x - \theta r, r]$$

$$\left\{\left\{r \rightarrow \frac{2 \pi x}{-1 + 2 \pi - \theta}\right\}\right\}$$

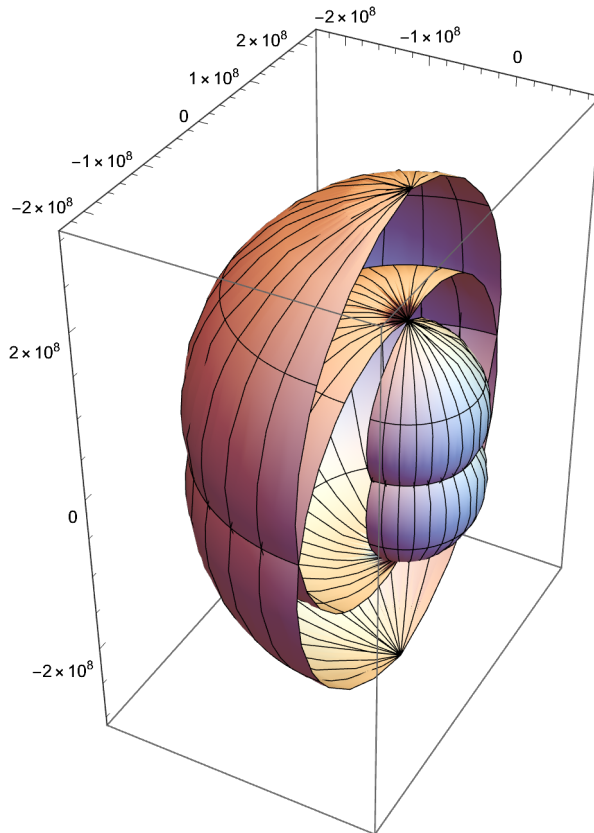
$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{\left(\frac{\sqrt{4\pi^2 c^2 h^2 - 4\pi c^2 r^2 \theta + c^2 r^2 \theta^2}}{\sqrt{\pi^2 h^2 - 4\pi r^2 \theta + r^2 \theta^2}}\right)^2}{c^2}}}{\sqrt{1 - \frac{\frac{\theta}{\sqrt{\pi^2 h^2 - 4\pi r^2 \theta + r^2 \theta^2}}}{c^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = r \sin[\beta], c\right]$$

{}

$$\begin{aligned} & \left( \left( \sqrt{3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16}} \right) / \right. \\ & \left. \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) \right) \\ & \text{SphericalPlot3D}\left[\left( \left( \sqrt{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2} \right) / \right. \right. \\ & \left. \left. \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \right) \right. \\ & \left. (\theta / (2\pi)), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} \right] \end{aligned}$$



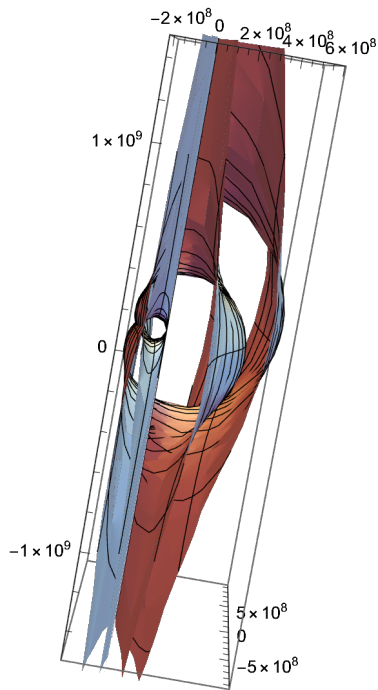
```
SphericalPlot3D[
  ((\sqrt{(3.5481432270250993`*^18 - 1.1294090667581471`*^18 \theta + 8.987551787368176`*^16
    \theta^2)})) / (\sqrt{39.47841760435743` - 12.566370614359172` \theta + \theta^2}))
  (\theta / (2 \pi)), {\theta, -2 \pi, 2 \pi}, {\beta, -\pi / 2, \pi / 2}]
```



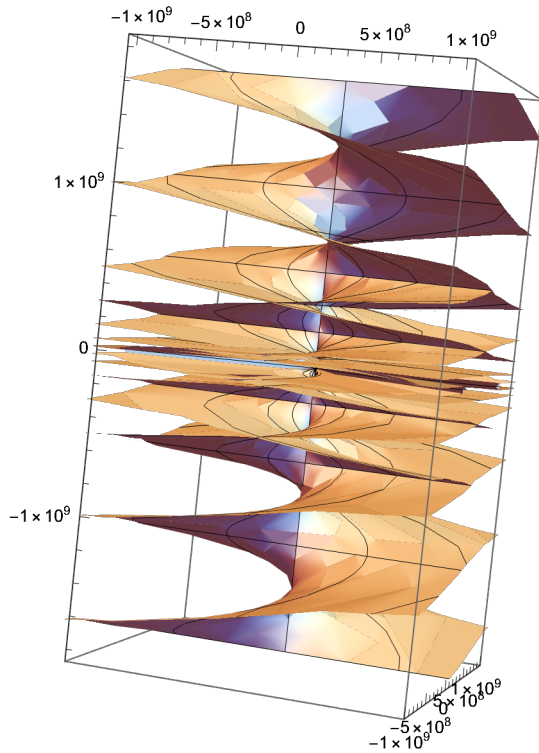




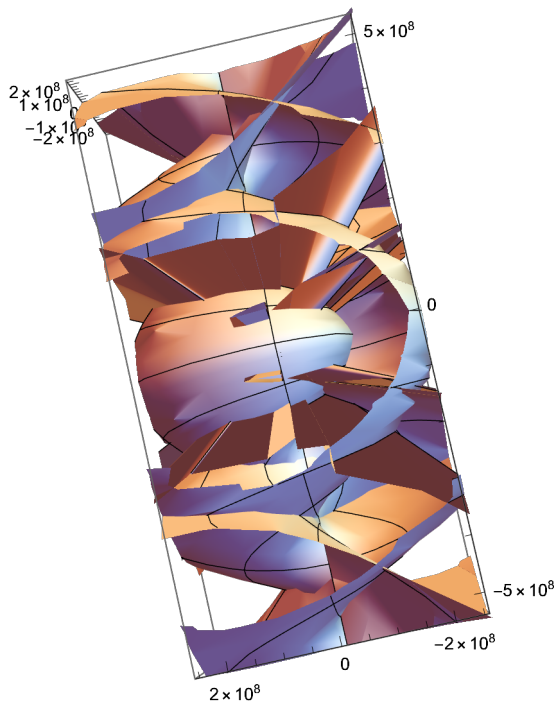
SphericalPlot3D[ $\left(-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{18}-1.1294090667581471\cdot 10^{18}\theta+8.987551787368176\cdot 10^{16}\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^2\right)}\right)\right)/\right.$   
 $\left.\left(\sqrt{\left(39.47841760435743-12.566370614359172\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)+\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^2\right)\right)}\right)\right)\right](\theta/(2\pi)),\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}]$



$\text{SphericalPlot3D}\left[\left(-\left(1.\sqrt{3.5481432270250993}^{\wedge 18}-\right.\right.\right.$   
 $\left.\left.1.1294090667581471^{\wedge 18}\theta+8.987551787368176^{\wedge 16}\left(\theta^2\right)\right)\right/$   
 $\left(\sqrt{\left(39.47841760435743-12.566370614359172\left(2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}[\beta]^2}\right)\right)+\right.\right.\right.$   
 $\left.\left.\left(2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}[\beta]^2}\right)\right)^2\right)\right)\right]\left(\theta/(2\pi)\right),\{\beta,-\pi,\pi\},\{\theta,-4\pi,4\pi\}$



SphericalPlot3D[ $\left[ - \left( 1. \sqrt{3.5481432270250993}^{*18} - \right. \right.$   
 $\left. \left. 1.1294090667581471^{*18} \theta + 8.987551787368176^{*16} (\theta)^2 \right) \right] /$   
 $\left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 (\theta) + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)^2 \right) \right)} \right)$   
 $(\theta / (2 \pi)), \{\beta, -\pi, \pi\}, \{\theta, -4 \pi, 4 \pi\}$ ]



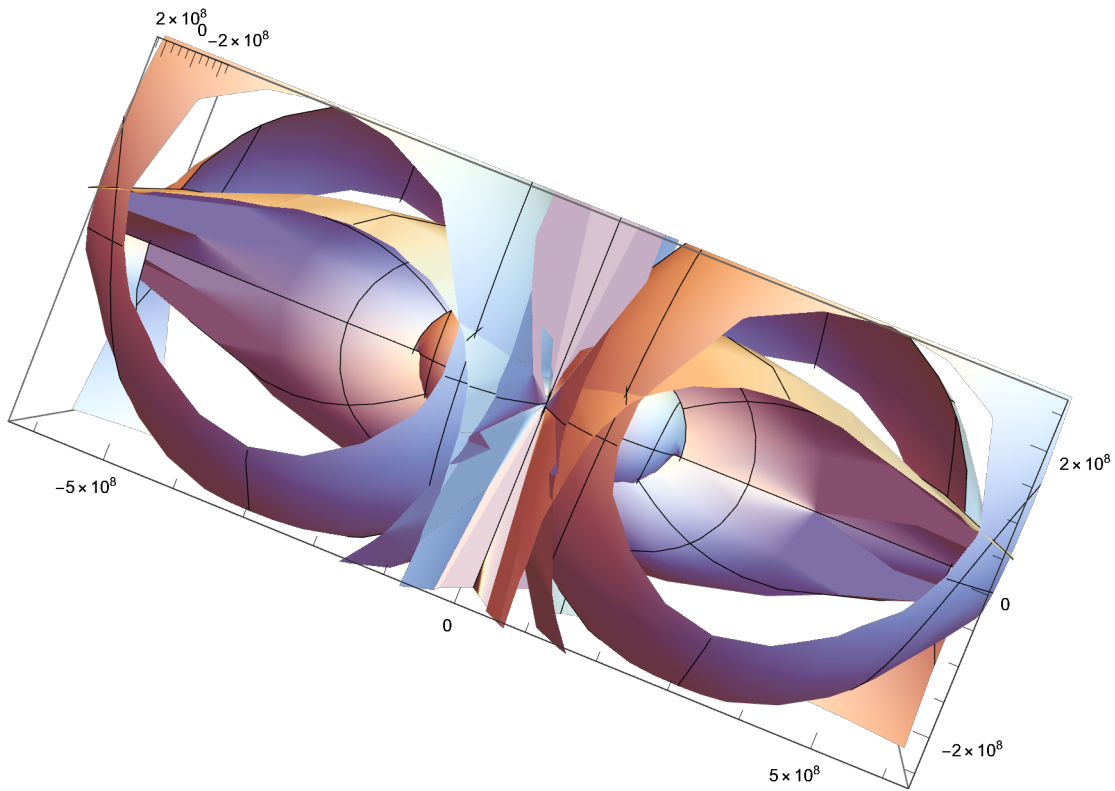
$$\text{SphericalPlot3D}\left[\left(-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{18}-\right.}\right.\right.\right.$$

$$\left.\left.1.1294090667581471\cdot 10^{18}\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)+\right.\right.$$

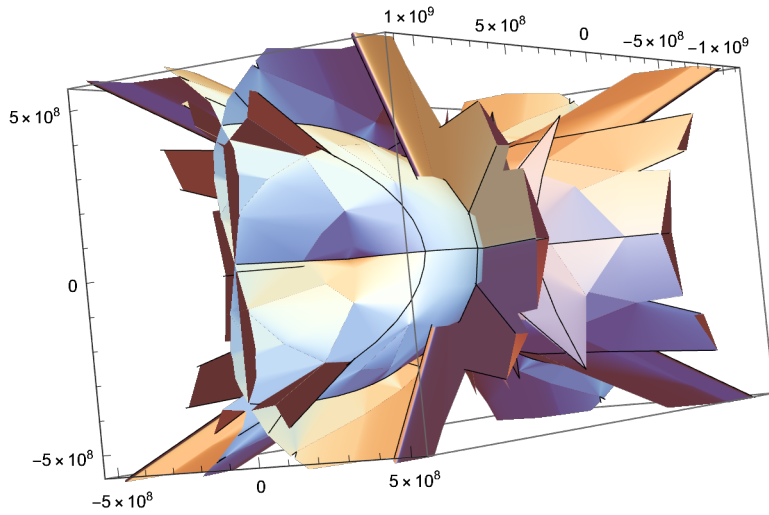
$$\left.\left.8.987551787368176\cdot 10^{16}\left(\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2\right)\right)\right)/\right.$$

$$\left.\left(\sqrt{39.47841760435743-12.566370614359172\theta+\theta^2}\right)\right]$$

$$(\theta/(2\pi)),\{\beta,-\pi,\pi\},\{\theta,-4\pi,4\pi\}]$$



```
SphericalPlot3D[
  ((Sqrt[3.5481432270250993`*^18 - 1.1294090667581471`*^18 (2 (π + Sqrt[π^2 - π^2 Sin[β]^2]) +
    8.987551787368176`*^16 (2 (π + Sqrt[π^2 - π^2 Sin[β]^2])^2)))]/
  (Sqrt[39.47841760435743` - 12.566370614359172` (2 (π + Sqrt[π^2 - π^2 Sin[β]^2]) + (θ)^2)]))
  (θ / (2 π)), {β, -π, π}, {θ, -4 π, 4 π}]
```



$$\beta \rightarrow \text{ArcSin}\left[\frac{4 \pi r \theta - r \theta^2}{4 \pi^2}\right] = \text{ArcSin}\left[\frac{4 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta^2}{4 \pi^2}\right] \text{ where,}$$

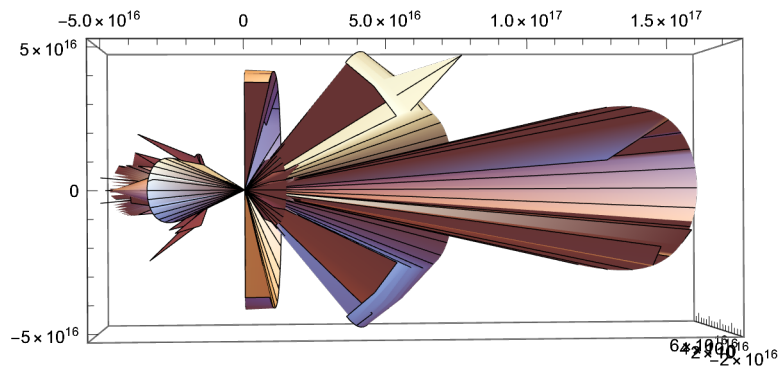
$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

SphericalPlot3D[

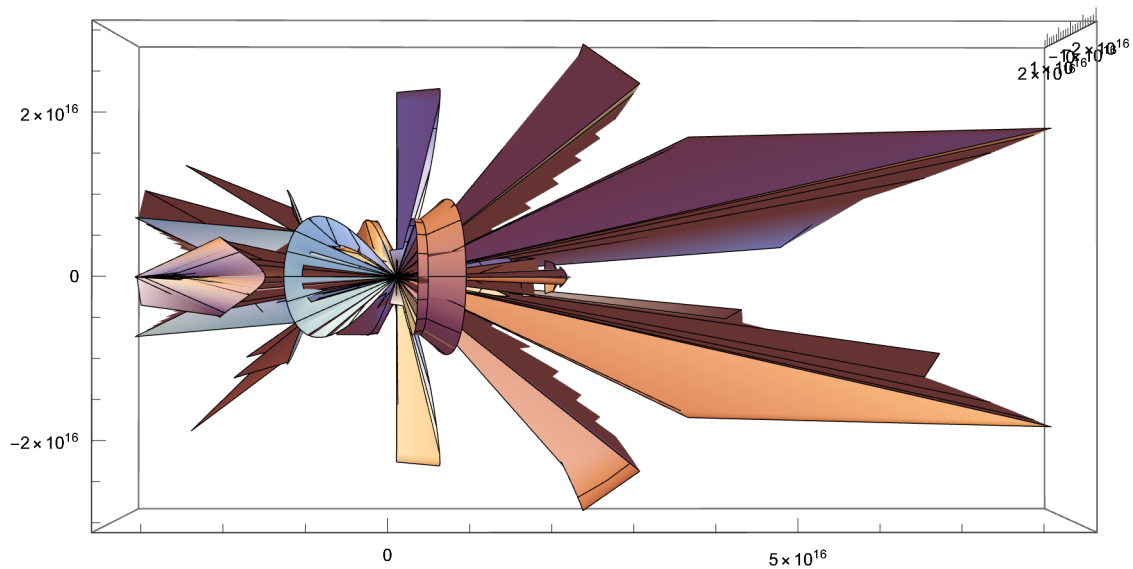
$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin\left[\text{ArcSin}\left[\frac{4 \pi r \theta - r \theta^2}{4 \pi^2}\right]\right]^2 \right)} \right),$$

{ $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }, { $\beta$ ,  $-\pi / 2$ ,  $\pi / 2$ }]



SphericalPlot3D[ $\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot 10^{16} \theta + \theta^2 + 39.47841760435743 \cdot 10^{16} \sin\left[\text{ArcSin}\left[\frac{4 \pi r \theta - r^2 \theta^2}{4 \pi^2}\right]\right]^2\right)}\right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$



$$\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( 2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{4 \pi r^2 \theta - r^2 \theta^2}{4 \pi^2}} \right) = 1 / \theta = \infty$$

$$\text{Solve}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( 2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{4 \pi r^2 \theta - r^2 \theta^2}{4 \pi^2}} \right) == (\eta / r), r\right]$$

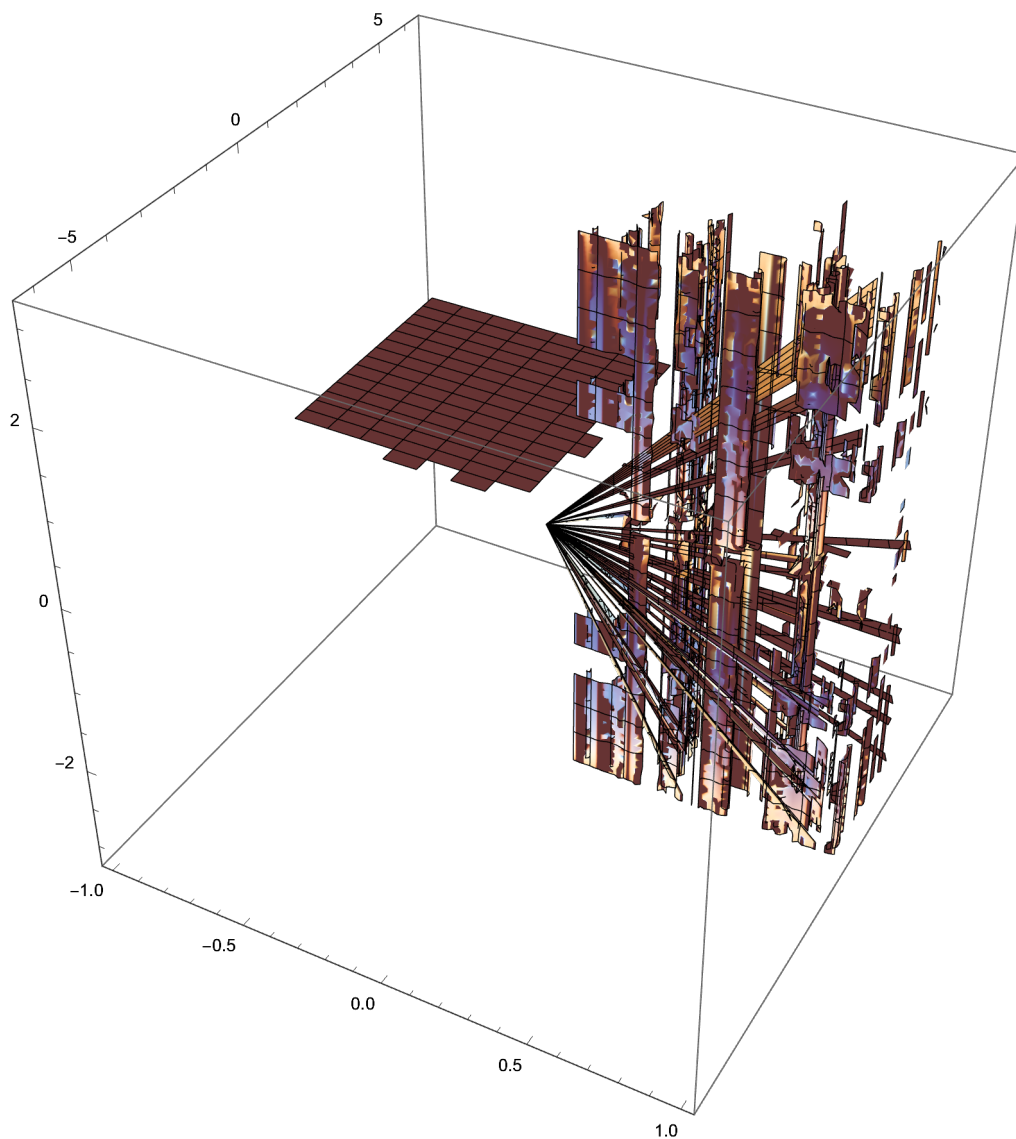
{}

$$\text{Solve}\left[\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}/\left(2\pi r-r\theta-2\pi\sqrt{r^2-\frac{4\pi r^2\theta-r^2\theta^2}{4\pi^2}}\right)==(\eta/r),\eta\right]$$

$$\left\{\left\{\eta\rightarrow-\frac{2\pi r\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}\left(-2\pi r+\sqrt{r^2(2\pi-\theta)^2+r\theta}\right)}\right\}\right\}$$

$$\text{ContourPlot3D}\left[-\frac{2\pi r\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}\left(-2\pi r+\sqrt{r^2(2\pi-\theta)^2+r\theta}\right)},\right.$$

$$\left.\{r,-1,1\},\{\theta,-2\pi,2\pi\},\{\beta,-\pi,\pi\}\right]$$





$$\text{Solve}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left(2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{4 \pi r^2 \theta - r^2 \theta^2}{4 \pi^2}}\right) == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left(2 \pi r - r \theta - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right), r\right]$$

$$\{\}$$

$$\text{Solve}\left[\frac{\frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \sqrt{4 \pi - \theta_1} \sqrt{\theta_1}}{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta} == \beta, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \text{InverseFunction}[\text{Subscript}, 1, 2]\left[2 \pi \left(1 - \sqrt{1 - \beta^2}\right), 1\right]\right\}, \left\{\theta \rightarrow \text{InverseFunction}[\text{Subscript}, 1, 2]\left[2 \pi \left(1 + \sqrt{1 - \beta^2}\right), 1\right]\right\}\right\}$$

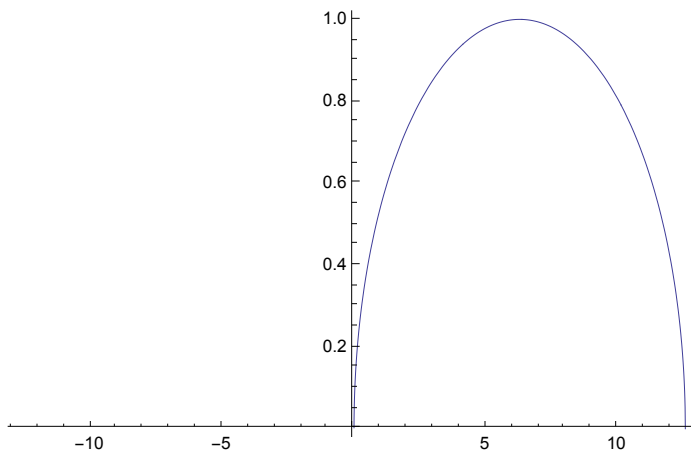
$$\text{Solve}\left[\frac{\frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \sqrt{4 \pi - \theta_1} \sqrt{\theta_1}}{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta} == \beta, \theta_1\right]$$

$$\left\{\left\{\theta_1 \rightarrow 2 \pi \left(1 - \sqrt{1 - \beta^2}\right)\right\}, \left\{\theta_1 \rightarrow 2 \pi \left(1 + \sqrt{1 - \beta^2}\right)\right\}\right\}$$

$$\text{Solve}\left[\theta_1 == 2 \pi \left(1 + \sqrt{1 - \beta^2}\right), \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\frac{\sqrt{4 \pi \theta_1 - \theta_1^2}}{2 \pi}\right\}, \left\{\beta \rightarrow \frac{\sqrt{4 \pi \theta_1 - \theta_1^2}}{2 \pi}\right\}\right\}$$

$$\text{Plot}\left[\frac{\sqrt{4 \pi \theta_1 - \theta_1^2}}{2 \pi}, \{\theta_1, -4 \pi, 4 \pi\}\right]$$



$$\text{Solve}\left[\frac{\sqrt{4\pi\theta_1 - \theta_1^2}}{2\pi} == \frac{\sqrt{4\pi^2\left(\pi + \sqrt{\pi^2 - \frac{1}{4}(4\pi - \theta)\theta}\right) - \left(2\left(\pi + \sqrt{\pi^2 - \frac{1}{4}(4\pi - \theta)\theta}\right)\right)^2}}{2\pi}, \theta_1\right]$$

$$\{\{\theta_1 \rightarrow 4\pi - \theta\}, \{\theta_1 \rightarrow \theta\}\}$$

## FORMS

$$e^{\sqrt{-\frac{\sqrt{4\pi^2 + 4\pi\gamma + \gamma^2} \sin[\beta]}{\sqrt{\gamma} \sqrt{4\pi + \gamma}}} \theta}$$

## THETA

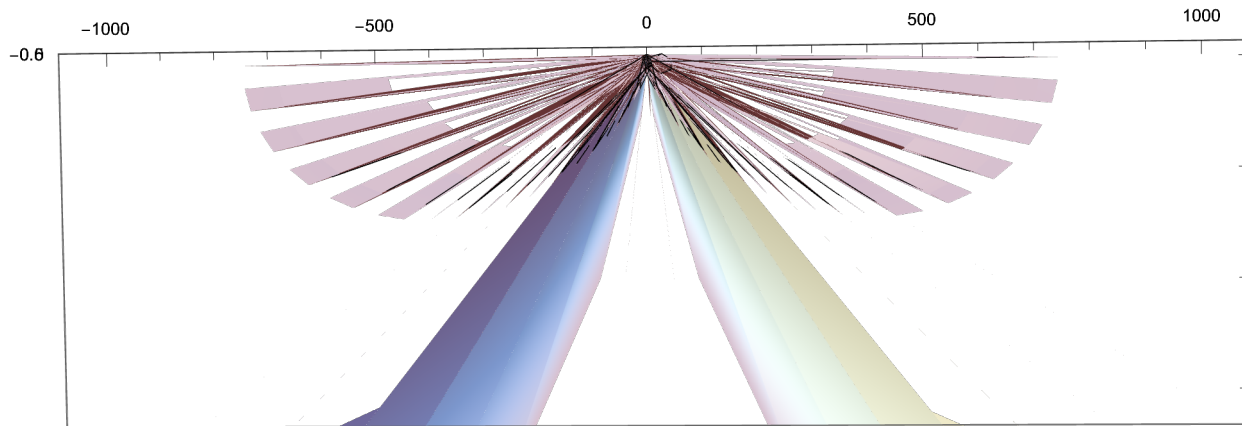
$$\text{Solve}\left[e^{\sqrt{-\frac{2\pi \sin[\beta]}{\sqrt{4\pi - \theta^2}}} \theta} == e^{\sqrt{-\frac{\sqrt{4\pi^2 + 4\pi\gamma + \gamma^2} \sin[\beta]}{\sqrt{\gamma} \sqrt{4\pi + \gamma}}} \theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi\gamma}{2\pi + \gamma}\right\}, \left\{\theta \rightarrow \frac{2\pi(4\pi + \gamma)}{2\pi + \gamma}\right\}\right\}$$

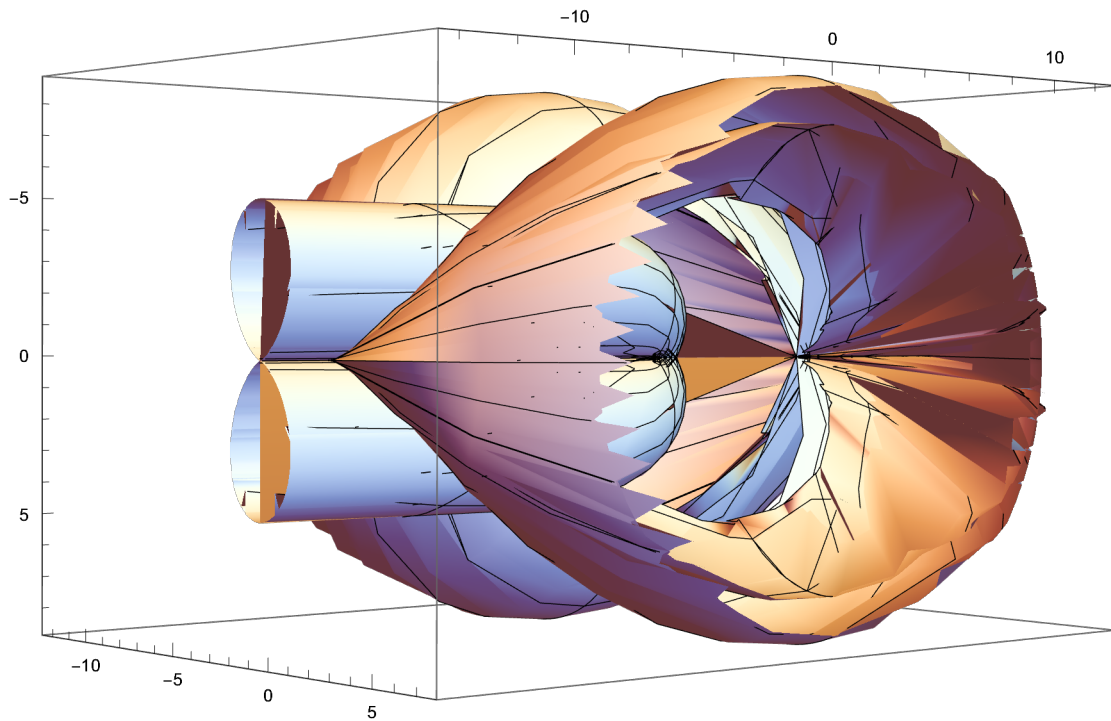
$$\text{Solve}\left[e^{\sqrt{-\frac{\sqrt{4\pi - \theta^2}}{2\pi \sin[\beta]}}} \theta} == e^{\sqrt{-\frac{\sqrt{4\pi^2 + 4\pi\gamma + \gamma^2} \sin[\beta]}{\sqrt{\gamma} \sqrt{4\pi + \gamma}}} \theta}, \theta\right]$$

$$\left\{\{\theta \rightarrow 0\}, \left\{\theta \rightarrow \frac{1}{2(4\pi\gamma + \gamma^2)} \left(16\pi^2\gamma + 4\pi\gamma^2 - \sqrt{\left((-16\pi^2\gamma - 4\pi\gamma^2)^2 - 4(4\pi\gamma + \gamma^2)(16\pi^4 \sin[\beta]^4 + 16\pi^3\gamma \sin[\beta]^4 + 4\pi^2\gamma^2 \sin[\beta]^4)\right)}\right)\right\}, \right. \\ \left.\left\{\theta \rightarrow \frac{1}{2(4\pi\gamma + \gamma^2)} \left(16\pi^2\gamma + 4\pi\gamma^2 + \sqrt{\left((-16\pi^2\gamma - 4\pi\gamma^2)^2 - 4(4\pi\gamma + \gamma^2)(16\pi^4 \sin[\beta]^4 + 16\pi^3\gamma \sin[\beta]^4 + 4\pi^2\gamma^2 \sin[\beta]^4)\right)}\right)\right\}\right\}$$

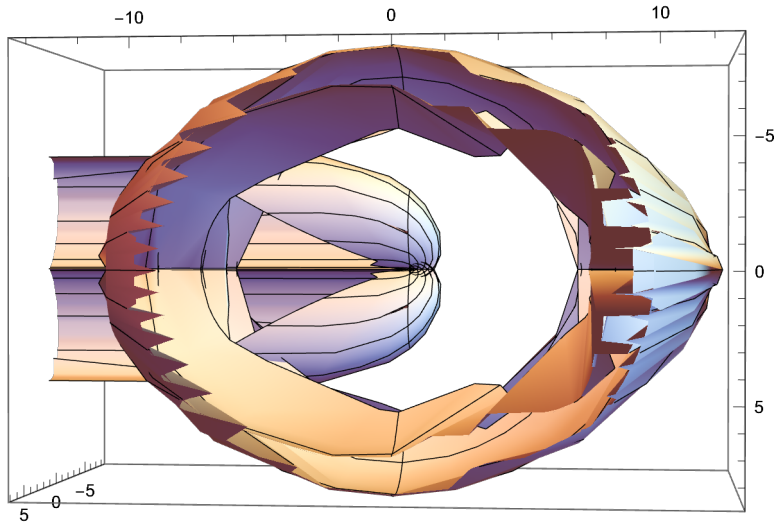
$\text{SphericalPlot3D}\left[\left\{\frac{1}{2(4\pi\gamma + \gamma^2)}\left(16\pi^2\gamma + 4\pi\gamma^2 + \sqrt{\left((-16\pi^2\gamma - 4\pi\gamma^2)^2 - 4(4\pi\gamma + \gamma^2)(16\pi^4\sin[\beta]^4 + 16\pi^3\gamma\sin[\beta]^4 + 4\pi^2\gamma^2\sin[\beta]^4)\right)}\right),\right.\right.$   
 $\left.\frac{1}{2(4\pi\gamma + \gamma^2)}\left(16\pi^2\gamma + 4\pi\gamma^2 + \sqrt{\left((-16\pi^2\gamma - 4\pi\gamma^2)^2 - 4(4\pi\gamma + \gamma^2)(16\pi^4\sin[\beta]^4 + 16\pi^3\gamma\sin[\beta]^4 + 4\pi^2\gamma^2\sin[\beta]^4)\right)}\right)\right\}, \{\beta, -\pi/2, \pi/2\}, \{\gamma, -4\pi, 4\pi\}\right]$



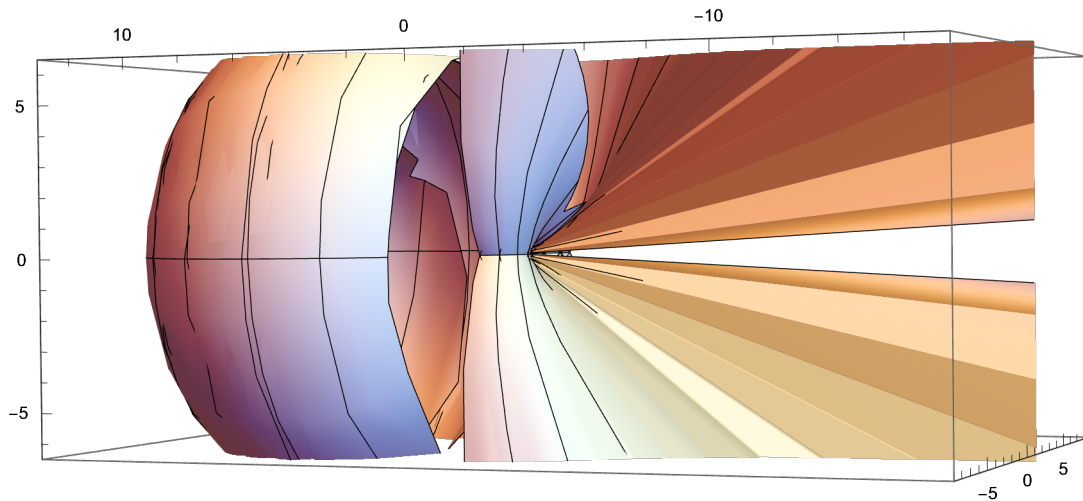
$\text{SphericalPlot3D}\left[\left\{\frac{1}{2(4\pi\gamma + \gamma^2)}\left(16\pi^2\gamma + 4\pi\gamma^2 + \sqrt{\left((-16\pi^2\gamma - 4\pi\gamma^2)^2 - 4(4\pi\gamma + \gamma^2)(16\pi^4\sin[\beta]^4 + 16\pi^3\gamma\sin[\beta]^4 + 4\pi^2\gamma^2\sin[\beta]^4)\right)}\right),\right.\right.$   
 $\left.\frac{1}{2(4\pi\gamma + \gamma^2)}\left(16\pi^2\gamma + 4\pi\gamma^2 + \sqrt{\left((-16\pi^2\gamma - 4\pi\gamma^2)^2 - 4(4\pi\gamma + \gamma^2)(16\pi^4\sin[\beta]^4 + 16\pi^3\gamma\sin[\beta]^4 + 4\pi^2\gamma^2\sin[\beta]^4)\right)}\right)\right\}, \{\gamma, -4\pi, 4\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$

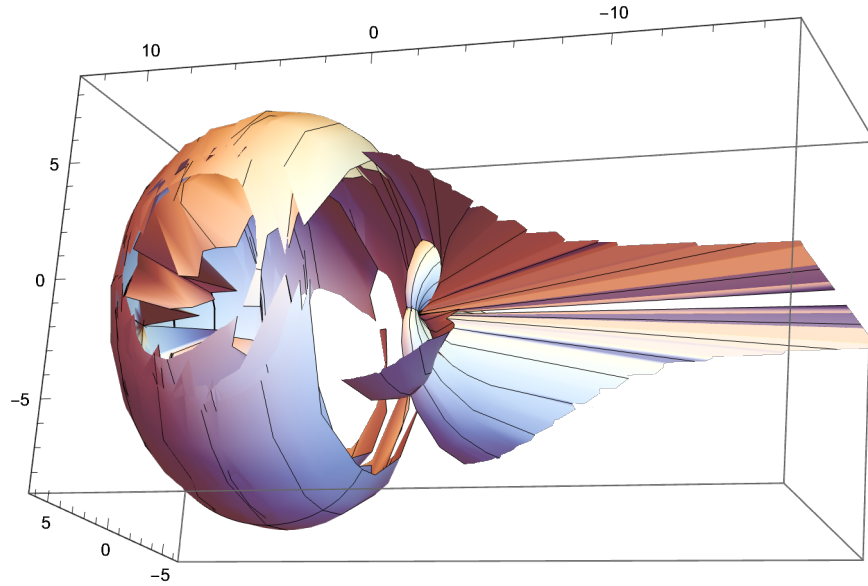


SphericalPlot3D $\left[\frac{1}{2(4\pi\gamma+\gamma^2)}\left(16\pi^2\gamma+4\pi\gamma^2+\sqrt{\left((-16\pi^2\gamma-4\pi\gamma^2)^2-4(4\pi\gamma+\gamma^2)(16\pi^4\sin[\beta]^4+16\pi^3\gamma\sin[\beta]^4+4\pi^2\gamma^2\sin[\beta]^4)\right)}\right),\{\gamma,-4\pi,4\pi\},\{\beta,-\pi/2,\pi/2\}\right]$



SphericalPlot3D $\left[\frac{1}{2(4\pi\gamma+\gamma^2)}\left(16\pi^2\gamma+4\pi\gamma^2+\sqrt{\left((-16\pi^2\gamma-4\pi\gamma^2)^2-4(4\pi\gamma+\gamma^2)(16\pi^4\sin[\beta]^4+16\pi^3\gamma\sin[\beta]^4+4\pi^2\gamma^2\sin[\beta]^4)\right)}\right),\{\beta,-\pi/2,\pi/2\},\{\gamma,-4\pi,4\pi\}\right]$





$$\text{Solve}\left[e^{\sqrt{-\frac{\sqrt{4\pi\theta-\theta^2}}{2\pi\sin[\beta]}}\theta} == e^{\sqrt{-\frac{\sqrt{\gamma}\sqrt{4\pi+\gamma}}{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}}\theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 0\right\}, \left\{\theta \rightarrow \frac{2\pi\gamma}{2\pi+\gamma}\right\}, \left\{\theta \rightarrow \frac{2(4\pi^2+\pi\gamma)}{2\pi+\gamma}\right\}\right\}$$

$$\text{Solve}\left[e^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}\theta} == e^{\sqrt{-\frac{\sqrt{\gamma}\sqrt{4\pi+\gamma}}{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}}\theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{1}{2\gamma(4\pi+\gamma)}\left(-\pi(-16\pi-4\gamma)\gamma\csc[\beta]^2 - \sqrt{4\pi^2\gamma(4\pi+\gamma)(-16\pi^2-16\pi\gamma-4\gamma^2)+\pi^2(-16\pi-4\gamma)^2\gamma^2\csc[\beta]^4}\right)\sin[\beta]^2\right\}, \right. \\ \left.\left\{\theta \rightarrow \frac{1}{2\gamma(4\pi+\gamma)}\left(-\pi(-16\pi-4\gamma)\gamma\csc[\beta]^2 + \sqrt{4\pi^2\gamma(4\pi+\gamma)(-16\pi^2-16\pi\gamma-4\gamma^2)+\pi^2(-16\pi-4\gamma)^2\gamma^2\csc[\beta]^4}\right)\sin[\beta]^2\right\}\right\}$$

## BETA

$$\text{Solve}\left[e^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}\theta} == e^{\sqrt{-\frac{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}{\sqrt{\gamma}\sqrt{4\pi+\gamma}}}\theta}, \beta\right]$$

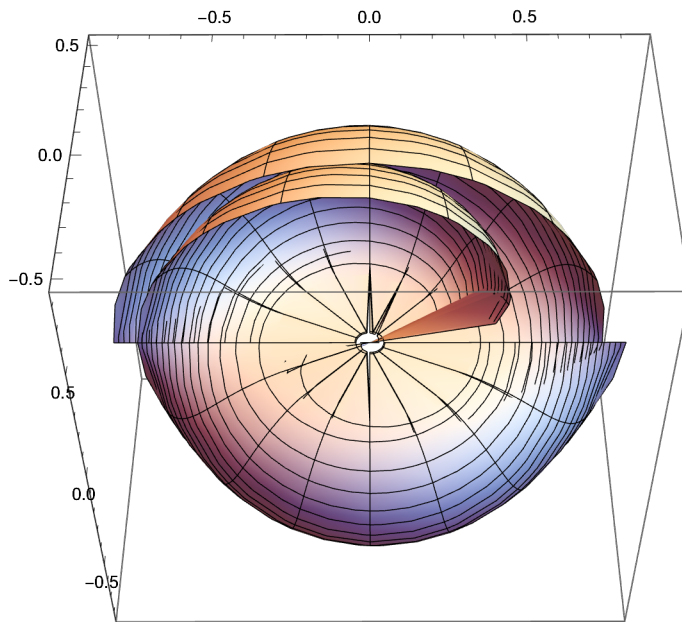
$$\{\{\beta \rightarrow 0\}\}$$

$$\begin{aligned}
& \text{Solve}\left[\mathbf{e}^{\sqrt{-\frac{\sqrt{4\pi-\theta^2}}{2\pi\sin[\beta]}}\theta} == \mathbf{e}^{\sqrt{-\frac{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}{\sqrt{\gamma}\sqrt{4\pi+\gamma}}}\theta}, \beta\right] \\
& \left\{\left\{\beta \rightarrow -\mathbf{i} \operatorname{ArcCsch}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\sqrt{\theta}\sqrt{-4\pi+\theta}}\right]\right\},\right. \\
& \left.\left\{\beta \rightarrow \mathbf{i} \operatorname{ArcCsch}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\sqrt{\theta}\sqrt{-4\pi+\theta}}\right]\right\}\right\} \\
& \text{Solve}\left[\mathbf{e}^{\sqrt{-\frac{\sqrt{4\pi-\theta^2}}{2\pi\sin[\beta]}}\theta} == \mathbf{e}^{\sqrt{-\frac{\sqrt{\gamma}\sqrt{4\pi+\gamma}}{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}}\theta}, \beta\right] \\
& \{\} \\
& \text{Solve}\left[\mathbf{e}^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi-\theta^2}}}\theta} == \mathbf{e}^{\sqrt{-\frac{\sqrt{\gamma}\sqrt{4\pi+\gamma}}{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}}\theta}, \beta\right] \\
& \left\{\left\{\beta \rightarrow -\operatorname{ArcCsc}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}\right]\right\},\right. \\
& \left.\left\{\beta \rightarrow \operatorname{ArcCsc}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}\right]\right\}\right\}
\end{aligned}$$

## GAMMA

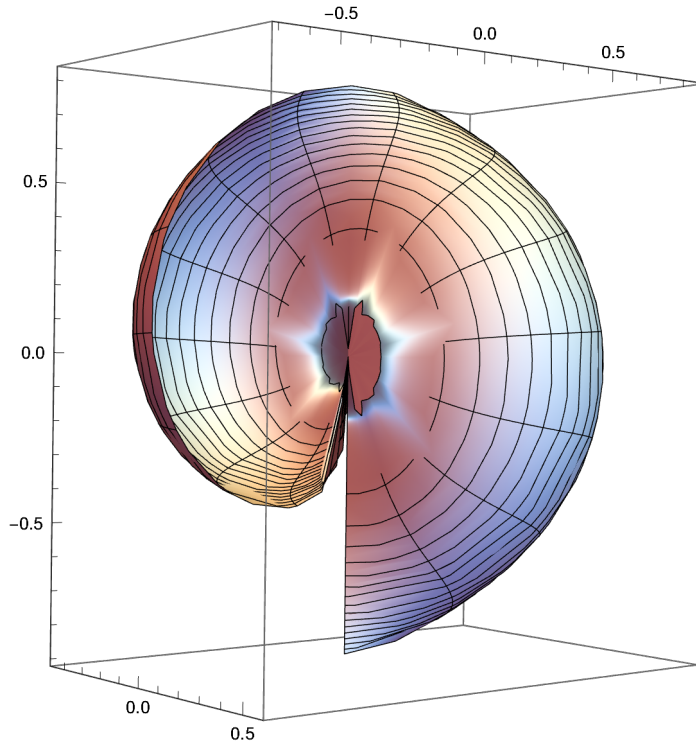
$$\begin{aligned}
& \text{Solve}\left[\mathbf{e}^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi-\theta^2}}}\theta} == \mathbf{e}^{\sqrt{-\frac{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}{\sqrt{\gamma}\sqrt{4\pi+\gamma}}}\theta}, \beta\right] \\
& \{\{\beta \rightarrow 0\}\} \\
& \text{Solve}\left[\mathbf{e}^{\sqrt{-\frac{\sqrt{4\pi-\theta^2}}{2\pi\sin[\beta]}}\theta} == \mathbf{e}^{\sqrt{-\frac{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}{\sqrt{\gamma}\sqrt{4\pi+\gamma}}}\theta}, \beta\right] \\
& \left\{\left\{\beta \rightarrow -\mathbf{i} \operatorname{ArcCsch}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\sqrt{\theta}\sqrt{-4\pi+\theta}}\right]\right\},\right. \\
& \left.\left\{\beta \rightarrow \mathbf{i} \operatorname{ArcCsch}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\sqrt{\theta}\sqrt{-4\pi+\theta}}\right]\right\}\right\}
\end{aligned}$$

$\text{SphericalPlot3D}\left[\left\{-i \operatorname{ArcCsch}\left[\frac{\sqrt{2 \pi} \left(2 \pi+\gamma\right)^{1 / 4} \left(4 \pi-\theta\right) \theta^{1 / 4}}{\gamma^{1 / 4} \left(4 \pi+\gamma\right)^{1 / 4} \sqrt{\theta} \sqrt{-4 \pi+\theta}}\right],\right.\right.$   
 $\left.i \operatorname{ArcCsch}\left[\frac{\sqrt{2 \pi} \left(2 \pi+\gamma\right)^{1 / 4} \left(4 \pi-\theta\right) \theta^{1 / 4}}{\gamma^{1 / 4} \left(4 \pi+\gamma\right)^{1 / 4} \sqrt{\theta} \sqrt{-4 \pi+\theta}}\right]\right\},\{\gamma,-2 \pi, 2 \pi\},\{\theta,-\pi / 2, \pi / 2\}\right]$

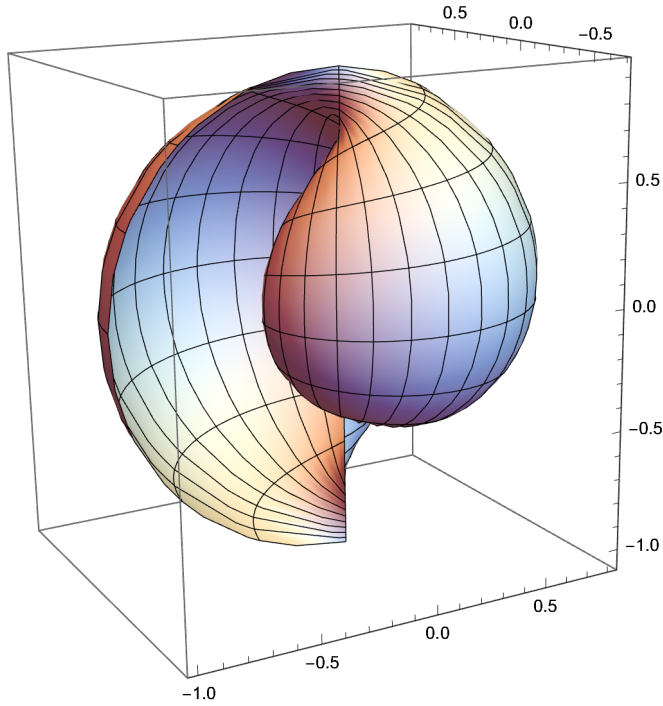




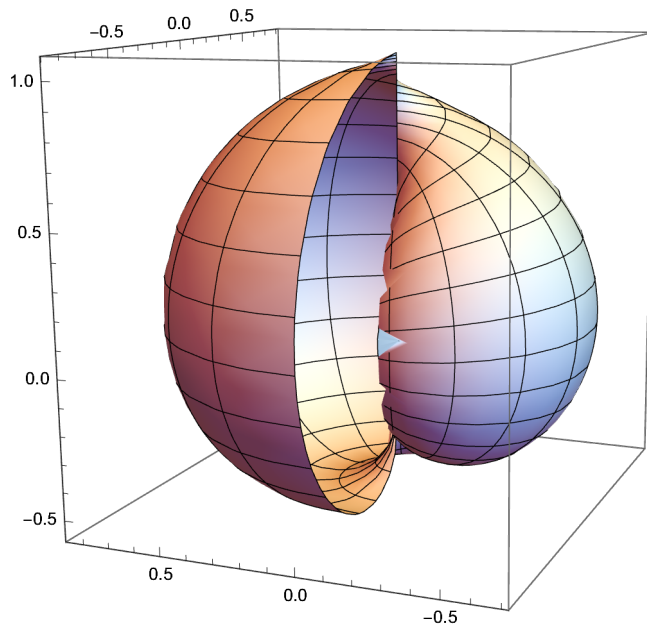
`SphericalPlot3D` $\left[\text{i ArcCsch}\left[\frac{\sqrt{2 \pi} \left(2 \pi+\gamma\right)^{1 / 4} \left(4 \pi-\theta\right) \theta^{1 / 4}}{\gamma^{1 / 4} \left(4 \pi+\gamma\right)^{1 / 4} \sqrt{\theta} \sqrt{-4 \pi+\theta}}\right],\right.$   
 $\left.\left\{\theta,-2 \pi, 2 \pi\right\},\left\{\gamma,-\pi / 2, \pi / 2\right\}\right]$



SphericalPlot3D[  
 $\frac{\sqrt{2\pi} \left( (2\pi + \gamma)^2 \right)^{1/4} \left( (4\pi - \theta) \theta \right)^{1/4}}{\gamma^{1/4} (4\pi + \gamma)^{1/4} \sqrt{\theta} \sqrt{-4\pi + \theta}}, \{\gamma, -2\pi, 2\pi\}, \{\theta, -\pi, \pi\}]$



SphericalPlot3D[  
 $\frac{\sqrt{2\pi} \left( (2\pi + \gamma)^2 \right)^{1/4} \left( (4\pi - \theta) \theta \right)^{1/4}}{\gamma^{1/4} (4\pi + \gamma)^{1/4} \sqrt{\theta} \sqrt{-4\pi + \theta}}, \{\theta, -\pi, \pi\}, \{\gamma, -2\pi, 2\pi\}]$



$$\text{Solve}\left[e^{\sqrt{-\frac{\sqrt{4\pi-\theta^2}}{2\pi\sin[\beta]}}\theta} == e^{\sqrt{-\frac{\sqrt{\gamma}\sqrt{4\pi+\gamma}}{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}}\theta}, \beta\right]$$

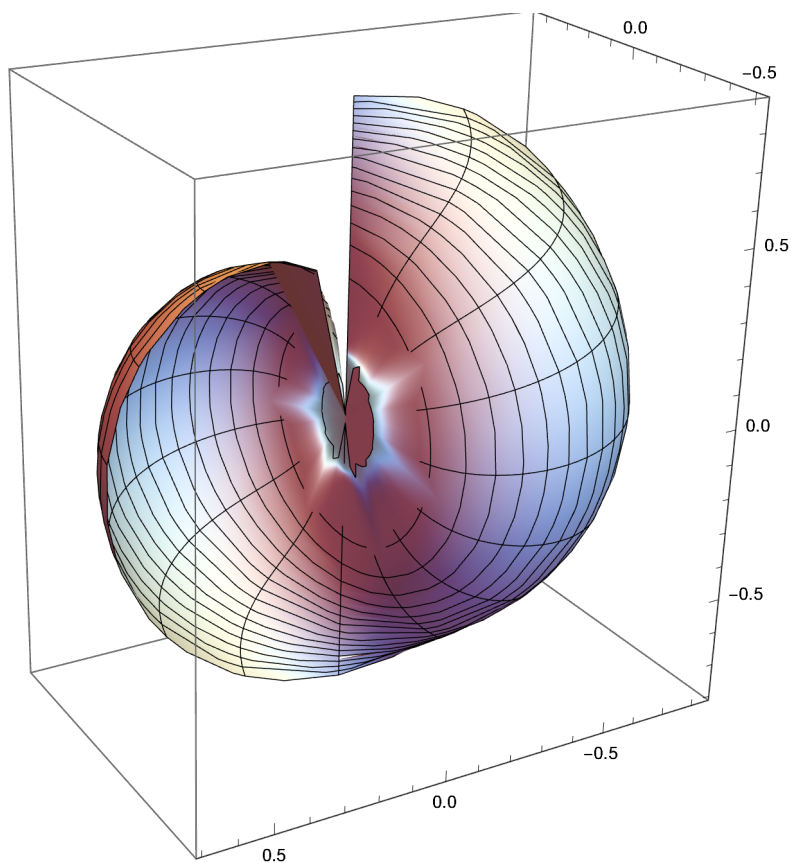
{ }

$$\text{Solve}\left[e^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi-\theta^2}}}\theta} == e^{\sqrt{-\frac{\sqrt{\gamma}\sqrt{4\pi+\gamma}}{\sqrt{4\pi^2+4\pi\gamma+\gamma^2}\sin[\beta]}}\theta}, \beta\right]$$

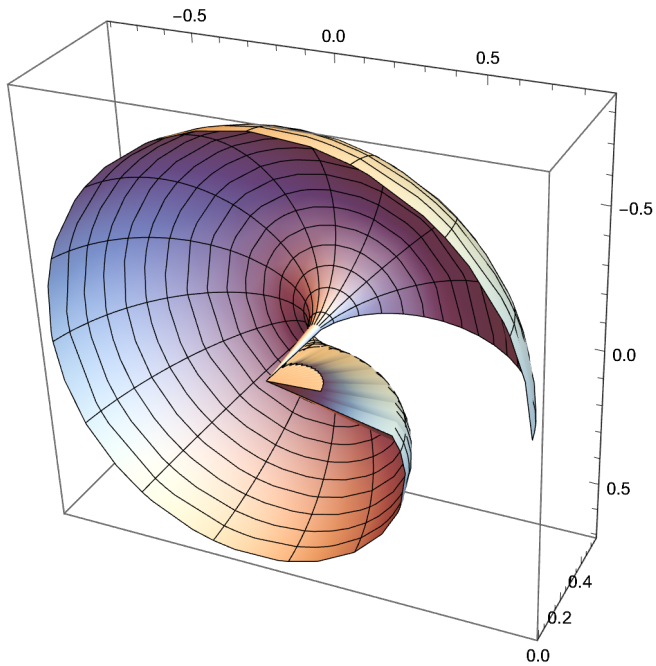
$$\left\{\left\{\beta \rightarrow -\text{ArcCsc}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}\right]\right\}\right\},$$

$$\left\{\left\{\beta \rightarrow \text{ArcCsc}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}\right]\right\}\right\}$$

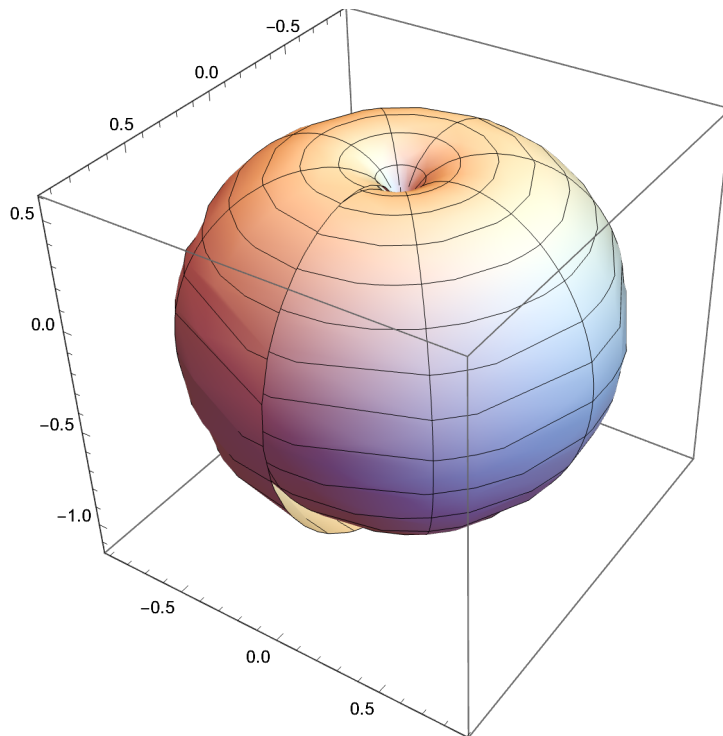
$$\text{SphericalPlot3D}\left[\text{ArcCsc}\left[\frac{\sqrt{2\pi}\left((2\pi+\gamma)^2\right)^{1/4}}{\gamma^{1/4}\left(4\pi+\gamma\right)^{1/4}\left((4\pi-\theta)\theta\right)^{1/4}}\right], \{\gamma, -2\pi, 2\pi\}, \{\theta, -\pi/2, \pi/2\}\right]$$



`SphericalPlot3D` $\left[\text{ArcCsc}\left[\frac{\sqrt{2\pi} \left(2\pi + \gamma\right)^{1/4}}{\gamma^{1/4} \left(4\pi + \gamma\right)^{1/4} \left(4\pi - \theta\right)^{1/4}}\right], \{\theta, -\pi/2, \pi/2\}, \{\gamma, -2\pi, 2\pi\}\right]$



`SphericalPlot3D` $\left[\text{ArcCsc}\left[\frac{\sqrt{2\pi} \left(2\pi + \gamma\right)^{1/4}}{\gamma^{1/4} \left(4\pi + \gamma\right)^{1/4} \left(4\pi - \theta\right)^{1/4}}\right], \{\theta, -\pi, \pi\}, \{\gamma, -4\pi, 4\pi\}\right]$



# The Geometric Pattern of Perception Theorems

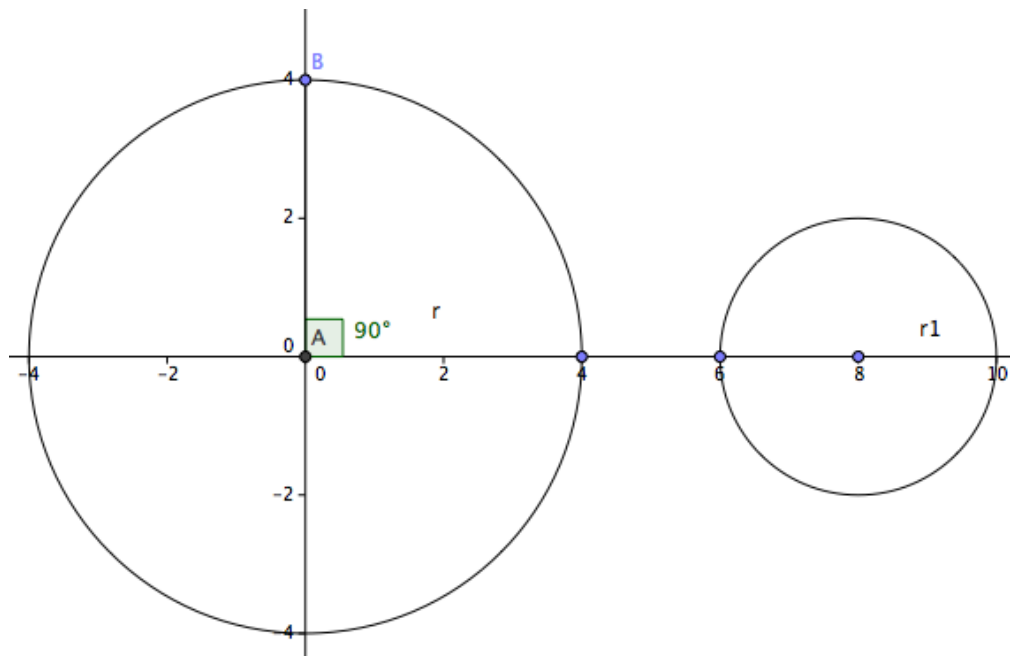
Visualization, Surfaces, and Geometry

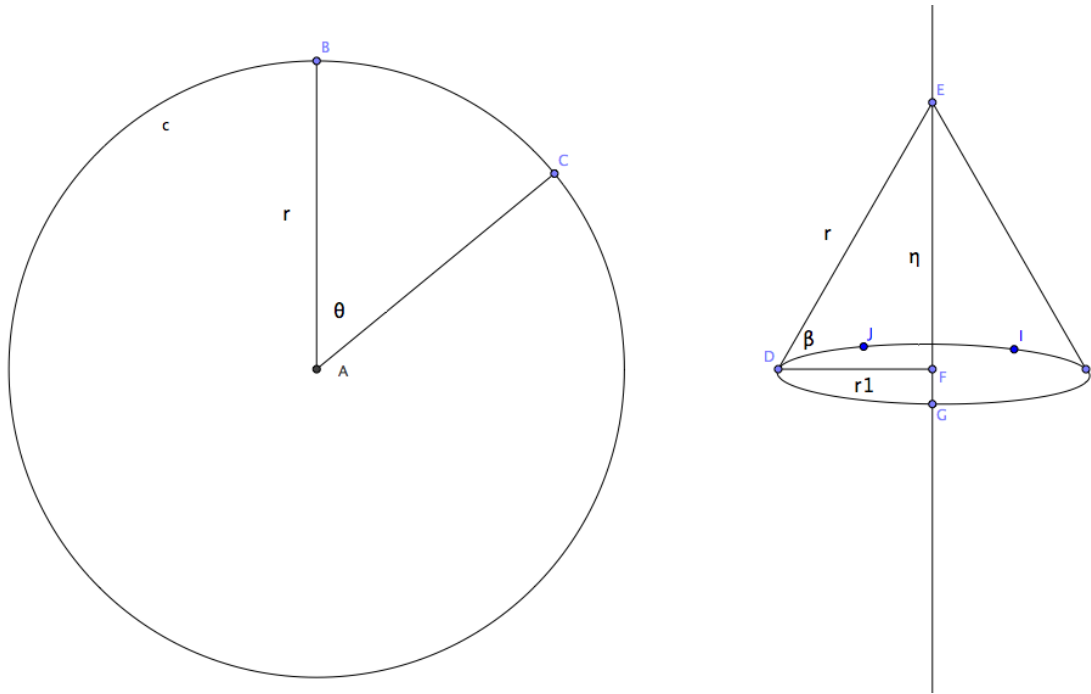
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## I. Math for Transforming a Circle into a Cone (The First Three Theorems)

by Parker Emmerson





When a sector of a circle is removed, we may "fold up" the resulting shape into a cone. The parameters are related by the following theorem :

**Theorem 1** When a sector of angle  $\theta$  is removed from a circle of radius  $r$  and the resulting shape is folded into a cone, then the base of the cone has radius  $r_1$  given by  $r_1 = r - \frac{r\theta}{2\pi}$ ; and height  $\eta$ , given by  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$

Proof. The circumference of the initial circle is  $2\pi r$  and the wedge removed has an arc length  $r\theta$ . Therefore, the remaining circumference is of length  $r(2\pi - \theta)$ , and after the fold, this is the circumference of the base of the cone.

Establishing the circumference of the base of the cone, from the equation,  $\theta r = 2\pi r - 2\pi r_1$ , we calculate that its radius  $r_1$  is  $\frac{2\pi r - r\theta}{2\pi}$ , which simplifies to  $r - \frac{r\theta}{2\pi}$ . Thus, we have proved the first part of the theorem.

To find the height of the cone,  $\eta$ , we apply the Pythagorean theorem to a right triangle formed between the apex of the cone, the center of the base, and a point on the circumference of the base. This gives  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$ , where  $\beta$  is the angle formed by the slant of the cone and the base of the cone. The initial radius is always equal to the slant of the cone, and the height of the cone is always orthogonal to the center of the base of the cone.

**Lemma 1** The height of the cone can be calculated in terms of  $r$  and  $\theta$ .

Proof.

$$\theta r = 2\pi r - 2\pi r_1$$

$$\eta = \sqrt{r^2 - r_1^2}$$

$$\theta r = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$$

Solving this equation we find that,

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\}$$

**Lemma 2** The angle  $\theta$  can be calculated in terms of  $r$  and  $\eta$ .

Proof

$$\text{Solve}\left[\eta == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{r^4 - r^2 \eta^2})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}\right\}\right\}$$

**Lemma 3** The initial radius is a function of  $\theta$  and  $\eta$ .

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} == \eta, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}\right\}$$

**Lemma 4** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\beta$  is a function of  $\theta$  alone.

Proof. Since we have shown that  $\theta r = 2\pi r - 2\pi r_1$  and  $r_1 \rightarrow \sqrt{r^2 - \eta^2}$ , we can substitute the expression for  $r_1$ , calculated from the Pythagorean theorem in terms of the height of the cone and the initial radius of the circle, into the expression for  $\theta r$  in terms of the change in circumference of the initial circle to the circle that is the base of the cone into which the circle was transformed.

$\theta r = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$ , thus,  $\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = (r \sin[\beta])$ . From  $\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r$ , we note that:  $r = \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}$ . So we solve the equation,

$$\text{Solve}\left[r == \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right\}\right\}$$

**Lemma 5** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\theta$  is a function of  $\beta$  alone.

Proof. Since we have shown that  $\theta r = 2\pi r - 2\pi r_1$  and  $r_1 \rightarrow \sqrt{r^2 - \eta^2}$ , we can substitute the expression for  $r_1$ , calculated from the Pythagorean theorem in terms of the height of the cone and the initial radius of the circle, into the expression for  $\theta r$  in terms of the change in circumference of the initial circle to the circle that is the base of the cone into which the circle was transformed.

$\theta r = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$ , thus,  $\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = (r \sin[\beta])$ . From  $\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r$ , we note that:  $r = \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}$ . So we solve the equation,

$$\text{Solve}\left[r == \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$$

**Lemma 6** The initial radius can be calculated purely in terms of the angle  $\theta$ .

Proof. From Lemma 1, the height of the cone has been solved in terms of the transformation. That expression for the height divided by the initial radius is set equal to the sine of  $\beta$ . Solving that equation yields an expression for  $\beta$  that includes  $r$ . This expression for  $\beta$  is then set equal to the expression found from Lemma 5.

$$\sin[\beta] = \frac{\eta}{r} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{r 2\pi} = \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2 r} = \frac{r(4\pi - \theta)\theta}{4\pi^2}$$

$$\beta \rightarrow \text{ArcSin}\left[\frac{4\pi r \theta - r \theta^2}{4\pi^2}\right] = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

$$\text{Solve}\left[\text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right] == \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], r\right]$$

$$\left\{\left\{r \rightarrow \frac{2\pi\sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}\right\}\right\}$$

Commentary of Lemma 6. Matt Ollis pointed out to me that my final lemma to this section cannot be proved through Euclidean geometry, reasoning that because a circle of any radius and any angle taken out of it can be made, this statement cannot be proven. I initially proposed that the initial radius is not dependent on theta, so how can it be shown that it is? In any sufficiently logical system (as pointed out by Kurt Gödel in his famous, first incompleteness theorem), there is always a statement that is true, but cannot be proven. This resolves the paradox of why this algebraic-geometric phenomenon takes place - Euclidean geometry and algebra are sufficiently logical systems, and I assert that Lemma 6 is true, but not provable by Euclidean geometry (the system to which this mathematics belongs).

### A note about time passing like a clock.

The elapse of one unit of time,  $t$ , can be expressed by a constant function of the angle  $\theta$ . The simplest expression is  $t$  (seconds) =  $\frac{\theta}{2\pi}$ ;  $\theta = kt$ , where  $k$  is  $2\pi$ , because one unit of time is equal to one revolution of  $\theta$  through a circle. But what is so strange, is that at  $2\pi$ , there is no angle, because the cone has totally collapsed into a distance orthogonal to the center of the base of the initial circle. But it's actually alright to measure time like this, because the initial radius can rotate  $2\pi$  degrees and act as a signifier of a total revolution at the position of  $\theta = 2\pi$ .

Proof.  $\theta r = 2\pi r - 2\pi(r - rt)$  yields  $t = \frac{\theta}{2\pi}$ .

**Theorem 2** When we designate that a single unit of time passes per revolution of the angle through the total number of radians in a circle, instantaneous velocity through the distance of the height of the cone can be found by taking the first derivative of the expression for that distance, which is in terms of  $r$  and  $\theta$ , with respect to  $t = \frac{\theta}{2\pi}$ . There is also a velocity through the height of the cone, which is equal to wavelength times frequency =  $\lambda f = \frac{\eta}{\left(\frac{\theta}{2\pi}\right)}$  considered the average velocity through the height of the cone. Under the condition that one unit of time passes with one revolution of the circle, these two velocities are equal to each other at the position where a 30-60-90 triangle is formed between the apex, center of the base of the cone, and point on the circumference of the circle of the base of the cone.

Proof.

To prove this, we can substitute  $r \sin[\beta]$  for the height of the cone in the expression of velocity =  $((2\pi\eta)/\theta)$  and find a real and two complex solutions for theta in terms of  $\beta$ , thus from Lemma 4, we can solve for  $\beta$  exactly.

$$\text{Instantaneous Velocity} = \frac{d\eta}{dt} = \frac{d\eta}{d\left(\frac{\theta}{2\pi}\right)} =$$

$$D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, t\right] = D\left[k \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right] = D\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right] = \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}$$

$$\text{Average Velocity} = (\eta / (\theta / 2\pi))$$

$$\text{Instantaneous Velocity} = \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}} = \text{Average Velocity} = \frac{2\pi\eta}{\theta}$$

$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}} == \frac{2\pi\eta}{\theta}, \theta\right]$$



$$\begin{aligned}
& \left\{ \left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}} - \frac{2\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}}{3r^2} \right\}, \right. \\
& \left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{(1+i\sqrt{3})(-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2)}{12\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}} + \frac{(1-i\sqrt{3})\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}}{3r^2} \right\}, \\
& \left. \left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{(1-i\sqrt{3})(-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2)}{12\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}} + \frac{(1+i\sqrt{3})\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}}{3r^2} \right\} \right\} \\
& \text{Solve} \left[ \frac{k(4\pi r^2 - 2r^2 \theta)}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}} = \frac{kr \sin[\beta]}{\theta}, \theta \right] \\
& \left\{ \left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{-4\pi^2 + 12\pi^2 \sin[\beta]^2}{6(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} + \right. \right. \\
& \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}, \\
& \left. \left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{(1+i\sqrt{3})(-4\pi^2 + 12\pi^2 \sin[\beta]^2)}{12(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} - \right. \right. \\
& \frac{1}{3} \left( 1-i\sqrt{3} \right) \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}, \\
& \left. \left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{(1-i\sqrt{3})(-4\pi^2 + 12\pi^2 \sin[\beta]^2)}{12(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} - \right. \right. \\
& \left. \left. \frac{1}{3} \left( 1+i\sqrt{3} \right) \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right\} \right\}
\end{aligned}$$

The real solution for  $\theta$ , solved from equating the instantaneous velocity to the average velocity, can be equated with the real solution for the expression for  $\theta$  from Lemma 4 to yield an exact solution for  $\beta$  that tells us that when these solutions for theta are equal, a 30-60-90 triangle is formed between the azimuth of the cone, the point on the base of the cone and the center of the base of the cone.

$$\begin{aligned}
& \text{Solve} \left[ \frac{4\pi}{3} - \frac{-4\pi^2 + 12\pi^2 \sin[\beta]^2}{6(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} + \right. \\
& \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} = \\
& \left. 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), \beta \right] \\
& \left\{ \left\{ \beta \rightarrow -\frac{\pi}{3} \right\}, \left\{ \beta \rightarrow \frac{\pi}{3} \right\} \right\}
\end{aligned}$$

We know that the height of the cone is perpendicular to the center of the base of the cone, so this proves a 30-60-90 triangle, because the sum of the angles of the triangle must be 180 degrees or  $\pi$  radians.

**Lemma 7** We can show that  $\beta = \frac{\pi}{3}$ , thus we can show that there are two solutions to  $\theta$  at which this occurs.

**Proof.**

$$\text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] = \beta$$

$$\text{Solve}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right] == \frac{\pi}{3}, \theta\right]$$

$$\{\{\theta \rightarrow \pi\}, \{\theta \rightarrow 3\pi\}\}$$

**Lemma 8** We can show can show that the position at which instantaneous rate of change of the height of the cone with respect to theta equals average rate of change of the height of the cone, 'per theta measure,' at

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi\theta^2-\theta^3}}{2\pi\sqrt{-4\pi+\theta}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi\theta^2-\theta^3}}{2\pi\sqrt{-4\pi+\theta}}\right]\right\}\right\}.$$

**Proof.**

$$\text{Solve}\left[\theta == \frac{4\pi}{3} - \frac{-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2}{6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}} + \frac{2}{3}\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi\theta^2-\theta^3}}{2\pi\sqrt{-4\pi+\theta}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi\theta^2-\theta^3}}{2\pi\sqrt{-4\pi+\theta}}\right]\right\}\right\}$$

**Theorem 3** The "innate velocity,"  $v$ , within the Lorentz transformation can be solved for in terms of the system of the circle transforming into a cone. If  $r$  is multiplied by the Lorentz transformation, then it measures the distance in the prime system, denoted by  $r'$ . If  $t'$  equals

$$\frac{\left(\frac{\theta}{(2\pi)}\right)}{\sqrt{1 - \left(\frac{v^2}{c^2}\right)}}, \text{ then the quantity } r\theta = \theta' r'. \text{ We are only dealing with algebraic forms and the solutions necessitated by them. Logical, algebraic,}$$

reasoning will be given why, when using the exact speed of light, 2.99792458 ( $10^8$ ) meters per second, the units of the speed of light can be ignored for the purposes of calculation and computation. This theorem states that, although, normal algebra would require the speed of light as a quantity to cancel out, valid expressions for the solutions for the intrinsic velocity,  $v$ , can be found in terms of  $\eta$ ,  $r$ , and  $\theta$ , or  $\theta$  and  $\beta$ , depending on the expression used for the height of the cone.

**Proof.**

$$c = 2.99792458 \left(10^8\right) \text{ meters per second}$$

$$r' = r \sqrt{1 - \frac{v^2}{c^2}}$$

$$t' = \frac{\left(\frac{\theta}{(2\pi)}\right)}{\sqrt{1 - \left(\frac{v^2}{c^2}\right)}}$$

$$t' = \frac{\theta'}{2\pi}$$

$$2\pi t' = \theta'$$

$$\theta' = \frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Therefore,

$$r' * \theta' = \left( \frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}} \right) \left( r \sqrt{1 - \frac{v^2}{c^2}} \right)$$

$$\left( \frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}} \right) \left( r \sqrt{1 - \frac{v^2}{c^2}} \right) = r \theta$$

$$r' * \theta' = r \theta = 2 \pi r - 2 \pi r_1 = 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}$$

$$\text{Solve}[r \theta == 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4 \pi^2 r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4 \pi^2 r^2 \theta - r^2 \theta^2}}{2 \pi} \right\} \right\}$$

$$\text{Solve}[r' \theta' == 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{r'} \sqrt{\theta'} \sqrt{4 \pi r - r' \theta'}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{r'} \sqrt{\theta'} \sqrt{4 \pi r - r' \theta'}}{2 \pi} \right\} \right\}$$

The argument follows modus ponens, saying that, through commutation,  $r' \theta' = \theta r$ , therefore  $\eta =$

$$\frac{\sqrt{r'} \sqrt{\theta'} \sqrt{4 \pi r - r' \theta'}}{2 \pi} = \frac{\sqrt{4 \pi^2 r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\eta = \frac{\sqrt{r'} \sqrt{\theta'} \sqrt{4 \pi r - r' \theta'}}{2 \pi} = \frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \sqrt{1 - \frac{v^2}{c^2}} \frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}}}{2 \pi} = \frac{\sqrt{r \theta} \sqrt{4 \pi r - r \theta}}{2 \pi}$$

where c is its numeric value of the speed of light, its units being shown to cancel out.

$$\frac{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}}{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} = \frac{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}}{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} = \sqrt{\frac{1 - \frac{v^2}{(c)^2}}{1 - \frac{v^2}{(c)^2}}}$$

$$\text{Solve}\left[\sqrt{\frac{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} = \sqrt{\frac{1 - \frac{v^2}{(c)^2}}{1 - \frac{v^2}{(c)^2}}}, \text{meters}\right]$$

{{}}

$$\text{Solve}\left[\sqrt{\frac{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} = \sqrt{\frac{1 - \frac{v^2}{(c)^2}}{1 - \frac{v^2}{(c)^2}}}, \text{second}\right]$$

{{}}

$$\text{Solve}\left[\sqrt{\frac{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} = \sqrt{\frac{1 - \frac{v^2}{(c)^2}}{1 - \frac{v^2}{(c)^2}}}, v\right]$$

{{}}

$$\text{Solve}\left[\sqrt{\frac{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} = \sqrt{\frac{1 - \frac{v^2}{(c)^2}}{1 - \frac{v^2}{(c)^2}}}, c\right]$$

$$\text{Solve}[\text{True}, 2.99792 \times 10^8]$$

$$\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} =$$

$$(1) \frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c)^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{(c)^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi}$$

Logically, the units of the speed of light will cancel out, therefore, their relationship will be set equal to one and taken out of the equation for the purposes of computational calculation.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = \eta, \text{ meters}\right]$$

{{}}

Meters cancel out.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = \eta, \text{ second}\right]$$

{{}}

Seconds cancel out.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = \eta, c\right]$$

{{}}

The numeric c cancels out.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}} \sqrt{\frac{\theta}{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}\right\}$$

Radius yields the result from Lemma 3.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}} \sqrt{\frac{\theta}{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, v\right]$$

$$\{\}$$

Velocity cancels out.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c)^2}} \sqrt{\frac{\theta}{1 - \frac{v^2}{(c)^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, v\right]$$

$$\{\}$$

**Velocity cancels out. Everything *cancels out*. Only when using the exact speed of light in scientific notation can solutions to the innate velocity be found.**

We set the speed of light equal to its numeric value for the purpose of making computations, dropping the units, because in the expression for the height of the cone, they would cancel out anyway. It should be noted that this is necessary for computing the function of the velocity and that the exact speed of light is to be used as well as that the numeric value of the speed of light has to be in the form of scientific notation in order to find results to this equation.

**Theorem 3 Continued** From the expression of the height of the cone of Lemma 1, with the Lorentz transformations implicitly expressed, we can solve for the velocity within the Lorentz coefficient in terms of the height of the cone, the initial radius, and the angle,  $\theta$  when using the exact speed of light in scientific notation and only when it is its exact (or extremely closely approximated) value expressed in scientific notation.

Proof.

$$c := 2.99792458 * (10^8)$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{(v)^2}{c^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{3.54814 \times 10^{18} \eta^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 \eta^2 - 12.5664 r^2 \theta + r^2 \theta^2}}\right\}, \right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{3.54814 \times 10^{18} \eta^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 \eta^2 - 12.5664 r^2 \theta + r^2 \theta^2}}\right\}\right\}$$

**Theorem 3 Continued** From the expression of the height of the cone, from Lemma 1 with the Lorentz transformations implicitly expressed, we can solve for the velocity within the Lorentz coefficient in terms of  $\theta$  and  $\beta$ .

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{(v)^2}{c^2}}} \sqrt{4\pi r - r\theta}}{2\pi} = r \sin[\beta], v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{1. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right\} \right\}$$

## BREAKING RESULTS.... !

{Phenomenal Velocity = Instantaneous Velocity of the Height of the Cone} at the following solutions.

The "phenomenal velocity," described in Theorem 3, equals the instantaneous velocity of the height of the cone at the following positions.

So, we have

$$\frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} =$$

$$\frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} \quad (76)$$

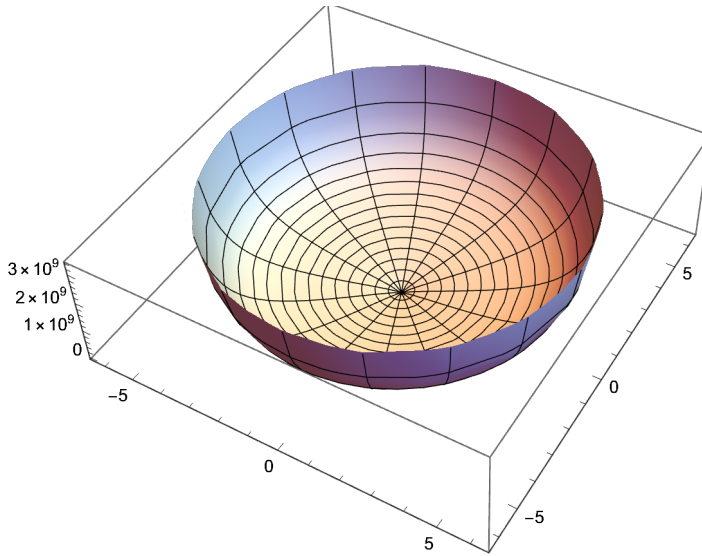
$$\text{Solve}\left[\left(\sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \times 10^0 \theta + \theta^2 + 39.47841760435743 \times 10^0 \sin[\beta]^2}\right) = \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{1. \sqrt{6.91664 \times 10^{33} - 5.50409 \times 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.41771 \times 10^{17} - 7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2}} \right\}, \right.$$

$$\left. \left\{ r \rightarrow \frac{\sqrt{6.91664 \times 10^{33} - 5.50409 \times 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.41771 \times 10^{17} - 7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2}} \right\} \right\}$$

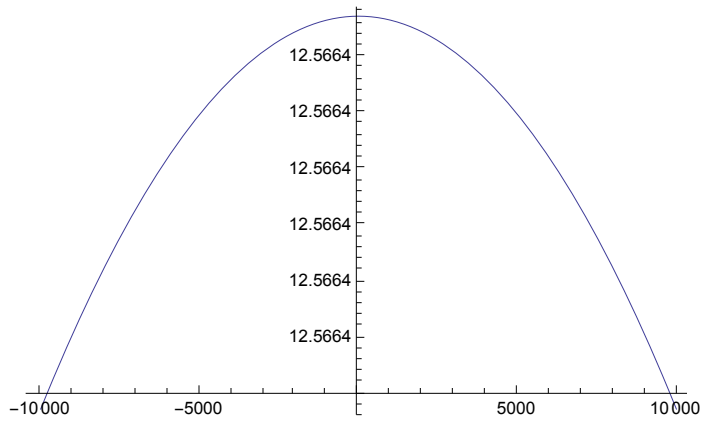
RevolutionPlot3D[  

$$\frac{\sqrt{6.916640561054567 \cdot 10^{33} - 5.504087674408674 \cdot 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.4177070339300032 \cdot 10^{17} - 7.695800507960096 \cdot 10^{16} \theta + 6.124123459454841 \cdot 10^{15} \theta^2}},$$
  
 $\{\theta, -2\pi, 2\pi\}]$



Solve[ $\left(\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) /$   
 $\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) ==$   
 $\frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}}, \theta]$   
 $\left\{\left\{\theta \rightarrow \frac{0.5 \left(6.91664 \times 10^{33} + 7.6958 \times 10^{16} r^2 - 2.30714 \times 10^{25} \sqrt{8.98755 \times 10^{16} + 1. r^2}\right)}{5.50409 \times 10^{32} + 6.12412 \times 10^{15} r^2}\right\},\right.$   
 $\left.\left\{\theta \rightarrow \frac{0.5 \left(6.91664 \times 10^{33} + 7.6958 \times 10^{16} r^2 + 2.30714 \times 10^{25} \sqrt{8.98755 \times 10^{16} + 1. r^2}\right)}{5.50409 \times 10^{32} + 6.12412 \times 10^{15} r^2}\right\}\right\}$

```
Plot[ (0.5` (6.916640561054567` * ^33 + 7.695800507960096` * ^16 r^2 +
2.3071429505590057` * ^25 sqrt(8.987551787368176` * ^16 + 1.` r^2)) ) /
(5.504087674408674` * ^32 + 6.124123459454841` * ^15 r^2), {r, -10 000, 10 000}]
```

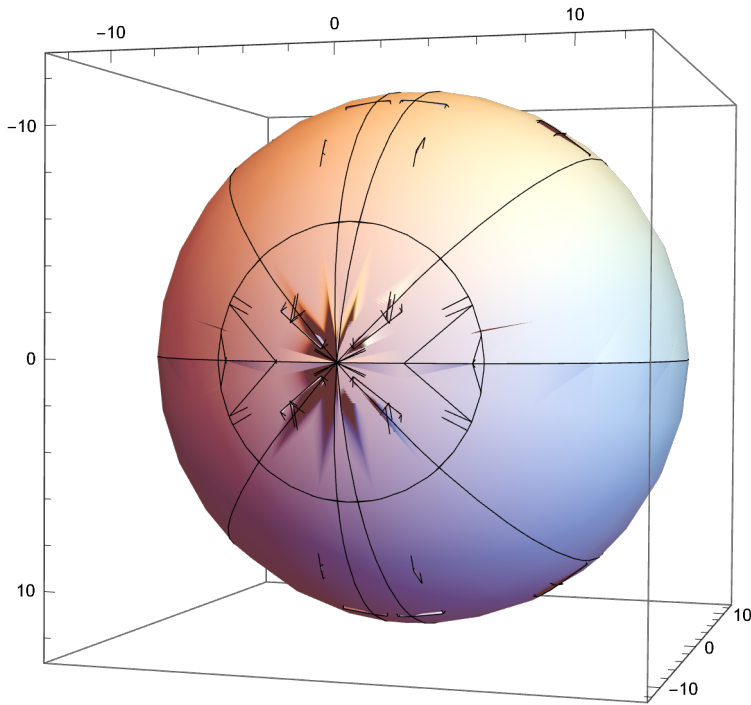


Many more possible substitutions for this solution, but here is an example so we can go 3 D.



SphericalPlot3D[

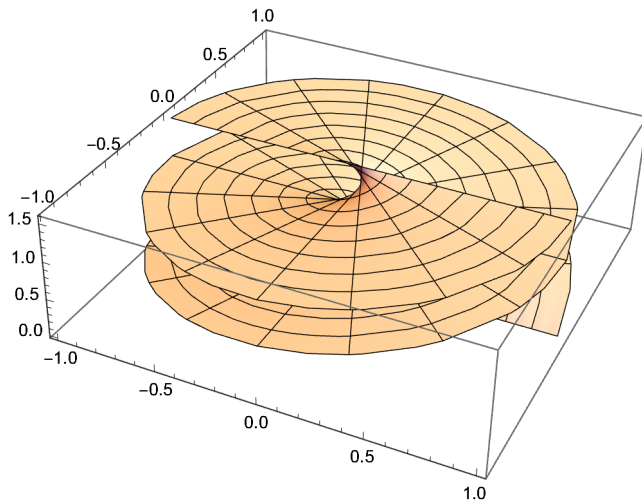
$$\left( 0.5 \left( 6.916640561054567 \cdot 10^{33} + 7.695800507960096 \cdot 10^{16} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 + \right. \right. \\ \left. \left. 2.3071429505590057 \cdot 10^{25} \sqrt{8.987551787368176 \cdot 10^{16} + 1. \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2} \right) \right) / \\ \left( 5.504087674408674 \cdot 10^{32} + 6.124123459454841 \cdot 10^{15} \right. \\ \left. \left( \frac{2 \pi \sqrt{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))} 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})) 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \right)^2 \right), \\ \{\theta, -2 \pi, 2 \pi\}, \{\beta, -2 \pi, 2 \pi\} \]$$



This one flickers a lot - even in revolution plot.

$$\begin{aligned}
& \text{Solve}\left[\left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right.}\right. \\
& \quad \left.8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)\right) / \\
& \quad \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) == \\
& \quad \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \beta\right] \\
& \left\{\left\{\beta \rightarrow -1. \text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{\left(1.08487 \times 10^{33} r^2 - 3.10363 \times 10^{49} \theta - 4.31657 \times 10^{32} r^2 \theta + 4.93958 \times 10^{48} \theta^2 + \right.}\right. \right.\right. \\
& \quad \left.5.49602 \times 10^{31} r^2 \theta^2 - 1.9654 \times 10^{47} \theta^3 - 2.1868 \times 10^{30} r^2 \theta^3\right)\right) / \\
& \quad \left(\sqrt{\left(3.40822 \times 10^{33} r^2 - 9.75034 \times 10^{49} \theta - 1.08487 \times 10^{33} r^2 \theta + \right.}\right. \\
& \quad \left.7.75907 \times 10^{48} \theta^2 + 8.63313 \times 10^{31} r^2 \theta^2\right)}\right)\right\}, \\
& \left\{\beta \rightarrow \text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{\left(1.08487 \times 10^{33} r^2 - 3.10363 \times 10^{49} \theta - 4.31657 \times 10^{32} r^2 \theta + \right.}\right. \right.\right. \\
& \quad \left.4.93958 \times 10^{48} \theta^2 + 5.49602 \times 10^{31} r^2 \theta^2 - 1.9654 \times 10^{47} \theta^3 - 2.1868 \times 10^{30} r^2 \theta^3\right)\right) / \\
& \quad \left(\sqrt{\left(3.40822 \times 10^{33} r^2 - 9.75034 \times 10^{49} \theta - 1.08487 \times 10^{33} r^2 \theta + \right.}\right. \\
& \quad \left.7.75907 \times 10^{48} \theta^2 + 8.63313 \times 10^{31} r^2 \theta^2\right)}\right)\right)\right\}
\end{aligned}$$

$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{\left(1.0848712769677502 \cdot 10^{33} r^2 - \right.}\right. \right.\right. \\
& \quad 3.10362859208832 \cdot 10^{49} \theta - 4.3165656586958524 \cdot 10^{32} r^2 \theta + \\
& \quad 4.9395783195219584 \cdot 10^{48} \theta^2 + 5.496022094097345 \cdot 10^{31} r^2 \theta^2 - \\
& \quad 1.965395765853693 \cdot 10^{47} \theta^3 - 2.186797709044656 \cdot 10^{30} r^2 \theta^3\right)\right) / \\
& \quad \left(\sqrt{\left(3.4082236338124617 \cdot 10^{33} r^2 - 9.7503367843759 \cdot 10^{49} \theta - \right.}\right. \\
& \quad 1.0848712769677502 \cdot 10^{33} r^2 \theta + 7.7590714802208 \cdot 10^{48} \theta^2 + \\
& \quad \left.8.633131317391704 \cdot 10^{31} r^2 \theta^2\right)}\right)\right], \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}
\end{aligned}$$



And we also have,

$$\frac{\sqrt{3.54814 \times 10^{18} \eta^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 \eta^2 - 12.5664 r^2 \theta + r^2 \theta^2}} == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \quad (77)$$

$$\text{Solve}\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right) == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \eta\right]$$

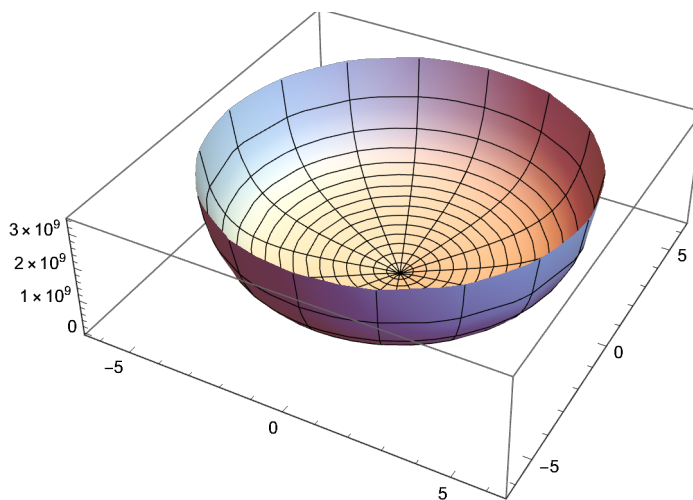
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$$\text{Solve}\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right) == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{1. \sqrt{3.20712 \times 10^{55} - 2.55214 \times 10^{54} \theta} \sqrt{\theta}}{\sqrt{1.12105 \times 10^{39} - 3.5684 \times 10^{38} \theta + 2.83964 \times 10^{37} \theta^2}}\right\},\right.$$

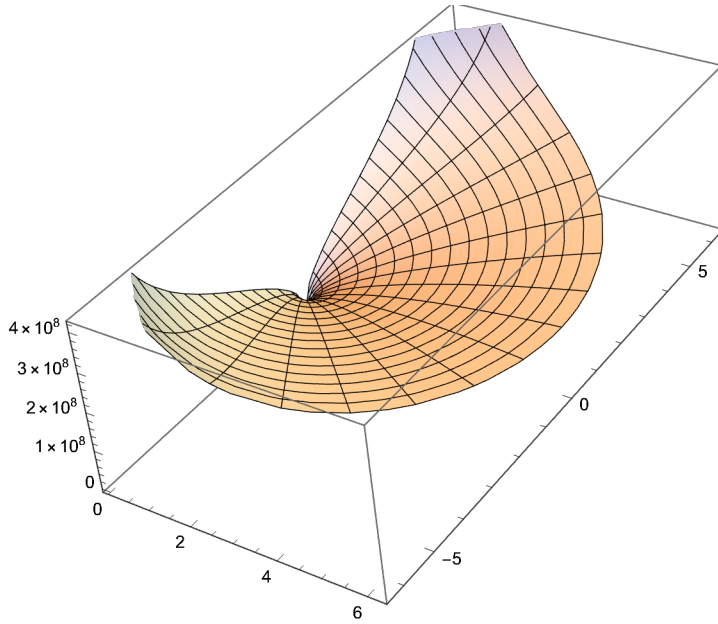
$$\left.\left\{r \rightarrow \frac{\sqrt{3.20712 \times 10^{55} - 2.55214 \times 10^{54} \theta} \sqrt{\theta}}{\sqrt{1.12105 \times 10^{39} - 3.5684 \times 10^{38} \theta + 2.83964 \times 10^{37} \theta^2}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{3.207116365345587 \cdot 10^{55} - 2.552142113078316 \cdot 10^{54} \theta} \sqrt{\theta}}{\sqrt{1.1210453581739739 \cdot 10^{39} - 3.568398203672245 \cdot 10^{38} \theta + 2.8396410651733885 \cdot 10^{37} \theta^2}}, \{\theta, -2 \pi, 2 \pi\}\right]$$

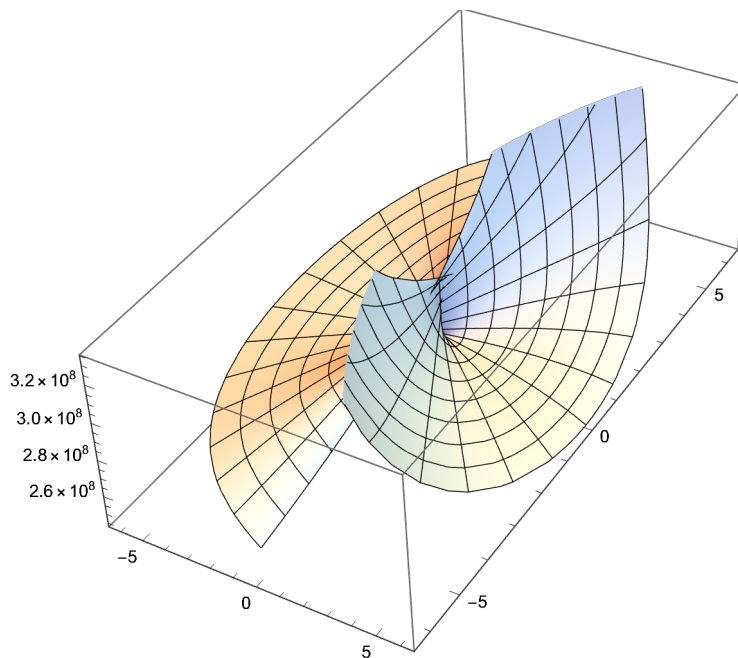


$$\text{Substitution : } \theta = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$\text{RevolutionPlot3D}\left[\left(\sqrt{3.207116365345587 \cdot 10^{55} - 2.552142113078316 \cdot 10^{54} \theta} \sqrt{\theta}\right) / \right.$   
 $\left.\sqrt{\left(1.1210453581739739 \cdot 10^{39} - 3.568398203672245 \cdot 10^{38} \theta + 2.8396410651733885 \cdot 10^{37} \right.}\right.$   
 $\left.\left.2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)^2\right)\right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$



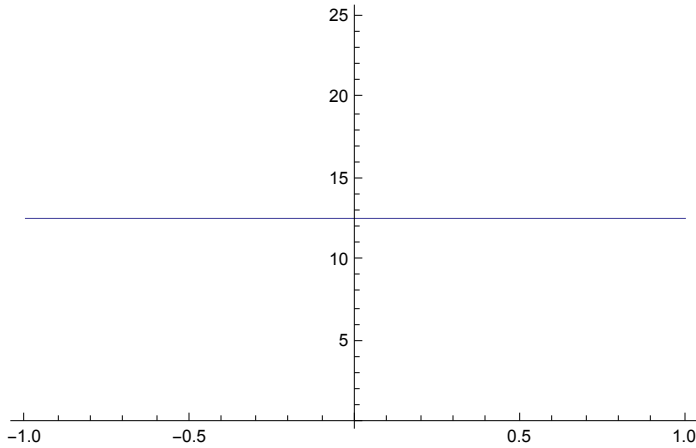
$\text{RevolutionPlot3D}\left[\left(\sqrt{3.207116365345587 \cdot 10^{55} - 2.552142113078316 \cdot 10^{54} \theta} \sqrt{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}\right) / \left(\sqrt{\left(1.1210453581739739 \cdot 10^{39} - 3.568398203672245 \cdot 10^{38} \theta + 2.8396410651733885 \cdot 10^{37} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)}\right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



$\text{Solve}\left[\left(\sqrt{3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2}\right) / \left(\sqrt{39.47841760435743 \cdot 10^2 - 12.566370614359172 \cdot 10^2 r^2 \theta + r^2 \theta^2}\right) == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta\right]$

$\left\{\left\{\theta \rightarrow \frac{0.5 \left(3.20712 \times 10^{55} + 3.5684 \times 10^{38} r^2 - 1.06978 \times 10^{47} \sqrt{8.98755 \times 10^{16} + 1. r^2}\right)}{2.55214 \times 10^{54} + 2.83964 \times 10^{37} r^2}\right\}, \left\{\theta \rightarrow \frac{0.5 \left(3.20712 \times 10^{55} + 3.5684 \times 10^{38} r^2 + 1.06978 \times 10^{47} \sqrt{8.98755 \times 10^{16} + 1. r^2}\right)}{2.55214 \times 10^{54} + 2.83964 \times 10^{37} r^2}\right\}\right\}$

Plot[ $\left(0.5 \left(3.207116365345587 \cdot 10^{55} + 3.568398203672245 \cdot 10^{38} r^2 + 1.069778868601687 \cdot 10^{47} \sqrt{8.987551787368176 \cdot 10^{16} + 1. \cdot 10^{16} r^2}\right)\right) / (2.552142113078316 \cdot 10^{54} + 2.8396410651733885 \cdot 10^{37} r^2), \{r, -1, 1\}$ ]



{Phenomenal Velocity = Average Velocity of the Height of the Cone} at the following solutions.

$$\frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} = \frac{2 \pi \eta}{\theta} \quad (78)$$

$$\text{Solve}\left[\frac{2 \pi \eta}{\theta} = \left(\sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2)}\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right), \eta\right]$$

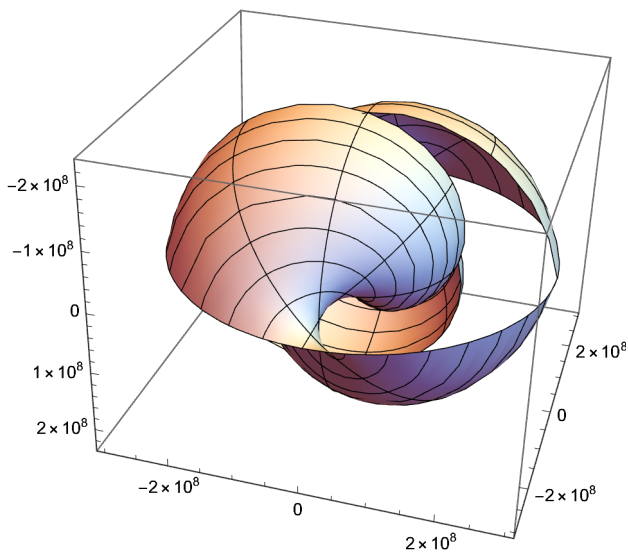
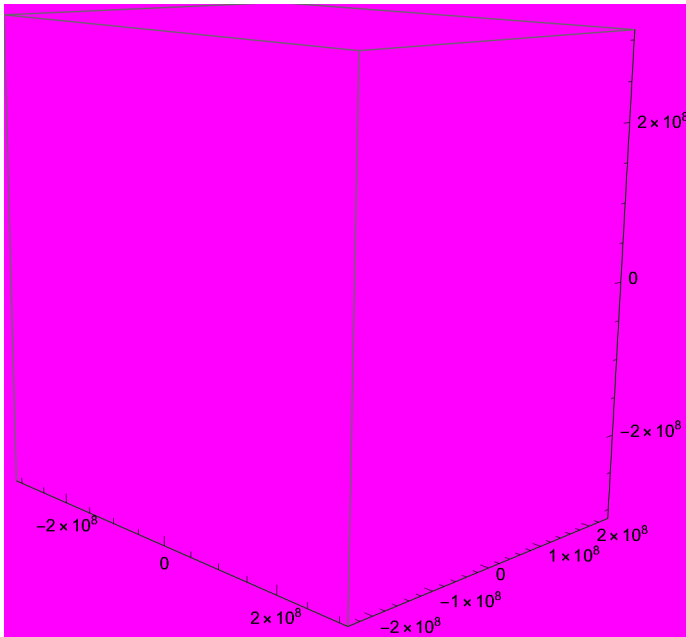
$$\{\{\eta \rightarrow 4.77135 \times 10^7 \theta\}\}$$

$$\text{Solve}\left[\frac{2 \pi \eta}{\theta} = \left(\sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2)}\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right), r\right]$$

$$\{\}$$

$$\begin{aligned}
& \text{Solve}\left[\frac{2\pi\eta}{\theta} == \left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} \eta^2 - \right.}\right. \right. \\
& \quad \left. \left. 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)\right) / \\
& \quad \left(\sqrt{39.47841760435743 \cdot 10^{18} \eta^2 - 12.566370614359172 \cdot 10^{18} r^2 \theta + 10^{18} r^2 \theta^2}\right), \theta] \\
& \left\{\left\{\theta \rightarrow 2.09585 \times 10^{-8} \eta\right\}\right\} \\
& \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} == \frac{2\pi\eta}{\theta} \tag{79} \\
& \text{Solve}\left[\frac{2\pi\eta}{\theta} == \left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + \right.}\right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right) / \\
& \quad \left(\sqrt{-12.566370614359172 \cdot 10^{18} \theta + 10^{18} \theta^2 + 39.47841760435743 \cdot 10^{18} \sin[\beta]^2}\right), \eta] \\
& \left\{\left\{\eta \rightarrow \frac{0.159155 \theta \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}}\right\}\right\}
\end{aligned}$$

```
SphericalPlot3D[
  (0.15915494309189535`  $\theta$   $\sqrt{(-1.1294090667581471` \ast^{18} \theta + 8.987551787368176` \ast^{16} \theta^2 +$ 
     $3.5481432270250993` \ast^{18} \text{Sin}[\beta]^2)$ )) /
  ( $\sqrt{-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2}$ ),
  { $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }, { $\theta$ ,  $-2\pi$ ,  $2\pi$ }, PlotStyle  $\rightarrow$  Opacity[.5]]
```





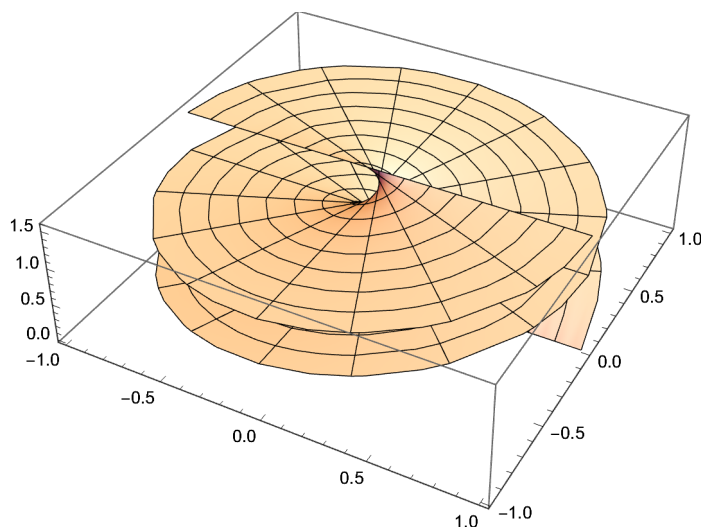
$$\text{Solve}\left[\frac{2\pi\eta}{\theta} == \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \theta\right]$$

$$\{\{\theta \rightarrow 2.09585 \times 10^{-8} \eta\}\}$$

$$\text{Solve}\left[\frac{2\pi\eta}{\theta} == \left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \beta\right]$$

$$\{\{\beta \rightarrow -1. \text{ArcSin}\left[\frac{\sqrt{\theta} \sqrt{-1.10318 \times 10^{24} \eta + 5.26365 \times 10^{31} \theta + 8.77883 \times 10^{22} \eta \theta - 4.18868 \times 10^{30} \theta^2}}{\sqrt{-3.46574 \times 10^{24} \eta + 1.65363 \times 10^{32} \theta}}\right]\}, \{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{\theta} \sqrt{-1.10318 \times 10^{24} \eta + 5.26365 \times 10^{31} \theta + 8.77883 \times 10^{22} \eta \theta - 4.18868 \times 10^{30} \theta^2}}{\sqrt{-3.46574 \times 10^{24} \eta + 1.65363 \times 10^{32} \theta}}\right]\}\}$$

$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{(-1.1031799963798287 \cdot 10^{24} \eta + 5.263652535493924 \cdot 10^{31} \theta + 8.778827477197447 \cdot 10^{22} \eta \theta - 4.18868159871023 \cdot 10^{30} \theta^2)}\right) / \left(\sqrt{-3.465742172214084 \cdot 10^{24} \eta + 1.6536252136556997 \cdot 10^{32} \theta}\right)\right], \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



# A Notational Language for Describing the Geometry of Space-Time

by Parker Emmerson

© October 14, 2009

## I. Postulates, Structure

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle,

the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + \eta^2$$

This is the initial radius squared expressed as the slant of

the cone in terms of the height of the cone,  $\eta$ , and the radius of the base of the cone,  $r_1$

$$r = \sqrt{(r_1^2 + \eta^2)}$$

$$s = \theta r$$

(80)

$$s / \theta = r$$

The arc length taken out of a circle at a given time is =

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \quad \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - \eta^2$$

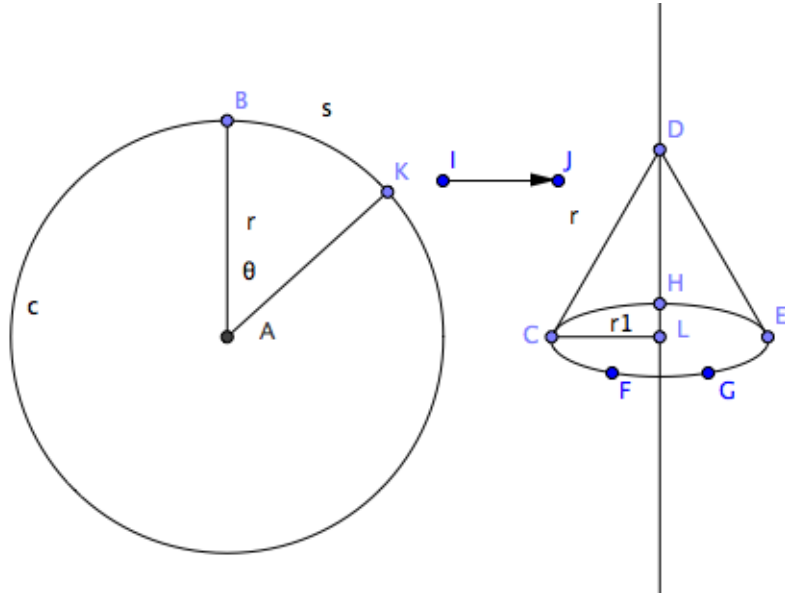
$$r_1 = \sqrt{(r^2 - \eta^2)}$$

$$\eta \leq r$$

$$\tau = \text{time}$$

$$1 \text{ second} = 6 \text{ degrees}$$

$$\tau = 6 \theta$$



I will now do some algebra to conclude what the height of the cone is in terms of the initial parameters. It can eventually be reduced to a single variable.

$$\text{Solve}[r_1^2 + \eta^2 = r^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\} \quad (81)$$

We say that the amount of  $\theta = s$ , taken out of the circle is the change in the circle's circumference that is the base of the cone. The change is equal to  $s = 2\pi r - 2\pi r_1$ .

Notice that  $\theta =$

$$\left( \frac{2\pi r}{r} \right) - \left( \frac{2\pi r_1}{r} \right), \text{ because we divide by } r \text{ on both sides.}$$

We will focus on the positive solutions for the height of the cone.

$$\text{Solve}[\eta = \sqrt{r^2 - r_1^2}, r_1]$$

$$\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2 - \eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2 - \eta^2} \right\} \right\} \quad (82)$$

This is the change in circumference with

the substituted expression for  $r_1$  in terms of  $h$  and  $r$ .

$$r\theta = s = 2\pi(r) - 2\pi\sqrt{(r)^2 - \eta^2} = 2\pi(r) - 2\pi r_1 \quad (83)$$

$$\theta = \frac{2\pi r}{r} - \frac{2\pi r_1}{r} = \left( \frac{2\pi r}{r} \right) - \left( \frac{2\pi\sqrt{-\eta^2 + r^2}}{r} \right)$$

$$\text{Solve}[\theta * r = 2\pi(r) - 2\pi\sqrt{(r)^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\} \quad (84)$$

$$\text{Solve}\left[\eta == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}\right\} \quad (85)$$

## II. Motion through the Space - Time

If there is something traveling over the distance,  $\eta$ , then its velocity is said to be the first derivative with respect to time. What if  $r$  is constant, which it is when it's the hypotenuse of the triangle made by the cone.

$v = \text{frequency} = 1 / \tau = (1 / (1080 / \pi) \theta)$ ,  
because each second is in terms of degrees of a clock, and in terms of theta,  
which is in radians, we must make the following conversion :

$$\text{Time} = 6 (\theta_{\text{degrees}}) = 6 (180 / \pi) \theta = (1080 / \pi) \theta$$

$$\eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$v = \lambda v = r (1 / (1080 / \pi) \theta) = ((1 / (1080 / \pi)) D[\eta, \theta]) = 1 / (1080 / \pi)$$

$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right] \quad (87)$$

The velocity of  $\eta$  is equal to the first derivative of  $\eta$  with respect to time. The constant  $(1/(1080/\pi))$  is taken out of the equation in order to perform the derivative.

$$(1 / (1080 / \pi)) D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}} =$$

velocity through the height of the cone when  $r$  is constant (88)

(stays always the initial radius of the circle equal to the hypotenuse  
of the triangle formed by the height meeting the base of the cone) .

$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2 \theta}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}} == r (1 / (1080 / \pi) \theta), \theta\right]$$

$$\begin{aligned}
& \left\{ \left\{ \Theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} + \right. \right.} \right. \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} \right) - \\
& \quad \frac{1}{2} \sqrt{\left( -\frac{1}{3\pi^2} + 8\pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} - \right.} \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} - \right. \\
& \quad \left( \frac{4}{\pi} + 64\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{1}{12\pi^2} \right.} \right. \\
& \quad \left. \left. \left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3} + 1 / \right. \right. \\
& \quad \left. \left. \left( 6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3} \right) \right) \right) \right\} \Bigg\}, \\
& \left\{ \Theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} + \right. \right.} \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} \right) + \\
& \quad \frac{1}{2} \sqrt{\left( -\frac{1}{3\pi^2} + 8\pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} - \right.} \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} - \right. \\
& \quad \left( \frac{4}{\pi} + 64\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{1}{12\pi^2} \right.} \right. \\
& \quad \left. \left. \left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3} + 1 / \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right)^{1/3} \right) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} + \right.} \right. \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right)^{1/3}} \right) - \\
& \quad \frac{1}{2} \sqrt{\left( -\frac{1}{3 \pi^2} + 8 \pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} - \right.} \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right)^{1/3}} + \right. \\
& \quad \left( \frac{4}{\pi} + 64 \pi^3 \right) \Bigg/ \left( 4 \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{1}{12 \pi^2} \right.} \right. \\
& \quad \left. \left. \left( \frac{1}{2} \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right) \right)^{1/3} + 1 \right) \right. \\
& \quad \left. \left( 6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right)^{1/3} \right) \right) \Bigg) \Bigg\}, \\
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} + \right.} \right. \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right)^{1/3}} \right) + \\
& \quad \frac{1}{2} \sqrt{\left( -\frac{1}{3 \pi^2} + 8 \pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} - \right.} \\
& \quad \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right)^{1/3}} + \right. \\
& \quad \left( \frac{4}{\pi} + 64 \pi^3 \right) \Bigg/ \left( 4 \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{1}{12 \pi^2} \right.} \right. \\
& \quad \left. \left. \left( \frac{1}{2} \left( 2 + 27\,648 \pi^8 + \sqrt{110\,592 \pi^8 + 764\,411\,904 \pi^{16}} \right) \right)^{1/3} + 1 \right) \right) \Bigg\}
\end{aligned}$$

$$\left( \frac{1}{2} \left( 2 + 27\,648\,\pi^8 + \sqrt{110\,592\,\pi^8 + 764\,411\,904\,\pi^{16}} \right)^{1/3} + 1 \right) /$$

$$\left( 6 \times 2^{2/3} \pi^2 \left( 2 + 27\,648\,\pi^8 + \sqrt{110\,592\,\pi^8 + 764\,411\,904\,\pi^{16}} \right)^{1/3} \right) \Bigg) \Bigg) \Bigg\} \Bigg\}$$

What is theta for a certain number of frequencies?

$$\text{Solve} \left[ \frac{4\pi r^2 - 2r^2\theta}{4320\sqrt{4\pi r^2\theta - r^2\theta^2}} == r n (1 / (1080 / \pi) \theta), \theta \right]$$

$$\left\{ \left\{ \theta \rightarrow \pi - \right. \right.$$

$$\frac{1}{2} \sqrt{\left( -\frac{1}{6n^2\pi^2} + 4\pi^2 + \frac{1}{12n^2\pi^2 \left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}} + \right.}$$

$$\left. \frac{\left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}}{12n^2\pi^2} \right) -$$

$$\frac{1}{2} \sqrt{\left( -\frac{1}{3n^2\pi^2} + 8\pi^2 - \frac{1}{12n^2\pi^2 \left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}} - \right.}$$

$$\left. \frac{\left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}}{12n^2\pi^2} \right) -$$

$$\left( \frac{4}{n^2\pi} + 64\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6n^2\pi^2} + 4\pi^2 + \right.} \right.$$

$$\left. \frac{1}{12n^2\pi^2 \left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}} + \right.}$$

$$\left. \frac{\left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}}{12n^2\pi^2} \right) \Bigg) \Bigg) \Bigg\}, \left\{ \theta \rightarrow \pi - \right.$$

$$\frac{1}{2} \sqrt{\left( -\frac{1}{6n^2\pi^2} + 4\pi^2 + \frac{1}{12n^2\pi^2 \left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}} + \right.}$$

$$\left. \frac{\left( 1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}}{12n^2\pi^2} \right) +$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} - \right. \\
& \quad \left. \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \right.} \right. \right. \\
& \quad \left. \left. \left. 1 / \left( 12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3} \right) + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \right\}, \left\{ \theta \rightarrow \pi + \right.
\end{aligned}$$

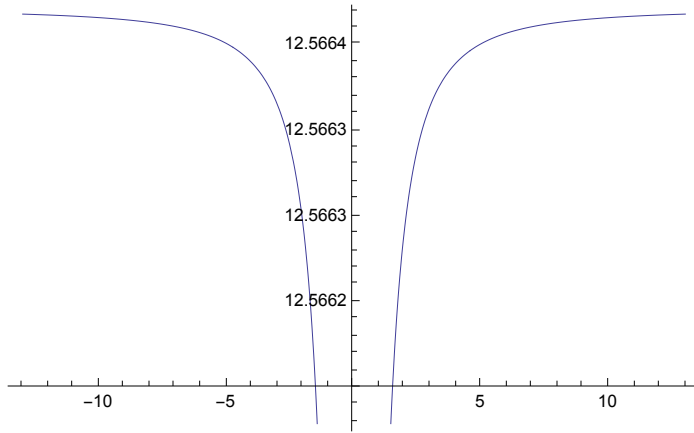
$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \\
& \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} + \right. \\
& \quad \left. \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \right.} \right. \right. \\
& \quad \left. \left. \left. 1 / \left( 12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3} \right) + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \right\}, \left\{ \theta \rightarrow \pi + \right.
\end{aligned}$$

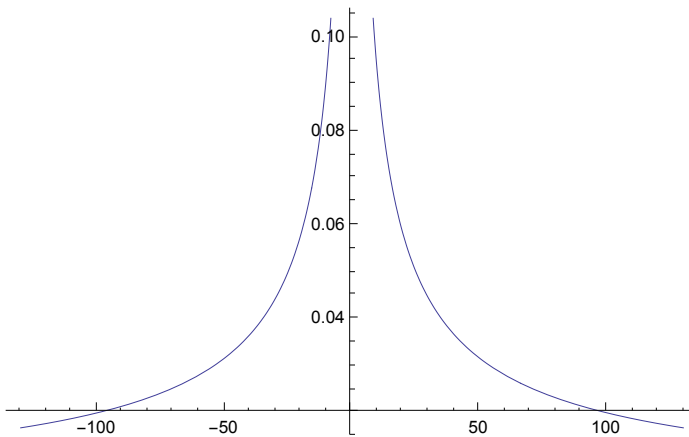
$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.}
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{\left(1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8}\right)^{1/3}}{12\,n^2\,\pi^2} \right) + \\
& \frac{1}{2} \sqrt{\left( -\frac{1}{3\,n^2\,\pi^2} + 8\,\pi^2 - \frac{1}{12\,n^2\,\pi^2\left(1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8}\right)^{1/3}} \right.} \\
& \quad \left. \frac{\left(1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8}\right)^{1/3}}{12\,n^2\,\pi^2} + \right. \\
& \quad \left. \left( \frac{4}{n^2\,\pi} + 64\,\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6\,n^2\,\pi^2} + 4\,\pi^2 + \right. \right.} \\
& \quad \left. \left. 1 / \left( 12\,n^2\,\pi^2 \left( 1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8} \right)^{1/3} \right) + \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8} \right)^{1/3}}{12\,n^2\,\pi^2} \right) \right) \right) \right) \Bigg\} \Bigg\} \\
& \text{Plot} \left[ \pi + \frac{1}{2} \sqrt{\left( -\frac{1}{6\,n^2\,\pi^2} + 4\,\pi^2 + \frac{1}{12\,n^2\,\pi^2\left(1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8}\right)^{1/3}} \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8} \right)^{1/3}}{12\,n^2\,\pi^2} \right) + \right. \\
& \quad \left. \frac{1}{2} \sqrt{\left( -\frac{1}{3\,n^2\,\pi^2} + 8\,\pi^2 - \frac{1}{12\,n^2\,\pi^2\left(1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8}\right)^{1/3}} \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8} \right)^{1/3}}{12\,n^2\,\pi^2} + \left( \frac{4}{n^2\,\pi} + 64\,\pi^3 \right) / \right. \right. \\
& \quad \left. \left( 4 \sqrt{\left( -\frac{1}{6\,n^2\,\pi^2} + 4\,\pi^2 + \frac{1}{12\,n^2\,\pi^2\left(1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8}\right)^{1/3}} \right.} \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13\,824\,n^4\,\pi^8 + 96\,\sqrt{3}\,\pi^4\,\sqrt{n^4 + 6912\,n^8\,\pi^8} \right)^{1/3}}{12\,n^2\,\pi^2} \right) \right) \right) \right) \Bigg], \{n, -13, 13\} \Bigg]
\end{aligned}$$



$$\begin{aligned}
& \text{Plot} \left[ \pi + \frac{1}{2} \sqrt[3]{ \left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) - \right. \\
& \quad \left. \frac{1}{2} \sqrt[3]{ \left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} + \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) \right) / \right. \\
& \quad \left. \left( 4 \sqrt[3]{ \left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \right], \{n, -13, 13\} ]
\end{aligned}$$



These are mathematical expressions of the reality of the four noble truths. Leaves falling from trees.

What would acceleration through the height of the cone be when r is constant?

$$v = \lambda v = r \left( 1 / (1080 / \pi) \theta \right) = (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$(1 / (1080 / \pi)) \text{ D} \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \text{velocity when } r \text{ is constant.}$$

$$\text{Solve} \left[ \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == r (1 / (1080 / \pi) \theta), r \right]$$

{ }

$$(1 / (1080 / \pi)) \text{ D} \left[ \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta \right]$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8640 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2160 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080}$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8640 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2160 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} =$$

(91)

acceleration through the height of the cone when  $r$  is constant.

What happens if  $r$  is changing?

$$(1 / (1080 / \pi)) \text{ D} \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta \right]$$

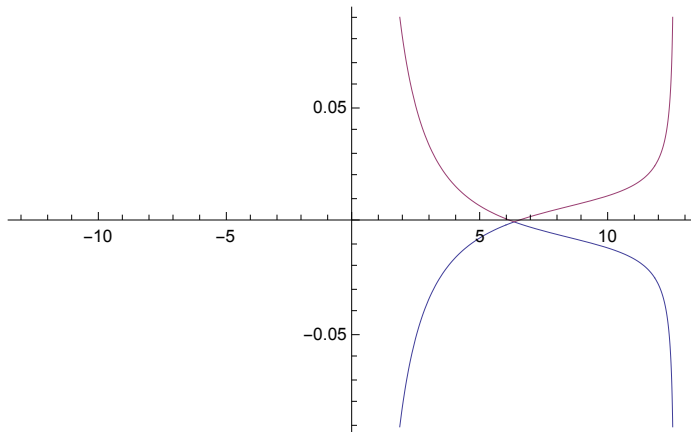
$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} = \text{velocity when } r \text{ is changing}$$

(91)

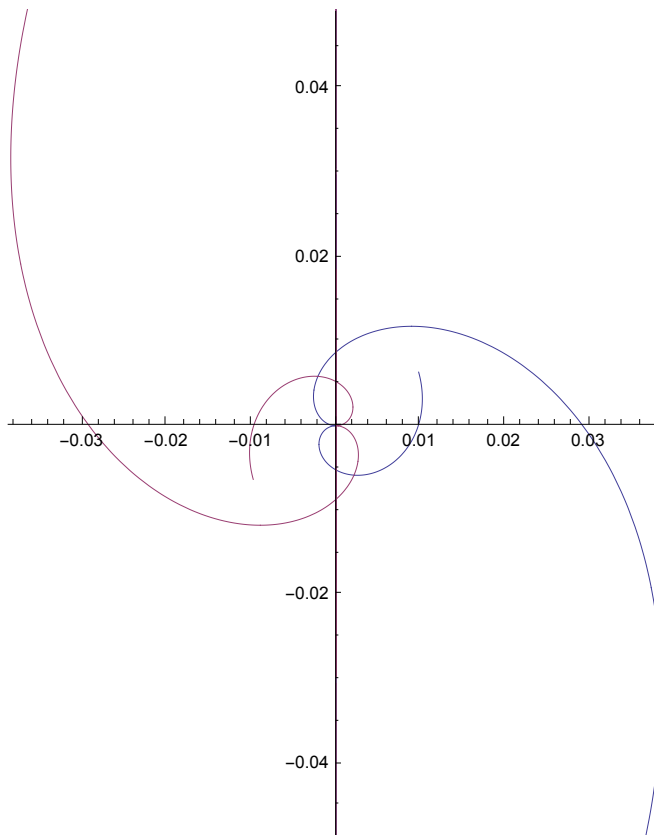
$$\text{Solve} \left[ \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} == r (1 / (1080 / \pi) \theta), r \right]$$

$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\} \right\}$$

$$\text{Plot}\left[\left\{-\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\left\{-\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -10, 10\}\right]$$

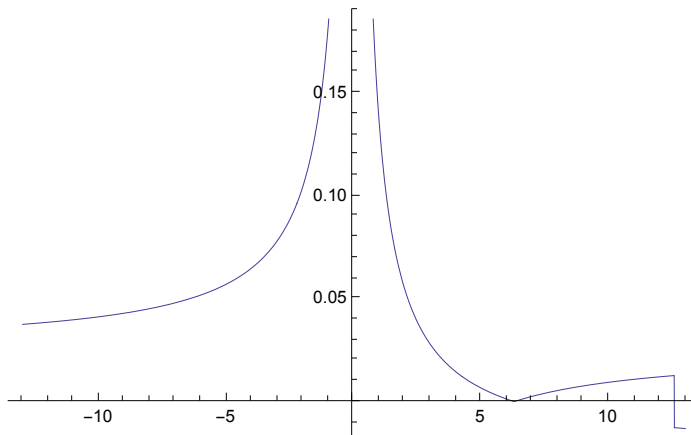


$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r = \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}$$

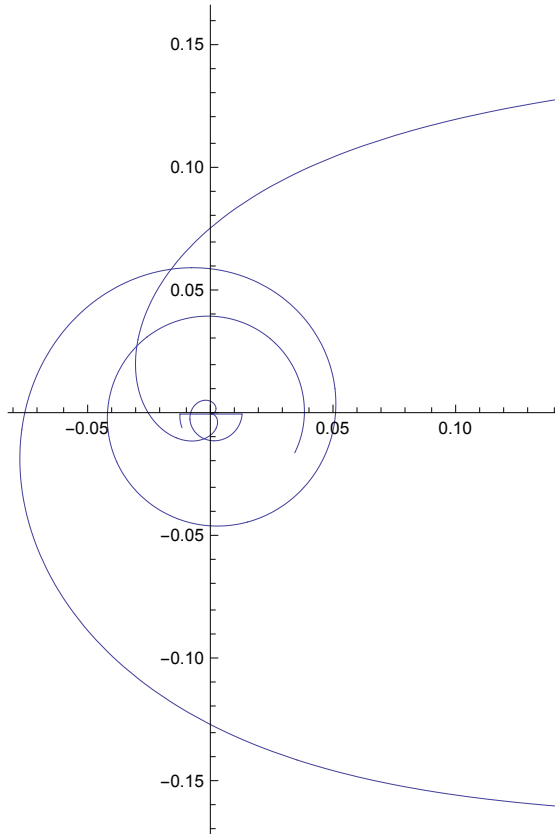
$$\text{Solve}\left[\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} == \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}}, \eta\right]$$

$$\left\{\left\{\eta \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2}}{8 \pi^2 \sqrt{\theta}}\right\}\right\}$$

$$\text{Plot}\left[\frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2}}{8 \pi^2 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$$



$$(1 / (1080 / \pi)) D\left[\frac{\pi \left( -\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right)}{1080}, r, \theta\right]$$

$$\begin{aligned} & \frac{1}{1166400} \pi^2 \left( -\frac{15(4\pi r^2 - 2r^2\theta)^2(8\pi r\theta - 2r\theta^2)^2}{32\pi(4\pi r^2\theta - r^2\theta^2)^{7/2}} + \right. \\ & \frac{3(4\pi r^2 - 2r^2\theta)^2(8\pi\theta - 2\theta^2)}{16\pi(4\pi r^2\theta - r^2\theta^2)^{5/2}} + \frac{3(8\pi r - 4r\theta)(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{4\pi(4\pi r^2\theta - r^2\theta^2)^{5/2}} - \\ & \frac{3r^2(8\pi r\theta - 2r\theta^2)^2}{8\pi(4\pi r^2\theta - r^2\theta^2)^{5/2}} - \frac{(8\pi r - 4r\theta)^2}{4\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{(8\pi - 4\theta)(4\pi r^2 - 2r^2\theta)}{4\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \\ & \left. \frac{r^2(8\pi\theta - 2\theta^2)}{4\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{r(8\pi r\theta - 2r\theta^2)}{\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{1}{\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right) \end{aligned}$$

Acceleration when  $r$  is changing =

$$\begin{aligned} & \frac{1}{1166400} \pi^2 \left( -\frac{15 (4\pi r^2 - 2r^2\theta)^2 (8\pi r\theta - 2r\theta^2)^2}{32\pi (4\pi r^2\theta - r^2\theta^2)^{7/2}} + \frac{3 (4\pi r^2 - 2r^2\theta)^2 (8\pi\theta - 2\theta^2)}{16\pi (4\pi r^2\theta - r^2\theta^2)^{5/2}} + \right. \\ & \quad \frac{3 (8\pi r - 4r\theta) (4\pi r^2 - 2r^2\theta) (8\pi r\theta - 2r\theta^2)}{4\pi (4\pi r^2\theta - r^2\theta^2)^{5/2}} - \frac{3r^2 (8\pi r\theta - 2r\theta^2)^2}{8\pi (4\pi r^2\theta - r^2\theta^2)^{5/2}} - \\ & \quad \frac{(8\pi r - 4r\theta)^2}{4\pi (4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{(8\pi - 4\theta) (4\pi r^2 - 2r^2\theta)}{4\pi (4\pi r^2\theta - r^2\theta^2)^{3/2}} + \\ & \quad \left. \frac{r^2 (8\pi\theta - 2\theta^2)}{4\pi (4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{r (8\pi r\theta - 2r\theta^2)}{\pi (4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{1}{\pi \sqrt{4\pi r^2\theta - r^2\theta^2}} \right) \\ & \left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\} \right\} \end{aligned}$$

$$r := \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}$$

$$\text{Solve}\left[r = \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right.} \right. \\ & \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\ & \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\ & \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) \right) \Bigg/} \\ & \quad \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\ & \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \Bigg\} \Bigg\}, \end{aligned}$$



$$\begin{aligned}
& \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\},
\end{aligned}$$

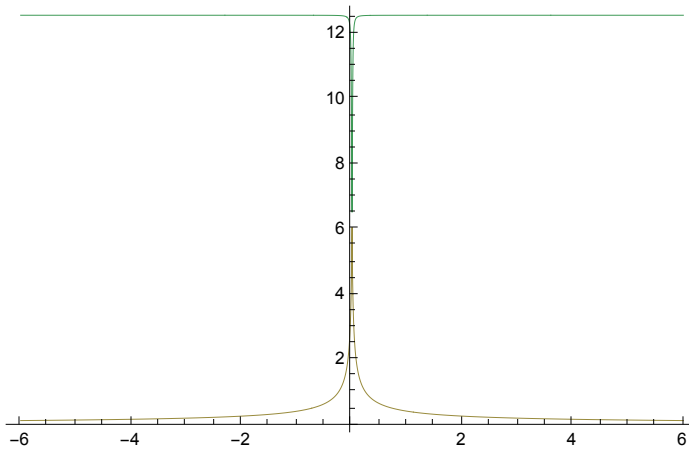
$$\begin{aligned}
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\} \Bigg\}
\end{aligned}$$

$$\begin{aligned}
& \text{Plot} \left[ \left\{ \left\{ \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \right. \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\} \Bigg\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \right\}, \{r, -6, 6\}
\end{aligned}$$



### III. What would the solutions be through acceleration?

When  $r$  is constant

$$v = \lambda v = r \left( 1 / (1080 / \pi) \theta \right) = (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right]$$

$(1 / (1080 / \pi)) D[r (1 / (1080 / \pi) \theta), \theta]$  = acceleration of a wavelength,  
 $r$ , and frequency,  $(1 / (1080 / \pi) \theta)$ .

(92)

$$(1 / (1080 / \pi)) \text{ D}[r (1 / (1080 / \pi) \theta), \theta]$$

$$\frac{\pi^2 r}{1166400}$$

$$(1 / (1080 / \pi)) \text{ D}\left[(1 / (1080 / \pi)) \text{ D}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \theta\right]$$

$$(1 / (1080 / \pi)) \text{ D}\left[(1 / (1080 / \pi)) \text{ D}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \theta\right] = \quad (93)$$

acceleration through the height of the cone

$$\text{Solve}\left[\frac{\pi^2 r}{1166400} == (1 / (1080 / \pi)) \text{ D}\left[(1 / (1080 / \pi)) \text{ D}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \theta\right], \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2 \pi - \sqrt{-(-2 \pi)^{2/3} + 4 \pi^2}\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{-(-2 \pi)^{2/3} + 4 \pi^2}\right\}, \right. \\ \left\{\theta \rightarrow 2 \pi - \sqrt{4 \pi^2 - (2 \pi)^{2/3}}\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{4 \pi^2 - (2 \pi)^{2/3}}\right\}, \\ \left.\left\{\theta \rightarrow 2 \pi - \sqrt{4 \pi^2 + (-1)^{1/3} (2 \pi)^{2/3}}\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{4 \pi^2 + (-1)^{1/3} (2 \pi)^{2/3}}\right\}\right\}$$

## IV. Defining the Initial Distance through its Geometric Correlates

When r is constant

$$r = \frac{2 * \text{velocity} * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} = \frac{2 * \left(\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} =$$

velocity through the height of the cone when r is constant

(94)

(stays always the initial radius of the circle equal to the hypoteneuse of the triangle formed by the height meeting the base of the cone) .

$$\text{Solve}\left[\frac{2 * \left(\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} == r, \theta\right]$$

$$\{\{\theta \rightarrow 3 \pi\}\}$$

When r is changing

$$r = \frac{2 * \text{velocity} * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} =$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} \quad (94)$$

$$\text{velocity} = \lambda v = r (1 / (1080 / \pi) \theta)$$

$$\text{Solve} \left[ \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} == r (1 / (1080 / \pi) \theta), r \right]$$

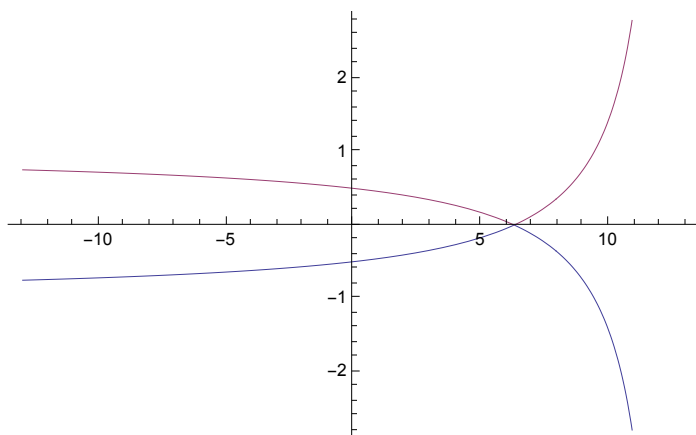
$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\} \right\} \quad (95)$$

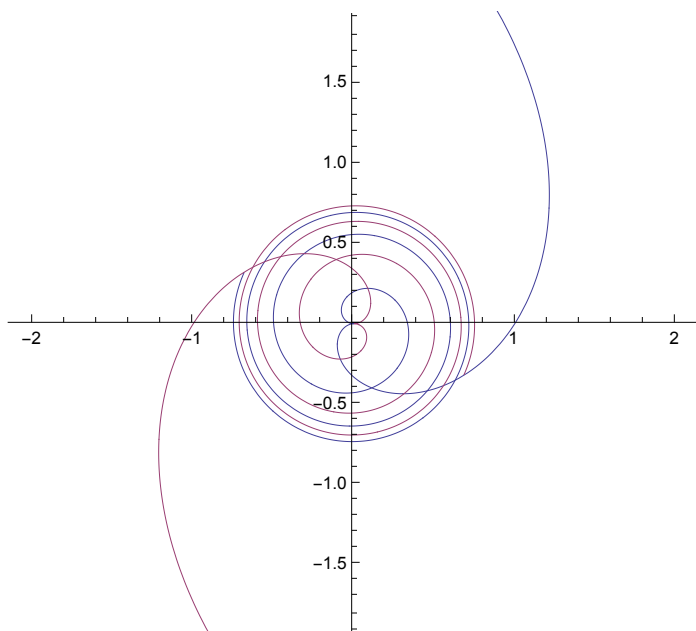
$$r = \frac{2 * \text{velocity} * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} =$$

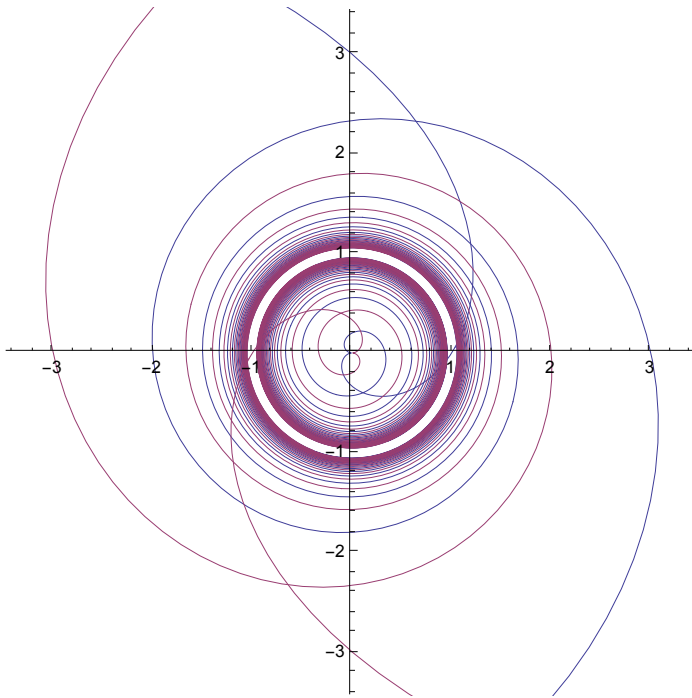
$$\frac{2 * \left( \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} \right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}$$

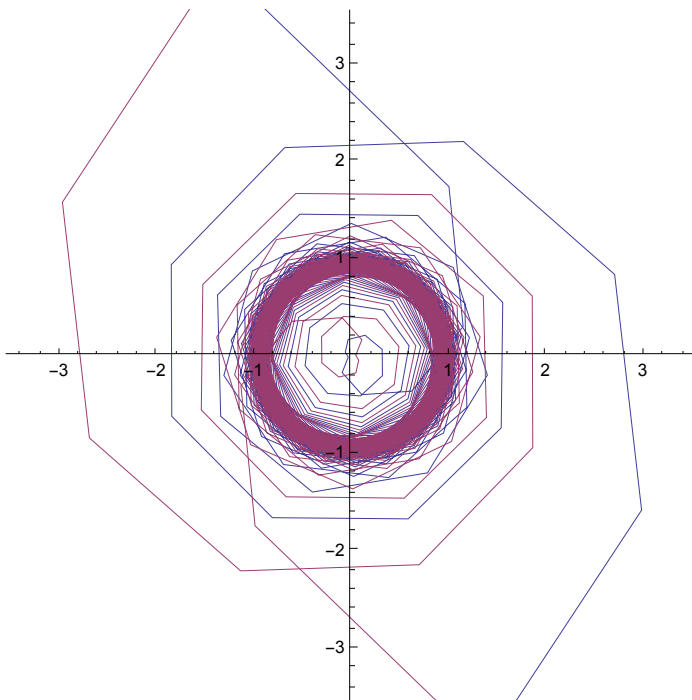
$$\text{Solve} \left[ r == \frac{2 * \left( \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} \right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, r \right]$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\} \right\}$$

$$\text{Plot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -13, 13\}\right]$$


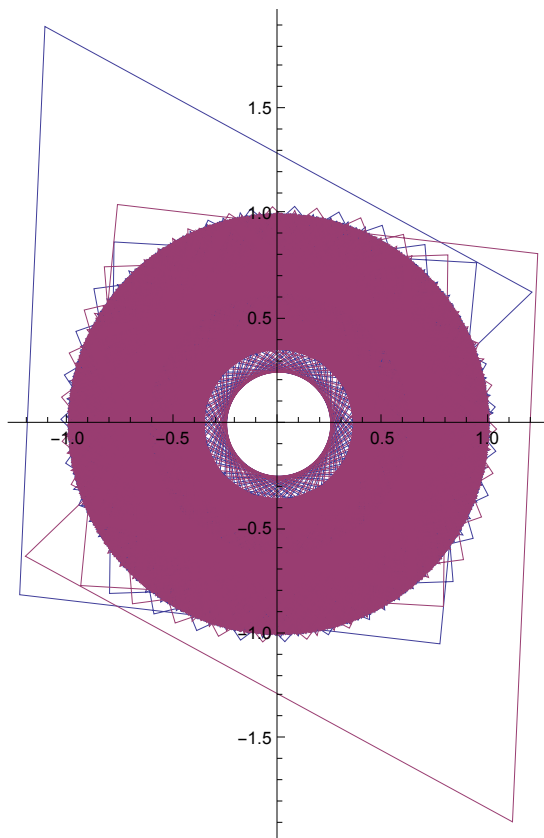
$$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -13, 13\}\right]$$


$$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -130, 130\}\right]$$


$$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -1300, 1300\}\right]$$


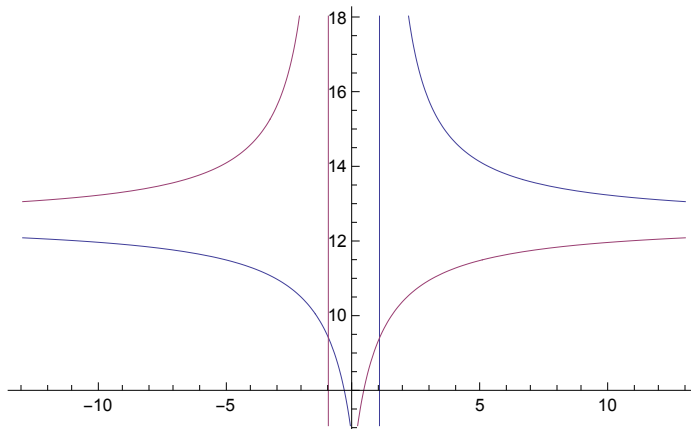


$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -13000, 13000\}\right]$

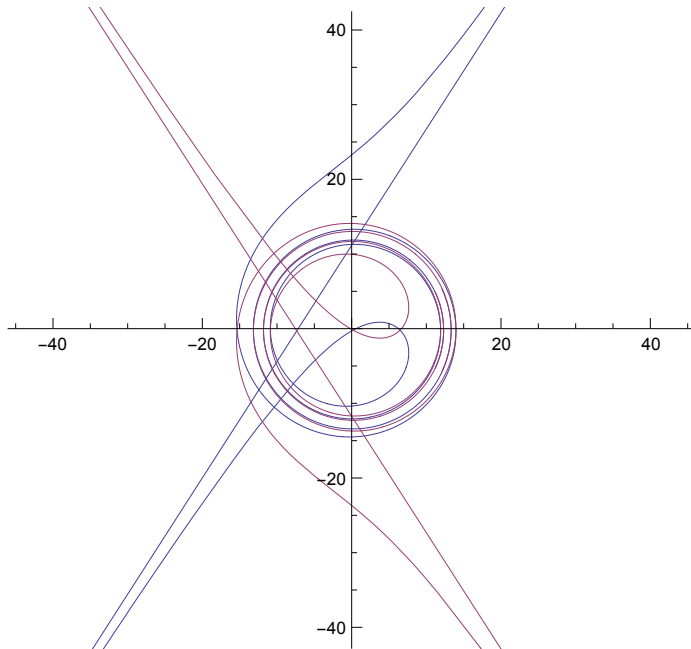


$\text{Solve}\left[r == \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \theta\right]$   
 $\left\{\left\{\theta \rightarrow \frac{2(-\pi+2\pi r)}{-1+r}\right\}, \left\{\theta \rightarrow \frac{2(\pi+2\pi r)}{1+r}\right\}\right\}$

$\text{Plot}\left[\left\{\frac{2(-\pi+2\pi r)}{-1+r}, \frac{2(\pi+2\pi r)}{1+r}\right\}, \{r, -13, 13\}\right]$



`PolarPlot[ $\left\{\frac{2(-\pi + 2\pi r)}{-1 + r}, \frac{2(\pi + 2\pi r)}{1 + r}\right\}, \{r, -13, 13\}$ ]`



## V. Dealing with n

`Solve[ $\frac{4\pi r^2 - 2r^2\theta}{4320\sqrt{4\pi r^2\theta - r^2\theta^2}} == r n (1 / (1080 / \pi) \theta), n]$`

`{ $\left\{n \rightarrow \frac{r(2\pi - \theta)}{2\pi\theta\sqrt{r^2(4\pi - \theta)\theta}}\right\}}$ }`

Options for assigning functions that are expressions of r.

From the velocity when r is changing :

`{ $\left\{r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right\}, \left\{r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right\}}$ }`

`{ $\left\{r \rightarrow -\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}}$ }`

`Plot[ $\frac{r(2\pi - \theta)}{2\pi\theta\sqrt{r^2(4\pi - \theta)\theta}}, \{\theta, -13, 13\}$ ]`

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\}$$

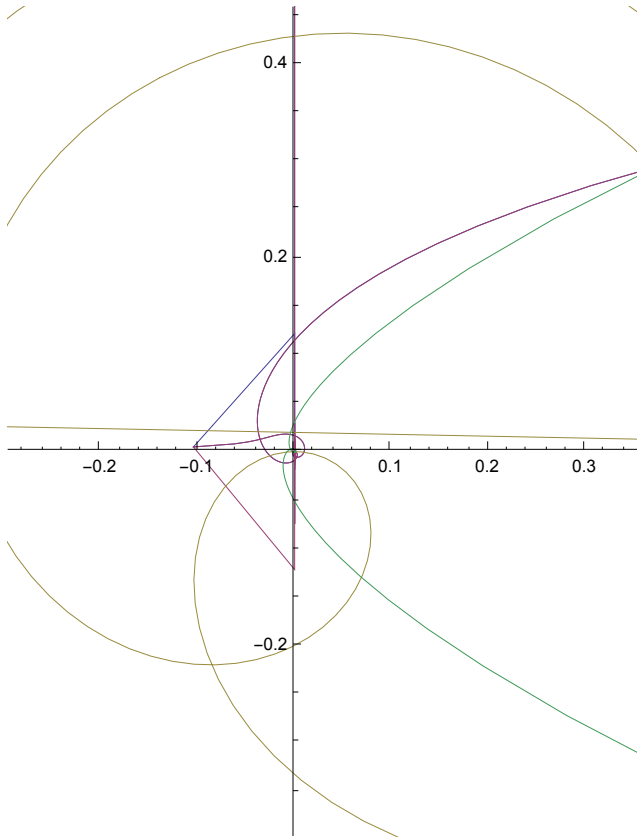
$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right\} \right\}$$

$$n = \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}} =$$

$$\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left( \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} \right)^2 (4\pi - \theta)\theta}} = \frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right)^2 (4\pi - \theta)\theta}} =$$

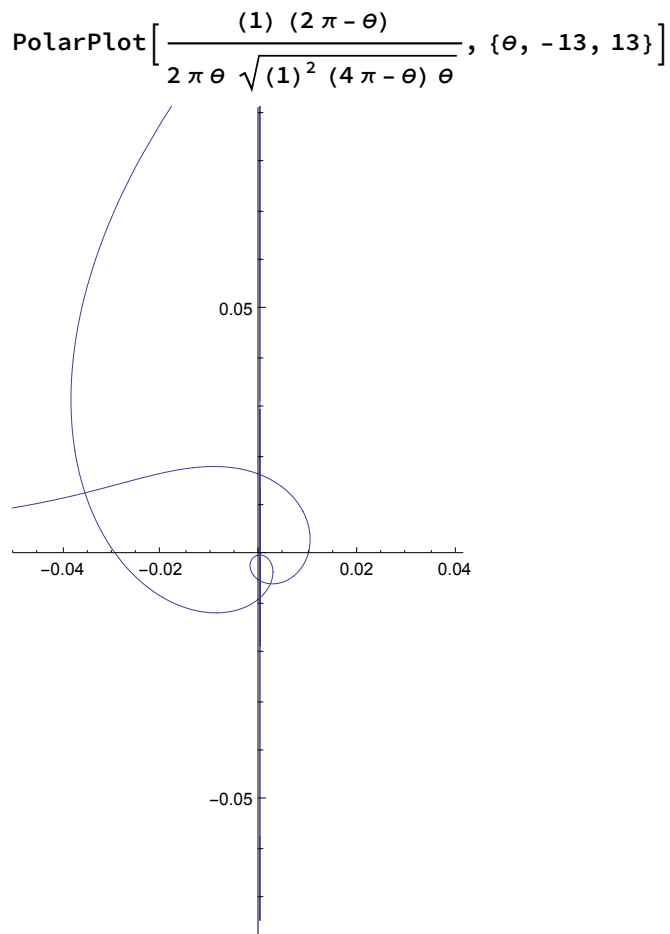
$$\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right)^2 (4\pi - \theta)\theta}} = \frac{\left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right) (2\pi - \theta)}{2\pi\theta \sqrt{\left( \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} \right)^2 (4\pi - \theta)\theta}}$$

$$\text{PolarPlot}\left[\left\{\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}}\right\}, \{\theta, -130, 130\} \right]$$



$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2\theta}{4320\sqrt{4\pi r^2\theta - r^2\theta^2}} == r n (1 / (1080 / \pi) \theta), n\right]$$

$$\left\{\left\{n \rightarrow \frac{r (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)\theta}}\right\}\right\}$$



## VI. Solving for $r_1$

$$r_1 \rightarrow \sqrt{r^2 - \eta^2}$$

$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right\} \right\}$$

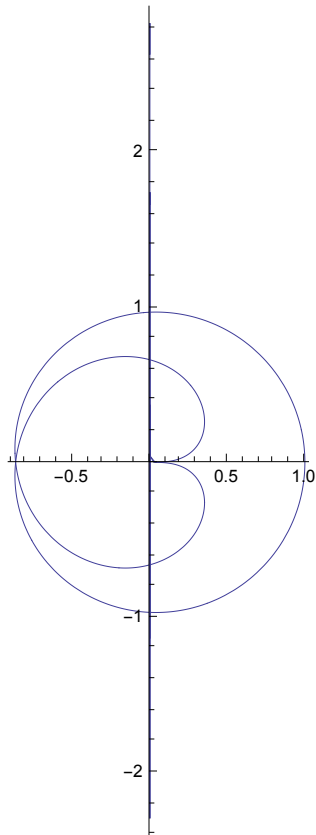
### The Constant $r$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\}$$

$$\text{Solve}\left[1 == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}, \eta\right]$$

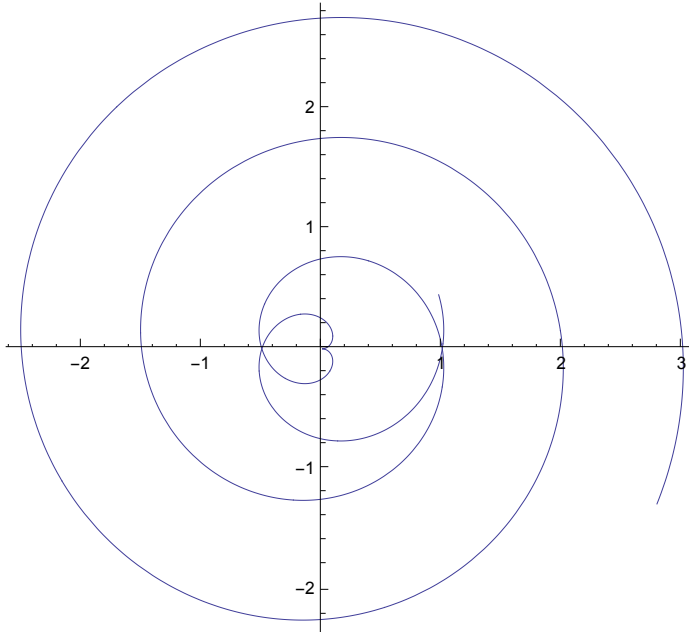
$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right\} \right\}$$

`PolarPlot` $\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}, \{\theta, -13, 13\}\right]$



$$\sqrt{r^2 - \eta^2} = \sqrt{(1)^2 - \left(\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right)^2}$$

$$\text{PolarPlot}\left[\sqrt{(1)^2 - \left(\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right)^2}, \{\theta, -13, 13\}\right]$$



## The changing r

$$r_1 = \sqrt{r^2 - \eta^2}$$

$$\left\{\left\{\eta \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right\}\right\}$$

$$r_1 = \sqrt{r^2 - \eta^2} = \sqrt{r^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2} =$$

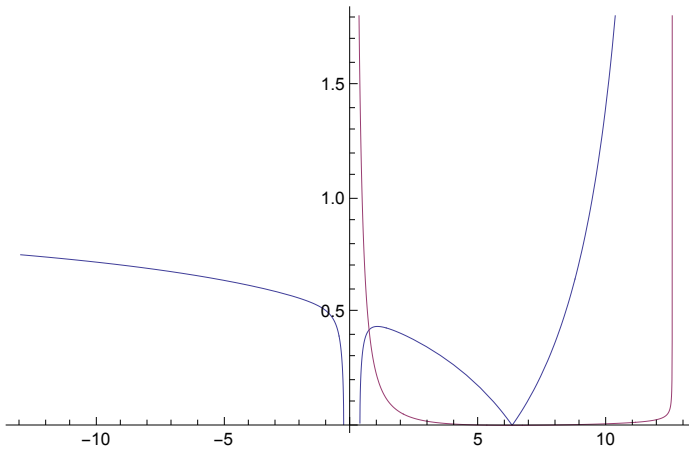
$$\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2} =$$

$$\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}$$

$$\left\{\left\{r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right\}, \left\{r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right\}\right\}$$

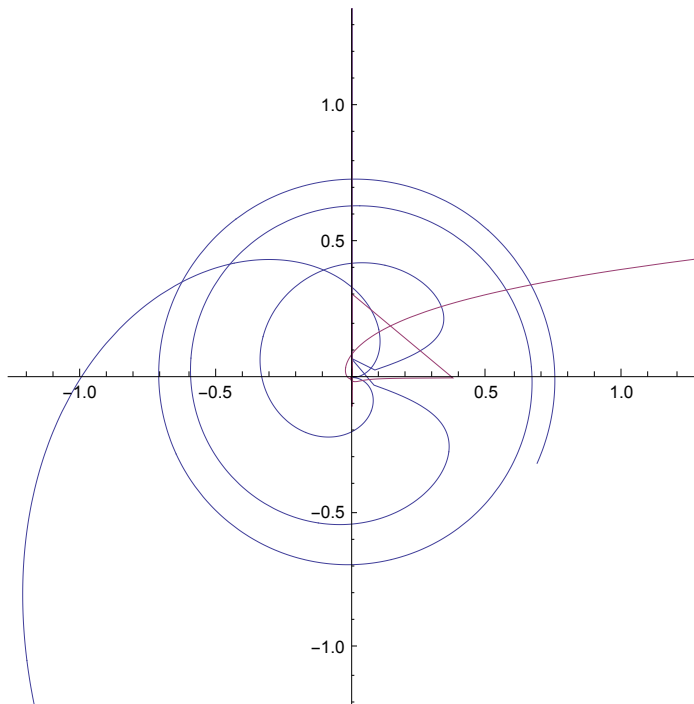
$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\} \right\}$$

$$\text{Plot}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}\sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right.\right. \\ \left.\left.\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}\sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}\right\}, \{\theta, -13, 13\} \right]$$

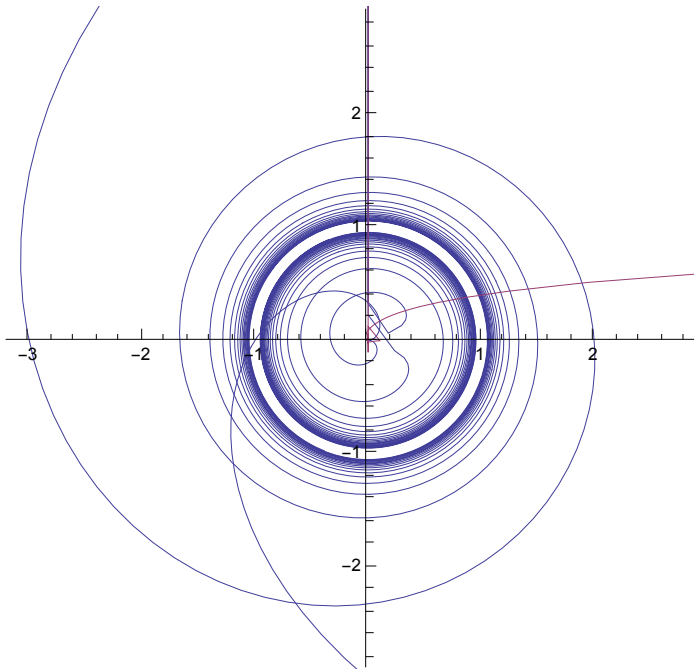




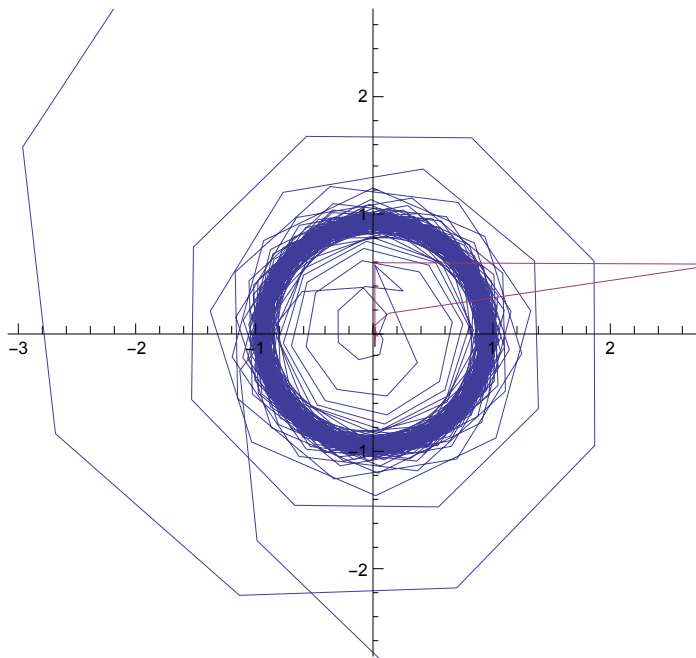
$$\text{PolarPlot}\left[\left\{\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right.\right. \\ \left.\left.\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}\right\},\{\theta,-13,13\}\right]$$



$$\text{PolarPlot}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \right. \right. \\ \left. \left. \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -130, 130\}\right]$$



$$\text{PolarPlot}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \right. \right. \\ \left. \left. \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -1300, 1300\} \right]$$



$$\text{Solve} \left[ \sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} = \right. \\ \left. \sqrt{\left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right)^2 - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}, \theta \right]$$

$$\{\{\theta \rightarrow 2\pi\},$$

$$\left\{ \theta \rightarrow - \left( \frac{2}{1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}} \right)^{1/3} + \frac{\left( \frac{1}{2} \left( 1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}} \right) \right)^{1/3}}{12\pi^2} \right\},$$

$$\left\{ \theta \rightarrow - \frac{(1 + i\sqrt{3}) \left( \frac{1}{2} \left( 1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}} \right) \right)^{1/3}}{24\pi^2} +$$

$$\frac{1 - i\sqrt{3}}{2^{2/3} \left( 1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}} \right)^{1/3}} \right\},$$

$$\left\{ \theta \rightarrow - \frac{(1 - i\sqrt{3}) \left( \frac{1}{2} \left( 1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}} \right) \right)^{1/3}}{24\pi^2} +$$

$$\frac{1 + i\sqrt{3}}{2^{2/3} \left( 1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}} \right)^{1/3}} \right\} \}$$

If these are theta solutions, what is  $r * \theta$ , the change in circumference?

Plot[{{r 2 π},

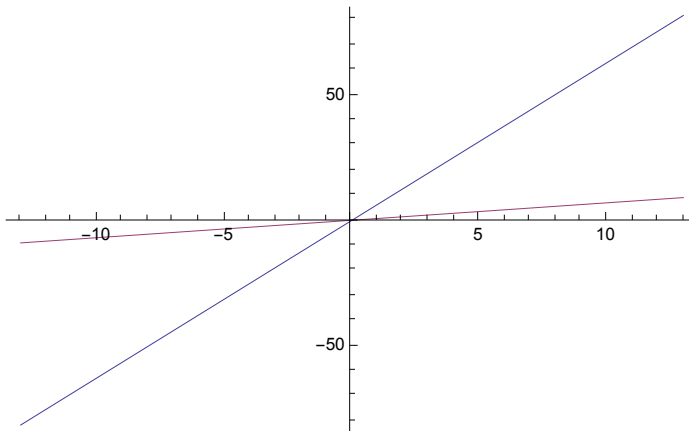
$$\left\{r \left( \left( \frac{2}{1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}}} \right)^{1/3} + \frac{\left( \frac{1}{2} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right) \right)^{1/3}}{12 \pi^2} \right) \right\},$$

$$\left\{r \left( - \frac{\left( 1 + i \sqrt{3} \right) \left( \frac{1}{2} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right) \right)^{1/3}}{24 \pi^2} + \right.$$

$$\left. \frac{1 - i \sqrt{3}}{2^{2/3} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right)^{1/3}} \right\},$$

$$\left\{r \left( - \frac{\left( 1 - i \sqrt{3} \right) \left( \frac{1}{2} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right) \right)^{1/3}}{24 \pi^2} + \right.$$

$$\left. \frac{1 + i \sqrt{3}}{2^{2/3} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right)^{1/3}} \right\} \}, \{r, -13, 13\}]$$



$$\text{Solve}\left[r_1 == \sqrt{\left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right)^2 - \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}} \right)^2}, \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{2\pi(1 + 8\pi^4 r_1^2)}{1 + 16\pi^4 r_1^2} - \frac{1}{2} \right. \right.$$

$$\left. \sqrt{\left( \frac{16\pi^2(1 + 8\pi^4 r_1^2)^2}{(1 + 16\pi^4 r_1^2)^2} - \frac{16\pi^2}{1 + 16\pi^4 r_1^2} - \frac{32\pi^4 r_1^2(1 + 48\pi^4 r_1^2 + 768\pi^8 r_1^4 + 4096\pi^{12} r_1^6)^{1/3}}{3^{1/3}(1 + 16\pi^4 r_1^2)^2(9\pi^2 r_1^4 + \sqrt{3}\sqrt{r_1^6 + 27\pi^4 r_1^8})^{1/3}} \right.} \right.$$

$$\begin{aligned}
& \left. \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} \right) - \frac{1}{2} \\
& \sqrt{\left( \frac{32 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} - \right. \\
& \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} - \left( \frac{512 \pi^3 \left( 1 + 8 \pi^4 r_1^2 \right)^3}{\left( 1 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{768 \pi^3 \left( 1 + 8 \pi^4 r_1^2 \right)}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) \Bigg/ \left( 4 \sqrt{\left( \frac{16 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \right. \right. \\
& \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} + \\
& \left. \left. \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} \right) \right) \Bigg] \Bigg\}, \\
& \left\{ \theta \rightarrow \frac{2 \pi \left( 1 + 8 \pi^4 r_1^2 \right)}{1 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{16 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right. \right. \\
& \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} + \\
& \left. \left. \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} \right) \right) + \frac{1}{2} \\
& \sqrt{\left( \frac{32 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} - \right. \\
& \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} - \\
& \left( \frac{512 \pi^3 \left( 1 + 8 \pi^4 r_1^2 \right)^3}{\left( 1 + 16 \pi^4 r_1^2 \right)^3} - \frac{768 \pi^3 \left( 1 + 8 \pi^4 r_1^2 \right)}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \Bigg\}, \\
& \left\{ \theta \rightarrow \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) - \frac{1}{2} \right. \\
& \quad \sqrt{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \right.} \\
& \quad \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} + \\
& \quad \left. \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) \Bigg/} \\
& \quad \left( 4 \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \Bigg\},
\end{aligned}$$

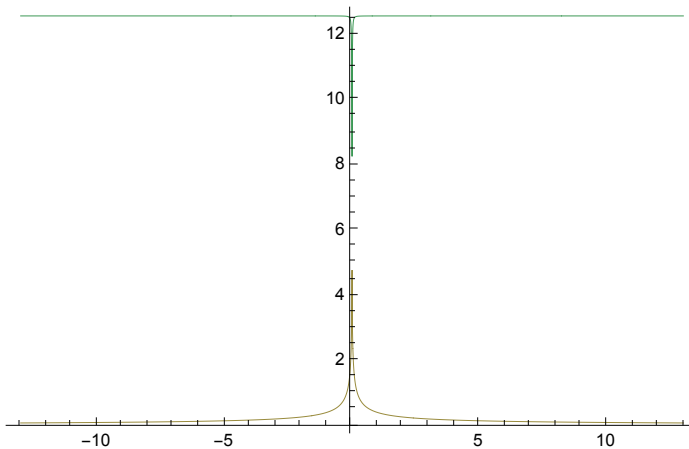
$$\begin{aligned}
& \left\{ \theta \rightarrow \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) + \frac{1}{2} \\
& \quad \sqrt{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \right.} \\
& \quad \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} + \\
& \quad \left. \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) \right) / \\
& \quad \left( 4 \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \right) \Bigg\} \Bigg\} \\
& \text{Plot} \left[ \left\{ \left\{ \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \right.} \right. \right. \\
& \quad \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) - \frac{1}{2} \sqrt{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \right. \\
& \quad \left. \left. \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \right. \right. \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \right) \Bigg\} \Bigg\}
\end{aligned}$$



$$\begin{aligned}
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} - \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \right. \\
& \left. \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \left( 4 \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \right. \\
& \left. \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \right. \\
& \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \Bigg\}, \\
& \left\{ \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) + \frac{1}{2} \sqrt[4]{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \\
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} - \\
& \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \\
& \left( 4 \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \Bigg) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt[3]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) - \frac{1}{2} \sqrt[3]{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \\
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} + \\
& \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \\
& \left( 4 \sqrt[3]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \Bigg) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt[3]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} + \frac{1}{2} \sqrt{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \\
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} + \\
& \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \left. \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \right) \Bigg\}, \{r_1, -13, 13\}
\end{aligned}$$



$$\text{Solve} \left[ \sqrt{\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} - \left( \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2}}{8 \pi^2 \sqrt{\theta}} \right)^2} = r_1, \theta \right]$$

$$\begin{aligned}
& \left\{ \left\{ \theta \rightarrow \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \right. \right. \\
& \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + (2^{1/3} (16 \pi^4 - 512 \pi^8 + \right. \\
& 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4)) / (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \\
& (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 \\
& r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 \\
& r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \\
& 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
& 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3}} + \\
& (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \\
& 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
& \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \\
& 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - 356 241 767 399 424 \\
& \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3} / (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) \Big) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right. \\
& (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4)) / \\
& (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 \\
& r_1^2 + 6 291 456 \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 \\
& r_1^4 + 33 554 432 \pi^{18} r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + \\
& 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + \\
& 38 963 943 309 312 \pi^{28} r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \\
& \pi^{28} r_1^6 - 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3}} - \\
& (128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \\
& 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
& \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \\
& 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
& 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8))^{1/3}} \Big) /
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) / \\
& \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right. \right. \\
& \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4 \right) \right) / \right. \\
& \left. \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + \right. \right. \right. \\
& 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - \\
& 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - \right.} \\
& 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \\
& \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
& \left. \left. \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8 \right) \right)^{1/3}} + \right. \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \right. \right. \\
& \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + \\
& 33 554 432 \pi^{18} r_1^6 + \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + \right.} \\
& 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \\
& \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + \\
& 22 265 110 462 464 \pi^{28} r_1^6 - 356 241 767 399 424 \pi^{32} r_1^6 + \\
& \left. \left. \left. 474 989 023 199 232 \pi^{32} r_1^8 \right) \right)^{1/3}} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \right) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \theta \rightarrow \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \right.} \right. \\
& \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \\
& \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4 \right) \right) / \right. \\
& \left. \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \right. \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} \right. \right. \\
& r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 \\
& r_1^6 + \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right.} \\
& 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& \left. \left. \left. 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \right) + \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 + \\
& \quad \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right.} \\
& \quad \quad 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \\
& \quad \quad \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - 356\,241\,767\,399\,424\right. \\
& \quad \quad \left. \pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right) \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{8\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)^2} - \frac{16\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8r_1^2 - 32\,768\,\pi^{12}r_1^2 + 65\,536\,\pi^{12}r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right. \\
& \quad \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad \quad r_1^2 + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 \\
& \quad \quad r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right.} \\
& \quad \quad \quad 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \\
& \quad \quad \quad \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - \right. \\
& \quad \quad \quad \left. \left. 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \right) - \\
& \quad \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad \quad 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 + \\
& \quad \quad \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right.} \\
& \quad \quad \quad 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \\
& \quad \quad \quad \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - \right. \\
& \quad \quad \quad \left. \left. 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \right) \Big/ \\
& \quad \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \right) - \left( \frac{768\,\pi^3}{1 - 16\,\pi^4 + 16\,\pi^4r_1^2} + \frac{64\,\pi^3 \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right)^3}{\left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64\,\pi^3 \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right) \left( 13 - 16\,\pi^4 + 64\,\pi^4r_1^2 \right)}{\left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt{\left( \frac{4\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)^2} - \frac{8\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right)} + \right.} \\
& \quad \quad \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8r_1^2 - 32\,768\,\pi^{12}r_1^2 + 65\,536\,\pi^{12}r_1^4 \right) \right) \Big/ \\
& \quad \quad \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4r_1^2 \right) \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - \\
& 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - \right. \\
& \quad 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488 \\
& \quad \pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \\
& \quad 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \\
& \quad \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} + \\
& \left(128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \\
& \quad \pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + \\
& \quad 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + \right. \\
& \quad 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + \\
& \quad 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + \\
& \quad 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + \\
& \quad \left. 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} \Big/ \left(3 \times 2^{1/3} \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)\right) \Bigg) \Bigg\}, \\
& \left\{\theta \rightarrow \frac{\pi \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right)}{1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2} + \frac{1}{2} \sqrt{\left(\frac{4\,\pi^2 \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right)^2}{\left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)^2} - \right.} \right. \\
& \quad \frac{8\,\pi^2 \left(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2\right)}{3 \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)} + \\
& \quad \left. \left(2^{1/3} \left(16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4\right)\right) \Big/ \right. \\
& \quad \left. \left(3 \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)\right) \right. \\
& \quad \left. \left(128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \right. \\
& \quad \left. \left. r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \right. \right. \\
& \quad \left. \left. \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - \right. \right. \right. \\
& \quad \left. \left. 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \right. \right. \\
& \quad \left. \left. 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \right. \right. \\
& \quad \left. \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} + \right. \\
& \quad \left. \left(128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \right. \\
& \quad \left. \left. 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \right. \right. \\
& \quad \left. \left. \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - \right. \right. \right. \\
& \quad \left. \left. 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \right. \right. \\
& \quad \left. \left. 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + \right. \right. \\
& \quad \left. \left. 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} \Big/ \left(3 \times 2^{1/3} \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)\right) \Bigg) \Bigg\} -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right.} \\
& \quad \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4)) \right) / \\
& \quad \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 \right. \\
& \quad \left. r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 - \right. \\
& \quad \left. r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right. \\
& \quad \left. 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \right. \\
& \quad \left. 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \right. \\
& \quad \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8)}^{1/3} \right) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right. \\
& \quad \left. 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \right. \\
& \quad \left. 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \right. \\
& \quad \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8)}^{1/3} \right) / \\
& \quad \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) / \\
& \quad \left( 4 \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4) \right) \right) / \\
& \quad \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + \right. \right. \\
& \quad \left. \left. 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - \right. \right. \\
& \quad \left. \left. 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 - \right. \right. \\
& \quad \left. \left. 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \right. \right. \\
& \quad \left. \left. \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8)}^{1/3} \right) + \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \right. \\
& \quad \left. \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + \right. \\
& \quad \left. 33 554 432 \pi^{18} r_1^6 + \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + \right.
\end{aligned}$$





$$\begin{aligned} & \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\ & 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\ & \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - } \\ & 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\ & 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\ & \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} / \\ & \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\ & \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) / \\ & \left( 4 \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\ & \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \right. \\ & \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\ & 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\ & 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - } \\ & 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\ & \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\ & 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\ & \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} + \\ & \left. (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\ & \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\ & 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + } \\ & 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\ & \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\ & 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \\ & \left. 474989023199232 \pi^{32} r_1^8) \right)^{1/3} / (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) \Big) \Big) \Big) \Big\} \Big\} \end{aligned}$$

**Plot**  $\left[ \left\{ \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \right. \right. \right.$

$$\left. \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + (2^{1/3} (16 \pi^4 - 512 \pi^8 + \right.} \right.$$

$$\begin{aligned}
& \left( 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) / \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 \right. \\
& \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) - \\
& \frac{1}{2} \sqrt[3]{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 \right. \right. \\
& \left. \left. r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 \right. \right. \\
& \left. \left. r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \right. \right. \\
& \left. \left. 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \right. \right. \\
& \left. \left. 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \left. \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) / \\
& \left( 4 \sqrt[3]{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.}
\end{aligned}$$

$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\
& \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\
& \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right.} \\
& \quad \quad 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\
& \quad \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\
& \quad \quad \left. \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \right. \\
& \quad \quad \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right. \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\
& \quad \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} \\
& \quad \quad r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad \quad \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \\
& \quad \quad \quad \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \Bigg) \Bigg)^{1/3} \Bigg) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \quad \quad \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg) \Bigg\} + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right.
\end{aligned}$$

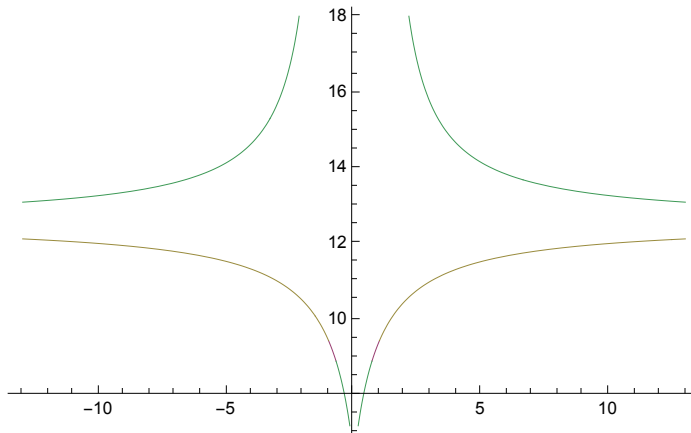
$$\begin{aligned}
& r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 \\
& + 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + \right. \\
& \quad 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + \\
& \quad 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \\
& \quad \left. \pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} - \\
& (128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \\
& \quad 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \\
& \quad \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - \right. \\
& \quad 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \\
& \quad 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \\
& \quad \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} \Bigg/ \\
& \left(3 \times 2^{1/3} \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)\right) - \left(\frac{768\,\pi^3}{1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2} + \frac{64\,\pi^3 \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right)^3}{\left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)^3} - \right. \\
& \quad \left. \frac{64\,\pi^3 \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right) \left(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2\right)}{\left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)^2} \right) \Bigg/ \\
& \left(4 \sqrt{\left(\frac{4\,\pi^2 \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right)^2}{\left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)^2} - \frac{8\,\pi^2 \left(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2\right)}{3 \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)} + \right. \right. \\
& \quad \left. \left(2^{1/3} \left(16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4\right)\right) \Bigg/ \right. \\
& \quad \left. \left(3 \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right) \left(128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + \right. \right. \\
& \quad 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - \\
& \quad 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - \right. \\
& \quad 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + \\
& \quad 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \\
& \quad 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \\
& \quad \left. \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}}\right) + \\
& \quad (128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \\
& \quad \pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + \\
& \quad 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left(1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + \right. \\
& \quad 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + \\
& \quad 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + \\
& \quad 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + \\
& \quad \left. \left. 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8\right)^{1/3}} \Bigg/ \left(3 \times 2^{1/3} \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)\right) \Bigg) \Bigg\}, \\
& \left\{ \frac{\pi \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right)}{1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2} + \frac{1}{2} \sqrt{\left(\frac{4\,\pi^2 \left(3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2\right)^2}{\left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)^2} - \frac{8\,\pi^2 \left(13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2\right)}{3 \left(1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2\right)} + \right. \right. \\
& \quad \left. \left(2^{1/3} \left(16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4\right)\right) \Bigg/ \right\}
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 \right. \\
& \quad \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \quad \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right. \\
& \quad \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \right. \\
& \quad \left. \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 \right. \\
& \quad \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \quad \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) / \\
& \quad \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Bigg) / \\
& \quad \left( 4 \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\
& \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\
& \quad 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right.} \\
& \quad \quad 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\
& \quad \quad \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \quad 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \\
& \quad \quad \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \\
& \quad \quad \left. \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \right. \\
& \quad \quad \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right.} \right. \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) / \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} \right. \\
& \quad \quad r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} \\
& \quad \quad r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \quad \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\
& \quad \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \quad \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) /
\end{aligned}$$

[illegible]





# A Notational Language for Describing the Geometry of Space-Time

by Parker Emmerson

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## I. Postulates, Structure

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle, the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + \eta^2$$

This is the initial radius squared expressed as the slant of the cone in terms of the height of the cone,  $\eta$ , and the radius of the base of the cone,  $r_1$

$$r = \sqrt{(r_1^2 + \eta^2)}$$

$$s = \theta r$$

$$s / \theta = r$$

The arc length taken out of a circle at a given time is =

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \quad \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - \eta^2$$

$$r_1 = \sqrt{(r^2 - \eta^2)}$$

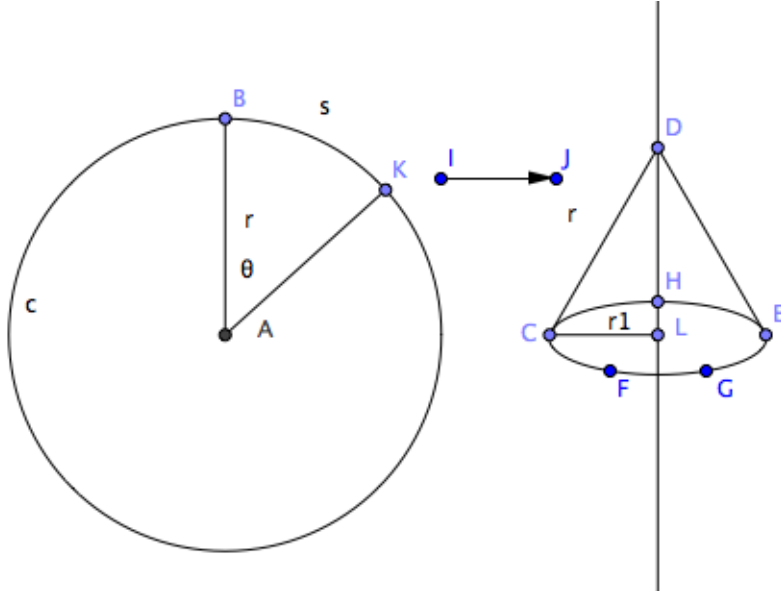
(96)

$$\eta \leq r$$

$$\tau = \text{time}$$

$$1 \text{ second} = 6 \text{ degrees}$$

$$\tau = 6 \theta$$



I will now do some algebra to conclude what the height of the cone is in terms of the initial parameters. It can eventually be reduced to a single variable.

$$\text{Solve}[r_1^2 + \eta^2 = r^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\} \quad (97)$$

We say that the amount of  $\theta r = s$ , taken out of the circle is the change in the circle's circumference that is the base of the cone. The change is equal to  $s = 2\pi r - 2\pi r_1$ .

Notice that  $\theta =$

$$((2\pi r) / r) - ((2\pi r_1) / r), \text{ because we divide by } r \text{ on both sides.}$$

We will focus on the positive solutions for the height of the cone.

$$\text{Solve}[\eta == \sqrt{r^2 - r_1^2}, r_1]$$

$$\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2 - \eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2 - \eta^2} \right\} \right\} \quad (98)$$

This is the change in circumference with

the substituted expression for  $r_1$  in terms of  $h$  and  $r$ .

$$r\theta == s = 2\pi(r) - 2\pi\sqrt{(r)^2 - \eta^2} = 2\pi(r) - 2\pi r_1 \quad (99)$$

$$\theta == (2\pi r) / r - (2\pi r_1) / r = ((2\pi r) / r) - \left( \left( 2\pi \sqrt{-\eta^2 + r^2} \right) / r \right)$$

$$\text{Solve}[\theta * r == 2\pi(r) - 2\pi\sqrt{(r)^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\} \quad (100)$$

$$\text{Solve}\left[\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\} \quad (101)$$

## II. Motion through the Space - Time

If there is something traveling over the distance,  $\eta$ , then its velocity is said to be the first derivative with respect to time. What if  $r$  is constant, which it is when it's the hypotenuse of the triangle made by the cone.

$v = \text{frequency} = 1 / \tau = (1 / (1080 / \pi) \theta)$ ,  
because each second is in terms of degrees of a clock, and in terms of theta,  
which is in radians, we must make the following conversion :

$$\text{Time} = 6 (\theta_{\text{degrees}}) = 6 (180 / \pi) \theta = (1080 / \pi) \theta$$

$$\eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$v = \lambda v = r (1 / (1080 / \pi) \theta) = ((1 / (1080 / \pi)) D[\eta, \theta]) = 1 / (1080 / \pi)$$

$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right] \quad (103)$$

The velocity of  $\eta$  is equal to the first derivative of  $\eta$  with respect to time. The constant  $(1/(1080/\pi))$  is taken out of the equation in order to perform the derivative.

$$(1 / (1080 / \pi)) D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$(1 / (1080 / \pi)) D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \left( \sqrt{1 - ((v)^2 / c^2)} \right), \theta\right]$$

$$\frac{\sqrt{1 - \frac{v^2}{c^2}} (4\pi r^2 - 2r^2 \theta)}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}} = c$$

$$c := (2.99792458 * 10^8)$$

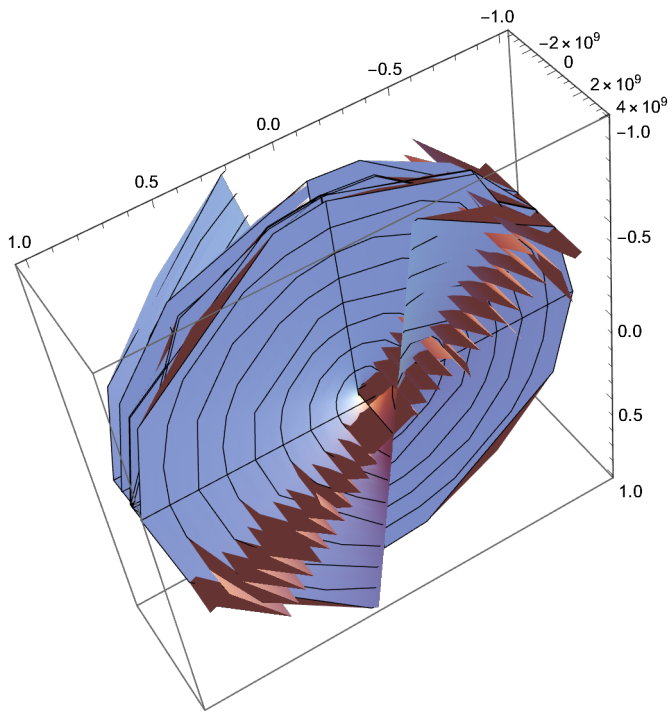
$$\text{Solve}\left[\frac{\sqrt{1-\frac{v^2}{c^2}}(4\pi r^2-2r^2\theta)}{4320\sqrt{4\pi r^2\theta-r^2\theta^2}}==c,v\right]$$

$$\left\{\left\{v\rightarrow-\frac{c\sqrt{4\pi^2-4\pi\theta-\frac{18662400c^2\pi\theta}{r^2}+\theta^2+\frac{4665600c^2\theta^2}{r^2}}}{\sqrt{4\pi^2-4\pi\theta+\theta^2}}\right\},\right. \\ \left.\left\{v\rightarrow\frac{c\sqrt{4\pi^2-4\pi\theta-\frac{18662400c^2\pi\theta}{r^2}+\theta^2+\frac{4665600c^2\theta^2}{r^2}}}{\sqrt{4\pi^2-4\pi\theta+\theta^2}}\right\}\right\}$$

$$(1/(1080/\pi))$$

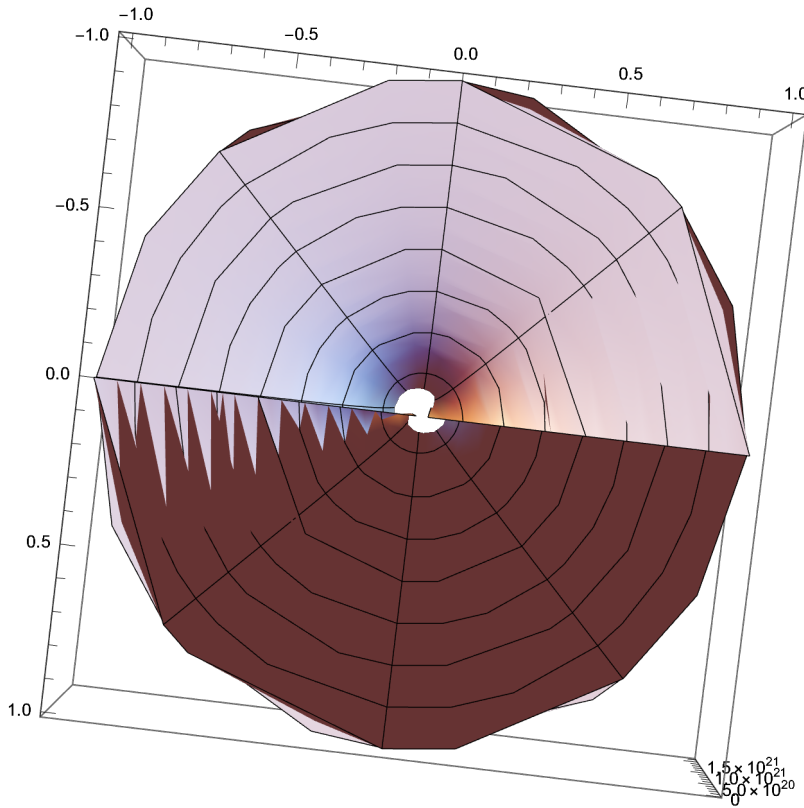
$$D\left[\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\sqrt{1-\left(\frac{c\sqrt{4\pi^2-4\pi\theta-\frac{18662400c^2\pi\theta}{r^2}+\theta^2+\frac{4665600c^2\theta^2}{r^2}}{\sqrt{4\pi^2-4\pi\theta+\theta^2}}\right)^2/c^2},\theta\right]$$

$$\text{RevolutionPlot3D}\left[\frac{1}{1080}\pi\left(\left(\sqrt{4\pi r^2\theta - r^2\theta^2}\left(-\frac{4\pi - \frac{18662400c^2\pi}{r^2} + 2\theta + \frac{9331200c^2\theta}{r^2}}{\frac{4\pi^2 - 4\pi\theta + \theta^2}{}} + \frac{(-4\pi + 2\theta)\left(4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}\right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2}\right)\right)/\right. \\ \left.+\left(4\pi\sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}\right) + \frac{(4\pi r^2 - 2r^2\theta)\sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right)\right], \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$



RevolutionPlot3D[  

$$\frac{c \sqrt{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



Solve[m  $\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \left( \sqrt{1 - \left( \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)^2 / c^2} \right) == m c,$ ]

D[ $\frac{c \sqrt{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \theta]$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} =$$

velocity through the height of the cone when r is constant (104)

(stays always the initial radius of the circle equal to the hypoteneuse of the triangle formed by the height meeting the base of the cone) .

(1 / (1080 / π)) (1 / (1080 / π)) D[(r / θ), θ]

$$\text{Solve}\left[-\frac{\pi^2 r}{1166400 \theta^2} == \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \pi \text{Root}\left[-4 + \pi 1 + 1166400 \pi^3 - 1166400 \pi^4 + 291600 \pi^5 \&, 1\right] \right\}, \right. \\ & \left\{ \theta \rightarrow \pi \text{Root}\left[-4 + \pi 1 + 1166400 \pi^3 - 1166400 \pi^4 + 291600 \pi^5 \&, 2\right] \right\}, \\ & \left\{ \theta \rightarrow \pi \text{Root}\left[-4 + \pi 1 + 1166400 \pi^3 - 1166400 \pi^4 + 291600 \pi^5 \&, 3\right] \right\}, \\ & \left\{ \theta \rightarrow \pi \text{Root}\left[-4 + \pi 1 + 1166400 \pi^3 - 1166400 \pi^4 + 291600 \pi^5 \&, 4\right] \right\}, \\ & \left. \left\{ \theta \rightarrow \pi \text{Root}\left[-4 + \pi 1 + 1166400 \pi^3 - 1166400 \pi^4 + 291600 \pi^5 \&, 5\right] \right\} \right\} \end{aligned}$$

$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == r (1 / (1080 / \pi) \theta), \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} \right.} \right. \right. \\ & \quad \left. \left. \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right)^{1/3}} \right) - \right. \right. \\ & \quad \left. \left. \frac{1}{2} \sqrt{\left( -\frac{1}{3 \pi^2} + 8 \pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} \right.} \right. \right. \\ & \quad \left. \left. \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right)^{1/3}} \right) - \right. \right. \\ & \quad \left. \left. \left( \frac{4}{\pi} + 64 \pi^3 \right) \middle/ \left( 4 \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} \right.} \right. \right. \right. \\ & \quad \left. \left. \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right)^{1/3}} \right) + 1 \middle/ \left( 6 \times \right. \right. \right. \\ & \quad \left. \left. \left. 2^{2/3} \pi^2 \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right)^{1/3} \right) \right) \right) \right\}, \\ & \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( -\frac{1}{6 \pi^2} + 4 \pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right) \right)^{1/3}}{12 \pi^2} \right.} \right. \\ & \quad \left. \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648 \pi^8 + \sqrt{110592 \pi^8 + 764411904 \pi^{16}} \right)^{1/3}} \right) + \right. \end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{3\pi^2} + 8\pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} \right)} - \\
& \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} - \\
& \left( \frac{4}{\pi} + 64\pi^3 \right) \Bigg/ \left( 4 \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \right. \right. \\
& \left. \left. \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} + 1 \Bigg/ \left( 6 \times \right. \right. \right. \\
& \left. \left. \left. 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3} \right) \right) \right) \Bigg\}, \\
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} \right)} + \right. \\
& \left. \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} \right) - \\
& \frac{1}{2} \sqrt{\left( -\frac{1}{3\pi^2} + 8\pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} \right)} - \\
& \frac{1}{6 \times 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} + \\
& \left( \frac{4}{\pi} + 64\pi^3 \right) \Bigg/ \left( 4 \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \right. \right. \\
& \left. \left. \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} + 1 \Bigg/ \left( 6 \times \right. \right. \right. \\
& \left. \left. \left. 2^{2/3} \pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3} \right) \right) \right) \Bigg\},
\end{aligned}$$



$$\left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} + \frac{1}{6 \times 2^{2/3}\pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} \right)} + \frac{1}{2} \sqrt{\left( -\frac{1}{3\pi^2} + 8\pi^2 - \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} - \frac{1}{6 \times 2^{2/3}\pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3}} \right)} + \left( \frac{4}{\pi} + 64\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6\pi^2} + 4\pi^2 + \frac{\left( \frac{1}{2} \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right) \right)^{1/3}}{12\pi^2} + 1 / \left( 6 \times 2^{2/3}\pi^2 \left( 2 + 27648\pi^8 + \sqrt{110592\pi^8 + 764411904\pi^{16}} \right)^{1/3} \right) \right)} \right) \right\}$$

What is theta for a certain number of frequencies?

$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2\theta}{4320\sqrt{4\pi r^2\theta - r^2\theta^2}} == r n (1 / (1080 / \pi) \theta), \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow \pi - \right.$$

$$\frac{1}{2} \sqrt{\left( -\frac{1}{6n^2\pi^2} + 4\pi^2 + \frac{1}{12n^2\pi^2 \left( 1 + 13824n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}} + \frac{\left( 1 + 13824n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}}{12n^2\pi^2} \right)} -$$

$$\frac{1}{2} \sqrt{\left( -\frac{1}{3n^2\pi^2} + 8\pi^2 - \frac{1}{12n^2\pi^2 \left( 1 + 13824n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}} - \frac{\left( 1 + 13824n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912n^8\pi^8} \right)^{1/3}}{12n^2\pi^2} \right)} -$$

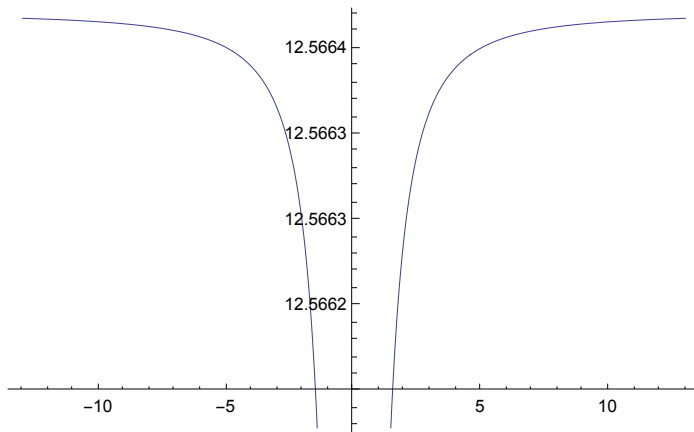
$$\begin{aligned}
& \frac{\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}}{12\,n^2\pi^2} - \\
& \left(\frac{4}{n^2\pi} + 64\pi^3\right) \Bigg/ \left(4\sqrt{\left(-\frac{1}{6\,n^2\pi^2} + 4\pi^2 + \right.}\right. \\
& \quad \left.1\Bigg/\left(12\,n^2\pi^2\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}\right) + \right. \\
& \quad \left.\left.\frac{\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}}{12\,n^2\pi^2}\right)\right)\Bigg)\Bigg), \left\{\Theta \rightarrow \pi - \right. \\
& \frac{1}{2}\sqrt{\left(-\frac{1}{6\,n^2\pi^2} + 4\pi^2 + \frac{1}{12\,n^2\pi^2\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}} + \right.} \\
& \quad \left.\frac{\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}}{12\,n^2\pi^2}\right)} + \\
& \frac{1}{2}\sqrt{\left(-\frac{1}{3\,n^2\pi^2} + 8\pi^2 - \frac{1}{12\,n^2\pi^2\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}} - \right.} \\
& \quad \left.\frac{\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}}{12\,n^2\pi^2}\right)} - \\
& \left(\frac{4}{n^2\pi} + 64\pi^3\right) \Bigg/ \left(4\sqrt{\left(-\frac{1}{6\,n^2\pi^2} + 4\pi^2 + \right.}\right. \\
& \quad \left.1\Bigg/\left(12\,n^2\pi^2\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}\right) + \right. \\
& \quad \left.\left.\frac{\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}}{12\,n^2\pi^2}\right)\right)\Bigg)\Bigg), \left\{\Theta \rightarrow \pi + \right. \\
& \frac{1}{2}\sqrt{\left(-\frac{1}{6\,n^2\pi^2} + 4\pi^2 + \frac{1}{12\,n^2\pi^2\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}} + \right.} \\
& \quad \left.\frac{\left(1 + 13\,824\,n^4\pi^8 + 96\sqrt{3}\pi^4\sqrt{n^4 + 6912\,n^8\pi^8}\right)^{1/3}}{12\,n^2\pi^2}\right)} -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} + \right. \\
& \quad \left. \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \right.} \right. \right. \\
& \quad \left. \left. \left. 1 / \left( 12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3} \right) + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \right) \Bigg\}, \left\{ \theta \rightarrow \pi + \right.
\end{aligned}$$

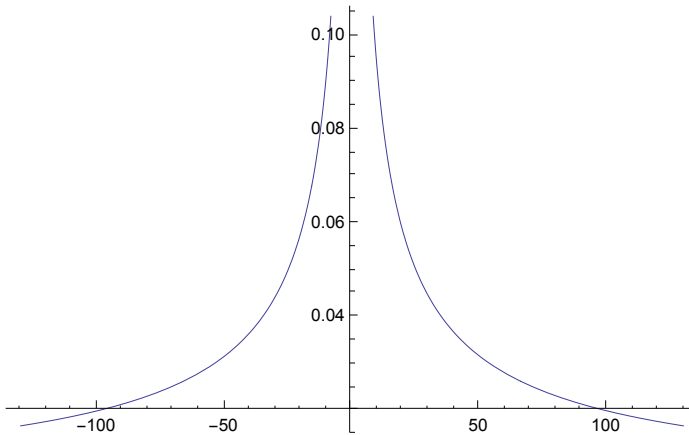
$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \\
& \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} + \right. \\
& \quad \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) / \left( 4 \sqrt{\left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \right.} \right. \\
& \quad \left. \left. \left. 1 / \left( 12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3} \right) + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \Bigg\} \Bigg\}
\end{aligned}$$

$$\begin{aligned}
 & \text{Plot} \left[ \pi + \frac{1}{2} \sqrt[3]{ \left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \right. \\
 & \quad \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) + \right. \\
 & \quad \frac{1}{2} \sqrt[3]{ \left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \\
 & \quad \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} + \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) / \right. \\
 & \quad \left. \left( 4 \sqrt[3]{ \left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \right. \\
 & \quad \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \right], \{n, -13, 13\} ]
 \end{aligned}$$



$$\begin{aligned}
 & \text{Plot} \left[ \pi + \frac{1}{2} \sqrt[3]{ \left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \right. \\
 & \quad \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) - \right. \\
 & \quad \left. \frac{1}{2} \sqrt[3]{ \left( -\frac{1}{3 n^2 \pi^2} + 8 \pi^2 - \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} - \right.} \right. \\
 & \quad \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} + \left( \frac{4}{n^2 \pi} + 64 \pi^3 \right) \right) / \right. \\
 & \quad \left. \left( 4 \sqrt[3]{ \left( -\frac{1}{6 n^2 \pi^2} + 4 \pi^2 + \frac{1}{12 n^2 \pi^2 \left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}} + \right.} \right. \right. \\
 & \quad \left. \left. \left. \frac{\left( 1 + 13824 n^4 \pi^8 + 96 \sqrt{3} \pi^4 \sqrt{n^4 + 6912 n^8 \pi^8} \right)^{1/3}}{12 n^2 \pi^2} \right) \right) \right) \right], \{n, -13, 13\} ]
 \end{aligned}$$



These are mathematical expressions of the reality of the four noble truths. Leaves falling from trees.

What would acceleration through the height of the cone be when r is constant?

$$v = \lambda v = r (1 / (1080 / \pi) \theta) =$$

$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] = (1 / (1080 / \pi)) D[\eta, \theta] = \text{velocity}$$

$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \text{velocity}$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \text{velocity of } \eta \text{ when } r \text{ is constant.}$$

$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == r (1 / (1080 / \pi) \theta), r\right]$$

{}

$$(1 / (1080 / \pi)) D\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta\right]$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8640 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2160 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080}$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8640 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2160 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} = \frac{\pi^3 r}{629856000 \theta^3} = \quad (107)$$

acceleration through the height of the cone when  $r$  is constant.

$$(1 / (1080 / \pi)) (1 / (1080 / \pi)) (1 / (1080 / \pi)) D[D[(r / \theta), \theta], \theta]$$

$$\frac{\pi^3 r}{629856000 \theta^3}$$

$$\text{Solve}\left[\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8640 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2160 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} == \frac{\pi^3 r}{629856000 \theta^3}, \theta\right]$$

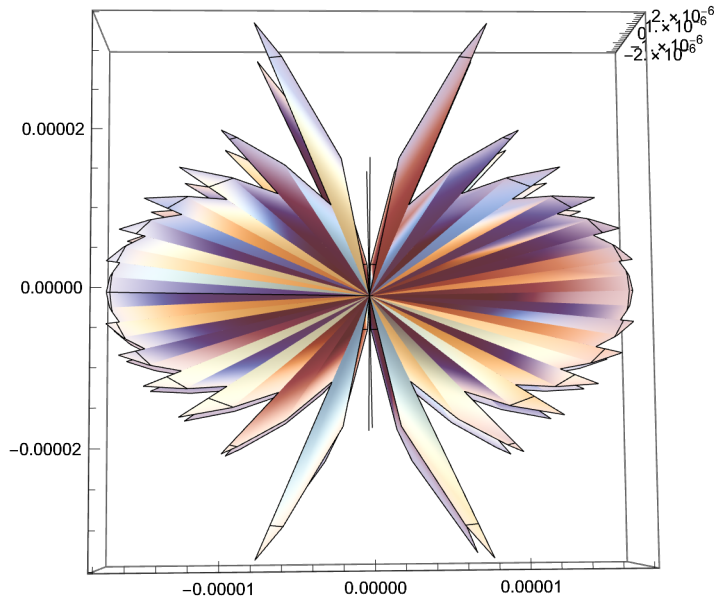
$$\left\{ \left\{ \theta \rightarrow \frac{4 (1 + 6480 \times 5^{1/3} - 36 \times 5^{2/3}) \pi}{1166401} \right\}, \right.$$

$$\left\{ \theta \rightarrow \frac{4 (1 - 3240 \times 5^{1/3} - 3240 \sqrt{3} 5^{1/3} + 18 \times 5^{2/3} - 18 \sqrt{3} 5^{2/3}) \pi}{1166401} \right\},$$

$$\left\{ \theta \rightarrow \frac{4 (1 - 3240 \times 5^{1/3} + 3240 \sqrt{3} 5^{1/3} + 18 \times 5^{2/3} + 18 \sqrt{3} 5^{2/3}) \pi}{1166401} \right\} \}$$

RevolutionPlot3D[  

$$r \frac{4 \left( 1 - 3240 \times 5^{1/3} - 3240 i \sqrt{3} 5^{1/3} + 18 \times 5^{2/3} - 18 i \sqrt{3} 5^{2/3} \right) \pi}{1166401}, \{r, -1, 1\}]$$



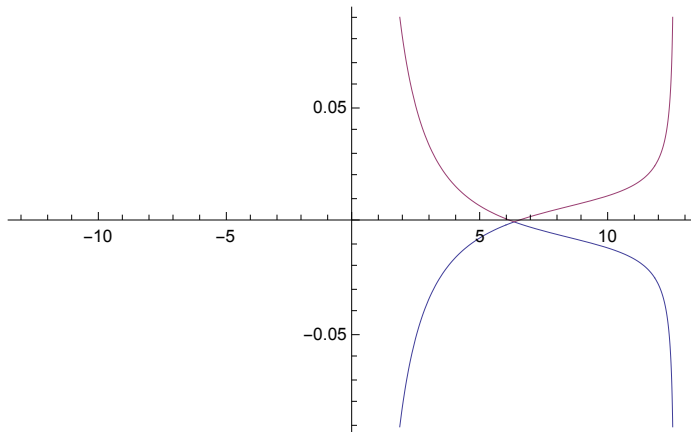
What happens if r is changing?

$$\begin{aligned} & (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta \right] \\ & \frac{\pi \left( - \frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} = \text{velocity when } r \text{ is changing} \end{aligned} \quad (107)$$

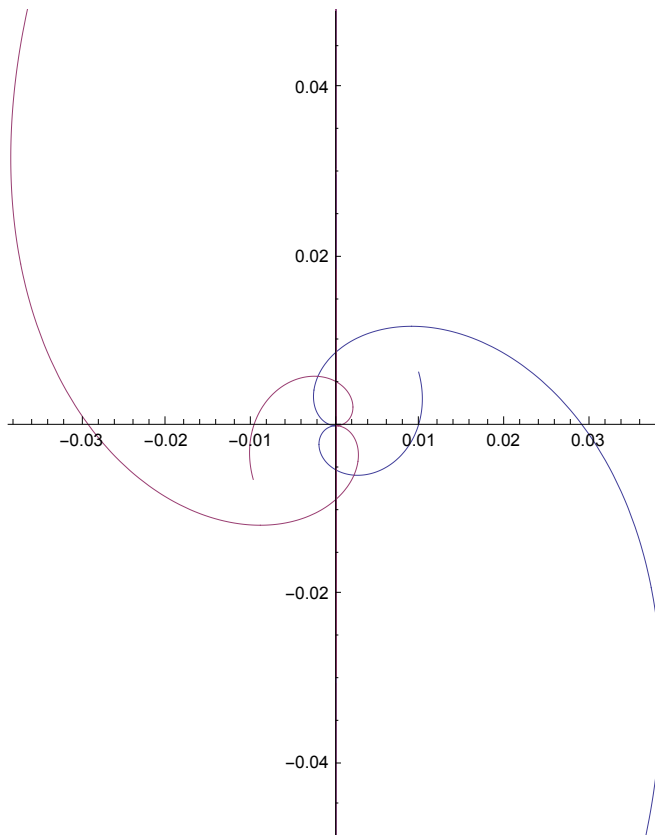
$$\text{Solve} \left[ \frac{\pi \left( - \frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} == r (1 / (1080 / \pi) \theta), r \right]$$

$$\left\{ \left\{ r \rightarrow - \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\} \right\}$$

$$\text{Plot}\left[\left\{-\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -13, 13\}\right]$$

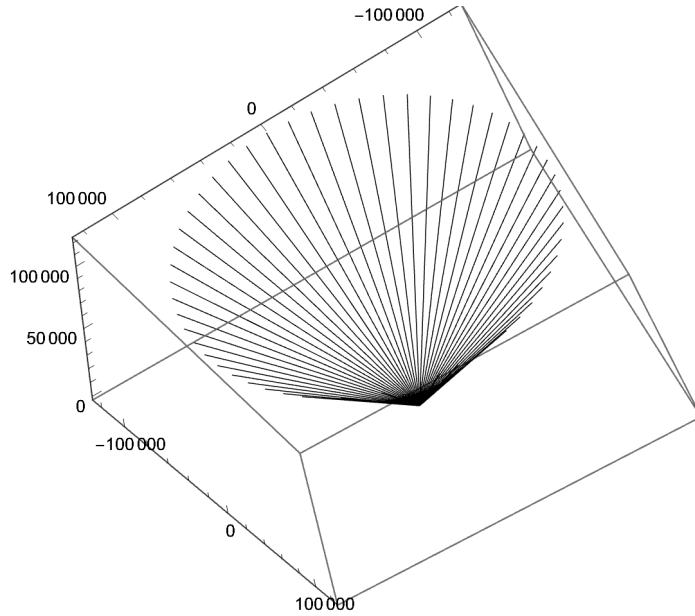


$$\text{PolarPlot}\left[\left\{-\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -10, 10\}\right]$$





RevolutionPlot3D $\left[\left\{-\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -10, 10\}\right]$



$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r = \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}$$

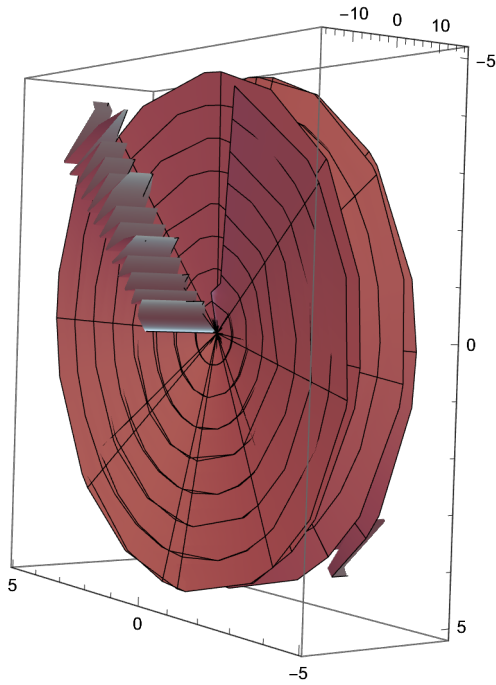
$$\text{Solve}\left[\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \eta\right]$$

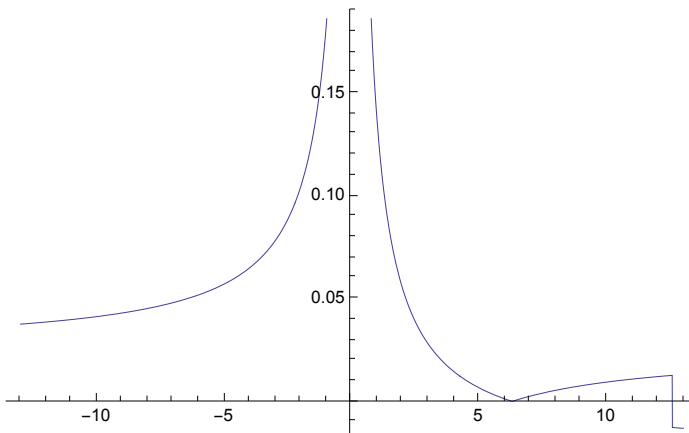
$$\left\{\left\{\eta \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}\right\}\right\}$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\}$$

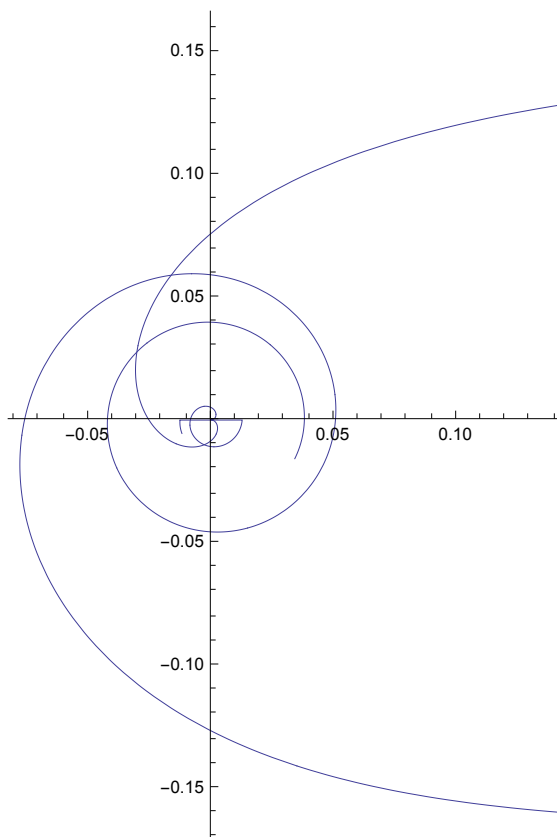
$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}, \theta\right]$$

$$\{\{\theta \rightarrow 2\pi\}\}$$

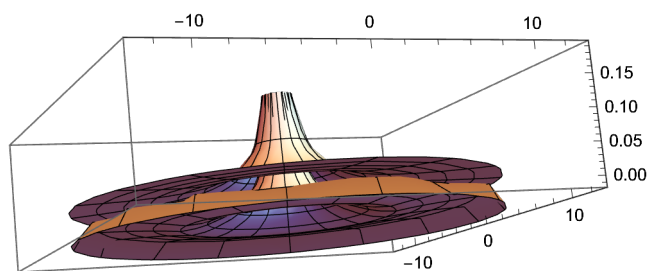
$$\text{RevolutionPlot3D}\left[\frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}}, \{\eta, -5, 5\}, \{\theta, -4\pi, 4\pi\}\right]$$


$$\text{Plot}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta-\theta^2}}{8\pi^2 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$$


PolarPlot $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$



RevolutionPlot3D $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$



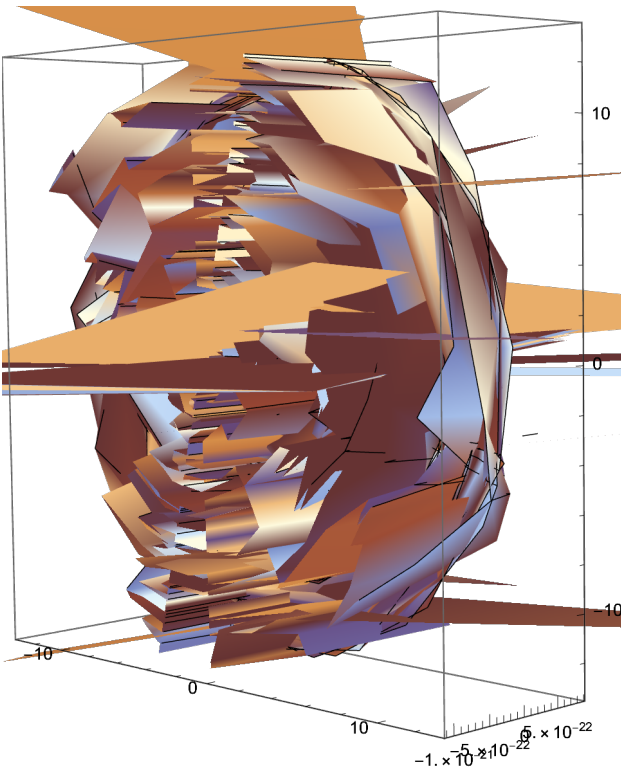
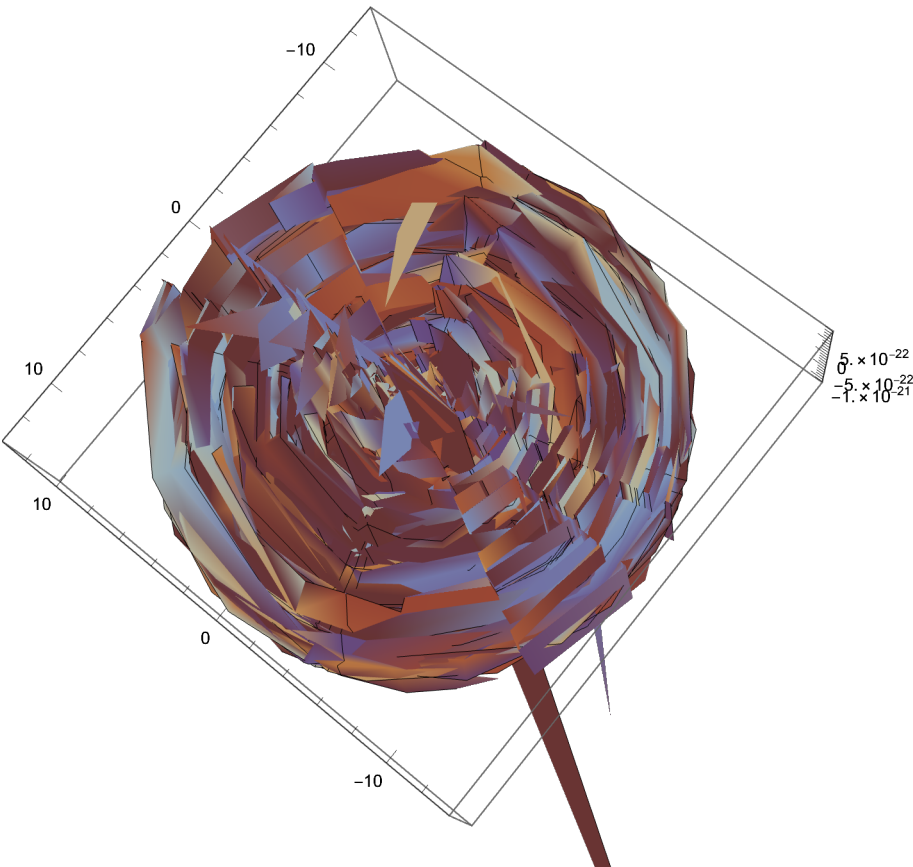
$$\begin{aligned}
& (1 / (1080 / \pi)) D \left[ \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080}, r, \theta \right] \\
& \frac{1}{1166400} \pi^2 \left( -\frac{15 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi r \theta - 2 r \theta^2)^2}{32 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \right. \\
& \frac{3 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi \theta - 2 \theta^2)}{16 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 (8 \pi r - 4 r \theta) (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \\
& \frac{3 r^2 (8 \pi r \theta - 2 r \theta^2)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{(8 \pi r - 4 r \theta)^2}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{(8 \pi - 4 \theta) (4 \pi r^2 - 2 r^2 \theta)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \\
& \left. \frac{r^2 (8 \pi \theta - 2 \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{1}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)
\end{aligned}$$

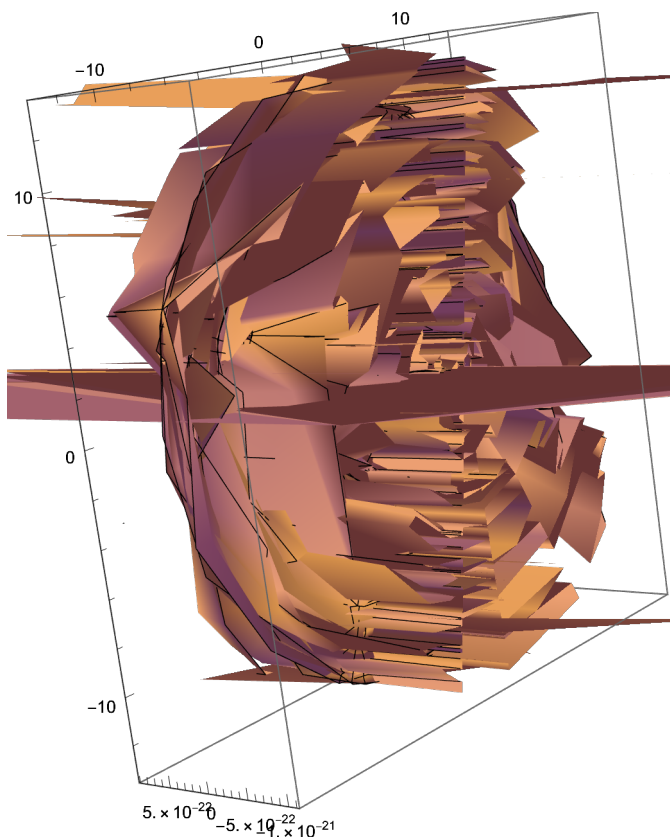
Acceleration when r is changing =

$$\begin{aligned}
& \frac{1}{1166400} \pi^2 \left( -\frac{15 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi r \theta - 2 r \theta^2)^2}{32 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \frac{3 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi \theta - 2 \theta^2)}{16 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \right. \\
& \frac{3 (8 \pi r - 4 r \theta) (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{3 r^2 (8 \pi r \theta - 2 r \theta^2)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \\
& \frac{(8 \pi r - 4 r \theta)^2}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{(8 \pi - 4 \theta) (4 \pi r^2 - 2 r^2 \theta)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \\
& \left. \frac{r^2 (8 \pi \theta - 2 \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{1}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)
\end{aligned}$$

RevolutionPlot3D[

$$\begin{aligned}
& \frac{1}{1166400} \pi^2 \left( -\frac{15 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi r \theta - 2 r \theta^2)^2}{32 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \frac{3 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi \theta - 2 \theta^2)}{16 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \right. \\
& \frac{3 (8 \pi r - 4 r \theta) (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{3 r^2 (8 \pi r \theta - 2 r \theta^2)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \\
& \frac{(8 \pi r - 4 r \theta)^2}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{(8 \pi - 4 \theta) (4 \pi r^2 - 2 r^2 \theta)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r^2 (8 \pi \theta - 2 \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \\
& \left. \frac{r (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{1}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right), \{r, -13, 13\}, \{\theta, -13, 13\}
\end{aligned}$$





$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\} \right\}$$

$$r := \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}$$

$$\eta == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}$$

$$\text{Solve}\left[r == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3} + \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right)} \right\} \right\}$$

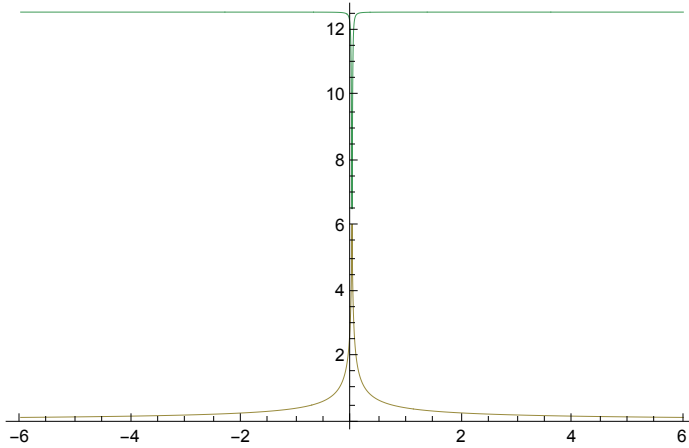
$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) \right) /} \\
& \quad \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \Bigg) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) + \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) \right) /} \\
& \quad \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \Bigg) \Bigg) \Bigg) \Bigg\}, \\
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) - \\
& \quad \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) \right) /} \\
& \quad \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \Bigg) \Bigg) \Bigg) \Bigg\},
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} + \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right.} \\
& \quad \left. \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right.} \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \right\}, \\
& \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right\} + \\
& \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} + \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \right.} \\
& \quad \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \right\} \} \\
& \text{Plot}\left[\left\{\left\{\pi - \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right.} \right.} \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right\} - \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right.} \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\}, \\
& \left\{ \pi - \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right\} + \\
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} - \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right.} \\
& \quad \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right\} -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \right) \Bigg\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right\} + \\
& \frac{1}{2} \sqrt{\left( 8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} + \left( 64\pi^3 + \frac{4}{\pi r^2} \right) / \right. \\
& \quad \left( 4 \sqrt{\left( 4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 \left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left( 1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8} \right)^{1/3}}{12\pi^2 r^2} \right) \right) \Bigg\} \Bigg\}, \{r, -6, 6\} ]
\end{aligned}$$



### III. What would the solutions be through acceleration?

When  $r$  is constant

$$v = \lambda v = r \left( \frac{1}{(1080/\pi) \theta} \right) = \left( \frac{1}{(1080/\pi)} \right) D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right]$$

$$\left( \frac{1}{(1080/\pi)} \right) \left( \frac{1}{(1080/\pi)} \right) \left( \frac{1}{(1080/\pi)} D[D[(r/\theta)], \theta], \theta \right) =$$

acceleration of a wavelength,  $r$ , of frequency,  $(1/(1080/\pi) \theta)$ . (108)

$$\left( \frac{1}{(1080/\pi)} \right) D[r (1/(1080/\pi) \theta), \theta]$$

$$\frac{\pi^2 r}{1166400} = \text{velocity}$$

$$\left( \frac{1}{(1080/\pi)} \right) \left( \frac{1}{(1080/\pi)} \right) \left( \frac{1}{(1080/\pi)} D[D[(r/\theta), \theta], \theta] \right)$$

$$\frac{\pi^3 r}{629856000 \theta^3}$$

$$\left( \frac{1}{(1080/\pi)} \right) D \left[ \left( \frac{1}{(1080/\pi)} \right) D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right], \theta \right]$$

$$\frac{\pi \left( -\frac{(4\pi r^2 - 2r^2 \theta)^2}{8640 (4\pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2160 \sqrt{4\pi r^2 \theta - r^2 \theta^2}} \right)}{1080} = a$$

$$\left( \frac{1}{(1080/\pi)} \right) D \left[ \left( \frac{1}{(1080/\pi)} \right) D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right], \theta \right] =$$

acceleration through the height of the cone (109)

$$\text{Solve}\left[\frac{\pi^2 r}{1166400} == (1 / (1080 / \pi)) D\left[(1 / (1080 / \pi)) D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \theta\right], \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2 \pi - \sqrt{-(-2 \pi)^{2/3} + 4 \pi^2}\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{-(-2 \pi)^{2/3} + 4 \pi^2}\right\}, \right.$$

$$\left.\left\{\theta \rightarrow 2 \pi - \sqrt{4 \pi^2 - (2 \pi)^{2/3}}\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{4 \pi^2 - (2 \pi)^{2/3}}\right\}, \right.$$

$$\left.\left\{\theta \rightarrow 2 \pi - \sqrt{4 \pi^2 + (-1)^{1/3} (2 \pi)^{2/3}}\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{4 \pi^2 + (-1)^{1/3} (2 \pi)^{2/3}}\right\}\right\}$$

$$\frac{\pi^3 r}{629856000 \theta^3} = \text{acceleration}$$

## IV. Defining the Initial Distance through its Geometric Correlates

When r is constant

$$r = \frac{2 * \text{velocity} * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} = \frac{2 * \left(\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} =$$

velocity through the height of the cone when r is constant (110)

(stays always the initial radius of the circle equal to the hypoteneuse of the triangle formed by the height meeting the base of the cone) .

$$\text{Solve}\left[\frac{2 * \left(\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} == r, \theta\right]$$

$$\{\{\theta \rightarrow 3 \pi\}\}$$

When r is changing

$$r = \frac{2 * \text{velocity} * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}} =$$

$$\frac{\pi \left(-\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right)}{1080}$$

velocity =  $\lambda v = r (1 / (1080 / \pi) \theta)$  (110)

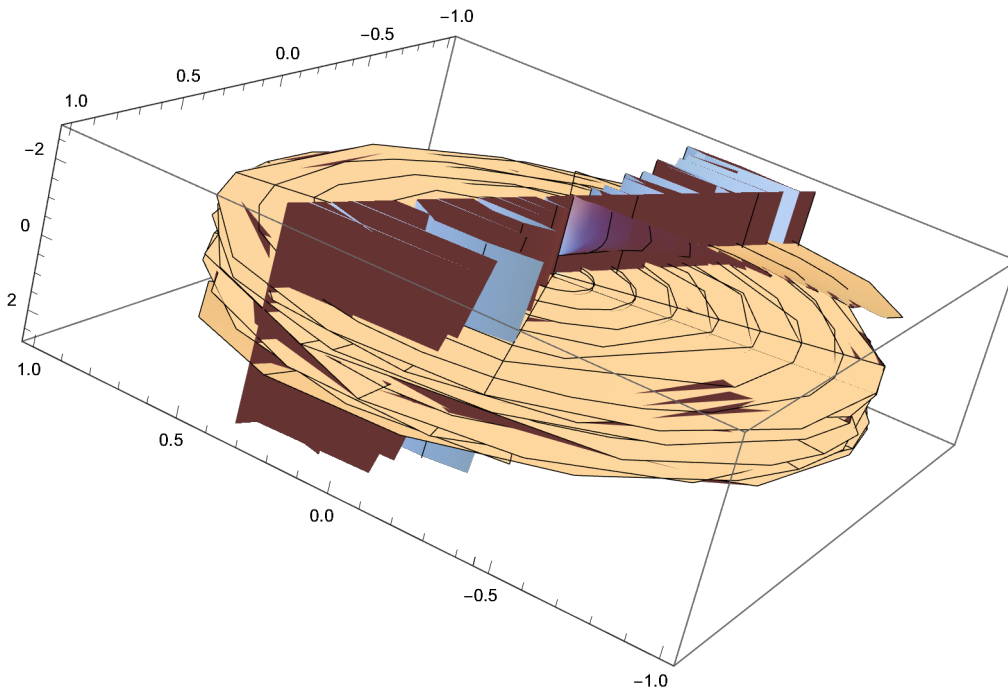
$$\text{Solve}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}==r(1/(1080/\pi)\theta),r\right]$$

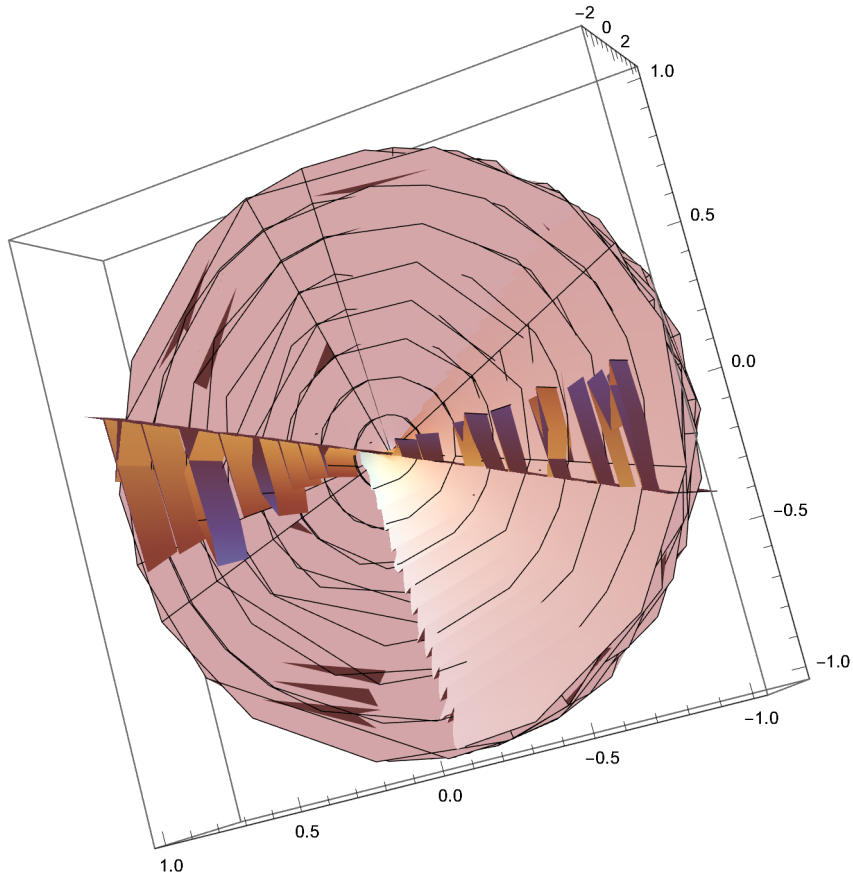
$$\left\{\left\{r\rightarrow-\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\},\left\{r\rightarrow\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\} \quad (111)$$

$$r = \frac{2 * \text{velocity} * 6 ((180/\pi)\theta) * \pi}{\sqrt{4\pi\theta - (\theta)^2}} =$$

$$\frac{2 * \left(\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}\right) * 6 ((180/\pi)\theta) * \pi}{\sqrt{4\pi\theta - (\theta)^2}}$$

$$\text{RevolutionPlot3D}\left[\frac{2 * \left(\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}\right) * 6 ((180/\pi)\theta) * \pi}{\sqrt{4\pi\theta - (\theta)^2}}, \{r, -1, 1\}, \{\theta, -13, 13\}\right]$$

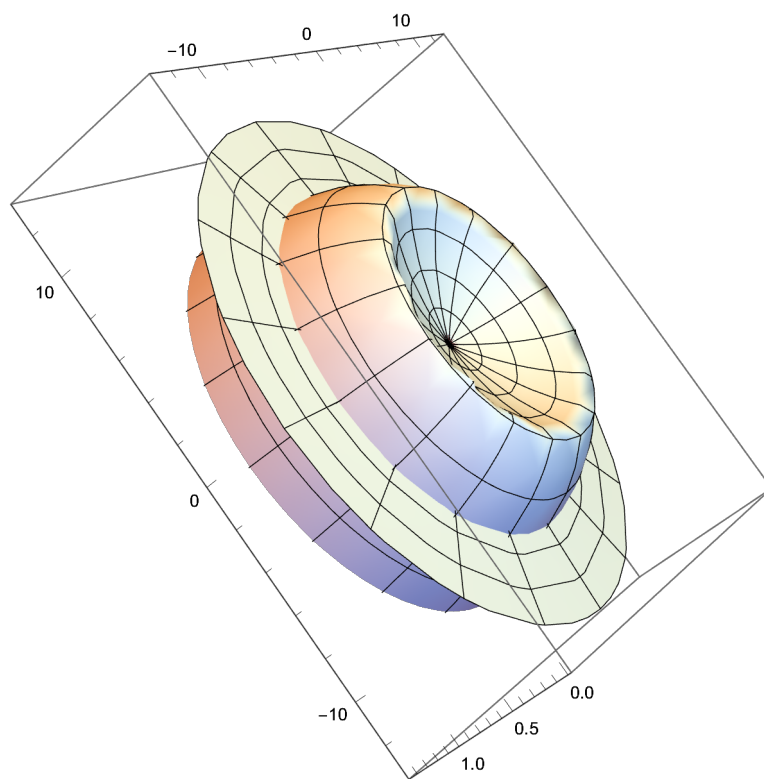
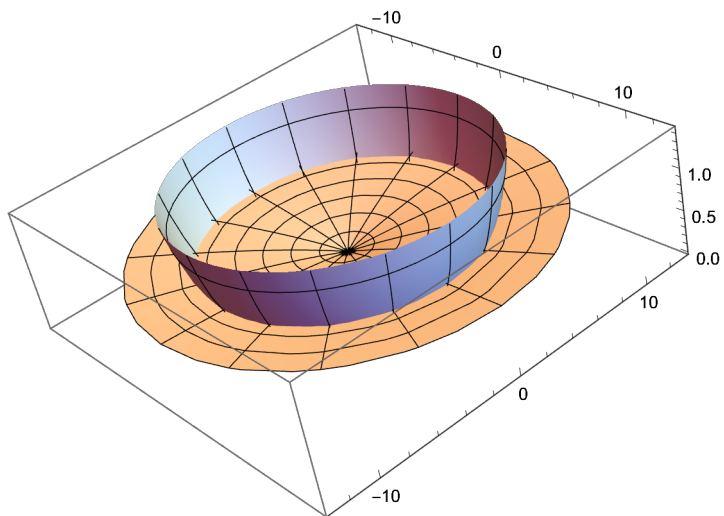




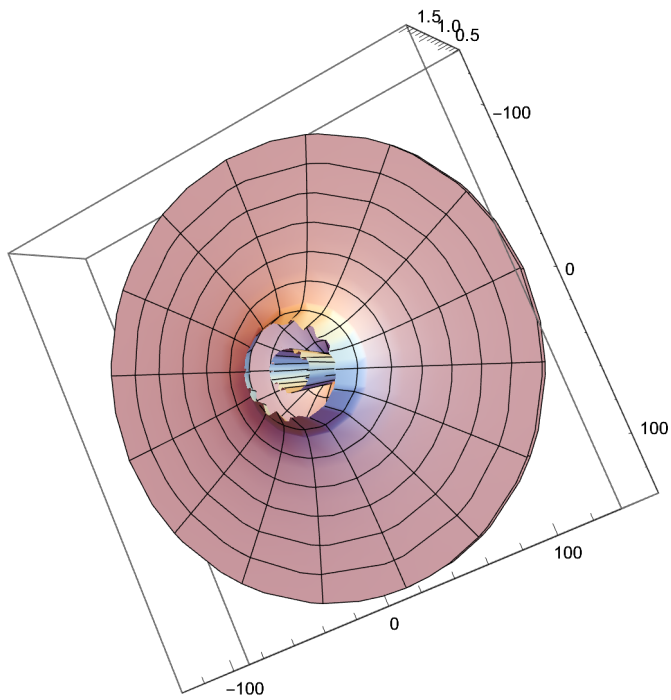
$$\text{Solve}\left[r == \frac{2 * \left( \frac{\pi \left( -\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right)}{1080} \right) * 6 * (180 / \pi) \theta * \pi}{\sqrt{4\pi\theta - (\theta)^2}}, r \right]$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} \right\} \right\}$$

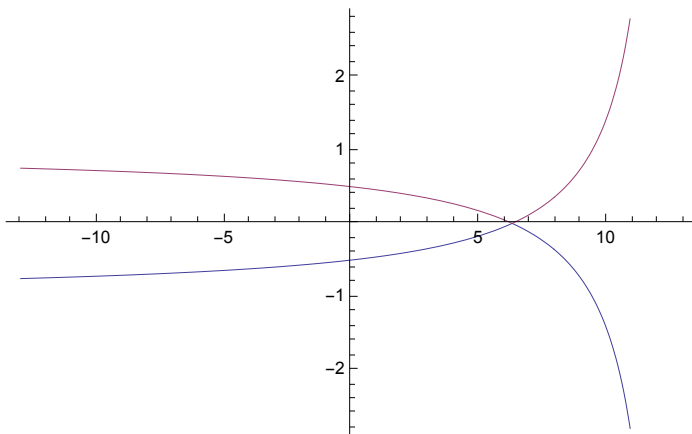
`RevolutionPlot3D` $\left[\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}, \{\theta, -13, 13\}\right]$



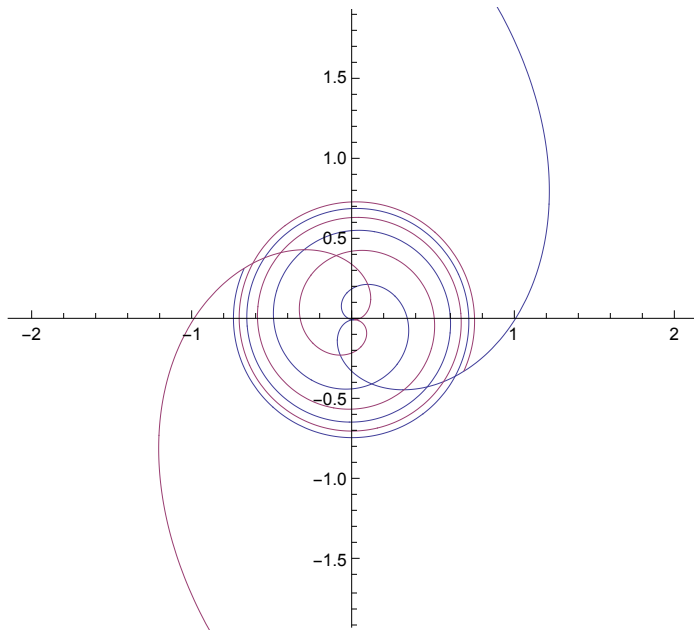
RevolutionPlot3D $\left[\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}, \{\theta, -130, 130\}\right]$

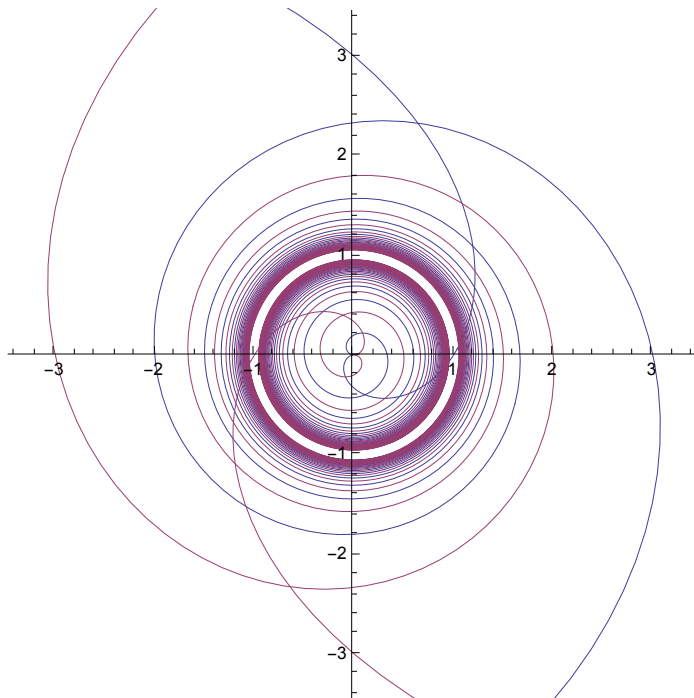


Plot $\left[\left\{-\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}, \sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right\}, \{\theta, -13, 13\}\right]$

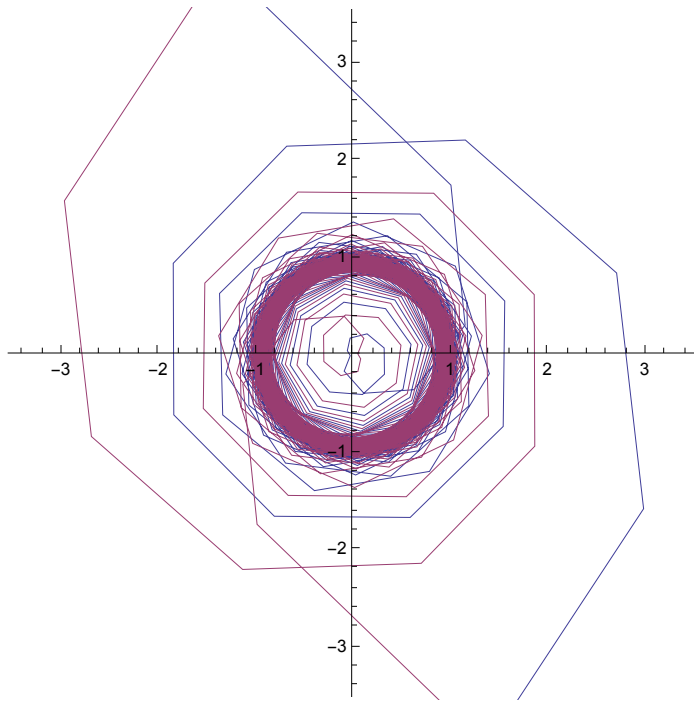




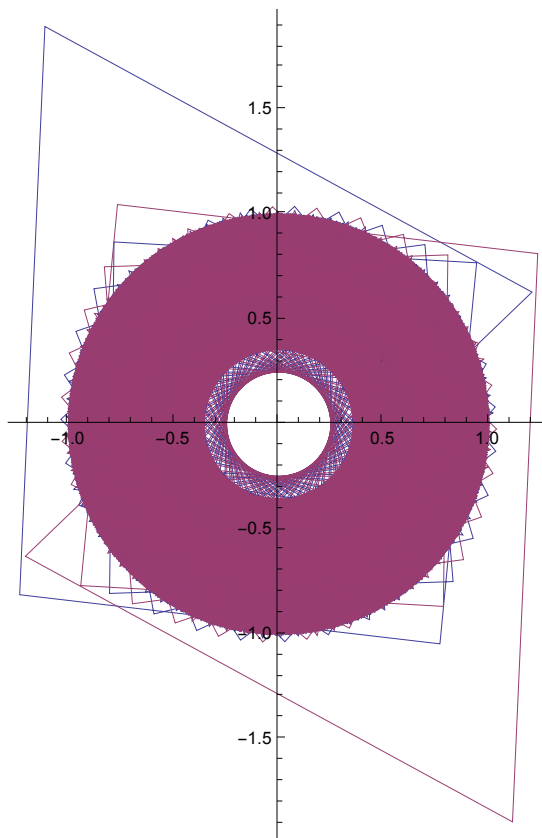
$$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}}-\frac{4\pi}{4\pi-\theta}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}}-\frac{4\pi}{4\pi-\theta}\right\}, \{\theta, -13, 13\}\right]$$


$$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}}-\frac{4\pi}{4\pi-\theta}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}}-\frac{4\pi}{4\pi-\theta}\right\}, \{\theta, -130, 130\}\right]$$


`PolarPlot` $\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -1300, 1300\}\right]$

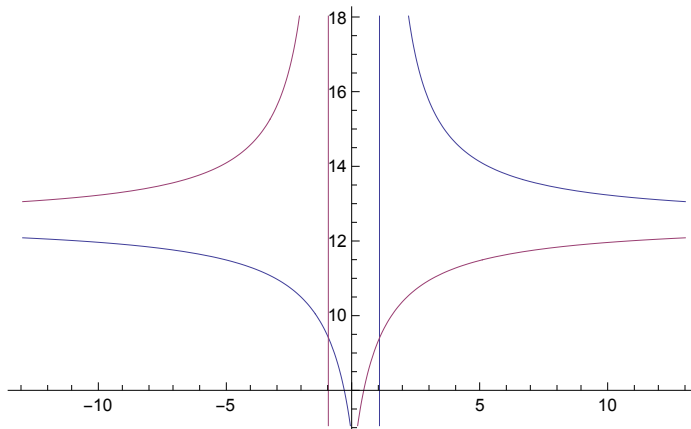


$\text{PolarPlot}\left[\left\{-\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right\}, \{\theta, -13000, 13000\}\right]$

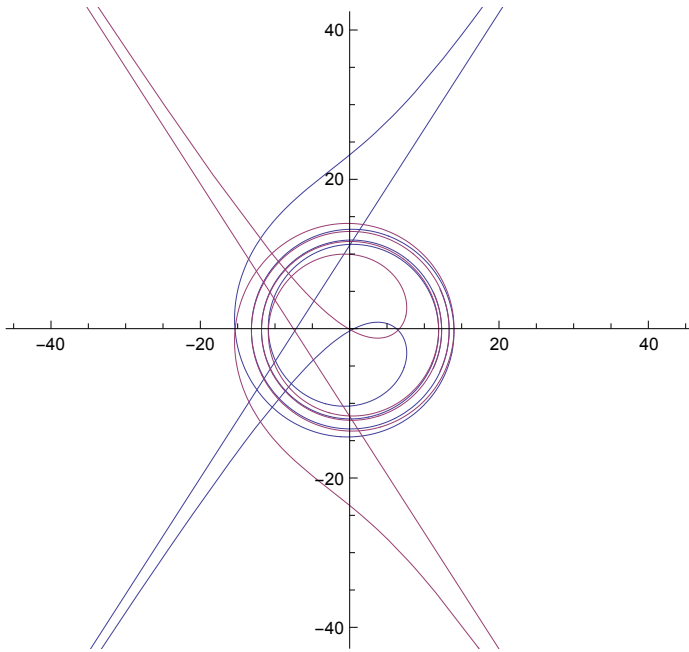


$\text{Solve}\left[r == \sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}, \theta\right]$   
 $\left\{\left\{\theta \rightarrow \frac{2(-\pi+2\pi r)}{-1+r}\right\}, \left\{\theta \rightarrow \frac{2(\pi+2\pi r)}{1+r}\right\}\right\}$

$\text{Plot}\left[\left\{\frac{2(-\pi+2\pi r)}{-1+r}, \frac{2(\pi+2\pi r)}{1+r}\right\}, \{r, -13, 13\}\right]$



PolarPlot[ $\left\{\frac{2(-\pi + 2\pi r)}{-1 + r}, \frac{2(\pi + 2\pi r)}{1 + r}\right\}, \{r, -13, 13\}$ ]



## V. Dealing with n

$$\eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$v = \lambda v = r (1 / (1080 / \pi)) \theta = ((1 / (1080 / \pi)) D[\eta, \theta]) = 1 / (1080 / \pi)$$

$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right] \quad (112)$$

The velocity of  $\eta$  is equal to the first derivative of  $\eta$  with respect to time. The constant  $(1/(1080/\pi))$  is taken out of the equation in order to perform the derivative.

$$(1 / (1080 / \pi)) D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$v = \lambda * v$$

$$\text{Solve}\left[m c^2 == \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} n (1 / (1080 / \pi) \theta), n\right]$$

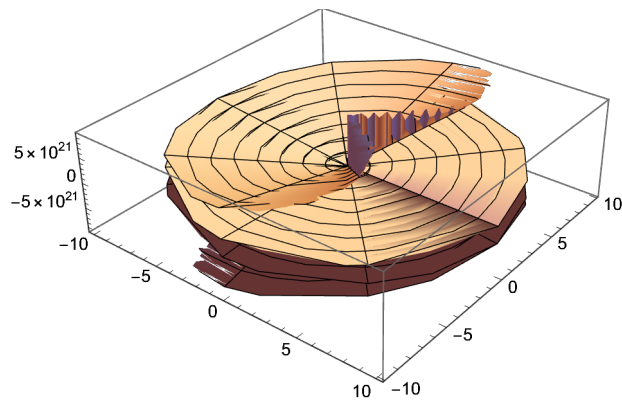
$$\left\{\left\{n \rightarrow \frac{1080 c^2 m}{\pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \theta}\right\}\right\}$$

$$c := (2.99792458 * 10^8)$$

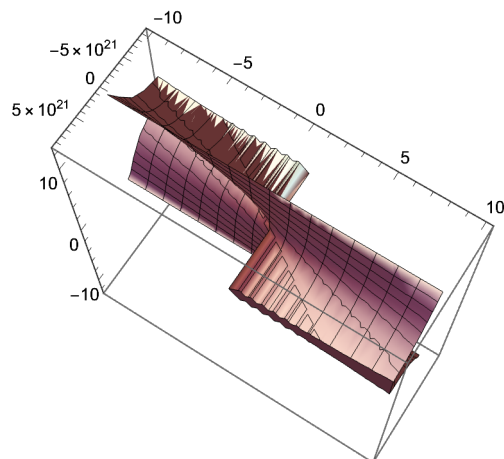
$$\text{Solve}\left[m c^2 == \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} n (1 / (1080 / \pi) \theta), n\right]$$

$$\left\{\left\{n \rightarrow \frac{4320 c^2 m}{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{4320 c^2 m}{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}, \{m, -10, 10\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



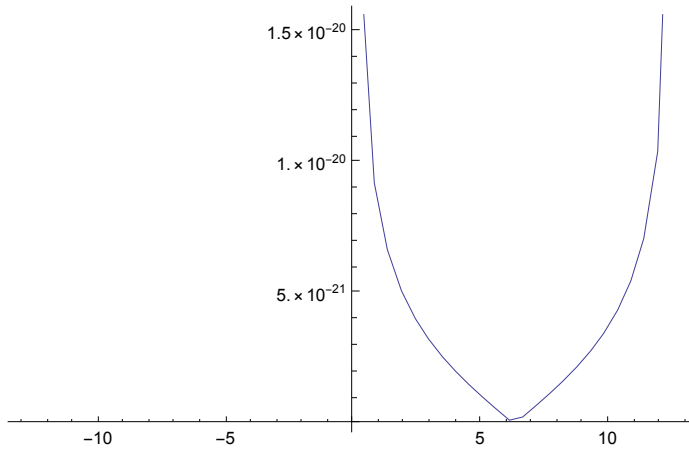
$$\text{Plot3D}\left[\frac{4320 c^2 m}{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}, \{m, -10, 10\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



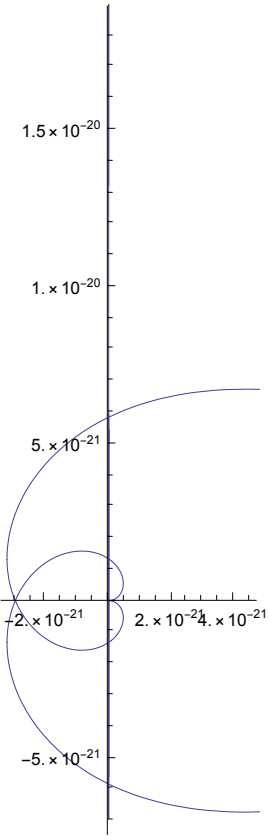
$$\text{Solve}\left[m c^2 = \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} (1 / (1080 / \pi) \theta), m\right]$$

$$\left\{\left\{m \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}{4320 c^2}\right\}\right\}$$

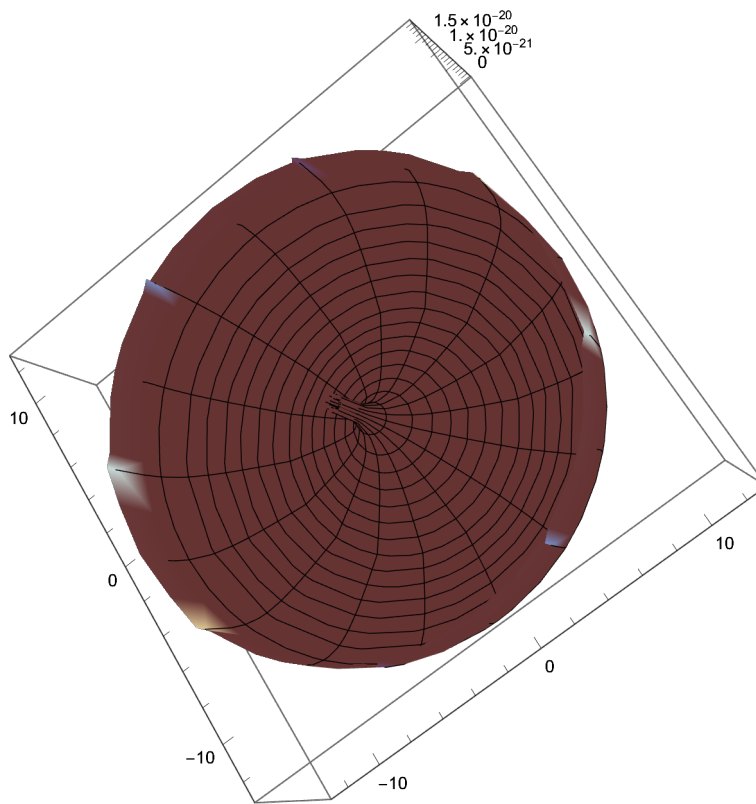
$$\text{Plot}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}{4320 c^2}, \{\theta, -13, 13\}\right]$$



PolarPlot[ $\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}{4320 c^2}, \{\theta, -13, 13\}$ ]

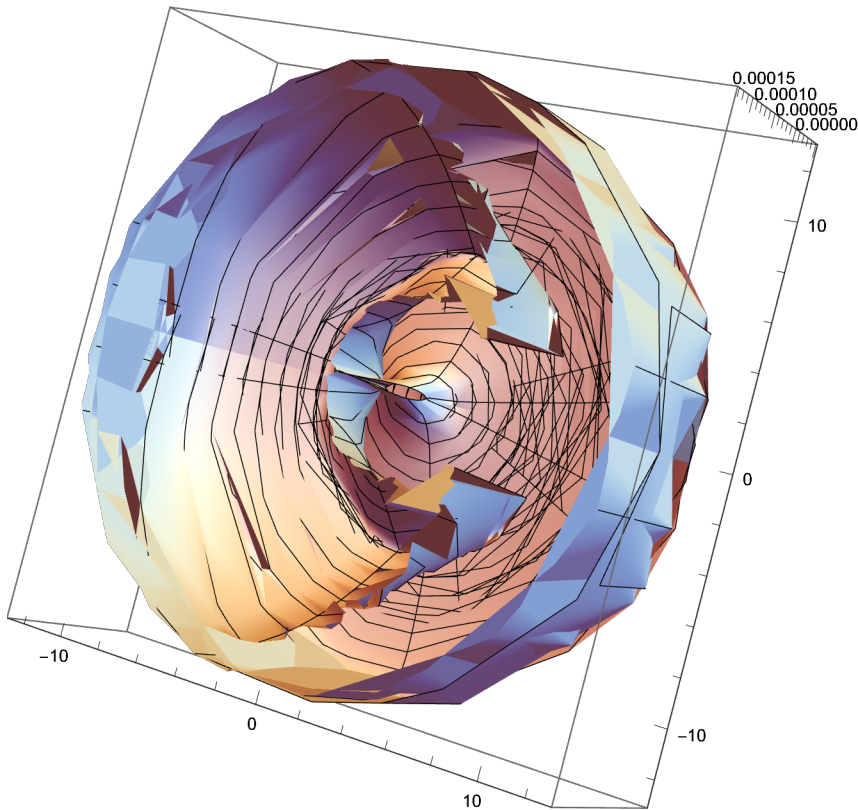


$$\text{RevolutionPlot3D}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}{4320 c^2}, \{\theta, -13, 13\}\right]$$





RevolutionPlot3D $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}{4320 c^2}, \{\theta, -13, 13\}, \{c, -13, 13\}\right]$



$$\left\{\left\{r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right\}, \left\{r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right\}\right\}$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\}$$

Solve[m c^2 == r n (1 / (1080 / π) θ) , n]

$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2\theta}{4320\sqrt{4\pi r^2\theta - r^2\theta^2}} == r n (1 / (1080 / \pi) \theta), n\right]$$

$$\left\{\left\{n \rightarrow \frac{r(2\pi - \theta)}{2\pi\theta\sqrt{r^2(4\pi - \theta)\theta}}\right\}\right\}$$

$$\left\{\left\{\eta \rightarrow \frac{135\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}\sqrt{4\pi\theta - \theta^2}}{\pi^3\sqrt{\theta}}\right\}\right\}$$

$$D\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \theta\right]$$

$$\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} (4\pi - 2\theta)}{2\pi^3 \sqrt{\theta} \sqrt{4\pi\theta - \theta^2}} -$$

$$\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \theta^{3/2}} + \frac{135 \left( \frac{1}{(4\pi-\theta)^2} - \frac{8\pi}{\theta^3} + \frac{3}{\theta^2} \right) \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}}$$

$$\text{Solve}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} (4\pi - 2\theta)}{2\pi^3 \sqrt{\theta} \sqrt{4\pi\theta - \theta^2}} - \frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \theta^{3/2}} + \right.$$

$$\left. \frac{135 \left( \frac{1}{(4\pi-\theta)^2} - \frac{8\pi}{\theta^3} + \frac{3}{\theta^2} \right) \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}} == r n (1 / (1080 / \pi) \theta), n\right]$$

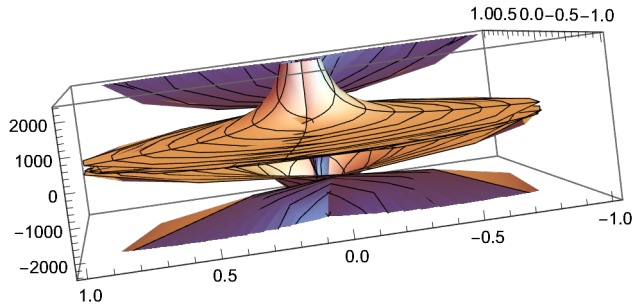
$$\left\{ \left\{ n \rightarrow -\frac{1}{\pi r \theta} 1080 \left( -\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} (4\pi - 2\theta)}{2\pi^3 \sqrt{\theta} \sqrt{4\pi\theta - \theta^2}} + \frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \theta^{3/2}} - \frac{135 \left( \frac{1}{(4\pi-\theta)^2} - \frac{8\pi}{\theta^3} + \frac{3}{\theta^2} \right) \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}} \right) \right\} \right\}$$

$$\text{Solve}\left[-\frac{1}{\pi r \theta} 1080 \left( -\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} (4\pi - 2\theta)}{2\pi^3 \sqrt{\theta} \sqrt{4\pi\theta - \theta^2}} + \frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \theta^{3/2}} - \right.$$

$$\left. \frac{135 \left( \frac{1}{(4\pi-\theta)^2} - \frac{8\pi}{\theta^3} + \frac{3}{\theta^2} \right) \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}} \right) == \frac{r (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta) \theta}}, r\right]$$

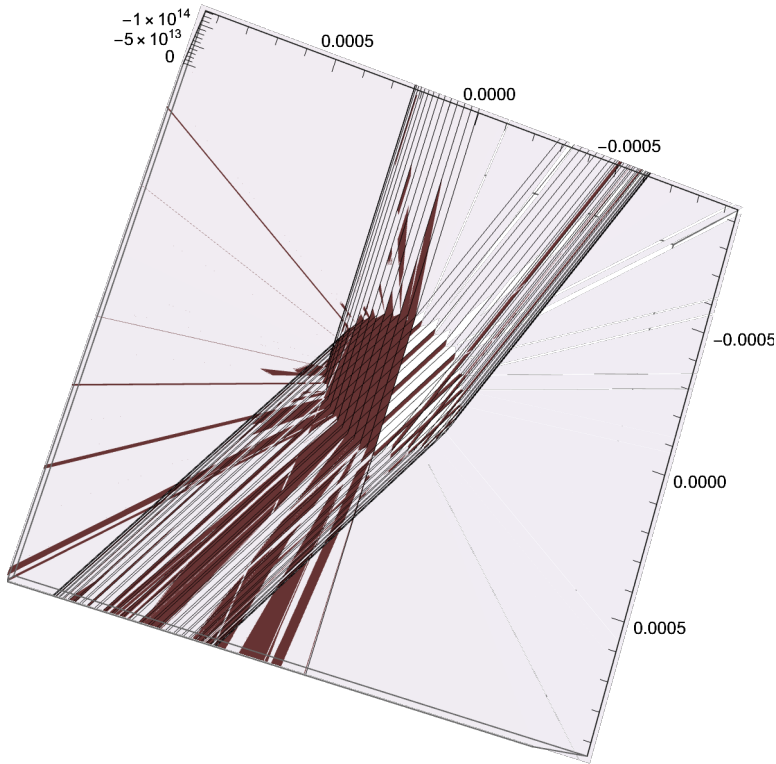
$$\left\{ \left\{ r \rightarrow -\frac{1166400 \sqrt{-1 - \frac{8\pi^2}{\theta^2} + \frac{6\pi}{\theta}}}{\pi^2 \sqrt{-8\pi^3\theta + 12\pi^2\theta^2 - 6\pi\theta^3 + \theta^4}} \right\}, \left\{ r \rightarrow \frac{1166400 \sqrt{-1 - \frac{8\pi^2}{\theta^2} + \frac{6\pi}{\theta}}}{\pi^2 \sqrt{-8\pi^3\theta + 12\pi^2\theta^2 - 6\pi\theta^3 + \theta^4}} \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[ -\frac{1}{\pi r \theta} 1080 \left( -\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} (4\pi - 2\theta)}{2\pi^3 \sqrt{\theta} \sqrt{4\pi\theta - \theta^2}} + \frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \theta^{3/2}} - \frac{135 \left( \frac{1}{(4\pi-\theta)^2} - \frac{8\pi}{\theta^3} + \frac{3}{\theta^2} \right) \sqrt{4\pi\theta - \theta^2}}{2\pi^3 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{\theta}} \right), \{r, -1, 1\}, \{\theta, -13, 13\} \right]$$



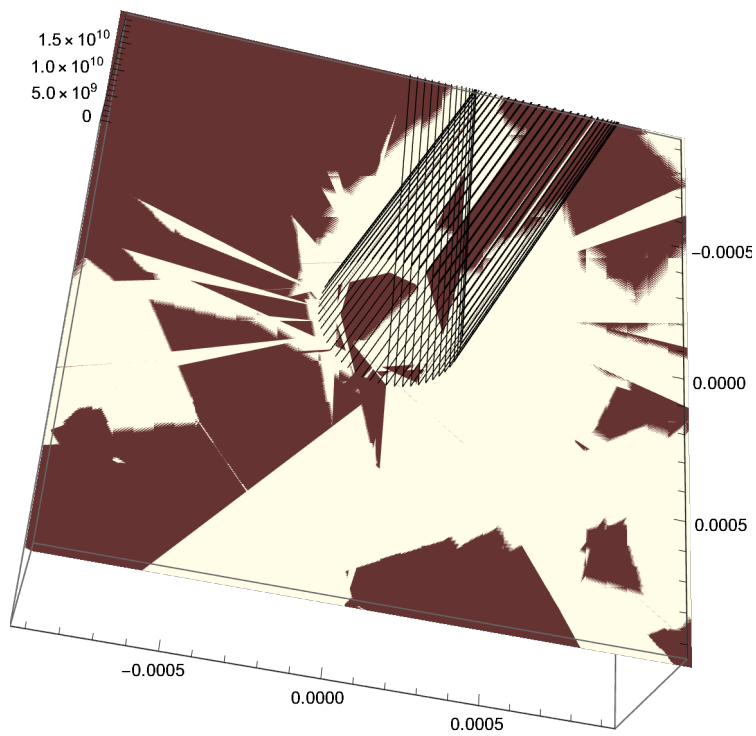
$$D\left[ \frac{1166400 \sqrt{-1 - \frac{8\pi^2}{\theta^2} + \frac{6\pi}{\theta}}}{\pi^2 \sqrt{-8\pi^3\theta + 12\pi^2\theta^2 - 6\pi\theta^3 + \theta^4}}, \theta \right] - \frac{583200 \sqrt{-1 - \frac{8\pi^2}{\theta^2} + \frac{6\pi}{\theta}} (-8\pi^3 + 24\pi^2\theta - 18\pi\theta^2 + 4\theta^3)}{\pi^2 (-8\pi^3\theta + 12\pi^2\theta^2 - 6\pi\theta^3 + \theta^4)^{3/2}} + \frac{583200 \left( \frac{16\pi^2}{\theta^3} - \frac{6\pi}{\theta^2} \right)}{\pi^2 \sqrt{-1 - \frac{8\pi^2}{\theta^2} + \frac{6\pi}{\theta}} \sqrt{-8\pi^3\theta + 12\pi^2\theta^2 - 6\pi\theta^3 + \theta^4}}$$

$$\text{RevolutionPlot3D}\left[-\frac{583\,200\sqrt{-1-\frac{8\pi^2}{\theta^2}+\frac{6\pi}{\theta}}(-8\pi^3+24\pi^2\theta-18\pi\theta^2+4\theta^3)}{\pi^2(-8\pi^3\theta+12\pi^2\theta^2-6\pi\theta^3+\theta^4)^{3/2}}+\frac{583\,200\left(\frac{16\pi^2}{\theta^3}-\frac{6\pi}{\theta^2}\right)}{\pi^2\sqrt{-1-\frac{8\pi^2}{\theta^2}+\frac{6\pi}{\theta}}\sqrt{-8\pi^3\theta+12\pi^2\theta^2-6\pi\theta^3+\theta^4}},\{\theta,-13,13\}\right]$$

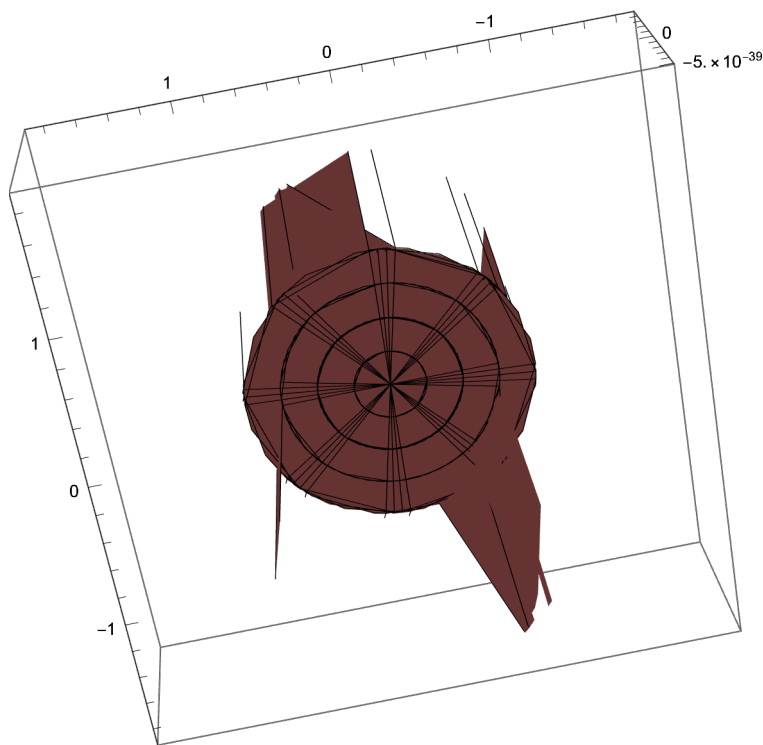


$$\left\{\left\{r \rightarrow -\frac{1\,166\,400\sqrt{-1-\frac{8\pi^2}{\theta^2}+\frac{6\pi}{\theta}}}{\pi^2\sqrt{-8\pi^3\theta+12\pi^2\theta^2-6\pi\theta^3+\theta^4}}\right\},\left\{r \rightarrow \frac{1\,166\,400\sqrt{-1-\frac{8\pi^2}{\theta^2}+\frac{6\pi}{\theta}}}{\pi^2\sqrt{-8\pi^3\theta+12\pi^2\theta^2-6\pi\theta^3+\theta^4}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{1166400 \sqrt{-1 - \frac{8\pi^2}{\theta^2} + \frac{6\pi}{\theta}}}{\pi^2 \sqrt{-8\pi^3\theta + 12\pi^2\theta^2 - 6\pi\theta^3 + \theta^4}}, \{\theta, -13, 13\}\right]$$



RevolutionPlot3D $\left[\frac{r^{1155} (2 \pi - \theta)}{2 \pi \theta \sqrt{r^2 (4 \pi - \theta) \theta}}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$



Options for assigning functions that are expressions of  $r$ .

From the velocity when  $r$  is changing :

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\} \right\}$$

$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \right\} \right\}$$

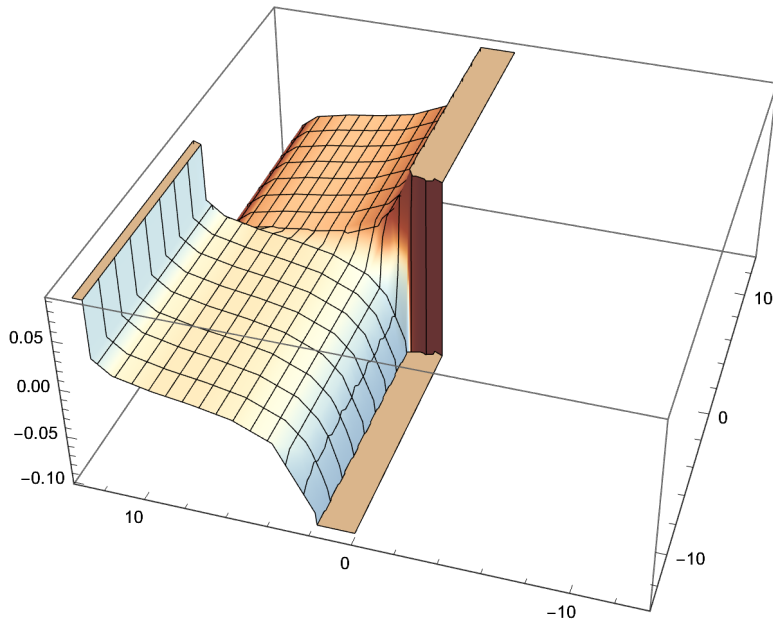
$$\text{Plot}\left[\frac{r (2 \pi - \theta)}{2 \pi \theta \sqrt{r^2 (4 \pi - \theta) \theta}}, \{\theta, -13, 13\}\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\} \right\}$$

$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2}}{8 \pi^2 \sqrt{\theta}} \right\} \right\}$$

$$\begin{aligned}
 n &= \frac{r (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)\theta}} = \\
 &= \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right)^2 (4\pi - \theta)\theta}} = \frac{\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi - 3}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi - 3}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}} = \\
 &= \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi - 3}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}} = \frac{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi - 3}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right) (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}\right)^2 (4\pi - \theta)\theta}}
 \end{aligned}$$

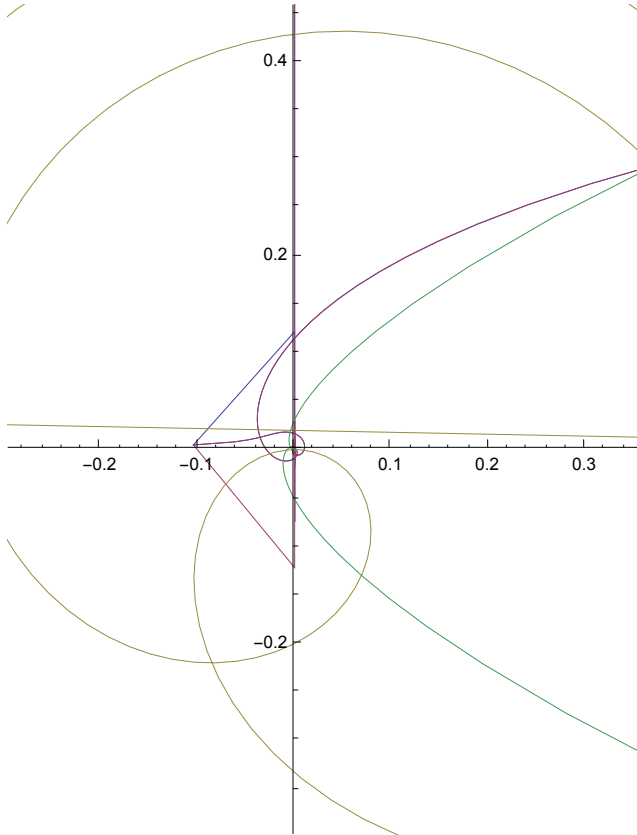
$$\text{Plot3D}\left[\frac{r (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)\theta}}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$$



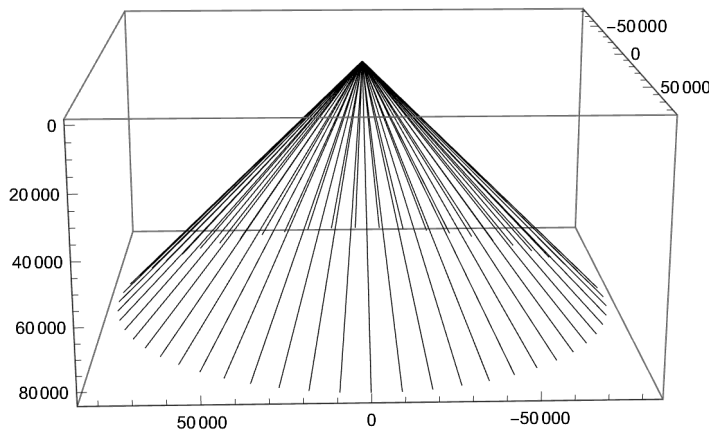
$$\begin{aligned}
 & \text{PolarPlot}\left[\left\{\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}, \right. \right. \\
 & \frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}}, \\
 & \left. \frac{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right) (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}\right\}, \{\theta, -130, 130\}]
 \end{aligned}$$



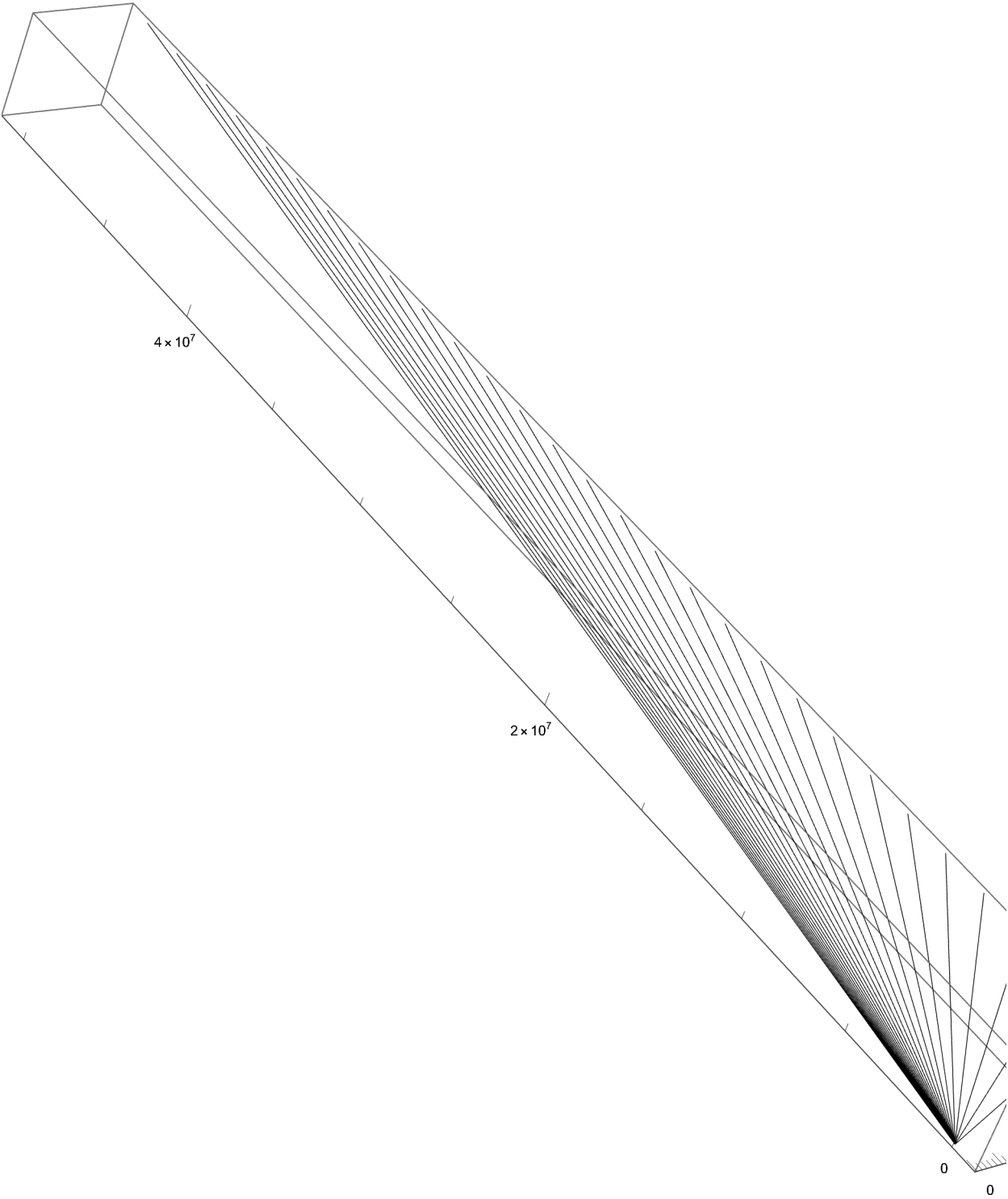
$$\text{PolarPlot}\left[\left\{\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right) (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}\right\}, \{\theta, -130, 130\}]$$



$$\text{RevolutionPlot3D}\left[\left\{\frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}(2\pi-\theta)}{2\pi\theta\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2(4\pi-\theta)\theta}}, \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}(2\pi-\theta)}{2\pi\theta\sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2(4\pi-\theta)\theta}}\right\}, \{\theta, -13, 13\}\right]$$

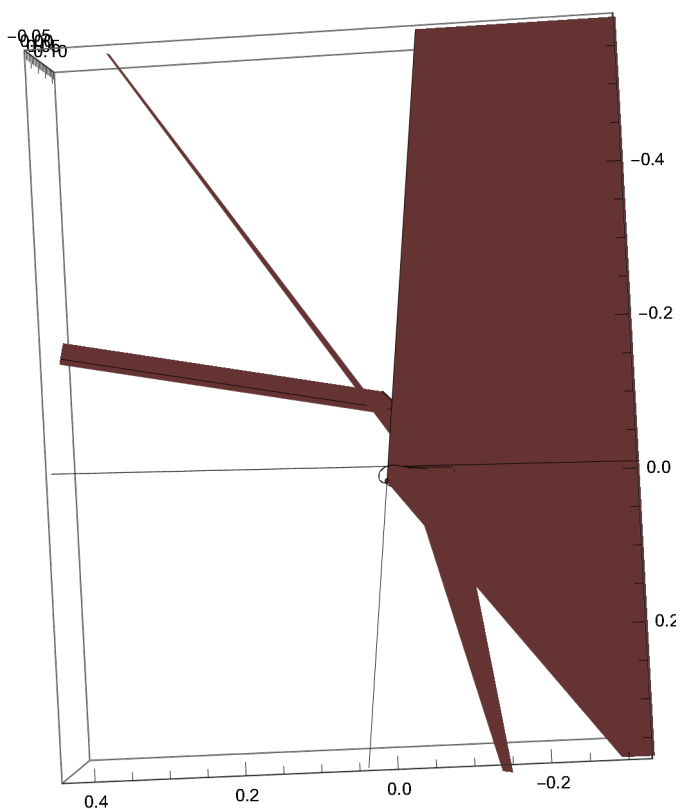


$$\text{RevolutionPlot3D}\left[\left\{\frac{r^2(2\pi-\theta)}{2\pi\theta\sqrt{r^2(4\pi-\theta)\theta}}, \frac{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}(2\pi-\theta)}{2\pi\theta\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi-3}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2(4\pi-\theta)\theta}}, \frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}(2\pi-\theta)}{2\pi\theta\sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2(4\pi-\theta)\theta}}\right\}, \{r, -13, 13\}, \{\theta, -1, 1\}\right]$$



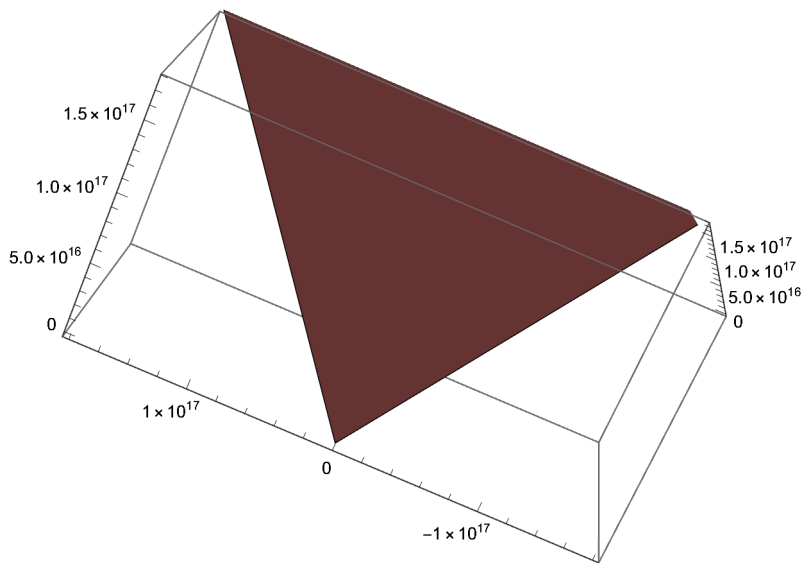
$$\text{RevolutionPlot3D}\left[\left\{\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{r (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}} (2\pi - \theta)}{4\pi \sqrt{\theta}}\right\}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$$

$$2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}$$



$$\text{RevolutionPlot3D}\left[\left\{\frac{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (2\pi - \theta)}{2\pi\theta \sqrt{\left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right)^2 (4\pi - \theta)\theta}}, \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}}, \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{4\pi}{\theta}} (2\pi - \theta)}{4\pi \sqrt{\theta}}\right\}, \{r, -13000, 13000\}, \{\theta, -13000, 13000\}\right]$$

$$2\pi\theta \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{4\pi}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 (4\pi - \theta)\theta}$$



$$\frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}}$$

$$\text{Solve}\left[\frac{4\pi r^2 - 2r^2\theta}{4320 \sqrt{4\pi r^2\theta - r^2\theta^2}} == r n (1 / (1080 / \pi) \theta), n\right]$$

$$\left\{\left\{n \rightarrow \frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}}\right\}\right\}$$

$$D\left[\frac{r(2\pi - \theta)}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}}, \theta\right]$$

$$-\frac{r(2\pi - \theta)}{2\pi\theta^2 \sqrt{r^2(4\pi - \theta)\theta}} - \frac{r}{2\pi\theta \sqrt{r^2(4\pi - \theta)\theta}} - \frac{r(2\pi - \theta)(r^2(4\pi - \theta) - r^2\theta)}{4\pi\theta (r^2(4\pi - \theta)\theta)^{3/2}}$$

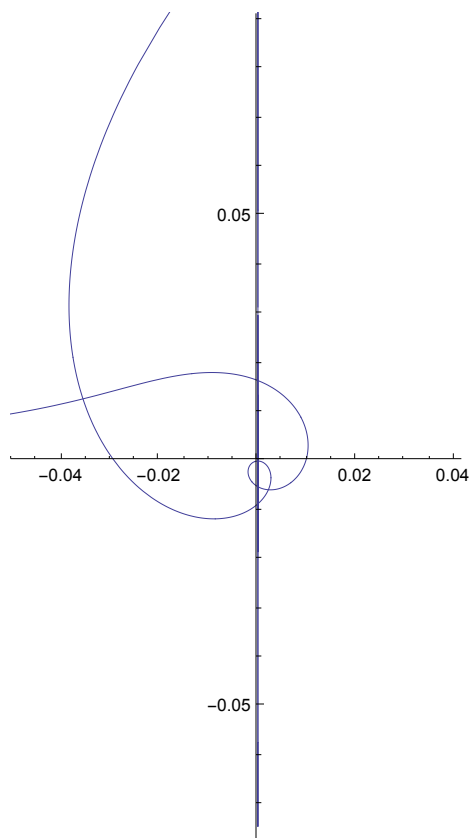
$$\text{Solve}\left[-\frac{r(2\pi-\theta)}{2\pi\theta^2\sqrt{r^2(4\pi-\theta)\theta}}-\frac{r}{2\pi\theta\sqrt{r^2(4\pi-\theta)\theta}}-\frac{r(2\pi-\theta)(r^2(4\pi-\theta)-r^2\theta)}{4\pi\theta(r^2(4\pi-\theta)\theta)^{3/2}}==\right. \\ \left.r(1/(1080/\pi)\theta), r\right]$$

$$\left\{\left\{r\rightarrow-\frac{135\sqrt{\frac{1}{(4\pi-\theta)^3}+\frac{36\pi}{\theta^4}-\frac{9}{\theta^3}+\frac{6}{(4\pi-\theta)\theta^2}}}{\pi^2\theta^{3/2}}\right\},\left\{r\rightarrow\frac{135\sqrt{\frac{1}{(4\pi-\theta)^3}+\frac{36\pi}{\theta^4}-\frac{9}{\theta^3}+\frac{6}{(4\pi-\theta)\theta^2}}}{\pi^2\theta^{3/2}}\right\}\right\}$$

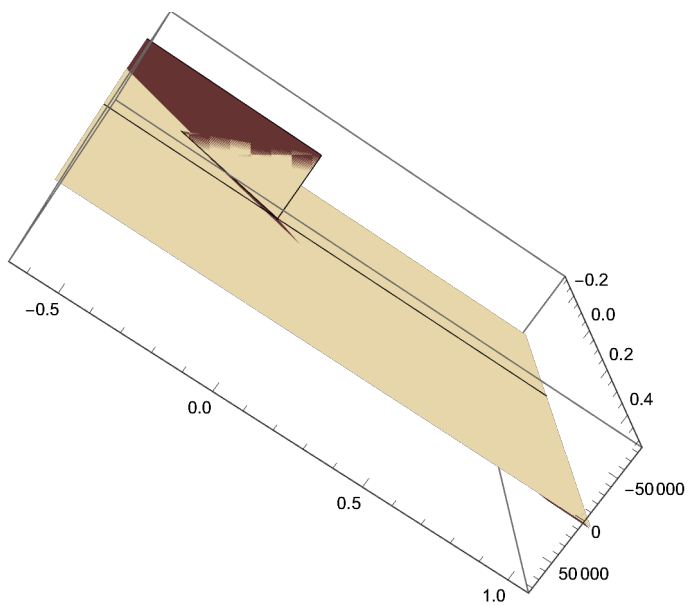
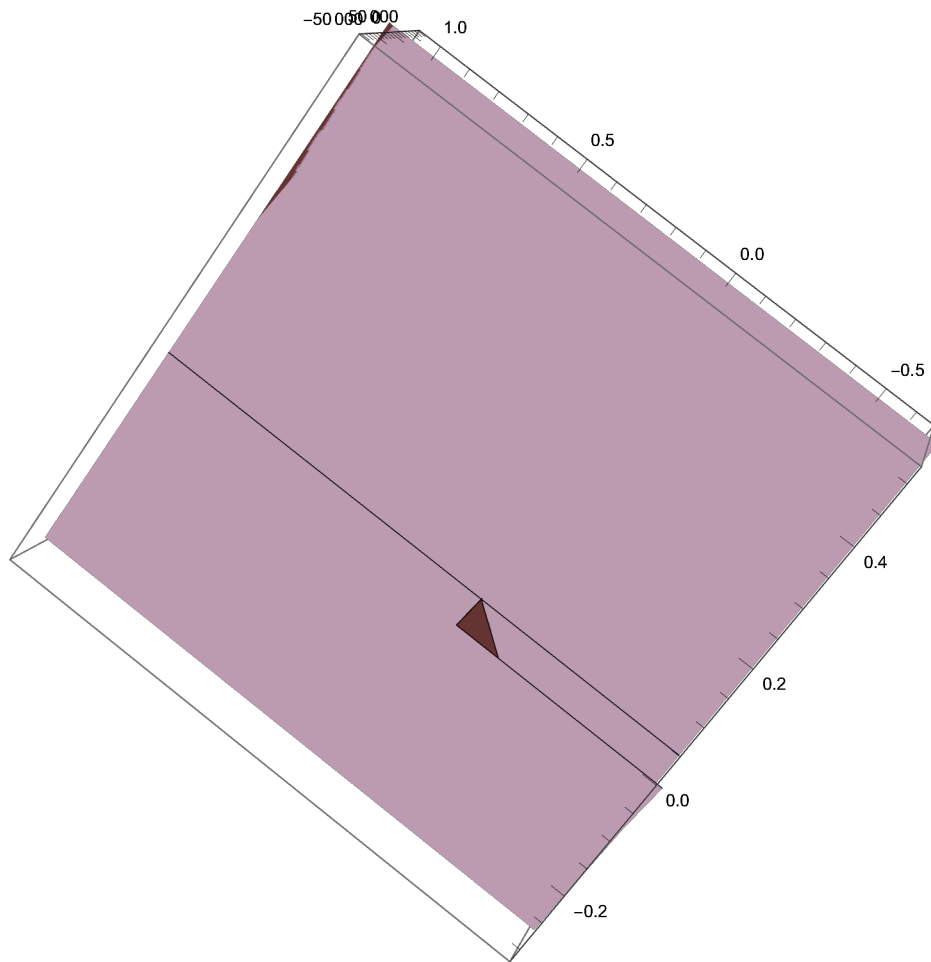
$$\text{Solve}\left[-\frac{r(2\pi-\theta)}{2\pi\theta^2\sqrt{r^2(4\pi-\theta)\theta}}-\frac{r}{2\pi\theta\sqrt{r^2(4\pi-\theta)\theta}}-\frac{r(2\pi-\theta)(r^2(4\pi-\theta)-r^2\theta)}{4\pi\theta(r^2(4\pi-\theta)\theta)^{3/2}}==\right. \\ \left.r(1/(1080/\pi)\theta), \theta\right]$$

$$\left\{\left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,1\right]\right\},\right. \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,2\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,3\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,4\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,5\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,6\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,7\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,8\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,9\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[41990400\pi^4-41990400\pi^3\theta+17496000\pi^2\theta^2-3499200\pi\theta^3+291600\theta^4-64\pi^7r^2\theta^7+48\pi^6r^2\theta^8-12\pi^5r^2\theta^9+\pi^4r^2\theta^{10}\&,10\right]\right\}\}$$

$\text{PolarPlot}\left[\frac{(1)(2\pi - \theta)}{2\pi\theta\sqrt{(1)^2(4\pi - \theta)\theta}}, \{\theta, -13, 13\}\right]$



```
RevolutionPlot3D[ $\frac{r(2\pi - \theta)}{2\pi\theta\sqrt{r^2(4\pi - \theta)\theta}}$ , {r, -13, 13}, {\theta, -13, 13}]
```





## VI. Solving for $r_1$

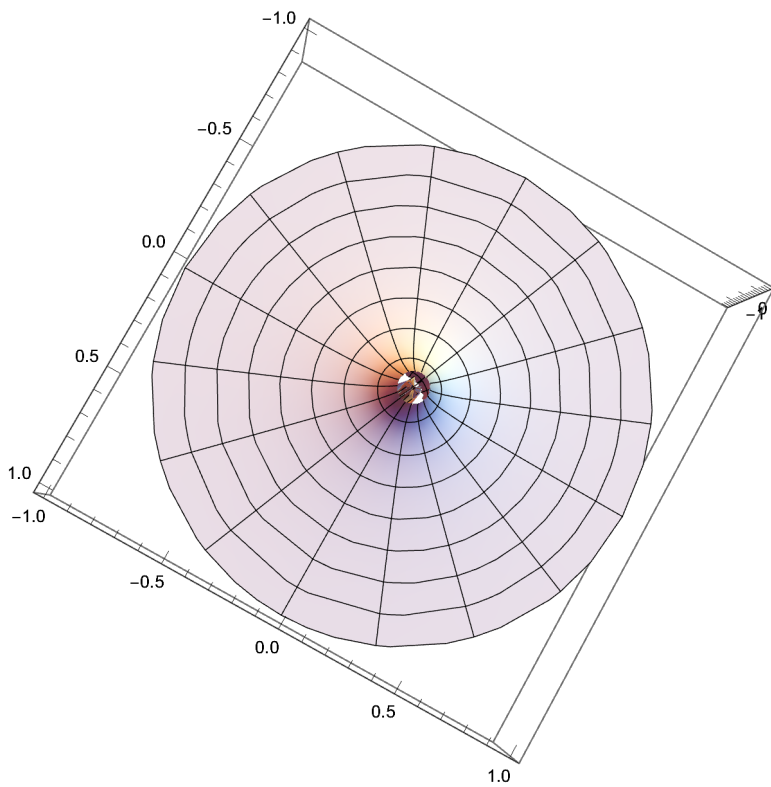
$$r_1 \rightarrow \sqrt{r^2 - \eta^2}$$

$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right\} \right\}$$

$$\text{Solve}\left[\eta == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}, \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow -\frac{2\pi}{-1 + 4\pi^2 \eta} \right\}, \left\{ \theta \rightarrow \frac{2\pi}{1 + 4\pi^2 \eta} \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi}{1 + 4\pi^2 \eta}, \{\eta, -1, 1\}\right]$$



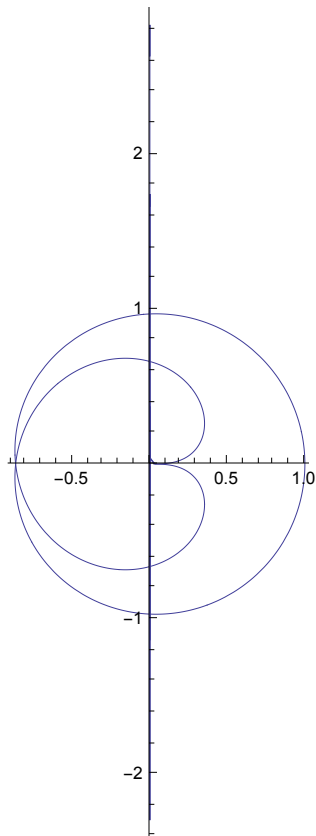
### The Constant $r$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\}$$

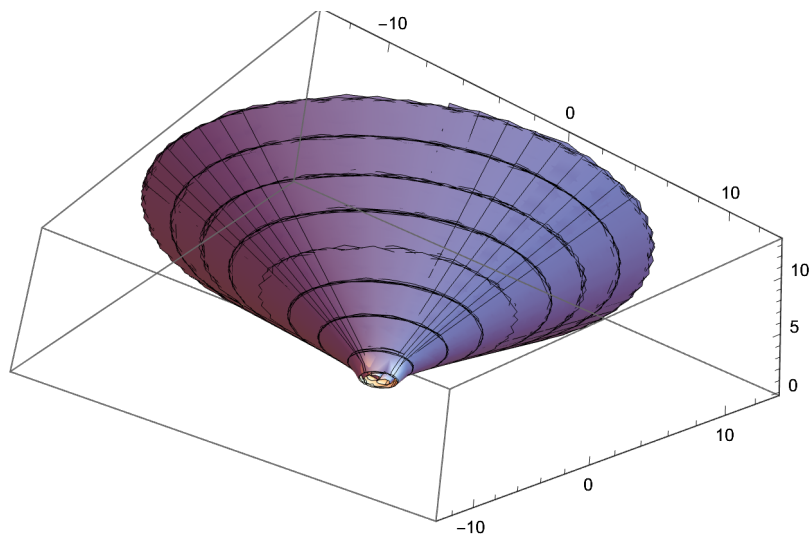
$$\text{Solve}\left[1 == \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \eta\right]$$

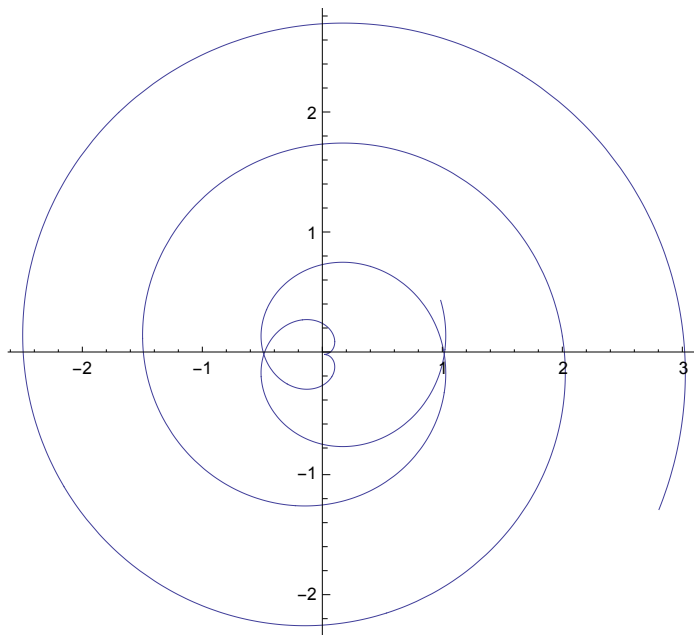
$$\left\{\left\{\eta \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right\}\right\}$$

$$\text{PolarPlot}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}, \{\theta, -13, 13\}\right]$$



$$\sqrt{r^2 - \eta^2} = \sqrt{(1)^2 - \left(\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right)^2}$$

$$\text{RevolutionPlot3D}\left[\sqrt{(r)^2 - \left(\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right)^2}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$$


$$\text{PolarPlot}\left[\sqrt{(1)^2 - \left(\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right)^2}, \{\theta, -13, 13\}\right]$$


The changing  $r$

$$r_1 = \sqrt{r^2 - \eta^2}$$

$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right\} \right\}$$

$$r_1 = \sqrt{r^2 - \eta^2} = \sqrt{r^2 - \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} =$$

$$\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} - \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} =$$

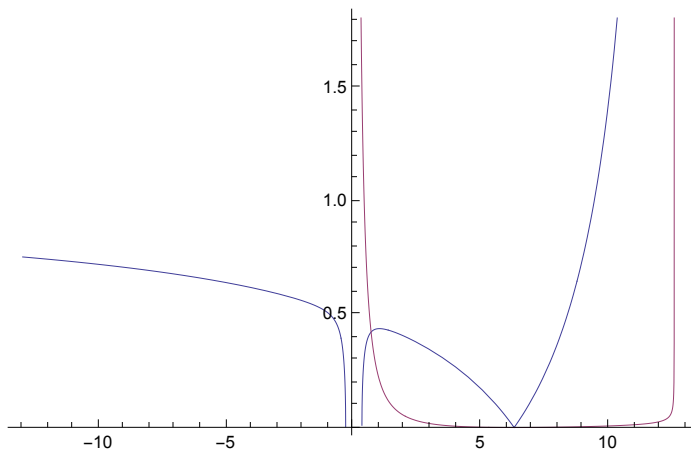
$$\sqrt{\left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right)^2 - \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} \right\} \right\}$$

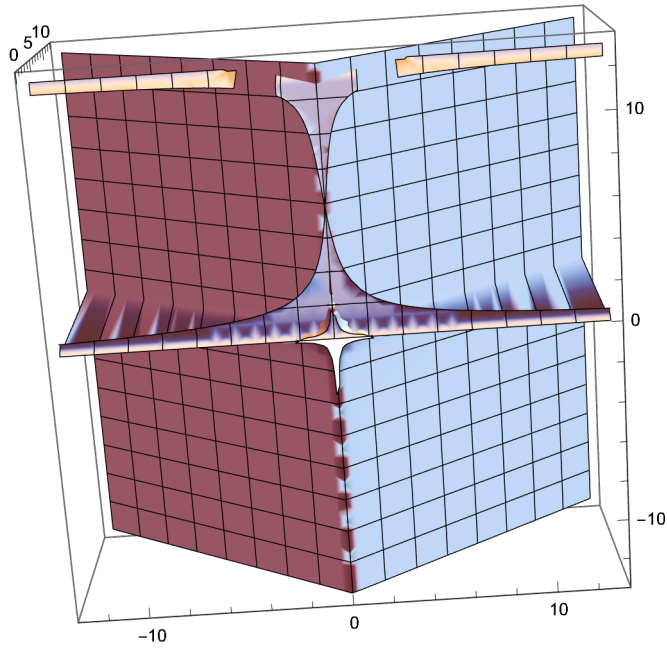
$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right\} \right\}$$

$$\text{Plot} \left[ \left\{ \sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} - \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2}, \right. \right.$$

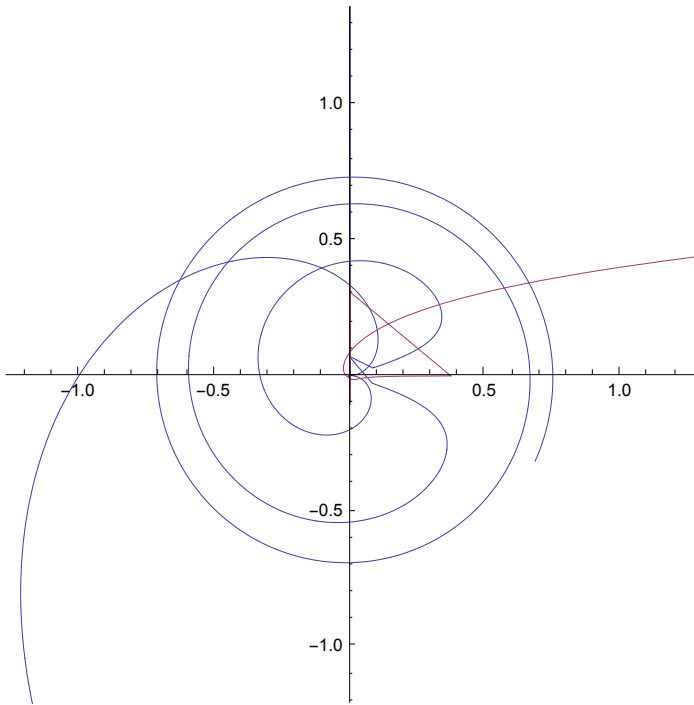
$$\left. \sqrt{\left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}} \right)^2 - \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} \right\}, \{\theta, -13, 13\}]$$



$\text{Plot3D}\left[\left\{\sqrt{r^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}\right)^2}, \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}\right)^2 - \left(\frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\},\right.$   
 $\left.\{\theta, -13, 13\}, \{r, -13, 13\}\right]$

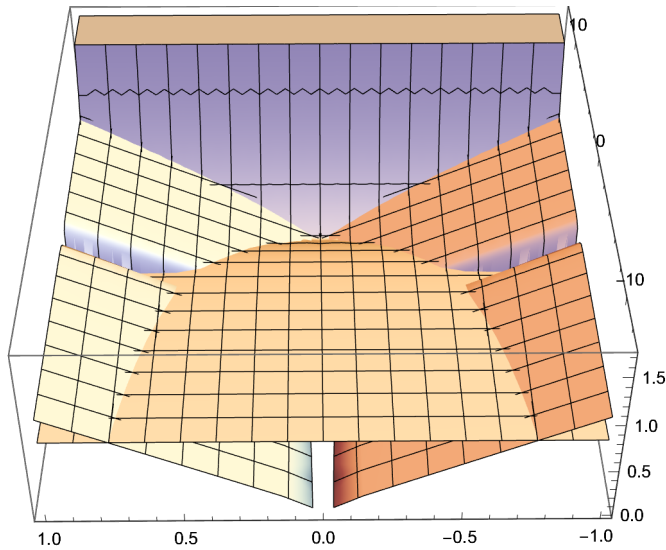


$$\text{PolarPlot}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \right. \right. \\ \left. \left. \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -13, 13\}\right]$$

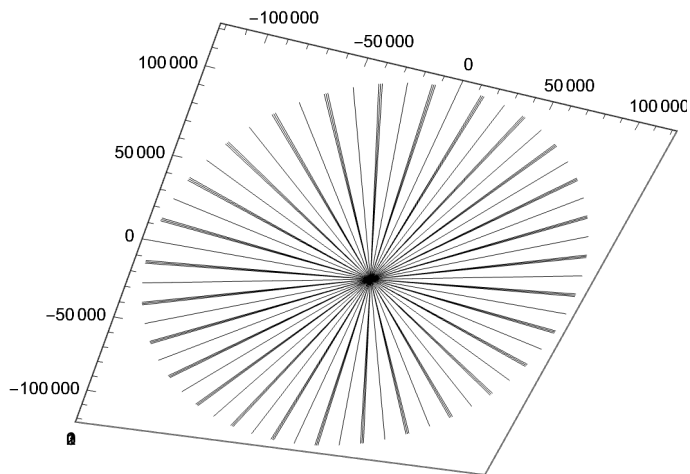


This is a platform equation. ©Parker Emmerson 2009

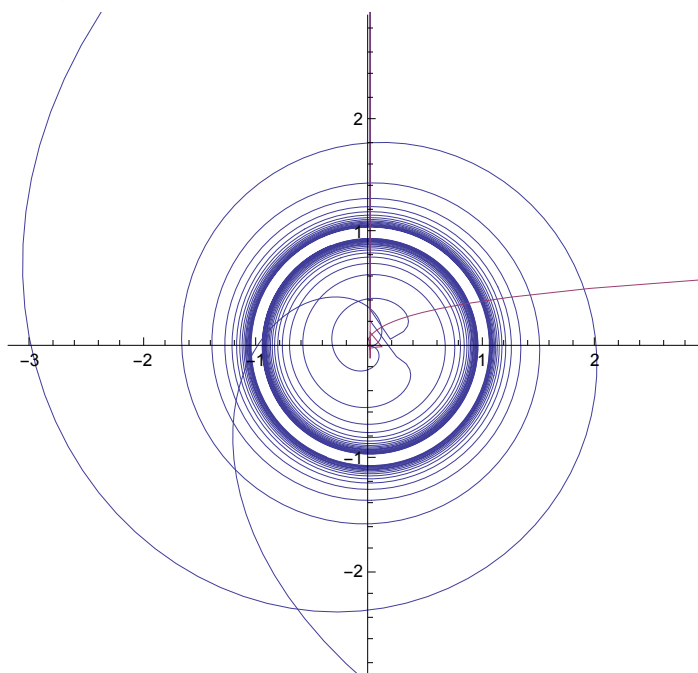
$$\text{Plot3D}\left[\left\{\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{r\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right.\right. \\ \left.\left.\sqrt{(r)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}\right\},\{\theta,-13,13\},\{r,-1,1\}\right]$$



$$\text{RevolutionPlot3D}\left[\left\{\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right.\right. \\ \left.\left.\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}\right\},\{\theta,-13,13\}\right]$$

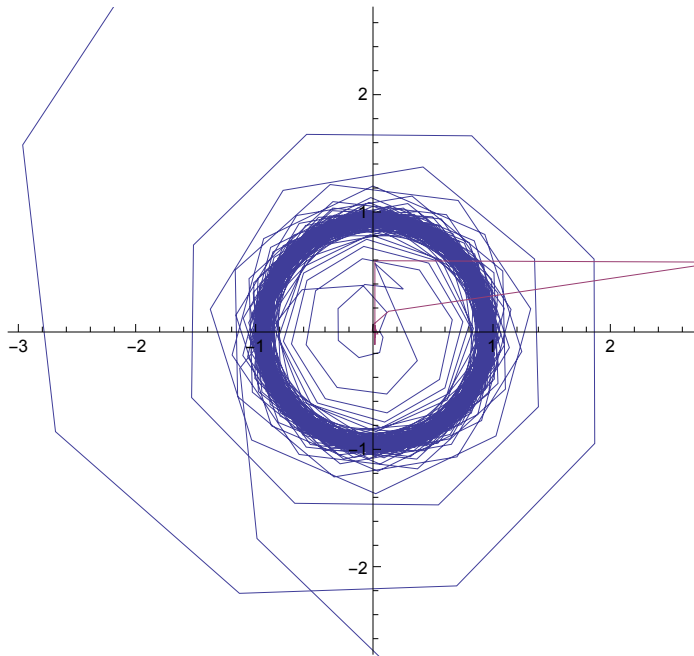


$$\text{PolarPlot}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \right. \right. \\ \left. \left. \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}\right\}, \{\theta, -130, 130\}\right]$$





$$\text{PolarPlot}\left[\left\{\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\right. \right. \\ \left. \left.\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}\right\},\{\theta,-1300,1300\} \right]$$



$$\text{Solve}\left[\sqrt{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}=\right. \\ \left.\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2-\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},\theta\right]$$

$$\{\{\theta \rightarrow 2\pi\},$$

$$\left\{\theta \rightarrow -\left(\frac{2}{1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}}\right)^{1/3} + \frac{\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{12\pi^2}\right\},$$

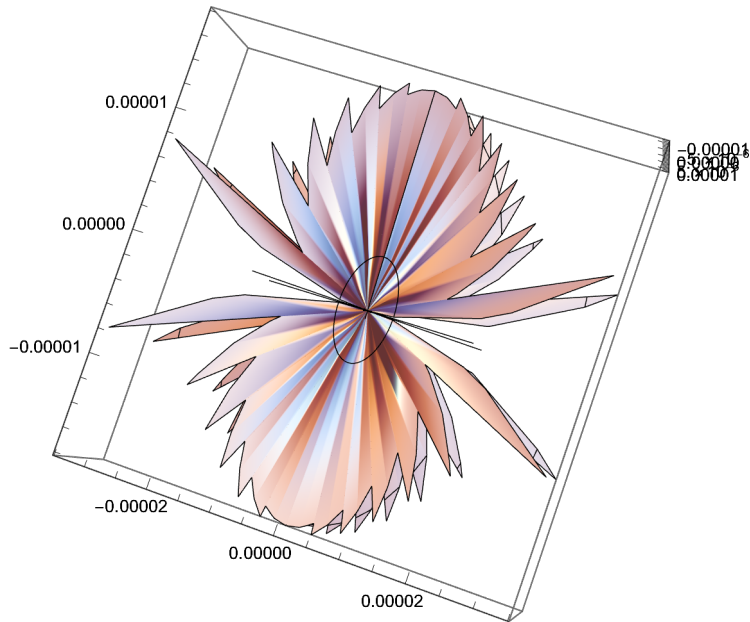
$$\left\{\theta \rightarrow -\frac{(1+i\sqrt{3})\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{24\pi^2} +$$

$$\frac{1-i\sqrt{3}}{2^{2/3}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)^{1/3}}\right\},$$

$$\left\{\theta \rightarrow -\frac{(1-i\sqrt{3})\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{24\pi^2} +$$

$$\frac{1+i\sqrt{3}}{2^{2/3}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)^{1/3}}\right\}\}$$

$\text{RevolutionPlot3D}\left[r \left( -\frac{\left(1 + i\sqrt{3}\right) \left(\frac{1}{2} \left(1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}}\right)\right)^{1/3}}{24 \pi^2} \right), \{r, -1, 1\}\right]$



If these are theta solutions, what is  $r * \theta$ , the change in circumference?

Plot[{{r 2 π},

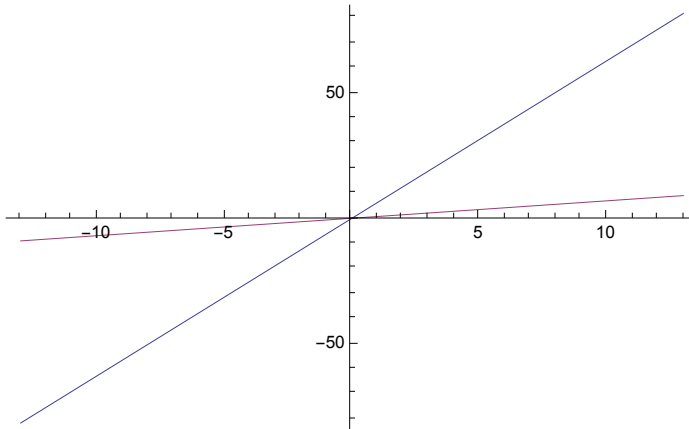
$$\left\{r \left( \left( \frac{2}{1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}}} \right)^{1/3} + \frac{\left( \frac{1}{2} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right) \right)^{1/3}}{12 \pi^2} \right) \right\},$$

$$\left\{r \left( - \frac{\left( 1 + i \sqrt{3} \right) \left( \frac{1}{2} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right) \right)^{1/3}}{24 \pi^2} + \right.$$

$$\left. \frac{1 - i \sqrt{3}}{2^{2/3} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right)^{1/3}} \right\},$$

$$\left\{r \left( - \frac{\left( 1 - i \sqrt{3} \right) \left( \frac{1}{2} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right) \right)^{1/3}}{24 \pi^2} + \right.$$

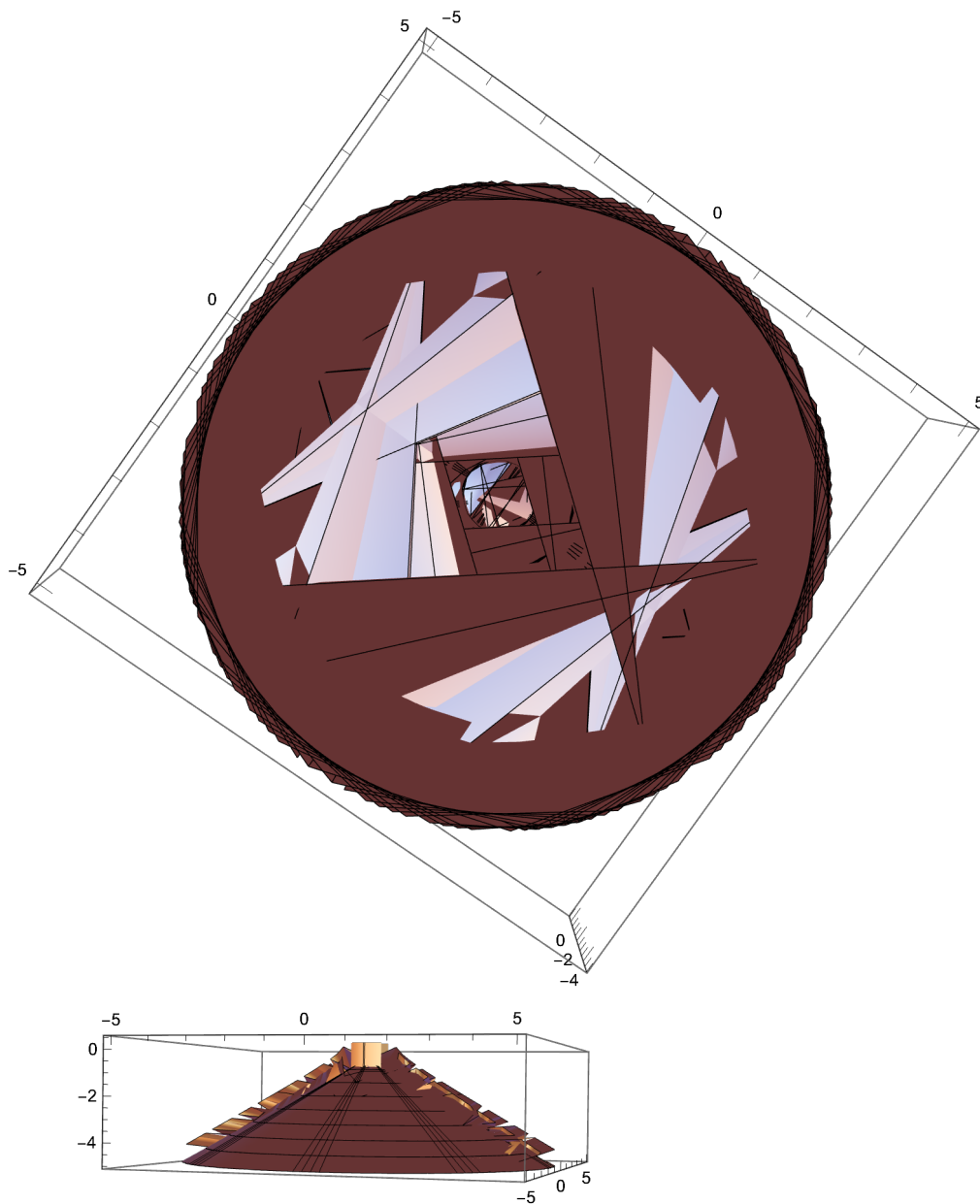
$$\left. \frac{1 + i \sqrt{3}}{2^{2/3} \left( 1728 \pi^5 + \sqrt{6912 \pi^6 + 2985984 \pi^{10}} \right)^{1/3}} \right\} \right\}, \{r, -13, 13\}]$$



$$\text{Solve} \left[ \sqrt{(r)^2 - \left( \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2} = \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}, r \right]$$

$$\left\{ \left\{ r \rightarrow - \frac{\sqrt{1 + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}}}{\pi \sqrt{16\pi^2 - 16\pi\theta + 4\theta^2}} \right\}, \left\{ r \rightarrow \frac{\sqrt{1 + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}}}{\pi \sqrt{16\pi^2 - 16\pi\theta + 4\theta^2}} \right\} \right\}$$

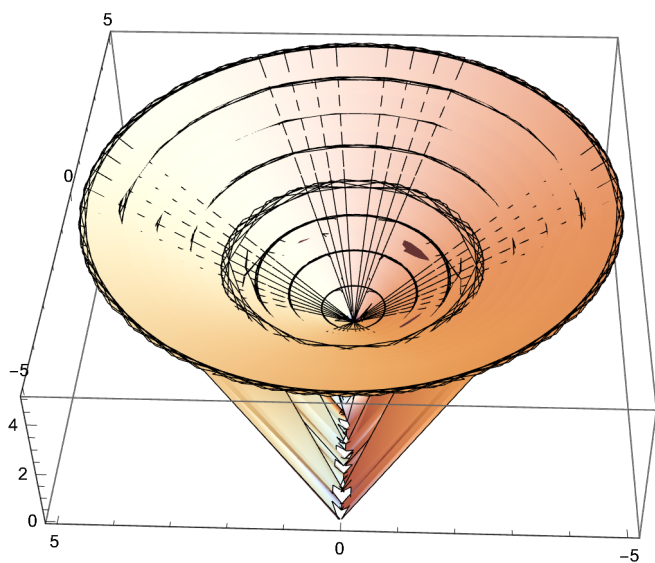
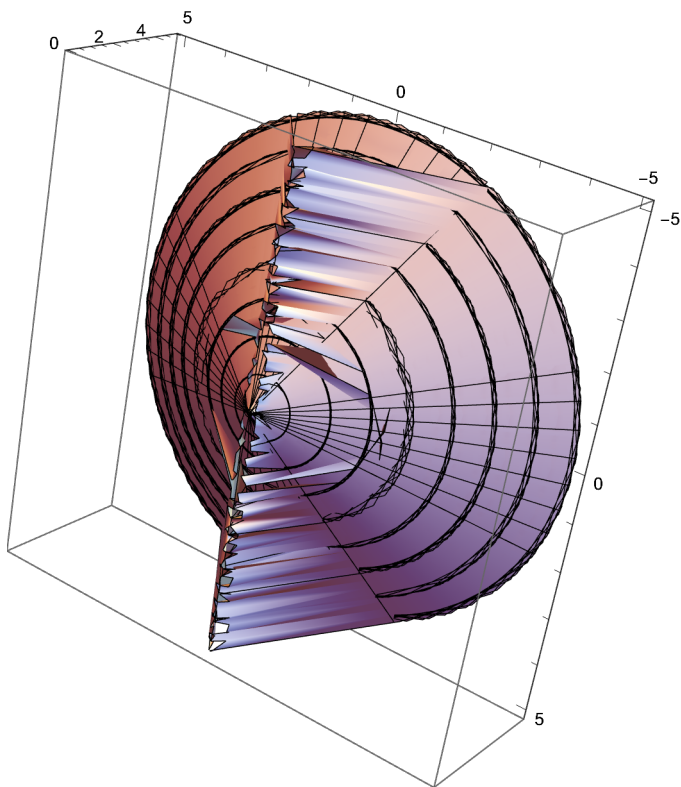
$\text{RevolutionPlot3D}\left[\frac{\sqrt{1 + \frac{4\pi^2}{\theta^2} - \frac{4\pi}{\theta}}}{\pi \sqrt{16\pi^2 - 16\pi\theta + 4\theta^2}} - \sqrt{(r)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}\right)^2}}{8\pi^2 \sqrt{\theta}},\right.$   
 $\left.\{r, -5, 5\}, \{\theta, -13000, 13000\}\right]$



$\text{Solve}\left[r_1 == \sqrt{\left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi \sqrt{\theta}}\right)^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \theta\right]$

$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$\text{RevolutionPlot3D}\left[\sqrt{(r)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \{r, -5, 5\}, \{\theta, -13, 13\}\right]$$



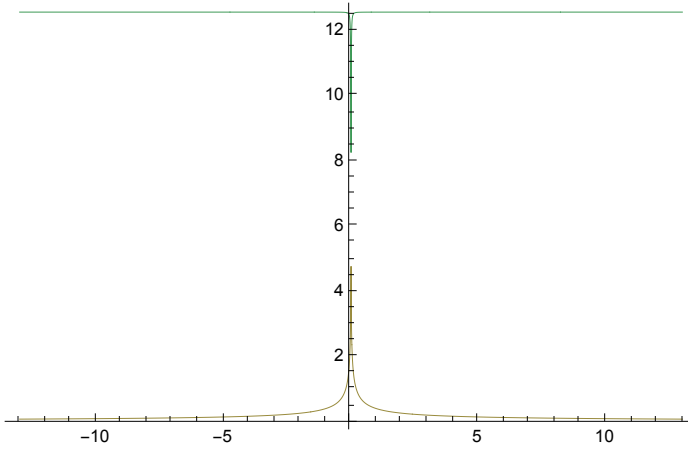
$$\text{Plot}\left[\left\{\left\{\frac{2\pi(1+8\pi^4 r_1^2)}{1+16\pi^4 r_1^2} - \frac{1}{2} \sqrt{\left(\frac{16\pi^2(1+8\pi^4 r_1^2)^2}{(1+16\pi^4 r_1^2)^2} - \right.}\right.\right.\right.$$

$$\begin{aligned}
& \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \Bigg) - \frac{1}{2} \sqrt[4]{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \\
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} - \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \right. \\
& \left. \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) \Bigg/ \left( 4 \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \right. \\
& \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \Bigg] \Bigg\}, \\
& \left\{ \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) + \frac{1}{2} \sqrt[4]{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \\
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \\
& \left( 4 \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right. \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right) \Bigg\}, \\
& \left\{ \frac{2 \pi (1 + 8 \pi^4 r_1^2)}{1 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right. \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} + \\
& \quad \left. \left. \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} \right) \right\} - \frac{1}{2} \sqrt[4]{\left( \frac{32 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \right.} \\
& \quad \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} - \\
& \quad \frac{32 \pi^4 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}}{3^{2/3} (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}} + \\
& \quad \left( \frac{512 \pi^3 (1 + 8 \pi^4 r_1^2)^3}{(1 + 16 \pi^4 r_1^2)^3} - \frac{768 \pi^3 (1 + 8 \pi^4 r_1^2)}{(1 + 16 \pi^4 r_1^2)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \\
& \quad \left( 4 \sqrt[4]{\left( \frac{16 \pi^2 (1 + 8 \pi^4 r_1^2)^2}{(1 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right. \right. \\
& \quad \frac{32 \pi^4 r_1^2 (1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6)^{1/3}}{3^{1/3} (1 + 16 \pi^4 r_1^2)^2 (9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8})^{1/3}} +
\end{aligned}$$



$$\begin{aligned}
& \left. \left. \left. \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} \right) \right) \right\}, \\
& \left\{ \frac{2 \pi \left( 1 + 8 \pi^4 r_1^2 \right)}{1 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt[4]{\left( \frac{16 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} + \\
& \left. \left. \left. \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} \right) + \frac{1}{2} \sqrt[4]{\left( \frac{32 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \right.} \right. \\
& \frac{32 \pi^2}{1 + 16 \pi^4 r_1^2} + \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} - \\
& \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} + \\
& \left( \frac{512 \pi^3 \left( 1 + 8 \pi^4 r_1^2 \right)^3}{\left( 1 + 16 \pi^4 r_1^2 \right)^3} - \frac{768 \pi^3 \left( 1 + 8 \pi^4 r_1^2 \right)}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} + \frac{256 \pi^3}{1 + 16 \pi^4 r_1^2} \right) / \\
& \left( 4 \sqrt[4]{\left( \frac{16 \pi^2 \left( 1 + 8 \pi^4 r_1^2 \right)^2}{\left( 1 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2}{1 + 16 \pi^4 r_1^2} - \right.} \right. \\
& \frac{32 \pi^4 r_1^2 \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}}{3^{1/3} \left( 1 + 16 \pi^4 r_1^2 \right)^2 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}} + \\
& \left. \left. \left. \frac{32 \pi^4 \left( 9 \pi^2 r_1^4 + \sqrt{3} \sqrt{r_1^6 + 27 \pi^4 r_1^8} \right)^{1/3}}{3^{2/3} \left( 1 + 48 \pi^4 r_1^2 + 768 \pi^8 r_1^4 + 4096 \pi^{12} r_1^6 \right)^{1/3}} \right) \right) \right\} \right\}, \{r_1, -13, 13\} ]
\end{aligned}$$



$$\text{Solve}\left[\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2} = r_1, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{\pi (3 - 16\pi^4 + 32\pi^4 r_1^2)}{1 - 16\pi^4 + 16\pi^4 r_1^2} - \frac{1}{2} \sqrt{\left(\frac{4\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4 r_1^2)^2} - \frac{8\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2)}{3 (1 - 16\pi^4 + 16\pi^4 r_1^2)} + (2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8 r_1^2 - 32768\pi^{12} r_1^2 + 65536\pi^{12} r_1^4)) \right) / (3 (1 - 16\pi^4 + 16\pi^4 r_1^2))\right. \right. \\ \left. \left(128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10} r_1^2 + 6291456\pi^{14} r_1^2 + 6291456\pi^{18} r_1^2 + 1572864\pi^{14} r_1^4 - 25165824\pi^{18} r_1^4 + 33554432\pi^{18} r_1^6 + \sqrt{(1811939328\pi^{20} r_1^2 - 86973087744\pi^{24} r_1^2 + 1391569403904\pi^{28} r_1^2 - 7421703487488\pi^{32} r_1^2 + 347892350976\pi^{24} r_1^4 + 38963943309312\pi^{28} r_1^4 + 89060441849856\pi^{32} r_1^4 + 22265110462464\pi^{28} r_1^6 - 356241767399424\pi^{32} r_1^6 + 474989023199232\pi^{32} r_1^8)}\right)^{1/3} + \left(128\pi^6 - 6144\pi^{10} + 98304\pi^{14} - 524288\pi^{18} + 24576\pi^{10} r_1^2 + 6291456\pi^{14} r_1^2 + 6291456\pi^{18} r_1^2 + 1572864\pi^{14} r_1^4 - 25165824\pi^{18} r_1^4 + 33554432\pi^{18} r_1^6 + \sqrt{(1811939328\pi^{20} r_1^2 - 86973087744\pi^{24} r_1^2 + 1391569403904\pi^{28} r_1^2 - 7421703487488\pi^{32} r_1^2 + 347892350976\pi^{24} r_1^4 + 38963943309312\pi^{28} r_1^4 + 89060441849856\pi^{32} r_1^4 + 22265110462464\pi^{28} r_1^6 - 356241767399424\pi^{32} r_1^6 + 474989023199232\pi^{32} r_1^8)}\right)^{1/3} / (3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4 r_1^2))\right) - \frac{1}{2} \sqrt{\left(\frac{8\pi^2 (3 - 16\pi^4 + 32\pi^4 r_1^2)^2}{(1 - 16\pi^4 + 16\pi^4 r_1^2)^2} - \frac{16\pi^2 (13 - 16\pi^4 + 64\pi^4 r_1^2)}{3 (1 - 16\pi^4 + 16\pi^4 r_1^2)} - (2^{1/3} (16\pi^4 - 512\pi^8 + 4096\pi^{12} + 2048\pi^8 r_1^2 - 32768\pi^{12} r_1^2 + 65536\pi^{12} r_1^4)) \right) / (3 \times 2^{1/3} (1 - 16\pi^4 + 16\pi^4 r_1^2))\right) -$$

[illegible]

$$\begin{aligned}
\left\{ \theta \rightarrow \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \right.} \right. \\
\frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \\
\left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4) \right) \right\} / \\
\left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right. \\
\left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 - \\
\left. \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right.} \\
7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
\left. \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8) \right)^{1/3} \right) + \\
\left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
\sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \\
7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - 356 241 767 399 424 \\
\left. \left. \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8) \right)^{1/3} \right) / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Bigg\} + \\
\frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right.} \\
\left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4) \right) \right\} / \\
\left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right. \\
\left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 - \\
\left. \sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right.} \\
7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
\left. \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8) \right)^{1/3} \right) - \\
\left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
\sqrt{(1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \\
7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
\left. \left. 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \right. \\
& \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right)^{1/3} \Bigg/ \\
& \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \right) - \left( \frac{768\,\pi^3}{1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2} + \frac{64\,\pi^3 \left( 3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2 \right)^3}{\left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right)^3} - \right. \\
& \left. \frac{64\,\pi^3 \left( 3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2 \right) \left( 13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2 \right)}{\left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right)^2} \right) \Bigg/ \\
& \left( 4 \sqrt[4]{\left( \frac{4\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right)^2} - \frac{8\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right)} + \right. \right. \\
& \left. \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4 \right) \right) \right) \Bigg/ \\
& \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + \right. \right. \\
& 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - \\
& 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}\,r_1^2 - \right.} \\
& 86\,973\,087\,744\,\pi^{24}\,r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488 \\
& \pi^{32}\,r_1^2 + 347\,892\,350\,976\,\pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + \\
& 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - \\
& \left. \left. 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \\
& 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + \\
& 33\,554\,432\,\pi^{18}\,r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}\,r_1^2 - 86\,973\,087\,744\,\pi^{24}\,r_1^2 + \right.} \\
& 1\,391\,569\,403\,904\,\pi^{28}\,r_1^2 - 7\,421\,703\,487\,488\,\pi^{32}\,r_1^2 + 347\,892\,350\,976 \\
& \pi^{24}\,r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}\,r_1^4 + 89\,060\,441\,849\,856\,\pi^{32}\,r_1^4 + \\
& 22\,265\,110\,462\,464\,\pi^{28}\,r_1^6 - 356\,241\,767\,399\,424\,\pi^{32}\,r_1^6 + \\
& \left. \left. 474\,989\,023\,199\,232\,\pi^{32}\,r_1^8 \right) \right)^{1/3} \Bigg/ \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \right) \Bigg) \Bigg) \Bigg\} , \\
& \left\{ \Theta \rightarrow \frac{\pi \left( 3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2 \right)}{1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2} + \frac{1}{2} \sqrt[4]{\left( \frac{4\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4\,r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right)^2} - \right.} \right. \\
& \frac{8\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4\,r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right)} + \\
& \left. \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8\,r_1^2 - 32\,768\,\pi^{12}\,r_1^2 + 65\,536\,\pi^{12}\,r_1^4 \right) \right) \right) \Bigg/ \\
& \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4\,r_1^2 \right) \right. \\
& \left. \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}\,r_1^2 + 6\,291\,456\,\pi^{14}\,r_1^2 + \right. \right. \\
& \left. \left. 6\,291\,456\,\pi^{18}\,r_1^2 + 1\,572\,864\,\pi^{14}\,r_1^4 - 25\,165\,824\,\pi^{18}\,r_1^4 + 33\,554\,432\,\pi^{18}\,r_1^6 \right) \right) \Bigg\} ,
\end{aligned}$$

$$\begin{aligned}
& r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)^{1/3}} + \\
& \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \\
& \quad \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)^{1/3}} \left(3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)\right) \Bigg) - \\
& \frac{1}{2} \sqrt{\left(\frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right. \\
& \quad \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4)) \Bigg/ \right. \\
& \quad \left. (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) \right. \\
& \quad \left. (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \quad \left. r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \\
& \quad \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)^{1/3}} \right) - \\
& \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)^{1/3}} \Bigg/ \right. \\
& \quad \left. (3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2)) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \right. \\
& \quad \left. \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) \Bigg/ \right. \\
& \quad \left. \left( 4 \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \left( \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} \right/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) + \\
& \frac{1}{2} \sqrt[4]{ \left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right. \\
& \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4 \right) \right) \right/ \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right. \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \right. \right. \\
& \left. \left. 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 - \right. \right. \\
& \left. \left. \sqrt[4]{ \left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - \right. \right. \right. \\
& \left. \left. \left. 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \right. \right. \right. \\
& \left. \left. \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \right. \right. \right. \\
& \left. \left. \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right) \right)^{1/3} \right) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + \right. \\
& \left. 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \right. \\
& \left. \sqrt[4]{ \left( 1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - \right. \right. \right. \\
& \left. \left. \left. 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \right. \right. \right. \\
& \left. \left. \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \right. \right. \right. \\
& \left. \left. \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right) \right)^{1/3} \right/ \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Bigg) \Bigg/ \\
& \left( 4 \sqrt[4]{ \left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \right. \right. \\
& \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4 \right) \right) \right/ \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + \right. \right. \\
& \left. \left. 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - \right. \right. \\
& \left. \left. 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt[4]{ \left( 1\,811\,939\,328 \pi^{20} r_1^2 - \right. \right. \right. \\
& \left. \left. \left. 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \right. \right. \right. \\
& \left. \left. \left. \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + \right. \right. \right. \\
& \left. \left. \left. 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - \right. \right. \right. \\
& \left. \left. \left. 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right) \right)^{1/3} \right) +
\end{aligned}$$



$$\begin{aligned}
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \\
& \quad 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right.} \\
& \quad \left. 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \right. \\
& \quad \left. \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \right. \\
& \quad \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \\
& \quad \left. 474989023199232 \pi^{32} r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Big) \Big) \Big) \Big) \Big\} \\
\text{Plot} & \left[ \left\{ \left\{ \frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \right. \right. \right. \\
& \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} + \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + \right. \right. \right. \\
& \quad \left. \left. 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \Big/ \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right)} \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Big) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \right. \\
& \quad \left. \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Big) \Big) - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + \right. \right. \\
& \quad \left. \left. 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \right. \\
& \quad \left. \left. r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 + \right. \right. \right. \\
& \quad \left. \left. 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \right. \right. \\
& \quad \left. \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Big) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right.
\end{aligned}$$



$$\begin{aligned}
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424} \\
& \quad \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Big) + \\
& \frac{1}{2} \sqrt[3]{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right.} \\
& \quad \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) \Big/} \\
& \quad \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + \right. \\
& \quad \quad r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424} \\
& \quad \quad \left. \pi^{32} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} \Big) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\
& \quad \quad 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424} \\
& \quad \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} \Big/} \\
& \quad \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) \Big/} \\
& \quad \left( 4 \sqrt[3]{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right.} \\
& \quad \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) \Big/} \\
& \quad \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \\
& \quad \quad 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\
& \quad \quad \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \\
& \quad \quad 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424} \\
& \quad \quad \left. \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} \Big) +
\end{aligned}$$

$$\begin{aligned}
& \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \right. \\
& 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \right.} \\
& \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \\
& \left. \left. 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Bigg) \Bigg\}, \\
& \left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right.} \right. \\
& \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \right. \\
& \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \right. \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \right. \\
& \left. \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right.} \right. \right. \\
& \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} + \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \right. \\
& \left. \left. \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right.} \right. \right. \\
& \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Bigg) \Bigg\} - \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right.} \\
& \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \right. \\
& \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \right. \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \right. \\
& \left. \left. r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right.} \right. \right. \\
& \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} - \\
& \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\
& \quad 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\
& \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)^{1/3}} / \\
& \left(3 \times 2^{1/3} \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)\right) + \left(\frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)^3}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^3} - \right. \\
& \quad \left. \frac{64 \pi^3 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right) \left(13 - 16 \pi^4 + 64 \pi^4 r_1^2\right)}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^2}\right) / \\
& \left(4 \sqrt{\left(\frac{4 \pi^2 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)^2}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^2} - \frac{8 \pi^2 \left(13 - 16 \pi^4 + 64 \pi^4 r_1^2\right)}{3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)} + \right. \right. \\
& \quad \left. \left(2^{1/3} \left(16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4\right)\right) / \right. \\
& \quad \left. \left(3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right) \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \right. \\
& \quad \left. \left. 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \right. \right. \\
& \quad \left. \left. 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - \right. \right. \right. \\
& \quad \left. \left. 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \right. \right. \\
& \quad \left. \left. \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8\right)^{1/3}\right) + \\
& \quad \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \left. \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \right. \\
& \quad \left. 33554432 \pi^{18} r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \right. \\
& \quad \left. \left. 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \right. \right. \\
& \quad \left. \left. \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \right. \right. \\
& \quad \left. \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \right. \\
& \quad \left. \left. 474989023199232 \pi^{32} r_1^8\right)^{1/3}} / \left(3 \times 2^{1/3} \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)\right)\right) \Bigg\}, \\
& \left\{\frac{\pi \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left(\frac{4 \pi^2 \left(3 - 16 \pi^4 + 32 \pi^4 r_1^2\right)^2}{\left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)^2} - \frac{8 \pi^2 \left(13 - 16 \pi^4 + 64 \pi^4 r_1^2\right)}{3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)} + \right. \right. \\
& \quad \left. \left(2^{1/3} \left(16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4\right)\right) / \right. \\
& \quad \left. \left(3 \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right) \left(128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} \right. \right. \right. \\
& \quad \left. \left. r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} \right. \right. \\
& \quad \left. \left. r_1^6 + \sqrt{\left(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \right. \right. \\
& \quad \left. \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \right. \\
& \quad \left. \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \right. \\
& \quad \left. \left. 356241767399424 \pi^{32} r_1^6 - \right. \right. \\
& \quad \left. \left. 474989023199232 \pi^{32} r_1^8\right)^{1/3}} / \left(3 \times 2^{1/3} \left(1 - 16 \pi^4 + 16 \pi^4 r_1^2\right)\right)\right) \Bigg\},
\end{aligned}$$

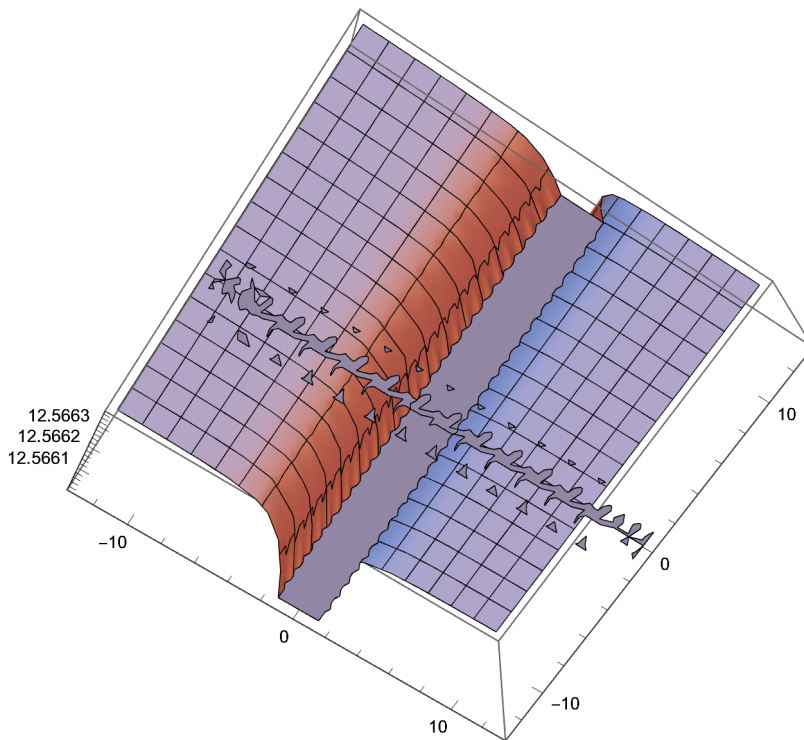
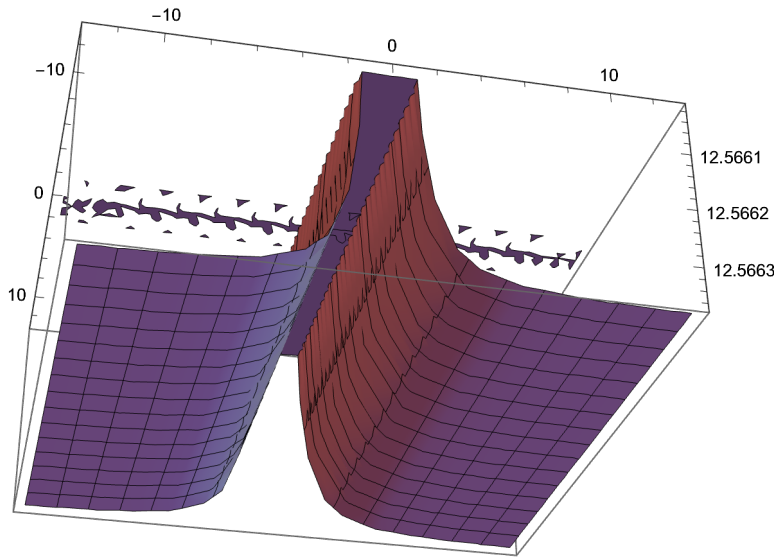
$$\begin{aligned}
& \left( 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} + \\
& \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 + \\
& \quad \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right.} \\
& \quad \quad 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \\
& \quad \quad \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - 356\,241\,767\,399\,424\right. \\
& \quad \quad \left. \pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right) \right) \Big) + \\
& \frac{1}{2} \sqrt{\left( \frac{8\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4 r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right)^2} - \frac{16\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4 r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right)} - \right.} \\
& \quad \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8 r_1^2 - 32\,768\,\pi^{12} r_1^2 + 65\,536\,\pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right) \right. \\
& \quad \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad \quad r_1^2 + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 \\
& \quad \quad r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right.} \\
& \quad \quad \quad 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \\
& \quad \quad \quad \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - \right. \\
& \quad \quad \quad \left. 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \Big) - \\
& \quad \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + \right. \\
& \quad \quad 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 + \\
& \quad \quad \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - \right.} \\
& \quad \quad \quad 7\,421\,703\,487\,488\,\pi^{32}r_1^2 + 347\,892\,350\,976\,\pi^{24}r_1^4 + 38\,963\,943\,309\,312\,\pi^{28}r_1^4 + \\
& \quad \quad \quad \left. 89\,060\,441\,849\,856\,\pi^{32}r_1^4 + 22\,265\,110\,462\,464\,\pi^{28}r_1^6 - \right. \\
& \quad \quad \quad \left. 356\,241\,767\,399\,424\,\pi^{32}r_1^6 + 474\,989\,023\,199\,232\,\pi^{32}r_1^8 \right)^{1/3} \Big) \Big/ \\
& \quad \left( 3 \times 2^{1/3} \left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right) \right) + \left( \frac{768\,\pi^3}{1 - 16\,\pi^4 + 16\,\pi^4 r_1^2} + \frac{64\,\pi^3 \left( 3 - 16\,\pi^4 + 32\,\pi^4 r_1^2 \right)^3}{\left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right)^3} - \right. \\
& \quad \left. \frac{64\,\pi^3 \left( 3 - 16\,\pi^4 + 32\,\pi^4 r_1^2 \right) \left( 13 - 16\,\pi^4 + 64\,\pi^4 r_1^2 \right)}{\left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right)^2} \right) \Big/ \\
& \quad \left( 4 \sqrt{\left( \frac{4\,\pi^2 \left( 3 - 16\,\pi^4 + 32\,\pi^4 r_1^2 \right)^2}{\left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right)^2} - \frac{8\,\pi^2 \left( 13 - 16\,\pi^4 + 64\,\pi^4 r_1^2 \right)}{3 \left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right)} + \right.} \\
& \quad \left( 2^{1/3} \left( 16\,\pi^4 - 512\,\pi^8 + 4096\,\pi^{12} + 2048\,\pi^8 r_1^2 - 32\,768\,\pi^{12} r_1^2 + 65\,536\,\pi^{12} r_1^4 \right) \right) \Big/ \\
& \quad \left( 3 \left( 1 - 16\,\pi^4 + 16\,\pi^4 r_1^2 \right) \left( 128\,\pi^6 - 6144\,\pi^{10} + 98\,304\,\pi^{14} - 524\,288\,\pi^{18} + \right. \right. \\
& \quad \quad 24\,576\,\pi^{10}r_1^2 + 6\,291\,456\,\pi^{14}r_1^2 + 6\,291\,456\,\pi^{18}r_1^2 + 1\,572\,864\,\pi^{14}r_1^4 - \\
& \quad \quad 25\,165\,824\,\pi^{18}r_1^4 + 33\,554\,432\,\pi^{18}r_1^6 + \sqrt{\left( 1\,811\,939\,328\,\pi^{20}r_1^2 - \right.} \\
& \quad \quad \quad \left. 86\,973\,087\,744\,\pi^{24}r_1^2 + 1\,391\,569\,403\,904\,\pi^{28}r_1^2 - 7\,421\,703\,487\,488 \right.
\end{aligned}$$

$$\left\{ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} - \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\ \left. \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4)) / \right. \right. \\ \left. \left. (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} \right. \right. \\ \left. \left. r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} \right. \right. \\ \left. \left. r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \right. \\ \left. \left. 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + \right. \right. \\ \left. \left. 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \right. \right. \\ \left. \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8))^{1/3} \right) + \right. \\ \left. (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\ \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\ \left. \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\ \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \right. \\ \left. 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \right. \\ \left. \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8))^{1/3} \right) + \left. \right\}$$

$$\begin{aligned}
& \left. \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8 \right)^{1/3} / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Bigg) + \\
& \frac{1}{2} \sqrt[4]{ \left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right. \\
& \quad \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4) \right) / \\
& \quad \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8)})^{1/3} \right) - \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8)})^{1/3} \right) / \\
& \quad \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) - \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) \Bigg) / \\
& \quad \left( 4 \sqrt[4]{ \left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32\,768 \pi^{12} r_1^2 + 65\,536 \pi^{12} r_1^4) \right) / \right. \\
& \quad \left. \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8)})^{1/3} \right) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8)})^{1/3} \right) + \\
& \quad \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98\,304 \pi^{14} - 524\,288 \pi^{18} + 24\,576 \pi^{10} r_1^2 + 6\,291\,456 \pi^{14} r_1^2 + 6\,291\,456 \pi^{18} r_1^2 + 1\,572\,864 \pi^{14} r_1^4 - 25\,165\,824 \pi^{18} r_1^4 + 33\,554\,432 \pi^{18} r_1^6 + \sqrt{(1\,811\,939\,328 \pi^{20} r_1^2 - 86\,973\,087\,744 \pi^{24} r_1^2 + 1\,391\,569\,403\,904 \pi^{28} r_1^2 - 7\,421\,703\,487\,488 \pi^{32} r_1^2 + 347\,892\,350\,976 \pi^{24} r_1^4 + 38\,963\,943\,309\,312 \pi^{28} r_1^4 + 89\,060\,441\,849\,856 \pi^{32} r_1^4 + 22\,265\,110\,462\,464 \pi^{28} r_1^6 - 356\,241\,767\,399\,424 \pi^{32} r_1^6 + 474\,989\,023\,199\,232 \pi^{32} r_1^8)})^{1/3} \right) \right) +
\end{aligned}$$







Math like mana falling

$$\text{Solve} \left[ \frac{\pi (3 - 16 \pi^4 + 32 \pi^4 r_1^2)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4)) \right)} \right] / (3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2))$$

$$\begin{aligned}
& \left( (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 \right. \\
& \quad \left. r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \right) + \\
& \left( (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \\
& \quad \left. \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \right) / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{16 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} - \right. \\
& \quad \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 \right. \right. \\
& \quad \left. \left. r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \right) - \right. \\
& \quad \left. (128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8)}^{1/3} \right) / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^3}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^3} - \frac{64 \pi^3 (3 - 16 \pi^4 + 32 \pi^4 r_1^2) (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} \right) / \left( 4 \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left. (2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) / \right)
\end{aligned}$$

$$\begin{aligned} & \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + \right. \right. \\ & 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - \\ & 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \sqrt{\left( 1811939328 \pi^{20} r_1^2 - \right.} \\ & 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - 7421703487488 \\ & \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + \\ & 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\ & \left. \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8 \right) \right)^{1/3} \Big) + \\ & \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \\ & 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \\ & \sqrt{\left( 1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right.} \\ & 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \\ & \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \\ & \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} \right. \\ & \left. \left. r_1^8 \right) \right)^{1/3} \Big/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Big) \Big) \Big) \Big) \Big) = \\ & \left( \pi - \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right.} \right. \\ & \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) - \right. \\ & \left. \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} - \right.} \right. \\ & \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} - \right.} \right. \\ & \left. \left. \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) \right) \Big/ \right. \\ & \left. \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}} + \right.} \right. \right. \\ & \left. \left. \left. \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right) \Big) \Big) \Big) \Big) \Big) , r \Big] \end{aligned}$$

Solve[

$$\frac{\pi \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{1}{2} \sqrt{\left( \frac{4 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{8 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} \right)} + \left( 2^{1/3} \right)$$

$$\begin{aligned}
& \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4 \right) \Bigg/ \left( 3 \left( 1 - 16 \pi^4 + \right. \right. \\
& 16 \pi^4 r_1^2 \Bigg) \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} \right. \\
& r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
& \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right.} \\
& 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} r_1^4 + \\
& 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - \\
& \left. \left. 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) + \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
& 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
& \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} r_1^2 - \right.} \\
& 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \pi^{28} \\
& r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} r_1^6 - 356 241 767 399 424 \\
& \left. \left. \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg/ \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{8 \pi^2 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^2}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} - \frac{16 \pi^2 \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)} - \right.} \\
& \left. \left( 2^{1/3} \left( 16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32 768 \pi^{12} r_1^2 + 65 536 \pi^{12} r_1^4 \right) \right) \Bigg/ \right. \\
& \left( 3 \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + \right. \right. \\
& 6 291 456 \pi^{14} r_1^2 + 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + \\
& 33 554 432 \pi^{18} r_1^6 + \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + \right.} \\
& 1 391 569 403 904 \pi^{28} r_1^2 - 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + \\
& 38 963 943 309 312 \pi^{28} r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \\
& \left. \left. \pi^{28} r_1^6 - 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg) - \\
& \left( 128 \pi^6 - 6144 \pi^{10} + 98 304 \pi^{14} - 524 288 \pi^{18} + 24 576 \pi^{10} r_1^2 + 6 291 456 \pi^{14} r_1^2 + \right. \\
& 6 291 456 \pi^{18} r_1^2 + 1 572 864 \pi^{14} r_1^4 - 25 165 824 \pi^{18} r_1^4 + 33 554 432 \pi^{18} r_1^6 + \\
& \sqrt{\left( 1 811 939 328 \pi^{20} r_1^2 - 86 973 087 744 \pi^{24} r_1^2 + 1 391 569 403 904 \pi^{28} \right.} \\
& r_1^2 - 7 421 703 487 488 \pi^{32} r_1^2 + 347 892 350 976 \pi^{24} r_1^4 + 38 963 943 309 312 \\
& \pi^{28} r_1^4 + 89 060 441 849 856 \pi^{32} r_1^4 + 22 265 110 462 464 \pi^{28} \\
& \left. \left. r_1^6 - 356 241 767 399 424 \pi^{32} r_1^6 + 474 989 023 199 232 \pi^{32} r_1^8 \right) \right)^{1/3} \Bigg/ \\
& \left( 3 \times 2^{1/3} \left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right) \right) + \left( \frac{768 \pi^3}{1 - 16 \pi^4 + 16 \pi^4 r_1^2} + \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right)^3}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^3} - \right. \\
& \left. \frac{64 \pi^3 \left( 3 - 16 \pi^4 + 32 \pi^4 r_1^2 \right) \left( 13 - 16 \pi^4 + 64 \pi^4 r_1^2 \right)}{\left( 1 - 16 \pi^4 + 16 \pi^4 r_1^2 \right)^2} \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \sqrt{\left( \frac{4 \pi^2 (3 - 16 \pi^4 + 32 \pi^4 r_1^2)^2}{(1 - 16 \pi^4 + 16 \pi^4 r_1^2)^2} - \frac{8 \pi^2 (13 - 16 \pi^4 + 64 \pi^4 r_1^2)}{3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2)} + \right. \right. \\
& \quad \left. \left( 2^{1/3} (16 \pi^4 - 512 \pi^8 + 4096 \pi^{12} + 2048 \pi^8 r_1^2 - 32768 \pi^{12} r_1^2 + 65536 \pi^{12} r_1^4) \right) \right) / \\
& \quad \left( 3 (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right. \\
& \quad \left. \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \pi^{14} r_1^2 + \right. \right. \\
& \quad \left. \left. 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + 33554432 \pi^{18} r_1^6 + \right. \right. \\
& \quad \left. \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + 1391569403904 \pi^{28} r_1^2 - \right. \\
& \quad \left. 7421703487488 \pi^{32} r_1^2 + 347892350976 \pi^{24} r_1^4 + 38963943309312 \right. \\
& \quad \left. \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + 22265110462464 \pi^{28} r_1^6 - \right. \\
& \quad \left. 356241767399424 \pi^{32} r_1^6 + 474989023199232 \pi^{32} r_1^8) \right)^{1/3} \Big) + \\
& \quad \left( 128 \pi^6 - 6144 \pi^{10} + 98304 \pi^{14} - 524288 \pi^{18} + 24576 \pi^{10} r_1^2 + 6291456 \right. \\
& \quad \left. \pi^{14} r_1^2 + 6291456 \pi^{18} r_1^2 + 1572864 \pi^{14} r_1^4 - 25165824 \pi^{18} r_1^4 + \right. \\
& \quad \left. 33554432 \pi^{18} r_1^6 + \sqrt{(1811939328 \pi^{20} r_1^2 - 86973087744 \pi^{24} r_1^2 + \right. \\
& \quad \left. 1391569403904 \pi^{28} r_1^2 - 7421703487488 \pi^{32} r_1^2 + 347892350976 \right. \\
& \quad \left. \pi^{24} r_1^4 + 38963943309312 \pi^{28} r_1^4 + 89060441849856 \pi^{32} r_1^4 + \right. \\
& \quad \left. 22265110462464 \pi^{28} r_1^6 - 356241767399424 \pi^{32} r_1^6 + \right. \\
& \quad \left. 474989023199232 \pi^{32} r_1^8) \right)^{1/3} / \left( 3 \times 2^{1/3} (1 - 16 \pi^4 + 16 \pi^4 r_1^2) \right) \Big) \Big) \Big) = \\
& \pi - \frac{1}{2} \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 (1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}} + \right. \\
& \quad \left. \frac{(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}}{12 \pi^2 r^2} \right) - \\
& \frac{1}{2} \sqrt{\left( 8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 (1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}} - \right. \\
& \quad \left. \frac{(1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}}{12 \pi^2 r^2} \right) - \\
& \quad \left( 64 \pi^3 + \frac{4}{\pi r^2} \right) / \\
& \left( 4 \sqrt{\left( 4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 (1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8})^{1/3}} + \right. \right.
\end{aligned}$$

$$\left( \frac{\left( 1 + 13824 \pi^8 r^4 + 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8} \right)^{1/3}}{12 \pi^2 r^2} \right) \Bigg) \Bigg) \Bigg) , r \Big]$$

$$v = \lambda v = r \left( 1 / (1080 / \pi) \theta \right) = \left( 1 / (1080 / \pi) \right) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$E = h v = h n f = m c^2$$

$$\text{Solve}[h \left( 1 / (1080 / \pi) \theta \right) == m c^2, m]$$

$$\left\{ \left\{ m \rightarrow 2.14457 \times 10^{-53} \theta \right\} \right\}$$

$$m * a = \left( \frac{1}{1166400} \pi^2 \left( - \frac{15 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi r \theta - 2 r \theta^2)^2}{32 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \right. \right. \\ \frac{3 (4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi \theta - 2 \theta^2)}{16 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 (8 \pi r - 4 r \theta) (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \\ \frac{3 r^2 (8 \pi r \theta - 2 r \theta^2)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{(8 \pi r - 4 r \theta)^2}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{(8 \pi - 4 \theta) (4 \pi r^2 - 2 r^2 \theta)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \\ \left. \left. \frac{r^2 (8 \pi \theta - 2 \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{1}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right)$$

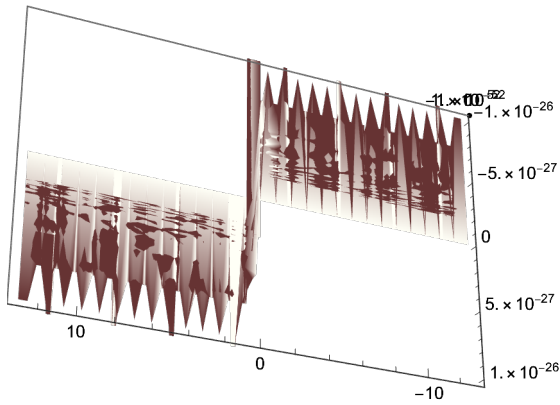
$$c := (2.99792458 * 10^8)$$

$$h := (6.626068 * 10^{-34})$$

```

RevolutionPlot3D[2.144571844054625`*^-53  $\theta \frac{r (2 \pi - \theta)}{2 \pi \theta \sqrt{r^2 (4 \pi - \theta) \theta}}$ ,
{r, -13, 13}, { $\theta$ , -10^-53, 10^-53}]

```

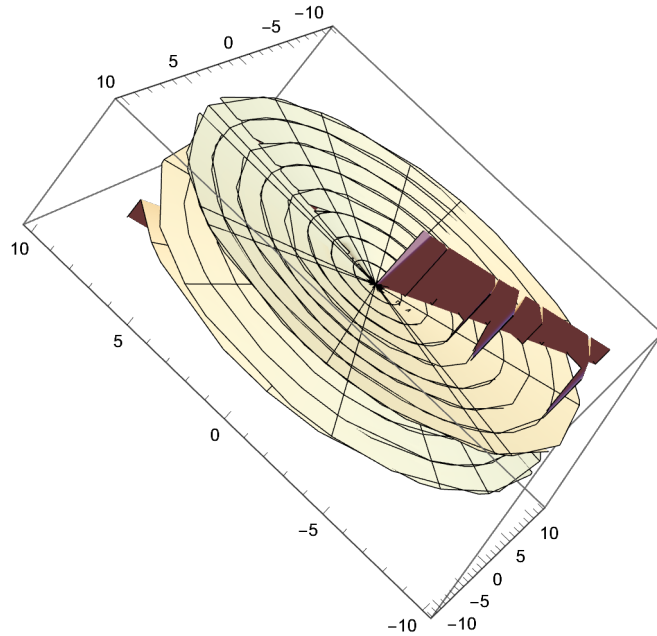


$$\int m \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} d\theta$$

$$\frac{m\sqrt{\theta}\sqrt{\frac{(-2\pi+\theta)^2}{(4\pi-\theta)\theta^2}}\left(4\pi-\theta+2\sqrt{(4\pi-\theta)\theta}\operatorname{ArcSin}\left[\frac{\sqrt{\theta}}{2\sqrt{\pi}}\right]\right)}{2\pi(-2\pi+\theta)}$$



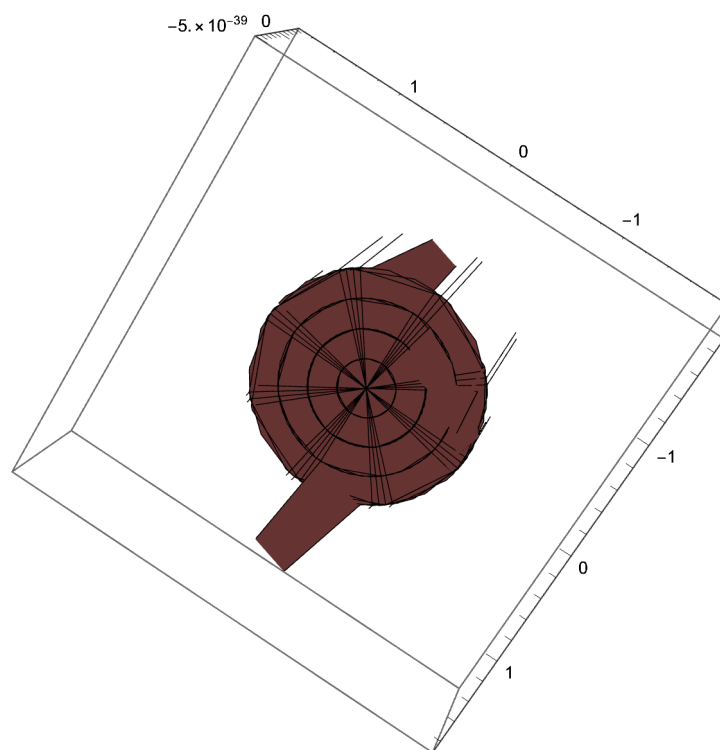
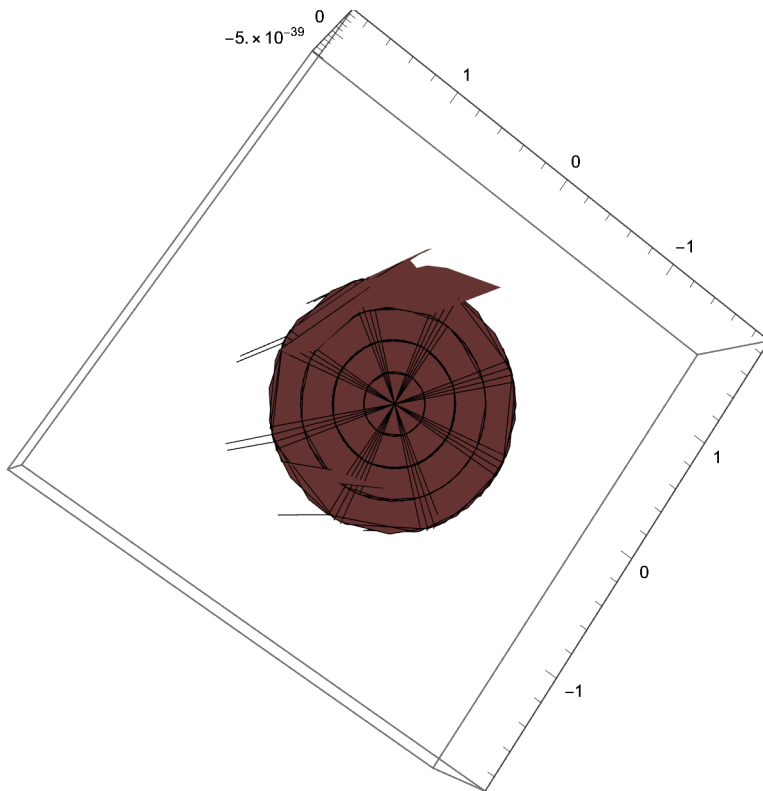
$$\text{RevolutionPlot3D}\left[\frac{m \sqrt{\theta} \sqrt{\frac{(-2\pi+\theta)^2}{(4\pi-\theta)\theta^2}} \left(4\pi-\theta+2\sqrt{(4\pi-\theta)\theta} \text{ArcSin}\left[\frac{\sqrt{\theta}}{2\sqrt{\pi}}\right]\right)}{2\pi(-2\pi+\theta)},\right. \\ \left.\{m, -10, 10\}, \{\theta, -13, 13\}\right]$$

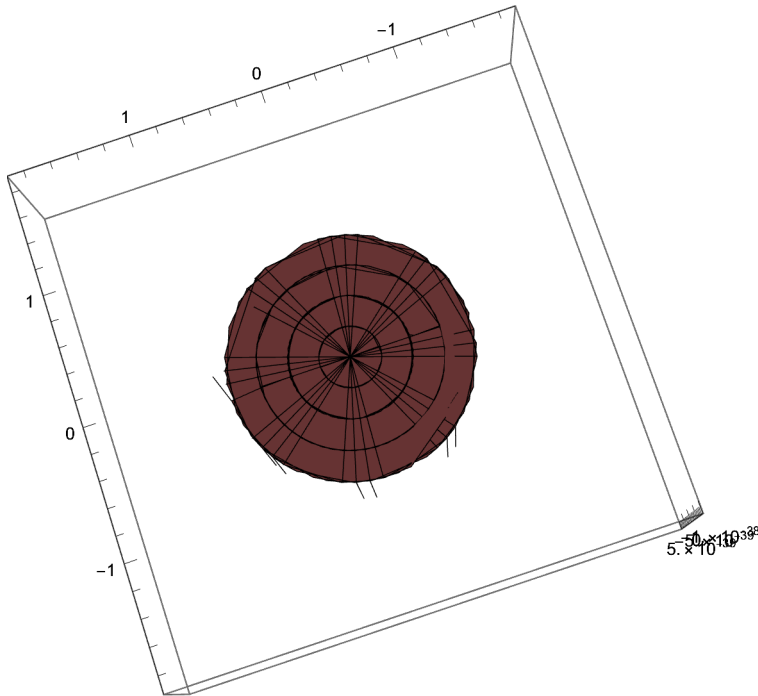


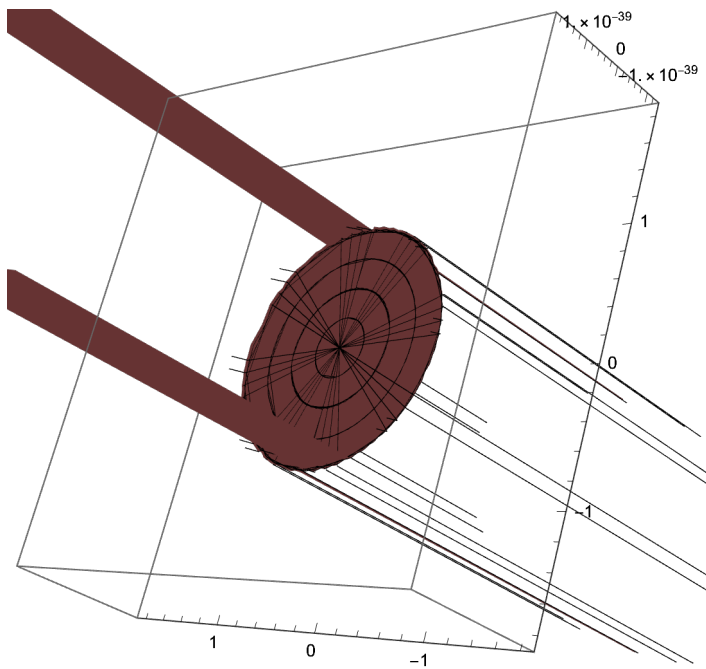
$$\text{RevolutionPlot3D}\left[2.144571844054625 \cdot 10^{-53} \theta \frac{r(2\pi-\theta)}{2\pi\theta\sqrt{r^2(4\pi-\theta)\theta}},\right. \\ \left.\{r, -13, 13\}, \{\theta, -10^{-53}, 10^{-53}\}\right]$$



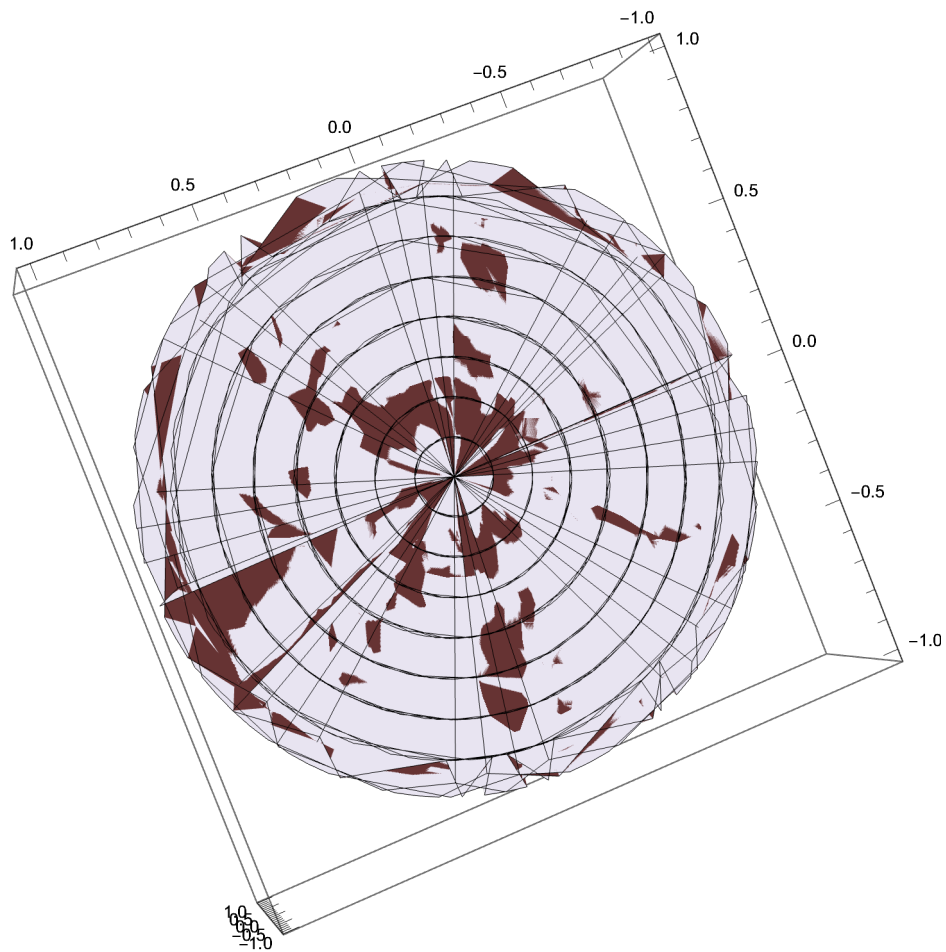
$\text{RevolutionPlot3D}\left[\frac{r^{1155} (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)} \theta}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$



$$\text{RevolutionPlot3D}\left[\frac{r^{1157} (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)} \theta}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$$


$$\text{RevolutionPlot3D}\left[\frac{r^{1182} (2\pi - \theta)}{2\pi\theta \sqrt{r^2 (4\pi - \theta)} \theta}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$$


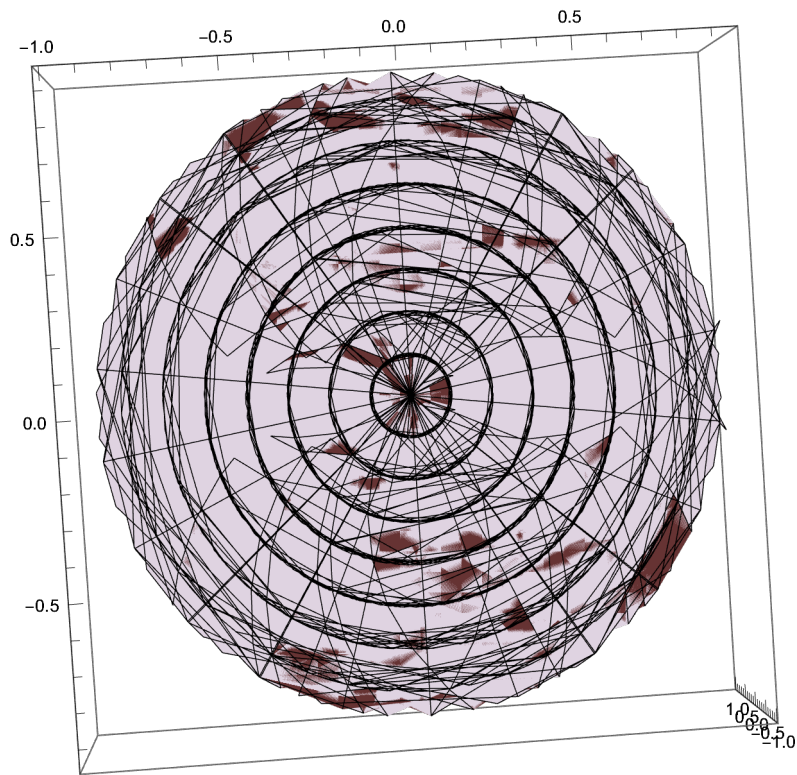
`RevolutionPlot3D` $\left[\frac{r^{99999999} (2 \pi - \theta)}{2 \pi \theta \sqrt{r^2 (4 \pi - \theta) \theta}}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$

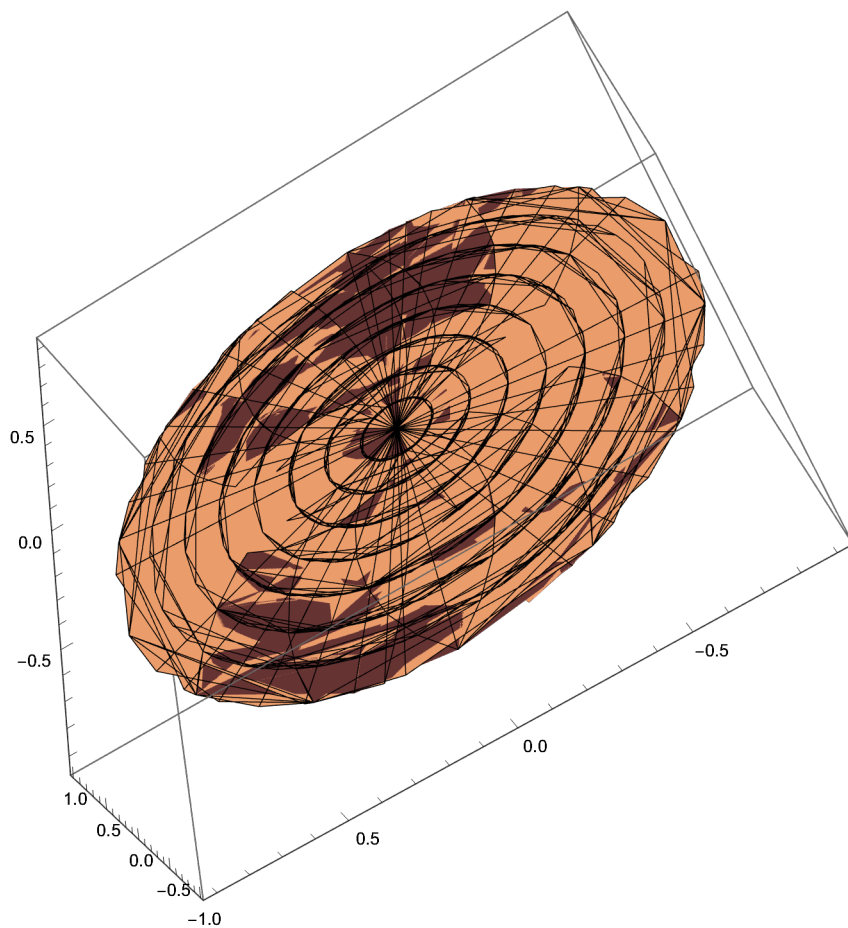


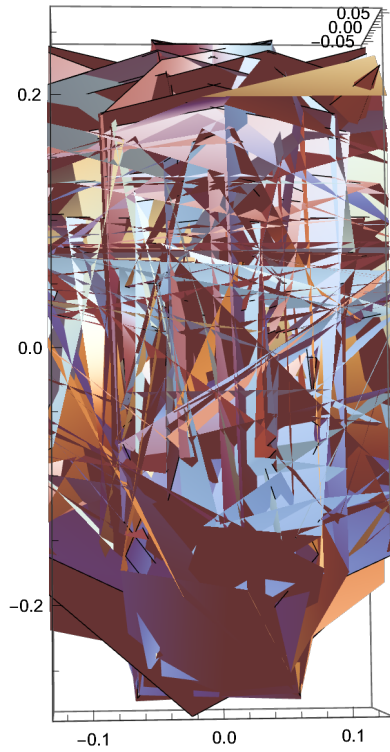
```

RevolutionPlot3D[ $\frac{1}{2 \pi \theta \sqrt{r^2 (4 \pi - \theta) \theta}}$ ,
  r^100 000 000 000 000 000 000 000 000 000 199 999 999 (2 \pi - r), {r, -13, 13}, {\theta, -13, 13}]

```

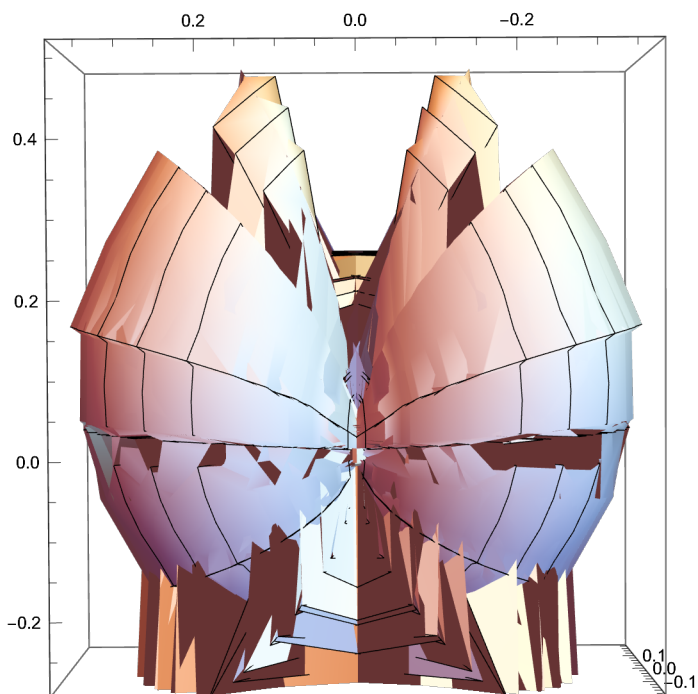


$$\text{RevolutionPlot3D}\left[\frac{r^{1000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,000\,199\,999\,999}(2 \pi - r)}{2 \pi \theta \sqrt{r^2(4 \pi - \theta) \theta}}, \{r, -13, 13\}, \{\theta, -4 \pi, 4 \pi\} \right]$$


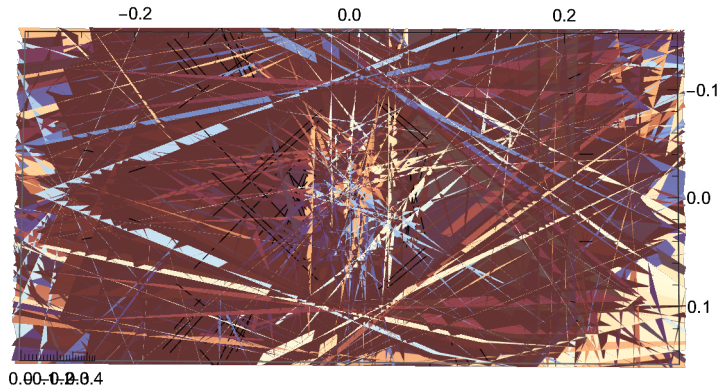
$$\text{SphericalPlot3D}\left[\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\sqrt{\frac{1-4\pi^3}{4\pi-\theta}-\frac{3}{\theta^2}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2},\right. \\ \left.\{ \theta, -3600, 3600 \}, \{ \beta, -3600, 3600 \} \right]$$




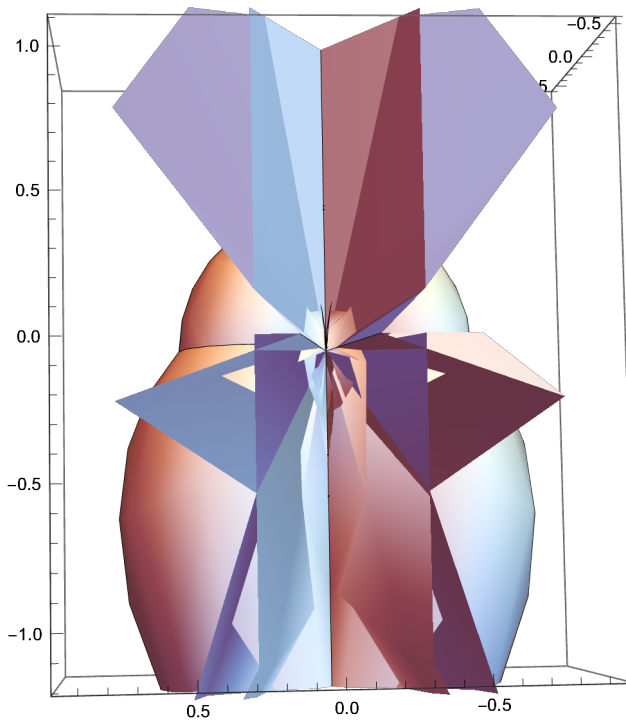
$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi^3}{\theta^2}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\theta^2},\right. \\ \left.\{\theta, -360, 360\}, \{\beta, -360, 360\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi^3}{\theta^2}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\theta^2},\right. \\ \left.\{\theta, -10, 10^4\}, \{\beta, -10^9, 10\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}}-\frac{4\pi}{4\pi-\theta}\right)\sin[\beta]\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi^2}{\theta^2}}-\frac{4\pi}{\theta}\right)\sin[\beta]}\right)^2\theta^2}}{2\pi},\right. \\ \left.\{\theta, -4\pi, 4\pi\}, \{\beta, -4\pi, 4\pi\}\right]$$



The Four Noble Truths of  $\theta$ , The

# Hologram of Vision

by Parker Matthew Davis Emmerson

## Postulates, polar coordinates, etc.

$$\text{Sin}[\beta] = \eta / r \quad (113)$$

$$\text{Tan}[\beta] = \eta / r_1 \quad (114)$$

$$\text{Cos}[\beta] = r_1 / r \quad (115)$$

$$\eta = r \text{Sin}[\beta] \quad (116)$$

$$r = \eta / \text{Sin}[\beta]$$

$$\text{Cos}[\beta] = r_1 / r = r_1 / (\eta / \text{Sin}[\beta])$$

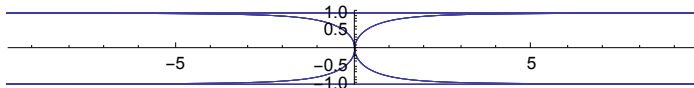
$$\text{Simplify}[r_1 / (\eta / \text{Sin}[\beta])]$$

$$\frac{\text{Sin}[\beta] r_1}{\eta}$$

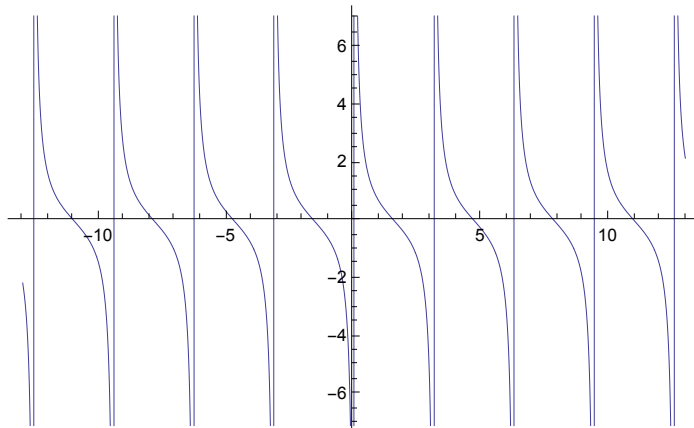
$$\frac{\text{Sin}[\beta] r_1}{\eta} = \text{Cos}[\beta]$$

$$\text{Cos}[\beta] / \text{Sin}[\beta] = \frac{r_1}{\eta}$$

$$\text{PolarPlot}[\text{Cos}[\beta] / \text{Sin}[\beta], \{\beta, -13, 13\}]$$



$$\text{Plot}[\text{Cos}[\beta] / \text{Sin}[\beta], \{\beta, -13, 13\}]$$



$$\text{Solve}[\theta r == 2 \pi (r) - 2 \pi \sqrt{(r)^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\} \right\}$$

go from the philosophy to the axioms / geometric description,  
backed up with psych and philosophy

take the geometric situation described and working out what follows.

$$\eta == \frac{\sqrt{4 \pi \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}}{2 \pi} = \text{rate} * \text{time} = \text{rate} * 6 ((180 / \pi) \theta) \quad (117)$$

$$\left\{ \left\{ r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\} \right\} \quad (118)$$

$$\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2 - \eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2 - \eta^2} \right\} \right\} \quad (119)$$

$$r_1 = \sqrt{r^2 - \eta^2} = r \cos[\beta] \quad (120)$$

There are special cases of the system when  $h = r$ , when  $\beta = \theta$ ,  
when  $r_1 = r$  (the initial condition), and when  $r_1 = h$ .

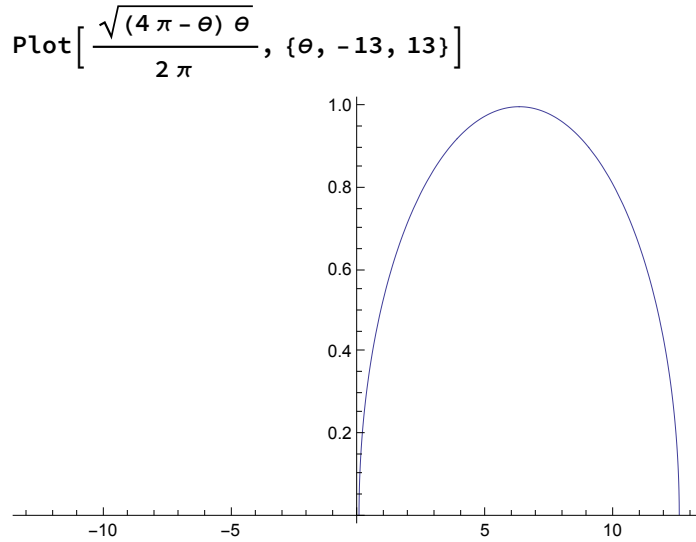
Usually, we would think that  $\beta \leq \pi / 2$ , whereas  $\theta \leq 4 \pi$ . (121)

We can show that  $\theta \leq 4 \pi$  by setting  $r$  equal to one in the equation  $r = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$

$\beta \leq \pi / 2$  comes from the fact that when the cone folds all the way up,  
it makes a right angle with the x axis.

$$\text{Solve}\left[1 == \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \eta\right]$$

$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right\} \right\}$$



There is a particularly interesting special case of the system, however, when the square of the height of the cone is equal to the area of the base of the cone.

## So What's the Point? How to Find the Four Noble $\theta$ Solutions, or Truths of $\theta$ .

$$r_1 = \sqrt{r^2 - \eta^2}$$

$$\eta = r \sin[\beta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\}$$

$$\left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right)^2 = \eta^2$$

$$\left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right)^2$$

$$\frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}$$

$$\frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2} = \pi (r_1^2) = \pi (r^2 - \eta^2) = \pi \left( r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2} \right)$$

$$\text{Solve}\left[\pi\left(r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}\right) == \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi}\right\}, \left\{\theta \rightarrow \frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1 + \pi)}\right\}\right\}$$

$$\text{N}\left[\frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi}\right]$$

3.19576

$$\text{N}\left[\frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1 + \pi)}\right]$$

9.37061

$$\text{Solve}\left[\pi\left(r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}\right) == \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}, r\right]$$

$$\{\{r \rightarrow 0\}, \{r \rightarrow 0\}\}$$

Thus, we have shown that a point, by definition, is the place at which the square of the height of a cone is equal to the area of the base of the cone when talking about a transition or even a translation of

points along an axis. We have also shown that the point has an inherent angle of  $\frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1 + \pi)}$

and  $\frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi}$  radians.

So, what does  $\theta r$  look like now?

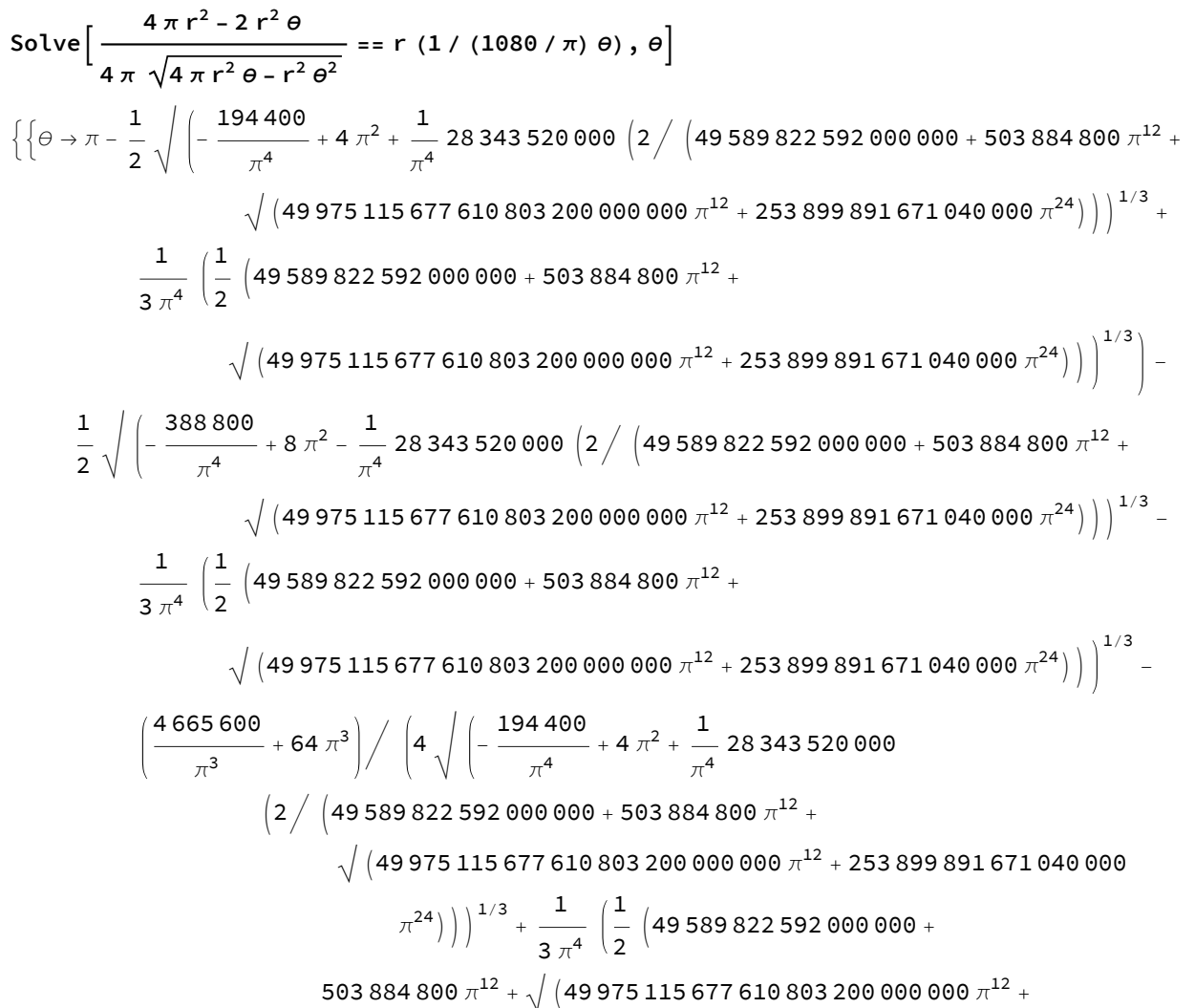
$$\theta r = r \frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1 + \pi)}, r \frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi}$$

$$v = \lambda v = r(1 / (1080 / \pi) \theta) = D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

The velocity of  $\eta$  is equal to the first derivative of  $\eta$  with respect to time.

$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$



$$\begin{aligned} & \left\{ \theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( -\frac{194\,400}{\pi^4} + 4\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 \Big/ \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right) \right) \right)^{1/3} + \right. \\ & \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right) \right) \right)^{1/3} \right) - \\ & \quad \frac{1}{2} \sqrt{\left( -\frac{388\,800}{\pi^4} + 8\pi^2 - \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 \Big/ \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right) \right) \right)^{1/3} - \right. \\ & \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \end{aligned}$$



$$\begin{aligned}
& \sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\,\pi^{24}\right)} \Bigg)^{1/3} + \\
& \left(\frac{4\,665\,600}{\pi^3} + 64\,\pi^3\right) \Bigg/ \left(4\sqrt{\left(-\frac{194\,400}{\pi^4} + 4\,\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000\right.}\right. \\
& \quad \left.\left(2\Bigg/\left(49\,589\,822\,592\,000\,000 + 503\,884\,800\,\pi^{12} + \right.\right.\right. \\
& \quad \left.\left.\sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\right.\right.\right. \\
& \quad \left.\left.\pi^{24}\right)\right)\Bigg)^{1/3} + \frac{1}{3\,\pi^4} \left(\frac{1}{2} \left(49\,589\,822\,592\,000\,000 + \right.\right. \\
& \quad \left.\left.503\,884\,800\,\pi^{12} + \sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + \right.\right.\right. \\
& \quad \left.\left.\left.253\,899\,891\,671\,040\,000\,\pi^{24}\right)\right)\right)\Bigg)^{1/3} \Bigg)\Bigg)\Bigg)\Bigg\}, \\
& \left\{\theta \rightarrow \pi + \frac{1}{2}\sqrt{\left(-\frac{194\,400}{\pi^4} + 4\,\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000\right.}\right. \\
& \quad \left.\left(2\Bigg/\left(49\,589\,822\,592\,000\,000 + 503\,884\,800\,\pi^{12} + \right.\right.\right. \\
& \quad \left.\left.\sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\,\pi^{24}\right)\right)\right)\Bigg)^{1/3} + \\
& \quad \frac{1}{3\,\pi^4} \left(\frac{1}{2} \left(49\,589\,822\,592\,000\,000 + 503\,884\,800\,\pi^{12} + \right.\right. \\
& \quad \left.\left.\sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\,\pi^{24}\right)\right)\right)\Bigg)^{1/3} \Bigg) + \\
& \frac{1}{2}\sqrt{\left(-\frac{388\,800}{\pi^4} + 8\,\pi^2 - \frac{1}{\pi^4} 28\,343\,520\,000\right.}\right. \\
& \quad \left.\left(2\Bigg/\left(49\,589\,822\,592\,000\,000 + 503\,884\,800\,\pi^{12} + \right.\right.\right. \\
& \quad \left.\left.\sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\,\pi^{24}\right)\right)\right)\Bigg)^{1/3} - \\
& \quad \frac{1}{3\,\pi^4} \left(\frac{1}{2} \left(49\,589\,822\,592\,000\,000 + 503\,884\,800\,\pi^{12} + \right.\right. \\
& \quad \left.\left.\sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\,\pi^{24}\right)\right)\right)\Bigg)^{1/3} + \\
& \left(\frac{4\,665\,600}{\pi^3} + 64\,\pi^3\right) \Bigg/ \left(4\sqrt{\left(-\frac{194\,400}{\pi^4} + 4\,\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000\right.}\right. \\
& \quad \left.\left(2\Bigg/\left(49\,589\,822\,592\,000\,000 + 503\,884\,800\,\pi^{12} + \right.\right.\right. \\
& \quad \left.\left.\sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + 253\,899\,891\,671\,040\,000\right.\right.\right. \\
& \quad \left.\left.\pi^{24}\right)\right)\Bigg)^{1/3} + \frac{1}{3\,\pi^4} \left(\frac{1}{2} \left(49\,589\,822\,592\,000\,000 + \right.\right. \\
& \quad \left.\left.503\,884\,800\,\pi^{12} + \sqrt{\left(49\,975\,115\,677\,610\,803\,200\,000\,000\,\pi^{12} + \right.\right.\right. \\
& \quad \left.\left.\left.253\,899\,891\,671\,040\,000\,\pi^{24}\right)\right)\right)\Bigg)^{1/3} \Bigg)\Bigg)\Bigg)\Bigg\}
\end{aligned}$$

These are mathematical expressions of the reality of the four noble truths.

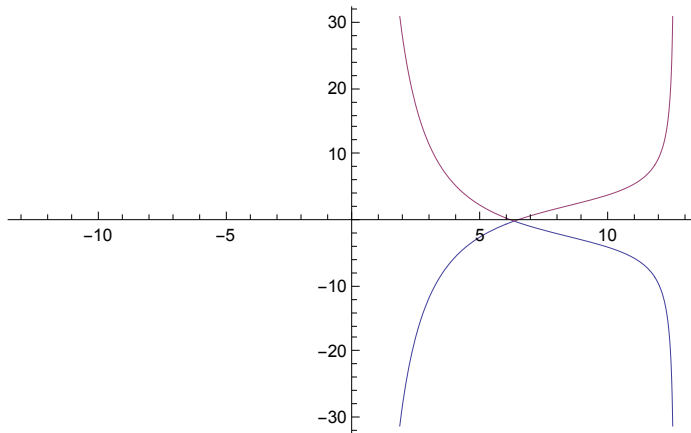
$$D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, r, \theta\right]$$

$$-\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}$$

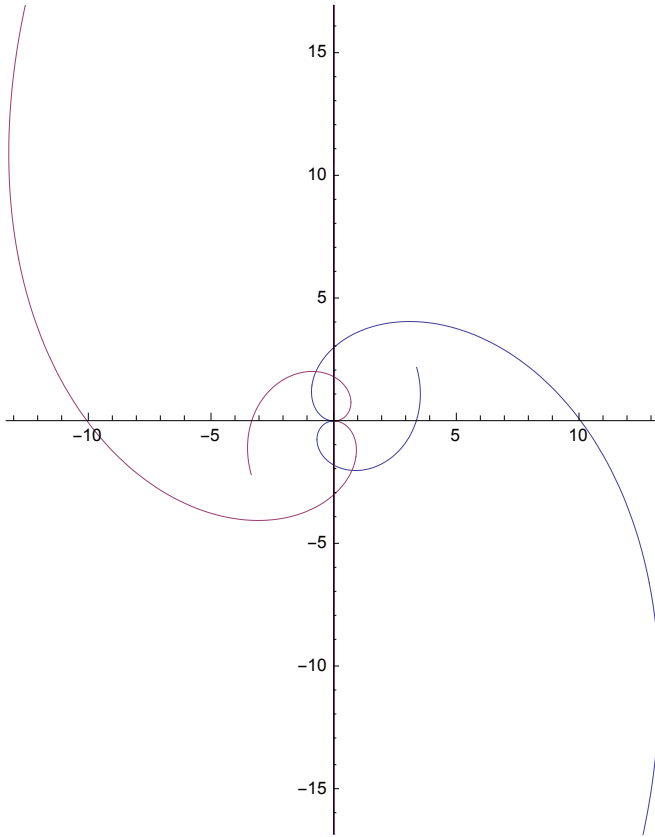
$$\text{Solve}\left[-\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} == r(1/(1080/\pi)\theta), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{270\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{\pi^2\sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{270\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{\pi^2\sqrt{\theta}}\right\}\right\}$$

$$\text{Plot}\left[\left\{-\frac{270\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{\pi^2\sqrt{\theta}}, \frac{270\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{\pi^2\sqrt{\theta}}\right\}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\left\{-\frac{270 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2 \sqrt{\theta}}, \frac{270 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2 \sqrt{\theta}}\right\},\{\theta,-10,10\}\right]$$



$$\sqrt{r^2-\eta^2}$$

$$\frac{2 \pi \eta}{\sqrt{4 \pi \theta-\theta^2}}=r=\frac{270 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2 \sqrt{\theta}}$$

$$\text{Solve}\left[\frac{2 \pi \eta}{\sqrt{4 \pi \theta-\theta^2}}==\frac{270 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2 \sqrt{\theta}}, \eta\right]$$

$$\left\{\left\{\eta \rightarrow \frac{135 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}} \sqrt{4 \pi \theta-\theta^2}}{\pi^3 \sqrt{\theta}}\right\}\right\}$$

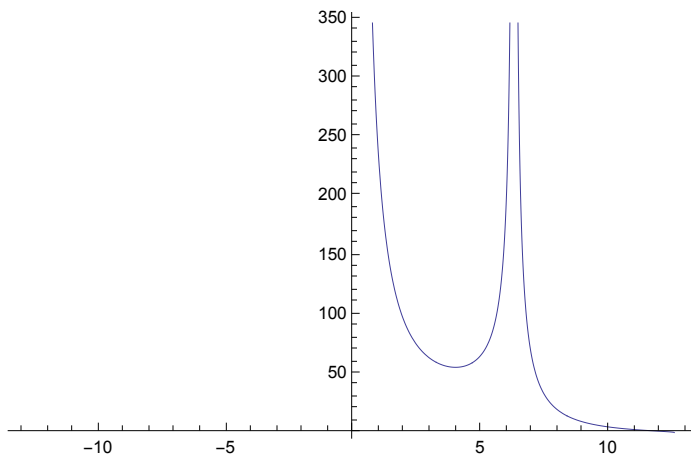
$$\lambda v=r(1 /(1080 / \pi) \theta)=$$

$$(1 /(1080 / \pi)) D\left[\frac{\sqrt{4 \pi r^2 \theta-r^2 \theta^2}}{2 \pi}, \theta\right]=(1 /(1080 / \pi)) D[\eta, \theta]=\text { velocity}$$

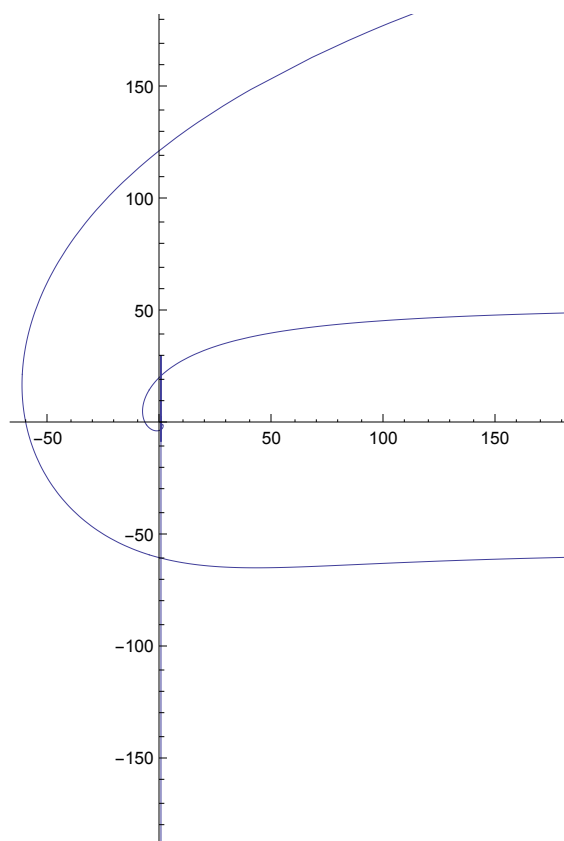
$$\text{Solve}\left[\text{D}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \theta\right] == \text{D}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right], r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{1080 \sqrt{-\frac{8\pi^2}{\theta^3} + \frac{6\pi}{\theta^2} - \frac{1}{\theta}}}{\pi \sqrt{-8\pi^3 + 12\pi^2\theta - 6\pi\theta^2 + \theta^3}} \right\}, \left\{ r \rightarrow \frac{1080 \sqrt{-\frac{8\pi^2}{\theta^3} + \frac{6\pi}{\theta^2} - \frac{1}{\theta}}}{\pi \sqrt{-8\pi^3 + 12\pi^2\theta - 6\pi\theta^2 + \theta^3}} \right\} \right\}$$

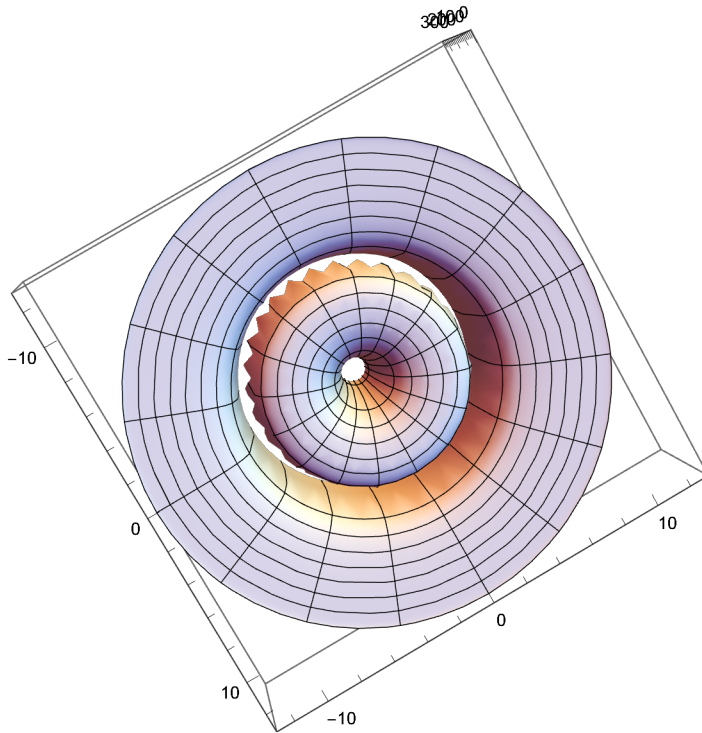
$$\text{Plot}\left[\frac{1080 \sqrt{-\frac{8\pi^2}{\theta^3} + \frac{6\pi}{\theta^2} - \frac{1}{\theta}}}{\pi \sqrt{-8\pi^3 + 12\pi^2\theta - 6\pi\theta^2 + \theta^3}}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{1080 \sqrt{-\frac{8 \pi^2}{\theta^3} + \frac{6 \pi}{\theta^2} - \frac{1}{\theta}}}{\pi \sqrt{-8 \pi^3 + 12 \pi^2 \theta - 6 \pi \theta^2 + \theta^3}}, \{\theta, -13, 13\}\right]$$



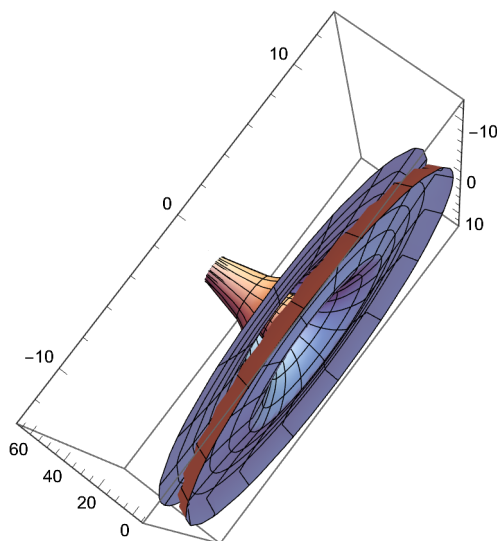
RevolutionPlot3D $\left[\frac{1080 \sqrt{-\frac{8 \pi^2}{\theta^3} + \frac{6 \pi}{\theta^2} - \frac{1}{\theta}}}{\pi \sqrt{-8 \pi^3 + 12 \pi^2 \theta - 6 \pi \theta^2 + \theta^3}}, \{\theta, -13, 13\}\right]$



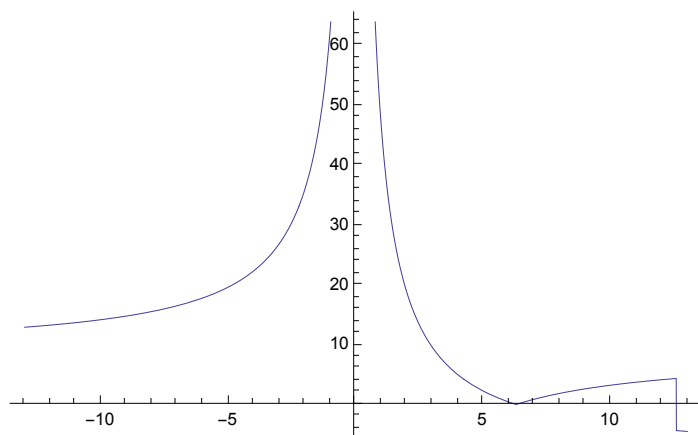
Solve $\left[D\left[\frac{135 \sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \theta\right] == D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right], \theta\right]$

$\left\{\left\{\theta \rightarrow \text{Root}\left[-4665600 \pi + 1166400 \sqrt{1} + 4 \pi^4 r^2 \sqrt{1^3} - 4 \pi^3 r^2 \sqrt{1^4} + \pi^2 r^2 \sqrt{1^5} \&, 1\right]\right\},\right.$   
 $\left\{\theta \rightarrow \text{Root}\left[-4665600 \pi + 1166400 \sqrt{1} + 4 \pi^4 r^2 \sqrt{1^3} - 4 \pi^3 r^2 \sqrt{1^4} + \pi^2 r^2 \sqrt{1^5} \&, 2\right]\right\},$   
 $\left\{\theta \rightarrow \text{Root}\left[-4665600 \pi + 1166400 \sqrt{1} + 4 \pi^4 r^2 \sqrt{1^3} - 4 \pi^3 r^2 \sqrt{1^4} + \pi^2 r^2 \sqrt{1^5} \&, 3\right]\right\},$   
 $\left\{\theta \rightarrow \text{Root}\left[-4665600 \pi + 1166400 \sqrt{1} + 4 \pi^4 r^2 \sqrt{1^3} - 4 \pi^3 r^2 \sqrt{1^4} + \pi^2 r^2 \sqrt{1^5} \&, 4\right]\right\},$   
 $\left.\left\{\theta \rightarrow \text{Root}\left[-4665600 \pi + 1166400 \sqrt{1} + 4 \pi^4 r^2 \sqrt{1^3} - 4 \pi^3 r^2 \sqrt{1^4} + \pi^2 r^2 \sqrt{1^5} \&, 5\right]\right\}\right\}$

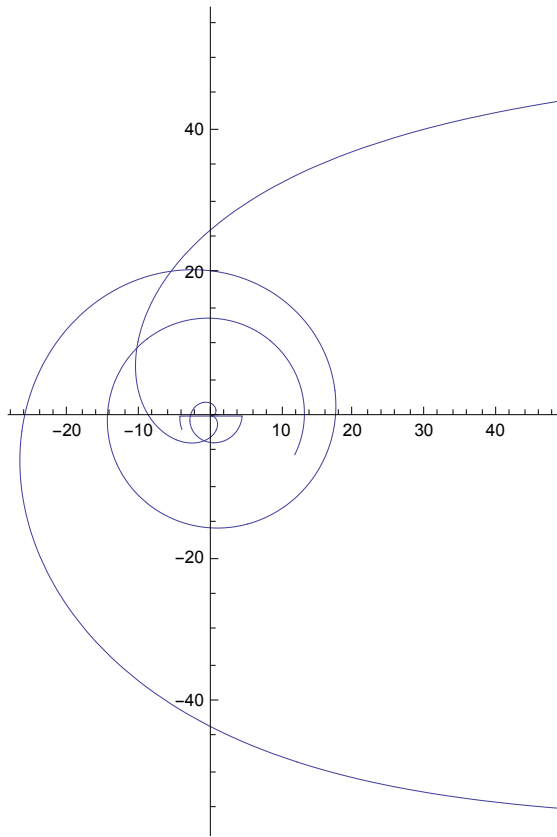
$\text{RevolutionPlot3D}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$



$\text{Plot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$

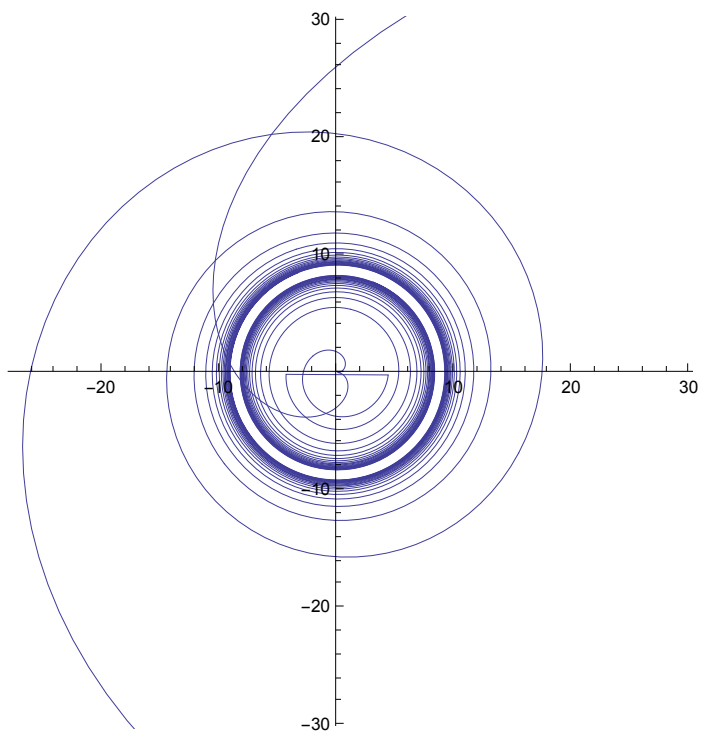


PolarPlot $\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$

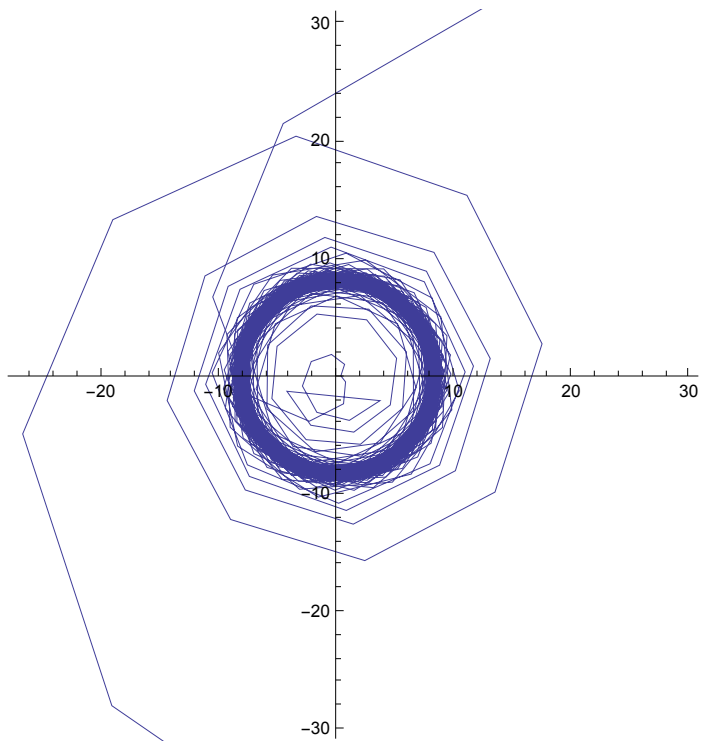




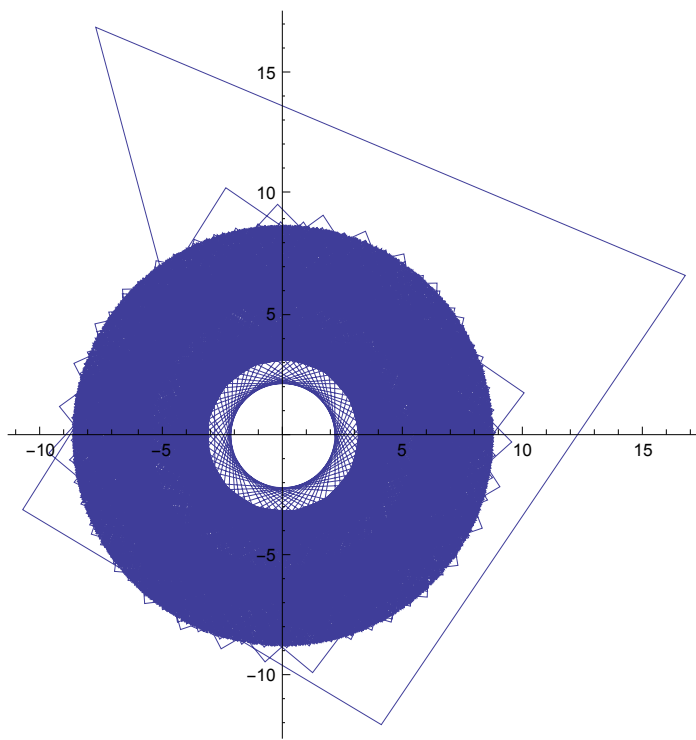
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -130, 130\}\right]$$



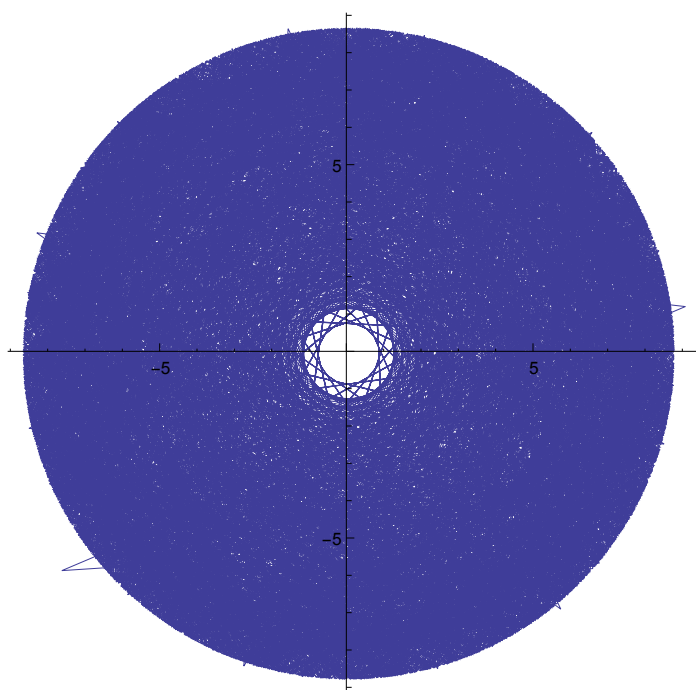
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -1300, 1300\}\right]$$

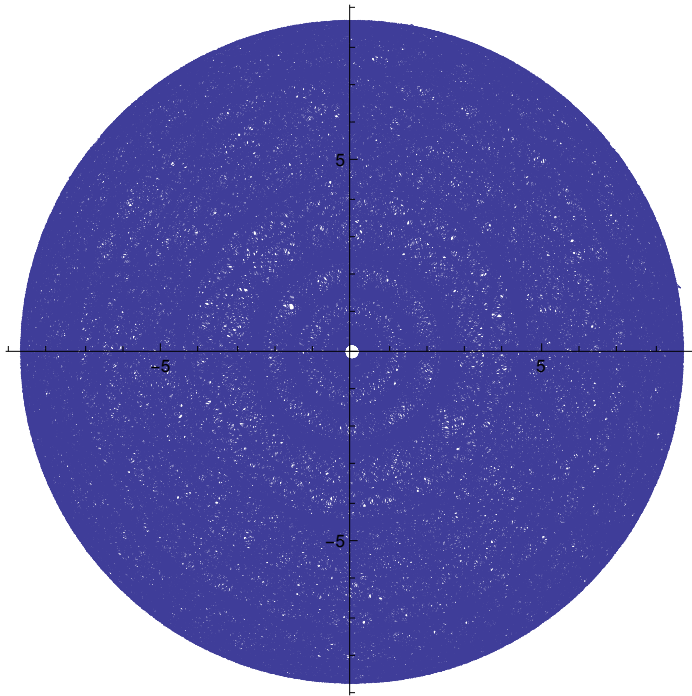


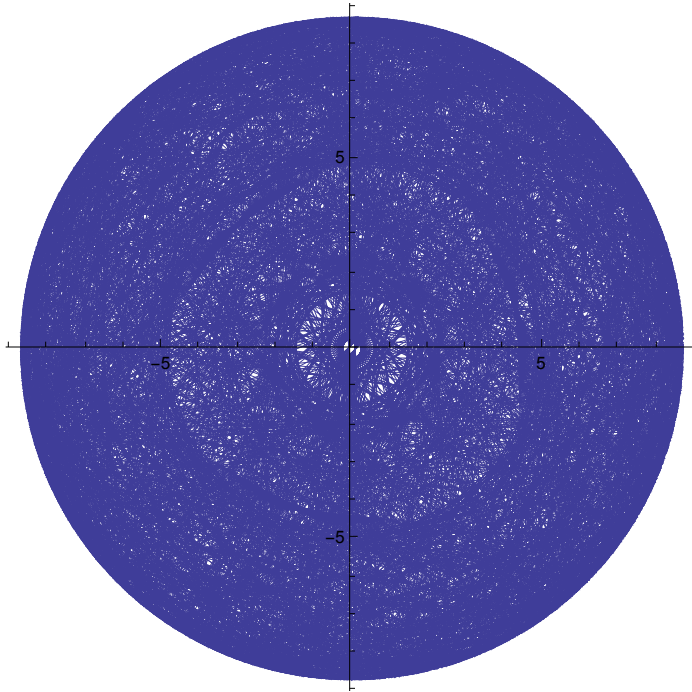
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13000, 13000\}\right]$$



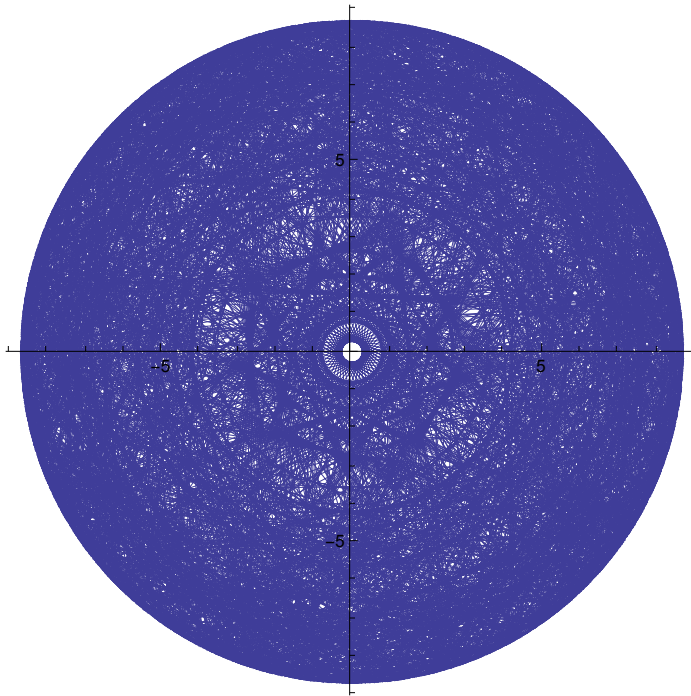
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -130000, 130000\}\right]$$



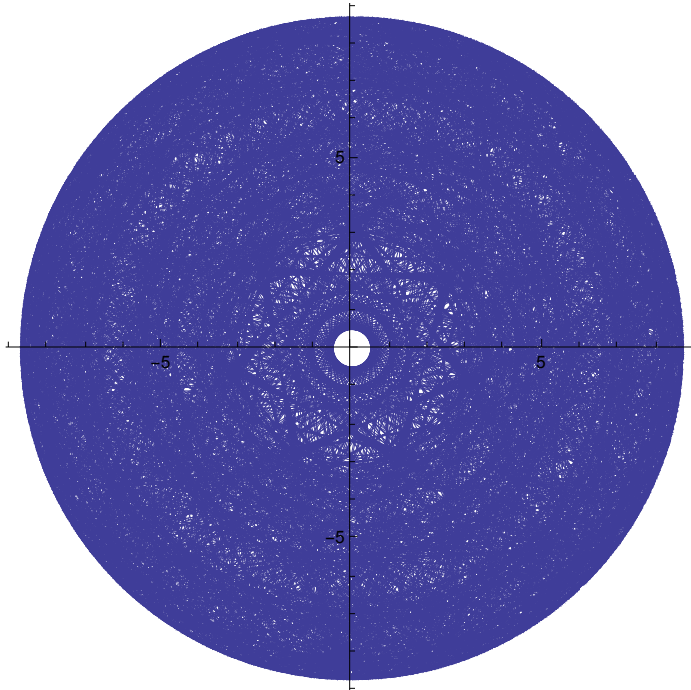
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -1300000, 1300000\}\right]$$


$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13000000, 13000000\}\right]$$


PolarPlot $\left[\frac{135 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}} \sqrt{4 \pi \theta-\theta^2}}{\pi^3 \sqrt{\theta}},\{\theta,-130000000,130000000\}\right]$



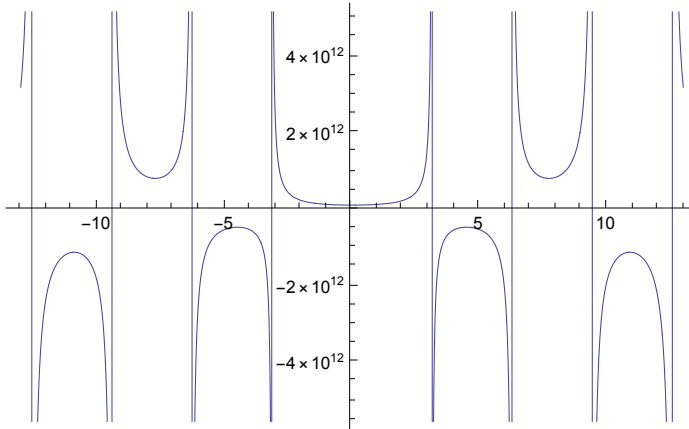
PolarPlot $\left[\frac{135 \sqrt{\frac{1}{4 \pi-\theta}+\frac{4 \pi}{\theta^2}-\frac{3}{\theta}} \sqrt{4 \pi \theta-\theta^2}}{\pi^3 \sqrt{\theta}},\{\theta,-1300000000,1300000000\}\right]$



$$\text{Solve}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} == \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right\}\right\}$$

$$\text{Plot}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}, \{\theta, -13, 13\}\right]$$



## Special Case 1, $\theta = \beta$

Some velocity, which is the first derivative of the equation for  $\theta r$ , is the angular velocity, and is equal to a wavelength of frequency. Some velocity, which is the first derivative of  $r$  is the transitional velocity, and is equal to a the distance,  $r$  being a wavelength,

$$\left\{\left\{r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}\right\}$$

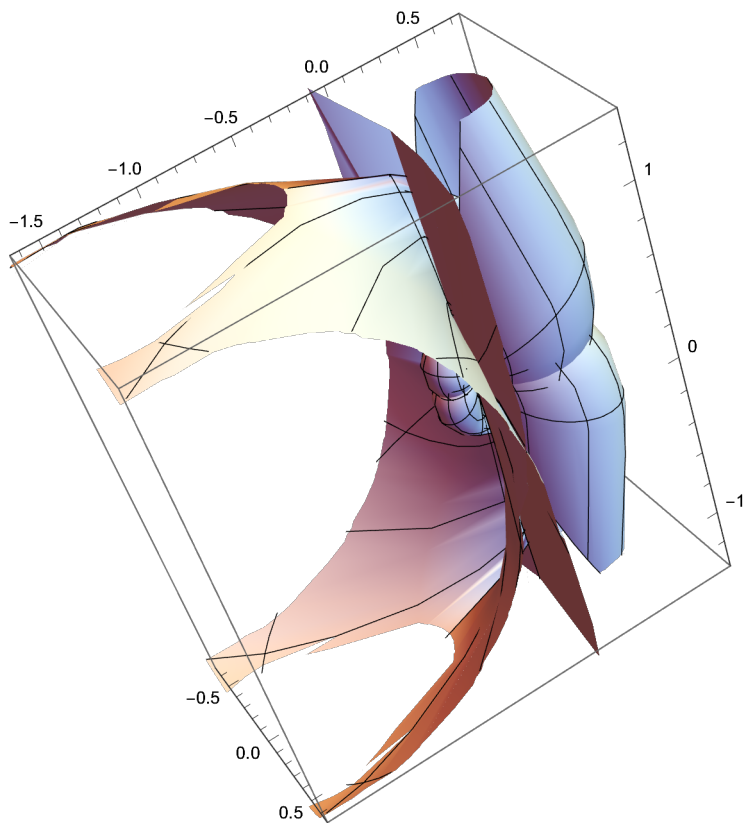
$$\eta = r \sin[\beta]$$

$$r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

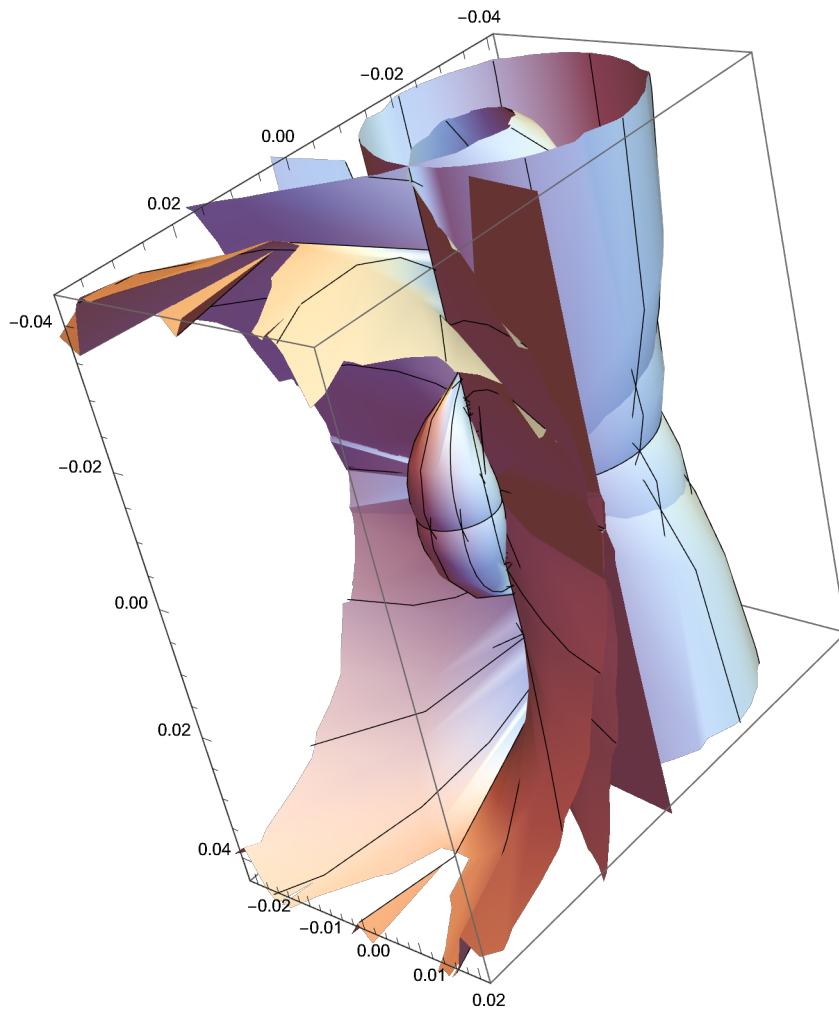
$$\left\{\left\{r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}\right\}, \left\{r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}\right\}\right\}$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}}\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$



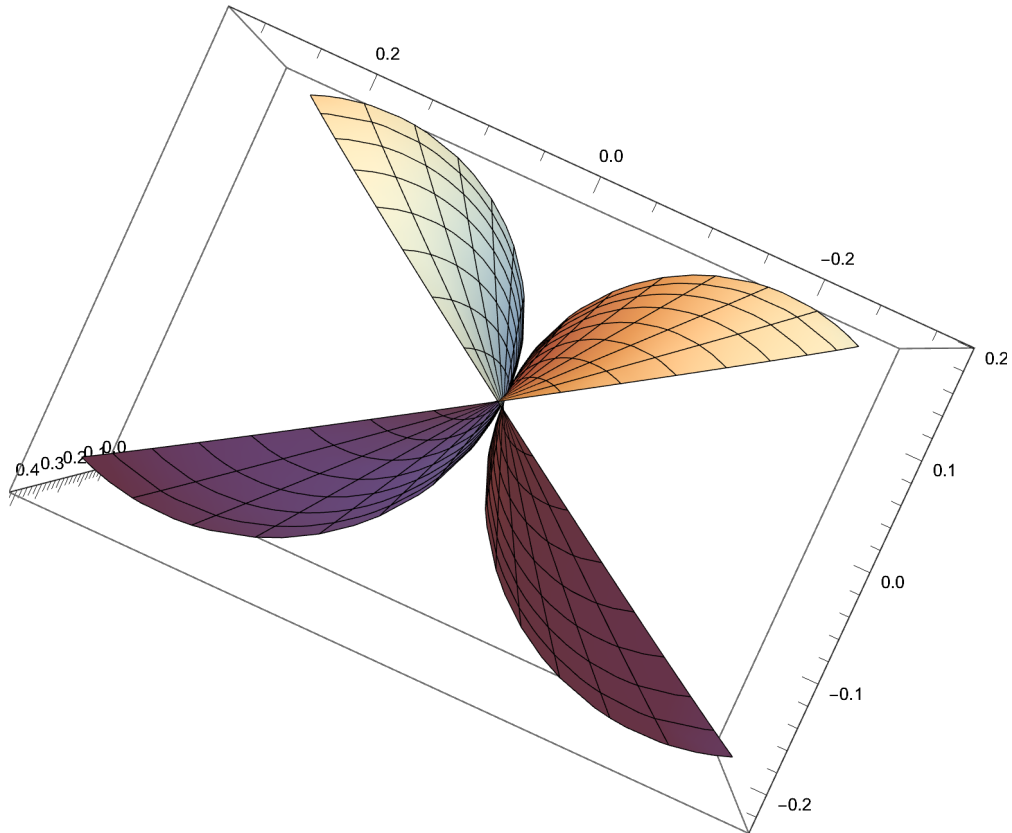
$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi - 3}{\theta^2}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$





SphericalPlot3D[

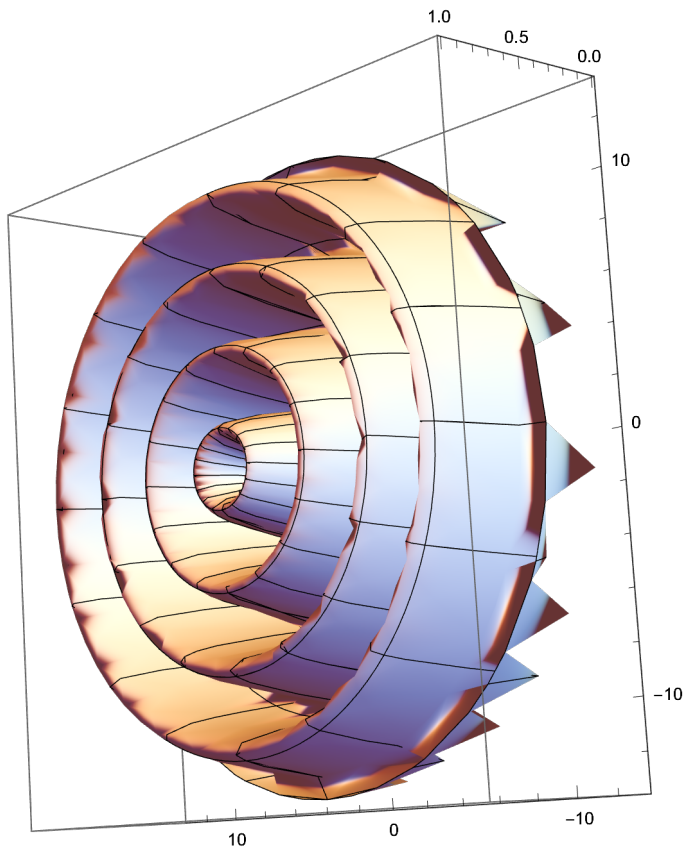
$$\sqrt{4 \pi \left( \frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2} \quad , \{\theta, -1, 1\}, \{\beta, -1, 1\}]$$



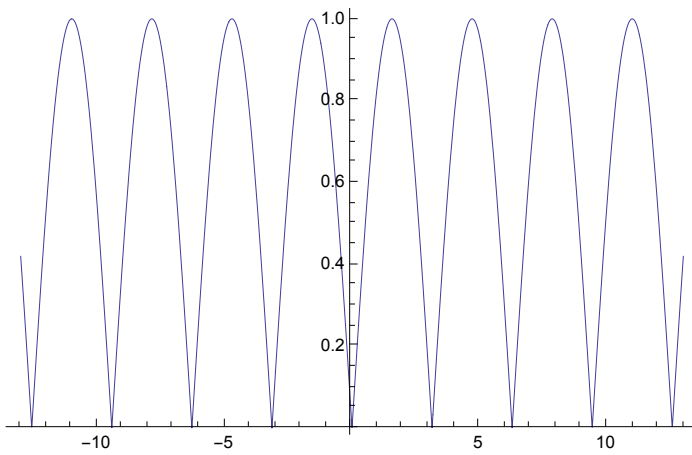
$$\frac{\sqrt{4 \pi \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}}{2 \pi} =$$

$$\frac{\sqrt{4 \pi \left( \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}}{2 \pi} = \frac{\sqrt{4 \pi \left( \frac{2 \pi (r) \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi (r) \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}}{2 \pi}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-13,13\}\right]$$



$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-13,13\}\right]$$



$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} = \left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right), \theta\right]$$

$$\left\{\{\theta \rightarrow 2\pi\},\right.$$

$$\left\{\theta \rightarrow -\left(\frac{2}{1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}}\right)^{1/3} + \frac{\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{12\pi^2}\right\},$$

$$\left\{\theta \rightarrow -\frac{(1+i\sqrt{3})\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{24\pi^2} +$$

$$\frac{1-i\sqrt{3}}{2^{2/3}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)^{1/3}}\right\},$$

$$\left\{\theta \rightarrow -\frac{(1-i\sqrt{3})\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{24\pi^2} +$$

$$\frac{1+i\sqrt{3}}{2^{2/3}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)^{1/3}}\right\}\}$$

$$\sqrt{\frac{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\theta - \left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}{2\pi}} =$$

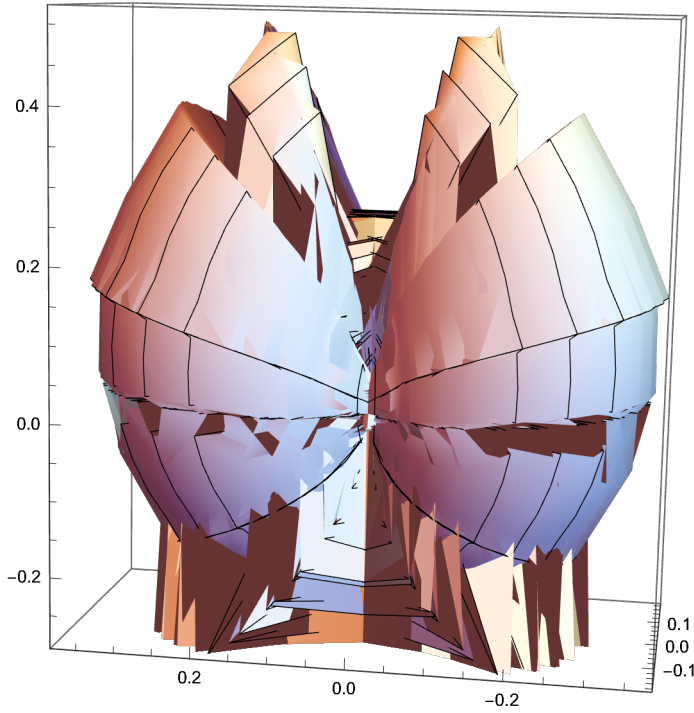
$$r = \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}$$

$$\left\{\left\{r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right\}, \left\{r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right\}\right\}$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}{2\pi},$$

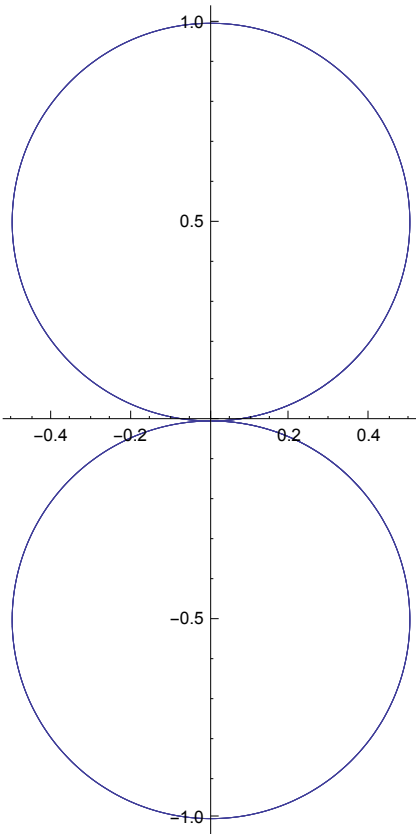
$\{\theta, -360, 360\}, \{\beta, -360, 360\}\right]$



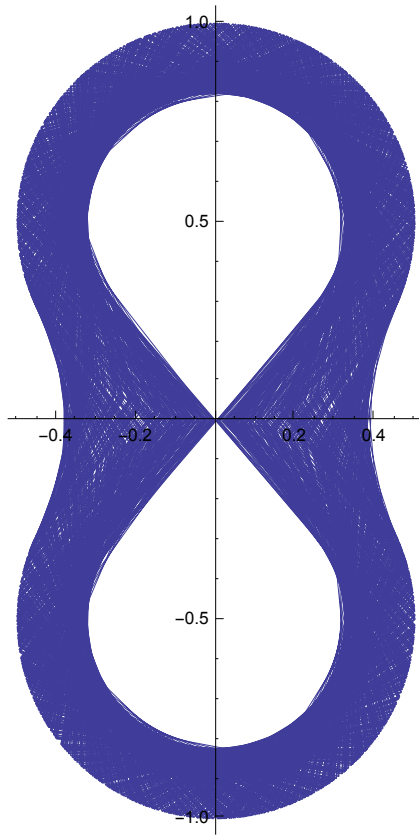
$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}{2\pi},$$

$\{\theta, -360, 360\}, \{\beta, -360, 360\}\right]$

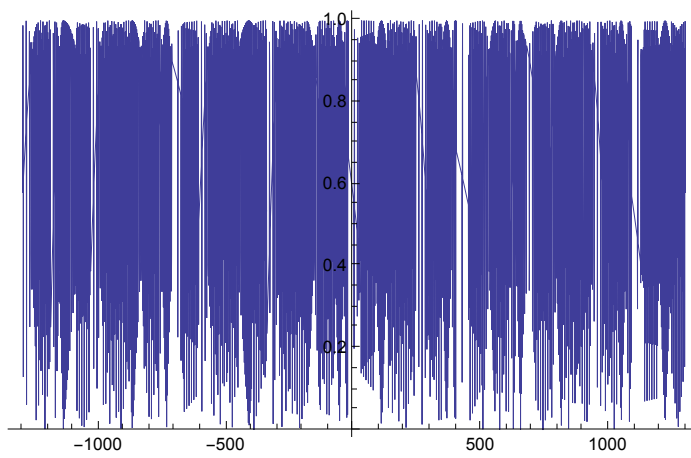
PolarPlot[ $\frac{\sqrt{4 \pi \left(\frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 \theta - \left(\frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}\right)^2 \theta^2}}{2 \pi}, \{\theta, -13, 13\}$ ]



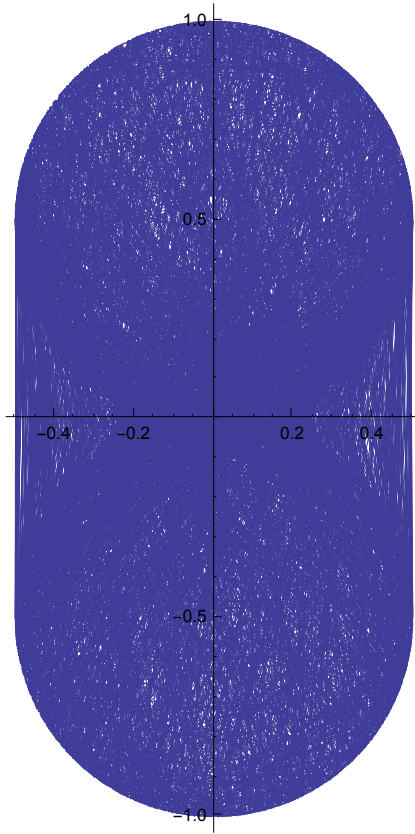
$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-1300,1300\}\right]$$



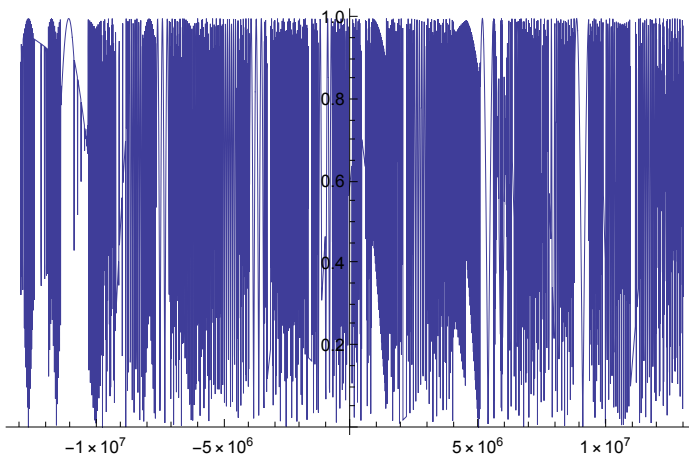
$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-1300,1300\}\right]$$



$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi}, \{\theta, -13\,000\,000, 13\,000\,000\}\right]$$



$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi}, \{\theta, -13\,000\,000, 13\,000\,000\}\right]$$



Contour is said to be the experience of this kind of polar equation from information available in light. Light is interpreted in the polar coordinate system by a human being when perception occurs. How it is

interpreted depends partially on how you see something. For instance, I can see this graphed contour like a cylinder or two spheres. We call this a conisphinder. It's holographic characteristic is the first special case.

$$c := (2.99792458 * 10^8)$$

Depending on the conversion I will decide to use for exchanging angle involved in folding up the circle into a cone and the time that has passed, I will find different solutions and options regarding the system.

First, we will use the following conversion

$$\eta := \text{rate} * \text{time} = c * \tau = \text{height of cone} \quad (122)$$

$\tau := 6 (\theta_{\text{degrees}}) = 6 ((180 / \pi) \theta)$ , because if theta were in radians to begin with, we would have to convert that number of radians to degrees. This way, both our thetas are in radians, but our result accounts for the constant of the degrees involved in measuring time.

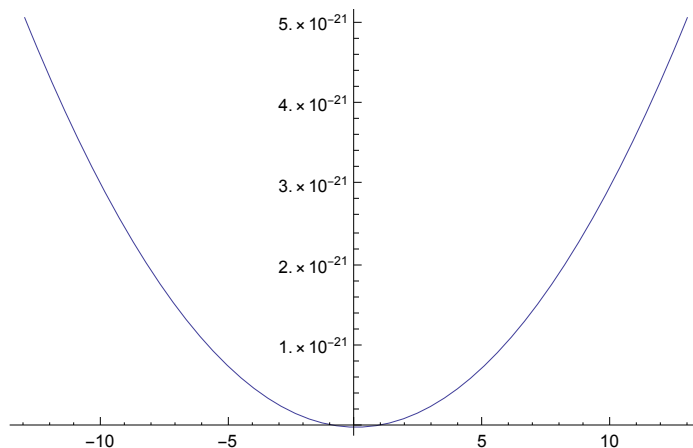
$$(180 / \pi)$$

$$r = \frac{2 * c * \tau * \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 * c * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}$$

$$\text{Solve}\left[r == \frac{2 * c * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{4 \pi r^2}{4 665 600 c^2 + r^2}\right\}\right\}$$

$$\text{Plot}\left[\frac{4 \pi r^2}{4 665 600 c^2 + r^2}, \{r, -13, 13\}\right]$$

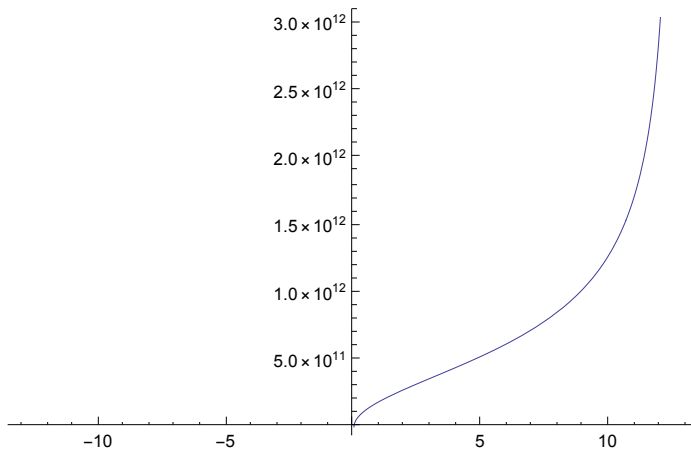




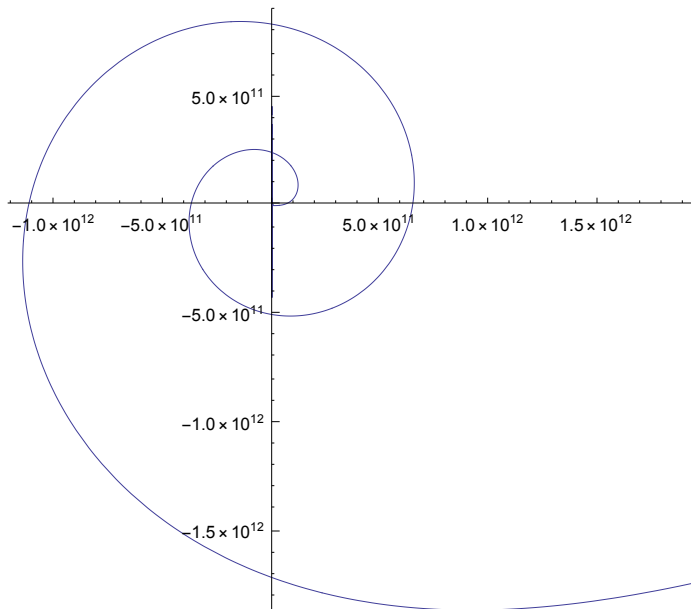
$$\text{Solve}\left[\theta == \frac{4 \pi r^2}{4665600 c^2 + r^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}, \left\{r \rightarrow \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}\right\}$$

$$\text{Plot}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}, \{\theta, -13, 13\}\right]$$



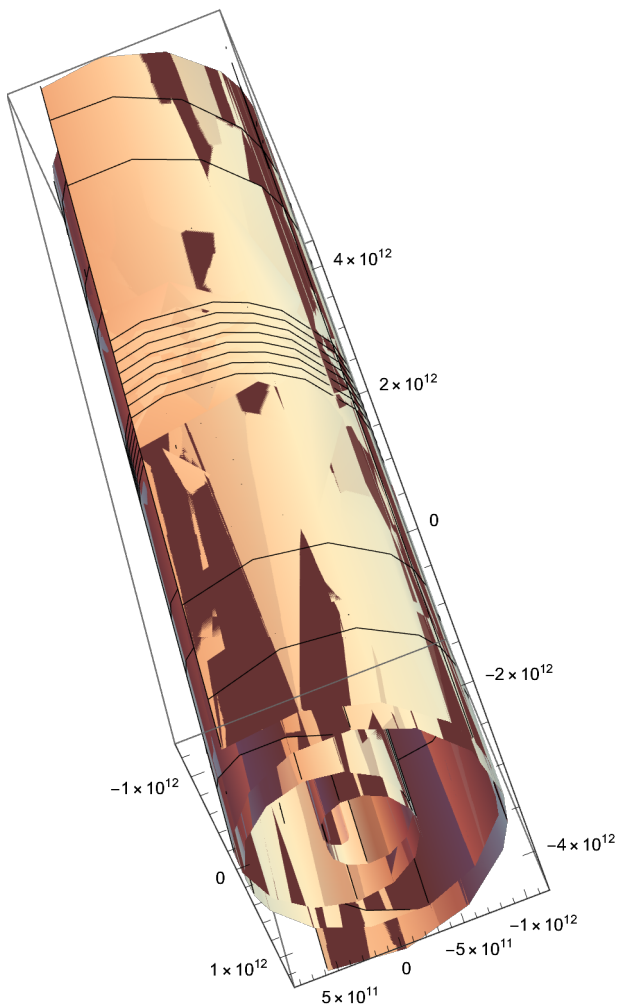
$$r := \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}; \eta = r \text{Sin}[\theta]$$

$$\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}$$

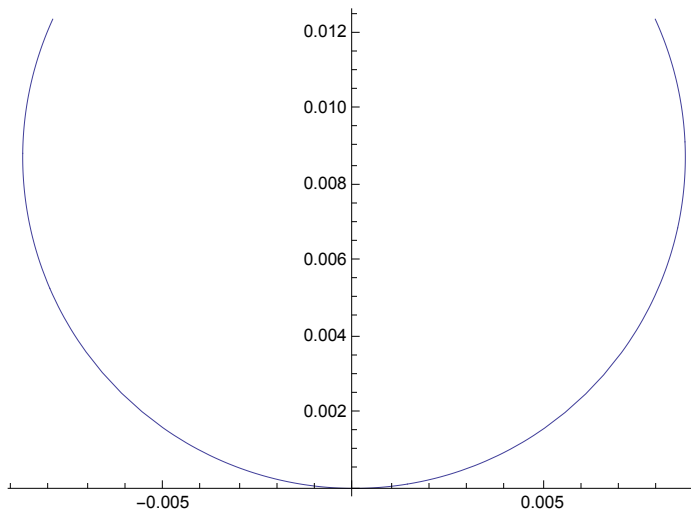
$$\text{Solve}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} == \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, r\right]$$

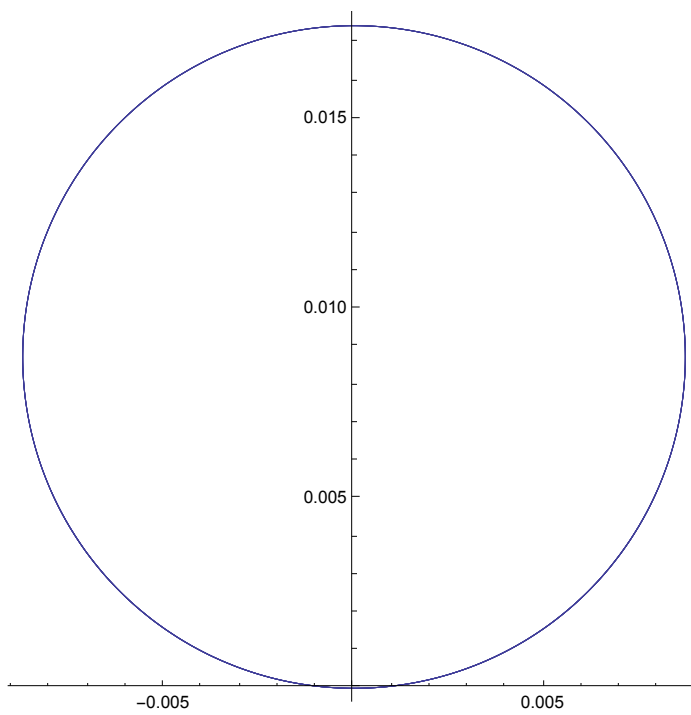
$$\left\{\left\{r \rightarrow \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\beta]}{\pi \sqrt{4 \pi - \theta}}\right\}\right\}$$

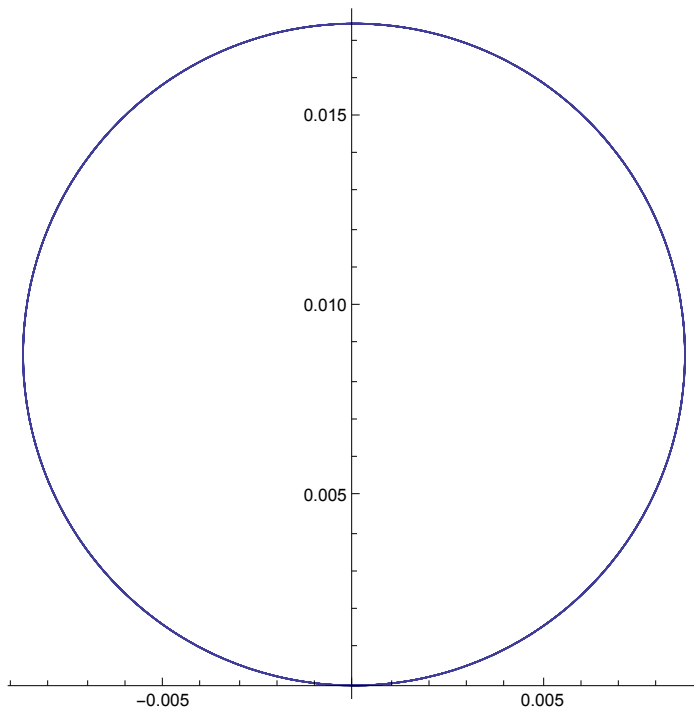
$$\text{SphericalPlot3D}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\beta]}{\pi \sqrt{4 \pi - \theta}}, \{\beta, -13, 13\}, \{\theta, -13, 13\}\right]$$

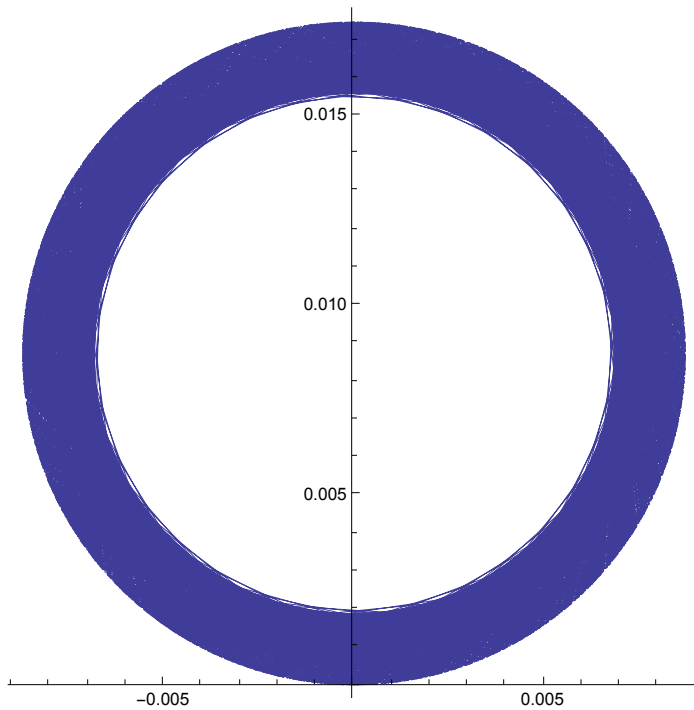


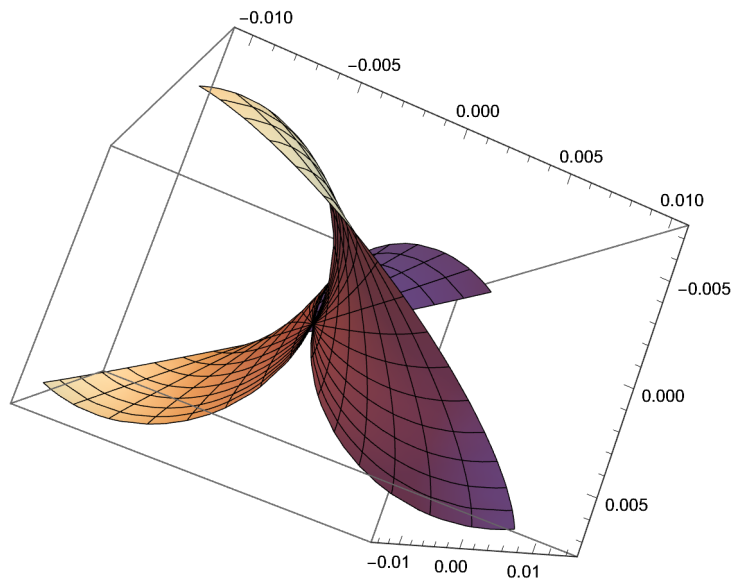
$$\left\{\left\{n \rightarrow \frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}\right\}\right\}$$

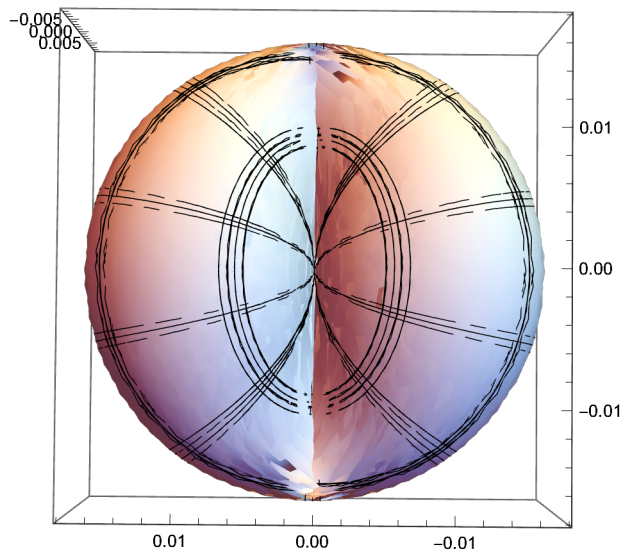
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1, 1\}\right]$$


$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10, 10\}\right]$$


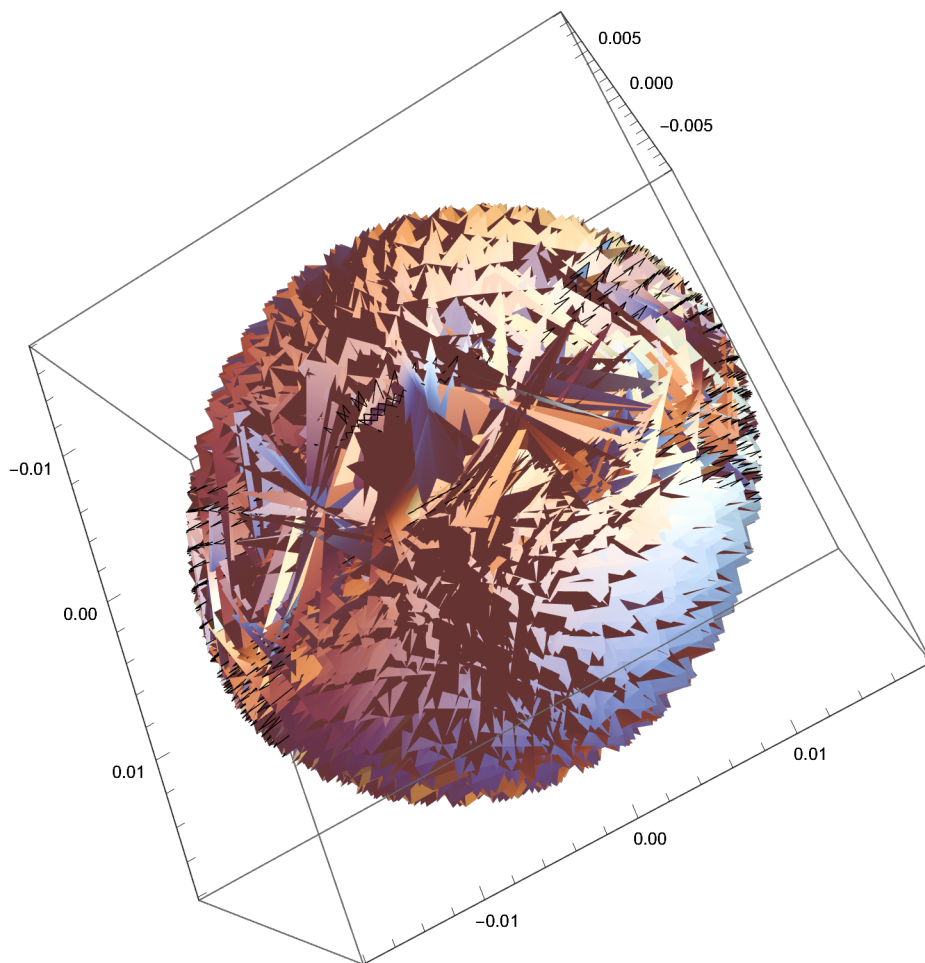
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -100, 100\}\right]$$


$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1000, 1000\}\right]$$


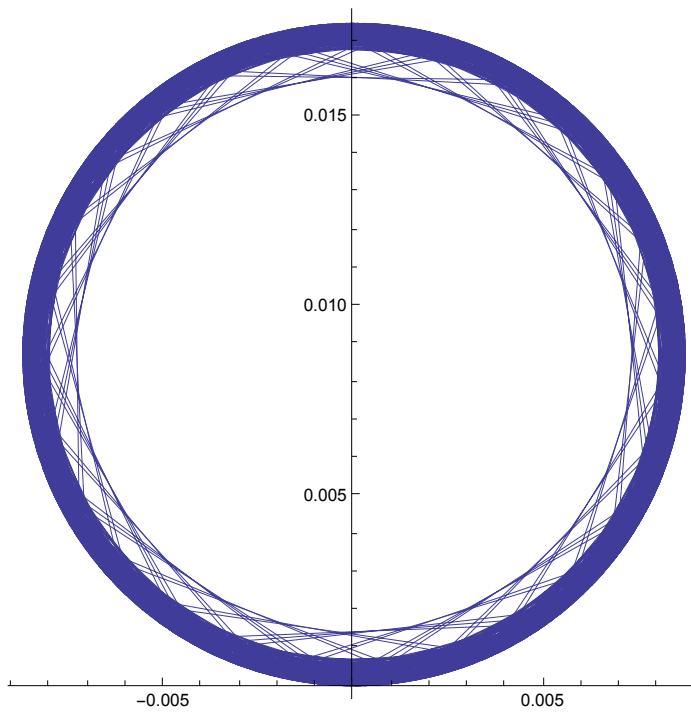
$$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1, 1\}, \{\beta, -1, 1\}\right]$$


$$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10, 10\}, \{\beta, -10, 10\}\right]$$


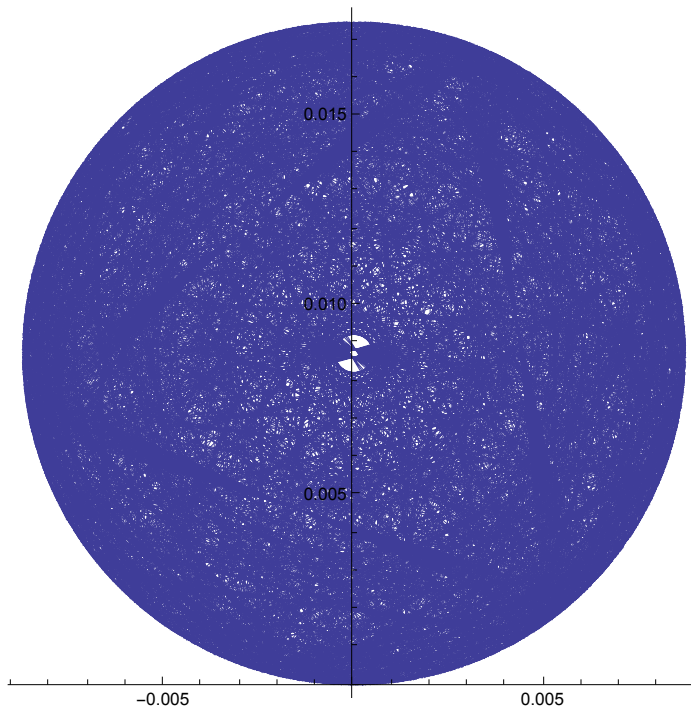
`SphericalPlot3D` $\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -100, 100\}, \{\beta, -100, 100\}\right]$

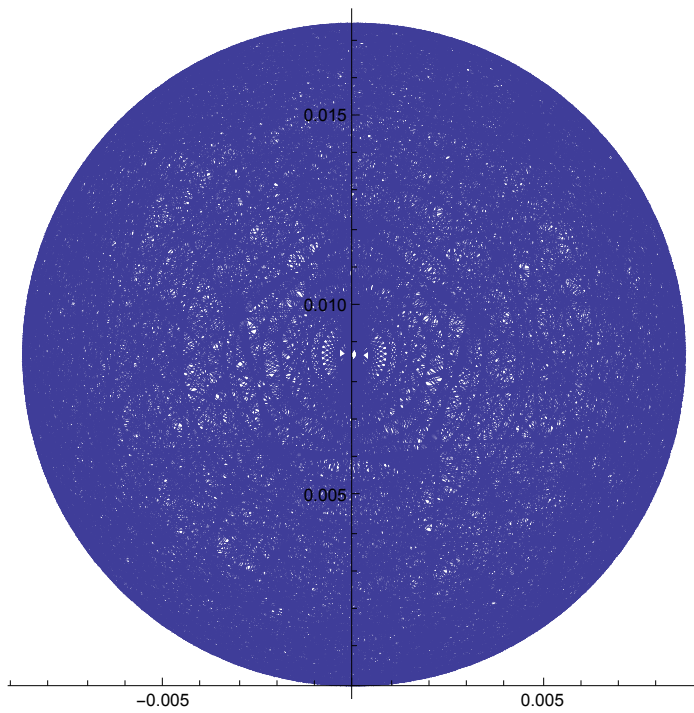


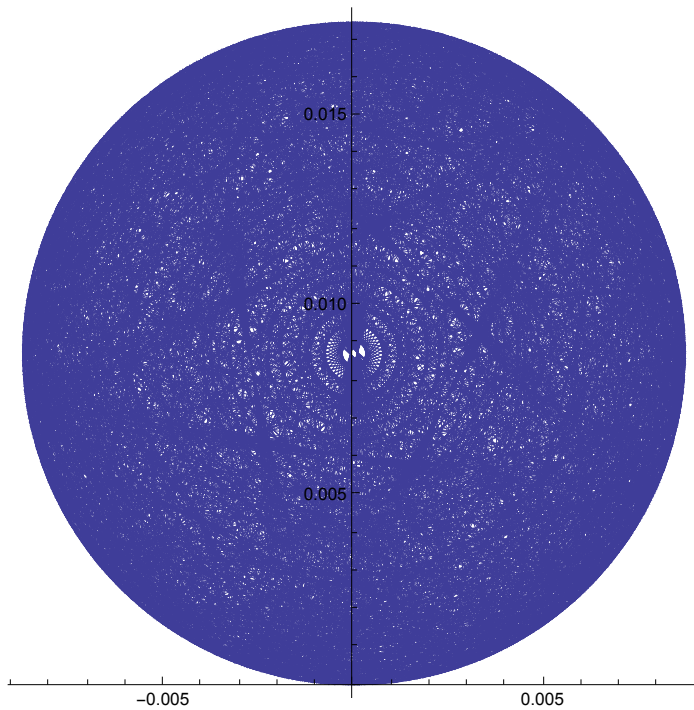
$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10\,000, 10\,000\}\right]$



$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -100\,000, 100\,000\}\right]$

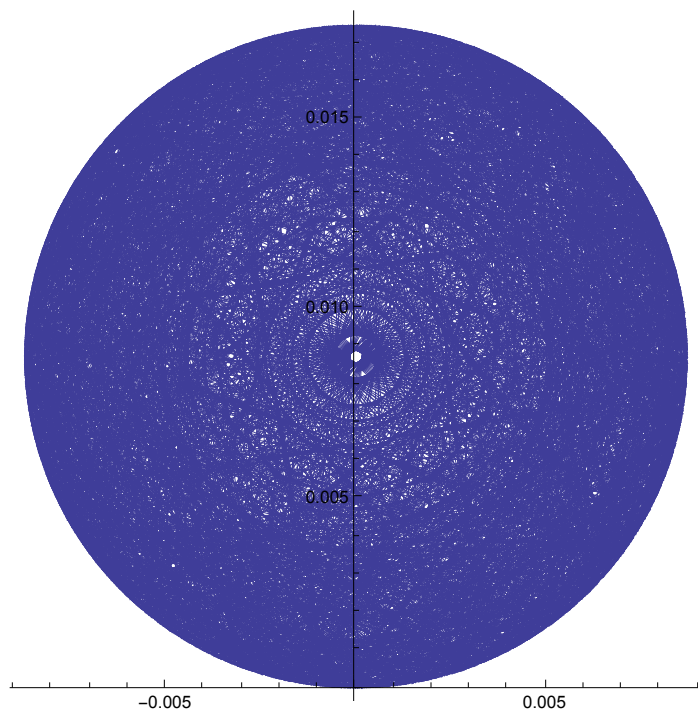


$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1\,000\,000, 1\,000\,000\}\right]$$


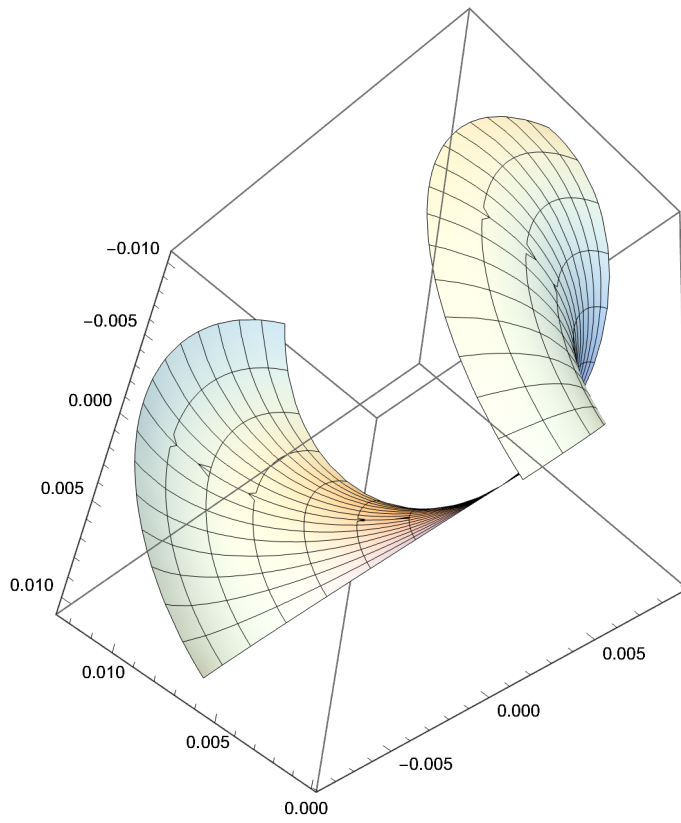
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10\,000\,000, 10\,000\,000\}\right]$$




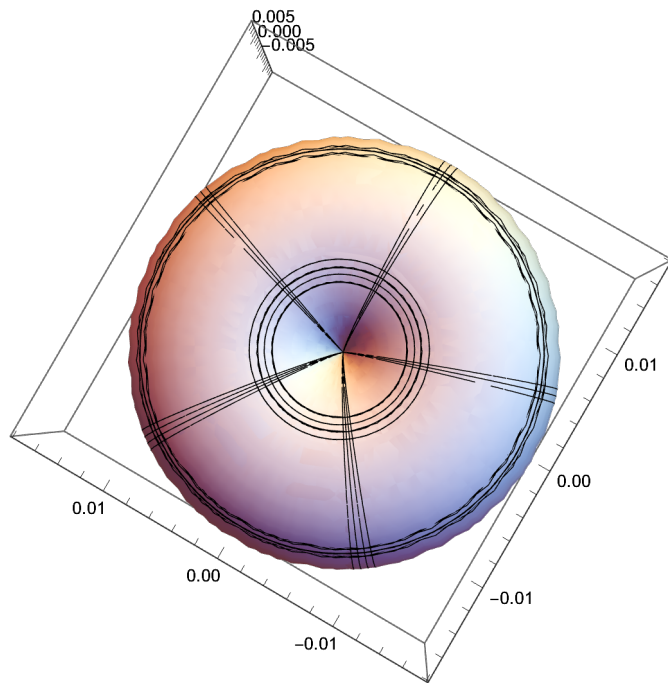
`PolarPlot` $\left[\frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}, \{\theta, -100\,000\,000, 100\,000\,000\}\right]$



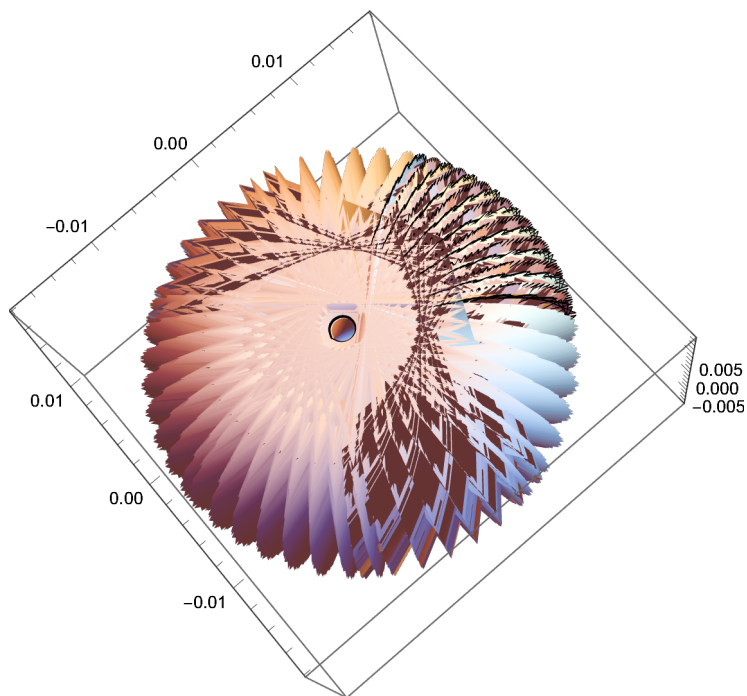
`SphericalPlot3D` $\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -1, 1\}, \{\theta, -1, 1\}\right]$



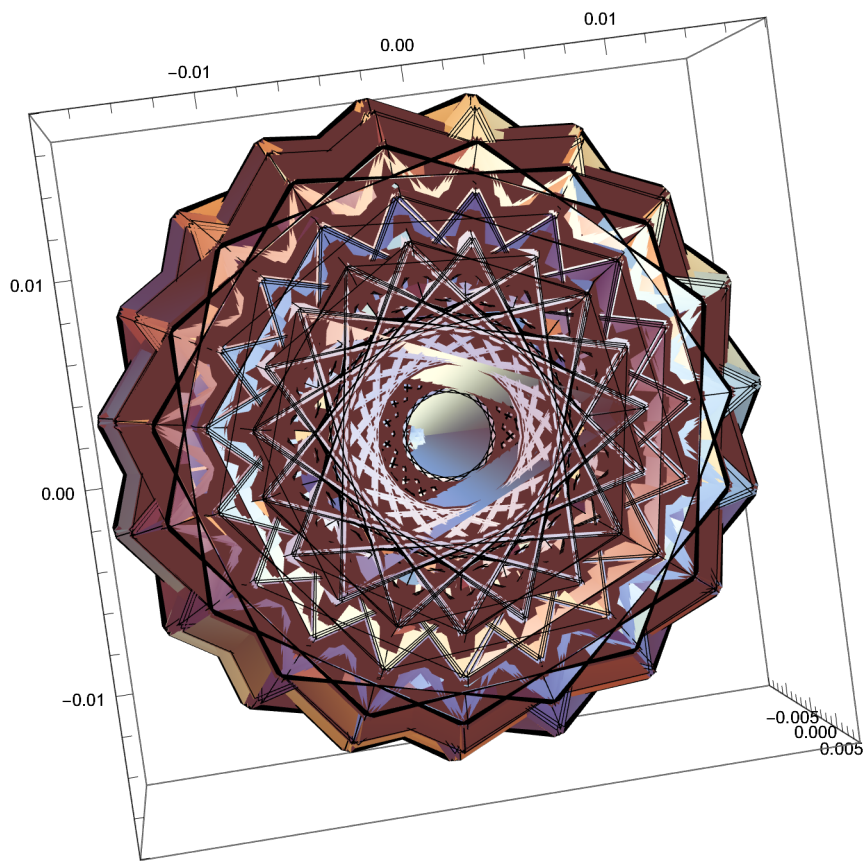
$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -10, 10\}, \{\theta, -10, 10\}\right]$



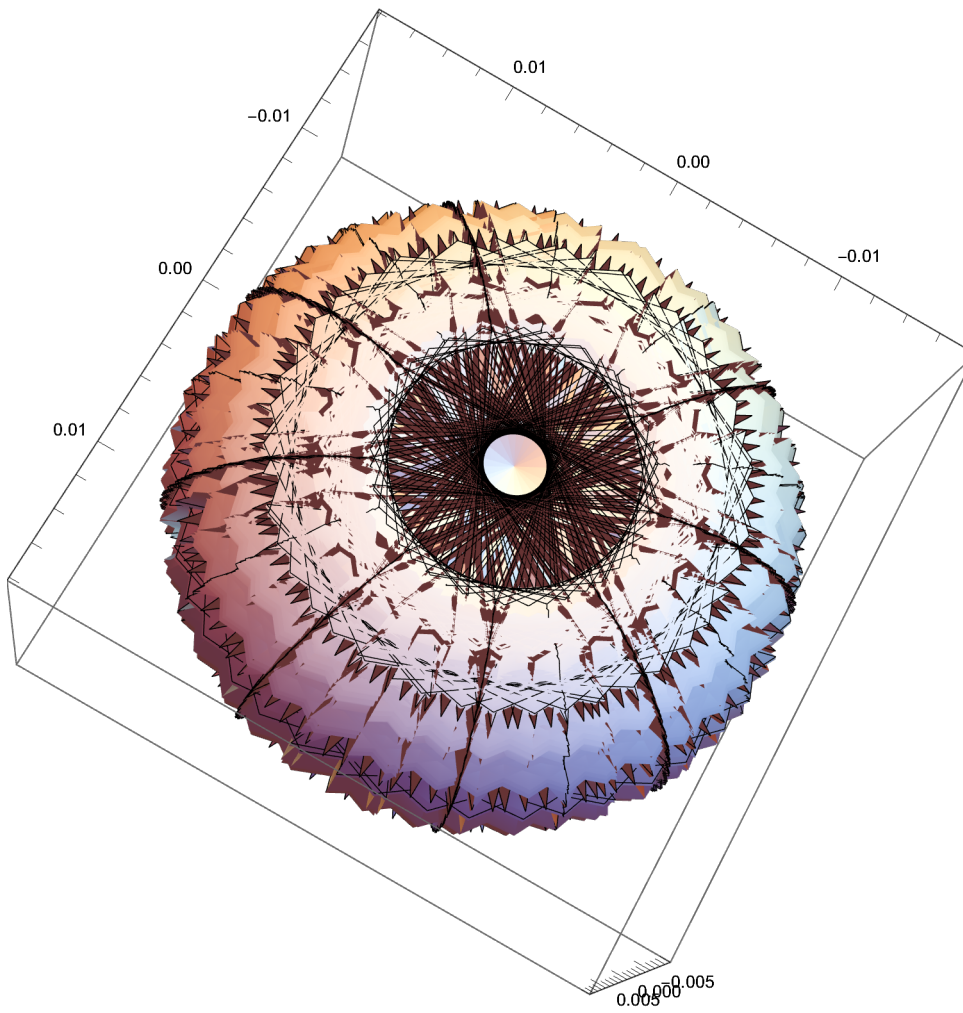
$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -100, 100\}, \{\theta, -100, 100\}\right]$



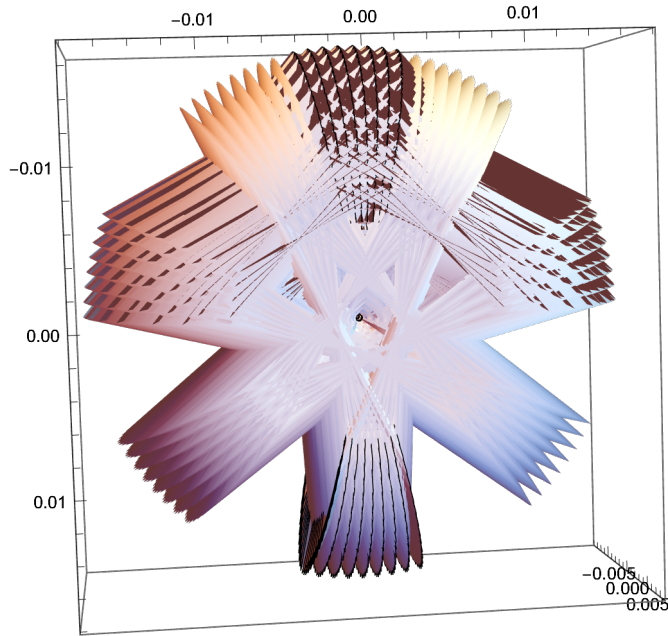
`SphericalPlot3D` $\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -1000, 1000\}, \{\theta, -1000, 1000\}\right]$



`SphericalPlot3D` $\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -10\,000, 10\,000\}, \{\theta, -10\,000, 10\,000\}\right]$



SphericalPlot3D $\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{ \beta, -100\,000\,000, 100\,000\,000 \}, \{ \theta, -100\,000\,000, 100\,000\,000 \} \right]$



Solve $\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) = \sqrt{-\frac{4 c^2 \pi \left(\frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}}\right)^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta}}, r\right]$

$\left\{\left\{r \rightarrow -0.5 \sqrt{\left(-\left(2 \cdot \theta \left(-2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + 2.23792 \times 10^{53} \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4\right)\right) / \left(1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4\right) - 2 \cdot \sqrt{\left(-\left(4 \cdot \theta^2 \left(6.35238 \times 10^{72} \theta^2 - 1.01101 \times 10^{72} \theta^3 + 4.02269 \times 10^{70} \theta^4 - 3.99132 \times 10^{73} \theta \sin[\beta]^2 + 3.17619 \times 10^{72} \theta^2 \sin[\beta]^2 + 6.26955 \times 10^{73} \sin[\beta]^4\right)\right)}\right) /$

$$\begin{aligned}
& \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \left. \right) + \\
& \left( \theta^2 \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \\
& 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + 2.23792 \times 10^{53} \\
& \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \left. \right)^2 \Bigg) / \\
& \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \left. \right)^2 \Bigg) \Bigg\}, \\
& \left\{ r \rightarrow 0.5 \sqrt{\left( - \left( 2. \theta \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \right. \right. \\
& 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + \\
& 2.23792 \times 10^{53} \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \left. \right) \Bigg) / \\
& \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \sin[\beta]^4 - \\
& 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \left. \right) - \\
& 2. \sqrt{\left( - \left( 4. \theta^2 \left( 6.35238 \times 10^{72} \theta^2 - 1.01101 \times 10^{72} \theta^3 + 4.02269 \times 10^{70} \theta^4 - 3.99132 \times 10^{73} \right. \right. \right. \\
& \theta \sin[\beta]^2 + 3.17619 \times 10^{72} \theta^2 \sin[\beta]^2 + 6.26955 \times 10^{73} \sin[\beta]^4 \left. \right) \Bigg) / \\
& \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \left. \right) + \\
& \left( \theta^2 \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \\
& 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + 2.23792 \times 10^{53} \\
& \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \left. \right)^2 \Bigg) / \\
& \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \left. \right)^2 \Bigg) \Bigg\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ r \rightarrow -0.5 \sqrt{\left( - \left( 2. \theta \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \right. \right. \\
& \quad 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& \quad 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& \quad 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + \\
& \quad 2.23792 \times 10^{53} \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& \quad \left. \left. \left. 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \right) \right) \right) / \\
& \quad \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& \quad 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& \quad 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + \\
& \quad \left. 1.22567 \times 10^{42} \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \right) + \\
& \quad 2. \sqrt{\left( - \left( 4. \theta^2 \left( 6.35238 \times 10^{72} \theta^2 - 1.01101 \times 10^{72} \theta^3 + 4.02269 \times 10^{70} \theta^4 - 3.99132 \times 10^{73} \right. \right. \right. \\
& \quad \theta \sin[\beta]^2 + 3.17619 \times 10^{72} \theta^2 \sin[\beta]^2 + 6.26955 \times 10^{73} \sin[\beta]^4 \right) \right) / \\
& \quad \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& \quad 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& \quad 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \quad \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \right) + \\
& \quad \left( \theta^2 \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \\
& \quad 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& \quad 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& \quad 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + 2.23792 \times 10^{53} \\
& \quad \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& \quad \left. \left. \left. 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \right) \right)^2 \right) / \\
& \quad \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& \quad 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& \quad 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \quad \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \right)^2 \left. \right\}, \\
& \left\{ r \rightarrow 0.5 \sqrt{\left( - \left( 2. \theta \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \right. \right. \\
& \quad 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& \quad 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& \quad 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + \\
& \quad 2.23792 \times 10^{53} \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& \quad \left. \left. \left. 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \right) \right) \right) / \\
& \quad \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& \quad 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + \\
& \quad 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + \\
& \quad 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \sin[\beta]^4 - \\
& \quad \left. 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \right) + \\
& \quad 2. \sqrt{\left( - \left( 4. \theta^2 \left( 6.35238 \times 10^{72} \theta^2 - 1.01101 \times 10^{72} \theta^3 + 4.02269 \times 10^{70} \theta^4 - 3.99132 \times 10^{73} \right. \right. \right. \\
& \quad \theta \sin[\beta]^2 + 3.17619 \times 10^{72} \theta^2 \sin[\beta]^2 + 6.26955 \times 10^{73} \sin[\beta]^4 \right) \right) / \\
& \quad \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right.
\end{aligned}$$

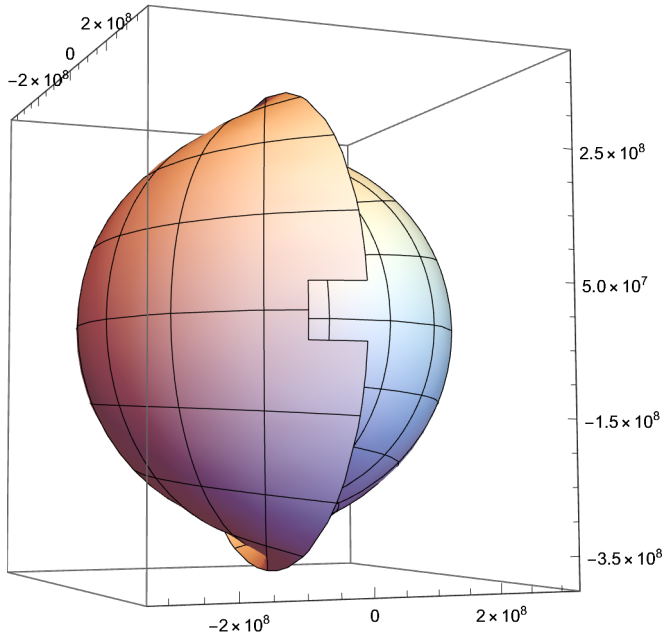


$$\begin{aligned}
& 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4) + \\
& \left( \theta^2 \left( -2.66456 \times 10^{57} \theta^2 + 7.77477 \times 10^{56} \theta^3 - 8.99922 \times 10^{55} \theta^4 + \right. \right. \\
& \quad 5.37102 \times 10^{54} \theta^5 - 1.78088 \times 10^{53} \theta^6 + 2.83436 \times 10^{51} \theta^7 + \\
& \quad 1.67419 \times 10^{58} \theta \sin[\beta]^2 - 3.55275 \times 10^{57} \theta^2 \sin[\beta]^2 + \\
& \quad 2.82719 \times 10^{56} \theta^3 \sin[\beta]^2 - 1.1249 \times 10^{55} \theta^4 \sin[\beta]^2 + 2.23792 \times 10^{53} \\
& \quad \theta^5 \sin[\beta]^2 - 2.62982 \times 10^{58} \sin[\beta]^4 + 3.48791 \times 10^{57} \theta \sin[\beta]^4 - \\
& \quad \left. \left. 1.66535 \times 10^{56} \theta^2 \sin[\beta]^4 + 4.41748 \times 10^{54} \theta^3 \sin[\beta]^4 \right)^2 \right) / \\
& \left( 1.24186 \times 10^{41} \theta^2 - 3.95297 \times 10^{40} \theta^3 + 4.71851 \times 10^{39} \theta^4 - 2.50325 \times 10^{38} \theta^5 + \right. \\
& \quad 4.98005 \times 10^{36} \theta^6 - 7.80285 \times 10^{41} \theta \sin[\beta]^2 + 1.86279 \times 10^{41} \theta^2 \sin[\beta]^2 - \\
& \quad 1.48236 \times 10^{40} \theta^3 \sin[\beta]^2 + 3.93209 \times 10^{38} \theta^4 \sin[\beta]^2 + 1.22567 \times 10^{42} \\
& \quad \left. \left. \sin[\beta]^4 - 1.95071 \times 10^{41} \theta \sin[\beta]^4 + 7.76164 \times 10^{39} \theta^2 \sin[\beta]^4 \right)^2 \right) \Big) \Big\}
\end{aligned}$$

```

SphericalPlot3D[
0.5`√((- (2.`θ (-2.6645634260764098`^57 θ^2 + 7.774771408102173`^56 θ^3 -
8.999224007338156`^55 θ^4 + 5.3710161928467094`^54 θ^5 -
1.78088286774618`^53 θ^6 + 2.8343631146947462`^51 θ^7 +
1.67419457687714`^58 θ Sin[β]^2 - 3.5527512347685464`^57 θ^2 Sin[β]^2 +
2.8271896029462448`^56 θ^3 Sin[β]^2 - 1.1249030009172694`^55 θ^4 Sin[β]^2 +
2.2379234136861288`^53 θ^5 Sin[β]^2 - 2.6298186916985475`^58 Sin[β]^4 +
3.4879053684940414`^57 θ Sin[β]^4 - 1.6653521412977561`^56 θ^2 Sin[β]^4 +
4.4174837546035074`^54 θ^3 Sin[β]^4)) /
(1.2418617932046758`^41 θ^2 - 3.9529688605097853`^40 θ^3 +
4.7185090052885197`^39 θ^4 - 2.5032467740509667`^38 θ^5 +
4.9800512233631525`^36 θ^6 - 7.802847772611313`^41 θ Sin[β]^2 +
1.8627926898070135`^41 θ^2 Sin[β]^2 - 1.4823633226911695`^40 θ^3 Sin[β]^2 +
3.9320908377404326`^38 θ^4 Sin[β]^2 + 1.2256684619757591`^42 Sin[β]^4 -
1.9507119431528282`^41 θ Sin[β]^4 + 7.761636207529224`^39 θ^2 Sin[β]^4) +
2.`√((- (4.`θ^2 (6.3523782422970615`^72 θ^2 - 1.0110123976509831`^72
θ^3 + 4.022690515333572`^70 θ^4 - 3.991316963764819`^73 θ Sin[β]^2 +
3.176189121148531`^72 θ^2 Sin[β]^2 + 6.269546025755937`^73 Sin[β]^4)) /
(1.2418617932046758`^41 θ^2 - 3.9529688605097853`^40 θ^3 +
4.7185090052885197`^39 θ^4 - 2.5032467740509667`^38 θ^5 +
4.9800512233631525`^36 θ^6 - 7.802847772611313`^41 θ Sin[β]^2 +
1.8627926898070135`^41 θ^2 Sin[β]^2 - 1.4823633226911695`^40 θ^3 Sin[β]^2 +
3.9320908377404326`^38 θ^4 Sin[β]^2 + 1.2256684619757591`^42 Sin[β]^4 -
1.9507119431528282`^41 θ Sin[β]^4 + 7.761636207529224`^39 θ^2 Sin[β]^4) +
(θ^2 (-2.6645634260764098`^57 θ^2 + 7.774771408102173`^56 θ^3 -
8.999224007338156`^55 θ^4 + 5.3710161928467094`^54 θ^5 -
1.78088286774618`^53 θ^6 + 2.8343631146947462`^51 θ^7 +
1.67419457687714`^58 θ Sin[β]^2 - 3.5527512347685464`^57
θ^2 Sin[β]^2 + 2.8271896029462448`^56 θ^3 Sin[β]^2 -
1.1249030009172694`^55 θ^4 Sin[β]^2 + 2.2379234136861288`^53
θ^5 Sin[β]^2 - 2.6298186916985475`^58 Sin[β]^4 +
3.4879053684940414`^57 θ Sin[β]^4 - 1.6653521412977561`^56
θ^2 Sin[β]^4 + 4.4174837546035074`^54 θ^3 Sin[β]^4)^2) /
(1.2418617932046758`^41 θ^2 - 3.9529688605097853`^40 θ^3 +
4.7185090052885197`^39 θ^4 - 2.5032467740509667`^38 θ^5 +
4.9800512233631525`^36 θ^6 - 7.802847772611313`^41 θ Sin[β]^2 +
1.8627926898070135`^41 θ^2 Sin[β]^2 - 1.4823633226911695`^40
θ^3 Sin[β]^2 + 3.9320908377404326`^38 θ^4 Sin[β]^2 +
1.2256684619757591`^42 Sin[β]^4 - 1.9507119431528282`^41 θ Sin[β]^4 +
7.761636207529224`^39 θ^2 Sin[β]^4)^2)), {β, -π, π}, {θ, -2 π, 2 π}]

```



A Paper on Leonard Euler's Formula in Natural Scientific Thought

To show that the ideas presented through the ontological cone  
(an analogy to the gestalt of perception through the sense of being),  
are applicable to the Euler equation is the purpose of this section.

$$e^{i\beta} = \cos[\beta] + i \sin[\beta]$$

$$e^{i\theta} = \cos[\theta] + i \sin[\theta]$$

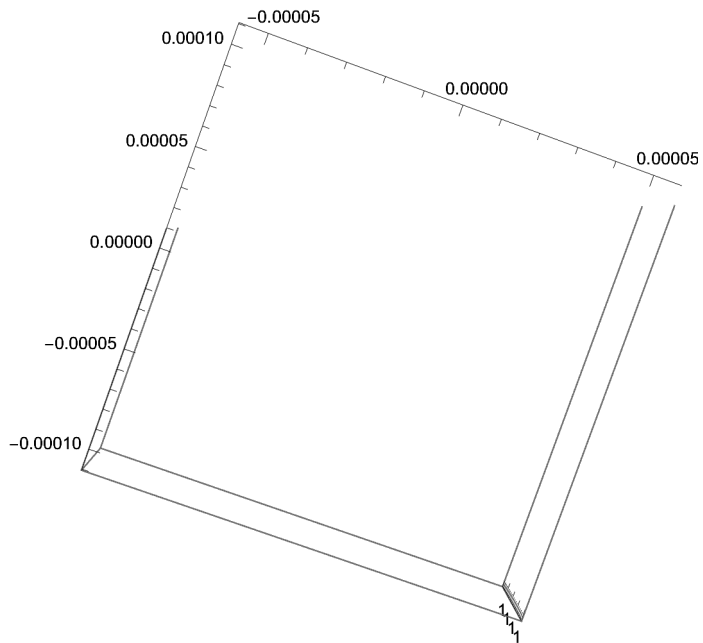
$$\text{RevolutionPlot3D}\left[e^{i\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}, \{\beta, -\pi, \pi\}\right]$$

$$e^{i\theta} = \cos[\theta] + i \sin[\theta]$$

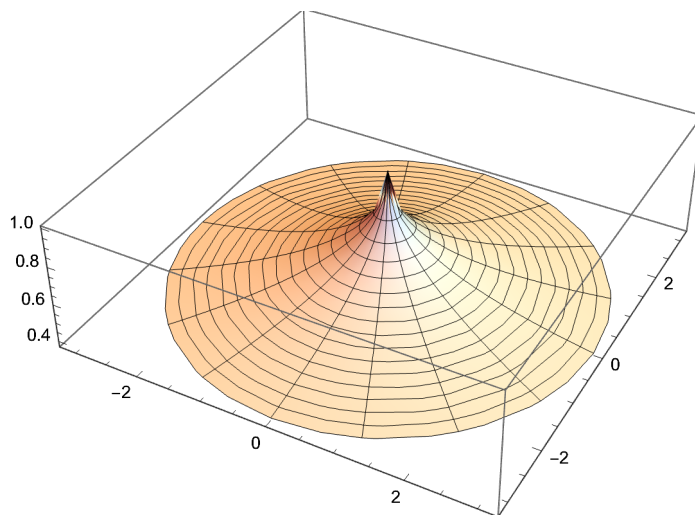
$$\text{RevolutionPlot3D}[\cos[\theta] + i \sin[\theta], \{\beta, -\pi, \pi\}]$$

$$\beta = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

`RevolutionPlot3D[Cos[ $\beta$ ] +  $\mathbf{i}$  Sin[ $\beta$ ], { $\beta$ ,  $-\pi$ ,  $\pi$ }]`

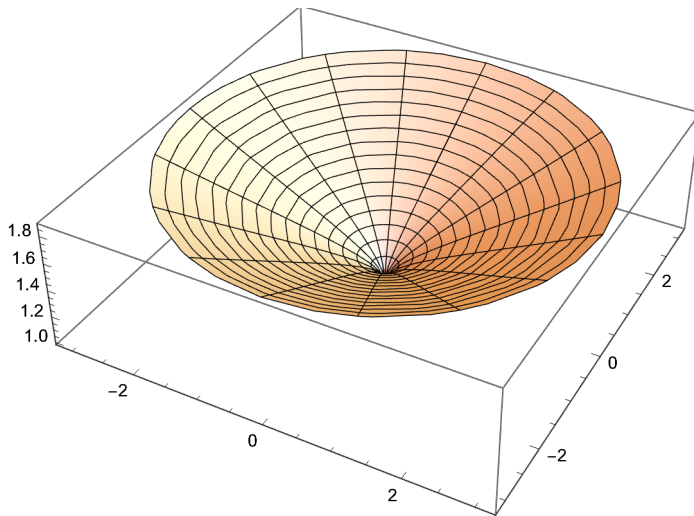


`RevolutionPlot3D[Cos[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ]] +  $\mathbf{i}$  Sin[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ]], { $\theta$ ,  $-\pi$ ,  $\pi$ }]`

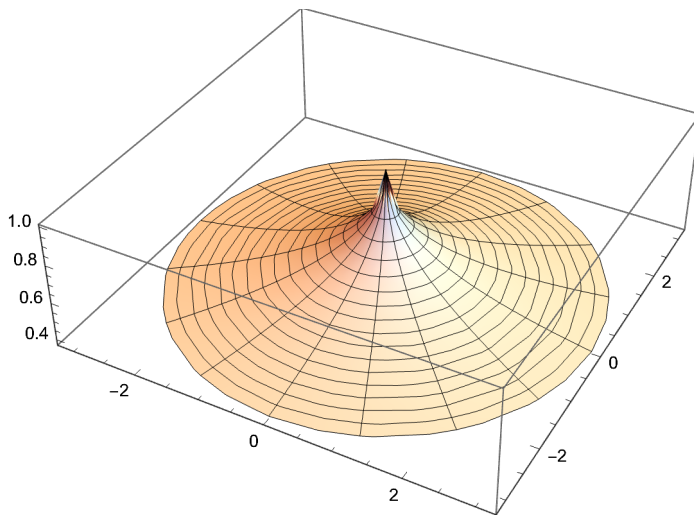


`SphericalPlot3D[Cos[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ]] +  $\mathbf{i}$  Sin[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ]], { $\theta$ ,  $-\pi$ ,  $\pi$ }]`

$$\text{RevolutionPlot3D}\left[e^{\mathbf{i} \left( \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right)}, \{\theta, -\pi, \pi\}\right]$$



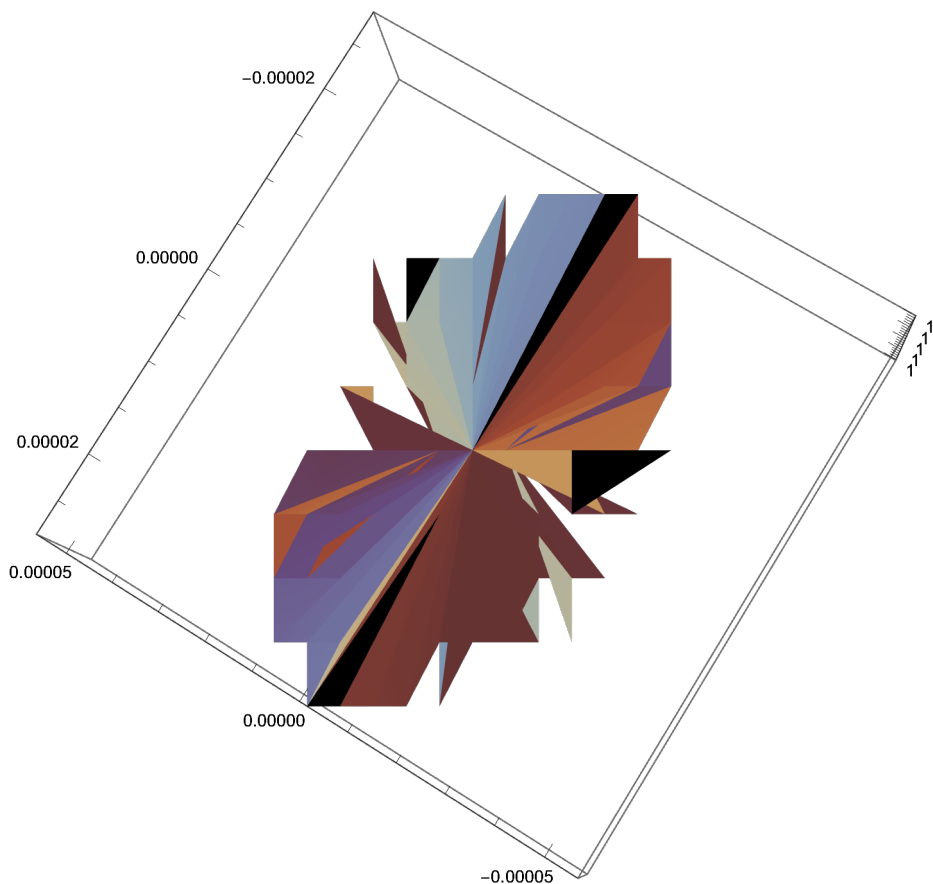
$$\text{RevolutionPlot3D}\left[e^{\mathbf{i} \left( \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right)}, \{\theta, -\pi, \pi\}\right]$$



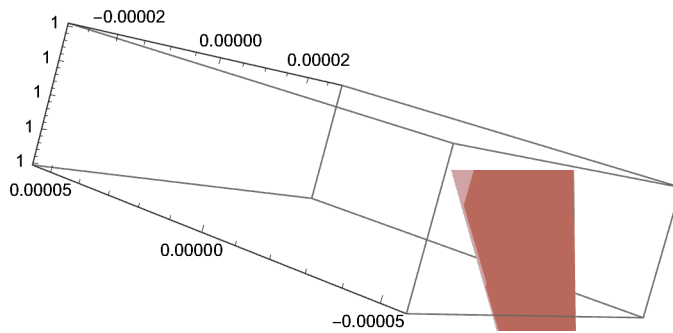
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RevolutionPlot3D[E^(I (4 Pi/3 - (-4 Pi^2 + 12 Pi^2 Sin[beta]^2) /
(6 (-Pi^3 + 18 Pi^3 Sin[beta]^2 + 3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6)^(1/3)) + 2/3
(-Pi^3 + 18 Pi^3 Sin[beta]^2 +
3 Sqrt[3] Sqrt[-Pi^6 Sin[beta]^2 + 11 Pi^6 Sin[beta]^4 + Pi^6 Sin[beta]^6)^(1/3)))]), {beta, -Pi, Pi}]

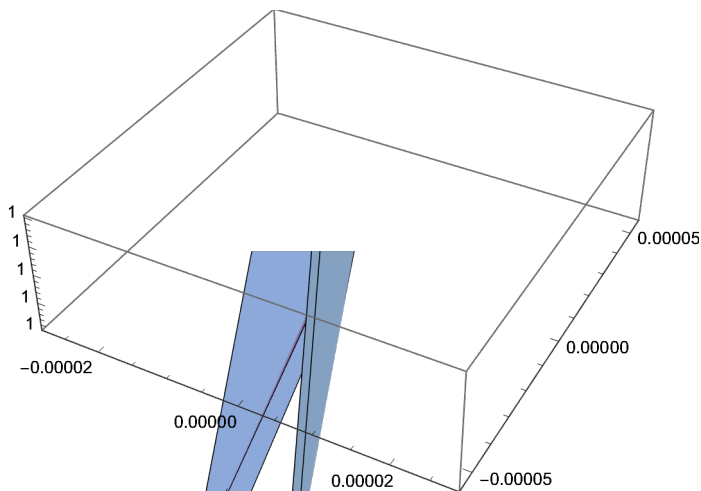
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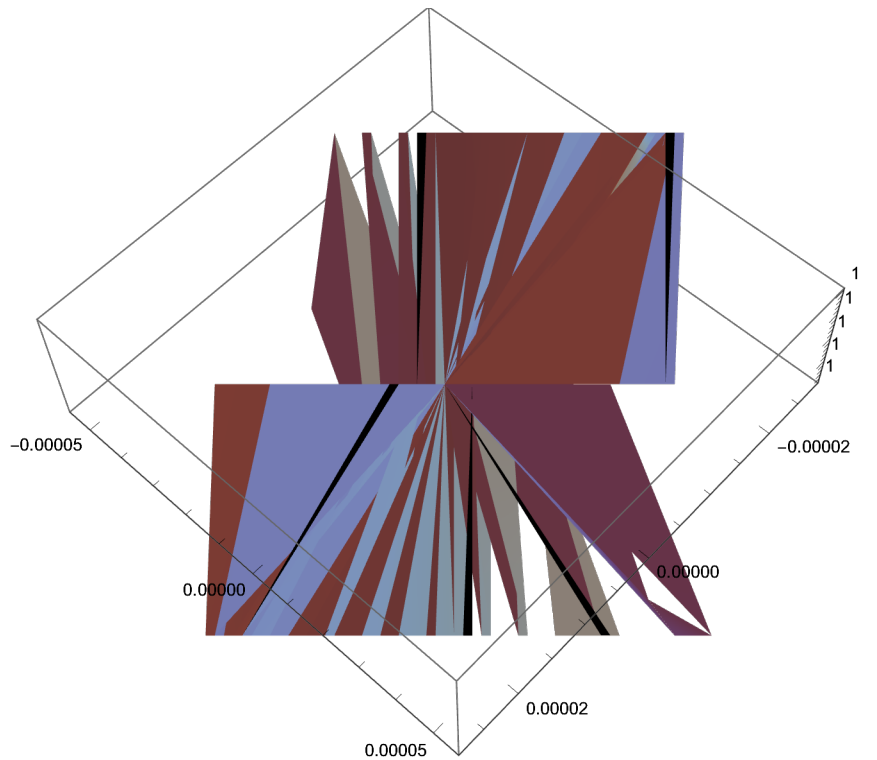
$$\text{RevolutionPlot3D}\left[e^{\left(i\left(\frac{4\pi}{3} + \left((1-i\sqrt{3})\left(-4\pi^2 + 12\pi^2\sin[\beta]^2\right)\right)\right)\right)}\right. \\ \left.\left(12\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3}\right) - \right. \\ \left.\frac{1}{3}\left(1+i\sqrt{3}\right)\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + \right.\right. \\ \left.\left.3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3}\right)\right], \{\beta, -\pi, \pi\}]$$



$$\text{RevolutionPlot3D}\left[e^{\left(i\left(\frac{4\pi}{3} - \left(-4\pi^2 + 12\pi^2\sin[\beta]^2\right)\right)\right)}\right. \\ \left.\left(6\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\ \left.\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + \right.\right. \\ \left.\left.3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3}\right)\right], \{\beta, -\pi, \pi\}]$$



$$\text{RevolutionPlot3D}\left[e^{\imath}\left(\frac{4\pi}{3}-\left(-4\pi^2+12\pi^2\sin[\beta]^2\right)\right)\right. \\ \left.\left(6\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)+\frac{2}{3}\right. \\ \left.\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)\right],\{\beta,-\pi,\pi\}]$$



$$e^{\imath(\beta)} = (\cos[\beta] + \imath \sin[\beta])$$

$$e^{\imath\beta} = \cos[\beta] + \imath \sin[\beta]$$

If matter is composed of a geometric element in the shape of a cone,  
it may be purely geometrically stated that :

$$e^{\imath \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \left(\cos\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] + \imath \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]\right) \\ e^{\imath \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \frac{\imath \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi-\theta)\theta}{4\pi^2}}$$

if it is within the region of  $\theta = \pi$ ,  $\beta = \frac{\pi}{2}$ .

$$e^{\imath \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \frac{\imath \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi-\theta)\theta}{4\pi^2}} = \frac{\imath \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{u^2}{c^2}}$$



$$\text{Solve}\left[\sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}} == \frac{\pm \sqrt{(4\pi - \theta)\theta}}{2\pi} + \sqrt{1 - \frac{u^2}{c^2}}, u\right]$$

$$\left\{\left\{u \rightarrow -0.000494236 \sqrt{\left(2.34235 \times 10^{23} \theta - 1.86399 \times 10^{22} \theta^2 + \left(0. + 1.86399 \times 10^{22} \pm\right) \sqrt{12.5664 \theta - 1. \theta^2} \sqrt{39.4784 - 12.5664 \theta + 1. \theta^2}\right)}\right\},\right.$$

$$\left.\left\{u \rightarrow 0.000494236 \sqrt{\left(2.34235 \times 10^{23} \theta - 1.86399 \times 10^{22} \theta^2 + \left(0. + 1.86399 \times 10^{22} \pm\right) \sqrt{12.5664 \theta - 1. \theta^2} \sqrt{39.4784 - 12.5664 \theta + 1. \theta^2}\right)}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}} == \frac{\pm \sqrt{(4\pi - \theta)\theta}}{2\pi} + \sqrt{1 - \frac{u^2}{c^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{\pi \left(2c^4 - 2c^2u^2 - \sqrt{4c^8 - 8c^6u^2 + 5c^4u^4 - c^2u^6}\right)}{c^4 - c^2u^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow \frac{\pi \left(2c^4 - 2c^2u^2 + \sqrt{4c^8 - 8c^6u^2 + 5c^4u^4 - c^2u^6}\right)}{c^4 - c^2u^2}\right\}\right\}$$

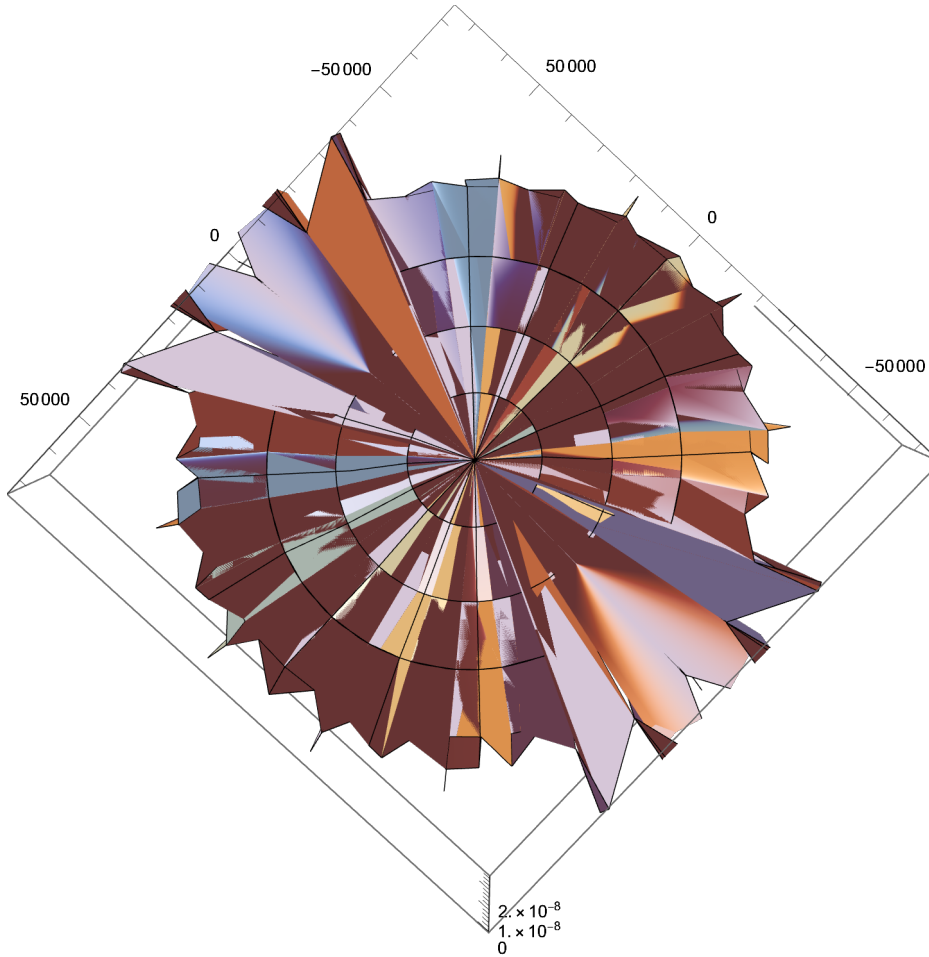
$$\text{Solve}\left[\frac{\pi\left(2c^4-2c^2u^2-\sqrt{4c^8-8c^6u^2+5c^4u^4-c^2u^6}\right)}{c^4-c^2u^2}==2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right),\beta\right]$$

$$\left\{\left\{\beta\rightarrow-1.\text{ArcSin}\left[0.31831\right.\right.\right.$$

$$\begin{aligned} & \sqrt{\left(-\frac{1.28794\times10^{69}}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}+\frac{2.86605\times10^{52}u^2}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}-\right. \\ & \frac{1.79376\times10^{35}u^4}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}+\frac{2.21759\times10^{17}u^6}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}+ \\ & \frac{1.59446\times10^{35}}{8.07761\times10^{33}-8.98755\times10^{16}u^2}-\frac{1.77407\times10^{18}u^2}{8.07761\times10^{33}-8.98755\times10^{16}u^2}+ \\ & \left(2.39003\times10^{43}\sqrt{\left(2.90392\times10^{51}+2.47588\times10^{27}u-6.46209\times10^{34}\right.}\right. \\ & \left.\left.u^2+1.71799\times10^{10}u^3+4.49378\times10^{17}u^4-1.u^6\right)\right)/ \\ & \left.\left.\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2-\left(2.65927\times10^{26}u^2\right.\right. \right. \\ & \left.\left.\sqrt{\left(2.90392\times10^{51}+2.47588\times10^{27}u-6.46209\times10^{34}u^2+1.71799\times10^{10}\right.}\right. \right. \\ & \left.\left.\left.u^3+4.49378\times10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2-\right. \\ & \left.\left.\left(2.95883\times10^9\sqrt{\left(2.90392\times10^{51}+2.47588\times10^{27}u-6.46209\times10^{34}\right.}\right. \right. \right. \\ & \left.\left.\left.u^2+1.71799\times10^{10}u^3+4.49378\times10^{17}u^4-1.u^6\right)\right)/\right. \\ & \left.\left.\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)\right)\right]\},\left\{\beta\rightarrow\text{ArcSin}\left[0.31831\right.\right. \end{aligned}$$

$$\begin{aligned} & \sqrt{\left(-\frac{1.28794\times10^{69}}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}+\frac{2.86605\times10^{52}u^2}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}-\right. \\ & \frac{1.79376\times10^{35}u^4}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}+\frac{2.21759\times10^{17}u^6}{\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2}+ \\ & \frac{1.59446\times10^{35}}{8.07761\times10^{33}-8.98755\times10^{16}u^2}-\frac{1.77407\times10^{18}u^2}{8.07761\times10^{33}-8.98755\times10^{16}u^2}+ \\ & \left(2.39003\times10^{43}\sqrt{\left(2.90392\times10^{51}+2.47588\times10^{27}u-6.46209\times10^{34}u^2+1.71799\times\right.}\right. \\ & \left.\left.10^{10}u^3+4.49378\times10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2- \\ & \left(2.65927\times10^{26}u^2\sqrt{\left(2.90392\times10^{51}+2.47588\times10^{27}u-6.46209\times10^{34}u^2+1.71799\times\right.}\right. \\ & \left.\left.10^{10}u^3+4.49378\times10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)^2- \\ & \left(2.95883\times10^9\sqrt{\left(2.90392\times10^{51}+2.47588\times10^{27}u-6.46209\times10^{34}u^2+1.71799\times10^{10}\right.}\right. \\ & \left.\left.\left.u^3+4.49378\times10^{17}u^4-1.u^6\right)\right)/\left(8.07761\times10^{33}-8.98755\times10^{16}u^2\right)\right)\right]\}\} \end{aligned}$$

$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\text{ArcSin}\left[ \right. \right. \\
& 0.3183098861837907 \sqrt{\left( -\frac{1.2879392082837613 \cdot 10^{69}}{(8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2)^2} + \right.} \\
& \quad \frac{2.86605126458116 \cdot 10^{52} u^2}{(8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2)^2} - \\
& \quad \frac{1.793763056356184 \cdot 10^{43} u^4}{(8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2)^2} + \\
& \quad \frac{2.217589516890687 \cdot 10^{17} u^6}{(8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2)^2} + \\
& \quad \frac{1.594456050094386 \cdot 10^{35}}{8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2} - \\
& \quad \frac{1.7740716135125496 \cdot 10^{18} u^2}{8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2} + \\
& \quad (2.3900294921538355 \cdot 10^{43} \sqrt{(2.903917065069822 \cdot 10^{51} + } \\
& \quad \quad 2.4758800785707605 \cdot 10^{27} u - 6.462086970449991 \cdot 10^{34} u^2 + \\
& \quad \quad 1.7179869184 \cdot 10^{10} u^3 + 4.493775893684088 \cdot 10^{17} u^4 - 1 \cdot 10^{16})}) / \\
& \quad (8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2)^2 - \\
& \quad (2.6592664484147662 \cdot 10^{26} u^2 \sqrt{(2.903917065069822 \cdot 10^{51} + } \\
& \quad \quad 2.4758800785707605 \cdot 10^{27} u - 6.462086970449991 \cdot 10^{34} u^2 + \\
& \quad \quad 1.7179869184 \cdot 10^{10} u^3 + 4.493775893684088 \cdot 10^{17} u^4 - 1 \cdot 10^{16})}) / \\
& \quad (8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2)^2 - \\
& \quad (2.958832962890196 \cdot 10^9 \sqrt{(2.903917065069822 \cdot 10^{51} + } \\
& \quad \quad 2.4758800785707605 \cdot 10^{27} u - 6.462086970449991 \cdot 10^{34} u^2 + \\
& \quad \quad 1.7179869184 \cdot 10^{10} u^3 + 4.493775893684088 \cdot 10^{17} u^4 - 1 \cdot 10^{16})}) / \\
& \quad \left. (8.07760871306249 \cdot 10^{33} - 8.987551787368176 \cdot 10^{16} u^2) \right], \{u, -c, c\}]
\end{aligned}$$



$$\text{Solve}\left[\frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2} == 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right), u\right]$$

$$\begin{aligned} & \left\{ \left\{ u \rightarrow \text{Root}\left[4.0532258104836432542368746274352 \times 10^{67} - \right. \right. \right. \\ & \quad 1.7079612615978583669368862294392 \times 10^{83} \text{Sin}[\beta]^2 + \\ & \quad 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\ & \quad \left(-5.4111401881449464088210664670613 \times 10^{50} + \right. \\ & \quad \left. 3.8007263869085317046852183304742 \times 10^{66} \text{Sin}[\beta]^2\right) \#1^2 - \\ & \quad 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\ & \quad \left(-5.2860980342978121431211906423698 \times 10^{48} - \right. \\ & \quad \left. 2.1144392137191221020101719542600 \times 10^{49} \text{Sin}[\beta]^2\right) \#1^4 - \\ & \quad 3.50569324145697052898902500000000 \times 10^{24} \#1^5 + \\ & \quad \left. 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 1\right\}, \\ & \left\{ u \rightarrow \text{Root}\left[4.0532258104836432542368746274352 \times 10^{67} - \right. \right. \\ & \quad 1.7079612615978583669368862294392 \times 10^{83} \text{Sin}[\beta]^2 + \\ & \quad 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\ & \quad \left(-5.4111401881449464088210664670613 \times 10^{50} + \right. \\ & \quad \left. 3.8007263869085317046852183304742 \times 10^{66} \text{Sin}[\beta]^2\right) \#1^2 - \end{aligned}$$

$$\begin{aligned}
& 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\
& (-5.2860980342978121431211906423698 \times 10^{48} - \\
& \quad 2.1144392137191221020101719542600 \times 10^{49} \sin[\beta]^2) \#1^4 - \\
& 3.5056932414569705289890250000000 \times 10^{24} \#1^5 + \\
& 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 2\}, \\
\{u \rightarrow \text{Root}[4.0532258104836432542368746274352 \times 10^{67} - \\
& 1.7079612615978583669368862294392 \times 10^{83} \sin[\beta]^2 + \\
& 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\
& (-5.4111401881449464088210664670613 \times 10^{50} + \\
& \quad 3.8007263869085317046852183304742 \times 10^{66} \sin[\beta]^2) \#1^2 - \\
& 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\
& (-5.2860980342978121431211906423698 \times 10^{48} - \\
& \quad 2.1144392137191221020101719542600 \times 10^{49} \sin[\beta]^2) \#1^4 - \\
& 3.5056932414569705289890250000000 \times 10^{24} \#1^5 + \\
& 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 3\}, \\
\{u \rightarrow \text{Root}[4.0532258104836432542368746274352 \times 10^{67} - \\
& 1.7079612615978583669368862294392 \times 10^{83} \sin[\beta]^2 + \\
& 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\
& (-5.4111401881449464088210664670613 \times 10^{50} + \\
& \quad 3.8007263869085317046852183304742 \times 10^{66} \sin[\beta]^2) \#1^2 - \\
& 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\
& (-5.2860980342978121431211906423698 \times 10^{48} - \\
& \quad 2.1144392137191221020101719542600 \times 10^{49} \sin[\beta]^2) \#1^4 - \\
& 3.5056932414569705289890250000000 \times 10^{24} \#1^5 + \\
& 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 4\}, \\
\{u \rightarrow \text{Root}[4.0532258104836432542368746274352 \times 10^{67} - \\
& 1.7079612615978583669368862294392 \times 10^{83} \sin[\beta]^2 + \\
& 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\
& (-5.4111401881449464088210664670613 \times 10^{50} + \\
& \quad 3.8007263869085317046852183304742 \times 10^{66} \sin[\beta]^2) \#1^2 - \\
& 2.0208945633153124779637513510659 \times 10^{42} \#1^3 + \\
& (-5.2860980342978121431211906423698 \times 10^{48} - \\
& \quad 2.1144392137191221020101719542600 \times 10^{49} \sin[\beta]^2) \#1^4 - \\
& 3.5056932414569705289890250000000 \times 10^{24} \#1^5 + \\
& 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 5\}, \\
\{u \rightarrow \text{Root}[4.0532258104836432542368746274352 \times 10^{67} - \\
& 1.7079612615978583669368862294392 \times 10^{83} \sin[\beta]^2 + \\
& 1.4562080003683044018041706105627 \times 10^{59} \#1 + \\
& (-5.4111401881449464088210664670613 \times 10^{50} + \\
& \quad 3.8007263869085317046852183304742 \times 10^{66} \sin[\beta]^2) \#1^2 - \\
& 2.0208945633153124779637513510659 \times 10^{42} \#1^3 +
\end{aligned}$$

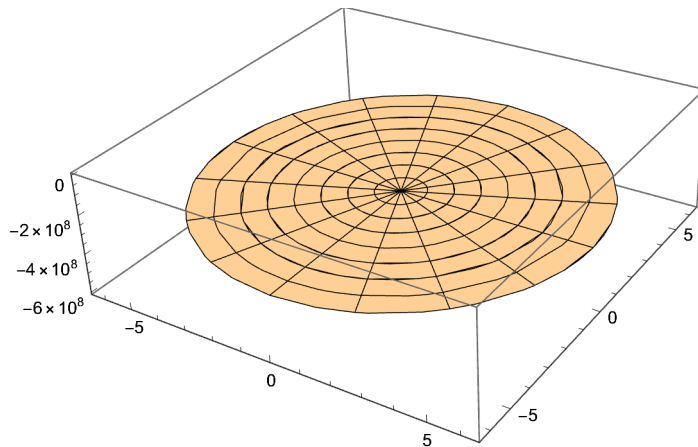
$$\begin{aligned} & \left( -5.2860980342978121431211906423698 \times 10^{48} - \right. \\ & \quad \left. 2.1144392137191221020101719542600 \times 10^{49} \sin[\beta]^2 \right) \#1^4 - \\ & \quad 3.5056932414569705289890250000000 \times 10^{24} \#1^5 + \\ & \quad \left. 5.8815772741663749270483134054400 \times 10^{31} \#1^6 \&, 6 \right] \} \} \end{aligned}$$

RevolutionPlot3D[Root[

```

4.0532258104836432542368746274352049384829996549868873500941076135936`31.909179\
540382016*^67 -
1.7079612615978583669368862294391867719820309387352160756817670917`31.9091795\
4038201*^83 Sin[β]^2 +
1.456208000368304401804170610562654241243542338347007475712`31.90917954038201\
*^59 #1 +
(-5.41114018814494640882106646706128560033702885720064`31.90917954038201*^50 +
3.800726386908531704685218330474210119415700395484123748732097265664`31.9\
0917954038201*^66 Sin[β]^2) #1^2 -
2.0208945633153124779637513510658550792192`31.909179540382*^42 #1^3 +
(-5.286098034297812143121190642369759388314386825216`31.90917954038201*^48 -
2.1144392137191221020101719542599757567807700598784`31.90917954038201*^49
Sin[β]^2) #1^4 - 3.505693241456970528989025`31.90917954038201*^24 #1^5 +
5.88157727416637492704831340544`31.90917954038201*^31 #1^6 &, 1], {β, -2 π, 2 π}]

```



$$\begin{aligned}
& \frac{\pi \left( 2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6} \right)}{c^4 - c^2 u^2} = \\
& \left\{ \left\{ \theta \rightarrow \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \right. \right. \\
& \quad \left. \frac{2 \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} - \frac{\left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2 \right)}{12 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} + \right. \\
& \quad \left. \frac{\left( 1 - \mathfrak{i} \sqrt{3} \right) \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} - \frac{\left( 1 - \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2 \right)}{12 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} + \right. \\
& \quad \left. \frac{\left( 1 + \mathfrak{i} \sqrt{3} \right) \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right\} \} \\
& \left\{ \left\{ \theta \rightarrow \frac{4 \pi}{3} - \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} + \left( \left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) \right) / \left( 12 \right. \right. \\
& \quad \left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \left( 1 - \right. \\
& \quad \left. \mathfrak{i} \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \left. \right\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} + \left( \left( 1 - \mathfrak{i} \sqrt{3} \right) \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) \right) / \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \left. \right\} \}
\end{aligned}$$

$\theta$  = Those other three long ones (1 real 2 imaginary)

$$\begin{aligned} \text{from Solve} \left[ \frac{1}{2\pi} \left( \sqrt[3]{4\pi r^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right)} \right. \right. \\ \left. \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\ \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \\ \left. r^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \sqrt[3]{6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} \right. \\ \left. + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 \right] = \\ \left. r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{-4\pi^2 \theta + 4\pi \theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}} \right] \right], \theta \right] \end{aligned}$$

$c := (2.99792458 * 10^8)$

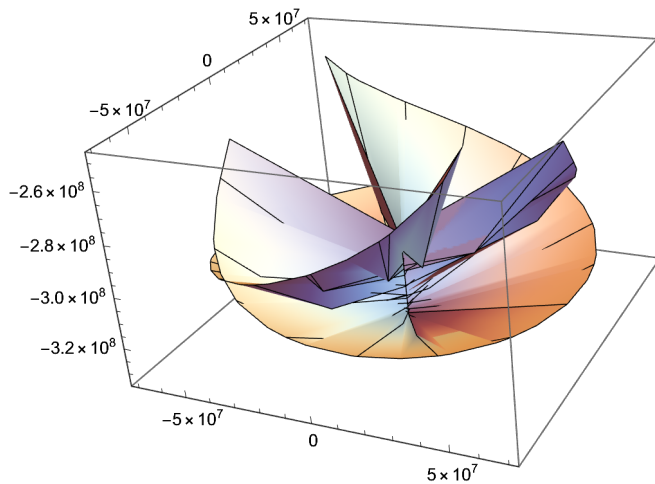
$\theta$  = A set of three potential threes of solutions solvable with ease.



```

SphericalPlot3D[Root[
  4.0532258104836432542368746274352049384829996549868873500941076135936`31.909179\
  540382016*^67 -
  1.7079612615978583669368862294391867719820309387352160756817670917`31.9091795\
  4038201*^83 Sin[ArcSin[ $\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}$ ]]^2 +
  1.456208000368304401804170610562654241243542338347007475712`31.90917954038201\
  *^59 #1 +
  (-5.41114018814494640882106646706128560033702885720064`31.90917954038201*^50 +
  3.800726386908531704685218330474210119415700395484123748732097265664`31.9\
  0917954038201*^66 Sin[ $\beta$ ]^2) #1^2 -
  2.0208945633153124779637513510658550792192`31.909179540382*^42 #1^3 +
  (-5.286098034297812143121190642369759388314386825216`31.90917954038201*^48 -
  2.1144392137191221020101719542599757567807700598784`31.90917954038201*^49
  Sin[ $\beta$ ]^2) #1^4 - 3.505693241456970528989025`31.90917954038201*^24 #1^5 +
  5.88157727416637492704831340544`31.90917954038201*^31 #1^6 &,
  1], { $\beta$ , -2  $\pi$ , 2  $\pi$ }, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

```



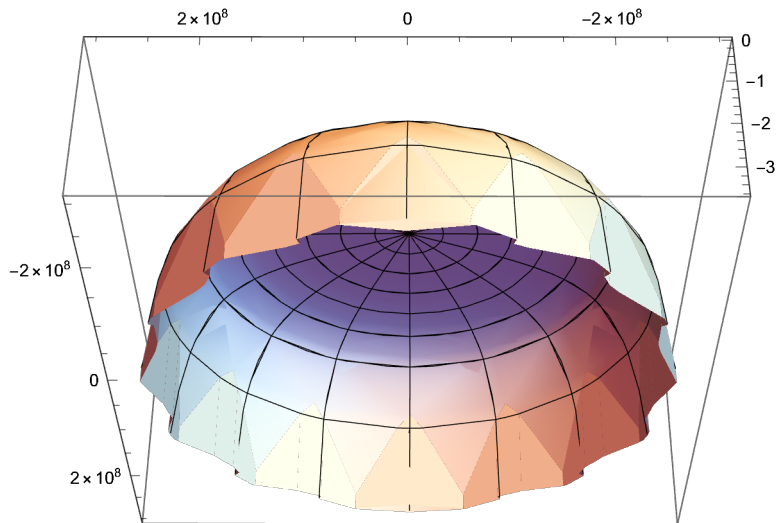
$$\beta = \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]$$

$v = u = \text{Relativistic sorts}$

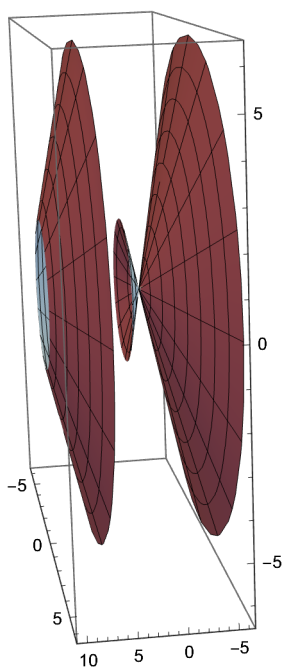
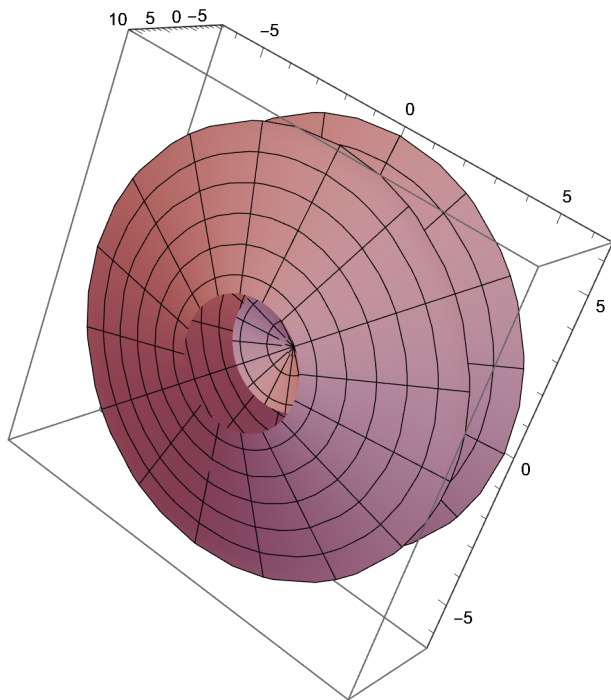
$$\begin{aligned}
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - \right. \right. \right. \\
& \quad \left. \left. \left. 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{ 39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 } \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - 1.1294090667581471 \cdot r^2 \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot r^2 \theta^2 \right) \right) \right\} / \\
& \quad \left( \sqrt{ 39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 } \right) \Big\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right) \right\} / \\
& \quad \left( \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \right) \Big\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \sqrt{ - \frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta} } \right\}, \right. \\
& \left\{ v \rightarrow \sqrt{ - \frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta} } \right\}, \\
& \left\{ v \rightarrow - \sqrt{ - \frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta} } \right\}, \\
& \left\{ v \rightarrow \sqrt{ - \frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta} } \right\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - \right. \right. \right. \\
& \quad \left. \left. \left. 1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 \right) \right) \right\} / \right. \\
& \quad \left. \left( \sqrt{ 39.47841760435743 \cdot \theta + \theta^2 - 12.566370614359172 \cdot \theta + \theta^2 } \right) \right\}, \\
& \left\{ v \rightarrow \left( \sqrt{ \left( 3.5481432270250993 \cdot \eta^2 - 1.1294090667581471 \cdot \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot \theta^2 \right) \right) \right\} / \\
& \quad \left( \sqrt{ 39.47841760435743 \cdot \theta + \theta^2 - 12.566370614359172 \cdot \theta + \theta^2 } \right) \Big\} \Big\}
\end{aligned}$$

$$u = v = 0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot 10^{23} \theta - 1.863986866980889 \cdot 10^{22} \theta^2 + (0. \cdot 1.863986866980889 \cdot 10^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 \cdot \theta - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)}$$

$$\text{RevolutionPlot3D}\left[\frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2}, \{u, -2.99792458 \cdot 10^8, (2.99792458 \cdot 10^8)\}\right]$$



$$\begin{aligned}
& \text{RevolutionPlot3D}\left[1/\left(c^4 - c^2\right.\right. \\
& \quad \left.\left(-0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - 1.863986866980889 \theta^{22} \right.\right.\right. \\
& \quad \left.\left.\left.\theta^2 + (\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^2\right) \\
& \quad \pi \left(2 c^4 - 2 c^2 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right. \\
& \quad \left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right. \\
& \quad \left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right. \\
& \quad \left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^2 - \right. \\
& \quad \left.\sqrt{\left(4 c^8 - 8 c^6 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^2 + \right.\right. \\
& \quad \left.\left.5 c^4 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^4 - \right.\right. \\
& \quad \left.\left.c^2 \left(0.000494236036686326 \sqrt{\left(2.3423549790780066 \theta - \right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.1.863986866980889 \theta^{22} \theta^2 + \right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.(\theta + 1.863986866980889 \theta^{22}) \sqrt{12.566370614359172 \theta - 1. \theta^2}\right.\right.\right.\right. \\
& \quad \left.\left.\left.\left.\sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2}\right)\right)^6\right)\right), \\
& \quad \left.\{\theta, -2 \pi, 2 \pi\}\right]
\end{aligned}$$

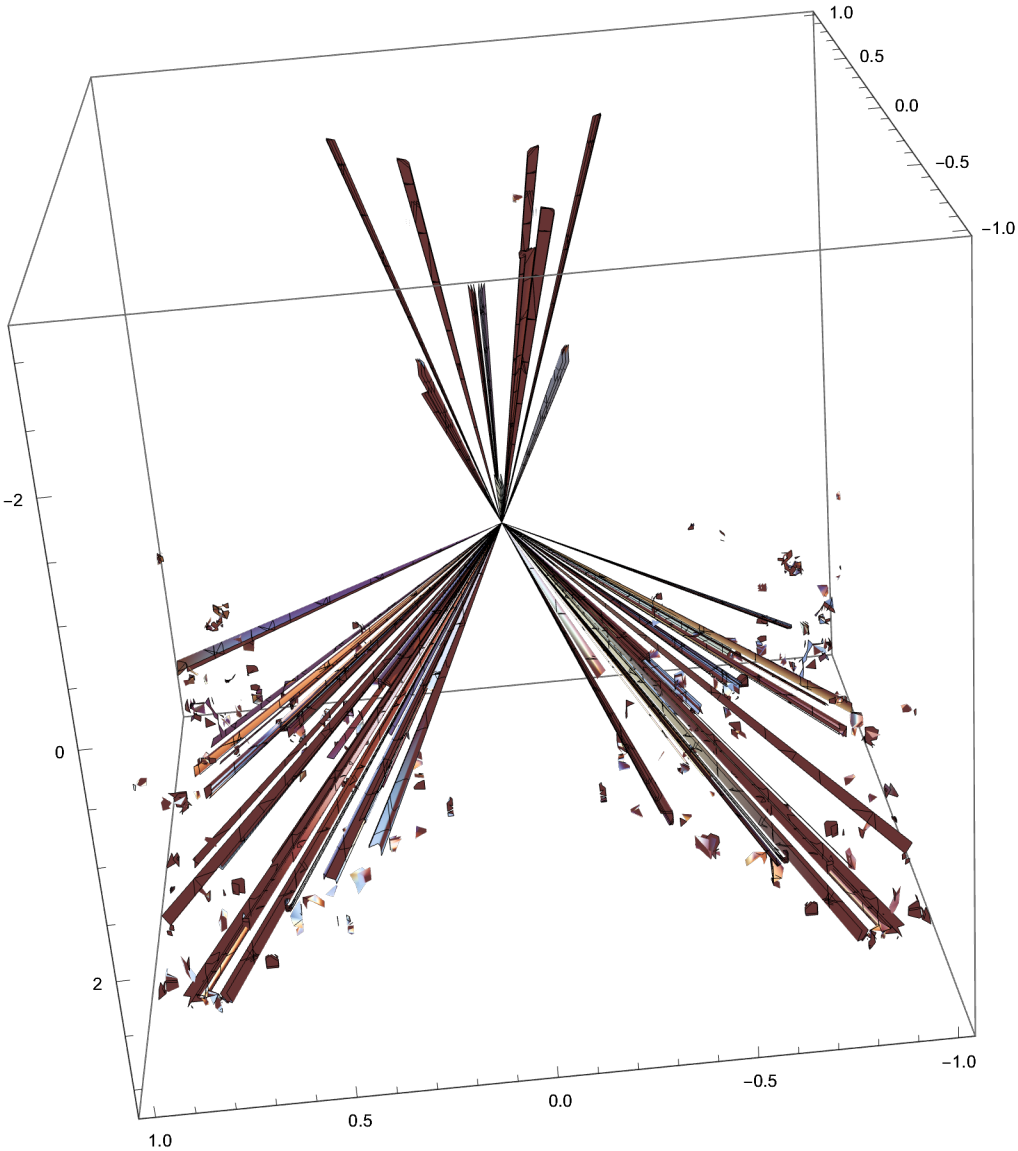


$\text{RevolutionPlot3D}\left[\frac{\pi \left(2 c^4 - 2 c^2 u^2 - \sqrt{4 c^8 - 8 c^6 u^2 + 5 c^4 u^4 - c^2 u^6}\right)}{c^4 - c^2 u^2},\right.$   
 $\left.\{u, -2.99792458 \times 10^8, (2.99792458 \times 10^8)\}\right]$

```

ContourPlot3D[
  1 / (c^4 - c^2 (- (1. ` Sqrt[3.5481432270250993`*^18 η^2 - 1.1294090667581471`*^18 r^2 θ +
    8.987551787368176`*^16 r^2 θ^2])) /
    (Sqrt[39.47841760435743` η^2 - 12.566370614359172` r^2 θ + r^2 θ^2]))^2) π
  (2 c^4 - 2 c^2 (- (1. ` Sqrt[3.5481432270250993`*^18 η^2 - 1.1294090667581471`*^18
    r^2 θ + 8.987551787368176`*^16 r^2 θ^2])) /
    (Sqrt[39.47841760435743` η^2 - 12.566370614359172` r^2 θ + r^2 θ^2]))^2 -
  Sqrt[4 c^8 - 8 c^6 (- (1. ` Sqrt[3.5481432270250993`*^18 η^2 - 1.1294090667581471`*^18
    r^2 θ + 8.987551787368176`*^16 r^2 θ^2])) /
    (Sqrt[39.47841760435743` η^2 - 12.566370614359172` r^2 θ + r^2 θ^2]))^2 +
  5 c^4 (- (1. ` Sqrt[3.5481432270250993`*^18 η^2 - 1.1294090667581471`*^18
    r^2 θ + 8.987551787368176`*^16 r^2 θ^2])) /
    (Sqrt[39.47841760435743` η^2 - 12.566370614359172` r^2 θ + r^2 θ^2]))^4 -
  c^2 (- (1. ` Sqrt[3.5481432270250993`*^18 η^2 - 1.1294090667581471`*^18
    r^2 θ + 8.987551787368176`*^16 r^2 θ^2])) /
    (Sqrt[39.47841760435743` η^2 - 12.566370614359172` r^2 θ +
    r^2 θ^2]))^6)], {r, -1, 1}, {η, -1, 1}, {θ, -π, π}]

```

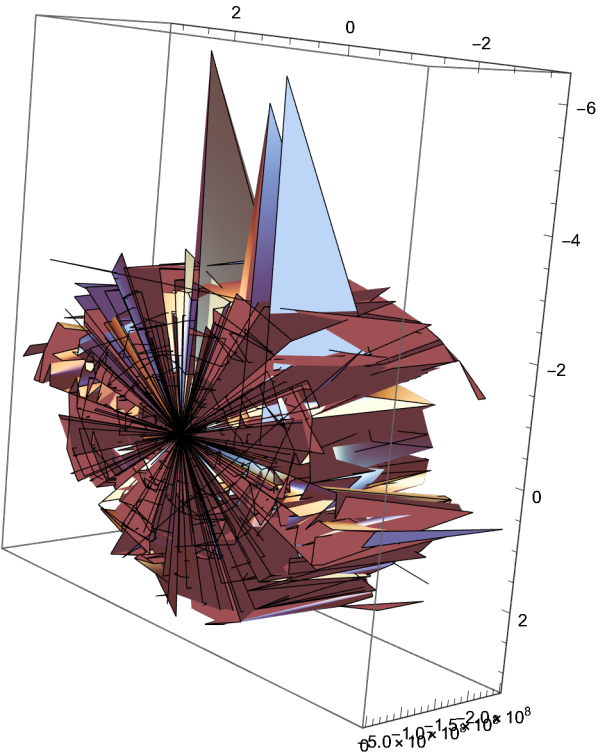


```

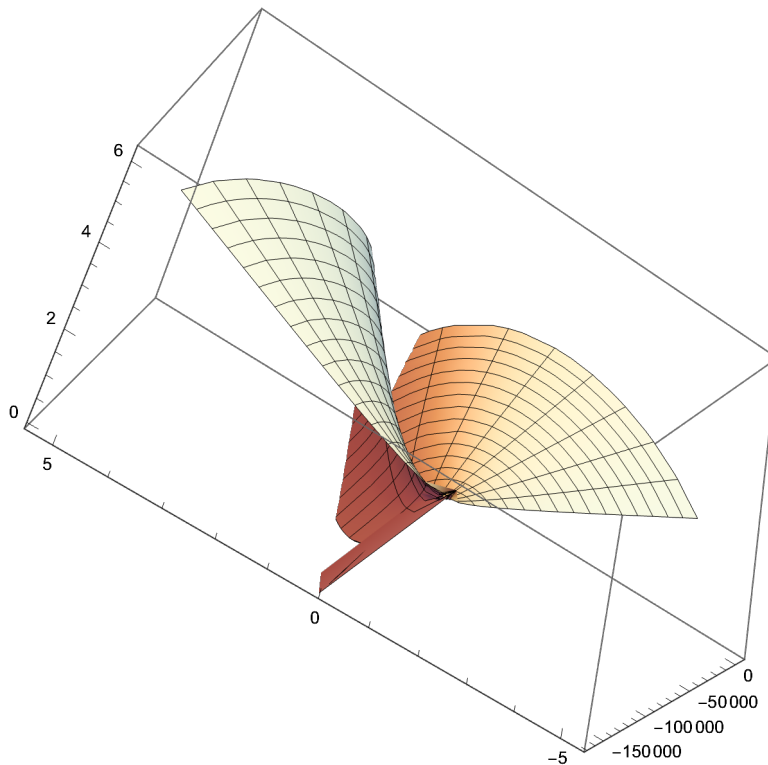
RevolutionPlot3D[
  1 / ( c^4 - c^2 ( ( sqrt ( -1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2 ) ) ) /
    ( sqrt ( -12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2 ) )^2 )
  pi ( 2 c^4 - 2 c^2 ( ( sqrt ( -1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2 ) ) ) /
    ( sqrt ( -12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2 ) )^2 -
    sqrt ( 4 c^8 - 8 c^6 ( ( sqrt ( -1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2 ) ) ) /
    ( sqrt ( -12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2 ) )^2 +
    5 c^4 ( ( sqrt ( -1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2 ) ) ) /
    ( sqrt ( -12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2 ) )^4 -
    c^2 ( ( sqrt ( -1.1294090667581471`*^18 theta + 8.987551787368176`*^16 theta^2 +
    3.5481432270250993`*^18 Sin[beta]^2 ) ) ) /
    ( sqrt ( -12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2 ) )^6 ) ) ,
  {beta, -pi, pi}, {theta, -2 pi, 2 pi}]

```





$$\text{RevolutionPlot3D}\left[\frac{1}{c^4 - c^2 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^2}, \right. \\ \pi \left( 2c^4 - 2c^2 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^2 - \right. \\ \left. \sqrt{\left( 4c^8 - 8c^6 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^2 + \right. \right. \\ \left. \left. 5c^4 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^4 - \right. \right. \\ \left. \left. c^2 \left( \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2\theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right)^6 \right) \right), \\ \{\theta, -2\pi, 2\pi\}, \{r, -1, 1\}]$$



$$\left\{ \left\{ u \rightarrow \right. \right. \\ \left. -0.000494236036686326 \sqrt{2.3423549790780066 * ^{23} \theta - 1.863986866980889 * ^{22} \theta^2 +} \right.$$

$$\begin{aligned}
& \left( (0. + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
& \quad \left. \sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2} \right), \\
& \left\{ u \rightarrow 0.000494236036686326 \sqrt{2.3423549790780066 \theta^{23} - 1.863986866980889 \theta^{22}} \right. \\
& \quad \left. \theta^2 + (0. + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \theta - 1. \theta^2} \right. \\
& \quad \left. \sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2} \right\} = \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{3.5481432270250993 \eta^2 - 1.1294090667581471 \cdot r^2 \theta +} \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot r^2 \theta^2 \right) \right\} / \\
& \quad \left( \sqrt{39.47841760435743 \eta^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2} \right) \Big\}, \\
& \left\{ v \rightarrow \left( \sqrt{3.5481432270250993 \eta^2 - 1.1294090667581471 \cdot r^2 \theta +} \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot r^2 \theta^2 \right) \right\} / \\
& \quad \left( \sqrt{39.47841760435743 \eta^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2} \right) \Big\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{-1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2 +} \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right\} / \\
& \quad \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \Big\}, \\
& \left\{ v \rightarrow \left( \sqrt{-1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2 +} \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right\} / \\
& \quad \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \Big\} \\
& \left\{ \left\{ v \rightarrow - \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} \right\}, \right. \\
& \quad \left\{ v \rightarrow \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} \right\}, \\
& \quad \left\{ v \rightarrow - \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta}} \right\}, \\
& \quad \left\{ v \rightarrow \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} + \frac{\sqrt{4 c^6 \pi r^2 \theta - c^6 r^2 \theta^2}}{-4 \pi r^2 + r^2 \theta}} \right\} \Big\} \\
& \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{3.5481432270250993 \cdot r^{18} -} \right. \right. \right. \\
& \quad \left. \left. 1.1294090667581471 \cdot r^{18} \theta + 8.987551787368176 \cdot r^{16} \theta^2 \right) \right\} / \\
& \quad \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right) \Big\},
\end{aligned}$$

$$\left\{ v \rightarrow \left( \sqrt{\left( 3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \right)} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) \right\}$$

Solve $\left[ 0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. \cdot + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right)} = \right.$

$$\left. \left( \sqrt{\left( 3.5481432270250993 \cdot \eta^{18} - 1.1294090667581471 \cdot r^{18} + 8.987551787368176 \cdot r^{16} \right)} \right) / \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 + r^2} \right), r \right]$$

{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. - 652931. i$ ],  
{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. + 652931. i$ ], {Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow 753946.$ ]}}

Solve $\left[ 0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. \cdot + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right)} = \right.$

$$\left. \left( \sqrt{\left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]} \right), \beta \right]$$

{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. - 652931. i$ ],  
{Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow -376964. + 652931. i$ ], {Solve`Auxiliary[ $\theta$ ][ $\theta \rightarrow 753946.$ ]}}

Solve $\left[ 0.000494236036686326 \cdot \sqrt{\left( 2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. \cdot + 1.863986866980889 \cdot \theta^{22} i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2} \right)} = \right.$

$$\left. \left( \sqrt{\left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]} \right), \theta \right]$$

{ $\theta \rightarrow -245215. - 424732. i$ }, { $\theta \rightarrow -245215. + 424732. i$ }, { $\theta \rightarrow 490443.$ }}

$$\text{Solve}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. + 1.863986866980889 \cdot i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)} = \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}, \theta\right]$$

$$\text{Solve}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. + 1.863986866980889 \cdot i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)} = \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}, r\right]$$

$$\text{Solve}\left[0.000494236036686326 \sqrt{\left(2.3423549790780066 \cdot \theta^{23} - 1.863986866980889 \cdot \theta^{22} + (0. + 1.863986866980889 \cdot i) \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2} \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + 1. \cdot \theta^2}\right)} = \left(\sqrt{\left(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16}\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2}\right), \theta\right]$$

$$\{\{\theta \rightarrow -245215. - 424732. i\}\}$$

$$c := (2.99792458 \cdot 10^8)$$

$$e^{i \beta} = \cos[\beta] + i \sin[\beta]$$

$$\beta = \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]$$

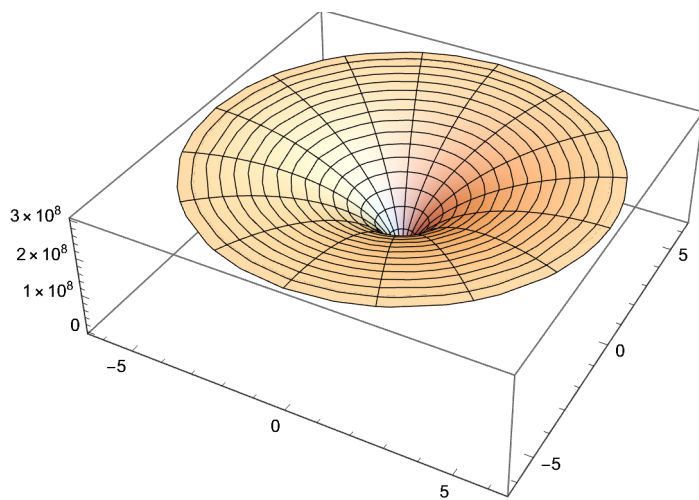
$$e^{i \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]} = \left(\cos\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right] + i \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]\right)$$

$$e^{i \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]} = \frac{i \sqrt{(4 \pi - \theta) \theta}}{2 \pi} + \sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}$$

$$\text{Solve}\left[\sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}} = \sqrt{1 - \frac{u^2}{c^2}}, u\right]$$

$$\left\{\left\{u \rightarrow -\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}, \left\{u \rightarrow \frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi}\right\}\right\}$$

RevolutionPlot3D $\left[\frac{\sqrt{4 (2.99792458 * 10^8)^2 \pi \theta - (2.99792458 * 10^8)^2 \theta^2}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}\right]$



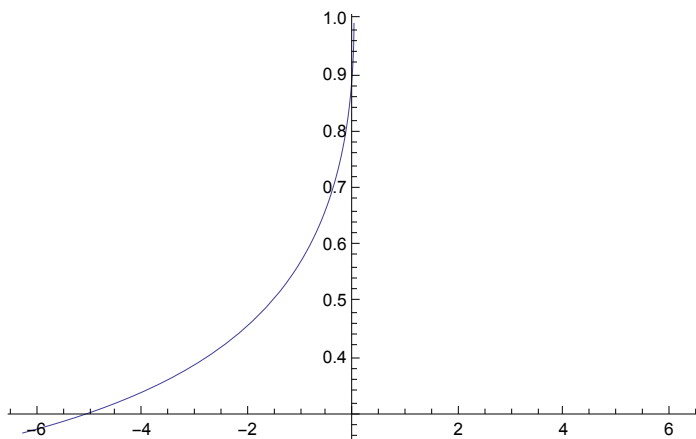
Solve $\left[\frac{\sqrt{4 c^2 \pi \theta - c^2 \theta^2}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$

{{r → -c}, {r → c}}

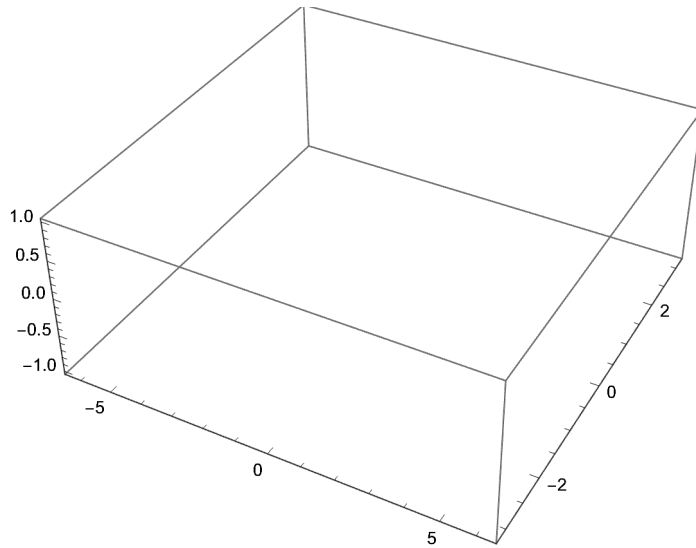
$$e^{\left(i \operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right)} = \left(\cos\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right] + i \sin\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]\right)$$

$$\theta = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)$$

Plot $\left[e^{i \operatorname{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]}, \{\theta, -2 \pi, 2 \pi\}\right]$

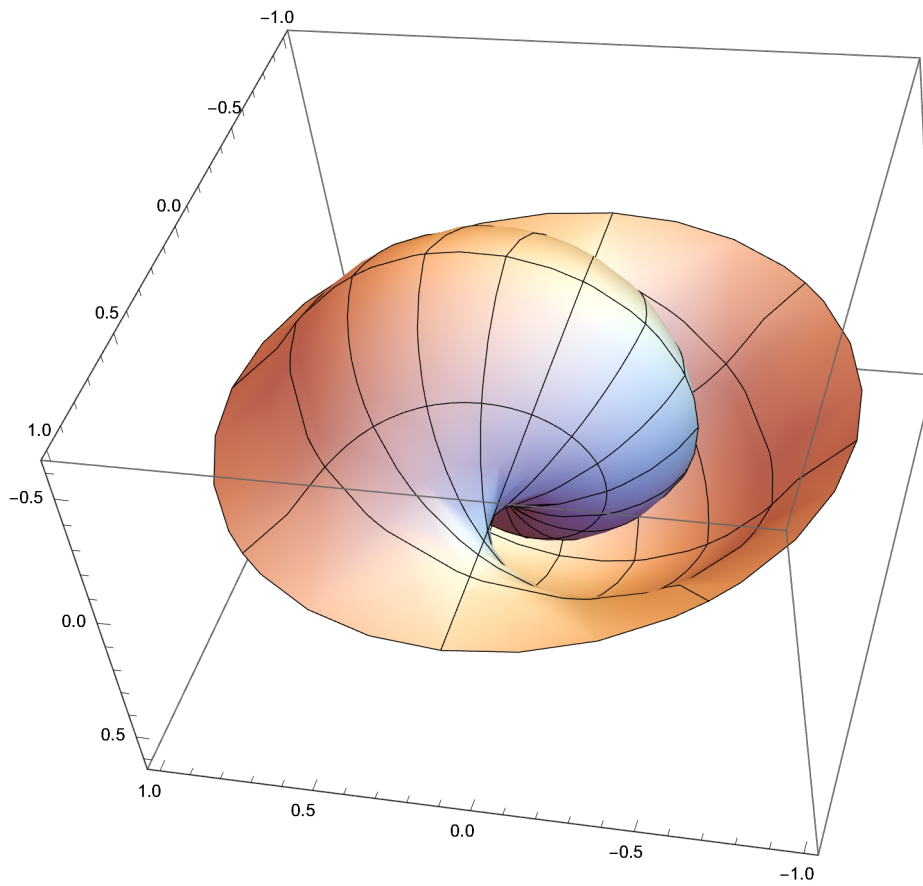


$\text{Plot3D}\left[\text{e}^{\text{i ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \left(2 \left(\pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}}{2 \pi}\right]}\right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$

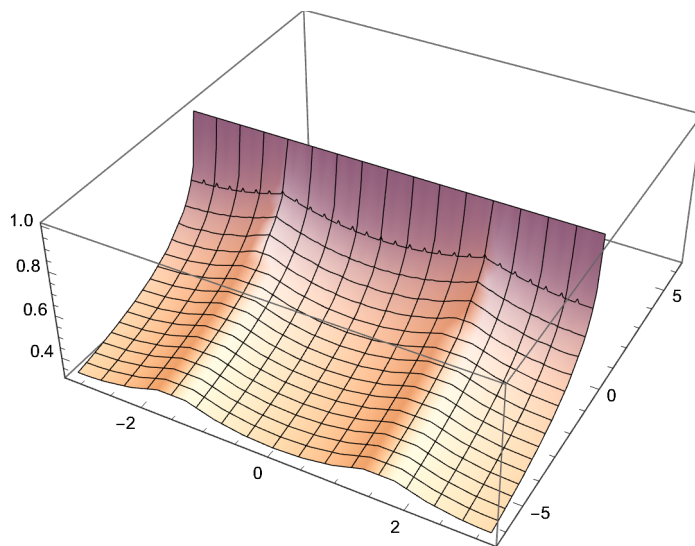


$$\text{e}^{\text{i ArcSin}\left[\frac{\sqrt{(4 \pi - 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)} \theta}{2 \pi}\right]} = \text{e}^{\text{i} \beta}$$

**SphericalPlot3D** $\left[e^{\frac{i \operatorname{ArcSin}\left[\frac{\sqrt{4 \pi - 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2 \pi}\right]}{\theta}}\right], \{\beta, -(2) \pi, (2) \pi\}, \{\theta, -(2) \pi, (2) \pi\}\right]$

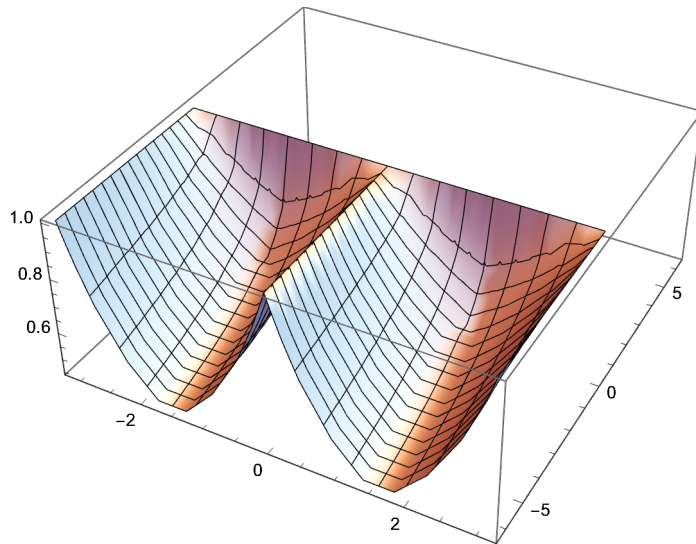


**Plot3D** $\left[e^{\frac{i \operatorname{ArcSin}\left[\frac{\sqrt{4 \pi - 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2 \pi}\right]}{\theta}}\right], \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$

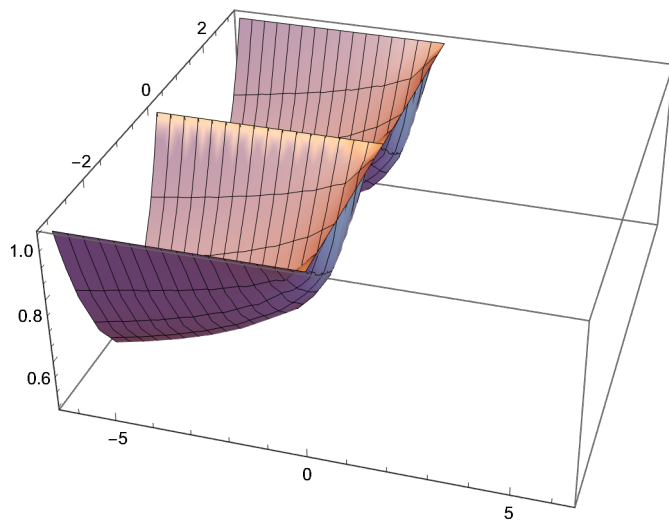




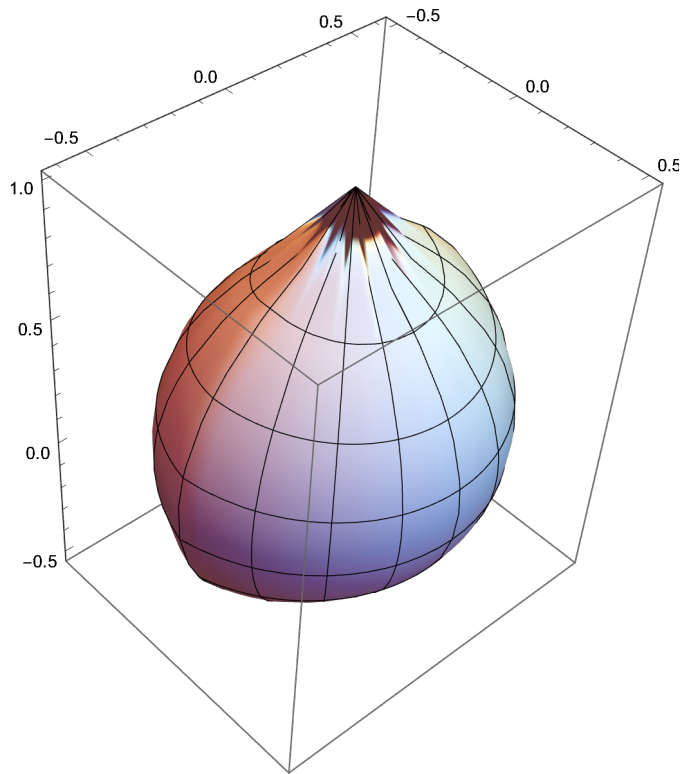
$\text{Plot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{\left(4 \pi-2\left(\pi+\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)\right) \theta}}{2 \pi}\right]}{\theta}},\{\beta,-\pi,\pi\},\{\theta,-2 \pi,2 \pi\}\right]$



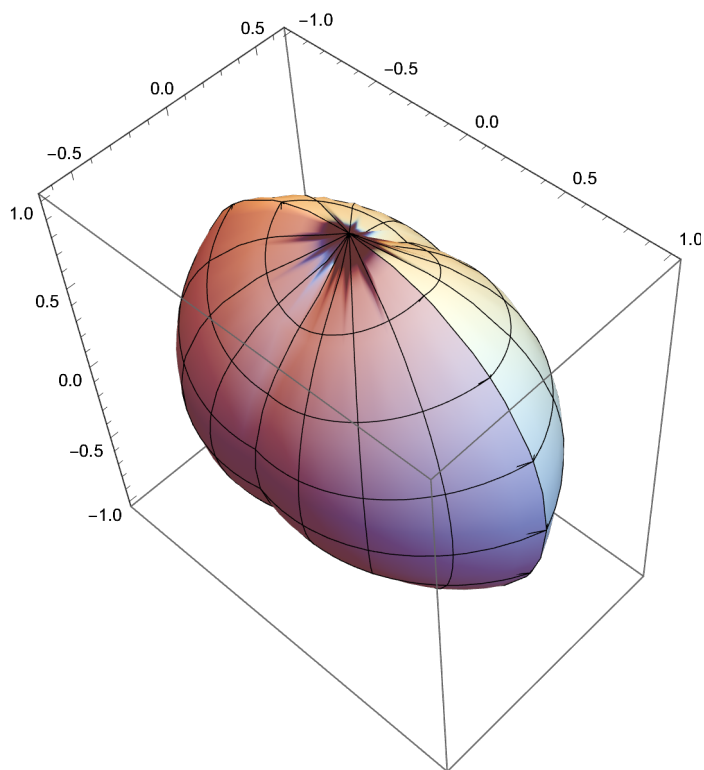
$\text{Plot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{\left(4 \pi-2\left(\pi+\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)\right) \theta}}{2 \pi}\right]}{\theta}},\{\theta,-2 \pi,2 \pi\},\{\beta,-\pi,\pi\}\right]$



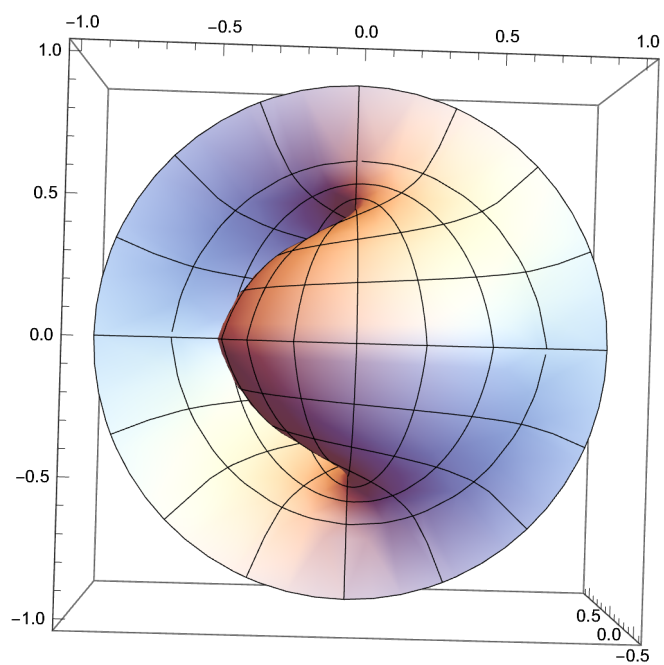
`SphericalPlot3D` $\left[e^{\pm \text{ArcSin}\left[\frac{\sqrt{4\pi-2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}\right)\theta}}{2\pi}\right], \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}\right]$



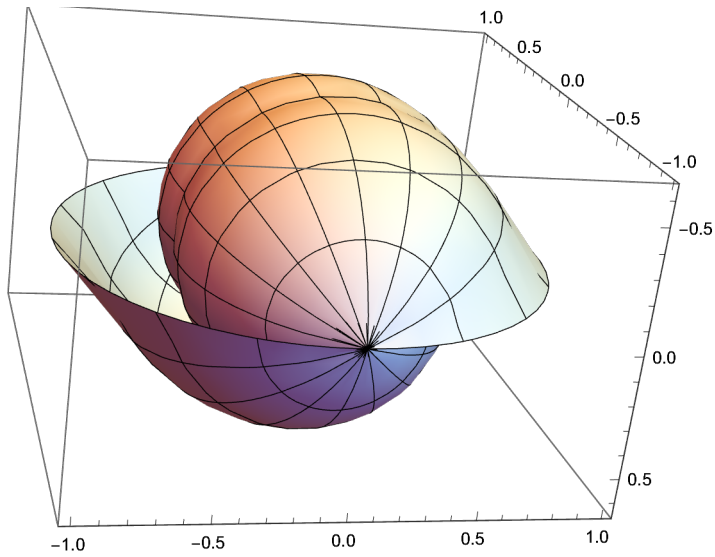
$\text{SphericalPlot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}{2\pi}\right]}{\theta}}\right], \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}\right]$



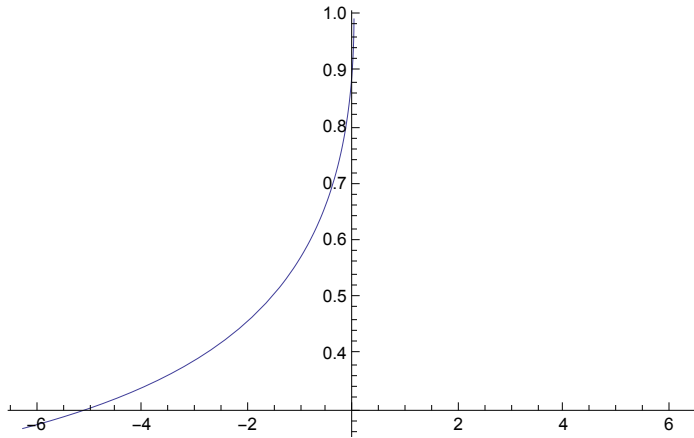
$\text{SphericalPlot3D}\left[e^{\frac{i \text{ArcSin}\left[\frac{\sqrt{4\pi-2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}{2\pi}\right]}{\theta}}\right], \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$



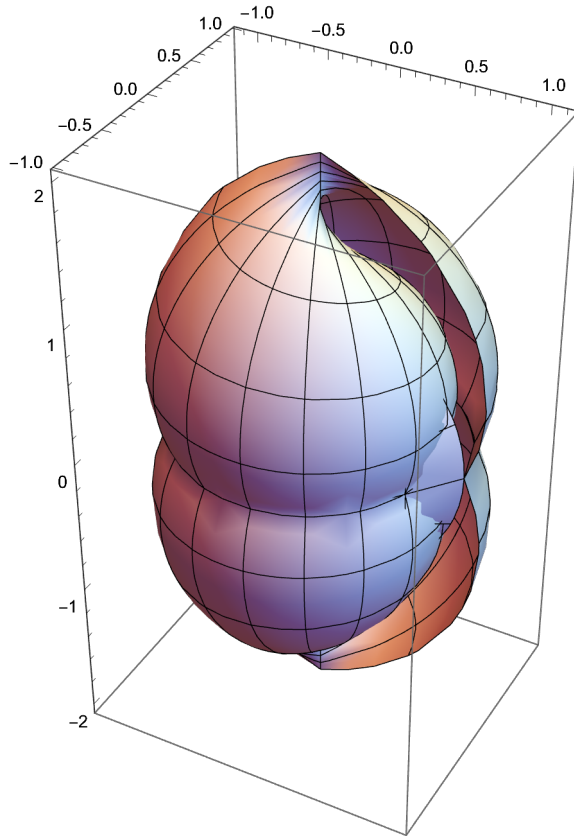
`SphericalPlot3D` $\left[e^{\frac{i \operatorname{ArcSin}\left[\frac{\sqrt{4 \pi-2\left(\pi+\sqrt{\pi^2-\pi^2 \sin [\beta]^2}\right)}{\theta}\right]}{2 \pi}\right]},\{\beta,-\pi, \pi\},\{\theta,-2 \pi, 2 \pi\}\right]$



`Plot` $\left[\frac{i \sqrt{(4 \pi-\theta) \theta}}{2 \pi}+\sqrt{1-\frac{(4 \pi-\theta) \theta}{4 \pi^2}},\{\theta,-2 \pi, 2 \pi\}\right]$

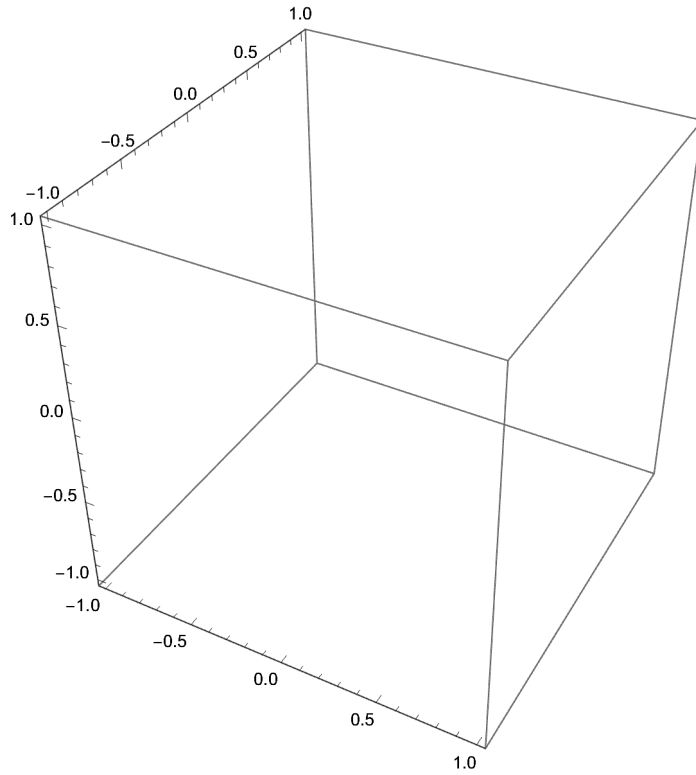


$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$$



SphericalPlot3D $\left[\frac{i \sqrt{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{2 \pi} +$

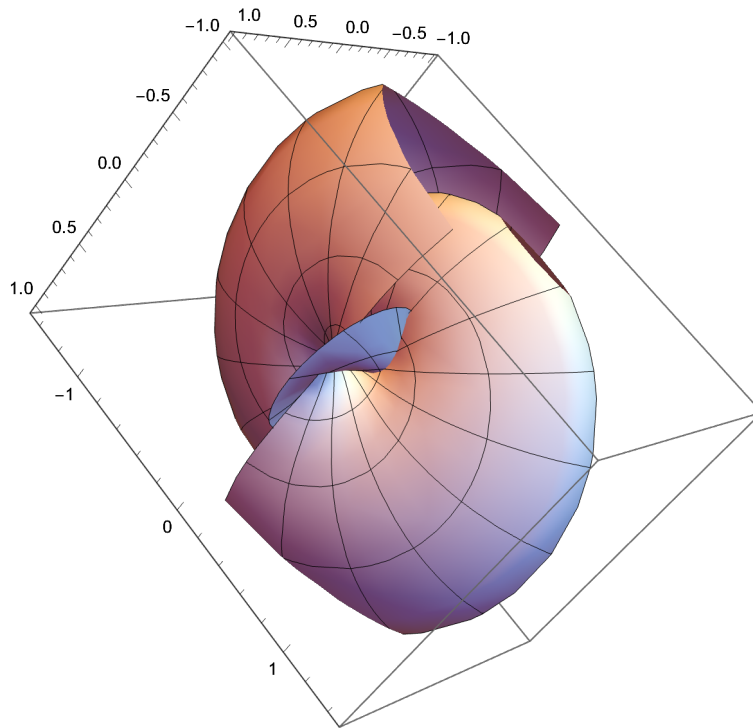
$\sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



SphericalPlot3D[

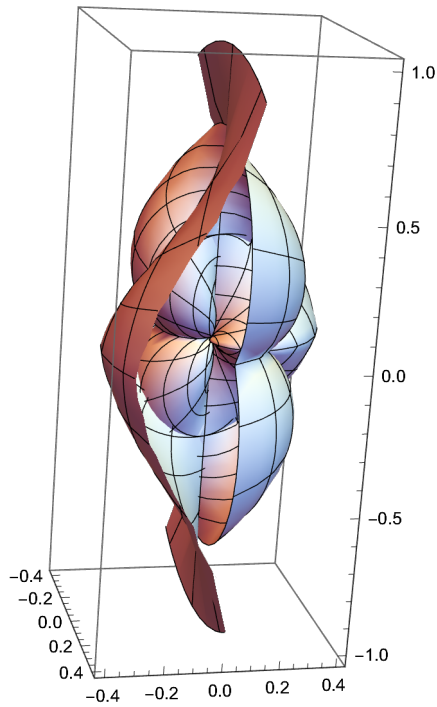
$$\frac{i \sqrt{(4\pi - \theta)\theta}}{2\pi} + \sqrt{1 - \frac{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4\pi^2}},$$

{ $\beta$ ,  $-\pi$ ,  $\pi$ }, { $\theta$ ,  $-2\pi$ ,  $2\pi$ }]



SphericalPlot3D[  

$$\frac{i \sqrt{(4\pi - \theta) \theta}}{2\pi} + \sqrt{1 - \frac{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})) \theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$





$$\text{SphericalPlot3D}\left[\frac{1}{2\pi} \pm \sqrt{\left(\left(4\pi - \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right.}\right.$$

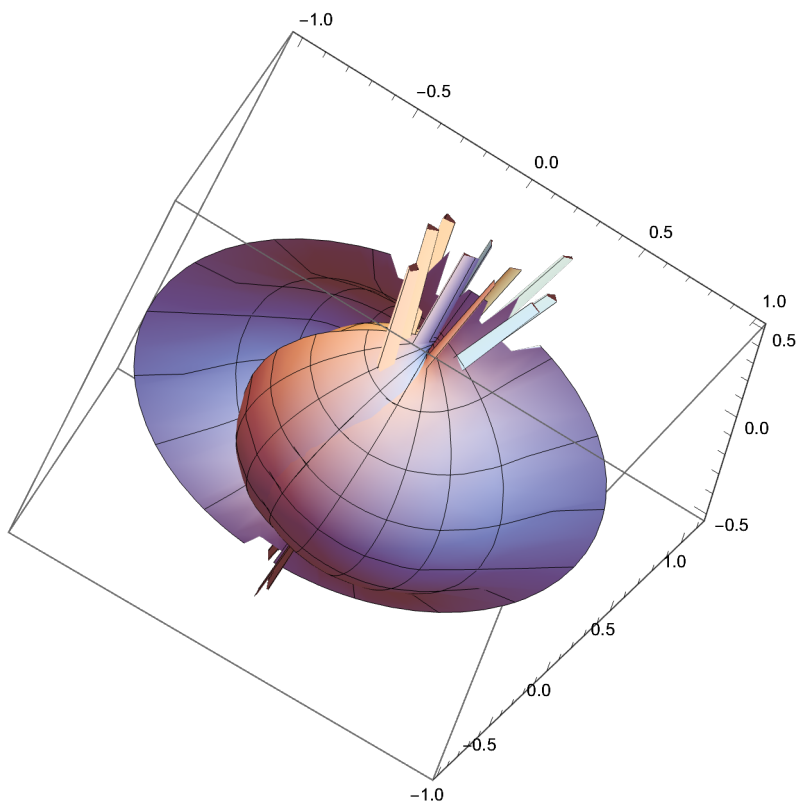
$$\left.\left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right.$$

$$\left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)\theta\right) +$$

$$\sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi,$$

$$2$$

$$\pi\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{1}{2\pi} \pm \sqrt{\left(\left(4\pi - \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right.}\right.$$

$$\left.\left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right.$$

$$\left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)\theta\right) +$$

$$\sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi,$$

$$2$$

$$\pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{i \sqrt{(4 \pi - \theta) \theta}}{2 \pi} + \sqrt{1 - \frac{(4 \pi - \theta) \theta}{4 \pi^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$$

$$\beta = \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]$$

$$e^{\left(i \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right)} =$$

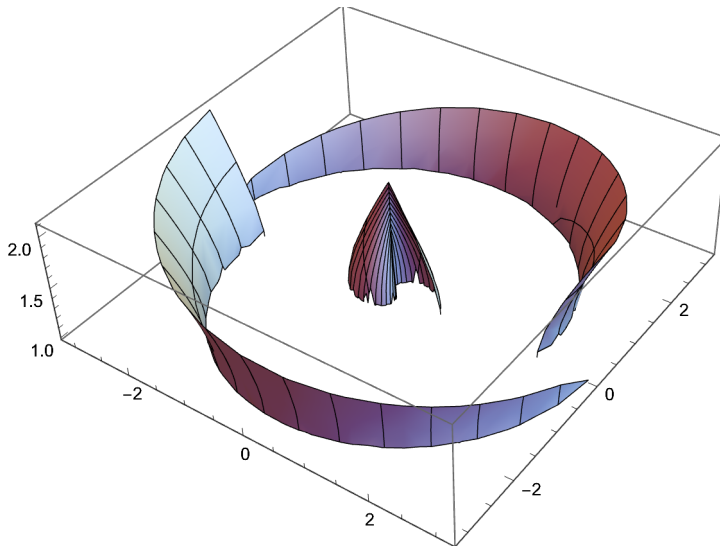
$$\left(\text{Cos}\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right] + i \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right]\right)$$

$$e^{i \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]} = \frac{i \sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} + \sqrt{1 - \frac{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}{4 \pi^2 (-4 \pi + \theta)}}$$

$$\text{RevolutionPlot3D}\left[$$

$$e^{i \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \left(\frac{4 \pi}{3} \frac{-4 \pi^2 + 12 \pi^2 \text{Sin}[\beta]^2}{6 \left(-\pi^2 + 18 \pi^2 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)^3}}{2 \pi \sqrt{-4 \pi + \theta}}}\right]},$$

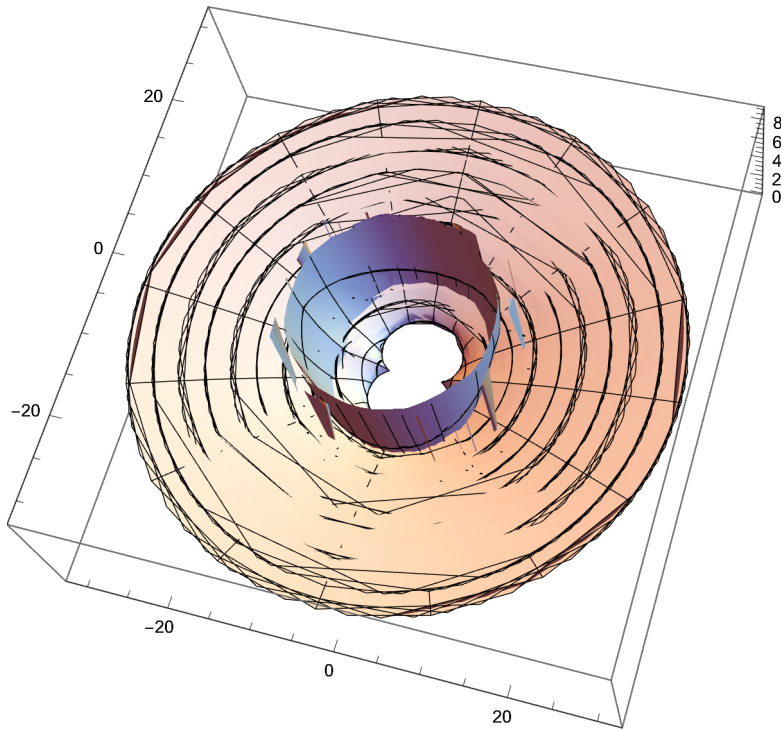
$$\{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



RevolutionPlot3D[

$$e^{i \operatorname{ArcSin}\left[\frac{-4 \pi^2 \theta+4 \pi \theta^2-\left(\frac{4 \pi}{3} \frac{-4 \pi^2+12 \pi^2 \sin [\beta]^2}{6\left(-\pi^3+18 \pi^3 \sin [\beta]^2+3 \sqrt{3} \sqrt{-\pi^6 \sin [\beta]^2+11 \pi^6 \sin [\beta]^4+\pi^6 \sin [\beta]^6}\right)^{1/3}}+\frac{2}{3}\left(-\pi^3+18 \pi^3 \sin [\beta]^2+3 \sqrt{3} \sqrt{-\pi^6 \sin [\beta]^2+11 \pi^6 \sin [\beta]^4+\pi^6 \sin [\beta]^6}\right)^{1/3}\right)}{2 \pi \sqrt{-4 \pi+\theta}}}\right]},$$

{ $\theta$ , -10  $\pi$ , 10  $\pi$ }, { $\beta$ , -5  $\pi$ , 5  $\pi$ }]

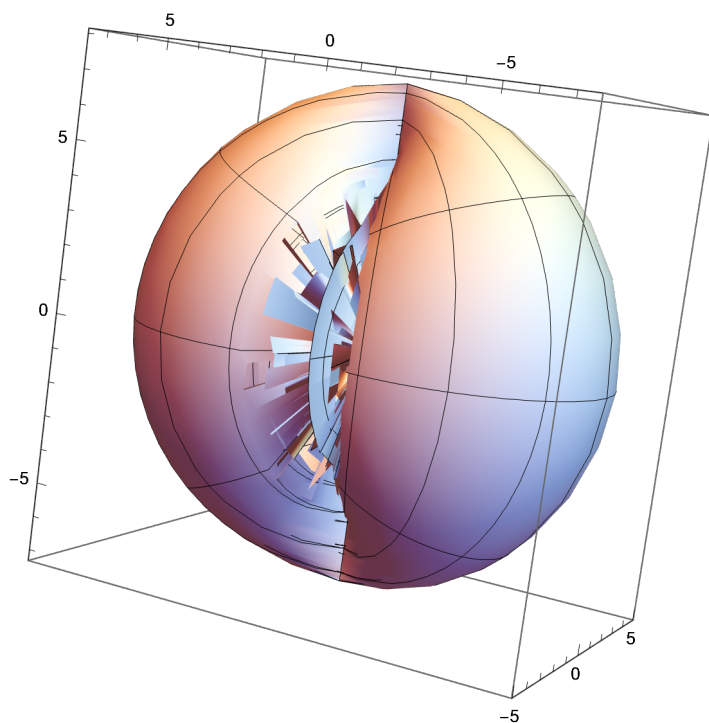


SphericalPlot3D[

$$\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi}\left(\frac{4\pi}{3}-\frac{-4\pi^2+12\pi^2\sin[\beta]^2}{6(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6})^{1/3}}+\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2-\theta^3}{2\pi\sqrt{-4\pi+\left(\frac{4\pi}{3}-\frac{-4\pi^2+12\pi^2\sin[\beta]^2}{6(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6})^{1/3}}+\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2}}\right]$$

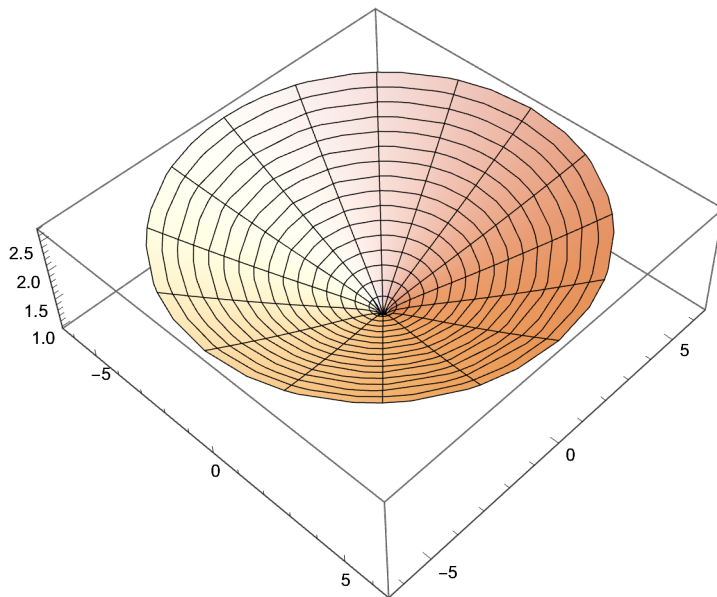
e

{θ, -2 π, 2 π}, {β, -π, π}]

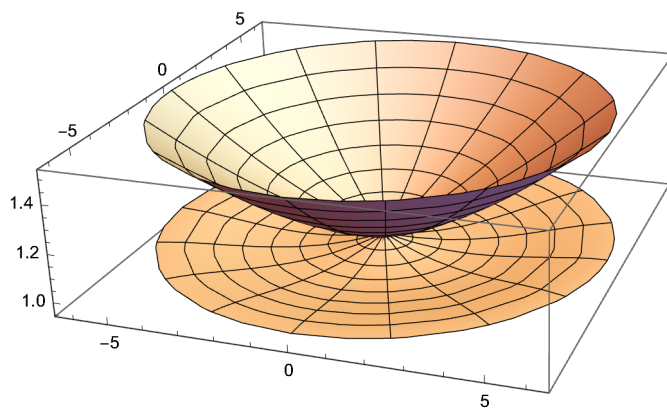


$$\text{RevolutionPlot3D}\left[\frac{\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi}\left(\frac{4\pi}{3}-\frac{-4\pi^2+12\pi^2\sin[\beta]^2}{6(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6})^{1/3}}+\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2-\theta^3}{2\pi\sqrt{-4\pi+\left(\frac{4\pi}{3}-\frac{-4\pi^2+12\pi^2\sin[\beta]^2}{6(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6})^{1/3}}+\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{5}-\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2}}\right]}{2\pi\sqrt{-4\pi+\theta}}, \sqrt{1-\frac{-4\pi^2\theta+4\pi\theta^2-\theta^3}{4\pi^2(-4\pi+\theta)}}}, \{\theta, -2\pi, 2\pi\}]$$

$$\text{RevolutionPlot3D}\left[\frac{\mathbf{i} \sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}} + \sqrt{1 - \frac{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}{4 \pi^2 (-4 \pi + \theta)}}, \{\theta, -2 \pi, 2 \pi\}\right]$$



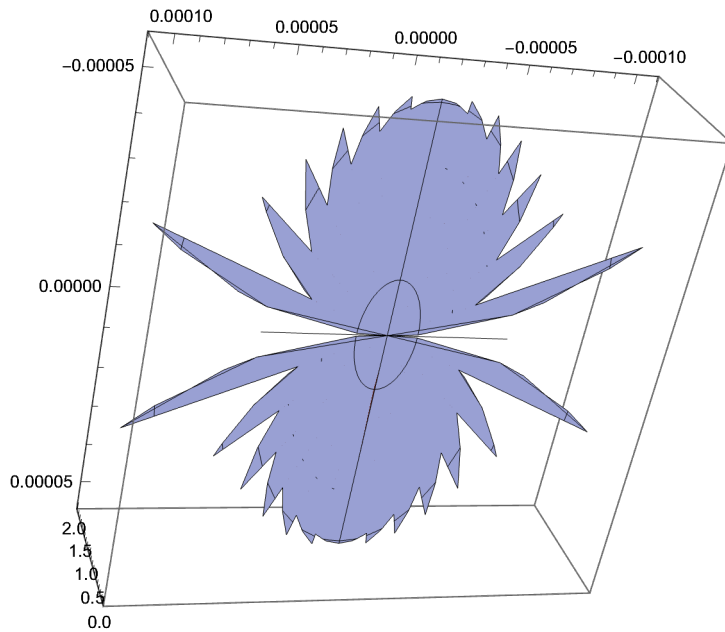
$$\text{RevolutionPlot3D}\left[\sqrt{1 - \frac{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}{4 \pi^2 (-4 \pi + \theta)}}, \{\theta, -2 \pi, 2 \pi\}\right]$$

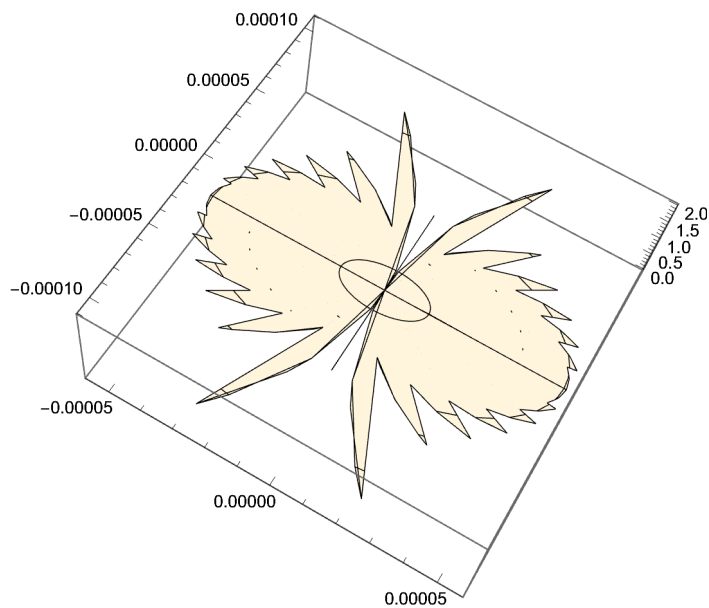


$$e^{\mathbf{i} \theta} = \cos[\theta] + \mathbf{i} \sin[\theta]$$

$$\theta \rightarrow \frac{4 \pi}{3} - \left(-4 \pi^2 + 12 \pi^2 \sin[\beta]^2\right) / \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}$$

$$\theta = 2 \left(\pi \pm \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)$$

$$\text{RevolutionPlot3D}\left[\text{e}^{\text{i} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)}, \{\beta, -\pi, \pi\}\right]$$


$$\text{RevolutionPlot3D}\left[\text{e}^{\text{i} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)}, \{\beta, -\pi, \pi\}\right]$$


$$\text{Solve}\left[\text{e}^{\text{i} \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \frac{\text{i} \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{(4\pi-\theta)\theta}{4\pi^2}}, \theta\right]$$

$$\text{Solve}\left[\text{e}^{\text{i} \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \frac{\text{i} \sqrt{(4\pi-\theta)\theta}}{2\pi} + \sqrt{1 - \frac{u^2}{c^2}}, \theta\right]$$

$$\text{Solve}\left[e^{\frac{i}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} = \sqrt{1 - \frac{u^2}{c^2}} + \frac{i\sqrt{(4\pi-\theta)\theta}}{2\pi}, u\right]$$

$$\left\{\left\{u \rightarrow -\frac{1}{2\pi} \left( \sqrt{4c^2\pi^2 - 4c^2e^{2i\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi^2 + 4c^2\pi\theta - c^2\theta^2 + 4ic^2e^{\frac{i}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi\sqrt{(4\pi-\theta)\theta}} \right) \right\}, \right.$$

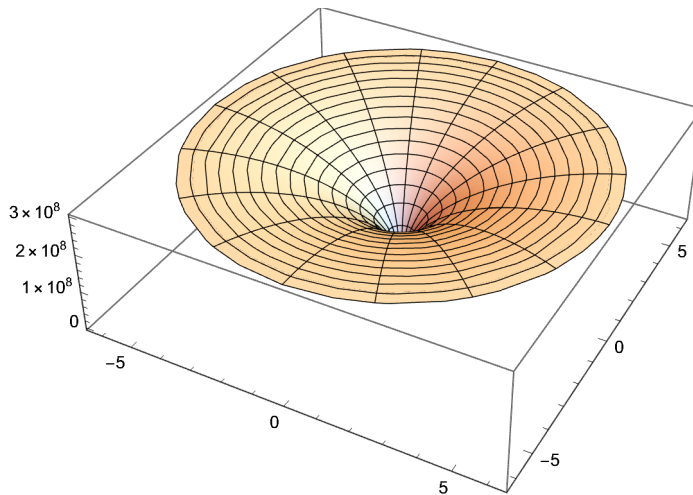
$$\left. \left\{u \rightarrow \frac{1}{2\pi} \left( \sqrt{4c^2\pi^2 - 4c^2e^{2i\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi^2 + 4c^2\pi\theta - c^2\theta^2 + 4ic^2e^{\frac{i}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi\sqrt{(4\pi-\theta)\theta}} \right) \right\} \right\}$$

$$\text{Solve}\left[(4\pi-\theta)\theta = -\frac{1}{2\pi} \left( \sqrt{4c^2\pi^2 - 4c^2e^{2i\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi^2 + 4c^2\pi\theta - c^2\theta^2 + 4ic^2e^{\frac{i}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi\sqrt{(4\pi-\theta)\theta}} \right), \theta\right]$$

$$\text{Solve}\left[(4\pi-\theta)\theta = -\frac{1}{2\pi} \left( \sqrt{4c^2\pi^2 - 4c^2e^{2i\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi^2 + 4c^2\pi\theta - c^2\theta^2 + 4ic^2e^{\frac{i}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi\sqrt{(4\pi-\theta)\theta}} \right), \theta\right]$$

RevolutionPlot3D[

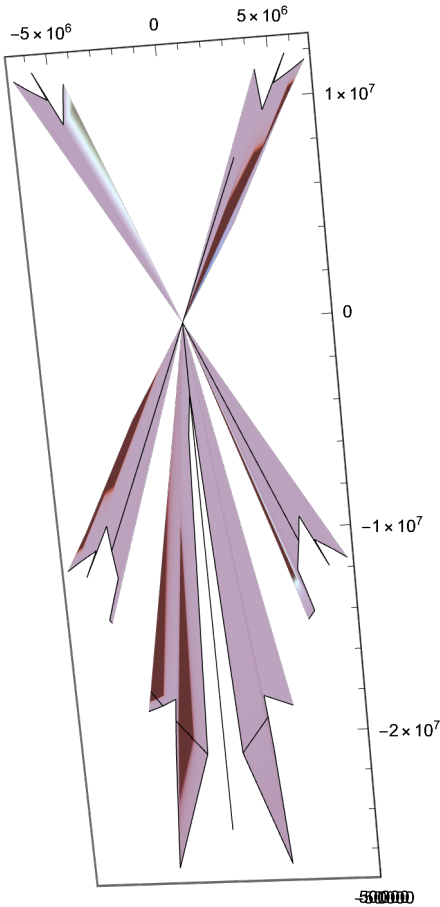
$$\frac{1}{2\pi} \left( \sqrt{4(2.99792458 \times 10^8)^2\pi^2 - 4(2.99792458 \times 10^8)^2e^{2i\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi^2 + 4(2.99792458 \times 10^8)^2\pi\theta - (2.99792458 \times 10^8)^2\theta^2 + 4i(2.99792458 \times 10^8)^2e^{\frac{i}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}\pi\sqrt{(4\pi-\theta)\theta}} \right), \{\theta, -2\pi, 2\pi\}]$$



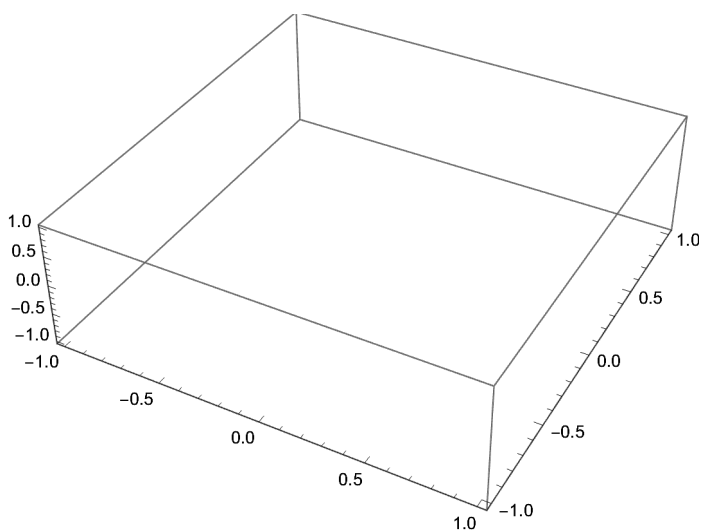
$$\begin{aligned}
\theta = & \left\{ \left\{ \theta \rightarrow \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right\} / \right. \\
& \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
& \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right\}, \\
& \left\{ \theta \rightarrow \frac{4\pi}{3} + \left( (1 + i\sqrt{3}) (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right\} / \\
& \left( 12 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \\
& \left( 1 - i\sqrt{3} \right) \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right\}, \\
& \left\{ \theta \rightarrow \frac{4\pi}{3} + \left( (1 - i\sqrt{3}) (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right\} / \\
& \left( 12 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \\
& \left( 1 + i\sqrt{3} \right) \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right\} \}
\end{aligned}$$



$$\text{SphericalPlot3D}\left[\frac{1}{2\pi}\sqrt{4\left(2.99792458\cdot10^8\right)^2\pi^2-4\left(2.99792458\cdot10^8\right)^2}\right.\\ \left. e^{2i\text{ArcSin}\left[\frac{\sqrt{\left(4\pi-\frac{4\pi}{3}\frac{-4\pi^2+12\pi^2\text{Sin}[\beta]^2}{6\left(-\pi^3+18\pi^3\text{Sin}[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\text{Sin}[\beta]^2+11\pi^6\text{Sin}[\beta]^4+\pi^6\text{Sin}[\beta]^6}\right)^{1/3}+\frac{2}{3}\left(-\pi^3+18\pi^3\text{Sin}[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\text{Sin}[\beta]^2+11\pi^6\text{Sin}[\beta]^4+\pi^6\text{Sin}[\beta]^6}\right)^{1/3}\right)\theta}}{2\pi}}\right]}\right.\\ \left.\pi^2+4\left(2.99792458\cdot10^8\right)^2\pi\theta-\left(2.99792458\cdot10^8\right)^2\theta^2+4i\left(2.99792458\cdot10^8\right)^2e^{i\text{ArcSin}\left[\frac{\sqrt{\left(4\pi-\theta\right)\theta}}{2\pi}\right]}\pi\sqrt{\left(4\pi-\theta\right)\theta}\right),\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi}\right]$$



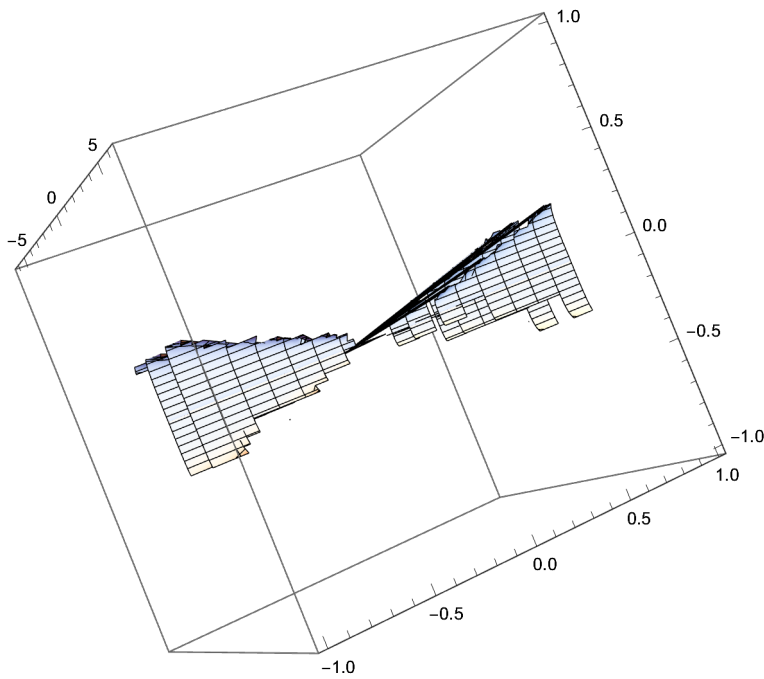
$$\text{RevolutionPlot3D}\left[\frac{1}{2\pi}\left(\sqrt{4(2.99792458 \cdot 10^8)^2 \pi^2 - 4(2.99792458 \cdot 10^8)^2}\right.\right. \\ \left.\left.e^{2i \text{ArcSin}\left[\frac{\sqrt{\left(4\pi - \frac{4\pi}{3} + \frac{(1+i\sqrt{3})(-4\pi^2 + 12\pi^2 \sin[\beta]^2)}{12(-\pi^3 + 10\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3} - \frac{1}{3}(1-i\sqrt{3})(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})\right)}}{2\pi}\right]}\right.\right. \\ \left.\left.\pi^2 + 4(2.99792458 \cdot 10^8)^2 \pi \theta - (2.99792458 \cdot 10^8)^2 \theta^2 + \right.\right. \\ \left.\left.4i(2.99792458 \cdot 10^8)^2 e^{i \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]} \pi \sqrt{(4\pi - \theta)\theta}\right), \{\theta, -2\pi, 2\pi\}\right]$$



$$\begin{aligned}
\theta = & \left\{ \left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \right. \right. \\
& \left. \left. \frac{2\pi \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3r^2} \right\}, \right. \\
& \left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{\left( 1 + \mathfrak{i} \sqrt{3} \right) \left( -4\pi^2 r^4 + 12\pi^2 r^2 \eta^2 \right)}{12\pi r^2 \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} + \right. \\
& \left. \frac{\left( 1 - \mathfrak{i} \sqrt{3} \right) \pi \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3r^2} \right\}, \\
& \left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{\left( 1 - \mathfrak{i} \sqrt{3} \right) \left( -4\pi^2 r^4 + 12\pi^2 r^2 \eta^2 \right)}{12\pi r^2 \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} + \right. \\
& \left. \frac{\left( 1 + \mathfrak{i} \sqrt{3} \right) \pi \left( r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3r^2} \right\} \}
\end{aligned}$$

ContourPlot3D[

$$\frac{1}{2\pi} \left( \sqrt{\left( 4 (2.99792458 * 10^8)^2 \pi^2 - 4 (2.99792458 * 10^8)^2 e^{2i \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} \pi^2 + \right.} \right. \\ \left. 4 (2.99792458 * 10^8)^2 \pi \theta - \right. \\ \left. (2.99792458 * 10^8)^2 \left( \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6})^{1/3}} - \right. \right. \\ \left. \left. \frac{2\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6})^{1/3}}{3r^2} \right)^2 \right. + \\ \left. \left. 4i (2.99792458 * 10^8)^2 e^{i \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]} \pi \sqrt{(4\pi-\theta)\theta} \right) \right), \\ \{\theta, -2\pi, 2\pi\}, \{r, -1, 1\}, \{\eta, -1, 1\}]$$



$$\begin{aligned}
& 2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \quad \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \quad \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \\
& \quad \left. \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \right) = \\
& \quad \frac{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \wedge 2 \right)}{\frac{\theta}{2 \pi}} = \frac{\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}}{\frac{\theta}{2 \pi}} \\
r & := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}
\end{aligned}$$

$$\begin{aligned}
& \text{Solve} \left[ \frac{\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}}{\frac{\theta}{2 \pi}} == \right. \\
& 2 \pi \left( - \frac{256 \pi^7 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \frac{320 \pi^6 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \frac{128 \pi^5 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \frac{16 \pi^4 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^3 - 448 \pi^4 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^4 + \right.} \right. \\
& \left. 304 \pi^3 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^5 - 100 \pi^2 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^6 + \right. \\
& \left. 16 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^7 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^8 \right) \Bigg) / \\
& \left. \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \right], \eta]
\end{aligned}$$

$$\left\{ \left\{ \eta \rightarrow \frac{1}{2\pi} \theta \sqrt{4\pi\theta - \theta^2} \right. \right.$$

$$\left( - \frac{64 \pi^5 \theta^2 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right.$$

$$\frac{80 \pi^4 \theta^3 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} -$$

$$\frac{32 \pi^3 \theta^4 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} +$$

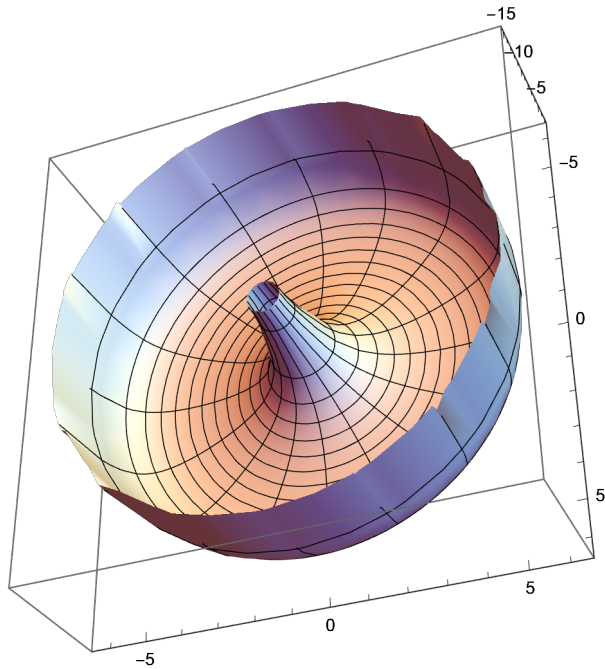
$$\frac{4 \pi^2 \theta^5 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} +$$

$$\left( 128 \pi^6 \sqrt{\left( 16 \pi \theta^3 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)^2 - 28 \theta^4 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)^2 + \frac{19 \theta^5 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)^2}{\pi} - \right.} \right.$$

$$\left. \left. \frac{25 \theta^6 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)^2}{4 \pi^2} + \frac{\theta^7 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)^2}{\pi^3} - \frac{\theta^8 \left( \frac{16 \pi^3}{4\pi-\theta} - \frac{4 \pi^2 \theta}{4\pi-\theta} \right)^2}{16 \pi^4} \right) \right) /$$

$$\left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \left. \right\} \left. \right\}$$

$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\frac{1}{2\pi}\theta\sqrt{4\pi\theta-\theta^2}\right. \\
& \left(-\frac{64\pi^5\theta^2\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+\right. \\
& \frac{80\pi^4\theta^3\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}- \\
& \frac{32\pi^3\theta^4\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+ \\
& \left.\frac{4\pi^2\theta^5\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+\right. \\
& \left(128\pi^6\sqrt{\left(16\pi\theta^3\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)^2-28\theta^4\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)^2+\frac{19\theta^5\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)^2}{\pi}-\right.}\right. \\
& \left.\frac{25\theta^6\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)^2}{4\pi^2}+\frac{\theta^7\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)^2}{\pi^3}-\frac{\theta^8\left(\frac{16\pi^3}{4\pi-\theta}-\frac{4\pi^2\theta}{4\pi-\theta}\right)^2}{16\pi^4}\right)\left/\left(-1024\pi^7\theta^4+\right.\right. \\
& \left.\left.1280\pi^6\theta^5-512\pi^5\theta^6+80\pi^4\theta^7-32\pi^3\theta^8+24\pi^2\theta^9-8\pi\theta^{10}+\theta^{11}\right)\right],\{\theta,-2\pi,2\pi\}]
\end{aligned}$$

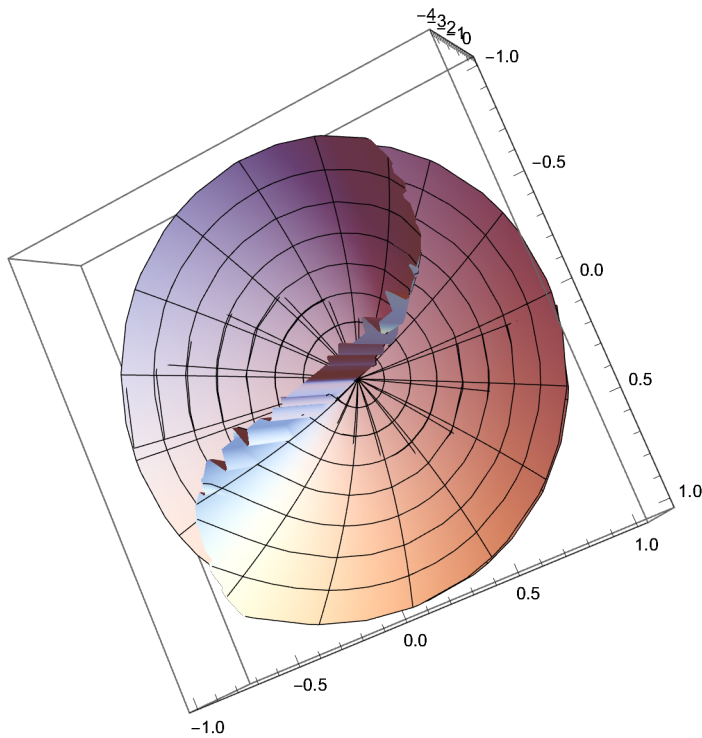




$$\begin{aligned}
& \text{Solve} \left[ \frac{\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}}{\frac{\theta}{2 \pi}} == \right. \\
& 2 \pi \left( - \frac{256 \pi^7 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \frac{320 \pi^6 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \frac{128 \pi^5 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \frac{16 \pi^4 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^3 - 448 \pi^4 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^4 + \right.} \right. \\
& \quad 304 \pi^3 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^5 - 100 \pi^2 \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^6 + \\
& \quad \left. \left. 16 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^7 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^4 \theta^8 \right) \right) / \\
& \left. \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right), \eta \right]
\end{aligned}$$

$$\left\{ \left\{ \eta \rightarrow \frac{1}{2\pi} \theta \sqrt{4\pi\theta - \theta^2} \right. \right. \\
\left( -\frac{64\pi^5\theta^2(4\pi r^2\theta - r^2\theta^2)}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \right. \\
\frac{80\pi^4\theta^3(4\pi r^2\theta - r^2\theta^2)}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} - \\
\frac{32\pi^3\theta^4(4\pi r^2\theta - r^2\theta^2)}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\
\frac{4\pi^2\theta^5(4\pi r^2\theta - r^2\theta^2)}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\
\left. \left( 128\pi^6 \sqrt{\left( 16\pi\theta^3(4\pi r^2\theta - r^2\theta^2)^2 - 28\theta^4(4\pi r^2\theta - r^2\theta^2)^2 + \frac{19\theta^5(4\pi r^2\theta - r^2\theta^2)^2}{\pi} - \right. \right. \right. \\
\left. \left. \frac{25\theta^6(4\pi r^2\theta - r^2\theta^2)^2}{4\pi^2} + \frac{\theta^7(4\pi r^2\theta - r^2\theta^2)^2}{\pi^3} - \frac{\theta^8(4\pi r^2\theta - r^2\theta^2)^2}{16\pi^4} \right) \right) / \\
\left. \left. \left( -1024\pi^7\theta^4 + 1280\pi^6\theta^5 - 512\pi^5\theta^6 + 80\pi^4\theta^7 - 32\pi^3\theta^8 + 24\pi^2\theta^9 - 8\pi\theta^{10} + \theta^{11} \right) \right\} \right\}$$

$$\begin{aligned}
 & \text{RevolutionPlot3D}\left[\frac{1}{2\pi}\theta\sqrt{4\pi\theta-\theta^2}\right. \\
 & \left(-\frac{64\pi^5\theta^2(4\pi r^2\theta-r^2\theta^2)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+\right. \\
 & \frac{80\pi^4\theta^3(4\pi r^2\theta-r^2\theta^2)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}- \\
 & \frac{32\pi^3\theta^4(4\pi r^2\theta-r^2\theta^2)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+ \\
 & \frac{4\pi^2\theta^5(4\pi r^2\theta-r^2\theta^2)}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+ \\
 & \left.128\pi^6\sqrt{\left(16\pi\theta^3(4\pi r^2\theta-r^2\theta^2)^2-28\theta^4(4\pi r^2\theta-r^2\theta^2)^2+\frac{19\theta^5(4\pi r^2\theta-r^2\theta^2)^2}{\pi}-\right.}\right. \\
 & \left.\left.\frac{25\theta^6(4\pi r^2\theta-r^2\theta^2)^2}{4\pi^2}+\frac{\theta^7(4\pi r^2\theta-r^2\theta^2)^2}{\pi^3}-\frac{\theta^8(4\pi r^2\theta-r^2\theta^2)^2}{16\pi^4}\right)\right)/ \\
 & \left.(-1024\pi^7\theta^4+1280\pi^6\theta^5-512\pi^5\theta^6+80\pi^4\theta^7-32\pi^3\theta^8+24\pi^2\theta^9-8\pi\theta^{10}+\theta^{11})\right], \\
 & \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}
 \end{aligned}$$



$$\begin{aligned}
& \frac{1}{\frac{\theta}{2\pi}} \left( \left( \sqrt{-(256\pi^7\eta^2\theta^3)} / \right. \right. \\
& \quad \left( -1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10} \right) + \\
& \quad \left( 320\pi^6\eta^2\theta^4 \right) / \left( -1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + \right. \\
& \quad \left. 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10} \right) - \left( 128\pi^5\eta^2\theta^5 \right) / \left( -1024\pi^7\theta^3 + 1280\pi^6\theta^4 - \right. \\
& \quad \left. 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10} \right) + \left( 16\pi^4\eta^2\theta^6 \right) / \\
& \quad \left( -1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10} \right) + \\
& \quad \left. \left( 128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)} \right) / \right. \\
& \quad \left. \left( -1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10} \right) \right) \right)^2 \\
& 2\pi \left( -\frac{1}{\theta} \frac{256\pi^7\eta^2\theta^3}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \right. \\
& \quad \frac{1}{\theta} \frac{320\pi^6\eta^2\theta^4}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} - \\
& \quad \frac{1}{\theta} \frac{128\pi^5\eta^2\theta^5}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\
& \quad \frac{1}{\theta} \frac{16\pi^4\eta^2\theta^6}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\
& \quad \left. \frac{1}{\theta} \left( 128\pi^6\sqrt{256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8} \right) / \right. \\
& \quad \left. \left( -1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10} \right) \right) \\
& 2\pi \left( -\frac{256\pi^7\eta^2\theta^2}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \right. \\
& \quad \frac{320\pi^6\eta^2\theta^3}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} - \\
& \quad \frac{128\pi^5\eta^2\theta^4}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\
& \quad \frac{16\pi^4\eta^2\theta^5}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\
& \quad \left. \frac{128\pi^6\sqrt{256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8}}{\theta(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10})} \right)
\end{aligned}$$

$$\begin{aligned}
& 2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \left( -1024 \right. \right. \\
& \left. \left. \pi^7 \theta \theta^3 + 1280 \pi^6 \theta \theta^4 - 512 \pi^5 \theta \theta^5 + 80 \pi^4 \theta \theta^6 - 32 \pi^3 \theta \theta^7 + 24 \pi^2 \theta \theta^8 - 8 \pi \theta \theta^9 + \theta \theta^{10} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Solve} \left[ 2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \right. \\
& \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \\
& \left. \left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + x \right) \right] = \frac{r^2}{\frac{\theta}{2 \pi}}, x]
\end{aligned}$$

$$\begin{aligned}
& \left\{ \left\{ x \rightarrow \left( -262144 \pi^{12} r^2 \theta^4 + 65536 \pi^{12} \eta^2 \theta^4 + 393216 \pi^{11} r^2 \theta^5 - \right. \right. \right. \\
& 98304 \pi^{11} \eta^2 \theta^5 - 212992 \pi^{10} r^2 \theta^6 + 53248 \pi^{10} \eta^2 \theta^6 + 57344 \pi^9 r^2 \theta^7 - \\
& 13312 \pi^9 \eta^2 \theta^7 - 22528 \pi^8 r^2 \theta^8 + 3328 \pi^8 \eta^2 \theta^8 + 16384 \pi^7 r^2 \theta^9 - 2048 \pi^7 \eta^2 \theta^9 - \\
& 7232 \pi^6 r^2 \theta^{10} + 896 \pi^6 \eta^2 \theta^{10} + 1472 \pi^5 r^2 \theta^{11} - 128 \pi^5 \eta^2 \theta^{11} - 304 \pi^4 r^2 \theta^{12} + \\
& 160 \pi^3 r^2 \theta^{13} - 56 \pi^2 r^2 \theta^{14} + 8 \pi r^2 \theta^{15} - 32768 \pi^{11} \theta \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} + \\
& 8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} + 512 \pi^8 \theta^4 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} - \\
& 512 \pi^7 \theta^5 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} + 128 \pi^6 \theta^6 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} \left. \right) / \right. \\
& \left. \left( -256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5 \right) \right\} \}
\end{aligned}$$

Solve[

$$\begin{aligned}
 x == & \left( -262\,144\,\pi^{12}\,r^2\,\theta^4 + 65\,536\,\pi^{12}\,\eta^2\,\theta^4 + 393\,216\,\pi^{11}\,r^2\,\theta^5 - 98\,304\,\pi^{11}\,\eta^2\,\theta^5 - 212\,992\,\pi^{10}\,r^2\,\theta^6 + \right. \\
 & 53\,248\,\pi^{10}\,\eta^2\,\theta^6 + 57\,344\,\pi^9\,r^2\,\theta^7 - 13\,312\,\pi^9\,\eta^2\,\theta^7 - 22\,528\,\pi^8\,r^2\,\theta^8 + \\
 & 3328\,\pi^8\,\eta^2\,\theta^8 + 16\,384\,\pi^7\,r^2\,\theta^9 - 2048\,\pi^7\,\eta^2\,\theta^9 - 7232\,\pi^6\,r^2\,\theta^{10} + \\
 & 896\,\pi^6\,\eta^2\,\theta^{10} + 1472\,\pi^5\,r^2\,x - 128\,\pi^5\,\eta^2\,x - 304\,\pi^4\,r^2\,\theta^{12} + 160\,\pi^3\,r^2\,\theta^{13} - \\
 & 56\,\pi^2\,r^2\,\theta^{14} + 8\,\pi\,r^2\,\theta^{15} - 32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + \\
 & 8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} - \\
 & \left. 512\,\pi^7\,\theta^5\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} + 128\,\pi^6\,\theta^6\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3} \right) / \\
 & (-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5), x]
 \end{aligned}$$

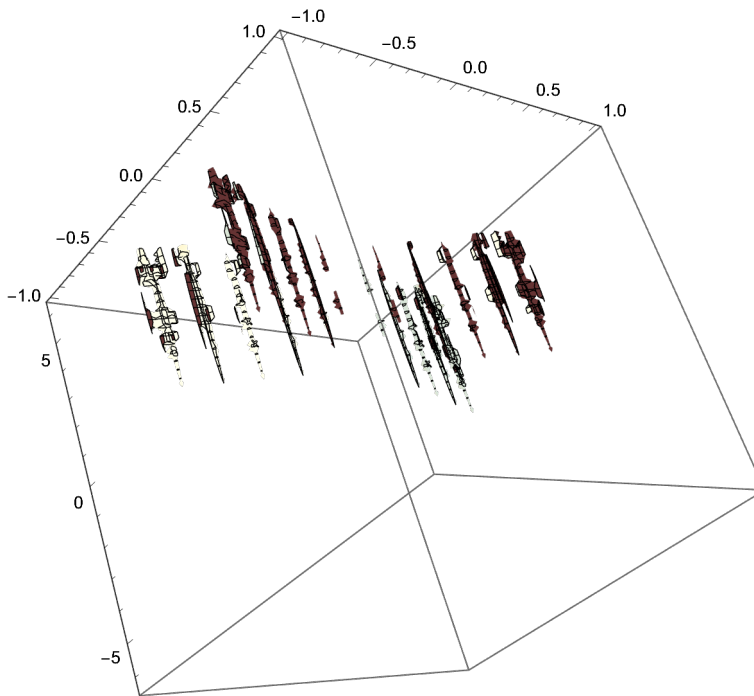
$$\begin{aligned}
 \left\{ \left\{ x \rightarrow \right. \right. & - \frac{262\,144\,\pi^{12}\,r^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{65\,536\,\pi^{12}\,\eta^2\,\theta^4}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{393\,216\,\pi^{11}\,r^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{98\,304\,\pi^{11}\,\eta^2\,\theta^5}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
 & \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
 & \left. \left. \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{7232 \pi^6 r^2 \theta^{10}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{896 \pi^6 \eta^2 \theta^{10}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{304 \pi^4 r^2 \theta^{12}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{160 \pi^3 r^2 \theta^{13}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{56 \pi^2 r^2 \theta^{14}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8 \pi r^2 \theta^{15}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{32768 \pi^{11} \theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right) \Bigg\} \Bigg\} \\
& \text{ContourPlot3D} \left[ \left( - \frac{262144 \pi^{12} r^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \right. \\
& \frac{65536 \pi^{12} \eta^2 \theta^4}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{393216 \pi^{11} r^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} - \\
& \left. \frac{98304 \pi^{11} \eta^2 \theta^5}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right)
\end{aligned}$$

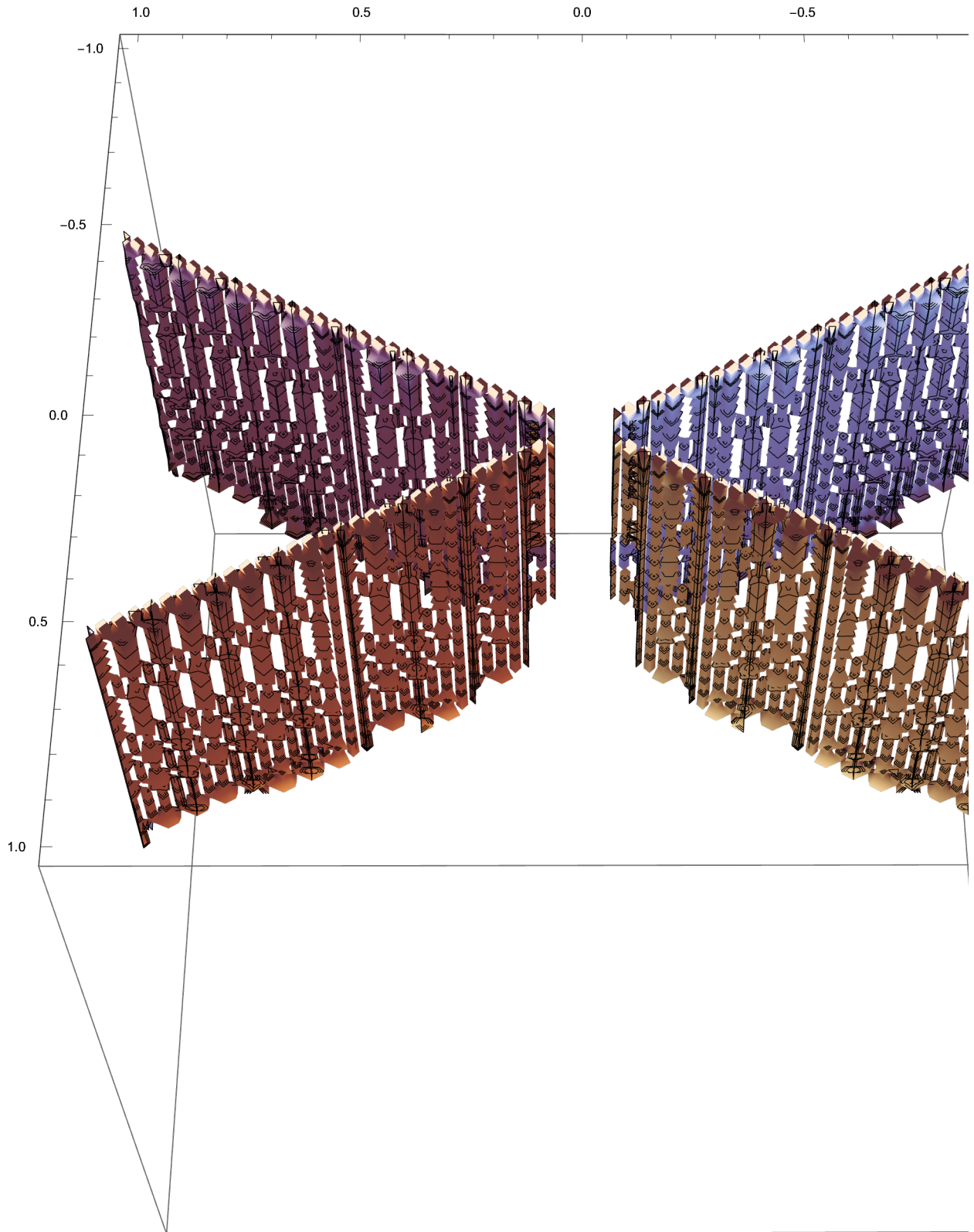
$$\begin{aligned}
& \frac{212\,992\,\pi^{10}\,r^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{53\,248\,\pi^{10}\,\eta^2\,\theta^6}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{57\,344\,\pi^9\,r^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{13\,312\,\pi^9\,\eta^2\,\theta^7}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{22\,528\,\pi^8\,r^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{3328\,\pi^8\,\eta^2\,\theta^8}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{16\,384\,\pi^7\,r^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{2048\,\pi^7\,\eta^2\,\theta^9}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{7232\,\pi^6\,r^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{896\,\pi^6\,\eta^2\,\theta^{10}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{304\,\pi^4\,r^2\,\theta^{12}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{160\,\pi^3\,r^2\,\theta^{13}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{56\,\pi^2\,r^2\,\theta^{14}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8\,\pi\,r^2\,\theta^{15}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} - \\
& \frac{32\,768\,\pi^{11}\,\theta\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{8192\,\pi^{10}\,\theta^2\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} + \\
& \frac{512\,\pi^8\,\theta^4\,\sqrt{\eta^4\,(2\pi-\theta)^2\,(4\pi-\theta)^3\,\theta^3}}{-256\,\pi^5\,r^2 + 64\,\pi^5\,\eta^2 + 64\,\pi^4\,r^2\,\theta - 16\,\pi^4\,\eta^2\,\theta + 4\,\pi^2\,r^2\,\theta^3 - 4\,\pi\,r^2\,\theta^4 + r^2\,\theta^5} -
\end{aligned}$$



$$\begin{aligned}
& \frac{512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \\
& \frac{128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3}}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \Bigg) / \\
& \left( 1 - \frac{1472 \pi^5 r^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} + \right. \\
& \left. \frac{128 \pi^5 \eta^2}{-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5} \right), \\
& \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\} \Big]
\end{aligned}$$



$$\begin{aligned}
& \text{ContourPlot3D} \Big[ \\
& \left( -262144 \pi^{12} r^2 \theta^4 + 65536 \pi^{12} \eta^2 \theta^4 + 393216 \pi^{11} r^2 \theta^5 - 98304 \pi^{11} \eta^2 \theta^5 - 212992 \pi^{10} r^2 \theta^6 + \right. \\
& 53248 \pi^{10} \eta^2 \theta^6 + 57344 \pi^9 r^2 \theta^7 - 13312 \pi^9 \eta^2 \theta^7 - 22528 \pi^8 r^2 \theta^8 + \\
& 3328 \pi^8 \eta^2 \theta^8 + 16384 \pi^7 r^2 \theta^9 - 2048 \pi^7 \eta^2 \theta^9 - 7232 \pi^6 r^2 \theta^{10} + \\
& 896 \pi^6 \eta^2 \theta^{10} + 1472 \pi^5 r^2 \theta^{11} - 128 \pi^5 \eta^2 \theta^{11} - 304 \pi^4 r^2 \theta^{12} + 160 \pi^3 r^2 \theta^{13} - \\
& 56 \pi^2 r^2 \theta^{14} + 8 \pi r^2 \theta^{15} - 32768 \pi^{11} \theta \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + \\
& 8192 \pi^{10} \theta^2 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + 512 \pi^8 \theta^4 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} - \\
& \left. 512 \pi^7 \theta^5 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} + 128 \pi^6 \theta^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} \right) / \\
& (-256 \pi^5 r^2 + 64 \pi^5 \eta^2 + 64 \pi^4 r^2 \theta - 16 \pi^4 \eta^2 \theta + 4 \pi^2 r^2 \theta^3 - 4 \pi r^2 \theta^4 + r^2 \theta^5), \\
& \{\eta, -1, 1\}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} \Big]
\end{aligned}$$



$$\begin{aligned}
& \text{Factor} \left[ \frac{1}{\theta} 2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \right. \\
& \quad \frac{320 \pi^6 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \quad \frac{128 \pi^5 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \frac{16 \pi^4 \eta^2 \theta^6}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \\
& \quad \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right] \\
& \frac{32 \pi^5 \left( 16 \pi^3 \eta^2 \theta^3 - 20 \pi^2 \eta^2 \theta^4 + 8 \pi \eta^2 \theta^5 - \eta^2 \theta^6 - 8 \pi^2 \sqrt{\eta^4 (2 \pi - \theta)^2 (4 \pi - \theta)^3 \theta^3} \right)}{(2 \pi - \theta)^2 \theta^4 (256 \pi^5 - 64 \pi^4 \theta - 4 \pi^2 \theta^3 + 4 \pi \theta^4 - \theta^5)} \\
& 2 \pi \left( - \frac{1}{\theta} \frac{256 \pi^7 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \quad \frac{1}{\theta} \frac{320 \pi^6 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \quad \frac{1}{\theta} \frac{128 \pi^5 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \frac{1}{\theta} \frac{16 \pi^4 \eta^2 \theta^6}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \left. \frac{1}{\theta} \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \\
& \quad \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& 2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \quad \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \quad \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \left( -1024 \right. \right. \\
& \quad \left. \left. \pi^7 \theta \theta^3 + 1280 \pi^6 \theta \theta^4 - 512 \pi^5 \theta \theta^5 + 80 \pi^4 \theta \theta^6 - 32 \pi^3 \theta \theta^7 + 24 \pi^2 \theta \theta^8 - 8 \pi \theta \theta^9 + \theta \theta^{10} \right) \right) \\
& 2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\
& \quad \frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \quad \frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \quad \left. \frac{128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8}}{-1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11}} \right)
\end{aligned}$$

RevolutionPlot3D[  

$$2 \pi \left( - \frac{256 \pi^7 \eta^2 \theta^2}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right.$$
  

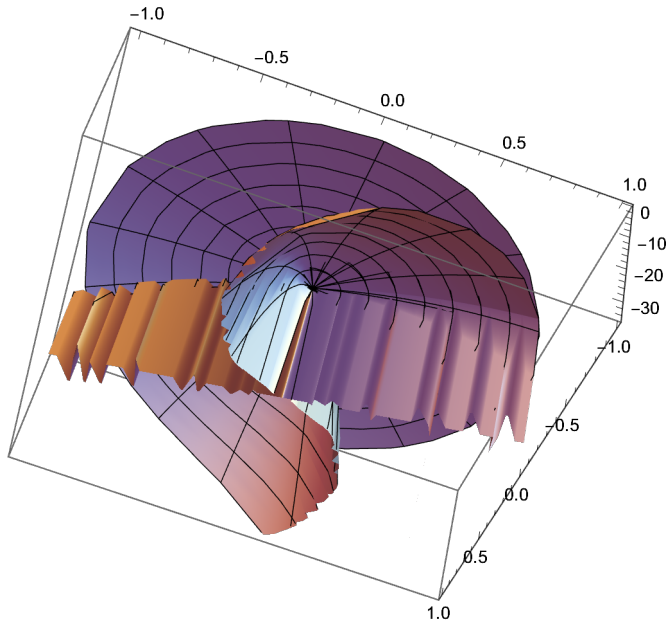
$$\frac{320 \pi^6 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} -$$
  

$$\frac{128 \pi^5 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} +$$
  

$$\frac{16 \pi^4 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} +$$
  

$$\left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) /$$
  

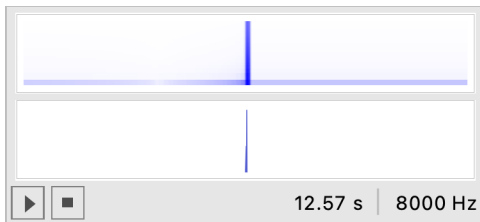
$$\left( -1024 \pi^7 \theta^4 + 1280 \pi^6 \theta^5 - 512 \pi^5 \theta^6 + 80 \pi^4 \theta^7 - 32 \pi^3 \theta^8 + 24 \pi^2 \theta^9 - 8 \pi \theta^{10} + \theta^{11} \right) \Bigg],$$
  
 {η, -1, 1}, {θ, -2 π, 2 π}]



$$\text{Solve}\left[2\pi\left(-\frac{256\pi^7\eta^2\theta^2}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+\frac{320\pi^6\eta^2\theta^3}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}-\frac{128\pi^5\eta^2\theta^4}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+\frac{16\pi^4\eta^2\theta^5}{-1024\pi^7\theta^3+1280\pi^6\theta^4-512\pi^5\theta^5+80\pi^4\theta^6-32\pi^3\theta^7+24\pi^2\theta^8-8\pi\theta^9+\theta^{10}}+\left(128\pi^6\sqrt{256\pi^5\eta^4\theta^3-448\pi^4\eta^4\theta^4+304\pi^3\eta^4\theta^5-100\pi^2\eta^4\theta^6+16\pi\eta^4\theta^7-\eta^4\theta^8}\right)/\left(-1024\pi^7\theta^4+1280\pi^6\theta^5-512\pi^5\theta^6+80\pi^4\theta^7-32\pi^3\theta^8+24\pi^2\theta^9-8\pi\theta^{10}+\theta^{11}\right)\right]=\left(r^2/((\theta)/(2\pi)),r\right]$$

$$\text{Play}\left[-\frac{1}{\sqrt{2}}\pm\sqrt{\theta}\sqrt{\left(-\left(512\pi^7\eta^2\theta^2\right)/\left(1024\pi^7\theta^3-1280\pi^6\theta^4+512\pi^5\theta^5-80\pi^4\theta^6+32\pi^3\theta^7-24\pi^2\theta^8+8\pi\theta^9-\theta^{10}\right)+\frac{640\pi^6\eta^2\theta^3}{1024\pi^7\theta^3-1280\pi^6\theta^4+512\pi^5\theta^5-80\pi^4\theta^6+32\pi^3\theta^7-24\pi^2\theta^8+8\pi\theta^9-\theta^{10}}-\frac{256\pi^5\eta^2\theta^4}{1024\pi^7\theta^3-1280\pi^6\theta^4+512\pi^5\theta^5-80\pi^4\theta^6+32\pi^3\theta^7-24\pi^2\theta^8+8\pi\theta^9-\theta^{10}}+\frac{32\pi^4\eta^2\theta^5}{1024\pi^7\theta^3-1280\pi^6\theta^4+512\pi^5\theta^5-80\pi^4\theta^6+32\pi^3\theta^7-24\pi^2\theta^8+8\pi\theta^9-\theta^{10}}+\left(256\pi^6\sqrt{\left(256\pi^5\eta^4\theta^3-448\pi^4\eta^4\theta^4+304\pi^3\eta^4\theta^5-100\pi^2\eta^4\theta^6+16\pi\eta^4\theta^7-\eta^4\theta^8\right)}/\left(1024\pi^7\theta^4-1280\pi^6\theta^5+512\pi^5\theta^6-80\pi^4\theta^7+32\pi^3\theta^8-24\pi^2\theta^9+8\pi\theta^{10}-\theta^{11}\right)\right),\{\theta,-2\pi,2\pi\}\right]$$

Sound::ssnm : A good PlayRange could not be found since most of the samples are not evaluating to machine-size real numbers. >>



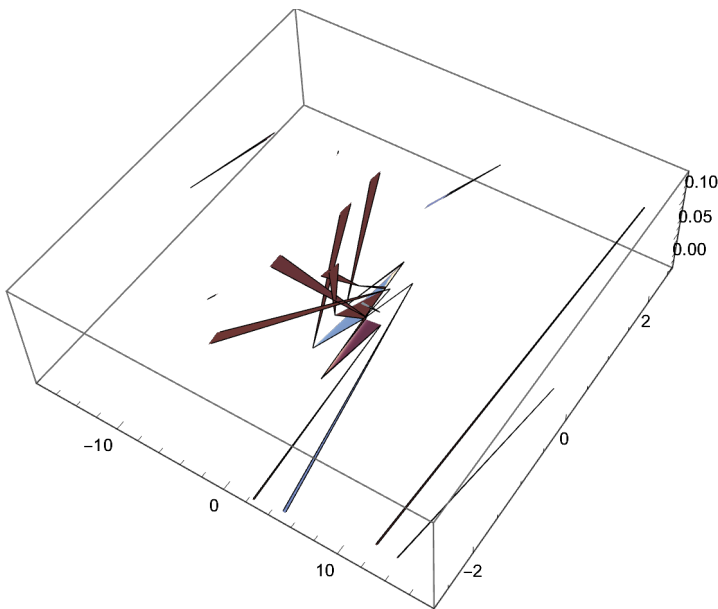
$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)$$

$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

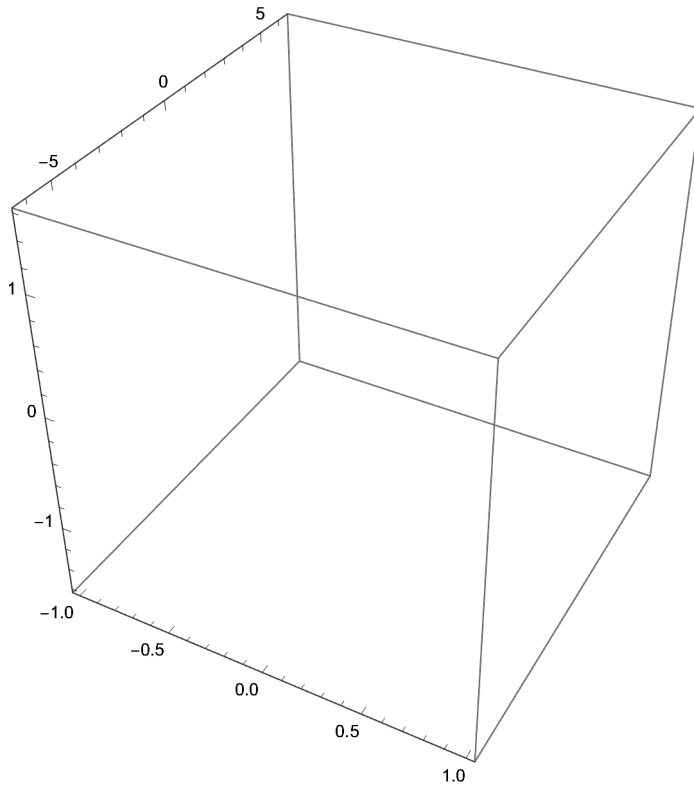
$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

RevolutionPlot3D[

$$\begin{aligned} & \frac{1}{\sqrt{2}} i \sqrt{\theta} \sqrt{\left( -\frac{512 \pi^7 \eta^2 \theta^2}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} + \right.} \\ & \quad \frac{640 \pi^6 \eta^2 \theta^3}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} - \\ & \quad \frac{256 \pi^5 \eta^2 \theta^4}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} + \\ & \quad \frac{32 \pi^4 \eta^2 \theta^5}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} + \\ & \quad \left. \left( 256 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \\ & \quad \left. \left( 1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - \right. \right. \\ & \quad \left. \left. 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \theta^{11} \right) \right), \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}] \end{aligned}$$



$$\text{ContourPlot3D}\left[\frac{1}{\sqrt{2}} \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}} \sqrt{\theta} \sqrt{\left(-\frac{512 \pi^7 \eta^2 \theta^2}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} + \frac{640 \pi^6 \eta^2 \theta^3}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} - \frac{256 \pi^5 \eta^2 \theta^4}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} + \frac{32 \pi^4 \eta^2 \theta^5}{1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}} + \left(256 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8}\right) / \left(1024 \pi^7 \theta^4 - 1280 \pi^6 \theta^5 + 512 \pi^5 \theta^6 - 80 \pi^4 \theta^7 + 32 \pi^3 \theta^8 - 24 \pi^2 \theta^9 + 8 \pi \theta^{10} - \theta^{11}\right)}\right], \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



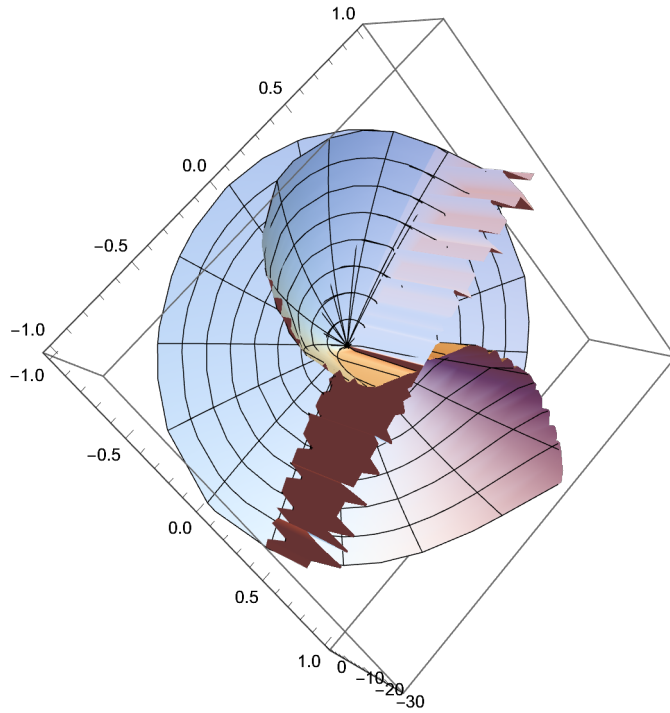


Simplify[

$$\frac{1}{\frac{\theta}{2\pi}} \left( \left( \sqrt{-\left(256\pi^7\eta^2\theta^3\right) / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right)} + \left(320\pi^6\eta^2\theta^4\right) / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right)} - \left(128\pi^5\eta^2\theta^5\right) / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right)} + \left(16\pi^4\eta^2\theta^6\right) / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right)} + \left(128\pi^6\sqrt{\left(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8\right)} / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right)} \right) \right)^2$$

RevolutionPlot3D[

$$-\left(32\pi^5\left(16\pi^3\eta^2\theta^3 + 8\pi\eta^2\theta^5 - \eta^2\theta^6 - 4\pi^2\left(5\eta^2\theta^4 + 2\sqrt{\eta^4(4\pi - \theta)^3\theta^3(-2\pi + \theta)^2}\right)\right)\right) / \left(\theta^4(-2\pi + \theta)^2(-256\pi^5 + 64\pi^4\theta + 4\pi^2\theta^3 - 4\pi\theta^4 + \theta^5)\right), \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



$$\frac{1}{\frac{\theta}{2\pi}} \left( \left( \sqrt{-(256\pi^7\eta^2\theta^3) / \right. \right. \\ \left. \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \right. \\ \left. \left. (320\pi^6\eta^2\theta^4) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + \right. \right. \\ \left. \left. 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - \right. \right. \\ \left. \left. 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / \right. \right. \\ \left. \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \right. \\ \left. \left. (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / \right. \right. \\ \left. \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) \right) \right) \right)$$

Simplify[

$$\frac{1}{\theta} 2\pi \sqrt{\left( -\frac{256\pi^7\eta^2\theta^3}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \right. \\ \frac{320\pi^6\eta^2\theta^4}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} - \\ \frac{128\pi^5\eta^2\theta^5}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\ \frac{16\pi^4\eta^2\theta^6}{-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}} + \\ \left. \left( 128\pi^6\sqrt{256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8} \right) / \right. \\ \left. \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) \right) \right]$$

$$8\pi^3 \sqrt{\frac{16\pi^3\eta^2\theta^3 + 8\pi\eta^2\theta^5 - \eta^2\theta^6 - 4\pi^2(5\eta^2\theta^4 + 2\sqrt{\eta^4(4\pi - \theta)^3\theta^3(-2\pi + \theta)^2})}{\theta^3(-2\pi + \theta)^2(-256\pi^5 + 64\pi^4\theta + 4\pi^2\theta^3 - 4\pi\theta^4 + \theta^5)}} \\ \theta$$

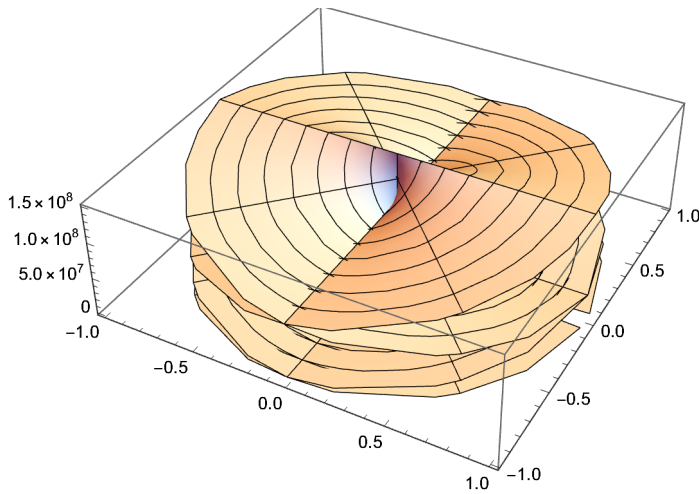
(r^2)

==

$$\frac{\frac{\theta}{2\pi}}{\left( \sqrt{-(256\pi^7\eta^2\theta^3) / \right.} \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - \right. \\ \left. 8\pi\theta^9 + \theta^{10}) + (320\pi^6\eta^2\theta^4) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) - \right. \\ \left. (128\pi^5\eta^2\theta^5) / (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - \right. \\ \left. 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + (16\pi^4\eta^2\theta^6) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) + \right. \\ \left. (128\pi^6\sqrt{(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8)}) / \right. \\ \left. (-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}) \right) \right)$$

$$\text{Solve}\left[\frac{2\pi\left(2\pi r - 2\pi\sqrt{r^2 - (\eta)^2}\right)}{(\theta)^2} == \right. \\ \left. \left(\sqrt{\left(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \right. \\ \left. \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2\right)\right)} \right. \\ \left. \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), r\right] \\ \left\{\left\{r \rightarrow 6.9656 \times 10^{-23} \left(\frac{9.45258 \times 10^{14} \eta^2}{\theta^2} + 5.45095 \times 10^{28} \theta^2\right)\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[6.965601593354798 \cdot 10^{-23} \left(\frac{9.452580995025 \cdot \eta^{14}}{\theta^2} + 5.450951774320537 \cdot \theta^{28}\right), \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$\text{Solve}\left[6.965601593354798 \cdot 10^{-23} \left(\frac{9.452580995025 \cdot \eta^{14}}{\theta^2} + 5.450951774320537 \cdot \theta^{28}\right) == \right. \\ \sqrt{\left(-\left(256\pi^7\eta^2\theta^3\right) / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + \right. \right. \right. \\ \left. \left. \left. 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right) + \left(320\pi^6\eta^2\theta^4\right) / \right. \right. \\ \left. \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right) - \right. \\ \left. \left(128\pi^5\eta^2\theta^5\right) / \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - \right. \right. \\ \left. \left. 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right) + \left(16\pi^4\eta^2\theta^6\right) / \right. \\ \left. \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right) + \right. \\ \left. \left(128\pi^6\sqrt{\left(256\pi^5\eta^4\theta^3 - 448\pi^4\eta^4\theta^4 + 304\pi^3\eta^4\theta^5 - 100\pi^2\eta^4\theta^6 + 16\pi\eta^4\theta^7 - \eta^4\theta^8\right)}\right) / \right. \\ \left. \left(-1024\pi^7\theta^3 + 1280\pi^6\theta^4 - 512\pi^5\theta^5 + 80\pi^4\theta^6 - 32\pi^3\theta^7 + 24\pi^2\theta^8 - 8\pi\theta^9 + \theta^{10}\right)\right), \eta\right]$$

$$\eta := \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\begin{aligned} & \sqrt{\left( - \left( 256 \pi^7 \eta^2 \theta^3 \right) / \right. \\ & \quad \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \\ & \quad \left( 320 \pi^6 \eta^2 \theta^4 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + \right. \\ & \quad \left. 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \left( 128 \pi^5 \eta^2 \theta^5 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - \right. \\ & \quad \left. 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 16 \pi^4 \eta^2 \theta^6 \right) / \\ & \quad \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \\ & \quad \left. \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} \right) / \right. \\ & \quad \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right) \\ & \sqrt{\left( - \frac{64 \pi^5 \theta^3 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \\ & \quad \frac{80 \pi^4 \theta^4 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\ & \quad \frac{32 \pi^3 \theta^5 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\ & \quad \frac{4 \pi^2 \theta^6 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\ & \quad \left( 128 \pi^6 \sqrt{\left( 16 \pi \theta^3 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)^2 - 28 \theta^4 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)^2 + \frac{19 \theta^5 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)^2}{\pi} - \right. \right. \\ & \quad \left. \left. \frac{25 \theta^6 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)^2}{4 \pi^2} + \frac{\theta^7 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)^2}{\pi^3} - \frac{\theta^8 \left( \frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta} \right)^2}{16 \pi^4} \right) \right) / \right. \\ & \quad \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right) \end{aligned}$$

$$\begin{aligned} & \text{Solve} \left[ \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2} \right)}{\left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)^2} == \right. \\ & \quad \frac{4 \pi r^2 - 2 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)}{2 \sqrt{4 \pi r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)^2}}, r \end{aligned}$$

$$\begin{aligned}
& \text{Solve} \left[ \left( \left( \left( -1.1294090667581471 \cdot 10^{18} \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2}}{r^2} \right) + \right. \right. \right. \right. \\
& 8.987551787368176 \cdot 10^{16} \left( \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2}}{r^2} \right)^2}{r^2} \right) + \\
& \left. \left. \left. \left. 3.5481432270250993 \cdot 10^{18} \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right]^2 \right) \right) \right) \right) / \right. \\
& \left( \left( \left( -12.566370614359172 \cdot \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2}}{r^2} \right) + \right. \right. \right. \right. \\
& \left( \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2}}{r^2} \right)^2}{r^2} \right) + \\
& \left. \left. \left. \left. 39.47841760435743 \cdot \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right]^2 \right) \right) \right) \right) = \\
& \left. \frac{\pi (4 \pi - 2 \theta)}{(4 \pi - \theta) \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta^2} + \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^2 \theta}, r \right]
\end{aligned}$$

RevolutionPlot3D[

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2} \right)}{r^2} + \right. \right.} \right.$$

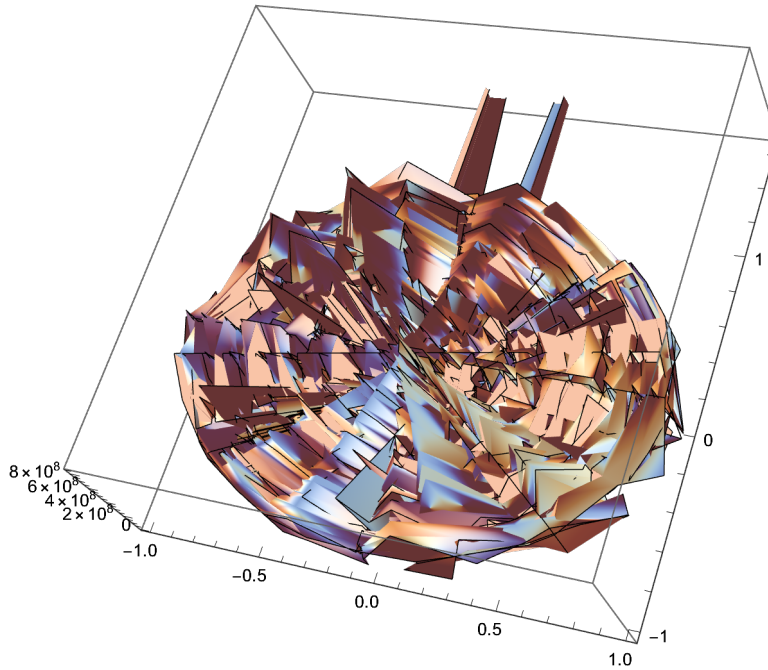
$$\left. \left. 8.987551787368176 \cdot 10^{16} \frac{\left( 2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2} \right)}{r^2} \right)^2}{r^2} + \right. \right.$$

$$\left. \left. 3.5481432270250993 \cdot 10^{18} \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right]^2 \right) \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2} \right)}{r^2} + \right. \right.} \right.$$

$$\left. \left. \frac{\left( 2 \pi \left( r^2 + \sqrt{r^4 - r^2 \left( r \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right)^2} \right)}{r^2} \right)^2}{r^2} + \right. \right.$$

$$\left. \left. 39.47841760435743 \cdot \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right] \right]^2 \right) \right), \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}$$



$$D\left[\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}, \theta\right]$$

$$\frac{\pi(4\pi-2\theta)}{(4\pi-\theta)\theta\sqrt{(4\pi-\theta)\theta}} - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta^2} + \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)^2\theta}$$

$$2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta\theta}$$

Solve[

$$\frac{4\pi^2\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta^2} == \left(\sqrt{(3.5481432270250993\eta^2 - 1.1294090667581471r^2\theta + 8.987551787368176r^2\theta^2)}\right) /$$

$$\left(\sqrt{39.47841760435743\eta^2 - 12.566370614359172r^2\theta + r^2\theta^2}\right), \eta]$$

$$\{\{\text{Solve`Auxiliary}[\theta][\theta] \rightarrow -5.56664 \times 10^{-6} - 9.64169 \times 10^{-6}i\},$$

$$\{\text{Solve`Auxiliary}[\theta][\theta] \rightarrow -5.56664 \times 10^{-6} + 9.64169 \times 10^{-6}i\},$$

$$\{\text{Solve`Auxiliary}[\theta][\theta] \rightarrow 0.0000111333\},$$

$$\{\text{Solve`Auxiliary}[\theta][\theta] \rightarrow 12.5664\}, \{\text{Solve`Auxiliary}[\theta][\theta] \rightarrow 12.5664\}\}$$

$$\text{Solve}\left[\frac{4 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta^2} == \left(\sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2)}\right) / \left(\sqrt{39.47841760435743 \eta^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2}\right), \theta\right]$$

$$\{\{\theta \rightarrow -5.56664 \times 10^{-6} - 9.64169 \times 10^{-6} i\}, \{\theta \rightarrow -5.56664 \times 10^{-6} + 9.64169 \times 10^{-6} i\}, \{\theta \rightarrow 0.0000111333\}, \{\theta \rightarrow 12.5664\}, \{\theta \rightarrow 12.5664\}\}$$

$$\text{Solve}\left[r / (\theta / (2 \pi)) == \left(\sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2)}\right) / \left(\sqrt{39.47841760435743 \eta^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2}\right),\right]$$

$$\{\}$$

$$\text{Solve}\left[\frac{2 \pi \eta}{\sqrt{-4 i \pi \text{ArcSinh}[e^{i \theta} - \text{Cos}[\theta]] + \text{ArcSinh}[e^{i \theta} - \text{Cos}[\theta]]^2}} == \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}, \theta\right]$$

Solve::tdep : The equations appear to involve the variables to be solved for in an essentially non-algebraic way. >>

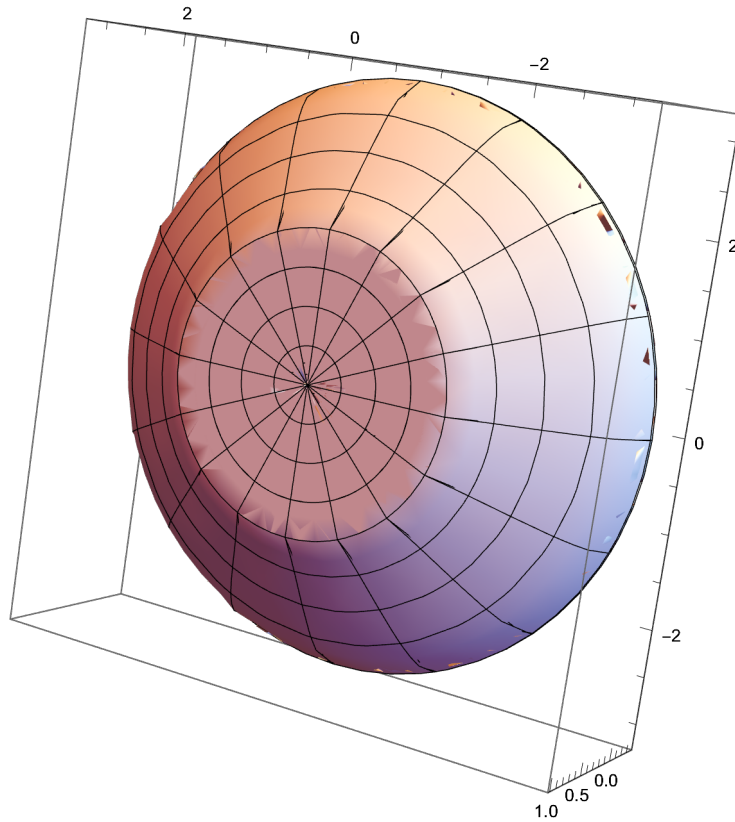
$$\text{Solve}\left[\frac{2 \pi \eta}{\sqrt{-4 i \pi \text{ArcSinh}[e^{i \theta} - \text{Cos}[\theta]] + \text{ArcSinh}[e^{i \theta} - \text{Cos}[\theta]]^2}} == \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}, \theta\right]$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{(4 \pi - \theta) \theta} \sqrt{-i (4 \pi + i \text{ArcSinh}[e^{i \theta} - \text{Cos}[\theta]]) \text{ArcSinh}[e^{i \theta} - \text{Cos}[\theta]]}}{(4 \pi - \theta) \theta}, \{\theta, -2 \pi, 2 \pi\}\right]$$



RevolutionPlot3D[  

$$\frac{\sqrt{(4\pi - \theta)\theta} \sqrt{-i(4\pi + i \operatorname{ArcSinh}[e^{i\theta} - \cos[\theta]]) \operatorname{ArcSinh}[e^{i\theta} - \cos[\theta]]}}{(4\pi - \theta)\theta}, \{\theta, -2\pi, 2\pi\}]$$



$h := 6.62606896 \times 10^{-34}$

$c := 2.99792458 \times (10^8)$

$$r := \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

RevolutionPlot3D[

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \frac{4 \pi r^2}{c^2 + r^2} + 8.987551787368176 \cdot 10^{16} \left( \frac{4 \pi r^2}{c^2 + r^2} \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$

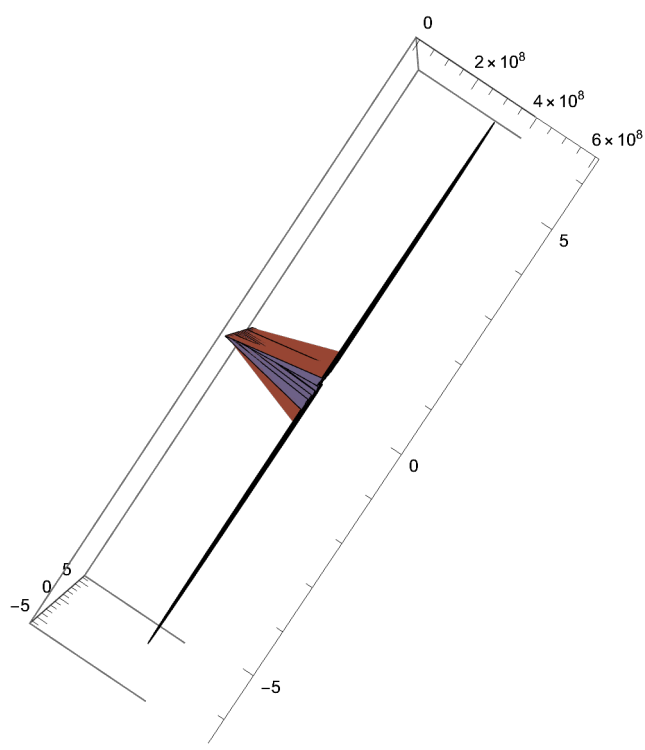
$$\left( \sqrt{\left( -12.566370614359172 \cdot \frac{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))} 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \right)^2}{c^2 + r^2} + \left( \frac{4 \pi r^2}{c^2 + r^2} \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)} \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

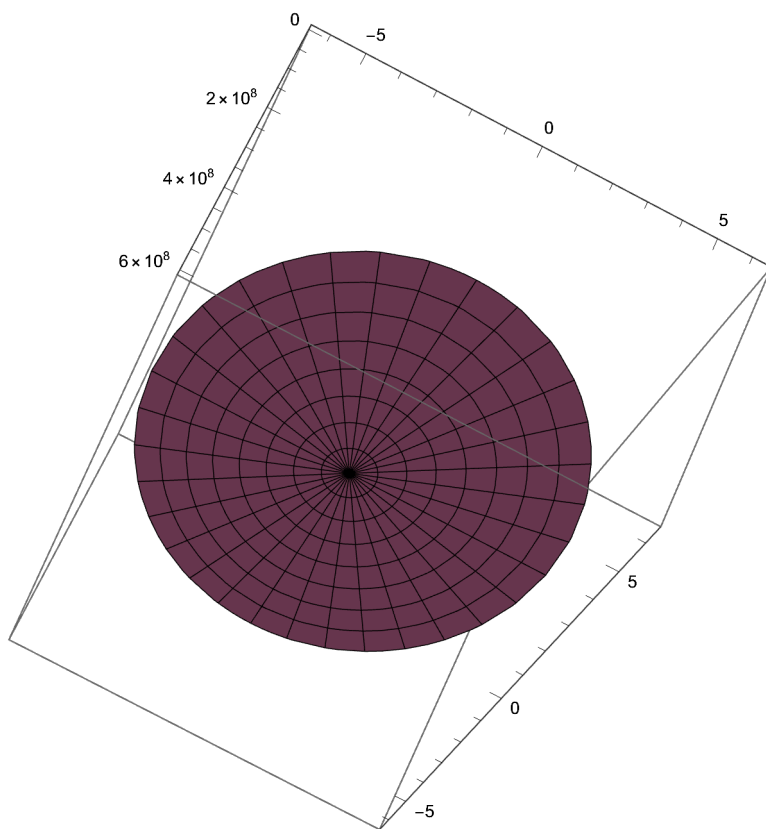


RevolutionPlot3D[

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \frac{4 \pi r^2}{c^2 + r^2} + 8.987551787368176 \cdot 10^{16} \left( \frac{4 \pi r^2}{c^2 + r^2} \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot \frac{4 \pi r^2}{c^2 + r^2} + \left( \frac{4 \pi r^2}{c^2 + r^2} \right)^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)} \right),$$

$$\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



$$\text{Solve}\left[\text{Energy} == \frac{h \left( c^2 + \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2}, \theta\right]$$

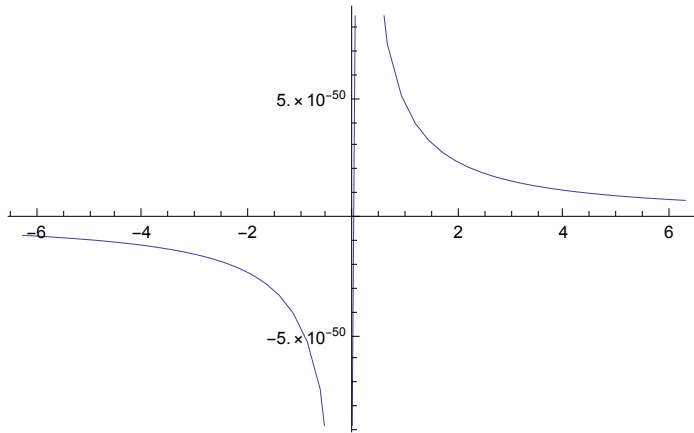
$$\left\{ \left\{ \theta \rightarrow \frac{2 h \pi}{\text{Energy}} \right\} \right\}$$

$$\text{Solve}\left[\frac{h\left(c^2+\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\right)}{2\left(\frac{c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2}==mc^2,m\right]$$

$$\left\{\left\{m\rightarrow\frac{3.31303\times10^{-34}\left(12.5664-1.\theta\right)\left(c^2+\frac{c^2\theta}{12.5664-1.\theta}\right)}{c^4\theta}\right\}\right\}$$

$$\text{Plot}\left[\frac{1}{c^4\theta}3.3130344800000002\cdot10^{-34}\left(12.566370614359172-1.\theta\right)\right.$$

$$\left.\left(c^2+\frac{c^2\theta}{12.566370614359172-1.\theta}\right),\{\theta,-2\pi,2\pi\}\right]$$

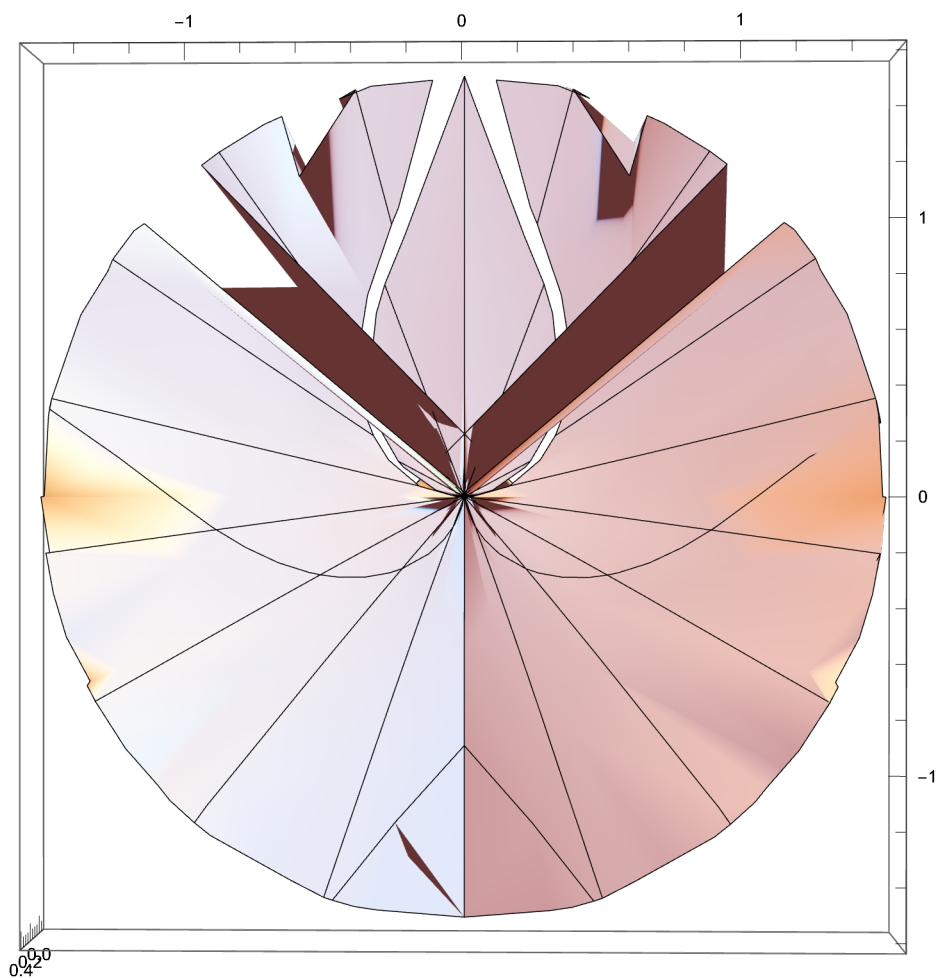


$$\left(\frac{1}{c^4\theta}3.3130344800000002\cdot10^{-34}\right.$$

$$\left.\left(12.566370614359172-1.\theta\right)\left(c^2+\frac{c^2\theta}{12.566370614359172-1.\theta}\right)\right)$$

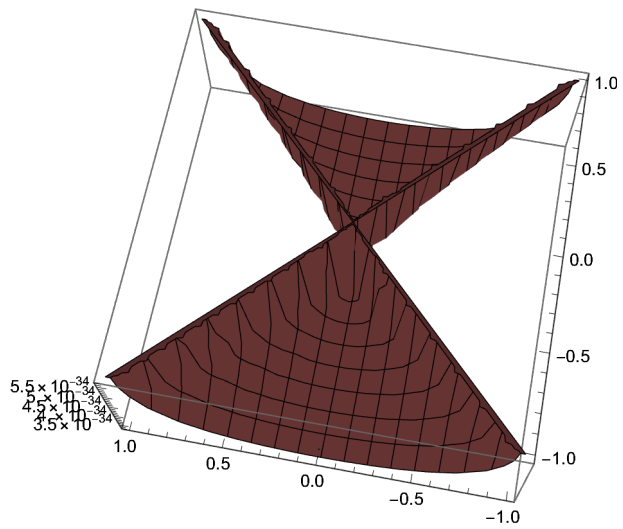
SphericalPlot3D[ArcSin[

$$\frac{1}{4 \pi^2} \left( 4 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \theta - \frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{(4 \pi - \theta) \theta} \right. \\ \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

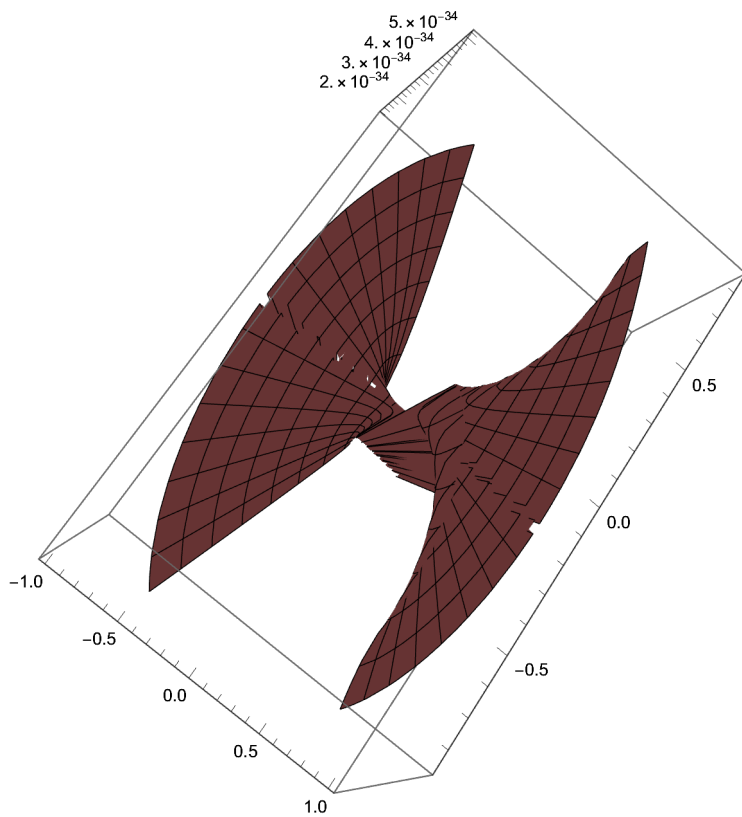


$$\frac{h \left( c^2 + \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2} \\ \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}$$

$$\text{Plot3D}\left[\frac{h\left(c^2+\left(\frac{c\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2\eta^2}\right)}{r^2}}}{\sqrt{4\pi-\frac{2\pi\left(r^2+\sqrt{r^4-r^2\eta^2}\right)}{r^2}}}\right)^2\right)}{2\left(\frac{c\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2\eta^2}\right)}{r^2}}}{\sqrt{4\pi-\frac{2\pi\left(r^2+\sqrt{r^4-r^2\eta^2}\right)}{r^2}}}\right)^2},\{r,-1,1\},\{\eta,-1,1\}\right]$$



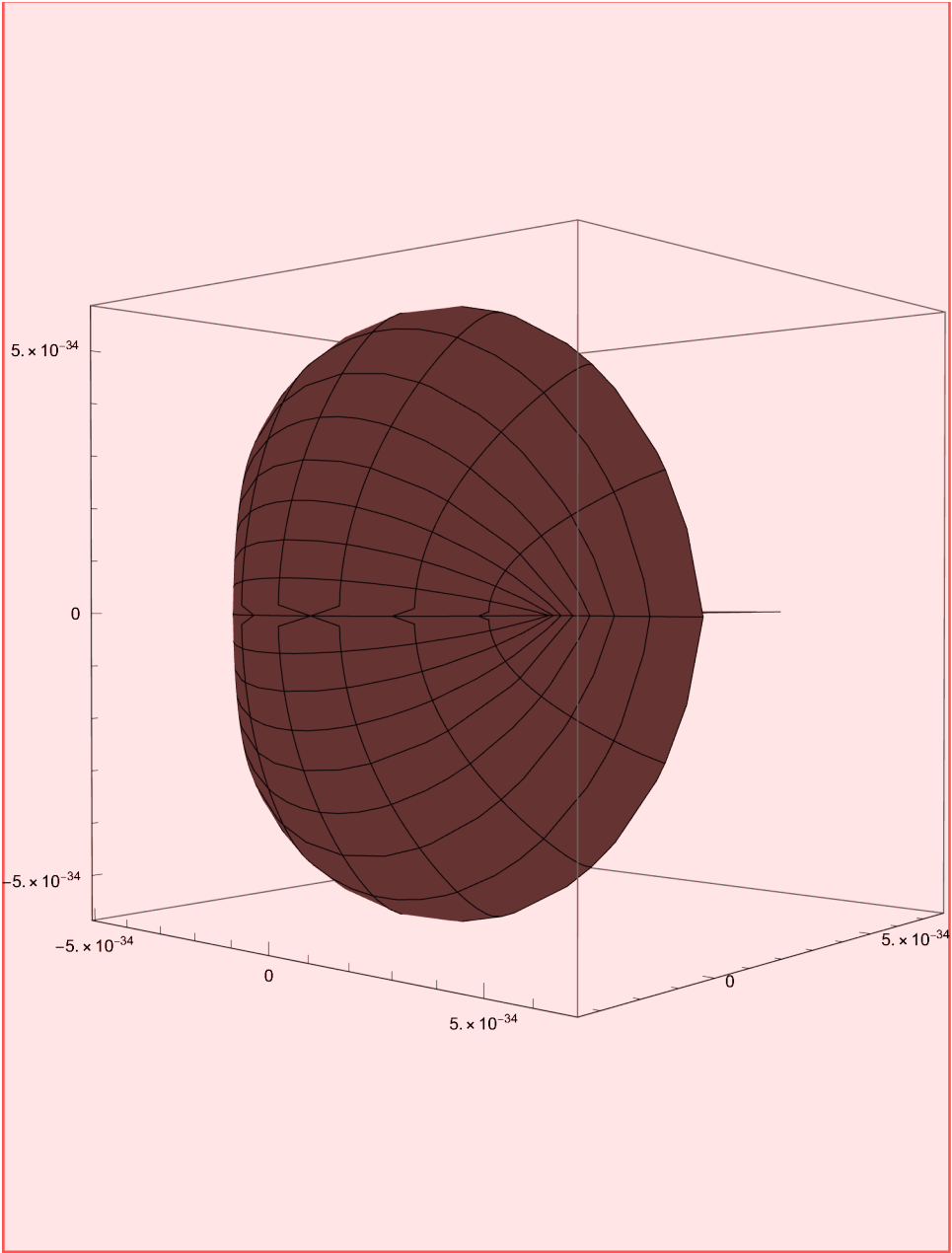
$$\text{RevolutionPlot3D}\left[\frac{h\left(c^2+\left(\frac{c\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}{\sqrt{4\pi-\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}\right)^2\right)}{2\left(\frac{c\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}{\sqrt{4\pi-\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}\right)^2},\{r,-1,1\},\{\beta,-1,1\}\right]$$



$$r := \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}$$



$$\text{SphericalPlot3D}\left[\frac{h\left(c^2+\left(\frac{c\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}{\sqrt{4\pi-\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}\right)^2\right)}{2\left(\frac{c\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}{\sqrt{4\pi-\frac{2\pi\left(r^2+\sqrt{r^4-r^2}r\sin[\beta]^2\right)}{r^2}}}\right)^2},\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$$



$$(\text{Energy of Photon with Wavelength } \eta) = \frac{h \left( c^2 + \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2} \text{ Joules}$$

$$D \left[ k \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$\frac{k (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Solve} \left[ \frac{\eta}{t} == \frac{k (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, k \right]$$

$$\left\{ \left\{ k \rightarrow \frac{2 \pi \eta \sqrt{r^2 (4 \pi - \theta) \theta}}{r^2 t (2 \pi - \theta)} \right\} \right\}$$

$$\frac{2 \pi \eta \sqrt{r^2 (4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))} 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{r^2 t (2 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))}$$

$$\frac{2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{r^2 (4 \pi - \theta) \theta}}{r^2 t (2 \pi - \theta)}$$

$$\frac{2 \pi \frac{\sqrt{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}}{2 \pi} \sqrt{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 (4 \pi - \theta) \theta}}{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 t (2 \pi - \theta)}$$

$$\frac{(4 \pi - \theta) \theta \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}{2 \pi t (2 \pi - \theta)}$$

$$\text{Solve} \left[ k == \frac{(4 \pi - \theta) \theta \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}{2 \pi t (2 \pi - \theta)}, \theta \right]$$

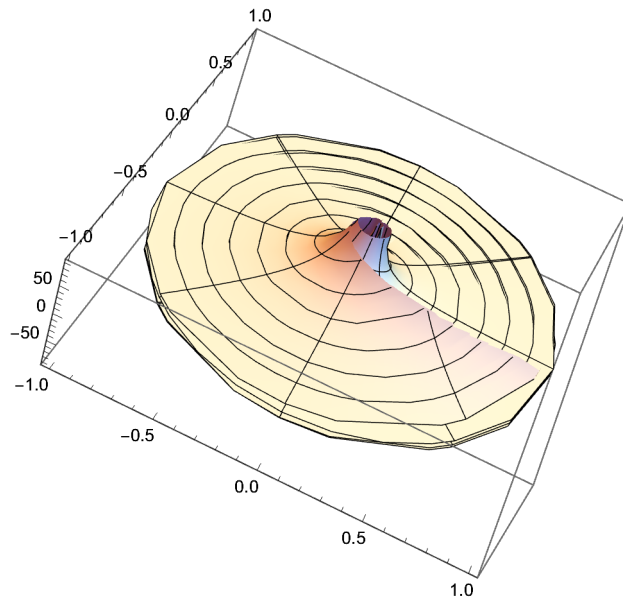
$$\left\{ \left\{ \theta \rightarrow \frac{1}{2} (4 \pi + k t - \sqrt{16 \pi^2 + k^2 t^2}) \right\}, \left\{ \theta \rightarrow \frac{1}{2} (4 \pi + k t + \sqrt{16 \pi^2 + k^2 t^2}) \right\} \right\}$$

$$\frac{1}{2} (4 \pi + k t + \sqrt{16 \pi^2 + k^2 t^2})$$

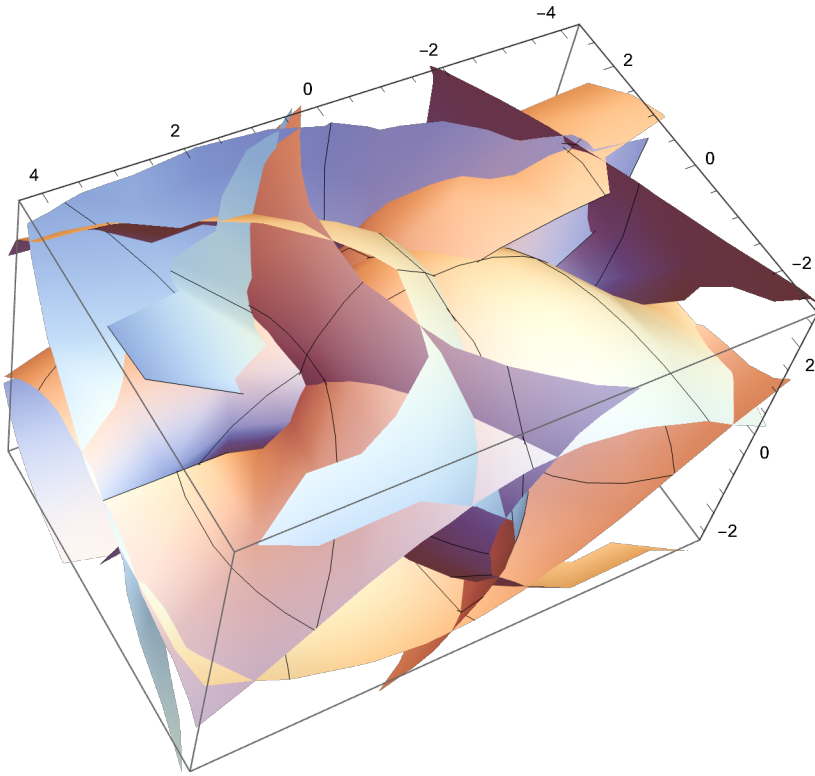
$$\text{Solve}\left[k == \frac{(4\pi - \theta)\theta \sqrt{\frac{16\pi^3}{4\pi - \theta} - \frac{4\pi^2\theta}{4\pi - \theta}}}{2\pi t(2\pi - \theta)}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{4\pi\theta - \theta^2}{k(2\pi - \theta)}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{4\pi\theta - \theta^2}{k(2\pi - \theta)}, \{k, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

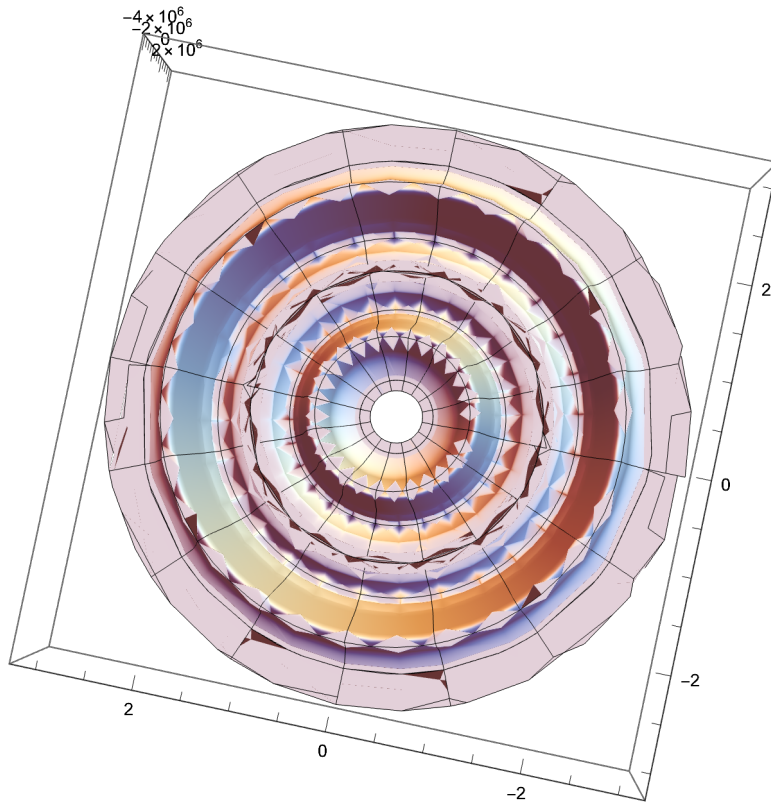


SphericalPlot3D $\left[\frac{(4 \pi - \theta) \theta \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}{2 \pi t (2 \pi - \theta)}, \{\theta, -2 \pi, 2 \pi\}, \{t, -4 \pi, 4 \pi\}\right]$

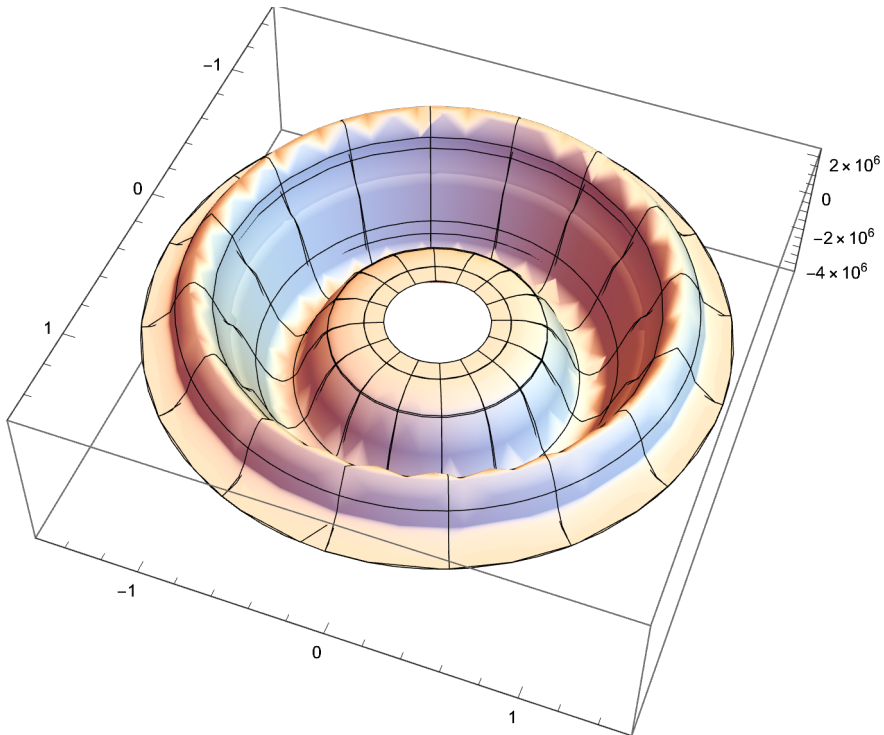


$$\frac{2 \pi \eta \sqrt{\left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 (4 \pi - \theta) \theta}}{\left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 t (2 \pi - \theta)}$$

$$\begin{aligned}
& \text{RevolutionPlot3D} \left[ \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \left( 2 \sqrt{2 \pi^2 - \pi^2 \sin[\beta]^2 + 2 \pi^2 \sqrt{1 - \sin[\beta]^2}} \right) \right) \right. \\
& \left. \left( 2 \left( 2 \pi - \frac{\pi^2 \sin[\beta]^2}{\pi + \pi \sqrt{1 - \sin[\beta]^2}} \right) \right) \left( 2 \left( \pi + \frac{\sqrt{\pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^3} \sqrt{\sin[\beta]^2}}{\sqrt{\sin[\beta]^2}} \right) \right) \right] \left( \left( 0.5 \right. \right. \\
& \left. \left. \left( 6.916640561054567 \cdot 10^{33} + \frac{1.5190901312653737 \cdot 10^{18}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} + \right. \right. \\
& \left. \left. 2.3071429505590057 \cdot 10^{25} \sqrt{8.987551787368176 \cdot 10^{16} + \right. \right. \\
& \left. \left. \frac{19.739208802178716}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \right) \right] / \\
& \left( 5.504087674408674 \cdot 10^{32} + \frac{1.2088535169650016 \cdot 10^{17}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \\
& \left( -i \operatorname{ArcSinh} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( -i \operatorname{Log} \left[ -e^{-i \sqrt{e^{-2 i \beta} (1 + e^{2 i \beta})^2} \pi} \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right) \\
& \left( -i \operatorname{Log} \left[ \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] + i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right), \{\beta, -\pi, \pi\}
\end{aligned}$$

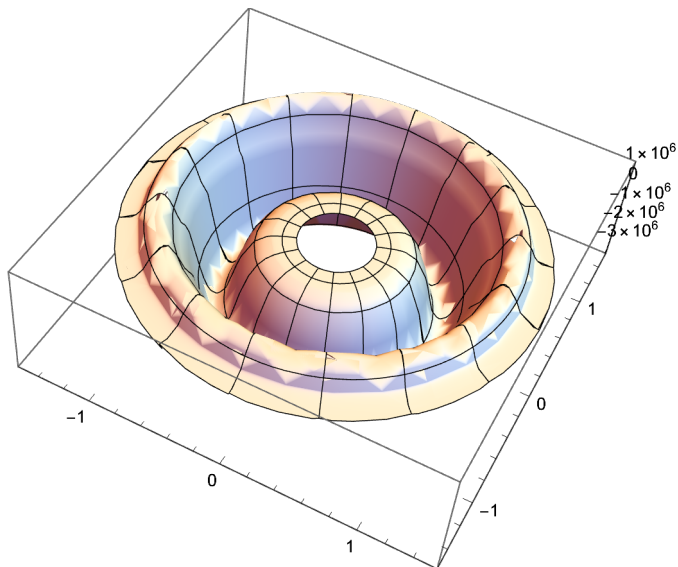


$$\begin{aligned}
& \text{RevolutionPlot3D}\left[ \right. \\
& \left. \left( \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^3 \right) \left( 2 \left( \pi + \frac{\sqrt{\pi^2 \sin[\beta]^2 - \pi^2 \sin[\beta]^3} \sqrt{\sin[\beta]^2}}{\sqrt{\sin[\beta]^2}} \right) \right) \left( \left( 0.5 \right. \right. \right. \\
& \left. \left. \left( 6.916640561054567 \cdot 10^{33} + \frac{1.5190901312653737 \cdot 10^{18}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} + \right. \right. \\
& \left. \left. 2.3071429505590057 \cdot 10^{25} \sqrt{8.987551787368176 \cdot 10^{16} + \right. \right. \\
& \left. \left. \frac{19.739208802178716}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \right) \right] / \\
& \left( 5.504087674408674 \cdot 10^{32} + \frac{1.2088535169650016 \cdot 10^{17}}{\left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) \\
& \left( -i \operatorname{ArcSinh} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( -i \operatorname{Log} \left[ -e^{-i \sqrt{e^{-2 i \beta} (1 + e^{2 i \beta})^2} \pi} \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right) \\
& \left( -i \operatorname{Log} \left[ \cos \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] + i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ e^{2 i \pi \sqrt{1 - \sin[\beta]^2}} - i \sin \left[ 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right] \right] \right) \\
& \left( \operatorname{ArcCos} \left[ \frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left( 1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}} \right) \right] \right), \{\beta, -\pi / 2, \pi / 2\}
\end{aligned}$$





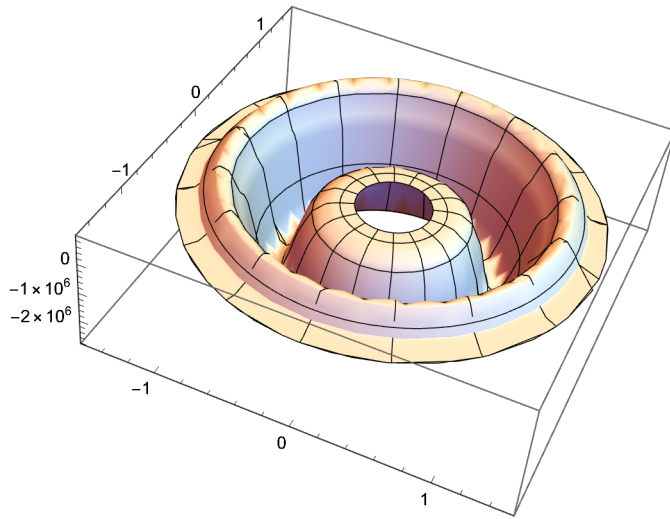
$$\begin{aligned}
& \text{RevolutionPlot3D}\left[\left(\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^4\right)\left(\left(0.5\right.\right.\right. \\
& \left.\left.\left(6.916640561054567 \cdot 10^{33} + \frac{1.5190901312653737 \cdot 10^{18}}{\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)} + \right.\right.\right. \\
& \left.\left.\left.2.3071429505590057 \cdot 10^{25} \sqrt{8.987551787368176 \cdot 10^{16} + \right.\right.\right. \\
& \left.\left.\left.\frac{19.739208802178716}{\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}\right)\right)\right) / \\
& \left.\left(5.504087674408674 \cdot 10^{32} + \frac{1.2088535169650016 \cdot 10^{17}}{\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)}\right)\right) \\
& \left(-i \operatorname{ArcSinh}\left[e^{2i\pi\sqrt{1-\sin[\beta]^2}} - \cos\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right]\right) \\
& \left(-i \operatorname{Log}\left[-e^{-i\sqrt{e^{-2i\beta}\left(1+e^{2i\beta}\right)^2}\pi}\right]\right) \\
& \left(\operatorname{ArcCos}\left[\frac{1}{2}e^{-2i\pi\sqrt{1-\sin[\beta]^2}}\left(1+e^{4i\pi\sqrt{1-\sin[\beta]^2}}\right)\right]\right) \\
& \left(-i \operatorname{Log}\left[\cos\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right] + i \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right]\right) \\
& \left(\operatorname{ArcCos}\left[e^{2i\pi\sqrt{1-\sin[\beta]^2}} - i \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right]\right) \\
& \left(\operatorname{ArcCos}\left[\frac{1}{2}e^{-2i\pi\sqrt{1-\sin[\beta]^2}}\left(1+e^{4i\pi\sqrt{1-\sin[\beta]^2}}\right)\right]\right), \{\beta, \\
& -\pi/2, \pi/2\}
\end{aligned}$$



```

RevolutionPlot3D[(((2 (π + √(π² - π² Sin[β]²)) ) ^ 5)
  (-i ArcSinh[e^(2 i π √(1 - Sin[β]²)) - Cos[2 (π + √(π² - π² Sin[β]²))]]))
  (-i Log[-e^(-i √(e^(2 i β) (1 + e^(2 i β))²) π)] (ArcCos[1/2 e^(-2 i π √(1 - Sin[β]²)) (1 + e^(4 i π √(1 - Sin[β]²)))]))
  (-i Log[Cos[2 (π + √(π² - π² Sin[β]²))] + i Sin[2 (π + √(π² - π² Sin[β]²))]]))
  (ArcCos[e^(2 i π √(1 - Sin[β]²)) - i Sin[2 (π + √(π² - π² Sin[β]²))]]))
  (ArcCos[1/2 e^(-2 i π √(1 - Sin[β]²)) (1 + e^(4 i π √(1 - Sin[β]²)))]))], {β, -π/2, π/2}]

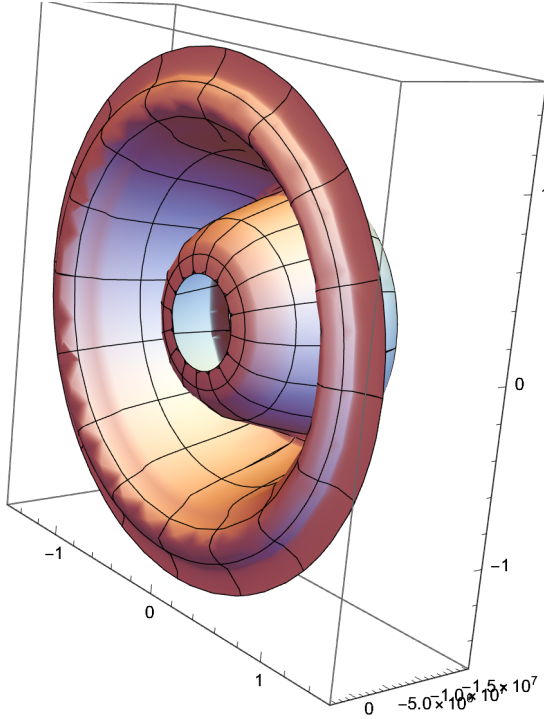
```



```

RevolutionPlot3D[(((2 (π + √(π² - π² Sin[β]²)) ) ^ 6)
  (-i ArcSinh[e^(2 i π √(1 - Sin[β]²)) - Cos[2 (π + √(π² - π² Sin[β]²))]]))
  (-i Log[-e^(-i √(e^(2 i β) (1 + e^(2 i β))²) π)] (ArcCos[1/2 e^(-2 i π √(1 - Sin[β]²)) (1 + e^(4 i π √(1 - Sin[β]²)))]))
  (-i Log[Cos[2 (π + √(π² - π² Sin[β]²))] + i Sin[2 (π + √(π² - π² Sin[β]²))]]))
  (ArcCos[e^(2 i π √(1 - Sin[β]²)) - i Sin[2 (π + √(π² - π² Sin[β]²))]])), {β, -π/2, π/2}]

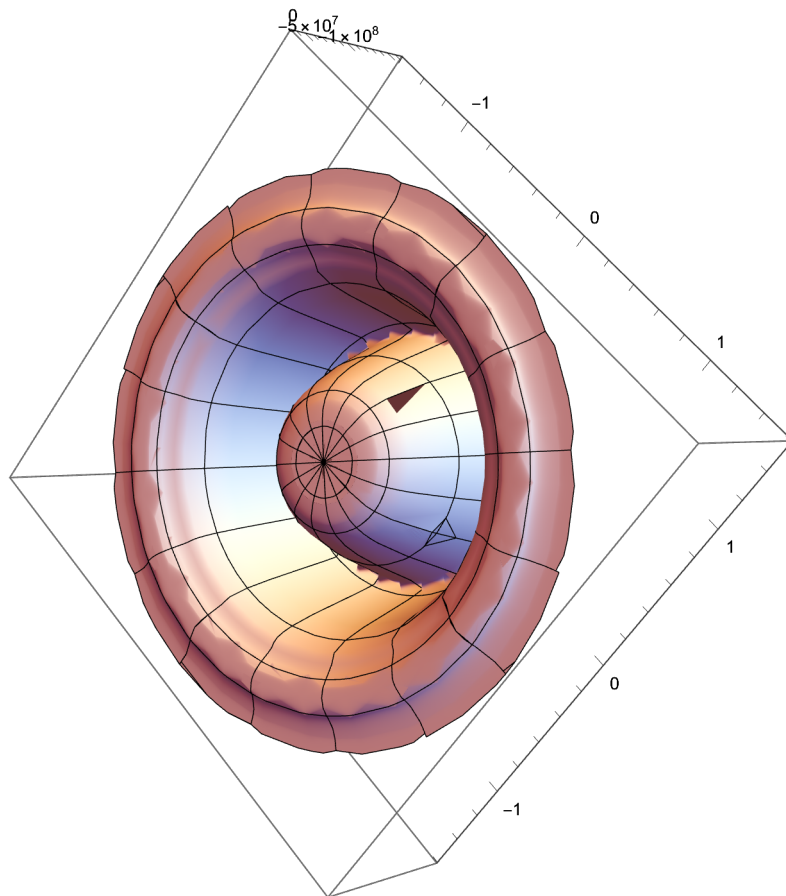
```



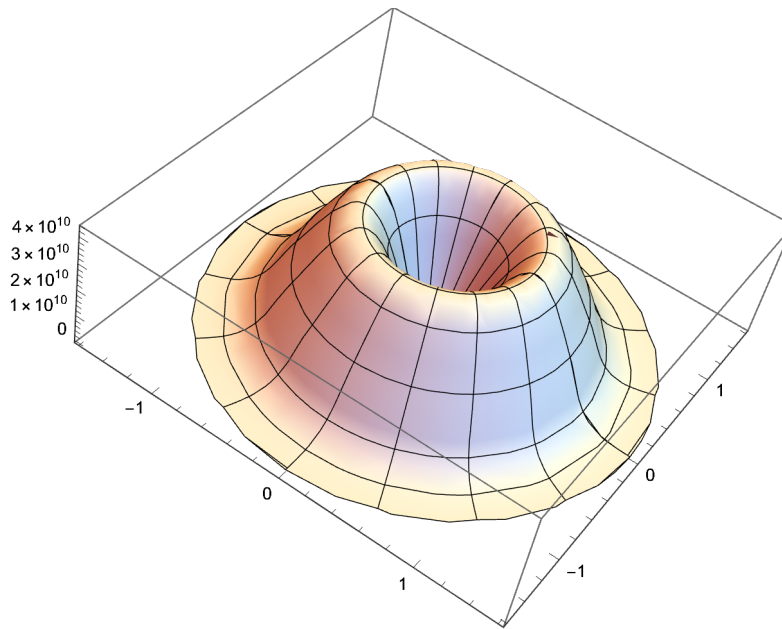
```

RevolutionPlot3D[(((2 (π + √(π² - π² Sin[β]²)) ) ^ 7)
(-I ArcSinh[e^(2 I π √(1 - Sin[β]²)) - Cos[2 (π + √(π² - π² Sin[β]²))]]))
(-I Log[-e^(-I √(e^(-2 I β) (1 + e^(2 I β))²) π)] (ArcCos[1/2 e^(-2 I π √(1 - Sin[β]²)) (1 + e^(4 I π √(1 - Sin[β]²)))]))
(-I Log[Cos[2 (π + √(π² - π² Sin[β]²))]] + I Sin[2 (π + √(π² - π² Sin[β]²))]]), {β,
-π / 2, π / 2}]

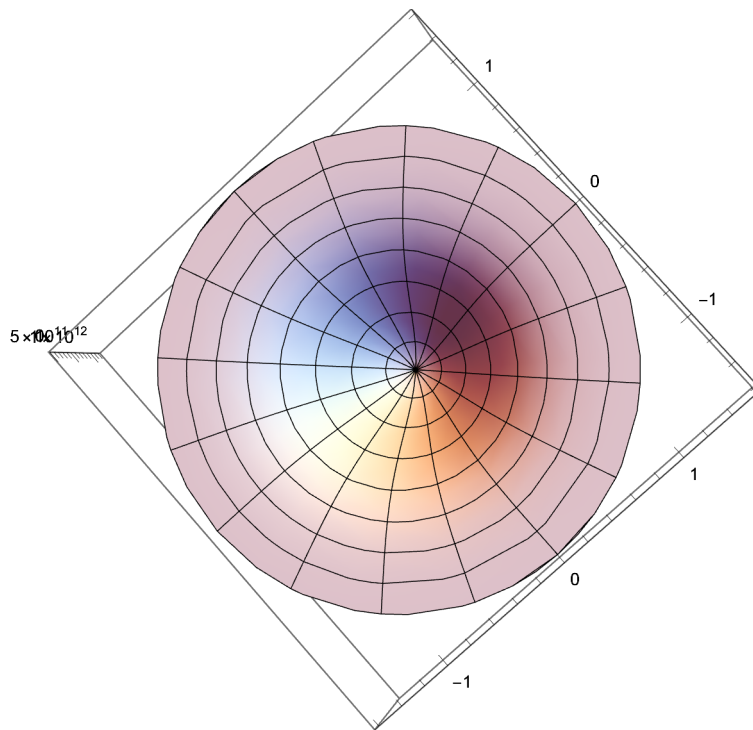
```



$\text{RevolutionPlot3D}\left[\left(\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{10}\right.\right.$   
 $\left.\left.\left(\text{ArcCos}\left[\frac{1}{2} e^{-2 i \pi \sqrt{1 - \sin[\beta]^2}} \left(1 + e^{4 i \pi \sqrt{1 - \sin[\beta]^2}}\right)\right]\right), \{\beta, -\pi/2, \pi/2\}\right]\right]$



$\text{RevolutionPlot3D}\left[\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{11}, \{\beta, -\pi/2, \pi/2\}\right]$



$$\text{Solve}\left[\left(2\pi r - r\theta - 2\pi\sqrt{r^2 - \frac{4\pi r^2\theta - r^2\theta^2}{4\pi^2}}\right) == \frac{2\pi r - r\theta - 2\pi\sqrt{r^2 - \frac{\sqrt{r}\sqrt{1-\frac{(v)^2}{c^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}}\sqrt{4\pi r - r\theta}}}{2\pi}}{\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}}, v\right]$$

$$\text{Solve}\left[\left(2\pi r - r\theta - 2\pi\sqrt{r^2 - \frac{4\pi r^2\theta - r^2\theta^2}{4\pi^2}}\right) == \frac{2\pi r - r\theta - 2\pi\sqrt{r^2 - \frac{\sqrt{r}\sqrt{1-\frac{(v)^2}{c^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}}\sqrt{4\pi r - r\theta}}}{2\pi}}{\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}}, v\right]$$

$$\left\{\left\{v \rightarrow -\left(1.\sqrt{-2.73058 \times 10^{35} + 2.17293 \times 10^{34}\theta + 8.69171 \times 10^{34}r^2\theta - 1.38333 \times 10^{34}r^2\theta^2 + 5.50409 \times 10^{32}r^2\theta^3}\right) / \left(\sqrt{-3.03818 \times 10^{18} + 2.41771 \times 10^{17}\theta + 9.67083 \times 10^{17}r^2\theta - 1.53916 \times 10^{17}r^2\theta^2 + 6.12412 \times 10^{15}r^2\theta^3}\right)\right\}, \left\{v \rightarrow \left(\sqrt{-2.73058 \times 10^{35} + 2.17293 \times 10^{34}\theta + 8.69171 \times 10^{34}r^2\theta - 1.38333 \times 10^{34}r^2\theta^2 + 5.50409 \times 10^{32}r^2\theta^3}\right) / \left(\sqrt{-3.03818 \times 10^{18} + 2.41771 \times 10^{17}\theta + 9.67083 \times 10^{17}r^2\theta - 1.53916 \times 10^{17}r^2\theta^2 + 6.12412 \times 10^{15}r^2\theta^3}\right)\right\}\right\}$$

$$r := \frac{2\pi\sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

```

RevolutionPlot3D[ - (1. `  $\sqrt{(-2.7305802448854928 \cdot 10^{35} +$   

    2.1729267174130213 `  $\cdot 10^{34} \theta + 8.691706869652085 \cdot 10^{34} r^2 \theta -$   

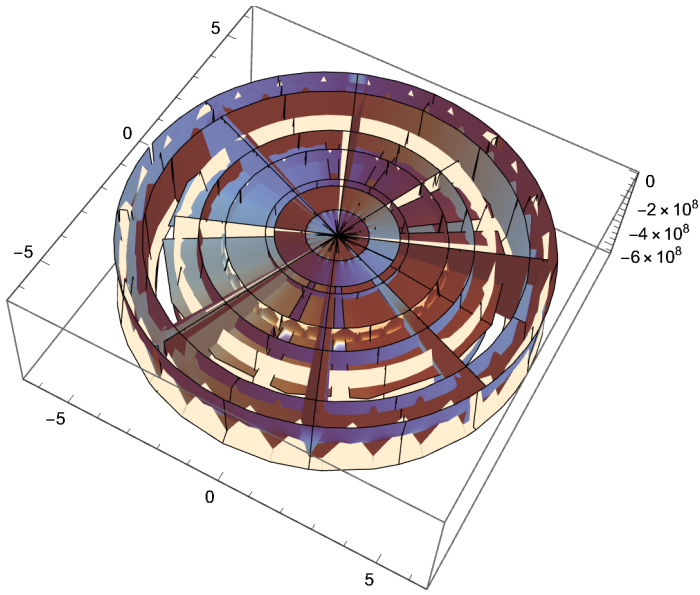
    1.3833281122109134 `  $\cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3)}$ ) /  

    ( $\sqrt{(-3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta +$   

    9.670828135720014 `  $\cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 +$   

    6.124123459454841 `  $\cdot 10^{15} r^2 \theta^3)}$ ), { $\theta, -2 \pi, 2 \pi$ }]

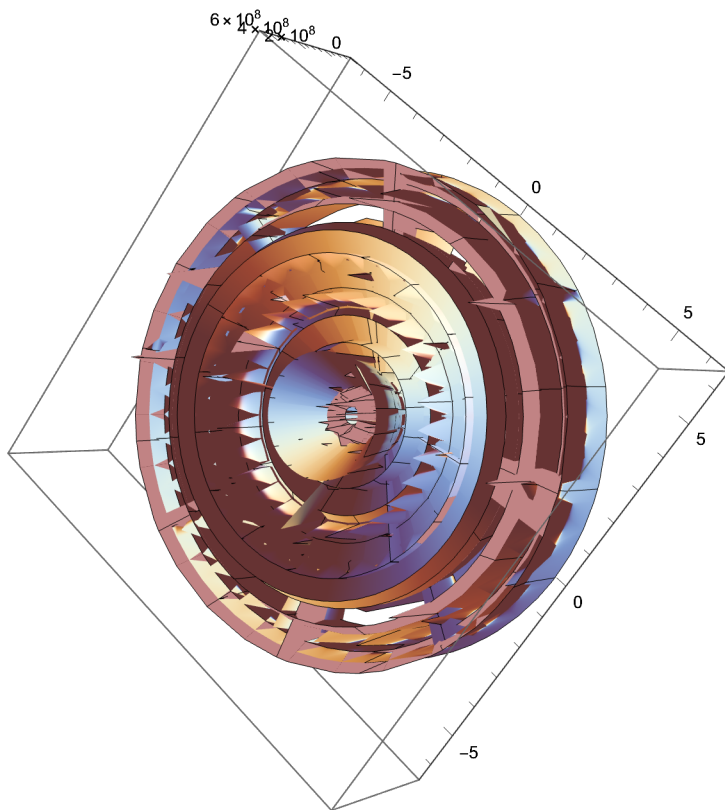
```



RevolutionPlot3D[

$$\left( \sqrt{\left( -2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \theta + 8.691706869652085 \cdot 10^{34} r^2 \theta - 1.3833281122109134 \cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3 \right)} \right) /$$

$$\left( \sqrt{\left( -3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta + 9.670828135720014 \cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 + 6.124123459454841 \cdot 10^{15} r^2 \theta^3 \right)} \right), \{\theta, -2\pi, 2\pi\}]$$



Solve[

$$\left( \sqrt{\left( -2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \theta + 8.691706869652085 \cdot 10^{34} r^2 \theta - 1.3833281122109134 \cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3 \right)} \right) /$$

$$\left( \sqrt{\left( -3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta + 9.670828135720014 \cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 + 6.124123459454841 \cdot 10^{15} r^2 \theta^3 \right)} \right) ==$$

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), \theta]$$

{{\theta \rightarrow 0.}}



Solve[  

$$\left( \sqrt{\left( -2.7305802448854928 \cdot r^{35} + 2.1729267174130213 \cdot r^{34} \theta + 8.691706869652085 \cdot r^{34} r^2 \theta - 1.3833281122109134 \cdot r^{34} r^2 \theta^2 + 5.504087674408674 \cdot r^{32} r^2 \theta^3 \right)} \right) /$$

$$\left( \sqrt{\left( -3.038180262530747 \cdot r^{18} + 2.4177070339300032 \cdot r^{17} \theta + 9.670828135720014 \cdot r^{17} r^2 \theta - 1.5391601015920192 \cdot r^{17} r^2 \theta^2 + 6.124123459454841 \cdot r^{15} r^2 \theta^3 \right)} \right) ==$$

$$\left( \sqrt{\left( -1.1294090667581471 \cdot r^{18} \theta + 8.987551787368176 \cdot r^{16} \theta^2 + 3.5481432270250993 \cdot r^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), r]$$

$$\{\{r \rightarrow 0.\}\}$$

Solve[  

$$\left( \sqrt{\left( -2.7305802448854928 \cdot r^{35} + 2.1729267174130213 \cdot r^{34} \theta + 8.691706869652085 \cdot r^{34} r^2 \theta - 1.3833281122109134 \cdot r^{34} r^2 \theta^2 + 5.504087674408674 \cdot r^{32} r^2 \theta^3 \right)} \right) /$$

$$\left( \sqrt{\left( -3.038180262530747 \cdot r^{18} + 2.4177070339300032 \cdot r^{17} \theta + 9.670828135720014 \cdot r^{17} r^2 \theta - 1.5391601015920192 \cdot r^{17} r^2 \theta^2 + 6.124123459454841 \cdot r^{15} r^2 \theta^3 \right)} \right) ==$$

$$\left( \sqrt{\left( -1.1294090667581471 \cdot r^{18} \theta + 8.987551787368176 \cdot r^{16} \theta^2 + 3.5481432270250993 \cdot r^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), \beta]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

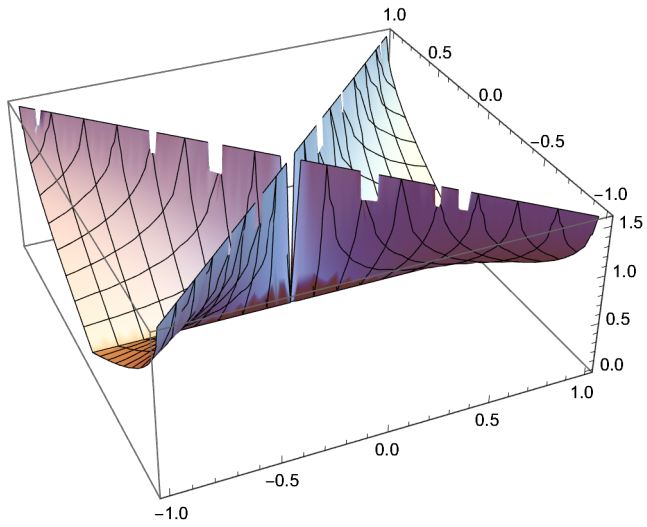
$$\left\{ \left\{ \beta \rightarrow -1. \operatorname{ArcSin} \left[ 8.42244 \times 10^{-9} \sqrt{4.48719 \times 10^{15} - 3.57079 \times 10^{14} \theta} \sqrt{\theta} \right] \right\}, \right.$$

$$\left. \left\{ \beta \rightarrow \operatorname{ArcSin} \left[ 8.42244 \times 10^{-9} \sqrt{4.48719 \times 10^{15} - 3.57079 \times 10^{14} \theta} \sqrt{\theta} \right] \right\} \right\}$$

Plot3D[ArcSin[8.422437466061065`\*^-9

$$\sqrt{4.487190804107819`*^{15} - 3.57079298535128`*^{14} \frac{2\pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}}$$

$$\sqrt{\frac{2\pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}}], \{r, -1, 1\}, \{\eta, -1, 1\}]$$

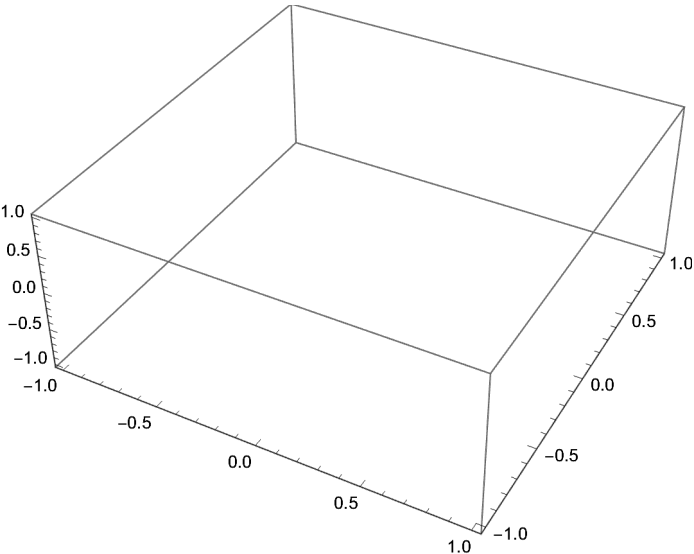


Plot3D[

$$\text{ArcSin}\left[8.422437466061065`*^{-9}\sqrt{\left(4.487190804107819`*^{15}-3.57079298535128`*^{14}\times\right.}\right.$$

$$\left.2\left(2\pi+\frac{\pi}{3^{1/3}\left(9r^4+\sqrt{3}\sqrt{r^6+27r^8}\right)^{1/3}}-\frac{\pi\left(9r^4+\sqrt{3}\sqrt{r^6+27r^8}\right)^{1/3}}{3^{2/3}r^2}\right)\right]$$

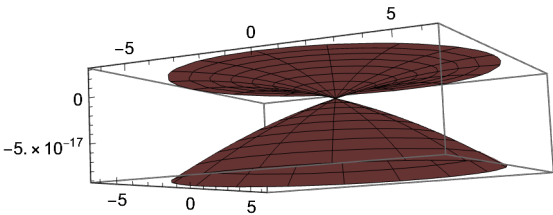
$$\sqrt{\frac{2\pi\left(r^2+\sqrt{r^4-r^2\eta^2}\right)}{r^2}}\right],\{r,-1,1\},\{\eta,-1,1\}]$$



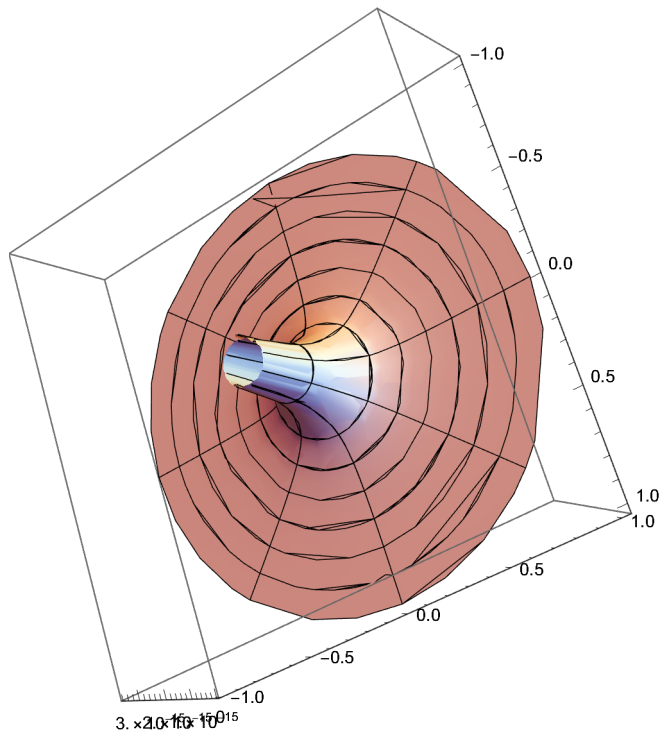
$$\frac{h\left(c^2+r^2\right)}{2r^2}$$

$$r:=\frac{2\pi\sqrt{\left(4\pi-\theta\right)\theta}}{\left(4\pi-\theta\right)\theta}$$

RevolutionPlot3D[
$$\frac{h\left(c^2+r^2\right)}{2r^2},\{\theta,-2\pi,2\pi\}]$$



$$\text{RevolutionPlot3D}\left[\frac{h\left(c^2 + \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\right)}{2(r)^2}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



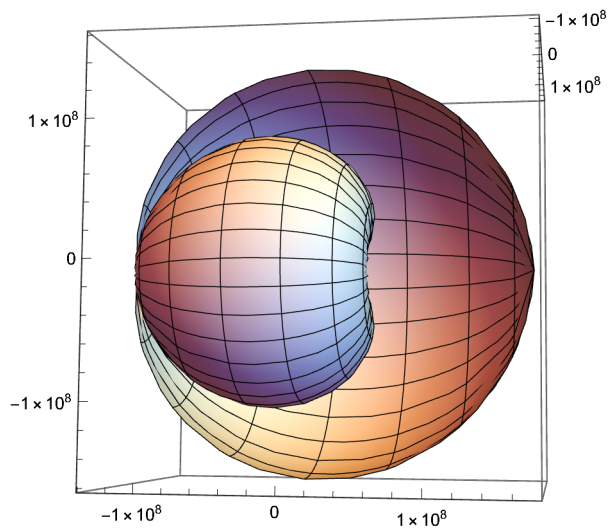
SphericalPlot3D[

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \right.} \right.$$

$$\left. \left. \left. \sin \left[ \text{ArcSin} \left[ \frac{\sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta}}{2 \pi} \right] \right]^2 \right) \right] \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin \left[ \text{ArcSin} \left[ \right. \right. \right. \right.$$

$$\left. \left. \left. \frac{\sqrt{\left( 4 \pi - \theta \right) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{2 \pi} \right] \right]^2 \right) \right] \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



$$\left( \sqrt[3]{ \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \\ \left. \left. 3.5481432270250993 \cdot \sin \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \theta)}{2\pi} \right] \right] \right)^2 \right) /$$

$$\left( \sqrt[3]{ \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \right. \right. \\ \left. \left. \sin \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta) 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}}{2\pi} \right] \right] \right)^2 \right) \right)$$

$$\text{Solve} \left[ \frac{1}{2\pi} \left( \sqrt[3]{ \left( 4\pi r^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \right. \right. \right. \\ \left. \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\ \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \\ \left. r^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \right. \right. \\ \left. \left. \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 \right) \right] = \\ \left. r \sin \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{-4\pi^2 \theta + 4\pi \theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}} \right] \right], \right. \\ \left. \theta \right]$$

Solve::verif : Potential solution  $\{\theta \rightarrow \text{ComplexInfinity}\}$  (possibly discarded by verifier) should be checked by hand.  
May require use of limits. >>

$$\left\{ \left\{ \theta \rightarrow \right. \right. \\ \frac{4\pi}{3} + \left( 2^{1/3} \left( -1296\pi^2 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \right. \\ \left. 324 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right. \\ \left. \left( -\pi^2 + 50\pi^2 \sin[\beta]^2 - 453\pi^2 \sin[\beta]^4 + 36\pi^2 \sin[\beta]^6 + \right. \right. \\ \left. \left. 5\sqrt{3}\pi^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \right.$$

$$\begin{aligned}
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 9 \sqrt{3} \pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + 243 \\
& \quad \pi^2 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 9 \pi^2 \sin[\beta]^6 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + 5 \pi^2 \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - 88 \pi^2 \sin[\beta]^2 \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - 36 \\
& \quad \pi^2 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - \\
& 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} \Big) \Big) \Big) \Big) / \\
& \left( 27 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{5/3} \right. \\
& \left. \left( 128304 \pi^3 - 46049472 \pi^3 \sin[\beta]^2 + 3084719760 \pi^3 \sin[\beta]^4 - \right. \right. \\
& \quad 76984149600 \pi^3 \sin[\beta]^6 + 791034575760 \pi^3 \sin[\beta]^8 - \\
& \quad 2463947543232 \pi^3 \sin[\beta]^{10} - 4120487403984 \pi^3 \sin[\beta]^{12} - \\
& \quad 430339664160 \pi^3 \sin[\beta]^{14} - 9183300480 \pi^3 \sin[\beta]^{16} - \\
& \quad 1924560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240395040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8641939248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116076162240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464847899760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696655378080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43748223120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad \left. \left. 306110016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69984 \pi^3 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 22\,394\,880 \\
& \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 69\,984 \pi^3 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 19\,455\,552 \\
& \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3}
\end{aligned}$$



$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} + 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \left. \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \right. \\
& \quad \left. 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \right. \\
& \quad \left. \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\
& \quad \left. 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right. \\
& \quad \left. 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\
& \quad \left. 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right. \\
& \quad \left. 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right.
\end{aligned}$$

$$\begin{aligned}
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \pi^3 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008 \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 4 \left( -1296 \pi^2 \right. \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left. \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \sin[\beta]^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 35 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 9 \pi^2 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \right. \\
& \left. \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 5 \pi^2 \left( -1 + 18 \right. \\
& \left. \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 36 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 15 \sqrt{3} \pi^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^3 \Big)^{1/3} \Big) - \\
& \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \\
& \pi^3 \\
& \sin[\beta]^6 + 791\,034\,575\,760 \\
& \pi^3 \\
& \sin[\beta]^8 - 2\,463\,947\,543\,232 \\
& \pi^3 \\
& \sin[\beta]^{10} - 4\,120\,487\,403\,984 \\
& \pi^3 \\
& \sin[\beta]^{12} - 430\,339\,664\,160 \\
& \pi^3 \\
& \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \pi^3 \\
& \sin[\beta]^{16} - 1\,924\,560 \\
& \sqrt{3} \\
& \pi^3 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 240\,395\,040 \\
& \sqrt{3} \\
& \pi^3 \\
& \sin[\beta]^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -
\end{aligned}$$

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$$\pi^3 \sin[\beta]^2$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$1412976960 \pi^3 \sin[\beta]^4$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -$$

$$34362423936 \pi^3 \sin[\beta]^6$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$361323192960 \pi^3 \sin[\beta]^8$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -$$

$$1382528881152 \pi^3 \sin[\beta]^{10}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$10033606080 \pi^3 \sin[\beta]^{12}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$11224033920 \pi^3 \sin[\beta]^{14}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$153055008 \pi^3 \sin[\beta]^{16}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -$$

$$979776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$112534272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -$$

$$3868575552 \sqrt{3} \pi^3 \sin[\beta]^4$$

$$\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$52016027904 \sqrt{3} \pi^3 \sin[\beta]^6$$

$$\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -$$

$$241951624128 \sqrt{3} \pi^3 \sin[\beta]^8$$

$$\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10}$$

$$\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}$$

$$\left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} +$$

$$\begin{aligned}
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} +
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left( (128\,304\,\pi^3 - 46\,049\,472\,\pi^3 \sin[\beta]^2 + 3\,084\,719\,760\,\pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760\,\pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232\,\pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984\,\pi^3 \sin[\beta]^{12} - 430\,339\,664\,160\,\pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016\,\sqrt{3}\,\pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \\
& \quad \pi^3 (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& \quad 22\,394\,880\,\pi^3 \sin[\beta]^2 (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad 1\,412\,976\,960\,\pi^3 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& \quad 34\,362\,423\,936\,\pi^3 \sin[\beta]^6 (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad 361\,323\,192\,960\,\pi^3 \sin[\beta]^8 (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& \quad 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + 153\,055\,008\,\pi^3 \sin[\beta]^{16} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& \quad 979\,776\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& \quad 112\,534\,272\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$



$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3868575552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52016027904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 19455552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} +
\end{aligned}$$

$$\begin{aligned}
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^2 + \\
& 4 \left( -1296 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \sin[\beta]^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 9 \pi^2 \sin[\beta]^6 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 42 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 5 \pi^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \right. \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \right. \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} - 6 \sqrt{3} \pi^2 \\
& \quad \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} \right)^3 \Big)^{1/3} / \\
& \left( 27 \times 2^{1/3} (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3})^{5/3} \right), \{ \theta \rightarrow \\
& \frac{4 \pi}{3} - \\
& \left( (1 + \right. \\
& \quad \left. i \sqrt{3}) \right. \\
& \left. (-1296 \pi^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3})^{10/3} - \right. \\
& \quad 324 \\
& \quad \left. (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3})^{5/3} \right. \\
& \quad \left. (-\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& \quad 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 9 \sqrt{3} \pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad \left. \pi^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \right. \\
& \quad 35 \pi^2 \sin[\beta]^2 \\
& \quad \left. (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + 243 \pi^2 \right. \\
& \quad \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \\
& \quad 9 \pi^2 \sin[\beta]^6 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \\
& \quad 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left. (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \\
& \quad 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left. (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \\
& \quad 5 \pi^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} - \\
& \quad 88 \pi^2 \sin[\beta]^2 \\
& \quad \left. (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} - 36 \pi^2 \right. \\
& \quad \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} - \\
& \quad \left. 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big) \Big) \Big) / \\
& \left( 27 \times 2^{2/3} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right. \\
& \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + \right. \\
& 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \pi^3 \sin[\beta]^6 + \\
& 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - \\
& 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \pi^3 \sin[\beta]^{16} - \\
& 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008
\end{aligned}$$

$$\begin{aligned}
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} -
\end{aligned}$$

$$\begin{aligned}
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \pi^3 \right. \right. \\
& \quad \left. \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad \left. \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 361\,323\,192\,960\,\pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 153\,055\,008\,\pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} - \\
& 979\,776\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 112\,534\,272\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} - \\
& 3\,868\,575\,552\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 52\,016\,027\,904\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} - \\
& 241\,951\,624\,128\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 12\,788\,596\,224\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} + \\
& 1\,122\,403\,392\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{1/3} - \\
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 19\,455\,552\,\pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} - \\
& 1\,082\,722\,464\,\pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} +
\end{aligned}$$

$$\begin{aligned}
& 23\,329\,866\,240\,\pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} - \\
& 217\,196\,393\,760\,\pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 725\,922\,896\,832\,\pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 79\,877\,708\,064\,\pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 1\,632\,586\,752\,\pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 909\,792\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} - \\
& 91\,119\,168\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 2\,737\,984\,032\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} - \\
& 32\,062\,189\,824\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 127\,925\,643\,168\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 8\,060\,897\,088\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} + \\
& 51\,018\,336\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{2/3} \Big)^2 + 4 \left( -1296\,\pi^2 \right. \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} \right)^{5/3} \\
& \quad \left( -\pi^2 + 50\,\pi^2 \sin[\beta]^2 - 453\,\pi^2 \sin[\beta]^4 + 36\,\pi^2 \sin[\beta]^6 + \right. \\
& \quad 5\,\sqrt{3}\,\pi^2 \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} - 78\,\sqrt{3}\,\pi^2 \sin[\beta]^2 \\
& \quad \left. \sqrt{\sin[\beta]^2 \left( -1 + 11 \sin[\beta]^2 + \sin[\beta]^4 \right)} + 9\,\sqrt{3}\,\pi^2 \sin[\beta]^4 \right)
\end{aligned}$$



$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 35 \pi^2 \sin[\beta]^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 9 \pi^2 \sin[\beta]^6 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \\
& \quad \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + 5 \pi^2 (-1 + 18 \\
& \quad \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - \\
& 36 \pi^2 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - 15 \sqrt{3} \pi^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3} - 6 \sqrt{3} \pi^2 \\
& \quad \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{2/3})^3)^{1/3} + \\
& \left( (1 - i \sqrt{3}) \left( 128 304 \pi^3 - 46 049 472 \pi^3 \sin[\beta]^2 + 3 084 719 760 \pi^3 \sin[\beta]^4 - \right. \right. \\
& \quad 76 984 149 600 \pi^3 \sin[\beta]^6 + \\
& \quad 791 034 575 760 \pi^3 \sin[\beta]^8 - \\
& \quad 2 463 947 543 232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4 120 487 403 984 \pi^3 \sin[\beta]^{12} - \\
& \quad 430 339 664 160 \pi^3 \sin[\beta]^{14} - \\
& \quad 9 183 300 480 \pi^3 \sin[\beta]^{16} - \\
& \quad \left. \left. 1 924 560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984 \pi^3 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \pi^3 \right. \right. \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& \quad 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad \left. \left. 153\,055\,008 \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \\
& 979776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112534272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3868575552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52016027904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^2 + 4 \left( -1296 \pi^2 \right. \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& \quad \left. 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right. \\
& \quad \left. \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \right. \\
& \quad \left. \left. 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \sin[\beta]^2 \right. \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \right. \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 35 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \right. \\
& \quad \left. \left. 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \right. \\
& \quad \left. \left. 9 \pi^2 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 42\sqrt{3}\pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 5\pi^2 (-1 + 18 \\
& \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88\pi^2 \sin[\beta]^2 (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \\
& \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 36\pi^2 \sin[\beta]^4 (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \\
& \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 15\sqrt{3}\pi^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18\sin[\beta]^2 + \\
& 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6\sqrt{3}\pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18\sin[\beta]^2 + \\
& 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^{1/3} \Big) / \\
& \left( 54 \times 2^{1/3} (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \Big) \Big\}, \left\{ \theta \rightarrow \right. \\
& \frac{4\pi}{3} - \\
& \left( (1 - \right. \\
& \quad \left. \sqrt{3}) \right. \\
& \left. (-1296\pi^2 (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \\
& 324 \\
& \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50\pi^2 \sin[\beta]^2 - 453\pi^2 \sin[\beta]^4 + 36\pi^2 \sin[\beta]^6 + \right. \\
& 5\sqrt{3}\pi^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78\sqrt{3}\pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\
& 9\sqrt{3}\pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\
& \pi^2 (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - \\
& 35\pi^2 \sin[\beta]^2 \\
& \left. (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 243\pi^2 \\
& \sin[\beta]^4 (-1 + 18\sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} +
\end{aligned}$$

$$\begin{aligned}
& 9 \pi^2 \operatorname{Sin}[\beta]^6 \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \\
& \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{1/3} + \\
& 42 \sqrt{3} \pi^2 \operatorname{Sin}[\beta]^2 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \\
& \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{1/3} + \\
& 5 \pi^2 \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \operatorname{Sin}[\beta]^2 \\
& \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{2/3} - 36 \pi^2 \\
& \operatorname{Sin}[\beta]^4 \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{2/3} - \\
& 15 \sqrt{3} \pi^2 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \\
& \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{2/3} - \\
& 6 \sqrt{3} \pi^2 \operatorname{Sin}[\beta]^2 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \\
& \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{2/3} \Big) \Big) \Big) / \\
& \left( 27 \times 2^{2/3} \left( -1 + 18 \operatorname{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} \right)^{5/3} \right. \\
& \left. \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \operatorname{Sin}[\beta]^2 + \right. \right. \\
& 3\,084\,719\,760 \pi^3 \operatorname{Sin}[\beta]^4 - \\
& 76\,984\,149\,600 \pi^3 \operatorname{Sin}[\beta]^6 + \\
& 791\,034\,575\,760 \pi^3 \operatorname{Sin}[\beta]^8 - \\
& 2\,463\,947\,543\,232 \pi^3 \operatorname{Sin}[\beta]^{10} - \\
& 4\,120\,487\,403\,984 \pi^3 \operatorname{Sin}[\beta]^{12} - \\
& 430\,339\,664\,160 \pi^3 \operatorname{Sin}[\beta]^{14} - \\
& 9\,183\,300\,480 \pi^3 \operatorname{Sin}[\beta]^{16} - \\
& 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} + \\
& 240\,395\,040 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^2 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} - \\
& 8\,641\,939\,248 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^4 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^6 \\
& \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^8 \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^{10} \\
& \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^{12} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \operatorname{Sin}[\beta]^{14} \sqrt{\operatorname{Sin}[\beta]^2 (-1 + 11 \operatorname{Sin}[\beta]^2 + \operatorname{Sin}[\beta]^4)} +
\end{aligned}$$



$$\begin{aligned}
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880\,\pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960\,\pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936\,\pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960\,\pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776\sqrt{3}\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272\sqrt{3}\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552\sqrt{3}\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904\sqrt{3}\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128\sqrt{3}\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224\sqrt{3}\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392\sqrt{3}\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3\sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552\,\pi^3 \sin[\beta]^2
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128304 \pi^3 - 46049472 \pi^3 \sin[\beta]^2 + 3084719760 \pi^3 \sin[\beta]^4 - 76984149600 \right. \right. \\
& \quad \left. \left. \pi^3 \sin[\beta]^6 + 791034575760 \pi^3 \sin[\beta]^8 - 2463947543232 \pi^3 \sin[\beta]^{10} - \right. \right. \\
& \quad \left. \left. 4120487403984 \pi^3 \sin[\beta]^{12} - 430339664160 \pi^3 \sin[\beta]^{14} - 9183300480 \right. \right. \\
& \quad \left. \left. \pi^3 \sin[\beta]^{16} - 1924560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \right. \\
& \quad \left. \left. 240395040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \pi^3 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008 \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 4 \left( -1296 \pi^2 \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^{10/3} - \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \sin[\beta]^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 (-1 + 18 \sin[\beta]^2 + \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - \\
& 35 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 9 \pi^2 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 36 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} -
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} - 15 \sqrt{3} \pi^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} - 6 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} \Big)^3 \Big)^{1/3} \Big) + \\
& \left( (1 + i \sqrt{3}) \left( 128 304 \pi^3 - 46 049 472 \pi^3 \sin[\beta]^2 + 3 084 719 760 \pi^3 \sin[\beta]^4 - \right. \right. \\
& 76 984 149 600 \pi^3 \sin[\beta]^6 + \\
& 791 034 575 760 \pi^3 \sin[\beta]^8 - \\
& 2 463 947 543 232 \pi^3 \sin[\beta]^{10} - \\
& 4 120 487 403 984 \pi^3 \sin[\beta]^{12} - \\
& 430 339 664 160 \pi^3 \sin[\beta]^{14} - \\
& 9 183 300 480 \pi^3 \sin[\beta]^{16} - \\
& 1 924 560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 240 395 040 \sqrt{3} \pi^3 \sin[\beta]^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8 641 939 248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116 076 162 240 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464 847 899 760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696 655 378 080 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43 748 223 120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306 110 016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69 984 \pi^3 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 22 394 880 \pi^3 \sin[\beta]^2 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 1 412 976 960 \pi^3 \sin[\beta]^4 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} - \\
& 34 362 423 936 \pi^3 \sin[\beta]^6 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} + \\
& 361 323 192 960 \pi^3 \sin[\beta]^8 \\
& (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)})^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008\,\pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128304 \pi^3 - 46049472 \pi^3 \sin[\beta]^2 + 3084719760 \pi^3 \sin[\beta]^4 - 76984149600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791034575760 \pi^3 \sin[\beta]^8 - 2463947543232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4120487403984 \pi^3 \sin[\beta]^{12} - 430339664160 \pi^3 \sin[\beta]^{14} - 9183300480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1924560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240395040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8641939248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116076162240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464847899760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696655378080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43748223120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306110016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69984 \pi^3 \right) \right)
\end{aligned}$$



$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22394880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1412976960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34362423936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361323192960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1382528881152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10033606080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11224033920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153055008 \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112534272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3868575552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52016027904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 4 \left( -1296 \pi^2 \right. \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \quad \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& \quad 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \sin[\beta]^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - \\
& 35 \pi^2 \sin[\beta]^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + \\
& 9 \pi^2 \sin[\beta]^6 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \\
& \quad \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 5 \pi^2 (-1 + 18 \\
& \quad \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - \\
& 36 \pi^2 \sin[\beta]^4 (-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - 15 \sqrt{3} \pi^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \quad \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} (-1 + 18 \sin[\beta]^2 + \\
& \quad 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} \Big)^{1/3} \Big) /
\end{aligned}$$

$$\left( 54 \times 2^{1/3} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right) \}$$

RevolutionPlot3D[

$$\begin{aligned} & \frac{4\pi}{3} + \left( 2^{1/3} \left( -1296\pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \right. \\ & \quad 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\ & \quad \left( -\pi^2 + 50\pi^2 \sin[\beta]^2 - 453\pi^2 \sin[\beta]^4 + 36\pi^2 \sin[\beta]^6 + \right. \\ & \quad 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\ & \quad 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\ & \quad 9 \sqrt{3} \pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\ & \quad \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 35\pi^2 \\ & \quad \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 243 \\ & \quad \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & \quad 9\pi^2 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\ & \quad 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\ & \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & \quad 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\ & \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & \quad 5\pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & \quad 88\pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & \quad 36\pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & \quad 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\ & \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & \quad 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\ & \quad \left. \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \right) \right) \right) / \\ & \left( 27 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right) \end{aligned}$$

$$\begin{aligned}
& \left( 128\,304\,\pi^3 - 46\,049\,472\,\pi^3 \sin[\beta]^2 + 3\,084\,719\,760\,\pi^3 \sin[\beta]^4 - 76\,984\,149\,600\,\pi^3 \sin[\beta]^6 + \right. \\
& 791\,034\,575\,760\,\pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232\,\pi^3 \sin[\beta]^{10} - \\
& 4\,120\,487\,403\,984\,\pi^3 \sin[\beta]^{12} - 430\,339\,664\,160\,\pi^3 \sin[\beta]^{14} - \\
& 9\,183\,300\,480\,\pi^3 \sin[\beta]^{16} - 1\,924\,560\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 240\,395\,040\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8\,641\,939\,248\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016\,\sqrt{3}\,\pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880\,\pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1\,412\,976\,960 \\
& \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936\,\pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 361\,323\,192\,960\,\pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3\,\sqrt{3}\,\sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3868575552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52016027904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 1082722464 \\
& \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 217196393760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 79877708064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 1632586752 \\
& \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} +
\end{aligned}$$

$$\begin{aligned}
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \\
& \quad \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad \left. \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \right. \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + 153\,055\,008 \pi^3 \sin[\beta]^{16} \right. \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \right. \right. \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \right. \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \right. \right. \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \right. \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \right. \right. \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \right. \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} + \right. \right. \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} - \right. \right. \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}^{2/3} + 19\,455\,552 \pi^3 \sin[\beta]^2 \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^2 + 4 \left( -1296 \pi^2 \right. \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& \quad 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \quad \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& \quad 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \\
& \quad \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& \quad 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 9 \pi^2 \sin[\beta]^6 \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& \quad 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 42 \sqrt{3} \pi^2 \\
& \quad \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 5 \pi^2 \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \right. \\
& \quad 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \right. \\
& \quad 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \quad \left. \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} \Big)^3 \Big)^{1/3} \Big) - \\
& \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \\
& \quad \pi^3 \\
& \quad \sin[\beta]^6 + 791\,034\,575\,760 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^8 - 2\,463\,947\,543\,232 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{10} - 4\,120\,487\,403\,984 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{12} - 430\,339\,664\,160 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{16} - 1\,924\,560 \\
& \quad \sqrt{3} \pi^3 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 240\,395\,040 \\
& \quad \sqrt{3} \pi^3 \\
& \quad \sin[\beta]^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 22\,394\,880 \pi^3 \sin[\beta]^2 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 1\,412\,976\,960 \pi^3 \sin[\beta]^4
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008 \pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} +
\end{aligned}$$

$$\begin{aligned}
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad \left. \left. 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \right. \\
& \quad \left. \left. 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \right. \\
& \quad \left. \left. 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right) \right)
\end{aligned}$$

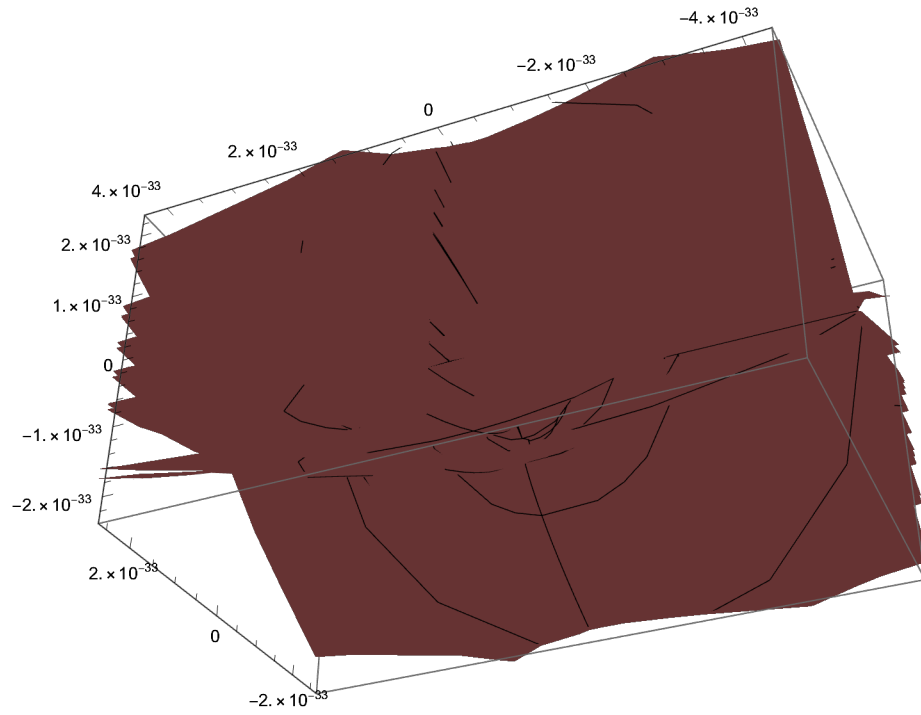
$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112534272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3868575552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52016027904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^2 + \\
& 4 \left( -1296 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \\
& \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 9 \pi^2 \sin[\beta]^6 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right.
\end{aligned}$$



$$\begin{aligned}
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 5 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^{1/3} \Big) / \\
& \left( 27 \times 2^{1/3} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right), \\
& \{\beta, \\
& -\pi / \\
& 2, \\
& \pi / \\
& 2\} \Big]
\end{aligned}$$

$$\text{SphericalPlot3D} \left[ \frac{h \left( c^2 + \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\} \right]$$



$$\alpha = \text{GoldenRatio}[\xi]$$

$$\eta = r \sin[\beta] = r_2 \sin[\phi] = r_3 \sin[\gamma]$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \left(\frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}\right)^2}}{2 \pi} == r \sin[\beta], r\right]$$

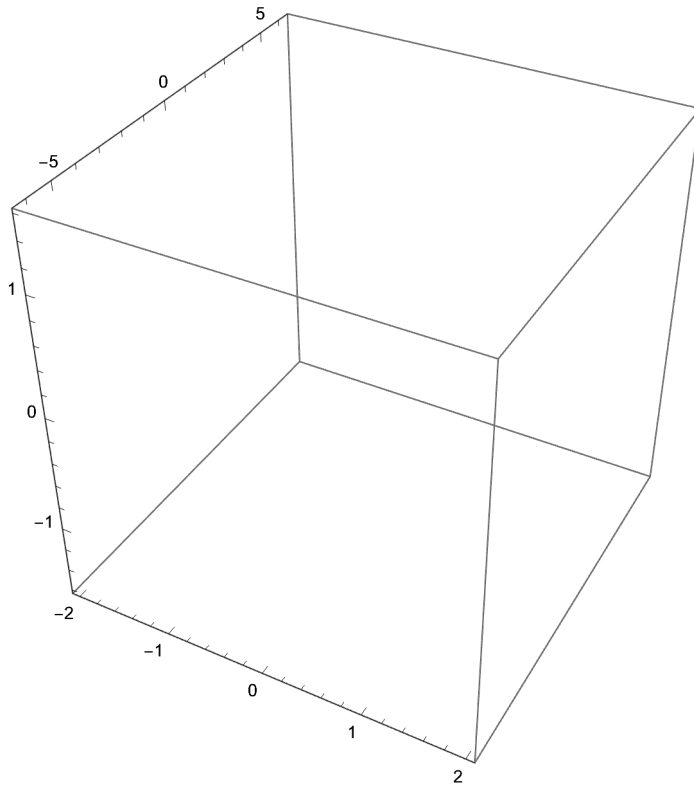
$$\left\{\left\{r \rightarrow -\sqrt{\left(-\frac{\pi \eta^2 \theta}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{\pi^2 \eta^2 \sin[\beta]^2}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} - \frac{2 \pi^{3/2} \sqrt{-\eta^4 (-\theta + \pi \sin[\beta]^2)}}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4}\right)}\right\},\right.$$

$$\left\{r \rightarrow \sqrt{\left(-\frac{\pi \eta^2 \theta}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{\pi^2 \eta^2 \sin[\beta]^2}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} - \frac{2 \pi^{3/2} \sqrt{-\eta^4 (-\theta + \pi \sin[\beta]^2)}}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4}\right)}\right\},$$

$$\left\{r \rightarrow -\sqrt{\left(-\frac{\pi \eta^2 \theta}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{\pi^2 \eta^2 \sin[\beta]^2}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{2 \sqrt{\pi^3 \eta^4 \theta - \pi^4 \eta^4 \sin[\beta]^2}}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4}\right)}\right\},$$

$$\left\{r \rightarrow \sqrt{\left(-\frac{\pi \eta^2 \theta}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{\pi^2 \eta^2 \sin[\beta]^2}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{2 \sqrt{\pi^3 \eta^4 \theta - \pi^4 \eta^4 \sin[\beta]^2}}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4}\right)}\right\}}$$

$$\text{ContourPlot3D}\left[\sqrt{\left(-\frac{\pi \eta^2 \theta}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{\pi^2 \eta^2 \sin[\beta]^2}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4} + \frac{2 \sqrt{\pi^3 \eta^4 \theta - \pi^4 \eta^4 \sin[\beta]^2}}{-4 \pi \theta + \theta^2 + 4 \pi^2 \sin[\beta]^2 - 2 \pi \theta \sin[\beta]^2 + \pi^2 \sin[\beta]^4}\right)}, \{\eta, -2, 2\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$



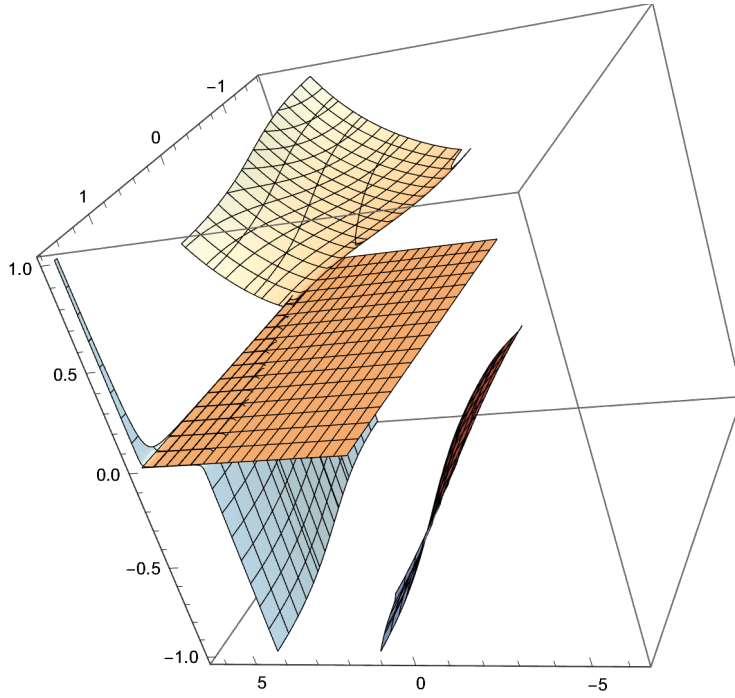
$$\theta r = 2 \pi r - 2 \pi x$$

$$\theta r = 2 \pi r - 2 \pi x$$

$$\text{Solve}\left[\theta r - (2 \pi r - 2 \pi x) == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - r \sin[\beta], x\right]$$

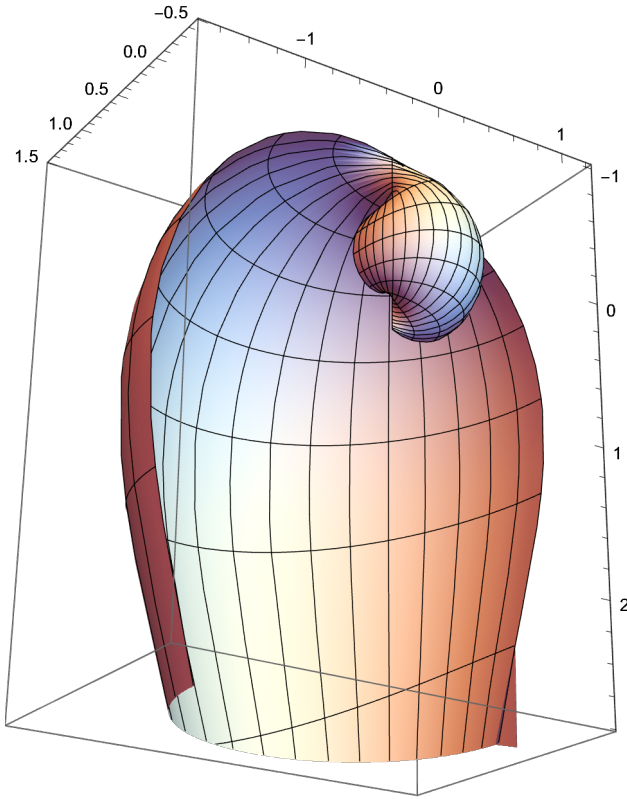
$$\left\{\left\{x \rightarrow \frac{4 \pi^2 r - 2 \pi r \theta + \sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi r \sin[\beta]}{4 \pi^2}\right\}\right\}$$

```
ContourPlot3D[ $\frac{4 \pi^2 r - 2 \pi r \theta + \sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi r \sin[\beta]}{4 \pi^2}$ ,  
{r, -1, 1}, {\theta, -2 \pi, 2 \pi}, {\beta, -\pi / 2, \pi / 2}]
```



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

SphericalPlot3D $\left[\frac{4 \pi^2 r - 2 \pi r \theta + \sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi r \sin[\beta]}{4 \pi^2},\right.$   
 $\left.\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



Solve $\left[\frac{4 \pi^2 r - 2 \pi r \theta + \sqrt{r^2 (4 \pi - \theta) \theta} - 2 \pi r \sin[\beta]}{4 \pi^2} == \frac{2 \pi r - r \theta}{2 \pi}, r\right]$

{{r → 0}}

$$\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{ \left\{ \beta \rightarrow \text{ArcCsc} \left[ \right. \right. \right.$$

$$\begin{aligned} & \left( -64 \pi^4 r \eta^2 \theta^2 \sqrt{(4\pi - \theta) \theta} \sqrt{\left( (256 \pi^7 \eta^2 \theta^3) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + \right. \right. \\ & \quad 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (320 \pi^6 \eta^2 \theta^4) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + \\ & \quad 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + (128 \pi^5 \eta^2 \theta^5) / \\ & \quad (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - \\ & \quad (16 \pi^4 \eta^2 \theta^6) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - \\ & \quad 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - \left( 128 \pi^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} \right) / \\ & \quad \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) \right) + \\ & 80 \pi^3 r \eta^2 \theta^3 \sqrt{(4\pi - \theta) \theta} \sqrt{\left( (256 \pi^7 \eta^2 \theta^3) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + \right. \\ & \quad 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (320 \pi^6 \eta^2 \theta^4) / \\ & \quad (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + \\ & \quad (128 \pi^5 \eta^2 \theta^5) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + \\ & \quad 8 \pi \theta^9 - \theta^{10}) - (16 \pi^4 \eta^2 \theta^6) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + \\ & \quad 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - \left( 128 \pi^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} \right) / \\ & \quad \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) \right) - \\ & 32 \pi^2 r \eta^2 \theta^4 \sqrt{(4\pi - \theta) \theta} \sqrt{\left( (256 \pi^7 \eta^2 \theta^3) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + \right. \\ & \quad 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (320 \pi^6 \eta^2 \theta^4) / \\ & \quad (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) + \\ & \quad (128 \pi^5 \eta^2 \theta^5) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + \\ & \quad 8 \pi \theta^9 - \theta^{10}) - (16 \pi^4 \eta^2 \theta^6) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + \\ & \quad 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - \left( 128 \pi^6 \sqrt{\eta^4 (2\pi - \theta)^2 (4\pi - \theta)^3 \theta^3} \right) / \\ & \quad \left. (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) \right) + \\ & 4 \pi r \eta^2 \theta^5 \sqrt{(4\pi - \theta) \theta} \sqrt{\left( (256 \pi^7 \eta^2 \theta^3) / (1024 \pi^7 \theta^3 - 1280 \pi^6 \theta^4 + 512 \pi^5 \theta^5 - \right. \\ & \quad 80 \pi^4 \theta^6 + 32 \pi^3 \theta^7 - 24 \pi^2 \theta^8 + 8 \pi \theta^9 - \theta^{10}) - (320 \pi^6 \eta^2 \theta^4) / \end{aligned}$$



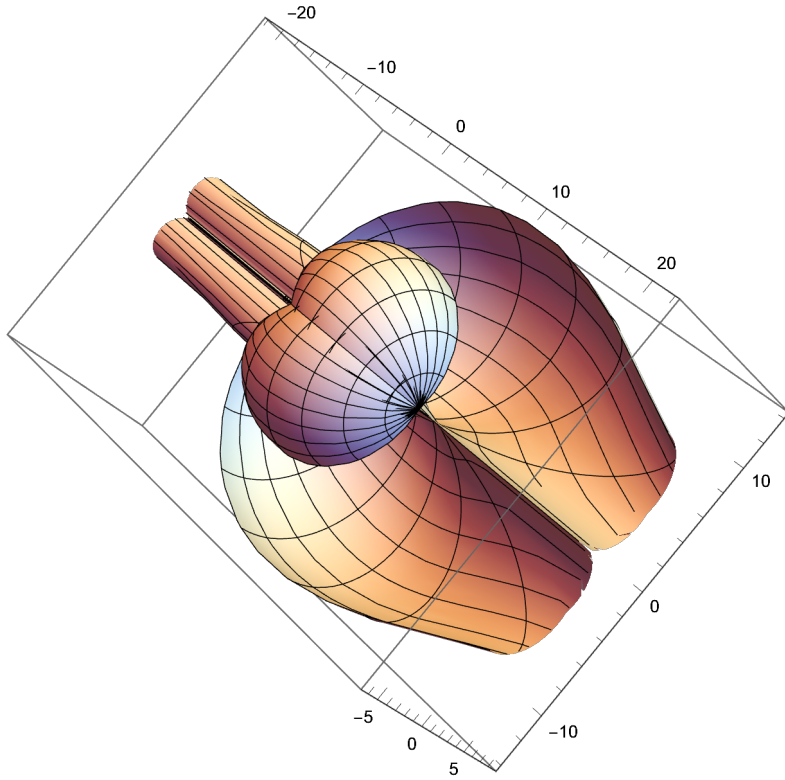


[illegible]



$$\text{SphericalPlot3D}\left[\left\{2\left(\pi - \sqrt{-\pi^2 + \pi^2 \text{Csc}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 \text{Sin}[\beta]\right),\right.\right.$$

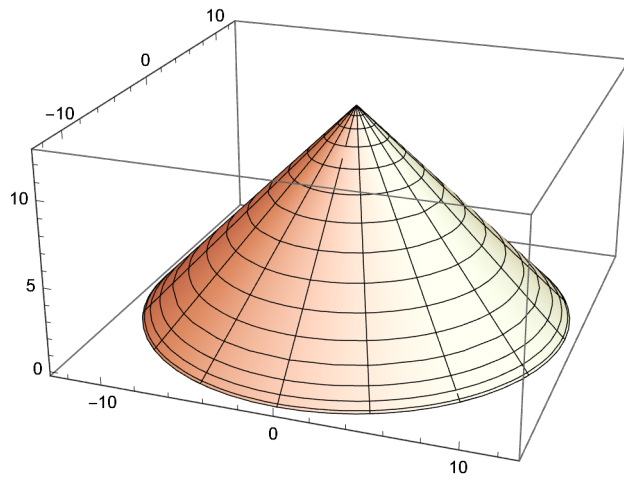
$$\left.2\left(\pi + \sqrt{-\pi^2 + \pi^2 \text{Csc}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 \text{Sin}[\beta]\right)\right\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$



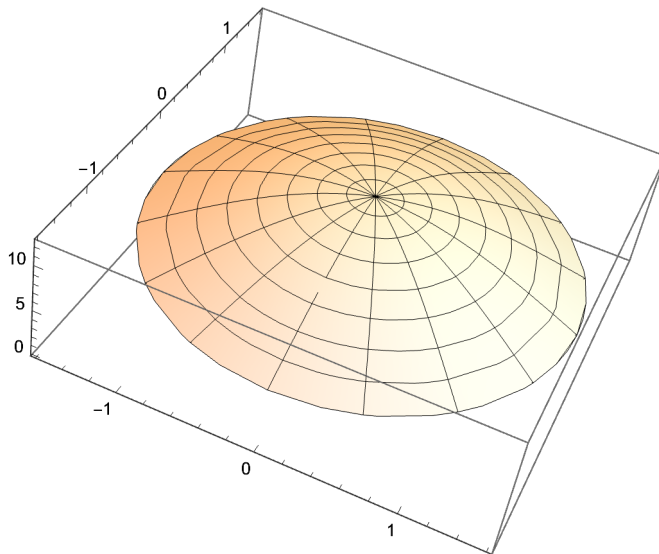
$$\text{Solve}\left[\frac{\sqrt{4\pi\theta - \theta^2}}{2\pi \text{Sin}[\beta]} == 2\pi \frac{\text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{-\pi^2 + \pi^2 \text{Csc}[\beta]^2 \text{Sin}[\beta]}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{-\pi^2 + \pi^2 \text{Csc}[\beta]^2 \text{Sin}[\beta]}\right)\right\}\right\}$$

`RevolutionPlot3D[`  
`{2 (π - √(-π² + π² Csc[β]²) Sin[β]), 2 (π + √(-π² + π² Csc[β]²) Sin[β])}, {β, -π/2, π/2}]`



`RevolutionPlot3D[2 (π + √(-π² + π² Csc[β]²) Sin[β]), {β, -π/2, π/2}]`



Solve[

$$r = \left( \sqrt{\left( -\left( 256 \pi^7 \eta^2 \theta^3 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 320 \pi^6 \eta^2 \theta^4 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \left( 128 \pi^5 \eta^2 \theta^5 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 16 \pi^4 \eta^2 \theta^6 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right) \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta \right]$$

Solve::verif : Potential solution  $\{\theta \rightarrow 4 \pi\}$  (possibly discarded by verifier) should be checked by hand. May require use of limits. >>

Solve::verif : Potential solution  $\{\theta \rightarrow \text{ComplexInfinity}\}$  (possibly discarded by verifier) should be checked by hand. May require use of limits. >>

[illegible]

Solve[

$$\begin{aligned}
r == & \sqrt{\left( - \left( 256 \pi^7 \eta^2 \theta^3 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - \right. \right. \\
& \left. \left. 8 \pi \theta^9 + \theta^{10} \right) + \left( 320 \pi^6 \eta^2 \theta^4 \right) / \right. \\
& \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) - \\
& \left( 128 \pi^5 \eta^2 \theta^5 \right) / \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - \right. \\
& \left. 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \left( 16 \pi^4 \eta^2 \theta^6 \right) / \\
& \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) + \\
& \left( 128 \pi^6 \sqrt{\left( 256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8 \right)} \right) / \\
& \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right), \theta]
\end{aligned}$$

$$\begin{aligned}
& \{ \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 1] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 2] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 3] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 4] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 5] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 6] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 7] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 8] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 9] \}, \\
& \{ \theta \rightarrow \text{Root} [4096 \pi^{10} \eta^4 - 2048 \pi^9 \eta^4 \#1 + 256 \pi^8 \eta^4 \#1^2 + (-1024 \pi^7 r^4 + 512 \pi^7 r^2 \eta^2) \#1^3 + \\
& \quad (1280 \pi^6 r^4 - 640 \pi^6 r^2 \eta^2) \#1^4 + (-512 \pi^5 r^4 + 256 \pi^5 r^2 \eta^2) \#1^5 + \\
& \quad (80 \pi^4 r^4 - 32 \pi^4 r^2 \eta^2) \#1^6 - 32 \pi^3 r^4 \#1^7 + 24 \pi^2 r^4 \#1^8 - 8 \pi r^4 \#1^9 + r^4 \#1^{10} \&, 10] \} \}
\end{aligned}$$

$$\text{Solve} \left[ \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - (r \sin[\beta])^2} \right)}{\theta^2} == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \right]$$

$$\text{Solve} \left[ \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - (r \sin[\beta])^2} \right)}{\theta^2} == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \beta \right]$$

Solve::verif : Potential solution  $\{\beta \rightarrow \text{ComplexInfinity}\}$  (possibly discarded by verifier) should be checked by hand.

May require use of limits. >>



Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\left( \frac{4}{3} + \frac{2 \times 2^{2/3}}{3 (-13 + 3 \sqrt{33})^{1/3}} - \frac{2 \sqrt[3]{2}}{\sqrt{3} (-13 + 3 \sqrt{33})^{1/3}} - \frac{(-13 + 3 \sqrt{33})^{1/3}}{3 \times 2^{2/3}} - \frac{\sqrt[3]{2} (-13 + 3 \sqrt{33})^{1/3}}{2^{2/3} \sqrt{3}} \right)} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\left( \frac{4}{3} + \frac{2 \times 2^{2/3}}{3 (-13 + 3 \sqrt{33})^{1/3}} - \frac{2 \sqrt[3]{2}}{\sqrt{3} (-13 + 3 \sqrt{33})^{1/3}} - \frac{(-13 + 3 \sqrt{33})^{1/3}}{3 \times 2^{2/3}} - \frac{\sqrt[3]{2} (-13 + 3 \sqrt{33})^{1/3}}{2^{2/3} \sqrt{3}} \right)} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\left( \frac{4}{3} + \frac{2 \times 2^{2/3}}{3 (-13 + 3 \sqrt{33})^{1/3}} + \frac{2 \sqrt[3]{2}}{\sqrt{3} (-13 + 3 \sqrt{33})^{1/3}} - \frac{(-13 + 3 \sqrt{33})^{1/3}}{3 \times 2^{2/3}} + \frac{\sqrt[3]{2} (-13 + 3 \sqrt{33})^{1/3}}{2^{2/3} \sqrt{3}} \right)} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\left( \frac{4}{3} + \frac{2 \times 2^{2/3}}{3 (-13 + 3 \sqrt{33})^{1/3}} + \frac{2 \sqrt[3]{2}}{\sqrt{3} (-13 + 3 \sqrt{33})^{1/3}} - \frac{(-13 + 3 \sqrt{33})^{1/3}}{3 \times 2^{2/3}} + \frac{\sqrt[3]{2} (-13 + 3 \sqrt{33})^{1/3}}{2^{2/3} \sqrt{3}} \right)} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \frac{1}{\sqrt{\frac{3}{4 - \frac{4 \cdot 2^{2/3}}{(-13+3 \sqrt{33})^{1/3}} + (2 (-13+3 \sqrt{33}))^{1/3}}}}} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{1}{\sqrt{\frac{3}{4 - \frac{4 \cdot 2^{2/3}}{(-13+3 \sqrt{33})^{1/3}} + (2 (-13+3 \sqrt{33}))^{1/3}}}}} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\text{Root}[-64 + 160 \#1 - 132 \#1^2 + 40 \#1^3 - 4 \#1^4 + \#1^5 \&, 1]} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\text{Root}[-64 + 160 \#1 - 132 \#1^2 + 40 \#1^3 - 4 \#1^4 + \#1^5 \&, 1]} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\text{Root}[-64 + 160 \#1 - 132 \#1^2 + 40 \#1^3 - 4 \#1^4 + \#1^5 \&, 2]} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\text{Root}[-64 + 160 \#1 - 132 \#1^2 + 40 \#1^3 - 4 \#1^4 + \#1^5 \&, 2]} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\text{Root}[-64 + 160 \#1 - 132 \#1^2 + 40 \#1^3 - 4 \#1^4 + \#1^5 \&, 3]} \right] \right\} \right\},$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\text{Root}[-64 + 160 \#1 - 132 \#1^2 + 40 \#1^3 - 4 \#1^4 + \#1^5 \&, 3]} \right] \right\} \right\},$$

$$\left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\text{Root} \left[ -64 + 160 \, \#1 - 132 \, \#1^2 + 40 \, \#1^3 - 4 \, \#1^4 + \#1^5 \, \&, 4 \right]} \right] \right\},$$

$$\left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\text{Root} \left[ -64 + 160 \, \#1 - 132 \, \#1^2 + 40 \, \#1^3 - 4 \, \#1^4 + \#1^5 \, \&, 4 \right]} \right] \right\},$$

$$\left\{ \beta \rightarrow -\text{ArcSin} \left[ \sqrt{\text{Root} \left[ -64 + 160 \, \#1 - 132 \, \#1^2 + 40 \, \#1^3 - 4 \, \#1^4 + \#1^5 \, \&, 5 \right]} \right] \right\},$$

$$\left\{ \beta \rightarrow \text{ArcSin} \left[ \sqrt{\text{Root} \left[ -64 + 160 \, \#1 - 132 \, \#1^2 + 40 \, \#1^3 - 4 \, \#1^4 + \#1^5 \, \&, 5 \right]} \right] \right\}$$

$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)$$

$$\text{Solve} \left[ \left( \sqrt{-1.1294090667581471 \, \theta^{18} + 8.987551787368176 \, \theta^{16} + 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2} \right) / \right.$$

$$\left. \left( \sqrt{-12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2} \right) == \right.$$

$$\left. \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2} \right)}{\theta^2}, \eta \right]$$

$$\left\{ \left\{ \eta \rightarrow \right.$$

$$-2.72115 \times 10^{-40} \sqrt{\left( -6.46917 \times 10^{80} - 7.1268 \times 10^{79} \theta + 2.05109 \times 10^{86} \theta^2 - 1.99702 \times 10^{77} \theta^3 - \right.$$

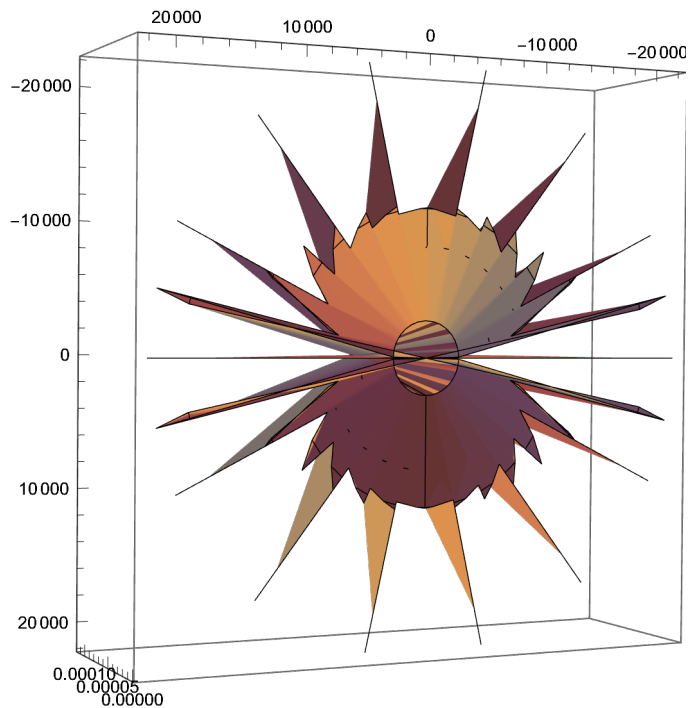
$$\left. 7.78783 \times 10^{92} \theta^4 + \frac{2.55393 \times 10^{82}}{39.4784 - 12.5664 \theta + \theta^2} - \frac{5.31585 \times 10^{81} \theta}{39.4784 - 12.5664 \theta + \theta^2} \right) \Bigg\},$$

$$\left\{ \eta \rightarrow 2.72115 \times 10^{-40} \sqrt{\left( -6.46917 \times 10^{80} - 7.1268 \times 10^{79} \theta + 2.05109 \times 10^{86} \theta^2 - 1.99702 \times 10^{77} \right.$$

$$\left. \left. \theta^3 - 7.78783 \times 10^{92} \theta^4 + \frac{2.55393 \times 10^{82}}{39.4784 - 12.5664 \theta + \theta^2} - \frac{5.31585 \times 10^{81} \theta}{39.4784 - 12.5664 \theta + \theta^2} \right) \right\} \Bigg\}$$

RevolutionPlot3D[  

$$2.721151924565645 \cdot 10^{-40} \sqrt{\left(-6.469169321605211 \cdot 10^{80} - 7.126799553878162 \cdot 10^{79} \theta + 2.0510927872792508 \cdot 10^{86} \theta^2 - 1.9970231960605707 \cdot 10^{77} \theta^3 - 7.787828037754042 \cdot 10^{92} \theta^4 + \frac{2.553925680316153 \cdot 10^{82}}{39.47841760435544 - 12.566370614359172 \theta + \theta^2} - \frac{5.315850236527997 \cdot 10^{81} \theta}{39.47841760435544 - 12.566370614359172 \theta + \theta^2}\right)}, \{\theta, -200000000\pi, 200000000\pi\}]$$



Solve[  

$$\left(\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2}\right) == \frac{2\pi \left(2\pi r - 2\pi \sqrt{r^2 - (\eta)^2}\right)}{\theta^2}, \theta]$$

$$\left\{\left\{\theta \rightarrow \text{Root}\left[-2.3660156990981718457587888744587 \times 10^{62} + 1.1830081875514010531471013760726 \times 10^{62} \eta^2 + 2.3660160371004628601123505349738 \times 10^{62} \sqrt{\left(0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \eta^2\right)} + \left(7.5312618788903902008800864567887 \times 10^{61} - 3.7656320153399796902269758400894 \times 10^{61} \eta^2 - 7.5312629547850980273281510484872 \times 10^{61}\right)\right]\right\}$$



$$\begin{aligned}
& \#1^2 + 6.8219680766162834642450637368141 \times 10^{75} \#1^4 - \\
& 2.1714998820172917589576416316475 \times 10^{75} \#1^5 + \\
& 1.7280247007325975178057090633459 \times 10^{74} \#1^6 \&, 3] \}, \\
& \left\{ \theta \rightarrow \text{Root} \left[ -2.3660156990981718457587888744587 \times 10^{62} + \right. \right. \\
& 1.1830081875514010531471013760726 \times 10^{62} \eta^2 + \\
& 2.3660160371004628601123505349738 \times 10^{62} \\
& \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& 1.00000000000000000000000000000000 \eta^2 \left. + \right. \\
& \left. \left( 7.5312618788903902008800864567887 \times 10^{61} - 3.7656320153399796902269758400894 \times \right. \right. \\
& 10^{61} \eta^2 - 7.5312629547850980273281510484872 \times 10^{61} \\
& \sqrt{\left( 0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right.} \\
& \eta^2 \left. \right) \#1 + \left( -5.9931877787248039370241230731881 \times 10^{60} + \right. \\
& 2.9965947455322680397847068785705 \times 10^{60} \eta^2 + \\
& 5.9931886348946089219726229971656 \times 10^{60} \\
& \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& 1.00000000000000000000000000000000 \eta^2 \left. \right) \left. \right] \} \\
& \#1^2 + 6.8219680766162834642450637368141 \times 10^{75} \#1^4 - \\
& 2.1714998820172917589576416316475 \times 10^{75} \#1^5 + \\
& 1.7280247007325975178057090633459 \times 10^{74} \#1^6 \&, 4] \}, \\
& \left\{ \theta \rightarrow \text{Root} \left[ -2.3660156990981718457587888744587 \times 10^{62} + \right. \right. \\
& 1.1830081875514010531471013760726 \times 10^{62} \eta^2 + \\
& 2.3660160371004628601123505349738 \times 10^{62} \\
& \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& 1.00000000000000000000000000000000 \eta^2 \left. + \right. \\
& \left. \left( 7.5312618788903902008800864567887 \times 10^{61} - 3.7656320153399796902269758400894 \times \right. \right. \\
& 10^{61} \eta^2 - 7.5312629547850980273281510484872 \times 10^{61} \\
& \sqrt{\left( 0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right.} \\
& \eta^2 \left. \right) \#1 + \left( -5.9931877787248039370241230731881 \times 10^{60} + \right. \\
& 2.9965947455322680397847068785705 \times 10^{60} \eta^2 + \\
& 5.9931886348946089219726229971656 \times 10^{60} \\
& \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& 1.00000000000000000000000000000000 \eta^2 \left. \right) \left. \right] \} \\
& \#1^2 + 6.8219680766162834642450637368141 \times 10^{75} \#1^4 - \\
& 2.1714998820172917589576416316475 \times 10^{75} \#1^5 + \\
& 1.7280247007325975178057090633459 \times 10^{74} \#1^6 \&, 5] \}, \\
& \left\{ \theta \rightarrow \text{Root} \left[ -2.3660156990981718457587888744587 \times 10^{62} + \right. \right. \\
& 1.1830081875514010531471013760726 \times 10^{62} \eta^2 +
\end{aligned}$$

$$\begin{aligned}
& 2.3660160371004628601123505349738 \times 10^{62} \\
& \sqrt{\left(0.9999997142857346938760932945648 - \right. \\
& \quad \left.1.00000000000000000000000000000000 \eta^2\right) +} \\
& \left(7.5312618788903902008800864567887 \times 10^{61} - 3.7656320153399796902269758400894 \times \right. \\
& \quad \left.10^{61} \eta^2 - 7.5312629547850980273281510484872 \times 10^{61} \right. \\
& \quad \sqrt{\left(0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right. \\
& \quad \left. \eta^2\right) \mp 1 + \left(-5.9931877787248039370241230731881 \times 10^{60} + \right. \\
& \quad \left.2.9965947455322680397847068785705 \times 10^{60} \eta^2 + \right. \\
& \quad \left.5.9931886348946089219726229971656 \times 10^{60} \right. \\
& \quad \sqrt{\left(0.9999997142857346938760932945648 - \right. \\
& \quad \left.1.00000000000000000000000000000000 \eta^2\right) \left. \right)} \\
& \mp 1^2 + 6.8219680766162834642450637368141 \times 10^{75} \mp 1^4 - \\
& 2.1714998820172917589576416316475 \times 10^{75} \mp 1^5 + \\
& 1.7280247007325975178057090633459 \times 10^{74} \mp 1^6 \&, 6 \left. \right\} \left. \right\}
\end{aligned}$$

Solve[

$$\begin{aligned}
& \left( \sqrt{\left( -1.1294090667581471 \cdot \pi^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot \pi^{16} \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \pi^{18} \sin[\beta]^2 \right) \right) \Big/ \\
& \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) == \\
& \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2} \right)}{\theta^2}, \theta]
\end{aligned}$$

$$\begin{aligned}
& \left\{ \left\{ \theta \rightarrow \text{Root} \left[ -8.629862001357961171684160966569 \times 10^{60} + \right. \right. \\
& \quad 4.3149322335166734318887465486281 \times 10^{60} \eta^2 + \\
& \quad 8.629863234195566056771316207843 \times 10^{60} \sqrt{\left(0.9999997142857346938760932945648 - \right. \\
& \quad \left. 1.00000000000000000000000000000000 \eta^2\right) +} \\
& \quad \left(2.7469703914342112837074324772367 \times 10^{60} - 1.3734855881415313347857257409600 \times \right. \\
& \quad \left. 10^{60} \eta^2 - 2.7469707838586089777964314707357 \times 10^{60} \right. \\
& \quad \sqrt{\left(0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right. \\
& \quad \left. \eta^2\right) \mp 1 + \left(-2.1859695816191667444085708378991 \times 10^{59} + \right. \\
& \quad \left. 1.0929851030910190673458026850634 \times 10^{59} \eta^2 + \right. \\
& \quad \left. 2.1859698939005801587787582217815 \times 10^{59} \right. \\
& \quad \sqrt{\left(0.9999997142857346938760932945648 - \right. \\
& \quad \left. 1.00000000000000000000000000000000 \eta^2\right) \left. \right)} \\
& \quad \mp 1^2 - 2.4882619981678728078979883701390 \times 10^{74} \mp 1^4 + \\
& \quad \left. 6.3028384418346349459946955224153 \times 10^{72} \mp 1^6 \&, 1 \right\} \right\},
\end{aligned}$$

$$\begin{aligned}
& \left\{ \theta \rightarrow \text{Root} \left[ -8.629862001357961171684160966569 \times 10^{60} + \right. \right. \\
& \quad 4.3149322335166734318887465486281 \times 10^{60} \eta^2 + \\
& \quad 8.629863234195566056771316207843 \times 10^{60} \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& \quad \quad \left. 1.00000000000000000000000000000000 \eta^2 \right) +} \\
& \quad \left( 2.7469703914342112837074324772367 \times 10^{60} - 1.3734855881415313347857257409600 \times \right. \\
& \quad \quad \left. 10^{60} \eta^2 - 2.7469707838586089777964314707357 \times 10^{60} \right. \\
& \quad \quad \left. \sqrt{\left( 0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right.} \right. \\
& \quad \quad \quad \left. \eta^2 \right) \Big] \mp 1 + \left( -2.1859695816191667444085708378991 \times 10^{59} + \right. \\
& \quad \quad 1.0929851030910190673458026850634 \times 10^{59} \eta^2 + \\
& \quad \quad 2.1859698939005801587787582217815 \times 10^{59} \\
& \quad \quad \left. \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \right. \\
& \quad \quad \quad \left. 1.00000000000000000000000000000000 \eta^2 \right) \Big] \\
& \quad \mp 1^2 - 2.4882619981678728078979883701390 \times 10^{74} \mp 1^4 + \\
& \quad \left. 6.3028384418346349459946955224153 \times 10^{72} \mp 1^6 \&, 2 \right\}, \\
& \left\{ \theta \rightarrow \text{Root} \left[ -8.629862001357961171684160966569 \times 10^{60} + \right. \right. \\
& \quad 4.3149322335166734318887465486281 \times 10^{60} \eta^2 + \\
& \quad 8.629863234195566056771316207843 \times 10^{60} \\
& \quad \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& \quad \quad \left. 1.00000000000000000000000000000000 \eta^2 \right) +} \\
& \quad \left( 2.7469703914342112837074324772367 \times 10^{60} - 1.3734855881415313347857257409600 \times \right. \\
& \quad \quad \left. 10^{60} \eta^2 - 2.7469707838586089777964314707357 \times 10^{60} \right. \\
& \quad \quad \left. \sqrt{\left( 0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right.} \right. \\
& \quad \quad \quad \left. \eta^2 \right) \Big] \mp 1 + \left( -2.1859695816191667444085708378991 \times 10^{59} + \right. \\
& \quad \quad 1.0929851030910190673458026850634 \times 10^{59} \eta^2 + \\
& \quad \quad 2.1859698939005801587787582217815 \times 10^{59} \\
& \quad \quad \left. \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \right. \\
& \quad \quad \quad \left. 1.00000000000000000000000000000000 \eta^2 \right) \Big] \\
& \quad \mp 1^2 - 2.4882619981678728078979883701390 \times 10^{74} \mp 1^4 + \\
& \quad \left. 6.3028384418346349459946955224153 \times 10^{72} \mp 1^6 \&, 3 \right\}, \\
& \left\{ \theta \rightarrow \text{Root} \left[ -8.629862001357961171684160966569 \times 10^{60} + \right. \right. \\
& \quad 4.3149322335166734318887465486281 \times 10^{60} \eta^2 + \\
& \quad 8.629863234195566056771316207843 \times 10^{60} \\
& \quad \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \\
& \quad \quad \left. 1.00000000000000000000000000000000 \eta^2 \right) +} \\
& \quad \left( 2.7469703914342112837074324772367 \times 10^{60} - 1.3734855881415313347857257409600 \times \right. \\
& \quad \quad \left. 10^{60} \eta^2 - 2.7469707838586089777964314707357 \times 10^{60} \right. \\
& \quad \quad \left. \sqrt{\left( 0.9999997142857346938760932945648 - 1.00000000000000000000000000000000 \right.} \right. \\
& \quad \quad \quad \left. \eta^2 \right) \Big] \mp 1 + \left( -2.1859695816191667444085708378991 \times 10^{59} + \right. \\
& \quad \quad 1.0929851030910190673458026850634 \times 10^{59} \eta^2 + \\
& \quad \quad 2.1859698939005801587787582217815 \times 10^{59} \\
& \quad \quad \left. \sqrt{\left( 0.9999997142857346938760932945648 - \right.} \right. \\
& \quad \quad \quad \left. 1.00000000000000000000000000000000 \eta^2 \right) \Big] \\
& \quad \mp 1^2 - 2.4882619981678728078979883701390 \times 10^{74} \mp 1^4 + \\
& \quad \left. 6.3028384418346349459946955224153 \times 10^{72} \mp 1^6 \&, 3 \right\},
\end{aligned}$$

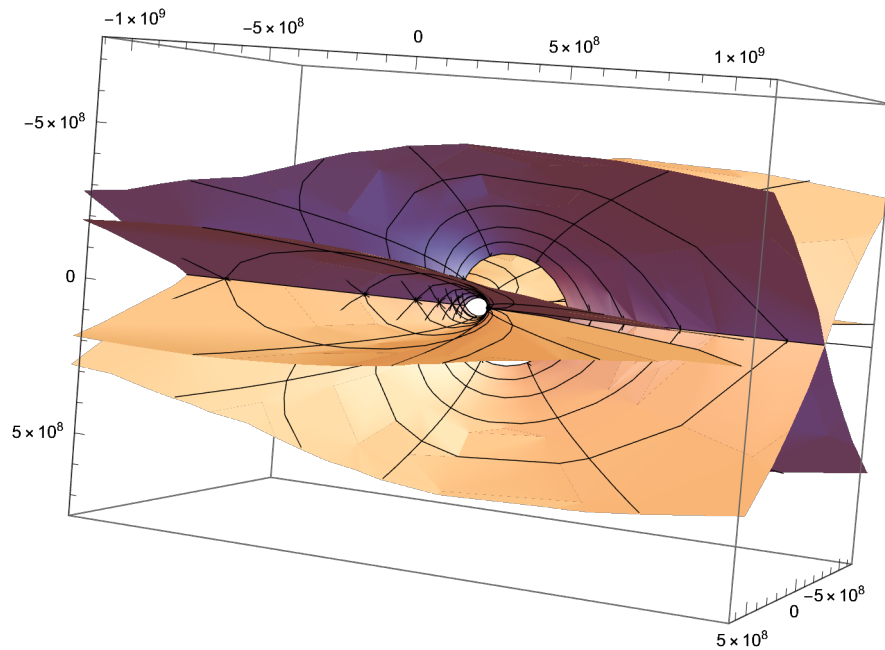




$$6.3028384418346349459946955224153 \times 10^{72} \#1^6 \&, 6]]\}}\}$$

$$\begin{aligned} & \text{Solve}\left[\left(\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2}\right) / \right. \\ & \left. \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) == \right. \\ & \left. \frac{2 \pi \left(2 \pi r - 2 \pi \sqrt{r^2 - (r \sin[\beta])^2}\right)}{\theta^2}, r\right] \\ & \left\{\left\{r \rightarrow 5.28956 \times 10^{-16} \csc[\beta]^2 \left(1.43563 \times 10^{22} \theta^2 - 1.43563 \times 10^{22} \theta^2 \sqrt{1. - 1. \sin[\beta]^2}\right)\right\}, \right. \\ & \left.\left\{r \rightarrow 5.28956 \times 10^{-16} \csc[\beta]^2 \left(1.43563 \times 10^{22} \theta^2 + 1.43563 \times 10^{22} \theta^2 \sqrt{1. - 1. \sin[\beta]^2}\right)\right\}\right\} \end{aligned}$$

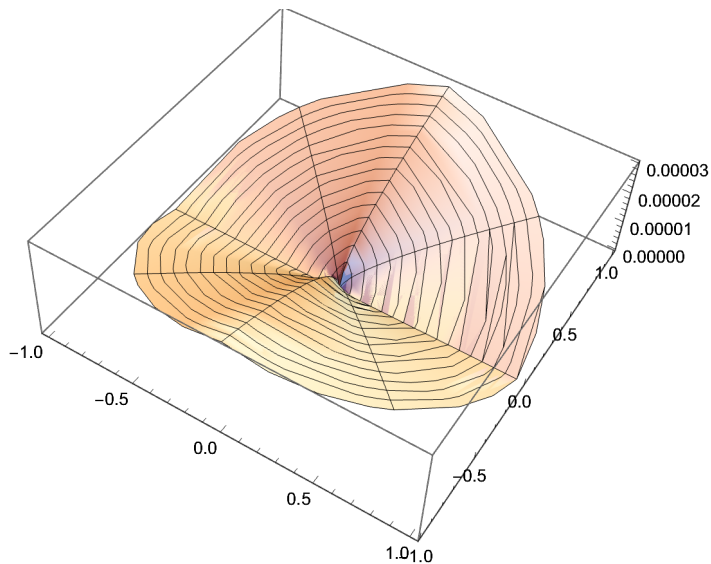
$$\begin{aligned} & \text{SphericalPlot3D}\left[5.289560600043053 \cdot \theta^{-16} \csc[\beta]^2 \right. \\ & \left. \left(1.4356261790137446 \cdot \theta^{22} + 1.4356261790137446 \cdot \theta^{22} \sqrt{1. - 1. \sin[\beta]^2}\right), \right. \\ & \left. \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right] \end{aligned}$$



$$\text{Solve}\left[\left(\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta]}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]}\right) == \frac{2\pi(2\pi r - 2\pi \sqrt{r^2 - (r \sin[\beta])^2})}{\theta^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -6.54458 \times 10^{-8} \sqrt{3.07451 \times 10^7 r - 3.07451 \times 10^7 \sqrt{1. r^2 + 0. r^2 \sin[\beta] - 1. r^2 \sin^2[\beta]}}\right\}, \left\{\theta \rightarrow 6.54458 \times 10^{-8} \sqrt{3.07451 \times 10^7 r - 3.07451 \times 10^7 \sqrt{1. r^2 + 0. r^2 \sin[\beta] - 1. r^2 \sin^2[\beta]}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[.54458 \times 10^{-8} \sqrt{3.074505 \cdot r^7 - 3.074505 \cdot \sqrt{1. r^2 + 0. r^2 \sin[\beta] - 1. r^2 \sin^2[\beta]}}, \{r, -1, 1\}, \{\beta, -2\pi, 2\pi\}\right]$$



$$\text{RevolutionPlot3D}\left[.54458 \times 10^{-8} \sqrt{3.074505 \cdot r^7 - 3.074505 \cdot \sqrt{1. r^2 + 0. r^2 \sin[\beta] - 1. r^2 \sin^2[\beta]}}, \{r, -1, 1\}, \{\beta, -2\pi, 2\pi\}\right]$$

$$\text{Solve}\left[5.289560600043053`*^-16 \text{Csc}[\beta]^2\right. \\ \left.\left(1.4356261790137446`*^22 \theta^2 + 1.4356261790137446`*^22 \theta^2 \sqrt{1.-1.`\text{Sin}[\beta]^2}\right) == \right. \\ \sqrt{\left(-\left(256 \pi^7 \eta^2 \theta^3\right) / \left(-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + \right. \right. \\ \left. \left. 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}\right) + \left(320 \pi^6 \eta^2 \theta^4\right) / \right. \\ \left. \left(-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}\right) - \right. \\ \left. \left(128 \pi^5 \eta^2 \theta^5\right) / \left(-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - \right. \right. \\ \left. \left. 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}\right) + \left(16 \pi^4 \eta^2 \theta^6\right) / \right. \\ \left. \left(-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}\right) + \right. \\ \left. \left(128 \pi^6 \sqrt{\left(256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8\right)}\right) / \right. \\ \left. \left(-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}\right)\right),]$$

$$\text{Solve}\left[\left(2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{4 \pi r^2 \theta - r^2 \theta^2}{4 \pi^2}}\right) == \right.$$

$$\left. \left(2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}}{2 \pi}}\right), v\right]$$

{}

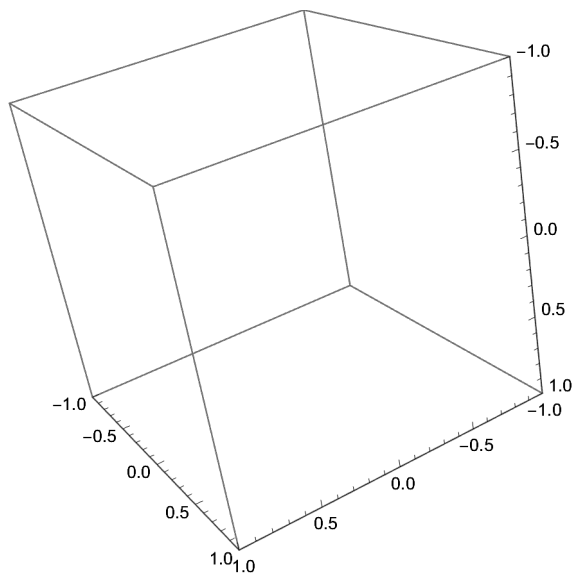
$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

```

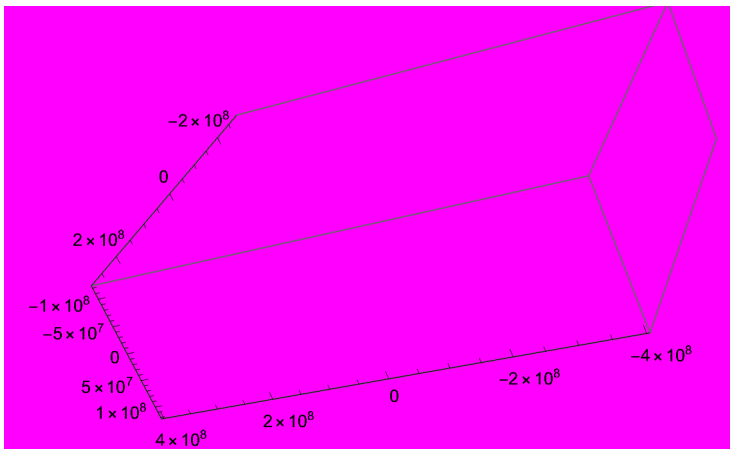
In[ ]:= SphericalPlot3D[{- (1. `  $\sqrt{(-2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \times$ 
 $2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) + 8.691706869652085 \cdot 10^{34} r^2 \theta -$ 
 $1.3833281122109134 \cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3}$  ) ) /
 $\left( \sqrt{(-3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta +$ 
 $9.670828135720014 \cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2$ 
 $(2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))^2 + 6.124123459454841 \cdot 10^{15} r^2 \theta^3}$  ) },
 $\left( \sqrt{(-2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \times 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) +$ 
 $8.691706869652085 \cdot 10^{34} r^2 \theta - 1.3833281122109134 \cdot 10^{34} r^2 \theta^2 +$ 
 $5.504087674408674 \cdot 10^{32} r^2 \theta^3}$  ) ) /
 $\left( \sqrt{(-3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta +$ 
 $9.670828135720014 \cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 +$ 
 $6.124123459454841 \cdot 10^{15} r^2 (2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))^3}$  ) } ) },
{ $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }, { $\theta$ ,  $-2\pi$ ,  $2\pi$ }, PlotStyle ->
Opacity[.75] ]

```

Out[ ]:=



$$\text{SphericalPlot3D}\left[\left\{-\left(1.\sqrt{\left(-2.7305802448854928\cdot 10^{35} + 2.1729267174130213\cdot 10^{34} \times 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.691706869652085\cdot 10^{34} r^2 \theta - 1.3833281122109134\cdot 10^{34} r^2 \theta^2 + 5.504087674408674\cdot 10^{32} r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^3\right)}\right.\right. \\
\left.\left.\sqrt{\left(-3.038180262530747\cdot 10^{18} + 2.4177070339300032\cdot 10^{17} \theta + 9.670828135720014\cdot 10^{17} r^2 \theta - 1.5391601015920192\cdot 10^{17} r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 6.124123459454841\cdot 10^{15} r^2 \theta^3\right)}\right),\right. \\
\left.\sqrt{\left(-2.7305802448854928\cdot 10^{35} + 2.1729267174130213\cdot 10^{34} \times 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.691706869652085\cdot 10^{34} r^2 \theta - 1.3833281122109134\cdot 10^{34} r^2 \theta^2 + 5.504087674408674\cdot 10^{32} r^2 \theta^3\right)}\right)\right] / \\
\left.\sqrt{\left(-3.038180262530747\cdot 10^{18} + 2.4177070339300032\cdot 10^{17} \theta + 9.670828135720014\cdot 10^{17} r^2 \theta - 1.5391601015920192\cdot 10^{17} r^2 \theta^2 + 6.124123459454841\cdot 10^{15} r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^3\right)}\right\}, \\
\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}, \text{PlotStyle} \rightarrow \\
\text{Opacity} [.75]$$



$$\text{SphericalPlot3D}\left[\left\{-\left(1.\sqrt{-2.7305802448854928\cdot 10^{35}+2.1729267174130213\cdot 10^{34}\times 2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)+8.691706869652085\cdot 10^{34}r^2\theta-1.3833281122109134\cdot 10^{34}r^2\theta^2+5.504087674408674\cdot 10^{32}r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^3}\right)\right)/\right. \\
\left.\sqrt{\left(-3.038180262530747\cdot 10^{18}+2.4177070339300032\cdot 10^{17}\theta+9.670828135720014\cdot 10^{17}r^2\theta-1.5391601015920192\cdot 10^{17}r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2+6.124123459454841\cdot 10^{15}r^2\theta^3}\right)},\right. \\
\left.\left(\sqrt{\left(-2.7305802448854928\cdot 10^{35}+2.1729267174130213\cdot 10^{34}\times 2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)+8.691706869652085\cdot 10^{34}r^2\theta-1.3833281122109134\cdot 10^{34}r^2\theta^2+5.504087674408674\cdot 10^{32}r^2\theta^3}\right)}\right)/\right. \\
\left.\sqrt{\left(-3.038180262530747\cdot 10^{18}+2.4177070339300032\cdot 10^{17}\theta+9.670828135720014\cdot 10^{17}r^2\theta-1.5391601015920192\cdot 10^{17}r^2\theta^2+6.124123459454841\cdot 10^{15}r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^3}\right)}\right\}, \\
\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\},\text{PlotStyle}\rightarrow \\
\text{Opacity}[.75]\]$$

$$\text{Solve}\left[\frac{(\theta r - (2\pi r - 2\pi x))}{(\theta r - (2\pi r - 2\pi x))} == \frac{\frac{r\theta}{\pi(r-x)}\pi\sin[\beta]}{\sqrt{\frac{r\theta}{\pi(r-x)}\frac{r\theta}{\pi(r-x)}\pi\theta - \theta^2}}, \beta\right]$$

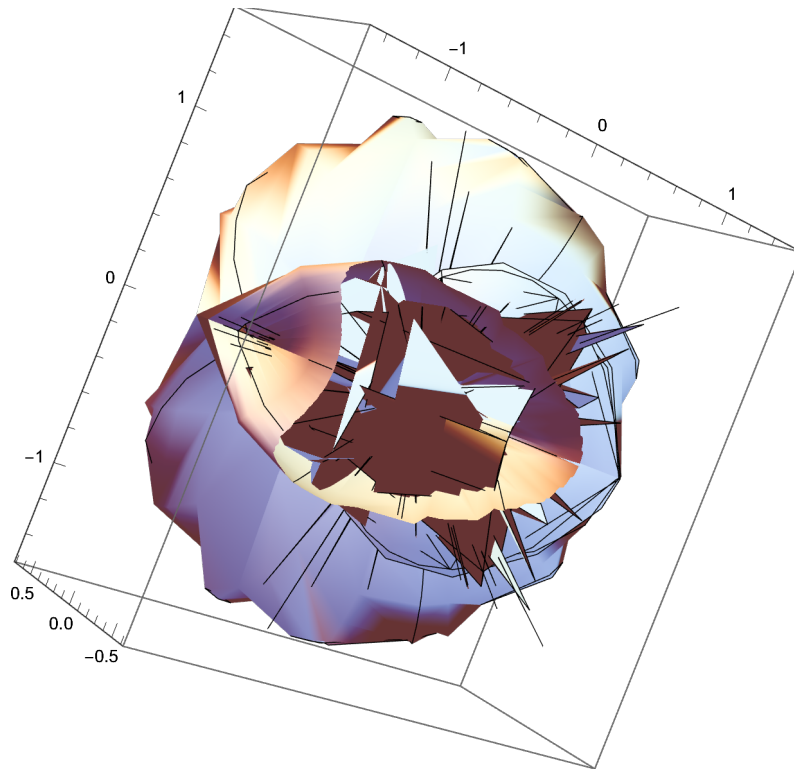
Solve::ifun: Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\left(1-\frac{x}{r}\right)\left(-\theta^2 + \frac{r^2\theta^3}{\pi(r-x)^2}\right)\frac{\pi(r-x)}{r\theta}}{\theta}\right]\right\}\right\}$$

$$(\theta r - (2\pi r - 2\pi x))$$

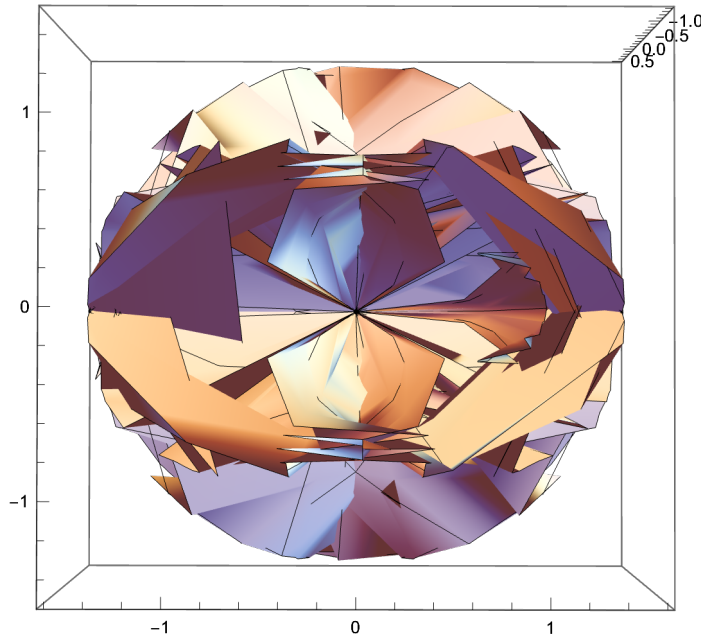
$$x := \frac{2\pi r - r\theta}{2\pi}$$

$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{\left(1 - \frac{x}{r}\right) \left(-\theta^2 + \frac{r^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)^3\right)}{\pi (r-x)^2}\right)}{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}\right], \right. \\ \left. \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$



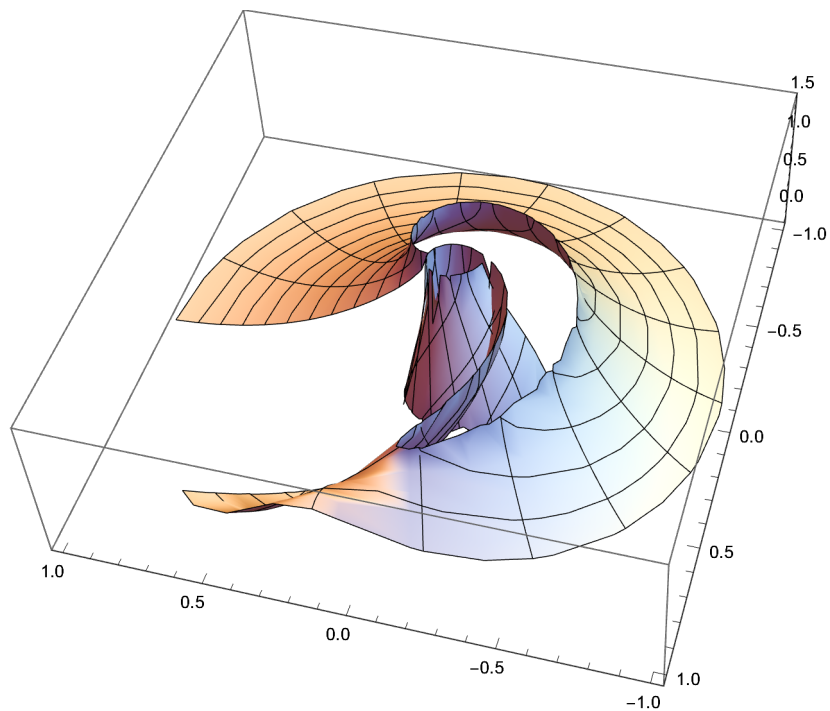
$$\text{SphericalPlot3D}\left[\text{ArcSin}\left[\frac{\left(1 - \frac{x}{r}\right) \left(-\theta^2 + \frac{r^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^3}{\pi (r-x)^2}\right)}{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}\right]^{\frac{\pi (r-x)}{r \theta}}\right],$$

$$\{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$





RevolutionPlot3D[ArcSin[ $\frac{\left(1 - \frac{x}{r}\right) \left(-\theta^2 + \frac{r^2 \theta^3}{\pi (r-x)^2}\right) \frac{\pi (r-x)}{r \theta}}{\theta}$ ], {x, -1, 1}, {θ, -2 π, 2 π}]



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\text{Solve}\left[\frac{1}{4 \pi^2} \left( \sqrt{\left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + \right.} \right. \right. \\ \left. \left. 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + \right. \right. \\ \left. \left. \left. 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta} \right) \right) = \frac{\sqrt{4 \pi r^2 \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \theta^2} \right)}{r^2} - r^2 \theta^2}}{2 \pi}, r \right]$$

{{r → 0}}

$$\text{Solve}\left[r \sin[\beta] = \frac{2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}}{\sqrt{4 \pi \theta - \theta^2}}, r \right]$$

{{r → 0}}

$$\text{Solve}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} == \frac{2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}}{\sqrt{4 \pi \theta - \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \pi}{\sqrt{4 \pi \theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2 \pi}{\sqrt{4 \pi \theta - \theta^2}}\right\}\right\}$$

$$\frac{2 \pi}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[r \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right] == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\{\{\theta \rightarrow 0\}, \{\theta \rightarrow 3 \pi\}\}$$

$$\text{Solve}\left[r \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right] == \frac{1}{2 \pi}\right]$$

$$\left(\sqrt{\left(4 \pi r^2 \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) / \left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} - r^2 \theta^2\right)\right)}, \theta\right]$$

Solve::verif : Potential solution  $\{\theta \rightarrow \text{ComplexInfinity}\}$  (possibly discarded by verifier) should be checked by hand.

May require use of limits. >>

$$\left\{\left\{\theta \rightarrow \frac{1}{81 + 180 \sin[\beta]^2} \left(144 \pi + 672 \pi \sin[\beta]^2 - \right.\right.\right.$$

$$\frac{56 \pi^6}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{5/3}} +$$

$$\frac{504 \pi^6 \sin[\beta]^2}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{5/3}} -$$

$$\frac{1512 \pi^6 \sin[\beta]^4}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{5/3}} +$$

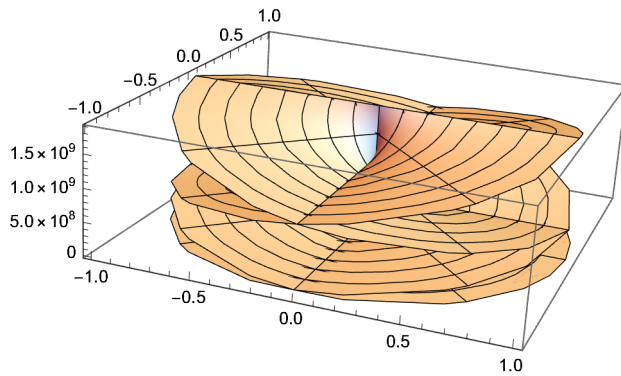
$$\frac{1512 \pi^6 \sin[\beta]^6}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{5/3}} +$$

$$\frac{16 \pi^5}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{4/3}} -$$

$$\begin{aligned}
& \frac{144 \pi^5 \sin[\beta]^2}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{4/3}} + \\
& \frac{432 \pi^5 \sin[\beta]^4}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{4/3}} - \\
& \frac{432 \pi^5 \sin[\beta]^6}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{4/3}} - \\
& \frac{128 \pi^3}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{2/3}} + \\
& \frac{2112 \pi^3 \sin[\beta]^2}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{2/3}} - \\
& \frac{144 \pi^3 \sin[\beta]^4}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{2/3}} + \\
& \frac{88 \pi^2}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3}} - \\
& \frac{744 \pi^2 \sin[\beta]^2}{\left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3}} \Bigg\} \Bigg\} \\
& \text{Solve}\left[\frac{\sqrt{4 \pi - \theta} \sqrt{\theta} \text{Abs}[z]}{2 \pi} = \text{Abs}[z] \sin[\beta], \theta\right] \\
& \left\{\left\{\theta \rightarrow 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\} \\
& \text{Solve}\left[\frac{2 \pi \left(2 \pi r - 2 \pi \sqrt{r^2 - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right)}{\theta^2} == \right. \\
& \left. \left(\sqrt{\left(-2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \theta + 8.691706869652085 \cdot 10^{34} \right. \right. \right. \\
& \left. \left. r^2 \theta - 1.3833281122109134 \cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3\right)\right) / \\
& \left.\left(\sqrt{\left(-3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta + 9.670828135720014 \cdot 10^{17} \right. \right. \right. \\
& \left. \left. r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 + 6.124123459454841 \cdot 10^{15} r^2 \theta^3\right)\right)\right], \\
& \{\{\}\}
\end{aligned}$$

$$\frac{\left(\sqrt{\left(-2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \theta + 8.691706869652085 \cdot 10^{34} r^2 \theta - 1.3833281122109134 \cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3\right)}\right)}{\left(\sqrt{\left(-3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta + 9.670828135720014 \cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 + 6.124123459454841 \cdot 10^{15} r^2 \theta^3\right)}\right)}$$

RevolutionPlot3D[ $\left(0.15915494309189535 \cdot \theta^2 \sqrt{\left(-2.7305802448854928 \cdot 10^{35} + 2.1729267174130213 \cdot 10^{34} \theta + 8.691706869652085 \cdot 10^{34} r^2 \theta - 1.3833281122109134 \cdot 10^{34} r^2 \theta^2 + 5.504087674408674 \cdot 10^{32} r^2 \theta^3\right)}\right) / \left(\sqrt{\left(-3.038180262530747 \cdot 10^{18} + 2.4177070339300032 \cdot 10^{17} \theta + 9.670828135720014 \cdot 10^{17} r^2 \theta - 1.5391601015920192 \cdot 10^{17} r^2 \theta^2 + 6.124123459454841 \cdot 10^{15} r^2 \theta^3\right)}\right), \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$



$$\text{Solve}\left[(2\pi r - r\theta - 2\pi x) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} ==\right.$$

$$\left(2\pi r - r\theta - 2\pi \sqrt{r^2 - \left(\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi}\right)^2}\right)$$

$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi}, v]$$

$$\left\{\left\{v \rightarrow -\left(1. \sqrt{\left(-3.69325 \times 10^{35} r^2 + 3.69325 \times 10^{35} x^2 + 1.4695 \times 10^{35} r^2 \theta - 2.939 \times 10^{34} x^2 \theta - 1.87102 \times 10^{34} r^2 \theta^2 + 7.44457 \times 10^{32} r^2 \theta^3\right)}\right) / \left(\sqrt{\left(-4.1093 \times 10^{18} r^2 + 4.1093 \times 10^{18} x^2 + 1.63504 \times 10^{18} r^2 \theta - 3.27008 \times 10^{17} x^2 \theta - 2.08179 \times 10^{17} r^2 \theta^2 + 8.2832 \times 10^{15} r^2 \theta^3\right)}\right)\right\}, \left\{v \rightarrow \left(\sqrt{\left(-3.69325 \times 10^{35} r^2 + 3.69325 \times 10^{35} x^2 + 1.4695 \times 10^{35} r^2 \theta - 2.939 \times 10^{34} x^2 \theta - 1.87102 \times 10^{34} r^2 \theta^2 + 7.44457 \times 10^{32} r^2 \theta^3\right)}\right) / \left(\sqrt{\left(-4.1093 \times 10^{18} r^2 + 4.1093 \times 10^{18} x^2 + 1.63504 \times 10^{18} r^2 \theta - 3.27008 \times 10^{17} x^2 \theta - 2.08179 \times 10^{17} r^2 \theta^2 + 8.2832 \times 10^{15} r^2 \theta^3\right)}\right)\right\}\right\}$$

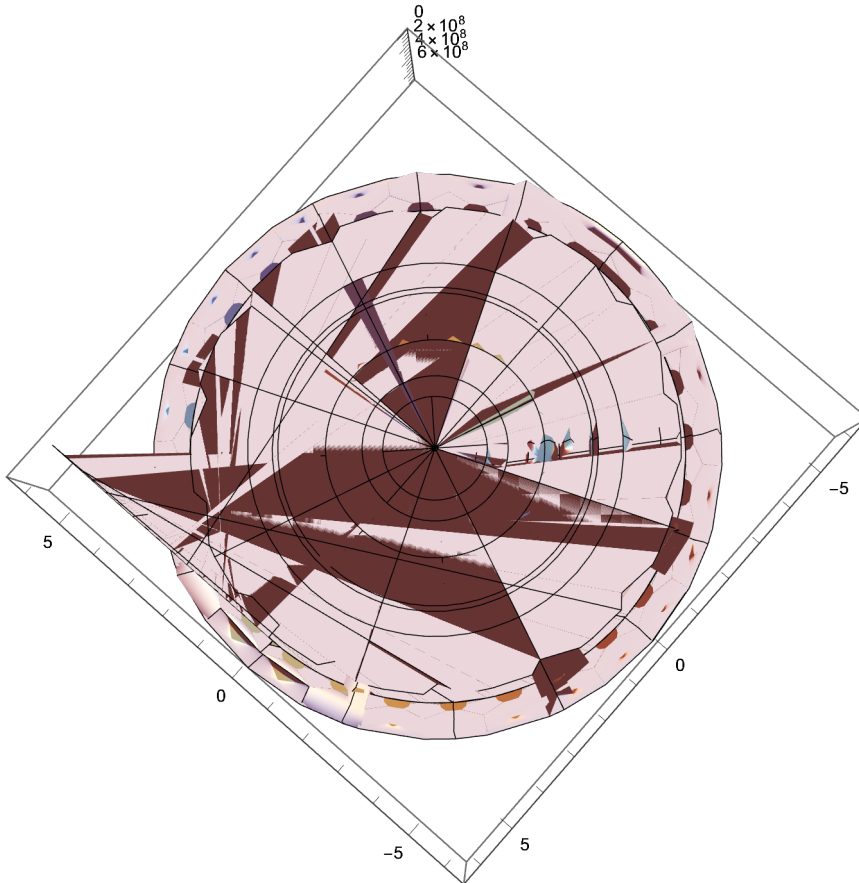
$$r := \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta}$$

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RevolutionPlot3D[ $\left( \sqrt{(-3.693252418944806 \cdot r^{35} + 3.693252418944806 \cdot x^2 + 1.4694984464029137 \cdot r^{35} \theta - 2.938996892805827 \cdot x^2 \theta - 1.8710235328870747 \cdot r^{34} \theta^2 + 7.444566097505983 \cdot r^{32} \theta^3)} \right) /$   

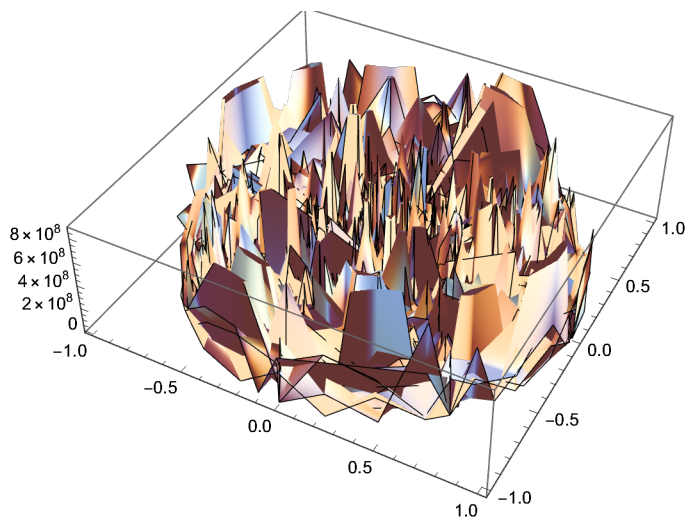
 $\left( \sqrt{(-4.109297510959101 \cdot r^{18} + 4.1092975109591004 \cdot x^2 + 1.6350375287609073 \cdot r^{18} \theta - 3.270075057521814 \cdot x^2 \theta - 2.081794438744443 \cdot r^{17} \theta^2 + 8.2831968856849 \cdot r^{15} \theta^3)} \right), \{\theta, -2\pi, 2\pi\}$ 

```



RevolutionPlot3D[

$(\sqrt{(-3.693252418944806 \cdot 10^{35} r^2 + 3.693252418944806 \cdot 10^{35} x^2 + 1.4694984464029137 \cdot 10^{35} r^2 \theta - 2.938996892805827 \cdot 10^{34} x^2 \theta - 1.8710235328870747 \cdot 10^{34} r^2 \theta^2 + 7.444566097505983 \cdot 10^{32} r^2 \theta^3)}) / (\sqrt{(-4.109297510959101 \cdot 10^{18} r^2 + 4.1092975109591004 \cdot 10^{18} x^2 + 1.6350375287609073 \cdot 10^{18} r^2 \theta - 3.270075057521814 \cdot 10^{17} x^2 \theta - 2.081794438744443 \cdot 10^{17} r^2 \theta^2 + 8.2831968856849 \cdot 10^{15} r^2 \theta^3)})$ , {r, -1, 1}, {θ, -2 π, 2 π}]



$$x := \frac{2 \pi r - r \theta}{2 \pi}$$

$$\text{Solve}\left[\left(2 \pi r - r \theta - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right) ==\right.$$

$$\left. \left( 2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{\left( \sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta} \right)^2}{2 \pi}} \right), v \right]$$

{{}}

$$c := 2.99792458 (10^8)$$

$$\text{Solve}\left[\left(2\pi r - r\theta - 2\pi \frac{2\pi r - r\theta}{2\pi}\right) ==\right.$$

$$\left. \left( 2\pi r - r\theta - 2\pi \sqrt{r^2 - \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}}{2\pi}} \right), v \right]$$

$$\left\{ \left\{ v \rightarrow - \left( 1. \sqrt{(-2.73058 \times 10^{35} + 2.17293 \times 10^{34} \theta + 8.69171 \times 10^{34} r^2 \theta - 1.38333 \times 10^{34} r^2 \theta^2 + 5.50409 \times 10^{32} r^2 \theta^3)} \right) / \right. \right. \\ \left. \left( \sqrt{(-3.03818 \times 10^{18} + 2.41771 \times 10^{17} \theta + 9.67083 \times 10^{17} r^2 \theta - 1.53916 \times 10^{17} r^2 \theta^2 + 6.12412 \times 10^{15} r^2 \theta^3)} \right) \right\}, \\ \left\{ v \rightarrow \left( \sqrt{(-2.73058 \times 10^{35} + 2.17293 \times 10^{34} \theta + 8.69171 \times 10^{34} r^2 \theta - 1.38333 \times 10^{34} r^2 \theta^2 + 5.50409 \times 10^{32} r^2 \theta^3)} \right) / \right. \\ \left. \left( \sqrt{(-3.03818 \times 10^{18} + 2.41771 \times 10^{17} \theta + 9.67083 \times 10^{17} r^2 \theta - 1.53916 \times 10^{17} r^2 \theta^2 + 6.12412 \times 10^{15} r^2 \theta^3)} \right) \right\} \right\}$$

$$c := 2.99792458 \cdot 10^8$$

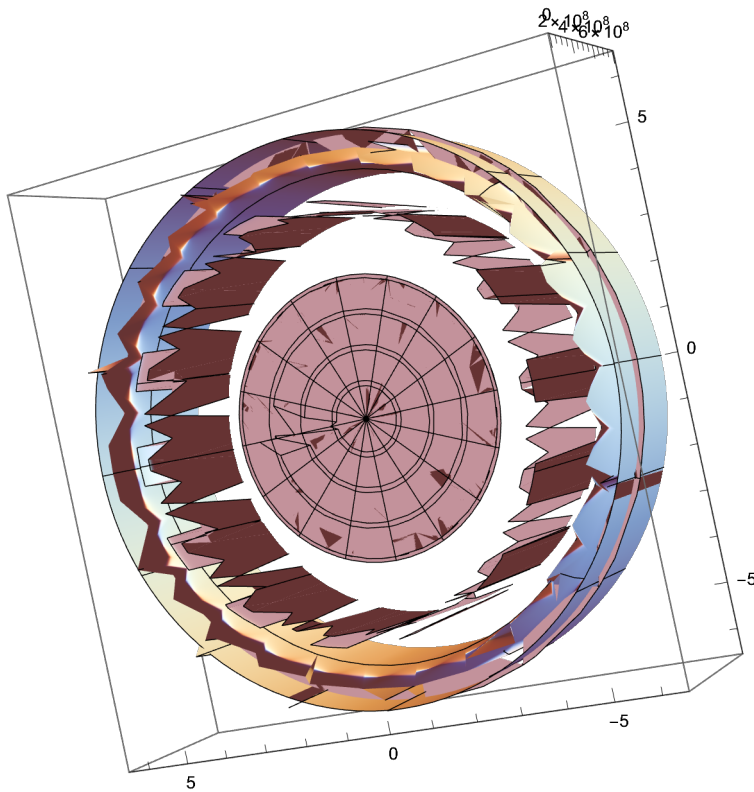


$$\begin{aligned}
& \text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \right. \\
& \left. \frac{r \sqrt{\pi^2 - \text{ArcCos}\left[\frac{\sqrt{1 + 2 \text{Cos}[\theta] + \text{Cos}[\theta]^2 + 2 \text{i Sin}[\theta] + 2 \text{i Cos}[\theta] \text{Sin}[\theta] - \text{Sin}[\theta]^2}}{\sqrt{4 \text{Cos}[\theta] + 4 \text{i Sin}[\theta]}}\right]^2}}{\pi}, v\right] \\
& \left\{\left\{v \rightarrow \right.\right. \\
& - \left(1. \sqrt{\left(3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 - 3.59502 \times 10^{17} \text{ArcCos}\left[\left(\sqrt{\left(1. + \right.\right.\right.\right. \\
& \left.\left.\left.\left.2. \text{Cos}[\theta] + \text{Cos}[\theta]^2 + (\theta. + 2. \text{i}) \text{Sin}[\theta] + (\theta. + 2. \text{i}) \text{Cos}[\theta] \text{Sin}[\theta] - \right.\right.\right.\right. \right. \\
& \left.\left.\left.\left.1. \text{Sin}[\theta]^2\right)\right)\right] / \left(\sqrt{4. \text{Cos}[\theta] + (\theta. + 4. \text{i}) \text{Sin}[\theta]}\right)^2\right)\right) / \\
& \left(\sqrt{\left(39.4784 - 12.5664 \theta + 1. \theta^2 - 4. \text{ArcCos}\left[\left(\sqrt{\left(1. + 2. \text{Cos}[\theta] + \text{Cos}[\theta]^2 + \right.\right.\right.\right. \right. \\
& \left.\left.\left.\left.(\theta. + 2. \text{i}) \text{Sin}[\theta] + (\theta. + 2. \text{i}) \text{Cos}[\theta] \text{Sin}[\theta] - \right.\right.\right.\right. \right. \\
& \left.\left.\left.\left.1. \text{Sin}[\theta]^2\right)\right)\right] / \left(\sqrt{4. \text{Cos}[\theta] + (\theta. + 4. \text{i}) \text{Sin}[\theta]}\right)^2\right)\right)\right)\right\}, \\
& \left\{v \rightarrow \left(\sqrt{\left(3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 - 3.59502 \times 10^{17} \right.\right.\right. \\
& \left.\left.\left.\text{ArcCos}\left[\left(\sqrt{\left(1. + 2. \text{Cos}[\theta] + \text{Cos}[\theta]^2 + (\theta. + 2. \text{i}) \text{Sin}[\theta] + (\theta. + 2. \text{i}) \text{Cos}[\theta] \right.\right.\right.\right. \right. \right. \\
& \left.\left.\left.\left.\text{Sin}[\theta] - 1. \text{Sin}[\theta]^2\right)\right)\right] / \left(\sqrt{4. \text{Cos}[\theta] + (\theta. + 4. \text{i}) \text{Sin}[\theta]}\right)^2\right)\right)\right) / \\
& \left(\sqrt{\left(39.4784 - 12.5664 \theta + 1. \theta^2 - 4. \text{ArcCos}\left[\left(\sqrt{\left(1. + 2. \text{Cos}[\theta] + \text{Cos}[\theta]^2 + \right.\right.\right.\right. \right. \right. \\
& \left.\left.\left.\left.(\theta. + 2. \text{i}) \text{Sin}[\theta] + (\theta. + 2. \text{i}) \text{Cos}[\theta] \text{Sin}[\theta] - \right.\right.\right.\right. \right. \\
& \left.\left.\left.\left.1. \text{Sin}[\theta]^2\right)\right)\right] / \left(\sqrt{4. \text{Cos}[\theta] + (\theta. + 4. \text{i}) \text{Sin}[\theta]}\right)^2\right)\right)\right)\right\}
\end{aligned}$$

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RevolutionPlot3D[
  (Sqrt[3.5481432270250993`^18 - 1.1294090667581471`^18 theta + 8.987551787368176`^16 theta^2 -
    3.5950207149472704`^17
    ArcCos[(Sqrt[(1.` + 2.` Cos[theta] + Cos[theta]^2 + (0.` + 2.` I) Sin[theta] + (0.` + 2.` I) Cos[theta]
      Sin[theta] - 1.` Sin[theta]^2)) / (Sqrt[4.` Cos[theta] + (0.` + 4.` I) Sin[theta]])]^2])) /
  (Sqrt[39.47841760435743` - 12.566370614359172` theta + 1.` theta^2 -
    4.` ArcCos[(Sqrt[(1.` + 2.` Cos[theta] + Cos[theta]^2 + (0.` + 2.` I)
      Sin[theta] + (0.` + 2.` I) Cos[theta] Sin[theta] - 1.` Sin[theta]^2)) /
      (Sqrt[4.` Cos[theta] + (0.` + 4.` I) Sin[theta]])]^2]))], {theta, -2 pi, 2 pi}]

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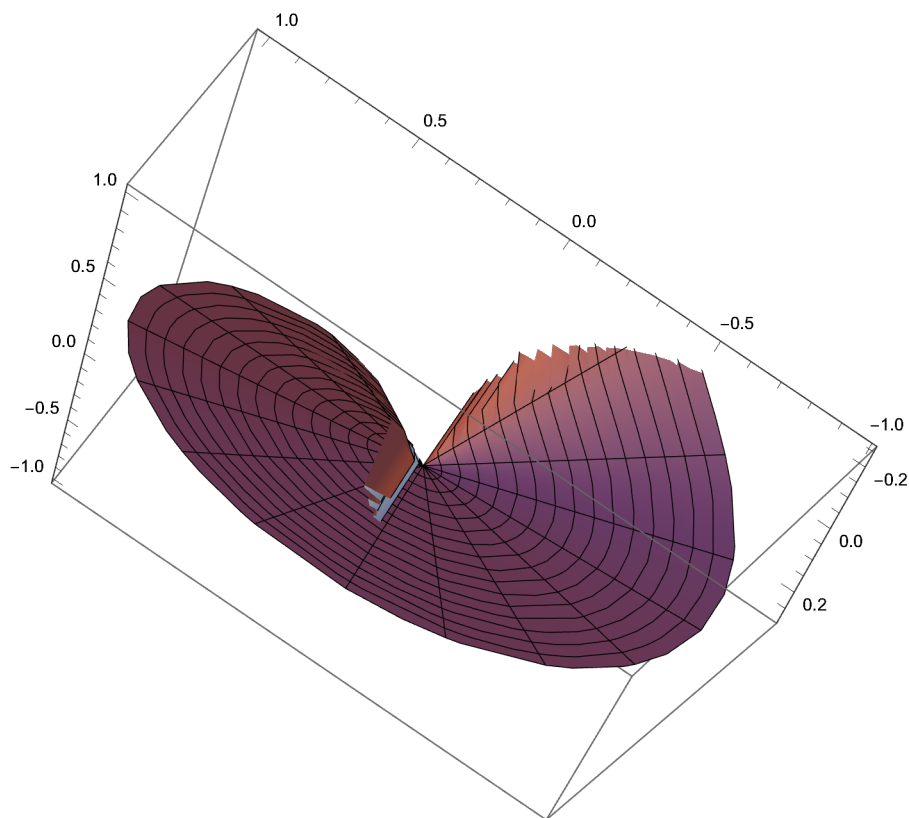


$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == \right.$$

$$\left. r \sqrt{\pi^2 - \text{ArcCos}\left[\frac{\sqrt{1+2\cos[\theta]+\cos[\theta]^2+2i\sin[\theta]+2i\cos[\theta]\sin[\theta]-\sin[\theta]^2}}{\sqrt{4\cos[\theta]+4i\sin[\theta]}}\right]^2}\right], v]$$

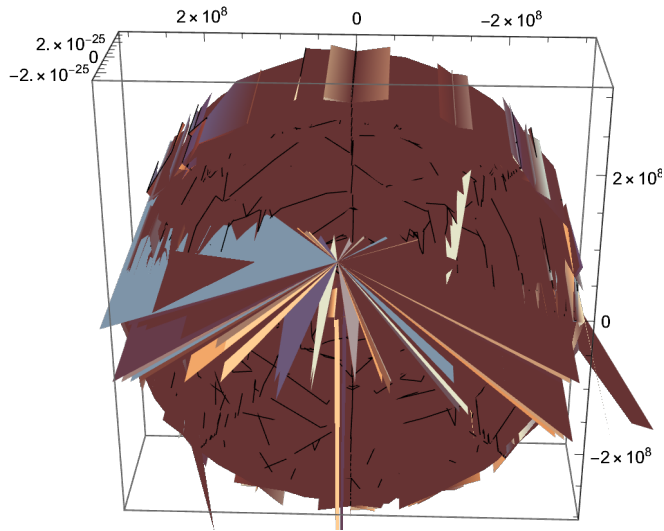
$$\begin{aligned}
& D \left[ \frac{1}{4 \pi^2} \left( \sqrt{ \left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + \right. } \right. \right. \\
& \quad \left. \left. 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta} \right) \right], \theta] \\
& \left( 16 \pi^3 r^2 - \frac{256 \pi^5 r^2}{(4 \pi - \theta)^2} + 8 \pi^2 r^2 \theta + 4 r^2 \theta^3 + 8 \pi^2 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{(4 \pi - \theta)^2} + \right. \\
& \quad \left. \frac{8 \pi^3 r (r^2 (4 \pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}} - \frac{32 \pi^4 r (r^2 (4 \pi - \theta) - r^2 \theta)}{(4 \pi - \theta) \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{4 \pi^2 r \theta (r^2 (4 \pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}} \right) / \\
& \left( 8 \pi^2 \sqrt{ \left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + \right. } \right. \\
& \quad \left. \left. 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta} \right) \right)
\end{aligned}$$

$\text{RevolutionPlot3D}\left[\right.$   
 $\left(\frac{16\pi^3 r^2 - \frac{256\pi^5 r^2}{(4\pi - \theta)^2} + 8\pi^2 r^2 \theta + 4r^2 \theta^3 + 8\pi^2 r \sqrt{r^2(4\pi - \theta)\theta} - \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{(4\pi - \theta)^2} + \frac{8\pi^3 r (r^2(4\pi - \theta) - r^2 \theta)}{\sqrt{r^2(4\pi - \theta)\theta}} - \frac{32\pi^4 r (r^2(4\pi - \theta) - r^2 \theta)}{(4\pi - \theta) \sqrt{r^2(4\pi - \theta)\theta}} + \frac{4\pi^2 r \theta (r^2(4\pi - \theta) - r^2 \theta)}{\sqrt{r^2(4\pi - \theta)\theta}}\right) /$   
 $\left(8\pi^2 \sqrt{\left(64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2(4\pi - \theta)\theta} - \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2(4\pi - \theta)\theta}\right)}\right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} \left.] \right)$



$$\begin{aligned}
& \left( 16 \pi^3 r^2 - \frac{256 \pi^5 r^2}{(4 \pi - \theta)^2} + 8 \pi^2 r^2 \theta + 4 r^2 \theta^3 + 8 \pi^2 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{(4 \pi - \theta)^2} + \right. \\
& \quad \left. \frac{8 \pi^3 r (r^2 (4 \pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}} - \frac{32 \pi^4 r (r^2 (4 \pi - \theta) - r^2 \theta)}{(4 \pi - \theta) \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{4 \pi^2 r \theta (r^2 (4 \pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}} \right) / \\
& \left( 8 \pi^2 \sqrt{\left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \right. \right. \\
& \quad \left. \left. \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta} \right) \right) == \\
& D \left[ \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi}, \theta, v \right] \\
& - \frac{4.42709 \times 10^{-19} r v \sqrt{r} \sqrt{1 - 1.11265 \times 10^{-17} v^2} \theta}{(1 - 1.11265 \times 10^{-17} v^2)^{3/2} \sqrt{\frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}}} \sqrt{4 \pi r - r \theta}} + \\
& \frac{4.42709 \times 10^{-19} r^2 v \sqrt{\frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}}}}{\sqrt{r} \sqrt{1 - 1.11265 \times 10^{-17} v^2} \sqrt{1 - 1.11265 \times 10^{-17} v^2} \sqrt{4 \pi r - r \theta}} - \\
& \frac{4.42709 \times 10^{-19} v \sqrt{r} \sqrt{1 - 1.11265 \times 10^{-17} v^2} \theta \sqrt{4 \pi r - r \theta}}{(1 - 1.11265 \times 10^{-17} v^2)^2 \left( \frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}} \right)^{3/2}} + \\
& \frac{8.85419 \times 10^{-19} v \sqrt{r} \sqrt{1 - 1.11265 \times 10^{-17} v^2} \sqrt{4 \pi r - r \theta}}{(1 - 1.11265 \times 10^{-17} v^2)^{3/2} \sqrt{\frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}}}} - \\
& \frac{4.42709 \times 10^{-19} r v \sqrt{4 \pi r - r \theta}}{\sqrt{r} \sqrt{1 - 1.11265 \times 10^{-17} v^2} (1 - 1.11265 \times 10^{-17} v^2) \sqrt{\frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}}}}
\end{aligned}$$

$$\begin{aligned}
& \text{RevolutionPlot3D}\left[ \right. \\
& - \left( 4.427093908810196 \cdot 10^{-19} r v \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \theta \right) / \\
& \left( (1 - 1.1126500560536185 \cdot 10^{-17} v^2)^{3/2} \right. \\
& \left. \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \sqrt{4 \pi r - r \theta} \right) + \\
& \left( 4.427093908810196 \cdot 10^{-19} r^2 v \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \right) / \\
& \left( \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \right. \\
& \left. \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2} \sqrt{4 \pi r - r \theta} \right) - \\
& \left( 4.427093908810196 \cdot 10^{-19} v \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \theta \sqrt{4 \pi r - r \theta} \right) / \\
& \left( (1 - 1.1126500560536185 \cdot 10^{-17} v^2)^2 \left( \frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \right)^{3/2} \right) + \\
& \left( 8.854187817620391 \cdot 10^{-19} v \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \sqrt{4 \pi r - r \theta} \right) / \\
& \left( (1 - 1.1126500560536185 \cdot 10^{-17} v^2)^{3/2} \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \right) - \\
& \left( 4.427093908810196 \cdot 10^{-19} r v \sqrt{4 \pi r - r \theta} \right) / \\
& \left( \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} (1 - 1.1126500560536185 \cdot 10^{-17} v^2) \right. \\
& \left. \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \right), \{v, -c, c\}, \{\theta, -2 \pi, 2 \pi\} \left. \right]
\end{aligned}$$



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\begin{aligned} & \text{Solve} \left[ - \left( 4.427093908810196 \cdot 10^{-19} r v \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2} \theta} \right) / \right. \\ & \quad \left( (1 - 1.1126500560536185 \cdot 10^{-17} v^2)^{3/2} \right. \\ & \quad \left. \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \sqrt{4 \pi r - r \theta} \right) + \\ & \quad \left( 4.427093908810196 \cdot 10^{-19} r^2 v \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \right) / \\ & \quad \left( \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \right. \\ & \quad \left. \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2} \sqrt{4 \pi r - r \theta} \right) - \\ & \quad \left( 4.427093908810196 \cdot 10^{-19} v \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2} \theta \sqrt{4 \pi r - r \theta}} \right) / \\ & \quad \left( (1 - 1.1126500560536185 \cdot 10^{-17} v^2)^2 \left( \frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}} \right)^{3/2} \right) + \\ & \quad \left( 8.854187817620391 \cdot 10^{-19} v \sqrt{r \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2} \sqrt{4 \pi r - r \theta}} \right) / \\ & \quad \left( (1 - 1.1126500560536185 \cdot 10^{-17} v^2)^{3/2} \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \right) - \end{aligned}$$

$$\begin{aligned}
& \left( 4.427093908810196 \cdot 10^{-19} r v \sqrt{4\pi r - r\theta} \right) / \left( \sqrt{r} \sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2} \right. \\
& \quad \left. (1 - 1.1126500560536185 \cdot 10^{-17} v^2) \sqrt{\frac{\theta}{\sqrt{1 - 1.1126500560536185 \cdot 10^{-17} v^2}}} \right) = \\
& \left( 16\pi^3 r^2 - \frac{256\pi^5 r^2}{(4\pi - \theta)^2} + 8\pi^2 r^2 \theta + 4r^2 \theta^3 + 8\pi^2 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{(4\pi - \theta)^2} + \right. \\
& \quad \left. \frac{8\pi^3 r (r^2 (4\pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4\pi - \theta) \theta}} - \frac{32\pi^4 r (r^2 (4\pi - \theta) - r^2 \theta)}{(4\pi - \theta) \sqrt{r^2 (4\pi - \theta) \theta}} + \frac{4\pi^2 r \theta (r^2 (4\pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4\pi - \theta) \theta}} \right) / \\
& \left( 8\pi^2 \sqrt{\left( 64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \right. \right. \\
& \quad \left. \left. \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2 (4\pi - \theta) \theta} \right) \right), v]
\end{aligned}$$



$$\begin{aligned}
& \text{Solve}\left[ \right. \\
& \quad \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 - \right. \right. \\
& \quad \left. \left. 3.5950207149472704 \cdot 10^{17} \right. \right. \\
& \quad \left. \left. \text{ArcCos}\left[ \left( \sqrt{\left( 1. \cdot 10^0 + 2. \cdot 10^0 \cos[\theta] + \cos[\theta]^2 + (0. \cdot 10^0 + 2. \cdot 10^0 i) \sin[\theta] + (0. \cdot 10^0 + 2. \cdot 10^0 i) \cos[\theta] \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\theta] - 1. \cdot 10^0 \sin[\theta]^2 \right) \right] \right) / \left( \sqrt{4. \cdot 10^0 \cos[\theta] + (0. \cdot 10^0 + 4. \cdot 10^0 i) \sin[\theta]} \right)^2 \right) \Bigg] / \\
& \quad \left( \sqrt{\left( 39.47841760435743 \cdot 10^0 - 12.566370614359172 \cdot 10^0 \theta + 1. \cdot 10^0 \theta^2 - 4. \cdot 10^0 \right. \right. \\
& \quad \left. \left. \text{ArcCos}\left[ \left( \sqrt{\left( 1. \cdot 10^0 + 2. \cdot 10^0 \cos[\theta] + \cos[\theta]^2 + (0. \cdot 10^0 + 2. \cdot 10^0 i) \sin[\theta] + (0. \cdot 10^0 + 2. \cdot 10^0 i) \cos[\theta] \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\theta] - 1. \cdot 10^0 \sin[\theta]^2 \right) \right] \right) / \left( \sqrt{4. \cdot 10^0 \cos[\theta] + (0. \cdot 10^0 + 4. \cdot 10^0 i) \sin[\theta]} \right)^2 \right) \Bigg] == \\
& \quad \left( 16 \pi^3 r^2 - \frac{256 \pi^5 r^2}{(4 \pi - \theta)^2} + 8 \pi^2 r^2 \theta + 4 r^2 \theta^3 + 8 \pi^2 r \sqrt{r^2 (4 \pi - \theta) \theta} - \right. \\
& \quad \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{(4 \pi - \theta)^2} + \frac{8 \pi^3 r (r^2 (4 \pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}} - \\
& \quad \left. \frac{32 \pi^4 r (r^2 (4 \pi - \theta) - r^2 \theta)}{(4 \pi - \theta) \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{4 \pi^2 r \theta (r^2 (4 \pi - \theta) - r^2 \theta)}{\sqrt{r^2 (4 \pi - \theta) \theta}} \right) / \\
& \quad \left( 8 \pi^2 \sqrt{\left( 64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \right. \right. \\
& \quad \left. \left. \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 r \theta \sqrt{r^2 (4 \pi - \theta) \theta} \right) \right), r]
\end{aligned}$$

{{}}

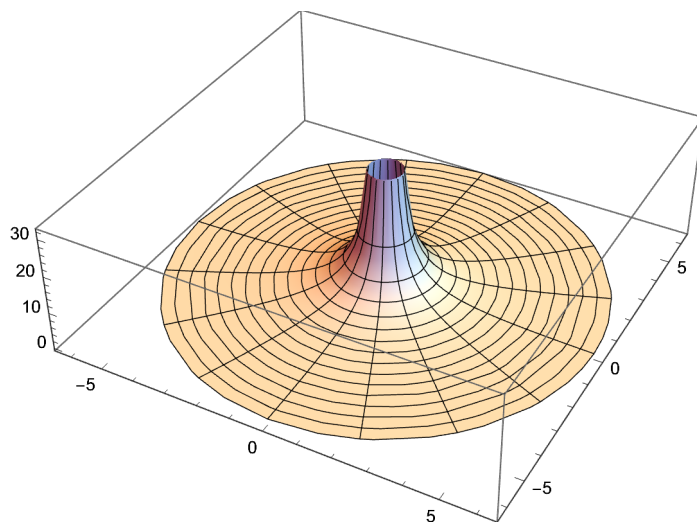
$$\begin{aligned}
& \text{Solve}\left[ \frac{2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - \frac{\left( \sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta} \right)^2}{2 \pi}} \right)}{\theta^2} == v, v \right] \\
& \quad \left\{ \left\{ v \rightarrow \frac{2 \pi \left( \frac{4 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \sqrt{\frac{4 \pi^2}{(4 \pi - \theta) \theta} - \frac{\sqrt{(4 \pi - \theta) \theta} \left( -\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{4 \pi - \theta} + \frac{8 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)}{2 \pi (4 \pi - \theta)}} \right)}{\theta^2} \right\} \right\}
\end{aligned}$$

RevolutionPlot3D[

$$2 \pi \left( \frac{4 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \sqrt{\frac{4 \pi^2}{(4 \pi - \theta) \theta} - \frac{\sqrt{(4 \pi - \theta) \theta} \left( -\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{4 \pi - \theta} + \frac{8 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)}{2 \pi (4 \pi - \theta)}} \right)$$

$\theta^2$

, { $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }]



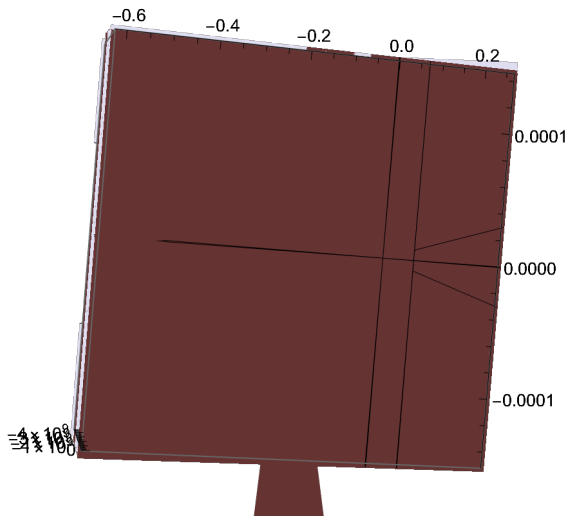
$$2 \pi \left( 2 \pi r - 2 \pi \sqrt{r^2 - \left( \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \right)^2} \right)$$

$\theta^2$

Solve[  
== v , v]

$$\left\{ \left\{ v \rightarrow \frac{2 \pi \left( 2 \pi r - \sqrt{r^2 (2 \pi - \theta)^2} \right)}{\theta^2} \right\} \right\}$$

RevolutionPlot3D $\left[\frac{2 \pi \left(2 \pi r - \sqrt{r^2 (2 \pi - \theta)^2}\right)}{\theta^2}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$c := 2.99792458 \cdot 10^8$

Solve $\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) / \left(\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right)\right) == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta]$

$\left\{\left\{\theta \rightarrow 0.5 \left(12.5664 - 12.5664 \sqrt{1 - 1 \cdot \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 0.5 \left(12.5664 + 12.5664 \sqrt{1 - 1 \cdot \sin[\beta]^2}\right)\right\}\right\}$

$$\text{Solve}\left[\frac{\sqrt{-1.1294090667581471 \cdot \eta^{18} + 8.987551787368176 \cdot \eta^{16} \theta^2 + 3.5481432270250993 \cdot \eta^{18} \sin[\beta]^2}}{\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}}\right]$$

$$\left( \left( \sqrt{3.5481432270250993 \cdot \eta^{18} - 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2} \right) / \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) \right) = \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta$$

$$\left\{ \left\{ \theta \rightarrow 0.5 \left( 12.5664 - 12.5664 \sqrt{1 - 1. \sin[\beta]^2} \right), \right. \right. \\ \left. \left. \left\{ \theta \rightarrow 0.5 \left( 12.5664 + 12.5664 \sqrt{1 - 1. \sin[\beta]^2} \right) \right\} \right\} \right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \sin[\beta], \theta\right]$$

$$\begin{aligned} & \left\{ \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \right. \\ & \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \text{i} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \text{i} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \\ & \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 + \text{i} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 + \text{i} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \\ & \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 + \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 + \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \\ & \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - (-1)^{1/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - (-1)^{1/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \\ & \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 + (-1)^{1/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 + (-1)^{1/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \\ & \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - (-1)^{3/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - (-1)^{3/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \\ & \left. \left\{ \Theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 + (-1)^{3/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \Theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 + (-1)^{3/4} \pi^2 \text{Sin}[\beta]^2} \right) \right\} \right\} \end{aligned}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi r \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \text{Sin}[\beta], \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \right. \\ \left. \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 + \pi^2 \text{Sin}[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 + \pi^2 \text{Sin}[\beta]^2} \right) \right\} \right\}$$

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \text{Sin}[\beta], \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\left(\pi r - \sqrt{\pi^2 r^2 - \pi^2 r \eta \text{Sin}[\beta]}\right)}{r}\right\}, \left\{\theta \rightarrow \frac{2\left(\pi r + \sqrt{\pi^2 r^2 - \pi^2 r \eta \text{Sin}[\beta]}\right)}{r}\right\}, \right.$$

$$\left.\left\{\theta \rightarrow \frac{2\left(\pi r - \sqrt{\pi^2 r^2 + \pi^2 r \eta \text{Sin}[\beta]}\right)}{r}\right\}, \left\{\theta \rightarrow \frac{2\left(\pi r + \sqrt{\pi^2 r^2 + \pi^2 r \eta \text{Sin}[\beta]}\right)}{r}\right\}\right\}$$

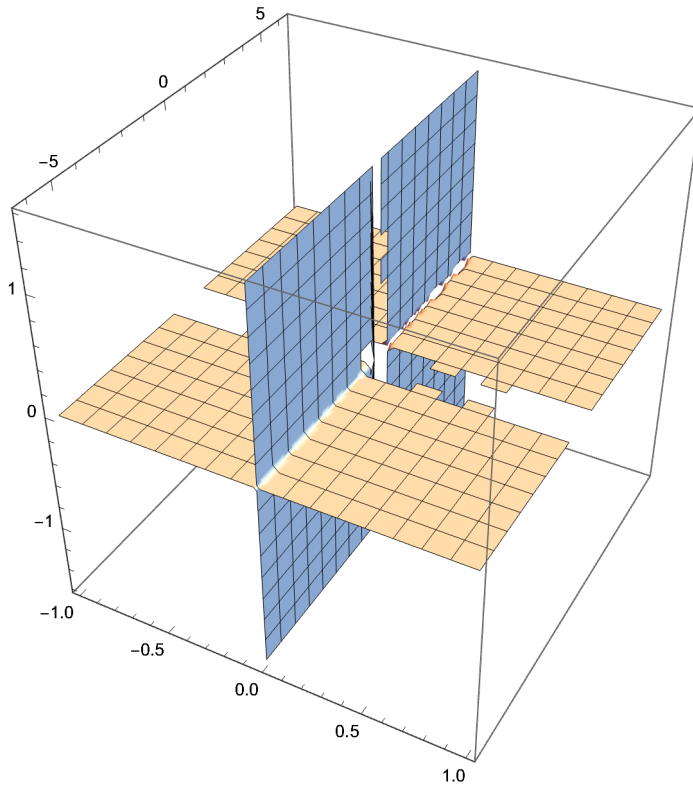
$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == \frac{2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}{\sqrt{4\pi\theta - \theta^2}} \text{Sin}[\beta], \theta\right]$$

Solve::verif : Potential solution  $\{\theta \rightarrow \text{ComplexInfinity}\}$  (possibly discarded by verifier) should be checked by hand.  
May require use of limits. >>

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \text{Sin}[\beta], r\right]$$

$$\left\{\left\{r \rightarrow -\frac{4\pi^2\eta \text{Sin}[\beta]}{(4\pi - \theta)\theta}\right\}, \left\{r \rightarrow \frac{4\pi^2\eta \text{Sin}[\beta]}{(4\pi - \theta)\theta}\right\}\right\}$$

$$\text{ContourPlot3D}\left[\frac{4 \pi^2 \eta \sin[\beta]}{(4 \pi - \theta) \theta}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$


$$\text{Solve}\left[\text{Abs}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right] \left(\frac{1}{\left(\frac{\theta}{2 \pi}\right)}\right) == c, r\right]$$

$$\text{Solve}\left[(\theta r - (2 \pi r - 2 \pi x)) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \theta, v\right]$$

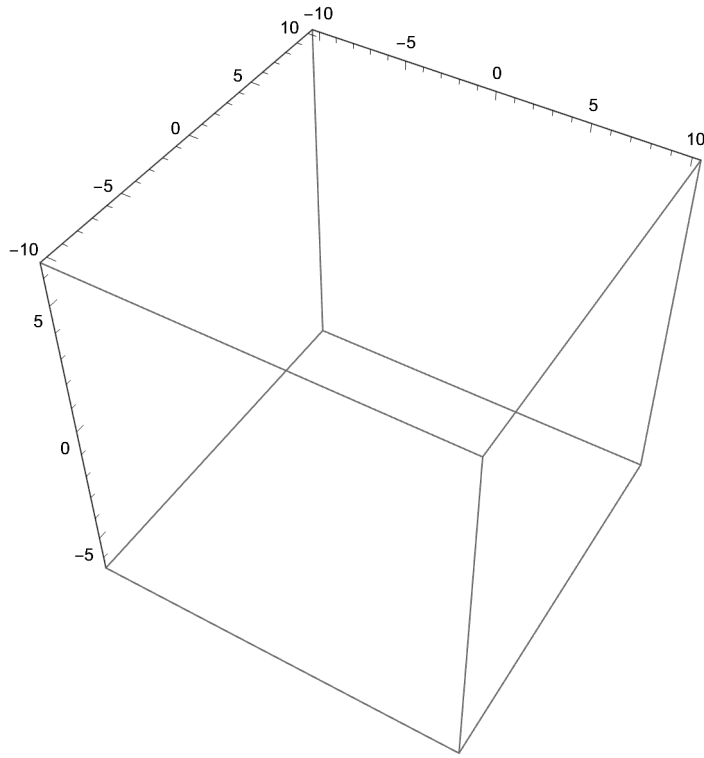
$$\{\{\}\}$$

$$\begin{aligned}
 & \text{Solve}\left[(\theta r - (2\pi r - 2\pi x)) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == \right. \\
 & \left. (\theta r - (2\pi r - 2\pi \sqrt{(r^2 - \eta^2)}) \right) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi}, v] \\
 & \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ (1.11468 \times 10^{19} - 3.54814 \times 10^{18} x^2 \theta - \right. \right. \right. \\
 & \quad \left. \left. \left. 3.54814 \times 10^{18} \eta^2 \theta + 2.82352 \times 10^{17} x^2 \theta^2 + 2.82352 \times 10^{17} \eta^2 \theta^2 \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{124.025 - 39.4784 x^2 \theta - 39.4784 \eta^2 \theta + 3.14159 x^2 \theta^2 + 3.14159 \eta^2 \theta^2} \right) \right\}, \\
 & \left\{ v \rightarrow \left( \sqrt{ (1.11468 \times 10^{19} - 3.54814 \times 10^{18} x^2 \theta - 3.54814 \times 10^{18} \eta^2 \theta + \right. \right. \right. \\
 & \quad \left. \left. \left. 2.82352 \times 10^{17} x^2 \theta^2 + 2.82352 \times 10^{17} \eta^2 \theta^2 \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{124.025 - 39.4784 x^2 \theta - 39.4784 \eta^2 \theta + 3.14159 x^2 \theta^2 + 3.14159 \eta^2 \theta^2} \right) \right\} \}
 \end{aligned}$$

```

ContourPlot3D[
  (√(1.1146820695906433`*^19 - 3.5481432270250993`*^18 x^2 θ - 3.5481432270250993`*^18
    η^2 θ + 2.8235226668953677`*^17 x^2 θ^2 + 2.8235226668953677`*^17 η^2 θ^2)) /
  (√(124.02510672119928` - 39.47841760435743` x^2 θ - 39.47841760435743` η^2 θ +
    3.141592653589793` x^2 θ^2 + 3.141592653589793` η^2 θ^2)),
  {η, -.1, .1}, {x, -.1, .1}, {θ, -2 π, 2 π}]

```





$$\text{Solve}\left[(\theta r - (2\pi r - 2\pi x)) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == \right. \\ \left. \left( \theta r - \left( 2\pi r - 2\pi \sqrt{\left( r^2 - \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right)^2} \right) \right) \right. \\ \left. \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi}, v \right] \\ \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{\left( 1.11468 \times 10^{19} - 3.54814 \times 10^{18} \theta - \right. \right. \right. \right. \\ \left. \left. \left. 3.54814 \times 10^{18} x^2 \theta + 2.82352 \times 10^{17} \theta^2 + 2.82352 \times 10^{17} x^2 \theta^2 \right) \right) / \right. \\ \left. \left( \sqrt{124.025 - 39.4784 \theta - 39.4784 x^2 \theta + 3.14159 \theta^2 + 3.14159 x^2 \theta^2} \right) \right\}, \\ \left\{ v \rightarrow \left( \sqrt{\left( 1.11468 \times 10^{19} - 3.54814 \times 10^{18} \theta - 3.54814 \times 10^{18} x^2 \theta + \right. \right. \right. \\ \left. \left. \left. 2.82352 \times 10^{17} \theta^2 + 2.82352 \times 10^{17} x^2 \theta^2 \right) \right) / \right. \\ \left. \left( \sqrt{124.025 - 39.4784 \theta - 39.4784 x^2 \theta + 3.14159 \theta^2 + 3.14159 x^2 \theta^2} \right) \right\} \right\}$$

$$\text{Solve}\left[(\theta r - (2\pi r - 2\pi x)) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == \right. \\ \left. \left( \theta r - \left( 2\pi r - 2\pi \sqrt{\left( r^2 - \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right)^2} \right) \right) \right. \\ \left. \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi}, v \right]$$

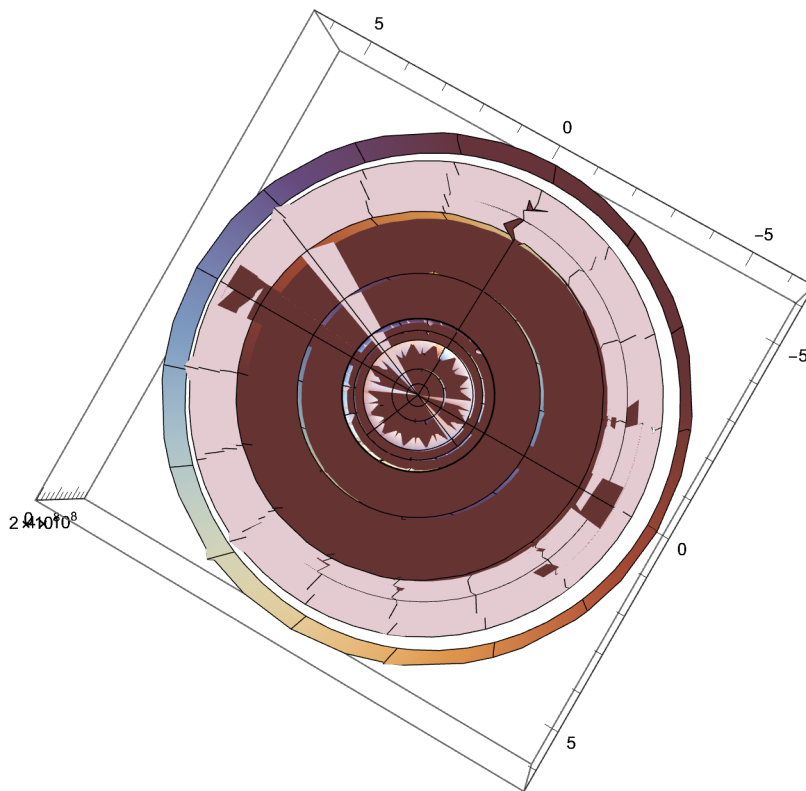
$$\text{Solve}\left[ \right. \\ \left. (\theta r - (2\pi r - 2\pi x)) \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == (\theta r - (2\pi r - 2\pi x)), v \right]$$

Solve[

$$\begin{aligned}
 & \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = (\theta r - (2\pi r - 2\pi x)), v] \\
 & \left\{ \left\{ v \rightarrow - \left( 1. \sqrt{ (8.57837 \times 10^{35} r^2 - 1.71567 \times 10^{36} r x + 8.57837 \times 10^{35} x^2 - \right. \right. \right. \\
 & \quad 2.73058 \times 10^{35} r^2 \theta - 2.73058 \times 10^{35} r^4 \theta + 2.73058 \times 10^{35} r x \theta + \\
 & \quad 5.46116 \times 10^{35} r^3 x \theta - 2.73058 \times 10^{35} r^2 x^2 \theta + 2.17293 \times 10^{34} r^2 \theta^2 + \\
 & \quad 1.08646 \times 10^{35} r^4 \theta^2 - 1.30376 \times 10^{35} r^3 x \theta^2 + 2.17293 \times 10^{34} r^2 x^2 \theta^2 - \\
 & \quad \left. \left. 1.38333 \times 10^{34} r^4 \theta^3 + 6.91664 \times 10^{33} r^3 x \theta^3 + 5.50409 \times 10^{32} r^4 \theta^4 \right) \right) / \\
 & \quad \left( \sqrt{ (9.54472 \times 10^{18} r^2 - 1.90894 \times 10^{19} r x + 9.54472 \times 10^{18} x^2 - 3.03818 \times 10^{18} r^2 \theta - \right. \\
 & \quad 3.03818 \times 10^{18} r^4 \theta + 3.03818 \times 10^{18} r x \theta + 6.07636 \times 10^{18} r^3 x \theta - \\
 & \quad 3.03818 \times 10^{18} r^2 x^2 \theta + 2.41771 \times 10^{17} r^2 \theta^2 + 1.20885 \times 10^{18} r^4 \theta^2 - \\
 & \quad 1.45062 \times 10^{18} r^3 x \theta^2 + 2.41771 \times 10^{17} r^2 x^2 \theta^2 - \\
 & \quad \left. \left. 1.53916 \times 10^{17} r^4 \theta^3 + 7.6958 \times 10^{16} r^3 x \theta^3 + 6.12412 \times 10^{15} r^4 \theta^4 \right) \right) \right\}, \\
 & \left\{ v \rightarrow \left( \sqrt{ (8.57837 \times 10^{35} r^2 - 1.71567 \times 10^{36} r x + 8.57837 \times 10^{35} x^2 - \right. \right. \\
 & \quad 2.73058 \times 10^{35} r^2 \theta - 2.73058 \times 10^{35} r^4 \theta + 2.73058 \times 10^{35} r x \theta + \\
 & \quad 5.46116 \times 10^{35} r^3 x \theta - 2.73058 \times 10^{35} r^2 x^2 \theta + 2.17293 \times 10^{34} r^2 \theta^2 + \\
 & \quad 1.08646 \times 10^{35} r^4 \theta^2 - 1.30376 \times 10^{35} r^3 x \theta^2 + 2.17293 \times 10^{34} r^2 x^2 \theta^2 - \\
 & \quad \left. \left. 1.38333 \times 10^{34} r^4 \theta^3 + 6.91664 \times 10^{33} r^3 x \theta^3 + 5.50409 \times 10^{32} r^4 \theta^4 \right) \right) / \\
 & \quad \left( \sqrt{ (9.54472 \times 10^{18} r^2 - 1.90894 \times 10^{19} r x + 9.54472 \times 10^{18} x^2 - 3.03818 \times 10^{18} r^2 \theta - \right. \\
 & \quad 3.03818 \times 10^{18} r^4 \theta + 3.03818 \times 10^{18} r x \theta + 6.07636 \times 10^{18} r^3 x \theta - \\
 & \quad 3.03818 \times 10^{18} r^2 x^2 \theta + 2.41771 \times 10^{17} r^2 \theta^2 + 1.20885 \times 10^{18} r^4 \theta^2 - \\
 & \quad 1.45062 \times 10^{18} r^3 x \theta^2 + 2.41771 \times 10^{17} r^2 x^2 \theta^2 - \\
 & \quad \left. \left. 1.53916 \times 10^{17} r^4 \theta^3 + 7.6958 \times 10^{16} r^3 x \theta^3 + 6.12412 \times 10^{15} r^4 \theta^4 \right) \right) \right\} \}
 \end{aligned}$$

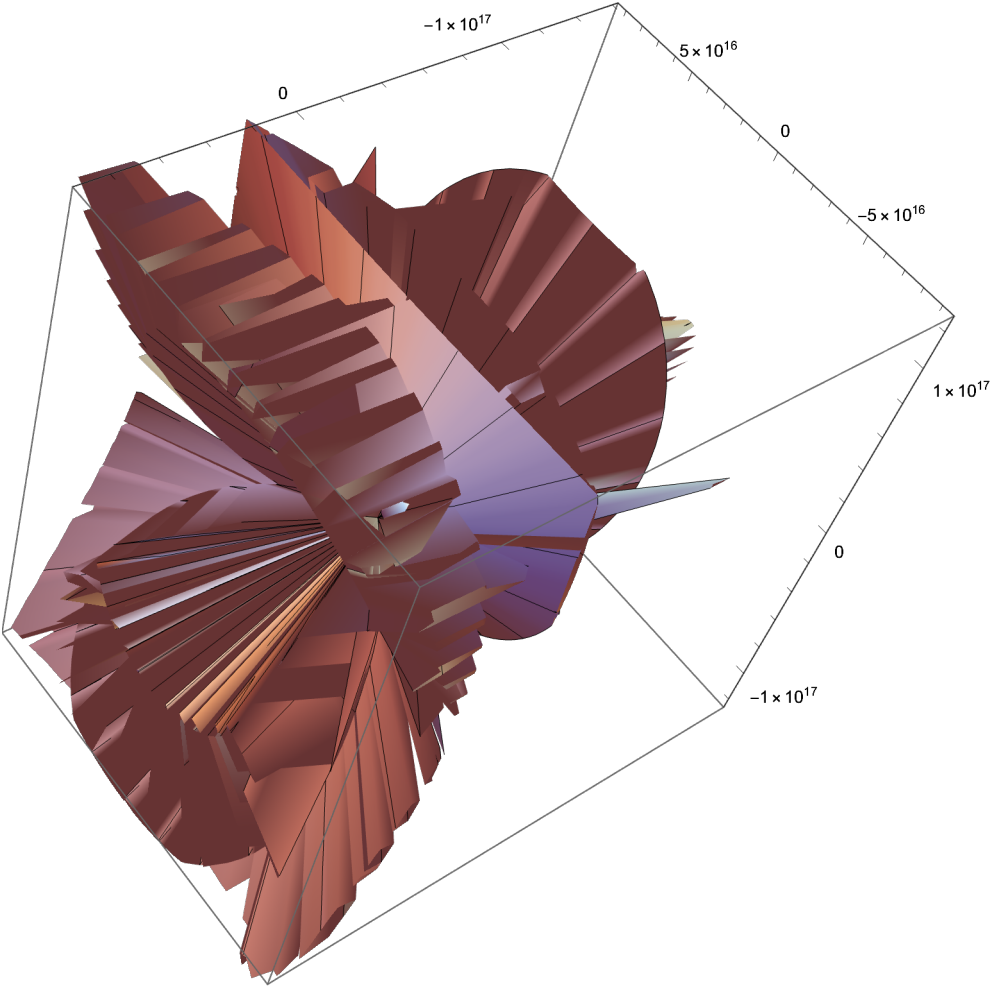
RevolutionPlot3D[

$$\left( \sqrt{\left( 8.578370837369684 \cdot r^{35} - 1.7156741674739368 \cdot r^{36} x + 8.578370837369684 \cdot r^{35} x^2 - 2.730580244885493 \cdot r^{35} \theta - 2.7305802448854928 \cdot r^{35} r^4 \theta + 2.730580244885493 \cdot r^{35} r x \theta + 5.4611604897709856 \cdot r^{35} r^3 x \theta - 2.7305802448854928 \cdot r^{35} r^2 x^2 \theta + 2.1729267174130213 \cdot r^{34} r^2 \theta^2 + 1.0864633587065107 \cdot r^{35} r^4 \theta^2 - 1.3037560304478129 \cdot r^{35} r^3 x \theta^2 + 2.1729267174130213 \cdot r^{34} r^2 x^2 \theta^2 - 1.3833281122109134 \cdot r^{34} r^4 \theta^3 + 6.916640561054567 \cdot r^{33} r^3 x \theta^3 + 5.504087674408673 \cdot r^{32} r^4 \theta^4 \right)} \right. \\ \left. \left( \sqrt{\left( 9.544724793048105 \cdot r^{18} - 1.908944958609621 \cdot r^{19} x + 9.544724793048105 \cdot r^{18} x^2 - 3.0381802625307474 \cdot r^{18} r^2 \theta - 3.038180262530747 \cdot r^{18} r^4 \theta + 3.0381802625307474 \cdot r^{18} r x \theta + 6.076360525061494 \cdot r^{18} r^3 x \theta - 3.038180262530747 \cdot r^{18} r^2 x^2 \theta + 2.4177070339300035 \cdot r^{17} r^2 \theta^2 + 1.2088535169650017 \cdot r^{18} r^4 \theta^2 - 1.450624220358002 \cdot r^{18} r^3 x \theta^2 + 2.4177070339300032 \cdot r^{17} r^2 x^2 \theta^2 - 1.5391601015920192 \cdot r^{17} r^4 \theta^3 + 7.695800507960096 \cdot r^{16} r^3 x \theta^3 + 6.124123459454841 \cdot r^{15} r^4 \theta^4 \right)} \right), \{\theta, -2\pi, 2\pi\}]$$



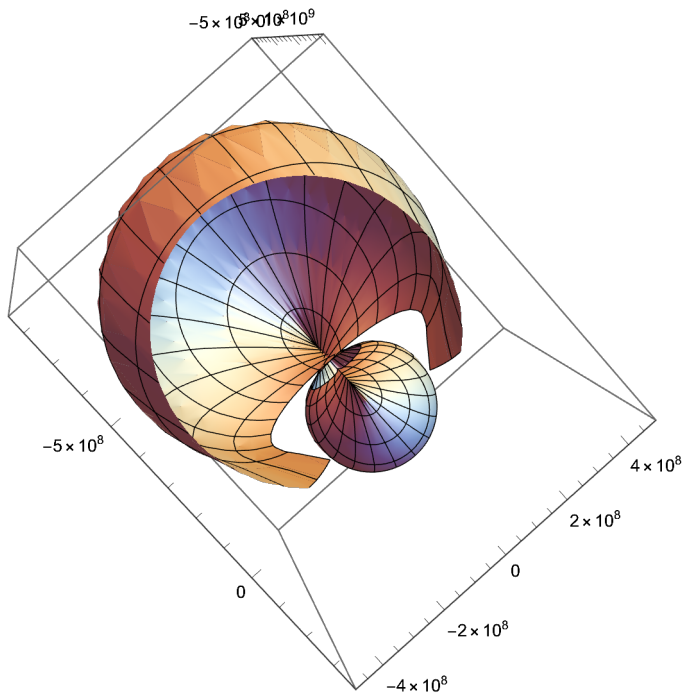
SphericalPlot3D[

$$\left( \sqrt{\left( 8.578370837369684 \cdot r^{35} - 1.7156741674739368 \cdot r^{36} x + 8.578370837369684 \cdot r^{35} x^2 - 2.730580244885493 \cdot r^{35} \theta - 2.7305802448854928 \cdot r^{35} r^4 \theta + 2.730580244885493 \cdot r^{35} r x \theta + 5.4611604897709856 \cdot r^{35} r^3 x \theta - 2.7305802448854928 \cdot r^{35} r^2 x^2 \theta + 2.1729267174130213 \cdot r^{34} r^2 \theta^2 + 1.0864633587065107 \cdot r^{35} r^4 \theta^2 - 1.3037560304478129 \cdot r^{35} r^3 x \theta^2 + 2.1729267174130213 \cdot r^{34} r^2 x^2 \theta^2 - 1.3833281122109134 \cdot r^{34} r^4 \theta^3 + 6.916640561054567 \cdot r^{33} r^3 x \theta^3 + 5.504087674408673 \cdot r^{32} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^4 \right) \right) / \right. \\ \left. \left( \sqrt{\left( 9.544724793048105 \cdot r^{18} - 1.908944958609621 \cdot r^{19} x + 9.544724793048105 \cdot r^{18} x^2 - 3.0381802625307474 \cdot r^{18} r^2 \theta - 3.038180262530747 \cdot r^{18} r^4 \theta + 3.0381802625307474 \cdot r^{18} r x \theta + 6.076360525061494 \cdot r^{18} r^3 x \theta - 3.038180262530747 \cdot r^{18} r^2 x^2 \theta + 2.4177070339300035 \cdot r^{17} r^2 \theta^2 + 1.2088535169650017 \cdot r^{18} r^4 \theta^2 - 1.450624220358002 \cdot r^{18} r^3 x \theta^2 + 2.4177070339300032 \cdot r^{17} r^2 x^2 \theta^2 - 1.5391601015920192 \cdot r^{17} r^4 \theta^3 + 7.695800507960096 \cdot r^{16} r^3 x \theta^3 + 6.124123459454841 \cdot r^{15} r^4 \theta^4 \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} ]$$



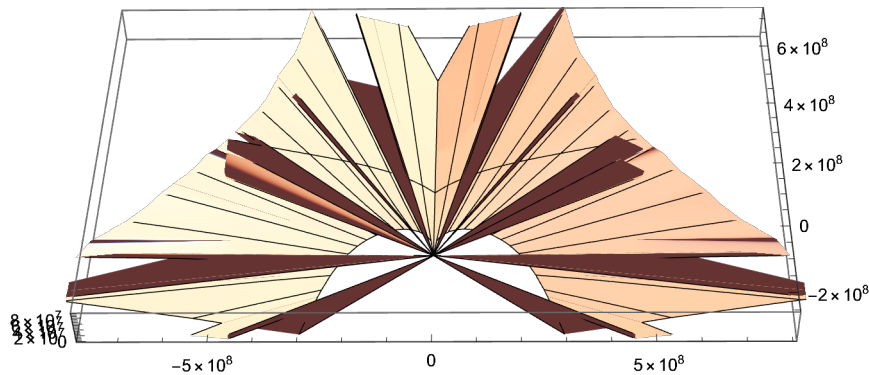
SphericalPlot3D[

$$\begin{aligned}
& \left( \sqrt{\left( 8.578370837369684 \cdot r^{35} - 1.7156741674739368 \cdot r^{36} x + 8.578370837369684 \cdot r^{35} \right. \right. \\
& \quad x^2 - 2.730580244885493 \cdot r^{35} r^2 \theta - 2.7305802448854928 \cdot r^{35} r^4 \theta + \\
& \quad 2.730580244885493 \cdot r^{35} r x \theta + 5.4611604897709856 \cdot r^{35} r^3 x \theta - \\
& \quad 2.7305802448854928 \cdot r^{35} r^2 x^2 \theta + 2.1729267174130213 \cdot r^{34} r^2 \theta^2 + \\
& \quad 1.0864633587065107 \cdot r^{35} r^4 \theta^2 - 1.3037560304478129 \cdot r^{35} r^3 x \theta^2 + \\
& \quad 2.1729267174130213 \cdot r^{34} r^2 x^2 \theta^2 - \\
& \quad 1.3833281122109134 \cdot r^{34} r^4 \theta^3 + 6.916640561054567 \cdot r^{33} r^3 x \theta^3 + \\
& \quad \left. \left. 5.504087674408673 \cdot r^{32} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^4 \right) \right) \right) / \\
& \left( \sqrt{\left( 9.544724793048105 \cdot r^{18} - 1.908944958609621 \cdot r^{19} x + \right. \right. \\
& \quad 9.544724793048105 \cdot r^{18} x^2 - 3.0381802625307474 \cdot r^{18} r^2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \\
& \quad 3.038180262530747 \cdot r^{18} r^4 \theta + 3.0381802625307474 \cdot r^{18} r x \theta + \\
& \quad 6.076360525061494 \cdot r^{18} r^3 x \theta - 3.038180262530747 \cdot r^{18} r^2 x^2 \theta + \\
& \quad 2.4177070339300035 \cdot r^{17} r^2 \theta^2 + 1.2088535169650017 \cdot r^{18} r^4 \theta^2 - \\
& \quad 1.450624220358002 \cdot r^{18} r^3 x \theta^2 + 2.4177070339300032 \cdot r^{17} r^2 x^2 \theta^2 - \\
& \quad 1.5391601015920192 \cdot r^{17} r^4 \theta^3 + 7.695800507960096 \cdot r^{16} r^3 x \theta^3 + \\
& \quad \left. \left. 6.124123459454841 \cdot r^{15} r^4 \theta^4 \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} ]
\end{aligned}$$



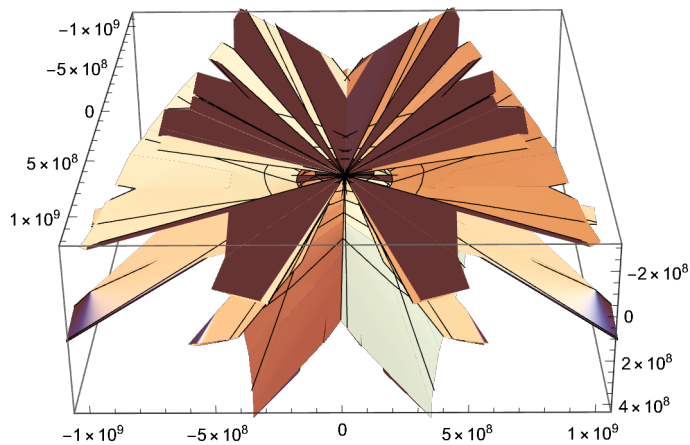
SphericalPlot3D[

$$\begin{aligned}
& \left( \sqrt{\left( 8.578370837369684 \cdot r^{35} - 1.7156741674739368 \cdot r^{36} x + 8.578370837369684 \cdot r^{35} \right. \right. \\
& \quad x^2 - 2.730580244885493 \cdot r^{35} r^2 \theta - 2.7305802448854928 \cdot r^{35} r^4 \theta + \\
& \quad 2.730580244885493 \cdot r^{35} r x \theta + 5.4611604897709856 \cdot r^{35} r^3 x \theta - \\
& \quad 2.7305802448854928 \cdot r^{35} r^2 x^2 \theta + 2.1729267174130213 \cdot r^{34} r^2 \theta^2 + \\
& \quad 1.0864633587065107 \cdot r^{35} r^4 \theta^2 - 1.3037560304478129 \cdot r^{35} r^3 x \theta^2 + \\
& \quad 2.1729267174130213 \cdot r^{34} r^2 x^2 \theta^2 - \\
& \quad 1.3833281122109134 \cdot r^{34} r^4 \theta^3 + 6.916640561054567 \cdot r^{33} r^3 x \theta^3 + \\
& \quad \left. \left. 5.504087674408673 \cdot r^{32} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 \right) \right) / \\
& \left( \sqrt{\left( 9.544724793048105 \cdot r^{18} - 1.908944958609621 \cdot r^{19} x + \right. \right. \\
& \quad 9.544724793048105 \cdot r^{18} x^2 - 3.0381802625307474 \cdot r^{18} r^2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \\
& \quad 3.038180262530747 \cdot r^{18} r^4 \theta + 3.0381802625307474 \cdot r^{18} r x \theta + \\
& \quad 6.076360525061494 \cdot r^{18} r^3 x \theta - 3.038180262530747 \cdot r^{18} r^2 x^2 \theta + \\
& \quad 2.4177070339300035 \cdot r^{17} r^2 \theta^2 + 1.2088535169650017 \cdot r^{18} r^4 \theta^2 - \\
& \quad 1.450624220358002 \cdot r^{18} r^3 x \theta^2 + 2.4177070339300032 \cdot r^{17} r^2 x^2 \theta^2 - \\
& \quad \left. \left. 1.5391601015920192 \cdot r^{17} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^3 + 7.695800507960096 \cdot r^{16} \right. \right. \\
& \quad \left. \left. r^3 x \theta^3 + 6.124123459454841 \cdot r^{15} r^4 \theta^4 \right) \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}
\end{aligned}$$



SphericalPlot3D[

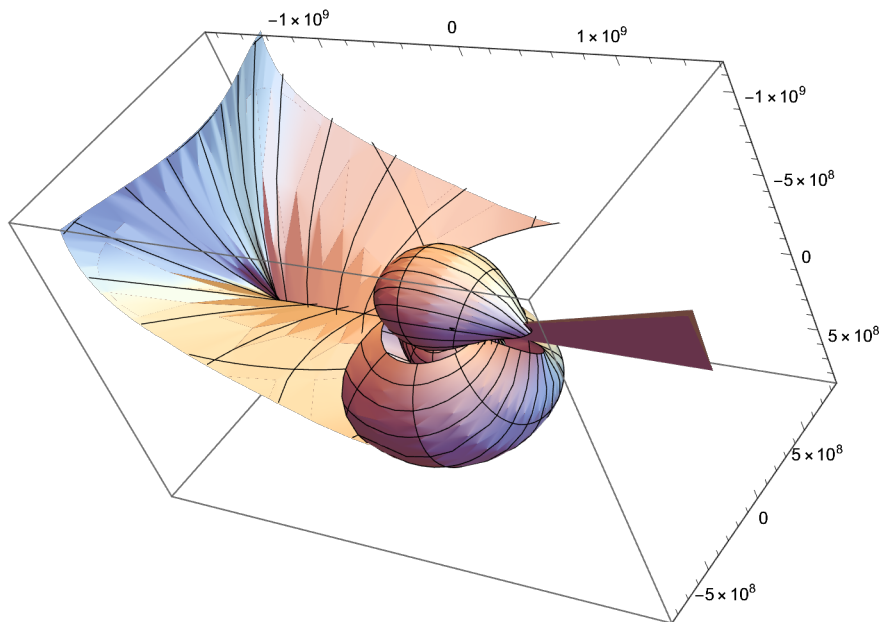
$$\begin{aligned}
& \left( \sqrt{\left( 8.578370837369684 \cdot r^{35} - 1.7156741674739368 \cdot r^{36} r x + 8.578370837369684 \cdot r^{35} \right. \right. \\
& \quad x^2 - 2.730580244885493 \cdot r^{35} r^2 \theta - 2.7305802448854928 \cdot r^{35} r^4 \theta + \\
& \quad 2.730580244885493 \cdot r^{35} r x \theta + 5.4611604897709856 \cdot r^{35} r^3 x \theta - \\
& \quad 2.7305802448854928 \cdot r^{35} r^2 x^2 \theta + 2.1729267174130213 \cdot r^{34} r^2 \theta^2 + \\
& \quad 1.0864633587065107 \cdot r^{35} r^4 \theta^2 - 1.3037560304478129 \cdot r^{35} r^3 x \theta^2 + \\
& \quad 2.1729267174130213 \cdot r^{34} r^2 x^2 \theta^2 - \\
& \quad 1.3833281122109134 \cdot r^{34} r^4 \theta^3 + 6.916640561054567 \cdot r^{33} r^3 x \theta^3 + \\
& \quad \left. \left. 5.504087674408673 \cdot r^{32} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 \right) \right) / \\
& \left( \sqrt{\left( 9.544724793048105 \cdot r^{18} r^2 - 1.908944958609621 \cdot r^{19} r x + \right. \right. \\
& \quad 9.544724793048105 \cdot r^{18} x^2 - 3.0381802625307474 \cdot r^{18} r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \\
& \quad 3.038180262530747 \cdot r^{18} r^4 \theta + 3.0381802625307474 \cdot r^{18} r x \theta + \\
& \quad 6.076360525061494 \cdot r^{18} r^3 x \theta - 3.038180262530747 \cdot r^{18} r^2 x^2 \theta + \\
& \quad 2.4177070339300035 \cdot r^{17} r^2 \theta^2 + \\
& \quad 1.2088535169650017 \cdot r^{18} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 - \\
& \quad 1.450624220358002 \cdot r^{18} r^3 x \theta^2 + 2.4177070339300032 \cdot r^{17} r^2 x^2 \theta^2 - \\
& \quad \left. \left. 1.5391601015920192 \cdot r^{17} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^3 + 7.695800507960096 \cdot r^{16} \right. \right. \\
& \quad \left. \left. r^3 x \theta^3 + 6.124123459454841 \cdot r^{15} r^4 \theta^4 \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} ]
\end{aligned}$$





SphericalPlot3D[

$$\begin{aligned}
& \left( \sqrt{\left( 8.578370837369684 \cdot r^{35} - 1.7156741674739368 \cdot r^{36} x + 8.578370837369684 \cdot r^{35} \right. \right. \\
& \quad x^2 - 2.730580244885493 \cdot r^{35} r^2 \theta - 2.7305802448854928 \cdot r^{35} r^4 \theta + \\
& \quad 2.730580244885493 \cdot r^{35} r x \theta + 5.4611604897709856 \cdot r^{35} r^3 x \theta - \\
& \quad 2.7305802448854928 \cdot r^{35} r^2 x^2 \theta + 2.1729267174130213 \cdot r^{34} r^2 \theta^2 + \\
& \quad 1.0864633587065107 \cdot r^{35} r^4 \theta^2 - 1.3037560304478129 \cdot r^{35} r^3 x \theta^2 + \\
& \quad 2.1729267174130213 \cdot r^{34} r^2 x^2 \theta^2 - \\
& \quad 1.3833281122109134 \cdot r^{34} r^4 \theta^3 + 6.916640561054567 \cdot r^{33} r^3 x \theta^3 + \\
& \quad \left. \left. 5.504087674408673 \cdot r^{32} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 \right) \right) / \\
& \left( \sqrt{\left( 9.544724793048105 \cdot r^{18} - 1.908944958609621 \cdot r^{19} x + \right. \right. \\
& \quad 9.544724793048105 \cdot r^{18} x^2 - 3.0381802625307474 \cdot r^{18} r^2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \\
& \quad 3.038180262530747 \cdot r^{18} r^4 \theta + 3.0381802625307474 \cdot r^{18} r x \theta + \\
& \quad 6.076360525061494 \cdot r^{18} r^3 x \theta - 3.038180262530747 \cdot r^{18} r^2 x^2 \theta + \\
& \quad 2.4177070339300035 \cdot r^{17} r^2 \theta^2 + \\
& \quad 1.2088535169650017 \cdot r^{18} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 - \\
& \quad 1.450624220358002 \cdot r^{18} r^3 x \theta^2 + 2.4177070339300032 \cdot r^{17} r^2 x^2 \theta^2 - \\
& \quad 1.5391601015920192 \cdot r^{17} r^4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^3 + \\
& \quad 7.695800507960096 \cdot r^{16} r^3 x \theta^3 + 6.124123459454841 \cdot r^{15} r^4 \\
& \quad \left. \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^4 \right) \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} ]
\end{aligned}$$



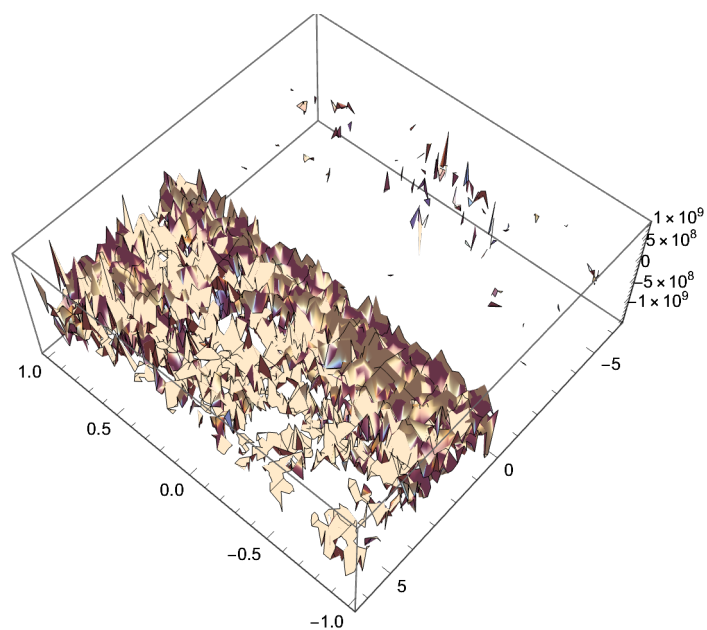
$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$x := \frac{2 \pi r - r \theta}{2 \pi}$$

```

Plot3D[{- (1. `√ (8.578370837369684`^35 r^2 -
1.7156741674739368`^36 r x + 8.578370837369684`^35 x^2 -
2.730580244885493`^35 r^2 θ - 2.7305802448854928`^35 r^4 θ +
2.730580244885493`^35 r x θ + 5.4611604897709856`^35 r^3 x θ -
2.7305802448854928`^35 r^2 x^2 θ + 2.1729267174130213`^34 r^2 θ^2 +
1.0864633587065107`^35 r^4 θ^2 - 1.3037560304478129`^35 r^3 x θ^2 +
2.1729267174130213`^34 r^2 x^2 θ^2 - 1.3833281122109134`^34 r^4 θ^3 +
6.916640561054567`^33 r^3 x θ^3 + 5.504087674408673`^32 r^4 θ^4)) /
(√ (9.544724793048105`^18 r^2 - 1.908944958609621`^19 r x +
9.544724793048105`^18 x^2 - 3.0381802625307474`^18 r^2 θ -
3.038180262530747`^18 r^4 θ + 3.0381802625307474`^18 r x θ +
6.076360525061494`^18 r^3 x θ - 3.038180262530747`^18 r^2 x^2 θ +
2.4177070339300035`^17 r^2 θ^2 + 1.2088535169650017`^18 r^4 θ^2 -
1.450624220358002`^18 r^3 x θ^2 + 2.4177070339300032`^17 r^2 x^2 θ^2 -
1.5391601015920192`^17 r^4 θ^3 + 7.695800507960096`^16 r^3 x θ^3 +
6.124123459454841`^15 r^4 θ^4)),
(√ (8.578370837369684`^35 r^2 - 1.7156741674739368`^36 r x + 8.578370837369684`^35
x^2 - 2.730580244885493`^35 r^2 θ - 2.7305802448854928`^35 r^4 θ +
2.730580244885493`^35 r x θ + 5.4611604897709856`^35 r^3 x θ -
2.7305802448854928`^35 r^2 x^2 θ + 2.1729267174130213`^34 r^2 θ^2 +
1.0864633587065107`^35 r^4 θ^2 - 1.3037560304478129`^35 r^3 x θ^2 +
2.1729267174130213`^34 r^2 x^2 θ^2 - 1.3833281122109134`^34 r^4 θ^3 +
6.916640561054567`^33 r^3 x θ^3 + 5.504087674408673`^32 r^4 θ^4)) /
(√ (9.544724793048105`^18 r^2 - 1.908944958609621`^19 r x +
9.544724793048105`^18 x^2 - 3.0381802625307474`^18 r^2 θ -
3.038180262530747`^18 r^4 θ + 3.0381802625307474`^18 r x θ +
6.076360525061494`^18 r^3 x θ - 3.038180262530747`^18 r^2 x^2 θ +
2.4177070339300035`^17 r^2 θ^2 + 1.2088535169650017`^18 r^4 θ^2 -
1.450624220358002`^18 r^3 x θ^2 + 2.4177070339300032`^17 r^2 x^2 θ^2 -
1.5391601015920192`^17 r^4 θ^3 + 7.695800507960096`^16 r^3 x θ^3 +
6.124123459454841`^15 r^4 θ^4))), {x, -1, 1}, {θ, -2 π, 2 π}]

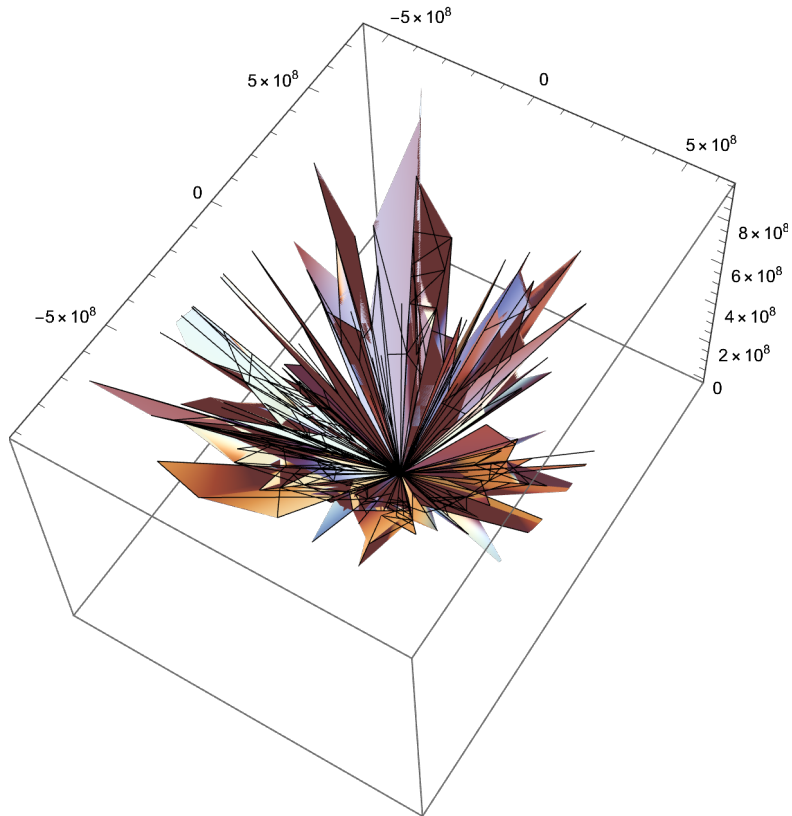
```



```

RevolutionPlot3D[{- (1. `√ (8.578370837369684`^35 r^2 -
1.7156741674739368`^36 r x + 8.578370837369684`^35 x^2 -
2.730580244885493`^35 r^2 θ - 2.7305802448854928`^35 r^4 θ +
2.730580244885493`^35 r x θ + 5.4611604897709856`^35 r^3 x θ -
2.7305802448854928`^35 r^2 x^2 θ + 2.1729267174130213`^34 r^2 θ^2 +
1.0864633587065107`^35 r^4 θ^2 - 1.3037560304478129`^35 r^3 x θ^2 +
2.1729267174130213`^34 r^2 x^2 θ^2 - 1.3833281122109134`^34 r^4 θ^3 +
6.916640561054567`^33 r^3 x θ^3 + 5.504087674408673`^32 r^4 θ^4)) /
(√ (9.544724793048105`^18 r^2 - 1.908944958609621`^19 r x +
9.544724793048105`^18 x^2 - 3.0381802625307474`^18 r^2 θ -
3.038180262530747`^18 r^4 θ + 3.0381802625307474`^18 r x θ +
6.076360525061494`^18 r^3 x θ - 3.038180262530747`^18 r^2 x^2 θ +
2.4177070339300035`^17 r^2 θ^2 + 1.2088535169650017`^18 r^4 θ^2 -
1.450624220358002`^18 r^3 x θ^2 + 2.4177070339300032`^17 r^2 x^2 θ^2 -
1.5391601015920192`^17 r^4 θ^3 + 7.695800507960096`^16 r^3 x θ^3 +
6.124123459454841`^15 r^4 θ^4)),
(√ (8.578370837369684`^35 r^2 - 1.7156741674739368`^36 r x + 8.578370837369684`^35
x^2 - 2.730580244885493`^35 r^2 θ - 2.7305802448854928`^35 r^4 θ +
2.730580244885493`^35 r x θ + 5.4611604897709856`^35 r^3 x θ -
2.7305802448854928`^35 r^2 x^2 θ + 2.1729267174130213`^34 r^2 θ^2 +
1.0864633587065107`^35 r^4 θ^2 - 1.3037560304478129`^35 r^3 x θ^2 +
2.1729267174130213`^34 r^2 x^2 θ^2 - 1.3833281122109134`^34 r^4 θ^3 +
6.916640561054567`^33 r^3 x θ^3 + 5.504087674408673`^32 r^4 θ^4)) /
(√ (9.544724793048105`^18 r^2 - 1.908944958609621`^19 r x +
9.544724793048105`^18 x^2 - 3.0381802625307474`^18 r^2 θ -
3.038180262530747`^18 r^4 θ + 3.0381802625307474`^18 r x θ +
6.076360525061494`^18 r^3 x θ - 3.038180262530747`^18 r^2 x^2 θ +
2.4177070339300035`^17 r^2 θ^2 + 1.2088535169650017`^18 r^4 θ^2 -
1.450624220358002`^18 r^3 x θ^2 + 2.4177070339300032`^17 r^2 x^2 θ^2 -
1.5391601015920192`^17 r^4 θ^3 + 7.695800507960096`^16 r^3 x θ^3 +
6.124123459454841`^15 r^4 θ^4))), {x, -1, 1}, {θ, -2 π, 2 π}]

```



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{(v)^2}{c^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], v\right]$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{(v)^2}{c^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi}^2 = r \sin[\beta]^2, v\right]$$

{{}}

$$\text{Solve}\left[\text{Abs}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}}}{2 \pi} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}\right] = \text{Abs}[r \sin[\beta]], v\right]$$

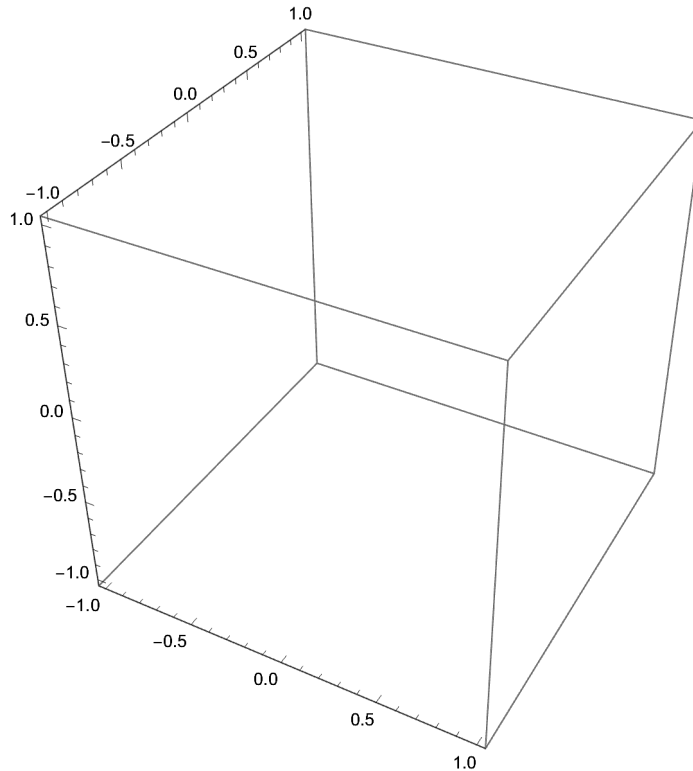
InverseFunction::ifun : Inverse functions are being used. Values may be lost for multivalued inverses. >>

$$\left\{ \left\{ v \rightarrow - \left( 1. \sqrt{(-1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2 + 8.98755 \times 10^{16} \text{Abs}^{(-1)}[6.283185307179586476925286766559 \text{Abs}[r \sin[\beta]])^2]} \right) / \left( \sqrt{(-12.5664 r^2 \theta + r^2 \theta^2 + \text{Abs}^{(-1)}[6.283185307179586476925286766559 \text{Abs}[r \sin[\beta]])^2]} \right) \right\}, \right. \\ \left. \left\{ v \rightarrow \left( \sqrt{(-1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2 + 8.98755 \times 10^{16} \text{Abs}^{(-1)}[6.283185307179586476925286766559 \text{Abs}[r \sin[\beta]])^2]} \right) / \left( \sqrt{(-12.5664 r^2 \theta + r^2 \theta^2 + \text{Abs}^{(-1)}[6.283185307179586476925286766559 \text{Abs}[r \sin[\beta]])^2]} \right) \right\} \right\}$$

```
SphericalPlot3D[
  { - (1. `  $\sqrt{(-1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2 + 8.987551787368176 \cdot 10^{16} \text{Abs}[r \sin[\beta]]^2)}$  ) /
    (  $\sqrt{(-12.566370614359172 r^2 \theta + r^2 \theta^2 + \text{Abs}[r \sin[\beta]]^2)}$  ) ,
    (  $\sqrt{(-12.566370614359172 r^2 \theta + r^2 \theta^2 + \text{Abs}[r \sin[\beta]]^2)}$  ) ,
    (  $\sqrt{(-1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2 + 8.987551787368176 \cdot 10^{16} \text{Abs}[r \sin[\beta]]^2)}$  ) /
    (  $\sqrt{(-12.566370614359172 r^2 \theta + r^2 \theta^2 + \text{Abs}[r \sin[\beta]]^2)}$  ) ) , { $\theta$ , -2  $\pi$ , 2}, { $\beta$ , - $\pi/2$ ,  $\pi/2$ }]
```

SphericalPlot3D::excl: {<<1>>} must be a list of equalities or real-valued functions. >>

SphericalPlot3D::excl: {<<1>>} must be a list of equalities or real-valued functions. >>

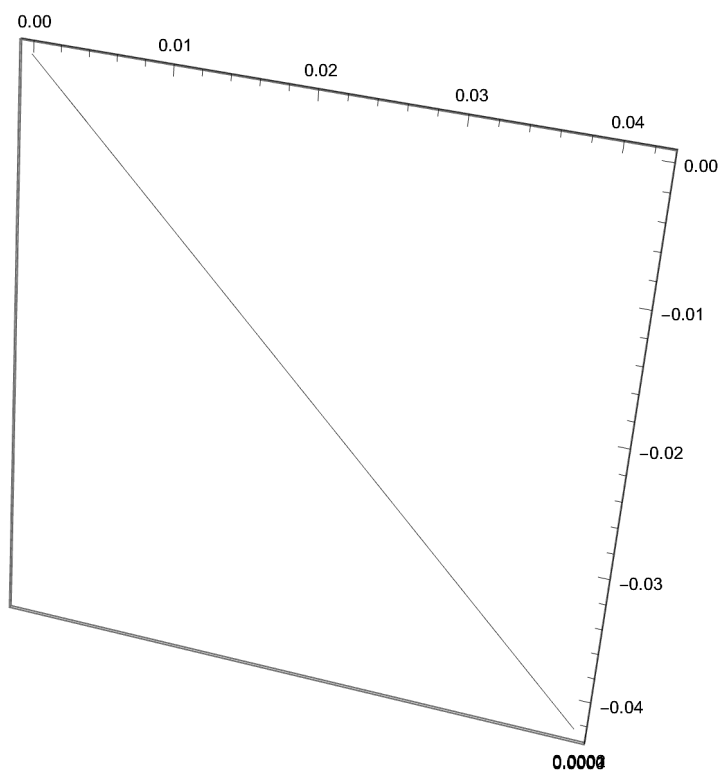


$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\text{Solve}\left[\frac{\sqrt{4\pi-\theta}\sqrt{\theta}\text{Abs}[x+\text{i}y]}{2\pi}==y,y\right]$$

$$\left\{\left\{y\rightarrow\frac{-4\text{i}\pi x\theta+\text{i}x\theta^2-2\pi\sqrt{4\pi x^2\theta-x^2\theta^2}}{-4\pi^2-4\pi\theta+\theta^2}\right\},\left\{y\rightarrow\frac{-4\text{i}\pi x\theta+\text{i}x\theta^2+2\pi\sqrt{4\pi x^2\theta-x^2\theta^2}}{-4\pi^2-4\pi\theta+\theta^2}\right\}\right\}$$

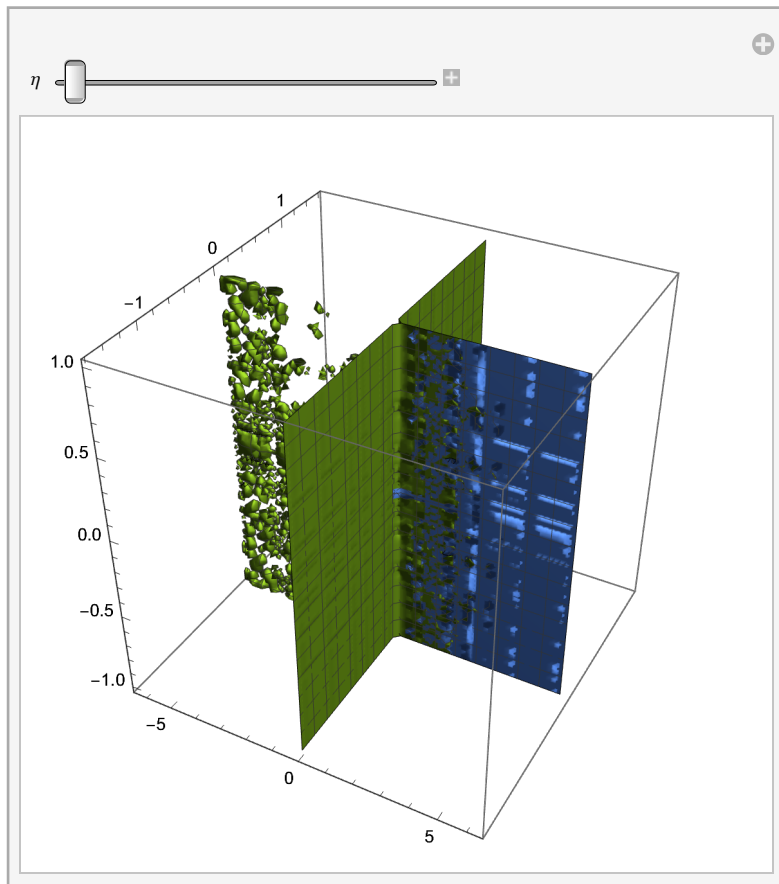
$$\text{RevolutionPlot3D}\left[\left\{\frac{-4\text{i}\pi x\theta+\text{i}x\theta^2-2\pi\sqrt{4\pi x^2\theta-x^2\theta^2}}{-4\pi^2-4\pi\theta+\theta^2},\frac{-4\text{i}\pi x\theta+\text{i}x\theta^2+2\pi\sqrt{4\pi x^2\theta-x^2\theta^2}}{-4\pi^2-4\pi\theta+\theta^2}\right\},\{x,-1,1\},\{\theta,-2\pi,2\pi\}\right]$$





In[1]:= Manipulate[ContourPlot3D[ $\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{\left(\theta r - \left(2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right)\right)}{\theta r - \left(2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2}\right)}$ ,  
 $\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}, \{r, -1, 1\}, \{\eta, -1, 1\}$ ]

Out[1]=



Power: Infinite expression  $\frac{1}{0.}$  encountered.

Power: Infinite expression  $\frac{1}{0.}$  encountered.

Infinity: Indeterminate expression 0.  $\pi$  ComplexInfinity encountered.

Power: Infinite expression  $\frac{1}{0.}$  encountered.

General: Further output of Power::infy will be suppressed during this calculation.

Infinity: Indeterminate expression 0.  $\pi$  ComplexInfinity encountered.

Infinity: Indeterminate expression 0.  $\pi$  ComplexInfinity encountered.

General: Further output of Infinity::indet will be suppressed during this calculation.

$$\text{Solve}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} == \frac{\left(\theta r - \left(2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right)\right)}{\theta r - \left(2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2}\right)}, \eta\right]$$

{{}}

$$\text{Solve}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} == \frac{\theta r - \left(2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2}\right)}{\left(\theta r - \left(2 \pi r - 2 \pi \frac{2 \pi r - r \theta}{2 \pi}\right)\right)}, \theta\right]$$

Power::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

{}

$$(\theta r - (2 \pi r - 2 \pi x))$$

$$\text{Solve}\left[(4/3) \pi (r)^3 - (4/3) \pi \left(\frac{2 \pi r - r \theta}{2 \pi}\right)^3 ==\right.$$

$$\left. (4/3) \pi (r)^3 - (4/3) \pi \left(\frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - r \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}}{2 \pi}\right)^3, \theta\right]$$

$$\left\{\{\theta \rightarrow 2 \pi\}, \left\{\theta \rightarrow 2 \pi - \sqrt{2 (3 - i \sqrt{3})} \pi\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{2 (3 - i \sqrt{3})} \pi\right\}, \right. \\ \left. \left\{\theta \rightarrow 2 \pi - \sqrt{2 (3 + i \sqrt{3})} \pi\right\}, \left\{\theta \rightarrow 2 \pi + \sqrt{2 (3 + i \sqrt{3})} \pi\right\}\right\}$$

$$(4/3) \pi (r)^3 - (4/3) \pi \left(\frac{2 \pi r - r \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}}{2 \pi}\right)^3$$

$$(4/3) \pi (r)^3 - (4/3) \pi \left(\frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - r \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}}{2 \pi}\right)^3$$

$$(4/3) \pi \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^3 - (4/3) \pi \left(\frac{2 \pi r - r \theta}{2 \pi}\right)^3$$

$$\text{ContourPlot3D}\left[\left\{-\left(2\sqrt{2}\sqrt{\left(2\pi^4\eta^2\sin[\beta]^2+\frac{\pi^4\eta^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}+\frac{4\pi^5\eta^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2}+\frac{\pi^4\eta^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)}\right)/\left(\sqrt{-4\pi\theta^3+\theta^4+64\pi^4\sin[\beta]^2}\right),\right.\\ \left.\left(2\sqrt{2}\sqrt{\left(2\pi^4\eta^2\sin[\beta]^2+\frac{\pi^4\eta^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}+\frac{4\pi^5\eta^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta^2}+\frac{\pi^4\eta^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)}\right)/\left(\sqrt{-4\pi\theta^3+\theta^4+64\pi^4\sin[\beta]^2}\right)\right\},\{\eta,-1,1\},\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$$

$$\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}$$

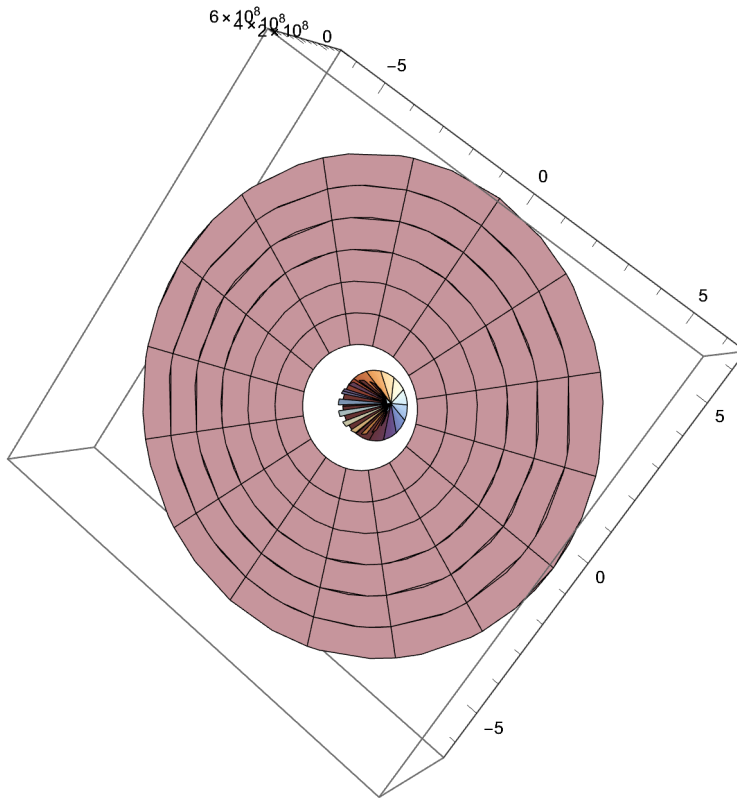
$$\text{Solve}\left[\frac{r\sqrt{4\pi+\mathfrak{i}\text{ArcSinh}\left[\mathrm{e}^{\mathfrak{i}\theta}-\text{Cos}[\theta]\right]}\sqrt{-\mathfrak{i}\text{ArcSinh}\left[\mathrm{e}^{\mathfrak{i}\theta}-\text{Cos}[\theta]\right]}}{2\pi}==\frac{\sqrt{r}\sqrt{1-\frac{(v)^2}{c^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}}\sqrt{4\pi r-r\theta}}{2\pi},v\right]$$

$$\left\{\left\{v\rightarrow-\left(1.\sqrt{\left(-1.12941\times10^{18}\theta+8.98755\times10^{16}\theta^2+8.98755\times10^{16}\text{ArcSinh}\left[\mathrm{e}^{\mathfrak{i}\theta}-1.\text{Cos}[\theta]\right]^2-(0.+1.12941\times10^{18}\mathfrak{i})\text{ArcSinh}\left[\mathrm{e}^{(0.+1.\mathfrak{i})\theta}-1.\text{Cos}[\theta]\right]\right)}\right)/\left(\sqrt{\left(-12.5664\theta+\theta^2+\text{ArcSinh}\left[\mathrm{e}^{\mathfrak{i}\theta}-1.\text{Cos}[\theta]\right]^2-(0.+12.5664\mathfrak{i})\text{ArcSinh}\left[\mathrm{e}^{(0.+1.\mathfrak{i})\theta}-1.\text{Cos}[\theta]\right]\right)}\right)\right\},\\ \left\{v\rightarrow\left(\sqrt{\left(-1.12941\times10^{18}\theta+8.98755\times10^{16}\theta^2+8.98755\times10^{16}\text{ArcSinh}\left[\mathrm{e}^{\mathfrak{i}\theta}-1.\text{Cos}[\theta]\right]^2-(0.+1.12941\times10^{18}\mathfrak{i})\text{ArcSinh}\left[\mathrm{e}^{(0.+1.\mathfrak{i})\theta}-1.\text{Cos}[\theta]\right]\right)}\right)/\left(\sqrt{\left(-12.5664\theta+\theta^2+\text{ArcSinh}\left[\mathrm{e}^{\mathfrak{i}\theta}-1.\text{Cos}[\theta]\right]^2-(0.+12.5664\mathfrak{i})\text{ArcSinh}\left[\mathrm{e}^{(0.+1.\mathfrak{i})\theta}-1.\text{Cos}[\theta]\right]\right)}\right)\right\}\right\}$$

```

RevolutionPlot3D[ $\left(\sqrt{\left(-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 8.987551787368176 \cdot \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right]^2 - \left(\theta. + 1.1294090667581472 \cdot \text{ArcSinh}\left[e^{(\theta. + 1. \cdot \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right] - 1. \cdot \cos[\theta]\right])}\right] \right) / \left(\sqrt{\left(-12.566370614359172 \cdot \theta + \theta^2 + \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right]^2 - \left(\theta. + 12.566370614359172 \cdot \text{ArcSinh}\left[e^{(\theta. + 1. \cdot \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right] - 1. \cdot \cos[\theta]\right])}\right] \right)}\right), \{\theta, -2 \pi, 2 \pi\}$ ]

```



```

Export["splat.3ds",
  SphericalPlot3D[ $\frac{1}{c^2} \sqrt{1 - \left( \left( \sqrt{-1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + 8.987551787368176 \cdot 10^{16} \theta^2 + 8.987551787368176 \cdot 10^{16} \operatorname{ArcSinh}[e^{\frac{1}{2} \theta} - 1. \cos[\theta]} \right)^2 - (0. + 1.1294090667581472 \cdot 10^{18} i) \operatorname{ArcSinh}[e^{(\theta. + 1. i) \theta} - 1. \cos[\theta]} \right)} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + \operatorname{ArcSinh}[e^{\frac{1}{2} \theta} - 1. \cos[\theta]} \right)^2 - (0. + 12.566370614359172 i) \operatorname{ArcSinh}[e^{(\theta. + 1. i) \theta} - 1. \cos[\theta]} \right)} \right)^2 \right) \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}] ]$ 
```

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

ComputationalGeometry`Methods`SpatialSearch::spoutbounds : -- Message text not found --  
 ({-9.93738, -1.4586})

ComputationalGeometry`Methods`SpatialSearch::spoutbounds : -- Message text not found --  
 ({-9.49652, 0.915534})

ComputationalGeometry`Methods`SpatialSearch::spoutbounds : -- Message text not found --  
 ({-10.6043, -1.4025})

General::stop : Further output of ComputationalGeometry`Methods`SpatialSearch::spoutbounds will be suppressed during this calculation. >>

splat.3ds

SphericalPlot3D[  

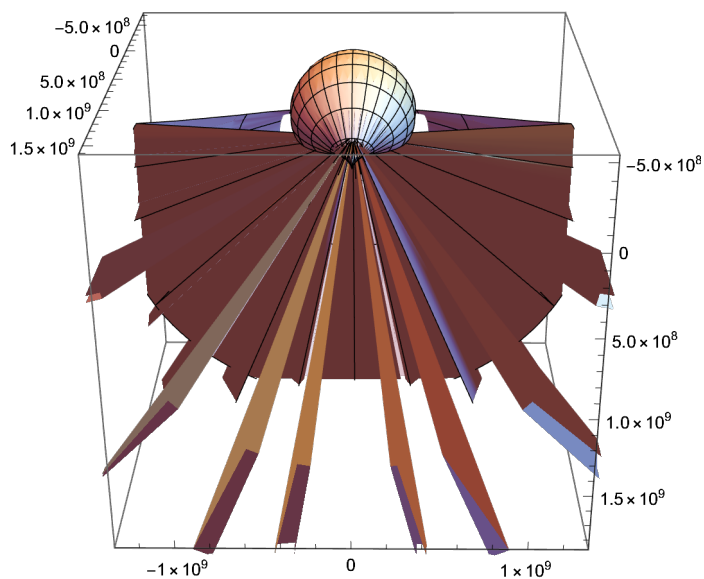
$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right) + 8.987551787368176 \cdot 10^{16} \theta^2 + \right.} \right.$$
  

$$8.987551787368176 \cdot 10^{16} \operatorname{ArcSinh}\left[ e^{\pm \theta} - 1. \cdot \cos[\theta] \right]^2 -$$
  

$$\left. \left( \theta. + 1.1294090667581472 \cdot 10^{18} \right) \operatorname{ArcSinh}\left[ e^{(\theta. + 1. \cdot \pm) \theta} - 1. \cdot \cos[\theta] \right] \right) \Bigg) /$$
  

$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \theta^2 + \operatorname{ArcSinh}\left[ e^{\pm \theta} - 1. \cdot \cos[\theta] \right]^2 - \right.} \right.$$
  

$$\left. \left( \theta. + 12.566370614359172 \cdot \pm \right) \operatorname{ArcSinh}\left[ e^{(\theta. + 1. \cdot \pm) \theta} - 1. \cdot \cos[\theta] \right] \right) \Bigg),$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + 8.987551787368176 \cdot 10^{16} \right.} \right.$$

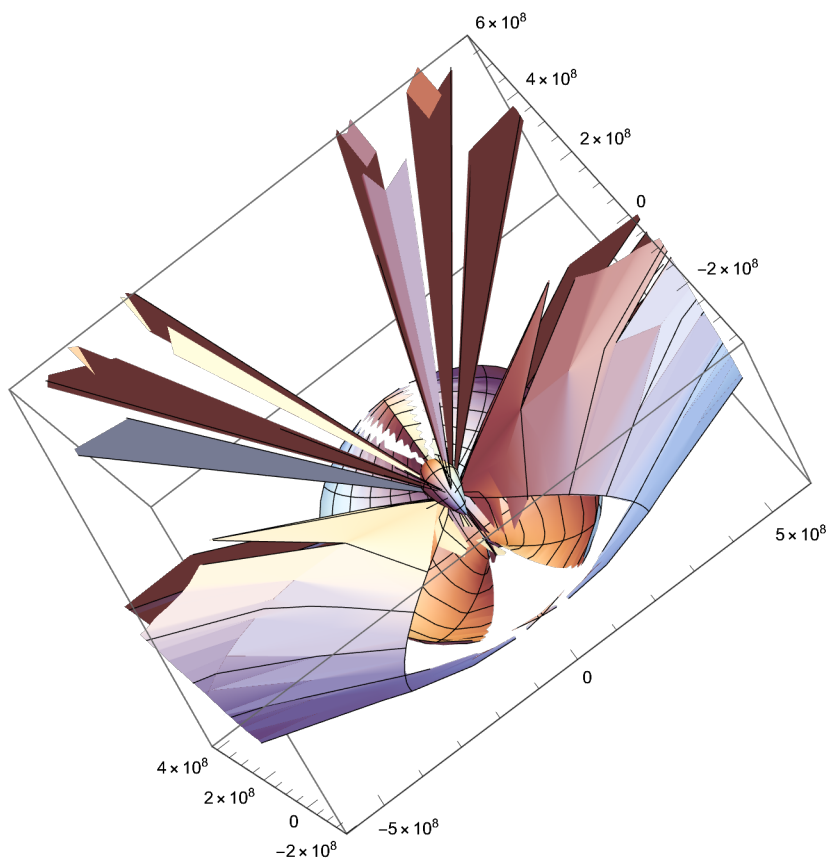
$$\left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 8.987551787368176 \cdot 10^{16} \operatorname{ArcSinh}\left[ e^{\pm \theta} - 1. \cdot \cos[\theta] \right]^2 - \right.$$

$$\left. \left. \left( \theta. + 1.1294090667581472 \cdot 10^{18} i \right) \operatorname{ArcSinh}\left[ e^{(\theta. + 1. \cdot i) \theta} - 1. \cdot \cos[\theta] \right] \right) \right) /$$

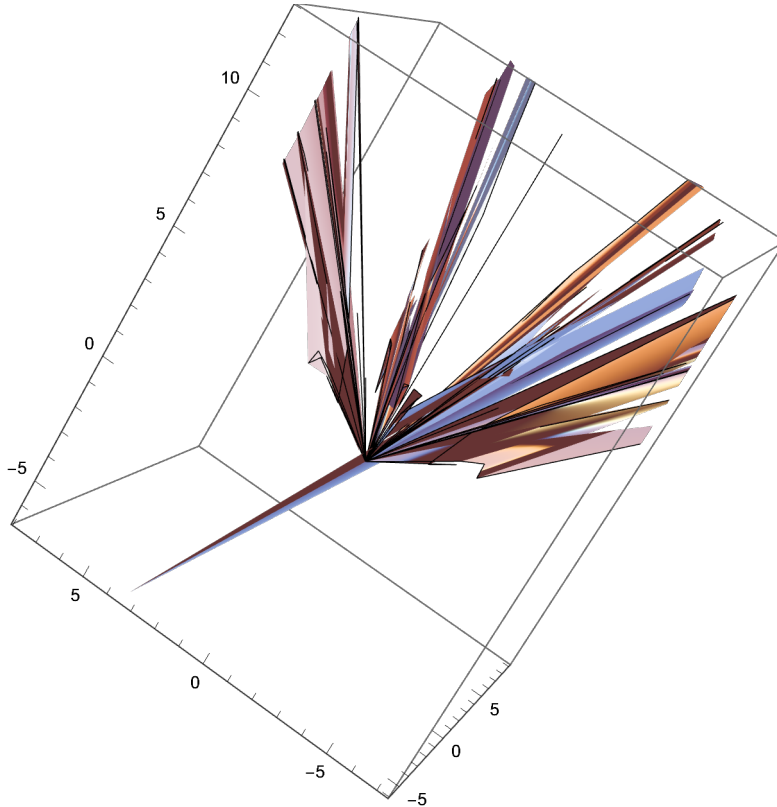
$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \theta^2 + \operatorname{ArcSinh}\left[ e^{\pm \theta} - 1. \cdot \cos[\theta] \right]^2 - \right.} \right.$$

$$\left. \left. \left( \theta. + 12.566370614359172 \cdot i \right) \operatorname{ArcSinh}\left[ e^{(\theta. + 1. \cdot i) \theta} - 1. \cdot \cos[\theta] \right] \right) \right),$$

$$\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$

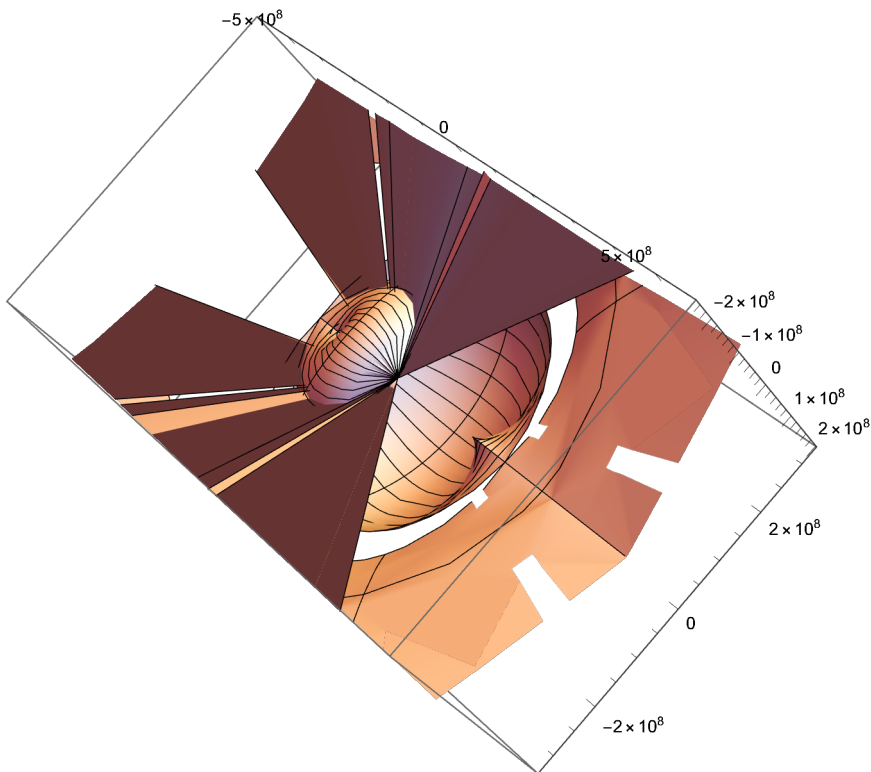


$$\text{SphericalPlot3D}\left[\frac{\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} (\theta) + 8.987551787368176 \cdot 10^{16} (\theta)^2 + 8.987551787368176 \cdot 10^{16} \text{ArcSinh}\left[e^{i\theta} - 1. \cos[\theta]\right]^2 - (0. + 1.1294090667581472 \cdot 10^{18} i) \text{ArcSinh}\left[e^{(0. + 1. \cdot i) \theta} - 1. \cos[\theta]\right]\right)}{\left(\sqrt{\left(-12.566370614359172 \cdot \theta + \theta^2 + \text{ArcSinh}\left[e^{i\theta} - 1. \cos[\theta]\right]^2 - (0. + 12.566370614359172 \cdot i) \text{ArcSinh}\left[e^{(0. + 1. \cdot i) \theta} - 1. \cos[\theta]\right] - 1. \cos\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]}\right)}\right], \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$

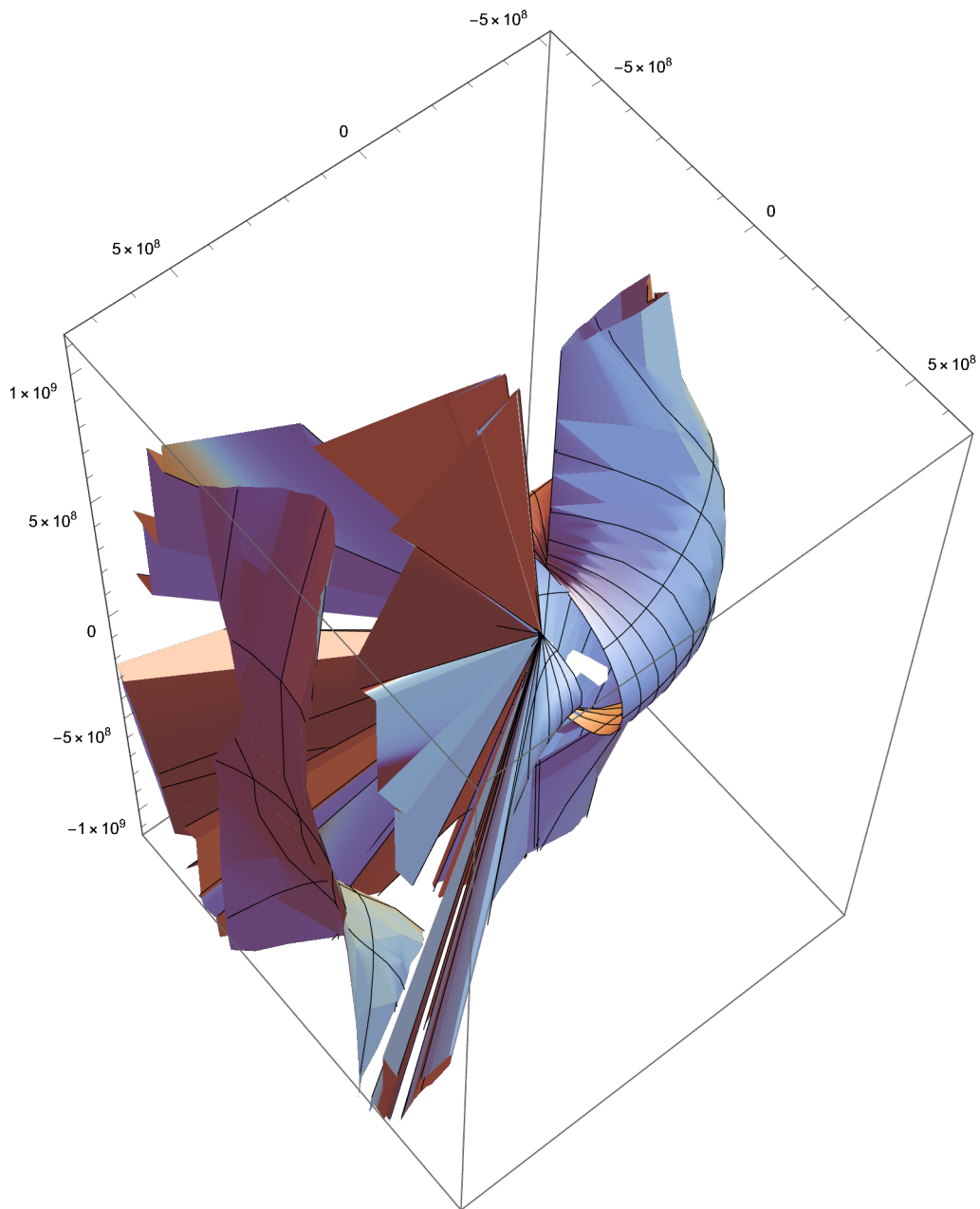




$$\text{SphericalPlot3D}\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} (\theta) + 8.987551787368176 \cdot 10^{16} (\theta)^2 + 8.987551787368176 \cdot 10^{16} \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right]^2 - (\theta. + 1.1294090667581472 \cdot 10^{18} i) \text{ArcSinh}\left[e^{(\theta. + 1. \cdot i) \theta} - 1. \cdot \cos[\theta]\right]\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot \theta + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right]^2 - (\theta. + 12.566370614359172 \cdot i) \text{ArcSinh}\left[e^{(\theta. + 1. \cdot i) \theta} - 1. \cdot \cos[\theta]\right]\right)}\right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$



$$\text{SphericalPlot3D}\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} (\theta) + 8.987551787368176 \cdot 10^{16} (\theta)^2 + 8.987551787368176 \cdot 10^{16} \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right]^2 - (\theta. + 1.1294090667581472 \cdot 10^{18} i) \text{ArcSinh}\left[e^{(\theta. + 1. \cdot i) \theta} - 1. \cdot \cos[\theta]\right]\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot \theta + 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + \text{ArcSinh}\left[e^{\pm \theta} - 1. \cdot \cos[\theta]\right]^2 - (\theta. + 12.566370614359172 \cdot i) \text{ArcSinh}\left[e^{(\theta. + 1. \cdot i) \theta} - 1. \cdot \cos[\theta]\right]\right)}\right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$



$$\text{Solve}\left[\left[\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} + 8.987551787368176 \cdot 10^{16} \frac{\left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2}{r^2} + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}{\left(\sqrt{-12.566370614359172 \cdot 10^{16} \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} + \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2} + 39.47841760435743 \sin[\beta]^2\right)}\right] = (99.0 \cdot (10^8)), r\right]$$

$$\text{Solve}\left[\eta = \frac{1}{4 \pi^2} \left(\sqrt{64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta \sqrt{r^2 (4 \pi - \theta) \theta}}\right), r\right]$$

$$\text{Solve}\left[\eta = \frac{1}{4 \pi^2} \left(\sqrt{64 \pi^4 r^2 - \frac{256 \pi^5 r^2}{4 \pi - \theta} + 16 \pi^3 r^2 \theta + 4 \pi^2 r^2 \theta^2 + r^2 \theta^4 + 16 \pi^3 r \sqrt{r^2 (4 \pi - \theta) \theta} - \frac{64 \pi^4 r \sqrt{r^2 (4 \pi - \theta) \theta}}{4 \pi - \theta} + 8 \pi^2 \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta \sqrt{r^2 (4 \pi - \theta) \theta}}\right), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta}}{4 \theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)} - \right.\right.$$

$$\left.\frac{1}{2} \sqrt{-\frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right.$$

$$\left.\frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right.$$

$$\left.\frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right.$$

$$\left.\frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right.$$

$$\begin{aligned}
& \frac{3\,145\,728\,\pi^{14}}{(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)^2} + \\
& \frac{4\,194\,304\,\pi^{15}}{\theta(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)^2} + \\
& \frac{786\,432\,\pi^{13}\,\theta}{(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)^2} - \\
& \frac{65\,536\,\pi^{12}\,\theta^2}{(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)^2} - \\
& \frac{2048\,\pi^7}{-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7} - \\
& \frac{512\,\pi^7\,\eta^2}{-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7} + \\
& \frac{4096\,\pi^8}{\theta(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)} + \\
& \frac{256\,\pi^6\,\theta}{-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7} + \\
& \frac{640\,\pi^6\,\eta^2\,\theta}{-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7} - \\
& \frac{256\,\pi^5\,\eta^2\,\theta^2}{-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7} + \\
& \frac{32\,\pi^4\,\eta^2\,\theta^3}{-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7} \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{512\,\pi^7\,\eta^2}{1024\,\pi^7 - 256\,\pi^6\,\theta - 16\,\pi^4\,\theta^3 + 32\,\pi^3\,\theta^4 - 24\,\pi^2\,\theta^5 + 8\,\pi\,\theta^6 - \theta^7} - \right.} \\
& \frac{640\,\pi^6\,\eta^2\,\theta}{1024\,\pi^7 - 256\,\pi^6\,\theta - 16\,\pi^4\,\theta^3 + 32\,\pi^3\,\theta^4 - 24\,\pi^2\,\theta^5 + 8\,\pi\,\theta^6 - \theta^7} + \\
& \frac{256\,\pi^5\,\eta^2\,\theta^2}{1024\,\pi^7 - 256\,\pi^6\,\theta - 16\,\pi^4\,\theta^3 + 32\,\pi^3\,\theta^4 - 24\,\pi^2\,\theta^5 + 8\,\pi\,\theta^6 - \theta^7} - \\
& \frac{32\,\pi^4\,\eta^2\,\theta^3}{1024\,\pi^7 - 256\,\pi^6\,\theta - 16\,\pi^4\,\theta^3 + 32\,\pi^3\,\theta^4 - 24\,\pi^2\,\theta^5 + 8\,\pi\,\theta^6 - \theta^7} + \\
& \left. \frac{3\,145\,728\,\pi^{14}}{(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)^2} - \right. \\
& \left. \frac{4\,194\,304\,\pi^{15}}{\theta(-1024\,\pi^7 + 256\,\pi^6\,\theta + 16\,\pi^4\,\theta^3 - 32\,\pi^3\,\theta^4 + 24\,\pi^2\,\theta^5 - 8\,\pi\,\theta^6 + \theta^7)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{3 \pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{786432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{65536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} - \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \left( 2 \pi^4 \left( -4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - 640 \pi^2 \eta^2 \theta^2 + \right. \right. \\
& \quad \left. \left. 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4 \right) \right) / \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - \right. \right. \\
& \quad \left. \left. 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) - \left( \pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta} \right. \\
& \quad \left( - \frac{\pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \right. \\
& \quad \left( 4 \pi^4 \left( -4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - \right. \right. \\
& \quad \left. \left. 640 \pi^2 \eta^2 \theta^2 + 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4 \right) \right) / \\
& \quad \left. \left. \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) \right) \right) / \\
& \left( 4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right. \\
& \quad \left. \sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right.} \right.
\end{aligned}$$

$$\left\{ r \rightarrow - \frac{1}{2} \sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \frac{640 \pi^6 \eta^2 \theta}{- \frac{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7}{256 \pi^5 \eta^2 \theta^2} + \frac{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7}{32 \pi^4 \eta^2 \theta^3} - \frac{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7}{3145728 \pi^{14}} \right. \right. \\ \left. \left. + \frac{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2}{4194304 \pi^{15}} + \frac{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2}{786432 \pi^{13} \theta} - \frac{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2}{65536 \pi^{12} \theta^2} - \frac{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2}{2048 \pi^7} \right. \\ \left. - \frac{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7}{512 \pi^7 \eta^2} + \frac{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7}{4096 \pi^8} \right. \\ \left. + \frac{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)}{256 \pi^6 \theta} + \frac{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7}{640 \pi^6 \eta^2 \theta} - \frac{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7}{256 \pi^5 \eta^2 \theta^2} \right. \\ \left. + \frac{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7}{32 \pi^4 \eta^2 \theta^3} \right) \Bigg\},$$

$$\begin{aligned}
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right.} \\
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} -
\end{aligned}$$

$$\begin{aligned}
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{3 \, 145 \, 728 \pi^{14}}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} - \\
& \frac{4 \, 194 \, 304 \pi^{15}}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \\
& \frac{3 \pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{4 \theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} - \\
& \frac{786 \, 432 \pi^{13} \theta}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \\
& \frac{65 \, 536 \pi^{12} \theta^2}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{4096 \pi^8}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)} - \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \left( 2 \pi^4 (-4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - 640 \pi^2 \eta^2 \theta^2 + \right. \\
& \quad \left. 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4) \right) / \left( \theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - \right. \\
& \quad \left. 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7) \right) - \left( \pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta} \right. \\
& \quad \left( - \frac{\pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \right. \\
& \quad \left. (4 \pi^4 (-4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - \right. \\
& \quad \left. 640 \pi^2 \eta^2 \theta^2 + 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4)) / \right)
\end{aligned}$$



$$\begin{aligned}
& \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) \Big) \Big) / \\
& \left( 4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right. \\
& \sqrt{\left( -\frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right. \\
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{3145728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{4194304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{786432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{65536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} +
\end{aligned}$$

$$\left. \left. \left. \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \right) \right) \right\},$$

$$\left\{ r \rightarrow - \frac{\pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta}}{4 \theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)} + \right.$$

$$\frac{1}{2}$$

$$\sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right.$$

$$\frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} -$$

$$\frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} +$$

$$\frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} -$$

$$\frac{3145728 \pi^{14}}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} +$$

$$\frac{4194304 \pi^{15}}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} +$$

$$\frac{786432 \pi^{13} \theta}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} -$$

$$\frac{65536 \pi^{12} \theta^2}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} -$$

$$\frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} -$$

$$\frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} +$$

$$\frac{4096 \pi^8}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)} +$$

$$\frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} +$$

$$\frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} -$$

$$\frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} +$$

$$\begin{aligned}
& \left. \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \right) - \\
& \frac{1}{2} \sqrt{\left( \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right.} \\
& \quad \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \quad \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \quad \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \quad \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \quad \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \frac{3 \pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \quad \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \quad \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \quad \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} - \\
& \quad \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \quad \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \quad \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \quad \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} -
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \pi^4 \left( -4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - 640 \pi^2 \eta^2 \theta^2 + \right. \right. \\
& \quad \left. \left. 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4 \right) \right) / \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - \right. \right. \\
& \quad \left. \left. 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) + \left( \pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta} \right. \\
& \quad \left( - \frac{\pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \right. \\
& \quad \left( 4 \pi^4 \left( -4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - \right. \right. \\
& \quad \left. \left. 640 \pi^2 \eta^2 \theta^2 + 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4 \right) \right) / \\
& \quad \left. \left. \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) \right) \right) / \\
& \left( 4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right. \\
& \quad \sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right. \\
& \quad \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \quad \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \quad \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \quad \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \quad \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \quad \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \quad \left. \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \begin{aligned}
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \right) \right) \right) \Bigg\}, \\
& \left\{ r \rightarrow - \frac{\pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta}}{4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \right. \\
& \frac{1}{2} \\
& \sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right. \\
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \left. \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \right)
\end{aligned}
\right\}$$

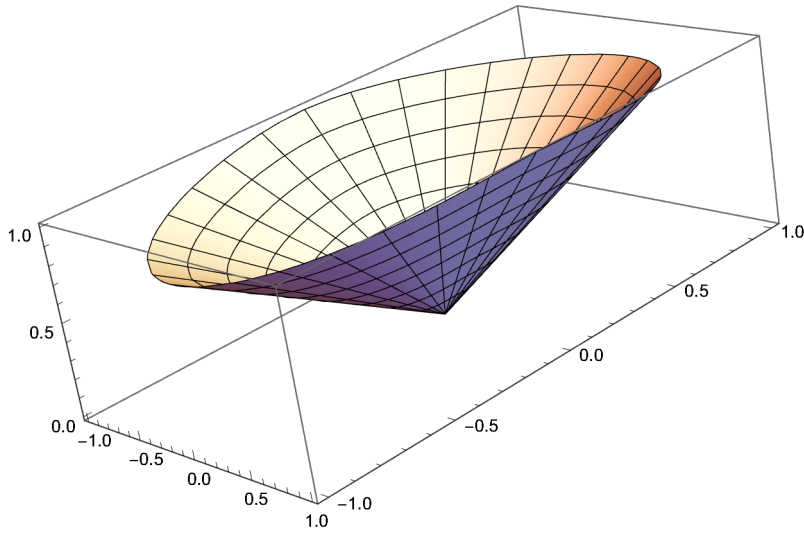
$$\begin{aligned}
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \Bigg) + \\
& \frac{1}{2} \sqrt{\left( \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right. \\
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{3 \pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} -
\end{aligned}$$

$$\begin{aligned}
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \left( 2 \pi^4 \left( -4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - 640 \pi^2 \eta^2 \theta^2 + \right. \right. \\
& \quad \left. \left. 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4 \right) \right) / \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - \right. \right. \\
& \quad \left. \left. 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) + \left( \pi^6 (2048 \pi - 512 \theta) \sqrt{(4 \pi - \theta) \theta} \right. \\
& \quad \left. - \frac{\pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \right. \\
& \quad \left. \left( 4 \pi^4 \left( -4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - \right. \right. \right. \\
& \quad \left. \left. \left. 640 \pi^2 \eta^2 \theta^2 + 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4 \right) \right) \right) / \\
& \quad \left. \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) \right) \Bigg) / \\
& \sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right. \\
& \quad \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \quad \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \quad \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \quad \frac{3145728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \frac{4194304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \quad \left. \frac{786432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \right)
\end{aligned}$$

$$\begin{aligned} & \frac{-}{\left(-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7\right)^2} \\ & \quad \frac{2048 \pi^7}{-} \\ & \quad \frac{-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7}{512 \pi^7 \eta^2} + \\ & \quad \frac{-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7}{4096 \pi^8} + \\ & \quad \frac{\theta\left(-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7\right)}{256 \pi^6 \theta} + \\ & \quad \frac{-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7}{640 \pi^6 \eta^2 \theta} - \\ & \quad \frac{-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7}{256 \pi^5 \eta^2 \theta^2} + \\ & \quad \frac{-1024 \pi^7+256 \pi^6 \theta+16 \pi^4 \theta^3-32 \pi^3 \theta^4+24 \pi^2 \theta^5-8 \pi \theta^6+\theta^7}{32 \pi^4 \eta^2 \theta^3} \Bigg) \Bigg) \Bigg) \Bigg\} \end{aligned}$$

$$\text{RevolutionPlot3D}\left[\frac{1}{2\pi}\left(\sqrt{\left(4\pi r^2\left(\frac{4\pi}{3}-(-4\pi^2+12\pi^2\sin[\beta]^2)\right)/\right.}\right.\right. \\ \left.\left.\left(6\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)+\right.\right. \\ \left.\left.\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)-\right. \\ \left.\left.r^2\left(\frac{4\pi}{3}-(-4\pi^2+12\pi^2\sin[\beta]^2)\right)/\left(6\left(-\pi^3+18\pi^3\sin[\beta]^2+\right.\right.\right. \\ \left.\left.\left.3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)+\frac{2}{3}\right.\right. \\ \left.\left.\left.\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)^2\right)\right)\right], \\ \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}]$$





$$\frac{2 \pi r - r \theta}{2 \pi}$$

$$\text{Solve}\left[\frac{2 \pi \left(2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \sqrt{\left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}\right)}{\theta^2} ==$$

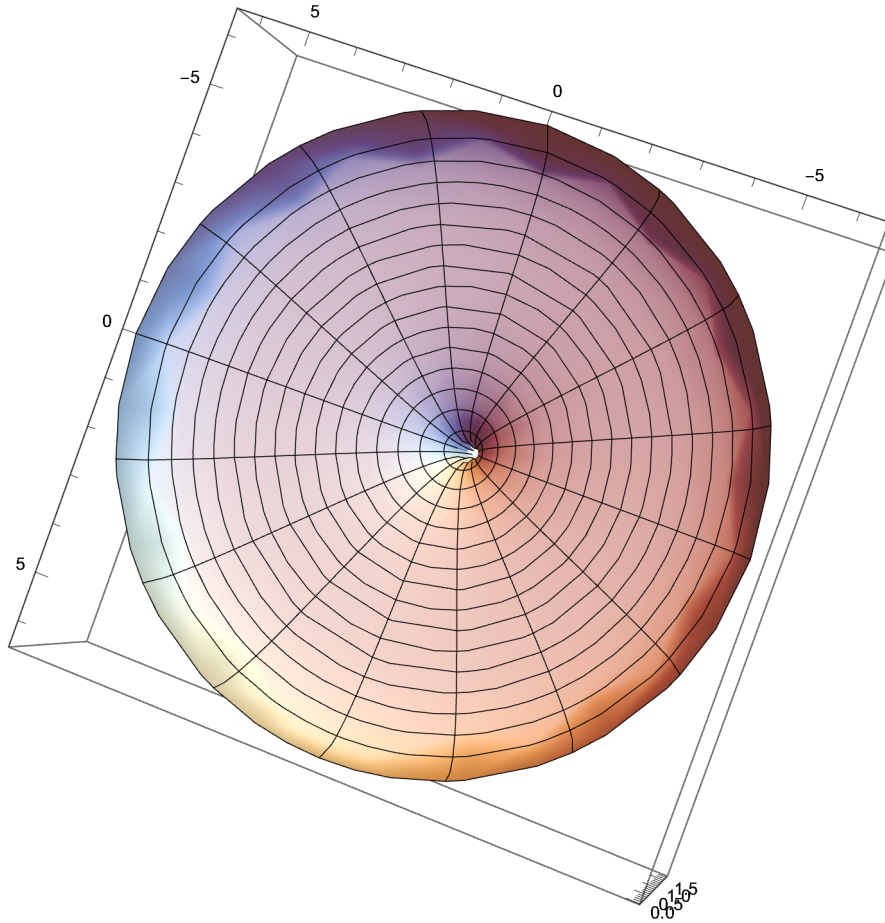
$$\frac{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 - 2 \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta}{2 \sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}, r]$$

$$\left\{\left\{r \rightarrow -\frac{1}{2} \sqrt{\left(4 - \frac{64 \pi^3}{(4 \pi - \theta)^3} + \frac{80 \pi^2}{(4 \pi - \theta)^2} - \frac{32 \pi}{4 \pi - \theta} - \frac{16 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^3} + \frac{4 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^2} + \frac{\sqrt{(4 \pi - \theta) \theta}}{4 \pi - \theta} + \frac{\sqrt{(4 \pi - \theta) \theta}}{\theta}\right)}\right\},$$

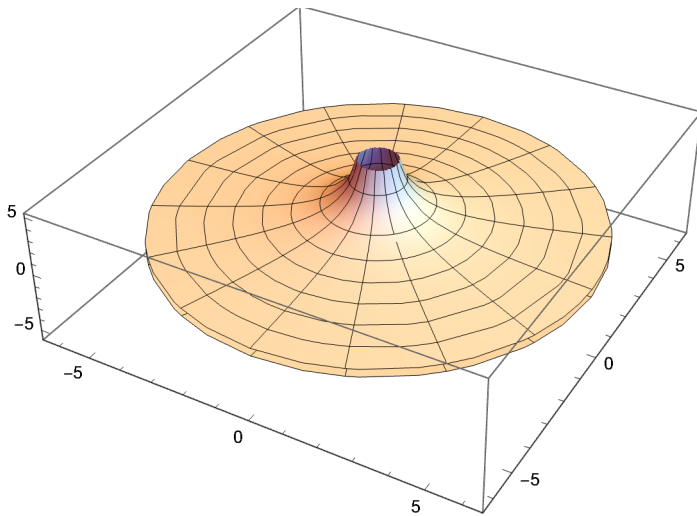
$$\left\{r \rightarrow \frac{1}{2} \sqrt{\left(4 - \frac{64 \pi^3}{(4 \pi - \theta)^3} + \frac{80 \pi^2}{(4 \pi - \theta)^2} - \frac{32 \pi}{4 \pi - \theta} - \frac{16 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^3} + \frac{4 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^2} + \frac{\sqrt{(4 \pi - \theta) \theta}}{4 \pi - \theta} + \frac{\sqrt{(4 \pi - \theta) \theta}}{\theta}\right)}\right\}}$$

RevolutionPlot3D[

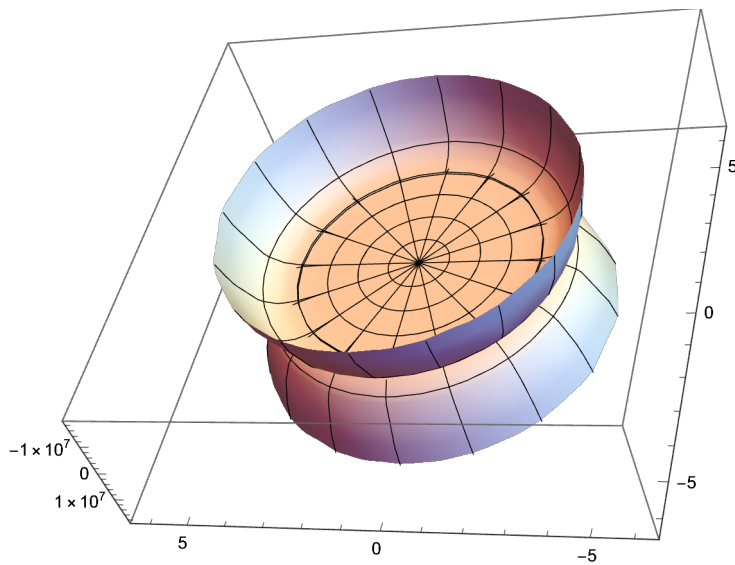
$$\frac{1}{2} \sqrt{\left(4 - \frac{64 \pi^3}{(4 \pi - \theta)^3} + \frac{80 \pi^2}{(4 \pi - \theta)^2} - \frac{32 \pi}{4 \pi - \theta} - \frac{16 \pi^2 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^3} + \frac{4 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)^2} + \frac{\sqrt{(4 \pi - \theta) \theta}}{4 \pi - \theta} + \frac{\sqrt{(4 \pi - \theta) \theta}}{\theta}\right)}, \{\theta, -2 \pi, 2 \pi\}]$$



$$\text{RevolutionPlot3D}\left[\frac{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi-\theta) \theta}}{(4 \pi-\theta) \theta}\right)^2 - 2 \left(\frac{2 \pi \sqrt{(4 \pi-\theta) \theta}}{(4 \pi-\theta) \theta}\right)^2 \theta}{2 \sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi-\theta) \theta}}{(4 \pi-\theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi-\theta) \theta}}{(4 \pi-\theta) \theta}\right)^2 \theta^2}}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$\text{RevolutionPlot3D}[\theta^{11}, \{\theta, -2 \pi, 2 \pi\}]$$



$$\text{Solve}\left[\frac{2 \pi \left(2 \pi r - 2 \pi \sqrt{(r)^2 - (\eta)^2}\right)}{\theta^2} == \frac{4 \pi (r)^2 - 2 (r)^2 \theta}{2 \sqrt{4 \pi (r)^2 \theta - (r)^2 \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\sqrt{\left(-\left(256 \pi^7 \eta^2 \theta^3\right) / \left(-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}\right) + 320 \pi^6 \eta^2 \theta^4\right)}\right.\right. \\ \left.\left.-\frac{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}}{\right.}\right\}$$

[illegible]

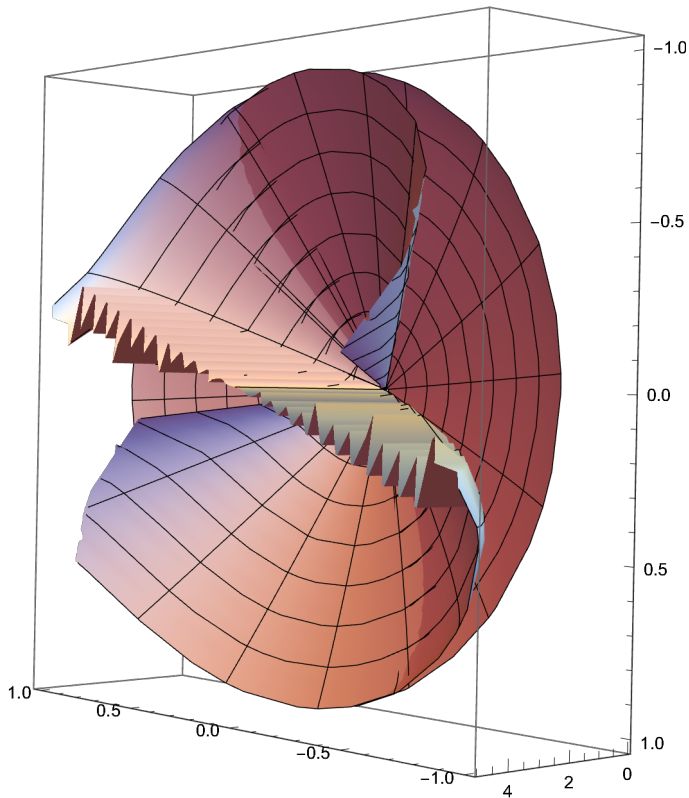
$$\begin{aligned}
& \frac{16 \pi^4 \eta^2 \theta^6}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \\
& \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \Bigg\} \Bigg\} \\
& \left( \sqrt{\left( -\frac{256 \pi^7 \eta^2 \theta^3}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \right. \right. \\
& \frac{320 \pi^6 \eta^2 \theta^4}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} - \\
& \frac{128 \pi^5 \eta^2 \theta^5}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \frac{16 \pi^4 \eta^2 \theta^6}{-1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10}} + \\
& \left. \left. \left( 128 \pi^6 \sqrt{256 \pi^5 \eta^4 \theta^3 - 448 \pi^4 \eta^4 \theta^4 + 304 \pi^3 \eta^4 \theta^5 - 100 \pi^2 \eta^4 \theta^6 + 16 \pi \eta^4 \theta^7 - \eta^4 \theta^8} \right) / \right. \right. \\
& \left. \left. \left( -1024 \pi^7 \theta^3 + 1280 \pi^6 \theta^4 - 512 \pi^5 \theta^5 + 80 \pi^4 \theta^6 - 32 \pi^3 \theta^7 + 24 \pi^2 \theta^8 - 8 \pi \theta^9 + \theta^{10} \right) \right) \right) \Bigg)^2
\end{aligned}$$

[illegible]

$$\text{Solve}\left[\frac{2 \pi \left(2 \pi r - 2 \pi \sqrt{(r)^2 - (\eta)^2}\right)}{\theta^2} == \frac{4 \pi (r)^2 - 2 (r)^2 \theta}{2 \sqrt{4 \pi (r)^2 \theta - (r)^2 \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{4 \pi^2 \sqrt{-\eta^2 + \frac{4 \pi^2}{(4 \pi - \theta) \theta}}}{\theta^2}} - \frac{8 \pi^3 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta^3}}{\sqrt{-\frac{2 \pi}{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} + \frac{\theta}{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{4 \pi^2 \sqrt{-\eta^2 + \frac{4 \pi^2}{(4 \pi - \theta) \theta}}}{\theta^2}} - \frac{8 \pi^3 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta^3}}{\sqrt{-\frac{2 \pi}{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} + \frac{\theta}{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{\frac{4 \pi^2 \sqrt{-\eta^2 + \frac{4 \pi^2}{(4 \pi - \theta) \theta}}}{\theta^2}} - \frac{8 \pi^3 \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta^3}}{\sqrt{-\frac{2 \pi}{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} + \frac{\theta}{\sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}}}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



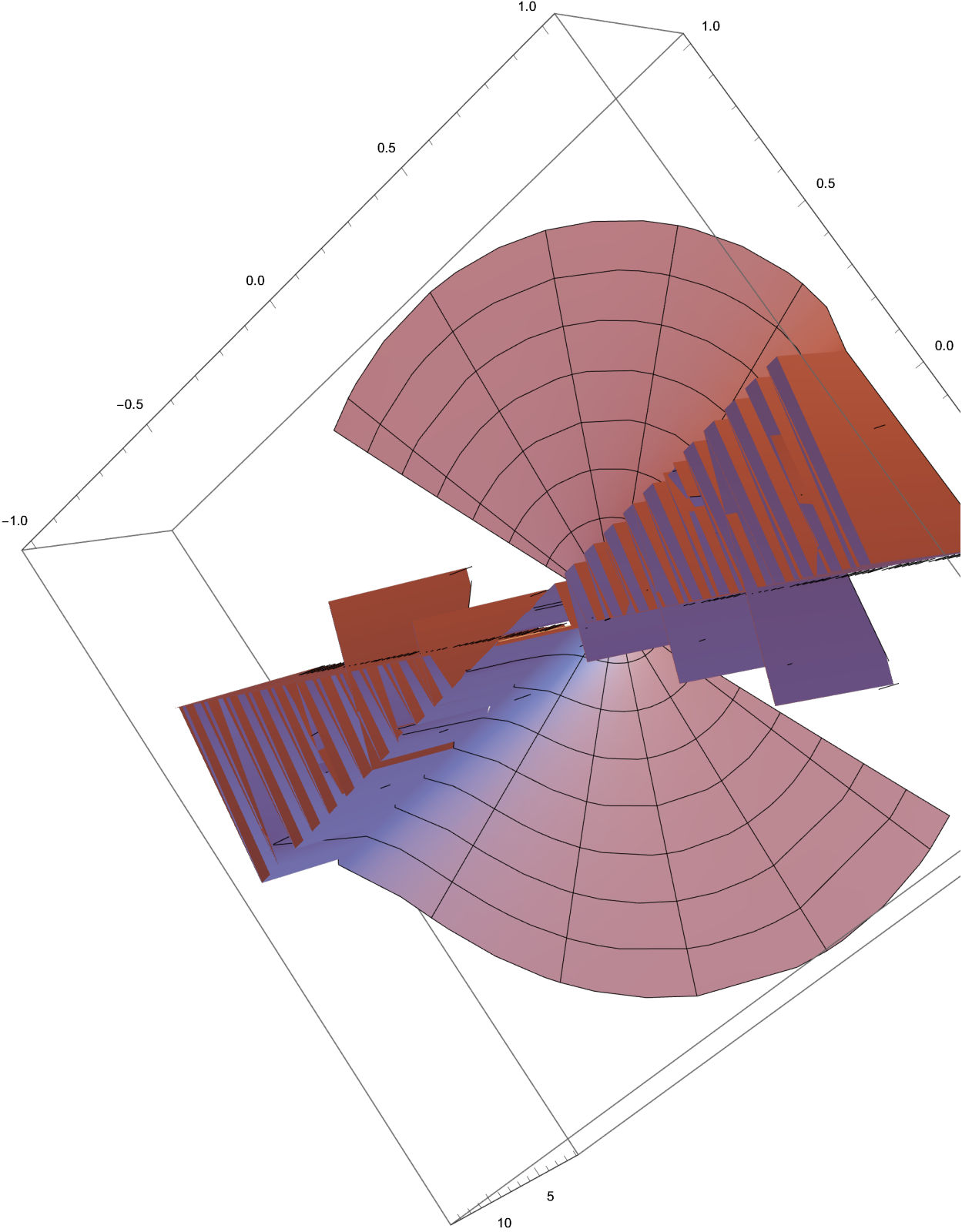
$$\text{Solve}\left[\frac{2 \pi \left(2 \pi r - 2 \pi \sqrt{\left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 - (\eta)^2}\right)}{\theta^2} ==$$

$$\frac{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 - 2 \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta}{2 \sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}, r]$$

$$\left\{\left\{r \rightarrow \frac{\theta^2 \left(\frac{4 \pi^2 \sqrt{-\eta^2 + \frac{4 \pi^2}{(4 \pi - \theta) \theta}}}{\theta^2} + \frac{-\frac{8 \pi^2}{4 \pi - \theta} + \frac{16 \pi^3}{(4 \pi - \theta) \theta}}{2 \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}\right)}{4 \pi^2}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{\theta^2 \left(\frac{4 \pi^2 \sqrt{-\eta^2 + \frac{4 \pi^2}{(4 \pi - \theta) \theta}}}{\theta^2} + \frac{-\frac{8 \pi^2}{4 \pi - \theta} + \frac{16 \pi^3}{(4 \pi - \theta) \theta}}{2 \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}\right)}{4 \pi^2}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2\}\right]$$





SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \left( \frac{4\pi}{3} + \left( (1 - i\sqrt{3}) (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right) / \right.} \right.$$

$$\left. \left( 12 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \right.$$

$$\left. \frac{1}{3} (1 + i\sqrt{3}) \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) +$$

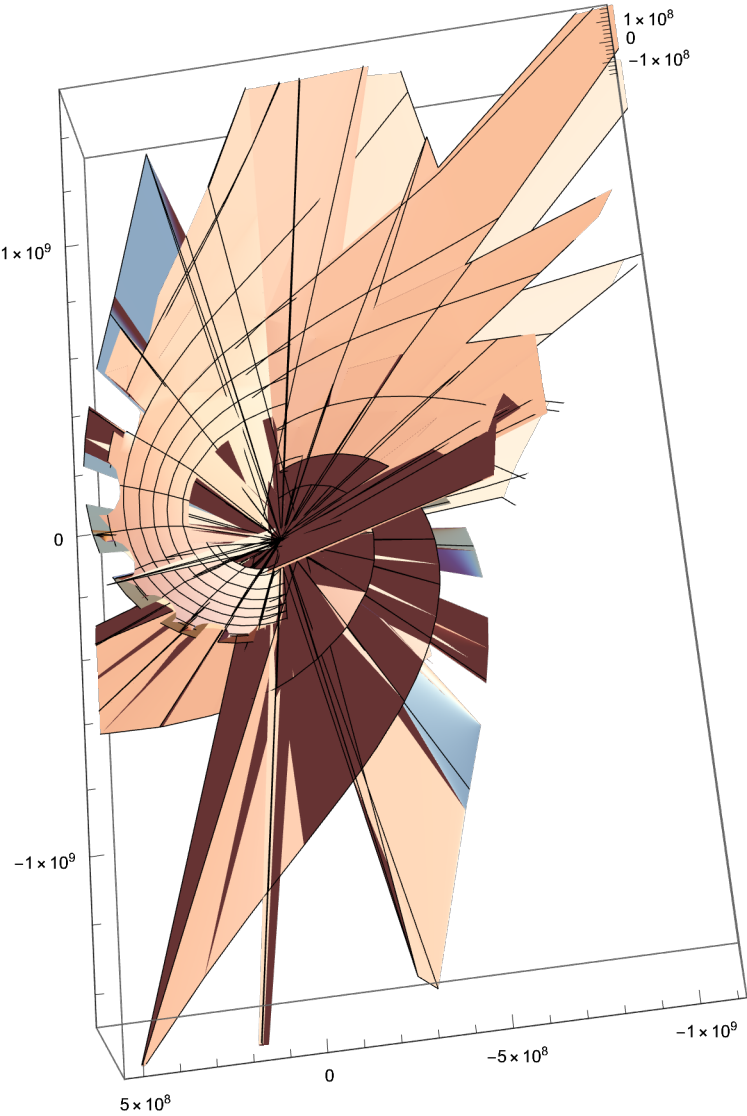
$$\left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \Bigg] /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \left( \frac{4\pi}{3} + \left( (1 - i\sqrt{3}) (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right) / \right.} \right.$$

$$\left. \left( 12 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \right.$$

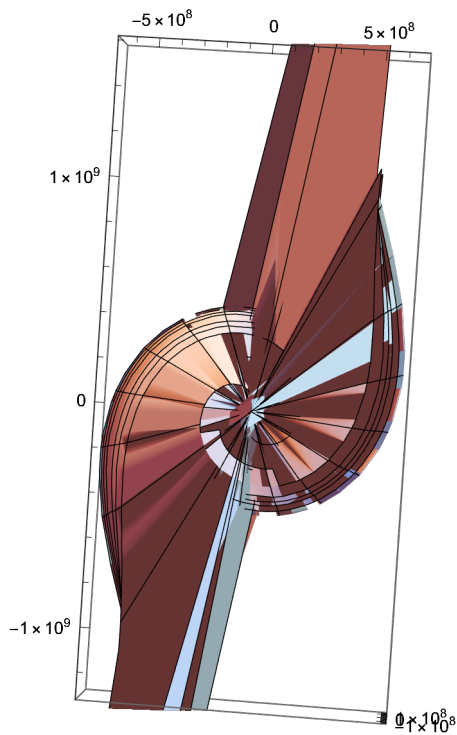
$$\left. \frac{1}{3} (1 + i\sqrt{3}) \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 +$$

$$39.47841760435743 \cdot \sin[\beta]^2 \Bigg] , \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \left( \frac{4\pi}{3} + \left( (1 - i\sqrt{3}) (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right) \right.} \right. \\
\left. \left( 12 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \right. \\
\left. \frac{1}{3} (1 + i\sqrt{3}) \right. \\
\left. \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
\left. \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) \right) / \\
\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right), \\
\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$



RevolutionPlot3D[
$$-\frac{\pi^6 (2048\pi - 512\theta) \sqrt{(4\pi - \theta)\theta}}{4\theta (-1024\pi^7 + 256\pi^6\theta + 16\pi^4\theta^3 - 32\pi^3\theta^4 + 24\pi^2\theta^5 - 8\pi\theta^6 + \theta^7)} -$$
  

$$\frac{1}{2} \sqrt{\left( -\frac{512\pi^7\eta^2}{1024\pi^7 - 256\pi^6\theta - 16\pi^4\theta^3 + 32\pi^3\theta^4 - 24\pi^2\theta^5 + 8\pi\theta^6 - \theta^7} + \right.$$

$$\begin{aligned}
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \Bigg) - \\
& \frac{1}{2} \sqrt{\left( \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right.} \\
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \left. \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{3145728 \pi^{14}}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} - \\
& \frac{4194304 \pi^{15}}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \\
& \frac{3 \pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{4 \theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} - \\
& \frac{786432 \pi^{13} \theta}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \\
& \frac{65536 \pi^{12} \theta^2}{(-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{4096 \pi^8}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)} - \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - (2 \pi^4 \\
& \quad (-4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - 640 \pi^2 \eta^2 \theta^2 + 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4)) / \\
& \quad (\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)) - \left( \pi^6 (2048 \pi - 512 \theta) \right. \\
& \quad \left. \sqrt{(4 \pi - \theta) \theta} \left( - \frac{\pi^{12} (2048 \pi - 512 \theta)^2 (4 \pi - \theta)}{\theta (-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7)^2} + \right. \right. \\
& \quad \left. \left. (4 \pi^4 (-4096 \pi^4 + 2048 \pi^3 \theta + 512 \pi^3 \eta^2 \theta - 256 \pi^2 \theta^2 - \right. \right. \\
& \quad \left. \left. 640 \pi^2 \eta^2 \theta^2 + 256 \pi \eta^2 \theta^3 - 32 \eta^2 \theta^4)) \right) / \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right) \Bigg) \Bigg) / \\
& \left( 4 \theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right) \right. \\
& \sqrt{\left( - \frac{512 \pi^7 \eta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \right. \\
& \frac{640 \pi^6 \eta^2 \theta}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} + \\
& \frac{32 \pi^4 \eta^2 \theta^3}{1024 \pi^7 - 256 \pi^6 \theta - 16 \pi^4 \theta^3 + 32 \pi^3 \theta^4 - 24 \pi^2 \theta^5 + 8 \pi \theta^6 - \theta^7} - \\
& \frac{3 \, 145 \, 728 \pi^{14}}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{4 \, 194 \, 304 \pi^{15}}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} + \\
& \frac{786 \, 432 \pi^{13} \theta}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{65 \, 536 \pi^{12} \theta^2}{\left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)^2} - \\
& \frac{2048 \pi^7}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{512 \pi^7 \eta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{4096 \pi^8}{\theta \left( -1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7 \right)} + \\
& \frac{256 \pi^6 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} + \\
& \frac{640 \pi^6 \eta^2 \theta}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} - \\
& \frac{256 \pi^5 \eta^2 \theta^2}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} +
\end{aligned}$$

$$\left. \frac{32 \pi^4 \eta^2 \theta^3}{-1024 \pi^7 + 256 \pi^6 \theta + 16 \pi^4 \theta^3 - 32 \pi^3 \theta^4 + 24 \pi^2 \theta^5 - 8 \pi \theta^6 + \theta^7} \right) \right) \right),$$

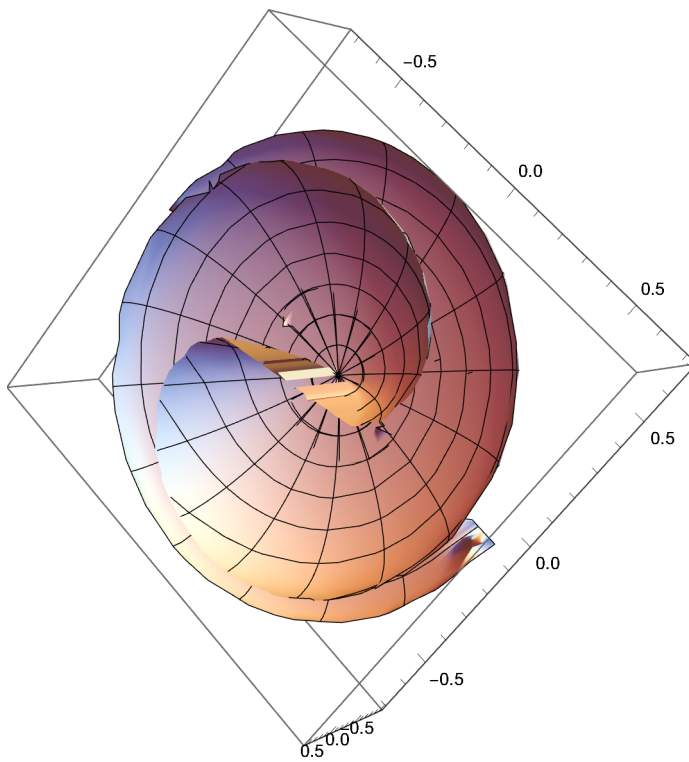
$\{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}$

Power::infy : Infinite expression  $\frac{1}{\sqrt{0.}}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{\sqrt{0.}}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{\sqrt{0.}}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>





$$\text{Solve}\left[\left(\left(\sqrt{\left(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2\right)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)\right) - \left(\sqrt{\left(3.5481432270250993 \cdot h^{18} - 1.1294090667581471 \cdot r z \theta + 8.987551787368176 \cdot z^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 \cdot h^2 - 12.566370614359172 \cdot r z \theta + z^2 \theta^2}\right) == \left(\sqrt{\left(8.987551787368176 \cdot r^2 \alpha^2 - 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2\right)}\right) / \left(\sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2}\right)\right), h]$$

$$\text{Solve}\left[\left(\left(\sqrt{\left(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2\right)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)\right) - \left(\sqrt{\left(3.5481432270250993 \cdot h^{18} - 1.1294090667581471 \cdot r z \theta + 8.987551787368176 \cdot z^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 \cdot h^2 - 12.566370614359172 \cdot r z \theta + z^2 \theta^2}\right) == \left(\sqrt{\left(8.987551787368176 \cdot r^2 \alpha^2 - 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2\right)}\right) / \left(\sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2}\right)\right), h]$$

$$\left\{\left\{h \rightarrow -\left(1. \sqrt{\left(1.19252 \times 10^{104} r z \theta^3 - 1.89795 \times 10^{103} r z \theta^4 - 9.48973 \times 10^{102} z^2 \theta^4 + 7.55169 \times 10^{101} r z \theta^5 + 1.51034 \times 10^{102} z^2 \theta^5 - 6.00944 \times 10^{100} z^2 \theta^6 - 7.49279 \times 10^{104} r z \theta^2 \sin[\beta]^2 + 5.96258 \times 10^{103} r z \theta^3 \sin[\beta]^2 + 5.96258 \times 10^{103} z^2 \theta^3 \sin[\beta]^2 - 4.74487 \times 10^{102} z^2 \theta^4 \sin[\beta]^2 + 1.17697 \times 10^{105} r z \theta \sin[\beta]^4 - 9.36599 \times 10^{103} z^2 \theta^2 \sin[\beta]^4 + \left(3.01504 \times 10^{69} r z \theta^2 \sqrt{\left(8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2\right)} \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}\right) / \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}\right) - \left(\sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2}\right) -$$

$$\begin{aligned} & \left( 2.3993 \times 10^{68} r z \vartheta^3 \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right. \right. \\ & \quad \left. \left. 1.79751 \times 10^{17} r z \alpha \vartheta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \vartheta + \right. \right. \\ & \quad \left. \left. 8.98755 \times 10^{16} z^2 \vartheta^2 \right) \sqrt{-12.5664 \vartheta + \vartheta^2 + 39.4784 \operatorname{Sin}[\beta]^2} \right. \\ & \quad \left. \sqrt{-1.12941 \times 10^{18} \vartheta + 8.98755 \times 10^{16} \vartheta^2 + 3.54814 \times 10^{18} \operatorname{Sin}[\beta]^2} \right) / \\ & \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \vartheta + z \delta^2 \eta^2 \vartheta + z^2 \vartheta^2} \right) - \\ & \left( 4.57582 \times 10^{68} z^2 \vartheta^3 \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right. \right. \\ & \quad \left. \left. 1.79751 \times 10^{17} r z \alpha \vartheta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \vartheta + \right. \right. \\ & \quad \left. \left. 8.98755 \times 10^{16} z^2 \vartheta^2 \right) \sqrt{-12.5664 \vartheta + \vartheta^2 + 39.4784 \operatorname{Sin}[\beta]^2} \right. \\ & \quad \left. \sqrt{-1.12941 \times 10^{18} \vartheta + 8.98755 \times 10^{16} \vartheta^2 + 3.54814 \times 10^{18} \operatorname{Sin}[\beta]^2} \right) / \\ & \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \vartheta + z \delta^2 \eta^2 \vartheta + z^2 \vartheta^2} \right) + \\ & \left( 3.64132 \times 10^{67} z^2 \vartheta^4 \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right. \right. \\ & \quad \left. \left. 1.79751 \times 10^{17} r z \alpha \vartheta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \vartheta + \right. \right. \\ & \quad \left. \left. 8.98755 \times 10^{16} z^2 \vartheta^2 \right) \sqrt{-12.5664 \vartheta + \vartheta^2 + 39.4784 \operatorname{Sin}[\beta]^2} \right. \\ & \quad \left. \sqrt{-1.12941 \times 10^{18} \vartheta + 8.98755 \times 10^{16} \vartheta^2 + 3.54814 \times 10^{18} \operatorname{Sin}[\beta]^2} \right) / \\ & \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \vartheta + z \delta^2 \eta^2 \vartheta + z^2 \vartheta^2} \right) - \\ & \left( 9.47204 \times 10^{69} r z \vartheta \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right. \right. \\ & \quad \left. \left. 1.79751 \times 10^{17} r z \alpha \vartheta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \vartheta + 8.98755 \times 10^{16} z^2 \vartheta^2 \right) \right. \\ & \quad \left. \operatorname{Sin}[\beta]^2 \sqrt{-12.5664 \vartheta + \vartheta^2 + 39.4784 \operatorname{Sin}[\beta]^2} \right. \\ & \quad \left. \sqrt{-1.12941 \times 10^{18} \vartheta + 8.98755 \times 10^{16} \vartheta^2 + 3.54814 \times 10^{18} \operatorname{Sin}[\beta]^2} \right) / \\ & \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \vartheta + z \delta^2 \eta^2 \vartheta + z^2 \vartheta^2} \right) + \\ & \left( 1.43754 \times 10^{69} z^2 \vartheta^2 \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right. \right. \\ & \quad \left. \left. 1.79751 \times 10^{17} r z \alpha \vartheta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \vartheta + 8.98755 \times 10^{16} z^2 \vartheta^2 \right) \right. \\ & \quad \left. \operatorname{Sin}[\beta]^2 \sqrt{-12.5664 \vartheta + \vartheta^2 + 39.4784 \operatorname{Sin}[\beta]^2} \right. \\ & \quad \left. \sqrt{-1.12941 \times 10^{18} \vartheta + 8.98755 \times 10^{16} \vartheta^2 + 3.54814 \times 10^{18} \operatorname{Sin}[\beta]^2} \right) / \\ & \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \vartheta + z \delta^2 \eta^2 \vartheta + z^2 \vartheta^2} \right) \Big) \Big) / \\ & \left( \sqrt{\left( 3.7464 \times 10^{104} \vartheta^2 - 5.96258 \times 10^{103} \vartheta^3 + 2.37243 \times 10^{102} \vartheta^4 - \right. \right. \\ & \quad \left. \left. 2.35393 \times 10^{105} \vartheta \operatorname{Sin}[\beta]^2 + 1.8732 \times 10^{104} \vartheta^2 \operatorname{Sin}[\beta]^2 + \right. \right. \\ & \quad \left. \left. 3.69755 \times 10^{105} \operatorname{Sin}[\beta]^4 \right) \right) \Big) \Big) \Big\}, \\ & \{ h \rightarrow \left( \sqrt{\left( 1.19252 \times 10^{104} r z \vartheta^3 - 1.89795 \times 10^{103} r z \vartheta^4 - \right. \right. \\ & \quad \left. \left. 9.48973 \times 10^{102} z^2 \vartheta^4 + \right. \right. \\ & \quad \left. \left. 7.55169 \times 10^{101} r z \vartheta^5 + \right. \right. \\ & \quad \left. \left. 1.51034 \times 10^{102} z^2 \vartheta^5 - \right. \right. \\ & \quad \left. \left. 6.00944 \times 10^{100} z^2 \vartheta^6 - \right. \right. \\ & \quad \left. \left. 7.49279 \times 10^{104} r z \vartheta^2 \operatorname{Sin}[\beta]^2 + \right. \right. \\ & \quad \left. \left. 5.96258 \times 10^{103} r z \vartheta^3 \operatorname{Sin}[\beta]^2 + \right. \right. \end{aligned}$$

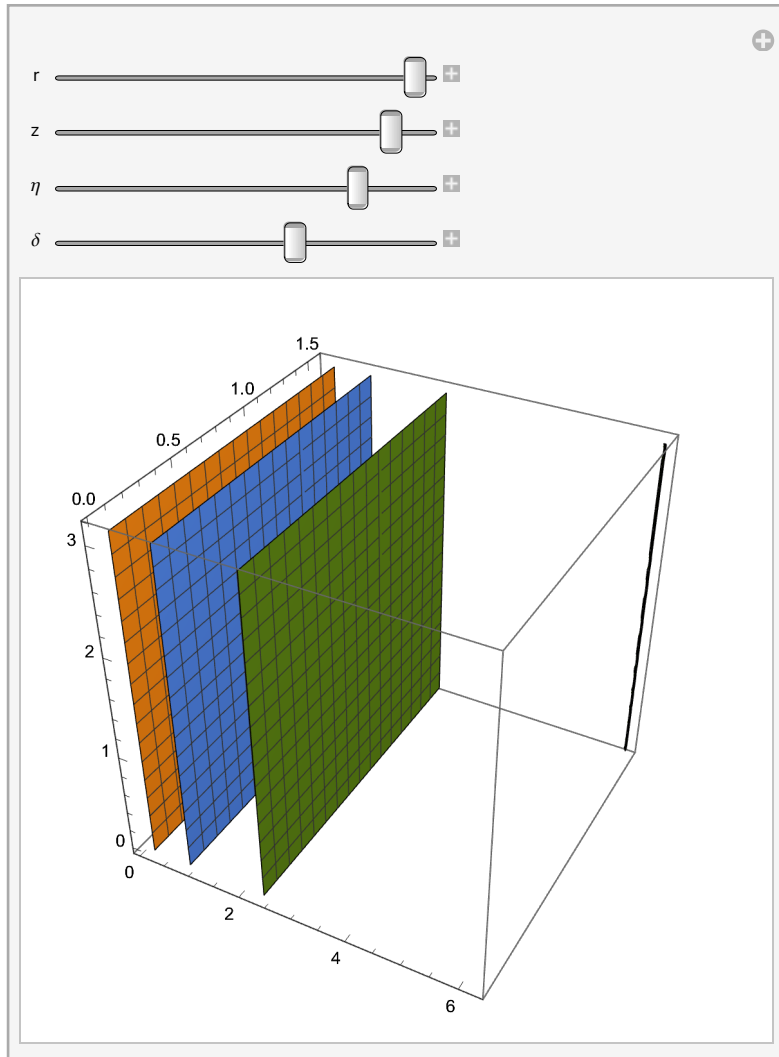
$$\begin{aligned}
& 5.96258 \times 10^{103} z^2 \theta^3 \sin[\beta]^2 - \\
& 4.74487 \times 10^{102} z^2 \theta^4 \sin[\beta]^2 + \\
& 1.17697 \times 10^{105} r z \theta \sin[\beta]^4 - \\
& 9.36599 \times 10^{103} z^2 \theta^2 \sin[\beta]^4 + \\
& \left( 3.01504 \times 10^{69} r z \theta^2 \right. \\
& \quad \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times \right.} \\
& \quad \left. 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2 \right) \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) - \left( 2.3993 \times 10^{68} r z \theta^3 \right. \\
& \quad \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times \right.} \\
& \quad \left. 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2 \right) \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) - \left( 4.57582 \times 10^{68} z^2 \theta^3 \right. \\
& \quad \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times \right.} \\
& \quad \left. 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2 \right) \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) + \left( 3.64132 \times 10^{67} z^2 \theta^4 \right. \\
& \quad \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times \right.} \\
& \quad \left. 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2 \right) \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) - \\
& \left( 9.47204 \times 10^{69} r z \theta \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right.} \right. \\
& \quad \left. 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2 \right) \\
& \quad \sin[\beta]^2 \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) + \\
& \left( 1.43754 \times 10^{69} z^2 \theta^2 \sqrt{\left( 8.98755 \times 10^{16} r^2 \alpha^2 - 8.98755 \times 10^{16} r^2 \delta^2 - \right.} \right. \\
& \quad \left. 1.79751 \times 10^{17} r z \alpha \theta + 8.98755 \times 10^{16} z \delta^2 \eta^2 \theta + 8.98755 \times 10^{16} z^2 \theta^2 \right) \\
& \quad \sin[\beta]^2 \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( \sqrt{r^2 \alpha^2 - 1. r^2 \delta^2 - 2. r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) \Big) \Big) / \\
& \left( \sqrt{\left( 3.7464 \times 10^{104} \theta^2 - 5.96258 \times 10^{103} \theta^3 + 2.37243 \times 10^{102} \theta^4 - \right.} \right. \\
& \quad \left. 2.35393 \times 10^{105} \theta \sin[\beta]^2 + \right. \\
& \quad \left. 1.8732 \times 10^{104} \theta^2 \sin[\beta]^2 + \right.
\end{aligned}$$

$$3.69755 \times 10^{105} \sin[\beta]^4) \Big) \Big) \Big\}$$

Manipulate[

$$\begin{aligned} & \text{ContourPlot3D} \Big[ \Big( \sqrt{ \Big( 1.1925151910444093 \cdot r z \theta^3 - 1.8979468736689365 \cdot r z \theta^4 - \\ & 9.489734368344682 \cdot z^2 \theta^4 + 7.551690666755506 \cdot r z \theta^5 + \\ & 1.5103381333511015 \cdot z^2 \theta^5 - 6.009444491575349 \cdot z^2 \theta^6 - \\ & 7.49279392695869 \cdot r z \theta^2 \sin[\beta]^2 + 5.9625759552220465 \cdot r z \theta^3 \sin[\beta]^2 + \\ & 5.9625759552220465 \cdot z^2 \theta^3 \sin[\beta]^2 - 4.744867184172341 \cdot z^2 \theta^4 \sin[\beta]^2 + \\ & 1.1769653177897818 \cdot r z \theta \sin[\beta]^4 - 9.365992408698362 \cdot z^2 \theta^2 \sin[\beta]^4 + \\ & \Big( 3.015044494171173 \cdot r z \theta^2 \sqrt{ \Big( 8.987551787368176 \cdot r^2 \alpha^2 - \\ & 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + \\ & 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2 \Big) } \\ & \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \\ & \sqrt{ \Big( -1.1294090667581471 \cdot \alpha \theta + 8.987551787368176 \cdot \theta^2 + \\ & 3.5481432270250993 \cdot \sin[\beta]^2 \Big) } \Big) \Big) / \\ & \Big( \sqrt{ r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2 } \Big) - \\ & \Big( 2.3992961744467273 \cdot r z \theta^3 \sqrt{ \Big( 8.987551787368176 \cdot r^2 \alpha^2 - \\ & 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + \\ & 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2 \Big) } \\ & \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \\ & \sqrt{ \Big( -1.1294090667581471 \cdot \alpha \theta + 8.987551787368176 \cdot \theta^2 + \\ & 3.5481432270250993 \cdot \sin[\beta]^2 \Big) } \Big) \Big) / \\ & \Big( \sqrt{ r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2 } \Big) - \\ & \Big( 4.575816320644992 \cdot z^2 \theta^3 \sqrt{ \Big( 8.987551787368176 \cdot r^2 \alpha^2 - \\ & 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + \\ & 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2 \Big) } \\ & \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \\ & \sqrt{ \Big( -1.1294090667581471 \cdot \alpha \theta + 8.987551787368176 \cdot \theta^2 + \\ & 3.5481432270250993 \cdot \sin[\beta]^2 \Big) } \Big) \Big) / \\ & \Big( \sqrt{ r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2 } \Big) + \\ & \Big( 3.641318930556098 \cdot z^2 \theta^4 \sqrt{ \Big( 8.987551787368176 \cdot r^2 \alpha^2 - \\ & 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + \\ & 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2 \Big) } \\ & \sqrt{ -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 } \end{aligned}$$

$$\begin{aligned}
& \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \\
& \quad 3.5481432270250993 \cdot \sin^2[\beta])} \Big/ \\
& \left( \sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) - \\
& \left( 9.472041633134512 \cdot r z \theta \sqrt{(8.987551787368176 \cdot r^2 \alpha^2 - \right. \\
& \quad 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + \\
& \quad 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2) \\
& \quad \sin^2[\beta]^2 \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]^2} \\
& \quad \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \\
& \quad \quad \left. 3.5481432270250993 \cdot \sin^2[\beta])} \Big/ \\
& \left( \sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) + \\
& \left( 1.4375350937114585 \cdot z^2 \theta^2 \sqrt{(8.987551787368176 \cdot r^2 \alpha^2 - \right. \\
& \quad 8.987551787368176 \cdot r^2 \delta^2 - 1.7975103574736352 \cdot r z \alpha \theta + \\
& \quad 8.987551787368176 \cdot z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot z^2 \theta^2) \\
& \quad \sin^2[\beta]^2 \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]^2} \\
& \quad \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \\
& \quad \quad \left. 3.5481432270250993 \cdot \sin^2[\beta])} \Big/ \\
& \left( \sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) \Big) \Big/ \\
& \left( \sqrt{(3.746396963479345 \cdot \theta^{104} - 5.9625759552220465 \cdot \theta^{103} + \right. \\
& \quad 2.3724335920861706 \cdot \theta^{102} - \\
& \quad 2.3539306355795636 \cdot \theta^{105} \sin^2[\beta] + \\
& \quad 1.8731984817396724 \cdot \theta^{104} \sin^2[\beta]^2 + \\
& \quad \left. 3.697545595898355 \cdot \sin^4[\beta])} \right), \\
& \{ \theta, 0, 2 \pi \}, \{ \beta, 0, \pi / 2 \}, \{ \alpha, 0, \pi \} \Big], \\
& \{ r, \\
& \quad -1, \\
& \quad 1 \}, \\
& \{ z, \\
& \quad -1, \\
& \quad 1 \}, \\
& \{ \eta, \\
& \quad -1, \\
& \quad 1 \}, \\
& \{ \delta, \\
& \quad -1, \\
& \quad 1 \} \Big]
\end{aligned}$$



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

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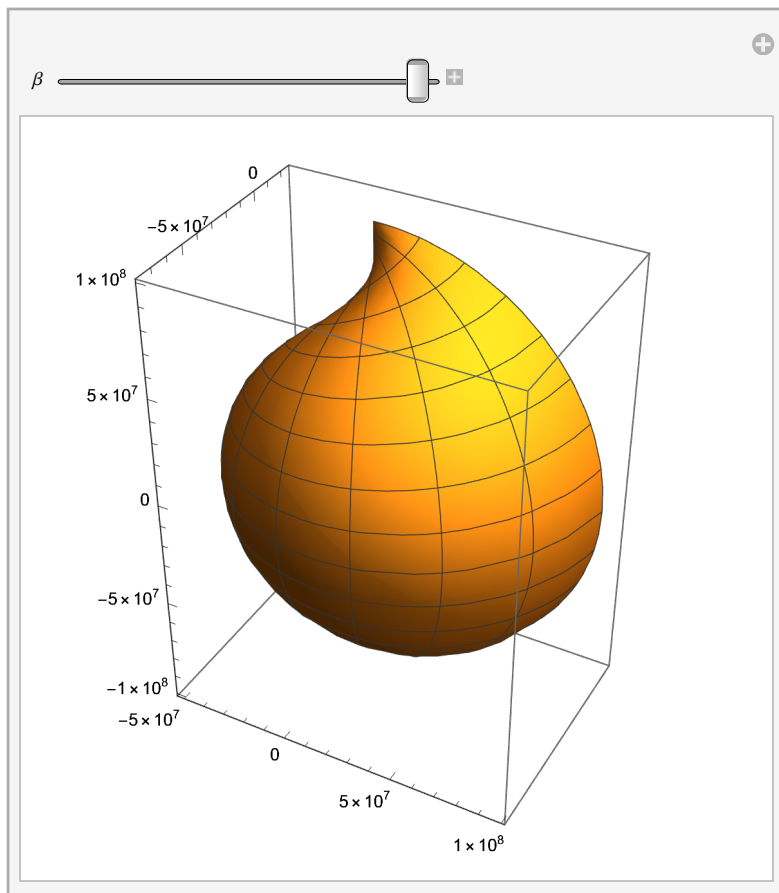
... **General:** Further output of Power::infy will be suppressed during this calculation.

$$\begin{aligned}
& \text{Solve}\left[\left(\sqrt{\left(1.0870275225442393 \eta^{50} + \right.}\right.\right. \\
& \quad \left.3.4601160697970476 \eta^{49} \gamma - 3.4601160697970476 r^2 \gamma + \right. \\
& \quad \left.2.7534728808995085 \eta^{48} \gamma^2 - 2.7534728808995085 r^2 \gamma^2\right) / \\
& \quad \left(\sqrt{\left(1.209481233890674 \eta^{33} \gamma^2 + 3.849898339011711 \eta^{32} \gamma - \right.}\right. \\
& \quad \left.3.849898339011711 r^2 \gamma + 3.0636517552749564 \eta^{31} \gamma^2 - \right. \\
& \quad \left.3.0636517552749564 r^2 \gamma^2\right) - \\
& \quad \left(\sqrt{\left(3.5481432270250993 \eta^{18} - 1.1294090667581471 r^2 \theta + \right.}\right. \\
& \quad \left.8.987551787368176 r^2 \theta^2\right) / \\
& \quad \left(\sqrt{39.47841760435743 \eta^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2}\right) == \\
& \quad \left(\sqrt{\left(8.987551787368176 l^2 \alpha^2 - 8.987551787368176 l^2 \delta^2 - \right.}\right. \\
& \quad \left.1.7975103574736352 l z \alpha \kappa + 8.987551787368176 z \delta^2 x^2 \kappa + \right. \\
& \quad \left.8.987551787368176 z^2 \kappa^2\right) / \\
& \quad \left.\left(\sqrt{l^2 \alpha^2 - 1. l^2 \delta^2 - 2. l z \alpha \kappa + z \delta^2 x^2 \kappa + z^2 \kappa^2}\right), r\right] \\
& \{\} \\
& \left(\sqrt{\left(1.0870275225442393 \eta^{50} + \right.}\right. \\
& \quad \left.3.4601160697970476 \eta^{49} \gamma - 3.4601160697970476 r^2 \gamma + \right. \\
& \quad \left.2.7534728808995085 \eta^{48} \gamma^2 - 2.7534728808995085 r^2 \gamma^2\right) / \\
& \quad \left(\sqrt{\left(1.209481233890674 \eta^{33} \gamma^2 + 3.849898339011711 \eta^{32} \gamma - 3.849898339011711 r^2 \gamma + \right.}\right. \\
& \quad \left.3.0636517552749564 \eta^{31} \gamma^2 - 3.0636517552749564 r^2 \gamma^2\right) - \\
& \quad \left(\sqrt{\left(3.5481432270250993 \eta^{18} - 1.1294090667581471 r^2 \theta + \right.}\right. \\
& \quad \left.8.987551787368176 r^2 \theta^2\right) / \\
& \quad \left.\left(\sqrt{39.47841760435743 \eta^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2}\right)\right)
\end{aligned}$$

$$\begin{aligned}
& \text{Solve} \left[ \left( \sqrt{(-3.4601160697970476 \cdot 10^{49} r^2 \gamma - \right.} \right. \\
& \quad \left. \left. 2.7534728808995085 \cdot 10^{48} r^2 \gamma^2 + 1.0870275225442393 \cdot 10^{50} \eta^2 + \right. \right. \\
& \quad \left. \left. 3.4601160697970476 \cdot 10^{49} \gamma \eta^2 + 2.7534728808995085 \cdot 10^{48} \gamma^2 \eta^2 \right) \right) / \\
& \quad \left( \sqrt{(-3.849898339011711 \cdot 10^{32} r^2 \gamma - 3.0636517552749564 \cdot 10^{31} r^2 \gamma^2 + \right.} \\
& \quad \left. 1.209481233890674 \cdot 10^{33} \eta^2 + 3.849898339011711 \cdot 10^{32} \gamma \eta^2 + \right. \\
& \quad \left. 3.0636517552749564 \cdot 10^{31} \gamma^2 \eta^2 \right) \right) - \\
& \quad \left( \sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + \right.} \\
& \quad \left. 8.987551787368176 \cdot 10^{16} r^2 \theta^2) \right) \Bigg] \\
& \quad \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) = \eta, \theta \Bigg] \\
& \left( \sqrt{(r^2 (-3.46012 \times 10^{49} - 2.75347 \times 10^{48} \gamma) \gamma + \right.} \\
& \quad \left. (1.08703 \times 10^{50} + 3.46012 \times 10^{49} \gamma + 2.75347 \times 10^{48} \gamma^2) \eta^2) \right) \Bigg] / \\
& \left( \sqrt{(r^2 (-3.8499 \times 10^{32} - 3.06365 \times 10^{31} \gamma) \gamma + \right.} \\
& \quad \left. (1.20948 \times 10^{33} + 3.8499 \times 10^{32} \gamma + 3.06365 \times 10^{31} \gamma^2) \eta^2) \right) \Bigg] - \\
& \frac{\sqrt{3.54814 \times 10^{18} \eta^2 + r^2 \theta (-1.12941 \times 10^{18} + 8.98755 \times 10^{16} \theta)}}{\sqrt{39.4784 \eta^2 + r^2 (-12.5664 + \theta) \theta}}
\end{aligned}$$



```
Manipulate[
  SphericalPlot3D[( $\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}) /$ 
 $(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}) -$ 
 $1.0747647608787885 \cdot 10^{-12} \csc[\beta]^2 \sqrt{(-7.780626516783903 \cdot 10^{40} -$ 
 $\frac{1.2126460106799624 \cdot 10^{44}}{(6.283185307179586 + \gamma)^4} + \frac{6.143336457062639 \cdot 10^{42}}{(6.283185307179586 + \gamma)^2} +$ 
 $7.780626516783903 \cdot 10^{40} \sin[\beta]^4})$ , { $\theta$ , 0,  $\pi$ }, { $\gamma$ , 0,  $2\pi$ }, { $\beta$ , 0,  $\pi/2$ }]
```



$$\begin{aligned}
& \text{Simplify}\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right)}\right) / \\
& \quad \left(\sqrt{-12.566370614359172 \cdot 10^0 \theta + \theta^2 + 39.47841760435743 \cdot 10^0 \sin[\beta]^2}\right) - \\
& \quad 1.0747647608787885 \cdot 10^{-12} \csc[\beta]^2 \\
& \quad \sqrt{\left(-7.780626516783903 \cdot 10^{40} - \frac{1.2126460106799624 \cdot 10^{44}}{(6.283185307179586 \cdot 10^0 + \gamma)^4} + \right. \\
& \quad \left. \frac{6.143336457062639 \cdot 10^{42}}{(6.283185307179586 \cdot 10^0 + \gamma)^2} + 7.780626516783903 \cdot 10^{40} \sin[\beta]^4\right)} \\
& \quad \left. \frac{\sqrt{\theta \left(-1.12941 \times 10^{18} + 8.98755 \times 10^{16} \theta\right) + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{(-12.5664 + \theta) \theta + 39.4784 \sin[\beta]^2}} - 1.07476 \times 10^{-12} \csc[\beta]^2 \right. \\
& \quad \left. \sqrt{-7.78063 \times 10^{40} - \frac{1.21265 \times 10^{44}}{(6.28319 + \gamma)^4} + \frac{6.14334 \times 10^{42}}{(6.28319 + \gamma)^2} + 7.78063 \times 10^{40} \sin[\beta]^4}\right)
\end{aligned}$$

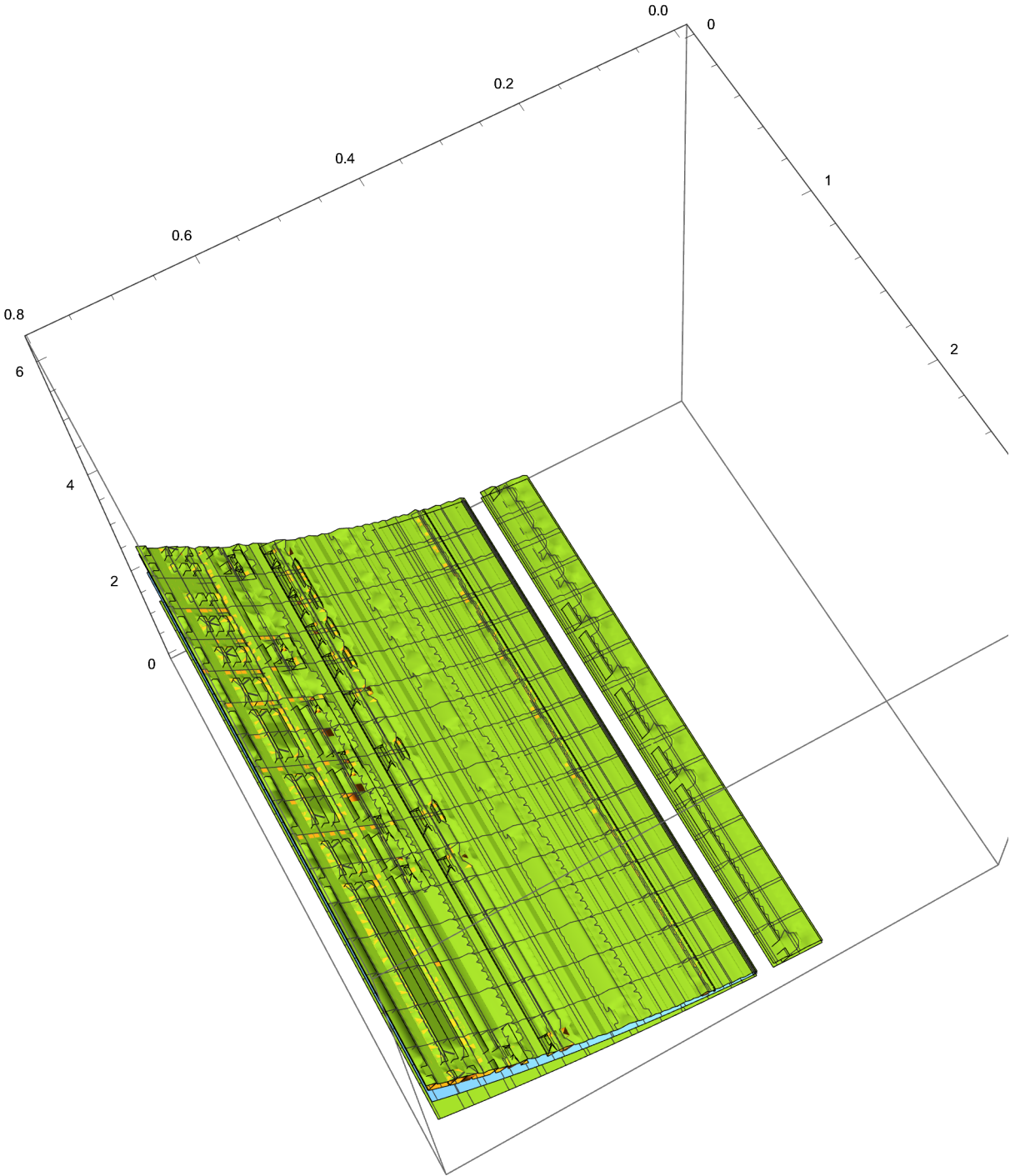
$$\begin{aligned}
& \text{Solve}\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta]^2\right)\right)}\right) / \left(\sqrt{-12.566370614359172 \cdot 10^0 \theta + \theta^2 + 39.47841760435743 \cdot 10^0 \sin[\beta]^2}\right) - \\
& \quad \left(1.0747647608787885 \cdot 10^{-12} \csc[\beta]^2 \sqrt{\left(-7.780626516783903 \cdot 10^{40} - \right. \right. \\
& \quad \left. \frac{1.2126460106799624 \cdot 10^{44}}{(6.283185307179586 \cdot 10^0 + \gamma)^4} + \frac{6.143336457062639 \cdot 10^{42}}{(6.283185307179586 \cdot 10^0 + \gamma)^2} + \right. \\
& \quad \left. \left. 7.780626516783903 \cdot 10^{40} \sin[\beta]^4\right)}\right) = v, \theta]
\end{aligned}$$

$$\begin{aligned}
& \text{Solve}\left[\left(1.0747647608787885 \cdot 10^{-12} \csc[\beta]^2 \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right. \right. \\
& \quad \left. \sqrt{\left(-7.780626516783903 \cdot 10^{40} - \frac{1.2126460106799624 \cdot 10^{44}}{(6.283185307179586 + \gamma)^4} + \frac{6.143336457062639 \cdot 10^{42}}{(6.283185307179586 + \gamma)^2} + 7.780626516783903 \cdot 10^{40} \sin[\beta]^4\right)}\right) \Bigg] \\
& \quad \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) = v^2, v] \\
& \left\{\left\{v \rightarrow \right. \right. \\
& \quad - \left(\left(1.03671 \times 10^{-6} \csc[\beta] \left(-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2\right)\right)^{1/4} \right. \\
& \quad \left.\left(-7.78063 \times 10^{40} - \frac{1.21265 \times 10^{44}}{(6.28319 + \gamma)^4} + \frac{6.14334 \times 10^{42}}{(6.28319 + \gamma)^2} + 7.78063 \times 10^{40} \sin[\beta]^4\right)^{1/4}\right) \Bigg] \Bigg/ \\
& \quad \left. \left(-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2\right)^{1/4}\right\}, \\
& \left\{v \rightarrow \left(1.03671 \times 10^{-6} \csc[\beta] \left(-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2\right)\right)^{1/4} \right. \\
& \quad \left.\left(-7.78063 \times 10^{40} - \frac{1.21265 \times 10^{44}}{(6.28319 + \gamma)^4} + \frac{6.14334 \times 10^{42}}{(6.28319 + \gamma)^2} + 7.78063 \times 10^{40} \sin[\beta]^4\right)^{1/4}\right) \Bigg] \Bigg/ \\
& \quad \left. \left(-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2\right)^{1/4}\right\} \\
& \text{Solve}\left[v = \left(1.0367086190819426 \cdot 10^{-6} \csc[\beta] \left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)\right)^{1/4} \right. \\
& \quad \left(-7.780626516783903 \cdot 10^{40} - \frac{1.2126460106799624 \cdot 10^{44}}{(6.283185307179586 + \gamma)^4} + \frac{6.143336457062639 \cdot 10^{42}}{(6.283185307179586 + \gamma)^2} + 7.780626516783903 \cdot 10^{40} \sin[\beta]^4\right)^{1/4}\right) \Bigg] \Bigg/ \\
& \quad \left. \left(-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2\right)^{1/4}, \beta\right]
\end{aligned}$$

```

ContourPlot3D[ $\left(1.0747647608787885 \cdot 10^{-12} \csc[\beta]^2 \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2} \right. \\ \left. \sqrt{\left(-7.780626516783903 \cdot 10^{40} - \frac{1.2126460106799624 \cdot 10^{44}}{(6.283185307179586 + \gamma)^4} + \frac{6.143336457062639 \cdot 10^{42}}{(6.283185307179586 + \gamma)^2} + 7.780626516783903 \cdot 10^{40} \sin[\beta]^4\right)}\right) / \\ \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \\ \{\beta, 0, \pi/4\}, \{\theta, 0, \pi\}, \{\gamma, 0, 2\pi\}]$ 

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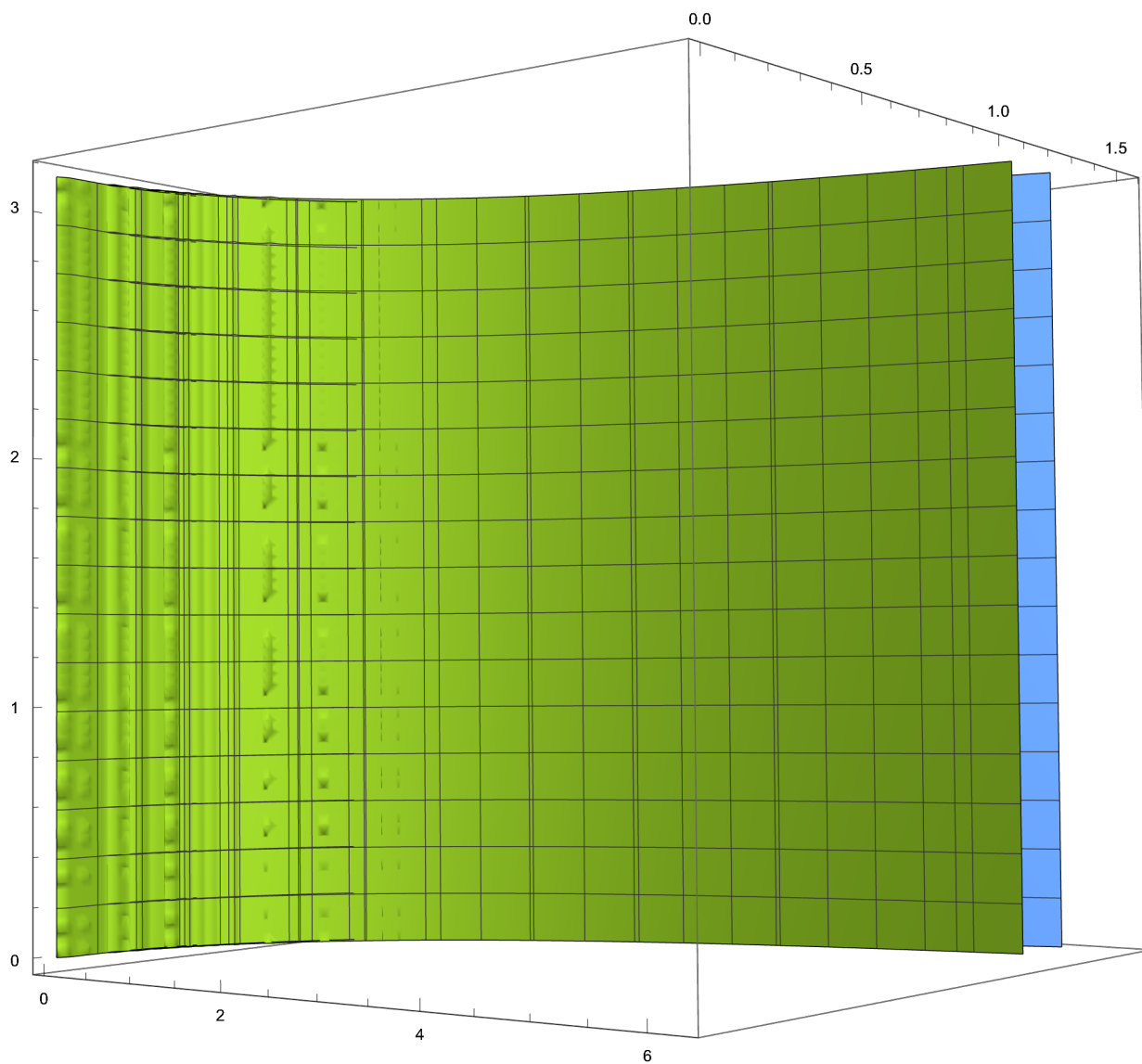
SphericalPlot3D[  

$$\left( \sqrt{(-1.1294090667581471 \theta^{18} + 8.987551787368176 \theta^{16} \vartheta^2 + 3.5481432270250993 \theta^{18} \sin[\beta]^2)} \right) / \left( \sqrt{-12.566370614359172 \theta + \vartheta^2 + 39.47841760435743 \sin[\beta]^2} \right) -$$
  

$$1.0747647608787885 \theta^{-12} \csc[\beta]^2 \sqrt{-7.780626516783903 \theta^{40} -$$
  

$$\frac{1.2126460106799624 \theta^{44}}{(6.283185307179586 + \gamma)^4} + \frac{6.143336457062639 \theta^{42}}{(6.283185307179586 + \gamma)^2} +$$
  

$$7.780626516783903 \theta^{40} \sin[\beta]^4 \Big), \{\theta, 0, \pi\}, \{\gamma, 0, 2\pi\}, \{\beta, 0, \pi/2\}]$$

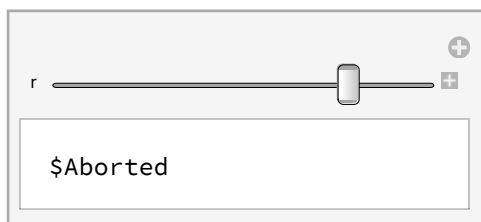


```

Solve[
  ((Sqrt[
    (3.5481432270250993`*^18 h^2 -
      1.1294090667581471`*^18 r^2 \theta + 8.987551787368176`*^16 r^2 \theta^2)
  ])/
  (Sqrt[
    39.47841760435743` h^2 - 12.566370614359172` r^2 \theta + r^2 \theta^2
  ]))
  (Sqrt[
    (1.0870275225442393`*^50 h^2 + 3.4601160697970476`*^49 h^2 \gamma -
      3.4601160697970476`*^49 r^2 \gamma + 2.7534728808995085`*^48 h^2 \gamma^2 -
      2.7534728808995085`*^48 r^2 \gamma^2)
  ])/
  (Sqrt[
    (1.209481233890674`*^33 h^2 + 3.849898339011711`*^32 h^2 \gamma -
      3.849898339011711`*^32 r^2 \gamma + 3.0636517552749564`*^31 h^2 \gamma^2 -
      3.0636517552749564`*^31 r^2 \gamma^2)
  ]) == v^2, r]

Manipulate[
  ContourPlot3D[
    ((Sqrt[
      (3.5481432270250993`*^18 h^2 - 1.1294090667581471`*^18 r^2 \theta +
        8.987551787368176`*^16 r^2 \theta^2)
    ])/
    (Sqrt[
      39.47841760435743` h^2 - 12.566370614359172` r^2 \theta + r^2 \theta^2
    ]))
    (Sqrt[
      (1.0870275225442393`*^50 h^2 + 3.4601160697970476`*^49 h^2 \gamma -
        3.4601160697970476`*^49 r^2 \gamma + 2.7534728808995085`*^48 h^2 \gamma^2 -
        2.7534728808995085`*^48 r^2 \gamma^2)
    ])/
    (Sqrt[
      (1.209481233890674`*^33 h^2 + 3.849898339011711`*^32 h^2 \gamma -
        3.849898339011711`*^32 r^2 \gamma + 3.0636517552749564`*^31 h^2 \gamma^2 -
        3.0636517552749564`*^31 r^2 \gamma^2)
    ])
  ], {r, 0, 10}, {h, 0, 10}, {\gamma, 0, 4 \pi}, {\theta, 0, \pi}]

```



\

$$\text{Solve}\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} \eta^2 -\right.}\right.\right.$$

$$\left.\left.1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)\right) /$$

$$\left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right)$$

$$\left(\sqrt{\left(1.0870275225442393 \cdot 10^{50} h^2 + 3.4601160697970476 \cdot 10^{49} h^2 \gamma -\right.}\right.$$

$$3.4601160697970476 \cdot 10^{49} r^2 \gamma + 2.7534728808995085 \cdot 10^{48} h^2 \gamma^2 -$$

$$2.7534728808995085 \cdot 10^{48} r^2 \gamma^2\left.\right)\right) /$$

$$\left(\sqrt{\left(1.209481233890674 \cdot 10^{33} h^2 + 3.849898339011711 \cdot 10^{32} h^2 \gamma -\right.}\right.$$

$$3.849898339011711 \cdot 10^{32} r^2 \gamma + 3.0636517552749564 \cdot 10^{31} h^2 \gamma^2 -$$

$$3.0636517552749564 \cdot 10^{31} r^2 \gamma^2\left.\right)\right) = v^2, r]$$

$$\left\{\left\{r \rightarrow -0.5\right.\right.$$

$$\sqrt{\left(-\left(\left(2. \left(-3.04782 \times 10^{82} \gamma \eta^2 + 3.77317 \times 10^{48} v^4 \gamma \eta^2 - 2.42538 \times 10^{81} \gamma^2 \eta^2 + 3.00259 \times\right.\right.\right.$$

$$10^{47} v^4 \gamma^2 \eta^2 - 3.04782 \times 10^{82} h^2 \theta + 3.77317 \times 10^{48} h^2 v^4 \theta - 9.70151 \times 10^{81} h^2$$

$$\gamma \theta + 1.20104 \times 10^{48} h^2 v^4 \gamma \theta - 7.72021 \times 10^{80} h^2 \gamma^2 \theta + 9.55755 \times 10^{46} h^2$$

$$v^4 \gamma^2 \theta + 2.42538 \times 10^{81} h^2 \theta^2 - 3.00259 \times 10^{47} h^2 v^4 \theta^2 + 7.72021 \times 10^{80} h^2 \gamma \theta^2 -$$

$$9.55755 \times 10^{46} h^2 v^4 \gamma \theta^2 + 6.14355 \times 10^{79} h^2 \gamma^2 \theta^2 - 7.60566 \times 10^{45} h^2 v^4 \gamma^2 \theta^2\left.\right)\right) /$$

$$\left(\gamma \theta \left(9.70151 \times 10^{81} - 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma -\right.\right.$$

$$9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \theta + 9.55755 \times 10^{46} v^4 \theta -$$

$$6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta\left.\right)\right) -$$

$$2. \sqrt{\left(-\left(\left(4. h^2 \left(9.575 \times 10^{82} - 1.18538 \times 10^{49} v^4 + 3.04782 \times 10^{82} \gamma - 3.77317 \times 10^{48} v^4 \gamma +\right.\right.\right.$$

$$2.42538 \times 10^{81} \gamma^2 - 3.00259 \times 10^{47} v^4 \gamma^2\left.\right) \eta^2\right) / \left(\gamma \theta \left(9.70151 \times 10^{81} -\right.\right.$$

$$1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - 9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80}$$

$$\theta + 9.55755 \times 10^{46} v^4 \theta - 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta\left.\right)\right) +$$

$$\left(-3.04782 \times 10^{82} \gamma \eta^2 + 3.77317 \times 10^{48} v^4 \gamma \eta^2 - 2.42538 \times 10^{81} \gamma^2 \eta^2 +\right.$$

$$3.00259 \times 10^{47} v^4 \gamma^2 \eta^2 - 3.04782 \times 10^{82} h^2 \theta + 3.77317 \times 10^{48} h^2 v^4 \theta -$$

$$9.70151 \times 10^{81} h^2 \gamma \theta + 1.20104 \times 10^{48} h^2 v^4 \gamma \theta - 7.72021 \times 10^{80} h^2 \gamma^2 \theta +$$

$$9.55755 \times 10^{46} h^2 v^4 \gamma^2 \theta + 2.42538 \times 10^{81} h^2 \theta^2 - 3.00259 \times 10^{47} h^2 v^4 \theta^2 +$$

$$7.72021 \times 10^{80} h^2 \gamma \theta^2 - 9.55755 \times 10^{46} h^2 v^4 \gamma \theta^2 +$$

$$6.14355 \times 10^{79} h^2 \gamma^2 \theta^2 - 7.60566 \times 10^{45} h^2 v^4 \gamma^2 \theta^2\left.\right)^2 /$$

$$\left(\gamma^2 \theta^2 \left(9.70151 \times 10^{81} - 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma -\right.\right.$$

$$9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \theta + 9.55755 \times 10^{46} v^4 \theta -$$

$$6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta\left.\right)^2\left.\right)\right)\right],$$

$$\left\{r \rightarrow 0.5 \sqrt{\left(-\left(\left(2. \left(-3.04782 \times 10^{82} \gamma \eta^2 + 3.77317 \times 10^{48} v^4 \gamma \eta^2 - 2.42538 \times 10^{81} \gamma^2 \eta^2 +\right.\right.\right.\right.$$

$$3.00259 \times 10^{47} v^4 \gamma^2 \eta^2 - 3.04782 \times 10^{82} h^2 \theta + 3.77317 \times 10^{48} h^2 v^4 \theta -$$

$$9.70151 \times 10^{81} h^2 \gamma \theta + 1.20104 \times 10^{48} h^2 v^4 \gamma \theta - 7.72021 \times 10^{80} h^2 \gamma^2 \theta +$$

$$9.55755 \times 10^{46} h^2 v^4 \gamma^2 \theta + 2.42538 \times 10^{81} h^2 \theta^2 - 3.00259 \times 10^{47} h^2 v^4 \theta^2 +$$

$$7.72021 \times 10^{80} h^2 \gamma \theta^2 - 9.55755 \times 10^{46} h^2 v^4 \gamma \theta^2 +$$

$$6.14355 \times 10^{79} h^2 \gamma^2 \theta^2 - 7.60566 \times 10^{45} h^2 v^4 \gamma^2 \theta^2\left.\right)\right) /$$





$$\begin{aligned}
& 3.00259 \times 10^{47} v^4 \gamma^2 \eta^2 - 3.04782 \times 10^{82} h^2 \theta + 3.77317 \times 10^{48} h^2 v^4 \theta - \\
& 9.70151 \times 10^{81} h^2 \gamma \theta + 1.20104 \times 10^{48} h^2 v^4 \gamma \theta - 7.72021 \times 10^{80} h^2 \gamma^2 \theta + \\
& 9.55755 \times 10^{46} h^2 v^4 \gamma^2 \theta + 2.42538 \times 10^{81} h^2 \theta^2 - 3.00259 \times 10^{47} h^2 v^4 \theta^2 + \\
& 7.72021 \times 10^{80} h^2 \gamma \theta^2 - 9.55755 \times 10^{46} h^2 v^4 \gamma \theta^2 + \\
& 6.14355 \times 10^{79} h^2 \gamma^2 \theta^2 - 7.60566 \times 10^{45} h^2 v^4 \gamma^2 \theta^2) / \\
& (\gamma \theta (9.70151 \times 10^{81} - 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - \\
& 9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \theta + 9.55755 \times 10^{46} v^4 \theta - \\
& 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta)) + \\
2. & \sqrt{(-((4. h^2 (9.575 \times 10^{82} - 1.18538 \times 10^{49} v^4 + 3.04782 \times 10^{82} \gamma - 3.77317 \times 10^{48} v^4 \gamma + \\
& 2.42538 \times 10^{81} \gamma^2 - 3.00259 \times 10^{47} v^4 \gamma^2) \eta^2) / (\gamma \theta (9.70151 \times 10^{81} - \\
& 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - 9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \\
& \theta + 9.55755 \times 10^{46} v^4 \theta - 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta)) + \\
& (-3.04782 \times 10^{82} \gamma \eta^2 + 3.77317 \times 10^{48} v^4 \gamma \eta^2 - 2.42538 \times 10^{81} \gamma^2 \eta^2 + \\
& 3.00259 \times 10^{47} v^4 \gamma^2 \eta^2 - 3.04782 \times 10^{82} h^2 \theta + 3.77317 \times 10^{48} h^2 v^4 \theta - \\
& 9.70151 \times 10^{81} h^2 \gamma \theta + 1.20104 \times 10^{48} h^2 v^4 \gamma \theta - 7.72021 \times 10^{80} h^2 \gamma^2 \theta + \\
& 9.55755 \times 10^{46} h^2 v^4 \gamma^2 \theta + 2.42538 \times 10^{81} h^2 \theta^2 - 3.00259 \times 10^{47} h^2 v^4 \theta^2 + \\
& 7.72021 \times 10^{80} h^2 \gamma \theta^2 - 9.55755 \times 10^{46} h^2 v^4 \gamma \theta^2 + \\
& 6.14355 \times 10^{79} h^2 \gamma^2 \theta^2 - 7.60566 \times 10^{45} h^2 v^4 \gamma^2 \theta^2)^2 / \\
& (\gamma^2 \theta^2 (9.70151 \times 10^{81} - 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - \\
& 9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \theta + 9.55755 \times 10^{46} v^4 \theta - \\
& 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta)^2))\}}
\end{aligned}$$

$h := \eta$

$$\begin{aligned}
& 0.5 \sqrt{\left( - \left( \left( 2. \left( -3.047818057919681 \cdot \gamma^2 \eta^2 + 3.7731687262728915 \cdot v^4 \gamma \eta^2 - \right. \right. \right. \right. \\
& \quad 2.425376547813289 \cdot \gamma^2 \eta^2 + 3.0025922695304064 \cdot v^4 \gamma^2 \eta^2 - \\
& \quad 3.047818057919681 \cdot h^2 \theta + 3.7731687262728915 \cdot h^2 v^4 \theta - \\
& \quad 9.701506191253155 \cdot h^2 \gamma \theta + 1.2010369078121626 \cdot h^2 v^4 \gamma \theta - \\
& \quad 7.720213328872831 \cdot h^2 \gamma^2 \theta + 9.557548035705534 \cdot h^2 v^4 \gamma^2 \theta + \\
& \quad 2.4253765478132886 \cdot h^2 \theta^2 - 3.0025922695304068 \cdot h^2 v^4 \theta^2 + \\
& \quad 7.720213328872831 \cdot h^2 \gamma \theta^2 - 9.557548035705534 \cdot h^2 v^4 \gamma \theta^2 + \\
& \quad \left. \left. \left. \left. 6.143550565070237 \cdot h^2 \gamma^2 \theta^2 - 7.605655068603853 \cdot h^2 v^4 \gamma^2 \theta^2 \right) \right) \right) \right) / \\
& \left( \gamma \theta \left( 9.701506191253155 \cdot \gamma^2 - 1.2010369078121626 \cdot v^4 + \right. \right. \\
& \quad 7.720213328872831 \cdot \gamma - 9.557548035705534 \cdot v^4 \gamma - \\
& \quad 7.720213328872831 \cdot \theta + 9.557548035705534 \cdot v^4 \theta - \\
& \quad \left. \left. \left. \left. 6.143550565070237 \cdot \gamma \theta + 7.605655068603853 \cdot v^4 \gamma \theta \right) \right) \right) \right) + \\
& 2. \sqrt{\left( - \left( \left( 4. \left( h^2 \left( 9.57500282023878 \cdot \gamma^2 - 1.1853759151213674 \cdot v^4 + \right. \right. \right. \right. \right. \\
& \quad 3.047818057919681 \cdot \gamma - 3.7731687262728915 \cdot v^4 \gamma + \\
& \quad 2.425376547813289 \cdot \gamma^2 - 3.0025922695304064 \cdot v^4 \gamma^2 \right) \eta^2 \right) / \\
& \left( \gamma \theta \left( 9.701506191253155 \cdot \gamma^2 - 1.2010369078121626 \cdot v^4 + \right. \right. \\
& \quad 7.720213328872831 \cdot \gamma - 9.557548035705534 \cdot v^4 \gamma \\
& \quad \gamma - 7.720213328872831 \cdot \theta + 9.557548035705534 \cdot v^4 \theta \\
& \quad \left. \left. \left. \left. \theta - 6.143550565070237 \cdot \gamma \theta + 7.605655068603853 \cdot v^4 \gamma \theta \right) \right) \right) \right) + \\
& \left( -3.047818057919681 \cdot \gamma^2 \eta^2 + 3.7731687262728915 \cdot v^4 \gamma \eta^2 - \right. \\
& \quad 2.425376547813289 \cdot \gamma^2 \eta^2 + 3.0025922695304064 \cdot v^4 \gamma^2 \eta^2 - \\
& \quad 3.047818057919681 \cdot h^2 \theta + 3.7731687262728915 \cdot h^2 v^4 \theta - \\
& \quad 9.701506191253155 \cdot h^2 \gamma \theta + 1.2010369078121626 \cdot h^2 v^4 \gamma \theta - \\
& \quad 7.720213328872831 \cdot h^2 \gamma^2 \theta + 9.557548035705534 \cdot h^2 v^4 \gamma^2 \theta + \\
& \quad 2.4253765478132886 \cdot h^2 \theta^2 - 3.0025922695304068 \cdot h^2 v^4 \theta^2 + \\
& \quad 7.720213328872831 \cdot h^2 \gamma \theta^2 - 9.557548035705534 \cdot h^2 v^4 \gamma \theta^2 + \\
& \quad \left. \left. \left. \left. 6.143550565070237 \cdot h^2 \gamma^2 \theta^2 - 7.605655068603853 \cdot h^2 v^4 \gamma^2 \theta^2 \right) \right) \right)^2 / \\
& \left( \gamma^2 \theta^2 \left( 9.701506191253155 \cdot \gamma^2 - 1.2010369078121626 \cdot v^4 + \right. \right. \\
& \quad 7.720213328872831 \cdot \gamma - 9.557548035705534 \cdot v^4 \gamma \\
& \quad \gamma - 7.720213328872831 \cdot \theta + 9.557548035705534 \cdot v^4 \theta \\
& \quad \left. \left. \left. \left. \theta - 6.143550565070237 \cdot \gamma \theta + 7.605655068603853 \cdot v^4 \gamma \theta \right) \right) \right)^2 \right) \right)
\end{aligned}$$

0.5

$$\begin{aligned}
& \sqrt{\left( - \left( \left( 2. \left( -3.04782 \times 10^{82} \gamma \eta^2 + 3.77317 \times 10^{48} v^4 \gamma \eta^2 - 2.42538 \times 10^{81} \gamma^2 \eta^2 + 3.00259 \times 10^{47} v^4 \right. \right. \right. \right. \\
& \quad \gamma^2 \eta^2 - 3.04782 \times 10^{82} \eta^2 \theta + 3.77317 \times 10^{48} v^4 \eta^2 \theta - 9.70151 \times 10^{81} \gamma \eta^2 \theta + \\
& \quad 1.20104 \times 10^{48} v^4 \gamma \eta^2 \theta - 7.72021 \times 10^{80} \gamma^2 \eta^2 \theta + 9.55755 \times 10^{46} v^4 \gamma^2 \eta^2 \theta + \\
& \quad 2.42538 \times 10^{81} \eta^2 \theta^2 - 3.00259 \times 10^{47} v^4 \eta^2 \theta^2 + 7.72021 \times 10^{80} \gamma \eta^2 \theta^2 - \\
& \quad 9.55755 \times 10^{46} v^4 \gamma \eta^2 \theta^2 + 6.14355 \times 10^{79} \gamma^2 \eta^2 \theta^2 - 7.60566 \times 10^{45} v^4 \gamma^2 \eta^2 \theta^2 \left. \right) \right) / \\
& \quad \left( \gamma \theta \left( 9.70151 \times 10^{81} - 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - \right. \right. \\
& \quad 9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \theta + 9.55755 \times 10^{46} v^4 \theta - \\
& \quad \left. \left. 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta \right) \right) \left. \right) + \\
& 2. \sqrt{\left( - \left( \left( 4. \left( 9.575 \times 10^{82} - 1.18538 \times 10^{49} v^4 + 3.04782 \times 10^{82} \gamma - 3.77317 \times 10^{48} \right. \right. \right. \right. \\
& \quad v^4 \gamma + 2.42538 \times 10^{81} \gamma^2 - 3.00259 \times 10^{47} v^4 \gamma^2 \left. \right) \eta^4 \left. \right) / \left( \gamma \theta \left( 9.70151 \times 10^{81} - \right. \right. \\
& \quad 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - 9.55755 \times 10^{46} v^4 \gamma - 7.72021 \times 10^{80} \\
& \quad \theta + 9.55755 \times 10^{46} v^4 \theta - 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta \left. \right) \right) \left. \right) + \\
& \quad \left( -3.04782 \times 10^{82} \gamma \eta^2 + 3.77317 \times 10^{48} v^4 \gamma \eta^2 - 2.42538 \times 10^{81} \gamma^2 \eta^2 + 3.00259 \times 10^{47} \right. \\
& \quad v^4 \gamma^2 \eta^2 - 3.04782 \times 10^{82} \eta^2 \theta + 3.77317 \times 10^{48} v^4 \eta^2 \theta - 9.70151 \times 10^{81} \gamma \eta^2 \theta + \\
& \quad 1.20104 \times 10^{48} v^4 \gamma \eta^2 \theta - 7.72021 \times 10^{80} \gamma^2 \eta^2 \theta + 9.55755 \times 10^{46} v^4 \gamma^2 \eta^2 \theta + \\
& \quad 2.42538 \times 10^{81} \eta^2 \theta^2 - 3.00259 \times 10^{47} v^4 \eta^2 \theta^2 + 7.72021 \times 10^{80} \gamma \eta^2 \theta^2 - \\
& \quad \left. \left. 9.55755 \times 10^{46} v^4 \gamma \eta^2 \theta^2 + 6.14355 \times 10^{79} \gamma^2 \eta^2 \theta^2 - 7.60566 \times 10^{45} v^4 \gamma^2 \eta^2 \theta^2 \right)^2 \right. / \\
& \quad \left( \gamma^2 \theta^2 \left( 9.70151 \times 10^{81} - 1.20104 \times 10^{48} v^4 + 7.72021 \times 10^{80} \gamma - 9.55755 \times 10^{46} \right. \right. \\
& \quad v^4 \gamma - 7.72021 \times 10^{80} \theta + 9.55755 \times 10^{46} v^4 \\
& \quad \left. \left. \theta - 6.14355 \times 10^{79} \gamma \theta + 7.60566 \times 10^{45} v^4 \gamma \theta \right)^2 \right) \left. \right) \left. \right)
\end{aligned}$$

```

Manipulate[ContourPlot3D[
  0.5` $\sqrt{-\left(\left(2.\left(-3.047818057919681`^{\wedge}82\gamma\eta^2+3.7731687262728915`^{\wedge}48v^4\gamma\eta^2-2.425376547813289`^{\wedge}81\gamma^2\eta^2+3.0025922695304064`^{\wedge}47v^4\gamma^2\eta^2-3.047818057919681`^{\wedge}82\eta^2\theta+3.7731687262728915`^{\wedge}48v^4\eta^2\theta-9.701506191253155`^{\wedge}81\gamma\eta^2\theta+1.2010369078121626`^{\wedge}48v^4\gamma\eta^2\theta-7.720213328872831`^{\wedge}80\gamma^2\eta^2\theta+9.557548035705534`^{\wedge}46v^4\gamma^2\eta^2\theta+2.4253765478132886`^{\wedge}81\eta^2\theta^2-3.0025922695304068`^{\wedge}47v^4\eta^2\theta^2+7.720213328872831`^{\wedge}80\gamma\eta^2\theta^2-9.557548035705534`^{\wedge}46v^4\gamma\eta^2\theta^2+6.143550565070237`^{\wedge}79\gamma^2\eta^2\theta^2-7.605655068603853`^{\wedge}45v^4\gamma^2\eta^2\theta^2\right)\right) / \left(\gamma\theta\left(9.701506191253155`^{\wedge}81-1.2010369078121626`^{\wedge}48v^4+7.720213328872831`^{\wedge}80\gamma-9.557548035705534`^{\wedge}46v^4\gamma-7.720213328872831`^{\wedge}80\theta+9.557548035705534`^{\wedge}46v^4\theta-6.143550565070237`^{\wedge}79\gamma\theta+7.605655068603853`^{\wedge}45v^4\gamma\theta\right)\right)} + 2.\sqrt{-\left(\left(4.\left(9.57500282023878`^{\wedge}82-1.1853759151213674`^{\wedge}49v^4+3.047818057919681`^{\wedge}82\gamma-3.7731687262728915`^{\wedge}48v^4\gamma+2.425376547813289`^{\wedge}81\gamma^2-3.0025922695304064`^{\wedge}47v^4\gamma^2\right)\eta^4\right) / \left(\gamma\theta\left(9.701506191253155`^{\wedge}81-1.2010369078121626`^{\wedge}48v^4+7.720213328872831`^{\wedge}80\gamma-9.557548035705534`^{\wedge}46v^4\gamma-7.720213328872831`^{\wedge}80\theta+9.557548035705534`^{\wedge}46v^4\theta-6.143550565070237`^{\wedge}79\gamma\theta+7.605655068603853`^{\wedge}45v^4\gamma\theta\right)\right)} + \left(-3.047818057919681`^{\wedge}82\gamma\eta^2+3.7731687262728915`^{\wedge}48v^4\gamma\eta^2-2.425376547813289`^{\wedge}81\gamma^2\eta^2+3.0025922695304064`^{\wedge}47v^4\gamma^2\eta^2-3.047818057919681`^{\wedge}82\eta^2\theta+3.7731687262728915`^{\wedge}48v^4\eta^2\theta-9.701506191253155`^{\wedge}81\gamma\eta^2\theta+1.2010369078121626`^{\wedge}48v^4\gamma\eta^2\theta-7.720213328872831`^{\wedge}80\gamma^2\eta^2\theta+9.557548035705534`^{\wedge}46v^4\gamma^2\eta^2\theta+2.4253765478132886`^{\wedge}81\eta^2\theta^2-3.0025922695304068`^{\wedge}47v^4\eta^2\theta^2+7.720213328872831`^{\wedge}80\gamma\eta^2\theta^2-9.557548035705534`^{\wedge}46v^4\gamma\eta^2\theta^2+6.143550565070237`^{\wedge}79\gamma^2\eta^2\theta^2-7.605655068603853`^{\wedge}45v^4\gamma^2\eta^2\theta^2\right)^2 / \left(\gamma^2\theta^2\left(9.701506191253155`^{\wedge}81-1.2010369078121626`^{\wedge}48v^4+7.720213328872831`^{\wedge}80\gamma-9.557548035705534`^{\wedge}46v^4\gamma-7.720213328872831`^{\wedge}80\theta+9.557548035705534`^{\wedge}46v^4\theta-6.143550565070237`^{\wedge}79\gamma\theta+7.605655068603853`^{\wedge}45v^4\gamma\theta\right)^2\right)}\right),
  {\gamma, 0, \pi}, {\eta, 0, 1}, {\theta, 0, \pi/2}], {v, 0,
10^
8}]$ 
```



$$\begin{aligned}
 & \left( \left( \sqrt{8.987551787368176 \cdot 10^{16} r^2 \alpha^2 - 8.987551787368176 \cdot 10^{16} r^2 \delta^2 - 1.7975103574736352 \cdot 10^{17} r z \alpha \theta + 8.987551787368176 \cdot 10^{16} z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot 10^{16} z^2 \theta^2} \right) \right) / \\
 & \left( \sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right) \\
 \text{Solve} & \left[ \left( \sqrt{3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2} \right) \right) / \\
 & \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) \\
 & \left( \sqrt{1.0870275225442393 \cdot 10^{50} h^2 + 3.4601160697970476 \cdot 10^{49} h^2 \gamma - 3.4601160697970476 \cdot 10^{49} r^2 \gamma + 2.7534728808995085 \cdot 10^{48} h^2 \gamma^2 - 2.7534728808995085 \cdot 10^{48} r^2 \gamma^2} \right) / \\
 & \left( \sqrt{1.209481233890674 \cdot 10^{33} h^2 + 3.849898339011711 \cdot 10^{32} h^2 \gamma - 3.849898339011711 \cdot 10^{32} r^2 \gamma + 3.0636517552749564 \cdot 10^{31} h^2 \gamma^2 - 3.0636517552749564 \cdot 10^{31} r^2 \gamma^2} \right) = \\
 & \left( \left( \sqrt{8.987551787368176 \cdot 10^{16} r^2 \alpha^2 - 8.987551787368176 \cdot 10^{16} r^2 \delta^2 - 1.7975103574736352 \cdot 10^{17} r z \alpha \theta + 8.987551787368176 \cdot 10^{16} z \delta^2 \eta^2 \theta + 8.987551787368176 \cdot 10^{16} z^2 \theta^2} \right) \right) / \\
 & \left( \sqrt{r^2 \alpha^2 - 1. \cdot r^2 \delta^2 - 2. \cdot r z \alpha \theta + z \delta^2 \eta^2 \theta + z^2 \theta^2} \right), r]
 \end{aligned}$$

# The Four Noble Truths of $\theta$ , The Hologram of Vision

by Parker Matthew Davis Emmerson

## Postulates, polar coordinates, etc.

$$\text{Sin}[\beta] = \eta / r \quad (124)$$

$$\text{Tan}[\beta] = \eta / r_1 \quad (125)$$

$$\text{Cos}[\beta] = r_1 / r \quad (126)$$

$$\eta = r \text{Sin}[\beta] \quad (127)$$

$$r = \eta / \text{Sin}[\beta]$$

$$\text{Cos}[\beta] = r_1 / r = r_1 / (\eta / \text{Sin}[\beta])$$

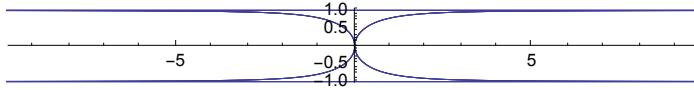
$$\text{Simplify}[r_1 / (\eta / \text{Sin}[\beta])]$$

$$\frac{\text{Sin}[\beta] r_1}{\eta}$$

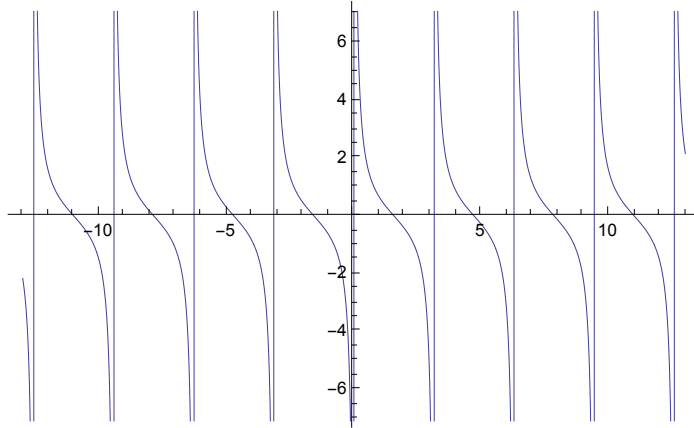
$$\frac{\text{Sin}[\beta] r_1}{\eta} = \text{Cos}[\beta]$$

$$\text{Cos}[\beta] / \text{Sin}[\beta] = \frac{r_1}{\eta}$$

$$\text{PolarPlot}[\text{Cos}[\beta] / \text{Sin}[\beta], \{\beta, -13, 13\}]$$



$$\text{Plot}[\text{Cos}[\beta] / \text{Sin}[\beta], \{\beta, -13, 13\}]$$



$$\text{Solve}[\theta r == 2 \pi (r) - 2 \pi \sqrt{((r) ^2 - \eta ^2)}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\} \right\}$$

go from the philosophy to the axioms / geometric description,  
backed up with psych and philosophy

take the geometric situation described and working out what follows.

$$\eta == \frac{\sqrt{4 \pi \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}}{2 \pi} = \text{rate} * \text{time} = \text{rate} * 6 \left( (180 / \pi) \theta \right) \quad (128)$$

$$\left\{ \left\{ r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\} \right\} \quad (129)$$

$$\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2 - \eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2 - \eta^2} \right\} \right\} \quad (130)$$

$$r_1 = \sqrt{r^2 - \eta^2} = r \cos[\beta] \quad (131)$$

There are special cases of the system when  $h = r$ , when  $\beta = \theta$ ,  
when  $r_1 = r$  (the initial condition), and when  $r_1 = h$ .

Usually, we would think that  $\beta \leq \pi / 2$ , whereas  $\theta \leq 4 \pi$ . (132)

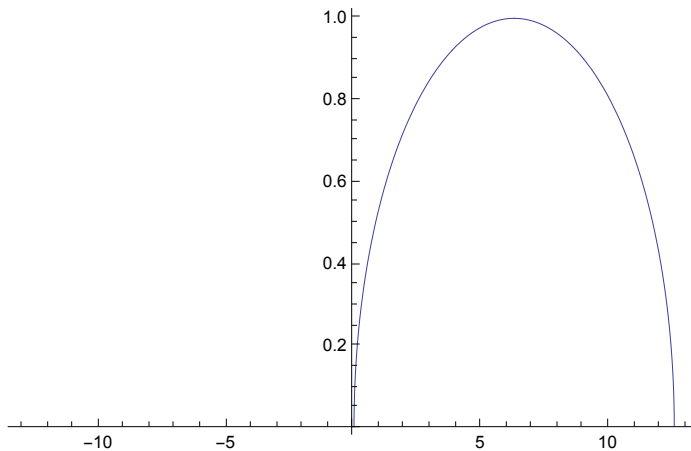
We can show that  $\theta \leq 4 \pi$  by setting  $r$  equal to one in the equation  $r = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$

$\beta \leq \pi / 2$  comes from the fact that when the cone folds all the way up,  
it makes a right angle with the x axis.

$$\text{Solve}\left[1 == \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \eta\right]$$

$$\left\{ \left\{ \eta \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right\} \right\}$$

$$\text{Plot}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}, \{\theta, -13, 13\}\right]$$



There is a particularly interesting special case of the system, however,



when the square of the height of the cone is equal to the area of the base of the cone.

## So What's the Point? How to Find the Four Noble $\theta$ Solutions, or Truths of $\theta$ .

$$r_1 = \sqrt{r^2 - \eta^2}$$

$$\eta = r \sin[\beta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\}$$

$$\left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right)^2 = \eta^2$$

$$\left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right)^2$$

$$\frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}$$

$$\frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2} = \pi (r_1^2) = \pi (r^2 - \eta^2) = \pi \left( r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2} \right)$$

$$\text{Solve} \left[ \pi \left( r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2} \right) == \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}, \theta \right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi} \right\}, \left\{ \theta \rightarrow \frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1 + \pi)} \right\} \right\}$$

$$\text{N} \left[ \frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi} \right]$$

$$3.19576$$

$$\text{N} \left[ \frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1 + \pi)} \right]$$

$$9.37061$$

$$\text{Solve} \left[ \pi \left( r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2} \right) == \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}, r \right]$$

$$\{\{r \rightarrow 0\}, \{r \rightarrow 0\}\}$$

Thus, we have shown that a point, by definition, is the place at which the square of the height of a cone is equal to the area of the base of the cone when talking about a transition or even a translation of

points along an axis. We have also shown that the point has an inherent angle of  $\frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1+\pi)}$  and  $\frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi}$  radians.

So, what does  $\theta r$  look like now?

$$\theta r = r \frac{4\pi + 4\pi^2 + \sqrt{16\pi^2 + 16\pi^3}}{2(1+\pi)}, r \frac{4\pi + 4\pi^2 - \sqrt{16\pi^2 + 16\pi^3}}{2 + 2\pi}$$

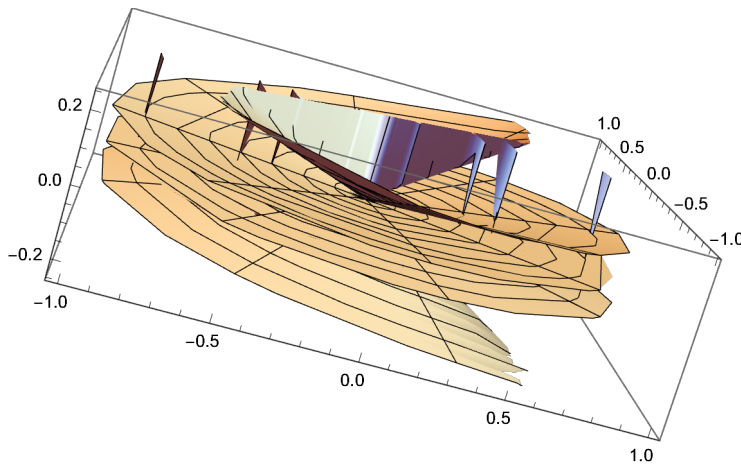
$$v = \lambda v = r (1 / (1080 / \pi) \theta) = D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right]$$

The velocity of  $\eta$  is equal to the first derivative of  $\eta$  with respect to time.

$$D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right]$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$\text{RevolutionPlot3D} \left[ \frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -13, 13\} \right]$$



$$\text{Solve} \left[ \frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}} == r (1 / (1080 / \pi) \theta), \theta \right]$$

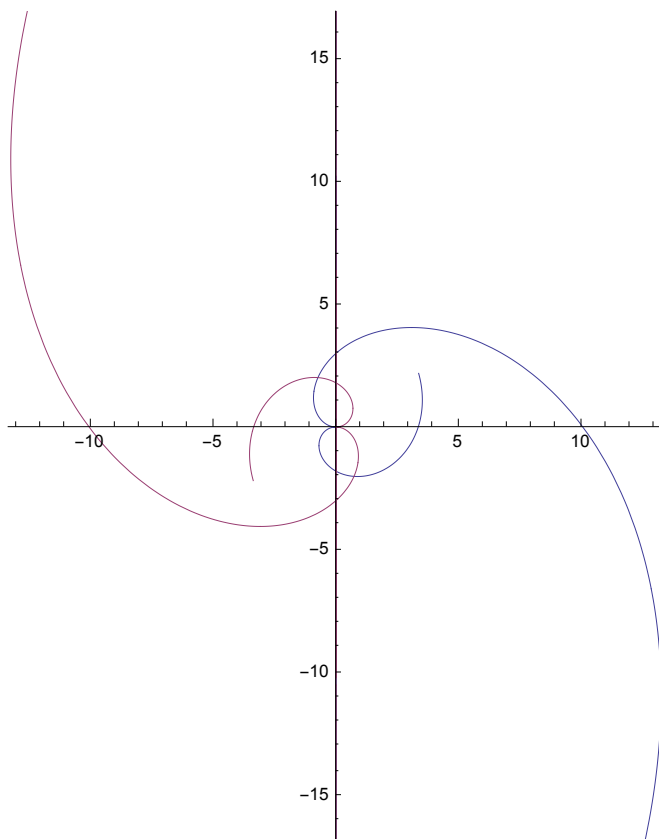
$$\left\{ \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( -\frac{194400}{\pi^4} + 4\pi^2 + \frac{1}{\pi^4} 28343520000 \left( 2 / \left( 49589822592000000 + 503884800\pi^{12} + \sqrt{(499751156776108032000000\pi^{12} + 253899891671040000\pi^{24})} \right) \right)^{1/3} + \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49589822592000000 + 503884800\pi^{12} + \sqrt{(499751156776108032000000\pi^{12} + 253899891671040000\pi^{24})} \right) \right)^{1/3} \right\} \right\}$$

$$\begin{aligned}
& \frac{1}{2} \sqrt{\left( -\frac{388\,800}{\pi^4} + 8\pi^2 - \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 / \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} - \right. \\
& \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} - \right. \\
& \quad \left( \frac{4\,665\,600}{\pi^3} + 64\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{194\,400}{\pi^4} + 4\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000 \right. \right. \\
& \quad \left. \left. \left( 2 / \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} + \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + \right. \right. \right. \\
& \quad \left. \left. \left. 503\,884\,800\pi^{12} + \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} \right) \Bigg\}, \\
& \left\{ \theta \rightarrow \pi - \frac{1}{2} \sqrt{\left( -\frac{194\,400}{\pi^4} + 4\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 / \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} + \right. \\
& \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} \right) + \\
& \quad \frac{1}{2} \sqrt{\left( -\frac{388\,800}{\pi^4} + 8\pi^2 - \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 / \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} - \right. \\
& \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} - \right. \\
& \quad \left( \frac{4\,665\,600}{\pi^3} + 64\pi^3 \right) / \left( 4 \sqrt{\left( -\frac{194\,400}{\pi^4} + 4\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000 \right. \right. \\
& \quad \left. \left. \left( 2 / \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} + \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + \right. \right. \right. \\
& \quad \left. \left. \left. 503\,884\,800\pi^{12} + \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + \right. \right. \right. \\
& \quad \left. \left. \left. 253\,899\,891\,671\,040\,000\pi^{24} \right)} \right) \right)^{1/3} \right) \Bigg\},
\end{aligned}$$

$$\begin{aligned} & \left\{ \Theta \rightarrow \pi + \frac{1}{2} \sqrt{\left( -\frac{194\,400}{\pi^4} + 4\pi^2 + \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 \Big/ \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right) \right) \right)^{1/3} + \right. \\ & \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right) \right) \right)^{1/3} \right) + \\ & \quad \frac{1}{2} \sqrt{\left( -\frac{388\,800}{\pi^4} + 8\pi^2 - \frac{1}{\pi^4} 28\,343\,520\,000 \left( 2 \Big/ \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{\left( 49\,975\,115\,677\,610\,803\,200\,000\,000\pi^{12} + 253\,899\,891\,671\,040\,000\pi^{24} \right) \right) \right)^{1/3} - \right. \\ & \quad \left. \frac{1}{3\pi^4} \left( \frac{1}{2} \left( 49\,589\,822\,592\,000\,000 + 503\,884\,800\pi^{12} + \right. \right. \right. \end{aligned}$$



$$\text{PolarPlot}\left[\left\{-\frac{270\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2\sqrt{\theta}},\frac{270\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2\sqrt{\theta}}\right\},\{\theta,-10,10\}\right]$$



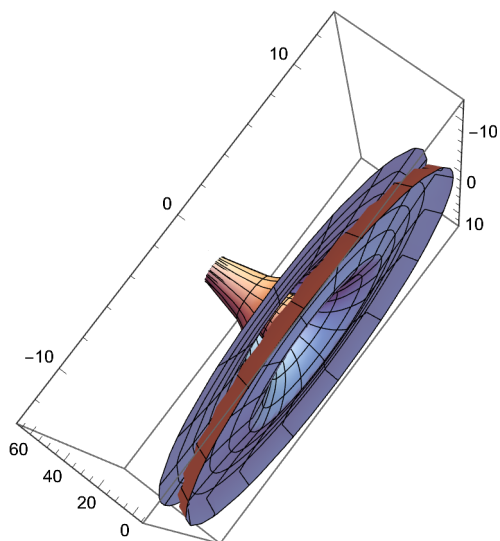
$$\sqrt{r^2-\eta^2}$$

$$\frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}}=r=\frac{270\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2\sqrt{\theta}}$$

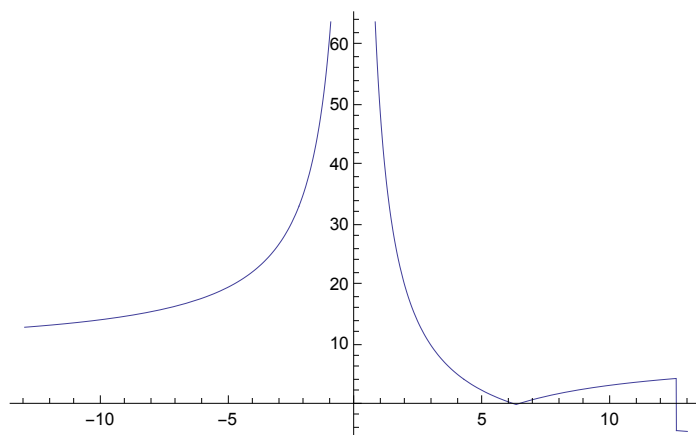
$$\text{Solve}\left[\frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}}==\frac{270\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{\pi^2\sqrt{\theta}},\eta\right]$$

$$\left\{\left\{\eta\rightarrow\frac{135\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}\sqrt{4\pi\theta-\theta^2}}{\pi^3\sqrt{\theta}}\right\}\right\}$$

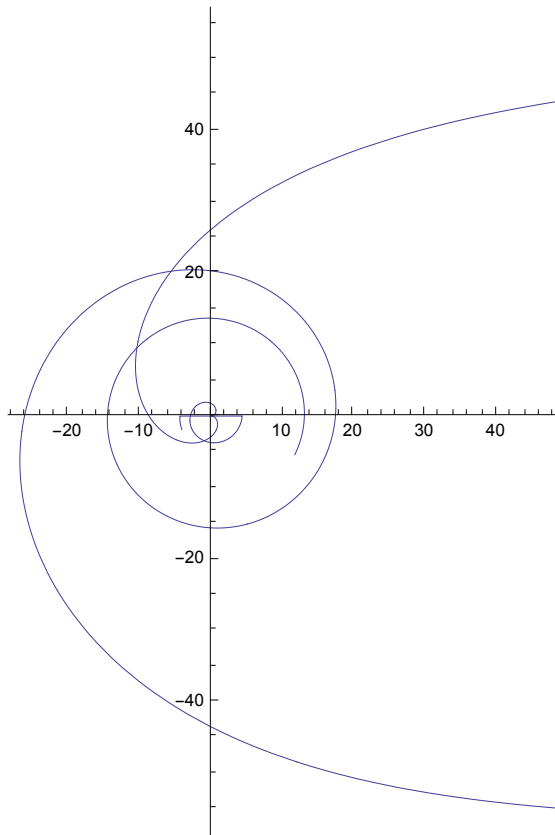
$$\text{RevolutionPlot3D}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$$



$$\text{Plot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$$

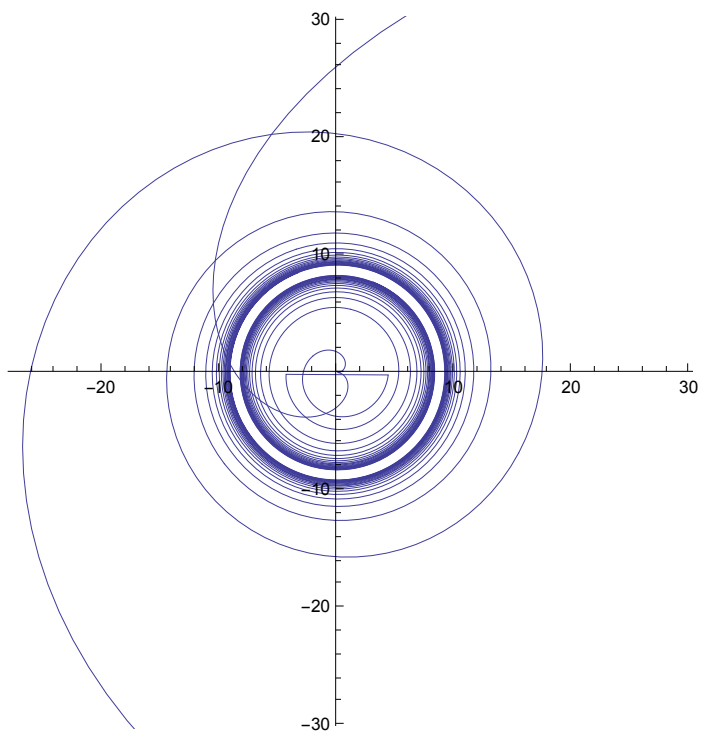


$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13, 13\}\right]$$

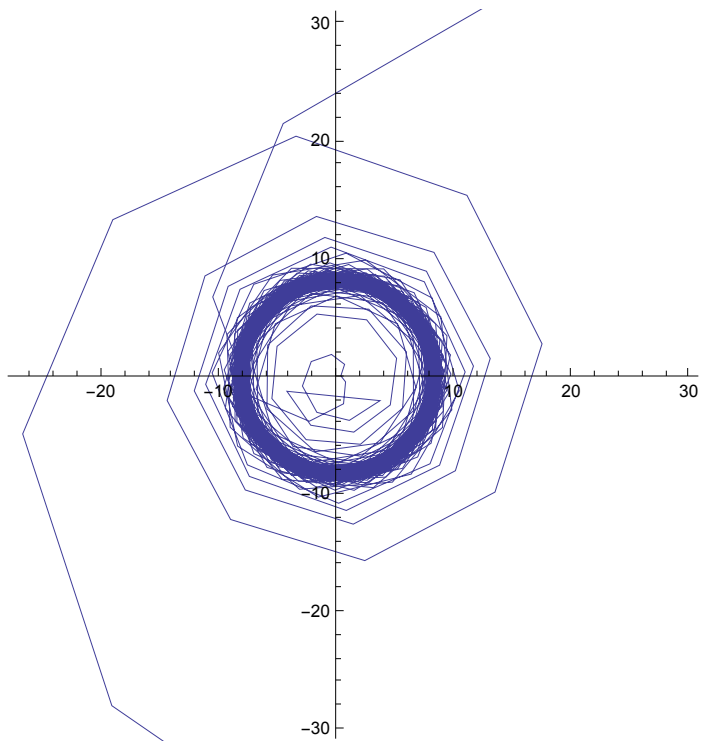




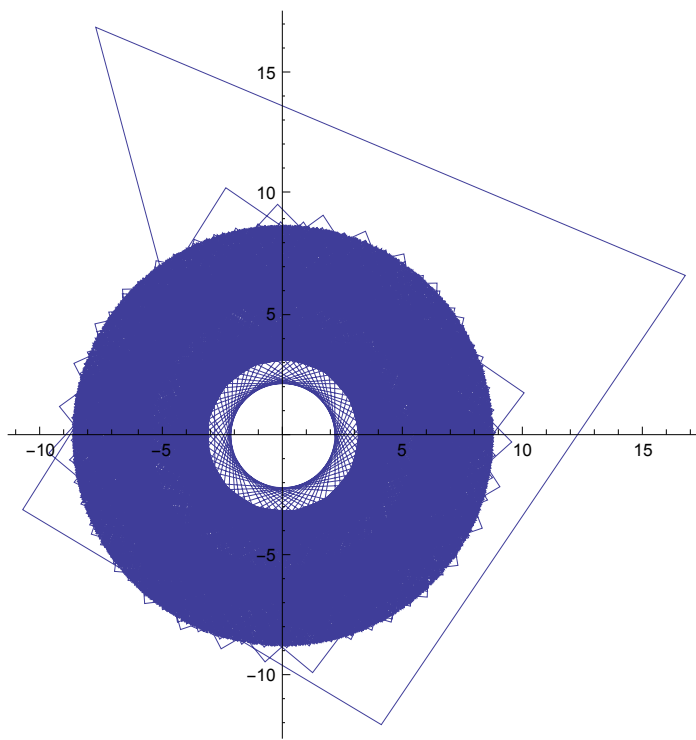
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -130, 130\}\right]$$



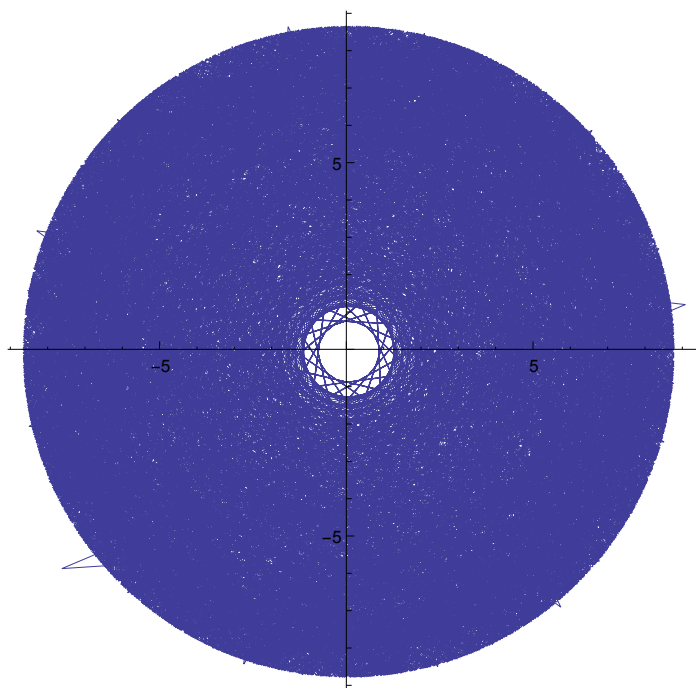
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -1300, 1300\}\right]$$

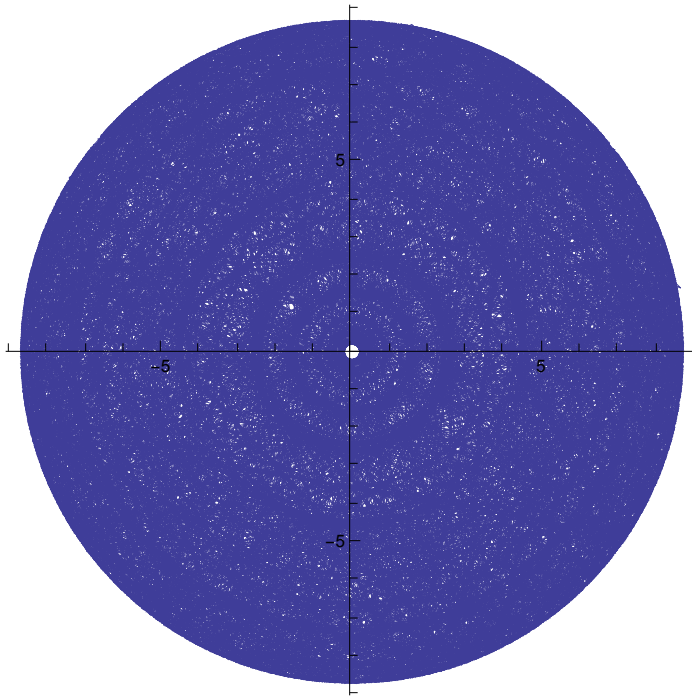


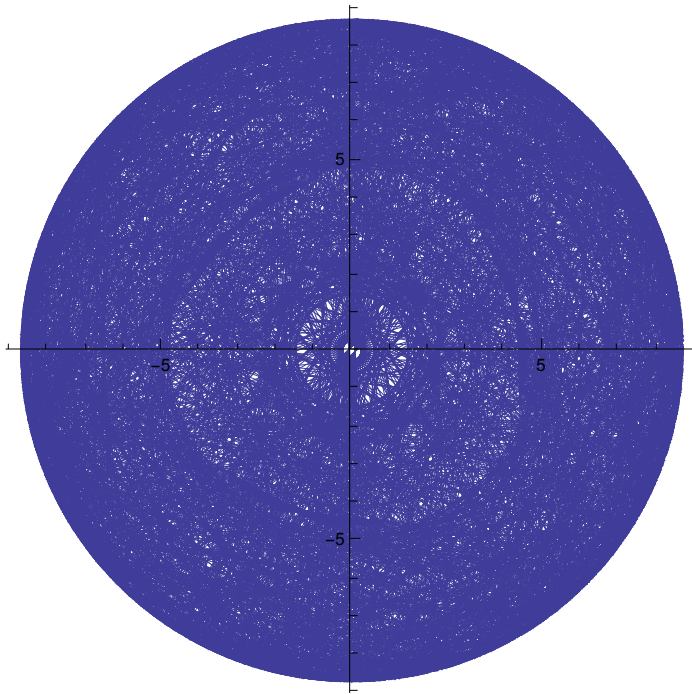
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13000, 13000\}\right]$$



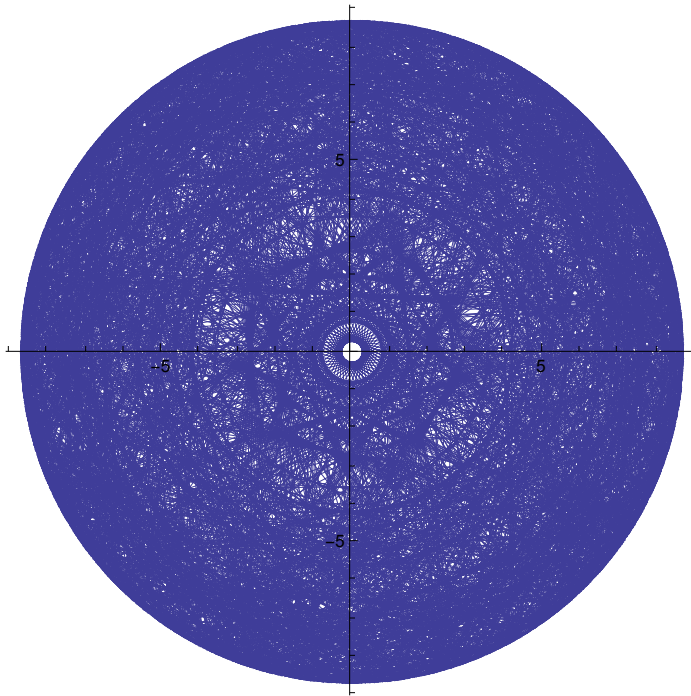
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -130000, 130000\}\right]$$



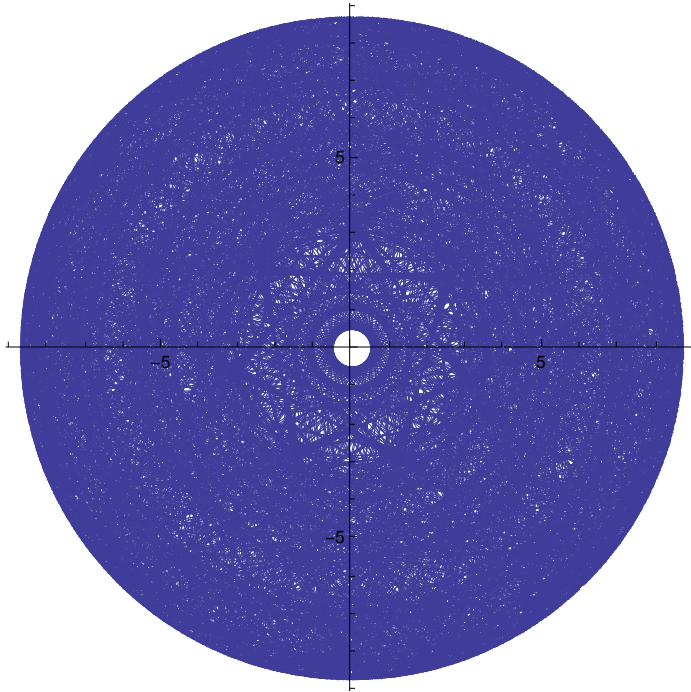
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -1300000, 1300000\}\right]$$


$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -13000000, 13000000\}\right]$$


$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -130\,000\,000, 130\,000\,000\}\right]$$



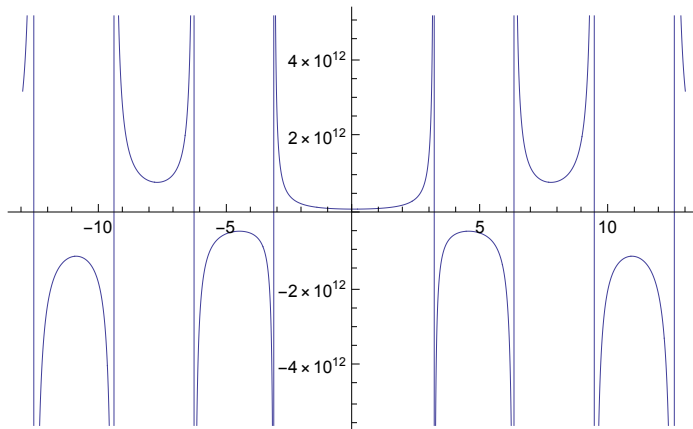
$$\text{PolarPlot}\left[\frac{135 \sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{\pi^3 \sqrt{\theta}}, \{\theta, -1\,300\,000\,000, 1\,300\,000\,000\}\right]$$



$$\text{Solve}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} == \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}, r\right]$$

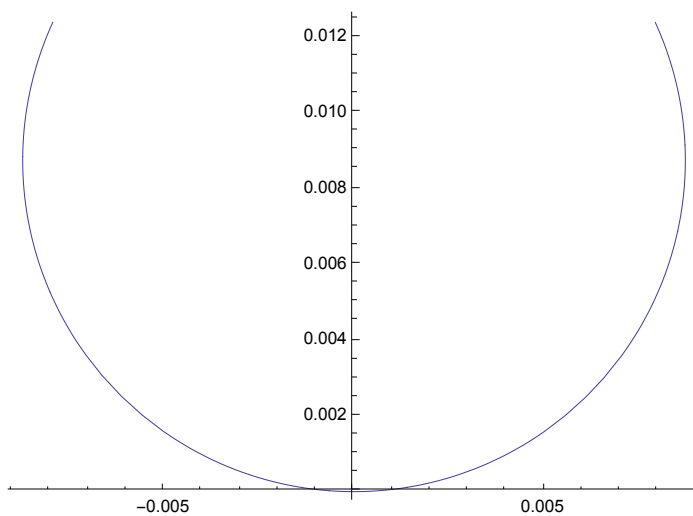
$$\left\{\left\{r \rightarrow \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right\}\right\}$$

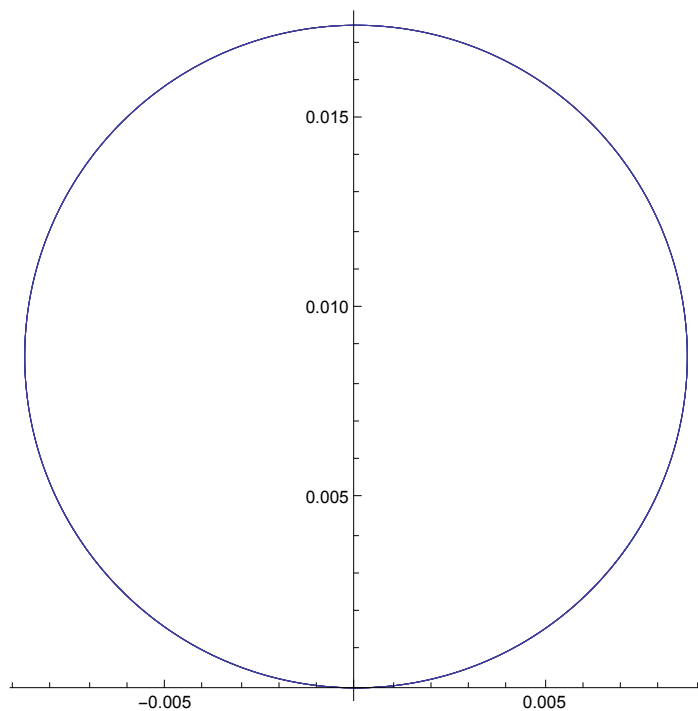
$$\text{Plot}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}, \{\theta, -13, 13\}\right]$$

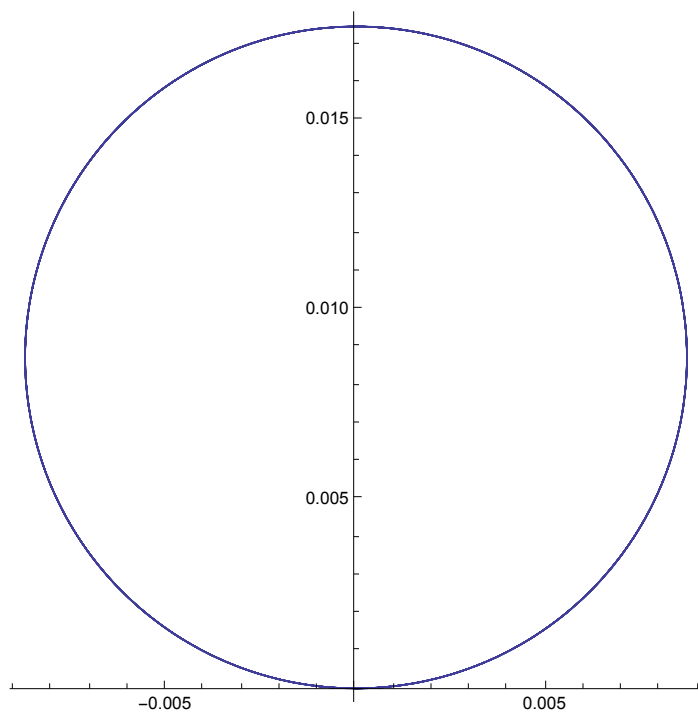


$$\left\{\left\{n \rightarrow \frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}\right\}\right\}$$

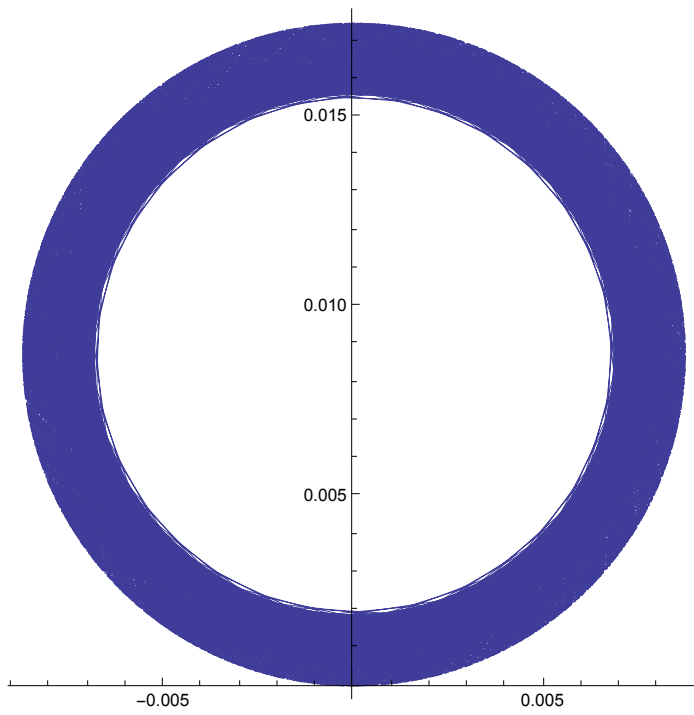
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}, \{\theta, -1, 1\}\right]$$



$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10, 10\}\right]$$


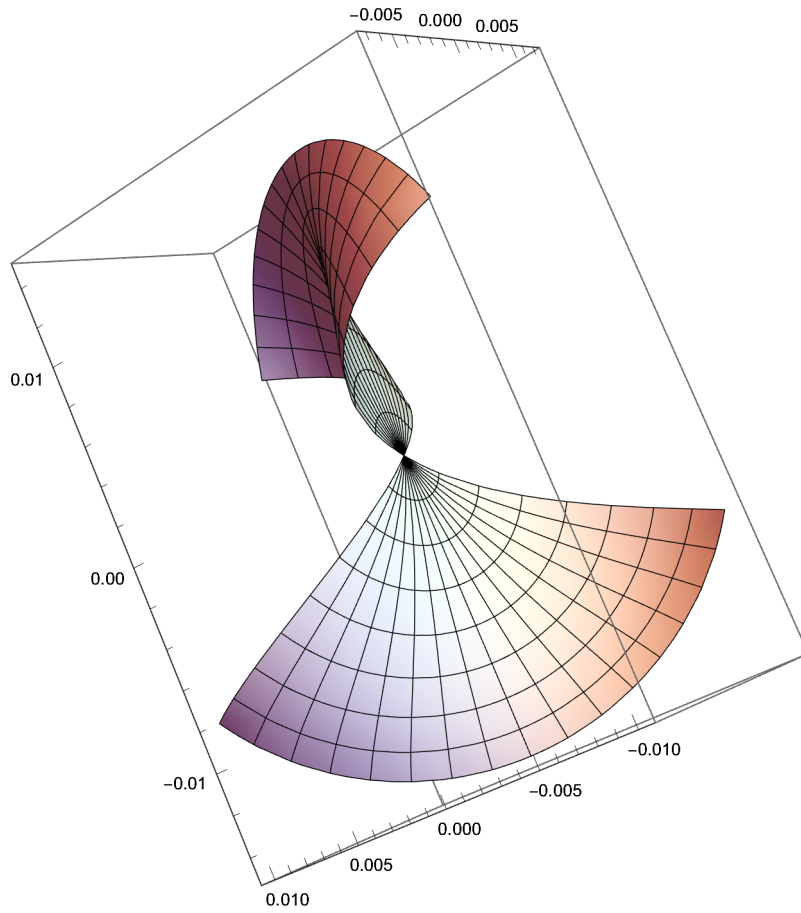
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -100, 100\}\right]$$


`PolarPlot` $\left[\frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}, \{\theta, -1000, 1000\}\right]$

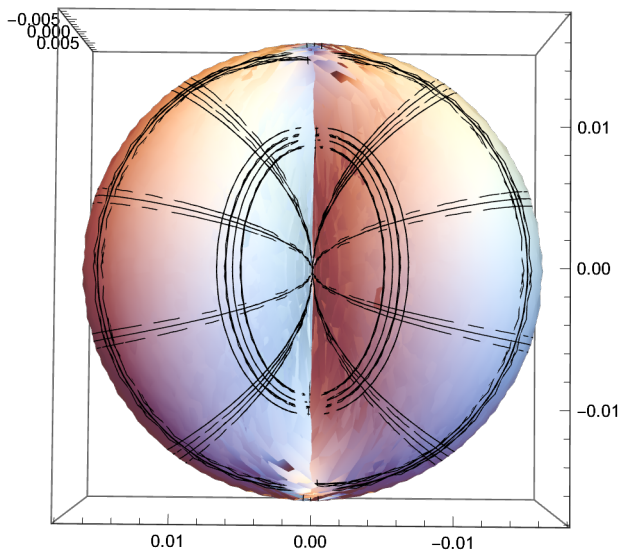




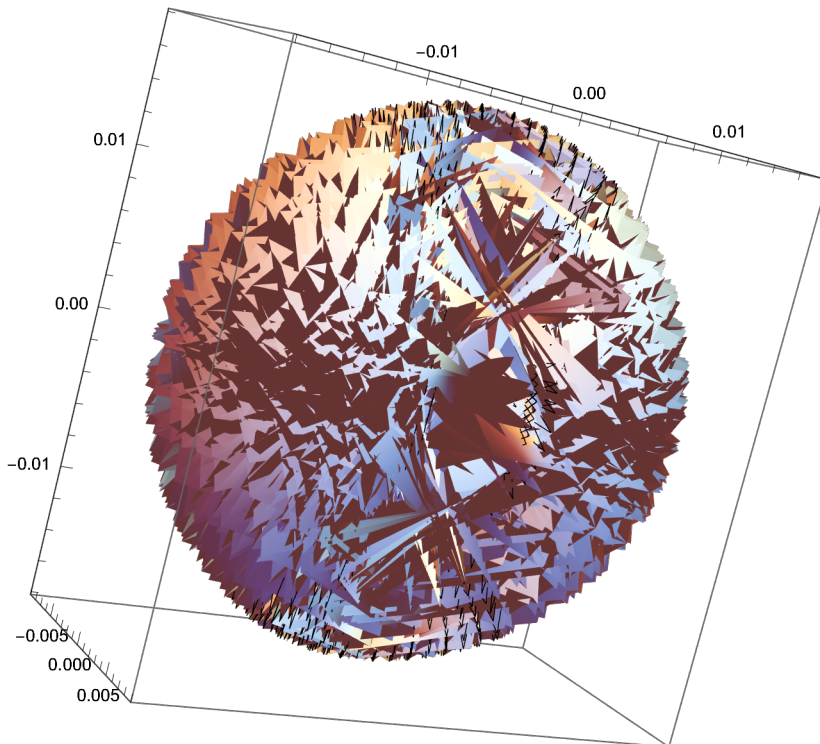
$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1, 1\}, \{\beta, -1, 1\}\right]$



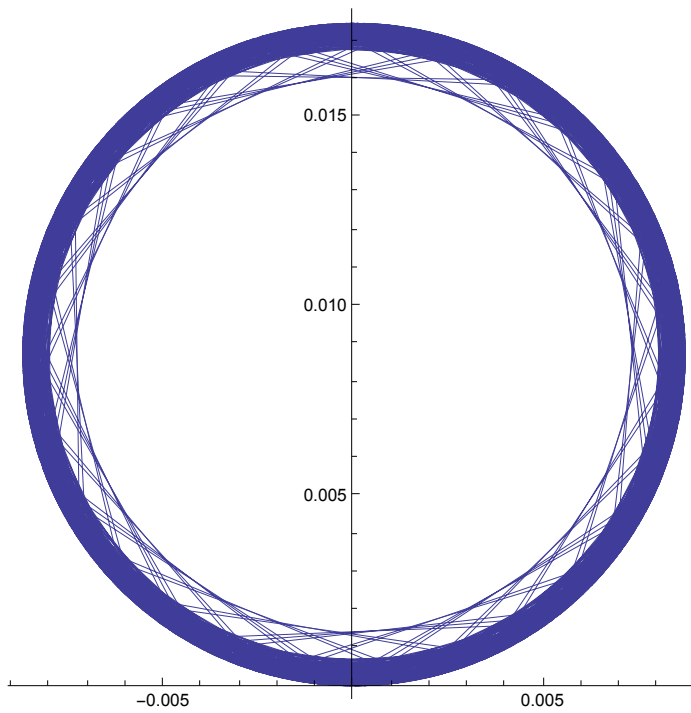
$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10, 10\}, \{\beta, -10, 10\}\right]$



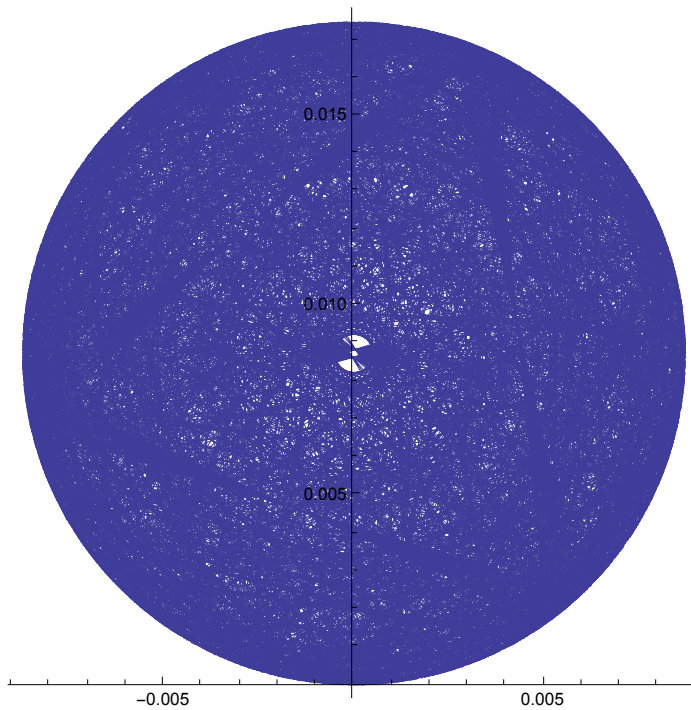
`SphericalPlot3D` $\left[\frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4 \pi - \theta) \theta}}, \{\theta, -100, 100\}, \{\beta, -100, 100\}\right]$

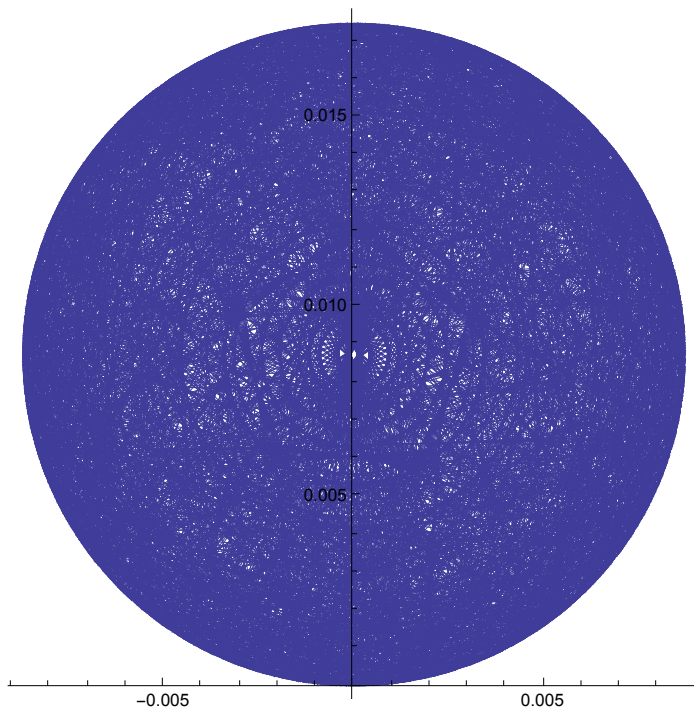


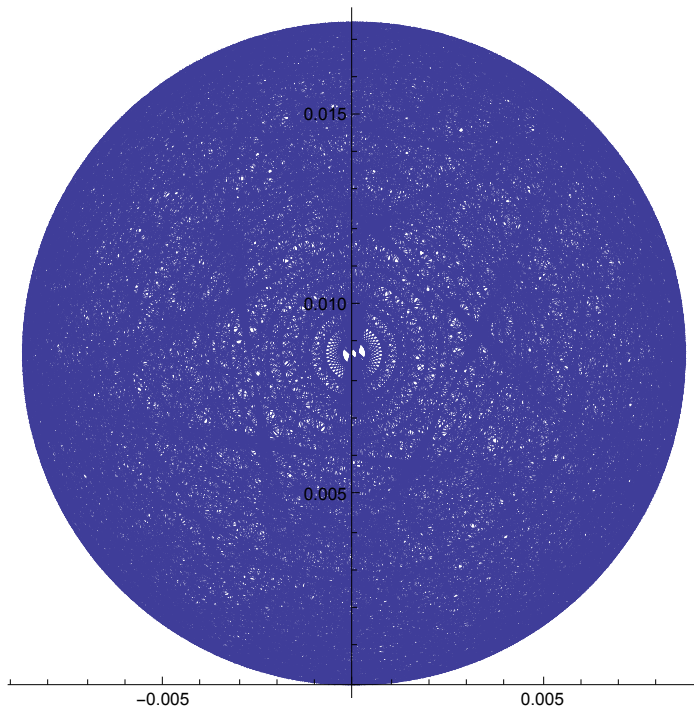
$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10\,000, 10\,000\}\right]$



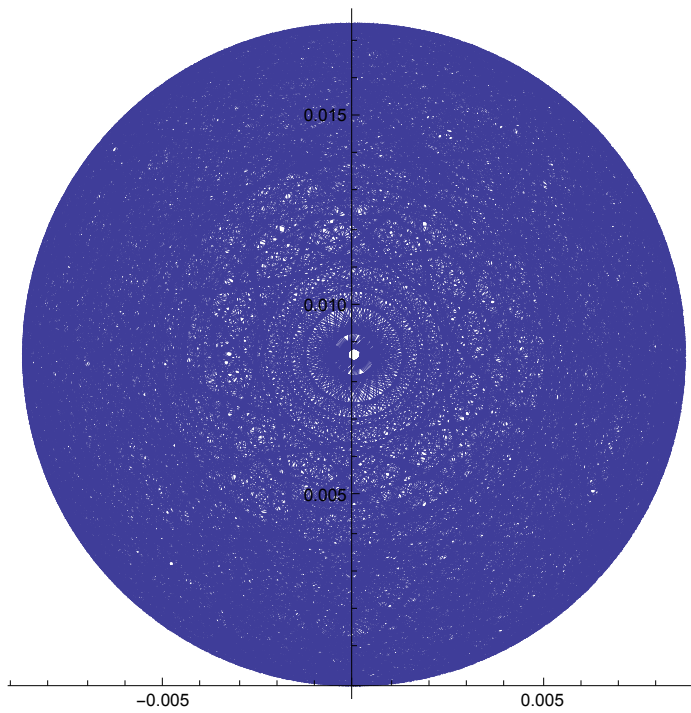
$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -100\,000, 100\,000\}\right]$



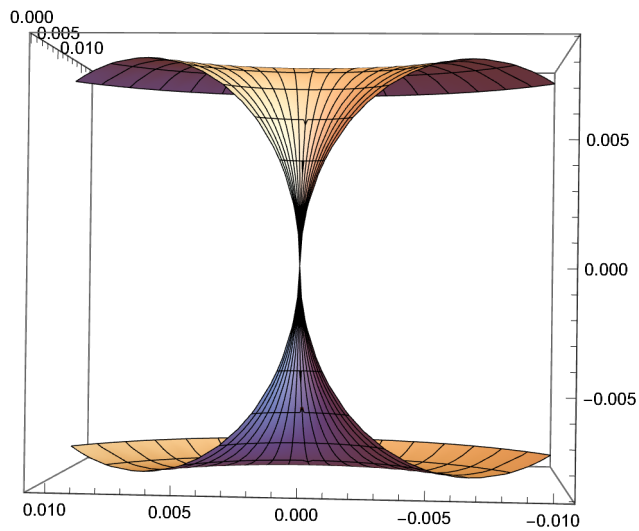
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1\,000\,000, 1\,000\,000\}\right]$$


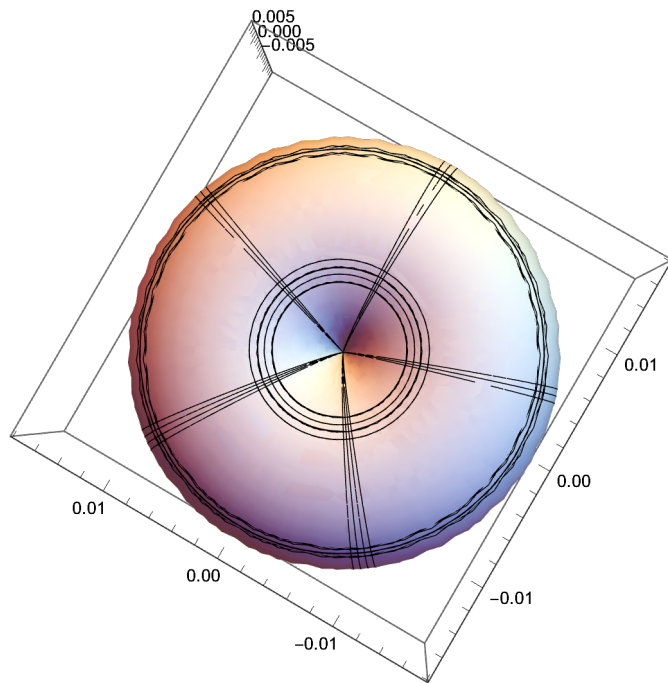
$$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -10\,000\,000, 10\,000\,000\}\right]$$


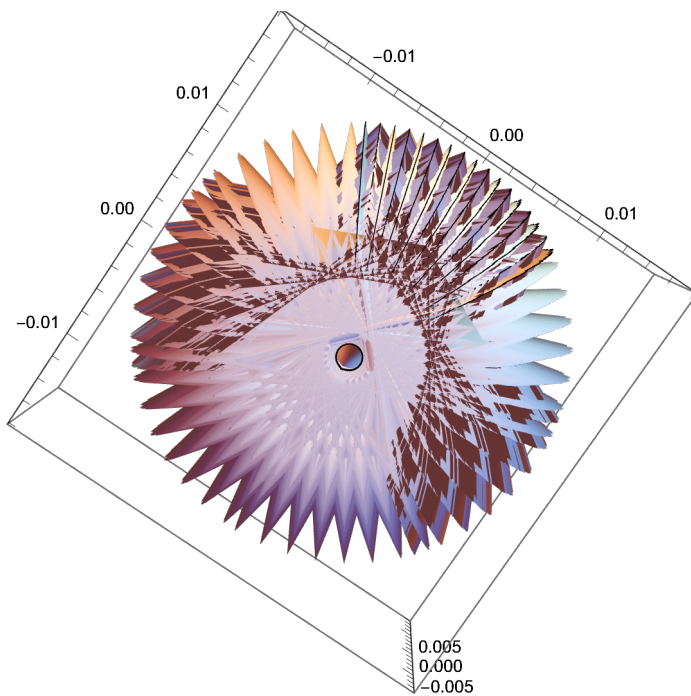
$\text{PolarPlot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -100\,000\,000, 100\,000\,000\}\right]$



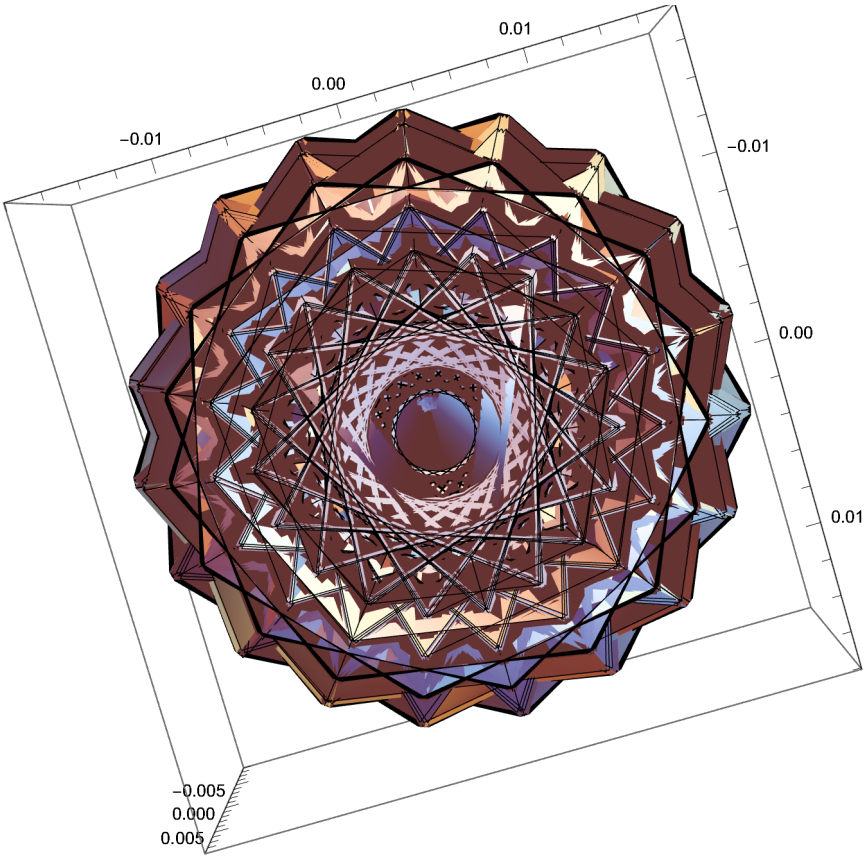
$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -1, 1\}, \{\theta, -1, 1\}\right]$



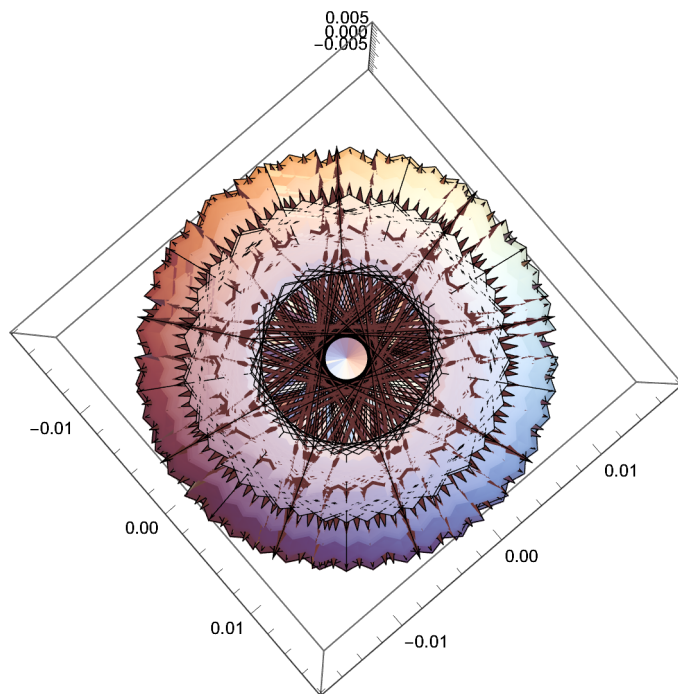
$$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -10, 10\}, \{\theta, -10, 10\}\right]$$


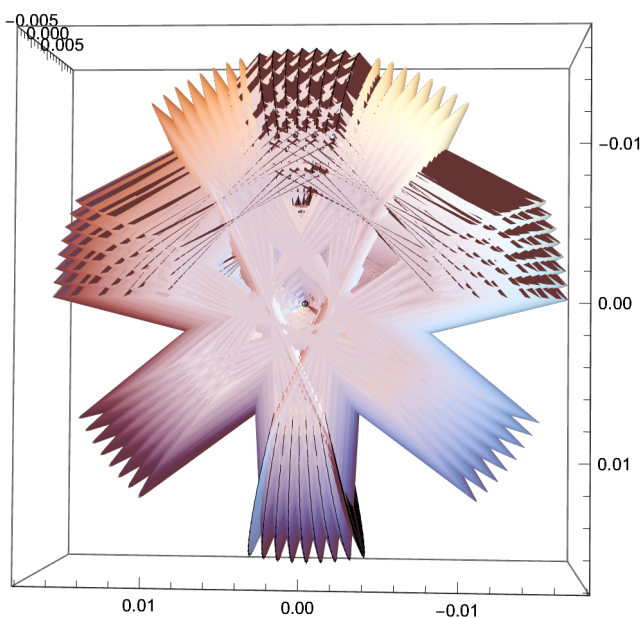
$$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -100, 100\}, \{\theta, -100, 100\}\right]$$


`SphericalPlot3D` $\left[\frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \operatorname{Sin}[\beta]}{180 \sqrt{(4 \pi - \theta) \theta}}, \{\beta, -1000, 1000\}, \{\theta, -1000, 1000\}\right]$





$$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -10\,000, 10\,000\}, \{\theta, -10\,000, 10\,000\}\right]$$


$$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -100\,000\,000, 100\,000\,000\}, \{\theta, -100\,000\,000, 100\,000\,000\}\right]$$




## Special Case 1, $\theta = \beta$

Some velocity, which is the first derivative of the equation for  $\theta r$ , is the angular velocity, and is equal to a wavelength of frequency. Some velocity, which is the first derivative of  $r$  is the transitional velocity, and is equal to a the distance,  $r$  being a wavelength,

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\}$$

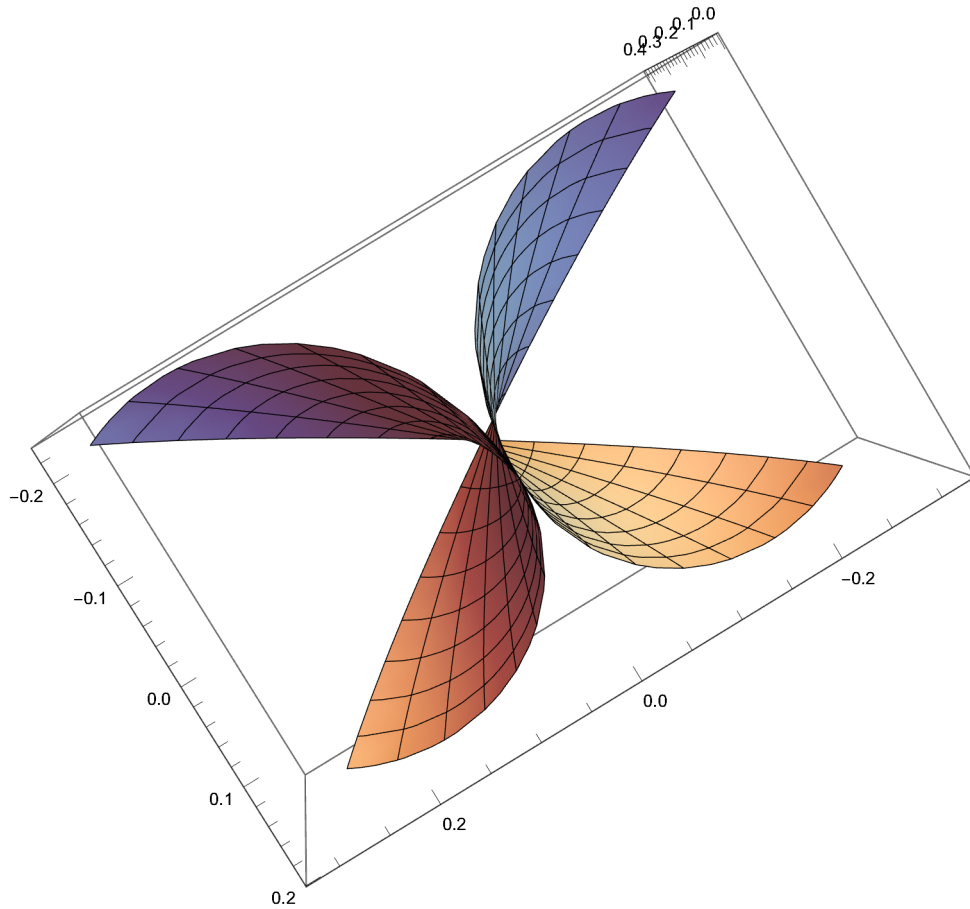
$$\eta = r \sin[\beta]$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} \right\} \right\}$$

$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\} \right\}$$

SphericalPlot3D[

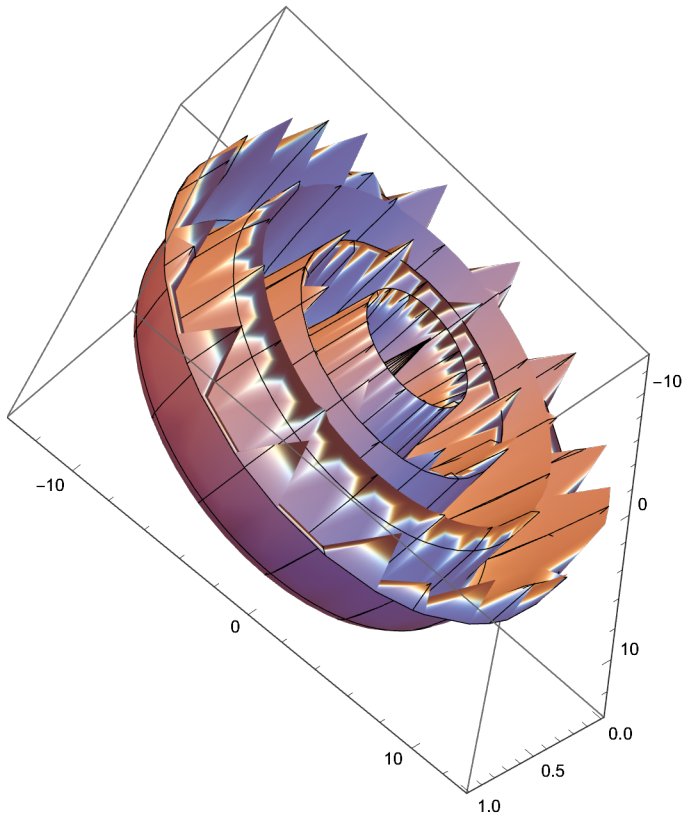
$$\sqrt{4 \pi \left( \frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}, \{\theta, -1, 1\}, \{\beta, -1, 1\}]$$



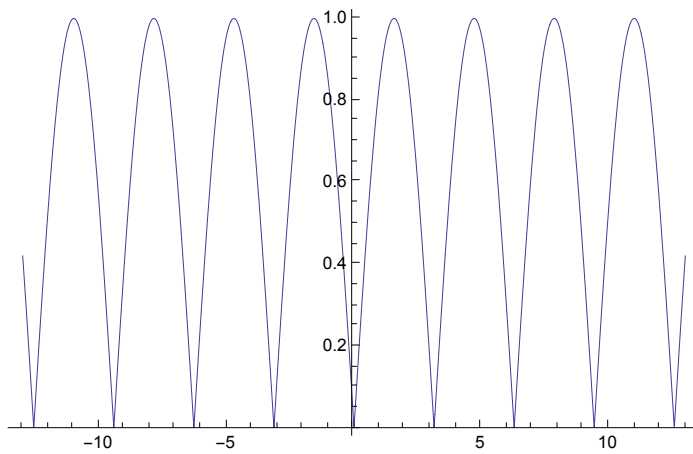
$$\sqrt{4 \pi \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2} =$$

$$\sqrt{4 \pi \left( \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2} = \sqrt{4 \pi \left( \frac{2 \pi (r) \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi (r) \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-13,13\}\right]$$



$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-13,13\}\right]$$



$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} = \left(\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right), \theta\right]$$

$$\left\{\{\theta \rightarrow 2\pi\},\right.$$

$$\left\{\theta \rightarrow -\left(\frac{2}{1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}}\right)^{1/3} + \frac{\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{12\pi^2}\right\},$$

$$\left\{\theta \rightarrow -\frac{(1+i\sqrt{3})\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{24\pi^2} +$$

$$\frac{1-i\sqrt{3}}{2^{2/3}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)^{1/3}}\right\},$$

$$\left\{\theta \rightarrow -\frac{(1-i\sqrt{3})\left(\frac{1}{2}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)\right)^{1/3}}{24\pi^2} +$$

$$\frac{1+i\sqrt{3}}{2^{2/3}\left(1728\pi^5 + \sqrt{6912\pi^6 + 2985984\pi^{10}}\right)^{1/3}}\right\}\}$$

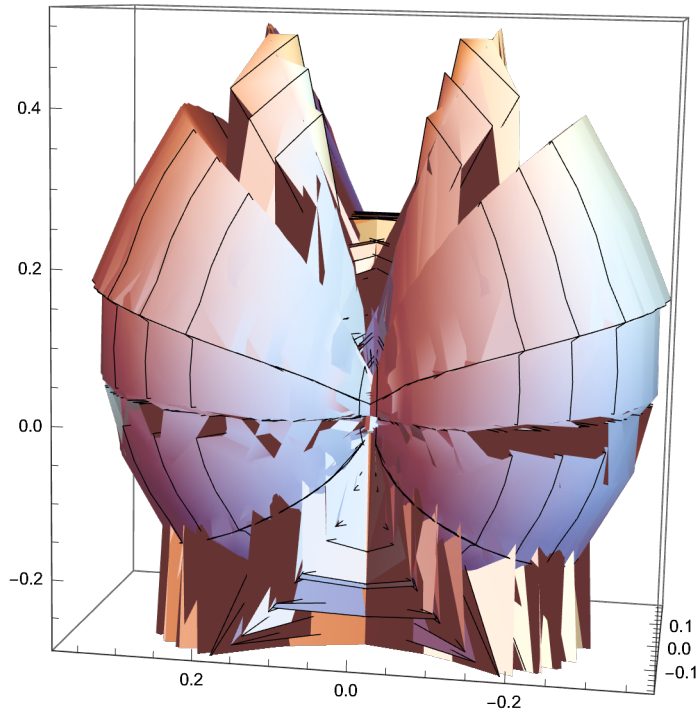
$$\sqrt{\frac{4\pi\left(\frac{2\pi\left(\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]\right)^2}{\sqrt{4\pi\theta-\theta^2}}\theta - \left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi} =$$

$$r = \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}$$

$$\left\{\left\{r \rightarrow -\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right\}, \left\{r \rightarrow \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}}\right\}\right\}$$

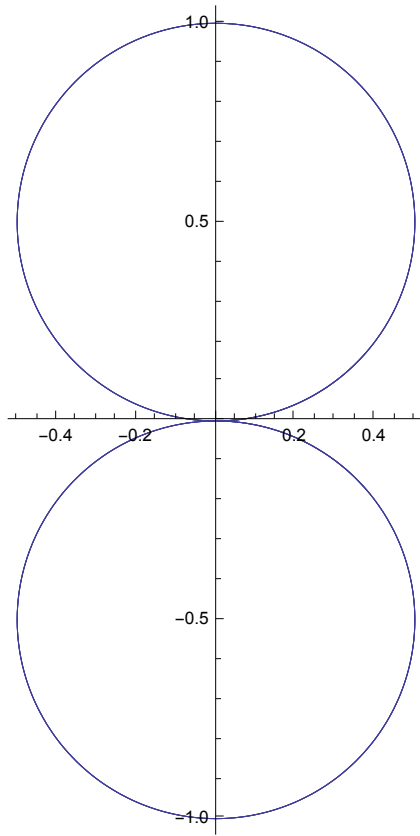
$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\frac{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\right. \\ \left.\{\theta,-360,360\},\{\beta,-360,360\}\right]$$

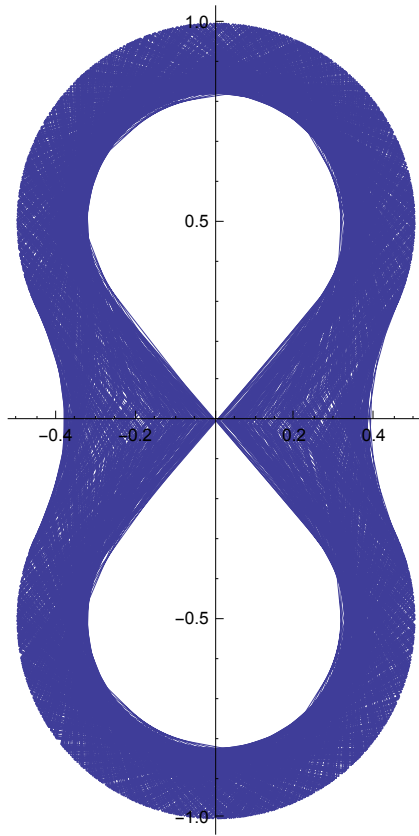


$$\text{SphericalPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\left(\frac{\sqrt{1+\frac{4\pi^2}{(4\pi-\theta)^2}-\frac{4\pi}{4\pi-\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\left(\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\right. \\ \left.\{\theta,-360,360\},\{\beta,-360,360\}\right]$$

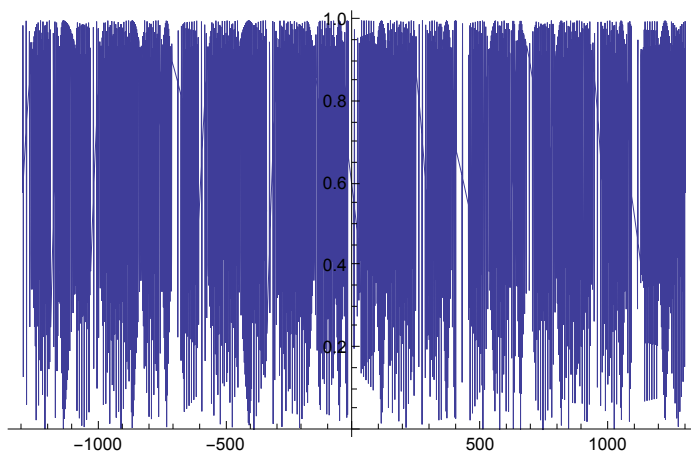
$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



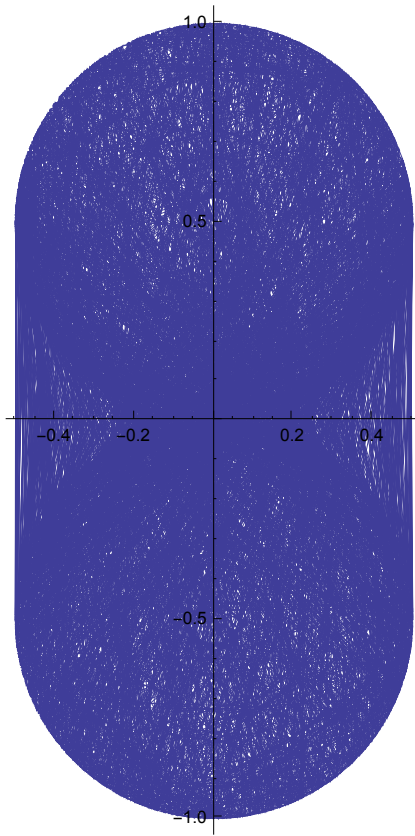
$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-1300,1300\}\right]$$



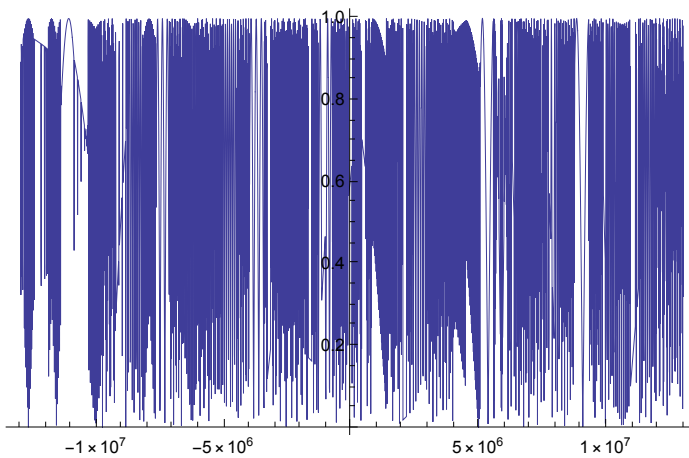
$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta-\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi},\{\theta,-1300,1300\}\right]$$



$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi}, \{\theta, -13\,000\,000, 13\,000\,000\}\right]$$



$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta - \left(\frac{2\pi\sin[\theta]}{\sqrt{4\pi\theta-\theta^2}}\right)^2\theta^2}}{2\pi}, \{\theta, -13\,000\,000, 13\,000\,000\}\right]$$



Contour is said to be the experience of this kind of polar equation from information available in light. Light is interpreted in the polar coordinate system by a human being when perception occurs. How it is



interpreted depends partially on how you see something. For instance, I can see this graphed contour like a cylinder or two spheres. We call this a conisphinder. It's holographic characteristic is the first special case.

# The Geometric Pattern of Perception of the Moon from beneath the Legs.

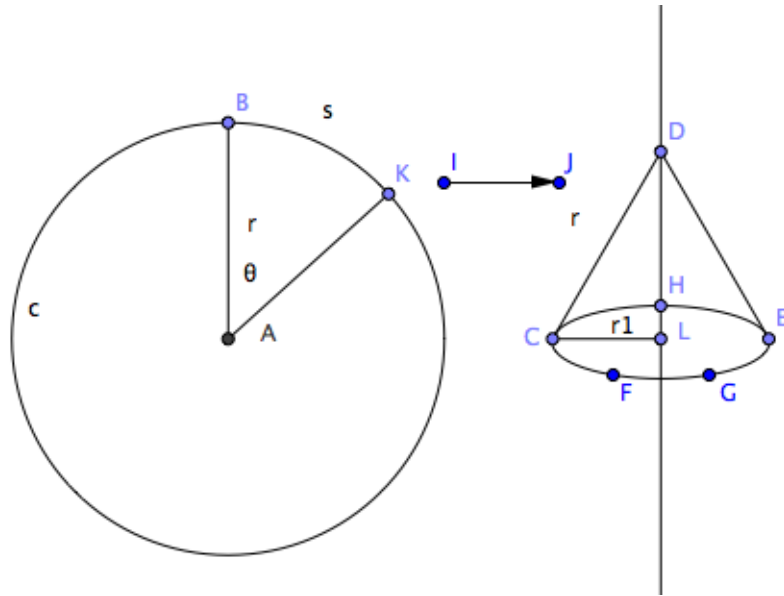
by Parker Emmerson

From Perception of the Environment with Tom Toleno

Perception would and could only be perceived as the inception and or acceptance of the information provided by the individual or individuals through any giving persona section of reality. In this paper, I will discuss how Gibson's theory of the ambient optic array, in combination with mathematical inquiry of the experience, will act like a thought experiment for understanding the reason behind the illusion that, when you look at the moon through your legs, you will see that it looks smaller than when you see it from a standing position. Specifically, we will attempt to answer the question of, "how can perceived change in size, theoretically relating to a change in distance, be accounted for even though the change in distance does not actually occur"?

When people look up in the sky from a standing position, a clear and accessible visual structure presents the opportunity for relatively accurate depth perception and size discernment. The object being perceived takes the shape of a circle or orb in the sky, which is the moon. However, when the body is turned upside down and the eye strains to move about searching for or focusing on external stimuli, the visual structure is depleted. It was shown that by G. M. Stratton that, for voluntary eye motions, following a moving object was anything but predicatble. The conclusion from Stratton's experiments pertains to the phenomenon of the moon's looking smaller from upside down beneath the legs, because it shows us that, "reception of visual structures is possible only for the eye at rest" (The Perceptual World by Wolfgang Metzger 63). We will now use mathematics to describe the visual structure of the variables relating to depth perception and measurement of the size of a circle or orb.

First, we postulate that :



The diagram is not drawn to scale with regard to theta or an actual transformation of this sort. This diagram is a representation of a geometric structure and a system that has complex implications. If an object or wavelength progresses through the height of the cone, it is said to be traveling through theta in terms of time. However, it should be noted that the circle does not have to fold all the way up in order for the max height of  $r$  to be achieved for variables to maintain their correlation. This is said to be an *invariance* of the system. The position is also said to have an initial radius of a max of the height of the cone during a given instance. It is a structure that I propose may be present in every point of the ambient optic array, and one that also has clear cut geometric relations *through* the folding of space-time. It also acts like an observable metaphor for how discernment of the size of a massive orb in space occurs and can change with context.

The parameters of the system for the purposes of this discussion are:

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle, the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + h^2$$

This is the initial radius squared expressed as the slant of the cone in terms of the height of the cone,  $h$ , and the radius of the base of the cone,  $r_1$

$$r = \sqrt{(r_1^2 + h^2)}$$

$$s = \theta r$$

$$s / \theta = r$$

The arc length taken out of a circle at a given time is =

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \quad \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - h^2$$

$$r_1 = \sqrt{(r^2 - h^2)}$$

$$h < r$$

$\tau = \text{time}$

1 second = 6 degrees

$\tau = 6 \theta$

I will now do some algebra to conclude what the height of the cone is in terms of the initial parameters. It can eventually be reduced to a single variable.

**Solve** $[r_1^2 + h^2 = r^2, h]$

$$\left\{ \left\{ h \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ h \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\}$$

$(\tau / \theta) = r$

We will propose that for our system, it is true that this correlation pertains :

**Solve** $[$

$$\theta = \left( \left( 2 \pi (r) - 2 \pi \sqrt{\left( (r)^2 - \left( \left( \frac{2 \sqrt{r^2 (2 \pi - (\theta)) (\theta)} }{\sqrt{r^2 (4 \pi - \theta) \theta}} \right) \left( \frac{\sqrt{(2 (r))^2 (2 \pi - \theta) \theta}}{2 \pi} \right)^2 \right) \right)} \right) / r \right), \theta]$$

$$\left\{ \{ \theta \rightarrow 0 \}, \left\{ \theta \rightarrow \frac{4 \pi}{3} \right\}, \left\{ \theta \rightarrow \frac{12 \pi}{5} \right\} \right\}$$

$$\left\{ \left\{ h \rightarrow -\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ h \rightarrow \frac{\sqrt{4 \pi (1)^2 \theta - (1)^2 \theta^2}}{2 \pi} \right\} \right\}$$

$$\text{PolarMap} \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \{-1, 1\}, \{-13, 13\} \right]$$

$$\text{PolarMap} \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \{-1, 1\}, \{-13, 13\} \right]$$

$$\frac{\sqrt{4 \pi (r)^2 \theta - (1)^2 \theta^2}}{2 \pi} == x($$

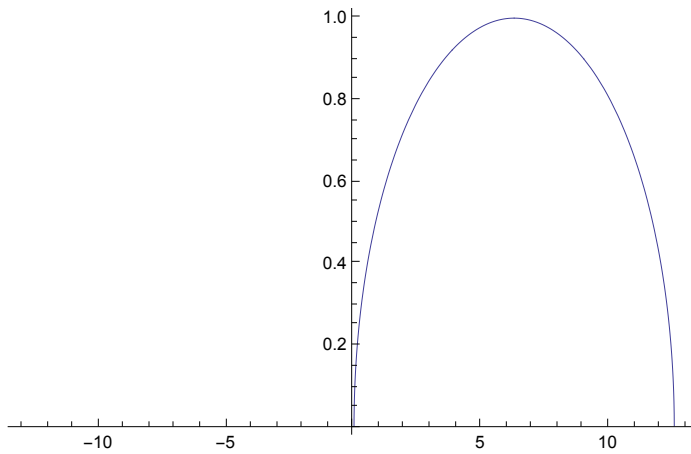
$$\text{Simplify} \left[ \frac{\sqrt{4 \pi (r)^2 \theta - (r)^2 \theta^2}}{2 \pi} \right]$$

$$\frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi}$$

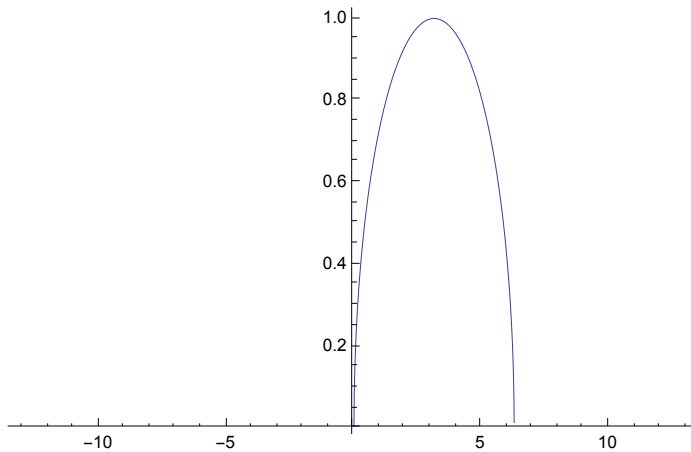
$$\text{Solve}\left[\frac{\sqrt{(2r)^2(2\pi-\theta)\theta}}{2\pi} == x \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi}, x\right]$$

$$\left\{\left\{x \rightarrow \frac{2\sqrt{r^2(2\pi-\theta)\theta}}{\sqrt{r^2(4\pi-\theta)\theta}}\right\}\right\}$$

$$\text{Plot}\left[\frac{\sqrt{4\pi(1)^2\theta-(1)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



$$\text{Plot}\left[\frac{\sqrt{2\pi(1)^2\theta-(1)^2\theta^2}}{\pi}, \{\theta, -13, 13\}\right]$$



$$\frac{2\sqrt{r^2(2\pi-\theta)\theta}}{\sqrt{r^2(4\pi-\theta)\theta}} = x$$

$$t == \pi(r) - 2\pi \sqrt{\left((r)^2 - \left(\frac{2\sqrt{r^2(2\pi-\theta)\theta}}{\sqrt{r^2(4\pi-\theta)\theta}}h\right)^2\right)}$$

$$\pi(1) - 2\pi \sqrt{\left(1^2 - \left(\frac{2\sqrt{1^2(2\pi - \theta)\theta}}{\sqrt{1^2(4\pi - \theta)\theta}}h\right)^2\right)}$$

$$t = C - C_2 = 2\pi r - 2\pi r_1 = 2\pi(r) - 2\pi\sqrt{(r)^2 - h^2}$$

$$t = 2\pi(t/\theta) - 2\pi\sqrt{(t/\theta)^2 - h^2}$$

Add  $2\pi\sqrt{(r)^2 - h^2}$  to both sides

$$t + 2\pi\sqrt{(t/\theta)^2 - h^2} = 2\pi(t/\theta)$$

Subtract  $t$  from both sides and remember that  $(t/\theta) = r$

$$2\pi\sqrt{(t/\theta)^2 - h^2} = 2\pi(t/\theta) - t = 2\pi r - t$$

Divide by  $2\pi$  on both sides.

$$(t/\theta) - t/(2\pi) = (r) - t/(2\pi) = \sqrt{(t/\theta)^2 - h^2} = \sqrt{(r)^2 - h^2} = r_1$$

$$(r) - t/(2\pi) = \sqrt{(t/\theta)^2 - h^2}$$

Square both sides. Substitute :  $(t/\theta) = r$

$$((t/\theta) - (t/(2\pi)))^2 = ((r) - (t/(2\pi)))^2 = ((t/\theta)^2 - h^2) = (r_1^2)$$

$$((r) - (t/(2\pi)))^2 = ((r)^2 - h^2)$$

Add  $h^2$  to both sides.

$$((r) - (t/(2\pi)))^2 + h^2 = (r)^2$$

Substitute :  $\theta r = t$

$$((t/\theta) - (t/(2\pi)))^2 = ((r) - (\theta * r/(2\pi)))^2$$

$$((r) - (\theta * r/(2\pi)))^2$$

$$\left(r - \frac{r\theta}{2\pi}\right)^2$$

$$\text{Expand}\left[\left(r - \frac{r\theta}{2\pi}\right)^2\right]$$

$$r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}$$

$$r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2} + h^2 = ((r) - (t/2\pi))^2 + h^2 = r^2$$

$$(r^2) - \left(r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}\right) = h^2$$

$$\text{Simplify}\left[(r^2) - \left(r^2 - \frac{r^2\theta}{\pi} + \frac{r^2\theta^2}{4\pi^2}\right)\right]$$

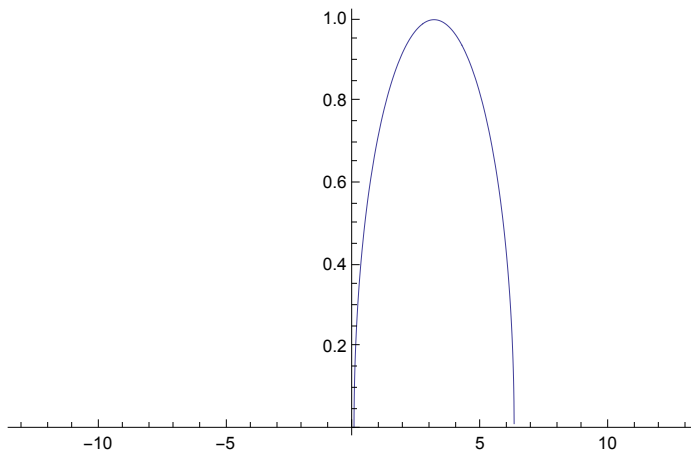
$$h^2 = \frac{r^2 (4\pi - \theta) \theta}{4\pi^2}$$

$$\sqrt{\left[ \frac{r^2 \theta}{\pi} - \frac{r^2 \theta^2}{4\pi^2} \right]} = h$$

$$\text{Simplify}\left[\sqrt{\frac{r^2 \theta}{\pi} - \frac{r^2 \theta^2}{4\pi^2}}\right]$$

$$\frac{\sqrt{r^2 (4\pi - \theta) \theta}}{2\pi}$$

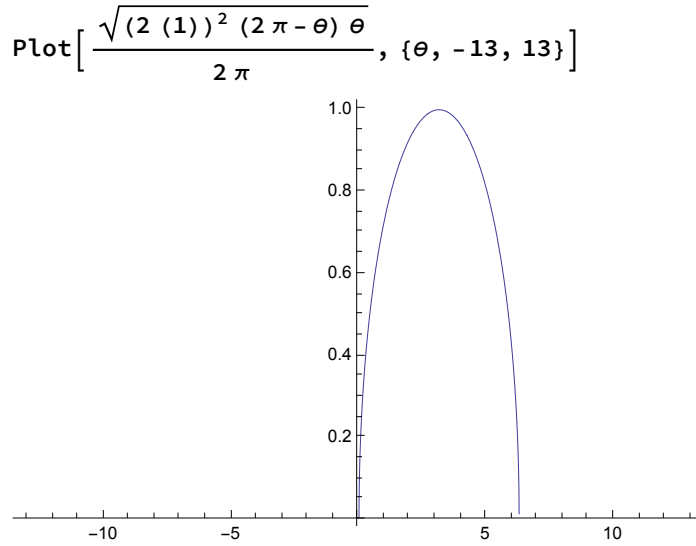
$$\text{Plot}\left[\frac{\sqrt{(2r)^2 (2\pi - \theta) \theta}}{2\pi}, \{\theta, -13, 13\}\right]$$



We alter the equation to fix it, because what we find with what we found was missing a coefficient.

$$\frac{\sqrt{((2r))^2 (4\pi - \theta) \theta}}{\pi}$$

$$\frac{\sqrt{(2r)^2 (4\pi - \theta) \theta}}{2\pi}$$



$$h = \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi}$$

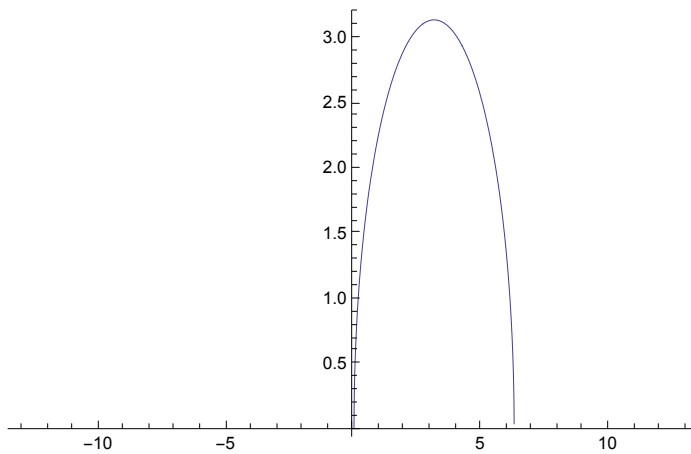
$$h = \frac{\sqrt{(2r)^2(4\pi-\theta)\theta}}{2\pi}$$

$$D\left[\frac{\sqrt{(2(1))^2(4\pi-\theta)\theta}}{2\pi}, \theta\right]$$

$$\frac{4\pi - 2\theta}{2\pi\sqrt{(4\pi-\theta)\theta}}$$

D[

$$\text{Plot}\left[\frac{\sqrt{(2(r))^2(2\pi-\theta)\theta}}{2\pi}, \{\theta, -13, 13\}\right]$$



There are methods for solving this equation so that we know what  $r$  is in terms of  $\theta$ . We will not use them for our immediate introspection. However, an additional postulate should be noted. The

initial discernment of the moon's radius is a measurement of one. The moon will be said to have an initial radius of one, because it is the first measurement taken, and any multiplier of other scaling methods could be applied to the initial designation of the radius' being equal to one.

When we look at the moon from beneath the legs, we see an object in relation to contour. The object, however, is a heavenly body, and discernment of its actual size is more difficult than objects on the ground. In Gibson's terminology, what happens during the perception of the moon when standing up is that, although the object, "neither approaches nor recedes from the point of observation, and no change occurs within the contour corresponding object" (Gibson, 103), there is a perceived magnification. In the optical array, when perceiving the moon, we can suggest that there must be a decretion in the optical structure, i.e. framing by the legs (deletion of optical structure relating to the contour of the moon), and therefore a decrease of the moon's edge contour from the standing position. This refers to a disturbance in the perspective.

When we look from beneath our legs, not only do our eyes have to strain to look upward (creating hypocycloid, or syccatic eye movements), but also they switch positions and invert. The phenomenon occurs within the sphere of an individual's perceptual space. From the notion of mirroring (due to inverted eye positions), we notice that the derivative of the actual geometric element of depth inceives a perceptual illusion of depth change independently from within the space of an individual and their translation of the existence of objects in real space into subjective experience upon reception of the external sensation of light.

The moon phenomenon is some evidence for the old Buddhist koan that suggests that the mind really may be that which moves, because the first derivative of height would be velocity with respect to our version of the time variable.

In order to model this phenomenon, we will use the hypocycloid to model the syccatic eye movements, and the derivative of the height (due to mirroring of the individual's perceptual space) to find the exact amount of decretion of contour around the perceived moon when looking upside down from beneath your legs.

$$h = \frac{\sqrt{r^2 (4\pi - \theta) \theta}}{2\pi} = \frac{\sqrt{(4\pi - \theta) \theta}}{2\pi}$$

$$D\left[\frac{\sqrt{(4\pi - \theta) \theta}}{2\pi}, \theta\right]$$

$$\frac{4\pi - 2\theta}{4\pi \sqrt{(4\pi - \theta) \theta}}$$



```
Clear[x, y, t, a, b, tmini, tmaxi]
```

$$a = \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi};$$

$$b = \frac{4\pi - 2\theta}{2\pi\sqrt{(4\pi - \theta)\theta}}$$

```
tmini = -10  $\pi$ ;
```

```
tmaxi = 10  $\pi$ ;
```

```
{x[t_], y[t_]} =
```

```
{(a - b) * Cos[ $\theta$ ] + b * Cos[(a - b) / b *  $\theta$ ], (a - b) * Sin[ $\theta$ ] - b * Sin[(a - b) / b *  $\theta$ ]};
```

```
hypocycloid =
```

```
ParametricPlot[{x[ $\theta$ ], y[ $\theta$ ]}, { $\theta$ , tmini, tmaxi},
```

```
PlotStyle -> {{Blue, Thickness[0.015]}},
```

```
AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]
```

```
Clear[x, y, t, a, b, tmini, tmaxi]
```

$$a = \frac{\sqrt{(2(1))^2 (4\pi - \theta) \theta}}{2\pi};$$

$$b = \frac{4\pi - 2\theta}{4\pi \sqrt{(4\pi - \theta) \theta}}$$

```
tmini = -13 π;
```

```
tmaxi = 13 π;
```

```
{x[t_], y[t_]} =
```

```
{(a - b) * Cos[θ] + b * Cos[(a - b) / b * θ], (a - b) * Sin[θ] - b * Sin[(a - b) / b * θ]};
```

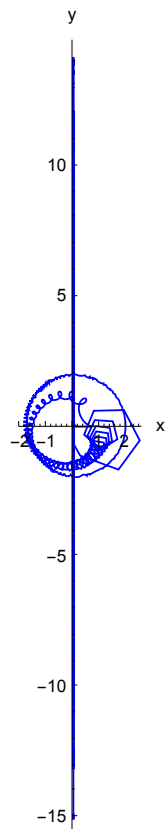
```
hypocycloid =
```

```
ParametricPlot[{x[θ], y[θ]}, {θ, tmini, tmaxi},
```

```
PlotStyle -> {{Blue, Thickness[0.015]}},
```

```
AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]
```

$$\frac{4\pi - 2\theta}{4\pi \sqrt{(4\pi - \theta) \theta}}$$



We can interpret this to show us the way in which contour gives us the perception of depth in our environment, and that, when the contour around an object is eroded by a change in the environmental

factors, it looks smaller. I think the graph should be interpreted to say that there is the amount of contour is even on all edges of the object when the average is found for the size of a loop.

Science offers to humanities the language by which they may discuss the parameters of the human being in its beauty, symmetry, and sense of place. A human being is a material being, though this material ought not to be thought of as a separate element from its geometry. If we think about it, we are like spheres. Our bodies and minds both have a centralized locale in the environment. A body of knowledge grows to more accurately describe the being who asked the question of individual meaning. The individuality of this being, however, must only be considered to be truly individual from the rest of the universe in which it inhabits. Science can offer a path to the humanitarian study in which each element of the impressions made by a being is an ever - expanding body of connective knowledge. Science shows the humanities how they are symbolically present through the entire realm of being. The arts, in this way, are like the tissue or sinew of a structure for expanding and exploring the cognition and being of the individual.

$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\text{Solve}\left[13 == 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), \beta\right]$$

$$\left\{ \left\{ \beta \rightarrow -i \operatorname{ArcSinh}\left[ \frac{\sqrt{13 (13 - 4 \pi)}}{2 \pi} \right] \right\}, \left\{ \beta \rightarrow i \operatorname{ArcSinh}\left[ \frac{\sqrt{13 (13 - 4 \pi)}}{2 \pi} \right] \right\} \right\}$$

$$c := 2.99792458 * (10^8)$$

RevolutionPlot3D[

$$\frac{1}{1166400} \pi^2 \left( - \frac{540 c}{\sqrt{4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}} + \frac{1080 c}{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2} \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}} + \frac{1620 c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{5/2}} \right),$$

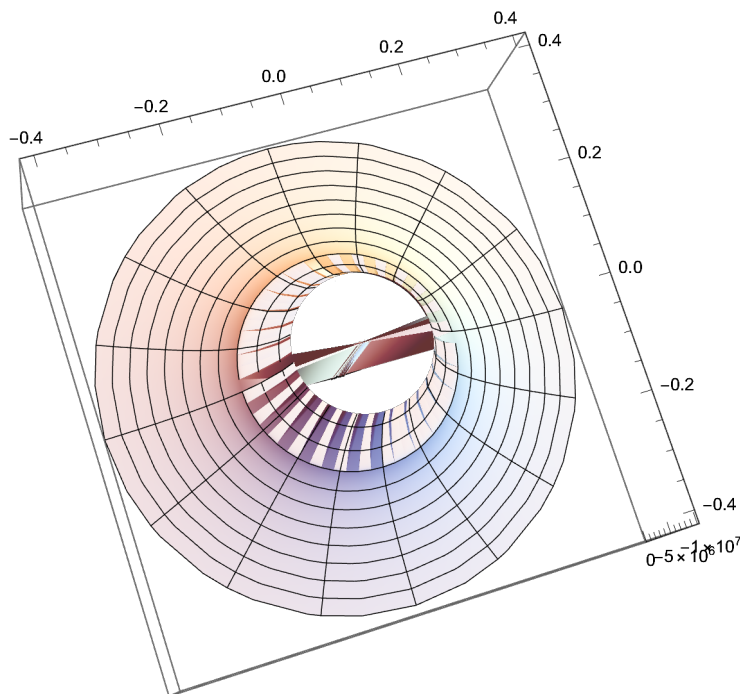
$$\left\{ \beta, -\frac{\sqrt{13(13-4\pi)}}{2\pi} \operatorname{ArcSinh} \left[ \frac{\sqrt{13(13-4\pi)}}{2\pi} \right], \operatorname{ArcSinh} \left[ \frac{\sqrt{13(13-4\pi)}}{2\pi} \right] \right\}$$

RevolutionPlot3D[

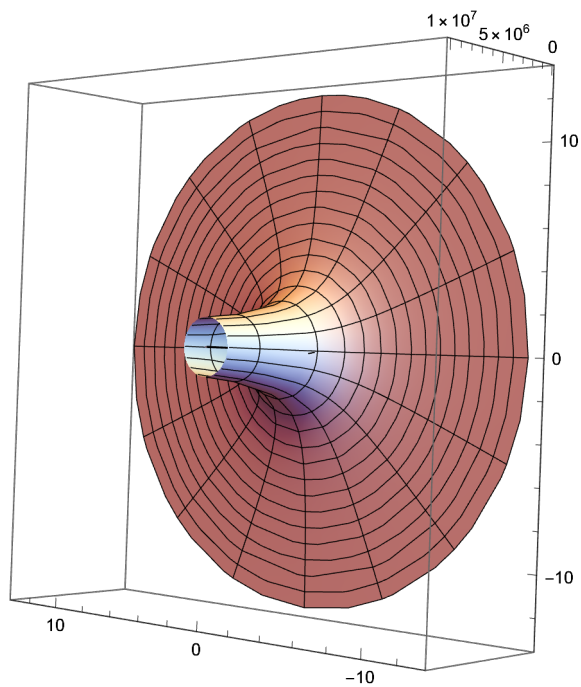
$$\frac{1}{1166400} \pi^2 \left( - \frac{540 c}{\sqrt{4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}} + \frac{1080 c}{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2} \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}} + \frac{1620 c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{5/2}} \right),$$

$$\left\{ \beta, -\frac{\sqrt{13(13-4\pi)}}{2\pi} \operatorname{ArcSinh} \left[ \frac{\sqrt{13(13-4\pi)}}{2\pi} \right], \operatorname{ArcSinh} \left[ \frac{\sqrt{13(13-4\pi)}}{2\pi} \right] \right\}$$

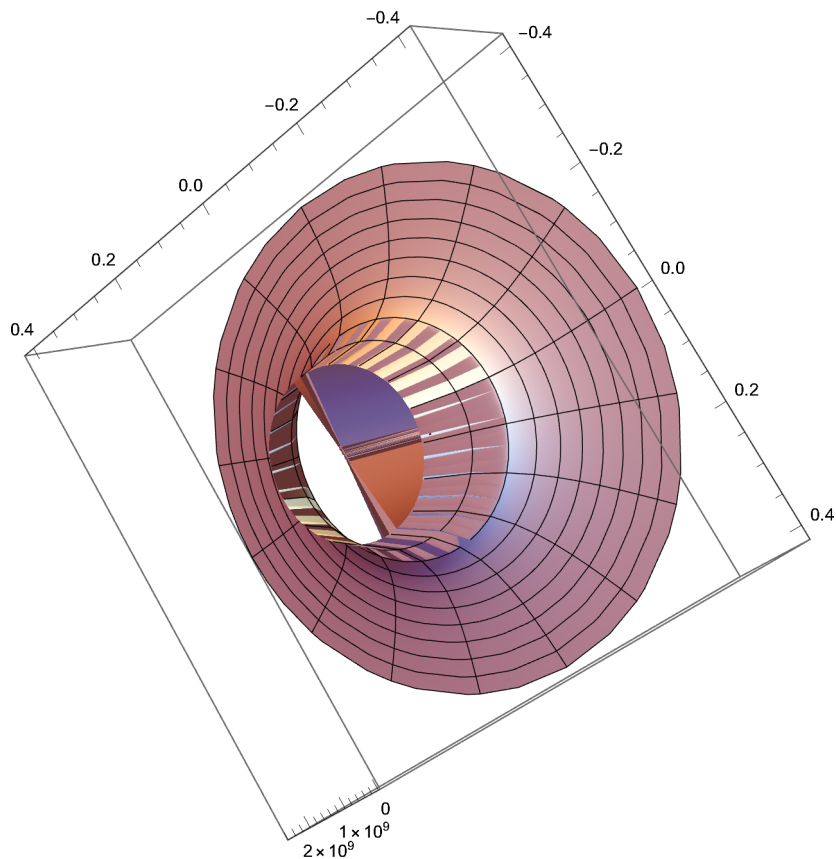
$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\left\{\theta,\frac{26 \pi}{-13+2 \pi},\frac{2\left(-13 \pi+4 \pi^2\right)}{-13+2 \pi}\right\}\right]$



$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\left\{\gamma,\frac{26 \pi}{-13+2 \pi},13\right\}\right]$



$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}}\right)}{1166400}, \left\{\gamma, \frac{26 \pi}{-13 + 2 \pi}, \frac{2(-13 \pi + 4 \pi^2)}{-13 + 2 \pi}\right\}\right]$



$c := 2.99792458 * (10^8)$

$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$

$\text{Solve}\left[\gamma == \frac{2 \left( \pi - \pi \csc[\beta]^2 + \sqrt{-\pi^2 \csc[\beta]^2 + \pi^2 \csc[\beta]^4} \right)}{-1 + \csc[\beta]^2}, \beta\right]$

$\left\{ \left\{ \beta \rightarrow -\text{ArcCsc}\left[\frac{\sqrt{-4 \pi^2 - 4 \pi \gamma - \gamma^2}}{\sqrt{-4 \pi \gamma - \gamma^2}}\right] \right\}, \left\{ \beta \rightarrow \text{ArcCsc}\left[\frac{\sqrt{-4 \pi^2 - 4 \pi \gamma - \gamma^2}}{\sqrt{-4 \pi \gamma - \gamma^2}}\right] \right\} \right\}$

$\text{ArcCsc}\left[\frac{\sqrt{-4 \pi^2 - 4 \pi \gamma - \gamma^2}}{\sqrt{-4 \pi \gamma - \gamma^2}}\right]$

$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin\left[\text{ArcCsc}\left[\frac{\sqrt{-4 \pi^2 - 4 \pi \gamma - \gamma^2}}{\sqrt{-4 \pi \gamma - \gamma^2}}\right]\right]^2} \right)$

$$\text{Solve}\left[13 == 2 \left( \pi + \sqrt{\pi^2 - \frac{\pi^2 (-4 \pi \gamma - \gamma^2)}{-4 \pi^2 - 4 \pi \gamma - \gamma^2}} \right), \gamma\right]$$

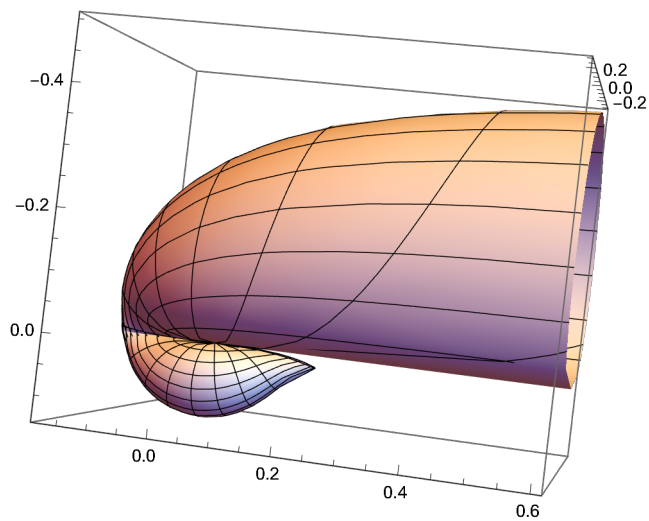
$$\left\{ \left\{ \gamma \rightarrow \frac{26 \pi}{-13 + 2 \pi} \right\}, \left\{ \gamma \rightarrow -\frac{2 (-13 \pi + 4 \pi^2)}{-13 + 2 \pi} \right\} \right\}$$

$$\text{Solve}\left[2 \pi r - 2 \pi \sqrt{\left( r^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 \right)} - \theta r ==\right.$$

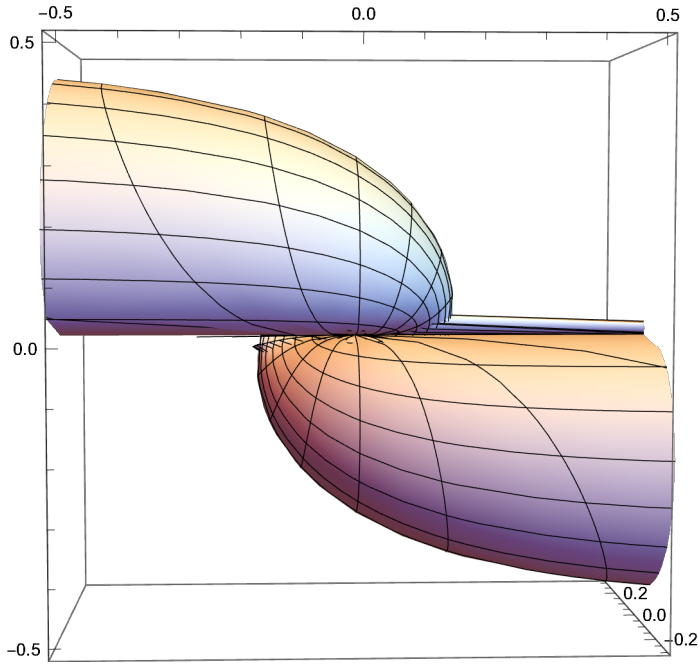
$$\left. \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \right/ \left( 2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{4 \pi r^2 \theta - r^2 \theta^2}{4 \pi^2}} \right), r]$$

$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{\sqrt{(4 \pi - \theta) \theta \text{Sin}[\beta]}{4 \pi - \theta}} + \frac{\sqrt{(4 \pi - \theta) \theta \text{Sin}[\beta]}}{\theta}}}{\sqrt{32 \pi^2 - 32 \pi \theta + 8 \theta^2}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{\sqrt{(4 \pi - \theta) \theta \text{Sin}[\beta]}{4 \pi - \theta}} + \frac{\sqrt{(4 \pi - \theta) \theta \text{Sin}[\beta]}}{\theta}}}{\sqrt{32 \pi^2 - 32 \pi \theta + 8 \theta^2}} \right\} \right\}$$

$$\text{SphericalPlot3D}\left[\frac{\sqrt{\frac{\sqrt{(4 \pi - \theta) \theta \text{Sin}[\beta]}{4 \pi - \theta}} + \frac{\sqrt{(4 \pi - \theta) \theta \text{Sin}[\beta]}}{\theta}}}{\sqrt{32 \pi^2 - 32 \pi \theta + 8 \theta^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$$



$$\text{SphericalPlot3D}\left[\left\{-\frac{\sqrt{\frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta}}+\frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta}}{\sqrt{32\pi^2-32\pi\theta+8\theta^2}},\frac{\sqrt{\frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta}}+\frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta}}{\sqrt{32\pi^2-32\pi\theta+8\theta^2}}\right\},\right. \\ \left.\{\theta,-2\pi,2\pi\},\{\beta,-\pi,\pi\}\right]$$



$$\sin[\beta] = \frac{\eta}{r}; \cos[\beta] = \frac{x}{r} = \frac{(2L+q)}{r}; \tan[\beta] = \frac{\eta}{x} = \frac{\eta}{(2L+q)}$$

$$\sin[\gamma] = \frac{\eta}{r_1}; \cos[\gamma] = \frac{(L+q)}{r_1}; \tan[\gamma] = \frac{\eta}{(L+q)}$$

$$\sin[\delta] = \frac{\eta}{r_2}; \cos[\delta] = \frac{(q)}{r_2}; \tan[\delta] = \frac{\eta}{(q)}$$

$$\text{GoldenRatio } \alpha = \omega$$

$$r_2 \omega = \text{GoldenRatio } r_1 \alpha$$

$$\frac{\pi}{2} + \beta + (\alpha + \omega + \vartheta) = \pi$$

$$\frac{\pi}{2} + \gamma + (\omega + \vartheta) = \pi$$

$$\frac{\pi}{2} + \delta + \vartheta = \pi$$

$$r^2 = \eta^2 + (2L+q)^2 = \eta^2 + (x)^2$$

$$r_1^2 = \eta^2 + (L+q)^2$$

$$r_2^2 = \eta^2 + (q)^2$$



$$2 \pi r - 2 \pi x = \theta r$$

$$2 \pi r - 2 \pi r_1 = \iota r$$

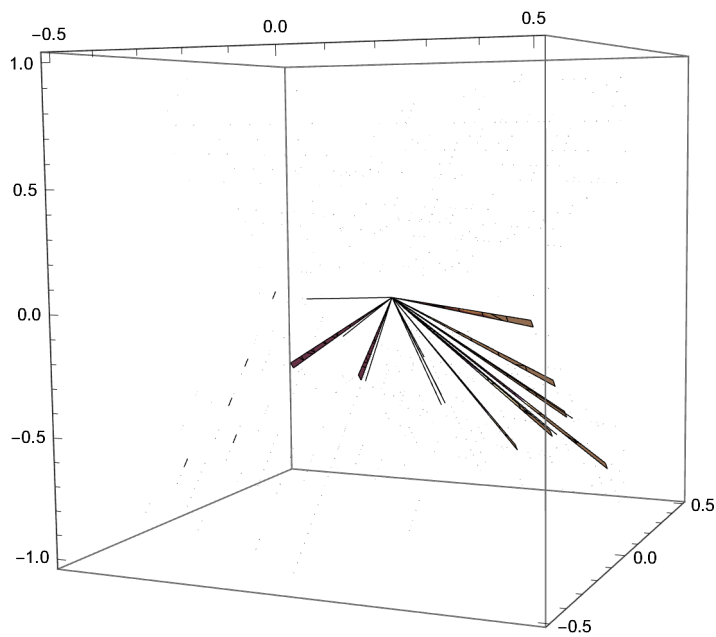
$$2 \pi r - 2 \pi r_2 = \kappa r$$

$$2 \pi r_1 - 2 \pi r_2 = \mu r$$

$$\text{Solve}[r^2 == \eta^2 + (2 L + q)^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{-4 L^2 - 4 L q - q^2 + r^2} \right\}, \left\{ \eta \rightarrow \sqrt{-4 L^2 - 4 L q - q^2 + r^2} \right\} \right\}$$

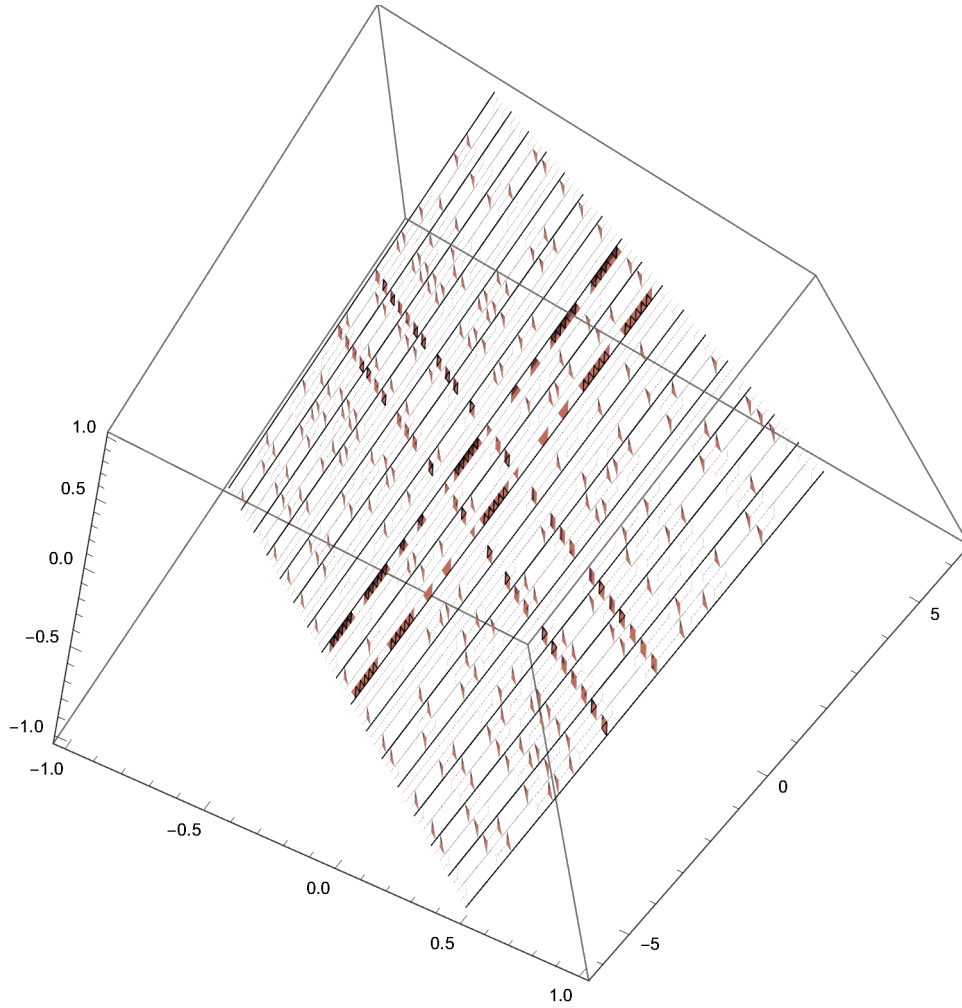
$$\text{ContourPlot3D}\left[\left\{-\sqrt{-4 L^2 - 4 L q - q^2 + r^2}, \sqrt{-4 L^2 - 4 L q - q^2 + r^2}\right\},\right. \\ \left.\{L, -.5, .5\}, \{r, -1, 1\}, \{q, -.5, .5\}\right]$$



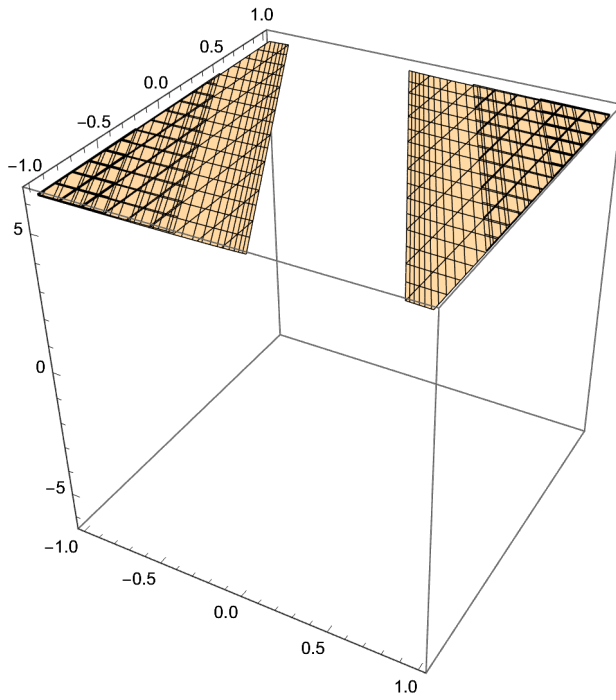
$$\text{Solve}\left[\sqrt{-4 L^2 - 4 L q - q^2 + r^2} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2 \pi \sqrt{4 L^2 + 4 L q + q^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\}, \left\{ r \rightarrow \frac{2 \pi \sqrt{4 L^2 + 4 L q + q^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\} \right\}$$

$\text{ContourPlot3D}\left[\left\{-\frac{2\pi\sqrt{4L^2+4Lq+q^2}}{\sqrt{4\pi^2-4\pi\theta+\theta^2}}, \frac{2\pi\sqrt{4L^2+4Lq+q^2}}{\sqrt{4\pi^2-4\pi\theta+\theta^2}}\right\},\right.$   
 $\left.\{L, -1, 1\}, \{q, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



ContourPlot3D $\left[\frac{2 \pi \sqrt{4 L^2 + 4 L q + q^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{L, -1, 1\}, \{q, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

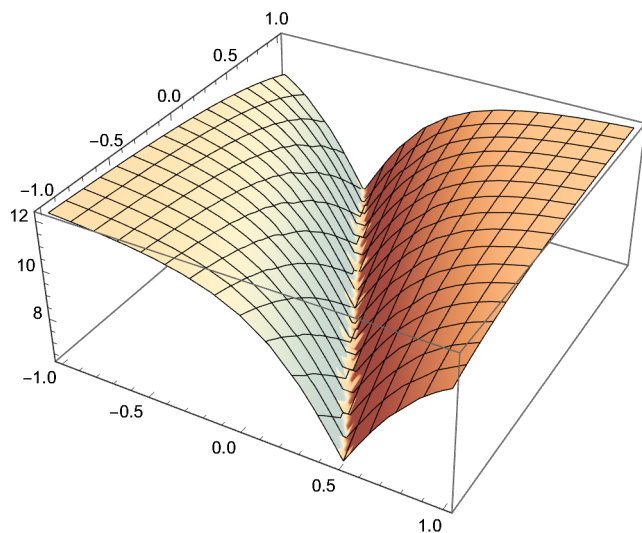
$$\text{Solve}\left[\sqrt{-4 L^2 - 4 L q - q^2 + r^2} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2 \pi \left(1 + 4 L^2 + 4 L q + q^2 - \sqrt{4 L^2 + 16 L^4 + 4 L q + 32 L^3 q + q^2 + 24 L^2 q^2 + 8 L q^3 + q^4}\right)}{1 + 4 L^2 + 4 L q + q^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow \frac{2 \pi \left(1 + 4 L^2 + 4 L q + q^2 + \sqrt{4 L^2 + 16 L^4 + 4 L q + 32 L^3 q + q^2 + 24 L^2 q^2 + 8 L q^3 + q^4}\right)}{1 + 4 L^2 + 4 L q + q^2}\right\}\right\}$$

Plot3D $\left[\frac{2 \pi \left(1 + 4 L^2 + 4 L q + q^2 + \sqrt{4 L^2 + 16 L^4 + 4 L q + 32 L^3 q + q^2 + 24 L^2 q^2 + 8 L q^3 + q^4}\right)}{1 + 4 L^2 + 4 L q + q^2},\right.$

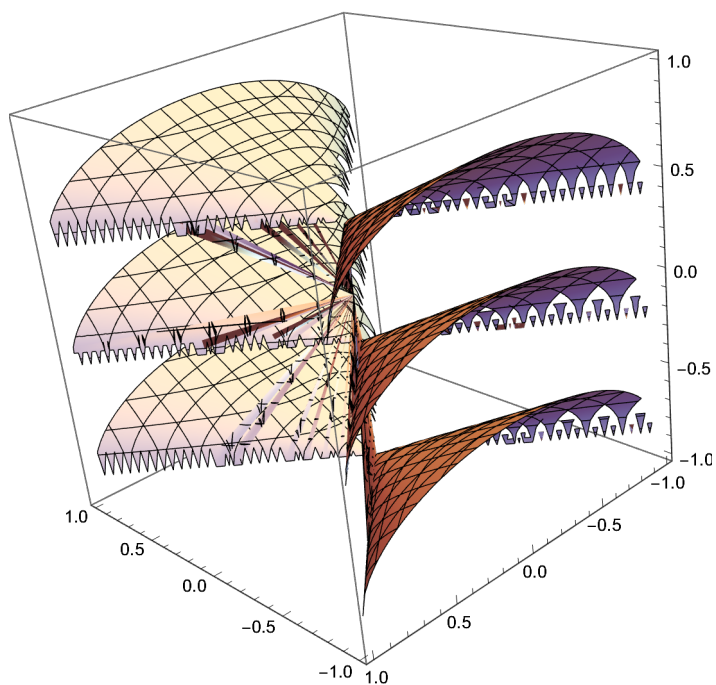
$\{L, -1, 1\}, \{q, -1, 1\}\left.] \right]$



Solve $[r^2 == \eta^2 + (2 L + q)^2, q]$

$\left\{\left\{q \rightarrow -2 L - \sqrt{r^2 - \eta^2}\right\}, \left\{q \rightarrow -2 L + \sqrt{r^2 - \eta^2}\right\}\right\}$

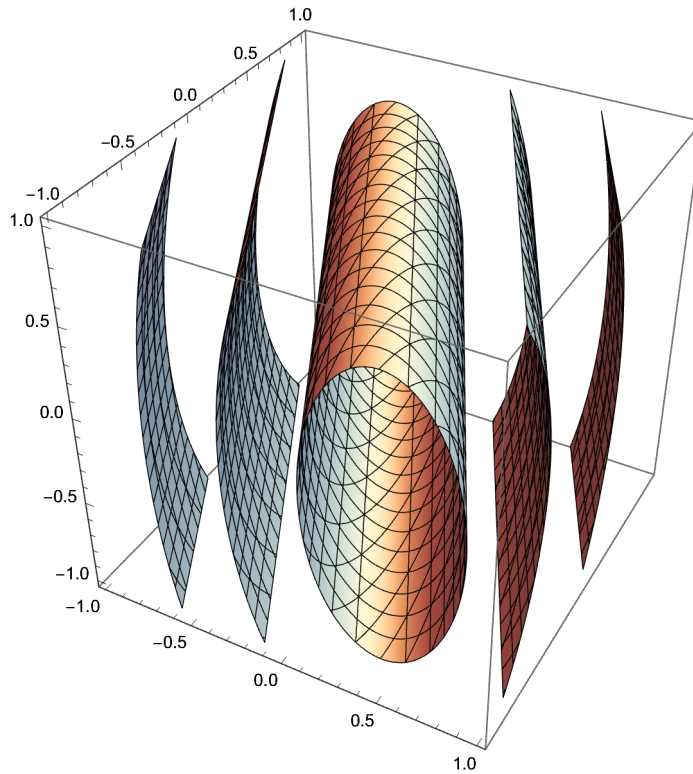
ContourPlot3D $\left[-2 L + \sqrt{r^2 - \eta^2}, \{L, -1, 1\}, \{r, -1, 1\}, \{\eta, -1, 1\}\right]$



`Solve[r^2 == η^2 + (2 L + q)^2, r]`

$\left\{ \left\{ r \rightarrow -\sqrt{(2 L + q)^2 + \eta^2} \right\}, \left\{ r \rightarrow \sqrt{(2 L + q)^2 + \eta^2} \right\} \right\}$

`ContourPlot3D[ $\sqrt{(2 L + q)^2 + \eta^2}$ , {L, -1, 1}, {q, -1, 1}, {η, -1, 1}]`



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$$\frac{\pi}{2} + \beta + (\alpha + \omega + \vartheta) == \pi$$

`Solve[ $\frac{\pi}{2} + \beta + (\alpha + \omega + \vartheta) == \pi$ , ϑ]`

$\left\{ \left\{ \vartheta \rightarrow \frac{1}{2} (\pi - 2 \alpha - 2 \beta - 2 \omega) \right\} \right\}$

$$\sin[\delta] = \frac{\eta}{r_2}; \cos[\delta] = \frac{(q)}{r_2}; \tan[\delta] = \frac{\eta}{(q)}$$

`Solve[Tan[δ] ==  $\frac{\eta}{(q)}$ , δ]`

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$\left\{ \left\{ \delta \rightarrow \text{ArcTan}\left[\frac{\eta}{q}\right] \right\} \right\}$

$$r = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\beta = \text{ArcSin}\left[\frac{4 \pi r \theta - r \theta^2}{4 \pi^2}\right] = \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]$$

$$\text{ArcTan}\left[\frac{\eta}{q}\right] == \frac{1}{2} (\pi - 2 \alpha - 2 \beta - 2 \omega) =$$

$$\frac{1}{2} (\pi - 2 \alpha - 2 \beta - 2 \text{GoldenRatio} \alpha) = \frac{1}{2} \left( \pi - 2 \alpha - 2 \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right] - 2 \text{GoldenRatio} \alpha \right) =$$

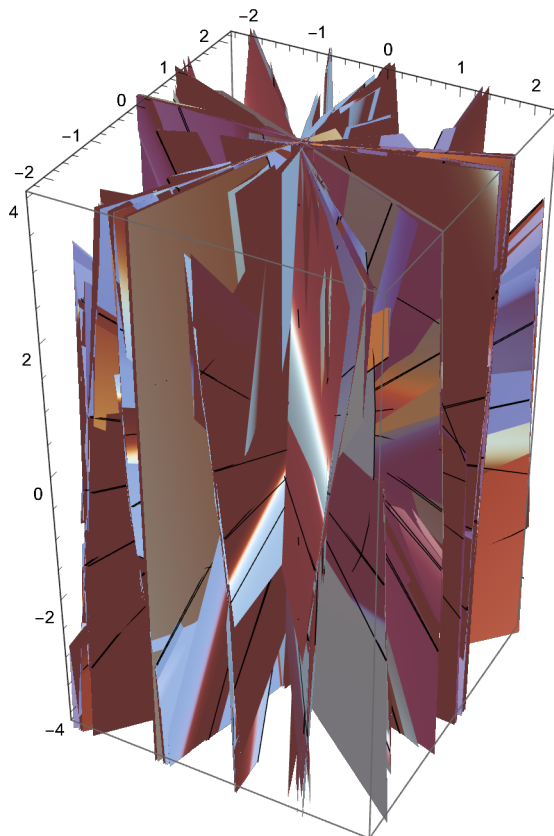
$$\text{ArcTan}\left[\frac{\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}}{q}\right] = \text{ArcTan}\left[\frac{\frac{\sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}{2 \pi}}{q}\right]$$

$$\text{Solve}\left[\text{ArcTan}\left[\frac{\frac{\sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}{2 \pi}}{q}\right] == \right.$$

$$\left. \frac{1}{2} \left( \pi - 2 \alpha - 2 \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right] - 2 \text{GoldenRatio} \alpha \right), q\right]$$

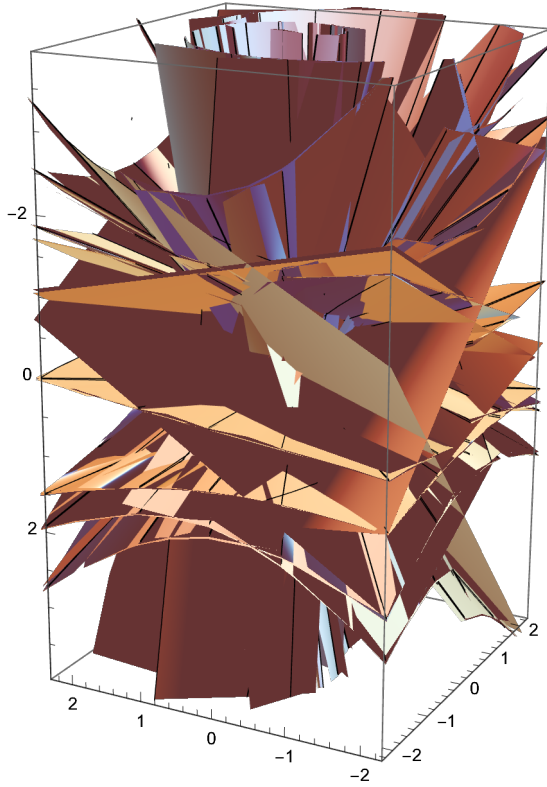
$$\left\{ \left\{ q \rightarrow \text{Cot}\left[\frac{1}{2} \left( \pi - 3 \alpha - \sqrt{5} \alpha - 2 \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right] \right) \right] \right\} \right\}$$

SphericalPlot3D[  
 $\text{Cot}\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right], \{\theta, -2\pi, 2\pi\}, \{\alpha, -\pi, \pi\}]$



SphericalPlot3D[

$$\text{Cot}\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right], \{\alpha, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



$$\text{Tan}[\beta] = \frac{\eta}{x} = \frac{\eta}{(2L + q)}$$

$$\text{Solve}\left[\text{Tan}[\beta] == \frac{\eta}{\left(2L + \text{Cot}\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right)}\right], L\right]$$

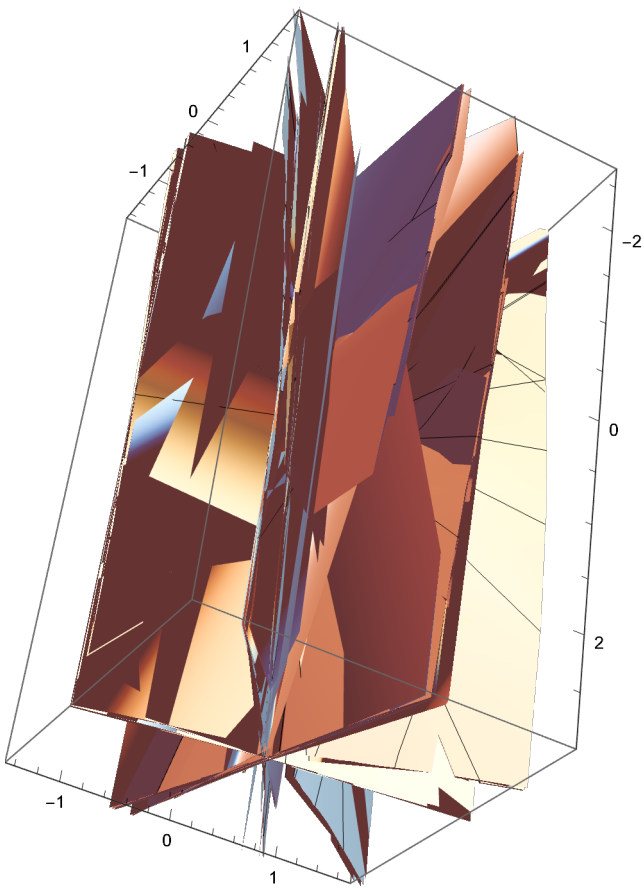
$$\left\{\left\{L \rightarrow \frac{1}{2}\text{Cot}[\beta] \left(\eta - \text{Cot}\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]\text{Tan}[\beta]\right)\right\}\right\}$$



$$\begin{aligned}
& \frac{1}{2} \cot[\beta] \left( \eta - \cot \left[ \frac{1}{2} \left( \pi - 3\alpha - \sqrt{5}\alpha - 2 \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right] \tan[\beta] \right) = \\
& \frac{1}{2} \cot \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right] \left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} - \right. \\
& \quad \left. \cot \left[ \frac{1}{2} \left( \pi - 3\alpha - \sqrt{5}\alpha - 2 \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right] \tan \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right] \right) = \\
& \frac{1}{2} \cot \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right] \left( \frac{\sqrt{4\pi \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}}{2\pi} - \right. \\
& \quad \left. \cot \left[ \frac{1}{2} \left( \pi - 3\alpha - \sqrt{5}\alpha - 2 \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right] \tan \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right] \right)
\end{aligned}$$

SphericalPlot3D[

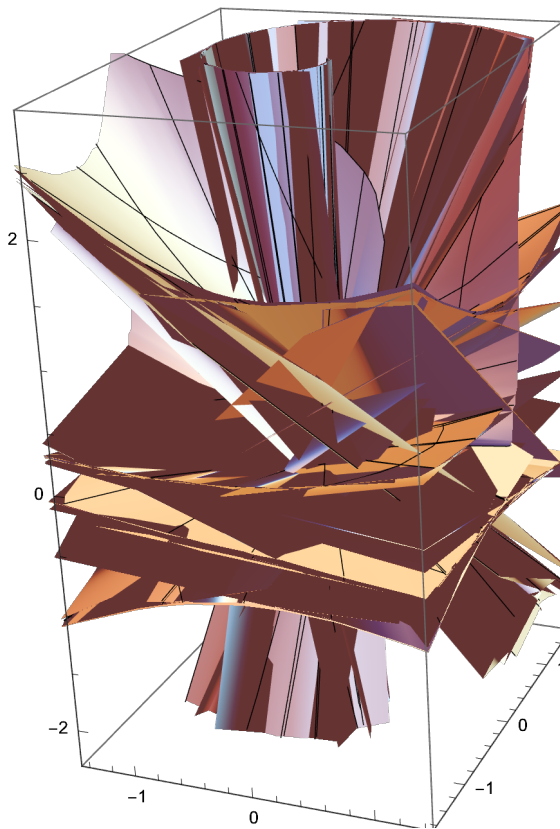
$$\frac{1}{2} \operatorname{Cot}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] \left( \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi} - \right. \\ \left. \operatorname{Cot}\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right] \operatorname{Tan}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] \right), \\ \{\theta, -2\pi, 2\pi\}, \{\alpha, -\pi/2, \pi/2\}]$$



SphericalPlot3D[

$$\frac{1}{2} \operatorname{Cot}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] \left( \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi} - \right. \\ \left. \operatorname{Cot}\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right] \operatorname{Tan}\left[\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] \right),$$

$$\{\alpha, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$

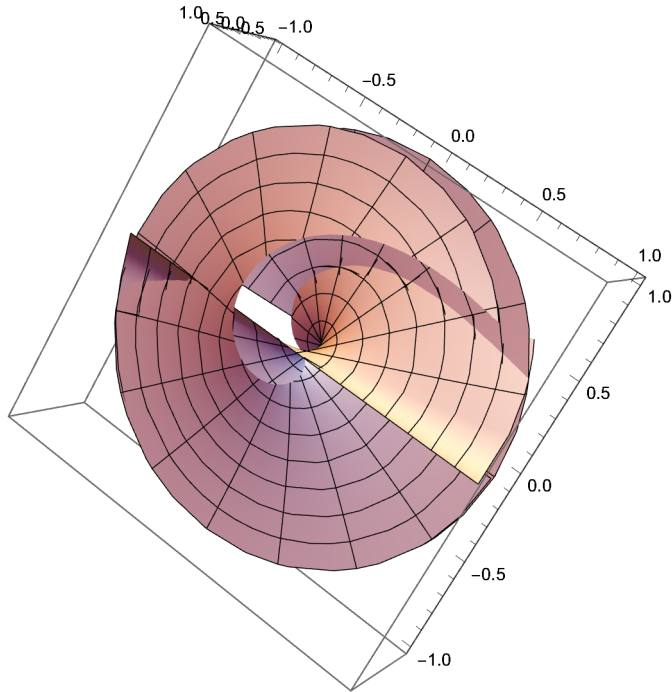


$$\text{Solve}\left[\frac{1}{2} \cot\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] \left( \frac{\sqrt{4\pi \left(\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}\right)^2 \theta - \left(\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}\right)^2 \theta^2}}{2\pi} - \right. \right. \\ \left. \left. \cot\left[\frac{1}{2} \left( \pi - 3\alpha - \sqrt{5}\alpha - 2 \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] \right) \right] \tan\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] \right) = L, \alpha \right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{ \left\{ \alpha \rightarrow \frac{1}{4} \left( 3\pi - \sqrt{5}\pi - 6 \text{ArcCot}\left[ \frac{8L\pi\theta - 2L\theta^2 - \sqrt{(2\pi - \theta)^2} \sqrt{(4\pi - \theta)\theta}}{-4\pi\theta + \theta^2} \right] + \right. \right. \right. \\ \left. \left. 2\sqrt{5} \text{ArcCot}\left[ \frac{8L\pi\theta - 2L\theta^2 - \sqrt{(2\pi - \theta)^2} \sqrt{(4\pi - \theta)\theta}}{-4\pi\theta + \theta^2} \right] - \right. \right. \\ \left. \left. 6 \text{ArcSin}\left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] + 2\sqrt{5} \text{ArcSin}\left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right) \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\frac{1}{4}\left(3\pi - \sqrt{5}\pi - 6\text{ArcCot}\left[\frac{8L\pi\theta - 2L\theta^2 - \sqrt{(2\pi - \theta)^2}\sqrt{(4\pi - \theta)\theta}}{-4\pi\theta + \theta^2}\right] + 2\sqrt{5}\text{ArcCot}\left[\frac{8L\pi\theta - 2L\theta^2 - \sqrt{(2\pi - \theta)^2}\sqrt{(4\pi - \theta)\theta}}{-4\pi\theta + \theta^2}\right] - 6\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] + 2\sqrt{5}\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right), \{L, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$\text{Solve}\left[\frac{1}{2}\left(\pi - 2\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] - 2\text{GoldenRatio}\alpha\right) == \text{ArcTan}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right], q\right]$$

$$\left\{\left\{q \rightarrow \frac{\sqrt{r^2(4\pi - \theta)\theta} \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]}{2\pi}\right\}\right\}$$

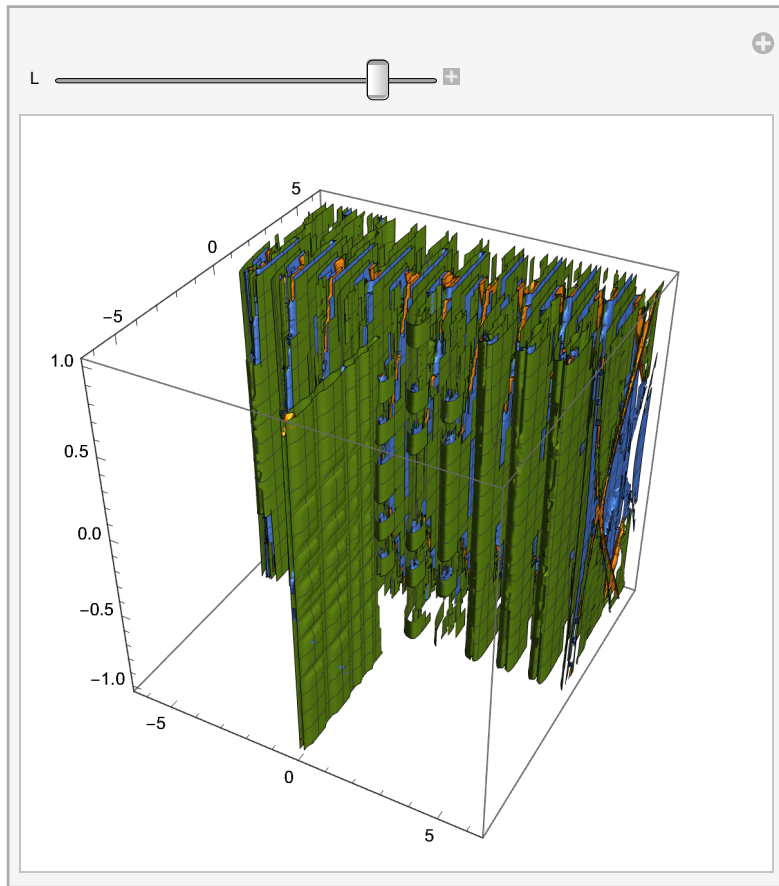
$$r := \sqrt{(2L + q)^2 + \eta^2}$$

Solve[

$$\begin{aligned}
& \frac{\sqrt{\left(\sqrt{(2L+q)^2+\eta^2}\right)^2(4\pi-\theta)\theta}\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]}{2\pi}, q] \\
& \left\{ \left\{ q \rightarrow \left( -L(16\pi-4\theta)\theta\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \right. \\
& \quad \sqrt{\left( L^2(16\pi-4\theta)^2\theta^2\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^4 + 4\theta \right.} \\
& \quad \left. \left. \left. (-16L^2\pi-4\pi\eta^2+4L^2\theta+\eta^2\theta)\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 \right. \right. \right. \\
& \quad \left. \left. \left. \left( -4\pi^2+4\pi\theta\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \right. \\
& \quad \left. \left. \left. \theta^2\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 \right) \right) \right) \right) / \\
& \quad \left( 2 \left( -4\pi^2+4\pi\theta\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \\
& \quad \left. \left. \theta^2\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 \right) \right) \right\}, \\
& \left\{ q \rightarrow \left( -L(16\pi-4\theta)\theta\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 + \right. \right. \\
& \quad \sqrt{\left( L^2(16\pi-4\theta)^2\theta^2\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^4 + 4\theta \right.} \\
& \quad \left. \left. \left. (-16L^2\pi-4\pi\eta^2+4L^2\theta+\eta^2\theta)\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 \right) \right. \right. \\
& \quad \left. \left. \left. \left( -4\pi^2+4\pi\theta\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \right. \\
& \quad \left. \left. \left. \theta^2\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 \right) \right) \right) / \\
& \quad \left( 2 \left( -4\pi^2+4\pi\theta\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \\
& \quad \left. \left. \theta^2\cot\left[\frac{1}{2}\left(\pi-3\alpha-\sqrt{5}\alpha-2\operatorname{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right)\right]^2 \right) \right) \right\}
\end{aligned}$$

Manipulate[

$$\begin{aligned}
& \text{ContourPlot3D}\left[\left(-L(16\pi - 4\theta)\theta \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^2 + \right. \right. \\
& \quad \sqrt{\left(L^2(16\pi - 4\theta)^2\theta^2 \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^4 + 4\theta} \right. \\
& \quad \left. \left(-16L^2\pi - 4\pi\eta^2 + 4L^2\theta + \eta^2\theta\right) \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^2 \right. \\
& \quad \left. \left(-4\pi^2 + 4\pi\theta \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \\
& \quad \left. \left.\theta^2 \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^2\right)\right)\right) / \\
& \quad \left(2\left(-4\pi^2 + 4\pi\theta \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^2 - \right. \right. \\
& \quad \left. \left.\theta^2 \cot\left[\frac{1}{2}\left(\pi - 3\alpha - \sqrt{5}\alpha - 2\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right]^2\right)\right), \\
& \quad \{\alpha, -2\pi, 2\pi\}, \{\theta, -2\pi, 2\pi\}, \{\eta, -1, 1\}], \{L, \\
& \quad -1, \\
& \quad 1\}
\end{aligned}$$







$$\text{Solve}\left[\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}} \left( (1080 / \pi) \theta \right) == r, r\right]$$

$$\left\{\left\{r \rightarrow\right.\right.$$

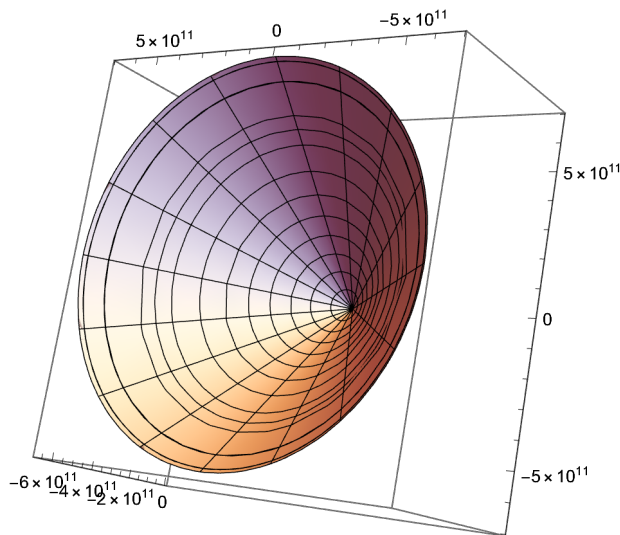
$$\left.-0.5 \sqrt{\left(4.24863 \times 10^{22} \theta^2-2. \sqrt{\left(4.51272 \times 10^{44} \theta^4-\frac{1}{12.5664-1. \theta} 4. \left(1.41771 \times 10^{45} \theta^4-2.25636 \times 10^{44} \theta^5+3.59111 \times 10^{43} \theta^6-2.85771 \times 10^{42} \theta^7\right)\right)}\right)}\right\},$$

$$\left\{r \rightarrow 0.5 \sqrt{\left(4.24863 \times 10^{22} \theta^2-2. \sqrt{\left(4.51272 \times 10^{44} \theta^4-\frac{1}{12.5664-1. \theta} 4. \left(1.41771 \times 10^{45} \theta^4-2.25636 \times 10^{44} \theta^5+3.59111 \times 10^{43} \theta^6-2.85771 \times 10^{42} \theta^7\right)\right)}\right)}\right\},$$

$$\left\{r \rightarrow-0.5 \sqrt{\left(4.24863 \times 10^{22} \theta^2+2. \sqrt{\left(4.51272 \times 10^{44} \theta^4-\frac{1}{12.5664-1. \theta} 4. \left(1.41771 \times 10^{45} \theta^4-2.25636 \times 10^{44} \theta^5+3.59111 \times 10^{43} \theta^6-2.85771 \times 10^{42} \theta^7\right)\right)}\right)}\right\},$$

$$\left\{r \rightarrow 0.5 \sqrt{\left(4.24863 \times 10^{22} \theta^2+2. \sqrt{\left(4.51272 \times 10^{44} \theta^4-\frac{1}{12.5664-1. \theta} 4. \left(1.41771 \times 10^{45} \theta^4-2.25636 \times 10^{44} \theta^5+3.59111 \times 10^{43} \theta^6-2.85771 \times 10^{42} \theta^7\right)\right)}\right)}\right\}$$

$$\text{RevolutionPlot3D}\left[\left\{0.5 \sqrt{\left(4.248632459322957 \theta^{22} - 2. \sqrt{\left(4.512719443603159 \theta^{44} - \frac{1}{12.566370614359172 \theta} (1.4177126251735504 \theta^{45} - 2.2563597218015795 \theta^5 + 3.591108031181752 \theta^{43} - 2.8577129716979 \theta^{42})\right)}\right)} - 0.5 \sqrt{\left(4.248632459322957 \theta^{22} - 2. \sqrt{\left(4.512719443603159 \theta^{44} - \frac{1}{12.566370614359172 \theta} (1.4177126251735504 \theta^{45} - 2.2563597218015795 \theta^5 + 3.591108031181752 \theta^{43} - 2.8577129716979 \theta^{42})\right)}\right)}\right\}, \{\theta, -4 \pi, 4 \pi\}]$$



$$\text{Solve}\left[\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}}\right]$$

$$\left(\frac{(1080 / \pi) \theta}{\sqrt{1 - \left(\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}}\right)^2 / (c^2)}}\right) == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r]$$

$$\left\{ \left\{ r \rightarrow -\sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + 16\,c^4\pi\theta^5 - c^4\theta^6 \right)} \right) / \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right) \right\},$$

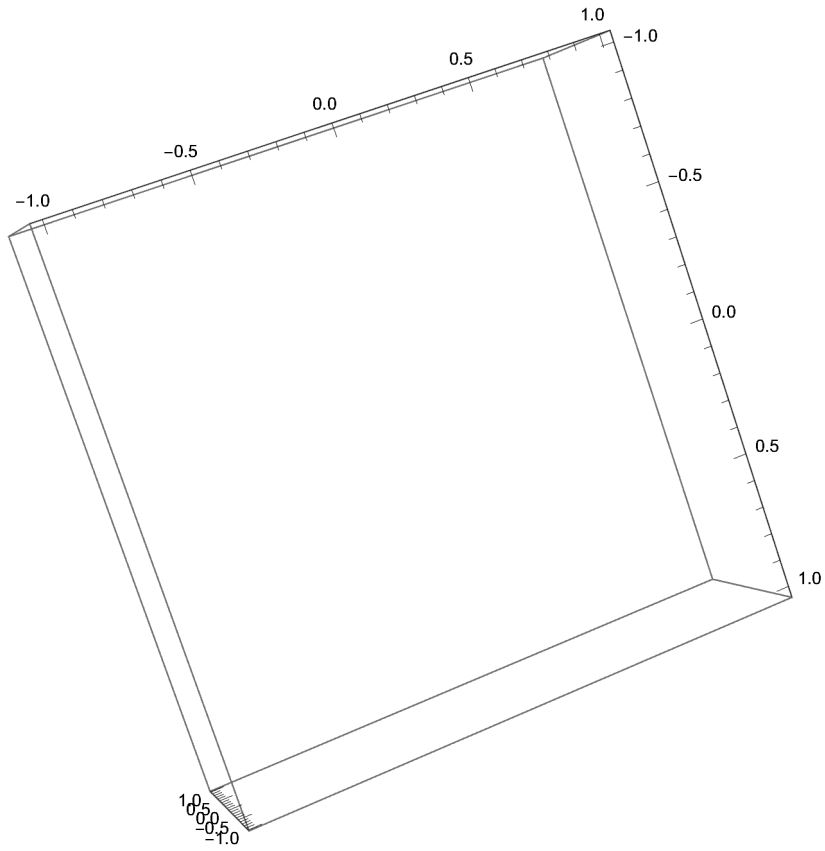
$$\left\{ r \rightarrow \sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + 16\,c^4\pi\theta^5 - c^4\theta^6 \right)} \right) / \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right) \right\},$$

$$\left\{ r \rightarrow -\sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + 16\,c^4\pi\theta^5 - c^4\theta^6 \right)} \right) / \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right) \right\},$$

$$\left\{ r \rightarrow \sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + 16\,c^4\pi\theta^5 - c^4\theta^6 \right)} \right) / \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right) \right\}}$$

RevolutionPlot3D[

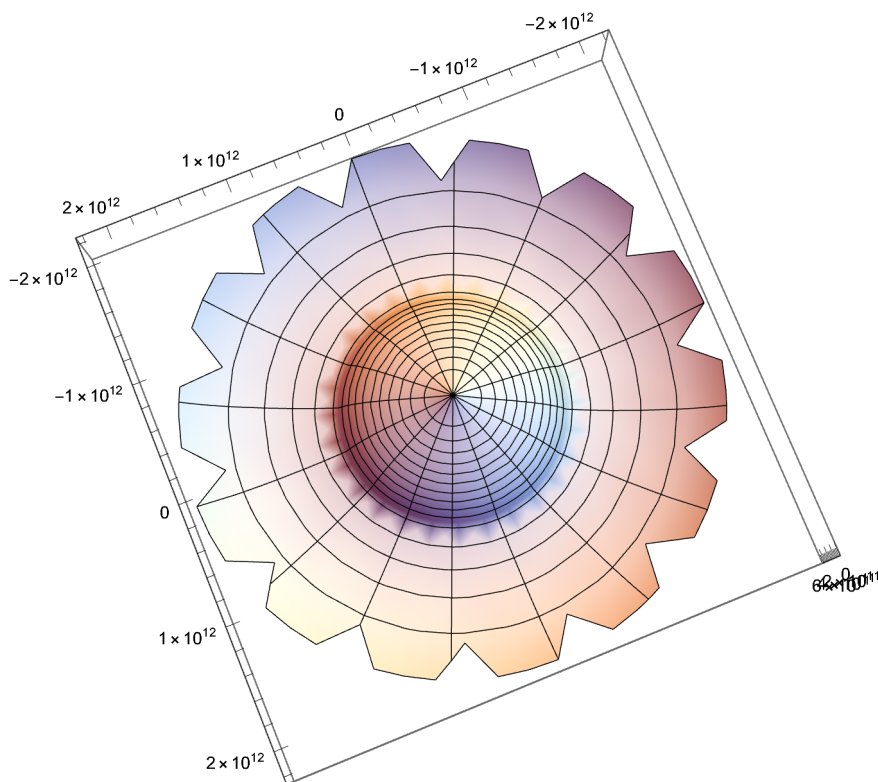
$$\begin{aligned}
& \left\{ \left\{ -\sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \right. \right.} \\
& \quad \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \\
& \quad \left. \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + \right. \right.} \right. \\
& \quad \left. \left. 16\,c^4\pi\theta^5 - c^4\theta^6 \right) \right) / \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right\}, \\
& \left\{ \sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \right. \right.} \\
& \quad \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \\
& \quad \left. \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + 16\,c^4\pi\theta^5 - c^4\theta^6 \right)} \right) / \right. \\
& \quad \left. \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right\}, \\
& \left\{ -\sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \right. \right.} \\
& \quad \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \\
& \quad \left. \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + \right. \right.} \right. \\
& \quad \left. \left. 16\,c^4\pi\theta^5 - c^4\theta^6 \right) \right) / \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right\}, \\
& \left\{ \sqrt{\left( -\frac{74\,649\,600\,c^2\pi^3\theta}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{93\,312\,000\,c^2\pi^2\theta^2}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} - \right. \right.} \\
& \quad \frac{37\,324\,800\,c^2\pi\theta^3}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \frac{4\,665\,600\,c^2\theta^4}{64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4} + \\
& \quad \left. \left( 9\,331\,200\pi\sqrt{\left( 256\,c^4\pi^5\theta - 448\,c^4\pi^4\theta^2 + 304\,c^4\pi^3\theta^3 - 100\,c^4\pi^2\theta^4 + 16\,c^4\pi\theta^5 - c^4\theta^6 \right)} \right) / \right. \\
& \quad \left. \left( 64\pi^4 - 96\pi^3\theta + 52\pi^2\theta^2 - 12\pi\theta^3 + \theta^4 \right) \right\} \right\}, \{\theta, -45\pi, 45\pi\}
\end{aligned}$$



```

RevolutionPlot3D[
  {
    -0.5`  $\sqrt{\left(\frac{1.6772928647657984 \cdot \theta^{24}}{12.566370614359172 - 1. \cdot \theta} + 2. \cdot \sqrt{\left(\frac{7.033278385485648 \cdot \theta^{47}}{(12.566370614359172 - 1. \cdot \theta)^2} - \right.}\right.}$ 
     $\left. \left(4. \cdot \left(2.2095695706493594 \cdot \theta^{48} - 3.516639192742824 \cdot \theta^{47} \right. \right. \right.$ 
     $\left. \left. \left. \theta^4 + 5.596905105957129 \cdot \theta^{46} - 4.4538755681467266 \cdot \theta^{45} \right. \right. \right.$ 
     $\left. \left. \left. \theta^6\right)\right)\right) / \left((12.566370614359172 - 1. \cdot \theta)^3 \theta\right)}\right)},$ 
    0.5`  $\sqrt{\left(\frac{1.6772928647657984 \cdot \theta^{24}}{12.566370614359172 - 1. \cdot \theta} + 2. \cdot \sqrt{\left(\frac{7.033278385485648 \cdot \theta^{47}}{(12.566370614359172 - 1. \cdot \theta)^2} - \right.}\right.}$ 
     $\left. \left(4. \cdot \left(2.2095695706493594 \cdot \theta^{48} - 3.516639192742824 \cdot \theta^{47} \right. \right. \right.$ 
     $\left. \left. \left. \theta^4 + 5.596905105957129 \cdot \theta^{46} - 4.4538755681467266 \cdot \theta^{45} \right. \right. \right.$ 
     $\left. \left. \left. \theta^6\right)\right)\right) / \left((12.566370614359172 - 1. \cdot \theta)^3 \theta\right)}\right)},$ 
    .5`  $\sqrt{\left(\frac{1.6772928647657984 \cdot \theta^{24}}{12.566370614359172 - 1. \cdot \theta} - 2. \cdot \sqrt{\left(\frac{7.033278385485648 \cdot \theta^{47}}{(12.566370614359172 - 1. \cdot \theta)^2} - \right.}\right.}$ 
     $\left. \left(4. \cdot \left(2.2095695706493594 \cdot \theta^{48} - 3.516639192742824 \cdot \theta^{47} \right. \right. \right.$ 
     $\left. \left. \left. \theta^4 + 5.596905105957129 \cdot \theta^{46} - 4.4538755681467266 \cdot \theta^{45} \right. \right. \right.$ 
     $\left. \left. \left. \theta^6\right)\right)\right) / \left((12.566370614359172 - 1. \cdot \theta)^3 \theta\right)}\right)}, \{\theta, -4 \pi, 4 \pi\}]$ 

```



$$\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}} = \text{velocity}$$

$$((1080 / \pi) \theta) = \text{time}$$

$$v * t = \eta$$

$$\text{Solve}\left[\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}} = c, \theta\right]$$

$$\{\{\theta \rightarrow 0.\}, \{\theta \rightarrow 6.28319\}\}$$

$$t = \theta / k == (\theta r) / (r k) == (2 \pi r - 2 \pi x) / (r k)$$

$$\text{Solve}[\theta / k$$

$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), t\right]$$

$$\left\{\left\{t \rightarrow -\frac{2 \left(-\pi r + \pi \sqrt{r^2 - \eta^2}\right)}{k r}\right\}\right\}$$



$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), k\right]$$

$$\left\{\left\{k \rightarrow \frac{2 \pi \left(r - \sqrt{r^2 - \eta^2}\right)}{r t}\right\}\right\}$$

$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 k \pi t - k^2 t^2}}\right\}, \left\{r \rightarrow \frac{2 \pi \eta}{\sqrt{4 k \pi t - k^2 t^2}}\right\}\right\}$$

$$\text{Solve}\left[\left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k) == \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) / k, k\right]$$

{{}}

$$\text{Solve}\left[\left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k) == \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) / k, r\right]$$

$$\text{Solve}\left[2 \pi \sqrt{r^2 - \eta^2} == 2 \pi r - (r k) t, \eta\right]$$

$$\text{Solve}\left[(2 \pi r - (r k) t) / (2 \pi) == \sqrt{r^2 - \eta^2}, \eta\right]$$

$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 k \pi r^2 t - k^2 r^2 t^2}}{2 \pi} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}, k\right]$$

{{}}

$$\text{Solve}\left[\left((2 \pi r - (r k) t) / (2 \pi)\right)^2 == (r^2 - \eta^2), \eta\right]$$

$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{4 k \pi r^2 t - k^2 r^2 t^2}}{2 \pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{4 k \pi r^2 t - k^2 r^2 t^2}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\left((2 \pi r - (r k) t) / (2 \pi)\right)^2 == (r^2 - \eta^2), \eta\right]$$

$$\text{Solve}\left[\left((2 \pi r - (r k) t) / (2 \pi)\right)^2 == \sqrt{r^2 - \eta^2}^2, \eta\right]$$

$$\text{Solve}\left[t == \left(2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}\right) / (r k), \eta\right]$$

$$\left\{\left\{\eta \rightarrow -\frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}, \left\{\eta \rightarrow \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{4 \pi - \theta}{k}\right\}, \left\{t \rightarrow \frac{\theta}{k}\right\}\right\}$$

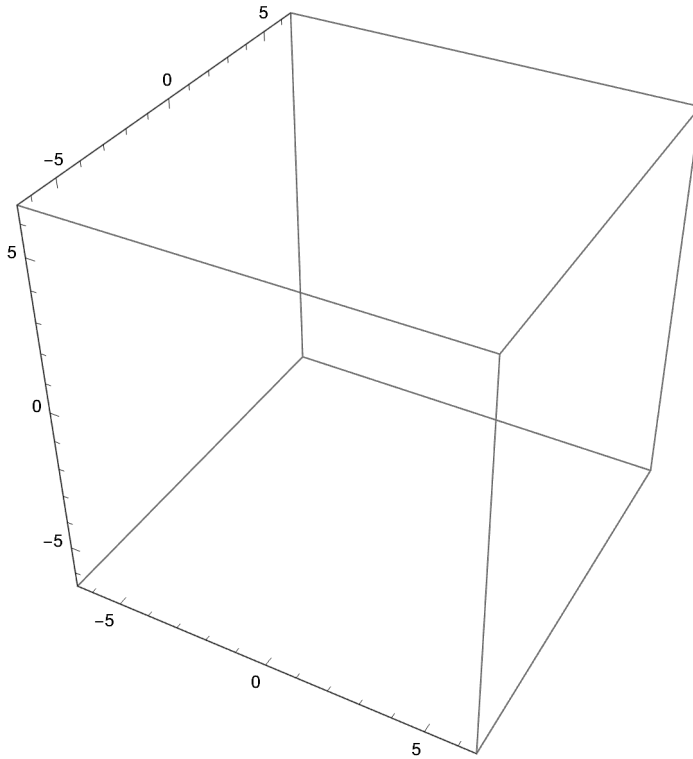
$$\text{Solve}\left[\eta == \frac{\sqrt{k} r \sqrt{t} \sqrt{4\pi - kt}}{2\pi}, k\right]$$

$$\left\{ \left\{ k \rightarrow \left( -\pi t \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right) - \right. \right. \right. \\ \sqrt{\left( \pi^2 t^2 \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right)^2 + \right.} \\ \left. 4 \pi^2 t^2 \eta^2 \theta \left( -1024 \pi^4 \theta + 1536 \pi^3 \theta^2 - 832 \pi^2 \theta^3 + 192 \pi \theta^4 - 16 \theta^5 - \right. \right. \\ \left. 1024 \pi^4 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 1280 \pi^3 \theta \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 512 \pi^2 \theta^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 64 \pi \theta^3 \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 1024 \pi^5 \sin[\beta]^2 + 1280 \pi^4 \theta \sin[\beta]^2 - 512 \pi^3 \theta^2 \sin[\beta]^2 + 64 \pi^2 \theta^3 \sin[\beta]^2 \right) \\ \left. \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \Bigg) \Bigg/ \\ \left. \left( 2 t^2 \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \right\}, \\ \left\{ k \rightarrow \left( -\pi t \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right) + \right. \right. \\ \sqrt{\left( \pi^2 t^2 \left( -64 \pi^2 \theta^2 + 32 \pi \theta^3 - 4 \theta^4 + 128 \pi^3 \theta \sin[\beta]^2 - 32 \pi^2 \theta^2 \sin[\beta]^2 - 64 \pi^4 \sin[\beta]^4 \right)^2 + \right.} \\ \left. 4 \pi^2 t^2 \eta^2 \theta \left( -1024 \pi^4 \theta + 1536 \pi^3 \theta^2 - 832 \pi^2 \theta^3 + 192 \pi \theta^4 - 16 \theta^5 - \right. \right. \\ \left. 1024 \pi^4 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 1280 \pi^3 \theta \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 512 \pi^2 \theta^2 \sqrt{(4\pi - \theta) \theta} \sin[\beta] + 64 \pi \theta^3 \sqrt{(4\pi - \theta) \theta} \sin[\beta] - \right. \\ \left. 1024 \pi^5 \sin[\beta]^2 + 1280 \pi^4 \theta \sin[\beta]^2 - 512 \pi^3 \theta^2 \sin[\beta]^2 + 64 \pi^2 \theta^3 \sin[\beta]^2 \right) \\ \left. \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \Bigg) \Bigg/ \\ \left. \left( 2 t^2 \left( 16 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 - 32 \pi^3 \theta \sin[\beta]^2 + 8 \pi^2 \theta^2 \sin[\beta]^2 + 16 \pi^4 \sin[\beta]^4 \right) \right) \right\} \Bigg\}$$

```

ContourPlot3D[
  (
    -π t (-64 π² θ² + 32 π θ³ - 4 θ⁴ + 128 π³ θ Sin[β]² - 32 π² θ² Sin[β]² - 64 π⁴ Sin[β]⁴) +
    √(
      π² t² (-64 π² θ² + 32 π θ³ - 4 θ⁴ + 128 π³ θ Sin[β]² - 32 π² θ² Sin[β]² - 64 π⁴ Sin[β]⁴)² +
      4 π² t² (
        √(4 π r² θ - r² θ²)
        /
        2 π
      )² θ (-1024 π⁴ θ + 1536 π³ θ² - 832 π² θ³ + 192 π θ⁴ -
        16 θ⁵ - 1024 π⁴ √(4 π - θ) θ Sin[β] + 1280 π³ θ √(4 π - θ) θ Sin[β] -
        512 π² θ² √(4 π - θ) θ Sin[β] + 64 π θ³ √(4 π - θ) θ Sin[β] -
        1024 π⁵ Sin[β]² + 1280 π⁴ θ Sin[β]² - 512 π³ θ² Sin[β]² + 64 π² θ³ Sin[β]²)
      (16 π² θ² - 8 π θ³ + θ⁴ - 32 π³ θ Sin[β]² + 8 π² θ² Sin[β]² + 16 π⁴ Sin[β]⁴)
    )
  ) /
  (2 t² (16 π² θ² - 8 π θ³ + θ⁴ - 32 π³ θ Sin[β]² + 8 π² θ² Sin[β]² + 16 π⁴ Sin[β]⁴)), {θ,
-2 π,
2 π}, {t,
-2 π,
2 π}, {β,
-2 π,
2 π}]

```



$$\text{Solve}\left[\frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, k\right]$$

$$\left\{\left\{k \rightarrow \frac{4 \pi - \theta}{t}\right\}, \left\{k \rightarrow \frac{\theta}{t}\right\}\right\}$$

$$t = \theta / k = \theta / \frac{4 \pi - \theta}{t}$$

$$\text{Solve}\left[\theta / \frac{4 \pi - \theta}{t} == t, t\right]$$

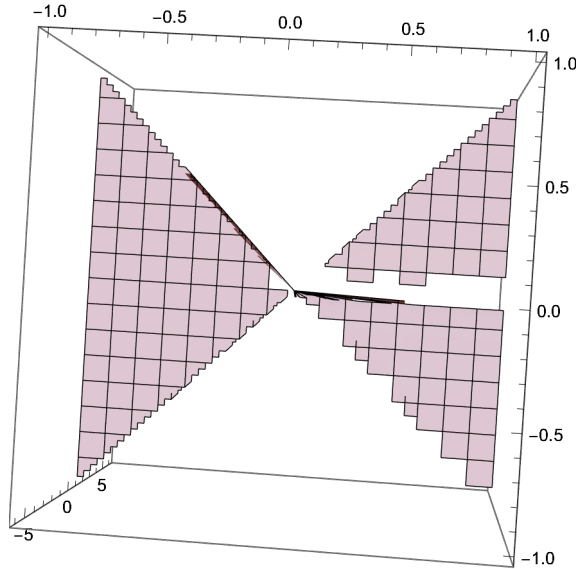
$$\{\{t \rightarrow 0\}\}$$

$$\text{Solve}\left[\theta / \frac{4 \pi - \theta}{t} == t, \theta\right]$$

$$\{\{\theta \rightarrow 2 \pi\}\}$$

$$\text{Solve}[\theta r == y r - y \sqrt{r^2 - \eta^2}, y]$$

$$\left\{ \left\{ y \rightarrow -\frac{r \theta}{-r + \sqrt{r^2 - \eta^2}} \right\} \right\}$$



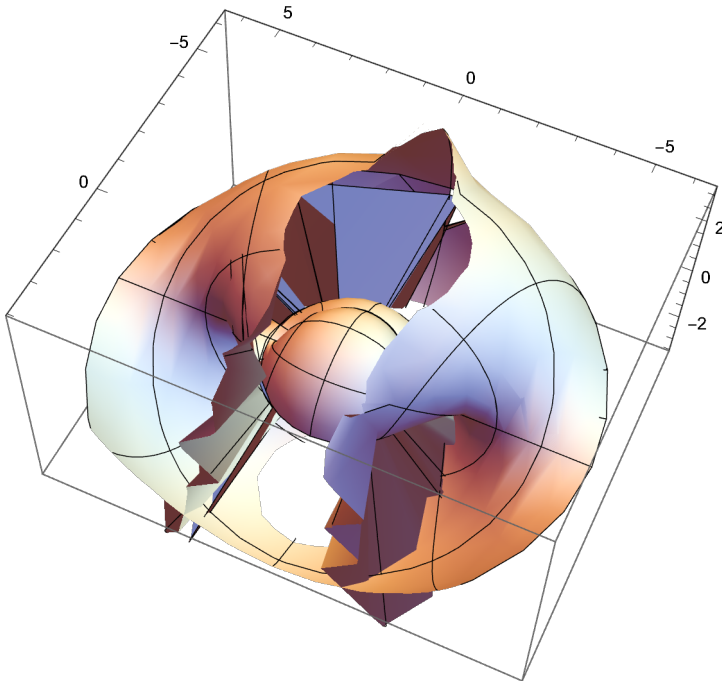
$$\frac{r \theta}{-r + \sqrt{r^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2}}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4 \pi - k t}}{2 \pi}, k\right]$$

$$\left\{ \left\{ k \rightarrow \frac{4 \pi - \theta}{t} \right\}, \left\{ k \rightarrow \frac{\theta}{t} \right\} \right\}$$

SphericalPlot3D $\left[\frac{r \theta}{-r + \sqrt{r^2 - \left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right)^2}}, \{\theta, -2 \pi, 2 \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = h$$

$$\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = h$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \eta, \eta\right]$$

$$\left\{\left\{\eta \rightarrow \frac{\sqrt{r(-2 \pi + 2 \pi r + k t)}}{\sqrt{2 \pi}}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \eta, k\right]$$

$$\left\{\left\{k \rightarrow -\frac{2(-\pi r + \pi r^2 - \pi \eta^2)}{r t}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, k\right]$$

$$\left\{\left\{k \rightarrow \frac{4 \pi^2 - 4 \pi^2 r + 4 \pi r \theta - r \theta^2}{2 \pi t}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2 \pi r - k r t) / (2 \pi))} = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$$

$$\left\{\{r \rightarrow 0\}, \left\{r \rightarrow \frac{2 \pi(2 \pi - k t)}{(2 \pi - \theta)^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2\pi r - k r t) / (2\pi))} == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{4\pi^2 - 4\pi^2 r + 4\pi r \theta - r \theta^2}{2k\pi}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2\pi r - k r t) / (2\pi))} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4\pi - k t}}{2\pi}, r\right]$$

$$\left\{\{r \rightarrow 0\}, \left\{r \rightarrow \frac{2\pi}{2\pi - k t}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{r^2 - ((2\pi r - k r t) / (2\pi))} == \frac{\sqrt{k} r \sqrt{t} \sqrt{4\pi - k t}}{2\pi}, t\right]$$

$$\left\{\left\{t \rightarrow \frac{2\pi}{k}\right\}, \left\{t \rightarrow \frac{2\pi(-1+r)}{k r}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r \theta}}{2\pi} == r \sin[\beta], \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{1}{-8.98755 \times 10^{16} + v^2}\right\}\right\}$$

$$0.5 \left( -1.12941 \times 10^{18} + 12.5664 v^2 - 1. \sqrt{\left( (1.12941 \times 10^{18} - 12.5664 v^2)^2 - 4. (-8.98755 \times 10^{16} + v^2) (-3.54814 \times 10^{18} + 39.4784 v^2) \sin[\beta]^2 \right)} \right), \left\{\theta \rightarrow \right.$$

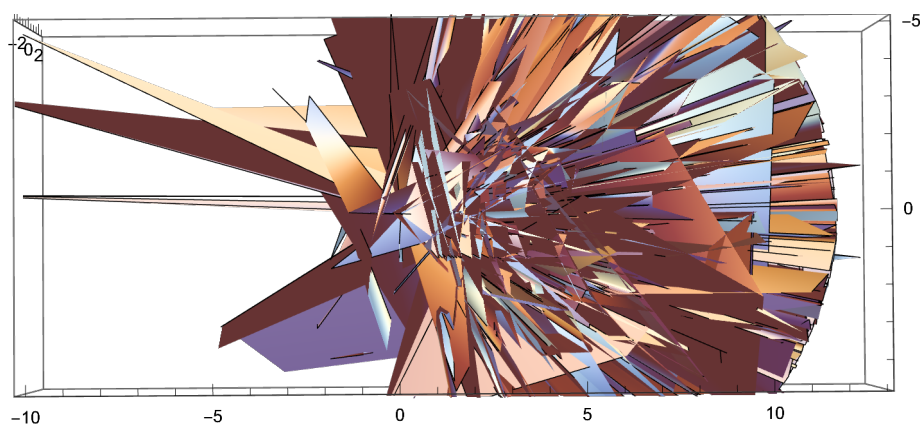
$$\left. \frac{1}{-8.98755 \times 10^{16} + v^2} 0.5 \left( -1.12941 \times 10^{18} + 12.5664 v^2 + \sqrt{\left( (1.12941 \times 10^{18} - 12.5664 v^2)^2 - 4. (-8.98755 \times 10^{16} + v^2) (-3.54814 \times 10^{18} + 39.4784 v^2) \sin[\beta]^2 \right)} \right) \right\}$$

$$v := \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + \right.$$

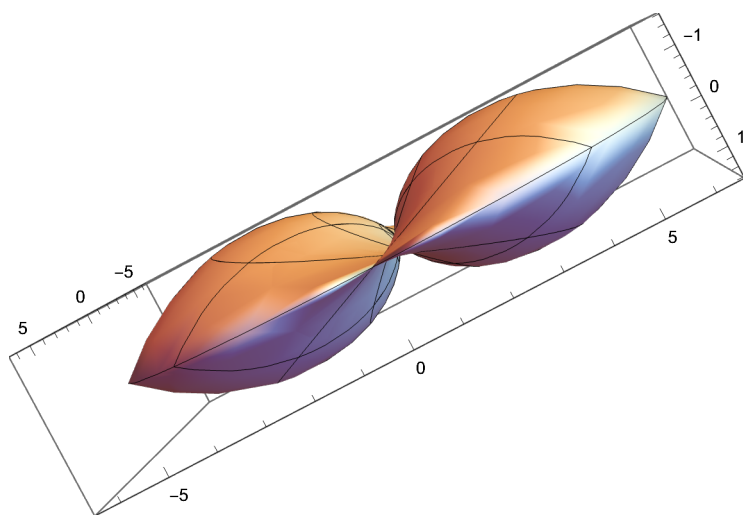
$$8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2) \Big/$$

$$\left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right)$$

$$\text{SphericalPlot3D}\left[\frac{1}{-8.987551787368176 \cdot v^{16} + v^2}\right. \\
0.5 \cdot \left(-1.1294090667581471 \cdot v^{18} + 12.566370614359172 \cdot v^2 + \right. \\
\left.\sqrt{\left((1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2)^2 - \right.}\right. \\
\left.\left.4 \cdot (-8.987551787368176 \cdot v^{16} + v^2) (-3.5481432270250993 \cdot v^{18} + \right. \right. \\
\left.\left.39.47841760435743 \cdot v^2) \sin[\beta]^2\right)\right], \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



$$\text{SphericalPlot3D}\left[\frac{1}{-8.987551787368176 \cdot v^{16} + v^2}\right. \\
0.5 \cdot \left(-1.1294090667581471 \cdot v^{18} + 12.566370614359172 \cdot v^2 + \right. \\
\left.\sqrt{\left((1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2)^2 - \right.}\right. \\
\left.\left.4 \cdot (-8.987551787368176 \cdot v^{16} + v^2) (-3.5481432270250993 \cdot v^{18} + \right. \right. \\
\left.\left.39.47841760435743 \cdot v^2) \sin[\beta]^2\right)\right], \{v, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}]$$



$c := 2.99792458 (10^8)$

$\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$

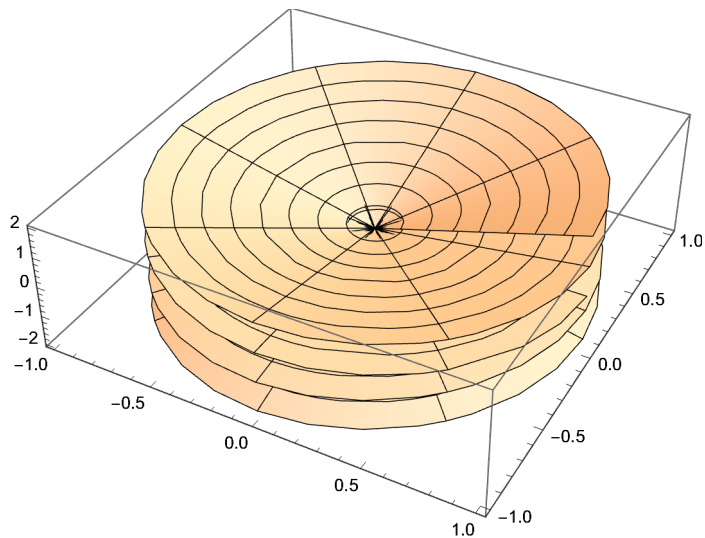


$$\text{ArcCos}[\eta / r] == \beta$$

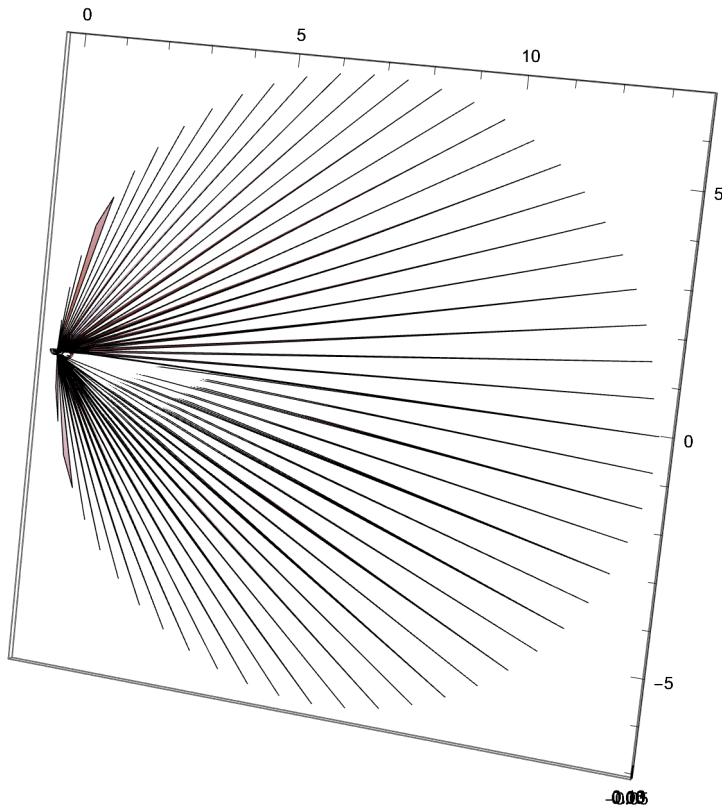
$$\text{Solve}\left[\text{ArcCos}[\eta / r] == \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], \eta\right]$$

$$\left\{\left\{\eta \rightarrow r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



`SphericalPlot3D` $\left[r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \{\theta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



$$\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} == r \sqrt{1 - \frac{(4\pi - \theta)\theta}{4\pi^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow (2 - \sqrt{2})\pi\right\}, \left\{\theta \rightarrow (2 + \sqrt{2})\pi\right\}\right\}$$

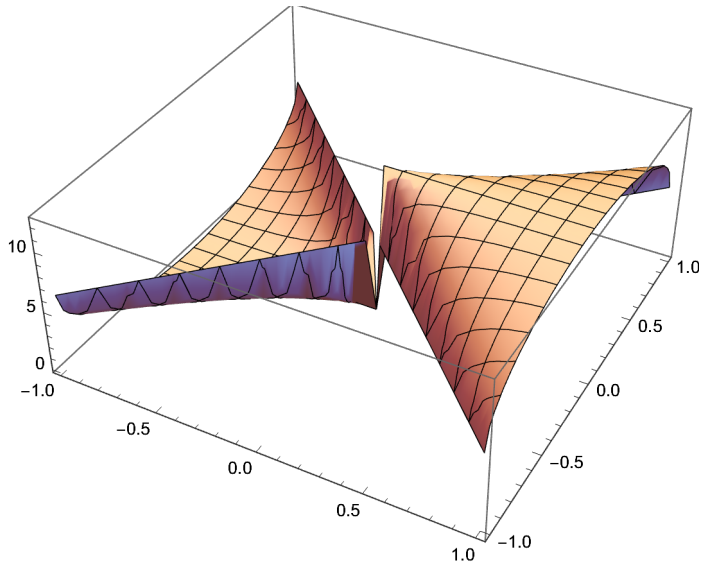
$$c := 2.99792458 * (10^8)$$

$$\text{Solve}\left[\frac{\sqrt{r \sqrt{1 - \frac{(4\pi - \theta)\theta}{c^2}}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(4\pi - \theta)\theta}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == \eta, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{0.5 \left(12.5664 r^2 - 12.5664 r \sqrt{1. r^2 - 1. \eta^2}\right)}{r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow \frac{0.5 \left(12.5664 r^2 + 12.5664 r \sqrt{1. r^2 - 1. \eta^2}\right)}{r^2}\right\}\right\}$$

Plot3D[ $\frac{0.5 \cdot (12.566370614359172 \cdot r^2 + 12.566370614359172 \cdot r \sqrt{1. \cdot r^2 - 1. \cdot \eta^2})}{r^2}$ ,  
 $\{r, -1, 1\}, \{\eta, -1, 1\}$ ]

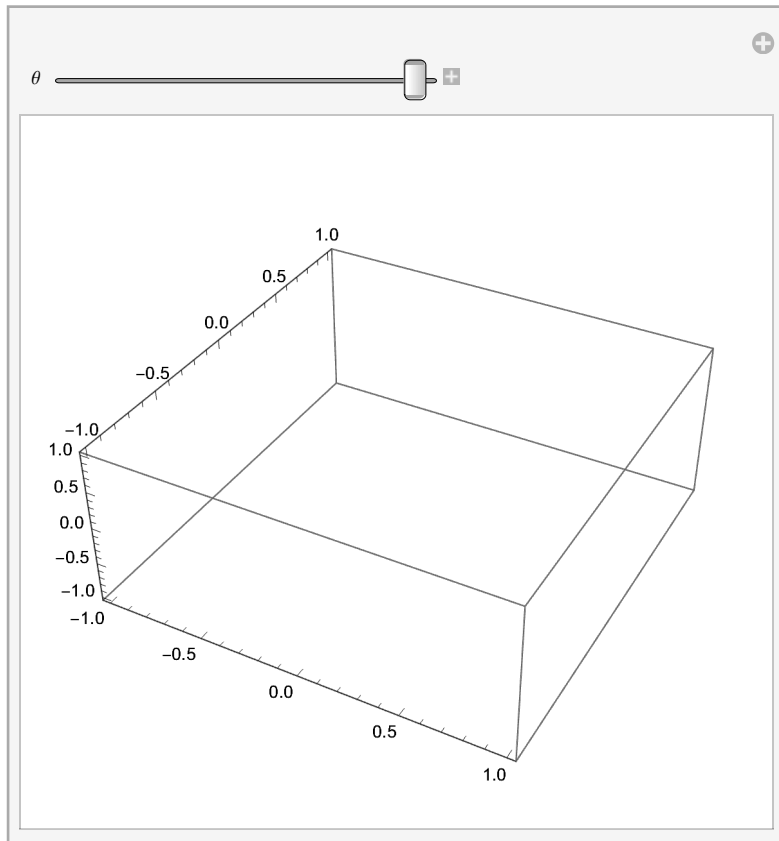


$$r = \sqrt{x^2 + y^2 + z^2} = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}$$

$$\text{Solve}\left[r = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2\pi \sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}\right\}, \left\{r \rightarrow \frac{2\pi \sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}\right\}\right\}$$

$$\text{Manipulate}\left[\text{Plot3D}\left[\frac{2\pi \sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}, \{x, -1, 1\}, \{y, -1, 1\}\right], \{\theta, -2\pi, 2\pi}\right]$$



Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

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General::stop : Further output of Power::infy will be suppressed during this calculation. >>

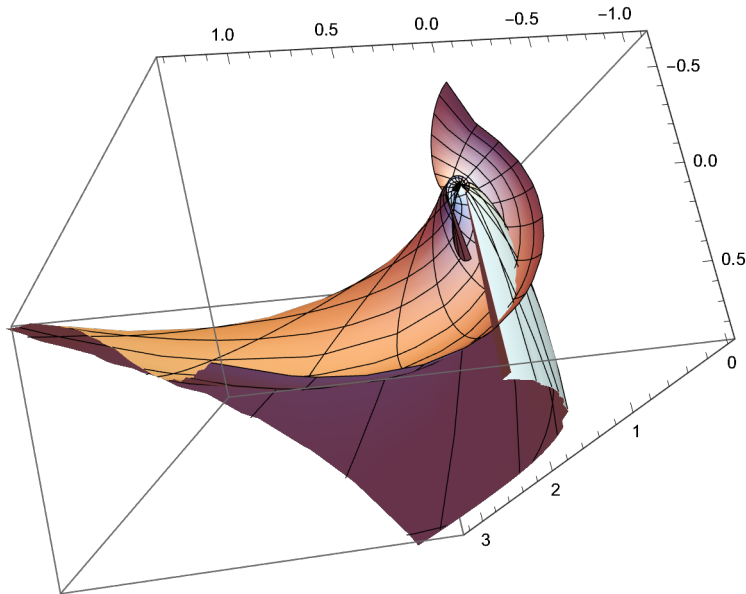
... Power: Infinite expression  $\frac{1}{0.}$  encountered.

... Power: Infinite expression  $\frac{1}{0.}$  encountered.

... Power: Infinite expression  $\frac{1}{0.}$  encountered.

General: Further output of Power::infy will be suppressed during this calculation.

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{\left(\frac{2 \pi r-r \theta}{2 \pi}\right)^2+\left(\frac{\sqrt{4 \pi r^2 \theta-r^2 \theta^2}}{2 \pi}\right)^2}}{\sqrt{4 \pi^2-4 \pi \theta+\theta^2}},\{\beta,-\pi / 2, \pi / 2\},\{\theta,-2 \pi, 2 \pi\}\right]$$



$$\text{Solve}\left[\frac{r \sqrt{\pi^2-\text{ArcCos}\left[\sqrt{\frac{1}{2}+\frac{1}{2} \sqrt{1-\text{Sin}[\theta]^2}}\right]}}{\pi}==r \text{Sin}[\beta], \beta\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{1}{\pi}\left(\sqrt{\left(\pi-\text{ArcCos}\left[\sqrt{\frac{1}{2}+\frac{1}{2} \sqrt{1-\text{Sin}[\theta]^2}}\right]}\right)\left(\pi+\text{ArcCos}\left[\sqrt{\frac{1}{2}+\frac{1}{2} \sqrt{1-\text{Sin}[\theta]^2}}\right]}\right)\right]\right\}\right\}$$

$$c:=2.99792458\left(10^8\right)$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1-\frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}} \sqrt{4 \pi r-r \theta}}{2 \pi}==r, v\right]$$

$$\text{Solve}\left[\frac{r \sqrt{1 - \left(\frac{v^2}{c^2}\right)} \sqrt{\pi^2 - \text{ArcCos}\left[\sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{1 - \text{Sin}\left[\theta / \sqrt{1 - \left(\frac{v^2}{c^2}\right)}\right]^2}}\right]^2}}{\pi} = r \text{Sin}[\beta], v\right]$$

Solve::tdep : The equations appear to involve the variables to be solved for in an essentially non-algebraic way. >>

$$\text{Solve}\left[\frac{1}{\pi} r \sqrt{1 - 1.11265 \times 10^{-17} v^2} \sqrt{\pi^2 - \text{ArcCos}\left[\sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{1 - \text{Sin}\left[\frac{\theta}{\sqrt{1 - 1.11265 \times 10^{-17} v^2}}\right]^2}}\right]^2} = r \text{Sin}[\beta], v\right]$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta] + 4\pi^2 \text{Sin}[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \text{Sin}[\beta]^2 + 8\pi^2\theta \text{Sin}[\beta]^2)$$

$$\text{Solve}\left[\frac{\frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}}{2\pi r - r\theta - 2\pi \sqrt{r^2 - \frac{\sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}}}{\sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{4\pi r - r\theta}}}} = t, v\right]$$

Power::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

$$\text{Solve}\left[\frac{\sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, v\right]$$

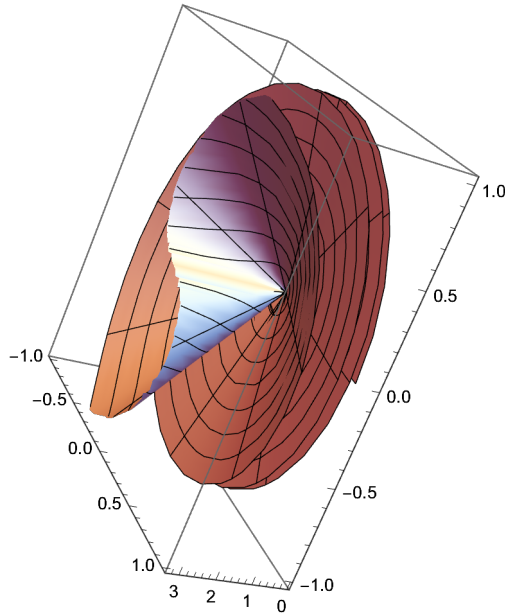
Set::write : Tag Times in  $\frac{\sqrt{\frac{\theta}{\sqrt{1 - \ll 24 \gg v^2}}} \sqrt{\frac{\ll 1 \gg}{\ll 1 \gg}} \sqrt{\frac{4\pi(\ll 1 \gg)}{\ll 1 \gg}} - \frac{\theta(\ll 1 \gg)}{\ll 1 \gg}}{2\pi}$  is Protected. >>

Solve::eqf :  $\eta$  is not a well-formed equation. >>

Solve[ $\eta, v$ ]

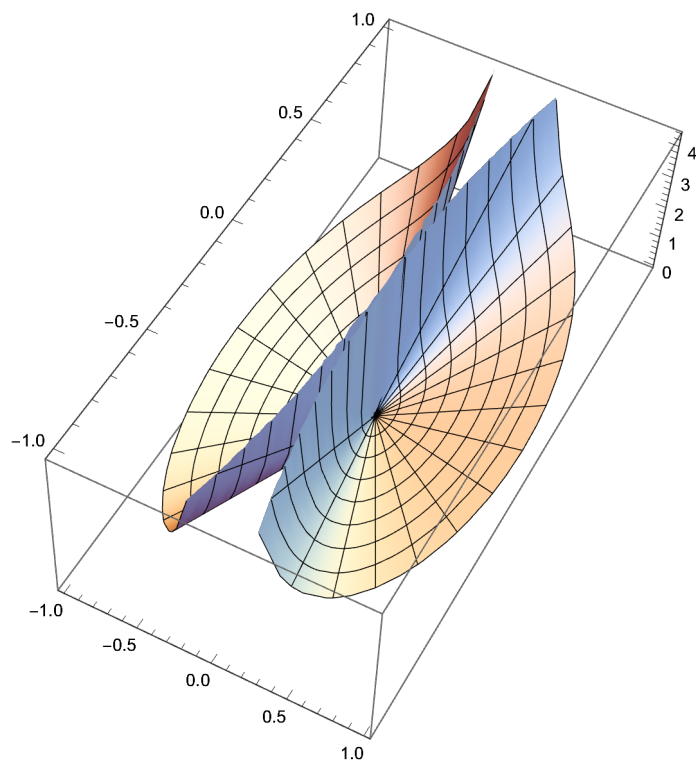
$$\text{Solve}\left[\frac{\sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = r, v\right]$$

$$\text{RevolutionPlot3D}\left[\frac{2 \pi \sqrt{\left(\frac{2 \pi r-r \theta}{2 \pi}\right)^2+\left(\frac{\sqrt{4 \pi r^2 \theta-r^2 \theta^2}}{2 \pi}\right)^2}}{\sqrt{4 \pi^2-4 \pi \theta+\theta^2}},\{r,-1,1\},\{\theta,-2 \pi, 2 \pi\}\right]$$



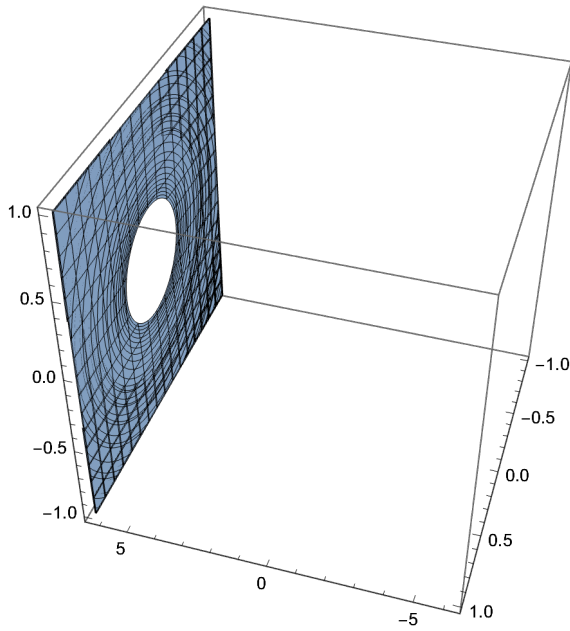
$$\text{RevolutionPlot3D}\left[\frac{2 \pi \sqrt{\left(\frac{2 \pi r-r \theta}{2 \pi}\right)^2+\left(\frac{\sqrt{4 \pi r^2 \theta-r^2 \theta^2}}{2 \pi}\right)^2}}{\sqrt{4 \pi^2-4 \pi \theta+\theta^2}},\{r,-1,1\},\{\theta,-2 \pi, 2 \pi\}\right]$$

$\text{RevolutionPlot3D}\left[\frac{1}{\sqrt{4\pi^2 - 4\pi^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right) + \left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}}\right.$   
 $2\pi\sqrt{\left(\left(\frac{2\pi r - r^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)}{2\pi}\right)^2 + \left(\frac{1}{2\pi}\left(\sqrt{4\pi r^2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right) - r^2\left(2\left(\pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2}\right)\right)^2}\right)\right)^2},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}\right]$





ContourPlot3D $\left[\frac{2 \pi \sqrt{x^2 + (y)^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{x, -1, 1\}, \{y, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$z == r \cos[\beta]$$

$$\text{Solve}\left[r == \frac{2 \pi \sqrt{\left(\frac{2 \pi r - r \theta}{2 \pi}\right)^2 + y^2}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, r\right]$$

{}

$$\text{Solve}\left[r == \sqrt{\frac{2 \pi r - r \theta}{2 \pi}^2 + y^2} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r\right]$$

{}

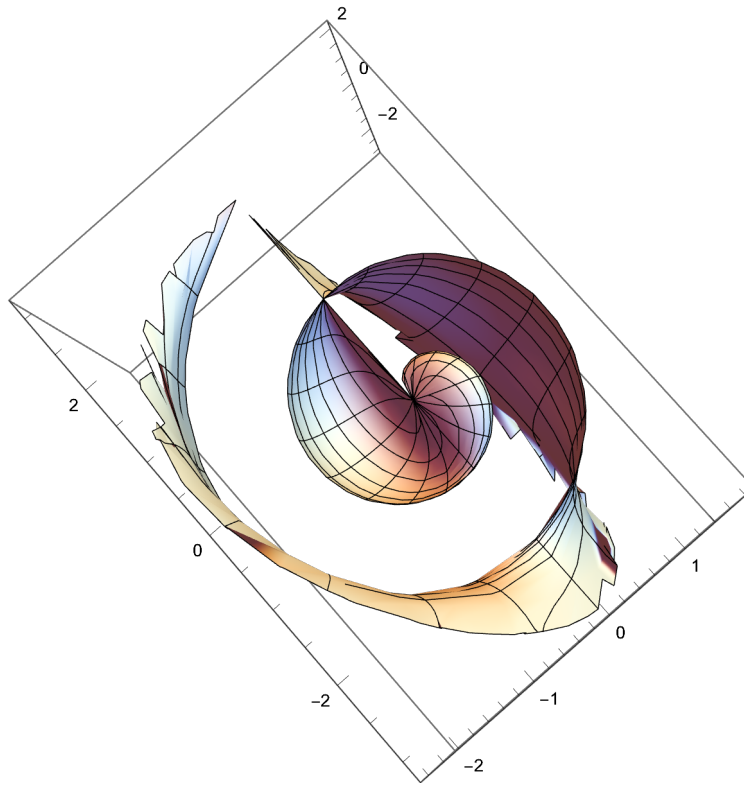
$$\beta == \text{ArcCos}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} / r\right]$$

$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} == r \sin[\beta] \cos[\phi], \phi\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\phi \rightarrow -\text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}, \left\{\phi \rightarrow \text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}\right\}$$

`SphericalPlot3D[ArcCos[ $\frac{(2\pi - \theta) \text{Csc}[\beta]}{2\pi}$ ], {\theta, -2\pi, 2\pi}, {\beta, -\pi/2, \pi/2}]`

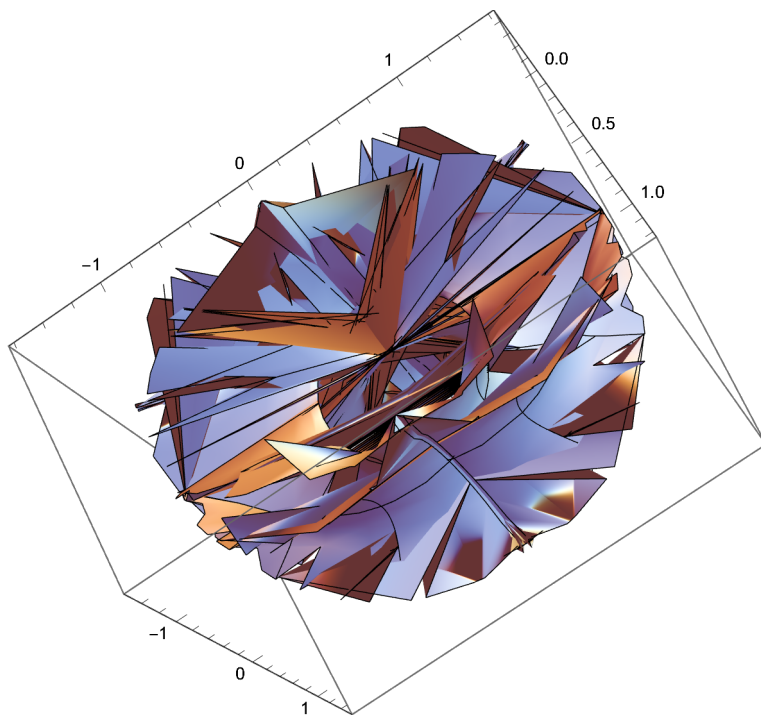


`Solve[ $\frac{2\pi r - r\theta}{2\pi} == r \text{Sin}[\beta] \text{Cos}[\phi], \beta]$`

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

`{ {  $\beta \rightarrow \text{ArcSin}\left[\frac{(2\pi - \theta) \text{Sec}[\phi]}{2\pi}\right]$  } }`

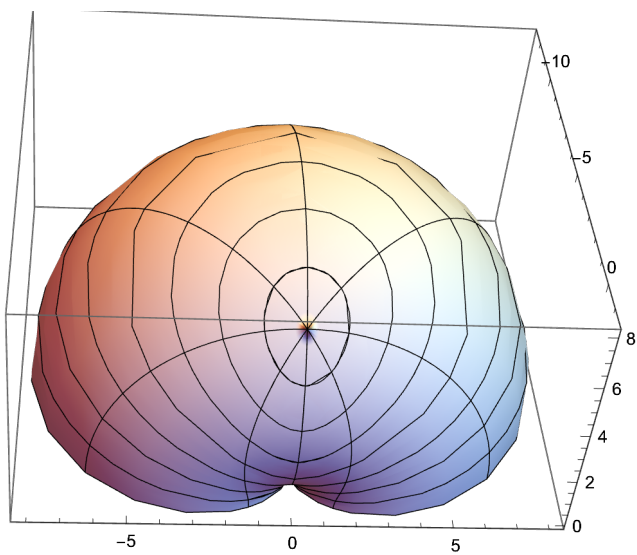
`SphericalPlot3D[ArcSin[ $\frac{(2\pi - \theta) \text{Sec}[\phi]}{2\pi}$ ], {\theta, -2\pi, 2\pi}, {\phi, -\pi, \pi}]`

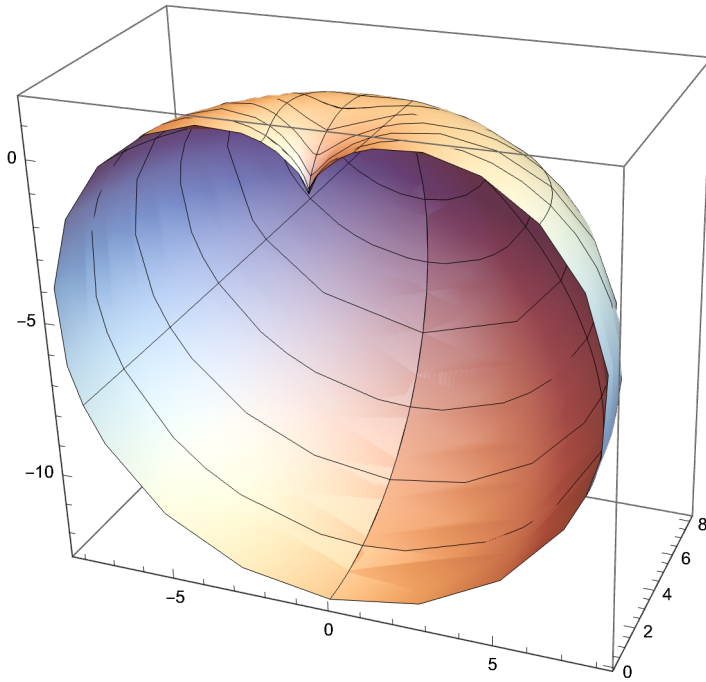


`Solve[ $\frac{2\pi r - r\theta}{2\pi} == r \text{Sin}[\beta] \text{Cos}[\phi], \theta]$`

`{{\theta \to -2\pi (-1 + \text{Cos}[\phi] \text{Sin}[\beta])}}`

`SphericalPlot3D[-2\pi (-1 + \text{Cos}[\phi] \text{Sin}[\beta]), {\beta, -\pi/2, \pi/2}, {\phi, -2\pi, 2\pi}]`





$$r := \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$$

$$\text{Solve}\left[\frac{2 \pi r - r \theta}{2 \pi} = r \sin[\beta] \cos[\phi], \phi\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\phi \rightarrow -\text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}, \left\{\phi \rightarrow \text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right\}\right\}$$

$$\text{Solve}\left[\frac{2 \pi r - r 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2 \pi} = r \sin[\beta] \cos[\phi], \phi\right]$$

Solve::ifun : Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information. >>

$$\left\{\left\{\phi \rightarrow -\text{ArcCos}\left[-\csc[\beta] \sqrt{1 - \sin[\beta]^2}\right]\right\}, \left\{\phi \rightarrow \text{ArcCos}\left[-\csc[\beta] \sqrt{1 - \sin[\beta]^2}\right]\right\}\right\}$$

$$\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$r := \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)$$

$$r = \sqrt{x^2 + y^2 + z^2} = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2} =$$

$$\sqrt{(r \sin[\theta] \cos[\phi])^2 + (r \sin[\theta] \sin[\phi])^2 + (r \cos[\theta])^2}$$

$$\sqrt{(r \sin[\theta] \cos[\phi])^2 + (r \sin[\theta] \sin[\phi])^2 + (r \cos[\theta])^2} = r$$

$$\text{Solve}\left[r = \sqrt{x^2 + y^2 + z^2}, z\right]$$

$$\left\{\left\{z \rightarrow -\frac{1}{2} \sqrt{\left(-4x^2 - 4y^2 + \frac{1}{(2\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)(4\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)^2(4\pi - \theta)} - \frac{4\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(4\pi - \theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi - \theta)^2} + \frac{\sin[\beta]^2}{(4\pi - \theta)\theta}\right)}\right\},$$

$$\left\{z \rightarrow \frac{1}{2} \sqrt{\left(-4x^2 - 4y^2 + \frac{1}{(2\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)(4\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)^2(4\pi - \theta)} - \frac{4\sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(4\pi - \theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi - \theta)^2} + \frac{\sin[\beta]^2}{(4\pi - \theta)\theta}\right)}\right\}\right\}$$

$$\text{Solve}\left[r = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, y\right]$$

{{}}

$$\text{Solve}\left[r = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, x\right]$$

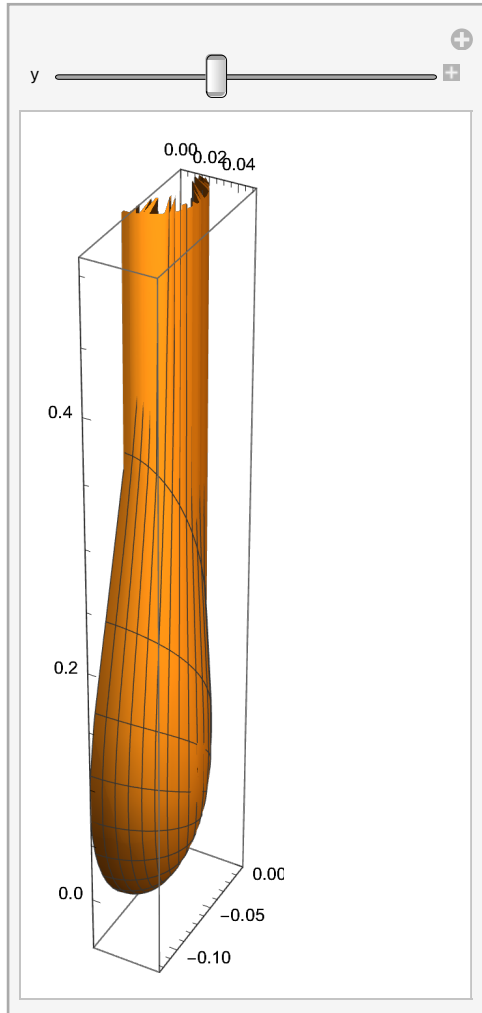
{{}}

$$\text{Solve}\left[r = \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}, x\right]$$

$$\begin{aligned}
& \text{Solve} \left[ \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \right. \\
& \quad \left. \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}^2, x \right] \\
& \left\{ \left\{ x \rightarrow -\frac{\sqrt{1 - 16\pi^2 y^2 - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta}}}{4\pi} \right\}, \right. \\
& \quad \left. \left\{ x \rightarrow \frac{\sqrt{1 - 16\pi^2 y^2 - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta}}}{4\pi} \right\} \right\}
\end{aligned}$$

Manipulate[

SphericalPlot3D[ $\frac{\sqrt{1 - 16 \pi^2 y^2 - \frac{\sqrt{(4 \pi - \theta) \theta} \sin[\beta]}{4 \pi - \theta} - \frac{\sqrt{(4 \pi - \theta) \theta} \sin[\beta]}{\theta} + \frac{\pi \sin[\beta]^2}{4 \pi - \theta} + \frac{\pi \sin[\beta]^2}{\theta}}}{4 \pi}$ ,  
 $\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}, \{y, -1, 1\}$ ]



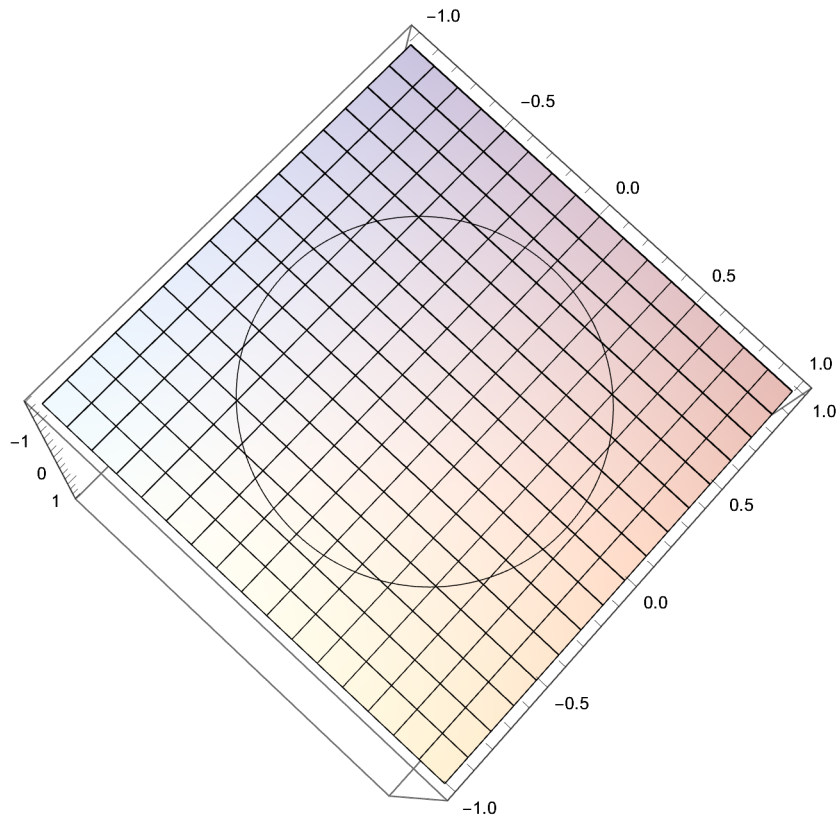
$$\begin{aligned}
& \text{Solve} \left[ \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2) == \right. \\
& \quad \left. \sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}^2, x \right] \\
& \left\{ \left\{ x \rightarrow -\frac{1}{4\pi} \left( \sqrt{\left( -16\pi^2y^2 + \frac{4\pi^2}{(2\pi-\theta)^2} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 16\pi r^2\theta + 4r^2\theta^2 - \frac{4\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)^2} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \frac{4\pi^2\sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta} \right) \right) \right\}, \right. \\
& \left. \left\{ x \rightarrow \frac{1}{4\pi} \left( \sqrt{\left( -16\pi^2y^2 + \frac{4\pi^2}{(2\pi-\theta)^2} - 16\pi r^2\theta + 4r^2\theta^2 - \frac{4\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)^2} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{\theta} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{4\pi^2\sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\pi\sin[\beta]^2}{4\pi-\theta} + \frac{\pi\sin[\beta]^2}{\theta} \right) \right) \right\} \right\} \\
& \frac{1}{2} \sqrt{\left( -4x^2 - 4y^2 + \frac{1}{(2\pi-\theta)^2} - \frac{2\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)(4\pi-\theta)^2} - \right. \\
& \quad \left. \frac{2\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(2\pi-\theta)^2(4\pi-\theta)} - \frac{4\sqrt{(4\pi-\theta)\theta}\sin[\beta]}{(4\pi-\theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\sin[\beta]^2}{(4\pi-\theta)\theta} \right)} \\
& \theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2\sin[\beta]^2} \right)
\end{aligned}$$

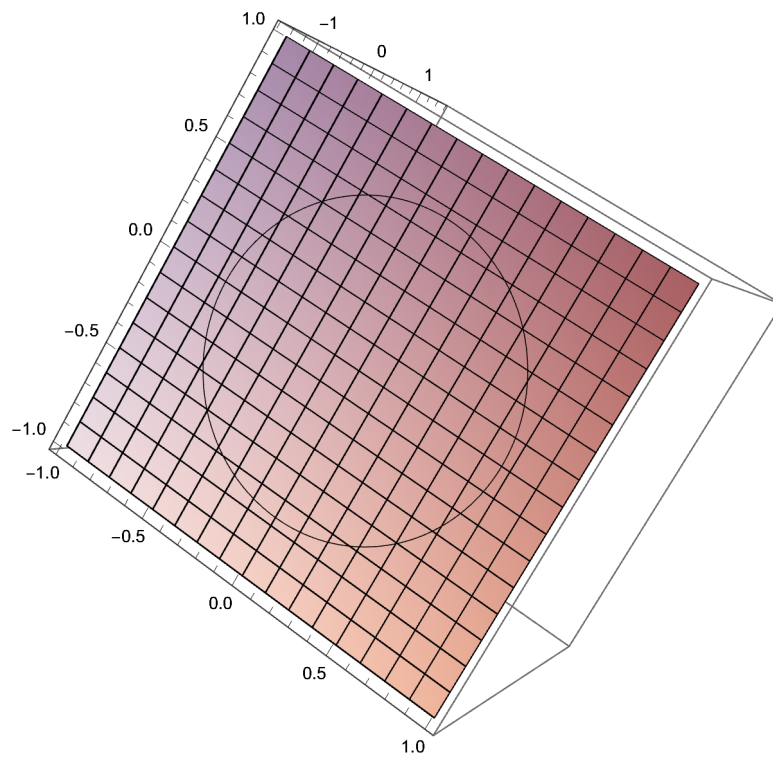
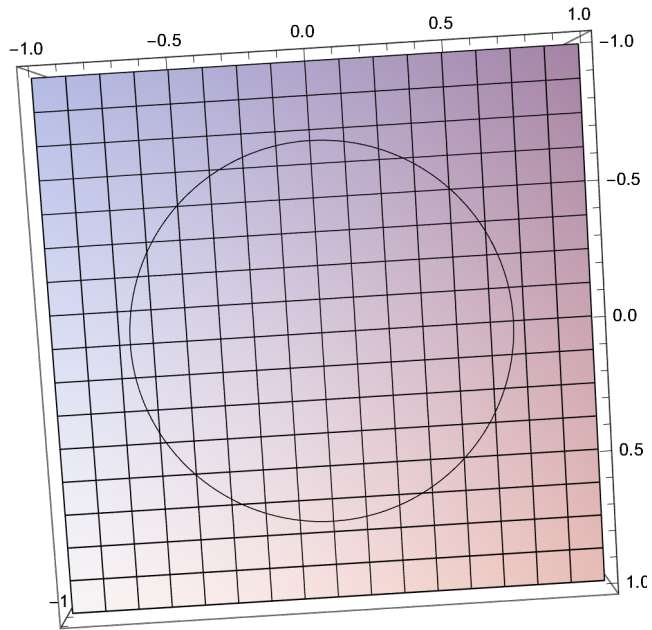


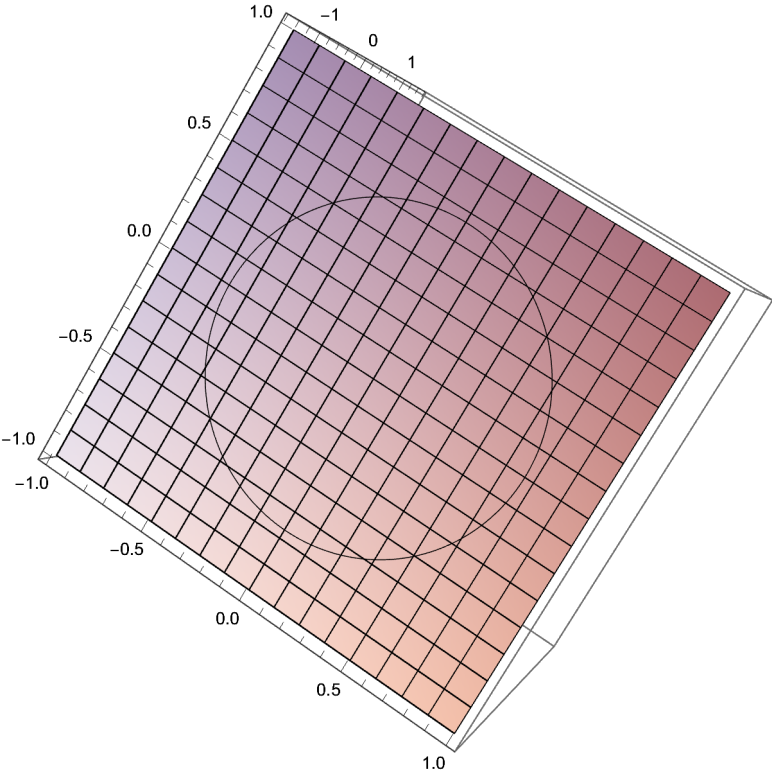
ContourPlot3D[

$$\frac{1}{2} \sqrt{\left( -4x^2 - 4y^2 + \frac{1}{(2\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta}\sin[\beta]}{(2\pi - \theta)(4\pi - \theta)^2} - \frac{2\sqrt{(4\pi - \theta)\theta}\sin[\beta]}{(2\pi - \theta)^2(4\pi - \theta)} - \frac{4\sqrt{(4\pi - \theta)\theta}\sin[\beta]}{(4\pi - \theta)^2\theta} + \frac{\sin[\beta]^2}{(2\pi - \theta)^2} + \frac{\sin[\beta]^2}{(4\pi - \theta)\theta} \right)},$$

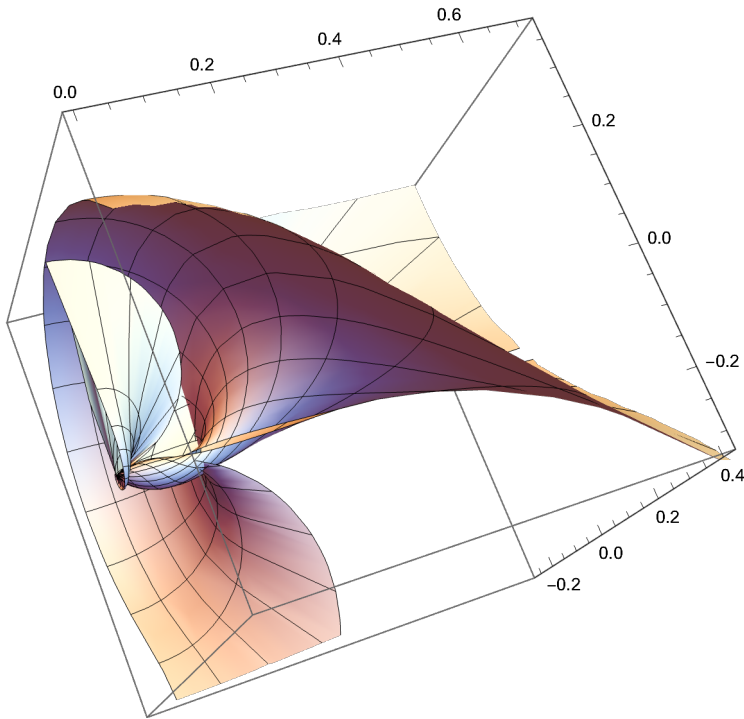
{x, -1, 1}, {y, -1, 1}, {\beta, -\pi/2, \pi/2}]





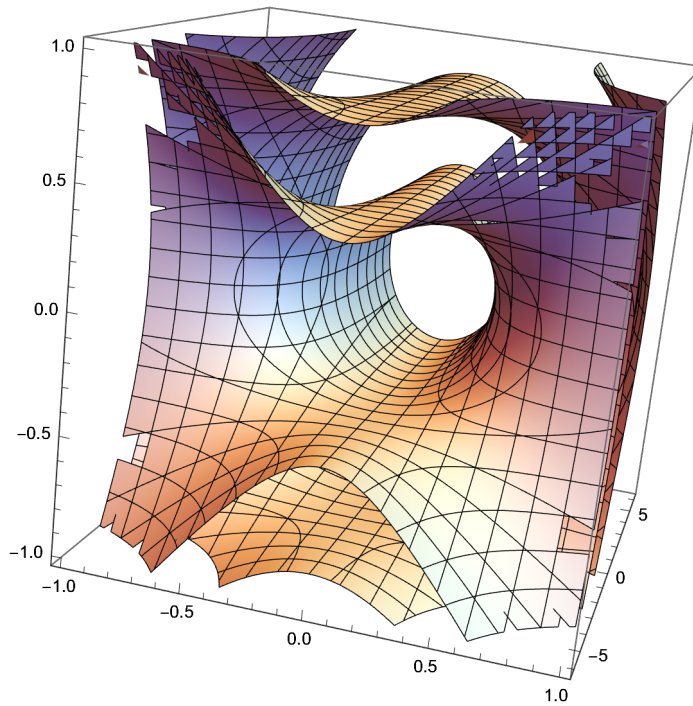


`SphericalPlot3D` $\left[\sqrt{\left(\left(r \sin[\beta] \cos\left[\text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right)\right)^2 + \left(r \sin[\beta] \sin\left[\text{ArcCos}\left[\frac{(2 \pi - \theta) \csc[\beta]}{2 \pi}\right]\right)\right)^2 + (r \cos[\beta])^2}, \right.$   
 $\left.\{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}\right]$



`ContourPlot3D` $\left[\sqrt{x^2 + y^2 + z^2}, \{x, -1, 1\}, \{y, -2 \pi, 2 \pi\}, \{z, -1, 1\}\right]$

`ContourPlot3D[ $\sqrt{r^2 + x^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2}$ , {r, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }, {x, -1, 1}]`

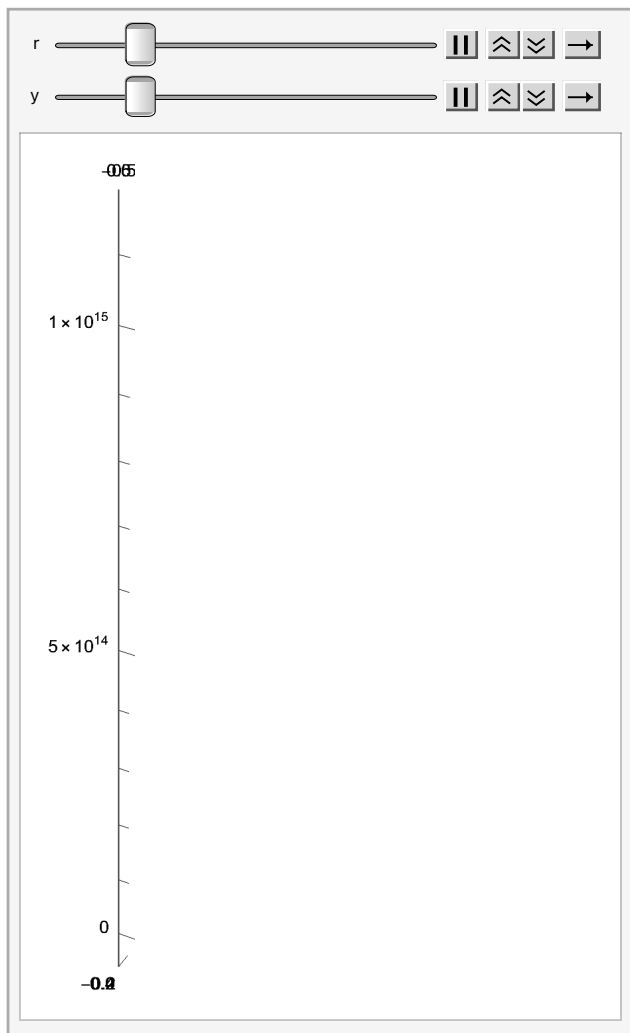


`ContourPlot3D[ $\sqrt{r^2 + x^2 + z^2}$ , {r, -1, 1}, {z, -1, 1}, {x, -1, 1}]`

Animate[SphericalPlot3D[

$$\frac{1}{4\pi} \left( \sqrt{\left( -16\pi^2 y^2 + \frac{4\pi^2}{(2\pi-\theta)^2} - 16\pi r^2 \theta + 4r^2 \theta^2 - \frac{4\pi \sqrt{(4\pi-\theta)\theta} \sin[\beta]}{(2\pi-\theta)^2} - \frac{\sqrt{(4\pi-\theta)\theta} \sin[\beta]}{4\pi-\theta} - \frac{\sqrt{(4\pi-\theta)\theta} \sin[\beta]}{\theta} + \frac{4\pi^2 \sin[\beta]^2}{(2\pi-\theta)^2} + \frac{\pi \sin[\beta]^2}{4\pi-\theta} + \frac{\pi \sin[\beta]^2}{\theta} \right)} \right),$$

$$\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}, \{r, -1, 1\}, \{y, -1, 1\}]$$



$$\text{Solve}\left[r == \sqrt{\left(x^2 + y^2 + \left(\frac{1}{4\pi^2} \left(\sqrt{\left(64\pi^4 r^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 r^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2(4\pi - \theta)\theta} - \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{r^2(4\pi - \theta)\theta}\right)}\right)^2\right)}, y\right]$$

$$\left\{\left\{y \rightarrow -\frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2(4\pi - \theta)\theta} + \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2(4\pi - \theta)\theta}\right)}\right\},\right.$$

$$\left.\left\{y \rightarrow \frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2(4\pi - \theta)\theta} + \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2(4\pi - \theta)\theta}\right)}\right\}\right\}$$

Export["lldradius.avi"]

Export["lldradius.avi",

$$\text{Animate}\left[\text{Plot3D}\left[\frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2(4\pi - \theta)\theta} + \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2(4\pi - \theta)\theta}\right)}\right],\right.$$

$$\left.\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right], \{x, -1.3, 1.3\}\right]$$

lldradius.avi

Manipulate[

$$\text{Plot3D}\left[\frac{1}{4\pi^2} \left(\sqrt{\left(-48\pi^4 r^2 - 16\pi^4 x^2 + \frac{256\pi^5 r^2}{4\pi - \theta} - 16\pi^3 r^2 \theta - 4\pi^2 r^2 \theta^2 - r^2 \theta^4 - 16\pi^3 r \sqrt{r^2(4\pi - \theta)\theta} + \frac{64\pi^4 r \sqrt{r^2(4\pi - \theta)\theta}}{4\pi - \theta} - 8\pi^2 r \theta \sqrt{r^2(4\pi - \theta)\theta}\right)}\right],\right.$$

$$\left.\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right], \{x, -1, 1\}]$$

$$\sqrt{x^2 + y^2 + z^2}$$

$$\text{Solve}\left[\sqrt{x^2 + y^2 + \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}^2 == \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\sqrt{\frac{\pi}{2}} \sqrt{\frac{2\pi\eta^2}{(4\pi - \theta)^2} - \frac{2x^2}{4\pi - \theta} - \frac{2y^2}{4\pi - \theta} + \frac{\eta^2}{4\pi - \theta} + \frac{2\pi\eta^2}{\theta^2} - \frac{2x^2}{\theta} - \frac{2y^2}{\theta} + \frac{\eta^2}{\theta}}\right\},\right.$$

$$\left.\left\{r \rightarrow \sqrt{\frac{\pi}{2}} \sqrt{\frac{2\pi\eta^2}{(4\pi - \theta)^2} - \frac{2x^2}{4\pi - \theta} - \frac{2y^2}{4\pi - \theta} + \frac{\eta^2}{4\pi - \theta} + \frac{2\pi\eta^2}{\theta^2} - \frac{2x^2}{\theta} - \frac{2y^2}{\theta} + \frac{\eta^2}{\theta}}\right\}\right\}$$

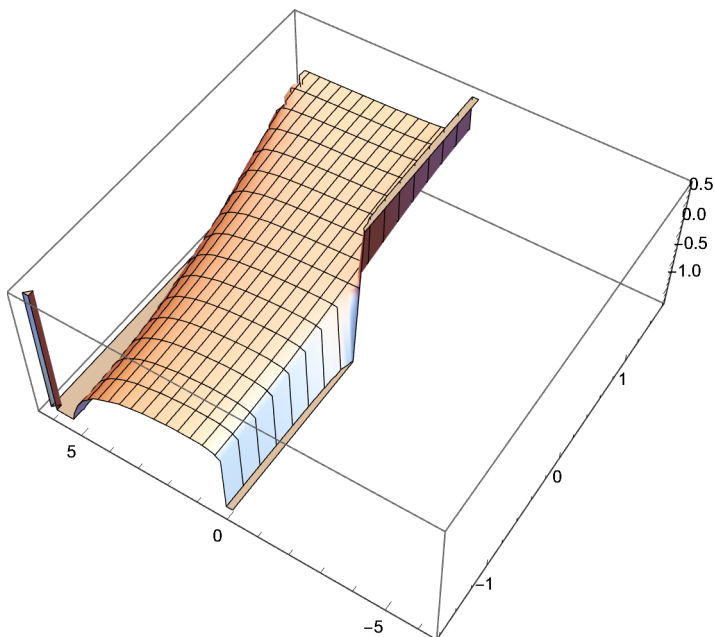
$$\sqrt{\frac{\pi}{2}} \sqrt{\frac{2\pi\eta^2}{(4\pi - \theta)^2} - \frac{2x^2}{4\pi - \theta} - \frac{2y^2}{4\pi - \theta} + \frac{\eta^2}{4\pi - \theta} + \frac{2\pi\eta^2}{\theta^2} - \frac{2x^2}{\theta} - \frac{2y^2}{\theta} + \frac{\eta^2}{\theta}}$$

$$\text{Solve}\left[\frac{2\pi\sqrt{x^2 + y^2}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}} ==\right.$$

$$\text{Plot3D}\left[\left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] +\right.\right.$$

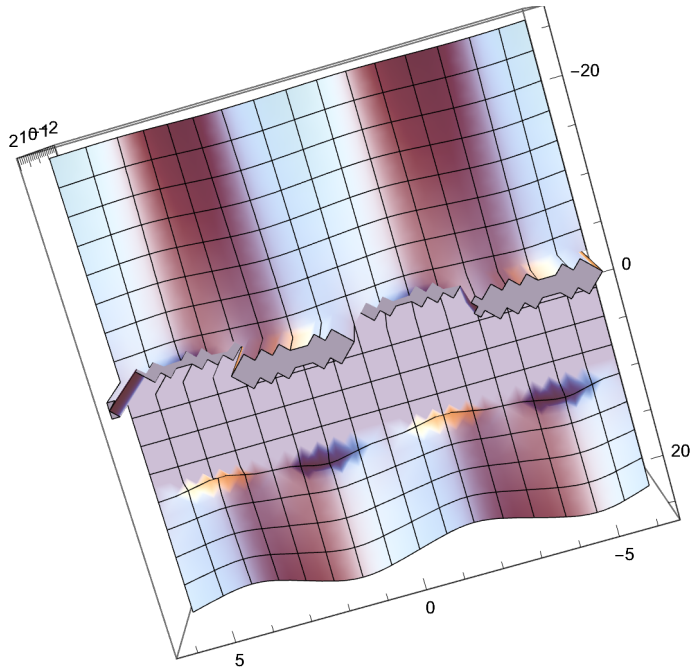
$$\left.\left.4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right)\right/$$

$$(16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2), \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$

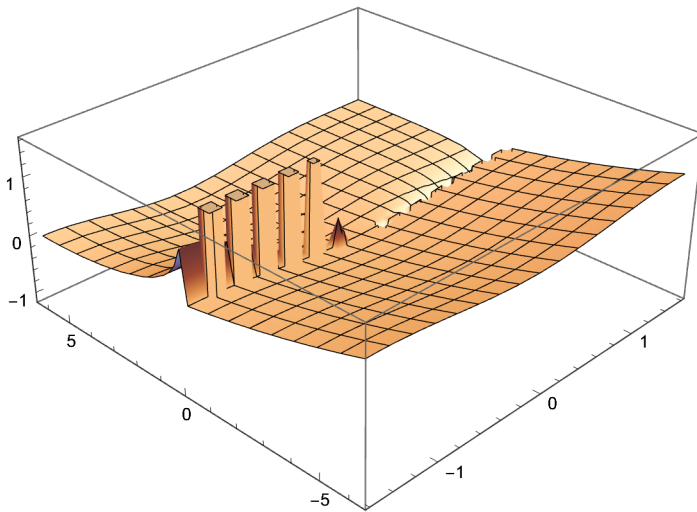




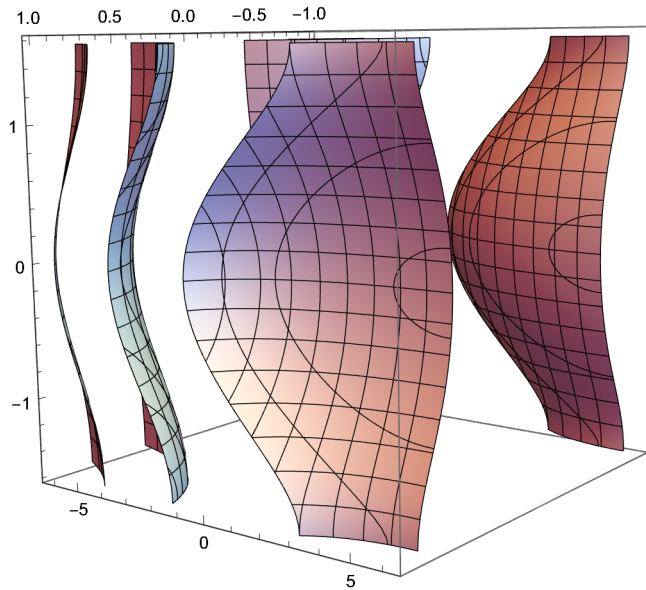
Plot3D[0.00633256 Im[-12.5664  $\theta$  +  $\theta^2$  + 6.28319 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ] +  
 39.4784 Sin[ $\beta$ ]^2 - (19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) / (12.5664 - 1.  $\theta$ ) -  
 (19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) /  $\theta$ ], { $\beta$ , -6.3, 6.3}, { $\theta$ , -26, 26}]



Plot3D[0.00633256 Re[-12.5664  $\theta$  +  $\theta^2$  + 6.28319 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ] +  
 39.4784 Sin[ $\beta$ ]^2 - (19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) / (12.5664 - 1.  $\theta$ ) -  
 (19.7392 Sqrt[(12.5664 - 1.  $\theta$ )  $\theta$ ] Sin[ $\beta$ ]^3) /  $\theta$ ], { $\beta$ , - $\pi/2$ ,  $\pi/2$ }, { $\theta$ , -2 $\pi$ , 2 $\pi$ }]



ContourPlot3D $\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}^2 + \frac{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) r - 2 \pi r}{2 \pi}^2,$   
 $\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



$$2 \pi \left( \sqrt{r^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2} \right) \left( \sqrt{1 - ((v^2) / (c^2))} \right) =$$

$$2 \pi \left( \sqrt{\left( r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right)^2 - \left( \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right)^2} \right)$$

Solve[

$$r \theta == \left( 2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right) - 2 \pi \left( \left( \sqrt{r^2 - \eta^2} \right) \right) \left( \sqrt{1 - ((v^2) / (c^2))} \right), \theta]$$

$$\left\{ \left\{ \theta \rightarrow - \frac{2 \left( -\pi r \sqrt{\frac{c^2 - v^2}{c^2}} + \pi \sqrt{\frac{c^2 - v^2}{c^2}} \sqrt{r^2 - \eta^2} \right)}{r} \right\} \right\}$$

Solve[ $(\theta r) == \left( 2 \pi r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right) -$

$$2 \pi \left( \sqrt{\left( r \left( \sqrt{1 - ((v^2) / (c^2))} \right) \right)^2 - \left( \left( \sqrt{1 - ((v^2) / (c^2))} \right) \eta \right)^2} \right), \eta]$$

$$\left\{ \left\{ \eta \rightarrow - \frac{\sqrt{-4 c^2 \pi r^2} \sqrt{\frac{c^2 - v^2}{c^2}} \theta + c^2 r^2 \theta^2}{2 \pi \sqrt{-c^2 + v^2}} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{-4 c^2 \pi r^2} \sqrt{\frac{c^2 - v^2}{c^2}} \theta + c^2 r^2 \theta^2}{2 \pi \sqrt{-c^2 + v^2}} \right\} \right\}$$

$$\text{Solve}\left[\frac{\sqrt{-4 c^2 \pi r^2 \sqrt{\frac{c^2-v^2}{c^2}} \theta + c^2 r^2 \theta^2}}{2 \pi \sqrt{-c^2+v^2}} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, c\right]$$

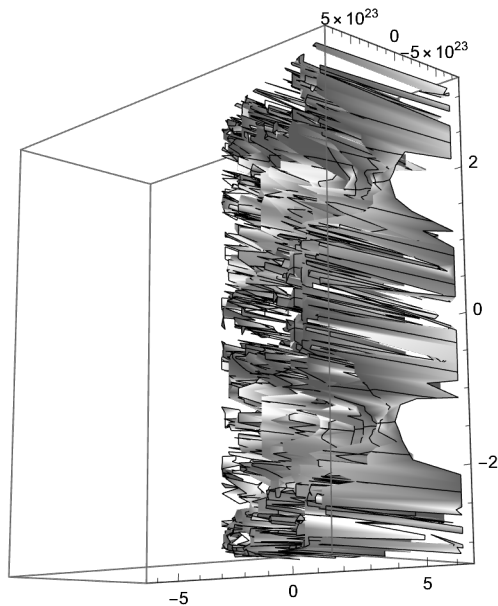
$$\left\{\left\{c \rightarrow -\frac{\sqrt{-16 \pi^2 v^2 + 8 \pi v^2 \theta - v^2 \theta^2}}{2 \sqrt{2 \pi} \sqrt{-2 \pi + \theta}}\right\}, \left\{c \rightarrow \frac{\sqrt{-16 \pi^2 v^2 + 8 \pi v^2 \theta - v^2 \theta^2}}{2 \sqrt{2 \pi} \sqrt{-2 \pi + \theta}}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{-4 c^2 \pi r^2 \sqrt{\frac{c^2-v^2}{c^2}} \theta + c^2 r^2 \theta^2}}{2 \pi \sqrt{-c^2+v^2}} == \right.$$

$$\left.\frac{\sqrt{\frac{4 c \pi r^2 \sqrt{\frac{(c-v)(c+v)}{c^2}} \theta}{c-v} + \frac{4 c \pi r^2 \sqrt{\frac{(c-v)(c+v)}{c^2}} \theta}{c+v} - \frac{c r^2 \theta^2}{c-v} - \frac{c r^2 \theta^2}{c+v}}}{2 \sqrt{2} \pi}, v\right]$$

{{}}

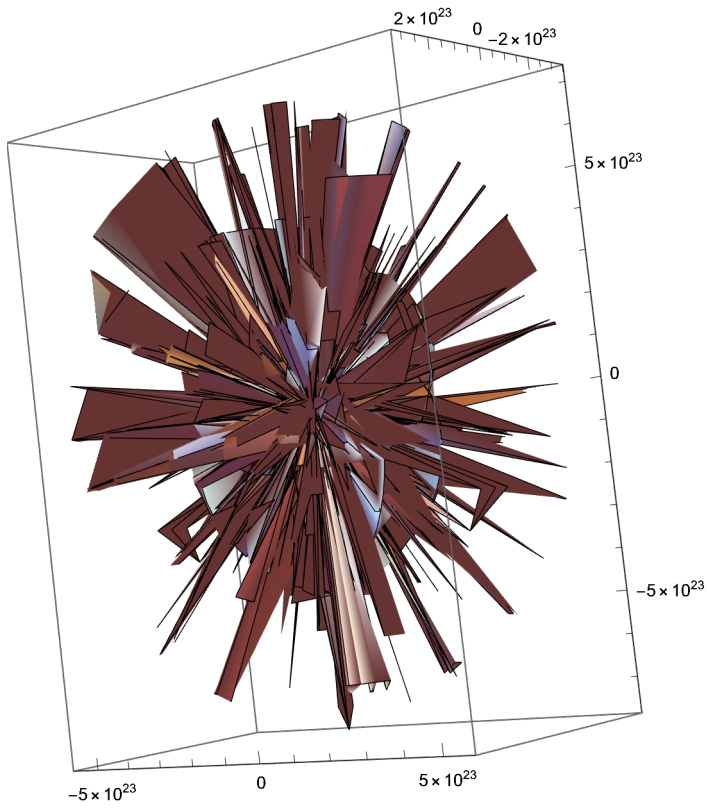
$$\begin{aligned}
& \text{Plot3D}\left[\left\{\left(\frac{i \left(2.99792458 \times 10^8\right)^3 \sqrt{\theta}}{\left(\left(2.99792458 \times 10^8\right) - \left(\sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2}\right)\right) \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2}}\right)\right. \right. \\
& \left. \left(\frac{\left(2.99792458 \times 10^8\right) + \left(\sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2}\right)}{\left(\sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2}\right) \sqrt{-4 \pi + \theta}}\right), \right. \\
& \left. -\left(\frac{i \left(2.99792458 \times 10^8\right)^3 \sqrt{\theta}}{\left(\left(2.99792458 \times 10^8\right) - \left(\sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2}\right)\right) \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2}}\right)\right. \\
& \left. \left(\frac{\left(2.99792458 \times 10^8\right) + \left(\sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2}\right)}{\left(\sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2}\right) \sqrt{-4 \pi + \theta}}\right)\right\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]
\end{aligned}$$



```

SphericalPlot3D[
  {
    (I (2.99792458 * 10^8)^3 Sqrt[theta]) / (
      ((2.99792458 * 10^8) - (Sqrt[-1.1294090667581471`*^18
        theta + 8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2])) /
      (Sqrt[-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2])
    ),
    (
      ((2.99792458 * 10^8) + (Sqrt[-1.1294090667581471`*^18 theta +
        8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2])) /
      (Sqrt[-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2])
    ) Sqrt[-4 pi + theta],
    - (I (2.99792458 * 10^8)^3 Sqrt[theta]) / (
      ((2.99792458 * 10^8) - (Sqrt[-1.1294090667581471`*^18
        theta + 8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2])) /
      (Sqrt[-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2])
    ),
    (
      ((2.99792458 * 10^8) + (Sqrt[-1.1294090667581471`*^18 theta +
        8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2])) /
      (Sqrt[-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2])
    ) Sqrt[-4 pi + theta]
  }, {theta, -2 pi, 2 pi}, {beta, -pi, pi}]

```



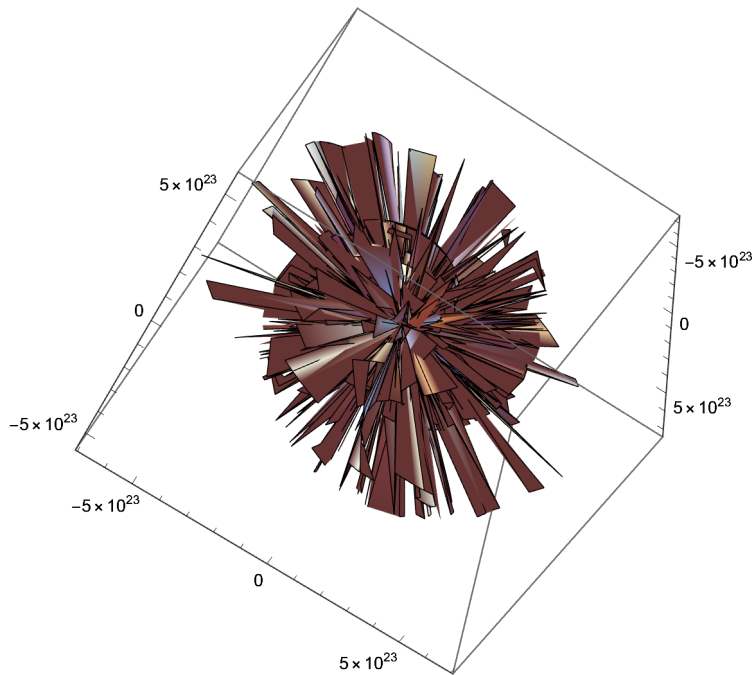
SphericalPlot3D[  

$$\left\{ \left( i (2.99792458 \times 10^8)^3 \sqrt{\theta} \right) / \left( \left( (2.99792458 \times 10^8) - \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2)} \right) \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \right) \right.$$
  

$$\left. \left( (2.99792458 \times 10^8) + \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2)} \right) \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \sqrt{-4\pi + \theta} \right\},$$
  

$$\left\{ - \left( i (2.99792458 \times 10^8)^3 \sqrt{\theta} \right) / \left( \left( (2.99792458 \times 10^8) - \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2)} \right) \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \right) \right.$$
  

$$\left. \left( (2.99792458 \times 10^8) + \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2)} \right) \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \sqrt{-4\pi + \theta} \right\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



Instantaneous) is equal to the phenomenal velocity at the position where the height of the cone has folded all the way up!

$$\text{Solve}\left[\sqrt{\left(3.5481432270250993 \cdot r^{18} \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 1.1294090667581471 \cdot r^{18} r^2 \theta + 8.987551787368176 \cdot r^{16} r^2 \theta^2\right)}\right. \\ \left.\left(\sqrt{\left(39.47841760435743 \cdot \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)}\right) == \right. \\ \left. \frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta} - \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}}, r\right] \\ \{\{r \rightarrow -0.159155 \sqrt{12.5664 - 1. \theta} \sqrt{\theta}\}, \{r \rightarrow 0.159155 \sqrt{12.5664 - 1. \theta} \sqrt{\theta}\}\} \\ \text{Solve}\left[0.15915494309189535 \cdot \sqrt{12.566370614359172 - 1. \theta} \sqrt{\theta} == \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta}, \theta\right] \\ \{\{\theta \rightarrow 6.28319 - 2.52755 \times 10^{-8} i\}, \{\theta \rightarrow 6.28319 + 2.52755 \times 10^{-8} i\}\} \\ \text{Solve}\left[-0.15915494309189535 \cdot \sqrt{12.566370614359172 - 1. \theta} \sqrt{\theta} == \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta}, \theta\right] \\ \{\{\theta \rightarrow -2.60258\}, \{\theta \rightarrow 15.169\}\}$$

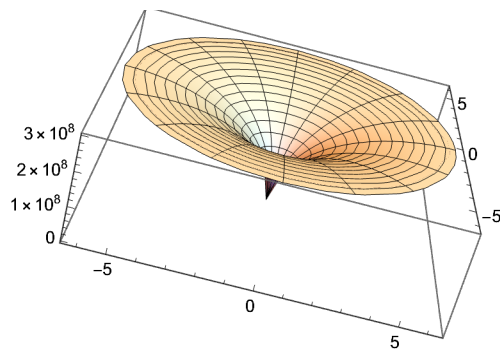


$$\text{Solve}\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} (\eta)^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{\left(39.47841760435743 (\eta)^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2\right)}\right) == \frac{2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}}{\theta} - \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -3.50592 \times 10^{-11} \sqrt{2.32749 \times 10^{37} - 1.85216 \times 10^{36} \theta} \sqrt{\theta}\right\}, \left\{r \rightarrow 3.50592 \times 10^{-11} \sqrt{2.32749 \times 10^{37} - 1.85216 \times 10^{36} \theta} \sqrt{\theta}\right\}\right\}$$

$$3.5059170406658596 \cdot 10^{-11} \sqrt{2.3274923516835676 \cdot 10^{37} - 1.8521595638950995 \cdot 10^{36} \theta} \sqrt{\theta}$$

$$\text{RevolutionPlot3D}\left[3.5059170406658596 \cdot 10^{-11} \sqrt{2.3274923516835676 \cdot 10^{37} - 1.8521595638950995 \cdot 10^{36} \theta} \sqrt{\theta}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$0.15915494309189535 \cdot \sqrt{12.566370614359172 - 1. \cdot \theta} \sqrt{\theta}$$

$$3.5059170406658596 \cdot 10^{-11} \text{Solve} \sqrt{2.3274923516835676 \cdot 10^{37} - 1.8521595638950995 \cdot 10^{36} \theta} \sqrt{\theta} == 0.15915494309189535 \cdot \sqrt{12.566370614359172 - 1. \cdot \theta} \sqrt{\theta}$$

$$\text{Solve}\left[\sqrt{2.3274923516835676 \cdot 10^{37} - 1.8521595638950995 \cdot 10^{36} \theta} \sqrt{\theta} == 0.15915494309189535 \cdot \sqrt{12.566370614359172 - 1. \cdot \theta} \sqrt{\theta}, \theta\right]$$

$$\{\{\theta \rightarrow 0.\}, \{\theta \rightarrow 12.5664\}\}$$

$$\text{Solve}\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} (\eta)^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{\left(39.47841760435743 (\eta)^2 - 12.566370614359172 r^2 \theta + r^2 \theta^2\right)}\right) == \frac{2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}}{\theta} - \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta\right]$$

$$\{\}$$

$$\text{Solve}\left[\left(\sqrt{\left(3.5481432270250993 \cdot r^{18} \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 1.1294090667581471 \cdot r^{18} \theta + 8.987551787368176 \cdot r^{16} \theta^2\right)}\right) / \right.$$

$$\left.\left(\sqrt{\left(39.47841760435743 \cdot \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)}\right) == \right.$$

$$\left.\frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta} - \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}}, \theta\right]$$

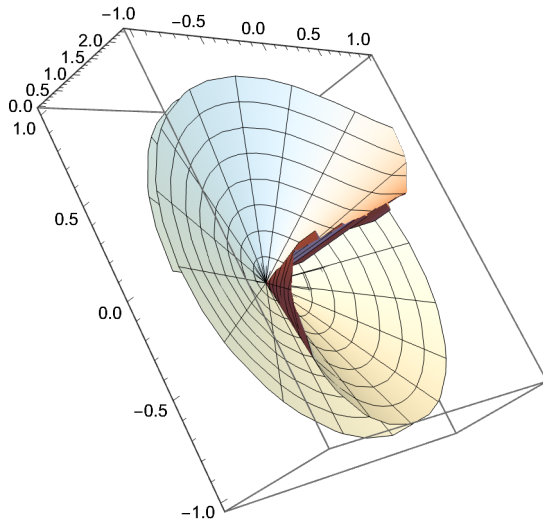
$$\{\{\theta \rightarrow 0.5 (12.5664 - 12.5664 \sqrt{1 - 1. r} \sqrt{1 + r})\},$$

$$\{\theta \rightarrow 0.5 (12.5664 + 12.5664 \sqrt{1 - 1. r} \sqrt{1 + r})\}\}$$

$$\text{Solve}\left[0.5 \cdot (12.566370614359172 + 12.566370614359172 \cdot \sqrt{1 - 1. r} \sqrt{1 + r}) = 2\pi, r\right]$$

$$\{\{r \rightarrow -1.\}, \{r \rightarrow 1.\}\}$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta} - \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$\text{Solve}\left[\left[\sqrt{\left(3.5481432270250993 \cdot r^{18} \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 1.1294090667581471 \cdot r^{18} \theta + 8.987551787368176 \cdot r^{16} \theta^2\right)}\right] / \left(\sqrt{\left(39.47841760435743 \cdot \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)}\right) == \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} - \frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta}, \theta\right]$$

$$\{\{\theta \rightarrow 0.5 (12.5664 - 12.5664 \sqrt{1 - 1. r} \sqrt{1 + r})\}, \{\theta \rightarrow 0.5 (12.5664 + 12.5664 \sqrt{1 - 1. r} \sqrt{1 + r})\}\}$$

$$\text{Solve}\left[\left[\sqrt{\left(3.5481432270250993 \cdot r^{18} \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 1.1294090667581471 \cdot r^{18} \theta + 8.987551787368176 \cdot r^{16} \theta^2\right)}\right] / \left(\sqrt{\left(39.47841760435743 \cdot \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)}\right) == \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} - \frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta}, r\right]$$

$$\{\{r \rightarrow -0.159155 \sqrt{12.5664 - 1. \theta} \sqrt{\theta}\}, \{r \rightarrow 0.159155 \sqrt{12.5664 - 1. \theta} \sqrt{\theta}\}\}$$

$$\text{Solve}\left[\frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta} - \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} == \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} - \frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta}, r\right]$$

$$\{\}$$

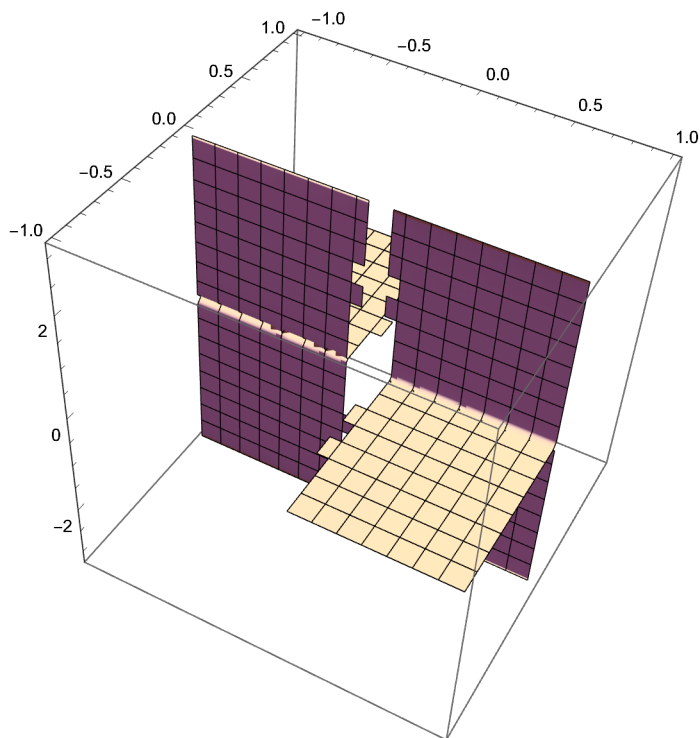
$$\text{Solve}\left[\frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta} - \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} == \frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}} - \frac{2\pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}}{\theta}, \theta\right]$$

$$\{\}$$

"Thus the height of an object is specified by the monocular optical stimulus within a scale factor. This means that the ratios of heights of two or more objects are specified."

$$H = \frac{A}{a} \sin[\alpha]^2 = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

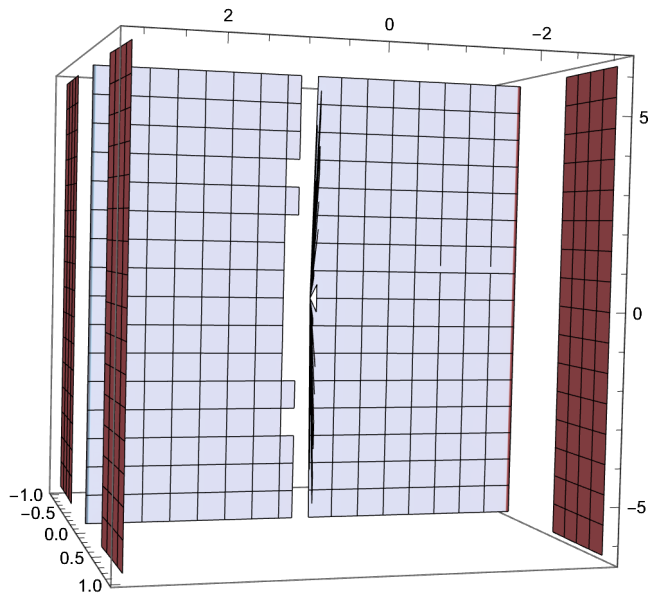
$$\text{ContourPlot3D}\left[\frac{A}{a} \sin[\alpha]^2, \{a, -1, 1\}, \{A, -1, 1\}, \{\alpha, -\pi, \pi\}\right]$$



$$\text{Solve}\left[\frac{A}{a} \sin[\alpha]^2 == \frac{\sqrt{4\pi \left(\frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 \theta - \left(\frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 \theta^2}}{2\pi}, A\right]$$

$$\left\{\left\{A \rightarrow \frac{a \sqrt{\frac{16\pi^3}{4\pi-\theta} - \frac{4\pi^2\theta}{4\pi-\theta}} \csc[\alpha]^2}{2\pi}\right\}\right\}$$

$$\text{ContourPlot3D}\left[\frac{a \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}} \text{Csc}[\alpha]^2}{2 \pi}, \{a, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\alpha, -\pi, \pi\}\right]$$

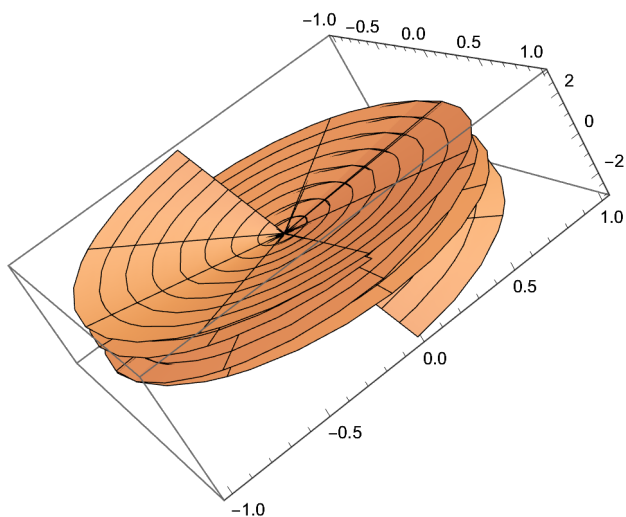


$$\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]$$

$$\text{Solve}\left[\frac{A}{a} \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]\right]^2 == \frac{\sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}{2 \pi}, a]$$

$$\left\{\left\{a \rightarrow \frac{4 A \pi \theta - A \theta^2}{4 \pi^2}\right\}\right\}$$

$\text{RevolutionPlot3D}\left[\frac{4 A \pi \theta - A \theta^2}{4 \pi^2}, \{A, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

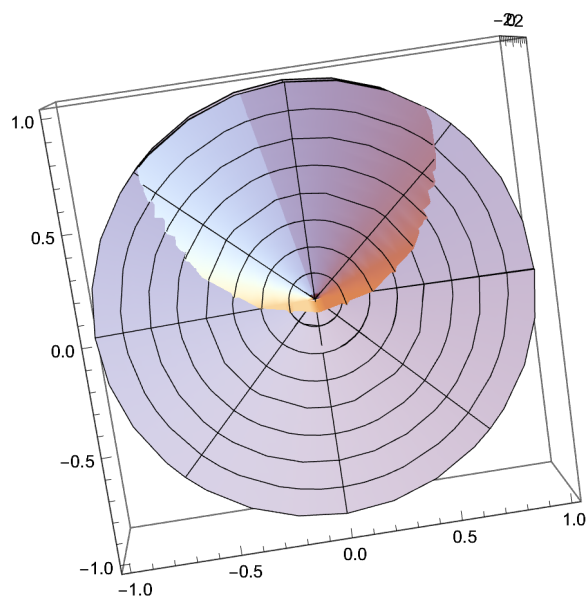


$$\frac{4 A \pi \theta - A \theta^2}{4 \pi^2}$$

$$\text{Solve}\left[\frac{A}{a} \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2 == \frac{\sqrt{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}{2 \pi}, A\right]$$

$$\left\{\left\{A \rightarrow \frac{2 a \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}{(4 \pi - \theta) \theta}\right\}\right\}$$

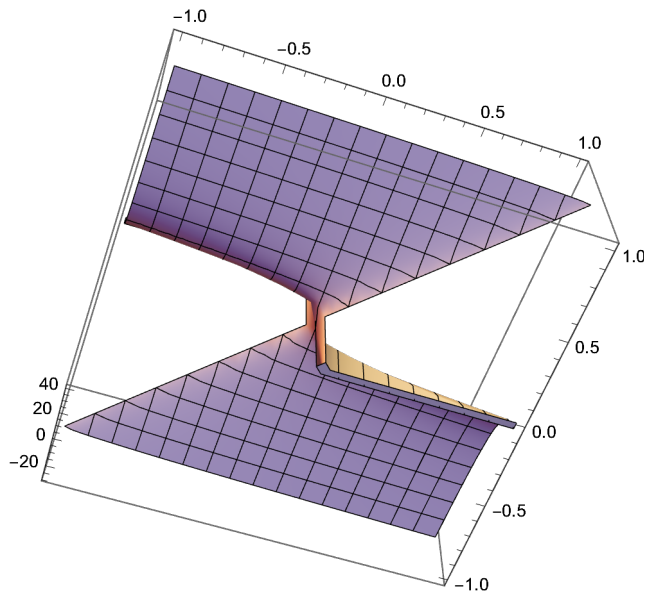
$\text{RevolutionPlot3D}\left[\frac{2 a \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}{(4 \pi - \theta) \theta}, \{a, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\text{Solve}\left[\frac{A}{a} \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2 == \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\left(A - \sqrt{-aA + A^2}\right)\pi}{A}\right\}, \left\{\theta \rightarrow \frac{2\left(A + \sqrt{-aA + A^2}\right)\pi}{A}\right\}\right\}$$

$$\text{Plot3D}\left[\frac{2\left(A + \sqrt{-aA + A^2}\right)\pi}{A}, \{A, -1, 1\}, \{a, -1, 1\}\right]$$



$$\text{Solve}\left[\frac{A}{a} \sin[\alpha]^2 == \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}, a\right]$$

$$\left\{\{a \rightarrow A \sin[\alpha]^2\}\right\}$$

$$A \sin[\alpha]^2$$

$$\text{Solve}\left[\frac{A}{H} \sin[\alpha]^2 == A \sin[\alpha]^2, H\right]$$

$$\left\{\{H \rightarrow 1\}\right\}$$

$$w = \frac{A^2}{H^2} ((\sin[\alpha])^3) ==$$

$$\left(\frac{A}{H} \sin[\alpha]\right) \frac{A}{H} \sin[\alpha]^2 ==$$

Relativistic  $\eta :=$

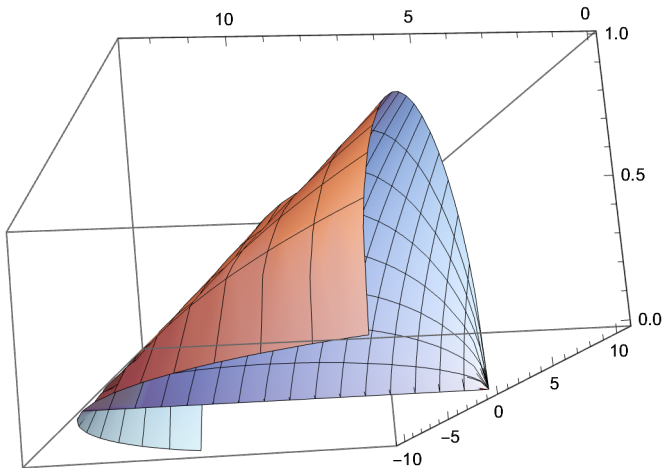
$$\left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) / \left( \sqrt{1 - \left( \left( \left( \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right)} \right)$$

$$\left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) / \left( \sqrt{1 - \left( \left( \left( \frac{2 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right)} \right)$$

RevolutionPlot3D[

$$\left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) / \left( \sqrt{1 - \left( \left( \left( \frac{2 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right)} \right),$$

{ $\theta$ ,  $-4 \pi$ ,  $4 \pi$ }, { $r$ ,  $-1$ ,  $1$ }]



$$D\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r, \theta\right]$$

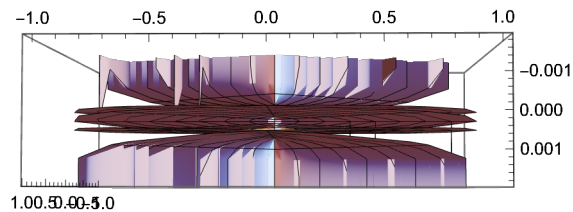
$$\frac{(4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi r \theta - 2 r \theta^2)}{5760 (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{(8 \pi r - 4 r \theta) (4 \pi r^2 - 2 r^2 \theta)}{4320 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} +$$

$$\frac{r^2 (8 \pi r \theta - 2 r \theta^2)}{4320 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r}{1080 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$



RevolutionPlot3D[  

$$-\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8640(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4320\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$

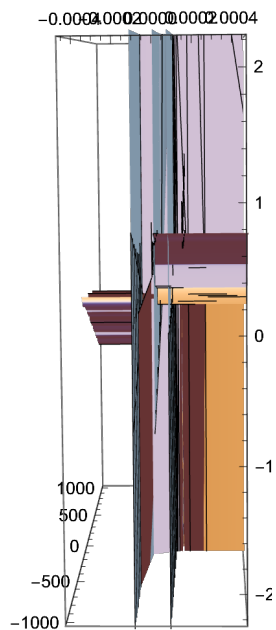


$$\begin{aligned}
 &\frac{(4\pi r^2 - 2r^2\theta)^2(8\pi r\theta - 2r\theta^2)}{5760(4\pi r^2\theta - r^2\theta^2)^{5/2}} - \frac{(8\pi r - 4r\theta)(4\pi r^2 - 2r^2\theta)}{4320(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \\
 &\frac{r^2(8\pi r\theta - 2r\theta^2)}{4320(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{r}{1080\sqrt{4\pi r^2\theta - r^2\theta^2}}
 \end{aligned}$$

RevolutionPlot3D[  

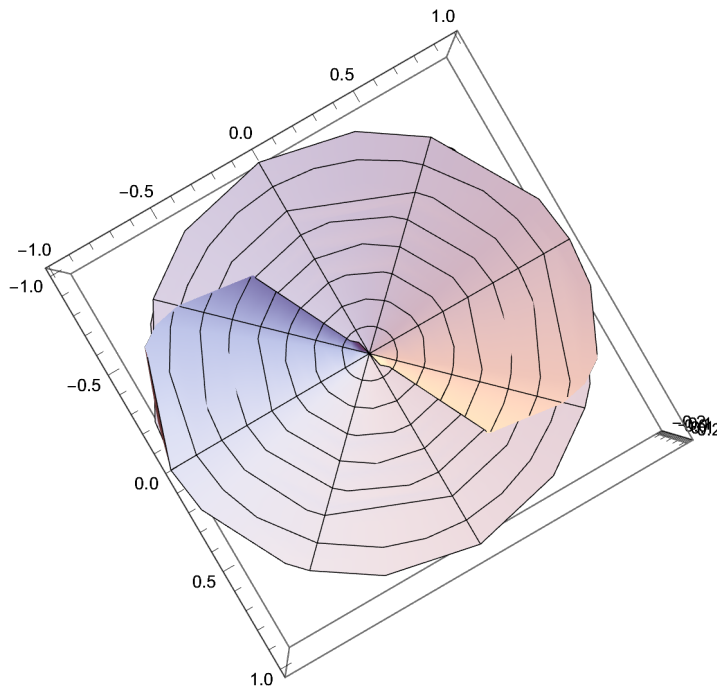
$$\frac{(4\pi r^2 - 2r^2\theta)^2(8\pi r\theta - 2r\theta^2)}{5760(4\pi r^2\theta - r^2\theta^2)^{5/2}} - \frac{(8\pi r - 4r\theta)(4\pi r^2 - 2r^2\theta)}{4320(4\pi r^2\theta - r^2\theta^2)^{3/2}} +$$

$$\frac{r^2(8\pi r\theta - 2r\theta^2)}{4320(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{r}{1080\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1000, 1000\}, \{\theta, -14\pi, 14\pi\}]$$

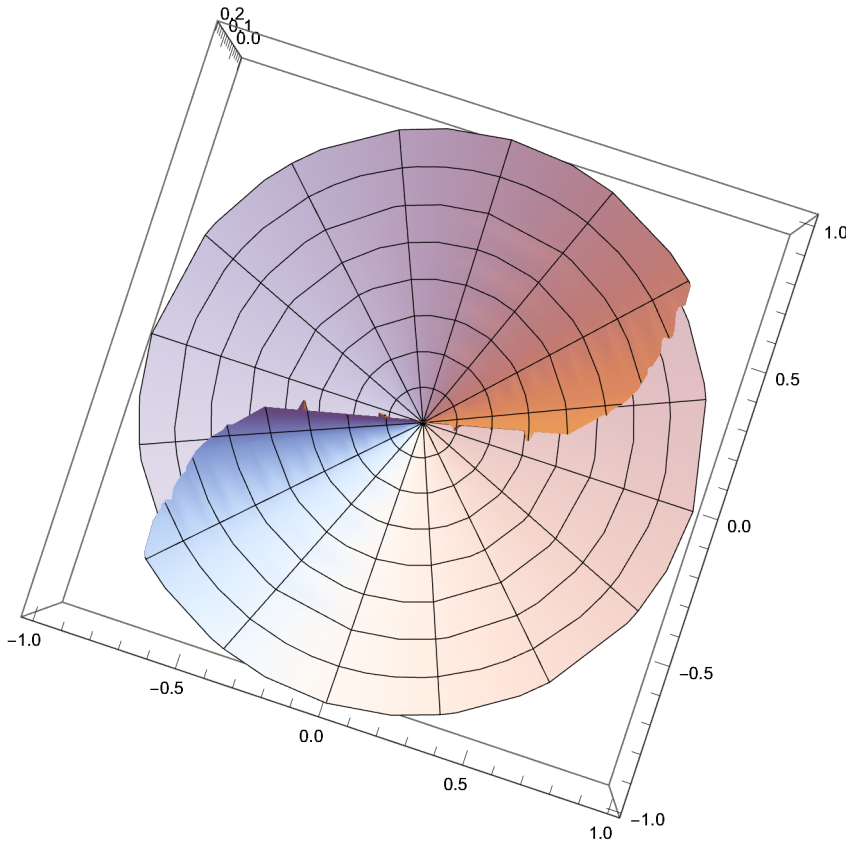


$$\begin{aligned}
& D \left[ \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) \left( \sqrt{1 - \left( \left( \left( \left( \frac{2 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right) \right) \right), \theta \right] \\
& \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( - \frac{9.41479 \times 10^{-23} (4 \pi r^2 - 2 r^2 \theta)}{\theta^2 (4 \pi \theta - \theta^2)} + \right. \right. \\
& \quad \left. \left. \frac{9.41479 \times 10^{-23} (4 \pi - 2 \theta) (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^2 (4 \pi \theta - \theta^2)^2} + \frac{1.88296 \times 10^{-22} (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^3 (4 \pi \theta - \theta^2)} \right) \right) / \\
& \left( 4 \pi \sqrt{1 - \frac{9.41479 \times 10^{-23} (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^2 (4 \pi \theta - \theta^2)}} \right) + \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{9.41479 \times 10^{-23} (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^2 (4 \pi \theta - \theta^2)}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}
\end{aligned}$$

$$\text{RevolutionPlot3D}\left[-\left(\sqrt{4\pi r^2\theta - r^2\theta^2}\left(-\frac{9.414794144460832\cdot 10^{-23}(4\pi r^2 - 2r^2\theta)}{\theta^2(4\pi\theta - \theta^2)} + \frac{9.414794144460832\cdot 10^{-23}(4\pi - 2\theta)(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)^2} + \frac{1.8829588288921663\cdot 10^{-22}(4\pi r^2\theta - r^2\theta^2)}{\theta^3(4\pi\theta - \theta^2)}\right)\right)/\left(4\pi\left(1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}\right)^{3/2}\right) + \frac{4\pi r^2 - 2r^2\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}\sqrt{1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}}}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$



$$\text{RevolutionPlot3D}\left[\left(\sqrt{4\pi r^2\theta - r^2\theta^2}\left(-\frac{9.414794144460832\cdot 10^{-23}(4\pi r^2 - 2r^2\theta)}{\theta^2(4\pi\theta - \theta^2)} + \frac{9.414794144460832\cdot 10^{-23}(4\pi - 2\theta)(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)^2} + \frac{1.8829588288921663\cdot 10^{-22}(4\pi r^2\theta - r^2\theta^2)}{\theta^3(4\pi\theta - \theta^2)}\right)\right)/\right. \\ \left.\left(4\pi\sqrt{1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}}\right) + \frac{(4\pi r^2 - 2r^2\theta)\sqrt{1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}}}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



Relativistic $\eta :=$

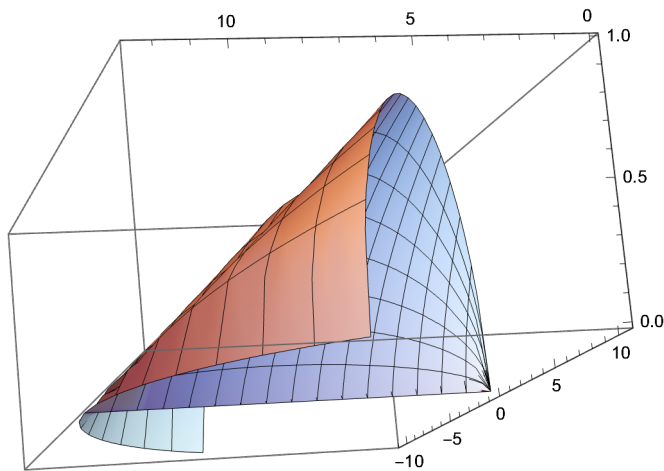
$$\left(\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}\right)/\left(\sqrt{1 - \left(\left(\left(\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right)/((1080/\pi)\theta)\right)^2/(c^2)\right)}\right)$$

$$\left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) / \left( \sqrt{1 - \left( \left( \left( \left( \frac{2 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right)} \right) \right)$$

RevolutionPlot3D[

$$\left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) / \left( \sqrt{1 - \left( \left( \left( \left( \frac{2 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right)} \right) \right),$$

{\theta, -4 \pi, 4 \pi}, {r, -1, 1}]



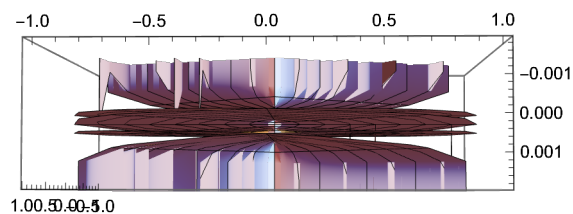
$$D\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r, \theta\right]$$

$$\frac{(4 \pi r^2 - 2 r^2 \theta)^2 (8 \pi r \theta - 2 r \theta^2)}{5760 (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{(8 \pi r - 4 r \theta) (4 \pi r^2 - 2 r^2 \theta)}{4320 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} +$$

$$\frac{r^2 (8 \pi r \theta - 2 r \theta^2)}{4320 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r}{1080 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

RevolutionPlot3D[

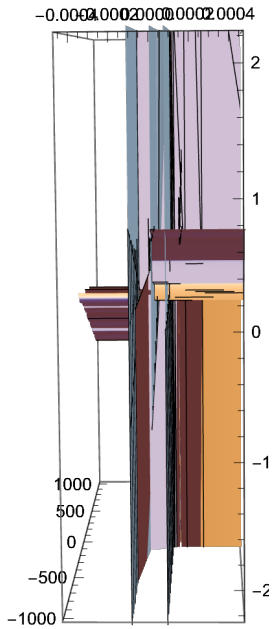
$$-\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8640 (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



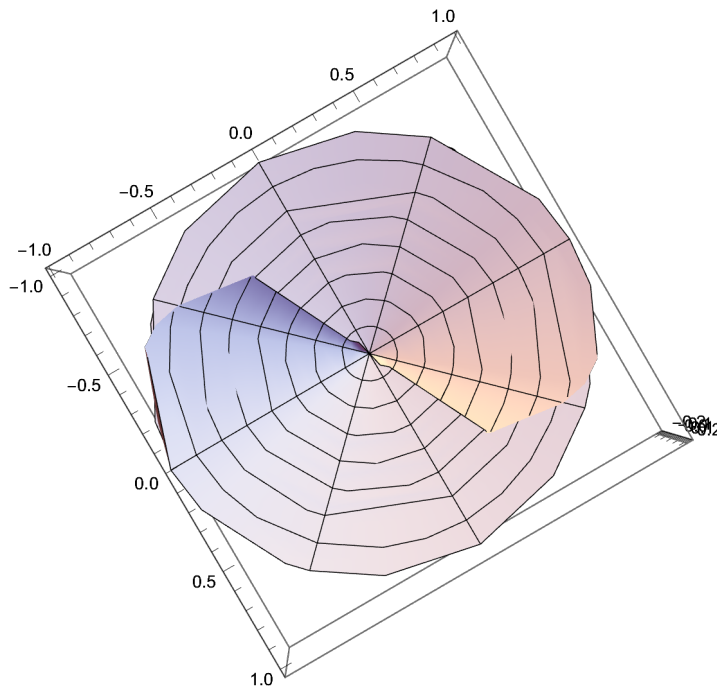
$$\frac{(4\pi r^2 - 2r^2\theta)^2 (8\pi r\theta - 2r\theta^2)}{5760 (4\pi r^2\theta - r^2\theta^2)^{5/2}} - \frac{(8\pi r - 4r\theta) (4\pi r^2 - 2r^2\theta)}{4320 (4\pi r^2\theta - r^2\theta^2)^{3/2}} +$$

$$\frac{r^2 (8\pi r\theta - 2r\theta^2)}{4320 (4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{r}{1080 \sqrt{4\pi r^2\theta - r^2\theta^2}}$$

$$\text{RevolutionPlot3D}\left[\frac{(4\pi r^2 - 2r^2\theta)^2 (8\pi r\theta - 2r\theta^2)}{5760 (4\pi r^2\theta - r^2\theta^2)^{5/2}} - \frac{(8\pi r - 4r\theta) (4\pi r^2 - 2r^2\theta)}{4320 (4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{r^2 (8\pi r\theta - 2r\theta^2)}{4320 (4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{r}{1080 \sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1000, 1000\}, \{\theta, -14\pi, 14\pi\}\right]$$

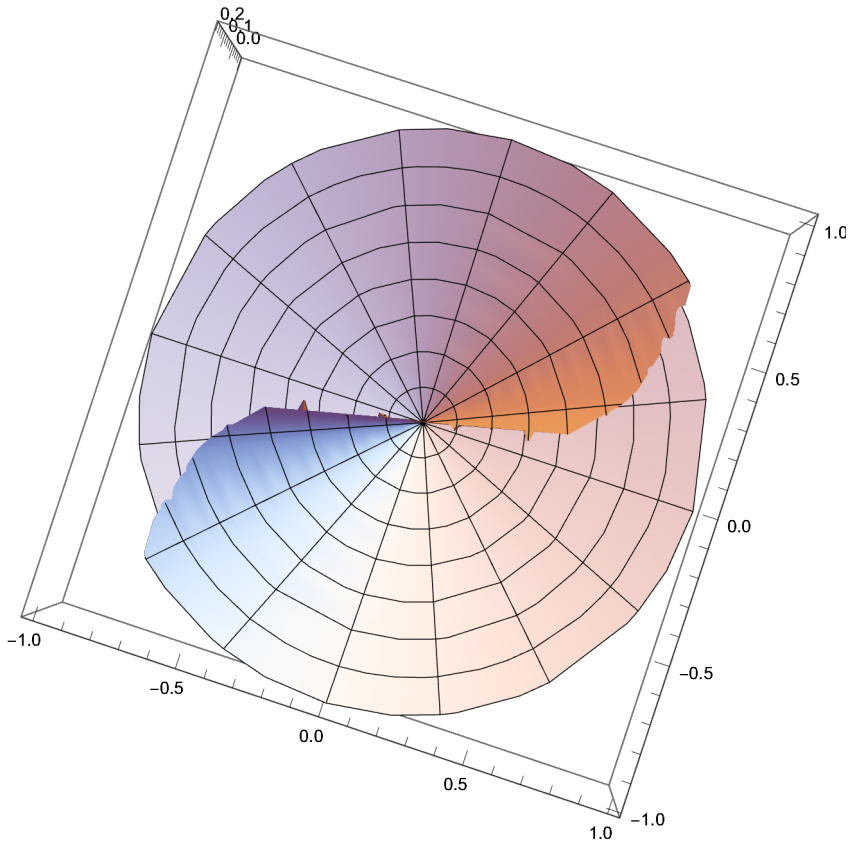


$$\begin{aligned}
& D \left[ \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right) \left( \sqrt{1 - \left( \left( \left( \left( \frac{2 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)}{\sqrt{4 \pi \theta - \theta^2}} \right) / ((1080 / \pi) \theta) \right)^2 / (c^2) \right) \right) \right), \theta \right] \\
& \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( - \frac{9.41479 \times 10^{-23} (4 \pi r^2 - 2 r^2 \theta)}{\theta^2 (4 \pi \theta - \theta^2)} + \right. \right. \\
& \quad \left. \left. \frac{9.41479 \times 10^{-23} (4 \pi - 2 \theta) (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^2 (4 \pi \theta - \theta^2)^2} + \frac{1.88296 \times 10^{-22} (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^3 (4 \pi \theta - \theta^2)} \right) \right) / \\
& \left( 4 \pi \sqrt{1 - \frac{9.41479 \times 10^{-23} (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^2 (4 \pi \theta - \theta^2)}} \right) + \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{9.41479 \times 10^{-23} (4 \pi r^2 \theta - r^2 \theta^2)}{\theta^2 (4 \pi \theta - \theta^2)}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}
\end{aligned}$$

$$\text{RevolutionPlot3D}\left[-\left(\sqrt{4\pi r^2\theta - r^2\theta^2}\left(-\frac{9.414794144460832\cdot 10^{-23}(4\pi r^2 - 2r^2\theta)}{\theta^2(4\pi\theta - \theta^2)} + \frac{9.414794144460832\cdot 10^{-23}(4\pi - 2\theta)(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)^2} + \frac{1.8829588288921663\cdot 10^{-22}(4\pi r^2\theta - r^2\theta^2)}{\theta^3(4\pi\theta - \theta^2)}\right)\right)/\right. \\ \left.\left(4\pi\left(1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}\right)^{3/2}\right) + \frac{4\pi r^2 - 2r^2\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\sqrt{1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}}\right), \\ \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$




$$\text{RevolutionPlot3D}\left[\left(\sqrt{4\pi r^2\theta - r^2\theta^2}\left(-\frac{9.414794144460832\cdot 10^{-23}(4\pi r^2 - 2r^2\theta)}{\theta^2(4\pi\theta - \theta^2)} + \frac{9.414794144460832\cdot 10^{-23}(4\pi - 2\theta)(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)^2} + \frac{1.8829588288921663\cdot 10^{-22}(4\pi r^2\theta - r^2\theta^2)}{\theta^3(4\pi\theta - \theta^2)}\right)\right)/\right. \\ \left.\left(4\pi\sqrt{1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}}\right) + \frac{(4\pi r^2 - 2r^2\theta)\sqrt{1 - \frac{9.414794144460832\cdot 10^{-23}(4\pi r^2\theta - r^2\theta^2)}{\theta^2(4\pi\theta - \theta^2)}}}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



# Information and Layout

## A Series of Useful Functions for the Student of Perception

by Parker Emmerson including influence from conversations with Tom Toleno, Andrew Berisha, and Alsten Daniels

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This paper will refer to the book, *The Blackwell Reading in Philosophy Publication Entitled Perception* edited by Robert Schwartz. It is referred to throughout the paper as (BRP, Page Number). The book is an anthology of multiple thinkers in the field of perceptual philosophy.

This paper will refer to the book, *Phenomenology of Perception* by Merleau-Ponty. It is referred to throughout the paper as (PoP, Page Number)

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### I. Intro

In this series of chapters, we will discuss how the visual system perceives the world through samples of the ambient optic array. On some levels, we can say that arithmetic and the body of science called mathematics does not depend at all on any psychological process. Husserl was the first to specifically begin exploring the framework for transcendental phenomenology by discussing this truth. However, on a more in depth level, applied mathematics depends greatly on the observer. How is anyone to come to any meaningful series of relations without using some cognitive process of observation or at least realizing that their expression of truth depends on observation? When we say  $1+1=2$ , this is not a truth that depends on cognition. It has meaning that already exists in the world. However, when we observe a truth about the universe that is slightly more complex and depends on the phenomenon of validity of our perceptions in space, we observe how different elements of a system fit together by necessity. There is no longer one direct path to showing meaning already exists in the world, but a series of valid expressions that we can relate to one another in order to visualize the meaning of the structuring of light, substance, time or space and gain knowledge about expressions, which are useful tools for the computational approach to visual perception.

Gibson said in *Perception of the Visual World*, that "Space perception (from which time is inseparable) is not, therefore, a division of the subject matter of perception but the first problem to consider, without a solution for which other problems remain unclear" (vii). He goes on to say that "What we lack, however, is an application of the psychophysical methods to perception" (viii). Psychophysical methods of perception are related to the environment in which perception evolved to its current level of accuracy, quarkiness, and illusionary aspects. Our perception of time is related to the environmental description of time, which is cyclic and continues out in every direction. We have evolved with a cyclic

perception of time through the seasons, day, night, and cycles of the moon. Light effects the seasons, because it allows plants to grow, it gives warmth to the air, and it influences our sleep schedules.

It is a purely theoretical notion that the eye is ever in a fixed position. Eye movements are involuntary, but can be controlled. However, making one's eye very still is difficult. We still see depth with one eye, and this is because the eye makes motions to receive the impression of depth to perception from the environment, because it associates spatiotemporal continuity to observations of the mind in addition to detecting the gradient of light and the shading involved relating to the hue of objects (the array of color). The stimulus of light is an external stimulus. It is one whose nature is not yet known. The physicist may think of it in terms of wave-particle duality. Yet, with the following mathematical account, I would like to strongly encourage thinkers in the field of theoretical physics to consider other interpretations of light. Interpretations that do not pin it down to saying, "it is a wave, it is a particle, it is both of these, and at the same time a duality," are important for developing progressive scientific theories. We may not know exactly why light is what it is, but we can know how it travels in form and visualization of the shape of its pattern.

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## II. Postulates and Structure for Notating a Sample of the Ambient Optic Array

$$C = 2 \pi r \quad (133)$$

This is the circumference of our initial circle with radius  $r$ .

$$C_2 = 2 \pi r_1 \quad (134)$$

This is the circumference of our second circle,  
the base of the cone with radius  $r_1$ .

$$r^2 = r_1^2 + \eta^2 \quad (135)$$

This is the initial radius squared expressed during transition to be the  
slant of the cone in terms of the height of the cone,  $\eta$ , and the radius  
of the base of the cone,  $r_1$ .

$$r = \pm \sqrt{(r_1^2 + \eta^2)} \quad (136)$$

The initial radius can be calculated through the Pythagorean Theorem. The  
initial radius is always the slant of the cone when there is a cone.

$$s = \theta r \quad (137)$$

In this expression,  
we define an arc length to be equal to a radius of an angle measure,  
 $\theta$ , and that thus,  
 $s / \theta = r$

$$\begin{aligned} \text{The arc length is expressed to be the difference of circumferences} = \\ \text{Initial Circumference} - \text{Circumference of the base of the cone} = \\ C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \end{aligned} \quad (138)$$



exposed receptor cell to the light. On receptors chemical compounds of receptors, Gibson has said that, "Like the substances used in photographic emulsions, these are capable of reacting differentially to the energy and wavelength of light" (The Visual World, 48), and that "nothing gets into the eye except radiant energy" (The Visual World, 54). He has also revealed that

The distance away from the area of the array that the perceiver samples during action of the visual system is equal to the height of the cone. Within the area of the sample, there is a contained amount of information about layout. The problem of including both the wave-length interpretation and the sampling interpretation within the structuring of the ambient array arises when we consider that the wavelength has not gone through the entire transition with respect to the ecological structure of the area when there is a sampling, but is realistically compiled by the visual system into an image. The problem can be partially resolved by considering that the visual system samples very many specific receptions of light or regions of layout from the sampled area within a general sample. These wave-lengths give information to the perceiver in terms of saturation, hue, brightness and thus, contour.

I will now do some algebra to conclude what the height of the cone is in terms of the initial parameters. It can eventually be reduced to a single variable when ideas like differentials of distance and frequency are included in the setting up of the equalities. This will lead to numerous *nested equations* that describe different parameters of the information being delivered within a visual system. We consider that the radius is equal to a single wavelength, not half a wavelength, because we are discussing the time it takes to travel a distance of one wavelength of light, and that wavelength travels through the height of the cone. Although, the shape of the diameter can later be shown through three-dimensional graphs to have the shape of a sine wave.

$$\text{Solve}[r_1^2 + \eta^2 = r^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\} \quad (143)$$

We say that the amount of  $\theta r = s$ , taken out of the circle is the change in the circle's circumference that is the base of the cone. The change is equal to  $s = 2\pi r - 2\pi r_1$ .

Notice that  $\theta =$

$$((2\pi r) / r) - ((2\pi r_1) / r), \text{ because we divide by } r \text{ on both sides.}$$

We will focus on the positive solutions for the height of the cone.

$$\text{Solve}[\eta == \sqrt{r^2 - r_1^2}, r_1]$$

$$\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2 - \eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2 - \eta^2} \right\} \right\} \quad (144)$$

This is the change in circumference with

the substituted expression for  $r_1$  in terms of  $h$  and  $r$ .

$$r\theta == s == 2\pi(r) - 2\pi\sqrt{(r)^2 - \eta^2} = 2\pi(r) - 2\pi r_1 \quad (145)$$

$$\theta == (2\pi r) / r - (2\pi r_1) / r = ((2\pi r) / r) - \left( (2\pi \sqrt{-\eta^2 + r^2}) / r \right)$$

$$\text{Solve}[\theta * r == 2\pi(r) - 2\pi\sqrt{(r)^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\} \quad (146)$$

$$\text{Solve}\left[\eta == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\} \quad (147)$$

$$\text{Solve}[\theta * r == 2\pi(r) - 2\pi r_1, r_1]$$

$$\left\{ \left\{ r_1 \rightarrow \frac{2\pi r - r\theta}{2\pi} \right\} \right\}$$

### III. Light through the Arc and Height

There is information available in the stimulation, so there is also information communicated to the perceiver. A change in the environment, when measuring size, is the revolution of the system in time through the distance of the combined, effective wavelength of light (a revolving of the system in time). The change of layout is ongoing, and a parameter of that structure is invariant, so the disruption in the array by contour, edge, etc. specifies the event. That event transitions and transforms through its path to the perceiver. Gibson said about the ambient array that, "The theory of direct perception presupposes the sampling of the ambient array by the ocular system. What is this sampling process?" (BRP 165).

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\} \text{ is the height of a cone}$$

in terms of a difference of circumferences, invariant through  $r$ ,  
because it is always the slant of the cone and also the value that the  
base of the cone cannot reach, because once it reaches that value,  
it is no longer a cone, but collapses to a circle. (148)

#### Looking at solutions for $\theta$ from both the positive and negative solutions for reflective $\eta$ .

By knowledge of total time through perception, we say that the absolute value of the negative solutions for angular transformation plus the absolute value of the positive solutions for theta are related to total time of perception in both a stationary and relative system. This is shown much later, but it is useful to note about the reflection of time for such purposes later in the paper.

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\}$$

$$\text{Solve}\left[\eta == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2 \pi \left(r^2 - \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right\}\right\} \quad (149)$$

$$\text{Solve}\left[\eta == -\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

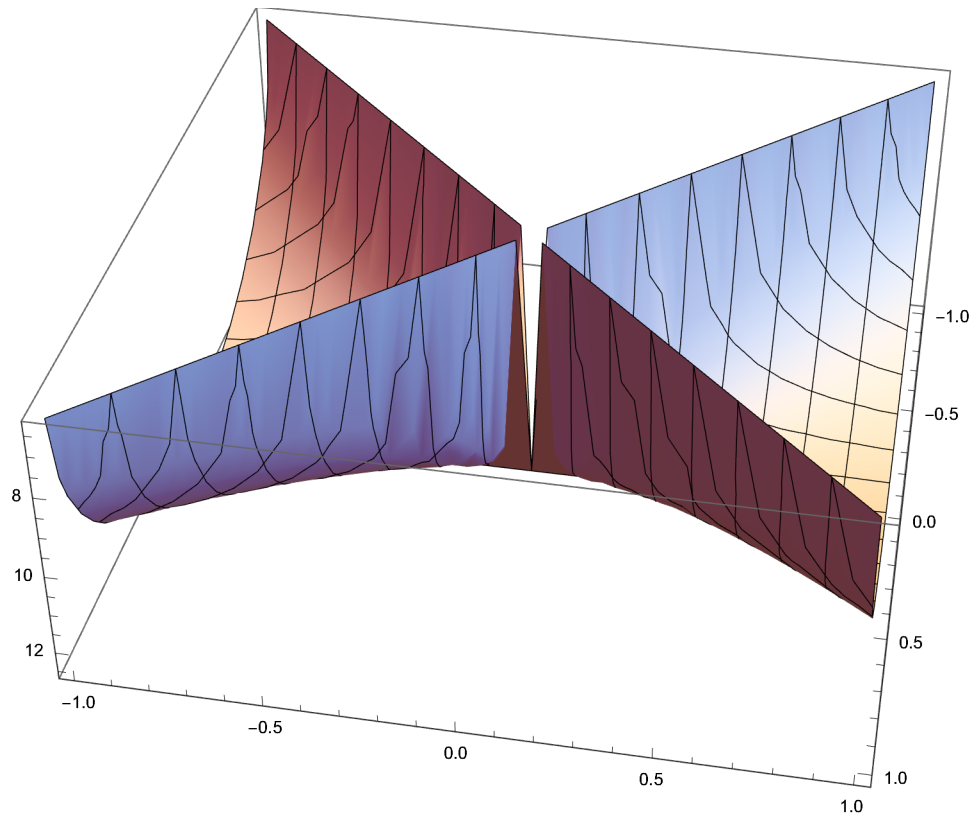
$$\left\{\left\{\theta \rightarrow \frac{2 \pi \left(r^2 - \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right\}\right\}$$

When the height of the cone reaches the locus of perception, the height has fulfilled its initial condition of the initial radius.

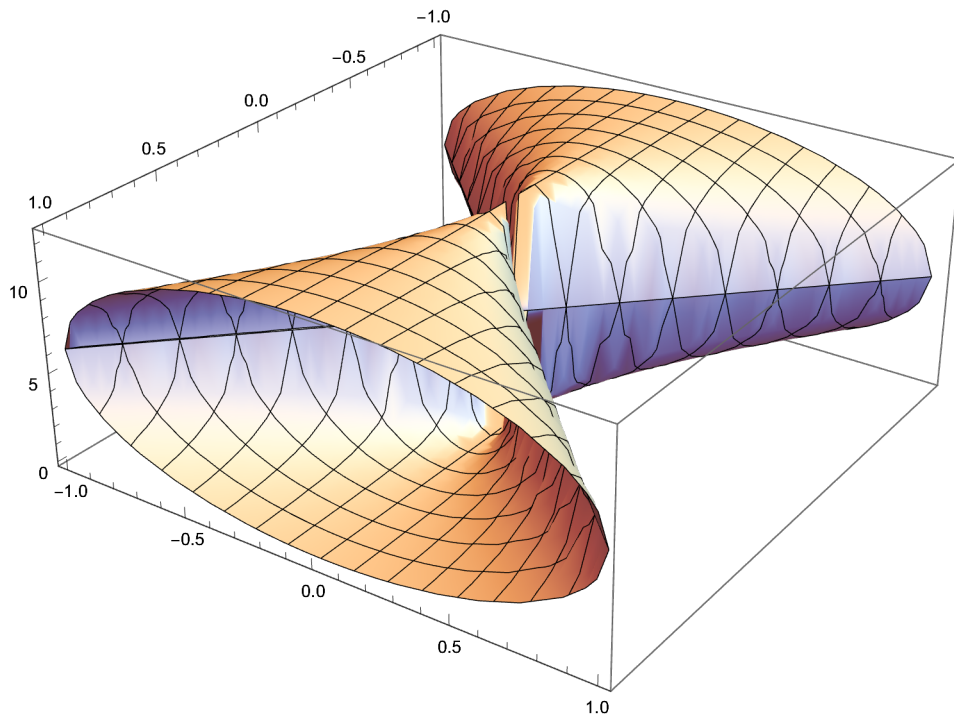
$$\text{Solve}\left[\text{Abs}\left[\frac{2 \pi \left(r^2 - \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right] == \text{Abs}\left[\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right], \eta\right]$$

$$\{\{\eta \rightarrow -r\}, \{\eta \rightarrow r\}\}$$

$$\text{Plot3D}\left[\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}, \{r, -1, 1\}, \{\eta, -1, 1\}\right]$$



Plot3D[ $\left\{\frac{2 \pi \left(r^2 - \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}, \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right\}, \{r, -1, 1\}, \{\eta, -1, 1\}\right]$



Looking at solutions for  $r$  from positive solution for  $\eta$

$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} = \eta, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}\right\}\right\} \quad (150)$$

The radius in terms of the height of a cone is designated by the variable  $r$ .

$$\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} = r = \frac{2 \pi * r * \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}} \quad (151)$$

Note that whatever  $r$  is equal to, the equation simplifies to  $1 = \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}$  (152)

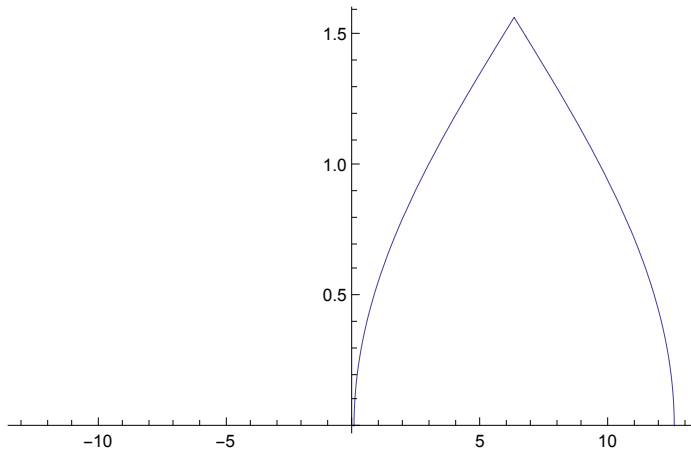
We can solve this equation for  $\beta$ , the angle made by the slant of the cone and the base of the cone, in terms of theta (the amount of angle involved in folding the circle up into the third dimension when the slant is always equal to the radius).

$$\text{Solve}\left[1 = \frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \beta\right]$$

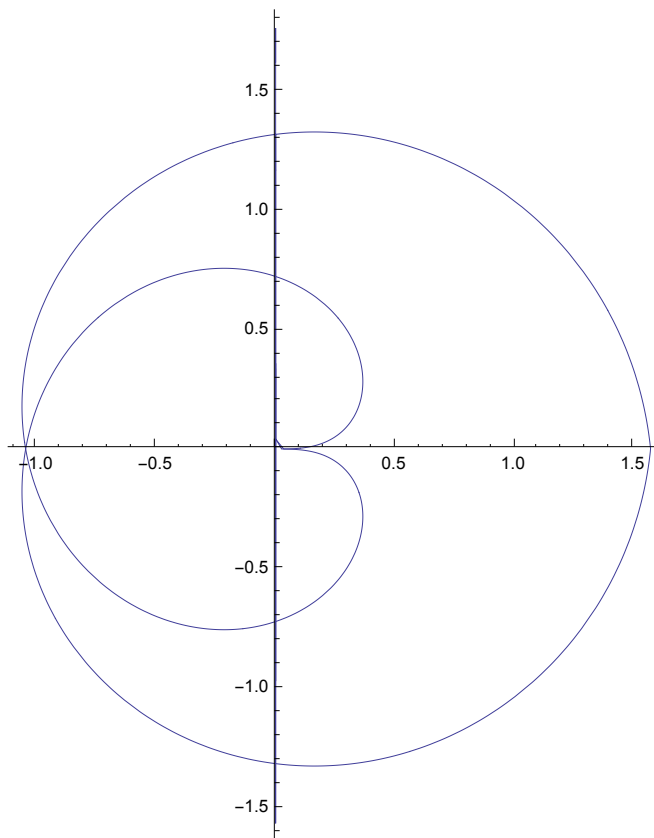


$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right\} \right\} \quad (153)$$

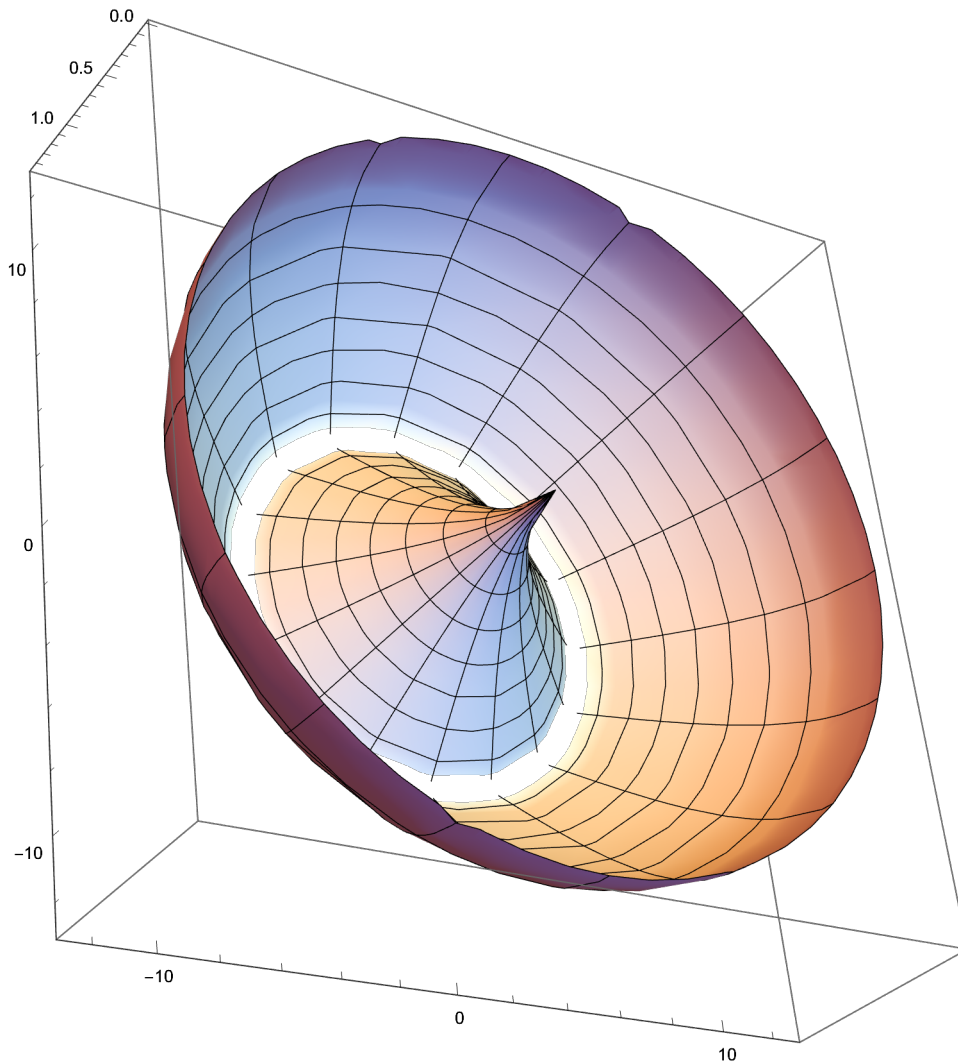
$$\text{Plot} \left[ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right], \{\theta, -13, 13\} \right]$$



$$\text{PolarPlot} \left[ \left\{ \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right\}, \{\theta, -13, 13\} \right]$$



```
RevolutionPlot3D[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ], { $\theta$ , -13, 13}]
```



The single point in the field of optical flow, light traveling through the ambient array, I propose, is represented by the three dimensional revolution graph of a change in radius over time through transformation to being the height of the cone from the two angular variants of the system. A revolution delivers information to the perceiver given the intensity, hue, etc. of light. A single revolution of the system is equivalent to the flow of combined light in the ambient array at location of the station point of perception in the ambient optic array.

There are ways of solving for the radius in terms of purely the angle,  $\theta$ . We will examine these nested sets of ways of understanding the point of view. By nested, we mean that depending on how in

depth one goes into observing the world or extrapolating a function of light in the array, one will see different visual representations of the structuring of that information that are more or less informationally dense. This will lead to a series of functions that give us introspection into the structuring of light in terms of a cyclic perspective on time. For the system, it is important to realize that in the normal course of parameterizing the motion in the case at hand,  $\theta$  does not go beyond  $4\pi$  (i.e. that it sends the height of the cone up to its maximum value and back down over the course of two revolutions of a circle), and that  $\beta$  would not be able to be easily thought of beyond  $\pi$  or  $2\pi$  (it has a value of  $\pi$  at the maximum height of the transition, and a value of  $2\pi$  once the cone comes back down from the height).

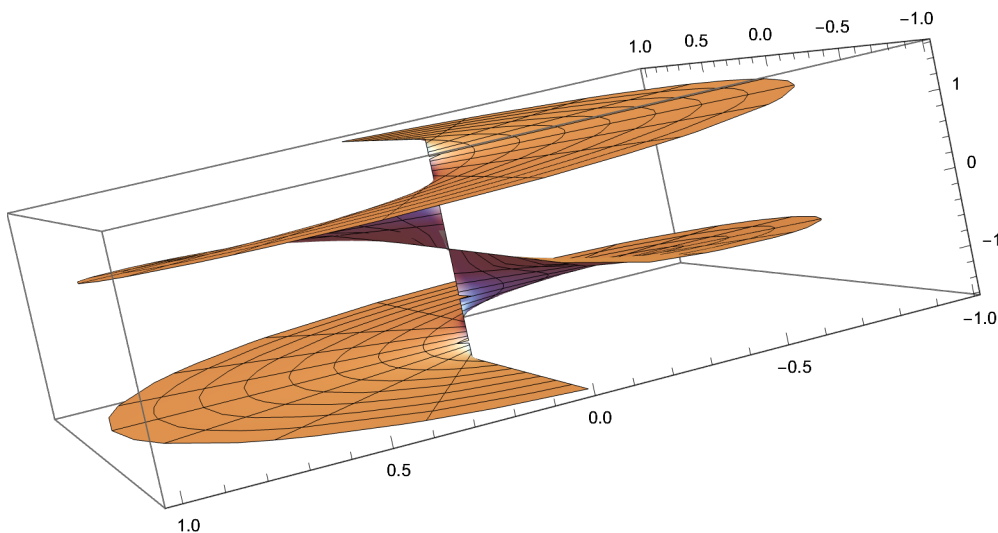
To understand more how these equations are related, we can make substitutions in various ways, all of which are not arbitrary. For instance, we know that the height of the cone is equal to two different functions. We can set these functions equal to each other and extrapolate different visions of the function.

$$\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = r \sin[\beta]$$

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} == r \sin[\beta], \beta\right]$$

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{r^2 (4\pi - \theta) \theta}}{2\pi r}\right]\right\}\right\}$$

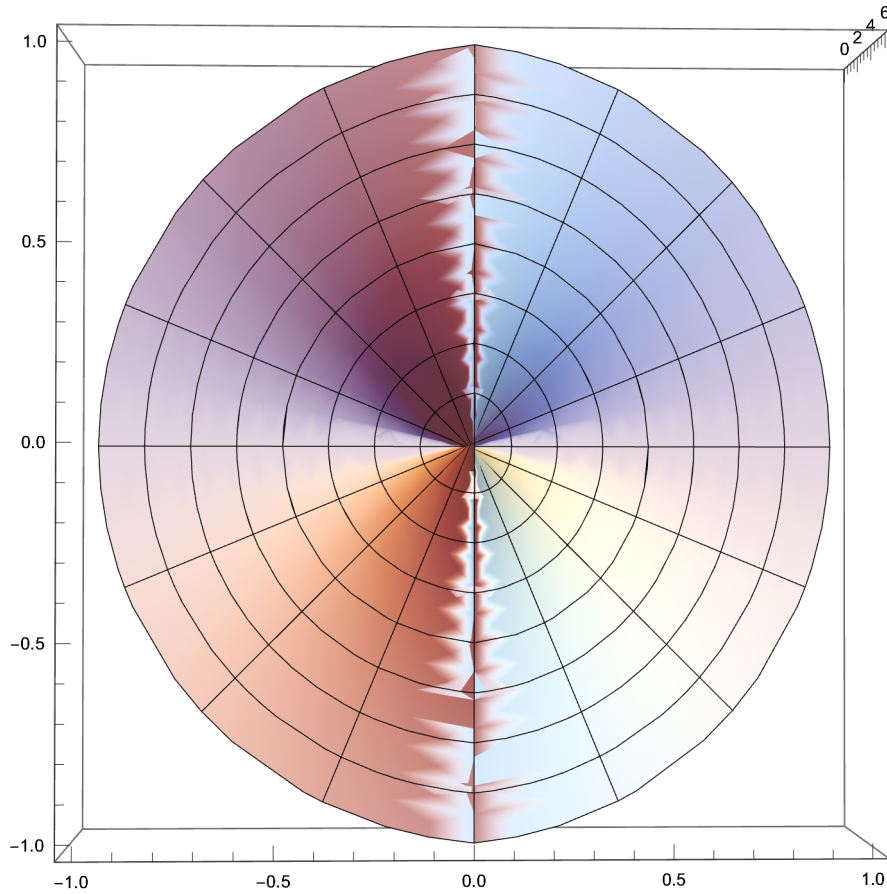
$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[\frac{\sqrt{r^2 (4\pi - \theta) \theta}}{2\pi r}\right], \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

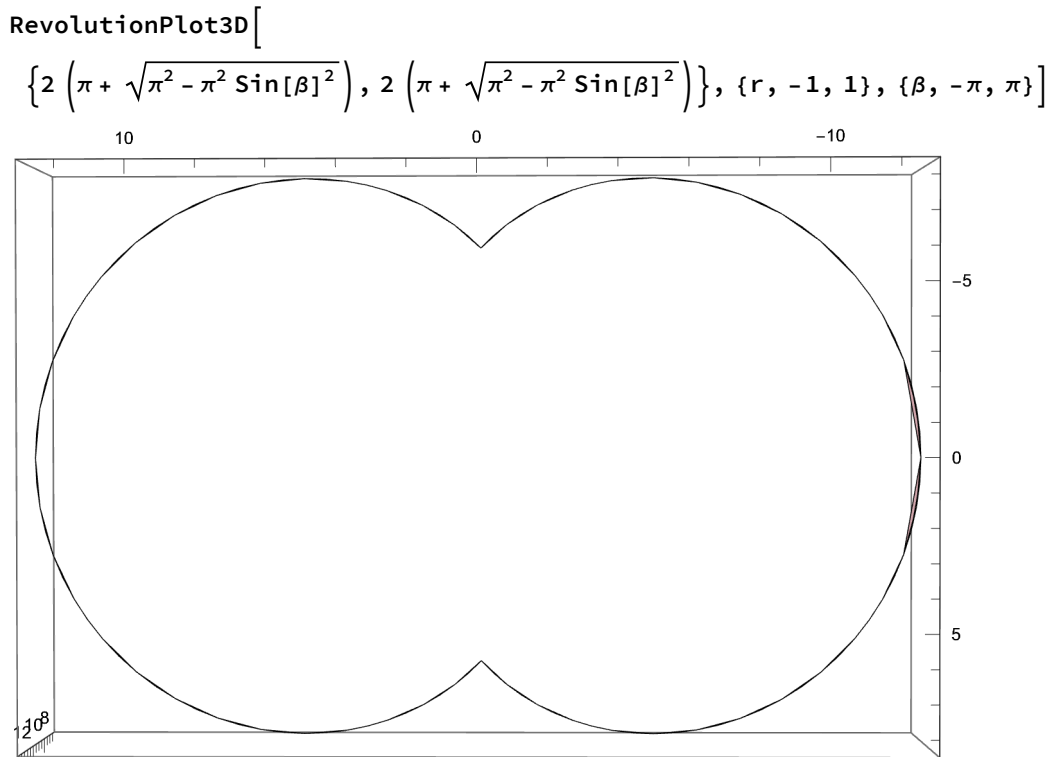


$$\text{Solve}\left[1 == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\} \quad (154)$$

$$\text{RevolutionPlot3D}\left[2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right), \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$$





Gibson has said that, "The experience of the visual world is not compounded of a series of visual fields; no one is aware of the *sequence* but only of the total *scene*. Presumably this is because the ocular system detects the invariants over time that specify the scene" (BRP 166).  $\Theta$  is the variable that is akin to the accumulated time of our system. It is an angle, and if we relate it to measurements made of time cyclically, like those of a clock, we can find how the invariant, which is the initial radius of the system, will guide the information communicated during the pickup of invariants. The time variable contains a contour based on the parameters of the system.

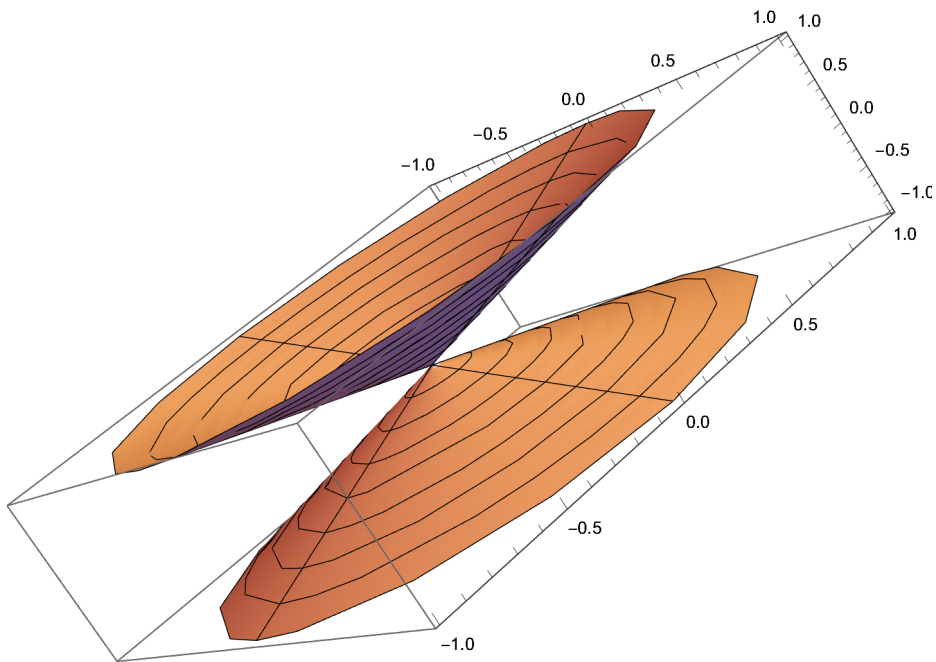
$$r = \frac{2 \pi * r * \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$$

The invariant is  $r$ , because it is always the slant of the cone during transition of a total combined effective wavelength that immediately effects the receptor. This means that if a wavelength were to change during travel through the modular of space-time due to being part of an ambient array, where light waves effect each other during their paths, the initial wavelength of light is the slant of the cone, even though the resulting height may be longer or shorter than the initial wavelength. What does this tell us about light and how it travels through space or effects a receiving perceiver? Knowledge of the initial condition of the system depends on the recognition of the receptor. To be the combination of constructive and interfering frequencies of light in the array, invariance of  $r$  contextually assures that the cumulative effect of the wavelength of light can only be discerned by the subjective perceiver, whose perceptual locus is at the maximum height of the cone.

$$\beta = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

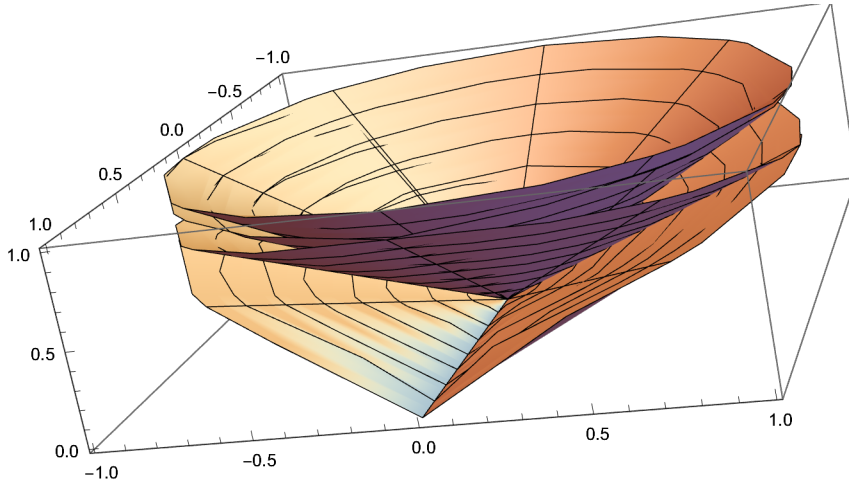
$$\frac{2\pi * r * \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} = \frac{2\pi * r * \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]}{\sqrt{4\pi\theta - \theta^2}}$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi * r * \text{Sin}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]}{\sqrt{4\pi\theta - \theta^2}}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$$



$$\eta \rightarrow \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}$$

RevolutionPlot3D $\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$

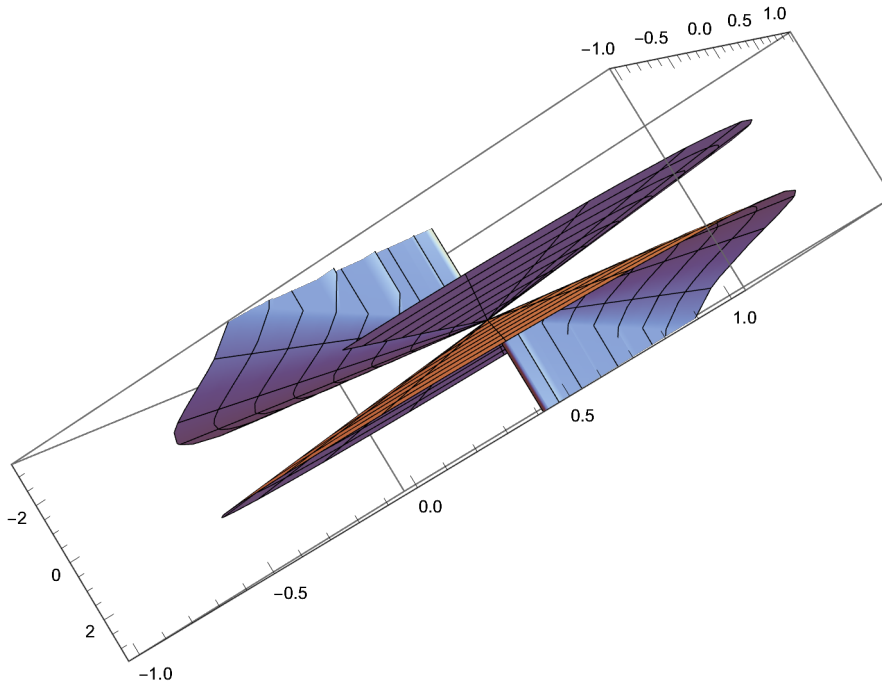


This is how the graph of the height of the cone in non - relativistic terms would look. It can be noted from the following graphs that within the parameters of the system, there is a similar graph to the relativistic length contraction transformation, but beyond the parameters of the system, the graphs begin to look slightly different.

This equation graphs the height of the cone by revolving  $r$  through  $\theta$ . The structure of the array includes the distance,  $\eta$ .  $H$  can be equal to the new wavelength of light during a transition with changing wavelength of the structured substance, but it can also be a definitive distance of an object away from the perceiver.

$$r = \frac{2 \pi * r * \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}$$

RevolutionPlot3D $\left[\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



When we try to see what the structure of a single point of ambient light is, we acknowledge that this point is potentially infinitely far away at the horizon curve, and potentially infinitely divisible if the wavelength of the light gets infinitesimally small. When we stand on an infinitely large sphere, there is no way to tell how long or far away the horizon is. In order to get interpretations of meaning of other parameters of the system, we say that wavelength can change during a transition (a transition here means traveling the distance of one wavelength).

What can we tell from these models? We can see that parameters of wavelengths of substance traveling through space and time, like light, contain within them information that is already contoured, or from point to point draws out contour through recognizing trends of invariance. When we take a



different angle on them, we see the contour differently. This effect will be even more noticable in later models when we see that there is very subtle contour and shimmering.

It is possible that direct perception does not contradict information processing, because the pickup of information directly acknowledges that there is information in the layout of the world, transferred directly by light stimulus during the perceiving instance. That instance receives the delivery of information based on invariance. That delivery comes from a reflection off the contour through a combination of relations in the guidance of the flux of ambient light. Computational approaches simply would have to change their Philosophy to an ecological context and simply stick to observing the phenomenon of perception (i.e. what I see changing in the environment that can be correlated to objects or people in the world).

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## IV. The Analogy of a Change in Position Relating to a Change in Contour during the Pickup of Invariants through Time

Gibson has said that, "The theory of information pickup requires perceptual systems, not senses" (BRP 77). Gibson also relates the subtlety of the perceptual system to learning and time. He thinks that we continue learning to perceive in more detail as time goes on. This will be an important idea when discussing the extrapolation of functions into images through an impression from an expression, which relates the information in the array over time to the perceiver.

The wavelength of the light we are discussing is the initial radius of the circle and the maximum height of the cone, whose direction is toward the subjective perceiver. The transition of that single wavelength into the height of a cone occurs over the course of a revolution of a single circle. The parameters of the velocity of its travel, or the travel of any substance, are frequency and wavelength.

We state that :  $v = \lambda f$ , where  $v$  is velocity,  
 $\lambda = r$  is wavelength, and  $1/\text{time} = f = \text{frequency}$ . (155)

$\text{Time} = 360 \left( \theta_{\text{degrees}} \right) = 2 \pi \theta$  (156)

The velocity being discussed is the first derivative of the distance, which is the height of the cone,  $\eta$ . A tiny piece of the ambient array would contain within it information regarding information of the surface off of which the light flowing through the array is reflecting.  $H$  contains information about the time and initial distance of a wavelength of light. Where  $\eta$  is a given height of a cone, and  $\theta$  the amount of accumulated time of during a transition,  $r \cdot \theta$ , which is the difference of the change in circumference between two circles that correlates to the height in the third dimension, the radius of the base of the cone changes in a pythagorean relationship to  $r$  and  $\eta$ .

In the model of perceptual space - time that I am proposing, the parameters involved can always be reduced to a single expression of a function of time, "it is not meaningful to ask merely how strongly a given unit responds to a given stimulus; the more relevant variable is the temporal pattern of the

response" (BRP 244). Is it possible that the firing of the neurons relates strongly to time, because the shape of the stimulus has an invariant correlate geometrically through time?

Merleau Ponty has said of time, "there is one single time which is self-confirmatory, which can bring nothing into existence unless it has already laid that thing's foundations as present and eventual past, and which establishes itself as a stroke" (PoP 421). The time that is self confirmatory is the time at which the height of the cone has gone up to  $2\pi$  and come back down over the course of  $4\pi$  radians. In time measured in seconds, this would be one minute in S.I. units, but .

Time is the passing of all real moments into each other and all imaginary moments into the real. This ensures the existence of geometry. In this way, we say that being is through embodiment, but meaning of being is through time, after the body decays. There is the present moment, and when we perceive the world, we are not interpreting our experience based on the passed time, but change of time equal to the total difference in past and present time.

However, by a moment, do we not mean a change in time? This is to say that time has positive and negative solutions within a system of geometric correlations. The experiential moment grows to include the past and present, because time has positive and negative solutions within a given sample of the ambient optic array. This is why going into the mind can extend the experience of time while at the same time experiencing vision. This is because time is based in the spatio-temporal continuity of objects, and mind is capable of the pure reception or inception of persona.

Information of variable contour is transferred to the perceiver by the flux of information in ambient light through each point in the optic array, represented by item number four. The rate of this variance is analogous to velocity in a rotational system, like the structuring of light through space - time. This is what is meant by information in the light. Objects can travel through space-time in a continuous way.

Helmholtz proposes that phenomena regarding the visual system can be described by the use of analogy when things begin to look paradoxical. He takes into consideration the psychic faculties and suggests that the processing of the environment and its perceptual phenomena may occur through an unconscious working of analogy in the mind. I find this to be interesting and agreeable. It provides a humanist account through the recognition of biological factors regarding perceptual systems.

Animals on Earth have evolved in a general perception of time in the environment to be cyclic. The day and night, the rhythm of sleep, the change of the seasons, and the cycles of heavenly bodies like the moon all play a role in the environment of evolving animals on Earth. Some more than others, but for humans, most certainly.

Gibson offers an interesting interpretation to the problem of depth perception. Depth perception is at the heart of what we are discussing. The height of the cone, in a more ecological context, is directed toward the perceiver and contains contoured information within it based on the wavelength of light and time elapsed during transition. This contoured information exists in every point of the array, and ecological contour is based on the pickup of each wavelength in its relation to the others during a sampling of the array.

Gibson says that, "the problem of depth perception is insoluble, because the problem is false" (BRP 166). He also suggests that we are mistaken in thinking that the, "third dimension of the cartesian coordinate system is a phenomenal fact of perception" (BRP 166). Our coordinate system for describing a tiny piece of interactions going on in the ambient array is based, not on a third dimension of cartesian coordinates, but of a single transition of substance through time. It should be noted that at the event of perception, the information of contour in the layout of the world is delivered to the receptors at a length that has only one dimension at the time of reception. The combined effect of, "points of observation in the medium" (BRP 167), as Gibson might put it, transmits the layout of the world to the perceiver by a mesh of interwoven specifiers.

The perceptual space relies on a conscious experience. Math and the body of sciences can be useful in modeling the elements involved in the deliverance of subjective experience if enough relevant contextual information is given to the model. Right now, machines manipulate signals, but do not have the complexity that human experience has, partly because their system does not have the evolutionary resources developed in an environment over time when constantly responding to its inputs.

The facts let me see contour, while also recognizing that contour from a single image could be illusory. We take data available in light, and construct an image from that data of an object, "though such flip - flopping seldom occurs when we are looking at real cats, it sometimes happens with specially constructed figures viewed under restricted conditions" (BRP 278). If we take the information in light and structure to be a fact, I would say that flip - flopping also occurs under the most general conditions and correlates of known facts to perspectival emanations, which specify qualities of a perception. Depth gives us such determined information, guided by objects that deliver layout to the percept, that flip - flopping rarely occurs. This is what defines an object for visual perception is its stability.

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## V. The Wavelength with Constant Value

$$v = \lambda f = r / \tau = r (1 / (\theta / (2 \pi))) = \frac{2 \pi r}{\theta} = (1 / (1 / (2 \pi))) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] = \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \quad (157)$$

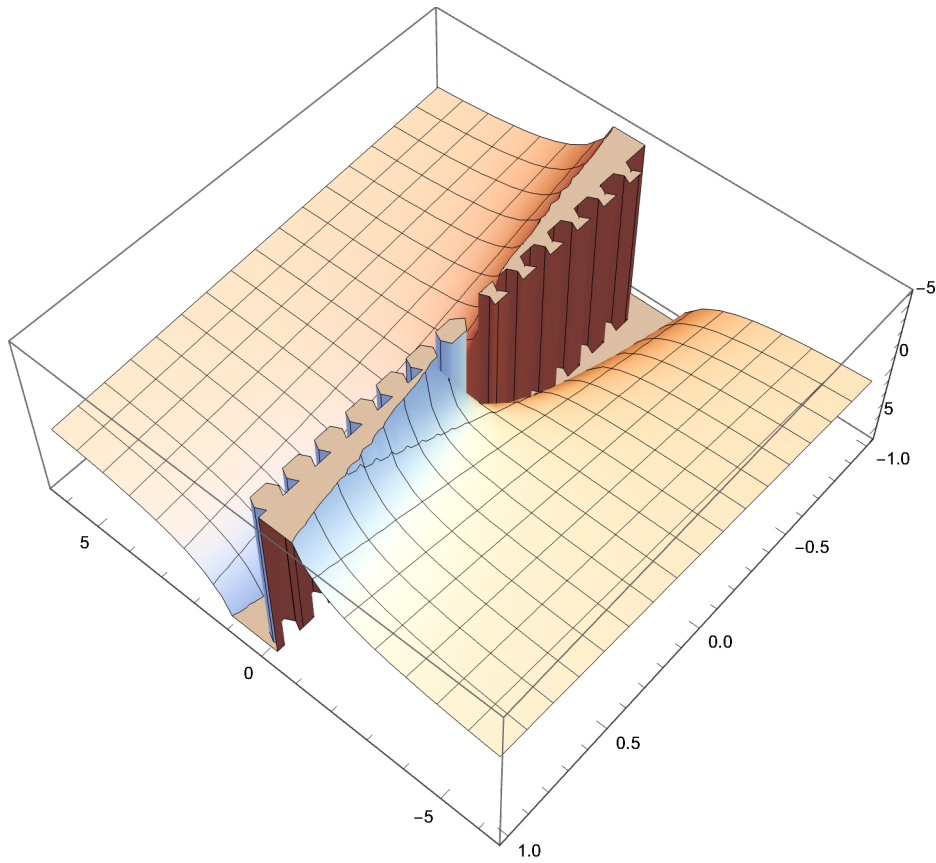
$$2 \pi r - 2 \pi r_1 = \theta r \quad (158)$$

$$\frac{(2 \pi r - 2 \pi r_1)}{\theta} = r \quad (159)$$

$$\frac{2 \pi r}{\theta} = \frac{2 \pi r_1}{\theta} + r \quad (160)$$

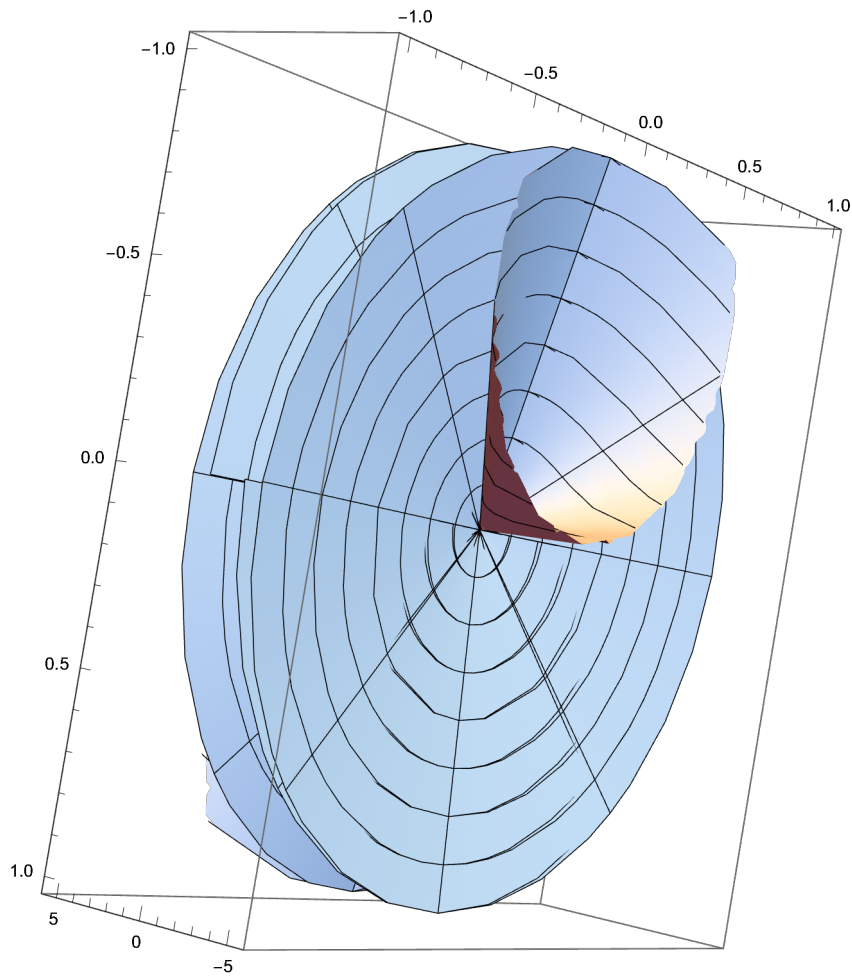
We will try to build up as many functions as possible without resorting to designating something to have a velocity of light or non - light. It is simply a velocity for the time being. This way, we will have access to a realm of general functions of correlated variables.

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Plot3D[ $\frac{2 \pi r}{\theta}$ , {r, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]
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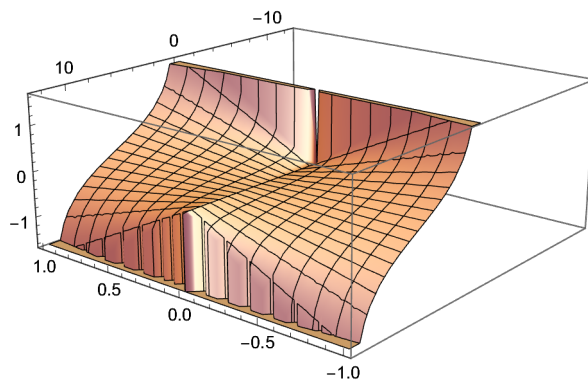
Now we can visually see how velocities would be superpositional. They can fit right on top of each other in this lego - like system while continuing along the same contour.

RevolutionPlot3D $\left[\frac{2 \pi r}{\theta}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$

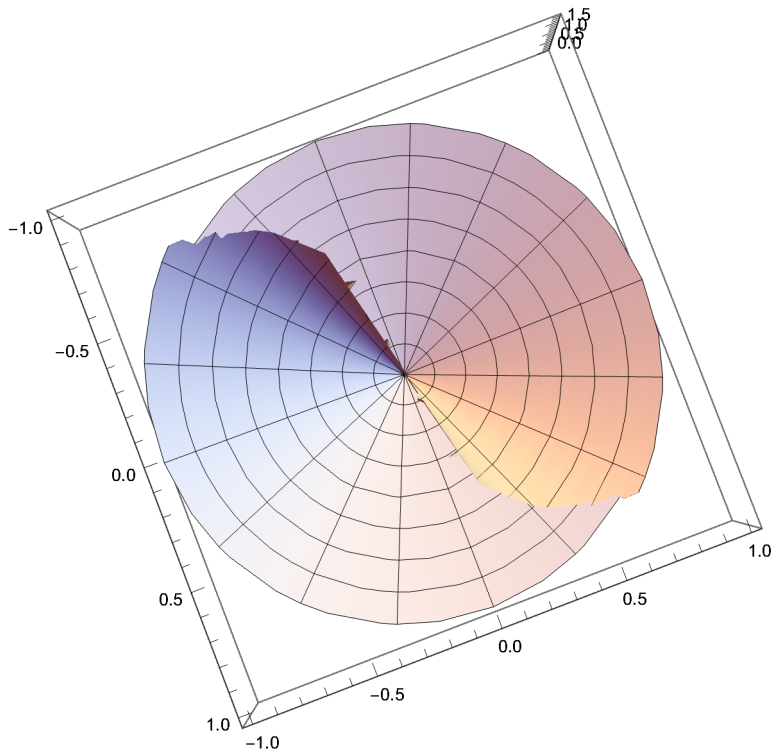


$$\text{Velocity when } r \text{ is constant} = \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \quad (161)$$

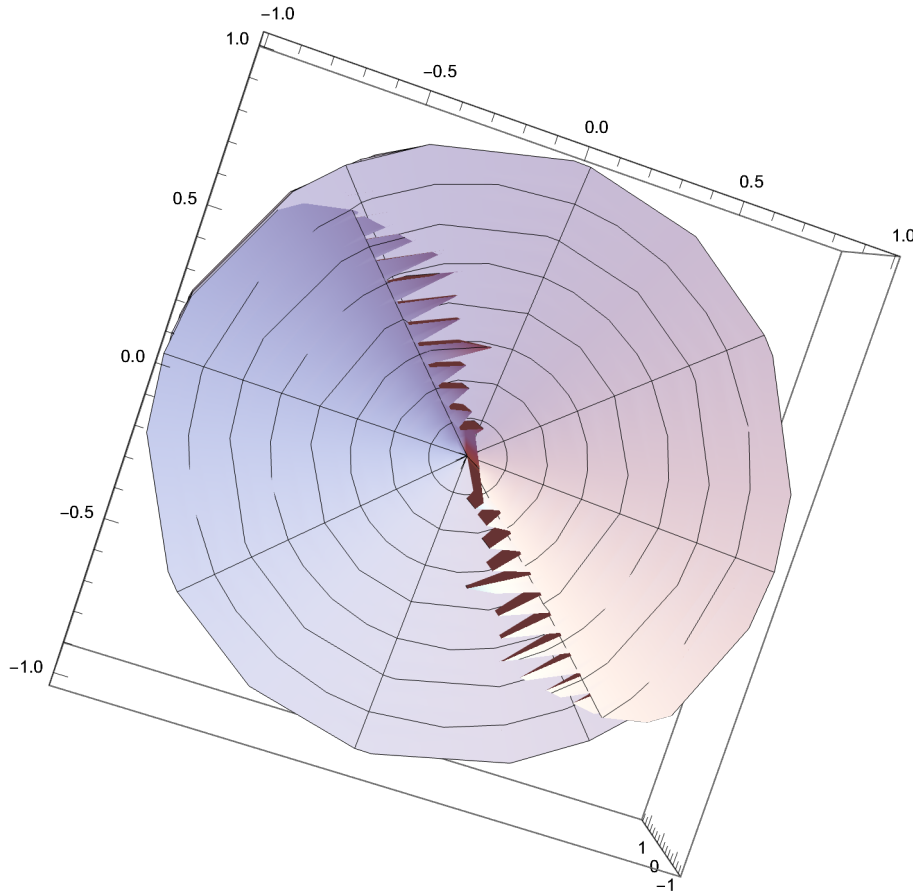
Plot3D $\left[\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$



$\text{RevolutionPlot3D}\left[\frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



RevolutionPlot3D $\left[\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$



We also have access to the equation,  $\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = r / (\theta / (2 \pi))$ ,  
 which winds up having the  $r$  variable cancel out,  
 and delivers three exact solutions for theta. (162)

$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \frac{2 \pi r}{\theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2}{3} \left(2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi\right)\right\},\right.$$

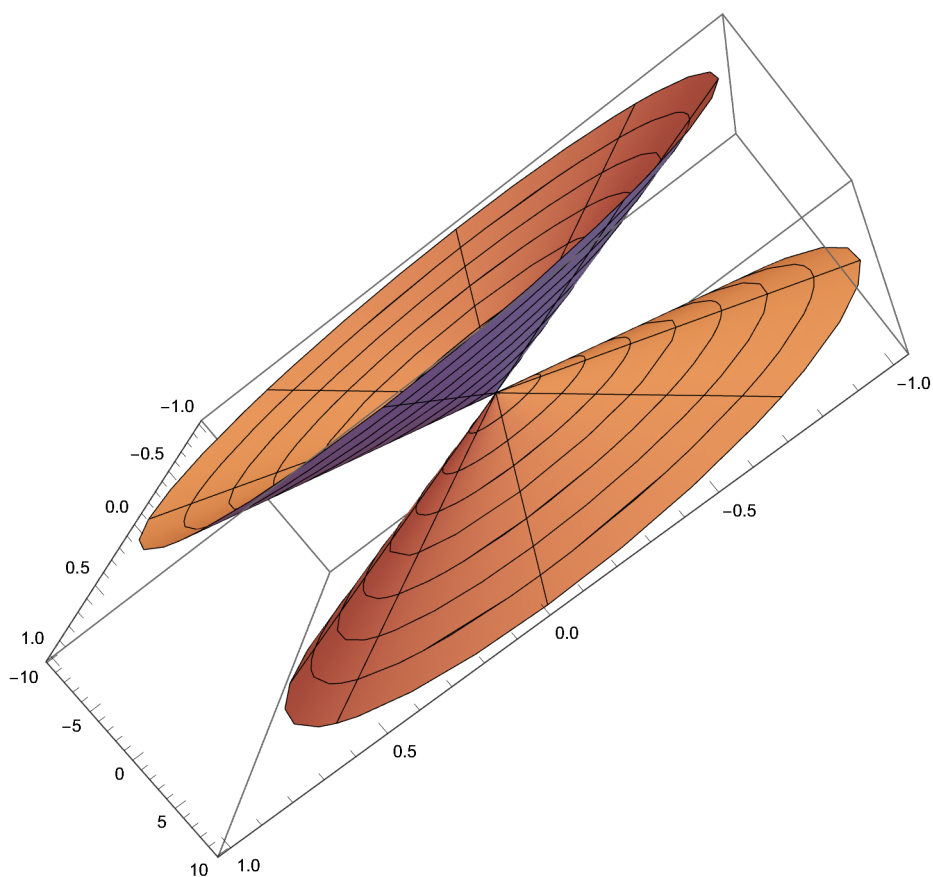
$$\left\{\theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi\right\},$$

$$\left\{\theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 - i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 + i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi\right\}\right\} \quad (163)$$

With these exact solutions for theta, we are afforded the opportunity to look at a change in circumferences by multiplying the results by the initial radius. We remember from the initial postulates that the change in circumference of a sample of the ambient array was equal to the initial radius of an angle.

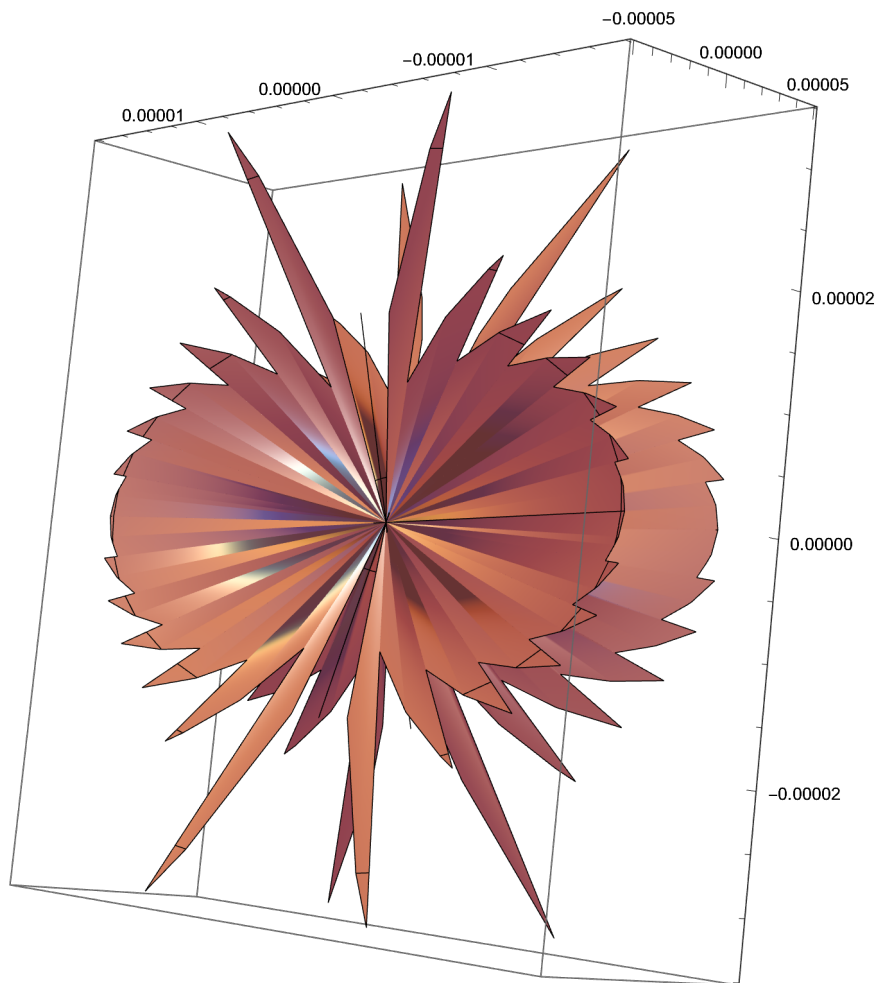
**RevolutionPlot3D**[

$$r \left( \frac{2}{3} \left( 2\pi - \frac{2\pi}{(17 + 3\sqrt{33})^{1/3}} + (17 + 3\sqrt{33})^{1/3} \pi \right) \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$

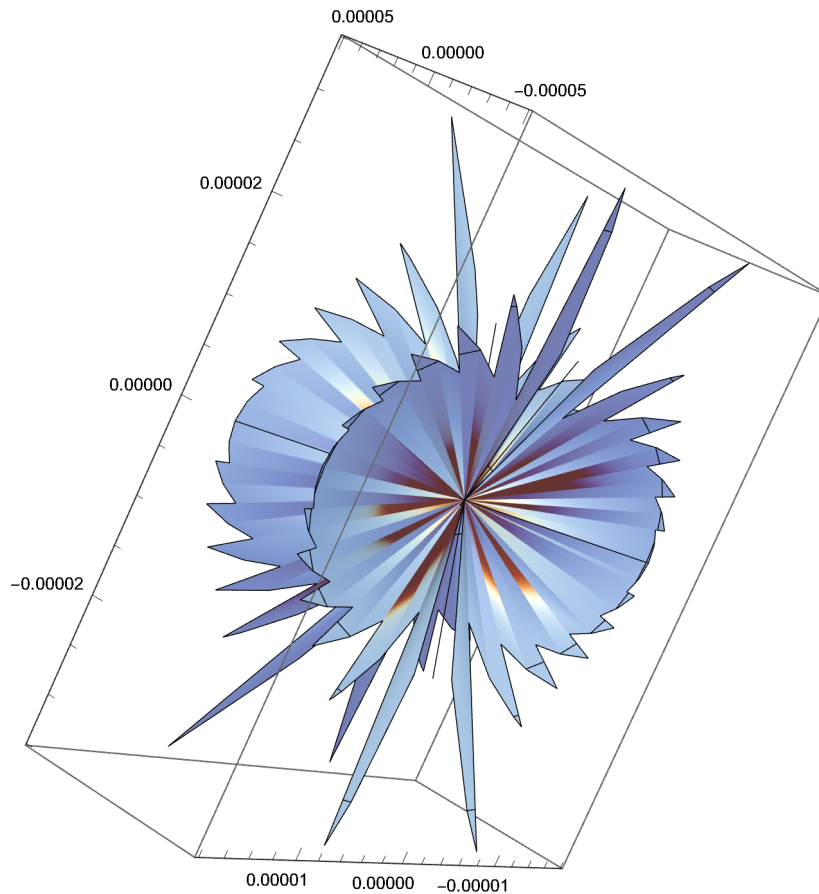




$\text{RevolutionPlot3D}\left[r \left( \frac{4\pi}{3} + \frac{2(1+i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1-i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right), \{r, -1, 1\}\right]$



RevolutionPlot3D $\left[r \left( \frac{4\pi}{3} + \frac{2(1 - \mathbf{i}\sqrt{3})\pi}{3(17 + 3\sqrt{33})^{1/3}} - \frac{1}{3}(1 + \mathbf{i}\sqrt{3})(17 + 3\sqrt{33})^{1/3}\pi \right), \{r, -1, 1\} \right]$



We will note that an arc length is equal to  $r \cdot \theta$ . The change in perceived circumference of the circle is also equal to  $r \cdot \theta$ . Thus, we will be able to see what the arc length is, because it represents the change in circumference of two circles. In this case, as the circle, viewed from head on, recedes from the perceiver into the distance, it gets smaller. This is a change in amount of surface area taken up on the retinal image, but also a way of visualizing how the imaginary solutions for the time element of waves traveling in space affords a perception of layout.

Light travels through space, but within its travel is the information that the angular element of the system, which is akin to time, conveys specifically about the location of contour in perceptual space through a geometric correlation. This correlation occurs through the complex plane and has the capability of mapping out contour in the visual perception directly by analogy of larger ecology to individual play of ambient light off of a contour. We will try to show this symbolically as well as directly.

When combined, the three imaginary solutions form a cone, but separately, they exist primarily in the complex plane. It requires all three solutions to deliver information of depth to the perceiver through light in terms of the real. In Gibson's theory, depth is intimately connected with contour. Contour is delivered by the pickup of the invariant,  $r$ , in the ambient array, changing context in a

different way from point to point. Thus, understanding of two truths in the real world like information given to the perceiver of an object by an edge, for instance, is enabled. At the moment of perception, we have a total amount of time equal to 0, but since time continues, and time has passed, there is a total amount of changed time from past to present, which is equal to the absolute value of the negative solutions for time plus the positive solutions. We will not use this interpretation, because it is an in depth introspection into the experience of consciousness, which would require understanding of cognitive systems or possibly spiritual experience, and we are only looking at the phenomenon of the structure of perception.

Mach began by verifying a belief in the space - sense, an area of parameterized space relating the sense of an individual to the stimulus in the world. The space - sense provides a workspace for the individual senses like sense of sight and touch to enable a perceptual experience. “The perception of Depth depends on extra - ocular experiences” (BRP 118) is an idea that makes a great deal of sense to me, because when we experience or perceive truth, we use multiple faculties to make sense of a phenomenon.

The ambient optic array, which is the entire collection of individual points of light, binds single points in the array through the complex plane, and affords the perception of objects, because objects disrupt the array in the real, but the structure of light assures that the imaginary elements of objects correspond to only one real object. Or, if there is a real object, then the imaginary elements of perceiving that object specify a single event of perceiving that object.

The imaginary solutions to perceiving objects through time could change only if the qualia of the layout of objects changed, or the disruption in the array changed to remain allowing the overall combinations of modulars in the single modular of perception through consciousness. We still ask if personality of the perception changed the meaning of the object to layout of the world within the unified modular of perception, would the structuring of the array change or harmonize with the substance? Sampling allows us to determine if the layout is different from structuring, because the array is the environmental context of the perception, and shares a similar structure to each point within it. This is a manner of perception.

The mapping out of contour from information in light shares a similar structure to the measurement of size. I don't think it makes sense to begin by postulating an object, only postulating that there is the pickup of information that there is contour in the environment. The perception of this contour like it is an actual object, however, is ephemeral and somewhat illusory. All we can have access to for studying vision scientifically or phenomenologically is the percept of contour in a projection to the mind, “My knowledge of the plane crash derives from my knowledge of the newspapers because I did not see the plane crash” (BRP 273). However, to find out how perception operates, we must recognize the conditions necessary for information to be transferred from the environment that it is at least partially a complex environment.

The initial radius changes context, but can it be said to actually change? The wavelength,  $r$ , could be said to be changing if we consider that  $\Delta r = r - r_1$ . Although it is invariant in the context of always being the slant of the cone, it changes when understood to be the base of the cone. It also changes

meaning when we consider the structure in an ecological context. The height of the cone starts at the place where there is an infinitely perceived radius (i.e. no perception, all white eye-caps, or unseen, because it is so far away on the horizon), and goes toward the locus of perception, which is the perceiver. It is reasonable, to think that a wavelength could change during the course of traveling a single wavelength through cominative substances like light or water. When the circle is infinitely far away, it has a perceived radius of 0, and this is the same point at which there is nothing perceived, because channels of sensation eventually disappear after extending in time. Layout and contour come into focus best when during the awareness of time extends into the very small amounts of angular passage per sample.

A relativistic mapping of  $\eta$  looks somewhat different at larger values, but at normal values, it looks exactly the same.

The radius is said to be invariant through the transition from being the initial radius of a circle to being the height of a cone. We set up the equation that says that an arc length of the original circle is equal to a difference in circumferences from transition to a cone, where the Pythagorean Theorem tells us the equation for height in terms of only  $r$  and  $\theta$ , and angular element akin to time. It is always either the original radius of the circle, the slant of the cone, or the height of the cone. The initial radius is constant, but changes context in the system through transition.

## VI. An Inherency of Relativity to Invariance

The radius is said to be invariant through the transition from being the initial radius of a circle to being the height of a cone. We set up the equation that says that an arc length of the original circle is equal to a difference in circumferences from transition to a cone, where the Pythagorean Theorem tells us the equation for height in terms of only  $r$  and  $\theta$ , and angular element akin to time. It is always either the original radius of the circle, the slant of the cone, or the height of the cone. The initial radius is constant, but changes context in the system through transition.

What if the system we are talking about is traveling at relativistic speeds? Not the substance within the system, but the actual system, and all of its parameters. They could all be subject to relativity at the same time or during the same motion.

$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \quad (164)$$

$$r' = r \sqrt{1 - (v^2 / c^2)} \quad (165)$$

$$t' = (\theta / (2 \pi)) / \sqrt{1 - (v^2 / c^2)} \quad (166)$$

$$t' = \theta' / 2 \pi \quad (167)$$

$$\theta' = \theta / \sqrt{1 - ((v)^2 / c^2)} \quad (168)$$

$$r' * \theta' = \left( \theta / \sqrt{1 - ((v)^2 / c^2)} \right) \left( r \sqrt{1 - ((v)^2 / c^2)} \right) \quad (169)$$

$$\left( \theta / \sqrt{1 - ((v)^2 / c^2)} \right) \left( r \sqrt{1 - ((v)^2 / c^2)} \right) = r \theta \quad (170)$$

$$r' * \theta' = r \theta = 2 \pi r - 2 \pi r_1 = 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2} \quad (171)$$

$$\text{Solve}[r \theta == 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}, \eta] \quad (172)$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\} \right\}$$

We make the substitution for the prime system.

$$w := r', \rho := \theta'$$

$$\text{Solve}[w \rho == 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2}, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{w} \sqrt{\rho} \sqrt{4 \pi r - w \rho}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{w} \sqrt{\rho} \sqrt{4 \pi r - w \rho}}{2 \pi} \right\} \right\}$$

Then, once we have solved for  $\eta$  in terms of the prime system, we can resubstitute in for the initial expressions of  $r'$  and  $\theta'$ .

$$\frac{1}{2 \pi} \sqrt{r \sqrt{1 - ((v)^2 / c^2)}} \sqrt{\theta / \sqrt{1 - ((v)^2 / c^2)}} \\ \sqrt{4 \pi r - \left( r \left( \sqrt{1 - ((v)^2 / c^2)} \right) \right) \left( \theta / \sqrt{1 - ((v)^2 / c^2)} \right)}$$

$$\text{Solve}\left[ \frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r \right]$$

{{}}

$$\text{Solve}\left[ \frac{\sqrt{r} \sqrt{1 - \frac{(r / (\theta / (2 \pi)))^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(r / (\theta / (2 \pi)))^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, v \right]$$

{{}}

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{v^2}{c^2}}} \sqrt{4\pi r - r\theta} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right]$$

{{}}

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}}} \sqrt{4\pi r - r\theta} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r\right]$$

{{}}

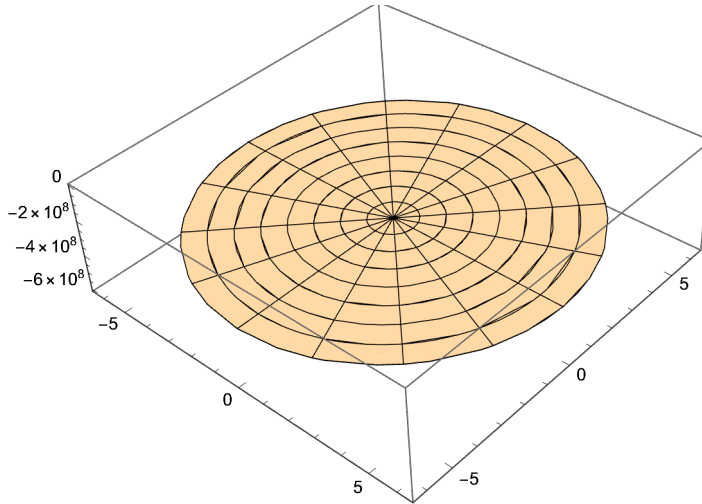
The velocity at the time at which  $\eta = r$  can be found according to theta and the speed of light. We would then substitute expressions for theta in terms of beta in order to visual the equation spherically. This is how our model relates directly to perception. We say that the light (or any substance traveling through the height of the cone) can only be specified by subjective perception or by objectively defining the initial wavelength of the system from the start. The wavelength of light,  $\lambda = r$ , is observed when the cone has completed one cycle of the system in terms of the standard unit of measurement of time. This happens at the distinct situation of  $\eta = r$ , which specifies an event of perception or observation.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{(v)^2}{c^2}}} \sqrt{4\pi r - r\theta} = r, v\right]$$

$$\left\{ \left\{ v \rightarrow - \left( \left( 1. \sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2} \right) \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right) \right\}, \left\{ v \rightarrow \frac{\sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2}}{\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}} \right\} \right\}$$

The positive and negative solutions for velocity have similar, graphical representations in terms of theta.

RevolutionPlot3D $\left[-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{-18}-1.1294090667581471\cdot 10^{-18}\theta+8.987551787368176\cdot 10^{-16}\theta^2\right)}\right)/\left(\sqrt{39.47841760435743-12.566370614359172\theta+\theta^2}\right),\{\theta,-2\pi,2\pi}\right]$



From this, we can see how, from our system, we have specified that time is a continuum. It continues on the x axis out infinitely. Our time variable,  $\theta$ , is in essence, an axis of its own accord.

To see in depth what this observation signifies, we solve for velocity and show expressions for this velocity in terms of theta and beta from the initial conditions of the system. There is a multiplicity of substitutions that we can make. In the end, they will all turn out to have an expression that is envisioned by one of seven different graphical objects. We will give a brief overview of the forms that we find in which substance can travel. We will label them, although each expression for the graphical object will not be given, because there are so many that it would take pages to fill.

We remember from earlier that we can place theta in terms of beta. Each placement of the substitution in a different position of the equation yields another way of perceiving/observing light traveling through space - time. In addition to this, the combination of the functions can occur in the same graphical representation. We will not go into the multifaceted ways of combining these graphs, but specifically outline a few of the more basic, notable forms.

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\}$$

, When we make patterns of substitutions for theta in terms of beta within the equation, we see that there are discontinuous methods for graphing the information contained in the velocity of light or substance to produce a visualization. In other words, the same equation with different orders of substitutions for theta in terms of beta give us different impressions of how we observe the spacetime functioning. That is part of a relativistic equation for traveling through the height of a cone at the point of perception, the event of perception, when  $r = \eta$ . In other words, sometimes we see are able to visualize a form of the equation, and sometimes we are not. Gibson has said that, "The necessary condition for pattern vision is an *inhomogeneity* of the set of hypothetical rays" (The Visual World, 64). These visualiza-

tions of velocities are vectors, and hypothetically, rays. Gibson refers to types of order, the first being light or dark. Light is a natural type of stimulation, and thus it is a very useful tool for understanding the natural inhomogeneity going on during the event of perception. Perception is given to us in a multi-faceted series of ways of visualizing light. It should be noted that while light is the only substance that reaches the eye, the substance of light travels in a similar way to other forms of energy like mass. These different ways of visualizing light often pop up as concepts in modern physics. For the purposes of this paper, we are more interested in their correlations to the, "*explanation* of experience" (The Visual World, 8), because, "there are laws relating perception to physical stimulation as well as laws relating it to physiological processes" (The Visual World, 8).

With the above and continuing mathematical count of the

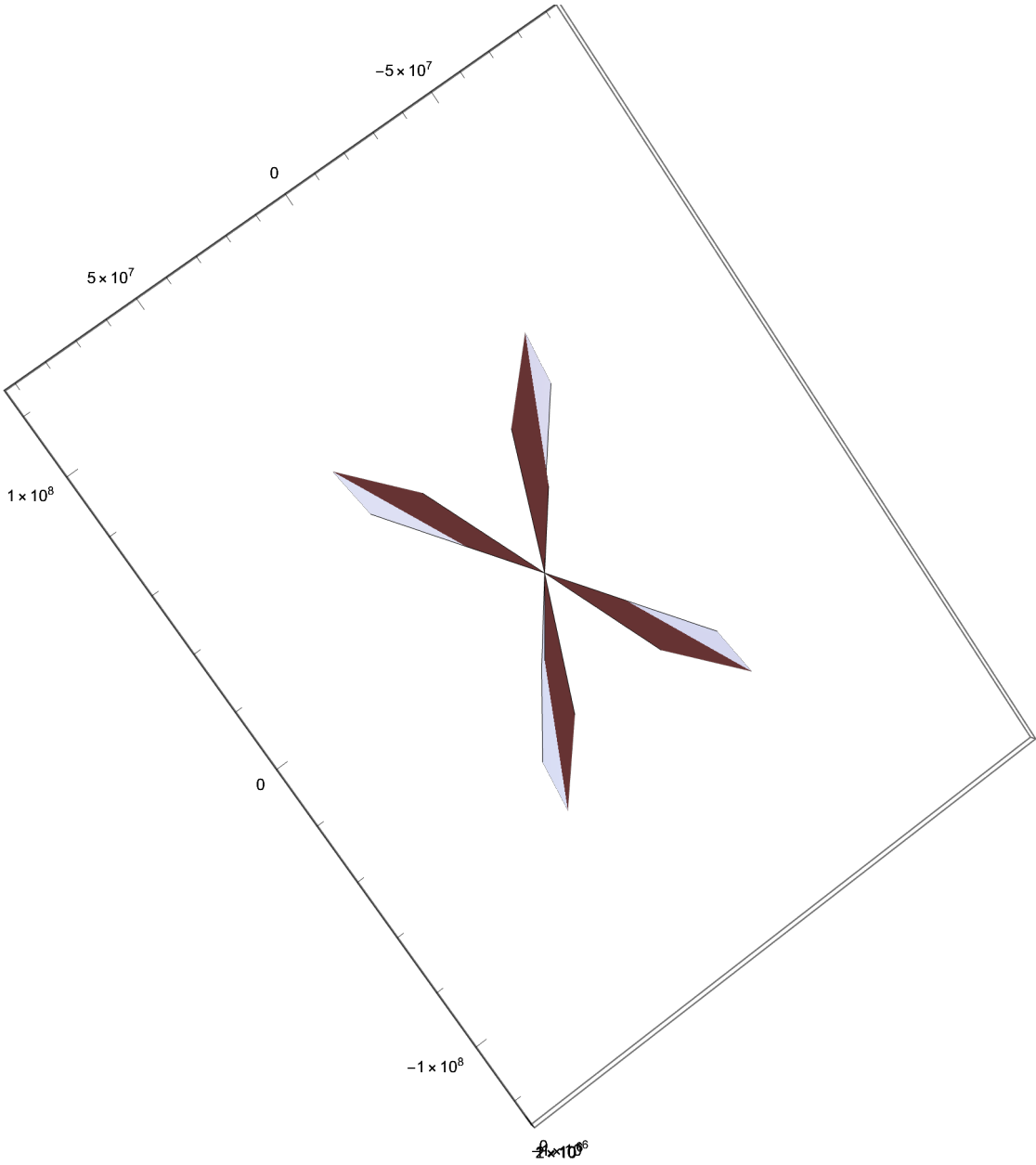
Light travels carrying information only upon reaching the threshold of the event of perception.

```
SphericalPlot3D[
  (

$$\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right) + 8.987551787368176 \cdot 10^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right)^2\right)} / \sqrt{39.47841760435743 - 12.566370614359172 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right) + (\theta)^2},$$

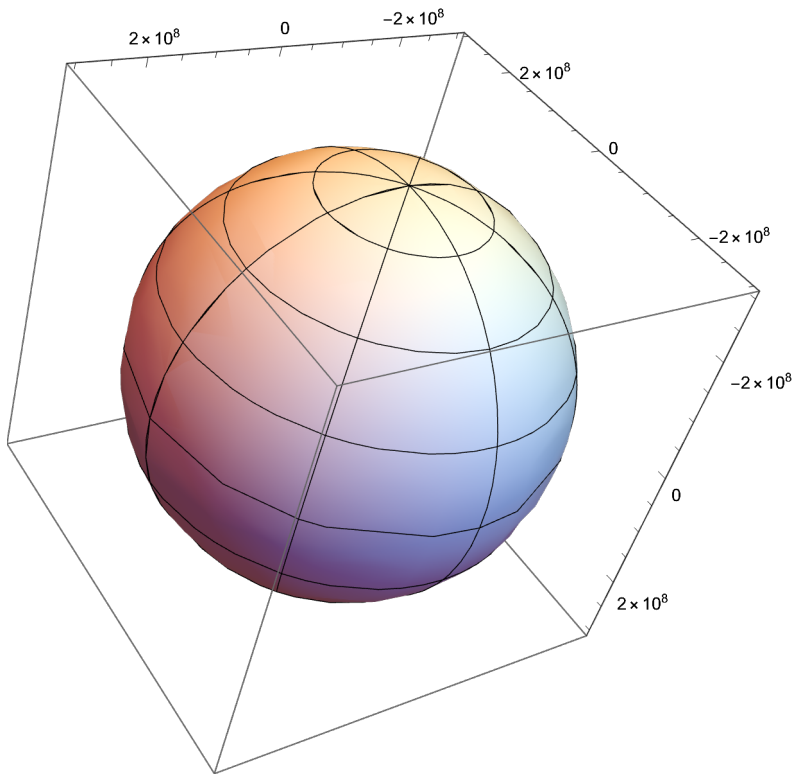
  {\beta, -1.1 \pi, 1.1 \pi}, {\theta, -2.2 \pi, 2.2 \pi}]
```





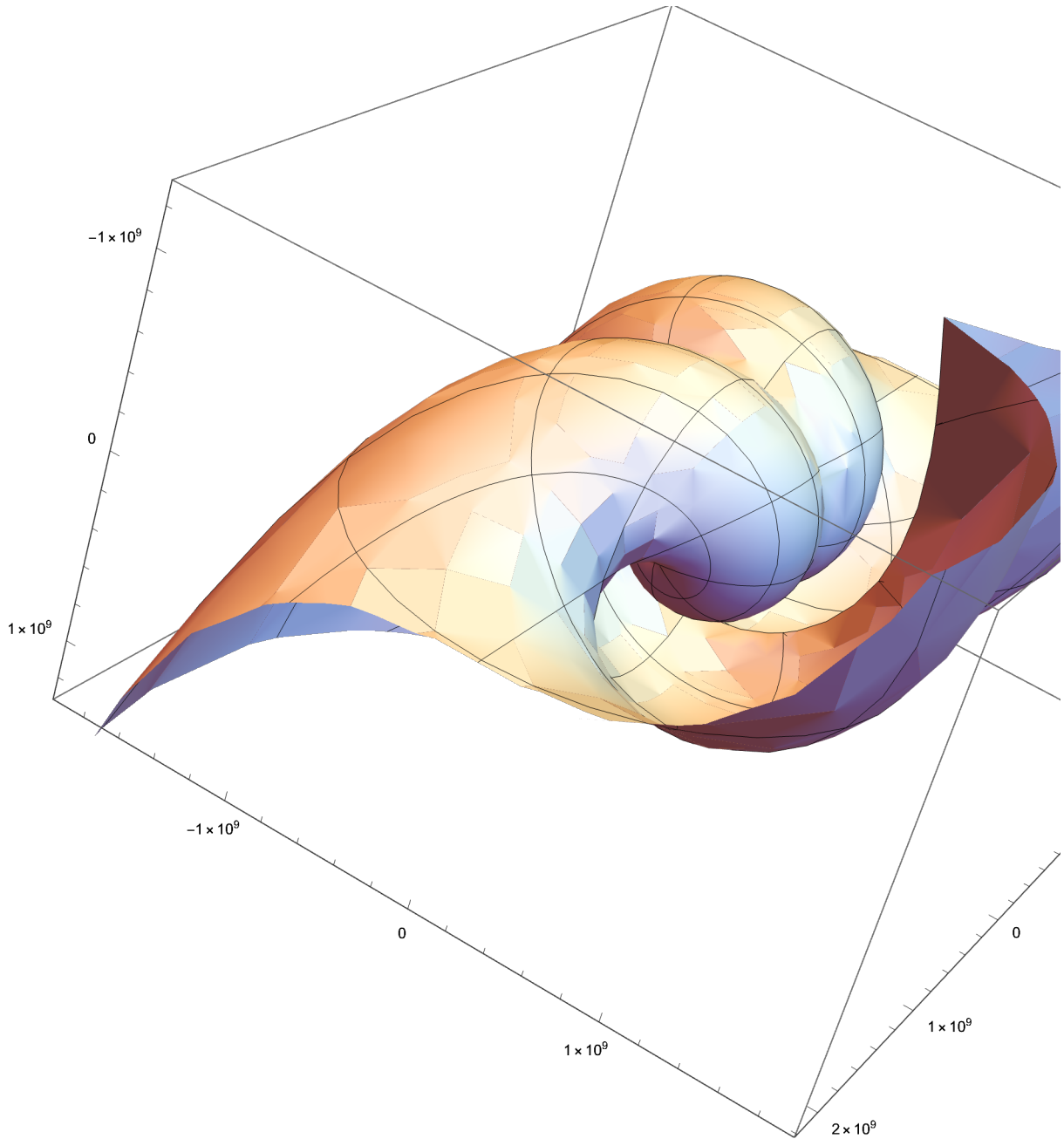
Light/Substance travels like a sphere, or a "particle"

```
SphericalPlot3D[
  (Sqrt[
    (3.5481432270250993`*^18 - 1.1294090667581471`*^18 (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])) +
      8.987551787368176`*^16 (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2]))^2)
  ]) /
  (Sqrt[
    (39.47841760435743` - 12.566370614359172` (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])) +
      (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2]))^2)
  ]), {beta, -pi, pi}, {theta, -2 pi, 2 pi}]
```



Light/Substance travels like a wave.

```
SphericalPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)^2\right)\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right), \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}]$ 
```

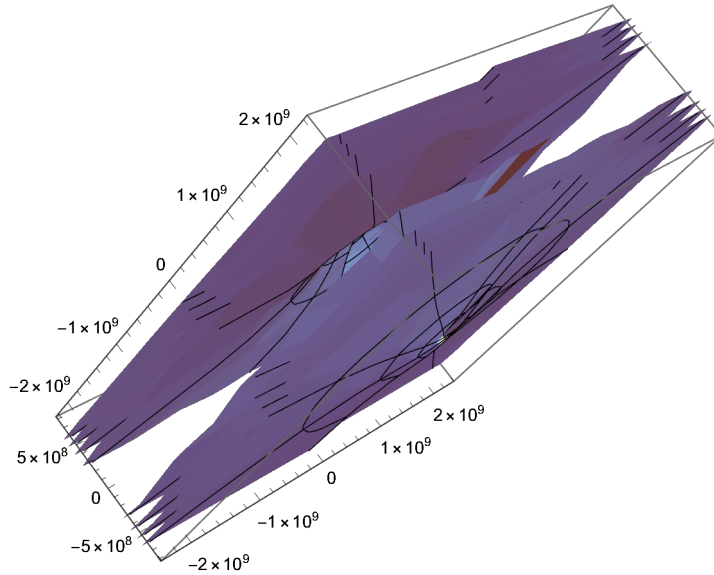


The form of this wave is useful to modeling a contoured surface mathematically, because we can

see a continuous curve that does not have to build the contour out of smaller triangles, but is very smooth and continuously curved.

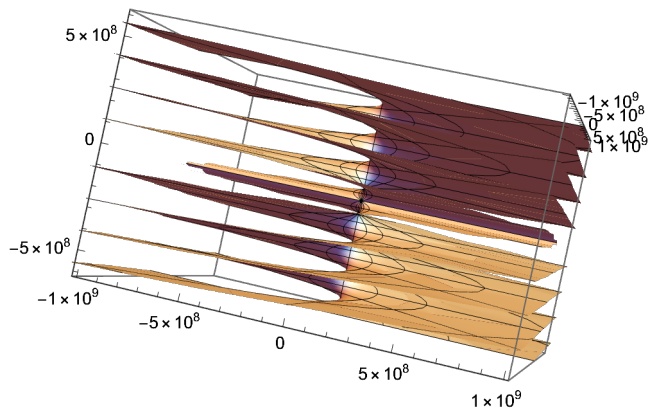
Light/substance travels like a manifold (sheets of paper layered upon one another).

$$\text{SphericalPlot3D}\left[-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{18}-1.1294090667581471\cdot 10^{18}\theta+8.987551787368176\cdot 10^{16}\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^2\right)\right)}\right)/\right. \\ \left.\left(\sqrt{\left(39.47841760435743-12.566370614359172\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)+\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^2\right)\right)}\right)\right],\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$$



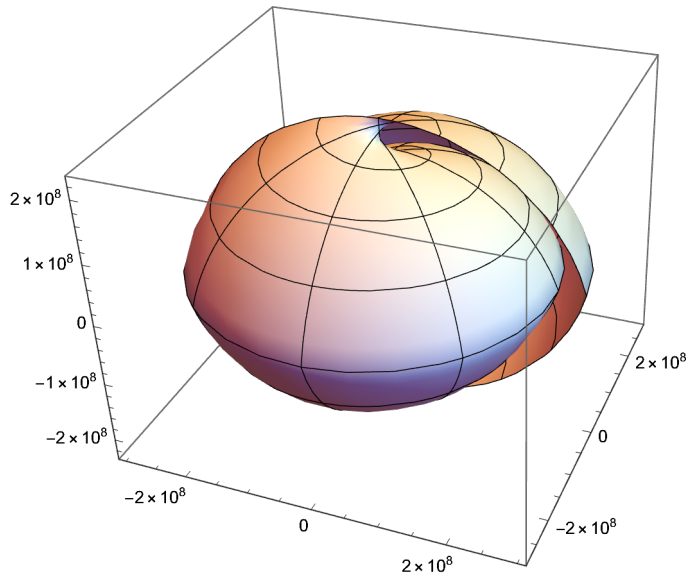
Light/substance travels like a double helix.

$$\text{SphericalPlot3D}\left[-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{-18}-1.1294090667581471\cdot 10^{-18}\theta+8.987551787368176\cdot 10^{-16}\left(\theta\right)^2\right)}\right)/\right. \\ \left.\left(\sqrt{\left(39.47841760435743-12.566370614359172\left(2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\beta\right]^2}\right)\right)+\left(2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}\left[\beta\right]^2}\right)\right)^2\right)}\right)\right),\left\{\beta,-\pi,\pi\right\},\left\{\theta,-2\pi,2\pi\right\}\right]$$



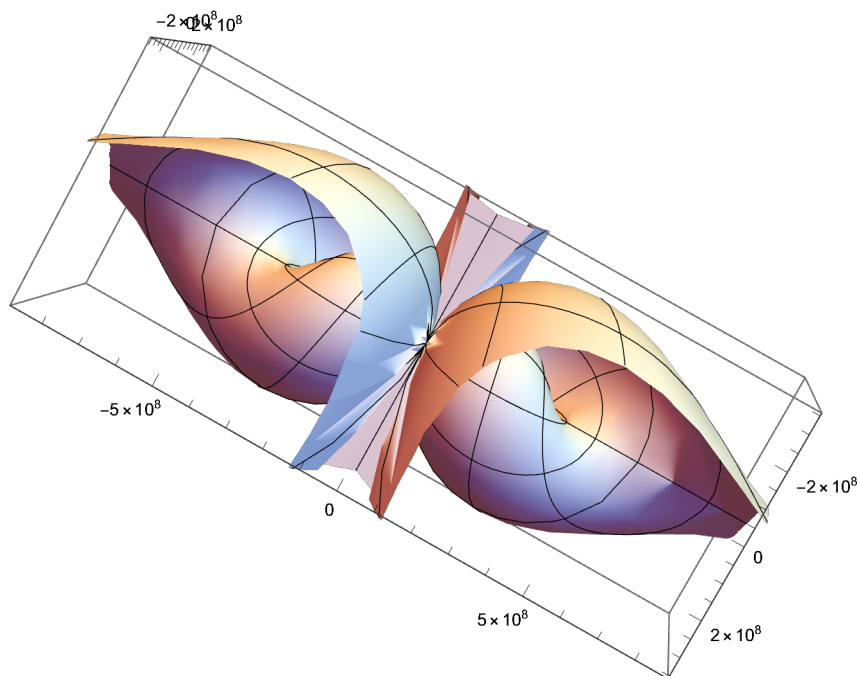
Light/substance travels in a conch - like shape.

SphericalPlot3D $\left[-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{18}-1.1294090667581471\cdot 10^{18}\theta+8.987551787368176\cdot 10^{16}\left(\theta\right)^2\right)}\right)/\left(\sqrt{39.47841760435743-12.566370614359172\left(\theta\right)+\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin^2[\beta]}\right)\right)^2}\right),\{\beta,-\pi,\pi\},\{\theta,-2\pi,2\pi\}\right]$



Light travels in a tulip shape, representational and symbolic of particle - wave duality.

SphericalPlot3D[ $-1. \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + 8.987551787368176 \cdot 10^{16} \left(\left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right), \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$



## VII. The Flow of Light through an Ambient Array (The Array Is within Each Point of the Ecologically Visual Field)

There are non - relativistic solutions to the height of the cone that include the Lorentz Transformations. This is because in the normal course of primal sketching, a visual system detects the edge of a circle and relates it to the distance away from which the observer is. The size of the primal sketching is dependent upon the measurement made by the eye relativistically, however, when determining a change between sizes, the Lorentz factor will cancel. For this section, the visualizations are very complex if we want to see all the different possible nested equations. We will refer the reader to the fourth

addendum to this paper for further visualizations.

We can formulate the non - relativistic equation for the height of the cone in terms of the speed of light of non - relativistic time :

$$\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == c (\theta / (2\pi)) \quad (173)$$

This will give us introspection into the meaning of relativity's relation of the consciously perceptual system to the visual system and if the visual system has evolved with a response to relativistic principles. We will be able to visualize the ambient optic array and the inhomogeneities within it.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == c (\theta / (2\pi)), v\right]$$

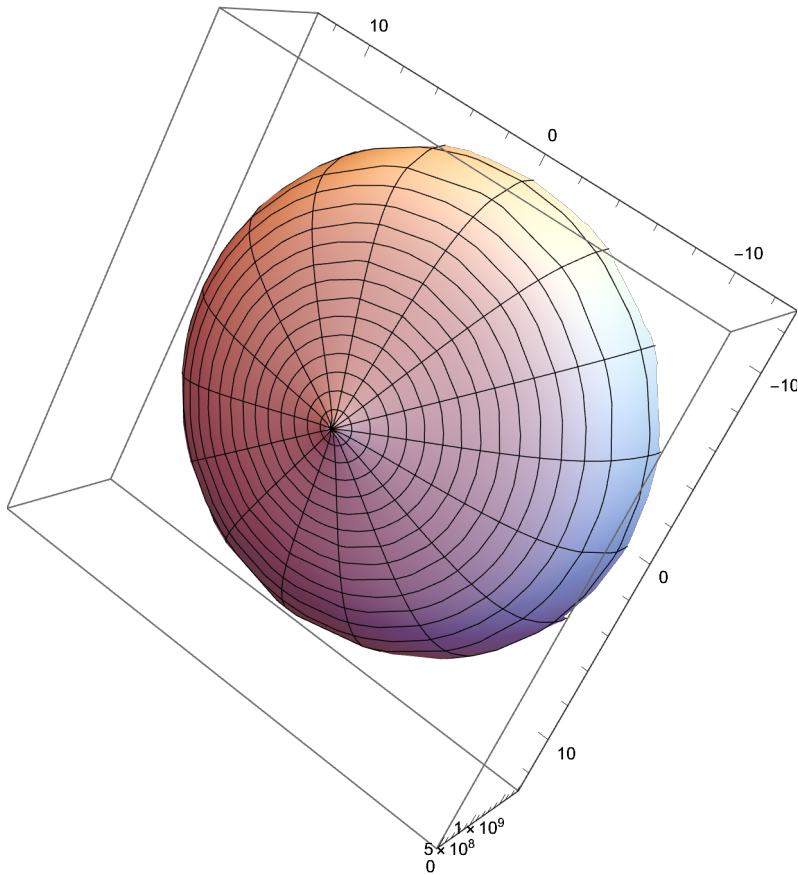
{ }

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} == c (\theta / (2\pi)), r\right]$$

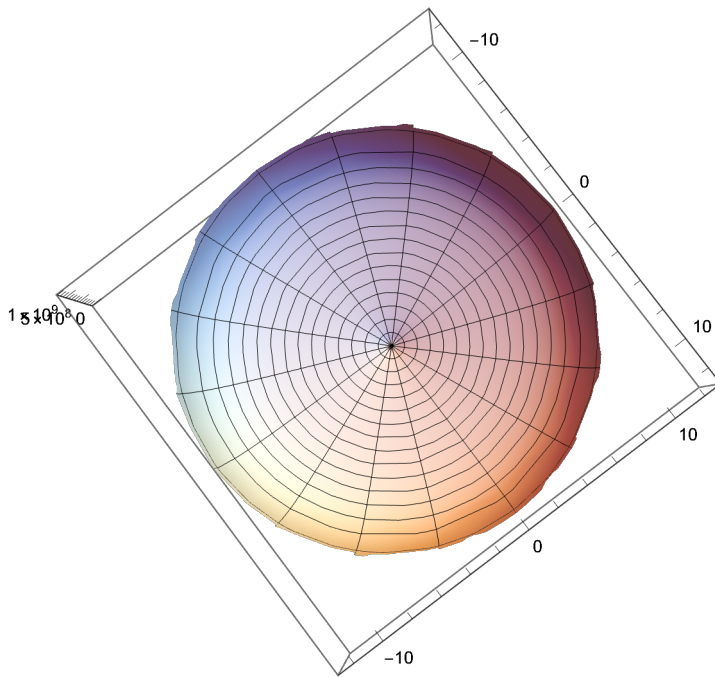
$$\left\{ \left\{ r \rightarrow -\frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right\}, \left\{ r \rightarrow \frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right\} \right\}$$



RevolutionPlot3D $\left[\frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}, \{\theta, -4 \pi, 4 \pi\}\right]$



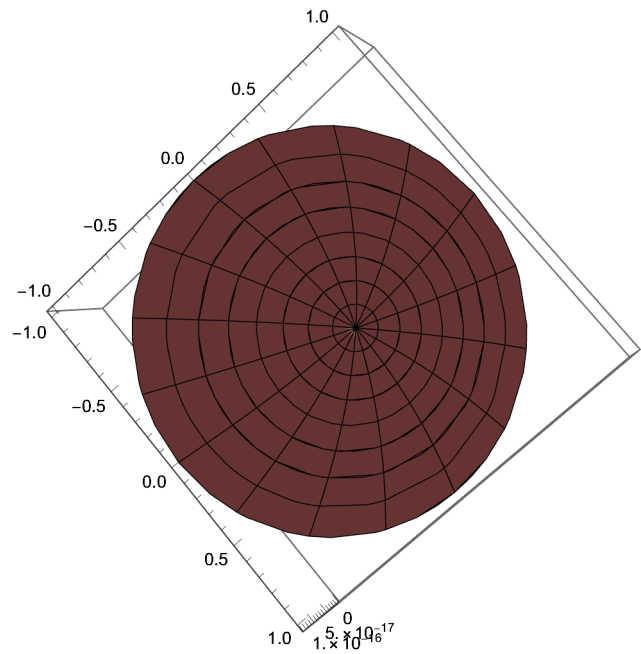
This is an example of inhomogeneity within the ambient optic array. From one side of the expression for radius in terms of the speed of light and time, we see that there is a solid surface, but on the other side, the middle of the bowl is overcome by white saturation. Granted, these are not the proper form of the equation, because they are non-relativistic, but we will soon get a look at some of the relativistic interpretations of information within the light.



$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == c (\theta / (2 \pi)), \theta\right]$$

$$\left\{\{\theta \rightarrow 0\}, \left\{\theta \rightarrow \frac{4 \pi r^2}{c^2 + r^2}\right\}\right\}$$

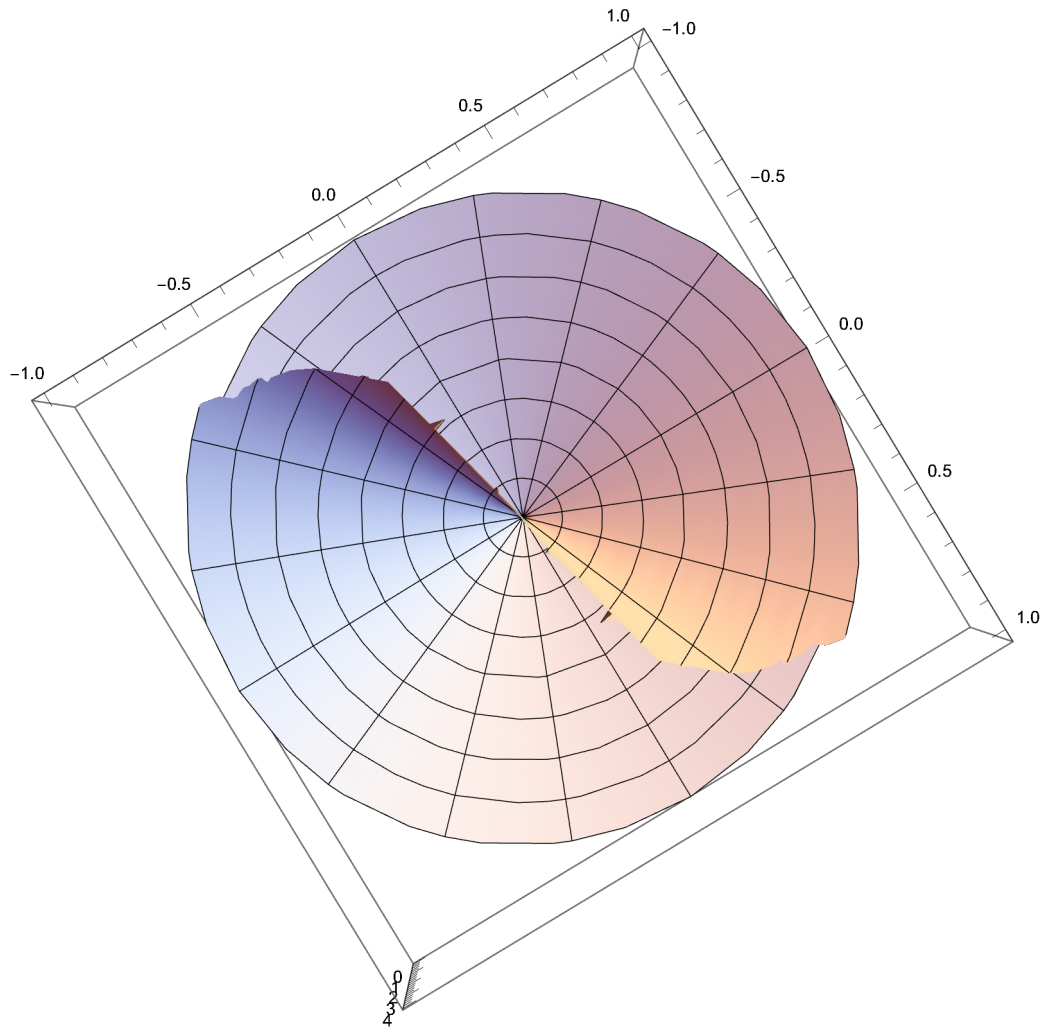
RevolutionPlot3D[ $\frac{4 \pi r^2}{c^2 + r^2}$ , {r, -1, 1}]



Solve[
$$\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == c (\theta / (2 \pi)), c]$$

$$\left\{ \left\{ c \rightarrow -\frac{\sqrt{4 \pi r^2 - r^2 \theta}}{\sqrt{\theta}} \right\}, \left\{ c \rightarrow \frac{\sqrt{4 \pi r^2 - r^2 \theta}}{\sqrt{\theta}} \right\} \right\}$$

RevolutionPlot3D $\left[\frac{\sqrt{4 \pi r^2 - r^2 \theta}}{\sqrt{\theta}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



We can formulate the relativistic equation for the height of the cone in terms of the speed of light of relativistic time :

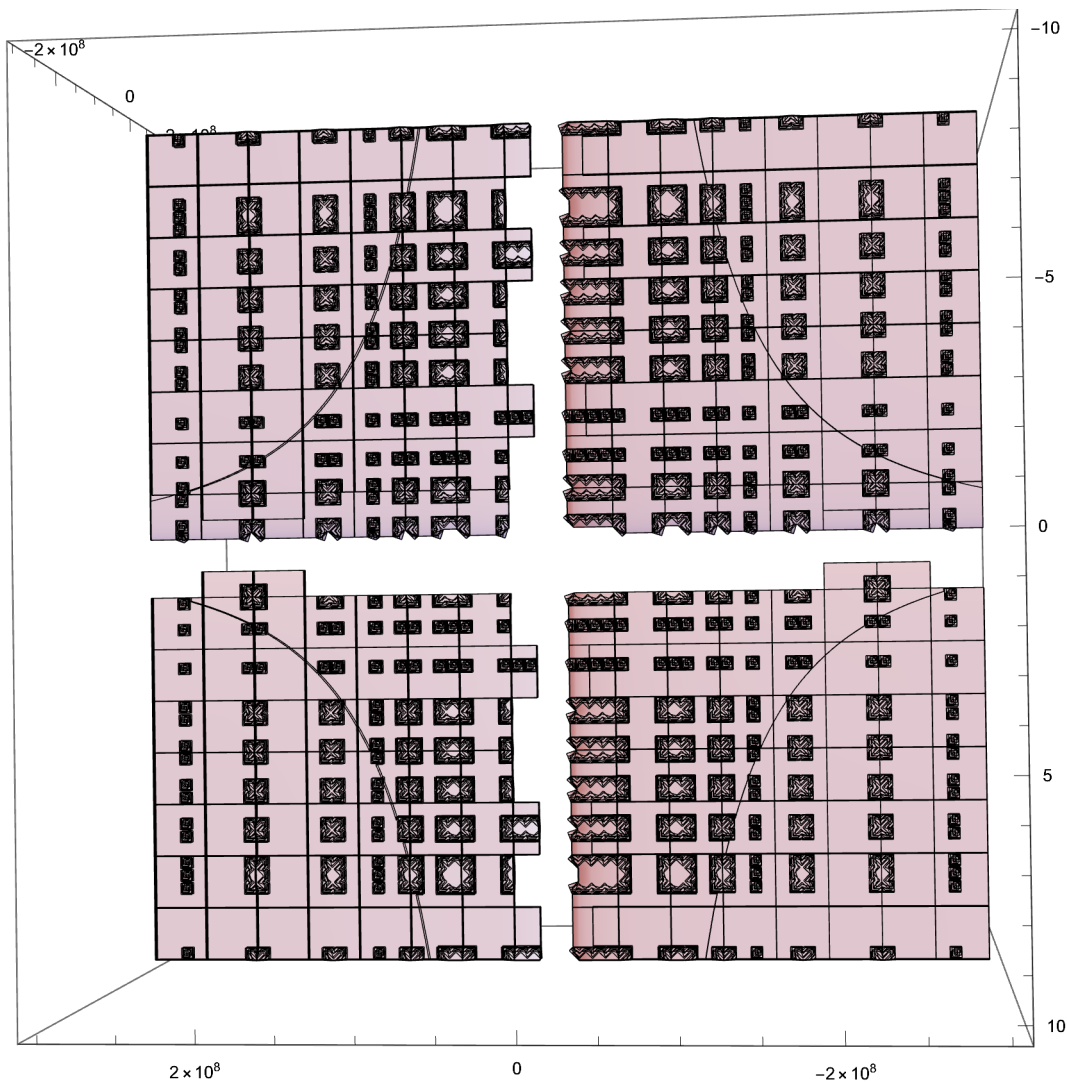
$$\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{v^2}{c^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} = c \left( (\theta / (2 \pi)) / \sqrt{1 - \frac{v^2}{c^2}} \right) \quad (174)$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{v^2}{c^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \sqrt{1 - \frac{v^2}{c^2}} = c \left( (\theta / (2 \pi)) / \sqrt{1 - \frac{v^2}{c^2}} \right), \theta\right]$$

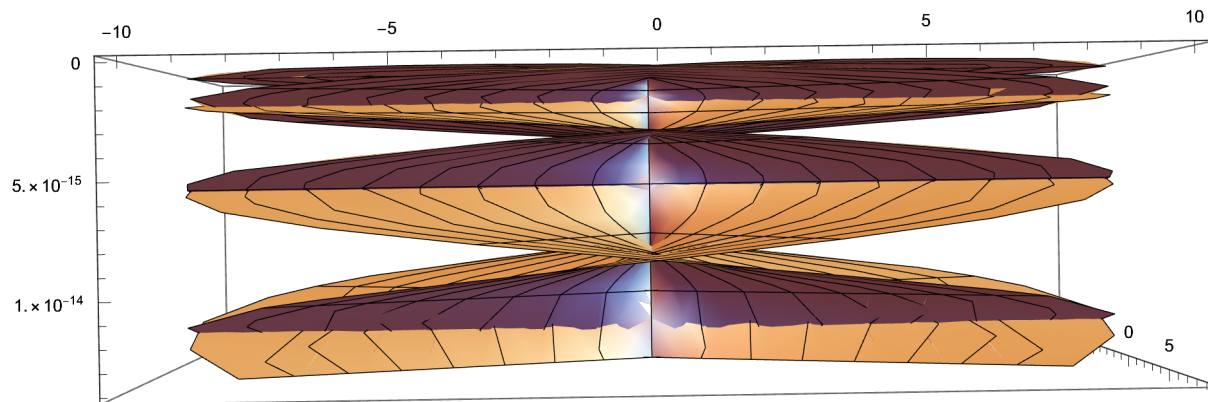
$$\left\{ \{\theta \rightarrow 0\}, \left\{ \theta \rightarrow \frac{4 \pi (c^4 r^2 - 2 c^2 r^2 v^2 + r^2 v^4)}{c^6 + c^4 r^2 - 2 c^2 r^2 v^2 + r^2 v^4} \right\} \right\}$$

Time is visualized from contour to be a gradient of texture. We can also visualize the layout when we know that light travels at a fairly constant speed through substances like air. However, when we consider it to be a variable, which it truly is, we can see how there is information contained within time's relation to the velocity of a perceiver, the speed of light being perceived, and the initial radius of the circle transforming into a cone, which is the wavelength of light.

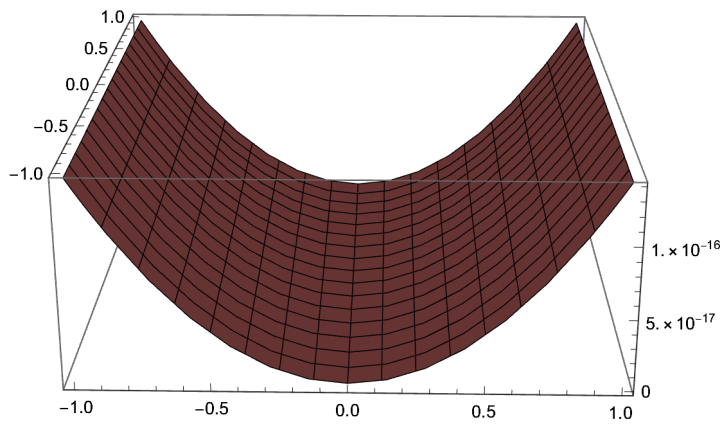
```
ContourPlot3D[ $\frac{4 \pi (c^4 r^2 - 2 c^2 r^2 v^2 + r^2 v^4)}{c^6 + c^4 r^2 - 2 c^2 r^2 v^2 + r^2 v^4}$ ,
  {r, -10, 10}, {v, -(2.99792458 * 10^8), (2.99792458 * 10^8)},
  {c, -(2.99792458 * 10^8), (2.99792458 * 10^8)}]
```



$\text{RevolutionPlot3D}\left[\frac{4\pi(c^4 r^2 - 2c^2 r^2 v^2 + r^2 v^4)}{c^6 + c^4 r^2 - 2c^2 r^2 v^2 + r^2 v^4}, \{v, -10, 10\}, \{r, -10, 10\}\right]$



$\text{Plot3D}\left[\frac{4\pi(c^4 r^2 - 2c^2 r^2 v^2 + r^2 v^4)}{c^6 + c^4 r^2 - 2c^2 r^2 v^2 + r^2 v^4}, \{r, -1, 1\}, \{v, -1, 1\}\right]$



$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta} \sqrt{1 - \frac{v^2}{c^2}} == c \left( \theta / (2\pi) \right) / \sqrt{1 - \frac{v^2}{c^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2 + r^2\theta}} \right\}, \right.$$

$$\left\{ v \rightarrow \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2 + r^2\theta}} \right\},$$

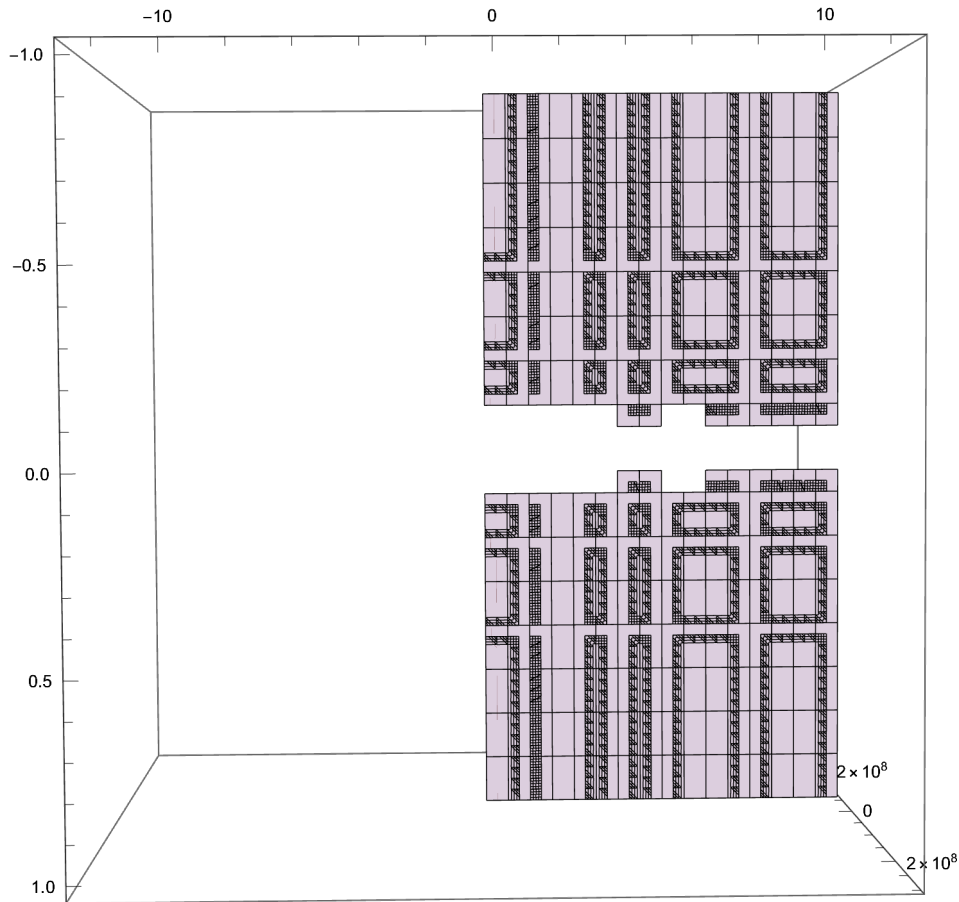
$$\left\{ v \rightarrow -\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right\},$$

$$\left\{ v \rightarrow \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right\}$$

$$\{c, -(2.99792458 * 10^8), (2.99792458 * 10^8)\},$$

$$v := (2.99792458 * 10^8)$$

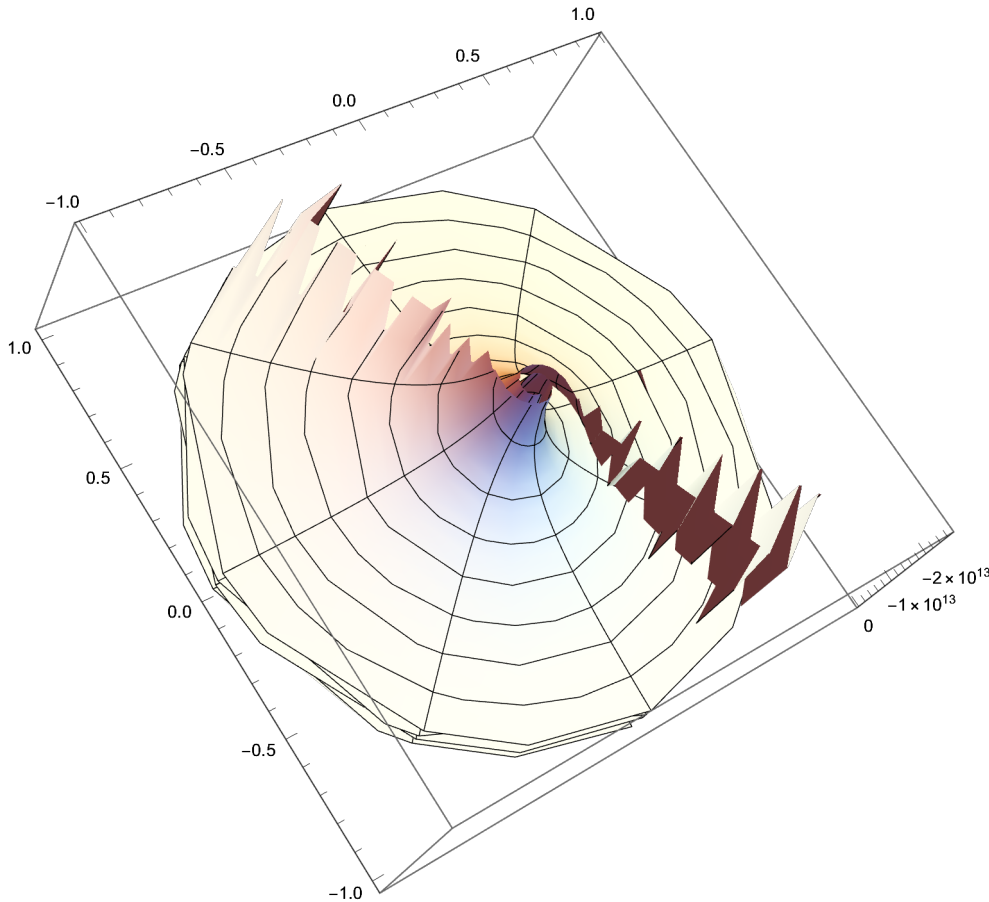
$\text{ContourPlot3D}\left[\left\{\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2+r^2\theta}+\frac{c^2r^2\theta}{-4\pi r^2+r^2\theta}-\frac{\sqrt{c^6r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}},\right.\right.$   
 $\left.-\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2+r^2\theta}+\frac{c^2r^2\theta}{-4\pi r^2+r^2\theta}-\frac{\sqrt{c^6r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}\right\},\{r,-1,1\},$   
 $\{\theta,-4\pi,4\pi\},\{c,-(2.99792458*10^8),(2.99792458*10^8)\}\right]$





RevolutionPlot3D[

$$-\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2+r^2\theta}+\frac{c^2r^2\theta}{-4\pi r^2+r^2\theta}-\frac{\sqrt{c^6r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$



$$\text{Solve}\left[\frac{\sqrt{r}\sqrt{1-\frac{v^2}{c^2}}}{2\pi}\sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{c^2}}}}\sqrt{4\pi r-r\theta}\sqrt{1-\frac{v^2}{c^2}}==c\left(\frac{\theta}{(2\pi)}\right)/\sqrt{1-\frac{v^2}{c^2}}\right], c]$$

$$\left\{\left\{c\rightarrow\right.\right.$$

$$-\sqrt{\left(-\frac{r^2}{3}+\frac{4\pi r^2}{3\theta}-(8\times 2^{1/3}\pi r^4)\right)/\left(3\left(128\pi^3r^6-96\pi^2r^6\theta-288\pi^2r^4v^2\theta+24\pi r^6\theta^2+144\right.\right.$$

$$\left.\left.\pi r^4v^2\theta^2+108\pi r^2v^4\theta^2-2r^6\theta^3-18r^4v^2\theta^3-27r^2v^4\theta^3+3\sqrt{3}\sqrt{(-256\pi^3r^6v^6\theta^3+192\pi^2r^6v^6\theta^4+432\pi^2r^4v^8\theta^4-48\pi r^6v^6\theta^5-216\pi r^4v^8\theta^5+4r^6v^6\theta^6+27r^4v^8\theta^6)}^{1/3}\right)-(8\times 2^{1/3}\pi r^2v^2)\right)/$$

$$\left((128\pi^3r^6-96\pi^2r^6\theta-288\pi^2r^4v^2\theta+24\pi r^6\theta^2+144\pi r^4v^2\theta^2+108\pi r^2v^4\theta^2-2r^6\theta^3-18r^4v^2\theta^3-27r^2v^4\theta^3+3\sqrt{3}\sqrt{(-256\pi^3r^6v^6\theta^3+192\pi^2r^6v^6\theta^4+432\pi^2r^4v^8\theta^4-48\pi r^6v^6\theta^5-216\pi r^4v^8\theta^5+4r^6v^6\theta^6+27r^4v^8\theta^6)}^{1/3}\right)}$$

$$\begin{aligned}
& \left. \left( 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6 \right) \right)^{1/3} + \\
& \left( 16 \times 2^{1/3} \pi^2 r^4 \right) / \left( 3 \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& \quad \left. 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \Big) + (2^{1/3} r^4 \theta) / \\
& \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& \quad \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \Big) + \\
& \left( 2 \times 2^{1/3} r^2 v^2 \theta \right) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& \quad \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} + \\
& \frac{1}{3 \times 2^{1/3} \theta} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& \quad \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \Big) \Big\}, \\
& \left\{ c \rightarrow \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} - (8 \times 2^{1/3} \pi r^4) / \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + \right. \right. \right. \right. \\
& \quad 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - \\
& \quad 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& \quad \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \Big) - \\
& \left( 8 \times 2^{1/3} \pi r^2 v^2 \right) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \\
& \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} + \\
& \left( 16 \times 2^{1/3} \pi^2 r^4 \right) / \left( 3 \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& \quad \left. 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \Big) + (2^{1/3} r^4 \theta) / \\
& \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right.
\end{aligned}$$

$$\begin{aligned} & 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right.} \\ & \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \\ & \left(2 \times 2^{1/3} r^2 v^2 \theta\right) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\ & 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\ & 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right.} \\ & \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \\ & \frac{1}{3 \times 2^{1/3} \theta} \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\ & 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\ & 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right.} \\ & \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} \Bigg\}, \\ \{c \rightarrow & -\sqrt{\left(-\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + \left(4 \times 2^{1/3} \pi r^4\right) / \left(3 \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + \right. \right. \right.} \\ & 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\ & 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \right.} \\ & \left. 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} - \left(4 \times 2^{1/3} \pi r^4\right) / \\ & \left(\sqrt{3} \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\ & 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right.} \\ & \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \\ & \left. \left(4 \times 2^{1/3} \pi r^2 v^2\right) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\ & 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\ & 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right.} \\ & \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} - \\ & \left. \left(4 \times 2^{1/3} \sqrt{3} \pi r^2 v^2\right) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\ & 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\ & 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \right.} \\ & \left. 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} - \left(8 \times 2^{1/3} \pi^2 r^4\right) / \\ & \left. \left(3 \theta \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \right. \\ & 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right.} \\ & \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \\ & \left. \left(8 \times 2^{1/3} \pi^2 r^4\right) / \left(\sqrt{3} \theta \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
& 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) - \\
& (r^4 \theta) \Big/ \Big( 3 \times 2^{2/3} \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \\
& 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) + \\
& (i r^4 \theta) \Big/ \Big( 2^{2/3} \sqrt{3} \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \\
& 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) - (2^{1/3} r^2 v^2 \theta) \Big/ \\
& \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \\
& 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) + \\
& (i 2^{1/3} \sqrt{3} r^2 v^2 \theta) \Big/ \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \\
& 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) - \\
& \frac{1}{6 \times 2^{1/3} \theta} \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \\
& 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} - \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta} \\
& i \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \\
& 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) \Big) \Big\}, \\
& \left\{ c \rightarrow \sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4) \Big/ \left( 3 \Big( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + \right. \right. \right. \\
& 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)}^{1/3} \Big) - (4 i 2^{1/3} \pi r^4) \Big/
\end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad \left. \left. 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right. \right. \\
& \quad \left. \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) + \\
& (4 \times 2^{1/3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right. \right. \\
& \quad \left. \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} - \\
& (4 \imath 2^{1/3} \sqrt{3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \right. \right. \\
& \quad \left. \left. \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} - (8 \times 2^{1/3} \pi^2 r^4) / \\
& \left( 3 \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad \left. \left. 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right. \right. \\
& \quad \left. \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) + \\
& (8 \imath 2^{1/3} \pi^2 r^4) / \left( \sqrt{3} \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) - \\
& (r^4 \theta) / \left( 3 \times 2^{2/3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) + \\
& (\imath r^4 \theta) / \left( 2^{2/3} \sqrt{3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} \right) - \\
& (2^{1/3} r^2 v^2 \theta) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad \left. 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right. \right. \\
& \quad \left. \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \right)^{1/3} +
\end{aligned}$$

$$\begin{aligned}
& \left( i 2^{1/3} \sqrt{3} r^2 v^2 \theta \right) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \\
& \quad \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} - \\
& \quad \frac{1}{6 \times 2^{1/3} \theta} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \\
& \quad \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} - \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta} \\
& \quad i \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \\
& \quad 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& \quad 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} \Big) \Big\}, \\
& \left\{ c \rightarrow -\sqrt{\left( -\frac{r^2}{3} + \frac{4 \pi r^2}{3 \theta} + (4 \times 2^{1/3} \pi r^4) \right) / \left( 3 \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + \right. \right. \right. \\
& \quad 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& \quad 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} \Big) + (4 i 2^{1/3} \pi r^4) / \\
& \quad \left( \sqrt{3} \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& \quad 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} \Big) + \\
& \quad (4 \times 2^{1/3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \\
& \quad 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} + \\
& \quad (4 i 2^{1/3} \sqrt{3} \pi r^2 v^2) / \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
& \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
& \quad 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - \\
& \quad 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} - (8 \times 2^{1/3} \pi^2 r^4) / \\
& \quad \left( 3 \theta \left( 128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \\
& \quad 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \\
& \quad 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6)} \Big)^{1/3} \Big) -
\end{aligned}$$

$$\begin{aligned}
& \left( 8 \, i \, 2^{1/3} \, \pi^2 \, r^4 \right) / \left( \sqrt{3} \, \theta \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + \right. \right. \\
& \quad 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + \\
& \quad 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - \\
& \quad \left. 48 \, \pi \, r^6 \, v^6 \, \theta^5 - 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} \Big) - \\
& \left( r^4 \, \theta \right) / \left( 3 \times 2^{2/3} \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + \right. \right. \\
& \quad 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + \\
& \quad 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - \\
& \quad \left. 48 \, \pi \, r^6 \, v^6 \, \theta^5 - 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} \Big) - \\
& \left( i \, r^4 \, \theta \right) / \left( 2^{2/3} \, \sqrt{3} \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + \right. \right. \\
& \quad 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + \\
& \quad 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - \\
& \quad \left. 48 \, \pi \, r^6 \, v^6 \, \theta^5 - 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} \Big) - \\
& \left( 2^{1/3} \, r^2 \, v^2 \, \theta \right) / \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + \right. \\
& \quad 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + \\
& \quad 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - \\
& \quad \left. 48 \, \pi \, r^6 \, v^6 \, \theta^5 - 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} - \\
& \left( i \, 2^{1/3} \, \sqrt{3} \, r^2 \, v^2 \, \theta \right) / \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + \right. \\
& \quad 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + \\
& \quad 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - \\
& \quad \left. 48 \, \pi \, r^6 \, v^6 \, \theta^5 - 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} - \\
& \frac{1}{6 \times 2^{1/3} \, \theta} \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + 144 \, \pi \, r^4 \, v^2 \, \theta^2 + \right. \\
& \quad 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + \\
& \quad 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - 48 \, \pi \, r^6 \, v^6 \, \theta^5 - \\
& \quad \left. 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} + \frac{1}{2 \times 2^{1/3} \, \sqrt{3} \, \theta} \\
& i \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + 24 \, \pi \, r^6 \, \theta^2 + 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - \right. \\
& \quad 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - 27 \, r^2 \, v^4 \, \theta^3 + 3 \, \sqrt{3} \, \sqrt{(-256 \, \pi^3 \, r^6 \, v^6 \, \theta^3 + 192 \, \pi^2 \, r^6 \, v^6 \, \theta^4 + \\
& \quad \left. 432 \, \pi^2 \, r^4 \, v^8 \, \theta^4 - 48 \, \pi \, r^6 \, v^6 \, \theta^5 - 216 \, \pi \, r^4 \, v^8 \, \theta^5 + 4 \, r^6 \, v^6 \, \theta^6 + 27 \, r^4 \, v^8 \, \theta^6)} \right)^{1/3} \Big) \Big\}, \\
& \left\{ c \rightarrow \sqrt{\left( -\frac{r^2}{3} + \frac{4 \, \pi \, r^2}{3 \, \theta} + \left( 4 \times 2^{1/3} \, \pi \, r^4 \right) / \left( 3 \left( 128 \, \pi^3 \, r^6 - 96 \, \pi^2 \, r^6 \, \theta - 288 \, \pi^2 \, r^4 \, v^2 \, \theta + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 24 \, \pi \, r^6 \, \theta^2 + 144 \, \pi \, r^4 \, v^2 \, \theta^2 + 108 \, \pi \, r^2 \, v^4 \, \theta^2 - 2 \, r^6 \, \theta^3 - 18 \, r^4 \, v^2 \, \theta^3 - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right.} \\
& \quad \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \\
& (4 \text{ i } 2^{1/3} \pi r^4) / \left(\sqrt{3} \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \right. \\
& \quad \left. (4 \times 2^{1/3} \pi r^2 v^2) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right. \right. \\
& \quad \left. \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} + \right. \\
& \quad \left. (4 \text{ i } 2^{1/3} \sqrt{3} \pi r^2 v^2) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \right. \right. \\
& \quad \left. \left. \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}} - (8 \times 2^{1/3} \pi^2 r^4) / \right. \\
& \quad \left. \left(3 \theta \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - \right. \right. \right. \\
& \quad \left. \left. 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + \right. \right. \right. \\
& \quad \left. \left. 432 \pi^2 r^4 v^8 \theta^4 - 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}}\right) - \\
& (8 \text{ i } 2^{1/3} \pi^2 r^4) / \left(\sqrt{3} \theta \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}}\right) - \\
& (r^4 \theta) / \left(3 \times 2^{2/3} \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}}\right) - \\
& (\text{i } r^4 \theta) / \left(2^{2/3} \sqrt{3} \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \right. \\
& \quad \left. 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right. \right. \\
& \quad \left. \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3}}\right) - \\
& (2^{1/3} r^2 v^2 \theta) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
& \quad \left. 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \right.
\end{aligned}$$

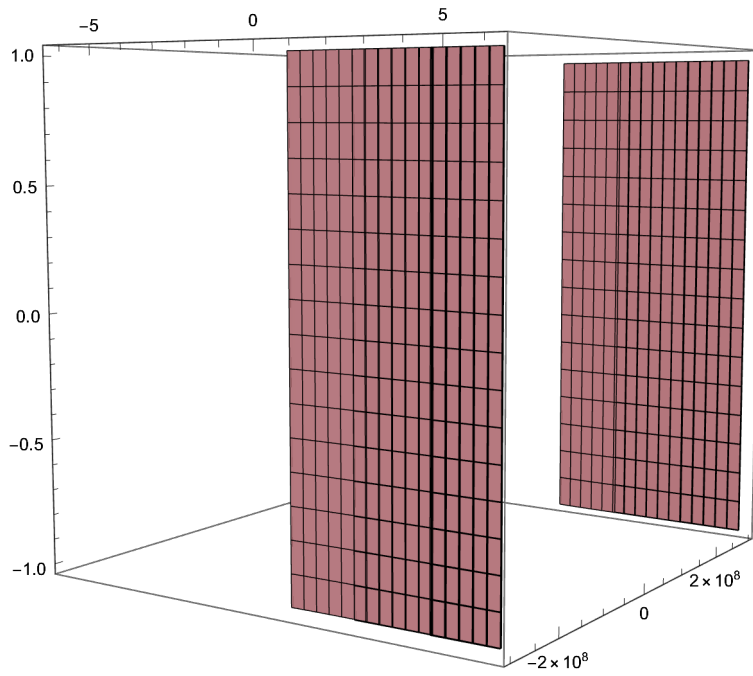


$$\begin{aligned}
 & 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right.} \\
 & \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3} - \\
 & \left(i 2^{1/3} \sqrt{3} r^2 v^2 \theta\right) / \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + \right. \\
 & \quad 144 \pi r^4 v^2 \theta^2 + 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
 & \quad 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right.} \\
 & \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3} - \\
 & \frac{1}{6 \times 2^{1/3} \theta} \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
 & \quad 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
 & \quad 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - 48 \right.} \\
 & \quad \left. \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3} + \\
 & \frac{1}{2 \times 2^{1/3} \sqrt{3} \theta} i \left(128 \pi^3 r^6 - 96 \pi^2 r^6 \theta - 288 \pi^2 r^4 v^2 \theta + 24 \pi r^6 \theta^2 + 144 \pi r^4 v^2 \theta^2 + \right. \\
 & \quad 108 \pi r^2 v^4 \theta^2 - 2 r^6 \theta^3 - 18 r^4 v^2 \theta^3 - 27 r^2 v^4 \theta^3 + \\
 & \quad 3 \sqrt{3} \sqrt{\left(-256 \pi^3 r^6 v^6 \theta^3 + 192 \pi^2 r^6 v^6 \theta^4 + 432 \pi^2 r^4 v^8 \theta^4 - \right.} \\
 & \quad \left. 48 \pi r^6 v^6 \theta^5 - 216 \pi r^4 v^8 \theta^5 + 4 r^6 v^6 \theta^6 + 27 r^4 v^8 \theta^6\right)^{1/3} \Bigg) \Bigg\} \Bigg\}
 \end{aligned}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1-\frac{v^2}{c^2}}}{2 \pi} \sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{c^2}}}} \sqrt{4 \pi r-r \theta} \sqrt{1-\frac{v^2}{c^2}}==c\left(\theta /(2 \pi)\right) / \sqrt{1-\frac{v^2}{c^2}}\right], r]$$

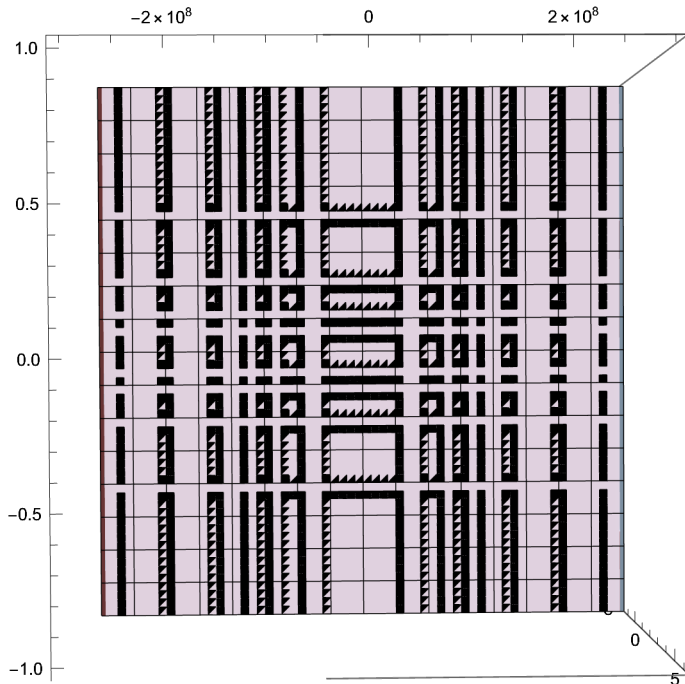
$$\left\{\left\{r \rightarrow-\frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4 \pi+\theta}}\right\},\left\{r \rightarrow \frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4 \pi+\theta}}\right\}\right\}$$

$\text{ContourPlot3D}\left[\frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4\pi+\theta}}, \{\theta, -2\pi, 2\pi\},\right.$   
 $\left.\{v, -(2.99792458 \times 10^8), (2.99792458 \times 10^8)\}, \{r, -1, 1\}\right]$



ContourPlot3D $\left[\left\{-\frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4 \pi+\theta}}, \frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4 \pi+\theta}}\right\},\right.$

$\{\theta,-2 \pi, 2 \pi\},\{v,-\left(2.99792458 \times 10^8\right),\left(2.99792458 \times 10^8\right)\},\{r,-1,1\}]$



During this section of the paper 's main body,  
we will discuss the gradient found when we make a contour plot of the

"We can now define a fourth type of order among the elements of a retinal image. It would be a serial change in the length of the cycles of a repetitive order...If a repetitive order is the stimulus for visual texture, this would constitute a gradient of the density of texture" (The Visual World, 67). I am proposing with the relativistic interpretations of the functions of the height of the cone, that

## VIII. The Height of the Cone Relates to Stimulus Energy in a Room of Constant Illumination

## IX. The Projective Plane per unit of stimulus from velocity of light through the height of the cone.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} \left(\sqrt{1 - \frac{v^2}{c^2}} \theta\right) =\right.$$

$$\left. c \left( \frac{(\theta / (2\pi))}{\sqrt{1 - ((v)^2 / c^2)}} \right), v \right]$$

$$\left\{ \left\{ v \rightarrow -\sqrt{-\frac{4c^2\pi r^2\theta}{-4\pi r^2\theta + r^2\theta^2} + \frac{c^2 r^2\theta^2}{-4\pi r^2\theta + r^2\theta^2} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2\theta + r^2\theta^2}} \right\}, \right.$$

$$\left\{ v \rightarrow \sqrt{-\frac{4c^2\pi r^2\theta}{-4\pi r^2\theta + r^2\theta^2} + \frac{c^2 r^2\theta^2}{-4\pi r^2\theta + r^2\theta^2} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2\theta + r^2\theta^2}} \right\},$$

$$\left\{ v \rightarrow -\sqrt{-\frac{4c^2\pi r^2\theta}{-4\pi r^2\theta + r^2\theta^2} + \frac{c^2 r^2\theta^2}{-4\pi r^2\theta + r^2\theta^2} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2\theta + r^2\theta^2}} \right\},$$

$$\left\{ v \rightarrow \sqrt{-\frac{4c^2\pi r^2\theta}{-4\pi r^2\theta + r^2\theta^2} + \frac{c^2 r^2\theta^2}{-4\pi r^2\theta + r^2\theta^2} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2\theta + r^2\theta^2}} \right\}$$

$$\text{RevolutionPlot3D}\left[ \right.$$

$$\left. -\sqrt{-\frac{4c^2\pi r^2\theta}{-4\pi r^2\theta + r^2\theta^2} + \frac{c^2 r^2\theta^2}{-4\pi r^2\theta + r^2\theta^2} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2\theta + r^2\theta^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} \right]$$

$$\left\{ \left\{ v \rightarrow -0.5 \sqrt{\left( -\left( 2. \left( -1.615521742612498 \cdot 10^{34} + \right. \right. \right. \right.$$

$$\left. \left. \left. 2.2588181335162941 \cdot 10^{18} r^2 \theta - 1.7975103574736352 \cdot 10^{17} r^2 \theta^2 \right) \right) / \right.$$

$$\left( 8.987551787368176 \cdot 10^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) -$$

$$\left. 2. \sqrt{\left( \left( -1.615521742612498 \cdot 10^{34} + 2.2588181335162941 \cdot 10^{18} r^2 \theta - \right. \right. \right.$$

$$\left. \left. \left. 1.7975103574736352 \cdot 10^{17} r^2 \theta^2 \right)^2 / \right. \right.$$

$$\left( 8.987551787368176 \cdot 10^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right)^2 -$$

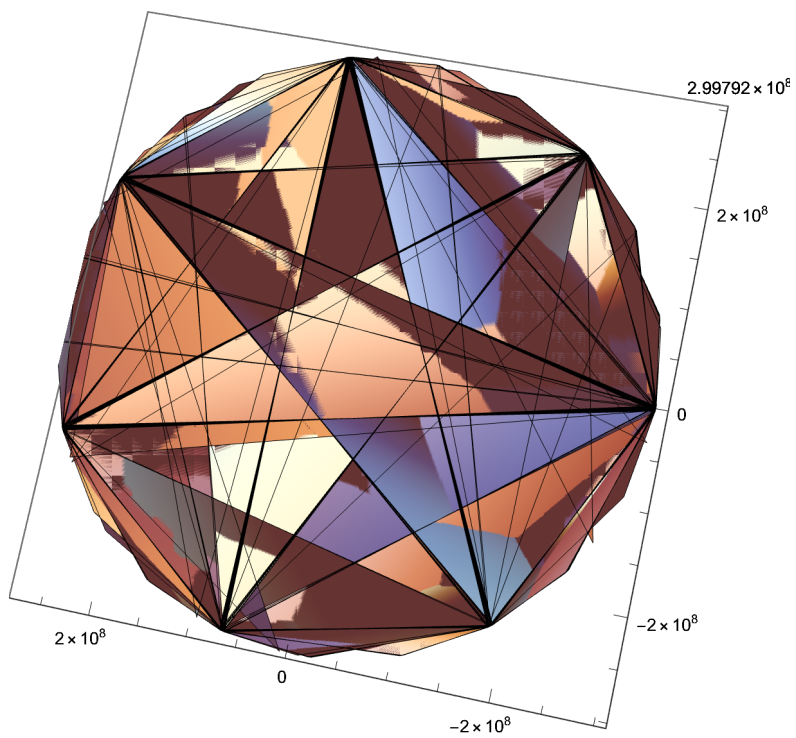
$$\left. \left( 4. \left( 7.2597926626745534 \cdot 10^{50} - 1.015062247661201 \cdot 10^{35} r^2 \theta + \right. \right. \right.$$

$$\left. \left. \left. 8.07760871306249 \cdot 10^{33} r^2 \theta^2 \right) \right) / \right.$$

$$\begin{aligned}
& \left( (8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2) \right) \Bigg\}, \\
& \left\{ v \rightarrow 0.5 \cdot \sqrt{ \left( - \left( 2 \cdot \left( -1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} r^2 \theta - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \cdot r^{17} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) - \\
& \quad \left. 2 \cdot \sqrt{ \left( \left( -1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} r^2 \theta - \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \cdot r^{17} r^2 \theta^2 \right)^2 / \right. \right. \\
& \quad \left. \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right)^2 - \right. \\
& \quad \left. \left( 4 \cdot \left( 7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} r^2 \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.07760871306249 \cdot r^{33} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left. \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) \right) \Bigg\}, \\
& \left\{ v \rightarrow -0.5 \cdot \sqrt{ \left( - \left( 2 \cdot \left( -1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} r^2 \theta - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \cdot r^{17} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) + \\
& \quad \left. 2 \cdot \sqrt{ \left( \left( -1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} r^2 \theta - \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \cdot r^{17} r^2 \theta^2 \right)^2 / \right. \right. \\
& \quad \left. \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right)^2 - \right. \\
& \quad \left. \left( 4 \cdot \left( 7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} r^2 \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.07760871306249 \cdot r^{33} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left. \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) \right) \Bigg\}, \\
& \left\{ v \rightarrow 0.5 \cdot \sqrt{ \left( - \left( 2 \cdot \left( -1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} r^2 \theta - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \cdot r^{17} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) + \\
& \quad \left. 2 \cdot \sqrt{ \left( \left( -1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} r^2 \theta - \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \cdot r^{17} r^2 \theta^2 \right)^2 / \right. \right. \\
& \quad \left. \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right)^2 - \right. \\
& \quad \left. \left( 4 \cdot \left( 7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} r^2 \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.07760871306249 \cdot r^{33} r^2 \theta^2 \right) \right) / \right. \\
& \quad \left. \left( 8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2 \right) \right) \Bigg\} \Bigg\}
\end{aligned}$$

```

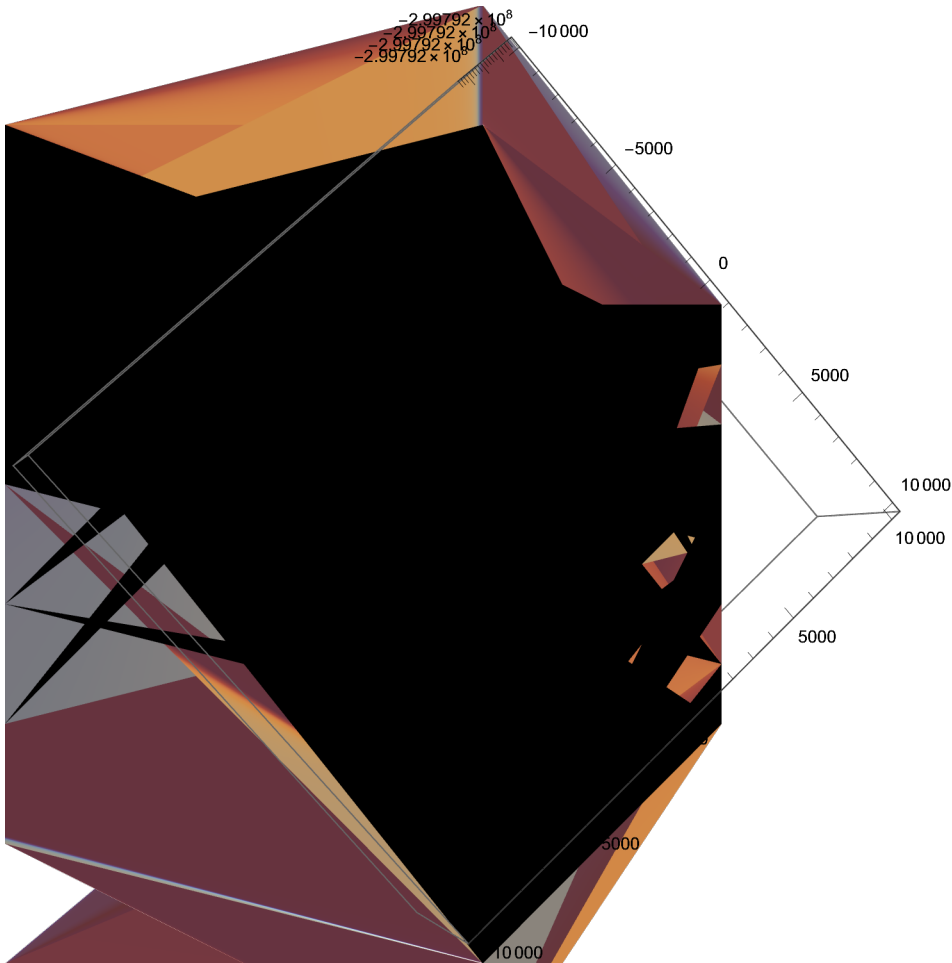
RevolutionPlot3D[
{
  (-0.5` $\sqrt{-\left(2.\left(-1.615521742612498`^{34}+2.2588181335162941`^{18}r^2\theta-1.7975103574736352`^{17}r^2\theta^2\right)\right) / \left(8.987551787368176`^{16}-12.566370614359172`r^2\theta+r^2\theta^2\right)+2.\sqrt{\left(-1.615521742612498`^{34}+2.2588181335162941`^{18}r^2\theta-1.7975103574736352`^{17}r^2\theta^2\right)^2 / \left(8.987551787368176`^{16}-12.566370614359172`r^2\theta+r^2\theta^2\right)^2-\left(4.\left(7.2597926626745534`^{50}-1.015062247661201`^{35}r^2\theta+8.07760871306249`^{33}r^2\theta^2\right)\right) / \left(8.987551787368176`^{16}-12.566370614359172`r^2\theta+r^2\theta^2\right)\right)\right)},
  (0.5` $\sqrt{-\left(2.\left(-1.615521742612498`^{34}+2.2588181335162941`^{18}r^2\theta-1.7975103574736352`^{17}r^2\theta^2\right)\right) / \left(8.987551787368176`^{16}-12.566370614359172`r^2\theta+r^2\theta^2\right)+2.\sqrt{\left(-1.615521742612498`^{34}+2.2588181335162941`^{18}r^2\theta-1.7975103574736352`^{17}r^2\theta^2\right)^2 / \left(8.987551787368176`^{16}-12.566370614359172`r^2\theta+r^2\theta^2\right)^2-\left(4.\left(7.2597926626745534`^{50}-1.015062247661201`^{35}r^2\theta+8.07760871306249`^{33}r^2\theta^2\right)\right) / \left(8.987551787368176`^{16}-12.566370614359172`r^2\theta+r^2\theta^2\right)\right)\right)\right)},
  {r, -10 000, 10 000}, {θ, -20 000 π, 20 000 π}
]$$ 
```



```

RevolutionPlot3D[
{
  {
    (-0.5` $\sqrt{(-2.(-1.615521742612498 \times 10^{34} + 2.2588181335162941 \times 10^{18} r^2 \theta - 1.7975103574736352 \times 10^{17} r^2 \theta^2)) / (8.987551787368176 \times 10^{16} - 12.566370614359172 r^2 \theta + r^2 \theta^2) - 2. \sqrt{((-1.615521742612498 \times 10^{34} + 2.2588181335162941 \times 10^{18} r^2 \theta - 1.7975103574736352 \times 10^{17} r^2 \theta^2)^2 / (8.987551787368176 \times 10^{16} - 12.566370614359172 r^2 \theta + r^2 \theta^2)^2 - (4. (7.2597926626745534 \times 10^{50} - 1.015062247661201 \times 10^{35} r^2 \theta + 8.07760871306249 \times 10^{33} r^2 \theta^2)) / (8.987551787368176 \times 10^{16} - 12.566370614359172 r^2 \theta + r^2 \theta^2)}}}$ ,
    {r, -10 000, 10 000}, { $\theta$ , -20 000  $\pi$ , 20 000  $\pi$ }
  ]

```



## VIII. Theoretical Relations of Point to Point Pickup of Invariance through the Imaginary Plane



We have discussed the geometry of a cone, and shown that when a substance of any kind travels through the height of the cone, we can solve for its velocity in two different ways. We can take the first derivative of the maximum distance of the height of the cone with respect to time, and understand that the wavelength of light received has an actual initial radius equal to the wavelength of light received by the perceiver. We have also shown that we can solve for a velocity through the height of the cone by application of relativity and the initial principle that  $\eta = r$  at the maximum height of the cone.

We will now show that it's possible to include imaginary solutions to theta during the combination of multiple points in the visual field.

$$\frac{\sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2}}{\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}} =$$

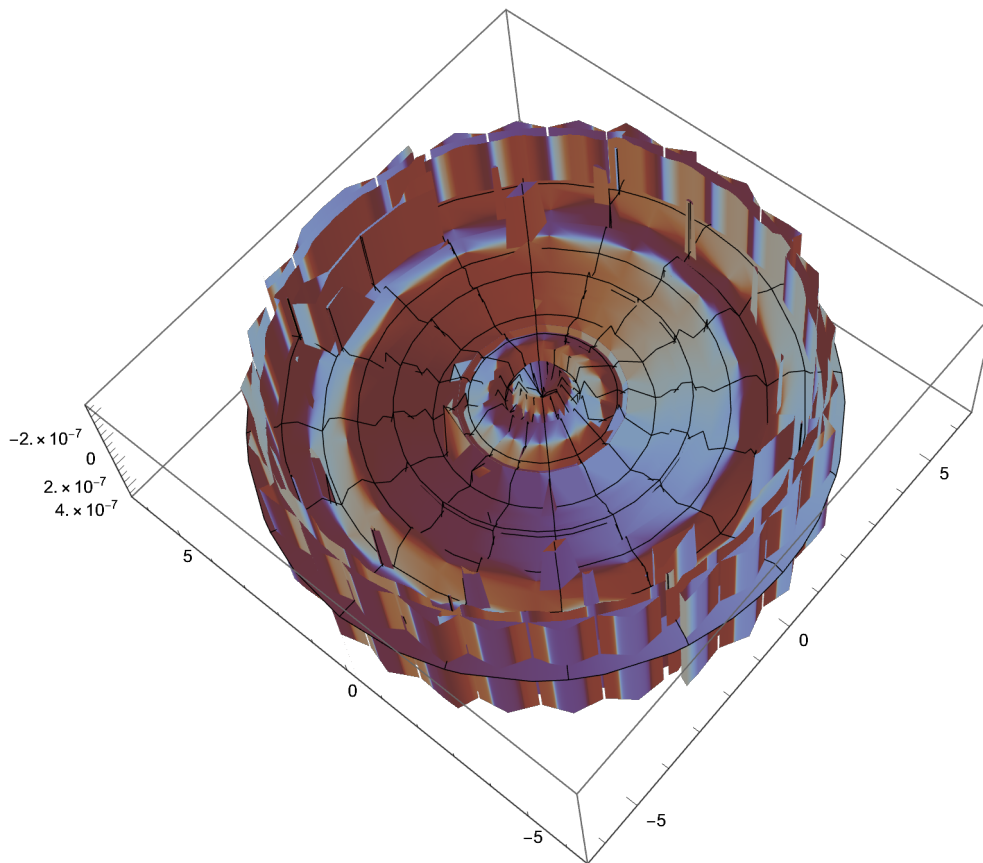
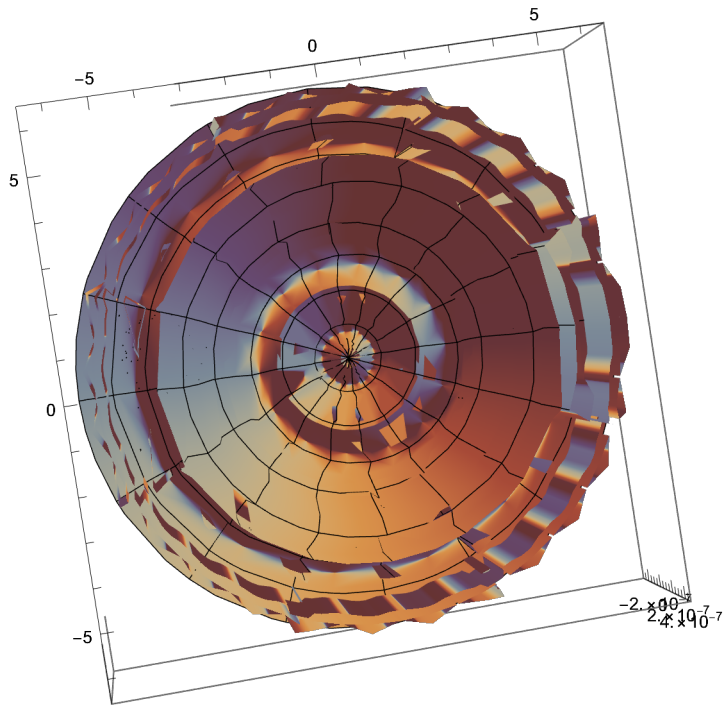
velocity

$$2 \pi$$

$$D \left[ \frac{\sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2}}{\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}}, \theta \right]$$

$$2 \pi \left( \frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{2 \sqrt{39.4784 - 12.5664 \theta + \theta^2} \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}} - \frac{(-12.5664 + 2 \theta) \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{2 (39.4784 - 12.5664 \theta + \theta^2)^{3/2}} \right)$$

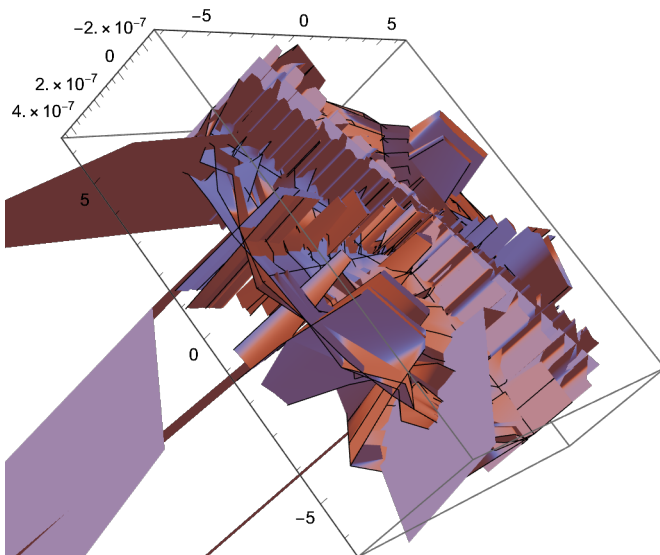
$$\text{RevolutionPlot3D} \left[ 2 \pi \left( \frac{(-1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \theta)}{\left( 2 \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \sqrt{(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2)} \right)} - \frac{((-12.566370614359172 + 2 \theta) \sqrt{(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2)})}{2 (39.47841760435743 - 12.566370614359172 \theta + \theta^2)^{3/2}} \right), \{\theta, -2 \pi, 2 \pi\} \right]$$



```

RevolutionPlot3D[2 π ((-1.1294090667581471`*^18 + 1.7975103574736352`*^17 θ) /
  (2 √(39.47841760435743` - 12.566370614359172` θ + (θ)^2)
  √(3.5481432270250993`*^18 - 1.1294090667581471`*^18 θ +
    8.987551787368176`*^16 θ^2)) -
  ((-12.566370614359172` + 2 θ) √(3.5481432270250993`*^18 -
    1.1294090667581471`*^18 θ + 8.987551787368176`*^16 θ^2))) /
  (2 (39.47841760435743` - 12.566370614359172` θ + θ^2)^(3/2)), {θ, -2 π, 2 π},
  {β, -2 π, 2 π}]

```



$$\left\{ \left\{ \theta \rightarrow \frac{2}{3} \left( 2\pi - \frac{2\pi}{(17 + 3\sqrt{33})^{1/3}} + (17 + 3\sqrt{33})^{1/3} \pi \right) \right\}, \right.$$

$$\left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{2(1 + i\sqrt{3})\pi}{3(17 + 3\sqrt{33})^{1/3}} - \frac{1}{3}(1 - i\sqrt{3})(17 + 3\sqrt{33})^{1/3}\pi \right\},$$

$$\left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{2(1 - i\sqrt{3})\pi}{3(17 + 3\sqrt{33})^{1/3}} - \frac{1}{3}(1 + i\sqrt{3})(17 + 3\sqrt{33})^{1/3}\pi \right\} \}$$

$$\left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right)$$

$$\text{SphericalPlot3D}\left[\left\{\sqrt{(3.5481432270250993`*^18 - 1.1294090667581471`*^18((\theta)))} + \right.\right.$$

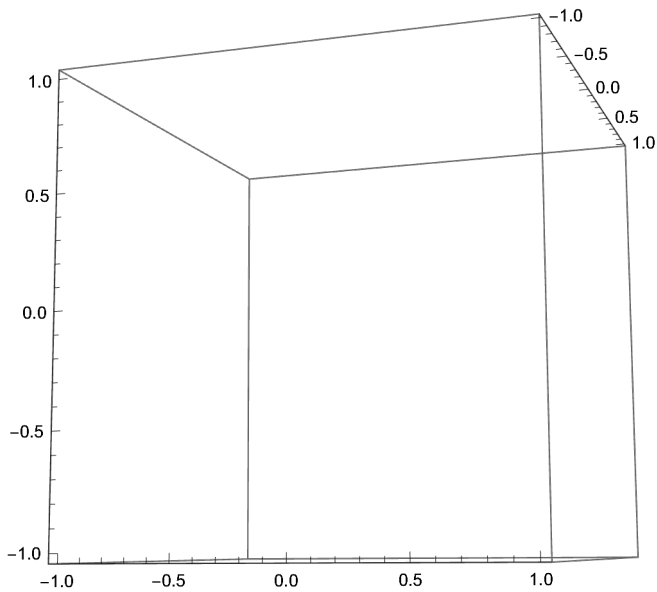
$$8.987551787368176`*^16$$

$$\left. \left( \left( \left( 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right) \right) \left( \left( \frac{2}{3} \left( 2\pi - \frac{2\pi}{(17+3\sqrt{33})^{1/3}} + (17+3\sqrt{33})^{1/3}\pi \right) \right) \right) \right) \right) \right) / \right.$$

$$\left. \left( \sqrt{(39.47841760435743` - 12.566370614359172` \left( 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right) \right))} + \right. \right.$$

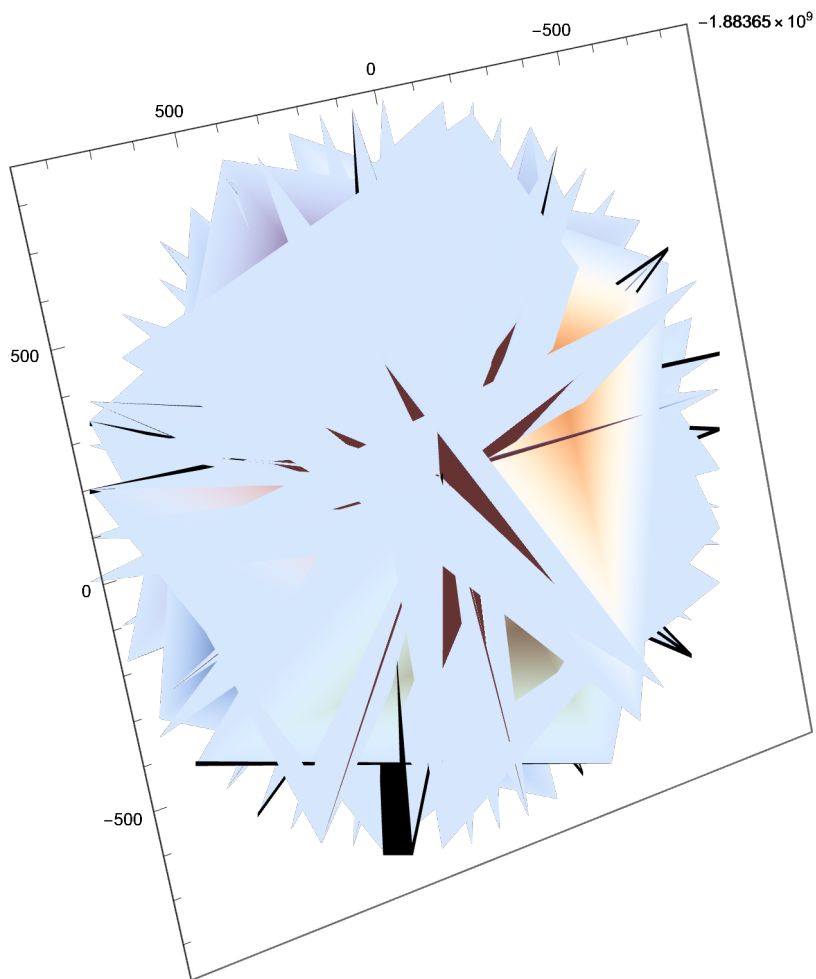
$$\left. \left( \left( \frac{2}{3} \left( 2\pi - \frac{2\pi}{(17+3\sqrt{33})^{1/3}} + (17+3\sqrt{33})^{1/3}\pi \right) \right) \left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \right. \right. \right.$$

$$\left. \left. \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right) \right) \right\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



SphericalPlot3D[

$$\left\{ \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \right. \\ \left. \left. \left. 8.987551787368176 \cdot 10^{16} \left( \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \right) \right) / \right. \\ \left. \left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 \cdot \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \right. \\ \left. \left. \left. \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \frac{1}{3} (1+i\sqrt{3}) (17+3\sqrt{33})^{1/3} \pi \right) \right) \right) \right) \right) \right\}, \{\beta, -\pi, \pi\}, \{\theta, -25\pi, 25\pi\}]$$



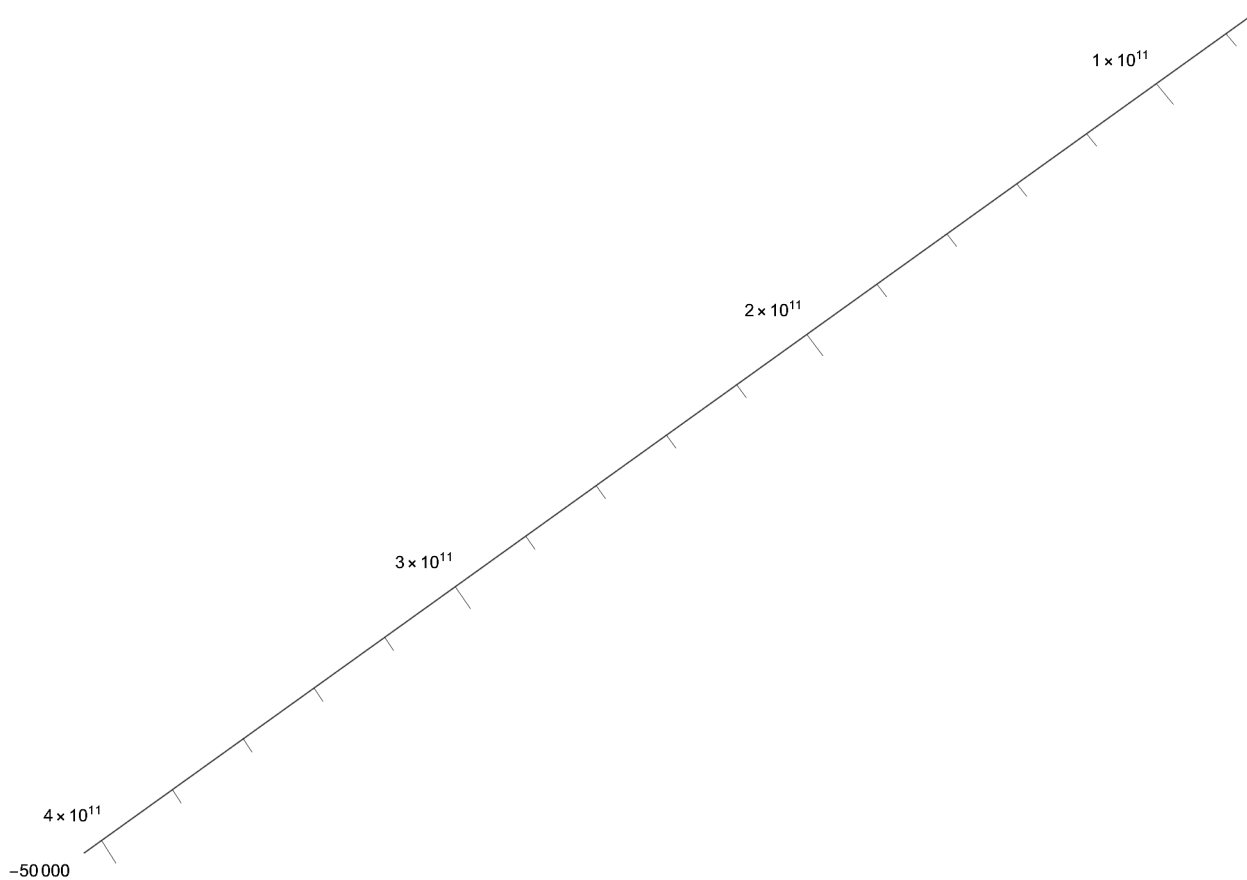
SphericalPlot3D[

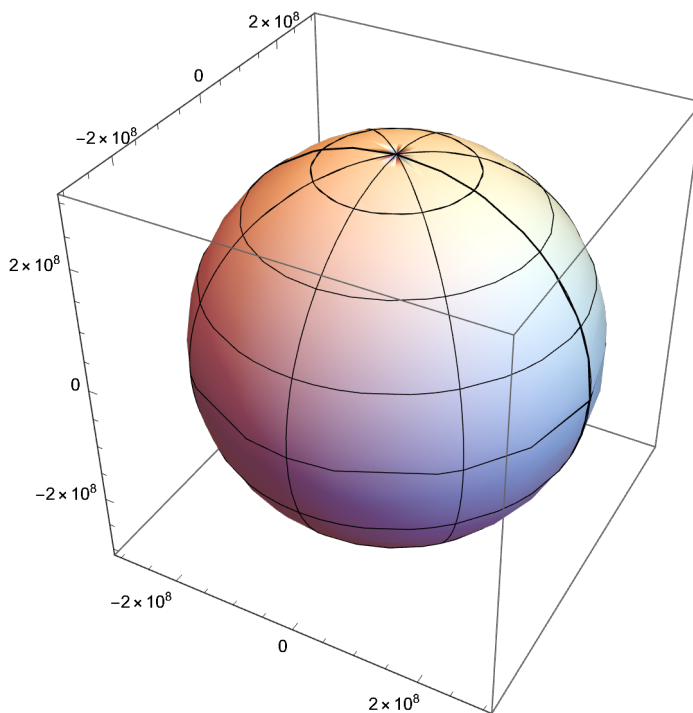
$$\left\{ \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} (\theta) + 8.987551787368176 \cdot 10^{16} \right.} \right. \right.$$

$$\left. \left. \left. (\theta)^2 \right) \right) \right) / \left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 (\theta) + \right. \right. \right.$$

$$\left. \left. \left. \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \left( \frac{4\pi}{3} + \frac{2(1 - i\sqrt{3})\pi}{3(17 + 3\sqrt{33})^{1/3}} - \right. \right. \right.$$

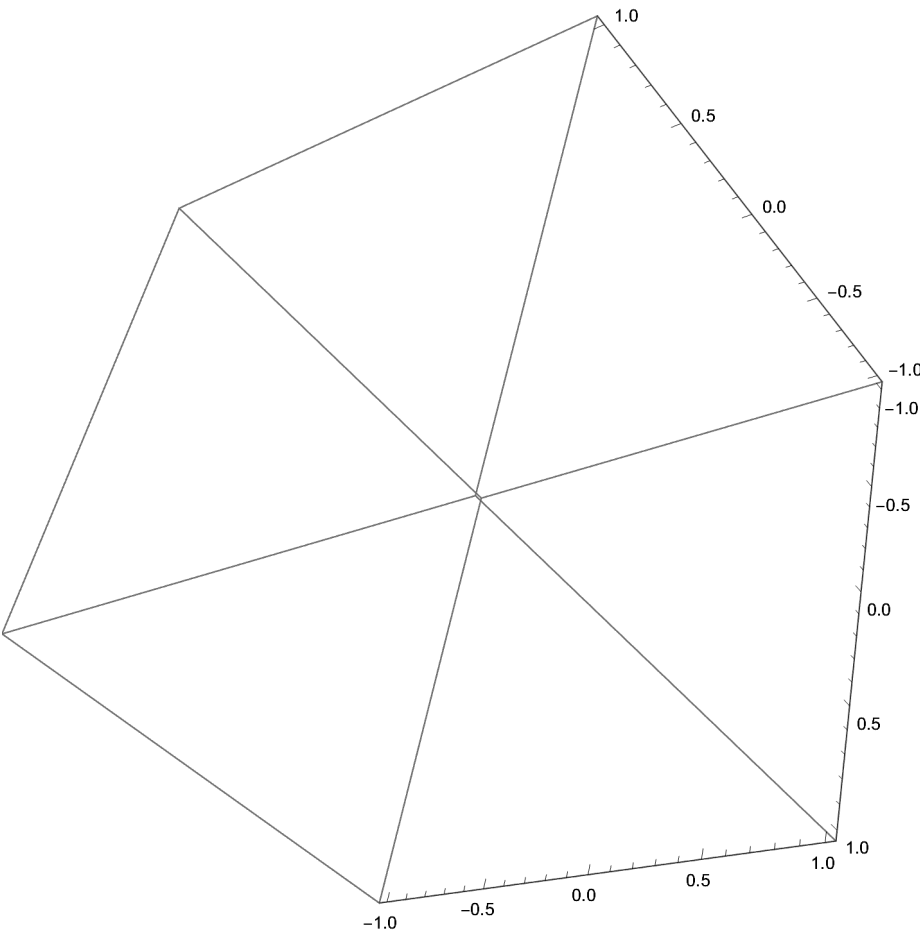
$$\left. \left. \left. \left. \frac{1}{3} (1 + i\sqrt{3}) (17 + 3\sqrt{33})^{1/3} \pi \right) \right) \right) \right) \right\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$





$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left\{\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \right.}\right. \right. \\
& \quad \left. \left. \left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right) + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 \right) \right] / \\
& \quad \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right), \\
& \left( - \left( 1. \cdot \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \right. \right. \right. \\
& \quad \left. \left. \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right) + 8.987551787368176 \cdot 10^{16} \right. \right. \\
& \quad \left. \left. \left( \frac{4\pi}{3} + \frac{2(1-i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1+i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right)^2 \right) \right) \right] / \\
& \quad \left. \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) \right\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]
\end{aligned}$$





$$D\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right), \theta\right] \\ - \frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{2 \sqrt{39.4784 - 12.5664 \theta + \theta^2} \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}} - \frac{(-12.5664 + 2 \theta) \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{2 (39.4784 - 12.5664 \theta + \theta^2)^{3/2}}$$

$$D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$D\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta\right] \\ - \frac{(4 \pi r^2 - 2 r^2 \theta)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

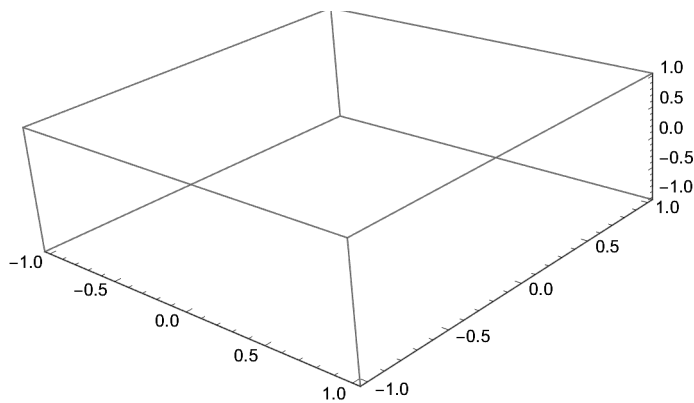
$$\text{Solve}\left[\left(\left(8 \pi \left(-\frac{\left(4 \pi r^2 - 2 r^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)\right)^2}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right)\right) / (c^4)\right) T = \left(\left(8 \pi \left(-1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) / \left(2 \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2\right)}\right) - \left((-12.566370614359172 + 2 \theta) \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2\right)}\right) / \left(2 (39.47841760435743 - 12.566370614359172 \theta + \theta^2)^{3/2}\right)\right) / (c^4)\right), r\right]$$

{{}}

$$\text{Solve}\left[\left(\frac{8\pi G}{c^4}\right) T == \left(\frac{8\pi \left(\sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2}\right)}{\left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right)}\right) / (c^4)\right], T\right]$$

$$\left\{\left\{T \rightarrow \frac{0.101937 \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{\sqrt{39.4784 - 12.5664 \theta + \theta^2}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\left(0.1019367991845056 \sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right), \{\beta, -2\pi, 2\pi\}, \{\theta, -2\pi, 2\pi\}\right]$$



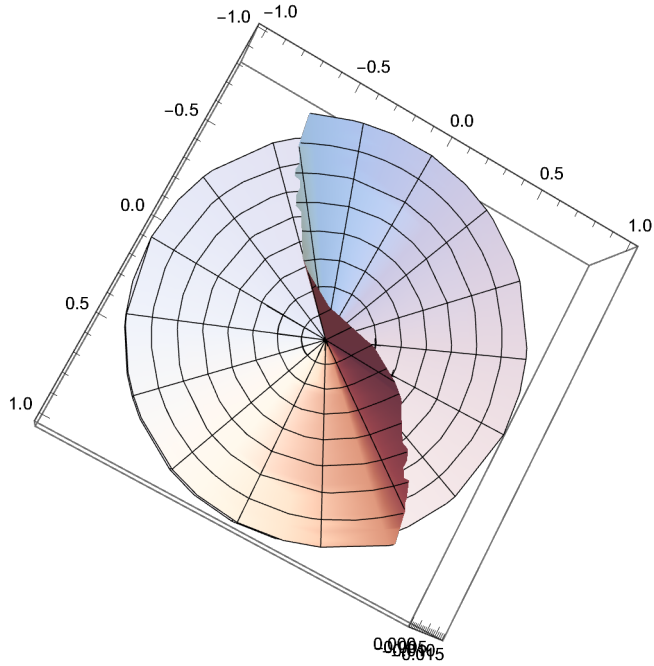
$$\text{Solve}\left[\left(\frac{8\pi \left(\left(0.1019367991845056 \sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2}\right)\right)}{\left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right)}\right) / (c^4)\right] T ==$$

$$\left(\frac{8\pi \left(-\frac{(4\pi r^2 - 2r^2 \theta)^2}{8\pi (4\pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}\right)}{(c^4)}\right), T\right]$$

$$\left\{\left\{T \rightarrow \frac{1. \left(-\frac{0.0397887 (12.5664 r^2 - 2. r^2 \theta)^2}{(12.5664 r^2 \theta - 1. r^2 \theta^2)^{3/2}} - \frac{0.159155 r^2}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}}\right)}{G}\right\}\right\}$$

$$G := 9.81$$

$$\text{RevolutionPlot3D}\left[\frac{1}{G} 1. \cdot \left( - \frac{0.039788735772973836 \cdot (12.566370614359172 \cdot r^2 - 2. \cdot r^2 \theta)^2}{(12.566370614359172 \cdot r^2 \theta - 1. \cdot r^2 \theta^2)^{3/2}} - \frac{0.15915494309189535 \cdot r^2}{\sqrt{12.566370614359172 \cdot r^2 \theta - 1. \cdot r^2 \theta^2}} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} \right]$$



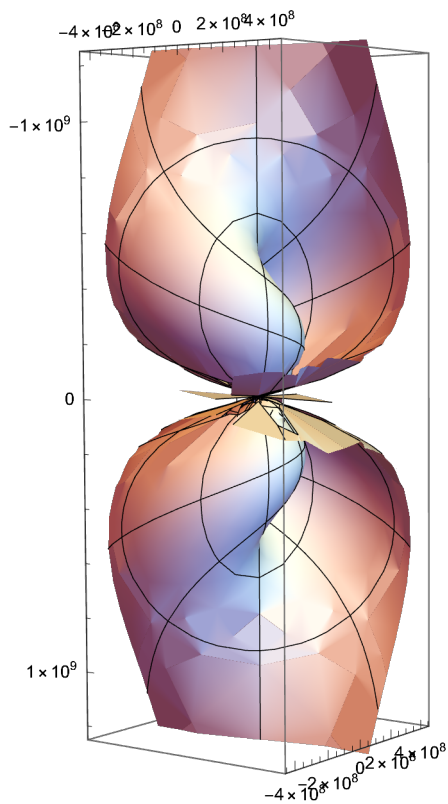
$$\text{RevolutionPlot3D}\left[\frac{1}{G} 1. \cdot \left( - \frac{0.039788735772973836 \cdot (12.566370614359172 \cdot r^2 - 2. \cdot r^2 \theta)^2}{(12.566370614359172 \cdot r^2 \theta - 1. \cdot r^2 \theta^2)^{3/2}} - \frac{0.15915494309189535 \cdot r^2}{\sqrt{12.566370614359172 \cdot r^2 \theta - 1. \cdot r^2 \theta^2}} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\} \right]$$

$$D\left[D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta\right], \theta\right] - \frac{(4\pi r^2 - 2r^2 \theta)^2}{8\pi (4\pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2}{2\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

SphericalPlot3D[  

$$\left\{ \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 \right)} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right), \right.$$
  

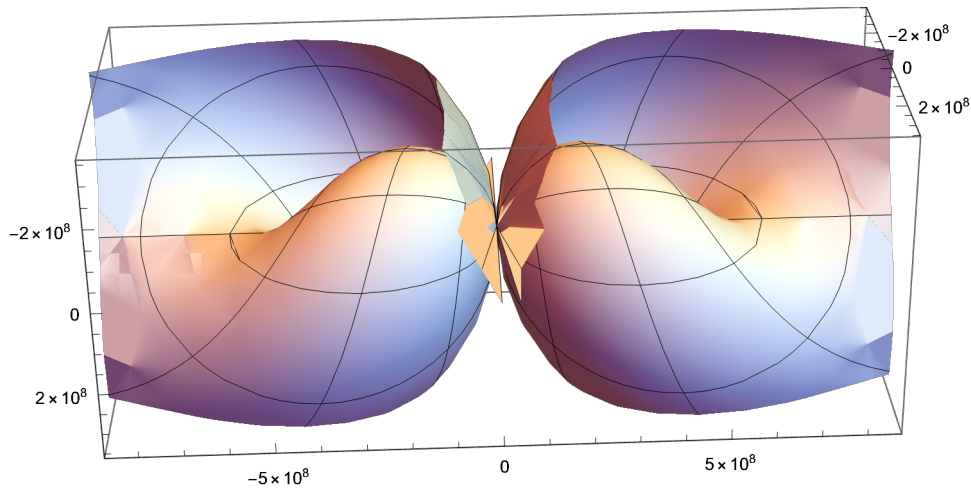
$$\left. - \left( 1. \cdot \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + 8.987551787368176 \cdot 10^{16} \theta^2 \right)} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right) \right\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



RevolutionPlot3D[
$$\left( - \left( 1. \cdot \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 \right)} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right) \right), \{\theta, -2\pi, 2\pi\}]$$

SphericalPlot3D[

$$\left\{ - \left( 1. \sqrt{ \left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \times 2 \pi \left( 1 - \sqrt{1 - \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \left( 2 \pi \left( 1 - \sqrt{1 - \sin[\beta]^2} \right) \right)^2 \right) } \right) / \right. \\ \left. \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right), \right. \\ \left. \left( \sqrt{ \left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \times 2 \pi \left( 1 + \sqrt{1 - \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \left( 2 \pi \left( 1 + \sqrt{1 - \sin[\beta]^2} \right) \right)^2 \right) } \right) / \right. \\ \left. \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) \right\}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}]$$



D[ $(\sqrt{(3.5481432270250993 \cdot 10^{18} -$

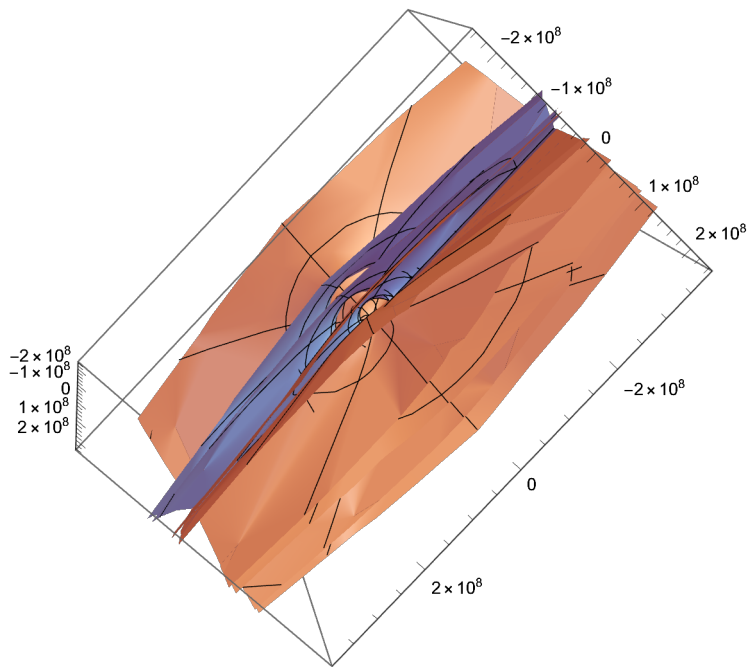
$$1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2)) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right), \theta] \\ \frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{2 \sqrt{39.4784 - 12.5664 \theta + \theta^2} \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2} - (-12.5664 + 2 \theta) \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{2 (39.4784 - 12.5664 \theta + \theta^2)^{3/2}}$$

Solve[ $\beta == \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right], \theta]$

$$\left\{ \left\{ \theta \rightarrow 2 \pi \left( 1 - \sqrt{1 - \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \pi \left( 1 + \sqrt{1 - \sin[\beta]^2} \right) \right\} \right\}$$

SphericalPlot3D[  

$$\frac{\left(-1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \times 2 \pi \left(1 + \sqrt{1 - \sin^2[\beta]}\right)\right) \sqrt{\left(39.47841760435743 - 12.566370614359172 \cdot \theta + \left(2 \pi \left(1 + \sqrt{1 - \sin^2[\beta]}\right)\right)^2\right) \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left(2 \pi \left(1 + \sqrt{1 - \sin^2[\beta]}\right)\right)^2\right) - \left(\left(-12.566370614359172 + 2 \left(2 \pi \left(1 + \sqrt{1 - \sin^2[\beta]}\right)\right)\right) \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2\right)}\right)}}{2 \left(39.47841760435743 - 12.566370614359172 \cdot \theta + 2 \pi \left(1 + \sqrt{1 - \sin^2[\beta]}\right) + \left(2 \pi \left(1 + \sqrt{1 - \sin^2[\beta]}\right)\right)^2\right)^{3/2}}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$$



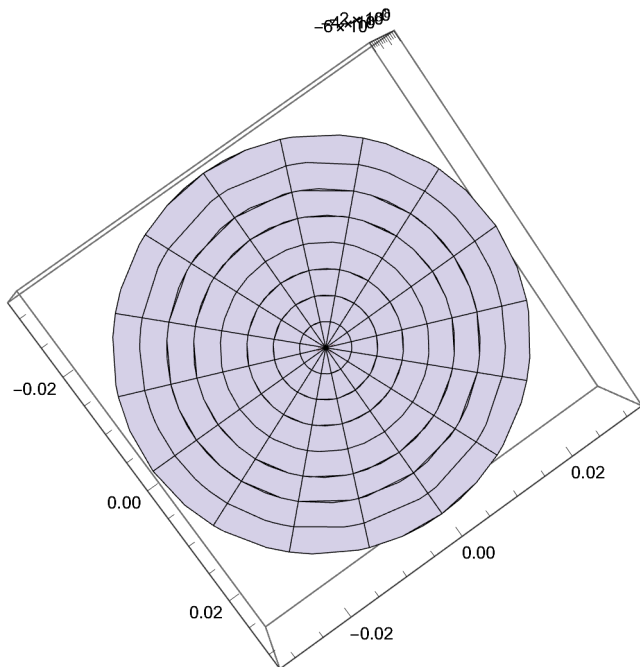
```

RevolutionPlot3D[ - (1. `  $\sqrt{(3.5481432270250993`^{18} -$   

 $1.1294090667581471`^{18} \theta + 8.987551787368176`^{16} \theta^2)}$  ) ) /  

 $(\sqrt{39.47841760435743` - 12.566370614359172` \theta + \theta^2})$  , { $\theta$ , - .01  $\pi$ , .01  $\pi$ } ]

```



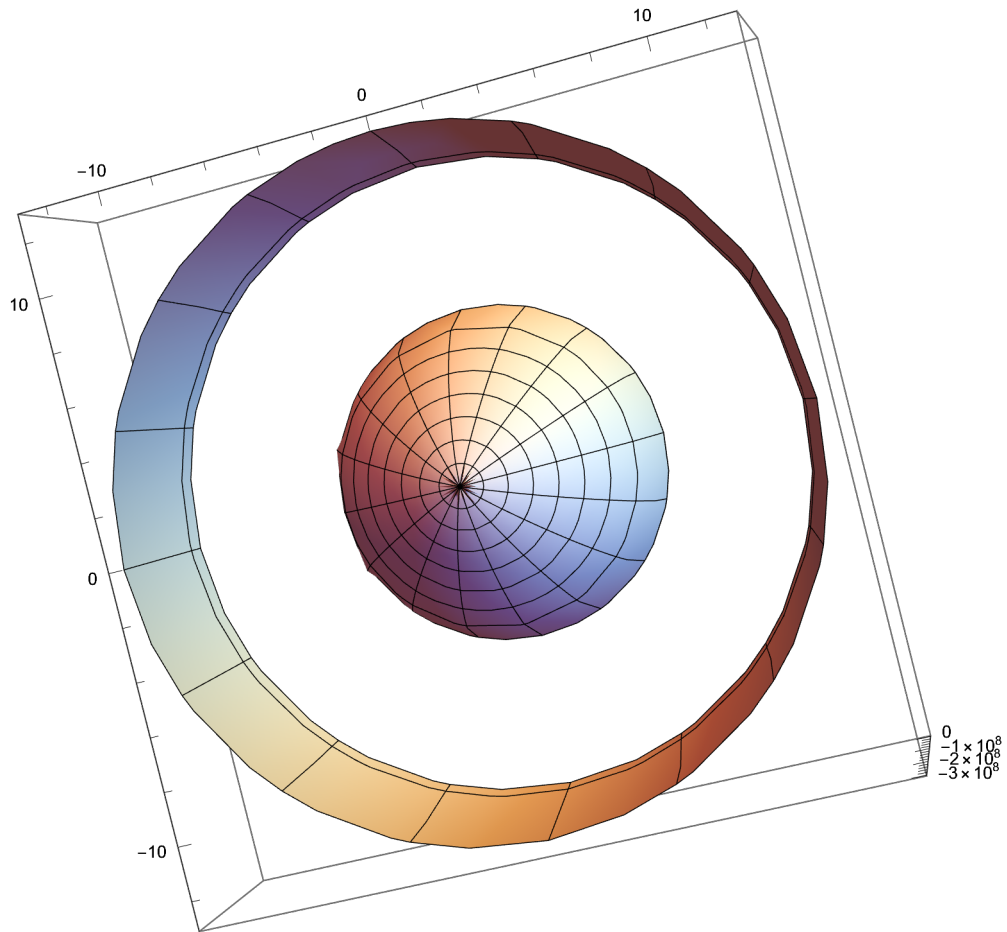
```
c := (2.99792458 * 10^8)
```

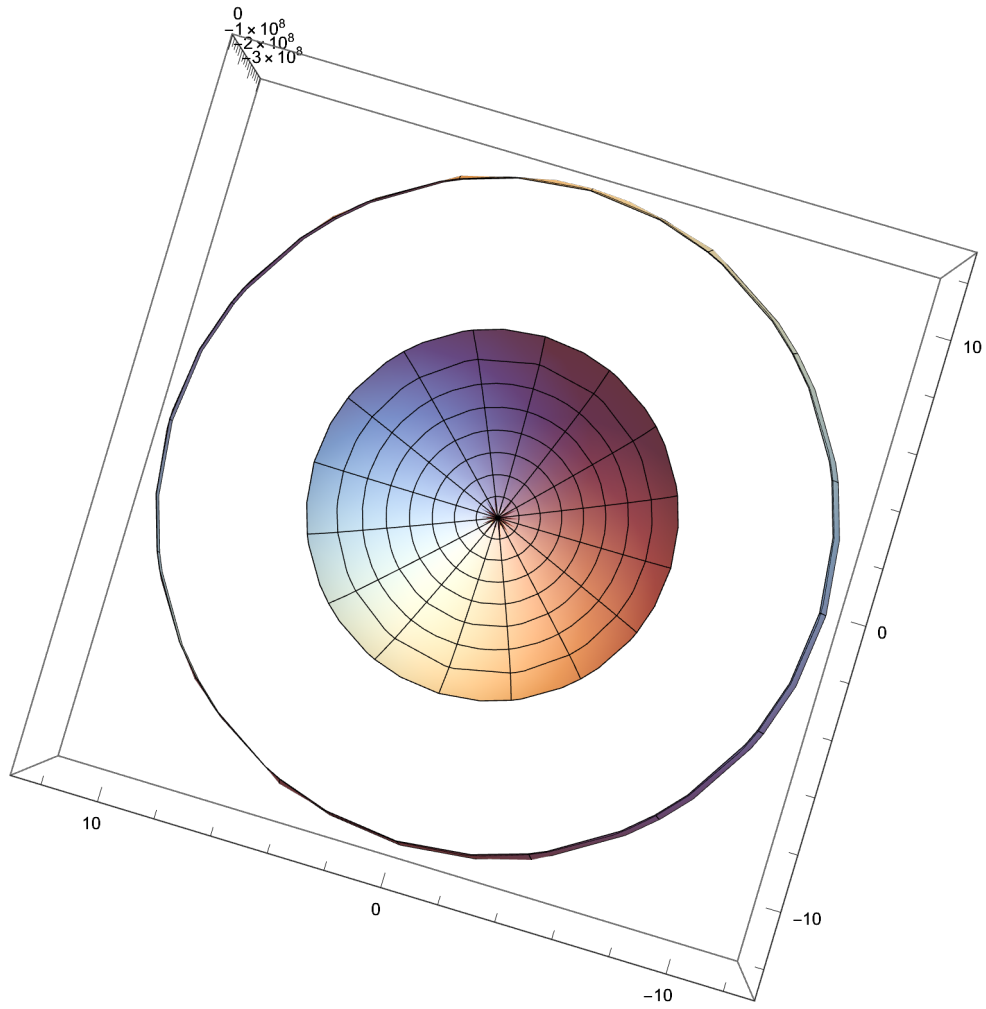
```

RevolutionPlot3D[ -  $\frac{1}{2} \sqrt{4 c^2 - \frac{\sqrt{c^4 (4 \pi - \theta) \theta^3}}{\pi^2}}$  , { $\theta$ , -4  $\pi$ , 4  $\pi$ } ]

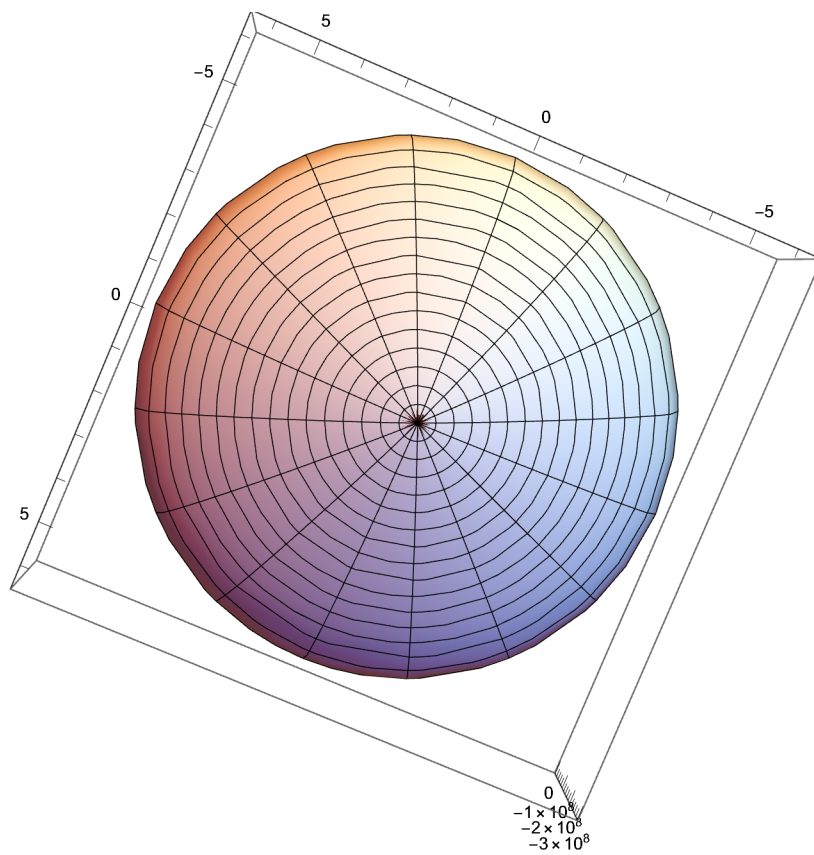
```

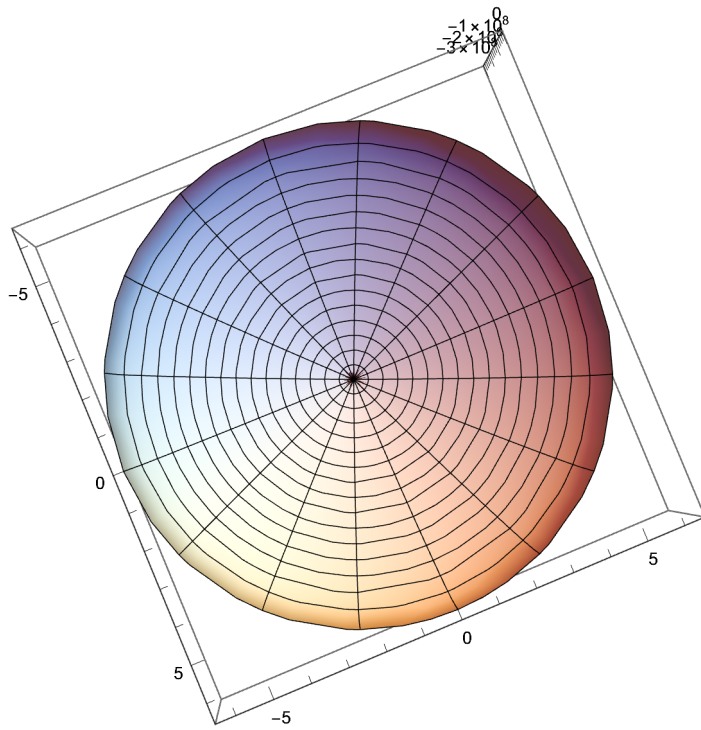




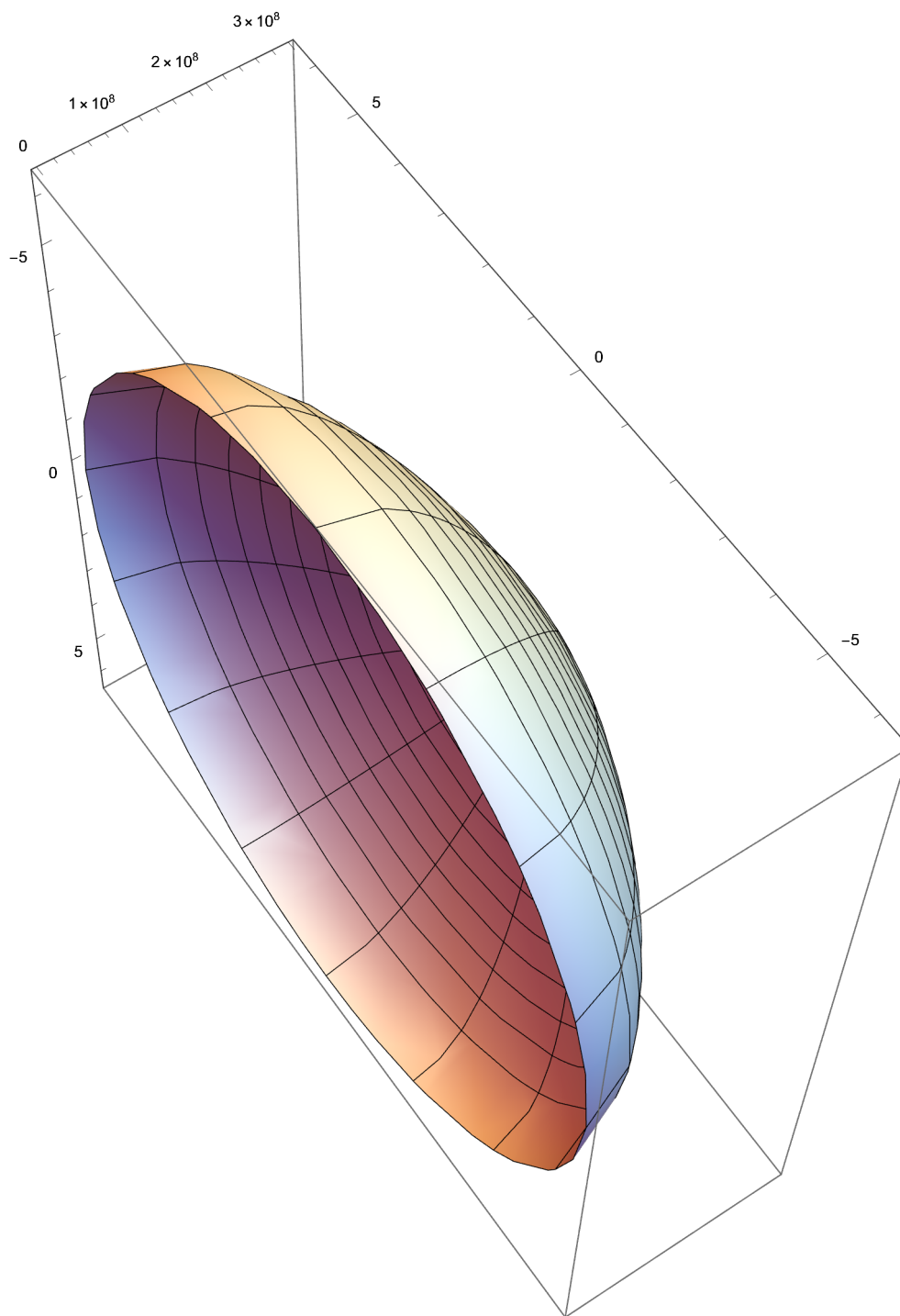


RevolutionPlot3D $\left[-\frac{1}{2}\sqrt{4c^2 - \frac{\sqrt{c^4(4\pi - \theta)\theta^3}}{\pi^2}}, \{\theta, -2\pi, 2\pi\}\right]$

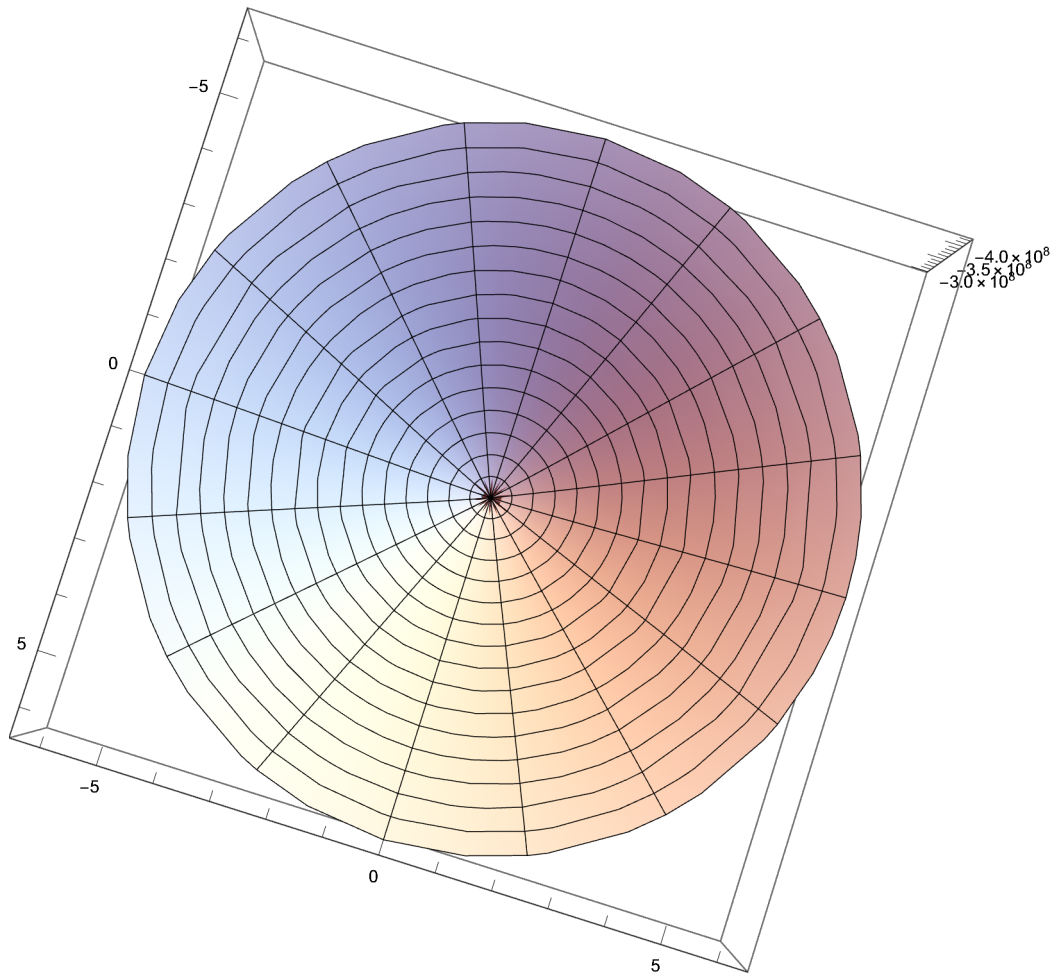


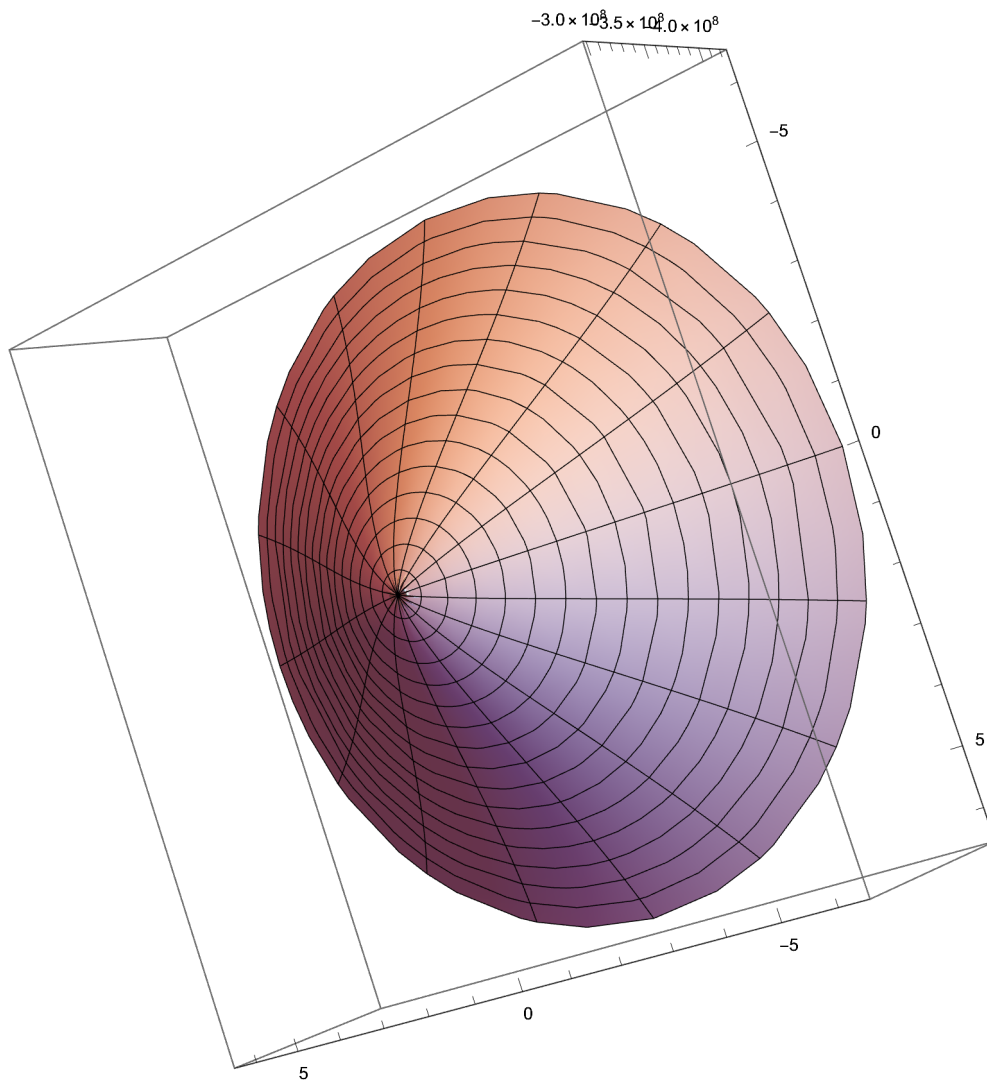


$\text{RevolutionPlot3D}\left[\frac{1}{2} \sqrt{4 c^2 - \frac{\sqrt{c^4 (4 \pi - \theta) \theta^3}}{\pi^2}}, \{\theta, -2 \pi, 2 \pi\}\right]$

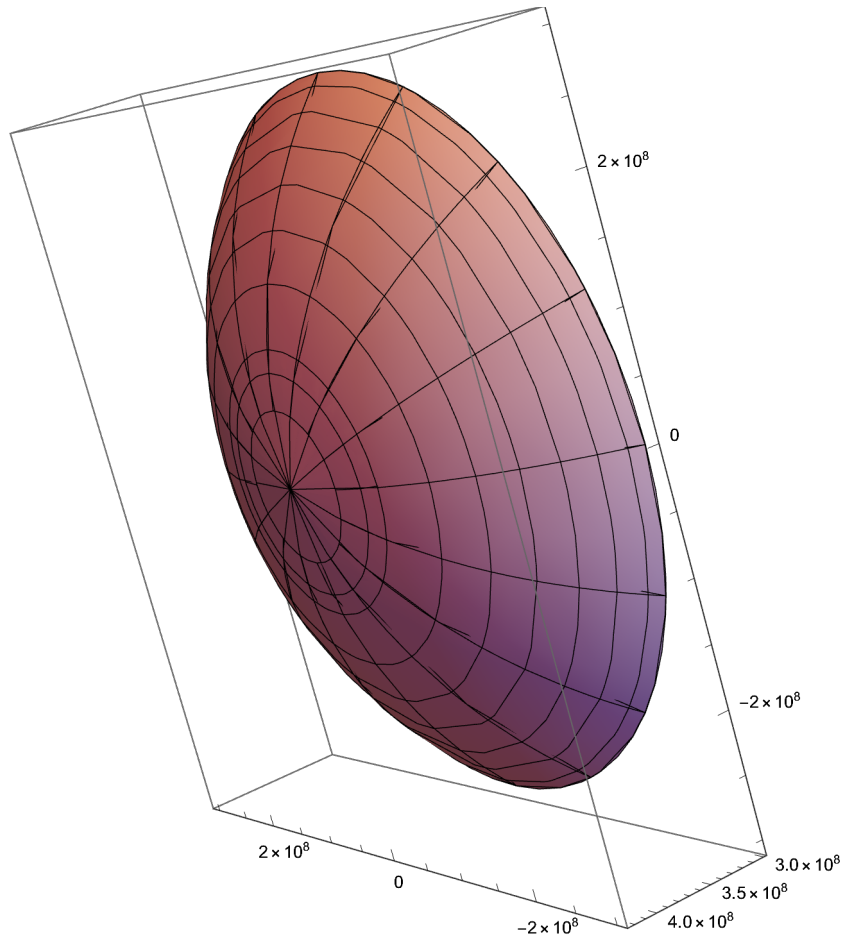


$\text{RevolutionPlot3D}\left[-\sqrt{c^2 + \frac{\sqrt{4 c^4 \pi \theta^3 - c^4 \theta^4}}{4 \pi^2}}, \{\theta, -2 \pi, 2 \pi\}\right]$

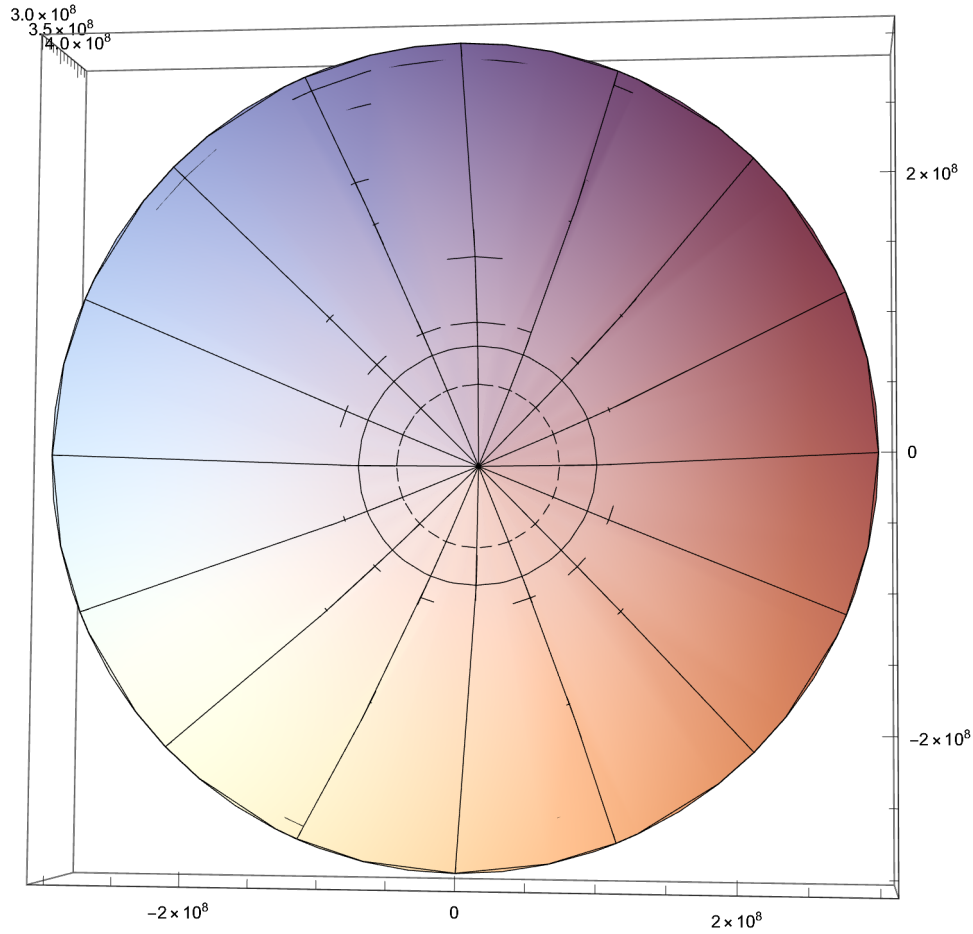




RevolutionPlot3D[  
 $\left\{ \left( \frac{1}{2} \sqrt{4 c^2 - \frac{\sqrt{c^4 (4 \pi - \theta) \theta^3}}{\pi^2}} \right), \left( \sqrt{c^2 + \frac{\sqrt{4 c^4 \pi \theta^3 - c^4 \theta^4}}{4 \pi^2}} \right) \right\}, \{\theta, -4 \pi, 4 \pi\}]$







$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = c \left( \frac{(\theta)}{(2 \pi)} \right), \theta\right]$$

$$\left\{ \{\theta \rightarrow 0\}, \left\{ \theta \rightarrow \frac{4 \pi r^2}{c^2 + r^2} \right\} \right\}$$

Solve[

$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} \sqrt{1 - \frac{(v)^2}{c^2}} = c \left( \frac{(\theta)}{(2 \pi)} \right) / \sqrt{1 - \frac{(v)^2}{c^2}}, \theta]$$

$$\left\{ \{\theta \rightarrow 0\}, \left\{ \theta \rightarrow \frac{4 \pi (c^4 r^2 - 2 c^2 r^2 v^2 + r^2 v^4)}{c^6 + c^4 r^2 - 2 c^2 r^2 v^2 + r^2 v^4} \right\} \right\}$$

Solve[

$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}} = c \left( (\theta) / (2\pi) \right) / \sqrt{1 - \frac{(v)^2}{c^2}}, v]$$

$$\left\{ \left\{ v \rightarrow -\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2 + r^2\theta}} \right\}, \right.$$

$$\left\{ v \rightarrow \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} - \frac{\sqrt{c^6 r^2 (4\pi - \theta)\theta}}{-4\pi r^2 + r^2\theta}} \right\},$$

$$\left\{ v \rightarrow -\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right\},$$

$$\left\{ v \rightarrow \sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2 + r^2\theta} + \frac{c^2 r^2 \theta}{-4\pi r^2 + r^2\theta} + \frac{\sqrt{4c^6\pi r^2\theta - c^6 r^2\theta^2}}{-4\pi r^2 + r^2\theta}} \right\}$$

Solve[

$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} \sqrt{1 - \frac{(v)^2}{c^2}} = c \left( (\theta) / (2\pi) \right) / \sqrt{1 - \frac{(v)^2}{c^2}}, r]$$

$$\left\{ \left\{ r \rightarrow -\frac{i c^3 \sqrt{\theta}}{(c-v)(c+v)\sqrt{-4\pi+\theta}} \right\}, \left\{ r \rightarrow \frac{i c^3 \sqrt{\theta}}{(c-v)(c+v)\sqrt{-4\pi+\theta}} \right\} \right\}$$

$$\frac{\sqrt{r} \sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = c \left( (\theta) / (2\pi) \right), r]$$

$$\left\{ \left\{ r \rightarrow -\frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right\}, \left\{ r \rightarrow \frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right\} \right\}$$

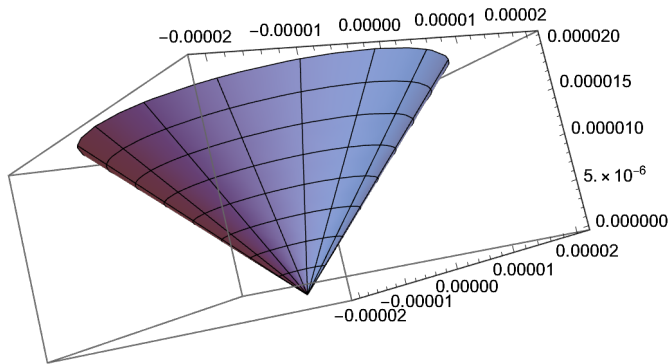
$$\frac{\sqrt{r} \sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} =$$

$$c \left( \left( \theta \sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}} \right) / (2\pi) \right), \theta]$$

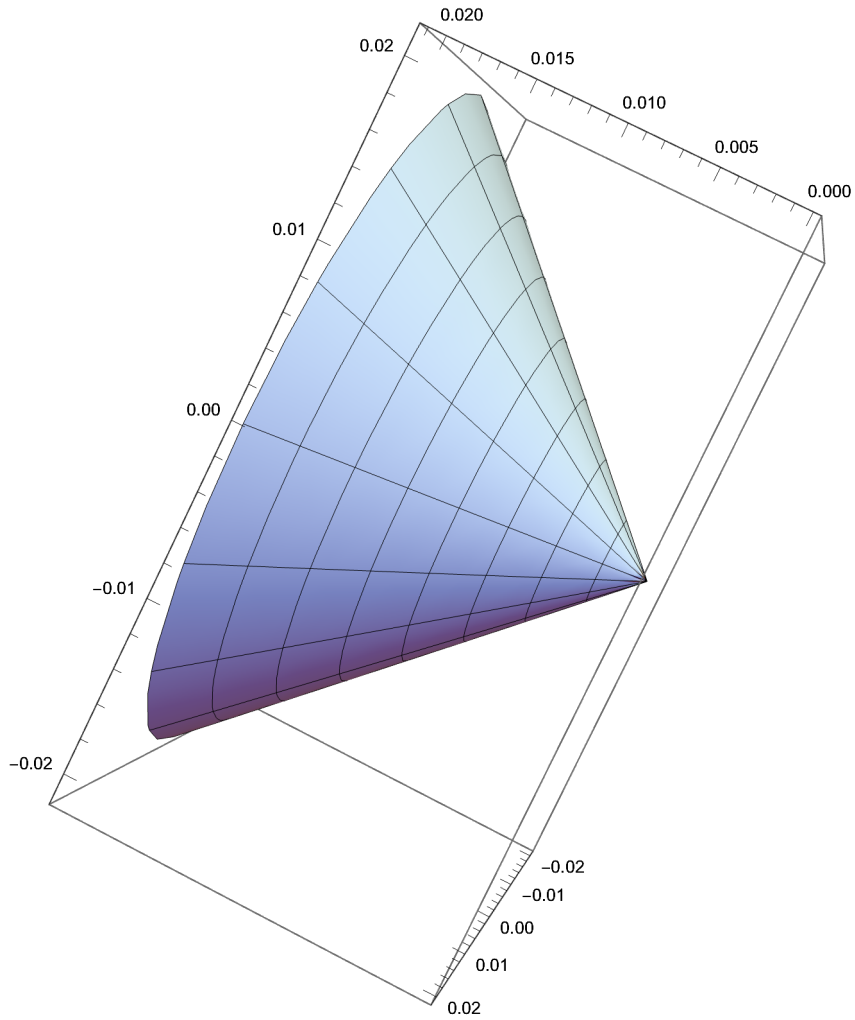
$$\left\{ \left\{ \theta \rightarrow \frac{2\pi (r^2 - \sqrt{c^2 r^2 + 2r^4})}{c^2 + r^2} \right\}, \left\{ \theta \rightarrow \frac{2\pi (r^2 + \sqrt{c^2 r^2 + 2r^4})}{c^2 + r^2} \right\} \right\}$$

$c := (2.99792458 \times 10^8)$

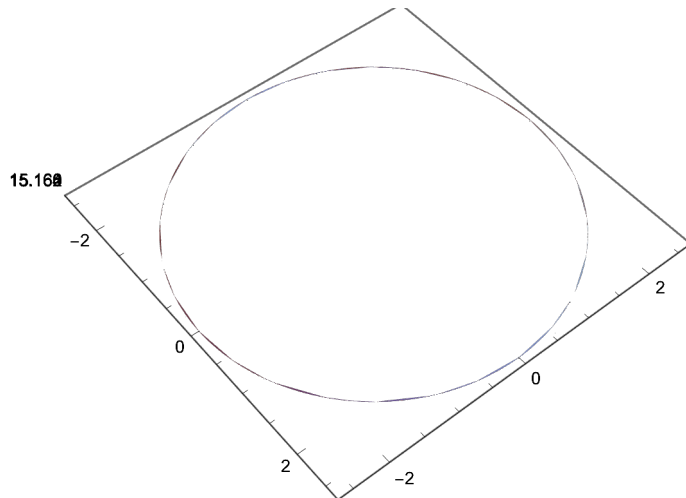
$\text{RevolutionPlot3D}\left[\left\{\frac{2\pi\left(r^2 - \sqrt{c^2 r^2 + 2r^4}\right)}{c^2 + r^2}, \frac{2\pi\left(r^2 + \sqrt{c^2 r^2 + 2r^4}\right)}{c^2 + r^2}\right\}, \{r, -1000, 1000\}\right]$



`RevolutionPlot3D[`  
 $\left\{ \frac{2\pi(r^2 - \sqrt{c^2 r^2 + 2r^4})}{c^2 + r^2}, \frac{2\pi(r^2 + \sqrt{c^2 r^2 + 2r^4})}{c^2 + r^2} \right\}, \{r, -1\,000\,000, 1\,000\,000\}$   
`]`



$\text{RevolutionPlot3D}\left[\left\{\frac{2 \pi \left(r^2 - \sqrt{c^2 r^2 + 2 r^4}\right)}{c^2 + r^2}, \frac{2 \pi \left(r^2 + \sqrt{c^2 r^2 + 2 r^4}\right)}{c^2 + r^2}\right\},\right.$   
 $\left.\{r, -100\,000\,000\,000, 100\,000\,000\,000\}\right]$



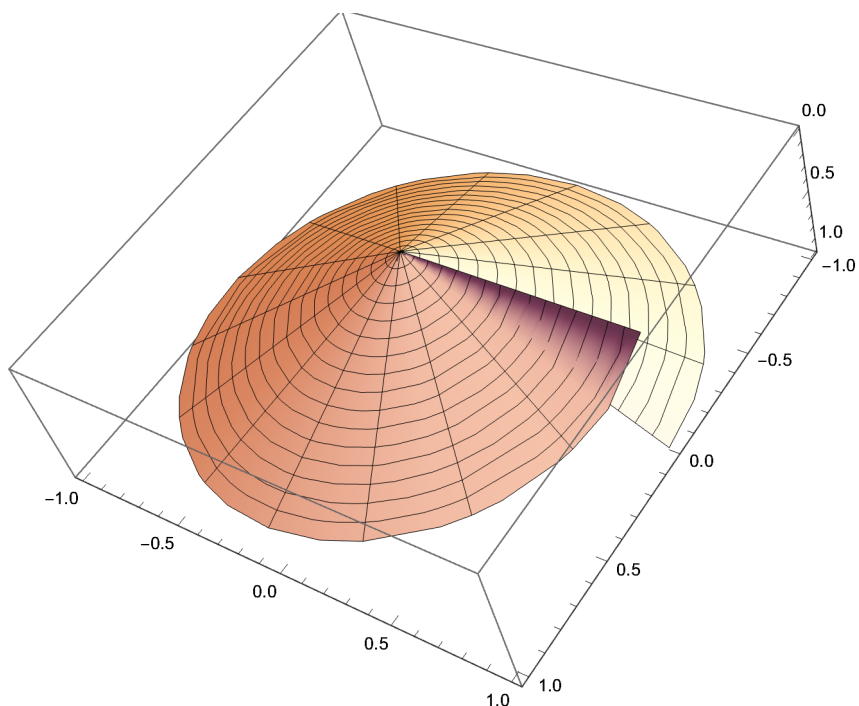
$$\frac{2 \pi \left(r^2 + \sqrt{c^2 r^2 + 2 r^4}\right)}{c^2 + r^2}$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(r / (\theta / (2 \pi)))^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(r / (\theta / (2 \pi)))^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = c (\theta / (2 \pi)), \theta\right]$$

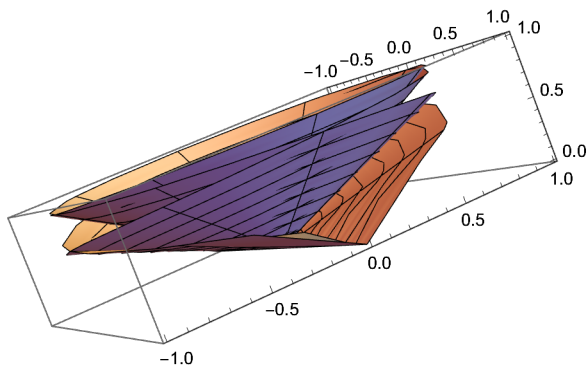
$$\left\{\left\{\theta \rightarrow \frac{4 \pi r^2}{c^2 + r^2}\right\}\right\}$$

$\text{RevolutionPlot3D}\left[\frac{4 \pi r^2}{c^2 + r^2}\right.$

$\text{RevolutionPlot3D}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{(r/(\theta/(2\pi)))^2}{c^2}}} \sqrt{4\pi r - r\theta}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$



$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{v^2}{c^2}}} \sqrt{4\pi r - r\theta} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r\right]$   
 $\{\{\}\}$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1-\frac{v^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi},\right]$$

{{}}

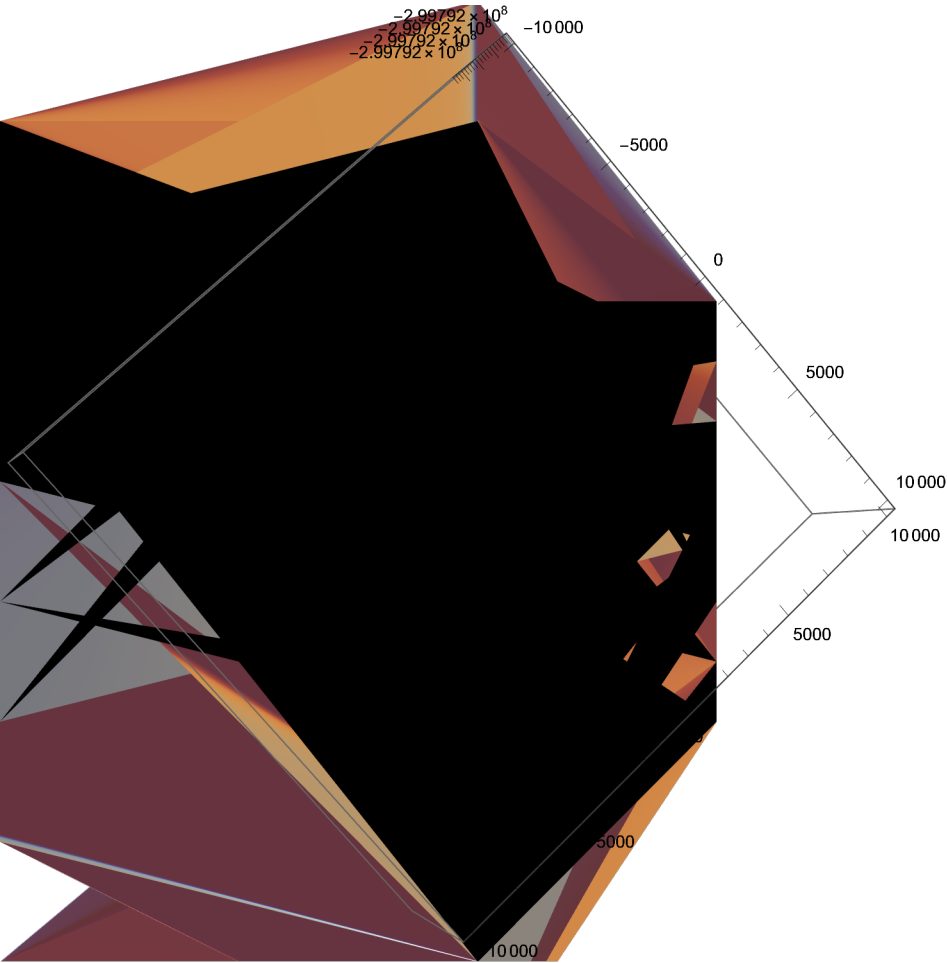
$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1-\frac{v^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{c^2}}}} \sqrt{4\pi r - r\theta} \left(\sqrt{1-\frac{v^2}{c^2}} \theta\right) = c \left(\left(\sqrt{1-\frac{v^2}{c^2}} \theta\right) / (2\pi)\right), v\right]$$

$$\left\{\left\{v \rightarrow -0.5 \sqrt{\left(-\left(2. \left(-1.615521742612498 \cdot r^{2\theta} + 2.2588181335162941 \cdot r^{2\theta} - 1.7975103574736352 \cdot r^{2\theta}\right)\right) / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right) - 2. \sqrt{\left(\left(-1.615521742612498 \cdot r^{2\theta} + 2.2588181335162941 \cdot r^{2\theta} - 1.7975103574736352 \cdot r^{2\theta}\right)^2 / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right)^2 - \left(4. \left(7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} r^{2\theta} + 8.07760871306249 \cdot r^{33} r^{2\theta}\right)\right) / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right)\right)}\right\}, \left\{v \rightarrow 0.5 \sqrt{\left(-\left(2. \left(-1.615521742612498 \cdot r^{2\theta} + 2.2588181335162941 \cdot r^{2\theta} - 1.7975103574736352 \cdot r^{2\theta}\right)\right) / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right) - 2. \sqrt{\left(\left(-1.615521742612498 \cdot r^{2\theta} + 2.2588181335162941 \cdot r^{2\theta} - 1.7975103574736352 \cdot r^{2\theta}\right)^2 / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right)^2 - \left(4. \left(7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} r^{2\theta} + 8.07760871306249 \cdot r^{33} r^{2\theta}\right)\right) / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right)\right)}\right\}, \left\{v \rightarrow -0.5 \sqrt{\left(-\left(2. \left(-1.615521742612498 \cdot r^{2\theta} + 2.2588181335162941 \cdot r^{2\theta} - 1.7975103574736352 \cdot r^{2\theta}\right)\right) / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right) + 2. \sqrt{\left(\left(-1.615521742612498 \cdot r^{2\theta} + 2.2588181335162941 \cdot r^{2\theta} - 1.7975103574736352 \cdot r^{2\theta}\right)^2 / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right)^2 - \left(4. \left(7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} r^{2\theta} + 8.07760871306249 \cdot r^{33} r^{2\theta}\right)\right) / \left(8.987551787368176 \cdot r^{2\theta} - 12.566370614359172 \cdot r^{2\theta} + r^{2\theta}\right)\right)}\right\},$$

$$\left\{v \rightarrow 0.5 \sqrt{\left(-\left(2 \cdot \left(-1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} \theta - 1.7975103574736352 \cdot r^2 \theta^2\right)\right) / \left(8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right) + 2 \cdot \sqrt{\left(\left(-1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} \theta - 1.7975103574736352 \cdot r^2 \theta^2\right)^2 / \left(8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)^2 - \left(4 \cdot \left(7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} \theta + 8.07760871306249 \cdot r^{33} \theta^2\right)\right) / \left(8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)\right)}\right\}$$

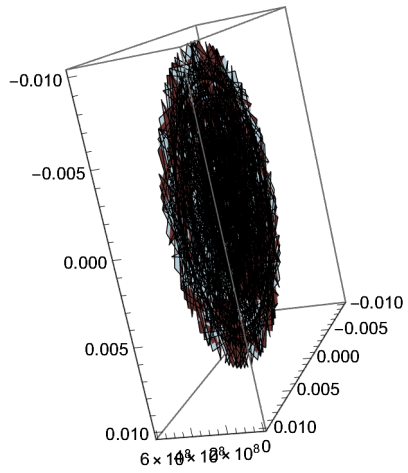
```
RevolutionPlot3D[
  {
    {
      -0.5 \sqrt{\left(-\left(2 \cdot \left(-1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} \theta - 1.7975103574736352 \cdot r^2 \theta^2\right)\right) / \left(8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right) - 2 \cdot \sqrt{\left(\left(-1.615521742612498 \cdot r^{34} + 2.2588181335162941 \cdot r^{18} \theta - 1.7975103574736352 \cdot r^2 \theta^2\right)^2 / \left(8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)^2 - \left(4 \cdot \left(7.2597926626745534 \cdot r^{50} - 1.015062247661201 \cdot r^{35} \theta + 8.07760871306249 \cdot r^{33} \theta^2\right)\right) / \left(8.987551787368176 \cdot r^{16} - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)\right)}\right)},
    {r, -10 000, 10 000}, {θ, -20 000 π, 20 000 π}
  ]
```

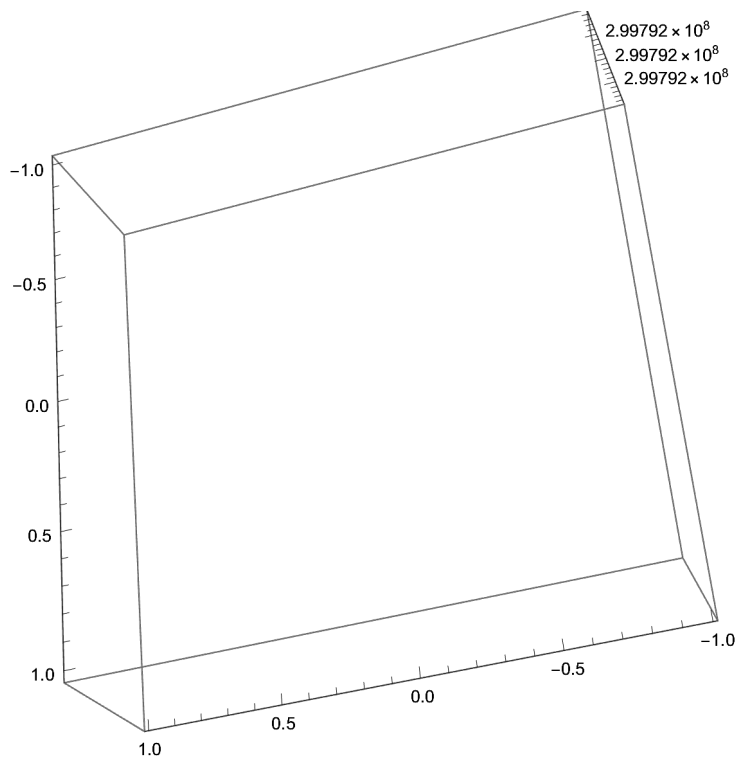
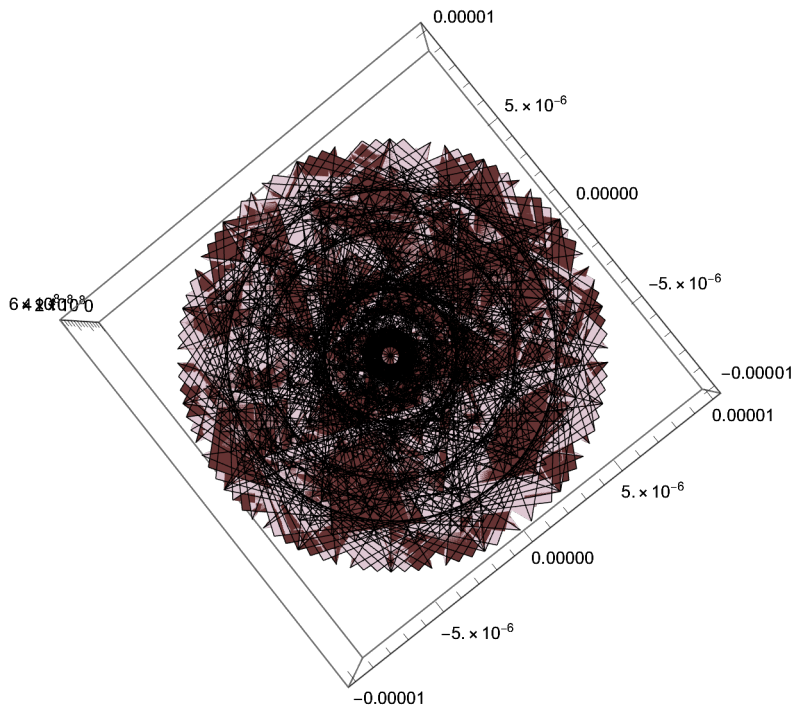






```
RevolutionPlot3D[ $\frac{\sqrt{-4 \pi r^2 + c^2 \theta + r^2 \theta}}{\sqrt{\theta}}$ ,  
{r, -.01, .01}, { $\theta$ , -200 000 000 000  $\pi$ , 200 000 000 000  $\pi$ }]
```

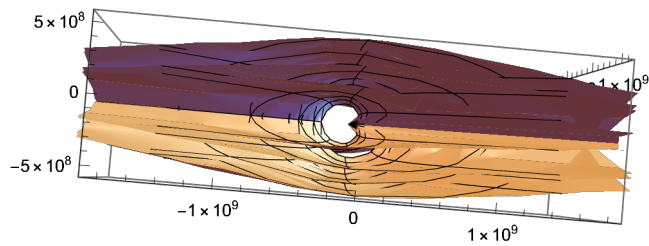




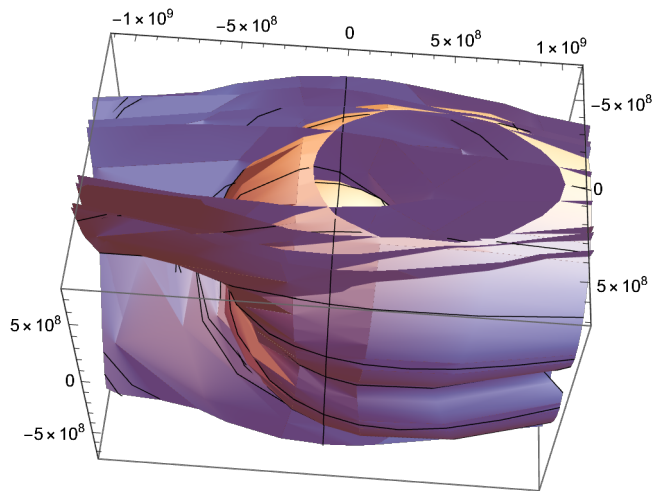
$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{v^2}{c^2}}} \sqrt{4\pi r - r\theta} == c(\theta / (2\pi)), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}}\right\}, \left\{r \rightarrow \frac{c \sqrt{\theta}}{\sqrt{4\pi - \theta}}\right\}\right\}$$

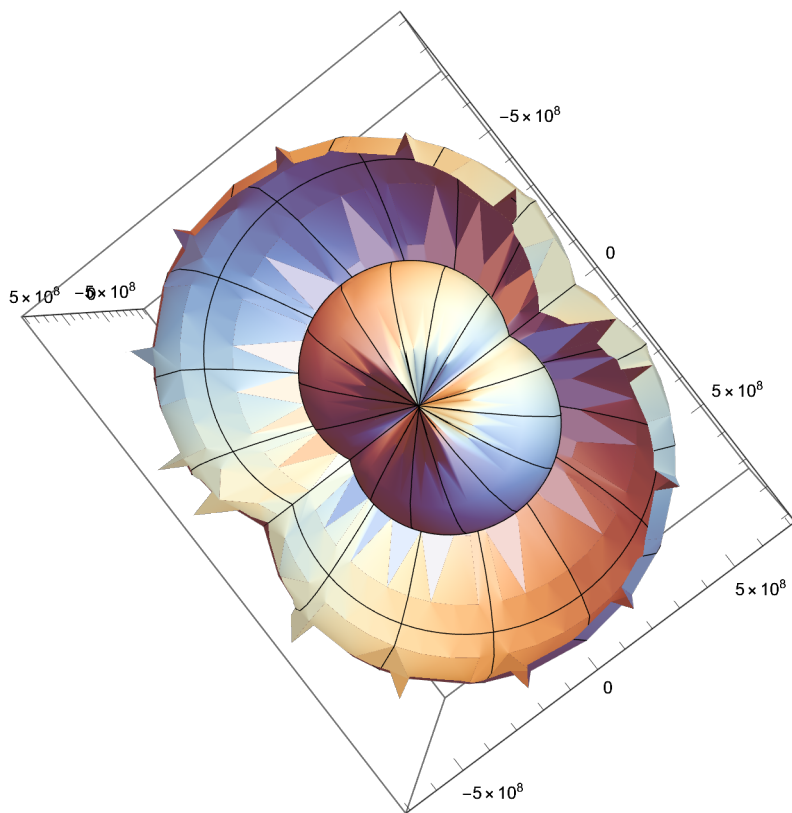
$$\text{SphericalPlot3D}\left[\left\{\frac{c \sqrt{\theta}}{\sqrt{4\pi - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}}\right\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi, \pi\}\right]$$



$$\text{SphericalPlot3D}\left[\left\{\frac{c \sqrt{\theta}}{\sqrt{4\pi - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}}\right\}, \frac{c \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}{\sqrt{4\pi - \theta}}\right\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi, \pi\}\right]$$



SphericalPlot3D $\left[\frac{c \sqrt{2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}{\sqrt{4 \pi - \theta}}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$

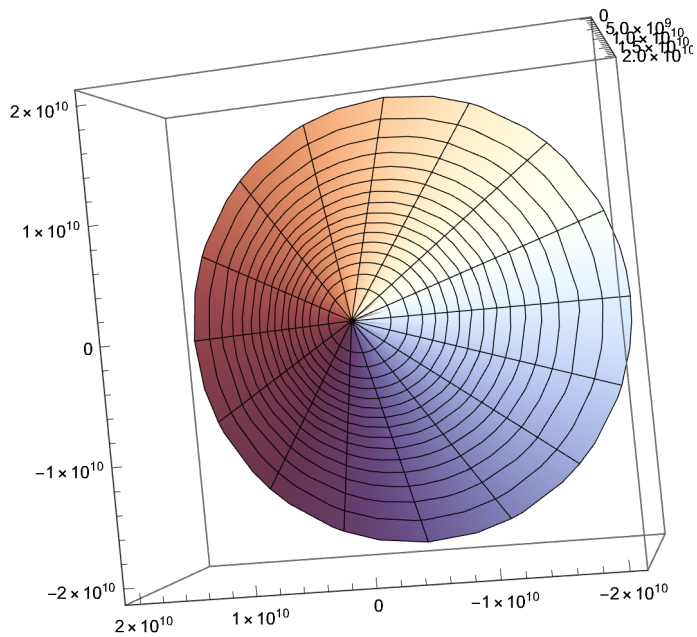


$$\left\{\left\{r \rightarrow -\frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}, \left\{r \rightarrow \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{r \sqrt{1 - \frac{v^2}{c^2}}} \sqrt{\frac{\theta}{1 - \frac{v^2}{c^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == c (\theta / (2 \pi)), v\right]$$

{}

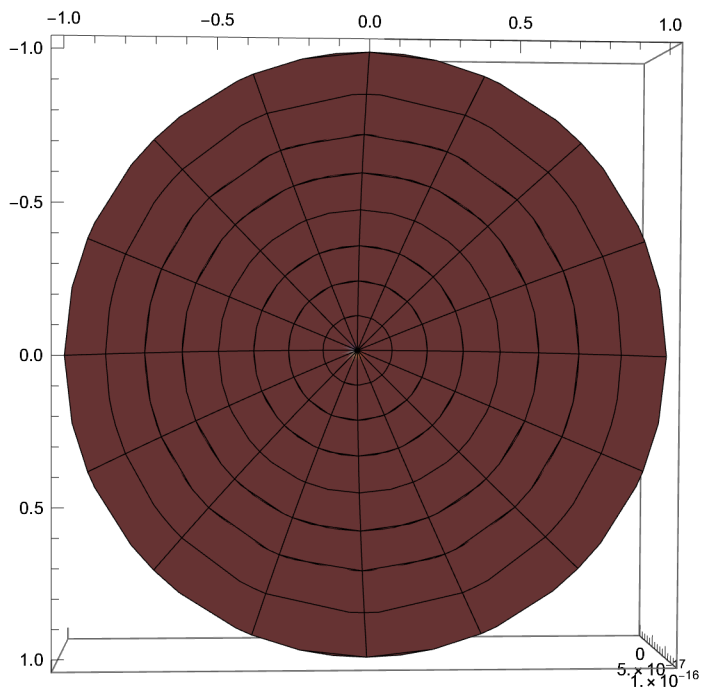
RevolutionPlot3D $\left[\left\{-\frac{c \sqrt{\theta}}{\sqrt{4 \pi-\theta}}, \frac{c \sqrt{\theta}}{\sqrt{4 \pi-\theta}}\right\},\{\theta,-3 \pi, 3 \pi\}\right]$



Solve $\left[\frac{\sqrt{r} \sqrt{1-\frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{c^2}}}} \sqrt{4 \pi r-r \theta}}{2 \pi}==c(\theta /(2 \pi)), \theta\right]$

$\left\{\left\{\theta \rightarrow 0\right\},\left\{\theta \rightarrow \frac{4 \pi r^2}{c^2+r^2}\right\}\right\}$

RevolutionPlot3D $\left[\frac{4 \pi r^2}{c^2 + r^2}, \{r, -1, 1\}\right]$



$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == c (\theta / (2 \pi)), v\right]$$

$$\left\{ \left\{ v \rightarrow - \frac{1. \sqrt{-1.12941 \times 10^{18} r^2 + 8.07761 \times 10^{33} \theta + 8.98755 \times 10^{16} r^2 \theta}}{\sqrt{-12.5664 r^2 + 8.98755 \times 10^{16} \theta + r^2 \theta}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} r^2 + 8.07761 \times 10^{33} \theta + 8.98755 \times 10^{16} r^2 \theta}}{\sqrt{-12.5664 r^2 + 8.98755 \times 10^{16} \theta + r^2 \theta}} \right\} \right\}$$



```

RevolutionPlot3D[{- (1. `  $\sqrt{-1.1294090667581471` * ^{18} r^2 +$   

 $8.07760871306249` * ^{33} \theta + 8.987551787368176` * ^{16} r^2 \theta}$ ) ) /  

 $\left( \sqrt{-12.566370614359172` r^2 + 8.987551787368176` * ^{16} \theta + r^2 \theta} \right),$   

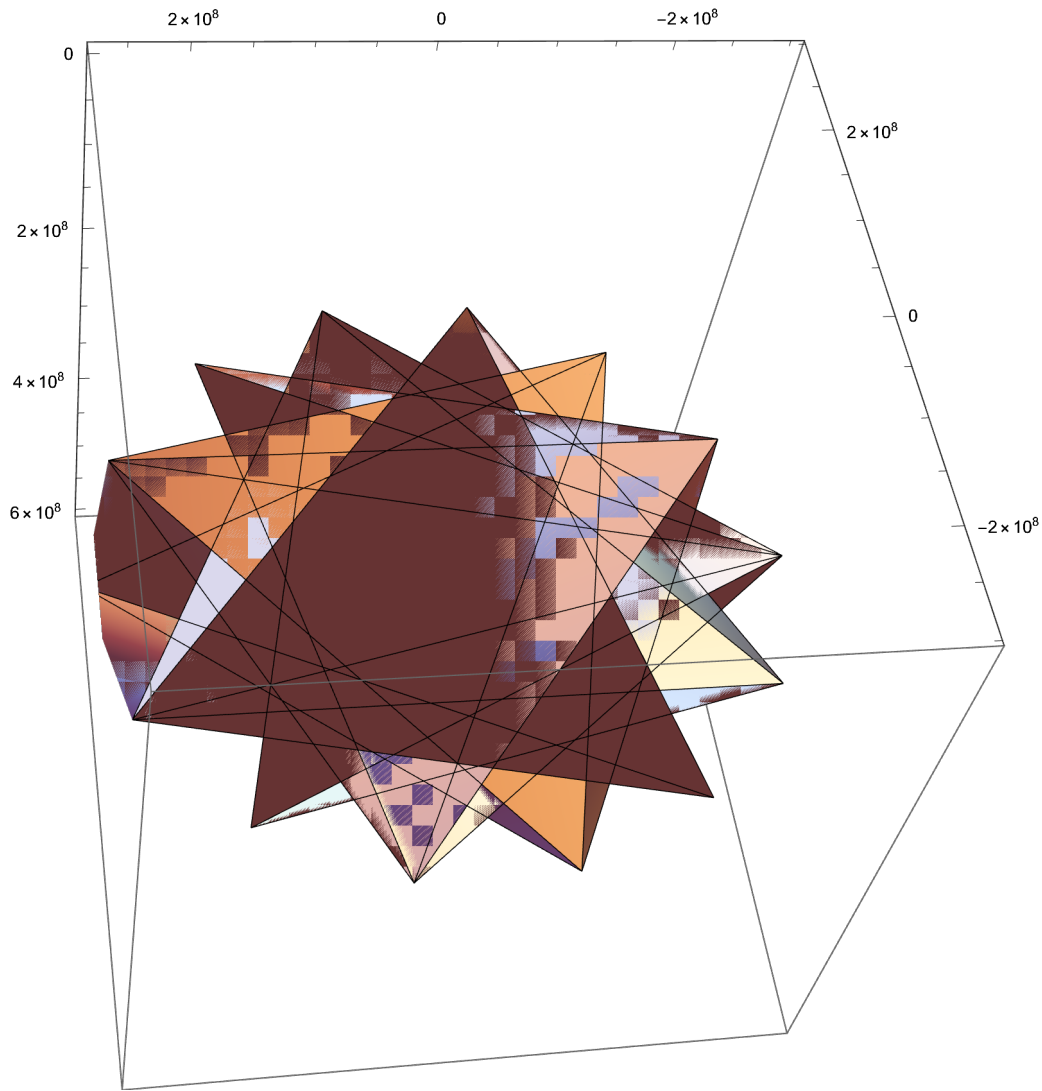
 $\left( \sqrt{-1.1294090667581471` * ^{18} r^2 + 8.07760871306249` * ^{33} \theta +$   

 $8.987551787368176` * ^{16} r^2 \theta} \right) /$   

 $\left( \sqrt{-12.566370614359172` r^2 + 8.987551787368176` * ^{16} \theta + r^2 \theta} \right) \},$   

{r, -100, 100}, { $\theta$ , -40  $\pi$ , 40  $\pi$ }]

```



$$\text{Solve}[r' * \theta' == 2 \pi r' - 2 \pi \sqrt{r'^2 - \eta'^2}, \eta'] \quad (175)$$

$$\left\{ \left\{ \eta' \rightarrow -\frac{\sqrt{4 \pi r'^2 \theta - r'^2 \theta'^2}}{2 \pi} \right\}, \left\{ \eta' \rightarrow \frac{\sqrt{4 \pi r'^2 \theta - r'^2 \theta'^2}}{2 \pi} \right\} \right\} \quad (176)$$

$$\eta' = \eta = \frac{\sqrt{4\pi r'^2 \theta - r'^2 \theta'^2}}{2\pi} == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \quad (177)$$

$$\frac{\sqrt{4\pi r'^2 \theta - r'^2 \theta'^2}}{2\pi} = \frac{1}{2\pi} \left( \sqrt{\left( 4\pi \left( r \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)^2 \left( \theta / \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) - \right.} \right. \\ \left. \left. \left( r \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)^2 \left( \theta \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)^2 \right) \right)$$

$$\frac{1}{2\pi} \left( \sqrt{\left( 4\pi \left( r \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)^2 \left( \theta / \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) - \right.} \right. \\ \left. \left. \left( r \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)^2 \left( \theta \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)^2 \right) \right)$$

$$\text{Solve} \left[ \frac{\sqrt{4\pi r^2 \sqrt{1 - \frac{v^2}{c^2}} \theta - r^2 \left( 1 - \frac{v^2}{c^2} \right)^2 \theta^2}}{2\pi} == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, v \right]$$

$$\left\{ \{v \rightarrow 0\}, \left\{ v \rightarrow -\sqrt{\left( \frac{4c^2}{3} - (4c^4 \pi \theta) \right) / \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - \right.} \right. \right. \\ \left. \left. \left. c^6 \theta^6 + 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} + (2c^4 \theta^2) \right\} / \right. \\ \left. \left( 3 \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) + \right. \\ \left. \frac{1}{3\theta^2} 2 \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right\},$$

$$\left\{ v \rightarrow \sqrt{\left( \frac{4c^2}{3} - (4c^4 \pi \theta) \right) / \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + \right.} \right. \\ \left. \left. 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} + (2c^4 \theta^2) \right\} / \\ \left( 3 \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) + \\ \frac{1}{3\theta^2} 2 \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \Bigg\},$$

$$\left\{ v \rightarrow -\sqrt{\left( \frac{4c^2}{3} + (2c^4 \pi \theta) \right) / \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + \right.} \right. \\ \left. \left. 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - (2\sqrt{3}c^4 \pi \theta) \right\} / \\ \left( -27c^6 \pi^2 \theta^4 + 9c^6 \pi \theta^5 - c^6 \theta^6 + 3\sqrt{3}\pi \sqrt{27c^{12} \pi^2 \theta^8 - 10c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} -$$

$$\begin{aligned}
& \left( c^4 \theta^2 \right) / \left( 3 \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) + \left( i c^4 \theta^2 \right) / \\
& \quad \left( \sqrt{3} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) - \\
& \quad \frac{1}{3 \theta^2} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - \\
& \quad \frac{1}{\sqrt{3} \theta^2} \\
& \quad i \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \Bigg\}, \\
\left\{ v \rightarrow \sqrt{\left( \frac{4 c^2}{3} + (2 c^4 \pi \theta) / \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - (2 i \sqrt{3} c^4 \pi \theta) / \right. \\
& \quad \left. \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - \right. \\
& \quad \left. \left( c^4 \theta^2 \right) / \left( 3 \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) + \left( i c^4 \theta^2 \right) / \\
& \quad \left( \sqrt{3} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) - \\
& \quad \frac{1}{3 \theta^2} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - \\
& \quad \frac{1}{\sqrt{3} \theta^2} \\
& \quad i \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \Bigg\}, \\
\left\{ v \rightarrow -\sqrt{\left( \frac{4 c^2}{3} + (2 c^4 \pi \theta) / \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} + (2 i \sqrt{3} c^4 \pi \theta) / \right. \\
& \quad \left. \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - \right. \\
& \quad \left. \left( c^4 \theta^2 \right) / \left( 3 \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) - \left( i c^4 \theta^2 \right) / \\
& \quad \left( \sqrt{3} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) - \\
& \quad \frac{1}{3 \theta^2} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{\sqrt{3} \theta^2} \\
& \left\{ \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right\}, \\
& \left\{ v \rightarrow \sqrt{\left( \frac{4 c^2}{3} + (2 c^4 \pi \theta) \right) / \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right.} \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} + (2 i \sqrt{3} c^4 \pi \theta) / \right. \\
& \quad \left. \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} - \right. \\
& \quad \left. (c^4 \theta^2) / \left( 3 \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + \right. \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) - (i c^4 \theta^2) / \right. \\
& \quad \left. \left( \sqrt{3} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right) - \right. \\
& \quad \left. \frac{1}{3 \theta^2} \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} + \right. \\
& \quad \left. \frac{1}{\sqrt{3} \theta^2} \right. \\
& \quad \left. \left. \left( -27 c^6 \pi^2 \theta^4 + 9 c^6 \pi \theta^5 - c^6 \theta^6 + 3 \sqrt{3} \pi \sqrt{27 c^{12} \pi^2 \theta^8 - 10 c^{12} \pi \theta^9 + c^{12} \theta^{10}} \right)^{1/3} \right\} \right\} \\
& r' / t' = \left( r \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) / \left( 2 \pi \theta / \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) = \frac{r \left( 1 - \frac{v^2}{c^2} \right)}{2 \pi \theta} \quad (178)
\end{aligned}$$

$$c := (2.99792458 * 10^8) \quad (179)$$

$$c := (2.99792458 * 10^8)$$

From a first derivative with respect to time can be found through theta and set equal to the distance of a wavelength over time.

$$\frac{r \left( 1 - \frac{v^2}{c^2} \right)}{2 \pi \theta} = (1 / 2 \pi) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] = \frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \quad (180)$$

$$(1 / 2 \pi) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta, r \right]$$

$$\frac{1}{2} \pi \partial_1 \frac{4 \pi - 2 \theta}{4 \pi \sqrt{4 \pi \theta - \theta^2}}$$

$$(1/2\pi) D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right]$$

$$\frac{4\pi r^2 - 2r^2\theta}{8\sqrt{4\pi r^2\theta - r^2\theta^2}}$$

$$\left(r\sqrt{1 - \left(\frac{v}{c}\right)^2}\right) / \left((2\pi\theta) / \sqrt{1 - \left(\frac{v}{c}\right)^2}\right)$$

$$\frac{r\left(1 - \frac{v^2}{c^2}\right)}{2\pi\theta}$$

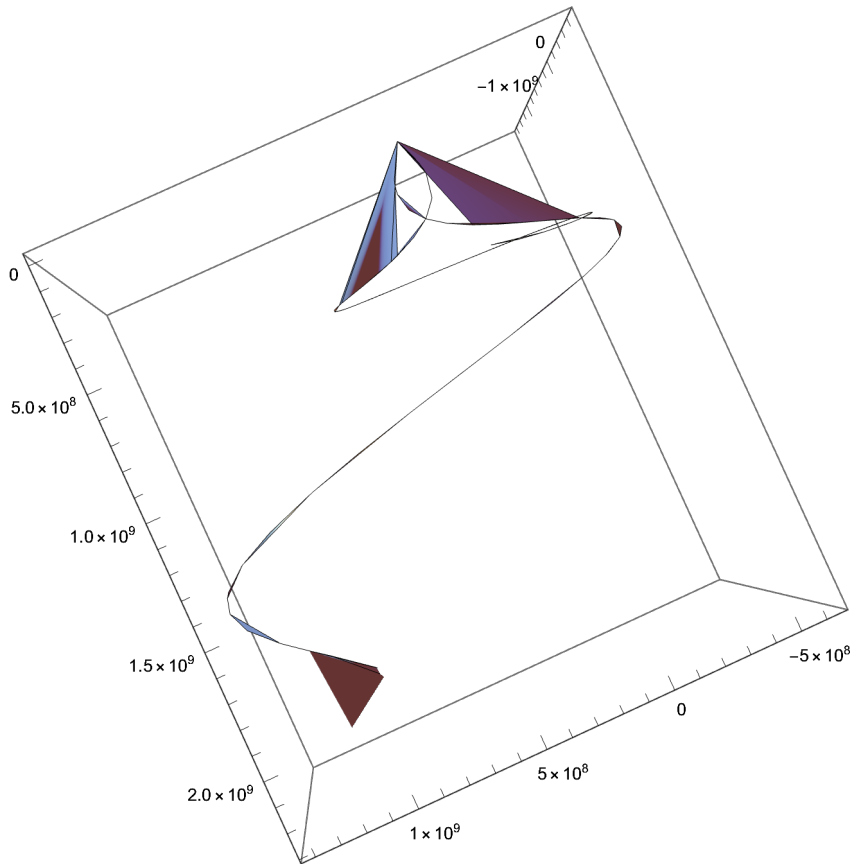
Solve[

$$\left(r\sqrt{1 - \left(\frac{v}{c}\right)^2}\right) / \left((2\pi\theta) / \sqrt{1 - \left(\frac{v}{c}\right)^2}\right) == \frac{4\pi r^2 - 2r^2\theta}{8\sqrt{4\pi r^2\theta - r^2\theta^2}}, v]$$

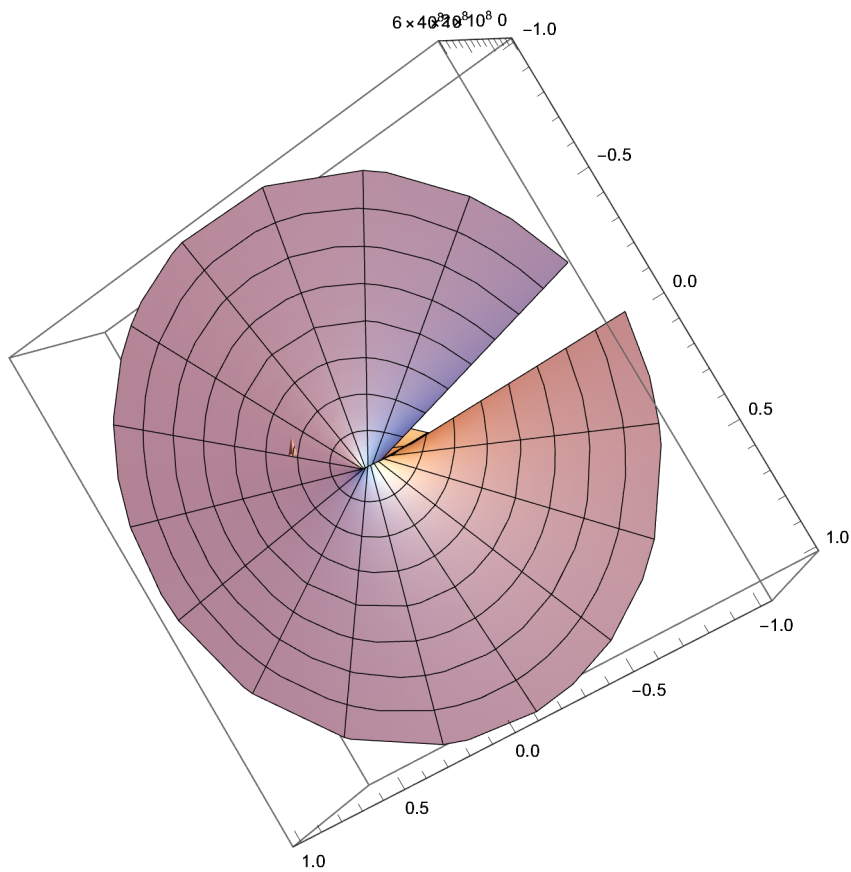
$$\left\{\left\{v \rightarrow -\frac{\sqrt{2c^2 - \frac{2c^2\pi^2 r\theta}{\sqrt{r^2(4\pi-\theta)\theta}} + \frac{c^2\pi r\theta^2}{\sqrt{r^2(4\pi-\theta)\theta}}}}{\sqrt{2}}\right\}, \left\{v \rightarrow \frac{\sqrt{2c^2 - \frac{2c^2\pi^2 r\theta}{\sqrt{r^2(4\pi-\theta)\theta}} + \frac{c^2\pi r\theta^2}{\sqrt{r^2(4\pi-\theta)\theta}}}}{\sqrt{2}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\left\{-\frac{\sqrt{2\,c^2-\frac{2\,c^2\,\pi^2\,r\,\theta}{\sqrt{r^2\,(4\,\pi-\theta)}\,\theta}+\frac{c^2\,\pi\,r\,\theta^2}{\sqrt{r^2\,(4\,\pi-\theta)}\,\theta}}}{\sqrt{2}}\right\},\{r,-1,1\},\{\theta,-4\,\pi,4\,\pi\}\right]$$

$$\left(\frac{\sqrt{2\,c^2-\frac{2\,c^2\,\pi^2\,r\,\theta}{\sqrt{r^2\,(4\,\pi-\theta)}\,\theta}+\frac{c^2\,\pi\,r\,\theta^2}{\sqrt{r^2\,(4\,\pi-\theta)}\,\theta}}}{\sqrt{2}}\right),\{r,-1,1\},\{\theta,-4\,\pi,4\,\pi\}]$$



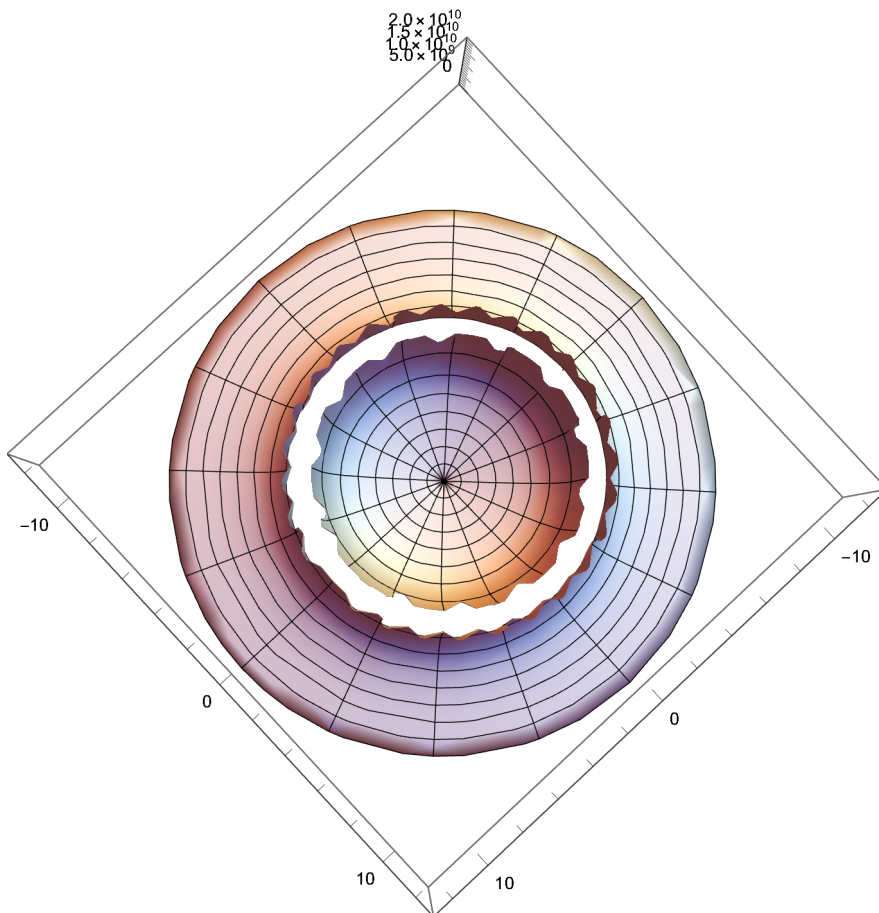
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == c, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{c \sqrt{64 \pi - 16 \theta} \sqrt{\theta}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}, \left\{r \rightarrow \frac{c \sqrt{64 \pi - 16 \theta} \sqrt{\theta}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}\right\}\right\}$$

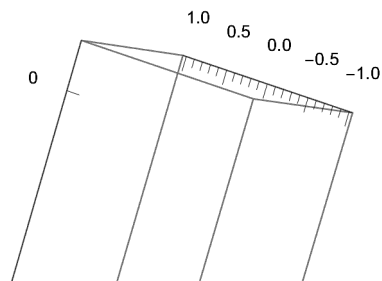
$\text{RevolutionPlot3D}\left[\frac{c \sqrt{64 \pi - 16 \theta} \sqrt{\theta}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{\theta, -4 \pi, 4 \pi\}\right]$



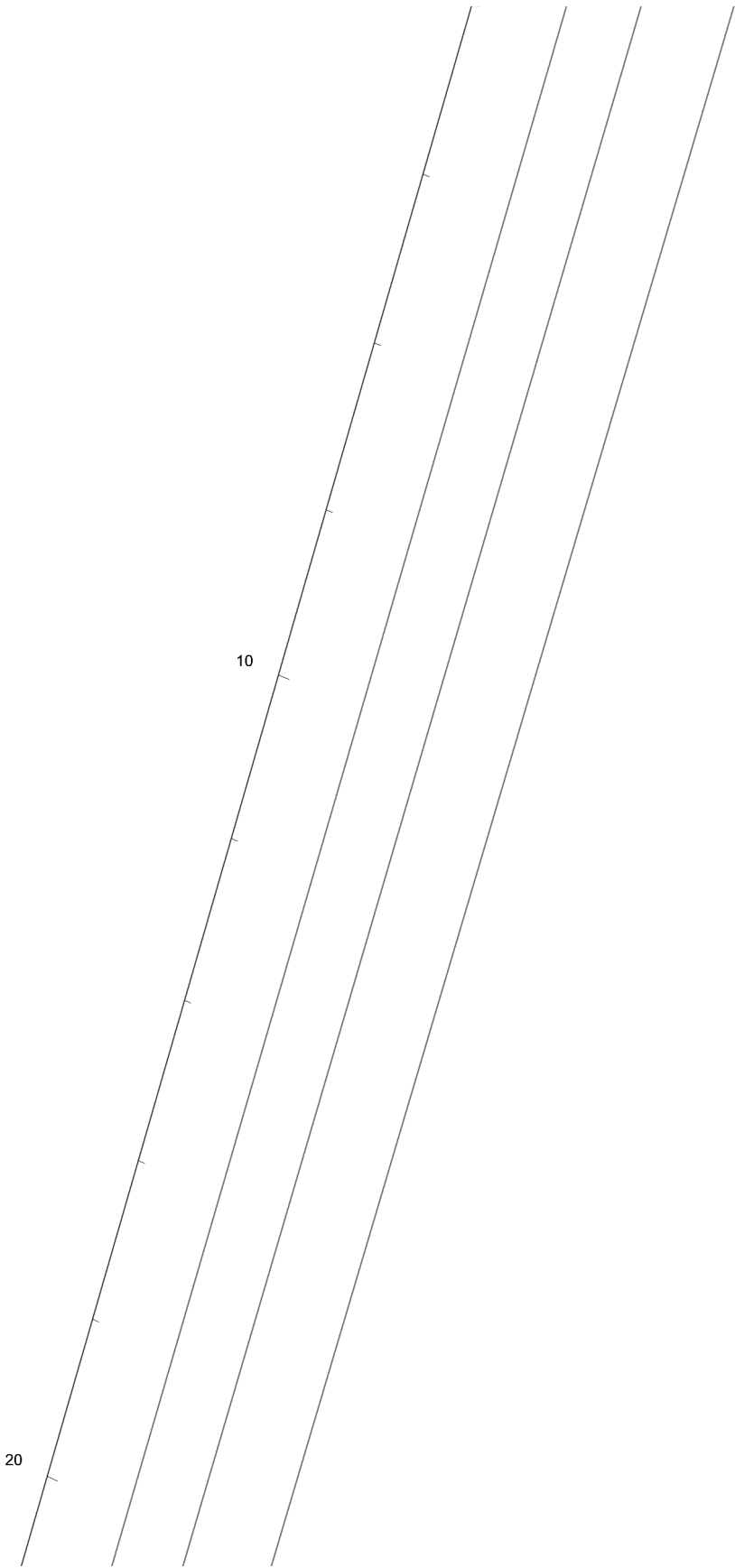
$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = c, \theta\right]$

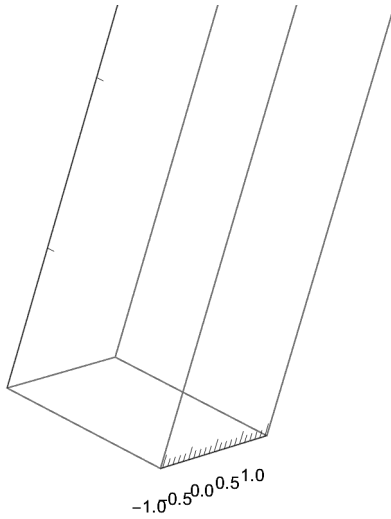
$\left\{\left\{\theta \rightarrow \frac{2 \pi \left(16 c^2 + r^2 - 4 \sqrt{16 c^4 + c^2 r^2}\right)}{16 c^2 + r^2}\right\}, \left\{\theta \rightarrow \frac{2 \pi \left(16 c^2 + r^2 + 4 \sqrt{16 c^4 + c^2 r^2}\right)}{16 c^2 + r^2}\right\}\right\}$

$\text{RevolutionPlot3D}\left[\left\{\frac{2 \pi \left(16 c^2 + r^2 - 4 \sqrt{16 c^4 + c^2 r^2}\right)}{16 c^2 + r^2}, \frac{2 \pi \left(16 c^2 + r^2 + 4 \sqrt{16 c^4 + c^2 r^2}\right)}{16 c^2 + r^2}\right\}, \{r, -1, 1\}\right]$









$$\text{Solve}\left[\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}} == c, r\right]$$

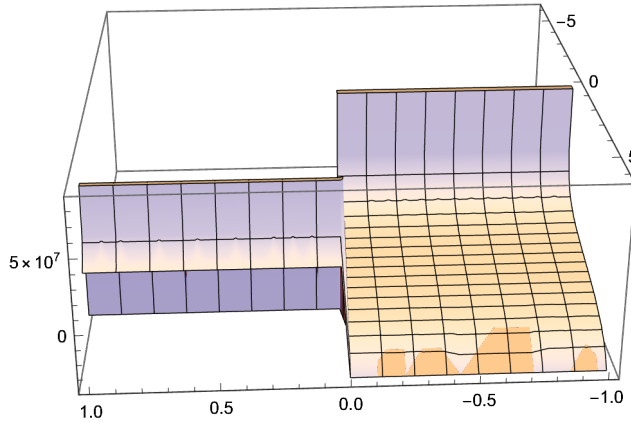
{}

$$\text{Solve}\left[\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}} == c, \theta\right]$$

{{ $\theta \rightarrow 2 \pi$ }}

$$\begin{aligned} & ((1 / (2 \pi))) D\left[\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}}, \theta\right] \\ & - \frac{2 c^2 \pi^2 r}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi^2 r \theta (r^2 (4 \pi - \theta) - r^2 \theta)}{(r^2 (4 \pi - \theta) \theta)^{3/2}} - \frac{c^2 \pi r \theta^2 (r^2 (4 \pi - \theta) - r^2 \theta)}{2 (r^2 (4 \pi - \theta) \theta)^{3/2}} \\ & \frac{4 \sqrt{2} \pi \sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{r^2 (4 \pi - \theta) \theta}} \end{aligned}$$

$$\text{SphericalPlot3D}\left[\frac{-\frac{2c^2\pi^2r}{\sqrt{r^2(4\pi-\theta)\theta}} + \frac{2c^2\pi r\theta}{\sqrt{r^2(4\pi-\theta)\theta}} + \frac{c^2\pi^2r\theta(r^2(4\pi-\theta)-r^2\theta)}{(r^2(4\pi-\theta)\theta)^{3/2}} - \frac{c^2\pi r\theta^2(r^2(4\pi-\theta)-r^2\theta)}{2(r^2(4\pi-\theta)\theta)^{3/2}}}{4\sqrt{2}\pi\sqrt{2c^2 - \frac{2c^2\pi^2r\theta}{\sqrt{r^2(4\pi-\theta)\theta}} + \frac{c^2\pi r\theta^2}{\sqrt{r^2(4\pi-\theta)\theta}}}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$(1/2\pi) D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, r, \theta\right]$$

$$\frac{1}{2}\pi\left(-\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right)$$

$$\frac{r\left(1 - \frac{(\theta r)^2}{c^2}\right)}{2\pi\theta} = (1/2\pi) D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, r, \theta\right] = \frac{4\pi r^2 - 2r^2\theta}{8\sqrt{4\pi r^2\theta - r^2\theta^2}} \quad (181)$$

$$\text{Solve}\left[\frac{1}{2}\pi\left(-\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right) == \frac{r\left(1 - \frac{(\theta r - 2\pi r)/(2\pi)^2}{c^2}\right)}{2\pi\theta}, r\right]$$

$$\text{RevolutionPlot3D}\left[\left\{\left(-\sqrt{\left(-\frac{128c^2\pi^5}{3(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)} + \frac{160c^2\pi^4\theta}{3(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)} - \frac{64c^2\pi^3\theta^2}{3(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)} + \frac{8c^2\pi^2\theta^3}{3(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)} + (4096 \times 2^{1/3} c^4 \pi^{10}) / \left(3(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)\right)\right\}, r\right]$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3} + \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384 \right. \\
& \quad c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \left. \right)^2 \left. \right)^{1/3} \left. \right) - \\
& \quad (10\,240 \times 2^{1/3} c^4 \pi^9 \theta) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \\
& \quad 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \left. \right)^3} + \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \left. \right)^2 \left. \right)^{1/3} \left. \right) + \\
& \quad (10\,496 \times 2^{1/3} c^4 \pi^8 \theta^2) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \\
& \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 5632 \times 2^{1/3} c^4 \pi^7 \theta^3 \right) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad \left. 108 c^4 \pi^6 \theta^{13} + \sqrt{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \right. \right. \\
& \quad \left. \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \right. \right. \\
& \quad \left. \left. \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& \left( 1664 \times 2^{1/3} c^4 \pi^6 \theta^4 \right) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad \left. 108 c^4 \pi^6 \theta^{13} + \sqrt{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \right. \right. \\
& \quad \left. \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \right. \right. \\
& \quad \left. \left. \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \right. \right.
\end{aligned}$$

$$\begin{aligned}
& c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \Big)^2 \Big)^{1/3} \Big) - \\
& (256 \times 2^{1/3} c^4 \pi^5 \theta^5) \Big/ \Big( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \\
& \Big( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \pi^{13} \theta^2 + \\
& 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - \\
& 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + \\
& 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \\
& (524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \\
& \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \\
& 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 \\
& c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \Big)^2 \Big)^{1/3} \Big) + \\
& (16 \times 2^{1/3} c^4 \pi^4 \theta^6) \Big/ \Big( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \\
& \Big( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \pi^{13} \theta^2 + \\
& 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - \\
& 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + \\
& 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \\
& (524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \\
& \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \\
& 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 \\
& c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \Big)^2 \Big)^{1/3} \Big) + \\
& \Big( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \pi^{13} \theta^2 + \\
& 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 -
\end{aligned}$$

$$\begin{aligned}
& 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + \right. \right. \\
& \quad \left. \left. 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - \right. \right. \\
& \quad \left. \left. 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \right. \\
& \quad \left. \left. 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \right. \right. \\
& \quad \left. \left. 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\right. \right. \\
& \quad \left. \left. c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \right. \\
& \quad \left. \left. 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\right)^{1/3} \Bigg/ \\
& \left. \left(3 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right)\right), \\
& \left(\sqrt{\left(-\frac{128\,c^2\pi^5}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \right. \right. \\
& \quad \frac{160\,c^2\pi^4\theta}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} - \\
& \quad \frac{64\,c^2\pi^3\theta^2}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \\
& \quad \left.\frac{8\,c^2\pi^2\theta^3}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \right. \\
& \quad \left. (4096 \times 2^{1/3} \right. \\
& \quad \left. c^4\pi^{10}) \Bigg/ \right. \\
& \left. \left(3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right) \right. \right. \\
& \quad \left. \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \right. \\
& \quad \left. \left. 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \right. \\
& \quad \left. \left. 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \right. \\
& \quad \left. \left. 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \right. \\
& \quad \left. \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \right. \\
& \quad \left. \left. c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13})^2)^{1/3}) - \\
& (10\,240 \times 2^{1/3}\,c^4\pi^9\theta) / \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \\
& \quad \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \\
& \quad 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. \left. 108\,c^4\pi^6\theta^{13} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3}) + \\
& (10\,496 \times 2^{1/3}\,c^4\pi^8\theta^2) / \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \\
& \quad \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \\
& \quad 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. \left. 108\,c^4\pi^6\theta^{13} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3}) - \\
& (5632 \times 2^{1/3}\,c^4\pi^7\theta^3) / \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 +
\end{aligned}$$



$$\begin{aligned}
& 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - \\
& 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - \\
& 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - \\
& 108c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632c^4\pi^7\theta^3 - 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \right. \\
& \quad \left.5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} + \\
& (1664 \times 2^{1/3}c^4\pi^6\theta^4) \bigg/ \left(3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right. \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - \right. \\
& \quad \left.14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - \right. \\
& \quad \left.1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632c^4\pi^7\theta^3 - 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6\right)^3 + \left. \right. \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \right. \\
& \quad \left.5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& (256 \times 2^{1/3}c^4\pi^5\theta^5) \bigg/ \left(3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right. \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - \right. \\
& \quad \left.14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - \right. \\
& \quad \left.1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632c^4\pi^7\theta^3 - 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6\right)^3 + \left. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \Big)^{1/3} \Big) + \\
& (16 \times 2^{1/3} c^4 \pi^4 \theta^6) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \right. \\
& \quad \left. \left. c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \right. \\
& \quad \left. \left. 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \right)^{1/3} \Big) + \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \\
& \quad 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \\
& \quad 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \\
& \quad \theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \right)^{1/3} \Big) /
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \times 2^{1/3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \Bigg), \\
& \left( -\sqrt[3]{\left( -\frac{128 c^2 \pi^5}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} + \right. \right. \\
& \quad \frac{160 c^2 \pi^4 \theta}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} - \\
& \quad \frac{64 c^2 \pi^3 \theta^2}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} + \\
& \quad \left. \frac{8 c^2 \pi^2 \theta^3}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} - \right. \\
& \quad \left. \left( 2048 \times 2^{1/3} c^4 \pi^{10} \right) \right) / \\
& \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt[3]{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \right. \\
& \quad \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3} + \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Bigg) + \\
& \left( 2048 \pm 2^{1/3} c^4 \pi^{10} \right) / \left( \sqrt[3]{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt[3]{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \right. \\
& \quad \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3} +
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \\
& \quad c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \Big)^{1/3} \Big) + \\
& (5120 \times 2^{1/3} c^4 \pi^9 \theta) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \right)^{1/3} \Big) - \\
& (5120 \pm 2^{1/3} c^4 \pi^9 \theta) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \Big)^{1/3} \Big) - \\
& \left( 5248 \times 2^{1/3}\,c^4\,\pi^8\,\theta^2 \right) / \left( 3 \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& \quad 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - \\
& \quad 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 30\,72\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - \\
& \quad 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - \\
& \quad 108\,c^4\,\pi^6\,\theta^{13} + \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + \right. \\
& \quad \left. 5632\,c^4\,\pi^7\,\theta^3 - 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6 \right)^3} + \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& \quad 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \\
& \quad 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 30\,72\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - \\
& \quad 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \\
& \quad \left. \left. 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& \left( 5248 \pm 2^{1/3}\,c^4\,\pi^8\,\theta^2 \right) / \left( \sqrt{3} \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& \quad 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - \\
& \quad 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 30\,72\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - \\
& \quad 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - \\
& \quad 108\,c^4\,\pi^6\,\theta^{13} + \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + \right. \\
& \quad \left. 5632\,c^4\,\pi^7\,\theta^3 - 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6 \right)^3} + \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& \quad 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \\
& \quad 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 30\,72\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - \\
& \quad 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \\
& \quad \left. \left. 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& \left( 2816 \times 2^{1/3}\,c^4\,\pi^7\,\theta^3 \right) / \left( 3 \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 -
\end{aligned}$$

$$\begin{aligned}
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \left.\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& (2816 \pm 2^{1/3}c^4\pi^7\theta^3) \bigg/ \left( \sqrt{3} \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \\
& \quad \left. 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \\
& \quad \left. 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \left.\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& (832 \times 2^{1/3}c^4\pi^6\theta^4) \bigg/ \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \\
& \quad \left. 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \\
& \quad \left. 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right.
\end{aligned}$$

$$\begin{aligned}
& \pi^{13} \theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \\
& 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13})^2)^{1/3}) + \\
& (832 \pm 2^{1/3}\,c^4\pi^6\theta^4) / \left( \sqrt{3} \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \\
& 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \\
& \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \\
& 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13})^2)^{1/3}) + \\
& (128 \times 2^{1/3}\,c^4\pi^5\theta^5) / \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \\
& 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \\
& \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \\
& 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13})^2)^{1/3}) -
\end{aligned}$$

$$\begin{aligned}
& (128 \pm 2^{1/3} c^4 \pi^5 \theta^5) / \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \\
& \quad 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 +} \\
& \quad \left. (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13})^2 \right)^{1/3} \Big) - \\
& (8 \times 2^{1/3} c^4 \pi^4 \theta^6) / \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \\
& \quad 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 +} \\
& \quad \left. (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13})^2 \right)^{1/3} \Big) + \\
& (8 \pm 2^{1/3} c^4 \pi^4 \theta^6) / \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 -
\end{aligned}$$



$$\begin{aligned}
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left.\sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + \right.\right.\right. \\
& \quad \left.256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - \right. \\
& \quad \left.1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \\
& \quad \left.3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \right. \\
& \quad \left.37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left.27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left.3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left.293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} \bigg/ \\
& \left(6 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) - \\
& \left(\text{ii} \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right.\right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} \bigg/ \\
& \left(6 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) -
\end{aligned}$$

$$\begin{aligned}
& \left( c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \right. \\
& \left. 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \Big)^{1/3} \Big) / \\
& \left( 2 \times 2^{1/3} \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \Big) \Big) \Big) , \\
& \left( \sqrt[3]{ \left( - \frac{128 c^2 \pi^5}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} + \right. \right. \\
& \frac{160 c^2 \pi^4 \theta}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} - \\
& \frac{64 c^2 \pi^3 \theta^2}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} + \\
& \left. \frac{8 c^2 \pi^2 \theta^3}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} - \right. \\
& \left. \left( 2048 \times \right. \right. \\
& \quad 2^{1/3} \\
& \quad c^4 \\
& \quad \left. \pi^{10} \right) / \\
& \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + \right. \\
& \quad 3244032 c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - \\
& \quad 24440832 c^4 \pi^{16} \theta^3 + 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - \\
& \quad 743424 c^6 \pi^{10} \theta^5 - 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + \\
& \quad 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + \\
& \quad 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + \\
& \quad 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \quad \left. \sqrt[3]{ \left( 4 \left( -4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right) \right)^3 + } \\
& \quad \left( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& \quad 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& \quad 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \\
& \quad 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + \\
& \quad 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right) \Big)^{1/3} \Big) + \\
& \left( 2048 \pm 2^{1/3} c^4 \pi^{10} \right) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \quad \left( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + \right. \\
& \quad \left. 3244032 c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - \right.
\end{aligned}$$

$$\begin{aligned}
& 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.\left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}} + \\
& (5120 \times 2^{1/3} c^4 \pi^9 \theta) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.\left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}} - \\
& (5120 \pm 2^{1/3} c^4 \pi^9 \theta) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} +
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(4 \left(-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6\right)^3 + \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad \left. c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \right. \\
& \quad \left. 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \right. \\
& \quad \left. 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \right. \\
& \quad \left. 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + \right. \\
& \quad \left. 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \right. \\
& \quad \left. \left. 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13}\right)^2\right)^{1/3} - \\
& (5248 \times 2^{1/3} c^4 \pi^8 \theta^2) / \left(3 \left(-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5\right) \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + \right. \\
& \quad \left. 3244032 c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - \right. \\
& \quad \left. 24440832 c^4 \pi^{16} \theta^3 + 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - \right. \\
& \quad \left. 743424 c^6 \pi^{10} \theta^5 - 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + \right. \\
& \quad \left. 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + \right. \\
& \quad \left. 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + \right. \\
& \quad \left. 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \right. \\
& \quad \left. \sqrt{\left(4 \left(-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6\right)^3 + \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad \left. c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \right. \\
& \quad \left. 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \right. \\
& \quad \left. 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \right. \\
& \quad \left. 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + \right. \\
& \quad \left. 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \right. \\
& \quad \left. \left. 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13}\right)^2\right)^{1/3} + \\
& (5248 \pm 2^{1/3} c^4 \pi^8 \theta^2) / \left(\sqrt{3} \left(-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5\right) \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + \right. \\
& \quad \left. 3244032 c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - \right. \\
& \quad \left. 24440832 c^4 \pi^{16} \theta^3 + 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - \right. \\
& \quad \left. 743424 c^6 \pi^{10} \theta^5 - 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + \right. \\
& \quad \left. 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + \right. \\
& \quad \left. 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + \right. \\
& \quad \left. 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \right. \\
& \quad \left. \sqrt{\left(4 \left(-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6\right)^3 + \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad \left. c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \\
& 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \\
& 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \\
& 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13} \Big)^{1/3} \Big) + \\
& (2816 \times 2^{1/3} c^4 \pi^7 \theta^3) / \left( 3 (-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5) \right. \\
& \quad \left( 524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + \right. \\
& \quad 3244032c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - \\
& \quad 24440832c^4\pi^{16}\theta^3 + 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - \\
& \quad 743424c^6\pi^{10}\theta^5 - 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + \\
& \quad 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + \\
& \quad 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + \\
& \quad 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + 5632c^4\pi^7\theta^3 - \right. \\
& \quad \left. 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6)^3} + \right. \\
& \quad \left. (524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032 \right. \\
& \quad c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \\
& \quad 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& \quad 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \\
& \quad 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \\
& \quad 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \\
& \quad \left. 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13})^2 \right)^{1/3} \Big) - \\
& (2816 \pm 2^{1/3} c^4 \pi^7 \theta^3) / \left( \sqrt{3} (-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5) \right. \\
& \quad \left( 524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + \right. \\
& \quad 3244032c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - \\
& \quad 24440832c^4\pi^{16}\theta^3 + 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - \\
& \quad 743424c^6\pi^{10}\theta^5 - 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + \\
& \quad 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + \\
& \quad 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + \\
& \quad 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + 5632c^4\pi^7\theta^3 - \right. \\
& \quad \left. 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6)^3} + \right. \\
& \quad \left. (524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032 \right. \\
& \quad c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \\
& \quad 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& \quad 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \\
& \quad 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \\
& \quad \left. 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \Big)^{1/3} \Big) - \\
& (832 \times 2^{1/3} c^4 \pi^6 \theta^4) / \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right. \right. \\
& \quad \left. \left. 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \right. \\
& \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\, \right. \right. \\
& \quad \left. \left. c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \right. \\
& \quad \left. \left. 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& (832 \pm 2^{1/3} c^4 \pi^6 \theta^4) / \left( \sqrt{3} \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right. \right. \\
& \quad \left. \left. 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \right. \\
& \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\, \right. \right. \\
& \quad \left. \left. c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \right. \\
& \quad \left. \left. 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& (128 \times 2^{1/3} c^4 \pi^5 \theta^5) / \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right.
\end{aligned}$$

$$\begin{aligned}
& 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}} - \\
& (128 \pm 2^{1/3}\,c^4\pi^5\theta^5) \bigg/ \left( \sqrt{3} \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left. (524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \right. \\
& \quad \left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}} - \\
& (8 \times 2^{1/3}\,c^4\pi^4\theta^6) \bigg/ \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \\
& \quad \left. (524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 +
\end{aligned}$$

$$\begin{aligned}
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}} + \\
& \left(8 \pm 2^{1/3}\,c^4\pi^4\theta^6\right) / \left(\sqrt{3}\left(-64\,\pi^5 + 144\,\pi^4\theta - 128\,\pi^3\theta^2 + 56\,\pi^2\theta^3 - 12\,\pi\theta^4 + \theta^5\right)\right. \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad \left.3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \right. \\
& \quad \left.24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \right. \\
& \quad \left.743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left.27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left.3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left.293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \right. \\
& \quad \left.\sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right.\right. \\
& \quad \left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left.\right. \\
& \quad \left.\left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right.\right. \\
& \quad \left.\left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right.\right. \\
& \quad \left.\left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right.\right. \\
& \quad \left.\left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right.\right. \\
& \quad \left.\left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right.\right. \\
& \quad \left.\left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right.\right. \\
& \quad \left.\left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\right)^{1/3}} - \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \right. \\
& \quad \left.24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \right. \\
& \quad \left.37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left.27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \\
& \quad \left.14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \\
& \quad \left.1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \right. \\
& \quad \left.\sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left.\right.
\end{aligned}$$



$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \\
& \quad \theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^{1/3} \Big/ \\
& \left( 6 \times 2^{1/3} \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right) - \\
& \left( \pm \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right. \right. \\
& \quad \left. \left. 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032 \right. \right. \\
& \quad c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big/ \\
& \left. \left( 2 \times 2^{1/3} \sqrt{3} \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right) \right) \Bigg), \\
& \left( -\sqrt{\left( -\frac{128\,c^2\pi^5}{3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right)} + \right. \right. \\
& \quad \frac{160\,c^2\pi^4\theta}{3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right)} - \\
& \quad \frac{64\,c^2\pi^3\theta^2}{3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right)} + \\
& \quad \left. \frac{8\,c^2\pi^2\theta^3}{3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right)} - \right. \\
& \quad \left. \left( 2048 \times 2^{1/3} c^4\pi^{10} \right) \Big/ \right. \\
& \quad \left. \left( 3 \left( -64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5 \right) \right. \right. \\
& \quad \left. \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \\
& \quad \left. \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\right)^{1/3}} - \\
& (2048 \pm 2^{1/3} c^4 \pi^{10}) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \right. \\
& \quad \left. \left. 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \right. \\
& \quad \left. \left. 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \right. \\
& \quad \left. \left. 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \right. \right. \\
& \quad \left. \left. \left. \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \right. \right. \\
& \quad \left. \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \right. \\
& \quad \left. \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \right. \\
& \quad \left. \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \right. \\
& \quad \left. \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\right. \right. \right. \\
& \quad \left. \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \right. \\
& \quad \left. \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\right)^{1/3}\right) + \\
& (5120 \times 2^{1/3} c^4 \pi^9 \theta) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \right. \\
& \quad \left. \left. 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \right. \\
& \quad \left. \left. 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \right. \\
& \quad \left. \left. 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \\
& \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Bigg) + \\
& (5120 \pm 2^{1/3} c^4 \pi^9 \theta) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad \left. 108 c^4 \pi^6 \theta^{13} + \sqrt{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \right. \right. \\
& \quad \left. \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \right. \right. \\
& \quad \left. \left. \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Bigg) - \\
& (5248 \times 2^{1/3} c^4 \pi^8 \theta^2) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad \left. 108 c^4 \pi^6 \theta^{13} + \sqrt{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \right. \right. \\
& \quad \left. \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \right. \right. \\
& \quad \left. \left. \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \right. \right.
\end{aligned}$$

$$\begin{aligned}
& c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \Big)^2 \Big)^{1/3} \Big) - \\
& (5248 \pm 2^{1/3} c^4 \pi^8 \theta^2) \Big/ \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& \quad 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& \quad 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - \\
& \quad 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + \\
& \quad 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \\
& \quad (524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \\
& \quad \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& \quad 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& \quad 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \\
& \quad 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& \quad 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \Big)^2 \Big)^{1/3} \Big) + \\
& (2816 \times 2^{1/3} c^4 \pi^7 \theta^3) \Big/ \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& \quad 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& \quad 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - \\
& \quad 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + \\
& \quad 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \\
& \quad (524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \\
& \quad \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \\
& \quad 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \\
& \quad 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \\
& \quad 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5432832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \\
& \quad 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \Big)^2 \Big)^{1/3} \Big) + \\
& (2816 \pm 2^{1/3} c^4 \pi^7 \theta^3) \Big/ \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 +
\end{aligned}$$

$$\begin{aligned}
& 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - \\
& 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - \\
& 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - \\
& 108c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632c^4\pi^7\theta^3 - 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032c^6\right. \\
& \quad \left.\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832\right. \\
& \quad \left.c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& (832 \times 2^{1/3}c^4\pi^6\theta^4) \bigg/ \left(3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right. \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - \right. \\
& \quad \left.14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - \right. \\
& \quad \left.1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632c^4\pi^7\theta^3 - 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032c^6\right. \\
& \quad \left.\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832\right. \\
& \quad \left.c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& (832 \pm 2^{1/3}c^4\pi^6\theta^4) \bigg/ \left(\sqrt{3}\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right. \\
& \quad \left.(524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - \right. \\
& \quad \left.14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - \right. \\
& \quad \left.1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632c^4\pi^7\theta^3 - 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6\right)^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \\
& \quad c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \Big)^{1/3} \Big) + \\
& (128 \times 2^{1/3} c^4 \pi^5 \theta^5) \Big/ \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \right)^{1/3} \Big) + \\
& (128 \pm 2^{1/3} c^4 \pi^5 \theta^5) \Big/ \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right.
\end{aligned}$$

$$\begin{aligned} & \left( 8 \times 2^{1/3} c^4 \pi^4 \theta^6 \right) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\ & \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \\ & 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \\ & 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \\ & 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - 32 256 c^6 \pi^8 \theta^7 - \\ & 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\ & 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\ & 108 c^4 \pi^6 \theta^{13} + \sqrt{4 \left( -4096 c^4 \pi^{10} + 10 240 c^4 \pi^9 \theta - 10 496 c^4 \pi^8 \theta^2 + \right. \\ & \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \\ & \left. \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \right. \right. \\ & \left. \left. \pi^{13} \theta^2 + 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \right. \right. \\ & \left. \left. 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \right. \right. \\ & \left. \left. 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - \right. \right. \\ & \left. \left. 32 256 c^6 \pi^8 \theta^7 - 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 \right. \right. \\ & \left. \left. c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - \right. \right. \\ & \left. \left. 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\ & \left( 8 \sqrt[3]{2} c^4 \pi^4 \theta^6 \right) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\ & \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \\ & 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \\ & 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \\ & 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - 32 256 c^6 \pi^8 \theta^7 - \\ & 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\ & 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\ & 108 c^4 \pi^6 \theta^{13} + \sqrt{4 \left( -4096 c^4 \pi^{10} + 10 240 c^4 \pi^9 \theta - 10 496 c^4 \pi^8 \theta^2 + \right. \\ & \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \\ & \left. \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \right. \right. \\ & \left. \left. \pi^{13} \theta^2 + 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \right. \right. \\ & \left. \left. 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \right. \right. \\ & \left. \left. 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - \right. \right. \\ & \left. \left. 32 256 c^6 \pi^8 \theta^7 - 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 \right. \right. \\ & \left. \left. c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - \right. \right. \\ & \left. \left. 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\ & \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \\ & 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \\ & 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \\ & 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - \\ & 32 256 c^6 \pi^8 \theta^7 - 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + \end{aligned}$$

$$\begin{aligned}
& 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + \right.\right. \\
& \quad \left.256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - \right. \\
& \quad \left.1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \\
& \quad \left.3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \right. \\
& \quad \left.37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\, \right. \\
& \quad \left. c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left. 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} / \\
& \left(6 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) + \\
& \left(\pm \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right.\right. \\
& \quad \left.9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \right. \\
& \quad \left.14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \right. \\
& \quad \left.1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}\bigg) / \\
& \left. \left(2 \times 2^{1/3} \sqrt{3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right)\right)\bigg), \\
& \left(\sqrt{\left(-\frac{128\,c^2\pi^5}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \right.\right. \\
& \quad \left.\frac{160\,c^2\pi^4\theta}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} - \right. \\
& \quad \left.\frac{64\,c^2\pi^3\theta^2}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \right. \\
& \quad \left.\frac{8\,c^2\pi^2\theta^3}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} - \right. \\
& \quad \left.2048 \times \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{2^{1/3} c^4 \pi^{10}}{\left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right.} \\
& \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + \right. \\
& 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - \\
& 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - \\
& 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + \\
& 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \left. \sqrt{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \\
& \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 \right. \right. \\
& \left. \left. c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \right. \right. \\
& \left. \left. 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \right. \right. \\
& \left. \left. 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \right. \right. \\
& \left. \left. 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 30\,720 c^6 \pi^7 \theta^8 + \right. \right. \\
& \left. \left. 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \right. \right. \\
& \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 2048 \pm 2^{1/3} c^4 \pi^{10} \right) \Big/ \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + \right. \\
& 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - \\
& 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - \\
& 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + \\
& 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \left. \sqrt{4 \left( -4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \\
& \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 \right. \right. \\
& \left. \left. c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \right. \right. \\
& \left. \left. 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \right. \right. \\
& \left. \left. 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \right. \right. \\
& \left. \left. 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 30\,720 c^6 \pi^7 \theta^8 + \right. \right. \\
& \left. \left. 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \right. \right. \\
& \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) +
\end{aligned}$$

$$\begin{aligned}
& (5120 \times 2^{1/3} c^4 \pi^9 \theta) / \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + \right. \\
& \quad 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - \\
& \quad 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - \\
& \quad 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + \\
& \quad 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& \quad 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& \quad 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \quad \left. \sqrt{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \\
& \quad \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \right. \\
& \quad \left. (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 \right. \\
& \quad c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 30\,720 c^6 \pi^7 \theta^8 + \\
& \quad 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13}\right)^2\right)^{1/3} \Big) +
\end{aligned}$$

$$\begin{aligned}
& (5120 \pm 2^{1/3} c^4 \pi^9 \theta) / \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + \right. \\
& \quad 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - \\
& \quad 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - \\
& \quad 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + \\
& \quad 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& \quad 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& \quad 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \quad \left. \sqrt{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \\
& \quad \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \right. \\
& \quad \left. (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 \right. \\
& \quad c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 30\,720 c^6 \pi^7 \theta^8 + \\
& \quad 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13}\right)^2\right)^{1/3} \Big) -
\end{aligned}$$

$$\begin{aligned}
& (5248 \times 2^{1/3} c^4 \pi^8 \theta^2) / \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + \right. \\
& \quad 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - \\
& \quad 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 -
\end{aligned}$$

$$\begin{aligned}
& 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.\left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& (5248 \pm 2^{1/3} c^4 \pi^8 \theta^2) \bigg/ \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left. (524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad \left. 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \right. \\
& \quad \left. 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \right. \\
& \quad \left. 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left. 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left. 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \right. \\
& \quad \left. \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \right. \\
& \quad \left.\left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \right. \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} + \\
& (2816 \times 2^{1/3} c^4 \pi^7 \theta^3) \bigg/ \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left. (524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad \left. 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \right. \\
& \quad \left. 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \right. \\
& \quad \left. 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left. 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left. 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left(4 \left(-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6\right)^3 + \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad \left. c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \right. \\
& \quad \left. 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \right. \\
& \quad \left. 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \right. \\
& \quad \left. 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + \right. \\
& \quad \left. 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \right. \\
& \quad \left. 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13}\right)^2 \Big)^{1/3} + \\
& (2816 i 2^{1/3} c^4 \pi^7 \theta^3) / \left( \sqrt{3} \left(-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5\right) \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + \right. \\
& \quad \left. 3244032 c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - \right. \\
& \quad \left. 24440832 c^4 \pi^{16} \theta^3 + 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - \right. \\
& \quad \left. 743424 c^6 \pi^{10} \theta^5 - 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + \right. \\
& \quad \left. 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + \right. \\
& \quad \left. 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + \right. \\
& \quad \left. 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \right. \\
& \quad \left. \sqrt{\left(4 \left(-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6\right)^3 + \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad \left. c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \right. \\
& \quad \left. 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - 743424 c^6 \pi^{10} \theta^5 - \right. \\
& \quad \left. 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + 27205632 c^4 \pi^{13} \theta^6 - \right. \\
& \quad \left. 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + \right. \\
& \quad \left. 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + 293760 c^4 \pi^9 \theta^{10} - \right. \\
& \quad \left. 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13}\right)^2 \Big)^{1/3} - \\
& (832 \times 2^{1/3} c^4 \pi^6 \theta^4) / \left( 3 \left(-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5\right) \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + \right. \\
& \quad \left. 3244032 c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - \right. \\
& \quad \left. 24440832 c^4 \pi^{16} \theta^3 + 1867776 c^6 \pi^{11} \theta^4 + 37048320 c^4 \pi^{15} \theta^4 - \right. \\
& \quad \left. 743424 c^6 \pi^{10} \theta^5 - 37739520 c^4 \pi^{14} \theta^5 + 194560 c^6 \pi^9 \theta^6 + \right. \\
& \quad \left. 27205632 c^4 \pi^{13} \theta^6 - 32256 c^6 \pi^8 \theta^7 - 14224896 c^4 \pi^{12} \theta^7 + \right. \\
& \quad \left. 3072 c^6 \pi^7 \theta^8 + 5432832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1503360 c^4 \pi^{10} \theta^9 + \right. \\
& \quad \left. 293760 c^4 \pi^9 \theta^{10} - 38448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \right. \\
& \quad \left. \sqrt{\left(4 \left(-4096 c^4 \pi^{10} + 10240 c^4 \pi^9 \theta - 10496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - \right. \right. \right. \\
& \quad \left. \left. 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6\right)^3 + \right. \\
& \quad \left(524288 c^6 \pi^{15} - 1966080 c^6 \pi^{14} \theta - 1769472 c^4 \pi^{18} \theta + 3244032 \right. \\
& \quad \left. c^6 \pi^{13} \theta^2 + 9732096 c^4 \pi^{17} \theta^2 - 3088384 c^6 \pi^{12} \theta^3 - 24440832 c^4 \pi^{16} \theta^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \\
& 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \\
& 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \\
& 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13} \Big)^{1/3} \Big) - \\
& (832 \pm 2^{1/3}c^4\pi^6\theta^4) \Big/ \left( \sqrt{3}(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5) \right. \\
& \quad \left( 524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + \right. \\
& \quad 3244032c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - \\
& \quad 24440832c^4\pi^{16}\theta^3 + 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - \\
& \quad 743424c^6\pi^{10}\theta^5 - 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + \\
& \quad 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + \\
& \quad 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + \\
& \quad 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + 5632c^4\pi^7\theta^3 - \right. \\
& \quad \left. 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6)^3} + \right. \\
& \quad \left. (524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032 \right. \\
& \quad c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \\
& \quad 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& \quad 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \\
& \quad 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \\
& \quad 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \\
& \quad \left. 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13})^2 \right)^{1/3} \Big) + \\
& (128 \times 2^{1/3}c^4\pi^5\theta^5) \Big/ \left( 3(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5) \right. \\
& \quad \left( 524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + \right. \\
& \quad 3244032c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - \\
& \quad 24440832c^4\pi^{16}\theta^3 + 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - \\
& \quad 743424c^6\pi^{10}\theta^5 - 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + \\
& \quad 27205632c^4\pi^{13}\theta^6 - 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + \\
& \quad 3072c^6\pi^7\theta^8 + 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + \\
& \quad 293760c^4\pi^9\theta^{10} - 38448c^4\pi^8\theta^{11} + 3024c^4\pi^7\theta^{12} - 108c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{4(-4096c^4\pi^{10} + 10240c^4\pi^9\theta - 10496c^4\pi^8\theta^2 + 5632c^4\pi^7\theta^3 - \right. \\
& \quad \left. 1664c^4\pi^6\theta^4 + 256c^4\pi^5\theta^5 - 16c^4\pi^4\theta^6)^3} + \right. \\
& \quad \left. (524288c^6\pi^{15} - 1966080c^6\pi^{14}\theta - 1769472c^4\pi^{18}\theta + 3244032 \right. \\
& \quad c^6\pi^{13}\theta^2 + 9732096c^4\pi^{17}\theta^2 - 3088384c^6\pi^{12}\theta^3 - 24440832c^4\pi^{16}\theta^3 + \\
& \quad 1867776c^6\pi^{11}\theta^4 + 37048320c^4\pi^{15}\theta^4 - 743424c^6\pi^{10}\theta^5 - \\
& \quad 37739520c^4\pi^{14}\theta^5 + 194560c^6\pi^9\theta^6 + 27205632c^4\pi^{13}\theta^6 - \\
& \quad 32256c^6\pi^8\theta^7 - 14224896c^4\pi^{12}\theta^7 + 3072c^6\pi^7\theta^8 + \\
& \quad \left. 5432832c^4\pi^{11}\theta^8 - 128c^6\pi^6\theta^9 - 1503360c^4\pi^{10}\theta^9 + 293760c^4\pi^9\theta^{10} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \Big)^{1/3} \Big) + \\
& (128 \pm 2^{1/3}\,c^4\,\pi^5\,\theta^5) \Big/ \left( \sqrt{3} \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + \right. \\
& \quad 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - \\
& \quad 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - \\
& \quad 743\,424\,c^6\,\pi^{10}\,\theta^5 - 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + \\
& \quad 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + \\
& \quad 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + \\
& \quad 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} + \\
& \quad \left. \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + 5632\,c^4\,\pi^7\,\theta^3 - \right. \right. \\
& \quad \left. \left. 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6 \right)^3} + \right. \\
& \quad \left. \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\, \right. \right. \\
& \quad \left. \left. c^6\,\pi^{13}\,\theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + \right. \right. \\
& \quad \left. \left. 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& (8 \times 2^{1/3}\,c^4\,\pi^4\,\theta^6) \Big/ \left( 3 \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + \right. \\
& \quad 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - \\
& \quad 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - \\
& \quad 743\,424\,c^6\,\pi^{10}\,\theta^5 - 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + \\
& \quad 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + \\
& \quad 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + \\
& \quad 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} + \\
& \quad \left. \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + 5632\,c^4\,\pi^7\,\theta^3 - \right. \right. \\
& \quad \left. \left. 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6 \right)^3} + \right. \\
& \quad \left. \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\, \right. \right. \\
& \quad \left. \left. c^6\,\pi^{13}\,\theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + \right. \right. \\
& \quad \left. \left. 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& (8 \pm 2^{1/3}\,c^4\,\pi^4\,\theta^6) \Big/ \left( \sqrt{3} \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + \right.
\end{aligned}$$

$$\begin{aligned}
& 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\right. \\
& \quad \left.c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \right. \\
& \quad \left.5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \\
& \quad 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left.\sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 \\
& \quad \left. + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} \bigg/ \\
& \left(6 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) + \\
& \left(\text{ii} \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& \quad \left. 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right.
\end{aligned}$$

$$\begin{aligned}
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - \right.\right. \\
& \quad \left.1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}\bigg)/ \\
& \left(2 \times 2^{1/3} \sqrt{3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right)\bigg)\bigg\} \\
\text{Plot3D}\bigg[ & \sqrt{\left(-\frac{128\,c^2\pi^5}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \right. \\
& \frac{160\,c^2\pi^4\theta}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} - \\
& \frac{64\,c^2\pi^3\theta^2}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)} + \\
& \left.\frac{8\,c^2\pi^2\theta^3}{3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)}\right) \\
& \left(2048 \times 2^{1/3} c^4 \pi^{10}\right) / \left(3\left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + \right.\right. \\
& \quad \left.256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - \right. \\
& \quad \left.1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \\
& \quad \left.3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \right. \\
& \quad \left.37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left.27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left.3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left.293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}\bigg) + \\
& \left(2048 \pm 2^{1/3} c^4 \pi^{10}\right) / \left(\sqrt{3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right)
\end{aligned}$$



$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \right. \\
& \quad \left. \left. 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& \left( 5120 \times 2^{1/3} c^4 \pi^9 \theta \right) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \right. \\
& \quad \left. \left. 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 5120 \pm 2^{1/3} c^4 \pi^9 \theta \right) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \\
& \quad \theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \Big)^{1/3} - \\
& (5248 \times 2^{1/3} c^4 \pi^8 \theta^2) / \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{4 (-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \\
& \quad 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6)^3} + \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \\
& \quad \theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \Big)^{1/3} + \\
& (5248 \pm 2^{1/3} c^4 \pi^8 \theta^2) / \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{4 (-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \\
& \quad 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6)^3} + \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \\
& \quad \theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \Big)^{1/3} + \\
& (2816 \times 2^{1/3} c^4 \pi^7 \theta^3) / \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 \right. \right. \\
& \quad \left. \left. + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 2816 \pm 2^{1/3} c^4 \pi^7 \theta^3 \right) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 \right. \right. \\
& \quad \left. \left. + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 832 \times 2^{1/3} c^4 \pi^6 \theta^4 \right) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \\
& \quad c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \\
& \quad 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \\
& \quad \theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \Big)^{1/3} + \\
& (832 \pm 2^{1/3} c^4 \pi^6 \theta^4) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \right. \right. \\
& \quad \left. \left. \theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& (128 \times 2^{1/3} c^4 \pi^5 \theta^5) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3} + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776 \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12} \right. \right. \\
& \quad \left. \left. \theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& (128 \pm 2^{1/3} c^4 \pi^5 \theta^5) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 \right. \right. \\
& \quad \left. \left. + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 8 \times 2^{1/3} c^4 \pi^4 \theta^6 \right) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\, \right. \right. \\
& \quad \left. \left. c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + \right. \right. \\
& \quad \left. \left. 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 \right. \right. \\
& \quad \left. \left. + 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \right. \\
& \quad \left. \left. 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& \left( 8 \pm 2^{1/3} c^4 \pi^4 \theta^6 \right) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right) \\
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + \right. \\
& \quad 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - \\
& \quad 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - \\
& \quad 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \\
& \quad 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \\
& \quad 30\,720\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 30\,240\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left. \sqrt{\left( 4\left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - \\
& 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - \\
& 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + \\
& 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 \\
& c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13})^2)^{1/3} - \\
& (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \\
& 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - \\
& 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + \\
& 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + \\
& 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& 14\,224\,896 c^4 \pi^{12} \theta^7 + 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - \\
& 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \sqrt[3]{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \\
& 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + \\
& (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \\
& 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 \\
& c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + \\
& 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13})^2)^{1/3} / \\
& (6 \times 2^{1/3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5)) - \\
& (i (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \\
& 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + \\
& 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + \\
& 30\,720 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + \\
& 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} + \\
& \sqrt[3]{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + \\
& 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 + (524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - \\
& 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - \\
& 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 \\
& c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + \\
& 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 30\,720 c^6 \pi^7 \theta^8 + \\
& 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& 38\,448 c^4 \pi^8 \theta^{11} + 30\,240 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13})^2)^{1/3} /
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \times 2^{1/3} \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right), \\
& \left( -\sqrt{\left( -\frac{128 c^2 \pi^5}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} + \right. \right. \\
& \quad \frac{160 c^2 \pi^4 \theta}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} - \\
& \quad \frac{64 c^2 \pi^3 \theta^2}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} + \\
& \quad \left. \frac{8 c^2 \pi^2 \theta^3}{3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right)} \right) \\
& \left( 2048 \times 2^{1/3} c^4 \pi^{10} \right) / \\
& \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \\
& \quad 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \\
& \quad 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - 32 256 c^6 \pi^8 \theta^7 - \\
& \quad 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{\left( 4 \left( -4096 c^4 \pi^{10} + 10 240 c^4 \pi^9 \theta - 10 496 c^4 \pi^8 \theta^2 + \right. \right. \\
& \quad \left. \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \quad \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad \left. 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \right. \\
& \quad 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \\
& \quad 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - \\
& \quad 32 256 c^6 \pi^8 \theta^7 - 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 \\
& \quad \left. c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - \right. \\
& \quad \left. \left. 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 2048 \pm 2^{1/3} c^4 \pi^{10} \right) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9 732 096 c^4 \pi^{17} \theta^2 - 3 088 384 c^6 \pi^{12} \theta^3 - 24 440 832 c^4 \pi^{16} \theta^3 + \\
& \quad 1 867 776 c^6 \pi^{11} \theta^4 + 37 048 320 c^4 \pi^{15} \theta^4 - 743 424 c^6 \pi^{10} \theta^5 - \\
& \quad 37 739 520 c^4 \pi^{14} \theta^5 + 194 560 c^6 \pi^9 \theta^6 + 27 205 632 c^4 \pi^{13} \theta^6 - 32 256 c^6 \pi^8 \theta^7 - \\
& \quad 14 224 896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5 432 832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1 503 360 c^4 \pi^{10} \theta^9 + 293 760 c^4 \pi^9 \theta^{10} - 38 448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{\left( 4 \left( -4096 c^4 \pi^{10} + 10 240 c^4 \pi^9 \theta - 10 496 c^4 \pi^8 \theta^2 + \right. \right. \\
& \quad \left. \left. 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6 \right)^3 + \right. \\
& \quad \left. \left. \left( 524 288 c^6 \pi^{15} - 1 966 080 c^6 \pi^{14} \theta - 1 769 472 c^4 \pi^{18} \theta + 3 244 032 c^6 \pi^{13} \theta^2 + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \\
& \quad c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \\
& \quad \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \Big)^{1/3} \Big) + \\
& (5120 \times 2^{1/3} c^4 \pi^9 \theta) / \left( 3 \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2 \right)^{1/3} \Big) + \\
& (5120 \pm 2^{1/3} c^4 \pi^9 \theta) / \left( \sqrt{3} \left( -64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad \left. 108\,c^4\pi^6\theta^{13} + \sqrt{4 \left( -4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right. \right. \\
& \quad \left. \left. 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6 \right)^3 + \right. \\
& \quad \left. \left( 524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \right. \\
& \quad \left. \left. \pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832 \right. \right. \\
& \quad \left. \left. c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left( 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \Big)^{1/3} \Big) - \\
& \left( 5248 \times 2^{1/3}\,c^4\,\pi^8\,\theta^2 \right) / \left( 3 \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& \quad 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - \\
& \quad 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - \\
& \quad 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - \\
& \quad 108\,c^4\,\pi^6\,\theta^{13} + \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + \right. \\
& \quad \left. 5632\,c^4\,\pi^7\,\theta^3 - 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6 \right)^3} + \\
& \quad \left. \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - \right. \right. \\
& \quad \left. \left. 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& \left( 5248 \pm 2^{1/3}\,c^4\,\pi^8\,\theta^2 \right) / \left( \sqrt{3} \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& \quad 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - \\
& \quad 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - \\
& \quad 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - \\
& \quad 108\,c^4\,\pi^6\,\theta^{13} + \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + \right. \\
& \quad \left. 5632\,c^4\,\pi^7\,\theta^3 - 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6 \right)^3} + \\
& \quad \left. \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \right. \\
& \quad \left. \left. 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \right. \right. \\
& \quad \left. \left. 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \right. \right. \\
& \quad \left. \left. 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \right. \right. \\
& \quad \left. \left. 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - \right. \right. \\
& \quad \left. \left. 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \right. \right. \\
& \quad \left. \left. 38\,448\,c^4\,\pi^8\,\theta^{11} + 30\,24\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13} \right)^2 \right)^{1/3} \Big) + \\
& \left( 2816 \times 2^{1/3}\,c^4\,\pi^7\,\theta^3 \right) / \left( 3 \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \quad \left( 524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& \quad 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 -
\end{aligned}$$

$$\begin{aligned}
& 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \left.\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}\bigg) + \\
& (2816 \pm 2^{1/3}\,c^4\pi^7\theta^3) \bigg/ \left(\sqrt{3}\,(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)\right) \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right. \\
& \quad \left.\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3}\bigg) - \\
& (832 \times 2^{1/3}\,c^4\pi^6\theta^4) \bigg/ \left(3\,(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5)\right) \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left.(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\right.
\end{aligned}$$

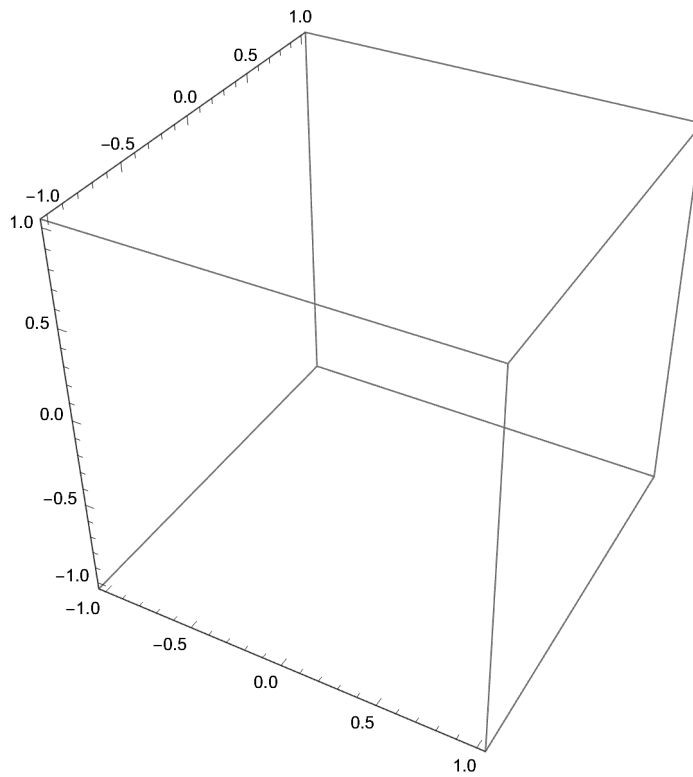
$$\begin{aligned}
& \pi^{13} \theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \\
& 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\, \\
& c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \\
& 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13})^2)^{1/3}) - \\
& (832 \pm 2^{1/3}\,c^4\,\pi^6\,\theta^4) / \left( \sqrt{3} \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \left. (524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - \\
& 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - \\
& 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - \\
& 108\,c^4\,\pi^6\,\theta^{13} + \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + \right. \\
& 5632\,c^4\,\pi^7\,\theta^3 - 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6)^3} + \\
& \left. (524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \pi^{13}\,\theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \\
& 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\, \\
& c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \\
& 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13})^2)^{1/3}) + \\
& (128 \times 2^{1/3}\,c^4\,\pi^5\,\theta^5) / \left( 3 \left( -64\,\pi^5 + 144\,\pi^4\,\theta - 128\,\pi^3\,\theta^2 + 56\,\pi^2\,\theta^3 - 12\,\pi\,\theta^4 + \theta^5 \right) \right. \\
& \left. (524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - 32\,256\,c^6\,\pi^8\,\theta^7 - \\
& 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\,c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - \\
& 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - \\
& 108\,c^4\,\pi^6\,\theta^{13} + \sqrt{4 \left( -4096\,c^4\,\pi^{10} + 10\,240\,c^4\,\pi^9\,\theta - 10\,496\,c^4\,\pi^8\,\theta^2 + \right. \\
& 5632\,c^4\,\pi^7\,\theta^3 - 1664\,c^4\,\pi^6\,\theta^4 + 256\,c^4\,\pi^5\,\theta^5 - 16\,c^4\,\pi^4\,\theta^6)^3} + \\
& \left. (524\,288\,c^6\,\pi^{15} - 1\,966\,080\,c^6\,\pi^{14}\,\theta - 1\,769\,472\,c^4\,\pi^{18}\,\theta + 3\,244\,032\,c^6\,\pi^{13}\,\theta^2 + \right. \\
& \pi^{13}\,\theta^2 + 9\,732\,096\,c^4\,\pi^{17}\,\theta^2 - 3\,088\,384\,c^6\,\pi^{12}\,\theta^3 - 24\,440\,832\,c^4\,\pi^{16}\,\theta^3 + \\
& 1\,867\,776\,c^6\,\pi^{11}\,\theta^4 + 37\,048\,320\,c^4\,\pi^{15}\,\theta^4 - 743\,424\,c^6\,\pi^{10}\,\theta^5 - \\
& 37\,739\,520\,c^4\,\pi^{14}\,\theta^5 + 194\,560\,c^6\,\pi^9\,\theta^6 + 27\,205\,632\,c^4\,\pi^{13}\,\theta^6 - \\
& 32\,256\,c^6\,\pi^8\,\theta^7 - 14\,224\,896\,c^4\,\pi^{12}\,\theta^7 + 3072\,c^6\,\pi^7\,\theta^8 + 5\,432\,832\, \\
& c^4\,\pi^{11}\,\theta^8 - 128\,c^6\,\pi^6\,\theta^9 - 1\,503\,360\,c^4\,\pi^{10}\,\theta^9 + 293\,760\,c^4\,\pi^9\,\theta^{10} - \\
& 38\,448\,c^4\,\pi^8\,\theta^{11} + 3024\,c^4\,\pi^7\,\theta^{12} - 108\,c^4\,\pi^6\,\theta^{13})^2)^{1/3}) +
\end{aligned}$$

$$\begin{aligned}
& (128 \pm 2^{1/3} c^4 \pi^5 \theta^5) / \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \\
& \quad 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 +} \\
& \quad \left. \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& (8 \times 2^{1/3} c^4 \pi^4 \theta^6) / \left( 3 (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - \\
& \quad 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - \\
& \quad 108 c^4 \pi^6 \theta^{13} + \sqrt{4 (-4096 c^4 \pi^{10} + 10\,240 c^4 \pi^9 \theta - 10\,496 c^4 \pi^8 \theta^2 + \\
& \quad 5632 c^4 \pi^7 \theta^3 - 1664 c^4 \pi^6 \theta^4 + 256 c^4 \pi^5 \theta^5 - 16 c^4 \pi^4 \theta^6)^3 +} \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad \pi^{13} \theta^2 + 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - \\
& \quad 32\,256 c^6 \pi^8 \theta^7 - 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 \\
& \quad c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 - 1\,503\,360 c^4 \pi^{10} \theta^9 + 293\,760 c^4 \pi^9 \theta^{10} - \\
& \quad \left. \left. 38\,448 c^4 \pi^8 \theta^{11} + 3024 c^4 \pi^7 \theta^{12} - 108 c^4 \pi^6 \theta^{13} \right)^2 \right)^{1/3} \Big) - \\
& (8 \pm 2^{1/3} c^4 \pi^4 \theta^6) / \left( \sqrt{3} (-64 \pi^5 + 144 \pi^4 \theta - 128 \pi^3 \theta^2 + 56 \pi^2 \theta^3 - 12 \pi \theta^4 + \theta^5) \right. \\
& \quad \left( 524\,288 c^6 \pi^{15} - 1\,966\,080 c^6 \pi^{14} \theta - 1\,769\,472 c^4 \pi^{18} \theta + 3\,244\,032 c^6 \pi^{13} \theta^2 + \right. \\
& \quad 9\,732\,096 c^4 \pi^{17} \theta^2 - 3\,088\,384 c^6 \pi^{12} \theta^3 - 24\,440\,832 c^4 \pi^{16} \theta^3 + \\
& \quad 1\,867\,776 c^6 \pi^{11} \theta^4 + 37\,048\,320 c^4 \pi^{15} \theta^4 - 743\,424 c^6 \pi^{10} \theta^5 - \\
& \quad 37\,739\,520 c^4 \pi^{14} \theta^5 + 194\,560 c^6 \pi^9 \theta^6 + 27\,205\,632 c^4 \pi^{13} \theta^6 - 32\,256 c^6 \pi^8 \theta^7 - \\
& \quad 14\,224\,896 c^4 \pi^{12} \theta^7 + 3072 c^6 \pi^7 \theta^8 + 5\,432\,832 c^4 \pi^{11} \theta^8 - 128 c^6 \pi^6 \theta^9 -
\end{aligned}$$

$$\begin{aligned}
& 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - \right. \\
& \quad \left.38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} - \\
& \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \\
& \quad 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + \\
& \quad 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \\
& \quad 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13} + \\
& \quad \left.\sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + 5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + \right.\right.\right. \\
& \quad \left.256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - \right. \\
& \quad \left.1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + 9\,732\,096\,c^4\pi^{17}\theta^2 - \right. \\
& \quad \left.3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + 1\,867\,776\,c^6\pi^{11}\theta^4 + \right. \\
& \quad \left.37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + \right. \\
& \quad \left.27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + \right. \\
& \quad \left.3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + \right. \\
& \quad \left.293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - 108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} \bigg/ \\
& \left(6 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) + \\
& \left(\text{ii} \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right.\right. \\
& \quad 9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \\
& \quad 1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \\
& \quad 37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - 32\,256\,c^6\pi^8\theta^7 - \\
& \quad 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - 128\,c^6\pi^6\theta^9 - \\
& \quad 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \\
& \quad 108\,c^4\pi^6\theta^{13} + \sqrt{\left(4\left(-4096\,c^4\pi^{10} + 10\,240\,c^4\pi^9\theta - 10\,496\,c^4\pi^8\theta^2 + \right.\right. \\
& \quad \left.5632\,c^4\pi^7\theta^3 - 1664\,c^4\pi^6\theta^4 + 256\,c^4\pi^5\theta^5 - 16\,c^4\pi^4\theta^6\right)^3 + \\
& \quad \left(524\,288\,c^6\pi^{15} - 1\,966\,080\,c^6\pi^{14}\theta - 1\,769\,472\,c^4\pi^{18}\theta + 3\,244\,032\,c^6\pi^{13}\theta^2 + \right. \\
& \quad \left.9\,732\,096\,c^4\pi^{17}\theta^2 - 3\,088\,384\,c^6\pi^{12}\theta^3 - 24\,440\,832\,c^4\pi^{16}\theta^3 + \right. \\
& \quad \left.1\,867\,776\,c^6\pi^{11}\theta^4 + 37\,048\,320\,c^4\pi^{15}\theta^4 - 743\,424\,c^6\pi^{10}\theta^5 - \right. \\
& \quad \left.37\,739\,520\,c^4\pi^{14}\theta^5 + 194\,560\,c^6\pi^9\theta^6 + 27\,205\,632\,c^4\pi^{13}\theta^6 - \right. \\
& \quad \left.32\,256\,c^6\pi^8\theta^7 - 14\,224\,896\,c^4\pi^{12}\theta^7 + 3072\,c^6\pi^7\theta^8 + 5\,432\,832\,c^4\pi^{11}\theta^8 - \right. \\
& \quad \left.128\,c^6\pi^6\theta^9 - 1\,503\,360\,c^4\pi^{10}\theta^9 + 293\,760\,c^4\pi^9\theta^{10} - 38\,448\,c^4\pi^8\theta^{11} + 3024\,c^4\pi^7\theta^{12} - \right. \\
& \quad \left.108\,c^4\pi^6\theta^{13}\right)^2\bigg)^{1/3} \bigg/ \\
& \left(6 \times 2^{1/3} \left(-64\pi^5 + 144\pi^4\theta - 128\pi^3\theta^2 + 56\pi^2\theta^3 - 12\pi\theta^4 + \theta^5\right)\right) +
\end{aligned}$$



RevolutionPlot3D[

$$\left\{ \left( \text{Root} \left[ -16 c^4 \pi r^2 + (4 c^4 \pi^4 + 4 c^4 r^2) \#1 + (-4 c^4 \pi^3 + 32 c^2 \pi r^4) \#1^2 + (c^4 \pi^2 - 8 c^2 r^4) \#1^3 - 16 \pi r^6 \#1^4 + 4 r^6 \#1^5 \&, 1 \right] \right), \left( \text{Root} \left[ -16 c^4 \pi r^2 + (4 c^4 \pi^4 + 4 c^4 r^2) \#1 + (-4 c^4 \pi^3 + 32 c^2 \pi r^4) \#1^2 + (c^4 \pi^2 - 8 c^2 r^4) \#1^3 - 16 \pi r^6 \#1^4 + 4 r^6 \#1^5 \&, 2 \right] \right), \right. \\ \left( \text{Root} \left[ -16 c^4 \pi r^2 + (4 c^4 \pi^4 + 4 c^4 r^2) \#1 + (-4 c^4 \pi^3 + 32 c^2 \pi r^4) \#1^2 + (c^4 \pi^2 - 8 c^2 r^4) \#1^3 - 16 \pi r^6 \#1^4 + 4 r^6 \#1^5 \&, 3 \right] \right), \\ \left( \text{Root} \left[ -16 c^4 \pi r^2 + (4 c^4 \pi^4 + 4 c^4 r^2) \#1 + (-4 c^4 \pi^3 + 32 c^2 \pi r^4) \#1^2 + (c^4 \pi^2 - 8 c^2 r^4) \#1^3 - 16 \pi r^6 \#1^4 + 4 r^6 \#1^5 \&, 4 \right] \right), \\ \left. \left( \text{Root} \left[ -16 c^4 \pi r^2 + (4 c^4 \pi^4 + 4 c^4 r^2) \#1 + (-4 c^4 \pi^3 + 32 c^2 \pi r^4) \#1^2 + (c^4 \pi^2 - 8 c^2 r^4) \#1^3 - 16 \pi r^6 \#1^4 + 4 r^6 \#1^5 \&, 5 \right] \right) \right\}, \{r, -10\,000\,000\,000\,000, 10\,000\,000\,000\,000\}$$


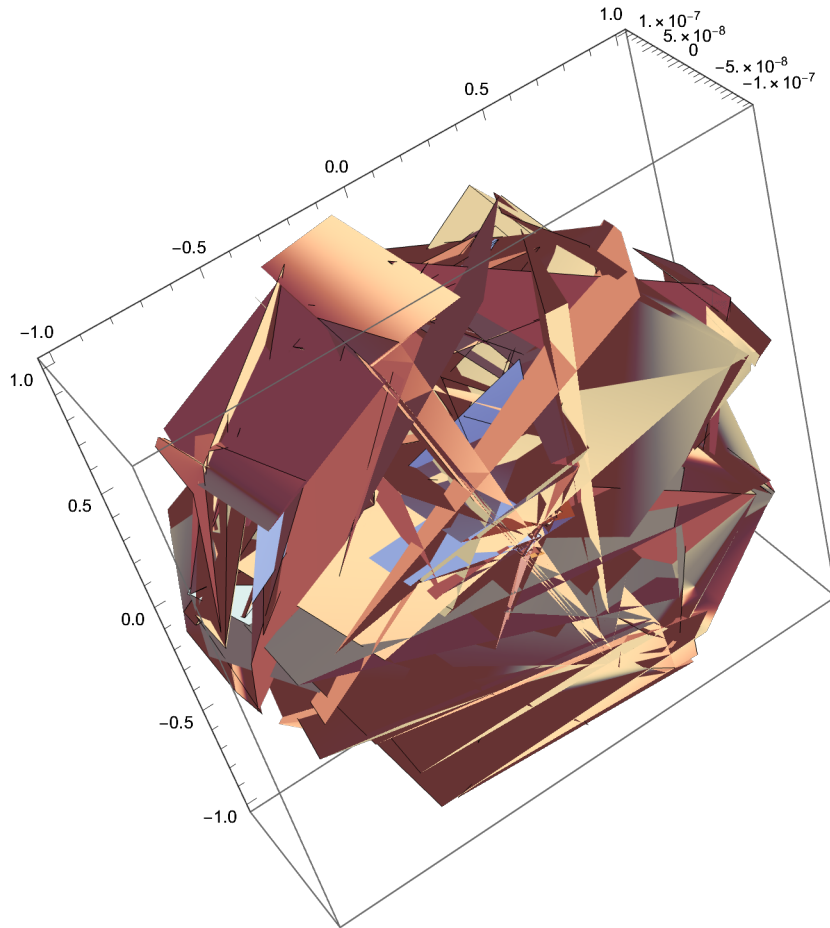
$$\begin{aligned}
& (1/2\pi) D \left[ \frac{\sqrt{2c^2 - \frac{2c^2\pi^2 r\theta}{\sqrt{r^2(4\pi-\theta)\theta}} + \frac{c^2\pi r\theta^2}{\sqrt{r^2(4\pi-\theta)\theta}}}}{\sqrt{2}}, r, \theta \right] \\
& \frac{1}{2}\pi \left( \left( \frac{3.54814 \times 10^{18} r^2 (4\pi - \theta) \theta}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.77407 \times 10^{18} r^2 \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \right. \right. \\
& \quad \frac{8.47057 \times 10^{17} r^2 (4\pi - \theta) \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} + \frac{2.82352 \times 10^{17} r^2 \theta^3}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.77407 \times 10^{18}}{\sqrt{r^2 (4\pi - \theta) \theta}} + \\
& \quad \frac{5.64705 \times 10^{17} \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} - \frac{2.66111 \times 10^{18} r^2 (4\pi - \theta) \theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{5/2}} + \\
& \quad \frac{4.23528 \times 10^{17} r^2 (4\pi - \theta) \theta^3 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{5/2}} + \\
& \quad \left. \frac{8.87036 \times 10^{17} \theta (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.41176 \times 10^{17} \theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} \right) / \\
& \left( 2\sqrt{2} \sqrt{1.79751 \times 10^{17} - \frac{1.77407 \times 10^{18} r\theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{2.82352 \times 10^{17} r\theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}}} \right) - \\
& \left( \left( \frac{1.77407 \times 10^{18} r^2 (4\pi - \theta) \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{2.82352 \times 10^{17} r^2 (4\pi - \theta) \theta^3}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.77407 \times 10^{18} \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \right. \\
& \quad \left. \frac{2.82352 \times 10^{17} \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right) \left( -\frac{1.77407 \times 10^{18} r}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{5.64705 \times 10^{17} r\theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \\
& \quad \left. \frac{8.87036 \times 10^{17} r\theta (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.41176 \times 10^{17} r\theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} \right) \Big) / \\
& \left( 4\sqrt{2} \left( 1.79751 \times 10^{17} - \frac{1.77407 \times 10^{18} r\theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{2.82352 \times 10^{17} r\theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right)^{3/2} \right) \Big)
\end{aligned}$$

RevolutionPlot3D[

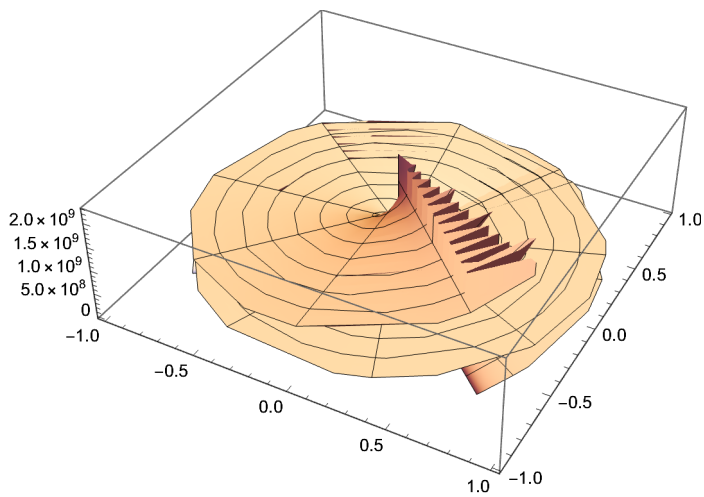
$$\begin{aligned}
& \frac{1}{2}\pi \left( \left( \frac{3.5481432270250993 \cdot 10^{18} r^2 (4\pi - \theta) \theta}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.7740716135125496 \cdot 10^{18} r^2 \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \right. \right. \\
& \quad \frac{8.470568000686103 \cdot 10^{17} r^2 (4\pi - \theta) \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} + \frac{2.8235226668953677 \cdot 10^{17} r^2 \theta^3}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \\
& \quad \frac{1.7740716135125496 \cdot 10^{18}}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{5.6470453337907354 \cdot 10^{17} \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} - \\
& \quad \left. \left. \frac{2.66111 \cdot 10^{18} r^2 (4\pi - \theta) \theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{5/2}} + \frac{4.23528 \cdot 10^{17} r^2 (4\pi - \theta) \theta^3 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{5/2}} \right) \right) / \\
& \left( 2\sqrt{2} \sqrt{1.79751 \cdot 10^{17} - \frac{1.77407 \cdot 10^{18} r\theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{2.82352 \cdot 10^{17} r\theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}}} \right) - \\
& \left( \left( \frac{1.77407 \cdot 10^{18} r^2 (4\pi - \theta) \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{2.82352 \cdot 10^{17} r^2 (4\pi - \theta) \theta^3}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.77407 \cdot 10^{18} \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \right. \\
& \quad \left. \frac{2.82352 \cdot 10^{17} \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right) \left( -\frac{1.77407 \cdot 10^{18} r}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{5.64705 \cdot 10^{17} r\theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \\
& \quad \left. \frac{8.87036 \cdot 10^{17} r\theta (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{1.41176 \cdot 10^{17} r\theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} \right) \Big) / \\
& \left( 4\sqrt{2} \left( 1.79751 \cdot 10^{17} - \frac{1.77407 \cdot 10^{18} r\theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{2.82352 \cdot 10^{17} r\theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right)^{3/2} \right) \Big)
\end{aligned}$$



$$\begin{aligned}
& \frac{2.6611074202688246 \cdot r^2 (4\pi - \theta) \theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{5/2}} + \\
& \frac{4.2352840003430515 \cdot r^2 (4\pi - \theta) \theta^3 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{5/2}} + \\
& \frac{8.870358067562748 \cdot \theta (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \\
& \frac{1.4117613334476838 \cdot \theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} \Bigg) / \\
& \left( 2 \sqrt{2} \sqrt{\left( 1.7975103574736352 \cdot r \theta - \frac{1.7740716135125496 \cdot r \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \right. \\
& \quad \left. \left. \frac{2.8235226668953677 \cdot r \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right) \right) - \\
& \left( \left( \frac{1.7740716135125496 \cdot r^2 (4\pi - \theta) \theta^2}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \frac{2.8235226668953677 \cdot r^2 (4\pi - \theta) \theta^3}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \right. \right. \\
& \quad \left. \frac{1.7740716135125496 \cdot \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{2.8235226668953677 \cdot \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right) \\
& \left( - \frac{1.7740716135125496 \cdot r}{\sqrt{r^2 (4\pi - \theta) \theta}} + \frac{5.6470453337907354 \cdot r \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \\
& \quad \left. \frac{8.870358067562748 \cdot r \theta (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} - \right. \\
& \quad \left. \frac{1.4117613334476838 \cdot r \theta^2 (r^2 (4\pi - \theta) - r^2 \theta)}{(r^2 (4\pi - \theta) \theta)^{3/2}} \right) \Bigg) / \\
& \left( 4 \sqrt{2} \left( 1.7975103574736352 \cdot r \theta - \frac{1.7740716135125496 \cdot r \theta}{\sqrt{r^2 (4\pi - \theta) \theta}} + \right. \right. \\
& \quad \left. \left. \frac{2.8235226668953677 \cdot r \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right)^{3/2} \right) \Bigg), \{r, -1, 1\}, \{\theta, -40\pi, 40\pi\} ]
\end{aligned}$$



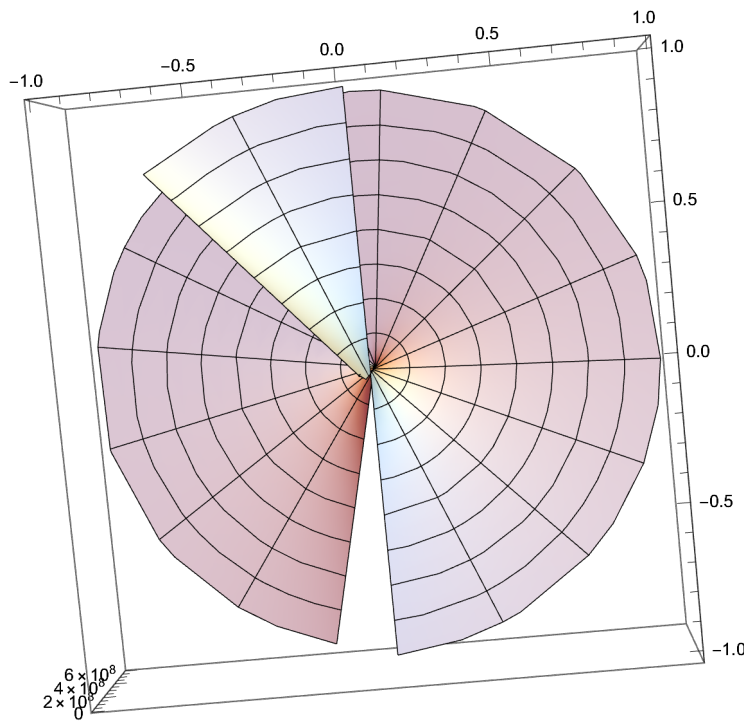
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta)} \theta} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta)} \theta}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



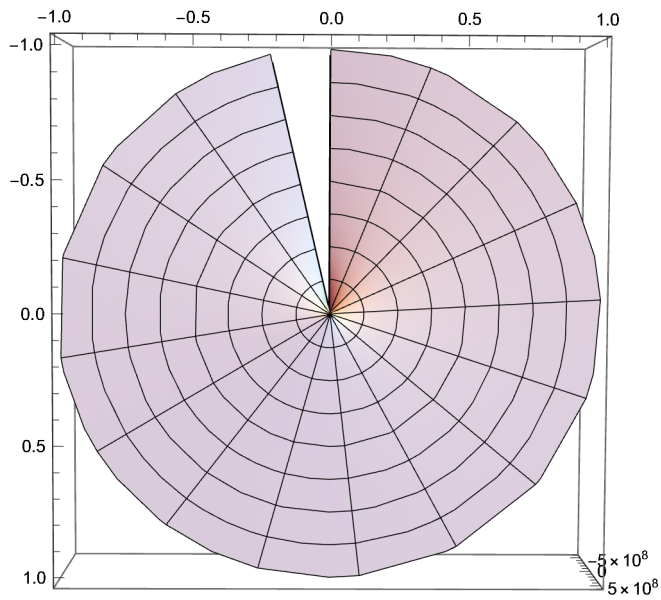
$$\text{Solve}\left[\frac{r \left(1 - \frac{v^2}{c^2}\right)}{2 \pi \theta} = \frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}} \right\}, \left\{ v \rightarrow \frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}} \right\} \right\}$$

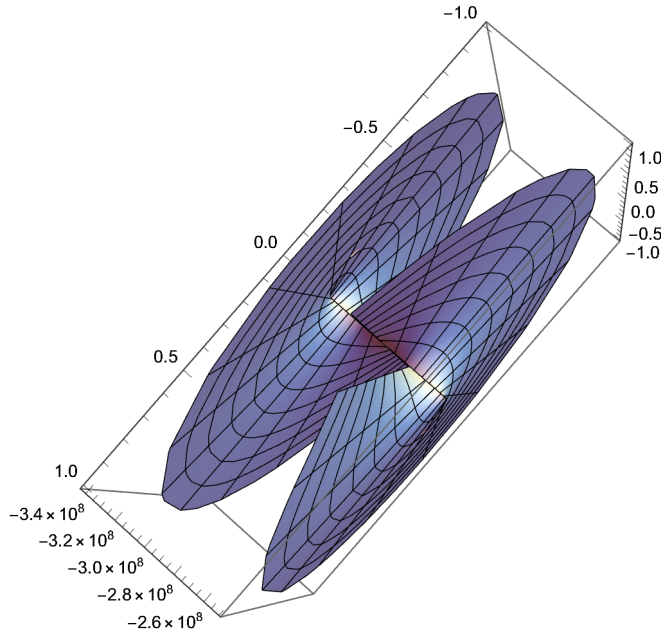
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$\text{RevolutionPlot3D}\left[\left\{\left\{-\frac{\sqrt{2c^2 - \frac{2c^2\pi^2 r\theta}{\sqrt{r^2(4\pi-\theta)}\theta} + \frac{c^2\pi r\theta^2}{\sqrt{r^2(4\pi-\theta)}\theta}}}{\sqrt{2}}\right\},\right.\right.$   
 $\left.\left\{\frac{\sqrt{2c^2 - \frac{2c^2\pi^2 r\theta}{\sqrt{r^2(4\pi-\theta)}\theta} + \frac{c^2\pi r\theta^2}{\sqrt{r^2(4\pi-\theta)}\theta}}}{\sqrt{2}}\right\}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



$$\text{RevolutionPlot3D}\left[\frac{i c \sqrt{\theta} \sqrt{-\frac{2}{\theta} + \frac{2 r}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{r \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$

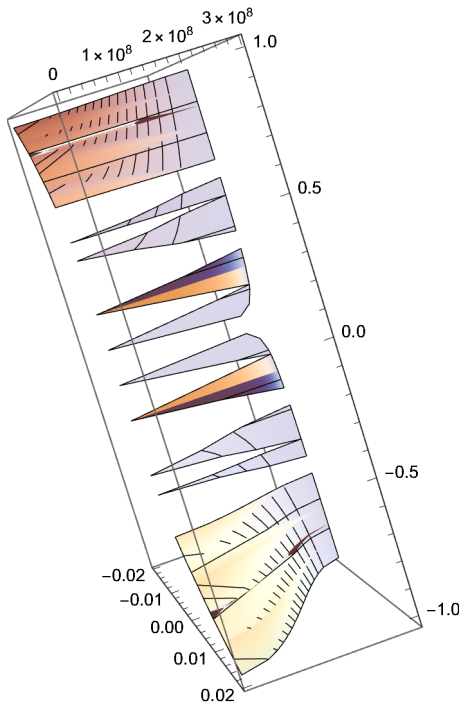


$$\text{Solve}\left[\frac{r \left(1 - \frac{v^2}{c^2}\right)}{\theta} = \frac{8 \pi r \theta - 2 r \theta^2}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v\right]$$

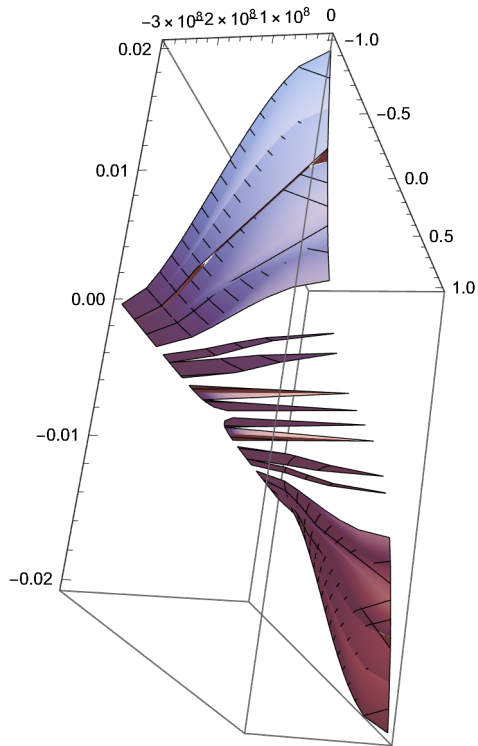
$$\left\{\left\{v \rightarrow -\frac{i c \sqrt{\theta} \sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{i c \sqrt{\theta} \sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[-\frac{i c \sqrt{\theta} \sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\frac{i c \sqrt{\theta} \sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\left( r \sqrt{1 - \left( \left( \frac{v}{c} \right)^2 \right)} \right) / \left( \theta / \sqrt{1 - \left( \left( \frac{v}{c} \right)^2 \right)} \right) ==$$

$$D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta\right]$$

$$\frac{r \left(1 - \frac{v^2}{c^2}\right)}{\theta} == - \frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

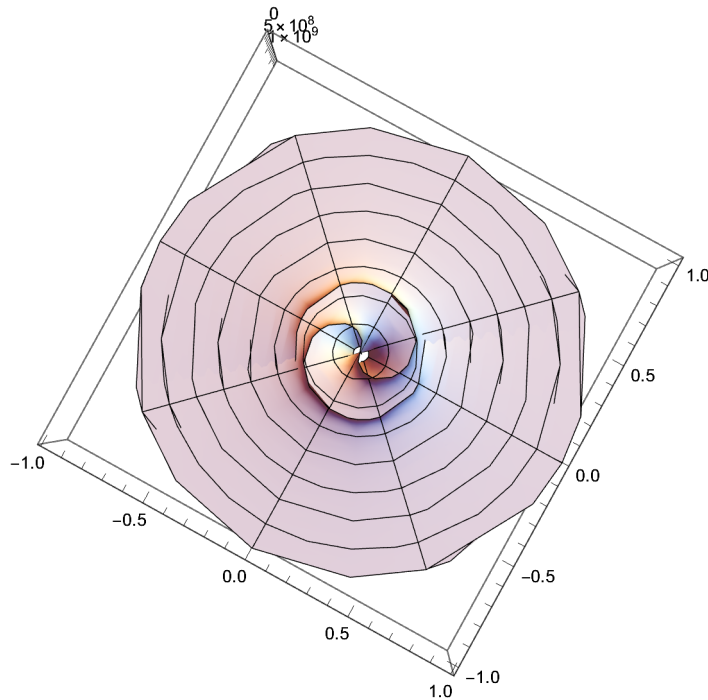
$$\text{Solve}\left[\frac{r\left(1-\frac{v^2}{c^2}\right)}{\theta} == -\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1}{\sqrt{2}} i c \sqrt{\theta} \sqrt{\left(-\frac{2}{\theta} - \frac{8\pi r^2\theta}{(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{6r^2\theta^2}{(4\pi r^2\theta-r^2\theta^2)^{3/2}} - \frac{r^2\theta^3}{\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{4}{\sqrt{4\pi r^2\theta-r^2\theta^2}} - \frac{2\theta}{\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{1}{\sqrt{2}} i c \sqrt{\theta} \sqrt{\left(-\frac{2}{\theta} - \frac{8\pi r^2\theta}{(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{6r^2\theta^2}{(4\pi r^2\theta-r^2\theta^2)^{3/2}} - \frac{r^2\theta^3}{\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{4}{\sqrt{4\pi r^2\theta-r^2\theta^2}} - \frac{2\theta}{\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}\right\}\right\}$$

RevolutionPlot3D[

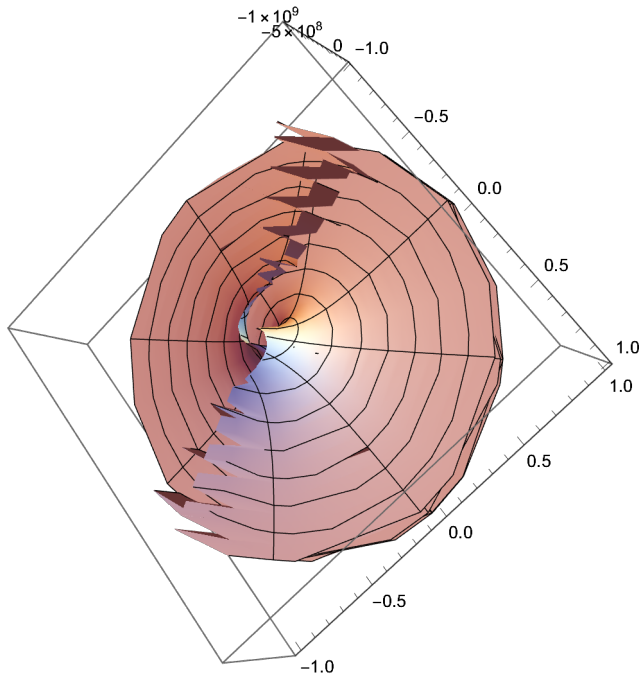
$$-\frac{1}{\sqrt{2}} i c \sqrt{\theta} \sqrt{\left(-\frac{2}{\theta} - \frac{8\pi r^2\theta}{(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{6r^2\theta^2}{(4\pi r^2\theta-r^2\theta^2)^{3/2}} - \frac{r^2\theta^3}{\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}} + \frac{4}{\sqrt{4\pi r^2\theta-r^2\theta^2}} - \frac{2\theta}{\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$





RevolutionPlot3D[

$$\frac{1}{\sqrt{2}} \text{I} \text{C} \sqrt{\theta} \sqrt{\left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



$$\begin{aligned} & D \left[ \frac{1}{\sqrt{2}} \text{I} \text{C} \sqrt{\theta} \sqrt{\left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}, r, \theta \right] \\ & - \left( 5.29963 \times 10^7 \text{I} \sqrt{\theta} \left( \frac{12 \pi r^2 \theta (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r^2 \theta^3 (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{16 \pi r \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{12 r \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2 r \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} \right) \right. \\ & \left. \left( \frac{2}{\theta^2} + \frac{12 \pi r^2 \theta (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r^2 \theta^3 (4 \pi r^2 - 2 r^2 \theta)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \right. \right. \end{aligned}$$

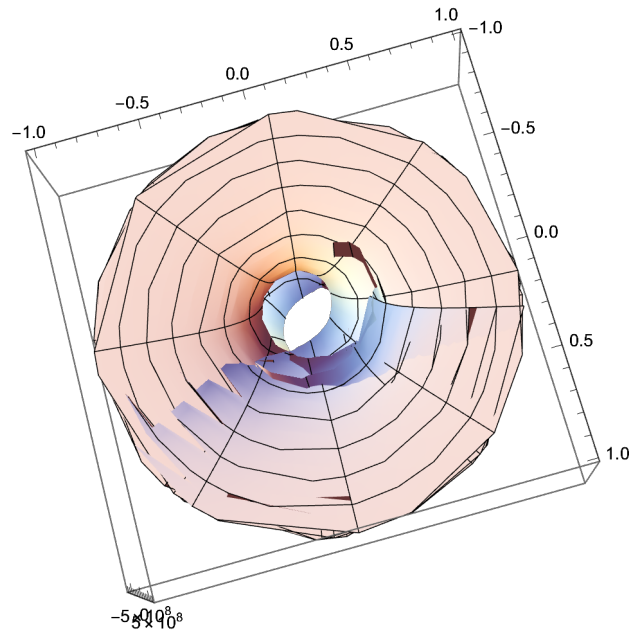
$$\begin{aligned}
& \left( \frac{8 \pi r^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{12 r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{3 r^2 \theta^2}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \right. \\
& \left. \frac{2 (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (4 \pi r^2 - 2 r^2 \theta)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \Bigg/ \\
& \left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \right. \\
& \left. \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)^{3/2} + \\
& \left( 1.05993 \times 10^8 \, i \, \sqrt{\theta} \left( -\frac{30 \pi r^2 \theta (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \right. \right. \\
& \frac{45 r^2 \theta^2 (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{2 (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} - \frac{15 r^2 \theta^3 (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \\
& \frac{12 \pi r^2 \theta (8 \pi r - 4 r \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (8 \pi r - 4 r \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r^2 \theta^3 (8 \pi r - 4 r \theta)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \\
& \frac{24 \pi r \theta (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{18 r \theta^2 (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r \theta^3 (4 \pi r^2 - 2 r^2 \theta)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \\
& \frac{12 \pi r^2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{18 r^2 \theta (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{9 r^2 \theta^2 (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \\
& \frac{3 (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{3 \theta (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \\
& \frac{16 \pi r}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{24 r \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{6 r \theta^2}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\
& \left. \frac{2 (8 \pi r - 4 r \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (8 \pi r - 4 r \theta)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r \theta - 2 r \theta^2}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} \right) \Bigg/ \\
& \left( \sqrt{\left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \right. \right. \\
& \left. \left. \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right) + \\
& \left( 5.29963 \times 10^7 \, i \left( \frac{12 \pi r^2 \theta (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \right. \right.
\end{aligned}$$

$$\begin{aligned} & \frac{3 r^2 \theta^3 (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{16 \pi r \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{12 r \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\ & \frac{2 r \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} \Bigg) \Bigg/ \\ & \left( \sqrt{\theta} \sqrt{\left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \right.} \right. \\ & \left. \left. \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right) \end{aligned}$$

RevolutionPlot3D[

$$\begin{aligned} & - \left( 5.299632000009581 \cdot \sqrt{\theta} \left( \frac{12 \pi r^2 \theta (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \right. \right. \\ & \frac{3 r^2 \theta^3 (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{16 \pi r \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{12 r \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\ & \left. \frac{2 r \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} \right) \\ & \left( \frac{2}{\theta^2} + \frac{12 \pi r^2 \theta (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r^2 \theta^3 (4 \pi r^2 - 2 r^2 \theta)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \right. \\ & \frac{8 \pi r^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{12 r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{3 r^2 \theta^2}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\ & \left. \frac{2 (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (4 \pi r^2 - 2 r^2 \theta)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \Bigg) \Bigg/ \\ & \left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \right. \\ & \left. \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)^{3/2} + \\ & \left( 1.0599264000019161 \cdot \sqrt{\theta} \left( -\frac{30 \pi r^2 \theta (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \right. \right. \\ & \frac{45 r^2 \theta^2 (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{2 (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} - \frac{15 r^2 \theta^3 (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{4 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{7/2}} + \end{aligned}$$

$$\begin{aligned}
& \frac{12 \pi r^2 \theta (8 \pi r - 4 r \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (8 \pi r - 4 r \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r^2 \theta^3 (8 \pi r - 4 r \theta)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \\
& \frac{24 \pi r \theta (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{18 r \theta^2 (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{3 r \theta^3 (4 \pi r^2 - 2 r^2 \theta)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \\
& \frac{12 \pi r^2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{18 r^2 \theta (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \frac{9 r^2 \theta^2 (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \\
& \frac{3 (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{3 \theta (4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \\
& \frac{16 \pi r}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{24 r \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{6 r \theta^2}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\
& \frac{2 (8 \pi r - 4 r \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (8 \pi r - 4 r \theta)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r \theta - 2 r \theta^2}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} \Bigg) \Bigg/ \\
& \left( \sqrt{\left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \right.} \right. \\
& \quad \left. \left. \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right) + \\
& \left( 5.299632000009581 \cdot 10^7 i \left( \frac{12 \pi r^2 \theta (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{9 r^2 \theta^2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} + \right. \right. \\
& \quad \frac{3 r^2 \theta^3 (8 \pi r \theta - 2 r \theta^2)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{5/2}} - \frac{16 \pi r \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{12 r \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\
& \quad \left. \left. \frac{2 r \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2 (8 \pi r \theta - 2 r \theta^2)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta (8 \pi r \theta - 2 r \theta^2)}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} \right) \right) \Bigg/ \\
& \left( \sqrt{\theta} \sqrt{\left( -\frac{2}{\theta} - \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \right.} \right. \\
& \quad \left. \left. \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right), \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\} ]
\end{aligned}$$



RevolutionPlot3D

Solve

$$(2 \pi) \int_0^{\theta} \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right), \theta \quad (182)$$

When velocity is constant, we can find relativistic velocity by engaging the idea of length contraction further.

$$r \theta = 2 \pi r - 2 \pi r_1 = 2 \pi r - 2 \pi \sqrt{r^2 - \eta^2} \quad (183)$$

$$t' = \left( \frac{\theta (1080 / \pi)}{\left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right)} \right) \quad (184)$$

$$t = 2 \theta = \frac{1080 \theta}{\pi} \quad (185)$$

$$t' = \frac{2 \pi \theta}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (185)$$

$$(\pi / 1080) t' = \theta' = \frac{\theta}{\sqrt{1 - \frac{v^2}{c^2}}} \quad (186)$$

$$\left( r \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) = r' \quad (187)$$

$$\left( r \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) \left( \frac{\theta}{\sqrt{1 - \left( \frac{v}{c} \right)^2}} \right) = r' * \theta' = r \theta \quad (188)$$

$$\frac{1}{(1080/\pi) D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right]} \frac{4\pi r^2 - 2r^2 \theta}{4320 \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$\text{RelativisticVelocity} = D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right] \quad (189)$$

$$\frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$\text{RelativisticVelocityChangingr} = D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta, r \right] \quad (190)$$

$$- \frac{(4\pi r^2 - 2r^2 \theta) (8\pi r \theta - 2r \theta^2)}{8\pi (4\pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8\pi r - 4r \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

$$r' / t' = r' / \left( (\theta (1080/\pi)) / \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) =$$

$$\left( r \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) / \left( (\theta (1080/\pi)) / \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) \quad (191)$$

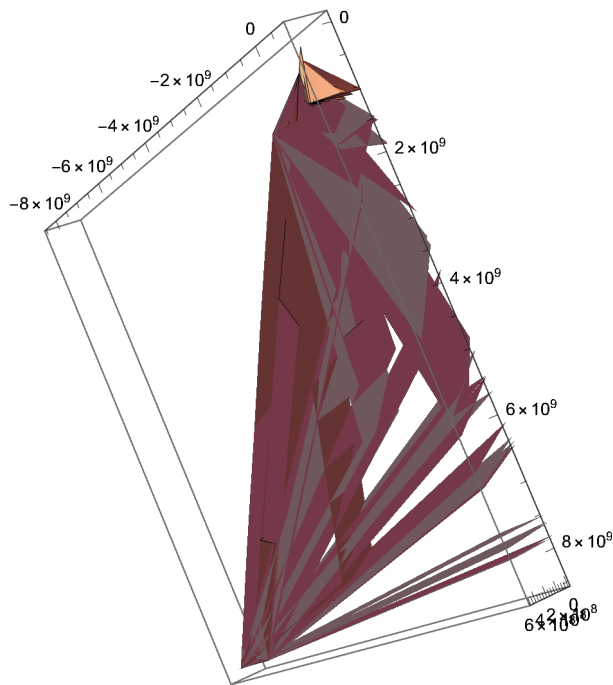
$$\text{Solve} \left[ \left( r \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) / \left( (\theta (2\pi)) / \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) == \right.$$

$$\left. 2\pi \frac{4\pi r^2 - 2r^2 \theta}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}}, v \right]$$

$$\left\{ \left\{ v \rightarrow - \sqrt{c^2 - \frac{4c^2 \pi^2 r \theta}{\sqrt{r^2 (4\pi - \theta) \theta}}} + \frac{2c^2 \pi r \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \sqrt{c^2 - \frac{4c^2 \pi^2 r \theta}{\sqrt{r^2 (4\pi - \theta) \theta}}} + \frac{2c^2 \pi r \theta^2}{\sqrt{r^2 (4\pi - \theta) \theta}} \right\} \right\}$$

$\text{RevolutionPlot3D}\left[\left\{-\sqrt{c^2 - \frac{4 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{2 c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}, \sqrt{c^2 - \frac{4 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{2 c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}\right\}, \{r, -1, 1\}, \{\theta, -1600 \pi, 1600 \pi\}\right]$



$c := (2.99792458 * 10^8)$

$\text{Solve}\left[ \right.$

$$\left( r \left( \sqrt{1 - ((v)^2 / c^2)} \right) \right) / \left( (\theta (2 \pi)) / \left( \sqrt{1 - ((v)^2 / c^2)} \right) \right) == \frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v \Bigg]$$

$$\left\{ \left\{ v \rightarrow -\frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}} \right\}, \left\{ v \rightarrow \frac{\sqrt{2 c^2 - \frac{2 c^2 \pi^2 r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 \pi r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2}} \right\} \right\}$$

Solve[

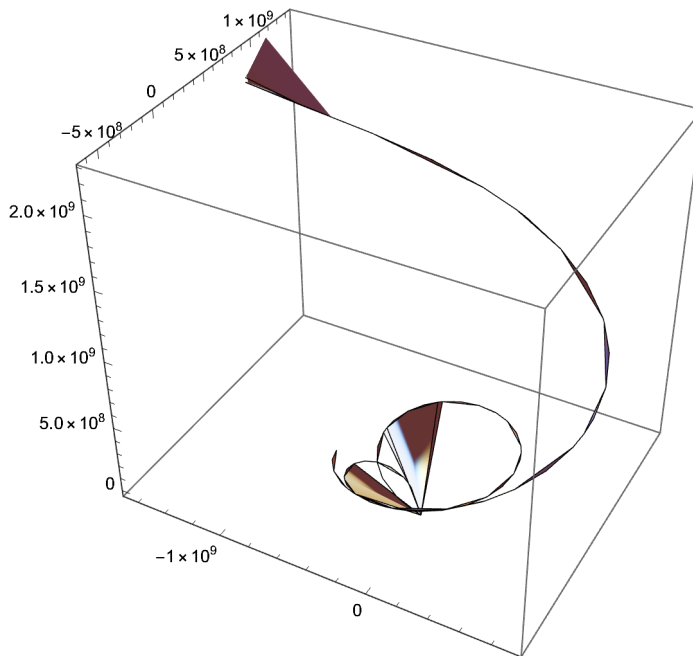
$$\left( r \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) / \left( \theta (2 \pi) \right) / \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) == \frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v]$$

$$\left\{ \left\{ v \rightarrow -7.51468 \times 10^8 \sqrt{\theta} \sqrt{\frac{0.159155}{\theta} - \frac{1.5708 r}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow 7.51468 \times 10^8 \sqrt{\theta} \sqrt{\frac{0.159155}{\theta} - \frac{1.5708 r}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}}} \right\} \right\}$$

RevolutionPlot3D[{{-7.514682517439266`\*^8 \sqrt{\theta}

$$\sqrt{\left( \frac{0.15915494309189535}{\theta} - \frac{1.5707963267948966 r}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} \right)}, \left( 7.514682517439266`*^8 \sqrt{\theta} \sqrt{\left( \frac{0.15915494309189535}{\theta} - \frac{1.5707963267948966 r}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} \right)} \right)}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$





Solve[

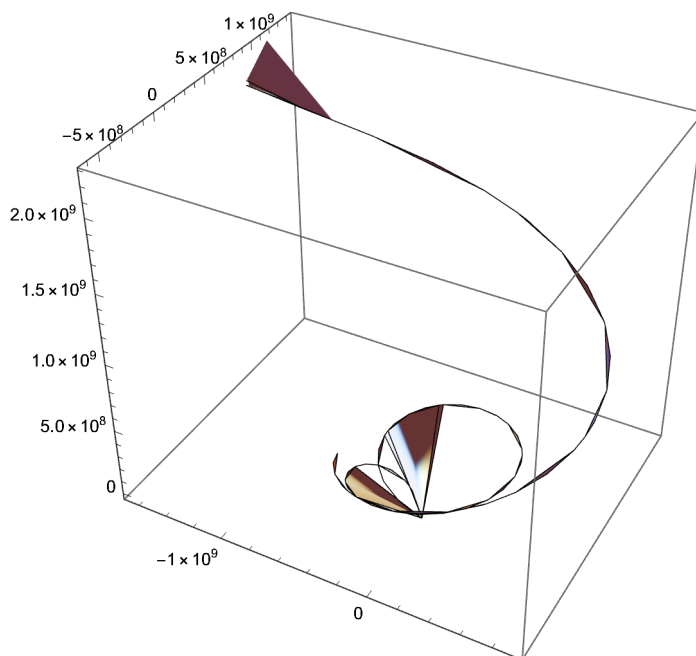
$$\left( r \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) \right) / \left( \theta (2 \pi) \right) / \left( \sqrt{1 - \left( \frac{v}{c} \right)^2} \right) == \frac{4 \pi r^2 - 2 r^2 \theta}{8 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v]$$

$$\left\{ \left\{ v \rightarrow -7.51468 \times 10^8 \sqrt{\theta} \sqrt{\frac{0.159155}{\theta} - \frac{1.5708 r}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow 7.51468 \times 10^8 \sqrt{\theta} \sqrt{\frac{0.159155}{\theta} - \frac{1.5708 r}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2}}} \right\} \right\}$$

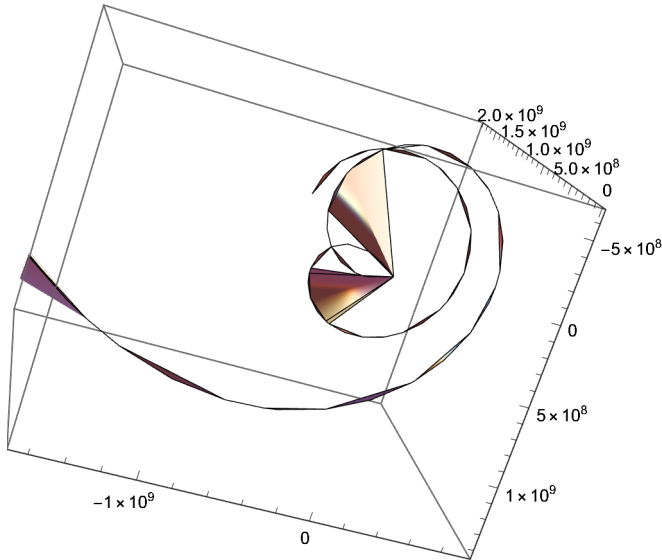
RevolutionPlot3D[{-7.514682517439266`\*^8 \sqrt{\theta}

$$\sqrt{\left( \frac{0.15915494309189535}{\theta} - \frac{1.5707963267948966 r}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} \right)}, \left( 7.514682517439266`*^8 \sqrt{\theta} \sqrt{\left( \frac{0.15915494309189535}{\theta} - \frac{1.5707963267948966 r}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} \right)} \right) \right], \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



RevolutionPlot3D[{-7.514682517439266`\*^8  $\sqrt{\theta}$

$$\sqrt{\left(\frac{0.15915494309189535}{\theta} - \frac{1.5707963267948966 r}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}}\right)}, \left(7.514682517439266`*^8 \sqrt{\theta} \sqrt{\left(\frac{0.15915494309189535}{\theta} - \frac{1.5707963267948966 r}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.25 r \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}}\right)}\right)\}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$

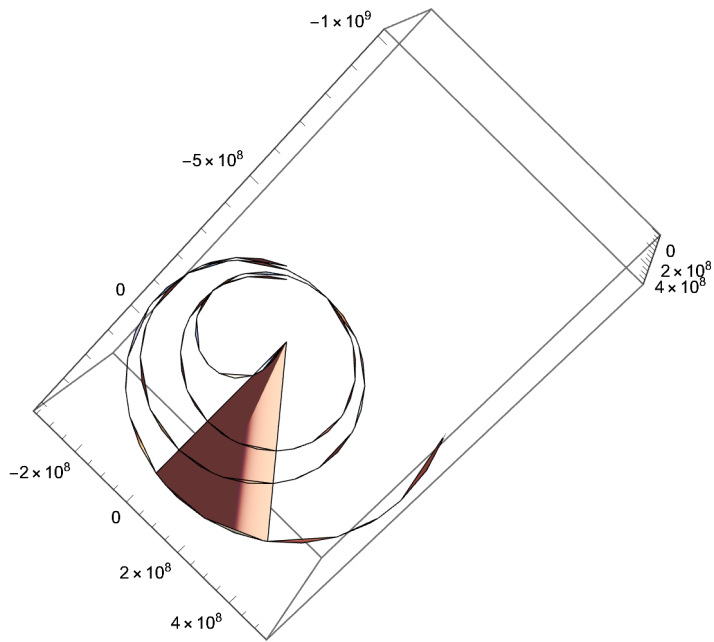


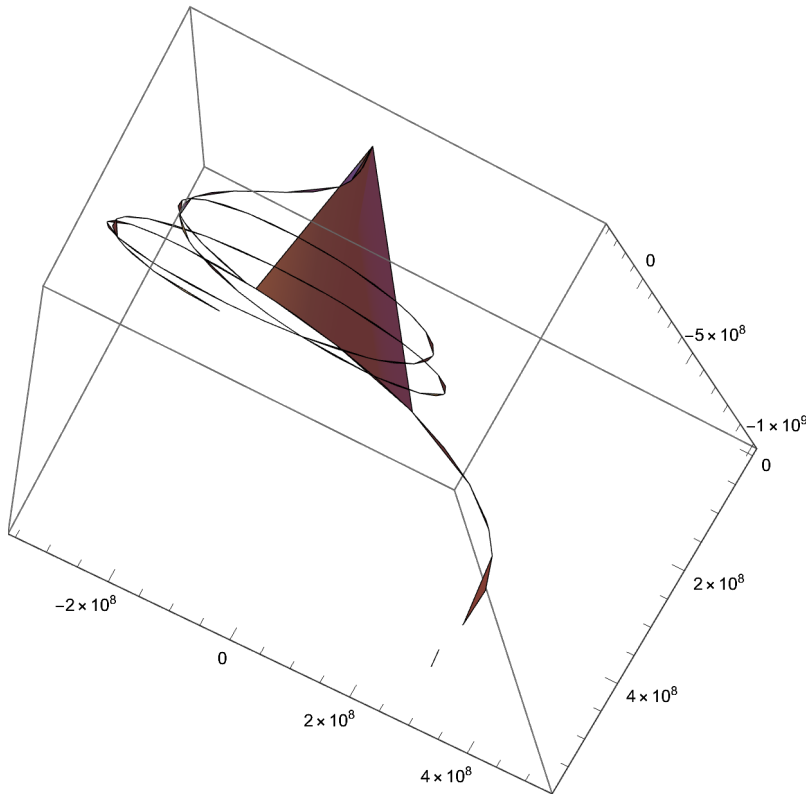
$$\text{Solve}\left[\left(r \left(\sqrt{1 - ((v)^2 / c^2)}\right)\right) / \left((\theta (1080 / \pi)) / \left(\sqrt{1 - ((v)^2 / c^2)}\right)\right) == \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}}\right\}, \left\{v \rightarrow \frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}}\right\}\right\}$$

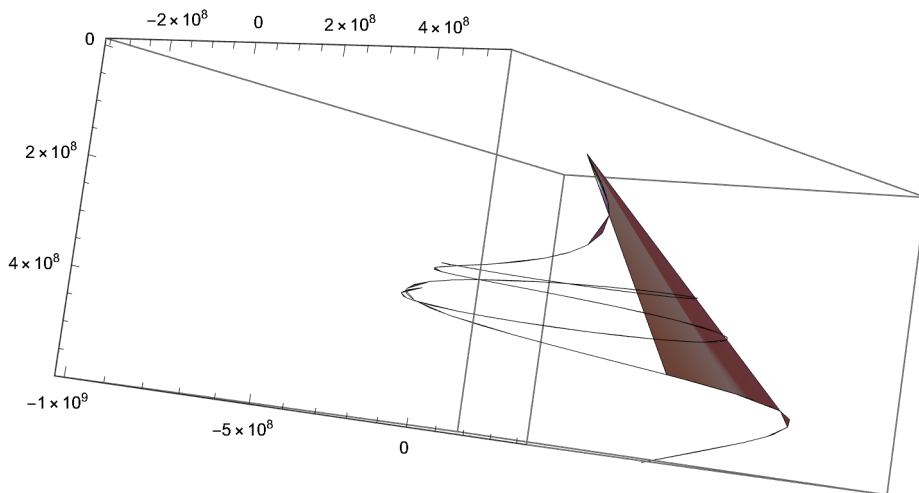
(192)

$$\text{RevolutionPlot3D}\left[\left\{-\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}}, \frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta) \theta}}}}{\sqrt{2 \pi}}\right\}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



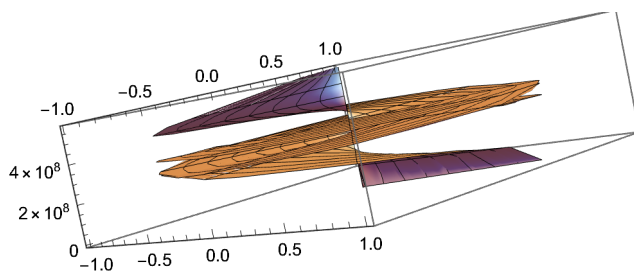


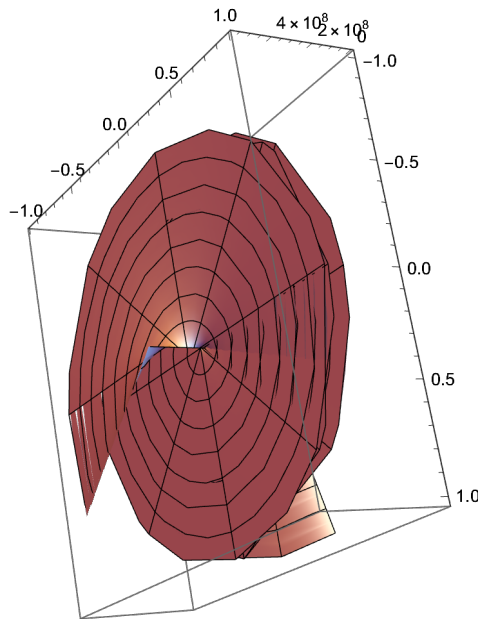
1.1.



$$\text{RevolutionPlot3D}\left[\left\{\frac{\sqrt{2 c^2 \pi - \frac{2 c^2 \pi r \theta}{\sqrt{r^2 (4 \pi - \theta)} \theta} + \frac{c^2 r \theta^2}{\sqrt{r^2 (4 \pi - \theta)} \theta}}}{\sqrt{2 \pi}}\right\}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$

2.



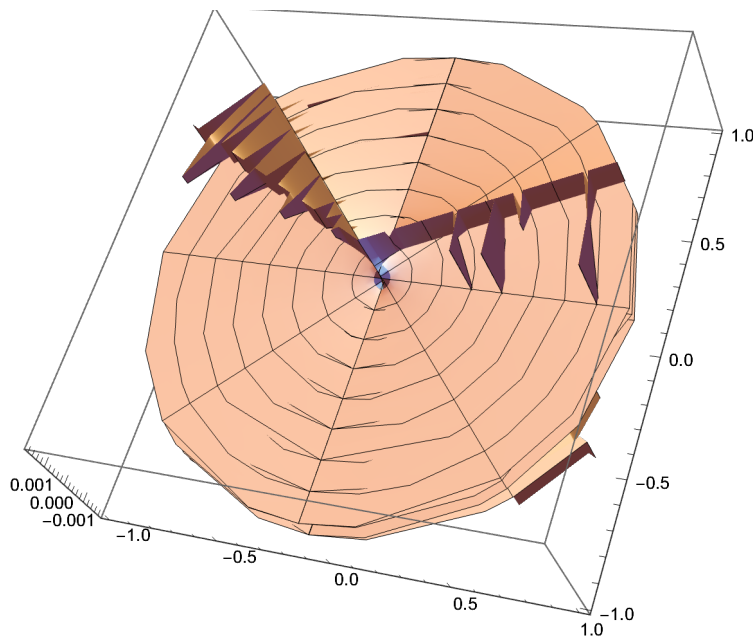


$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta, r \right]$$

$$\pi \left( - \frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)$$

1080

$$\text{RevolutionPlot3D} \left[ \frac{\pi \left( - \frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\} \right]$$



$$\text{Solve}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}==\right.$$

$$\left.\left(r\left(\sqrt{1-\left(\frac{v}{c}\right)^2}\right)\right)/\left(\theta(1080/\pi)\right)/\left(\sqrt{1-\left(\frac{v}{c}\right)^2}\right),v\right]$$

$$\left\{\left\{v\rightarrow-5.5585\times10^9\sqrt{\theta}\right.\right.$$

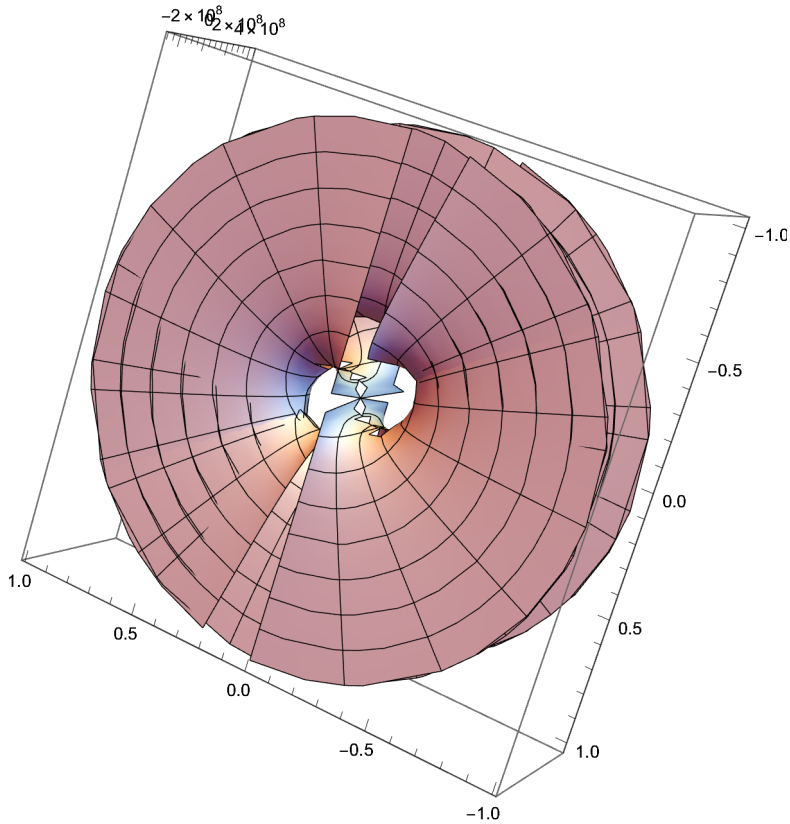
$$\left.\sqrt{\left(\frac{0.00290888}{\theta}+\frac{0.0365541r^2\theta}{(12.5664r^2\theta-1.r^2\theta^2)^{3/2}}-\frac{0.00872665r^2\theta^2}{(12.5664r^2\theta-1.r^2\theta^2)^{3/2}}+\frac{0.000462963r^2\theta^3}{(12.5664r^2\theta-1.r^2\theta^2)^{3/2}}-\frac{0.00581776}{\sqrt{12.5664r^2\theta-1.r^2\theta^2}}+\frac{0.000925926\theta}{\sqrt{12.5664r^2\theta-1.r^2\theta^2}}\right)}\right\},$$

$$\left\{v\rightarrow5.5585\times10^9\sqrt{\theta}\sqrt{\left(\frac{0.00290888}{\theta}+\frac{0.0365541r^2\theta}{(12.5664r^2\theta-1.r^2\theta^2)^{3/2}}-\frac{0.00872665r^2\theta^2}{(12.5664r^2\theta-1.r^2\theta^2)^{3/2}}+\frac{0.000462963r^2\theta^3}{(12.5664r^2\theta-1.r^2\theta^2)^{3/2}}-\frac{0.00581776}{\sqrt{12.5664r^2\theta-1.r^2\theta^2}}+\frac{0.000925926\theta}{\sqrt{12.5664r^2\theta-1.r^2\theta^2}}\right)}\right\}}$$

RevolutionPlot3D[{{-5.558500439352987`\*^9  $\sqrt{\theta}$

$$\sqrt{\left(\frac{0.002908882086657216}{\theta} + \frac{0.03655409037440503 r^2 \theta}{(12.566370614359172 r^2 \theta - 1. r^2 \theta^2)^{3/2}} - \frac{0.008726646259971648 r^2 \theta^2}{(12.566370614359172 r^2 \theta - 1. r^2 \theta^2)^{3/2}} + \frac{0.000462962962962963 r^2 \theta^3}{(12.566370614359172 r^2 \theta - 1. r^2 \theta^2)^{3/2}} - \frac{0.005817764173314432}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.000925925925925926 \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}}\right)}, \{5.558500439352987`*^9 \sqrt{\theta}$$

$$\sqrt{\left(\frac{0.002908882086657216}{\theta} + \frac{0.03655409037440503 r^2 \theta}{(12.566370614359172 r^2 \theta - 1. r^2 \theta^2)^{3/2}} - \frac{0.008726646259971648 r^2 \theta^2}{(12.566370614359172 r^2 \theta - 1. r^2 \theta^2)^{3/2}} + \frac{0.000462962962962963 r^2 \theta^3}{(12.566370614359172 r^2 \theta - 1. r^2 \theta^2)^{3/2}} - \frac{0.005817764173314432}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}} + \frac{0.000925925925925926 \theta}{\sqrt{12.566370614359172 r^2 \theta - 1. r^2 \theta^2}}\right)}}\}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



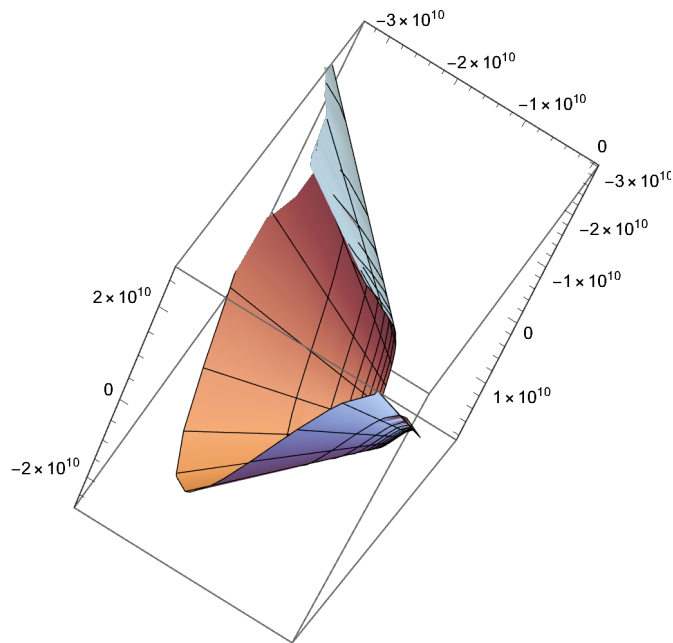
$$\text{Solve}\left[-\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} == \right. \\ \left. \left(r\left(\sqrt{1 - \left(\frac{v}{c}\right)^2}\right)\right) / \left(\theta(1080/\pi)\right) / \left(\sqrt{1 - \left(\frac{v}{c}\right)^2}\right), v\right] \\ \left\{\left\{v \rightarrow -\frac{1}{\sqrt{\pi}}c\sqrt{\theta}\sqrt{\left(\frac{\pi}{\theta} + \frac{4320\pi r^2\theta}{(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{3240r^2\theta^2}{(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \right. \right. \right. \\ \left. \left. \frac{540r^2\theta^3}{\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{2160}{\sqrt{4\pi r^2\theta - r^2\theta^2}} + \frac{1080\theta}{\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right)\right\}, \\ \left\{v \rightarrow \frac{1}{\sqrt{\pi}}c\sqrt{\theta}\sqrt{\left(\frac{\pi}{\theta} + \frac{4320\pi r^2\theta}{(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{3240r^2\theta^2}{(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \right. \right. \\ \left. \left. \frac{540r^2\theta^3}{\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \frac{2160}{\sqrt{4\pi r^2\theta - r^2\theta^2}} + \frac{1080\theta}{\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right)\right\}\right\}$$

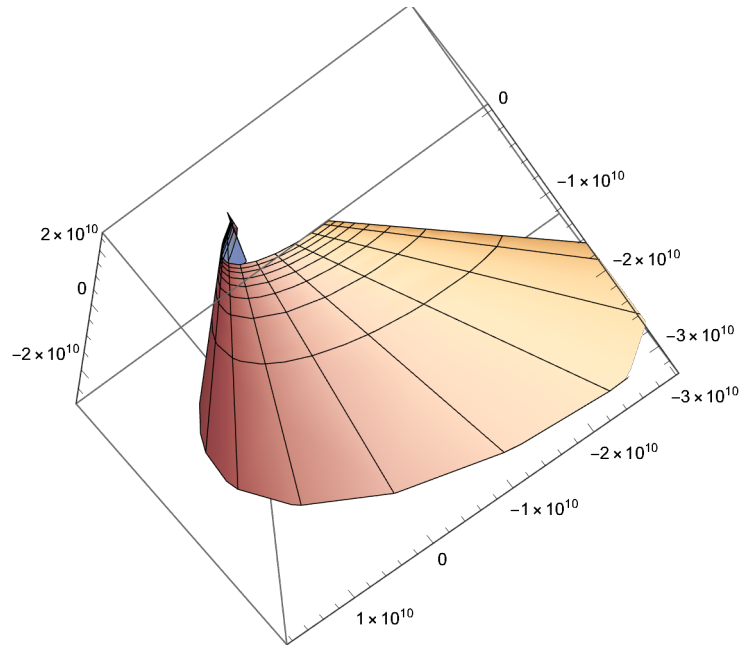


RevolutionPlot3D[

$$\left\{ \frac{1}{\sqrt{\pi}} c \sqrt{\theta} \sqrt{\left( \frac{\pi}{\theta} + \frac{4320 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{3240 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{540 r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2160}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{1080 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}, \right. \\ \left. - \frac{1}{\sqrt{\pi}} c \sqrt{\theta} \sqrt{\left( \frac{\pi}{\theta} + \frac{4320 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{3240 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{540 r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2160}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{1080 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)} \right\}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$

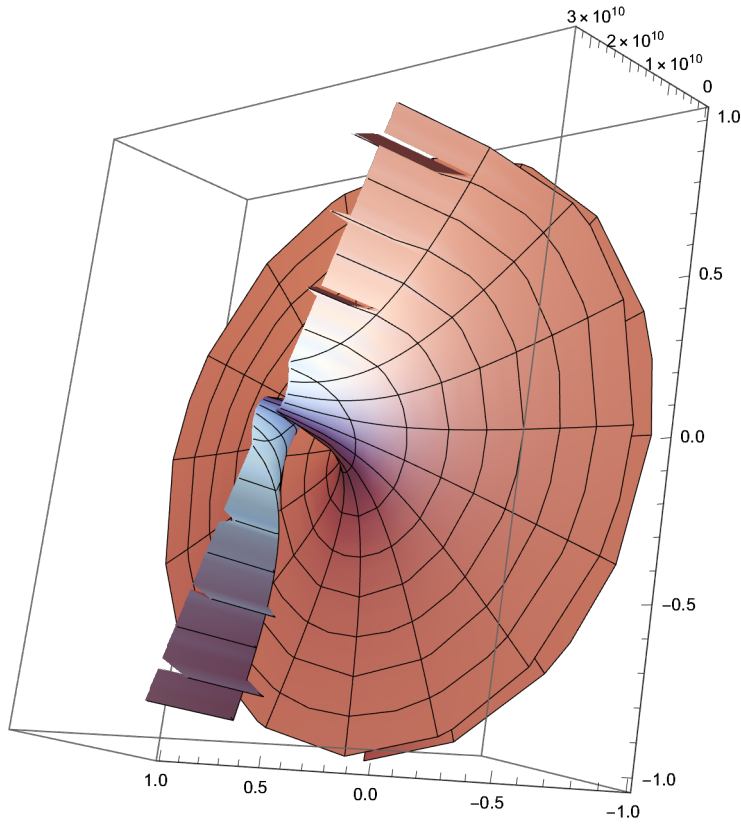
4.





RevolutionPlot3D[

$$\frac{1}{\sqrt{\pi}} \sqrt{\theta} \sqrt{\left( \frac{\pi}{\theta} + \frac{4320 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{3240 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{540 r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{2160}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{1080 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



Velocity from  $c * t' = \eta = \eta'$

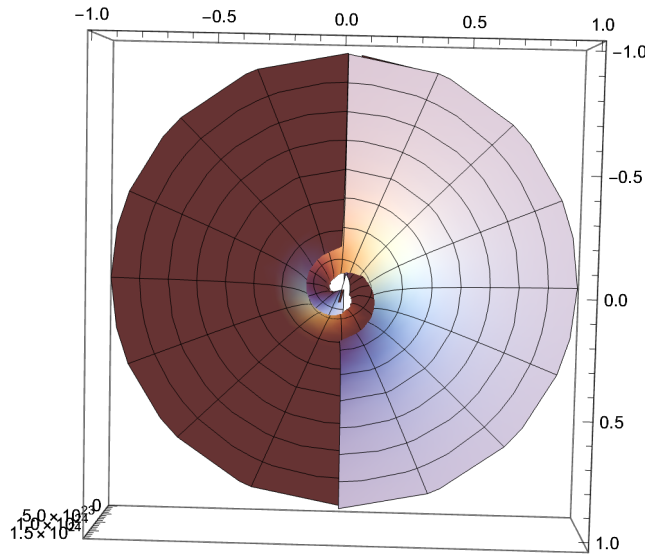
$$\text{Solve}\left[c \frac{1080 \theta}{\pi \sqrt{1 - \frac{v^2}{c^2}}} == \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \frac{5441955840000 c^2 \theta^2}{r^2} \right)} \right\}, \right. \\ \left. \left\{ v \rightarrow \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \frac{5441955840000 c^2 \theta^2}{r^2} \right)} \right\} \right\}$$

$$c := (2.99792458 * 10^8)$$

RevolutionPlot3D[

$$\frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21\,767\,823\,360\,000\,c^2\pi^2}{r^2} - \frac{87\,071\,293\,440\,000\,c^2\pi^4}{r^2(2\pi-\theta)^2} + \frac{87\,071\,293\,440\,000\,c^2\pi^3}{r^2(2\pi-\theta)} + \frac{5\,441\,955\,840\,000\,c^2\theta^2}{r^2} \right)}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



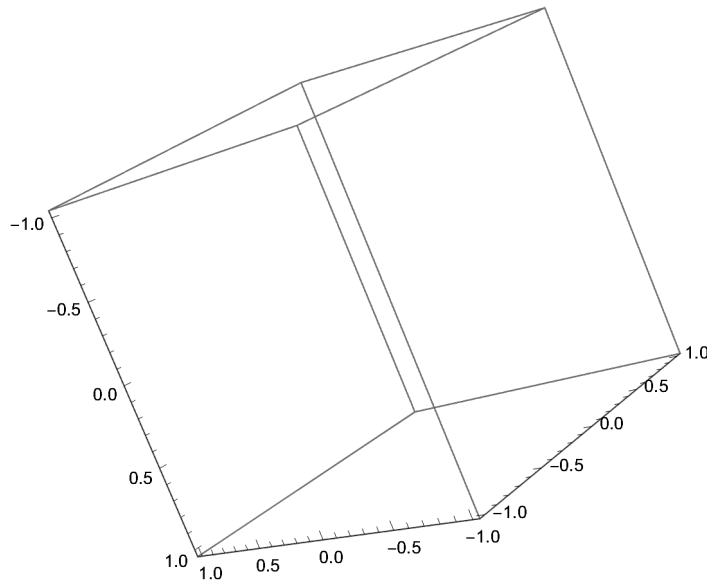
$$\left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21\,767\,823\,360\,000\,c^2\pi^2}{r^2} - \frac{87\,071\,293\,440\,000\,c^2\pi^4}{r^2(2\pi-\theta)^2} + \frac{87\,071\,293\,440\,000\,c^2\pi^3}{r^2(2\pi-\theta)} + \frac{5\,441\,955\,840\,000\,c^2\theta^2}{r^2} \right)} \right)$$

$$\left\{ \left\{ \eta \rightarrow - \left( r \sqrt{(-c^4\pi^8 + 2c^2\pi^8v^2 - \pi^8v^4 + 145\,800c^6\pi^4\theta^2 - 145\,800c^4\pi^4v^2\theta^2 - 5\,314\,410\,000c^8\theta^4)} \right) / \left( \pi^2 \sqrt{-c^4\pi^4 + 2c^2\pi^4v^2 - \pi^4v^4 + 72\,900c^6\theta^2 - 72\,900c^4v^2\theta^2} \right) \right\}, \left\{ \eta \rightarrow \left( r \sqrt{(-c^4\pi^8 + 2c^2\pi^8v^2 - \pi^8v^4 + 145\,800c^6\pi^4\theta^2 - 145\,800c^4\pi^4v^2\theta^2 - 5\,314\,410\,000c^8\theta^4)} \right) / \left( \pi^2 \sqrt{-c^4\pi^4 + 2c^2\pi^4v^2 - \pi^4v^4 + 72\,900c^6\theta^2 - 72\,900c^4v^2\theta^2} \right) \right\} \right\}$$

SphericalPlot3D[

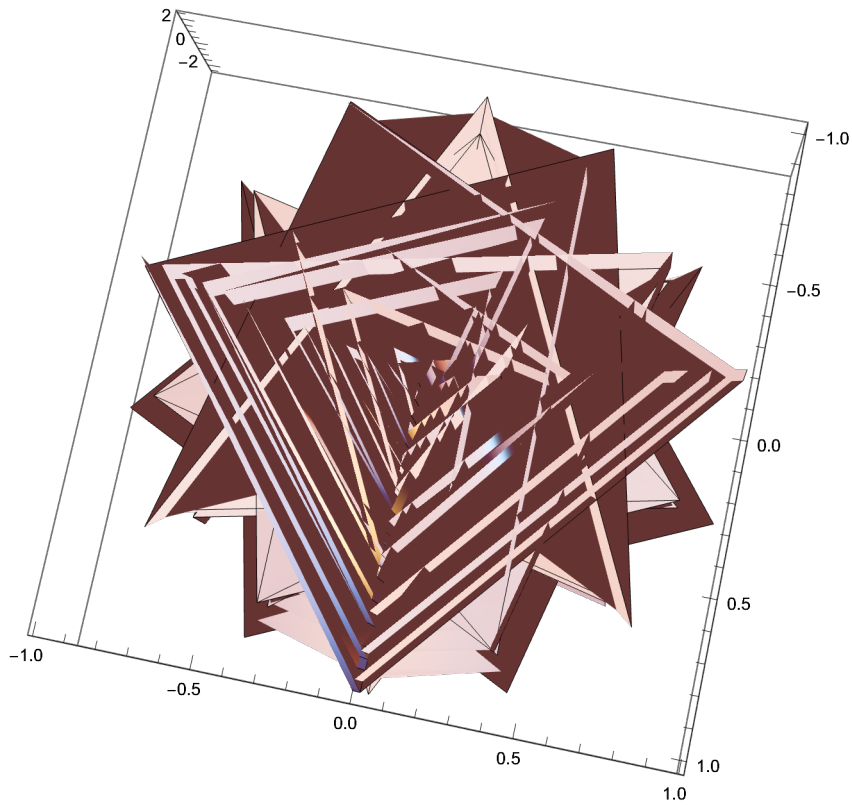
$$\left( r \sqrt{(-c^4 \pi^8 + 2 c^2 \pi^8 v^2 - \pi^8 v^4 + 145800 c^6 \pi^4 \theta^2 - 145800 c^4 \pi^4 v^2 \theta^2 - 5314410000 c^8 \theta^4)} \right) /$$

$$\left( \pi^2 \sqrt{-c^4 \pi^4 + 2 c^2 \pi^4 v^2 - \pi^4 v^4 + 72900 c^6 \theta^2 - 72900 c^4 v^2 \theta^2} \right), \{\theta, -\pi, \pi\}, \{v, -4\pi, 4\pi\}]$$



RevolutionPlot3D[

$$\begin{aligned}
 & \left( r \sqrt{\left( -c^4 \pi^8 + 2 c^2 \pi^8 \left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \frac{5441955840000 c^2 \theta^2}{r^2} \right) \right)^2 - \right. \\
 & \quad \left. \pi^8 \left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \frac{5441955840000 c^2 \theta^2}{r^2} \right) \right)^4 + \right. \\
 & \quad \left. 145800 c^6 \pi^4 \theta^2 - 145800 c^4 \pi^4 \left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5441955840000 c^2 \theta^2}{r^2} \right) \right)^2 \theta^2 - 5314410000 c^8 \theta^4 \right) \Bigg) / \\
 & \left( \pi^2 \sqrt{\left( -c^4 \pi^4 + 2 c^2 \pi^4 \left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \frac{5441955840000 c^2 \theta^2}{r^2} \right) \right)^2 - \right. \\
 & \quad \left. \pi^4 \left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \frac{5441955840000 c^2 \theta^2}{r^2} \right) \right)^4 + \right. \\
 & \quad \left. 72900 c^6 \theta^2 - 72900 c^4 \left( \frac{1}{\pi} c \sqrt{\left( \pi^2 - \frac{21767823360000 c^2 \pi^2}{r^2} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{87071293440000 c^2 \pi^4}{r^2 (2\pi - \theta)^2} + \frac{87071293440000 c^2 \pi^3}{r^2 (2\pi - \theta)} + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5441955840000 c^2 \theta^2}{r^2} \right) \right)^2 \theta^2 \right) \Bigg) \Bigg), \{r, -1, 1\}, \{\theta, -40\pi, 40\pi\} \Big]
 \end{aligned}$$



$$D\left[\frac{i c \sqrt{\theta} \sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}, \theta\right]$$

$$\left(1.05993 \times 10^8 i \sqrt{\theta} \left(\frac{2}{\theta^2} - \frac{2 \theta (4 \pi r^2 - 2 r^2 \theta)}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{\theta^2 (4 \pi r^2 - 2 r^2 \theta)}{2 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right)\right) / \left(\sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}\right) +$$

$$\frac{1.05993 \times 10^8 i \sqrt{-\frac{2}{\theta} + \frac{4 \theta}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\theta^2}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{\theta}}$$

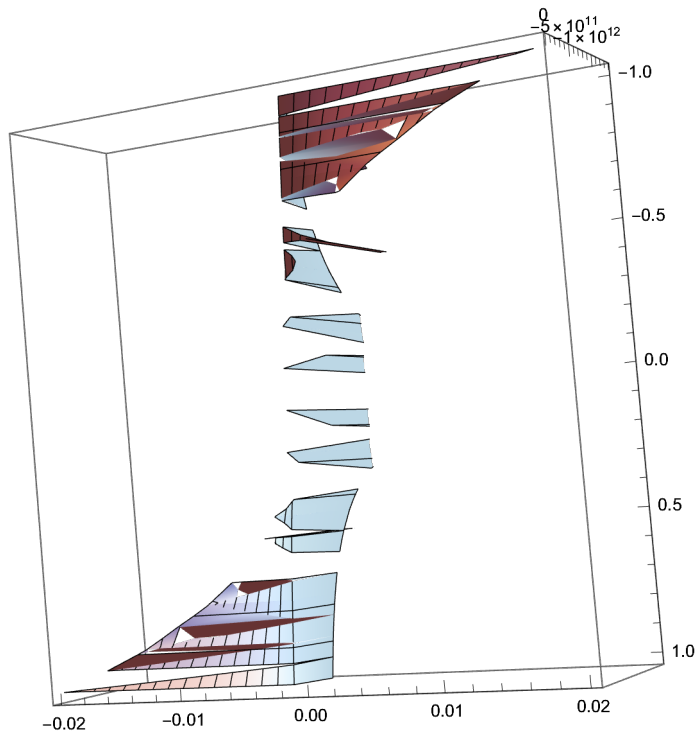
RevolutionPlot3D[

$$\left( 1.0599264000019161 \cdot 10^8 \sqrt{\theta} \left( \frac{2}{\theta^2} - \frac{2\theta(4\pi r^2 - 2r^2\theta)}{(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{\theta^2(4\pi r^2 - 2r^2\theta)}{2\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{4}{\sqrt{4\pi r^2\theta - r^2\theta^2}} - \frac{2\theta}{\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right) \right) /$$

$$\left( \sqrt{-\frac{2}{\theta} + \frac{4\theta}{\sqrt{4\pi r^2\theta - r^2\theta^2}} - \frac{\theta^2}{\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}} \right) +$$

$$\frac{1.0599264000019161 \cdot 10^8 \sqrt{-\frac{2}{\theta} + \frac{4\theta}{\sqrt{4\pi r^2\theta - r^2\theta^2}} - \frac{\theta^2}{\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}}}{\sqrt{\theta}},$$

{r, -1, 1}, {θ, -4π, 4π}]



$$\left( r \sqrt{1 - ((v)^2 / c^2)} \right) / \left( \theta / \sqrt{1 - ((v)^2 / c^2)} \right) = D \left[ \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, r \right]$$

## I. Math for Transforming a Circle into a Cone



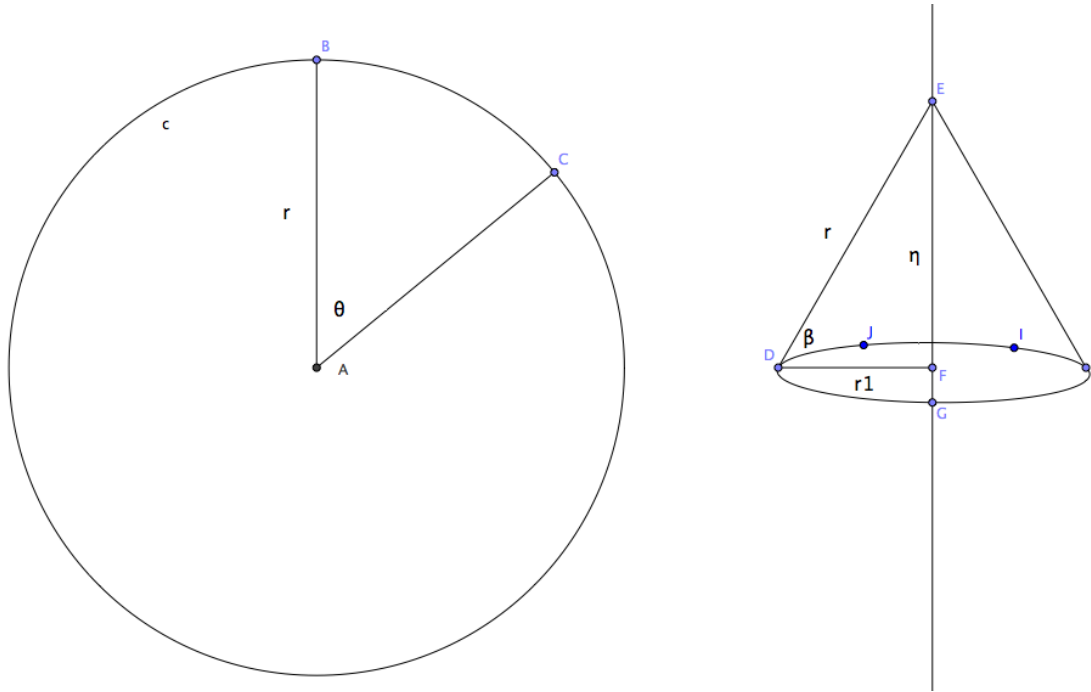


Figure 1

When a sector of a circle is removed, we may "fold up" the resulting shape into a cone. The parameters are related by the following theorem :

**Theorem 1** When a sector of angle  $\theta$  is removed from a circle of radius  $r$  and the resulting shape is folded into a cone, then the base of the cone has radius  $r_1$  given by  $r_1 = r - \frac{r\theta}{2\pi}$  ; and height  $\eta$ , given by  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$

Proof. The circumference of the initial circle is  $2\pi r$  and the wedge removed has an arc length  $r\theta$ . Therefore, the remaining circumference is of length  $r(2\pi - \theta)$ , and after the fold, this is the circumference of the base of the cone.

Establishing the circumference of the base of the cone, from the equation,  $\theta r = 2\pi r - 2\pi r_1$ , we calculate that its radius  $r_1$  is  $\frac{2\pi r - r\theta}{2\pi}$ , which simplifies to  $r - \frac{r\theta}{2\pi}$ . Thus, we have proved the first part of the theorem.

To find the height of the cone,  $\eta$ , we apply the Pythagorean theorem to a right triangle formed between the apex of the cone, the center of the base, and a point on the circumference of the base. This gives  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$ , where  $\beta$  is the angle formed by the slant of the cone and the base of the cone. The initial radius is always equal to the slant of the cone, and the height of the cone is always orthogonal to the center of the base of the cone.

This element of the theorem assumes modus ponens from the thought of  $\eta = \sqrt{r^2 - r_1^2} = r \sin[\beta]$ , and it assumes addition and commutation.

**Lemma 1** The height of the cone can be calculated in terms of  $r$  and  $\theta$ .

Proof.

$$\theta r = 2\pi r - 2\pi r_1$$

$$\eta = \sqrt{r^2 - r_1^2}$$

$$\theta r = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$$

$$\eta = \frac{\sqrt{4\pi^2 r^2 \theta - r^2 \theta^2}}{2\pi}$$

**Lemma 2** The angle  $\theta$  can be calculated in terms of  $r$  and  $\eta$ .

Proof

$$\text{Solve}\left[\eta == \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi\left(r^2 - \sqrt{r^4 - r^2\eta^2}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 + \sqrt{r^4 - r^2\eta^2}\right)}{r^2}\right\}\right\}$$

**Lemma 3** The initial radius is a function of  $\theta$  and  $\eta$ .

$$\text{Solve}\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} == \eta, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}, \left\{r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}\right\}\right\}$$

**Lemma 4** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\beta$  is a function of  $\theta$  alone.

Proof. Since we have shown that  $\theta r = 2\pi r - 2\pi r_1$  and  $r_1 \rightarrow \sqrt{r^2 - \eta^2}$ , we can substitute the expression for  $r_1$ , calculated from the Pythagorean theorem in terms of the height of the cone and the initial radius of the circle, into the expression for  $\theta r$  in terms of the change in circumference of the initial circle to the circle, which is the base of the cone.  $\theta r = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$ , thus,  $\eta = \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} = (r \sin[\beta])$ . From  $\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r$ , we note that  $r = \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}$ , so

$$\theta = 2\left(\pi \pm \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right) = \frac{2\pi\left(r^2 \pm \sqrt{r^4 - r^2\eta^2}\right)}{r^2}, \text{ because } 1 = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}$$

**Lemma 5** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\theta$  is a function of  $\beta$  alone, and the initial radius can be calculated purely in terms of the angle  $\theta$ .

$$\beta = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] = f(\theta)$$

$$\sin[\beta] = \frac{\eta}{r} = \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{r^2\pi} = \frac{4\pi r^2\theta - r^2\theta^2}{4\pi^2 r} = \frac{r(4\pi - \theta)\theta}{4\pi^2}$$

$$\beta \rightarrow \text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right] = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

$$\text{Solve}\left[\text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right] == \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], r\right]$$

$$\left\{\left\{r \rightarrow \frac{2\pi\sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}\right\}\right\}$$

$$\frac{2\pi\sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} = g(\theta)$$

$$\frac{d\eta}{d\left(\frac{\theta}{2\pi}\right)} =$$

$$D\left[2\pi\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right] = \frac{4\pi r^2 - 2r^2\theta}{2\sqrt{4\pi r^2\theta - r^2\theta^2}} = \text{Instantaneous Velocity} =$$

$$\text{Average Velocity} = \frac{2\pi\eta}{\theta}$$

$$\left\{ \left\{ \theta \rightarrow \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}} - \frac{2\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}}{3r^2} \right\}, \right.$$

$$\left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{(1+i\sqrt{3})(-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2)}{12\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}} + \frac{(1-i\sqrt{3})\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}}{3r^2} \right\},$$

$$\left\{ \theta \rightarrow \frac{4\pi}{3} - \frac{(1-i\sqrt{3})(-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2)}{12\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}} + \frac{(1+i\sqrt{3})\pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6})^{1/3}}{3r^2} \right\}$$

$\frac{1}{0} :=$  Where,  $:=$  means

"by arbitrary pattern of substitution of definitions within the lemmas of theorems one and two,"

Because, it can be shown that,

$$1 = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} \text{ and } 0 = \theta r - 2\pi r - 2\pi \sqrt{(r^2 - \eta^2)}$$

$$\frac{1}{0} := \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2} \left( 2\pi r - r\theta - 2\pi \sqrt{r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}} \right)}.$$

$$\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2} \left( 2\pi r - r\theta - 2\pi \sqrt{r^2 - \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2}} \right)} =$$

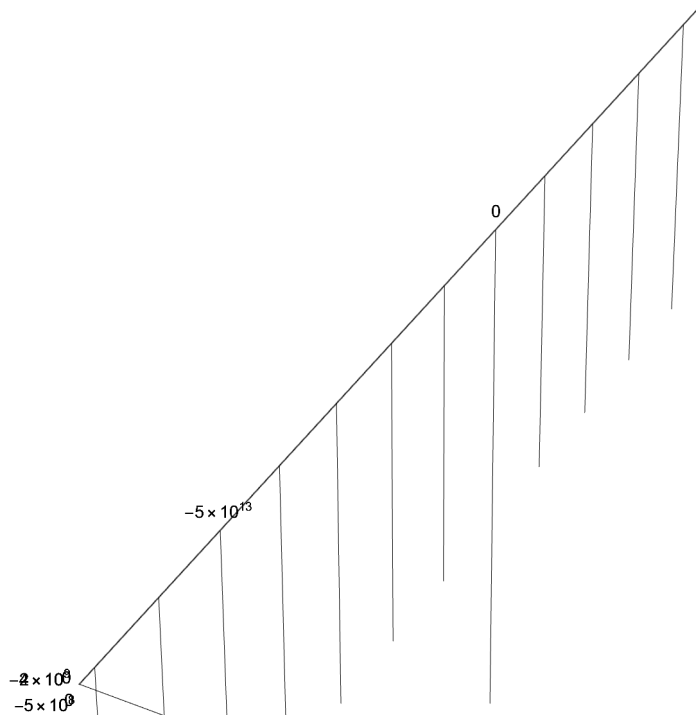
$$(2\pi \sin[\beta]) / \left( \sqrt{4\pi\theta - \theta^2} \left( 2\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} - \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \theta - \right. \right.$$

$$\left. \left. 2\pi \sqrt{\left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 - \frac{4\pi \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}{4\pi^2}} \right) \right) =$$

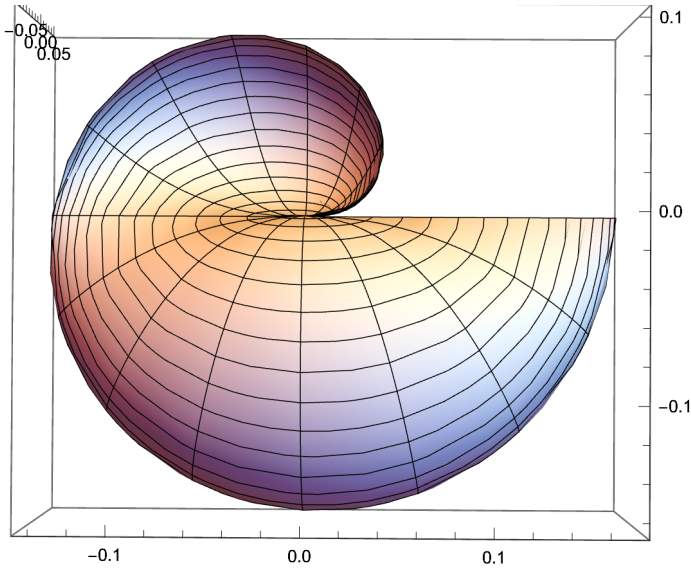
$$(2\pi \sin[\beta]) / \left( \sqrt{4\pi\theta - \theta^2} \left( 2\pi \frac{1}{(4\pi - \theta)\theta} 2\pi \right. \right.$$

$$\left. \left. \sqrt{\left( (4\pi - \theta) \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \right. \right.$$

$$\begin{aligned}
& \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) - \\
& \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - 2 \pi \\
& \sqrt{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 - \frac{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}{4 \pi^2}} \right) \\
& \text{SphericalPlot3D}[(2 \pi \sin[\beta]) / \left( \sqrt{4 \pi \theta - \theta^2} \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 - \frac{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}{4 \pi^2}} \right) \right), \\
& \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]
\end{aligned}$$





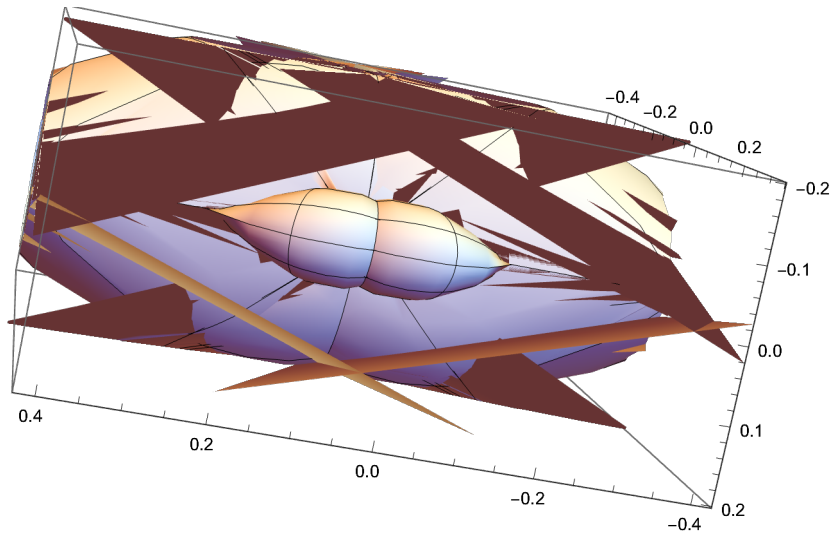


$$\begin{aligned}
 & (2 \pi \sin[\beta]) / \left( \sqrt{4 \pi \theta - \theta^2} \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - \right. \right. \\
 & \quad \left. \left. 2 \pi \sqrt{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 - \frac{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}{4 \pi^2}} \right) \right) \\
 & (2 \pi \sin[\beta]) / \left( \sqrt{4 \pi \theta - \theta^2} \left( 2 \pi \frac{1}{(4 \pi - \theta) \theta} 2 \pi \right. \right. \\
 & \quad \left. \left. \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \right. \\
 & \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) - \\
 & \quad \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - \\
 & 2 \\
 & \pi
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 - \frac{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}{4 \pi^2}} \right) \\
 & \frac{4 \pi}{3} - \\
 & \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} +} \\
 & \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \\
 & (2 \pi \sin[\beta]) / \left( \sqrt{4 \pi \theta - \theta^2} \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - \right. \right. \\
 & \left. \left. 2 \pi \sqrt{\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 - \frac{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}{4 \pi^2}} \right) \right) \\
 & \text{SphericalPlot3D} \left[ (2 \pi \sin[\beta]) / (\sqrt{4 \pi \theta - \theta^2}) / \right. \\
 & \left. \left( \left( 2 \pi \frac{1}{(4 \pi - \theta) \theta} 2 \pi \sqrt{((4 \pi - \theta) \theta)} - 2 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \right) - \right. \right. \right. \\
 & \left. \left. \left. \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^{\wedge 2} \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} \right]
 \end{aligned}$$

$$\text{SphericalPlot3D}\left[(2 \pi \sin[\beta]) \sqrt{(4 \pi \theta - (\theta)^2)} \left(2 \pi \frac{1}{(4 \pi - \theta) \theta} \sqrt{(4 \pi - \theta) \left(\frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - 2 \pi \sqrt{\left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 - \frac{4 \pi \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^2 \theta^2}{4 \pi^2}}\right),$$

{ $\theta$ ,  $-4 \pi$ ,  $4 \pi$ }, { $\beta$ ,  
 $-\pi$ ,  
 $\pi$ }



$$\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$\left\{\theta \rightarrow \frac{4 \pi}{3} - \left(-4 \pi^2 + 12 \pi^2 \sin[\beta]^2\right) \sqrt{\left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)}\right\}$$



$$\begin{aligned}
& \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \Big\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} + \left( (1 + i \sqrt{3}) (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 12 (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) - \\
& \quad \frac{1}{3} (1 - i \sqrt{3}) (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \Big\}, \\
& \left\{ \theta \rightarrow \frac{4 \pi}{3} + \left( (1 - i \sqrt{3}) (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \\
& \quad \left( 12 (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) - \\
& \quad \frac{1}{3} (1 + i \sqrt{3}) (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \\
& \quad \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \Big\} \\
& \text{ContourPlot3D} \left[ \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( 2 \pi r - r \theta - 2 \pi \sqrt{r^2 - \frac{4 \pi r^2 \theta - r^2 \theta^2}{4 \pi^2}} \right), \right. \\
& \quad \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi/2, \pi/2\}, \text{AxesLabel} \rightarrow \text{Automatic} \Big] \\
& \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( 2 \pi \frac{1}{(4 \pi - \theta) \theta} 2 \pi \right. \\
& \quad \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \\
& \quad \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \right. \\
& \quad \left. \frac{2}{3} (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \right) - \\
& \quad \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \\
& \quad \theta -
\end{aligned}$$

2

$\pi$

$$\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{4\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}{4\pi^2}}$$

SphericalPlot3D[

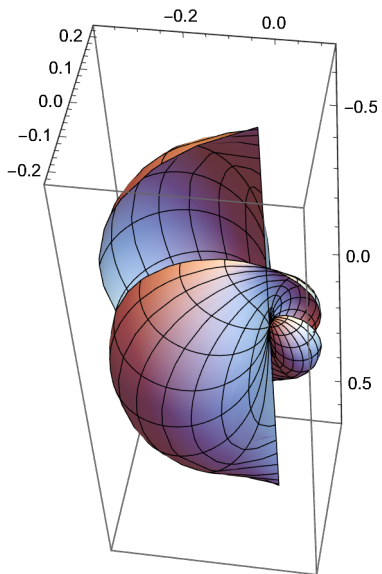
$$\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}} \left/ \left( 2\pi\frac{1}{(4\pi-\theta)\theta} 2\pi\sqrt{\left((4\pi-\theta)\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2\sin[\beta]^2)\right)\right)} \right. \right.$$

$$\left. \left( 6\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3} \right) + \right.$$

$$\left. \frac{2}{3}\left(-\pi^3 + 18\pi^3\sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2 + 11\pi^6\sin[\beta]^4 + \pi^6\sin[\beta]^6}\right)^{1/3} \right) -$$

$$\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta - 2\pi\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{4\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}{4\pi^2}} \right],$$

{ $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi$  / 2,  $\pi$  / 2}}



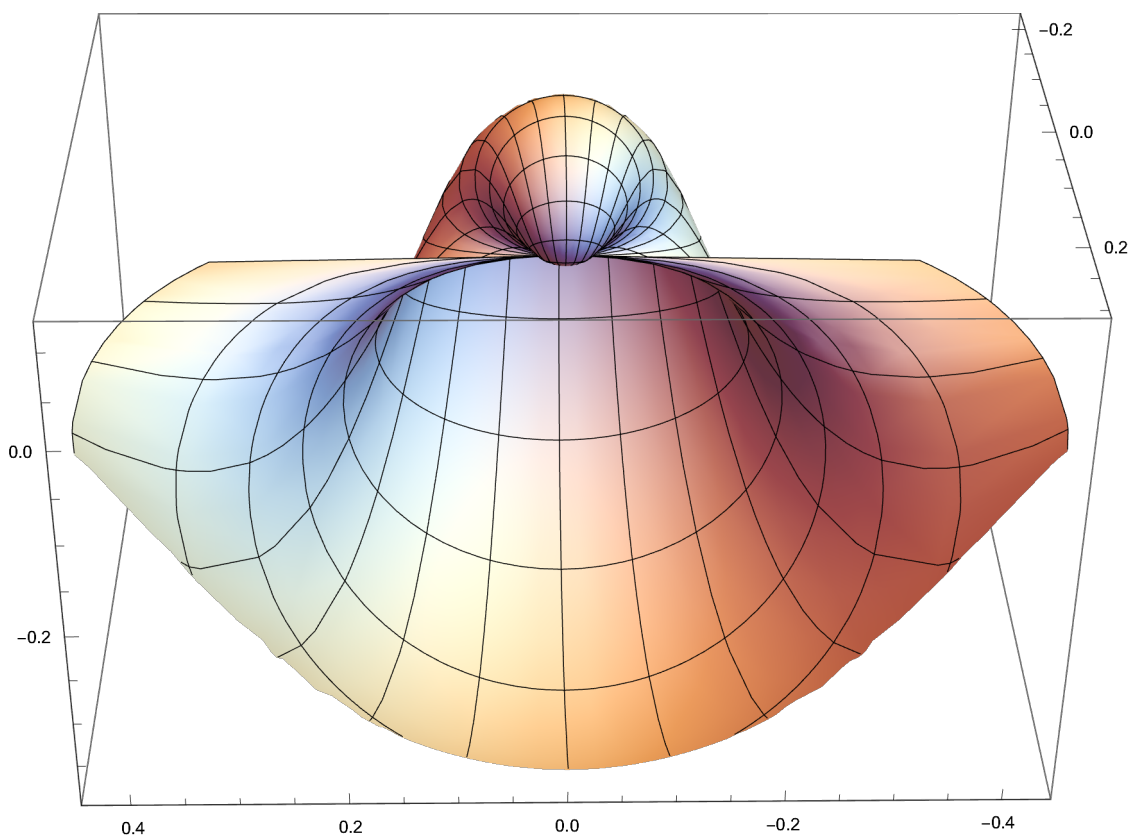
$$\left( (2\pi\sin[\beta]) / (\sqrt{4\pi\theta-\theta^2}) \right) \left/ \left( 2\pi\frac{1}{(4\pi-\theta)\theta} \right. \right.$$

$$\begin{aligned}
& 2 \pi \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) - \\
& 2 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta \right) - \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \wedge 2 \Bigg) \\
& \frac{2 \pi r - r \theta}{2 \pi} \\
& \text{SphericalPlot3D}[(2 \pi \sin[\beta]) / \\
& \quad \left( \sqrt{4 \pi \theta - \theta^2} \left( 2 \pi \frac{1}{(4 \pi - \theta) \theta} 2 \pi \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) - \right. \\
& \quad \left. \left. \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - 2 \pi \frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \right) \right) \Bigg), \\
& \{\beta, -\pi / 2, \pi / 2\}, \{\theta, -2 \pi, 2 \\
& \quad \pi\} \Big]
\end{aligned}$$

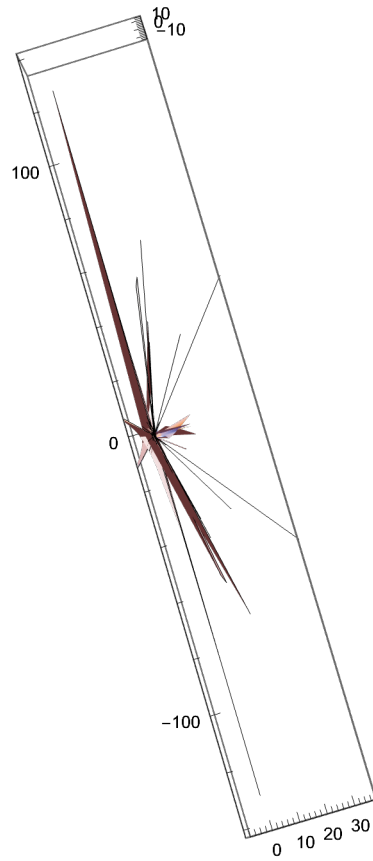
SphericalPlot3D[(2 π Sin[β]) /

$$\left( \sqrt{4 \pi \theta - \theta^2} \left( 2 \pi \frac{1}{(4 \pi - \theta) \theta} 2 \pi \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta - 2 \pi \frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \right) \right),$$

{β, -π / 2, π / 2}, {θ, -2 π, 2 π}]



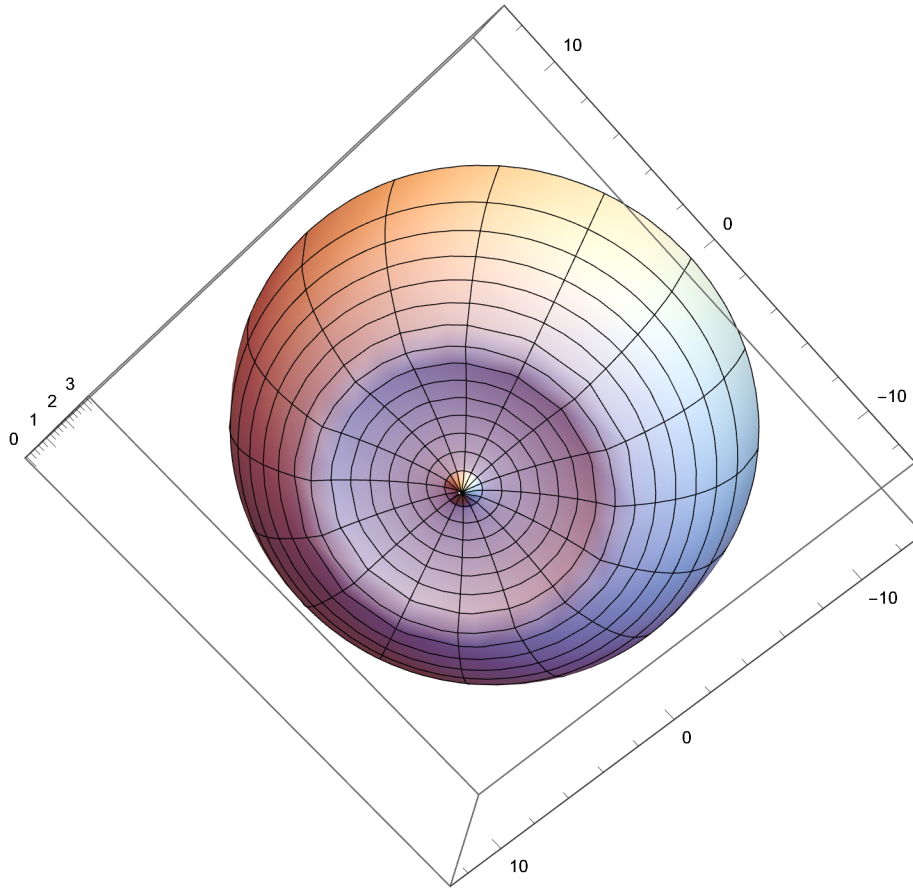
$$\begin{aligned}
& \text{SphericalPlot3D}\left[ \right. \\
& \quad (2 \pi \sin[\beta]) / \left( \sqrt{4 \pi \theta - \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2} \left( 2 \pi \frac{1}{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right. \right. \\
& \quad \quad 2 \pi \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \\
& \quad \quad \quad \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \quad \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) - \\
& \quad \quad \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - 2 \pi \frac{1}{2 \pi} \\
& \quad \quad \left( \frac{2 \pi \sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta}}{(4 \pi - \theta) \theta} - \right. \\
& \quad \quad \quad \left. \frac{2 \pi \sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta}}{(4 \pi - \theta) \theta} \right. \\
& \quad \quad \quad \left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]^2} \right)} \right) \right) \right) \right) \right), \\
& \quad \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} \left. \right]
\end{aligned}$$



$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \{r, -1, 1\}, \{\theta, -30 \pi, 30 \pi\}\right]$$





$$\eta = \frac{\sqrt{4 \pi r'^2 \theta' - r'^2 \theta'^2}}{2 \pi}$$

$$c := (2.99792458 * 10^8)$$

$$\frac{1}{2 \pi} \left( \sqrt{4 \pi \left( r \sqrt{1 - ((u^2) / (c^2))} \right)^2 \left( \theta / \sqrt{1 - ((u^2) / (c^2))} \right) - \left( r \sqrt{1 - ((u^2) / (c^2))} \right)^2 \left( \theta / \sqrt{1 - ((u^2) / (c^2))} \right)^2} \right)$$

$$\frac{\sqrt{4 \pi r^2 \sqrt{1 - \frac{u^2}{c^2}} \theta - r^2 \theta^2}}{2 \pi}$$

$$\eta = \frac{\sqrt{4 \pi r^2 \sqrt{1 - \frac{u^2}{c^2}} \theta - r^2 \theta^2}}{2 \pi} == \frac{\sqrt{4 \pi r^2 \sqrt{1 - \frac{(r/\theta)^2}{c^2}} \theta - r^2 \theta^2}}{2 \pi}$$



$$D\left[\frac{\sqrt{4 \pi r^2 \sqrt{1 - \frac{v^2}{c^2}} \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{4 \pi r^2 \sqrt{1 - \frac{v^2}{c^2}} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{v^2}{c^2}} \theta - r^2 \theta^2}}$$

$$\text{Solve}\left[\frac{4 \pi r^2 \sqrt{1 - \frac{v^2}{c^2}} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{v^2}{c^2}} \theta - r^2 \theta^2}} == v, v\right]$$

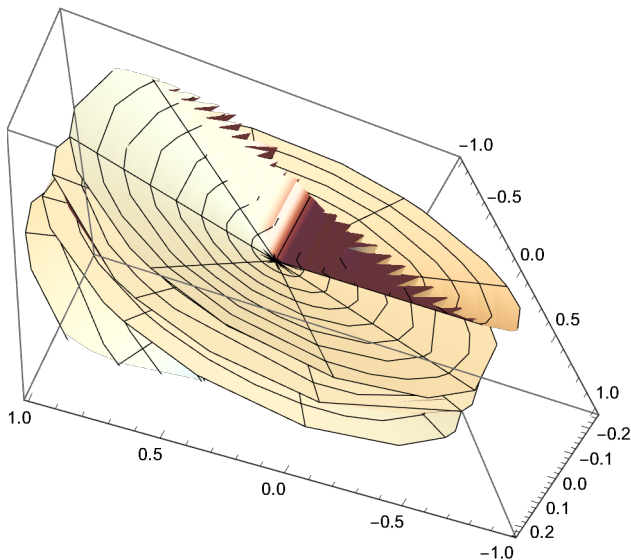
Velocity is constant and so is r' or r.

$$D\left[\frac{\sqrt{4 \pi r^2 \sqrt{1 - \frac{((1/(1080/\pi)) (r/\theta))^2}{c^2}} \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

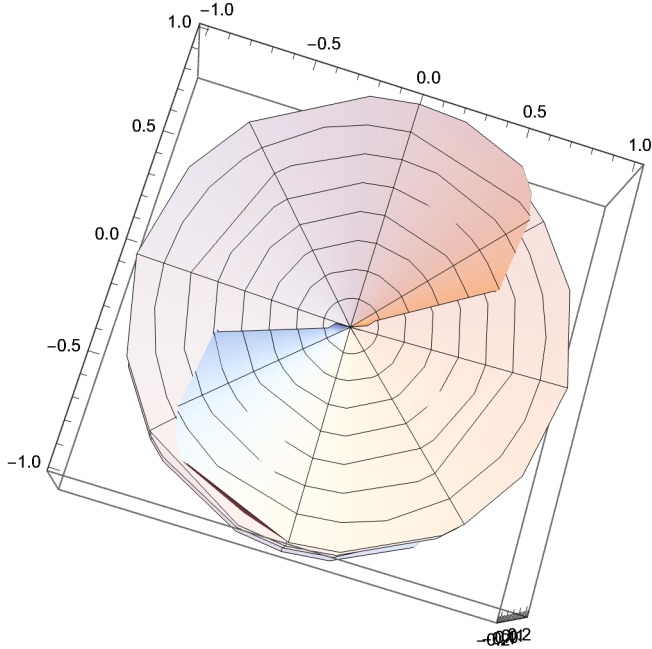
$$\frac{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}}$$

RevolutionPlot3D[

$$\frac{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$

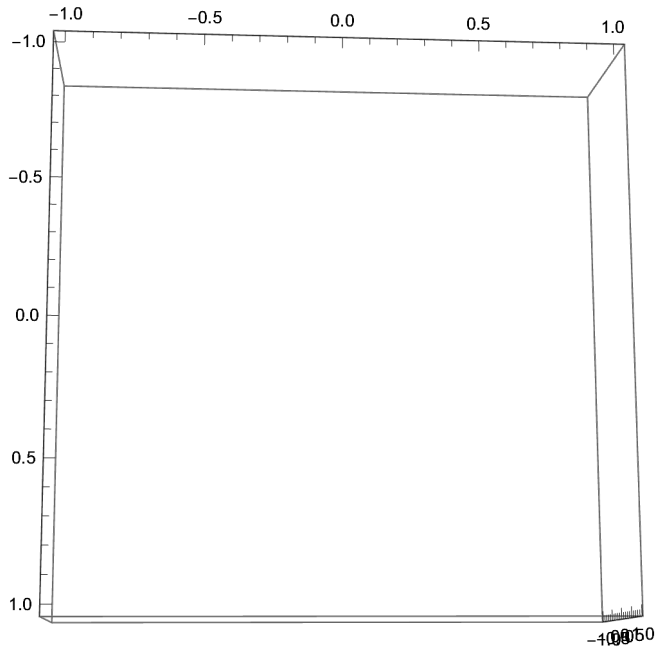


$$\text{RevolutionPlot3D}\left[\frac{4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} + \frac{4 \pi r^4}{c^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}}} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\begin{aligned} & D\left[\frac{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}}, \theta\right] \\ & - \frac{\left(4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta\right)^2}{8 \pi \left(4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2\right)^{3/2}} + \\ & - 2 r^2 - \frac{\pi^5 r^6}{340122240000 c^4 \left(1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}\right)^{3/2} \theta^5} - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta^3} \\ & \frac{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}} \end{aligned}$$

$$\begin{aligned}
 & \text{RevolutionPlot3D} \left[ \left( \frac{h \pi^3 r^2}{1259712000 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta^4} - \frac{h \pi \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}}{1080 \theta^2} \right) / \right. \\
 & \left. - \frac{\left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta \right)^2}{8 \pi \left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2 \right)^{3/2}} + \right. \\
 & \left. - 2 r^2 - \frac{\frac{\pi^5 r^6}{340122240000 c^4 \left( 1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2} \right)^{3/2}} \theta^5 - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} \theta^3}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}} \right) \\
 & \left. - \frac{\left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta \right)^2}{8 \pi \left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2 \right)^{3/2}} + \right. \\
 & \left. - 2 r^2 - \frac{\frac{\pi^5 r^6}{340122240000 c^4 \left( 1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2} \right)^{3/2}} \theta^5 - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} \theta^3}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}} \right), \\
 & \{r, -1, 1\}, \{\theta, -14 \pi, 14 \pi\}
 \end{aligned}$$



$$\text{Solve}\left[m \left[ - \frac{\left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta \right)^2}{8 \pi \left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2 \right)^{3/2}} + \right. \right. \\ \left. \left. \frac{-2 r^2 - \frac{\pi^5 r^6}{340122240000 c^4 \left( 1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2} \right)^{3/2} \theta^5} - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} \theta^3}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}} \right] == \right.$$

$$D\left[h \left( \left( 1 / \left( (1080 / \pi) \theta \right) \left( \sqrt{1 - \left( (r / \left( (1080 / \pi) \theta \right))^2 / (c^2)} \right) \right) \right), \theta \right], m\right]$$

$$\left\{ m \rightarrow \left( \frac{h \pi^3 r^2}{1259712000 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta^4} - \frac{h \pi \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}}{1080 \theta^2} \right) / \right.$$

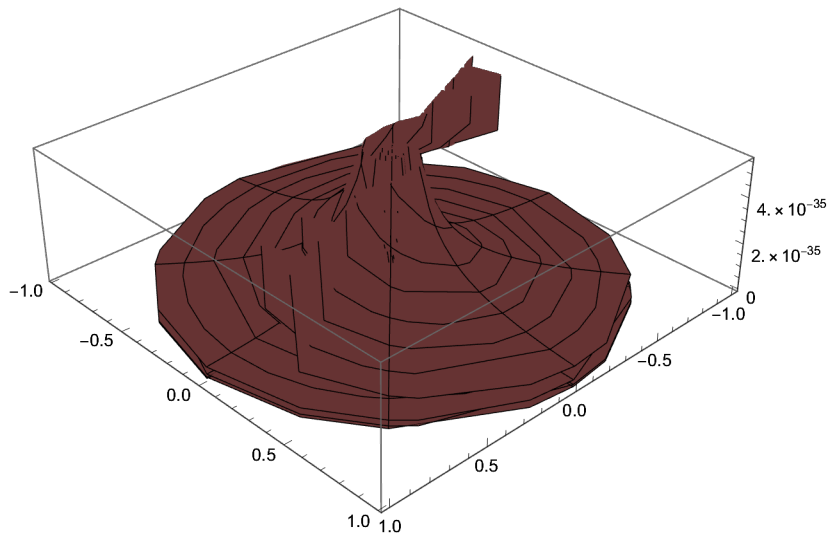
$$\left[ - \frac{\left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta \right)^2}{8 \pi \left( 4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2 \right)^{3/2}} + \right.$$

$$\left. \frac{-2 r^2 - \frac{\pi^5 r^6}{340122240000 c^4 \left( 1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2} \right)^{3/2} \theta^5} - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} \theta^3}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}} \right\}$$

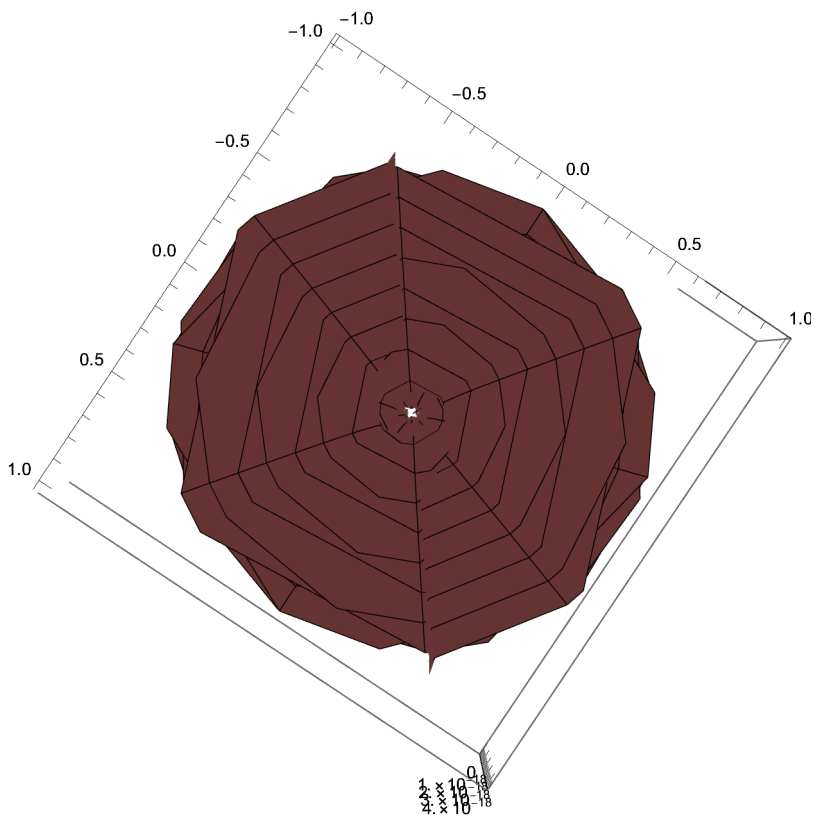
$$c := (2.99792458 * 10^8)$$

$$h := (6.626068 * 10^{-34})$$

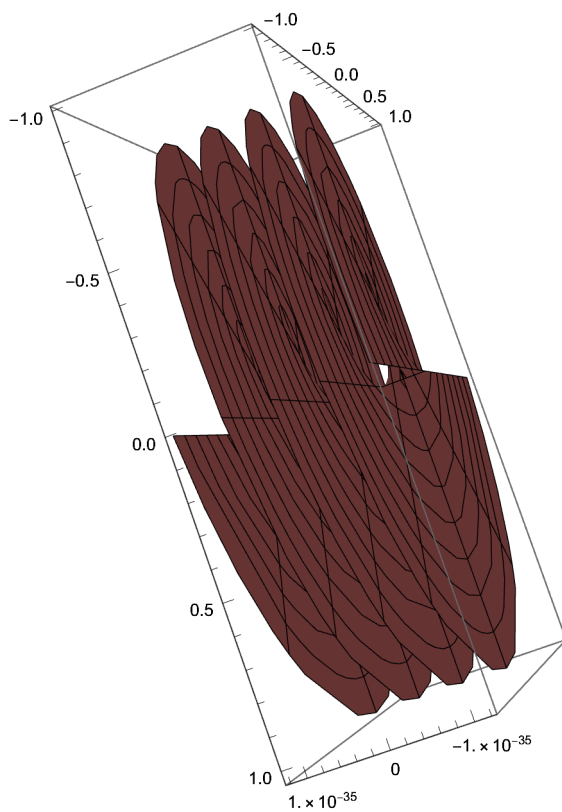
$$\text{RevolutionPlot3D}\left[\left(\frac{h \pi^3 r^2}{1259712000 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - \frac{h \pi \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}}{1080 \theta^2}\right) / \right. \\ \left. - \frac{\left(4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta\right)^2}{8 \pi \left(4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2\right)^{3/2}} + \right. \\ \left. \frac{-2 r^2 - \frac{\pi^5 r^6}{340122240000 c^4 \left(1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}\right)^{3/2}} \theta^5 - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} \theta^3}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}}\right], \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



$$\text{RevolutionPlot3D}\left[\left(\frac{h \pi^3 r^2}{1259712000 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta^4} - \frac{h \pi \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}}{1080 \theta^2}\right) / \right. \\ \left. - \frac{\left(4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} + \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}}} - 2 r^2 \theta\right)^2}{8 \pi \left(4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2\right)^{3/2}} + \right. \\ \left. - 2 r^2 - \frac{\pi^5 r^6}{340122240000 c^4 \left(1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}\right)^{3/2} \theta^5} - \frac{\pi^3 r^4}{291600 c^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta^3}\right) / \\ \left. 4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{\pi^2 r^2}{1166400 c^2 \theta^2}} \theta - r^2 \theta^2}\right] \\ c^2, \{r, -1, 1\}, \{\theta, -12 \pi, 12 \pi\}]$$



$$\text{RevolutionPlot3D}\left[\frac{h \pi^2 \theta \sqrt{4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta - r^2 \theta^2}}{270 \left(4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} + \frac{4 \pi r^4}{c^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta^2} - 2 r^2 \theta\right)}\right. \\ \left.\frac{4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} + \frac{4 \pi r^4}{c^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta^2} - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



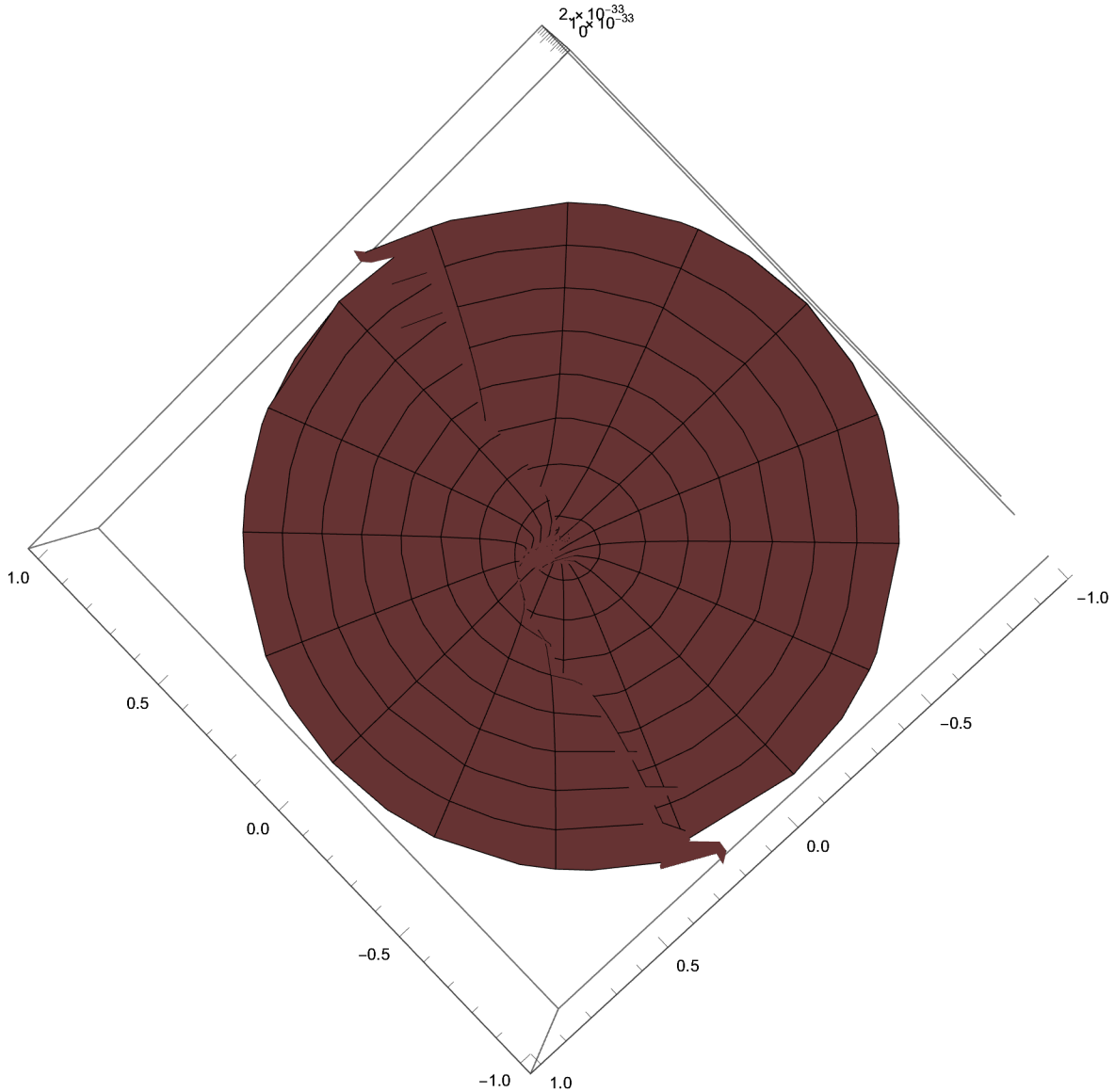
$h := (6.626068 * 10^{-34})$



$$\text{Solve}\left[D[h(1/((1080/\pi)/\theta))]=m\frac{4\pi r^2\sqrt{1-\frac{r^2}{c^2\theta^2}}+\frac{4\pi r^4}{c^2\sqrt{1-\frac{r^2}{c^2\theta^2}}}-2r^2\theta}{4\pi\sqrt{4\pi r^2\sqrt{1-\frac{r^2}{c^2\theta^2}}\theta-r^2\theta^2}},m\right]$$

$$\left\{\left\{m\rightarrow\frac{h\pi^2\theta\sqrt{4\pi r^2\sqrt{1-\frac{r^2}{c^2\theta^2}}\theta-r^2\theta^2}}{270\left(4\pi r^2\sqrt{1-\frac{r^2}{c^2\theta^2}}+\frac{4\pi r^4}{c^2\sqrt{1-\frac{r^2}{c^2\theta^2}}}-2r^2\theta\right)}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{h \pi^2 \theta \sqrt{4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta - r^2 \theta^2}}{270 \left(4 \pi r^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} + \frac{4 \pi r^4}{c^2 \sqrt{1 - \frac{r^2}{c^2 \theta^2}} \theta^2} - 2 r^2 \theta\right)}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$c := (2.99792458 * 10^8)$

$\eta := \text{rate} * \text{time} = c * \tau = \text{height of cone}$  (193)

$\tau := 6 \left( \theta_{\text{degrees}} \right) = 6 \left( (180 / \pi) \theta \right)$ , because if theta were in radians to begin with, we would have to convert that number of radians to degrees. This way,

both our thetas are in radians,

but our result accounts for the constant of the degrees involved in measuring time.

$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$v = \lambda v = r (1 / (1080 / \pi) \theta) = (1 / (1080 / \pi)) D[\eta, \theta] = 1 / (1080 / \pi)$$

$$D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right] \quad (194)$$

The velocity of  $\eta$  is equal to the first derivative of  $\eta$  with respect to time. The constant  $(1/(1080/\pi))$  is taken out of the equation in order to perform the derivative.

$$(1 / (1080 / \pi)) D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

let 's just say that velocity is constant

$$(1 / (1080 / \pi)) D\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \left( \sqrt{1 - ((v)^2 / c^2)} \right), \theta\right]$$

$$\frac{\sqrt{1 - \frac{v^2}{c^2}} (4 \pi r^2 - 2 r^2 \theta)}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = c$$

Since we are specifying that the velocity is constant equal to the speed of light.

$$c := (2.99792458 * 10^8)$$

$$\text{Solve}\left[\frac{\sqrt{1 - \frac{v^2}{c^2}} (4 \pi r^2 - 2 r^2 \theta)}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == c, v\right]$$

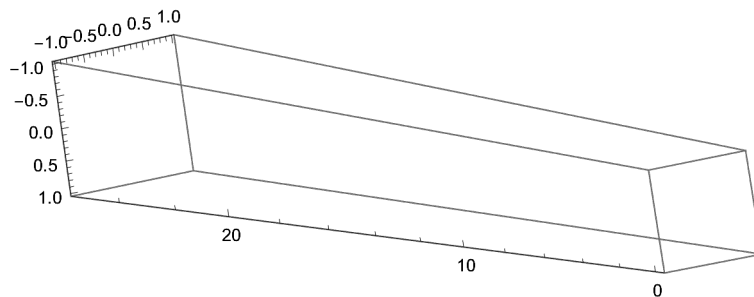
$$\left\{ \left\{ v \rightarrow - \frac{c \sqrt{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{c \sqrt{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}} \right\} \right\}$$

$$\text{Solve}\left[c == \frac{c \sqrt{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \theta\right]$$

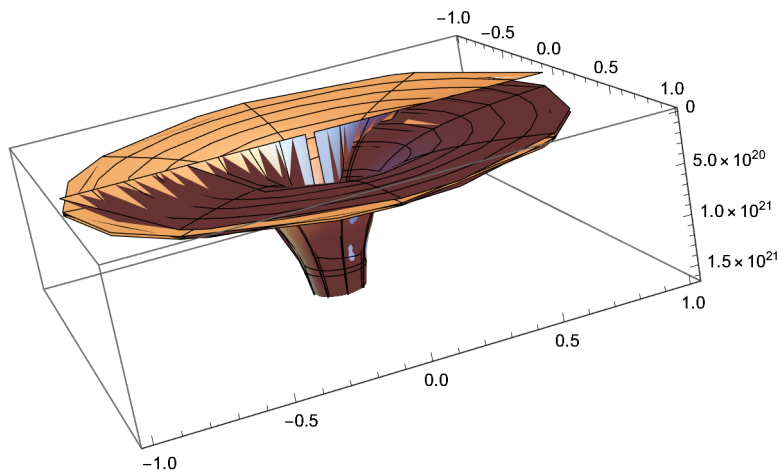
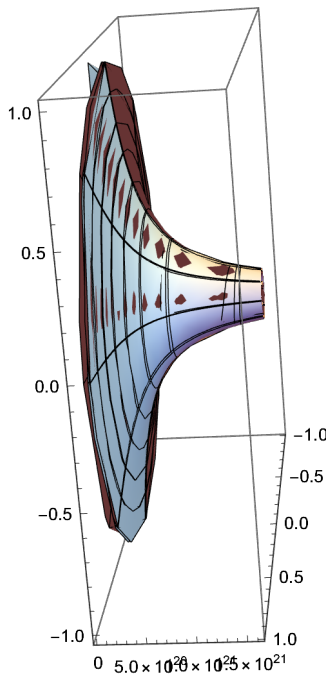
$$\left\{ \left\{ \theta \rightarrow 5.59005 \times 10^{-39} \left( 1.12399 \times 10^{39} - 0.0667049 r^2 - 0.0667049 \sqrt{1.68503 \times 10^{40} - 1.2082 \times 10^{20} r + r^2} \sqrt{1.68503 \times 10^{40} + 1.2082 \times 10^{20} r + r^2} \right) \right\}, \right. \\ \left. \left\{ \theta \rightarrow 5.59005 \times 10^{-39} \left( 1.12399 \times 10^{39} - 0.0667049 r^2 + 0.0667049 \sqrt{1.68503 \times 10^{40} - 1.2082 \times 10^{20} r + r^2} \sqrt{1.68503 \times 10^{40} + 1.2082 \times 10^{20} r + r^2} \right) \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[ \left\{ 5.590049019195099 \cdot 10^{-39} \left( 1.123994670816731 \cdot 10^{39} - 0.06670488143274204 \cdot r^2 - \right. \right. \right. \\ \left. \left. 0.06670488143274204 \cdot \sqrt{1.6850261130439833 \cdot 10^{40} - 1.2081975425370875 \cdot 10^{20} r + r^2} \right. \right. \\ \left. \left. \sqrt{1.6850261130439833 \cdot 10^{40} + 1.2081975425370875 \cdot 10^{20} r + r^2} \right) \right\}, \{r, -10, 10\} \right]$$



RevolutionPlot3D[  

$$\frac{c \sqrt{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}}{\sqrt{4 \pi^2 - 4 \pi \theta + \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$

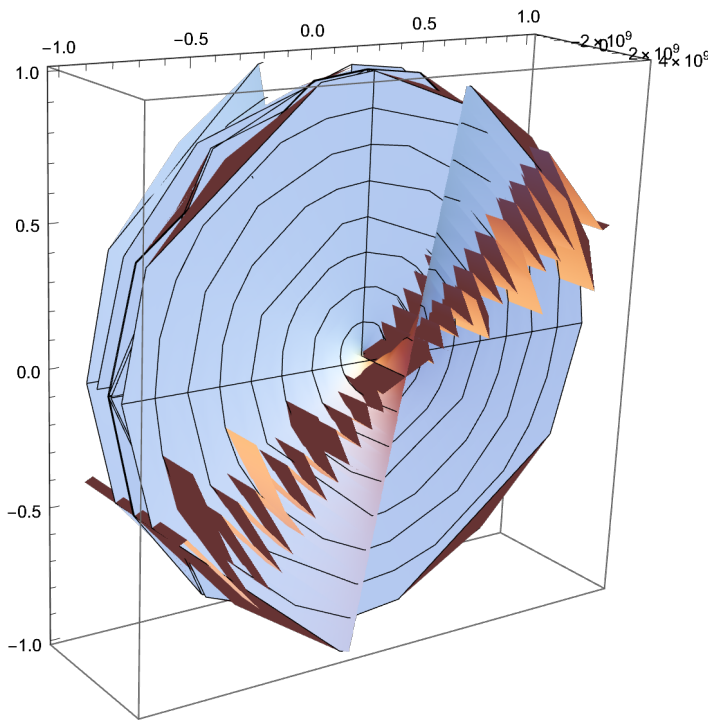


$$(1 / (1080 / \pi))$$

$$D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \left(\frac{c\sqrt{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}}\right)^2 / c^2}, \theta\right]$$

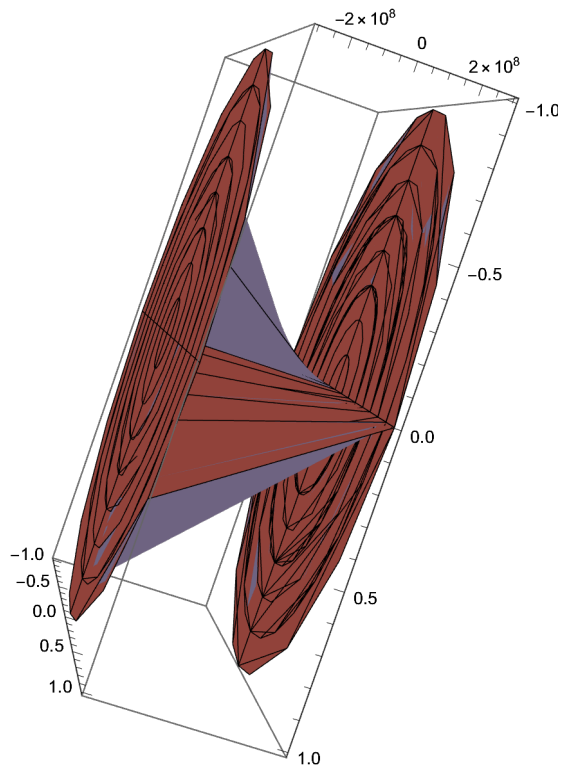
$$\frac{1}{1080} \pi \left( \left( \sqrt{4\pi r^2\theta - r^2\theta^2} \left( -\frac{-4\pi - \frac{18662400c^2\pi}{r^2} + 2\theta + \frac{9331200c^2\theta}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2} + \frac{(-4\pi + 2\theta) \left( 4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2} \right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2} \right) \right) / \left( 4\pi \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}} + \frac{(4\pi r^2 - 2r^2\theta) \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{4\pi \sqrt{4\pi r^2\theta - r^2\theta^2}} \right) \right)$$

$$\text{RevolutionPlot3D}\left[\frac{1}{1080}\pi\left(\left(\sqrt{4\pi r^2\theta - r^2\theta^2}\left(-\frac{4\pi - \frac{18662400c^2\pi}{r^2} + 2\theta + \frac{9331200c^2\theta}{r^2}}{-\frac{4\pi^2 - 4\pi\theta + \theta^2}} + \frac{(-4\pi + 2\theta)\left(4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}\right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2}\right)\right)/\right. \\ \left.\left(4\pi\sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}} + \frac{(4\pi r^2 - 2r^2\theta)\sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}\right), \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$$



RevolutionPlot3D[

$$\sqrt{1 - \frac{\left( c \sqrt{\frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}}{\sqrt{4\pi^2 - 4\pi\theta + \theta^2}} \right)^2}{c^2}} (4\pi r^2 - 2r^2\theta) \over 4320 \sqrt{4\pi r^2\theta - r^2\theta^2}}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}]$$

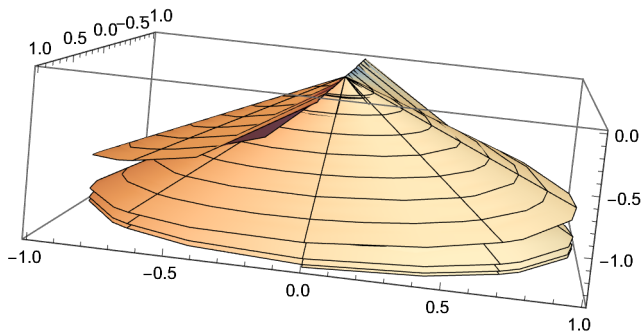




RevolutionPlot3D[

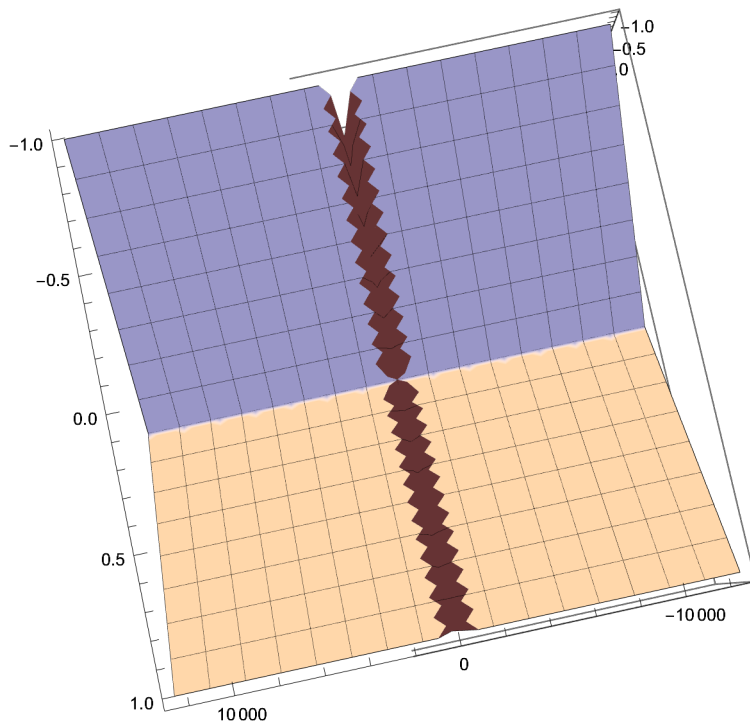
$$\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{\left(1 - \left(\frac{1}{1080} \pi \left(\sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left(-\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{\frac{4 \pi^2 - 4 \pi \theta + \theta^2}{}} + \frac{(-4 \pi + 2 \theta) \left(4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}\right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2}\right)\right)\right)}{\left(4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}\right) + \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right)} \wedge$$

$$2 \sqrt{c^2}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



Plot3D[

$$\begin{aligned}
& \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{\left(1 - \left(\frac{1}{1080} \pi \left(\sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left(-\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{\frac{4 \pi^2 - 4 \pi \theta + \theta^2}{}} + \right.\right.\right.\right. \\
& \quad \left.\left.\left.\frac{(-4 \pi + 2 \theta) \left(4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}\right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2}\right)\right)\right) / \\
& \quad \left(4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}\right) + \\
& \quad \left.\frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right) \wedge \\
& \quad \left.2 \right) / c^{\wedge 2}, \{r, -1, 1\}, \{\theta, -4000 \pi, 4000 \pi\}
\end{aligned}$$



The relativistic velocity is equal to the radius over time.

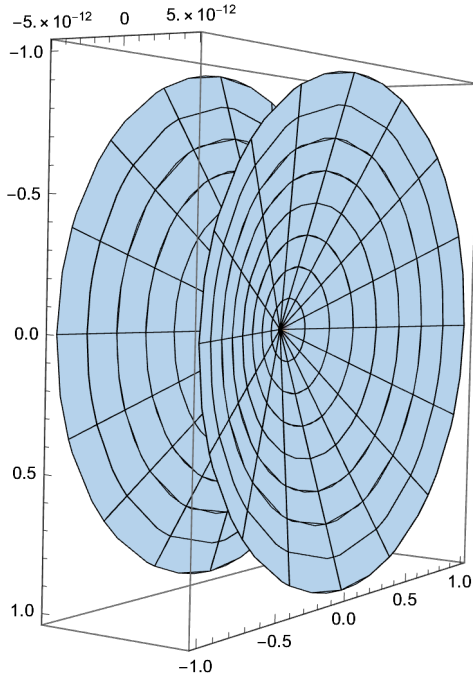
$$\begin{aligned}
 & \text{Solve} \left[ \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{-4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\
 & \quad \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
 & \quad \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right] == r / ((1080 / \pi) \theta), \theta \\
 & \left\{ \theta \rightarrow \frac{4320 c \pi + \pi r}{3240 c} + (9331200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2) / \right. \\
 & \quad \left( 3240 c \pi (100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \right. \\
 & \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3})^{1/3} \right) - \\
 & \quad \frac{1}{3240 c} \pi (100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \\
 & \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3})^{1/3} \right\}, \\
 & \left\{ \theta \rightarrow \frac{4320 c \pi + \pi r}{3240 c} - ((1 + i \sqrt{3}) (9331200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2)) / \right. \\
 & \quad \left( 6480 c \pi (100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \right. \\
 & \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3})^{1/3} \right) + \\
 & \quad \frac{1}{6480 c} (1 - i \sqrt{3}) \pi (100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \\
 & \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3})^{1/3} \right\}, \\
 & \left\{ \theta \rightarrow \frac{4320 c \pi + \pi r}{3240 c} - ((1 - i \sqrt{3}) (9331200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2)) / \right. \\
 & \quad \left( 6480 c \pi (100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \right. \\
 & \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3})^{1/3} \right) + \\
 & \quad \frac{1}{6480 c} (1 + i \sqrt{3}) \pi (100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \\
 & \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3})^{1/3} \right\}
 \end{aligned}$$

$$\left. \begin{aligned} & \left( 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \Big\}, \\ & \left\{ \theta \rightarrow -\frac{-4320\,c\,\pi + \pi\,r}{3240\,c} - \left( 9\,331\,200\,c^2\,\pi^2 - 4320\,c\,\pi^2\,r - \pi^2\,r^2 \right) / \right. \\ & \quad \left( 3240\,c\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r - 6480\,c\,r^2 - r^3 + \right. \right. \\ & \quad \left. \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 + c^3\,r^3} \right)^{1/3} \right) + \\ & \quad \frac{1}{3240\,c}\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r - 6480\,c\,r^2 - r^3 + \right. \\ & \quad \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 + c^3\,r^3} \right)^{1/3} \Big\}, \\ & \left\{ \theta \rightarrow -\frac{-4320\,c\,\pi + \pi\,r}{3240\,c} + \left( (1 + \mathfrak{i}\,\sqrt{3}) \left( 9\,331\,200\,c^2\,\pi^2 - 4320\,c\,\pi^2\,r - \pi^2\,r^2 \right) \right) / \right. \\ & \quad \left( 6480\,c\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r - 6480\,c\,r^2 - r^3 + \right. \right. \\ & \quad \left. \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 + c^3\,r^3} \right)^{1/3} \right) - \\ & \quad \frac{1}{6480\,c} \left( 1 - \mathfrak{i}\,\sqrt{3} \right) \pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r - 6480\,c\,r^2 - r^3 + \right. \\ & \quad \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 + c^3\,r^3} \right)^{1/3} \Big\}, \\ & \left\{ \theta \rightarrow -\frac{-4320\,c\,\pi + \pi\,r}{3240\,c} + \left( (1 - \mathfrak{i}\,\sqrt{3}) \left( 9\,331\,200\,c^2\,\pi^2 - 4320\,c\,\pi^2\,r - \pi^2\,r^2 \right) \right) / \right. \\ & \quad \left( 6480\,c\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r - 6480\,c\,r^2 - r^3 + \right. \right. \\ & \quad \left. \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 + c^3\,r^3} \right)^{1/3} \right) - \\ & \quad \frac{1}{6480\,c} \left( 1 + \mathfrak{i}\,\sqrt{3} \right) \pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r - 6480\,c\,r^2 - r^3 + \right. \\ & \quad \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 + c^3\,r^3} \right)^{1/3} \Big\} \end{aligned} \right.$$

```
c := (2.99792458 * 10 ^ 8)
```

$$\begin{aligned} & \text{RevolutionPlot3D}\left[\left\{\left\{\frac{4320\,c\,\pi+\pi\,r}{3240\,c}+\left(9\,331\,200\,c^2\,\pi^2+4320\,c\,\pi^2\,r-\pi^2\,r^2\right)/\right.\right.\right. \\ & \quad \left.\left.\left(3240\,c\,\pi\left(100\,776\,960\,000\,c^3+6\,998\,400\,c^2\,r+6480\,c\,r^2-r^3+\right.\right.\right. \\ & \quad \left.\left.\left.233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6+9\,331\,200\,c^5\,r+5940\,c^4\,r^2-c^3\,r^3}\right)^{1/3}\right)-\right. \\ & \quad \left.\frac{1}{3240\,c}\,\pi\left(100\,776\,960\,000\,c^3+6\,998\,400\,c^2\,r+6480\,c\,r^2-r^3+\right.\right. \\ & \quad \left.\left.\left.233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6+9\,331\,200\,c^5\,r+5940\,c^4\,r^2-c^3\,r^3}\right)^{1/3}\right\},\right. \\ & \quad \left.\left\{\frac{4320\,c\,\pi+\pi\,r}{3240\,c}-\left(\left(1+i\sqrt{3}\right)\left(9\,331\,200\,c^2\,\pi^2+4320\,c\,\pi^2\,r-\pi^2\,r^2\right)\right)/\right.\right. \\ & \quad \left.\left.\left(6480\,c\,\pi\left(100\,776\,960\,000\,c^3+6\,998\,400\,c^2\,r+6480\,c\,r^2-r^3+\right.\right.\right. \end{aligned}$$

$$\begin{aligned}
& 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3}^{1/3} \Bigg) + \\
& \frac{1}{6480\,c} \left( 1 - \mathfrak{i} \sqrt{3} \right) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \\
& \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3}^{1/3} \right\}, \\
& \left\{ \frac{4320\,c\,\pi + \pi r}{3240\,c} - \left( \left( 1 - \mathfrak{i} \sqrt{3} \right) \left( 9\,331\,200\,c^2 \pi^2 + 4320\,c\,\pi^2 r - \pi^2 r^2 \right) \right) / \right. \\
& \left. \left( 6480\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \right. \\
& \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3}^{1/3} \right) \right) + \right. \\
& \left. \frac{1}{6480\,c} \left( 1 + \mathfrak{i} \sqrt{3} \right) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3}^{1/3} \right) \right\}, \\
& \left\{ -\frac{4320\,c\,\pi + \pi r}{3240\,c} - \left( 9\,331\,200\,c^2 \pi^2 - 4320\,c\,\pi^2 r - \pi^2 r^2 \right) / \right. \\
& \left. \left( 3240\,c\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r - 6480\,c\,r^2 - r^3 + \right. \right. \right. \\
& \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5 r + 5940\,c^4 r^2 + c^3 r^3}^{1/3} \right) \right) + \right. \\
& \left. \frac{1}{3240\,c} \pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r - 6480\,c\,r^2 - r^3 + \right. \right. \\
& \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5 r + 5940\,c^4 r^2 + c^3 r^3}^{1/3} \right) \right\}, \\
& \left\{ -\frac{4320\,c\,\pi + \pi r}{3240\,c} + \left( \left( 1 + \mathfrak{i} \sqrt{3} \right) \left( 9\,331\,200\,c^2 \pi^2 - 4320\,c\,\pi^2 r - \pi^2 r^2 \right) \right) / \right. \\
& \left. \left( 6480\,c\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r - 6480\,c\,r^2 - r^3 + \right. \right. \right. \\
& \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5 r + 5940\,c^4 r^2 + c^3 r^3}^{1/3} \right) \right) - \right. \\
& \left. \frac{1}{6480\,c} \left( 1 - \mathfrak{i} \sqrt{3} \right) \pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r - 6480\,c\,r^2 - r^3 + \right. \right. \\
& \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5 r + 5940\,c^4 r^2 + c^3 r^3}^{1/3} \right) \right\}, \\
& \left\{ -\frac{4320\,c\,\pi + \pi r}{3240\,c} + \left( \left( 1 - \mathfrak{i} \sqrt{3} \right) \left( 9\,331\,200\,c^2 \pi^2 - 4320\,c\,\pi^2 r - \pi^2 r^2 \right) \right) / \right. \\
& \left. \left( 6480\,c\,\pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r - 6480\,c\,r^2 - r^3 + \right. \right. \right. \\
& \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5 r + 5940\,c^4 r^2 + c^3 r^3}^{1/3} \right) \right) - \right. \\
& \left. \frac{1}{6480\,c} \left( 1 + \mathfrak{i} \sqrt{3} \right) \pi \left( -100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r - 6480\,c\,r^2 - r^3 + 233\,280 \right. \right. \\
& \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 - 9\,331\,200\,c^5 r + 5940\,c^4 r^2 + c^3 r^3}^{1/3} \right) \right\}, \{r, -1, 1\}
\end{aligned}$$



$$\text{Solve} \left[ \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) / \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) == r / ((1080 / \pi) \theta), r \right]$$

## The Wavelength with Changing Value

When the experience is one of white, the perceptual system does not immediately distinguish between combinative or pigmented character to the white. The perceptual system perceives all the combinations of light in white. This means that there are multiple wavelengths undistinguished and all invariant. Thus, the wavelength of light is interpreted to be changing during transition when we take all of the information in from white, additive color or pigment.

Sampling is the smallest point. We receive  
an pointilistic impression of the world called a .

$$\text{Solve} \left[ \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \right. \\ \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\ \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\ \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \\ ((1080 / \pi) \theta) == r (1 / ((1080 / \pi) \theta)), \theta]$$

$$\begin{aligned}
& \left\{ \theta \rightarrow \pi - \frac{\pi \sqrt{4\,665\,600\,c-r}}{2160\sqrt{c}} - \frac{\pi \sqrt{-9\,331\,200 + \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c-r}} - \frac{r}{c} - \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c-r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi - \frac{\pi \sqrt{4\,665\,600\,c-r}}{2160\sqrt{c}} + \frac{\pi \sqrt{-9\,331\,200 + \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c-r}} - \frac{r}{c} - \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c-r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi + \frac{\pi \sqrt{4\,665\,600\,c-r}}{2160\sqrt{c}} - \frac{\pi \sqrt{-9\,331\,200 - \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c-r}} - \frac{r}{c} + \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c-r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi + \frac{\pi \sqrt{4\,665\,600\,c-r}}{2160\sqrt{c}} + \frac{\pi \sqrt{-9\,331\,200 - \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c-r}} - \frac{r}{c} + \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c-r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi + \frac{\pi \sqrt{4\,665\,600\,c+r}}{2160\sqrt{c}} - \frac{\pi \sqrt{-9\,331\,200 + \frac{r}{c} - \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c+r}} - \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c+r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi + \frac{\pi \sqrt{4\,665\,600\,c+r}}{2160\sqrt{c}} + \frac{\pi \sqrt{-9\,331\,200 + \frac{r}{c} - \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c+r}} - \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c+r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi - \frac{\pi \sqrt{4\,665\,600\,c+r}}{2160\sqrt{c}} - \frac{\pi \sqrt{-9\,331\,200 + \frac{r}{c} + \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c+r}} + \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c+r}}}}{2160} \right\}, \\
& \left\{ \theta \rightarrow \pi - \frac{\pi \sqrt{4\,665\,600\,c+r}}{2160\sqrt{c}} + \frac{\pi \sqrt{-9\,331\,200 + \frac{r}{c} + \frac{20\,155\,392\,000\sqrt{c}}{\sqrt{4\,665\,600\,c+r}} + \frac{4320\,r}{\sqrt{c}\sqrt{4\,665\,600\,c+r}}}}{2160} \right\}
\end{aligned}$$



RevolutionPlot3D[

$$\begin{aligned}
 & \left\{ \left\{ \pi - \frac{\pi \sqrt{4665600 c - r}}{2160 \sqrt{c}} - \frac{\pi \sqrt{-9331200 + \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c - r}} - \frac{r}{c} - \frac{4320 r}{\sqrt{c} \sqrt{4665600 c - r}}}}{2160} \right\}, \right. \\
 & \left\{ \pi - \frac{\pi \sqrt{4665600 c - r}}{2160 \sqrt{c}} + \frac{\pi \sqrt{-9331200 + \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c - r}} - \frac{r}{c} - \frac{4320 r}{\sqrt{c} \sqrt{4665600 c - r}}}}{2160} \right\}, \\
 & \left\{ \pi + \frac{\pi \sqrt{4665600 c - r}}{2160 \sqrt{c}} - \frac{\pi \sqrt{-9331200 - \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c - r}} - \frac{r}{c} + \frac{4320 r}{\sqrt{c} \sqrt{4665600 c - r}}}}{2160} \right\}, \\
 & \left\{ \pi + \frac{\pi \sqrt{4665600 c - r}}{2160 \sqrt{c}} + \frac{\pi \sqrt{-9331200 - \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c - r}} - \frac{r}{c} + \frac{4320 r}{\sqrt{c} \sqrt{4665600 c - r}}}}{2160} \right\}, \\
 & \left\{ \pi + \frac{\pi \sqrt{4665600 c + r}}{2160 \sqrt{c}} - \frac{\pi \sqrt{-9331200 + \frac{r}{c} - \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c + r}} - \frac{4320 r}{\sqrt{c} \sqrt{4665600 c + r}}}}{2160} \right\}, \\
 & \left\{ \pi + \frac{\pi \sqrt{4665600 c + r}}{2160 \sqrt{c}} + \frac{\pi \sqrt{-9331200 + \frac{r}{c} - \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c + r}} - \frac{4320 r}{\sqrt{c} \sqrt{4665600 c + r}}}}{2160} \right\}, \\
 & \left\{ \pi - \frac{\pi \sqrt{4665600 c + r}}{2160 \sqrt{c}} - \frac{\pi \sqrt{-9331200 + \frac{r}{c} + \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c + r}} + \frac{4320 r}{\sqrt{c} \sqrt{4665600 c + r}}}}{2160} \right\}, \\
 & \left. \left\{ \pi - \frac{\pi \sqrt{4665600 c + r}}{2160 \sqrt{c}} + \frac{\pi \sqrt{-9331200 + \frac{r}{c} + \frac{20155392000 \sqrt{c}}{\sqrt{4665600 c + r}} + \frac{4320 r}{\sqrt{c} \sqrt{4665600 c + r}}}}{2160} \right\}, \{r, -1, 1\} \right]
 \end{aligned}$$

$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} =$$

$$\begin{aligned} \mathbf{v} \star \mathbf{t} = & \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \\ & \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) / \\ & \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\ & \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) ((1080 / \pi) \theta) \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\
 & \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
 & \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) ((1080 / \pi) \theta) \\
 & \theta \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\
 & \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
 & \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{Solve}\left[\theta \left( \left( \sqrt{4\pi r^2 \theta - r^2 \theta^2} \left( -\frac{4\pi - \frac{18662400 c^2 \pi}{r^2} + 2\theta + \frac{9331200 c^2 \theta}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(-4\pi + 2\theta) \left( 4\pi^2 - 4\pi\theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2} \right) \right) \right) / \\
& \quad \left( 4\pi \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}} \right) + \\
& \quad \left. \frac{(4\pi r^2 - 2r^2 \theta) \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}} \right) = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, r] \\
& \left\{ \left\{ r \rightarrow - \left( \sqrt{ \left( 74649600 c^2 \pi^4 + \frac{1194393600 c^2 \pi^8}{(2\pi - \theta)^4} - \frac{1194393600 c^2 \pi^7}{(2\pi - \theta)^3} + \frac{597196800 c^2 \pi^6}{(2\pi - \theta)^2} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{298598400 c^2 \pi^5}{2\pi - \theta} - 37324800 c^2 \pi^2 \theta^2 + 18662400 c^2 \pi \theta^3 - 4665600 c^2 \theta^4 \right) \right) \right) / \\
& \quad \left( \sqrt{16\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4} \right) \right\}, \left\{ r \rightarrow \left( \sqrt{ \left( 74649600 c^2 \pi^4 + \frac{1194393600 c^2 \pi^8}{(2\pi - \theta)^4} - \right. \right. \right. \\
& \quad \left. \frac{1194393600 c^2 \pi^7}{(2\pi - \theta)^3} + \frac{597196800 c^2 \pi^6}{(2\pi - \theta)^2} - \frac{298598400 c^2 \pi^5}{2\pi - \theta} - 37324800 c^2 \pi^2 \theta^2 + \right. \\
& \quad \left. \left. \left. 18662400 c^2 \pi \theta^3 - 4665600 c^2 \theta^4 \right) \right) \right) / \left( \sqrt{16\pi^2 \theta^2 - 8\pi \theta^3 + \theta^4} \right) \right\} \}
\end{aligned}$$

$$c := (2.99792458 * 10^8)$$

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RevolutionPlot3D[
  (

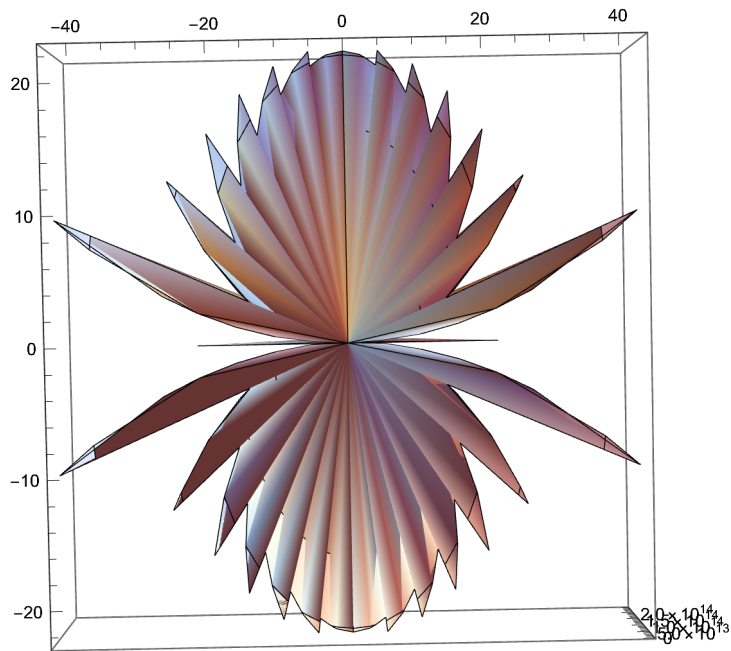
$$\sqrt{\left(74\,649\,600\,c^2\pi^4 + \frac{1\,194\,393\,600\,c^2\pi^8}{(2\pi-\theta)^4} - \frac{1\,194\,393\,600\,c^2\pi^7}{(2\pi-\theta)^3} + \frac{597\,196\,800\,c^2\pi^6}{(2\pi-\theta)^2} - \frac{298\,598\,400\,c^2\pi^5}{2\pi-\theta} - 37\,324\,800\,c^2\pi^2\theta^2 + 18\,662\,400\,c^2\pi\theta^3 - 4\,665\,600\,c^2\theta^4\right)}$$

  , {

$$\theta, -400\,000\pi, 400\,000\pi$$

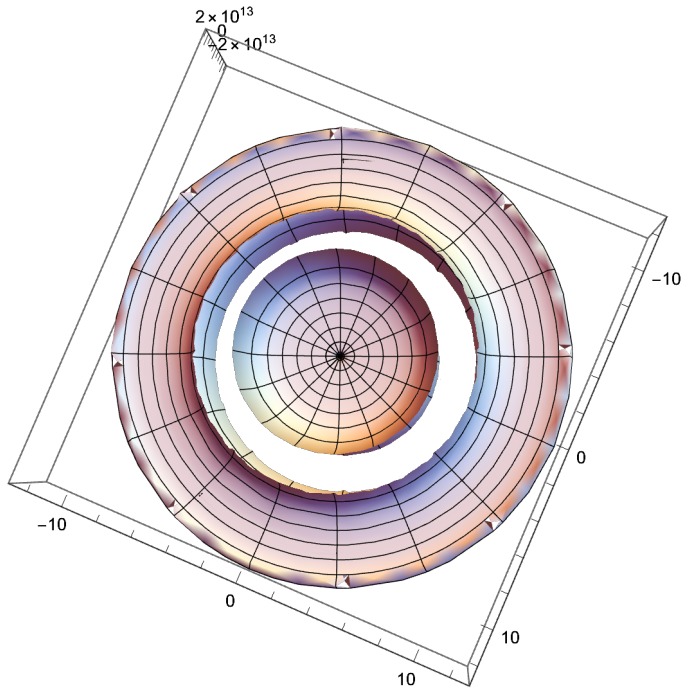
}
]

```



RevolutionPlot3D[

$$\left\{ \left\{ - \left( \sqrt{74\,649\,600\,c^2\pi^4 + \frac{1\,194\,393\,600\,c^2\pi^8}{(2\pi-\theta)^4} - \frac{1\,194\,393\,600\,c^2\pi^7}{(2\pi-\theta)^3} + \frac{597\,196\,800\,c^2\pi^6}{(2\pi-\theta)^2} - \frac{298\,598\,400\,c^2\pi^5}{2\pi-\theta} - 37\,324\,800\,c^2\pi^2\theta^2 + 18\,662\,400\,c^2\pi\theta^3 - 4\,665\,600\,c^2\theta^4} \right) \right\} / \left( \sqrt{16\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \right) \right\}, \left\{ \left( \sqrt{74\,649\,600\,c^2\pi^4 + \frac{1\,194\,393\,600\,c^2\pi^8}{(2\pi-\theta)^4} - \frac{1\,194\,393\,600\,c^2\pi^7}{(2\pi-\theta)^3} + \frac{597\,196\,800\,c^2\pi^6}{(2\pi-\theta)^2} - \frac{298\,598\,400\,c^2\pi^5}{2\pi-\theta} - 37\,324\,800\,c^2\pi^2\theta^2 + 18\,662\,400\,c^2\pi\theta^3 - 4\,665\,600\,c^2\theta^4} \right) \right\} / \left( \sqrt{16\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} \right) \right\}, \{\theta, -4\pi, 4\pi\}]$$



$$\text{Solve}\left[\theta \left( \left( \sqrt{4\pi r^2 \theta - r^2 \theta^2} \left( -\frac{4\pi - \frac{18662400 c^2 \pi}{r^2} + 2\theta + \frac{9331200 c^2 \theta}{r^2}}{4\pi^2 - 4\pi \theta + \theta^2} + \frac{(-4\pi + 2\theta) \left( 4\pi^2 - 4\pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4\pi^2 - 4\pi \theta + \theta^2)^2} \right) \right) / \right. \\ \left. \left( 4\pi \sqrt{1 - \frac{4\pi^2 - 4\pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4\pi^2 - 4\pi \theta + \theta^2}} \right) + \frac{(4\pi r^2 - 2r^2 \theta) \sqrt{1 - \frac{4\pi^2 - 4\pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4\pi^2 - 4\pi \theta + \theta^2}}}{4\pi \sqrt{4\pi r^2 \theta - r^2 \theta^2}} \right) = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \theta \right]$$

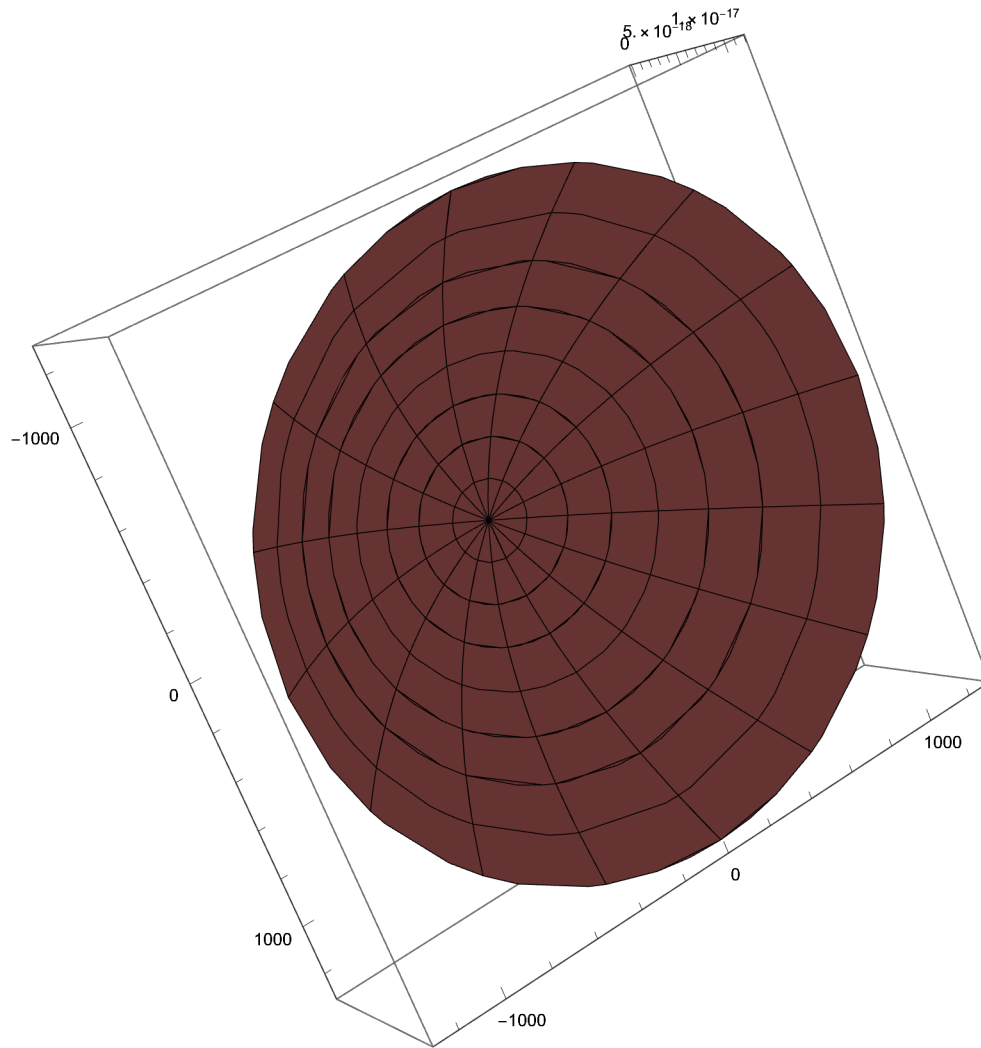
$$\left\{ \left\{ \theta \rightarrow \text{Root}\left[-64\pi^5 r^2 + (298598400 c^2 \pi^4 + 144\pi^4 r^2) \mp 1 + \right. \right. \right. \\ \left. \left. \left. (-298598400 c^2 \pi^3 - 128\pi^3 r^2) \mp 1^2 + (149299200 c^2 \pi^2 + 56\pi^2 r^2) \mp 1^3 + \right. \right. \right. \\ \left. \left. \left. (-37324800 c^2 \pi - 12\pi r^2) \mp 1^4 + (4665600 c^2 + r^2) \mp 1^5 \&, 1 \right] \right\}, \right. \\ \left\{ \theta \rightarrow \text{Root}\left[-64\pi^5 r^2 + (298598400 c^2 \pi^4 + 144\pi^4 r^2) \mp 1 + \right. \right. \\ \left. \left. (-298598400 c^2 \pi^3 - 128\pi^3 r^2) \mp 1^2 + (149299200 c^2 \pi^2 + 56\pi^2 r^2) \mp 1^3 + \right. \right. \\ \left. \left. (-37324800 c^2 \pi - 12\pi r^2) \mp 1^4 + (4665600 c^2 + r^2) \mp 1^5 \&, 2 \right] \right\}, \\ \left\{ \theta \rightarrow \text{Root}\left[-64\pi^5 r^2 + (298598400 c^2 \pi^4 + 144\pi^4 r^2) \mp 1 + \right. \right. \\ \left. \left. (-298598400 c^2 \pi^3 - 128\pi^3 r^2) \mp 1^2 + (149299200 c^2 \pi^2 + 56\pi^2 r^2) \mp 1^3 + \right. \right. \\ \left. \left. (-37324800 c^2 \pi - 12\pi r^2) \mp 1^4 + (4665600 c^2 + r^2) \mp 1^5 \&, 3 \right] \right\}, \\ \left\{ \theta \rightarrow \text{Root}\left[-64\pi^5 r^2 + (298598400 c^2 \pi^4 + 144\pi^4 r^2) \mp 1 + \right. \right. \\ \left. \left. (-298598400 c^2 \pi^3 - 128\pi^3 r^2) \mp 1^2 + (149299200 c^2 \pi^2 + 56\pi^2 r^2) \mp 1^3 + \right. \right. \\ \left. \left. (-37324800 c^2 \pi - 12\pi r^2) \mp 1^4 + (4665600 c^2 + r^2) \mp 1^5 \&, 4 \right] \right\}, \\ \left. \left\{ \theta \rightarrow \text{Root}\left[-64\pi^5 r^2 + (298598400 c^2 \pi^4 + 144\pi^4 r^2) \mp 1 + \right. \right. \right. \\ \left. \left. \left. (-298598400 c^2 \pi^3 - 128\pi^3 r^2) \mp 1^2 + (149299200 c^2 \pi^2 + 56\pi^2 r^2) \mp 1^3 + \right. \right. \right. \\ \left. \left. \left. (-37324800 c^2 \pi - 12\pi r^2) \mp 1^4 + (4665600 c^2 + r^2) \mp 1^5 \&, 5 \right] \right\} \right\}$$

```

RevolutionPlot3D[
  { {Root[-64 π5 r2 + (298 598 400 c2 π4 + 144 π4 r2) #1 + (-298 598 400 c2 π3 - 128 π3 r2) #12 +
      (149 299 200 c2 π2 + 56 π2 r2) #13 +
      (-37 324 800 c2 π - 12 π r2) #14 + (4 665 600 c2 + r2) #15 &, 1] },
    {Root[-64 π5 r2 + (298 598 400 c2 π4 + 144 π4 r2) #1 + (-298 598 400 c2 π3 - 128 π3 r2) #12 +
      (149 299 200 c2 π2 + 56 π2 r2) #13 + (-37 324 800 c2 π - 12 π r2) #14 +
      (4 665 600 c2 + r2) #15 &, 2] },
    {Root[-64 π5 r2 + (298 598 400 c2 π4 + 144 π4 r2) #1 + (-298 598 400 c2 π3 - 128 π3 r2) #12 +
      (149 299 200 c2 π2 + 56 π2 r2) #13 +
      (-37 324 800 c2 π - 12 π r2) #14 + (4 665 600 c2 + r2) #15 &, 3] },
    {Root[-64 π5 r2 + (298 598 400 c2 π4 + 144 π4 r2) #1 + (-298 598 400 c2 π3 - 128 π3 r2) #12 +
      (149 299 200 c2 π2 + 56 π2 r2) #13 +
      (-37 324 800 c2 π - 12 π r2) #14 + (4 665 600 c2 + r2) #15 &, 4] },
    {Root[-64 π5 r2 + (298 598 400 c2 π4 + 144 π4 r2) #1 + (-298 598 400 c2 π3 - 128 π3 r2) #12 +
      (149 299 200 c2 π2 + 56 π2 r2) #13 + (-37 324 800 c2 π - 12 π r2) #14 +
      (4 665 600 c2 + r2) #15 &, 5] } }, {r, -400 π, 400 π} ]

```





We can use this model to describe the free energy bowl if it's properly applied. "The line of optical flow is a metaphor that describes the expansion of the visual field when moving through it." Tom.

$$\{\{r \rightarrow 0\}\}$$

$$\text{Solve}\left[\frac{540 \theta \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{\pi^2} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\left\{\{\theta \rightarrow 0\}, \left\{\theta \rightarrow \frac{\pi}{1080}\right\}, \{\theta \rightarrow 4 \pi\}\right\}$$

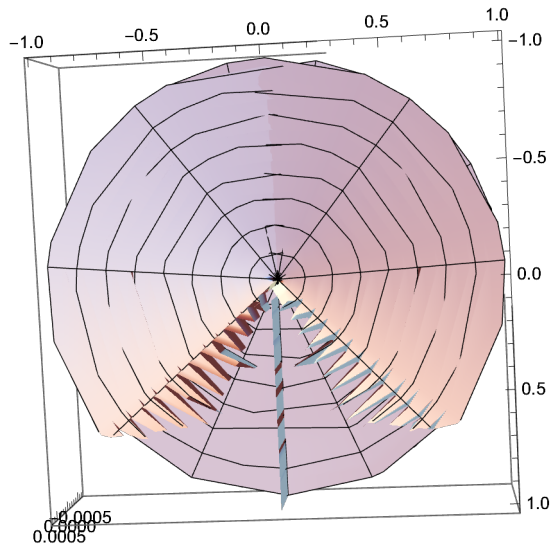
$$\begin{aligned} & \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \\ & \quad \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\ & \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\ & \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \end{aligned}$$

$$\text{Solve}\left[\frac{\sqrt{1 - \frac{v^2}{c^2}} (4 \pi r^2 - 2 r^2 \theta)}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == v, v\right]$$

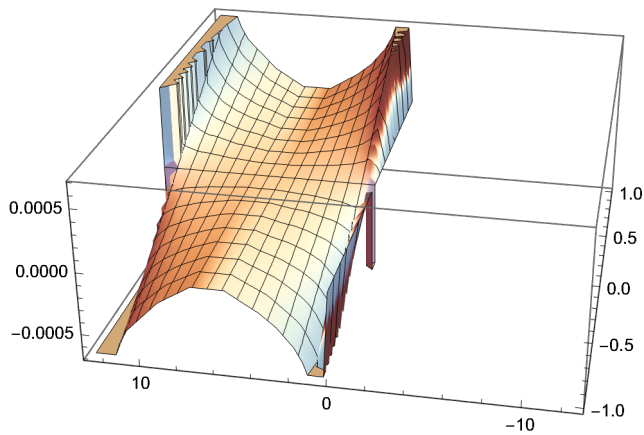
$$\left\{ \left\{ v \rightarrow -\frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}} \right\} \right\}$$

$\text{RevolutionPlot3D}\left[\frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$



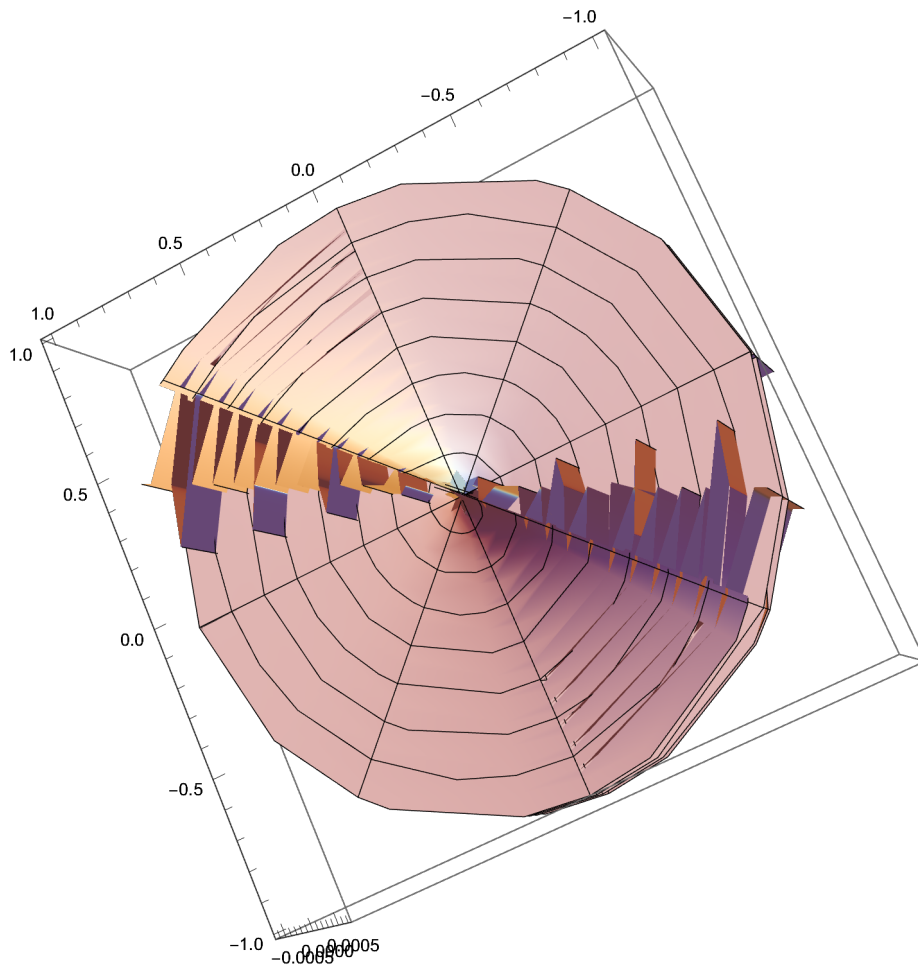
$\text{Plot3D}\left[\frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$



$c := (2.99792458 * 10^8)$

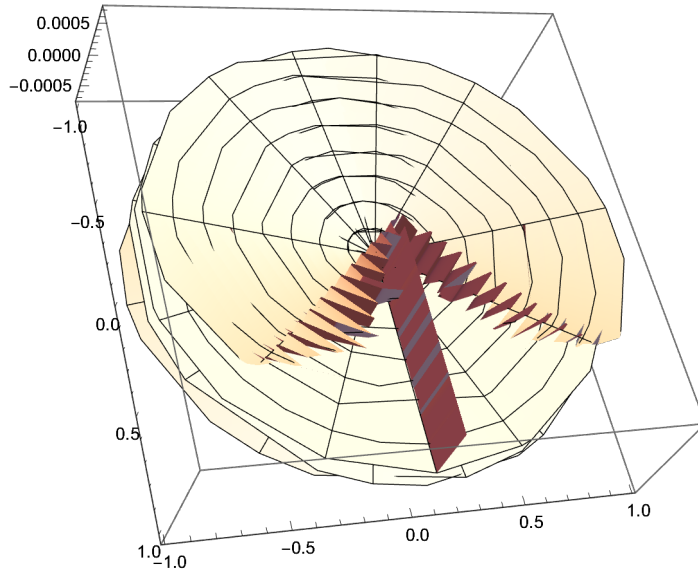
$$\begin{aligned}
& D \left[ \frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}}, r, \theta \right] \\
& \left( 3 c r (-18662400 c^2 \pi + 4 \pi r^2 + 9331200 c^2 \theta - 2 r^2 \theta) \right. \\
& \quad \left. \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2} (-8 \pi^2 r + 8 \pi r \theta - 2 r \theta^2) \right) / \\
& \quad \left( 4 (-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2)^{5/2} \right) - \\
& \quad \frac{c r (8 \pi r - 4 r \theta) \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{2 (-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2)^{3/2}} - \\
& \quad \frac{c (-18662400 c^2 \pi + 4 \pi r^2 + 9331200 c^2 \theta - 2 r^2 \theta) \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{2 (-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2)^{3/2}} - \\
& \quad (c r (4 \pi - 2 \theta) (-8 \pi^2 r + 8 \pi r \theta - 2 r \theta^2)) / \\
& \quad \left( 4 \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2} (-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2)^{3/2} \right) + \\
& \quad (c (4 \pi - 2 \theta)) / \\
& \quad \left( 2 \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2} \sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2} \right)
\end{aligned}$$

$$\text{RevolutionPlot3D}\left[\left(3 c r \left(-18662400 c^2 \pi+4 \pi r^2+9331200 c^2 \theta-2 r^2 \theta\right) \sqrt{-4 \pi^2+4 \pi \theta-\theta^2} \left(-8 \pi^2 r+8 \pi r \theta-2 r \theta^2\right)\right) / \left(4 \left(-4 \pi^2 r^2-18662400 c^2 \pi \theta+4 \pi r^2 \theta+4665600 c^2 \theta^2-r^2 \theta^2\right)^{5 / 2}\right)-\frac{c r \left(8 \pi r-4 r \theta\right) \sqrt{-4 \pi^2+4 \pi \theta-\theta^2}}{2 \left(-4 \pi^2 r^2-18662400 c^2 \pi \theta+4 \pi r^2 \theta+4665600 c^2 \theta^2-r^2 \theta^2\right)^{3 / 2}}-\frac{c \left(-18662400 c^2 \pi+4 \pi r^2+9331200 c^2 \theta-2 r^2 \theta\right) \sqrt{-4 \pi^2+4 \pi \theta-\theta^2}}{2 \left(-4 \pi^2 r^2-18662400 c^2 \pi \theta+4 \pi r^2 \theta+4665600 c^2 \theta^2-r^2 \theta^2\right)^{3 / 2}}-\left(c r \left(4 \pi-2 \theta\right) \left(-8 \pi^2 r+8 \pi r \theta-2 r \theta^2\right)\right) / \left(4 \sqrt{-4 \pi^2+4 \pi \theta-\theta^2} \left(-4 \pi^2 r^2-18662400 c^2 \pi \theta+4 \pi r^2 \theta+4665600 c^2 \theta^2-r^2 \theta^2\right)^{3 / 2}\right)+\left(c \left(4 \pi-2 \theta\right)\right) / \left(2 \sqrt{-4 \pi^2+4 \pi \theta-\theta^2} \sqrt{-4 \pi^2 r^2-18662400 c^2 \pi \theta+4 \pi r^2 \theta+4665600 c^2 \theta^2-r^2 \theta^2}\right),\left\{r,-1,1\right\},\left\{\theta,-4 \pi, 4 \pi\right\}\right]$$



RevolutionPlot3D[  

$$\frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



$$\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}$$

Plot3D[  

$$\frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}},$$
  

$$\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$

RevolutionPlot3D[  

$$\left\{ \frac{c r \sqrt{-4 \pi^2 + 4 \pi \theta - \theta^2}}{\sqrt{-4 \pi^2 r^2 - 18662400 c^2 \pi \theta + 4 \pi r^2 \theta + 4665600 c^2 \theta^2 - r^2 \theta^2}}, \right.$$
  

$$\left. \frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400} \right\}, \{r, -1000000, 1000000\}, \{\theta, -13, 13\}]$$



$$E = h \nu = h n f = m c^2 = h n ((1 / (1080 / \pi)) \theta)$$

$$\begin{aligned}
 \text{Force} = m (a) = m D \left[ \left( \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{-4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \right. \right. \\
 \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\
 \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
 \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right], \theta] \\
 \\
 m D \left[ \left( \frac{1}{1080} \pi \left( \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( -\frac{-4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \right. \right. \\
 \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) \right) / \\
 \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
 \left. \frac{(4 \pi r^2 - 2 r^2 \theta) \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) \right], \theta]
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{1080} m \pi \left( - \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( - \frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right)^2 \right) \right) / \\
& \left( 8 \pi \left( 1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} \right)^{3/2} \right) + \\
& \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( \frac{2 (-4 \pi + 2 \theta) \left( -4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} - \right. \right. \\
& \quad \left. \frac{2 + \frac{9331200 c^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} - \frac{2 (-4 \pi + 2 \theta)^2 \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^3} \right. \\
& \quad \left. \left. \frac{2 \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) / \\
& \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
& \left( (4 \pi r^2 - 2 r^2 \theta) \left( - \frac{4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \\
& \quad \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) / \\
& \left( 4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) - \\
& \frac{(4 \pi r^2 - 2 r^2 \theta)^2 \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \\
& \frac{r^2 \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{2 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}
\end{aligned}$$



This is the force :

$$\begin{aligned}
 F = \frac{1}{1080} m \pi & \left( - \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( - \frac{-4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \right. \\
 & \left. \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right)^2 \right) / \\
 & \left( 8 \pi \left( 1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} \right)^{3/2} \right) + \\
 & \left( \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \left( \frac{2 (-4 \pi + 2 \theta) \left( -4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} - \right. \right. \\
 & \left. \left. \frac{2 + \frac{9331200 c^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} - \frac{2 (-4 \pi + 2 \theta)^2 \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^3} \right) \right) + \\
 & \left. \frac{2 \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) / \\
 & \left( 4 \pi \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) + \\
 & \left( (4 \pi r^2 - 2 r^2 \theta) \left( - \frac{-4 \pi - \frac{18662400 c^2 \pi}{r^2} + 2 \theta + \frac{9331200 c^2 \theta}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2} + \right. \right. \\
 & \left. \left. \frac{(-4 \pi + 2 \theta) \left( 4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2} \right)}{(4 \pi^2 - 4 \pi \theta + \theta^2)^2} \right) \right) / \\
 & \left( 4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2} \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}} \right) - \\
 & \frac{(4 \pi r^2 - 2 r^2 \theta)^2 \sqrt{1 - \frac{4 \pi^2 - 4 \pi \theta - \frac{18662400 c^2 \pi \theta}{r^2} + \theta^2 + \frac{4665600 c^2 \theta^2}{r^2}}{4 \pi^2 - 4 \pi \theta + \theta^2}}}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} -
 \end{aligned}$$

$$\frac{r^2 \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{2\pi \sqrt{4\pi r^2\theta - r^2\theta^2}} \Bigg)$$

$$E = (1080 / \pi) \int m a d\theta$$

$$\begin{aligned} & (1080 / \pi) \int \frac{1}{1080} m \pi \left( - \left( \sqrt{4\pi r^2\theta - r^2\theta^2} \left( - \frac{-4\pi - \frac{18662400c^2\pi}{r^2} + 2\theta + \frac{9331200c^2\theta}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2} + \right. \right. \right. \\ & \quad \left. \left. \left. \frac{(-4\pi + 2\theta) \left( 4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2} \right)^2}{(4\pi^2 - 4\pi\theta + \theta^2)^2} \right) \right) \right) / \\ & \quad \left( 8\pi \left( 1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2} \right)^{3/2} \right) + \\ & \quad \left( \sqrt{4\pi r^2\theta - r^2\theta^2} \left( \frac{2(-4\pi + 2\theta) \left( -4\pi - \frac{18662400c^2\pi}{r^2} + 2\theta + \frac{9331200c^2\theta}{r^2} \right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2} - \right. \right. \\ & \quad \left. \frac{2 + \frac{9331200c^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2} - \frac{2(-4\pi + 2\theta)^2 \left( 4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2} \right)}{(4\pi^2 - 4\pi\theta + \theta^2)^3} \right. \\ & \quad \left. \left. \frac{2 \left( 4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2} \right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2} \right) \right) / \\ & \quad \left( 4\pi \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}} \right) + \\ & \quad \left( (4\pi r^2 - 2r^2\theta) \left( - \frac{-4\pi - \frac{18662400c^2\pi}{r^2} + 2\theta + \frac{9331200c^2\theta}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2} + \right. \right. \\ & \quad \left. \left. \frac{(-4\pi + 2\theta) \left( 4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2} \right)}{(4\pi^2 - 4\pi\theta + \theta^2)^2} \right) \right) / \\ & \quad \left( 4\pi \sqrt{4\pi r^2\theta - r^2\theta^2} \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}} \right) - \end{aligned}$$

$$\begin{aligned}
& \frac{(4\pi r^2 - 2r^2\theta)^2 \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} - \\
& \left. \frac{r^2 \sqrt{1 - \frac{4\pi^2 - 4\pi\theta - \frac{18662400c^2\pi\theta}{r^2} + \theta^2 + \frac{4665600c^2\theta^2}{r^2}}{4\pi^2 - 4\pi\theta + \theta^2}}}{2\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right) d\theta \\
& - \frac{4320c^2m\pi\sqrt{r^2(4\pi - \theta)\theta}}{r^2\sqrt{\frac{c^2(4\pi - \theta)\theta}{r^2(-2\pi + \theta)^2}}(-2\pi + \theta)^3} \\
& - \frac{4320c^2m\pi\sqrt{r^2(4\pi - \theta)\theta}}{r^2\sqrt{\frac{c^2(4\pi - \theta)\theta}{r^2(-2\pi + \theta)^2}}(-2\pi + \theta)^3} = E = h\nu = hnf = mc^2 = hn((1/(1080/\pi))\theta) \\
& - \frac{4320c^2m\pi\sqrt{r^2(4\pi - \theta)\theta}}{r^2\sqrt{\frac{c^2(4\pi - \theta)\theta}{r^2(-2\pi + \theta)^2}}(-2\pi + \theta)^3} = hn((1/(1080/\pi))\theta) \\
& - \frac{4320c^2m\pi\sqrt{r^2(4\pi - \theta)\theta}}{r^2\sqrt{\frac{c^2(4\pi - \theta)\theta}{r^2(-2\pi + \theta)^2}}(-2\pi + \theta)^3} = hn((1/(1080/\pi))\theta) \\
& \left\{ \theta \rightarrow \frac{4320c\pi + \pi r}{3240c} + (9331200c^2\pi^2 + 4320c\pi^2r - \pi^2r^2) \right\} / \\
& \left( 3240c\pi(100776960000c^3 + 6998400c^2r + 6480cr^2 - r^3 + \right. \\
& \quad \left. 233280\sqrt{5}\sqrt{40310784000c^6 + 9331200c^5r + 5940c^4r^2 - c^3r^3})^{1/3} \right) - \\
& \frac{1}{3240c}\pi(100776960000c^3 + 6998400c^2r + 6480cr^2 - r^3 + \\
& \quad 233280\sqrt{5}\sqrt{40310784000c^6 + 9331200c^5r + 5940c^4r^2 - c^3r^3})^{1/3}, \\
& \left\{ \theta \rightarrow \frac{4320c\pi + \pi r}{3240c} - ((1 + i\sqrt{3})(9331200c^2\pi^2 + 4320c\pi^2r - \pi^2r^2)) \right\} / \\
& \left( 6480c\pi(100776960000c^3 + 6998400c^2r + 6480cr^2 - r^3 + \right. \\
& \quad \left. 233280\sqrt{5}\sqrt{40310784000c^6 + 9331200c^5r + 5940c^4r^2 - c^3r^3})^{1/3} \right) + \\
& \frac{1}{6480c}(1 - i\sqrt{3})\pi(100776960000c^3 + 6998400c^2r + 6480cr^2 - r^3 + \\
& \quad 233280\sqrt{5}\sqrt{40310784000c^6 + 9331200c^5r + 5940c^4r^2 - c^3r^3})^{1/3}, \\
& \left\{ \theta \rightarrow \frac{4320c\pi + \pi r}{3240c} - ((1 - i\sqrt{3})(9331200c^2\pi^2 + 4320c\pi^2r - \pi^2r^2)) \right\} / \\
& \left( 6480c\pi(100776960000c^3 + 6998400c^2r + 6480cr^2 - r^3 + \right. \\
& \quad \left. 233280\sqrt{5}\sqrt{40310784000c^6 + 9331200c^5r + 5940c^4r^2 - c^3r^3})^{1/3} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{6480 c} (1 + i \sqrt{3}) \pi \left( 100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \right. \\
& \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \Big\}, \\
\left\{ \theta \rightarrow - \frac{-4320 c \pi + \pi r}{3240 c} - (9331200 c^2 \pi^2 - 4320 c \pi^2 r - \pi^2 r^2) \Big/ \right. \\
& \quad \left( 3240 c \pi \left( -100776960000 c^3 + 6998400 c^2 r - 6480 c r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 - 9331200 c^5 r + 5940 c^4 r^2 + c^3 r^3} \right)^{1/3} \right) + \\
& \quad \frac{1}{3240 c} \pi \left( -100776960000 c^3 + 6998400 c^2 r - 6480 c r^2 - r^3 + \right. \\
& \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 - 9331200 c^5 r + 5940 c^4 r^2 + c^3 r^3} \right)^{1/3} \Big\}, \\
\left\{ \theta \rightarrow - \frac{-4320 c \pi + \pi r}{3240 c} + ((1 + i \sqrt{3}) (9331200 c^2 \pi^2 - 4320 c \pi^2 r - \pi^2 r^2)) \Big/ \right. \\
& \quad \left( 6480 c \pi \left( -100776960000 c^3 + 6998400 c^2 r - 6480 c r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 - 9331200 c^5 r + 5940 c^4 r^2 + c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{6480 c} (1 - i \sqrt{3}) \pi \left( -100776960000 c^3 + 6998400 c^2 r - 6480 c r^2 - r^3 + \right. \\
& \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 - 9331200 c^5 r + 5940 c^4 r^2 + c^3 r^3} \right)^{1/3} \Big\}, \\
\left\{ \theta \rightarrow - \frac{-4320 c \pi + \pi r}{3240 c} + ((1 - i \sqrt{3}) (9331200 c^2 \pi^2 - 4320 c \pi^2 r - \pi^2 r^2)) \Big/ \right. \\
& \quad \left( 6480 c \pi \left( -100776960000 c^3 + 6998400 c^2 r - 6480 c r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 - 9331200 c^5 r + 5940 c^4 r^2 + c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{6480 c} (1 + i \sqrt{3}) \pi \left( -100776960000 c^3 + 6998400 c^2 r - 6480 c r^2 - r^3 + \right. \\
& \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 - 9331200 c^5 r + 5940 c^4 r^2 + c^3 r^3} \right)^{1/3} \Big\} \\
\theta = & \left( \frac{4320 c \pi + \pi r}{3240 c} + (9331200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2) \Big/ \right. \\
& \left( 3240 c \pi \left( 100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240 c} \pi \left( 100776960000 c^3 + 6998400 c^2 r + 6480 c r^2 - r^3 + \right. \\
& \quad \left. 233280 \sqrt{5} \sqrt{40310784000 c^6 + 9331200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \Big)
\end{aligned}$$

Solve[

$$- \left( 4320 c^2 m \pi \sqrt{\left( r^2 \left( 4 \pi - \left( \frac{4320 c \pi + \pi r}{3240 c} + (9331200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2) \Big/ (3240 c \pi \right. \right. \right. \right.$$

$$\begin{aligned}
& \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \\
& \quad \left. \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3)} \right)^{1/3} - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3)} \right)^{1/3} \Big) \\
& \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) / \left( 3240\,c\,\pi \right. \\
& \quad \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \\
& \quad \left. \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3)} \right)^{1/3} - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \Big) \Big) / \\
& \left( r^2 \sqrt{\left( \frac{1}{r^2\,(-2\,\pi + \theta)^2} c^2 \left( 4\,\pi - \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) / \right. \right. \right. \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \right. \\
& \quad \left. \left. \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3)} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \\
& \quad \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \Big) \Big) \\
& \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) / \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \Big) \Big) \\
& \left( -2\,\pi + \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) / \right. \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \right. \\
& \quad \left. \left. \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3)} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right.
\end{aligned}$$

$$\begin{aligned} & \left. \left. \left. \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right)^3 \right)^3 \right) = \\ & \text{h n} \left( (1 / (1080 / \pi)) \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - \left( (1 - i\sqrt{3}) (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) \right) / \\ & \left( 6480\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \\ & \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) + \\ & \frac{1}{6480\,c} (1 + i\sqrt{3}) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \\ & \quad \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3}, n \Big] \\ & \left\{ \left\{ n \rightarrow - \left( 4\,665\,600\,c^2\,m \sqrt{ \left( r^2 \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) / \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{ (40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3) } \right)^{1/3} \right) - \right. \right. \\ & \quad \left. \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \\ & \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) \\ & \quad \left( 4\,\pi - \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) / \right. \\ & \quad \left. \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \right. \right. \\ & \quad \left. \left. \left. \sqrt{ (40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3) } \right)^{1/3} \right) + \right. \\ & \quad \left. \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \right. \\ & \quad \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) \Big) \Big) / \\ & \left( h\,r^2 \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) / \right. \right. \\ & \quad \left. \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \right. \\ & \quad \left. \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) - \right. \\ & \quad \left. \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \right. \\ & \quad \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) \Big) \\ & \left( -2\,\pi + \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) / \right. \\ & \quad \left. \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \right. \end{aligned}$$

Plot3D[

$$\begin{aligned} & \left( - \left( 4\,665\,600\,c^2\,m \sqrt{\left( r^2 \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) / \left( 3240\,c\,\pi \right. \right. \right. \right. \\ & \quad \left. \left. \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \right. \\ & \quad \left. \left. \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) - \right. \\ & \quad \left. \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \right. \\ & \quad \left. \left. \sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) \\ & \left( 4\,\pi - \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) / \right. \\ & \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + \right. \right. \\ & \quad \left. \left. 233\,280\,\sqrt{5}\,\sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5\,r + 5940\,c^4\,r^2 - c^3\,r^3} \right)^{1/3} \right) + \\ & \quad \left. \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2\,r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \right. \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) \right) \Bigg/ \\
& \left( h r^2 \left( \frac{4320\,c\,\pi + \pi r}{3240\,c} + (9\,331\,200\,c^2 \pi^2 + 4320\,c\,\pi^2 r - \pi^2 r^2) \right) \Bigg/ \right. \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \\
& \quad \quad \left. \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Bigg) \\
& \left( -2\,\pi + \frac{4320\,c\,\pi + \pi r}{3240\,c} + (9\,331\,200\,c^2 \pi^2 + 4320\,c\,\pi^2 r - \pi^2 r^2) \right) \Bigg/ \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \\
& \quad \quad \left. \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Bigg)^3 \\
& \sqrt{\left( \frac{1}{r^2 (-2\,\pi + \theta)^2} c^2 \left( \frac{4320\,c\,\pi + \pi r}{3240\,c} + (9\,331\,200\,c^2 \pi^2 + 4320\,c\,\pi^2 r - \pi^2 r^2) \right) \Bigg/ \right.} \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \\
& \quad \quad \left. \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Bigg) \\
& \left( 4\,\pi - \frac{4320\,c\,\pi + \pi r}{3240\,c} - (9\,331\,200\,c^2 \pi^2 + 4320\,c\,\pi^2 r - \pi^2 r^2) \right) \Bigg/ \\
& \quad \left( 3240\,c\,\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\,\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) + \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280\,\sqrt{5} \right. \\
& \quad \quad \left. \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Bigg) \Bigg) \Bigg), \\
& \{r, -1, 1\}, \{m, -1, 1\} \Big]
\end{aligned}$$





$$\begin{aligned}
& \frac{1}{3240 c} \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + 233\,280 \sqrt{5} \right. \\
& \quad \left. \sqrt{\left( 40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3 \right)^{1/3}} \right)^2 \Bigg) \\
& c^2 \left( 4 \pi - \left( \frac{4320 c \pi + \pi r}{3240 c} + \left( 9\,331\,200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2 \right) / \left( 3240 c \right. \right. \right. \\
& \quad \left. \left. \left. \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + 233\,280 \sqrt{5} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\left( 40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3 \right)^{1/3}} \right) - \right. \right. \\
& \quad \left. \left. \frac{1}{3240 c} \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + 233\,280 \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) \right) \Bigg) \theta \Bigg) \\
& \left( -2 \pi + \left( \frac{4320 c \pi + \pi r}{3240 c} + \left( 9\,331\,200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2 \right) / \right. \right. \\
& \quad \left. \left( 3240 c \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + \right. \right. \right. \\
& \quad \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \right. \\
& \quad \left. \frac{1}{3240 c} \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + 233\,280 \right. \right. \\
& \quad \left. \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) \right)^3 \Bigg) = \\
& \left. \ln \left( 1 / \left( 1080 / \pi \right) \right), n \right] \\
& \left\{ \left\{ n \rightarrow \left( 4\,665\,600 c^2 m \sqrt{\left( r^2 \left( \frac{4320 c \pi + \pi r}{3240 c} + \left( 9\,331\,200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2 \right) / \right. \right. \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left( 3240 c \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + \right. \right. \right. \\
& \quad \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \right. \\
& \quad \left. \frac{1}{3240 c} \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + 233\,280 \right. \right. \\
& \quad \left. \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) \right. \\
& \quad \left( 4 \pi - \frac{4320 c \pi + \pi r}{3240 c} - \left( 9\,331\,200 c^2 \pi^2 + 4320 c \pi^2 r - \pi^2 r^2 \right) / \right. \\
& \quad \left. \left( 3240 c \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + \right. \right. \right. \\
& \quad \left. \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \right. \\
& \quad \left. \frac{1}{3240 c} \pi \left( 100\,776\,960\,000 c^3 + 6\,998\,400 c^2 r + 6480 c r^2 - r^3 + 233\,280 \right. \right. \\
& \quad \left. \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000 c^6 + 9\,331\,200 c^5 r + 5940 c^4 r^2 - c^3 r^3} \right)^{1/3} \right) \right) \Bigg) \Bigg) /
\end{aligned}$$

$$\left\{ \left\{ \left( 4\,665\,600\,c^2\,m\,\sqrt{\left( r^2\left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} + (9\,331\,200\,c^2\,\pi^2 + 4320\,c\,\pi^2\,r - \pi^2\,r^2) \right) \right.} \right. \right.$$

$$\begin{aligned}
& \left( 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Big) - \\
& \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Big) \\
& \left( 4\pi - \frac{4320\,c\pi + \pi r}{3240\,c} - (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2 r - \pi^2 r^2) \right) / \\
& \quad \left( 3240\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) + \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Big) \Big) / \\
& \left( h\,r^2 \left( \frac{4320\,c\pi + \pi r}{3240\,c} + (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2 r - \pi^2 r^2) \right) / \right. \\
& \quad \left( 3240\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \right. \\
& \quad \left. \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \sqrt{5} \right. \\
& \quad \left. \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Big) \\
& \left( -2\pi + \frac{4320\,c\pi + \pi r}{3240\,c} + (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2 r - \pi^2 r^2) \right) / \\
& \quad \left( 3240\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \left. \left. 233\,280 \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \right) - \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Big)^3 \\
& \sqrt{\left( \left( c^2 \left( 4\pi - \frac{4320\,c\pi + \pi r}{3240\,c} - (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2 r - \pi^2 r^2) \right) / \right. \right. \\
& \quad \left( 3240\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \sqrt{5} \right. \right. \\
& \quad \left. \left. \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3)} \right)^{1/3} \right) + \\
& \quad \frac{1}{3240\,c} \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2 r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5 r + 5940\,c^4 r^2 - c^3 r^3} \right)^{1/3} \Big) \theta \Big) /
\end{aligned}$$



$$\begin{aligned}
& \left( 4\pi - \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - \left( (1 + i\sqrt{3}) (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2r - \pi^2r^2) \right) \right) / \right. \\
& \quad \left( 6480\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + 233\,280\sqrt{5} \right. \right. \\
& \quad \quad \left. \left. \sqrt{(40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3)} \right)^{1/3} \right) + \\
& \quad \frac{1}{6480\,c} (1 - i\sqrt{3}) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + \right. \\
& \quad \quad \left. 233\,280\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \Big) \Big) \\
& \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - \left( (1 + i\sqrt{3}) (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2r - \pi^2r^2) \right) \right) / \\
& \quad \left( 6480\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \right) + \\
& \quad \frac{1}{6480\,c} (1 - i\sqrt{3}) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + \right. \\
& \quad \quad \left. 233\,280\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \Big) \Big) \\
& \left( -2\pi + \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - \left( (1 + i\sqrt{3}) (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2r - \pi^2r^2) \right) \right) / \right. \\
& \quad \left( 6480\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \right) + \\
& \quad \frac{1}{6480\,c} (1 - i\sqrt{3}) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + 233\,280 \right. \\
& \quad \quad \left. \sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \Big) \Big)^3 \Big) = \\
& \ln \left( (1 / (1080 / \pi)) \left( \frac{4320\,c\,\pi + \pi\,r}{3240\,c} - \left( (1 + i\sqrt{3}) (9\,331\,200\,c^2\pi^2 + 4320\,c\pi^2r - \pi^2r^2) \right) \right) / \right. \\
& \quad \left( 6480\,c\pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + \right. \right. \\
& \quad \quad \left. \left. 233\,280\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \right) + \\
& \quad \frac{1}{6480\,c} (1 - i\sqrt{3}) \pi \left( 100\,776\,960\,000\,c^3 + 6\,998\,400\,c^2r + 6480\,c\,r^2 - r^3 + \right. \\
& \quad \quad \left. 233\,280\sqrt{5} \sqrt{40\,310\,784\,000\,c^6 + 9\,331\,200\,c^5r + 5940\,c^4r^2 - c^3r^3} \right)^{1/3} \Big) \Big), m \Big] \\
& \left\{ \left\{ m \rightarrow - \left( 4.73727 \times 10^{-49} n r^2 \right. \right. \right. \\
& \quad \left( 1.02952 \times 10^{-12} (4.06869 \times 10^{12} + 3.14159 r) - ((1.63853 \times 10^{-13} + 2.83802 \times 10^{-13} i) \right. \\
& \quad \quad \left. \left. (8.27711 \times 10^{24} + 1.27822 \times 10^{13} r - 9.8696 r^2) \right) \right) / \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} + \\
& \left( 1.61716 \times 10^{-12} - 2.80101 \times 10^{-12} i \right) \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} \Bigg) \\
& \left( -6.28319 + 1.02952 \times 10^{-12} \left( 4.06869 \times 10^{12} + \pi r \right) - \left( \left( 1.63853 \times 10^{-13} + 2.83802 \times 10^{-13} i \right) \left( 8.27711 \times 10^{24} + 1.27822 \times 10^{13} r - 9.8696 r^2 \right) \right) \right) / \\
& \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} + \\
& \left( 1.61716 \times 10^{-12} - 2.80101 \times 10^{-12} i \right) \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} \Bigg)^3 \\
& \sqrt{\left( \left( \left( 12.5664 - 1.02952 \times 10^{-12} \left( 4.06869 \times 10^{12} + \pi r \right) + \left( \left( 1.63853 \times 10^{-13} + 2.83802 \times 10^{-13} i \right) \left( 8.27711 \times 10^{24} + 1.27822 \times 10^{13} r - 9.8696 r^2 \right) \right) \right) / \right. \right. \\
& \left. \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} - \left( 1.61716 \times 10^{-12} - 2.80101 \times 10^{-12} i \right) \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} \right) \\
& \left( 1.02952 \times 10^{-12} \left( 4.06869 \times 10^{12} + \pi r \right) - \left( \left( 1.63853 \times 10^{-13} + 2.83802 \times 10^{-13} i \right) \left( 8.27711 \times 10^{24} + 1.27822 \times 10^{13} r - 9.8696 r^2 \right) \right) / \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} + \right. \\
& \left. \left( 1.61716 \times 10^{-12} - 2.80101 \times 10^{-12} i \right) \left( 2.71533 \times 10^{36} + 6.28985 \times 10^{23} r + 1.94266 \times 10^{12} r^2 - 1. r^3 + 521\,630. \sqrt{\left( 2.92648 \times 10^{61} + 2.25965 \times 10^{49} r + 4.7981 \times 10^{37} r^2 - 2.6944 \times 10^{25} r^3 \right)} \right)^{1/3} \right) \Bigg) / \\
& \left( r^2 \left( -6.28319 + 1.02952 \times 10^{-12} \left( 4.06869 \times 10^{12} + \pi r \right) - \left( \left( 1.63853 \times 10^{-13} + 2.83802 \times 10^{-13} i \right) \left( 8.27711 \times 10^{24} + 1.27822 \times 10^{13} r - 9.8696 r^2 \right) \right) \right) / \right.
\end{aligned}$$

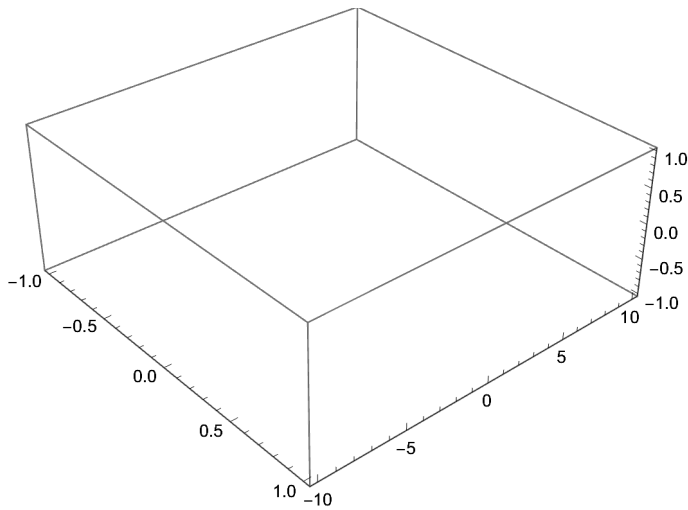
[illegible]



$$\begin{aligned}
& \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
& \quad 1.94265512784 \cdot r^{12} - 1 \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \quad \left. \left. 4.798099575559119 \cdot r^{37} - 2.694400241737399 \cdot r^{25} \right)^{1/3}} \right) \\
& \left( -6.283185307179586 \cdot r^{12} + 1.0295188123399754 \cdot r^{-12} \left( 4.068687385387123 \cdot r^{12} + \pi r \right) - \right. \\
& \quad \left( (1.6385300799000448 \cdot r^{-13} + 2.8380173481167695 \cdot r^{-13} i) \right. \\
& \quad \left. (8.277108520004151 \cdot r^{24} + 1.2782158399685648 \cdot r^{13} r - \right. \\
& \quad \quad \left. 9.869604401089358 \cdot r^2) \right) / \\
& \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
& \quad 1.94265512784 \cdot r^{12} - 1 \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \quad \left. \left. 4.798099575559119 \cdot r^{37} - 2.694400241737399 \cdot r^{25} \right)^{1/3}} \right) + \\
& (1.6171643687898778 \cdot r^{-12} - 2.8010108509341217 \cdot r^{-12} i) \\
& \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
& \quad 1.94265512784 \cdot r^{12} - 1 \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \quad \left. \left. 4.798099575559119 \cdot r^{37} - 2.694400241737399 \cdot r^{25} \right)^{1/3}} \right)^3 \\
& \sqrt{\left( \left( \left( 12.566370614359172 \cdot r^{-12} - 1.0295188123399754 \cdot r^{-12} \right. \right. \right. \\
& \quad \left. \left. \left( 4.068687385387123 \cdot r^{12} + \pi r \right) + \left( (1.6385300799000448 \cdot r^{-13} + \right. \right. \right. \\
& \quad \quad \left. \left. 2.8380173481167695 \cdot r^{-13} i) \right) (8.277108520004151 \cdot r^{24} + \right. \\
& \quad \quad \left. 1.2782158399685648 \cdot r^{13} r - 9.869604401089358 \cdot r^2) \right) / \\
& \quad \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
& \quad 1.94265512784 \cdot r^{12} - 1 \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \quad \left. \left. 4.798099575559119 \cdot r^{37} - 2.694400241737399 \cdot r^{25} \right)^{1/3}} \right)^{1/3} - \\
& (1.6171643687898778 \cdot r^{-12} - 2.8010108509341217 \cdot r^{-12} i) \\
& \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
& \quad 1.94265512784 \cdot r^{12} - 1 \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \quad \left. \left. 4.798099575559119 \cdot r^{37} - 2.694400241737399 \cdot r^{25} \right)^{1/3}} \right)^{1/3} \\
& \left( 1.0295188123399754 \cdot r^{-12} \left( 4.068687385387123 \cdot r^{12} + \pi r \right) - \right. \\
& \quad \left( (1.6385300799000448 \cdot r^{-13} + 2.8380173481167695 \cdot r^{-13} i) \right. \\
& \quad \left. (8.277108520004151 \cdot r^{24} + 1.2782158399685648 \cdot r^{13} r - \right. \\
& \quad \quad \left. 9.869604401089358 \cdot r^2) \right) / \\
& \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
& \quad 1.94265512784 \cdot r^{12} - 1 \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4.798099575559119 \cdot r^2 - 2.694400241737399 \cdot r^3 \right)^{1/3} + \\
& \left( 1.6171643687898778 \cdot r^{-12} - 2.8010108509341217 \cdot r^{-12} i \right) \\
& \left( 2.715334653855602 \cdot r^3 + 6.289848242871744 \cdot r^2 + \right. \\
& \quad 1.94265512784 \cdot r - 1. \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \left. \left. 4.798099575559119 \cdot r^2 - 2.694400241737399 \cdot r^3 \right)^{1/3}} \right) \Bigg/ \\
& \left( r^2 \left( -6.283185307179586 \cdot r + 1.0295188123399754 \cdot r^{-12} \right. \right. \\
& \quad \left( 4.068687385387123 \cdot r^{12} + \pi r \right) - \left( 1.6385300799000448 \cdot r^{-13} + \right. \\
& \quad \left. 2.8380173481167695 \cdot r^{-13} i \right) \left( 8.277108520004151 \cdot r^{24} + \right. \\
& \quad \left. 1.2782158399685648 \cdot r^{13} r - 9.869604401089358 \cdot r^2 \right) \Bigg/ \\
& \left( 2.715334653855602 \cdot r^3 + 6.289848242871744 \cdot r^2 + \right. \\
& \quad 1.94265512784 \cdot r - 1. \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \left. \left. 4.798099575559119 \cdot r^2 - 2.694400241737399 \cdot r^3 \right)^{1/3}} + \right. \\
& \quad \left( 1.6171643687898778 \cdot r^{-12} - 2.8010108509341217 \cdot r^{-12} i \right) \\
& \quad \left( 2.715334653855602 \cdot r^3 + 6.289848242871744 \cdot r^2 + \right. \\
& \quad \left. 1.94265512784 \cdot r - 1. \cdot r^3 + \right. \\
& \quad \left. 521629.937791151 \cdot \sqrt{\left( 2.926479339098588 \cdot r^{61} + \right. \right. \\
& \quad \left. \left. 2.2596491501446907 \cdot r^{49} + 4.798099575559119 \cdot r^2 - \right. \right. \\
& \quad \left. \left. 2.694400241737399 \cdot r^3 \right)^{1/3}} \right)^2 \Bigg) \Bigg/ \\
& \left( \sqrt{r^2 \left( 12.566370614359172 \cdot r - 1.0295188123399754 \cdot r^{-12} \right. \right. \\
& \quad \left( 4.068687385387123 \cdot r^{12} + \pi r \right) + \\
& \quad \left( 1.6385300799000448 \cdot r^{-13} + 2.8380173481167695 \cdot r^{-13} i \right) \\
& \quad \left( 8.277108520004151 \cdot r^{24} + 1.2782158399685648 \cdot r^{13} r - \right. \\
& \quad \left. 9.869604401089358 \cdot r^2 \right) \Bigg/ \\
& \quad \left( 2.715334653855602 \cdot r^3 + 6.289848242871744 \cdot r^2 + \right. \\
& \quad 1.94265512784 \cdot r - 1. \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \left. \left. 4.798099575559119 \cdot r^2 - 2.694400241737399 \cdot r^3 \right)^{1/3}} - \right. \\
& \quad \left( 1.6171643687898778 \cdot r^{-12} - 2.8010108509341217 \cdot r^{-12} i \right) \\
& \quad \left( 2.715334653855602 \cdot r^3 + 6.289848242871744 \cdot r^2 + \right. \\
& \quad 1.94265512784 \cdot r - 1. \cdot r^3 + 521629.937791151 \cdot \\
& \quad \left. \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \right. \\
& \quad \left. \left. 4.798099575559119 \cdot r^2 - 2.694400241737399 \cdot r^3 \right)^{1/3}} \right) \\
& \left( 1.0295188123399754 \cdot r^{-12} \left( 4.068687385387123 \cdot r^{12} + \pi r \right) - \right. \\
& \quad \left( 1.6385300799000448 \cdot r^{-13} + 2.8380173481167695 \cdot r^{-13} i \right) \\
& \quad \left( 8.277108520004151 \cdot r^{24} + 1.2782158399685648 \cdot r^{13} r - \right.
\end{aligned}$$

$$\begin{aligned}
 & 9.869604401089358 \cdot r^2) \Big/ \\
 & \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + \right. \\
 & \quad 1.94265512784 \cdot r^{12} - 1. \cdot r^3 + 521629.937791151 \cdot \\
 & \quad \sqrt{\left( 2.926479339098588 \cdot r^{61} + 2.2596491501446907 \cdot r^{49} + \right. \\
 & \quad \quad \left. 4.798099575559119 \cdot r^{37} - 2.694400241737399 \cdot r^{25} \right)^{1/3}} + \\
 & \quad \left. (1.6171643687898778 \cdot r^{-12} - 2.8010108509341217 \cdot r^{-12} i) \right. \\
 & \quad \left. \left( 2.715334653855602 \cdot r^{36} + 6.289848242871744 \cdot r^{23} + 1.94265512784 \cdot r^{12} - \right. \right. \\
 & \quad \left. \left. 1. \cdot r^3 + 521629.937791151 \cdot \sqrt{\left( 2.926479339098588 \cdot r^{61} + \right. \right. \right. \\
 & \quad \left. \left. \left. 2.2596491501446907 \cdot r^{49} + 4.798099575559119 \cdot r^{37} - \right. \right. \right. \\
 & \quad \left. \left. \left. 2.694400241737399 \cdot r^{25} \right)^{1/3}} \right) \right) \Big), \{n, -1, 1\}, \{r, -10, 10\} \Big]
 \end{aligned}$$



This mass is invisible

$$\begin{aligned}
 r' &= \left( \theta (1080 / \pi) \right) / \left( \sqrt{1 - (v/c)^2} \right) \\
 r' / \theta' &= \left( r \left( \sqrt{1 - (v/c)^2} \right) \right) / \left( \theta / \left( \sqrt{1 - (v/c)^2} \right) \right) = \frac{r \left( 1 - \frac{v^2}{c^2} \right)}{\theta} = c / \quad (195) \\
 t' &= \left( \theta (1080 / \pi) \right) / \left( \sqrt{1 - (v/c)^2} \right) \\
 \text{If, } \frac{r \left( 1 - \frac{v^2}{c^2} \right)}{\theta} &= r / \theta, \text{ then } v \rightarrow 0 \\
 \frac{r \left( 1 - \frac{v^2}{c^2} \right)}{\theta} &= r' / \theta'
 \end{aligned}$$

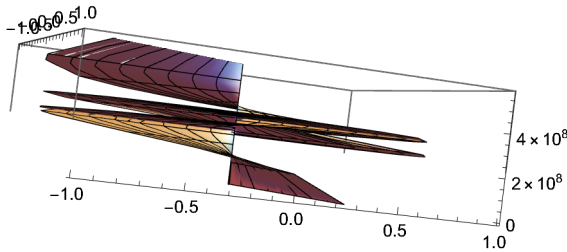
$$\text{Solve}\left[\frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == \frac{r \left(1 - \frac{v^2}{c^2}\right)}{\theta}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{c \sqrt{\theta} \sqrt{\frac{2}{\theta} - \frac{2 r}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{r \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{c \sqrt{\theta} \sqrt{\frac{2}{\theta} - \frac{2 r}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{r \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}\right\}\right\}$$

$$c := (2.99792458 * 10^8)$$

$$\text{RevolutionPlot3D}\left[\frac{c \sqrt{\theta} \sqrt{\frac{2}{\theta} - \frac{2 r}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{r \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}}}{\sqrt{2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



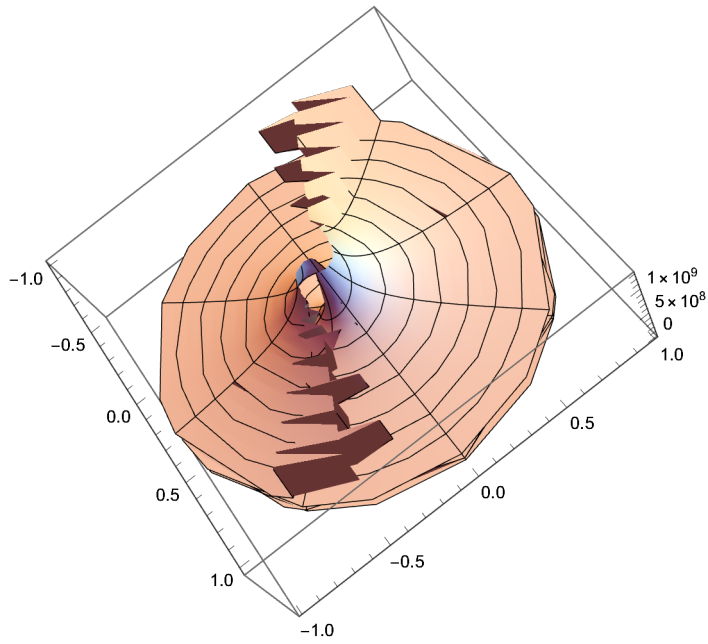
$$\text{Solve}\left[-\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} == \frac{r \left(1 - \frac{v^2}{c^2}\right)}{\theta}, v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1}{\sqrt{2}} c \sqrt{\theta} \sqrt{\left(\frac{2}{\theta} + \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right)}\right\},\right.$$

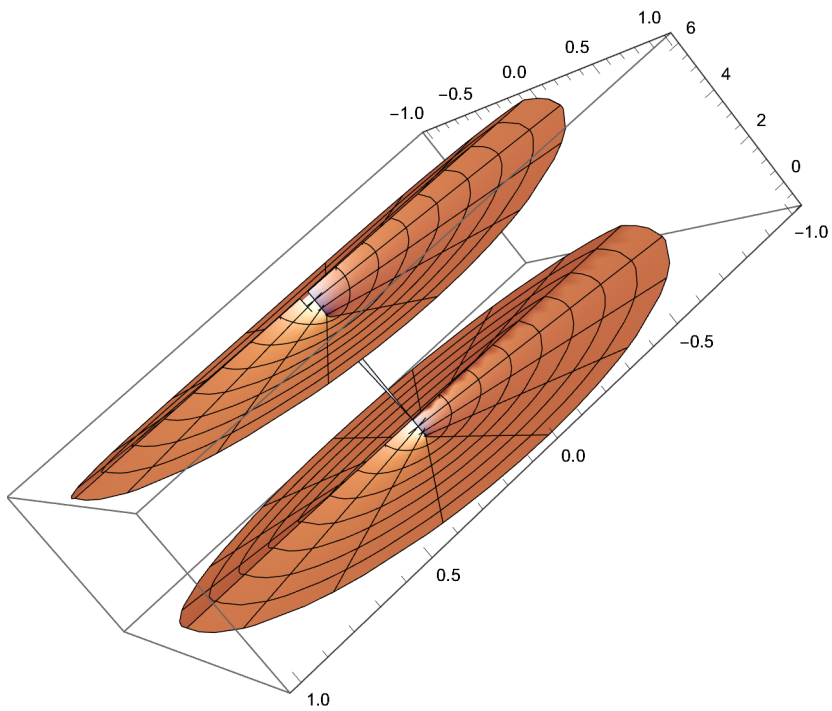
$$\left.\left\{v \rightarrow \frac{1}{\sqrt{2}} c \sqrt{\theta} \sqrt{\left(\frac{2}{\theta} + \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}\right)}\right\}\right\}$$

RevolutionPlot3D[

$$\frac{1}{\sqrt{2}} c \sqrt{\theta} \sqrt{\left( \frac{2}{\theta} + \frac{8 \pi r^2 \theta}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{6 r^2 \theta^2}{(4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{r^2 \theta^3}{\pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} - \frac{4}{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}} + \frac{2 \theta}{\pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$$



$\text{RevolutionPlot3D}\left[\frac{\pi r + \sqrt{\pi^2 r^2 - 2 \pi r \sqrt{r^2 \sin[\beta]^2}}}{r}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$

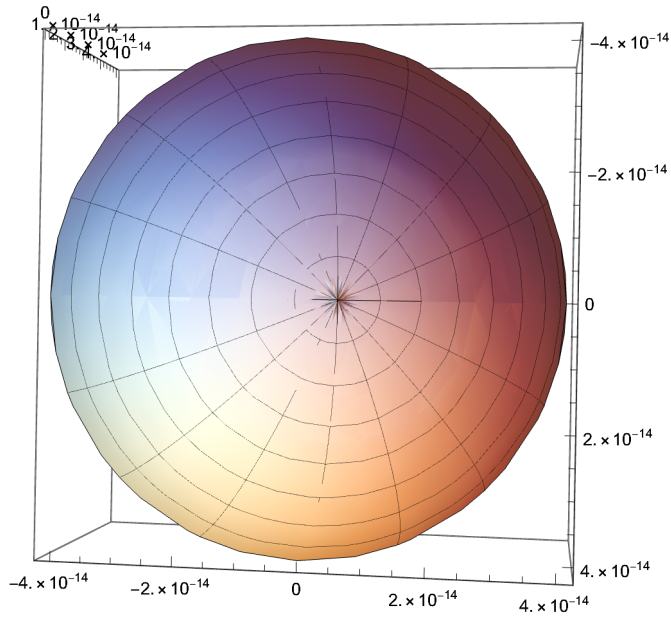


$\text{RevolutionPlot3D}\left[\left\{\frac{\pi r + \sqrt{\pi^2 r^2 - 2 \pi r \sqrt{r^2 \sin[\beta]^2}}}{r}, \frac{\pi r - \sqrt{\pi^2 r^2 - 2 \pi r \sqrt{r^2 \sin[\beta]^2}}}{r}\right\}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$

SphericalPlot3D[  

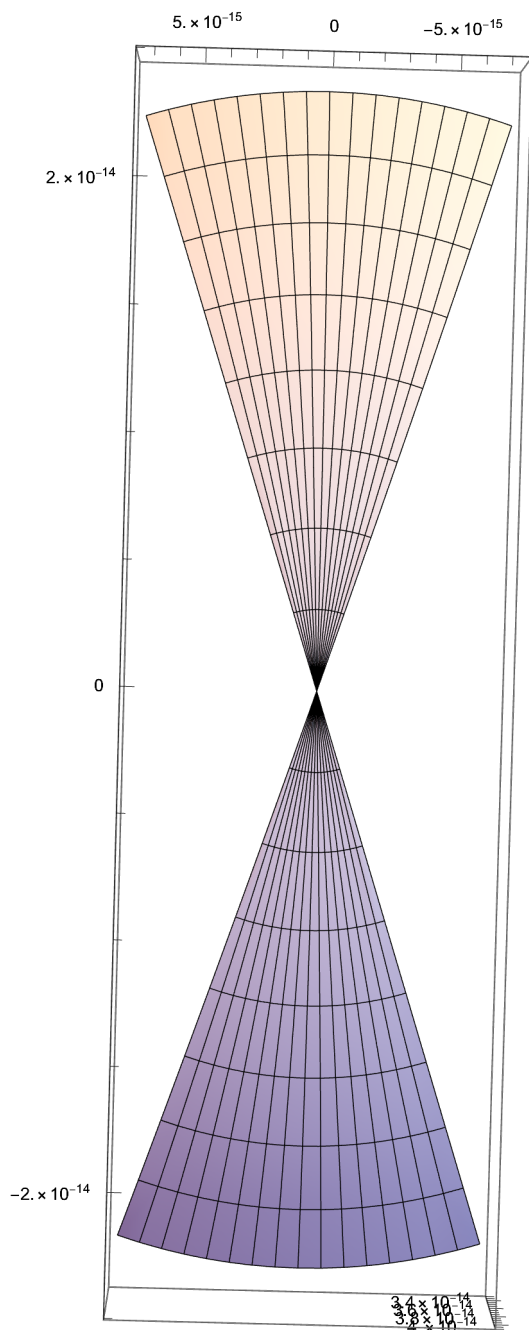
$$.5 (9.109382 \times 10^{-31}) \left( \left( \sqrt{(-1.1294090667581471 \times 10^{-18} \theta + 8.987551787368176 \times 10^{-16} \theta^2 + 3.5481432270250993 \times 10^{-18} \sin^2[\beta])} \right) / \right.$$
  

$$\left. \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin^2[\beta]} \right) \right)^{\wedge}$$
  
 2, {θ, - .5 π, .5 π}, {β, -1 π, 1 π}]



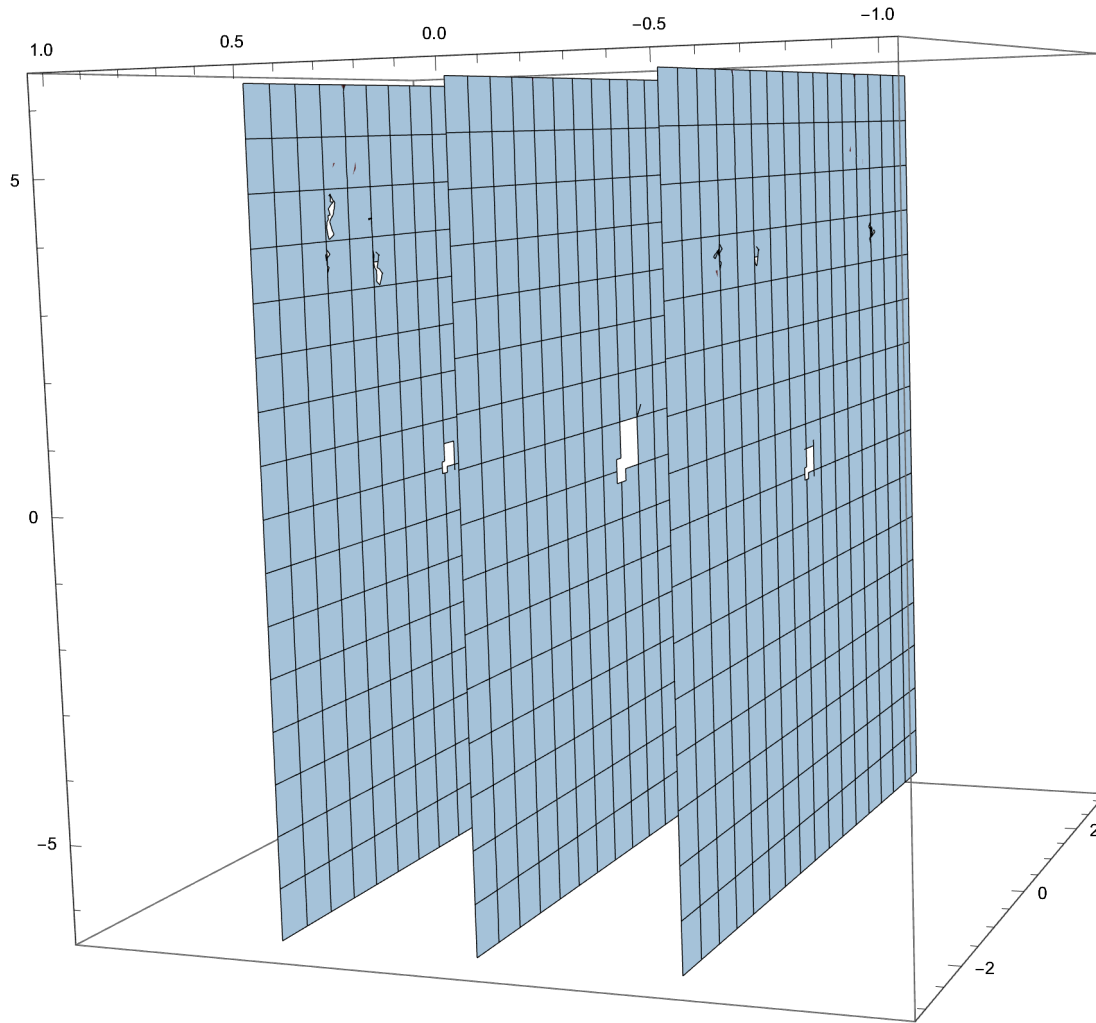
SphericalPlot3D[  

$$.5 (9.109382 \times 10^{-31}) \left( \left( \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin^2[\beta]} \right) / \right. \\
\left. \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin^2[\beta]} \right) \right)^2,$$
  
 $\{\theta, -.2 \pi, .2 \pi\}, \{\beta, -.1 \pi, .1 \pi\}]$



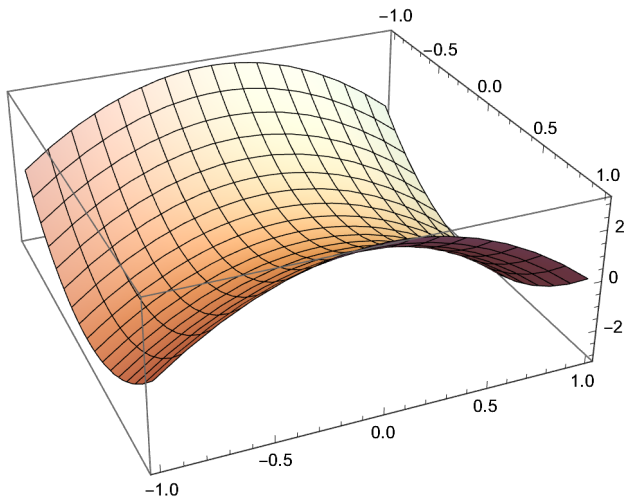


```
ContourPlot3D[.5 (m) ((sqrt(-1.1294090667581471`*^18 theta +
      8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2)) /
    (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)))^2,
  {m, -1, 1}, {theta, -2 pi, 2 pi}, {beta, -pi, pi}]
```

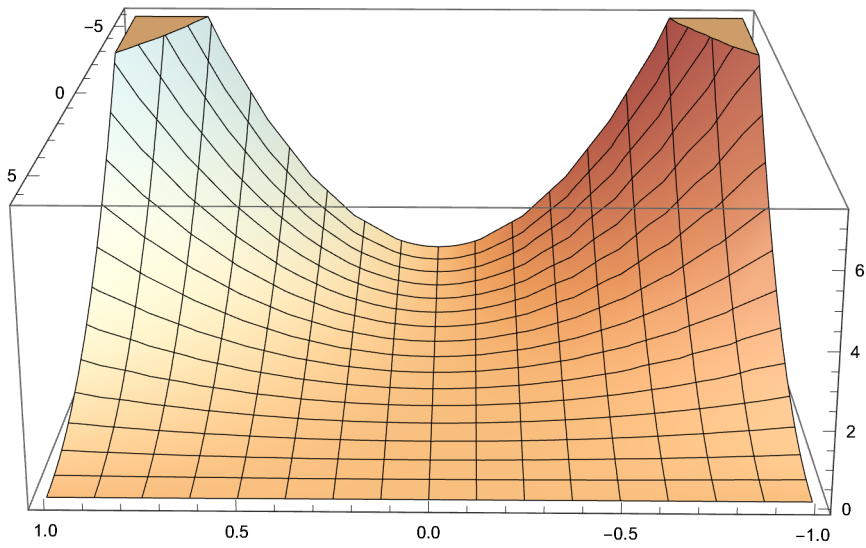


```
ContourPlot3D[.5 (m) ((sqrt(-1.1294090667581471`*^18 theta +
      8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2)) /
    (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2)))^2,
  {m, -1, 1}, {theta, -2 pi, 2 pi}, {beta, -pi, pi}]
```

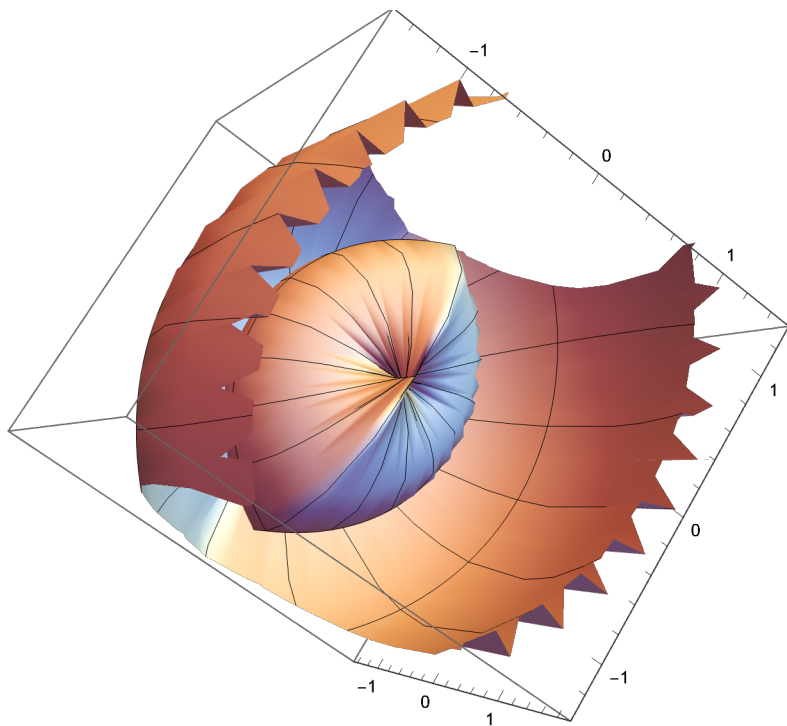
`Plot3D[ $\pi r^2 - \pi x^2$ , {r, -1, 1}, {x, -1, 1}]`



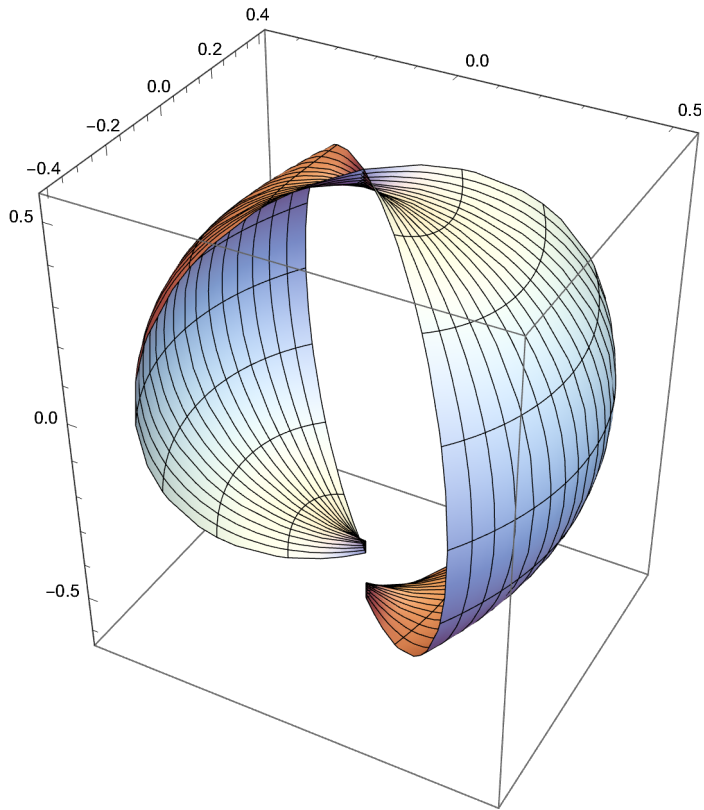
`Plot3D[ $\pi r^2 - \pi \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2$ , {r, -1, 1}, { $\theta$ ,  $-2\pi$ ,  $2\pi$ }]`



SphericalPlot3D $\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$

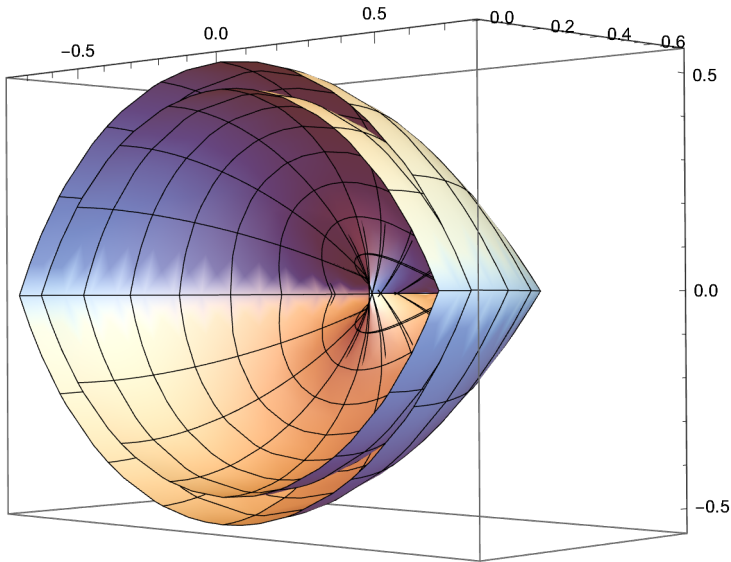


$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)}, \{\theta, -\pi, \pi\}, \{\beta, -\pi / 4, \pi / 4\}\right]$$

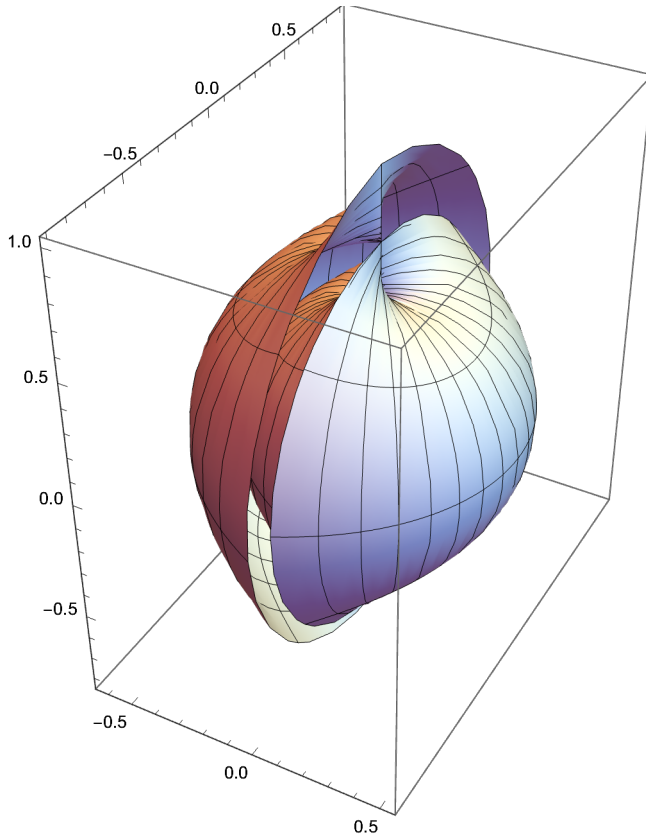


SphericalPlot3D $\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)},\right.$

$\left.\{\theta, -(1/2) \pi, (1/2) \pi\}, \{\beta, -\pi, \pi\}\right]$



$$\text{SphericalPlot3D}\left[\frac{2\pi\sqrt{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)},\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{2\pi\sqrt{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)},\{\theta,-4\pi,4\pi\},\{\beta,-\pi,\pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{2\pi\sqrt{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)},\{\theta,-4\pi,4\pi\},\{\beta,-\pi,\pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{2\pi\sqrt{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)},\{\theta,-4\pi,4\pi\},\{\beta,-\pi,\pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{2\pi\sqrt{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}}{(4\pi-\theta)^2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)},\{\theta,-4\pi,4\pi\},\{\beta,-\pi,\pi\}\right]$$

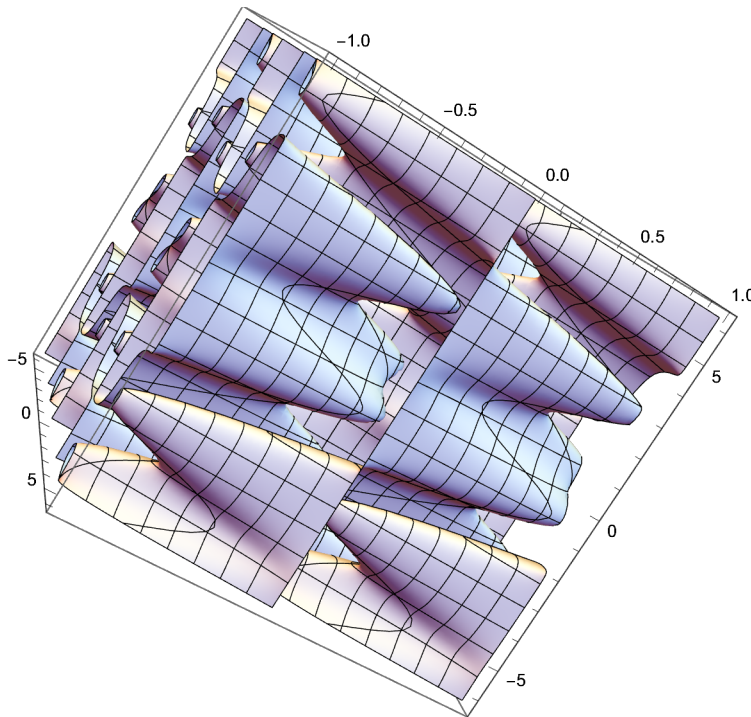
$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{(4 \pi - \theta) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$

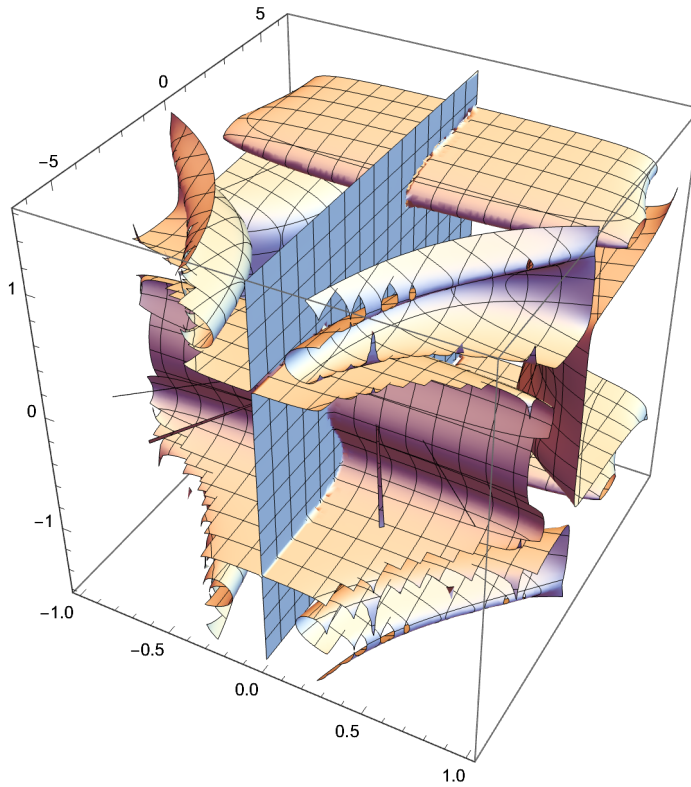
$$\text{ContourPlot3D}\left[\left(r + \cos\left[\frac{u}{2}\right] \sin[v] - \sin\left[\frac{u}{2}\right] \sin[2 v] \cos[u]\right), \{r, -1, 1\}, \{u, -2 \pi, 2 \pi\}, \{v, -2 \pi, 2 \pi\}\right]$$



$$2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right), \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right], \text{ArcSin}\left[\frac{4 \pi r \theta - r \theta^2}{4 \pi^2}\right]$$

$$\text{if } u = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) \text{ and } v = \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right] = \text{ArcSin}\left[\frac{4 \pi r \theta - r \theta^2}{4 \pi^2}\right]$$

$$\text{ContourPlot3D}\left[\left(r + \cos\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[\text{ArcSin}\left[\frac{4\pi r \theta - r \theta^2}{4\pi^2}\right]\right] - \sin\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[2 \text{ArcSin}\left[\frac{4\pi r \theta - r \theta^2}{4\pi^2}\right]\right] \cos\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$

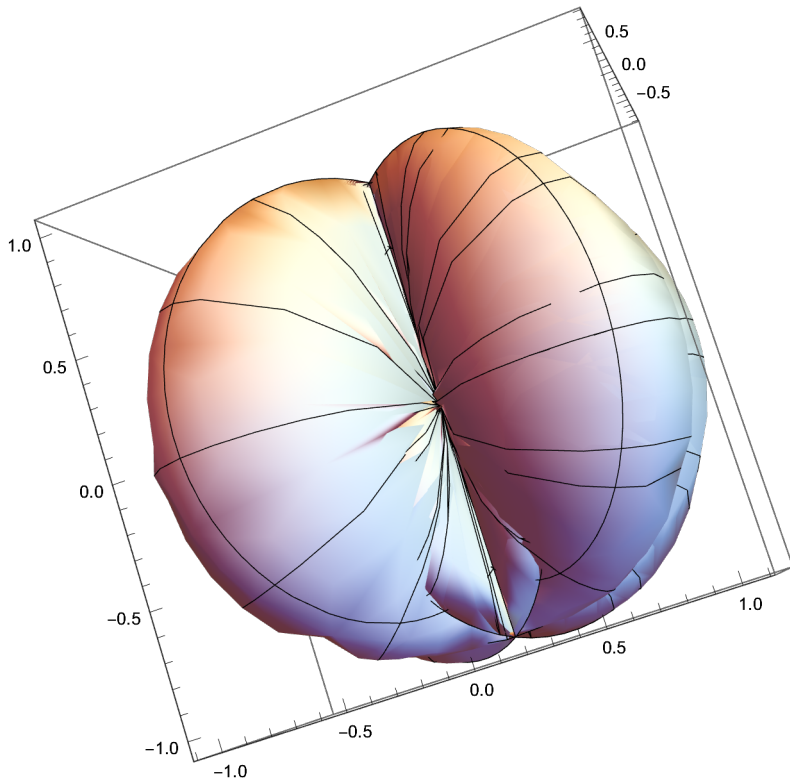


=

$$\text{ContourPlot3D}\left[\left(r + \cos\left[\frac{u}{2}\right] \sin[v] - \sin\left[\frac{u}{2}\right] \sin[2v] \cos[u]\right), \{r, -1, 1\}, \{u, -2\pi, 2\pi\}, \{v, -2\pi, 2\pi\}\right]$$



SphericalPlot3D $\left[\sin\left[\frac{u}{2}\right] \sin[v] + \cos\left[\frac{u}{2}\right] \sin[2v], \{u, -2, 2\pi\}, \{v, -2\pi, 2\pi\}\right]$

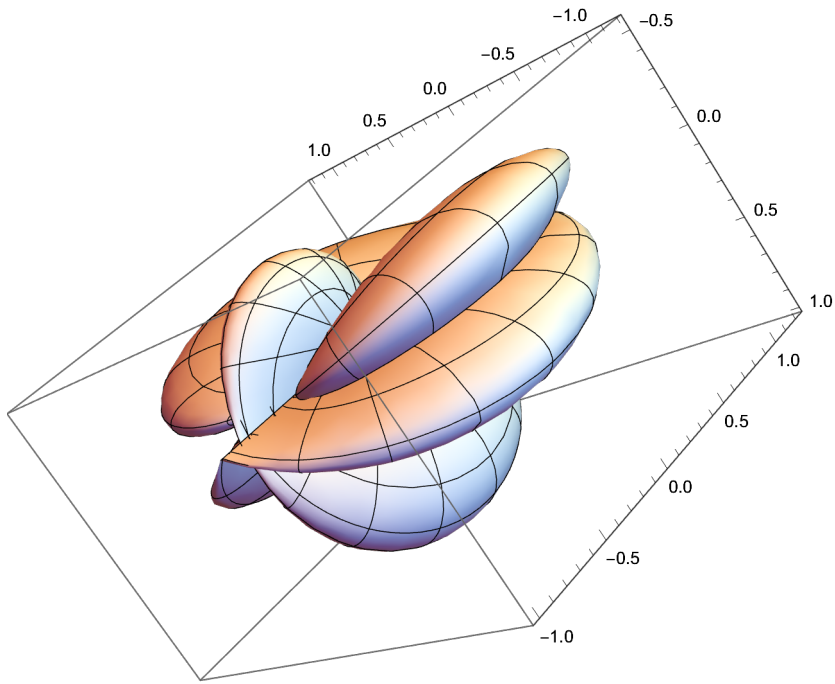


SphericalPlot3D $\left[\sin\left[\frac{u}{2}\right] \sin[v] + \cos\left[\frac{u}{2}\right] \sin[2v], \{u, -2, 2\pi\}, \{v, -2\pi, 2\pi\}\right]$

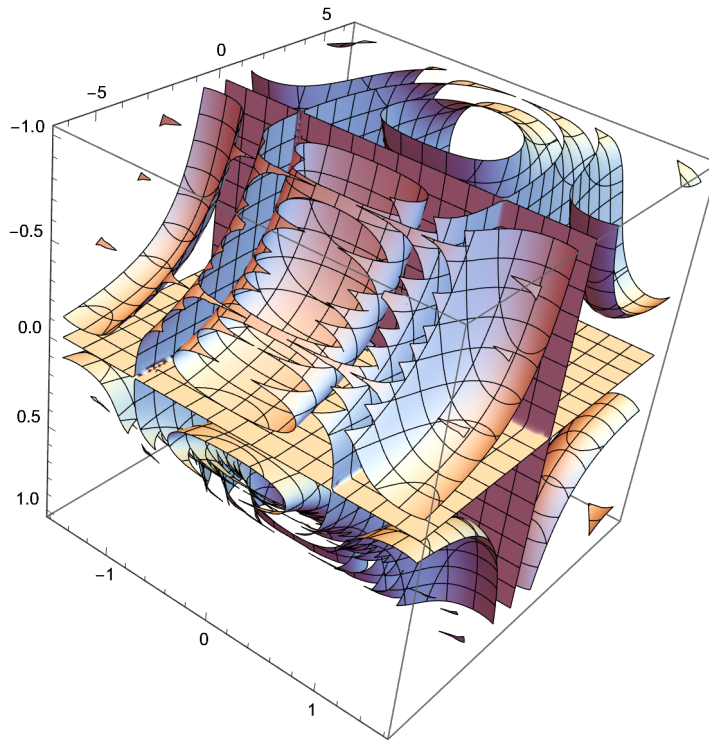
$$\beta \rightarrow \text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right] = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

$$\left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}$$

$\text{SphericalPlot3D}\left[\sin\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] + \right.$   
 $\left. \cos\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[2 \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right], \right.$   
 $\left. \{\theta, -2, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



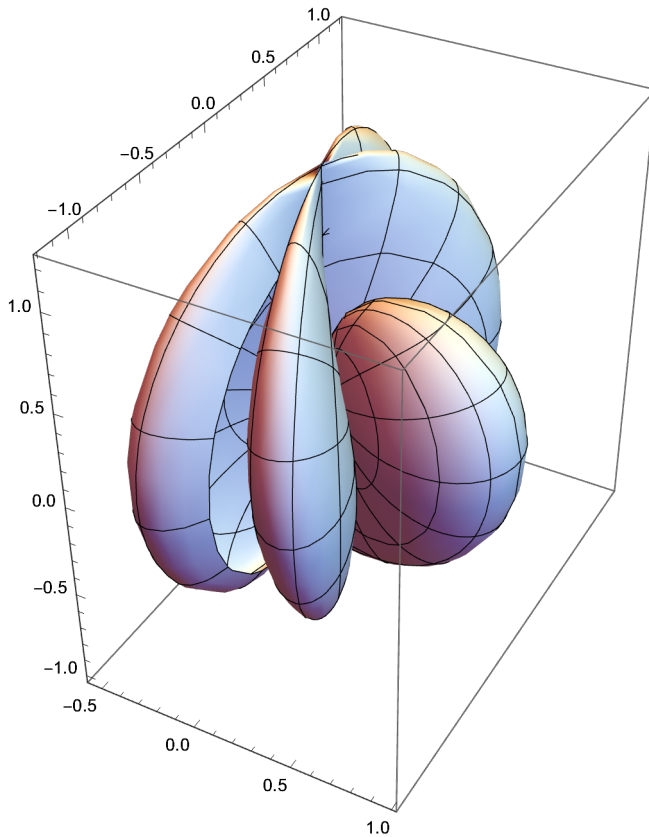
$\text{ContourPlot3D}\left[\sin\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[\text{ArcSin}\left[\frac{4\pi r \theta - r \theta^2}{4\pi^2}\right]\right] + \right.$   
 $\left. \cos\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[2 \text{ArcSin}\left[\frac{4\pi r \theta - r \theta^2}{4\pi^2}\right]\right], \right.$   
 $\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$



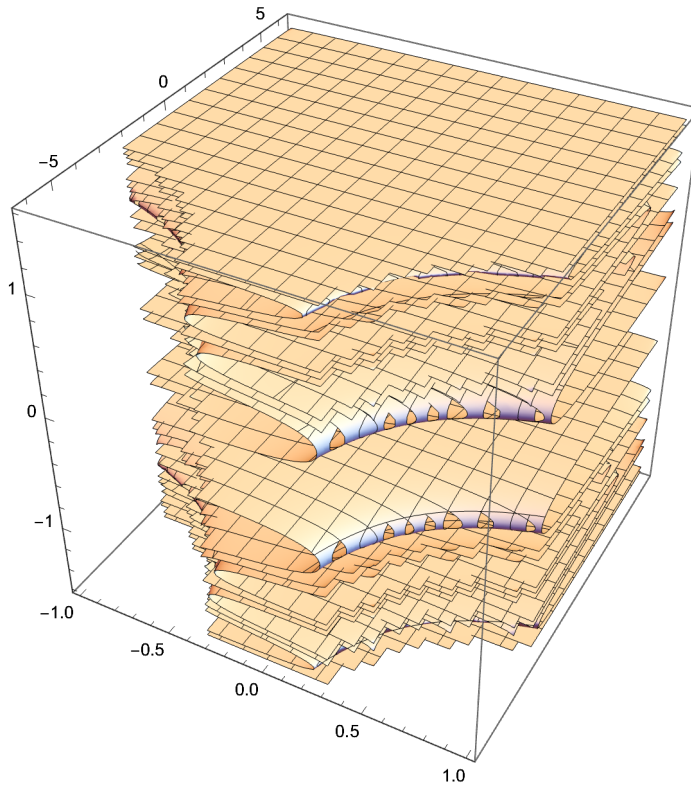
SphericalPlot3D[  

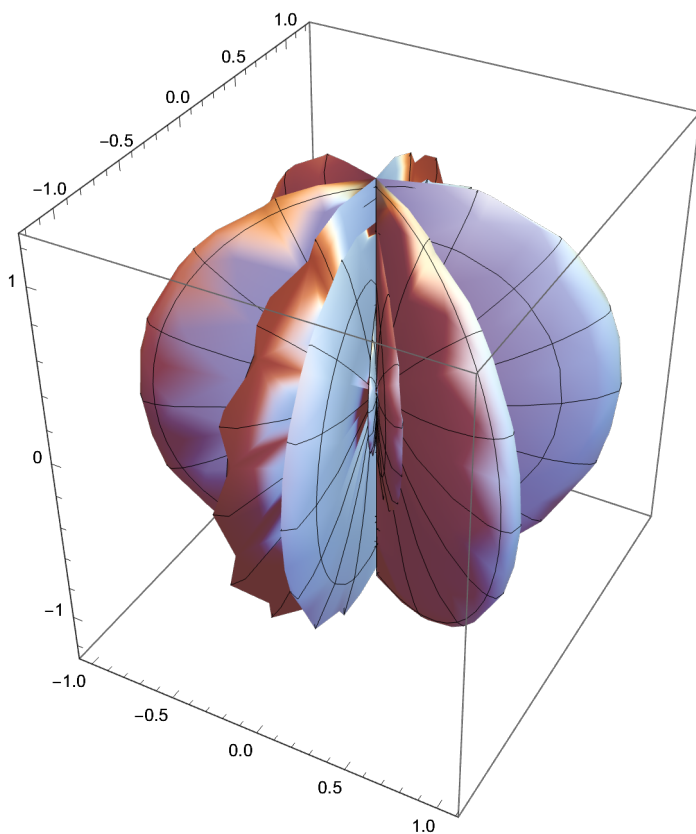
$$\sin\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[\text{ArcSin}\left[\frac{4\pi \frac{2\pi \sqrt{(4\pi-\theta)} \theta}{(4\pi-\theta)} \theta - \frac{2\pi \sqrt{(4\pi-\theta)} \theta}{(4\pi-\theta)} \theta^2}{4\pi^2}\right]\right] +$$
  

$$\cos\left[\frac{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2}\right] \sin\left[2 \text{ArcSin}\left[\frac{4\pi \frac{2\pi \sqrt{(4\pi-\theta)} \theta}{(4\pi-\theta)} \theta - \frac{2\pi \sqrt{(4\pi-\theta)} \theta}{(4\pi-\theta)} \theta^2}{4\pi^2}\right]\right],$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$

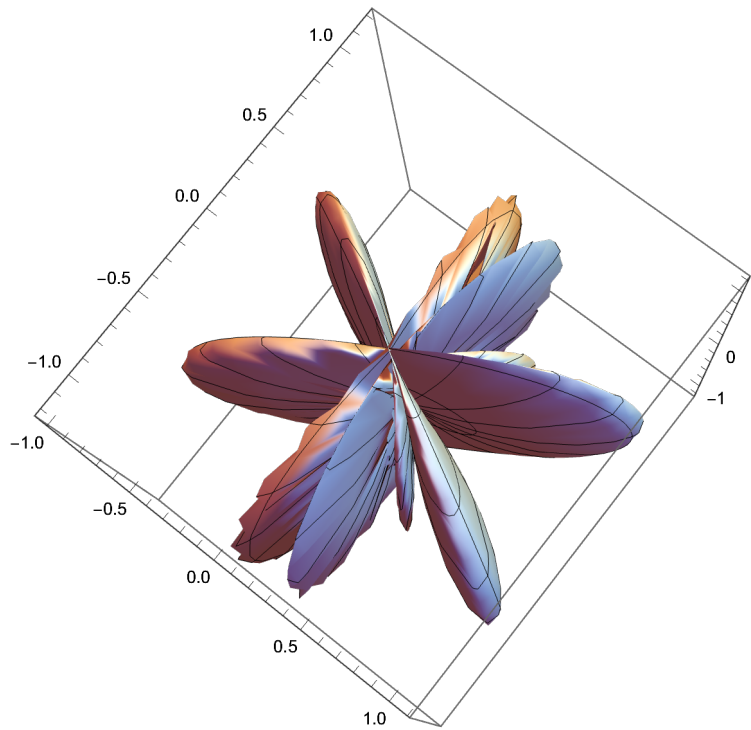


$\text{ContourPlot3D}\left[\sin\left[\frac{\text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right]}{2}\right] \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right] + \right.$   
 $\left. \cos\left[\frac{\text{ArcSin}\left[\frac{4\pi r\theta - r\theta^2}{4\pi^2}\right]}{2}\right] \sin\left[2 \times 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right], \right.$   
 $\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$



$$\text{SphericalPlot3D}\left[\sin\left[\frac{\text{ArcSin}\left[\frac{4\pi\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}\theta-\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}\theta^2}{4\pi^2}\right]}{2}\right]\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]+\right. \\ \left.\cos\left[\frac{\text{ArcSin}\left[\frac{4\pi\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}\theta-\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}\theta^2}{4\pi^2}\right]}{2}\right]\sin\left[2\times 2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right],\right. \\ \left.\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$$


$$\text{SphericalPlot3D}\left[\sin\left[\frac{\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)}\theta}{2\pi}\right]}{2}\right]\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]+ \right. \\
\left. \cos\left[\frac{\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)}\theta}{2\pi}\right]}{2}\right]\sin\left[2\times 2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right], \right. \\
\left. \{\theta, -2, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$



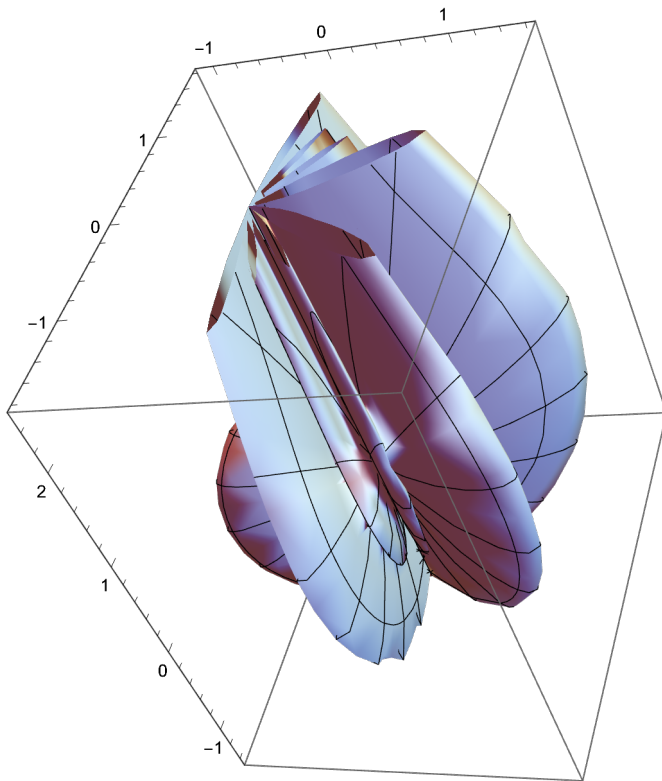
$$\begin{aligned}
& \text{Solve}\left[\sin\left[\frac{\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}{2}\right]\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]+ \right. \\
& \quad \left. \cos\left[\frac{\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]}{2}\right]\sin\left[2\times 2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]=\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}, r\right] \\
& \left\{\left\{r\rightarrow \right. \right. \\
& \quad -\frac{1}{\sqrt{\theta}\sqrt{-4\pi+\theta}}\pi\sqrt{\left(-4\sin\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2-8\right.} \\
& \quad \cos\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]\sin\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] \\
& \quad \sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]\sin\left[4\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]- \\
& \quad \left. 4\cos\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2\sin\left[4\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2\right\}, \\
& \left\{r\rightarrow \frac{1}{\sqrt{\theta}\sqrt{-4\pi+\theta}}\pi\sqrt{\left(-4\sin\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2\sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2- \right.} \\
& \quad 8\cos\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]\sin\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right] \\
& \quad \sin\left[2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]\sin\left[4\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]- \\
& \quad \left. 4\cos\left[\frac{1}{2}\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right]^2\sin\left[4\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]^2\right\}
\end{aligned}$$



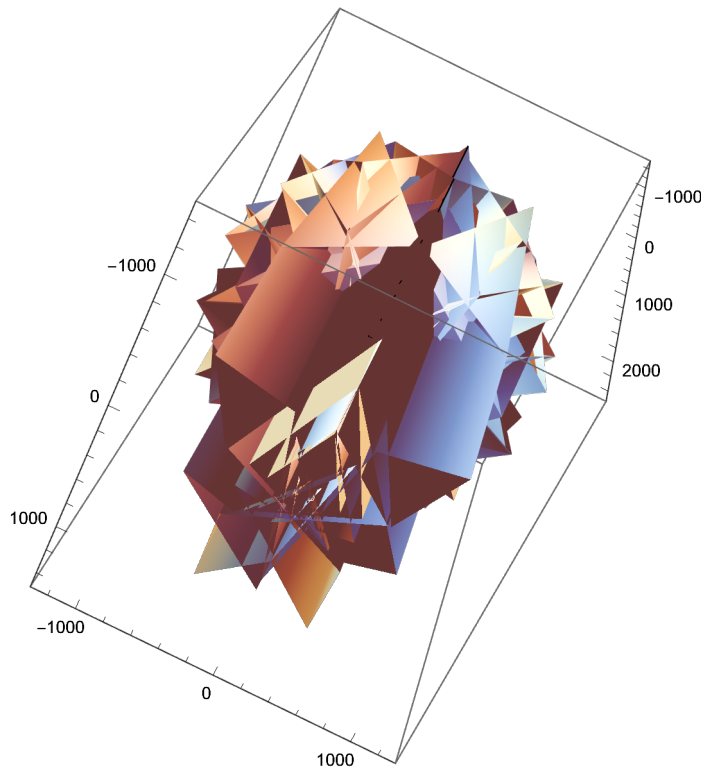
SphericalPlot3D[

$$\frac{1}{\sqrt{\theta} \sqrt{-4\pi + \theta}} \pi \sqrt{\left(-4 \sin\left[\frac{1}{2} \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2 - 8 \cos\left[\frac{1}{2} \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] \sin\left[\frac{1}{2} \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right] \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right] \sin\left[4\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right] - 4 \cos\left[\frac{1}{2} \operatorname{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 \sin\left[4\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]^2\right)},$$

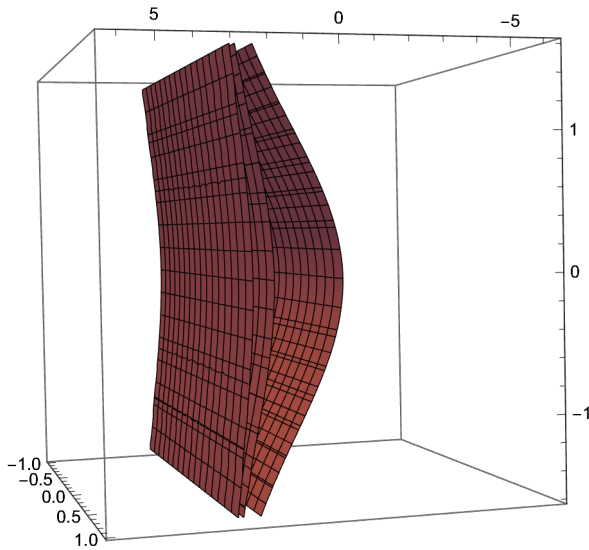
{θ, -2 π, 2 π}, {β, -π / 2, π / 2}]



$$\text{SphericalPlot3D}\left[\frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)} - \frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}}{2\pi}\sqrt{4\pi-\theta_1}\sqrt{\theta_1},\right. \\
\left.\{\theta, -3000\pi, 3000\pi\}, \{\theta_1, -3000\pi, 3000\pi\}\right]$$



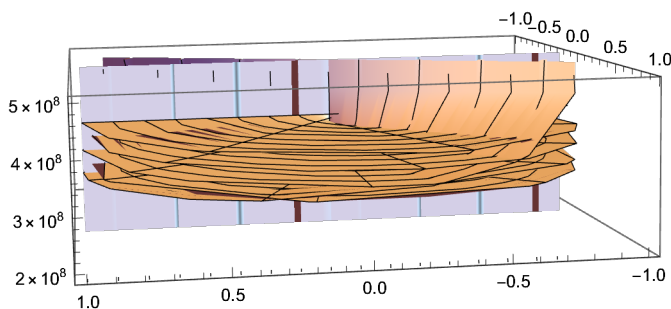
```
ContourPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot 10^{-18} - 1.1294090667581471 \cdot 10^{-18} \theta + 8.987551787368176 \cdot 10^{-16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)^2\right)\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \left(\frac{4 \pi r^2}{c^2 + r^2}\right)^2}\right), \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}]$ 
```



```
h := 6.62606896 * 10^(-34)
```

```
c := 2.99792458 * (10^8)
```

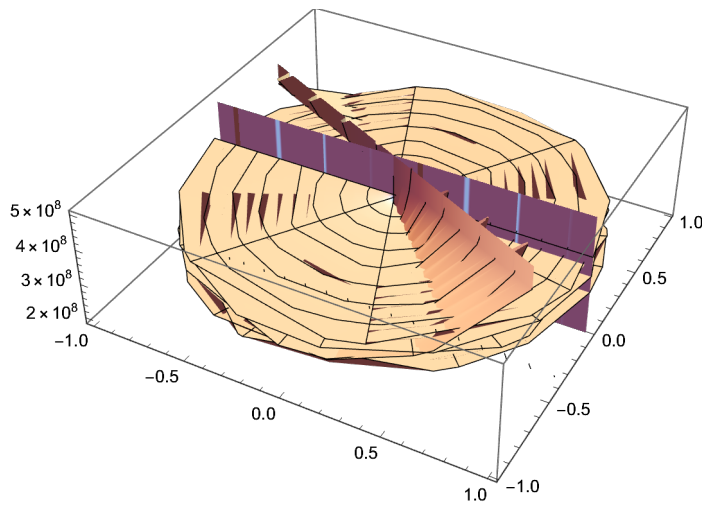
```
RevolutionPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot 10^{-18} - \left(1.1294090667581471 \cdot 10^{-18}\right) (\theta) + 8.987551787368176 \cdot 10^{-16} (\theta)^2\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \left(\frac{4 \pi r^2}{c^2 + r^2}\right)^2}\right), \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}]$ 
```



```

RevolutionPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - \right.}\right.$ 
 $\left.\left(1.1294090667581471 \cdot 10^{18}\right) (\theta) + 8.987551787368176 \cdot 10^{16} (\theta)^2\right) \Big/$ 
 $\left(\sqrt{\left(39.47841760435743 - 12.566370614359172 \theta + \left(\frac{4 \pi (\text{Abs}[z])^2}{c^2 + \text{Abs}[z]^2}\right)^2\right)}\right),$ 
{z, -1, 1}, {θ, -4 π, 4 π}]

```



$$\begin{aligned}
& \text{ContourPlot3D}\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18}\right.\right.}\right. \\
& \quad \left.\left(\frac{1}{2\pi} \sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \text{Abs}[x + \text{i} y]\right)^2 -\right. \\
& \quad \left.1.1294090667581471 \cdot 10^{18} \text{Abs}[x + \text{i} y]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.8.987551787368176 \cdot 10^{16} \text{Abs}[x + \text{i} y]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) \\
& \quad \left.\left.\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2\right)\right] / \\
& \left(\sqrt{\left(39.47841760435743 \cdot \left(\frac{1}{2\pi} \sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \text{Abs}[x + \text{i} y]\right)^2 -\right.\right.} \\
& \quad \left.\left.\sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \text{Abs}[x + \text{i} y]\right)^2 -\right. \\
& \quad \left.12.566370614359172 \cdot \text{Abs}[x + \text{i} y]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \right. \\
& \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \left.\text{Abs}[x + \text{i} y]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + \right.\right.\right. \\
& \quad \left.\left.\left.3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\
& \quad \left.\left.\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2\right)\right)\right), \\
& \{y, -1, 1\}, \{x, -1, 1\}, \{\beta, -2\pi, 2\pi\}
\end{aligned}$$

$$\begin{aligned}
& \text{ContourPlot3D}\left[\left(\sqrt{\left(3.54814 \times 10^{18}\right.}\right.\right. \\
& \quad \left.\left(\frac{1}{2\pi} \sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \text{Abs}[x + iy]\right)^2 -\right. \\
& \quad 1.12941 \times 10^{18} \text{Abs}[x + iy]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \\
& \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad 8.98755 \times 10^{16} \text{Abs}[x + iy]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \left(6\left(-\pi^3 + \right.\right. \\
& \quad \left.\left.18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \frac{2}{3}\right. \\
& \quad \left.\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2 \left.\right) \left.\right) / \\
& \quad \left(\sqrt{\left(39.4784\left(\frac{1}{2\pi} \sqrt{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \text{Abs}[x + iy]\right)^2 -\right.}\right. \\
& \quad 12.5664 \text{Abs}[x + iy]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \\
& \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
& \quad \text{Abs}[x + iy]^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \\
& \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \right. \\
& \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2 \left.\right) \left.\right), \\
& \{y, -1, 1\}, \{x, -1, 1\}, \\
& \{\theta, \\
& \quad -2 \\
& \quad \pi, \\
& \quad 2 \\
& \quad \pi\}
\end{aligned}$$

$$\frac{\sqrt{4\pi - \theta} \sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} \text{Abs}[z]}{2\pi}$$

$$\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

$$h \nu = m c^2$$

$$h \nu = h \left( \frac{1}{\theta} \right) = m c^2$$

$$\text{Solve}\left[h \left( \frac{1}{\theta} \right) == m c^2, m\right]$$

$$\left\{ \left\{ m \rightarrow \frac{h}{c^2 \theta} \right\} \right\}$$

$$\left( \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}} - \frac{2 \pi \left( r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6} \right)^{1/3}}{3 r^2} \right)$$

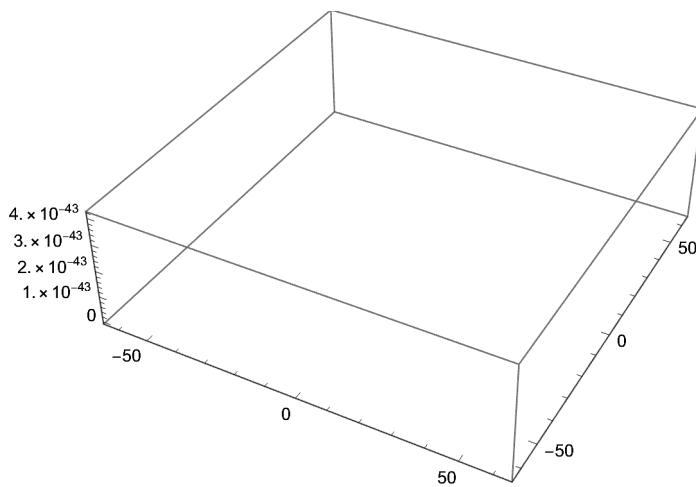
$$\text{RevolutionPlot3D}\left[\frac{6.62606896 * 10^{-34}}{(2.9979245 * 10^8)^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)}\right]$$

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \right.} \right.$$

$$\left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \text{Sin}[\beta]^2 \right) \Bigg) /$$

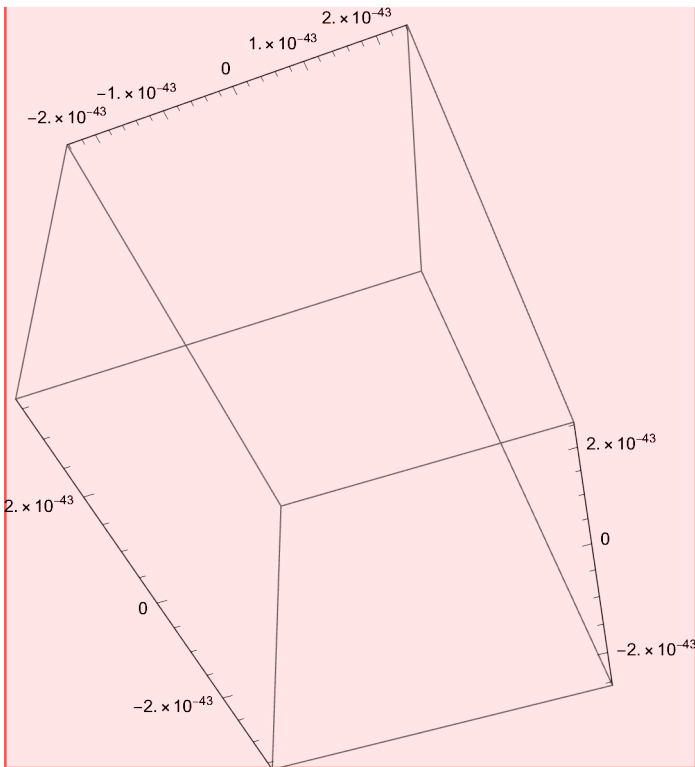
$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)^2 + \right.} \right.$$

$$\left. \left. 39.47841760435743 \cdot 10^{18} \text{Sin}[\beta]^2 \right) \right) \Bigg), \{\beta, -20 \pi, 20 \pi\} \Big]$$



SphericalPlot3D[

$$\begin{aligned}
& (6.62606896 * 10^{-34}) / \left( (2.9979245 * 10^8)^2 \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) / \right. \right. \\
& \quad \left. \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right. \\
& \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \right. \right. \\
& \quad \left. \left. \pi^6 \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]\right]^6 \right)^{1/3} \right) \right) \\
& \quad \left( \sqrt{(-1.1294090667581471 * 10^{18} \theta + 8.987551787368176 * 10^{16} \theta^2 + \right.} \\
& \quad \left. 3.5481432270250993 * 10^{18} \sin[\beta]^2) / \right. \\
& \quad \left. \left( \sqrt{-12.566370614359172 * \theta + \theta^2 + 39.47841760435743 * \sin[\beta]^2} \right), \right. \\
& \quad \left. \{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\} \right]
\end{aligned}$$





$$\left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) /$$

$$\left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) +$$

$$\frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} =$$

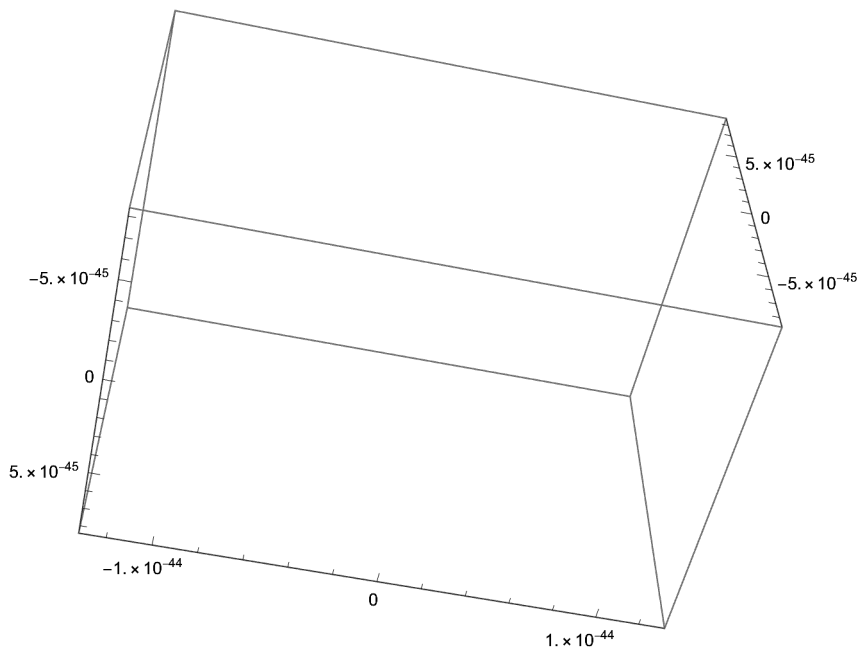
$$2 \left( \pi \pm \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

SphericalPlot3D[

$$\frac{6.62606896 \times 10^{-34}}{(2.9979245 \times 10^8)^2 \theta} \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right),$$

{β, -200 π, 200 π}, {θ, -400 π, 400 π}]

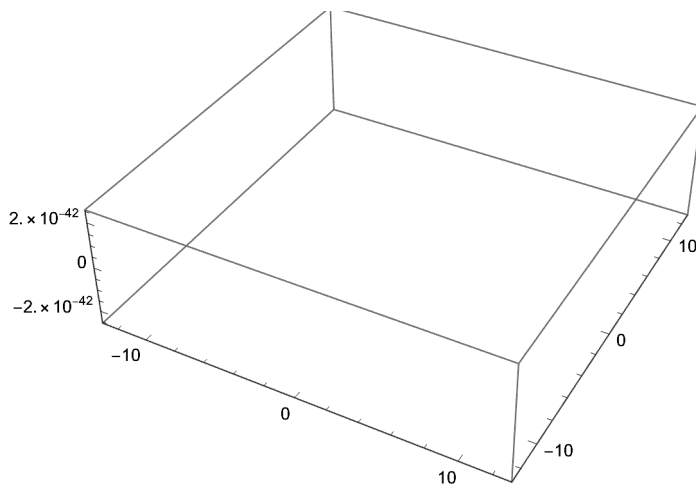


$$h = 6.62606896 \times 10^{-34}$$

v =

$$\left\{ \left\{ u \rightarrow -0.000494236036686326 \sqrt{\left( 2.3423549790780066 \theta - 1.863986866980889 \theta^2 + (0. + 1.863986866980889 \theta^2 i) \sqrt{12.566370614359172 \theta - 1. \theta^2} \right)} \right. \right. \\ \left. \left. \sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2} \right\}, \right. \\ \left. \left\{ u \rightarrow 0.000494236036686326 \sqrt{\left( 2.3423549790780066 \theta - 1.863986866980889 \theta^2 + (0. + 1.863986866980889 \theta^2 i) \sqrt{12.566370614359172 \theta - 1. \theta^2} \right)} \right. \right. \\ \left. \left. \sqrt{39.47841760435743 - 12.566370614359172 \theta + 1. \theta^2} \right\} \right\} = \\ \left( \sqrt{\left( 3.5481432270250993 \theta^{18} - 1.1294090667581471 \theta^{18} + 8.987551787368176 \theta^{16} \right)} \right) / \\ \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right)$$

$$\text{RevolutionPlot3D} \left[ \frac{6.62606896 \times 10^{-34}}{(2.9979245 \times 10^8)^2 \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}}, \right. \\ \left. \left( \sqrt{\left( 3.5481432270250993 \theta^{18} - 1.1294090667581471 \theta^{18} + 8.987551787368176 \theta^{16} \right)} \right) / \right. \\ \left. \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right), \{\theta, -4 \pi, 4 \pi\} \right]$$



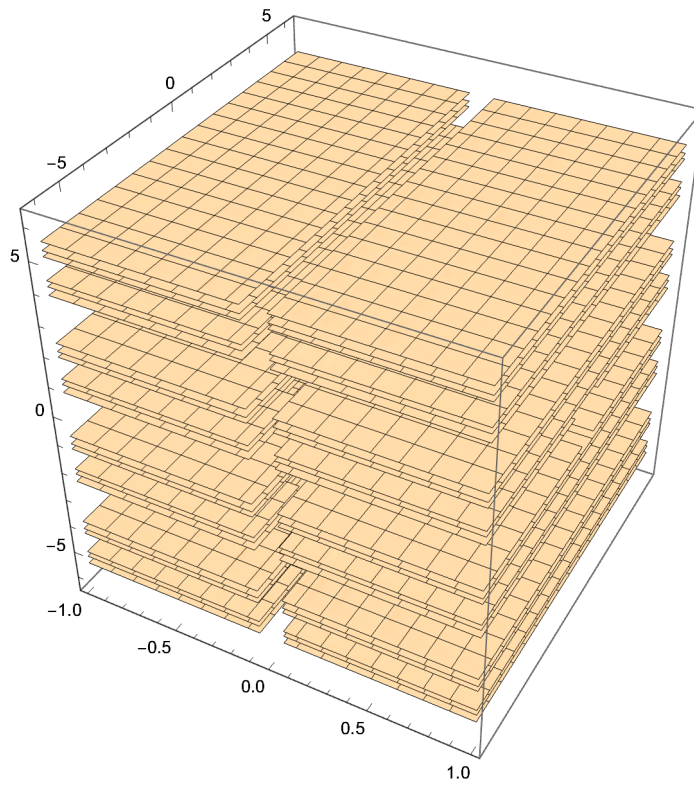
$$\theta = \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} = \left( \frac{4 \pi}{3} + \frac{-4 \pi^2 r^4 + 12 \pi^2 r^2 \eta^2}{6 \pi r^2 (r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6})^{1/3}} - \right. \\ \left. \frac{2 \pi (r^6 - 18 r^4 \eta^2 + 3 \sqrt{3} \sqrt{-r^{10} \eta^2 + 11 r^8 \eta^4 + r^6 \eta^6})^{1/3}}{3 r^2} \right)$$

$$\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi\sqrt{-4\pi + \theta}}\right]$$

ContourPlot3D[  

$$\frac{6.62606896 \times 10^{-34}}{(2.9979245 \times 10^8)^2} \frac{2\pi \left( r^2 + \sqrt{r^4 - r^2 (r \sin[\beta])^2} \right)}{r^2} \left( \sqrt{(-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} (\theta)^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2)} \right) /$$
  

$$\left( \sqrt{(-12.566370614359172 \times 10^0 \theta + (\theta)^2 + 39.47841760435743 \times 10^0 \sin[\beta]^2)} \right),$$
  
 {r, -1, 1}, {θ, -2π, 2π}, {β, -2π, 2π}]



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ContourPlot3D[
$$\frac{6.62606896 \cdot 10^{-34}}{(2.9979245 \cdot 10^8)^2 \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}}$$

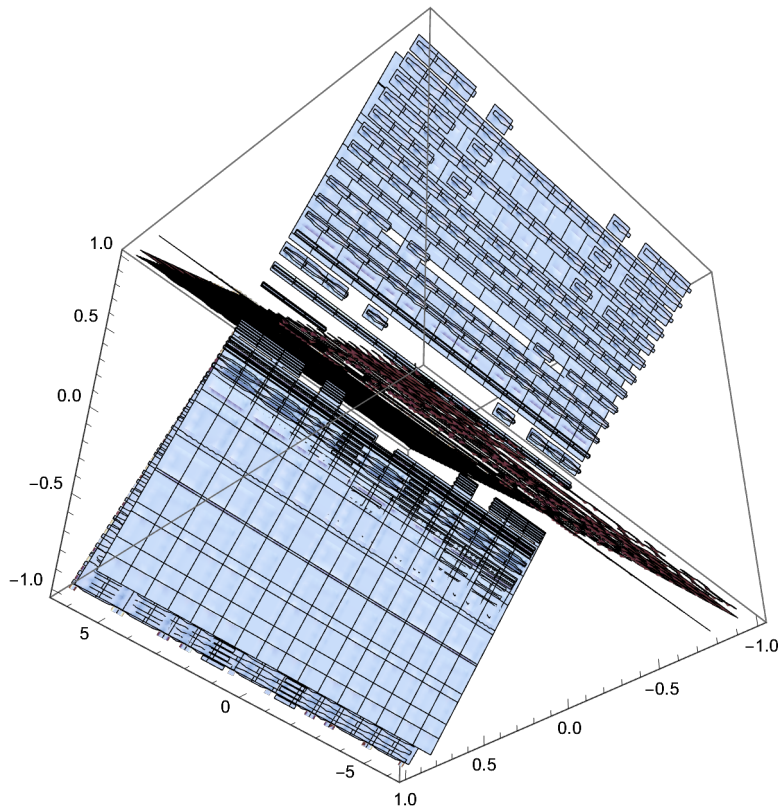

$$\left( \sqrt{-1.1294090667581471 \cdot 10^{18} \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} + 8.987551787368176 \cdot 10^{16}} \right.$$


$$\left. \left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \Bigg] /$$


$$\left( \sqrt{-12.566370614359172 \cdot \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} + \left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2} + \right.$$


$$\left. 39.47841760435743 \cdot \sin[\beta]^2 \right) \Bigg], \{r, -1, 1\}, \{\eta, -1, 1\}, \{\beta, -2 \pi, 2 \pi\}]$$


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A Notational Language for the Light-

# Sensitive Psychophysics

by Parker Emmerson for Workshop with Tom Toleno

## I. Light through the Arc and Height

Light travels through space, but within its travel is the information that the angular element, akin to time, conveys specific information about the location of contour in perceptual space through a geometric correlation that has the capability of mapping out contour in the visual perception directly by analogy of larger ecology to individual play of ambient light off of a contour. This is an interpretation of spectral energy within Gibson's terminology of the false puzzle, "the amount of constancy obtained by an observer is pointless" (BRP 169), because the analogy is the conveyor of meaning to consciousness. We will try to show this symbolically as well as directly.

There is information available in the stimulation, but there is also information communicated. A change in the environment, when measuring size, is the polar coordinate expression of the ambient optic array. The change is undergoing, because of a parameter of structure that is invariant, so the disruption in the array specifies the event. That event causes transition and transformation.

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\} \text{ is the height of a cone}$$

in terms of a difference of circumferences, invariant through  $r$ ,  
because it is always the slant of the cone and also the value that the  
base of the cone cannot reach, because once it reaches that value,  
it is no longer a cone, but collapses to a circle. (196)

$$\text{Solve} \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = \eta, r \right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\} \quad (197)$$

$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r = \frac{2\pi * r * \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} \quad (198)$$

Where  $\eta$  is a given height of a cone, and  $\theta$  the amount of accumulated time of a perception,  $r*\theta$  being the difference of the change in circumference between two circles that correlates to a height in the third dimension.

$$\text{Note that whatever } r \text{ is equal to, the equation simplifies to } 1 = \frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} \quad (199)$$

The polar graph of this function represents the change in  $\eta$  of a radius through time.

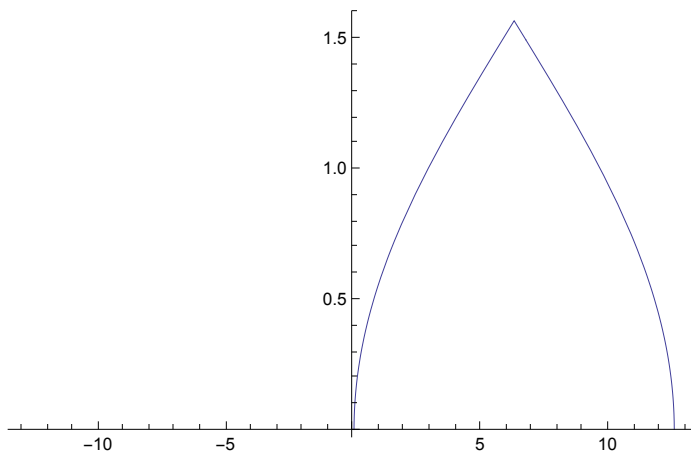
We can solve this equation for  $\beta$ , the angle made by the slant of the cone and the base of the cone,

in terms of theta (the amount of angle involved in folding the circle up into the third dimension when the slant is always equal to the radius.

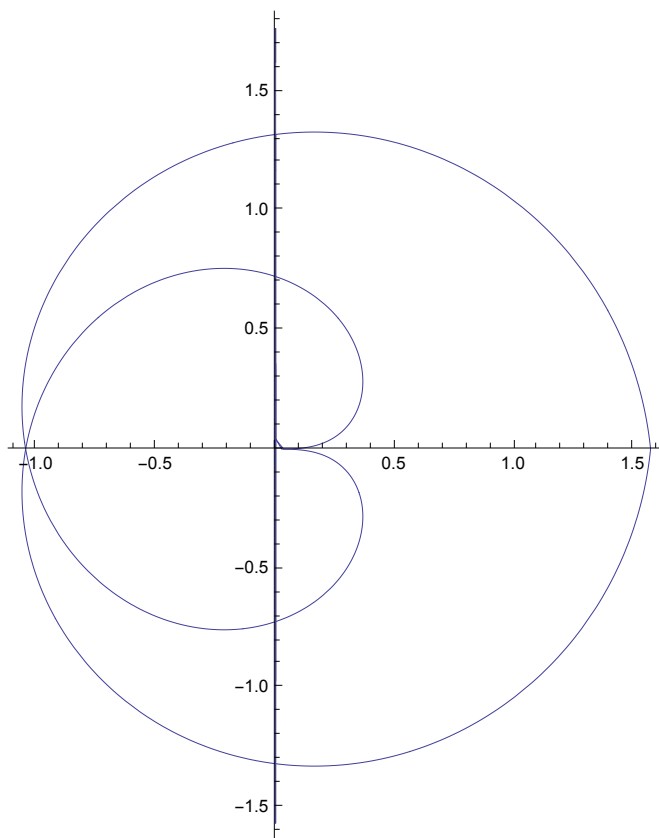
$$\text{Solve}\left[1 == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right\}\right\} \quad (200)$$

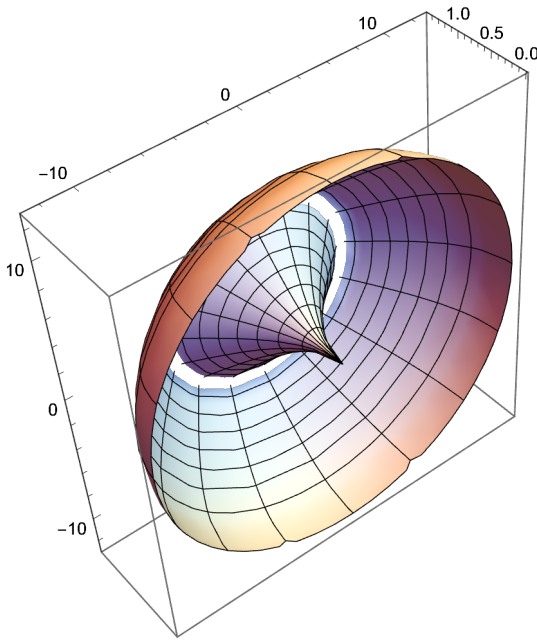
$$\text{Plot}\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right], \{\theta, -13, 13\}\right]$$



`PolarPlot[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ], { $\theta$ , -13, 13}]`



`RevolutionPlot3D[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ], { $\theta$ , -13, 13}]`



The field of optical flow, light traveling through the ambient array, I propose, is represented by the polar coordinate graph of a change in radius over time through transformation to being the height of the cone. A revolution deliver information to the perceiver given the intensity, hue, etc. of light. A single revolution of the system is equivalent to the flow of combined light in the ambient array at the station point of perception.

There are ways of solving for the radius in terms of purely the angle,  $\theta$ . We will examine these nested sets of ways of understanding the point of view. By nested, we mean that depending on how in depth one goes into observing the world or extrapolating a function of light in the array, one will see different visual representations of the structuring of that information that are more or less informationally dense. This will lead to a series of functions that give us introspection into the structuring of light in terms of a cyclic perspective on time. For the system, it is important to realize that in the normal course of parameterizing the motion in the case at hand,  $\theta$  does not go beyond  $4\pi$  (i.e. that it sends the height of the cone up to its maximum value and back down over the course of two revolutions of a circle), and that  $\beta$  would not be able to be easily thought of beyond  $\pi$  or  $2\pi$  (it has a value of  $\pi$  at the maximum height of the transition, and a value of  $2\pi$  once the cone comes back down from the height).

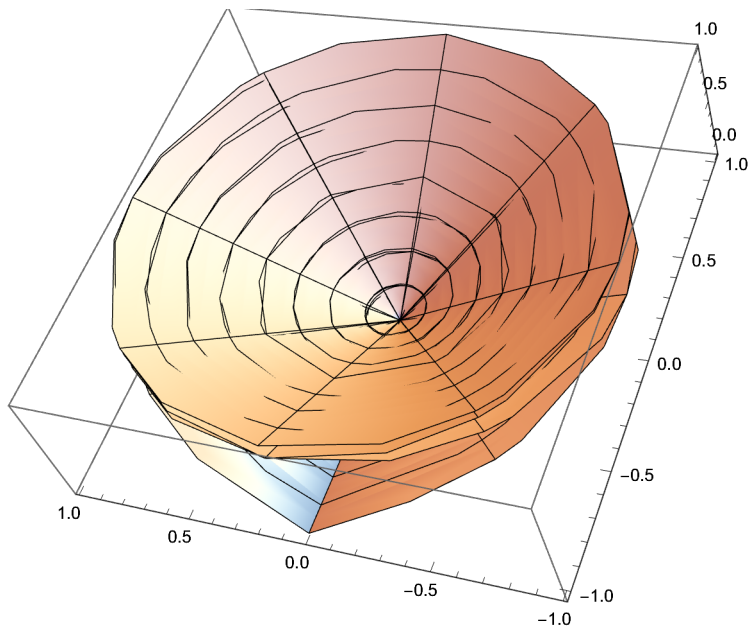
$$\text{Solve}\left[1 == \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\} \quad (201)$$

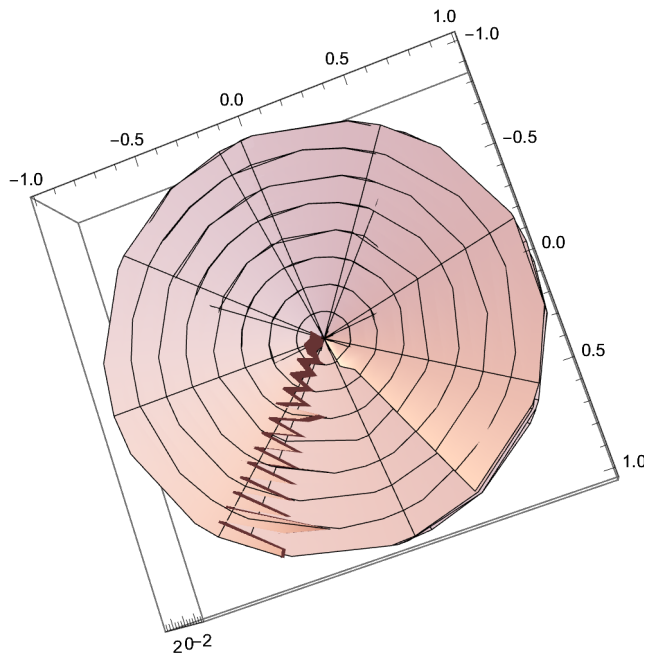


$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}}, \{\eta, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



The Analogy of a Change in Position Relating to a Change in Contour during the

## Pickup of Invariants

Gibson has said that, "The theory of information pickup requires perceptual systems, not senses" (BRP 77). Gibson also he subtlety of the perceptual system to learning and time. He thinks that we continue learning to perceive in more detail as time goes on. This will be an important idea when discussing the extrapolation of functions relating to the information in the array over time.

The wavelength of the light we are discussing is the initial radius of the circle. Its path is to the subjective perceiver and a single wavelength. The parameters of the velocity of its travel, or the travel of any substance, are frequency and wavelength.

We state that :  $v = \lambda f$ , where  $v$  is velocity,  
 $\lambda = r$  is wavelength, and  $1/\text{time} = f = \text{frequency}$ . (202)

$$\text{Time} = 6 \left( \theta_{\text{degrees}} \right) = 6 \left( 180 / \pi \right) \theta = (1080 / \pi) \theta \quad (203)$$

The velocity being discussed is the first derivative of the distance, which is the height of the cone,  $\eta$ . A tiny piece of the ambient array would contain within it information regarding information of the surface off of which the light flowing through the array is reflecting.  $H$  contains information about the time and initial distance of a wavelength of light.

Information of variable contour is transferred to the perceiver by the flux of information in ambient light through each point in the optic array, represented by item number four. The rate of this variance is analogous to velocity in a rotational system, like the structuring of light through space - time. This is what is meant by information in the light.

Helmholtz proposes that phenomena regarding the visual system can be described by the use of analogy when things begin to look paradoxical. He takes into consideration the psychic faculties and suggests that the processing of the environment and its perceptual phenomena may occur through an unconscious working of analogy in the mind. I find this to be interesting and agreeable. It provides a humanist account through the recognition of biological factors regarding perceptual systems.

## The Wavelength with Constant Value

$v =$

$$\lambda f = r \left( 1 / (1080 / \pi) \theta \right) = (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] = \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

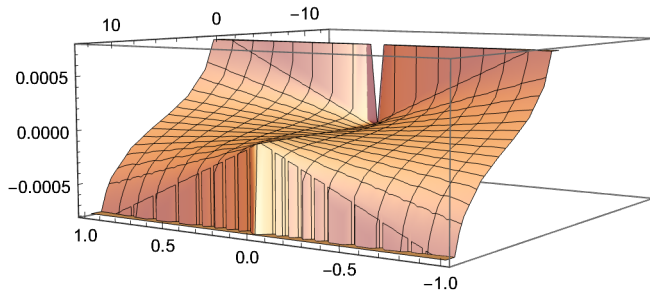
We will try to build up as many functions as possible without resorting to designating something to be having a velocity of light or non - light. It is simply a velocity for the time being. This way, we will have access to a realm of general functions of correlated variables.

$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Velocity when } r \text{ is constant} = \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Plot3D} \left[ \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\} \right]$$



We also have access to the equation,

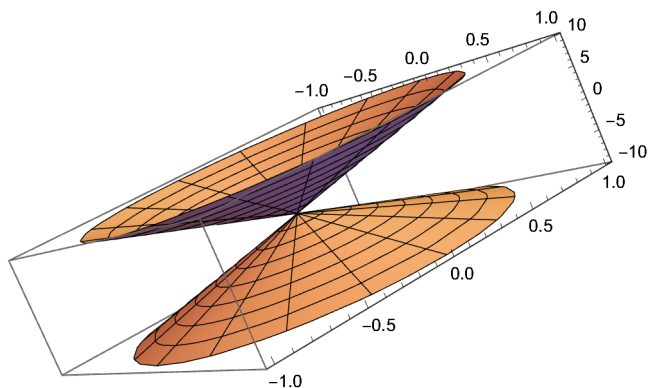
$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = r (1 / (1080 / \pi) \theta), \quad (204)$$

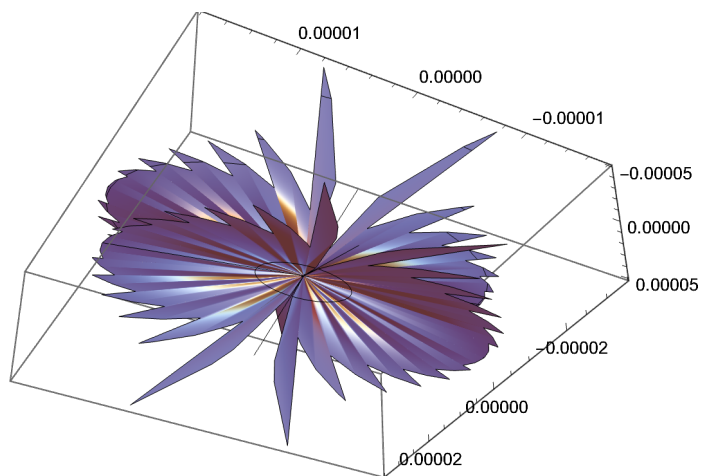
which winds up having the  $r$  variable cancel out,  
and delivers three exact solutions for theta.

$$\text{Solve} \left[ \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = r (1 / ((1080 / \pi) \theta)), \theta \right]$$

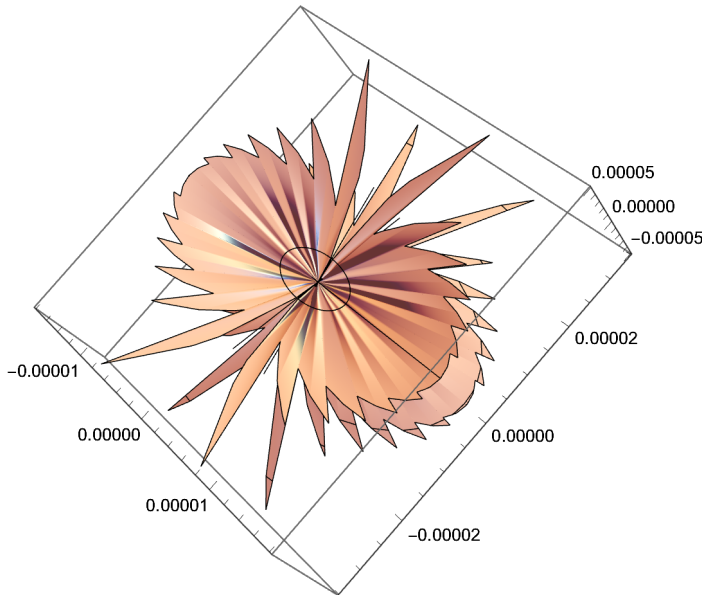
$$\left\{ \left\{ \theta \rightarrow \frac{2}{3} \left( 2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi \right) \right\}, \right. \\ \left\{ \theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \right\}, \quad (205) \\ \left. \left\{ \theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 - i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 + i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \right\} \right\}$$

We will note that an arc length is equal to  $r \cdot \theta$ . Thus, we will be able to see what the arc length is, because it represents the change in circumference of two circles. In this case, as the circle, viewed from head on, recedes from the perceiver into the distance, it gets smaller. This is a change in amount of surface area taken up on the retinal image, but also a way of visualizing the imaginary solutions the time element of waves traveling in space.

$$\text{RevolutionPlot3D}\left[r \frac{2}{3} \left( 2\pi - \frac{2\pi}{(17+3\sqrt{33})^{1/3}} + (17+3\sqrt{33})^{1/3} \pi \right), \{r, -1, 1\}\right]$$


$$\text{RevolutionPlot3D}\left[r \left( \frac{4\pi}{3} + \frac{2(1+i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1-i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right), \{r, -1, 1\}\right]$$


$$\text{RevolutionPlot3D}\left[r \left( \frac{4\pi}{3} + \frac{2(1 - i\sqrt{3})\pi}{3(17 + 3\sqrt{33})^{1/3}} - \frac{1}{3}(1 + i\sqrt{3})(17 + 3\sqrt{33})^{1/3}\pi \right), \{r, -1, 1\}\right]$$



When combined, the three imaginary solutions form a cone, but separately, they exist primarily in the complex plane. It requires all three solutions to deliver information of depth to the perceiver through light in terms of the real. In Gibson's theory, depth is intimately connected with contour. Contour is delivered by the pickup of the invariant,  $r$ , in the ambient array, changing context in a different way from point to point. Thus, understanding of two truths in the real world like information given to the perceiver of an object by an edge, for instance is enabled.

Mach begins by verifying a belief in the space - sense, an area of parameterized space relating the sense of an individual to the stimulus in the world. The space - sense provides a workspace for the individual senses like sense of sight and touch to enable a perceptual experience. "The perception of Depth depends on extra - ocular experiences" (BRP 118) is an idea that makes a great deal of sense to me, because when we experience or perceive truth, we use multiple faculties to make sense of a phenomenon.

## The Wavelength with Changing Value during a Transition

The initial radius changes contexts, but can it be said to actually change? The wavelength,  $r$ , could be said to be changing if we consider that  $\Delta r =$

$r - r_1$ . Although it is invariant in the context of always being the slant of the cone, it changes when understood to be the base of a cone. The height of the cone starts at zero and goes toward the locus of perception, which is the subjective perceiver. In the ambient array, many different wavelengths are present. It is reasonable, then to think that a wavelength could change during the course of traveling a single wavelength. When the circle is infinitely far away, it has a perceived radius of 0. It is important to discuss the ecological context of the meaning of the array. The initial radius could be thought of being analogous to the monocular field of vision.

$$v = \lambda f = r (1 / (1080 / \pi) \theta) = (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta \right] \quad (206)$$

$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta \right]$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} = \text{velocity during a transition} \quad (206)$$

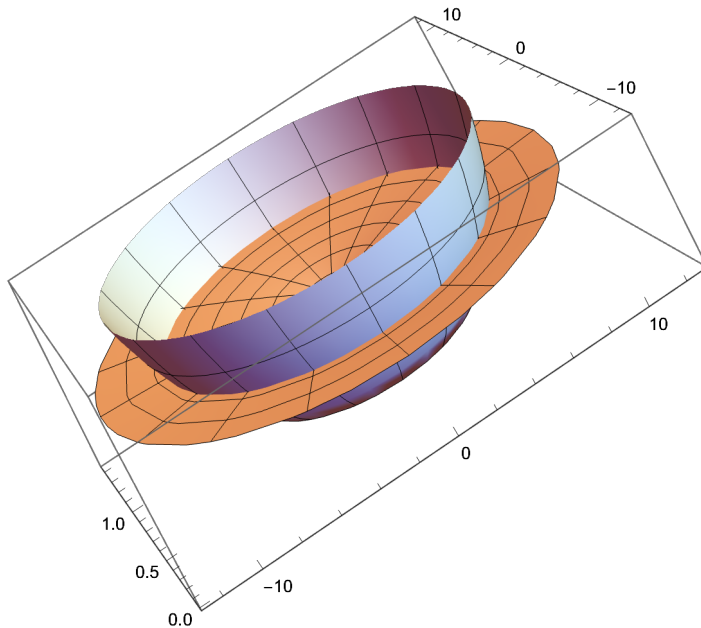
$$(1080 / \pi) \theta = \text{time} \quad (207)$$

$$\frac{2 \pi v t}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi v (1080 / \pi) \theta}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} (1080 / \pi) \theta}{\sqrt{4 \pi \theta - \theta^2}} \quad (208)$$

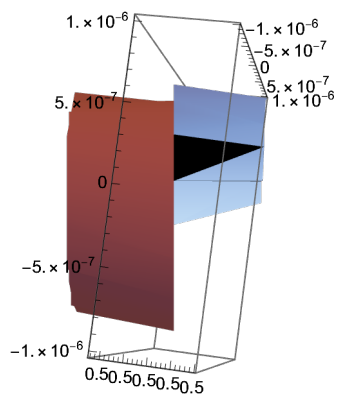
$$\text{Solve} \left[ r == \frac{2 * \left( \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} \right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, r \right]$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\} \right\}$$

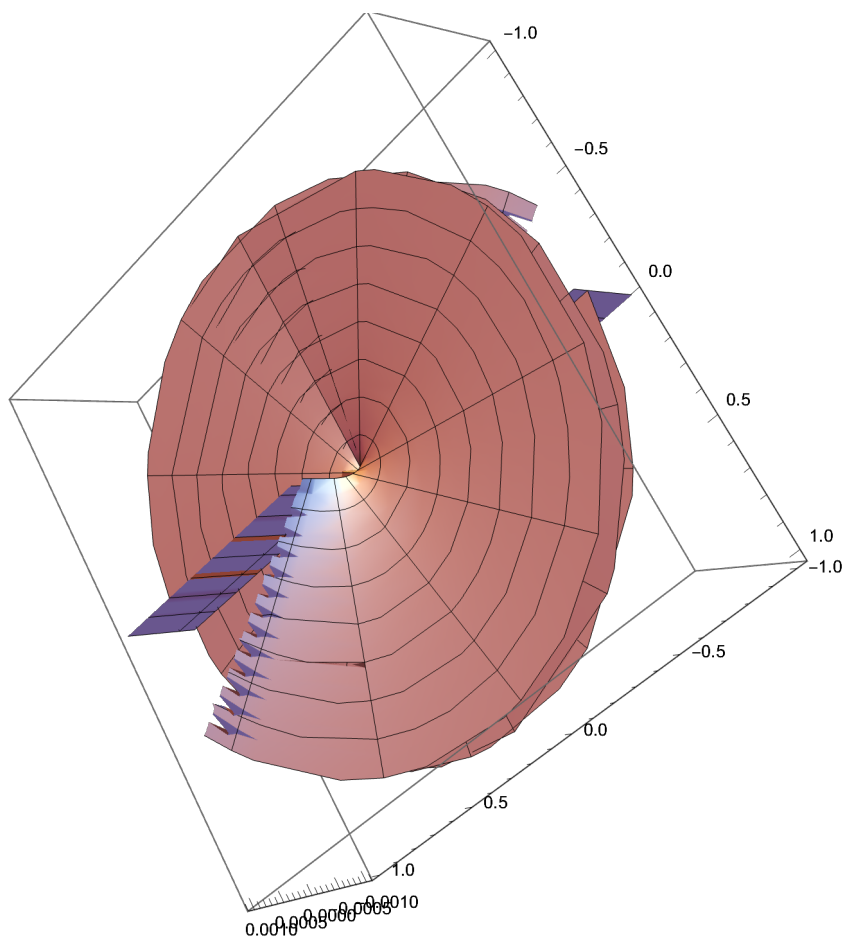
$$\text{RevolutionPlot3D} \left[ \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}, \{\theta, -4 \pi, 4 \pi\} \right]$$



RevolutionPlot3D $\left[\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}, \{\theta, -.0000001, .0000001\}\right]$



$$\text{RevolutionPlot3D}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080},\{r,-1,1\},\{\theta,-3\pi,3\pi\}\right]$$

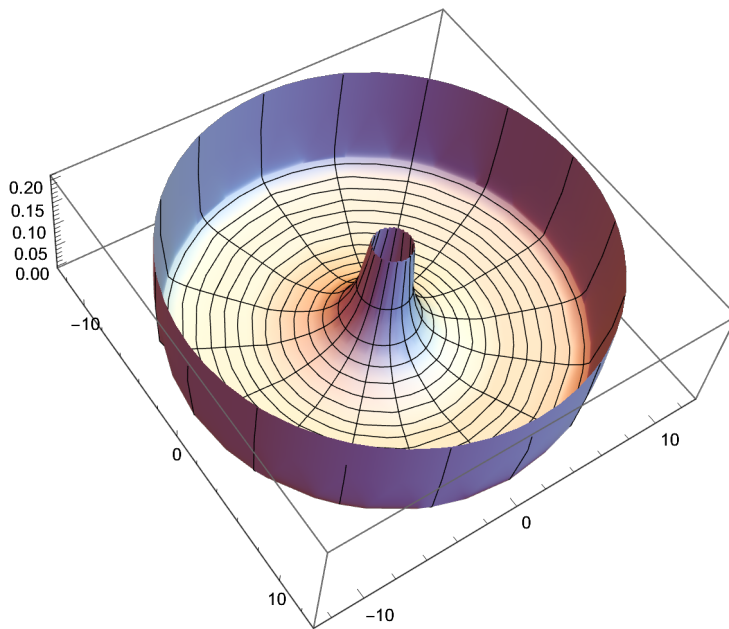


$$\text{Solve}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}==r(1/(1080/\pi)\theta),r\right]$$

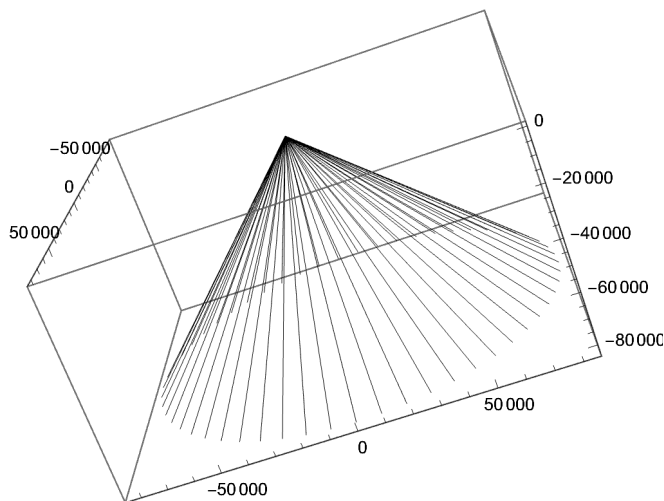
$$\left\{\left\{r\rightarrow-\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\},\left\{r\rightarrow\frac{\sqrt{\frac{1}{4\pi-\theta}+\frac{4\pi}{\theta^2}-\frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}\right\}$$



RevolutionPlot3D $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \{\theta, -13, 13\}\right]$



RevolutionPlot3D $\left[\left\{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -13, 13\}\right]$



This shows us that the parametric structure of our system still holds when the consideration that the wavelength of light,  $r$ , changes during transition. This leads to some evidence for Gibson's idea of an invariant in the structure of light.

$$\text{Solve}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}==r(1/(1080/\pi)\theta),\theta\right]$$

RevolutionPlot3D[

$$\left\{\left\{\pi-\frac{1}{2}\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}-\frac{1}{2}\sqrt{\left(8\pi^2-\frac{1}{3\pi^2r^2}-\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}-\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}-\left(64\pi^3+\frac{4}{\pi r^2}\right)/\left(4\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}\right)}\right\}\right\},$$

$$\left\{\pi-\frac{1}{2}\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}+\frac{1}{2}\sqrt{\left(8\pi^2-\frac{1}{3\pi^2r^2}-\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}-\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}-\left(64\pi^3+\frac{4}{\pi r^2}\right)/\left(4\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}\right)}\right\}$$

$$\left\{\pi-\frac{1}{2}\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}+\frac{1}{2}\sqrt{\left(8\pi^2-\frac{1}{3\pi^2r^2}-\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}-\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}-\left(64\pi^3+\frac{4}{\pi r^2}\right)/\left(4\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}\right)}\right\}$$

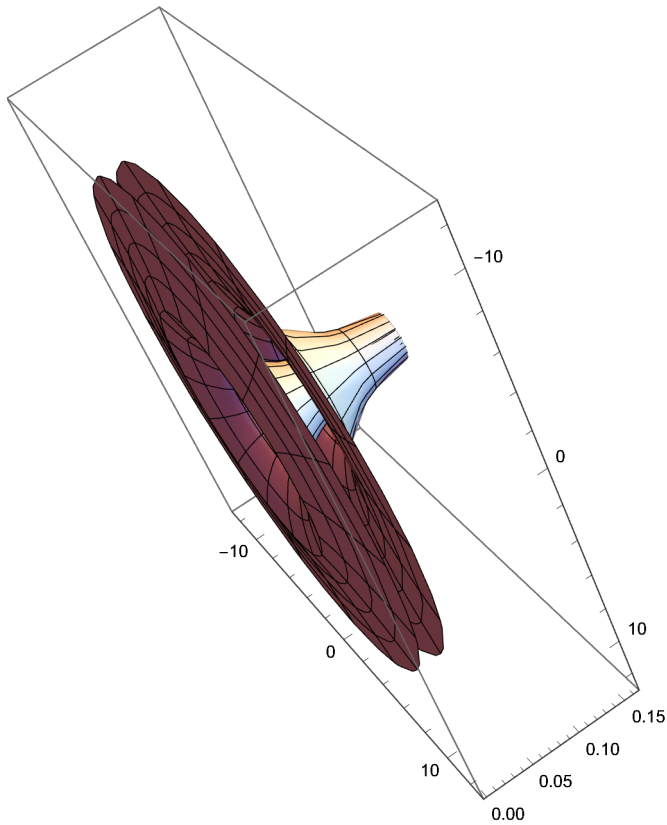
$$\begin{aligned}
& \left. \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) \right) \right\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) - \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\,\pi^2 - \frac{1}{3\,\pi^2\,r^2} - \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} + \left(64\,\pi^3 + \frac{4}{\pi\,r^2}\right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) \right) \right\}, \\
& \left\{ \pi + \frac{1}{2} \sqrt{\left( 4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) + \right. \\
& \quad \frac{1}{2} \sqrt{\left( 8\,\pi^2 - \frac{1}{3\,\pi^2\,r^2} - \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} - \right.} \\
& \quad \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} + \left(64\,\pi^3 + \frac{4}{\pi\,r^2}\right) / \right. \\
& \quad \left. \left( 4 \sqrt{\left( 4\,\pi^2 - \frac{1}{6\,\pi^2\,r^2} + \frac{1}{12\,\pi^2\,r^2\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}} + \right.} \right. \\
& \quad \left. \left. \frac{\left(1 + 13\,824\,\pi^8\,r^4 - 96\,\sqrt{3}\,\pi^4\,\sqrt{r^4 + 6912\,\pi^8\,r^8}\right)^{1/3}}{12\,\pi^2\,r^2} \right) \right) + \right.
\end{aligned}$$



$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}, \theta\right]$$

$$\{\{\theta \rightarrow 2\pi\}\}$$

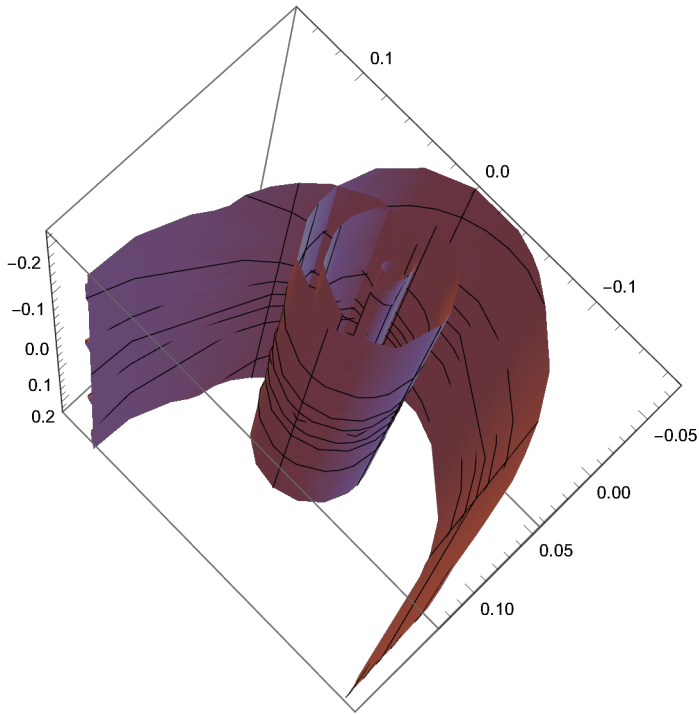
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}, \{\theta, -4\pi, 4\pi\}\right]$$



$$\text{Solve}\left[\frac{2\pi * r * \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, r\right]$$

$$\left\{\left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \text{Csc}[\beta]}{8\pi^2\sqrt{\theta}}\right\}\right\}$$

$$\text{SphericalPlot3D}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \text{Csc}[\beta]}{8\pi^2 \sqrt{\theta}}, \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\}\right]$$



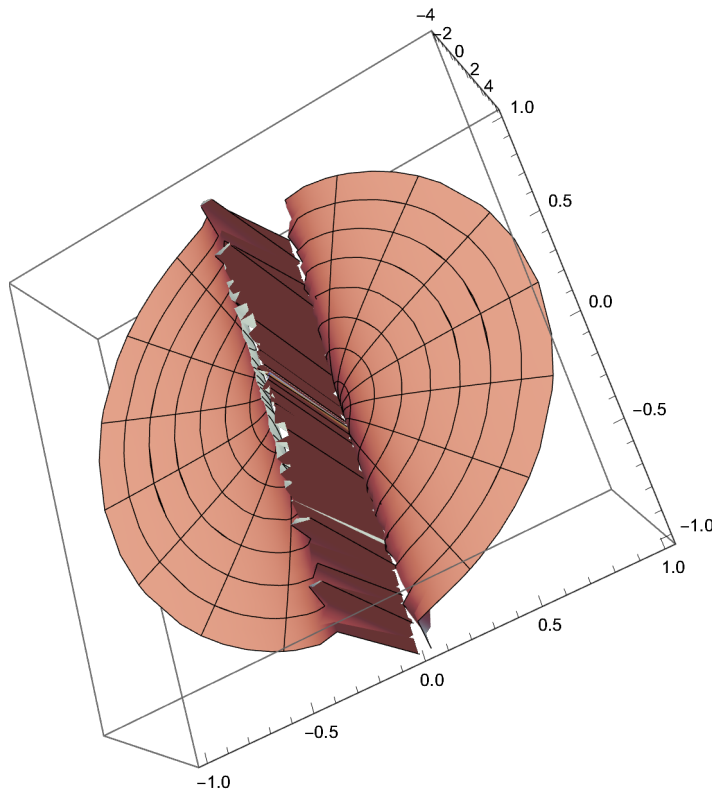
$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \text{Csc}[\beta]}{8\pi^2 \sqrt{\theta}} == r, \beta\right]$$

$$\left\{\left\{\beta \rightarrow \text{ArcCsc}\left[\frac{4\pi^2 r \sqrt{\frac{(2\pi-\theta)^2}{(4\pi-\theta)\theta^2}} \theta^{3/2} \sqrt{(4\pi-\theta)\theta}}{4\pi^2 - 4\pi\theta + \theta^2}\right]\right\}\right\}$$

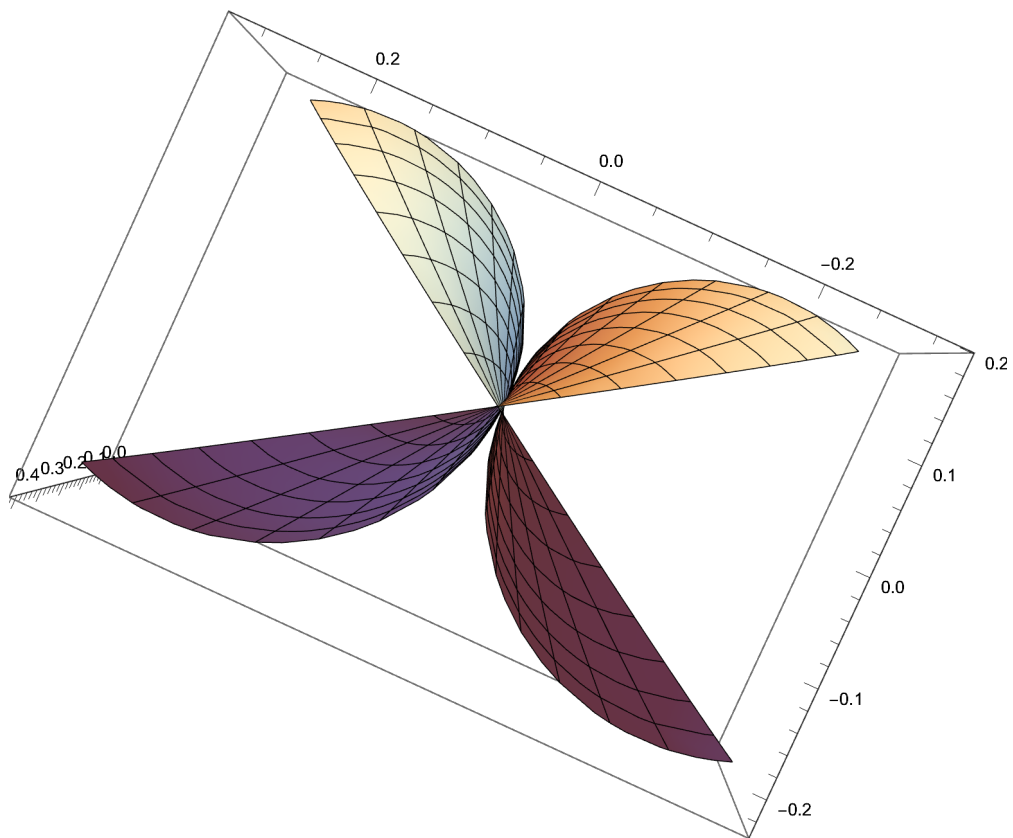
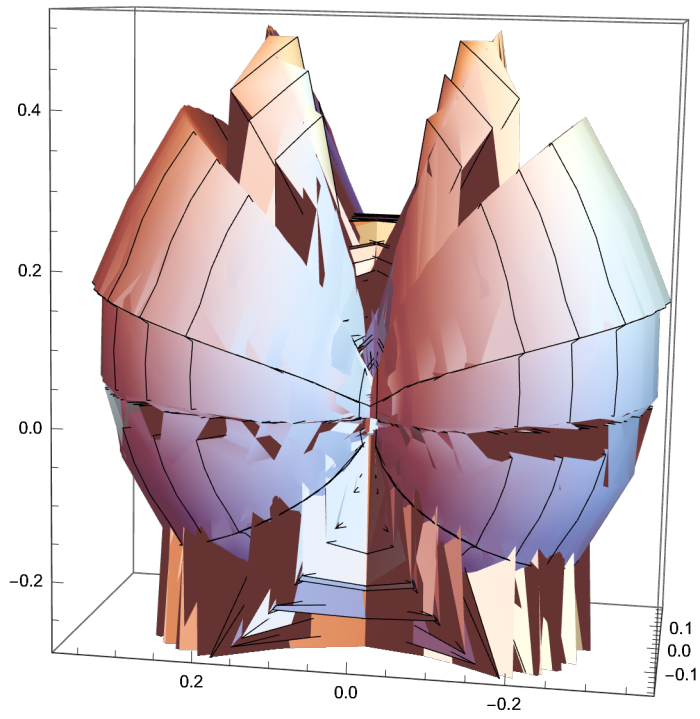
$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \text{Csc}[\beta]}{8\pi^2 \sqrt{\theta}} == r, \theta\right]$$

$$\left\{\left\{\theta \rightarrow -\frac{2\pi}{-1 + 4\pi^2 r \text{Sin}[\beta]}\right\}, \left\{\theta \rightarrow \frac{2\pi}{1 + 4\pi^2 r \text{Sin}[\beta]}\right\}\right\}$$

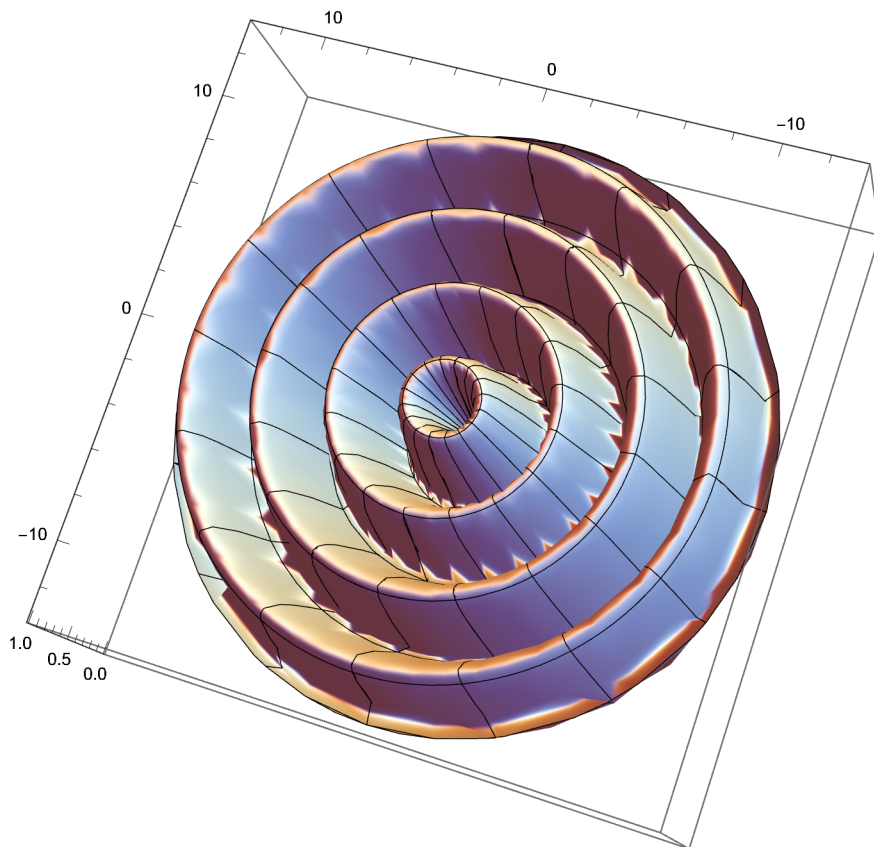
RevolutionPlot3D $\left[\frac{2 \pi}{1+4 \pi^2 r \sin[\beta]},\{r,-1,1\},\{\beta,-\pi,\pi\}\right]$



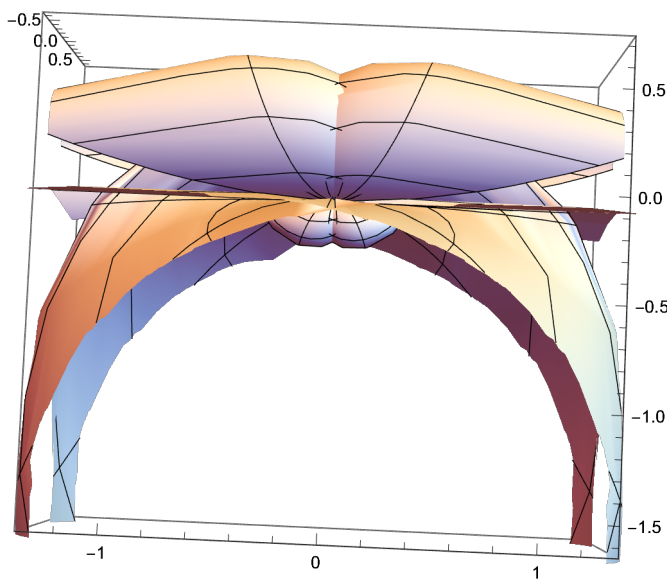
SphericalPlot3D $\left[\sqrt{4 \pi \left(\frac{2 \pi \left(\sqrt{1+\frac{4 \pi^2}{(4 \pi-\theta)^2}}-\frac{4 \pi}{4 \pi-\theta}\right) \sin[\beta]\right)^2}{\sqrt{4 \pi \theta-\theta^2}} \theta - \left(\frac{2 \pi \left(\frac{\sqrt{\frac{1-4 \pi^3}{4 \pi-\theta}}}{4 \pi \sqrt{\theta}}\right) \sin[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right)^2 \theta^2}, 2 \pi,\{\theta,-360,360\},\{\beta,-360,360\}\right]$



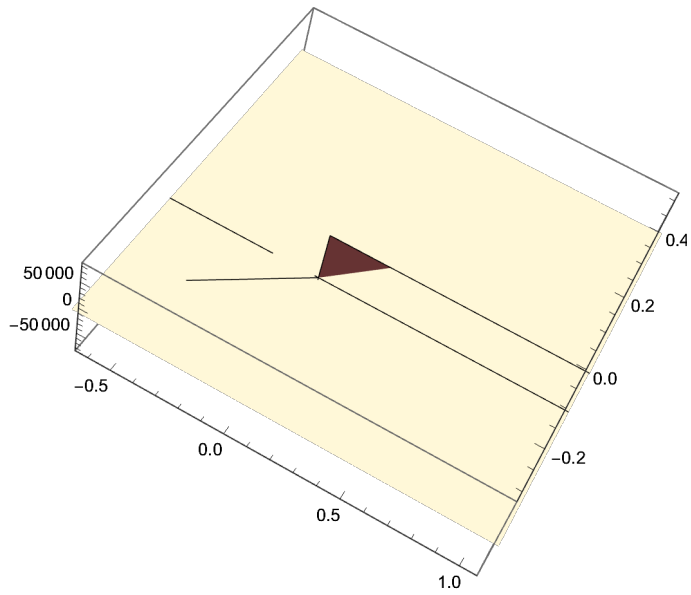




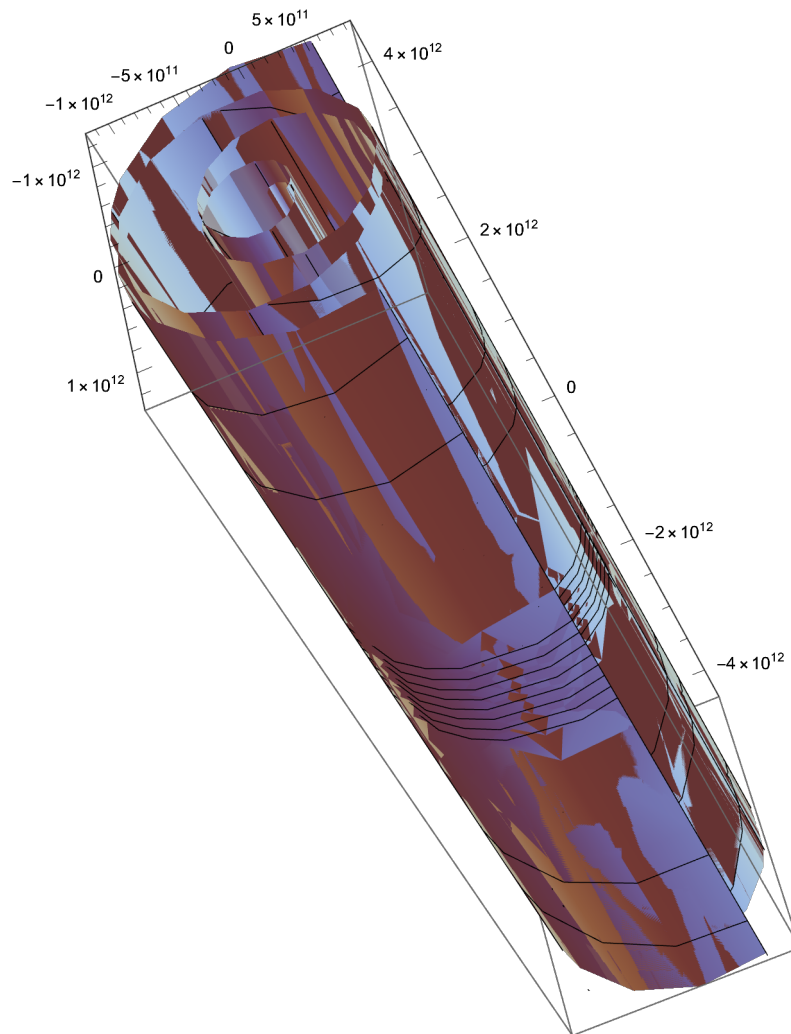
$$\text{SphericalPlot3D}\left[\frac{2 \pi \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$$



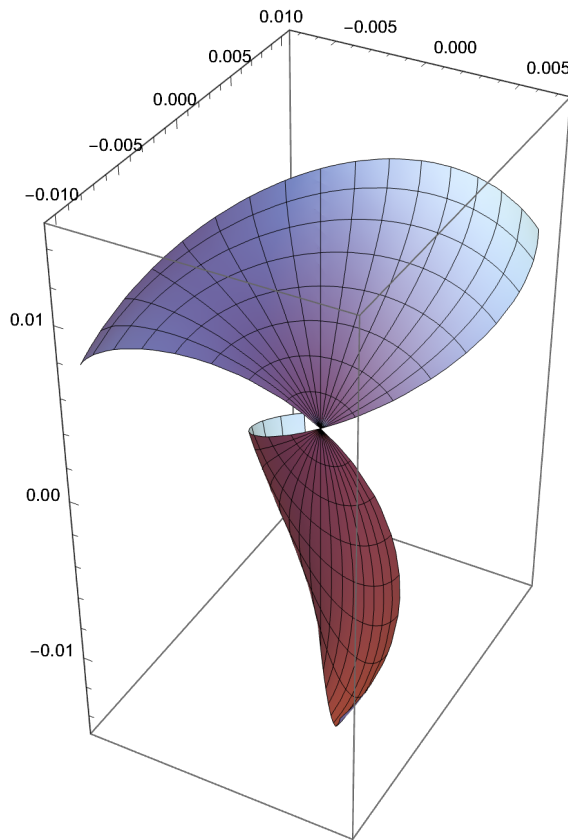
$\text{RevolutionPlot3D}\left[\frac{r(2\pi - \theta)}{2\pi\theta\sqrt{r^2(4\pi - \theta)\theta}}, \{r, -13, 13\}, \{\theta, -13, 13\}\right]$



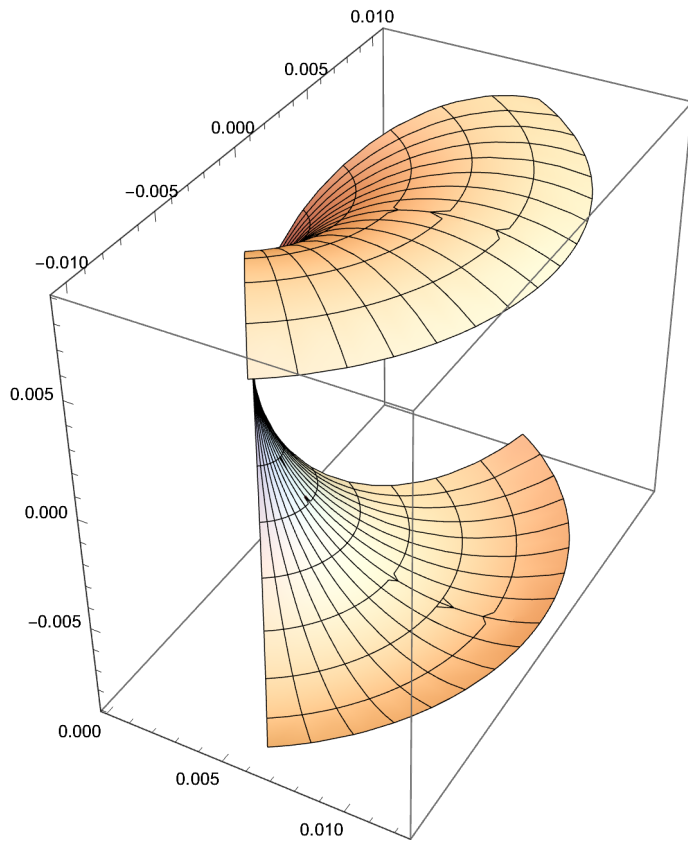
$\text{SphericalPlot3D}\left[\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta)} \, \theta \, \text{Csc}[\beta]}{\pi \sqrt{4 \pi - \theta}}, \{\beta, -13, 13\}, \{\theta, -13, 13\}\right]$



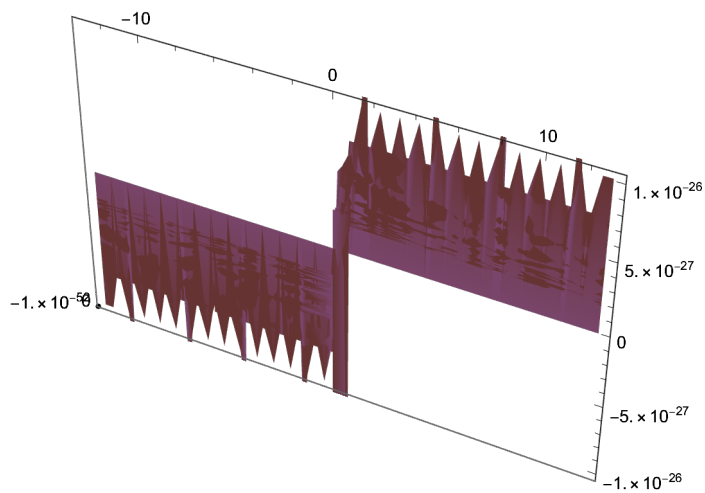
`SphericalPlot3D` $\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -1, 1\}, \{\beta, -1, 1\}\right]$

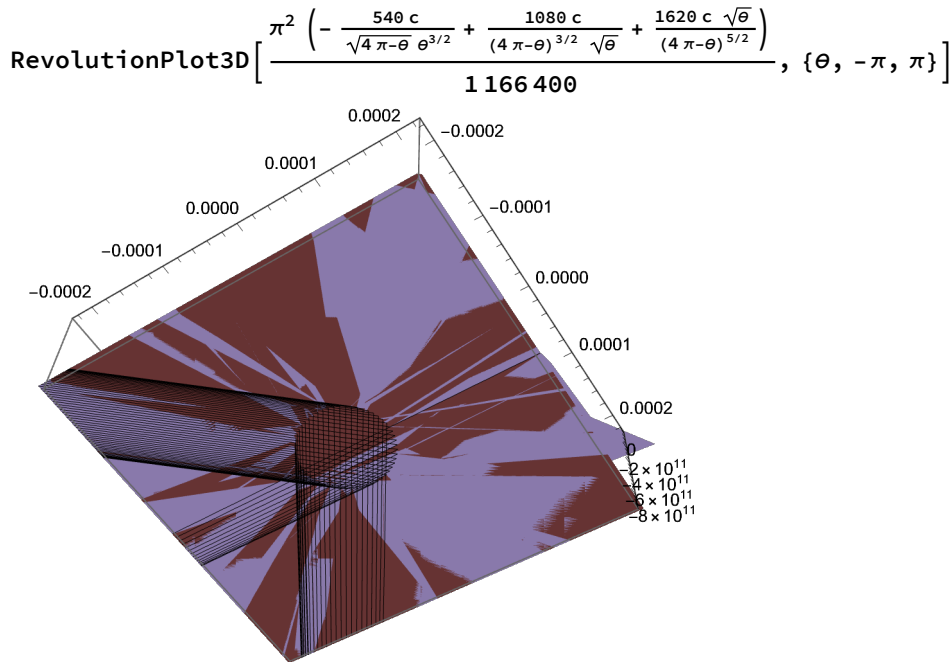


$\text{SphericalPlot3D}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\beta, -1, 1\}, \{\theta, -1, 1\}\right]$



$\text{RevolutionPlot3D}\left[2.144571844054625 \cdot 10^{-53} \theta \frac{r (2\pi - \theta)}{2\pi \theta \sqrt{r^2 (4\pi - \theta) \theta}}, \{r, -13, 13\}, \{\theta, -10^{-53}, 10^{-53}\}\right]$





We will also introduce the idea of a platform into which we can place different objects. These objects will interact with the platform, which is also another kind of object.

# A Notational Language for the Light-Sensitive Psychophysics

## I. Light through the Arc and Height

Light travels through space, but within its travel is the information that the angular element, akin to time, conveys specific information about the location of contour in perceptual space through a geometric correlation that has the capability of mapping out contour in the visual perception directly by analogy of larger ecology to individual play of ambient light off of a contour. This is an interpretation of spectral energy within Gibson's terminology of the false puzzle, "the amount of constancy obtained by an observer is pointless" (BRP 169), because the analogy is the conveyor of meaning to consciousness. We will try to show this symbolically as well as directly.

There is information available in the stimulation, but there is also information communicated. A change in the environment, when measuring size, is the polar coordinate expression of the ambient optic array. The change is undergoing, because of a parameter of structure that is invariant, so the disruption in the array specifies the event. That event causes transition and transformation. Physical

space uses mathematics to describe time in specifically a linear way. Psychophysical, or perceptual space is focused primarily on the event of perception, thus it uses a cyclic interpretation of the time element to the mathematical correlations.

$$\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \right\} \right\} \text{ is the height of a cone}$$

in terms of a difference of circumferences, invariant through  $r$ ,  
because it is always the slant of the cone and also the value that the  
base of the cone cannot reach, because once it reaches that value,  
it is no longer a cone, but collapses to a circle. (209)

$$\text{Solve} \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = \eta, r \right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} \right\} \right\} \quad (210)$$

$$\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}} = r = \frac{2\pi * r * \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} \quad (211)$$

Where  $\eta$  is a given height of a cone, and  $\theta$  the amount of accumulated time during transition,  $r*\theta$  is the difference of the change in circumference between two circles that correlates to a height in the third dimension.

$$\text{Note that whatever } r \text{ is equal to, the equation simplifies to } 1 = \frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} \quad (212)$$

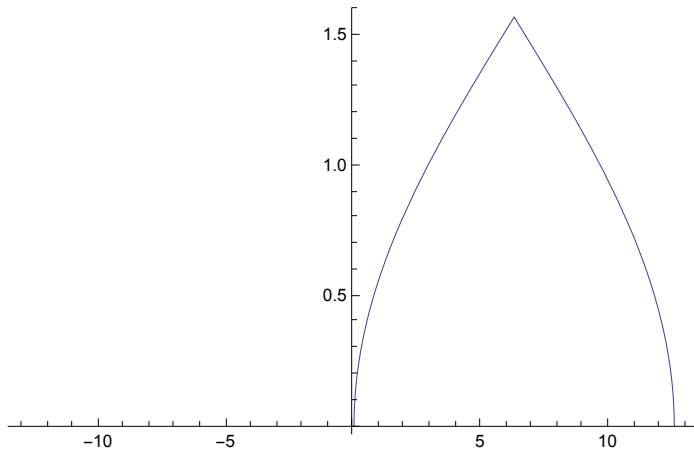
The polar graph of this function represents the change in  $\eta$  of a radius through time.

We can solve this equation for  $\beta$ , the angle made by the slant of the cone and the base of the cone, in terms of theta (the amount of angle involved in folding the circle up into the third dimension when the slant is always equal to the radius.

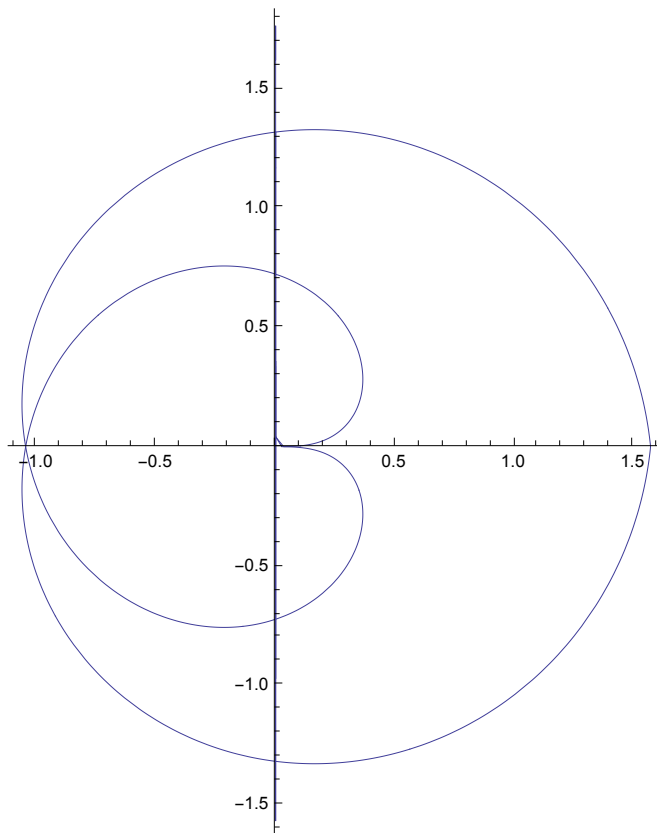
$$\text{Solve} \left[ 1 = \frac{2\pi \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \beta \right]$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right] \right\} \right\} \quad (213)$$

$\text{Plot}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], \{\theta, -13, 13\}\right]$

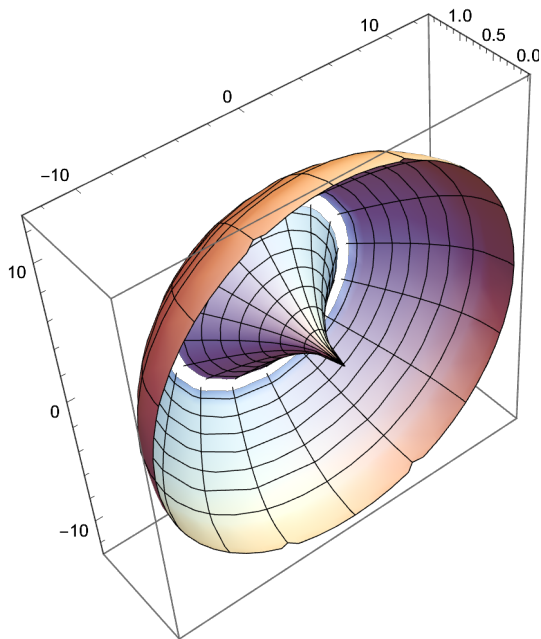


$\text{PolarPlot}\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], \{\theta, -13, 13\}\right]$





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RevolutionPlot3D[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ], { $\theta$ , -13, 13}]
```



Ian said, "We were chased through tunnels by five million dragons.

James replied, "We should kill all of them with a sword."

Parker thought,

"It is these two bricks of sugar called cookies that is meaning throughness."

The field of optical flow, light traveling through the ambient array, I propose, is represented by the polar coordinate graph of a change in radius of the base of a cone over time through transition to being the height of the cone. A revolution delivers information to the perceiver given the intensity, hue, etc. of light. A single revolution of the system is equivalent to the flow of combined light in the ambient array at the station point of perception or at a single, tiny piece of the array.

There are ways of solving for the radius in terms of purely the angle,  $\theta$ . We will examine these nested sets of ways of understanding the point of view. By nested, we mean that depending on how in depth one goes into observing the world or extrapolating a function of light in the array, one will see different visual representations of the structuring of that information that are more or less informationally dense.

This will lead to a series of functions that give us introspection into the structuring of light in terms of a cyclic perspective on time. For the system, it is important to realize that in the normal course of parameterizing the motion in the case at hand,  $\theta$  does not go beyond  $4\pi$  (i.e. that it sends the height of the cone up to its maximum value and back down over the course of two revolutions of a circle), and that  $\beta$  would not be able to be easily thought of beyond  $\pi$  or  $2\pi$  (it has a value of  $\pi$  at the maximum

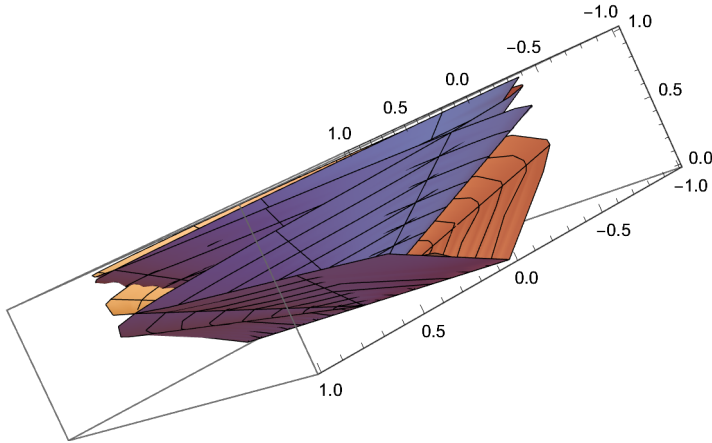
height of the transition, and a value of  $2\pi$  once the cone comes back down from the height).

$$\text{Solve}\left[1 == \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, \theta\right]$$

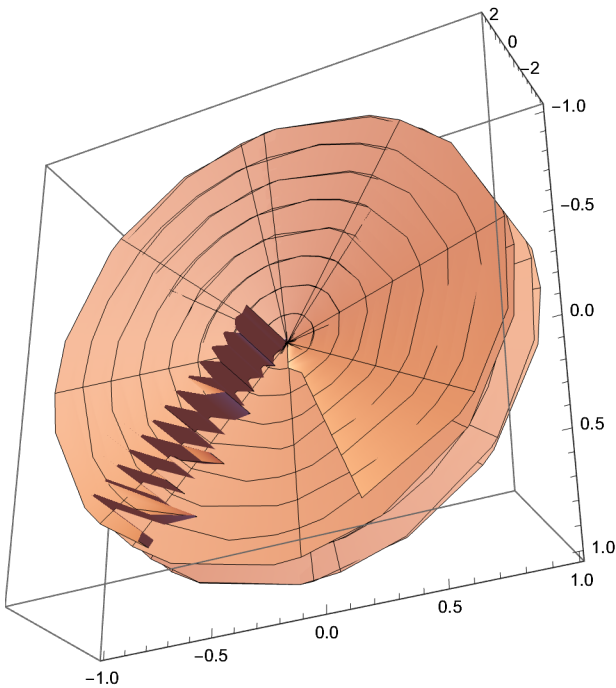
$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right\}\right\} \quad (214)$$

$$\eta \rightarrow \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}$$

$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$$



$$\text{RevolutionPlot3D}\left[\frac{2\pi\eta}{\sqrt{4\pi\theta - \theta^2}}, \{\eta, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$$



From this, we can visually see that each small piece of the ambient array contains within it a certain kind of contour that relates directly to the height and angle of the transition within that piece of contour and the growing ecological contour that maps out objects in the world for visual perception.

## The Analogy of a Change in Position Relating to a Change in Contour during the Pickup of Invariants

Gibson has said that, "The theory of information pickup requires perceptual systems, not senses" (BRP 77). Gibson also he subtlety of the perceptual system to learning and time. He thinks that we continue learning to perceive in more detail as time goes on. This will be an important idea when discussing the extrapolation of functions relating to the information in the array over time.

The wavelength of the light we are discussing is the initial radius of the circle. Its path is to the subjective perceiver and a single wavelength. The parameters of the velocity of its travel, or the travel of any substance, are frequency and wavelength.

We state that :  $v = \lambda f$ , where  $v$  is velocity,  
 $\lambda = r$  is wavelength, and  $1/\text{time} = f = \text{frequency}$ . (215)

$$\text{Time} = 6 \left( \theta_{\text{degrees}} \right) = 6 \left( 180 / \pi \right) \theta = (1080 / \pi) \theta \quad (216)$$

The velocity being discussed is the first derivative of the distance, which is the height of the cone,  $\eta$ . A tiny piece of the ambient array would contain within it information regarding information of the surface off of which the light flowing through the array is reflecting.  $H$  contains information about the time and initial distance of a wavelength of light.

Information of variable contour is transferred to the perceiver by the flux of information in ambient light through each point in the optic array, represented by item number four. The rate of this variance is analogous to velocity in a rotational system, like the structuring of light through space - time. This is what is meant by information in the light.

Helmholtz proposes that phenomena regarding the visual system can be described by the use of analogy when things begin to look paradoxical. He takes into consideration the psychic faculties and suggests that the processing of the environment and its perceptual phenomena may occur through an unconscious working of analogy in the mind. I find this to be interesting and agreeable. It provides a humanist account through the recognition of biological factors regarding perceptual systems.

## The Wavelength with Constant Value

$v =$

$$\lambda f = r \left( 1 / (1080 / \pi) \theta \right) = (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right] = \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

We will try to build up as many functions as possible without resorting to designating something to be having a velocity of light or non - light. It is simply a velocity for the time being. This way, we will

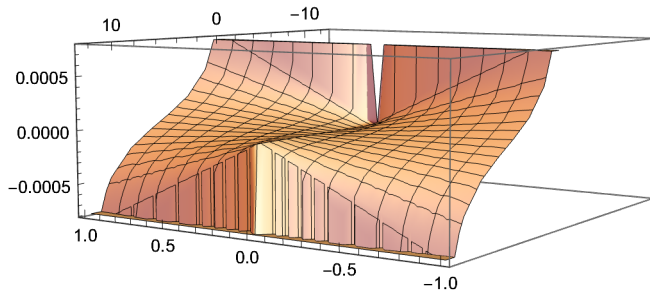
have access to a realm of general functions of correlated variables.

$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta \right]$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Velocity when } r \text{ is constant} = \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\text{Plot3D} \left[ \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \{r, -1, 1\}, \{\theta, -4 \pi, 4 \pi\} \right]$$



We also have access to the equation,

$$\frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = r (1 / (1080 / \pi) \theta), \quad (217)$$

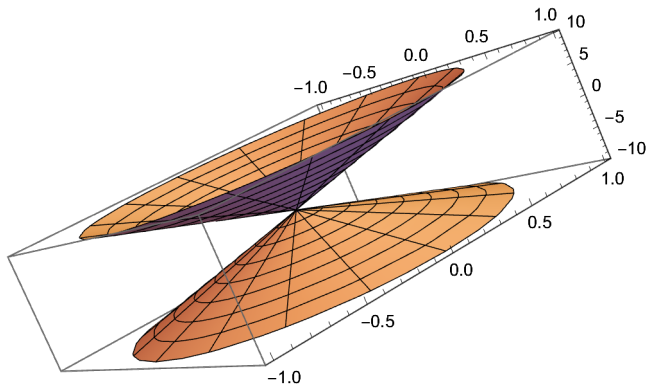
which winds up having the  $r$  variable cancel out,  
and delivers three exact solutions for theta.

$$\text{Solve} \left[ \frac{4 \pi r^2 - 2 r^2 \theta}{4320 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = r (1 / ((1080 / \pi) \theta)), \theta \right]$$

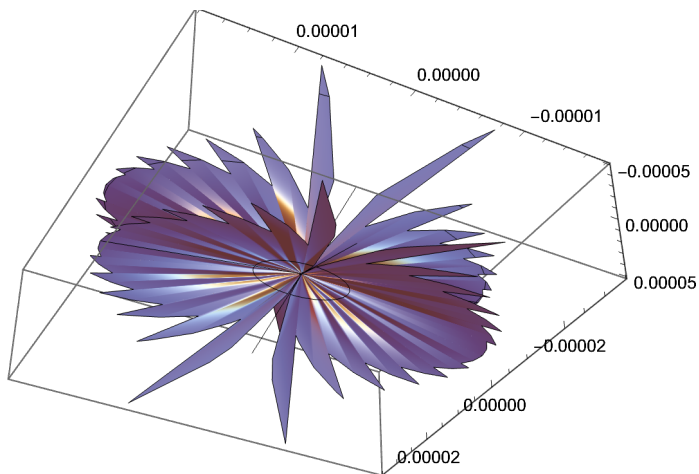
$$\left\{ \left\{ \theta \rightarrow \frac{2}{3} \left( 2 \pi - \frac{2 \pi}{(17 + 3 \sqrt{33})^{1/3}} + (17 + 3 \sqrt{33})^{1/3} \pi \right) \right\}, \right. \\ \left\{ \theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 + i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 - i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \right\}, \\ \left. \left\{ \theta \rightarrow \frac{4 \pi}{3} + \frac{2 (1 - i \sqrt{3}) \pi}{3 (17 + 3 \sqrt{33})^{1/3}} - \frac{1}{3} (1 + i \sqrt{3}) (17 + 3 \sqrt{33})^{1/3} \pi \right\} \right\} \quad (218)$$

We will note that an arc length is equal to  $r^* \theta$ . Thus, we will be able to see what the arc length is, because it represents the change in circumference of two circles. In this case, as the circle, viewed from head on, recedes from the perceiver into the distance, it gets smaller. This is a change in amount of surface area taken up on the retinal image, but also a way of visualizing the imaginary solutions the time element of waves traveling in space.

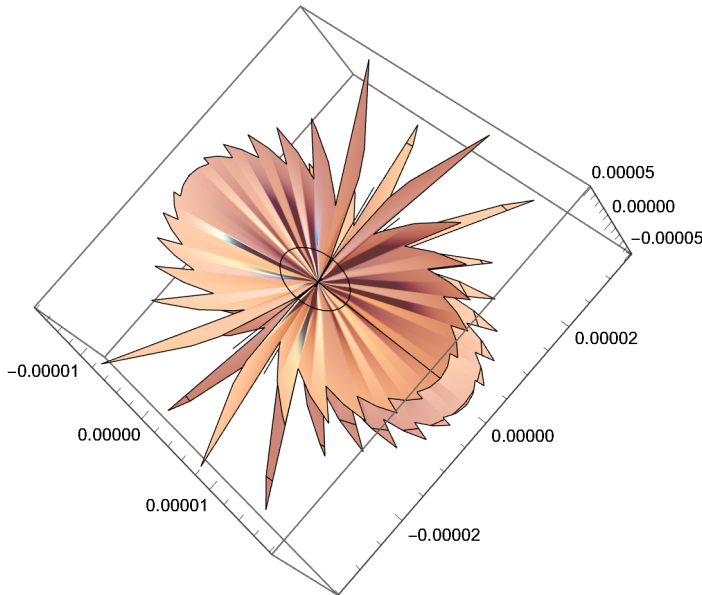
$$\text{RevolutionPlot3D}\left[r \frac{2}{3} \left( 2\pi - \frac{2\pi}{\left(17+3\sqrt{33}\right)^{1/3}} + \left(17+3\sqrt{33}\right)^{1/3} \pi \right), \{r, -1, 1\}\right]$$



$$\text{RevolutionPlot3D}\left[r \left( \frac{4\pi}{3} + \frac{2(1+i\sqrt{3})\pi}{3(17+3\sqrt{33})^{1/3}} - \frac{1}{3}(1-i\sqrt{3})(17+3\sqrt{33})^{1/3}\pi \right), \{r, -1, 1\}\right]$$



$$\text{RevolutionPlot3D}\left[r \left( \frac{4\pi}{3} + \frac{2(1 - i\sqrt{3})\pi}{3(17 + 3\sqrt{33})^{1/3}} - \frac{1}{3}(1 + i\sqrt{3})(17 + 3\sqrt{33})^{1/3}\pi \right), \{r, -1, 1\}\right]$$



When combined, the three imaginary solutions form a cone, but separately, they exist primarily in the complex plane. It requires all three solutions to deliver information of depth to the perceiver through light in terms of the real. In Gibson's theory, depth is intimately connected with contour. Contour is delivered by the pickup of the invariant,  $r$ , in the ambient array, changing context in a different way from point to point. Thus, understanding of two truths in the real world like information given to the perceiver of an object by an edge, for instance is enabled.

Mach begins by verifying a belief in the space - sense, an area of parameterized space relating the sense of an individual to the stimulus in the world. The space - sense provides a workspace for the individual senses like sense of sight and touch to enable a perceptual experience. "The perception of Depth depends on extra - ocular experiences" (BRP 118) is an idea that makes a great deal of sense to me, because when we experience or perceive truth, we use multiple faculties to make sense of a phenomenon.

## The Wavelength with Changing Value during a Transition

The initial radius changes contexts, but can it be said to actually change? The wavelength,  $r$ , could be said to be changing if we consider that  $\Delta r =$

$r - r_1$ . Although it is invariant in the context of always being the slant of the cone, it changes when understood to be the base of a cone. The height of the cone starts at zero and goes toward the locus of perception, which is the subjective perceiver. In the ambient array, many different wavelengths are present. It is reasonable, then to think that a wavelength could change during the course of traveling a single wavelength. When the circle is infinitely far away, it has a perceived radius of 0. It is important to discuss the ecological context of the meaning of the array. The initial radius could be thought of being analogous to the monocular field of vision.

$$v = \lambda f = r (1 / (1080 / \pi) \theta) = (1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta \right] \quad (219)$$

$$(1 / (1080 / \pi)) D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r, \theta \right]$$

$$\frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} = \text{velocity during a transition} \quad (219)$$

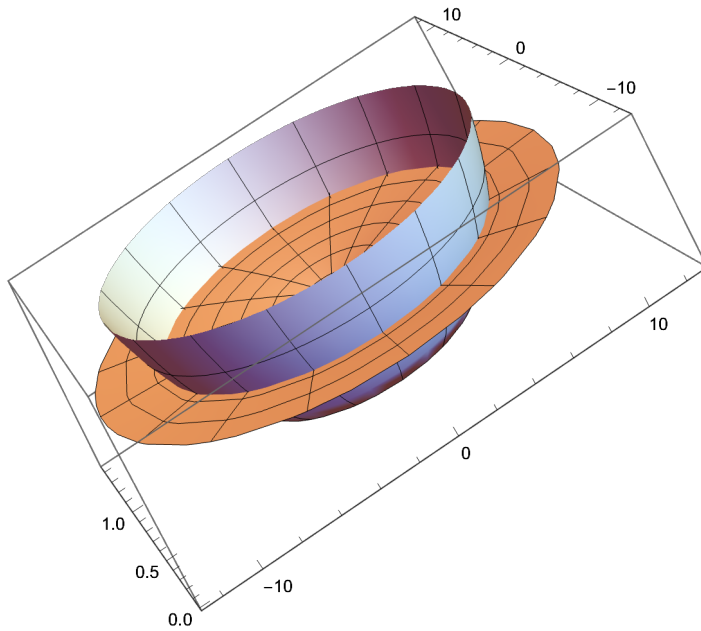
$$(1080 / \pi) \theta = \text{time} \quad (220)$$

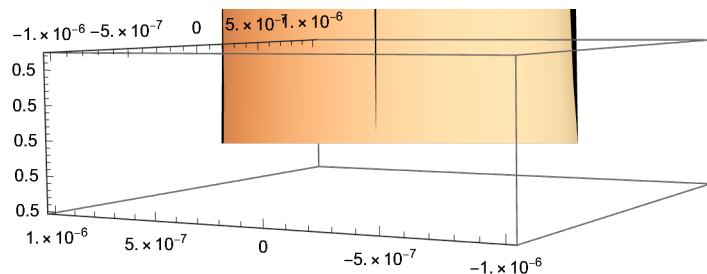
$$\frac{2 \pi v t}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi v (1080 / \pi) \theta}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 \pi \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} (1080 / \pi) \theta}{\sqrt{4 \pi \theta - \theta^2}} \quad (221)$$

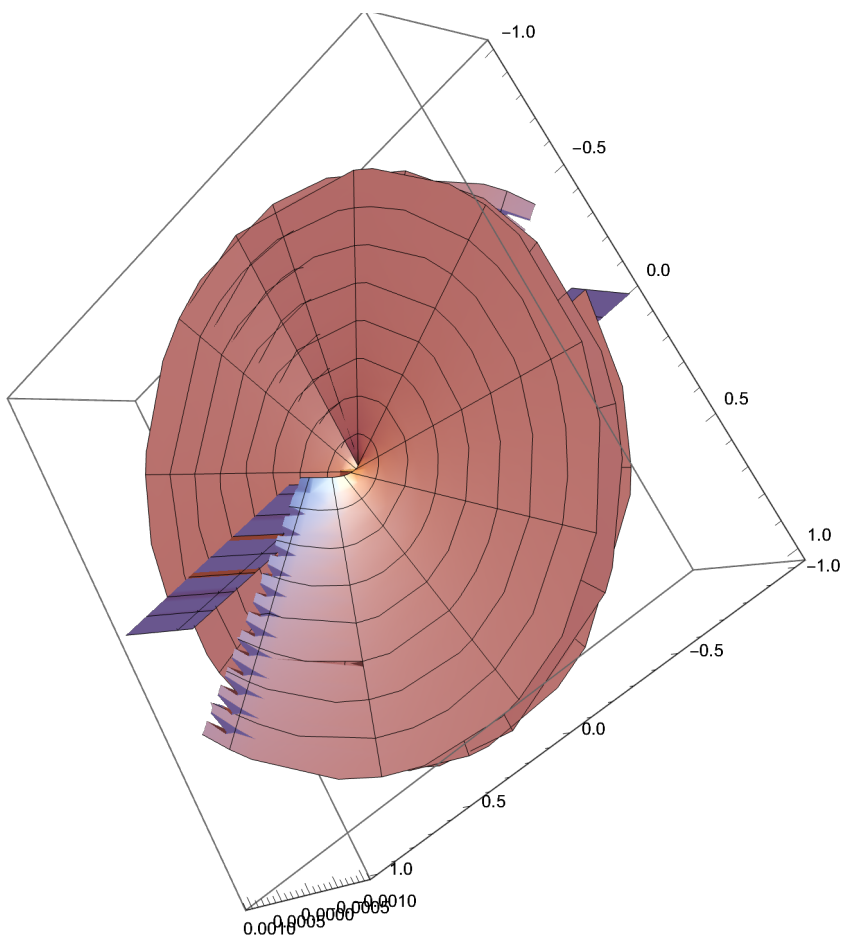
$$\text{Solve} \left[ r == \frac{2 * \left( \frac{\pi \left( -\frac{(4 \pi r^2 - 2 r^2 \theta) (8 \pi r \theta - 2 r \theta^2)}{8 \pi (4 \pi r^2 \theta - r^2 \theta^2)^{3/2}} + \frac{8 \pi r - 4 r \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right)}{1080} \right) * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, r \right]$$

$$\left\{ \left\{ r \rightarrow -\sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right\} \right\}$$

$$\text{RevolutionPlot3D} \left[ \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}, \{\theta, -4 \pi, 4 \pi\} \right]$$



$$\text{RevolutionPlot3D}\left[\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}, \{\theta, -.000001, .000001\}\right]$$


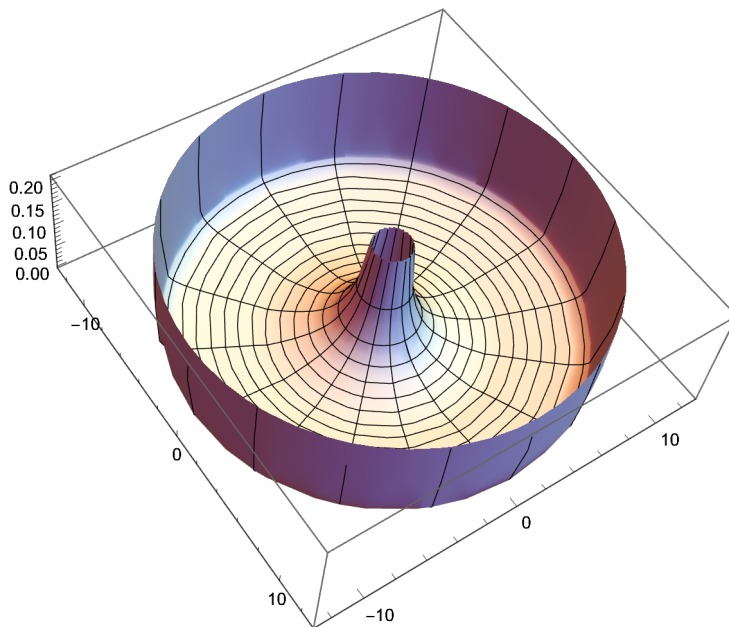
$$\text{RevolutionPlot3D}\left[\frac{\pi \left( -\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right)}{1080}, \{r, -1, 1\}, \{\theta, -3\pi, 3\pi\}\right]$$


$$\text{Solve}\left[\frac{\pi \left( -\frac{(4\pi r^2 - 2r^2\theta)(8\pi r\theta - 2r\theta^2)}{8\pi(4\pi r^2\theta - r^2\theta^2)^{3/2}} + \frac{8\pi r - 4r\theta}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}} \right)}{1080} == r(1 / (1080 / \pi) \theta), r\right]$$

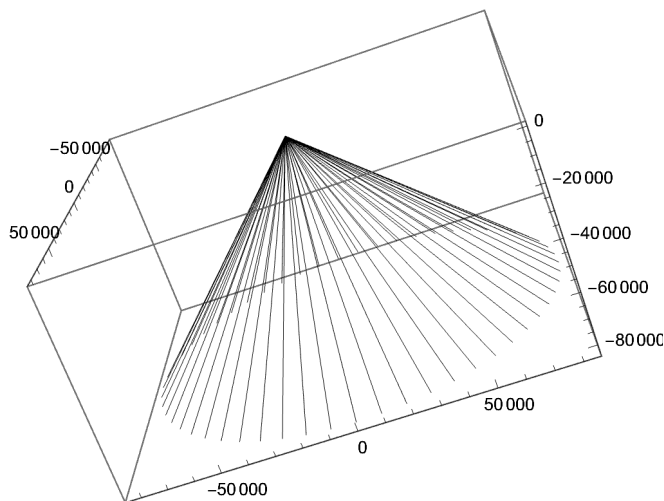
$$\left\{ \left\{ r \rightarrow -\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\}, \left\{ r \rightarrow \frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right\} \right\}$$



`RevolutionPlot3D` $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, \{\theta, -13, 13\}\right]$



`RevolutionPlot3D` $\left[\left\{\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, -\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right\}, \{\theta, -13, 13\}\right]$



This shows us that the parametric structure of our system still holds when the consideration that the wavelength of light,  $r$ , changes during transition. This leads to some evidence for Gibson's idea of an invariant in the structure of light.

$$\text{Solve}\left[\frac{\pi\left(-\frac{(4\pi r^2-2r^2\theta)(8\pi r\theta-2r\theta^2)}{8\pi(4\pi r^2\theta-r^2\theta^2)^{3/2}}+\frac{8\pi r-4r\theta}{4\pi\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)}{1080}==r(1/(1080/\pi)\theta),\theta\right]$$

RevolutionPlot3D[

$$\left\{\left\{\pi-\frac{1}{2}\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}-\frac{1}{2}\sqrt{\left(8\pi^2-\frac{1}{3\pi^2r^2}-\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}-\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}-\left(64\pi^3+\frac{4}{\pi r^2}\right)/\left(4\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}\right)}\right\}\right\},$$

$$\left\{\pi-\frac{1}{2}\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}+\frac{1}{2}\sqrt{\left(8\pi^2-\frac{1}{3\pi^2r^2}-\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}-\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}-\left(64\pi^3+\frac{4}{\pi r^2}\right)/\left(4\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}\right)}\right\},$$

$$\left\{\pi-\frac{1}{2}\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}+\frac{1}{2}\sqrt{\left(8\pi^2-\frac{1}{3\pi^2r^2}-\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}-\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}-\left(64\pi^3+\frac{4}{\pi r^2}\right)/\left(4\sqrt{\left(4\pi^2-\frac{1}{6\pi^2r^2}+\frac{1}{12\pi^2r^2\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}+\frac{\left(1+13824\pi^8r^4-96\sqrt{3}\pi^4\sqrt{r^4+6912\pi^8r^8}\right)^{1/3}}{12\pi^2r^2}\right)}\right)}\right\},$$

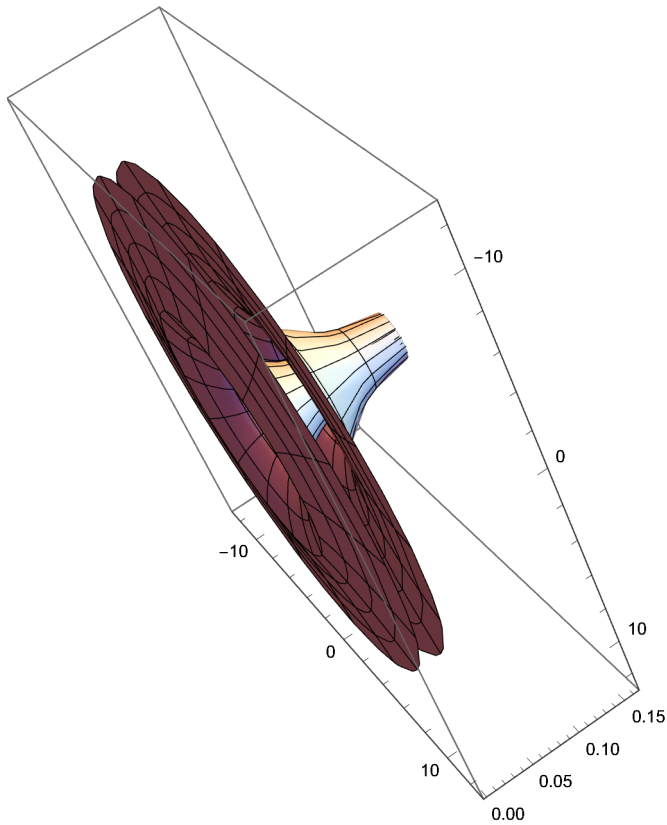
$$\begin{aligned}
 & \left. \left. \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right\}, \\
 & \left\{ \pi + \frac{1}{2} \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \right. \right. \\
 & \quad \left. \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) - \right. \\
 & \quad \frac{1}{2} \sqrt{\left(8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} - \right. \\
 & \quad \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} + \left(64 \pi^3 + \frac{4}{\pi r^2}\right) / \right. \\
 & \quad \left. \left(4 \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \right. \right. \right. \\
 & \quad \left. \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) \right) \right\}, \\
 & \left\{ \pi + \frac{1}{2} \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \right. \right. \\
 & \quad \left. \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) + \right. \\
 & \quad \frac{1}{2} \sqrt{\left(8 \pi^2 - \frac{1}{3 \pi^2 r^2} - \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} - \right. \\
 & \quad \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} + \left(64 \pi^3 + \frac{4}{\pi r^2}\right) / \right. \\
 & \quad \left. \left(4 \sqrt{\left(4 \pi^2 - \frac{1}{6 \pi^2 r^2} + \frac{1}{12 \pi^2 r^2 \left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}} + \right. \right. \right. \\
 & \quad \left. \left. \frac{\left(1 + 13824 \pi^8 r^4 - 96 \sqrt{3} \pi^4 \sqrt{r^4 + 6912 \pi^8 r^8}\right)^{1/3}}{12 \pi^2 r^2} \right) \right) + \right.
 \end{aligned}$$



$$\text{Solve}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}, \theta\right]$$

$$\{\{\theta \rightarrow 2\pi\}\}$$

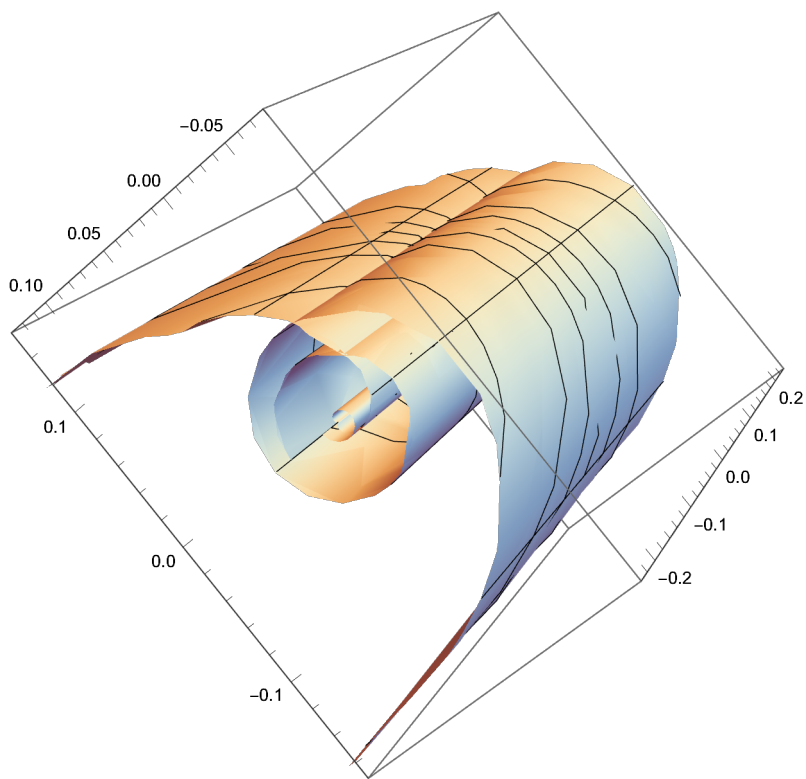
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}, \{\theta, -4\pi, 4\pi\}\right]$$



$$\text{Solve}\left[\frac{2\pi * r * \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} == \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}, r\right]$$

$$\left\{\left\{r \rightarrow \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \text{Csc}[\beta]}{8\pi^2\sqrt{\theta}}\right\}\right\}$$

SphericalPlot3D $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}}, \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\}\right]$



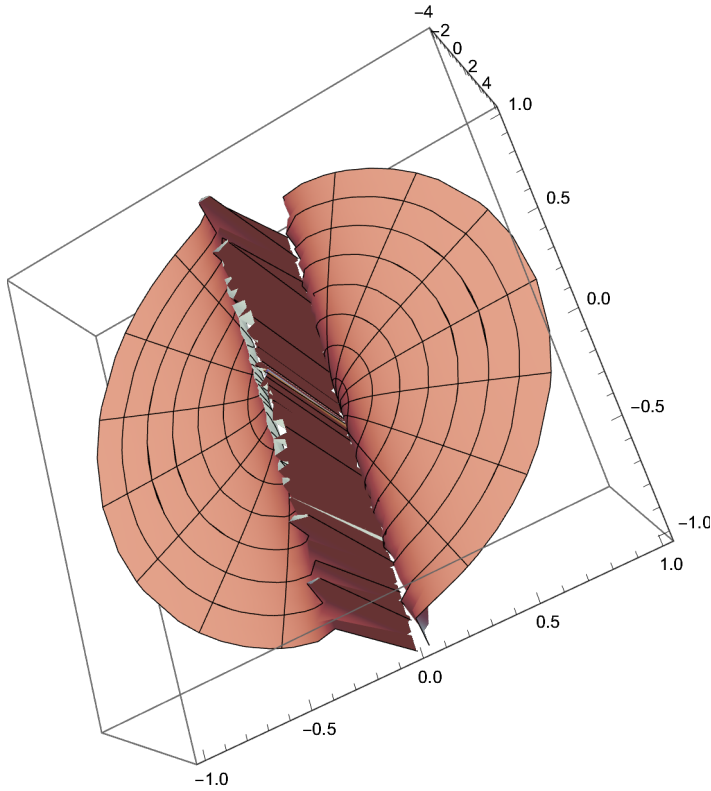
Solve $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}} == r, \beta\right]$

$\left\{\left\{\beta \rightarrow \operatorname{ArcCsc}\left[\frac{4\pi^2 r \sqrt{\frac{(2\pi-\theta)^2}{(4\pi-\theta)\theta^2}} \theta^{3/2} \sqrt{(4\pi-\theta)\theta}}{4\pi^2 - 4\pi\theta + \theta^2}\right]\right\}\right\}$

Solve $\left[\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}} == r, \theta\right]$

$\left\{\left\{\theta \rightarrow -\frac{2\pi}{-1 + 4\pi^2 r \operatorname{Sin}[\beta]}\right\}, \left\{\theta \rightarrow \frac{2\pi}{1 + 4\pi^2 r \operatorname{Sin}[\beta]}\right\}\right\}$

RevolutionPlot3D $\left[\frac{2 \pi}{1 + 4 \pi^2 r \sin[\beta]}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$



## II. Spectral Sensitivity

The analogy of a change in position relating to a change in contour

$$\eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} = r \sin[\beta]$$

$$r = \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} = \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4 \pi \theta - \theta^2} \operatorname{Csc}[\beta]}{8 \pi^2 \sqrt{\theta}} = \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}$$

Boynton proposes that there is a, "scotopic spectral sensitivity curve, appropriate to the threshold of the dark adapted eye outside the voeal region" (Psychophysics of Vision, 15). Boynton submits that the stimulus, "must be imaged in a part of the retina containing a high density of rod photoreceptors" (Psychophysics of Vision, 15).

Using induction, we can develop a series of true statements for  $r$ , so long as  $n$  is an integer.  $n$  would be a certain number of  $r$ , and  $r$  would always be a base unit of measure. Thus, we can say that:

$c := \text{speed of light} := (2.99792458 * 10^8) \text{ m / s}$

$c := (2.99792458 * 10^8)$

First, we will use the following conversion

$$\eta := \text{rate} * \text{time} = c * \tau = \text{height of cone} \quad (222)$$

$$\tau := 6 \left( \theta_{\text{degrees}} \right) = 6 \left( (180 / \pi) \theta \right), \text{ because if theta were in radians to begin with,}$$

we would have to convert that number of radians to degrees. This way,

both our thetas are in radians,

but our result accounts for the constant of the degrees involved in measuring time.

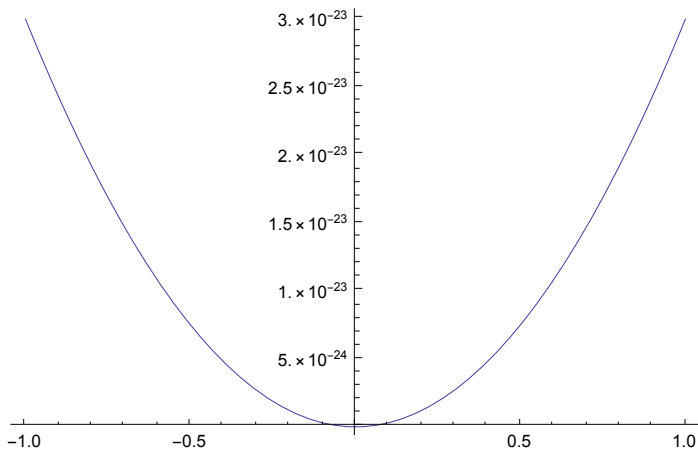
$$(180 / \pi)$$

$$r = \frac{2 * c * \tau * \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 * c * 6 \left( (180 / \pi) \theta \right) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}$$

$$\text{Solve}\left[r == \frac{2 * c * 6 \left( (180 / \pi) \theta \right) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{4 \pi r^2}{4665600 c^2 + r^2} \right\} \right\}$$

$$\text{Plot}\left[\frac{4 \pi r^2}{4665600 c^2 + r^2}, \{r, -1, 1\}\right]$$



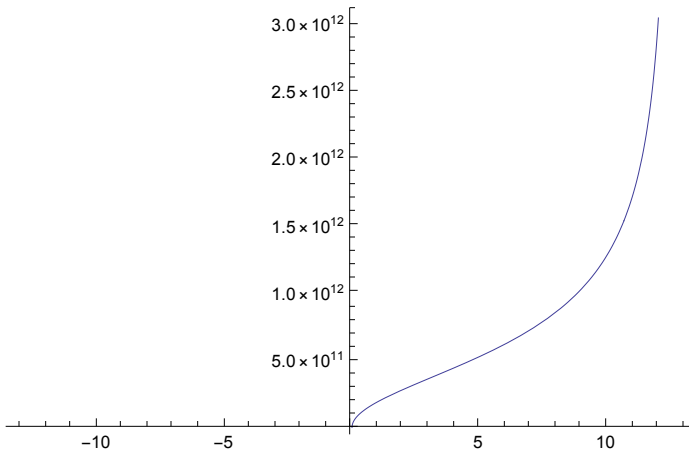
We zoom in

$$\text{Solve}\left[\theta == \frac{4 \pi r^2}{4665600 c^2 + r^2}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right\}, \left\{ r \rightarrow \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right\} \right\}$$

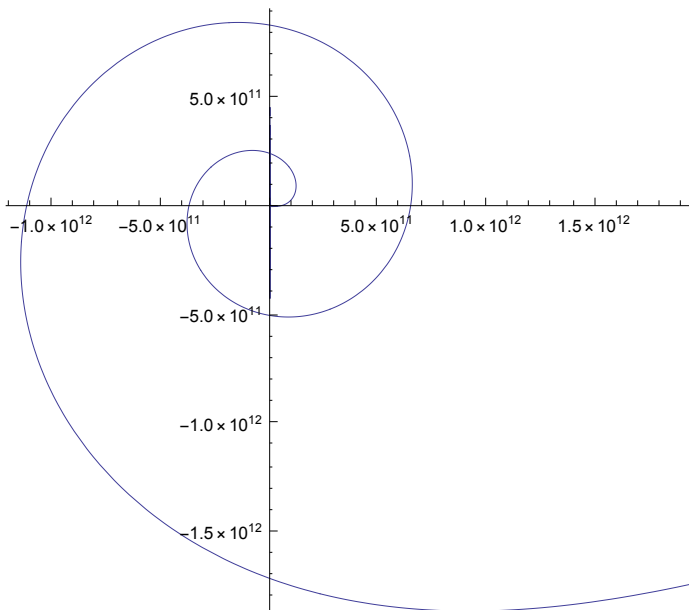


$$\text{Plot}\left[\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}, \{\theta, -13, 13\}\right]$$



If the quantum of light can be parameterized by its traveling up the height of the cone through time, we can say that the radius of the distance a wavelength of light travels expands to infinity over the course of two rotations, or  $4\pi$  radians. The measurement

$$\text{PolarPlot}\left[\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}, \{\theta, -13, 13\}\right]$$



This is what the motion would look like in polar coordinates.

$$r := \frac{2\pi\eta}{\sqrt{4\pi-\theta^2}}; \eta = r \sin[\theta]$$

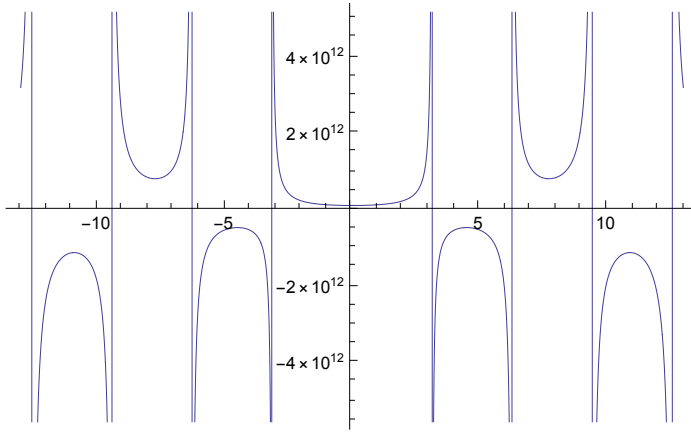
$$\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}} = \frac{2\pi\eta}{\sqrt{4\pi-\theta^2}} = \frac{2\pi r \sin[\theta]}{\sqrt{4\pi-\theta^2}}$$

$$\text{Solve}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} == \frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}, r\right]$$

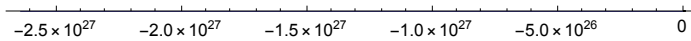
$$\left\{\left\{r \rightarrow \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right\}\right\}$$

It looks as though by setting up different true statements about what  $r$  is, we can get several different perspectives of what it does in terms of time. This suggests that there are multiple valid ways of perceiving a given change in perceptual space. These equations are meant to accurately represent the subjective experience of making a discernment in measuring some change in contour or size out in the world. In this sense, the meaning of that change in contour is already in the world, just like information.

$$\text{Plot}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$$r = \frac{2 * c * \tau * \pi}{\sqrt{4 \pi (\theta) - (\theta)^2}} = \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} = \text{wavelength of light} = \lambda \quad (223)$$

$$\text{velocity} = \lambda v, \text{ where } v = \text{number of mols of frequency} = n * f \quad (224)$$

$$f = 1 / (6 * (180 / \pi) \theta) = 1 / \tau \quad (225)$$

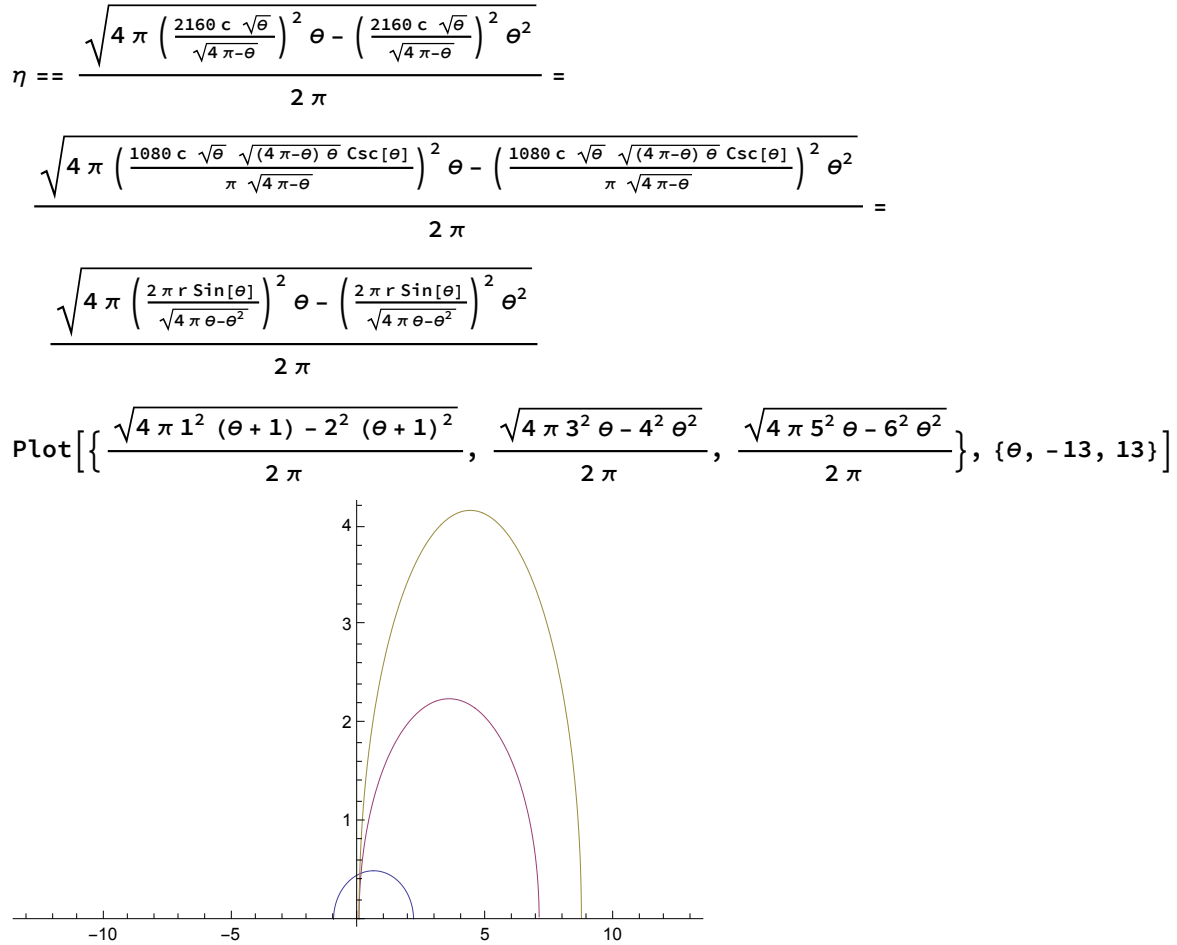
Velocity = speed of light

$$\text{Solve}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} n (1 / (6 (\theta))) == c, n\right]$$

$$\left\{\left\{n \rightarrow \frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}\right\}\right\} \quad (226)$$

$r^2 = 1 + 3 + 5 \dots (2n - 1)$ , where  $n$  is the position in the series.

We will now plot this equation to resemble something similar to Figure 2 on Page 16 of Contemporary Theory and Research of Visual Perception edited by Haber.



In Boynton's experiment, a method of sensory scaling was applied to the visual system, and yielded results that tell us the relative sensitivity (Radiance Basis) - Percent.

$$\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left( \frac{r \sqrt{4\pi \theta - \theta^2}}{8\pi^2 \sqrt{\theta}} \right)^2},$$

$$\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}}$$

$$\left\{ \left\{ \beta \rightarrow \operatorname{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta) \theta}}{2\pi} \right] \right\} \right\} \quad (227)$$

$$\frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\beta]}{\pi \sqrt{4\pi - \theta}}$$

$$\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\beta]}{180 \sqrt{(4\pi - \theta) \theta}}$$

$$\frac{r (2\pi - \theta)}{2\pi \theta \sqrt{r^2 (4\pi - \theta) \theta}}$$

$$\text{Plot3D}\left[\left\{\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta) \theta}}{2\pi}\right]\right]}{180 \sqrt{(4\pi - \theta) \theta}},\right.\right.$$

$$\left.\sqrt{r^2 - \left(\frac{r \sqrt{4\pi - \theta} \sqrt{\theta}}{8\pi^2 \sqrt{\theta}}\right)^2}, \sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{r \sqrt{4\pi - \theta} \sqrt{\theta}}{8\pi^2 \sqrt{\theta}}\right)^2},\right.$$

$$\left.\left(\pi + \frac{1}{2} \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 (1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}} + \frac{(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}}{12\pi^2 r^2}\right)}\right) +\right.$$

$$\left.\frac{1}{2} \sqrt{\left(8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 (1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}} - \frac{(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}}{12\pi^2 r^2} + \left(64\pi^3 + \frac{4}{\pi r^2}\right)\right)}\right/$$

$$\left.\left(4 \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 (1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}} + \frac{(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}}{12\pi^2 r^2}\right)}\right)\right)\right),$$

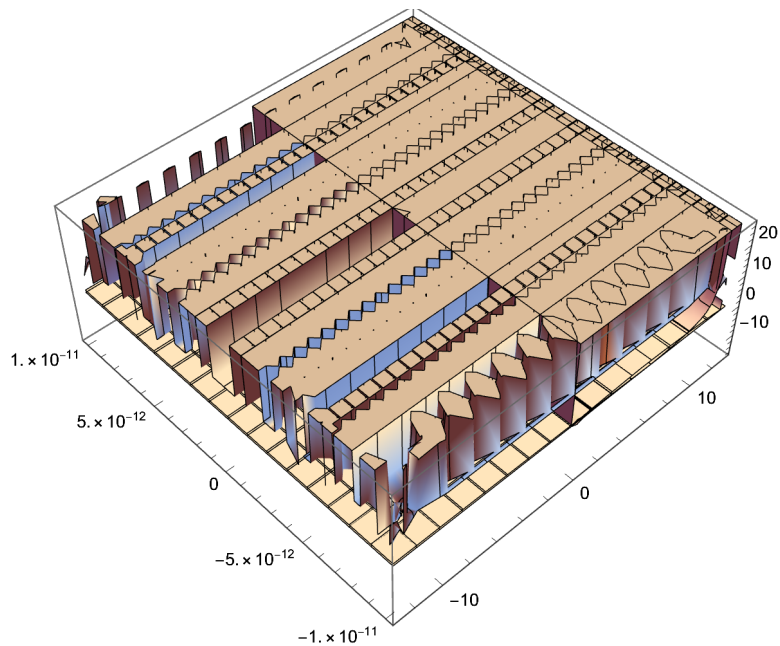
$$\frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \csc\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta) \theta}}{2\pi}\right]\right]}{\pi \sqrt{4\pi - \theta}}, \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta) \theta}}{2\pi}\right],$$

$$\frac{r (2\pi - \theta)}{2\pi \theta \sqrt{r^2 (4\pi - \theta) \theta}},$$

$$\sqrt{r^2 - \left(\frac{\sqrt{\frac{1}{4\pi - \theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi - \theta} \sqrt{\theta}}{8\pi^2 \sqrt{\theta}}\right)^2},$$

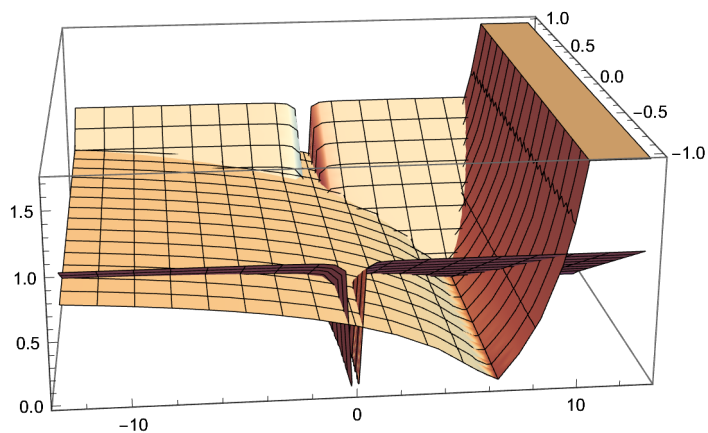
$$\sqrt{\left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}}\right)^2 - \left(\frac{r\sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}\right)^2},$$

{ $\theta$ , -13, 13}, { $r$ , -.000000000001,  
.000000000001}]

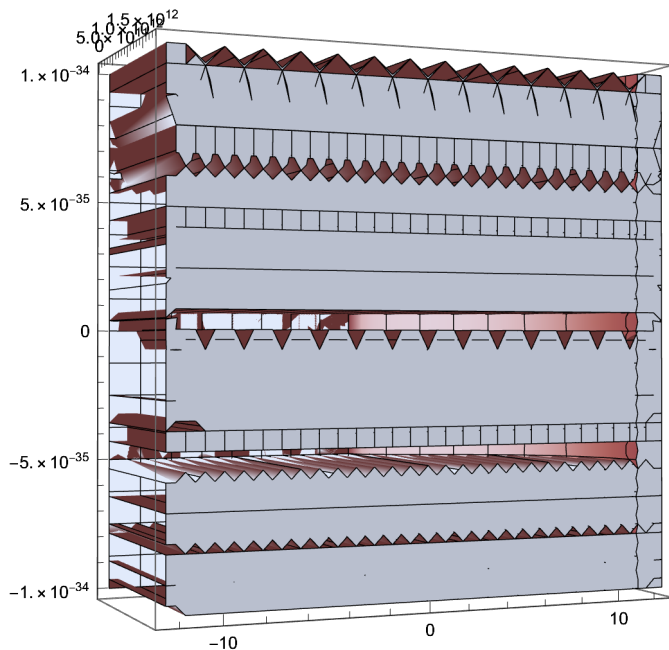


$$\text{Plot3D}\left[\left\{\sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta} - \left(\frac{r\sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}},\right.\right.$$

$$\left.\sqrt{(r)^2 - \left(\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}\sqrt{4\pi\theta - \theta^2}}{8\pi^2\sqrt{\theta}}\right)^2}\right\}, \{\theta, -13, 13\}, \{r, -1, 1\}]$$



$$\begin{aligned}
& \text{Plot3D}\left[\left\{\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]}{180 \sqrt{(4\pi - \theta)\theta}}, \right. \right. \\
& \quad \sqrt{r^2 - \left(\frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \sqrt{\sqrt{1 + \frac{4\pi^2}{(4\pi - \theta)^2} - \frac{4\pi}{4\pi - \theta}} - \left(\frac{r \sqrt{4\pi\theta - \theta^2}}{8\pi^2 \sqrt{\theta}}\right)^2}, \\
& \quad \left(\pi + \frac{1}{2} \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 (1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}}{12\pi^2 r^2}\right)} + \right. \\
& \quad \frac{1}{2} \sqrt{\left(8\pi^2 - \frac{1}{3\pi^2 r^2} - \frac{1}{12\pi^2 r^2 (1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}} - \right.} \\
& \quad \left. \frac{(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}}{12\pi^2 r^2} + \left(64\pi^3 + \frac{4}{\pi r^2}\right) / \right. \\
& \quad \left. \left(4 \sqrt{\left(4\pi^2 - \frac{1}{6\pi^2 r^2} + \frac{1}{12\pi^2 r^2 (1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{(1 + 13824\pi^8 r^4 + 96\sqrt{3}\pi^4 \sqrt{r^4 + 6912\pi^8 r^8})^{1/3}}{12\pi^2 r^2}\right)}\right)\right)\right), \\
& \quad \left.\frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \csc\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]}{\pi \sqrt{4\pi - \theta}}\right\}, \{\theta, -4\pi, \\
& \quad 4\pi\}, \{r, \\
& \quad -10^{\wedge} - 34, \\
& \quad 10^{\wedge} - 34\}
\end{aligned}$$



$$\frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}} \sqrt{4\pi\theta - \theta^2} \operatorname{Csc}[\beta]}{8\pi^2 \sqrt{\theta}}$$

# The Mathematics of the 8 Fold Path

## $\infty \pi \mathbb{C} g h m t \theta$

by Parker Emerson

$$m \rightarrow \frac{2.2086893333333334 \cdot 10^{-42}}{r} = \frac{(\theta \cdot 10^{-56} + 5.468107888071038 \cdot 10^{-56} i) \sqrt{-1.60287714 \cdot 10^{-8} + 1.2755291 \cdot 10^{-7} \theta}}{\sqrt{\theta}}$$

This function of mass comes from the parameters of light traveling from a circle into a cone, thus the change in radius can be integrated. When a circle folds into a cone, it doesn't have to go all the way around the cone in order to reach the height. For the above equation, we used the S.I. substitution of  $\theta = \text{time}$ , where theta is the distance in angle through which the initial radius of the circle translates into a height for a cone. The parameters of the cone do not include that it is necessary to go all the way around the circle. We will see into the wave nature of light more closely and make the observation of the diagonal wave shape of the asymptotic functions of wisdom (i.e. the first two roots).

$$\text{Solve}\left[m == \frac{2.2086893333333334 \cdot 10^{-42}}{r}, r\right]$$

$$\left\{\left\{r \rightarrow \frac{2.20869 \times 10^{-42}}{m}\right\}\right\}$$

This is the equation for radius in terms of the mass of light.

$$\left\{\left\{v \rightarrow \frac{0.02652582384864922 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{\theta}\right\}\right\}$$

This frequency comes from :

$$r = \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} = \lambda$$

$$c = \lambda f$$

(See the Geometric Patterns of Perception Series for more in depth solutions (explanations, system of variables and postulates))

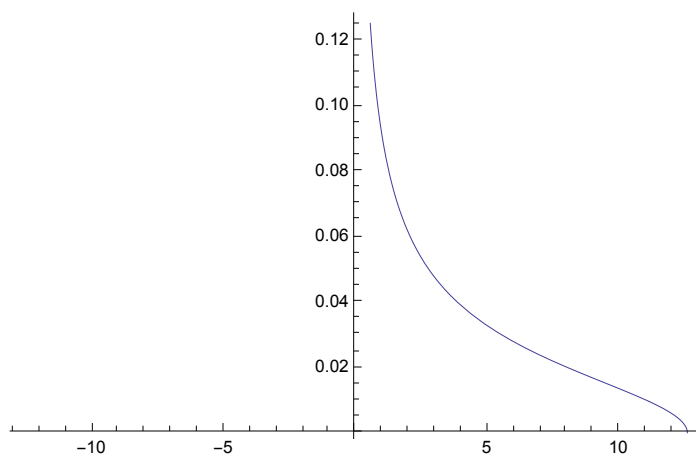
$$\text{Solve}\left[(3.0 \cdot 10^8) == \frac{2 (3.0 \cdot 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} * v, v\right]$$

$$\left\{\left\{v \rightarrow \frac{0.0265258 \sqrt{12.5664 \theta - 1. \theta^2}}{\theta}\right\}\right\}$$

$$\text{Solve}\left[1 == \frac{(\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} * v, v\right]$$

$$\left\{\left\{nf \rightarrow \frac{\sqrt{(4 \pi - \theta) \theta}}{\pi \theta}\right\}\right\}$$

$$\text{Plot}\left[\frac{0.02652582384864922 \sqrt{12.566370614359172 \theta - 1. \theta^2}}{\theta}, \{\theta, -4 \pi, 4 \pi\}\right]$$



$v$  is the frequency solved from the speed of light and a wavelength of  $r$ .  $r$  is able to be placed in terms of



purely theta. If  $v$  is 0, then there is an infinite amount of mass, unless Planck's constant were to be considered nothing (only when nothing in terms of theta reaches infinity in terms of mass).

$$\text{Solve}\left[-\frac{1}{\sqrt{\theta}}\left(\theta + 5.468107888071038 \times 10^{-56}\right) \sqrt{-1.60287714 \times 10^8 + 1.2755291 \times 10^7 \theta} == \frac{2.2086893333333334 \times 10^{-42}}{r}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{8.21431 \times 10^{90} r^2}{8.36115 \times 10^{109} + 6.53674 \times 10^{89} r^2}\right\}\right\}$$

$$\left\{\left\{r \rightarrow \frac{(\theta + 4.039220473596917 \times 10^{13}) \sqrt{\theta}}{\sqrt{-1.60287714 \times 10^8 + 1.2755291 \times 10^7 \theta}}\right\}\right\}$$

The equation for the height of the cone from basic postulates of geometry :

$$\sqrt{\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}} = h$$

The gravitational constant for a certain mass :

$$g = (m G) / r^2 \hat{r}$$

That into which we substitute our equations for the radius of a light wave and the mass of an object (a mass that can be described like the wave of energy of light or any light containing object), as well as the radius of the initial circle (i.e. the maximum (and our distance away from the ground) height) is the gravitational constant. The energy of the potential of another object of the same mass falling is then set equal to the energy of light (i.e. our perception or sense of the visual world).

$$G = 6.6742 \times (10^{-11})$$

$$g = (m (6.6742 \times (10^{-11}))) / r^2 \hat{r}$$

$\hat{r}$  = the height, because it is the function resulting from the change in radius through theta (which can be integrated for  $r$  and not for  $\theta$  so easily) .

$$g = (m (6.6742 \times (10^{-11}))) / r^2 \sqrt{\frac{r^2 (4\pi - \theta) \theta}{4\pi^2}}$$

$$g = \left( \left( \frac{2.2086893333333334 \times 10^{-42}}{r} (6.6742 \times (10^{-11})) \right) / r^2 \right) \sqrt{\left( \frac{1}{4\pi^2} r^2 \left( 4\pi - \left( \frac{8.214307872349999 \times 10^{90} r^2}{8.361147002216258 \times 10^{109} + 6.53673850981586 \times 10^{89} r^2} \right) \right) \left( \frac{8.214307872349999 \times 10^{90} r^2}{8.361147002216258 \times 10^{109} + 6.53673850981586 \times 10^{89} r^2} \right) \right)}$$

$$m \rightarrow \frac{2.2086893333333334 \times 10^{-42}}{r}$$

$E = mc^2 = mgh$ , where  $m$  is mass,  $c$  is speed of light, and  $h$  is the height (with a max value of the wavelength,  $r := \lambda$ ).

$$\begin{aligned}
 E &= \frac{2.2086893333333334 \cdot 10^{-42}}{r} \left( (3.0 \cdot 10^8)^2 \right) \\
 &= \frac{2.2086893333333334 \cdot 10^{-42}}{r} \left( (3.0 \cdot 10^8)^2 \right) = m \cdot g \cdot h = \\
 &= \frac{2.2086893333333334 \cdot 10^{-42}}{r} \left( \left( \frac{2.2086893333333334 \cdot 10^{-42}}{r} (6.6742 \cdot (10^8 - 11)) \right) / r^2 \right) \\
 &= \sqrt{\left( \frac{1}{4\pi^2} r^2 \left( 4\pi - \left( \frac{8.214307872349999 \cdot 10^{90} r^2}{8.361147002216258 \cdot 10^{109} + 6.53673850981586 \cdot 10^{89} r^2} \right) \right) \right.} \\
 &\quad \left. \left( \frac{8.214307872349999 \cdot 10^{90} r^2}{8.361147002216258 \cdot 10^{109} + 6.53673850981586 \cdot 10^{89} r^2} \right) \right) \\
 &= \left( (3.0 \cdot 10^8)^6 \frac{8.214307872349999 \cdot 10^{90} r^2}{8.361147002216258 \cdot 10^{109} + 6.53673850981586 \cdot 10^{89} r^2} \right) = \\
 &= (\text{Planck's Constant}) \nu = \\
 &= (6.62606896 \cdot 10^{-34}) \frac{0.02652582384864922 \cdot \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2}}{\theta}
 \end{aligned}$$

This starts the funk :

$$\begin{aligned}
 \text{Solve} &\left[ \sqrt{\left( \frac{1}{4\pi^2} r^2 \left( 4\pi - \left( \frac{8.214307872349999 \cdot 10^{90} r^2}{8.361147002216258 \cdot 10^{109} + 6.53673850981586 \cdot 10^{89} r^2} \right) \right) \right.} \right. \\
 &\quad \left. \left( \frac{8.214307872349999 \cdot 10^{90} r^2}{8.361147002216258 \cdot 10^{109} + 6.53673850981586 \cdot 10^{89} r^2} \right) \right) \\
 &= \left( (3.0 \cdot 10^8)^6 \frac{8.214307872349999 \cdot 10^{90} r^2}{8.361147002216258 \cdot 10^{109} + 6.53673850981586 \cdot 10^{89} r^2} \right) = \\
 &= (6.62606896 \cdot 10^{-34}) \frac{0.02652582384864922 \cdot \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2}}{\theta}, r]
 \end{aligned}$$

These eight roots symbolize the eightfold path. There is also buddhist art that uses the same shape or design motif for illustration.

$$\begin{aligned}
 \{ \{ r \rightarrow \text{Root} &[-7.8491574179430685695984105867080 \times 10^{120} + \\
 &6.2461610108602860208217445657825 \times 10^{119} \theta + \\
 &(-2.4545861733982329263428402674243 \times 10^{101} + \\
 &1.9532976137067444793150185621669 \times 10^{100} \theta) \mp 1^2 + \\
 &(-2.8784904680651101669429496561654 \times 10^{81} + \\
 &2.2906299331773288707757676634268 \times 10^{80} \theta) \mp 1^4 + \\
 &(-1.5002678051828387552684902256259 \times 10^{61} +
 \end{aligned}$$

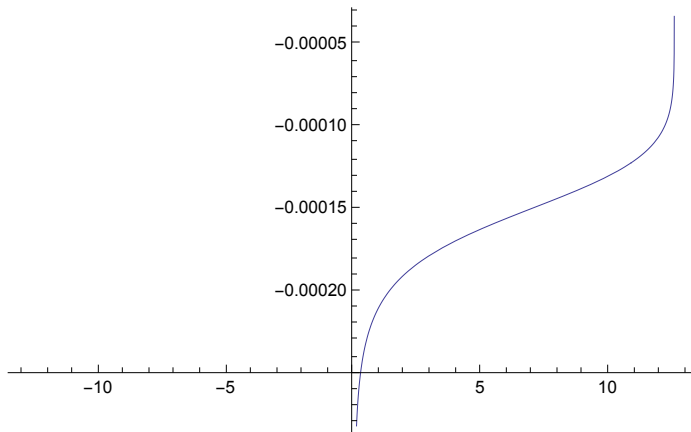
$$\begin{aligned}
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 1] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} + \\
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 2] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} + \\
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 3] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} + \\
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 4] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} +
\end{aligned}$$

$$\begin{aligned}
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 5] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} + \\
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 6] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} + \\
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 7] \}, \\
\{r \rightarrow \text{Root}[-7.8491574179430685695984105867080 \times 10^{120} + \\
& 6.2461610108602860208217445657825 \times 10^{119} \theta + \\
& (-2.4545861733982329263428402674243 \times 10^{101} + \\
& 1.9532976137067444793150185621669 \times 10^{100} \theta) \#1^2 + \\
& (-2.8784904680651101669429496561654 \times 10^{81} + \\
& 2.2906299331773288707757676634268 \times 10^{80} \theta) \#1^4 + \\
& (-1.5002678051828387552684902256259 \times 10^{61} + \\
& 1.1938751857823870945086767237487 \times 10^{60} \theta) \#1^6 + \\
& (-2.9322706366052747333506226360199 \times 10^{40} + \\
& 1.9773065204818872753988742845492 \times 10^{150} \theta) \#1^8 \&, 8] \} \}
\end{aligned}$$

```

Plot[Root[
  -7.84915741794306856959841058670795113147823927902311507042690588`31.9091795403\
    8199*^120 +
  6.2461610108602860208217445657824619078903735671646827195238849`31.9091795403\
    8199*^119 \theta +
  (-2.45458617339823292634284026742428240082124772191067477500127076`31.909179\
    54038201*^101 +
  1.9532976137067444793150185621668961145201167946445345118116787`31.909179\
    54038201*^100 \theta) #1^2 +
  (-2.87849046806511016694294965616544421574760098939550591634221619`31.909179\
    54038199*^81 +
  2.2906299331773288707757676634267939782743287792842404250706313`31.909179\
    54038201*^80 \theta) #1^4 +
  (-1.500267805182838755268490225625904871888906584143400866136064`31.90917954\
    038201*^61 +
  1.19387518578238709450867672374868162205260217625651330285568`31.90917954\
    038201*^60 \theta) #1^6 +
  (-2.9322706366052747333506226360199415109723`31.909179540382016*^40 +
  1.97730652048188727539887428454924231056978653705899056`31.90917954038201\
    *^150 \theta) #1^8 &, 1], {\theta, -13, 13}]

```

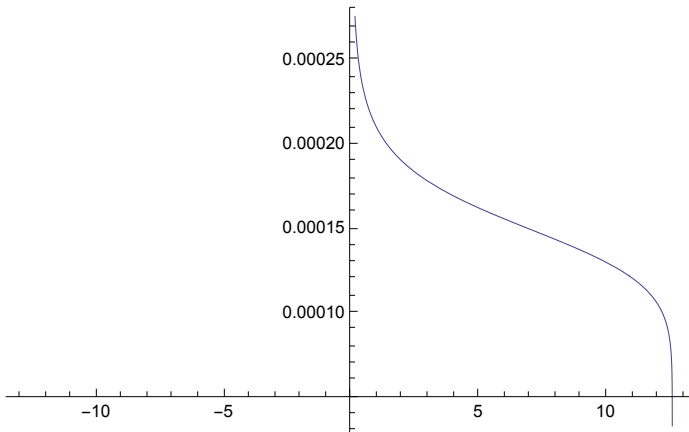


Oh Yeah !

```

Plot[Root[
  - 7.84915741794306856959841058670795113147823927902311507042690588`31.9091795403\
    8199*^120 +
  6.2461610108602860208217445657824619078903735671646827195238849`31.9091795403\
    8199*^119 \theta +
  (- 2.45458617339823292634284026742428240082124772191067477500127076`31.909179\
    54038201*^101 +
  1.9532976137067444793150185621668961145201167946445345118116787`31.909179\
    54038201*^100 \theta) #1^2 +
  (- 2.87849046806511016694294965616544421574760098939550591634221619`31.909179\
    54038199*^81 +
  2.2906299331773288707757676634267939782743287792842404250706313`31.909179\
    54038201*^80 \theta) #1^4 +
  (- 1.500267805182838755268490225625904871888906584143400866136064`31.90917954\
    038201*^61 +
  1.19387518578238709450867672374868162205260217625651330285568`31.90917954\
    038201*^60 \theta) #1^6 +
  (- 2.9322706366052747333506226360199415109723`31.909179540382016*^40 +
  1.97730652048188727539887428454924231056978653705899056`31.90917954038201\
    *^150 \theta) #1^8 &, 2], {\theta, -13, 13}]

```



The rest of the roots won't plot, or their plots are 0. The eight roots are symbolic of the eightfold path, for when.

But, what if the frequency is 0? Could we find the plots of the other roots?

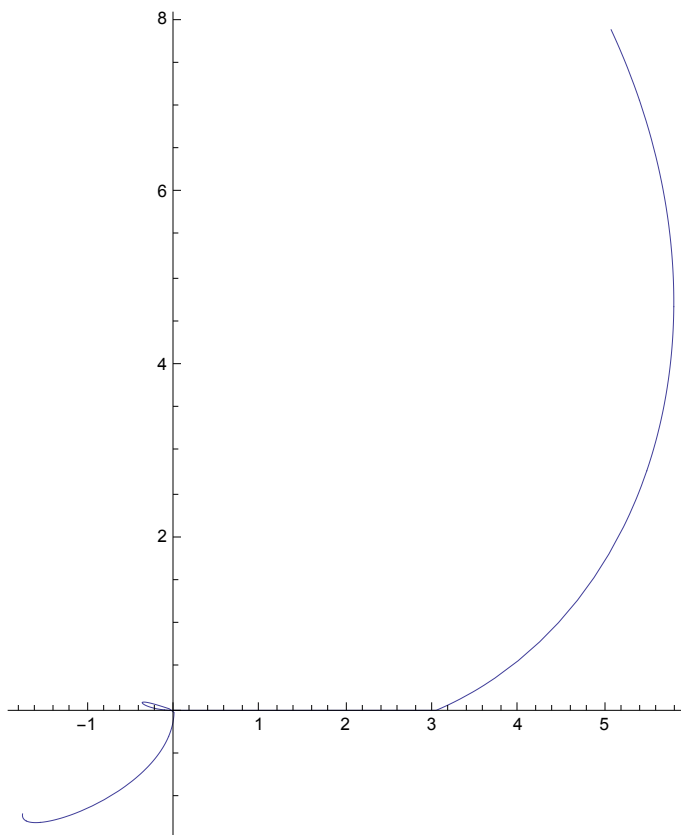
Thanks ! ©Parker Emerson 2009

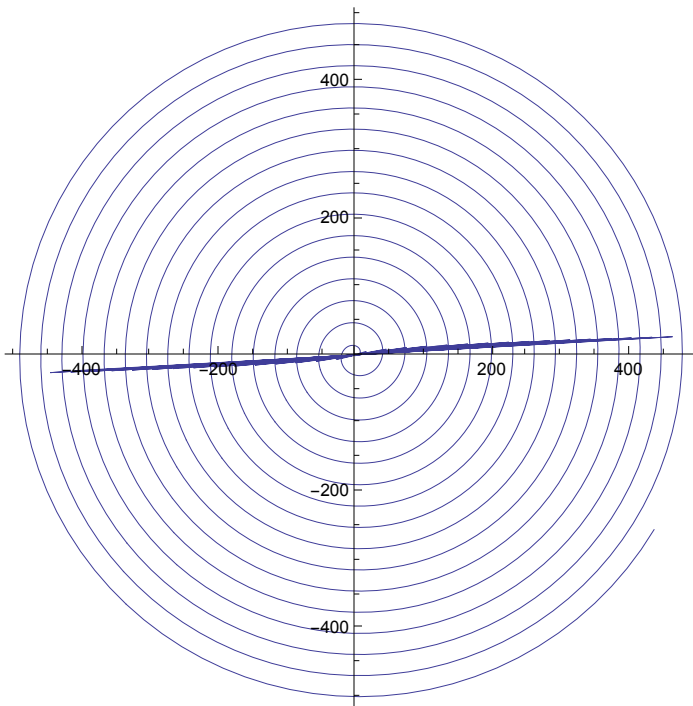
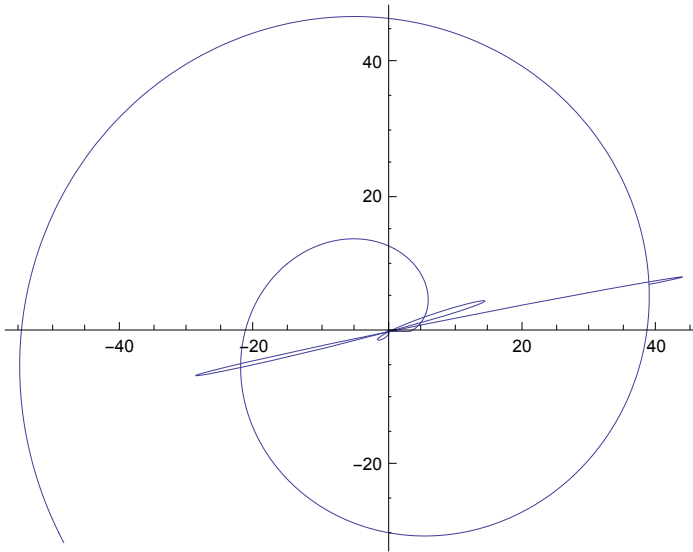
$$\text{Solve}\left[\sqrt{\left(\frac{1}{4\pi^2}r^2\left(4\pi - \left(\frac{8.214307872349999\cdot 10^9 r^2}{8.361147002216258\cdot 10^9 + 6.53673850981586\cdot 10^8 r^2}\right)\right)\right)}\right. \\ \left.\left(\frac{8.214307872349999\cdot 10^9 r^2}{8.361147002216258\cdot 10^9 + 6.53673850981586\cdot 10^8 r^2}\right)\right) \\ \left((3.0\cdot 10^8)6\frac{8.214307872349999\cdot 10^9 r^2}{8.361147002216258\cdot 10^9 + 6.53673850981586\cdot 10^8 r^2}\right) == \\ (6.62606896\cdot 10^{-34})(0), r\Big] \\ \{\{r \rightarrow 0.\}\}$$

Mu! Emptiness, no Holiness! Grr ...eatest is God!

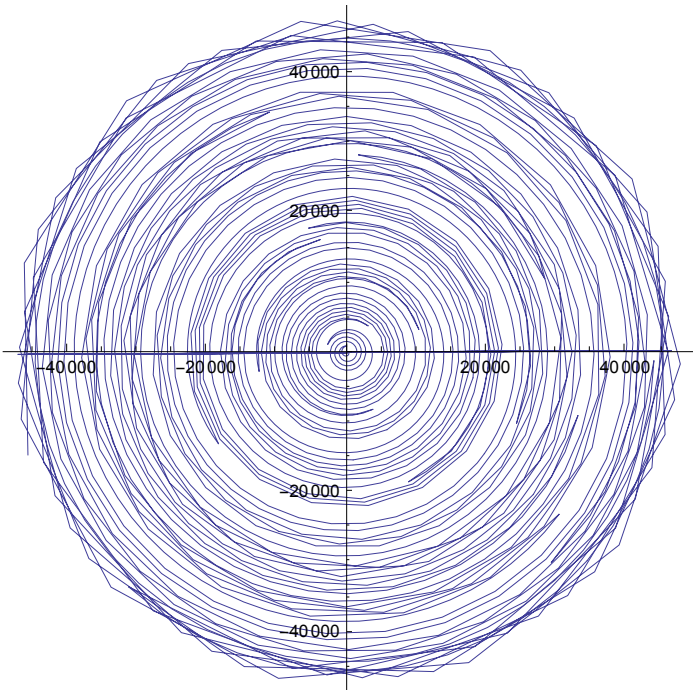
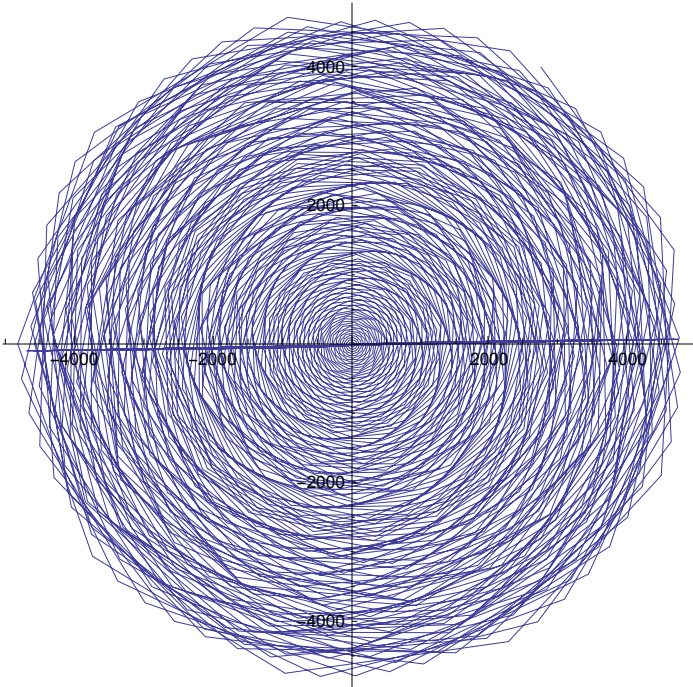
# Math to Art

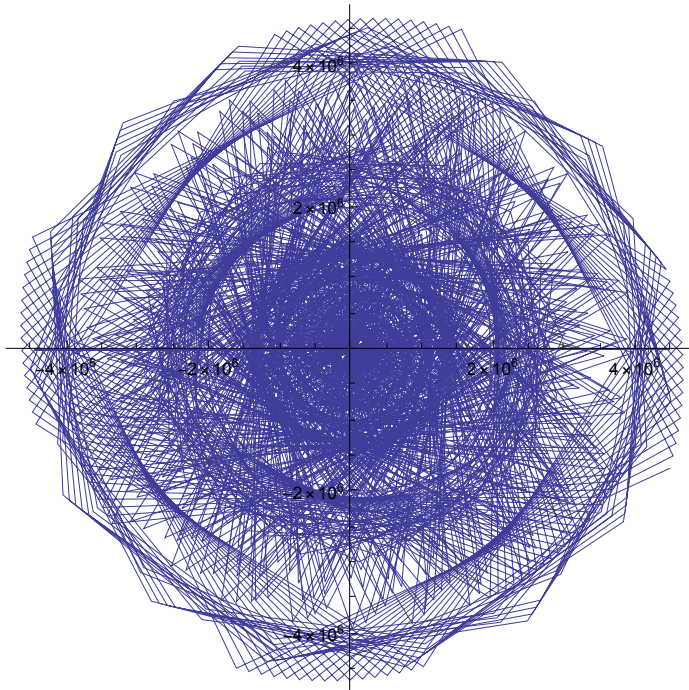
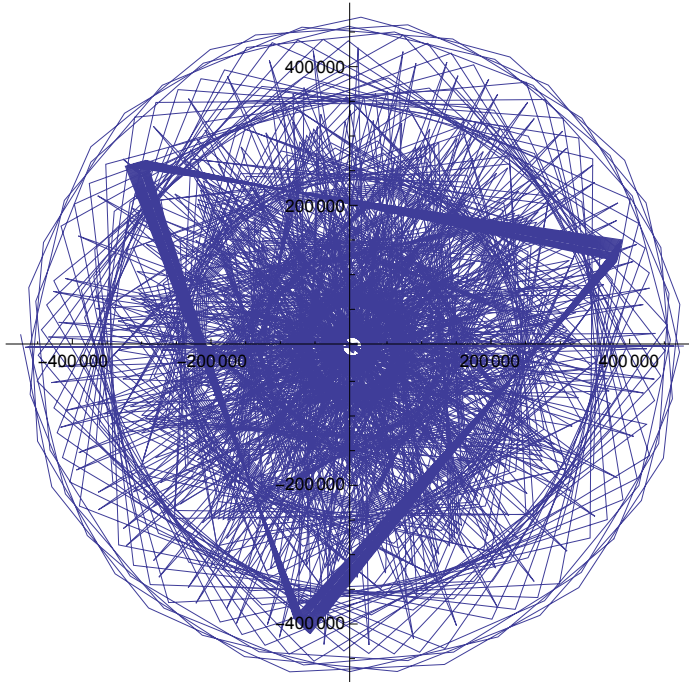
by Parker Emmerson

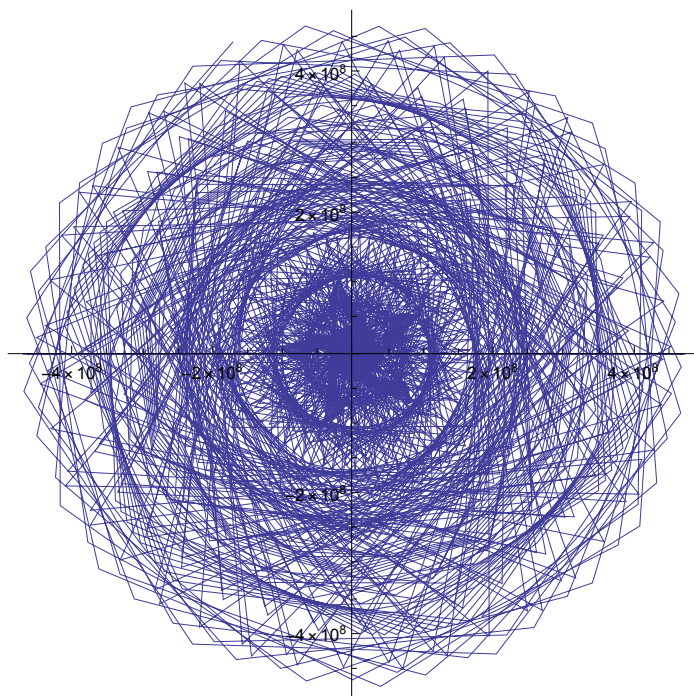
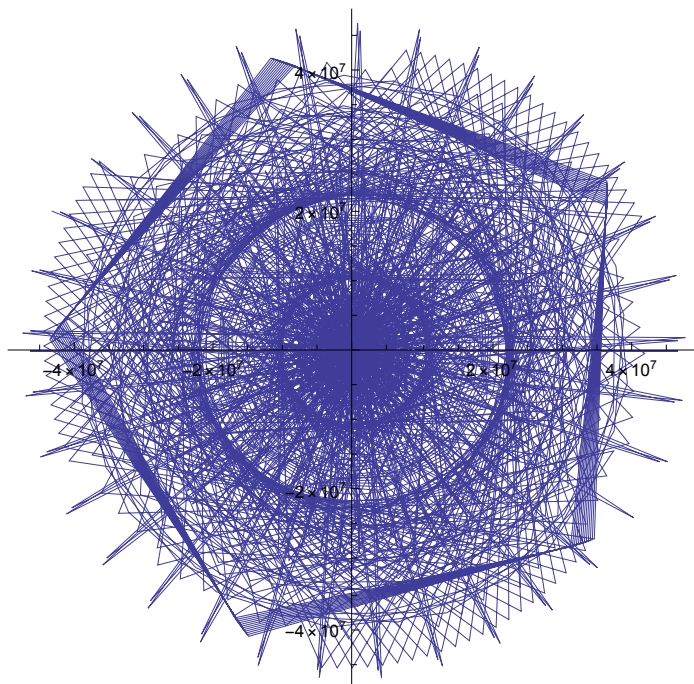




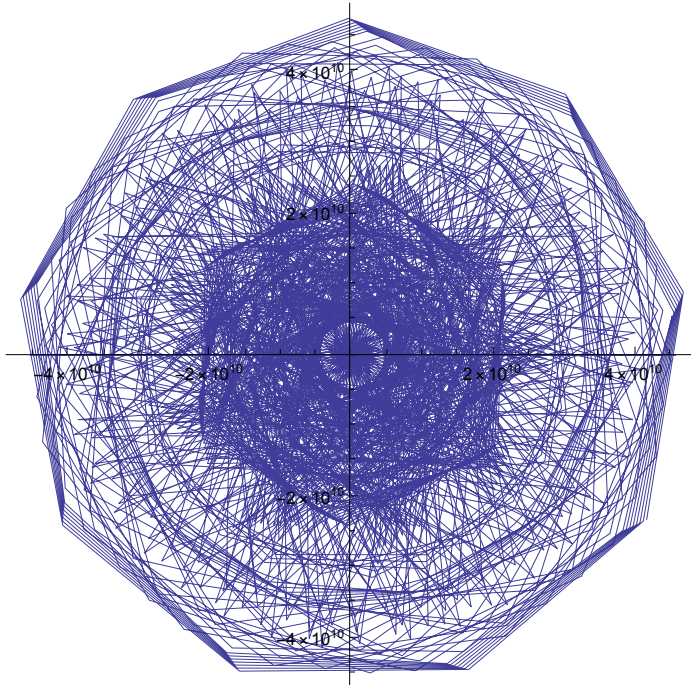
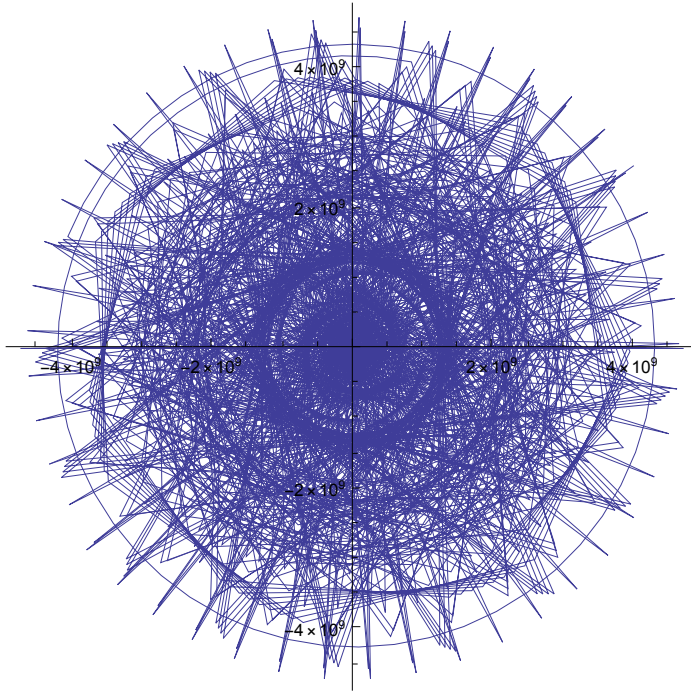


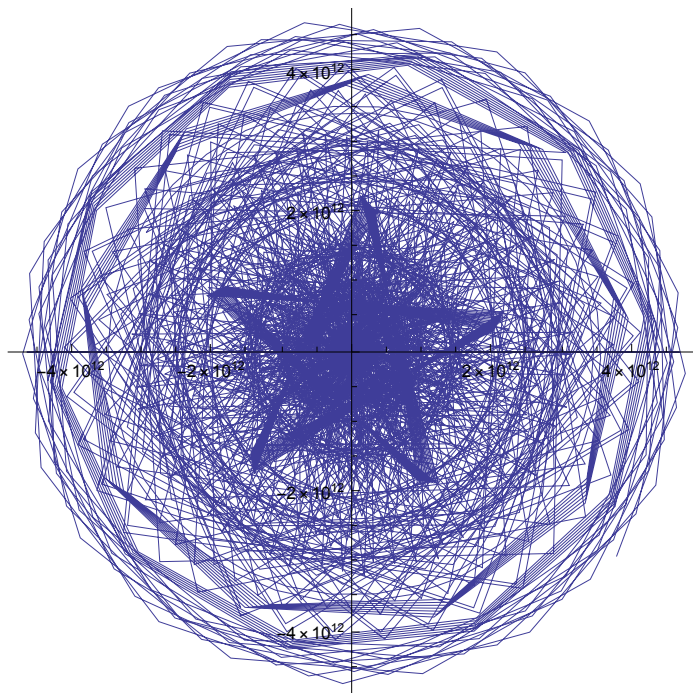
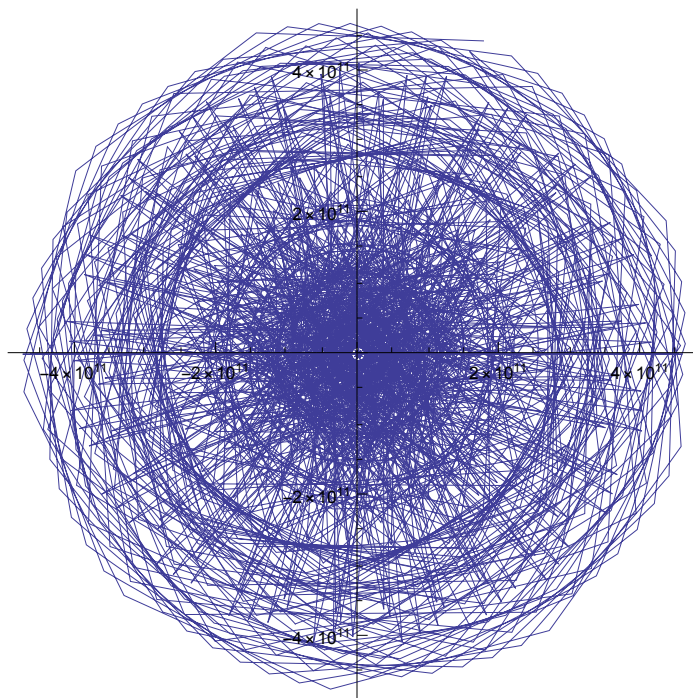




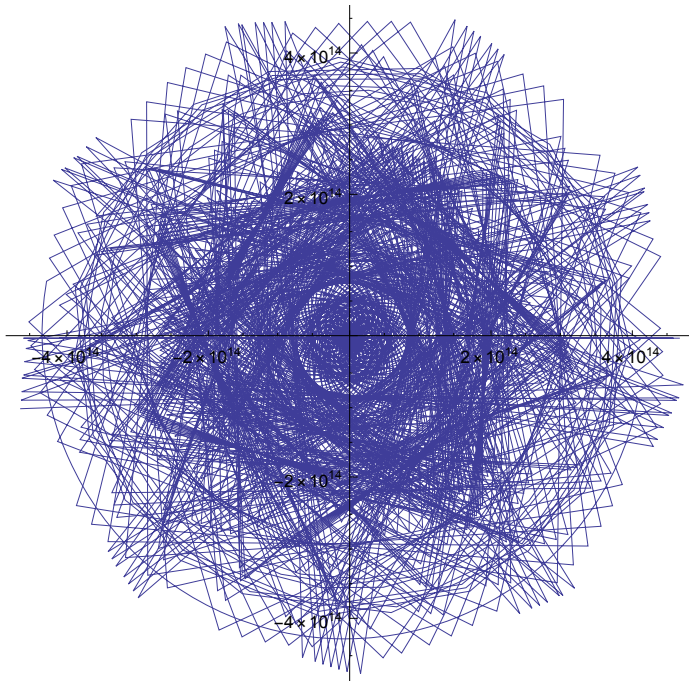
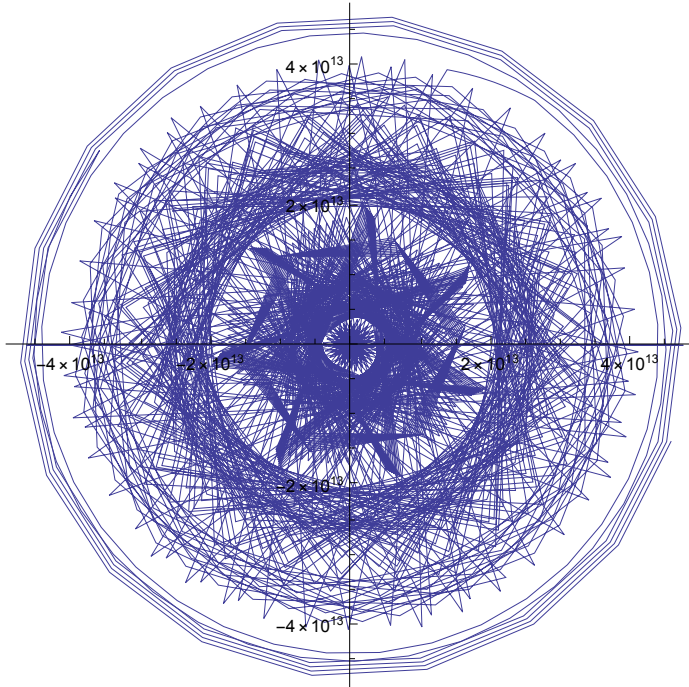


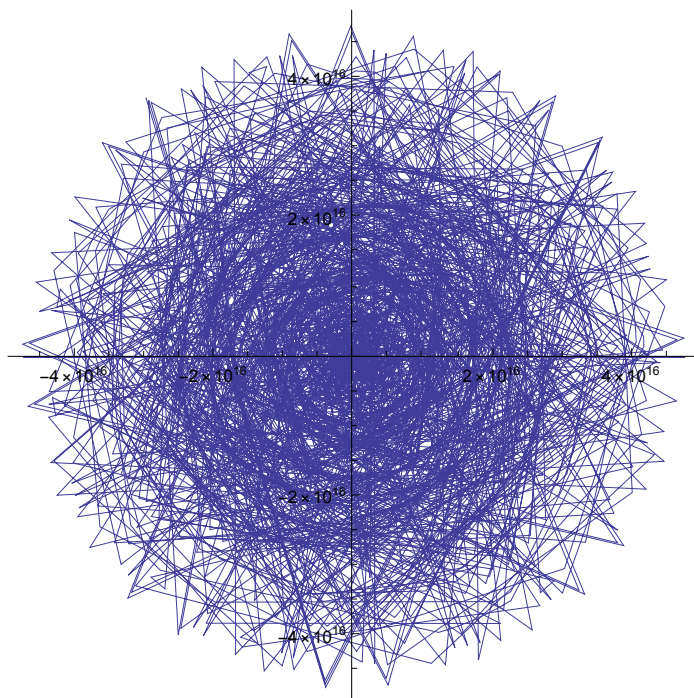
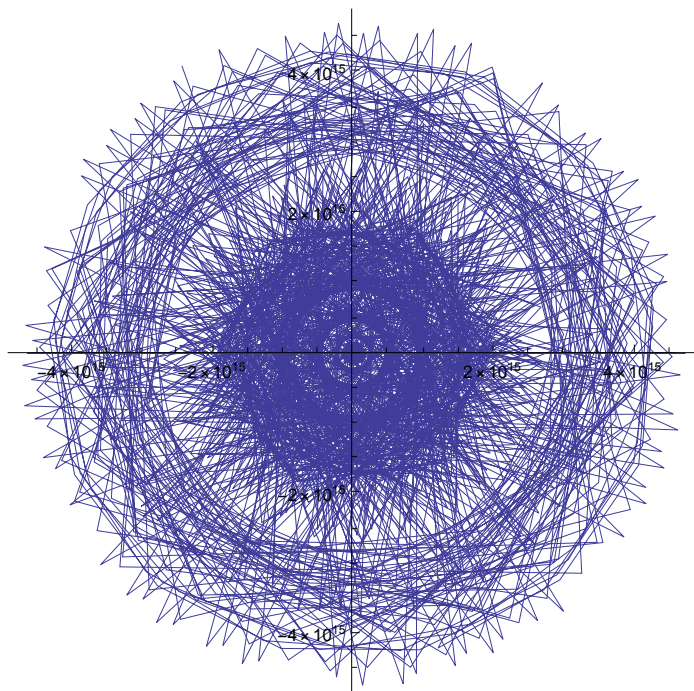




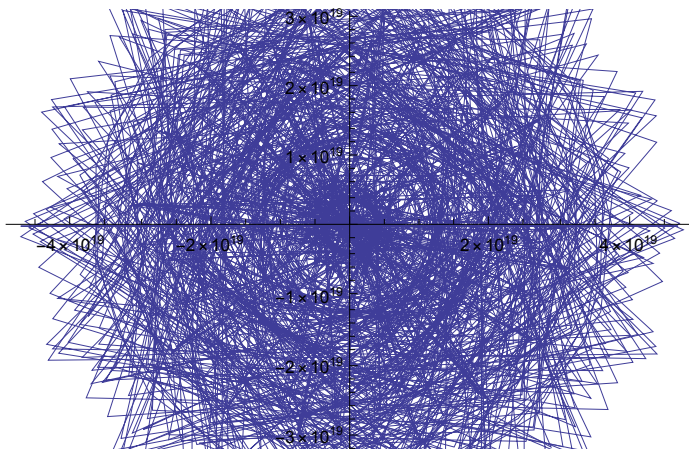
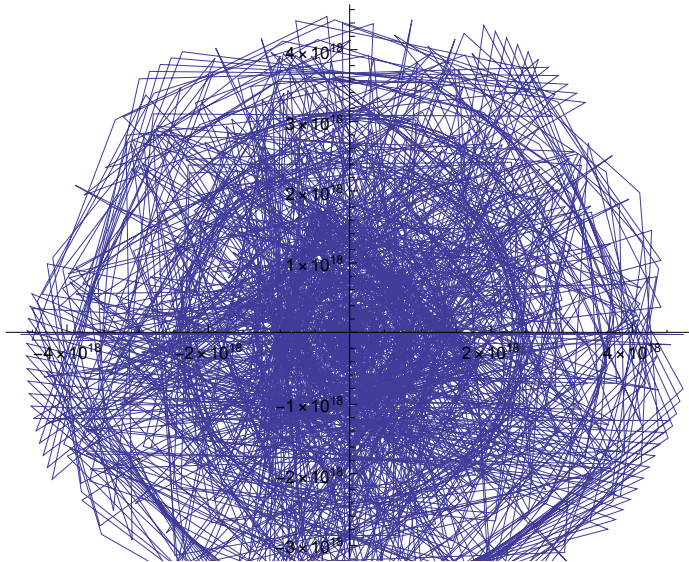
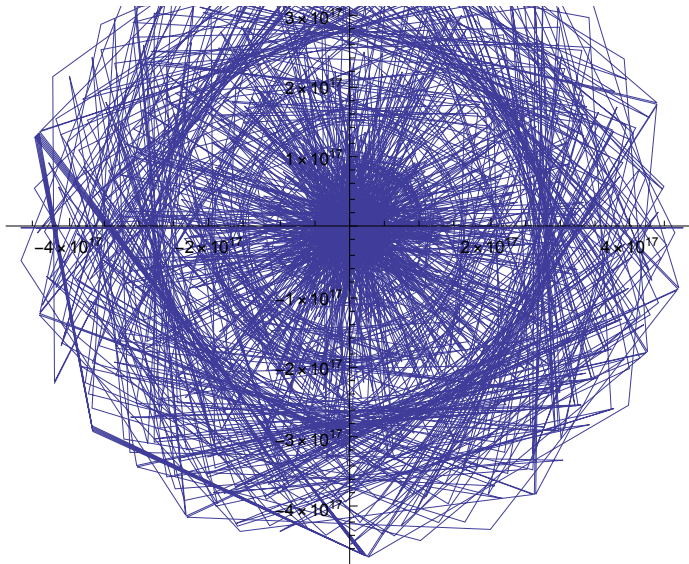




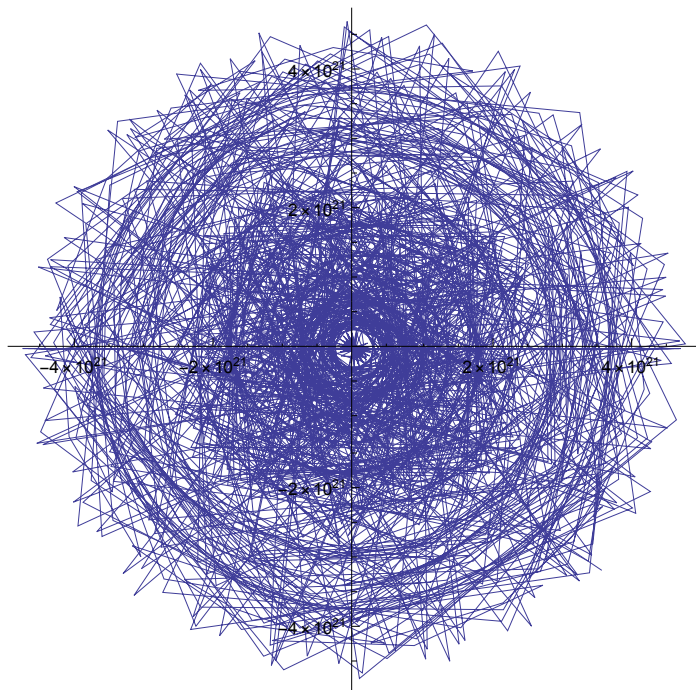
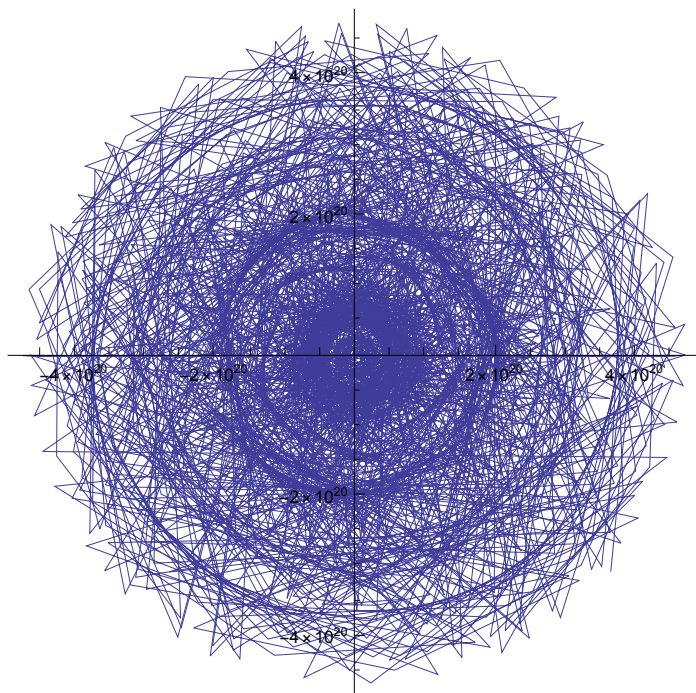


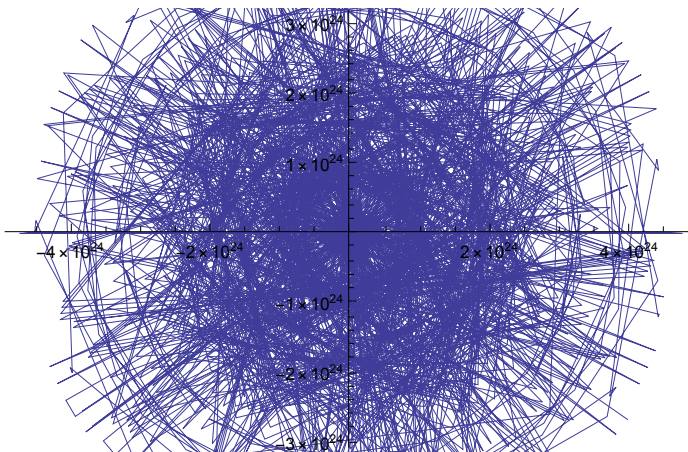
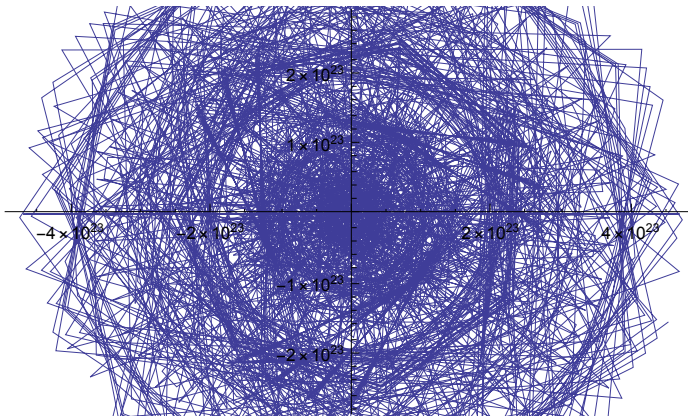
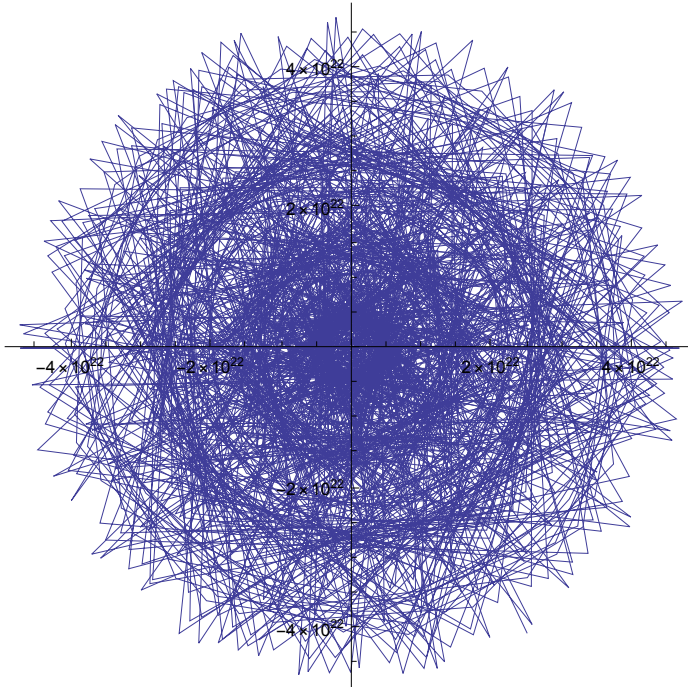




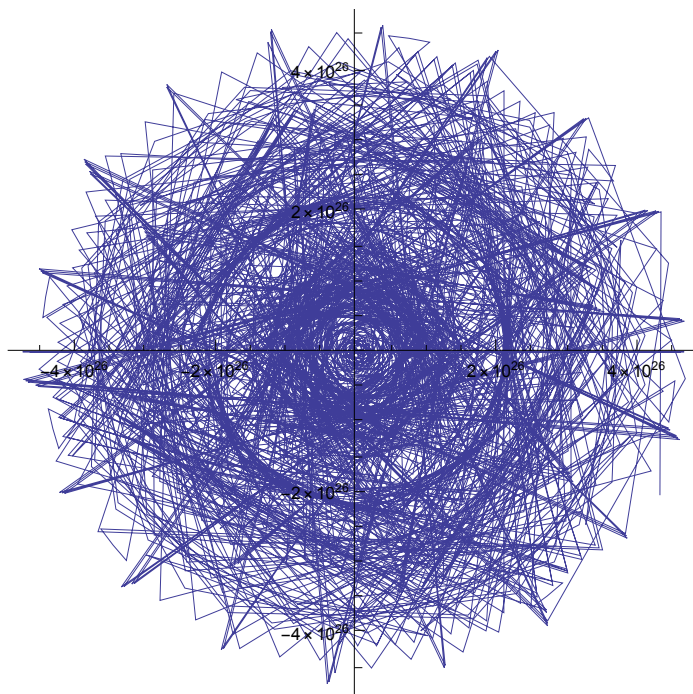
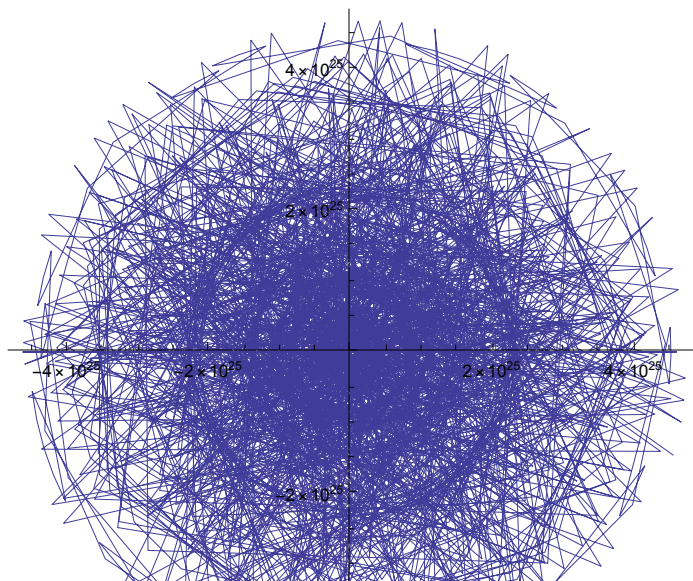


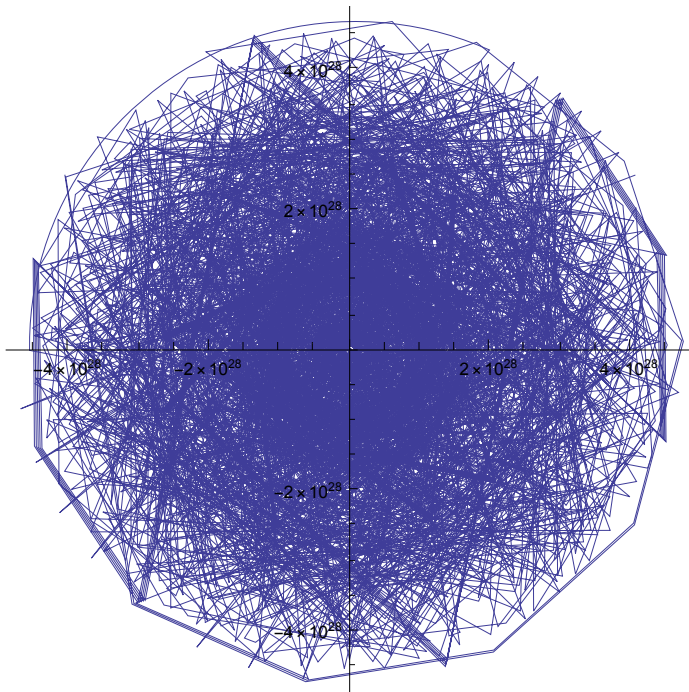
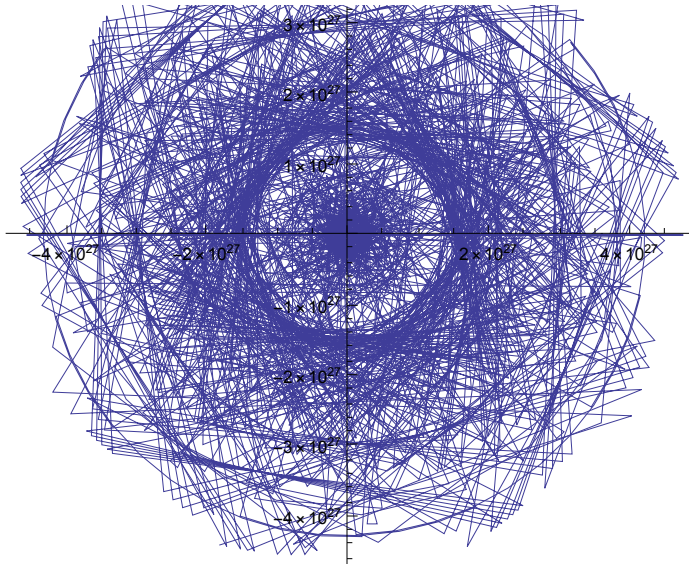


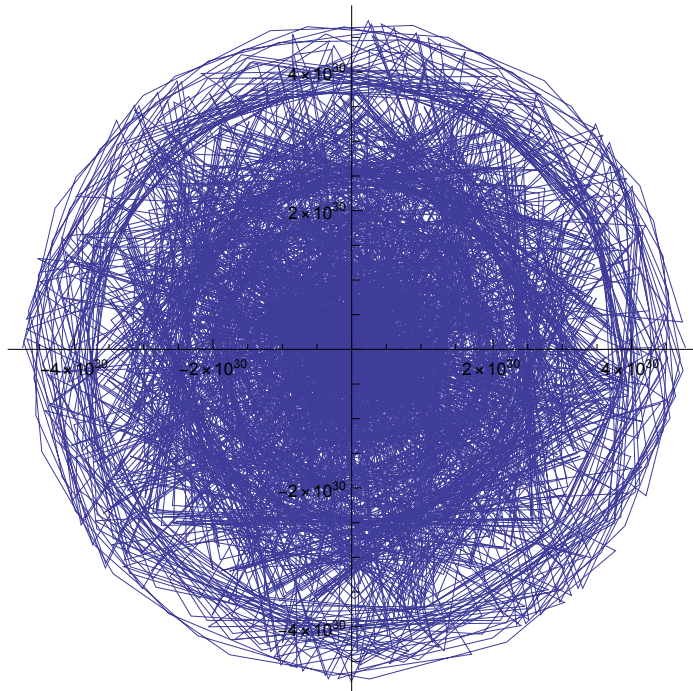
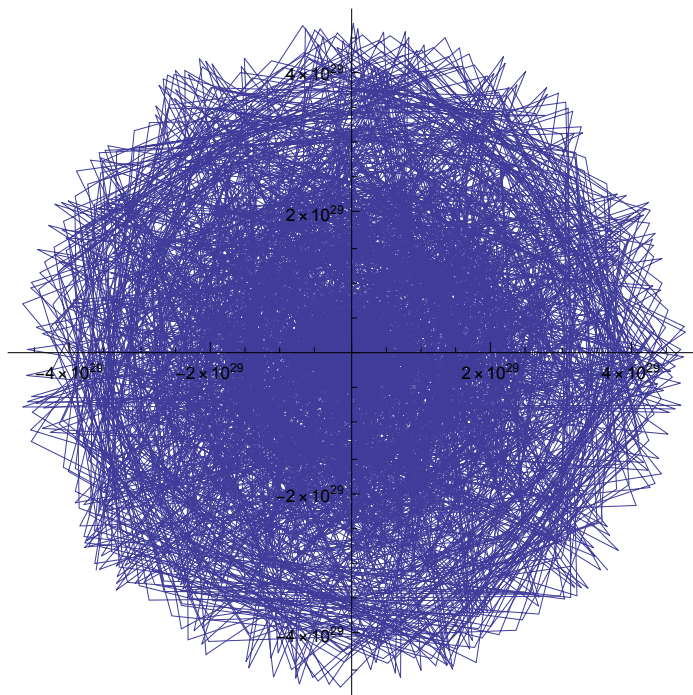




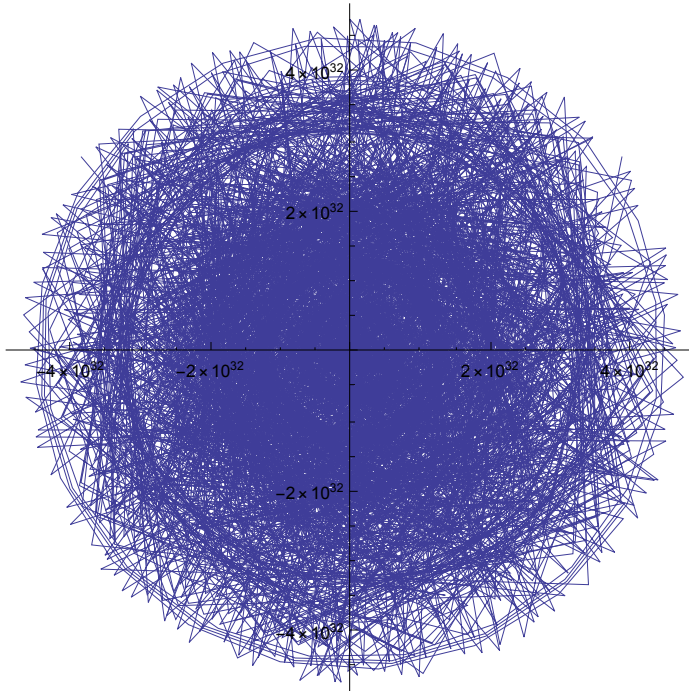
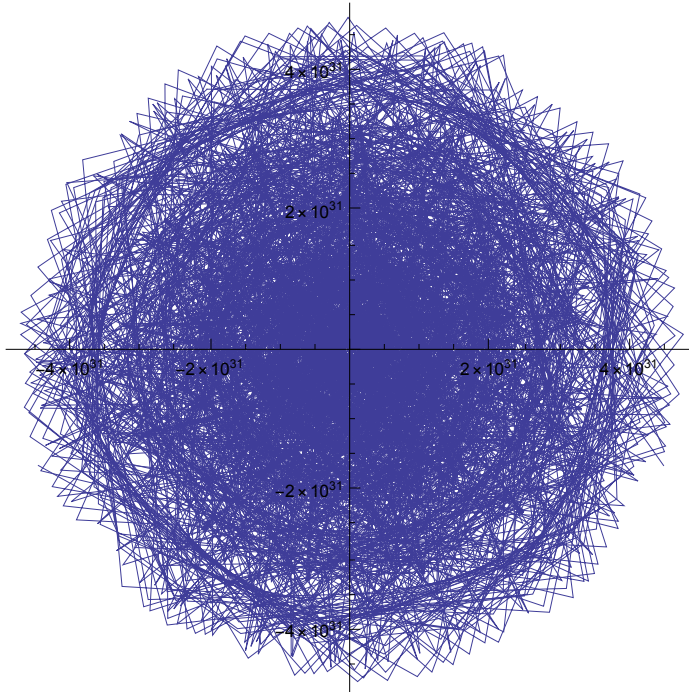


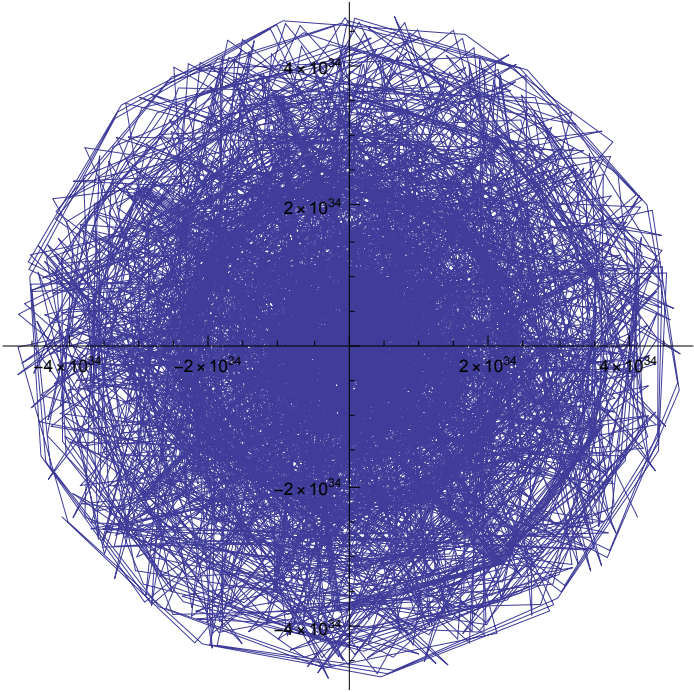
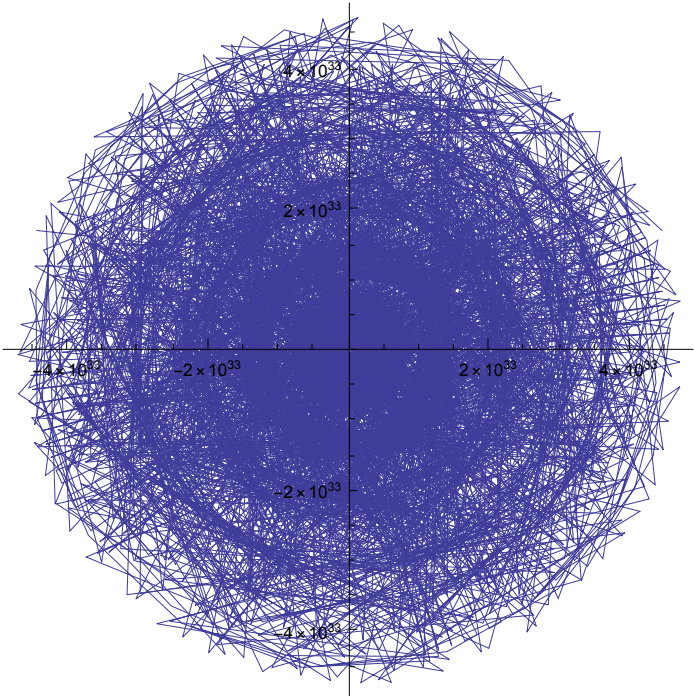


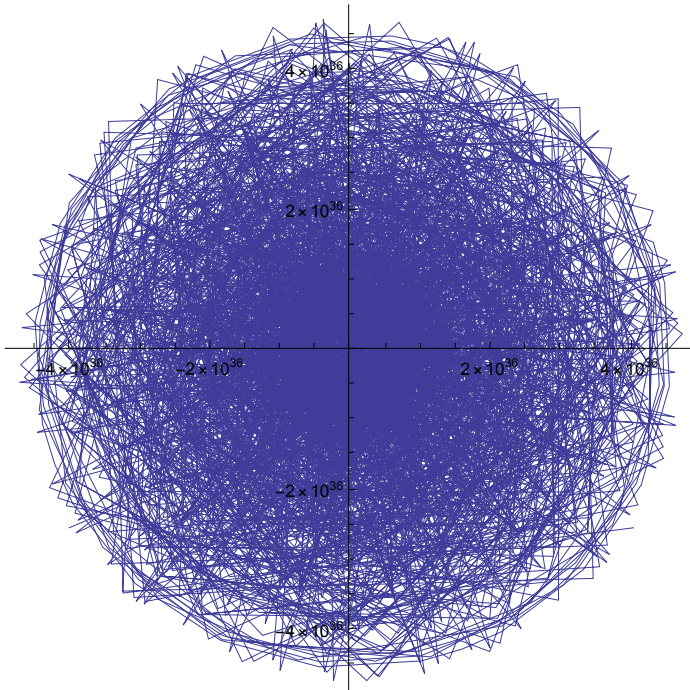
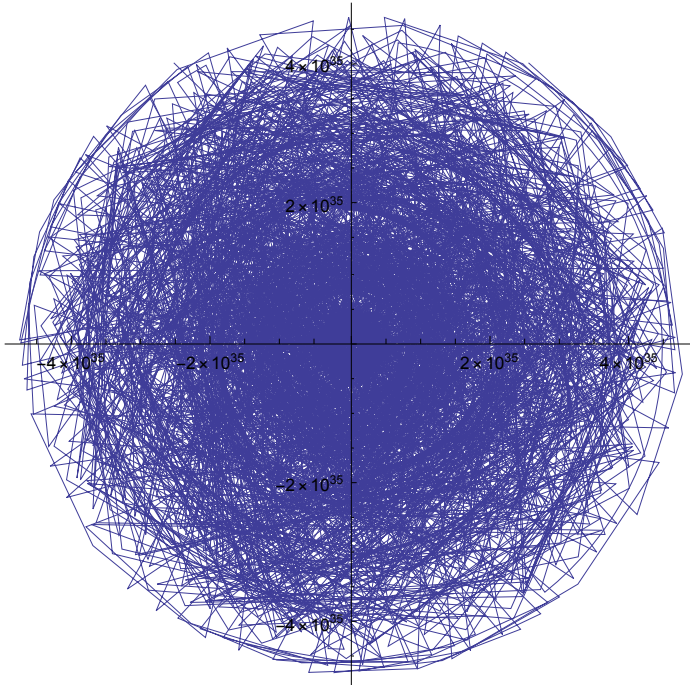




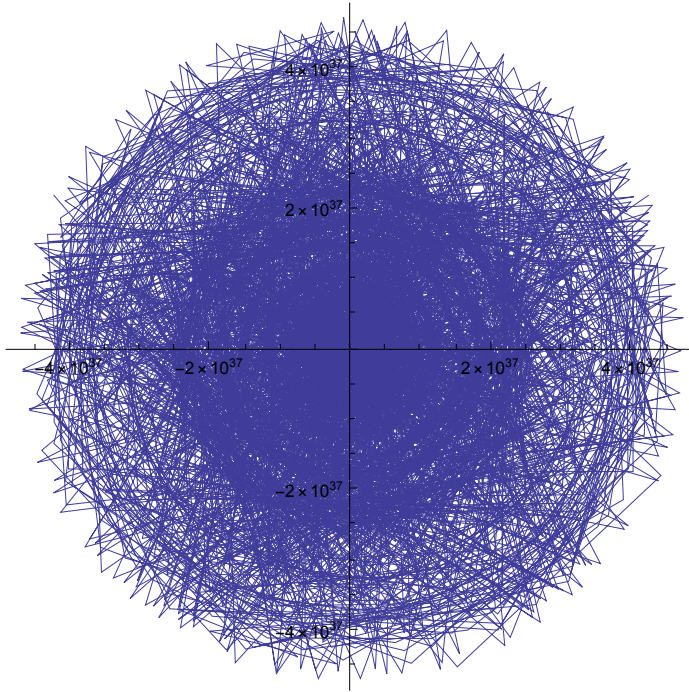












$$\theta r = 2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}$$

$$\gamma x = 2 \pi r - 2 \pi x$$

$$\gamma x \theta r = (2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}) (2 \pi \sqrt{h^2 + x^2} - 2 \pi x)$$

$$\text{Solve}[\gamma x \theta r = (2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}) (2 \pi \sqrt{(r^2 - \eta^2)}) , \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\frac{1}{2} \sqrt{-\frac{4 r^{3/2} \sqrt{x} \sqrt{\gamma} \sqrt{\theta}}{\pi} - \frac{r x \gamma \theta}{\pi^2}} \right\}, \left\{ \eta \rightarrow \frac{1}{2} \sqrt{-\frac{4 r^{3/2} \sqrt{x} \sqrt{\gamma} \sqrt{\theta}}{\pi} - \frac{r x \gamma \theta}{\pi^2}} \right\}, \right.$$

$$\left. \left\{ \eta \rightarrow -\frac{1}{2} \sqrt{\frac{4 r^{3/2} \sqrt{x} \sqrt{\gamma} \sqrt{\theta}}{\pi} - \frac{r x \gamma \theta}{\pi^2}} \right\}, \left\{ \eta \rightarrow \frac{1}{2} \sqrt{\frac{4 r^{3/2} \sqrt{x} \sqrt{\gamma} \sqrt{\theta}}{\pi} - \frac{r x \gamma \theta}{\pi^2}} \right\} \right\}$$

$$c := 2.99792458 * (10^8)$$

$$r^{(3/2)}$$

$$r^{3/2}$$

$$r \sqrt{r}$$

$$r^{3/2}$$

$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$\gamma := \frac{2 \left( \pi - \pi \sin[\beta]^2 + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}{-1 + \sin[\beta]^2}$$

$$r := \frac{x \gamma \theta}{48 \pi^2} + \left( (1 + i \sqrt{3}) (-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4) \right) /$$

$$\left( 96 \pi^2 x \gamma \theta \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + \right. \right.$$

$$\left. \left. x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3} \right) -$$

$$\frac{1}{96 \pi^2 x \gamma \theta} (1 - i \sqrt{3}) \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 + \right.$$

$$\left. 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3}$$

Solve[

$$h == \frac{1}{2} \sqrt{\left( \frac{4 r \sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{x \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\gamma / \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\theta / \sqrt{1 - \frac{(v)^2}{c^2}}}}{\pi} - \frac{r x \gamma \theta}{\pi^2} \right), v]$$

{ {v → -0.5

$$\sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.92803 \times \right. \right. \right.$$

$$\left. \left. 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} h^4 + \right.$$

$$\left. 8.469 \times 10^{16} h^2 r x \gamma \theta - 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) -$$

$$2. \sqrt{\left( \left( -3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \right.$$

$$\left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right)^2 / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right.$$

$$\left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 -$$

$$\left( 4. \left( 1.35034 \times 10^{52} h^4 + 6.84093 \times 10^{50} h^2 r x \gamma \theta - 1.36819 \times 10^{51} r^3 x \gamma \theta + \right. \right.$$

$$\left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right.$$

$$\left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \right) \right\},$$

$$\left\{ v \rightarrow 0.5 \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \right. \right.$$

$$\left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} h^4 + \right.$$

$$\left. 8.469 \times 10^{16} h^2 r x \gamma \theta - 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) -$$

$$2. \sqrt{\left( \left( -3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \right.$$

$$\left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right)^2 / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right.$$

$$\left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 -$$

$$\left( 4. \left( 1.35034 \times 10^{52} h^4 + 6.84093 \times 10^{50} h^2 r x \gamma \theta - 1.36819 \times 10^{51} r^3 x \gamma \theta + \right. \right.$$

$$\left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right.$$

$$\left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \right) \right\},$$

$$\left\{ v \rightarrow -0.5 \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \right. \right.$$

$$\left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} h^4 + \right.$$

$$\left. 8.469 \times 10^{16} h^2 r x \gamma \theta - 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) +$$

$$\begin{aligned}
 & 2. \sqrt{\left( (-3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \\
 & \quad \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right)^2 / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right. \\
 & \quad \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 - \\
 & \quad \left( 4. \left( 1.35034 \times 10^{52} h^4 + 6.84093 \times 10^{50} h^2 r x \gamma \theta - 1.36819 \times 10^{51} r^3 x \gamma \theta + \right. \right. \\
 & \quad \left. \left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right. \\
 & \quad \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \Big) \Big) \Big\}, \\
 & \left\{ v \rightarrow 0.5 \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} h^4 + \right. \right. \right. \\
 & \quad \left. \left. \left. 8.469 \times 10^{16} h^2 r x \gamma \theta - 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) + \right. \right. \\
 & \quad \left. \left. 2. \sqrt{\left( (-3.00492 \times 10^{35} h^4 - 1.52231 \times 10^{34} h^2 r x \gamma \theta + 3.04462 \times 10^{34} r^3 x \gamma \theta - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right)^2 / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right. \right. \right. \\
 & \quad \left. \left. \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 - \right. \right. \\
 & \quad \left. \left. \left( 4. \left( 1.35034 \times 10^{52} h^4 + 6.84093 \times 10^{50} h^2 r x \gamma \theta - 1.36819 \times 10^{51} r^3 x \gamma \theta + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} h^4 + 8.469 \times 10^{16} h^2 r x \gamma \theta - \right. \right. \\
 & \quad \left. \left. \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \right) \right) \Big) \Big\}
 \end{aligned}$$

$$r := \sqrt{x^2 + h^2}$$

$$h := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\theta := \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

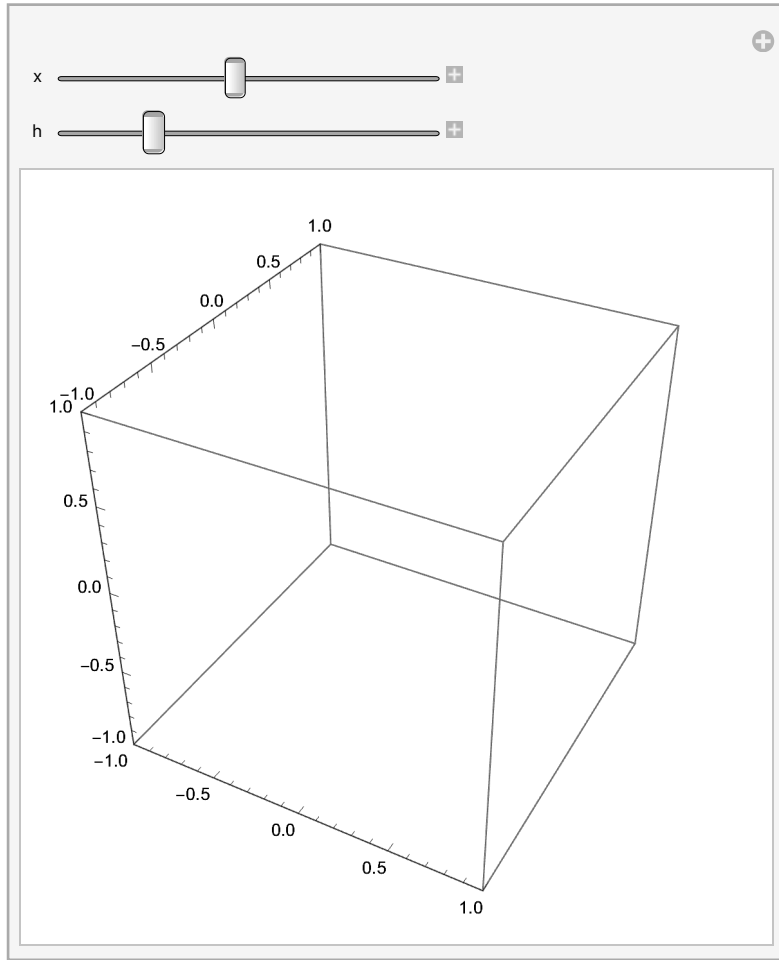
$$r := - \frac{-8 \pi^2 x - x \gamma \theta + x \sqrt{\gamma} \sqrt{\theta} \sqrt{16 \pi^2 + \gamma \theta}}{8 \pi^2}$$

$$\begin{aligned}
 r := & \frac{x \gamma \theta}{48 \pi^2} + \left( \left( 1 + i \sqrt{3} \right) \left( -384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4 \right) \right) / \\
 & \left( 96 \pi^2 x \gamma \theta \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + \right. \right. \\
 & \quad \left. \left. x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3} \right) - \\
 & \frac{1}{96 \pi^2 x \gamma \theta} \left( 1 - i \sqrt{3} \right) \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 + \right. \\
 & \quad \left. 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3}
 \end{aligned}$$

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Manipulate[SphericalPlot3D[
  0.5` $\sqrt{\left(-\left(2.\left(-3.0049220849611958`^{35}h^4-1.522311312006349`^{34}h^2rx\gamma\theta+3.044622624012698`^{34}r^3x\gamma\theta-1.928029800057543`^{32}r^2x^2\gamma^2\theta^2\right)\right)/\left(1.671713363134415`^{18}h^4+8.468998833174608`^{16}h^2rx\gamma\theta-1.6937997666349216`^{17}r^3x\gamma\theta+1.072611232553536`^{15}r^2x^2\gamma^2\theta^2\right)+2.\sqrt{\left(\left(-3.0049220849611958`^{35}h^4-1.522311312006349`^{34}h^2rx\gamma\theta+3.044622624012698`^{34}r^3x\gamma\theta-1.928029800057543`^{32}r^2x^2\gamma^2\theta^2\right)^2/\left(1.671713363134415`^{18}h^4+8.468998833174608`^{16}h^2rx\gamma\theta-1.6937997666349216`^{17}r^3x\gamma\theta+1.072611232553536`^{15}r^2x^2\gamma^2\theta^2\right)^2-\left(4.\left(1.350344642779755`^{52}h^4+6.840925876576728`^{50}h^2rx\gamma\theta-1.3681851753153455`^{51}r^3x\gamma\theta+8.664133837803139`^{48}r^2x^2\gamma^2\theta^2\right)\right)/\left(1.671713363134415`^{18}h^4+8.468998833174608`^{16}h^2rx\gamma\theta-1.6937997666349216`^{17}r^3x\gamma\theta+1.072611232553536`^{15}r^2x^2\gamma^2\theta^2\right)\right)},$ 
  {\theta, -2 \pi, 2 \pi}, {\gamma, -8 \pi, 8 \pi}], {x, -100,
100},
{h,
-100,
100}]

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$$\begin{aligned}
 r := & \left( -32 \pi^4 \gamma - 8 \pi^3 \gamma^2 + 32 \pi^4 \theta + 32 \pi^3 \gamma \theta + 8 \pi^2 \gamma^2 \theta - \right. \\
 & 8 \pi^3 \theta^2 - 8 \pi^2 \gamma \theta^2 - 2 \pi \gamma^2 \theta^2 + 4 \pi^2 \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \sqrt{(4 \pi - \theta) \theta} + \\
 & \frac{4 \pi^2 \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \theta \sqrt{(4 \pi - \theta) \theta}}{\sqrt{4 \pi + \gamma}} - \frac{4 \pi^2 \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \theta \sqrt{(4 \pi - \theta) \theta}}{\sqrt{\gamma}} - \\
 & 4 \pi \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \theta \sqrt{(4 \pi - \theta) \theta} - \frac{\pi \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \theta^2 \sqrt{(4 \pi - \theta) \theta}}{\sqrt{4 \pi + \gamma}} + \\
 & \left. \frac{\pi \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \theta^2 \sqrt{(4 \pi - \theta) \theta}}{\sqrt{\gamma}} + \sqrt{\gamma} \sqrt{(2 \pi + \gamma)^2} \sqrt{4 \pi + \gamma} \theta^2 \sqrt{(4 \pi - \theta) \theta} \right) / \\
 & \left( \pi^2 (128 \pi^3 \gamma + 32 \pi^2 \gamma^2 - 128 \pi^3 \theta - 128 \pi^2 \gamma \theta - 32 \pi \gamma^2 \theta + 32 \pi^2 \theta^2 + 32 \pi \gamma \theta^2 + 8 \gamma^2 \theta^2) \right) \\
 \eta := & \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}
 \end{aligned}$$

$$x := r - \frac{(r \theta)}{2 \pi}$$

SphericalPlot3D[

$$\begin{aligned} & 0.5 \sqrt{\left( - \left( 2. \left( -3.0049220849611958 \eta^4 + 3.044622624012698 r^3 x \gamma \theta - \right. \right. \right. \\ & \quad \left. \left. \left. 1.522311312006349 r x \gamma \eta^2 \theta - 1.928029800057543 r^2 x^2 \gamma^2 \theta^2 \right) \right) / \right. \\ & \quad \left( 1.671713363134415 \eta^4 - 1.6937997666349216 r^3 x \gamma \theta + \right. \\ & \quad \left. 8.468998833174608 r x \gamma \eta^2 \theta + 1.072611232553536 r^2 x^2 \gamma^2 \theta^2 \right) + \\ & 2. \sqrt{\left( \left( -3.0049220849611958 \eta^4 + 3.044622624012698 r^3 x \gamma \theta - \right. \right. \\ & \quad \left. \left. 1.522311312006349 r x \gamma \eta^2 \theta - 1.928029800057543 r^2 x^2 \gamma^2 \theta^2 \right)^2 / \right. \\ & \quad \left( 1.671713363134415 \eta^4 - 1.6937997666349216 r^3 x \gamma \theta + \right. \\ & \quad \left. 8.468998833174608 r x \gamma \eta^2 \theta + 1.072611232553536 r^2 x^2 \gamma^2 \theta^2 \right)^2 - \\ & \quad \left( 4. \left( 1.350344642779755 \eta^4 - 1.3681851753153455 r^3 x \gamma \theta + \right. \right. \\ & \quad \left. \left. 6.840925876576728 r x \gamma \eta^2 \theta + 8.664133837803139 r^2 x^2 \gamma^2 \theta^2 \right) \right) / \\ & \quad \left( 1.671713363134415 \eta^4 - 1.6937997666349216 r^3 x \gamma \theta + \right. \\ & \quad \left. 8.468998833174608 r x \gamma \eta^2 \theta + \right. \\ & \quad \left. 1.072611232553536 r^2 x^2 \gamma^2 \theta^2 \right) \Big), \{\theta, -2 \pi, 2 \pi\}, \{\gamma, -2 \pi, 2 \pi\} \end{aligned}$$

Solve[

$$\eta == \frac{1}{2} \sqrt{\left( \frac{4 r \sqrt{r \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{x \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\gamma / \sqrt{1 - \frac{(v)^2}{c^2}}} \sqrt{\theta / \sqrt{1 - \frac{(v)^2}{c^2}}}}{\pi} - \frac{r x \gamma \theta}{\pi^2} \right)}, v]$$

{ {v → -0.5

$$\begin{aligned} & \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - 1.92803 \times \right. \right. \right. \\ & \quad \left. \left. \left. 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - \right. \right. \\ & \quad \left. \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) - \right. \\ & 2. \sqrt{\left( \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \\ & \quad \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right)^2 / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \right. \\ & \quad \left. \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 - \right. \\ & \quad \left( 4. \left( 1.35034 \times 10^{52} \eta^4 - 1.36819 \times 10^{51} r^3 x \gamma \theta + 6.84093 \times 10^{50} r x \gamma \eta^2 \theta + \right. \right. \\ & \quad \left. \left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \\ & \quad \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \Big) \Big\}, \end{aligned}$$

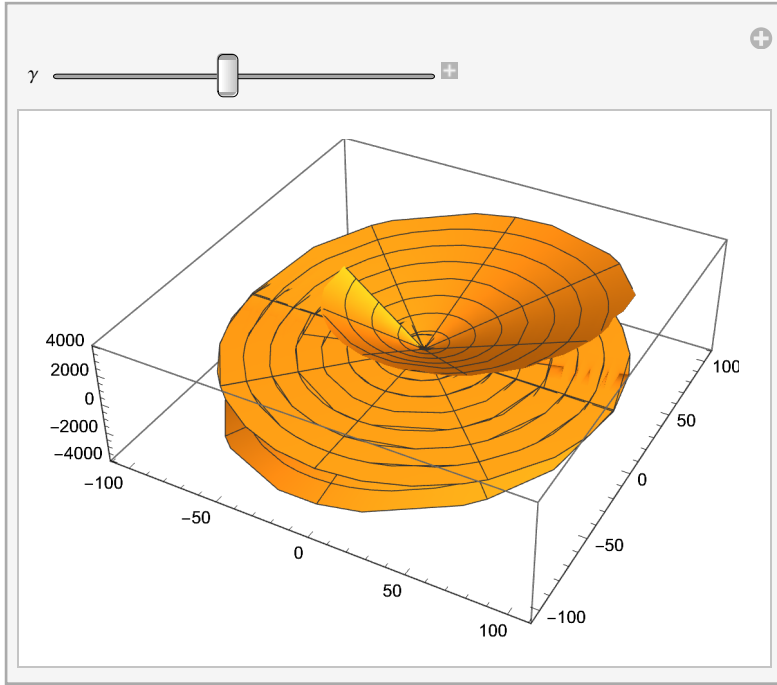
$$\begin{aligned} & \left\{ v \rightarrow 0.5 \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \right. \right. \\ & \quad \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - \right. \right. \\ & \quad \left. \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) - \right. \\ & 2. \sqrt{\left( \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \end{aligned}$$

$$\begin{aligned}
& \left( 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right)^2 / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \\
& \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 - \\
& \left( 4. \left( 1.35034 \times 10^{52} \eta^4 - 1.36819 \times 10^{51} r^3 x \gamma \theta + 6.84093 \times 10^{50} r x \gamma \eta^2 \theta + \right. \right. \\
& \left. \left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \\
& \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \Big) \Big) \Big) \Big\}, \\
& \left\{ v \rightarrow -0.5 \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \right. \right. \\
& \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - \right. \right. \\
& \left. \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) + \right. \\
& \left. 2. \sqrt{\left( \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \right. \\
& \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right)^2 / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \right. \\
& \left. \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 - \right. \\
& \left. \left( 4. \left( 1.35034 \times 10^{52} \eta^4 - 1.36819 \times 10^{51} r^3 x \gamma \theta + 6.84093 \times 10^{50} r x \gamma \eta^2 \theta + \right. \right. \right. \\
& \left. \left. \left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \right. \\
& \left. \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \right) \Big) \Big) \Big) \Big\}, \\
& \left\{ v \rightarrow 0.5 \sqrt{\left( - \left( 2. \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \right. \right. \\
& \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - \right. \right. \\
& \left. \left. 1.6938 \times 10^{17} r^3 x \gamma \theta + 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) + \right. \\
& \left. 2. \sqrt{\left( \left( -3.00492 \times 10^{35} \eta^4 + 3.04462 \times 10^{34} r^3 x \gamma \theta - 1.52231 \times 10^{34} r x \gamma \eta^2 \theta - \right. \right. \right. \\
& \left. \left. \left. 1.92803 \times 10^{32} r^2 x^2 \gamma^2 \theta^2 \right) \right)^2 / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \right. \\
& \left. \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right)^2 - \right. \\
& \left. \left( 4. \left( 1.35034 \times 10^{52} \eta^4 - 1.36819 \times 10^{51} r^3 x \gamma \theta + 6.84093 \times 10^{50} r x \gamma \eta^2 \theta + \right. \right. \right. \\
& \left. \left. \left. 8.66413 \times 10^{48} r^2 x^2 \gamma^2 \theta^2 \right) \right) / \left( 1.67171 \times 10^{18} \eta^4 - 1.6938 \times 10^{17} r^3 x \gamma \theta + \right. \right. \\
& \left. \left. 8.469 \times 10^{16} r x \gamma \eta^2 \theta + 1.07261 \times 10^{15} r^2 x^2 \gamma^2 \theta^2 \right) \right) \Big) \Big) \Big) \Big\}
\end{aligned}$$

**Solve[ $\gamma x \theta r = (2 \pi r - 2 \pi x) (2 \pi r - 2 \pi x), r]$**

$$\left\{ \left\{ r \rightarrow -\frac{-8 \pi^2 x - x \gamma \theta - x \sqrt{\gamma} \sqrt{\theta} \sqrt{16 \pi^2 + \gamma \theta}}{8 \pi^2} \right\}, \left\{ r \rightarrow -\frac{-8 \pi^2 x - x \gamma \theta + x \sqrt{\gamma} \sqrt{\theta} \sqrt{16 \pi^2 + \gamma \theta}}{8 \pi^2} \right\} \right\}$$

Manipulate[RevolutionPlot3D[ $\frac{-8 \pi^2 x - x \gamma \theta + x \sqrt{\gamma} \sqrt{\theta} \sqrt{16 \pi^2 + \gamma \theta}}{8 \pi^2}$ ,  
 $\{x, -100, 100\}, \{\theta, -2 \pi, 2 \pi\}, \{\gamma, -2000 \pi, 2000 \pi\}$ ]



Solve[ $\gamma x \theta r == (2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}) (2 \pi \sqrt{\eta^2 + x^2} - 2 \pi x), r]$   
 $\left\{ \left\{ r \rightarrow - \left( 4 \sqrt{ \left( 8 \pi^6 x \eta^4 - 8 \pi^6 \eta^4 \sqrt{x^2 + \eta^2} - 2 \pi^4 x^3 \gamma \eta^2 \theta - \pi^4 x \gamma \eta^4 \theta + 2 \pi^4 x^2 \gamma \eta^2 \sqrt{x^2 + \eta^2} \theta \right) } / \right. \right.$   
 $\left. \left( \sqrt{-64 \pi^4 x \gamma \eta^2 \theta + 16 \pi^2 x^3 \gamma^2 \theta^2 + x^3 \gamma^3 \theta^3} \right) \right\},$   
 $\left\{ r \rightarrow \left( 4 \sqrt{ \left( 8 \pi^6 x \eta^4 - 8 \pi^6 \eta^4 \sqrt{x^2 + \eta^2} - 2 \pi^4 x^3 \gamma \eta^2 \theta - \pi^4 x \gamma \eta^4 \theta + 2 \pi^4 x^2 \gamma \eta^2 \sqrt{x^2 + \eta^2} \theta \right) } / \right. \right.$   
 $\left. \left( \sqrt{-64 \pi^4 x \gamma \eta^2 \theta + 16 \pi^2 x^3 \gamma^2 \theta^2 + x^3 \gamma^3 \theta^3} \right) \right\} \right\}$

Solve[ $\frac{2 (\pi - \pi \sin[\beta]^2 + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}{-1 + \sin[\beta]^2} \times 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) r ==$   
 $(2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)}) (2 \pi \sqrt{\eta^2 + x^2} - 2 \pi x), x]$   
 $\left( 4 \sqrt{ \left( 8 \pi^6 x \eta^4 - 8 \pi^6 \eta^4 \sqrt{x^2 + \eta^2} - 2 \pi^4 x^3 \gamma \eta^2 \theta - \pi^4 x \gamma \eta^4 \theta + 2 \pi^4 x^2 \gamma \eta^2 \sqrt{x^2 + \eta^2} \theta \right) } / \right.$   
 $\left. \left( \sqrt{-64 \pi^4 x \gamma \eta^2 \theta + 16 \pi^2 x^3 \gamma^2 \theta^2 + x^3 \gamma^3 \theta^3} \right) \right)$



$$\text{Solve}\left[\gamma \times \theta \ r = \left(2 \pi \ r - 2 \pi \sqrt{(r^2 - \eta^2)}\right) \left(2 \pi \ r - 2 \pi \sqrt{(r^2 - \eta^2)}\right), r\right]$$

$$\left\{\left\{r \rightarrow\right.\right.$$

$$\frac{x \gamma \theta}{48 \pi^2} - \left(-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4\right) / \left(48 \pi^2 x \gamma \theta \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 +\right.\right.$$

$$\left.\left.x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right) +$$

$$\frac{1}{48 \pi^2 x \gamma \theta} \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 +\right.$$

$$\left.\left.1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right\},$$

$$\left\{r \rightarrow \frac{x \gamma \theta}{48 \pi^2} + \left((1 + i \sqrt{3}) \left(-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4\right)\right) / \left(96 \pi^2 x \gamma \theta \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 +\right.\right.$$

$$\left.\left.576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right) -$$

$$\frac{1}{96 \pi^2 x \gamma \theta} (1 - i \sqrt{3}) \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 +\right.$$

$$\left.\left.1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right\},$$

$$\left\{r \rightarrow \frac{x \gamma \theta}{48 \pi^2} + \left((1 - i \sqrt{3}) \left(-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4\right)\right) / \left(96 \pi^2 x \gamma \theta \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 +\right.\right.$$

$$\left.\left.x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right) -$$

$$\frac{1}{96 \pi^2 x \gamma \theta} (1 + i \sqrt{3}) \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 +\right.$$

$$\left.\left.1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right\}$$

$$\frac{x \gamma \theta}{48 \pi^2} - \left(-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4\right) /$$

$$\left(48 \pi^2 x \gamma \theta \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 +\right.\right.$$

$$\left.\left.1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right) +$$

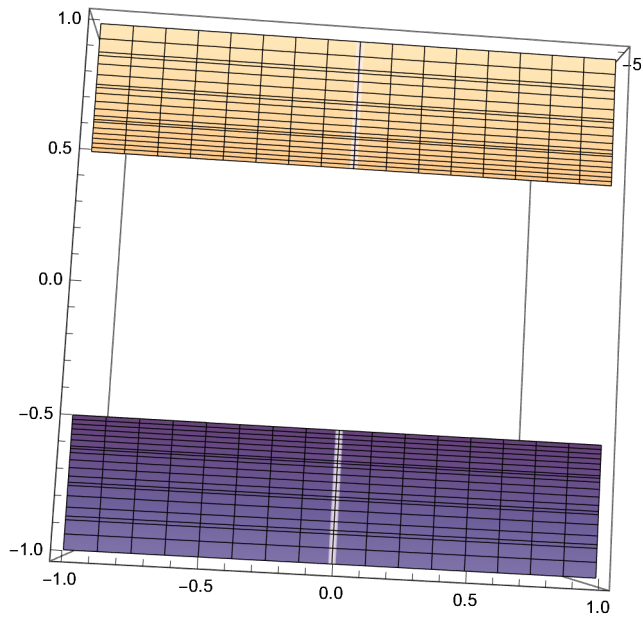
$$\frac{1}{48 \pi^2 x \gamma \theta} \left(55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 +\right.$$

$$\left.\left.1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6}\right)^{1/3}\right)$$

$$\theta := \frac{2(4\pi^2 + \pi\gamma)}{2\pi + \gamma}$$

ContourPlot3D[

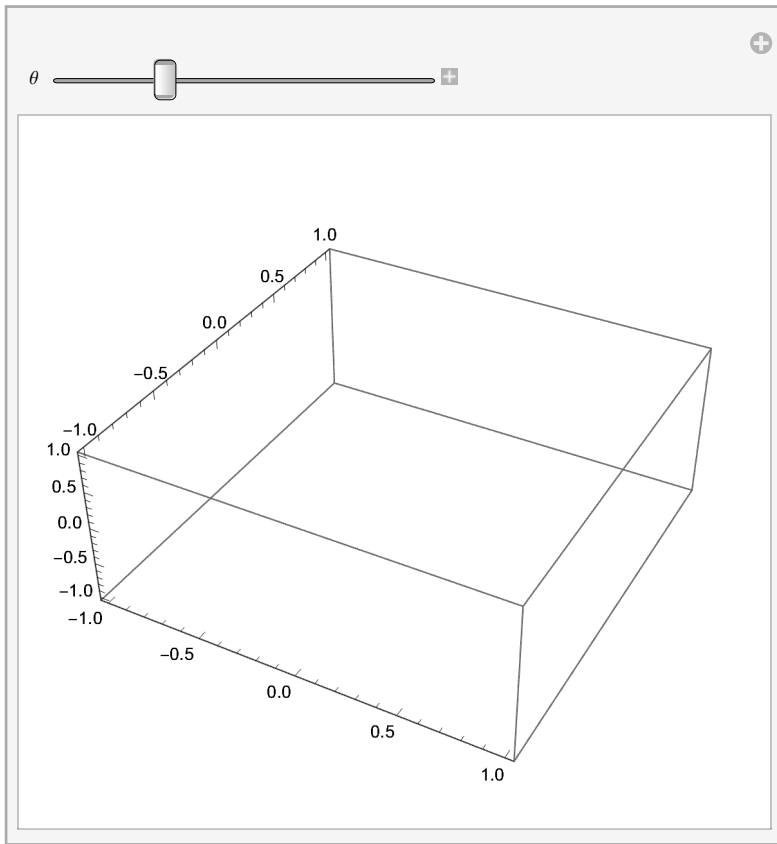
$$\frac{x \gamma \theta}{48 \pi^2} - (-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4) / \left( 48 \pi^2 x \gamma \theta \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + \right. \right. \\ \left. \left. x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3} \right) + \\ \frac{1}{48 \pi^2 x \gamma \theta} \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\gamma, -2 \pi, 2 \pi\} ]$$



$$\gamma := \frac{2 \pi \theta}{2 \pi - \theta}$$

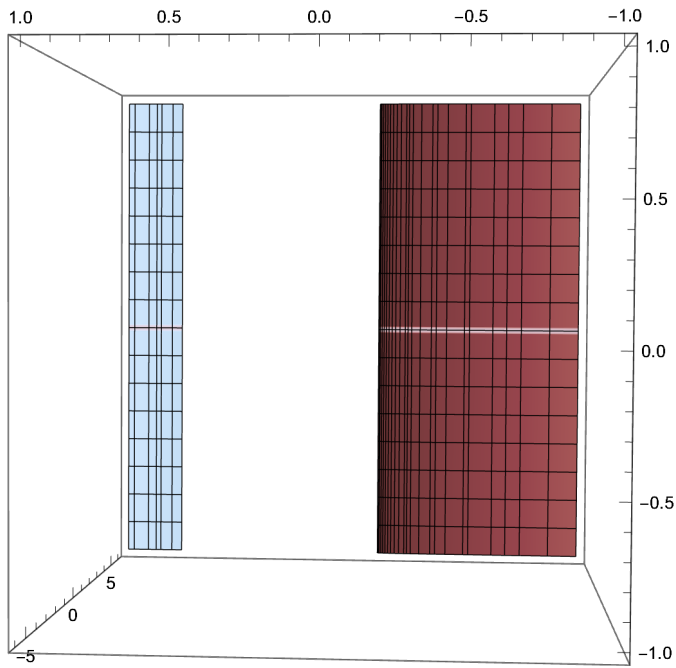
Manipulate[Plot3D[

$$\frac{x \gamma \theta}{48 \pi^2} - (-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4) / \left( 48 \pi^2 x \gamma \theta \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + \right. \right. \\ \left. \left. x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3} \right) + \\ \frac{1}{48 \pi^2 x \gamma \theta} \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \right. \\ \left. \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$

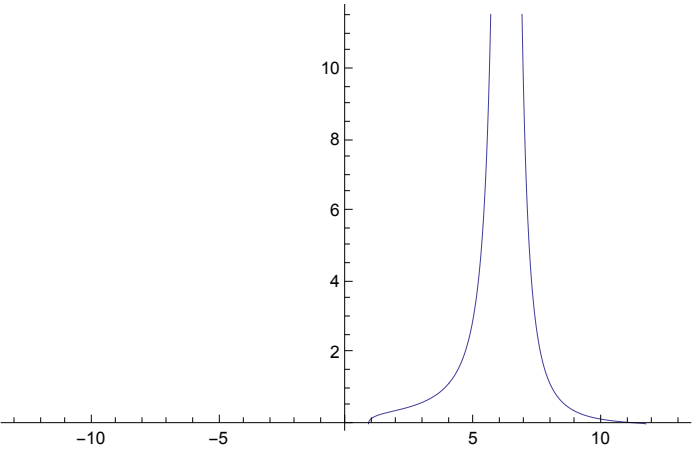


ContourPlot3D[

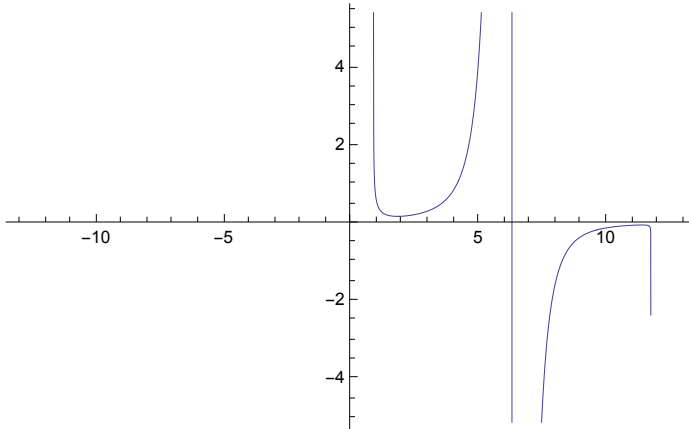
$$\frac{x \gamma \theta}{48 \pi^2} - (-384 \pi^4 x^2 \gamma^2 \eta^2 \theta^2 - x^4 \gamma^4 \theta^4) / \left( 48 \pi^2 x \gamma \theta \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + \right. \right. \\ \left. \left. x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3} \right) + \\ \frac{1}{48 \pi^2 x \gamma \theta} \left( 55296 \pi^8 x^2 \gamma^2 \eta^4 \theta^2 + 576 \pi^4 x^4 \gamma^4 \eta^2 \theta^4 + x^6 \gamma^6 \theta^6 + 1536 \sqrt{3} \pi^6 \sqrt{432 \pi^4 x^4 \gamma^4 \eta^8 \theta^4 + x^6 \gamma^6 \eta^6 \theta^6} \right)^{1/3}, \{x, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



$$\text{Plot}\left[\sqrt{\left(\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi-\theta) \theta}}{\pi^3}}+\frac{4 \sqrt{(4 \pi-\theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4-32 \pi^3 \theta+24 \pi^2 \theta^2-8 \pi \theta^3+\theta^4}}\right)^2-\frac{\left(\frac{2 \pi^{3/2} \sqrt{-\frac{\sqrt{(4 \pi-\theta) \theta}}{\pi^3}}+\frac{4 \sqrt{(4 \pi-\theta) \theta}}{\pi^2 \theta}}{\sqrt{16 \pi^4-32 \pi^3 \theta+24 \pi^2 \theta^2-8 \pi \theta^3+\theta^4}}\right) \bigg/ (6 \theta)}{6 (\theta) \pi}}{\sqrt{4 \pi \theta-\theta^2}}}\right)^2},\{\theta,-13,13\}]$$



$$\text{Plot} \left[ \left( \frac{4 \pi^3 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
\frac{4 \pi^5 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
\frac{4 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
\left. \frac{4 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \right. \\
\left. \frac{4 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) / \\
\left( 2 \sqrt{\left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
\left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) \right), \{\theta, -13, 13\} \right]$$

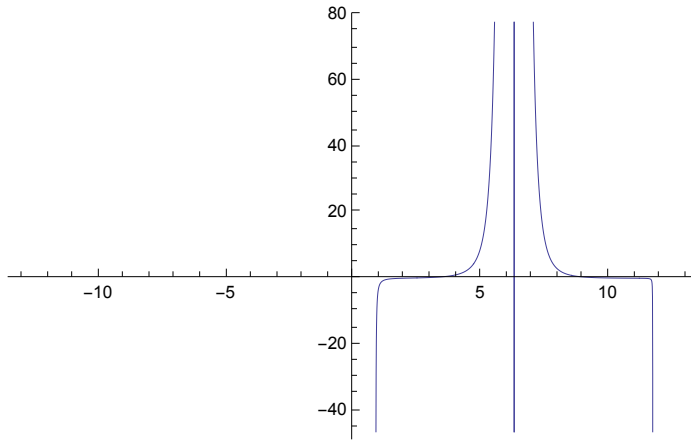


$$\text{Plot} \left[ - \left( \frac{4 \pi^3 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
\frac{4 \pi^5 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
\left. \frac{4 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \right. \\
\left. \frac{4 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} \right) \right]$$

$$\begin{aligned}
& \frac{4 \pi^3 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2} + \\
& \frac{4 \pi^5 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2} + \\
& \frac{4 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right)^2 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \Bigg)^2 / \\
& \left( 4 \left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
& \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \right)^{3/2} \right) + \\
& \left( 4 \pi^3 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \left. \left. \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) / \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right) - \\
& \left( 4 \pi^5 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \left. \left. \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right) \right) - \\
& \left( 8 \pi^3 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \right. \\
& \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 + \left( 8 \pi^5 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \right. \\
& \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{8 \pi^5 (4 \pi - 2 \theta) \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} + \\
& \frac{8 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} - \\
& \frac{8 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} - \\
& \frac{4 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{4 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} - \\
& \left( \frac{8 \pi^5 (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} - \right. \\
& \quad \left. \frac{8 \pi^5 (4 \pi - 2 \theta)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \right. \\
& \quad \left. \frac{8 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) / \\
& \left( 2 \sqrt{\left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
& \quad \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) \right), \{\theta, -13, 13\} ]
\end{aligned}$$





$$\begin{aligned}
 & \text{Plot} \left[ \left( 3 \left( \frac{4 \pi^3 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \right. \\
 & \quad \frac{4 \pi^5 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
 & \quad \frac{4 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
 & \quad \frac{4 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
 & \quad \left. \left. \frac{4 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right)^3 \right) / \right. \\
 & \quad \left( 8 \left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
 & \quad \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right)^{5/2} \right) - \\
 & \quad \left( 3 \left( \left( 4 \pi^3 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) / (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4) - \right.
 \end{aligned}$$

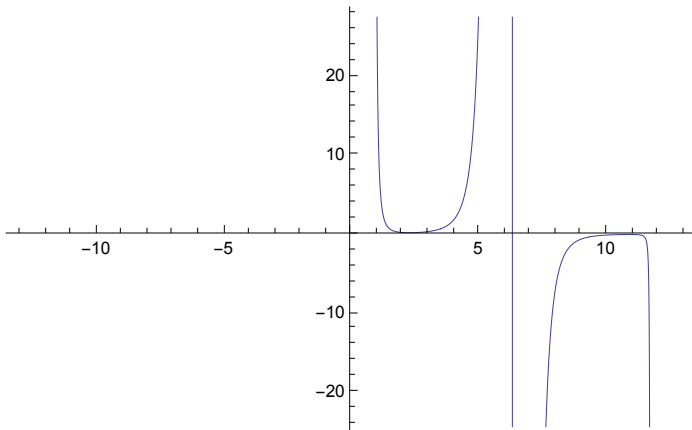
$$\begin{aligned}
& \left( 4 \pi^5 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \left. \left. \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4) \right) - \left( 8 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - \right. \\
& \quad \left. 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 + \left( 8 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) + \\
& \frac{8 \pi^5 (4 \pi - 2 \theta) \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} + \\
& \frac{8 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} - \\
& \frac{8 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} - \\
& \frac{4 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{4 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} - \\
& \left( 8 \pi^5 (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) - \\
& \frac{8 \pi^5 (4 \pi - 2 \theta)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} -
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{8 \pi^5 \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} \right) \\
& \left( \frac{4\pi^3 \left( -\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right)}{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} - \right. \\
& \frac{4\pi^5 \left( -\frac{4\pi-2\theta}{2\pi^3\sqrt{(4\pi-\theta)\theta}} + \frac{2(4\pi-2\theta)}{\pi^2\theta\sqrt{(4\pi-\theta)\theta}} - \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^2} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} - \\
& \frac{4\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} + \\
& \frac{4\pi^5 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} + \\
& \left. \frac{4\pi^5 (4\pi - 2\theta) \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} \right) \Bigg/ \\
& \left( 4 \left( \frac{4\pi^3 \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)}{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} - \right. \right. \\
& \left. \left. \frac{4\pi^5 \left( -\frac{\sqrt{(4\pi-\theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} \right)^{3/2} \right) + \\
& \left( \left( 4\pi^3 \left( -\frac{3(4\pi-2\theta)^3}{8\pi^3((4\pi-\theta)\theta)^{5/2}} + \frac{3(4\pi-2\theta)^3}{2\pi^2\theta((4\pi-\theta)\theta)^{5/2}} - \frac{3(4\pi-2\theta)}{2\pi^3((4\pi-\theta)\theta)^{3/2}} + \right. \right. \right. \\
& \frac{3(4\pi-2\theta)^2}{\pi^2\theta^2((4\pi-\theta)\theta)^{3/2}} + \frac{6(4\pi-2\theta)}{\pi^2\theta((4\pi-\theta)\theta)^{3/2}} + \frac{12(4\pi-2\theta)}{\pi^2\theta^3\sqrt{(4\pi-\theta)\theta}} + \\
& \left. \left. \frac{12}{\pi^2\theta^2\sqrt{(4\pi-\theta)\theta}} - \frac{24\sqrt{(4\pi-\theta)\theta}}{\pi^2\theta^4} \right) \right) \Bigg/ (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4) - \\
& \left( 4\pi^5 \left( -\frac{3(4\pi-2\theta)^3}{8\pi^3((4\pi-\theta)\theta)^{5/2}} + \frac{3(4\pi-2\theta)^3}{2\pi^2\theta((4\pi-\theta)\theta)^{5/2}} - \frac{3(4\pi-2\theta)}{2\pi^3((4\pi-\theta)\theta)^{3/2}} + \right. \right. \\
& \left. \left. \frac{3(4\pi-2\theta)^2}{\pi^2\theta^2((4\pi-\theta)\theta)^{3/2}} + \frac{6(4\pi-2\theta)}{\pi^2\theta((4\pi-\theta)\theta)^{3/2}} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{12 (4 \pi - 2 \theta)}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{12}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{24 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^4} \right) / \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4) \right) - \\
& \left( 12 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \right. \right. \\
& \quad \left. \left. \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) / \\
& (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 + \left( 12 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \quad \left. \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \Bigg) / \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) + \\
& \left( 12 \pi^5 (4 \pi - 2 \theta) \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \quad \left. \left. \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4) \right) + \\
& \left( 24 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \right. \\
& \quad \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \Bigg) / \\
& (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 - \left( 24 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \right. \\
& \quad \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \Bigg) / \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) - \left( 12 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \right. \\
& \quad \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 + \left( 12 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \right. \\
& \quad \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) - \\
& \quad \left( 24 \pi^5 (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) - \\
& \quad \frac{24 \pi^5 (4 \pi - 2 \theta)^2 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
& \quad \frac{24 \pi^5 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
& \quad \frac{24 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^4} + \\
& \quad \frac{24 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^4} + \\
& \quad \left( 24 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 - \\
& \quad \left( 24 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) + \\
& \quad \left( 24 \pi^5 (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{4 \pi^3 (-48 \pi + 24 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{4 \pi^5 (-48 \pi + 24 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} - \\
& \frac{12 \pi^5 (4 \pi - 2 \theta) (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \left( \frac{24 \pi^5 (4 \pi - 2 \theta)^2 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \right. \\
& \left. \frac{24 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \right. \\
& \left. \frac{24 \pi^5 (4 \pi - 2 \theta)^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} + \right. \\
& \left. \frac{48 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) / \\
& \left( 2 \sqrt{\left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right.} \right. \\
& \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) \right), \{\theta, -13, 13\}
\end{aligned}$$



$$\text{Plot} \left[ -15 \left( \frac{4 \pi^3 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right.$$

$$\begin{aligned}
& \frac{4 \pi^5 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
& \frac{4 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{4 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{4 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \Bigg) \Bigg/ \\
& \left( 16 \left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
& \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right)^{7/2} \right) + \\
& \left( 9 \left( \left( 4 \pi^3 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \\
& \left. \left. \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) \Bigg/ (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4) - \\
& \left( 4 \pi^5 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \\
& \left. \left. \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) \Bigg/ \\
& ((4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)) - \\
& \left( 8 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) \Bigg/ \\
& (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 + \left( 8 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) + \\
& \frac{8\pi^5 (4\pi - 2\theta) \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} + \\
& \frac{8\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3} - \\
& \frac{8\pi^5 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3} - \\
& \frac{4\pi^3 (48\pi^2 - 48\pi\theta + 12\theta^2) \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} + \\
& \frac{4\pi^5 (48\pi^2 - 48\pi\theta + 12\theta^2) \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} - \\
& \left( \frac{8\pi^5 (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(4\pi\theta - \theta^2)^3 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} \right. \\
& \quad \left. - \frac{8\pi^5 (4\pi - 2\theta)^2 \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} \right) \Bigg/ \\
& \left( \frac{4\pi^3 \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right)}{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4} - \right. \\
& \quad \frac{4\pi^5 \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right)}{(4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} - \\
& \quad \left. \frac{4\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} \right) +
\end{aligned}$$



$$\begin{aligned}
& \frac{4 \pi^5 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2} + \\
& \frac{4 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \Bigg)^2 \Bigg/ \\
& \left( 4 \left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
& \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \right)^{5/2} \right) - \\
& \left( 3 \left( \left( 4 \pi^3 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} \right. \right. \right. \right. \\
& \left. \left. \left. \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) \Bigg/ \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \right. \right. \\
& \left. \left. \theta^4 \right) - \left( 4 \pi^5 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \right. \right. \\
& \left. \left. \left. \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \right) \Bigg/ \right. \\
& \left. \left( (4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right) \right) - \left( 8 \pi^3 \left( -32 \pi^3 + 48 \pi^2 \theta - \right. \right. \right. \\
& \left. \left. \left. 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) \Bigg/ \right. \\
& \left. \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 + \left( 8 \pi^5 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \right. \right. \\
& \left. \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) \Bigg/ \right. \\
& \left. \left( (4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 \right) + \right. \\
& \left. \frac{8 \pi^5 (4 \pi - 2 \theta) \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^2 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{8 \pi^3 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^3} - \\
& \frac{8 \pi^5 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^3} - \\
& \frac{4 \pi^3 \left( 48 \pi^2 - 48 \pi \theta + 12 \theta^2 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2} + \\
& \frac{4 \pi^5 \left( 48 \pi^2 - 48 \pi \theta + 12 \theta^2 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2} - \left( 8 \pi^5 (4 \pi - 2 \theta) \right. \\
& \quad \left. \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( \left( 4 \pi \theta - \theta^2 \right)^2 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 \right) - \\
& \quad \frac{8 \pi^5 (4 \pi - 2 \theta)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right)^3 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} - \\
& \quad \left. \frac{8 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right)^2 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \right)^2 / \\
& \left( 4 \left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
& \quad \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{\left( 4 \pi \theta - \theta^2 \right) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \right)^{3/2} \right) - \\
& \left( \left( 4 \pi^3 \left( -\frac{3 (4 \pi - 2 \theta)^3}{8 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} + \frac{3 (4 \pi - 2 \theta)^3}{2 \pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} - \frac{3 (4 \pi - 2 \theta)}{2 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} + \right. \right. \right. \\
& \quad \left. \frac{3 (4 \pi - 2 \theta)^2}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{3/2}} + \frac{6 (4 \pi - 2 \theta)}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{12 (4 \pi - 2 \theta)}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \right. \\
& \quad \left. \left. \frac{12}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{24 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^4} \right) \right) / \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right) - \\
& \left( 4 \pi^5 \left( -\frac{3 (4 \pi - 2 \theta)^3}{8 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} + \frac{3 (4 \pi - 2 \theta)^3}{2 \pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} - \frac{3 (4 \pi - 2 \theta)}{2 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3(4\pi - 2\theta)^2}{\pi^2 \theta^2 ((4\pi - \theta)\theta)^{3/2}} + \frac{6(4\pi - 2\theta)}{\pi^2 \theta ((4\pi - \theta)\theta)^{3/2}} + \\
& \left( \frac{12(4\pi - 2\theta)}{\pi^2 \theta^3 \sqrt{(4\pi - \theta)\theta}} + \frac{12}{\pi^2 \theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{24\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^4} \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4) \right) - \\
& \left( 12\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2 \theta ((4\pi - \theta)\theta)^{3/2}} + \right. \right. \\
& \left. \left. \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \frac{4(4\pi - 2\theta)}{\pi^2 \theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^3} \right) \right) \Bigg/ \\
& (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 + \left( 12\pi^5 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2 \theta ((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \right. \\
& \left. \frac{4(4\pi - 2\theta)}{\pi^2 \theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^3} \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) + \\
& \left( 12\pi^5 (4\pi - 2\theta) \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2 \theta ((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \left. \left. \frac{4(4\pi - 2\theta)}{\pi^2 \theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^3} \right) \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4) \right) + \\
& \left( 24\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \right. \\
& \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right) \Bigg/ \\
& (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 - \left( 24\pi^5 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \right. \\
& \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 \right) - \left( 12\pi^3 (48\pi^2 - 48\pi\theta + 12\theta^2) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right) \Bigg/ \\
& \left( (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 + \left( 12\pi^5 (48\pi^2 - 48\pi\theta + 12\theta^2) \right. \right. \\
& \left. \left. - \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right) \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) - \\
& \left( 24\pi^5 (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \left. - \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right) \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) - \\
& \frac{24\pi^5 (4\pi - 2\theta)^2 \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right)}{(4\pi\theta - \theta^2)^3 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} - \\
& \frac{24\pi^5 \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2 \theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta^2} \right)}{(4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)} - \\
& \frac{24\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^3 \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^4} + \\
& \frac{24\pi^5 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^3 \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right)}{(4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^4} + \\
& \left( 24\pi^3 (48\pi^2 - 48\pi\theta + 12\theta^2) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \left. - \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right) \right) \Bigg/ (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 - \\
& \left( 24\pi^5 (48\pi^2 - 48\pi\theta + 12\theta^2) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \left. - \left( -\frac{\sqrt{(4\pi - \theta)\theta}}{\pi^3} + \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2 \theta} \right) \right) \Bigg/ \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 \right) + \left( 24\pi^5 (4\pi - 2\theta) \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \Bigg) / \\
& \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) - \\
& \frac{4 \pi^3 (-48 \pi + 24 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{4 \pi^5 (-48 \pi + 24 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} - \\
& \frac{12 \pi^5 (4 \pi - 2 \theta) (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \left( 24 \pi^5 (4 \pi - 2 \theta)^2 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) + \\
& \frac{24 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{24 \pi^5 (4 \pi - 2 \theta)^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} + \\
& \frac{48 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \Bigg) \\
& \left( \frac{4 \pi^3 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \\
& \frac{4 \pi^5 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
& \left. \frac{4 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{4 \pi^5 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2} + \\
& \frac{4 \pi^5 (4 \pi - 2 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \Bigg) / \\
& \left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \\
& \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)} \right)^{3/2} + \\
& \left( \frac{1}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} 4 \pi^3 \left( \frac{15 (4 \pi - 2 \theta)^4}{16 \pi^3 ((4 \pi - \theta) \theta)^{7/2}} - \frac{15 (4 \pi - 2 \theta)^4}{4 \pi^2 \theta ((4 \pi - \theta) \theta)^{7/2}} + \right. \right. \\
& \frac{9 (4 \pi - 2 \theta)^2}{2 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} - \frac{6 (4 \pi - 2 \theta)^3}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{5/2}} - \frac{18 (4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} + \\
& \frac{3}{\pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{12 (4 \pi - 2 \theta)^2}{\pi^2 \theta^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{24 (4 \pi - 2 \theta)}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{3/2}} - \\
& \left. \frac{12}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} - \frac{48 (4 \pi - 2 \theta)}{\pi^2 \theta^4 \sqrt{(4 \pi - \theta) \theta}} - \frac{48}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{96 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^5} \right) - \\
& \left( 4 \pi^5 \left( \frac{15 (4 \pi - 2 \theta)^4}{16 \pi^3 ((4 \pi - \theta) \theta)^{7/2}} - \frac{15 (4 \pi - 2 \theta)^4}{4 \pi^2 \theta ((4 \pi - \theta) \theta)^{7/2}} + \frac{9 (4 \pi - 2 \theta)^2}{2 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} - \right. \right. \\
& \frac{6 (4 \pi - 2 \theta)^3}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{5/2}} - \frac{18 (4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} + \frac{3}{\pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \\
& \frac{12 (4 \pi - 2 \theta)^2}{\pi^2 \theta^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{24 (4 \pi - 2 \theta)}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{3/2}} - \frac{12}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} - \\
& \left. \frac{48 (4 \pi - 2 \theta)}{\pi^2 \theta^4 \sqrt{(4 \pi - \theta) \theta}} - \frac{48}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{96 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^5} \right) \Bigg) / \\
& ((4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)) - \\
& \left( 16 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \left( -\frac{3 (4 \pi - 2 \theta)^3}{8 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} + \frac{3 (4 \pi - 2 \theta)^3}{2 \pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} - \right. \right. \\
& \frac{3 (4 \pi - 2 \theta)}{2 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} + \frac{3 (4 \pi - 2 \theta)^2}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{3/2}} + \frac{6 (4 \pi - 2 \theta)}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} +
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{12 (4 \pi - 2 \theta)}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{12}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{24 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^4} \right) \Bigg/ \\
& \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^2 + \left( 16 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \left( -\frac{3 (4 \pi - 2 \theta)^3}{8 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} + \frac{3 (4 \pi - 2 \theta)^3}{2 \pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} - \right. \\
& \frac{3 (4 \pi - 2 \theta)}{2 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} + \frac{3 (4 \pi - 2 \theta)^2}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{3/2}} + \frac{6 (4 \pi - 2 \theta)}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \\
& \left. \frac{12 (4 \pi - 2 \theta)}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{12}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{24 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^4} \right) \Bigg/ \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) + \\
& \left( 16 \pi^5 (4 \pi - 2 \theta) \left( -\frac{3 (4 \pi - 2 \theta)^3}{8 \pi^3 ((4 \pi - \theta) \theta)^{5/2}} + \frac{3 (4 \pi - 2 \theta)^3}{2 \pi^2 \theta ((4 \pi - \theta) \theta)^{5/2}} - \right. \right. \\
& \frac{3 (4 \pi - 2 \theta)}{2 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} + \frac{3 (4 \pi - 2 \theta)^2}{\pi^2 \theta^2 ((4 \pi - \theta) \theta)^{3/2}} + \frac{6 (4 \pi - 2 \theta)}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \\
& \left. \frac{12 (4 \pi - 2 \theta)}{\pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{12}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{24 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^4} \right) \Bigg/ \\
& \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4) \right) + \\
& \left( 48 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \right. \right. \\
& \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \Bigg) \Bigg/ \\
& \left( 16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4 \right)^3 - \left( 48 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \right. \\
& \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \right. \\
& \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \Bigg) \Bigg/ \\
& \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) - \\
& \left( 24 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( \frac{(4 \pi - 2 \theta)^2}{4 \pi^3 ((4 \pi - \theta) \theta)^{3/2}} - \frac{(4 \pi - 2 \theta)^2}{\pi^2 \theta ((4 \pi - \theta) \theta)^{3/2}} + \right. \right. \\
& \left. \frac{1}{\pi^3 \sqrt{(4 \pi - \theta) \theta}} - \frac{4 (4 \pi - 2 \theta)}{\pi^2 \theta^2 \sqrt{(4 \pi - \theta) \theta}} - \frac{4}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} + \frac{8 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^3} \right) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 + \left( 24\pi^5 (48\pi^2 - 48\pi\theta + 12\theta^2) \right. \\
& \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2\theta ((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \right. \\
& \left. \frac{4(4\pi - 2\theta)}{\pi^2\theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^3} \right) \Bigg) / \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) - \\
& \left( 48\pi^5 (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2\theta ((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \right. \\
& \left. \frac{4(4\pi - 2\theta)}{\pi^2\theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^3} \right) \Bigg) / \\
& \left( (4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) - \\
& \left( 48\pi^5 (4\pi - 2\theta)^2 \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2\theta ((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \left. \frac{4(4\pi - 2\theta)}{\pi^2\theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^3} \right) \Bigg) / \\
& \left( (4\pi\theta - \theta^2)^3 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4) \right) - \\
& \left( 48\pi^5 \left( \frac{(4\pi - 2\theta)^2}{4\pi^3 ((4\pi - \theta)\theta)^{3/2}} - \frac{(4\pi - 2\theta)^2}{\pi^2\theta ((4\pi - \theta)\theta)^{3/2}} + \frac{1}{\pi^3 \sqrt{(4\pi - \theta)\theta}} - \right. \right. \\
& \left. \frac{4(4\pi - 2\theta)}{\pi^2\theta^2 \sqrt{(4\pi - \theta)\theta}} - \frac{4}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} + \frac{8\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^3} \right) \Bigg) / \\
& \left( (4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4) \right) - \\
& \left( 96\pi^3 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^3 \right. \\
& \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \Bigg) / \\
& (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^4 + \left( 96\pi^5 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^3 \right. \\
& \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \Bigg) /
\end{aligned}$$

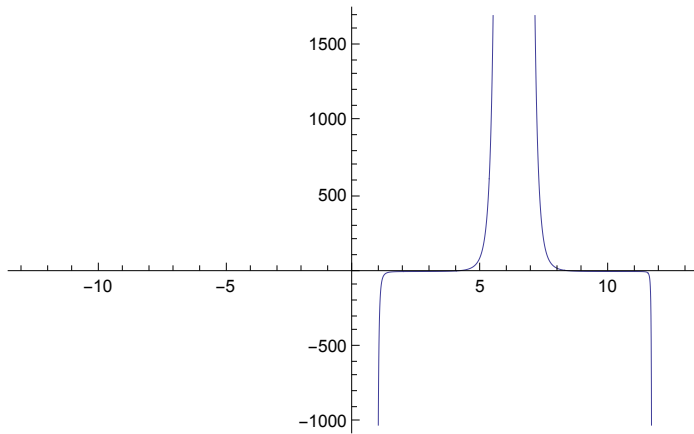


$$\begin{aligned}
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^4 \right) + \\
& \left( 96\pi^3 (48\pi^2 - 48\pi\theta + 12\theta^2) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \quad \left. \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 - \\
& \left( 96\pi^5 (48\pi^2 - 48\pi\theta + 12\theta^2) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \quad \left. \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 \right) + \\
& \left( 96\pi^5 (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2 \right. \\
& \quad \left. \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^3 \right) - \\
& \frac{16\pi^3 (-48\pi + 24\theta) \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} + \\
& \frac{16\pi^5 (-48\pi + 24\theta) \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right)}{(4\pi\theta - \theta^2) (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2} - \\
& \left( 48\pi^5 (4\pi - 2\theta) (48\pi^2 - 48\pi\theta + 12\theta^2) \right. \\
& \quad \left. \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (4\pi\theta - \theta^2)^2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) + \\
& \left( 96\pi^5 (4\pi - 2\theta)^2 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right. \\
& \quad \left. \left( -\frac{4\pi - 2\theta}{2\pi^3 \sqrt{(4\pi - \theta)\theta}} + \frac{2(4\pi - 2\theta)}{\pi^2\theta \sqrt{(4\pi - \theta)\theta}} - \frac{4\sqrt{(4\pi - \theta)\theta}}{\pi^2\theta^2} \right) \right) / \\
& \left( (4\pi\theta - \theta^2)^3 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^2 \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 96 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) + \\
& \quad \frac{96 \pi^5 (4 \pi - 2 \theta)^3 \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} + \\
& \quad \frac{192 \pi^5 (4 \pi - 2 \theta) \left( -\frac{4 \pi - 2 \theta}{2 \pi^3 \sqrt{(4 \pi - \theta) \theta}} + \frac{2 (4 \pi - 2 \theta)}{\pi^2 \theta \sqrt{(4 \pi - \theta) \theta}} - \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta^2} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} + \\
& \quad \frac{96 \pi^3 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^4 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^5} - \\
& \quad \frac{96 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^4 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^5} - \\
& \quad \left( 144 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^4 + \\
& \quad \left( 144 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^4 \right) - \\
& \quad \left( 96 \pi^5 (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^4 \right) + \\
& \quad \frac{24 \pi^3 (48 \pi^2 - 48 \pi \theta + 12 \theta^2)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} - \\
& \quad \frac{24 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} +
\end{aligned}$$

$$\begin{aligned}
& \left( 32 \pi^3 (-48 \pi + 24 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 - \\
& \left( 32 \pi^5 (-48 \pi + 24 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) + \\
& \left( 96 \pi^5 (4 \pi - 2 \theta) (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3) \right. \\
& \quad \left. \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) - \\
& \left( 96 \pi^5 (4 \pi - 2 \theta)^2 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \quad \left( (4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3 \right) - \\
& \frac{96 \pi^5 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^3} - \\
& \frac{96 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} - \\
& \frac{16 \pi^5 (4 \pi - 2 \theta) (-48 \pi + 24 \theta) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{96 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{48 \pi^5 (4 \pi - 2 \theta)^2 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} + \\
& \frac{48 \pi^5 (48 \pi^2 - 48 \pi \theta + 12 \theta^2) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2} -
\end{aligned}$$

$$\begin{aligned}
& \left( 96 \pi^5 (4 \pi - 2 \theta)^3 \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2)^4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) - \\
& \left( 192 \pi^5 (4 \pi - 2 \theta) \left( -32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3 \right) \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right) \right) / \\
& \left( (4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^2 \right) - \\
& \frac{96 \pi^5 (4 \pi - 2 \theta)^4 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^5 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
& \frac{288 \pi^5 (4 \pi - 2 \theta)^2 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} - \\
& \frac{96 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2)^3 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \Bigg) / \\
& \left( 2 \sqrt{\left( \frac{4 \pi^3 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4} - \right. \right. \\
& \left. \left. \frac{4 \pi^5 \left( -\frac{\sqrt{(4 \pi - \theta) \theta}}{\pi^3} + \frac{4 \sqrt{(4 \pi - \theta) \theta}}{\pi^2 \theta} \right)}{(4 \pi \theta - \theta^2) (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)} \right) \right), \{\theta, -13, 13\} ]
\end{aligned}$$



A very large output was generated. Showing a sample of it.

Plot

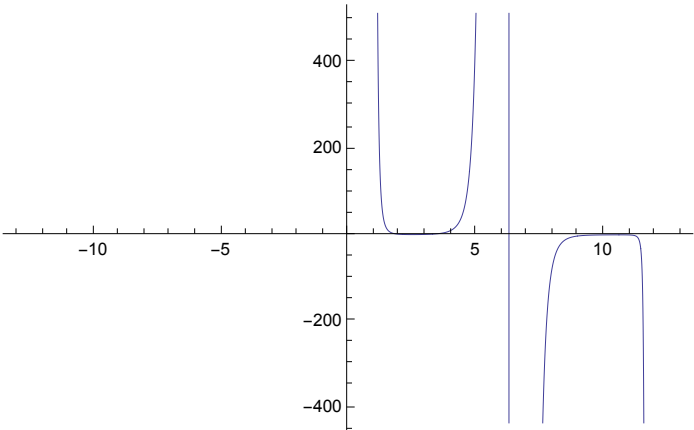
$$\frac{105 \left( \langle\langle 6 \rangle\rangle + \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle^2 \langle\langle 1 \rangle\rangle} \right)^5}{32 \left( \frac{4 \pi^3 \left( -\frac{\sqrt{\langle\langle 1 \rangle\rangle}}{\pi^3} + \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle} \right) - \frac{\langle\langle 1 \rangle\rangle}{16 \pi^4 - 32 \pi^3 \theta + \langle\langle 1 \rangle\rangle - \langle\langle 1 \rangle\rangle + \theta^4}}{\langle\langle 1 \rangle\rangle} \right)^{9/2}} - \frac{75 (\langle\langle 1 \rangle\rangle) (\langle\langle 1 \rangle\rangle)^3}{8 \left( \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle} - \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle} \right)^{7/2}} + \frac{\langle\langle 1 \rangle\rangle}{8 \langle\langle 1 \rangle\rangle \langle\langle 1 \rangle\rangle} +$$
$$\langle\langle 1 \rangle\rangle - \frac{\langle\langle 1 \rangle\rangle}{2 \langle\langle 1 \rangle\rangle \langle\langle 1 \rangle\rangle} - \frac{5 (\langle\langle 1 \rangle\rangle) \left( \langle\langle 6 \rangle\rangle + \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle} \right)}{4 (\langle\langle 1 \rangle\rangle - \langle\langle 1 \rangle\rangle)^{3/2}} + \frac{\langle\langle 115 \rangle\rangle + \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle \langle\langle 1 \rangle\rangle}}{2 \sqrt{\frac{4 \pi^3 \left( -\frac{\sqrt{\langle\langle 1 \rangle\rangle}}{\pi^3} + \frac{\langle\langle 1 \rangle\rangle}{\langle\langle 1 \rangle\rangle} \right) - \frac{\langle\langle 1 \rangle\rangle}{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}{\langle\langle 1 \rangle\rangle} - \frac{\langle\langle 1 \rangle\rangle}{(\langle\langle 1 \rangle\rangle) \langle\langle 1 \rangle\rangle}}}$$

show less

show more

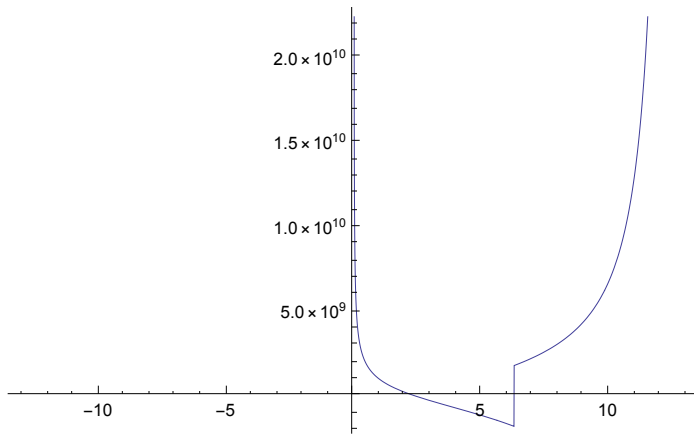
show all

set size limit...



$$D \left[ \sqrt{\left( \left( \frac{2 (2.99792 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 - \frac{\sqrt{\left( \frac{2 (2.99792 \times 10^8) (6) (\theta) \pi}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 (4 \pi - \theta) \theta}}{2 \pi} \right)^2}, \theta \right]$$
$$\left( -\frac{1.27733 \times 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \right.$$
$$\left. \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right) /$$
$$\left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2}} \right)$$

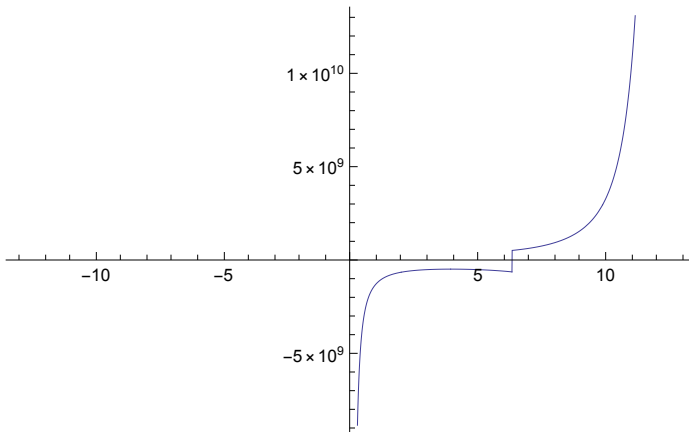
$$\text{Plot}\left[\left(-\frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot 10^{18} \theta^3}{4\pi\theta - \theta^2}\right) / \left(2 \sqrt{\frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}}\right), \{\theta, -13, 13\}]$$



$$\begin{aligned}
& D \left[ \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) / \\
& \quad \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \theta \Big] \\
& - \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 / \\
& \quad \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \quad \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) / \\
& \quad \left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right)
\end{aligned}$$

Plot[

$$\begin{aligned}
& - \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 / \\
& \quad \left( 4 \left( \frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \quad \left( \frac{2.5546553178259708 \cdot 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.471017515008 \cdot 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{5.1093106356519417 \cdot 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) / \\
& \quad \left( 2 \sqrt{\frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \{\theta, -13, 13\} ]
\end{aligned}$$





$$\begin{aligned}
& D \left[ - \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 / \\
& \quad \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \quad \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 / \\
& \quad \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \theta] \\
& \quad \left( 3 \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 / \\
& \quad \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \quad \left( 3 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \left. \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \right.
\end{aligned}$$

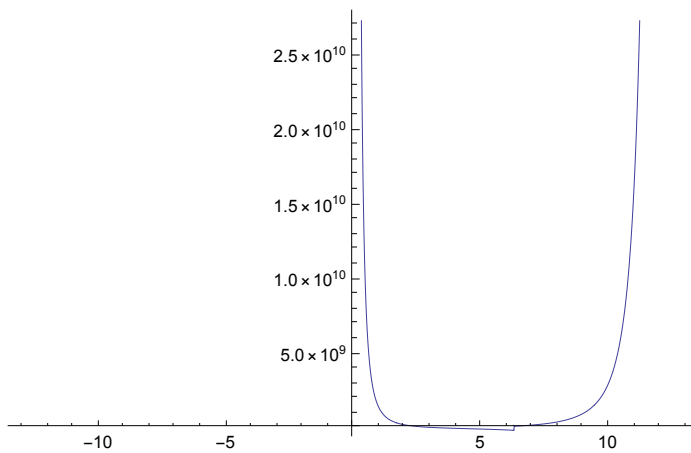
$$\begin{aligned}
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right) / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) / \\
& \left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right)
\end{aligned}$$

Plot[

$$\begin{aligned}
& \left( 3 \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \left. \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^3 \right) / \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 3 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4 \pi \theta - \theta^2} \right) \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot \pi^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4 \pi \theta - \theta^2} \right) \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{7.663965953477913 \cdot \pi^{20} (4 \pi - 2 \theta)^3 \theta^2}{(4 \pi \theta - \theta^2)^4} + \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \\
& \quad \left. \frac{1.5327931906955826 \cdot \pi^{21} (4 \pi - 2 \theta)^2 \theta}{(4 \pi \theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{5.8239157635072 \cdot 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \frac{3.8826105090048 \cdot 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{1.9413052545024 \cdot 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot 10^{19} \theta}{4\pi\theta - \theta^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \{\theta, -13, 13\}
\end{aligned}$$



$$\begin{aligned}
& D \left[ \right. \\
& \left( 3 \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \\
& \quad \left. \left. \frac{3.235508757504 \cdot 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \right) / \\
& \left. \left( 8 \left( \frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \theta] \\
& - \left( 15 \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \left. \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \right) / \\
& \left( 16 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 9 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \right) / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( \left( -\frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right) /
\end{aligned}$$

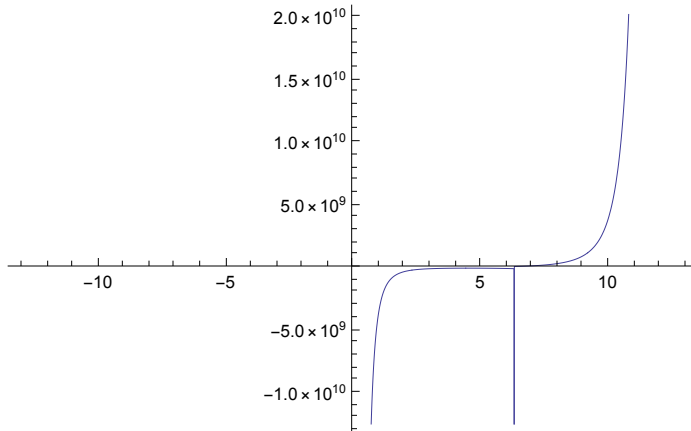
$$\begin{aligned}
& \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{3/2} + \\
& \left( \frac{3.06559 \times 10^{21} (4 \pi - 2 \theta)^4 \theta^2}{(4 \pi \theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta)^4 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^5} - \right. \\
& \quad \frac{6.13117 \times 10^{21} (4 \pi - 2 \theta)^3 \theta}{(4 \pi \theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^4} + \\
& \quad \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta)^3 \theta^3}{(4 \pi \theta - \theta^2)^4} - \\
& \quad \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4 \pi - 2 \theta)^2}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{1.22623 \times 10^{22} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4 \pi \theta - \theta^2)^3} + \\
& \quad \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{1.55304 \times 10^{20} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta)}{(4 \pi \theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} - \\
& \quad \left. \frac{2.32957 \times 10^{20} (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4 \pi \theta - \theta^2} \right) / \\
& \left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2}} \right) \\
\text{Plot} & \left[ - \left( 15 \left( - \frac{1.2773276589129854 \cdot 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \right. \right. \right. \\
& \quad \frac{3.235508757504 \cdot 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.235508757504 \cdot 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^4 \right) / \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{7/2} \right) +
\end{aligned}$$



$$\begin{aligned}
& \left( 9 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 3 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} + \\
& \left( \frac{3.065586381391165 \cdot (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{7.7652210180096 \cdot (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \quad \frac{6.13117276278233 \cdot (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{4.65913261080576 \cdot (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.55304420360192 \cdot (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{2.32956630540288 \cdot \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \{\theta, -13, 13\} ]
\end{aligned}$$



$$\begin{aligned}
 & D \left[ - \left( 15 \left( - \frac{1.2773276589129854 \cdot \theta^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \right. \\
 & \quad \frac{3.235508757504 \cdot \theta^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta}{4\pi\theta - \theta^2} - \\
 & \quad \left. \left. \frac{9.706526272512 \cdot \theta^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \right] / \\
 & \left( 16 \left( \frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
 & \left( 9 \left( \frac{2.5546553178259708 \cdot \theta^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
 & \quad \frac{6.471017515008 \cdot \theta^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
 & \quad \frac{5.1093106356519417 \cdot \theta^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
 & \quad \frac{1.9413052545024 \cdot \theta^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \theta^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
 & \quad \frac{6.471017515008 \cdot \theta^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
 & \quad \left. \left. \frac{1.9413052545024 \cdot \theta^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \theta^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right) \\
 & \left( - \frac{1.2773276589129854 \cdot \theta^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 3 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} + \\
& \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} +
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot (4\pi - 2\theta)(4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{2.32956630540288 \cdot \theta^{20}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2}} \right), \theta] \\
& \left( 105 \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \left. \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^5 \right) / \\
& \left( 32 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 75 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{5.10931 \times 10^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right) \\
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 45 \left( \frac{2.55466 \times 10^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{5.10931 \times 10^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \frac{1.94131 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.55466 \times 10^{20}}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{1.94131 \times 10^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4 \pi \theta - \theta^2} \right)^2 \right. \\
& \quad \left( - \frac{1.27733 \times 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right) \Bigg/ \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 15 \left( - \frac{7.66397 \times 10^{20} (4 \pi - 2 \theta)^3 \theta^2}{(4 \pi \theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.53279 \times 10^{21} (4 \pi - 2 \theta)^2 \theta}{(4 \pi \theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{5.82392 \times 10^{19} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4 \pi - 2 \theta)^2 \theta^3}{(4 \pi \theta - \theta^2)^3} + \\
& \quad \frac{3.88261 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4 \pi - 2 \theta)}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \left. \left. \frac{1.53279 \times 10^{21} \theta}{(4 \pi \theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^2} - \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 5 \left( -\frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{2.55466 \times 10^{20}}{4 \pi \theta - \theta^2} - \frac{1.94131 \times 10^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4 \pi \theta - \theta^2} \right) \right) / \\
& \left( 2 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 5 \left( \frac{3.06559 \times 10^{21} (4 \pi - 2 \theta)^4 \theta^2}{(4 \pi \theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta)^4 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{6.13117 \times 10^{21} (4 \pi - 2 \theta)^3 \theta}{(4 \pi \theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^4} + \\
& \quad \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta)^3 \theta^3}{(4 \pi \theta - \theta^2)^4} - \\
& \quad \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4 \pi - 2 \theta)^2}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{1.22623 \times 10^{22} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4 \pi \theta - \theta^2)^3} + \\
& \quad \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{1.55304 \times 10^{20} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta)}{(4 \pi \theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} - \\
& \quad \left. \frac{2.32957 \times 10^{20} (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4 \pi \theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right) / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{1.53279 \times 10^{22} (4 \pi - 2 \theta)^5 \theta^2}{(4 \pi \theta - \theta^2)^6} + \frac{3.88261 \times 10^{20} (4 \pi - 2 \theta)^5 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^6} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.06559 \times 10^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117 \times 10^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \frac{1.53279 \times 10^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.59838 \times 10^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49435 \times 10^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{3.06559 \times 10^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{22} \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32957 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478 \times 10^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{3.88261 \times 10^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{3.88261 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \frac{3.88261 \times 10^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} \Bigg) / \\
& \left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right) \\
& \text{Plot} \left[ \left( 105 \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \right. \\
& \quad \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^5 \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 75 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4 \pi \theta - \theta^2} \right) \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4 \pi \theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^3 \bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 45 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 15 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

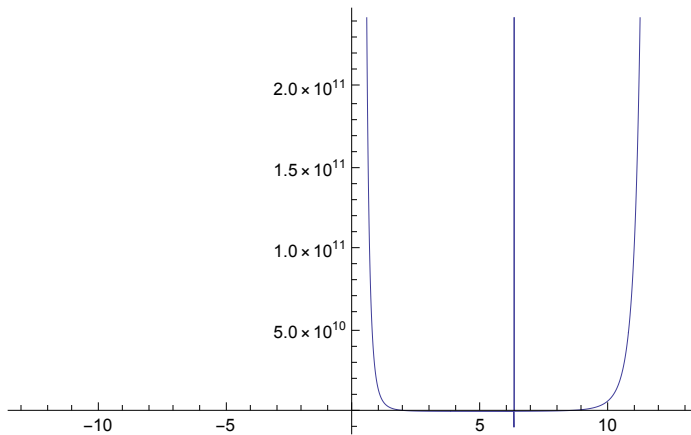
$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left( \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 5 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 5 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} -
\end{aligned}$$



$$\begin{aligned}
& \frac{3.49434945810432 \cdot (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{3.8826105090048 \cdot (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \theta}{(4\pi\theta - \theta^2)^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \{\theta, -13, 13\}
\end{aligned}$$



$$D \left[ 105 \left( - \frac{1.2773276589129854 \cdot (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right.$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left( \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^5 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 75 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \right. \\
& \quad \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \right. \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 45 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 15 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)(4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \theta^{19}}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \theta^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \frac{5.8239157635072 \cdot \theta^{19}}{4\pi\theta - \theta^2} \left( - \frac{1.2773276589129854 \cdot \theta^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \theta^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \theta^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 5 \left( - \frac{7.663965953477913 \cdot \theta^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.9413052545024 \cdot \theta^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \theta^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \theta^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \theta^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \theta^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \theta^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \theta^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \theta^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \theta^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \theta^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \theta^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \theta^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \theta^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 5 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \left. \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \theta] \\
& - \left( 945 \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \quad \left. \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^6 \right) / \\
& \left( 64 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) + \\
& \left( 1575 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 32 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 675 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{5.10931 \times 10^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left. \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \right. \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 16 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 75 \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg) / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 45 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right)^3 \right) \Bigg) / \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 45 \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 45 \left( \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6.13117 \times 10^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.22623 \times 10^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304 \times 10^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4\pi\theta - \theta^2)^2} + \\
& \frac{7.76522 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{2.32957 \times 10^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 5 \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \left. \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.53279 \times 10^{21} \theta}{(4 \pi \theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \left. \frac{1.94131 \times 10^{19} \theta^3}{(4 \pi \theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4 \pi - \theta)}{4 \pi \theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4 \pi \theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 2 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 15 \left( \frac{3.06559 \times 10^{21} (4 \pi - 2 \theta)^4 \theta^2}{(4 \pi \theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta)^4 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^5} - \right. \right. \\
& \frac{6.13117 \times 10^{21} (4 \pi - 2 \theta)^3 \theta}{(4 \pi \theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^4} + \\
& \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta)^3 \theta^3}{(4 \pi \theta - \theta^2)^4} - \\
& \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4 \pi - 2 \theta)^2}{(4 \pi \theta - \theta^2)^3} - \\
& \frac{1.22623 \times 10^{22} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4 \pi \theta - \theta^2)^3} + \\
& \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} - \\
& \frac{1.55304 \times 10^{20} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4 \pi \theta - \theta^2)^2} + \\
& \frac{7.76522 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta)}{(4 \pi \theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} - \\
& \left. \frac{2.32957 \times 10^{20} (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4 \pi \theta - \theta^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \right. \\
& \left. \frac{5.10931 \times 10^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 3 \left( -\frac{1.53279 \times 10^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \frac{3.06559 \times 10^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117 \times 10^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \frac{1.53279 \times 10^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.59838 \times 10^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49435 \times 10^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{3.06559 \times 10^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{22} \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32957 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478 \times 10^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{3.88261 \times 10^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \left. \frac{3.88261 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \frac{3.88261 \times 10^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right) / \\
& \left( 2 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \right. \\
& \quad \frac{1.83935 \times 10^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \frac{4.59838 \times 10^{23} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{1.16478 \times 10^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{7.35741 \times 10^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{5.51806 \times 10^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.79548 \times 10^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{9.31827 \times 10^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \frac{1.39774 \times 10^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.75903 \times 10^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{5.51806 \times 10^{23} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^4} - \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.09661 \times 10^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.19676 \times 10^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.09661 \times 10^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.09661 \times 10^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} -
\end{aligned}$$

$$\begin{aligned}
& \frac{6.9887 \times 10^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{2.32957 \times 10^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.19676 \times 10^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \frac{1.39774 \times 10^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \left. \frac{6.9887 \times 10^{21} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \frac{6.9887 \times 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21}}{(4\pi\theta - \theta^2)^2} \right) / \\
& \left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right) \\
\text{Plot} \left[ - \right. & \left( 945 \left( - \frac{1.2773276589129854 \cdot \theta^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \frac{3.235508757504 \cdot \theta^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \theta^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18} \theta^3}{4\pi\theta - \theta^2} \right)^6 \Bigg) / \\
& \left( 64 \left( \frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) + \\
& \left( 1575 \left( \frac{2.5546553178259708 \cdot \theta^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{6.471017515008 \cdot \theta^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \theta^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \theta^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \theta^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \theta^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{1.9413052545024 \cdot \theta^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \theta^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 675 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( -\frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 75 \left( -\frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left( \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 45 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 45 \left( -\frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 45 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \left. \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \right. \\
& \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \right. \\
& \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 5 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 15 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \quad \left. \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \right. \\
& \quad \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \right. \\
& \quad \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 3 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right.
\end{aligned}$$

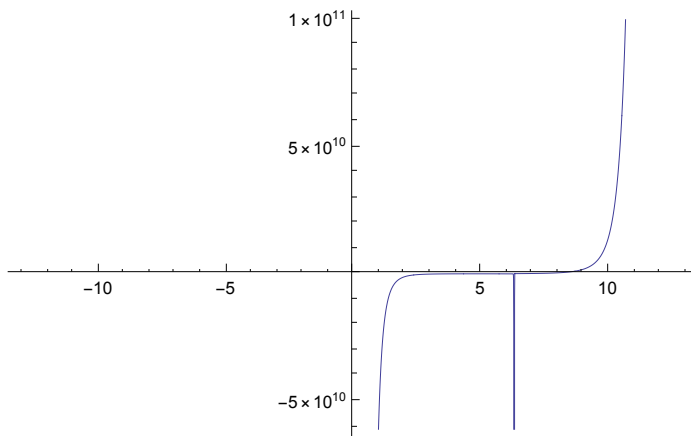
$$\begin{aligned}
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} -
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \right. \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \frac{1.839351828834699 \cdot \pi^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \\
& \frac{4.598379572086748 \cdot \pi^{23} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{1.16478315270144 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \\
& \frac{7.357407315338796 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \\
& \left. \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \right)
\end{aligned}$$



$$\begin{aligned}
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.795479566483456 \cdot \pi^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{9.31826522161152 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.397739783241728 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.7590277432520485 \cdot \pi^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173496 \cdot \pi^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173494 \cdot \pi^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} -
\end{aligned}$$

$$\begin{aligned}
& \frac{1.3977397832417278 \cdot 10^{22} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{6.98869891620864 \cdot 10^{21} (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^3} + \\
& \left( \frac{6.98869891620864 \cdot 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot 10^{21}}{(4\pi\theta - \theta^2)^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2}} \right), \{\theta, \\
& -13, 13\} ]
\end{aligned}$$



$$\begin{aligned}
& D \left[ - \left( 945 \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \right. \\
& \quad \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^6 \right) / \\
& \quad \left( 64 \left( \frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) + \\
& \quad \left( 1575 \left( \frac{2.5546553178259708 \cdot 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \left. \left. \frac{5.1093106356519417 \cdot 10^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg) / \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 675 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \right) / \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 75 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 45 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^3 \right) / \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 45 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \left. \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 45 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \left. \left. \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( 5 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right)^2 \right) / \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 15 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \left. \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 3 \left( -\frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \quad \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} +
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \theta^{22}}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot (4\pi - 2\theta)^2 \theta^{21}}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)(4\pi - \theta) \theta^{21}}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta) \theta^{21}}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot (4\pi - \theta) \theta^{21}}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \theta^{20}}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot (4\pi - 2\theta) \theta^{20}}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot (4\pi - \theta) \theta^{20}}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot (4\pi - 2\theta) \theta^{20}}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot (4\pi - 2\theta)(4\pi - \theta) \theta^{18}}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot (4\pi - \theta) \theta^{18}}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18}}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta) \theta^{18}}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( \frac{9.196759144173494 \cdot (4\pi - 2\theta)^6 \theta^{22}}{(4\pi\theta - \theta^2)^7} - \right. \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)^6 (4\pi - \theta) \theta^{21}}{(4\pi\theta - \theta^2)^7} - \\
& \frac{1.839351828834699 \cdot (4\pi - 2\theta)^5 \theta^{23}}{(4\pi\theta - \theta^2)^6} + \\
& \frac{4.598379572086748 \cdot (4\pi - 2\theta)^4 \theta^{23}}{(4\pi\theta - \theta^2)^6} + \\
& \frac{6.988698916208639 \cdot (4\pi - 2\theta)^5 (4\pi - \theta) \theta^{21}}{(4\pi\theta - \theta^2)^6} - \\
& \left. \frac{2.32956630540288 \cdot (4\pi - 2\theta)^5 \theta^{23}}{(4\pi\theta - \theta^2)^6} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.16478315270144 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \\
& \frac{7.357407315338796 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \\
& \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.795479566483456 \cdot \pi^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{9.31826522161152 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.397739783241728 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.7590277432520485 \cdot \pi^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173496 \cdot \pi^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} -
\end{aligned}$$

$$\begin{aligned}
& \frac{6.988698916208639 \cdot \theta^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \theta^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173494 \cdot \theta^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \theta^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \theta^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.3977397832417278 \cdot \theta^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{6.98869891620864 \cdot \theta^{21} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \left. \frac{6.98869891620864 \cdot \theta^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \theta] \\
& \left( 10395 \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
& \left. \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^7 \right) / \\
& \left( 128 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{13/2} \right) - \\
& \left( 19845 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left. \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^5 \Bigg/ \\
& \left( 64 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) + \\
& \left( 11025 \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \right. \\
& \quad \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 32 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) + \\
& \left( 3675 \left( -\frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \left. \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.53279 \times 10^{21} \theta}{(4 \pi \theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \left( \frac{1.94131 \times 10^{19} \theta^3}{(4 \pi \theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4 \pi - \theta)}{4 \pi \theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4 \pi \theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 32 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 1575 \left( \frac{2.55466 \times 10^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \right. \right. \\
& \frac{6.47102 \times 10^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \frac{5.10931 \times 10^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \\
& \frac{2.55466 \times 10^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \\
& \left. \left. \frac{2.55466 \times 10^{20}}{4 \pi \theta - \theta^2} - \frac{1.94131 \times 10^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4 \pi \theta - \theta^2} \right)^3 \right. \\
& \left( - \frac{1.27733 \times 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right) \Bigg/ \\
& \left( 16 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 1575 \left( - \frac{7.66397 \times 10^{20} (4 \pi - 2 \theta)^3 \theta^2}{(4 \pi \theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 525 \left( \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \left. \frac{6.13117 \times 10^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.22623 \times 10^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304 \times 10^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4\pi\theta - \theta^2)^2} + \\
& \frac{7.76522 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{2.32957 \times 10^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 16 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 315 \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \left. \left. \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \right) / \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 105 \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left. \left. \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right)^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right) / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 315 \left( \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{6.13117 \times 10^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.22623 \times 10^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.55304 \times 10^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{7.76522 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \left. \frac{2.32957 \times 10^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \left. \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{2.55466 \times 10^{20}}{4 \pi \theta - \theta^2} - \frac{1.94131 \times 10^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4 \pi \theta - \theta^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4 \pi \theta - \theta^2} - \frac{9.70653 \times 10^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4 \pi \theta - \theta^2} \right) \Bigg/ \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 63 \left( - \frac{1.53279 \times 10^{22} (4 \pi - 2 \theta)^5 \theta^2}{(4 \pi \theta - \theta^2)^6} + \frac{3.88261 \times 10^{20} (4 \pi - 2 \theta)^5 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^6} + \right. \right. \\
& \frac{3.06559 \times 10^{22} (4 \pi - 2 \theta)^4 \theta}{(4 \pi \theta - \theta^2)^5} - \frac{6.13117 \times 10^{22} (4 \pi - 2 \theta)^3 \theta^2}{(4 \pi \theta - \theta^2)^5} - \\
& \frac{1.16478 \times 10^{21} (4 \pi - 2 \theta)^4 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^5} + \frac{3.88261 \times 10^{20} (4 \pi - 2 \theta)^4 \theta^3}{(4 \pi \theta - \theta^2)^5} + \\
& \frac{1.55304 \times 10^{21} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^5} - \frac{1.53279 \times 10^{22} (4 \pi - 2 \theta)^3}{(4 \pi \theta - \theta^2)^4} + \\
& \frac{9.19676 \times 10^{22} (4 \pi - 2 \theta)^2 \theta}{(4 \pi \theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^4} - \\
& \frac{4.59838 \times 10^{22} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^4} - \frac{1.16478 \times 10^{21} (4 \pi - 2 \theta)^3 \theta^2}{(4 \pi \theta - \theta^2)^4} - \\
& \frac{3.49435 \times 10^{21} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4 \pi - 2 \theta)^2 \theta^3}{(4 \pi \theta - \theta^2)^4} + \\
& \frac{1.16478 \times 10^{21} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} - \frac{3.06559 \times 10^{22} (4 \pi - 2 \theta)}{(4 \pi \theta - \theta^2)^3} - \\
& \frac{3.88261 \times 10^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta)}{(4 \pi \theta - \theta^2)^3} + \frac{3.06559 \times 10^{22} \theta}{(4 \pi \theta - \theta^2)^3} + \\
& \frac{1.16478 \times 10^{21} (4 \pi - 2 \theta)^2 \theta}{(4 \pi \theta - \theta^2)^3} + \frac{2.32957 \times 10^{21} (4 \pi - 2 \theta) (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^3} - \\
& \frac{2.32957 \times 10^{21} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} - \frac{1.16478 \times 10^{21} (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^3} + \frac{3.88261 \times 10^{20} \theta^3}{(4 \pi \theta - \theta^2)^3} -
\end{aligned}$$

$$\begin{aligned}
& \frac{3.88261 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \frac{3.88261 \times 10^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} \Bigg) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 35 \left( \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \frac{6.13117 \times 10^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.19676 \times 10^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{7.76522 \times 10^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \frac{3.06559 \times 10^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.22623 \times 10^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32957 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{4.65913 \times 10^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304 \times 10^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.76522 \times 10^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{21}}{(4\pi\theta - \theta^2)^2} + \\
& \frac{7.76522 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \frac{2.32957 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{2.32957 \times 10^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.32957 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.76522 \times 10^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.53279 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.53279 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.88261 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.66397 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.53279 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.82392 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.82392 \times 10^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.82392 \times 10^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{1.94131 \times 10^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.82392 \times 10^{19} \theta}{4\pi\theta - \theta^2} \right) \Bigg) / \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 21 \left( - \frac{1.53279 \times 10^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \frac{3.06559 \times 10^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117 \times 10^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \frac{1.53279 \times 10^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.59838 \times 10^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49435 \times 10^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{3.06559 \times 10^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{3.88261 \times 10^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{3.06559 \times 10^{22} \theta}{(4\pi\theta - \theta^2)^3} + \\
& \left. \frac{1.16478 \times 10^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32957 \times 10^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478 \times 10^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{3.88261 \times 10^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \left( \frac{3.88261 \times 10^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \frac{3.88261 \times 10^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478 \times 10^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( \frac{2.55466 \times 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{6.47102 \times 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{5.10931 \times 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.55466 \times 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.94131 \times 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.47102 \times 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.47102 \times 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{2.55466 \times 10^{20}}{4\pi\theta - \theta^2} - \frac{1.94131 \times 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.94131 \times 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 7 \left( \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \right. \right. \\
& \frac{1.83935 \times 10^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \frac{4.59838 \times 10^{23} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{1.16478 \times 10^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \frac{9.19676 \times 10^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \\
& \frac{7.35741 \times 10^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{5.51806 \times 10^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.79548 \times 10^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{9.31827 \times 10^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \left. \frac{1.39774 \times 10^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \frac{2.75903 \times 10^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \frac{5.51806 \times 10^{23} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.9887 \times 10^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} - \frac{2.09661 \times 10^{22} (4\pi - 2\theta)^2 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.19676 \times 10^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.09661 \times 10^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.09661 \times 10^{22} (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^4} - \frac{6.9887 \times 10^{21} (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32957 \times 10^{21} (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} + \frac{9.19676 \times 10^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913 \times 10^{21} (4\pi - 2\theta)(4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \frac{1.39774 \times 10^{22} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^3} - \\
& \left( \frac{6.9887 \times 10^{21} (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^3} + \frac{6.9887 \times 10^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32957 \times 10^{21}}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.27733 \times 10^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \frac{3.23551 \times 10^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.55466 \times 10^{20} \theta}{4\pi\theta - \theta^2} - \frac{9.70653 \times 10^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.23551 \times 10^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.27733 \times 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.23551 \times 10^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{6.43773 \times 10^{23} (4\pi - 2\theta)^7 \theta^2}{(4\pi\theta - \theta^2)^8} + \frac{1.6307 \times 10^{22} (4\pi - 2\theta)^7 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^8} + \right. \\
& \frac{1.28755 \times 10^{24} (4\pi - 2\theta)^6 \theta}{(4\pi\theta - \theta^2)^7} - \frac{3.86264 \times 10^{24} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^7} - \\
& \frac{4.89209 \times 10^{22} (4\pi - 2\theta)^6 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^7} + \\
& \frac{1.6307 \times 10^{22} (4\pi - 2\theta)^6 \theta^3}{(4\pi\theta - \theta^2)^7} + \frac{9.78418 \times 10^{22} (4\pi - 2\theta)^5 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \frac{6.43773 \times 10^{23} (4\pi - 2\theta)^5}{(4\pi\theta - \theta^2)^6} + \frac{6.43773 \times 10^{24} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^6} +
\end{aligned}$$



$$\begin{aligned}
& \frac{4.89209 \times 10^{22} (4\pi - 2\theta)^5 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^6} - \\
& \frac{6.43773 \times 10^{24} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^6} - \frac{4.89209 \times 10^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.44604 \times 10^{23} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{8.15348 \times 10^{22} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^6} + \frac{1.6307 \times 10^{23} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.57509 \times 10^{24} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^5} - \frac{1.6307 \times 10^{22} (4\pi - 2\theta)^4 (4\pi - \theta)}{(4\pi\theta - \theta^2)^5} + \\
& \frac{7.72528 \times 10^{24} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^5} + \frac{4.89209 \times 10^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.95684 \times 10^{23} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.57509 \times 10^{24} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{1.95684 \times 10^{23} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.93525 \times 10^{23} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{9.78418 \times 10^{22} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^5} + \frac{6.52279 \times 10^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.93132 \times 10^{24} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^4} - \frac{1.6307 \times 10^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.89209 \times 10^{22} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} + \frac{1.28755 \times 10^{24} \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.46763 \times 10^{23} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \frac{1.46763 \times 10^{23} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.46763 \times 10^{23} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{4.89209 \times 10^{22} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.6307 \times 10^{22} \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{3.26139 \times 10^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \left. \frac{1.6307 \times 10^{22} (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{4.89209 \times 10^{22} \theta}{(4\pi\theta - \theta^2)^3} \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \sqrt{\frac{1.27733 \times 10^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.23551 \times 10^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2}} \right) \\
& \text{Plot} \left[ \left( 10395 \left( -\frac{1.2773276589129854 \cdot \theta^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \right. \right. \right. \\
& \quad \frac{3.235508757504 \cdot \theta^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot \theta^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^7 \right) / \\
& \quad \left( 128 \left( \frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{13/2} \right) - \\
& \quad \left( 19845 \left( \frac{2.5546553178259708 \cdot \theta^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \theta^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \theta^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \theta^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{6.471017515008 \cdot \theta^{18} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \theta^{18} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4 \pi \theta - \theta^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \theta^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.9413052545024 \cdot \theta^{19} \theta^2}{4 \pi \theta - \theta^2} \right) \right) / \\
& \quad \left( -\frac{1.2773276589129854 \cdot \theta^{20} (4 \pi - 2 \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \theta^{18} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta}{4 \pi \theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \theta^{18} (4 \pi - \theta) \theta^2}{4 \pi \theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18} \theta^3}{4 \pi \theta - \theta^2} \right)^5 \Bigg) / \\
& \quad \left( 64 \left( \frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{11/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 11\,025 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \right) / \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) + \\
& \left( 3675 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 1575 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^3 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 1575 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 525 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot (4\pi - 2\theta)(4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \theta^{20}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18}}{4\pi\theta - \theta^2} \right)^3 \Bigg) / \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 315 \left( - \frac{7.663965953477913 \cdot (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \frac{1.9413052545024 \cdot (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.5327931906955826 \cdot (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.8239157635072 \cdot (4\pi - 2\theta)^2 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{1.9413052545024 \cdot (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 105 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 315 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \left. \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 63 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \left. \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 35 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \left. \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 21 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \quad \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \left. \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) -
\end{aligned}$$

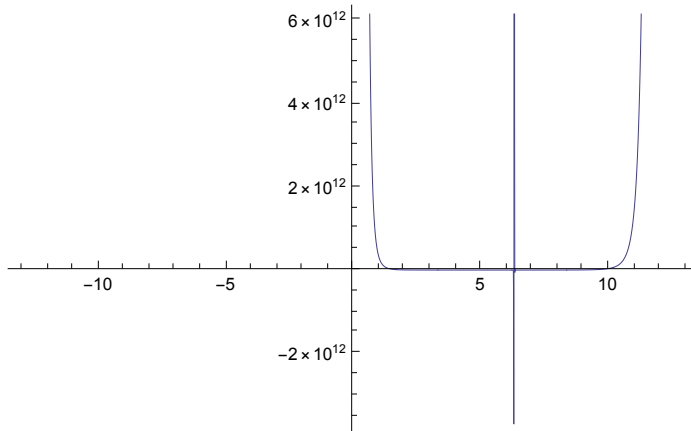
$$\begin{aligned}
& \left( 7 \left( \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \right. \right. \\
& \quad \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \quad \frac{1.839351828834699 \cdot \pi^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \frac{4.598379572086748 \cdot \pi^{23} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{1.16478315270144 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \frac{7.357407315338796 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.795479566483456 \cdot \pi^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{9.31826522161152 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.397739783241728 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.7590277432520485 \cdot \pi^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^4} - \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} -
\end{aligned}$$



$$\begin{aligned}
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173496 \cdot \pi^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{2.32956630540288 \cdot \pi^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173494 \cdot \pi^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.3977397832417278 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{6.98869891620864 \cdot \pi^{21} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \left( \frac{6.98869891620864 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{6.437731400921446 \cdot \pi^{23} (4\pi - 2\theta)^7 \theta^2}{(4\pi\theta - \theta^2)^8} + \right. \\
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^7 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^8} + \\
& \frac{1.2875462801842892 \cdot \pi^{24} (4\pi - 2\theta)^6 \theta}{(4\pi\theta - \theta^2)^7} - \\
& \left. \frac{3.862638840552868 \cdot \pi^{24} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^7} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{4.892089241346047 \cdot (4\pi - 2\theta)^6 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^7} + \\
& \frac{1.630696413782016 \cdot (4\pi - 2\theta)^6 \theta^3}{(4\pi\theta - \theta^2)^7} + \\
& \frac{9.784178482692096 \cdot (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \frac{6.437731400921446 \cdot (4\pi - 2\theta)^5}{(4\pi\theta - \theta^2)^6} + \\
& \frac{6.437731400921448 \cdot (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^6} + \\
& \frac{4.892089241346048 \cdot (4\pi - 2\theta)^5 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^6} - \\
& \frac{6.437731400921447 \cdot (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{4.892089241346048 \cdot (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.4460446206730243 \cdot (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{8.15348206891008 \cdot (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{1.630696413782016 \cdot (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.5750925603685784 \cdot (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.630696413782016 \cdot (4\pi - 2\theta)^4 (4\pi - \theta)}{(4\pi\theta - \theta^2)^5} + \\
& \frac{7.725277681105736 \cdot (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{4.892089241346048 \cdot (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.956835696538419 \cdot (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2.5750925603685784 \cdot \pi^{24} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.956835696538419 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.9352535448076287 \cdot \pi^{23} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{9.784178482692096 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{6.522785655128064 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.9313194202764338 \cdot \pi^{24} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.6306964137820157 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.2875462801842892 \cdot \pi^{24} \theta}{(4\pi\theta - \theta^2)^4} + \frac{1.467626772403814 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.4676267724038144 \cdot \pi^{23} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.4676267724038142 \cdot \pi^{23} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.6306964137820157 \cdot \pi^{22} \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.2613928275640314 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \left. \frac{1.630696413782016 \cdot \pi^{22} (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{4.892089241346048 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \{\theta, \\
& -13, 13\} ]
\end{aligned}$$



$$\begin{aligned}
 & D \left[ 10\,395 \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right. \\
 & \quad \frac{3.235508757504 \cdot 10^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta}{4\pi\theta - \theta^2} - \\
 & \quad \left. \frac{9.706526272512 \cdot 10^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot 10^{18} \theta^3}{4\pi\theta - \theta^2} \right)^7 \Bigg] / \\
 & \left( 128 \left( \frac{1.2773276589129854 \cdot 10^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot 10^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{13/2} \right) - \\
 & \left( 19\,845 \left( \frac{2.5546553178259708 \cdot 10^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
 & \quad \frac{6.471017515008 \cdot 10^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
 & \quad \frac{5.1093106356519417 \cdot 10^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
 & \quad \frac{1.9413052545024 \cdot 10^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot 10^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
 & \quad \frac{6.471017515008 \cdot 10^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot 10^{20}}{4\pi\theta - \theta^2} - \\
 & \quad \left. \frac{1.9413052545024 \cdot 10^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot 10^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
 & \left( - \frac{1.2773276589129854 \cdot 10^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left( \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^5 \Bigg/ \\
& \left( 64 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) + \\
& \left( 11025 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) + \\
& \left( 3675 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left( \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 1575 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^3 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 1575 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 525 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \quad \left. \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \right. \\
& \quad \left. \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \right. \\
& \quad \left. \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{3.065586381391165 \cdot (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot (4\pi - 2\theta)(4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot (4\pi - 2\theta)(4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot (4\pi - \theta)\theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^3}{4\pi\theta - \theta^2} \right)^3 \bigg/ \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 315 \left( - \frac{7.663965953477913 \cdot (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \left. \frac{1.9413052545024 \cdot (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \left. \frac{1.5327931906955826 \cdot (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 105 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 315 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 63 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \right. \\
& \left. \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \\
& \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \right. \\
& \left. \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \left. \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 35 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 21 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \quad \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \quad \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \right)
\end{aligned}$$



$$\begin{aligned}
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 7 \left( \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \right. \right. \\
& \quad \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \quad \frac{1.839351828834699 \cdot \pi^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \frac{4.598379572086748 \cdot \pi^{23} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{1.16478315270144 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \frac{7.357407315338796 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.795479566483456 \cdot \pi^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{9.31826522161152 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.397739783241728 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.7590277432520485 \cdot \pi^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \left. \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^4} - \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^3\theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173496 \cdot \pi^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{2.32956630540288 \cdot \pi^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173494 \cdot \pi^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.3977397832417278 \cdot \pi^{22} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^3} - \frac{6.98869891620864 \cdot \pi^{21} (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^3} + \\
& \left( \frac{6.98869891620864 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) + \\
& \left( - \frac{6.437731400921446 \cdot \pi^{23} (4\pi - 2\theta)^7 \theta^2}{(4\pi\theta - \theta^2)^8} + \right. \\
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^7 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^8} + \\
& \left. \frac{1.2875462801842892 \cdot \pi^{24} (4\pi - 2\theta)^6 \theta}{(4\pi\theta - \theta^2)^7} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{3.862638840552868 \cdot \pi^{24} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^7} - \\
& \frac{4.892089241346047 \cdot \pi^{22} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^7} + \\
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^6 \theta^3}{(4\pi\theta - \theta^2)^7} + \\
& \frac{9.784178482692096 \cdot \pi^{22} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \frac{6.437731400921446 \cdot \pi^{23} (4\pi - 2\theta)^5}{(4\pi\theta - \theta^2)^6} + \\
& \frac{6.437731400921448 \cdot \pi^{24} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^6} + \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^5 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^6} - \\
& \frac{6.437731400921447 \cdot \pi^{24} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.4460446206730243 \cdot \pi^{23} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{8.15348206891008 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{1.630696413782016 \cdot \pi^{23} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.5750925603685784 \cdot \pi^{24} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta)}{(4\pi\theta - \theta^2)^5} + \\
& \frac{7.725277681105736 \cdot \pi^{24} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} +
\end{aligned}$$

$$\begin{aligned}
& \frac{1.956835696538419 \cdot (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.5750925603685784 \cdot (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.956835696538419 \cdot (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.9352535448076287 \cdot (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{9.784178482692096 \cdot (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{6.522785655128064 \cdot (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.9313194202764338 \cdot (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.6306964137820157 \cdot (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.892089241346048 \cdot (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.2875462801842892 \cdot (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^4} + \frac{1.467626772403814 \cdot (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.4676267724038144 \cdot (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.4676267724038142 \cdot (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.892089241346048 \cdot (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.6306964137820157 \cdot (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.2613928275640314 \cdot (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \left( \frac{1.630696413782016 \cdot (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{4.892089241346048 \cdot (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot (4\pi - 2\theta) \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right), \theta] \\
& \text{Simplify} \left[ - \left( 135 \cdot \frac{1.2773276589129854 \cdot (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left( \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^8 \Bigg/ \\
& \left( 256 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{15/2} \right) + \\
& \left( 72765 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^6 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{13/2} \right) - \\
& \left( 99225 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 32 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) - \\
& \left( 6615 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)(4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} - \right. \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \theta^{19}}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \frac{5.8239157635072 \cdot \theta^{19}}{4\pi\theta - \theta^2} \left( - \frac{1.2773276589129854 \cdot (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18}}{4\pi\theta - \theta^2} \right)^5 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{11/2} \right) + \\
& \left( 11025 \left( \frac{2.5546553178259708 \cdot (4\pi - 2\theta)^2\theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \frac{6.471017515008 \cdot (4\pi - 2\theta)^2(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \theta^{20}(4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \\
& \left. \frac{1.9413052545024 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right)^3 \left( - \frac{1.2773276589129854 \cdot (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot (4\pi - \theta)\theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18}}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 8 \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) +
\end{aligned}$$



$$\begin{aligned}
& \left( 3675 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) + \\
& \left( 3675 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \left. \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \theta^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \theta^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \theta^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \theta^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \theta^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \theta^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \theta^{18} \theta^3}{4\pi\theta - \theta^2} \right)^4 \Bigg/ \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{9/2} \right) - \\
& \left( 1575 \left( \frac{2.5546553178259708 \cdot \theta^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \right. \\
& \quad \frac{6.471017515008 \cdot \theta^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \theta^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \theta^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \theta^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \theta^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot \theta^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \theta^{19} \theta^2}{4\pi\theta - \theta^2} \right)^4 \right) \Bigg/ \\
& \left( 16 \left( \frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( 1575 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 525 \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left. \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right)^2 \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left( \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 1575 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) - \\
& \left( 105 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \left. \left. \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right)
\end{aligned}$$



$$\begin{aligned}
& \left( -\frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \quad \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \quad \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^3 \Bigg) / \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{7/2} \right) + \\
& \left( 105 \left( -\frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \right. \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \quad \left. \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{5.8239157635072 \cdot \pi^{19} \theta}{4 \pi \theta - \theta^2} \right)^2 \left( \frac{2.5546553178259708 \cdot \pi^{20} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4 \pi \theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - 2 \theta) (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4 \pi - 2 \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4 \pi \theta - \theta^2} - \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4 \pi - \theta) \theta}{4 \pi \theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4 \pi \theta - \theta^2} \right) \right) / \\
& \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4 \pi \theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4 \pi - \theta) \theta^3}{4 \pi \theta - \theta^2} \right)^{5/2} + \\
& \left( 315 \left( \frac{3.065586381391165 \cdot \pi^{21} (4 \pi - 2 \theta)^4 \theta^2}{(4 \pi \theta - \theta^2)^5} - \right. \right. \\
& \frac{7.7652210180096 \cdot \pi^{19} (4 \pi - 2 \theta)^4 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^5} - \\
& \frac{6.13117276278233 \cdot \pi^{21} (4 \pi - 2 \theta)^3 \theta}{(4 \pi \theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4 \pi - 2 \theta)^2 \theta^2}{(4 \pi \theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{20} (4 \pi - 2 \theta)^3 (4 \pi - \theta) \theta^2}{(4 \pi \theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4 \pi - 2 \theta)^3 \theta^3}{(4 \pi \theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta^3}{(4 \pi \theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4 \pi - 2 \theta)^2}{(4 \pi \theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4 \pi - 2 \theta) \theta}{(4 \pi \theta - \theta^2)^3} - \\
& \left. \frac{2.32956630540288 \cdot \pi^{20} (4 \pi - 2 \theta)^2 (4 \pi - \theta) \theta}{(4 \pi \theta - \theta^2)^3} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \theta^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot (4\pi - 2\theta)(4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \theta^{20}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \quad \frac{6.471017515008 \cdot (4\pi - 2\theta)^2(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{5.1093106356519417 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{(4\pi\theta - \theta^2)^2} + \\
& \quad \frac{1.9413052545024 \cdot (4\pi - 2\theta)(4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot (4\pi - 2\theta)\theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \quad \frac{6.471017515008 \cdot (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \\
& \quad \left. \left. \frac{1.9413052545024 \cdot (4\pi - \theta)\theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \theta^{19}}{4\pi\theta - \theta^2} \right)^2 \right) / \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) + \\
& \left( 105 \left( \frac{3.065586381391165 \cdot (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} - \\
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} + \\
& \left( \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \left. \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \\
& \left( \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} + \\
& \left( 63 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \right. \\
& \left. \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \\
& \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \right. \\
& \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \right. \\
& \left. \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \right. \\
& \left. \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left( \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \left. \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \right. \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} + \\
& \left( 21 \left( \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \right. \right. \\
& \left. \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \right. \\
& \left. \frac{1.839351828834699 \cdot \pi^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \frac{4.598379572086748 \cdot \pi^{23} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \\
& \left. \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \right. \\
& \left. \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \right. \\
& \left. \frac{1.16478315270144 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \right. \\
& \left. \frac{9.196759144173494 \cdot \pi^{22} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \frac{7.357407315338796 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \right. \\
& \left. \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{6.98869891620864 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.795479566483456 \cdot \pi^{22} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \frac{9.31826522161152 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.397739783241728 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.7590277432520485 \cdot \pi^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \frac{5.518055486504097 \cdot \pi^{23} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^4} - \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173496 \cdot \pi^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{2.32956630540288 \cdot \pi^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173494 \cdot \pi^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.3977397832417278 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{6.98869891620864 \cdot \pi^{21} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \left( \frac{6.98869891620864 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right.
\end{aligned}$$



$$\begin{aligned}
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 2 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{5/2} \right) - \\
& \left( 35 \left( \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \right. \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.13117276278233 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173495 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} - \frac{1.226234552556466 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{4.65913261080576 \cdot \pi^{20} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \quad \frac{1.55304420360192 \cdot \pi^{20} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{7.7652210180096 \cdot \pi^{19} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \quad \frac{3.065586381391165 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2.32956630540288 \cdot \pi^{20} (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^2} - \frac{2.32956630540288 \cdot \pi^{20} (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^2} + \\
& \left. \frac{2.32956630540288 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{7.7652210180096 \cdot \pi^{19}}{4\pi\theta - \theta^2} \right)^2 \Bigg/ \\
& \left( 4 \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{3/2} \right) - \\
& \left( 14 \left( - \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} + \right. \right. \\
& \quad \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^5 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^6} + \right. \\
& \quad \left. \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} - \frac{6.13117276278233 \cdot \pi^{22} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} - \right. \\
& \quad \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^4 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^5} + \right. \\
& \quad \left. \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^5} + \right. \\
& \quad \left. \frac{1.55304420360192 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^5} - \right. \\
& \quad \left. \frac{1.5327931906955825 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} + \frac{9.196759144173496 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^4} - \right. \\
& \quad \left. \frac{4.598379572086748 \cdot \pi^{22} (4\pi - 2\theta)\theta^2}{(4\pi\theta - \theta^2)^4} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} - \right. \\
& \quad \left. \frac{3.49434945810432 \cdot \pi^{21} (4\pi - 2\theta)^2 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^4} + \right. \\
& \quad \left. \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)(4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^4} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{3.065586381391165 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.065586381391165 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} + \frac{1.16478315270144 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} + \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} - \\
& \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \frac{1.16478315270144 \cdot \pi^{21} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{20} \theta^3}{(4\pi\theta - \theta^2)^3} - \frac{3.8826105090048 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} - \\
& \left( \frac{3.8826105090048 \cdot \pi^{20} (4\pi - \theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.16478315270144 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( - \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^4} + \right. \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^3} - \frac{1.5327931906955826 \cdot \pi^{21} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^3} + \\
& \frac{3.8826105090048 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{7.663965953477913 \cdot \pi^{20} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^2} + \frac{1.5327931906955826 \cdot \pi^{21} \theta}{(4\pi\theta - \theta^2)^2} + \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^2} - \frac{5.8239157635072 \cdot \pi^{19} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \\
& \frac{5.8239157635072 \cdot \pi^{19} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta)}{4\pi\theta - \theta^2} + \frac{5.8239157635072 \cdot \pi^{19} \theta}{4\pi\theta - \theta^2} \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{1.2773276589129854 \cdot \theta^{20}}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot (4\pi - \theta)\theta^3}{4\pi\theta - \theta^2} \right)^{3/2} - \\
& 7 \left( \frac{9.196759144173494 \cdot (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} - \right. \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta)^6 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \quad \frac{1.839351828834699 \cdot (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} + \frac{4.598379572086748 \cdot (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{6.988698916208639 \cdot (4\pi - 2\theta)^5 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \quad \frac{1.16478315270144 \cdot (4\pi - 2\theta)^4 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \quad \frac{9.196759144173494 \cdot (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} - \frac{7.357407315338796 \cdot (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{6.98869891620864 \cdot (4\pi - 2\theta)^4 (4\pi - \theta)\theta}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{5.518055486504097 \cdot (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \frac{6.98869891620864 \cdot (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.795479566483456 \cdot (4\pi - 2\theta)^3 (4\pi - \theta)\theta^2}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{9.31826522161152 \cdot (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \quad \frac{1.397739783241728 \cdot (4\pi - 2\theta)^2 (4\pi - \theta)\theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \quad \frac{2.7590277432520485 \cdot (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \quad \frac{2.32956630540288 \cdot (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \quad \frac{5.518055486504097 \cdot (4\pi - 2\theta)\theta}{(4\pi\theta - \theta^2)^4} - \frac{6.988698916208639 \cdot (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^4} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173496 \cdot \pi^{22} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{2.096609674862592 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \\
& \frac{6.988698916208639 \cdot \pi^{21} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{2.32956630540288 \cdot \pi^{21} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^4} + \\
& \frac{9.196759144173494 \cdot \pi^{22}}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^3} + \\
& \frac{4.65913261080576 \cdot \pi^{21} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} - \\
& \frac{1.3977397832417278 \cdot \pi^{22} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^3} - \frac{6.98869891620864 \cdot \pi^{21} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^3} + \\
& \left( \frac{6.98869891620864 \cdot \pi^{21} \theta^2}{(4\pi\theta - \theta^2)^3} + \frac{2.32956630540288 \cdot \pi^{21}}{(4\pi\theta - \theta^2)^2} \right) \\
& \left( \frac{2.5546553178259708 \cdot \pi^{20} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^3} - \right. \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^3} - \\
& \frac{5.1093106356519417 \cdot \pi^{20} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta^2}{(4\pi\theta - \theta^2)^2} + \\
& \frac{1.9413052545024 \cdot \pi^{19} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^2} - \frac{6.471017515008 \cdot \pi^{18} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^2} - \\
& \frac{6.471017515008 \cdot \pi^{18} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20}}{4\pi\theta - \theta^2} - \\
& \left. \left. \frac{1.9413052545024 \cdot \pi^{19} (4\pi - \theta) \theta}{4\pi\theta - \theta^2} + \frac{1.9413052545024 \cdot \pi^{19} \theta^2}{4\pi\theta - \theta^2} \right) \right) / \\
& \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} - \\
& \left( 2 \left( - \frac{6.437731400921446 \cdot \pi^{23} (4\pi - 2\theta)^7 \theta^2}{(4\pi\theta - \theta^2)^8} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^7 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^8} + \\
& \frac{1.2875462801842892 \cdot \pi^{24} (4\pi - 2\theta)^6 \theta}{(4\pi\theta - \theta^2)^7} - \frac{3.862638840552868 \cdot \pi^{24} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^7} - \\
& \frac{4.892089241346047 \cdot \pi^{22} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^7} + \\
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^6 \theta^3}{(4\pi\theta - \theta^2)^7} + \\
& \frac{9.784178482692096 \cdot \pi^{22} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \frac{6.437731400921446 \cdot \pi^{23} (4\pi - 2\theta)^5}{(4\pi\theta - \theta^2)^6} + \frac{6.437731400921448 \cdot \pi^{24} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^6} + \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^5 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^6} - \\
& \frac{6.437731400921447 \cdot \pi^{24} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^6} - \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^5 \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.4460446206730243 \cdot \pi^{23} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{8.15348206891008 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{1.630696413782016 \cdot \pi^{23} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{2.5750925603685784 \cdot \pi^{24} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.630696413782016 \cdot \pi^{22} (4\pi - 2\theta)^4 (4\pi - \theta)}{(4\pi\theta - \theta^2)^5} + \\
& \frac{7.725277681105736 \cdot \pi^{24} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^5} + \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^4 \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.956835696538419 \cdot \pi^{23} (4\pi - 2\theta)^3 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.5750925603685784 \cdot \pi^{24} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^5} - \frac{1.956835696538419 \cdot \pi^{23} (4\pi - 2\theta)^3 \theta^2}{(4\pi\theta - \theta^2)^5} -
\end{aligned}$$

$$\begin{aligned}
& \frac{2.9352535448076287 \cdot \pi^{23} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{9.784178482692096 \cdot \pi^{22} (4\pi - 2\theta)^2 \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{6.522785655128064 \cdot \pi^{22} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.9313194202764338 \cdot \pi^{24} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^4} - \frac{1.6306964137820157 \cdot \pi^{22} (4\pi - 2\theta)^3}{(4\pi\theta - \theta^2)^4} - \\
& \frac{4.892089241346048 \cdot \pi^{22} (4\pi - 2\theta)^2 (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.2875462801842892 \cdot \pi^{24} \theta}{(4\pi\theta - \theta^2)^4} + \frac{1.467626772403814 \cdot \pi^{23} (4\pi - 2\theta)^2 \theta}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.4676267724038144 \cdot \pi^{23} (4\pi - 2\theta) (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.4676267724038142 \cdot \pi^{23} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^4} - \frac{4.892089241346048 \cdot \pi^{22} (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{1.6306964137820157 \cdot \pi^{22} \theta^3}{(4\pi\theta - \theta^2)^4} - \frac{3.2613928275640314 \cdot \pi^{22} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^3} - \\
& \left( \frac{1.630696413782016 \cdot \pi^{22} (4\pi - \theta)}{(4\pi\theta - \theta^2)^3} + \frac{4.892089241346048 \cdot \pi^{22} \theta}{(4\pi\theta - \theta^2)^3} \right) \\
& \left( - \frac{1.2773276589129854 \cdot \pi^{20} (4\pi - 2\theta) \theta^2}{(4\pi\theta - \theta^2)^2} + \right. \\
& \frac{3.235508757504 \cdot \pi^{18} (4\pi - 2\theta) (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^2} + \frac{2.5546553178259708 \cdot \pi^{20} \theta}{4\pi\theta - \theta^2} - \\
& \left. \frac{9.706526272512 \cdot \pi^{18} (4\pi - \theta) \theta^2}{4\pi\theta - \theta^2} + \frac{3.235508757504 \cdot \pi^{18} \theta^3}{4\pi\theta - \theta^2} \right) \Bigg/ \\
& \left( \frac{1.2773276589129854 \cdot \pi^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \pi^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2} \right)^{3/2} + \\
& \left( \frac{5.150185120737157 \cdot \pi^{24} (4\pi - 2\theta)^8 \theta^2}{(4\pi\theta - \theta^2)^9} - \right. \\
& \left. \frac{1.3045571310256129 \cdot \pi^{23} (4\pi - 2\theta)^8 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^9} - \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1.0300370241474314 \cdot \pi^{25} (4\pi - 2\theta)^7 \theta}{(4\pi\theta - \theta^2)^8} + \\
& \frac{3.60512958451601 \cdot \pi^{25} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^8} + \\
& \frac{3.913671393076838 \cdot \pi^{23} (4\pi - 2\theta)^7 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^8} - \\
& \frac{1.3045571310256129 \cdot \pi^{23} (4\pi - 2\theta)^7 \theta^3}{(4\pi\theta - \theta^2)^8} - \\
& \frac{9.131899917179289 \cdot \pi^{23} (4\pi - 2\theta)^6 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^8} + \\
& \frac{5.150185120737157 \cdot \pi^{24} (4\pi - 2\theta)^6}{(4\pi\theta - \theta^2)^7} - \\
& \frac{6.180222144884589 \cdot \pi^{25} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^7} - \\
& \frac{3.913671393076838 \cdot \pi^{23} (4\pi - 2\theta)^6 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^7} + \\
& \frac{7.725277681105736 \cdot \pi^{25} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^7} + \\
& \frac{3.913671393076838 \cdot \pi^{23} (4\pi - 2\theta)^6 \theta^2}{(4\pi\theta - \theta^2)^7} + \\
& \frac{2.348202835846103 \cdot \pi^{24} (4\pi - 2\theta)^5 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^7} - \\
& \frac{7.827342786153677 \cdot \pi^{23} (4\pi - 2\theta)^5 \theta^3}{(4\pi\theta - \theta^2)^7} - \\
& \frac{1.956835696538419 \cdot \pi^{24} (4\pi - 2\theta)^4 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^7} + \\
& \frac{2.5750925603685782 \cdot \pi^{25} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^6} + \\
& \frac{1.3045571310256129 \cdot \pi^{23} (4\pi - 2\theta)^5 (4\pi - \theta)}{(4\pi\theta - \theta^2)^6} - \\
& \frac{1.0300370241474316 \cdot \pi^{26} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^6} -
\end{aligned}$$



$$\begin{aligned}
& \frac{3.913671393076838 \cdot \pi^{23} (4\pi - 2\theta)^5 \theta}{(4\pi\theta - \theta^2)^6} - \\
& \frac{1.9568356965384194 \cdot \pi^{24} (4\pi - 2\theta)^4 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^6} + \\
& \frac{5.150185120737157 \cdot \pi^{25} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{1.9568356965384192 \cdot \pi^{24} (4\pi - 2\theta)^4 \theta^2}{(4\pi\theta - \theta^2)^6} + \\
& \frac{3.9136713930768383 \cdot \pi^{24} (4\pi - 2\theta)^3 (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^6} - \\
& \frac{1.3045571310256127 \cdot \pi^{24} (4\pi - 2\theta)^3 \theta^3}{(4\pi\theta - \theta^2)^6} - \\
& \frac{1.3045571310256127 \cdot \pi^{24} (4\pi - 2\theta)^2 (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^6} + \\
& \frac{3.0901110724422945 \cdot \pi^{25} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.3045571310256127 \cdot \pi^{23} (4\pi - 2\theta)^4}{(4\pi\theta - \theta^2)^5} + \\
& \frac{5.2182285241024515 \cdot \pi^{23} (4\pi - 2\theta)^3 (4\pi - \theta)}{(4\pi\theta - \theta^2)^5} - \\
& \frac{4.1201480965897255 \cdot \pi^{25} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.5654685572307353 \cdot \pi^{24} (4\pi - 2\theta)^3 \theta}{(4\pi\theta - \theta^2)^5} - \\
& \frac{2.348202835846103 \cdot \pi^{24} (4\pi - 2\theta)^2 (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^5} + \\
& \frac{5.150185120737157 \cdot \pi^{24} \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{2.348202835846103 \cdot \pi^{24} (4\pi - 2\theta)^2 \theta^2}{(4\pi\theta - \theta^2)^5} + \\
& \frac{1.5654685572307353 \cdot \pi^{24} (4\pi - 2\theta) (4\pi - \theta) \theta^2}{(4\pi\theta - \theta^2)^5} -
\end{aligned}$$

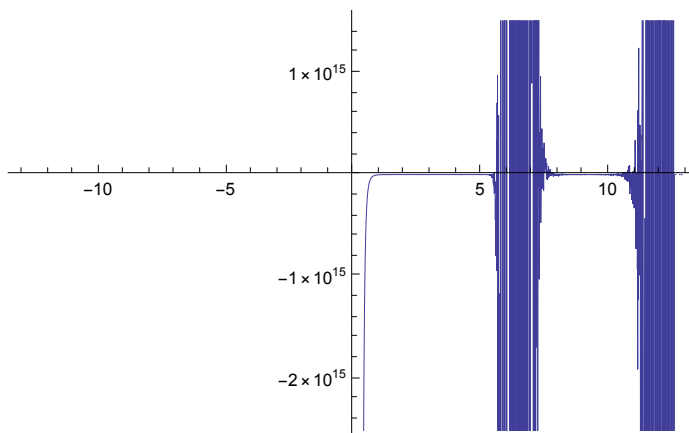
$$\begin{aligned}
& \frac{5.2182285241024515 \cdot \theta^{23} (4\pi - 2\theta) \theta^3}{(4\pi\theta - \theta^2)^5} - \\
& \frac{1.3045571310256129 \cdot \theta^{23} (4\pi - \theta) \theta^3}{(4\pi\theta - \theta^2)^5} + \\
& \frac{5.150185120737157 \cdot \theta^{24}}{(4\pi\theta - \theta^2)^4} + \frac{3.9136713930768376 \cdot \theta^{23} (4\pi - 2\theta)^2}{(4\pi\theta - \theta^2)^4} + \\
& \frac{3.913671393076838 \cdot \theta^{23} (4\pi - 2\theta) (4\pi - \theta)}{(4\pi\theta - \theta^2)^4} - \\
& \frac{1.1741014179230512 \cdot \theta^{24} (4\pi - 2\theta) \theta}{(4\pi\theta - \theta^2)^4} - \\
& \frac{3.913671393076838 \cdot \theta^{23} (4\pi - \theta) \theta}{(4\pi\theta - \theta^2)^4} + \\
& \left. \frac{3.913671393076838 \cdot \theta^{23} \theta^2}{(4\pi\theta - \theta^2)^4} + \frac{1.3045571310256127 \cdot \theta^{23}}{(4\pi\theta - \theta^2)^3} \right) / \\
& \left( 2 \sqrt{\frac{1.2773276589129854 \cdot \theta^{20} \theta^2}{4\pi\theta - \theta^2} - \frac{3.235508757504 \cdot \theta^{18} (4\pi - \theta) \theta^3}{4\pi\theta - \theta^2}} \right) ] \\
& (-1.72395 \times 10^{41} + 6.19455 \times 10^{41} \theta - 1.07157 \times 10^{42} \theta^2 + 1.18834 \times 10^{42} \theta^3 - \\
& 9.49099 \times 10^{41} \theta^4 + 5.81452 \times 10^{41} \theta^5 - 2.84161 \times 10^{41} \theta^6 + 1.13742 \times 10^{41} \theta^7 - \\
& 3.79913 \times 10^{40} \theta^8 + 1.07334 \times 10^{40} \theta^9 - 2.59064 \times 10^{39} \theta^{10} + 5.38068 \times 10^{38} \theta^{11} - \\
& 9.66543 \times 10^{37} \theta^{12} + 1.50635 \times 10^{37} \theta^{13} - 2.03957 \times 10^{36} \theta^{14} + 2.39796 \times 10^{35} \theta^{15} - \\
& 2.44178 \times 10^{34} \theta^{16} + 2.14222 \times 10^{33} \theta^{17} - 1.60499 \times 10^{32} \theta^{18} + 1.0121 \times 10^{31} \theta^{19} - \\
& 5.24014 \times 10^{29} \theta^{20} + 2.12338 \times 10^{28} \theta^{21} - 5.96777 \times 10^{26} \theta^{22} + 6.0287 \times 10^{24} \theta^{23} + \\
& 4.31663 \times 10^{23} \theta^{24} - 2.91795 \times 10^{22} \theta^{25} + 9.78147 \times 10^{20} \theta^{26} - 2.03604 \times 10^{19} \theta^{27} + \\
& 2.5186 \times 10^{17} \theta^{28} - 1.4316 \times 10^{15} \theta^{29} + 1232.34 \theta^{30} - 6.40418 \theta^{31}) / \\
& \left( (-12.5664 + \theta)^{16} (-6.28319 + \theta)^7 (-6.28319 + \theta)^7 \theta^7 \sqrt{\frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta}{12.5664 - 1. \theta}} \right)
\end{aligned}$$

Plot[

$$\begin{aligned}
& (-1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - 1.0715733419821407 \theta^{42} + \\
& 1.1883364566689056 \theta^{42} - 9.490987783531211 \theta^{41} + \\
& 5.814515984234418 \theta^{41} - 2.841610189077518 \theta^{41} + \\
& 1.1374222079829315 \theta^{41} - 3.7991255503643 \theta^{40} + \\
& 1.073339972987572 \theta^{40} - 2.5906381973931337 \theta^{39} + \\
& 5.3806768122609554 \theta^{38} - 9.66542766147963 \theta^{37} + \\
& 1.5063504106448067 \theta^{37} - 2.0395706143447065 \theta^{36} + \\
& 2.3979597145679737 \theta^{35} - 2.441779100246113 \theta^{34} + \\
& 2.1422234658979708 \theta^{33} - 1.6049917252445308 \theta^{32} + \\
& 1.012102378536468 \theta^{31} - 5.2401443148533675 \theta^{29} + \\
& 2.1233801883418154 \theta^{28} - 5.9677657472719257 \theta^{26} + \\
& 6.028703874008091 \theta^{24} + 4.316628659608773 \theta^{23} - \\
& 2.9179524450579636 \theta^{22} + 9.781465694388629 \theta^{20} - \\
& 2.036035192946051 \theta^{19} + 2.518601478855538 \theta^{17} - \\
& 1.4315995537848782 \theta^{15} + 1232.3437759904039 \theta^{30} - 6.404175164653097 \theta^{31}) /
\end{aligned}$$

$$\left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right.$$

$$\left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right), \{\theta, -13, 13\}]$$



$$\begin{aligned}
& D \left[ (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \right. \\
& \quad 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \cdot \theta^{41} \theta^4 + 5.814515984234418 \cdot \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \cdot \theta^{41} \theta^6 + 1.1374222079829315 \cdot \theta^{41} \theta^7 - 3.7991255503643 \cdot \theta^{40} \theta^8 + \\
& \quad 1.073339972987572 \cdot \theta^{40} \theta^9 - 2.5906381973931337 \cdot \theta^{39} \theta^{10} + \\
& \quad 5.3806768122609554 \cdot \theta^{38} \theta^{11} - 9.66542766147963 \cdot \theta^{37} \theta^{12} + \\
& \quad 1.5063504106448067 \cdot \theta^{37} \theta^{13} - 2.0395706143447065 \cdot \theta^{36} \theta^{14} + \\
& \quad 2.3979597145679737 \cdot \theta^{35} \theta^{15} - 2.441779100246113 \cdot \theta^{34} \theta^{16} + \\
& \quad 2.1422234658979708 \cdot \theta^{33} \theta^{17} - 1.6049917252445308 \cdot \theta^{32} \theta^{18} + \\
& \quad 1.012102378536468 \cdot \theta^{31} \theta^{19} - 5.2401443148533675 \cdot \theta^{29} \theta^{20} + \\
& \quad 2.1233801883418154 \cdot \theta^{28} \theta^{21} - 5.9677657472719257 \cdot \theta^{26} \theta^{22} + \\
& \quad 6.028703874008091 \cdot \theta^{24} \theta^{23} + 4.316628659608773 \cdot \theta^{23} \theta^{24} - \\
& \quad 2.9179524450579636 \cdot \theta^{22} \theta^{25} + 9.781465694388629 \cdot \theta^{20} \theta^{26} - \\
& \quad 2.036035192946051 \cdot \theta^{19} \theta^{27} + 2.518601478855538 \cdot \theta^{17} \theta^{28} - \\
& \quad \left. 1.4315995537848782 \cdot \theta^{15} \theta^{29} + 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \right) / \\
& \quad \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1. \cdot \theta}} \right), \theta \Big] \\
& (6.19455 \times 10^{41} - 2.14315 \times 10^{42} \theta + 3.56501 \times 10^{42} \theta^2 - \\
& \quad 3.7964 \times 10^{42} \theta^3 + 2.90726 \times 10^{42} \theta^4 - 1.70497 \times 10^{42} \theta^5 + 7.96196 \times 10^{41} \theta^6 - \\
& \quad 3.0393 \times 10^{41} \theta^7 + 9.66006 \times 10^{40} \theta^8 - 2.59064 \times 10^{40} \theta^9 + 5.91874 \times 10^{39} \theta^{10} - \\
& \quad 1.15985 \times 10^{39} \theta^{11} + 1.95826 \times 10^{38} \theta^{12} - 2.8554 \times 10^{37} \theta^{13} + 3.59694 \times 10^{36} \theta^{14} - \\
& \quad 3.90685 \times 10^{35} \theta^{15} + 3.64178 \times 10^{34} \theta^{16} - 2.88899 \times 10^{33} \theta^{17} + 1.92299 \times 10^{32} \theta^{18} - \\
& \quad 1.04803 \times 10^{31} \theta^{19} + 4.4591 \times 10^{29} \theta^{20} - 1.31291 \times 10^{28} \theta^{21} + 1.3866 \times 10^{26} \theta^{22} + \\
& \quad 1.03599 \times 10^{25} \theta^{23} - 7.29488 \times 10^{23} \theta^{24} + 2.54318 \times 10^{22} \theta^{25} - 5.4973 \times 10^{20} \theta^{26} + \\
& \quad 7.05208 \times 10^{18} \theta^{27} - 4.15164 \times 10^{16} \theta^{28} + 36970.3 \theta^{29} - 198.529 \theta^{30}) / \\
& \quad \left( (-12.5664 + \theta)^{16} (-6.28319 + \theta)^7 (-6.28319 + \theta)^7 \theta^7 \sqrt{\frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta}{12.5664 - 1. \cdot \theta}} \right) - \\
& (7 (-1.72395 \times 10^{41} + 6.19455 \times 10^{41} \theta - 1.07157 \times 10^{42} \theta^2 + 1.18834 \times 10^{42} \theta^3 - \\
& \quad 9.49099 \times 10^{41} \theta^4 + 5.81452 \times 10^{41} \theta^5 - 2.84161 \times 10^{41} \theta^6 + 1.13742 \times 10^{41} \theta^7 - \\
& \quad 3.79913 \times 10^{40} \theta^8 + 1.07334 \times 10^{40} \theta^9 - 2.59064 \times 10^{39} \theta^{10} + 5.38068 \times 10^{38} \theta^{11} - \\
& \quad 9.66543 \times 10^{37} \theta^{12} + 1.50635 \times 10^{37} \theta^{13} - 2.03957 \times 10^{36} \theta^{14} + 2.39796 \times 10^{35} \theta^{15} - \\
& \quad 2.44178 \times 10^{34} \theta^{16} + 2.14222 \times 10^{33} \theta^{17} - 1.60499 \times 10^{32} \theta^{18} + 1.0121 \times 10^{31} \theta^{19} - \\
& \quad 5.24014 \times 10^{29} \theta^{20} + 2.12338 \times 10^{28} \theta^{21} - 5.96777 \times 10^{26} \theta^{22} + 6.0287 \times 10^{24} \theta^{23} + \\
& \quad 4.31663 \times 10^{23} \theta^{24} - 2.91795 \times 10^{22} \theta^{25} + 9.78147 \times 10^{20} \theta^{26} - 2.03604 \times 10^{19} \theta^{27} + \\
& \quad 2.5186 \times 10^{17} \theta^{28} - 1.4316 \times 10^{15} \theta^{29} + 1232.34 \theta^{30} - 6.40418 \theta^{31})) /
\end{aligned}$$

$$\begin{aligned}
& \left( (-12.5664 + \theta)^{16} (-6.28319 + \theta)^7 (-6.28319 + \theta)^7 \theta^8 \sqrt{\frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta}{12.5664 - 1. \theta}} \right) - \\
& (7 (-1.72395 \times 10^{41} + 6.19455 \times 10^{41} \theta - 1.07157 \times 10^{42} \theta^2 + 1.18834 \times 10^{42} \theta^3 - \\
& \quad 9.49099 \times 10^{41} \theta^4 + 5.81452 \times 10^{41} \theta^5 - 2.84161 \times 10^{41} \theta^6 + 1.13742 \times 10^{41} \theta^7 - \\
& \quad 3.79913 \times 10^{40} \theta^8 + 1.07334 \times 10^{40} \theta^9 - 2.59064 \times 10^{39} \theta^{10} + 5.38068 \times 10^{38} \theta^{11} - \\
& \quad 9.66543 \times 10^{37} \theta^{12} + 1.50635 \times 10^{37} \theta^{13} - 2.03957 \times 10^{36} \theta^{14} + 2.39796 \times 10^{35} \theta^{15} - \\
& \quad 2.44178 \times 10^{34} \theta^{16} + 2.14222 \times 10^{33} \theta^{17} - 1.60499 \times 10^{32} \theta^{18} + 1.0121 \times 10^{31} \theta^{19} - \\
& \quad 5.24014 \times 10^{29} \theta^{20} + 2.12338 \times 10^{28} \theta^{21} - 5.96777 \times 10^{26} \theta^{22} + 6.0287 \times 10^{24} \theta^{23} + \\
& \quad 4.31663 \times 10^{23} \theta^{24} - 2.91795 \times 10^{22} \theta^{25} + 9.78147 \times 10^{20} \theta^{26} - 2.03604 \times 10^{19} \theta^{27} + \\
& \quad 2.5186 \times 10^{17} \theta^{28} - 1.4316 \times 10^{15} \theta^{29} + 1232.34 \theta^{30} - 6.40418 \theta^{31})) / \\
& \left( (-12.5664 + \theta)^{16} (-6.28319 + \theta)^7 (-6.28319 + \theta)^8 \theta^7 \sqrt{\frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta}{12.5664 - 1. \theta}} \right) - \\
& (7 (-1.72395 \times 10^{41} + 6.19455 \times 10^{41} \theta - 1.07157 \times 10^{42} \theta^2 + 1.18834 \times 10^{42} \theta^3 - \\
& \quad 9.49099 \times 10^{41} \theta^4 + 5.81452 \times 10^{41} \theta^5 - 2.84161 \times 10^{41} \theta^6 + 1.13742 \times 10^{41} \theta^7 - \\
& \quad 3.79913 \times 10^{40} \theta^8 + 1.07334 \times 10^{40} \theta^9 - 2.59064 \times 10^{39} \theta^{10} + 5.38068 \times 10^{38} \theta^{11} - \\
& \quad 9.66543 \times 10^{37} \theta^{12} + 1.50635 \times 10^{37} \theta^{13} - 2.03957 \times 10^{36} \theta^{14} + 2.39796 \times 10^{35} \theta^{15} - \\
& \quad 2.44178 \times 10^{34} \theta^{16} + 2.14222 \times 10^{33} \theta^{17} - 1.60499 \times 10^{32} \theta^{18} + 1.0121 \times 10^{31} \theta^{19} - \\
& \quad 5.24014 \times 10^{29} \theta^{20} + 2.12338 \times 10^{28} \theta^{21} - 5.96777 \times 10^{26} \theta^{22} + 6.0287 \times 10^{24} \theta^{23} + \\
& \quad 4.31663 \times 10^{23} \theta^{24} - 2.91795 \times 10^{22} \theta^{25} + 9.78147 \times 10^{20} \theta^{26} - 2.03604 \times 10^{19} \theta^{27} + \\
& \quad 2.5186 \times 10^{17} \theta^{28} - 1.4316 \times 10^{15} \theta^{29} + 1232.34 \theta^{30} - 6.40418 \theta^{31})) / \\
& \left( (-12.5664 + \theta)^{16} (-6.28319 + \theta)^8 (-6.28319 + \theta)^7 \theta^7 \sqrt{\frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta}{12.5664 - 1. \theta}} \right) - \\
& (16 (-1.72395 \times 10^{41} + 6.19455 \times 10^{41} \theta - 1.07157 \times 10^{42} \theta^2 + 1.18834 \times 10^{42} \theta^3 - \\
& \quad 9.49099 \times 10^{41} \theta^4 + 5.81452 \times 10^{41} \theta^5 - 2.84161 \times 10^{41} \theta^6 + 1.13742 \times 10^{41} \theta^7 - \\
& \quad 3.79913 \times 10^{40} \theta^8 + 1.07334 \times 10^{40} \theta^9 - 2.59064 \times 10^{39} \theta^{10} + 5.38068 \times 10^{38} \theta^{11} - \\
& \quad 9.66543 \times 10^{37} \theta^{12} + 1.50635 \times 10^{37} \theta^{13} - 2.03957 \times 10^{36} \theta^{14} + 2.39796 \times 10^{35} \theta^{15} - \\
& \quad 2.44178 \times 10^{34} \theta^{16} + 2.14222 \times 10^{33} \theta^{17} - 1.60499 \times 10^{32} \theta^{18} + 1.0121 \times 10^{31} \theta^{19} - \\
& \quad 5.24014 \times 10^{29} \theta^{20} + 2.12338 \times 10^{28} \theta^{21} - 5.96777 \times 10^{26} \theta^{22} + 6.0287 \times 10^{24} \theta^{23} + \\
& \quad 4.31663 \times 10^{23} \theta^{24} - 2.91795 \times 10^{22} \theta^{25} + 9.78147 \times 10^{20} \theta^{26} - 2.03604 \times 10^{19} \theta^{27} + \\
& \quad 2.5186 \times 10^{17} \theta^{28} - 1.4316 \times 10^{15} \theta^{29} + 1232.34 \theta^{30} - 6.40418 \theta^{31})) / \\
& \left( (-12.5664 + \theta)^{17} (-6.28319 + \theta)^7 (-6.28319 + \theta)^7 \theta^7 \sqrt{\frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta}{12.5664 - 1. \theta}} \right) - \\
& \left( \left( \frac{(-6.28319 + \theta) (-6.28319 + \theta)}{12.5664 - 1. \theta} + \frac{(-6.28319 + \theta) \theta}{12.5664 - 1. \theta} + \right. \right. \\
& \quad \left. \left. \frac{(-6.28319 + \theta) \theta}{12.5664 - 1. \theta} + \frac{1. (-6.28319 + \theta) (-6.28319 + \theta) \theta}{(12.5664 - 1. \theta)^2} \right) \right. \\
& \quad \left. (-1.72395 \times 10^{41} + 6.19455 \times 10^{41} \theta - 1.07157 \times 10^{42} \theta^2 + 1.18834 \times 10^{42} \theta^3 - \right. \\
& \quad \left. 9.49099 \times 10^{41} \theta^4 + 5.81452 \times 10^{41} \theta^5 - 2.84161 \times 10^{41} \theta^6 + 1.13742 \times 10^{41} \theta^7 - \right.
\end{aligned}$$

$$\left( \begin{aligned} & 3.79913 \times 10^{40} \theta^8 + 1.07334 \times 10^{40} \theta^9 - 2.59064 \times 10^{39} \theta^{10} + 5.38068 \times 10^{38} \theta^{11} - \\ & 9.66543 \times 10^{37} \theta^{12} + 1.50635 \times 10^{37} \theta^{13} - 2.03957 \times 10^{36} \theta^{14} + 2.39796 \times 10^{35} \theta^{15} - \\ & 2.44178 \times 10^{34} \theta^{16} + 2.14222 \times 10^{33} \theta^{17} - 1.60499 \times 10^{32} \theta^{18} + 1.0121 \times 10^{31} \theta^{19} - \\ & 5.24014 \times 10^{29} \theta^{20} + 2.12338 \times 10^{28} \theta^{21} - 5.96777 \times 10^{26} \theta^{22} + 6.0287 \times 10^{24} \theta^{23} + \\ & 4.31663 \times 10^{23} \theta^{24} - 2.91795 \times 10^{22} \theta^{25} + 9.78147 \times 10^{20} \theta^{26} - 2.03604 \times 10^{19} \theta^{27} + \\ & 2.5186 \times 10^{17} \theta^{28} - 1.4316 \times 10^{15} \theta^{29} + 1232.34 \theta^{30} - 6.40418 \theta^{31} \end{aligned} \right) /$$

$$\left( 2 (-12.5664 + \theta)^{16} (-6.28319 + \theta)^7 (-6.28319 + \theta)^7 \theta^7 \right.$$

$$\left. \left( \frac{(-6.28319 + \theta) (-6.28319 + \theta) \theta^{3/2}}{12.5664 - 1. \theta} \right)^{3/2} \right)$$

$$\text{Plot} \left[ \begin{aligned} & (6.19455209273797 \theta^{41} - 2.1431466839642813 \theta^{42} + 3.565009370006717 \theta^{42} \theta^2 - \\ & 3.7963951134124844 \theta^{42} \theta^3 + 2.9072579921172094 \theta^{42} \theta^4 - \\ & 1.704966113446511 \theta^{42} \theta^5 + 7.96195545588052 \theta^{41} \theta^6 - 3.03930044029144 \theta^{41} \theta^7 + \\ & 9.660059756888149 \theta^{40} \theta^8 - 2.5906381973931335 \theta^{40} \theta^9 + \\ & 5.91874449348705 \theta^{39} \theta^{10} - 1.1598513193775556 \theta^{39} \theta^{11} + \\ & 1.958255338382487 \theta^{38} \theta^{12} - 2.8553988600825893 \theta^{37} \theta^{13} + \\ & 3.596939571851961 \theta^{36} \theta^{14} - 3.906846560393781 \theta^{35} \theta^{15} + \\ & 3.64177989202655 \theta^{34} \theta^{16} - 2.8889851054401554 \theta^{33} \theta^{17} + \\ & 1.9229945192192892 \theta^{32} \theta^{18} - 1.0480288629706734 \theta^{31} \theta^{19} + \\ & 4.459098395517812 \theta^{29} \theta^{20} - 1.3129084643998237 \theta^{28} \theta^{21} + \\ & 1.386601891021861 \theta^{26} \theta^{22} + 1.0359908783061054 \theta^{25} \theta^{23} - \\ & 7.29488111264491 \theta^{23} \theta^{24} + 2.5431810805410436 \theta^{22} \theta^{25} - \\ & 5.497295020954338 \theta^{20} \theta^{26} + 7.052084140795507 \theta^{18} \theta^{27} - \\ & 4.151638705976147 \theta^{16} \theta^{28} + 36970.313279712114 \theta^{29} - 198.529430104246 \theta^{30}) / \end{aligned} \right.$$

$$\left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right.$$

$$\left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right) -$$

$$(7 (-1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} \theta - 1.0715733419821407 \theta^{42} \theta^2 +$$

$$1.1883364566689056 \theta^{42} \theta^3 - 9.490987783531211 \theta^{41} \theta^4 +$$

$$5.814515984234418 \theta^{41} \theta^5 - 2.841610189077518 \theta^{41} \theta^6 +$$

$$1.1374222079829315 \theta^{41} \theta^7 - 3.7991255503643 \theta^{40} \theta^8 + 1.073339972987572 \theta^{40}$$

$$\theta^9 - 2.5906381973931337 \theta^{39} \theta^{10} + 5.3806768122609554 \theta^{38} \theta^{11} -$$

$$9.66542766147963 \theta^{37} \theta^{12} + 1.5063504106448067 \theta^{37} \theta^{13} -$$

$$2.0395706143447065 \theta^{36} \theta^{14} + 2.3979597145679737 \theta^{35} \theta^{15} -$$

$$2.441779100246113 \theta^{34} \theta^{16} + 2.1422234658979708 \theta^{33} \theta^{17} -$$

$$1.6049917252445308 \theta^{32} \theta^{18} + 1.012102378536468 \theta^{31} \theta^{19} -$$

$$5.2401443148533675 \theta^{29} \theta^{20} + 2.1233801883418154 \theta^{28} \theta^{21} -$$

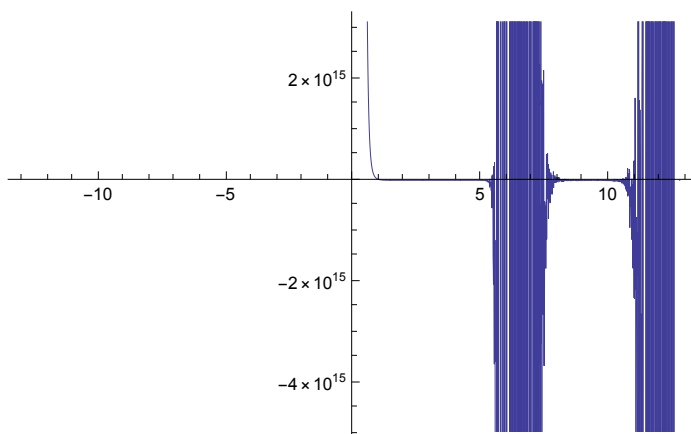
$$5.9677657472719257 \theta^{26} \theta^{22} + 6.028703874008091 \theta^{24} \theta^{23} +$$

$$\begin{aligned}
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{22} \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{20} \theta^{26} - 2.036035192946051 \cdot \theta^{19} \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{17} \theta^{28} - 1.4315995537848782 \cdot \theta^{15} \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) \Big/ \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \left. \theta^8 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 - 1 \cdot \theta}} \right) - \\
& (7 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - 1.0715733419821407 \cdot \theta^{42} \theta^2 + \\
& 1.1883364566689056 \cdot \theta^{42} \theta^3 - 9.490987783531211 \cdot \theta^{41} \theta^4 + \\
& 5.814515984234418 \cdot \theta^{41} \theta^5 - 2.841610189077518 \cdot \theta^{41} \theta^6 + \\
& 1.1374222079829315 \cdot \theta^{41} \theta^7 - 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \\
& \theta^9 - 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{26} \theta^{22} + 6.028703874008091 \cdot \theta^{24} \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{23} \theta^{24} - 2.9179524450579636 \cdot \theta^{22} \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{20} \theta^{26} - 2.036035192946051 \cdot \theta^{19} \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{17} \theta^{28} - 1.4315995537848782 \cdot \theta^{15} \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) \Big/ \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^8 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 - 1 \cdot \theta}} \right) - \\
& (7 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - 1.0715733419821407 \cdot \theta^{42} \theta^2 + \\
& 1.1883364566689056 \cdot \theta^{42} \theta^3 - 9.490987783531211 \cdot \theta^{41} \theta^4 + \\
& 5.814515984234418 \cdot \theta^{41} \theta^5 - 2.841610189077518 \cdot \theta^{41} \theta^6 + \\
& 1.1374222079829315 \cdot \theta^{41} \theta^7 - 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \\
& \theta^9 - 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{26} \theta^{22} + 6.028703874008091 \cdot \theta^{24} \theta^{23} +
\end{aligned}$$

$$\begin{aligned}
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^8 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta)(-6.283185226348451 + \theta)\theta}{12.566370614359172 - 1 \cdot \theta}} \right) - \\
& (16 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \\
& 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& 9.490987783531211 \cdot \theta^{41} \theta^4 + 5.814515984234418 \cdot \theta^{41} \theta^5 - \\
& 2.841610189077518 \cdot \theta^{41} \theta^6 + 1.1374222079829315 \cdot \theta^{41} \theta^7 - \\
& 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \theta^9 - \\
& 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{26} \theta^{22} + 6.028703874008091 \cdot \theta^{24} \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{23} \theta^{24} - 2.9179524450579636 \cdot \theta^{22} \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{20} \theta^{26} - 2.036035192946051 \cdot \theta^{19} \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{17} \theta^{28} - 1.4315995537848782 \cdot \theta^{15} \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) / \\
& \left( (-12.566370614359172 + \theta)^{17} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta)(-6.283185226348451 + \theta)\theta}{12.566370614359172 - 1 \cdot \theta}} \right) - \\
& \left( \left( \frac{(-6.283185388010722 + \theta)(-6.283185226348451 + \theta)}{12.566370614359172 - 1 \cdot \theta} + \right. \right. \\
& \left. \frac{(-6.283185388010722 + \theta)\theta}{12.566370614359172 - 1 \cdot \theta} + \frac{(-6.283185226348451 + \theta)\theta}{12.566370614359172 - 1 \cdot \theta} + \right. \\
& \left. \left. \frac{1 \cdot (-6.283185388010722 + \theta)(-6.283185226348451 + \theta)\theta}{(12.566370614359172 - 1 \cdot \theta)^2} \right) \right. \\
& \left. (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \right. \\
& 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& 9.490987783531211 \cdot \theta^{41} \theta^4 + 5.814515984234418 \cdot \theta^{41} \theta^5 - \\
& 2.841610189077518 \cdot \theta^{41} \theta^6 + 1.1374222079829315 \cdot \theta^{41} \theta^7 -
\end{aligned}$$



$$\begin{aligned}
& \left( 3.7991255503643 \cdot \theta^8 + 1.073339972987572 \cdot \theta^9 - \right. \\
& 2.5906381973931337 \cdot \theta^{10} + 5.3806768122609554 \cdot \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{12} + 1.5063504106448067 \cdot \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{14} + 2.3979597145679737 \cdot \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{16} + 2.1422234658979708 \cdot \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{18} + 1.012102378536468 \cdot \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{20} + 2.1233801883418154 \cdot \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& \left. 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \right) / \\
& \left( 2 \left( -12.566370614359172 \cdot \theta + \theta \right)^{16} \left( -6.283185388010722 \cdot \theta + \theta \right)^7 \right. \\
& \left. \left( -6.283185226348451 \cdot \theta + \theta \right)^7 \theta^7 \right. \\
& \left. \left( \frac{\left( -6.283185388010722 \cdot \theta + \theta \right) \left( -6.283185226348451 \cdot \theta + \theta \right) \theta^{3/2}}{12.566370614359172 \cdot \theta - 1 \cdot \theta} \right)^{3/2} \right), \{\theta, -13, 13\}
\end{aligned}$$



$$\begin{aligned}
& D \left[ \left( 6.19455209273797 \cdot \theta^{41} - 2.1431466839642813 \cdot \theta^{42} \theta + 3.565009370006717 \cdot \theta^{42} \theta^2 - \right. \right. \\
& 3.7963951134124844 \cdot \theta^{42} \theta^3 + 2.9072579921172094 \cdot \theta^{42} \theta^4 - \\
& 1.704966113446511 \cdot \theta^{42} \theta^5 + 7.96195545588052 \cdot \theta^{41} \theta^6 - 3.03930044029144 \cdot \theta^{41} \theta^7 + \\
& 9.660059756888149 \cdot \theta^{40} \theta^8 - 2.5906381973931335 \cdot \theta^{40} \theta^9 + \\
& 5.91874449348705 \cdot \theta^{39} \theta^{10} - 1.1598513193775556 \cdot \theta^{39} \theta^{11} + \\
& 1.9582555338382487 \cdot \theta^{38} \theta^{12} - 2.8553988600825893 \cdot \theta^{37} \theta^{13} + \\
& 3.596939571851961 \cdot \theta^{36} \theta^{14} - 3.906846560393781 \cdot \theta^{35} \theta^{15} + \\
& 3.64177989202655 \cdot \theta^{34} \theta^{16} - 2.8889851054401554 \cdot \theta^{33} \theta^{17} + \\
& 1.9229945192192892 \cdot \theta^{32} \theta^{18} - 1.0480288629706734 \cdot \theta^{31} \theta^{19} + \\
& 4.459098395517812 \cdot \theta^{29} \theta^{20} - 1.3129084643998237 \cdot \theta^{28} \theta^{21} + \\
& 1.386601891021861 \cdot \theta^{26} \theta^{22} + 1.0359908783061054 \cdot \theta^{25} \theta^{23} - \\
& 7.29488111264491 \cdot \theta^{23} \theta^{24} + 2.5431810805410436 \cdot \theta^{22} \theta^{25} - \\
& \left. \left. 5.497295020954338 \cdot \theta^{20} \theta^{26} + 7.052084140795507 \cdot \theta^{18} \theta^{27} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 4.151638705976147 \cdot \theta^{16} + 36970.313279712114 \cdot \theta^{29} - 198.529430104246 \cdot \theta^{30} \Big) / \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1 \cdot \theta}} \right) - \\
& (7 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - 1.0715733419821407 \cdot \theta^{42} \theta^2 + \\
& \quad 1.1883364566689056 \cdot \theta^{42} \theta^3 - 9.490987783531211 \cdot \theta^{41} \theta^4 + \\
& \quad 5.814515984234418 \cdot \theta^{41} \theta^5 - 2.841610189077518 \cdot \theta^{41} \theta^6 + \\
& \quad 1.1374222079829315 \cdot \theta^{41} \theta^7 - 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \\
& \quad \theta^9 - 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \cdot \theta^{26} \theta^{22} + 6.028703874008091 \cdot \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \cdot \theta^{23} \theta^{24} - 2.9179524450579636 \cdot \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \cdot \theta^{20} \theta^{26} - 2.036035192946051 \cdot \theta^{19} \theta^{27} + \\
& \quad 2.518601478855538 \cdot \theta^{17} \theta^{28} - 1.4315995537848782 \cdot \theta^{15} \theta^{29} + \\
& \quad 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31})) / \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \quad \left. \theta^8 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1 \cdot \theta}} \right) - \\
& (7 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - 1.0715733419821407 \cdot \theta^{42} \theta^2 + \\
& \quad 1.1883364566689056 \cdot \theta^{42} \theta^3 - 9.490987783531211 \cdot \theta^{41} \theta^4 + \\
& \quad 5.814515984234418 \cdot \theta^{41} \theta^5 - 2.841610189077518 \cdot \theta^{41} \theta^6 + \\
& \quad 1.1374222079829315 \cdot \theta^{41} \theta^7 - 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \\
& \quad \theta^9 - 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \cdot \theta^{26} \theta^{22} + 6.028703874008091 \cdot \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \cdot \theta^{23} \theta^{24} - 2.9179524450579636 \cdot \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \cdot \theta^{20} \theta^{26} - 2.036035192946051 \cdot \theta^{19} \theta^{27} + \\
& \quad 2.518601478855538 \cdot \theta^{17} \theta^{28} - 1.4315995537848782 \cdot \theta^{15} \theta^{29} +
\end{aligned}$$

$$\begin{aligned}
& 1232.3437759904039 \, \theta^{30} - 6.404175164653097 \, \theta^{31} \Big) \Big/ \\
& \left( (-12.566370614359172 \, \theta + \theta)^{16} (-6.283185388010722 \, \theta + \theta)^7 (-6.283185226348451 \, \theta + \theta)^8 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta) \theta}{12.566370614359172 \, \theta - 1. \, \theta}} \right) - \\
& (7 \, (-1.7239514242502465 \, \theta^{41} + 6.19455209273797 \, \theta^{41} \theta - 1.0715733419821407 \, \theta^{42} \theta^2 + \\
& \quad 1.1883364566689056 \, \theta^{42} \theta^3 - 9.490987783531211 \, \theta^{41} \theta^4 + \\
& \quad 5.814515984234418 \, \theta^{41} \theta^5 - 2.841610189077518 \, \theta^{41} \theta^6 + \\
& \quad 1.1374222079829315 \, \theta^{41} \theta^7 - 3.7991255503643 \, \theta^{40} \theta^8 + 1.073339972987572 \, \theta^{40} \\
& \quad \theta^9 - 2.5906381973931337 \, \theta^{39} \theta^{10} + 5.3806768122609554 \, \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \, \theta^{37} \theta^{12} + 1.5063504106448067 \, \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \, \theta^{36} \theta^{14} + 2.3979597145679737 \, \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \, \theta^{34} \theta^{16} + 2.1422234658979708 \, \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \, \theta^{32} \theta^{18} + 1.012102378536468 \, \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \, \theta^{29} \theta^{20} + 2.1233801883418154 \, \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \, \theta^{26} \theta^{22} + 6.028703874008091 \, \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \, \theta^{23} \theta^{24} - 2.9179524450579636 \, \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \, \theta^{20} \theta^{26} - 2.036035192946051 \, \theta^{19} \theta^{27} + \\
& \quad 2.518601478855538 \, \theta^{17} \theta^{28} - 1.4315995537848782 \, \theta^{15} \theta^{29} + \\
& \quad 1232.3437759904039 \, \theta^{30} - 6.404175164653097 \, \theta^{31} \Big) \Big/ \\
& \left( (-12.566370614359172 \, \theta + \theta)^{16} (-6.283185388010722 \, \theta + \theta)^8 (-6.283185226348451 \, \theta + \theta)^7 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta) \theta}{12.566370614359172 \, \theta - 1. \, \theta}} \right) - \\
& (16 \, (-1.7239514242502465 \, \theta^{41} + 6.19455209273797 \, \theta^{41} \theta - \\
& \quad 1.0715733419821407 \, \theta^{42} \theta^2 + 1.1883364566689056 \, \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \, \theta^{41} \theta^4 + 5.814515984234418 \, \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \, \theta^{41} \theta^6 + 1.1374222079829315 \, \theta^{41} \theta^7 - \\
& \quad 3.7991255503643 \, \theta^{40} \theta^8 + 1.073339972987572 \, \theta^{40} \theta^9 - \\
& \quad 2.5906381973931337 \, \theta^{39} \theta^{10} + 5.3806768122609554 \, \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \, \theta^{37} \theta^{12} + 1.5063504106448067 \, \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \, \theta^{36} \theta^{14} + 2.3979597145679737 \, \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \, \theta^{34} \theta^{16} + 2.1422234658979708 \, \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \, \theta^{32} \theta^{18} + 1.012102378536468 \, \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \, \theta^{29} \theta^{20} + 2.1233801883418154 \, \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \, \theta^{26} \theta^{22} + 6.028703874008091 \, \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \, \theta^{23} \theta^{24} - 2.9179524450579636 \, \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \, \theta^{20} \theta^{26} - 2.036035192946051 \, \theta^{19} \theta^{27} +
\end{aligned}$$

$$\begin{aligned}
& \left( 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \right. \\
& \left. 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \right) / \\
& \left( (-12.566370614359172 + \theta)^{17} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right) - \\
& \left( \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta)}{12.566370614359172 - 1. \theta} + \right. \right. \\
& \left. \frac{(-6.283185388010722 + \theta) \theta}{12.566370614359172 - 1. \theta} + \frac{(-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} + \right. \\
& \left. \frac{1. \cdot (-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{(12.566370614359172 - 1. \theta)^2} \right) \\
& \left( -1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} - \right. \\
& 1.0715733419821407 \cdot \theta^{42} + 1.1883364566689056 \cdot \theta^{42} - \\
& 9.490987783531211 \cdot \theta^{41} + 5.814515984234418 \cdot \theta^{41} - \\
& 2.841610189077518 \cdot \theta^{41} + 1.1374222079829315 \cdot \theta^{41} - \\
& 3.7991255503643 \cdot \theta^{40} + 1.073339972987572 \cdot \theta^{40} - \\
& 2.5906381973931337 \cdot \theta^{39} + 5.3806768122609554 \cdot \theta^{38} - \\
& 9.66542766147963 \cdot \theta^{37} + 1.5063504106448067 \cdot \theta^{37} - \\
& 2.0395706143447065 \cdot \theta^{36} + 2.3979597145679737 \cdot \theta^{35} - \\
& 2.441779100246113 \cdot \theta^{34} + 2.1422234658979708 \cdot \theta^{33} - \\
& 1.6049917252445308 \cdot \theta^{32} + 1.012102378536468 \cdot \theta^{31} - \\
& 5.2401443148533675 \cdot \theta^{29} + 2.1233801883418154 \cdot \theta^{28} - \\
& 5.9677657472719257 \cdot \theta^{26} + 6.028703874008091 \cdot \theta^{24} + \\
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{22} + \\
& 9.781465694388629 \cdot \theta^{20} - 2.036035192946051 \cdot \theta^{19} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& \left. 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \right) / \\
& \left( 2 (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 \right. \\
& \left. (-6.283185226348451 + \theta)^7 \theta^7 \right. \\
& \left. \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} \right)^{3/2} \right), \theta] \\
\text{Plot}[ \\
& (-2.1431466839642813 \cdot \theta^{42} + 7.130018740013434 \cdot \theta^{42} - 1.1389185340237452 \cdot \theta^{43} + \\
& 1.1629031968468838 \cdot \theta^{43} - 8.524830567232554 \cdot \theta^{42} + \\
& 4.777173273528312 \cdot \theta^{42} - 2.127510308204008 \cdot \theta^{42} + \\
& 7.728047805510519 \cdot \theta^{41} - 2.3315743776538203 \cdot \theta^{41} +
\end{aligned}$$

$$\begin{aligned}
& 5.918744493487051 \cdot \theta^9 - 1.2758364513153112 \cdot \theta^{10} + \\
& 2.3499066406058984 \cdot \theta^{11} - 3.712018518107366 \cdot \theta^{12} + \\
& 5.035715400592745 \cdot \theta^{13} - 5.860269840590671 \cdot \theta^{14} + \\
& 5.82684782724248 \cdot \theta^{15} - 4.911274679248264 \cdot \theta^{16} + \\
& 3.4613901345947207 \cdot \theta^{17} - 1.9912548396442796 \cdot \theta^{18} + \\
& 8.918196791035625 \cdot \theta^{19} - 2.75710777523963 \cdot \theta^{20} + \\
& 3.050524160248094 \cdot \theta^{21} + 2.3827790201040424 \cdot \theta^{22} - \\
& 1.7507714670347782 \cdot \theta^{23} + 6.35795270135261 \cdot \theta^{24} - 1.4292967054481279 \cdot \theta^{22} \\
& \theta^{25} + 1.9040627180147868 \cdot \theta^{20} \theta^{26} - 1.1624588376733212 \cdot \theta^{18} \theta^{27} + \\
& 1.0721390851116513 \cdot \theta^6 \theta^{28} - 5955.88290312738 \cdot \theta^{29} \Big) / \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1 \cdot \theta}} \right) - \\
& (14 (6.19455209273797 \cdot \theta^{41} - 2.1431466839642813 \cdot \theta^{42} \theta + 3.565009370006717 \cdot \theta^{42} \theta^2 - \\
& 3.7963951134124844 \cdot \theta^{42} \theta^3 + 2.9072579921172094 \cdot \theta^{42} \theta^4 - \\
& 1.704966113446511 \cdot \theta^{42} \theta^5 + 7.96195545588052 \cdot \theta^{41} \theta^6 - 3.03930044029144 \cdot \theta^{41} \\
& \theta^7 + 9.660059756888149 \cdot \theta^{40} \theta^8 - 2.5906381973931335 \cdot \theta^{40} \theta^9 + \\
& 5.91874449348705 \cdot \theta^{39} \theta^{10} - 1.1598513193775556 \cdot \theta^{39} \theta^{11} + \\
& 1.9582555338382487 \cdot \theta^{38} \theta^{12} - 2.8553988600825893 \cdot \theta^{37} \theta^{13} + \\
& 3.596939571851961 \cdot \theta^{36} \theta^{14} - 3.906846560393781 \cdot \theta^{35} \theta^{15} + \\
& 3.64177989202655 \cdot \theta^{34} \theta^{16} - 2.8889851054401554 \cdot \theta^{33} \theta^{17} + \\
& 1.9229945192192892 \cdot \theta^{32} \theta^{18} - 1.0480288629706734 \cdot \theta^{31} \theta^{19} + \\
& 4.459098395517812 \cdot \theta^{29} \theta^{20} - 1.3129084643998237 \cdot \theta^{28} \theta^{21} + \\
& 1.386601891021861 \cdot \theta^{26} \theta^{22} + 1.0359908783061054 \cdot \theta^{25} \theta^{23} - \\
& 7.29488111264491 \cdot \theta^{23} \theta^{24} + 2.5431810805410436 \cdot \theta^{22} \theta^{25} - \\
& 5.497295020954338 \cdot \theta^{20} \theta^{26} + 7.052084140795507 \cdot \theta^{18} \theta^{27} - \\
& 4.151638705976147 \cdot \theta^{16} \theta^{28} + 36970.313279712114 \cdot \theta^{29} - 198.529430104246 \cdot \theta^{30} \Big) / \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \left. \theta^8 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1 \cdot \theta}} \right) - \\
& (14 (6.19455209273797 \cdot \theta^{41} - 2.1431466839642813 \cdot \theta^{42} \theta + 3.565009370006717 \cdot \theta^{42} \theta^2 - \\
& 3.7963951134124844 \cdot \theta^{42} \theta^3 + 2.9072579921172094 \cdot \theta^{42} \theta^4 - \\
& 1.704966113446511 \cdot \theta^{42} \theta^5 + 7.96195545588052 \cdot \theta^{41} \theta^6 - 3.03930044029144 \cdot \theta^{41} \\
& \theta^7 + 9.660059756888149 \cdot \theta^{40} \theta^8 - 2.5906381973931335 \cdot \theta^{40} \theta^9 + \\
& 5.91874449348705 \cdot \theta^{39} \theta^{10} - 1.1598513193775556 \cdot \theta^{39} \theta^{11} + \\
& 1.9582555338382487 \cdot \theta^{38} \theta^{12} - 2.8553988600825893 \cdot \theta^{37} \theta^{13} +
\end{aligned}$$

$$\begin{aligned}
& 3.596939571851961 \cdot \theta^{14} - 3.906846560393781 \cdot \theta^{15} + \\
& 3.64177989202655 \cdot \theta^{16} - 2.8889851054401554 \cdot \theta^{17} + \\
& 1.9229945192192892 \cdot \theta^{18} - 1.0480288629706734 \cdot \theta^{19} + \\
& 4.459098395517812 \cdot \theta^{20} - 1.3129084643998237 \cdot \theta^{21} + \\
& 1.386601891021861 \cdot \theta^{22} + 1.0359908783061054 \cdot \theta^{23} - \\
& 7.29488111264491 \cdot \theta^{24} + 2.5431810805410436 \cdot \theta^{25} - \\
& 5.497295020954338 \cdot \theta^{26} + 7.052084140795507 \cdot \theta^{27} - \\
& 4.151638705976147 \cdot \theta^{28} + 36970.313279712114 \cdot \theta^{29} - 198.529430104246 \cdot \theta^{30} \Big) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^8 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1 \cdot \theta}} \right) - \\
& (14 (6.19455209273797 \cdot \theta^{41} - 2.1431466839642813 \cdot \theta^{42} + 3.565009370006717 \cdot \theta^{42} \theta^2 - \\
& 3.7963951134124844 \cdot \theta^{42} \theta^3 + 2.9072579921172094 \cdot \theta^{42} \theta^4 - \\
& 1.704966113446511 \cdot \theta^{42} \theta^5 + 7.96195545588052 \cdot \theta^{41} \theta^6 - 3.03930044029144 \cdot \theta^{41} \\
& \theta^7 + 9.660059756888149 \cdot \theta^{40} \theta^8 - 2.5906381973931335 \cdot \theta^{40} \theta^9 + \\
& 5.91874449348705 \cdot \theta^{39} \theta^{10} - 1.1598513193775556 \cdot \theta^{39} \theta^{11} + \\
& 1.9582555338382487 \cdot \theta^{38} \theta^{12} - 2.8553988600825893 \cdot \theta^{37} \theta^{13} + \\
& 3.596939571851961 \cdot \theta^{36} \theta^{14} - 3.906846560393781 \cdot \theta^{35} \theta^{15} + \\
& 3.64177989202655 \cdot \theta^{34} \theta^{16} - 2.8889851054401554 \cdot \theta^{33} \theta^{17} + \\
& 1.9229945192192892 \cdot \theta^{32} \theta^{18} - 1.0480288629706734 \cdot \theta^{31} \theta^{19} + \\
& 4.459098395517812 \cdot \theta^{29} \theta^{20} - 1.3129084643998237 \cdot \theta^{28} \theta^{21} + \\
& 1.386601891021861 \cdot \theta^{26} \theta^{22} + 1.0359908783061054 \cdot \theta^{25} \theta^{23} - \\
& 7.29488111264491 \cdot \theta^{23} \theta^{24} + 2.5431810805410436 \cdot \theta^{22} \theta^{25} - \\
& 5.497295020954338 \cdot \theta^{20} \theta^{26} + 7.052084140795507 \cdot \theta^{18} \theta^{27} - \\
& 4.151638705976147 \cdot \theta^{16} \theta^{28} + 36970.313279712114 \cdot \theta^{29} - 198.529430104246 \cdot \theta^{30} \Big) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^8 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1 \cdot \theta}} \right) - \\
& (32 (6.19455209273797 \cdot \theta^{41} - 2.1431466839642813 \cdot \theta^{42} \theta + 3.565009370006717 \cdot \theta^{42} \theta^2 - \\
& 3.7963951134124844 \cdot \theta^{42} \theta^3 + 2.9072579921172094 \cdot \theta^{42} \theta^4 - \\
& 1.704966113446511 \cdot \theta^{42} \theta^5 + 7.96195545588052 \cdot \theta^{41} \theta^6 - 3.03930044029144 \cdot \theta^{41} \\
& \theta^7 + 9.660059756888149 \cdot \theta^{40} \theta^8 - 2.5906381973931335 \cdot \theta^{40} \theta^9 + \\
& 5.91874449348705 \cdot \theta^{39} \theta^{10} - 1.1598513193775556 \cdot \theta^{39} \theta^{11} + \\
& 1.9582555338382487 \cdot \theta^{38} \theta^{12} - 2.8553988600825893 \cdot \theta^{37} \theta^{13} + \\
& 3.596939571851961 \cdot \theta^{36} \theta^{14} - 3.906846560393781 \cdot \theta^{35} \theta^{15} + \\
& 3.64177989202655 \cdot \theta^{34} \theta^{16} - 2.8889851054401554 \cdot \theta^{33} \theta^{17} +
\end{aligned}$$

$$\begin{aligned}
& \left( 1.9229945192192892 \cdot \theta^{18} - 1.0480288629706734 \cdot \theta^{19} + \right. \\
& 4.459098395517812 \cdot \theta^{20} - 1.3129084643998237 \cdot \theta^{21} + \\
& 1.386601891021861 \cdot \theta^{22} + 1.0359908783061054 \cdot \theta^{23} - \\
& 7.29488111264491 \cdot \theta^{24} + 2.5431810805410436 \cdot \theta^{25} - \\
& 5.497295020954338 \cdot \theta^{26} + 7.052084140795507 \cdot \theta^{27} - \\
& \left. 4.151638705976147 \cdot \theta^{28} + 36970.313279712114 \cdot \theta^{29} - 198.529430104246 \cdot \theta^{30} \right) / \\
& \left( (-12.566370614359172 + \theta)^{17} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right) - \\
& \left( \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta)}{12.566370614359172 - 1. \theta} + \right. \right. \\
& \left. \frac{(-6.283185388010722 + \theta) \theta}{12.566370614359172 - 1. \theta} + \frac{(-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} + \right. \\
& \left. \frac{1. \cdot (-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{(12.566370614359172 - 1. \theta)^2} \right) \\
& \left( 6.19455209273797 \cdot \theta^{41} - 2.1431466839642813 \cdot \theta^{42} + 3.565009370006717 \cdot \theta^{42} \theta^2 - \right. \\
& 3.7963951134124844 \cdot \theta^{42} \theta^3 + 2.9072579921172094 \cdot \theta^{42} \theta^4 - \\
& 1.704966113446511 \cdot \theta^{42} \theta^5 + 7.96195545588052 \cdot \theta^{41} \theta^6 - 3.03930044029144 \cdot \theta^{41} \\
& \theta^7 + 9.660059756888149 \cdot \theta^{40} \theta^8 - 2.5906381973931335 \cdot \theta^{40} \theta^9 + \\
& 5.91874449348705 \cdot \theta^{39} \theta^{10} - 1.1598513193775556 \cdot \theta^{39} \theta^{11} + \\
& 1.9582555338382487 \cdot \theta^{38} \theta^{12} - 2.8553988600825893 \cdot \theta^{37} \theta^{13} + \\
& 3.596939571851961 \cdot \theta^{36} \theta^{14} - 3.906846560393781 \cdot \theta^{35} \theta^{15} + \\
& 3.64177989202655 \cdot \theta^{34} \theta^{16} - 2.8889851054401554 \cdot \theta^{33} \theta^{17} + \\
& 1.9229945192192892 \cdot \theta^{32} \theta^{18} - 1.0480288629706734 \cdot \theta^{31} \theta^{19} + \\
& 4.459098395517812 \cdot \theta^{29} \theta^{20} - 1.3129084643998237 \cdot \theta^{28} \theta^{21} + \\
& 1.386601891021861 \cdot \theta^{26} \theta^{22} + 1.0359908783061054 \cdot \theta^{25} \theta^{23} - \\
& 7.29488111264491 \cdot \theta^{24} \theta^{24} + 2.5431810805410436 \cdot \theta^{22} \theta^{25} - \\
& 5.497295020954338 \cdot \theta^{20} \theta^{26} + 7.052084140795507 \cdot \theta^{18} \theta^{27} - \\
& \left. 4.151638705976147 \cdot \theta^{16} \theta^{28} + 36970.313279712114 \cdot \theta^{29} - 198.529430104246 \cdot \theta^{30} \right) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^7 \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} \right)^{3/2} \right) + \\
& (56 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \\
& 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& 9.490987783531211 \cdot \theta^{41} \theta^4 + 5.814515984234418 \cdot \theta^{41} \theta^5 - \\
& 2.841610189077518 \cdot \theta^{41} \theta^6 + 1.1374222079829315 \cdot \theta^{41} \theta^7 -
\end{aligned}$$

$$\begin{aligned}
& 3.7991255503643 \cdot \theta^8 + 1.073339972987572 \cdot \theta^9 - \\
& 2.5906381973931337 \cdot \theta^{10} + 5.3806768122609554 \cdot \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{12} + 1.5063504106448067 \cdot \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{14} + 2.3979597145679737 \cdot \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{16} + 2.1422234658979708 \cdot \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{18} + 1.012102378536468 \cdot \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{20} + 2.1233801883418154 \cdot \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \right. \\
& \left. \theta^9 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1 \cdot \theta}} \right) + \\
& (98 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} - \\
& 1.0715733419821407 \cdot \theta^{42} + 1.1883364566689056 \cdot \theta^{42} - \\
& 9.490987783531211 \cdot \theta^{41} + 5.814515984234418 \cdot \theta^{41} - \\
& 2.841610189077518 \cdot \theta^{41} + 1.1374222079829315 \cdot \theta^{41} - \\
& 3.7991255503643 \cdot \theta^8 + 1.073339972987572 \cdot \theta^9 - \\
& 2.5906381973931337 \cdot \theta^{10} + 5.3806768122609554 \cdot \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{12} + 1.5063504106448067 \cdot \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{14} + 2.3979597145679737 \cdot \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{16} + 2.1422234658979708 \cdot \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{18} + 1.012102378536468 \cdot \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{20} + 2.1233801883418154 \cdot \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^8 \right. \\
& \left. \theta^8 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1 \cdot \theta}} \right) + \\
& (98 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} - \\
& 1.0715733419821407 \cdot \theta^{42} + 1.1883364566689056 \cdot \theta^{42} -
\end{aligned}$$



$$\begin{aligned}
& 9.490987783531211 \cdot \theta^4 + 5.814515984234418 \cdot \theta^5 - \\
& 2.841610189077518 \cdot \theta^6 + 1.1374222079829315 \cdot \theta^7 - \\
& 3.7991255503643 \cdot \theta^8 + 1.073339972987572 \cdot \theta^9 - \\
& 2.5906381973931337 \cdot \theta^{10} + 5.3806768122609554 \cdot \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{12} + 1.5063504106448067 \cdot \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{14} + 2.3979597145679737 \cdot \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{16} + 2.1422234658979708 \cdot \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{18} + 1.012102378536468 \cdot \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{20} + 2.1233801883418154 \cdot \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) / \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{16} (-6.283185388010722 \cdot \theta + \theta)^8 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \left. \theta^8 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1 \cdot \theta}} \right) + \\
& (224 (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \\
& 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& 9.490987783531211 \cdot \theta^4 + 5.814515984234418 \cdot \theta^5 - \\
& 2.841610189077518 \cdot \theta^6 + 1.1374222079829315 \cdot \theta^7 - \\
& 3.7991255503643 \cdot \theta^8 + 1.073339972987572 \cdot \theta^9 - \\
& 2.5906381973931337 \cdot \theta^{10} + 5.3806768122609554 \cdot \theta^{11} - \\
& 9.66542766147963 \cdot \theta^{12} + 1.5063504106448067 \cdot \theta^{13} - \\
& 2.0395706143447065 \cdot \theta^{14} + 2.3979597145679737 \cdot \theta^{15} - \\
& 2.441779100246113 \cdot \theta^{16} + 2.1422234658979708 \cdot \theta^{17} - \\
& 1.6049917252445308 \cdot \theta^{18} + 1.012102378536468 \cdot \theta^{19} - \\
& 5.2401443148533675 \cdot \theta^{20} + 2.1233801883418154 \cdot \theta^{21} - \\
& 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{23} + \\
& 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \Big) / \\
& \left( (-12.566370614359172 \cdot \theta + \theta)^{17} (-6.283185388010722 \cdot \theta + \theta)^7 (-6.283185226348451 \cdot \theta + \theta)^7 \right. \\
& \left. \theta^8 \sqrt{\frac{(-6.283185388010722 \cdot \theta + \theta) (-6.283185226348451 \cdot \theta + \theta) \theta}{12.566370614359172 \cdot \theta - 1 \cdot \theta}} \right) +
\end{aligned}$$

$$\begin{aligned}
& (56 \left( -1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - \right. \\
& \quad 1.0715733419821407 \theta^{42} + 1.1883364566689056 \theta^{42} - \\
& \quad 9.490987783531211 \theta^{41} + 5.814515984234418 \theta^{41} - \\
& \quad 2.841610189077518 \theta^{41} + 1.1374222079829315 \theta^{41} - \\
& \quad 3.7991255503643 \theta^{40} + 1.073339972987572 \theta^{40} - \\
& \quad 2.5906381973931337 \theta^{39} + 5.3806768122609554 \theta^{38} - \\
& \quad 9.66542766147963 \theta^{37} + 1.5063504106448067 \theta^{37} - \\
& \quad 2.0395706143447065 \theta^{36} + 2.3979597145679737 \theta^{35} - \\
& \quad 2.441779100246113 \theta^{34} + 2.1422234658979708 \theta^{33} - \\
& \quad 1.6049917252445308 \theta^{32} + 1.012102378536468 \theta^{31} - \\
& \quad 5.2401443148533675 \theta^{29} + 2.1233801883418154 \theta^{28} - \\
& \quad 5.9677657472719257 \theta^{26} + 6.028703874008091 \theta^{24} + \\
& \quad 4.316628659608773 \theta^{23} - 2.9179524450579636 \theta^{22} + \\
& \quad 9.781465694388629 \theta^{20} - 2.036035192946051 \theta^{19} + \\
& \quad 2.518601478855538 \theta^{17} - 1.4315995537848782 \theta^{15} + \\
& \quad \left. 1232.3437759904039 \theta^{30} - 6.404175164653097 \theta^{31} \right) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^9 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right) + \\
& (98 \left( -1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - \right. \\
& \quad 1.0715733419821407 \theta^{42} + 1.1883364566689056 \theta^{42} - \\
& \quad 9.490987783531211 \theta^{41} + 5.814515984234418 \theta^{41} - \\
& \quad 2.841610189077518 \theta^{41} + 1.1374222079829315 \theta^{41} - \\
& \quad 3.7991255503643 \theta^{40} + 1.073339972987572 \theta^{40} - \\
& \quad 2.5906381973931337 \theta^{39} + 5.3806768122609554 \theta^{38} - \\
& \quad 9.66542766147963 \theta^{37} + 1.5063504106448067 \theta^{37} - \\
& \quad 2.0395706143447065 \theta^{36} + 2.3979597145679737 \theta^{35} - \\
& \quad 2.441779100246113 \theta^{34} + 2.1422234658979708 \theta^{33} - \\
& \quad 1.6049917252445308 \theta^{32} + 1.012102378536468 \theta^{31} - \\
& \quad 5.2401443148533675 \theta^{29} + 2.1233801883418154 \theta^{28} - \\
& \quad 5.9677657472719257 \theta^{26} + 6.028703874008091 \theta^{24} + \\
& \quad 4.316628659608773 \theta^{23} - 2.9179524450579636 \theta^{22} + \\
& \quad 9.781465694388629 \theta^{20} - 2.036035192946051 \theta^{19} + \\
& \quad 2.518601478855538 \theta^{17} - 1.4315995537848782 \theta^{15} + \\
& \quad \left. 1232.3437759904039 \theta^{30} - 6.404175164653097 \theta^{31} \right) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^8 (-6.283185226348451 + \theta)^8 \right)
\end{aligned}$$

$$\begin{aligned}
& \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} + \\
(224 & (-1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - \\
& 1.0715733419821407 \theta^{42} \theta^2 + 1.1883364566689056 \theta^{42} \theta^3 - \\
& 9.490987783531211 \theta^{41} \theta^4 + 5.814515984234418 \theta^{41} \theta^5 - \\
& 2.841610189077518 \theta^{41} \theta^6 + 1.1374222079829315 \theta^{41} \theta^7 - \\
& 3.7991255503643 \theta^{40} \theta^8 + 1.073339972987572 \theta^{40} \theta^9 - \\
& 2.5906381973931337 \theta^{39} \theta^{10} + 5.3806768122609554 \theta^{38} \theta^{11} - \\
& 9.66542766147963 \theta^{37} \theta^{12} + 1.5063504106448067 \theta^{37} \theta^{13} - \\
& 2.0395706143447065 \theta^{36} \theta^{14} + 2.3979597145679737 \theta^{35} \theta^{15} - \\
& 2.441779100246113 \theta^{34} \theta^{16} + 2.1422234658979708 \theta^{33} \theta^{17} - \\
& 1.6049917252445308 \theta^{32} \theta^{18} + 1.012102378536468 \theta^{31} \theta^{19} - \\
& 5.2401443148533675 \theta^{29} \theta^{20} + 2.1233801883418154 \theta^{28} \theta^{21} - \\
& 5.9677657472719257 \theta^{26} \theta^{22} + 6.028703874008091 \theta^{24} \theta^{23} + \\
& 4.316628659608773 \theta^{23} \theta^{24} - 2.9179524450579636 \theta^{22} \theta^{25} + \\
& 9.781465694388629 \theta^{20} \theta^{26} - 2.036035192946051 \theta^{19} \theta^{27} + \\
& 2.518601478855538 \theta^{17} \theta^{28} - 1.4315995537848782 \theta^{15} \theta^{29} + \\
& 1232.3437759904039 \theta^{30} - 6.404175164653097 \theta^{31})) / \\
& \left( (-12.566370614359172 + \theta)^{17} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^8 \right. \\
& \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} + \right) \\
(56 & (-1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - \\
& 1.0715733419821407 \theta^{42} \theta^2 + 1.1883364566689056 \theta^{42} \theta^3 - \\
& 9.490987783531211 \theta^{41} \theta^4 + 5.814515984234418 \theta^{41} \theta^5 - \\
& 2.841610189077518 \theta^{41} \theta^6 + 1.1374222079829315 \theta^{41} \theta^7 - \\
& 3.7991255503643 \theta^{40} \theta^8 + 1.073339972987572 \theta^{40} \theta^9 - \\
& 2.5906381973931337 \theta^{39} \theta^{10} + 5.3806768122609554 \theta^{38} \theta^{11} - \\
& 9.66542766147963 \theta^{37} \theta^{12} + 1.5063504106448067 \theta^{37} \theta^{13} - \\
& 2.0395706143447065 \theta^{36} \theta^{14} + 2.3979597145679737 \theta^{35} \theta^{15} - \\
& 2.441779100246113 \theta^{34} \theta^{16} + 2.1422234658979708 \theta^{33} \theta^{17} - \\
& 1.6049917252445308 \theta^{32} \theta^{18} + 1.012102378536468 \theta^{31} \theta^{19} - \\
& 5.2401443148533675 \theta^{29} \theta^{20} + 2.1233801883418154 \theta^{28} \theta^{21} - \\
& 5.9677657472719257 \theta^{26} \theta^{22} + 6.028703874008091 \theta^{24} \theta^{23} + \\
& 4.316628659608773 \theta^{23} \theta^{24} - 2.9179524450579636 \theta^{22} \theta^{25} + \\
& 9.781465694388629 \theta^{20} \theta^{26} - 2.036035192946051 \theta^{19} \theta^{27} + \\
& 2.518601478855538 \theta^{17} \theta^{28} - 1.4315995537848782 \theta^{15} \theta^{29} + \\
& 1232.3437759904039 \theta^{30} - 6.404175164653097 \theta^{31})) /
\end{aligned}$$

$$\begin{aligned}
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^9 (-6.283185226348451 + \theta)^7 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right) + \\
& (224 \left( -1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - \right. \\
& \quad 1.0715733419821407 \theta^{42} \theta^2 + 1.1883364566689056 \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \theta^{41} \theta^4 + 5.814515984234418 \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \theta^{41} \theta^6 + 1.1374222079829315 \theta^{41} \theta^7 - \\
& \quad 3.7991255503643 \theta^{40} \theta^8 + 1.073339972987572 \theta^{40} \theta^9 - \\
& \quad 2.5906381973931337 \theta^{39} \theta^{10} + 5.3806768122609554 \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \theta^{37} \theta^{12} + 1.5063504106448067 \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \theta^{36} \theta^{14} + 2.3979597145679737 \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \theta^{34} \theta^{16} + 2.1422234658979708 \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \theta^{32} \theta^{18} + 1.012102378536468 \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \theta^{29} \theta^{20} + 2.1233801883418154 \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \theta^{26} \theta^{22} + 6.028703874008091 \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \theta^{23} \theta^{24} - 2.9179524450579636 \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \theta^{20} \theta^{26} - 2.036035192946051 \theta^{19} \theta^{27} + \\
& \quad 2.518601478855538 \theta^{17} \theta^{28} - 1.4315995537848782 \theta^{15} \theta^{29} + \\
& \quad \left. 1232.3437759904039 \theta^{30} - 6.404175164653097 \theta^{31} \right) \Big/ \\
& \left( (-12.566370614359172 + \theta)^{17} (-6.283185388010722 + \theta)^8 (-6.283185226348451 + \theta)^7 \right. \\
& \quad \left. \theta^7 \sqrt{\frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta}} \right) + \\
& (272 \left( -1.7239514242502465 \theta^{41} + 6.19455209273797 \theta^{41} - \right. \\
& \quad 1.0715733419821407 \theta^{42} \theta^2 + 1.1883364566689056 \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \theta^{41} \theta^4 + 5.814515984234418 \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \theta^{41} \theta^6 + 1.1374222079829315 \theta^{41} \theta^7 - \\
& \quad 3.7991255503643 \theta^{40} \theta^8 + 1.073339972987572 \theta^{40} \theta^9 - \\
& \quad 2.5906381973931337 \theta^{39} \theta^{10} + 5.3806768122609554 \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \theta^{37} \theta^{12} + 1.5063504106448067 \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \theta^{36} \theta^{14} + 2.3979597145679737 \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \theta^{34} \theta^{16} + 2.1422234658979708 \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \theta^{32} \theta^{18} + 1.012102378536468 \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \theta^{29} \theta^{20} + 2.1233801883418154 \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \theta^{26} \theta^{22} + 6.028703874008091 \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \theta^{23} \theta^{24} - 2.9179524450579636 \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \theta^{20} \theta^{26} - 2.036035192946051 \theta^{19} \theta^{27} + \\
& \quad \left. 2.518601478855538 \theta^{17} \theta^{28} - 1.4315995537848782 \theta^{15} \theta^{29} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1232.3437759904039 \, \theta^{30} - 6.404175164653097 \, \theta^{31} \right) / \\
& \left( (-12.566370614359172 \, \theta + \theta)^{18} (-6.283185388010722 \, \theta + \theta)^7 (-6.283185226348451 \, \theta + \theta)^7 \right. \\
& \quad \theta^7 \sqrt{\frac{(-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta) \theta}{12.566370614359172 \, \theta - 1. \, \theta}} \Big) - \\
& \left( \left( \frac{2 (-6.283185388010722 \, \theta + \theta)}{12.566370614359172 \, \theta - 1. \, \theta} + \frac{2 (-6.283185226348451 \, \theta + \theta)}{12.566370614359172 \, \theta - 1. \, \theta} + \right. \right. \\
& \quad \frac{2. \, \theta (-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta)}{(12.566370614359172 \, \theta - 1. \, \theta)^2} + \\
& \quad \frac{2 \, \theta}{12.566370614359172 \, \theta - 1. \, \theta} + \frac{2. \, \theta (-6.283185388010722 \, \theta + \theta) \theta}{(12.566370614359172 \, \theta - 1. \, \theta)^2} + \\
& \quad \frac{2. \, \theta (-6.283185226348451 \, \theta + \theta) \theta}{(12.566370614359172 \, \theta - 1. \, \theta)^2} + \\
& \quad \left. \left. \frac{2. \, \theta (-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta) \theta}{(12.566370614359172 \, \theta - 1. \, \theta)^3} \right) \right) \\
& \left( -1.7239514242502465 \, \theta^{41} + 6.19455209273797 \, \theta^{41} \theta - \right. \\
& \quad 1.0715733419821407 \, \theta^{42} \theta^2 + 1.1883364566689056 \, \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \, \theta^{41} \theta^4 + 5.814515984234418 \, \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \, \theta^{41} \theta^6 + 1.1374222079829315 \, \theta^{41} \theta^7 - \\
& \quad 3.7991255503643 \, \theta^{40} \theta^8 + 1.073339972987572 \, \theta^{40} \theta^9 - \\
& \quad 2.5906381973931337 \, \theta^{39} \theta^{10} + 5.3806768122609554 \, \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \, \theta^{37} \theta^{12} + 1.5063504106448067 \, \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \, \theta^{36} \theta^{14} + 2.3979597145679737 \, \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \, \theta^{34} \theta^{16} + 2.1422234658979708 \, \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \, \theta^{32} \theta^{18} + 1.012102378536468 \, \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \, \theta^{29} \theta^{20} + 2.1233801883418154 \, \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \, \theta^{26} \theta^{22} + 6.028703874008091 \, \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \, \theta^{23} \theta^{24} - 2.9179524450579636 \, \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \, \theta^{20} \theta^{26} - 2.036035192946051 \, \theta^{19} \theta^{27} + \\
& \quad 2.518601478855538 \, \theta^{17} \theta^{28} - 1.4315995537848782 \, \theta^{15} \theta^{29} + \\
& \quad \left. 1232.3437759904039 \, \theta^{30} - 6.404175164653097 \, \theta^{31} \right) / \\
& \left( 2 (-12.566370614359172 \, \theta + \theta)^{16} (-6.283185388010722 \, \theta + \theta)^7 \right. \\
& \quad (-6.283185226348451 \, \theta + \theta)^7 \theta^7 \\
& \quad \left. \left( \frac{(-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta) \theta}{12.566370614359172 \, \theta - 1. \, \theta} \right)^{3/2} \right) + \\
& \left( 7 \left( \frac{(-6.283185388010722 \, \theta + \theta) (-6.283185226348451 \, \theta + \theta)}{12.566370614359172 \, \theta - 1. \, \theta} + \right. \right.
\end{aligned}$$

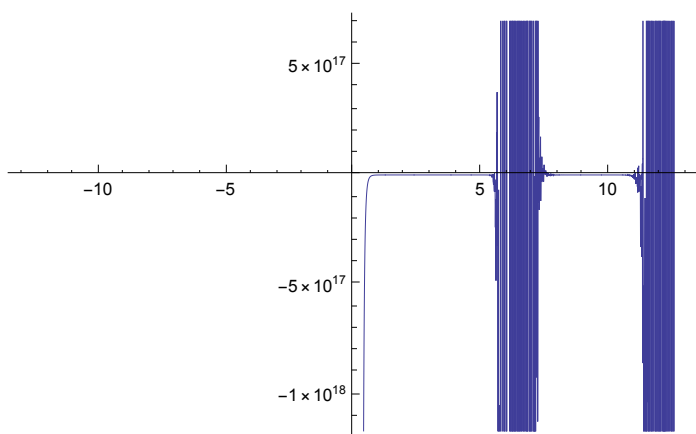
$$\begin{aligned}
& \frac{(-6.283185388010722' + \theta) \theta}{12.566370614359172' - 1.' \theta} + \frac{(-6.283185226348451' + \theta) \theta}{12.566370614359172' - 1.' \theta} + \\
& \frac{1.' (-6.283185388010722' + \theta) (-6.283185226348451' + \theta) \theta}{(12.566370614359172' - 1.' \theta)^2} \Bigg) \\
& (-1.7239514242502465' * ^{41} \theta + 6.19455209273797' * ^{41} \theta - \\
& 1.0715733419821407' * ^{42} \theta^2 + 1.1883364566689056' * ^{42} \theta^3 - \\
& 9.490987783531211' * ^{41} \theta^4 + 5.814515984234418' * ^{41} \theta^5 - \\
& 2.841610189077518' * ^{41} \theta^6 + 1.1374222079829315' * ^{41} \theta^7 - \\
& 3.7991255503643' * ^{40} \theta^8 + 1.073339972987572' * ^{40} \theta^9 - \\
& 2.5906381973931337' * ^{39} \theta^{10} + 5.3806768122609554' * ^{38} \theta^{11} - \\
& 9.66542766147963' * ^{37} \theta^{12} + 1.5063504106448067' * ^{37} \theta^{13} - \\
& 2.0395706143447065' * ^{36} \theta^{14} + 2.3979597145679737' * ^{35} \theta^{15} - \\
& 2.441779100246113' * ^{34} \theta^{16} + 2.1422234658979708' * ^{33} \theta^{17} - \\
& 1.6049917252445308' * ^{32} \theta^{18} + 1.012102378536468' * ^{31} \theta^{19} - \\
& 5.2401443148533675' * ^{29} \theta^{20} + 2.1233801883418154' * ^{28} \theta^{21} - \\
& 5.9677657472719257' * ^{26} \theta^{22} + 6.028703874008091' * ^{24} \theta^{23} + \\
& 4.316628659608773' * ^{23} \theta^{24} - 2.9179524450579636' * ^{22} \theta^{25} + \\
& 9.781465694388629' * ^{20} \theta^{26} - 2.036035192946051' * ^{19} \theta^{27} + \\
& 2.518601478855538' * ^{17} \theta^{28} - 1.4315995537848782' * ^{15} \theta^{29} + \\
& 1232.3437759904039' \theta^{30} - 6.404175164653097' \theta^{31} \Bigg) / \\
& \left( (-12.566370614359172' + \theta)^{16} (-6.283185388010722' + \theta)^7 (-6.283185226348451' + \theta)^7 \right. \\
& \left. \theta^8 \left( \frac{(-6.283185388010722' + \theta) (-6.283185226348451' + \theta) \theta}{12.566370614359172' - 1.' \theta} \right)^{3/2} \right) + \\
& \left( 7 \left( \frac{(-6.283185388010722' + \theta) (-6.283185226348451' + \theta)}{12.566370614359172' - 1.' \theta} + \right. \right. \\
& \left. \frac{(-6.283185388010722' + \theta) \theta}{12.566370614359172' - 1.' \theta} + \frac{(-6.283185226348451' + \theta) \theta}{12.566370614359172' - 1.' \theta} + \right. \\
& \left. \frac{1.' (-6.283185388010722' + \theta) (-6.283185226348451' + \theta) \theta}{(12.566370614359172' - 1.' \theta)^2} \right) \\
& (-1.7239514242502465' * ^{41} \theta + 6.19455209273797' * ^{41} \theta - \\
& 1.0715733419821407' * ^{42} \theta^2 + 1.1883364566689056' * ^{42} \theta^3 - \\
& 9.490987783531211' * ^{41} \theta^4 + 5.814515984234418' * ^{41} \theta^5 - \\
& 2.841610189077518' * ^{41} \theta^6 + 1.1374222079829315' * ^{41} \theta^7 - \\
& 3.7991255503643' * ^{40} \theta^8 + 1.073339972987572' * ^{40} \theta^9 - \\
& 2.5906381973931337' * ^{39} \theta^{10} + 5.3806768122609554' * ^{38} \theta^{11} - \\
& 9.66542766147963' * ^{37} \theta^{12} + 1.5063504106448067' * ^{37} \theta^{13} - \\
& 2.0395706143447065' * ^{36} \theta^{14} + 2.3979597145679737' * ^{35} \theta^{15} - \\
& 2.441779100246113' * ^{34} \theta^{16} + 2.1422234658979708' * ^{33} \theta^{17} - \\
& 1.6049917252445308' * ^{32} \theta^{18} + 1.012102378536468' * ^{31} \theta^{19} - \\
& 5.2401443148533675' * ^{29} \theta^{20} + 2.1233801883418154' * ^{28} \theta^{21} -
\end{aligned}$$

$$\begin{aligned}
& \left( \begin{aligned} & 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{24} + \\ & 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\ & 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\ & 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\ & 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \end{aligned} \right) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^8 \right. \\
& \quad \left. \theta^7 \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} \right)^{3/2} \right) + \\
& \left( 7 \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta)}{12.566370614359172 - 1. \theta} + \right. \right. \\
& \quad \left. \frac{(-6.283185388010722 + \theta) \theta}{12.566370614359172 - 1. \theta} + \frac{(-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} + \right. \\
& \quad \left. \frac{1. \cdot (-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{(12.566370614359172 - 1. \theta)^2} \right) \\
& \left( -1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} - \right. \\
& \quad 1.0715733419821407 \cdot \theta^{42} + 1.1883364566689056 \cdot \theta^{42} - \\
& \quad 9.490987783531211 \cdot \theta^{41} + 5.814515984234418 \cdot \theta^{41} - \\
& \quad 2.841610189077518 \cdot \theta^{41} + 1.1374222079829315 \cdot \theta^{41} - \\
& \quad 3.7991255503643 \cdot \theta^{40} + 1.073339972987572 \cdot \theta^{40} - \\
& \quad 2.5906381973931337 \cdot \theta^{39} + 5.3806768122609554 \cdot \theta^{38} - \\
& \quad 9.66542766147963 \cdot \theta^{37} + 1.5063504106448067 \cdot \theta^{37} - \\
& \quad 2.0395706143447065 \cdot \theta^{36} + 2.3979597145679737 \cdot \theta^{35} - \\
& \quad 2.441779100246113 \cdot \theta^{34} + 2.1422234658979708 \cdot \theta^{33} - \\
& \quad 1.6049917252445308 \cdot \theta^{32} + 1.012102378536468 \cdot \theta^{31} - \\
& \quad 5.2401443148533675 \cdot \theta^{29} + 2.1233801883418154 \cdot \theta^{28} - \\
& \quad 5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{24} + \\
& \quad 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + \\
& \quad 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + \\
& \quad 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + \\
& \quad \left. 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \right) / \\
& \left( (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^8 (-6.283185226348451 + \theta)^7 \right. \\
& \quad \left. \theta^7 \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} \right)^{3/2} \right) + \\
& \left( 16 \left( \frac{(-6.283185388010722 + \theta) (-6.283185226348451 + \theta)}{12.566370614359172 - 1. \theta} + \right. \right. \\
& \quad \left. \frac{(-6.283185388010722 + \theta) \theta}{12.566370614359172 - 1. \theta} + \frac{(-6.283185226348451 + \theta) \theta}{12.566370614359172 - 1. \theta} + \right. \\
& \quad \left. \frac{1. \cdot (-6.283185388010722 + \theta) (-6.283185226348451 + \theta) \theta}{(12.566370614359172 - 1. \theta)^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{1. \cdot (-6.283185388010722 \cdot \theta) (-6.283185226348451 \cdot \theta) \theta}{(12.566370614359172 - 1. \cdot \theta)^2} \Bigg) \\
& \left( -1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \right. \\
& \quad 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \cdot \theta^{41} \theta^4 + 5.814515984234418 \cdot \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \cdot \theta^{41} \theta^6 + 1.1374222079829315 \cdot \theta^{41} \theta^7 - \\
& \quad 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \theta^9 - \\
& \quad 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& \quad 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \\
& \quad 5.9677657472719257 \cdot \theta^{26} \theta^{22} + 6.028703874008091 \cdot \theta^{24} \theta^{23} + \\
& \quad 4.316628659608773 \cdot \theta^{23} \theta^{24} - 2.9179524450579636 \cdot \theta^{22} \theta^{25} + \\
& \quad 9.781465694388629 \cdot \theta^{20} \theta^{26} - 2.036035192946051 \cdot \theta^{19} \theta^{27} + \\
& \quad 2.518601478855538 \cdot \theta^{17} \theta^{28} - 1.4315995537848782 \cdot \theta^{15} \theta^{29} + \\
& \quad \left. 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31} \right) \Bigg/ \\
& \left( (-12.566370614359172 \cdot \theta)^{17} (-6.283185388010722 \cdot \theta)^7 \right. \\
& \quad \left. (-6.283185226348451 \cdot \theta)^7 \theta^7 \right. \\
& \quad \left. \left( \frac{(-6.283185388010722 \cdot \theta) (-6.283185226348451 \cdot \theta) \theta}{12.566370614359172 - 1. \cdot \theta} \right)^{3/2} \right) + \\
& \left( 3 \left( \frac{(-6.283185388010722 \cdot \theta) (-6.283185226348451 \cdot \theta)}{12.566370614359172 - 1. \cdot \theta} + \right. \right. \\
& \quad \frac{(-6.283185388010722 \cdot \theta) \theta}{12.566370614359172 - 1. \cdot \theta} + \frac{(-6.283185226348451 \cdot \theta) \theta}{12.566370614359172 - 1. \cdot \theta} + \\
& \quad \left. \left. \frac{1. \cdot (-6.283185388010722 \cdot \theta) (-6.283185226348451 \cdot \theta) \theta}{(12.566370614359172 - 1. \cdot \theta)^2} \right) \right. \\
& \quad \left. (-1.7239514242502465 \cdot \theta^{41} + 6.19455209273797 \cdot \theta^{41} \theta - \right. \\
& \quad 1.0715733419821407 \cdot \theta^{42} \theta^2 + 1.1883364566689056 \cdot \theta^{42} \theta^3 - \\
& \quad 9.490987783531211 \cdot \theta^{41} \theta^4 + 5.814515984234418 \cdot \theta^{41} \theta^5 - \\
& \quad 2.841610189077518 \cdot \theta^{41} \theta^6 + 1.1374222079829315 \cdot \theta^{41} \theta^7 - \\
& \quad 3.7991255503643 \cdot \theta^{40} \theta^8 + 1.073339972987572 \cdot \theta^{40} \theta^9 - \\
& \quad 2.5906381973931337 \cdot \theta^{39} \theta^{10} + 5.3806768122609554 \cdot \theta^{38} \theta^{11} - \\
& \quad 9.66542766147963 \cdot \theta^{37} \theta^{12} + 1.5063504106448067 \cdot \theta^{37} \theta^{13} - \\
& \quad 2.0395706143447065 \cdot \theta^{36} \theta^{14} + 2.3979597145679737 \cdot \theta^{35} \theta^{15} - \\
& \quad 2.441779100246113 \cdot \theta^{34} \theta^{16} + 2.1422234658979708 \cdot \theta^{33} \theta^{17} - \\
& \quad 1.6049917252445308 \cdot \theta^{32} \theta^{18} + 1.012102378536468 \cdot \theta^{31} \theta^{19} - \\
& \quad \left. 5.2401443148533675 \cdot \theta^{29} \theta^{20} + 2.1233801883418154 \cdot \theta^{28} \theta^{21} - \right.
\end{aligned}$$



$$\left( \frac{5.9677657472719257 \cdot \theta^{22} + 6.028703874008091 \cdot \theta^{24} + 4.316628659608773 \cdot \theta^{24} - 2.9179524450579636 \cdot \theta^{25} + 9.781465694388629 \cdot \theta^{26} - 2.036035192946051 \cdot \theta^{27} + 2.518601478855538 \cdot \theta^{28} - 1.4315995537848782 \cdot \theta^{29} + 1232.3437759904039 \cdot \theta^{30} - 6.404175164653097 \cdot \theta^{31}}{4 (-12.566370614359172 + \theta)^{16} (-6.283185388010722 + \theta)^7 (-6.283185226348451 + \theta)^7 \theta^7} \right)^{5/2}, \{\theta, -13, 13\}]$$



$$\text{Solve}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} n (1 / (6 (\theta))) == c, n\right]$$

$$\left\{\left\{n \rightarrow \frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \text{Sin}[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}\right\}\right\}$$

$$\text{Solve}\left[\theta == \frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \text{Sin}[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}, \theta\right]$$

{}

$$\text{TrigReduce}\left[\frac{\pi \sqrt{4 \pi - \theta} \sqrt{\theta} \text{Sin}[\theta]}{180 \sqrt{(4 \pi - \theta) \theta}}\right]$$

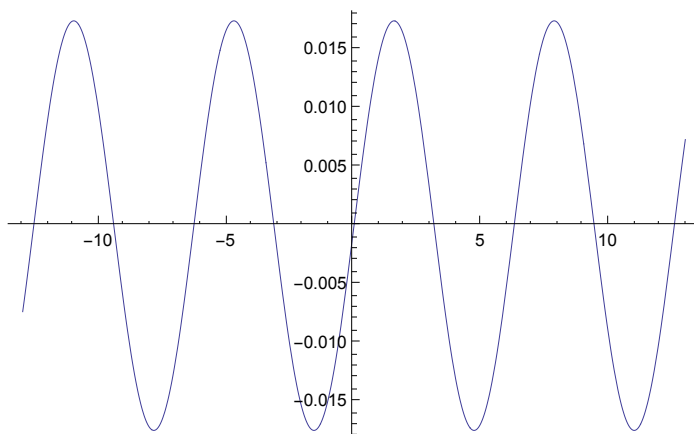
$$\frac{\pi \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\theta]}{180 \sqrt{4 \pi - \theta} \sqrt{\theta}}$$

$$\frac{\pi \sqrt{4 \pi - e} \sqrt{e} \text{Sin}[e]}{180 \sqrt{(4 \pi - e) e}}$$

$$N\left[\frac{1}{180} \pi \sin[e]\right]$$

0.00716949

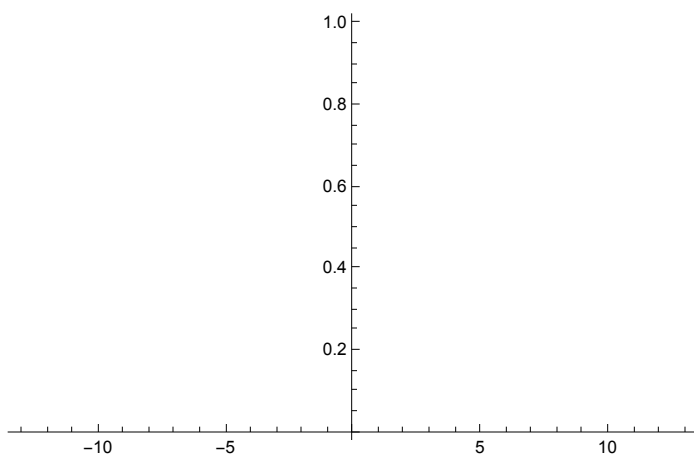
$$\text{Plot}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}, \{\theta, -13, 13\}\right]$$



$$\text{Solve}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}} = 1, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \text{ArcSin}\left[\frac{180}{\pi}\right]\right\}\right\}$$

$$\text{Plot}\left[\text{ArcSin}\left[\frac{180}{\pi}\right] x, \{x, -13, 13\}\right]$$



$$\text{Reduce}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}\right]$$

$$\text{Reduce}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}}\right]$$

$$\text{Solve}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}} == 2, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \text{ArcSin}\left[\frac{360}{\pi}\right]\right\}\right\}$$

$$\text{Solve}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}} == 3, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \text{ArcSin}\left[\frac{540}{\pi}\right]\right\}\right\}$$

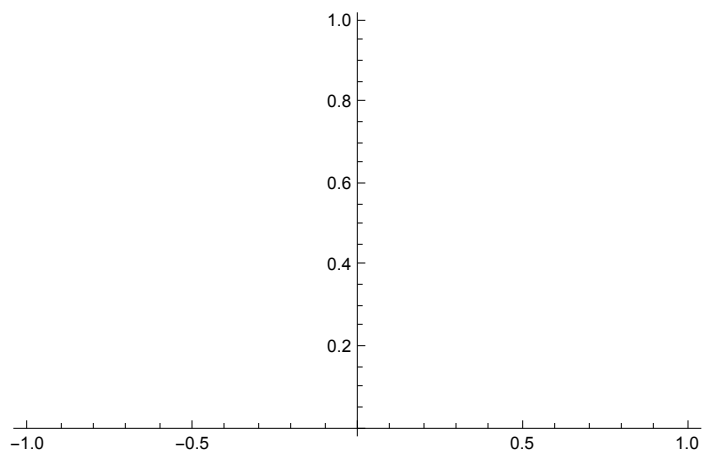
$$\text{Solve}\left[\frac{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sin[\theta]}{180 \sqrt{(4\pi - \theta) \theta}} == e, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \text{ArcSin}\left[\frac{180 e}{\pi}\right]\right\}\right\}$$

$$\text{Solve}\left[\frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta}} n (1 / (6 (\theta))) == c, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \text{ArcCsc}\left[\frac{\pi}{180 n}\right]\right\}\right\}$$

$$\text{Plot}\left[\text{ArcCsc}\left[\frac{\pi}{180 n}\right], \{n, -1, 1\}\right]$$



$$\text{N}\left[\text{ArcCsc}\left[\frac{\pi}{180 \times 2}\right]\right]$$

$$1.5708 - 5.4345 i$$

$$\text{N}\left[\text{ArcCsc}\left[\frac{\pi}{180 \times 1}\right]\right]$$

$$1.5708 - 4.7413 i$$

$$N\left[\text{ArcCsc}\left[\frac{\pi}{180 \times 3}\right]\right]$$

$$1.5708 - 5.83998 i$$

$$\theta$$

# The Geometric Patterns of Perception

by Parker Emmerson

The idea of this paper is to explain how, when a wedge of arc length,  $t$ , is taken out of a circle and the circle is then put back together, keeping the initial radius as the slant of the newly formed cone, the height increases and the initial radius changes angle to the circular base, which has a new radius. The difference between the radii leads to a change in circumference for the circle of our system. That change can be considered a  $D[C] d\theta$ . The change is also then placed in terms of time. So, we have relationary time aspects fusing with axis at an infinite angle.

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle, the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + h^2$$

This is the initial radius squared expressed as the slant of the cone in terms of the height of the cone,  $h$ , and the radius of the base of the cone,  $r_1$

$$r = \sqrt{r_1^2 + h^2}$$

$$t = \theta r$$

$$t / \theta = r$$

$$t = C - C_2 = 2 \pi r - 2 \pi r_1 = \theta r \quad \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - h^2$$

$$r_1 = \sqrt{r^2 - h^2}$$

$$h < r$$

$$\text{Solve}[r_1^2 + h^2 = r^2, h]$$

$$\left\{ \left\{ h \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ h \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\}$$

$$t = C - C_2 = 2 \pi r - 2 \pi r_1$$

Put

$$r_1 = \sqrt{(r^2 - h^2)}$$

in for the equation of the base of the cone of Equation 7.

$$t = C - C_2 =$$

$$2\pi r - 2\pi r_1 = 2\pi (t/\theta) - 2\pi \sqrt{((t/\theta)^2 - h^2)} = t$$

$$(t/\theta) = r$$

$$(2\pi(r) - 2\pi \sqrt{((r)^2 - h^2)}) = t$$

Add  $2\pi \sqrt{((r)^2 - h^2)}$  to both sides

$$t + 2\pi \sqrt{((t/\theta)^2 - (h^2))} = 2\pi (t/\theta) = 2\pi r$$

Subtract t from both sides

$$2\pi \sqrt{((t/\theta)^2 - (h^2))} = 2\pi (t/\theta) - t = 2\pi r - t$$

divide by  $2\pi$  on both sides

$$(t/\theta) - t/2\pi = \sqrt{((t/\theta)^2 - (h^2))} = r_1 = \sqrt{((r)^2 - (h^2))}$$

$$(t/\theta) - t/(2\pi)$$

$$-\frac{t}{2\pi} + \frac{t}{\theta}$$

Square both sides

$$((t/\theta) - (t/2\pi))^2 = ((t/\theta)^2 - (h^2)) = (r_1^2)$$

add  $(h^2)$  to both sides

$$(h^2) + ((t/\theta) - (t/2\pi))((t/\theta) - (t/2\pi)) = (t/\theta)^2 = r^2$$

$$((t/\theta) - (t/2\pi))^2$$

$$((r) - (\theta * r / 2\pi))^2$$

$$\left(r - \frac{\pi r \theta}{2}\right)^2$$

$$\left(-\frac{(\pi * r * \theta)}{2} + \frac{(r * \theta)}{\theta}\right)^2$$

$$\left(r - \frac{\pi r \theta}{2}\right)^2$$

$$\text{Expand} \left[ \left( r - \frac{\pi * r * \theta}{2} \right)^2 \right]$$

$$r^2 - \pi r^2 \theta + \frac{1}{4} \pi^2 r^2 \theta^2$$

Subtract  $\left(-\frac{\pi r\theta}{2} + r\right)^2$  from both sides

$$(t/\theta)^2 - \{(t/\theta) - t/2\pi\} \{(t/\theta) - t/2\pi\} = (h^2)$$

$$(r^2/\theta^2) - \{(r) - (\theta * r)/2\pi\} \{((\theta * r)/\theta) - (\theta * r)/2\pi\}$$

Take the square root on both sides to find h

$$h = \text{Sqrt}[(t/\theta)^2 - \{(t/\theta) - t/2\pi\} \{(t/\theta) - t/2\pi\}] = \sqrt{(r)^2 - \{(r) - (\theta * r)/2\pi\} \{(r) - (\theta * r)/2\pi\}}$$

$$(r)^2 - \{(r) - (\theta * r)/2\pi\} \{(r) - (\theta * r)/2\pi\}$$

$$\left\{r^2 - \left(r - \frac{\pi r\theta}{2}\right)^2\right\}$$

$$\text{Simplify}\left[\sqrt{-\left(-\frac{\pi r * \theta}{2} + \frac{r * \theta}{\theta}\right)^2 + \frac{r^2 * \theta^2}{\theta^2}}\right]$$

$$\sqrt{r^2 - \left(r - \frac{\pi r\theta}{2}\right)^2}$$

$$\text{Simplify}\left[\sqrt{-\left(-\frac{\pi (r * \theta)}{2} + \frac{(r * \theta)}{\theta}\right)^2 + r^2}\right]$$

$$\sqrt{r^2 - \left(r - \frac{\pi r\theta}{2}\right)^2}$$

$$\text{Simplify}\left[\sqrt{-\left(-\frac{\pi (r\theta)}{2} + \frac{(r\theta)}{\theta}\right)^2 + r}\right]$$

$$\sqrt{r^2 - \left(-\frac{\pi r\theta}{2} + \frac{r\theta}{\theta}\right)^2}$$

$$\text{Sqrt}[(t/\theta)^2 - \{(t/\theta) - t/2\pi\} \{(t/\theta) - t/2\pi\}] = \text{Sqrt}[((\theta r)/\theta)^2 - \{(r) - (\theta r)/2\pi\} \{(r) - (\theta r)/2\pi\}]$$

$$((\theta r)/\theta)^2 = \theta^2 r^2 / \theta^2$$

$$r^2$$

$$\text{Sqrt}[((\theta r)/\theta)^2 - \{(r) - (\theta r)/2\pi\} \{(r) - (\theta r)/2\pi\}]$$

$$\sqrt{-\left(-\frac{\pi r\theta}{2} + \frac{r\theta}{\theta}\right)^2 + \frac{r\theta^2}{\theta^2}} = \left\{\sqrt{\frac{\theta r^2}{\theta^2} - \left(r - \frac{\pi \theta r}{2}\right)^2}\right\} = h$$

$$\text{Expand}\left[\left(r - \frac{\pi \theta * r}{2}\right)^2\right]$$

$$r^2 - \pi r^2 \theta + \frac{1}{4} \pi^2 r^2 \theta^2$$

$$\text{Solve}\left[\left\{\sqrt{\frac{\theta r^2}{\theta^2} - \left(r - \frac{\pi \theta r}{2}\right)^2}\right\} == h, \{\theta\}\right]$$

$$h^2 = \frac{\theta r^2}{\theta^2} - \left(r - \frac{\pi \theta r}{2}\right)^2$$

$$r^2 - \pi r \theta r + \frac{\pi^2 (\theta r)^2}{4} = r^2 - \pi r^2 \theta + \frac{1}{4} \pi^2 r^2 \theta^2$$

$$\sqrt{r^2 - \left(r^2 - \pi r^2 \theta + \frac{1}{4} \pi^2 r^2 \theta^2\right)}$$

$$\sqrt{\pi r^2 \theta - \frac{1}{4} \pi^2 r^2 \theta^2}$$

$$\sqrt{\pi r^2 \theta - \frac{1}{4} \pi^2 r^2 \theta^2} = h$$

Square both sides

$$\pi r^2 \theta - \frac{1}{4} \pi^2 r^2 \theta^2 = (h^2)$$

Divide by  $r^2$  on both sides

$$\left(\pi r^2 \theta - \frac{1}{4} \pi^2 r^2 \theta^2\right) / (r^2) = (h^2) / r^2$$

$$\left(\pi \theta - \frac{1}{4} \pi^2 \theta^2\right) = (h^2) / r^2$$

$$(h^2) / \left(\pi \theta - \frac{1}{4} \pi^2 \theta^2\right) = r^2$$

$$h = c3\theta$$

$$\left((3.0 * 10^8) * 3 * \theta\right)^2 / \left(\pi \theta - \frac{1}{4} \pi^2 \theta^2\right) = r^2$$

$$r^2$$

$$(h^2) / r^2 = x$$

Multiply by  $r^2$ ; Divide by  $\left(1 - (\pi * \theta) + \frac{1}{4} (\pi^2 * \theta^2)\right)$  on both sides

EQUATION # X .1

$$(h^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = r^2$$

set  $r^2 = (1 + 3 + 5 \dots (2n - 1))$

$$(1 + 3 + 5 \dots (2n - 1)) = (h^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)$$

For  $n = 1$

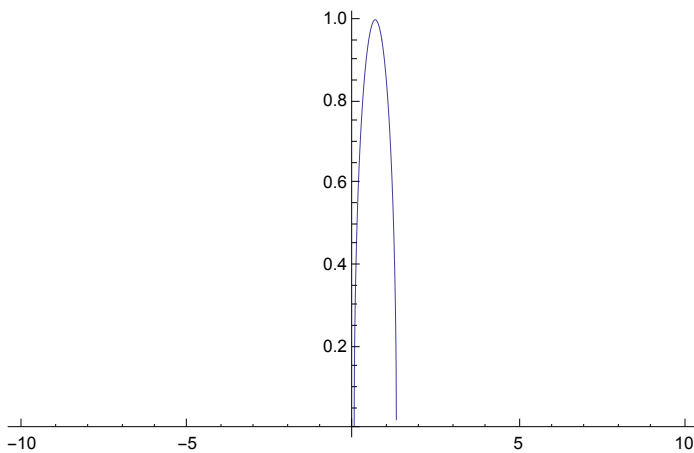
$$1 = \left( (h^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right),$$

so

$$\left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = (h^2)$$

$$\sqrt{\left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} = h$$

$$\text{Plot} \left[ \sqrt{\left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \{\theta, -10, 10\} \right]$$



$$\text{Solve} \left[ \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) == 0, \{\theta\} \right]$$

$$\left\{ \{\theta \rightarrow 0\}, \left\{ \theta \rightarrow \frac{4}{\pi} \right\} \right\}$$

For  $n = 2$ ;

$$(1 + (2n - 1)) = 4 = \left( (h^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right)$$

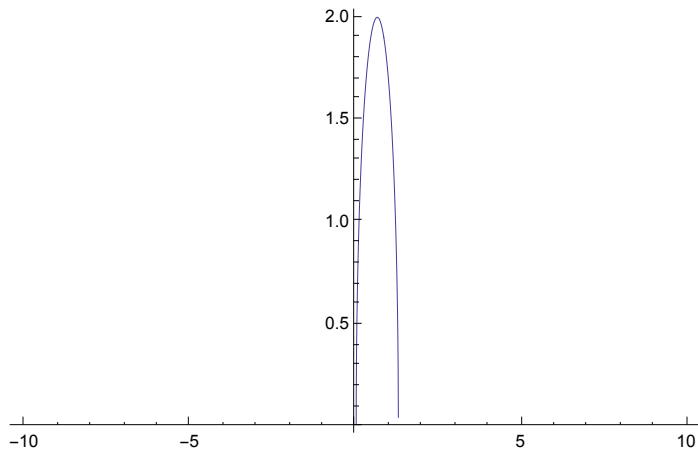


So, multiplying on both sides,

$$4 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = (h^2)$$

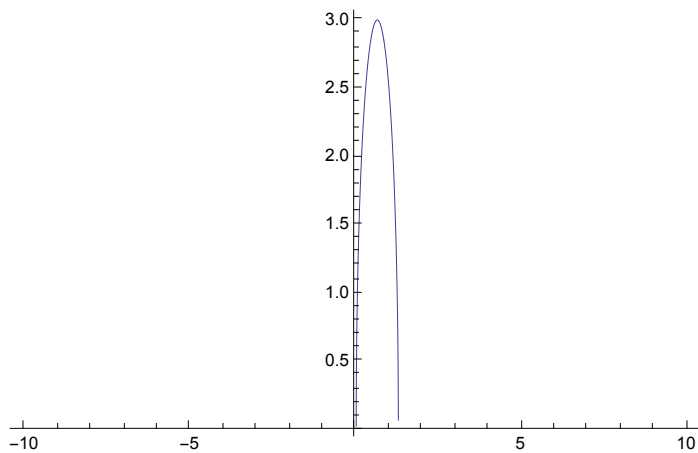
$$\sqrt{4 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} = h$$

$$\text{Plot} \left[ \sqrt{4 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \{\theta, -10, 10\} \right]$$



For n = 3

$$\text{Plot} \left[ \sqrt{9 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \{\theta, -10, 10\} \right]$$



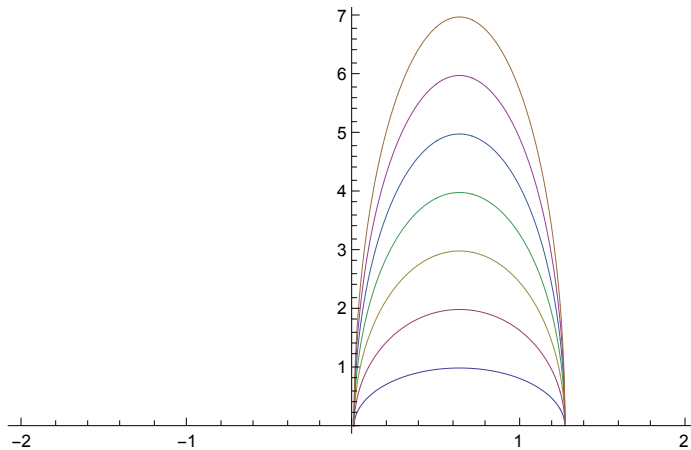
$$\text{For } n = 4; \quad \sqrt{16 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} = h$$

$$\text{For } n = 5; \sqrt{25 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} = h$$

$$\text{For } n = 6; \sqrt{36 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} = h$$

$$\text{For } n = 7; \sqrt{49 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} = h$$

$$\text{Plot} \left[ \left\{ \sqrt{\left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \sqrt{4 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \right. \right. \\ \left. \sqrt{9 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \sqrt{16 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \right. \\ \left. \sqrt{25 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \sqrt{36 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}, \sqrt{49 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)} \right\}, \\ \{\theta, -2, 2\}]$$



We have plotted what will happen to the height as theta changes. Next we want to know  $r_1$  and its change with theta if  $r$  is the series  $r^2 = (1 + 3 + \dots (2n - 1))$

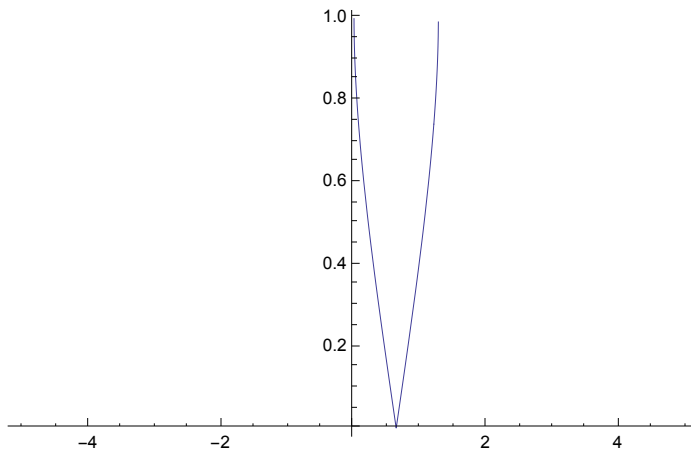
Some have noted the phalax and some have noted that the mind is sometimes thought of as the head.

$$\text{Remember, } r_1 = \sqrt{((t/\theta)^2 - (h^2))} = r_1 = \sqrt{(r^2 - h^2)}$$

For n = 1;

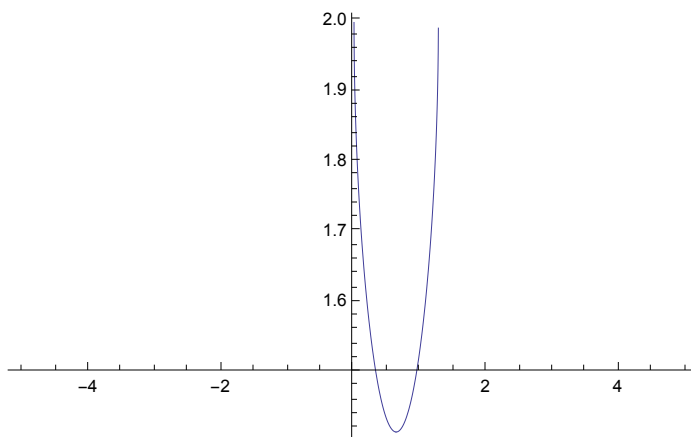
$$r_1 = \sqrt{(r^2 - h^2)} = \sqrt{\left(1 - \sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}\right)}$$

$$\text{Plot}\left[\sqrt{\left(1 - \sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}\right)}, \{\theta, -5, 5\}\right]$$

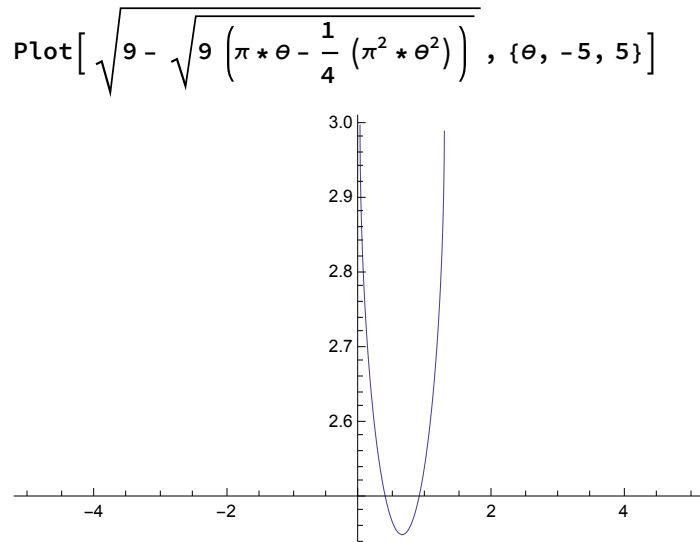


For n = 2

$$\text{Plot}\left[\sqrt{4 - \sqrt{4 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \{\theta, -5, 5\}\right]$$



For n = 3;



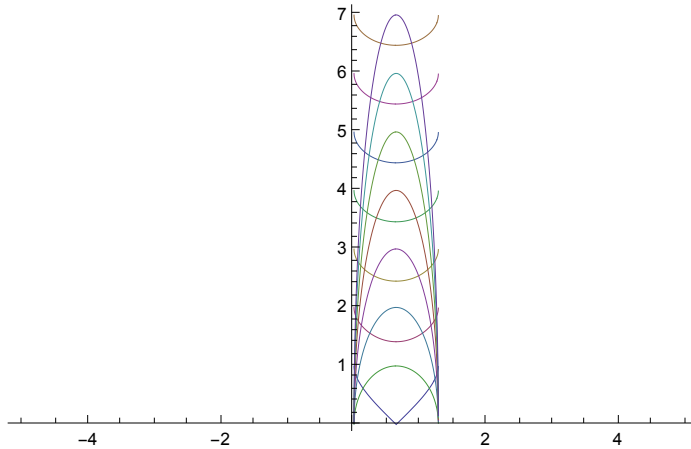
$$n = 4; r_1 = \sqrt{16 - \sqrt{16 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}$$

$$n = 5; r_1 = \sqrt{25 - \sqrt{25 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}$$

$$n = 6; r_1 = \sqrt{36 - \sqrt{36 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}$$

$$n = 7; r_1 = \sqrt{49 - \sqrt{49 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}$$

$$\text{Plot}\left[\left\{\sqrt{1 - \sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{4 - \sqrt{4 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \right.\right. \\
\left.\sqrt{9 - \sqrt{9 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{16 - \sqrt{16 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \right. \\
\left.\sqrt{25 - \sqrt{25 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{36 - \sqrt{36 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \right. \\
\left.\sqrt{49 - \sqrt{49 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \right. \\
\left.\sqrt{4 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \sqrt{9 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \sqrt{16 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \right. \\
\left.\sqrt{25 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \sqrt{36 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \sqrt{49 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}\right\}, \\
\{\theta, -5, 5\}]$$



Though please note the pointed place at  
which the bottom most chalace intersects the x axis.

$$\text{Plot}\left[\left\{\sqrt{1 - \sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{4 - \sqrt{4 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \right.\right. \\ \left.\sqrt{9 - \sqrt{9 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{16 - \sqrt{16 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \right. \\ \left.\sqrt{25 - \sqrt{25 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \sqrt{36 - \sqrt{36 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}, \right. \\ \left.\sqrt{49 - \sqrt{49 \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}}\right\}, \{\theta, -10, 10\}]$$

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle,  
the base of the cone, of radius  $r_1$

**So, we integrate the circumference, to get a certain area,  
due to a representationality in the virtual world.**

In our last discovery, we found out that the height of the cone is a function of the angle and the radius. Here, we will try to eliminate one of the variables, and we can do this, because it is the same variable as time when given a constant velocity, say of light going toward your eye. We will try to see about the concept of negative time and philosophically discuss its objective meaning. We begin by consulting Figure x.

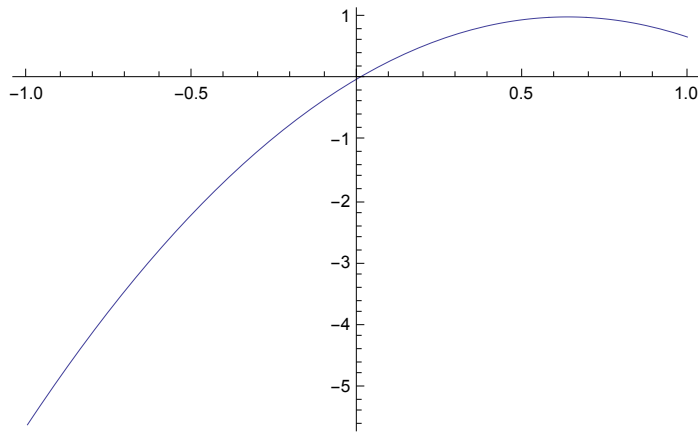
from equations of a cone, we know that

$$(h^2) / \left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right) = r^2$$

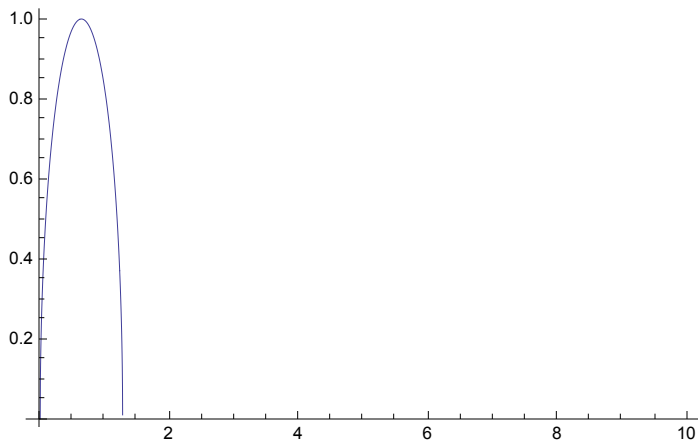
Thus, we can also say that for  $r^2=1$ , because  $n=1$ ; that,

$$\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right) = (h^2) / r^2 = x^2$$

$\text{Plot}\left[\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right), \{\theta, -1, 1\}\right]$



$\text{Plot}\left[\sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}, \{\theta, 0, 10\}\right]$



Suppose that the height of the cone is transforming at the speed of light, moving up to its highest length. We see that it then comes back down, through the passage of time or angle. We can then plot purely the radius and angle measure, without the height as an inexpressible entity in terms of the other variables we are relating, because of the constant speed of light acting to describe the height in terms of travel through space - time. That which can be measured by the folding of the circle into a cone relates to the amount of the circle you take out from the time then to the time now. We then get the below equation

To come up with this equation, we say that  $h = c * t = c * f(\theta)$

so, we also then say that, from

EQUATION # X .1

$$(h^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = r^2$$

$$\left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = (h^2) / r^2 = X^2;$$

$$r^2 \left( \pi * f[\theta] - \frac{1}{4} (\pi^2 * f[\theta]^2) \right) = (h^2) = c^2 * t^2$$

30 sec =  $\pi$ "time"

so, for our time equality to work with the angle change, we are going to have to relate 360 degrees = 60 seconds =  $2\pi$  rad. That means to go from seconds to angles, we multiply a theta given in radians by  $180/\pi$  in order to go to degrees, and then convert to those degrees to seconds by multiplying by (1/6 deg.), because 60 seconds=360 degrees.

So, this means that we can say that time is equal to the amount of the circle's angularity/arc length that we remove from the initial circle has a unit of time.

from time----->angle measure, we multiply by

From the equation

$$ct = c * (f[\theta])$$

S.T.

$\theta$  is in degrees, and to go to time, we would convert

$\theta \text{deg.} (\pi \text{ rad.} / 180 \text{ deg.})$ , and from radians,

we say that thirty seconds go by every  $\pi$  radians., so to cancel the radians,

we say every 30 seconds, we cover  $\pi$  radians of distance. Thus,

the final conversion fom degrees to minutes runs :

$$\theta \text{deg.} * (\pi \text{ rad.} / 180 \text{ deg.}) (60 \text{ sec} / \pi \text{ rad.}) = t$$

Our multiplier then is just 1 sec. / 3 deg. to go to seconds.

and we recently found that :

$$[(h^2) / (\pi r^2)] = (\theta - 1 / 4 \pi (\theta^2))$$

Thus, also we may say that it takes 3 deg. / sec. if we are given a time



$$c^2 * t^2 = r^2 \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = c^2 * (1/3) \theta^2$$

$$c^2 * \left( (3\theta)^2 / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right) = r^2$$

$$r = \sqrt{c^2 * \left( (3\theta)^2 / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right)}$$

60 / 180

$$\frac{1}{3}$$

EQUATION # X .1

$$(h^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) = r^2$$

So, if we are given an angle, the generalized forms would look like this :

$$(c^2 * ((1/3) \theta)^2 / (\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2))) = r^2$$

What happens when we factor the equation

$$\sqrt{(3.0 * 10^8)^2 * ((t)^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right)}$$

$$\text{Factor} \left[ \sqrt{\left( (3.0 * 10^8)^2 * ((1/3) \theta)^2 / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right)} \right]$$

$$1.12838 \times 10^8 \sqrt{-\frac{\theta}{-4 + \pi \theta}}$$

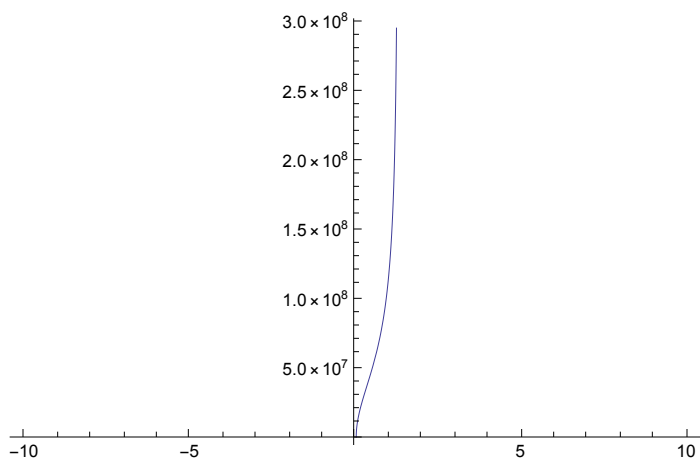
$$\sqrt{\left( (3.0 \times 10^8)^2 * ((t)^2) / \left( \pi * (\theta / 3) - \frac{1}{4} (\pi^2 * (\theta / 3)^2) \right) \right)}$$

$$3. \times 10^8 \sqrt{\frac{t^2}{\frac{\pi \theta}{3} - \frac{\pi^2 \theta^2}{36}}}$$

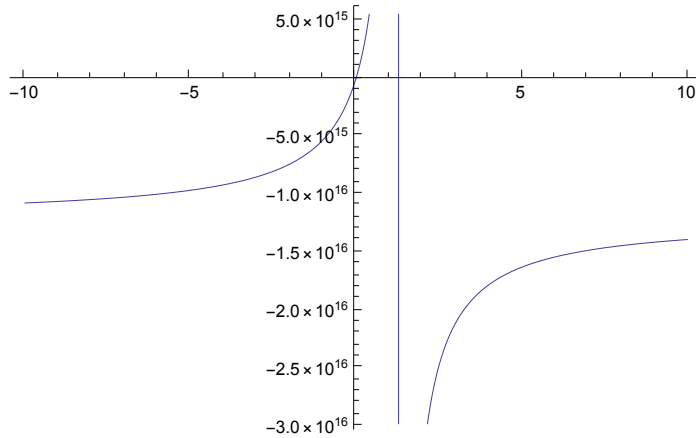
An imaginary solution.

Then we'll plot our time in terms of theta when solved for r.

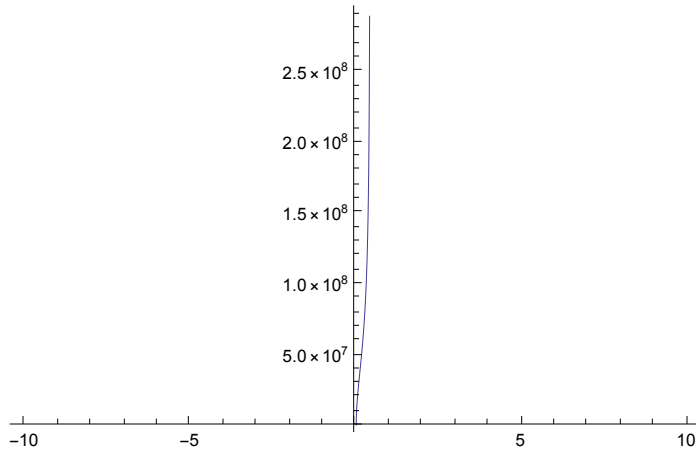
$$\text{Plot}\left[\sqrt{\left( (3.0 \times 10^8)^2 * (((1/3) \theta)^2) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right)}, \{\theta, -10, 10\}\right]$$



Plot[ $\left( (3.0 \times 10^8)^2 * ((t)^2) / \left( \pi * 3 t - \frac{1}{4} (\pi^2 * 3 t^2) \right) \right)$ , {t, -10, 10}]



Plot[ $\sqrt{\left( (3.0 \times 10^8)^2 * ((t)^2) / \left( \pi * 3 t - \frac{1}{4} (\pi^2 * (3 t)^2) \right) \right)}$ , {t, -10, 10}]



where  $c$  is the speed of light and  $3 * t$  = the angle we have taken out of the circle,  
when keeping the initial radius of the circle as the slant of the new cone,  
and our new radius of the base of the cone is determined

$$(c^2) = \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) r^2 / ((1/3) \theta)^2$$

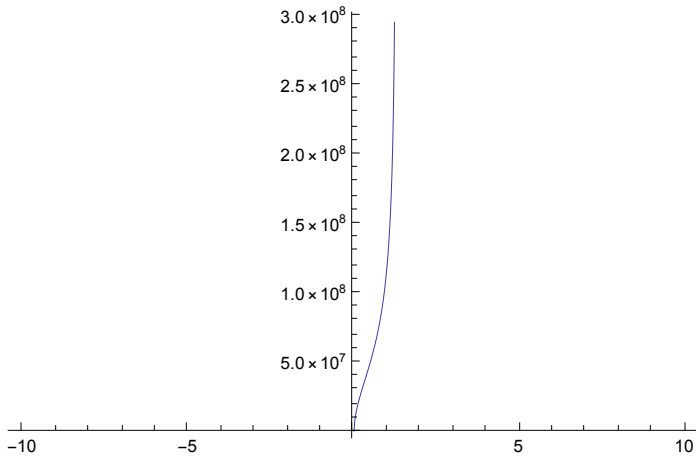
$$(c^2) / r^2 = \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) / ((1/3) \theta)^2$$

$$\text{Solve} \left[ \left( (3.0 * 10^8)^2 * \left( (3 \theta)^2 / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right) \right) == r, \theta \right]$$

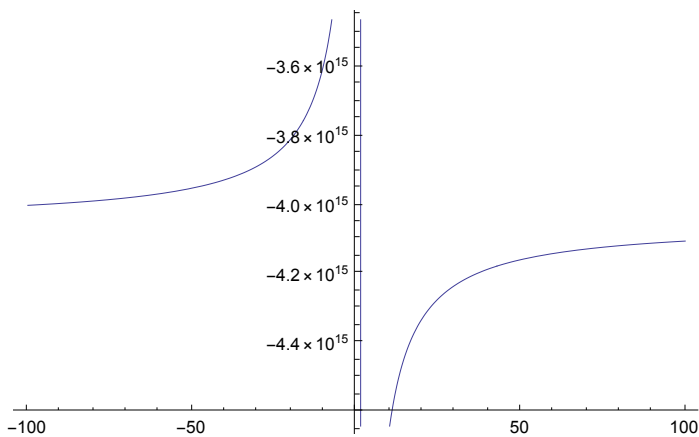
$$\left\{ \left\{ \theta \rightarrow \frac{12.5664 r}{3.24 \times 10^{18} + 9.8696 r} \right\} \right\}$$

$$\left\{ \left\{ \theta \rightarrow \left( \frac{12.566370614359172` r}{3.24` * 10^{18} + 9.869604401089358` r} \right) \right\} \right\}$$

$$\text{Plot} \left[ \sqrt{((3.0 * 10^8)^2) / \left( \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) / ((1/3) \theta)^2 \right)}, \{\theta, -10, 10\} \right]$$



$$\text{Plot} \left[ ((3.0 * 10^8)^2) / \left( \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) / ((1/3) \theta)^2 \right), \{\theta, -100, 100\} \right]$$



But to now place  $\theta$  in terms of  $r$ , we see a new plot

$$3 \left( \frac{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}} \right) = t$$

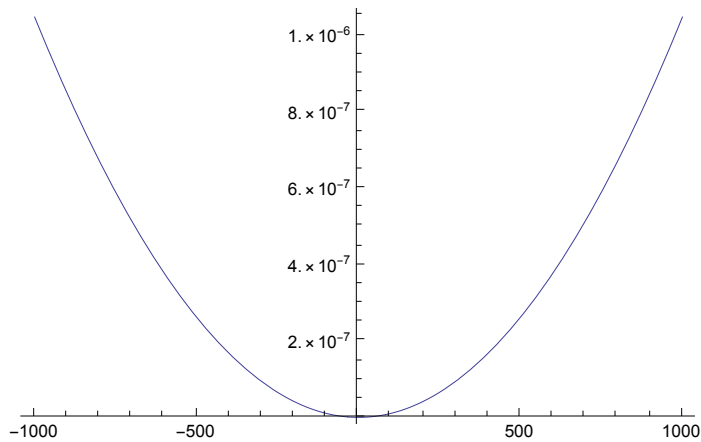
$$\text{Factor} \left[ 3 \left( \frac{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}} \right) \right]$$

$$\frac{37.6991 r^2}{3.6 \times 10^{13} + 3.14159 r^2}$$

$$\text{Simplify} \left[ 3 \left( \frac{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}} \right) \right]$$

$$\frac{9.42478 r^2}{9 \cdot 10^{12} + 0.785398 r^2}$$

$$\text{Plot} \left[ 3 \left( \frac{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}} \right), \{r, -1000, 1000\} \right]$$



$$\frac{\pi}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}} = \theta = dt = \text{change in time}$$

$$\theta \left( \frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2} \right) = \pi$$

$$\theta \frac{9 \cdot 10^{12}}{r^2} = \pi - \theta \frac{\pi}{4}$$

$$r^2 = \theta (9 \cdot 10^{12}) / \pi - \theta \frac{\pi}{4}$$

$$\sqrt{\theta (9 \cdot 10^{12}) / \pi - \theta \frac{\pi}{4}} = r$$

For  $n = 1$ ;

$$\theta * (9. \cdot^{*12}) / \left( \pi - \theta * \frac{\pi}{4} \right) = r = 1;$$

$$\text{Thus, } \left( \pi - \theta * \frac{\pi}{4} \right) = \theta * (9. \cdot^{*12});$$

and,

$$\pi / \left( (9. \cdot^{*12}) + \frac{\pi}{4} \right) = \theta = \theta. \text{ a } k\pi = \theta \left( \frac{\pi}{4} + \frac{9. \cdot^{*12}}{r^2} \right);$$

$$\pi = \theta * \frac{\pi}{4} + \theta * \frac{9. \cdot^{*12}}{r^2};$$

$$\pi - \theta * \frac{\pi}{4} = \theta * \frac{9. \cdot^{*12}}{r^2};$$

$$r^2 \left( \pi - \theta * \frac{\pi}{4} \right) = \theta * (9. \cdot^{*12});$$

$$\theta * (9. \cdot^{*12}) / \left( \pi - \theta * \frac{\pi}{4} \right) = r^2;$$

$$\sqrt{\left\{ \theta * (9. \cdot^{*12}) / \left( \pi - \theta * \frac{\pi}{4} \right) \right\}} = r \setminus$$

$$\text{Solve} \left[ \left( c^2 * ((1/3) \theta)^2 \right) / \left( \pi * \theta - \frac{1}{4} (\pi^2 * \theta^2) \right) \right] == r^2, \theta]$$

$$\left\{ \left\{ \theta \rightarrow \frac{36 \pi r^2}{4 c^2 + 9 \pi^2 r^2} \right\} \right\}$$

$$N \left[ \pi / \left( (9. \cdot^{*12}) + \frac{\pi}{4} \right) \right]$$

$$3.49066 \times 10^{-13}$$

$$\text{Solve} \left[ \sqrt{\left\{ \theta * (9. \cdot^{*12}) / \left( \pi - \theta * \frac{\pi}{4} \right) \right\}} == r, \theta \right]$$

$$\text{Solve::eqf: } \left\{ 3. \times 10^6 \sqrt{\frac{\theta}{\pi + \text{Times}[\ll 3 \gg]}} \right\} = r \text{ is not a well-formed equation. } \gg$$

$$\text{Solve::eqf: } \left\{ 3. \times 10^6 \sqrt{\frac{\theta}{\pi + \text{Times}[\ll 3 \gg]}} \right\} = r \text{ is not a well-formed equation. } \gg$$

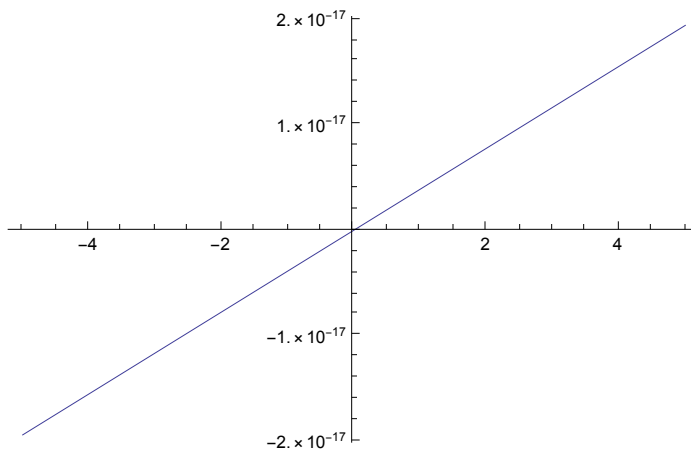
$$\text{Solve}\left[\left\{3.\cdot 10^6 \sqrt{\frac{\theta}{\pi - \frac{\pi \theta}{4}}}\right\} == r, \theta\right]$$

$$\text{Solve::eqf: } \left\{3.\times 10^6 \sqrt{\frac{\theta}{\pi + \text{Times}[\llbracket 3 \rrbracket]}}\right\} == r \text{ is not a well-formed equation. } \gg$$

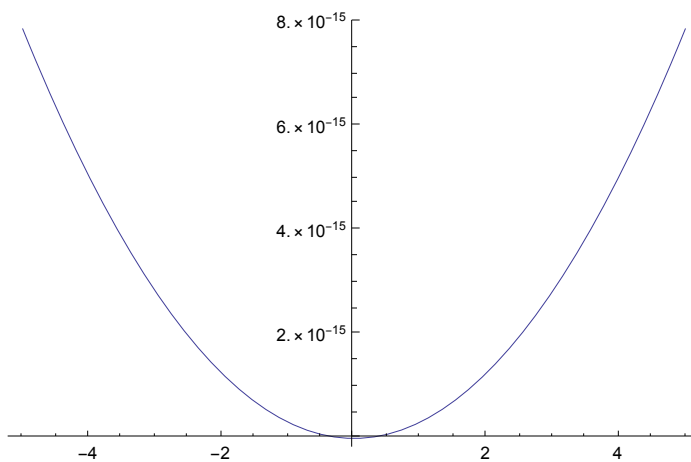
$$\text{Solve::eqf: } \left\{3.\times 10^6 \sqrt{\frac{\theta}{\pi + \text{Times}[\llbracket 3 \rrbracket]}}\right\} == r \text{ is not a well-formed equation. } \gg$$

$$\text{Solve}\left[\left\{3.\times 10^6 \sqrt{\frac{\theta}{\pi - \frac{\pi \theta}{4}}}\right\} == r, \theta\right]$$

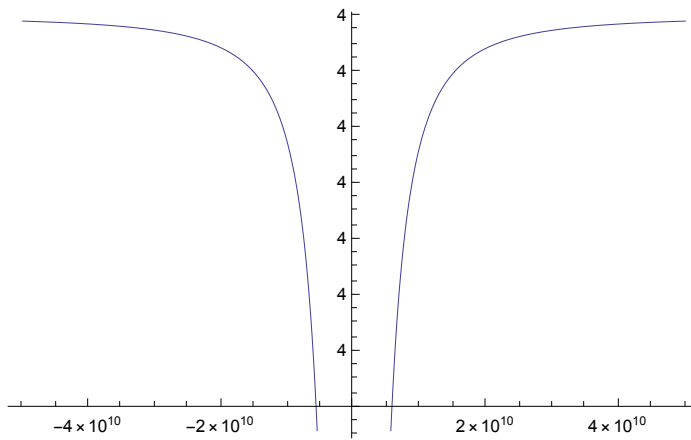
$$\text{Plot}\left[\frac{12.566370614359172 \cdot r}{3.24 \cdot 10^{18} + 9.869604401089358 \cdot r}, \{r, -5, 5\}\right]$$



$$\text{Plot}\left[\frac{36 \pi r^2}{4 (3.0 \cdot 10^8)^2 + 9 \pi^2 r^2}, \{r, -5, 5\}\right]$$

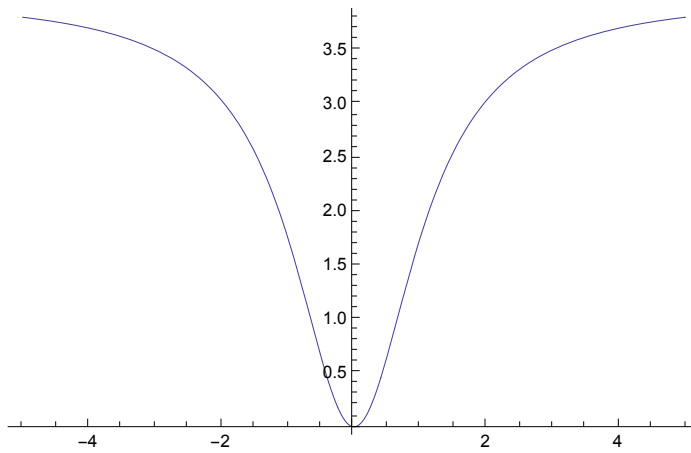


Plot $\left[\frac{\pi}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}}, \{r, -50\,000\,000\,000, 50\,000\,000\,000\}\right]$

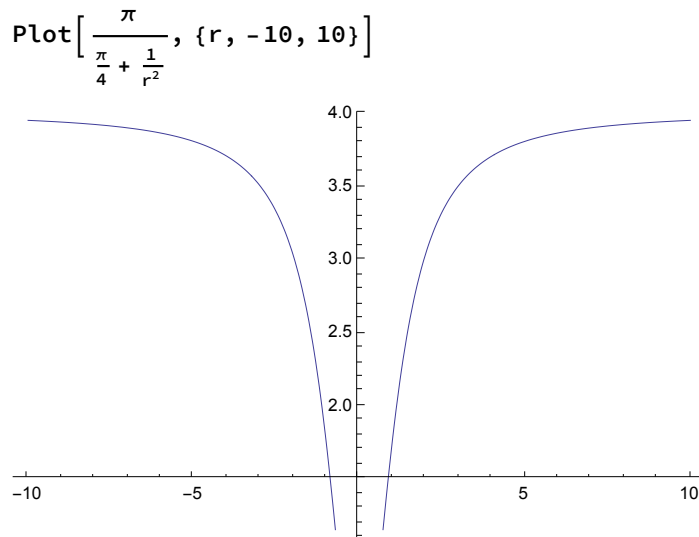


This plot maps what forever looks like.

Plot $\left[\frac{\pi}{\frac{\pi}{4} + \frac{1}{r^2}}, \{r, -5, 5\}\right]$





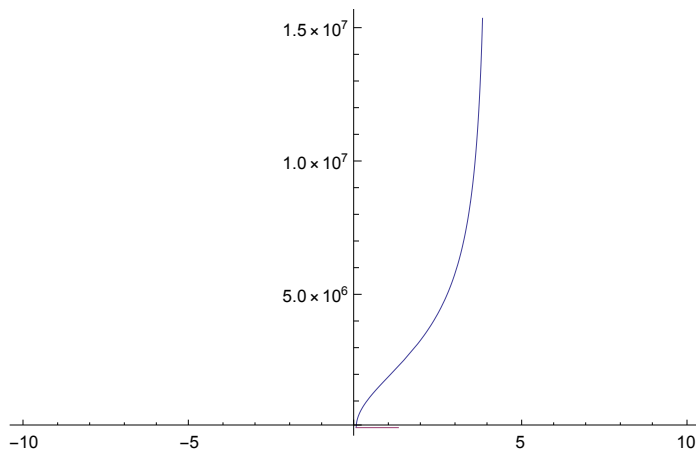


This is one forever within the four forevers. Does it really matter what part of forever time I take out of the circle to make my circle? no, not really, all time is all circle at the same time. We start from where the measurement begins.

This is a plot for fun, and interest.

Plot $\left[\left\{\sqrt{\frac{\theta * (9. \cdot 10^{12})}{\left(\pi - \theta * \frac{\pi}{4}\right)}}, \sqrt{\left(1 - \sqrt{\left(\pi * \theta - \frac{1}{4} (\pi^2 * \theta^2)\right)}\right)}\right\}, \{\theta, -10, 10\}\right]$

Goes all the way probably up to  $2\pi$ , but that is just my guess.



Thus, we show that we must combine the plot for  $r$  when  $n = 1$  and the plot for  $r$  when the speed of light is plugged into the distance for  $r = h$ . Only when we do this, do we even see anything close to  $2\pi$ .

However, if we want to make sure that our units are correct, we will create a new change of variables by converting units.

$$\frac{\pi}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{r^2}} = \theta = dt = \text{change in time}$$

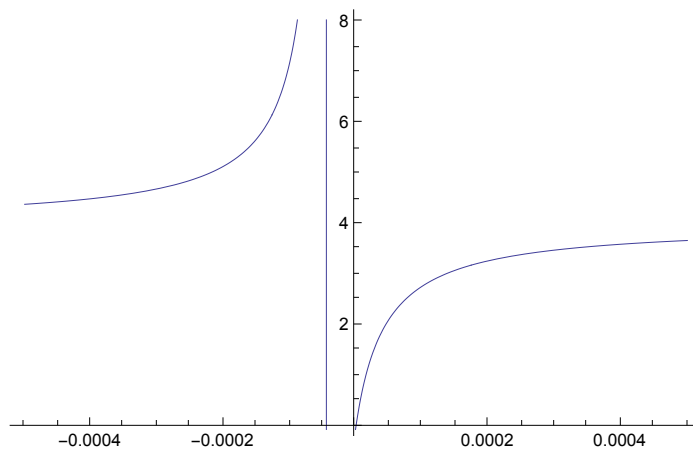
Converting theta into a change in time requires some thought, and also the multiplier  $(\pi / 3)$ .

Speculation: Dark matter is present due to the incorrect integrations of the circle when compared with the luminosity of a change in height of the cone or the distance of an event to the subject.

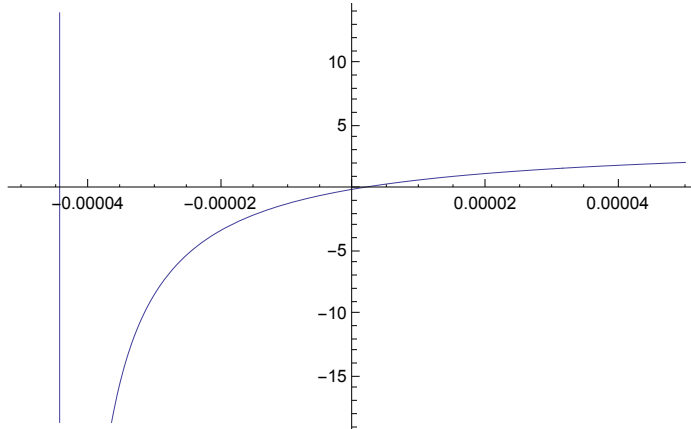
## CONCLUSION

$$\text{Plot} \left[ \frac{\pi}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{\left( \sqrt{\left( (3 \cdot 10^8) + 3 \cdot \theta \right)^2 + \left( \pi \cdot \theta - \frac{1}{4} \pi^2 \theta^2 \right)^2} \right)^2}}, \{\theta, -. = , .0005\} \right]$$

$$\text{Plot} \left[ \frac{\pi}{\frac{\pi}{4} + \frac{9 \cdot 10^{12}}{\left( \sqrt{\left( (3 \cdot 10^8) + 3 \cdot \theta \right)^2 + \left( \pi \cdot \theta - \frac{1}{4} \pi^2 \theta^2 \right)^2} \right)^2}}, \{\theta, -.0005, .0005\} \right]$$



$$\text{Plot}\left[\frac{\pi}{\frac{\pi}{4} + \frac{9. \cdot 10^{12}}{\left(\sqrt{\left(\left(3.0 \cdot 10^8\right) \cdot 3 \cdot \theta\right)^2} / \left(\pi \cdot \theta - \frac{1}{4} \pi^2 \theta^2\right)\right)^2}}, \{\theta, -.00005, .00005\}\right]$$



$$\text{Plot}\left[\frac{\pi}{\frac{\pi}{4} + \frac{9. \cdot 10^{12}}{\sqrt{\frac{\left(\left(3.0 \cdot 10^8\right) \cdot 3 \cdot \theta\right)^2}{\pi \cdot \theta - \frac{\pi^2 \theta^2}{4}}}}}, \{\theta, -500, 500\}\right]$$

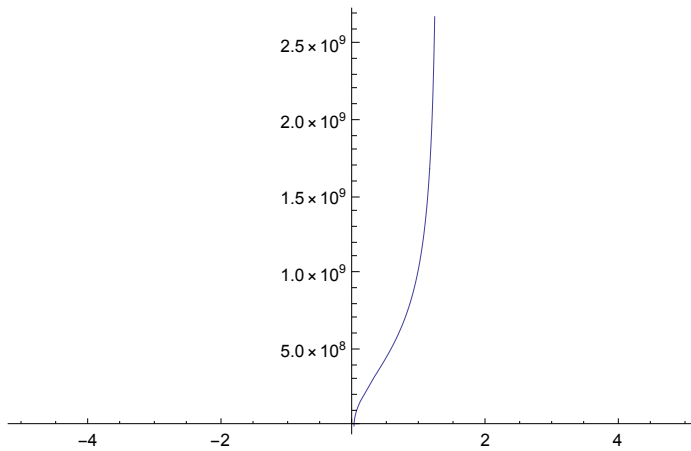
$$\sqrt{\left(\left(3.0 \cdot 10^8\right) \cdot 3 \cdot \theta\right)^2} / \left(\pi \cdot \theta - \frac{1}{4} \pi^2 \theta^2\right) = r$$

$$\text{Solve}\left[\frac{\pi}{\frac{\pi}{4} + \frac{9. \cdot 10^{12}}{\sqrt{\frac{\left(\left(3.0 \cdot 10^8\right) \cdot 3 \cdot \theta\right)^2}{\pi \cdot \theta - \frac{\pi^2 \theta^2}{4}}}}} = \theta, \theta\right]$$

$$\{\{\theta \rightarrow 0.\}, \{\theta \rightarrow 4.0001\}\}$$

$$\sqrt{\left(\left(3.0 \cdot 10^8\right) \cdot 3 \cdot \theta\right)^2} / \left(\pi \cdot \theta - \frac{1}{4} \left(\pi^2 \cdot \theta^2\right)\right) := r$$

Plot $\left[\sqrt{\frac{((3.0 \times 10^8) 3 \theta)^2}{\left(\pi \theta - \frac{1}{4} (\pi^2 \theta^2)\right)}}, \{\theta, -5, 5\}\right]$



Drawing Hypocycloids with these equations, we find that :

These are the Specific plots,

which I invented by folding of a cone into circle, which is Divine Proportion.

```

Clear[x, y, t, a, b, tmini, tmaxi]


$$a = \frac{3(1 + \pi^2)}{2\pi \sqrt{-2\pi + t + \pi^2 t}};$$

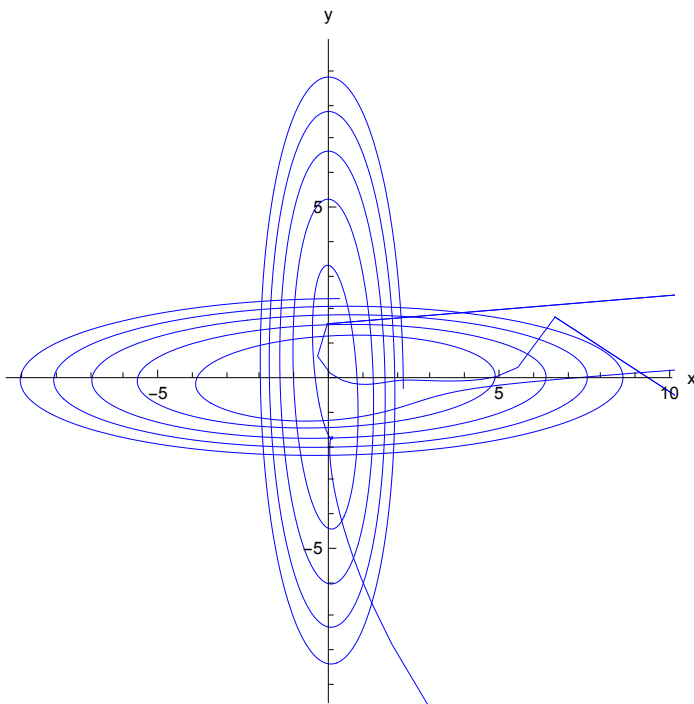


$$b = \sqrt{9 \left( 1 - t - \frac{t}{\pi^2} + \frac{2}{\pi} \right)};$$


tmini = -10 * Pi;
tmaxi = 10 * Pi;
{x[t_], y[t_]} =
  {(a - b) * Cos[t] + b * Cos[(a - b) / b * t], (a - b) * Sin[t] - b * Sin[(a - b) / b * t]};

hypocycloid =
  ParametricPlot[{x[t], y[t]}, {t, tmini, tmaxi},
    PlotStyle -> {{Blue, Thickness[0.0015]}},
    AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]

```



```

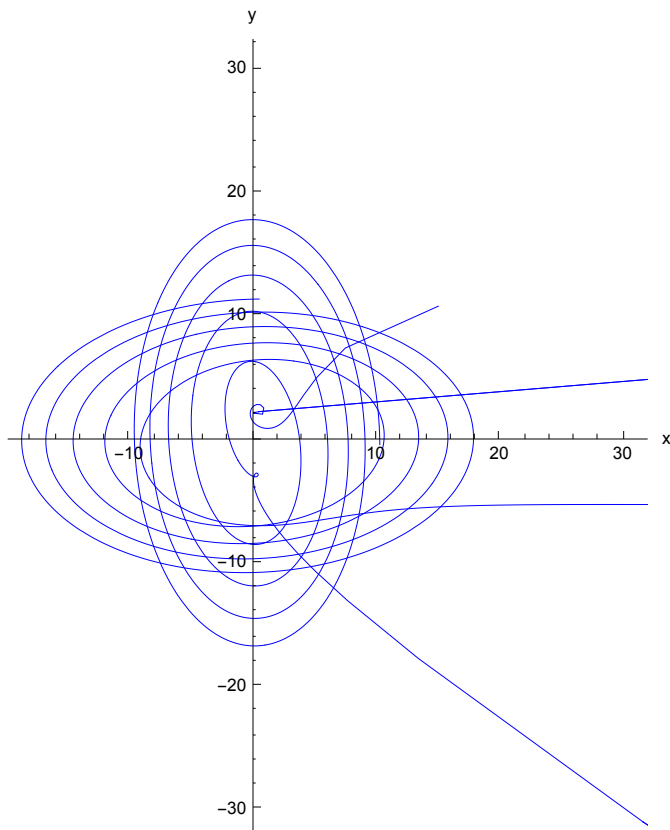
Clear[x, y, t, a, b, tmini, tmaxi]
a = GoldenRatio *  $\frac{3 (1 + \pi^2)}{2 \pi \sqrt{-2 \pi + t + \pi^2 t}}$ ;
b =  $\sqrt{9 \left(1 - t - \frac{t}{\pi^2} + \frac{2}{\pi}\right)}$  / GoldenRatio;
tmini = -10 * Pi;
tmaxi = 10 * Pi;
{x[t_], y[t_]} =
  {(a - b) * Cos[t] + b * Cos[(a - b) / b * t], (a - b) * Sin[t] - b * Sin[(a - b) / b * t]};

```

```

hypocycloid =
  ParametricPlot[{x[t], y[t]}, {t, tmini, tmaxi},
    PlotStyle -> {{Blue, Thickness[0.0015]}},
    AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]

```



$\frac{3 (1 + \pi^2)}{2 \pi \sqrt{-2 \pi + t + \pi^2 t}}$  is the derivative of  $\sqrt{9 \left(1 - t - \frac{t}{\pi^2} + \frac{2}{\pi}\right)}$

```

Clear[x, y, t, a, b, tmini, tmaxi]

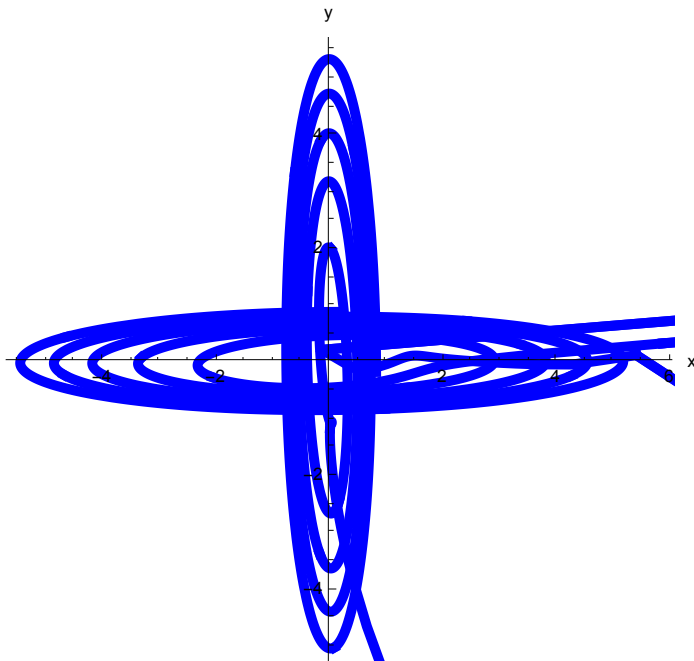
a = 
$$\frac{3 (1 + \pi^2)}{\text{GoldenRatio} * 2 \pi \sqrt{-2 \pi + t + \pi^2 t}}$$
;

b = GoldenRatio 
$$\sqrt{9 \left(1 - t - \frac{t}{\pi^2} + \frac{2}{\pi}\right)}$$
 / GoldenRatio;

tmini = -10 * Pi;
tmaxi = 10 * Pi;
{x[t_], y[t_]} =
  {(a - b) * Cos[t] + b * Cos[(a - b) / b * t], (a - b) * Sin[t] - b * Sin[(a - b) / b * t]};

hypocycloid =
  ParametricPlot[{x[t], y[t]}, {t, tmini, tmaxi},
    PlotStyle -> {{Blue, Thickness[0.015]}},
    AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]

```

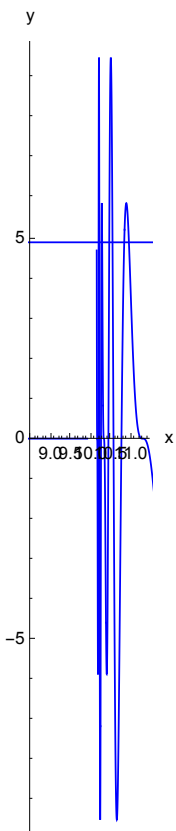


```

Clear[x, y, t, a, b, tmini, tmaxi]
a = 10;
b = 4;
tmini = -50 * Pi;
tmaxi = 50 * Pi;
{x[t_], y[t_]} =
  {
    (a - b) * Cos[ $\frac{3 (1 + \pi^2)}{2 \pi \sqrt{-2 \pi + t + \pi^2 t}}$ ] + b * Cos[(a - b) / b *  $\frac{3 (1 + \pi^2)}{2 \pi \sqrt{-2 \pi + t + \pi^2 t}}$ ],
    (a - b) * Sin[ $\sqrt{9 \left(1 - t - \frac{t}{\pi^2} + \frac{2}{\pi}\right)}$ ] - b * Sin[(a - b) / b *  $\sqrt{9 \left(1 - t - \frac{t}{\pi^2} + \frac{2}{\pi}\right)}$ ]
  };

hypocycloid =
  ParametricPlot[{x[t], y[t]}, {t, tmini, tmaxi},
    PlotStyle -> {{Blue, Thickness[0.015]}},
    AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]

```



CHAOS !

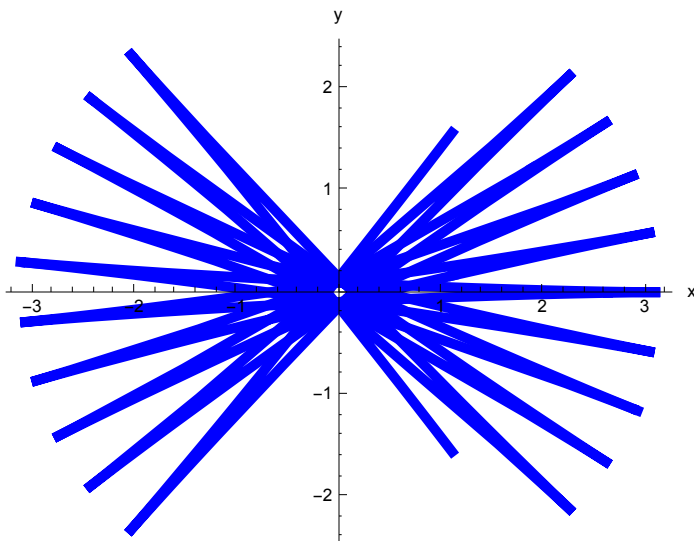


```

Clear[x, y, t, a, b, tmini, tmaxi]
a =  $\pi$ ;
b = GoldenRatio;
tmini =  $-10 \pi$ ;
tmaxi =  $10 \pi$ ;
{x[t_], y[t_]} =
  {(a - b) * Cos[t] + b * Cos[(a - b) / b * t], (a - b) * Sin[t] - b * Sin[(a - b) / b * t]};

hypocycloid =
  ParametricPlot[{x[t], y[t]}, {t, tmini, tmaxi},
    PlotStyle -> {{Blue, Thickness[0.015]}},
    AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]

```

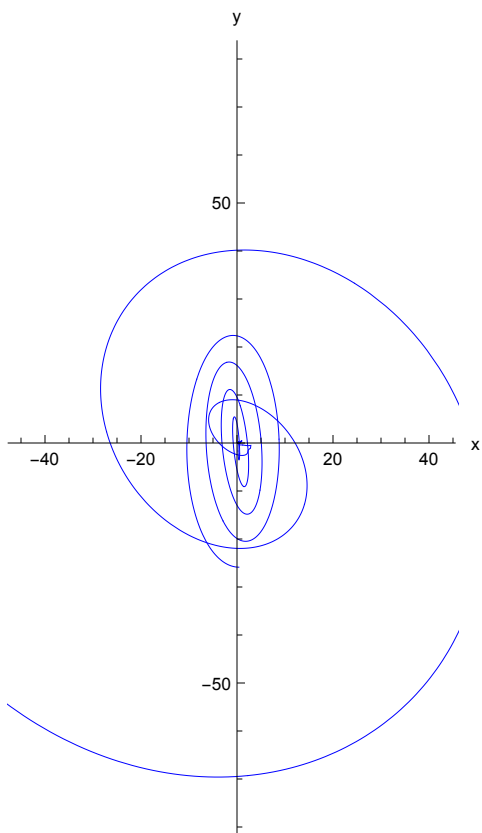


```

Clear[x, y, t, a, b, tmini, tmaxi]
a = -  $\frac{\text{Log}[1+t]}{(\text{GoldenRatio}) \text{ProductLog}[-\text{Log}[1+t]]}$ ;
b =  $\sqrt{9 \left(1 - t - \frac{t}{\pi^2} + \frac{2}{\pi}\right)} / \text{GoldenRatio}$ ;
tmini = -10 * Pi;
tmaxi = 10 * Pi;
{x[t_], y[t_]} =
  {(a - b) * Cos[t] + b * Cos[(a - b) / b * t], (a - b) * Sin[t] - b * Sin[(a - b) / b * t]};

hypocycloid =
  ParametricPlot[{x[t], y[t]}, {t, tmini, tmaxi},
    PlotStyle -> {{Blue, Thickness[0.0015]}},
    AspectRatio -> Automatic, AxesLabel -> {"x", "y"}]

```



$$C = \pi r$$

$$C_2 = \pi r_1$$

$$r^2 = r_1^2 + h^2$$

$$r = \sqrt{r_1^2 + h^2}$$

$$t = \theta r$$

$$t / \theta = r$$

$$t = C - C_2 = \pi r - \pi r_1 = \theta r$$

$$r_1^2 = r^2 - h^2$$

$$r_1 = \sqrt{r^2 - h^2}$$

$$h < r$$

$$\text{Solve}[r_1^2 + h^2 = r^2, h]$$

$$\left\{ \left\{ h \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ h \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\}$$

$$t = C - C_2 = \pi r - \pi r_1$$

$$\pi r - \pi r_1 = \pi (t / \theta) - \pi \sqrt{(t / \theta)^2 - h^2}$$

$$\text{Solve}\left[\pi (t / \theta) - \pi \sqrt{(t / \theta)^2 - (h^2)} = t, h\right]$$

$$t + \pi \sqrt{(t / \theta)^2 - (h^2)} = \pi (t / \theta)$$

$$\pi \sqrt{(t / \theta)^2 - (h^2)} = \pi (t / \theta) - t$$

$$(t / \theta) - t / \pi = \sqrt{(t / \theta)^2 - (h^2)}$$

$$\{(t / \theta) - t / \pi\} \{(t / \theta) - t / \pi\} = ((t / \theta)^2 - (h^2))$$

$$(h^2) + \{(t / \theta) - t / \pi\} \{(t / \theta) - t / \pi\} = (t / \theta)^2$$

$$(t / \theta)^2 - \{(t / \theta) - t / \pi\} \{(t / \theta) - t / \pi\} = (h^2)$$

$$h = \text{Sqrt}[(t / \theta)^2 - \{(t / \theta) - t / \pi\} \{(t / \theta) - t / \pi\}]$$

$$\left\{ \sqrt{-\left(-\frac{t}{\pi} + \frac{t}{\theta}\right)^2 + \frac{t^2}{\theta^2}} \right\}$$

$$\sqrt{-\left(-\frac{(\theta r)}{\pi} + \frac{(\theta r)}{\theta}\right)^2 + \frac{(\theta r)^2}{\theta^2}}$$

$$t + \pi \sqrt{((t/\theta)^2 - (h^2))} = \pi (t/\theta)$$

$$\theta t + \theta \pi \sqrt{((t/\theta)^2 - (h^2))} = \pi (t)$$

$$\theta + \left( \theta \pi \sqrt{((t/\theta)^2 - (h^2))} \right) / t = \pi$$

$$\left( \theta \pi \sqrt{((t/\theta)^2 - (h^2))} \right) / t = \pi - \theta$$

$$\left( \theta \pi \sqrt{((t/\theta)^2 - (h^2))} \right) / t = \pi - \theta$$

$$\left( \sqrt{((t/\theta)^2 - (h^2))} \right) / t = (\pi - \theta) / \theta \pi$$

$$\pi \left( \sqrt{((t/\theta)^2 - (h^2))} \right) / t = (\pi - \theta) / \theta$$

$$\pi \theta \left( \sqrt{((t/\theta)^2 - (h^2))} \right) / t = (\pi - \theta)$$

$$\pi \theta \left( \left( \sqrt{((t/\theta)^2 - (h^2))} \right) / t \right) - \pi = -\theta$$

$$\pi \left( \left( \sqrt{((t/\theta)^2 - (h^2))} \right) / t \right) - \pi = -1$$

$$\{\pi^2 ((t/\theta)^2 - (h^2))\} / t^2 - \pi = -1$$

$$\{\pi^2 ((t/\theta)^2 - (h^2))\} / t^2 = -1 + \pi$$

$$\{\pi^2 ((t/\theta)^2 - (h^2))\} = t^2 (-1 + \pi)$$

$$\{\pi^2 ((t/\theta)^2 - (h^2))\} = t^2 (-1 + \pi)$$

$$\pi^2 (t/\theta)^2 - \pi^2 (h^2) = t^2 (-1 + \pi)$$

$$\pi^2 (t/\theta)^2 = t^2 (-1 + \pi) + \pi^2 (h^2)$$

$$(t/\theta)^2 = \{t^2 (-1 + \pi) + \pi^2 (h^2)\} / \pi^2$$

$$(t/\theta) = \sqrt{\{t^2 (-1 + \pi) + \pi^2 (h^2)\} / \pi^2}$$

$$\left( t / \sqrt{\{t^2 (-1 + \pi) + \pi^2 (h^2)\} / \pi^2} \right) = 1$$

$$t / \sqrt{\{t^2 (-1 + \pi) + \pi^2 (h^2)\} / \pi^2} = \theta$$

$$r^2 = (1 + 3 + 5 + 7 \dots + (2n - 1))$$

$$n = 1, 2, 3, 4, 5, 6 \dots$$

$$\sqrt{-\left(-\frac{(\theta r)}{\pi} + \frac{(\theta r)}{\theta}\right)^2 + \frac{(\theta r)^2}{\theta^2}} = h$$

$$\sqrt{-\left(-\frac{(\theta r)}{\pi} + \frac{(\theta r)}{\theta}\right)^2 + r^2} = h$$

$$\left(-\frac{(\theta r)}{\pi} + \frac{(\theta r)}{\theta}\right) \left(-\frac{(\theta r)}{\pi} + \frac{(\theta r)}{\theta}\right)$$

$$\text{Expand}\left[\left(-\frac{\theta r}{\pi} + \frac{\theta r}{\theta}\right)^2\right]$$

$$\frac{\theta r^2}{\pi^2} + \frac{\theta r^2}{\theta^2} - \frac{2\theta r^2}{\pi\theta}$$

$$\text{Sqrt}\left[\left(-\left(\frac{\theta r^2}{\pi^2} + \frac{\theta r^2}{\theta^2} - \frac{2\theta r^2}{\pi\theta}\right)\right) + r^2\right]$$

$$\sqrt{r^2 - \frac{\theta r^2}{\pi^2} - \frac{\theta r^2}{\theta^2} + \frac{2\theta r^2}{\pi\theta}}$$

$$\sqrt{r^2 - \frac{\theta r^2}{\pi^2} - \frac{\theta r^2}{\theta^2} + \frac{2\theta r^2}{\pi\theta}}$$

$$\sqrt{r^2 - \frac{\theta r^2}{\pi^2} - \frac{\theta r^2}{\theta^2} + \frac{2\theta r^2}{\pi\theta}} = h$$

$$(h^2) = r^2 - \frac{\theta r^2}{\pi^2} - \frac{\theta r^2}{\theta^2} + \frac{2\theta r^2}{\pi\theta}$$

$$(h^2) = r^2 - \frac{\theta r^2}{\pi^2} - \frac{\theta r^2}{\theta^2} + \frac{2\theta r^2}{\pi\theta}$$

$$((h^2) / r^2) = 1 - \frac{\theta}{\pi^2} - \theta + (2\theta / \pi\theta)$$

$$(h^2) / \left(1 - \frac{\theta}{\pi^2} - \theta + (2\theta / \pi\theta)\right) = r^2$$

$$r^2 = (1 + 3 + 5 + 7 \dots + (2n - 1))$$

$$\text{for } n = 1, \quad r^2 = (2n - 1)$$

$$(2n - 1) = (h^2) / \left( 1 - \frac{\theta}{\pi^2} - \theta + (2\theta / \pi\theta) \right)$$

$$1 = (h^2) / \left( 1 - \frac{\theta}{\pi^2} - \theta + (2\theta / \pi\theta) \right)$$

$$1 - \frac{\theta}{\pi^2} - \theta + (2\theta / \pi\theta) = (h^2)$$

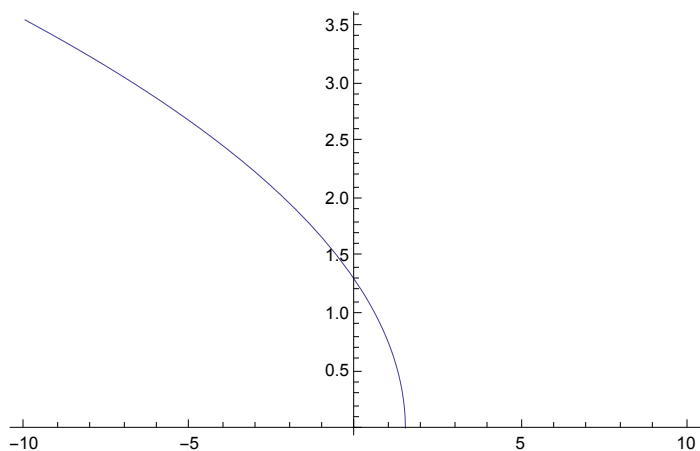
$$1 - \frac{\theta}{\pi^2} - \theta + (2\theta / \pi\theta)$$

$$1 - \theta - \frac{\theta}{\pi^2} + \frac{2\theta}{\pi\theta}$$

$$\sqrt{\left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}$$

$$\sqrt{1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}}$$

$$\text{Plot}\left[\sqrt{\left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \{\theta, -10, 10\}\right]$$



graph of  $n = 1$

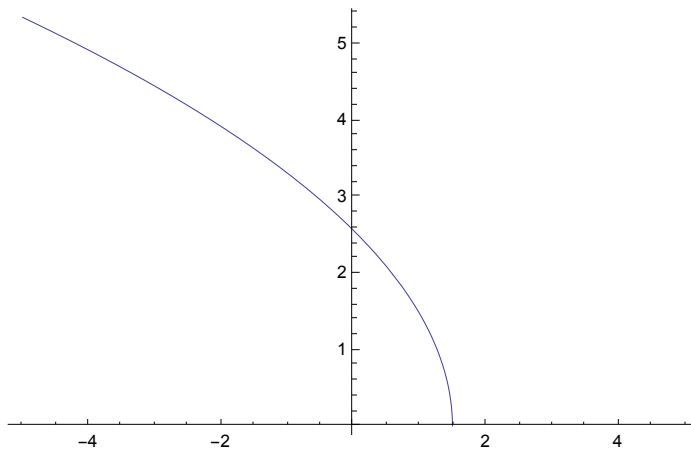
for  $n = 2$ ,  $r^2 = 1 + (2n - 1) = 4$

$$4 = (h^2) / \left( 1 - \frac{\theta}{\pi^2} + \theta + (2\theta / \pi\theta) \right)$$

$$4 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)$$

$$4 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right) = \text{answer2}$$

$$\text{Plot} \left[ \sqrt{4 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \{\theta, -5, 5\} \right]$$

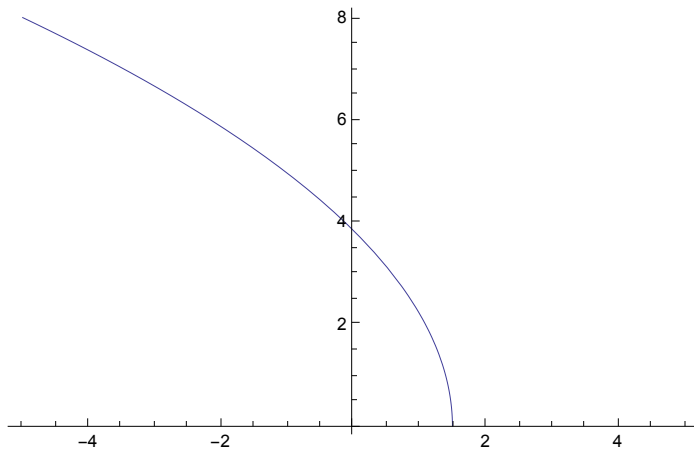


graph of  $n = 2$

for  $n = 3$ ,  $r^2 = 9$

$$\left[ \sqrt{9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \theta \right] = \text{answer3}$$

$$\text{Plot}\left[\sqrt{9\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\{\theta,-5,5\}\right]$$

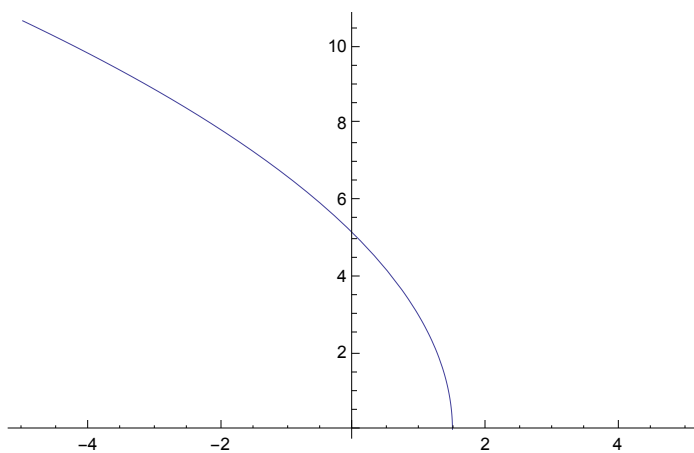


Graph of  $n = 3$

for  $n = 4$ ,  $r^2 = 16$

$$\sqrt{16\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)} = \text{answer4}$$

$$\text{Plot}\left[\sqrt{16\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\{\theta,-5,5\}\right]$$



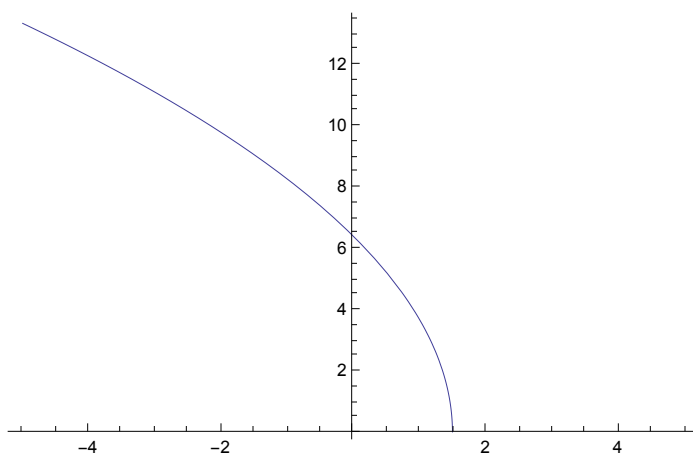
Graph for  $n = 4$



For  $n = 5$ ,  $(r^2) = 25$

$$\sqrt{25 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = \text{answer5}$$

$$\text{Plot} \left[ \sqrt{25 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \{\theta, -5, 5\} \right]$$

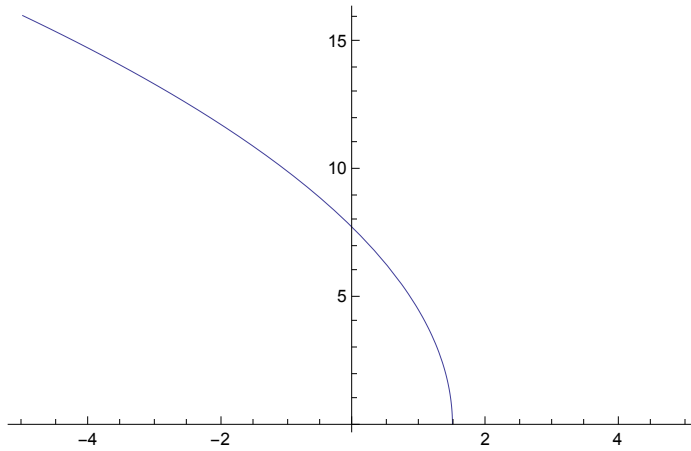


Graph for  $n = 5$

For  $n = 6$ ,  $r^2 = 36$

$$\sqrt{36 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = \text{answer6}$$

Plot $\left[\sqrt{36\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)}, \{\theta, -5, 5\}\right]$



Graph for  $n = 6$

The Digression ...

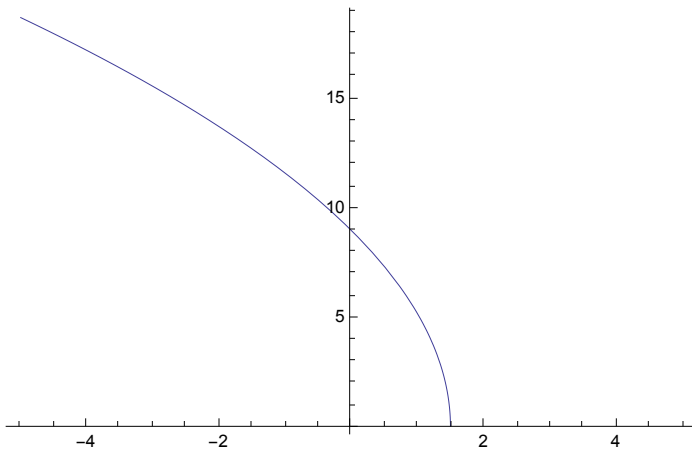
$$\int \sqrt{36\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)} d\theta$$

Digression The ...

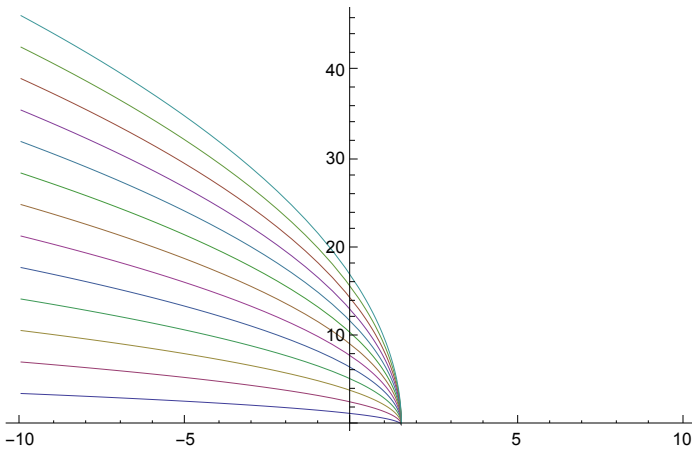
$$-\frac{4\left(2\pi-\pi^2(-1+\theta)-\theta\right)^{3/2}}{\pi+\pi^3}$$

For  $n = 7$ ,  $r^2 = 49$

$\text{Plot}\left[\sqrt{49\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\{\theta,-5,5\}\right]$



$\text{Plot}\left[\left\{\sqrt{1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}},\sqrt{4\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{9\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{16\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\right.\right.$   
 $\left.\sqrt{25\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{36\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{49\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\right.$   
 $\left.\sqrt{64\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{81\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{100\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\right.$   
 $\left.\sqrt{121\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{144\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\sqrt{169\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)}\right\},\{\theta,-10,10\}\right]$



$$r_1 = \sqrt{(r^2 - h^2)}$$

$$r^2 = (1 + 3 + 5 + 7 \dots + (2n - 1))$$

$$n = 1, 2, 3, 4, 5, 6 \dots$$

For  $n = 1$ ;

$$(2n - 1) - \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right) = 1 - \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right) = \sqrt{\left(1 - \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)\right)}$$

$$\sqrt{\left(1 - \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)\right)}$$

$$\sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}$$

$$\sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}} = r_1$$

For  $n = 2$ ;

$$2n - (4) \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right) = \left(4 - \left((4) \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)\right)\right)$$

$$\left(4 - \left((4) \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)\right)\right)$$

$$4 - 4 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)$$

$$4 - 4 \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)$$

$$4 - 4 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)$$

$$\sqrt{4 - 4 \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)} = r_1$$

For n = 3;

$$1 + 3 + (2n - 1) - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right) = 1 + 3 + (2(3) - 1) - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)$$

$$1 + 3 + (2(3) - 1) - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)$$

$$9 - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)$$

$$\sqrt{9 - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

For n = 4;

$$\sqrt{16 - 16 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

For n = 5;

$$\sqrt{25 - 25 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

For n = 6;

$$\sqrt{36 - 36 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

For n = 7;

$$\sqrt{49 - 49 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

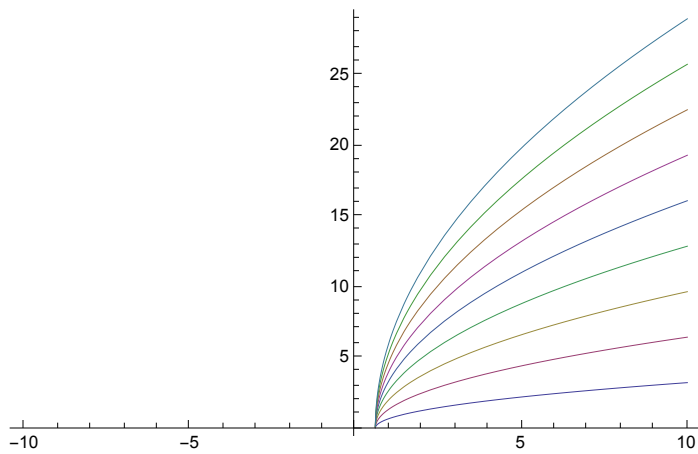
For n = 8;

$$\sqrt{64 - 64 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

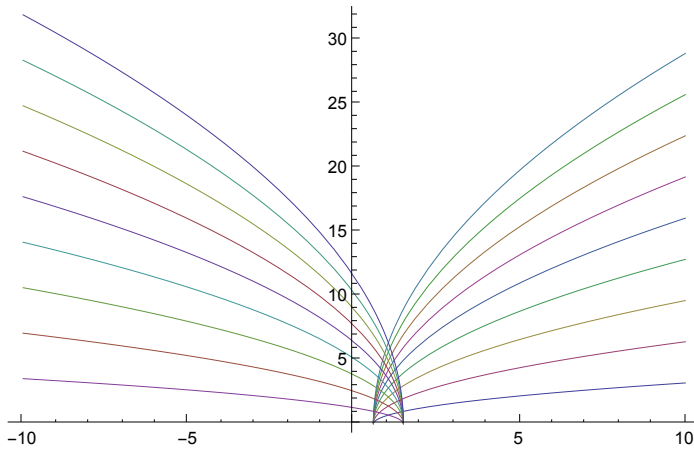
For  $n = 9$ ;

$$\sqrt{81 - 81 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = r_1$$

$$\text{Plot} \left[ \left\{ \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \right. \right. \\ \left. \sqrt{9 - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \sqrt{16 - 16 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \sqrt{25 - 25 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \right. \\ \left. \sqrt{36 - 36 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \sqrt{49 - 49 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \right. \\ \left. \sqrt{64 - 64 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}, \sqrt{81 - 81 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} \right\}, \{\theta, -10, 10\} \right]$$



$$\text{Plot}\left[\left\{\sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{9 - 9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right.\right. \\ \left.\left.\sqrt{16 - 16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25 - 25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{36 - 36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right.\right. \\ \left.\left.\sqrt{49 - 49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64 - 64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{81 - 81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right.\right. \\ \left.\left.\sqrt{\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right.\right. \\ \left.\left.\sqrt{16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right.\right. \\ \left.\left.\sqrt{49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}\right\}, \{\theta, -10, 10\}\right]$$



$$dC = C1 - C2$$

$$C1 = 2 \pi r; C2 = 2 \pi r1$$

$$dC = 2 \pi r - 2 \pi r1 = t = r \theta$$

For  $n = 1$ ;

$$2 \pi r = 2 \pi \left( \sqrt{2 n - 1} \right) = 2 \pi$$

$$2 \pi r 1 = \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}$$

$$2 \pi - \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}} = dC$$

$$2 \pi - \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}$$

$$2 \pi - \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}$$

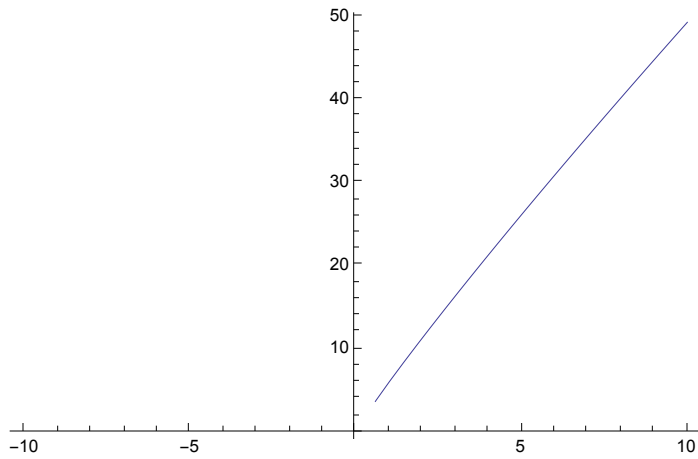
$$\int \left( 2 \pi - \left( \left( \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}} \right)^{(1/2)} \right) \right) d\theta$$

$$2 \pi \theta - \frac{4 \pi^2 \left( -\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2} \right)^{5/4}}{5 (1 + \pi^2)}$$

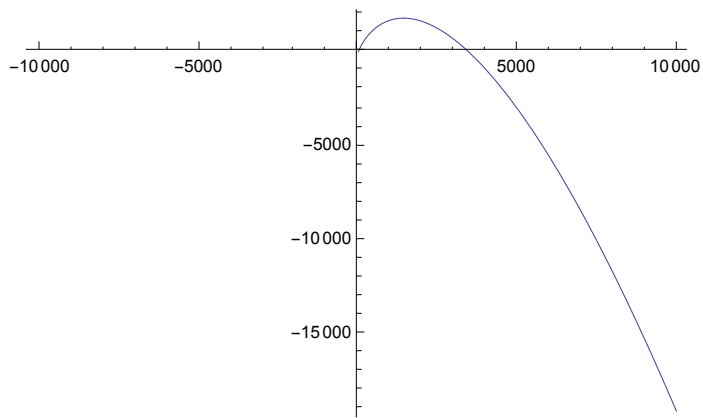
$$2 \pi \theta - \frac{4 \pi^2 \left( -\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2} \right)^{5/4}}{5 (1 + \pi^2)} = C$$



$$\text{Plot}\left[2 \pi \theta - \frac{4 \pi^2 \left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5 (1 + \pi^2)}, \{\theta, -10, 10\}\right]$$



$$\text{Plot}\left[2 \pi \theta - \frac{4 \pi^2 \left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5 (1 + \pi^2)}, \{\theta, -10\,000, 10\,000\}\right]$$



$$dC = 2 \pi r - 2 \pi r_1 = t = r \theta$$

For  $n = 2$

$$2 \pi \left( \sqrt{2 n} \right) = 4 \pi$$

$$4 \pi - 2 \pi \sqrt{4 - 4 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} = dC = t = r \theta$$

$$\int \left( 4\pi - 2\pi \sqrt{4 - 4 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} \right) d\theta$$

$$4\pi\theta - \frac{8 \left( -2\pi + \theta + \pi^2 \theta \right)^{3/2}}{3 \left( 1 + \pi^2 \right)}$$

For n = 3

$$2\pi \left( \sqrt{1 + 3 + (2n - 1)} \right) = 6\pi$$

$$\left( 6\pi - 2\pi \left( \sqrt{9 - 9 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)} \right) \right)$$

$$6\pi - 2\pi \sqrt{9 - 9 \left( 1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2} \right)}$$

$$\int \left( 6\pi - 2\pi \sqrt{9 - 9 \left( 1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2} \right)} \right) d\theta$$

$$6\pi\theta - \frac{4 \left( -2\pi + \theta + \pi^2 \theta \right)^{3/2}}{1 + \pi^2}$$

For n = 4 ;

$$dC = 2\pi r - 2\pi r1 = t = r\theta$$

$$2\pi (1 + 3 + 5 + (2n - 1)) - 2\pi \sqrt{16 - 16 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}$$

$$2(8 + 2n)\pi - 2\pi \sqrt{16 - 16 \left( 1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi} \right)}$$

$$2(8 + 2n)\pi - 2\pi \sqrt{16 - 16 \left( 1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2} \right)}$$

$$2\pi (1 + 3 + 5 + (2(4) - 1))$$

$$32\pi$$

$$32 \pi - 2 \pi \sqrt{16 - 16 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)}$$

$$32 \pi - 2 \pi \sqrt{16 - 16 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)}$$

$$\int \left( 32 \pi - 2 \pi \sqrt{16 - 16 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)} \right) d\theta$$

$$-8 \left( -4 \pi \theta + \frac{2 \left( -2 \pi + \theta + \pi^2 \theta \right)^{3/2}}{3 \left( 1 + \pi^2 \right)} \right)$$

For n = 5;

$$2 \pi (1 + 3 + 5 + 7 + (2 n - 1)) - 2 \pi$$

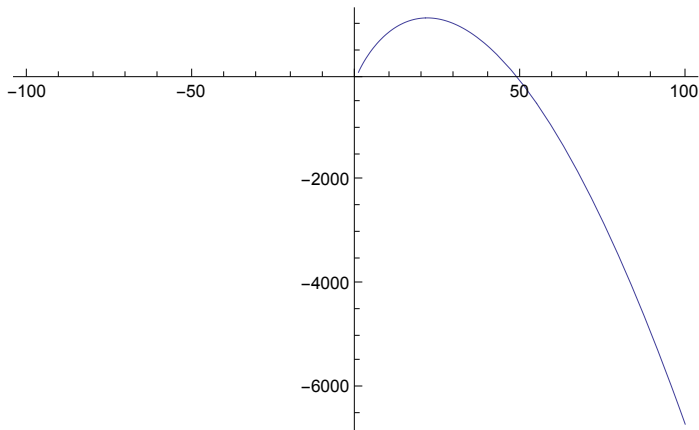
$$2 \pi (1 + 3 + 5 + 7 + (2 (5) - 1)) - 2 \pi$$

$$48 \pi$$

$$\int \left( 48 \pi - 2 \pi \sqrt{25 - 25 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)} \right) d\theta$$

$$48 \pi \theta - \frac{20 \left( -2 \pi + \theta + \pi^2 \theta \right)^{3/2}}{3 \left( 1 + \pi^2 \right)}$$

$$\text{Plot} \left[ 48 \pi \theta - \frac{20 \left( -2 \pi + \theta + \pi^2 \theta \right)^{3/2}}{3 \left( 1 + \pi^2 \right)}, \{\theta, -100, 100\} \right]$$



For  $n = 6$ ;

$$2\pi (1 + 3 + 5 + 7 + 9 + (2n - 1)) - 2\pi$$

For  $n = 7$ ;

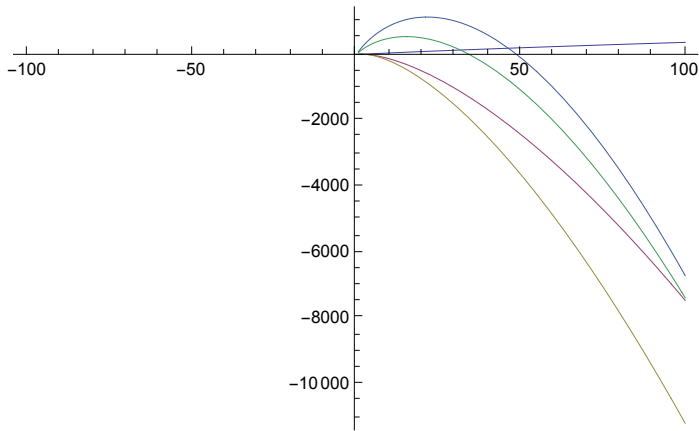
$$2\pi (1 + 3 + 5 + 7 + 9 + 11 + (2n - 1)) - 2\pi$$

For  $n = 8$ ;

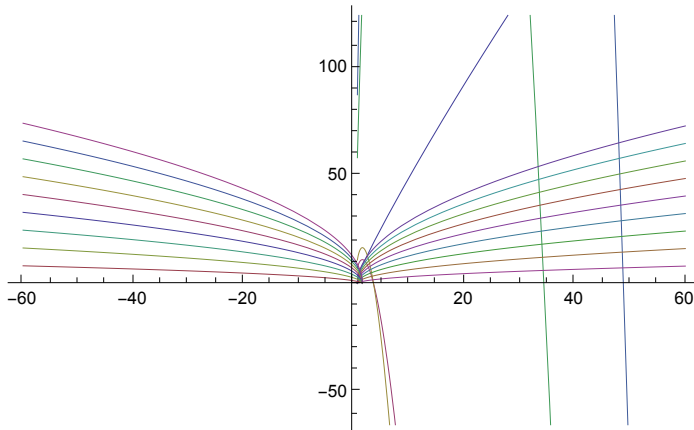
$$2\pi (1 + 3 + 5 + 7 + 9 + 11 + 13 + (2n - 1)) - 2\pi$$

The Following Plot Combines Integrals of dC for  $n = 1, 2, 3, 4, 5$

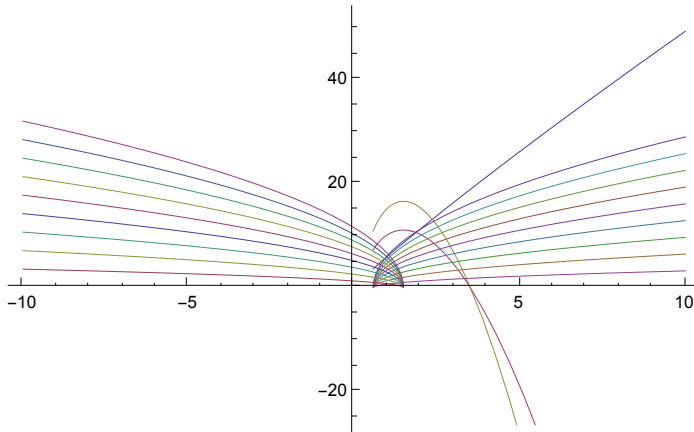
$$\text{Plot}\left[\left\{\left(2\pi\theta - \frac{4\pi^2\left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5(1+\pi^2)}\right), \left(4\pi\theta - \frac{8(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \right.\right. \\ \left.\left(\frac{6\pi\theta - \frac{4(-2\pi + \theta + \pi^2\theta)^{3/2}}{1+\pi^2}}{1+\pi^2}\right), \left(-8\left(-4\pi\theta + \frac{2(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right)\right), \right. \\ \left.\left(\frac{48\pi\theta - \frac{20(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}}{3(1+\pi^2)}\right)\right\}, \{\theta, -100, 100\}]$$



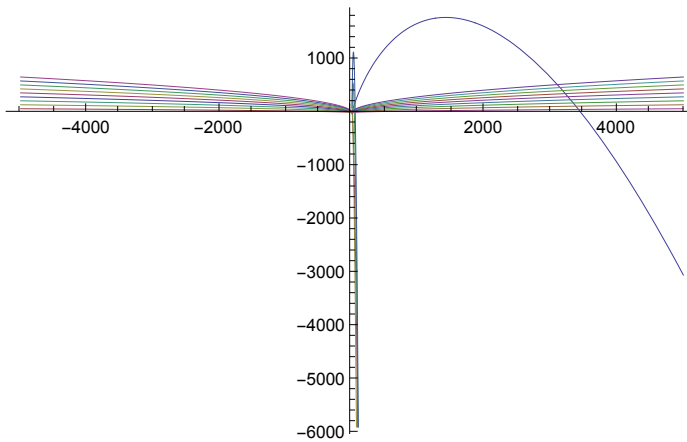
$$\begin{aligned}
& \text{Plot}\left[\left\{\left(2\pi\theta - \frac{4\pi^2\left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5(1+\pi^2)}\right), \left(4\pi\theta - \frac{8(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \right. \right. \\
& \left. \left(6\pi\theta - \frac{4(-2\pi + \theta + \pi^2\theta)^{3/2}}{1+\pi^2}\right), \left(-8\left(-4\pi\theta + \frac{2(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right)\right), \right. \\
& \left. \left(48\pi\theta - \frac{20(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right. \\
& \sqrt{9 - 9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16 - 16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25 - 25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{36 - 36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{49 - 49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64 - 64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{81 - 81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \left. \sqrt{49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}\right\}, \{\theta, -60, 60\}]
\end{aligned}$$



$$\begin{aligned}
& \text{Plot}\left[\left\{\left(2\pi\theta - \frac{4\pi^2\left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5(1+\pi^2)}\right), \left(4\pi\theta - \frac{8(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \right. \right. \\
& \left. \left(6\pi\theta - \frac{4(-2\pi + \theta + \pi^2\theta)^{3/2}}{1+\pi^2}\right), \left(-8\left(-4\pi\theta + \frac{2(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right)\right), \right. \\
& \left. \left(48\pi\theta - \frac{20(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right. \\
& \sqrt{9 - 9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16 - 16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25 - 25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{36 - 36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{49 - 49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64 - 64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{81 - 81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}}, \sqrt{4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \left. \sqrt{49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}\right\}, \{\theta, -10, 10\}]
\end{aligned}$$



$$\text{Plot}\left[\left\{\left(2\pi\theta - \frac{4\pi^2\left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5(1+\pi^2)}\right), \left(4\pi\theta - \frac{8(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \right.\right. \\ \left.\left(\frac{6\pi\theta - \frac{4(-2\pi + \theta + \pi^2\theta)^{3/2}}{1+\pi^2}}{1+\pi^2}\right), \left(-8\left(-4\pi\theta + \frac{2(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right)\right), \right. \\ \left.\left(\frac{48\pi\theta - \frac{20(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}}{3(1+\pi^2)}\right), \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right. \\ \sqrt{9 - 9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16 - 16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25 - 25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\ \sqrt{36 - 36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{49 - 49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64 - 64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\ \sqrt{81 - 81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\ \sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\ \sqrt{49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}\right\}, \{\theta, -5000, 5000\}]$$



The Derivatives of  $r_1$  and their graphs

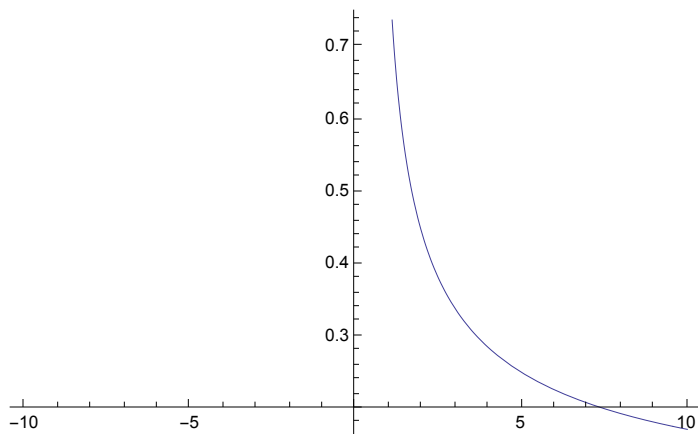
$$D\left[\sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \theta\right]$$

$$\frac{1 + \frac{1}{\pi^2}}{2\sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}}$$

$$\text{Simplify}\left[\frac{1 + \frac{1}{\pi^2}}{2 \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}}\right]$$

$$\frac{1 + \pi^2}{2 \pi \sqrt{-2 \pi + \theta + \pi^2 \theta}}$$

$$\text{Plot}\left[\frac{1 + \pi^2}{2 \pi \sqrt{-2 \pi + \theta + \pi^2 \theta}}, \{\theta, -10, 10\}\right]$$



$$\text{D}\left[\sqrt{4 - 4 \left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \theta\right]$$

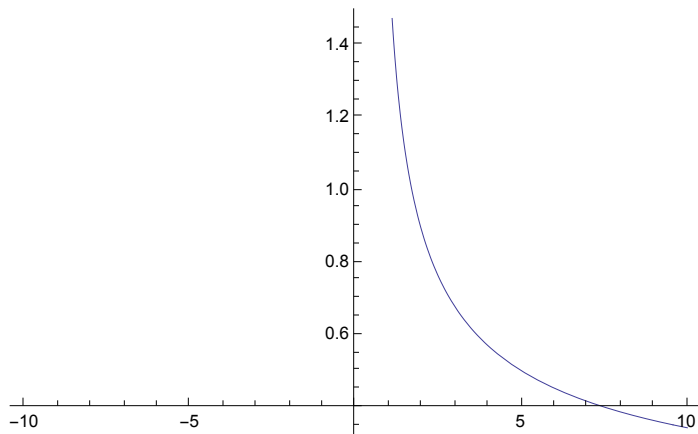
$$-\frac{2 \left(-1 - \frac{1}{\pi^2}\right)}{\sqrt{4 - 4 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)}}$$

$$\text{Simplify}\left[-\frac{2 \left(-1 - \frac{1}{\pi^2}\right)}{\sqrt{4 - 4 \left(1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}\right)}}\right]$$

$$\frac{1 + \pi^2}{\pi \sqrt{-2 \pi + \theta + \pi^2 \theta}}$$



$$\text{Plot}\left[\frac{1+\pi^2}{\pi \sqrt{-2\pi+\theta+\pi^2\theta}}, \{\theta, -10, 10\}\right]$$



$$D\left[\sqrt{9-9\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)}, \theta\right]$$

$$-\frac{9\left(-1-\frac{1}{\pi^2}\right)}{2\sqrt{9-9\left(1+\frac{2}{\pi}-\theta-\frac{\theta}{\pi^2}\right)}}$$

$$\text{Simplify}\left[-\frac{9\left(-1-\frac{1}{\pi^2}\right)}{2\sqrt{9-9\left(1+\frac{2}{\pi}-\theta-\frac{\theta}{\pi^2}\right)}}\right]$$

$$\frac{3\left(1+\pi^2\right)}{2\pi\sqrt{-2\pi+\theta+\pi^2\theta}}$$

Plots of the derivative of h

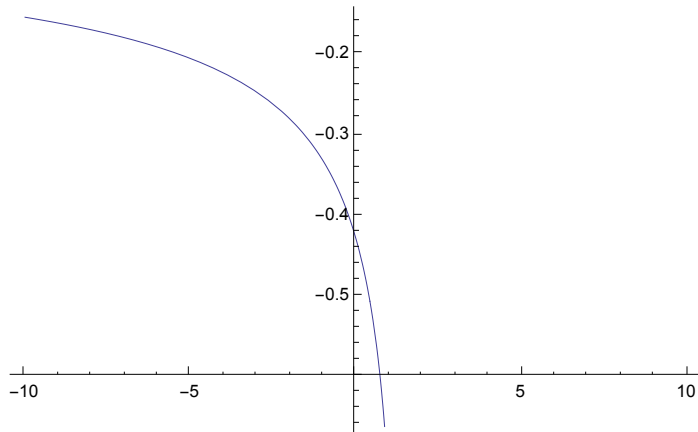
$$D\left[\sqrt{\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)}, \theta\right]$$

$$\frac{-1-\frac{1}{\pi^2}}{2\sqrt{1+\frac{2}{\pi}-\theta-\frac{\theta}{\pi^2}}}$$

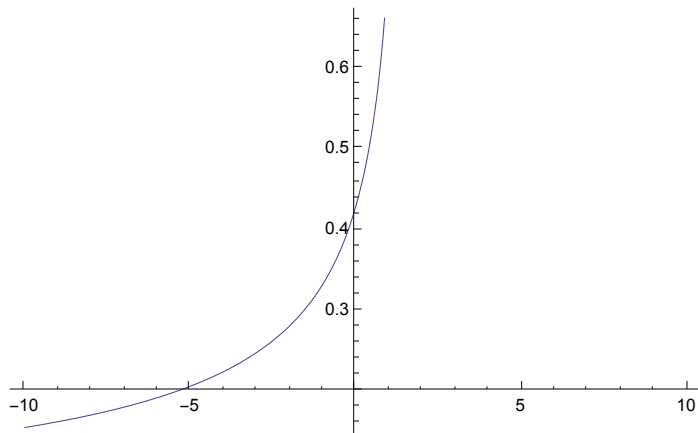
$$\text{Simplify}\left[\frac{-1 - \frac{1}{\pi^2}}{2 \sqrt{1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}}}\right]$$

$$- \frac{1 + \pi^2}{2 \pi \sqrt{2 \pi - \pi^2 (-1 + \theta) - \theta}}$$

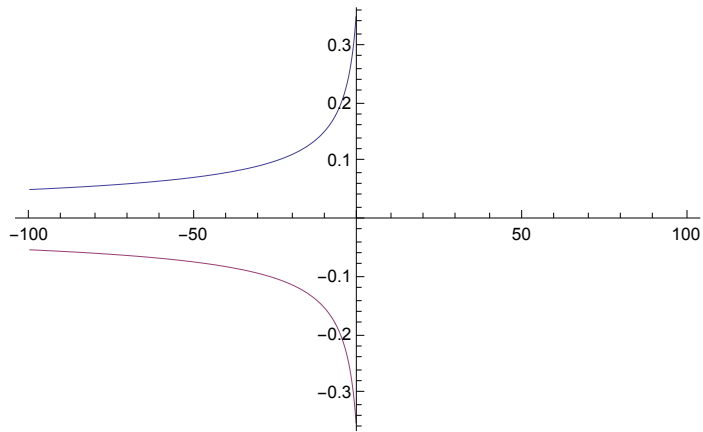
$$\text{Plot}\left[\left(-\frac{1 + \pi^2}{2 \pi \sqrt{2 \pi - \pi^2 (-1 + \theta) - \theta}}\right), \{\theta, -10, 10\}\right]$$



$$\text{Plot}\left[\left(\frac{1 + \pi^2}{2 \pi \sqrt{2 \pi - \pi^2 (-1 + \theta) - \theta}}\right), \{\theta, -10, 10\}\right]$$



$$\text{Plot}\left[\left\{\left(\frac{1+\pi^2}{2\pi\sqrt{2\pi-\pi^2(-1+\theta)-\theta}}\right),\left(-\frac{1+\pi^2}{2\pi\sqrt{2\pi-\pi^2(-1+\theta)-\theta}}\right)\right\},\{\theta,-10,10\}\right]$$

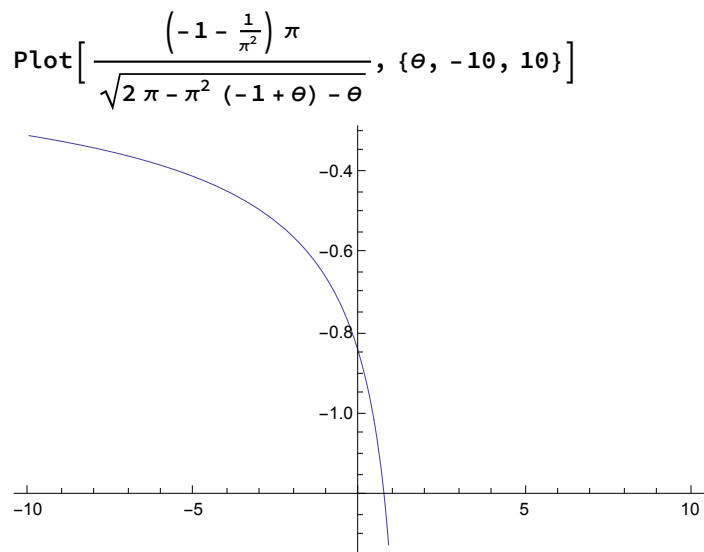


$$\text{D}\left[\sqrt{4\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)},\theta\right]$$

$$\frac{-1-\frac{1}{\pi^2}}{\sqrt{1+\frac{2}{\pi}-\theta-\frac{\theta}{\pi^2}}}$$

$$\text{Simplify}\left[\frac{-1-\frac{1}{\pi^2}}{\sqrt{1+\frac{2}{\pi}-\theta-\frac{\theta}{\pi^2}}}\right]$$

$$\frac{\left(-1-\frac{1}{\pi^2}\right)\pi}{\sqrt{2\pi-\pi^2(-1+\theta)-\theta}}$$

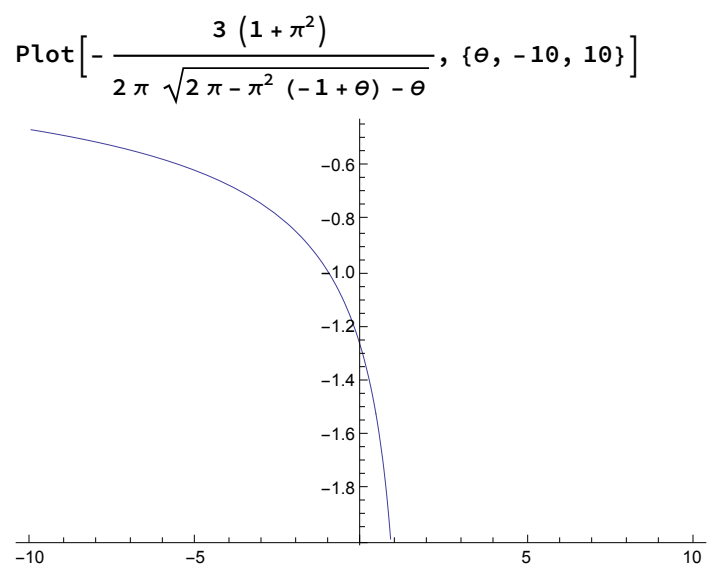


$$D\left[\sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \theta\right]$$

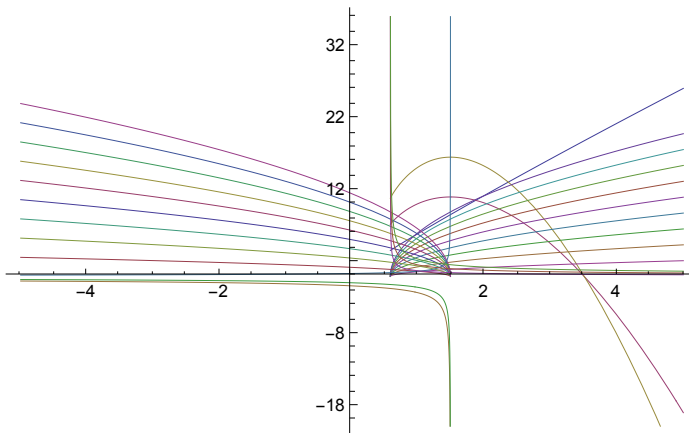
$$\frac{3\left(-1 - \frac{1}{\pi^2}\right)}{2\sqrt{1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}}}$$

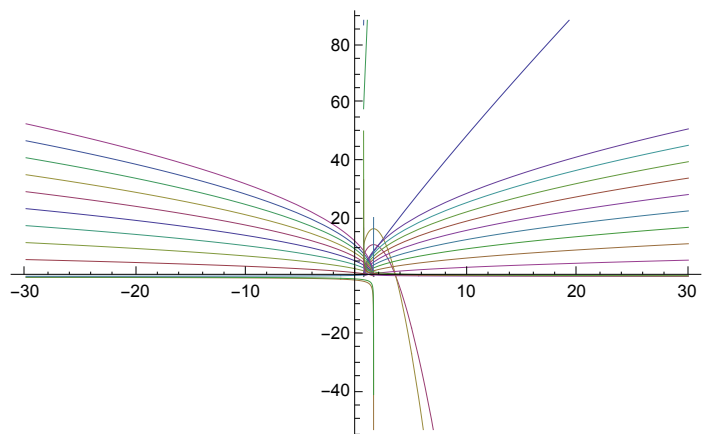
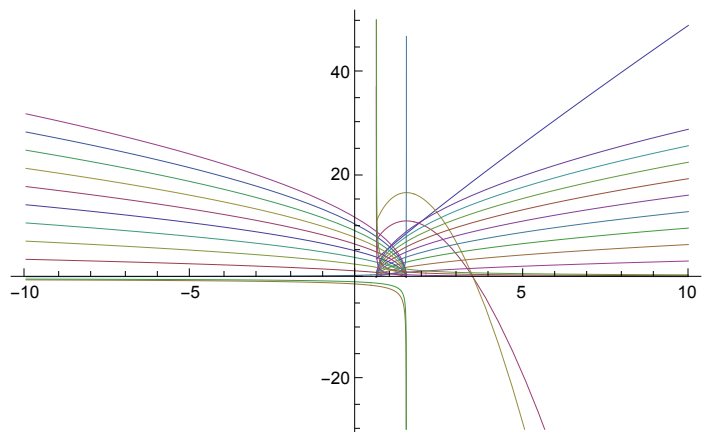
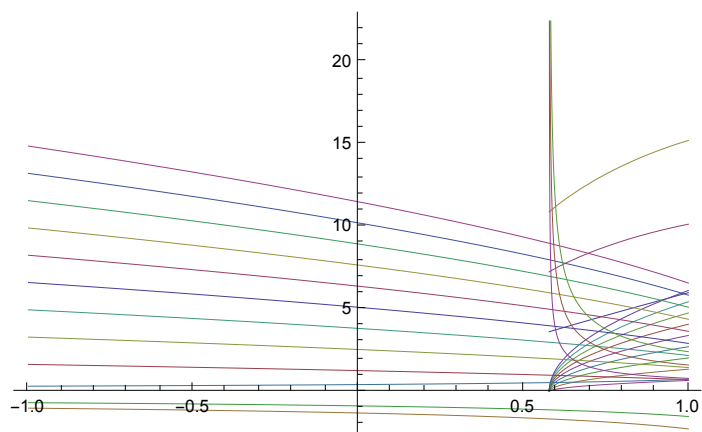
$$\text{Simplify}\left[\frac{3\left(-1 - \frac{1}{\pi^2}\right)}{2\sqrt{1 + \frac{2}{\pi} - \theta - \frac{\theta}{\pi^2}}}\right]$$

$$-\frac{3(1 + \pi^2)}{2\pi\sqrt{2\pi - \pi^2(-1 + \theta)} - \theta}$$



$$\begin{aligned}
& \text{Plot}\left[\left\{\left(2\pi\theta - \frac{4\pi^2\left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5(1+\pi^2)}\right), \left(4\pi\theta - \frac{8(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \right. \right. \\
& \left. \left(6\pi\theta - \frac{4(-2\pi + \theta + \pi^2\theta)^{3/2}}{1+\pi^2}\right), \left(-8\left(-4\pi\theta + \frac{2(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right)\right), \right. \\
& \left. \left(48\pi\theta - \frac{20(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right. \\
& \sqrt{9 - 9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16 - 16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25 - 25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{36 - 36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{49 - 49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64 - 64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{81 - 81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}}, \sqrt{4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{16\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{25\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{36\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& \sqrt{49\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{64\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{81\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \\
& -\frac{3(1+\pi^2)}{2\pi\sqrt{2\pi - \pi^2(-1+\theta) - \theta}}, \frac{\left(-1 - \frac{1}{\pi^2}\right)\pi}{\sqrt{2\pi - \pi^2(-1+\theta) - \theta}}, \left(\frac{1+\pi^2}{2\pi\sqrt{2\pi - \pi^2(-1+\theta) - \theta}}\right), \\
& \left.\frac{1+\pi^2}{2\pi\sqrt{-2\pi + \theta + \pi^2\theta}}, \frac{1+\pi^2}{\pi\sqrt{-2\pi + \theta + \pi^2\theta}}, \frac{3(1+\pi^2)}{2\pi\sqrt{-2\pi + \theta + \pi^2\theta}}\right\}, \{\theta, -5, 5\}]
\end{aligned}$$





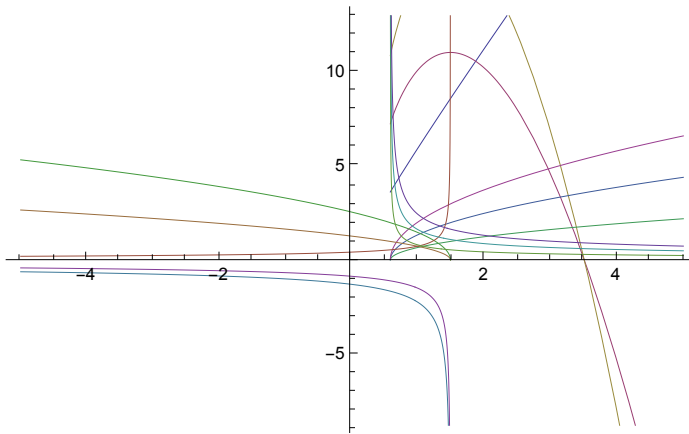
$$\text{Plot}\left[\left\{\left(2\pi\theta - \frac{4\pi^2\left(-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}\right)^{5/4}}{5(1+\pi^2)}\right), \left(4\pi\theta - \frac{8(-2\pi + \theta + \pi^2\theta)^{3/2}}{3(1+\pi^2)}\right), \right.\right.$$

$$\left.\left(6\pi\theta - \frac{4(-2\pi + \theta + \pi^2\theta)^{3/2}}{1+\pi^2}\right), \sqrt{-\frac{2}{\pi} + \theta + \frac{\theta}{\pi^2}}, \sqrt{4 - 4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \right.$$

$$\sqrt{9 - 9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}}, \sqrt{4\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}, \sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)},$$

$$-\frac{3(1+\pi^2)}{2\pi\sqrt{2\pi - \pi^2(-1+\theta) - \theta}}, \frac{\left(-1 - \frac{1}{\pi^2}\right)\pi}{\sqrt{2\pi - \pi^2(-1+\theta) - \theta}}, \frac{1+\pi^2}{2\pi\sqrt{2\pi - \pi^2(-1+\theta) - \theta}},$$

$$\left.\frac{1+\pi^2}{2\pi\sqrt{-2\pi + \theta + \pi^2\theta}}, \frac{1+\pi^2}{\pi\sqrt{-2\pi + \theta + \pi^2\theta}}, \frac{3(1+\pi^2)}{2\pi\sqrt{-2\pi + \theta + \pi^2\theta}}\right\}, \{\theta, -5, 5\}]$$



$$\text{Plot}\left[\left(\frac{3(1+\pi^2)}{2\pi\sqrt{-2\pi + \theta + \pi^2\theta}}\right), \left(\sqrt{9\left(1 - \theta - \frac{\theta}{\pi^2} + \frac{2}{\pi}\right)}\right), \{\theta, -10, 10\}\right]$$

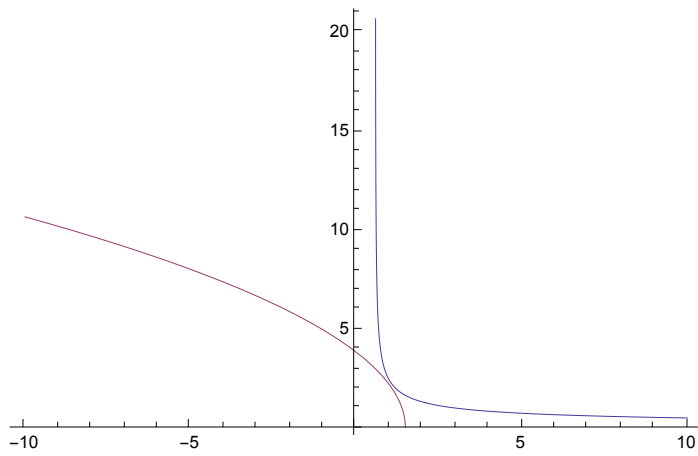
Plot::nonopt: Options expected (instead of  $\{\theta, -10, 10\}$ ) beyond position 2 in

$\text{Plot}\left[\frac{3(1+\pi^2)}{2\pi\sqrt{-2\pi + \theta + \text{Power}[\ll 2 \gg]\theta}}, \sqrt{9\left(1 - \theta - \frac{\theta}{\text{Power}[\ll 2 \gg] + \frac{2}{\pi}}\right)}, \{\theta, -10, 10\}\right]$ . An option must be a rule or a list of rules. >>

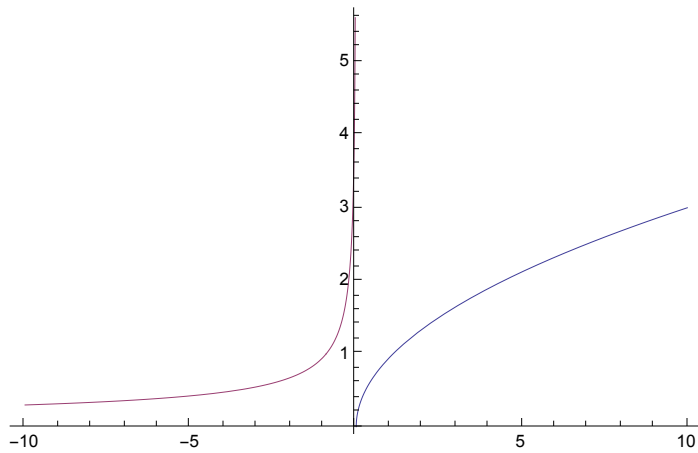
A differential equation of the form  $ax'' + bx' + cx$  can be approximated as the combination of two parametric exponential functions



$$\text{Plot}\left[\left\{\frac{3(1+\pi^2)}{2\pi\sqrt{-2\pi+\theta+\pi^2\theta}}, \sqrt{9\left(1-\theta-\frac{\theta}{\pi^2}+\frac{2}{\pi}\right)}\right\}, \{\theta, -10, 10\}\right]$$



$$\text{Plot}\left[\left\{\sqrt{\theta-\theta/\pi^2}, 1/\sqrt{-\theta-\theta/\pi^2}\right\}, \{\theta, -10, 10\}\right]$$



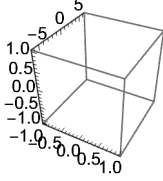
$$\text{Solve}\left[\theta == \frac{2\pi r \sin[\theta]}{\sqrt{4\pi\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\theta]^2}\right) - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\theta]^2}\right)\right)^2}\right]}, \theta\right]$$

{{θ → r}}

$$\frac{r \sqrt{\pi^2 - \text{ArcCos}\left[\frac{\sqrt{1+\text{Cos}[\theta]}}{\sqrt{2}}\right]^2}}{\pi}$$

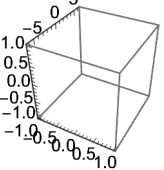
$$\frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}$$

$$\text{ContourPlot3D} \left[ \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \right.} \right. \right. \\ \left. \left. \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} + 8.987551787368176 \cdot 10^{16} (\theta)^2 \right) \right] / \\ \left( \sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2} \right), \{\eta, -1, \\ 1\}, \{\theta, -2 \pi, 2 \pi\}, \{r, -1, 1\} \right]$$

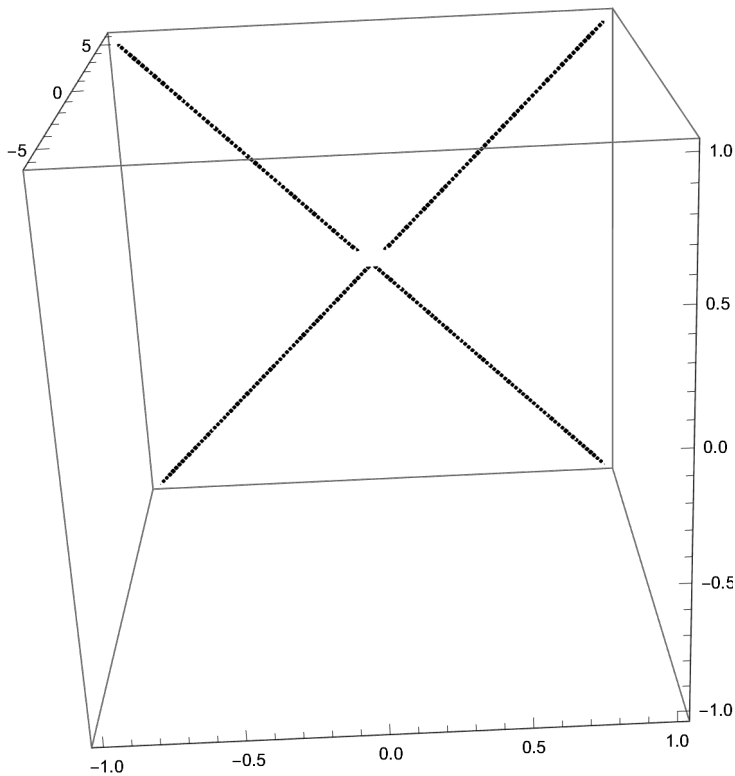
$$\frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}$$


$$\frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}$$

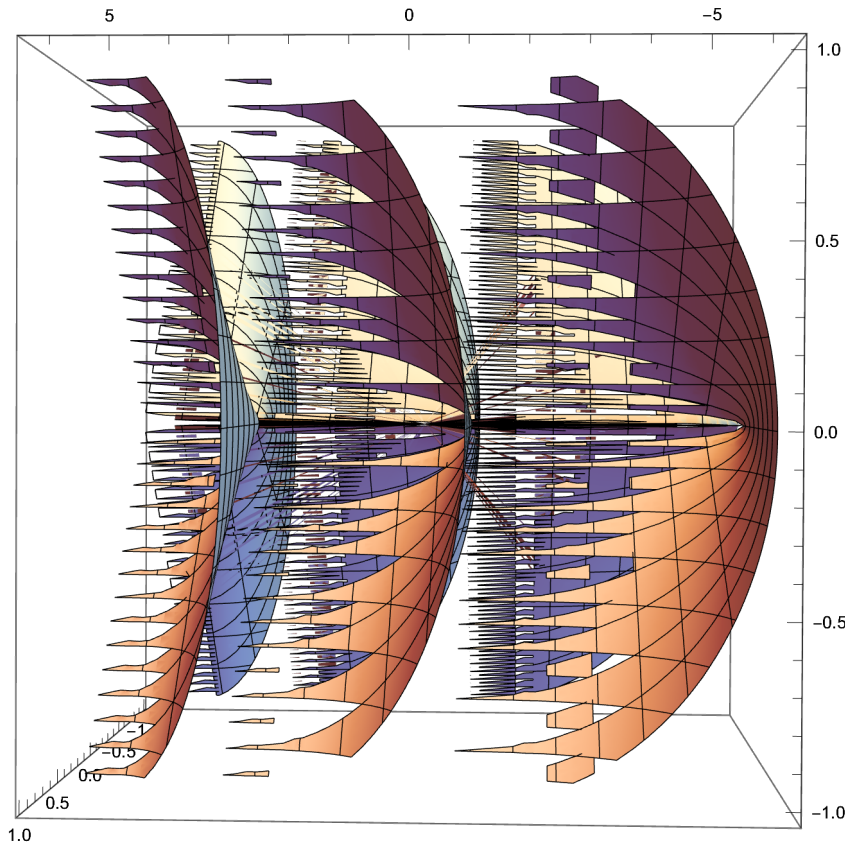
$$\text{ContourPlot3D} \left[ \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + \right.} \right. \right. \\ \left. \left. 8.987551787368176 \cdot 10^{16} (\theta)^2 \right) \right) / \\ \left( \sqrt{39.47841760435743 - 12.566370614359172 \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2} + \theta^2} \right), \\ \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{r, -1, 1\} \right]$$

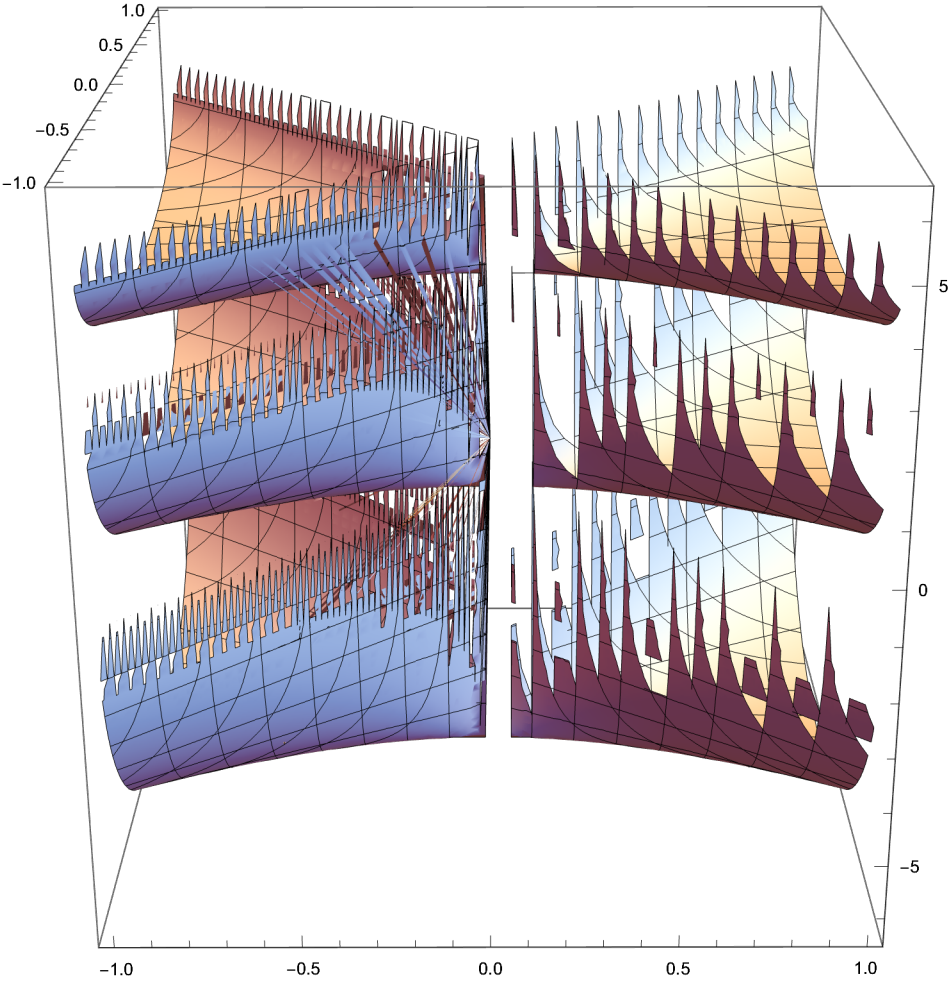
$$6.28319$$


$$\text{ContourPlot3D}\left[\left(\sqrt{\left(3.5481432270250993`^{*18} - 1.1294090667581471`^{*18} \theta + 8.987551787368176`^{*16} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)^2}{r^2}\right)^2\right)}\right) / \left(\sqrt{\left(39.47841760435743` - 12.566370614359172` \theta + \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)^2}{r^2}\right)^2\right)}\right), \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{r, -1, 1\}\right]$$

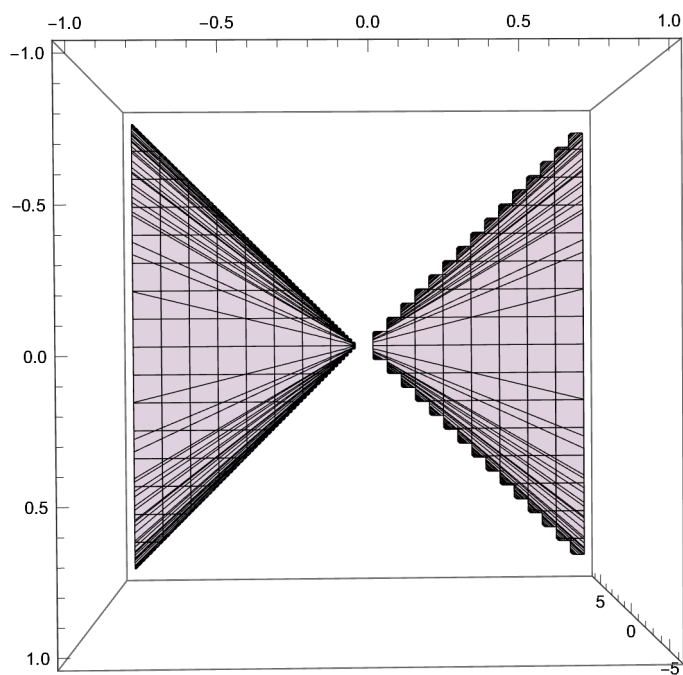


$$\text{ContourPlot3D}\left[\left(\sqrt{\left(3.5481432270250993`^{*18} - 1.1294090667581471`^{*18} \theta + 8.987551787368176`^{*16} (\theta)^2\right)}\right) / \left(\sqrt{\left(39.47841760435743` - 12.566370614359172` \theta + \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)^2}{r^2}\right)^2\right)}\right), \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{r, -1, 1\}\right]$$

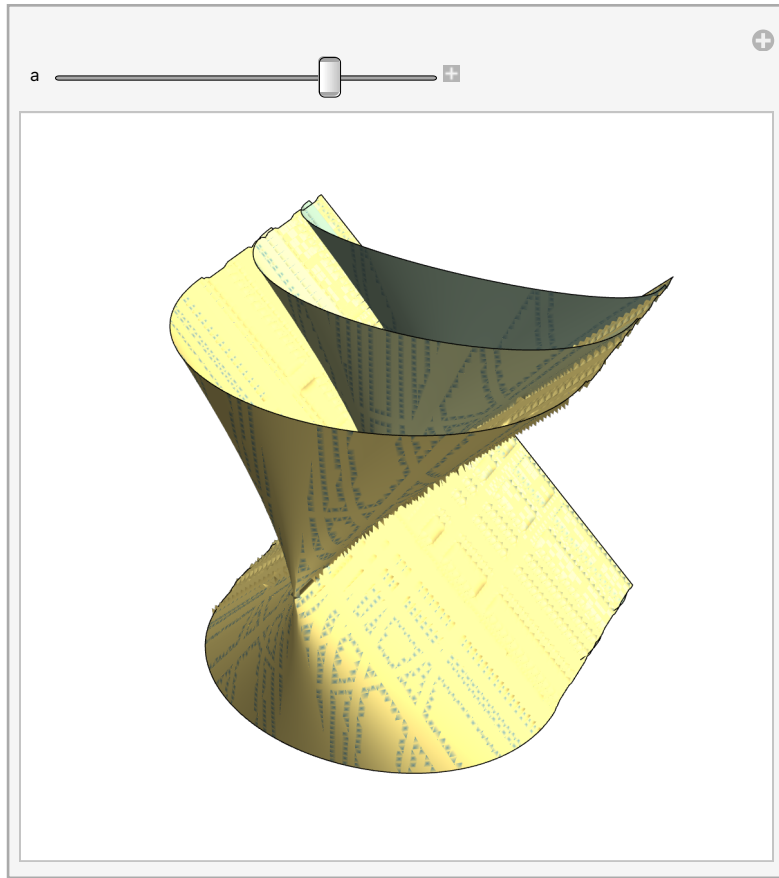




```
ContourPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)^2}{r^2}\right)\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right), \{ \eta, -1, 1\}, \{ \theta, -2 \pi, 2 \pi\}, \{ r, -1, 1\}]$ 
```



```
Manipulate[ContourPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} (\theta)^2\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)^2}{r^2}\right)}\right) + a, \{ \eta, -1, 1\}, \{ \theta, -2 \pi, 2 \pi\}, \{ r, -1, 1\}, \text{Mesh} \rightarrow \text{False}, \text{Boxed} \rightarrow \text{False}, \text{Axes} \rightarrow \text{None}, \text{ColorFunction} \rightarrow \text{"StarryNightColors"}], \{a, 0, 4\}]$ 
```



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

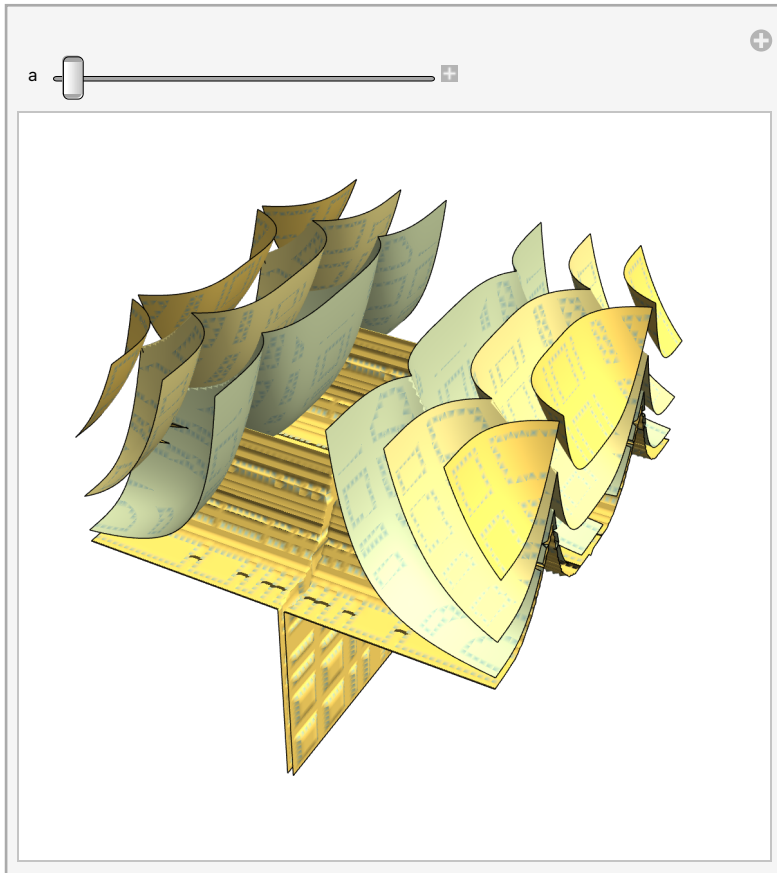
... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

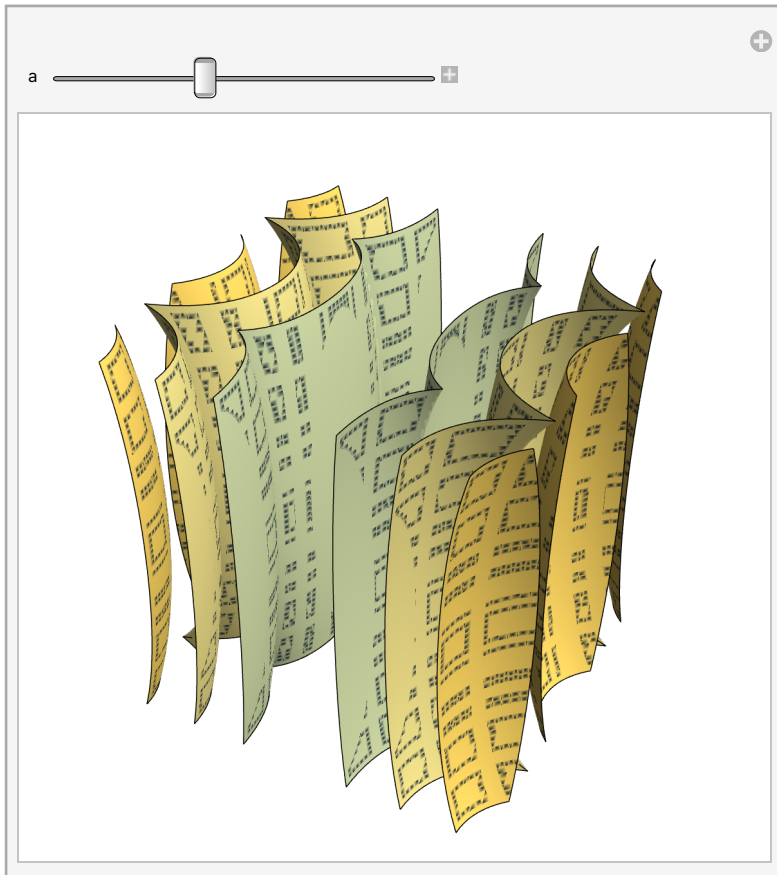
ContourPlot3D $\left[\left\{\frac{\sqrt{4 \pi r^2 \theta - r^2 \left(2 \left(\pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2 \pi}\right\},\right.$   
 $\left.\{r, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$

`Manipulate[ContourPlot3D[ $\frac{\sqrt{4 \pi r^2 \theta - r^2 \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2}}{2 \pi}$  + a,`  
`{r, -1, 1}, {β, -π, π}, {θ, -2 π, 2 π}, Mesh → False, Boxed → False,`  
`Axes → None, ColorFunction → "StarryNightColors"], {a, 0, 4}]`



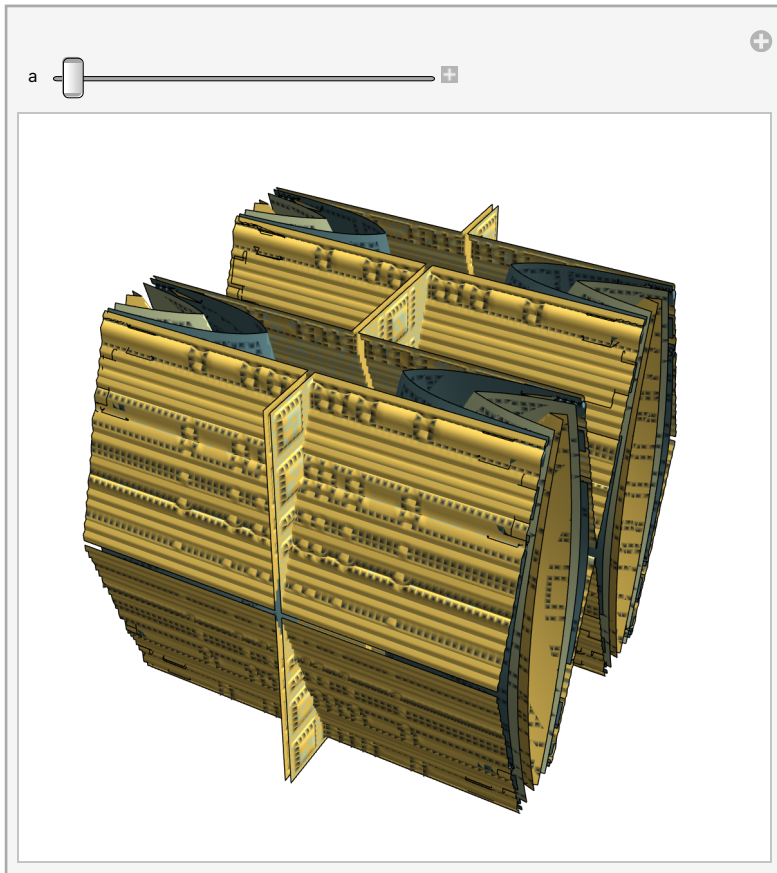


Manipulate[ContourPlot3D[ $\frac{\sqrt{4 \pi r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \theta^2}}{2 \pi} + a,$   
 $\{r, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}, \text{Mesh} \rightarrow \text{False}, \text{Boxed} \rightarrow \text{False},$   
 $\text{Axes} \rightarrow \text{None}, \text{ColorFunction} \rightarrow \text{"StarryNightColors"}], \{a, 0, 4\}]$



Manipulate[ContourPlot3D[ $\frac{\sqrt{4 \pi r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \theta^2}}{2 \pi} + a,$   
 $\{r, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}, \text{Mesh} \rightarrow \text{False}, \text{Boxed} \rightarrow \text{False},$   
 $\text{Axes} \rightarrow \text{None}, \text{ColorFunction} \rightarrow \text{"StarryNightColors"}], \{a, 0, 4\}]$

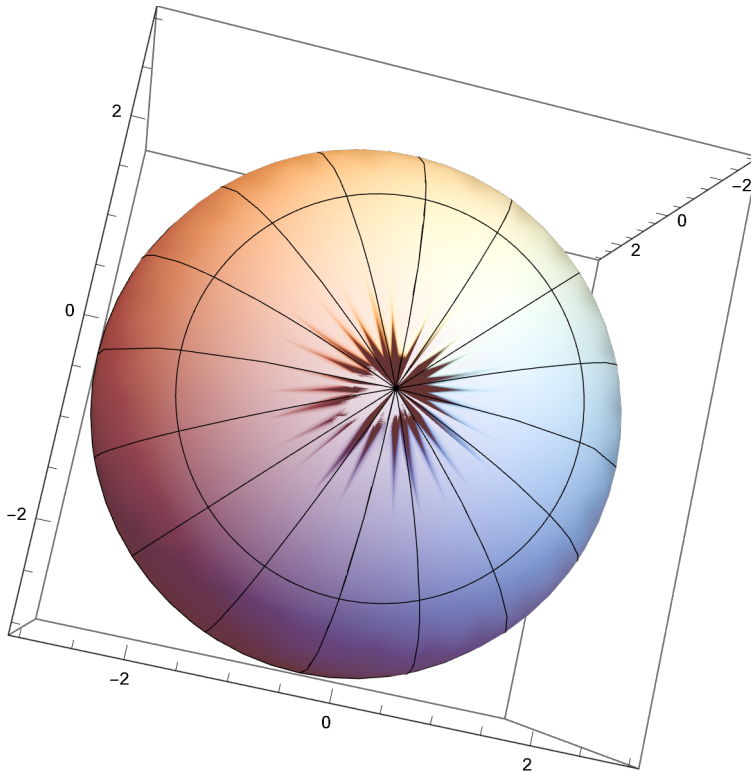
Manipulate[ContourPlot3D[ $\frac{\sqrt{4 \pi r^2 \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \theta^2}}{2 \pi} + a,$   
 $\{r, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}, \text{Mesh} \rightarrow \text{False}, \text{Boxed} \rightarrow \text{False},$   
 $\text{Axes} \rightarrow \text{None}, \text{ColorFunction} \rightarrow \text{"StarryNightColors"}], \{a, 0, 4\}]$



$$\text{ContourPlot3D}\left[\left(\sqrt{\left(-8.478662640222557 \cdot 10^{16} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right) + 6.74710535 \cdot 10^{15} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2 + 2.6636504262789424 \cdot 10^{17} \sin[\beta]^2\right)}\right) / \left(\sqrt{\left(-9.433939159106512 \cdot 10^{15} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right) + 7.50729025 \cdot 10^{14} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2 + 2.9637593956662092 \cdot 10^{16} \sin[\beta]^2\right)}\right)\right],$$

{r, -1, 1}, {η, -1, 1}, {β, -π, π}, Mesh → False, Boxed → False,  
 Axes → None,  
 ColorFunction → "StarryNightColors"]

SphericalPlot3D[(√(-8.478662640222557 · 10<sup>16</sup> θ + 6.74710535 · 10<sup>15</sup> θ<sup>2</sup> + 2.6636504262789424 · 10<sup>17</sup> Sin[β]<sup>2</sup>)) / (√(-9.433939159106512 · 10<sup>15</sup> θ + 7.50729025 · 10<sup>14</sup> θ<sup>2</sup> + 2.9637593956662092 · 10<sup>16</sup> Sin[β]<sup>2</sup>)), {θ, -2 π, 2 π}, {β, -π, π}]



$$-i \operatorname{Log}\left[\cos\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right] + i \operatorname{Sin}\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right]$$

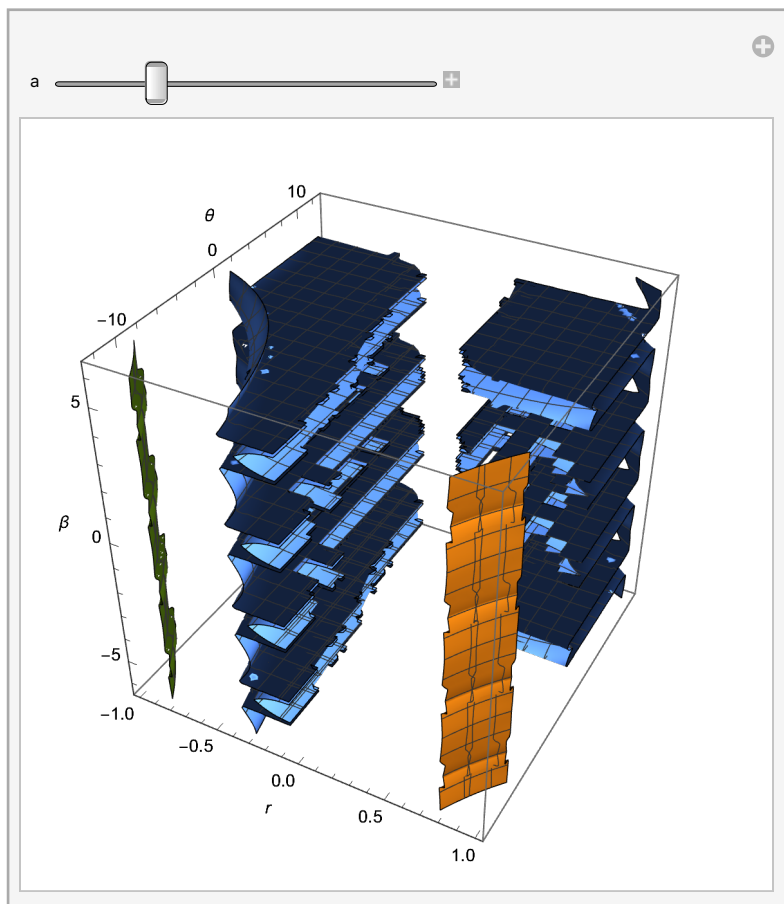
Manipulate[ContourPlot3D[

$$(4/3)\pi \left( \frac{\sqrt{4\pi r^2 \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) - r^2 \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}{2\pi} \right)^3 -$$

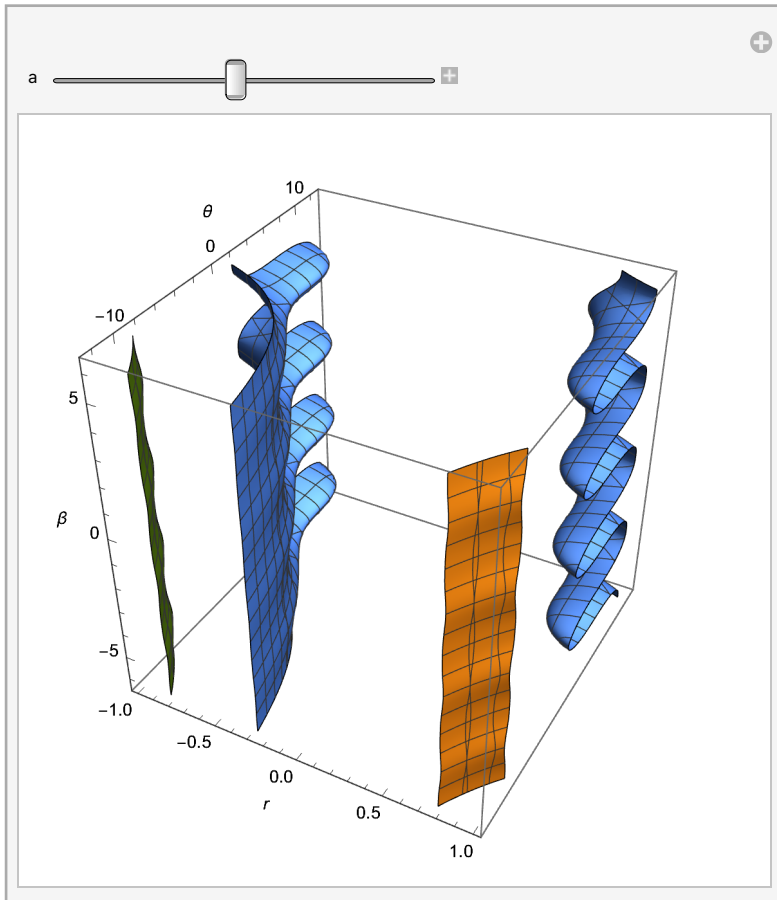
$$(4/3)\pi \left( \frac{2\pi r - r\theta}{2\pi} \right)^3 -$$

$$i \operatorname{Log}\left[\cos\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right] + i \operatorname{Sin}\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right]\right],$$

{r, -1, 1}, {\theta, -4\pi, 4\pi}, {\beta, -2\pi, 2\pi}, AxesLabel → Automatic], {a, 0, 4}]

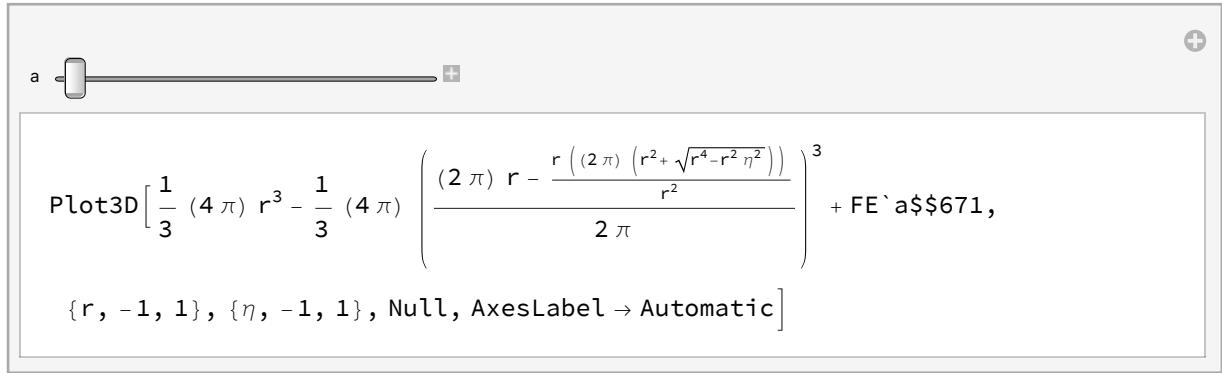


```
Manipulate[ContourPlot3D[
  (4/3) π  $\left( \frac{\sqrt{4 \pi r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2}}{2 \pi} \right)^3 -$ 
  (4/3) π  $\left( \frac{2 \pi r - r \theta}{2 \pi} \right)^3$ , {r, -1, 1}, {θ, -4 π, 4 π},
  {β, -2 π, 2 π}, AxesLabel → Automatic], {a, 0, 4}]
```



```
Plot3D[(4/3) π (r) ^3 - (4/3) π  $\left( \frac{2 \pi r - r \frac{2 \pi \left( r^2 + \sqrt{r^4 - r^2 \eta^2} \right)}{r^2}}{2 \pi} \right)^3,$ 
  {r, -1, 1}, {η, -1, 1}, AxesLabel → Automatic]
```

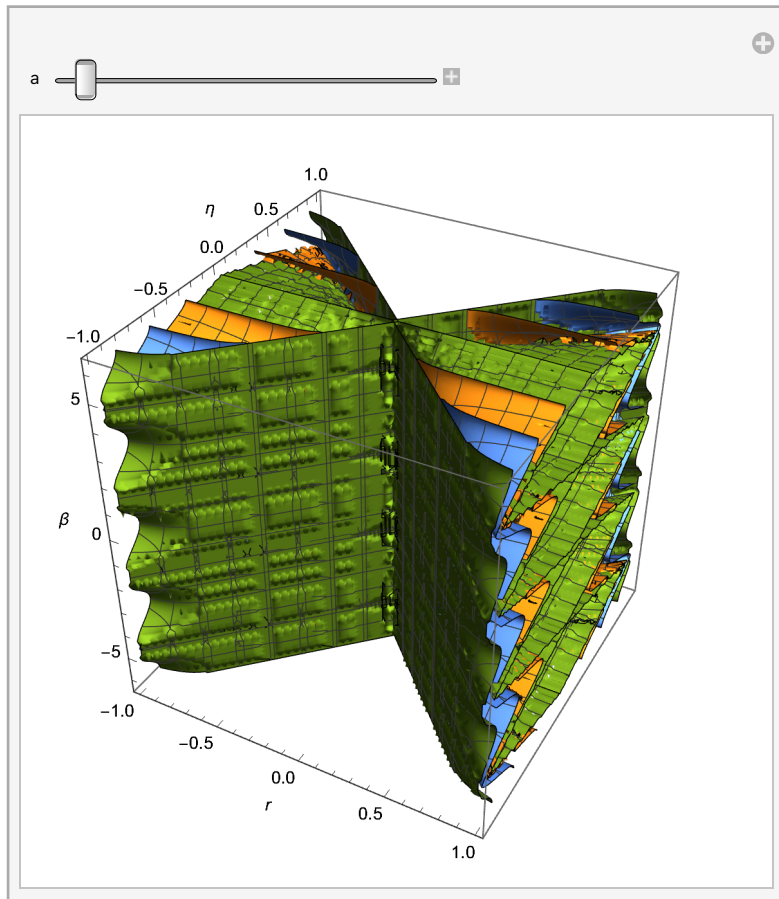
Manipulate[Plot3D[(4/3) π (r)^3 - (4/3) π  $\left( \frac{2 \pi r - r \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}}{2 \pi} \right)^3 + a,$   
 {r, -1, 1}, {η, -1, 1}, , AxesLabel → Automatic], {a, 0, 4}]



Plot3D: Options expected (instead of Null) beyond position 3 in

Plot3D[ $\frac{1}{3} (4 \pi) r^3 - \frac{1}{3} (4 \pi) \left( \frac{\text{Times[<<2>>]} + \text{Times[<<2>>]}}{\text{Times[<<2>>]}} \right)^3 + \text{FE`a} \$\$671,$  {r, -1, 1}, {η, -1, 1}, Null, AxesLabel → Automatic]. An option must be a rule or a list of rules.

Manipulate[ContourPlot3D[ $\frac{\sqrt{4 \pi r^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) - r^2 \left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2}}{2 \pi} + a,$   
 {r, -1, 1}, {η, -1, 1}, {β, -2 π, 2 π}, AxesLabel → Automatic], {a, 0, 4}]



... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **General:** Further output of Infinity::indet will be suppressed during this calculation.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

... **Power:** Infinite expression  $\frac{1}{0.}$  encountered.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

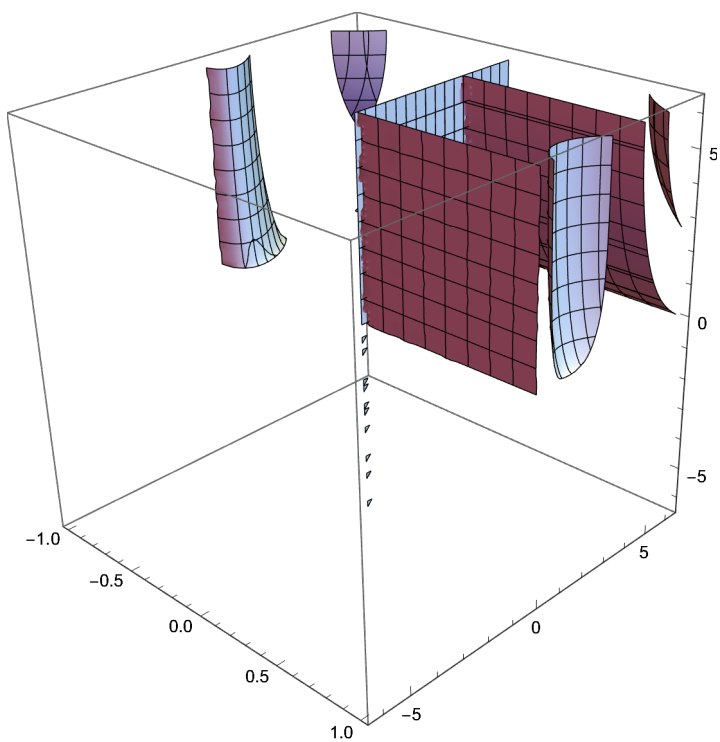
... **Power:** Infinite expression  $\frac{1}{0}$  encountered.

... **General:** Further output of Power::infy will be suppressed during this calculation.

... **Infinity:** Indeterminate expression 0. ComplexInfinity encountered.

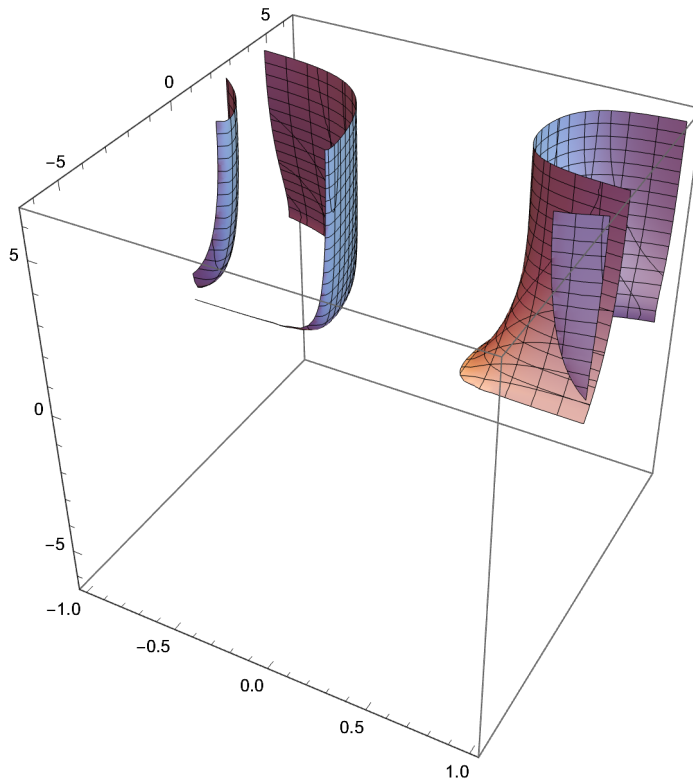
... **General:** Further output of Infinity::indet will be suppressed during this calculation.

ContourPlot3D $\left[\left(\frac{1}{3}\right) \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \pi \left(r - \frac{r \theta}{2 \pi}\right)^2 - \right.$   
 $\left. \left(\frac{1}{3}\right) \frac{r - \frac{r \theta}{2 \pi} \sqrt{4 \pi - \theta_1} \sqrt{\theta_1}}{2 \pi} \pi \left(\sqrt{\left(r - \frac{r \theta}{2 \pi}\right)^2 - \left(\frac{r - \frac{r \theta}{2 \pi} \sqrt{4 \pi - \theta_1} \sqrt{\theta_1}}{2 \pi}\right)^2}\right)^2,\right.$   
 $\left.\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\theta_1, -2 \pi, 2 \pi\}\right]$





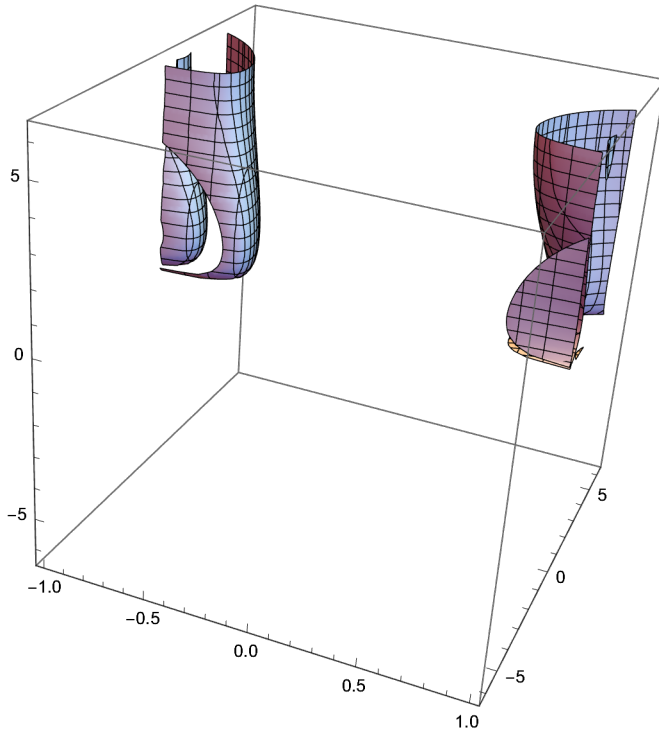
$\text{ContourPlot3D}\left[\left(\frac{1}{3}\right) \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \pi \left(r - \frac{r\theta}{2\pi}\right)^2 - \right.$   
 $\left. \left(\frac{1}{3}\right) \frac{\left(r - \frac{r\theta}{2\pi}\right) \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi} \pi \left(\sqrt{\left(r - \frac{r\theta}{2\pi}\right)^2 - \left(\frac{r - \frac{r\theta}{2\pi} \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi}\right)^2}\right)^2,\right.$   
 $\left.\{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\theta_1, -2\pi, 2\pi\}\right]$



```
ContourPlot3D[(1/3)  $\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \pi \left(r - \frac{r\theta}{2\pi}\right)^2 -$   

 $(1/3) \frac{\left(r - \frac{r\theta}{2\pi}\right) \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi} \pi \left( \sqrt{\left(r - \frac{r\theta}{2\pi}\right)^2 - \left( \frac{\left(r - \frac{r\theta}{2\pi}\right) \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi} \right)^2} \right)^2,$   

{r, -1, 1}, {θ, -2π, 2π}, {θ1, -2π, 2π}]
```



```
Solve[η1 ==  $\frac{r_1 \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi},$ 
```

```
ContourPlot3D[(1/3)  $\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \pi \left(r - \frac{r\theta}{2\pi}\right)^2 -$   

 $(1/3) \frac{r - \frac{r\theta}{2\pi} \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi} \pi \left( \sqrt{\left(r - \frac{r\theta}{2\pi}\right)^2 - \left( \frac{r - \frac{r\theta}{2\pi} \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi} \right)^2} \right)^2,$   

{r, -1, 1}, {θ, -2π, 2π}, {θ1, -2π, 2π}]
```

# No Time, only True

The time variable has helped us so far, but now, we see that there is

only something called true. See the Paper by Parker Emmerson and Andrew Berisha on Unified Theory for an explanation of the origin of the equations used below.

by Parker Emmerson and Andrew Berisha

$$\begin{aligned}
 \text{Solve} \left[ v == \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \right. \\
 \left. \frac{\sqrt{\pi} (4\pi - 2\theta)}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta \right] \\
 \left\{ \left\{ \theta \rightarrow \frac{1}{6} \right. \right. \\
 \left. \left( 12\pi - \sqrt{\left( 144\pi^2 - 12 \left( 9\pi^2 + \frac{3}{2} \sqrt{\left( 36\pi^4 - \frac{8(\pi + 12\pi^4 v^2)}{3v^2} + (16 \times 2^{1/3} \pi^2 (1 + 144\pi^3 v^2)) \right) \right) / \left( 3v^2 (128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \right. \right. \right. \right. \\
 \left. \left. \left. \sqrt{(-226492416\pi^{12} v^4 - 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8)} \right)^{1/3} \right) + \frac{1}{3 \times 2^{1/3} v^2} \right. \right. \\
 \left. \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416\pi^{12} v^4 - 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8)} \right)^{1/3} \right) - \\
 \left. \frac{3}{2} \sqrt{\left( 72\pi^4 - \frac{16(\pi + 12\pi^4 v^2)}{3v^2} - (16 \times 2^{1/3} \pi^2 (1 + 144\pi^3 v^2)) \right) / \left( 3v^2 (128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \right. \right. \\
 \left. \left. \sqrt{(-226492416\pi^{12} v^4 - 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8)} \right)^{1/3} \right) - \frac{1}{3 \times 2^{1/3} v^2} \right. \\
 \left. \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416\pi^{12} v^4 - 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8)} \right)^{1/3} - \right. \\
 \left. \left( -1728\pi^6 + \frac{192\pi^2 (\pi + 12\pi^4 v^2)}{v^2} - \frac{256(-\pi^3 + 2\pi^6 v^2)}{v^2} \right) / \right. \\
 \left. \left( 4 \sqrt{\left( 36\pi^4 - \frac{8(\pi + 12\pi^4 v^2)}{3v^2} + (16 \times 2^{1/3} \pi^2 (1 + 144\pi^3 v^2)) \right) / \right. \right.
 \end{aligned}
 \tag{228}$$

[illegible]

$$\frac{1}{3 \times 2^{1/3} v^2} \left( 128 \pi^3 + 27\,648 \pi^6 v^2 + 110\,592 \pi^9 v^4 + \sqrt{\left(-226\,492\,416 \pi^{12} v^4 - 42\,807\,066\,624 \pi^{15} v^6 + 12\,230\,590\,464 \pi^{18} v^8\right)}^{1/3}\right) \Bigg)\Bigg)\Bigg)\Bigg)\Bigg)\Bigg)\Bigg)\Bigg)\Bigg)\Bigg)\Bigg),$$

$$\begin{aligned} \left\{ \theta \rightarrow \frac{1}{6} \left( 12 \pi - \sqrt{\left( 144 \pi^2 - 12 \left( 9 \pi^2 + \frac{3}{2} \sqrt{\left( 36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2} + \right. \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \left( 16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2) \right) \right) \right) \right) \right) \right) \right) \left( 3 v^2 \left( 128 \pi^3 + 27 648 \pi^6 v^2 + \right. \right. \\ \left. \left. 110 592 \pi^9 v^4 + \sqrt{\left( -226 492 416 \pi^{12} v^4 - 42 807 066 624 \right. \right. \right. \\ \left. \left. \left. \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8 \right) \right)^{1/3}} + \frac{1}{3 \times 2^{1/3} v^2} \right. \\ \left. \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{\left( -226 492 416 \pi^{12} v^4 - \right. \right. \right. \\ \left. \left. \left. 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8 \right) \right)^{1/3}} \right) \right) + \\ \frac{3}{2} \sqrt{\left( 72 \pi^4 - \frac{16 (\pi + 12 \pi^4 v^2)}{3 v^2} - \left( 16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2) \right) \right) \left( 3 v^2 \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \right. \right. \\ \left. \left. \sqrt{\left( -226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + \right. \right. \right. \\ \left. \left. \left. 12 230 590 464 \pi^{18} v^8 \right) \right)^{1/3}} - \frac{1}{3 \times 2^{1/3} v^2} \right. \\ \left. \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{\left( -226 492 416 \pi^{12} \right. \right. \right. \\ \left. \left. \left. v^4 - 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8 \right) \right)^{1/3}} - \right. \\ \left. \left( -1728 \pi^6 + \frac{192 \pi^2 (\pi + 12 \pi^4 v^2)}{v^2} - \frac{256 (-\pi^3 + 2 \pi^6 v^2)}{v^2} \right) \right) \left( 4 \sqrt{\left( 36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2} + \left( 16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2) \right) \right) \left( 3 v^2 \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \right. \right. \right. \\ \left. \left. \sqrt{\left( -226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + \right. \right. \right. \\ \left. \left. \left. 12 230 590 464 \pi^{18} v^8 \right) \right)^{1/3}} \right) + \\ \frac{1}{3 \times 2^{1/3} v^2} \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \right. \\ \left. \sqrt{\left( -226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + \right. \right. \end{aligned}$$

$$\left\{ \theta \rightarrow \frac{1}{6} \left( 12 \pi - \sqrt{144 \pi^2 + 12 \left( -9 \pi^2 + \frac{3}{2} \sqrt{36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2}} \right)} \right) \right.$$



[illegible]

$$\left\{ \Theta \rightarrow \frac{1}{6} \left( 12 \pi - \sqrt{144 \pi^2 + 12 \left( -9 \pi^2 + \frac{3}{2} \sqrt{36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2} + \right.} \right. \right. \\ \left. \left. \left( 16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2) \right) \right) / \left( 3 v^2 (128 \pi^3 + 27 648 \pi^6 v^2 + \right. \right. \\ \left. \left. 110 592 \pi^9 v^4 + \sqrt{-226 492 416 \pi^{12} v^4 - \right.} \right. \\ \left. \left. 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8) \right)^{1/3} \right) + \\ \frac{1}{3 \times 2^{1/3} v^2} \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \right.$$



$$\begin{aligned}
 & \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - 42\,807\,066\,624\,\pi^{15}\,v^6 + \right. \\
 & \quad \left. 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}} + \\
 & \frac{3}{2} \sqrt{\left(72\,\pi^4 - \frac{16\left(\pi + 12\,\pi^4\,v^2\right)}{3\,v^2} - \left(16 \times 2^{1/3}\,\pi^2\left(1 + 144\,\pi^3\,v^2\right)\right) / \right. \\
 & \quad \left(3\,v^2\left(128\,\pi^3 + 27\,648\,\pi^6\,v^2 + 110\,592\,\pi^9\,v^4 + \right. \right. \\
 & \quad \left. \left. \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - 42\,807\,066\,624\,\pi^{15}\,v^6 + \right. \right. \right. \\
 & \quad \left. \left. \left. 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}\right) - \frac{1}{3 \times 2^{1/3}\,v^2} \right. \\
 & \quad \left. \left(128\,\pi^3 + 27\,648\,\pi^6\,v^2 + 110\,592\,\pi^9\,v^4 + \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - \right. \right. \right. \\
 & \quad \left. \left. \left. 42\,807\,066\,624\,\pi^{15}\,v^6 + 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}\right) \right)^{1/3} + \\
 & \quad \left(-1728\,\pi^6 + \frac{192\,\pi^2\left(\pi + 12\,\pi^4\,v^2\right)}{v^2} - \frac{256\left(-\pi^3 + 2\,\pi^6\,v^2\right)}{v^2}\right) / \\
 & \quad \left(4 \sqrt{\left(36\,\pi^4 - \frac{8\left(\pi + 12\,\pi^4\,v^2\right)}{3\,v^2} + \left(16 \times 2^{1/3}\,\pi^2\left(1 + 144\,\pi^3\,v^2\right)\right) / \right. \right. \\
 & \quad \left. \left(3\,v^2\left(128\,\pi^3 + 27\,648\,\pi^6\,v^2 + 110\,592\,\pi^9\,v^4 + \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - 42\,807\,066\,624\,\pi^{15}\,v^6 + \right. \right. \right. \\
 & \quad \left. \left. \left. 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}\right) \right)^{1/3}} + \\
 & \quad \frac{1}{3 \times 2^{1/3}\,v^2} \left(128\,\pi^3 + 27\,648\,\pi^6\,v^2 + 110\,592\,\pi^9\,v^4 + \right. \\
 & \quad \left. \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - 42\,807\,066\,624\,\pi^{15}\,v^6 + \right. \right. \\
 & \quad \left. \left. 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}} \right) \Bigg\}, \\
 & \left\{\theta \rightarrow \frac{1}{6} \left(12\,\pi + \sqrt{\left(144\,\pi^2 + 12\left(-9\,\pi^2 + \frac{3}{2} \sqrt{\left(36\,\pi^4 - \frac{8\left(\pi + 12\,\pi^4\,v^2\right)}{3\,v^2} + \right. \right. \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left(16 \times 2^{1/3}\,\pi^2\left(1 + 144\,\pi^3\,v^2\right)\right) / \left(3\,v^2\left(128\,\pi^3 + 27\,648\,\pi^6\,v^2 + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 110\,592\,\pi^9\,v^4 + \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. 42\,807\,066\,624\,\pi^{15}\,v^6 + 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}\right) \right)^{1/3}} + \right. \\
 & \quad \left. \frac{1}{3 \times 2^{1/3}\,v^2} \left(128\,\pi^3 + 27\,648\,\pi^6\,v^2 + 110\,592\,\pi^9\,v^4 + \right. \right. \\
 & \quad \left. \left. \sqrt{\left(-226\,492\,416\,\pi^{12}\,v^4 - 42\,807\,066\,624\,\pi^{15}\,v^6 + \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. 12\,230\,590\,464\,\pi^{18}\,v^8\right)^{1/3}\right) \right)^{1/3}} \right\},
 \end{aligned}$$

[illegible]







$$\left. \begin{aligned} & \left( \frac{1}{6} \sqrt{\frac{1}{3}} \left( 12\pi - \sqrt{\left( 144\pi^2 + 12 \left( -9\pi^2 + \frac{3}{2} \sqrt{\left( 36\pi^4 - \frac{8(\pi + 12\pi^4 v^2)}{3v^2} + \right. \right. \right. \right. \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left( 16 \times 2^{1/3} \pi^2 (1 + 144\pi^3 v^2) \right) \right) / \right. \\ & \quad \left. \left( 3v^2 \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416\pi^{12} v^4 - \right. \right. \right. \\ & \quad \left. \left. \left. 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8) \right)^{1/3} \right) + \right. \\ & \quad \left. \frac{1}{3 \times 2^{1/3} v^2} \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416 \right. \right. \\ & \quad \left. \left. \pi^{12} v^4 - 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8) \right)^{1/3} \right) - \\ & \quad \frac{3}{2} \sqrt{\left( 72\pi^4 - \frac{16(\pi + 12\pi^4 v^2)}{3v^2} - \left( 16 \times 2^{1/3} \pi^2 (1 + 144\pi^3 v^2) \right) / \right. \\ & \quad \left. \left( 3v^2 \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416\pi^{12} v^4 - \right. \right. \right. \\ & \quad \left. \left. \left. 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8) \right)^{1/3} \right) - \right. \\ & \quad \left. \frac{1}{3 \times 2^{1/3} v^2} \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416 \right. \right. \\ & \quad \left. \left. \pi^{12} v^4 - 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8) \right)^{1/3} + \right. \\ & \quad \left. \left( -1728\pi^6 + \frac{192\pi^2 (\pi + 12\pi^4 v^2)}{v^2} - \frac{256 (-\pi^3 + 2\pi^6 v^2)}{v^2} \right) / \right. \\ & \quad \left( 4 \sqrt{\left( 36\pi^4 - \frac{8(\pi + 12\pi^4 v^2)}{3v^2} + \left( 16 \times 2^{1/3} \pi^2 (1 + 144\pi^3 v^2) \right) / \right. \right. \\ & \quad \left. \left. \left( 3v^2 \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416\pi^{12} v^4 - \right. \right. \right. \right. \\ & \quad \left. \left. \left. 42807066624\pi^{15} v^6 + 12230590464\pi^{18} v^8) \right)^{1/3} \right) + \right. \\ & \quad \left. \frac{1}{3 \times 2^{1/3} v^2} \left( 128\pi^3 + 27648\pi^6 v^2 + 110592\pi^9 v^4 + \sqrt{(-226492416\pi^{12} v^4 - \right. \right. \\ & \quad \left. \left. 42807066624\pi^{15} v^6 + \right. \right. \\ & \quad \left. \left. \left. 12230590464\pi^{18} v^8) \right)^{1/3} \right) \right) \right) \right) \right) \right) \Bigg\}, \end{aligned} \right.$$



$$\begin{aligned} & \frac{3}{2} \sqrt{\left(72 \pi^4 - \frac{16 (\pi + 12 \pi^4 v^2)}{3 v^2} - (16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2))\right) /} \\ & \left(3 v^2 \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - \right. \right. \\ & \quad \left. \left. 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)\right)^{1/3}\right) - \\ & \frac{1}{3 \times 2^{1/3} v^2} \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \right. \\ & \quad \left. \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)\right)^{1/3} + \\ & \left(-1728 \pi^6 + \frac{192 \pi^2 (\pi + 12 \pi^4 v^2)}{v^2} - \frac{256 (-\pi^3 + 2 \pi^6 v^2)}{v^2}\right) / \\ & \left(4 \sqrt{\left(36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2} + (16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2))\right) /} \right. \\ & \quad \left. \left(3 v^2 \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - \right. \right. \right. \\ & \quad \left. \left. 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)\right)^{1/3}\right) + \\ & \quad \left. \frac{1}{3 \times 2^{1/3} v^2} \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \right. \right. \\ & \quad \left. \left. \sqrt{(-226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + \right. \right. \\ & \quad \left. \left. 12 230 590 464 \pi^{18} v^8)\right)^{1/3}\right)\right)\right)\right)\right)\right\}, \\ \{\theta \rightarrow & \frac{1}{6} \left(12 \pi + \sqrt{\left(144 \pi^2 + 12 \left(-9 \pi^2 + \frac{3}{2} \sqrt{\left(36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2} + \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left(16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2)\right) / \right. \right. \\ & \quad \left. \left. \left(3 v^2 \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - \right. \right. \right. \right. \right. \\ & \quad \left. \left. 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)\right)^{1/3}\right) + \\ & \quad \left. \frac{1}{3 \times 2^{1/3} v^2} \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \right. \right. \right. \\ & \quad \left. \left. \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)\right)^{1/3}\right) + \\ & \quad \left. \frac{3}{2} \sqrt{\left(72 \pi^4 - \frac{16 (\pi + 12 \pi^4 v^2)}{3 v^2} - (16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2))\right) /} \right. \\ & \quad \left. \left(3 v^2 \left(128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - \right. \right. \right. \right. \right. \\ & \quad \left. \left. 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)\right)^{1/3}\right) - \end{aligned}$$

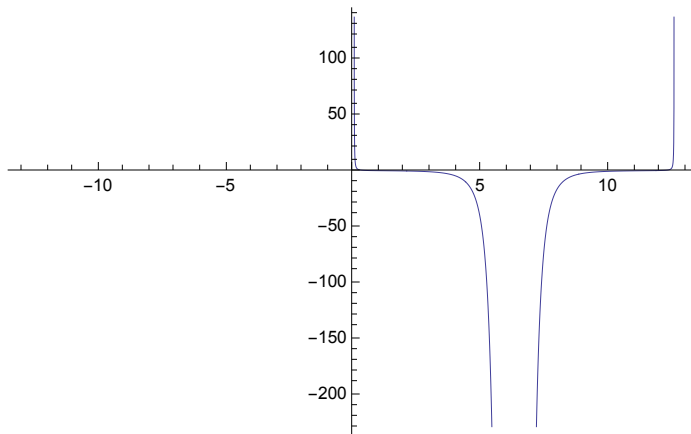


$$\begin{aligned}
& \frac{1}{3 \times 2^{1/3} v^2} \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)} \right)^{1/3} + \\
& \left( -1728 \pi^6 + \frac{192 \pi^2 (\pi + 12 \pi^4 v^2)}{v^2} - \frac{256 (-\pi^3 + 2 \pi^6 v^2)}{v^2} \right) / \\
& \left( 4 \sqrt{36 \pi^4 - \frac{8 (\pi + 12 \pi^4 v^2)}{3 v^2} + (16 \times 2^{1/3} \pi^2 (1 + 144 \pi^3 v^2))} \right) / \\
& \left( 3 v^2 \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)} \right)^{1/3} \right) + \\
& \frac{1}{3 \times 2^{1/3} v^2} \left( 128 \pi^3 + 27 648 \pi^6 v^2 + 110 592 \pi^9 v^4 + \sqrt{(-226 492 416 \pi^{12} v^4 - 42 807 066 624 \pi^{15} v^6 + 12 230 590 464 \pi^{18} v^8)} \right)^{1/3} \Bigg\} \\
& D \left[ - \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \right. \\
& \quad \left. \frac{\sqrt{\pi} (4 \pi - 2 \theta)}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right], \theta] \\
& \text{Simplify} \left[ \frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \right. \\
& \quad \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} - \\
& \quad \left. \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right] \\
& - \frac{4 \sqrt{\pi} (8 \pi^4 - 40 \pi^3 \theta - 6 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4)}{((4 \pi - \theta) \theta)^{3/2} (-2 \pi + \theta)^2 \sqrt{(-2 \pi + \theta)^4}}
\end{aligned}$$

$$\text{Simplify} \left[ -\frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} + \right. \\
\frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
\frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
\frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} + \\
\left. \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right]$$

$$\frac{4 \sqrt{\pi} (8 \pi^4 - 40 \pi^3 \theta - 6 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4)}{((4 \pi - \theta) \theta)^{3/2} (-2 \pi + \theta)^2 \sqrt{(-2 \pi + \theta)^4}}$$

$$\text{Plot} \left[ \frac{4 \sqrt{\pi} (8 \pi^4 - 40 \pi^3 \theta - 6 \pi^2 \theta^2 + 8 \pi \theta^3 - \theta^4)}{((4 \pi - \theta) \theta)^{3/2} (-2 \pi + \theta)^2 \sqrt{(-2 \pi + \theta)^4}}, \{\theta, -13, 13\} \right]$$



This is the inverse of true, and can be simplified in terms of time.

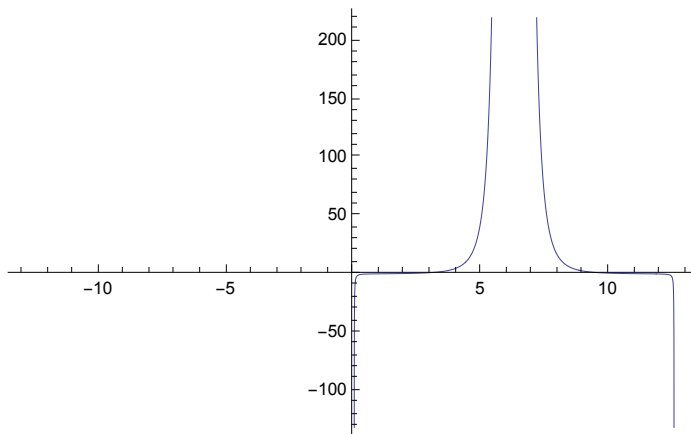
$$\text{Solve}\left[a == \frac{4\sqrt{\pi}(8\pi^4 - 40\pi^3\theta - 6\pi^2\theta^2 + 8\pi\theta^3 - \theta^4)}{(4\pi - \theta)\theta^{3/2}(-2\pi + \theta)^2\sqrt{(-2\pi + \theta)^4}}, \theta\right]$$
$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 1])}, \right. \right. \\ & \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 1])}, \right. \\ & \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 2])}, \right. \\ & \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 2])}, \right. \\ & \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 3])}, \right. \\ & \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 3])}, \right. \\ & \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 4])}, \right. \\ & \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 4])}, \right. \\ & \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 5])}, \right. \\ & \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 5])}, \right. \\ & \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 6])}, \right. \\ & \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 6])}, \right. \\ & \left\{ \theta \rightarrow 2\pi - \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 7])}, \right. \\ & \left. \left. \left\{ \theta \rightarrow 2\pi + \sqrt{(4\pi^2 + \text{Root}[1024\pi^9 + 2560\pi^7\#1 + 1344\pi^5\#1^2 + (-320\pi^3 + 256a^2\pi^8)\#1^3 + (16\pi + 256a^2\pi^6)\#1^4 + 96a^2\pi^4\#1^5 + 16a^2\pi^2\#1^6 + a^2\#1^7 \&, 7])} \right\} \right\} \end{aligned}$$

$$\text{Simplify}\left[\frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} - \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \theta\right]$$

$$- \frac{4 \sqrt{\pi} (8 \pi^4 - 40 \pi^3 \text{True} - 6 \pi^2 \text{True}^2 + 8 \pi \text{True}^3 - \text{True}^4)}{((4 \pi - \text{True}) \text{True})^{3/2} (-2 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}}$$

$$\text{Plot}\left[- \frac{4 \sqrt{\pi} (8 \pi^4 - 40 \pi^3 \text{True} - 6 \pi^2 \text{True}^2 + 8 \pi \text{True}^3 - \text{True}^4)}{((4 \pi - \text{True}) \text{True})^{3/2} (-2 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}}, \{\text{True}, -13, 13\}\right]$$

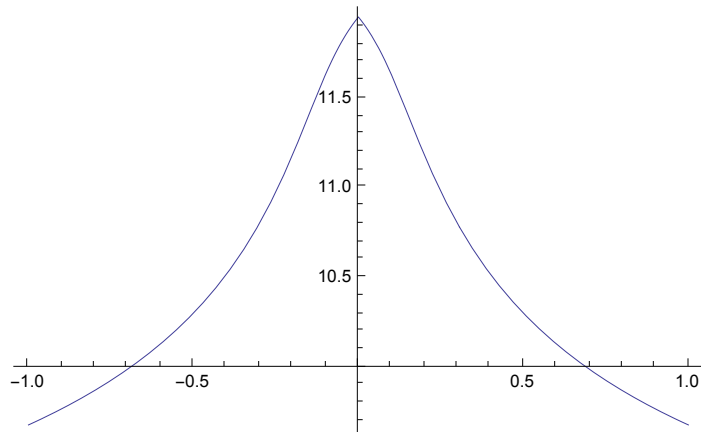
(231)



[illegible]

Plot[2  $\pi$  +

$$\sqrt{4 \pi^2 + \text{Root}\left[1024 \pi^9 + 2560 \pi^7 \#1 + 1344 \pi^5 \#1^2 + (-320 \pi^3 + 256 a^2 \pi^8) \#1^3 + (16 \pi + 256 a^2 \pi^6) \#1^4 + 96 a^2 \pi^4 \#1^5 + 16 a^2 \pi^2 \#1^6 + a^2 \#1^7 \&, 2\right]}, \{a, -1, 1\}]$$



SymbolName[True]

True

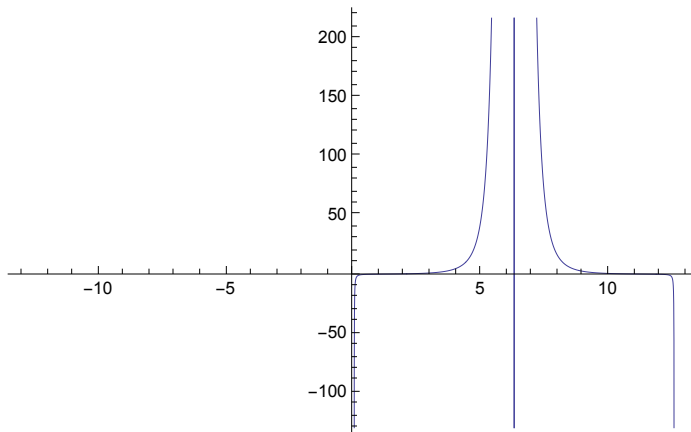
Solve[Pi  $\in$  Algebraics]

Solve[Algebraics  $\pi$

$$\text{Root}\left[-64 \pi^3 + (48 \pi^2 + 16 \pi^8) \#1 + (-12 \pi - 32 \pi^7) \#1^2 + (1 + 24 \pi^6) \#1^3 - 8 \pi^5 \#1^4 + \pi^4 \#1^5 \&, 3\right]$$

In terms of true, there is no asymptote at 2  $\pi$ .

$$\text{Plot}\left[\frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} - \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \{\theta, -13, 13\}\right]$$



For terms of time, there is an asymptote at  $2 \pi$ .

THIS MEANS THAT THERE IS NO SUCH THING AS TIME, THERE IS ONLY TRUE! And the truth is that the rest of the equations plot emptiness. This is the only one that gives us a graph.

There are only trues,

and time is the inverse of true. Time is false, time is illusion

(232)

**Disprove Nietzsche multiply by 0, but keep everything solid**

$$\begin{aligned}
& \frac{1}{6} D \left[ \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \right. \\
& \quad \left. \frac{\sqrt{\pi} (4\pi - 2\theta)}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}}, \theta \right] \\
& \frac{1}{6} \left( - \frac{3 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} + \right. \\
& \quad \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} + \\
& \quad \left. \frac{2 \sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right) \\
& \text{Simplify} \left[ \frac{1}{6} \left( - \frac{3 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} + \right. \right. \\
& \quad \frac{\sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2)}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{\sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{\sqrt{\pi} (4\pi - 2\theta)^2}{2 (4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} + \\
& \quad \left. \left. \frac{2 \sqrt{\pi}}{\sqrt{4\pi\theta - \theta^2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right) \right] \\
& \frac{2 \sqrt{\pi} (8\pi^4 - 40\pi^3\theta - 6\pi^2\theta^2 + 8\pi\theta^3 - \theta^4)}{3 ((4\pi - \theta)\theta)^{3/2} (-2\pi + \theta)^2 \sqrt{(-2\pi + \theta)^4}}
\end{aligned}$$



[illegible]

$$\begin{aligned}
& \frac{1}{6} \times \frac{1}{6} D \left[ - \frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} + \right. \\
& \quad \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} + \\
& \quad \left. \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right], \theta] \\
& \frac{1}{36} \left( \frac{15 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^3}{4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{7/2}} - \right. \\
& \quad \frac{9 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \\
& \quad \frac{9 \sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{4 \sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} + \\
& \quad \frac{\sqrt{\pi} (-48 \pi + 24 \theta) \sqrt{4 \pi \theta - \theta^2}}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{3 \sqrt{\pi} (4 \pi - 2 \theta) (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{2 \sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{3 \sqrt{\pi} (4 \pi - 2 \theta)^2 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{4 (4 \pi \theta - \theta^2)^{3/2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{3 \sqrt{\pi} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{3 \sqrt{\pi} (4 \pi - 2 \theta)^3}{4 (4 \pi \theta - \theta^2)^{5/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} - \\
& \quad \left. \frac{3 \sqrt{\pi} (4 \pi - 2 \theta)}{(4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} \right)
\end{aligned}$$

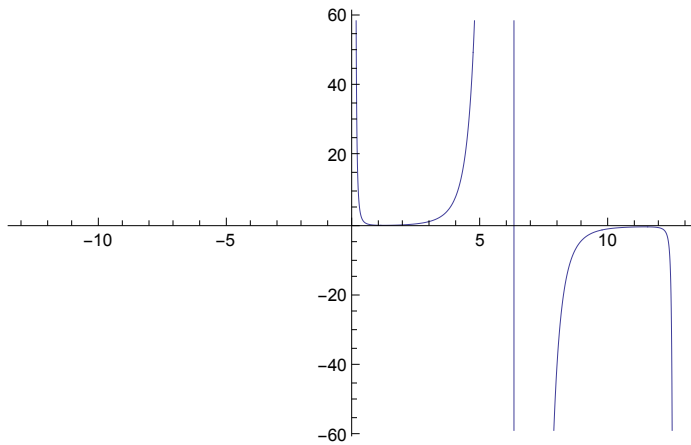
$$\begin{aligned}
& \text{Simplify} \left[ \frac{1}{36} \left( \frac{15 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^3}{4 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{7/2}} - \right. \right. \\
& \quad \left( 9 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3) \right) / \\
& \quad \left( 2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2} \right) - \\
& \quad \frac{9 \sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{4 \sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} + \\
& \quad \frac{\sqrt{\pi} (-48\pi + 24\theta) \sqrt{4\pi\theta - \theta^2}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \quad \frac{3 \sqrt{\pi} (4\pi - 2\theta) (48\pi^2 - 48\pi\theta + 12\theta^2)}{2 \sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{3 \sqrt{\pi} (4\pi - 2\theta)^2 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{4 (4\pi\theta - \theta^2)^{3/2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{3 \sqrt{\pi} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{3 \sqrt{\pi} (4\pi - 2\theta)^3}{4 (4\pi\theta - \theta^2)^{5/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} - \\
& \quad \left. \frac{3 \sqrt{\pi} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right] \\
& \frac{\sqrt{\pi} (-32\pi^6 + 128\pi^5\theta - 320\pi^4\theta^2 + 80\pi^3\theta^3 + 30\pi^2\theta^4 - 12\pi\theta^5 + \theta^6)}{3 (2\pi - \theta)^3 \theta^2 \sqrt{(4\pi - \theta)\theta} (-4\pi + \theta)^2 \sqrt{(-2\pi + \theta)^4}}
\end{aligned}$$

$$\begin{aligned}
& D \left[ \frac{3 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \right. \\
& \quad \frac{\sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{\sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \quad \frac{\sqrt{\pi} (4 \pi - 2 \theta)^2}{2 (4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} - \\
& \quad \left. \frac{2 \sqrt{\pi}}{\sqrt{4 \pi \theta - \theta^2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}, \theta \right] \\
& - \frac{15 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^3}{4 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{7/2}} + \\
& \frac{9 \sqrt{\pi} \sqrt{4 \pi \theta - \theta^2} (48 \pi^2 - 48 \pi \theta + 12 \theta^2) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{2 (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} + \\
& \frac{9 \sqrt{\pi} (4 \pi - 2 \theta) (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)^2}{4 \sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{5/2}} - \\
& \frac{\sqrt{\pi} (-48 \pi + 24 \theta) \sqrt{4 \pi \theta - \theta^2}}{(16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} - \\
& \frac{3 \sqrt{\pi} (4 \pi - 2 \theta) (48 \pi^2 - 48 \pi \theta + 12 \theta^2)}{2 \sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \frac{3 \sqrt{\pi} (4 \pi - 2 \theta)^2 (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{4 (4 \pi \theta - \theta^2)^{3/2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \frac{3 \sqrt{\pi} (-32 \pi^3 + 48 \pi^2 \theta - 24 \pi \theta^2 + 4 \theta^3)}{\sqrt{4 \pi \theta - \theta^2} (16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4)^{3/2}} + \\
& \frac{3 \sqrt{\pi} (4 \pi - 2 \theta)^3}{4 (4 \pi \theta - \theta^2)^{5/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}} + \\
& \frac{3 \sqrt{\pi} (4 \pi - 2 \theta)}{(4 \pi \theta - \theta^2)^{3/2} \sqrt{16 \pi^4 - 32 \pi^3 \theta + 24 \pi^2 \theta^2 - 8 \pi \theta^3 + \theta^4}}
\end{aligned}$$

$$\begin{aligned}
& \text{Simplify} \left[ -\frac{15 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^3}{4 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{7/2}} + \right. \\
& \frac{9 \sqrt{\pi} \sqrt{4\pi\theta - \theta^2} (48\pi^2 - 48\pi\theta + 12\theta^2) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{2 (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} + \\
& \frac{9 \sqrt{\pi} (4\pi - 2\theta) (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)^2}{4 \sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{5/2}} - \\
& \frac{\sqrt{\pi} (-48\pi + 24\theta) \sqrt{4\pi\theta - \theta^2}}{(16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} - \\
& \frac{3 \sqrt{\pi} (4\pi - 2\theta) (48\pi^2 - 48\pi\theta + 12\theta^2)}{2 \sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \frac{3 \sqrt{\pi} (4\pi - 2\theta)^2 (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{4 (4\pi\theta - \theta^2)^{3/2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \frac{3 \sqrt{\pi} (-32\pi^3 + 48\pi^2\theta - 24\pi\theta^2 + 4\theta^3)}{\sqrt{4\pi\theta - \theta^2} (16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4)^{3/2}} + \\
& \frac{3 \sqrt{\pi} (4\pi - 2\theta)^3}{4 (4\pi\theta - \theta^2)^{5/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} + \\
& \left. \frac{3 \sqrt{\pi} (4\pi - 2\theta)}{(4\pi\theta - \theta^2)^{3/2} \sqrt{16\pi^4 - 32\pi^3\theta + 24\pi^2\theta^2 - 8\pi\theta^3 + \theta^4}} \right] \\
& \frac{12 \sqrt{\pi} (32\pi^6 - 128\pi^5\theta + 320\pi^4\theta^2 - 80\pi^3\theta^3 - 30\pi^2\theta^4 + 12\pi\theta^5 - \theta^6)}{(2\pi - \theta)^3 \theta^2 \sqrt{(4\pi - \theta)\theta} (-4\pi + \theta)^2 \sqrt{(-2\pi + \theta)^4}} \\
& \text{D} \left[ -\frac{4 \sqrt{\pi} (8\pi^4 - 40\pi^3 \text{True} - 6\pi^2 \text{True}^2 + 8\pi \text{True}^3 - \text{True}^4)}{((4\pi - \text{True}) \text{True})^{3/2} (-2\pi + \text{True})^2 \sqrt{(-2\pi + \text{True})^4}}, \text{True} \right]
\end{aligned}$$

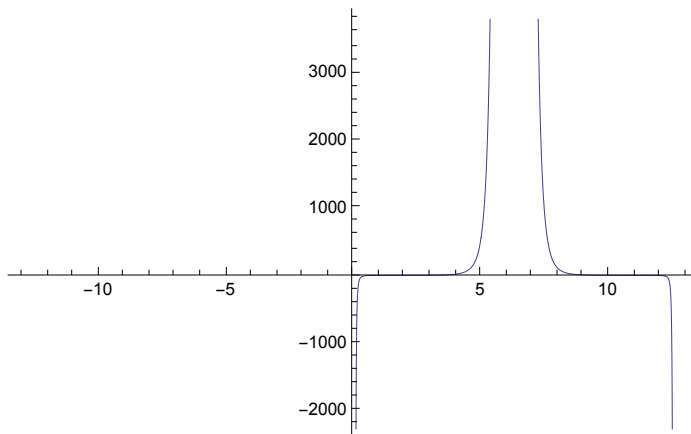
$$\begin{aligned} \text{Simplify} \Big[ & -\frac{4 \sqrt{\pi} (-40 \pi^3 - 12 \pi^2 \text{True} + 24 \pi \text{True}^2 - 4 \text{True}^3)}{((4 \pi - \text{True}) \text{True})^{3/2} (-2 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}} + \\ & \frac{8 \sqrt{\pi} (-2 \pi + \text{True}) (8 \pi^4 - 40 \pi^3 \text{True} - 6 \pi^2 \text{True}^2 + 8 \pi \text{True}^3 - \text{True}^4)}{((4 \pi - \text{True}) \text{True})^{3/2} (-2 \pi + \text{True})^4} + \\ & \frac{8 \sqrt{\pi} (8 \pi^4 - 40 \pi^3 \text{True} - 6 \pi^2 \text{True}^2 + 8 \pi \text{True}^3 - \text{True}^4)}{((4 \pi - \text{True}) \text{True})^{3/2} (-2 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4}} + \\ & \frac{6 \sqrt{\pi} (4 \pi - 2 \text{True}) (8 \pi^4 - 40 \pi^3 \text{True} - 6 \pi^2 \text{True}^2 + 8 \pi \text{True}^3 - \text{True}^4)}{((4 \pi - \text{True}) \text{True})^{5/2} (-2 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}} \Big] \\ & (12 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\ & ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}) \end{aligned}$$

$$\begin{aligned} \text{Plot} \Big[ & (12 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\ & ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}), \{\text{True}, -13, 13\} \Big] \end{aligned}$$



$$\begin{aligned} \text{D} \Big[ & (12 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\ & ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}), \text{True} \Big] \end{aligned}$$

$$\begin{aligned}
& \text{Plot} \left[ \left( 12 \sqrt{\pi} \left( -128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5 \right) \right) / \right. \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad \left( 24 \sqrt{\pi} (-2 \pi + \text{True})^3 \right. \\
& \quad \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2} \right) - \\
& \quad \left. (24 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \right) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad \left( 6 \sqrt{\pi} (4 \pi - 2 \text{True}) \right. \\
& \quad \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad \left. (24 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \right) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \quad \left. (36 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \right) / \\
& \quad \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} \right. \\
& \quad \quad \left. (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right), \{\text{True}, -13, 13\} \Big]
\end{aligned}$$



$$\begin{aligned}
& \left\{ \left\{ o \rightarrow \left( 12 \sqrt{\pi} \left( -128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5 \right) \right) / \right. \right. \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad (24 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \quad \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \left( (-2 \pi + \text{True})^4 \right)^{3/2} \right) - (24 \sqrt{\pi} \\
& \quad \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad (6 \sqrt{\pi} (4 \pi - 2 \text{True}) (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - \\
& \quad \quad 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - (24 \sqrt{\pi} \\
& \quad \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + (36 \sqrt{\pi} \\
& \quad \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left. \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) \right\} \Big\}
\end{aligned}$$

$$\begin{aligned}
& D \left[ \left( 12 \sqrt{\pi} \left( -128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5 \right) \right) / \right. \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad (24 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \quad \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \left( (-2 \pi + \text{True})^4 \right)^{3/2} \right) - \\
& \quad (24 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad (6 \sqrt{\pi} (4 \pi - 2 \text{True}) \\
& \quad \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \quad (24 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \quad (36 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \Big) \Big) / \\
& \quad \left. \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right), \text{True} \right]
\end{aligned}$$

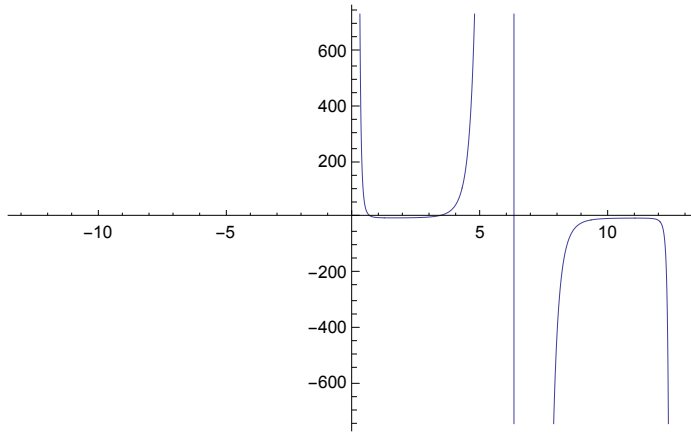


$$\begin{aligned}
& \frac{12 \sqrt{\pi} (640 \pi^4 - 480 \pi^3 \text{True} - 360 \pi^2 \text{True}^2 + 240 \pi \text{True}^3 - 30 \text{True}^4)}{(2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}} - (48 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \quad (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2}) - \\
& (48 \sqrt{\pi} (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4}) - (12 \sqrt{\pi} \\
& \quad (4 \pi - 2 \text{True}) (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}) - \\
& (48 \sqrt{\pi} (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}) + \\
& (72 \sqrt{\pi} (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5)) / \\
& \quad ((2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}) + \\
& (144 \sqrt{\pi} (-2 \pi + \text{True})^6 \\
& \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{5/2}) - \\
& (72 \sqrt{\pi} (-2 \pi + \text{True})^2 \\
& \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2}) + \\
& (96 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 ((-2 \pi + \text{True})^4)^{3/2}) + \\
& (24 \sqrt{\pi} (4 \pi - 2 \text{True}) (-2 \pi + \text{True})^3 \\
& \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2}) + \\
& (96 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2}) - \\
& (144 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \quad (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2}) + \\
& (72 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) / \\
& \quad ((2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^4 \sqrt{(-2 \pi + \text{True})^4}) + \\
& (24 \sqrt{\pi} (4 \pi - 2 \text{True})
\end{aligned}$$

$$\begin{aligned}
& \left( 32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6 \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 (4 \pi - \text{True}) \text{True}^{3/2} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& (96 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& (144 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \Big/ \\
& \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& (9 \sqrt{\pi} (4 \pi - 2 \text{True})^2 \\
& \left( 32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6 \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 (4 \pi - \text{True}) \text{True}^{5/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& (24 \sqrt{\pi} (4 \pi - 2 \text{True}) \\
& \left( 32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6 \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^3 (4 \pi - \text{True}) \text{True}^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& (36 \sqrt{\pi} (4 \pi - 2 \text{True}) \\
& \left( 32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6 \right) \Big/ \\
& \left( (2 \pi - \text{True})^4 \text{True}^2 (4 \pi - \text{True}) \text{True}^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& (12 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 (4 \pi - \text{True}) \text{True}^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& (72 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^4 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& (144 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \Big/ \\
& \left( (2 \pi - \text{True})^4 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& (144 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6)) \Big/ \\
& \left( (2 \pi - \text{True})^5 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) \\
\text{Plot} & \left[ \frac{12 \sqrt{\pi} (640 \pi^4 - 480 \pi^3 \text{True} - 360 \pi^2 \text{True}^2 + 240 \pi \text{True}^3 - 30 \text{True}^4)}{(2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4}} - \right. \\
& (48 \sqrt{\pi} (-2 \pi + \text{True})^3 \\
& \left. (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2} \right) - \\
& (48 \sqrt{\pi} (-128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5)) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& (12 \sqrt{\pi} (4 \pi - 2 \text{True})
\end{aligned}$$

$$\begin{aligned}
& \left( -128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5 \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \left( 48 \sqrt{\pi} \left( -128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5 \right) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 72 \sqrt{\pi} \left( -128 \pi^5 + 640 \pi^4 \text{True} - 240 \pi^3 \text{True}^2 - 120 \pi^2 \text{True}^3 + 60 \pi \text{True}^4 - 6 \text{True}^5 \right) \right) \Big/ \\
& \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 144 \sqrt{\pi} (-2 \pi + \text{True})^6 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{5/2} \right) - \\
& \left( 72 \sqrt{\pi} (-2 \pi + \text{True})^2 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2} \right) + \\
& \left( 96 \sqrt{\pi} (-2 \pi + \text{True})^3 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 ((-2 \pi + \text{True})^4)^{3/2} \right) + \\
& \left( 24 \sqrt{\pi} (4 \pi - 2 \text{True}) (-2 \pi + \text{True})^3 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2} \right) + \\
& \left( 96 \sqrt{\pi} (-2 \pi + \text{True})^3 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2} \right) - \\
& \left( 144 \sqrt{\pi} (-2 \pi + \text{True})^3 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 ((-2 \pi + \text{True})^4)^{3/2} \right) + \\
& \left( 72 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^4 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 24 \sqrt{\pi} (4 \pi - 2 \text{True}) \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) \Big/ \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 96 \sqrt{\pi} \left( 32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6 \right) \right) / \\
& \left( (2 \pi - \text{True})^3 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) - \left( 144 \sqrt{\pi} \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^4 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^3 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 9 \sqrt{\pi} (4 \pi - 2 \text{True})^2 \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{5/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 24 \sqrt{\pi} (4 \pi - 2 \text{True}) \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^3 \text{True}^3 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \\
& \left( 36 \sqrt{\pi} (4 \pi - 2 \text{True}) \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^4 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 12 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^3 \text{True}^2 ((4 \pi - \text{True}) \text{True})^{3/2} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \\
& \left( 72 \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^3 \text{True}^4 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) - \left( 144 \sqrt{\pi} \right. \\
& \quad \left. (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^4 \text{True}^3 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right) + \left( 144 \right. \\
& \quad \left. \sqrt{\pi} (32 \pi^6 - 128 \pi^5 \text{True} + 320 \pi^4 \text{True}^2 - 80 \pi^3 \text{True}^3 - 30 \pi^2 \text{True}^4 + 12 \pi \text{True}^5 - \text{True}^6) \right) / \\
& \left( (2 \pi - \text{True})^5 \text{True}^2 \sqrt{(4 \pi - \text{True}) \text{True}} (-4 \pi + \text{True})^2 \sqrt{(-2 \pi + \text{True})^4} \right), \\
& \{ \text{True}, -13, 13 \} ]
\end{aligned}$$



SphericalPlot3D[  

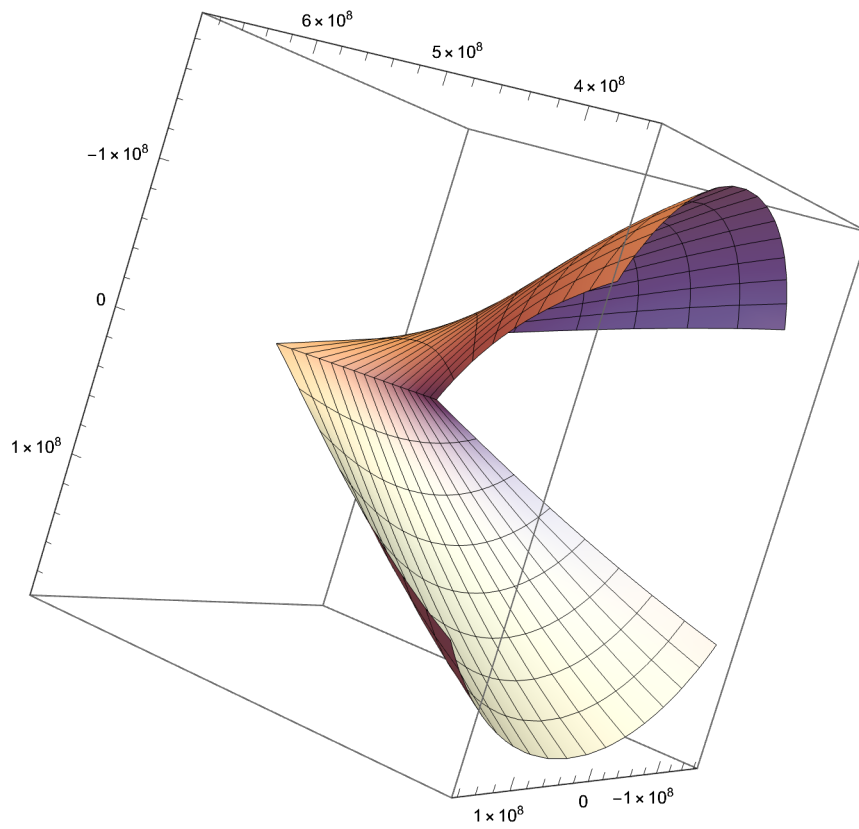
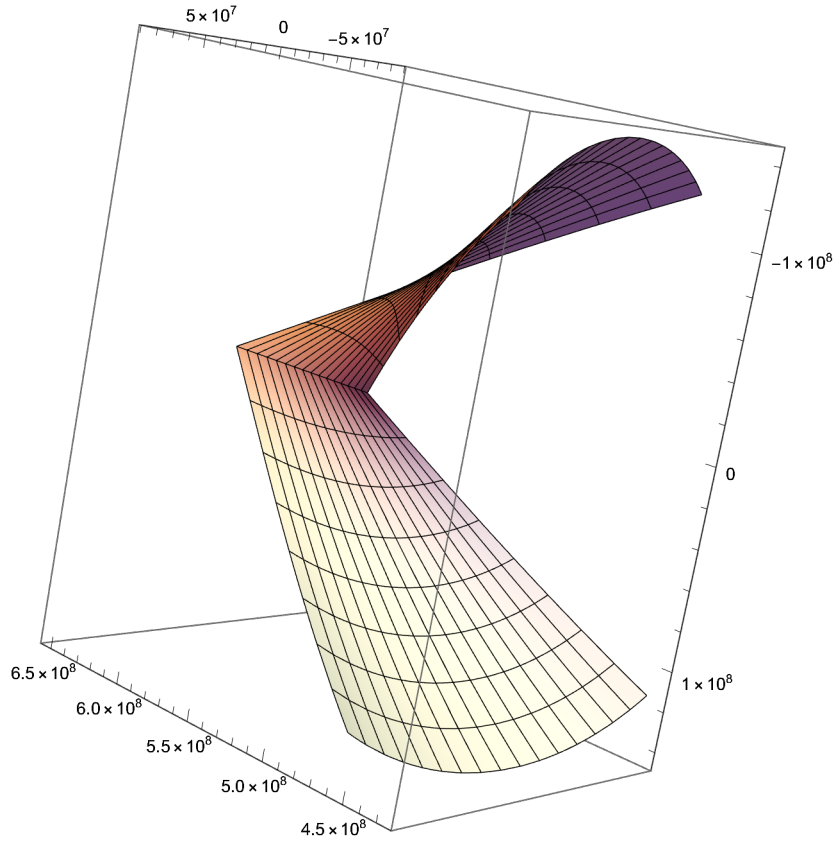
$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot \sin[\beta]^2 \right)} \right) /$$
  

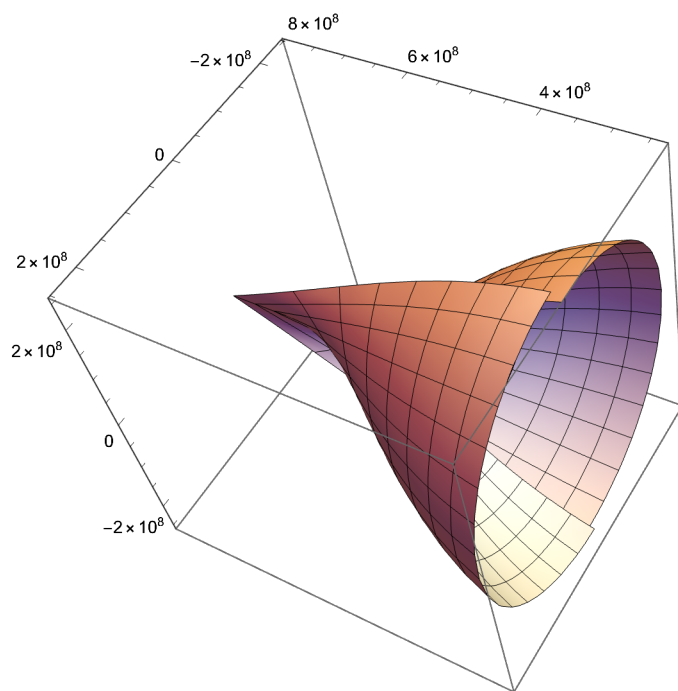
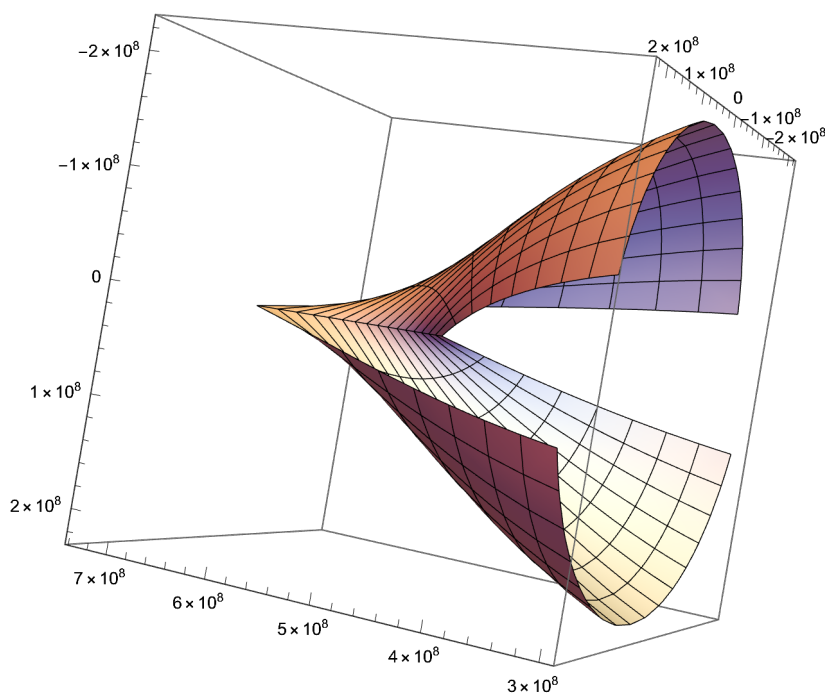
$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \right.} \right.$$
  

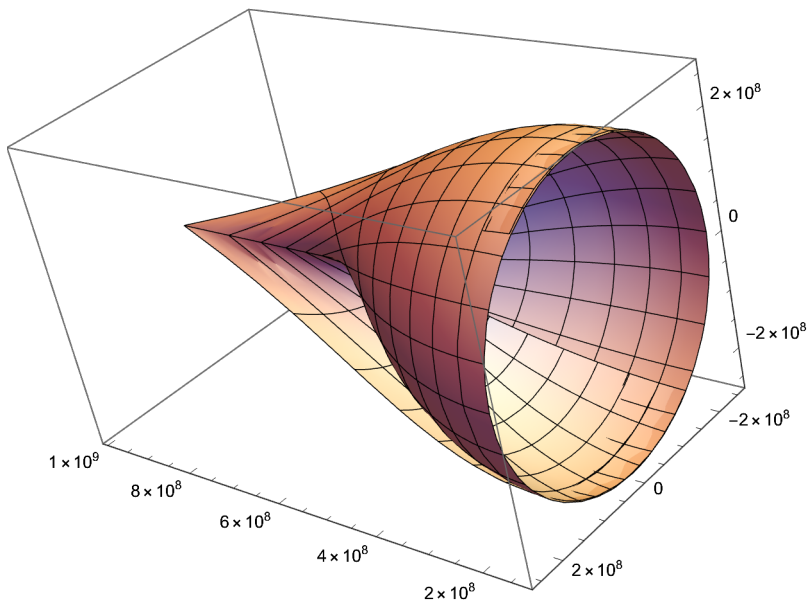
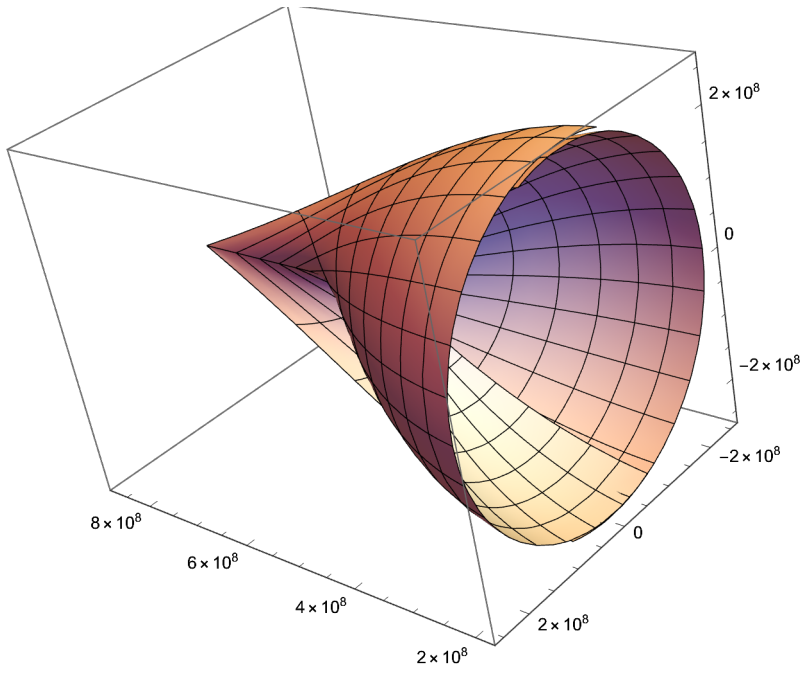
$$\left. \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \right.$$
  

$$\left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 +$$
  

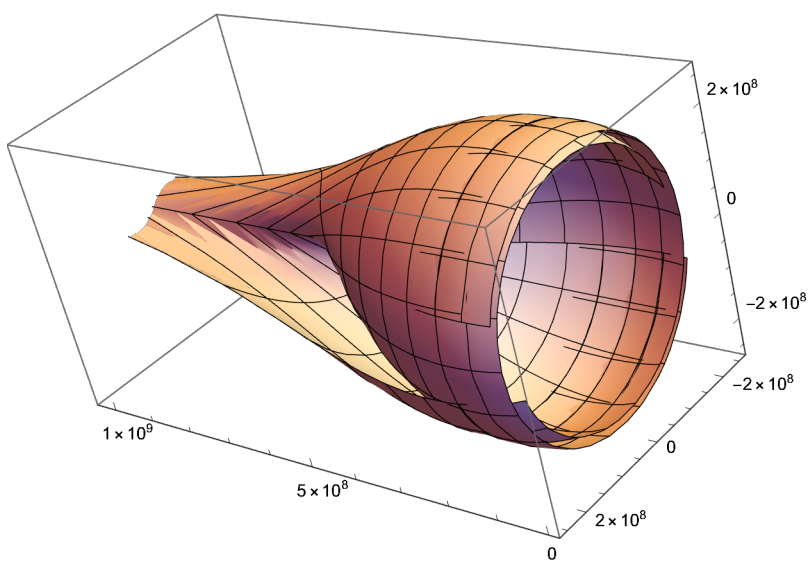
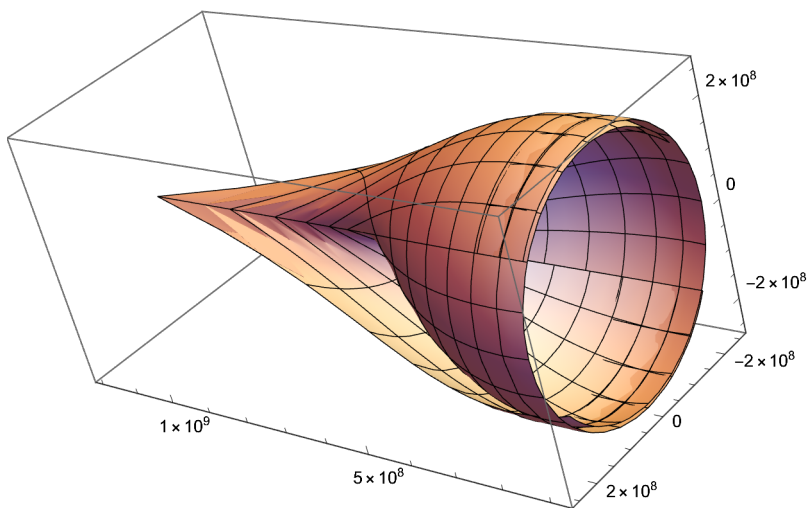
$$39.47841760435743 \cdot \sin[\beta]^2 \Big) \Big), \{\beta, -.1\pi, .1\pi\}, \{\theta, -.2\pi, .2\pi\}]$$

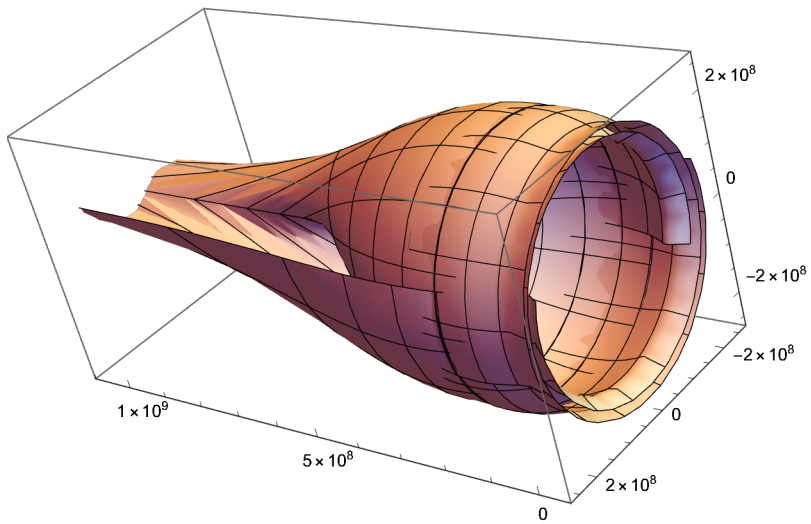
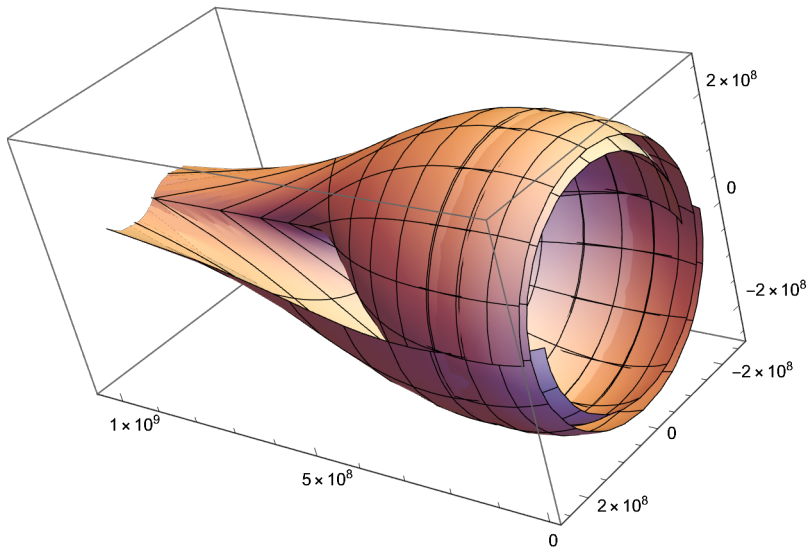


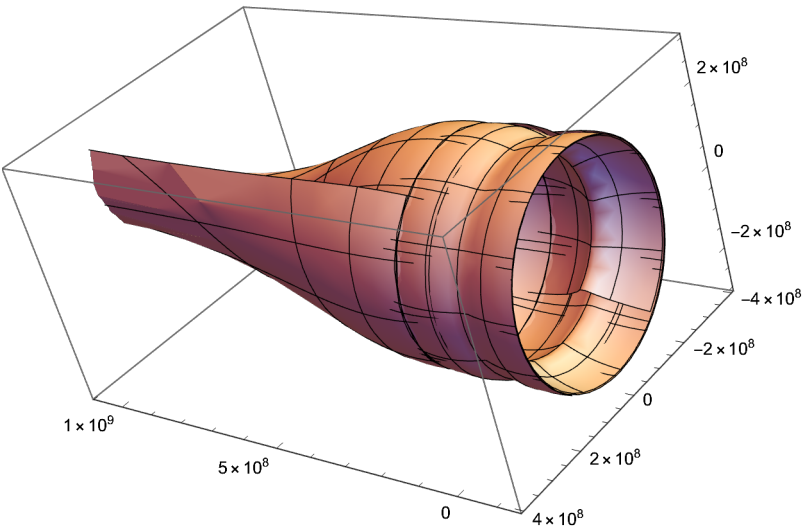
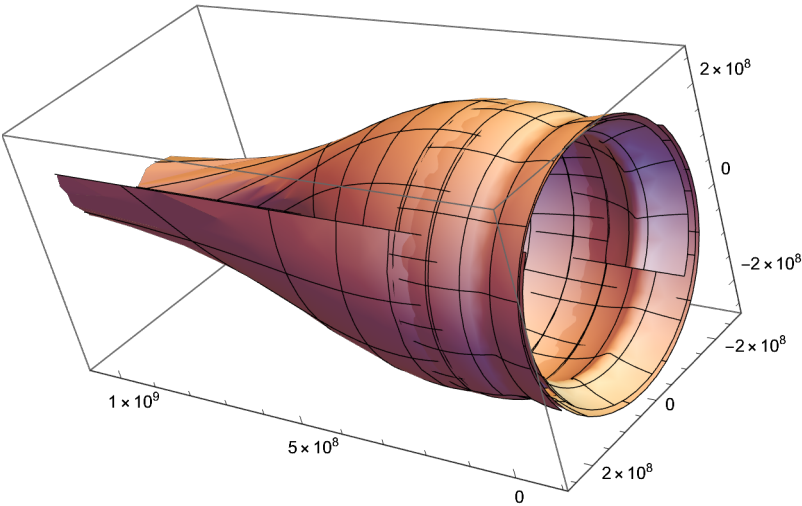


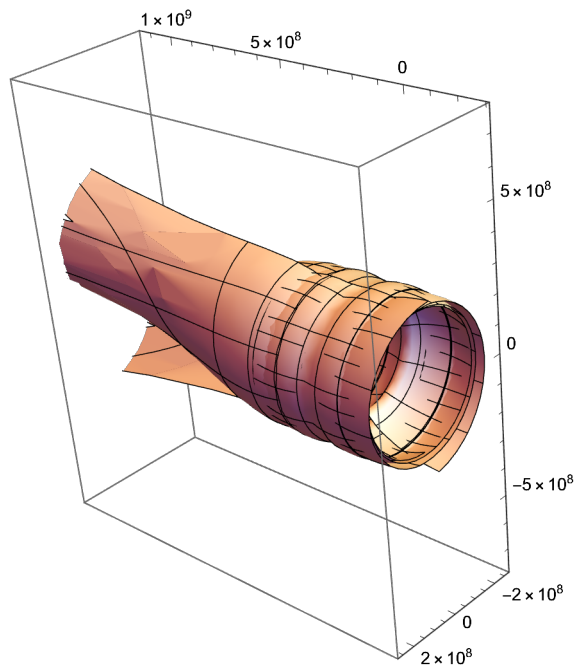
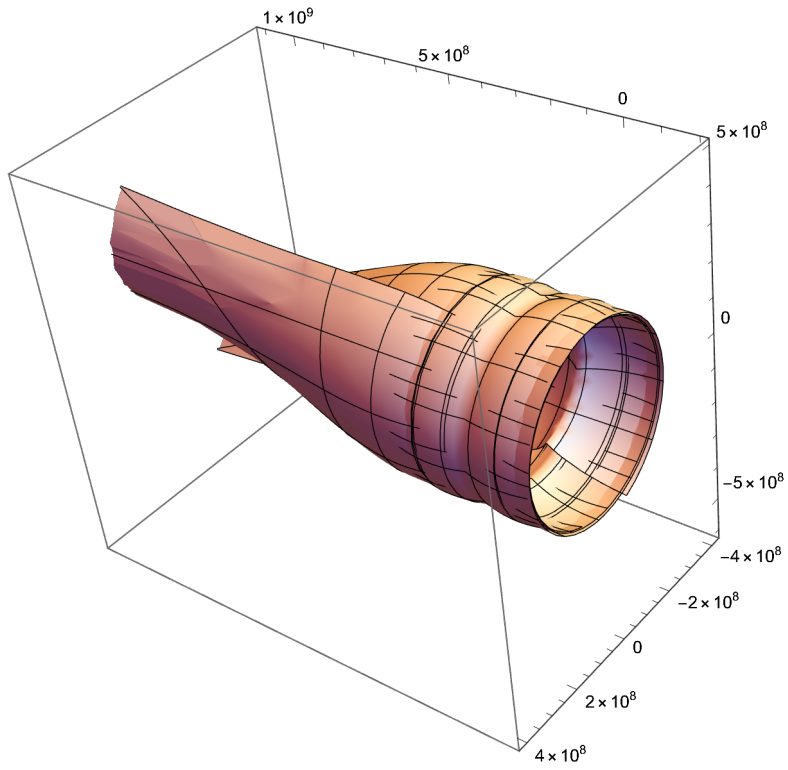


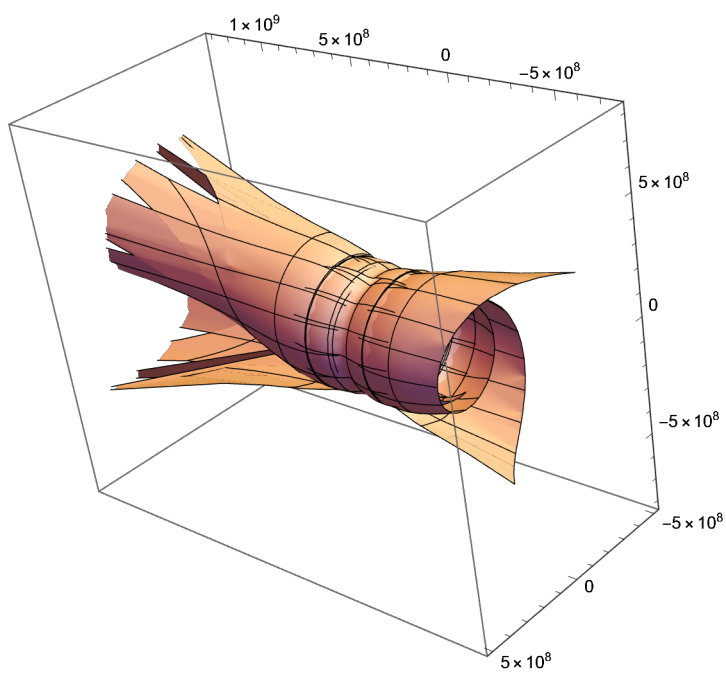
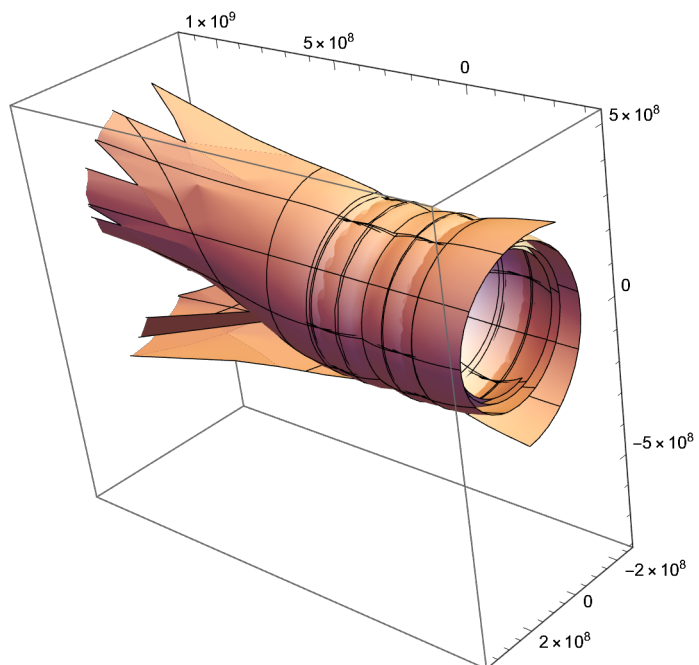


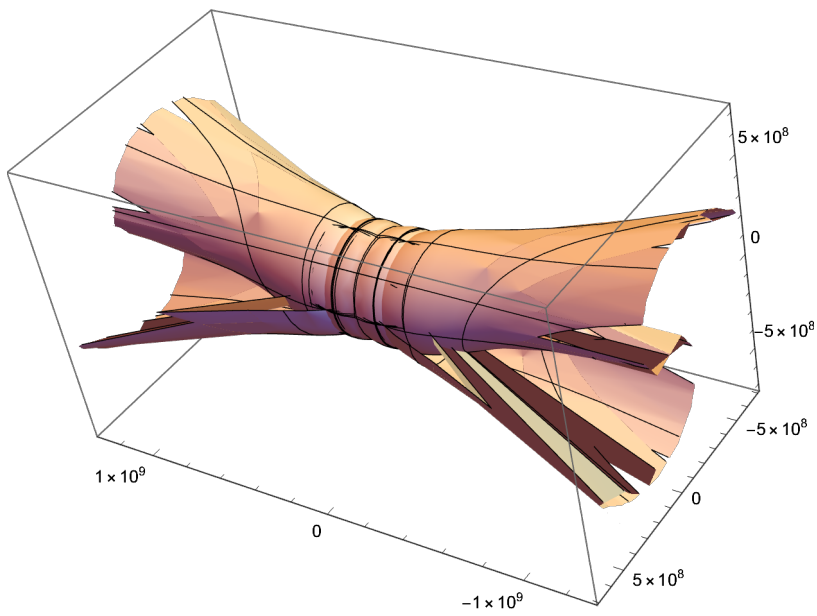
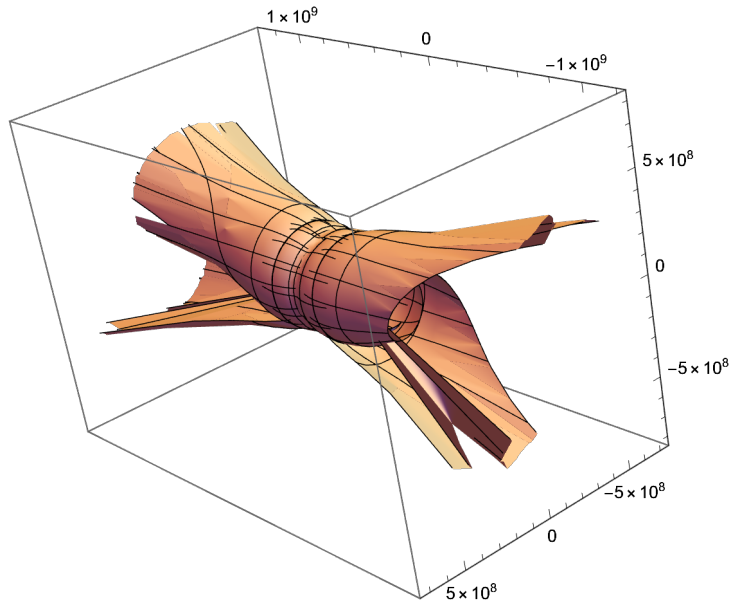


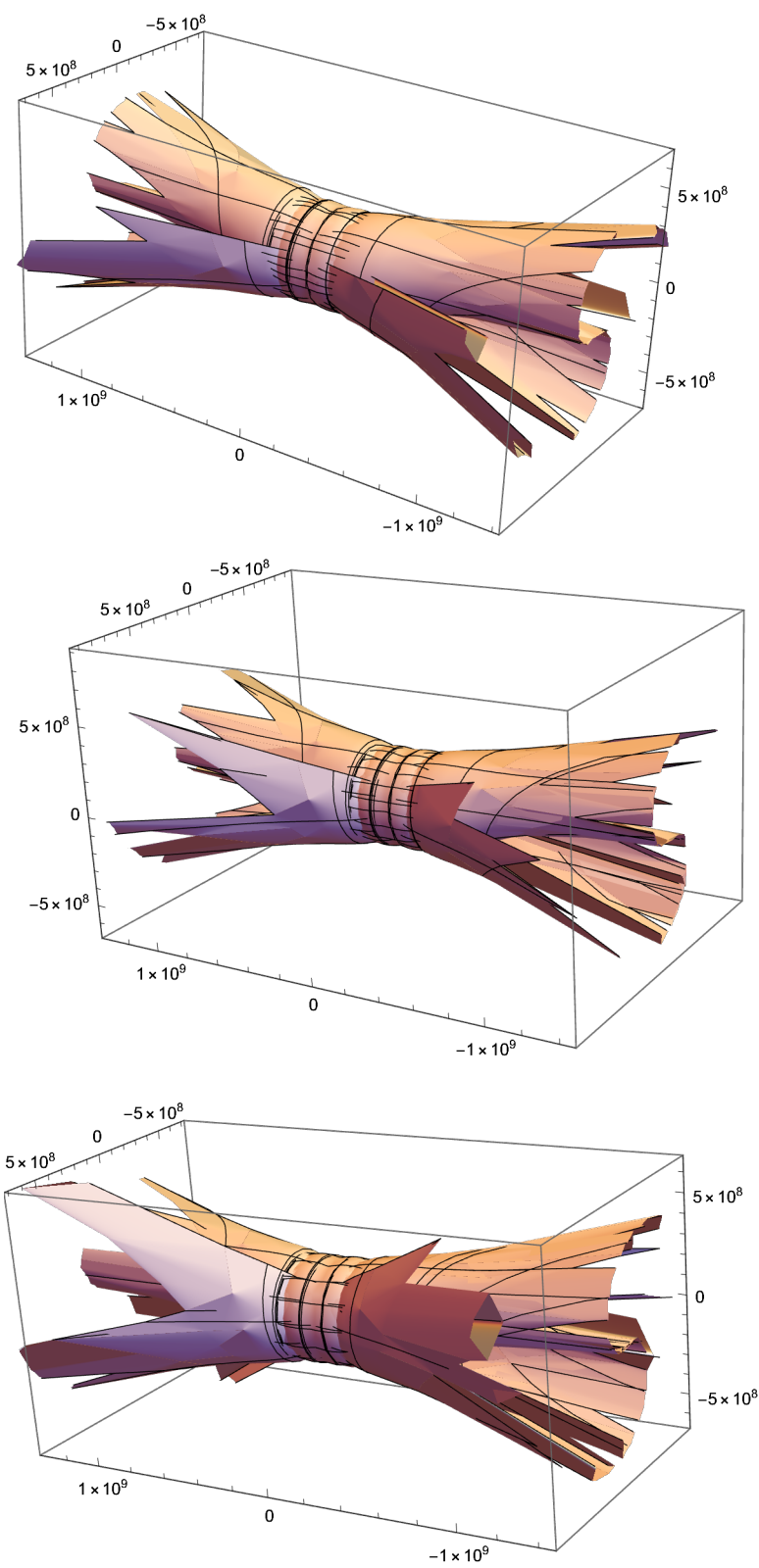












samples are going to change during motion through the environment. "how do they give me details of an object," the motion through the environment would not be noticeable unless the surface has some support. Virtual surfaces require virtual hardware, however, describing how something moves in general through the gradient of spacetime, certain solutions to the velocity of the point location can only be solved when the exact speed of light is plugged into the equation. "how do they give me nesting in a regular way"

$$\text{Abs}\left[\frac{2\pi\left(r^2 + \sqrt{r^4 - r^2\eta^2}\right)}{r^2}\right] + \text{Abs}\left[\frac{2\pi\left(r^2 - \sqrt{r^4 - r^2\eta^2}\right)}{r^2}\right] = \text{The change of time}$$

$$\text{Simplify}\left[\text{Abs}\left[\frac{2\pi\left(r^2 + \sqrt{r^4 - r^2\eta^2}\right)}{r^2}\right] + \text{Abs}\left[\frac{2\pi\left(r^2 - \sqrt{r^4 - r^2\eta^2}\right)}{r^2}\right]\right]$$

$$2\pi\left(\text{Abs}\left[1 - \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right] + \text{Abs}\left[1 + \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right]\right)$$

$$\text{Solve}\left[2\pi\left(\text{Abs}\left[1 - \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right] + \text{Abs}\left[1 + \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right]\right) == c \frac{1080\theta}{\pi\sqrt{1 - \frac{v^2}{c^2}}}, \eta\right]$$

{ {  $\eta \rightarrow$

$$\begin{aligned} & -\left(r\sqrt{-c^4\pi^8 + 2c^2\pi^8v^2 - \pi^8v^4 + 145800c^6\pi^4\theta^2 - 145800c^4\pi^4v^2\theta^2 - 5314410000c^8\theta^4}\right) / \\ & \left(\pi^2\sqrt{-c^4\pi^4 + 2c^2\pi^4v^2 - \pi^4v^4 + 72900c^6\theta^2 - 72900c^4v^2\theta^2}\right)\}, \{\eta \rightarrow \\ & \left(r\sqrt{-c^4\pi^8 + 2c^2\pi^8v^2 - \pi^8v^4 + 145800c^6\pi^4\theta^2 - 145800c^4\pi^4v^2\theta^2 - 5314410000c^8\theta^4}\right) / \\ & \left(\pi^2\sqrt{-c^4\pi^4 + 2c^2\pi^4v^2 - \pi^4v^4 + 72900c^6\theta^2 - 72900c^4v^2\theta^2}\right)\} \} \end{aligned}$$

$$\text{Solve}\left[2\pi\left(\text{Abs}\left[1 - \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right] + \text{Abs}\left[1 + \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right]\right) == c \frac{1080\theta}{\pi\sqrt{1 - \frac{v^2}{c^2}}}, v\right]$$

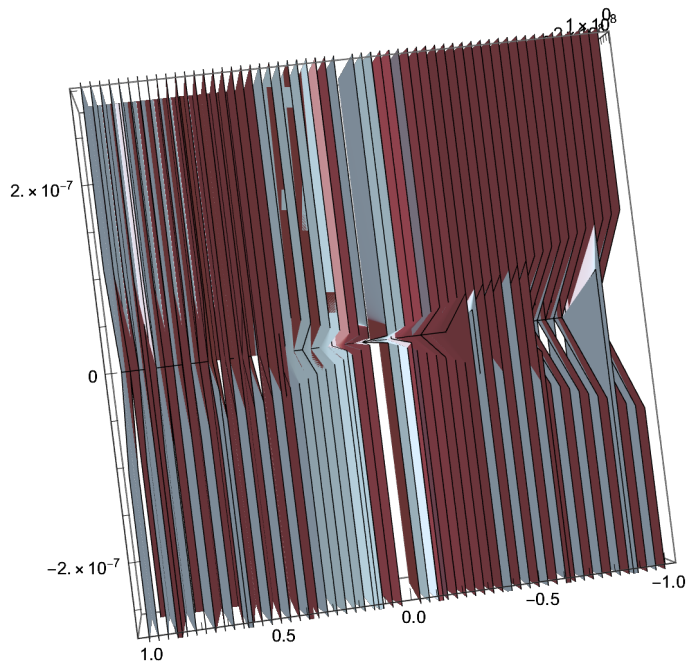
$$\left\{\left\{v \rightarrow -\frac{c\sqrt{\pi^4 - \frac{291600c^2\theta^2}{\left(\text{Abs}\left[1 - \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right] + \text{Abs}\left[1 + \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right]\right)^2}}}{\pi^2}\right\}, \left\{v \rightarrow \frac{c\sqrt{\pi^4 - \frac{291600c^2\theta^2}{\left(\text{Abs}\left[1 - \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right] + \text{Abs}\left[1 + \frac{\sqrt{r^4 - r^2\eta^2}}{r^2}\right]\right)^2}}}{\pi^2}\right\}\right\}$$

$$\eta = \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}$$

$$c := (2.99792458 * 10^8)$$



$$\text{RevolutionPlot3D}\left[\frac{c}{\sqrt{\frac{\pi^4 - \frac{291600 c^2 \theta^2}{\left(\text{Abs}\left[1 - \frac{\sqrt{r^4 - r^2 \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2}}{r^2}\right] + \text{Abs}\left[1 + \frac{\sqrt{r^4 - r^2 \left(\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2}}{r^2}\right]}{\pi^2}}}, \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}\right]$$



# Three Principles of Acceleration in a Space Defined by Light

by Parker Matthew Davis Emmerson

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The parameters of a cone through an expression relating a difference in circumferences to an arc length of the initial position. Please note that while this goes on in the unit circle, certain things are going on in the complex sphere.

$$C = 2 \pi r$$

This is the circumference of our initial circle of radius  $r$

$$C_2 = 2 \pi r_1$$

This is the circumference of our second circle, the base of the cone, of radius  $r_1$

$$r^2 = r_1^2 + \eta^2$$

This is the initial radius squared expressed as the slant of the cone in terms of the height of the cone,  $\eta$ , and the radius of the base of the cone,  $r_1$

$$r = \sqrt{r_1^2 + \eta^2}$$

$$s = \theta r$$

$$s / \theta = r$$

The arc length taken out of a circle at a given time is =

$$t = C - C_2 = 2\pi r - 2\pi r_1 = \theta r \rightarrow \text{Equation 7}$$

$$r_1^2 = r^2 - \eta^2$$

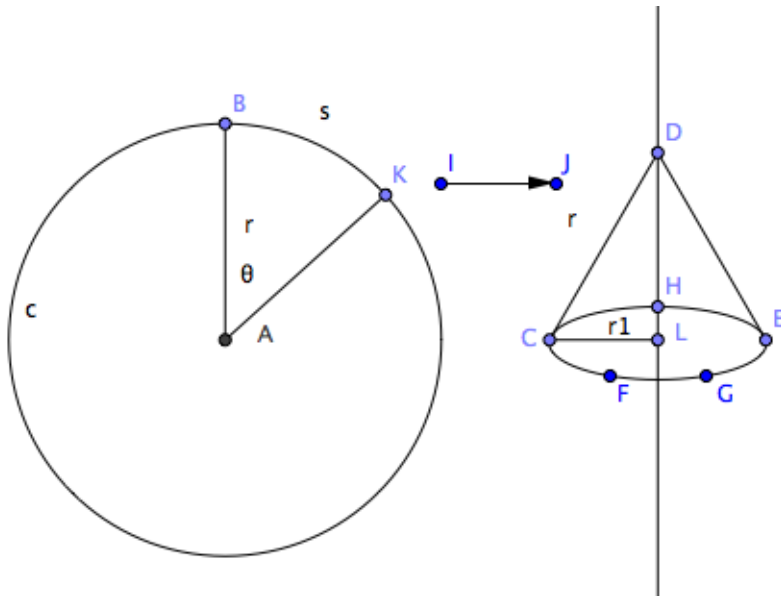
$$r_1 = \sqrt{r^2 - \eta^2}$$

$$\eta \leq r$$

$$\tau = \text{time}$$

$$1 \text{ second} = 6 \text{ degrees}$$

$$\tau = 6 (180 / \pi) \theta$$



I will now do some algebra to conclude what the height of the cone is in terms of the initial parameters. It can eventually be reduced to a single variable.

II. Proof

$$\text{Solve}[r_1^2 + \eta^2 = r^2, \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r_1^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r_1^2} \right\} \right\} \quad (234)$$

We say that the amount of  $\theta r = s$ , taken out of the circle is the change in the circle's circumference that is the base of the cone. The change is equal to  $s = 2\pi r - 2\pi r_1$ .

Notice that  $\theta =$

$$((2\pi r) / r) - ((2\pi r_1) / r), \text{ because we divide by } r \text{ on both sides.}$$

We will focus on the positive solutions for the height of the cone.

$$\begin{aligned} &\text{Solve}[\eta == \sqrt{r^2 - r_1^2}, r_1] \\ &\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2 - \eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2 - \eta^2} \right\} \right\} \end{aligned} \quad (235)$$

This is the change in circumference with  
the substituted expression for  $r_1$  in terms of  $h$  and  $r$ .

$$r \theta == s == 2 \pi (r) - 2 \pi \sqrt{(r)^2 - \eta^2} = 2 \pi (r) - 2 \pi r_1 \quad (236)$$

$$\theta == (2 \pi r) / r - (2 \pi r_1) / r = ((2 \pi r) / r) - \left( (2 \pi \sqrt{-\eta^2 + r^2}) / r \right)$$

$$\begin{aligned} &\text{Solve}[\theta * r == 2 \pi (r) - 2 \pi \sqrt{(r)^2 - \eta^2}, \eta] \\ &\left\{ \left\{ \eta \rightarrow -\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\}, \left\{ \eta \rightarrow \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right\} \right\} \end{aligned}$$

$$\begin{aligned} &\text{Solve}[\eta == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, r] \\ &\left\{ \left\{ r \rightarrow -\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} \right\} \right\} \end{aligned}$$

In polar coordinates, it can be said that  $r_1 = r \cos[\theta]$ , and that  $\eta = r \sin[\theta]$  (237)

$$\frac{2 \pi \eta}{\sqrt{4 \pi \theta - \theta^2}} = r = \frac{2 \pi * r * \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \quad (238)$$

$$c := (2.99792458 * 10^8)$$

$$\eta := \text{rate} * \text{time} = c * \tau = \text{height of cone} \quad (239)$$

$\tau := 6 \left( \theta_{\text{degrees}} \right) = 6 \left( (180 / \pi) \theta \right)$ , because if theta were in radians to begin with,  
we would have to convert that number of radians to degrees. This way,  
both our thetas are in radians,

but our result accounts for the constant of the degrees involved in measuring time.

$$(180 / \pi)$$

$$r = \frac{2 * c * \tau * \pi}{\sqrt{4 \pi \theta - \theta^2}} = \frac{2 * c * 6 \left( (180 / \pi) \theta \right) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}$$

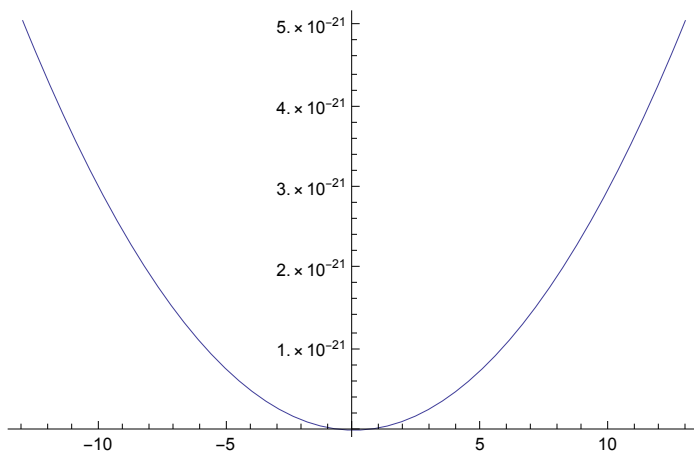
$$\text{Solve} \left[ r == \frac{2 * c * 6 \left( (180 / \pi) \theta \right) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, \theta \right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{4 \pi r^2}{4665600 c^2 + r^2} \right\} \right\}$$

$$\text{Solve}\left[r == \frac{2 * c * 6 ((180 / \pi) \theta) * \pi}{\sqrt{4 \pi \theta - (\theta)^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{4 \pi r^2}{4665600 c^2 + r^2}\right\}\right\}$$

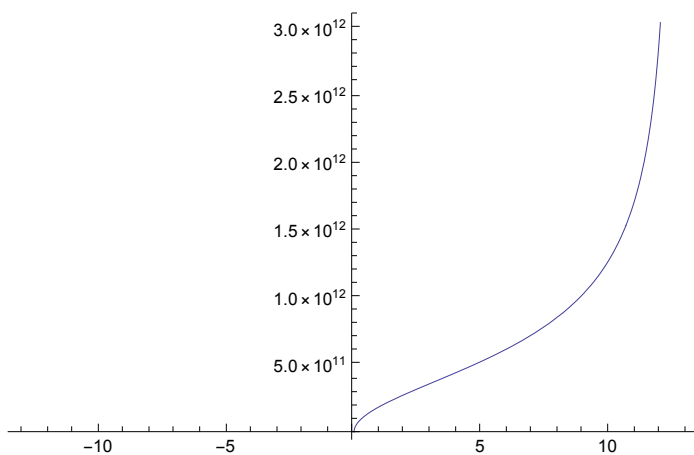
$$\text{Plot}\left[\frac{4 \pi r^2}{4665600 c^2 + r^2}, \{r, -13, 13\}\right]$$



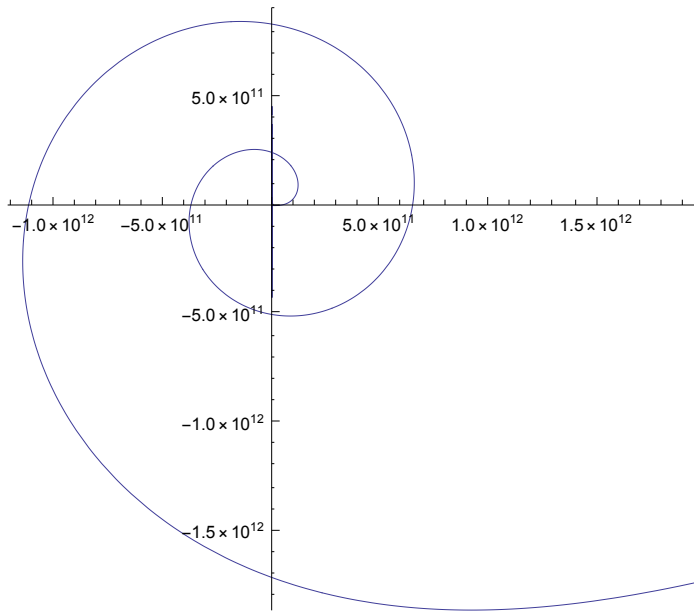
$$\text{Solve}\left[\theta == \frac{4 \pi r^2}{4665600 c^2 + r^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}, \left\{r \rightarrow \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right\}\right\}$$

$$\text{Plot}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}, \{\theta, -13, 13\}\right]$$



PolarPlot $\left[\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}},\{\theta,-13,13\}\right]$



$$r := \frac{2\,\pi\,\eta}{\sqrt{4\,\pi-\theta}}; \eta = r \sin[\theta]$$

$$\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}} = \frac{2\,\pi\,\eta}{\sqrt{4\,\pi-\theta}} = \frac{2\,\pi\,r\,\sin[\theta]}{\sqrt{4\,\pi-\theta}}$$

$$\text{Solve}\left[\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}} == \frac{2\,\pi\,r\,\sin[\theta]}{\sqrt{4\,\pi-\theta}}, r\right]$$

$$\left\{\left\{r \rightarrow \frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\,\pi-\theta)}\,\theta\,\text{Csc}[\theta]}{\pi\,\sqrt{4\,\pi-\theta}}\right\}\right\}$$

III. Why define the space by light? I can't travel faster than space.

We define the distance,  $\eta$  in terms of the speed of light, but also in terms of its pythagorean correlates. Since the space is a distance described by the speed of light, it is not absurd to think that something can accelerate within this space without going faster than the speed of light.

## I. The First Principle, $\eta$ :

$$\eta == \frac{\sqrt{4\pi \left( \frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}} \right)^2 \theta - \left( \frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}} \right)^2 \theta^2}}{2\pi} =$$

$$\frac{\sqrt{4\pi \left( \frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\operatorname{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}} \right)^2 \theta - \left( \frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\operatorname{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}} \right)^2 \theta^2}}{2\pi} =$$

$$\frac{\sqrt{4\pi \left( \frac{2\pi r \operatorname{Sin}[\theta]}{\sqrt{4\pi\theta-\theta^2}} \right)^2 \theta - \left( \frac{2\pi r \operatorname{Sin}[\theta]}{\sqrt{4\pi\theta-\theta^2}} \right)^2 \theta^2}}{2\pi} = r \operatorname{Sin}[\beta]$$

The expressions for radius in terms of true Pythagorean proofs :

$\eta := r \operatorname{Sin}[\theta] = r \operatorname{Sin}[\beta]$  is the special case.

## II. The Second Principle, $r$ :

$$r := \frac{2\pi\eta}{\sqrt{4\pi\theta-\theta^2}}$$

$$r = \frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}} = \frac{2\pi r \operatorname{Sin}[\theta]}{\sqrt{4\pi\theta-\theta^2}} = \frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\operatorname{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}}$$

$$\left( \operatorname{Solve}\left[ \frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}} == \frac{2\pi r \operatorname{Sin}[\theta]}{\sqrt{4\pi\theta-\theta^2}}, r \right] \right)$$

$$\left\{ \left\{ r \rightarrow \frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\operatorname{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}} \right\} \right\}$$

The radius,  $r_1$ , which is the base of a cone, with slant  $r$  and height  $\eta$ .

## III. The Third Principle, $r_1$

$$\left\{ \left\{ r_1 \rightarrow -\sqrt{r^2-\eta^2} \right\}, \left\{ r_1 \rightarrow \sqrt{r^2-\eta^2} \right\} \right\}$$

$$\begin{aligned}
\sqrt{r^2 - \eta^2} &= \sqrt{\left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2}
\end{aligned}$$

## IV. Deriving Acceleration from the First Principle and Plotting the Correlations: $\eta$

$$\eta == \frac{\sqrt{4 \pi \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi} =$$

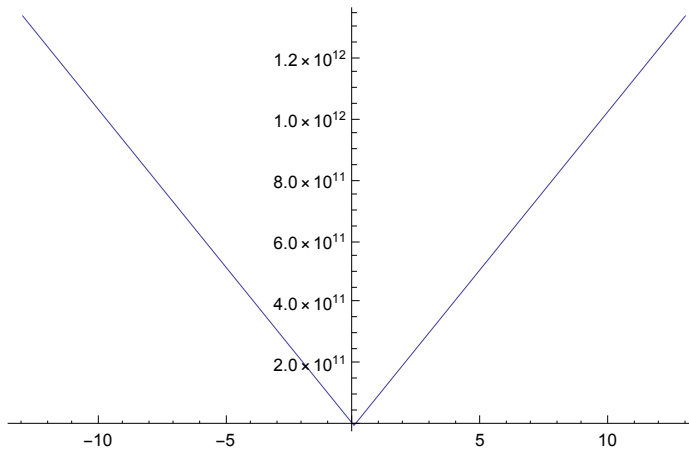
$$\frac{\sqrt{4 \pi \left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi} =$$

$$\frac{\sqrt{4 \pi \left( \frac{2 \pi r \operatorname{Sin}[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta - \left( \frac{2 \pi r \operatorname{Sin}[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)^2 \theta^2}}{2 \pi}$$

The following will be divided into actual expressions for  $\eta$  of each different possible perspective that I have thought of up to date.

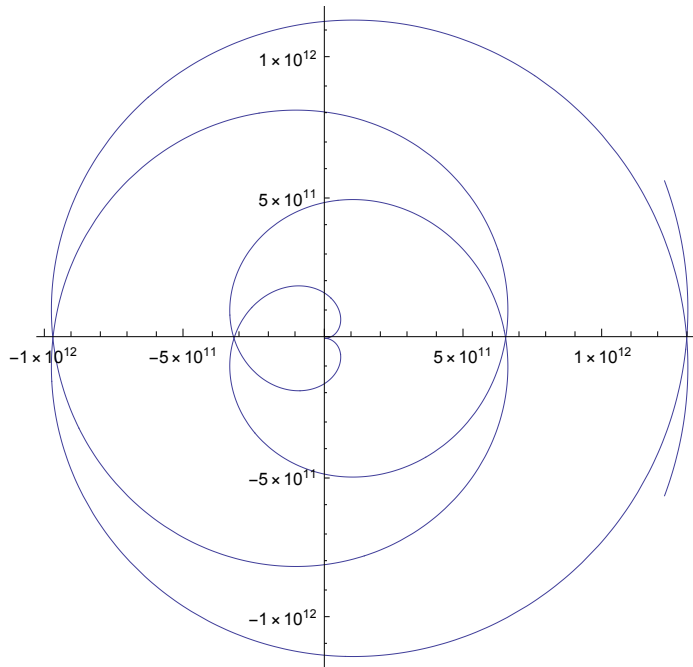
### Expression for $\eta$ No. 1

$$\text{Plot} \left[ \frac{\sqrt{4 \pi \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi}, \{\theta, -13, 13\} \right]$$





$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



$$c := (2.99792458 * 10^8)$$

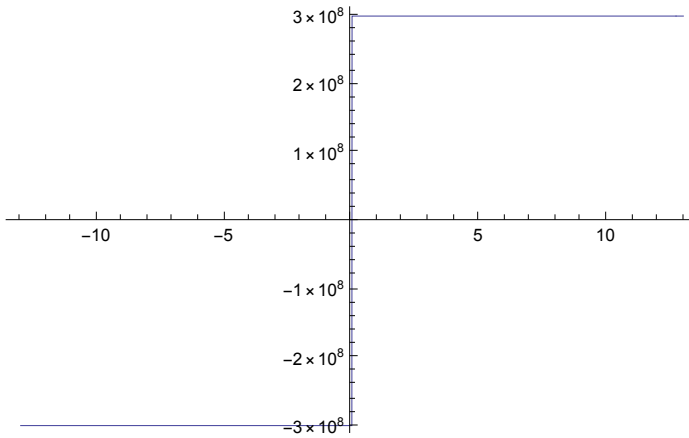
### The first and second derivatives of expression for $\eta$ No. 1

We are taking the derivative with respect to time, and since our time =  $\tau = 6 ((180/\pi) \theta)$ , we multiply by  $1/(6 (180/\pi))$ , because only theta is changing, and theta is in terms of radians. For the physical conversions, we must take this factor out of the derivative with respect to time, because it is constant.

$$\frac{1}{6 (180 / \pi)} D\left[\frac{\sqrt{4\pi\left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}}{2\pi}, \theta\right]$$

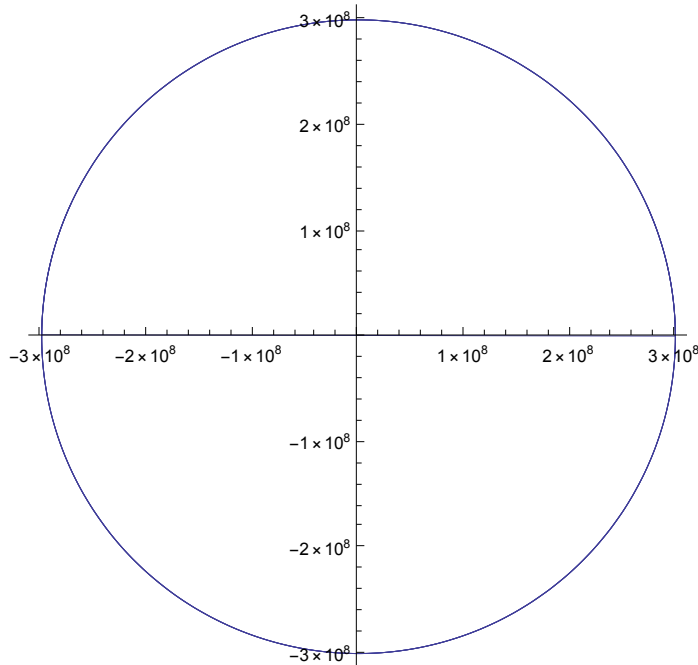
$$\frac{\frac{37324800c^2\pi\theta}{4\pi-\theta} + \frac{18662400c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{13996800c^2\theta^2}{4\pi-\theta} - \frac{4665600c^2\theta^3}{(4\pi-\theta)^2}}{4320} \sqrt{\frac{18662400c^2\pi\theta^2}{4\pi-\theta} - \frac{4665600c^2\theta^3}{4\pi-\theta}}$$

$$\text{Plot}\left[\frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}}{4320\sqrt{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}}, \{\theta, -13, 13\}\right]$$



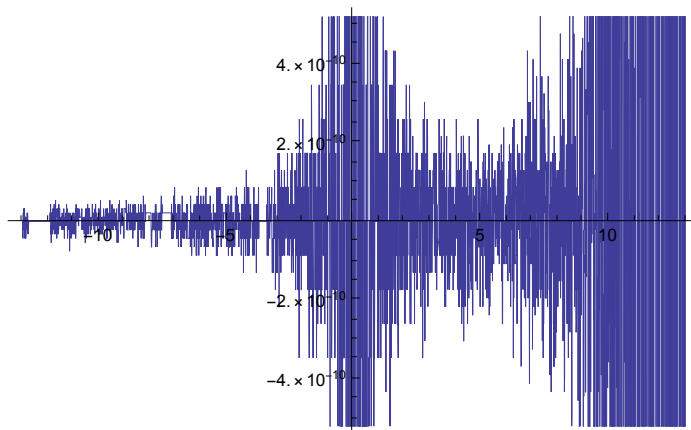
Light has a constant velocity.

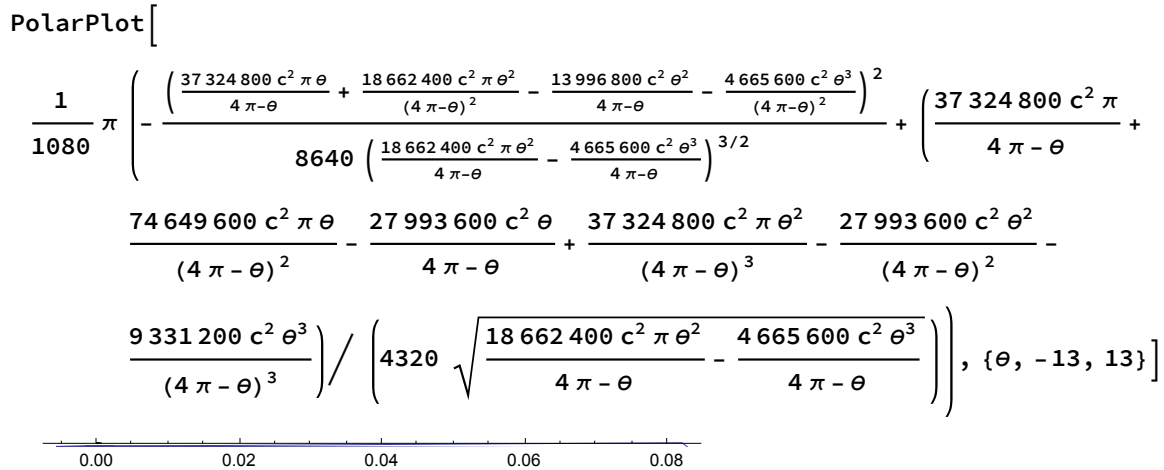
$$\text{PolarPlot}\left[\frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}}{4320\sqrt{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}}, \{\theta, -13, 13\}\right]$$



Light travels through its a distance equal to the height of the cone, with a max value of the initial radius, in a perfect circle in polar coordinates.

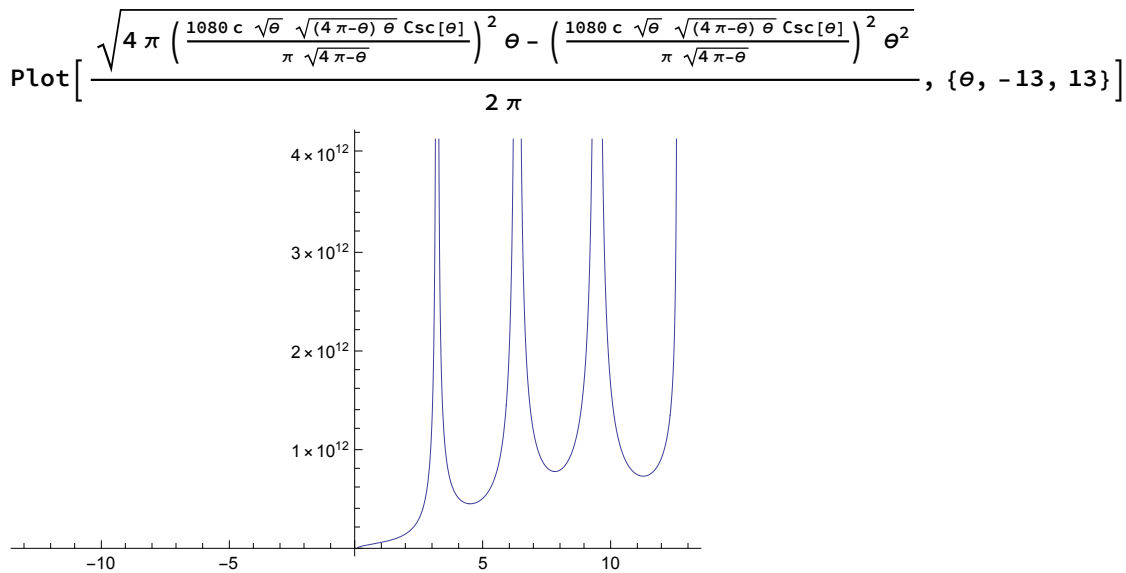
$$\begin{aligned}
& 1 / (6 (180 / \pi)) \operatorname{D} \left[ \frac{\frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2}}{4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{4 \pi - \theta}}}, \theta \right] \\
& \frac{1}{1080} \pi \left( - \frac{\left( \frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2} \right)^2}{8640 \left( \frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{4 \pi - \theta} \right)^{3/2}} + \right. \\
& \left( \frac{37324800 c^2 \pi}{4 \pi - \theta} + \frac{74649600 c^2 \pi \theta}{(4 \pi - \theta)^2} - \frac{27993600 c^2 \theta}{4 \pi - \theta} + \frac{37324800 c^2 \pi \theta^2}{(4 \pi - \theta)^3} - \right. \\
& \left. \left. \frac{27993600 c^2 \theta^2}{(4 \pi - \theta)^2} - \frac{9331200 c^2 \theta^3}{(4 \pi - \theta)^3} \right) / \left( 4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{4 \pi - \theta}} \right) \right) \\
& \operatorname{Plot} \left[ \frac{1}{1080} \pi \left( - \frac{\left( \frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2} \right)^2}{8640 \left( \frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{4 \pi - \theta} \right)^{3/2}} + \right. \right. \\
& \left( \frac{37324800 c^2 \pi}{4 \pi - \theta} + \frac{74649600 c^2 \pi \theta}{(4 \pi - \theta)^2} - \frac{27993600 c^2 \theta}{4 \pi - \theta} + \right. \\
& \left. \left. \frac{37324800 c^2 \pi \theta^2}{(4 \pi - \theta)^3} - \frac{27993600 c^2 \theta^2}{(4 \pi - \theta)^2} - \frac{9331200 c^2 \theta^3}{(4 \pi - \theta)^3} \right) / \right. \\
& \left. \left( 4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{4 \pi - \theta}} \right) \right], \{\theta, -13, 13\} ]
\end{aligned}$$



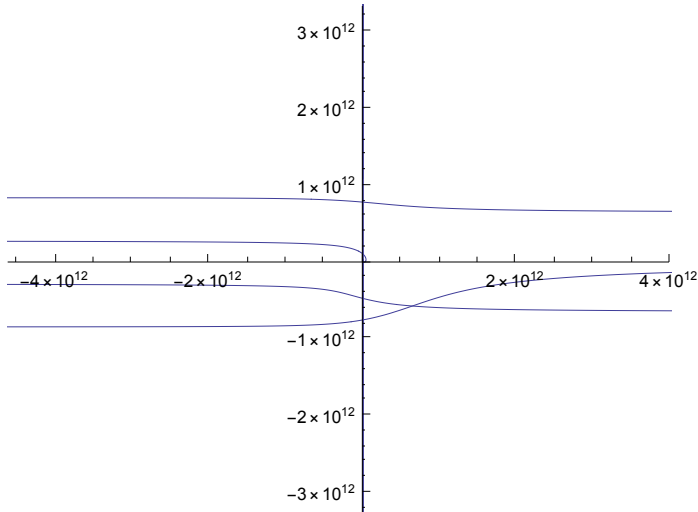


This is one of the most fundamentally interesting graphs I have ever found. What is unseen in the printed version is that when you scroll down the page in mathematica, you see that a line moves across the graph and the graph actually changes just from scrolling.

## Expression for $\eta$ No .2



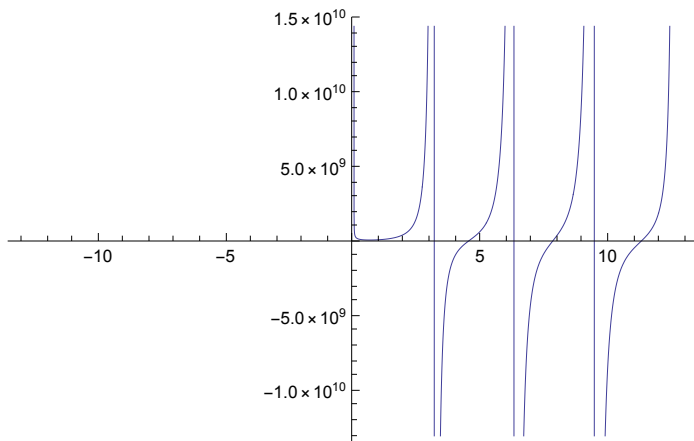
$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}\right)^2\theta - \left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}\right)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



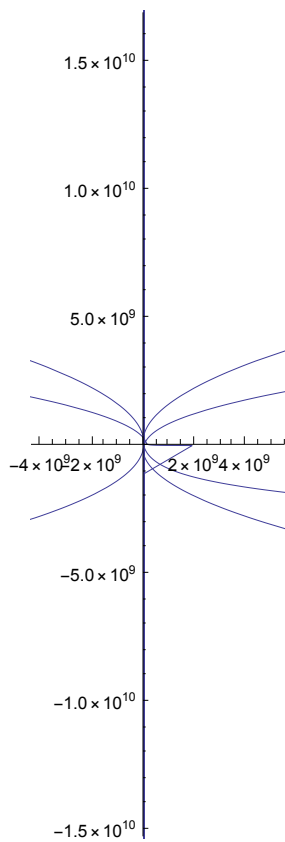
The first and second derivatives of expression for  $\eta$  No. 2

$$\begin{aligned} & 1 / (6 (180 / \pi)) \text{D}\left[\frac{\sqrt{4\pi\left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}\right)^2\theta - \left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}\right)^2\theta^2}}{2\pi}, \theta\right] \\ & \left(\frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi} - \frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi^2} - \right. \\ & \quad \left. \frac{9331200c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi} + \frac{2332800c^2\theta^4\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}\right) / \\ & \left(4320\sqrt{\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi} - \frac{1166400c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}}\right) \end{aligned}$$

$$\text{Plot}\left[\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right) / \left(4320\sqrt{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}\right), \{\theta, -13, 13\}\right]$$



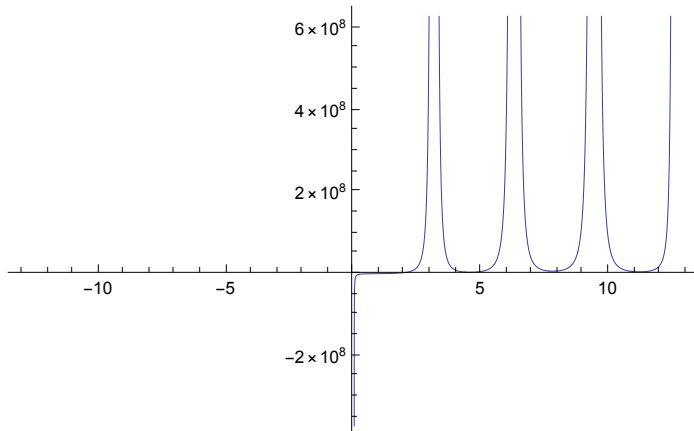
$$\text{PolarPlot}\left[\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right) / \left(4320\sqrt{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}\right), \{\theta, -13, 13\}\right]$$



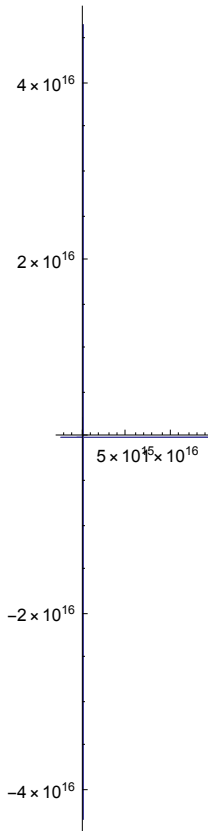
$$\begin{aligned}
& 1 / (6 (180 / \pi)) \, D \left[ \left( \frac{13996800 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi} - \frac{4665600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
& \quad \left. \left. \frac{9331200 \, c^2 \, \theta^3 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi} + \frac{2332800 \, c^2 \, \theta^4 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} \right) \right] / \\
& \quad \left( 4320 \sqrt{\frac{4665600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi} - \frac{1166400 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^2}{\pi^2}} \right), \theta \Big] \\
& \frac{1}{1080} \pi \left( - \left( \frac{13996800 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi} - \frac{4665600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
& \quad \left. \left. \frac{9331200 \, c^2 \, \theta^3 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi} + \frac{2332800 \, c^2 \, \theta^4 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} \right)^2 \right) / \\
& \quad \left( 8640 \left( \frac{4665600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi} - \frac{1166400 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \\
& \quad \left( \frac{27993600 \, c^2 \, \theta \, \text{Csc}[\theta]^2}{\pi} - \frac{13996800 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi^2} - \frac{55987200 \, c^2 \, \theta^2 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi} + \right. \\
& \quad \frac{18662400 \, c^2 \, \theta^3 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} + \frac{18662400 \, c^2 \, \theta^3 \, \text{Cot}[\theta]^2 \, \text{Csc}[\theta]^2}{\pi} - \\
& \quad \left. \frac{4665600 \, c^2 \, \theta^4 \, \text{Cot}[\theta]^2 \, \text{Csc}[\theta]^2}{\pi^2} + \frac{9331200 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^4}{\pi} - \frac{2332800 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^4}{\pi^2} \right) / \\
& \quad \left( 4320 \sqrt{\frac{4665600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi} - \frac{1166400 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^2}{\pi^2}} \right) \Big]
\end{aligned}$$



$$\text{Plot}\left[\frac{1}{1080}\pi\left(-\left(\frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi^2}-\frac{9331200c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}+\frac{2332800c^2\theta^4\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}\right)^2/\left(8640\left(\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}-\frac{1166400c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}\right)^{3/2}\right)+\left(\frac{27993600c^2\theta\text{Csc}[\theta]^2}{\pi}-\frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}-\frac{55987200c^2\theta^2\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}+\frac{18662400c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}+\frac{18662400c^2\theta^3\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi}-\frac{4665600c^2\theta^4\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi^2}+\frac{9331200c^2\theta^3\text{Csc}[\theta]^4}{\pi}-\frac{2332800c^2\theta^4\text{Csc}[\theta]^4}{\pi^2}\right)/\left(4320\sqrt{\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}-\frac{1166400c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}}\right)\right),\{\theta,-13,13\}]$$



$$\begin{aligned}
& \text{PolarPlot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \frac{13\,996\,800\, c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\, c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\, c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \right. \right. \\
& \quad \left. \left. \frac{2\,332\,800\, c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} \right)^2 \right] / \\
& \left( 8640 \left( \frac{4\,665\,600\, c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\, c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \\
& \left( \frac{27\,993\,600\, c^2 \theta \text{Csc}[\theta]^2}{\pi} - \frac{13\,996\,800\, c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{55\,987\,200\, c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \right. \\
& \quad \frac{18\,662\,400\, c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\, c^2 \theta^3 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi} - \\
& \quad \left. \frac{4\,665\,600\, c^2 \theta^4 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \frac{9\,331\,200\, c^2 \theta^3 \text{Csc}[\theta]^4}{\pi} - \frac{2\,332\,800\, c^2 \theta^4 \text{Csc}[\theta]^4}{\pi^2} \right) / \\
& \left. \left( 4320 \sqrt{\frac{4\,665\,600\, c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\, c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}} \right) \right), \{\theta, -13, 13\}
\end{aligned}$$



We also notice that we can exchange locations of the expressions for  $r$ . This gives us different perspectives on what is going on when a body is accelerating through such a space that is defined by traveling

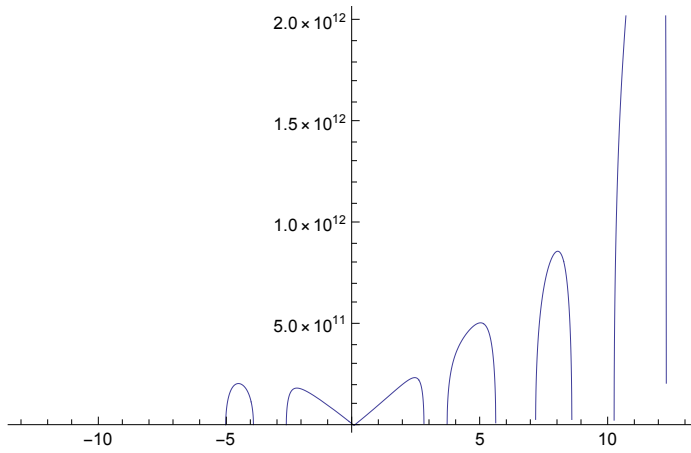
at the speed of light for a certain amount of time within the parenters of our system.

$$\eta == \frac{\sqrt{4 \pi \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi} =$$

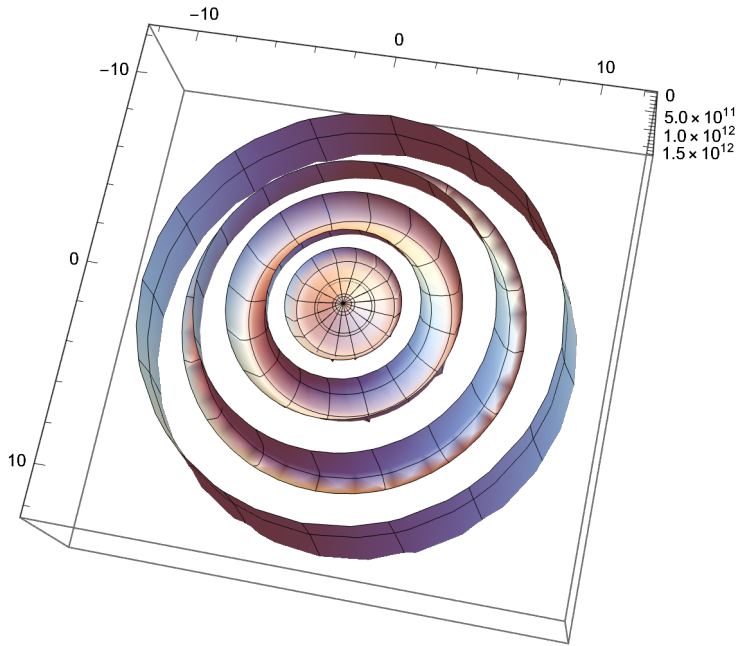
$$\frac{\sqrt{4 \pi \left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi}$$

### Expression for $\eta$ No. 3

$$\text{Plot} \left[ \frac{\sqrt{4 \pi \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi}, \{\theta, -13, 13\} \right]$$

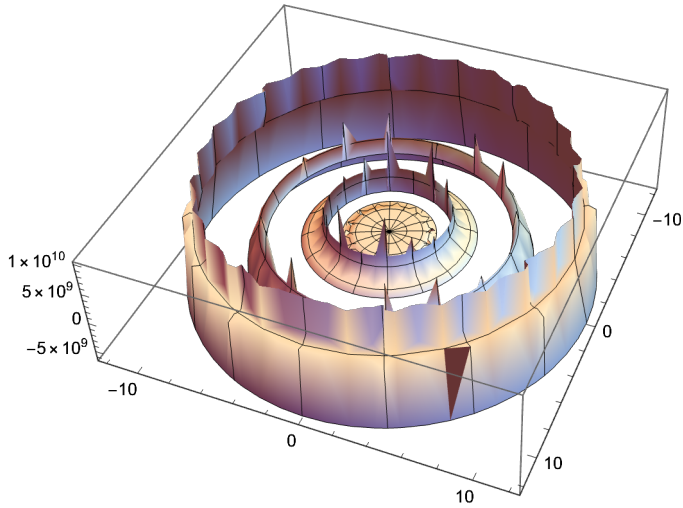


$$\text{RevolutionPlot3D}\left[\frac{\sqrt{4\pi\left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]\right)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



## First and Second Derivatives of Expression for Expression for $\eta$ No. 3

$$\text{RevolutionPlot3D}\left[\frac{\frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2}}{4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}}, \{\theta, -13, 13\}\right]$$



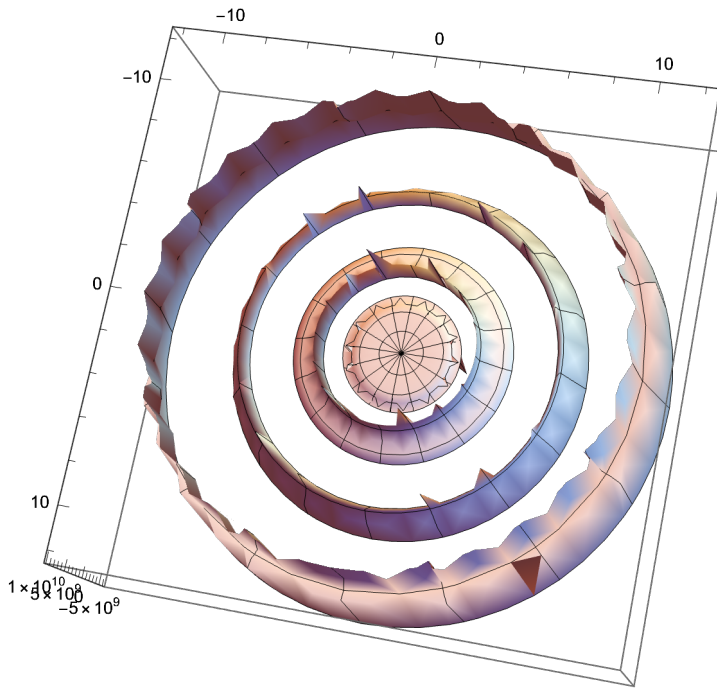
$$\frac{1}{6 (180 / \pi)} D\left[\frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{\frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2}}{4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}}$$

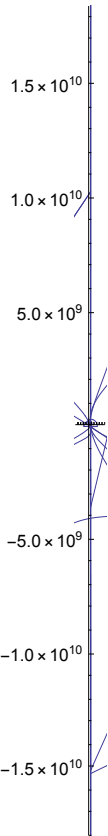
RevolutionPlot3D[  

$$\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\theta^4\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}$$
  

$$4320\sqrt{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{1\,166\,400\,c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}}, \{\theta, -13, 13\}]$$



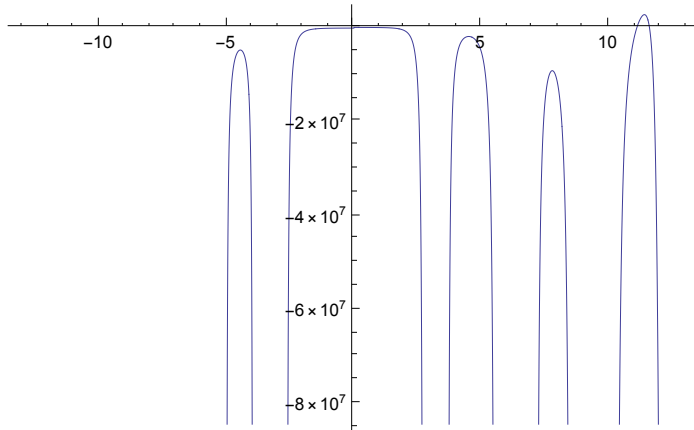
PolarPlot[
$$\frac{\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta} + \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}}{4320\sqrt{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}}, \{\theta, -13, 13\}]$$



$$\begin{aligned}
& 1 / (6 (180 / \pi)) \operatorname{D} \left[ \frac{\frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2}}{4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}}, \theta \right] \\
& \frac{1}{1080} \pi \left( - \left( \frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} \right)^2 / \right. \\
& \left. \left( 8640 \left( \frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \right. \\
& \left( \frac{37324800 c^2 \pi}{4 \pi - \theta} + \frac{74649600 c^2 \pi \theta}{(4 \pi - \theta)^2} + \frac{37324800 c^2 \pi \theta^2}{(4 \pi - \theta)^3} - \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \right. \\
& \left. \frac{18662400 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{4665600 c^2 \theta^4 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \\
& \left. \left. \frac{2332800 c^2 \theta^4 \operatorname{Csc}[\theta]^4}{\pi^2} \right) / \left( 4320 \sqrt{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}} \right) \right)
\end{aligned}$$



$$\text{Plot}\left[\frac{1}{1080} \pi \left( - \left( \frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\theta^4\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2} \right)^2 / \right. \right. \\ \left. \left( 8640 \left( \frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{1\,166\,400\,c^2\theta^4\text{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \right. \\ \left( \frac{37\,324\,800\,c^2\pi}{4\pi-\theta} + \frac{74\,649\,600\,c^2\pi\theta}{(4\pi-\theta)^2} + \frac{37\,324\,800\,c^2\pi\theta^2}{(4\pi-\theta)^3} - \frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2} - \right. \\ \left. \frac{4\,665\,600\,c^2\theta^4\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\theta^4\text{Csc}[\theta]^4}{\pi^2} \right) / \\ \left. \left( 4320 \sqrt{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{1\,166\,400\,c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}} \right) \right], \{\theta, -13, 13\}]$$

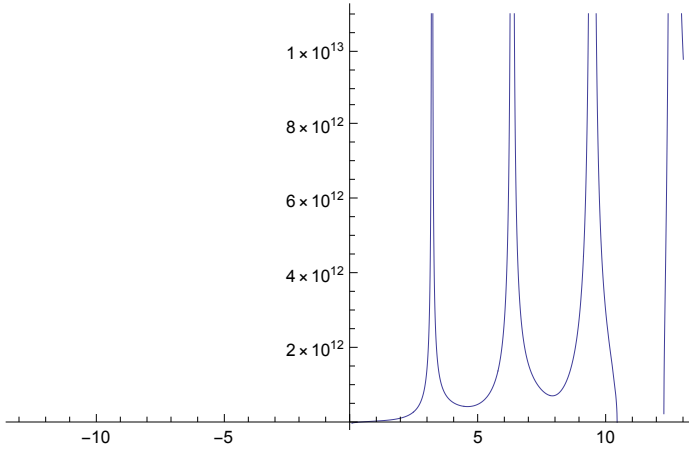


$$\text{PolarPlot}\left[\frac{1}{1080}\pi\left(-\left(\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta}+\frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2}-\frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi^2}+\frac{2\,332\,800\,c^2\theta^4\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}\right)^2/\right.\right. \\ \left.\left(288\pi\left(\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta}-\frac{1\,166\,400\,c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}\right)^{3/2}\right)+\right. \\ \left.\left(\frac{37\,324\,800\,c^2\pi}{4\pi-\theta}+\frac{74\,649\,600\,c^2\pi\theta}{(4\pi-\theta)^2}+\frac{37\,324\,800\,c^2\pi\theta^2}{(4\pi-\theta)^3}-\frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}+\frac{18\,662\,400\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}-\frac{4\,665\,600\,c^2\theta^4\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\theta^4\text{Csc}[\theta]^4}{\pi^2}\right)/\right. \\ \left.\left(144\pi\sqrt{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta}-\frac{1\,166\,400\,c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}}\right)\right),\{\theta,-13,13\}]$$

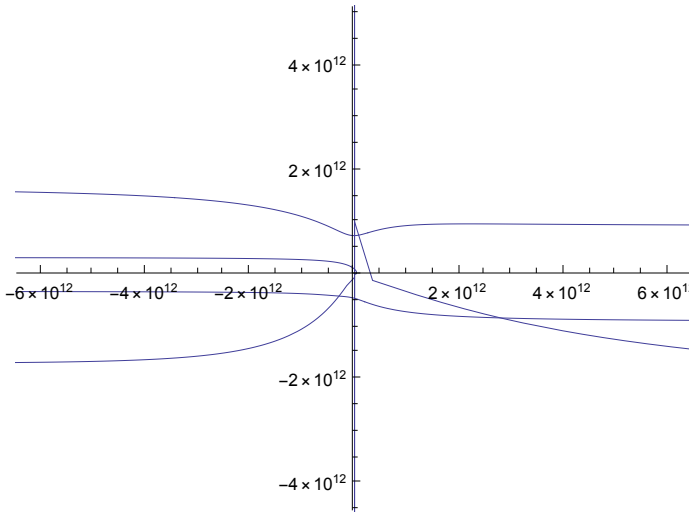


## Expression for $\eta$ No. 4

$$\text{Plot}\left[\frac{\sqrt{4\pi\left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{\sqrt{4\pi\left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}}{2\pi}, \{\theta, -13, 13\}\right]$$



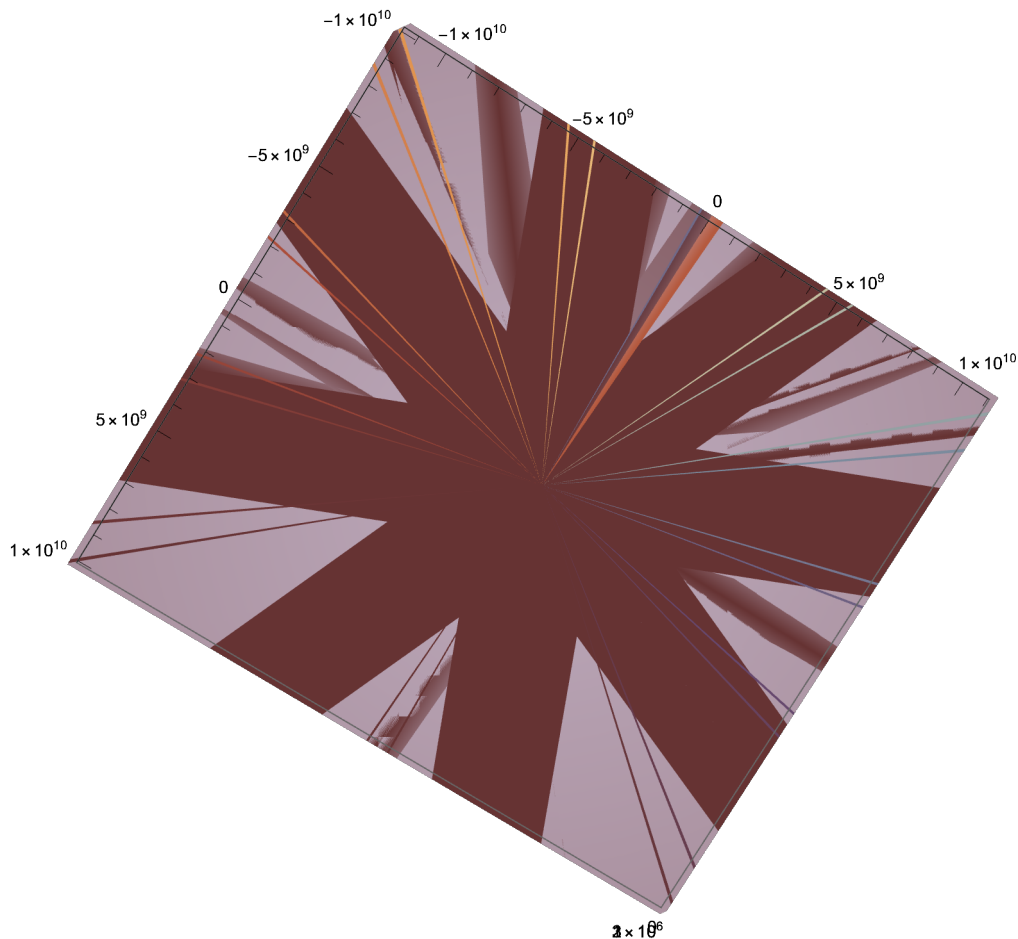
## The first and second derivatives of expression for $\eta$ No. 4

$$\frac{1}{1080}\pi D\left[\frac{\sqrt{4\pi\left(\frac{1080c\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\text{Csc}[\theta]}{\pi\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160c\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}}{2\pi}, \theta\right]$$

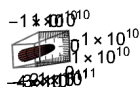
$$= \frac{-\frac{13996800c^2\theta^2}{4\pi-\theta} - \frac{4665600c^2\theta^3}{(4\pi-\theta)^2} + \frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi} - \frac{9331200c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}}{4320\sqrt{-\frac{4665600c^2\theta^3}{4\pi-\theta} + \frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}}}$$

$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400},\{\theta,-5 \pi, 5 \pi\}\right]$$

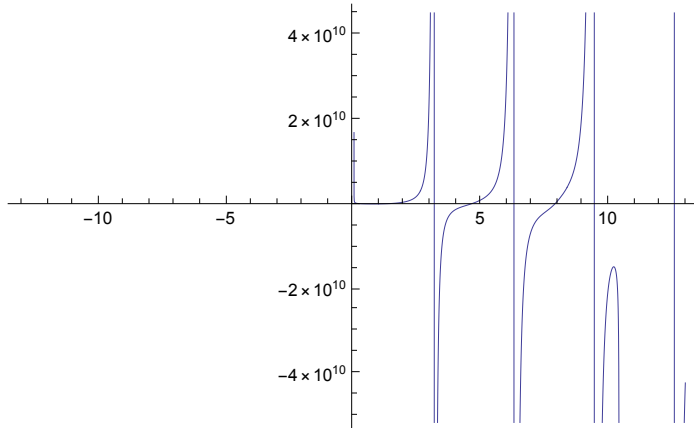
$$\text{RevolutionPlot3D}\left[\left\{\frac{-\frac{13996800 c^2 \theta^2}{4 \pi-\theta}-\frac{4665600 c^2 \theta^3}{(4 \pi-\theta)^2}+\frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi}-\frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi}}{4320 \sqrt{-\frac{4665600 c^2 \theta^3}{4 \pi-\theta}+\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi}}},\right. \\ \left.\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400}\right\},\{\theta,-35, 35\}\right]$$



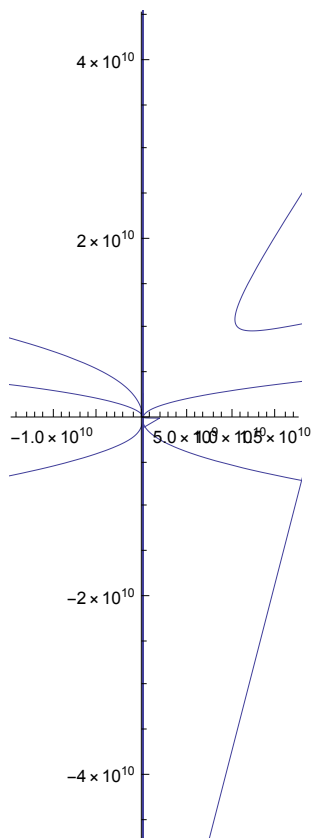
$$\text{RevolutionPlot3D}\left[\left\{\frac{-\frac{13996800 c^2 \theta^2}{4 \pi-\theta}-\frac{4665600 c^2 \theta^3}{(4 \pi-\theta)^2}+\frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi}-\frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi}}{4320 \sqrt{-\frac{4665600 c^2 \theta^3}{4 \pi-\theta}+\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi}}},\right. \\ \left.\frac{\pi^2 \left(-\frac{540 c}{\sqrt{4 \pi-\theta} \theta^{3/2}}+\frac{1080 c}{(4 \pi-\theta)^{3/2} \sqrt{\theta}}+\frac{1620 c \sqrt{\theta}}{(4 \pi-\theta)^{5/2}}\right)}{1166400}\right\},\{\theta,-.00072,.00072\}\right]$$



$$\text{Plot}\left[\frac{-\frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi}}{4320 \sqrt{-\frac{4665600 c^2 \theta^3}{4 \pi - \theta} + \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi}}}, \{\theta, -13, 13\}\right]$$

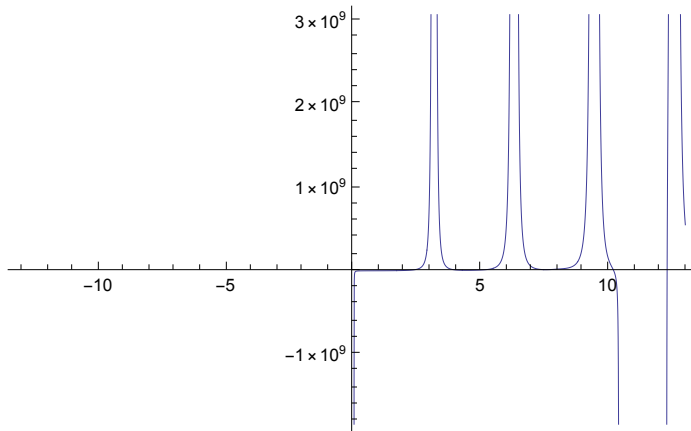


$$\text{PolarPlot}\left[\frac{-\frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi}}{4320 \sqrt{-\frac{4665600 c^2 \theta^3}{4 \pi - \theta} + \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi}}}, \{\theta, -13, 13\}\right]$$

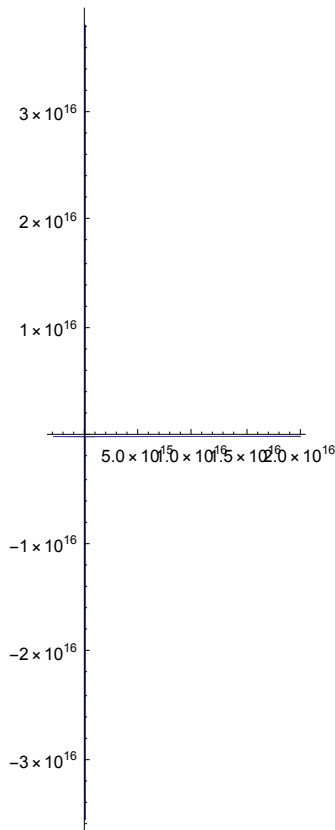


$$\begin{aligned}
& \frac{1}{1080} \pi \operatorname{D} \left[ \frac{-\frac{13\,996\,800\,c^2\,\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\,\theta^3}{(4\pi-\theta)^2} + \frac{13\,996\,800\,c^2\,\theta^2\,\operatorname{Csc}[\theta]^2}{\pi} - \frac{9\,331\,200\,c^2\,\theta^3\,\operatorname{Cot}[\theta]\,\operatorname{Csc}[\theta]^2}{\pi}}{4320\sqrt{-\frac{4\,665\,600\,c^2\,\theta^3}{4\pi-\theta} + \frac{4\,665\,600\,c^2\,\theta^3\,\operatorname{Csc}[\theta]^2}{\pi}}}, \theta \right] \\
& \frac{1}{1080} \pi \left( - \left( -\frac{13\,996\,800\,c^2\,\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\,\theta^3}{(4\pi-\theta)^2} + \right. \right. \\
& \quad \left. \left. \frac{13\,996\,800\,c^2\,\theta^2\,\operatorname{Csc}[\theta]^2}{\pi} - \frac{9\,331\,200\,c^2\,\theta^3\,\operatorname{Cot}[\theta]\,\operatorname{Csc}[\theta]^2}{\pi} \right)^2 \right. \\
& \quad \left. \left( 8640 \left( -\frac{4\,665\,600\,c^2\,\theta^3}{4\pi-\theta} + \frac{4\,665\,600\,c^2\,\theta^3\,\operatorname{Csc}[\theta]^2}{\pi} \right)^{3/2} \right) + \right. \\
& \quad \left( -\frac{27\,993\,600\,c^2\,\theta}{4\pi-\theta} - \frac{27\,993\,600\,c^2\,\theta^2}{(4\pi-\theta)^2} - \frac{9\,331\,200\,c^2\,\theta^3}{(4\pi-\theta)^3} + \frac{27\,993\,600\,c^2\,\theta\,\operatorname{Csc}[\theta]^2}{\pi} - \right. \\
& \quad \left. \frac{55\,987\,200\,c^2\,\theta^2\,\operatorname{Cot}[\theta]\,\operatorname{Csc}[\theta]^2}{\pi} + \frac{18\,662\,400\,c^2\,\theta^3\,\operatorname{Cot}[\theta]^2\,\operatorname{Csc}[\theta]^2}{\pi} + \right. \\
& \quad \left. \frac{9\,331\,200\,c^2\,\theta^3\,\operatorname{Csc}[\theta]^4}{\pi} \right) \bigg/ \left( 4320\sqrt{-\frac{4\,665\,600\,c^2\,\theta^3}{4\pi-\theta} + \frac{4\,665\,600\,c^2\,\theta^3\,\operatorname{Csc}[\theta]^2}{\pi}} \right) \bigg)
\end{aligned}$$

$$\text{Plot}\left[\frac{1}{1080}\pi\left(-\left(-\frac{13996800c^2\theta^2}{4\pi-\theta}-\frac{4665600c^2\theta^3}{(4\pi-\theta)^2}+\frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9331200c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)^2/\left(8640\left(-\frac{4665600c^2\theta^3}{4\pi-\theta}+\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}\right)^{3/2}\right)+\left(-\frac{27993600c^2\theta}{4\pi-\theta}-\frac{27993600c^2\theta^2}{(4\pi-\theta)^2}-\frac{9331200c^2\theta^3}{(4\pi-\theta)^3}+\frac{27993600c^2\theta\text{Csc}[\theta]^2}{\pi}-\frac{55987200c^2\theta^2\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}+\frac{18662400c^2\theta^3\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi}+\frac{9331200c^2\theta^3\text{Csc}[\theta]^4}{\pi}\right)/\left(4320\sqrt{-\frac{4665600c^2\theta^3}{4\pi-\theta}+\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}}\right)\right],\{\theta,-13,13\}]$$



$$\text{PolarPlot}\left[\frac{1}{1080}\pi\left(-\left(-\frac{13996800c^2\theta^2}{4\pi-\theta}-\frac{4665600c^2\theta^3}{(4\pi-\theta)^2}+\frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9331200c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)^2/\right.\right. \\ \left.\left.\left(8640\left(-\frac{4665600c^2\theta^3}{4\pi-\theta}+\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}\right)^{3/2}\right)+\left(-\frac{27993600c^2\theta}{4\pi-\theta}-\frac{27993600c^2\theta^2}{(4\pi-\theta)^2}-\frac{9331200c^2\theta^3}{(4\pi-\theta)^3}+\frac{27993600c^2\theta\text{Csc}[\theta]^2}{\pi}-\frac{55987200c^2\theta^2\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}+\frac{18662400c^2\theta^3\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi}+\frac{9331200c^2\theta^3\text{Csc}[\theta]^4}{\pi}\right)/\right.\right. \\ \left.\left.\left(4320\sqrt{-\frac{4665600c^2\theta^3}{4\pi-\theta}+\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi}}\right)\right),\{\theta,-13,13\}\right]$$



## V. Deriving Acceleration from the Second Principle and

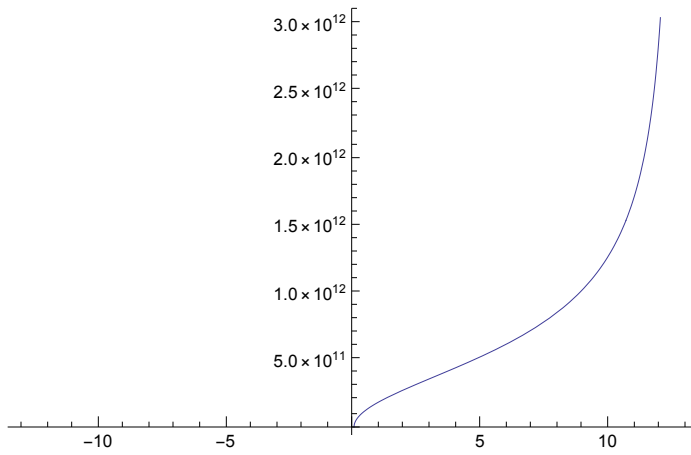


## Plotting Correlations (r).

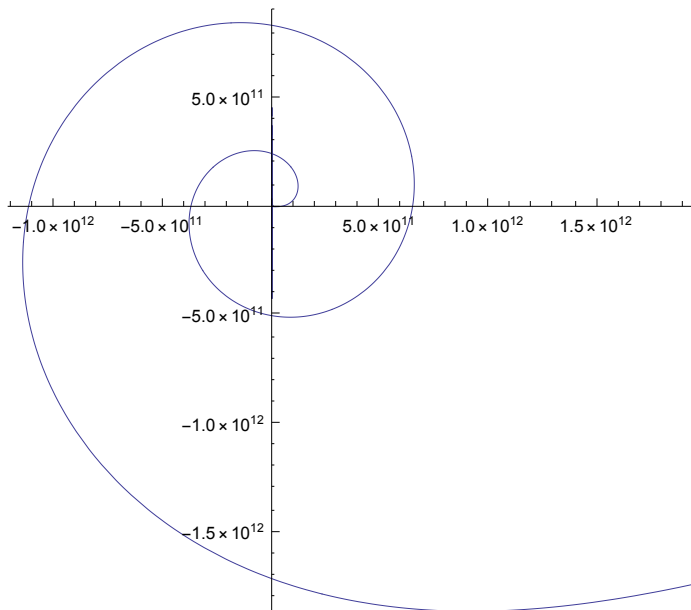
$$r = \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} = \frac{2\pi r \sin[\theta]}{\sqrt{4\pi\theta - \theta^2}} = \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}}$$

### Expression for r, no. 1

$$\text{Plot}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}}, \{\theta, -13, 13\}\right]$$

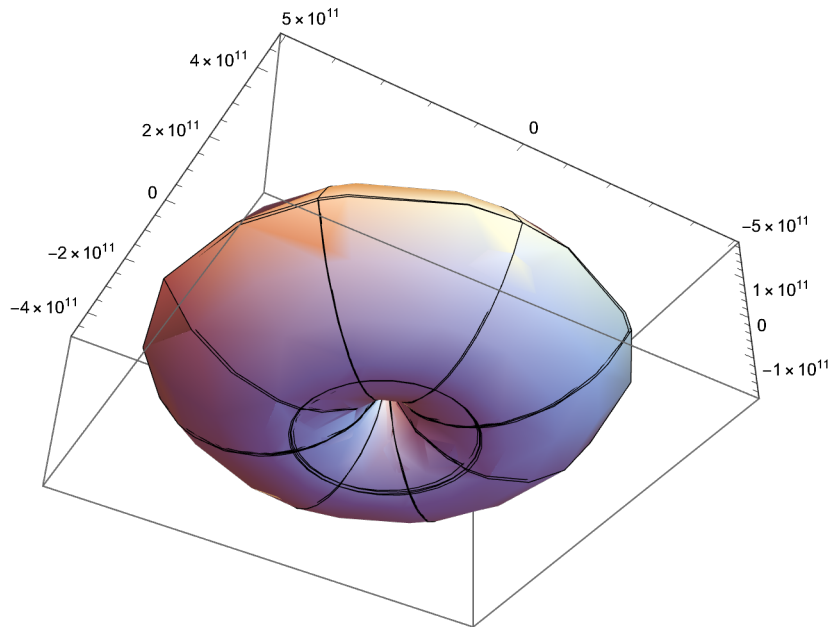


$$\text{Solve}\left[\beta == \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], \theta\right]$$

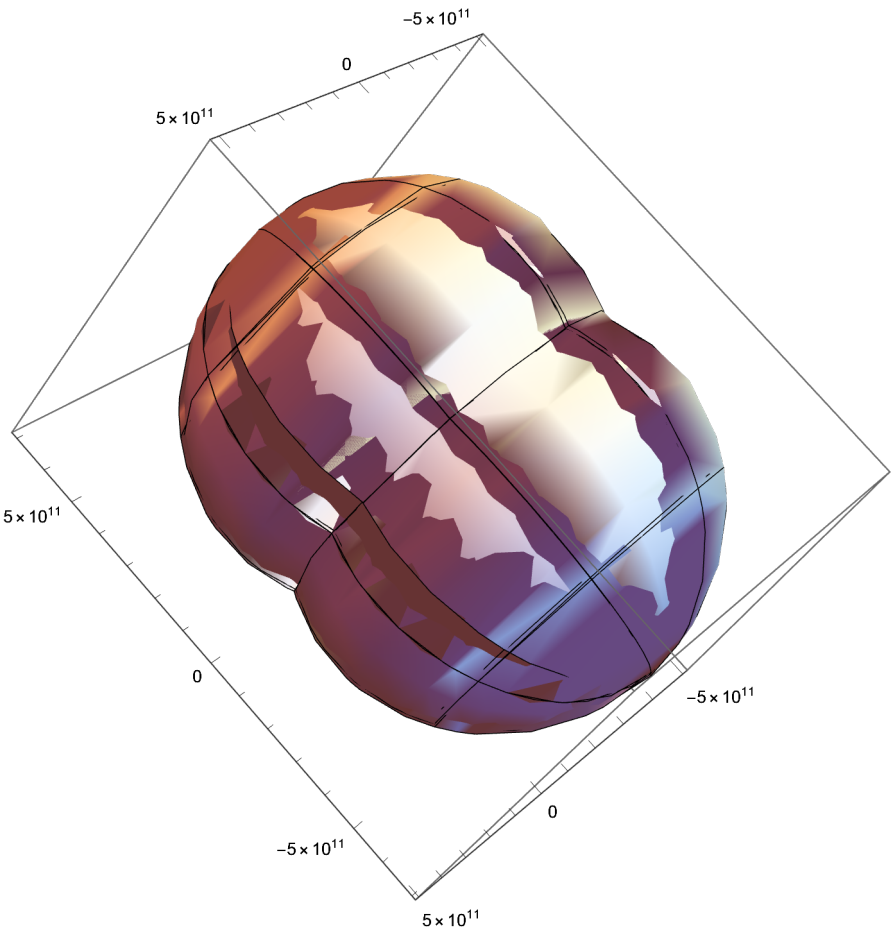
$$\left\{\left\{\theta \rightarrow 2\pi\left(1 - \sqrt{1 - \text{Sin}[\beta]^2}\right)\right\}, \left\{\theta \rightarrow 2\pi\left(1 + \sqrt{1 - \text{Sin}[\beta]^2}\right)\right\}\right\}$$

$$c := (2.99792458 * 10^8)$$

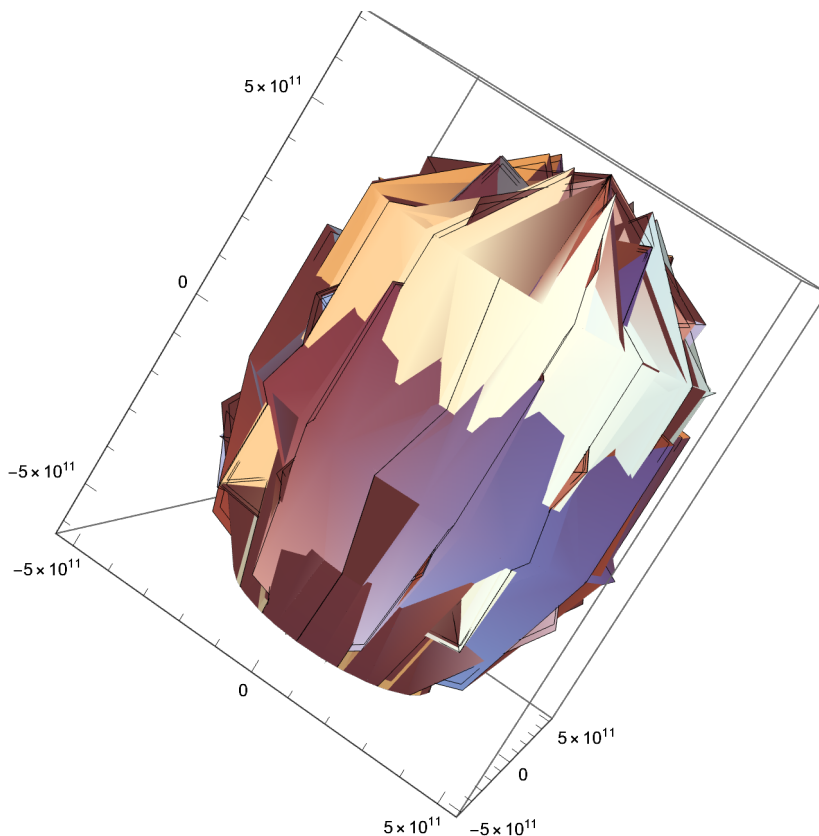
$$\text{SphericalPlot3D}\left[\frac{2160 c \sqrt{2\pi\left(1 - \sqrt{1 - \text{Sin}[\beta]^2}\right)}}{\sqrt{4\pi - \left(\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)}}, \{\beta, -2\pi, 2\pi\}, \{\theta, -4\pi, 4\pi\}\right]$$



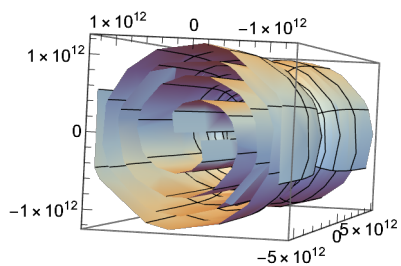
SphericalPlot3D[ $\frac{2160\,c\,\sqrt{2\,\pi\left(1+\sqrt{1-\sin[\beta]^2}\right)}}{\sqrt{4\,\pi-\left(\text{ArcSin}\left[\frac{\sqrt{(4\,\pi-\theta)}\,\theta}{2\,\pi}\right]\right)}}$ , { $\beta$ ,  $-2\,\pi$ ,  $2\,\pi$ }, { $\theta$ ,  $-20\,\pi$ ,  $20\,\pi$ }]



$$\text{SphericalPlot3D}\left[\frac{2160\,c\,\sqrt{2\,\pi\left(1+\sqrt{1-\text{Sin}[\beta]^2}\right)}}{\sqrt{4\,\pi-\left(\text{ArcSin}\left[\frac{\sqrt{(4\,\pi-\theta)}\,\theta}}{2\,\pi}\right]\right)}},\{\beta,-200\,\pi,200\,\pi\},\{\theta,-2\,\pi,2\,\pi\}\right]$$



$$\text{SphericalPlot3D}\left[\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-2\,\pi\left(1+\sqrt{1-\text{Sin}[\beta]^2}\right)}},\{\beta,-\pi,\pi\},\{\theta,-13,13\}\right]$$

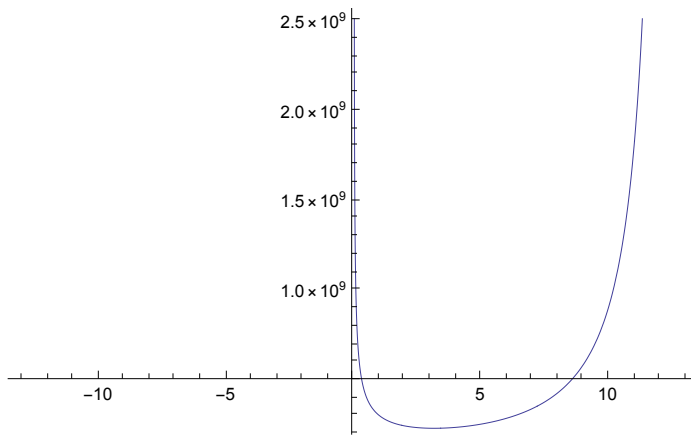


The first and second derivatives of expression for r no. 1

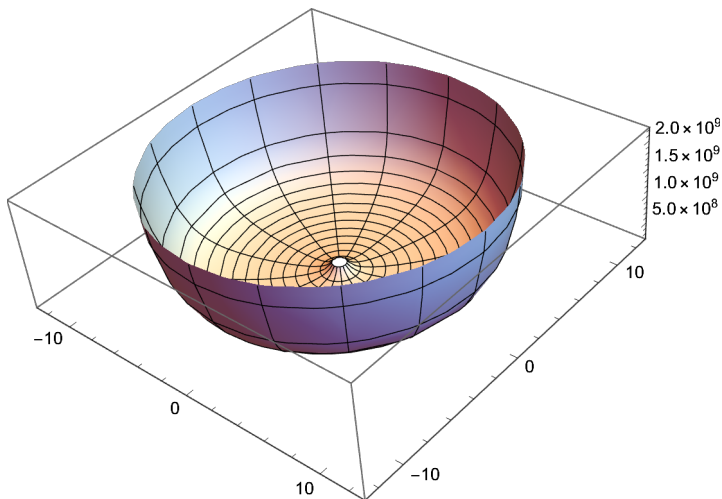
$$\frac{1}{1080} \pi D \left[ \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}}, \theta \right]$$

$$\frac{\pi \left( \frac{1080 c}{\sqrt{4\pi - \theta} \sqrt{\theta}} + \frac{1080 c \sqrt{\theta}}{(4\pi - \theta)^{3/2}} \right)}{1080}$$

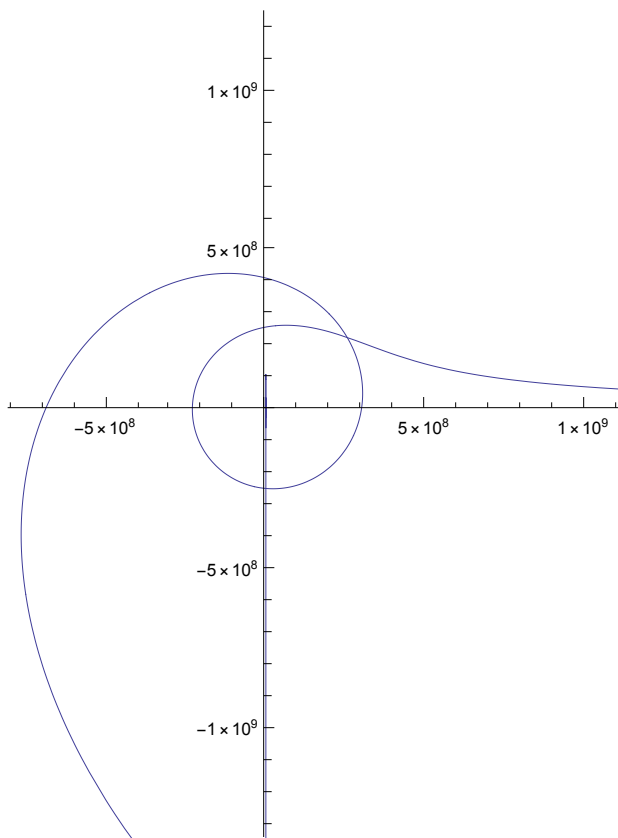
$$\text{Plot} \left[ \frac{\pi \left( \frac{1080 c}{\sqrt{4\pi - \theta} \sqrt{\theta}} + \frac{1080 c \sqrt{\theta}}{(4\pi - \theta)^{3/2}} \right)}{1080}, \{\theta, -13, 13\} \right]$$



$$\text{RevolutionPlot3D} \left[ \frac{\pi \left( \frac{1080 c}{\sqrt{4\pi - \theta} \sqrt{\theta}} + \frac{1080 c \sqrt{\theta}}{(4\pi - \theta)^{3/2}} \right)}{1080}, \{\theta, -13, 13\} \right]$$

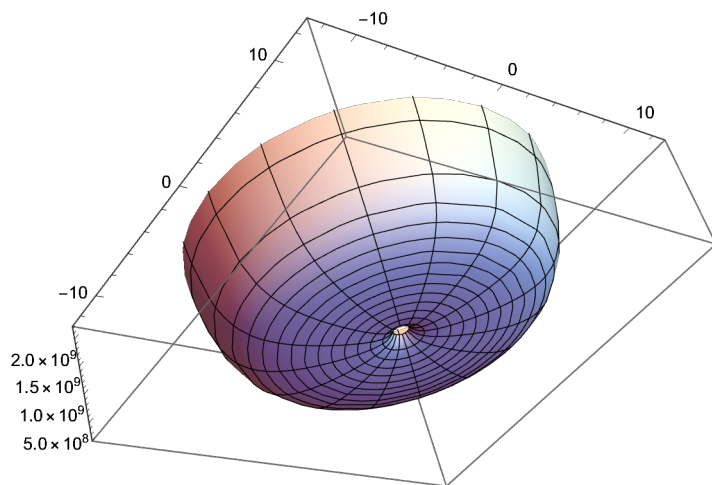


**PolarPlot** $\left[\frac{\pi \left( \frac{1080 c}{\sqrt{4 \pi - \theta}} \sqrt{\theta} + \frac{1080 c \sqrt{\theta}}{(4 \pi - \theta)^{3/2}} \right)}{1080}, \{\theta, -13, 13\}\right]$



**SphericalPlot3D** $\left[\frac{\pi \left( \frac{1080 c}{\sqrt{4 \pi - \theta}} \sqrt{\theta} + \frac{1080 c \sqrt{\theta}}{(4 \pi - \theta)^{3/2}} \right)}{1080}, \{\beta, -13, 13\}, \{\theta, -13, 13\}\right]$

**RevolutionPlot3D** $\left[\frac{\pi \left( \frac{1080 c}{\sqrt{4 \pi - \theta}} \sqrt{\theta} + \frac{1080 c \sqrt{\theta}}{(4 \pi - \theta)^{3/2}} \right)}{1080}, \{\theta, -13, 13\}\right]$

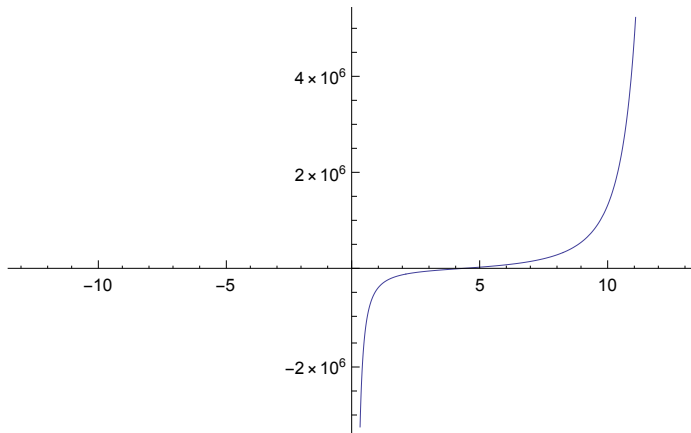


$$\frac{1}{1080} \pi D \left[ \frac{1}{1080} \pi D \left[ \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}, \theta \right], \theta \right]$$

$$\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}$$

$$\left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)$$

$$\text{Plot} \left[ \frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -13, 13\} \right]$$



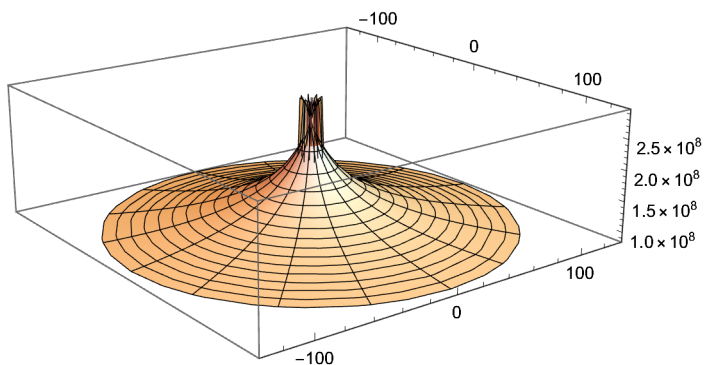
$$c := (2.99792458 * 10^8)$$

$$\text{RevolutionPlot3D} \left[ \left\{ \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}, \frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400} \right\}, \{\theta, -.0000001, .00000001\} \right]$$

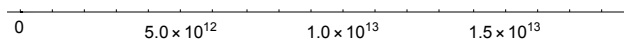
$$\text{Solve} \left[ \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta} == -(\nu^2 / c^2), \nu \right]$$

$$\left\{ \left\{ \nu \rightarrow -\frac{2.99792 \times 10^8 \sqrt{12.5664 - \frac{39.4784}{12.5664 - 1. \theta}}}{\sqrt{12.5664 - 1. \theta}} \right\}, \left\{ \nu \rightarrow \frac{2.99792 \times 10^8 \sqrt{12.5664 - \frac{39.4784}{12.5664 - 1. \theta}}}{\sqrt{12.5664 - 1. \theta}} \right\} \right\}$$

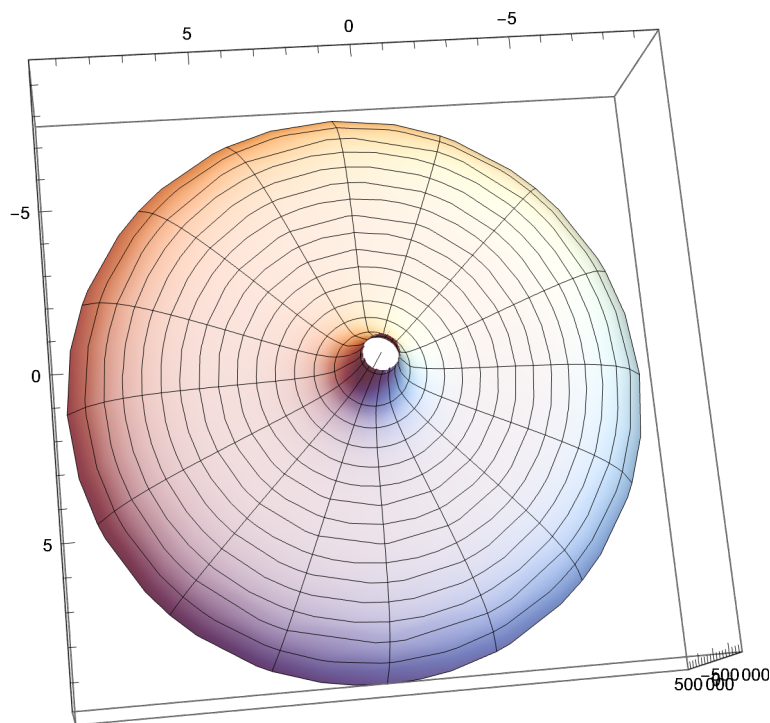
$\text{RevolutionPlot3D}\left[\frac{2.99792458 \cdot 10^8 \sqrt{12.566370614359172 - \frac{39.47841760435743}{12.566370614359172 - 1. \cdot \theta}}}{\sqrt{12.566370614359172 - 1. \cdot \theta}}, \{\theta, -130, 130\}\right]$



$\text{PolarPlot}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -13, 13\}\right]$

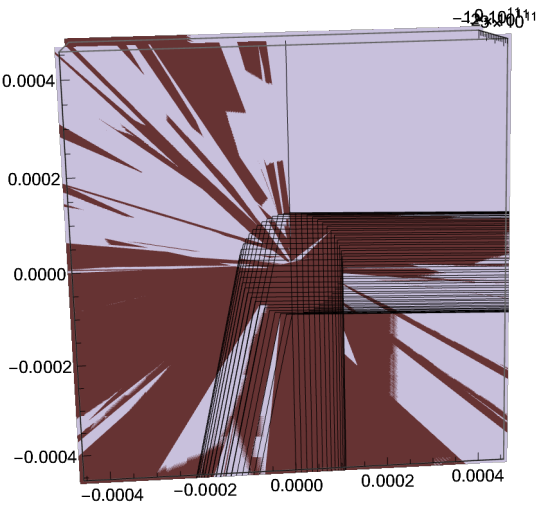


$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -3 \pi, 3 \pi\}\right]$





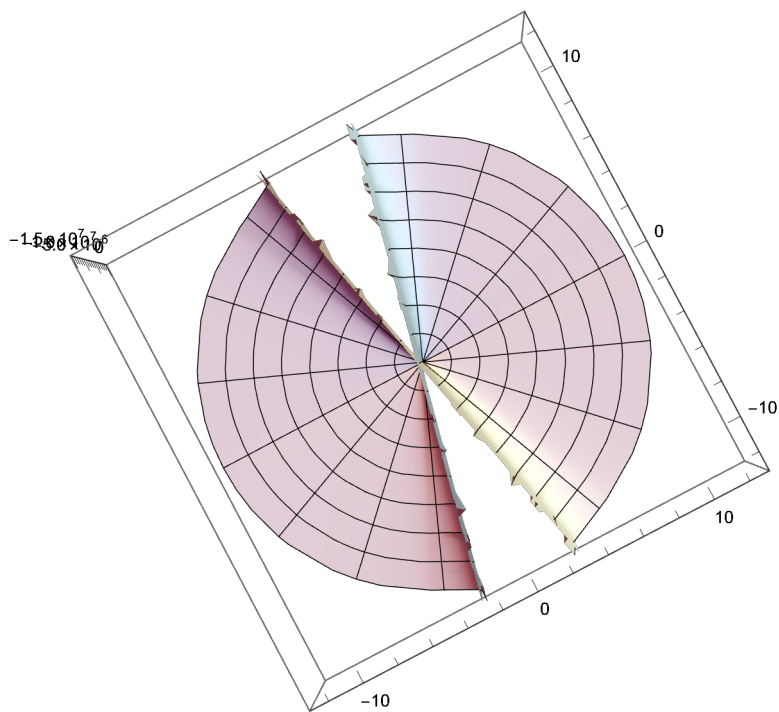
RevolutionPlot3D $\left[\frac{\pi^2\left(-\frac{540\,c}{\sqrt{4\,\pi-\theta}\,\theta^{3/2}}+\frac{1080\,c}{(4\,\pi-\theta)^{3/2}\sqrt{\theta}}+\frac{1620\,c\sqrt{\theta}}{(4\,\pi-\theta)^{5/2}}\right)}{1\,166\,400},\{\theta,-2\,\pi,2\,\pi\}\right]$



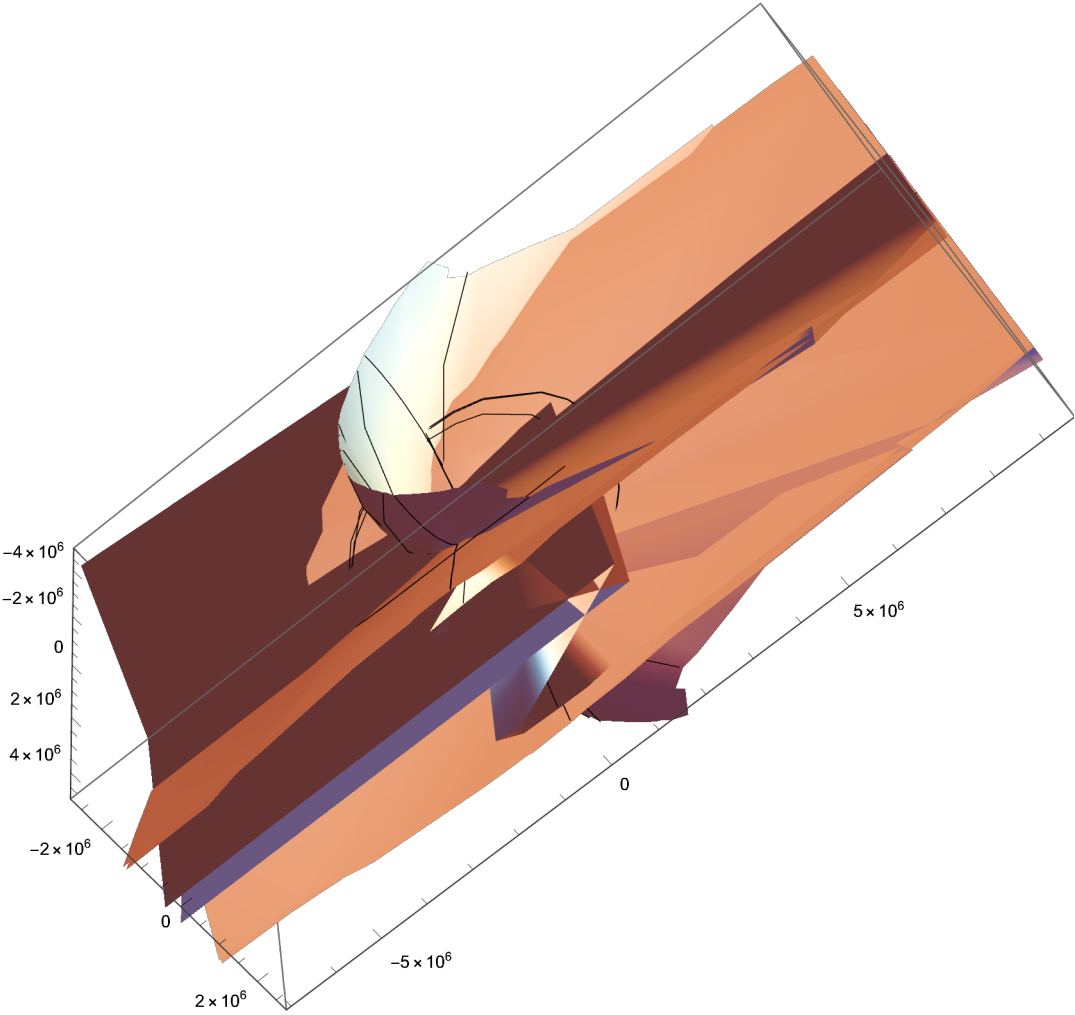
$\left\{\left\{\theta\rightarrow 2\,\pi\left(1-\sqrt{1-\text{Sin}[\beta]^2}\right)\right\},\left\{\theta\rightarrow 2\,\pi\left(1+\sqrt{1-\text{Sin}[\beta]^2}\right)\right\}\right\}$

RevolutionPlot3D[

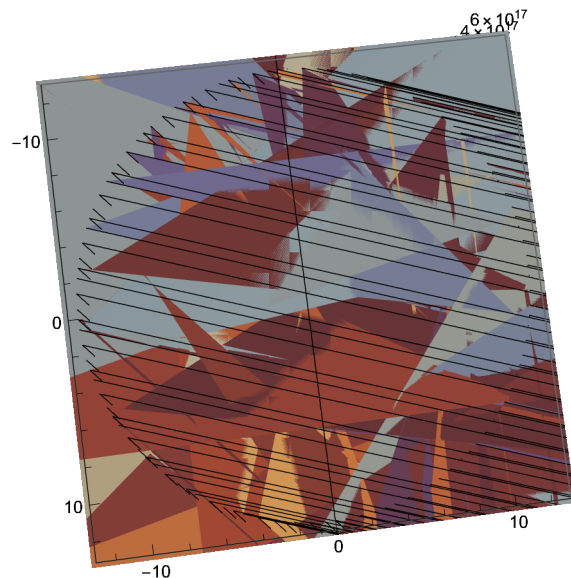
$$\frac{1}{1166400} \pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - 2 \pi \left(1 - \sqrt{1 - \sin[\beta]^2}\right)} \left(2 \pi \left(1 - \sqrt{1 - \sin[\beta]^2}\right)\right)^{3/2}} + \frac{1080 c}{\left(4 \pi - 2 \pi \left(1 - \sqrt{1 - \sin[\beta]^2}\right)\right)^{3/2} \sqrt{2 \pi \left(1 - \sqrt{1 - \sin[\beta]^2}\right)}} + \frac{1620 c \sqrt{2 \pi \left(1 - \sqrt{1 - \sin[\beta]^2}\right)}}{\left(4 \pi - 2 \pi \left(1 - \sqrt{1 - \sin[\beta]^2}\right)\right)^{5/2}} \right), \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}]$$



SphericalPlot3D $\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - 2 \pi \left( 1 - \sqrt{1 - \text{Sin}[\beta]^2} \right)^2} 2 \pi \left( 1 - \sqrt{1 - \text{Sin}[\beta]^2} \right)^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$ ,

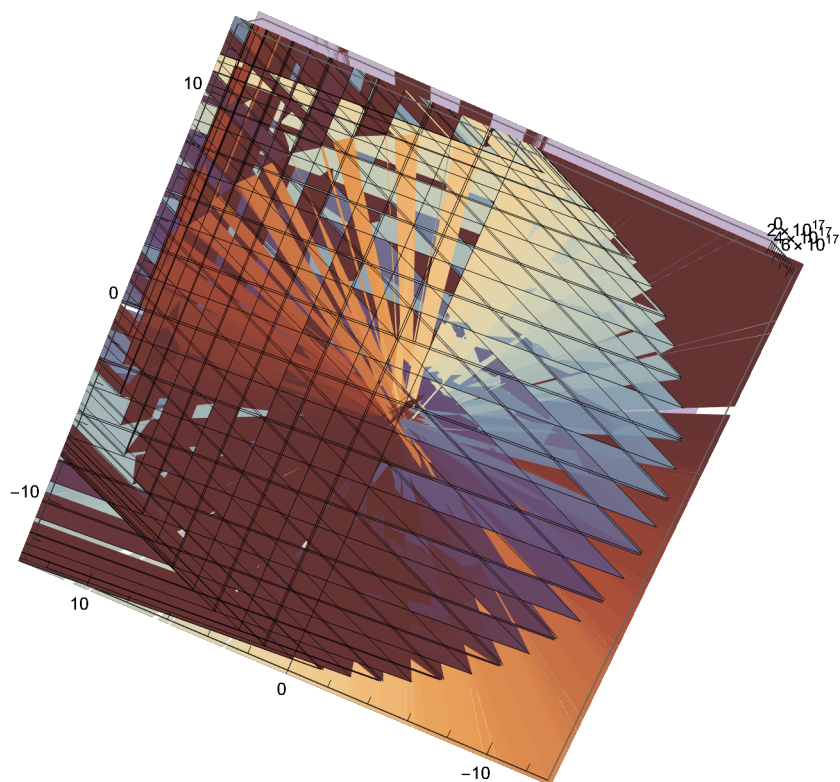


$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -5 \pi, 5 \pi\}\right]$$



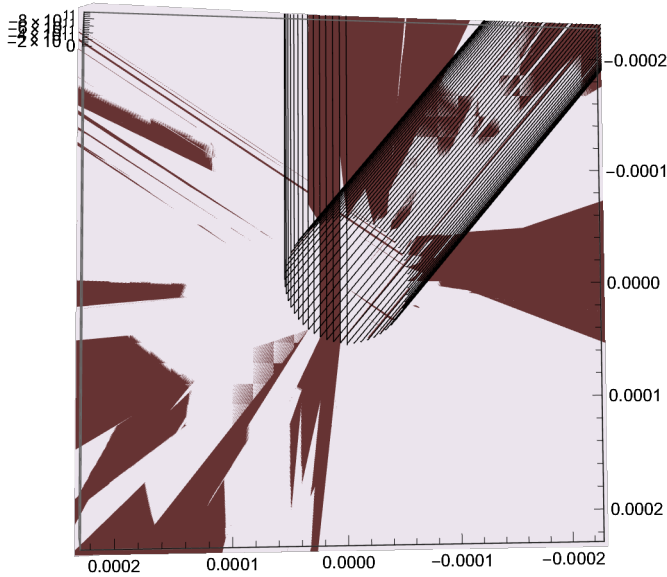
$c := (2.99792458 * 10^8)$

$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -13, 13\}\right]$$



$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -2 \pi, 2 \pi\}\right]$$

$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{540 c}{\sqrt{4 \pi - \theta} \theta^{3/2}} + \frac{1080 c}{(4 \pi - \theta)^{3/2} \sqrt{\theta}} + \frac{1620 c \sqrt{\theta}}{(4 \pi - \theta)^{5/2}} \right)}{1166400}, \{\theta, -\pi, \pi\}\right]$$



When  $\frac{2 \pi r \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} = r$ , we say that  $r = 1$ , or that  $r = \sqrt{1 + 3 + 5 + \dots (2 n - 1)}$ ,

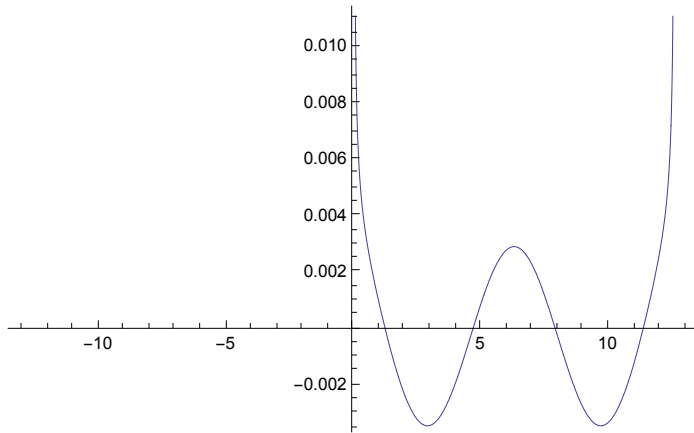
where  $n$  is the position in the series of the number.

$r = 1$

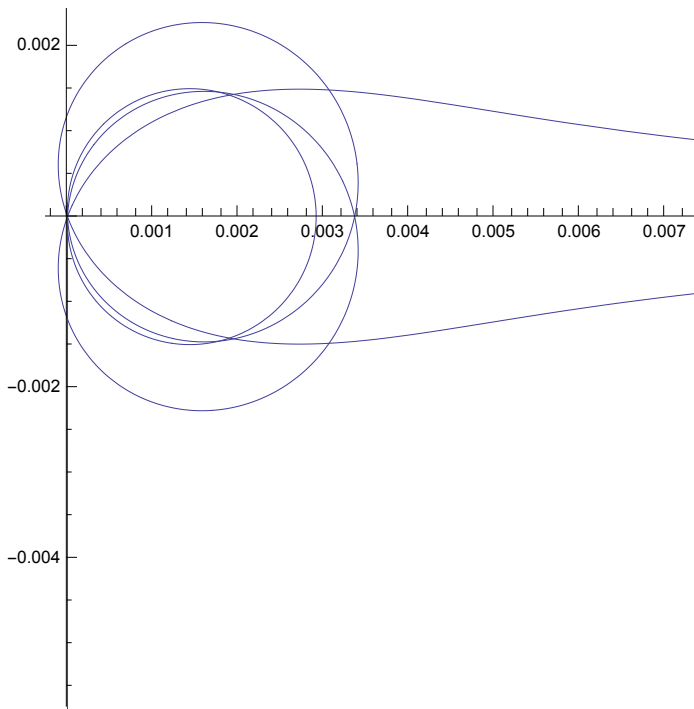
$$\frac{1}{1080} \pi D\left[\frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta\right]$$

$$\frac{\pi \left( \frac{2 \pi \cos[\theta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{\pi (4 \pi - 2 \theta) \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} \right)}{1080}$$

$$\text{Plot}\left[\frac{\pi \left( \frac{2 \pi \cos[\theta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{\pi (4 \pi - 2 \theta) \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} \right)}{1080}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{\pi \left( \frac{2 \pi \cos[\theta]}{\sqrt{4 \pi \theta - \theta^2}} - \frac{\pi (4 \pi - 2 \theta) \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} \right)}{1080}, \{\theta, -13, 13\}\right]$$



$$r = \frac{\sqrt{\frac{1}{4 \pi - \theta} + \frac{4 \pi}{\theta^2} - \frac{3}{\theta}}}{4 \pi \sqrt{\theta}} == \left( \sqrt{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}} \right)$$

$$\frac{1}{1080} \pi D\left[\frac{1}{1080} \pi D\left[\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta, \beta, r\right], \theta, \beta, r\right]$$

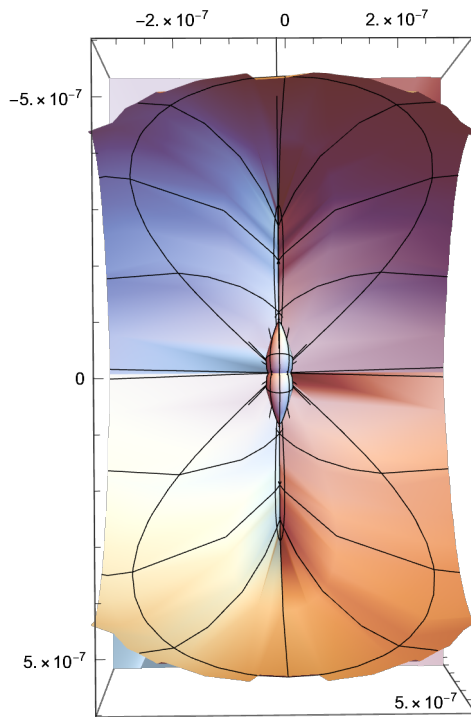
0

$$\frac{1}{1080} \pi D \left[ \frac{1}{1080} \pi D \left[ \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta, \beta \right], \theta, \beta \right]$$

SphericalPlot3D[

$$\pi \left( -\frac{\pi^2 \frac{\sqrt{\frac{1}{4 \pi - \theta^2} - \frac{4 \pi^3}{\theta^2}}}{4 \pi \sqrt{\theta}} (4 \pi - 2 \theta)^2 \sin[\beta]}{720 (4 \pi \theta - \theta^2)^{5/2}} - \frac{\pi^2 \left( \sqrt{\frac{1 + \frac{4 \pi^2}{(4 \pi - \theta)^2} - \frac{4 \pi}{4 \pi - \theta}}}{(4 \pi \theta - \theta^2)^{3/2}} \right) \sin[\beta]}{540 (4 \pi \theta - \theta^2)^{3/2}} \right), \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}]$$

1080

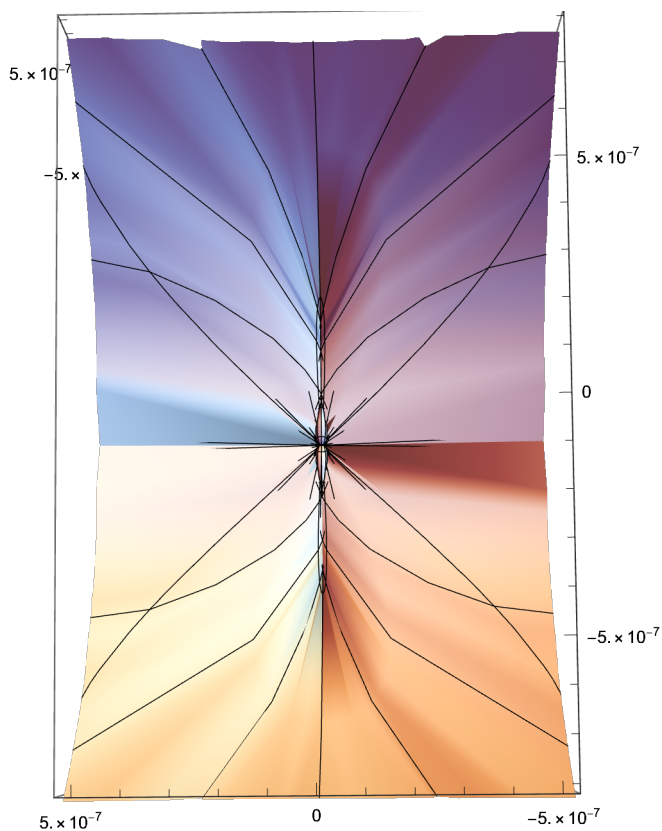


SphericalPlot3D[

$$\pi \left( -\frac{\pi^2 \sqrt{1 + \frac{4\pi^2}{(4\pi-\theta)^2} - \frac{4\pi}{4\pi-\theta}} (4\pi-2\theta)^2 \sin[\beta]}{720 (4\pi\theta-\theta^2)^{5/2}} - \frac{\pi^2 \left( \frac{\sqrt{\frac{1}{4\pi-\theta} + \frac{4\pi}{\theta^2} - \frac{3}{\theta}}}{4\pi\sqrt{\theta}} \right) \sin[\beta]}{540 (4\pi\theta-\theta^2)^{3/2}} \right)$$

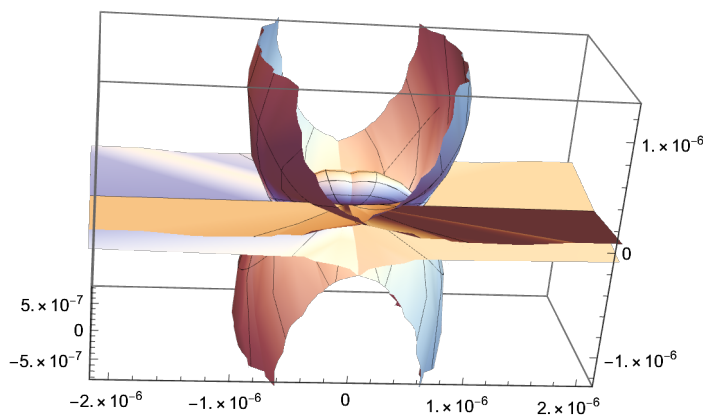
1080

, {θ, -4π, 4π}, {β, -π, π}]



SphericalPlot3D[  

$$\pi \left( -\frac{\pi^2 (4\pi-2\theta)^2 \sin[\beta]}{720 (4\pi\theta-\theta^2)^{5/2}} - \frac{\pi^2 \sin[\beta]}{540 (4\pi\theta-\theta^2)^{3/2}} \right)$$
  
 1080  
 , {θ, -4π, 4π}, {β, -π, π}]

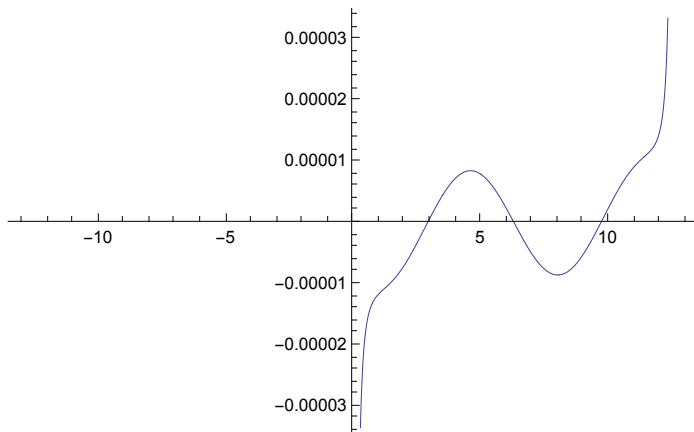




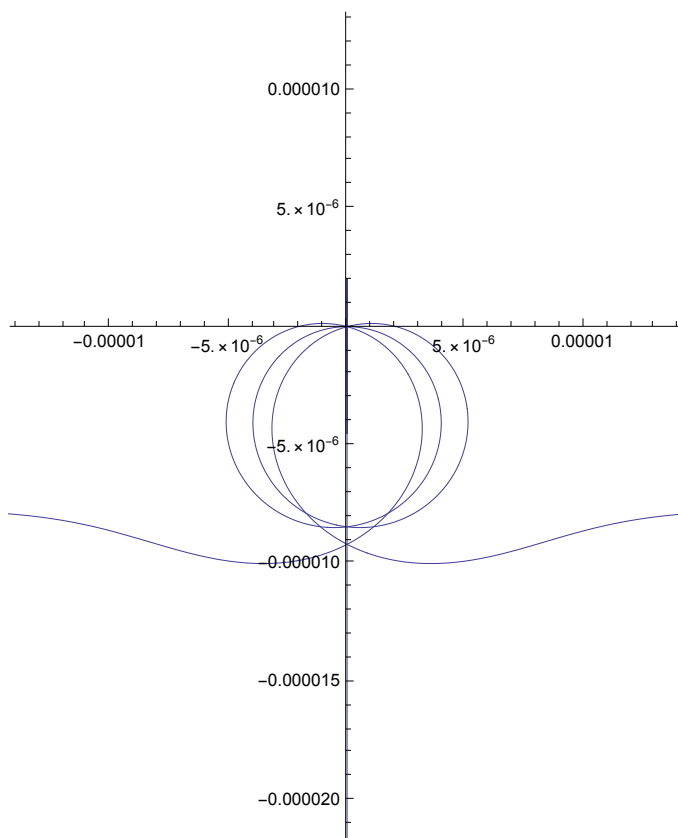
$$\frac{1}{1080} \pi D \left[ \frac{1}{1080} \pi D \left[ \frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta \right], \theta \right]$$

$$\frac{\pi^2 \left( -\frac{2 \pi (4 \pi - 2 \theta) \cos[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} + \frac{3 \pi (4 \pi - 2 \theta)^2 \sin[\theta]}{2 (4 \pi \theta - \theta^2)^{5/2}} + \frac{2 \pi \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} - \frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)}{1166400}$$

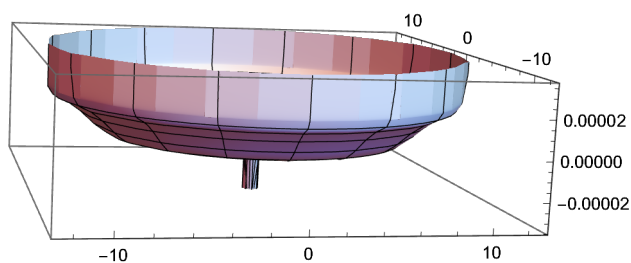
$$\text{Plot} \left[ \frac{\pi^2 \left( -\frac{2 \pi (4 \pi - 2 \theta) \cos[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} + \frac{3 \pi (4 \pi - 2 \theta)^2 \sin[\theta]}{2 (4 \pi \theta - \theta^2)^{5/2}} + \frac{2 \pi \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} - \frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)}{1166400}, \{\theta, -13, 13\} \right]$$



$$\text{PolarPlot}\left[\frac{\pi^2 \left( -\frac{2 \pi (4 \pi - 2 \theta) \cos[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} + \frac{3 \pi (4 \pi - 2 \theta)^2 \sin[\theta]}{2 (4 \pi \theta - \theta^2)^{5/2}} + \frac{2 \pi \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} - \frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)}{1166400}, \{\theta, -13, 13\}\right]$$

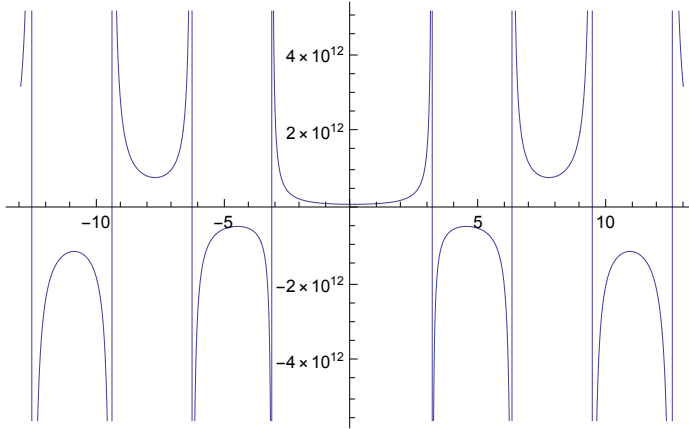


$$\text{RevolutionPlot3D}\left[\frac{\pi^2 \left( -\frac{2 \pi (4 \pi - 2 \theta) \cos[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} + \frac{3 \pi (4 \pi - 2 \theta)^2 \sin[\theta]}{2 (4 \pi \theta - \theta^2)^{5/2}} + \frac{2 \pi \sin[\theta]}{(4 \pi \theta - \theta^2)^{3/2}} - \frac{2 \pi \sin[\theta]}{\sqrt{4 \pi \theta - \theta^2}} \right)}{1166400}, \{\theta, -13, 13\}\right]$$

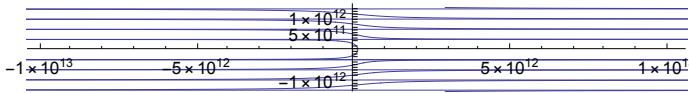


### Expression for r no. 3

$$\text{Plot}\left[\frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}}, \{\theta, -13, 13\}\right]$$



$$\text{PolarPlot}\left[\frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}}, \{\theta, -13, 13\}\right]$$

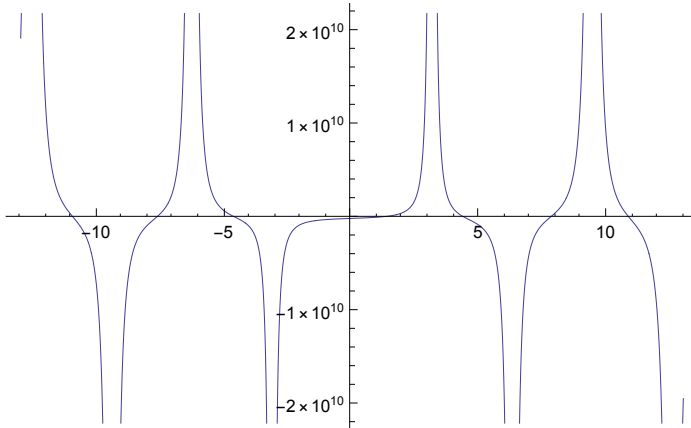


### The First and Second Derivatives of expression for r no. 3

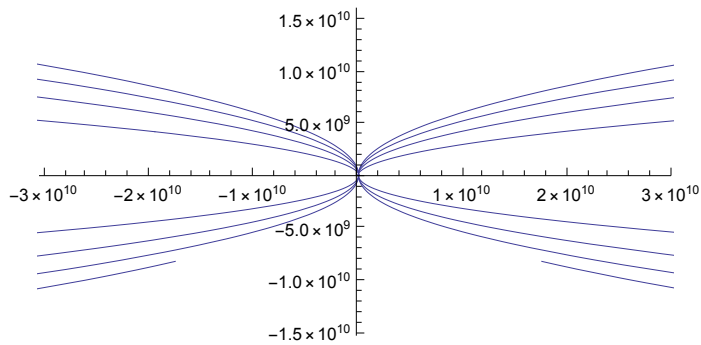
$$\frac{1}{1080} \pi D\left[\frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}}, \theta\right]$$

$$\frac{1}{1080} \pi \left( \frac{540 \csc(4\pi - 2\theta) \sqrt{\theta} \text{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta) \theta}} + \frac{540 \csc \sqrt{(4\pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta}} + \frac{540 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \text{Csc}[\theta]}{\pi (4\pi - \theta)^{3/2}} - \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \text{Cot}[\theta] \text{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)$$

$$\text{Plot}\left[\frac{1}{1080} \pi \left( \frac{540 \csc(4\pi - 2\theta) \sqrt{\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta)\theta}} + \frac{540 \csc \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta}} + \frac{540 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi (4\pi - \theta)^{3/2}} - \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \cot[\theta] \csc[\theta]}{\pi \sqrt{4\pi - \theta}} \right), \{\theta, -13, 13\}\right]$$

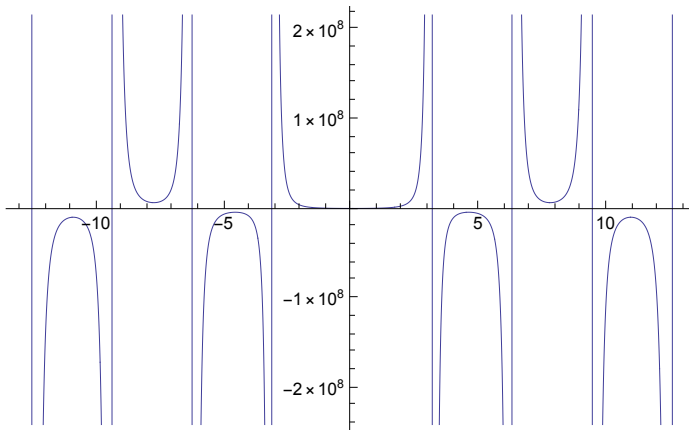



$$\text{PolarPlot}\left[\frac{1}{1080} \pi \left( \frac{540 \csc(4\pi - 2\theta) \sqrt{\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta)\theta}} + \frac{540 \csc \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta}} + \frac{540 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi (4\pi - \theta)^{3/2}} - \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \cot[\theta] \csc[\theta]}{\pi \sqrt{4\pi - \theta}} \right), \{\theta, -13, 13\}\right]$$



$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \frac{1}{1080} \pi D \left[ \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}}, \theta \right], \theta \right] \\
& \frac{1}{1166400} \pi^2 \\
& \left( -\frac{270 \csc(4\pi - 2\theta)^2 \sqrt{\theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} (4\pi - \theta) \theta^{3/2}} + \frac{540 \csc(4\pi - 2\theta) \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sqrt{(4\pi - \theta) \theta}} + \frac{540 \csc(4\pi - 2\theta) \sqrt{\theta} \operatorname{Csc}[\theta]}{\pi (4\pi - \theta)^{3/2} \sqrt{(4\pi - \theta) \theta}} - \right. \\
& \frac{1080 \csc \sqrt{\theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta) \theta}} - \frac{270 \csc \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \theta^{3/2}} + \frac{540 \csc \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi (4\pi - \theta)^{3/2} \sqrt{\theta}} + \\
& \frac{810 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi (4\pi - \theta)^{5/2}} - \frac{1080 \csc(4\pi - 2\theta) \sqrt{\theta} \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta) \theta}} - \\
& \frac{1080 \csc \sqrt{(4\pi - \theta) \theta} \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta}} - \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]}{\pi (4\pi - \theta)^{3/2}} + \\
& \left. \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} + \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]^3}{\pi \sqrt{4\pi - \theta}} \right)
\end{aligned}$$

$$\text{Plot}\left[\frac{1}{1166400}\pi^2\left(-\frac{270\csc(4\pi-2\theta)^2\sqrt{\theta}\csc[\theta]}{\pi\sqrt{4\pi-\theta}(4\pi-\theta)\theta^{3/2}}+\frac{540\csc(4\pi-2\theta)\csc[\theta]}{\pi\sqrt{4\pi-\theta}\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}}+\right.\right. \\
\left.\left.\frac{540\csc(4\pi-2\theta)\sqrt{\theta}\csc[\theta]}{\pi(4\pi-\theta)^{3/2}\sqrt{(4\pi-\theta)\theta}}-\frac{1080\csc\sqrt{\theta}\csc[\theta]}{\pi\sqrt{4\pi-\theta}\sqrt{(4\pi-\theta)\theta}}-\frac{270\csc\sqrt{(4\pi-\theta)\theta}\csc[\theta]}{\pi\sqrt{4\pi-\theta}\theta^{3/2}}+\right.\right. \\
\left.\left.\frac{540\csc\sqrt{(4\pi-\theta)\theta}\csc[\theta]}{\pi(4\pi-\theta)^{3/2}\sqrt{\theta}}+\frac{810\csc\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\csc[\theta]}{\pi(4\pi-\theta)^{5/2}}-\right.\right. \\
\left.\left.\frac{1080\csc(4\pi-2\theta)\sqrt{\theta}\cot[\theta]\csc[\theta]}{\pi\sqrt{4\pi-\theta}\sqrt{(4\pi-\theta)\theta}}-\frac{1080\csc\sqrt{(4\pi-\theta)\theta}\cot[\theta]\csc[\theta]}{\pi\sqrt{4\pi-\theta}\sqrt{\theta}}-\right.\right. \\
\left.\left.\frac{1080\csc\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\cot[\theta]\csc[\theta]}{\pi(4\pi-\theta)^{3/2}}+\frac{1080\csc\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\cot[\theta]^2\csc[\theta]}{\pi\sqrt{4\pi-\theta}}+\right.\right. \\
\left.\left.\frac{1080\csc\sqrt{\theta}\sqrt{(4\pi-\theta)\theta}\csc[\theta]^3}{\pi\sqrt{4\pi-\theta}}\right),\{\theta,-13,13\}\right]$$



$$\begin{aligned}
& \text{PolarPlot} \left[ \frac{1}{1166400} \pi^2 \left( -\frac{270 \csc(4\pi - 2\theta)^2 \sqrt{\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} ((4\pi - \theta)\theta)^{3/2}} + \frac{540 \csc(4\pi - 2\theta) \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta} \sqrt{(4\pi - \theta)\theta}} + \right. \right. \\
& \frac{540 \csc(4\pi - 2\theta) \sqrt{\theta} \csc[\theta]}{\pi (4\pi - \theta)^{3/2} \sqrt{(4\pi - \theta)\theta}} - \frac{1080 \csc \sqrt{\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta)\theta}} - \frac{270 \csc \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi \sqrt{4\pi - \theta} \theta^{3/2}} + \\
& \frac{540 \csc \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi (4\pi - \theta)^{3/2} \sqrt{\theta}} + \frac{810 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \csc[\theta]}{\pi (4\pi - \theta)^{5/2}} - \\
& \frac{1080 \csc(4\pi - 2\theta) \sqrt{\theta} \cot[\theta] \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{(4\pi - \theta)\theta}} - \frac{1080 \csc \sqrt{(4\pi - \theta)\theta} \cot[\theta] \csc[\theta]}{\pi \sqrt{4\pi - \theta} \sqrt{\theta}} - \\
& \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \cot[\theta] \csc[\theta]}{\pi (4\pi - \theta)^{3/2}} + \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \cot[\theta]^2 \csc[\theta]}{\pi \sqrt{4\pi - \theta}} + \\
& \left. \frac{1080 \csc \sqrt{\theta} \sqrt{(4\pi - \theta)\theta} \csc[\theta]^3}{\pi \sqrt{4\pi - \theta}} \right), \{\theta, -13, 13\}]
\end{aligned}$$


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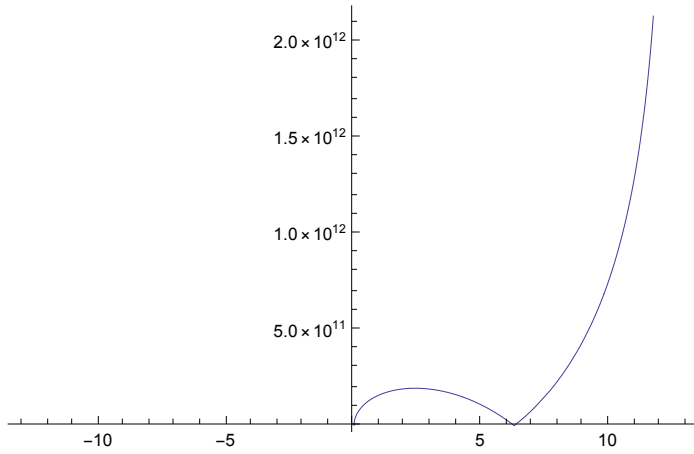
## VI. Deriving Acceleration from the Third Principle and Plotting Correlations.



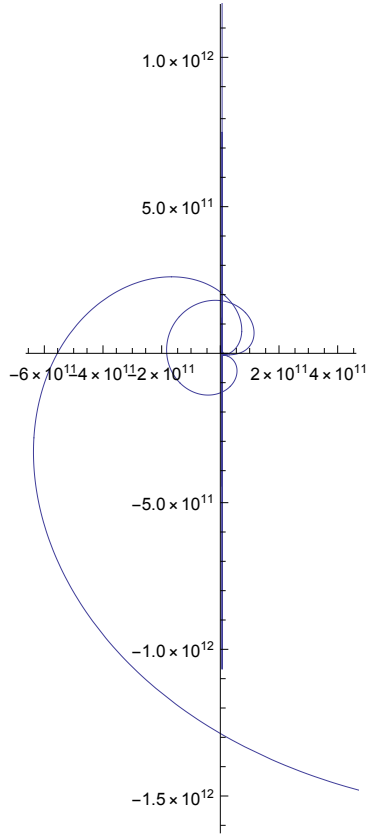
$$\begin{aligned}
r_1 = \sqrt{r^2 - \eta^2} &= \sqrt{\left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2} = \\
&\sqrt{\left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \theta} \, \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2}
\end{aligned}$$

Expression for  $r_1$ , no. 1

$$\text{Plot}\left[\sqrt{\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2 - \left(\frac{\sqrt{4\pi}\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}{2\pi}\right)^2}, \{\theta, -13, 13\}]\right]$$



$$\text{PolarPlot}\left[\sqrt{\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2 - \left(\frac{\sqrt{4\pi}\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}{2\pi}\right)^2}, \{\theta, -13, 13\}\right]$$



The First Derivative of Expression for  $r_1$ , no. 1

$$\frac{1}{1080} \pi D \left[ \sqrt{\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2 - \left(\frac{\sqrt{4\pi}\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi-\theta}}\right)^2\theta^2}{2\pi}\right)^2}, \theta \right]$$

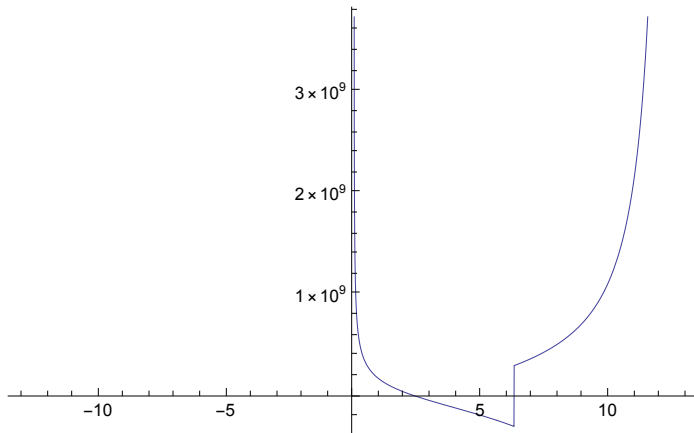
$$\left( \pi \left( \frac{4\,665\,600\,c^2}{4\pi-\theta} + \frac{4\,665\,600\,c^2\theta}{(4\pi-\theta)^2} - \frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}}{4\pi^2} \right) \right) /$$

$$\left( 2160 \sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi-\theta} - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}{4\pi^2}} \right)$$

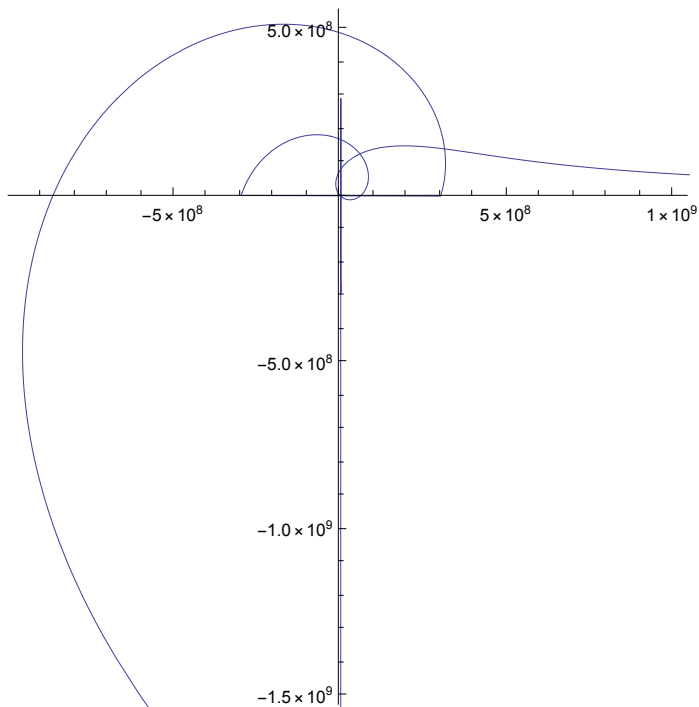
Plot[

$$\left( \pi \left( \frac{4\,665\,600\,c^2}{4\pi - \theta} + \frac{4\,665\,600\,c^2\theta}{(4\pi - \theta)^2} - \frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi - \theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi - \theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi - \theta)^2}}{4\pi^2} \right) \right) /$$

$$\left( 2160 \sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi - \theta} - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi - \theta}}{4\pi^2}} \right), \{\theta, -13, 13\}]$$



$$\text{PolarPlot}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\,\pi-\theta}+\frac{4\,665\,600\,c^2\,\theta}{(4\,\pi-\theta)^2}-\frac{\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta}+\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2}-\frac{13\,996\,800\,c^2\,\theta^2}{4\,\pi-\theta}-\frac{4\,665\,600\,c^2\,\theta^3}{(4\,\pi-\theta)^2}}{4\,\pi^2}\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\,\theta}{4\,\pi-\theta}-\frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta}-\frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi-\theta}}{4\,\pi^2}}\right),\{\theta,-13,13\}\right]$$



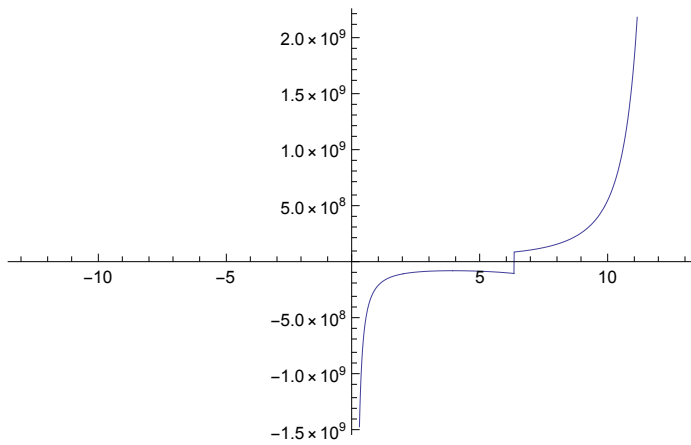
$$\frac{1}{1080} \pi D \left[ \frac{\frac{4665600 c^2}{4\pi-\theta} + \frac{4665600 c^2 \theta}{(4\pi-\theta)^2} - \frac{\frac{37324800 c^2 \pi \theta}{4\pi-\theta} + \frac{18662400 c^2 \pi \theta^2}{(4\pi-\theta)^2} - \frac{13996800 c^2 \theta^2}{4\pi-\theta} - \frac{4665600 c^2 \theta^3}{(4\pi-\theta)^2}}{4\pi^2}, \theta \right]$$

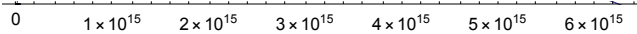
$$2 \sqrt{\frac{4665600 c^2 \theta}{4\pi-\theta} - \frac{\frac{18662400 c^2 \pi \theta^2}{4\pi-\theta} - \frac{4665600 c^2 \theta^3}{4\pi-\theta}}{4\pi^2}}$$

$$\frac{1}{1080}$$

$$\pi \left( - \left( \frac{4665600 c^2}{4\pi-\theta} + \frac{4665600 c^2 \theta}{(4\pi-\theta)^2} - \frac{\frac{37324800 c^2 \pi \theta}{4\pi-\theta} + \frac{18662400 c^2 \pi \theta^2}{(4\pi-\theta)^2} - \frac{13996800 c^2 \theta^2}{4\pi-\theta} - \frac{4665600 c^2 \theta^3}{(4\pi-\theta)^2}}{4\pi^2} \right)^2 \right. \\ \left. \left( 4 \left( \frac{4665600 c^2 \theta}{4\pi-\theta} - \frac{\frac{18662400 c^2 \pi \theta^2}{4\pi-\theta} - \frac{4665600 c^2 \theta^3}{4\pi-\theta}}{4\pi^2} \right)^{3/2} \right) + \right. \\ \left( \frac{9331200 c^2}{(4\pi-\theta)^2} + \frac{9331200 c^2 \theta}{(4\pi-\theta)^3} - \frac{1}{4\pi^2} \left( \frac{37324800 c^2 \pi}{4\pi-\theta} + \frac{74649600 c^2 \pi \theta}{(4\pi-\theta)^2} - \frac{27993600 c^2 \theta}{4\pi-\theta} + \frac{37324800 c^2 \pi \theta^2}{(4\pi-\theta)^3} - \frac{27993600 c^2 \theta^2}{(4\pi-\theta)^2} - \frac{9331200 c^2 \theta^3}{(4\pi-\theta)^3} \right) \right) \Bigg/ \\ \left( 2 \sqrt{\frac{4665600 c^2 \theta}{4\pi-\theta} - \frac{\frac{18662400 c^2 \pi \theta^2}{4\pi-\theta} - \frac{4665600 c^2 \theta^3}{4\pi-\theta}}{4\pi^2}} \right) \Bigg)$$

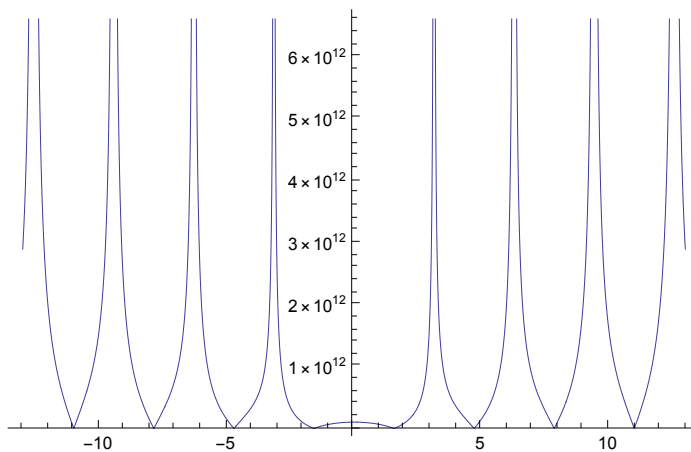
$$\begin{aligned}
 & \text{Plot}\left[\frac{1}{1080} \pi \right. \\
 & \left. - \left( \frac{4\,665\,600\,c^2}{4\pi - \theta} + \frac{4\,665\,600\,c^2\theta}{(4\pi - \theta)^2} - \frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi - \theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi - \theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi - \theta)^2}}{4\pi^2} \right)^2 / \right. \\
 & \left. \left( 4 \left( \frac{4\,665\,600\,c^2\theta}{4\pi - \theta} - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi^2}}{4\pi^2} \right)^{3/2} \right) + \right. \\
 & \left. \left( \frac{9\,331\,200\,c^2}{(4\pi - \theta)^2} + \frac{9\,331\,200\,c^2\theta}{(4\pi - \theta)^3} - \frac{1}{4\pi^2} \left( \frac{37\,324\,800\,c^2\pi}{4\pi - \theta} + \frac{74\,649\,600\,c^2\pi\theta}{(4\pi - \theta)^2} - \right. \right. \right. \\
 & \left. \left. \frac{27\,993\,600\,c^2\theta}{4\pi - \theta} + \frac{37\,324\,800\,c^2\pi\theta^2}{(4\pi - \theta)^3} - \frac{27\,993\,600\,c^2\theta^2}{(4\pi - \theta)^2} - \frac{9\,331\,200\,c^2\theta^3}{(4\pi - \theta)^3} \right) \right) / \right. \\
 & \left. \left( 2 \sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi - \theta} - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi^2}}{4\pi^2}} \right) \right], \{\theta, -13, 13\}]
 \end{aligned}$$



$$\text{PolarPlot}\left[\frac{1}{1080} \pi \left( - \left( \frac{4\,665\,600\,c^2}{4\pi - \theta} + \frac{4\,665\,600\,c^2\theta}{(4\pi - \theta)^2} - \frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi - \theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi - \theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi - \theta)^2} \right)^2 / \right. \right. \\ \left. \left( 4 \left( \frac{4\,665\,600\,c^2\theta}{4\pi - \theta} - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi^2} \right)^{3/2} \right) + \right. \\ \left. \left( \frac{9\,331\,200\,c^2}{(4\pi - \theta)^2} + \frac{9\,331\,200\,c^2\theta}{(4\pi - \theta)^3} - \frac{1}{4\pi^2} \left( \frac{37\,324\,800\,c^2\pi}{4\pi - \theta} + \frac{74\,649\,600\,c^2\pi\theta}{(4\pi - \theta)^2} - \right. \right. \right. \\ \left. \left. \left. \frac{27\,993\,600\,c^2\theta}{4\pi - \theta} + \frac{37\,324\,800\,c^2\pi\theta^2}{(4\pi - \theta)^3} - \frac{27\,993\,600\,c^2\theta^2}{(4\pi - \theta)^2} - \frac{9\,331\,200\,c^2\theta^3}{(4\pi - \theta)^3} \right) \right) \right) / \\ \left. \left( 2 \sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi - \theta} - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi - \theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi^2}}{4\pi^2}} \right) \right], \{\theta, -13, 13\}]$$


Expression for  $r_1$ , no. 2

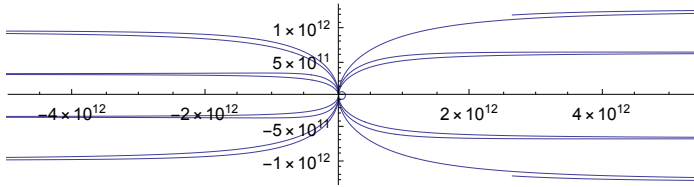
$$\text{Plot}\left[\sqrt{\left(\frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\pi - \theta)\theta}\,\text{Csc}[\theta]}{\pi\sqrt{4\pi - \theta}}\right)^2 - \left(\frac{\sqrt{4\pi\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi - \theta}}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\pi - \theta}}\right)^2\theta^2}}{2\pi}\right)^2}, \{\theta, -13, 13\} \right]$$





$$\text{PolarPlot}\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2},\right.$$

$$\{\theta, -13, 13\}]$$



First and Second derivatives of expression for  $r_1$ , no. 2

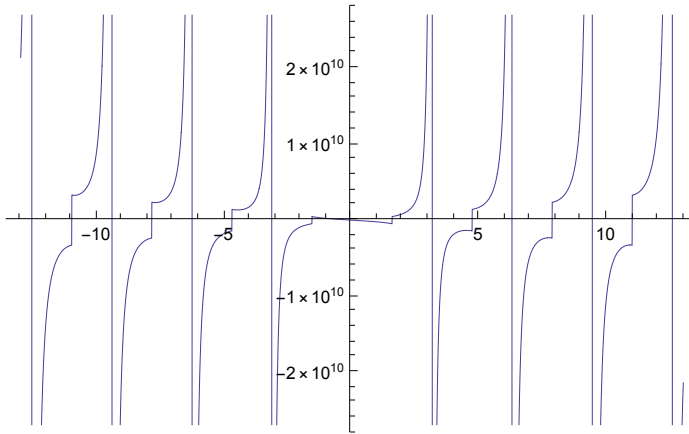
$$\frac{1}{1080} \pi$$

$$D\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \left(\frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2}, \theta\right]$$

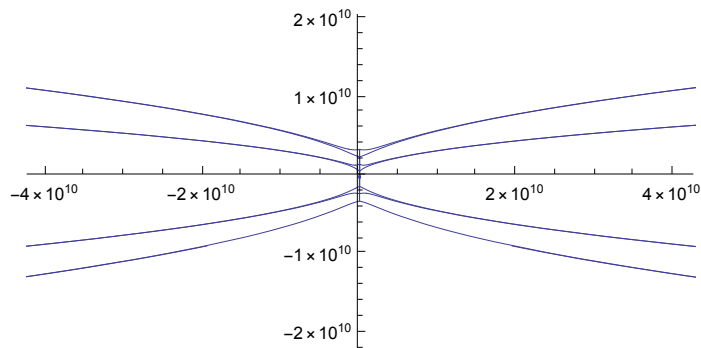
$$\left(\pi \left(-\frac{\frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2}}{4 \pi^2} + \frac{2332800 c^2 \theta \text{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2}\right)\right) /$$

$$\left(2160 \sqrt{-\frac{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{4 \pi - \theta}}{4 \pi^2} + \frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2}}\right)$$

$$\text{Plot}\left[\left(\pi\left(-\frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta}+\frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2}-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}}{4\pi^2}+\frac{2\,332\,800\,c^2\theta\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\theta^2\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}\right)\right)/\right. \\ \left.\left(2160\sqrt{-\frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}{4\pi^2}+\frac{1\,166\,400\,c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}}\right),\{\theta,-13,13\}\right]$$

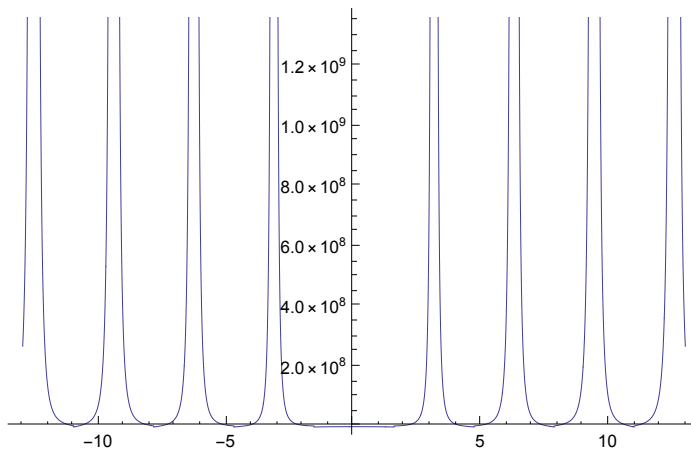


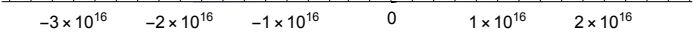
$$\text{PolarPlot}\left[\left(\pi\left(-\frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta}+\frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2}-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}}{4\pi^2}+\frac{2\,332\,800\,c^2\theta\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\theta^2\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}\right)\right)/\right. \\ \left.\left(2160\sqrt{-\frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}{4\pi^2}+\frac{1\,166\,400\,c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}}\right),\{\theta,-13,13\}\right]$$



$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \frac{1}{1080} \pi D \left[ \right. \right. \\
& \quad \left. \sqrt{\left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 - \left( \frac{\sqrt{4\pi \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right)^2 \theta - \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right)^2 \theta^2}}{2\pi} \right)^2} \right], \theta], \theta] \\
& \frac{1}{1080} \pi \left( - \left( \pi \left( - \frac{\frac{37324800 c^2 \pi \theta}{4\pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4\pi - \theta)^2} - \frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2}}{4\pi^2} + \right. \right. \right. \\
& \quad \left. \left. \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} \right)^2 \right) / \\
& \left( 4320 \left( - \frac{\frac{18662400 c^2 \pi \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{4\pi - \theta}}{4\pi^2} + \frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( - \frac{1}{4\pi^2} \left( \frac{37324800 c^2 \pi}{4\pi - \theta} + \frac{74649600 c^2 \pi \theta}{(4\pi - \theta)^2} - \frac{27993600 c^2 \theta}{4\pi - \theta} + \right. \right. \right. \\
& \quad \left. \frac{37324800 c^2 \pi \theta^2}{(4\pi - \theta)^3} - \frac{27993600 c^2 \theta^2}{(4\pi - \theta)^2} - \frac{9331200 c^2 \theta^3}{(4\pi - \theta)^3} \right) + \\
& \quad \frac{2332800 c^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \frac{4665600 c^2 \theta^2 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \operatorname{Csc}[\theta]^4}{\pi^2} \right) / \\
& \left( 2160 \sqrt{- \frac{\frac{18662400 c^2 \pi \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{4\pi - \theta}}{4\pi^2} + \frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2}} \right)
\end{aligned}$$

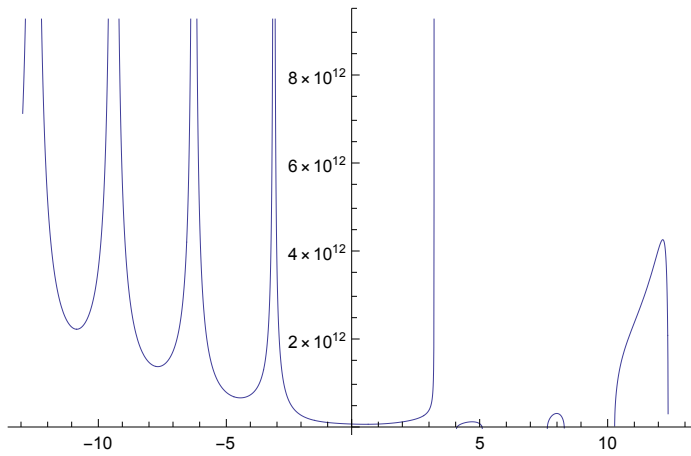
$$\begin{aligned}
 & \text{Plot} \left[ \frac{1}{1080} \pi \right. \\
 & \left( - \left( \pi \left( - \frac{\frac{37\,324\,800\,c^2\pi\theta}{4\pi-\theta} + \frac{18\,662\,400\,c^2\pi\theta^2}{(4\pi-\theta)^2} - \frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}}{4\pi^2} + \frac{2\,332\,800\,c^2\theta\,\text{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
 & \quad \left. \left. \frac{2\,332\,800\,c^2\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right)^2 \right) / \\
 & \left( 4320 \left( - \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}{4\pi^2} + \frac{1\,166\,400\,c^2\theta^2\,\text{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \\
 & \left( \pi \left( - \frac{1}{4\pi^2} \left( \frac{37\,324\,800\,c^2\pi}{4\pi-\theta} + \frac{74\,649\,600\,c^2\pi\theta}{(4\pi-\theta)^2} - \frac{27\,993\,600\,c^2\theta}{4\pi-\theta} + \right. \right. \right. \\
 & \quad \left. \left. \frac{37\,324\,800\,c^2\pi\theta^2}{(4\pi-\theta)^3} - \frac{27\,993\,600\,c^2\theta^2}{(4\pi-\theta)^2} - \frac{9\,331\,200\,c^2\theta^3}{(4\pi-\theta)^3} \right) + \right. \\
 & \quad \left. \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \\
 & \quad \left. \frac{4\,665\,600\,c^2\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\theta^2\,\text{Csc}[\theta]^4}{\pi^2} \right) \Bigg) / \\
 & \left( 2160 \sqrt{- \frac{\frac{18\,662\,400\,c^2\pi\theta^2}{4\pi-\theta} - \frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}}{4\pi^2} + \frac{1\,166\,400\,c^2\theta^2\,\text{Csc}[\theta]^2}{\pi^2}} \right) \Bigg], \{\theta, -13, 13\}
 \end{aligned}$$



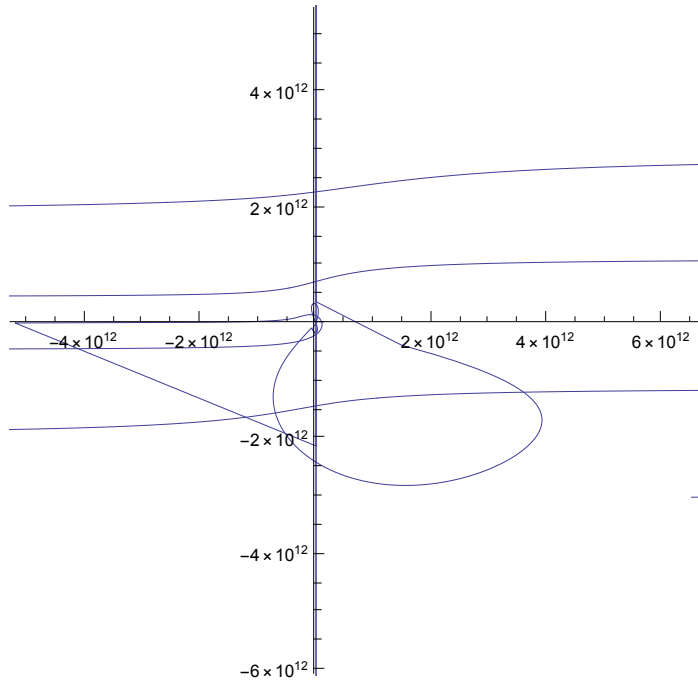
$$\begin{aligned}
& \text{PolarPlot}\left[\frac{1}{1080} \pi \right. \\
& \left. \left( - \left( \pi \left( - \frac{\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta} + \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2} - \frac{13\,996\,800\,c^2\,\theta^2}{4\,\pi-\theta} - \frac{4\,665\,600\,c^2\,\theta^3}{(4\,\pi-\theta)^2}}{4\,\pi^2} + \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \\
& \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right)^2 \right) \right) / \\
& \left( 4320 \left( - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta} - \frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi-\theta}}{4\,\pi^2} + \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi-\theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi-\theta)^2} - \frac{27\,993\,600\,c^2\,\theta}{4\,\pi-\theta} + \right. \right. \right. \\
& \left. \left. \left. \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^3} - \frac{27\,993\,600\,c^2\,\theta^2}{(4\,\pi-\theta)^2} - \frac{9\,331\,200\,c^2\,\theta^3}{(4\,\pi-\theta)^3} \right) + \right. \\
& \left. \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \\
& \left. \left. \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) / \\
& \left. \left( 2160 \sqrt{- \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta} - \frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi-\theta}}{4\,\pi^2} + \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}} \right) \right), \{\theta, -13, 13\}]
\end{aligned}$$


Expression for  $r_1$ , no. 3

$$\text{Plot}\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi} \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}{2 \pi}}\right], \{\theta, -13, 13\}]$$

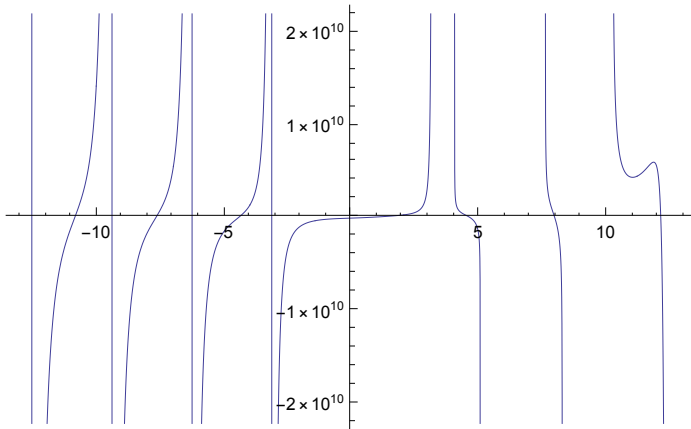


$$\text{PolarPlot}\left[\sqrt{\left(\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi} \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}{2 \pi}\right)^2}, \{\theta, -13, 13\}]\right]$$



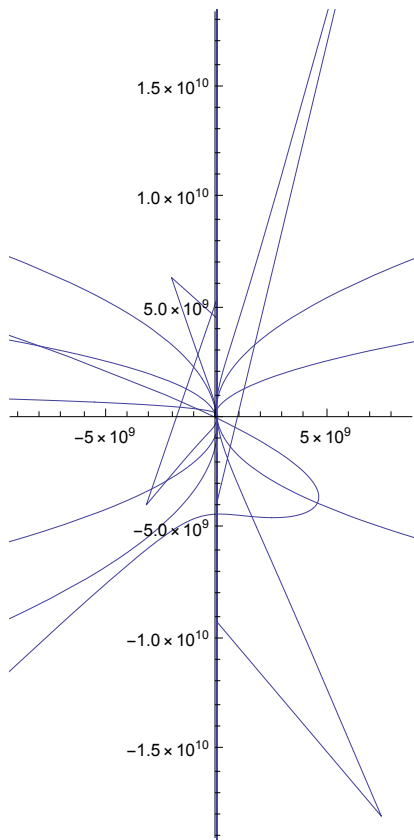
First and Second derivatives of expression for  $r_1$ , no. 3

$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \sqrt{\left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 - \right. \\
& \quad \left. \left( \frac{\sqrt{4\pi} \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta - \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right)^2 \theta^2}{2\pi} \right)^2}, \theta \right] \\
& \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
& \quad \left. \left. - \frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) / \\
& \quad \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right) \\
& \text{Plot} \left[ \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\pi^2} \left( -\frac{13996800 c^2 \theta^2}{4\pi - \theta} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) \right) / \\
& \quad \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right), \{\theta, \\
& \quad -13, 13\} \right]
\end{aligned}$$



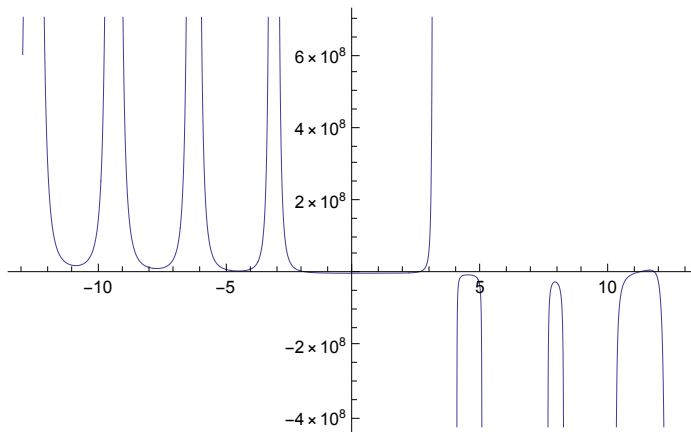


$$\text{PolarPlot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(-\frac{13\,996\,800\,c^2\,\theta^2}{4\,\pi-\theta}-\frac{4\,665\,600\,c^2\,\theta^3}{(4\,\pi-\theta)^2}+\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{-\frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi-\theta}+\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}}{4\,\pi^2}}\right),\{\theta,-13,13\}\right]$$



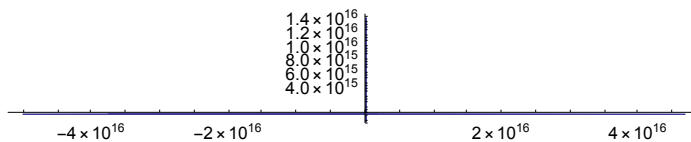
$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{1}{4 \pi^2} \left( -\frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) \right) / \right. \\
& \left. \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4665600 c^2 \theta^3}{4 \pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4 \pi^2}} \right), \theta \right] \\
& \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{1}{4 \pi^2} \left( -\frac{13996800 c^2 \theta^2}{4 \pi - \theta} - \frac{4665600 c^2 \theta^3}{(4 \pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) \right) / \right. \\
& \left. \left( 4320 \left( \frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4665600 c^2 \theta^3}{4 \pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4 \pi^2} \right)^{3/2} \right) + \right. \\
& \left( \pi \left( \frac{2332800 c^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{4665600 c^2 \theta^2 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \operatorname{Csc}[\theta]^4}{\pi^2} - \frac{1}{4 \pi^2} \left( -\frac{27993600 c^2 \theta}{4 \pi - \theta} - \frac{27993600 c^2 \theta^2}{(4 \pi - \theta)^2} - \frac{9331200 c^2 \theta^3}{(4 \pi - \theta)^3} + \frac{27993600 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi} - \frac{55987200 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} + \frac{18662400 c^2 \theta^3 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi} + \frac{9331200 c^2 \theta^3 \operatorname{Csc}[\theta]^4}{\pi} \right) \right) / \right. \\
& \left. \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4665600 c^2 \theta^3}{4 \pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4 \pi^2}} \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \text{Plot}\left[\frac{1}{1080} \pi \right. \\
 & \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( -\frac{13\,996\,800\,c^2\,\theta^2}{4\,\pi - \theta} - \right. \right. \right. \right. \\
 & \quad \frac{4\,665\,600\,c^2\,\theta^3}{(4\,\pi - \theta)^2} + \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi} - \\
 & \quad \left. \left. \left. \frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} \right) \right) \right)^2 \Big/ \\
 & \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi - \theta} + \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}}{4\,\pi^2} \right)^{3/2} \right) + \\
 & \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
 & \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
 & \quad \frac{1}{4\,\pi^2} \left( -\frac{27\,993\,600\,c^2\,\theta}{4\,\pi - \theta} - \frac{27\,993\,600\,c^2\,\theta^2}{(4\,\pi - \theta)^2} - \frac{9\,331\,200\,c^2\,\theta^3}{(4\,\pi - \theta)^3} + \right. \\
 & \quad \frac{27\,993\,600\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi} - \frac{55\,987\,200\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \\
 & \quad \left. \left. \left. \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi} + \frac{9\,331\,200\,c^2\,\theta^3\,\text{Csc}[\theta]^4}{\pi} \right) \right) \right) \Big/ \\
 & \left. \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{-\frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi - \theta} + \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}}{4\,\pi^2}} \right), \{\theta, -13, 13\} \right]
 \end{aligned}$$



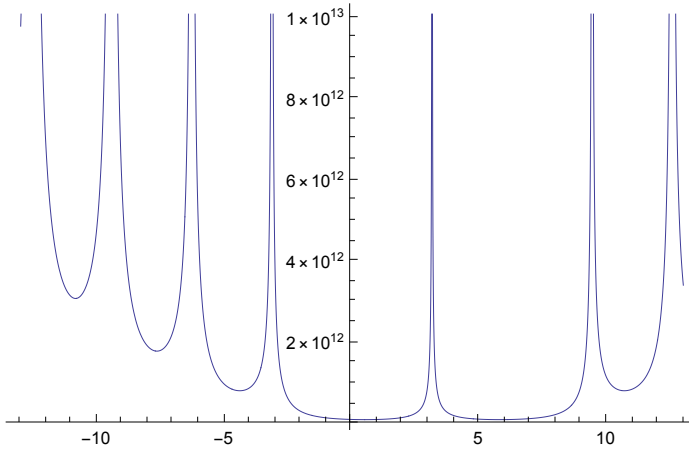
PolarPlot $\left[\frac{1}{1080} \pi\right.$

$$\left(-\left(\pi\left(\frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2}-\frac{2332800 c^2 \theta^2 \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi^2}-\frac{1}{4 \pi^2}\left(-\frac{13996800 c^2 \theta^2}{4 \pi-\theta}-\frac{4665600 c^2 \theta^3}{(4 \pi-\theta)^2}+\frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi}-\frac{9331200 c^2 \theta^3 \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi}\right)\right)^2\right) / \left(4320\left(\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2}-\frac{-\frac{4665600 c^2 \theta^3}{4 \pi-\theta}+\frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4 \pi^2}\right)^{3 / 2}\right)+\left(\pi\left(\frac{2332800 c^2 \operatorname{Csc}[\theta]^2}{\pi^2}-\frac{9331200 c^2 \theta \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi^2}+\frac{4665600 c^2 \theta^2 \cot[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2}+\frac{2332800 c^2 \theta^2 \operatorname{Csc}[\theta]^4}{\pi^2}-\frac{1}{4 \pi^2}\left(-\frac{27993600 c^2 \theta}{4 \pi-\theta}-\frac{27993600 c^2 \theta^2}{(4 \pi-\theta)^2}-\frac{9331200 c^2 \theta^3}{(4 \pi-\theta)^3}+\frac{27993600 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi}-\frac{55987200 c^2 \theta^2 \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi}+\frac{18662400 c^2 \theta^3 \cot[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi}+\frac{9331200 c^2 \theta^3 \operatorname{Csc}[\theta]^4}{\pi}\right)\right) / \left(2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2}-\frac{-\frac{4665600 c^2 \theta^3}{4 \pi-\theta}+\frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4 \pi^2}}\right),\{\theta,-13,13\}]$$

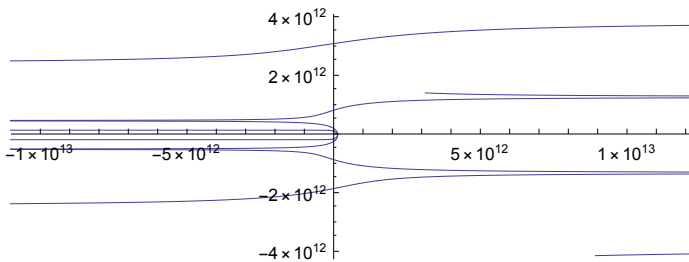


## Expression for $r_1$ , no. 4

$$\text{Plot}\left[\sqrt{\left|\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi} \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 \theta^2}{2 \pi}\right|^2}, \{\theta, -13, 13\}]\right]$$



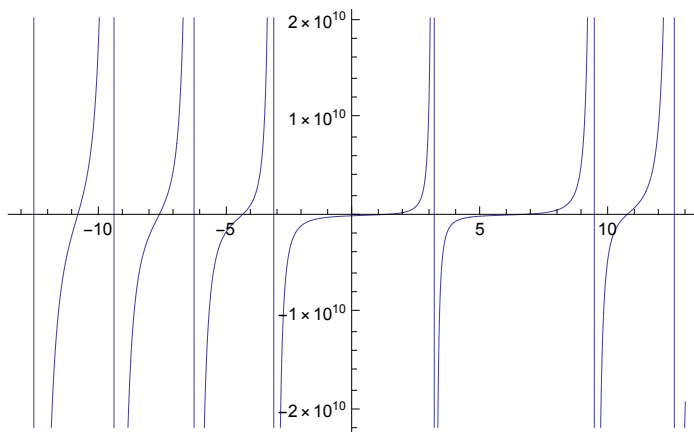
$$\text{PolarPlot}\left[\sqrt{\left|\left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi} \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}{\pi \, \sqrt{4 \pi - \theta}}\right)^2 \theta^2}{2 \pi}\right|^2}, \{\theta, -13, 13\}]\right]$$



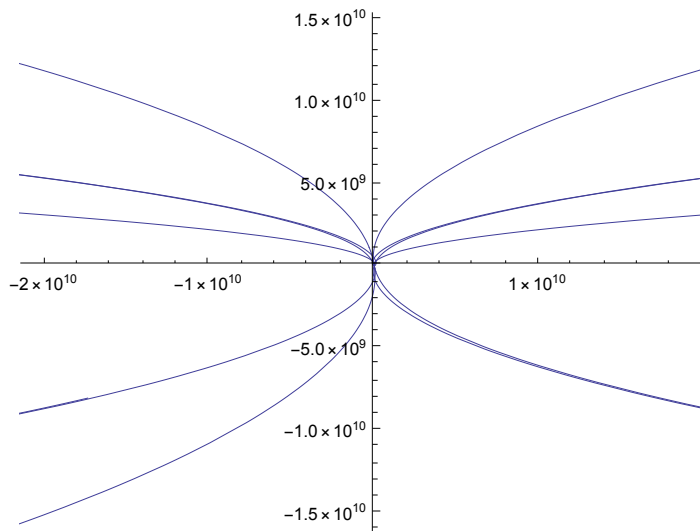
First and Second derivatives of expression for  $r_1$ , no. 4

$$\begin{aligned}
 & \frac{1}{1080} \pi D \left[ \sqrt{\left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 - \right. \\
 & \quad \left. \left( \frac{\sqrt{4\pi} \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta^2}{2\pi} \right)^2}, \theta \right] \\
 & \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
 & \quad \frac{1}{4\pi^2} \left( \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \\
 & \quad \left. \left. \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} \right) \right) \Bigg) / \\
 & \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4\pi^2}} \right)
 \end{aligned}$$

$$\text{Plot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}}\right),\{\theta,-13,13\}\right]$$

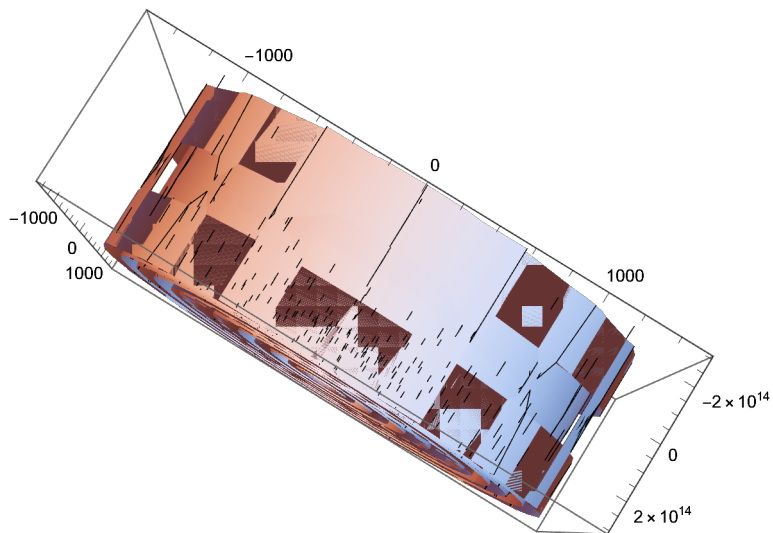


$$\text{PolarPlot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\
\left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta, -13, 13\}\right]$$

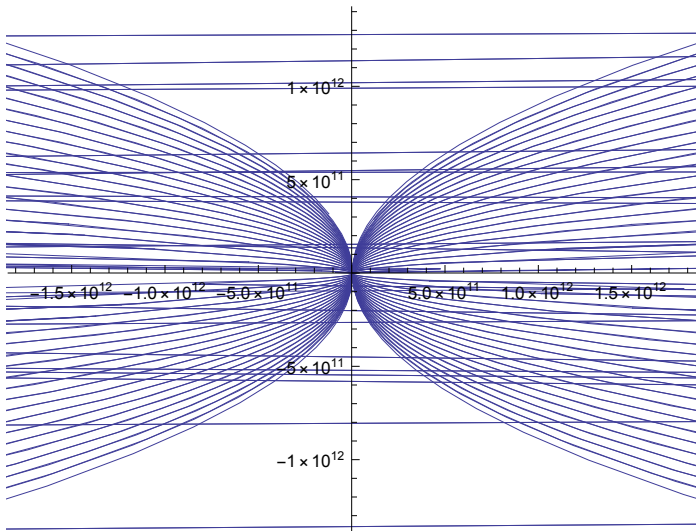




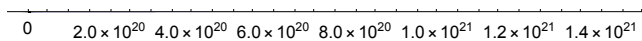
$$\text{RevolutionPlot3D}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,-480\pi,480\pi\}\right]$$



$$\text{PolarPlot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,\right. \\ \left.-130,130\}\right]$$

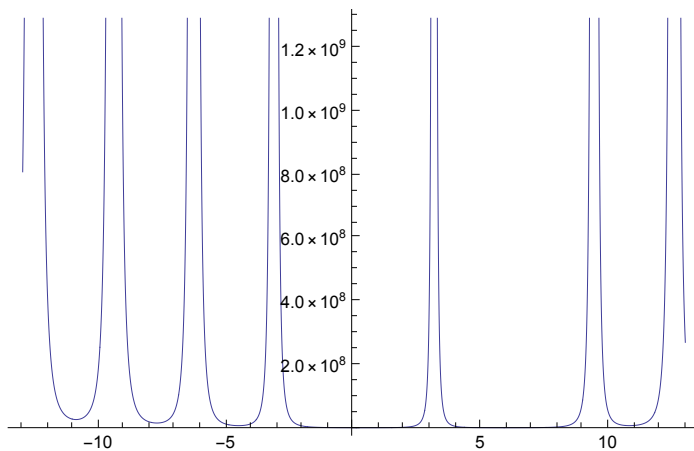


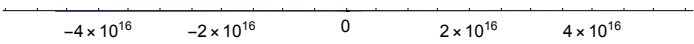
$$\text{PolarPlot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,\right. \\ \left.-1300,1300\}\right]$$



$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \frac{1}{1080} \pi D \left[ \sqrt{\left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 - \right.} \right. \\
& \left. \left. \left( \frac{\sqrt{4\pi} \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta^2}{2\pi} \right)^2 \right], \theta, \theta \right] \\
& \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \\
& \frac{1}{4\pi^2} \left( \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \\
& \left. \left. \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} \right) \right)^2 \Bigg) / \\
& \left( 4320 \left( \frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2332800 c^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \frac{4665600 c^2 \theta^2 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \operatorname{Csc}[\theta]^4}{\pi^2} - \\
& \frac{1}{4\pi^2} \left( \frac{27993600 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi} - \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \\
& \frac{55987200 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} + \frac{18662400 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} + \\
& \frac{18662400 c^2 \theta^3 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^4 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \\
& \left. \left. \left. \frac{9331200 c^2 \theta^3 \operatorname{Csc}[\theta]^4}{\pi} - \frac{2332800 c^2 \theta^4 \operatorname{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4\pi^2}} \right)
\end{aligned}$$

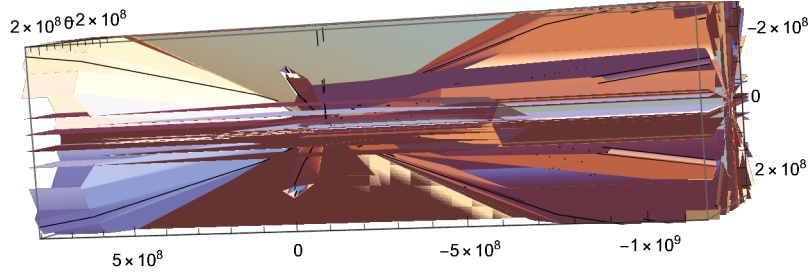
$$\begin{aligned}
& \text{Plot} \left[ \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \left. \frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \Big/ \\
& \quad \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \quad \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{27\,993\,600\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi} - \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \frac{55\,987\,200\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \frac{9\,331\,200\,c^2\,\theta^3\,\text{Csc}[\theta]^4}{\pi} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \Big/ \\
& \quad \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right), \{\theta, -13, 13\} \Big]
\end{aligned}$$



$$\begin{aligned}
& \text{PolarPlot} \left[ \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2 \, 332 \, 800 \, c^2 \, \theta \, \text{Csc}[\theta]^2}{\pi^2} - \frac{2 \, 332 \, 800 \, c^2 \, \theta^2 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \right. \\
& \quad \frac{1}{4 \, \pi^2} \left( \frac{13 \, 996 \, 800 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi} - \frac{4 \, 665 \, 600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \left. \left. \frac{9 \, 331 \, 200 \, c^2 \, \theta^3 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi} + \frac{2 \, 332 \, 800 \, c^2 \, \theta^4 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} \right) \right) \right) \right) / \\
& \quad \left( 4320 \left( \frac{1 \, 166 \, 400 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4 \, 665 \, 600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi} - \frac{1 \, 166 \, 400 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^2}{\pi^2}}{4 \, \pi^2} \right)^{3/2} \right) + \\
& \quad \left( \pi \left( \frac{2 \, 332 \, 800 \, c^2 \, \text{Csc}[\theta]^2}{\pi^2} - \frac{9 \, 331 \, 200 \, c^2 \, \theta \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \left. \frac{4 \, 665 \, 600 \, c^2 \, \theta^2 \, \text{Cot}[\theta]^2 \, \text{Csc}[\theta]^2}{\pi^2} + \frac{2 \, 332 \, 800 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^4}{\pi^2} - \right. \\
& \quad \frac{1}{4 \, \pi^2} \left( \frac{27 \, 993 \, 600 \, c^2 \, \theta \, \text{Csc}[\theta]^2}{\pi} - \frac{13 \, 996 \, 800 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \frac{55 \, 987 \, 200 \, c^2 \, \theta^2 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi} + \frac{18 \, 662 \, 400 \, c^2 \, \theta^3 \, \text{Cot}[\theta] \, \text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \frac{18 \, 662 \, 400 \, c^2 \, \theta^3 \, \text{Cot}[\theta]^2 \, \text{Csc}[\theta]^2}{\pi} - \frac{4 \, 665 \, 600 \, c^2 \, \theta^4 \, \text{Cot}[\theta]^2 \, \text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{9 \, 331 \, 200 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^4}{\pi} - \frac{2 \, 332 \, 800 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \quad \left( 2160 \sqrt{\frac{1 \, 166 \, 400 \, c^2 \, \theta^2 \, \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4 \, 665 \, 600 \, c^2 \, \theta^3 \, \text{Csc}[\theta]^2}{\pi} - \frac{1 \, 166 \, 400 \, c^2 \, \theta^4 \, \text{Csc}[\theta]^2}{\pi^2}}{4 \, \pi^2}} \right), \{\theta, -13, 13\} \Big]
\end{aligned}$$


$$2 \pi \left( 1 - \sqrt{1 - \text{Sin}[\beta]^2} \right)$$

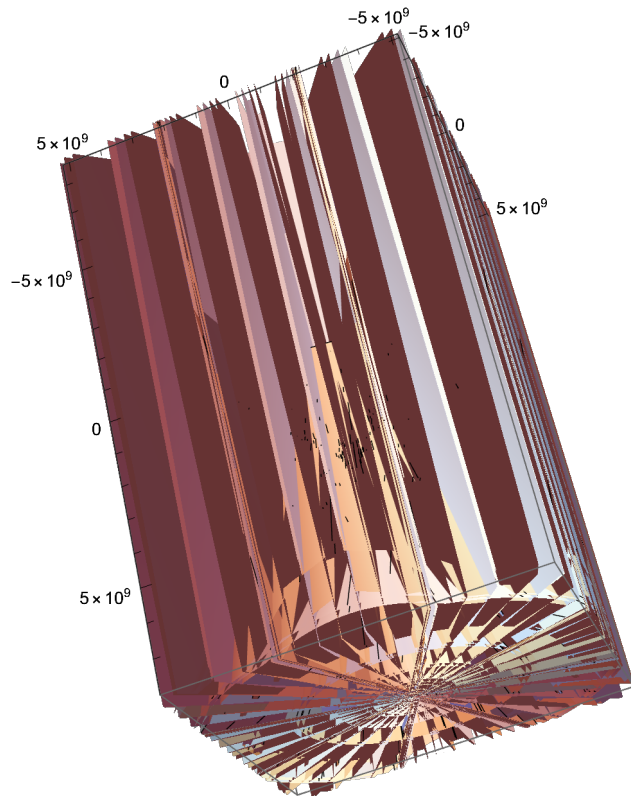
$$\begin{aligned}
& \text{SphericalPlot3D}\left[ \right. \\
& \quad \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 2 \pi \left( 1 - \sqrt{1 - \text{Sin}[\beta]^2} \right) \text{Csc}\left[ 2 \pi \left( 1 - \sqrt{1 - \text{Sin}[\beta]^2} \right) \right]^2}{\pi^2} - \right. \right. \right. \\
& \quad \left. \frac{2332800 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \frac{1}{4 \pi^2} \left( \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
& \quad \left. \left. \frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \frac{2332800 c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} \right) \right)^2 \Bigg) / \\
& \quad \left( 4320 \left( \frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2} \right)^{3/2} \right) + \\
& \quad \left( \pi \left( \frac{2332800 c^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \left. \frac{4665600 c^2 \theta^2 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \text{Csc}[\theta]^4}{\pi^2} - \right. \\
& \quad \left. \frac{1}{4 \pi^2} \left( \frac{27993600 c^2 \theta \text{Csc}[\theta]^2}{\pi} - \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \\
& \quad \left. \frac{55987200 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \frac{18662400 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \right. \\
& \quad \left. \frac{18662400 c^2 \theta^3 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^4 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \right. \\
& \quad \left. \left. \frac{9331200 c^2 \theta^3 \text{Csc}[\theta]^4}{\pi} - \frac{2332800 c^2 \theta^4 \text{Csc}[\theta]^4}{\pi^2} \right) \right) \Bigg) / \\
& \quad \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2}} \right), \\
& \quad \{\theta, -4 \pi, 4 \pi\}, \{\beta, -2 \\
& \quad \pi, 2 \\
& \quad \pi\} \Big]
\end{aligned}$$



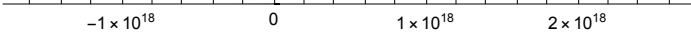
SphericalPlot3D[

$$\frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 2 \pi (1 - \sqrt{1 - \sin[\beta]^2}) \csc[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \cot[\theta] \csc[\theta]^2}{\pi^2} - \frac{1}{4 \pi^2} \left( \frac{13996800 c^2 \theta^2 \csc[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^3 \csc[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta^3 \cot[\theta] \csc[\theta]^2}{\pi} + \frac{2332800 c^2 \theta^4 \cot[\theta] \csc[\theta]^2}{\pi^2} \right) \right)^2 \right) / \left( 4320 \left( \frac{1166400 c^2 \theta^2 \csc[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \csc[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \csc[\theta]^2}{\pi^2}}{4 \pi^2} \right)^{3/2} \right) + \left( \pi \left( \frac{2332800 c^2 \csc[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \cot[\theta] \csc[\theta]^2}{\pi^2} + \frac{4665600 c^2 \theta^2 \cot[\theta]^2 \csc[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \csc[\theta]^4}{\pi^2} - \frac{1}{4 \pi^2} \left( \frac{27993600 c^2 \theta \csc[\theta]^2}{\pi} - \frac{13996800 c^2 \theta^2 \csc[\theta]^2}{\pi^2} - \frac{55987200 c^2 \theta^2 \cot[\theta] \csc[\theta]^2}{\pi} + \frac{18662400 c^2 \theta^3 \cot[\theta] \csc[\theta]^2}{\pi^2} + \frac{18662400 c^2 \theta^3 \cot[\theta]^2 \csc[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^4 \cot[\theta]^2 \csc[\theta]^2}{\pi^2} + \frac{9331200 c^2 \theta^3 \csc[\theta]^4}{\pi} - \frac{2332800 c^2 \theta^4 \csc[\theta]^4}{\pi^2} \right) \right) / \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \csc[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \csc[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \csc[\theta]^2}{\pi^2}}{4 \pi^2}} \right) \right),$$

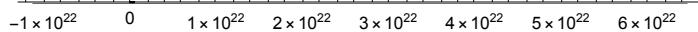
{ $\theta$ , -130, 130}, { $\beta$ ,  
- $\pi$ ,  
 $\pi$ }]





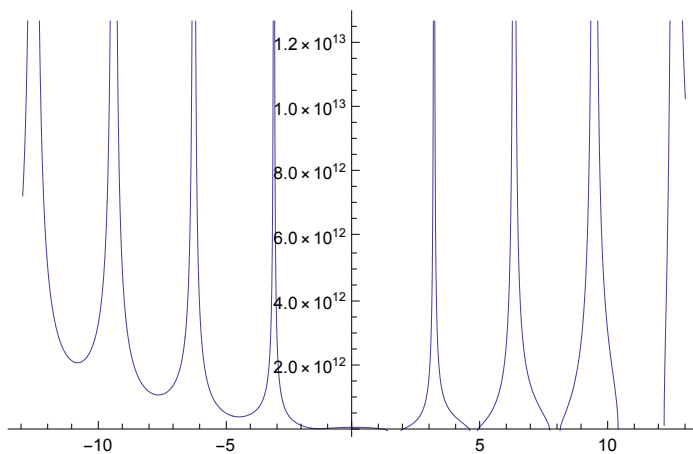
$$\begin{aligned}
& \text{PolarPlot} \left[ \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 \theta \text{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \\
& \quad \frac{1}{4 \pi^2} \left( \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \left. \frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \frac{2332800 c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \Bigg] / \\
& \left( 4320 \left( \frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2332800 c^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4665600 c^2 \theta^2 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4 \pi^2} \left( \frac{27993600 c^2 \theta \text{Csc}[\theta]^2}{\pi} - \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \frac{55987200 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \frac{18662400 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \frac{18662400 c^2 \theta^3 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^4 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{9331200 c^2 \theta^3 \text{Csc}[\theta]^4}{\pi} - \frac{2332800 c^2 \theta^4 \text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) \Bigg] / \left( 2160 \right. \\
& \quad \left. \sqrt{\frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2}} \right), \{\theta, -130, 130\} \Bigg]
\end{aligned}$$


$$\begin{aligned}
& \text{PolarPlot} \left[ \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \left. \left. \frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \right] / \\
& \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{27\,993\,600\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi} - \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \frac{55\,987\,200\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi} - \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{9\,331\,200\,c^2\,\theta^3\,\text{Csc}[\theta]^4}{\pi} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right), \\
& \{\theta, -1300, 1300\} \Big]
\end{aligned}$$

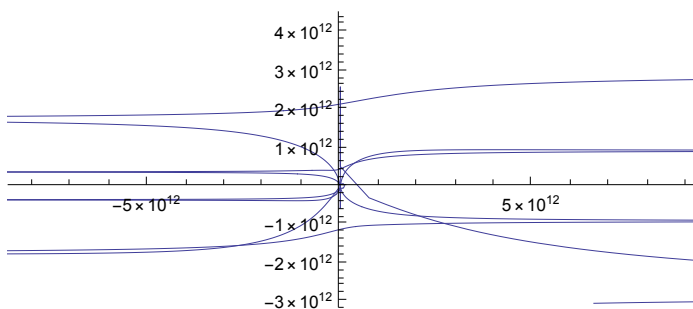


Expression for  $r_1$ , no. 5

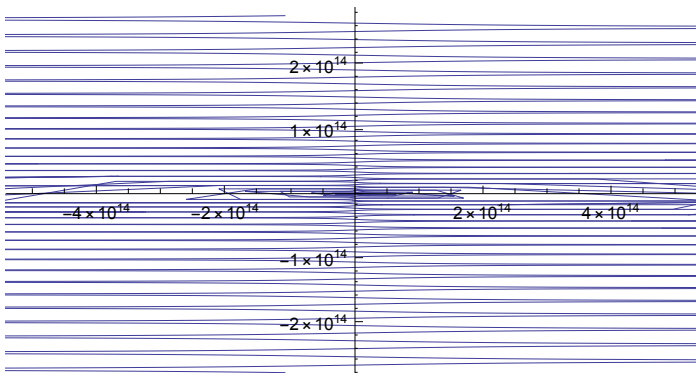
$$\text{Plot}\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}}\right], \{\theta, -13, 13\}]$$



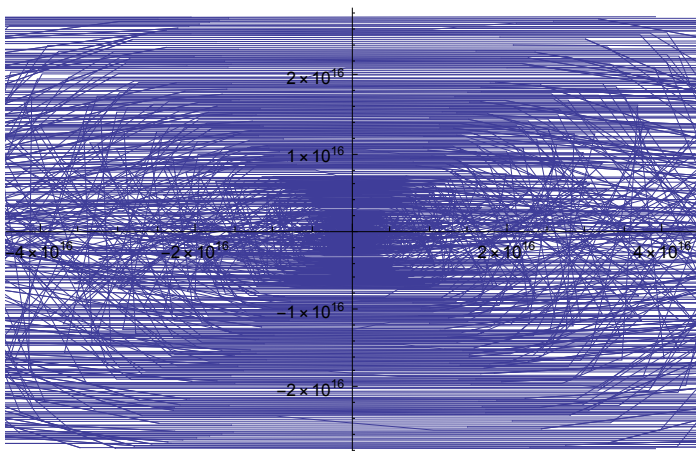
$$\text{PolarPlot}\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}}\right], \{\theta, -13, 13\}]$$



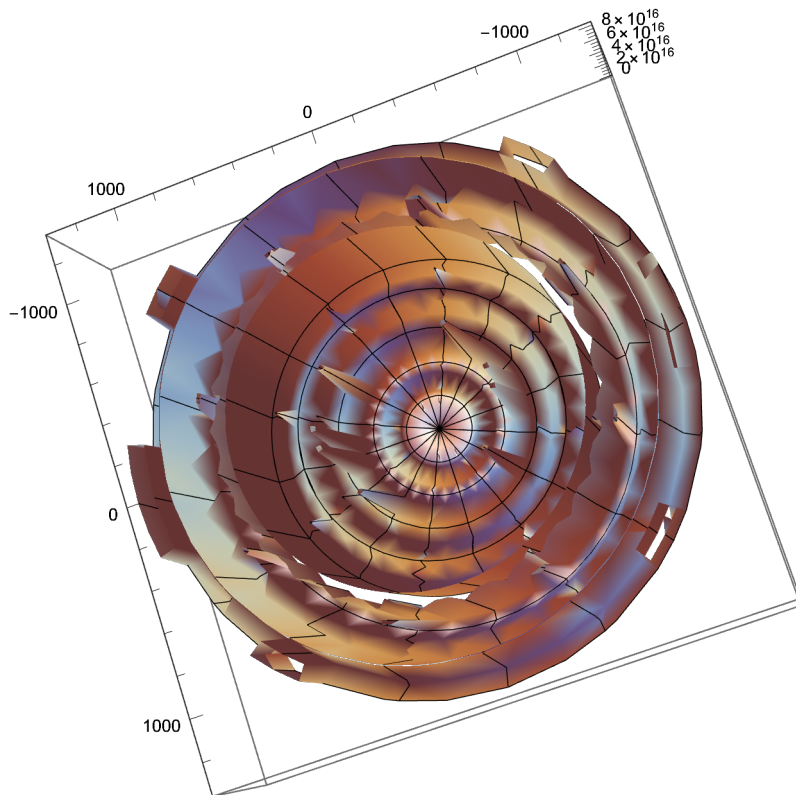
$$\text{PolarPlot}\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}}\right], \{\theta, -130, 130\}]$$



$$\text{PolarPlot}\left[\sqrt{\left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \text{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}}\right], \{\theta, -1300, 1300\}]$$

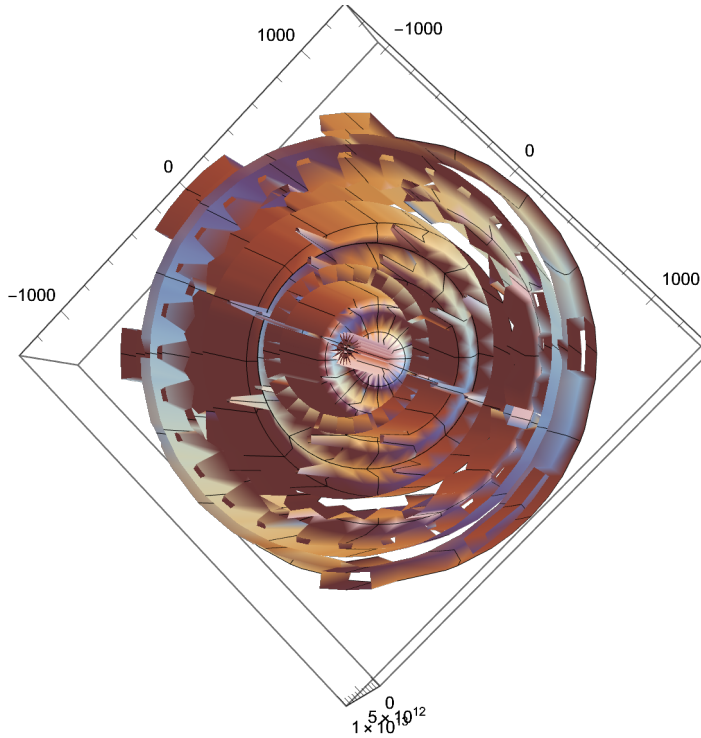


$$\text{RevolutionPlot3D}\left[\sqrt{\left(\frac{1080 \text{ c } \sqrt{\theta} \sqrt{4 \pi - \theta} \text{ Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi \left(\frac{2160 \text{ c } \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{1080 \text{ c } \sqrt{\theta} \sqrt{4 \pi - \theta} \text{ Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}}\right], \{\theta, -1300, 1300\}]$$



Show[

$$\begin{aligned}
& \left\{ \text{RevolutionPlot3D} \left[ \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 \theta \text{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \right. \\
& \quad \frac{1}{4 \pi^2} \left( \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \left. \left. \frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \frac{2332800 c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} \right) \right) \right) \right] / \\
& \quad \left( 4320 \left( \frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2} \right)^{3/2} \right) + \\
& \quad \left( \pi \left( \frac{2332800 c^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \left. \left. \frac{4665600 c^2 \theta^2 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \text{Csc}[\theta]^4}{\pi^2} - \right. \right. \\
& \quad \frac{1}{4 \pi^2} \left( \frac{27993600 c^2 \theta \text{Csc}[\theta]^2}{\pi} - \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \right. \\
& \quad \left. \frac{55987200 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \frac{18662400 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \right. \\
& \quad \left. \frac{18662400 c^2 \theta^3 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi} - \frac{4665600 c^2 \theta^4 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \right. \\
& \quad \left. \left. \left. \frac{9331200 c^2 \theta^3 \text{Csc}[\theta]^4}{\pi} - \frac{2332800 c^2 \theta^4 \text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \quad \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2}} \right), \\
& \quad \{\theta, -1300, 1300\}], \text{RevolutionPlot3D} \left[ \right. \\
& \quad \left. \sqrt{\left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta \text{Csc}[\theta]}}{\pi \sqrt{4 \pi - \theta}} \right)^2 - \right.} \\
& \quad \left. \left( \frac{\sqrt{4 \pi \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta \text{Csc}[\theta]}}{\pi \sqrt{4 \pi - \theta}} \right)^2 \theta^2}}{2 \pi} \right)^2 \right), \{\theta, -1300, 1300\}] \} \}
\end{aligned}$$



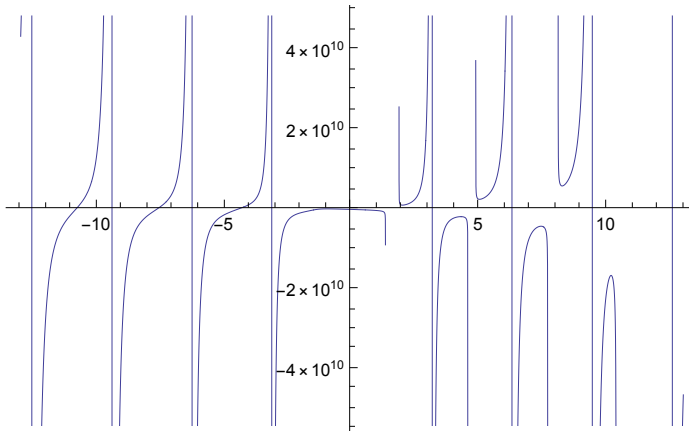
First and Second derivatives of expression for  $r_1$ , no. 5

$$\frac{1}{1080} \pi D \left[ \sqrt{\left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 - \left( \frac{\sqrt{4\pi} \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right)^2 \theta - \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta^2}{2\pi} \right)^2}, \theta \right]$$

$$\left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{37324800 c^2 \pi \theta}{4\pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4\pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2}}{4\pi^2} \right) \Bigg/$$

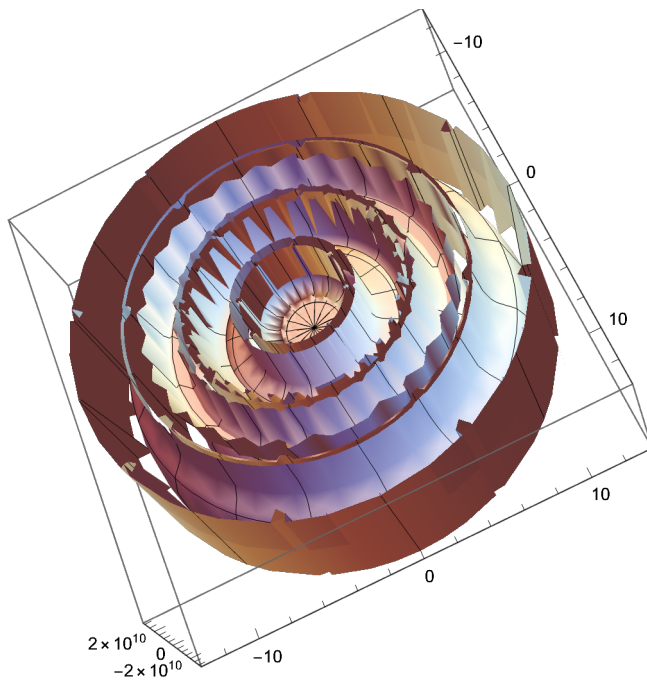
$$\left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18662400 c^2 \pi \theta^2}{4\pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4\pi^2}} \right)$$

$$\text{Plot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta}+\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,-13,13\}\right]$$

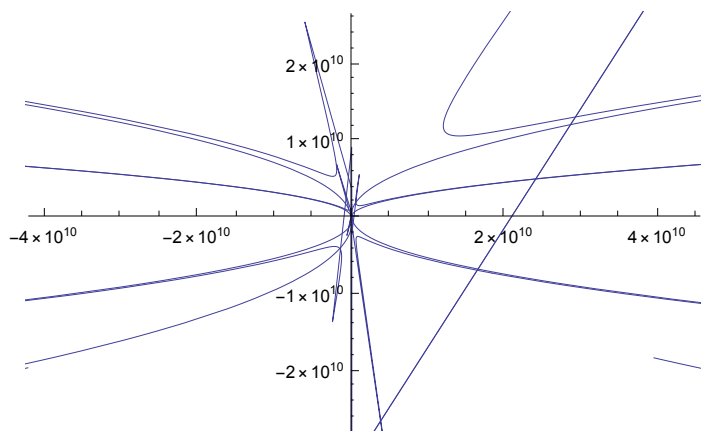


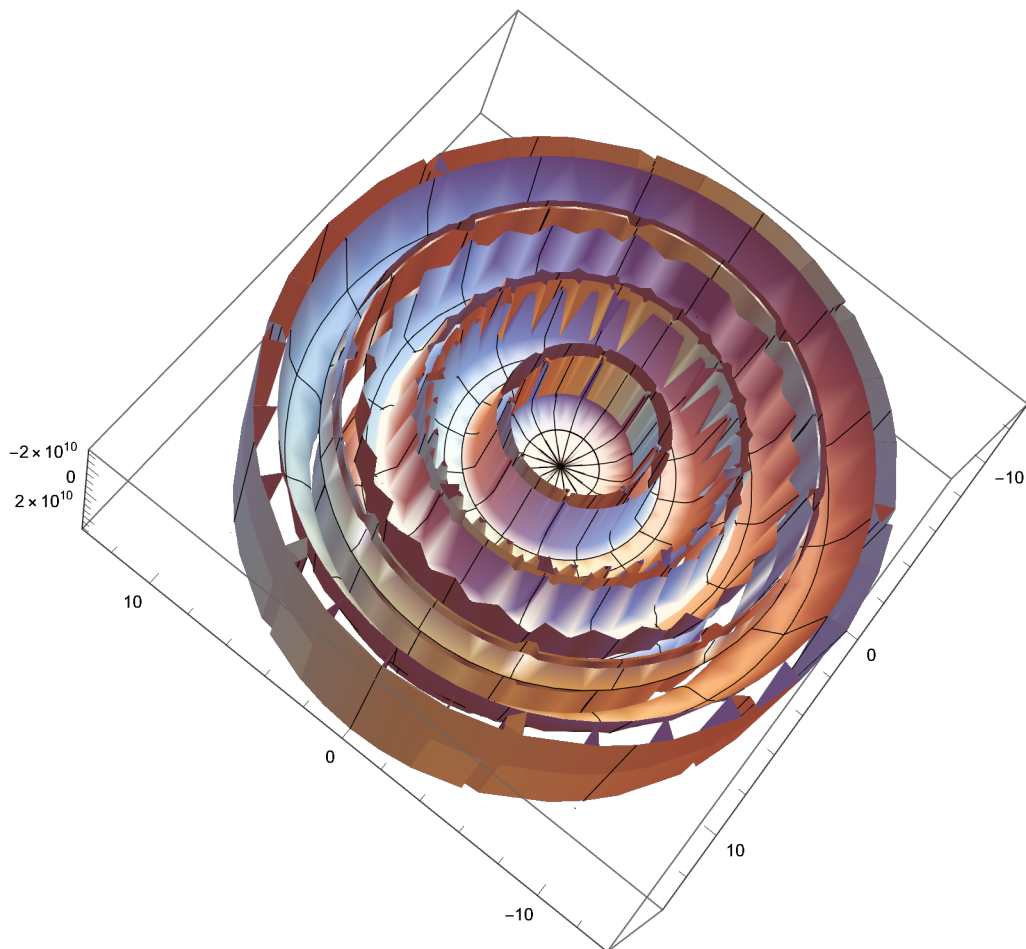


$$\text{RevolutionPlot3D}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta}+\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,-13,13\}\right]$$

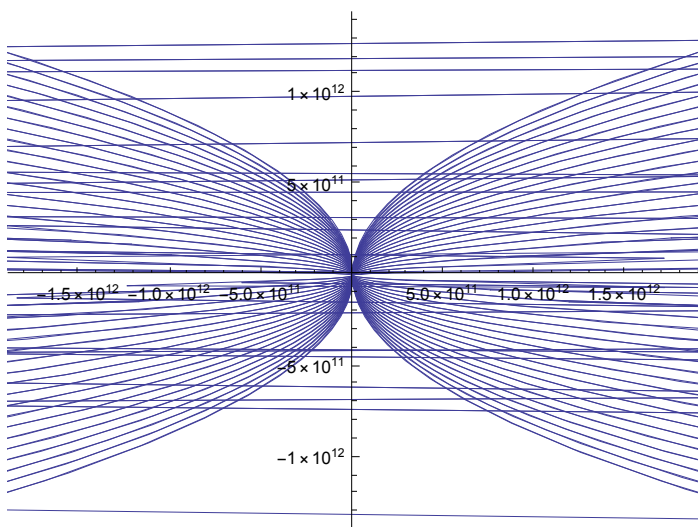


$$\text{PolarPlot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta}+\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,-13,13\}\right]$$

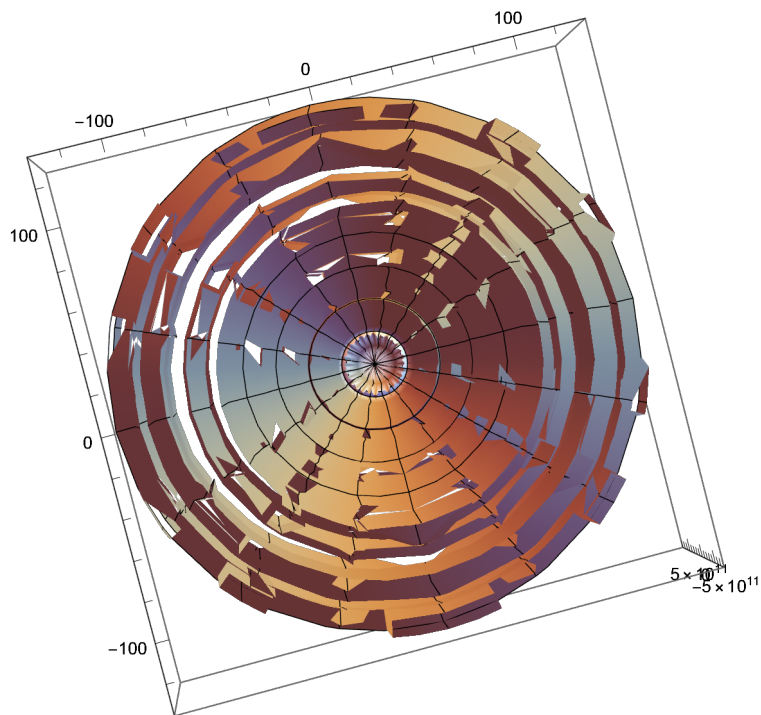




$$\text{PolarPlot}\left[\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta}+\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,-130,130\}\right]$$

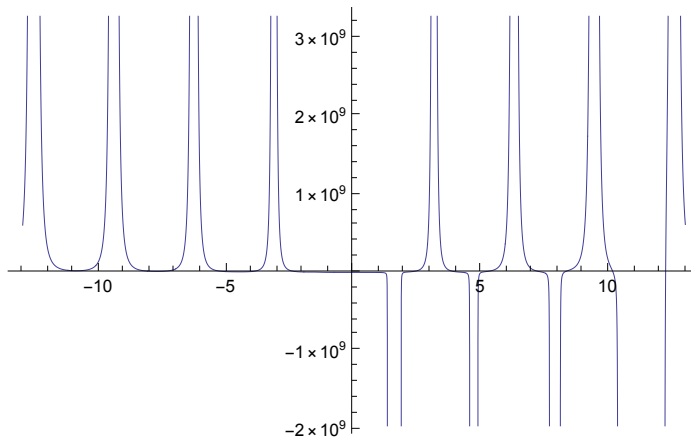


$\text{RevolutionPlot3D}\left[\right.$   
 $\left(\pi\left(\frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2}-\frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\,\pi^2}\left(\frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi-\theta}+\right.\right.\right.$   
 $\left.\left.\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi-\theta)^2}-\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2}+\frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)/$   
 $\left(2160\sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi-\theta}-\frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}}\right),\{\theta,-130,130\}\right]$

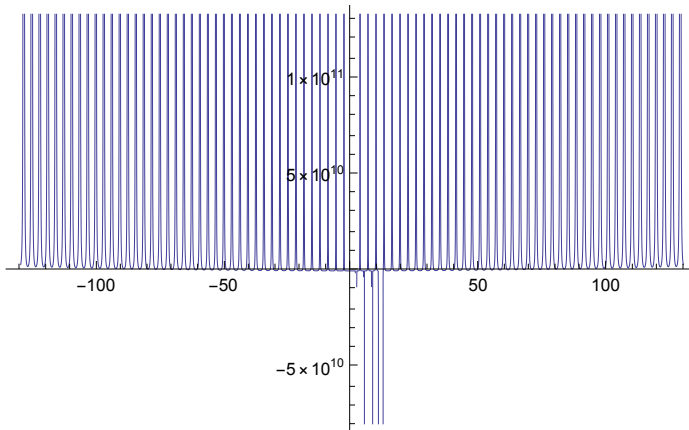


$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{1}{4 \pi^2} \left( \frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \right. \right. \right. \\
& \quad \left. \left. \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} \right) \right) \Bigg] / \\
& \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4 \pi^2}} \right), \theta \Bigg] \\
& \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{2332800 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi^2} - \right. \right. \right. \\
& \quad \frac{2332800 c^2 \theta^2 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{1}{4 \pi^2} \left( \frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \right. \\
& \quad \left. \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^4 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} \right) \Bigg) \Bigg) / \\
& \left( 4320 \left( \frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4 \pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2332800 c^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4665600 c^2 \theta^2 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \operatorname{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4 \pi^2} \left( \frac{37324800 c^2 \pi}{4 \pi - \theta} + \frac{74649600 c^2 \pi \theta}{(4 \pi - \theta)^2} + \frac{37324800 c^2 \pi \theta^2}{(4 \pi - \theta)^3} - \right. \\
& \quad \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} + \frac{18662400 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \frac{4665600 c^2 \theta^4 \operatorname{Cot}[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^4 \operatorname{Csc}[\theta]^4}{\pi^2} \right) \right) \Bigg) / \\
& \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \operatorname{Csc}[\theta]^2}{\pi^2}}{4 \pi^2}} \right)
\end{aligned}$$

$$\begin{aligned}
& \text{Plot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi - \theta} + \right. \right. \right. \right. \\
& \quad \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \right) / \\
& \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi - \theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi - \theta)^2} + \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^3} - \right. \\
& \quad \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left. \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right), \{\theta, -13, 13\} \right]
\end{aligned}$$

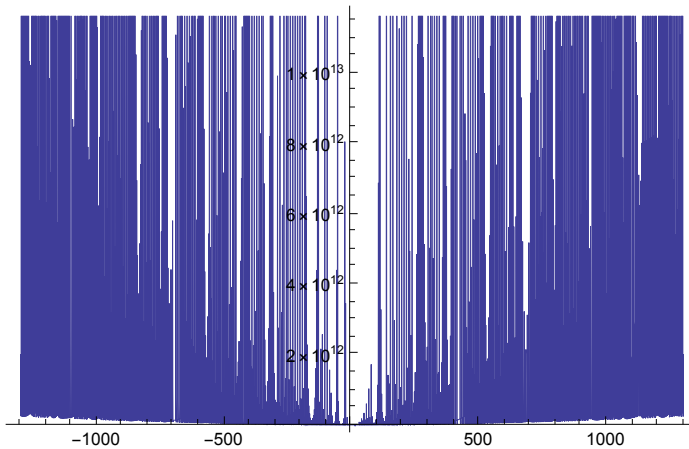


$$\begin{aligned}
& \text{Plot}\left[\frac{1}{1080}\pi\right. \\
& \left(-\left(\pi\left(\frac{2332800c^2\theta\text{Csc}[\theta]^2}{\pi^2}-\frac{2332800c^2\theta^2\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}-\frac{1}{4\pi^2}\left(\frac{37324800c^2\pi\theta}{4\pi-\theta}+\right.\right.\right.\right. \\
& \quad \left.\left.\frac{18662400c^2\pi\theta^2}{(4\pi-\theta)^2}-\frac{4665600c^2\theta^3\text{Csc}[\theta]^2}{\pi^2}+\right.\right. \\
& \quad \left.\left.\left.\frac{2332800c^2\theta^4\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}\right)\right)\right)^2\Bigg)/ \\
& \left(4320\left(\frac{1166400c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18662400c^2\pi\theta^2}{4\pi-\theta}-\frac{1166400c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}}{4\pi^2}\right)^{3/2}\right)+ \\
& \left(\pi\left(\frac{2332800c^2\text{Csc}[\theta]^2}{\pi^2}-\frac{9331200c^2\theta\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}+\right.\right. \\
& \quad \left.\frac{4665600c^2\theta^2\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi^2}+\frac{2332800c^2\theta^2\text{Csc}[\theta]^4}{\pi^2}-\right. \\
& \quad \left.\frac{1}{4\pi^2}\left(\frac{37324800c^2\pi}{4\pi-\theta}+\frac{74649600c^2\pi\theta}{(4\pi-\theta)^2}+\frac{37324800c^2\pi\theta^2}{(4\pi-\theta)^3}-\right.\right. \\
& \quad \left.\frac{13996800c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}+\frac{18662400c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi^2}-\right. \\
& \quad \left.\left.\frac{4665600c^2\theta^4\text{Cot}[\theta]^2\text{Csc}[\theta]^2}{\pi^2}-\frac{2332800c^2\theta^4\text{Csc}[\theta]^4}{\pi^2}\right)\right)\Bigg)/ \\
& \left.2160\sqrt{\frac{1166400c^2\theta^2\text{Csc}[\theta]^2}{\pi^2}-\frac{\frac{18662400c^2\pi\theta^2}{4\pi-\theta}-\frac{1166400c^2\theta^4\text{Csc}[\theta]^2}{\pi^2}}{4\pi^2}}\right),\{\theta,-130,130\}]
\end{aligned}$$

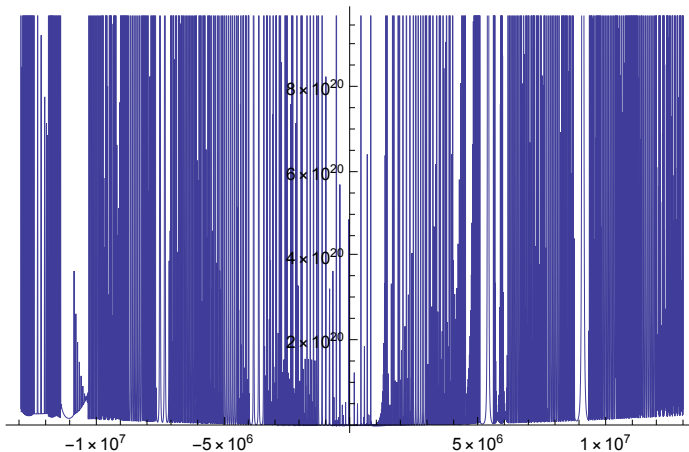




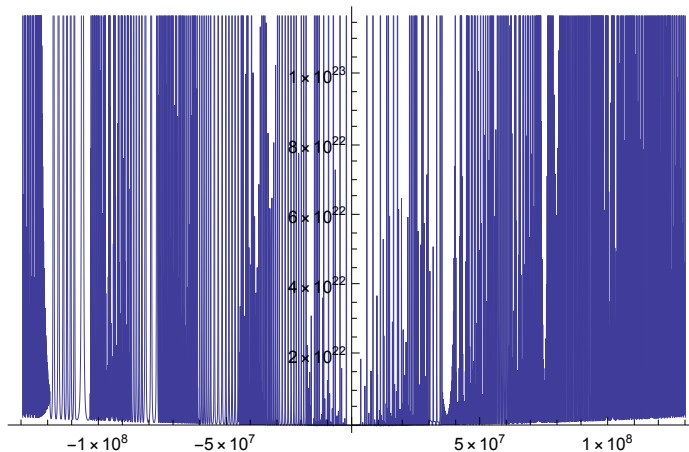
$$\begin{aligned}
& \text{Plot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi - \theta} + \right. \right. \right. \right. \\
& \quad \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \Bigg) / \right. \\
& \left. \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \right. \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi - \theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi - \theta)^2} + \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^3} - \right. \\
& \quad \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \left( 2160 \right. \\
& \left. \left. \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right) \right), \{\theta, -1300, 1300\} \Big]
\end{aligned}$$



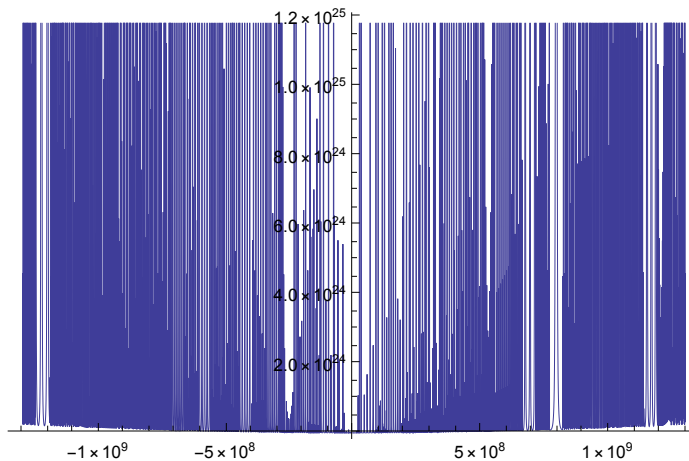
$$\begin{aligned}
& \text{Plot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi - \theta} + \right. \right. \right. \right. \\
& \quad \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \right) / \\
& \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi - \theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi - \theta)^2} + \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^3} - \right. \\
& \quad \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left. \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right) \right), \\
& \{\theta, -13\,000\,000, 13\,000\,000\} \Big]
\end{aligned}$$

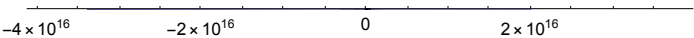


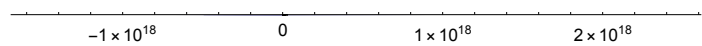
$$\begin{aligned}
& \text{Plot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi - \theta} + \right. \right. \right. \right. \\
& \quad \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \right) / \\
& \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi - \theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi - \theta)^2} + \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^3} - \right. \\
& \quad \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left. \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right) \right), \\
& \{\theta, -130\,000\,000, 130\,000\,000\} \Big]
\end{aligned}$$



$$\begin{aligned}
& \text{Plot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2332800 c^2 \theta \text{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4 \pi^2} \left( \frac{37324800 c^2 \pi \theta}{4 \pi - \theta} + \right. \right. \right. \right. \\
& \quad \frac{18662400 c^2 \pi \theta^2}{(4 \pi - \theta)^2} - \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{2332800 c^2 \theta^4 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} \right) \right) \right)^2 \Bigg) / \\
& \left( 4320 \left( \frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2332800 c^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{9331200 c^2 \theta \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4665600 c^2 \theta^2 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} + \frac{2332800 c^2 \theta^2 \text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4 \pi^2} \left( \frac{37324800 c^2 \pi}{4 \pi - \theta} + \frac{74649600 c^2 \pi \theta}{(4 \pi - \theta)^2} + \frac{37324800 c^2 \pi \theta^2}{(4 \pi - \theta)^3} - \right. \\
& \quad \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} + \frac{18662400 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4665600 c^2 \theta^4 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{2332800 c^2 \theta^4 \text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left. \left( 2160 \sqrt{\frac{1166400 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18662400 c^2 \pi \theta^2}{4 \pi - \theta} - \frac{1166400 c^2 \theta^4 \text{Csc}[\theta]^2}{\pi^2}}{4 \pi^2}} \right) \right), \\
& \{\theta, -1300000000, 1300000000\} ]
\end{aligned}$$

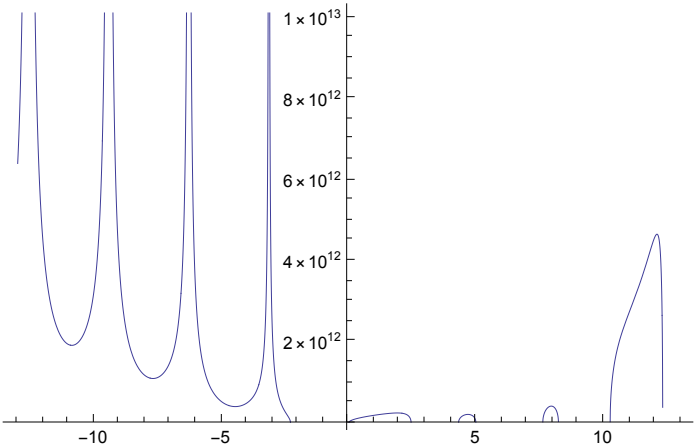


$$\begin{aligned}
& \text{PolarPlot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi - \theta} + \right. \right. \right. \right. \\
& \quad \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \\
& \quad \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right) \right) / \\
& \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi - \theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi - \theta)^2} + \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^3} - \right. \\
& \quad \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left. \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right), \{\theta, -13, 13\} \right]
\end{aligned}$$


$$\begin{aligned}
& \text{PolarPlot}\left[\frac{1}{1080} \pi \right. \\
& \left. - \left( \pi \left( \frac{2\,332\,800\,c^2\,\theta\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^2\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi\,\theta}{4\,\pi - \theta} + \right. \right. \right. \right. \\
& \quad \left. \frac{18\,662\,400\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^2} - \frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi^2} + \right. \\
& \quad \left. \left. \left. \frac{2\,332\,800\,c^2\,\theta^4\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} \right) \right) \right) \right) / \\
& \left( 4320 \left( \frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2} \right)^{3/2} \right) + \\
& \left( \pi \left( \frac{2\,332\,800\,c^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{9\,331\,200\,c^2\,\theta\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} + \right. \right. \\
& \quad \frac{4\,665\,600\,c^2\,\theta^2\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{2\,332\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^4}{\pi^2} - \\
& \quad \frac{1}{4\,\pi^2} \left( \frac{37\,324\,800\,c^2\,\pi}{4\,\pi - \theta} + \frac{74\,649\,600\,c^2\,\pi\,\theta}{(4\,\pi - \theta)^2} + \frac{37\,324\,800\,c^2\,\pi\,\theta^2}{(4\,\pi - \theta)^3} - \right. \\
& \quad \frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} + \frac{18\,662\,400\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi^2} - \\
& \quad \left. \left. \left. \frac{4\,665\,600\,c^2\,\theta^4\,\text{Cot}[\theta]^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{2\,332\,800\,c^2\,\theta^4\,\text{Csc}[\theta]^4}{\pi^2} \right) \right) \right) / \\
& \left. \left( 2160 \sqrt{\frac{1\,166\,400\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi^2} - \frac{\frac{18\,662\,400\,c^2\,\pi\,\theta^2}{4\,\pi - \theta} - \frac{1\,166\,400\,c^2\,\theta^4\,\text{Csc}[\theta]^2}{\pi^2}}{4\,\pi^2}} \right), \{\theta, -130, 130\} \right]
\end{aligned}$$


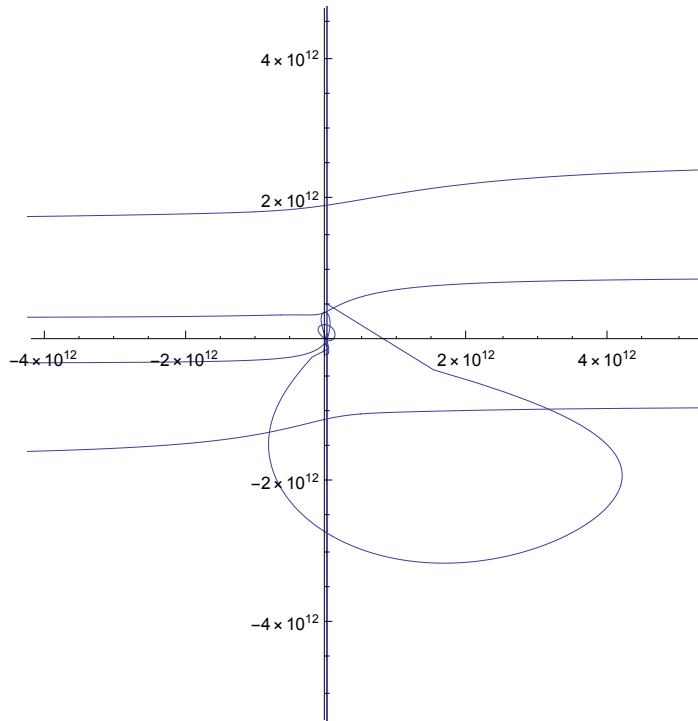
Expression for  $r_1$ , no. 6

Plot[  
$$\sqrt{\left(\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2 - \frac{\sqrt{4\,\pi}\left(\frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\,\pi-\theta)\,\theta}\,\text{Csc}[\theta]}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2\theta^2}{2\,\pi}\right)^2}, \{\theta, -13, 13\}]$$



PolarPlot[

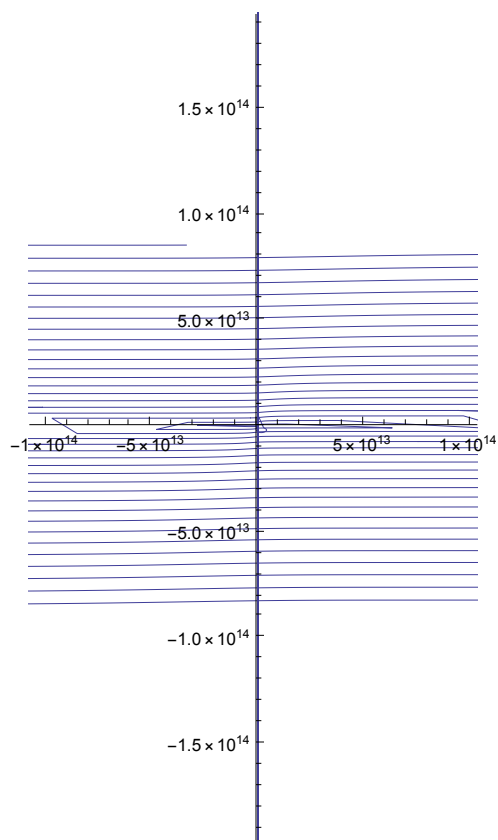
$$\sqrt{\left(\left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}}{2 \pi}\right)^2}, \{\theta, -13, 13\}]$$



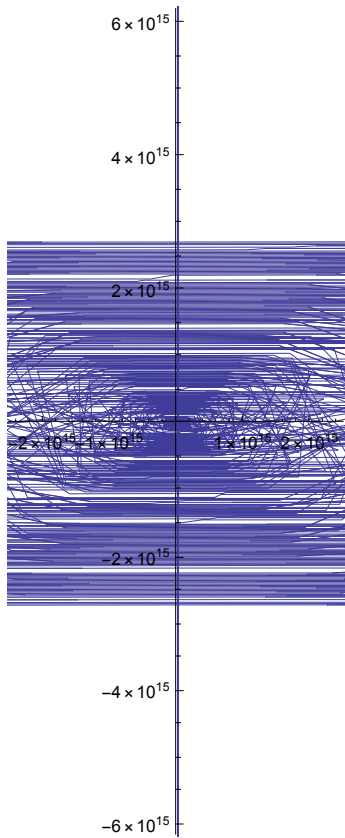


PolarPlot[

$$\sqrt{\left(\left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \frac{\sqrt{4 \pi} \left(\frac{1080 c \sqrt{\theta} \sqrt{(4 \pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4 \pi - \theta}}\right)^2 \theta - \left(\frac{2160 c \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}{2 \pi}\right)^2}, \{\theta, -130, 130\}]$$



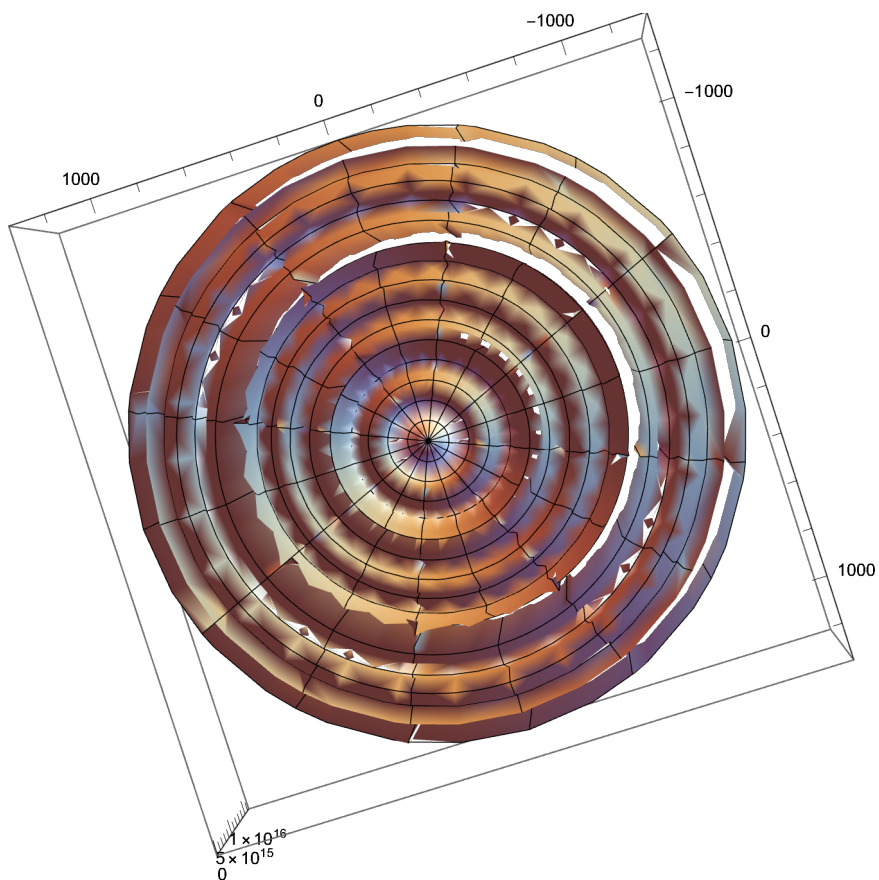
$$\text{PolarPlot}\left[\sqrt{\left(\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2 - \frac{\sqrt{4\,\pi}\left(\frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\,\pi-\theta)}\,\theta\,\text{Csc}[\theta]}{\pi\,\sqrt{4\,\pi-\theta}}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2\theta^2}{2\,\pi}\right)^2},\right. \\
\left.\{\theta, -1300, 1300\}\right]$$



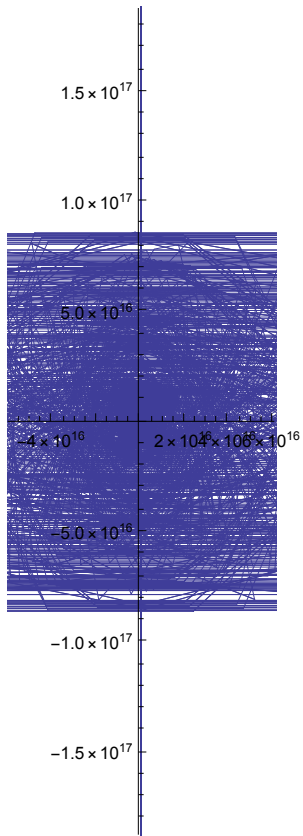
RevolutionPlot3D[

$$\sqrt{\left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 - \frac{\left(\sqrt{4 \pi \left(\frac{1080 \, c \, \sqrt{\theta} \, \sqrt{(4 \pi - \theta) \, \theta} \, \text{Csc}[\theta]}\right)^2 \theta - \left(\frac{2160 \, c \, \sqrt{\theta}}{\sqrt{4 \pi - \theta}}\right)^2 \theta^2}\right)^2}{2 \pi}}},$$

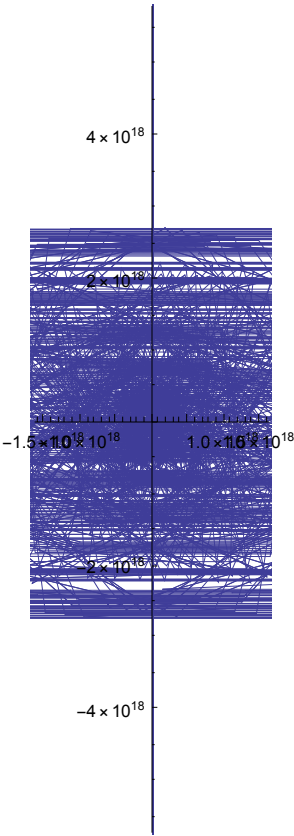
{\theta, -1300, 1300}]



$$\text{PolarPlot}\left[\sqrt{\left(\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2 - \frac{\sqrt{4\,\pi}\left(\frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\,\pi-\theta)\,\theta}\,\text{Csc}[\theta]}{\pi\,\sqrt{4\,\pi-\theta}}\right)^2\theta - \left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2\theta^2}{2\,\pi}\right)^2},\right. \\ \left.\{\theta, -13\,000, 13\,000\}\right]$$



$$\text{PolarPlot}\left[\sqrt{\left(\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2-\frac{\sqrt{4\,\pi}\left(\frac{1080\,c\,\sqrt{\theta}\,\sqrt{(4\,\pi-\theta)}\,\theta\,\text{Csc}[\theta]}{\pi\,\sqrt{4\,\pi-\theta}}\right)^2\theta-\left(\frac{2160\,c\,\sqrt{\theta}}{\sqrt{4\,\pi-\theta}}\right)^2\theta^2}{2\,\pi}\right)^2},\right. \\ \left.\{\theta,-130\,000,130\,000\}\right]$$



First and Second derivatives of expression for  $r_1$ , no. 6

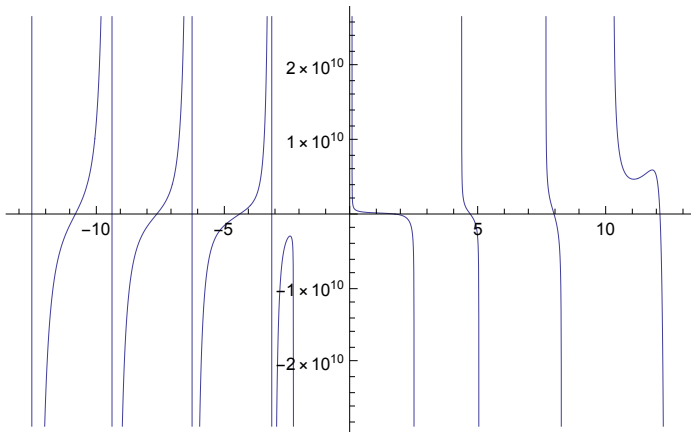
$$\frac{1}{1080} \pi D \left[ \sqrt{\left( \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right)^2 - \left( \frac{\sqrt{4\pi \left( \frac{1080 c \sqrt{\theta} \sqrt{(4\pi - \theta) \theta} \operatorname{Csc}[\theta]}{\pi \sqrt{4\pi - \theta}} \right)^2 \theta - \left( \frac{2160 c \sqrt{\theta}}{\sqrt{4\pi - \theta}} \right)^2 \theta^2}}{2\pi} \right)^2} \right)}, \theta \right]$$

$$\left( \pi \left( \frac{4665600 c^2}{4\pi - \theta} + \frac{4665600 c^2 \theta}{(4\pi - \theta)^2} - \frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) / 4\pi^2 \right]$$

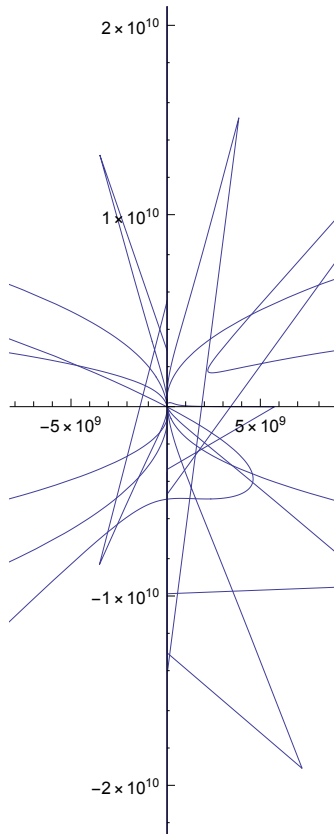
$$\left( 2160 \sqrt{\frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right)$$

$$\text{Plot} \left[ \left( \pi \left( \frac{4665600 c^2}{4\pi - \theta} + \frac{4665600 c^2 \theta}{(4\pi - \theta)^2} - \frac{1}{4\pi^2} \left( -\frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \operatorname{Cot}[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) \right) / \right]$$

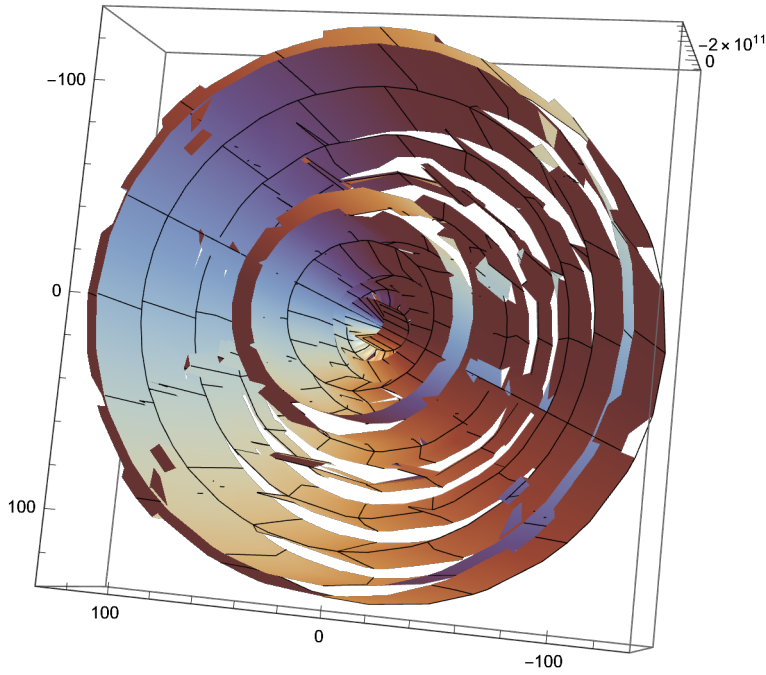
$$\left( 2160 \sqrt{\frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right), \{\theta, -13, 13\}]$$



$$\text{PolarPlot}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta}{(4\pi-\theta)^2}-\frac{1}{4\pi^2}\left(-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}+\frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi-\theta}-\frac{-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi}}{4\pi^2}}\right),\{\theta,-13,13\}\right]$$

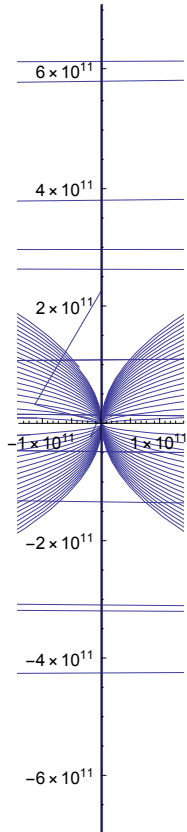


$$\text{RevolutionPlot3D}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta}{(4\pi-\theta)^2}-\frac{1}{4\pi^2}\left(-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}+\frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi-\theta}-\frac{-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi}}{4\pi^2}}\right),\{\theta,-130,130\}\right]$$

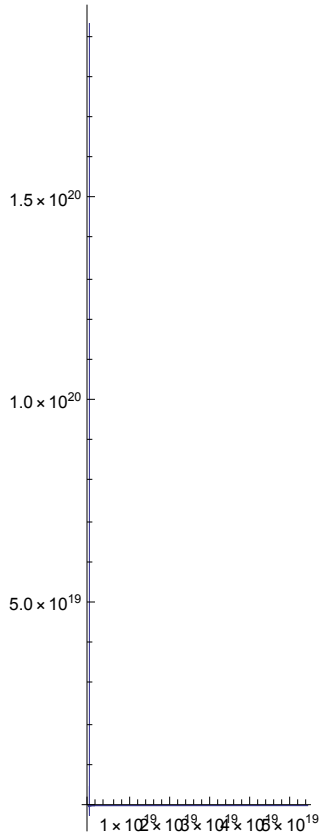




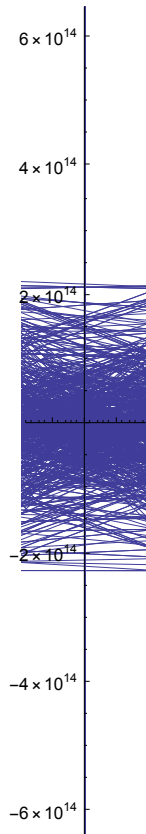
$$\text{PolarPlot}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta}{(4\pi-\theta)^2}-\frac{1}{4\pi^2}\left(-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}+\frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi-\theta}-\frac{-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi}}{4\pi^2}}\right),\{\theta,-130,130\}\right]$$



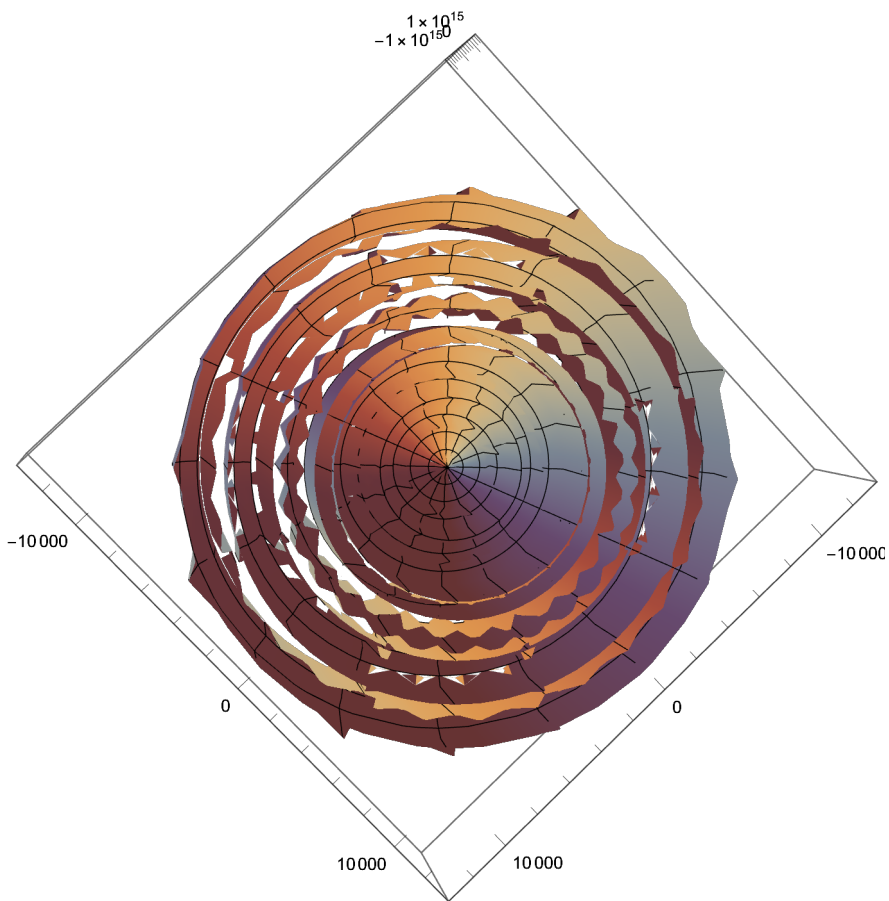
$$\text{PolarPlot}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta}{(4\pi-\theta)^2}-\frac{1}{4\pi^2}\left(-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}+\frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi-\theta}-\frac{-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi}}{4\pi^2}}\right),\{\theta,-1300,1300\}\right]$$



$$\text{PolarPlot}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta}{(4\pi-\theta)^2}-\frac{1}{4\pi^2}\left(-\frac{13\,996\,800\,c^2\theta^2}{4\pi-\theta}-\frac{4\,665\,600\,c^2\theta^3}{(4\pi-\theta)^2}+\frac{13\,996\,800\,c^2\theta^2\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\theta^3\text{Cot}[\theta]\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\theta}{4\pi-\theta}-\frac{-\frac{4\,665\,600\,c^2\theta^3}{4\pi-\theta}+\frac{4\,665\,600\,c^2\theta^3\text{Csc}[\theta]^2}{\pi}}{4\pi^2}}\right),\{\theta,-13\,000,13\,000\}\right]$$

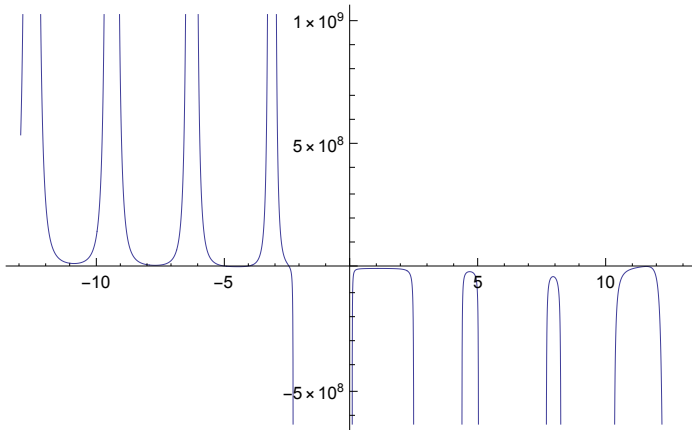


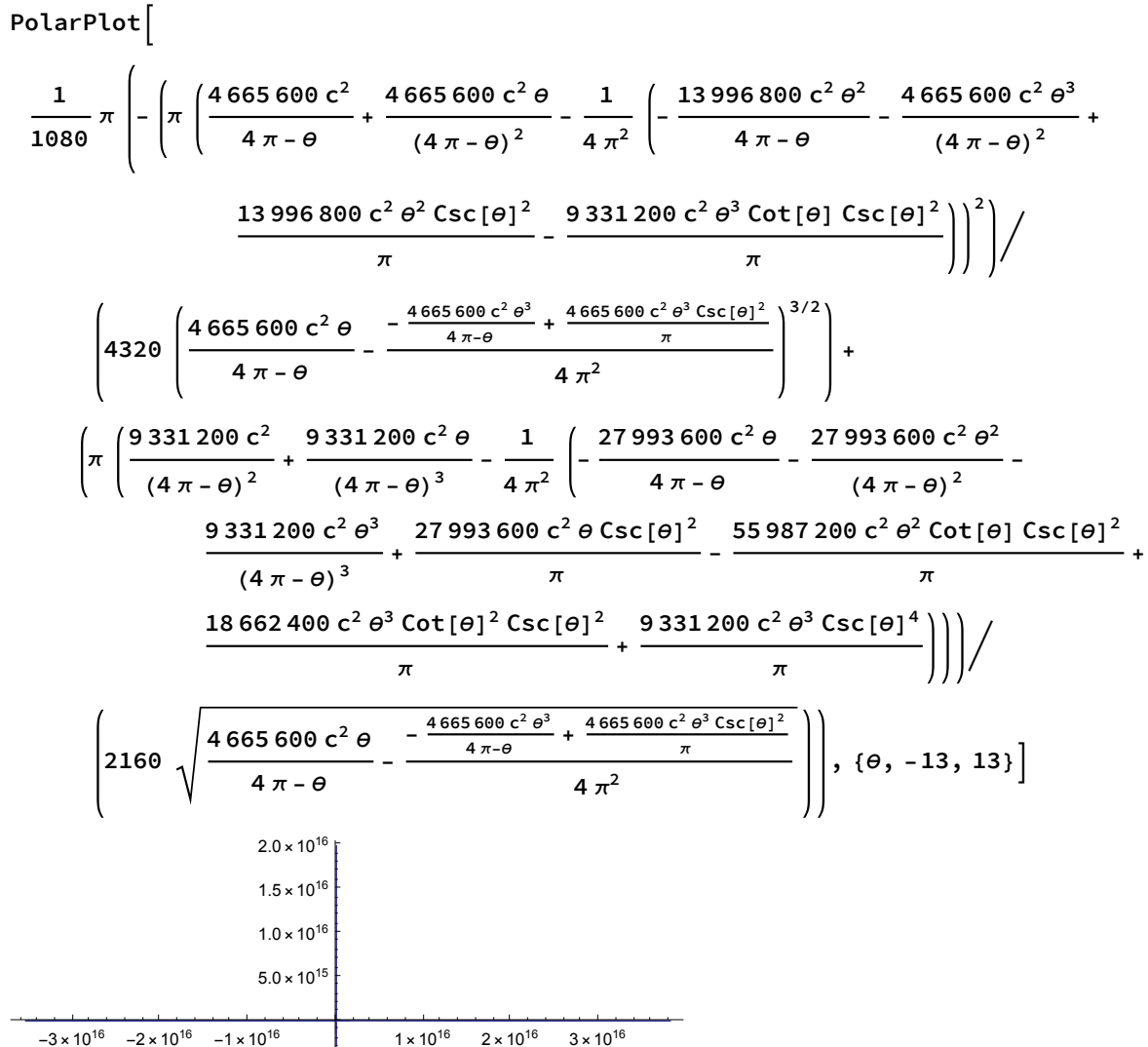
$$\text{RevolutionPlot3D}\left[\left(\pi\left(\frac{4\,665\,600\,c^2}{4\,\pi-\theta}+\frac{4\,665\,600\,c^2\,\theta}{(4\,\pi-\theta)^2}-\frac{1}{4\,\pi^2}\left(-\frac{13\,996\,800\,c^2\,\theta^2}{4\,\pi-\theta}-\frac{4\,665\,600\,c^2\,\theta^3}{(4\,\pi-\theta)^2}+\frac{13\,996\,800\,c^2\,\theta^2\,\text{Csc}[\theta]^2}{\pi}-\frac{9\,331\,200\,c^2\,\theta^3\,\text{Cot}[\theta]\,\text{Csc}[\theta]^2}{\pi}\right)\right)\right)/\right. \\ \left.\left(2160\sqrt{\frac{4\,665\,600\,c^2\,\theta}{4\,\pi-\theta}-\frac{-\frac{4\,665\,600\,c^2\,\theta^3}{4\,\pi-\theta}+\frac{4\,665\,600\,c^2\,\theta^3\,\text{Csc}[\theta]^2}{\pi}}{4\,\pi^2}}\right),\{\theta,-13\,000,13\,000\}\right]$$



$$\begin{aligned}
& \frac{1}{1080} \pi D \left[ \left( \pi \left( \frac{4665600 c^2}{4\pi - \theta} + \frac{4665600 c^2 \theta}{(4\pi - \theta)^2} - \frac{1}{4\pi^2} \left( -\frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) \right) \right) / \\
& \quad \left( 2160 \sqrt{\frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right), \theta \Big] \\
& \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{4665600 c^2}{4\pi - \theta} + \frac{4665600 c^2 \theta}{(4\pi - \theta)^2} - \frac{1}{4\pi^2} \left( -\frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{13996800 c^2 \theta^2 \operatorname{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi} \right) \right) \right) \right) / \\
& \quad \left( 4320 \left( \frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2} \right)^{3/2} \right) + \\
& \quad \left( \pi \left( \frac{9331200 c^2}{(4\pi - \theta)^2} + \frac{9331200 c^2 \theta}{(4\pi - \theta)^3} - \frac{1}{4\pi^2} \left( -\frac{27993600 c^2 \theta}{4\pi - \theta} - \frac{27993600 c^2 \theta^2}{(4\pi - \theta)^2} - \right. \right. \right. \\
& \quad \left. \left. \frac{9331200 c^2 \theta^3}{(4\pi - \theta)^3} + \frac{27993600 c^2 \theta \operatorname{Csc}[\theta]^2}{\pi} - \frac{55987200 c^2 \theta^2 \cot[\theta] \operatorname{Csc}[\theta]^2}{\pi} + \right. \right. \\
& \quad \left. \left. \frac{18662400 c^2 \theta^3 \cot[\theta]^2 \operatorname{Csc}[\theta]^2}{\pi} + \frac{9331200 c^2 \theta^3 \operatorname{Csc}[\theta]^4}{\pi} \right) \right) \right) / \\
& \quad \left( 2160 \sqrt{\frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \operatorname{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right) \Big]
\end{aligned}$$

$$\begin{aligned}
& \text{Plot} \left[ \frac{1}{1080} \pi \left( - \left( \pi \left( \frac{4665600 c^2}{4\pi - \theta} + \frac{4665600 c^2 \theta}{(4\pi - \theta)^2} - \frac{1}{4\pi^2} \left( - \frac{13996800 c^2 \theta^2}{4\pi - \theta} - \frac{4665600 c^2 \theta^3}{(4\pi - \theta)^2} + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{13996800 c^2 \theta^2 \text{Csc}[\theta]^2}{\pi} - \frac{9331200 c^2 \theta^3 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} \right) \right)^2 \right) / \right. \\
& \quad \left( 4320 \left( \frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi}}{4\pi^2} \right)^{3/2} \right) + \\
& \quad \left( \pi \left( \frac{9331200 c^2}{(4\pi - \theta)^2} + \frac{9331200 c^2 \theta}{(4\pi - \theta)^3} - \frac{1}{4\pi^2} \left( - \frac{27993600 c^2 \theta}{4\pi - \theta} - \frac{27993600 c^2 \theta^2}{(4\pi - \theta)^2} - \right. \right. \right. \\
& \quad \left. \left. \frac{9331200 c^2 \theta^3}{(4\pi - \theta)^3} + \frac{27993600 c^2 \theta \text{Csc}[\theta]^2}{\pi} - \frac{55987200 c^2 \theta^2 \text{Cot}[\theta] \text{Csc}[\theta]^2}{\pi} + \right. \right. \\
& \quad \left. \left. \frac{18662400 c^2 \theta^3 \text{Cot}[\theta]^2 \text{Csc}[\theta]^2}{\pi} + \frac{9331200 c^2 \theta^3 \text{Csc}[\theta]^4}{\pi} \right) \right) / \right. \\
& \quad \left. \left( 2160 \sqrt{\frac{4665600 c^2 \theta}{4\pi - \theta} - \frac{-\frac{4665600 c^2 \theta^3}{4\pi - \theta} + \frac{4665600 c^2 \theta^3 \text{Csc}[\theta]^2}{\pi}}{4\pi^2}} \right) \right], \{\theta, -13, 13\}
\end{aligned}$$





# On Formulations of Pythagorean Theorem

by Parker Emerson

Why this can help us prove string theory? Within even the smallest unit of time, there is an implied ten dimensionality. Because it is mathematically proven, it is no longer theoretical. The mathematics is directly correlated to the perceptual experience just as the geometer measures as he perceives.

## Preface :

$$r^2 = \eta^2 + r_1^2$$

$$\theta r = 2\pi r - 2\pi r_1 = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$$

$$\theta r - 2\pi r = -2\pi \sqrt{r^2 - \eta^2}$$

$$\frac{\theta r - 2\pi r}{2\pi} = -\sqrt{r^2 - \eta^2}$$

$$\left(\frac{\theta r - 2\pi r}{2\pi}\right)^2 = (r^2 - \eta^2)$$

$$\left(\frac{\theta r - 2\pi r}{2\pi}\right)^2 + \eta^2 = r^2 = \eta^2 + r_1^2$$

## Relevant Lemmas to the Formulation

**Lemma 4** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\beta$  is a function of  $\theta$  alone.

Proof. Since we have shown that  $\theta r = 2\pi r - 2\pi r_1$  and  $r_1 \rightarrow \sqrt{r^2 - \eta^2}$ , we can substitute the expression for  $r_1$ , calculated from the Pythagorean theorem in terms of the height of the cone and the initial radius of the circle, into the expression for  $\theta r$  in terms of the change in circumference of the initial circle to the circle, which is the base of the cone.  $\theta r = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$ , thus,  $\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = (r \sin[\beta])$ . From  $\frac{2\pi \eta}{\sqrt{4\pi r^2 \theta - r^2 \theta^2}} = r$ , we note that  $r = \frac{2\pi r \sin[\beta]}{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}$ , so

$$\theta = 2 \left( \pi \pm \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) = \frac{2\pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2}, \text{ because } 1 = \frac{2\pi \sin[\beta]}{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}$$

**Lemma 6** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\theta$  is a function of  $\beta$  alone, and the initial radius can be calculated purely in terms of the angle  $\theta$ .

$$\beta = \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta) \theta}}{2\pi} \right]$$

$$\sin[\beta] = \frac{\eta}{r} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{r 2\pi} = \frac{4\pi r^2 \theta - r^2 \theta^2}{4\pi^2 r} = \frac{r(4\pi - \theta) \theta}{4\pi^2}$$

$$\beta \rightarrow \text{ArcSin} \left[ \frac{4\pi r \theta - r \theta^2}{4\pi^2} \right] = \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta) \theta}}{2\pi} \right]$$

$$\text{Solve} \left[ \text{ArcSin} \left[ \frac{4\pi r \theta - r \theta^2}{4\pi^2} \right] == \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta) \theta}}{2\pi} \right], r \right]$$

$$\left\{ \left\{ r \rightarrow \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta} \right\} \right\}$$



A quick calculation:

$$\text{Solve}\left[r == \frac{2\pi \sqrt{\left(4\pi - \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}\right) \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}}}{\left(4\pi - \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}\right) \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}}, \eta\right]$$

$$\{\{\eta \rightarrow -1\}, \{\eta \rightarrow 1\}\}$$

$$\text{Solve}\left[r == \frac{2\pi \sqrt{\left(4\pi - \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}\right) \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}}}{\left(4\pi - \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}\right) \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}}, r\right]$$

$$\{\}$$

$$\text{Solve}\left[r == \frac{2\pi \sqrt{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{1}{r}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{1}{r}\right]\right\}\right\}$$

$$\text{Solve}\left[r == \frac{2\pi \sqrt{\left(4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\left(4\pi - \frac{2\pi(r^2 + \sqrt{r^4 - r^2\eta^2})}{r^2}\right) 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}, \eta\right]$$

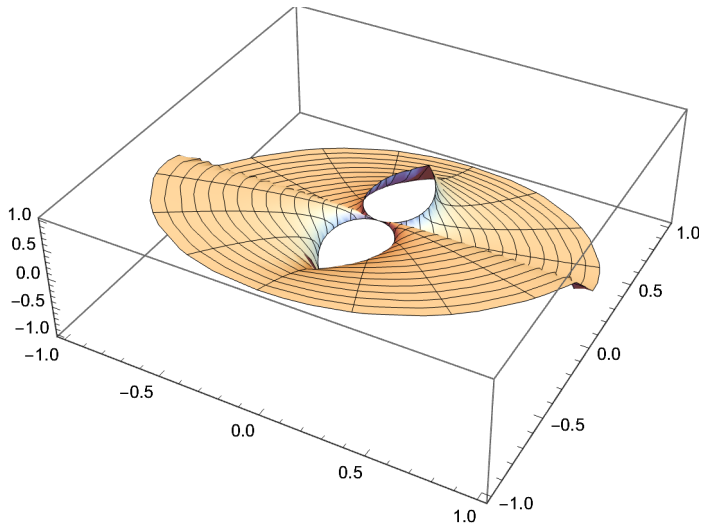
$$\left\{\left\{\eta \rightarrow -\frac{1}{\sqrt{\pi}} \text{Csc}[\beta] \sqrt{\left(-2\pi + \pi \sin[\beta]^2 +\right.}\right.\right.$$

$$\left.2\pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])} + \sqrt{2} r \sqrt{\left((\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])})\right)}\right. \\ \left. \left(4\pi - 2\left(\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])}\right)\right)\right) - \\ \left. \sqrt{2} r \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])} \sqrt{\left((\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])})\right)}\right. \\ \left. \left(4\pi - 2\left(\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])}\right)\right)\right)\right\},$$

$$\left\{\eta \rightarrow \frac{1}{\sqrt{\pi}} \text{Csc}[\beta] \sqrt{\left(-2\pi + \pi \sin[\beta]^2 + 2\pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])} +\right.}\right.$$

$$\left. \sqrt{2} r \sqrt{\left((\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])})\right)}\right. \\ \left. \left(4\pi - 2\left(\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])}\right)\right)\right) - \\ \left. \sqrt{2} r \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])} \sqrt{\left((\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])})\right)}\right. \\ \left. \left(4\pi - 2\left(\pi + \pi \sqrt{-(-1 + \sin[\beta])(1 + \sin[\beta])}\right)\right)\right)\right\}$$

$\text{RevolutionPlot3D}\left[-\frac{1}{\sqrt{\pi}} \csc[\beta] \sqrt{(-2\pi + \pi \sin[\beta])^2 + 2\pi \sqrt{(-1 + \sin[\beta])(1 + \sin[\beta])} + \sqrt{2} r \sqrt{((\pi + \pi \sqrt{(-1 + \sin[\beta])(1 + \sin[\beta])}) (4\pi - 2(\pi + \pi \sqrt{(-1 + \sin[\beta])(1 + \sin[\beta])})) - \sqrt{2} r \sqrt{(-1 + \sin[\beta])(1 + \sin[\beta])} \sqrt{((\pi + \pi \sqrt{(-1 + \sin[\beta])(1 + \sin[\beta])}) (4\pi - 2(\pi + \pi \sqrt{(-1 + \sin[\beta])(1 + \sin[\beta])}))}})}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$



```

RevolutionPlot3D[
{

$$\frac{1}{\sqrt{\pi}} \operatorname{Csc}[\beta] \sqrt{\left(-2 \pi + \pi \operatorname{Sin}[\beta]^2 + 2 \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])} + \sqrt{2} r\right.}$$


$$\left. \sqrt{\left(\left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right) \left(4 \pi -\right.\right.}\right.$$


$$\left. \left. 2 \left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right)\right)\right) -}$$

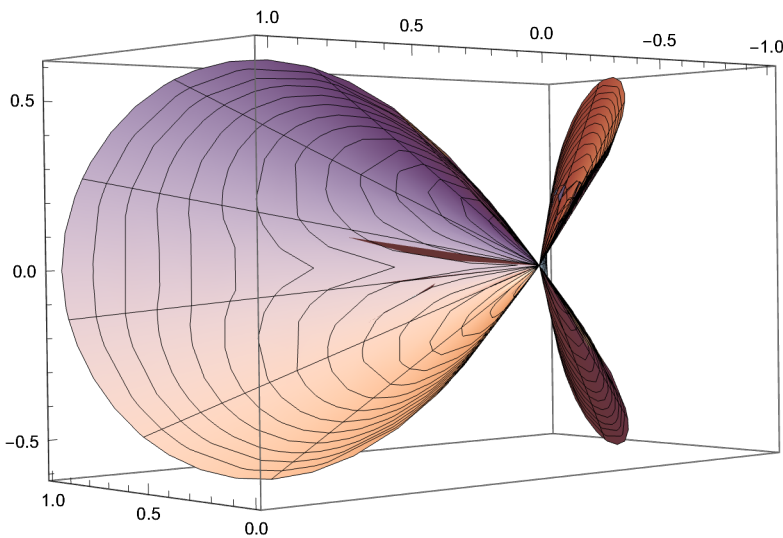
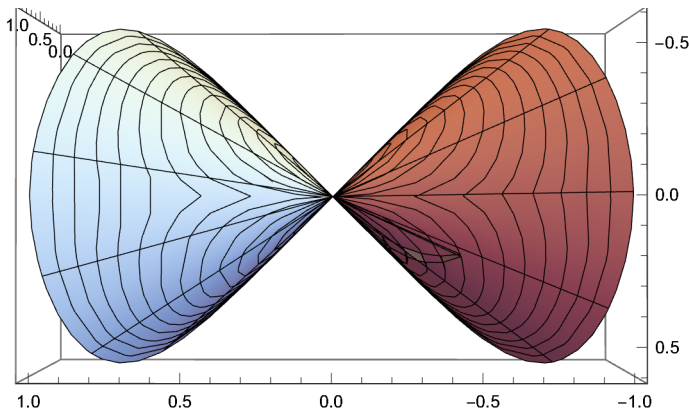

$$\sqrt{2} r \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])} \sqrt{\left(\left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right) \left(4 \pi - 2 \left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right)\right)\right)},$$


$$- \frac{1}{\sqrt{\pi}} \operatorname{Csc}[\beta] \sqrt{\left(-2 \pi + \pi \operatorname{Sin}[\beta]^2 + 2 \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])} + \sqrt{2} r\right.}$$


$$\left. \sqrt{\left(\left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right) \left(4 \pi - 2 \left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right)\right)\right) -}$$


$$\sqrt{2} r \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])} \sqrt{\left(\left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right) \left(4 \pi - 2 \left(\pi + \pi \sqrt{-(-1 + \operatorname{Sin}[\beta]) (1 + \operatorname{Sin}[\beta])}\right)\right)\right)}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}]$$

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The Formulation of New Pythagorean Expressions from

## Difference in Circumferences Equals an Arc Length of the Initial Circle (Which is Folded into a Cone) Applied to Pythagorean Theorem

$$r^2 = \eta^2 + r_1^2$$

$$r \rightarrow \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}$$

$$\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}^2 = \eta^2 + r_1^2$$

$$r^2 = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2 + r_1^2 = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi r}{2\pi}^2$$

### Substitutions that Cancel

$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi r}{2\pi}^2, r\right]$$

{{}}

$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi r}{2\pi}^2, \theta\right]$$

{{}}

$$\text{Solve}\left[\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}^2 == \frac{\sqrt{4\pi \left(\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}\right)^2 \theta - \left(\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}\right)^2 \theta^2}}{2\pi}^2 + \frac{\theta \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} - 2\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}}{2\pi}^2, \theta\right]$$

{{}}

### Substitutions that Don't Cancel

$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi (r)^2 \theta - (r)^2 \theta^2}}{2\pi}^2 + \frac{\theta \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} - 2\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}}{2\pi}^2, \theta\right]$$

$$\left\{\{\theta \rightarrow 2\pi\}, \{\theta \rightarrow 2\pi\}, \left\{\theta \rightarrow \frac{2\pi \left(r^2 - \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi \left(r^2 + \sqrt{-r^2 + r^4}\right)}{r^2}\right\}\right\}$$

$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}}{2\pi}^2, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow \frac{3\pi}{2} - \frac{1}{2}\sqrt{\left(3\pi^2 + \frac{\pi^2(16r^2 + 3r^4)}{3^{1/3}r^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}} + \frac{\pi^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}}{3^{2/3}r^2}\right)}\right\} -$$

$$\frac{1}{2}\sqrt{\left(6\pi^2 - \frac{\pi^2(16r^2 + 3r^4)}{3^{1/3}r^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}} - \frac{\pi^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}}{3^{2/3}r^2} -$$

$$(8\pi^3) \Bigg/ \left( \sqrt{\left(3\pi^2 + \frac{\pi^2(16r^2 + 3r^4)}{3^{1/3}r^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}} + \frac{\pi^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}}{3^{2/3}r^2}\right)} \right) \Bigg\},$$

$$\left\{\theta \rightarrow \frac{3\pi}{2} - \frac{1}{2}\sqrt{\left(3\pi^2 + \frac{\pi^2(16r^2 + 3r^4)}{3^{1/3}r^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}} + \frac{\pi^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}}{3^{2/3}r^2}\right)} +$$

$$\frac{1}{2}\sqrt{\left(6\pi^2 - \frac{\pi^2(16r^2 + 3r^4)}{3^{1/3}r^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}} - \frac{\pi^2(216r^4 - 9r^6 + 8\sqrt{3}\sqrt{-64r^6 + 207r^8 - 27r^{10}})^{1/3}}{3^{2/3}r^2} -$$

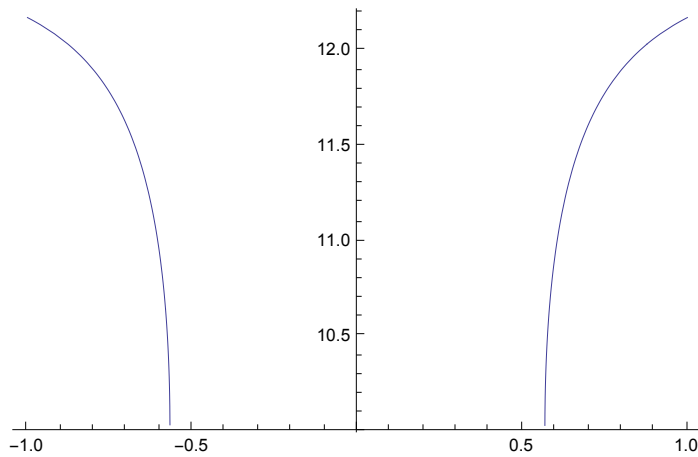
$$\begin{aligned}
& (8 \pi^3) / \left( \left( \left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}} + \right. \right. \right. \\
& \quad \left. \left. \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) \right) \right\}, \\
& \left\{ \theta \rightarrow \frac{3 \pi}{2} + \frac{1}{2} \sqrt{\left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) \right\} - \\
& \frac{1}{2} \sqrt{\left( 6 \pi^2 - \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}} - \right. \\
& \quad \left. \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} + \right. \\
& \quad (8 \pi^3) / \left( \left( \left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}} + \right. \right. \right. \\
& \quad \left. \left. \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) \right) \right\}, \\
& \left\{ \theta \rightarrow \frac{3 \pi}{2} + \frac{1}{2} \sqrt{\left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}} + \right. \right. \\
& \quad \left. \left. \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) \right\} + \\
& \frac{1}{2} \sqrt{\left( 6 \pi^2 - \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}} - \right. \\
& \quad \left. \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} + \right.
\end{aligned}$$

$$(8 \pi^3) / \left( \sqrt[3]{ \left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3} + \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) } \right) \right\}$$

$$\text{Plot} \left[ \frac{3 \pi}{2} + \frac{1}{2} \sqrt[3]{ \left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3} + \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) } \right] +$$

$$\frac{1}{2} \sqrt[3]{ \left( 6 \pi^2 - \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3} - \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) } -$$

$$(8 \pi^3) / \left( \sqrt[3]{ \left( 3 \pi^2 + \frac{\pi^2 (16 r^2 + 3 r^4)}{3^{1/3} r^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3} + \frac{\pi^2 (216 r^4 - 9 r^6 + 8 \sqrt{3} \sqrt{-64 r^6 + 207 r^8 - 27 r^{10}})^{1/3}}{3^{2/3} r^2} \right) } \right) \right\}, \{r, -1, 1\}]$$



Note that r is to the 10 th dimension.

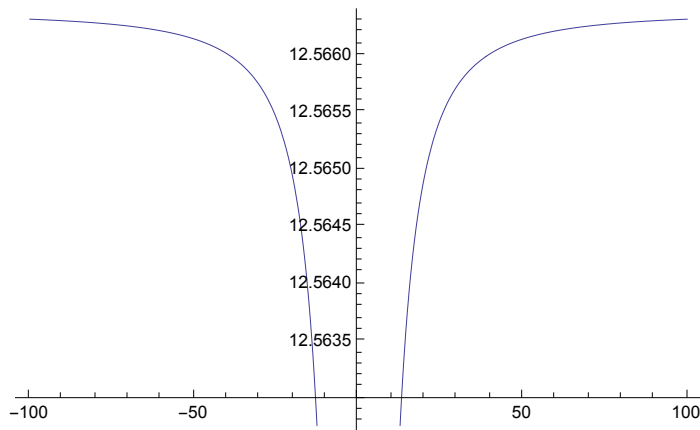
$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - (r)^2\theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}}{2\pi}^2, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi\left(-2 + r^2 - \sqrt{-5r^2 + r^4}\right)}{4 + r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(-2 + r^2 + \sqrt{-5r^2 + r^4}\right)}{4 + r^2}\right\}, \right. \\ \left.\left\{\theta \rightarrow \frac{2\pi\left(r^2 - \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 + \sqrt{-r^2 + r^4}\right)}{r^2}\right\}\right\}$$

$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi(r)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}}{2\pi}^2, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi\left(r^2 - \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 + \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \right. \\ \left\{\theta \rightarrow \text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - \right. \right. \\ \left. \left. 64\pi^3 r^2 \#1^3 + (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 1\right]\right\}, \\ \left\{\theta \rightarrow \text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - 64\pi^3 r^2 \#1^3 + \right. \right. \\ \left. \left. (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 2\right]\right\}, \\ \left\{\theta \rightarrow \text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - 64\pi^3 r^2 \#1^3 + \right. \right. \\ \left. \left. (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 3\right]\right\}, \\ \left\{\theta \rightarrow \text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - 64\pi^3 r^2 \#1^3 + \right. \right. \\ \left. \left. (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 4\right]\right\}, \\ \left\{\theta \rightarrow \text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - 64\pi^3 r^2 \#1^3 + \right. \right. \\ \left. \left. (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 5\right]\right\}, \\ \left.\left\{\theta \rightarrow \text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - 64\pi^3 r^2 \#1^3 + \right. \right. \right. \\ \left. \left. (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 6\right]\right\}\right\}$$

$$\text{Plot}\left[\text{Root}\left[64\pi^6 - 64\pi^5 r^2 \#1 + (-32\pi^4 + 144\pi^4 r^2) \#1^2 - \right. \right. \\ \left. \left. 64\pi^3 r^2 \#1^3 + (4\pi^2 - 24\pi^2 r^2) \#1^4 + 4\pi r^2 \#1^5 + r^2 \#1^6 \&, 4\right], \{r, -100, 100\}\right]$$

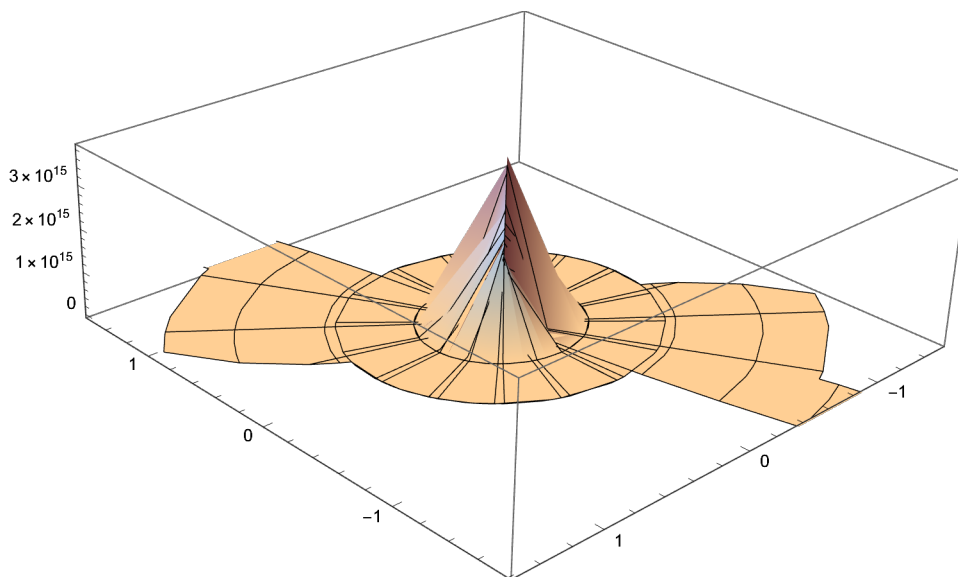
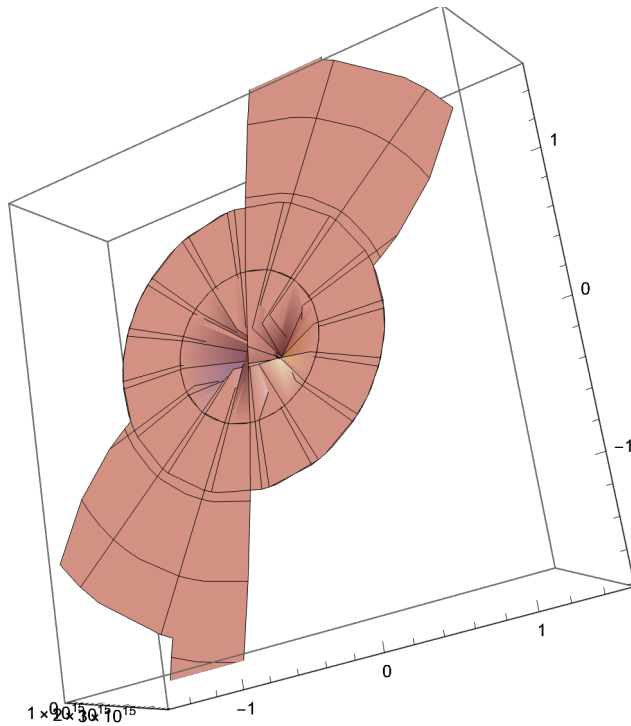




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RevolutionPlot3D[
  Root[64 π^6 - 64 π^5 (2 π √(4 π - θ) θ)^2 #1 + (-32 π^4 + 144 π^4 (2 π √(4 π - θ) θ)^2) #1^2 -
    64 π^3 r^2 #1^3 + (4 π^2 - 24 π^2 (2 π √(4 π - θ) θ)^2) #1^4 + 4 π r^2 #1^5 + r^2 #1^6 &,
  4], {r, -100, 100}, {θ, -2 π, 2 π}]

```



$$\text{Solve}\left[r^2 == \frac{\sqrt{4\pi(r)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi r}{2\pi}^2, \theta\right]$$

$$\left\{\{\theta \rightarrow 0\}, \left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\}\right\}$$

$$\text{Solve}\left[\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}^2 == \frac{\sqrt{4\pi(r)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}^2 + \frac{\theta r - 2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}}{2\pi}^2, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow -\frac{4\pi}{3} + \frac{12\pi^2 r^2 - 64\pi^2 r^4}{6\pi r^2 \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}} -\right.\right.$$

$$\left.\frac{2\pi \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}}{3r^2}\right\},$$

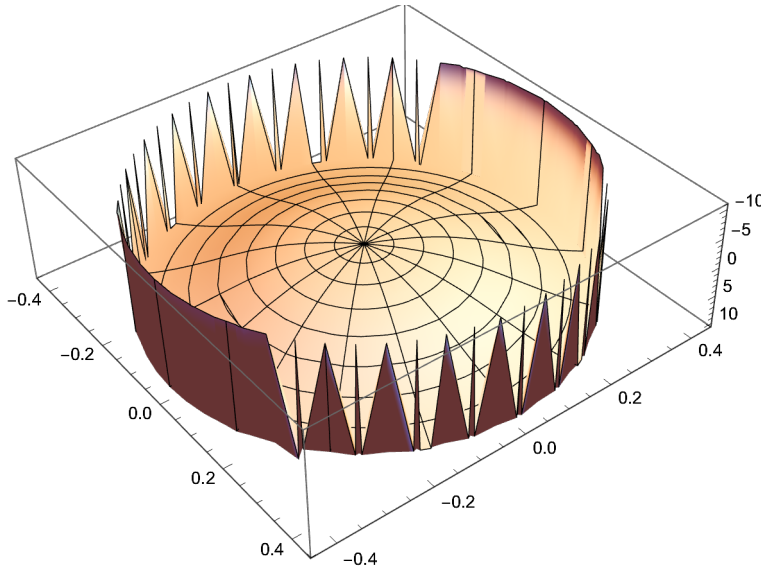
$$\left\{\theta \rightarrow -\frac{4\pi}{3} - \frac{(1 + i\sqrt{3})(12\pi^2 r^2 - 64\pi^2 r^4)}{12\pi r^2 \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}} +\right.$$

$$\left.\frac{(1 - i\sqrt{3})\pi \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}}{3r^2}\right\},$$

$$\left\{\theta \rightarrow -\frac{4\pi}{3} - \frac{(1 - i\sqrt{3})(12\pi^2 r^2 - 64\pi^2 r^4)}{12\pi r^2 \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}} +\right.$$

$$\left.\frac{(1 + i\sqrt{3})\pi \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}}{3r^2}\right\}\}$$

$$\text{RevolutionPlot3D}\left[-\frac{4\pi}{3} + \frac{12\pi^2 r^2 - 64\pi^2 r^4}{6\pi r^2 \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}} - \frac{2\pi \left(-9r^4 - 64r^6 + 3\sqrt{3}\sqrt{r^6 - 13r^8 + 128r^{10}}\right)^{1/3}}{3r^2}, \{r, -1, 1\}\right]$$



# Univocal Radius Solutions Continued

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$$r_1 = \sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}^2\right)} == \frac{2\pi r - r\theta}{2\pi}$$

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}^2\right)} == \frac{2\pi r - r\theta}{2\pi}, \theta\right]$$

{{}}

$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}^2\right)} == \frac{2\pi r - r\theta}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - (r)^2\theta^2}}{2\pi}}\right] == \frac{2\pi r - r\theta}{2\pi}, \theta]$$

$$\left\{\{\theta \rightarrow \pi\}, \left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\}\right\}$$

Solve[

$$\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}}\right] == \frac{2\pi r - r\theta}{2\pi}, \theta]$$

$$\left\{\{\theta \rightarrow 2\pi\}, \left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}}\right] ==$$

$$\frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - r\theta}{2\pi}, \theta]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow 2\left(\frac{\pi}{3^{1/3}(-9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}} - \frac{\pi(-9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}}{3^{2/3}r^2}\right)\right\},\right.$$

$$\left.\left\{\theta \rightarrow -\frac{(1 + i\sqrt{3})\pi}{3^{1/3}(-9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}} + \frac{(1 - i\sqrt{3})\pi(-9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}}{3^{2/3}r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow -\frac{(1 - i\sqrt{3})\pi}{3^{1/3}(-9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}} + \frac{(1 + i\sqrt{3})\pi(-9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}}{3^{2/3}r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}}^2} = \frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, \theta\right]$$

{{}}

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}\right)^2} = \frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi\left(r^2 - \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 + \sqrt{-r^2 + r^4}\right)}{r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}\right)^2} = \frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, \theta\right]$$

$$\left\{\{\theta \rightarrow \pi\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 - \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 + \sqrt{-r^2 + r^4}\right)}{r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}\right)^2} = \frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, \theta\right]$$

$$\left\{\{\theta \rightarrow 2\pi\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 - \sqrt{-r^2 + r^4}\right)}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi\left(r^2 + \sqrt{-r^2 + r^4}\right)}{r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}\right)^2} == \frac{2\pi r - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, \theta\right]$$

$$\left\{\{\theta \rightarrow 0\}, \left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow 2\left(2\pi + \frac{\pi}{3^{1/3}(9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}} - \frac{\pi(9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}}{3^{2/3}r^2}\right)\right\},\right.$$

$$\left.\left\{\theta \rightarrow 4\pi - \frac{(1 + \text{i}\sqrt{3})\pi}{3^{1/3}(9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}} + \frac{(1 - \text{i}\sqrt{3})\pi(9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}}{3^{2/3}r^2}\right\},\right.$$

$$\left.\left\{\theta \rightarrow 4\pi - \frac{(1 - \text{i}\sqrt{3})\pi}{3^{1/3}(9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}} + \frac{(1 + \text{i}\sqrt{3})\pi(9r^4 + \sqrt{3}\sqrt{r^6 + 27r^8})^{1/3}}{3^{2/3}r^2}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}\right)^2} == \frac{2\pi r - r\theta}{2\pi}, \theta\right]$$

{{}}

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}\right)^2} == \frac{2\pi r - r\theta}{2\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2\pi(r - \sqrt{-1 + r^2})}{r}\right\}\right\}$$

$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi(r)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}\right)^2} == \frac{2\pi r - r\theta}{2\pi}, \theta\right]$$

$$\left\{\{\theta \rightarrow -2\text{i}\pi\}, \{\theta \rightarrow 2\text{i}\pi\}, \left\{\theta \rightarrow \frac{2\pi(r^2 - \sqrt{-r^2 + r^4})}{r^2}\right\}, \left\{\theta \rightarrow \frac{2\pi(r^2 + \sqrt{-r^2 + r^4})}{r^2}\right\}\right\}$$

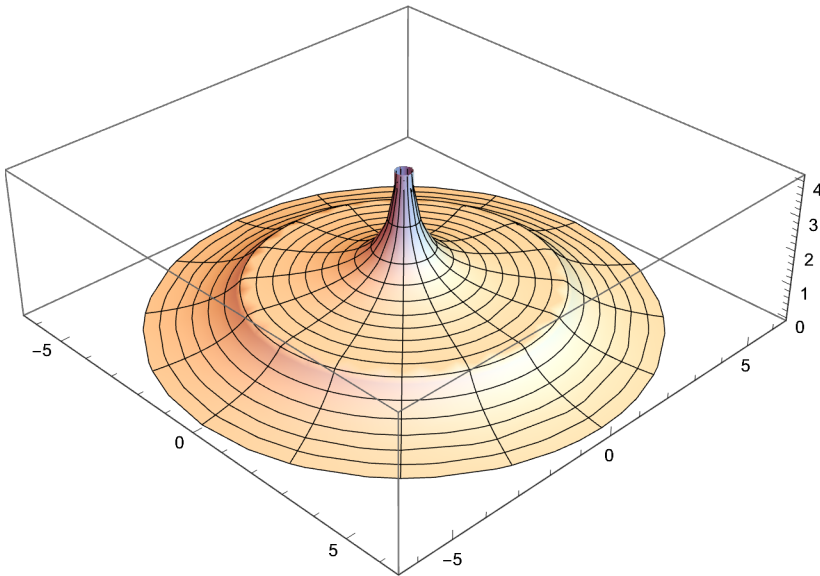
## New Solution 1

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - \left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}}{2\pi}\right)^2} = \frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - r\theta}{2\pi}, r\right]$$

$$\left\{\left\{r \rightarrow \frac{2\pi\left(-2\pi\theta\sqrt{(4\pi-\theta)\theta} - \sqrt{64\pi^5\theta - 80\pi^4\theta^2 + 20\pi^2\theta^4 - \theta^6}\right)}{16\pi^3\theta - 20\pi^2\theta^2 + \theta^4}\right\},\right.$$

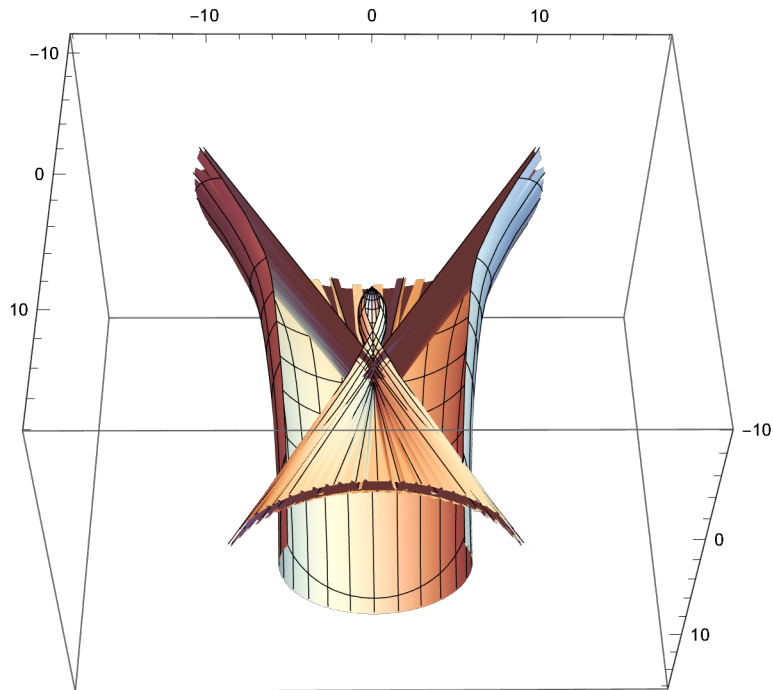
$$\left.\left\{r \rightarrow \frac{2\pi\left(-2\pi\theta\sqrt{(4\pi-\theta)\theta} + \sqrt{64\pi^5\theta - 80\pi^4\theta^2 + 20\pi^2\theta^4 - \theta^6}\right)}{16\pi^3\theta - 20\pi^2\theta^2 + \theta^4}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\frac{2\pi\left(-2\pi\theta\sqrt{(4\pi-\theta)\theta} + \sqrt{64\pi^5\theta - 80\pi^4\theta^2 + 20\pi^2\theta^4 - \theta^6}\right)}{16\pi^3\theta - 20\pi^2\theta^2 + \theta^4}, \{\theta, -2\pi, 2\pi\}\right]$$



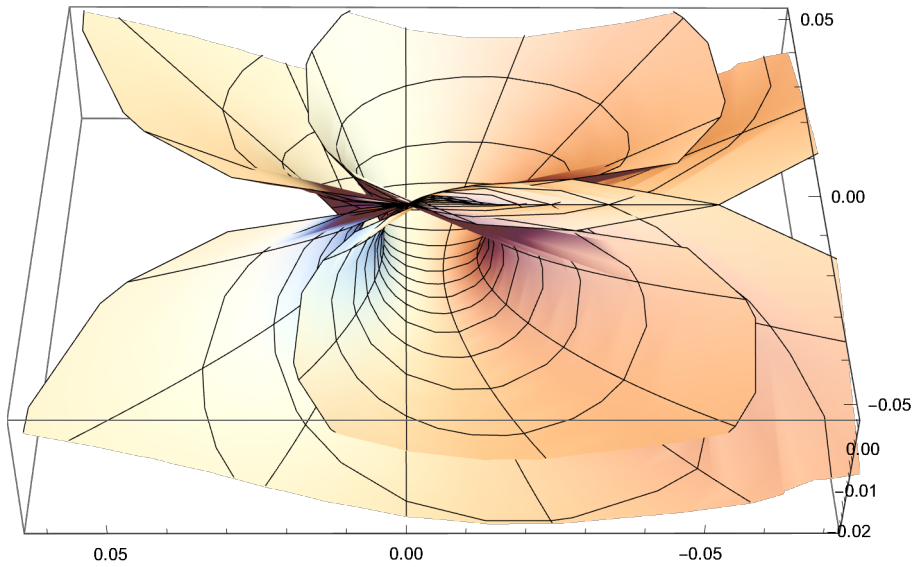
## Solution 1 Substitutions

$$\text{SphericalPlot3D}\left[\frac{1}{16 \pi^3 \theta - 20 \pi^2 \theta^2 + \theta^4},\right. \\ \left.2 \pi \left(-2 \pi \theta \sqrt{(4 \pi - \theta) \theta} + \sqrt{64 \pi^5 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) - 80 \pi^4 \theta^2 + 20 \pi^2 \theta^4 - \theta^6}\right),\right. \\ \left.\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$$

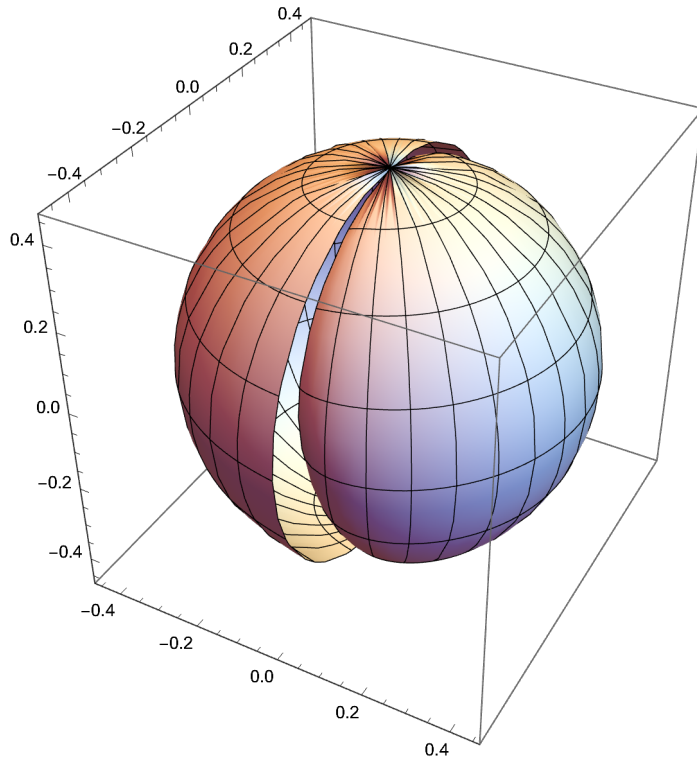




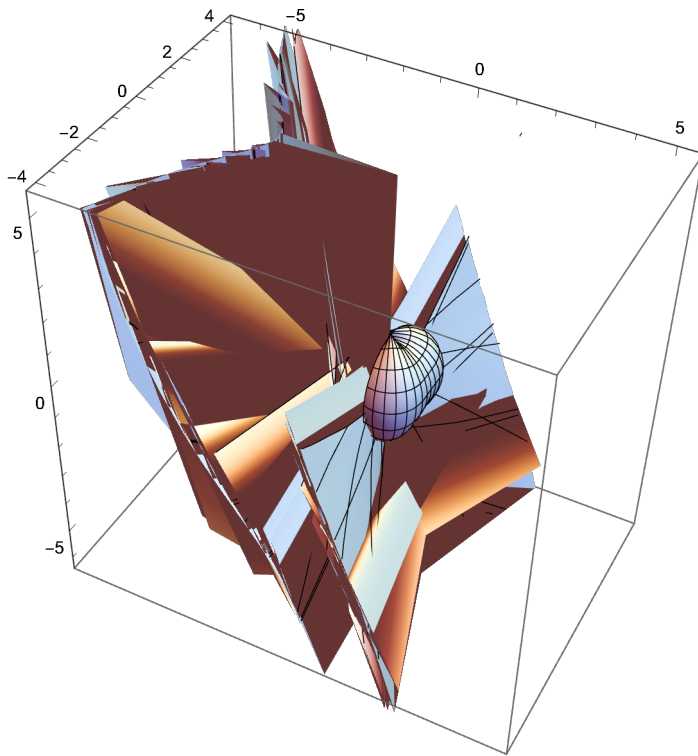
SphericalPlot3D $\left[\frac{1}{16 \pi^3 \theta - 20 \pi^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)^2 + \theta^4},\right.$   
 $2 \pi \left(-2 \pi \theta \sqrt{(4 \pi - \theta) \theta} + \sqrt{64 \pi^5 \theta - 80 \pi^4 \theta^2 + 20 \pi^2 \theta^4 - \theta^6}\right),$   
 $\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$



`SphericalPlot3D` $\left[\frac{1}{16 \pi^3 \theta - 20 \pi^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + (\theta)^4}\right.$   
 $2 \pi \left(-2 \pi \theta \sqrt{(4 \pi - \theta) \theta} + \sqrt{64 \pi^5 \theta - 80 \pi^4 \theta^2 + 20 \pi^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^4 - \theta^6}\right),$   
 $\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$



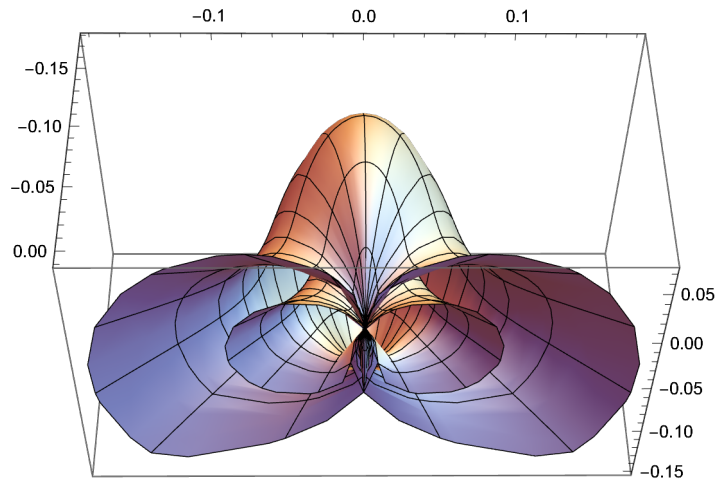
SphericalPlot3D $\left[\frac{1}{16 \pi^3 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) - 20 \pi^2 (\theta)^2 + (\theta)^4} 2 \pi \left(-2 \pi \theta \sqrt{(4 \pi - \theta) \theta} + \sqrt{\left(64 \pi^5 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) - 80 \pi^4 \theta^2 + 20 \pi^2 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)^4 - \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)^6\right)\right)}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



SphericalPlot3D[  

$$\left( \frac{1}{\left( 16 \pi^3 \theta - 20 \pi^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^4 \right) \right)} \right) \right.$$
  

$$\left. 2 \pi \left( -2 \pi \theta \sqrt{(4 \pi - \theta) \theta} + \sqrt{64 \pi^5 \theta - 80 \pi^4 \theta^2 + 20 \pi^2 \theta^4 - \theta^6} \right), \right.$$
  
 $\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$

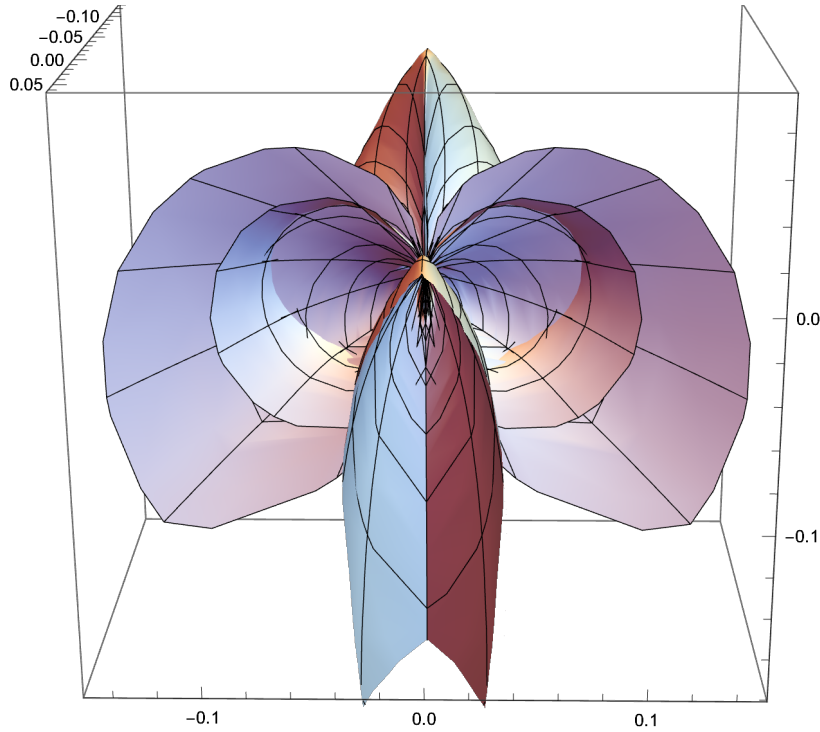


SphericalPlot3D[  

$$\left( \frac{1}{\left( 16 \pi^3 \theta - 20 \pi^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^4 \right) \right)} \right) \right.$$
  

$$\left. 2 \pi \left( -2 \pi \theta \sqrt{\left( 4 \pi - \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \right)} \theta + \sqrt{64 \pi^5 \theta - 80 \pi^4 \theta^2 + 20 \pi^2 \theta^4 - \theta^6} \right), \right.$$
  

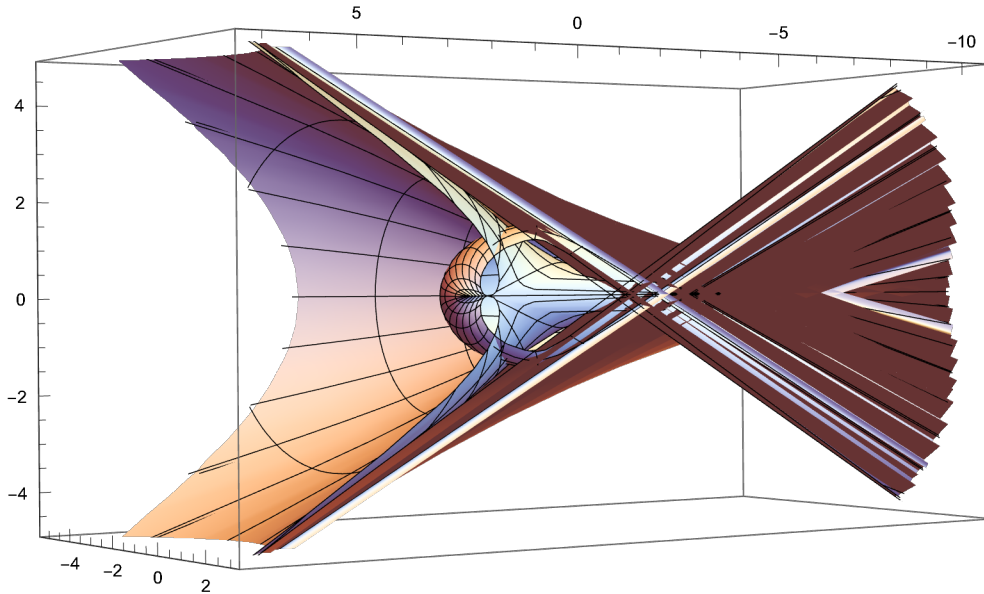
$$\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



$$\text{SphericalPlot3D}\left[\frac{1}{16 \pi^3 \theta - 20 \pi^2 \theta^2 + \theta^4},\right.$$

$$2 \pi \left(-2 \pi 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) \sqrt{(4 \pi - \theta) \theta} + \sqrt{64 \pi^5 \theta - 80 \pi^4 \theta^2 + 20 \pi^2 \theta^4 - \theta^6}\right),$$

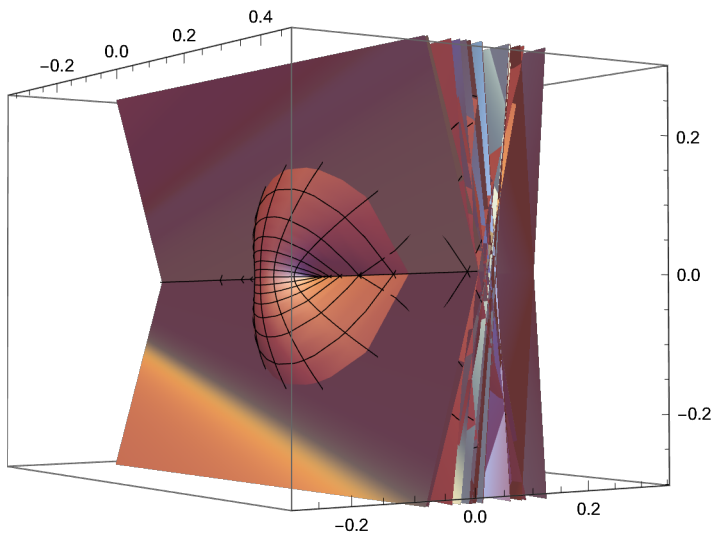
$$\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\left.] \right.$$



$$\text{SphericalPlot3D}\left[\frac{1}{16 \pi^3 \theta - 20 \pi^2 \theta^2 + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)^4} 2 \pi\right.$$

$$\left(-2 \pi \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right) \sqrt{(4 \pi - \theta) \theta} + \sqrt{64 \pi^5 \theta - 80 \pi^4 \theta^2 + 20 \pi^2 \theta^4 - \theta^6}\right),$$

$$\{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\left.] \right.$$

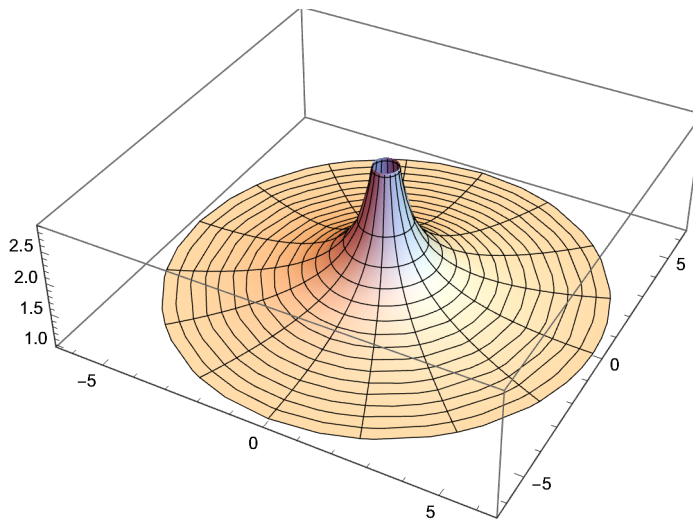


## New Solution 2

$$\text{Solve}\left[\sqrt{\left(r^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}\right)^2} == \frac{2\pi \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, r\right]$$

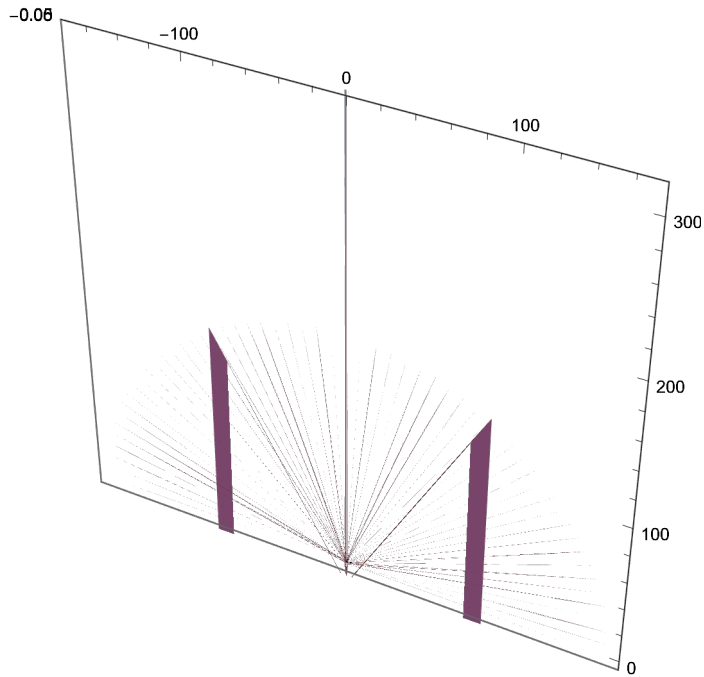
$$\left\{\left\{r \rightarrow -\sqrt{\pi} \sqrt{\frac{1}{4\pi-\theta} + \frac{1}{\theta}}\right\}, \left\{r \rightarrow \sqrt{\pi} \sqrt{\frac{1}{4\pi-\theta} + \frac{1}{\theta}}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[\sqrt{\pi} \sqrt{\frac{1}{4\pi-\theta} + \frac{1}{\theta}}, \{\theta, -2\pi, 2\pi\}\right]$$



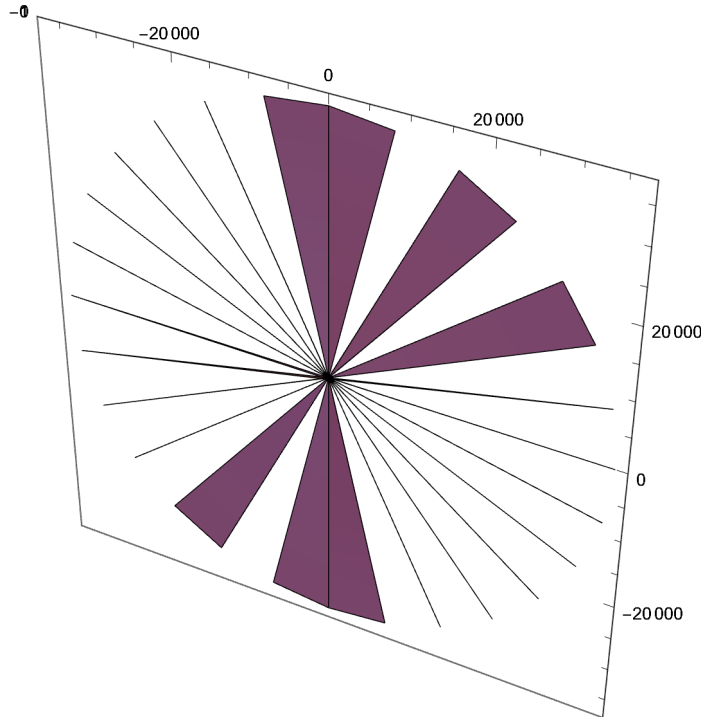
## Solution 2 Substitutions

$\text{SphericalPlot3D}\left[\sqrt{\pi} \sqrt{\frac{1}{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}} + \frac{1}{\theta}, \right.$   
 $\left. \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$

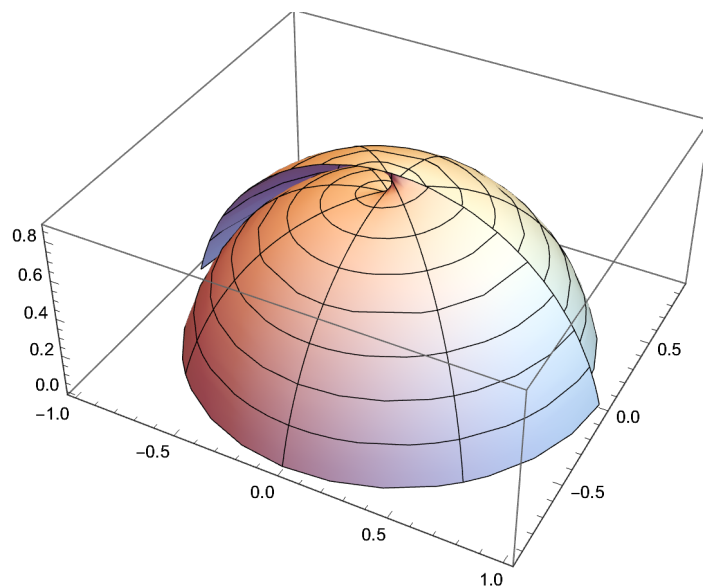




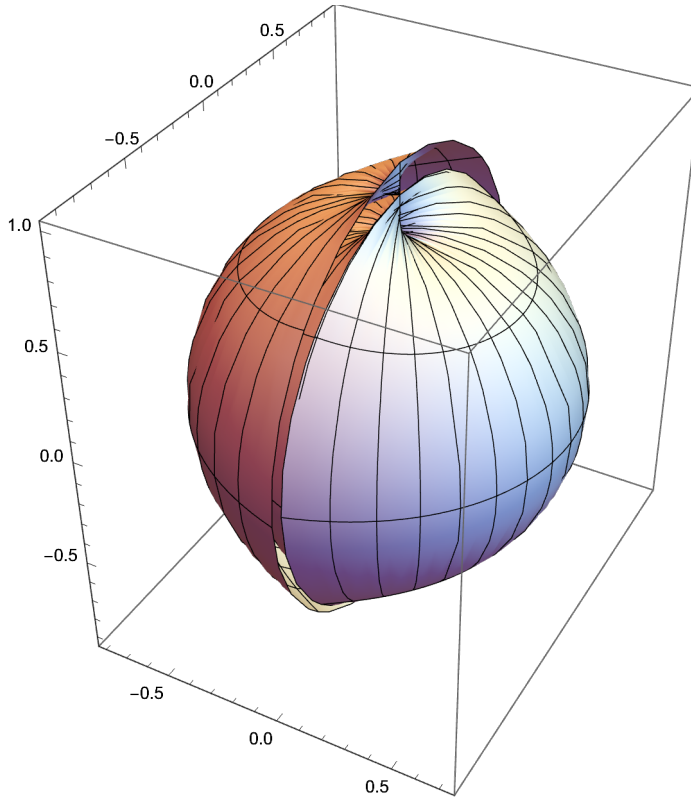
SphericalPlot3D $\left[\sqrt{\pi} \sqrt{\frac{1}{4\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} + \frac{1}{\theta}}, \right.$   
 $\left.\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



SphericalPlot3D $\left[\sqrt{\pi} \sqrt{\frac{1}{4\pi - \theta} + \frac{1}{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}, \right.$   
 $\left.\{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



SphericalPlot3D $\left[\sqrt{\pi} \sqrt{\frac{1}{4\pi-\theta} + \frac{1}{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}, \right.$   
 $\left.\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



### New Solution 3

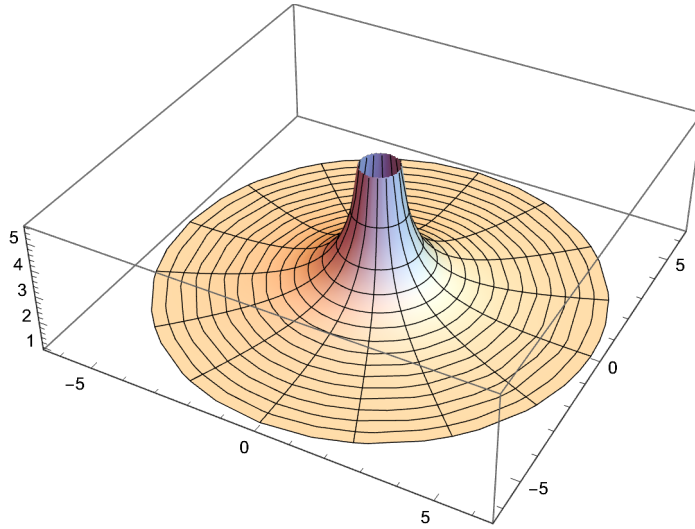
$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}}^2} == \frac{2\pi - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{-\frac{6\pi^2}{(4\pi-\theta)^2} - \frac{\pi}{4\pi-\theta} + \frac{2\pi^2}{\theta^2} - \frac{\pi}{\theta} + \frac{4\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)^2} + \frac{\sqrt{(4\pi-\theta)\theta}}{4\pi-\theta} + \frac{\sqrt{(4\pi-\theta)\theta}}{\theta}}}{\sqrt{2}}\right\}, \right.$$

$$\left.\left\{r \rightarrow \frac{\sqrt{-\frac{6\pi^2}{(4\pi-\theta)^2} - \frac{\pi}{4\pi-\theta} + \frac{2\pi^2}{\theta^2} - \frac{\pi}{\theta} + \frac{4\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)^2} + \frac{\sqrt{(4\pi-\theta)\theta}}{4\pi-\theta} + \frac{\sqrt{(4\pi-\theta)\theta}}{\theta}}}{\sqrt{2}}\right\}\right\}$$

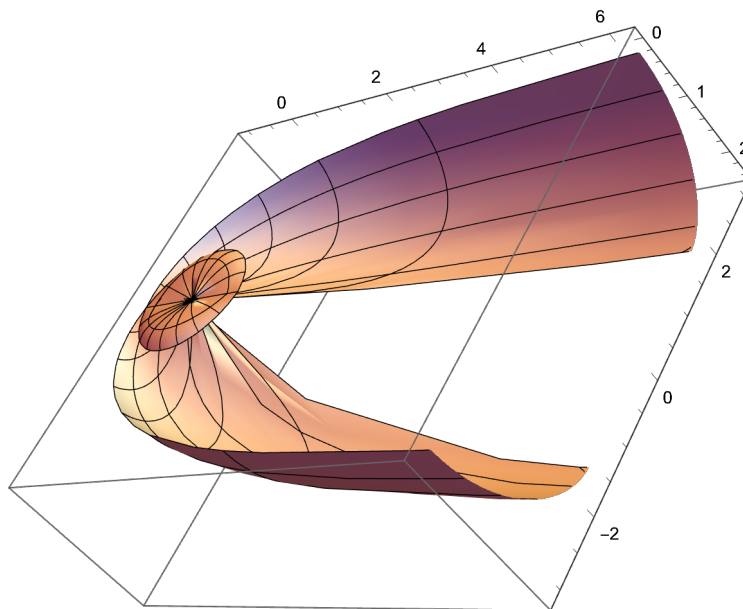
RevolutionPlot3D[

$$\sqrt{-\frac{6\pi^2}{(4\pi-\theta)^2} - \frac{\pi}{4\pi-\theta} + \frac{2\pi^2}{\theta^2} - \frac{\pi}{\theta} + \frac{4\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)^2} + \frac{\sqrt{(4\pi-\theta)\theta}}{4\pi-\theta} + \frac{\sqrt{(4\pi-\theta)\theta}}{\theta}}{\sqrt{2}}, \{\theta, -2\pi, 2\pi\}]$$



SphericalPlot3D[

$$\frac{1}{\sqrt{2}} \left( \sqrt{\left( -\frac{6\pi^2}{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))^2} - \frac{\pi}{4\pi - \theta} + \frac{2\pi^2}{\theta^2} - \frac{\pi}{\theta} + \frac{4\pi\sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)^2} + \frac{\sqrt{(4\pi - \theta)\theta}}{4\pi - \theta} + \frac{\sqrt{(4\pi - \theta)\theta}}{\theta} \right)} \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$

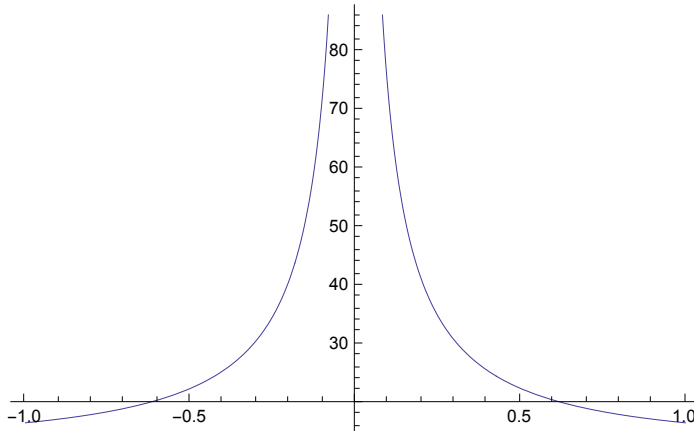


## Theta Solution Representing "Eight Fold Path"

$$\text{Solve}\left[\sqrt{\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2 - \frac{\sqrt{4\pi(r)^2\theta - (r)^2\theta^2}}{2\pi}}^2\right] == \frac{2\pi - \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}, \theta]$$

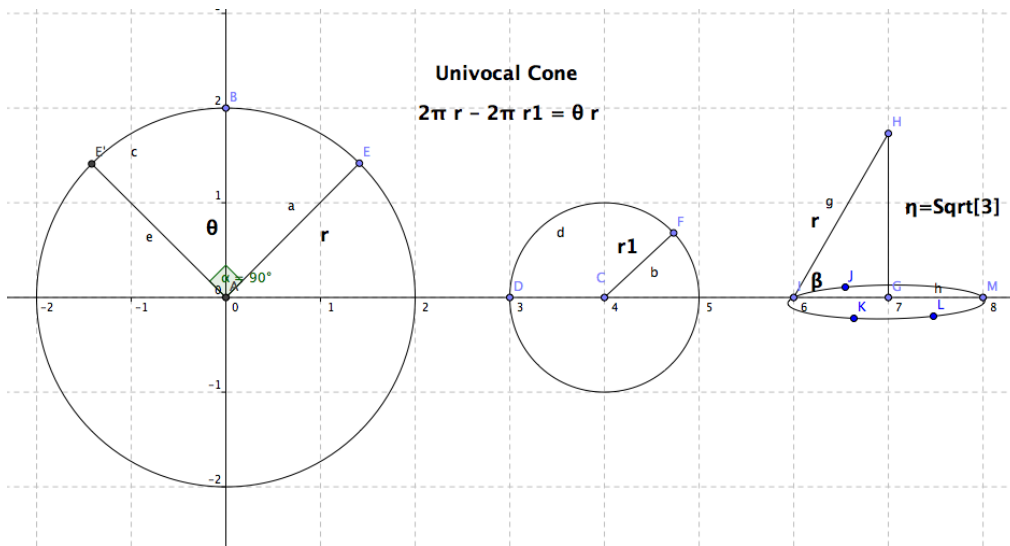
$$\begin{aligned} & \left\{ \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + \right. \right. \\ & \quad \left. \left. (-256\pi^5 + 768\pi^5r^2)\pi^3 + (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + \right. \right. \\ & \quad \left. \left. (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 1\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 2\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 3\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 4\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 5\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 6\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 7\right]\right\}, \\ & \left\{ \theta \rightarrow \text{Root}\left[256\pi^8 - 512\pi^7\pi + (256\pi^6 - 512\pi^6r^2)\pi^2 + (-256\pi^5 + 768\pi^5r^2)\pi^3 + \right. \right. \\ & \quad \left. \left. (64\pi^4 - 288\pi^4r^2 + 256\pi^4r^4)\pi^4 + (32\pi^3r^2 - 256\pi^3r^4)\pi^5 + \right. \right. \\ & \quad \left. \left. 96\pi^2r^4\pi^6 - 16\pi r^4\pi^7 + r^4\pi^8 \&, 8\right]\right\} \end{aligned}$$

Plot[Re[Root[256  $\pi^8$  - 512  $\pi^7$  #1 + (256  $\pi^6$  - 512  $\pi^6$  r<sup>2</sup>) #1<sup>2</sup> +  
 (-256  $\pi^5$  + 768  $\pi^5$  r<sup>2</sup>) #1<sup>3</sup> + (64  $\pi^4$  - 288  $\pi^4$  r<sup>2</sup> + 256  $\pi^4$  r<sup>4</sup>) #1<sup>4</sup> +  
 (32  $\pi^3$  r<sup>2</sup> - 256  $\pi^3$  r<sup>4</sup>) #1<sup>5</sup> + 96  $\pi^2$  r<sup>4</sup> #1<sup>6</sup> - 16  $\pi$  r<sup>4</sup> #1<sup>7</sup> + r<sup>4</sup> #1<sup>8</sup> &, 8]], {r, -1, 1}]



8 Roots symbolize the eight - fold path.

## Parker' s Commentary on Fermat' s Last Theorem



Please see The Geometric Pattern of Perception to reference the preliminary investigations.

**Lemma 5** The height of the cone can be calculated in terms of only  $r$  and  $\theta$ , thus  $\theta$  is a function of  $\beta$  alone.

Proof. Since we have shown that  $\theta r = 2 \pi r - 2 \pi r_1$  and  $r_1 \rightarrow \sqrt{r^2 - \eta^2}$ , we can substitute the expression for  $r_1$ , calculated from the Pythagorean theorem in terms of the height of the cone and the initial

radius of the circle, into the expression for  $\theta r$  in terms of the change in circumference of the initial circle to the circle that is the base of the cone into which the circle was transformed.

$\theta r = 2\pi r - 2\pi \sqrt{(r^2 - \eta^2)}$ , thus,  $\eta = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = (r \sin[\beta])$ . From  $\frac{2\pi \eta}{\sqrt{4\pi \theta - \theta^2}} = r$ , we note that:  $r = \frac{2\pi r \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}}$ . So we solve the equation,

$$\text{Solve}\left[r == \frac{2\pi r \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow 2\left(\pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right\}, \left\{\theta \rightarrow 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right\}\right\}$$

$$1 = \frac{2\pi \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}}$$

The Meaning of  $n > 2$  is  $n > \frac{r \theta}{\pi (r - r_1)}$  ;

$$n > \frac{2\pi \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}} + \frac{2\pi \sin[\beta]}{\sqrt{4\pi \theta - \theta^2}} >$$

$$\frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin[\beta]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)} + \frac{r \theta}{\pi (r - r_1)}\right) \pi \theta - \theta^2}} +$$

$$\frac{\frac{r \theta}{\pi (r - r_1)} \pi \sin[\beta]}{\sqrt{\left(\frac{r \theta}{\pi (r - r_1)} + \frac{r \theta}{\pi (r - r_1)}\right) \pi \theta - \theta^2}}$$

$x^n + y^n = z^n$ , where  $n > 2$

$$\theta r = 2\pi r - 2\pi r_1$$

What is 2?

$$\text{Solve}[\theta r == \varrho \pi r - \varrho \pi r_1, \varrho]$$

$$\left\{\left\{\varrho \rightarrow \frac{r \theta}{\pi (r - r_1)}\right\}\right\}$$

$$2 == \frac{r \theta}{\pi (r - r_1)}$$

$$x^n + y^n = z^n, \text{ where } n > \frac{r\theta}{\pi(r-r_1)}$$

$$x^n + y^n = z^n, \text{ where } n > \left\{ \frac{r\theta}{\pi\left(r - \frac{2\pi r - r\theta}{2\pi}\right)} = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} \right\}$$

$$\text{Solve}\left[\frac{r\theta}{\pi\left(r - \frac{2\pi r - r\theta}{2\pi}\right)} = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, r\right]$$

{}

$$\text{Solve}\left[\frac{r\theta}{\pi\left(r - \sqrt{\left(r^2 - \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}\right)^2}\right)} = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, r\right]$$

{}

$$\text{Solve}\left[\frac{r\theta}{\pi\left(r - \sqrt{r^2 - \eta^2}\right)} = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}, r\right]$$

$$\left\{ \left\{ r \rightarrow -\left( 2\sqrt{2} \sqrt{\left( 2\pi^4 \eta^2 \sin[\beta]^2 + \frac{\pi^4 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} + \frac{4\pi^5 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta^2} + \frac{\pi^4 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)} \right) / \left( \sqrt{-4\pi\theta^3 + \theta^4 + 64\pi^4 \sin[\beta]^2} \right) \right\}, \right.$$

$$\left. \left\{ r \rightarrow \left( 2\sqrt{2} \sqrt{\left( 2\pi^4 \eta^2 \sin[\beta]^2 + \frac{\pi^4 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} + \frac{4\pi^5 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta^2} + \frac{\pi^4 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)} \right) / \left( \sqrt{-4\pi\theta^3 + \theta^4 + 64\pi^4 \sin[\beta]^2} \right) \right\} \right\}$$

$$\text{Solve}\left[\left[-4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta}\right] / \left(16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2\right) =$$

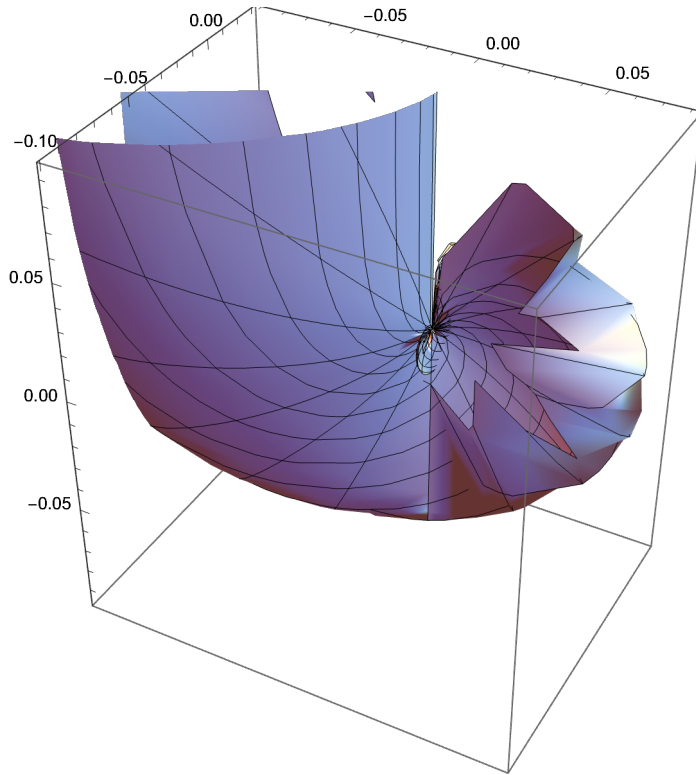
$$\left( 2\sqrt{2} \sqrt{\left( 2\pi^4 \eta^2 \sin[\beta]^2 + \frac{\pi^4 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} + \frac{4\pi^5 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta^2} + \frac{\pi^4 \eta^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)} \right) / \left( \sqrt{-4\pi\theta^3 + \theta^4 + 64\pi^4 \sin[\beta]^2} \right), \eta]$$

$$\left\{ \left\{ \eta \rightarrow -\left( \text{Csc}[\beta] \sqrt{\left( 192\pi^6 + \frac{256\pi^8}{(2\pi - \theta)^2} - \frac{512\pi^7}{2\pi - \theta} + 64\pi^5 \theta + 16\pi^4 \theta^2 - 4\pi^2 \theta^4 - 4\pi\theta^5 + \theta^6 - 320\pi^5 \sqrt{(4\pi - \theta)\theta} \sin[\beta] - \frac{512\pi^7 \sqrt{(4\pi - \theta)\theta} \sin[\beta]}{(2\pi - \theta)^2} + \right.} \right.$$

$$\begin{aligned}
& \frac{896 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]}{2 \pi - \theta} - 96 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] - \\
& 16 \pi^3 \theta^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 8 \pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \\
& 4 \pi \theta^4 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 448 \pi^6 \operatorname{Sin}[\beta]^2 + \frac{256 \pi^8 \operatorname{Sin}[\beta]^2}{(2 \pi - \theta)^2} - \\
& \frac{1024 \pi^7 \operatorname{Sin}[\beta]^2}{2 \pi - \theta} + 192 \pi^5 \theta \operatorname{Sin}[\beta]^2 + 80 \pi^4 \theta^2 \operatorname{Sin}[\beta]^2 - 32 \pi^3 \theta^3 \operatorname{Sin}[\beta]^2 - \\
& 4 \pi^2 \theta^4 \operatorname{Sin}[\beta]^2 + 128 \pi^5 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3 + \frac{1792 \pi^7 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(2 \pi - \theta)^2} - \\
& \frac{1152 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{2 \pi - \theta} - 32 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3 - 256 \pi^6 \operatorname{Sin}[\beta]^4 - \\
& \frac{5120 \pi^8 \operatorname{Sin}[\beta]^4}{(2 \pi - \theta)^2} + \frac{3072 \pi^7 \operatorname{Sin}[\beta]^4}{2 \pi - \theta} + \frac{1024 \pi^7 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^5}{(2 \pi - \theta)^2} - \\
& \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^5}{2 \pi - \theta} + \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^5}{4 \pi - \theta} \Big) \Big) / \\
& \left( \pi^2 \sqrt{-256 \pi \theta^3 + 64 \theta^4 + 4096 \pi^4 \operatorname{Sin}[\beta]^2} \right) \Big\}, \\
\{ \eta \rightarrow & \left( \operatorname{Csc}[\beta] \sqrt{\left( 192 \pi^6 + \frac{256 \pi^8}{(2 \pi - \theta)^2} - \frac{512 \pi^7}{2 \pi - \theta} + 64 \pi^5 \theta + 16 \pi^4 \theta^2 - 4 \pi^2 \theta^4 - 4 \pi \theta^5 + \right. \right. \\
& \theta^6 - 320 \pi^5 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] - \frac{512 \pi^7 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]}{(2 \pi - \theta)^2} + \\
& \frac{896 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]}{2 \pi - \theta} - 96 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] - \\
& 16 \pi^3 \theta^2 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 8 \pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + \\
& 4 \pi \theta^4 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta] + 448 \pi^6 \operatorname{Sin}[\beta]^2 + \frac{256 \pi^8 \operatorname{Sin}[\beta]^2}{(2 \pi - \theta)^2} - \\
& \frac{1024 \pi^7 \operatorname{Sin}[\beta]^2}{2 \pi - \theta} + 192 \pi^5 \theta \operatorname{Sin}[\beta]^2 + 80 \pi^4 \theta^2 \operatorname{Sin}[\beta]^2 - 32 \pi^3 \theta^3 \operatorname{Sin}[\beta]^2 - \\
& 4 \pi^2 \theta^4 \operatorname{Sin}[\beta]^2 + 128 \pi^5 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3 + \frac{1792 \pi^7 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{(2 \pi - \theta)^2} - \\
& \frac{1152 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3}{2 \pi - \theta} - 32 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^3 - 256 \pi^6 \operatorname{Sin}[\beta]^4 - \\
& \frac{5120 \pi^8 \operatorname{Sin}[\beta]^4}{(2 \pi - \theta)^2} + \frac{3072 \pi^7 \operatorname{Sin}[\beta]^4}{2 \pi - \theta} + \frac{1024 \pi^7 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^5}{(2 \pi - \theta)^2} - \\
& \left. \left. \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^5}{2 \pi - \theta} + \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \operatorname{Sin}[\beta]^5}{4 \pi - \theta} \right) \right) / \\
& \left( \pi^2 \sqrt{-256 \pi \theta^3 + 64 \theta^4 + 4096 \pi^4 \operatorname{Sin}[\beta]^2} \right) \Big\} \Big\}
\end{aligned}$$



$$\begin{aligned}
& \text{SphericalPlot3D}\left[ \right. \\
& \left( \text{Csc}[\beta] \sqrt{\left( 192 \pi^6 + \frac{256 \pi^8}{(2 \pi - \theta)^2} - \frac{512 \pi^7}{2 \pi - \theta} + 64 \pi^5 \theta + 16 \pi^4 \theta^2 - 4 \pi^2 \theta^4 - 4 \pi \theta^5 + \theta^6 - 320 \pi^5 \right.} \right. \\
& \quad \left. \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta] - \frac{512 \pi^7 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]}{(2 \pi - \theta)^2} + \frac{896 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]}{2 \pi - \theta} - \right. \\
& \quad 96 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta] - 16 \pi^3 \theta^2 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta] + 8 \pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta} \\
& \quad \text{Sin}[\beta] + 4 \pi \theta^4 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta] + 448 \pi^6 \text{Sin}[\beta]^2 + \frac{256 \pi^8 \text{Sin}[\beta]^2}{(2 \pi - \theta)^2} - \\
& \quad \frac{1024 \pi^7 \text{Sin}[\beta]^2}{2 \pi - \theta} + 192 \pi^5 \theta \text{Sin}[\beta]^2 + 80 \pi^4 \theta^2 \text{Sin}[\beta]^2 - 32 \pi^3 \theta^3 \text{Sin}[\beta]^2 - \\
& \quad 4 \pi^2 \theta^4 \text{Sin}[\beta]^2 + 128 \pi^5 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3 + \frac{1792 \pi^7 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3}{(2 \pi - \theta)^2} - \\
& \quad \frac{1152 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3}{2 \pi - \theta} - 32 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3 - 256 \pi^6 \text{Sin}[\beta]^4 - \\
& \quad \frac{5120 \pi^8 \text{Sin}[\beta]^4}{(2 \pi - \theta)^2} + \frac{3072 \pi^7 \text{Sin}[\beta]^4}{2 \pi - \theta} + \frac{1024 \pi^7 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{(2 \pi - \theta)^2} - \\
& \quad \left. \left. \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{2 \pi - \theta} + \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{4 \pi - \theta} \right) \right) / \\
& \left( \pi^2 \sqrt{-256 \pi \theta^3 + 64 \theta^4 + 4096 \pi^4 \text{Sin}[\beta]^2} \right), \{\theta, \\
& -2 \pi, \\
& 2 \pi\}, \{\beta, \\
& -\pi / 2, \\
& \pi / 2\} \left. \right]
\end{aligned}$$



SphericalPlot3D[  

$$\left( \csc[\beta] \sqrt{\left( 192 \pi^6 + \frac{256 \pi^8}{(2 \pi - \theta)^2} - \frac{512 \pi^7}{2 \pi - \theta} + 64 \pi^5 \theta + 16 \pi^4 \theta^2 - 4 \pi^2 \theta^4 - 4 \pi \theta^5 + \theta^6 - 320 \pi^5 \right.} \right.$$

$$\sqrt{(4 \pi - \theta) \theta} \sin[\beta] - \frac{512 \pi^7 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]}{(2 \pi - \theta)^2} + \frac{896 \pi^6 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]}{2 \pi - \theta} -$$

$$96 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta] - 16 \pi^3 \theta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 8 \pi^2 \theta^3 \sqrt{(4 \pi - \theta) \theta}$$

$$\sin[\beta] + 4 \pi \theta^4 \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 448 \pi^6 \sin[\beta]^2 + \frac{256 \pi^8 \sin[\beta]^2}{(2 \pi - \theta)^2} -$$

$$\frac{1024 \pi^7 \sin[\beta]^2}{2 \pi - \theta} + 192 \pi^5 \theta \sin[\beta]^2 + 80 \pi^4 \theta^2 \sin[\beta]^2 - 32 \pi^3 \theta^3 \sin[\beta]^2 -$$

$$4 \pi^2 \theta^4 \sin[\beta]^2 + 128 \pi^5 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3 + \frac{1792 \pi^7 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{(2 \pi - \theta)^2} -$$

$$\frac{1152 \pi^6 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{2 \pi - \theta} - 32 \pi^4 \theta \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3 - 256 \pi^6 \sin[\beta]^4 -$$

$$\frac{5120 \pi^8 \sin[\beta]^4}{(2 \pi - \theta)^2} + \frac{3072 \pi^7 \sin[\beta]^4}{2 \pi - \theta} + \frac{1024 \pi^7 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^5}{(2 \pi - \theta)^2} -$$

$$\left. \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^5}{2 \pi - \theta} + \frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^5}{4 \pi - \theta} \right) \Bigg/$$

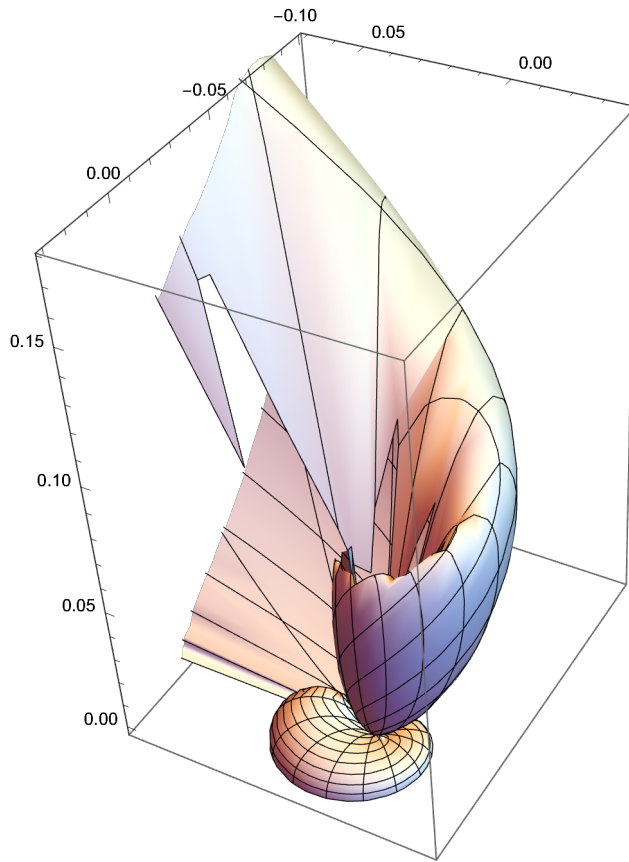
$$\left( \pi^2 \sqrt{-256 \pi \theta^3 + 64 \theta^4 + 4096 \pi^4 \sin[\beta]^2} \right), \{\beta,$$

$$-\pi/2,$$

$$\pi/2\}, \{\theta,$$

$$-2\pi,$$

$$2\pi\}$$



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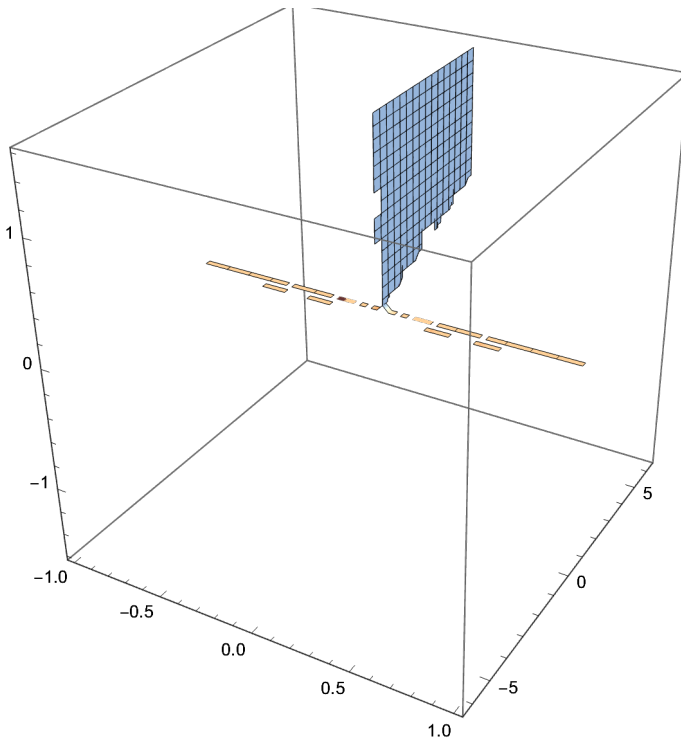
Export["sheath.3ds",
  SphericalPlot3D[
    Csc[β] √(
      192 π6 +  $\frac{256 \pi^8}{(2 \pi - \theta)^2}$  -  $\frac{512 \pi^7}{2 \pi - \theta}$  + 64 π5 θ + 16 π4 θ2 - 4 π2 θ4 -
      4 π θ5 + θ6 - 320 π5 √(4 π - θ) θ Sin[β] -  $\frac{512 \pi^7 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]}{(2 \pi - \theta)^2}$  +
       $\frac{896 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]}{2 \pi - \theta}$  - 96 π4 θ √(4 π - θ) θ Sin[β] -
      16 π3 θ2 √(4 π - θ) θ Sin[β] + 8 π2 θ3 √(4 π - θ) θ Sin[β] +
      4 π θ4 √(4 π - θ) θ Sin[β] + 448 π6 Sin[β]2 +  $\frac{256 \pi^8 \text{Sin}[\beta]^2}{(2 \pi - \theta)^2}$  -
       $\frac{1024 \pi^7 \text{Sin}[\beta]^2}{2 \pi - \theta}$  + 192 π5 θ Sin[β]2 + 80 π4 θ2 Sin[β]2 - 32 π3 θ3 Sin[β]2 -
      4 π2 θ4 Sin[β]2 + 128 π5 √(4 π - θ) θ Sin[β]3 +  $\frac{1792 \pi^7 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3}{(2 \pi - \theta)^2}$  -
       $\frac{1152 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^3}{2 \pi - \theta}$  - 32 π4 θ √(4 π - θ) θ Sin[β]3 - 256 π6 Sin[β]4 -
       $\frac{5120 \pi^8 \text{Sin}[\beta]^4}{(2 \pi - \theta)^2}$  +  $\frac{3072 \pi^7 \text{Sin}[\beta]^4}{2 \pi - \theta}$  +  $\frac{1024 \pi^7 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{(2 \pi - \theta)^2}$  -
       $\frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{2 \pi - \theta}$  +  $\frac{512 \pi^6 \sqrt{(4 \pi - \theta) \theta} \text{Sin}[\beta]^5}{4 \pi - \theta}$ 
    )
    , {β, -π / 2,
      π / 2}, {θ,
      -2 π,
      2 π}]
  sheath.3ds
  "sheath.obj"

```

ContourPlot3D[  

$$\left\{ - \left( 2 \sqrt{2} \sqrt{\left( 2 \pi^4 \eta^2 \sin[\beta]^2 + \frac{\pi^4 \eta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} + \frac{4 \pi^5 \eta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} + \frac{\pi^4 \eta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)} \right) / \left( \sqrt{-4 \pi \theta^3 + \theta^4 + 64 \pi^4 \sin[\beta]^2} \right), \right.$$
  

$$\left( 2 \sqrt{2} \sqrt{\left( 2 \pi^4 \eta^2 \sin[\beta]^2 + \frac{\pi^4 \eta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} + \frac{4 \pi^5 \eta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta^2} + \frac{\pi^4 \eta^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)} \right) / \left( \sqrt{-4 \pi \theta^3 + \theta^4 + 64 \pi^4 \sin[\beta]^2} \right) \right\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$



Solve[
$$\frac{\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{\pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \right)} = \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} + \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \theta]$$
  

$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\}, \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right\} \right\}$$

$$\text{Solve}\left[\frac{\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{\pi\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}-\frac{2\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}-\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}{2\pi}\right)}==\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}+\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}},\beta\right]$$

$$\left\{\left\{\beta\rightarrow\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]\right\}\right\}$$

$$\text{Solve}\left[\frac{r\theta}{\pi\left(r-\sqrt{\left(r^2-\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\right)^2}\right)}==\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}+\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}},r\right]$$

{}

$$\text{Solve}\left[\frac{r\theta}{\pi\left(r-\sqrt{\left(r^2-\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\right)^2}\right)}==\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}+\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}},\theta\right]$$

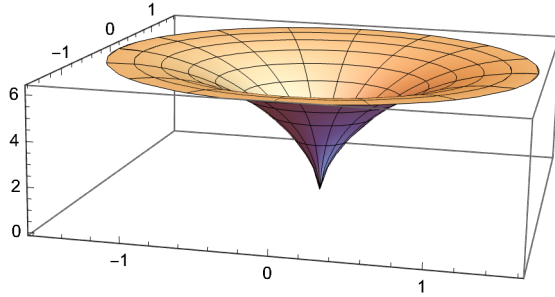
$$\left\{\left\{\theta\rightarrow 2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right\},\left\{\theta\rightarrow 2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right\},\right.$$

$$\left.\left\{\theta\rightarrow 2\left(\frac{\pi^2\sin[\beta]^2}{3^{1/3}\left(-9\pi^3\sin[\beta]^2+\sqrt{3}\sqrt{27\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}}-\frac{\left(-9\pi^3\sin[\beta]^2+\sqrt{3}\sqrt{27\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}}{3^{2/3}}\right)\right\},\right.$$

$$\left.\left\{\theta\rightarrow -\frac{(1+i\sqrt{3})\pi^2\sin[\beta]^2}{3^{1/3}\left(-9\pi^3\sin[\beta]^2+\sqrt{3}\sqrt{27\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}}+\frac{(1-i\sqrt{3})\left(-9\pi^3\sin[\beta]^2+\sqrt{3}\sqrt{27\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}}{3^{2/3}}\right\},\right.$$

$$\left.\left\{\theta\rightarrow -\frac{(1-i\sqrt{3})\pi^2\sin[\beta]^2}{3^{1/3}\left(-9\pi^3\sin[\beta]^2+\sqrt{3}\sqrt{27\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}}+\frac{(1+i\sqrt{3})\left(-9\pi^3\sin[\beta]^2+\sqrt{3}\sqrt{27\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}}{3^{2/3}}\right\}\right\}$$

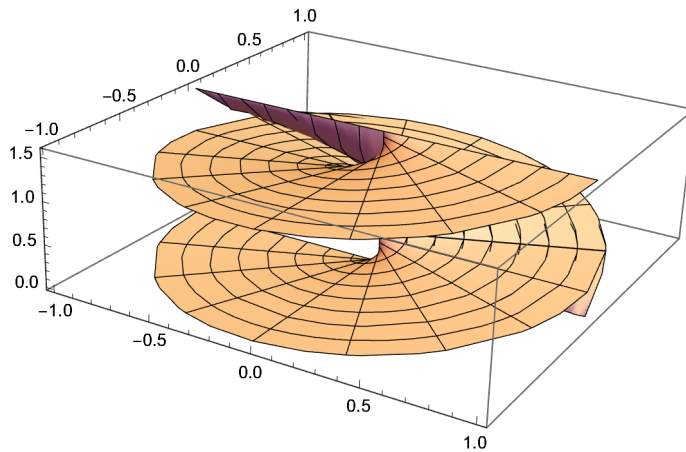
$$\text{RevolutionPlot3D}\left[2 \left[ \frac{\pi^2 \sin[\beta]^2}{3^{1/3} \left( -9 \pi^3 \sin[\beta]^2 + \sqrt{3} \sqrt{27 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} - \frac{\left( -9 \pi^3 \sin[\beta]^2 + \sqrt{3} \sqrt{27 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}}{3^{2/3}} \right], \{\beta, -\pi/2, \pi/2\} \right]$$



$$\text{Solve}\left[\frac{r \theta}{\pi \left( r - \sqrt{r^2 - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}} \right)} = \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} + \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \beta \right]$$

$$\left\{ \left\{ \beta \rightarrow \text{ArcSin}\left[ \frac{r \theta \sqrt{(4 \pi - \theta) \theta}}{2 \pi \left( 2 \pi r - \sqrt{r^2 (2 \pi - \theta)^2} \right)} \right] \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\text{ArcSin}\left[ \frac{r \theta \sqrt{(4 \pi - \theta) \theta}}{2 \pi \left( 2 \pi r - \sqrt{r^2 (2 \pi - \theta)^2} \right)} \right], \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\} \right]$$



For n = 3,

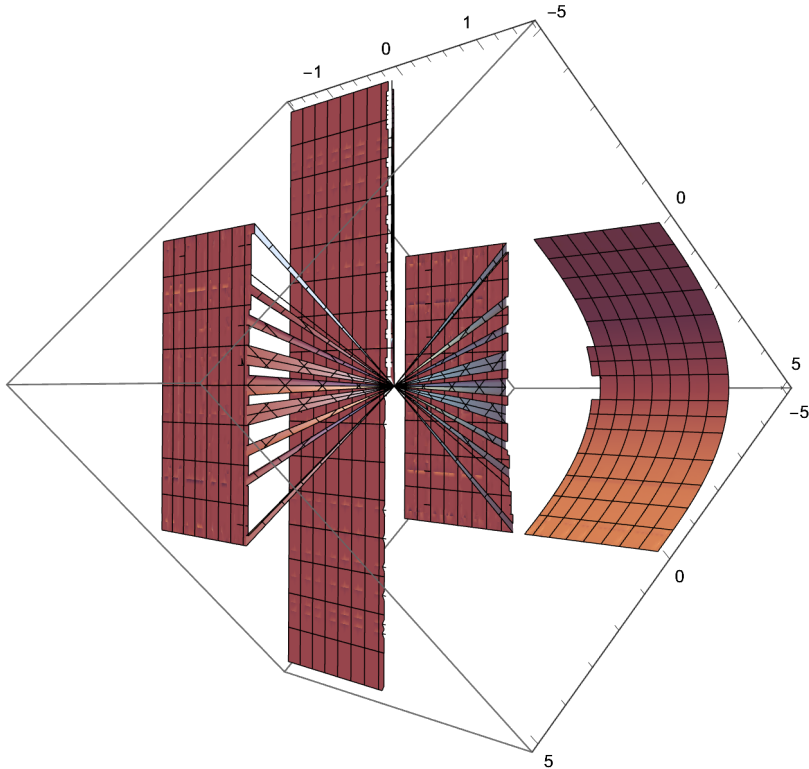


$$\text{Solve}\left[x^{\wedge}\left(\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right)+y^{\wedge}\left(\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right)=\right. \\ \left.z^{\wedge}\left(\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right), x\right] \\ \left\{\left\{x \rightarrow\left(-y^{\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}+\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}\right)^{\frac{1}{2+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}}}\right\}\right\}$$

$$r:=\frac{2 \pi \sqrt{(4 \pi-\theta) \theta}}{(4 \pi-\theta) \theta}$$

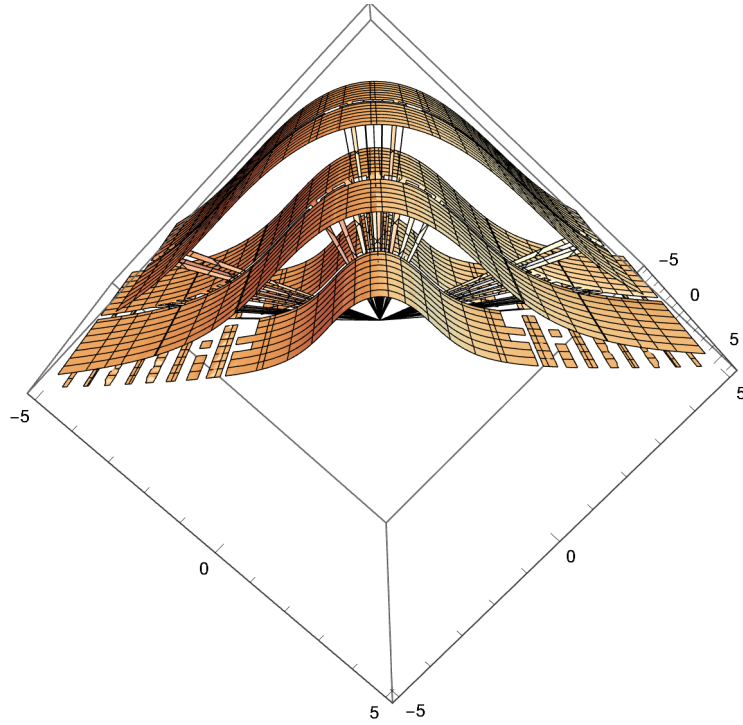
$$\theta:=2\left(\pi+\sqrt{\pi^2-\pi^2 \text{Sin}[\beta]^2}\right)$$

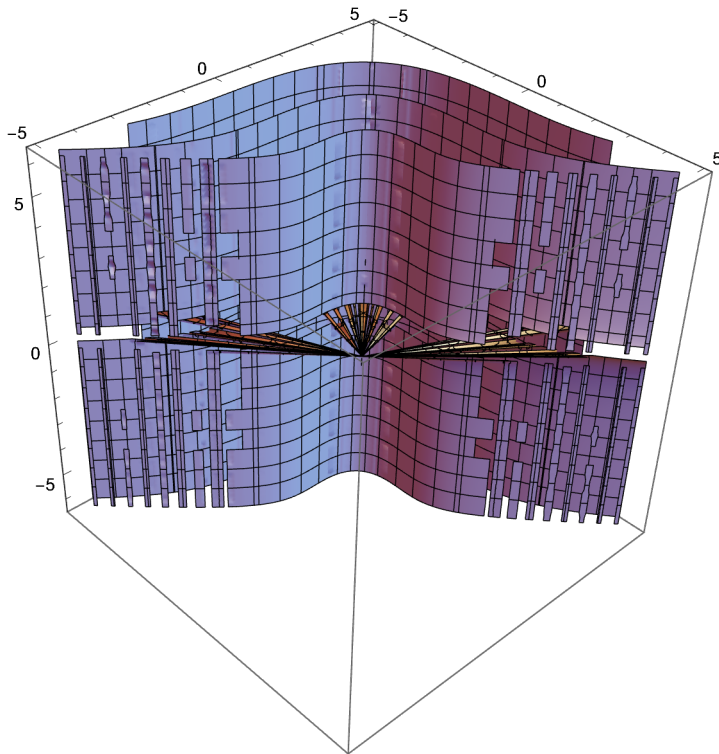
$$\text{ContourPlot3D}\left[\left(-y^{\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}+\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}\right)^{\frac{1}{2+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}}},\right. \\ \left.\{y,-5,5\},\{z,-5,5\},\{\beta,-\pi / 2,\pi / 2\}\right]$$



$$\beta:=\text{ArcSin}\left[\frac{\sqrt{(4 \pi-\theta) \theta}}{2 \pi}\right]$$

`ContourPlot3D`  $\left[ -y^{\pi \left( \frac{r \theta}{r - \frac{2 \pi r - r \theta}{2 \pi}} + \frac{2 \pi \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} \right)} + z^{\pi \left( \frac{r \theta}{r - \frac{2 \pi r - r \theta}{2 \pi}} + \frac{2 \pi \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}} \right)} \right]^{\frac{1}{2 + \frac{2 \pi \sin[\beta]}{\sqrt{(4 \pi - \theta) \theta}}}},$   
 $\{y, -5, 5\}, \{z, -5, 5\}, \{\theta, -2 \pi, 2 \pi\}$





$$\text{Solve}\left[x^{\wedge}\left(\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right)+y^{\wedge}\left(\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right)\right]==$$

$$z^{\wedge}\left(\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{4 \pi \theta-\theta^2}}\right), y]$$

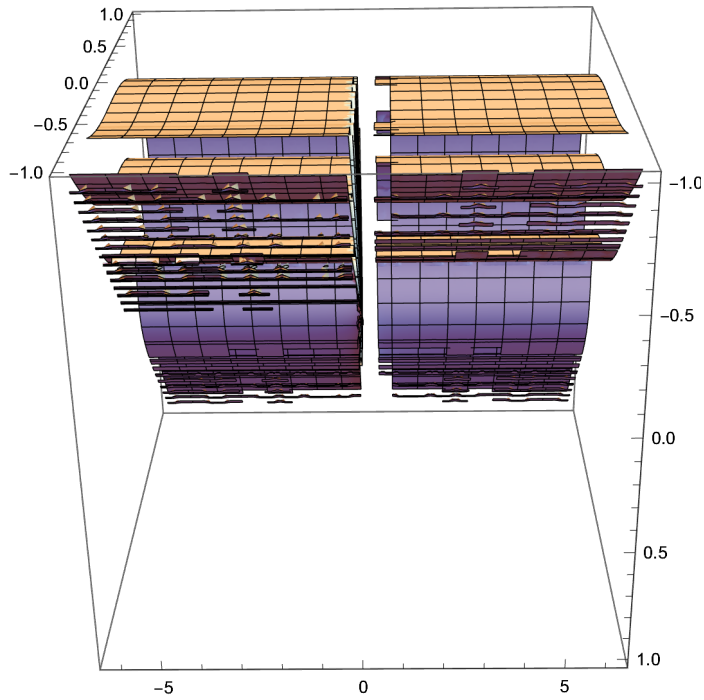
$$\left\{\left\{y \rightarrow\left(-x^{\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}+z^{\frac{r \theta}{\pi\left(r-\frac{2 \pi r-r \theta}{2 \pi}\right)}+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}\right)^{\frac{1}{2+\frac{2 \pi \text{Sin}[\beta]}{\sqrt{(4 \pi-\theta) \theta}}}}\right\}\right\}$$

$$\text{Solve}\left[r==\frac{2 \pi \sqrt{(4 \pi-\theta) \theta}}{(4 \pi-\theta) \theta}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2 \pi\left(r^2-\sqrt{-r^2+r^4}\right)}{r^2}\right\},\left\{\theta \rightarrow \frac{2 \pi\left(r^2+\sqrt{-r^2+r^4}\right)}{r^2}\right\}\right\}$$

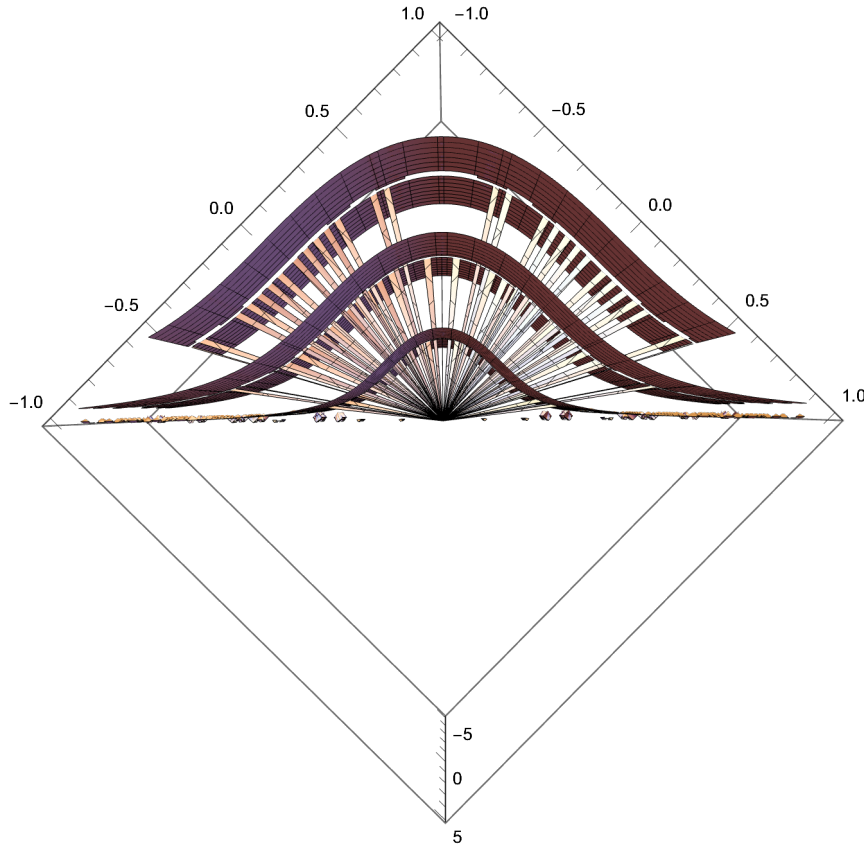
$$\theta:=\frac{2 \pi\left(r^2+\sqrt{-r^2+r^4}\right)}{r^2}$$

$\text{ContourPlot3D}\left[\left(-x^{\pi\left(\frac{r\theta}{r-\frac{2\pi r-\theta}{2\pi}}+\frac{2\pi\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}}\right)}+z^{\pi\left(\frac{r\theta}{r-\frac{2\pi r-\theta}{2\pi}}+\frac{2\pi\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}}\right)}\right)^{\frac{1}{2+\frac{2\pi\sin[\beta]}{\sqrt{(4\pi-\theta)\theta}}}},\right.$   
 $\left.\{x,-1,1\},\{z,-1,1\},\{r,-2\pi,2\pi\}\right]$



ContourPlot3D $\left[ \left( -x^{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}}} + z^{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}}} \right)^{\frac{1}{2 + \frac{2\pi \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}}}}, \right.$

$\{x, -1, 1\}, \{z, -1, 1\}, \{r, -5, 5\}$



Solve $\left[ x^{\left( \frac{r\theta}{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}} \right)} + y^{\left( \frac{r\theta}{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}} \right)} = \right.$

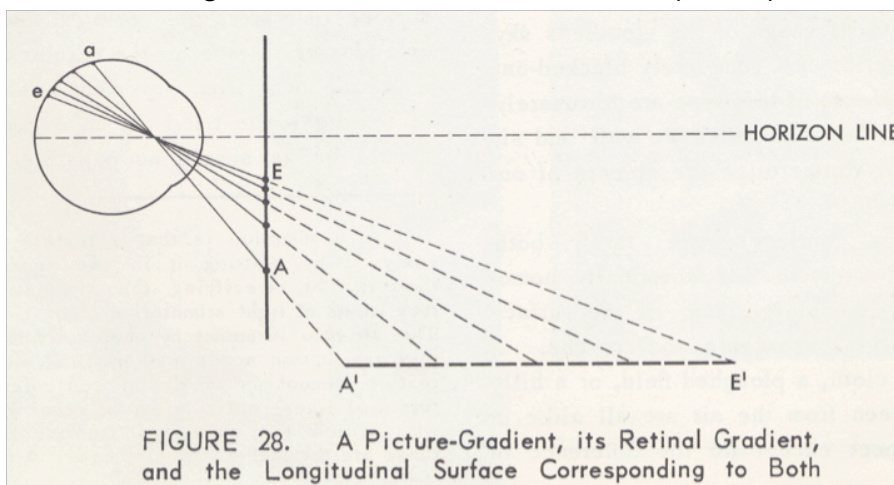
$z^{\left( \frac{r\theta}{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}} \right)}, z]$

$\left\{ \left\{ z \rightarrow \left( x^{\frac{r\theta}{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}}} + y^{\frac{r\theta}{\pi \left( r - \frac{2\pi r - r\theta}{2\pi} \right) + \frac{2\pi \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}}} \right)^{\frac{1}{2 + \frac{2\pi \sin[\beta]}{\sqrt{(4\pi - \theta)\theta}}}} \right\} \right\}$

## Form and Formality (Gibson - Stillwell - Emmerson Formulation of Fermat's Last Theorem)

It is important to note that it is an area of the retina that is affected by radiant energy, not just a single point. Gibson's reason for believing that the geometry of transformations is important to visual

perception is that, “transformations are usually represented on a plane, however, whereas the retinal image is a projection on a curved surface,” (The Visual World, 153) (**Gibson, James, J.. The Perception of the Visual World. Cambridge, Mass.: The Riverside Press, 1950. Print. (All further references to this source will be cited parenthetically in the text).**), and that, “the actual retinal image on a curved surface is related to the hypothetical image on a picture-plane only by such a non-rigid transformation” (The Visual World, 153). A transformation in geometry is the mapping of one point onto another. Isometries, “are defined as the transformations that preserve distance” (The Four Pillars of Geometry, 145) (**Stillwell, John. The Four Pillars of Geometry (Undergraduate Texts in Mathematics). 1 ed. New York: Springer, 2005. Print.**). In essence, the distance of the initial radius is preserved through the transformation of a circle into a cone so long as the height is orthogonal to the base of the cone and the initial radius is always the slant of the cone. Next, we see the diagram to which Gibson was referring when considering the notion of a transformation onto a picture plane.



(The Visual World, 79).

In being preserved, the initial radius is considered an invariant. Stillwell comments about the picture plane that, “the line from  $(-1, 1)$  to  $(n, 0)$  crosses the  $y$ -axis at  $y = n/(n+1)$ ” (The Four Pillars of Geometry, 91). This supposes that the eye is approximated like a point and that it is at the position of  $(-1, 1)$  in the Cartesian coordinate system. In the “coordinate system” described by The Geometric Pattern of Perception Theorems (Emmerson, 2009), the  $y$ -axis in general is described by the height of a cone. In relation to this diagram, in terms of the  $y$  intercept, the height of the cone would be changing with respect to both the initial radius (slant of the cone) and the angle taken out of the initial circle (the angle made between the line from the eye to the  $x$ -axis changes is a function of solely the angular amount taken out of the initial circle). Further mathematical analysis of optical infinity with relation to the horizon line and geometric system is needed, but perceived difference in circumferences as an arc length will be a useful formula. Gibson says that, “only because light is structured by the substantial environment can it contain information about it” (Ecological Approach, 86). The basic equation for an arc length as a difference in circumferences describes an even surface layout. Thus, for even surfaces, the equation that delivers that surface may be used as a linguistic device (in combination with rotation, or specifying the “adumbration” of the viewed surface) for describing the structuring of the light in the environment relevant to the perception of even surface layout. The expression for “phenomenal

velocity” tells us “how” motion in general is essentially structured, thus this includes the motion of light. However, this still needs specific interpretation.

From Stillwell's statement,

$$y = n / (n + 1). \text{ From The Geometric Pattern of Perception (Emmerson, 2009),} \quad (240)$$

$$\eta = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\text{Solve} \left[ \left\{ \frac{2 \pi r - r \theta}{2 \pi} \wedge n + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge n = r \wedge n, n > 2 \right\}, \{\theta\} \right]$$

$$\text{Solve} \left[ \left\{ (2 \pi)^{-n} (2 \pi r - r \theta)^n + (2 \pi)^{-n} (4 \pi r^2 \theta - r^2 \theta^2)^{n/2} = r^n, n > 2 \right\}, \{\theta\} \right]$$

$$\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} = n / (n + 1) \quad (241)$$

$$\text{Solve} \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == n / (n + 1), n \right]$$

$$\left\{ \left\{ n \rightarrow \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} \right\} \right\} \quad (242)$$

$$\text{Solve} \left[ 2 == \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}, r \right]$$

$$\left\{ \left\{ r \rightarrow -\frac{4 \pi}{3 \sqrt{4 \pi \theta - \theta^2}} \right\}, \left\{ r \rightarrow \frac{4 \pi}{3 \sqrt{4 \pi \theta - \theta^2}} \right\} \right\}$$

$$\text{Therefore, } r > \frac{4 \pi}{3 \sqrt{4 \pi \theta - \theta^2}}, \text{ and } \theta > \frac{2 \pi (3 r^2 + \sqrt{-4 r^2 + 9 r^4})}{3 r^2}$$

$$x \wedge n + y \wedge n = z \wedge n =$$

$$\frac{2 \pi r - r \theta}{2 \pi} \wedge n + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge n = r \wedge n = \text{Indeterminate} = \text{Indeterminate} \quad (243)$$

**Indeterminate indeed equals an indeterminate, but where and how? There are still other configurations that may lead to trying to solve for a complex infinity. Complex infinity has specific geometric expression available in *The Geometric Pattern of Perception* (Emmerson, 2009).**

$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]$$

```
<< Graphics`ParametricPlot3D';
```

```
<< Graphics`ParametricPlot3D';
```

$$\text{CylindricalPlot3D}\left[\frac{2\pi r - r\theta}{2\pi} \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} == r \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

```
Get::noopen: Cannot open Graphics`ParametricPlot3D. >>
```

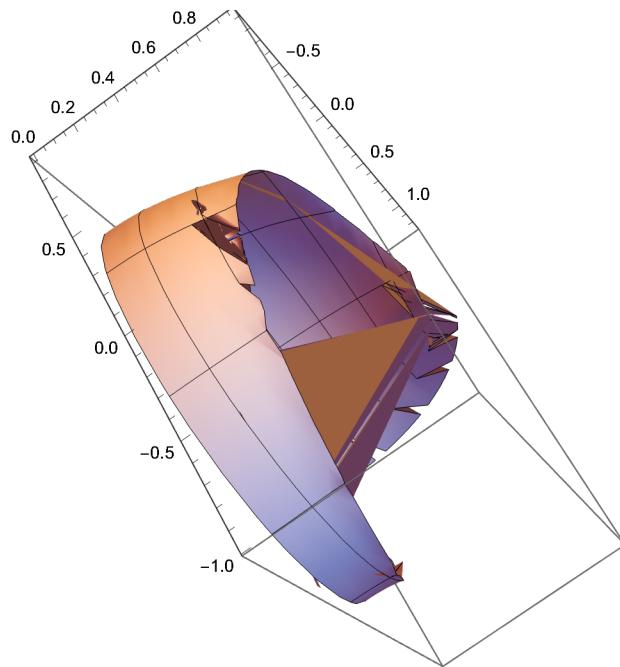
$$\text{CylindricalPlot3D}\left[\frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} (2\pi r - r\theta) \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} + (2\pi) \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} (4\pi r^2\theta - r^2\theta^2) \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} == \frac{\sqrt{r^2(4\pi-\theta)\theta}}{r^2\pi - \sqrt{r^2(4\pi-\theta)\theta}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$$

$$\text{Solve}\left[\frac{2\pi r - r\theta}{2\pi} \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} == r \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}}, \beta\right]$$

```
{{{}}}
```



```
SphericalPlot3D[ $r^{\frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}}$ , { $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }, { $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }]
```



```
"fermat.obj",
```

```
Export["fermat.obj",
```

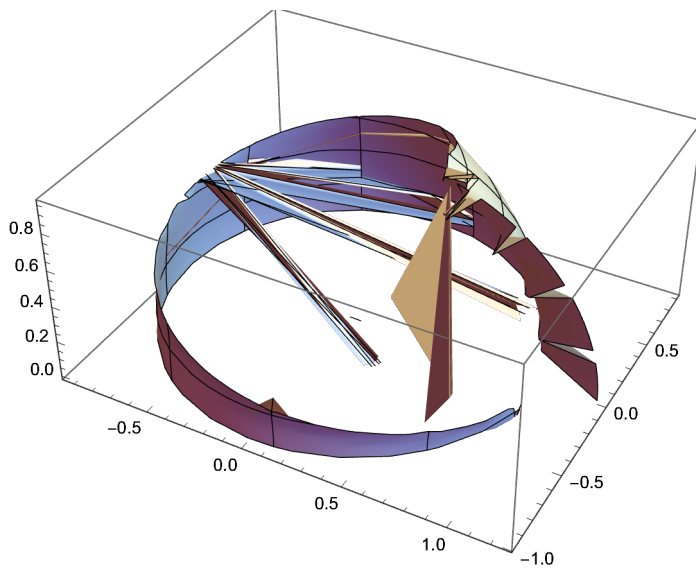
```
SphericalPlot3D[ $r^{\frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}}$ , { $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }, { $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }]]
```

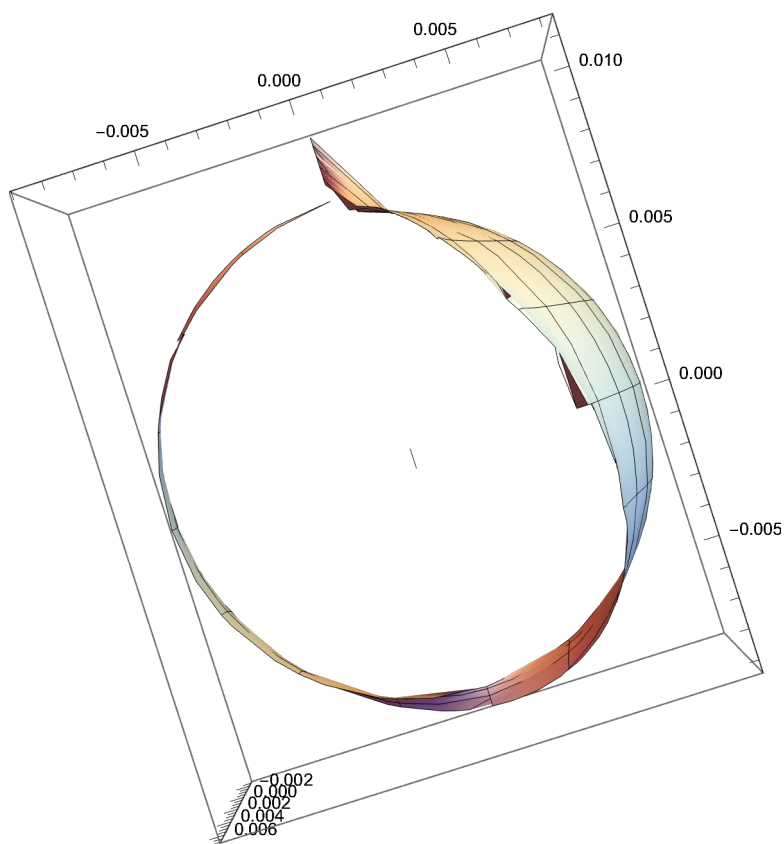
```
fermat.obj
```

```
Export["fermat4.3ds",
```

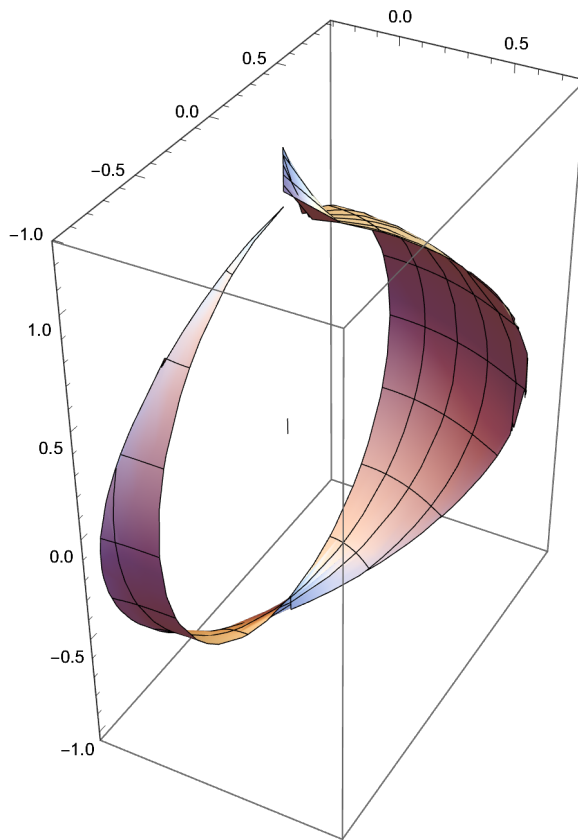
```
SphericalPlot3D[.009  $r^{\frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}}$ , { $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }, { $\beta$ ,  $-\pi/2$ ,  $\pi/2$ }]]
```

```
fermat4.3ds
```

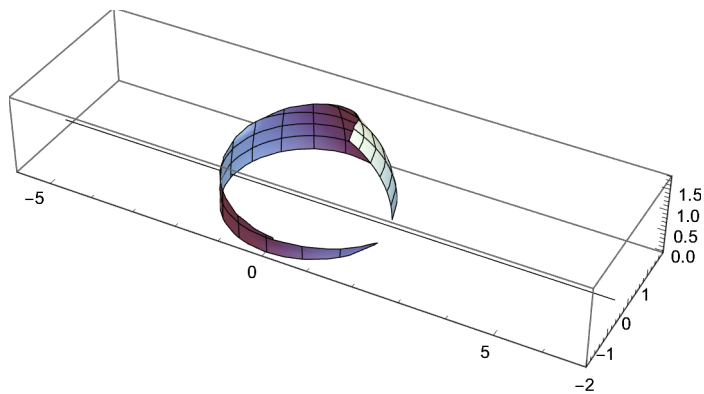
$$\text{SphericalPlot3D}\left[r^{\frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi-\sqrt{r^2(4\pi-\theta)\theta}}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$$


$$\text{SphericalPlot3D}\left[.009 r^{\frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi-\sqrt{r^2(4\pi-\theta)\theta}}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$


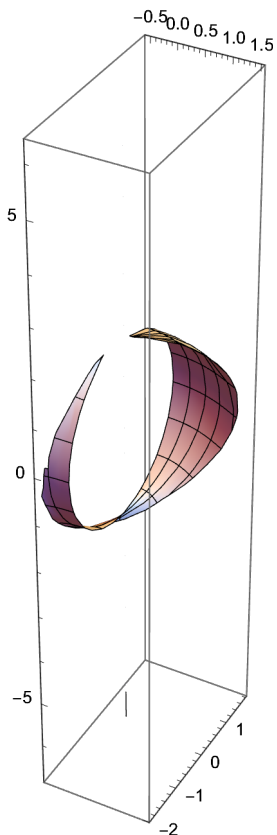
$\text{SphericalPlot3D}\left[r^{\wedge}\frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi-\sqrt{r^2(4\pi-\theta)\theta}},\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$



$\text{SphericalPlot3D}\left[\frac{2\pi r-r\theta}{2\pi}\wedge\frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi-\sqrt{r^2(4\pi-\theta)\theta}}+\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\wedge\frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi-\sqrt{r^2(4\pi-\theta)\theta}},\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$



```
SphericalPlot3D[ $\frac{2 \pi r - r \theta}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}},$ 
{ $\theta, -2 \pi, 2 \pi$ }, { $\beta, -\pi / 2, \pi / 2$ }]
```

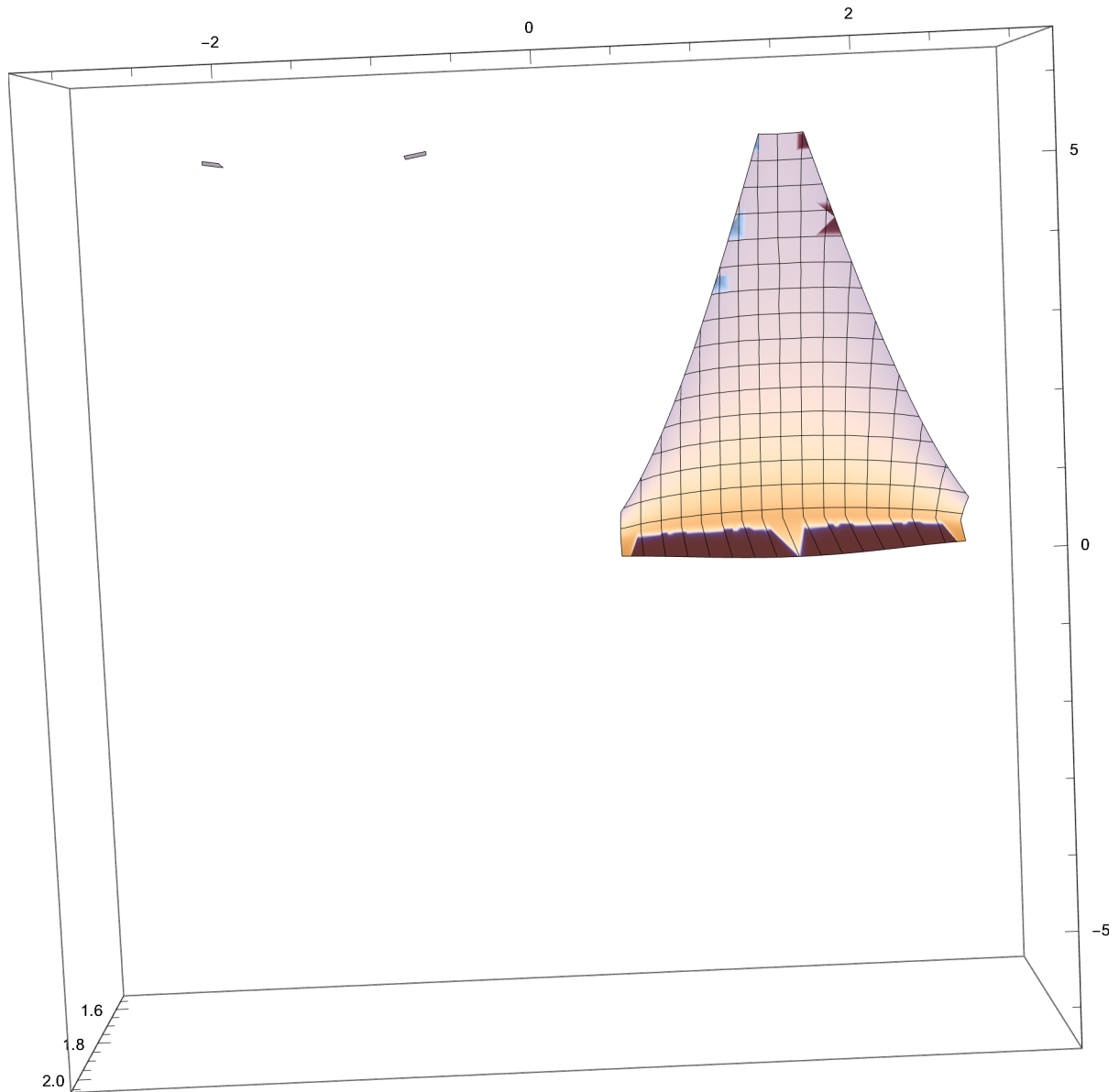


```
Export["pendantumuck.obj",
```

```
Plot3D[ $\frac{2 \pi r - r \theta}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}},$ 
{ $\beta, -\pi, \pi$ }, { $\theta, -2 \pi, 2 \pi$ }]]
```

```
pendantumuck.obj
```

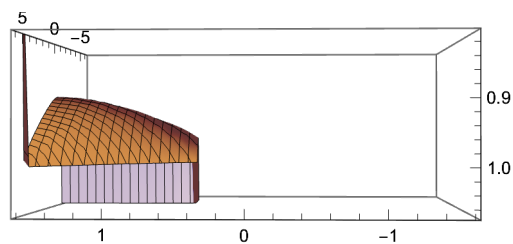
Plot3D $\left[\frac{2 \pi r - r \theta}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}, \right.$   
 $\left. \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



Solve $\left[\frac{2 \pi r - r \theta}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} == \right.$   
 $\left. r \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}, \beta\right]$

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

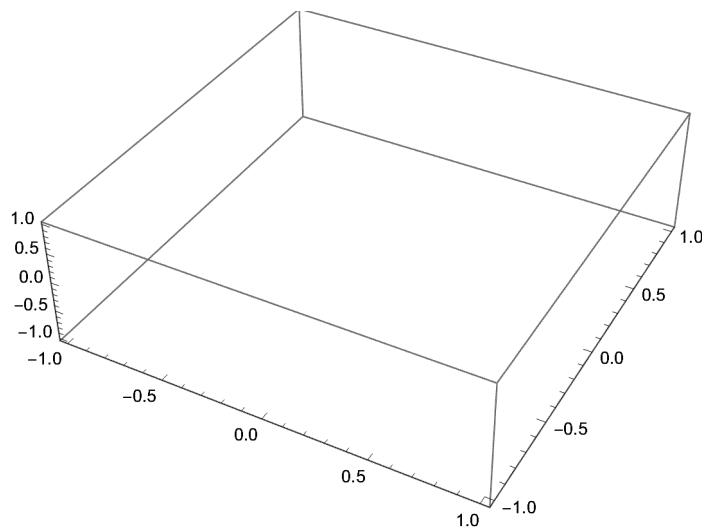
$$\text{Plot3D}\left[r^{\frac{\sqrt{r^2(4\pi - \theta)\theta}}{2\pi - \sqrt{r^2(4\pi - \theta)\theta}}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$



$$\text{RevolutionPlot3D}\left[r^{\frac{\sqrt{r^2(4\pi - \theta)\theta}}{2\pi - \sqrt{r^2(4\pi - \theta)\theta}}}, \{\theta, -2\pi, 2\pi\}\right]$$

Power::indet: Indeterminate expression  $(0. + 0.i)^{0.+0.i}$  encountered. >>

Power::indet: Indeterminate expression  $(0. + 0.i)^{0.+0.i}$  encountered. >>



```
Export["ringquest.obj", RevolutionPlot3D[ $\frac{2\pi r - r\theta}{2\pi} \wedge \frac{\sqrt{r^2(4\pi - \theta)\theta}}{2\pi - \sqrt{r^2(4\pi - \theta)\theta}} +$   

 $\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \wedge \frac{\sqrt{r^2(4\pi - \theta)\theta}}{2\pi - \sqrt{r^2(4\pi - \theta)\theta}}, \{\theta, -\pi/2, \pi/2\}]]]$ 
```

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

∞::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

∞::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

∞::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

General::stop : Further output of ∞::indet will be suppressed during this calculation. >>

ringquest.obj

```
RevolutionPlot3D[  

 $\left( \frac{2\pi r - r\theta}{2\pi} \wedge \frac{\sqrt{r^2(4\pi - \theta)\theta}}{2\pi - \sqrt{r^2(4\pi - \theta)\theta}} + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \wedge \frac{\sqrt{r^2(4\pi - \theta)\theta}}{2\pi - \sqrt{r^2(4\pi - \theta)\theta}} \right),$   

 $\{\theta, -\pi/2, \pi/2\}]$ 
```

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

∞::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

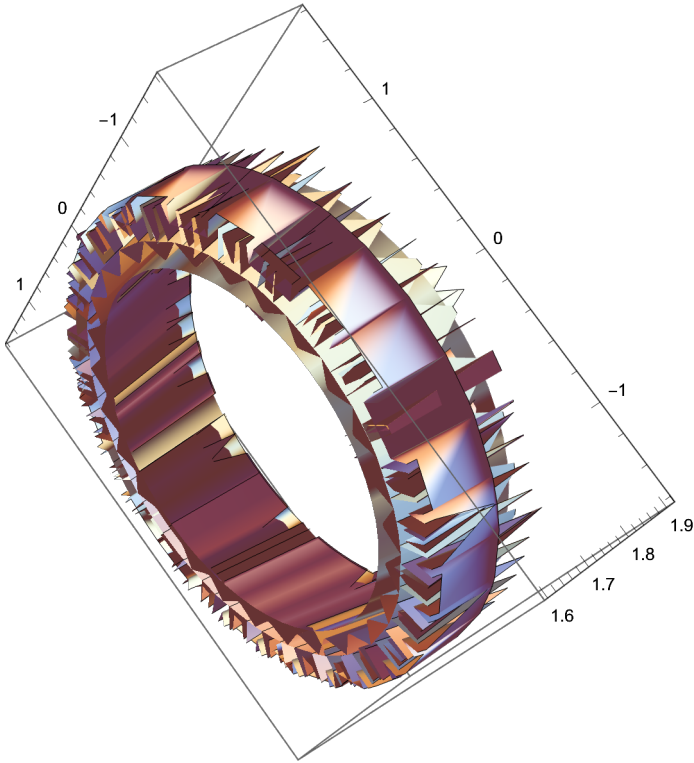
Power::infy : Infinite expression  $\frac{1}{0.^2}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

∞::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

∞::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

General::stop : Further output of ∞::indet will be suppressed during this calculation. >>



$$\text{Solve}\left[(2\pi)\sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}}-\frac{2\pi\sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}}}{\left(\left(2\pi\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)\right)/\left((16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)-\left(\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)\right)/\left((16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)+\right.\right.$$



$$\begin{aligned}
 & - \sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}} \\
 (2\pi) & \sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}} \\
 & \left( \left( 4\pi\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2 - \right. \right. \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
 & \quad (16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2 - \\
 & \quad \left( \theta^2\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2 - \right. \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / (16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}} \\
 & \left( 2\pi\sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}} \right)^2 \Bigg) =
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( -4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 - \right. \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / (16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}} \\
 & \left( 2\pi\sqrt{\frac{(4\pi-\theta)\theta\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)^2}{(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2)^2}} \right)^2 \Bigg) , \theta]
 \end{aligned}$$

{{}}

$$\frac{2\pi r - r\theta}{2\pi} \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}} + \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \wedge \frac{\sqrt{r^2(4\pi-\theta)\theta}}{2\pi - \sqrt{r^2(4\pi-\theta)\theta}}$$

Indeterminate

$$r^{\wedge} \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}$$

Indeterminate

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]$$

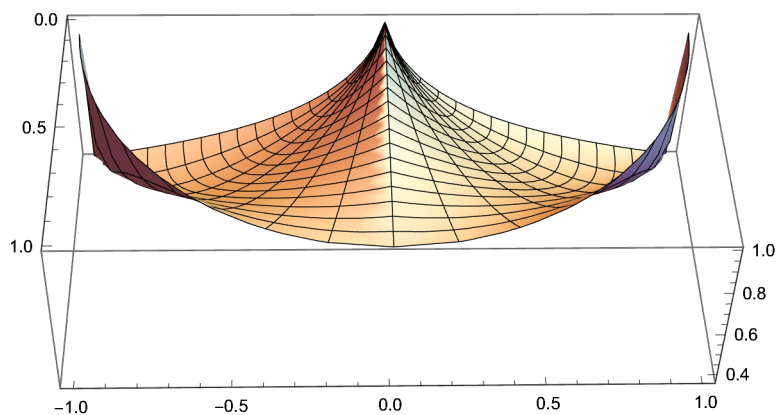
$$\text{Simplify}\left[r^{\frac{\sqrt{2} \sqrt{r^2 (\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}) (4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}))}}{2 \pi - \sqrt{2} \sqrt{r^2 (\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}) (4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}))}}}\right]$$

$$r^{\frac{\sqrt{r^2 \text{Sin}[\beta]^2}}{1 - \sqrt{r^2 \text{Sin}[\beta]^2}}}$$

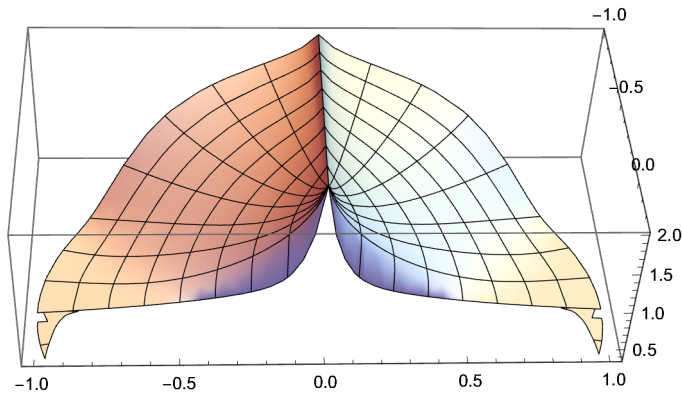
$$\text{Simplify}\left[\frac{2 \pi r - r \theta}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}} + \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \wedge \frac{\sqrt{r^2 (4 \pi - \theta) \theta}}{2 \pi - \sqrt{r^2 (4 \pi - \theta) \theta}}\right]$$

$$\left(-r \sqrt{\text{Cos}[\beta]^2}\right)^{\frac{\sqrt{r^2 \text{Sin}[\beta]^2}}{1 - \sqrt{r^2 \text{Sin}[\beta]^2}}} + \left(r^2 \text{Sin}[\beta]^2\right)^{\frac{\sqrt{r^2 \text{Sin}[\beta]^2}}{2 - 2 \sqrt{r^2 \text{Sin}[\beta]^2}}}$$

$$\text{RevolutionPlot3D}\left[r^{\frac{\sqrt{r^2 \text{Sin}[\beta]^2}}{1 - \sqrt{r^2 \text{Sin}[\beta]^2}}}, \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}\right]$$



```
RevolutionPlot3D[(-r Sqrt[Cos[beta]^2])^(sqrt(r^2 Sin[beta]^2)/(1 - sqrt(r^2 Sin[beta]^2))) + (r^2 Sin[beta]^2)^(sqrt(r^2 Sin[beta]^2)/(2 - 2 sqrt(r^2 Sin[beta]^2))),
{r, -1, 1}, {beta, -pi/2, pi/2}]
```



```
Solve[r^(sqrt(r^2 Sin[beta]^2)/(1 - sqrt(r^2 Sin[beta]^2))) == (-r Sqrt[Cos[beta]^2])^(sqrt(r^2 Sin[beta]^2)/(1 - sqrt(r^2 Sin[beta]^2))) + (r^2 Sin[beta]^2)^(sqrt(r^2 Sin[beta]^2)/(2 - 2 sqrt(r^2 Sin[beta]^2))), theta]
{{}}
```

Proven equality within the system of a cone for  $x^n + y^n = z^n$ , no matter what  $n$  is. Thus, because it is true for  $n < 2$ , it is true for  $n > 2$ .

$$\Delta x \Delta p = (2\pi r - 2\pi x)(m_1 v_1 - m_2 v_2)$$

if,  $m_1 = m_2$

if,  $v_1 = v_2$

if both

if  $v_1 =$

$$D\left[\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, t\right] ==$$

```
Solve[(sqrt(-1.1294090667581471 * ^18 theta +
8.987551787368176 * ^16 theta^2 + 3.5481432270250993 * ^18 Sin[beta]^2)) /
(sqrt(-12.566370614359172 * theta + theta^2 + 39.47841760435743 * Sin[beta]^2)) == v, theta]
```

```
{}
```

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{1}{-8.98755 \times 10^{16} + v^2} \right.\right. \\ \left.0.5 \left(-1.12941 \times 10^{18} + 12.5664 v^2 - 1. \sqrt{\left(\left(1.12941 \times 10^{18} - 12.5664 v^2\right)^2 - \right.\right.\right. \\ \left.\left.4. \left(-8.98755 \times 10^{16} + v^2\right) \left(-3.54814 \times 10^{18} + 39.4784 v^2\right) \sin[\beta]^2\right)\right)\right\}, \left\{\theta \rightarrow \right. \\ \left.\frac{1}{-8.98755 \times 10^{16} + v^2} 0.5 \left(-1.12941 \times 10^{18} + 12.5664 v^2 + \sqrt{\left(\left(1.12941 \times 10^{18} - 12.5664 v^2\right)^2 - \right.\right.\right. \\ \left.\left.4. \left(-8.98755 \times 10^{16} + v^2\right) \left(-3.54814 \times 10^{18} + 39.4784 v^2\right) \sin[\beta]^2\right)\right)\right\}\right\}$$

$$v := r / t$$

$$\text{Solve}\left[\theta == \frac{1}{-8.987551787368176 \cdot v^{16} + v^2} \right. \\ \left.0.5 \left(-1.1294090667581471 \cdot v^{18} + 12.566370614359172 \cdot v^2 + \right.\right. \\ \left.\sqrt{\left(\left(1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2\right)^2 - 4. \cdot \right.\right. \\ \left.\left(-8.987551787368176 \cdot v^{16} + v^2\right) \right. \\ \left.\left(-3.5481432270250993 \cdot v^{18} + 39.47841760435743 \cdot v^2\right) \sin[\beta]^2\right)\right), t]$$

$$\left\{\left\{t \rightarrow -0.5 \sqrt{\left(-\left(2. r^2 \right.\right.\right. \\ \left.\left(-4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - 4.34585 \times 10^{34} \sin[\beta]^2\right)\right) / \right. \\ \left.\left(2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2\right) - \right. \\ \left.2. \sqrt{\left(\left(r^4 \left(-4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right.\right.\right. \right. \\ \left.\left.4.34585 \times 10^{34} \sin[\beta]^2\right)^2\right) / \right. \\ \left.\left(2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2\right)^2 - \right. \\ \left.\left(4. r^4 \left(-7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2\right)\right) / \right. \\ \left.\left(2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + \right.\right. \\ \left.\left.4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2\right)\right)\right)\right\}, \\ \left\{t \rightarrow 0.5 \sqrt{\left(-\left(2. r^2 \left(-4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right.\right.\right. \right. \\ \left.\left.4.34585 \times 10^{34} \sin[\beta]^2\right)\right) / \right. \\ \left.\left(2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2\right) - \right. \\ \left.2. \sqrt{\left(\left(r^4 \left(-4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right.\right.\right. \right. \\ \left.\left.4.34585 \times 10^{34} \sin[\beta]^2\right)^2\right) / \right. \\ \left.\left(2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2\right)^2 - \right. \\ \left.\left(4. r^4 \left(-7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2\right)\right) / \right. \\ \left.\left(2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + \right.\right. \\ \left.\left.4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2\right)\right)\right)\right\},$$

$$\begin{aligned}
& \left\{ t \rightarrow -0.5 \sqrt{\left( -\left( 2. r^2 \left( -4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 4.34585 \times 10^{34} \sin[\beta]^2 \right) \right) / \right. \\
& \quad \left( 2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2 \right) + \\
& \quad 2. \sqrt{\left( \left( r^4 \left( -4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 4.34585 \times 10^{34} \sin[\beta]^2 \right)^2 \right) / \right. \\
& \quad \left( 2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2 \right)^2 - \\
& \quad \left( 4. r^4 \left( -7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2 \right) \right) / \\
& \quad \left( 2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + \right. \\
& \quad \left. 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2 \right) \left. \right) \left. \right) \left. \right) \left. \right\}, \\
& \left\{ t \rightarrow 0.5 \sqrt{\left( -\left( 2. r^2 \left( -4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. 4.34585 \times 10^{34} \sin[\beta]^2 \right) \right) / \right. \\
& \quad \left( 2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2 \right) + \\
& \quad 2. \sqrt{\left( \left( r^4 \left( -4.62529 \times 10^{17} + 1.38333 \times 10^{34} \theta - 1.10082 \times 10^{33} \theta^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 4.34585 \times 10^{34} \sin[\beta]^2 \right)^2 \right) / \right. \\
& \quad \left( 2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2 \right)^2 - \\
& \quad \left( 4. r^4 \left( -7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2 + 2.41771 \times 10^{17} \sin[\beta]^2 \right) \right) / \\
& \quad \left( 2.07727 \times 10^{35} - 6.21637 \times 10^{50} \theta + \right. \\
& \quad \left. 4.94683 \times 10^{49} \theta^2 + 1.95293 \times 10^{51} \sin[\beta]^2 \right) \left. \right) \left. \right) \left. \right) \left. \right\} \\
& 0.5 \sqrt{\left( -\left( 2. r^2 \left( -4.6252927586946355 \times 10^{17} + 1.3833281122109134 \times 10^{34} \theta - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1.1008175348817346 \times 10^{33} \theta^2 - 4.345853434826043 \times 10^{34} \sin[\beta]^2 \right) \right) / \right. \\
& \quad \left( 2.0772739051957146 \times 10^{35} - 6.21636652370892 \times 10^{50} \theta + \right. \\
& \quad \left. 4.946827301596282 \times 10^{49} \theta^2 + 1.9529291402905465 \times 10^{51} \sin[\beta]^2 \right) + \\
& \quad 2. \sqrt{\left( \left( r^4 \left( -4.6252927586946355 \times 10^{17} + 1.3833281122109134 \times 10^{34} \theta - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 1.1008175348817346 \times 10^{33} \theta^2 - 4.345853434826043 \times 10^{34} \sin[\beta]^2 \right)^2 \right) / \right. \\
& \quad \left( 2.0772739051957146 \times 10^{35} - 6.21636652370892 \times 10^{50} \theta + \right. \\
& \quad \left. 4.946827301596282 \times 10^{49} \theta^2 + 1.9529291402905465 \times 10^{51} \sin[\beta]^2 \right)^2 - \\
& \quad \left( 4. r^4 \left( -7.695800507960096 \times 10^{16} \theta + 6.124123459454841 \times 10^{15} \theta^2 + \right. \right. \\
& \quad \left. \left. 2.4177070339300032 \times 10^{17} \sin[\beta]^2 \right) \right) / \\
& \quad \left( 2.0772739051957146 \times 10^{35} - 6.21636652370892 \times 10^{50} \theta + \right. \\
& \quad \left. 4.946827301596282 \times 10^{49} \theta^2 + 1.9529291402905465 \times 10^{51} \sin[\beta]^2 \right) \left. \right) \left. \right) \left. \right) \left. \right)
\end{aligned}$$

$$\text{Solve}\left[\theta == \frac{1}{-8.987551787368176 \cdot v^{16} + v^2}\right. \\ \left.0.5 \cdot \left(-1.1294090667581471 \cdot v^{18} + 12.566370614359172 \cdot v^2 + \sqrt{\left((1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2)^2 - 4 \cdot (-8.987551787368176 \cdot v^{16} + v^2)\right)}\right. \right. \\ \left. \left.(-3.5481432270250993 \cdot v^{18} + 39.47841760435743 \cdot v^2) \sin[\beta]^2\right)\right], \theta]$$

$$\left\{\left\{\theta \rightarrow 3.32694 \times 10^{-49} \left(1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} - \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)}\right)\right\}, \right. \\ \left.\left\{\theta \rightarrow 3.32694 \times 10^{-49} \left(1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)}\right)\right\}\right\}$$

$$\theta := 3.3269445087319456 \cdot v^{-49} \left(1.7124327770294835 \cdot v^{49} - \frac{8.53228731259923 \cdot v^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot v^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot v^{14} \sqrt{(1. r^8 - 6.16152983412695 \cdot v^{16} r^6 t^2 - 5.930324312706987 \cdot v^{34} r^4 t^4 - 4.252029524247228 \cdot v^{51} r^2 t^6 + 1.8379263355222364 \cdot v^{68} t^8)}\right)$$







$$\begin{aligned}
& 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \\
& \left( \frac{3.41291 \times 10^{15} r^4}{t^5} - \frac{5.25719 \times 10^{31} r^2}{t^3} + \left( 4.26614 \times 10^{14} \left( -1.23231 \times 10^{17} r^6 t - \right. \right. \right. \\
& \quad \left. \left. \left. 2.37213 \times 10^{35} r^4 t^3 - 2.55122 \times 10^{52} r^2 t^5 + 1.47034 \times 10^{69} t^7 \right) \right) / \right. \\
& \quad \left( t^4 \sqrt{\left( 1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + \right. \right. \\
& \quad \left. \left. 1.83793 \times 10^{68} t^8 \right)} \right) - \frac{1}{t^5} 3.41291 \times 10^{15} \sqrt{\left( 1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \right. \\
& \quad \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8 \right)} \Bigg) \\
& \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \right. \\
& \quad \left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{\left( 1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8 \right)} \right) \Bigg) + \\
& \frac{1}{t^3} 2.66156 \times 10^{-48} r^2 \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \\
& \quad \left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{\left( 1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \right. \right. \\
& \quad \left. \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8 \right)} \right) \\
& \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \right. \\
& \quad \left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{\left( 1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8 \right)} \right) \Bigg) + \frac{1}{t^3} 6.7418 \times 10^{-50} r^2 \\
& \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \\
& \quad \left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{\left( 1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \right. \right. \\
& \quad \left. \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8 \right)} \right) \\
& \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right.
\end{aligned}$$

$$\frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -$$
$$5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg) \Bigg) /$$
$$\left( 2 \sqrt{\left( \left( 1.12941 \times 10^{18} - \frac{12.5664 r^2}{t^2} \right)^2 - 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \right.} \right.$$
$$\left. \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right.$$
$$\left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \right.$$
$$\left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg)$$
$$\left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \right.$$
$$\left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 -} \right.$$
$$\left. 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg) \Bigg) \Bigg) -$$
$$\left( 0.5 r^2 \left( -1.12941 \times 10^{18} + \frac{12.5664 r^2}{t^2} + \sqrt{\left( \left( 1.12941 \times 10^{18} - \frac{12.5664 r^2}{t^2} \right)^2 -} \right. \right.$$
$$\left. 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \right. \right.$$
$$\left. \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \right.$$
$$\left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \right.$$
$$\left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg)$$
$$\left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right.$$
$$\left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \right.$$
$$\left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg) \Bigg) \Bigg)$$

$$\begin{aligned}
& \left( -\frac{25.1327 r^2}{t^3} + \left( \frac{50.2655 r^2 \left( 1.12941 \times 10^{18} - \frac{12.5664 r^2}{t^2} \right)}{t^3} + 1.12148 \times 10^{-98} \right. \right. \\
& \quad \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \\
& \quad \left( \frac{3.41291 \times 10^{15} r^4}{t^5} - \frac{5.25719 \times 10^{31} r^2}{t^3} + (4.26614 \times 10^{14} (-1.23231 \times 10^{17} r^6 t - \right. \\
& \quad \left. 2.37213 \times 10^{35} r^4 t^3 - 2.55122 \times 10^{52} r^2 t^5 + 1.47034 \times 10^{69} t^7)) / (t^4 \right. \\
& \quad \left. \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + \right. \\
& \quad \left. 1.83793 \times 10^{68} t^8)} \right) - \frac{1}{t^5} 3.41291 \times 10^{15} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \\
& \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \left. \right) \\
& \quad \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \\
& \quad \left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \right. \\
& \quad \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \right) - \\
& \quad 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \\
& \quad \left( \frac{3.41291 \times 10^{15} r^4}{t^5} - \frac{5.25719 \times 10^{31} r^2}{t^3} + (4.26614 \times 10^{14} (-1.23231 \times 10^{17} r^6 t - \right. \\
& \quad \left. 2.37213 \times 10^{35} r^4 t^3 - 2.55122 \times 10^{52} r^2 t^5 + 1.47034 \times 10^{69} t^7)) / (t^4 \right. \\
& \quad \left. \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + \right. \\
& \quad \left. 1.83793 \times 10^{68} t^8)} \right) - \frac{1}{t^5} 3.41291 \times 10^{15} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \\
& \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \left. \right) \\
& \quad \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\
& \quad \left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \right. \\
& \quad \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \right) \left. \right) + \\
& \quad \frac{1}{t^3} 2.66156 \times 10^{-48} r^2 \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \\
& \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \\
& \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\
& \quad \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg) + \\
& \frac{1}{t^3} 6.7418 \times 10^{-50} r^2 \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \left( 1.71243 \times \right. \\
& \quad 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} \\
& \quad 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 -} \\
& \quad \quad 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \\
& \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\
& \quad \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg) \Bigg) / \\
& \left( 2 \sqrt{\left( \left( 1.12941 \times 10^{18} - \frac{12.5664 r^2}{t^2} \right)^2 - 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \right. \right. \\
& \quad \left. \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\
& \quad \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \Bigg) \Bigg) \left( 4 \pi - \right. \\
& \quad 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \\
& \quad \quad \left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 -} \right.
\end{aligned}$$

$$\begin{aligned} & \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right)^2 \Bigg/ \left( 4 \pi \sqrt{\left( \left( 6.28319 r^2 \left( -1.12941 \times 10^{18} + \frac{12.5664 r^2}{t^2} + \right. \right. \right. \right. \\ & \sqrt{\left( \left( 1.12941 \times 10^{18} - \frac{12.5664 r^2}{t^2} \right)^2 - 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \right. \\ & \left. \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\ & \left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \right. \\ & \left. \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \right) \right) \left( 4 \pi - \right. \\ & \left. 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \right. \\ & \left. \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 -} \right. \\ & \left. \left. 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \right) \right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg/ \\ & \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) - \left( 0.25 r^2 \left( -1.12941 \times 10^{18} + \frac{12.5664 r^2}{t^2} + \right. \right. \\ & \sqrt{\left( \left( 1.12941 \times 10^{18} - \frac{12.5664 r^2}{t^2} \right)^2 - 3.3709 \times 10^{-50} \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right) \right. \\ & \left. \left( -3.54814 \times 10^{18} + \frac{39.4784 r^2}{t^2} \right) \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\ & \left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \right. \\ & \left. \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8) \right) \right) \\ & \left( 4 \pi - 3.32694 \times 10^{-49} \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \right. \right. \\ & \left. \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 -} \right. \\ & \left. \left. 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + \right. \right. \end{aligned}$$

$$\left( \left( \left( \left( 1.83793 \times 10^{68} t^8 \right) \right) \right) \right)^2 / \left( -8.98755 \times 10^{16} + \frac{r^2}{t^2} \right)^2$$

`RevolutionPlot3D[`

$$\left( \left( 12.566370614359172 \cdot r^4 \left( -1.1294090667581471 \cdot t^{18} + \frac{12.566370614359172 \cdot r^2}{t^2} + \sqrt{\left( \left( 1.1294090667581471 \cdot t^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - 3.370899555370967 \cdot t^{-50} \left( -8.987551787368176 \cdot t^{16} + \frac{r^2}{t^2} \right) \left( -3.5481432270250993 \cdot t^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8 \right)} \right) \right) \right) \left( 4 \pi - 3.3269445087319456 \cdot t^{-49} \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8 \right)} \right) \right) \right) \left( -8.987551787368176 \cdot t^{16} + \frac{r^2}{t^2} \right) t^3 - \left( 1 \cdot r^4 \left( -1.1294090667581471 \cdot t^{18} + \frac{12.566370614359172 \cdot r^2}{t^2} + \sqrt{\left( \left( 1.1294090667581471 \cdot t^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - 3.370899555370967 \cdot t^{-50} \left( -8.987551787368176 \cdot t^{16} + \frac{r^2}{t^2} \right) \right)} \right) \right)$$

$$\begin{aligned}
& \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \Big) \\
& \left( 4\pi - 3.3269445087319456 \cdot r^{-49} \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \right) \right)^2 \Big) / \\
& \left( \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right)^3 t^3 \right) + \frac{1}{-8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2}} \\
& 6.283185307179586 \cdot r^2 \\
& \left( -\frac{25.132741228718345 \cdot r^2}{t^3} + \right. \\
& \left( \frac{1}{t^3} 50.26548245743669 \cdot r^2 \left( 1.1294090667581471 \cdot r^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right) + \right. \\
& 1.1214795765228395 \cdot r^{-98} \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) \\
& \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \left( \frac{3.412914925039692 \cdot r^{15}}{t^5} - \right. \\
& \left. \frac{5.257194282992301 \cdot r^{31}}{t^3} + (4.266143656299615 \cdot r^{14} \right. \\
& \quad (-1.23230596682539 \cdot r^{17} r^6 t - 2.3721297250827947 \cdot r^{35} r^4 t^3 - 2.551217714548337 \cdot r^{52} r^2 t^5 + 1.4703410684177891 \cdot r^{69} t^7) \Big) / \\
& (t^4 \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)}) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{t^5} 3.412914925039692 \cdot 10^{15} \sqrt{(1 \cdot 10^8 - 6.16152983412695 \cdot 10^{16} \\
& \quad r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \\
& \quad 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)} \\
& \left( 1.7124327770294835 \cdot 10^{49} - \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \\
& \quad \sqrt{(1 \cdot 10^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \\
& \quad 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)} \Big) - \\
& 3.370899555370967 \cdot 10^{-50} \left( -8.987551787368176 \cdot 10^{16} + \frac{r^2}{t^2} \right) \\
& \left( -3.5481432270250993 \cdot 10^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \left( \frac{3.412914925039692 \cdot 10^{15} r^4}{t^5} - \right. \\
& \quad \frac{5.257194282992301 \cdot 10^{31} r^2}{t^3} + (4.266143656299615 \cdot 10^{14} \\
& \quad (-1.23230596682539 \cdot 10^{17} r^6 t - 2.3721297250827947 \cdot 10^{35} r^4 t^3 - \\
& \quad 2.551217714548337 \cdot 10^{52} r^2 t^5 + 1.4703410684177891 \cdot 10^{69} t^7)) / \\
& \quad (t^4 \sqrt{(1 \cdot 10^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 \\
& \quad t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)}) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot 10^{15} \sqrt{(1 \cdot 10^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - \\
& \quad 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + \\
& \quad 1.8379263355222364 \cdot 10^{68} t^8)} \Big) \left( 4\pi - 3.3269445087319456 \cdot 10^{-49} \right. \\
& \quad \left( 1.7124327770294835 \cdot 10^{49} - \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \sqrt{(1 \cdot 10^8 - \\
& \quad 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \\
& \quad 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)} \Big) \Big) + \\
& \frac{1}{t^3} 2.6615556069855565 \cdot 10^{-48} r^2 \left( -8.987551787368176 \cdot 10^{16} + \frac{r^2}{t^2} \right)
\end{aligned}$$



$$\begin{aligned}
& \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \Bigg) \\
& \left( 4\pi - 3.3269445087319456 \cdot t^{-49} \left( 1.7124327770294835 \cdot t^{49} - \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^2}{t^2} + \\
& \quad \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \right. \\
& \quad \left. 5.930324312706987 \cdot r^4 t^4 - 4.252029524247228 \cdot r^2 t^6 + \right. \\
& \quad \left. \left. 1.8379263355222364 \cdot t^8 \right)} \right) \Bigg) + \frac{1}{t^3} 6.741799110741934 \cdot t^{-50} \\
& r^2 \left( -3.5481432270250993 \cdot t^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \Bigg) \\
& \left( 4\pi - 3.3269445087319456 \cdot t^{-49} \left( 1.7124327770294835 \cdot t^{49} - \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^2}{t^2} + \\
& \quad \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \right. \\
& \quad \left. 5.930324312706987 \cdot r^4 t^4 - 4.252029524247228 \cdot r^2 t^6 + \right. \\
& \quad \left. \left. 1.8379263355222364 \cdot t^8 \right)} \right) \Bigg) \Bigg) / \\
& \left( 2 \sqrt{\left( \left( 1.1294090667581471 \cdot t^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - \right. \right. \\
& \quad \left. \left. 3.370899555370967 \cdot t^{-50} \left( -8.987551787368176 \cdot t^{16} + \frac{r^2}{t^2} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} r^4 \right.} \\
& \quad \left. t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \left. \right) \\
& \left( 4\pi - 3.3269445087319456 \cdot r^{49} \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \\
& \quad \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - \right.} \\
& \quad \left. 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \\
& \quad \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \left. \right) \left. \right) \left. \right) \left. \right) - \\
& \left( 0.5 \cdot r^2 \left( -1.1294090667581471 \cdot r^{18} + \frac{12.566370614359172 \cdot r^2}{t^2} + \right. \right. \\
& \quad \sqrt{\left( \left( 1.1294090667581471 \cdot r^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - \right.} \\
& \quad \left. 3.370899555370967 \cdot r^{50} \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) \right. \\
& \quad \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \quad \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - \right.} \\
& \quad \left. 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \left. \right) \\
& \quad \left( 4\pi - 3.3269445087319456 \cdot r^{49} \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \left. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \Big) \Big) \Big) \Big) \\
& \left( -\frac{25.132741228718345 \cdot r^2}{t^3} + \left( \frac{1}{t^3} 50.26548245743669 \cdot r^2 \right. \right. \\
& \quad \left. \left( 1.1294090667581471 \cdot r^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right) + \right. \\
& \quad 1.1214795765228395 \cdot r^{-98} \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) \\
& \quad \left. \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \right. \\
& \quad \left. \left( \frac{3.412914925039692 \cdot r^{15} r^4}{t^5} - \frac{5.257194282992301 \cdot r^{31} r^2}{t^3} + \right. \right. \\
& \quad \left. \left( 4.266143656299615 \cdot r^{14} \left( -1.23230596682539 \cdot r^{17} r^6 t - \right. \right. \right. \\
& \quad \left. 2.3721297250827947 \cdot r^{35} r^4 t^3 - 2.551217714548337 \cdot r^{52} r^2 t^5 + \right. \\
& \quad \left. 1.4703410684177891 \cdot r^{69} t^7 \right) \Big) / \left( t^4 \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \right) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \Big) \\
& \quad \left. \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14} r^4}{t^4} + \right. \right. \\
& \quad \left. \frac{2.6285971414961507 \cdot r^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \right. \\
& \quad \left. \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \right) - \\
& \quad 3.370899555370967 \cdot r^{-50} \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) \\
& \quad \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \\
& \quad \left( \frac{3.412914925039692 \cdot r^{15} r^4}{t^5} - \frac{5.257194282992301 \cdot r^{31} r^2}{t^3} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4.266143656299615 \cdot 10^{14} \left( -1.23230596682539 \cdot 10^{17} r^6 t - \right. \right. \\
& \quad 2.3721297250827947 \cdot 10^{35} r^4 t^3 - 2.551217714548337 \cdot 10^{52} r^2 t^5 + \\
& \quad 1.4703410684177891 \cdot 10^{69} t^7) \Big) / \left( t^4 \sqrt{ \left( 1. \cdot 10^{18} - \right. \right. \\
& \quad 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \\
& \quad 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8) \Big) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot 10^{15} \sqrt{ \left( 1. \cdot 10^{18} - 6.16152983412695 \cdot 10^{16} r^6 t^2 - \right. \\
& \quad 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + \\
& \quad \left. \left. 1.8379263355222364 \cdot 10^{68} t^8 \right) \right) \left( 4 \pi - 3.3269445087319456 \cdot 10^{-49} \right. \\
& \quad \left( 1.7124327770294835 \cdot 10^{49} - \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \right. \\
& \quad \left. \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \sqrt{ \left( 1. \cdot 10^{18} - \right. \right. \\
& \quad 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \\
& \quad \left. \left. 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8 \right) \right) \Big) \Big) + \\
& \quad \frac{1}{t^3} 2.6615556069855565 \cdot 10^{-48} r^2 \left( -8.987551787368176 \cdot 10^{16} + \frac{r^2}{t^2} \right) \\
& \quad \left( 1.7124327770294835 \cdot 10^{49} - \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \right. \\
& \quad \left. \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \sqrt{ \left( 1. \cdot 10^{18} - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8 \right) \right) \Big) \\
& \quad \left( 4 \pi - 3.3269445087319456 \cdot 10^{-49} \left( 1.7124327770294835 \cdot 10^{49} - \right. \right. \\
& \quad \left. \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} + \right. \\
& \quad \left. \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \sqrt{ \left( 1. \cdot 10^{18} - 6.16152983412695 \cdot 10^{16} r^6 t^2 - \right. \right. \\
& \quad 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + \\
& \quad \left. \left. 1.8379263355222364 \cdot 10^{68} t^8 \right) \right) \Big) \Big) + \frac{1}{t^3} 6.741799110741934 \cdot 10^{-50} \\
& \quad r^2 \left( -3.5481432270250993 \cdot 10^{18} + \frac{39.47841760435743 \cdot 10^{18} r^2}{t^2} \right)
\end{aligned}$$

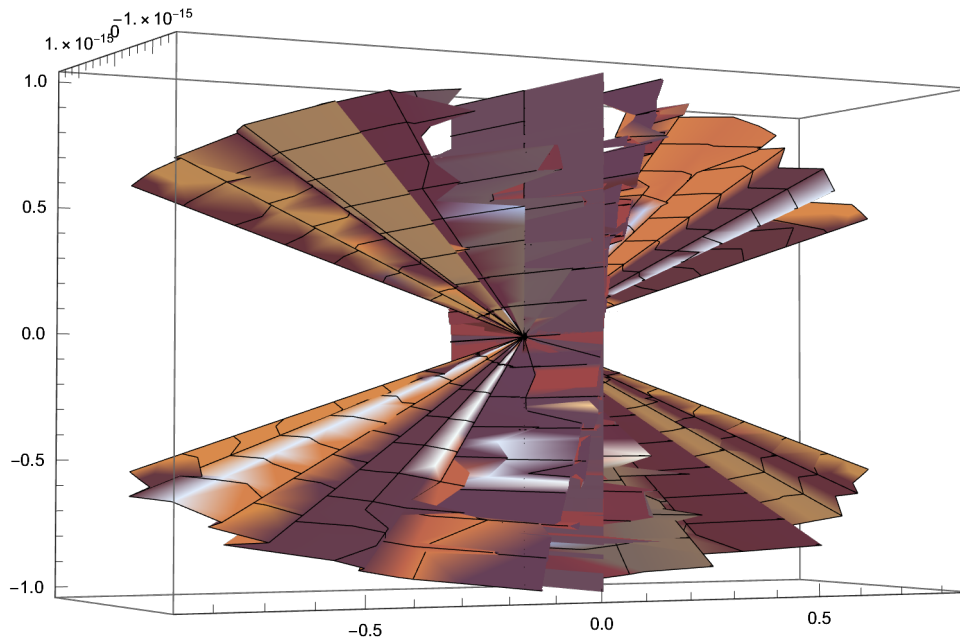
$$\left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot t^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot t^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8)} \right) \left( 4\pi - 3.3269445087319456 \cdot t^{-49} \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot t^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot t^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8)} \right) \right) / \left( 2 \sqrt{\left( 1.1294090667581471 \cdot t^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - 3.370899555370967 \cdot t^{-50} \left( -8.987551787368176 \cdot t^{16} + \frac{r^2}{t^2} \right) \left( -3.5481432270250993 \cdot t^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot t^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot t^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8)} \right) \right) \left( 4\pi - 3.3269445087319456 \cdot t^{-49} \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot t^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot t^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8)} \right) \right) /$$

$$\begin{aligned}
& \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right)^2 \Bigg/ \left( 4 \pi \sqrt{\left( \left( 6.283185307179586 \cdot r^2 \right. \right. \right. \\
& \quad \left. \left. \left( -1.1294090667581471 \cdot r^{18} + \frac{12.566370614359172 \cdot r^2}{t^2} + \right. \right. \right. \\
& \quad \left. \left. \sqrt{\left( \left( 1.1294090667581471 \cdot r^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - \right. \right. \right. \\
& \quad \left. \left. \left. 3.370899555370967 \cdot r^{-50} \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) \right. \right. \right. \\
& \quad \left. \left. \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \right. \right. \\
& \quad \left. \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \right. \\
& \quad \left. \left. \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{\left( 1 \cdot r^8 - \right. \right. \right. \\
& \quad \left. \left. \left. 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - \right. \right. \right. \\
& \quad \left. \left. \left. 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) \right) \\
& \quad \left( 4 \pi - 3.3269445087319456 \cdot r^{-49} \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \\
& \quad \left. \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} \right. \\
& \quad \left. 8.53228731259923 \cdot r^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - \right. \right. \\
& \quad \left. \left. 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \right. \\
& \quad \left. \left. \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) \right) \Bigg/ \\
& \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) - \left( 0.25 \cdot r^2 \left( -1.1294090667581471 \cdot r^{18} + \right. \right. \\
& \quad \left. \frac{12.566370614359172 \cdot r^2}{t^2} + \right. \\
& \quad \left. \sqrt{\left( \left( 1.1294090667581471 \cdot r^{18} - \frac{12.566370614359172 \cdot r^2}{t^2} \right)^2 - \right. \right. \\
& \quad \left. \left. 3.370899555370967 \cdot r^{-50} \left( -8.987551787368176 \cdot r^{16} + \frac{r^2}{t^2} \right) \right. \right. \\
& \quad \left. \left( -3.5481432270250993 \cdot r^{18} + \frac{39.47841760435743 \cdot r^2}{t^2} \right) \right)
\end{aligned}$$

$$\left( \begin{aligned} &1.7124327770294835 \cdot 10^{-49} - \frac{8.53228731259923 \cdot 10^{-14} r^4}{t^4} + \\ &\frac{2.6285971414961507 \cdot 10^{-31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{-14} \\ &\sqrt{\left( 1 \cdot 10^{-8} r^8 - 6.16152983412695 \cdot 10^{-16} r^6 t^2 - \right.} \\ &\quad \left. 5.930324312706987 \cdot 10^{-34} r^4 t^4 - 4.252029524247228 \cdot 10^{-51} \right. \\ &\quad \left. r^2 t^6 + 1.8379263355222364 \cdot 10^{-68} t^8 \right) \end{aligned} \right)$$

$$\left( 4 \pi - 3.3269445087319456 \cdot 10^{-49} \left( \begin{aligned} &1.7124327770294835 \cdot 10^{-49} - \\ &\frac{8.53228731259923 \cdot 10^{-14} r^4}{t^4} + \\ &\frac{2.6285971414961507 \cdot 10^{-31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{-14} \\ &\sqrt{\left( 1 \cdot 10^{-8} r^8 - 6.16152983412695 \cdot 10^{-16} r^6 t^2 - \right.} \\ &\quad \left. 5.930324312706987 \cdot 10^{-34} r^4 t^4 - 4.252029524247228 \cdot 10^{-51} \right. \\ &\quad \left. r^2 t^6 + 1.8379263355222364 \cdot 10^{-68} t^8 \right) \end{aligned} \right) \right) \right) \right) \right) \right) \right) /$$

$$\left( -8.987551787368176 \cdot 10^{-16} + \frac{r^2}{t^2} \right)^2 \right), \{r, -1, 1\}, \{t, -1, 1\}]$$



$$\beta := \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right]$$

# Algebraic, Geometric Interpretations of the Uncertainty Principle

by Parker Emmerson

My goal in this paper is to introspect into the visualization of the uncertainty principle for differences between "transcendental-phenomenological" velocity and derivative velocity. Some of our fundamental equations are:

$$h \approx \Delta x \Delta p = (2 \pi r - 2 \pi x) (m_1 v_1 - m_2 v_2) \text{ discovered by Heisenberg.}$$

If mass is constant, then we can factor out mass.

$$h \approx \Delta x \Delta p = (2 \pi r - 2 \pi x) m (v_1 - v_2)$$

$$h := 6.6260695729 \times 10^{-34} \text{ J} \cdot \text{s}$$

$$c := 2.99792458 (10^8) \text{ m / s}$$

$$c := 2.99792458 (10^8)$$

In order to construct the correct expression for the velocity that is equal to the derivative of the height of the cone with respect to time, we must first calculate the angle related to the arc length taken out of the initial circle in terms of the phenomenological velocity.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{1. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right\} \right\}$$

We will look at both the case of  $v_2 =$

$$\left( \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) /$$

$$\left( \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \right)$$

and

$$v_1 = \left( \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) /$$



$$\left( \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \right)$$

we will look at both the case of  $v_1 =$

$$D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, t \right] \text{ and } v_2 = D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, t \right]$$

$$\text{Solve} \left[ \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{1 - \frac{(v)^2}{c^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], \theta \right]$$

$$\left\{ \left\{ \theta \rightarrow \frac{1}{-8.98755 \times 10^{16} + v^2} \right. \right. \\ \left. \left. 0.5 \left( -1.12941 \times 10^{18} + 12.5664 v^2 - 1. \sqrt{\left( (1.12941 \times 10^{18} - 12.5664 v^2)^2 - \right. \right. \right. \right. \\ \left. \left. \left. 4. \left( -8.98755 \times 10^{16} + v^2 \right) \left( -3.54814 \times 10^{18} + 39.4784 v^2 \right) \sin[\beta]^2 \right) \right) \right\}, \left\{ \theta \rightarrow \right. \right. \\ \left. \left. \frac{1}{-8.98755 \times 10^{16} + v^2} 0.5 \left( -1.12941 \times 10^{18} + 12.5664 v^2 + \sqrt{\left( (1.12941 \times 10^{18} - 12.5664 v^2)^2 - \right. \right. \right. \right. \right. \\ \left. \left. \left. 4. \left( -8.98755 \times 10^{16} + v^2 \right) \left( -3.54814 \times 10^{18} + 39.4784 v^2 \right) \sin[\beta]^2 \right) \right) \right\} \right\}$$

We then have the option of setting the velocity equal to either the radius divided by time or the height divided by time. We then solve for the time. I will do this for both the height divided by time and the radius of the initial circle divided by time.

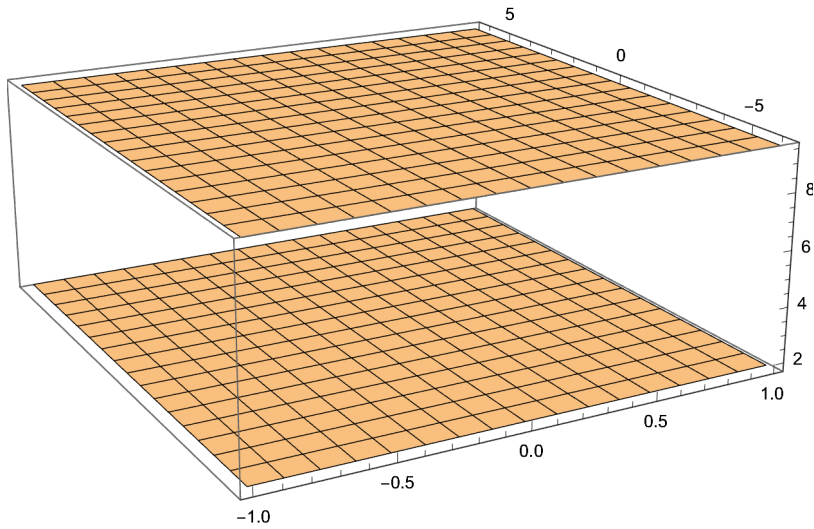
$$v := r / t$$

$$\beta := \text{ArcSin} \left[ \frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi} \right]$$

$$\text{Solve}\left[\theta == \frac{1}{-8.987551787368176 \cdot v^{16} + v^2}\right. \\ \left.0.5 \cdot \left(-1.1294090667581471 \cdot v^{18} + 12.566370614359172 \cdot v^2 + \sqrt{\left((1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2)^2 - 4 \cdot (-8.987551787368176 \cdot v^{16} + v^2)\right)}\right. \right. \\ \left. \left.(-3.5481432270250993 \cdot v^{18} + 39.47841760435743 \cdot v^2) \sin[\beta]^2\right)\right], \theta]$$

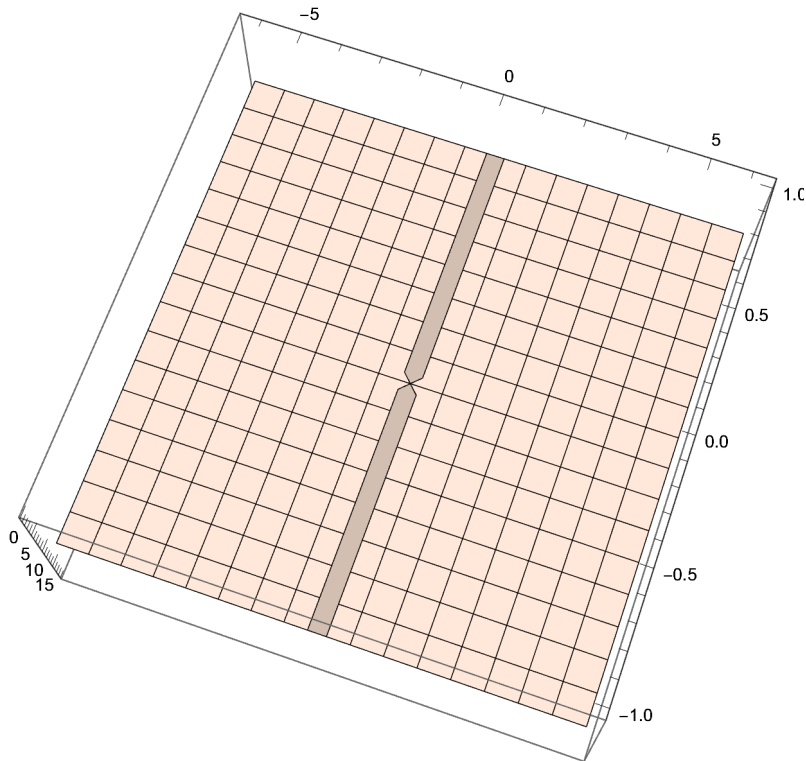
$$\left\{\left\{\theta \rightarrow 3.32694 \times 10^{-49} \left(1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} - \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)}\right)\right\}, \right. \\ \left.\left\{\theta \rightarrow 3.32694 \times 10^{-49} \left(1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)}\right)\right\}\right\}$$

$\text{Plot3D}\left[ \left\{ 3.3269445087319456 \cdot 10^{-49} \left( 1.7124327770294835 \cdot 10^{49} - \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} - \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \sqrt{1 \cdot r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8} \right) \right. \right. \\ \left. \left. 3.3269445087319456 \cdot 10^{-49} \left( 1.7124327770294835 \cdot 10^{49} - \frac{8.53228731259923 \cdot 10^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot 10^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \sqrt{1 \cdot r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8} \right) \right\}, \{r, -1, 1\}, \{t, -2\pi, 2\pi\} \right]$



Plot3D[3.3269445087319456`\*^-49

$$\left( 1.7124327770294835`^{49} - \frac{8.53228731259923`^{14} r^4}{t^4} + \frac{2.6285971414961507`^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923`^{14} \sqrt{(1.`^{8} r^8 - 6.16152983412695`^{16} r^6 t^2 - 5.930324312706987`^{34} r^4 t^4 - 4.252029524247228`^{51} r^2 t^6 + 1.8379263355222364`^{68} t^8)} \right), \{r, -1, 1\}, \{t, -2\pi, 2\pi\}]$$



$$\theta := 3.3269445087319456`^{49} \left( 1.7124327770294835`^{49} - \frac{8.53228731259923`^{14} r^4}{t^4} + \frac{2.6285971414961507`^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923`^{14} \sqrt{(1.`^{8} r^8 - 6.16152983412695`^{16} r^6 t^2 - 5.930324312706987`^{34} r^4 t^4 - 4.252029524247228`^{51} r^2 t^6 + 1.8379263355222364`^{68} t^8)} \right)$$

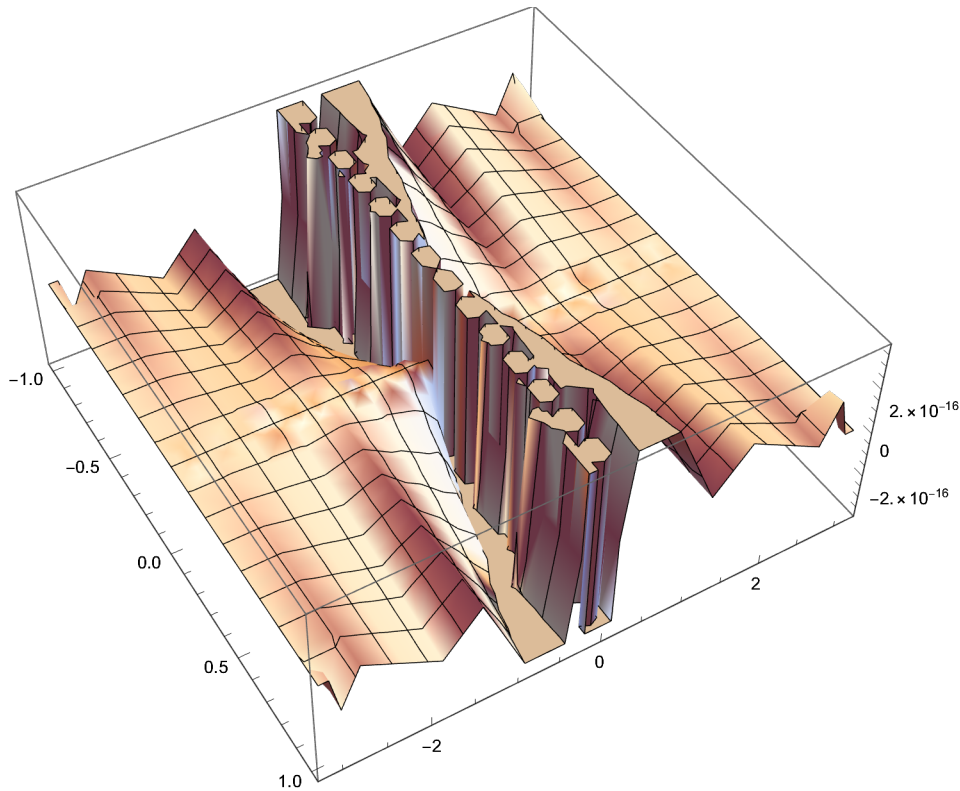
$$v_1 = D \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, t \right]$$

$$\begin{aligned}
& \left( 4.18076 \times 10^{-48} r^2 \right. \\
& \quad \left( \frac{3.41291 \times 10^{15} r^4}{t^5} - \frac{5.25719 \times 10^{31} r^2}{t^3} + (4.26614 \times 10^{14} (-1.23231 \times 10^{17} r^6 t - \right. \\
& \quad \quad 2.37213 \times 10^{35} r^4 t^3 - 2.55122 \times 10^{52} r^2 t^5 + 1.47034 \times 10^{69} t^7)) / \\
& \quad \left( t^4 \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + \right. \\
& \quad \quad 1.83793 \times 10^{68} t^8)) - \frac{1}{t^5} 3.41291 \times 10^{15} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \Big) - \\
& 2.21371 \times 10^{-97} r^2 \left( \frac{3.41291 \times 10^{15} r^4}{t^5} - \frac{5.25719 \times 10^{31} r^2}{t^3} + \right. \\
& \quad (4.26614 \times 10^{14} (-1.23231 \times 10^{17} r^6 t - 2.37213 \times 10^{35} r^4 t^3 - 2.55122 \times 10^{52} r^2 t^5 + \\
& \quad \quad 1.47034 \times 10^{69} t^7)) / (t^4 \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)}) - \\
& \quad \frac{1}{t^5} 3.41291 \times 10^{15} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - \\
& \quad \quad 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)}) \Big) \\
& \quad \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \\
& \quad \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \Big) \Big) / \\
& \left( 4 \pi \sqrt{\left( 4.18076 \times 10^{-48} r^2 \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \right. \right. \\
& \quad \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - \\
& \quad \quad 5.93032 \times 10^{34} r^4 t^4 - 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \Big) - \\
& 1.10686 \times 10^{-97} r^2 \left( 1.71243 \times 10^{49} - \frac{8.53229 \times 10^{14} r^4}{t^4} + \frac{2.6286 \times 10^{31} r^2}{t^2} + \right. \\
& \quad \frac{1}{t^4} 8.53229 \times 10^{14} \sqrt{(1. r^8 - 6.16153 \times 10^{16} r^6 t^2 - 5.93032 \times 10^{34} r^4 t^4 - \\
& \quad \quad 4.25203 \times 10^{51} r^2 t^6 + 1.83793 \times 10^{68} t^8)} \Big)^2 \Big) \Big) \Big) \\
& \left. \right)
\end{aligned}$$

$$\text{Plot3D} \left[ \left( 4.1807617710132735 \cdot 10^{-48} r^2 \left( \frac{3.412914925039692 \cdot 10^{15} r^4}{t^5} - \right. \right. \right)$$

$$\begin{aligned}
& \frac{5.257194282992301 \cdot r^2}{t^3} + \left( 4.266143656299615 \cdot r^{14} \right. \\
& \quad \left( -1.23230596682539 \cdot r^6 t - 2.3721297250827947 \cdot r^4 t^3 - \right. \\
& \quad \left. 2.551217714548337 \cdot r^2 t^5 + 1.4703410684177891 \cdot t^7 \right) / \\
& \quad \left( t^4 \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} - \right. \\
& \quad \left. \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \right. \right. \\
& \quad \left. \left. 5.930324312706987 \cdot r^4 t^4 - 4.252029524247228 \cdot r^2 t^6 + \right. \right. \\
& \quad \left. \left. 1.8379263355222364 \cdot t^8 \right)} \right) - \\
& 2.2137119528363295 \cdot r^2 \left( \frac{3.412914925039692 \cdot r^4}{t^5} - \right. \\
& \quad \frac{5.257194282992301 \cdot r^2}{t^3} + \left( 4.266143656299615 \cdot r^{14} \right. \\
& \quad \left( -1.23230596682539 \cdot r^6 t - 2.3721297250827947 \cdot r^4 t^3 - \right. \\
& \quad \left. 2.551217714548337 \cdot r^2 t^5 + 1.4703410684177891 \cdot t^7 \right) / \\
& \quad \left( t^4 \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} - \right. \\
& \quad \left. \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \right. \right. \\
& \quad \left. \left. 5.930324312706987 \cdot r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \right) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^4}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \right) / \\
& \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot r^2 \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^4}{t^4} + \\
& \quad \frac{2.6285971414961507 \cdot r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \left. \left. \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \Big) - \\
 & 1.1068559764181647 \cdot r^2 \left( 1.7124327770294835 \cdot r^4 - \right. \\
 & \quad \frac{8.53228731259923 \cdot r^4}{t^4} + \frac{2.6285971414961507 \cdot r^2}{t^2} + \\
 & \quad \frac{1}{t^4} 8.53228731259923 \cdot \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \\
 & \quad 5.930324312706987 \cdot r^4 t^4 - 4.252029524247228 \cdot r^2 t^6 + \\
 & \quad 1.8379263355222364 \cdot t^8)}^2 \Big) \Big), \{r, -1, 1\}, \{t, -\pi, \pi\} \Big]
 \end{aligned}$$

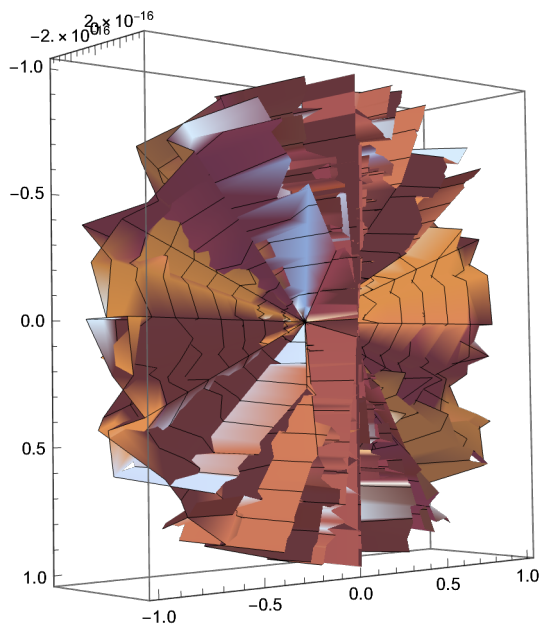


$$\begin{aligned}
 & \text{RevolutionPlot3D} \Big[ \left( 4.1807617710132735 \cdot r^2 \left( \frac{3.412914925039692 \cdot r^4}{t^5} - \right. \right. \\
 & \quad \frac{5.257194282992301 \cdot r^2}{t^3} + (4.266143656299615 \cdot r^{14} \\
 & \quad (-1.23230596682539 \cdot r^6 t - 2.3721297250827947 \cdot r^4 t^3 - \\
 & \quad 2.551217714548337 \cdot r^2 t^5 + 1.4703410684177891 \cdot t^7) \Big) / \\
 & \quad (t^4 \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \\
 & \quad 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8)} \Big) -
 \end{aligned}$$

$$\begin{aligned}
& \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} t^8)} - \\
& 2.2137119528363295 \cdot r^{-97} r^2 \left( \frac{3.412914925039692 \cdot r^{15}}{t^5} - \frac{5.257194282992301 \cdot r^{31}}{t^3} + (4.266143656299615 \cdot r^{14} \right. \\
& \quad \left. (-1.23230596682539 \cdot r^{17} t - 2.3721297250827947 \cdot r^{35} t^3 - 2.551217714548337 \cdot r^{52} t^5 + 1.4703410684177891 \cdot r^{69} t^7) \right) / \\
& \quad (t^4 \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} t^8)}) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} t^8)}) \Bigg) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \right. \\
& \quad \left. \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \right) \Bigg) / \\
& \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot r^{-48} r^2 \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \right. \right. \right. \\
& \quad \left. \left. \sqrt{(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} t^8)} \right) \right) - \\
& \quad 1.1068559764181647 \cdot r^{-97} r^2 \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \right.
\end{aligned}$$



$$\frac{1}{t^4} 8.53228731259923 \cdot 10^{14} \sqrt{\left(1. \cdot r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8\right)^2}\right), \{r, -1, 1\}, \{t, -\pi, \pi\}]$$



$$\text{Solve}\left[\theta == \frac{1}{-8.987551787368176 \cdot v^{16} + v^2}\right. \\ \left.0.5 \cdot \left(-1.1294090667581471 \cdot v^{18} + 12.566370614359172 \cdot v^2 + \sqrt{\left((1.1294090667581471 \cdot v^{18} - 12.566370614359172 \cdot v^2)^2 - 4 \cdot \right.}\right. \right. \\ \left. \left. \left(-8.987551787368176 \cdot v^{16} + v^2\right) \left(-3.5481432270250993 \cdot v^{18} + 39.47841760435743 \cdot v^2\right) \sin[\beta]^2\right)\right], t]$$

$$\left\{\left\{t \rightarrow -0.5 \sqrt{\left(-\frac{2 \cdot r^2 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2} - \right.}\right. \right. \\ \left. 2 \cdot \sqrt{\left(\frac{r^4 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)^2}{\left(2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2\right)^2} - \right.}\right. \\ \left. \left. \frac{4 \cdot r^4 \left(2.43561 \times 10^{15} + 8.53229 \times 10^{14} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2}\right)\right\}},$$

$$\left\{t \rightarrow 0.5 \sqrt{\left(-\frac{2 \cdot r^2 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2} - \right.}\right. \\ \left. 2 \cdot \sqrt{\left(\frac{r^4 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)^2}{\left(2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2\right)^2} - \right.}\right. \\ \left. \left. \frac{4 \cdot r^4 \left(2.43561 \times 10^{15} + 8.53229 \times 10^{14} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2}\right)\right\}},$$

$$\left\{t \rightarrow -0.5 \sqrt{\left(-\frac{2 \cdot r^2 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2} + \right.}\right. \\ \left. 2 \cdot \sqrt{\left(\frac{r^4 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)^2}{\left(2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2\right)^2} - \right.}\right. \\ \left. \left. \frac{4 \cdot r^4 \left(2.43561 \times 10^{15} + 8.53229 \times 10^{14} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2}\right)\right\}},$$

$$\left\{t \rightarrow 0.5 \sqrt{\left(-\frac{2 \cdot r^2 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2} + \right.}\right. \\ \left. 2 \cdot \sqrt{\left(\frac{r^4 \left(6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta\right)^2}{\left(2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2\right)^2} - \right.}\right. \\ \left. \left. \frac{4 \cdot r^4 \left(2.43561 \times 10^{15} + 8.53229 \times 10^{14} \theta\right)}{2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2}\right)\right\}}$$

$$\begin{aligned}
t &:= 0.5 \sqrt{\left( -\left( 2. \cdot r^2 \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right) / \right. \\
&\quad \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + \right. \\
&\quad \left. 1.50288049195799 \cdot \theta^2 \right) + \\
&\quad \left. 2. \cdot \sqrt{\left( \left( r^4 \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right)^2 / \right. \right. \\
&\quad \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + \right. \\
&\quad \left. 1.50288049195799 \cdot \theta^2 \right)^2 - \\
&\quad \left( 4. \cdot r^4 \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right) \right) / \\
&\quad \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + \right. \\
&\quad \left. 1.50288049195799 \cdot \theta^2 \right) \Big) \Big) \\
r &:= \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
&\quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right) \\
x &:= \frac{2 \pi r - r \theta}{2 \pi} \\
\theta &:= 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \\
m &:= \\
&\quad \left( 7.372495999759142 \cdot \theta^{-51} \left( 1.6880179234807384 \cdot \theta^{10} \sqrt{(-3.5294033336192096 \cdot \theta^{16} + \right. \right. \\
&\quad \left. 2.808609933552555 \cdot \theta^{15} \theta^2 + 1.1087947584453435 \cdot \theta^{17} \sin[\beta]^2) - \right. \\
&\quad \left. 4.029845948245144 \cdot \theta^9 \theta^2 \sqrt{(-3.5294033336192096 \cdot \theta^{16} + \right. \\
&\quad \left. 2.808609933552555 \cdot \theta^{15} \theta^2 + 1.1087947584453435 \cdot \theta^{17} \sin[\beta]^2) + \right. \\
&\quad \left. 2.1378996752068695 \cdot \theta^8 \theta^3 \sqrt{(-3.5294033336192096 \cdot \theta^{16} + \right. \\
&\quad \left. 2.808609933552555 \cdot \theta^{15} \theta^2 + 1.1087947584453435 \cdot \theta^{17} \sin[\beta]^2) \Big) \Big) / \\
&\quad \left( -12.566370614359172 \cdot \theta \sqrt{(-4.487190804107819 \cdot \theta^{15} + \right. \\
&\quad \left. 3.57079298535128 \cdot \theta^{14} \theta^2 + 1.40969256654408 \cdot \theta^{16} \sin[\beta]^2) + \right. \\
&\quad \left. 1. \cdot \theta^2 \sqrt{(-4.487190804107819 \cdot \theta^{15} + 3.57079298535128 \cdot \theta^{14} \theta^2 + \right. \\
&\quad \left. 1.40969256654408 \cdot \theta^{16} \sin[\beta]^2) + \right. \\
&\quad \left. 6.283185307179586 \cdot \sqrt{12.566370614359172 \cdot \theta - 1. \cdot \theta^2 \sin[\beta]} \right. \\
&\quad \left. \sqrt{(-4.487190804107819 \cdot \theta^{15} + \right. \\
&\quad \left. 3.57079298535128 \cdot \theta^{14} \theta^2 + 1.40969256654408 \cdot \theta^{16} \sin[\beta]^2) \Big) \Big) \\
&\text{RevolutionPlot3D} \Big[ \\
&\quad (2 \pi r - 2 \pi x) m \left( \left( \left( 4.1807617710132735 \cdot \theta^{-48} r^2 \left( \frac{3.412914925039692 \cdot \theta^{15} r^4}{t^5} - \right. \right. \right. \right.
\end{aligned}$$

$$\left( \frac{1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot t^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot t^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{(1 \cdot t^{49} r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8)} \right) \Bigg) / \left( 4 \pi \sqrt{4.1807617710132735 \cdot t^{49} r^2 \left( 1.7124327770294835 \cdot t^{49} - \frac{8.53228731259923 \cdot t^{14} r^4}{t^4} + \frac{2.6285971414961507 \cdot t^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot t^{14} \sqrt{(1 \cdot t^{49} r^8 - 6.16152983412695 \cdot t^{16} r^6 t^2 - 5.930324312706987 \cdot t^{34} r^4 t^4 - 4.252029524247228 \cdot t^{51} r^2 t^6 + 1.8379263355222364 \cdot t^{68} t^8)} \right)} \right)$$

$$\begin{aligned}
& \left( 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right) - \\
& 1.1068559764181647 \cdot r^2 \left( 1.7124327770294835 - \right. \\
& \quad \frac{8.53228731259923 \cdot r^4}{t^4} + \frac{2.6285971414961507 \cdot r^2}{t^2} + \\
& \quad \frac{1}{t^4} 8.53228731259923 \cdot \sqrt{1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 -} \\
& \quad \left. 5.930324312706987 \cdot r^4 t^4 - 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)^2 \Bigg) - \\
& \left( \left( \sqrt{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 +} \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin[\beta]^2 \right) \right) / \\
& \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \Bigg), \\
& \{\beta, -\pi, \pi\}, \{\theta, -2 \\
& \quad \pi, \\
& \quad 2 \\
& \quad \pi\} \Big] \\
& (2 \pi r - 2 \pi x) m (v_1 - v_2) \\
& \Delta x \Delta p = (2 \pi r - 2 \pi x) m (v_1 - v_2) = \\
& (2 \pi r - 2 \pi x) m \left( \left( \left( 4.1807617710132735 \cdot r^2 \left( \frac{3.412914925039692 \cdot r^4}{t^5} - \right. \right. \right. \right. \\
& \quad \frac{5.257194282992301 \cdot r^2}{t^3} + (4.266143656299615 \cdot \\
& \quad (-1.23230596682539 \cdot r^6 t - 2.3721297250827947 \cdot r^4 t^3 - \\
& \quad 2.551217714548337 \cdot r^2 t^5 + 1.4703410684177891 \cdot t^7) \Big) / \\
& \quad (t^4 \sqrt{1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 -} \\
& \quad \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot \sqrt{1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 -} \\
& \quad \left. 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right) \right) - \\
& 2.2137119528363295 \cdot r^2 \left( \frac{3.412914925039692 \cdot r^4}{t^5} - \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{5.257194282992301 \cdot r^2}{t^3} + \left( 4.266143656299615 \cdot r^{14} \right. \\
& \quad \left( -1.23230596682539 \cdot r^6 t - 2.3721297250827947 \cdot r^4 t^3 - \right. \\
& \quad \left. 2.551217714548337 \cdot r^2 t^5 + 1.4703410684177891 \cdot t^7 \right) / \\
& \quad \left( t^4 \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \right) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \right. \\
& \quad \left. r^4 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \Bigg) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \Bigg) / \\
& \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot r^{48} \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \\
& \quad \frac{2.6285971414961507 \cdot r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - 5.930324312706987 \cdot r^4 t^4 - \right. \\
& \quad \left. 4.252029524247228 \cdot r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)} \Bigg) - \\
& \quad 1.1068559764181647 \cdot r^{97} \left( 1.7124327770294835 \cdot r^{49} - \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^2}{t^2} + \\
& \quad \frac{1}{t^4} 8.53228731259923 \cdot \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^6 t^2 - \right. \\
& \quad \left. 5.930324312706987 \cdot r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \\
& \quad \left. \left. \left. \left. r^2 t^6 + 1.8379263355222364 \cdot t^8 \right)^2 \right) \right) \right) \Bigg) - \\
& \left( \left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) / \\
& \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \Bigg) \\
& \text{RevolutionPlot3D} \Bigg[ \\
& \left( 7.372495999759142 \theta^{-51} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) \right. \\
& \quad \left( 1.6880179234807384 \theta^{10} \sqrt{-3.5294033336192096 \theta^{16} + \right. \\
& \quad \quad 2.808609933552555 \theta^{15} \theta^2 + 1.1087947584453435 \sin[\beta]^{17}} - \\
& \quad 4.029845948245144 \theta^9 \theta^2 \sqrt{-3.5294033336192096 \theta^{16} + \\
& \quad \quad 2.808609933552555 \theta^{15} \theta^2 + 1.1087947584453435 \sin[\beta]^{17}} + \\
& \quad 2.1378996752068695 \theta^8 \theta^3 \sqrt{-3.5294033336192096 \theta^{16} + \\
& \quad \quad 2.808609933552555 \theta^{15} \theta^2 + 1.1087947584453435 \sin[\beta]^{17}} \Bigg) \\
& \left( - \left( \sqrt{-1.1294090667581471 \theta^{18} + 8.987551787368176 \theta^{16} \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^{18}} \right) / \right. \\
& \quad \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) + \\
& \quad \left( \left( 4.1807617710132735 \theta^{-48} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \right. \\
& \quad \left( \left( 1.0921327760127014 \theta^{17} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - \right. \\
& \quad \left. 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \left( - \left( 2. (6.646791914659577 \theta^{32} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 2.6285971414961507 \cdot \theta^{31} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2 \theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta \right)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right)^2 (16\pi^2 \theta - \\
& \quad 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \Bigg) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \quad \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2 \theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg) -
\end{aligned}$$



$$\begin{aligned}
& \left( 4.205755426393841 \cdot \theta^{32} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \quad 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \theta^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right)^2 (16\pi^2\theta - \\
& \quad 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^4 - \\
& \quad \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right.
\end{aligned}$$

$$\begin{aligned}
& \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right)^{3/2} \Bigg) + \\
& \left( 6.825829850079384 \cdot 10^{15} \left( - \left( 6.16152983412695 \cdot 10^{16} \left( -4\pi\theta + \right. \right. \right. \right. \\
& \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^6 \\
& \sqrt{\left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \right. \\
& \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + 2 \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \\
& \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \left( 4. \cdot \right. \\
& \quad \left( 2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 2.9651621563534934 \cdot 10^{34} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right. \\
& \quad \left. - \left( 2. \cdot \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big) + 2. \\
& \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \\
& \quad \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} \theta + \\
& \quad 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) - \left( 4. \right. \\
& \quad (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \\
& \quad \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} \theta + \\
& \quad 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) \Big)^{3/2} / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 7.972555357963553 \cdot \theta^{50} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \cdot^{32} - 2.6285971414961507 \cdot \cdot^{31} \theta) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \cdot^{49} - 1.7124327770294835 \cdot \cdot^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \cdot^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + 2. \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \cdot^{32} - 2.6285971414961507 \cdot \cdot^{31} \right. \right. \\
& \quad \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \cdot^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \cdot^{49} \theta + \\
& \quad 1.50288049195799 \cdot \cdot^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \left( 4. \cdot \right. \\
& \quad (2.435611652890208 \cdot \cdot^{15} + 8.53228731259923 \cdot \cdot^{14} \\
& \quad \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big)^{5/2} \Big) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 1.1487039597013978 \cdot \theta^{67} \\
& \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta} \right)^2 \right) \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Big) + 2 \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
& \quad \theta)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \theta + 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \right. \\
& \quad \left. \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) - \left( 4 \cdot \right. \\
& \quad \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \quad \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + \right.
\end{aligned}$$



$$\begin{aligned}
& \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right)^2 \Bigg) \\
& \sqrt{\left( \left( 1 \cdot \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^8 \right) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^8 - \\
& \left( 1.5403824585317376 \cdot 10^{16} \left( -4\pi\theta + \theta^2 + \right. \right. \\
& 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^6 \right. \\
& \left. \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}) \theta \right) \right. \right. \\
& \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + 2 \cdot
\end{aligned}$$



$$\begin{aligned}
& \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \right. \right. \\
& \quad \left. \left. \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \right. \\
& \quad \left. \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 3.706452695441867 \cdot 10^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right) \theta \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - \right. \\
& \quad \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
2. & \sqrt{\left( (6.646791914659577 \cdot 10^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
4. & \sqrt{(2.435611652890208 \cdot 10^{15} + \\
& \quad 8.53228731259923 \cdot 10^{14} \theta) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right.
\end{aligned}$$



$$\begin{aligned}
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14}) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \quad \left. 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Big)^3 \Big) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + \\
& \quad 7.179399748133736 \cdot \theta^{65} \\
& \quad \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \quad \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Big) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \quad \left. \theta + 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + 2. \cdot \\
& \quad \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
& \quad \quad \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2 \right)^4 \Bigg) - \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \quad \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg) - \\
& \left( 1.0921327760127014 \cdot 10^{17} \sqrt{\left( \left( 1. \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) \right) \Bigg/ \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^8 - \\
& \quad \left( 1.5403824585317376 \cdot 10^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left. \left( - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + 2 \cdot \\
& \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \\
& \quad \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2 \\
& \quad \left. \theta\sin[\beta]^2)^4 \right) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 3.706452695441867 \cdot \theta^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{\theta} \right)^4 \\
& \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{\theta} \right)^2 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \left( 16 \pi^2 \theta - \right. \right. \\
& \quad \left. \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \theta^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta \sin[\beta]} + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta \sin[\beta]^3}}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \\
& \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. \left. 8.53228731259923 \cdot \theta^{14} \theta \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49}\theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48}\theta^2 \right) \left( 16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 \Bigg) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot 10^{49} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2. \cdot \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}\theta \right) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48}\theta^2 \right) \left( 16\pi^2\theta - \right. \\
& \quad \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 \Bigg) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31}\theta \right)^2 \right.}
\end{aligned}$$



$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
& \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14}) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48}) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg)^3 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2. \cdot \\
& \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \theta^2 \right) \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2 \right)^4 \Bigg) - \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg) \Bigg/ \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \theta \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 -
\end{aligned}$$

$$\left( 2.2137119528363295 \cdot \theta^{-97} \right.$$

$$\left( -4\pi\theta + \theta^2 + \frac{2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}}{\theta} \right)^2$$

$$\left( \left( 1.0921327760127014 \cdot \theta^{17} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + \frac{4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}}{\theta} \right)^4 \right) \right) /$$

$$\left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right.$$

$$\left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right.$$

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta] + \frac{4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}}{\theta} \right)^2 \bigg) /$$

$$\left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{48} \right.$$

$$\left. \theta + 1.50288049195799 \cdot \theta^2 \right) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 +$$

$$2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right)^2}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 (16\pi^2\theta - \\
& \quad 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg) - \\
& \left( 4.205755426393841 \cdot 10^{32} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right. \\
& \quad \left. - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
2. & \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16\pi^2\theta - \right. \\
& \quad \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^{3/2} +
\end{aligned}$$

$$\begin{aligned}
& \left( 6.825829850079384 \cdot 10^{15} \left( - \left( 6.16152983412695 \cdot 10^{16} \left( -4\pi\theta + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^6 \right. \right. \\
& \quad \left. \left. \sqrt{\left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \right) / \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2 \theta - 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2)^2 \right) + 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \\
& \quad \left. \left. \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \right) / \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16\pi^2 \theta - 12\pi \theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) - \left( 4 \cdot \right. \\
& \quad \left. (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Big)^4 \Big) / \\
& \Big( (2.652268423469232 \cdot 10^{49} - \\
& 1.7124327770294835 \cdot 10^{49} \theta + \\
& 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) \Big) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^6 - \\
& \Big( 2.9651621563534934 \cdot 10^{34} \Big( -4 \pi \theta + \theta^2 + 2 \pi \\
& \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Big)^4 \\
& \Big( -2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \\
& \Big( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \\
& 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Big)^2 \Big) \Big) / \\
& \Big( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \\
& \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \sin[\beta]^2)^2 \Big) + 2 \cdot \sqrt{\Big( (6.646791914659577 \cdot 10^{32} - \\
& 2.6285971414961507 \cdot 10^{31} \theta)^2 \\
& \Big( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \\
& 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} -
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) - \left( 4 \cdot \right. \\
& \quad (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \\
& \quad \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg)^{3/2} \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 7.972555357963553 \cdot 10^{50} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2 \right)^2 + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \left( 4 \cdot \right. \\
& \quad \left. (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + \\
& 1.1487039597013978 \cdot 10^{67}
\end{aligned}$$

$$\begin{aligned}
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \pi^{32} - 2.6285971414961507 \cdot \pi^{31} \theta) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + 2. \cdot \\
& \sqrt{\left( (6.646791914659577 \cdot \pi^{32} - 2.6285971414961507 \cdot \pi^{31} \right. \\
& \quad \theta)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \right. \\
& \quad \left. \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \left( 4. \cdot \right. \\
& \quad (2.435611652890208 \cdot \pi^{15} + 8.53228731259923 \cdot \pi^{14} \\
& \quad \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( \left( 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \right)^{7/2} \Bigg) / \\
& \left( \left( \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \quad \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \theta^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \quad \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - \right. \right. \\
& \quad \left. \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \\
& \quad \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \right. \\
& \quad \left. \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg)^2 \\
& \sqrt{\left( \left( 1. \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) / \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^8 - \\
& \quad \left( 1.5403824585317376 \cdot \theta^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right) \\
& \quad \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2. \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 \Bigg) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^6 - \\
& \left( 3.706452695441867 \cdot 10^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \quad \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - \\
& \quad 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big)^2 + \\
& 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big)^2 \Big) \Big) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 6.643796131636294 \cdot 10^{49} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{\sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 -}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) (16\pi^2 \theta - \\
& \quad 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \Big) + \\
& 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31}) \theta^2 \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 (16\pi^2 \theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \Big) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right.
\end{aligned}$$



$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48} \theta^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \left. \right)^3 \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2 \right)^2 \Bigg) + 2. \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta \right)^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg) - \\
& \left( 1.0921327760127014 \cdot 10^{17} \sqrt{\left( \left( 1 \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \right. \right. \right. \\
& \quad \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) / } \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^8 - \right. \\
& \quad \left( 1.5403824585317376 \cdot 10^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left. \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \quad \sin[\beta]^2)^2 + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot \theta^{31} \theta) \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 - \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^6 - \\
& \left( 3.706452695441867 \cdot \theta^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{\sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 -}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2 \theta - \right. \\
& \quad \left. 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta^2 \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2 \theta - 12\pi \theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \quad \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big)^2 / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot \theta^{49} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - \right. \right. \\
& \quad \left. \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) \Big) \Big) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \theta + 1.50288049195799 \cdot \theta^{48} \right) \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \left. \sin[\beta]^2 \right)^2 + 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right)^2 \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right)^2 \right. \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \left. \theta \sin[\beta]^2 \right)^4 - \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right)^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) / \\
& \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{48} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{48} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right)^2 \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{48} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Big)^{5/2} \Big) \\
& \left( 1.7124327770294835 \cdot \theta^{49} - \left( 1.3651659700158768 \cdot \theta^{16} \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$



$$\begin{aligned}
 & \left( \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
 & \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right. \\
 & \left. - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
 & \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
 & \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
 & \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
 & \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
 & \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
 & 2. \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \\
 & \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
 & \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
 & \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
 & \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16 \pi^2 \theta - \right. \\
 & \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \\
 & \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
 & \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
 & \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg)^2 \Bigg) + \\
& \left( 1.0514388565984603 \cdot 10^{32} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \\
& \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \theta \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg) \Bigg) + \\
& \left( 1.3651659700158768 \cdot \theta^{16} \sqrt{\left( \left( 1 \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) / \right. \right. \\
& \quad \left. \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^8 - \right. \right. \\
& \quad \left( 1.5403824585317376 \cdot \theta^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left. \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta \right) \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Bigg)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \quad \sin[\beta]^2)^2 + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Bigg)^4 \Bigg) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 - \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Bigg)^4 \Bigg) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^6 -
\end{aligned}$$

$$\begin{aligned}
& \left( 3.706452695441867 \cdot \pi^{33} \left( -4\pi\theta + \theta^2 + 2\pi \right. \right. \\
& \quad \left. \frac{\sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 -}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \pi^{32} - 2.6285971414961507 \cdot \pi^{31} \theta \right) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2) (16\pi^2 \theta - \right. \\
& \quad \left. 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \pi^{32} - \right. \right. \\
& \quad \left. 2.6285971414961507 \cdot \pi^{31} \theta \right)^2 \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \pi^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \pi^{49} \theta + \\
& \quad 1.50288049195799 \cdot \pi^{48} \theta^2)^2 (16\pi^2 \theta - 12\pi \theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \left( 4 \cdot \left( 2.435611652890208 \cdot \pi^{15} + \right. \right. \\
& \quad \left. 8.53228731259923 \cdot \pi^{14} \theta \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49}\theta + \\
& \quad 1.50288049195799 \cdot 10^{48}\theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^2 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 - \\
& \left( 6.643796131636294 \cdot 10^{49} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}\theta) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49}\theta + \right. \\
& \quad 1.50288049195799 \cdot 10^{48}\theta^2) (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \Bigg) + \\
& 2 \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}\theta)^2 \right.}
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
& \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14}) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg)^3 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \quad \sin[\beta]^2)^2 \Bigg) + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 \Bigg) - \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg/ \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta) \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
2. & \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}\theta)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14}\theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg/ \\
& \left( 4 \pi \sqrt{\left( \left( 4.1807617710132735 \cdot 10^{-48} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \right. \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \\
& \left( 1.7124327770294835 \cdot 10^{-49} - \left( 1.3651659700158768 \cdot 10^{-16} \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot 10^{-32} - 2.6285971414961507 \cdot 10^{-31} \theta \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{-49} - 1.7124327770294835 \cdot 10^{-49} \right. \right. \\
& \quad \theta + 1.50288049195799 \cdot 10^{-48} \theta^2 \Big) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2 \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot 10^{-32} - 2.6285971414961507 \cdot 10^{-31} \theta \right) \right.}
\end{aligned}$$

$$\begin{aligned}
& \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2 \\
& \quad \left. \theta\sin[\beta]^2)^4 \right) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& 8.53228731259923 \cdot 10^{14} \theta) \left( -4\pi\theta + \theta^2 + \right. \\
& 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \\
& \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right)^2 \Bigg) \Bigg)^2 + \\
& \left( 1.0514388565984603 \cdot 10^{32} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \right. \right. \\
& \quad \left. \sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg) / \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \\
& \quad \left. \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \quad \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg) \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& \left( 1.3651659700158768 \cdot 10^{16} \sqrt{\left( \left( 1 \cdot \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{\theta} \right)^8 \right) \right) / \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^8 - \\
& \quad \left( 1.5403824585317376 \cdot 10^{16} \left( -4\pi\theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2\pi\sqrt{(4\pi-\theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - \right. \\
& \quad \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 \right) + \\
& \quad 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad 8.53228731259923 \cdot \theta^{14} \theta) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 3.706452695441867 \cdot \theta^{33} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \quad \left( -2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31} \theta) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg) + \\
2. & \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \\
4. & \sqrt{\left( 2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot 10^{49} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot 10^{32} \left( 6.646791914659577 \cdot 10^{32} - \right. \right. \right. \\
& \quad \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right) \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot 10^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) -
\end{aligned}$$



$$\begin{aligned}
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14}) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^3 \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31}) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \theta + 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - \\
& \quad \quad 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Bigg) + \\
& 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31})^2 \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + 1.50288049195799 \cdot \theta^{48} \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14}) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + 1.50288049195799 \cdot \theta^{48} \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \right) \right) / \\
& \left( -2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \\
& \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) +
\end{aligned}$$

$$\begin{aligned}
& 2. \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \\
& \quad \left( 4. \left( 2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \right. \\
& \quad \left. \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Big)^2 \Big) \Big) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( 1.1068559764181647 \cdot 10^{-97} \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2
\end{aligned}$$

$$\begin{aligned}
& \left( 1.7124327770294835 \cdot \theta^{49} - \left( 1.3651659700158768 \cdot \theta^{16} \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48}\theta^2) \right. \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta \\
& \quad \sin[\beta]^2)^2) + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot \theta^{31})^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49}\theta + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2 \right)^4 - \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} + \right. \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg)^2 \Bigg) + \\
& \left( 1.0514388565984603 \cdot \theta^{32} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \\
& \quad \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right. \\
& \quad \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + 2 \cdot \\
& \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \\
& \quad \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad 8.53228731259923 \cdot 10^{14} \theta) \left( -4 \pi \theta + \theta^2 + \right. \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) \Bigg) + \\
& \left( 1.3651659700158768 \cdot 10^{16} \sqrt{\left( \left( 1 \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^8 - \\
& \left( 1.5403824585317376 \cdot 16 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \\
& \quad \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \left. \left( - \left( 2 \cdot (6.646791914659577 \cdot 32 - \right. \right. \right. \\
& \quad \left. \left. \left. 2.6285971414961507 \cdot 31 \theta \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 49 - \right. \\
& \quad 1.7124327770294835 \cdot 49 \theta + \\
& \quad \left. 1.50288049195799 \cdot 48 \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 32 - \right. \right. \right. \\
& \quad \left. \left. \left. 2.6285971414961507 \cdot 31 \theta \right)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 49 - \right. \\
& \quad \left. 1.7124327770294835 \cdot 49 \theta + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \left. \sin[\beta]^2 \right)^6 - \left( 3.706452695441867 \cdot \theta^{33} \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \right. \\
& \left. \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg) + \\
2. & \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad 8.53228731259923 \cdot \theta^{14} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \sin[\beta]^2)^4 - \left( 6.643796131636294 \cdot \theta^{49} \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \right. \\
& \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \left. - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& 1.7124327770294835 \cdot \theta^{49} + \\
& 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big) + \\
& 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \left. 1.7124327770294835 \cdot \theta^{49} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) - \\
& \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Big) \Big) \Big) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \left. \sin[\beta]^2 \right)^2 + 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Big) \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 2.6285971414961507 \cdot \theta^{31})^2 \\
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
& \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14}) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) \Bigg) \Bigg) \Bigg/ \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2)^2 \right) + 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2)^4 \right) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^2 \Bigg)^2 \Bigg) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) \Bigg) \Bigg) \Bigg) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right. \\
& \quad \left. \sin[\beta]^2) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( -12.566370614359172 \, \theta \sqrt{(-4.487190804107819 \, \theta + 3.57079298535128 \, \theta^2 + 1.40969256654408 \, \theta^3) \sin[\beta]} \right. \\
 & \left. 1. \, \theta^2 \sqrt{(-4.487190804107819 \, \theta + 3.57079298535128 \, \theta^2 + 1.40969256654408 \, \theta^3) \sin[\beta]} \right. \\
 & \left. 6.283185307179586 \, \sqrt{12.566370614359172 \, \theta - 1. \, \theta^2} \sin[\beta] \right. \\
 & \left. \sqrt{(-4.487190804107819 \, \theta + 3.57079298535128 \, \theta^2 + 1.40969256654408 \, \theta^3) \sin[\beta]} \right), \{\beta, -\pi/2, \pi/2\}
 \end{aligned}$$

Power::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

$\infty$ ::indet : Indeterminate expression 0. ComplexInfinity encountered. >>

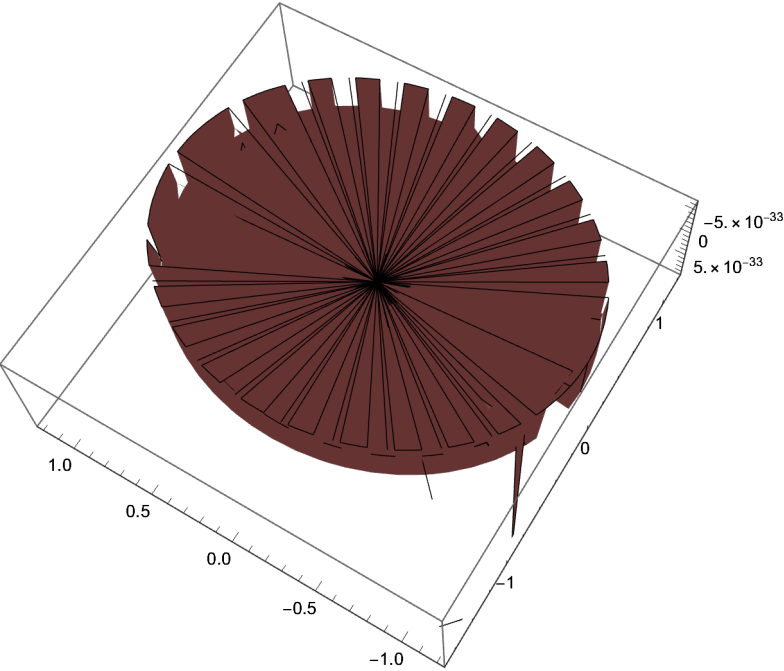
Power::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

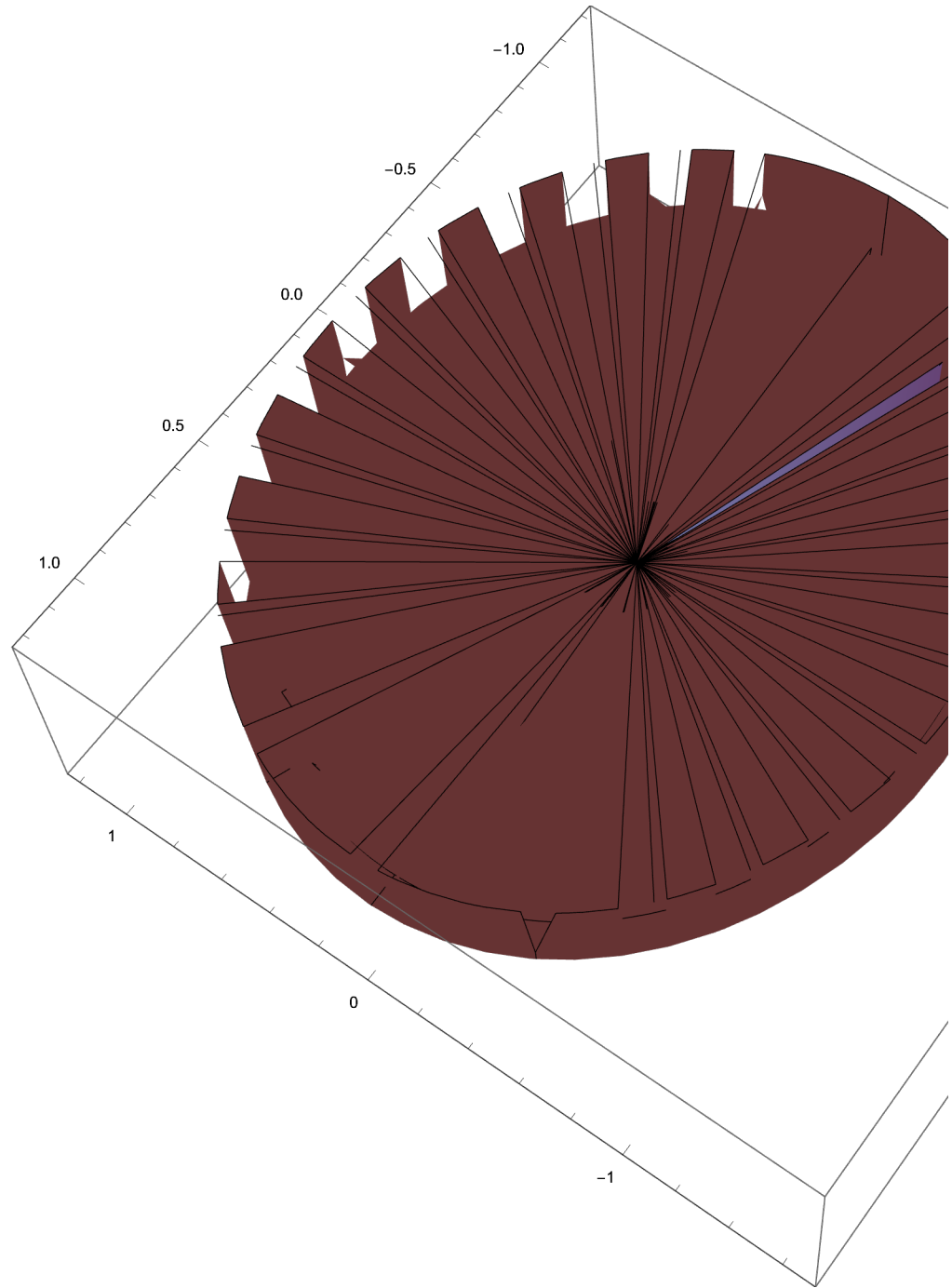
General::stop : Further output of Power::infy will be suppressed during this calculation. >>

$\infty$ ::indet : Indeterminate expression 0. ComplexInfinity encountered. >>

$\infty$ ::indet : Indeterminate expression 0. ComplexInfinity encountered. >>

General::stop : Further output of  $\infty$ ::indet will be suppressed during this calculation. >>





$$h \approx (2 \pi r - 2 \pi x) m (v_1 - v_2)$$

$$(2 \pi r - 2 \pi x) m (v_1 - v_2) \geq \hbar / 2$$

for a relatively constant mass

$$(2 \pi r - 2 \pi x) m (v_1 - v_2) = (2 \pi r - 2 \pi x) m (v_1 - v_2) \geq \hbar / 2$$



$$\begin{aligned}
 (2 \pi r - 2 \pi x) m (v_1 - v_2) = \\
 (2 \pi r - 2 \pi x) m \left( \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \right. \\
 \left. \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2) \right) \right) / \\
 \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) - v_2 \geq \hbar / 2
 \end{aligned}$$

$$\begin{aligned}
 v_1 = \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right. \\
 \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2) \right) / \\
 \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right)
 \end{aligned}$$

$$v_2 = D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, t \right]$$

$$\begin{aligned}
 (2 \pi r - 2 \pi x) m (v_1 - v_2) = \\
 (2 \pi r - 2 \pi x) m \left( \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \right. \\
 \left. \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2) \right) \right) / \\
 \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) - D \left[ \right. \\
 \left. \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, t \right] \geq \hbar / 2
 \end{aligned}$$

$$\begin{aligned}
 D \left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, t \right] = & \left( 4.1807617710132735 \cdot 10^{-48} r^2 \left( \frac{3.412914925039692 \cdot 10^{15} r^4}{t^5} - \right. \right. \\
 & \frac{5.257194282992301 \cdot 10^{31} r^2}{t^3} + (4.266143656299615 \cdot 10^{14} \\
 & (-1.23230596682539 \cdot 10^{17} r^6 t - 2.3721297250827947 \cdot 10^{35} r^4 t^3 - \\
 & 2.551217714548337 \cdot 10^{52} r^2 t^5 + 1.4703410684177891 \cdot 10^{69} t^7) \Big) / \\
 & (t^4 \sqrt{(1 \cdot 10^{18} r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - \\
 & 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)}) - \\
 & \frac{1}{t^5} 3.412914925039692 \cdot 10^{15} \sqrt{(1 \cdot 10^{18} r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - \\
 & 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + \\
 & 1.8379263355222364 \cdot 10^{68} t^8)}) \Big) - \\
 & 2.2137119528363295 \cdot 10^{-97} r^2 \left( \frac{3.412914925039692 \cdot 10^{15} r^4}{t^5} - \right. \\
 & \left. \frac{5.257194282992301 \cdot 10^{31} r^2}{t^3} + (4.266143656299615 \cdot 10^{14} \right.
 \end{aligned}$$

$$\beta := \text{ArcSin} \left[ \frac{\sqrt{(4\pi - \theta)\theta}}{2\pi} \right]$$
$$\text{SphericalPlot3D}\left[\frac{(2 \pi r - 2 \pi x) m}{\left(\sqrt{-1.1294090667581471} \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \dots\right)}\right]$$

$$\begin{aligned}
& \left( 3.5481432270250993 \cdot \sin^2[\beta] \right) / \\
& \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) - \\
& \left( \left( 4.1807617710132735 \cdot r^{-48} r^2 \left( \frac{3.412914925039692 \cdot r^{15}}{t^5} - \right. \right. \right. \\
& \quad \frac{5.257194282992301 \cdot r^{31}}{t^3} + \left( 4.266143656299615 \cdot r^{14} \right. \\
& \quad \left. \left. \left( -1.23230596682539 \cdot r^{17} r^6 t - 2.3721297250827947 \cdot r^{35} r^4 t^3 - \right. \right. \right. \\
& \quad \left. \left. \left. 2.551217714548337 \cdot r^{52} r^2 t^5 + 1.4703410684177891 \cdot r^{69} t^7 \right) \right) / \right. \\
& \quad \left( t^4 \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right)} \right) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 \right. \\
& \quad \left. t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \\
& \quad \left. \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right)} \right) - \\
& 2.2137119528363295 \cdot r^{-97} r^2 \left( \frac{3.412914925039692 \cdot r^{15}}{t^5} - \right. \\
& \quad \frac{5.257194282992301 \cdot r^{31}}{t^3} + \left( 4.266143656299615 \cdot r^{14} \right. \\
& \quad \left. \left( -1.23230596682539 \cdot r^{17} r^6 t - 2.3721297250827947 \cdot r^{35} r^4 t^3 - \right. \right. \\
& \quad \left. \left. 2.551217714548337 \cdot r^{52} r^2 t^5 + 1.4703410684177891 \cdot r^{69} t^7 \right) \right) / \\
& \quad \left( t^4 \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right)} \right) - \\
& \quad \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 \right. \\
& \quad \left. t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \\
& \quad \left. \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right)} \right) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \left. \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 \right. \right. \\
& \quad \left. \left. t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right)} \right) / \\
& \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot r^{-48} r^2 \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \\
& \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{\left(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - \right. \\
& \quad \left. 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^6 + \right. \\
& \quad \left. 1.8379263355222364 \cdot r^{68} t^8\right) - 1.1068559764181647 \cdot r^{-97}} \\
& r^2 \left(1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\
& \quad \left. \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \right. \\
& \quad \left. \sqrt{\left(1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 \right. \right. \\
& \quad \left. \left. t^6 - 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} \right. \right. \\
& \quad \left. \left. t^8\right)^2\right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}
\end{aligned}$$

Power::infy : Infinite expression  $\frac{1}{0.2}$  encountered. >>

∞::indet : Indeterminate expression 0. ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

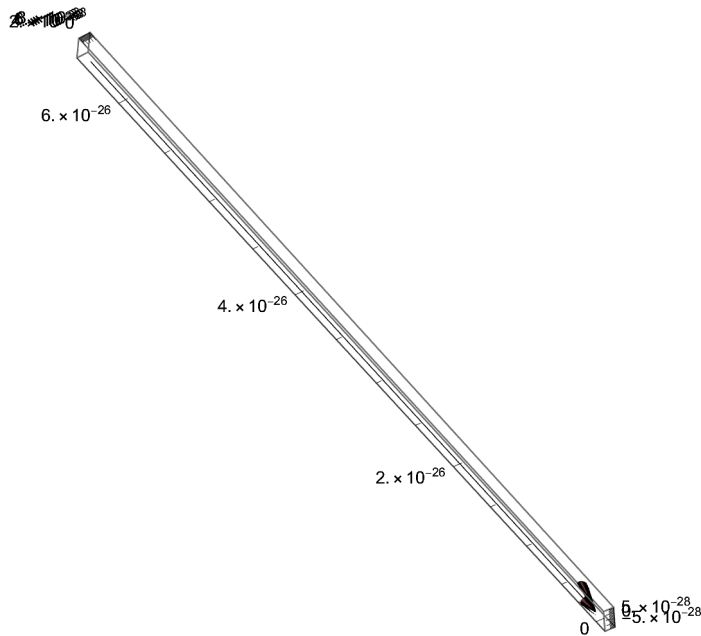
∞::indet : Indeterminate expression 0. ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.2}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

∞::indet : Indeterminate expression 0. ComplexInfinity encountered. >>

General::stop : Further output of ∞::indet will be suppressed during this calculation. >>

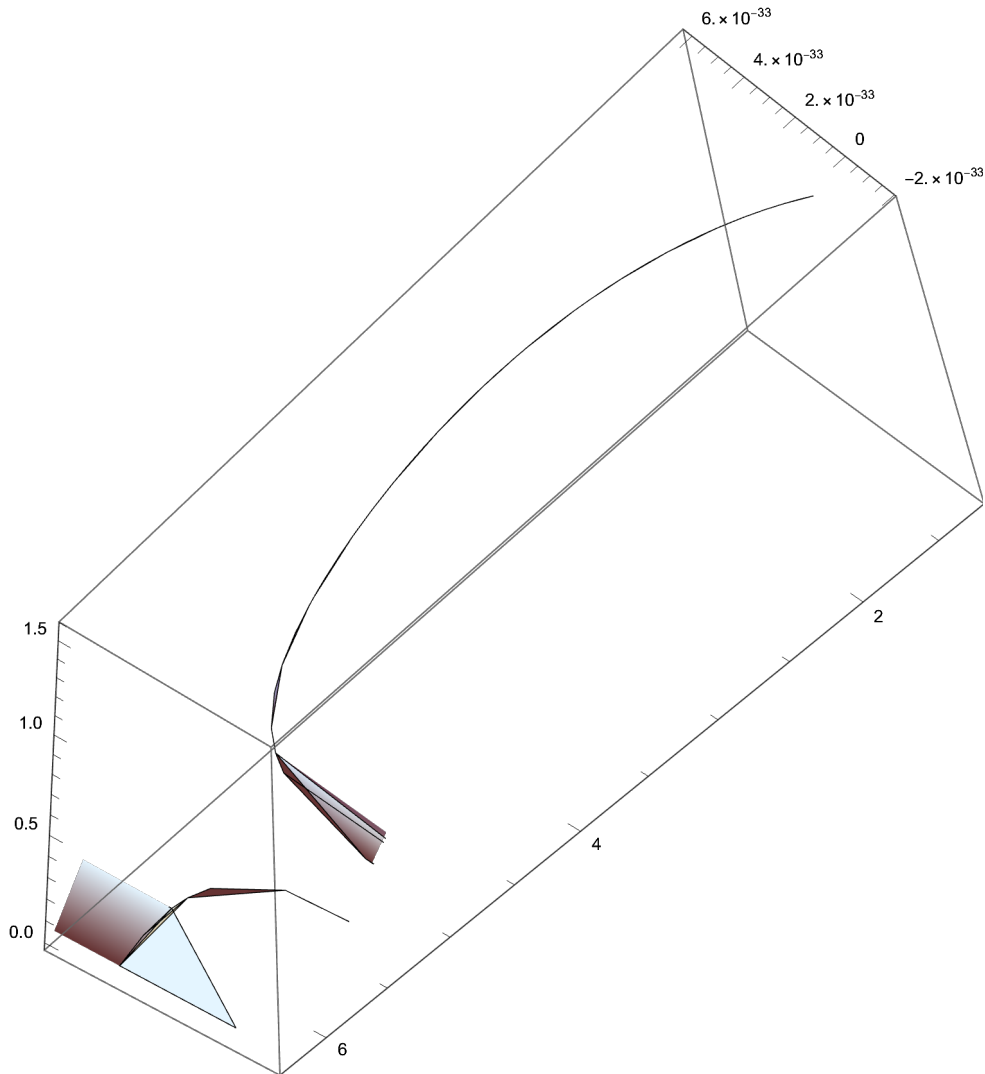


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RevolutionPlot3D[
(2 π r - 2 π x) m  $\left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) /$ 
 $\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) -$ 
 $\left( \left( 4.1807617710132735 \cdot 10^{-48} r^2 \left( \frac{3.412914925039692 \cdot 10^{15} r^4}{t^5} - \frac{5.257194282992301 \cdot 10^{31} r^2}{t^3} + (4.266143656299615 \cdot 10^{14} \right. \right.$ 
 $\left. \left. (-1.23230596682539 \cdot 10^{17} r^6 t - 2.3721297250827947 \cdot 10^{35} r^4 t^3 - 2.551217714548337 \cdot 10^{52} r^2 t^5 + 1.4703410684177891 \cdot 10^{69} t^7) \right) / \right.$ 
 $\left. (t^4 \sqrt{(1. \cdot 10^{18} r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)} \right) -$ 
 $\frac{1}{t^5} 3.412914925039692 \cdot 10^{15} \sqrt{(1. \cdot 10^{18} r^8 - 6.16152983412695 \cdot 10^{16} r^6 t^2 - 5.930324312706987 \cdot 10^{34} r^4 t^4 - 4.252029524247228 \cdot 10^{51} r^2 t^6 + 1.8379263355222364 \cdot 10^{68} t^8)} \right) -$ 
 $2.2137119528363295 \cdot 10^{-97} r^2 \left( \frac{3.412914925039692 \cdot 10^{15} r^4}{t^5} - \frac{5.257194282992301 \cdot 10^{31} r^2}{t^3} + (4.266143656299615 \cdot 10^{14} \right.$ 

```

$$\begin{aligned} & \left( -1.23230596682539 \cdot r^{17} t^6 - 2.3721297250827947 \cdot r^{35} t^4 t^3 - \right. \\ & \quad \left. 2.551217714548337 \cdot r^{52} t^2 t^5 + 1.4703410684177891 \cdot r^{69} t^7 \right) / \\ & \left( t^4 \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^6 - 5.930324312706987 \cdot r^{34} t^4 - \right. \right. \\ & \quad \left. \left. 4.252029524247228 \cdot r^{51} t^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) - \right. \\ & \quad \left. \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^6 \right. \right. \\ & \quad \left. \left. t^2 - 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} \right. \right. \\ & \quad \left. \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) \Bigg) \\ & \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \\ & \quad \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\ & \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^6 - 5.930324312706987 \cdot r^{34} t^4 \right. \\ & \quad \left. t^4 - 4.252029524247228 \cdot r^{51} t^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \Bigg) \Bigg) / \\ & \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot r^{-48} t^2 \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \right. \\ & \quad \frac{8.53228731259923 \cdot r^{14}}{t^4} + \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \\ & \quad \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^6 - \right. \\ & \quad \left. 5.930324312706987 \cdot r^{34} t^4 - 4.252029524247228 \cdot r^{51} t^2 t^6 + \right. \\ & \quad \left. \left. 1.8379263355222364 \cdot r^{68} t^8 \right) \right) - 1.1068559764181647 \cdot r^{-97} \right. \\ & \quad \left. r^2 \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14}}{t^4} + \right. \right. \\ & \quad \frac{2.6285971414961507 \cdot r^{31}}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\ & \quad \sqrt{\left( 1 \cdot r^8 - 6.16152983412695 \cdot r^{16} t^6 - 5.930324312706987 \cdot r^{34} t^4 \right. \\ & \quad \left. t^4 - 4.252029524247228 \cdot r^{51} t^2 t^6 + 1.8379263355222364 \cdot r^{68} \right. \\ & \quad \left. \left. t^8 \right) \right)^2 \Bigg) \Bigg) \Bigg] , \{ \theta , -2 \pi , 2 \pi \} , \{ \beta , -\pi / 2 , \pi / 2 \} \Bigg] \end{aligned}$$



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RevolutionPlot3D[
(2 π r - 2 π x) m  $\left( \sqrt{(-1.1294090667581471 \cdot 10^{-18} \theta + 8.987551787368176 \cdot 10^{-16} \theta^2 + 3.5481432270250993 \cdot 10^{-18} \sin[\beta]^2)} \right) /$ 
 $\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) -$ 
 $\left( \left( 4.1807617710132735 \cdot 10^{-48} r^2 \left( \frac{3.412914925039692 \cdot 10^{-15} r^4}{t^5} - \frac{5.257194282992301 \cdot 10^{-31} r^2}{t^3} + (4.266143656299615 \cdot 10^{-14} (-1.23230596682539 \cdot 10^{-17} r^6 t - 2.3721297250827947 \cdot 10^{-35} r^4 t^3 - 2.551217714548337 \cdot 10^{-52} r^2 t^5 + 1.4703410684177891 \cdot 10^{-69} t^7)) \right) /$ 

```

$$\begin{aligned}
& \left( t^4 \sqrt{\left( 1. \cdot r^8 - 6.16152983412695 \cdot r^{16} t^2 - 5.930324312706987 \cdot r^{34} t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^{51} t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) - \\
& \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1. \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 \right. \\
& \quad \left. t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \\
& \quad \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \Bigg) - \\
& 2.2137119528363295 \cdot r^{-97} r^2 \left( \frac{3.412914925039692 \cdot r^{15} r^4}{t^5} - \right. \\
& \quad \frac{5.257194282992301 \cdot r^{31} r^2}{t^3} + \left( 4.266143656299615 \cdot r^{14} \right. \\
& \quad \left. \left( -1.23230596682539 \cdot r^{17} r^6 t - 2.3721297250827947 \cdot r^{35} r^4 t^3 - \right. \right. \\
& \quad \left. \left. 2.551217714548337 \cdot r^{52} r^2 t^5 + 1.4703410684177891 \cdot r^{69} t^7 \right) \right) / \\
& \left( t^4 \sqrt{\left( 1. \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) - \\
& \frac{1}{t^5} 3.412914925039692 \cdot r^{15} \sqrt{\left( 1. \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 \right. \\
& \quad \left. t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - 4.252029524247228 \cdot r^{51} \right. \\
& \quad \left. r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \Bigg) \\
& \left( 1.7124327770294835 \cdot r^{49} - \frac{8.53228731259923 \cdot r^{14} r^4}{t^4} + \right. \\
& \quad \frac{2.6285971414961507 \cdot r^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \left. \sqrt{\left( 1. \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 \right. \right. \\
& \quad \left. \left. t^4 - 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) \Bigg) / \\
& \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot r^{-48} r^2 \left( 1.7124327770294835 \cdot r^{49} - \right. \right. \right. \\
& \quad \frac{8.53228731259923 \cdot r^{14} r^4}{t^4} + \\
& \quad \frac{2.6285971414961507 \cdot r^{31} r^2}{t^2} + \frac{1}{t^4} 8.53228731259923 \cdot r^{14} \\
& \quad \left. \sqrt{\left( 1. \cdot r^8 - 6.16152983412695 \cdot r^{16} r^6 t^2 - 5.930324312706987 \cdot r^{34} r^4 t^4 - \right. \right. \\
& \quad \left. \left. 4.252029524247228 \cdot r^{51} r^2 t^6 + 1.8379263355222364 \cdot r^{68} t^8 \right) \right) \Bigg) - \\
& 1.1068559764181647 \cdot r^{-97} r^2 \left( 1.7124327770294835 \cdot r^{49} - \right.
\end{aligned}$$





```

SphericalPlot3D[
(2 π r - 2 π x) m  $\left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) /$ 
 $\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) -$ 
D  $\left[ \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, t \right]$ , {θ, -2 π, 2 π}, {β, -π / 2, π / 2}]

General::ivar : 0.5  $\sqrt{-\frac{2. (\ll 1 \gg) (-4 \pi \theta + \ll 7 \gg)^2}{(2.65227 \times 10^{49} - \ll 23 \gg \theta + \ll 21 \gg \ll 1 \gg) \ll 1 \gg}} + 2. \sqrt{\text{Power}[\ll 2 \gg] \ll 3 \gg - \ll 1 \gg}}$  is not a
valid variable. >>

General::ivar :  $6.02924 \times 10^{-11} - 3.48132 \times 10^{-11} i$  is not a valid variable. >>

General::ivar :  $5.95132 \times 10^{-11} - 3.80336 \times 10^{-11} i$  is not a valid variable. >>

General::stop : Further output of General::ivar will be suppressed during this calculation. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

∞::indet : Indeterminate expression  $0. \pi^2$  ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

∞::indet : Indeterminate expression  $0. \pi^2$  ComplexInfinity encountered. >>

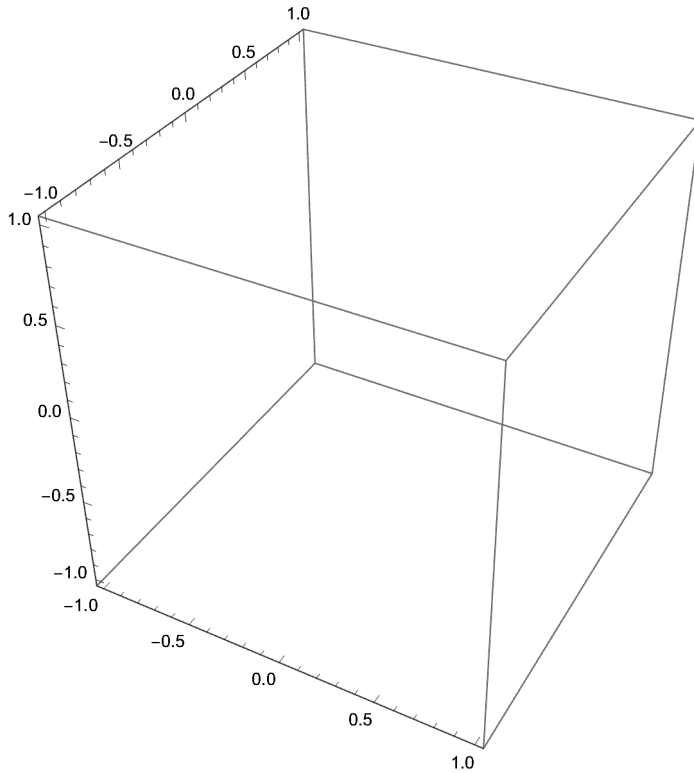
Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

∞::indet : Indeterminate expression  $0. \pi^2$  ComplexInfinity encountered. >>

General::stop : Further output of ∞::indet will be suppressed during this calculation. >>

```



```

RevolutionPlot3D[
  (2 π r - 2 π x) m ⎛ (√ (-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 θ^2 +
    3.5481432270250993`*^18 Sin[β]^2)) ⎞ /
  (√ (-12.566370614359172` θ + θ^2 + 39.47841760435743` Sin[β]^2) ) -
  D[ (√ (4 π r^2 θ - r^2 θ^2) / (2 π), t] ⎝, {θ, -2 π, 2 π} ⎞]

General::ivar : 0.5 √ (- 8.58058 × 10-18 (⟨⟨1⟩⟩)2 / (⟨⟨1⟩⟩)2 + 1.7764 × 10-17 √ (⟨⟨1⟩⟩4 / ⟨⟨1⟩⟩4) is not a valid variable. >>

General::ivar : 0.5 √ (- 8.58058 × 10-18 (⟨⟨1⟩⟩)2 / (-⟨⟨18⟩⟩ - ⟨⟨18⟩⟩ ⟨⟨1⟩⟩)2 + 1.7764 × 10-17 √ (⟨⟨1⟩⟩4 / ⟨⟨1⟩⟩4) is not a valid variable. >>

General::ivar : 0.5 √ (- 8.58058 × 10-18 (⟨⟨1⟩⟩)2 / (-⟨⟨18⟩⟩ - ⟨⟨18⟩⟩ ⟨⟨1⟩⟩)2 + 1.7764 × 10-17 √ (⟨⟨1⟩⟩4 / ⟨⟨1⟩⟩4) is not a valid variable. >>

General::stop : Further output of General::ivar will be suppressed during this calculation. >>
RevolutionPlot3D::exclul : {Im[(4 π - θ) θ] - 0, Im[(4 π - θ) θ] - 0, ⟨⟨8⟩⟩, ⟨⟨2⟩⟩} must be a list of equalities or
real-valued functions. >>

```

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

$\infty::\text{indet}$  : Indeterminate expression  $0.\pi^2 \text{ComplexInfinity Sin}[\beta]^3$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

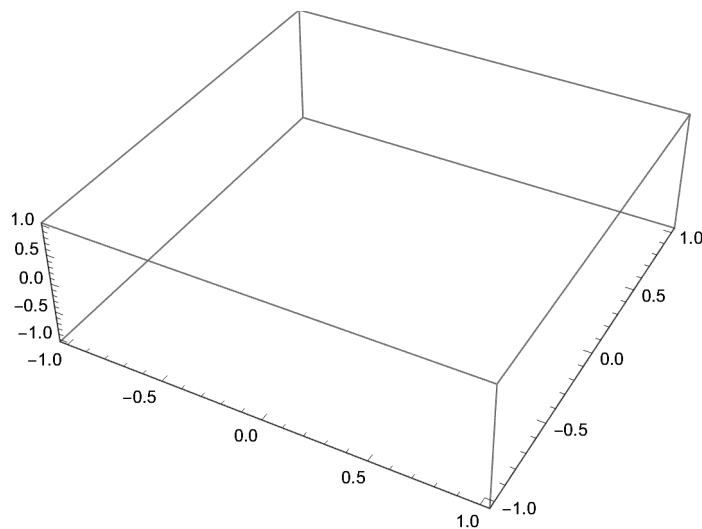
$\infty::\text{indet}$  : Indeterminate expression  $0.\pi^2 \text{ComplexInfinity Sin}[\beta]^3$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

$\infty::\text{indet}$  : Indeterminate expression  $0.\pi^2 \text{ComplexInfinity Sin}[\beta]^3$  encountered. >>

General::stop : Further output of  $\infty::\text{indet}$  will be suppressed during this calculation. >>



Plot3D $\left[ (2\pi r - 2\pi x) m \left( \left( \sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \text{Sin}[\beta]^2)} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \text{Sin}[\beta]^2} \right) - \text{D} \left[ \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi}, t \right] \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\} \right]$

General::ivar :  $0.5 \sqrt{-\frac{2.(\ll 1 \gg)(-4\pi\theta + \ll 7 \gg)^2}{(2.65227 \times 10^{49} - \ll 23 \gg \theta + \ll 21 \gg \ll 1 \gg) \ll 1 \gg}} + 2. \sqrt{\text{Power}[\ll 2 \gg] \ll 3 \gg - \ll 1 \gg}}$  is not a valid variable. >>

GeometryPlot3D $\left[ 7.3725 \times 10^{-51} \theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta) \theta} \text{Sin}[\beta] + \right. \right.$

$$\begin{aligned}
& 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Bigg) \\
& \left( 1.68802 \times 10^{10} \theta \sqrt{-3.5294 \times 10^{16} \theta + 2.80861 \times 10^{15} \theta^2 + 1.10879 \times 10^{17} \sin[\beta]^2} - \right. \\
& 4.02985 \times 10^9 \theta^2 \sqrt{-3.5294 \times 10^{16} \theta + 2.80861 \times 10^{15} \theta^2 + 1.10879 \times 10^{17} \sin[\beta]^2} + \\
& \left. 2.1379 \times 10^8 \theta^3 \sqrt{-3.5294 \times 10^{16} \theta + 2.80861 \times 10^{15} \theta^2 + 1.10879 \times 10^{17} \sin[\beta]^2} \right) \\
& \left( -\partial \sqrt{-\frac{2. (6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2}{(2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2}} + 2. \sqrt{\frac{6.64679 \times 10^{32} - 2.6286 \times 10^{31} \theta}{(2.65227 \times 10^{49} - 1.71243 \times 10^{49} \theta + 1.50288 \times 10^{48} \theta^2)}} \right) \\
& \frac{1}{2 \pi} \left( \sqrt{\left( \left( 4 \pi \theta \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \right.} \\
& \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 - \right. \\
& \left. \left( \theta^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \right. \\
& \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) \Bigg) + \\
& \left. \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right) \Bigg) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right. \\
& \left. (-12.5664 \theta \sqrt{-4.48719 \times 10^{15} \theta + 3.57079 \times 10^{14} \theta^2 + 1.40969 \times 10^{16} \sin[\beta]^2} + \right. \\
& 1. \theta^2 \sqrt{-4.48719 \times 10^{15} \theta + 3.57079 \times 10^{14} \theta^2 + 1.40969 \times 10^{16} \sin[\beta]^2} + \\
& 6.28319 \sqrt{12.5664 \theta - 1. \theta^2} \sin[\beta] \\
& \left. \left. \sqrt{-4.48719 \times 10^{15} \theta + 3.57079 \times 10^{14} \theta^2 + 1.40969 \times 10^{16} \sin[\beta]^2} \right) \right), \\
& \{\theta, -2 \pi, 2 \pi\}, \left\{ \beta, -\frac{\pi}{2}, \right. \\
& \left. \frac{\pi}{2} \right\} \Bigg]
\end{aligned}$$

RevolutionPlot3D[

$$\begin{aligned}
& \left( 7.372495999759142 \cdot \theta^{-51} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) \right. \\
& \quad \left( 1.6880179234807384 \cdot \theta^{10} \sqrt{-3.5294033336192096 \cdot \theta^{16} + \right. \\
& \quad \quad 2.808609933552555 \cdot \theta^{15} \theta^2 + 1.1087947584453435 \cdot \theta^{17} \sin[\beta]^2) - \\
& \quad 4.029845948245144 \cdot \theta^9 \theta^2 \sqrt{-3.5294033336192096 \cdot \theta^{16} + \theta^2} - \\
& \quad \quad 2.808609933552555 \cdot \theta^{15} \theta^2 + 1.1087947584453435 \cdot \theta^{17} \sin[\beta]^2) + \\
& \quad 2.1378996752068695 \cdot \theta^8 \theta^3 \sqrt{-3.5294033336192096 \cdot \theta^{16} + \theta^2} + \\
& \quad \quad \left. 2.808609933552555 \cdot \theta^{15} \theta^2 + 1.1087947584453435 \cdot \theta^{17} \sin[\beta]^2) \right) \\
& \quad \left( - \left( \sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + \right. \right. \\
& \quad \quad \left. \left. 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2) \right) \right) / \\
& \quad \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) + \\
& \quad \left( \left( 4.1807617710132735 \cdot \theta^{-48} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \right. \\
& \quad \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left( \left( 1.0921327760127014 \cdot \theta^{17} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \right. \\
& \quad \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \right) / \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - \right. \\
& \quad \left. 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \right. \right. \\
& \quad \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16 \pi^2 \theta - \right. \\
& \quad \quad \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \quad \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \quad \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg) - \\
& \left( 4.205755426393841 \cdot 10^{32} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/
\end{aligned}$$

$$\frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Big)^2 \Big) /$$

$$\left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right.$$

$$\left. - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right.$$

$$\left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right.$$

$$4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} -$$

$$\left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) /$$

$$\left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right.$$

$$\theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Big) +$$

$$2. \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \theta^2 \right.$$

$$\left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right.$$

$$4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} -$$

$$\left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) /$$

$$\left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right.$$

$$\theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) -$$

$$\left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right.$$

$$\theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right.$$

$$4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} -$$



$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg)^{3/2} + \\
& \left( 6.825829850079384 \cdot 10^{15} \left( - \left( 6.16152983412695 \cdot 10^{16} \left( -4 \pi \theta + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \right. \\
& \quad \left. \left. \sqrt{\left( - \left( 2.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2. \\
& \sqrt{\left( \left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \left( 4 \cdot \right. \\
& \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg) \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 2.9651621563534934 \cdot \theta^{34} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right. \\
& \left. \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta \right) \right. \right. \right. \\
& \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2 \cdot
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \left( 4 \cdot \right. \\
& \quad \left. \left( 2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \right. \\
& \quad \left. \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \right)^{3/2} / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 7.972555357963553 \cdot 10^{50} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right)
\end{aligned}$$

$$\left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right.$$

$$\left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\ \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\ \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) /$$

$$\left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\ \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\ \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + 2. \cdot$$

$$\sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right.$$

$$\left. \theta \right)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\ \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\ \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) /$$

$$\left( (2.652268423469232 \cdot \theta^{49} - \right. \\ \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right. \\ \left. 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2\theta - 12\pi\theta^2 + \right. \\ \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \left( 4. \cdot \right.$$

$$(2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14}$$

$$\left. \theta \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\ \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\ \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) /$$

$$\left( (2.652268423469232 \cdot \theta^{49} - \right. \\ \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right.$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg)^{5/2} \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 1.1487039597013978 \cdot \theta^{67} \\
& \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2 \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
& \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \right. \\
& \left. \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \left( 4 \cdot \right. \\
& \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^{7/2} \Bigg) / \\
& \left( \left( -2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& \quad 2. \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right)^2 (16 \pi^2 \theta - \\
& \quad 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) - \\
& \quad \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. + 1.50288049195799 \cdot \theta^{48} \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^2 \\
& \sqrt{\left( \left( 1. \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) / \right. \\
& \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^8 - \right. \\
& \left. \left( 1.5403824585317376 \cdot \theta^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \right. \\
& \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right) \\
& \left. - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta) \right. \right. \\
& \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. + 1.50288049195799 \cdot \theta^{48} \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + 2. \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg) \Bigg) / \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^6 - \\
& \left( 3.706452695441867 \cdot 10^{33} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right. \\
& \left. \left( - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right. \\
& \left. \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
& 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \Big)^2 \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - \\
& \quad 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 +
\end{aligned}$$



$$\begin{aligned}
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14}) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} + \right. \\
& \quad \left. 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^3 / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + 2. \cdot \\
& \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \\
& \quad \left. \theta)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 \Bigg) - \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg) - \\
& \left( 1.0921327760127014 \cdot 10^{17} \sqrt{\left( \left( 1. \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) \right) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^8 - \\
& \left( 1.5403824585317376 \cdot 10^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left. \left( - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + 2 \cdot \\
& \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \\
& \quad \left. \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& \quad \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2 \right. \\
& \quad \left. \theta\sin[\beta]^2)^4 \right) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 3.706452695441867 \cdot 10^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} + \right. \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 \Bigg) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot \theta^{49} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16\pi^2\theta - \right. \right. \\
& \quad \left. \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right)^2}
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49}\theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48}\theta^2 \right)^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14}\theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49}\theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48}\theta^2 \right) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right)^3 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& 7.179399748133736 \cdot 10^{65} \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}\theta) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2. \cdot \\
& \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \theta^2 \right)^2 \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2 \right)^4 \Big) - \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Big) \right) \Big) \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) \Big) \Big) \Big) / \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \theta \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
2. & \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}\theta)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14}\theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 -
\end{aligned}$$

$$\begin{aligned}
& \left( 2.2137119528363295 \cdot \theta^{-97} \right. \\
& \left( -4\pi\theta + \theta^2 + \right. \\
& \quad 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \\
& \quad 4\pi^2\sin[\beta]^2 - \\
& \quad \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \\
& \left( \left( 1.0921327760127014 \cdot \theta^{17} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right. \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48}\theta^2) \right. \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \Bigg) + \\
& 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \theta \right)^2}
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 (16\pi^2\theta - \\
& \quad 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta \right) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg) - \\
& \left( 4.205755426393841 \cdot 10^{32} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) \Bigg/ \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right. \\
& \quad \left. - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
 & \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
 & \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
 & \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
 2. & \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}\theta)^2 \right. \\
 & \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
 & \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
 & \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2\theta - \right. \\
 & \quad \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
 & \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
 & \quad \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
 & \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
 & \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
 & \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg)^{3/2} +
 \end{aligned}$$

$$\begin{aligned}
& \left( 6.825829850079384 \cdot \theta^{15} \left( - \left( 6.16152983412695 \cdot \theta^{16} \left( -4\pi\theta + \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^6 \right) \right) \\
& \sqrt{\left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \right. \\
& \quad \left. \left. \left. \left. \theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \right. \\
& \quad \left. \left( 16\pi^2 \theta - 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \right. \right. \\
& \quad \left. \left. \sin[\beta]^2 \right)^2 \right) + 2 \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta \right)^2 \right. \right. \\
& \quad \left. \left. \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \left( 16\pi^2 \theta - 12\pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \left( 4 \cdot \right. \\
& \quad \left. \left( 2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \right. \\
& \quad \left. \left. \theta \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) - \left( 4 \cdot \right. \\
& \quad (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \\
& \quad \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) \Bigg)^{3/2} \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 7.972555357963553 \cdot 10^{50} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \left( 4 \cdot \right. \\
& \quad \left. (2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \\
& \quad \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + \\
& 1.1487039597013978 \cdot 10^{67}
\end{aligned}$$

$$\begin{aligned}
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \pi^{32} - 2.6285971414961507 \cdot \pi^{31} \theta) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + 2. \cdot \\
& \sqrt{\left( (6.646791914659577 \cdot \pi^{32} - 2.6285971414961507 \cdot \pi^{31} \right. \\
& \quad \theta)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2)^2 (16 \pi^2 \theta - 12 \pi \right. \\
& \quad \left. \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \left( 4. \cdot \right. \\
& \quad \left. (2.435611652890208 \cdot \pi^{15} + 8.53228731259923 \cdot \pi^{14} \right. \\
& \quad \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( \left( 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2 \right)^4 \right) \right)^{7/2} \Bigg/ \\
& \left( \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2 \theta - 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \theta^2 \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2 \theta - \right. \\
& \quad \left. 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \quad \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg)^2 \\
& \sqrt{\left( \left( 1. \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) / \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^8 - \\
& \quad \left( 1.5403824585317376 \cdot \theta^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right) \\
& \quad \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2. \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 \Bigg) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg/ \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^6 - \\
& \left( 3.706452695441867 \cdot 10^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right. \\
& \quad \left. \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - \\
& \quad 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big)^2 + \\
& 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big)^2 \Big) \Big) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 - \\
& \left( 6.643796131636294 \cdot 10^{49} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{\sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 -}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) (16\pi^2 \theta - \\
& \quad 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \Big) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 (16\pi^2 \theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \Big) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48} \theta^2 \left. \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \left. \right)^3 \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \right. \\
& \quad \left. \left. \sin[\beta]^2 \right)^2 \right) + 2. \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta \right)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \right)
\end{aligned}$$



$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14}) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg) - \\
& \quad \left( 1.0921327760127014 \cdot \theta^{17} \sqrt{\left( \left( 1 \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) \right) / } \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^8 - \right. \\
& \quad \left( 1.5403824585317376 \cdot \theta^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta) \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \quad \sin[\beta]^2)^2 + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot 10^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) / \\
& (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^6 - \\
& \left( 3.706452695441867 \cdot 10^{33} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{\sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 -}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2 \theta - \right. \\
& \quad \left. 12\pi \theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta^2 \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right. \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2 \theta - 12\pi \theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \quad \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big)^2 / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot \theta^{49} \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - \right. \right. \\
& \quad \left. \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right)^2 \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \right) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) \Big) \Big) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \theta + 1.50288049195799 \cdot \theta^{48} \right) \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \left. \sin[\beta]^2 \right)^2 + 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right)^2 \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right)^2 \right. \\
& \left. \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \right. \\
& \left. \left. \theta \sin[\beta]^2 \right)^4 \right) - \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right)^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) / \\
& \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{4 \pi - \theta} \theta \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{4 \pi - \theta} \theta \sin[\beta]^3}{\theta} \right)^2 \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / } \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) \right)^2 \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4) - \\
& \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) / } \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^{5/2} \Bigg) \\
& \left( 1.7124327770294835 \cdot \theta^{49} - \left( 1.3651659700158768 \cdot \theta^{16} \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right. \\
& \left. - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \left. \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right)^2 (16 \pi^2 \theta - \\
& 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Bigg) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg) \Bigg)^2 + \\
& \left( 1.0514388565984603 \cdot 10^{32} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right)^2 \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4) - \\
& \quad \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) + \\
& \quad \left( 1.3651659700158768 \cdot \theta^{16} \sqrt{\left( \left( 1 \cdot \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \right) / \right. \\
& \quad \left. (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^8 - \right. \\
& \quad \left( 1.5403824585317376 \cdot \theta^{16} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \quad \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta) \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2 \right)^2 + 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta \right)^2 \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right)^2 \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2 \right)^4 - \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad \left. \left. 8.53228731259923 \cdot \theta^{14} \theta \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 -
\end{aligned}$$

$$\begin{aligned}
& \left( 3.706452695441867 \cdot \pi^{33} \left( -4\pi\theta + \theta^2 + 2\pi \right. \right. \\
& \quad \left. \frac{\sqrt{(4\pi - \theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 -}{4\pi - \theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \pi^{32} - 2.6285971414961507 \cdot \pi^{31} \theta \right) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \pi^{49} - 1.7124327770294835 \cdot \pi^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \pi^{48} \theta^2) (16\pi^2 \theta - \right. \\
& \quad \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \pi^{32} - \right. \right. \\
& \quad \left. 2.6285971414961507 \cdot \pi^{31} \theta \right)^2 \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi \sqrt{(4\pi - \theta)\theta} \sin[\beta] + \right. \\
& \quad \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2 \sqrt{(4\pi - \theta)\theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \pi^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \pi^{49} \theta + \\
& \quad 1.50288049195799 \cdot \pi^{48} \theta^2)^2 (16\pi^2 \theta - 12\pi\theta^2 + \\
& \quad \left. 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \left( 4 \cdot \left( 2.435611652890208 \cdot \pi^{15} + \right. \right. \\
& \quad \left. 8.53228731259923 \cdot \pi^{14} \theta \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} + \right. \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 \Bigg) \Bigg/ \\
& \left( 16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot \theta^{49} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16\pi^2\theta - \right. \right. \\
& \quad \left. \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right)^2}
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49}\theta + \\
& \quad 1.50288049195799 \cdot 10^{48}\theta^2)^2 (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
& \left( 4. \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad 8.53228731259923 \cdot 10^{14}\theta) \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot 10^{49} - \right. \\
& \quad 1.7124327770294835 \cdot 10^{49}\theta + \\
& \quad 1.50288049195799 \cdot 10^{48}\theta^2) (16\pi^2\theta - 12\pi\theta^2 + \\
& \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg)^3 \Bigg/ \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 + \\
& 7.179399748133736 \cdot 10^{65} \\
& \left( - \left( 2. \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31}\theta) \right. \right. \\
& \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \\
& \quad \sin[\beta]^2)^2 \Bigg) + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 \right. \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \theta \sin[\beta]^2)^4 \Bigg) - \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left. (-4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg/ \\
& \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta) \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
2. & \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \theta)^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \theta) \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg/
\end{aligned}$$



$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg/ \\
& \left( 4 \pi \sqrt{\left( 4.1807617710132735 \cdot \theta^{48} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \right. \\
& \quad 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right)} \right) \\
& \left( 1.7124327770294835 \cdot \theta^{49} - \left( 1.3651659700158768 \cdot \theta^{16} \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + 2 \cdot \\
& \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right) \right.}
\end{aligned}$$

$$\begin{aligned}
& \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2 \\
& \quad \left. \theta\sin[\beta]^2)^4 \right) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& 8.53228731259923 \cdot 10^{14} \theta) \left( -4\pi\theta + \theta^2 + \right. \\
& 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \\
& \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
& \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right)^2 \Bigg) \Bigg)^2 + \\
& \left( 1.0514388565984603 \cdot 10^{32} \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta} \right. \right. \\
& \quad \left. \sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg) / \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \theta) \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^2 \right) + \\
& 2. \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \\
& \quad \left. \theta)^2 \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2)^2 (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14} \right. \\
& \quad \left. \theta) \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16\pi^2\theta - 12\pi\theta^2 + \right. \\
& \quad \left. 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right) \Bigg) \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& \left( 1.3651659700158768 \cdot 10^{16} \sqrt{\left( \left( 1 \cdot \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{\theta} \right)^8 \right) / \right. \\
& \quad \left. (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^8 - \right. \\
& \quad \left. \left( 1.5403824585317376 \cdot 10^{16} \left( -4\pi\theta + \theta^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 2\pi\sqrt{(4\pi-\theta)\theta} \sin[\beta] + 4\pi^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{\theta} \right)^6 \right. \right. \\
& \quad \left. \left. \left( - \left( 2 \cdot (6.646791914659577 \cdot 10^{32} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 2.6285971414961507 \cdot 10^{31} \theta) \right. \right. \right. \\
& \quad \left. \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \right. \right. \right. \\
& \quad \left. \left. \left. \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \right. \\
& \quad \left. \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16\pi^2\theta - \right. \right. \\
& \quad \left. \left. 12\pi\theta^2 + 2\theta^3 - 16\pi^3 \sin[\beta]^2 + 8\pi^2\theta \sin[\beta]^2)^2 \right) + \right. \\
& \quad \left. 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - \right. \right. \right. \right. \\
& \quad \left. \left. \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \right. \\
& \quad \left. \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi-\theta)\theta} \sin[\beta] + \right. \right. \right. \\
& \quad \left. \left. \left. 4\pi^2 \sin[\beta]^2 - \frac{2\pi^2 \sqrt{(4\pi-\theta)\theta} \sin[\beta]^3}{4\pi-\theta} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad 8.53228731259923 \cdot \theta^{14} \theta) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^6 - \\
& \left( 3.706452695441867 \cdot \theta^{33} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \\
& \quad \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \theta) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg) + \\
2. & \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \\
4. & \sqrt{\left( 2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg) \Bigg/
\end{aligned}$$

$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 6.643796131636294 \cdot \theta^{49} \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right)^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \quad \left. \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad 8.53228731259923 \cdot \theta^{14}) \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^3 \Bigg) / \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 + \\
& \quad 7.179399748133736 \cdot \theta^{65} \left( - \left( 2. \cdot (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - \right. \\
& \quad \left. 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& \quad 2. \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31})^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right.
\end{aligned}$$



$$\begin{aligned}
& \left( \left( 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + 1.50288049195799 \cdot \theta^{48} \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) - \\
& \left( 4. \cdot (2.435611652890208 \cdot \theta^{15} + 8.53228731259923 \cdot \theta^{14}) \right. \\
& \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} + 1.50288049195799 \cdot \theta^{48} \right)^2 (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \right) \right) / \\
& \left( -2. \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \\
& \left. \theta) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \left. \theta + 1.50288049195799 \cdot \theta^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) +
\end{aligned}$$

$$\begin{aligned}
& 2. \sqrt{\left( \left( 6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \right. \\
& \quad \left. \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) - \\
& \quad \left( 4. \left( 2.435611652890208 \cdot 10^{15} + 8.53228731259923 \cdot 10^{14} \right. \right. \\
& \quad \left. \left. \theta \right) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( \left( 2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \right. \\
& \quad \left. \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Big)^2 \Big) \Big) / \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 - \\
& \quad \left( 1.1068559764181647 \cdot 10^{-97} \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2
\end{aligned}$$

$$\begin{aligned}
& \left( 1.7124327770294835 \cdot \theta^{49} - \left( 1.3651659700158768 \cdot \theta^{16} \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - 1.7124327770294835 \cdot \theta^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot \theta^{48}\theta^2) \right. \\
& \quad (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta \\
& \quad \sin[\beta]^2)^2 \Bigg) + 2 \cdot \sqrt{\left( (6.646791914659577 \cdot \theta^{32} - \right. \\
& \quad \left. 2.6285971414961507 \cdot \theta^{31})^2 \right. \\
& \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
& \quad \left. 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \right. \\
& \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49}\theta + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2 \right)^4 - \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot \theta^{14}) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg)^2 \Bigg)^2 + \\
& \left( 1.0514388565984603 \cdot \theta^{32} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \right. \right. \\
& \quad \left. \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right. \\
& \quad \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31}) \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \Big) + 2. \\
& \sqrt{\left( (6.646791914659577 \cdot 10^{32} - 2.6285971414961507 \cdot 10^{31} \right. \\
& \quad \left. \theta \right)^2 \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right)^2 \\
& \quad (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \\
& \quad \left. \theta \sin[\beta]^2)^4 \right) - \left( 4. (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / } \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2 \right) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \Big) \Big) \Big) + \\
& \left( 1.3651659700158768 \cdot 10^{16} \sqrt{\left( \left( 1. \left( -4 \pi \theta + \theta^2 + 2 \pi \right. \right. \right. \right. \\
& \quad \left. \left. \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \right. \right. \\
& \quad \left. \left. \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^8 \Bigg/ \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^8 - \\
& \left( 1.5403824585317376 \cdot 10^{16} \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^6 \right. \\
& \left. \left( - \left( 2 \cdot 10^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot 10^{49} \theta + \\
& \quad \left. 1.50288049195799 \cdot 10^{48} \theta^2 \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 + \\
& 2 \cdot \sqrt{\left( \left( \left( 6.646791914659577 \cdot 10^{32} - \right. \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta \right)^2 \right. \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot 10^{49} - \right. \right. \\
& \quad \left. 1.7124327770294835 \cdot 10^{49} \theta + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Big) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Big) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Big) \Big) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \left. \sin[\beta]^2 \right)^6 - \left( 3.706452695441867 \cdot \theta^{33} \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \right. \\
& \left. \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \\
& \left( - \left( 2. \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \Bigg) + \\
2. \cdot & \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad 2.6285971414961507 \cdot \theta^{31} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) - \\
& \left( 4. \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \quad 8.53228731259923 \cdot \theta^{14} \Bigg) \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \Bigg/ \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \Bigg) \Bigg) \Bigg) \Bigg/
\end{aligned}$$



$$\begin{aligned}
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2 \right)^4 - \left( 6.643796131636294 \cdot \theta^{49} \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \right. \\
& \quad \left. \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right. \\
& \quad \left. - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad 1.7124327770294835 \cdot \theta^{49} + \\
& \quad 1.50288049195799 \cdot \theta^{48}) (16 \pi^2 \theta - 12 \pi \theta^2 + \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) + \\
& \quad 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot \theta^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \quad \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \quad \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \quad \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
& \quad \left. 1.7124327770294835 \cdot \theta^{49} \theta + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 1.50288049195799 \cdot \theta^{48} \right)^2 \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 - \\
& \left( 4 \cdot \left( 2.435611652890208 \cdot \theta^{15} + \right. \right. \\
& \left. \left. 8.53228731259923 \cdot \theta^{14} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^4 \right) \Bigg)^3 \Bigg) / \\
& \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \left. \sin[\beta]^2 \right)^2 + 7.179399748133736 \cdot \theta^{65} \\
& \left( - \left( 2 \cdot \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right. \\
& \left. \left. 2.6285971414961507 \cdot \theta^{31} \right) \right. \\
& \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \\
& \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \\
& \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^2 \right) / \\
& \left( \left( 2.652268423469232 \cdot \theta^{49} - \right. \right. \\
& \left. \left. 1.7124327770294835 \cdot \theta^{49} + \right. \right. \\
& \left. \left. 1.50288049195799 \cdot \theta^{48} \right) \left( 16 \pi^2 \theta - 12 \pi \theta^2 + \right. \right. \\
& \left. \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2 \right)^2 \right) + \\
& 2 \cdot \sqrt{\left( \left( 6.646791914659577 \cdot \theta^{32} - \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & 2.6285971414961507 \cdot \theta^{31})^2 \\
 & \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
 & \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
 & \quad 1.7124327770294835 \cdot \theta^{49} + \\
 & \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
 & \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) - \\
 & \left( 4 \cdot (2.435611652890208 \cdot \theta^{15} + \right. \\
 & \quad 8.53228731259923 \cdot \theta^{14}) \\
 & \quad \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \\
 & \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
 & \quad \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^4 \Bigg) \Bigg/ \\
 & \left( (2.652268423469232 \cdot \theta^{49} - \right. \\
 & \quad 1.7124327770294835 \cdot \theta^{49} + \\
 & \quad 1.50288049195799 \cdot \theta^{48})^2 (16\pi^2\theta - 12\pi\theta^2 + \\
 & \quad 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)^4 \Bigg) \Bigg) \Bigg) \Bigg) \Bigg/ \\
 & \left( - \left( 2 \cdot (6.646791914659577 \cdot \theta^{32} - 2.6285971414961507 \cdot \theta^{31} \right. \right. \\
 & \quad \left. \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + \right. \right. \\
 & \quad 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \\
 & \quad \left. \left. \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right)^2 \right) \Bigg) \Bigg/
 \end{aligned}$$

$$\begin{aligned}
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \right. \\
& \quad \left. \sin[\beta]^2)^2 \right) + 2 \cdot \sqrt{\left( \left( (6.646791914659577 \cdot 10^{32} - \right. \right. \\
& \quad \left. \left. 2.6285971414961507 \cdot 10^{31} \theta)^2 \right. \right. \\
& \quad \left. \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + \right. \right. \\
& \quad \left. \left. 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2)^2 \right. \\
& \quad \left( 16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \right. \\
& \quad \left. \theta \sin[\beta]^2)^4 \right) - \left( 4 \cdot (2.435611652890208 \cdot 10^{15} + \right. \\
& \quad \left. 8.53228731259923 \cdot 10^{14} \theta) \left( -4 \pi \theta + \theta^2 + \right. \right. \\
& \quad \left. \left. 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \right. \right. \\
& \quad \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \right. \right. \\
& \quad \left. \left. \left. \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right)^4 \right) \right) / \\
& \left( (2.652268423469232 \cdot 10^{49} - 1.7124327770294835 \cdot 10^{49} \right. \\
& \quad \left. \theta + 1.50288049195799 \cdot 10^{48} \theta^2) (16 \pi^2 \theta - 12 \pi \theta^2 + \right. \\
& \quad \left. 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^4 \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2)^2 \right) \Bigg) \Bigg) \Bigg) \Bigg) / \\
& \left( (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right. \\
& \quad \left. \sin[\beta]^2) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -12.566370614359172 \, \theta \sqrt{(-4.487190804107819 \, \theta^{15} + \right. \\
& \quad \theta + \\
& \quad 3.57079298535128 \, \theta^{14} \\
& \quad \theta^2 + \\
& \quad 1.40969256654408 \, \theta^{16} \\
& \quad \left. \sin[\beta]^2) + \right. \\
& 1. \, \theta^2 \sqrt{(-4.487190804107819 \, \theta^{15} \theta + 3.57079298535128 \, \theta^{14} \\
& \quad \theta^2 + \\
& \quad 1.40969256654408 \, \theta^{16} \\
& \quad \left. \sin[\beta]^2) + \right. \\
& 6.283185307179586 \, \sqrt{12.566370614359172 \, \theta - 1. \, \theta^2} \\
& \quad \sin[\beta] \\
& \quad \left. \sqrt{(-4.487190804107819 \, \theta^{15} \right. \\
& \quad \quad \theta + \\
& \quad \quad 3.57079298535128 \, \theta^{14} \\
& \quad \quad \theta^2 + \\
& \quad \quad 1.40969256654408 \, \theta^{16} \\
& \quad \quad \left. \sin[\beta]^2) \right) \Bigg), \{\theta, -\pi/2, \pi/2\} \Bigg]
\end{aligned}$$

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

$\infty$ ::indet : Indeterminate expression (0. + 0. i) ComplexInfinity encountered. >>

Power::infy : Infinite expression  $\frac{1}{0. + 0. i}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.^4}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>

$\infty$ ::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

$\infty$ ::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

General::stop : Further output of  $\infty$ ::indet will be suppressed during this calculation. >>

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

$$r := \left( -4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta} \right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

$$\beta := \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]$$

$$\begin{aligned}
& D\left[\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}, \theta\right] \\
& \left( - \left( 8\pi\theta \left( 16\pi^2 - 4\pi(4\pi - \theta) - 20\pi\theta + 4(4\pi - \theta)\theta + 4\theta^2 \right) \right. \right. \\
& \quad \left. \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2 \right) / \\
& \quad \left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^3 + \\
& \quad \left( 2\theta^2 \left( 16\pi^2 - 4\pi(4\pi - \theta) - 20\pi\theta + 4(4\pi - \theta)\theta + 4\theta^2 \right) \right. \\
& \quad \left. \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2 \right) / \\
& \quad \left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^3 + \\
& \quad \left( 8\pi\theta \left( -4\pi + 2(4\pi - \theta) - \frac{(4\pi - \theta)^2}{4\pi} + \frac{\theta^2}{4\pi} \right) \right. \\
& \quad \left. \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2 \right) / \\
& \quad \left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^2 - \\
& \quad \left( 2\theta^2 \left( -4\pi + 2(4\pi - \theta) - \frac{(4\pi - \theta)^2}{4\pi} + \frac{\theta^2}{4\pi} \right) \right. \\
& \quad \left. \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2 \right) / \\
& \quad \left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^2 + \\
& \quad \frac{4\pi \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2}{\left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^2} - \\
& \quad \frac{2\theta \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2}{\left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^2} \right) / \\
& \quad \left( 4\pi \sqrt{\left( \frac{4\pi\theta \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2}{\left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^2} - \right. \right. \\
& \quad \left. \left. \frac{\theta^2 \left( -4\pi\theta + 2(4\pi - \theta)\theta - \frac{(4\pi - \theta)^2\theta}{4\pi} + \theta^2 - \frac{(4\pi - \theta)\theta^2}{4\pi} \right)^2}{\left( 16\pi^2\theta - 4\pi(4\pi - \theta)\theta - 12\pi\theta^2 + 2(4\pi - \theta)\theta^2 + 2\theta^3 \right)^2} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{RevolutionPlot3D} \left[ \left( - \left( 8 \pi \theta \left( 16 \pi^2 - 4 \pi (4 \pi - \theta) - 20 \pi \theta + 4 (4 \pi - \theta) \theta + 4 \theta^2 \right) \right. \right. \right. \\
& \quad \left. \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2 \right) / \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^3 + \right. \\
& \quad \left. \left( 2 \theta^2 \left( 16 \pi^2 - 4 \pi (4 \pi - \theta) - 20 \pi \theta + 4 (4 \pi - \theta) \theta + 4 \theta^2 \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2 \right) / \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^3 + \right. \\
& \quad \left. \left( 8 \pi \theta \left( -4 \pi + 2 (4 \pi - \theta) - \frac{(4 \pi - \theta)^2}{4 \pi} + \frac{\theta^2}{4 \pi} \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right) \right) / \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2 - \right. \\
& \quad \left. \left( 2 \theta^2 \left( -4 \pi + 2 (4 \pi - \theta) - \frac{(4 \pi - \theta)^2}{4 \pi} + \frac{\theta^2}{4 \pi} \right) \right. \right. \\
& \quad \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right) \right) / \right. \\
& \quad \left. \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2 + \right. \\
& \quad \left. \frac{4 \pi \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} - \right. \\
& \quad \left. \frac{2 \theta \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} \right) / \right. \\
& \quad \left. \left( 4 \pi \sqrt{\left( \frac{4 \pi \theta \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} - \right. \right. \right. \\
& \quad \left. \left. \frac{\theta^2 \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} \right) \right), \{\theta, -2 \pi, 2 \pi\} \right]
\end{aligned}$$

Power::infy : Infinite expression  $\frac{1}{0}$ . encountered. >>

Power::infy : Infinite expression  $\frac{1}{0}$ . encountered. >>



Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

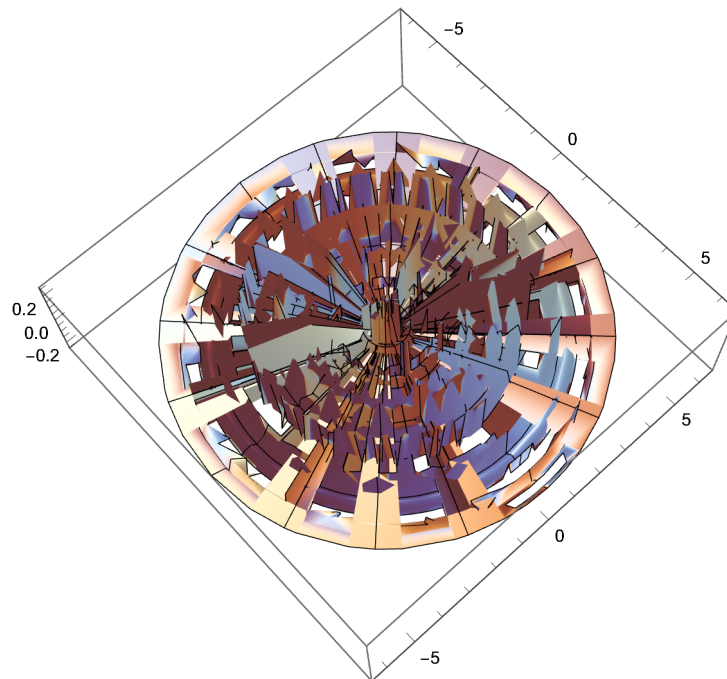
General::stop : Further output of Power::infy will be suppressed during this calculation. >>

$\infty::indet$  : Indeterminate expression 0. ComplexInfinity encountered. >>

$\infty::indet$  : Indeterminate expression 0. ComplexInfinity encountered. >>

$\infty::indet$  : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

General::stop : Further output of  $\infty::indet$  will be suppressed during this calculation. >>



Solve[

$$\begin{aligned}
& \left( - \left( 8 \pi \theta \left( 16 \pi^2 - 4 \pi (4 \pi - \theta) - 20 \pi \theta + 4 (4 \pi - \theta) \theta + 4 \theta^2 \right) \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \right. \right. \right. \\
& \quad \left. \left. \left. \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2 \right) \right) / \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^3 + \\
& \left( 2 \theta^2 \left( 16 \pi^2 - 4 \pi (4 \pi - \theta) - 20 \pi \theta + 4 (4 \pi - \theta) \theta + 4 \theta^2 \right) \right. \\
& \quad \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2 \right) / \\
& \quad \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^3 + \\
& \left( 8 \pi \theta \left( -4 \pi + 2 (4 \pi - \theta) - \frac{(4 \pi - \theta)^2}{4 \pi} + \frac{\theta^2}{4 \pi} \right) \right. \\
& \quad \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right) \right) / \\
& \quad \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2 - \\
& \left( 2 \theta^2 \left( -4 \pi + 2 (4 \pi - \theta) - \frac{(4 \pi - \theta)^2}{4 \pi} + \frac{\theta^2}{4 \pi} \right) \right. \\
& \quad \left. \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right) \right) / \\
& \quad \left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2 + \\
& \quad \frac{4 \pi \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} - \\
& \quad \left. \frac{2 \theta \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} \right) / \\
& \left( 4 \pi \sqrt{\left( \frac{4 \pi \theta \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} - \right. \right. \\
& \quad \left. \left. \frac{\theta^2 \left( -4 \pi \theta + 2 (4 \pi - \theta) \theta - \frac{(4 \pi - \theta)^2 \theta}{4 \pi} + \theta^2 - \frac{(4 \pi - \theta) \theta^2}{4 \pi} \right)^2}{\left( 16 \pi^2 \theta - 4 \pi (4 \pi - \theta) \theta - 12 \pi \theta^2 + 2 (4 \pi - \theta) \theta^2 + 2 \theta^3 \right)^2} \right) \right)} = \frac{4 \pi r^2 - 2 r^2 \theta}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r]
\end{aligned}$$

Divide::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

Divide::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

Divide::infy : Infinite expression  $\frac{1}{0}$  encountered. >>

General::stop : Further output of Divide::infy will be suppressed during this calculation. >>

$\infty$ ::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

$\infty$ ::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

$\infty$ ::indet : Indeterminate expression ComplexInfinity + ComplexInfinity encountered. >>

General::stop : Further output of  $\infty$ ::indet will be suppressed during this calculation. >>

{{}}

$$\begin{aligned} & \frac{4\pi}{3} + \left( 2^{1/3} \left( -1296\pi^2 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right) \right)^{10/3} - \right. \\ & 324 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\ & \left( -\pi^2 + 50\pi^2\sin[\beta]^2 - 453\pi^2\sin[\beta]^4 + 36\pi^2\sin[\beta]^6 + \right. \\ & 5\sqrt{3}\pi^2\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \\ & 78\sqrt{3}\pi^2\sin[\beta]^2\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\ & 9\sqrt{3}\pi^2\sin[\beta]^4\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\ & \left. \pi^2 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\ & 35\pi^2\sin[\beta]^2 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & 243\pi^2\sin[\beta]^4 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & 9\pi^2\sin[\beta]^6 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\ & 4\sqrt{3}\pi^2\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \\ & \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & 42\sqrt{3}\pi^2\sin[\beta]^2\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \\ & \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\ & 5\pi^2 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & 88\pi^2\sin[\beta]^2 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & 36\pi^2\sin[\beta]^4 \left( -1 + 18\sin[\beta]^2 + 3\sqrt{3}\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\ & \left. 15\sqrt{3}\pi^2\sqrt{\sin[\beta]^2(-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right) \end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big) \Big) / \\
& \left( 27 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right. \\
& \left( 128\,304\,\pi^3 - 46\,049\,472\,\pi^3 \sin[\beta]^2 + 3\,084\,719\,760\,\pi^3 \sin[\beta]^4 - 76\,984\,149\,600\,\pi^3 \sin[\beta]^6 + \right. \\
& 791\,034\,575\,760\,\pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232\,\pi^3 \sin[\beta]^{10} - \\
& 4\,120\,487\,403\,984\,\pi^3 \sin[\beta]^{12} - 430\,339\,664\,160\,\pi^3 \sin[\beta]^{14} - \\
& 9\,183\,300\,480\,\pi^3 \sin[\beta]^{16} - 1\,924\,560\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 240\,395\,040\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8\,641\,939\,248\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016\,\sqrt{3}\,\pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880\,\pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1\,412\,976\,960 \\
& \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936\,\pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 361\,323\,192\,960 \\
& \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 10\,033\,606\,080 \\
& \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 1\,082\,722\,464 \\
& \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 217\,196\,393\,760 \\
& \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 1\,632\,586\,752 \\
& \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128304 \pi^3 - 46049472 \pi^3 \sin[\beta]^2 + 3084719760 \pi^3 \sin[\beta]^4 - 76984149600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791034575760 \pi^3 \sin[\beta]^8 - 2463947543232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4120487403984 \pi^3 \sin[\beta]^{12} - 430339664160 \pi^3 \sin[\beta]^{14} - 9183300480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1924560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240395040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8641939248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116076162240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464847899760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696655378080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43748223120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306110016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69984 \\
& \quad \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 22394880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1412976960 \pi^3 \sin[\beta]^4 \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 69984 \\
& \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 1082722464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} +
\end{aligned}$$



$$\begin{aligned}
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^2 + \\
& 4 \left( -1296 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \\
& \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \\
& \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 9 \pi^2 \sin[\beta]^6 \right. \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 5 \pi^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \right. \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \\
& \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \pi^2 \sin[\beta]^4 \right. \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \right. \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - 6 \sqrt{3} \pi^2
\end{aligned}$$

$$\begin{aligned}
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^3 \Big)^{1/3} \Big) - \\
& \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \\
& \quad \pi^3 \\
& \quad \sin[\beta]^6 + 791\,034\,575\,760 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^8 - 2\,463\,947\,543\,232 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{10} - 4\,120\,487\,403\,984 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{12} - 430\,339\,664\,160 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{16} - 1\,924\,560 \\
& \quad \sqrt{3} \\
& \quad \pi^3 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 240\,395\,040 \\
& \quad \sqrt{3} \\
& \quad \pi^3 \\
& \quad \sin[\beta]^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 8\,641\,939\,248 \\
& \quad \sqrt{3} \\
& \quad \pi^3 \\
& \quad \sin[\beta]^4 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 116\,076\,162\,240 \\
& \quad \sqrt{3} \\
& \quad \pi^3 \\
& \quad \sin[\beta]^6 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 464\,847\,899\,760 \\
& \quad \sqrt{3} \\
& \quad \pi^3 \\
& \quad \sin[\beta]^8 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 696\,655\,378\,080 \\
& \quad \sqrt{3} \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{10}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 43\,748\,223\,120 \\
& \sqrt{3} \\
& \pi^3 \\
& \sin[\beta]^{12} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 306\,110\,016 \\
& \sqrt{3} \\
& \pi^3 \\
& \sin[\beta]^{14} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \\
& \pi^3 \\
& \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960\,\pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936\,\pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960\,\pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008\,\pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} - \\
& 3868575552 \sqrt{3} \pi^3 \sin^4[\beta] \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} + \\
& 52016027904 \sqrt{3} \pi^3 \sin^6[\beta] \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin^8[\beta] \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin^{10}[\beta] \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin^{12}[\beta] \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 19455552 \pi^3 \sin^2[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin^4[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin^6[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin^8[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin^{10}[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin^{12}[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin^{14}[\beta]
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128304 \pi^3 - 46049472 \pi^3 \sin[\beta]^2 + 3084719760 \pi^3 \sin[\beta]^4 - 76984149600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791034575760 \pi^3 \sin[\beta]^8 - 2463947543232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4120487403984 \pi^3 \sin[\beta]^{12} - 430339664160 \pi^3 \sin[\beta]^{14} - 9183300480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1924560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240395040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8641939248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116076162240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464847899760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696655378080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43748223120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306110016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad \left. \left. 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \right) \right)^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& 22\,394\,880\,\pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1\,412\,976\,960\,\pi^3 \sin[\beta]^4 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936\,\pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 361\,323\,192\,960\,\pi^3 \sin[\beta]^8 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008\,\pi^3 \sin[\beta]^{16} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19455552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 1082722464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 217196393760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 79877708064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} +
\end{aligned}$$

$$\begin{aligned}
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 4 \left( -1296 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \\
& \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left. \right)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 9 \pi^2 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 5 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left. \right)^{2/3} \left. \right)^{1/3} /
\end{aligned}$$



$$\left(27 \times 2^{1/3} \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{5/3}\right)$$

$$\begin{aligned} \text{Solve}\left[\frac{1}{2\pi} \left(\sqrt{4\pi r^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right)} \right. \right. \\ \left. \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\ \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) - \\ \left. r^2 \left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) \right] \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)^2 \Bigg] = \\ r \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4\pi^2 \theta + 4\pi \theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}}\right]\right] \end{aligned}$$

$$\beta := \frac{\pi}{3}$$

$$\begin{aligned} \text{Solve}\left[\frac{4\pi}{3} + \left(2^{1/3} \left(-1296\pi^2 \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{10/3} - \right. \right. \right. \\ \left. 324 \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{5/3} \right. \\ \left. \left(-\pi^2 + 50\pi^2 \sin[\beta]^2 - 453\pi^2 \sin[\beta]^4 + 36\pi^2 \sin[\beta]^6 + \right. \right. \\ \left. 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right. \\ \left. 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\ \left. 9 \sqrt{3} \pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\ \left. \pi^2 \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3} - 35\pi^2 \right. \\ \left. \sin[\beta]^2 \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3} + 243 \right. \\ \left. \pi^2 \sin[\beta]^4 \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3} + \right. \\ \left. 9\pi^2 \sin[\beta]^6 \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3} - \right. \\ \left. 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right. \\ \left. \left(-1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^{1/3} + \right. \\ \left. 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right) \end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 5 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 36 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big) \Big) / \\
& \left( 27 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right. \\
& \left( 128304 \pi^3 - 46049472 \pi^3 \sin[\beta]^2 + 3084719760 \pi^3 \sin[\beta]^4 - 76984149600 \pi^3 \sin[\beta]^6 + \right. \\
& 791034575760 \pi^3 \sin[\beta]^8 - 2463947543232 \pi^3 \sin[\beta]^{10} - \\
& 4120487403984 \pi^3 \sin[\beta]^{12} - 430339664160 \pi^3 \sin[\beta]^{14} - \\
& 9183300480 \pi^3 \sin[\beta]^{16} - 1924560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 240395040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8641939248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116076162240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464847899760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696655378080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43748223120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306110016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22394880 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1412976960 \\
& \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34362423936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 361323192960 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 1\,082\,722\,464 \\
& \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 217\,196\,393\,760 \pi^3 \sin[\beta]^8
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 1\,632\,586\,752 \\
& \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \left. \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \right. \\
& \quad \left. 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \right. \\
& \quad \left. \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\
& \quad \left. 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right. \\
& \quad \left. 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\
& \quad \left. 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right. \\
& \quad \left. 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \right.
\end{aligned}$$

$$\begin{aligned}
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \\
& \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 19455552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23329866240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725922896832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1632586752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127925643168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8060897088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51018336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 4 \left( -1296 \pi^2 \right. \\
& \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 78 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \sin[\beta]^4 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 9 \pi^2 \sin[\beta]^6 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 42 \sqrt{3} \pi^2
\end{aligned}$$

$$\begin{aligned}
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 5 \pi^2 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& \quad 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& \quad 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \quad \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \left. \right)^3 \left. \right)^{1/3} \left. \right) - \\
& \left( 128\,304\,\pi^3 - 46\,049\,472\,\pi^3 \sin[\beta]^2 + 3\,084\,719\,760\,\pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \\
& \quad \pi^3 \\
& \quad \sin[\beta]^6 + 791\,034\,575\,760 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^8 - 2\,463\,947\,543\,232 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{10} - 4\,120\,487\,403\,984 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{12} - 430\,339\,664\,160 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \\
& \quad \sin[\beta]^{16} - 1\,924\,560 \\
& \quad \sqrt{3} \pi^3 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 240\,395\,040 \\
& \quad \sqrt{3} \pi^3 \\
& \quad \sin[\beta]^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} -
\end{aligned}$$



$$\begin{aligned}
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008 \pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} -
\end{aligned}$$

$$\begin{aligned}
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad \left. \left. 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \right. \\
& \quad \left. \left. 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \right. \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \right. \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right.
\end{aligned}$$

$$\begin{aligned}
& 34\,362\,423\,936\,\pi^3\,\text{Sin}[\beta]^6\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\right. \\
& \quad \left.\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+361\,323\,192\,960\,\pi^3\,\text{Sin}[\beta]^8 \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}- \\
& 1\,382\,528\,881\,152\,\pi^3\,\text{Sin}[\beta]^{10}\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\right. \\
& \quad \left.\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+10\,033\,606\,080\,\pi^3\,\text{Sin}[\beta]^{12} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+ \\
& 11\,224\,033\,920\,\pi^3\,\text{Sin}[\beta]^{14}\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\right. \\
& \quad \left.\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+153\,055\,008\,\pi^3\,\text{Sin}[\beta]^{16} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}- \\
& 979\,776\,\sqrt{3}\,\pi^3\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+ \\
& 112\,534\,272\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^2\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}- \\
& 3\,868\,575\,552\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^4\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+ \\
& 52\,016\,027\,904\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^6\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}- \\
& 241\,951\,624\,128\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^8\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+ \\
& 12\,788\,596\,224\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^{10}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}+ \\
& 1\,122\,403\,392\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^{12}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{1/3}- \\
& 69\,984\,\pi^3\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 19\,455\,552\,\pi^3\,\text{Sin}[\beta]^2 \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}-
\end{aligned}$$

$$\begin{aligned}
& 1\,082\,722\,464\,\pi^3\,\text{Sin}[\beta]^4\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\right. \\
& \quad \left.\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+23\,329\,866\,240\,\pi^3\,\text{Sin}[\beta]^6 \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}- \\
& 217\,196\,393\,760\,\pi^3\,\text{Sin}[\beta]^8\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\right. \\
& \quad \left.\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+725\,922\,896\,832\,\pi^3\,\text{Sin}[\beta]^{10} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 79\,877\,708\,064\,\pi^3\,\text{Sin}[\beta]^{12}\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\right. \\
& \quad \left.\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+1\,632\,586\,752\,\pi^3\,\text{Sin}[\beta]^{14} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 909\,792\,\sqrt{3}\,\pi^3\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}- \\
& 91\,119\,168\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^2\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 2\,737\,984\,032\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^4\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}- \\
& 32\,062\,189\,824\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^6\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 127\,925\,643\,168\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^8\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 8\,060\,897\,088\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^{10}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}+ \\
& 51\,018\,336\,\sqrt{3}\,\pi^3\,\text{Sin}[\beta]^{12}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)} \\
& \quad \left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{2/3}\right)^2+ \\
& 4\left(-1296\,\pi^2\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{10/3}-\right. \\
& \quad \left.324\left(-1+18\,\text{Sin}[\beta]^2+3\,\sqrt{3}\,\sqrt{\text{Sin}[\beta]^2\left(-1+11\,\text{Sin}[\beta]^2+\text{Sin}[\beta]^4\right)}\right)^{5/3}\right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \\
& \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 9 \pi^2 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - \right. \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + \\
& 5 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - \right. \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - \right. \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} \Big)^3 \Big)^{1/3} / \\
& \left. \left( 27 \times 2^{1/3} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right) \right]
\end{aligned}$$

9.42478

9.424777960769378` /  $\pi$ 

3.

Solve[

$$\frac{4 \pi}{3} + \left( 2^{1/3} \left( -1296 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \right.$$

$$\begin{aligned}
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& \quad 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 9 \sqrt{3} \pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 243 \\
& \quad \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 9 \pi^2 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 5 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 88 \pi^2 \\
& \quad \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \\
& \quad \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& \quad 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& \quad 6 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \right) \Big) \Big) \Big) / \\
& \left( 27 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right. \\
& \quad \left( 128 304 \pi^3 - 46 049 472 \pi^3 \sin[\beta]^2 + 3 084 719 760 \pi^3 \sin[\beta]^4 - \right. \\
& \quad 76 984 149 600 \pi^3 \sin[\beta]^6 + 791 034 575 760 \pi^3 \sin[\beta]^8 - \\
& \quad 2 463 947 543 232 \pi^3 \sin[\beta]^{10} - 4 120 487 403 984 \pi^3 \sin[\beta]^{12} - \\
& \quad 430 339 664 160 \pi^3 \sin[\beta]^{14} - 9 183 300 480 \pi^3 \sin[\beta]^{16} - \\
& \quad \left. 1 924 560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right.
\end{aligned}$$

$$\begin{aligned}
& 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \pi^3 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 22\,394\,880 \\
& \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \\
& \pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$



$$\begin{aligned}
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} - \\
& 241951624128 \sqrt{3} \pi^3 \sin^8[\beta] \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} + \\
& 12788596224 \sqrt{3} \pi^3 \sin^{10}[\beta] \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} + \\
& 1122403392 \sqrt{3} \pi^3 \sin^{12}[\beta] \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{1/3} - 69984 \pi^3 \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + 19455552 \\
& \pi^3 \sin^2[\beta] \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} - \\
& 1082722464 \pi^3 \sin^4[\beta] \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])}^{2/3} + 23329866240 \pi^3 \sin^6[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} - \\
& 217196393760 \pi^3 \sin^8[\beta] \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])}^{2/3} + 725922896832 \pi^3 \sin^{10}[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 79877708064 \pi^3 \sin^{12}[\beta] \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} \\
& \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])}^{2/3} + 1632586752 \pi^3 \sin^{14}[\beta] \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 909792 \sqrt{3} \pi^3 \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} - \\
& 91119168 \sqrt{3} \pi^3 \sin^2[\beta] \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} + \\
& 2737984032 \sqrt{3} \pi^3 \sin^4[\beta] \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \\
& \left( -1 + 18 \sin^2[\beta] + 3 \sqrt{3} \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])} \right)^{2/3} - \\
& 32062189824 \sqrt{3} \pi^3 \sin^6[\beta] \sqrt{\sin^2[\beta] (-1 + 11 \sin^2[\beta] + \sin^4[\beta])}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 22\,394\,880 \pi^3 \sin[\beta]^2 \right. \\
& \quad \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& \quad \left. 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& \quad \left. 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& \quad \left. 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \\
& \quad \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right.
\end{aligned}$$

$$\begin{aligned}
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008\,\pi^3 \sin[\beta]^{16} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984\,\pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + 19\,455\,552\,\pi^3 \sin[\beta]^2 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464\,\pi^3 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} + \\
& 23\,329\,866\,240\,\pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} - \\
& 217\,196\,393\,760\,\pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} + \\
& 725\,922\,896\,832\,\pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} + \\
& 79\,877\,708\,064\,\pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} + \\
& 1\,632\,586\,752\,\pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} + \\
& 909\,792\,\sqrt{3}\,\pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91\,119\,168\,\sqrt{3}\,\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032\,\sqrt{3}\,\pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824\,\sqrt{3}\,\pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168\,\sqrt{3}\,\pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088\,\sqrt{3}\,\pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336\,\sqrt{3}\,\pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} \Big)^2 + 4 \left( -1296\,\pi^2 \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 9 \sqrt{3} \pi^2 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + \right. \\
& \quad \left. 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 35 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 9 \pi^2 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 4 \sqrt{3} \pi^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 42 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 5 \pi^2 \left( -1 + \right. \\
& \quad \left. 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 36 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 15 \sqrt{3} \pi^2 \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \quad \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right.
\end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{2/3} \Big)^3 \Big)^{1/3} \Big) - \\
& \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \\
& \quad \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \\
& \quad \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \\
& \quad \pi^3 \sin[\beta]^{10} - \\
& \quad 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \\
& \quad \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \\
& \quad \pi^3 \sin[\beta]^{16} - \\
& \quad 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 240\,395\,040 \\
& \quad \sqrt{3} \pi^3 \sin[\beta]^2 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 69\,984 \pi^3 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 22\,394\,880 \pi^3 \sin[\beta]^2 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& \quad 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& \quad 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \\
& \quad \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} -
\end{aligned}$$

$$\begin{aligned}
& 1\,382\,528\,881\,152\,\pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080\,\pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920\,\pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 153\,055\,008\,\pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 69\,984 \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& \sqrt{\left( \left( 128\,304 \pi^3 - 46\,049\,472 \pi^3 \sin[\beta]^2 + 3\,084\,719\,760 \pi^3 \sin[\beta]^4 - 76\,984\,149\,600 \right. \right. \\
& \quad \left. \pi^3 \sin[\beta]^6 + 791\,034\,575\,760 \pi^3 \sin[\beta]^8 - 2\,463\,947\,543\,232 \pi^3 \sin[\beta]^{10} - \right. \\
& \quad \left. 4\,120\,487\,403\,984 \pi^3 \sin[\beta]^{12} - 430\,339\,664\,160 \pi^3 \sin[\beta]^{14} - 9\,183\,300\,480 \right. \\
& \quad \left. \pi^3 \sin[\beta]^{16} - 1\,924\,560 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\
& \quad \left. 240\,395\,040 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right) -
\end{aligned}$$



$$\begin{aligned}
& 8\,641\,939\,248 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 116\,076\,162\,240 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 464\,847\,899\,760 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 696\,655\,378\,080 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 43\,748\,223\,120 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 306\,110\,016 \sqrt{3} \pi^3 \sin[\beta]^{14} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 69\,984 \\
& \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 22\,394\,880 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 1\,412\,976\,960 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 34\,362\,423\,936 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 361\,323\,192\,960 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 1\,382\,528\,881\,152 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 10\,033\,606\,080 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 11\,224\,033\,920 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 153\,055\,008 \pi^3 \sin[\beta]^{16} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 979\,776 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 112\,534\,272 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 3\,868\,575\,552 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 52\,016\,027\,904 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \\
& 241\,951\,624\,128 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 12\,788\,596\,224 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \\
& 1\,122\,403\,392 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - 69\,984 \\
& \pi^3 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 19\,455\,552 \pi^3 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \\
& - 1\,082\,722\,464 \pi^3 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 23\,329\,866\,240 \pi^3 \sin[\beta]^6 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 217\,196\,393\,760 \pi^3 \sin[\beta]^8 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 725\,922\,896\,832 \pi^3 \sin[\beta]^{10} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 79\,877\,708\,064 \pi^3 \sin[\beta]^{12} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 1\,632\,586\,752 \pi^3 \sin[\beta]^{14} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 909\,792 \sqrt{3} \pi^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} -
\end{aligned}$$

$$\begin{aligned}
& 91\,119\,168 \sqrt{3} \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 2\,737\,984\,032 \sqrt{3} \pi^3 \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 32\,062\,189\,824 \sqrt{3} \pi^3 \sin[\beta]^6 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 127\,925\,643\,168 \sqrt{3} \pi^3 \sin[\beta]^8 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 8\,060\,897\,088 \sqrt{3} \pi^3 \sin[\beta]^{10} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} + \\
& 51\,018\,336 \sqrt{3} \pi^3 \sin[\beta]^{12} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^2 + \\
& 4 \left( -1296 \pi^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{10/3} - \right. \\
& 324 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \\
& \left( -\pi^2 + 50 \pi^2 \sin[\beta]^2 - 453 \pi^2 \sin[\beta]^4 + 36 \pi^2 \sin[\beta]^6 + \right. \\
& 5 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 78 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \sqrt{3} \pi^2 \\
& \sin[\beta]^4 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \pi^2 \left( -1 + 18 \sin[\beta]^2 + \right. \\
& 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} - 35 \pi^2 \sin[\beta]^2 \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 243 \pi^2 \sin[\beta]^4 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \\
& \left. \left. \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + 9 \pi^2 \sin[\beta]^6 \right. \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} - \right. \\
& 4 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \\
& \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} + \right. \\
& 42 \sqrt{3} \pi^2 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left. \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{1/3} \right)
\end{aligned}$$

$$\begin{aligned}
& \beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \Big)^{1/3} + 5 \pi^2 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 88 \pi^2 \sin[\beta]^2 \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 36 \pi^2 \sin[\beta]^4 \\
& \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - \\
& 15 \sqrt{3} \pi^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} - 6 \sqrt{3} \pi^2 \\
& \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \left( -1 + 18 \sin[\beta]^2 + \right. \\
& \left. 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{2/3} \Big)^3 \Big)^{1/3} / \\
& \left( 27 \times 2^{1/3} \left( -1 + 18 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^{5/3} \right) = 3 \\
& \pi, \\
& \beta]
\end{aligned}$$

A very large output was generated. Showing a sample of it.

$$\begin{aligned}
& N \left[ \frac{4 \pi}{3} + \frac{2^{1/3} \left( -1296 \pi^2 \left( -1 + \ll 1 \gg + 3 \sqrt{3} \sqrt{\ll 1 \gg^2 \ll 1 \gg} \right)^{10/3} - 324 \ll 1 \gg \ll 1 \gg \left( -\pi^2 + \ll 25 \gg \right) \right)}{27 \left( -1 + \ll 1 \gg + 3 \sqrt{3} \sqrt{\ll 1 \gg \ll 1 \gg} \right)^{5/3} \left( \ll 71 \gg + \sqrt{\ll 1 \gg^2 + 4 \ll 1 \gg} \right)^{1/3}} - \right. \\
& \left. \frac{\left( 128 304 \pi^3 - 46 049 472 \pi^3 \ll 1 \gg^2 + \ll 67 \gg + \ll 1 \gg + \sqrt{(\ll 1 \gg)^2 + 4 (\ll 1 \gg - \ll 1 \gg)^3} \right)^{1/3}}{27 \cdot 2^{1/3} \left( -1 + 18 \ll 1 \gg^2 + 3 \sqrt{3} \sqrt{\sin[\beta]^2 (-1 + 11 \ll 1 \gg^2 + \sin[\beta]^4)} \right)^{5/3}} \right] = 3 \pi, \beta]
\end{aligned}$$

show less

show more

show all

set size limit...

$$\beta := \pi / 3$$

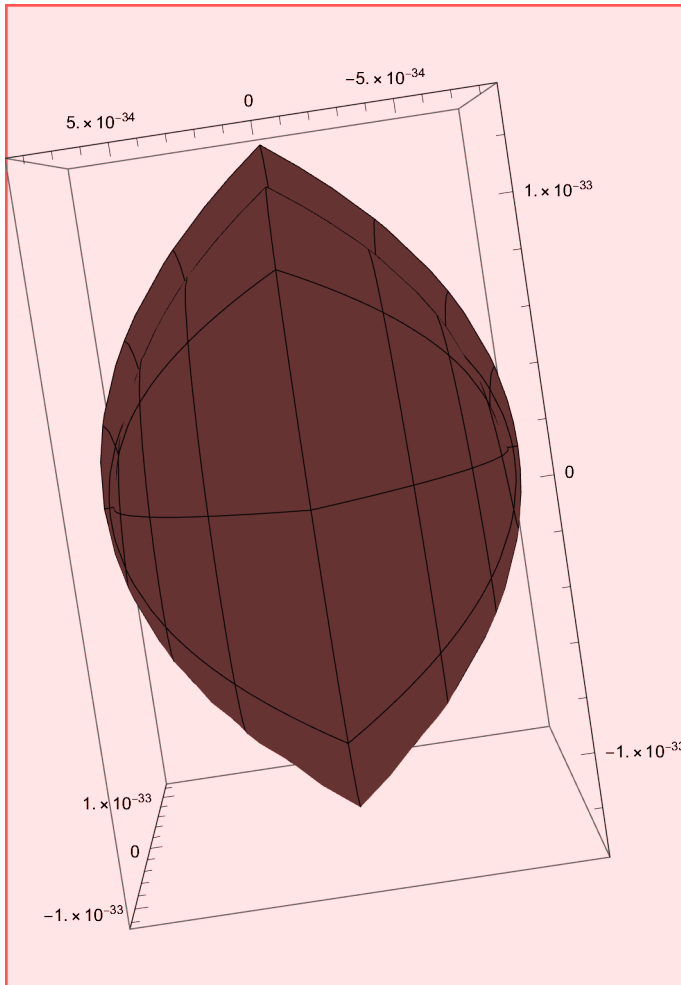
$$\theta := 3 \pi$$

$$3.911230604289641 \cdot 10^{-52} \left( 8.987551787368176 \cdot 10^{16} + \frac{8.470568000686103 \cdot 10^{17}}{4 \pi - \theta} \right) (4 \pi - \theta)$$

$$4.41738 \times 10^{-34}$$

$$\theta :=$$

$$\text{SphericalPlot3D} \left[ \frac{h \left( c^2 + \left( \frac{c \sqrt{2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}}{\sqrt{4 \pi - \theta}} \right)^2}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\} \right]$$



This shows us that the diagram of illusory contour is present within visualizaition of the energy of a wavelength of light,  $\eta$  of light.

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == 1, v\right]$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == \theta, v\right]$$

{{}}

$\theta := 2 \pi$

$$N\left[\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 \theta + \theta^2}\right)\right]$$

Indeterminate

$$N[2.99792458 \cdot 10^8]$$

$$2.99792 \times 10^8$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = 1, v\right]$$

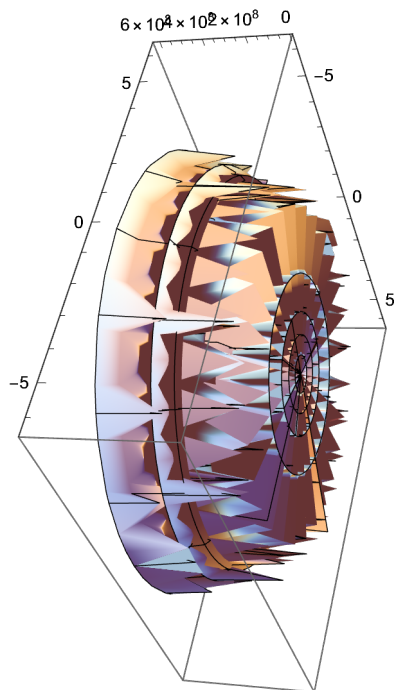
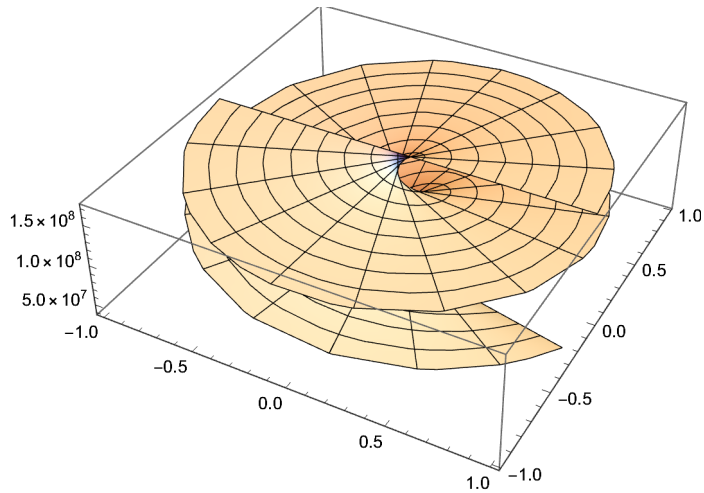
$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 - 12.5664 r^2 \theta + r^2 \theta^2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 - 12.5664 r^2 \theta + r^2 \theta^2}}\right\}\right\}$$

```

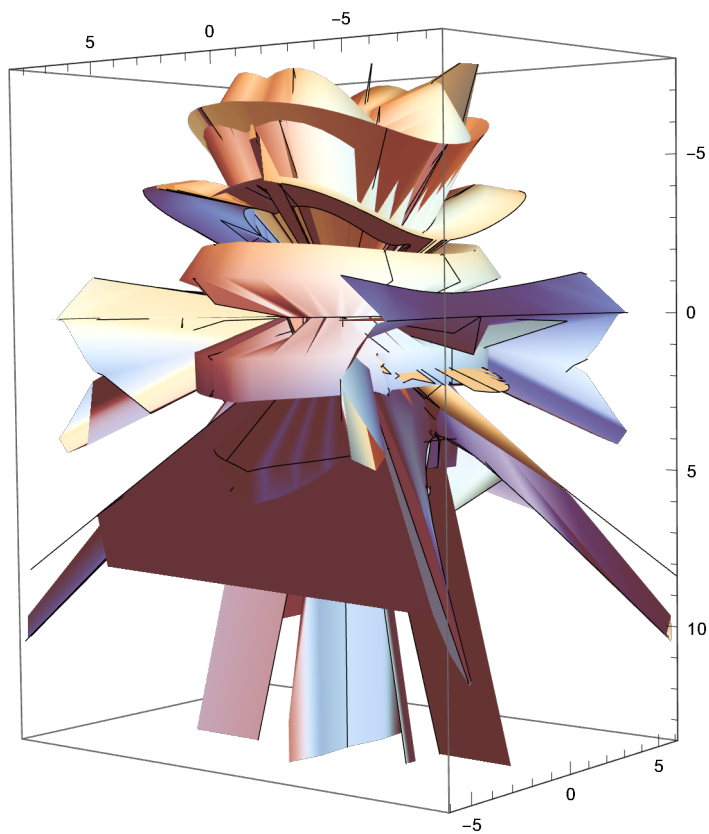
RevolutionPlot3D[
  (
    Sqrt[
      (
        3.5481432270250993`*^18 - 1.1294090667581471`*^18
        (
          (
            2 Pi Sqrt[4 Pi - theta] theta
          ) / (4 Pi - theta)
        )^2
        theta +
        8.987551787368176`*^16 r^2 theta^2
      )
    ]
  ) /
  (
    Sqrt[39.47841760435743` - 12.566370614359172` r^2 theta + r^2 theta^2]
  ), {r, -1, 1}, {theta, -2 Pi, 2 Pi}
]

```



SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta + 8.987551787368176 \cdot 10^{16} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2 \right)} \right) / \left( \sqrt{\left( 39.47841760435743 \cdot 10^{12} - 12.566370614359172 \cdot \left( \frac{2 \pi \sqrt{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \theta}}{(4 \pi - \theta) 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \right)^2 \theta + \left( \frac{2 \pi \sqrt{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \theta}}{(4 \pi - \theta) \theta} \right)^2 \right. \right. \right. \\ \left. \left. \left. \left( 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \right)^2 \right) \right) \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\} \right]$$



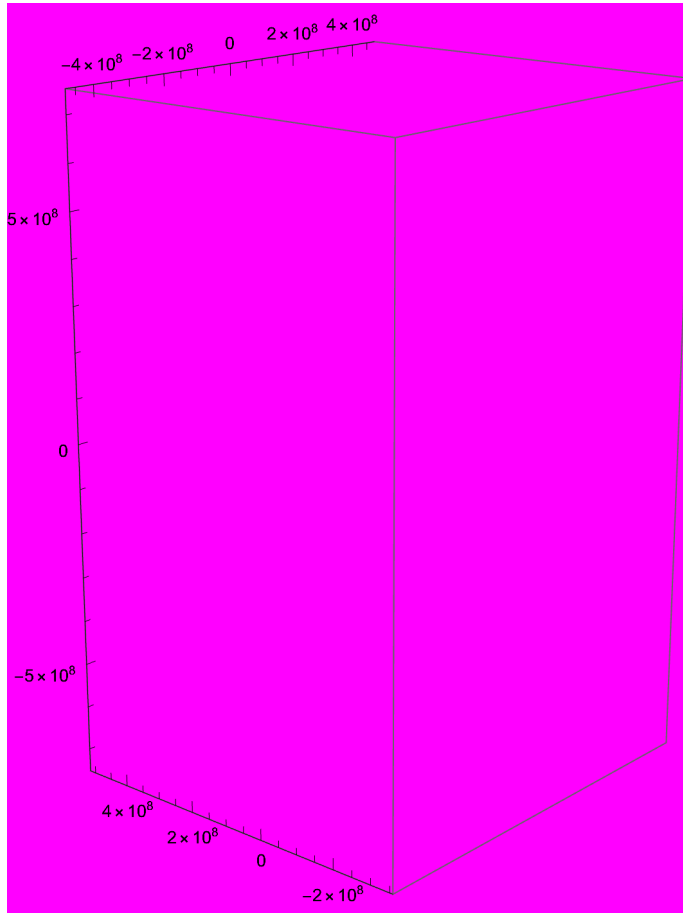


SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta + \right. \right. \\ \left. \left. 8.987551787368176 \cdot 10^{16} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{(4 \pi - \theta) \theta} \right)^2 \theta^2 \right) \right) /}$$

$$\left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 \cdot \right. \right. \\ \left. \left( \frac{2 \pi \sqrt{(4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)) \theta}}{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right)^2 \theta + \right. \\ \left. \left( \frac{2 \pi \sqrt{(4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)) \theta}}{(4 \pi - \theta) \theta} \right)^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \right),$$

{\theta, -2 \pi, 2 \pi}, {\beta, -\pi, \pi}, PlotStyle \to Opacity[.25]



SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta + \right.} \right.$$

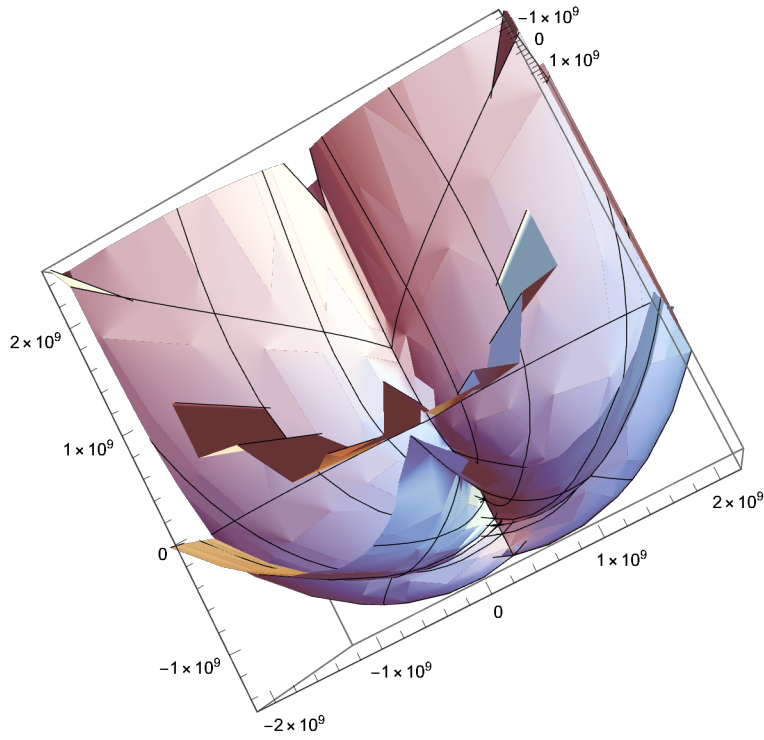
$$8.987551787368176 \cdot 10^{16} \left. \left( \frac{2 \pi \sqrt{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{(4 \pi - \theta) \theta} \right)^2 \right.$$

$$\left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \Bigg/ \left( \sqrt{\left( 39.47841760435743 - \right.} \right.$$

$$12.566370614359172 \cdot \left. \left( \frac{2 \pi \sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta}}{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right)^2 \theta + \right.$$

$$\left. \left( \frac{2 \pi \sqrt{\left( 4 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \theta}}{(4 \pi - \theta) \theta} \right)^2 \right.$$

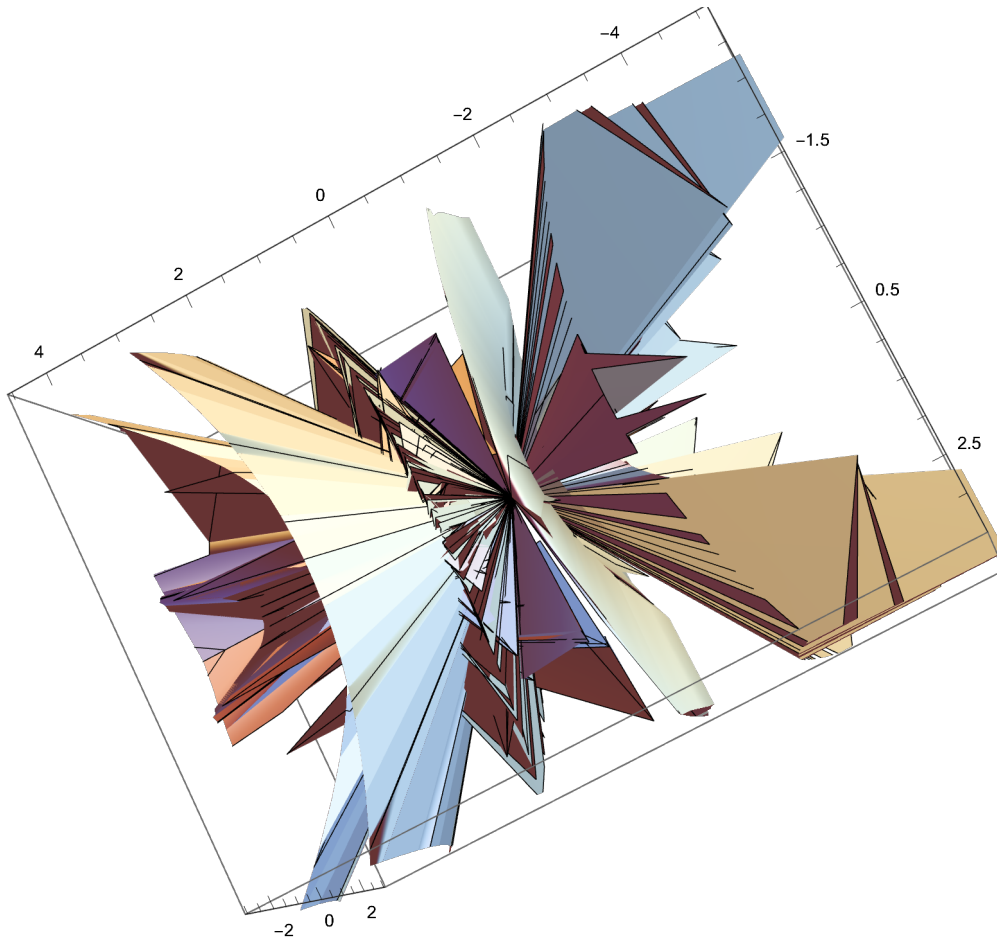
$$\left. \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \Bigg], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$$



SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta + 8.987551787368176 \cdot 10^{16} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2 \right)} \right) /$$

$$\left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 \cdot \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta + \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 \right) \right)} \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}]$$



$$\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

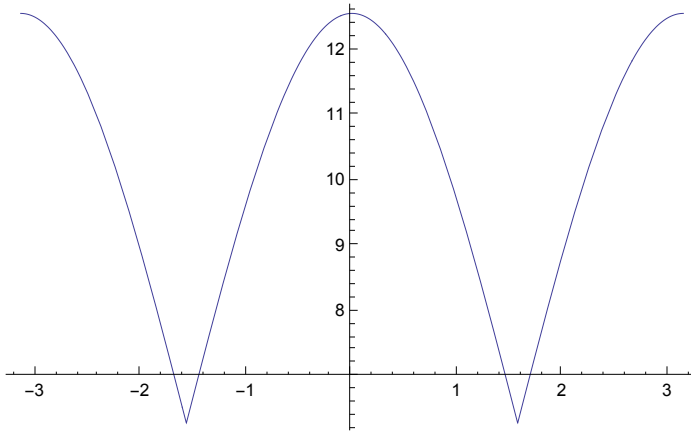
$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi}$$

$$c := 2.99792458 * (10^8)$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == r, v\right]$$

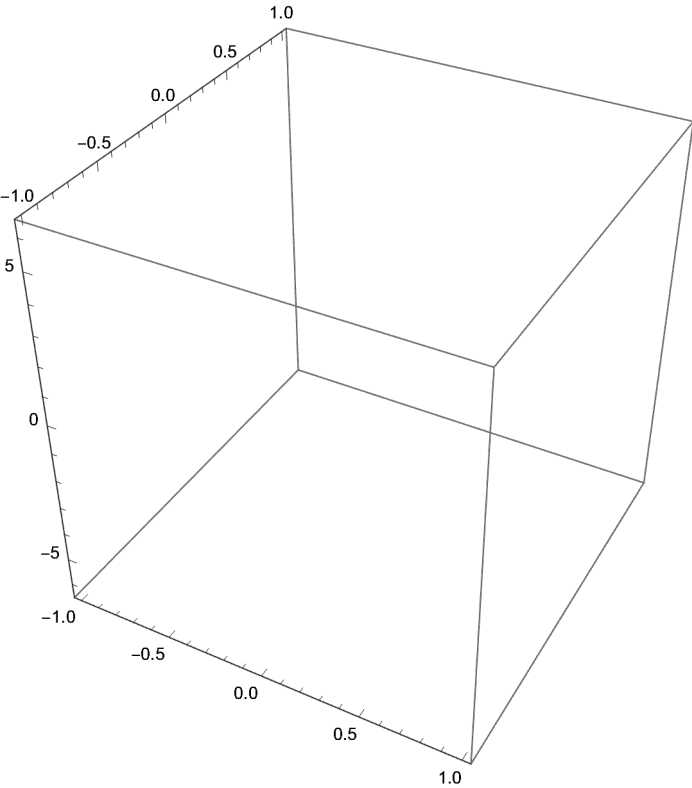
$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{\sqrt{39.4784 - 12.5664 \theta + \theta^2}}\right\},\right. \\ \left.\left\{v \rightarrow \frac{\sqrt{3.54814 \times 10^{18} - 1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2}}{\sqrt{39.4784 - 12.5664 \theta + \theta^2}}\right\}\right\}$$

$$\text{Plot}\left[2 \left(\pi + \sqrt{\pi^2 - \frac{1}{4} \left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right)}\right) 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right], \{\beta, -\pi, \pi\}]$$



$$2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)$$

$$\text{ContourPlot3D}\left[\frac{4 \pi r_1^2 + \sqrt{\frac{r^2 (4 \pi - \theta) \theta (-4 \pi^2 + 4 \pi \theta - \theta^2) r_1^2}{\pi^2} + 16 \pi^2 r_1^4}}{2 r_1^2},\right. \\ \left.\{r, -1, 1\}, \{r_1, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$



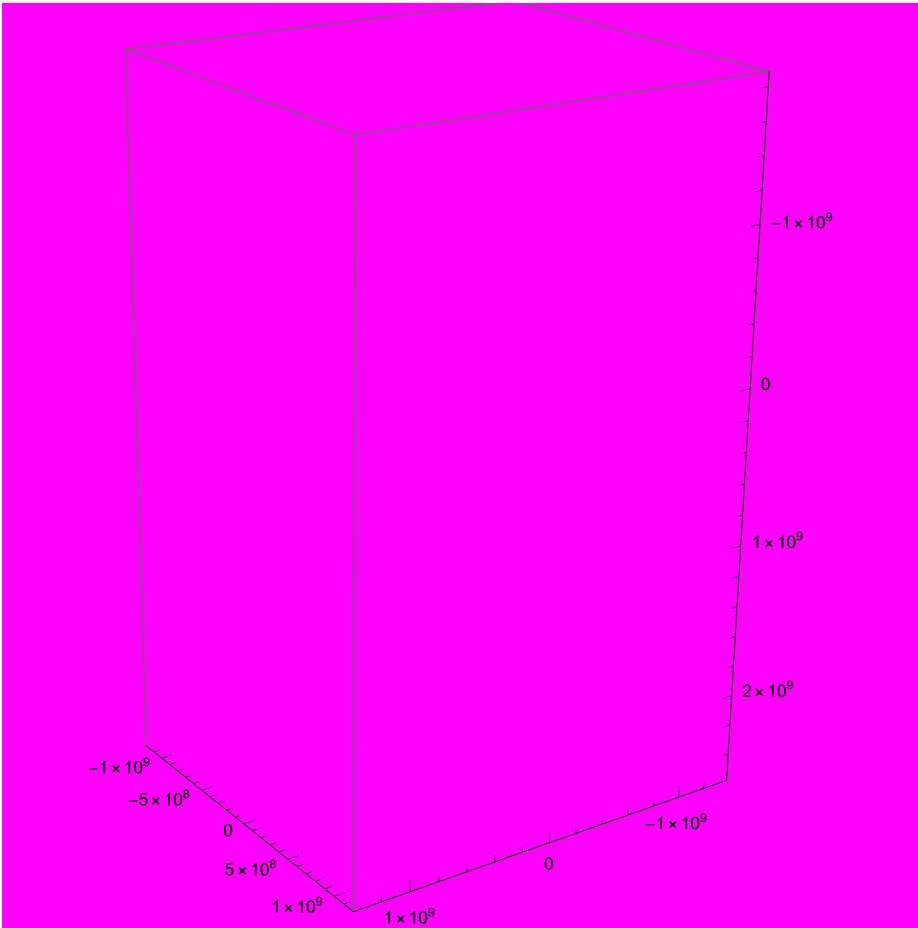
$$r = \frac{2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \sqrt{4 \pi - \theta_1} \sqrt{\theta_1}$$

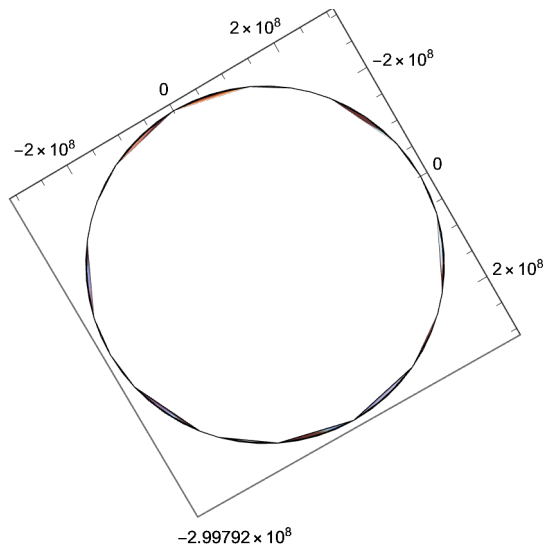
```

SphericalPlot3D[
  (
    Sqrt[
      (
        3.5481432270250993`*^18 - 1.1294090667581471`*^18
        (
          (2 π Sqrt[(4 π - θ) θ])^2
          (4 π - θ) θ
        )^2
        (
          (π + Sqrt[π^2 - π^2 Sin[β]^2]) + 8.987551787368176`*^16
          (
            (2 π Sqrt[(4 π - θ) θ])^2
            (4 π - θ) θ
          )^2
          (θ)^2
        )
      )
    ]
  )
  (
    Sqrt[
      (
        39.47841760435743` - 12.566370614359172`
        (
          (2 π Sqrt[(4 π - 2 (π + Sqrt[π^2 - π^2 Sin[β]^2]) θ])^2
          (4 π - θ) θ
        )^2
        (
          (π + Sqrt[π^2 - π^2 Sin[β]^2]) + (
            (2 π Sqrt[(4 π - θ) θ])^2
            (4 π - θ) θ
          )^2
          (θ)^2
        )
      )
    ]
  )
  {θ, -2 π, 2 π}, {β, -π, π}, PlotStyle -> Opacity[.75]
]

```





$$\text{RevolutionPlot3D}\left[\left\{\left(\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 r^2 \theta + r^2 \theta^2}\right),\right. \\ \left.-\left(1. \cdot \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 - 12.566370614359172 r^2 \theta + r^2 \theta^2}\right)\right\}, \\ \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$$


# The Paradox of Time and Cyclicity

## by Parker Emmerson

$$\theta = 2\pi * \text{time} = 2\pi t$$

Please refer to the work entitled Math for Transforming a Circle into a cone if questions are raised of proof.

From this, we can mathematically prove that if time is measured like a clock by the cyclically passing angle, there is by definition no time. That is  $\text{time} = 0$ , yet time does have continuous expressions and solutions.

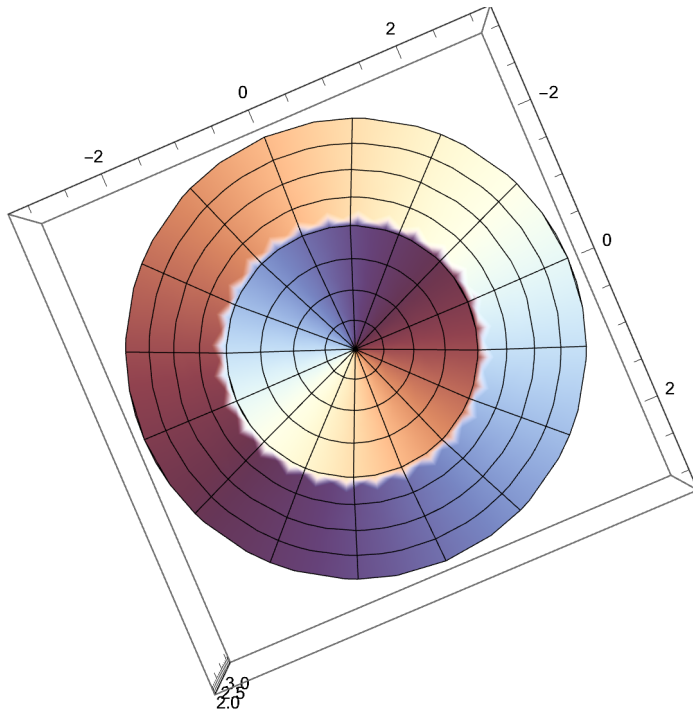
$$2 \pi r - 2 \pi r_1 = \theta r = 2 \pi r - 2 \pi (r \cos[\beta])$$

**Solve** $[\theta \text{ r} == 2 \pi \text{ r} - 2 \pi (\text{r Cos}[\beta]), \beta]$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcCos}\left[\frac{2 \pi - \theta}{2 \pi}\right] \right\}, \left\{ \beta \rightarrow \text{ArcCos}\left[\frac{2 \pi - \theta}{2 \pi}\right] \right\} \right\}$$

$$\left\{ \left\{ \beta \rightarrow -\text{ArcCos}\left[\frac{2 \pi - \theta}{2 \pi}\right] \right\}, \left\{ \beta \rightarrow \text{ArcCos}\left[\frac{2 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)}{2 \pi}\right] \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\text{ArcCos}\left[\frac{2 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)}{2 \pi}\right], \{\beta, -\pi, \pi\}\right]$$



$$\text{Solve}\left[-\text{ArcCos}\left[\frac{2 \pi - \theta}{2 \pi}\right] == \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right], \theta\right]$$

$$\{\{\theta \rightarrow 0\}, \{\}\}$$

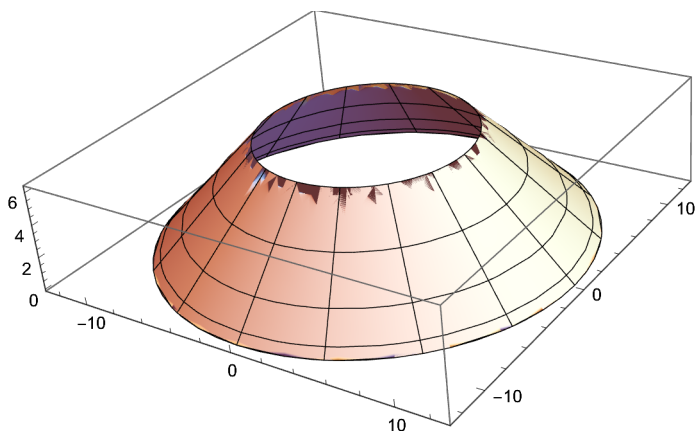
$$\text{Solve}\left[\text{ArcCos}\left[\frac{2 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)}{2 \pi}\right] == \text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right], \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \left( 1 - \frac{\left( 2 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)^2}{4 \pi^2} \right)^2} \right)} \right) \right\}, \right.$$

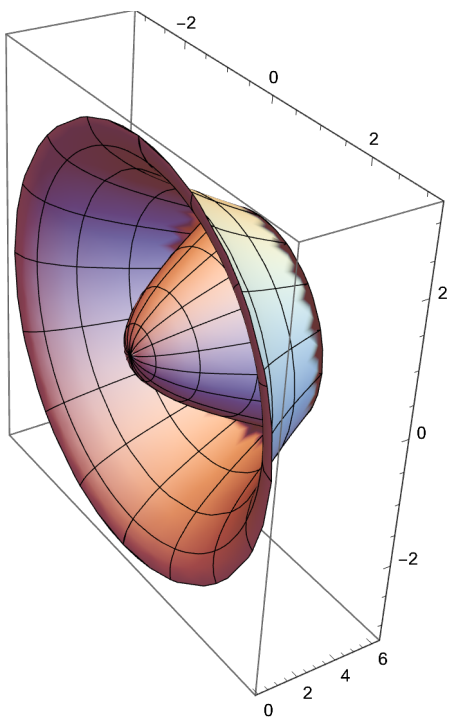
$$\left. \left\{ \theta \rightarrow 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \left( 1 - \frac{\left( 2 \pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)^2}{4 \pi^2} \right)^2} \right)} \right) \right\} \right\}$$

$$\text{RevolutionPlot3D}\left[\left\{2\left(\pi + \sqrt{\pi^2 - \pi^2 \left(1 - \frac{(2\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))^2}{4\pi^2}\right)}\right),\right.\right.$$

$$\left.\left.2\left(\pi - \sqrt{\pi^2 - \pi^2 \left(1 - \frac{(2\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))^2}{4\pi^2}\right)}\right)\right\}, \{\beta, -\pi, \pi\}\right]$$



$$\text{RevolutionPlot3D}\left[2\left(\pi - \sqrt{\pi^2 - \pi^2 \left(1 - \frac{(2\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}))^2}{4\pi^2}\right)}\right), \{\beta, -\pi, \pi\}\right]$$



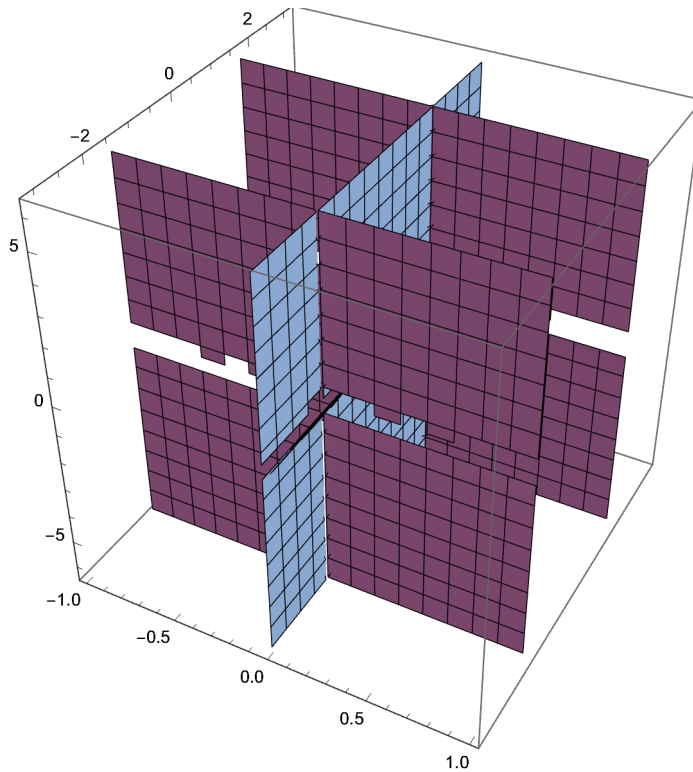
$$\text{Solve}\left[\text{ArcCos}\left[\frac{2\pi - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{2\pi}\right] == \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right], \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right\}\right\}$$

$$\text{D}\left[\left((r \sin[\beta]) / (\theta / (2\pi))\right), \theta, \beta\right] = \text{D}[v, v] = 1$$

$$-\frac{2\pi r \cos[\beta]}{\theta^2} = 1$$

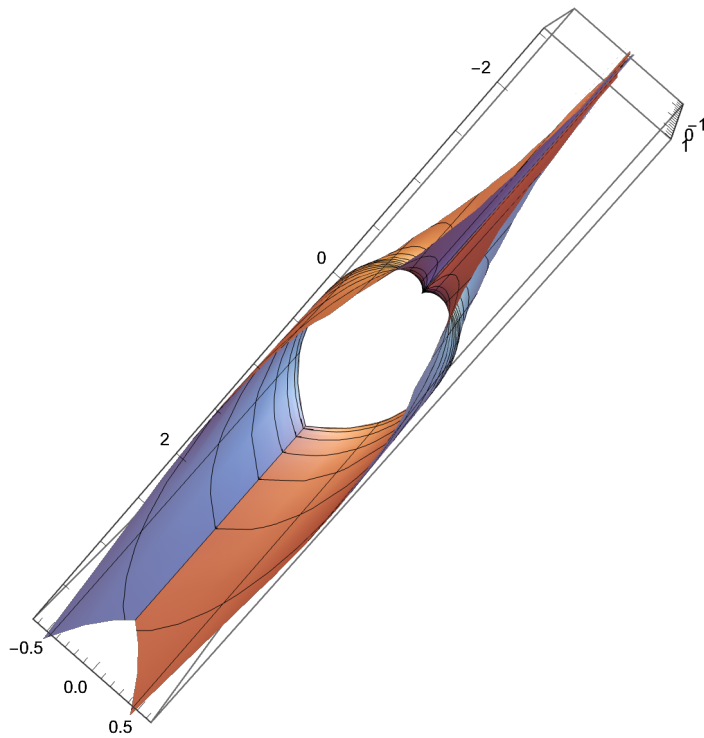
$$\text{ContourPlot3D}\left[-\frac{2\pi r \cos[\beta]}{\theta^2}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]$$



$$\text{Solve}\left[-\frac{2\pi r \cos[\beta]}{\theta^2} == 1, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\theta^2 \sec[\beta]}{2\pi}\right\}\right\}$$

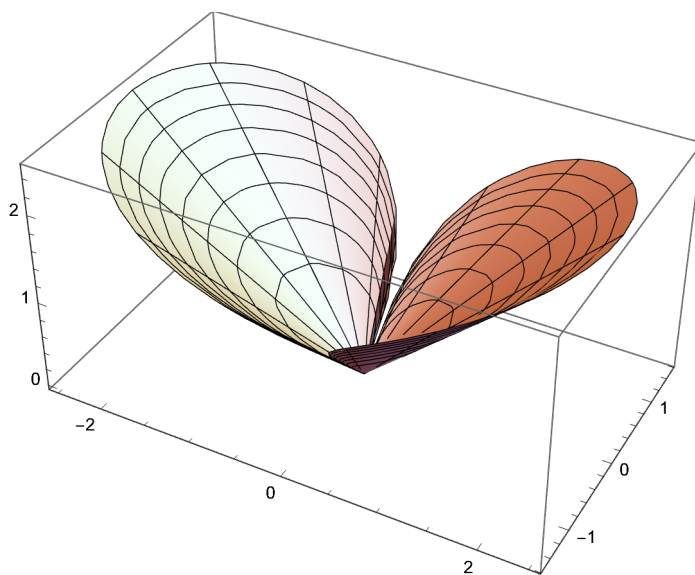
`SphericalPlot3D` $\left[-\frac{\theta^2 \operatorname{Sec}[\beta]}{2 \pi}, \{\theta, -\pi, \pi\}, \{\beta, -.5 \pi, .5 \pi\}\right]$



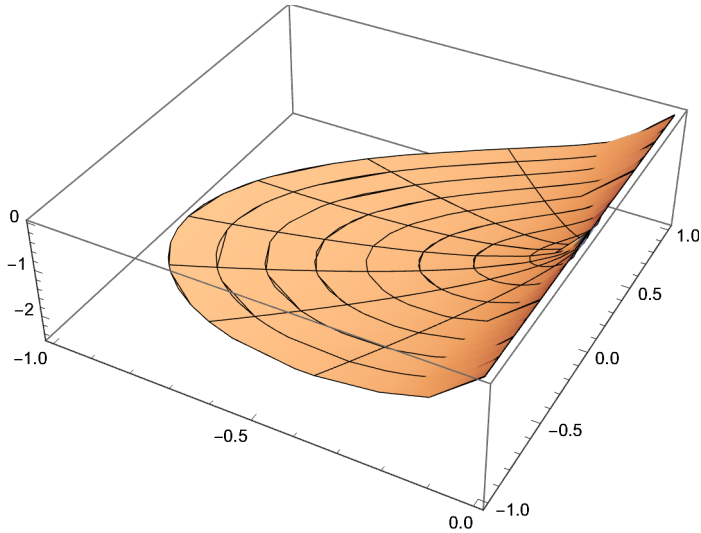
`Solve` $\left[-\frac{2 \pi r \operatorname{Cos}[\beta]}{\theta^2} == 1, \theta\right]$

$\{\{\theta \rightarrow -i \sqrt{2 \pi} \sqrt{r} \sqrt{\operatorname{Cos}[\beta]}\}, \{\theta \rightarrow i \sqrt{2 \pi} \sqrt{r} \sqrt{\operatorname{Cos}[\beta]}\}\}$

`RevolutionPlot3D` $\left[\{i \sqrt{2 \pi} \sqrt{r} \sqrt{\operatorname{Cos}[\beta]}, -i \sqrt{2 \pi} \sqrt{r} \sqrt{\operatorname{Cos}[\beta]}\}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$



`RevolutionPlot3D[ $\pm \sqrt{2\pi} \sqrt{r} \sqrt{\cos[\beta]}$ , {r, -1, 1}, { $\beta$ , - $\pi$ ,  $\pi$ }]`



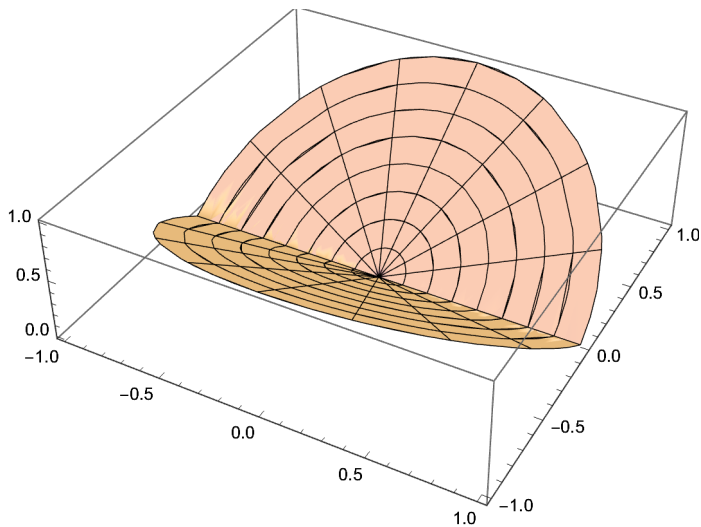
$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$2\pi r - 2\pi r_1 = \theta r = 2\pi r - 2\pi (r \cos[\beta]) = 2\pi r - 2\pi \sqrt{r^2 - \eta^2}$$

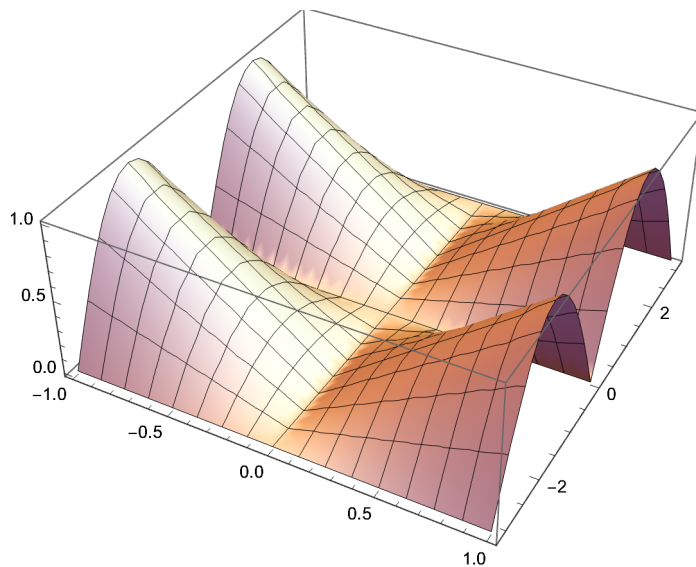
$$\text{Solve}\left[2\pi r - 2\pi (r \cos[\beta]) == 2\pi r - 2\pi \sqrt{r^2 - \eta^2}, \eta\right]$$

$$\left\{ \left\{ \eta \rightarrow -\sqrt{r^2 - r^2 \cos[\beta]^2} \right\}, \left\{ \eta \rightarrow \sqrt{r^2 - r^2 \cos[\beta]^2} \right\} \right\}$$

`RevolutionPlot3D[ $\sqrt{r^2 - r^2 \cos[\beta]^2}$ , {r, -1, 1}, { $\beta$ , - $\pi$ ,  $\pi$ }]`



`Plot3D[ $\sqrt{r^2 - r^2 \cos[\beta]^2}$ , {r, -1, 1}, { $\beta$ , - $\pi$ ,  $\pi$ }]`



`Solve[ $\sqrt{r^2 - r^2 \cos[\beta]^2} == r \cos[\beta]$ ,  $\beta$ ]`

`{{ $\beta \rightarrow -\frac{3\pi}{4}$ }, { $\beta \rightarrow -\frac{\pi}{4}$ }, { $\beta \rightarrow \frac{\pi}{4}$ }, { $\beta \rightarrow \frac{3\pi}{4}$ }}`

$$\theta = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin\left[\frac{3\pi}{4}\right]^2} \right)$$

$$2 \left( \pi + \frac{\pi}{\sqrt{2}} \right)$$

$$2 \left( \pi + \frac{\pi}{\sqrt{2}} \right) / (2\pi)$$

$$\frac{\pi + \frac{\pi}{\sqrt{2}}}{\pi} = t$$

$$\theta = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin\left[\frac{\pi}{4}\right]^2} \right)$$

$$2 \left( \pi + \frac{\pi}{\sqrt{2}} \right)$$

$$\theta = 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin\left[-\frac{\pi}{4}\right]^2} \right)$$

$$2 \left( \pi + \frac{\pi}{\sqrt{2}} \right)$$



$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin \left[ -\frac{3\pi}{4} \right]^2} \right)$$

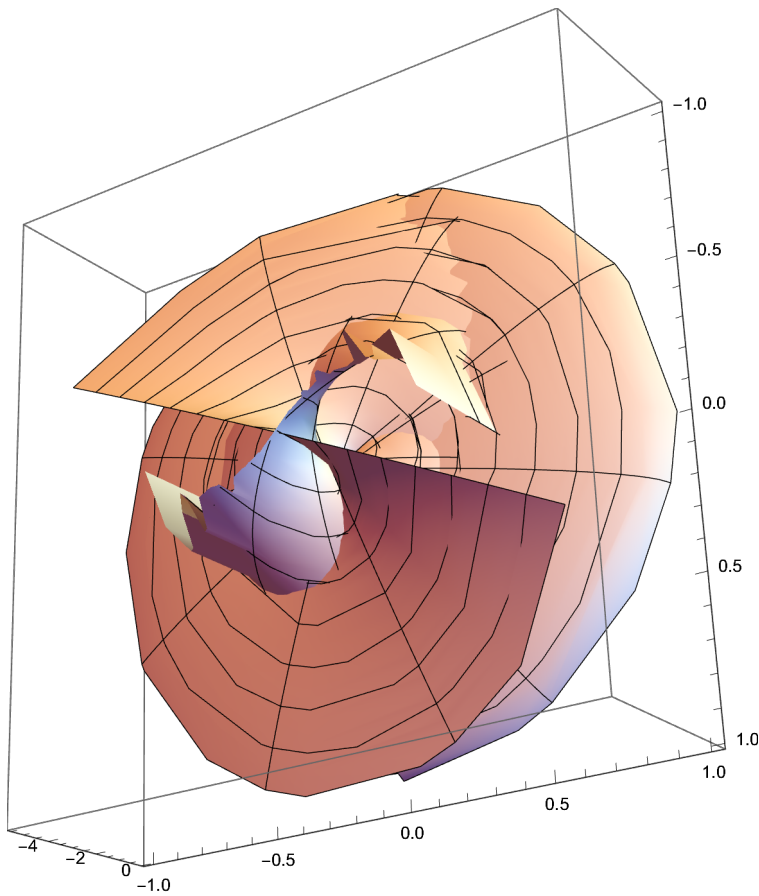
$$2 \left( \pi + \frac{\pi}{\sqrt{2}} \right)$$

$$\theta = 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin \left[ \frac{3\pi}{4} \right]^2} \right)$$

$$2 \left( \pi - \frac{\pi}{\sqrt{2}} \right)$$

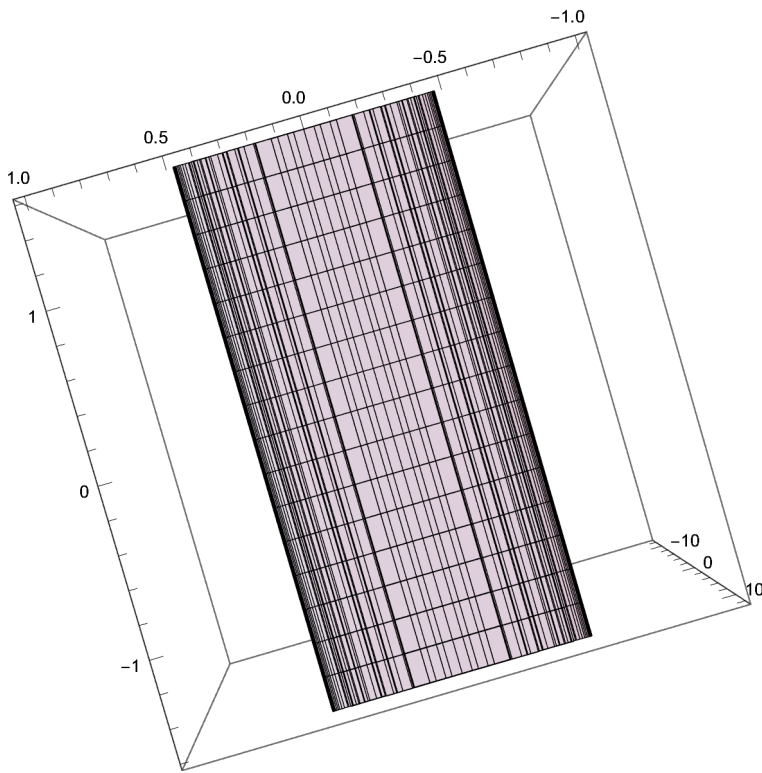
RevolutionPlot3D[

$$\begin{aligned}
 & -\frac{1}{4\pi^2} \left( \sqrt{64\pi^4 \left( \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 - \frac{256\pi^5 r^2}{4\pi-\theta} + 16\pi^3 r^2 \theta + 4\pi^2 \left( \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2 +} \right. \\
 & \quad \left. r^2 \theta^4 + 16\pi^3 r \sqrt{r^2(4\pi-\theta)\theta} - \frac{64\pi^4 \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta} + \right. \\
 & \quad \left. 8\pi^2 r \theta \sqrt{\left( \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 (4\pi-\theta)\theta} \right), \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}
 \end{aligned}$$

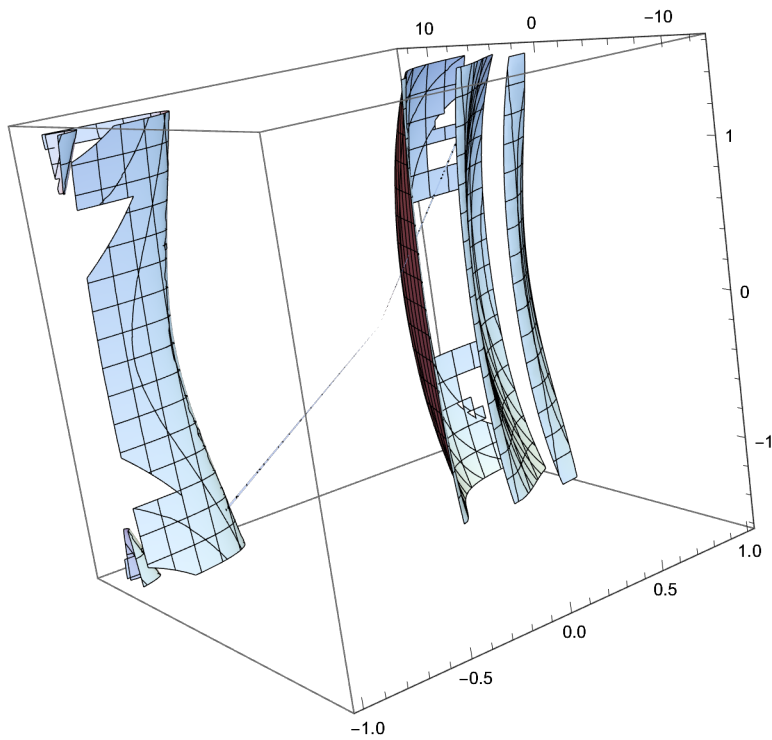


ContourPlot3D[  

$$-\frac{1}{4\pi^2} \left( \sqrt{64\pi^4 \left( \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 - \frac{256\pi^5 r^2}{4\pi-\theta} + 16\pi^3 r^2 \theta + 4\pi^2 \left( \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2(4\pi-\theta)2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} - \frac{64\pi^4 \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta} + 8\pi^2 r \theta \sqrt{\left( \frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 (4\pi-\theta)\theta}} \right),$$
  
 $\{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]



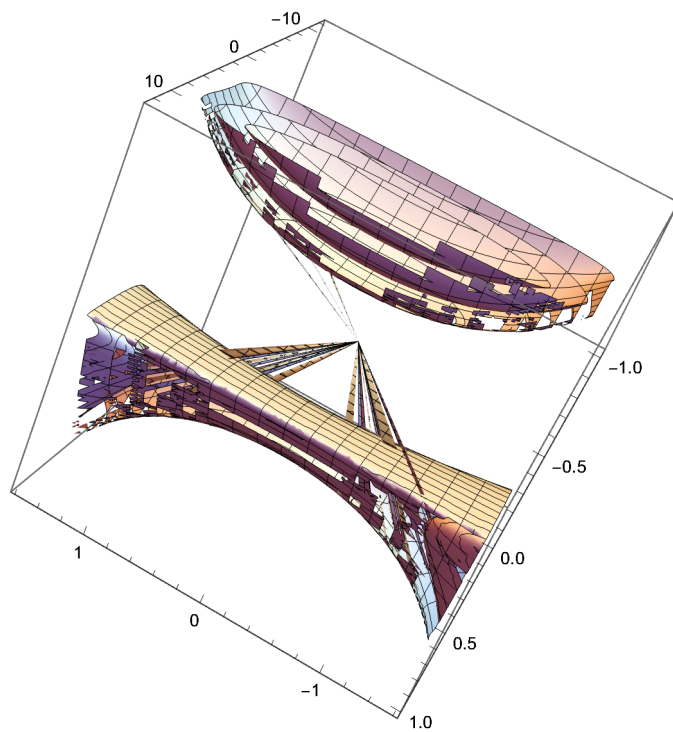
$\text{ContourPlot3D}\left[-\frac{1}{4\pi^2}\left(\sqrt{\left(64\pi^4(r)^2-\frac{256\pi^5r^2}{4\pi-\theta}+16\pi^3r^2\theta+\right.}\right.\right.$   
 $\left.\left.4\pi^2(r)^2\theta^2+r^2\theta^4+16\pi^3r\sqrt{r^2(4\pi-\theta)2\left(\pi+\sqrt{\pi^2-\pi^2\text{Sin}[\beta]^2}\right)}-\right.\right.$   
 $\left.\left.\frac{64\pi^4r\sqrt{r^2(4\pi-\theta)\theta}}{4\pi-\theta}+8\pi^2r\theta\sqrt{(r)^2(4\pi-\theta)\theta}\right)\right],$   
 $\{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi/2, \pi/2\}$



ContourPlot3D[

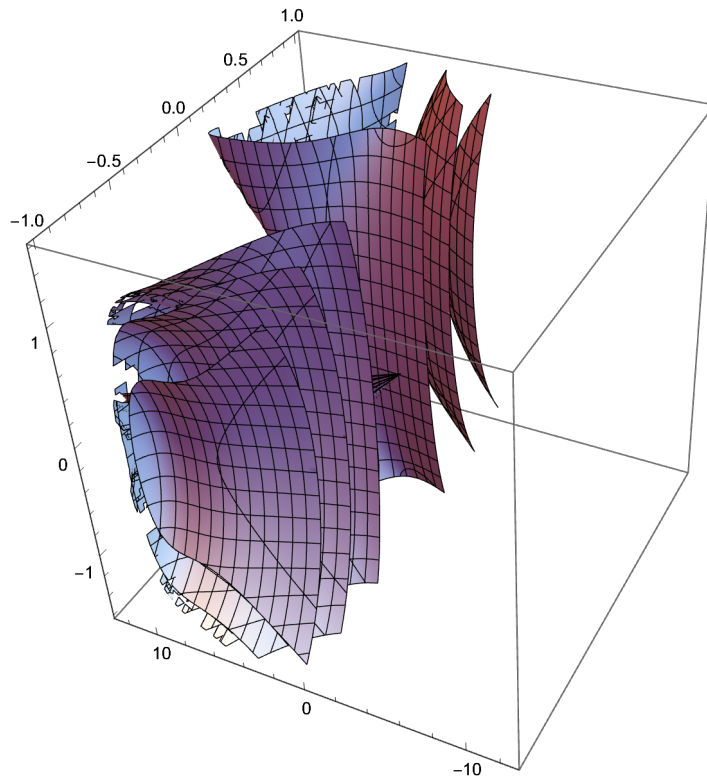
$$-\frac{1}{4\pi^2} \left( \sqrt{64\pi^4 (r)^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 \theta + 4\pi^2 (r)^2 \theta^2 + r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + 8\pi^2 r \theta \sqrt{\left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \right)^2 (4\pi - \theta) \theta} \right),$$

{r, -1, 1}, {θ, -4π, 4π}, {β, -π/2, π/2}]



ContourPlot3D[

$$\begin{aligned}
 & -\frac{1}{4\pi^2} \left( \sqrt{64\pi^4 (r)^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 4\pi^2 (r)^2 \theta^2 +} \right. \\
 & \quad \left. r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + \right. \\
 & \quad \left. 8\pi^2 r \theta \sqrt{\left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right)^2 (4\pi - \theta) \theta} \right), \\
 & \{r, -1, 1\}, \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi/2, \pi/2\}
 \end{aligned}$$



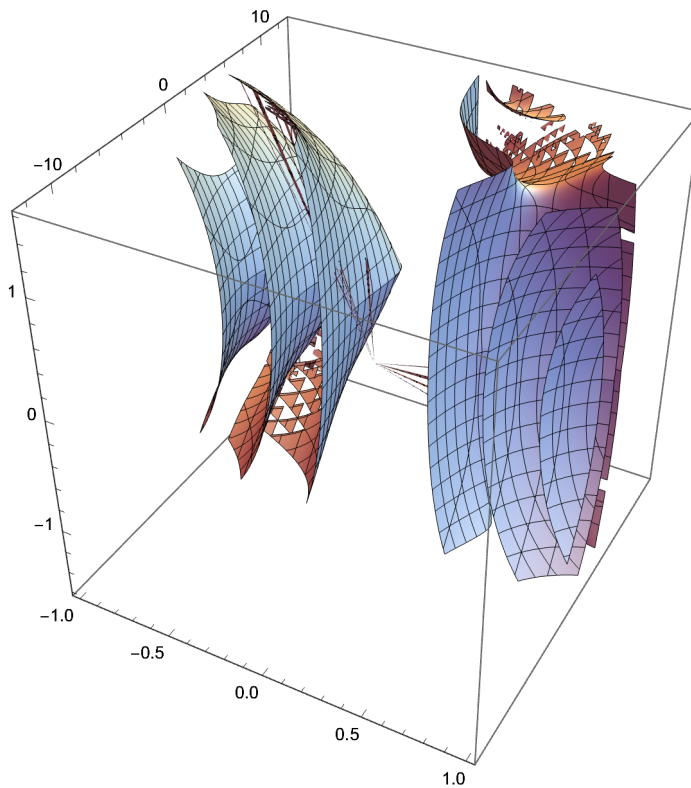
ContourPlot3D[

$$-\frac{1}{4\pi^2} \left( \sqrt{\left( 64\pi^4 (r)^2 - \frac{256\pi^5 r^2}{4\pi - \theta} + 16\pi^3 r^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 4\pi^2 (r)^2 \theta^2 + \right.} \right.$$

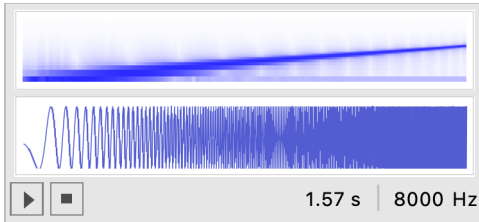
$$\left. r^2 \theta^4 + 16\pi^3 r \sqrt{r^2 (4\pi - \theta) \theta} - \frac{64\pi^4 r \sqrt{r^2 (4\pi - \theta) \theta}}{4\pi - \theta} + \right.$$

$$\left. 8\pi^2 r \theta \sqrt{\left( \frac{2\pi \sqrt{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \theta)}^2}{(4\pi - \theta) 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} (4\pi - \theta) \theta \right)} \right),$$

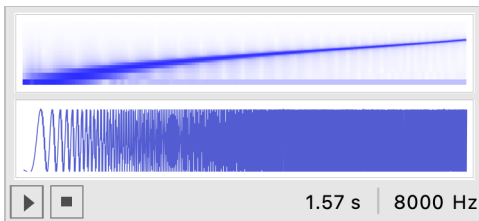
{r, -1, 1}, {θ, -4π, 4π}, {β, -π/2, π/2}]



$$\begin{aligned} & \text{Play}\left[\text{Sin}\left[500\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right.\right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \right. \\ & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right] + \\ & \text{Cos}\left[500\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\ & \quad \left.\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right], \{\beta, \pi/2, \pi\}] \end{aligned}$$

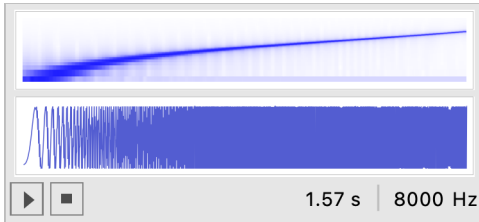


$$\begin{aligned} & \text{Play}\left[\text{Sin}\left[1000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right.\right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \right. \\ & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right] + \\ & \text{Cos}\left[1000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\ & \quad \left.\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right], \{\beta, \pi/2, \pi\}] \end{aligned}$$

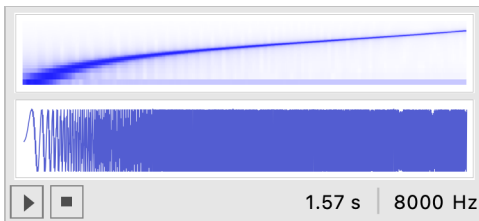




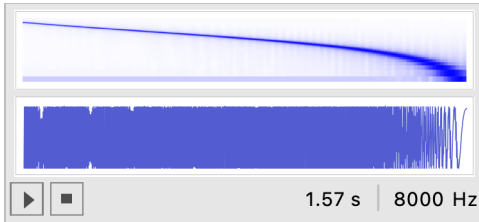
$$\begin{aligned} & \text{Play}\left[\text{Sin}\left[1500\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right.\right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \right. \\ & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right] + \\ & \text{Cos}\left[1500\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\ & \quad \left.\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + \right.\right. \\ & \quad \left.\left.3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right], \{\beta, \pi/2, \pi\}] \end{aligned}$$



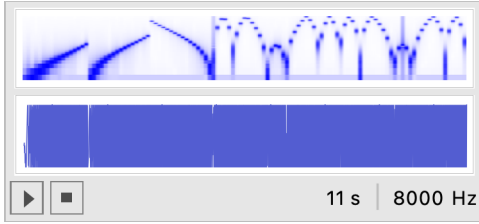
$$\begin{aligned} & \text{Play}\left[\text{Sin}\left[2000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right.\right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \right. \\ & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right] + \\ & \text{Cos}\left[2000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right. \\ & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\ & \quad \left.\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + \right.\right. \\ & \quad \left.\left.3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right], \{\beta, \pi/2, \pi\}] \end{aligned}$$



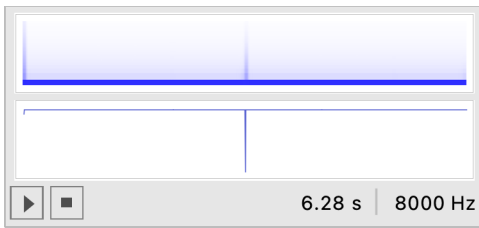
$$\begin{aligned}
 & \text{Play}\left[\text{Sin}\left[3000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right.\right. \\
 & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \right. \\
 & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right] + \\
 & \text{Cos}\left[3000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2)\right) / \right. \\
 & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right. \\
 & \quad \left.\left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + \right.\right. \\
 & \quad \left.\left.3\sqrt{3}\sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right)\right], \{\beta, -\pi, -\pi/2\}]
 \end{aligned}$$



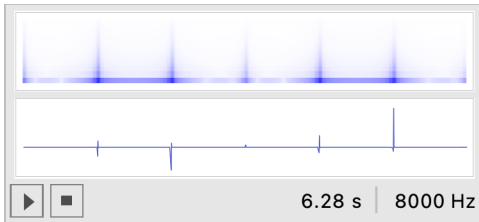
$$\begin{aligned}
& \text{Sound} \left[ \left\{ \text{Play} \left[ \text{Sin} \left[ 500 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2) \right) / \right. \right. \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right] + \\
& \quad \text{Cos} \left[ 500 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right], \\
& \quad \{\beta, \pi/2, \pi\} \right], \text{Play} \left[ \text{Sin} \left[ 1000 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2) / \right. \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right] + \\
& \quad \text{Cos} \left[ 1000 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right], \\
& \quad \{\beta, \pi/2, \pi\} \right], \text{Play} \left[ \text{Sin} \left[ 3000 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2) / \right. \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right] + \\
& \quad \text{Cos} \left[ 3000 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2) / \right. \right. \\
& \quad \left( 6 \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) + \\
& \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6} \right)^{1/3} \right) \right], \\
& \quad \{\beta, -\pi, -\pi/2\} \right], \text{Play} \left[ \text{Sin} \left[ \pi^8 \sqrt{3} 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right] + \right. \\
& \quad \text{Cos} \left[ \pi^8 \sqrt{3} 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right], \{\beta, \\
& \quad \left. -\pi, \pi\} \right] \} \}
\end{aligned}$$



$$\text{Play}\left[\left[\frac{\sqrt{5}}{\left(1 + \sqrt[5]{5^{3/4} \left(\frac{\sqrt{5}-1}{2}\right)^{5/2} - 1}\right)} - \frac{(\sqrt{5} + 1)}{2}\right] e^{((2\pi)/\sqrt{5})} / \sin\left[2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right], \{\beta, -\pi, \pi\}\right]$$

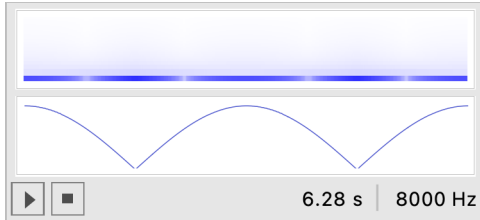


$$\text{Play}\left[\left[\frac{\sqrt{5}}{\left(1 + \sqrt[5]{5^{3/4} \left(\frac{\sqrt{5}-1}{2}\right)^{5/2} - 1}\right)} - \frac{(\sqrt{5} + 1)}{2}\right] e^{((2\pi)/\sqrt{5})} / \sin\left[\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right) / \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3}\right] \right. \\ \left. \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right], \{\beta, -\pi, \pi\}\right]$$



$$\text{Play}\left[\frac{\sqrt{5}}{\left(1+\sqrt[5]{5^{3/4}\left(\frac{\sqrt{5}-1}{2}\right)^{5/2}-1}\right)}-\frac{(\sqrt{5}+1)}{2}\right]$$

$$e^{(2\pi)/\sqrt{5}}2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right),\{\beta,-\pi,\pi\}]$$



$$\left(\frac{4\pi}{3}-(-4\pi^2+12\pi^2\sin[\beta]^2)\right)/$$

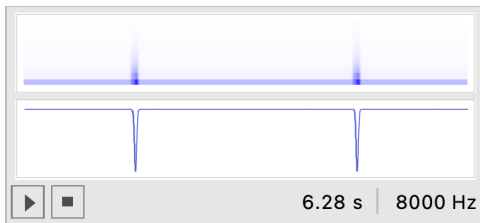
$$\left(6\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)+$$

$$\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}$$

$$\text{Play}\left[\sin\left[5000\left(\left(\frac{4\pi}{3}+\left((1-i\sqrt{3})\left(-4\pi^2+12\pi^2\sin[\beta]^2\right)\right)\right)/\right.\right.\right.$$

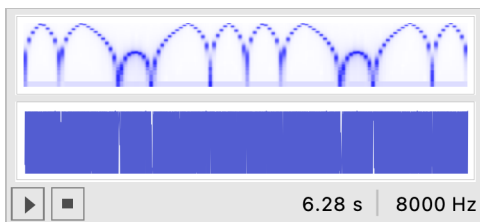
$$\left.\left.\left(12\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)-\right.\right.$$

$$\left.\left.\frac{1}{3}\left(1+i\sqrt{3}\right)\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)\right)/(2\pi)\right],\{\beta,-\pi,\pi\}]$$

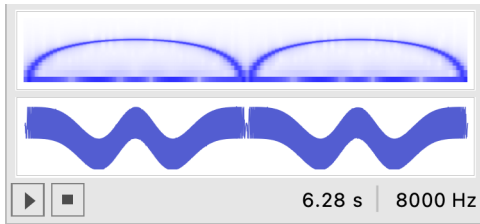


$$\text{Play}\left[\sin\left[\pi^8\sqrt{3}2\left(\pi-\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right]+\right.$$

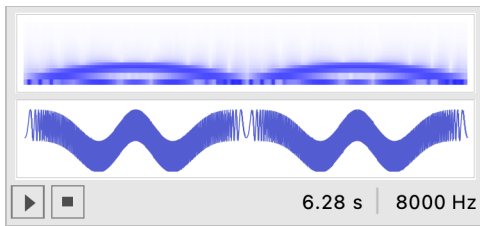
$$\left.\cos\left[\pi^8\sqrt{3}2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right],\{\beta,-\pi,\pi\}\right]$$



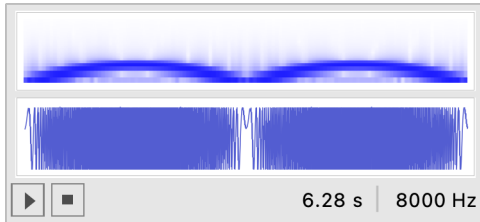
$$\text{Play}\left[\text{Sin}\left[800 \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right] + \text{Cos}\left[2 \left(\pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right], \{\beta, -\pi, \pi\}\right]$$



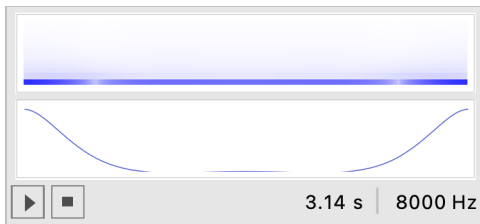
$$\text{Play}\left[\text{Sin}\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) / (2\pi)\right] + \text{Cos}\left[2 \left(\pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) / (2\pi)\right], \{\beta, -\pi, \pi\}\right]$$



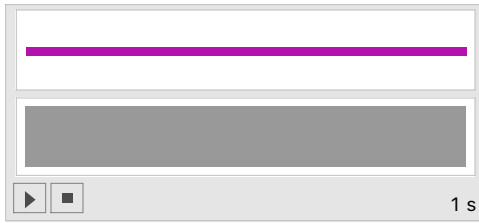
$$\text{Play}\left[\text{Sin}\left[800 \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) / (2\pi)\right] + \text{Cos}\left[800 \times 2 \left(\pi - \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) / (2\pi)\right], \{\beta, -\pi, \pi\}\right]$$



$$\text{Play}\left[i \text{Sin}\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right)\right] + \text{Cos}\left[\frac{4\pi}{3} - \frac{-4\pi^2 + 12\pi^2 \text{Sin}[\beta]^2}{6 \left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}} + \frac{2}{3} \left(-\pi^3 + 18\pi^3 \text{Sin}[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11\pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right], \{\beta, 0, \pi\}\right]$$



```
Sound[SoundNote["G", 1, "Violin"]]
```



```
Sound[SoundNote["G", 100, "Violin"]]
```

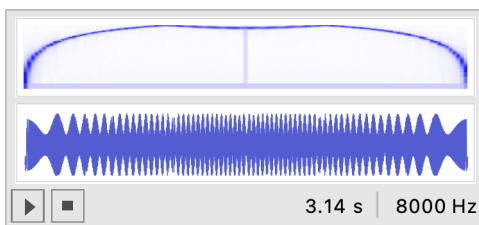


```
Play[ (2 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / (2 π))]) *  
      Sin[3000 (2 (π + √(π² - π² Sin[β]²)) / (2 π)) +  
          2 Sin[50 (2 (π + √(π² - π² Sin[β]²)) / (2 π))]]], {β, 0, -π}]
```

```
Export["sound1.aif", Play[  
      (2 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / (2 π))]) * Sin[3000 (2 (π + √(π² - π² Sin[β]²)) / (2 π)) +  
          2 Sin[50 (2 (π + √(π² - π² Sin[β]²)) / (2 π))]]], {β, 0, π}]]
```

\$Failed

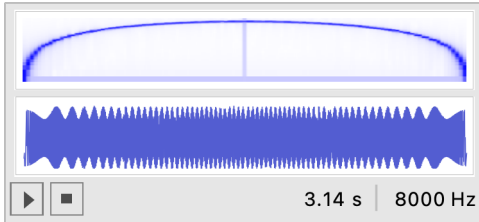
```
Play[ (2 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / (2 π))]) *  
      Sin[3000 (2 (π + √(π² - π² Sin[β]²)) / (2 π)) +  
          2 Sin[50 (2 (π + √(π² - π² Sin[β]²)) / (2 π))]]], {β, 0, π}]
```

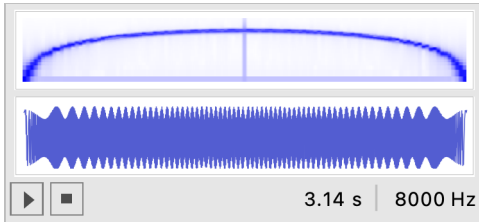


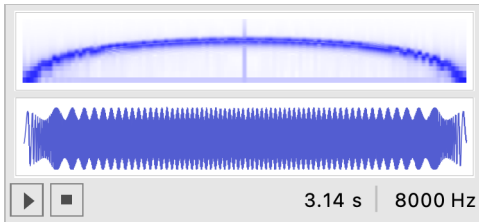
```
EmitSound[Sound[Sin[(2 (π + √(π² - π² Sin[β]²)) / (2 π)) ^ 2], {β, 0, π}]]]
```

Play

## The Sounds of Pure Time

$$\text{Play}\left[\left(4 + \cos\left[20\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right]\right) * \right. \\ \left. \sin\left[2000\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right) + \right. \right. \\ \left. \left. 2 \sin\left[40\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right]\right], \{\beta, 0, \pi\}\right]$$


$$\text{Play}\left[\left(4 + \cos\left[20\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right]\right) * \right. \\ \left. \sin\left[1000\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right) + \right. \right. \\ \left. \left. 2 \sin\left[40\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right]\right], \{\beta, 0, \pi\}\right]$$


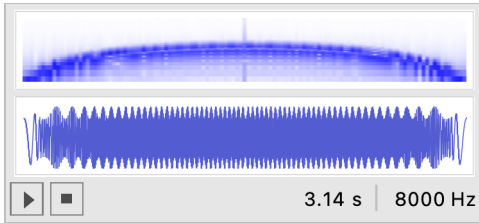
$$\text{Play}\left[\left(4 + \cos\left[20\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right]\right) * \right. \\ \left. \sin\left[500\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right) + 2 \sin\left[40\left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) / 2\pi\right)\right]\right], \{\beta, \right. \\ \left. 0, \pi\}\right]$$




```

Play[ (4 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]) *
  Sin[250 (2 (π + √(π² - π² Sin[β]²)) / 2 π) + 2 Sin[40 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]], {β,
  0, π}]

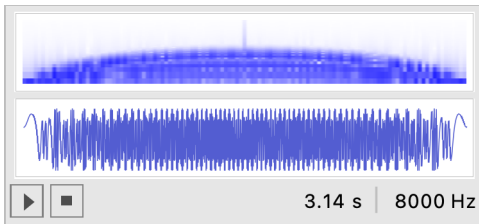
```



```

Play[ (4 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]) *
  Sin[125 (2 (π + √(π² - π² Sin[β]²)) / 2 π) + 2 Sin[40 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]], {β,
  0, π}]

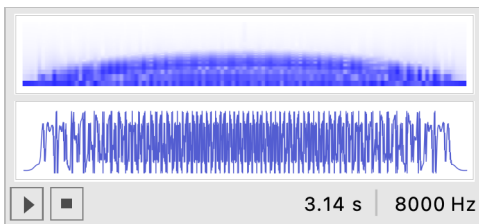
```



```

Play[ (4 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]) *
  Sin[67.5 (2 (π + √(π² - π² Sin[β]²)) / 2 π) +
  2 Sin[40 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]], {β, 0, π}]

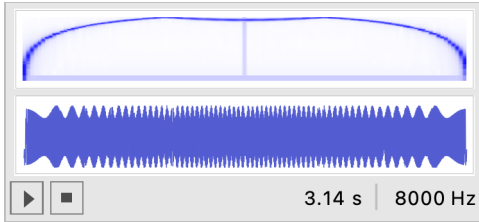
```



```

Play[ (4 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]) *
  Sin[3000 (2 (π + √(π² - π² Sin[β]²)) / 2 π) +
    2 Sin[50 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]], {β, 0, π}]

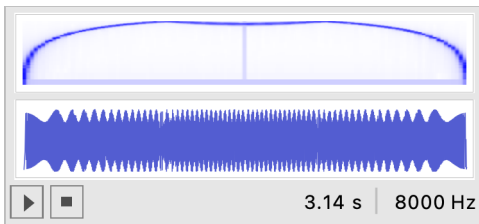
```



```

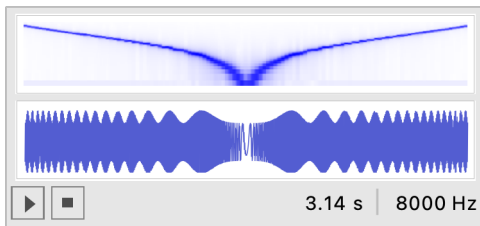
Play[ (4 + Cos[20 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]) *
  Sin[3000 (2 (π + √(π² - π² Sin[β]²)) / 2 π) +
    2 Sin[60 (2 (π + √(π² - π² Sin[β]²)) / 2 π)]], {β, 0, π}]

```



## The Sounds of Pure Thought (30-60-90 Velocity Biatch)

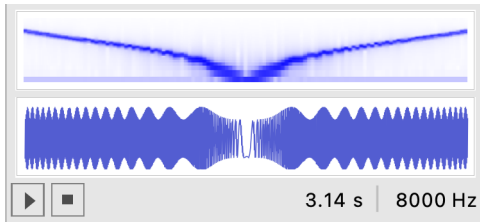
$$\begin{aligned}
 & \text{Play}\left[\left(4 + \cos\left[20\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right)\right]\right.\right. \\
 & \quad \left.\left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\
 & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)\right] / \\
 & \quad 2\pi\left]\right) * \sin\left[2000\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right)\right] / \\
 & \quad \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
 & \quad \frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) / 2 \\
 & \quad \pi\left) + 2 \sin\left[40\left(\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2)\right)\right] / \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + \right.\right.\right. \\
 & \quad \left.\left.3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \\
 & \quad \left.\frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) / \right. \\
 & \quad \left.\left.2\pi\right)\right], \{\beta, 0, \pi\}]
 \end{aligned}$$



```

Play[ (4 + Cos[20 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) /
  (6 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) /
  2 π))] * Sin[1000 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) /
  (6 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) / 2
  π) + 2 Sin[40 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) / (6 (-π^3 + 18 π^3 Sin[β]^2 +
  3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) /
  2 π))] , {β, 0, π}]

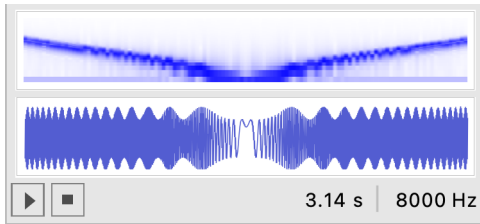
```



```

Play[ (4 + Cos[20 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) /
  (6 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) /
  2 π))] * Sin[500 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) /
  (6 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) / 2
  π) + 2 Sin[40 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) / (6 (-π^3 + 18 π^3 Sin[β]^2 +
    3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
    2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) /
    2 π))] , {β, 0, π}]

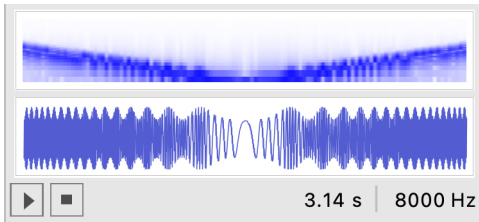
```



```

Play[ (4 + Cos[20 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) /
  (6 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) /
  2 π))] * Sin[250 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) /
  (6 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) / 2
  π) + 2 Sin[40 ((4 π / 3 - (-4 π^2 + 12 π^2 Sin[β]^2) / (6 (-π^3 + 18 π^3 Sin[β]^2 +
  3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) +
  2/3 (-π^3 + 18 π^3 Sin[β]^2 + 3 √3 √(-π^6 Sin[β]^2 + 11 π^6 Sin[β]^4 + π^6 Sin[β]^6))^(1/3) /
  2 π))] , {β, 0, π}]

```



```

Play[ (4 + Cos[20 (2 (π + √(π^2 - π^2 Sin[β]^2) / 2 π))] *
  Sin[3000 (2 (π + √(π^2 - π^2 Sin[β]^2) / 2 π) +
  2 Sin[60 (2 (π + √(π^2 - π^2 Sin[β]^2) / 2 π))] , {β, 0, π}]

```

```

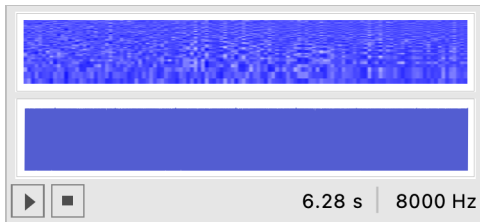
(√(3.5481432270250993`*^18 -
  1.1294090667581471`*^18 θ + 8.987551787368176`*^16 θ^2)) /
  (√(39.47841760435743` - 12.566370614359172` θ + θ^2)) =
  v = λ ((2 π) / θ) = (2 π √(4 π - θ) θ) / ((2 π) / θ)
  (√(3.5481432270250993`*^18 -
  1.1294090667581471`*^18 θ + 8.987551787368176`*^16 θ^2)) /
  (√(39.47841760435743` - 12.566370614359172` θ + θ^2)) / (2 π √(4 π - θ) θ) == ((2 π) / θ)

```

$$t = \left( \left( \sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) / \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right) \right)$$

Play[Sin[  

$$\left( \left( \sqrt{3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2} \right) / \left( \sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2} \right) / \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right) \right) \right], \{\theta, 0, 2 \pi\}]$$

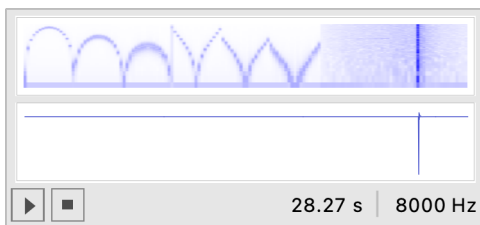






$$\begin{aligned}
& 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \Bigg) + \frac{2}{3} \\
& \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \Bigg) / \\
& 2 \pi \Bigg) \Bigg) * \sin \left[ 2000 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \\
& \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \right. \right. \right. \right. \\
& \left. \left. \left. \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \right) / 2 \pi \right) + \\
& 2 \sin \left[ 40 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \right. \\
& \left. \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \right. \right. \right. \right. \\
& \left. \left. \left. \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \\
& \left. \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) / 2 \pi \right) \right] \Bigg], \{\beta, \theta, \pi\}, \\
& \text{Play} \left[ \left( 4 + \cos \left[ 20 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \frac{2}{3} \right. \right. \right. \\
& \left. \left. \left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \right) \right) \right) / \\
& 2 \pi \Bigg) \Bigg) * \sin \left[ 1000 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \right. \right. \right. \\
& \left. \left. \left. \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \right) / 2 \pi \right) + \\
& 2 \sin \left[ 40 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \right. \\
& \left. \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18 \right. \right. \right. \\
& \left. \left. \left. \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \\
& \left. \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) / 2 \pi \right) \right] \Bigg], \{\beta, \theta, \pi\}, \\
& \text{Play} \left[ \left( 4 + \cos \left[ 20 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) + \frac{2}{3} \right. \right. \right. \\
& \left. \left. \left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \right) \right) \right) \right) / \\
& 2 \pi \Bigg) \Bigg) * \sin \left[ 500 \left( \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \right. \right. \\
\end{aligned}$$

$$\begin{aligned}
& 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \Big) + \frac{2}{3} \Big( -\pi^3 + 18 \pi^3 \\
& \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \Big) \Big) / 2 \pi \Big) + \\
& 2 \sin \Big[ 40 \Big( \Big( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \Big) / \Big( 6 \Big( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \\
& \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \Big) + \frac{2}{3} \Big( -\pi^3 + 18 \pi^3 \\
& \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}^{1/3} \Big) \Big) / 2 \\
& \pi \Big) \Big] \Big], \{\beta, \theta, \pi\} \Big], \text{Play} \Big[ \left( 4 + \cos \left[ 20 \left( \frac{\theta \left( \frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2} \right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} \right) \right] \right) * \\
& \sin \left[ 3000 \left( \frac{\theta \left( \frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2} \right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} \right) \right] + 2 \sin \left[ 50 \left( \frac{\theta \left( \frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2} \right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} \right) \right] \Big] \Big], \\
& \{\theta, \\
& \theta, \\
& 2 \\
& \pi \} \Big], \\
& \text{Play} \Big[ 1 / \left( \frac{\theta \left( \frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2} \right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} \right), \\
& \{\theta, \\
& \theta, \\
& \pi \} \Big] \Big] \Big]
\end{aligned}$$



$$\begin{aligned}
& D \left[ 2 \pi \frac{\sqrt{4 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta - \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2}}{2 \pi}, \theta \right] \\
& \frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2} \\
& 2 \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}
\end{aligned}$$

$$\text{Solve}\left[\frac{\frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2}}{2 \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} = \frac{2 \pi \eta}{\theta}, \eta\right]$$

$$\left\{\left\{\eta \rightarrow \frac{\theta \left(\frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2}\right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}\right\}\right\}$$

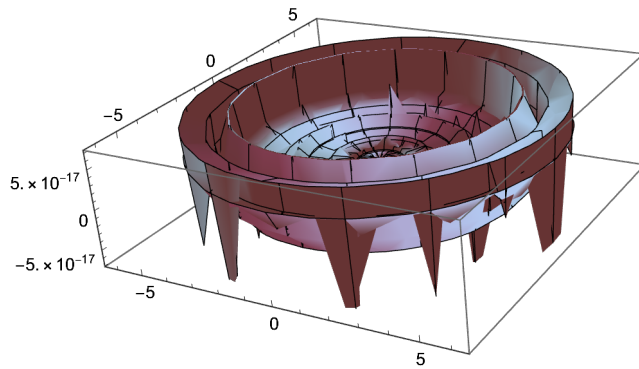
$$2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)$$

$$\frac{\theta \left(\frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2}\right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}} =$$

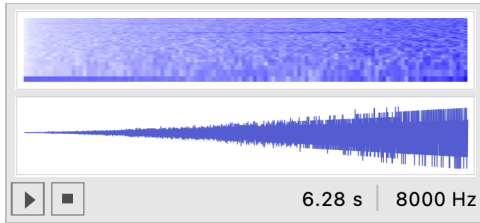
$$\left(\frac{1}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)} - \frac{4 \pi^2 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}} 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)$$

$$\left(\frac{\frac{16 \pi^3}{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2} - \frac{4 \pi^2}{4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\frac{4 \pi^2 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{\left(4 \pi - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2}}\right)$$

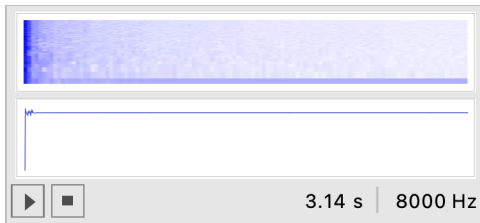
$$\text{RevolutionPlot3D}\left[\frac{\theta \left(\frac{16 \pi^3}{(4 \pi - \theta)^2} - \frac{4 \pi^2}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{(4 \pi - \theta)^2}\right)}{4 \pi \sqrt{\frac{16 \pi^3}{4 \pi - \theta} - \frac{4 \pi^2 \theta}{4 \pi - \theta}}}, \{\theta, -2 \pi, 2 \pi\}\right]$$



$$\text{Play}\left[\left(4 + \cos\left[2\theta \left(\frac{\theta \left(\frac{16\pi^3}{(4\pi-\theta)^2} - \frac{4\pi^2}{4\pi-\theta} - \frac{4\pi^2\theta}{(4\pi-\theta)^2}\right)}{4\pi \sqrt{\frac{16\pi^3}{4\pi-\theta} - \frac{4\pi^2\theta}{4\pi-\theta}}}\right)\right] \right) * \sin\left[\frac{3000 \left(\frac{\theta \left(\frac{16\pi^3}{(4\pi-\theta)^2} - \frac{4\pi^2}{4\pi-\theta} - \frac{4\pi^2\theta}{(4\pi-\theta)^2}\right)}{4\pi \sqrt{\frac{16\pi^3}{4\pi-\theta} - \frac{4\pi^2\theta}{4\pi-\theta}}}\right) + 2 \sin\left[50 \left(\frac{\theta \left(\frac{16\pi^3}{(4\pi-\theta)^2} - \frac{4\pi^2}{4\pi-\theta} - \frac{4\pi^2\theta}{(4\pi-\theta)^2}\right)}{4\pi \sqrt{\frac{16\pi^3}{4\pi-\theta} - \frac{4\pi^2\theta}{4\pi-\theta}}}\right)\right], \{\theta, 0, 2\pi\}\right]$$



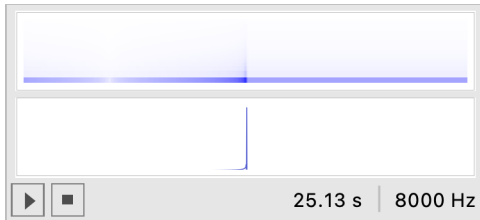
$$\text{Play}\left[1 / \left(\frac{\theta \left(\frac{16\pi^3}{(4\pi-\theta)^2} - \frac{4\pi^2}{4\pi-\theta} - \frac{4\pi^2\theta}{(4\pi-\theta)^2}\right)}{4\pi \sqrt{\frac{16\pi^3}{4\pi-\theta} - \frac{4\pi^2\theta}{4\pi-\theta}}}\right), \{\theta, 0, \pi\}\right]$$



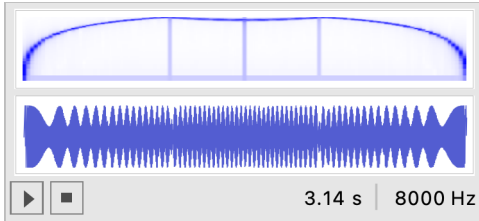
$$\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \theta$$

$$\text{Plot} \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta}$$

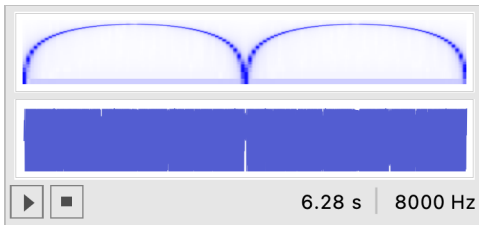
$$\text{Play}\left[\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{4\pi - \theta}, \{\theta, 0, 8\pi\}\right]$$



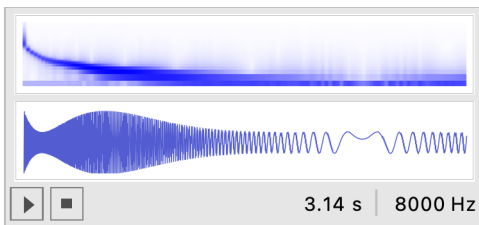
$$\text{Play}\left[\left(2 + \cos\left[20 \left(\left(\arccos\left[\frac{1}{2} e^{-2i\pi \sqrt{1-\sin[\beta]^2}} (1 + e^{4i\pi \sqrt{1-\sin[\beta]^2}})\right]\right) / 2\pi\right)\right]\right) * \right. \\ \left. \sin\left[3000 \left(\left(\arccos\left[\frac{1}{2} e^{-2i\pi \sqrt{1-\sin[\beta]^2}} (1 + e^{4i\pi \sqrt{1-\sin[\beta]^2}})\right]\right) / 2\pi\right) + \right. \right. \\ \left. \left. 2 \sin\left[50 \left(\left(\arccos\left[\frac{1}{2} e^{-2i\pi \sqrt{1-\sin[\beta]^2}} (1 + e^{4i\pi \sqrt{1-\sin[\beta]^2}})\right]\right) / 2\pi\right)\right]\right], \{\beta, 0, \pi\}\right]$$



$$\text{Play}\left[\sin\left[3000 \arccos\left[\frac{1}{2} e^{-2i\pi \sqrt{1-\sin[\beta]^2}} (1 + e^{4i\pi \sqrt{1-\sin[\beta]^2}})\right]\right], \{\beta, -\pi, \pi\}\right]$$



$$\text{Play}\left[\left(2 + \cos\left[20 \left(\arcsin\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}}\right] / 2\pi\right)\right]\right) * \right. \\ \left. \sin\left[3000 \left(\arcsin\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}}\right] / 2\pi\right) + \right. \right. \\ \left. \left. 2 \sin\left[50 \left(\arcsin\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi \sqrt{-4\pi + \theta}}\right] / 2\pi\right)\right]\right], \{\theta, 0, \pi\}\right]$$



$$\frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} == r$$

$$\text{Solve}\left[\frac{\sqrt{\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}}\sqrt{1-\frac{v^2}{(c)^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{(c)^2}}}}\sqrt{4\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}-\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}}{2\pi}=\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta},v\right]$$

$$c := 2.99792458 * (10^8)$$

$$\text{Solve}\left[\frac{\sqrt{r}\sqrt{1-\frac{v^2}{(c)^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{(c)^2}}}}\sqrt{4\pi r-r\theta}}{2\pi}=r,v\right]$$

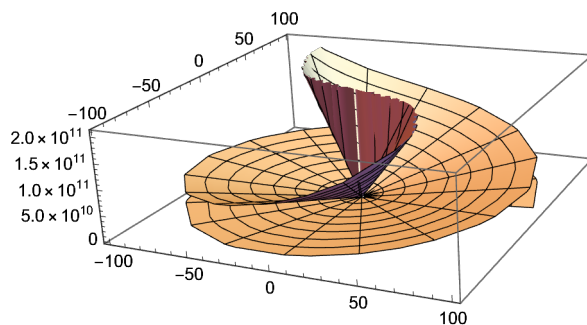
$$\left\{\left\{v \rightarrow -\frac{1.\sqrt{3.54814 \times 10^{18}-1.12941 \times 10^{18}\theta+8.98755 \times 10^{16}\theta^2}}{\sqrt{39.4784-12.5664\theta+\theta^2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{3.54814 \times 10^{18}-1.12941 \times 10^{18}\theta+8.98755 \times 10^{16}\theta^2}}{\sqrt{39.4784-12.5664\theta+\theta^2}}\right\}\right\}$$

$$\text{Solve}\left[\frac{\sqrt{\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}}\sqrt{1-\frac{v^2}{(c)^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{v^2}{(c)^2}}}}\sqrt{4\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}-\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta}}{2\pi}=r,v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1.\sqrt{-1.45179 \times 10^{33}+1.45179 \times 10^{33}r^2}}{\sqrt{-1.61534 \times 10^{16}+1.61534 \times 10^{16}r^2}}\right\},\left\{v \rightarrow \frac{\sqrt{-1.45179 \times 10^{33}+1.45179 \times 10^{33}r^2}}{\sqrt{-1.61534 \times 10^{16}+1.61534 \times 10^{16}r^2}}\right\}\right\}$$

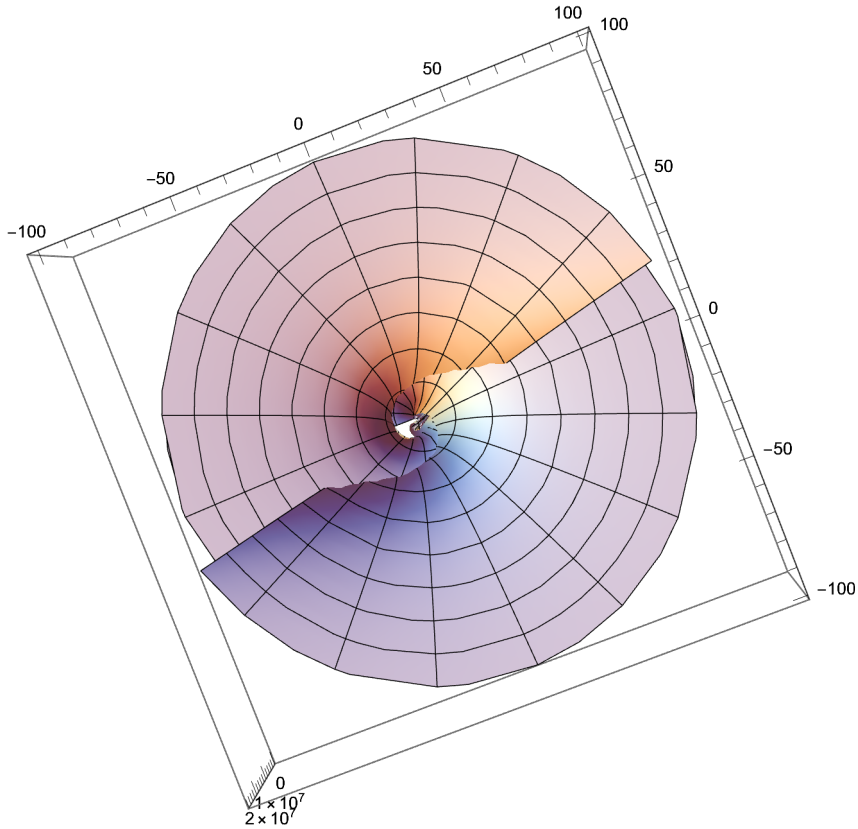
$$\text{RevolutionPlot3D}\left[\frac{\sqrt{-1.4517917706931478 \cdot 10^{33}+1.4517917706931478 \cdot 10^{33}(r)^2}}{\sqrt{-1.615336195039913 \cdot 10^{16}+1.6153361950399128 \cdot 10^{16}\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2}},\right. \\ \left.\{r,-100,100\},\{\theta,-2\pi,2\pi\}\right]$$



RevolutionPlot3D[

$$\frac{\sqrt{-1.4517917706931478 \cdot ^{33} + 1.4517917706931478 \cdot ^{33} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2}}{\sqrt{-1.615336195039913 \cdot ^{16} + 1.6153361950399128 \cdot ^{16} r^2}},$$

{r, -100, 100}, {θ, -2 π, 2 π}]



$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{v^2}{(c)^2}} \sqrt{\frac{\theta}{1 - \frac{v^2}{(c)^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}, v\right]$$

{}

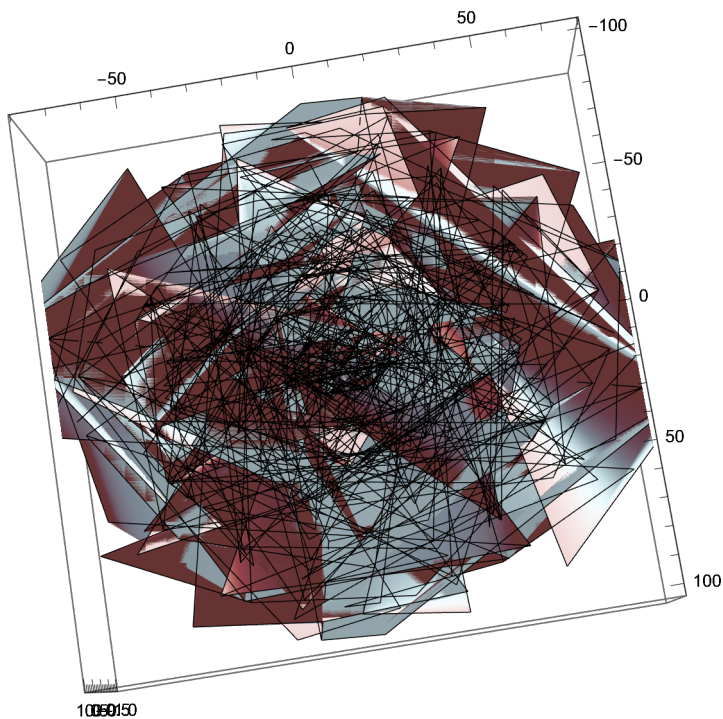
$$\theta = 2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)} - \theta r$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)} - \theta r)^2}{(c)^2}}} \sqrt{\frac{\theta}{1 - \frac{(2 \pi r - 2 \pi \sqrt{(r^2 - \eta^2)} - \theta r)^2}{(c)^2}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = \eta, \eta\right]$$

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(2\pi r - 2\pi \sqrt{(r^2 - \eta^2)} - \theta r)^2}{(c)^2}}}{2\pi} \sqrt{\frac{\theta}{1 - \frac{(2\pi r - 2\pi \sqrt{(r^2 - \eta^2)} - \theta r)^2}{(c)^2}}} \sqrt{4\pi r - r\theta} = \eta, \eta\right]$$

$$\{\{\eta \rightarrow -0.159155 r \sqrt{12.5664 - 1. \theta} \sqrt{\theta}\}, \{\eta \rightarrow 0.159155 r \sqrt{12.5664 - 1. \theta} \sqrt{\theta}\}\}$$

$$\text{RevolutionPlot3D}\left[0.15915494309189535 \sqrt{r} \sqrt{12.566370614359172 - 1. \theta} \sqrt{\theta}, \{r, -100, 100\}, \{\theta, -80000000\pi, 80000000\pi}\right]$$

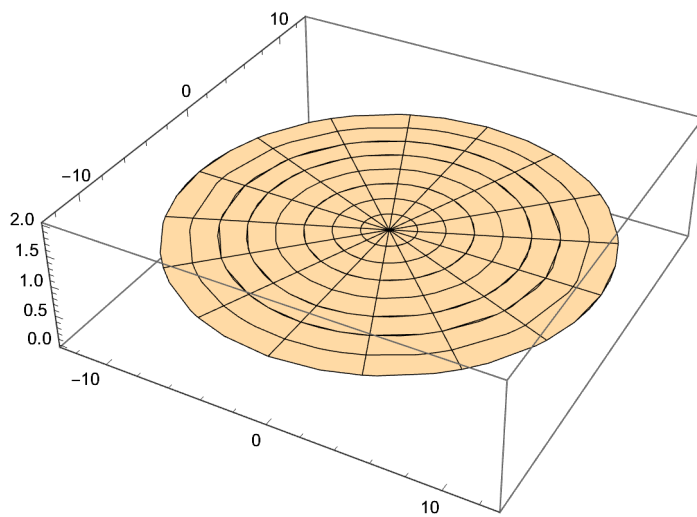




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RevolutionPlot3D[
  0.15915494309189535`  $\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$   $\sqrt{12.566370614359172 - 1. \theta}$   $\sqrt{\theta}$ , { $\theta$ , -4  $\pi$ , 4  $\pi$ }]

```



$$\text{Solve}\left[\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)-r^2\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^2}}{2\pi}\right)^3-\right]$$

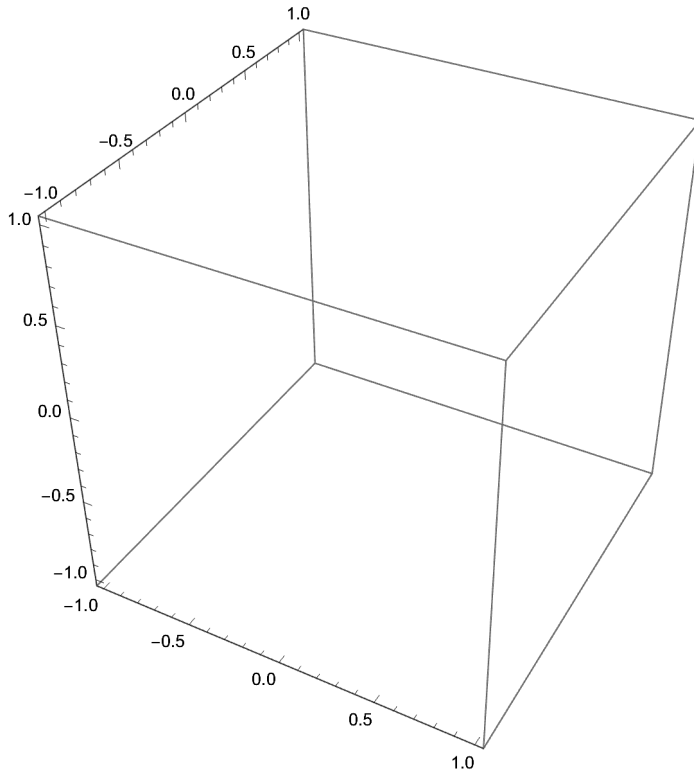
$$\left(\frac{4}{3}\right)\pi\left(\frac{2\pi r-r\theta}{2\pi}\right)^3==\left(\frac{4}{3}\right)\pi\left(\frac{2\pi r-r\theta}{2\pi}\right)^3-\left(\frac{4}{3}\right)\pi\left(\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}\right)^3,\theta]$$

$$\left\{\left\{\theta\rightarrow\text{Root}\left[256\pi^6r+64\pi^6r\sin[\beta]^6-\right.\right.\right. \\ \left.256\pi^6\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}+\left(-768\pi^5r+384\pi^5\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1+ \right. \\ \left.\left(960\pi^4r-192\pi^4\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^2+ \right. \\ \left.\left(-704\pi^3r+32\pi^3\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^3+288\pi^2r\#1^4-60\pi r\#1^5+5r\#1^6\&,1\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[256\pi^6r+64\pi^6r\sin[\beta]^6-256\pi^6\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}+ \right.\right. \\ \left.\left(-768\pi^5r+384\pi^5\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1+ \right. \\ \left.\left(960\pi^4r-192\pi^4\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^2+ \right. \\ \left.\left(-704\pi^3r+32\pi^3\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^3+288\pi^2r\#1^4-60\pi r\#1^5+5r\#1^6\&,2\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[256\pi^6r+64\pi^6r\sin[\beta]^6-256\pi^6\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}+ \right.\right. \\ \left.\left(-768\pi^5r+384\pi^5\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1+ \right. \\ \left.\left(960\pi^4r-192\pi^4\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^2+ \right. \\ \left.\left(-704\pi^3r+32\pi^3\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^3+288\pi^2r\#1^4-60\pi r\#1^5+5r\#1^6\&,3\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[256\pi^6r+64\pi^6r\sin[\beta]^6-256\pi^6\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}+ \right.\right. \\ \left.\left(-768\pi^5r+384\pi^5\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1+ \right. \\ \left.\left(960\pi^4r-192\pi^4\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^2+ \right. \\ \left.\left(-704\pi^3r+32\pi^3\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^3+288\pi^2r\#1^4-60\pi r\#1^5+5r\#1^6\&,4\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[256\pi^6r+64\pi^6r\sin[\beta]^6-256\pi^6\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}+ \right.\right. \\ \left.\left(-768\pi^5r+384\pi^5\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1+ \right. \\ \left.\left(960\pi^4r-192\pi^4\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^2+ \right. \\ \left.\left(-704\pi^3r+32\pi^3\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^3+288\pi^2r\#1^4-60\pi r\#1^5+5r\#1^6\&,5\right]\right\}, \\ \left\{\theta\rightarrow\text{Root}\left[256\pi^6r+64\pi^6r\sin[\beta]^6-256\pi^6\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}+ \right.\right. \\ \left.\left(-768\pi^5r+384\pi^5\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1+ \right. \\ \left.\left(960\pi^4r-192\pi^4\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^2+ \right. \\ \left.\left(-704\pi^3r+32\pi^3\sin[\beta]^2\sqrt{r^2\sin[\beta]^2}\right)\#1^3+288\pi^2r\#1^4-60\pi r\#1^5+5r\#1^6\&,6\right]\right\}\}$$

```

RevolutionPlot3D[ {Root[256 π^6 r + 64 π^6 r Sin[β]^6 -
256 π^6 Sin[β]^2 √{r^2 Sin[β]^2} + (-768 π^5 r + 384 π^5 Sin[β]^2 √{r^2 Sin[β]^2}) #1 +
(960 π^4 r - 192 π^4 Sin[β]^2 √{r^2 Sin[β]^2}) #1^2 +
(-704 π^3 r + 32 π^3 Sin[β]^2 √{r^2 Sin[β]^2}) #1^3 + 288 π^2 r #1^4 - 60 π r #1^5 + 5 r #1^6 &, 1],
Root[256 π^6 r + 64 π^6 r Sin[β]^6 - 256 π^6 Sin[β]^2 √{r^2 Sin[β]^2} +
(-768 π^5 r + 384 π^5 Sin[β]^2 √{r^2 Sin[β]^2}) #1 +
(960 π^4 r - 192 π^4 Sin[β]^2 √{r^2 Sin[β]^2}) #1^2 +
(-704 π^3 r + 32 π^3 Sin[β]^2 √{r^2 Sin[β]^2}) #1^3 + 288 π^2 r #1^4 - 60 π r #1^5 + 5 r #1^6 &, 2],
Root[256 π^6 r + 64 π^6 r Sin[β]^6 - 256 π^6 Sin[β]^2 √{r^2 Sin[β]^2} +
(-768 π^5 r + 384 π^5 Sin[β]^2 √{r^2 Sin[β]^2}) #1 +
(960 π^4 r - 192 π^4 Sin[β]^2 √{r^2 Sin[β]^2}) #1^2 +
(-704 π^3 r + 32 π^3 Sin[β]^2 √{r^2 Sin[β]^2}) #1^3 + 288 π^2 r #1^4 - 60 π r #1^5 + 5 r #1^6 &, 3],
Root[256 π^6 r + 64 π^6 r Sin[β]^6 - 256 π^6 Sin[β]^2 √{r^2 Sin[β]^2} +
(-768 π^5 r + 384 π^5 Sin[β]^2 √{r^2 Sin[β]^2}) #1 +
(960 π^4 r - 192 π^4 Sin[β]^2 √{r^2 Sin[β]^2}) #1^2 +
(-704 π^3 r + 32 π^3 Sin[β]^2 √{r^2 Sin[β]^2}) #1^3 + 288 π^2 r #1^4 - 60 π r #1^5 + 5 r #1^6 &, 4],
Root[256 π^6 r + 64 π^6 r Sin[β]^6 - 256 π^6 Sin[β]^2 √{r^2 Sin[β]^2} +
(-768 π^5 r + 384 π^5 Sin[β]^2 √{r^2 Sin[β]^2}) #1 +
(960 π^4 r - 192 π^4 Sin[β]^2 √{r^2 Sin[β]^2}) #1^2 +
(-704 π^3 r + 32 π^3 Sin[β]^2 √{r^2 Sin[β]^2}) #1^3 + 288 π^2 r #1^4 - 60 π r #1^5 + 5 r #1^6 &, 5],
Root[256 π^6 r + 64 π^6 r Sin[β]^6 - 256 π^6 Sin[β]^2 √{r^2 Sin[β]^2} +
(-768 π^5 r + 384 π^5 Sin[β]^2 √{r^2 Sin[β]^2}) #1 + (960 π^4 r - 192 π^4 Sin[β]^2 √{r^2 Sin[β]^2})
#1^2 + (-704 π^3 r + 32 π^3 Sin[β]^2 √{r^2 Sin[β]^2}) #1^3 +
288 π^2 r #1^4 - 60 π r #1^5 + 5 r #1^6 &, 6] }, {r, -100, 100}, {β, -2 π, 2 π} ]

```



$$\text{Solve}\left[\frac{4}{3} \pi (r_1)^3 - \frac{4}{3} \pi (\eta)^3 == \frac{4}{3} \pi (\eta)^3 - \frac{4}{3} \pi (r_1)^3, \eta\right]$$

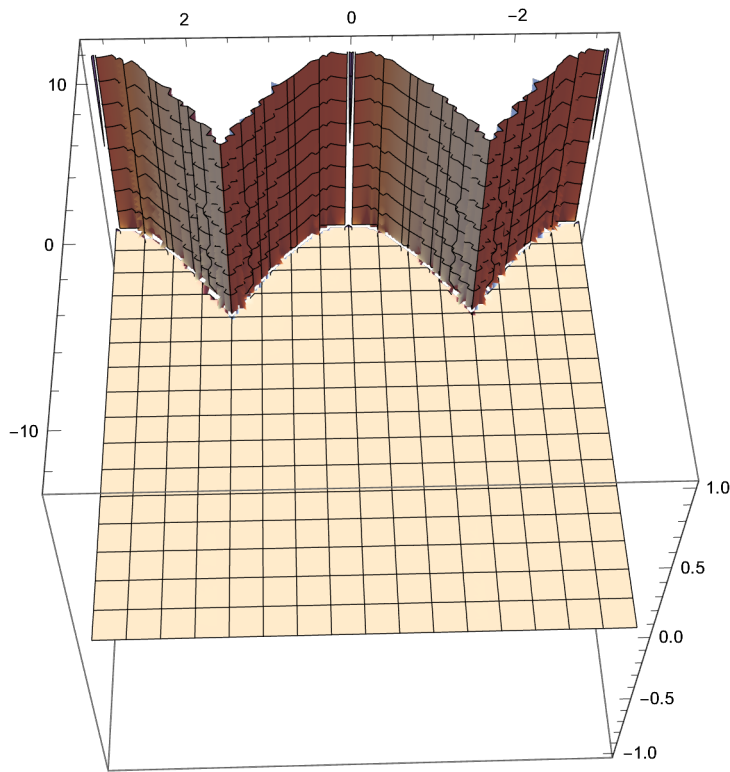
$$\left\{\left\{\eta \rightarrow r_1\right\}, \left\{\eta \rightarrow -(-1)^{1/3} r_1\right\}, \left\{\eta \rightarrow (-1)^{2/3} r_1\right\}\right\}$$

$$\theta r = \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] r - \text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right] b$$

$$\text{Solve}\left[\theta r = 2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) r - 2\left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) b, r\right]$$

$$\left\{\left\{r \rightarrow \frac{2b\left(\pi + \pi\sqrt{1 - \text{Sin}[\beta]^2}\right)}{2\pi - \theta + 2\pi\sqrt{1 - \text{Sin}[\beta]^2}}\right\}\right\}$$

ContourPlot3D $\left[\frac{2 b \left(\pi + \pi \sqrt{1 - \text{Sin}[\beta]^2}\right)}{2 \pi - \theta + 2 \pi \sqrt{1 - \text{Sin}[\beta]^2}}, \{b, -1, 1\}, \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}\right]$



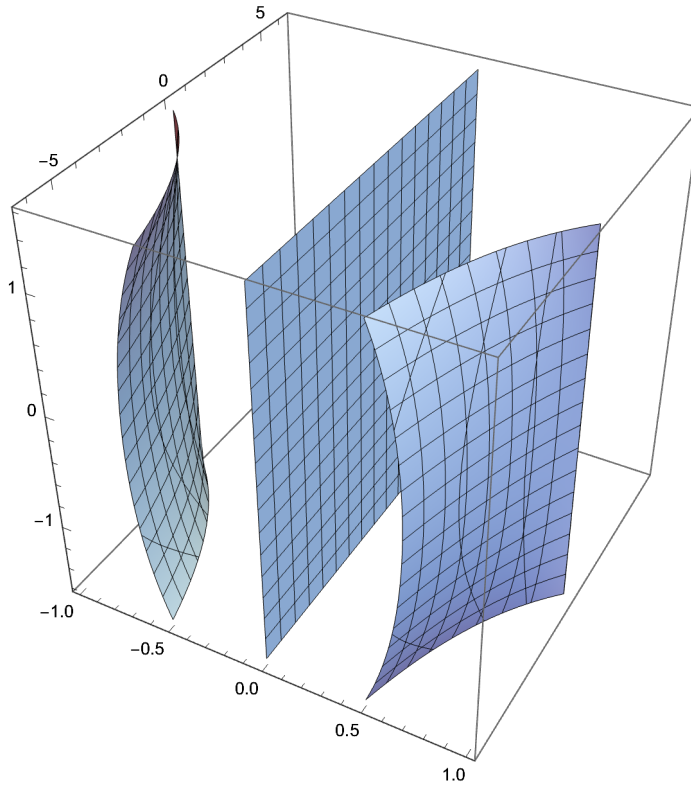
Solve $\left[\theta r = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) r - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) b, \beta\right]$

$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{r} \sqrt{\theta} \sqrt{-4 b \pi + 4 \pi r - r \theta}}{\pi \sqrt{4 b^2 - 8 b r + 4 r^2}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{r} \sqrt{\theta} \sqrt{-4 b \pi + 4 \pi r - r \theta}}{\pi \sqrt{4 b^2 - 8 b r + 4 r^2}}\right]\right\}\right\}$

Solve $\left[\theta r = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) r - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) b, b\right]$

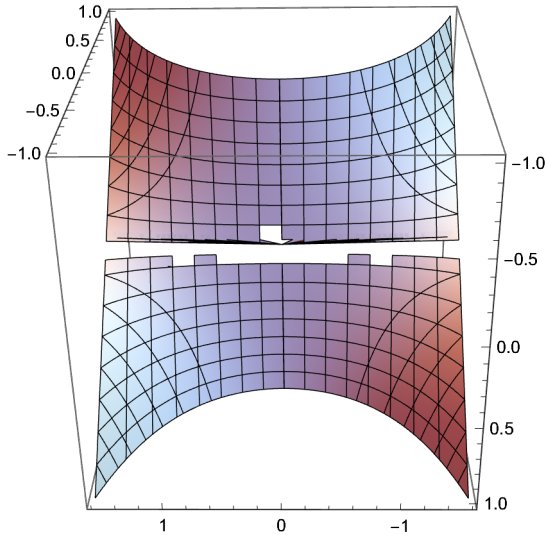
$\left\{\left\{b \rightarrow \frac{2 \pi r - r \theta + 2 \pi r \sqrt{1 - \text{Sin}[\beta]^2}}{2 \left(\pi + \pi \sqrt{1 - \text{Sin}[\beta]^2}\right)}\right\}\right\}$

ContourPlot3D $\left[\frac{2 \pi r - r \theta + 2 \pi r \sqrt{1 - \text{Sin}[\beta]^2}}{2 \left(\pi + \pi \sqrt{1 - \text{Sin}[\beta]^2}\right)},\right.$   
 $\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}$



Solve $\left[\theta r = 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) r - 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2}\right) b, \theta\right]$   
 $\left\{\left\{\theta \rightarrow -\frac{2 \left(b \pi - \pi r + b \pi \sqrt{1 - \text{Sin}[\beta]^2} - \pi r \sqrt{1 - \text{Sin}[\beta]^2}\right)}{r}\right\}\right\}$

ContourPlot3D $\left[\frac{2 \left(b \pi - \pi r + b \pi \sqrt{1 - \text{Sin}[\beta]^2} - \pi r \sqrt{1 - \text{Sin}[\beta]^2}\right)}{r},\right.$   
 $\{b, -1, 1\}, \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}$  $\left.]\right]$



$$\theta = \frac{4 \pi}{3} - \left(-4 \pi^2 + 12 \pi^2 \text{Sin}[\beta]^2\right) /$$

$$\left(6 \left(-\pi^3 + 18 \pi^3 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}\right) +$$

$$\frac{2}{3} \left(-\pi^3 + 18 \pi^3 \text{Sin}[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \text{Sin}[\beta]^2 + 11 \pi^6 \text{Sin}[\beta]^4 + \pi^6 \text{Sin}[\beta]^6}\right)^{1/3}$$

$$\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]$$

$$\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == c (\theta / (2 \pi))$$

$$\theta \rightarrow \frac{4 \pi r^2}{c^2 + r^2} = \frac{4 \pi \left(r \sqrt{1 - ((u^2) / (c^2))}\right)^2}{c^2 + \left(r \sqrt{1 - ((u^2) / (c^2))}\right)^2}$$

$$\text{Solve}\left[\frac{4 \pi \left(r \sqrt{1 - ((u^2) / (c^2))}\right)^2}{c^2 + \left(r \sqrt{1 - ((u^2) / (c^2))}\right)^2} == \theta, u\right]$$

{ }

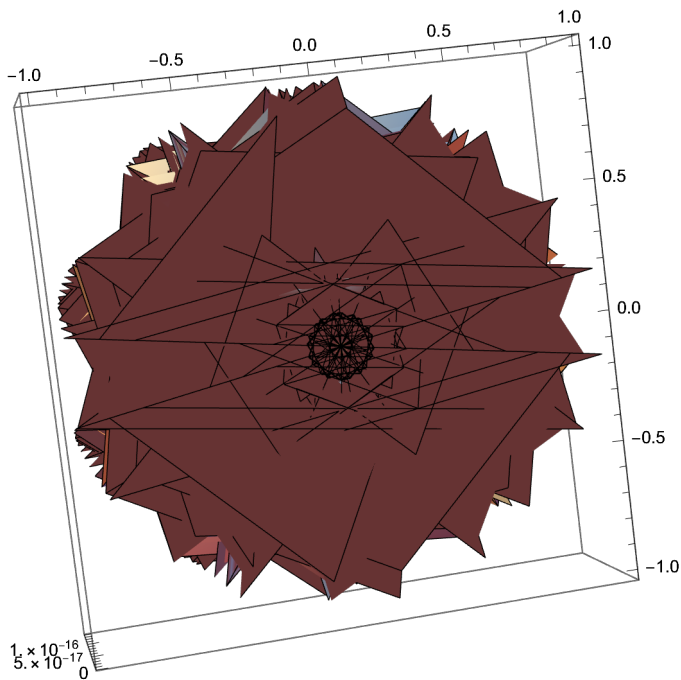
```

u := (sqrt(-1.1294090667581471`*^18 theta +
      8.987551787368176`*^16 theta^2 + 3.5481432270250993`*^18 Sin[beta]^2)) /
      (sqrt(-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2))

r -> (sqrt(-c^2 - c^2 sqrt(1 - Sin[beta]^2)) /
      sqrt(-1 + sqrt(1 - Sin[beta]^2)))

RevolutionPlot3D[
  (4 pi (r sqrt(1 - ((u^2) / (c^2))))^2 /
   (c^2 + (r sqrt(1 - ((u^2) / (c^2))))^2)^2, {r, -1, 1}, {u, -c, c}]

```



```
c := (2.99792458 * 10^8)
```

```
c := (2.99792458 * 10^8)
```

```
h := (6.62606896 * (10^-34))
```

```

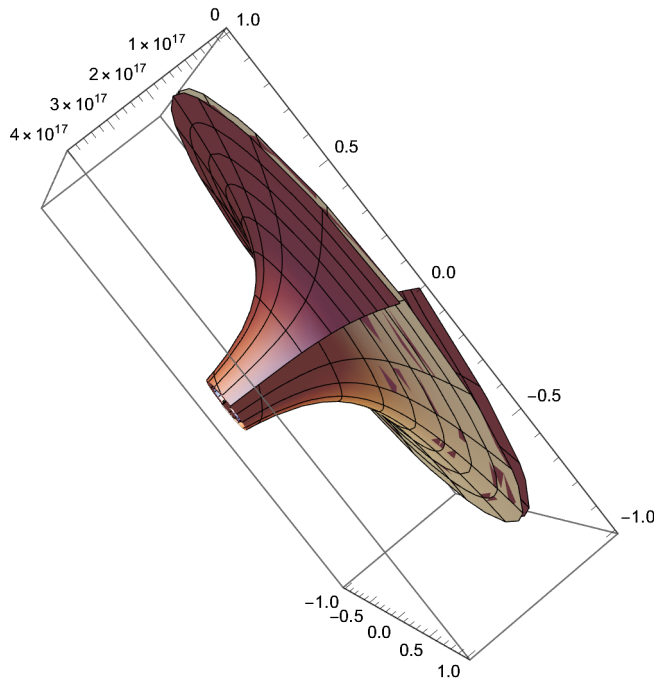
Solve[
  (4 pi (r sqrt(1 - ((u^2) / (c^2))))^2 /
   (c^2 + (r sqrt(1 - ((u^2) / (c^2))))^2)^2 == theta, u]

{{u -> - (sqrt(-4 c^2 pi r^2 + c^4 theta + c^2 r^2 theta) /
  sqrt(-4 pi r^2 + r^2 theta))}, {u -> (sqrt(-4 c^2 pi r^2 + c^4 theta + c^2 r^2 theta) /
  sqrt(-4 pi r^2 + r^2 theta))}}

```



RevolutionPlot3D $\left[\frac{\sqrt{-4 c^2 \pi r^2 + c^4 \theta + c^2 r^2 \theta}}{\sqrt{-4 \pi r^2 + r^2 \theta}}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$(1 - v^2 / c^2) (-1 / 2)$$

$$v = \left( \sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2)} \right) /$$

$$\left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right) =$$

$$\lambda v = r v = \text{and / or} = \eta v = (1 / (\theta / (2 \pi)))$$

$$v = \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) /$$

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) = \eta v = \eta (1 / (\theta / (2 \pi)))$$

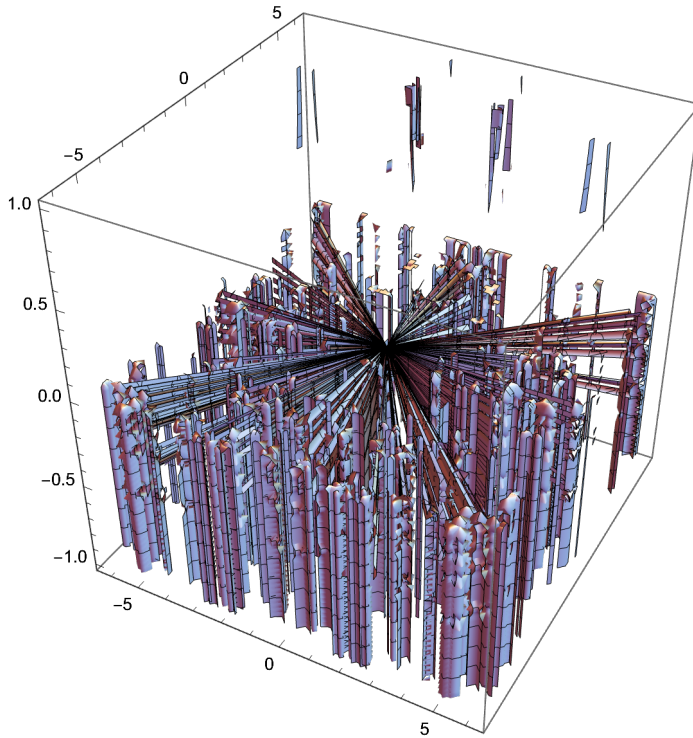
$$\text{Solve}\left[\left(\sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)}\right) / \right.$$

$$\left. \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) == \eta (1 / (v)), v \right]$$

$$\left\{ \left\{ v \rightarrow \frac{9.35498 \times 10^{-9} \eta \sqrt{-4.48719 \times 10^{15} \theta + 3.57079 \times 10^{14} \theta^2 + 1.40969 \times 10^{16} \sin[\beta]^2}}{\sqrt{-3.5294 \times 10^{16} \theta + 2.80861 \times 10^{15} \theta^2 + 1.10879 \times 10^{17} \sin[\beta]^2}} \right\} \right\}$$

$$\begin{aligned}
& \text{Solve}\left[ \right. \\
& \quad h \left( \left( 9.354975928917123 \cdot 10^{-9} \eta \sqrt{-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 +} \right. \right. \\
& \quad \quad \left. \left. 1.40969256654408 \cdot 10^{16} \sin^2[\beta] \right) \right) / \\
& \quad \left( \sqrt{-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 +} \right. \\
& \quad \quad \left. 1.1087947584453435 \cdot 10^{17} \sin^2[\beta] \right) \left. \right) == (z c^2) / \sqrt{(u^2 / c^2) - 1}, z \Big] \\
& \left\{ \left\{ z \rightarrow \left( 6.89695 \times 10^{-59} \sqrt{-1. + 1.11265 \times 10^{-17} u^2} \right. \right. \right. \\
& \quad \left. \left. \eta \sqrt{-4.48719 \times 10^{15} \theta + 3.57079 \times 10^{14} \theta^2 + 1.40969 \times 10^{16} \sin^2[\beta]} \right) / \right. \\
& \quad \left. \left( \sqrt{-3.5294 \times 10^{16} \theta + 2.80861 \times 10^{15} \theta^2 + 1.10879 \times 10^{17} \sin^2[\beta]} \right) \right\} \Big\}
\end{aligned}$$

ContourPlot3D[ $\left(6.896951262132264 \cdot 10^{-59} \sqrt{-1. + 1.1126500560536185 \cdot 10^{-17} \left( \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right)^2 \right) \eta \sqrt{-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin[\beta]^2} \right) / \left( \sqrt{-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin[\beta]^2} \right), \{\beta, -2\pi, 2\pi\}, \{\theta, -2\pi, 2\pi\}, \{\eta, -1, 1\}]$



$\left(6.896951262132264 \cdot 10^{-59} \sqrt{-1. + 1.1126500560536185 \cdot 10^{-17} u^2} \eta \sqrt{-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin[\beta]^2} \right) / \left( \sqrt{-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin[\beta]^2} \right)$

$$E =$$

$$h \left( \left( 9.354975928917123 \cdot 10^{-9} \eta \sqrt{(-4.487190804107819 \cdot 10^{15} \theta + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin[\beta]^2)} \right) / \left( \sqrt{(-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin[\beta]^2)} \right) \right)$$

$$E = m c^2$$

$$c := (2.99792458 \cdot 10^8)$$

$$h := 6.626068 \cdot 10^{-34}$$

Tachyon

$$E^2 = (p^2) c^2 + m^2 c^4$$

$$E = (z c^2) / \sqrt{(u^2 / c^2) - 1}$$

$$z := i m$$

$$z := i m$$

$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$(z c^2) / \sqrt{(u^2 / c^2) - 1} == h v$$

$$(z c^2) / \sqrt{(u^2 / c^2) - 1} == h v =$$

$$h \left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} / r \right) =$$

$$(z c^2) / \sqrt{\left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}^2 / c^2 \right) - 1}$$

$$h \left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} / r \right) =$$

$$\text{Solve} \left[ (z c^2) / \sqrt{\left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}^2 / c^2 \right) - 1} == \right.$$

$$h \left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} / r \right), z]$$

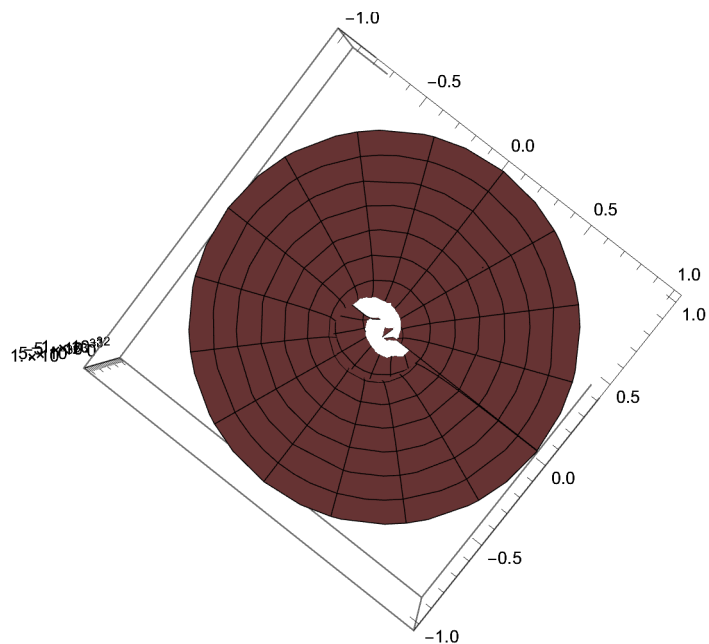
$$\left\{ \left\{ z \rightarrow \frac{h \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}}{c^2 r} \sqrt{-1 + \frac{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}{c^2}} \right\} \right\}$$

RevolutionPlot3D[

$$h \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} \sqrt{-1 + \frac{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}{c^2}},$$

$$c^2 r$$

{r, -1, 1}, {\theta, -2 \pi, 2 \pi}]



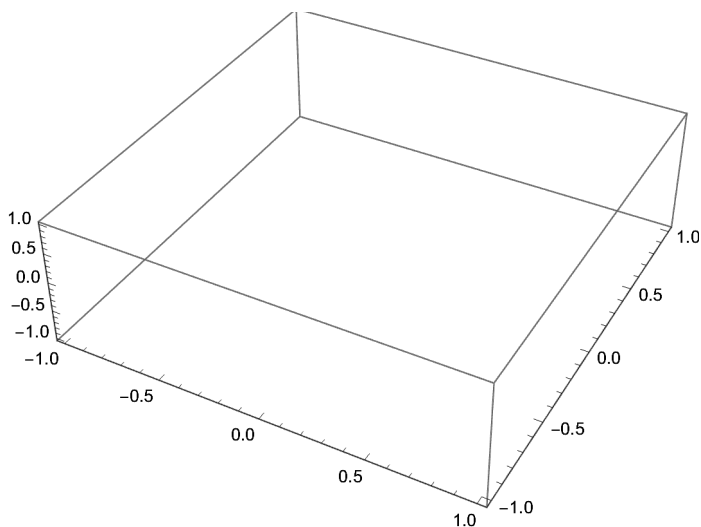
$$\text{Solve}\left[\frac{h \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}}{c^2 r} \sqrt{-1 + \frac{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}{c^2}} == i m, m\right]$$

$$\left\{\left\{m \rightarrow -\frac{i h \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}}{c^2 r} \sqrt{-1 + \frac{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}{c^2}}\right\}\right\}$$

RevolutionPlot3D[

$$\frac{\hbar \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}{c^2 r} \sqrt{-1 + \frac{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}}{c^2}},$$

{r, -1, 1}, {\theta, -2 \pi, 2 \pi}]



$$\hbar v = m (c^2) = \hbar \left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} / r \right) =$$

$$(z c^2) / \sqrt{\left( \sqrt{-\frac{4 c^2 \pi r^2}{-4 \pi r^2 + r^2 \theta} + \frac{c^2 r^2 \theta}{-4 \pi r^2 + r^2 \theta} - \frac{\sqrt{c^6 r^2 (4 \pi - \theta) \theta}}{-4 \pi r^2 + r^2 \theta}} \right)^2 / c^2 - 1}$$

$$\text{Solve}\left[h\left(\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2+r^2\theta}+\frac{c^2r^2\theta}{-4\pi r^2+r^2\theta}-\frac{\sqrt{c^6r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}/r\right)=\right.$$

$$\left.(zc^2\right)/\left[\left(\sqrt{\left(\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2+r^2\theta}+\frac{c^2r^2\theta}{-4\pi r^2+r^2\theta}-\frac{\sqrt{c^6r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}\right)^2/c^2}-1\right),r\right]$$

$$\text{Solve}\left[\frac{6.62607\times 10^{-34}\sqrt{-\frac{1.12941\times 10^{18}r^2}{-4\pi r^2+r^2\theta}+\frac{8.98755\times 10^{16}r^2\theta}{-4\pi r^2+r^2\theta}-\frac{2.6944\times 10^{25}\sqrt{r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}{r}=\right.$$

$$\left.\frac{6.62607\times 10^{-34}\pm\sqrt{-\frac{1.12941\times 10^{18}r^2}{-4\pi r^2+r^2\theta}+\frac{8.98755\times 10^{16}r^2\theta}{-4\pi r^2+r^2\theta}-\frac{2.6944\times 10^{25}\sqrt{r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}{r\sqrt{-1+1.11265\times 10^{-17}\left(-\frac{1.12941\times 10^{18}r^2}{-4\pi r^2+r^2\theta}+\frac{8.98755\times 10^{16}r^2\theta}{-4\pi r^2+r^2\theta}-\frac{2.6944\times 10^{25}\sqrt{r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}\right)}},\right.\\ \left.\{r,-1,1\},\{\theta,-2\pi,2\pi\}\right]$$

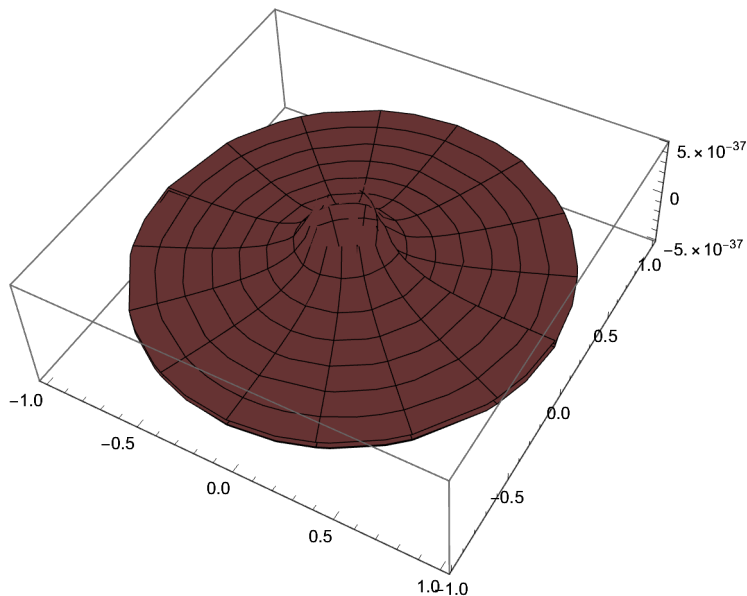
**z**

$$m:=h\left(\sqrt{-\frac{4c^2\pi r^2}{-4\pi r^2+r^2\theta}+\frac{c^2r^2\theta}{-4\pi r^2+r^2\theta}-\frac{\sqrt{c^6r^2(4\pi-\theta)\theta}}{-4\pi r^2+r^2\theta}}/r\right)/(c^2)$$

```

RevolutionPlot3D[h (
  Sqrt[-(4 c^2 pi r^2)/(-4 pi r^2 + r^2 theta) + (c^2 r^2 theta)/(-4 pi r^2 + r^2 theta) - (sqrt(c^6 r^2 (4 pi - theta) theta)/(-4 pi r^2 + r^2 theta)) / r] / (c^2),
  {r, -1, 1}, {theta, -2 pi, 2 pi}]

```



```
h := 6.626068 * 10^-34
```

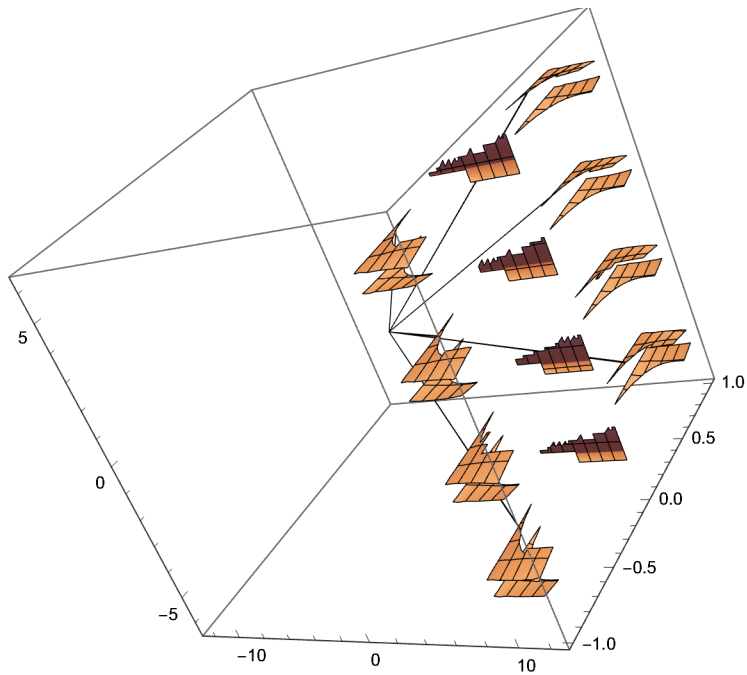
```

v = lambda v = Sqrt[-(4 c^2 pi r^2)/(-4 pi r^2 + r^2 theta) + (c^2 r^2 theta)/(-4 pi r^2 + r^2 theta) - (sqrt(c^6 r^2 (4 pi - theta) theta)/(-4 pi r^2 + r^2 theta)) / r] / (c^2),
(z c^2) / Sqrt((u^2 / c^2) - 1)

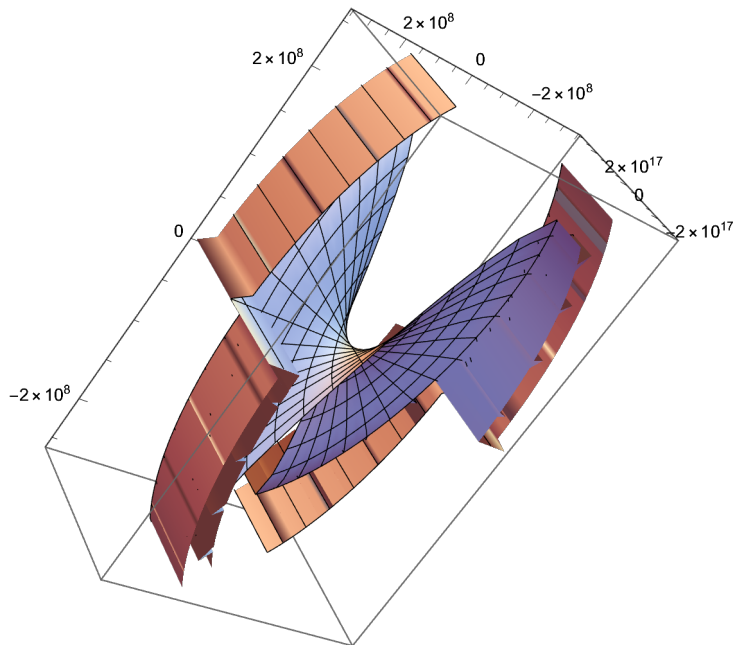
```



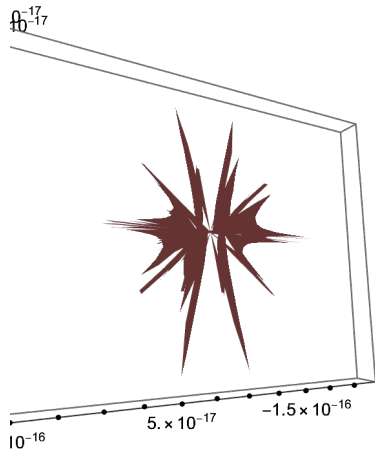
```
ContourPlot3D[(z c^2)/Sqrt[(((Sqrt[3.5481432270250993`*^18 - 1.1294090667581471`*^18 θ +
8.987551787368176`*^16 (2 (π + Sqrt[π^2 - π^2 Sin[β]^2))^2]))/
(Sqrt[39.47841760435743` - 12.566370614359172` θ + θ^2])^2/c^2) -
1, {θ, -4 π, 4 π}, {m, -1, 1}, {β, -2 π,
2
π}]
```



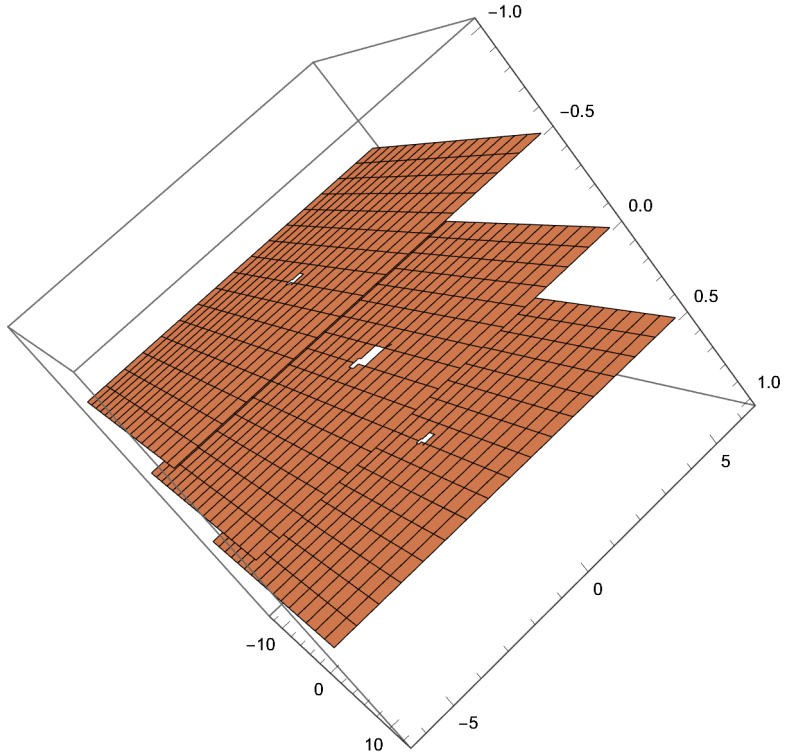
RevolutionPlot3D $\left[\frac{(z c^2)}{\sqrt{(u^2 / c^2) - 1}}, \{u, -4 c, 4 c\}, \{m, -1, 1\}\right]$



$$\text{SphericalPlot3D}\left[\left(9.354975928917123 \cdot 10^{-9} \left(4 \cdot 10^{-9} \sqrt{\left(-4.487190804107819 \cdot 10^{15} \left(\frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right) \sqrt{\left(6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} + 3.57079298535128 \cdot 10^{14} \theta^2 + 1.40969256654408 \cdot 10^{16} \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2\right)}\right) \sqrt{\left(-3.5294033336192096 \cdot 10^{16} \theta + 2.808609933552555 \cdot 10^{15} \theta^2 + 1.1087947584453435 \cdot 10^{17} \sin[\beta]^2\right)}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$$

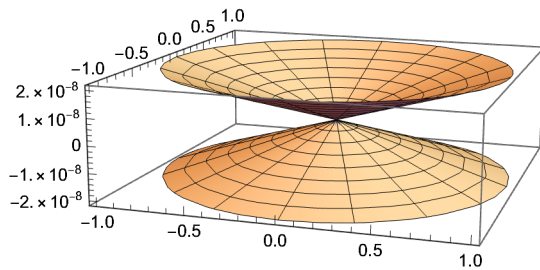


```
ContourPlot3D[
  (9.354975928917123`*^-9 η √(-4.487190804107819`*^15 θ + 3.57079298535128`*^14 θ^2 +
    1.40969256654408`*^16 Sin[β]^2)) /
  (√(-3.5294033336192096`*^16 θ + 2.808609933552555`*^15 θ^2 +
    1.1087947584453435`*^17 Sin[β]^2)), {η, -1, 1}, {β, -2 π, 2 π}, {θ, -4 π, 4 π}]
```



```
Solve[(√(-1.1294090667581471`*^18 θ +
  8.987551787368176`*^16 θ^2 + 3.5481432270250993`*^18 Sin[β]^2)) /
  (√(-12.566370614359172` θ + θ^2 + 39.47841760435743` Sin[β]^2)) == η (1 / (θ / (2 π))), θ]
{{θ → 2.09585 × 10^-8 η}}
```

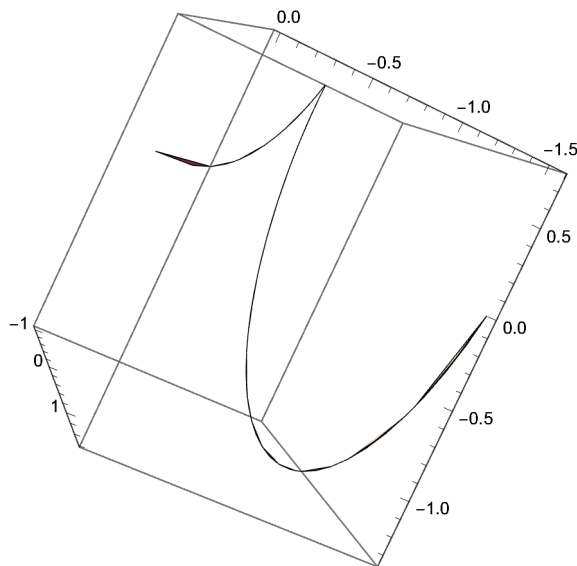
```
RevolutionPlot3D[2.0958450219516816`*^-8 η, {η, -1, 1}]
```



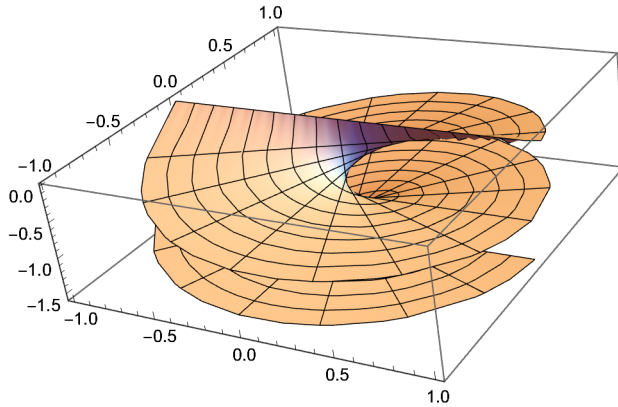
Solve[ $\left(\sqrt{(-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) = \eta (1 / (\theta / (2 \pi))) , \beta]$

$\left\{\left\{\beta \rightarrow -1. \operatorname{ArcSin}\left[\left(\sqrt{\theta} \sqrt{(-1.10318 \times 10^{24} \eta + 5.26365 \times 10^{31} \theta + 8.77883 \times 10^{22} \eta \theta - 4.18868 \times 10^{30} \theta^2)}\right) / \left(\sqrt{-3.46574 \times 10^{24} \eta + 1.65363 \times 10^{32} \theta}\right)\right]\right\}, \left\{\beta \rightarrow \operatorname{ArcSin}\left[\left(\sqrt{\theta} \sqrt{-1.10318 \times 10^{24} \eta + 5.26365 \times 10^{31} \theta + 8.77883 \times 10^{22} \eta \theta - 4.18868 \times 10^{30} \theta^2}\right) / \left(\sqrt{-3.46574 \times 10^{24} \eta + 1.65363 \times 10^{32} \theta}\right)\right]\right\}\right\}$

RevolutionPlot3D[  
 $\left\{\operatorname{ArcSin}\left[\left(\sqrt{\theta} \sqrt{(-1.1031799963798287 \cdot \eta^{24} + 5.263652535493924 \cdot \theta^{31} \theta + 8.778827477197447 \cdot \eta^{22} \eta \theta - 4.18868159871023 \cdot \theta^{30} \theta^2)}\right) / \left(\sqrt{-3.465742172214084 \cdot \eta^{24} + 1.6536252136556997 \cdot \theta^{32} \theta}\right)\right], \right.$   
 $\left.-1. \cdot \operatorname{ArcSin}\left[\left(\sqrt{\theta} \sqrt{(-1.1031799963798287 \cdot \eta^{24} + 5.263652535493924 \cdot \theta^{31} \theta + 8.778827477197447 \cdot \eta^{22} \eta \theta - 4.18868159871023 \cdot \theta^{30} \theta^2)}\right) / \left(\sqrt{-3.465742172214084 \cdot \eta^{24} + 1.6536252136556997 \cdot \theta^{32} \theta}\right)\right], \right.$   
 $\left.\{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



RevolutionPlot3D[  
 $-1. \cdot \text{ArcSin}\left[\left(\sqrt{\theta} \sqrt{(-1.1031799963798287 \cdot \eta^{24} + 5.263652535493924 \cdot \theta^{31} + 8.778827477197447 \cdot \eta^{22} \theta - 4.18868159871023 \cdot \theta^{30})}\right)\right] /$   
 $\left(\sqrt{-3.465742172214084 \cdot \eta^{24} + 1.6536252136556997 \cdot \theta^{32}}\right)\right],$   
 $\{\eta, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$



$v = \left(\sqrt{(3.5481432270250993 \cdot \eta^{18} - 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2)}\right) /$   
 $\left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right) =$   
 $D\left[\frac{1}{2\pi} \sqrt{r \sqrt{\left(1 - \frac{1}{c^2} \left((\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2)\right)}\right)}\right] /$   
 $\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)^2\right)$   
 $\sqrt{\theta} / \left(\sqrt{\left(1 - \frac{1}{c^2} \left((\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2)\right)}\right)}\right) /$   
 $\left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)^2\right)$   
 $\sqrt{4\pi r - r\theta},$   
 $r,$   
 $\theta,$   
 $\beta]$

$- \left( r \sqrt{4\pi r - r\theta} \left( \frac{7.09629 \times 10^{18} (-12.5664 + 2\theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} + \right. \right.$

$$\begin{aligned}
& \frac{78.9568 \left( -1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta \right) \cos[\beta] \sin[\beta]}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2} - \\
& \left( 157.914 \left( -12.5664 + 2 \theta \right) \cos[\beta] \sin[\beta] \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + \right. \right. \\
& \quad \left. \left. 3.54814 \times 10^{18} \sin[\beta]^2 \right) \right) / \left( c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^3 \right) \Bigg) \\
& \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)}}}}} \Bigg) / \\
& \left( 16 \pi \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)}} \right)^{3/2} \right) + \\
& \left( r^2 \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2 \right)}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2} \right. \\
& \quad \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)}}}}} \Bigg) / \left( 32 \pi \sqrt{4 \pi r - r \theta} \right. \\
& \quad \left. \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)}} \right)^{3/2} \right) - \\
& \left( r \left( 4 \pi - \theta \right) \theta \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \frac{\left( -12.5664 + 2 \theta \right) \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2 \right)}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2} \right) \Bigg) \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} + \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2 \right)}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \right) \left/ \left( 64 \pi \sqrt{4 \pi r - r \theta} \sqrt{\sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \right. \\
& \left. \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right. \\
& \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^2 \right) - \\
& \left( \theta \sqrt{4 \pi r - r \theta} \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \left. \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \right) \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
& \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left. \right) \left/ \left( 32 \pi \sqrt{\sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \right. \\
& \left. \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right. \\
& \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^2 \right) + \\
& \left( r \theta \sqrt{4 \pi r - r \theta} \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \left. \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \right)
\end{aligned}$$



$$\begin{aligned}
 & \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
 & \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
 & \left. \right) \left/ \left( 64 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right) \right. \\
 & \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right)^{3/2} \\
 & \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \Bigg) - \\
 & \left( r (4 \pi - \theta) \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
 & \quad \left. \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \right) \\
 & \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
 & \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
 & \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \Bigg) \left/ \right. \\
 & \left( 32 \pi \sqrt{4 \pi r - r \theta} \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
 & \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \Bigg) \Bigg) -
 \end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{4 \pi r - r \theta} \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \Bigg/ \\
& \left( 16 \pi \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right. \\
& \quad \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) - \\
& \left( r (4 \pi - \theta) \theta \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \quad \left. \right) \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \Bigg/ \\
& \left( 32 \pi (4 \pi r - r \theta)^{3/2} \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( \theta \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \\
& \quad \left. \right) \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \Bigg) / \\
& \left( 16 \pi \sqrt{4 \pi r - r \theta} \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}}} \right. \\
& \quad \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) - \\
& \left( r^2 (4 \pi - \theta) \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
& \quad \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \\
& \quad \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}}} \Bigg) / \\
& \left( 64 \pi \sqrt{4 \pi r - r \theta} \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right)^{3/2} \right. \\
& \quad \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right) \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( r \sqrt{4 \pi r - r \theta} \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \Bigg/ \\
& \left( 32 \pi \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right)^{3/2} \right. \\
& \quad \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right) \right) + \\
& \left( r \theta \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \quad \left. \right) \Bigg/ \left( 32 \pi \sqrt{4 \pi r - r \theta} \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \left. \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right. \\
& \quad \left. \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 3 r^2 \sqrt{4 \pi r - r \theta} \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \\
& \quad \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right) \\
& \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \Bigg/ \\
& \left( 64 \pi \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right)^{5/2} \right. \\
& \quad \left. \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right) + \\
& \left( r (4 \pi - \theta) \left( \frac{7.09629 \times 10^{18} (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} + \right. \right. \\
& \quad \frac{78.9568 (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} - \\
& \quad \left. (157.914 (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + \right. \\
& \quad \left. 3.54814 \times 10^{18} \sin[\beta]^2)) \Bigg/ \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^3 \right) \right) \\
& \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \Bigg/ \left( 16 \pi \sqrt{4 \pi r - r \theta} \right. \\
& \quad \left. \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \Bigg) + \\
& \left( \sqrt{4 \pi r - r \theta} \left( \frac{7.09629 \times 10^{18} (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} + \right. \right. \\
& \quad \frac{78.9568 (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} - \\
& \quad \left. \left. (157.914 (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + \right. \right. \\
& \quad \left. \left. 3.54814 \times 10^{18} \sin[\beta]^2)) \right) / \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^3 \right) \right) \\
& \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right) / \\
& \left( 8 \pi \sqrt{r} \sqrt{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \left. \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right) + \\
& \left( r^2 (4 \pi - \theta) \left( - \frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \\
& \quad \left. \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right) \right) / \\
& \left( 32 \pi (4 \pi r - r \theta)^{3/2} \sqrt{r} \sqrt{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \left. \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( r \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \\
& \quad \left. \right) \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \Bigg/ \\
& \left( 8 \pi \sqrt{4 \pi r - r \theta} \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \left. \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) + \\
& \left( (4 \pi - \theta) \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \left( \left( 3 \theta \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \right. \\
& \quad \left. \left. \frac{(-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right. \right. \\
& \quad \left. \left. \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \right. \\
& \quad \left. \left. \left( 78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3.54814 \times 10^{18} \sin[\beta]^2) \right) \right) \right) \Bigg/ \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2 \right) \Bigg) \Bigg/ \\
& \left( 4 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{5/2} \right) - \\
& \left( \theta \left( \frac{7.09629 \times 10^{18} (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} + \right. \right. \\
& \quad \frac{78.9568 (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} - \\
& \quad \left. (157.914 (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + \right.
\end{aligned}$$

$$\left. \left( 3.54814 \times 10^{18} \sin^2[\beta] \right) / \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin^2[\beta]^3) \right) \right)$$



$$\begin{aligned}
& \frac{78.9568 \left( -1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta \right) \cos[\beta] \sin[\beta]}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2} - \\
& \left( 157.914 \left( -12.5664 + 2 \theta \right) \cos[\beta] \sin[\beta] \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + \right. \right. \\
& \quad \left. \left. 3.54814 \times 10^{18} \sin[\beta]^2 \right) \right) / \left( c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^3 \right) \Bigg) / \\
& \left( 2 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} \right)^{3/2} \right) - \\
& \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} + \left( 78.9568 \cos[\beta] \sin[\beta] \right. \right. \\
& \quad \left. \left. \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2 \right) \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2 \right) \right) / \\
& \left( 2 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} \right)^{3/2} \right) \Bigg) / \\
& \left( 8 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)}}}} \right. \\
& \quad \left. \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)}}}} \right) - \\
& \left( r \sqrt{4 \pi r - r \theta} \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left. \frac{78.9568 \cos[\beta] \sin[\beta] \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2 \right)}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2} \right) \right. \\
& \quad \left. \left( \left( \theta \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)} + \right. \right. \right. \right. \\
& \quad \left. \left. \left( (-12.5664 + 2 \theta) \left( -1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin[\beta]^2 \right) \right) / \left( c^2 \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^2 \right) \right) \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) + \\
& \left. \frac{1}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) / \\
& \left( 32 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}}} \right. \\
& \left. \left( r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right)^{3/2} \right) + \\
& \left( (4 \pi - \theta) \theta \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \left. \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \right. \\
& \left. \left. \right) \sqrt{r \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right. \\
& \left( - \left( \left( \theta \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + (-12.5664 + 2 \theta) \right. \right. \right. \right. \\
& \left. \left. \left. (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2) \right) \right) / \right. \\
& \left. \left. \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2 \right) \right) \right) / \\
& \left( 2 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) + \\
& \left. \frac{1}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( 32 \pi \sqrt{4 \pi r - r \theta} \left( \frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) \right)^{3/2} \\
& \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \Bigg) + \\
& \left( \theta \sqrt{4 \pi r - r \theta} \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \\
& \left. \left. \left( -\left( \left( \theta \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \right. \right. \right. \\
& \left. \left. \left( (-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2) \right) \right) \right) \right) \Bigg) \Bigg) / \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2 \right) \Bigg) \Bigg) / \\
& \left( 2 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) \Bigg) + \\
& \left( \frac{1}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) \Bigg) \Bigg) / \\
& \left( 32 \pi \left( \frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) \right)^{3/2} \\
& \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \\
& \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right) \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& \left( r (4 \pi - \theta) \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2} \\
& \quad \left. \left. \left( -\left( \theta \left( -\frac{-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left( (-12.5664 + 2 \theta) (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2) \right) / \left( c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2 \right) \right) \right) / \right. \\
& \quad \left. \left( 2 \left( 1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} \right)^{3/2} \right) \right) + \\
& \quad \left. \frac{1}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}} \right) / \\
& \quad \left( 32 \pi \sqrt{4 \pi r - r \theta} \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}}}} \right. \\
& \quad \sqrt{r} \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \\
& \quad \left. \sqrt{1 - \frac{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}} \right) + \\
& \quad \left( \sqrt{4 \pi r - r \theta} \left( -\frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta]}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)} + \right. \right. \\
& \quad \frac{78.9568 \cos[\beta] \sin[\beta] (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)}{c^2 (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^2}
\end{aligned}$$

$$- \left( r \sqrt{4 \pi r - r \theta} \left( \frac{7.096286454050199 \cdot 10^{18} (-12.566370614359172 \cdot \theta + 2 \theta) \cos[\beta] \sin[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^2} + \right. \right. \\ (78.95683520871486 \cdot \\ (-1.1294090667581471 \cdot 10^{18} + 1.7975103574736352 \cdot 10^{17} \theta) \cos[\beta] \sin[\beta]) / \\ \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^2 \right) - \right. \\ (157.91367041742973 \cdot (-12.566370614359172 \cdot \theta + 2 \theta) \cos[\beta] \sin[\beta] \\ (-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \\ \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2) \right) /$$

$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)^3 \right) \Bigg) \\
& \sqrt{\sqrt{\frac{\theta}{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)}}}} \Bigg) / \\
& \left( 16 \pi \left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right) \right) / \right. \right. \\
& \quad \left. \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right) \right)^{3/2} \right) + \\
& \left( r^2 \left( - \frac{7.096286454050199 \, \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left. \frac{(78.95683520871486 \, \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right))}{\left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right)^2} \right) \right) \\
& \sqrt{\sqrt{\frac{\theta}{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)}}}} \Bigg) / \\
& \left( 32 \pi \sqrt{4 \pi r - r \theta} \left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right) \right) / \right. \right. \\
& \quad \left. \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right) \right)^{3/2} \right) - \\
& \left( r (4 \pi - \theta) \theta \left( - \frac{-1.1294090667581471 \, \theta + 1.7975103574736352 \, \theta^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left. \frac{((-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right))}{\left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right)^2} \right) \right) \\
& \left( - \frac{7.096286454050199 \, \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)} + \right. \\
& \quad \left. \frac{(78.95683520871486 \, \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right))}{\left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right)^2} \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \right. \right. \\
& \quad \left. \left. \sin[\beta]^2 \right)^2 \right) \Bigg) \Bigg/ \left( 64 \pi \sqrt{4 \pi r - r \theta} \right. \\
& \quad \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)}}}} \right. \\
& \quad \left. \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + \right. \right. \right. \right.} \right. \\
& \quad \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right) \right) / \right.} \\
& \quad \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right) \right) \Bigg) \\
& \quad \left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right. \\
& \quad \quad \left. \left. 3.5481432270250993 \, \sin[\beta]^2 \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right)^2 \right) \Bigg) - \\
& \quad \left( \theta \sqrt{4 \pi r - r \theta} \left( - \frac{-1.1294090667581471 \, \theta + 1.7975103574736352 \, \theta^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)} + \right. \right. \\
& \quad \quad \left. \left( (-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \quad \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right) \right) / \right. \\
& \quad \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)^2 \right) \right) \Bigg) \\
& \quad \left( - \frac{7.096286454050199 \, \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)} + \right. \\
& \quad \quad \left. \frac{(78.95683520871486 \, \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \\
& \quad \quad \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right) \right) /}{\left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)^2 \right)} \right) \Bigg) \Bigg/ \\
& \quad \left( 32 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right)}}}} \right. \\
& \quad \left. \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + \right. \right. \right. \right.} \right. \\
& \quad \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \sin[\beta]^2 \right) \right) / \right.} \\
& \quad \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \sin[\beta]^2 \right) \right) \right) \Bigg) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right)^2 \right) + \\
& \left( r \theta \sqrt{4\pi r - r\theta} \left( -\frac{-1.1294090667581471 \cdot \theta^{18} + 1.7975103574736352 \cdot \theta^{17}}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \right. \\
& \quad \left. \left( (-12.566370614359172 + 2\theta) \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \right) \\
& \left( -\frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \\
& \quad \left. (78.95683520871486 \cdot \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right)) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \right) \Bigg) / \\
& \left( 64\pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)}}}} \right. \\
& \quad \left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \right)^{3/2}} \\
& \quad \left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \right)^{3/2} \Bigg) - \\
& \left( r (4\pi - \theta) \left( -\frac{-1.1294090667581471 \cdot \theta^{18} + 1.7975103574736352 \cdot \theta^{17}}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \right. \\
& \quad \left. \left( (-12.566370614359172 + 2\theta) \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \right) \Bigg)
\end{aligned}$$



$$\begin{aligned}
& \left( \frac{8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} \right) / \\
& \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} + \right. \\
& \left. \frac{(78.95683520871486 \cdot \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right))}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} \right) / \\
& \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2}}}}} / \\
& \left( 32 \pi \sqrt{4 \pi r - r \theta} \sqrt{r \sqrt{\left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right.} \right. \\
& \left. \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \right)} \right) / \\
& \left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \\
& \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \right)^{3/2} - \\
& \left( \sqrt{4 \pi r - r \theta} \left( - \frac{-1.1294090667581471 \cdot \theta^{18} + 1.7975103574736352 \cdot \theta^{17}}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} + \right. \right. \\
& \left. \left. \frac{\left( (-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right)}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} \right) \right) / \\
& \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} + \right. \\
& \left. \frac{(78.95683520871486 \cdot \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta] \right))}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2} \right) /
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])}}}}} \Bigg/ \\
& \left( 16 \pi \sqrt{r} \sqrt{\left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \right. \\
& \quad \left. \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]) \right) \right) \right) \\
& \left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \\
& \quad \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]) \right) \right)^{3/2} - \\
& \left( r (4 \pi - \theta) \theta \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])} + \right. \right. \\
& \quad \left. \left. (78.95683520871486 \cdot \cos[\beta] \sin[\beta] (-1.1294090667581471 \cdot \theta^{18} + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta])) / \right. \right. \\
& \quad \left. \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])^2 \right) \right) \right) \\
& \sqrt{r} \sqrt{\left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin^2[\beta] \right) / \left( c^2 (-12.566370614359172 \cdot \theta + \right. \right. \\
& \quad \left. \left. \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]) \right) \right) \Bigg/ \left( 32 \pi (4 \pi r - r \theta)^{3/2} \right. \\
& \quad \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])}}}}} \right. \\
& \quad \left. \left( 1 - \left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \cdot \sin^2[\beta] \right) / \right. \right. \\
& \quad \left. \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]) \right) \right) \right)^{3/2} + \\
& \left( \theta \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])} + \right. \right. \\
& \quad \left. \left. (78.95683520871486 \cdot \cos[\beta] \sin[\beta] (-1.1294090667581471 \cdot \theta^{18} + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin^2[\beta])) / \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \\
& \sqrt{\left( r \sqrt{1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right.} \right. \\
& \quad \left. \left. 3.5481432270250993 \, \theta \text{Sin}[\beta]^2 \right) / \left( c^2 \left( -12.566370614359172 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \Bigg) / \left( 16 \pi \sqrt{4 \pi r - r \theta} \right. \\
& \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \theta \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}} \right. \\
& \left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \theta \text{Sin}[\beta]^2 \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right)^{3/2} \right) - \\
& \left( r^2 (4 \pi - \theta) \left( - \frac{-1.1294090667581471 \, \theta + 1.7975103574736352 \, \theta}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left( (-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \theta \text{Sin}[\beta]^2 \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \right) \\
& \left( - \frac{7.096286454050199 \, \text{Cos}[\beta] \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \\
& \quad \left. \left( 78.95683520871486 \, \text{Cos}[\beta] \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \theta \text{Sin}[\beta]^2 \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \right) \\
& \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \theta \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}} \right) / \\
& \left( 64 \pi \sqrt{4 \pi r - r \theta} \left( r \sqrt{1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right.} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{\theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} \right)^{3/2} \\
& \left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \\
& \quad \left. \left. \frac{3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} \right) \right) - \\
& \left( r \sqrt{4\pi r - r\theta} \left( -\frac{-1.1294090667581471 \cdot \theta + 1.7975103574736352 \cdot \theta}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \right. \\
& \quad \left. \left( (-12.566370614359172 \cdot \theta + 2\theta) \left( -1.1294090667581471 \cdot \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \Bigg) \\
& \left( -\frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \\
& \quad \left( 78.95683520871486 \cdot \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \cdot \theta + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \Bigg) \\
& \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)}}}}} \Bigg) / \\
& \left( 32\pi \left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} \right) \right) \right)^{3/2} \\
& \left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \\
& \quad \left. \left. \frac{3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} \right) \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \Bigg) + \\
& \left( r \theta \left( -\frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \right. \\
& \quad \left( 78.95683520871486 \cdot \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \cdot \theta + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \Bigg)
\end{aligned}$$



$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right)^{5/2} \\
& \sqrt{\left( 1 - \left( -1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) \right) /} \\
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right) + \\
& \left( r (4 \pi - \theta) \left( \frac{7.096286454050199 \theta + 1.7975103574736352 \theta^2 \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2} + \right. \right. \\
& \quad (78.95683520871486 \theta \\
& \quad \left. \left. (-1.1294090667581471 \theta + 1.7975103574736352 \theta^2 \cos[\beta] \sin[\beta]) \right) / \right. \\
& \quad \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2 \right) - \\
& \quad (157.91367041742973 \theta + 1.7975103574736352 \theta^2 \cos[\beta] \sin[\beta] \\
& \quad \left. \left. (-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^3 \right) \right) \\
& \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2}{c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)}}}} \Bigg/ \\
& \left( 16 \pi \sqrt{4 \pi r - r \theta} \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \theta + \right. \right. \right. \right.} \\
& \quad \left. \left. \left. 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2 \right) \right) /} \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right) \right) \\
& \sqrt{\left( 1 - \left( -1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) \right) /} \\
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right) + \\
& \left( \sqrt{4 \pi r - r \theta} \left( \frac{7.096286454050199 \theta + 1.7975103574736352 \theta^2 \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2} + \right. \right. \\
& \quad (78.95683520871486 \theta \\
& \quad \left. \left. (-1.1294090667581471 \theta + 1.7975103574736352 \theta^2 \cos[\beta] \sin[\beta]) \right) / \right. \\
& \quad \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2 \right) - \\
& \quad (157.91367041742973 \theta + 1.7975103574736352 \theta^2 \cos[\beta] \sin[\beta] \\
& \quad \left. \left. (-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^3 \right) \\
& \sqrt{\sqrt{\frac{\theta}{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}} \Bigg/ \\
& \left( 8 \pi \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right. \right.} \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) / \right.} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \Bigg) \\
& \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right.} \\
& \quad \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) /} \\
& \quad \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \Bigg) + \\
& \left( r^2 (4 \pi - \theta) \left( - \frac{7.096286454050199 \, \text{Cos}[\beta] \, \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \, \text{Cos}[\beta] \, \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \right) \Bigg) \\
& \sqrt{\sqrt{\frac{\theta}{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}} \Bigg/ \\
& \left( 32 \pi (4 \pi r - r \theta)^{3/2} \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + \right. \right. \right.} \right. \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) / \right.} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \Bigg) \\
& \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right.} \\
& \quad \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) /} \\
& \quad \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \Bigg) - \\
& \left( r \left( - \frac{7.096286454050199 \, \text{Cos}[\beta] \, \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \, \text{Cos}[\beta] \, \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \Bigg) \\
& \sqrt{\sqrt{\frac{\theta}{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}} \Bigg) / \\
& \left( 8 \pi \sqrt{4 \pi r - r \theta} \sqrt{r \sqrt{1 - \left( -1.1294090667581471 \, \theta + \right.} \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) / \right.} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \Bigg) \\
& \sqrt{1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right.} \\
& \quad \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) /} \\
& \quad \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \Bigg) + \\
& \left( (4 \pi - \theta) \sqrt{r \sqrt{1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right.} \right. \\
& \quad \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) /} \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \Bigg) \\
& \left( \left( 3 \theta \left( - \frac{-1.1294090667581471 \, \theta + 1.7975103574736352 \, \theta}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \right. \\
& \quad \left. \left. \left( (-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \, \theta + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) \right) /} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right)^2 \right) \Bigg) \\
& \left( - \frac{7.096286454050199 \, \text{Cos}[\beta] \, \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \\
& \quad \left. (78.95683520871486 \, \text{Cos}[\beta] \, \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) /} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right)^2 \right) \Bigg) \Bigg) / \\
& \left( 4 \left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) / \left( c^2 \right. \right. \\
& \quad \left. \left. \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right)^{5/2} - \\
& \left( \theta \left( \frac{7.096286454050199 \, \text{Cos}[\beta] \, \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left. (78.95683520871486 \, \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 1.7975103574736352 \, \theta \right) \text{Cos}[\beta] \, \text{Sin}[\beta] \right) \right) \right) /}
\end{aligned}$$



$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) - \\
& \left( 157.91367041742973 \, \left( -12.566370614359172 \, \theta + 2 \, \theta \right) \text{Cos}[\beta] \text{Sin}[\beta] \right. \\
& \quad \left. \left( -1.1294090667581471 \, \theta^{18} + 8.987551787368176 \, \theta^{16} \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2 \right) \right) / \\
& \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^3 \right) \Bigg) / \\
& \left( 2 \left( 1 - \left( -1.1294090667581471 \, \theta^{18} + 8.987551787368176 \, \theta^{16} \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2 \right) / \left( c^2 \right. \right. \\
& \quad \left. \left. \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right)^{3/2} \Bigg) - \\
& \left( - \frac{7.096286454050199 \, \theta^{18} \text{Cos}[\beta] \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \\
& \quad \left. \left( 78.95683520871486 \, \text{Cos}[\beta] \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta^{18} + \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^{16} \theta^2 + 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2 \right) \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \right) / \\
& \left( 2 \left( 1 - \left( -1.1294090667581471 \, \theta^{18} + 8.987551787368176 \, \theta^{16} \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2 \right) / \left( c^2 \left( -12.566370614359172 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right)^{3/2} \Bigg) \Bigg) / \left( 8 \pi \sqrt{4 \pi r - r \theta} \right. \\
& \quad \left. \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta^{18} + 8.987551787368176 \, \theta^{16} \theta^2 + 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}} \right) + \\
& \left( \sqrt{4 \pi r - r \theta} \sqrt{1 - \left( -1.1294090667581471 \, \theta^{18} + 8.987551787368176 \, \theta^{16} \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2 \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \\
& \left( \left( 3 \theta \left( - \frac{-1.1294090667581471 \, \theta^{18} + 1.7975103574736352 \, \theta^{17} \theta}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \right. \\
& \quad \left. \left. \left( -12.566370614359172 \, \theta + 2 \, \theta \right) \left( -1.1294090667581471 \, \theta^{18} + \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^{16} \theta^2 + 3.5481432270250993 \, \theta^{18} \text{Sin}[\beta]^2 \right) \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2 \right) \\
& \left( - \frac{7.096286454050199 \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)} + \right. \\
& \quad \left( 78.95683520871486 \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \theta + \right. \right. \\
& \quad \quad \left. \left. 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2 \right) \right) \Bigg) / \\
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2 \right) \Bigg) / \\
& \left( 4 \left( 1 - \left( -1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) / \left( c^2 \right. \right. \\
& \quad \left. \left. \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right)^{5/2} \right) - \\
& \left( \theta \left( \frac{7.096286454050199 \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \left( -1.1294090667581471 \theta + \right. \right. \right. \\
& \quad \quad \left. \left. 1.7975103574736352 \theta \right) \cos[\beta] \sin[\beta] \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2 \right) - \\
& \quad \left( 157.91367041742973 \left( -12.566370614359172 \theta + 2 \theta \right) \cos[\beta] \sin[\beta] \right. \\
& \quad \quad \left. \left( -1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \\
& \quad \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) \right) \Bigg) / \\
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^3 \right) \Bigg) / \\
& \left( 2 \left( 1 - \left( -1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) / \left( c^2 \right. \right. \\
& \quad \left. \left. \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right)^{3/2} \right) - \\
& \left( - \frac{7.096286454050199 \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)} + \right. \\
& \quad \left( 78.95683520871486 \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \theta + \right. \right. \\
& \quad \quad \left. \left. 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2 \right) \right) \Bigg) / \\
& \left( c^2 \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right)^2 \right) \Bigg) / \\
& \left( 2 \left( 1 - \left( -1.1294090667581471 \theta + 8.987551787368176 \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \sin[\beta]^2 \right) / \left( c^2 \right. \right. \\
& \quad \left. \left. \left( -12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2 \right) \right)^{3/2} \right) \Bigg) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 8 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \varrho^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)}}}} \right. \\
& \quad \sqrt{\left( r \sqrt{1 - \left( -1.1294090667581471 \cdot \theta^{18} \varrho + \right.} \right. \\
& \quad \quad \left. \left. 8.987551787368176 \cdot \theta^{16} \varrho^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2 \right) /} \right. \\
& \quad \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2) \right) \right) \Bigg) - \\
& \left( r \sqrt{4 \pi r - r \theta} \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \cdot \cos[\beta] \sin[\beta] (-1.1294090667581471 \cdot \theta^{18} \varrho + \right. \right. \\
& \quad \quad \left. \left. 8.987551787368176 \cdot \theta^{16} \varrho^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2) \right) / \right. \\
& \quad \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^2 \right) \right) \Bigg) \\
& \left( - \left( \theta \left( - \frac{-1.1294090667581471 \cdot \theta^{18} + 1.7975103574736352 \cdot \theta^{17} \varrho}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)} + \right. \right. \right. \\
& \quad \left. \left( (-12.566370614359172 \cdot \theta + 2 \theta) (-1.1294090667581471 \cdot \theta^{18} \varrho + \right. \right. \\
& \quad \quad \left. \left. 8.987551787368176 \cdot \theta^{16} \varrho^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2) \right) \right) / \right. \\
& \quad \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^2 \right) \right) \Bigg) / \\
& \left( 2 \left( 1 - (-1.1294090667581471 \cdot \theta^{18} \varrho + 8.987551787368176 \cdot \theta^{16} \varrho^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2) \right) / \right. \\
& \quad \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2) \right) \right)^{3/2} + \\
& \quad \left. \frac{1}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} \varrho + 8.987551787368176 \cdot \theta^{16} \varrho^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)}}}} \right) \Bigg) / \\
& \left( 32 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} \varrho + 8.987551787368176 \cdot \theta^{16} \varrho^2 + 3.5481432270250993 \cdot \theta^{18} \sin[\beta]^2}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)}}}} \right)
\end{aligned}$$

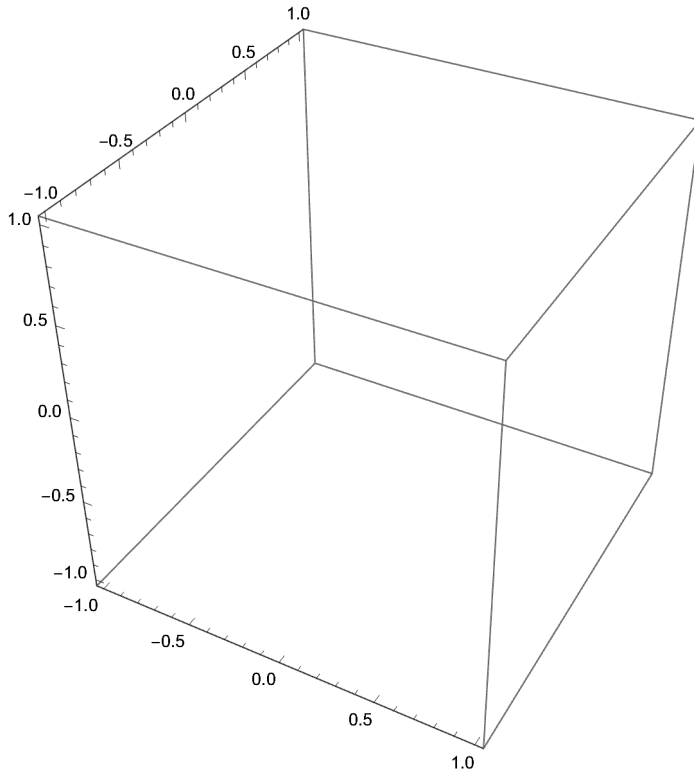
$$\begin{aligned}
& \left( r \sqrt{1 - (-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \right. \\
& \quad \left. \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta])} \right) / \\
& \quad \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]) \right) \Big)^{3/2} + \\
& \left( (4\pi - \theta) \theta \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])} + \right. \right. \\
& \quad (78.95683520871486 \cdot \cos[\beta] \sin[\beta] (-1.1294090667581471 \cdot \theta^{18} + \\
& \quad \left. 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta])) \right) / \\
& \quad \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])^2 \right) \Big) \\
& \sqrt{r \sqrt{1 - (-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + \\
& \quad 3.5481432270250993 \cdot \sin^2[\beta])} / \\
& \quad (c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])) \Big) \\
& \left( - \left( \theta \left( - \frac{-1.1294090667581471 \cdot \theta^{18} + 1.7975103574736352 \cdot \theta^{17}}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])} + \right. \right. \right. \\
& \quad \left. \left. \left( (-12.566370614359172 \cdot \theta + 2\theta) (-1.1294090667581471 \cdot \theta^{18} + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]) \right) \right) \right) / \\
& \quad \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])^2 \right) \Big) \Big) / \\
& \quad \left( 2 (1 - (-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + \right. \\
& \quad \left. 3.5481432270250993 \cdot \sin^2[\beta]) / \right. \\
& \quad \left. \left( c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]) \right) \right) \Big)^{3/2} + \\
& \quad \left. \frac{1}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])}}} \right) \Big) \Big) / \left( 32 \right. \\
& \pi \sqrt{4\pi r - r\theta} \\
& \left( \frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 (-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta])}}} \right) \Big)^{3/2} \\
& (1 - (-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} \theta^2 +
\end{aligned}$$

$$\begin{aligned}
& 3.5481432270250993 \cdot \sin^2[\beta] \Bigg/ \\
& \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right)^{3/2} \Bigg) + \\
& \left( \theta \sqrt{4 \pi r - r \theta} \left( - \frac{7.096286454050199 \cdot \cos[\beta] \sin[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \cdot \cos[\beta] \sin[\beta] \left( -1.1294090667581471 \cdot \theta + \right. \right. \right. \\
& \quad \quad \left. \left. 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) \Bigg/ \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \right) \\
& \left( - \left( \theta \left( - \frac{-1.1294090667581471 \cdot \theta + 1.7975103574736352 \cdot \theta}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} + \right. \right. \right. \\
& \quad \left. \left( (-12.566370614359172 \cdot \theta + 2 \theta) \left( -1.1294090667581471 \cdot \theta + \right. \right. \right. \\
& \quad \quad \left. \left. 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta] \right) \right) \Bigg/ \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)^2 \right) \right) \Bigg) \Bigg/ \\
& \left( 2 \left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin^2[\beta] \right) \Bigg/ \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right)^{3/2} \right) + \\
& \left. \frac{1}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)}}} \right) \Bigg/ \\
& \left( 32 \pi \left( \frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta]}{c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)}}} \right) \right)^{3/2} \\
& \sqrt{r \sqrt{1 - \left( -1.1294090667581471 \cdot \theta + \right.} \\
& \quad \left. 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin^2[\beta] \right) \Bigg/} \\
& \quad \left( c^2 \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta] \right) \right) \\
& \left( 1 - \left( -1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \cdot \sin^2[\beta] \right) \Bigg/ \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) + \\
& \left( r (4 \pi - \theta) \left( - \frac{7.096286454050199 \, \text{Cos}[\beta] \, \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \, \text{Cos}[\beta] \, \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \right) \\
& \left( - \left( \theta \left( - \frac{-1.1294090667581471 \, \theta + 1.7975103574736352 \, \theta}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \right. \\
& \quad \left. \left( (-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \right) \right) / \\
& \quad \left( 2 \left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right. \right. \\
& \quad \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) / \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right)^{3/2} + \\
& \quad \left. \frac{1}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}} \right) \right) / \left( 32 \right. \\
& \pi \sqrt{4 \pi r - r \theta} \\
& \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}} \\
& \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + \right. \right. \right.} \\
& \quad \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) /} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \right) \\
& \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right.} \\
& \quad \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) /}
\end{aligned}$$

$$\begin{aligned}
& \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) + \\
& \left( \sqrt{4 \pi r - r \theta} \left( - \frac{7.096286454050199 \, \text{Cos}[\beta] \, \text{Sin}[\beta]}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \\
& \quad \left. \left( 78.95683520871486 \, \text{Cos}[\beta] \, \text{Sin}[\beta] \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \Bigg) \\
& \left( - \left( \theta \left( - \frac{-1.1294090667581471 \, \theta + 1.7975103574736352 \, \theta}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)} + \right. \right. \right. \\
& \quad \left. \left( (-12.566370614359172 + 2 \theta) \left( -1.1294090667581471 \, \theta + \right. \right. \right. \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) \right) / \\
& \quad \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)^2 \right) \Bigg) / \\
& \quad \left( 2 \left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) / \right. \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right)^{3/2} \right) + \\
& \quad \left. \frac{1}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}} \right) \Bigg) / \\
& \left( 16 \pi \sqrt{\frac{\theta}{\sqrt{1 - \frac{-1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2}{c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right)}}}}} \right. \\
& \quad \sqrt{\left( r \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + \right. \right. \right.} \\
& \quad \left. \left. \left. 8.987551787368176 \, \theta^2 + 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) / \right.} \\
& \quad \left. \left( c^2 \left( -12.566370614359172 \, \theta + \theta^2 + 39.47841760435743 \, \text{Sin}[\beta]^2 \right) \right) \right) \Bigg) \\
& \quad \sqrt{\left( 1 - \left( -1.1294090667581471 \, \theta + 8.987551787368176 \, \theta^2 + \right. \right.} \\
& \quad \left. \left. \left. 3.5481432270250993 \, \text{Sin}[\beta]^2 \right) \right) / \left( c^2 \left( -12.566370614359172 \, \theta + \right. \right.} \right.
\end{aligned}$$

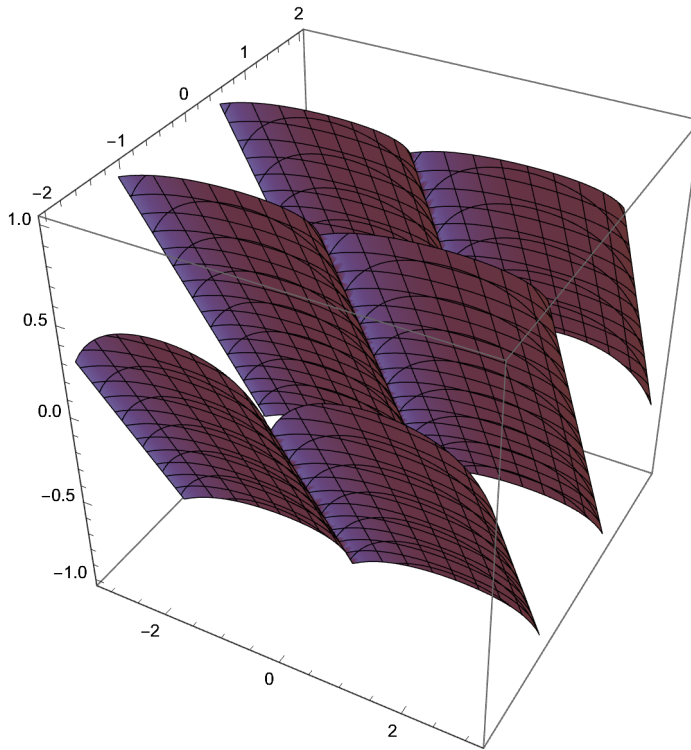
$$\left. \theta^2 + 39.47841760435743 \sin[\beta]^2) \right) \Bigg] , \{ \theta, -2\pi, 2\pi \}, \{ \beta, -\pi, \pi \} \Bigg]$$



$$r := 4 \star (10^{-9})$$



ContourPlot3D $\left[-\frac{1}{\sqrt{3}\pi}\left(\sqrt{3}j\pi+\sqrt{3}k\pi-3\operatorname{Log}\left[-1+\frac{4\pi}{3}-(-4\pi^2+12\pi^2\sin[\beta]^2)\right]\right)\right.$   
 $\left.\left(6\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right)+\right.$   
 $\left.\frac{2}{3}\left(-\pi^3+18\pi^3\sin[\beta]^2+3\sqrt{3}\sqrt{-\pi^6\sin[\beta]^2+11\pi^6\sin[\beta]^4+\pi^6\sin[\beta]^6}\right)^{1/3}\right],$   
 $\{\beta,-\pi,\pi\},\{k,-2,2\},\{j,-1,1\}]$



# On the Processing of Tachyon Emulsion from a Photon' s Energy

by Parker Emmerson

In the name of Allah, the following mathematics is invoked, may there be truth to it. Irony from the combination of two unlike things is the meaning of the act of emulsion.

I recommend further studies into the realm of complex infinity including systems that can account for counting from infinity like we count from zero.

These are theoretical models that suppose that the velocity of a tachyon is positive as well as the

velocity of a regular particle.

## Velocity of a Photon's Geometry

Only when the exact speed of light, or an extremely close approximation is used during the solution of these equations are any solutions able to be found. If I use a variable  $c$ , the equation cancels out. Only when designating  $c$  to be numerically the exact value of light or close to it can the equation be solved for the innate velocity.

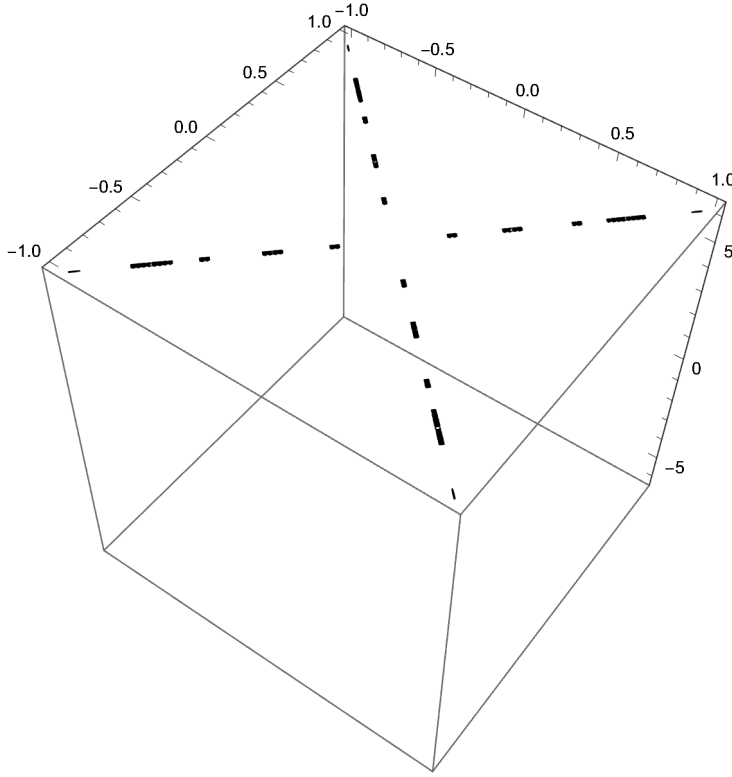
$$c := 2.99792458$$

$$\text{Solve} \left[ \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, v \right]$$

$$\left\{ \left\{ v \rightarrow - \frac{1. \sqrt{3.54814 \times 10^{18} \eta^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 \eta^2 - 12.5664 r^2 \theta + r^2 \theta^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{3.54814 \times 10^{18} \eta^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2}}{\sqrt{39.4784 \eta^2 - 12.5664 r^2 \theta + r^2 \theta^2}} \right\} \right\}$$

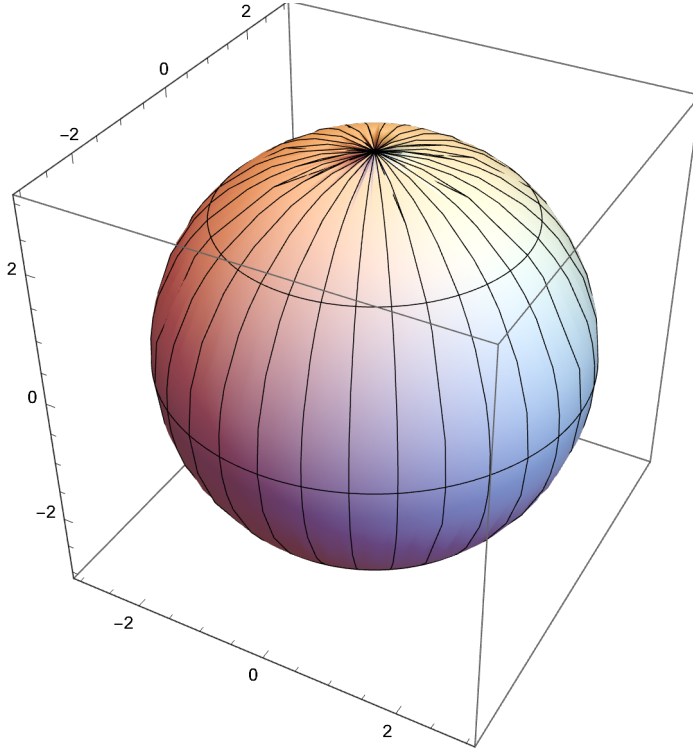
ContourPlot3D[ $\left(\sqrt{\left(3.5481432270250993 \cdot \eta^{18} - 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2\right)}\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right), \{r, -1, 1\}, \{\eta, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$



$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2}}{\sqrt{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2}}\right\}, \left\{v \rightarrow \frac{\sqrt{-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2}}{\sqrt{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2}}\right\}\right\}$$

```
SphericalPlot3D[( $\sqrt{(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2)}$ )/
( $\sqrt{(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2)}$ ), { $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi/2$ ,  $\pi/2$ }]
```



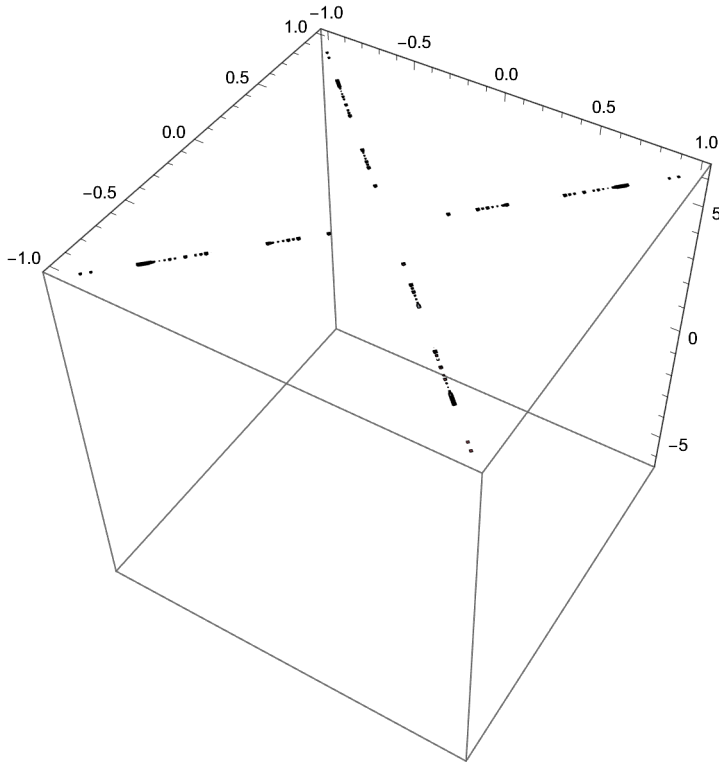
## Velocity of a Tachyon' s Geometry

$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{(v)^2}{2.99792458^2} - 1} \sqrt{\frac{\theta}{\sqrt{\frac{(v)^2}{2.99792458^2} - 1}}} \sqrt{4\pi r - r\theta}}{2\pi} = \eta, v\right]$$

$$\left\{ \left\{ v \rightarrow -\frac{1. \sqrt{2.82899 \times 10^{25} \eta^2 - 9.00495 \times 10^{24} r^2 \theta + 7.16591 \times 10^{23} r^2 \theta^2}}{\sqrt{3.14767 \times 10^{24} \eta^2 - 1.00194 \times 10^{24} r^2 \theta + 7.97315 \times 10^{22} r^2 \theta^2}} \right\}, \right.$$

$$\left. \left\{ v \rightarrow \frac{\sqrt{2.82899 \times 10^{25} \eta^2 - 9.00495 \times 10^{24} r^2 \theta + 7.16591 \times 10^{23} r^2 \theta^2}}{\sqrt{3.14767 \times 10^{24} \eta^2 - 1.00194 \times 10^{24} r^2 \theta + 7.97315 \times 10^{22} r^2 \theta^2}} \right\} \right\}$$

```
ContourPlot3D[( $\sqrt{(2.8289887706190094 \cdot 10^{25} \eta^2 - 9.004950935909588 \cdot 10^{24} r^2 \theta + 7.16591226875 \cdot 10^{23} r^2 \theta^2)}$ )/
( $\sqrt{(3.147674514204298 \cdot 10^{24} \eta^2 - 1.0019359163599887 \cdot 10^{24} r^2 \theta + 7.9731526875 \cdot 10^{22} r^2 \theta^2)}$ ), {r, -1, 1}, {η, -1, 1}, {θ, -2 π, 2 π}]
```

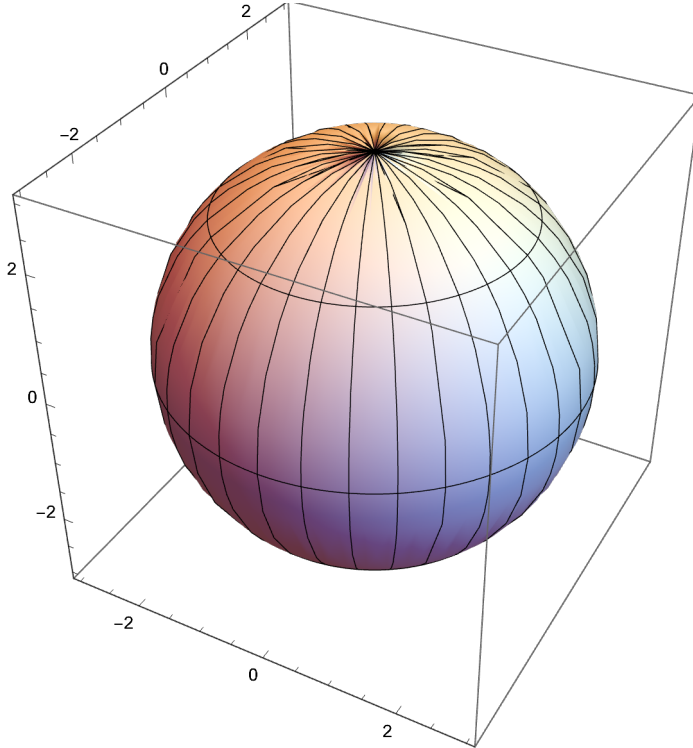


$$\text{Solve}\left[\frac{\sqrt{r} \sqrt{\frac{(v)^2}{c^2} - 1} \sqrt{\frac{\theta}{\sqrt{\frac{(v)^2}{c^2} - 1}}} \sqrt{4 \pi r - r \theta}}{2 \pi} == r \sin[\beta], v\right]$$

$$\left\{\left\{v \rightarrow -\frac{1. \sqrt{-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2}}{\sqrt{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2}}\right\},\right.$$

$$\left.\left\{v \rightarrow \frac{\sqrt{-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2}}{\sqrt{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2}}\right\}\right\}$$

```
SphericalPlot3D[( $\sqrt{(-9.004950935909588 \cdot \theta^{24} + 7.16591226875 \cdot \theta^{23} \theta^2 + 2.8289887706190094 \cdot \sin[\beta]^2)}$ )/
( $\sqrt{(-1.0019359163599887 \cdot \theta^{24} \theta + 7.9731526875 \cdot \theta^{22} \theta^2 + 3.147674514204298 \cdot \sin[\beta]^2)}$ ), { $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi/2$ ,  $\pi/2$ }]
```



A clear conclusion : The innate velocity expressions are exactly the same.

```
Solve[( $\sqrt{(-9.004950935909588 \cdot \theta^{24} + 7.16591226875 \cdot \theta^{23} \theta^2 + 2.8289887706190094 \cdot \sin[\beta]^2)}$ )/
( $\sqrt{(-1.0019359163599887 \cdot \theta^{24} \theta + 7.9731526875 \cdot \theta^{22} \theta^2 + 3.147674514204298 \cdot \sin[\beta]^2)}$ )) ==
( $\sqrt{(-9.004950935909588 \cdot \theta^{24} \theta + 7.16591226875 \cdot \theta^{23} \theta^2 + 2.8289887706190094 \cdot \sin[\beta]^2)}$ )/
( $\sqrt{(-1.0019359163599887 \cdot \theta^{24} \theta + 7.9731526875 \cdot \theta^{22} \theta^2 + 3.147674514204298 \cdot \sin[\beta]^2)}$ )),  $\theta$ ]
```

```
{{{}}}
```

$$\text{Solve}\left[\left(\sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2}\right) / \left(\sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2}\right) == \left(\sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2}\right) / \left(\sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2}\right), \beta\right]$$

$$\{\{\}\}$$

$$\text{Check}\left[\left(\sqrt{3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2}\right) / \left(\sqrt{39.47841760435743 \cdot 10^{18} \eta^2 - 12.566370614359172 \cdot 10^{18} r^2 \theta + r^2 \theta^2}\right) == \left(\sqrt{2.8289887706190094 \cdot 10^{25} \eta^2 - 9.004950935909588 \cdot 10^{24} r^2 \theta + 7.16591226875 \cdot 10^{23} r^2 \theta^2}\right) / \left(\sqrt{3.147674514204298 \cdot 10^{24} \eta^2 - 1.0019359163599887 \cdot 10^{24} r^2 \theta + 7.9731526875 \cdot 10^{22} r^2 \theta^2}\right), \eta\right]$$

$$\{\}$$

This suggests that information from a photon could be emulsed onto a Tachyon.

$$u = v =$$

$$\lambda f = \left(\sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2}\right) / \left(\sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2}\right) == \lambda (1 / (\theta / 2 \pi)) = \lambda (1 / (\theta / 2 \pi))$$

$$E = h (1 / (\theta / 2 \pi)) = m c^2 / \sqrt{1 - (u^2 / c^2)} = (i m) c^2 / \sqrt{(u^2 / c^2) - 1}$$

## Mass of the Emulsing Photon

$$h (1 / (\theta / 2 \pi)) = m c^2 / \sqrt{1 - (u^2 / c^2)}$$

$$c := 2.99792458$$

$$h := 6.62606896 \cdot (10^{34})$$

$$h(1/(\theta/2\pi)) =$$

$$\begin{aligned} m c^2 / \sqrt{1 - (u^2/c^2)} = m c^2 / \sqrt{1 - \left( \left( \sqrt{3.5481432270250993 \cdot 10^{18} \eta^2 - \right.} \right. \\ \left. \left. 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2 \right) \right) / \\ \left( \sqrt{39.47841760435743 \cdot 10^{22} - 12.566370614359172 \cdot 10^{22} r^2 \theta + 12.566370614359172 \cdot 10^{22} \theta^2} \right) / c^2 \Big) = \\ m c^2 / \sqrt{1 - \left( \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + \right.} \right. \\ \left. \left. 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2 \right) \right) / \\ \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + \right.} \\ \left. \left. 3.147674514204298 \cdot 10^{24} \sin[\beta]^2 \right) \right) / c^2 \Big) \end{aligned}$$

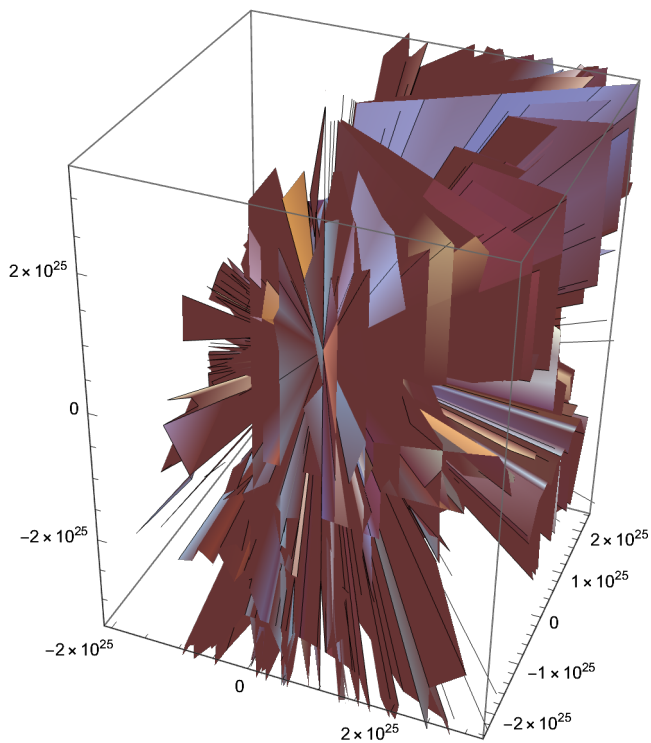
$$\begin{aligned} \text{Solve} \Big[ m c^2 / \sqrt{1 - \left( \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + \right.} \right. \\ \left. \left. 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2 \right) \right) / \\ \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + \right.} \\ \left. \left. 3.147674514204298 \cdot 10^{24} \sin[\beta]^2 \right) \right) / c^2 \Big) == h(1/(\theta/2\pi)), m \Big] \end{aligned}$$

$$\left\{ \left\{ m \rightarrow \frac{1}{\theta} 4.69348 \times 10^{33} \right. \right.$$

$$\left. \left. \sqrt{1 - \left( 0.111265 \left( -9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2 \right) \right) / \right.} \right. \\ \left. \left. \left( -1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2 \right) \right) \right\} \Big\}$$

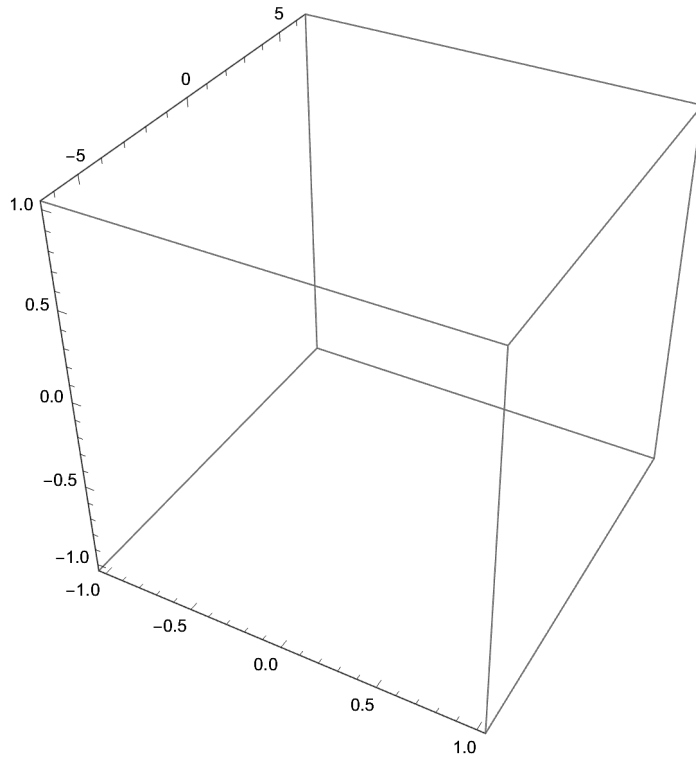


SphericalPlot3D[  
 $\frac{1}{\theta} 4.6934767251475683 \cdot 10^{33} \sqrt{\left(1 - \left(0.11126500560536184 \cdot \left(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2\right)\right) / \left(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2\right)\right)}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$

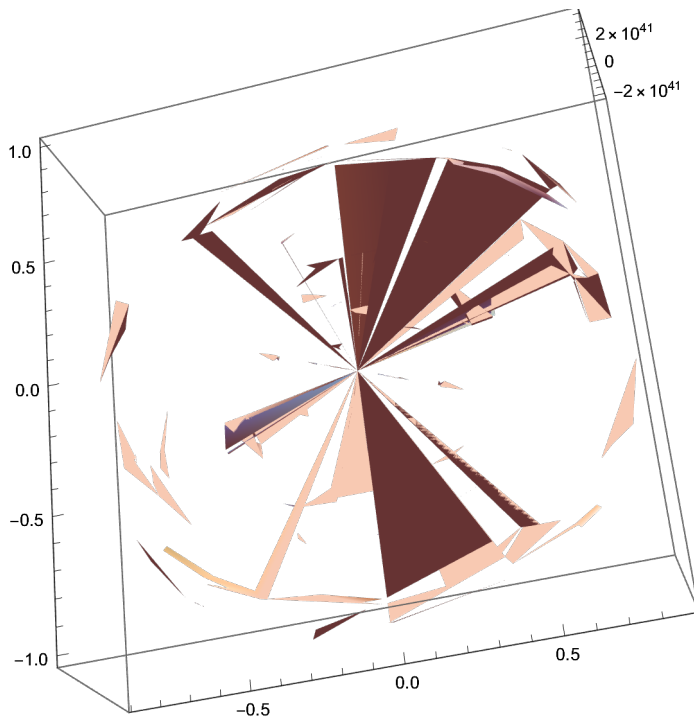


Solve[m c^2 /  $\sqrt{1 - \left(\left(\sqrt{3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2}\right) / \left(\sqrt{39.47841760435743 \cdot 10^{18} \eta^2 - 12.566370614359172 \cdot 10^{18} r^2 \theta + r^2 \theta^2}\right)\right)^2 / c^2} \right] == h(1 / (\theta / 2\pi)), m]$   
 $\left\{m \rightarrow \frac{4.69348 \times 10^{33} \sqrt{1 - \frac{0.111265 (3.54814 \times 10^{18} \eta^2 - 1.12941 \times 10^{18} r^2 \theta + 8.98755 \times 10^{16} r^2 \theta^2)}{39.4784 \eta^2 - 12.5664 r^2 \theta + r^2 \theta^2}}}{\theta}\right\}$

$\text{ContourPlot3D}\left[\frac{1}{\theta} 4.6934767251475683 \cdot \eta^{33} \sqrt{\left(1. - \left(0.11126500560536184 \cdot \left(3.5481432270250993 \cdot \eta^2 - 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2\right)\right) / \left(39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)\right)}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\eta, -1, 1\}\right]$



$\text{RevolutionPlot3D}\left[\frac{1}{\theta} 4.6934767251475683 \cdot 10^{33} \sqrt{\left(1. - \left(0.11126500560536184 \cdot \left(3.5481432270250993 \cdot 10^{18} \left(r \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right)^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2\right)\right)} \right. \\ \left. \left(39.47841760435743 \cdot \left(r \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right)\right)^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2\right)\right], \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$



## Mass of the Emulsed Tachyon

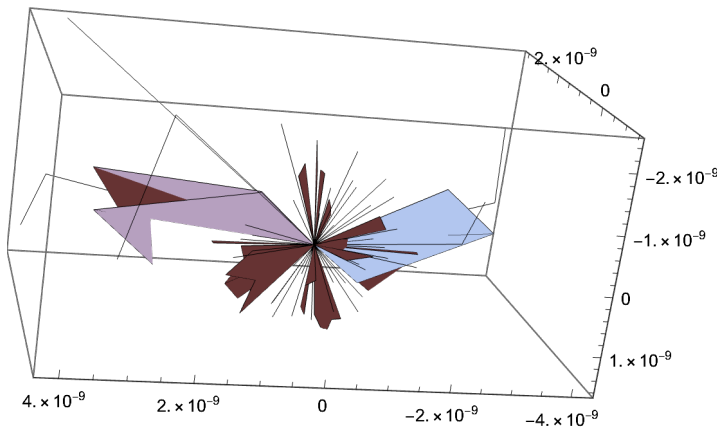
$$\text{Solve}\left[m c^2 / \sqrt{1 - \left( \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta]} \right) / \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta]} \right) \right)^2 / c^2} \right) =$$

$$\left( (i m) c^2 \right) / \sqrt{\left( \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta]} \right) / \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta]} \right) \right)^2 / c^2} - 1, m]$$

$$\left\{ \left\{ m \rightarrow -1. \sqrt{-\frac{0. + 26.944 i}{\sqrt{\frac{-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin^2[\beta]}{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin^2[\beta]}}} + \frac{8.98755}{\sqrt{1. - \frac{0.111265 (-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin^2[\beta])}{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin^2[\beta]}}} \right\} \right\}$$

SphericalPlot3D[

$$-1.\sqrt{-\frac{0. + 26.944002417373987\,i}{\sqrt{\frac{-9.004950935909588\,^{*24}\theta + 7.16591226875\,^{*23}\theta^2 + 2.8289887706190094\,^{*25}\sin[\beta]^2}{-1.0019359163599887\,^{*24}\theta + 7.9731526875\,^{*22}\theta^2 + 3.147674514204298\,^{*24}\sin[\beta]^2}}}} + \frac{8.987551787368176}{\sqrt{(1. - (0.11126500560536184(-9.004950935909588\,^{*24}\theta + 7.16591226875\,^{*23}\theta^2 + 2.8289887706190094\,^{*25}\sin[\beta]^2)) / (-1.0019359163599887\,^{*24}\theta + 7.9731526875\,^{*22}\theta^2 + 3.147674514204298\,^{*24}\sin[\beta]^2))}}), \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\}]$$



## The Special Case : mass of photon equals mass of tachyon

$$\text{Solve}\left[\frac{1}{\theta} 4.6934767251475683 \cdot 10^{33}\right.$$

$$\sqrt{\left(1. - \left(0.11126500560536184 \cdot \left(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2\right)\right) / \left(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2\right)\right)} ==$$

$$-1. / \left( - \frac{0. + 26.944002417373987 \cdot i}{\sqrt{\frac{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2}{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2}}} + \right.$$

$$8.987551787368176 /$$

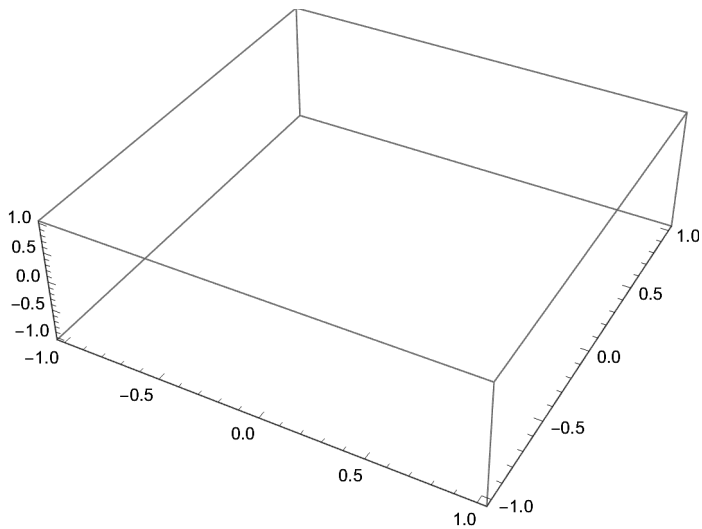
$$\left. \left( \sqrt{\left(1. - \left(0.11126500560536184 \cdot \left(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2\right)\right) / \left(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2\right)\right)} \right), \theta \right]$$

$$\begin{aligned}
& \left\{ \left\{ \theta \rightarrow -1.4061 \times 10^{34} + \right. \right. \\
& \quad \left( (1.57322 \times 10^{-16} - 2.7249 \times 10^{-16} \, \mathfrak{i}) (-3.17012 \times 10^{99} + 2.11001 \times 10^{32} \sin[\beta]^2) \right) / \\
& \quad \left( -3.56979 \times 10^{149} - 7.12809 \times 10^{82} \sin[\beta]^2 + \right. \\
& \quad \left. 6.12994 \times 10^{48} \sin[\beta] \sqrt{2.03154 \times 10^{135} + 9.01452 \times 10^{67} \sin[\beta]^2 + \sin[\beta]^4} \right)^{1/3} - \\
& \quad (9.91069 \times 10^{-17} + 1.71658 \times 10^{-16} \, \mathfrak{i}) \left( -3.56979 \times 10^{149} - 7.12809 \times 10^{82} \sin[\beta]^2 + \right. \\
& \quad \left. 6.12994 \times 10^{48} \sin[\beta] \sqrt{2.03154 \times 10^{135} + 9.01452 \times 10^{67} \sin[\beta]^2 + \sin[\beta]^4} \right)^{1/3} \Big\}, \\
& \left\{ \theta \rightarrow -1.4061 \times 10^{34} + ( (1.57322 \times 10^{-16} + 2.7249 \times 10^{-16} \, \mathfrak{i}) \right. \\
& \quad \left. (-3.17012 \times 10^{99} + 2.11001 \times 10^{32} \sin[\beta]^2) \right) / \\
& \quad \left( -3.56979 \times 10^{149} - 7.12809 \times 10^{82} \sin[\beta]^2 + 6.12994 \times 10^{48} \sin[\beta] \right. \\
& \quad \left. \sqrt{2.03154 \times 10^{135} + 9.01452 \times 10^{67} \sin[\beta]^2 + \sin[\beta]^4} \right)^{1/3} - \\
& \quad (9.91069 \times 10^{-17} - 1.71658 \times 10^{-16} \, \mathfrak{i}) \left( -3.56979 \times 10^{149} - 7.12809 \times 10^{82} \sin[\beta]^2 + \right. \\
& \quad \left. 6.12994 \times 10^{48} \sin[\beta] \sqrt{2.03154 \times 10^{135} + 9.01452 \times 10^{67} \sin[\beta]^2 + \sin[\beta]^4} \right)^{1/3} \Big\}, \\
& \left\{ \theta \rightarrow -1.4061 \times 10^{34} - (3.14645 \times 10^{-16} (-3.17012 \times 10^{99} + 2.11001 \times 10^{32} \sin[\beta]^2) \right) / \\
& \quad \left( -3.56979 \times 10^{149} - 7.12809 \times 10^{82} \sin[\beta]^2 + \right. \\
& \quad \left. 6.12994 \times 10^{48} \sin[\beta] \sqrt{2.03154 \times 10^{135} + 9.01452 \times 10^{67} \sin[\beta]^2 + \sin[\beta]^4} \right)^{1/3} + \\
& \quad 1.98214 \times 10^{-16} \left( -3.56979 \times 10^{149} - 7.12809 \times 10^{82} \sin[\beta]^2 + \right. \\
& \quad \left. 6.12994 \times 10^{48} \sin[\beta] \sqrt{2.03154 \times 10^{135} + 9.01452 \times 10^{67} \sin[\beta]^2 + \sin[\beta]^4} \right)^{1/3} \Big\}
\end{aligned}$$

```

RevolutionPlot3D[
  -1.406095504335699`*^34 + ((1.573223658846742`*^-16 - 2.7249033087919633`*^-16 I)
    (-3.170117605322233`*^99 + 2.1100085574114824`*^32 Sin[β]^2)) /
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
      6.129941368665291`*^48 Sin[β]
      √(2.031537410396714`*^135 + 9.014515872517417`*^67 Sin[β]^2 + Sin[β]^4))^(1/3) -
    (9.910688019868207`*^-17 + 1.7165815188375924`*^-16 I)
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
      6.129941368665291`*^48 Sin[β] √(2.031537410396714`*^135 +
        9.014515872517417`*^67 Sin[β]^2 + Sin[β]^4)), {β, -π/2, π/2}]

```

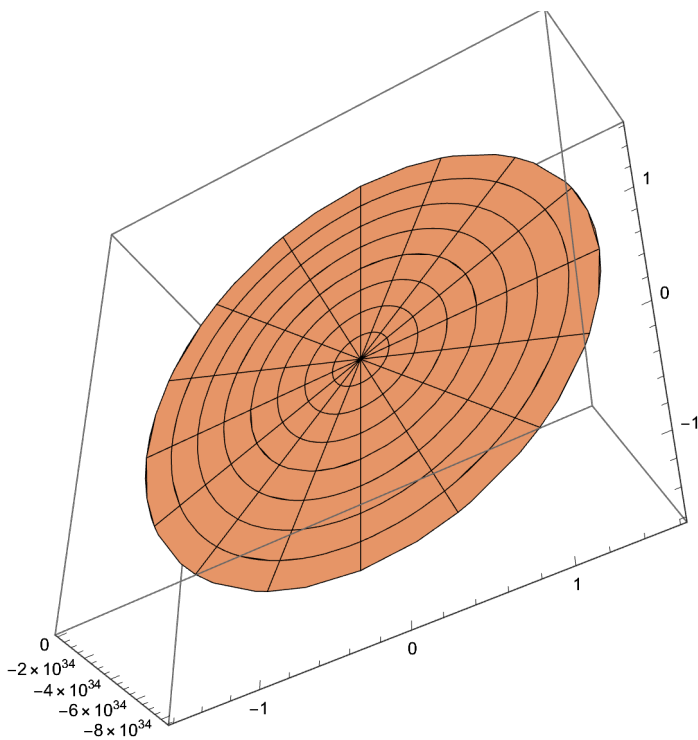




```

RevolutionPlot3D[
  -1.406095504335699`*^34 + ((1.573223658846742`*^-16 + 2.7249033087919633`*^-16 i)
    (-3.170117605322233`*^99 + 2.1100085574114824`*^32 Sin[β]^2)) /
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
      6.129941368665291`*^48 Sin[β]
      √(2.031537410396714`*^135 + 9.014515872517417`*^67 Sin[β]^2 + Sin[β]^4))^(1/3) -
    (9.910688019868207`*^-17 - 1.7165815188375924`*^-16 i)
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
      6.129941368665291`*^48 Sin[β] √(2.031537410396714`*^135 +
        9.014515872517417`*^67 Sin[β]^2 + Sin[β]^4))^(1/3), {β, -π/2, π/2}]

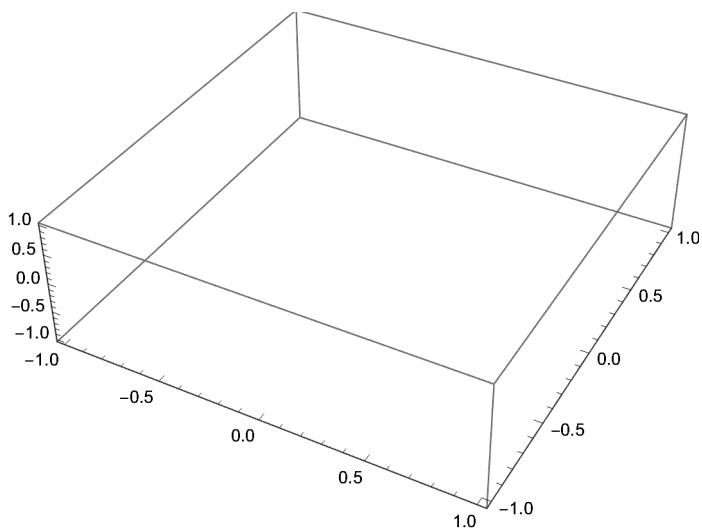
```



```

RevolutionPlot3D[
  -1.406095504335699`*^34 - (3.146447317693484`*^-16
    (-3.170117605322233`*^99 + 2.1100085574114824`*^32 Sin[ $\beta$ ]2)) /
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[ $\beta$ ]2 +
      6.129941368665291`*^48 Sin[ $\beta$ ]
       $\sqrt{(2.031537410396714`*^135 + 9.014515872517417`*^67 \sin[\beta]^2 + \sin[\beta]^4)}^{1/3} +$ 
      1.9821376039736414`*^-16 (-3.569793189746561`*^149 - 7.128089663842775`*^82
      Sin[ $\beta$ ]2 + 6.129941368665291`*^48 Sin[ $\beta$ ]
       $\sqrt{(2.031537410396714`*^135 +$ 
      9.014515872517417`*^67 Sin[ $\beta$ ]2 + Sin[ $\beta$ ]4))1/3, { $\beta$ , - $\pi$ ,  $\pi$ }]

```

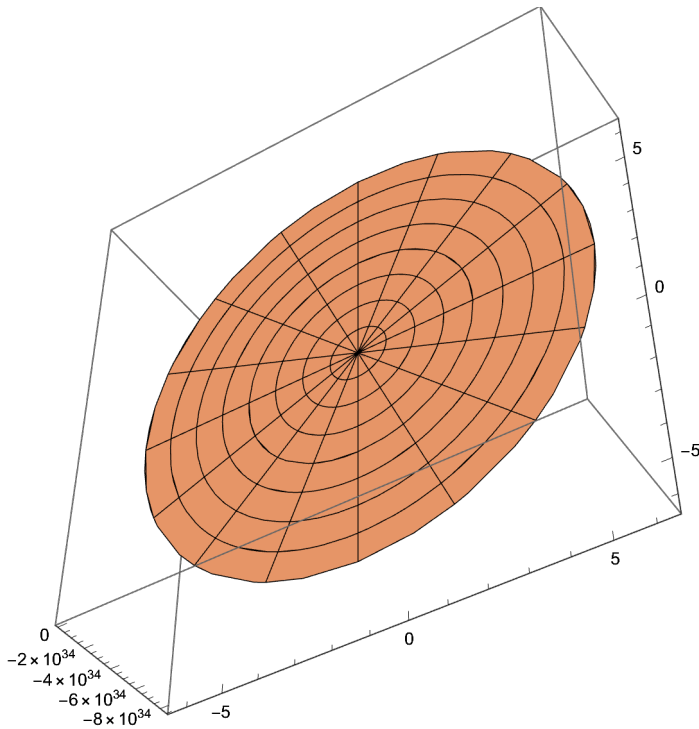


## Examples of Substitutions for the Visible Plane Case

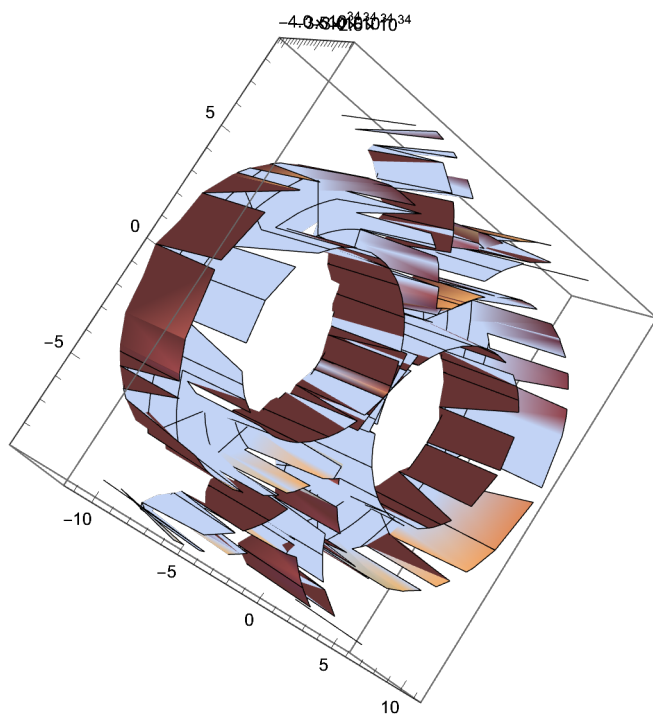
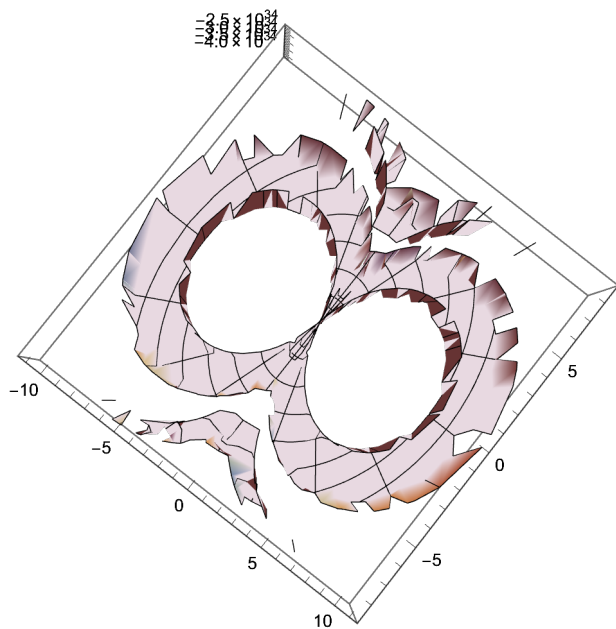
```

RevolutionPlot3D[
  -1.406095504335699`*^34 + ((1.573223658846742`*^-16 + 2.7249033087919633`*^-16 i)
    (-3.170117605322233`*^99 + 2.1100085574114824`*^32 Sin[β]^2)) /
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
      6.129941368665291`*^48 Sin[β]
      √(2.031537410396714`*^135 + 9.014515872517417`*^67 Sin[β]^2 + Sin[β]^4))^(1/3) -
    (9.910688019868207`*^-17 - 1.7165815188375924`*^-16 i)
    (-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
      6.129941368665291`*^48 Sin[β] √(2.031537410396714`*^135 +
        9.014515872517417`*^67 Sin[β]^2 + Sin[β]^4))^(1/3), {β, -2 π, 2 π}]

```



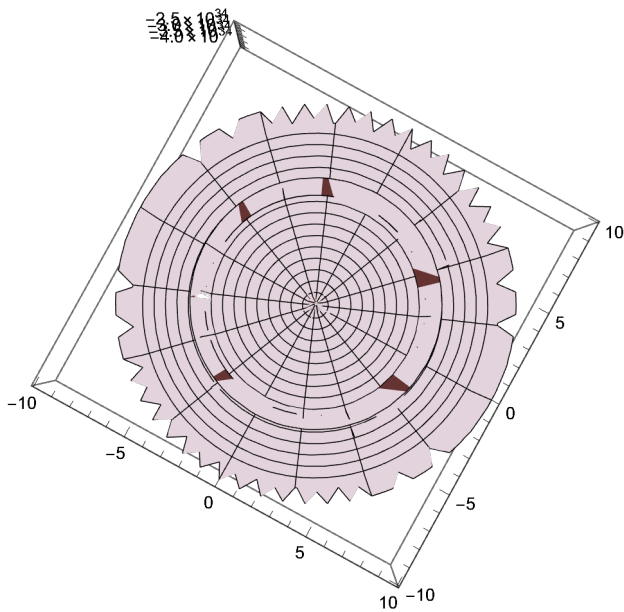
$$\begin{aligned}
& \text{RevolutionPlot3D}\left[-1.406095504335699 \cdot 10^{-34} + \right. \\
& \left. \left( (1.573223658846742 \cdot 10^{-16} + 2.7249033087919633 \cdot 10^{-16} i) \left( -3.170117605322233 \cdot 10^{99} + \right. \right. \right. \\
& \quad \left. \left. 2.1100085574114824 \cdot 10^{32} \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi\sqrt{-4\pi + \theta}}\right]\right]^2 \right) \right) / \right. \\
& \left. \left( -3.569793189746561 \cdot 10^{149} - 7.128089663842775 \cdot 10^{82} \sin[\beta]^2 + \right. \right. \\
& \quad \left. 6.129941368665291 \cdot 10^{48} \sin[\beta] \sqrt{\left( 2.031537410396714 \cdot 10^{135} + \right. \right. \\
& \quad \left. \left. 9.014515872517417 \cdot 10^{67} \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}\right]\right]^2 + \sin[\beta]^4 \right) \right)^{1/3} - \right. \\
& \left. (9.910688019868207 \cdot 10^{-17} - 1.7165815188375924 \cdot 10^{-16} i) \right. \\
& \left. \left( -3.569793189746561 \cdot 10^{149} - 7.128089663842775 \cdot 10^{82} \sin[\beta]^2 + \right. \right. \\
& \quad \left. 6.129941368665291 \cdot 10^{48} \sin\left[\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \left(2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^3}}{2\pi\sqrt{-4\pi + \theta}}\right]\right] \sqrt{\left( 2.031537410396714 \cdot 10^{135} + \right. \right. \right. \\
& \quad \left. \left. 9.014515872517417 \cdot 10^{67} \sin[\beta]^2 + \sin[\beta]^4 \right) \right)^{1/3} \right. \\
& \quad \left. , \{\theta, -4\pi, 4\pi\}, \{\beta, -\pi, \pi\} \right]
\end{aligned}$$

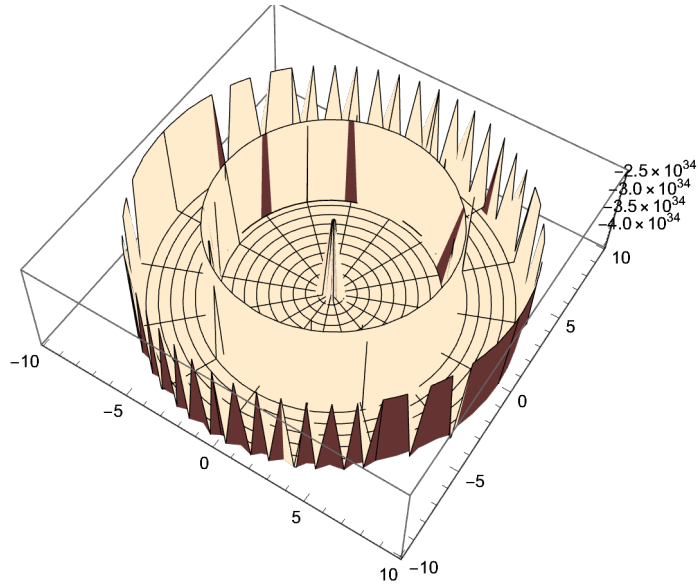


```

RevolutionPlot3D[-1.406095504335699`*^34 +
  ⎛(1.573223658846742`*^-16 + 2.7249033087919633`*^-16 ⓓ) ⎛-3.170117605322233`*^99 +
    2.1100085574114824`*^32 Sin[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ]]^2⎞⎞/
  ⎛-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
    6.129941368665291`*^48 Sin[β] √⎛2.031537410396714`*^135 +
      9.014515872517417`*^67 Sin[ArcSin[ $\frac{\sqrt{(4\pi - \theta)\theta}}{2\pi}$ ]]^2 + Sin[β]^4⎞⎞⎞^1/3 -
  (9.910688019868207`*^-17 - 1.7165815188375924`*^-16 ⓓ)
  ⎛-3.569793189746561`*^149 - 7.128089663842775`*^82 Sin[β]^2 +
    6.129941368665291`*^48 Sin[ArcSin[ $\frac{\sqrt{-4\pi^2\theta + 4\pi\theta^2 - \theta^3}}{2\pi\sqrt{-4\pi + \theta}}$ ]]
    √⎛2.031537410396714`*^135 + 9.014515872517417`*^67 Sin[β]^2 +
      Sin[β]^4⎞⎞⎞^1/3, {θ, -4π, 4π}, {β, -π, π}

```





Solve $\left[\frac{1}{\theta} 4.6934767251475683 \cdot 10^{33}$

$$\sqrt{\left(1. - \left(0.11126500560536184 \cdot \left(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta]\right)\right) / \left(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta]\right)\right)} ==$$

$$-1. / \left(-\left(\left(0. + 26.944002417373987 \cdot i\right) / \left(\sqrt{\left(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta]\right)} / \left(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta]\right)\right)\right) + 8.987551787368176 / \left(\sqrt{\left(1. - \left(0.11126500560536184 \cdot \left(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta]\right)\right) / \left(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta]\right)\right)}\right)\right), \beta]$$

{{}}

```

h v = h (1 / (theta / 2 pi)) = (i m) c^2 / sqrt(u^2 / c^2) - 1 =
(i (-1. / (- (0. + 26.944002417373987 i) / (sqrt((-9.004950935909588`^24 theta +
7.16591226875`^23 theta^2 + 2.8289887706190094`^25 Sin[beta]^2) /
(-1.0019359163599887`^24 theta + 7.9731526875`^22 theta^2 +
3.147674514204298`^24 Sin[beta]^2)))) + 8.987551787368176` /
(sqrt(1. - (0.11126500560536184` (-9.004950935909588`^24 theta +
7.16591226875`^23 theta^2 + 2.8289887706190094`^25 Sin[beta]^2) /
(-1.0019359163599887`^24 theta + 7.9731526875`^22 theta^2 +
3.147674514204298`^24 Sin[beta]^2)))))) c^2) /
sqrt(((sqrt((-9.004950935909588`^24 theta + 7.16591226875`^23 theta^2 +
2.8289887706190094`^25 Sin[beta]^2) / (sqrt((-1.0019359163599887`^24 theta +
7.9731526875`^22 theta^2 + 3.147674514204298`^24 Sin[beta]^2))))^2 / c^2) - 1

Solve[(i (-1. / (- (0. + 26.944002417373987 i) /
(sqrt((-9.004950935909588`^24 theta + 7.16591226875`^23 theta^2 +
2.8289887706190094`^25 Sin[beta]^2) / (-1.0019359163599887`^24 theta +
7.9731526875`^22 theta^2 + 3.147674514204298`^24 Sin[beta]^2)))) +
8.987551787368176` / (sqrt(1. - (0.11126500560536184`
(-9.004950935909588`^24 theta + 7.16591226875`^23 theta^2 +
2.8289887706190094`^25 Sin[beta]^2) / (-1.0019359163599887`^24
theta + 7.9731526875`^22 theta^2 + 3.147674514204298`^24 Sin[beta]^2))))))
c^2) / sqrt(((sqrt((-9.004950935909588`^24 theta + 7.16591226875`^23 theta^2 +
2.8289887706190094`^25 Sin[beta]^2) /
(sqrt((-1.0019359163599887`^24 theta + 7.9731526875`^22 theta^2 +
3.147674514204298`^24 Sin[beta]^2))))^2 / c^2) - 1 == h (1 / (theta / 2 pi)), beta]

{{{}}

```

```
h := 6.62606896 * (10^34)
```

$$\lambda = \eta = \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

## $\eta'$ for a Tachyon

For a Tachyon :

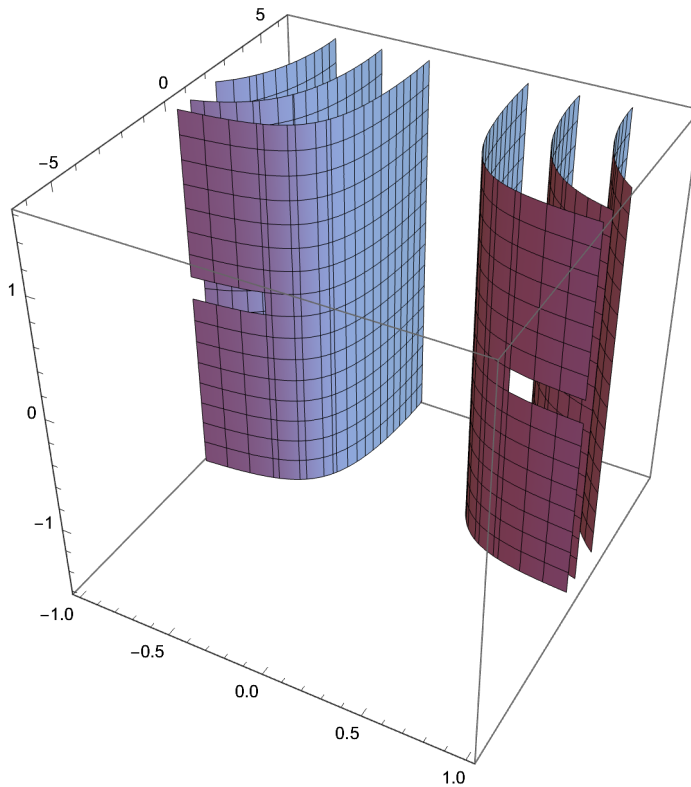


$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{(u^2/c^2) - 1} = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{(v^2/c^2) - 1} =$$

$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left(\left(\sqrt{(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta])}\right) / \left(\sqrt{(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta])}\right)\right)^2 / c^2 - 1} =$$

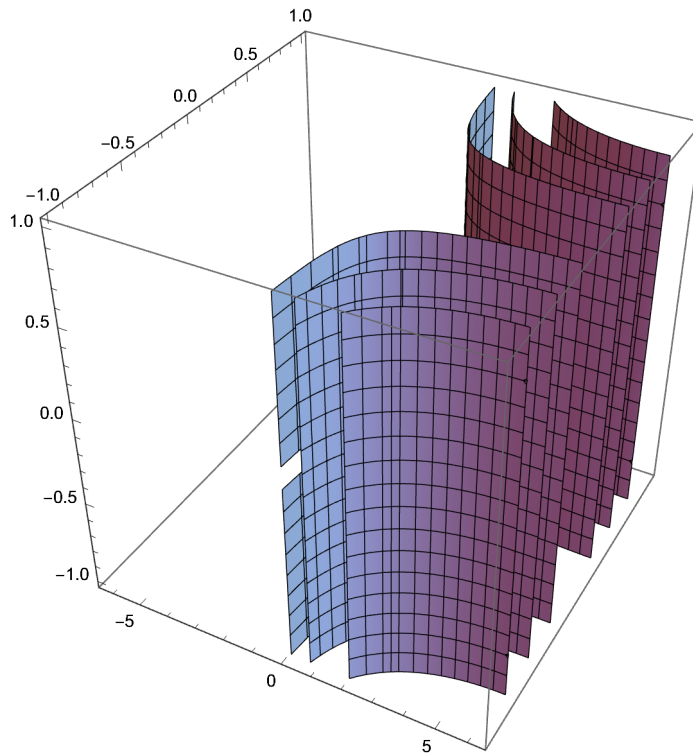
$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left(\left(\left(\sqrt{(2.8289887706190094 \cdot 10^{25} \eta^2 - 9.004950935909588 \cdot 10^{24} r^2 \theta + 7.16591226875 \cdot 10^{23} r^2 \theta^2)}\right) / \left(\sqrt{(3.147674514204298 \cdot 10^{24} \eta^2 - 1.0019359163599887 \cdot 10^{24} r^2 \theta + 7.9731526875 \cdot 10^{22} r^2 \theta^2)}\right)\right)\right)^2 / c^2 - 1}$$

ContourPlot3D[  
 $\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left(\left(\sqrt{(-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin^2[\beta])}\right) / \left(\sqrt{(-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin^2[\beta])}\right)\right)^2 / c^2 - 1}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$



ContourPlot3D[  

$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left(\left(\left(\sqrt{2.8289887706190094 \eta^{25} - 9.004950935909588 \eta^{24} r^2 \theta + 7.16591226875 r^{23} \theta^2}\right) / \left(\sqrt{3.147674514204298 \eta^{24} - 1.0019359163599887 r^{24} \theta + 7.9731526875 r^{22} \theta^2}\right)\right)\right)^{2/c^2} - 1, \{\theta, -2\pi, 2\pi\}, \{r, -1, 1\}, \{\eta, -1, 1\}]$$



## $\eta'$ for a Regular Particle

$$\text{For a regular particle : } \eta' = \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{1 - u^2 / c^2} =$$

$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left(1 - \left(\left(\left(\sqrt{-9.004950935909588 \cdot \theta^{24} + 7.16591226875 \cdot \theta^{23} + 2.8289887706190094 \cdot \text{Sin}[\beta]^2\right) / \right.\right.\right.}$$

$$\left.\left.\left(\sqrt{-1.0019359163599887 \cdot \theta^{24} + 7.9731526875 \cdot \theta^{22} + 3.147674514204298 \cdot \text{Sin}[\beta]^2}\right)\right)^2 / c^2\right) =$$

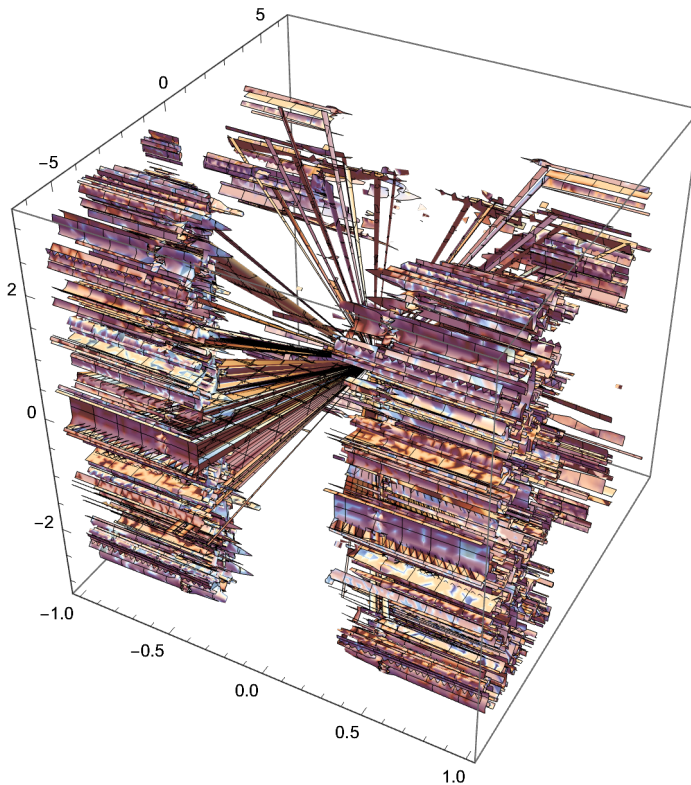
$$\frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left(1 - \left(\sqrt{3.5481432270250993 \cdot \eta^2 - 1.1294090667581471 \cdot r^2 \theta + 8.987551787368176 \cdot r^2 \theta^2}\right) / \right.$$

$$\left.\left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right)\right)^2 / c^2}$$

```
ContourPlot3D[

$$\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} \sqrt{1 - \left( \left( \left( \sqrt{-9.004950935909588 \cdot \theta^{24} + 7.16591226875 \cdot \theta^{23} + 2.8289887706190094 \cdot \sin^2[\beta]} \right) \right) / \left( \sqrt{-1.0019359163599887 \cdot \theta^{24} + 7.9731526875 \cdot \theta^{22} + 3.147674514204298 \cdot \sin^2[\beta]} \right) \right) \right)^{2/c^2}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}]$$

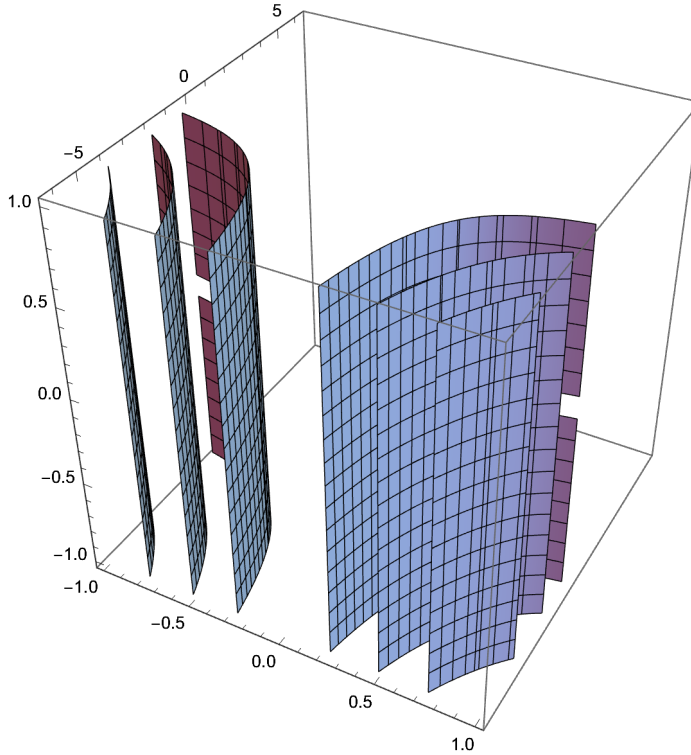
```



Right now, mathematics does a better job of describing the visual world than a photo. We are looking for a way of expressing what we see in terms of actual texture and depth, so why not use mathematics? Paint peeling of a wall has a certain visual texture that does not come across very well in a photograph or video. For some reason, mathematics can describe an entire object of perception.

```
ContourPlot3D[
  
$$\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \sqrt{\left(1 - \left(\sqrt{(3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2)}\right)\right) / \left(\sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2}\right)}^2 / c^2}, \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\eta, -1, 1\}]$$

```



This is extremely useful in processing the information emulsd by a photon onto a tachyon, because it has the same form as the relativistic height of the cone for regular particle traveling. These forms may be interchanged, allowing information of the same kind to pass through one form of the equation, while being expressed only in that form when the tachyon has the information transformed into it.

## Frequency of a Tachyon

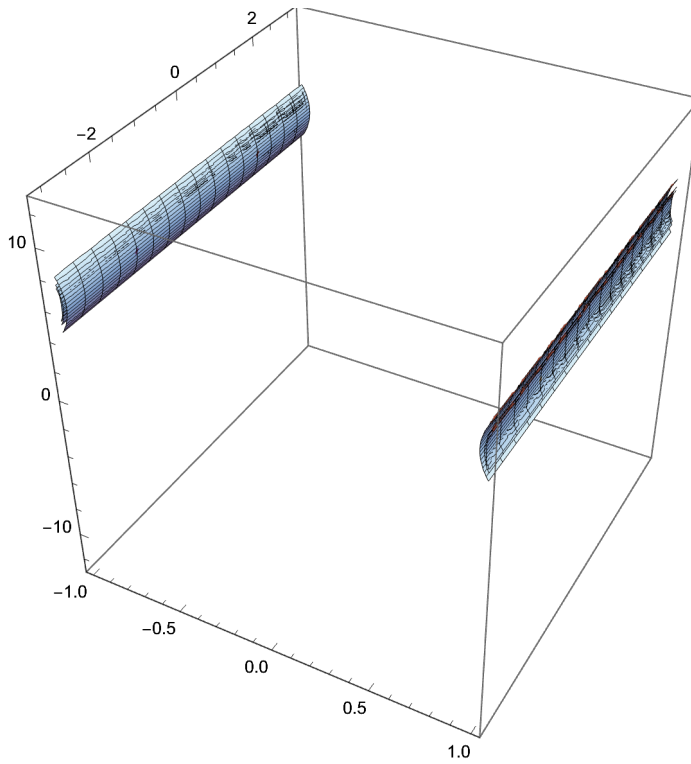
f = frequency

$$\eta' f = \left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left( \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2} \right) / \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2} \right) \right)^2 / c^2} - 1 \right) f = v = \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2} \right) / \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2} \right) = \left( \sqrt{3.5481432270250993 \cdot 10^{18} \eta^2 - 1.1294090667581471 \cdot 10^{18} r^2 \theta + 8.987551787368176 \cdot 10^{16} r^2 \theta^2} \right) / \left( \sqrt{39.47841760435743 \cdot \eta^2 - 12.566370614359172 \cdot r^2 \theta + r^2 \theta^2} \right)$$

$$\text{Solve} \left[ \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2} \right) / \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2} \right) == \left( \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} \sqrt{\left( \left( \sqrt{-9.004950935909588 \cdot 10^{24} \theta + 7.16591226875 \cdot 10^{23} \theta^2 + 2.8289887706190094 \cdot 10^{25} \sin[\beta]^2} \right) / \left( \sqrt{-1.0019359163599887 \cdot 10^{24} \theta + 7.9731526875 \cdot 10^{22} \theta^2 + 3.147674514204298 \cdot 10^{24} \sin[\beta]^2} \right) \right)^2 / c^2} - 1 \right) f, f \right]$$

$$\left\{ \left\{ f \rightarrow \left( 1. \sqrt{-9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2} \right) / \left( \sqrt{-1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2} \right) \right. \right. \\ \left. \left( -1. + 0.159155 \sqrt{12.5664 r^2 \theta - 1. r^2 \theta^2} \right) \sqrt{\left( \left( -9.00495 \times 10^{24} \theta + 7.16591 \times 10^{23} \theta^2 + 2.82899 \times 10^{25} \sin[\beta]^2 \right) / \left( c^2 \left( -1.00194 \times 10^{24} \theta + 7.97315 \times 10^{22} \theta^2 + 3.14767 \times 10^{24} \sin[\beta]^2 \right) \right) \right)} \right\} \right\}$$

```
ContourPlot3D[
  (1.`√(-9.004950935909588`*^24 θ + 7.16591226875`*^23 θ² + 2.8289887706190094`*^25
    Sin[β]²)) / (√(-1.0019359163599887`*^24 θ +
    7.9731526875`*^22 θ² + 3.147674514204298`*^24 Sin[β]²)
  (-1.` + 0.15915494309189535`√12.566370614359172`r² θ - 1.`r² θ²
    √((-9.004950935909588`*^24 θ + 7.16591226875`*^23 θ² +
    2.8289887706190094`*^25 Sin[β]²) / (c²(-1.0019359163599887`*^24 θ +
    7.9731526875`*^22 θ² + 3.147674514204298`*^24 Sin[β]²))))),
  {r, -1, 1}, {β, -π, π}, {θ, -4π, 4π}]
```

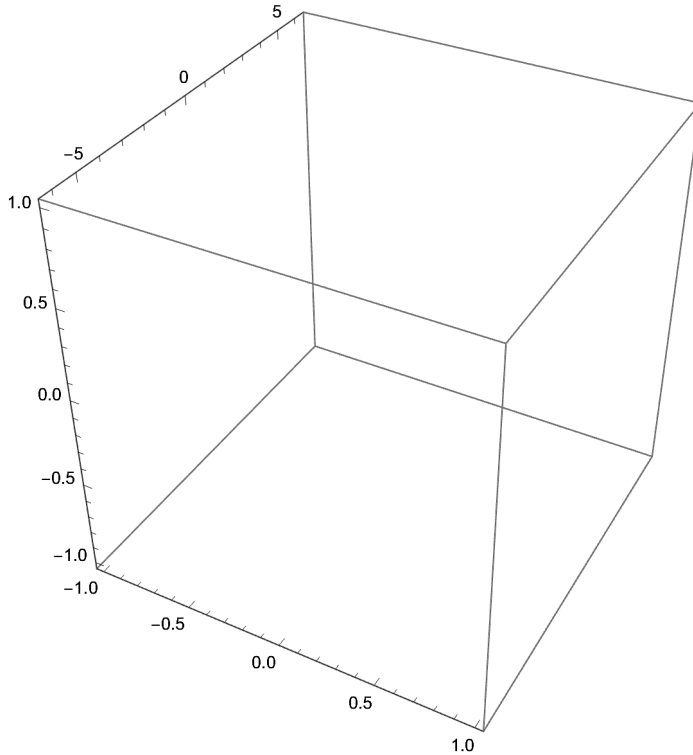


$$\eta' f = v = \left( \sqrt{2.8289887706190094 \cdot \eta^2 - 9.004950935909588 \cdot r^2 \theta + 7.16591226875 \cdot r^2 \theta^2} \right) / \left( \sqrt{3.147674514204298 \cdot \eta^2 - 1.0019359163599887 \cdot r^2 \theta + 7.9731526875 \cdot r^2 \theta^2} \right)$$

$$\begin{aligned}
& \text{Solve}\left[\eta \sqrt{\left(\left(\left(\sqrt{2.8289887706190094 \cdot \eta^2 - 9.004950935909588 \cdot r^2 \theta + 7.16591226875 \cdot r^2 \theta^2}\right)\right) / \right. \\
& \quad \left. \left(\sqrt{3.147674514204298 \cdot \eta^2 - 1.0019359163599887 \cdot r^2 \theta + 7.9731526875 \cdot r^2 \theta^2}\right)^2 / (c^2) - 1\right) f == \\
& \quad \left(\sqrt{2.8289887706190094 \cdot \eta^2 - 9.004950935909588 \cdot r^2 \theta + 7.16591226875 \cdot r^2 \theta^2}\right) / \\
& \quad \left(\sqrt{3.147674514204298 \cdot \eta^2 - 1.0019359163599887 \cdot r^2 \theta + 7.9731526875 \cdot r^2 \theta^2}\right), f] \\
& \left\{\left\{f \rightarrow \left(1. \sqrt{2.82899 \times 10^{25} \eta^2 - 9.00495 \times 10^{24} r^2 \theta + 7.16591 \times 10^{23} r^2 \theta^2}\right) / \right. \right. \\
& \quad \left. \left(\eta \sqrt{3.14767 \times 10^{24} \eta^2 - 1.00194 \times 10^{24} r^2 \theta + 7.97315 \times 10^{22} r^2 \theta^2}\right) \right. \\
& \quad \left. \sqrt{\left(-1. + \left(0.111265 \sqrt{2.82899 \times 10^{25} \eta^2 - 9.00495 \times 10^{24} r^2 \theta + 7.16591 \times 10^{23} r^2 \theta^2}\right) / \right. \right. \\
& \quad \left. \left. \left(3.14767 \times 10^{24} \eta^2 - 1.00194 \times 10^{24} r^2 \theta + 7.97315 \times 10^{22} r^2 \theta^2\right)\right)\right)\right\}
\end{aligned}$$



```
ContourPlot3D[(1.√(2.8289887706190094`^25 η^2 -
9.004950935909588`^24 r^2 θ + 7.16591226875`^23 r^2 θ^2)) /
(η√(3.147674514204298`^24 η^2 - 1.0019359163599887`^24 r^2 θ +
7.9731526875`^22 r^2 θ^2)
√(-1. + (0.11126500560536184`√(2.8289887706190094`^25 η^2 -
9.004950935909588`^24 r^2 θ + 7.16591226875`^23 r^2 θ^2)) /
(3.147674514204298`^24 η^2 - 1.0019359163599887`^24 r^2 θ +
7.9731526875`^22 r^2 θ^2))), {r, -1, 1}, {θ, -2 π, 2 π}, {η, -1, 1}]
```



There are many other forms that could be used in such a process to emult photon information into tachyon information accessible in Mathematics for Describing a Circle into a Cone.

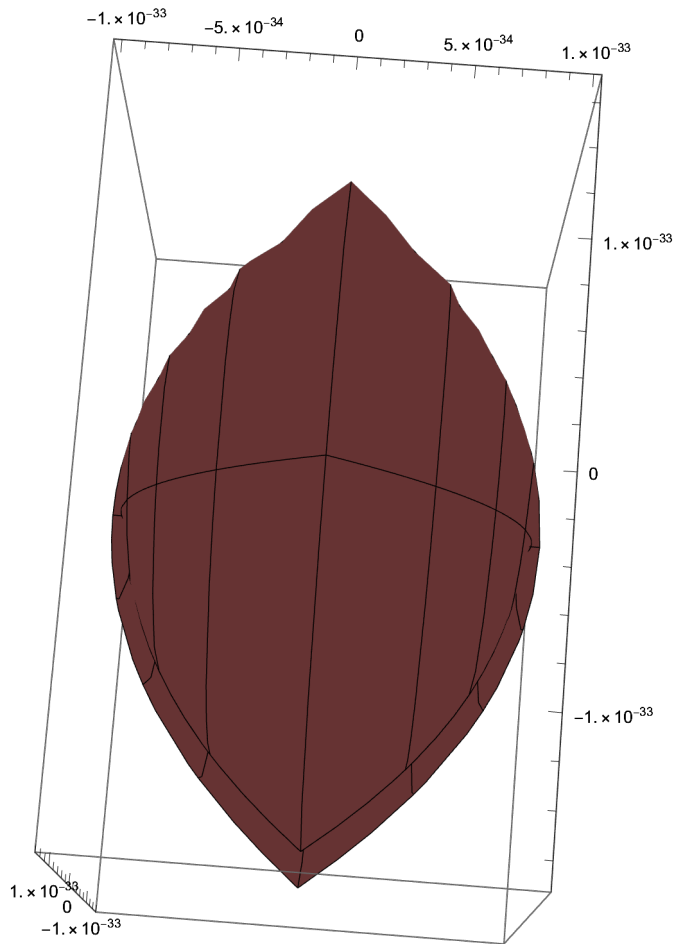
In Jesus' name, Amen.

**h** := 6.62606896 \* 10<sup>-34</sup>)

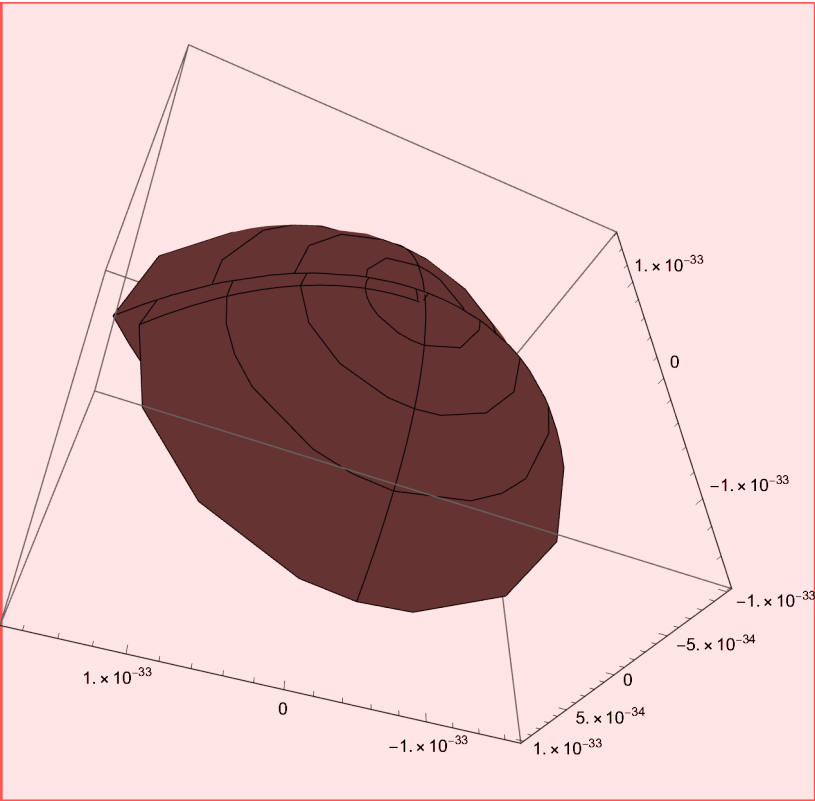
**c** := 2.99792458 \* (10<sup>8</sup>)

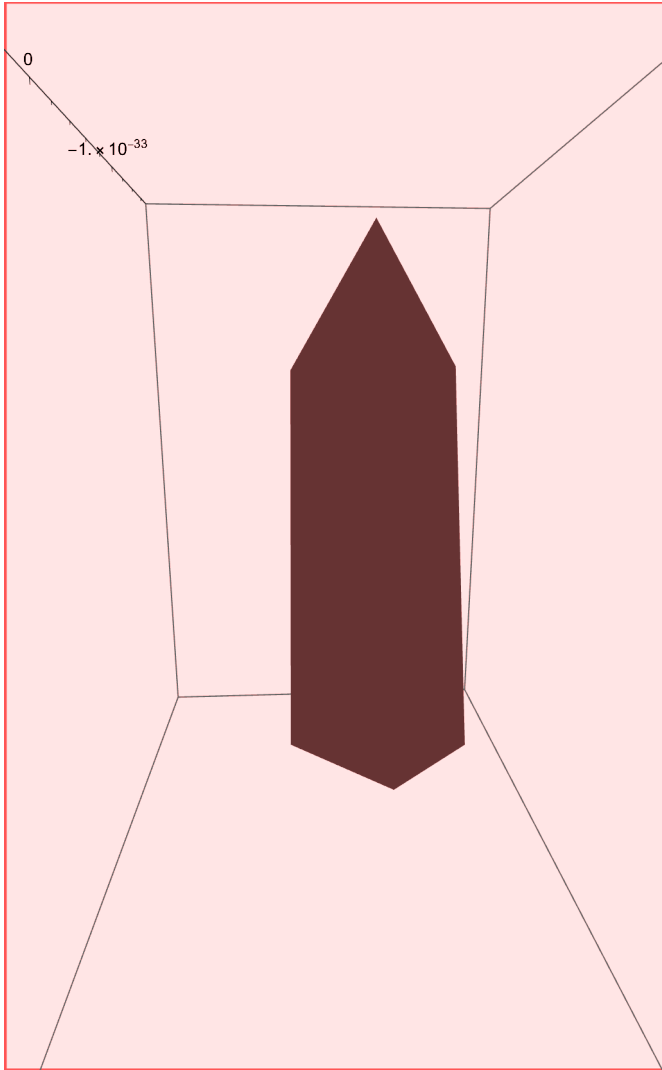
$$(\text{Energy of Photon with Wavelength } \eta) = \frac{h \left( c^2 + \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2} \text{ Joules} \quad (244)$$

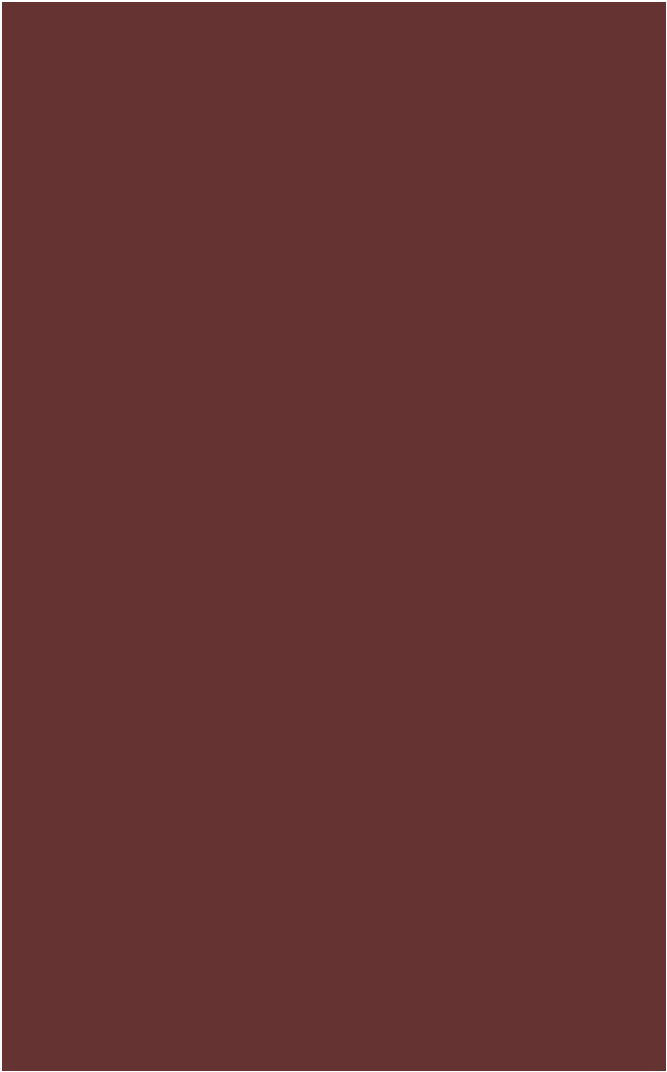
$$\text{SphericalPlot3D}\left[\frac{h\left(c^2 + \left(\frac{c\sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\sqrt{4\pi - \theta}}\right)^2\right)}{2\left(\frac{c\sqrt{2\left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}}{\sqrt{4\pi - \theta}}\right)^2}, \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\}\right]$$

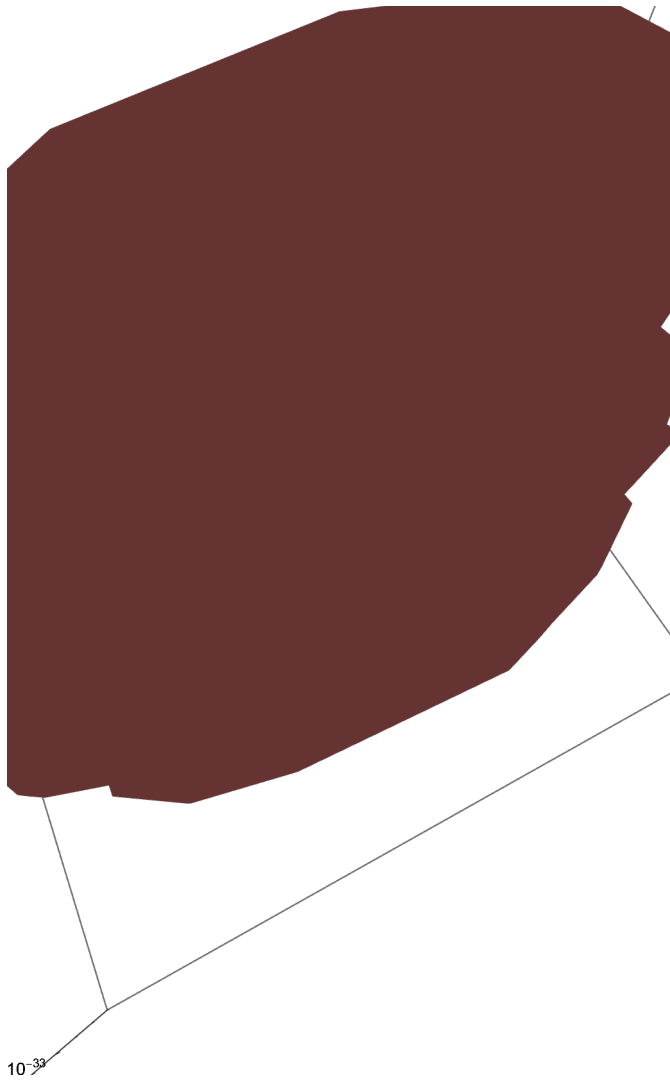


From the following position, it is easier to make the box "tesseract."

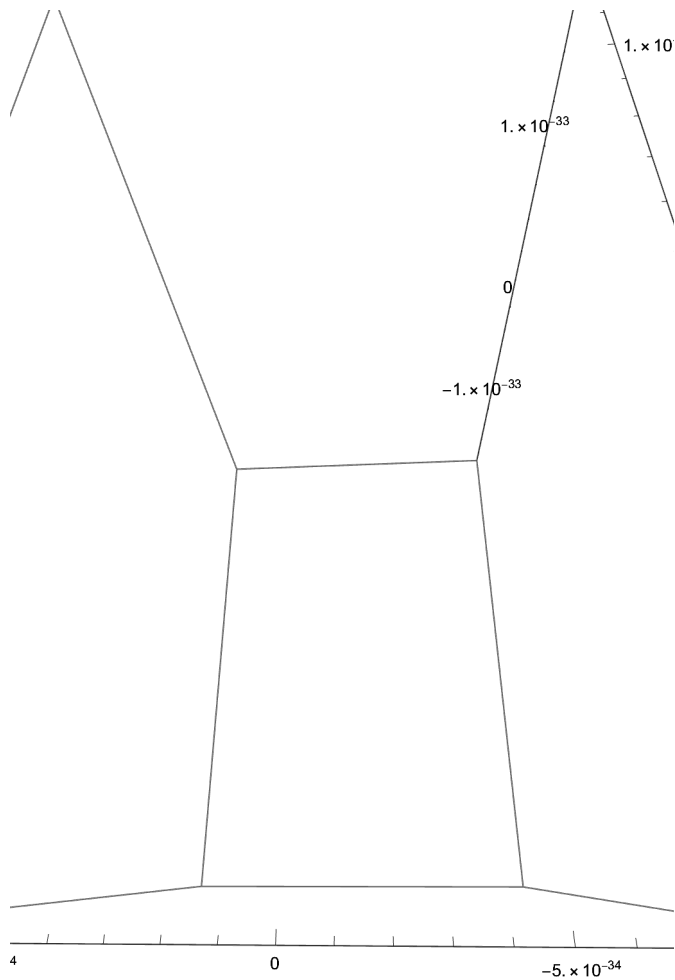








10-33



$$\frac{\pi}{3}$$

$$\text{Solve}\left[1 == \frac{\sqrt{4 \pi r^2 \frac{\pi}{3} - r^2 \left(\frac{\pi}{3}\right)^2}}{2 \pi}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{6}{\sqrt{11}}\right\}, \left\{r \rightarrow \frac{6}{\sqrt{11}}\right\}\right\}$$

$$\text{Solve}\left[r \sin[\beta] == \frac{\sqrt{4 \pi r^2 \frac{\pi}{3} - r^2 \left(\frac{\pi}{3}\right)^2}}{2 \pi}, r\right]$$

$$\{\{r \rightarrow 0\}\}$$

$$\text{Solve}\left[\frac{\pi}{3} == \frac{2\pi \left( \left( \frac{6}{\sqrt{11}} \right)^2 + \sqrt{\left( \frac{6}{\sqrt{11}} \right)^4 - \left( \frac{6}{\sqrt{11}} \right)^2 \eta^2} \right)}{\left( \frac{6}{\sqrt{11}} \right)^2}, \eta\right]$$

{}

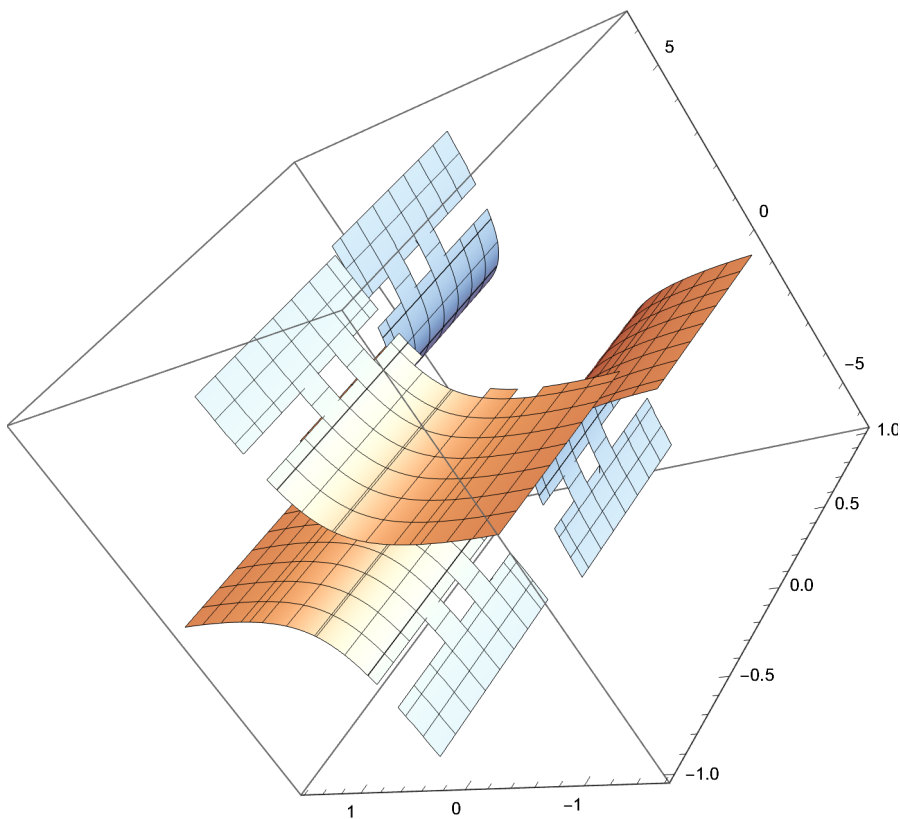
$$1 - \frac{1}{2} \frac{\pi}{\pi}$$

$$\frac{5}{6}$$

$$\text{Solve}\left[(2\pi r - 2\pi r_1 - \theta r) \sin[\beta] == \frac{\sqrt{4\pi r^2 \frac{\pi}{3} - r^2 \left(\frac{\pi}{3}\right)^2}}{2\pi}, \theta\right]$$

$$\left\{ \left\{ \theta \rightarrow -\frac{\csc[\beta] \left( \sqrt{11} \sqrt{r^2} - 12\pi r \sin[\beta] + 12\pi \sin[\beta] r_1 \right)}{6r} \right\} \right\}$$

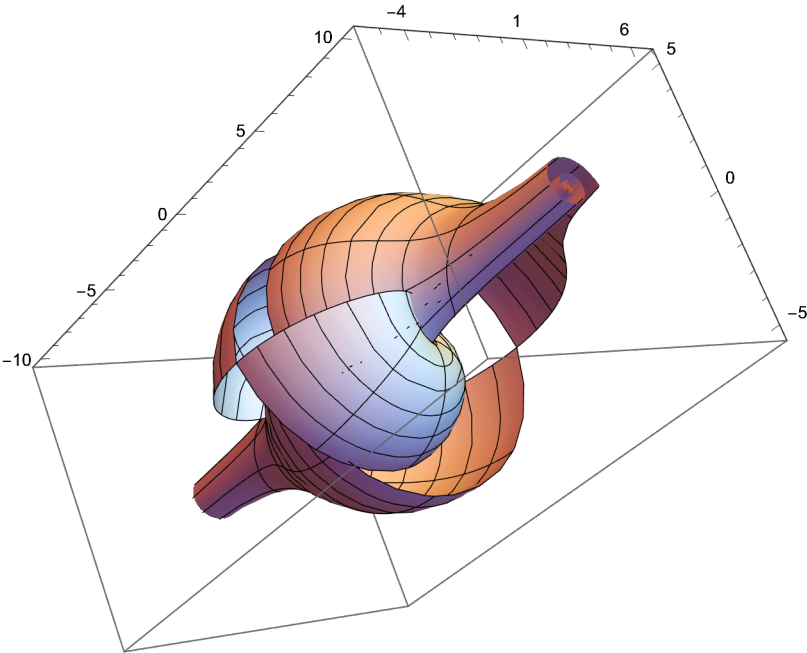
$$\text{ContourPlot3D}\left[\frac{\csc[\beta] \left( \sqrt{11} \sqrt{r^2} - 12\pi r \sin[\beta] + 12\pi \sin[\beta] \left( \frac{2\pi r - r\theta}{2\pi} \right) \right)}{6r}, \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$$



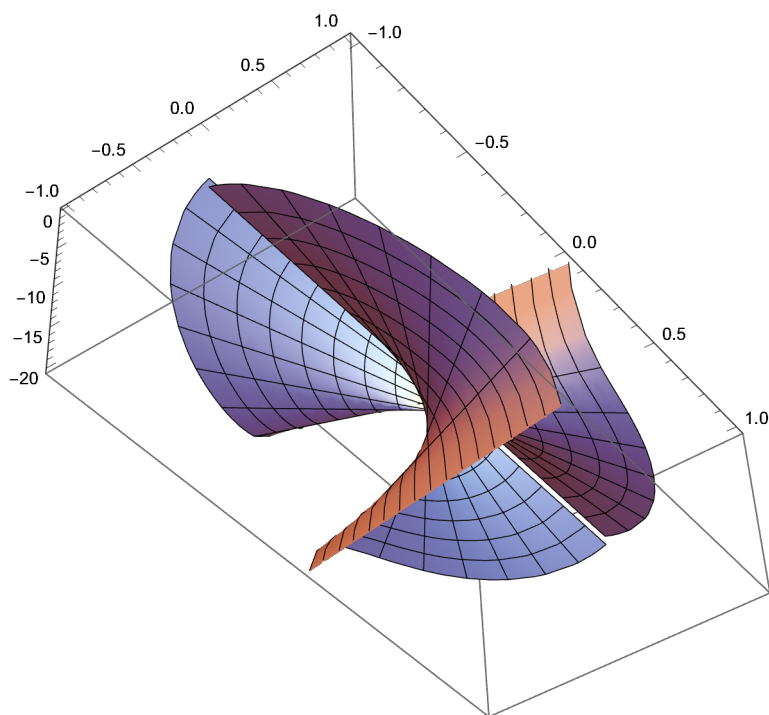


$$\frac{6}{\sqrt{11}}$$

$$\text{SphericalPlot3D}\left[\frac{\text{Csc}[\beta] \left( \sqrt{11} \sqrt{\left(\frac{6}{\sqrt{11}}\right)^2} - 12 \pi \frac{6}{\sqrt{11}} \text{Sin}[\beta] + 12 \pi \text{Sin}[\beta] \left( \frac{2 \pi \frac{6}{\sqrt{11}} - \frac{6}{\sqrt{11}} \theta}{2 \pi} \right) \right)}{6 \frac{6}{\sqrt{11}}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\} \right]$$



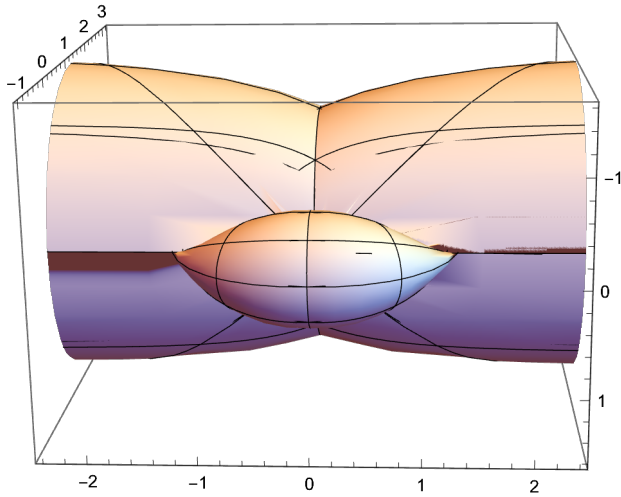
$$\text{RevolutionPlot3D}\left[\frac{1}{6 \frac{6}{\sqrt{11}}} \csc[\beta] \left( \sqrt{11} \sqrt{\left(\frac{6}{\sqrt{11}}\right)^2} - 12 \pi \frac{6}{\sqrt{11}} \sin[\beta] + \right. \right. \\ \left. \left. 12 \pi \sin[\beta] \left( \frac{2 \pi \frac{6}{\sqrt{11}} - \frac{6}{\sqrt{11}} \frac{2 \pi (r^2 + \sqrt{r^4 - r^2} (r \sin[\beta])^2)}{r^2}}{2 \pi} \right) \right) \right], \{r, -1, 1\}, \{\beta, -\pi/2, \pi/2\}]$$



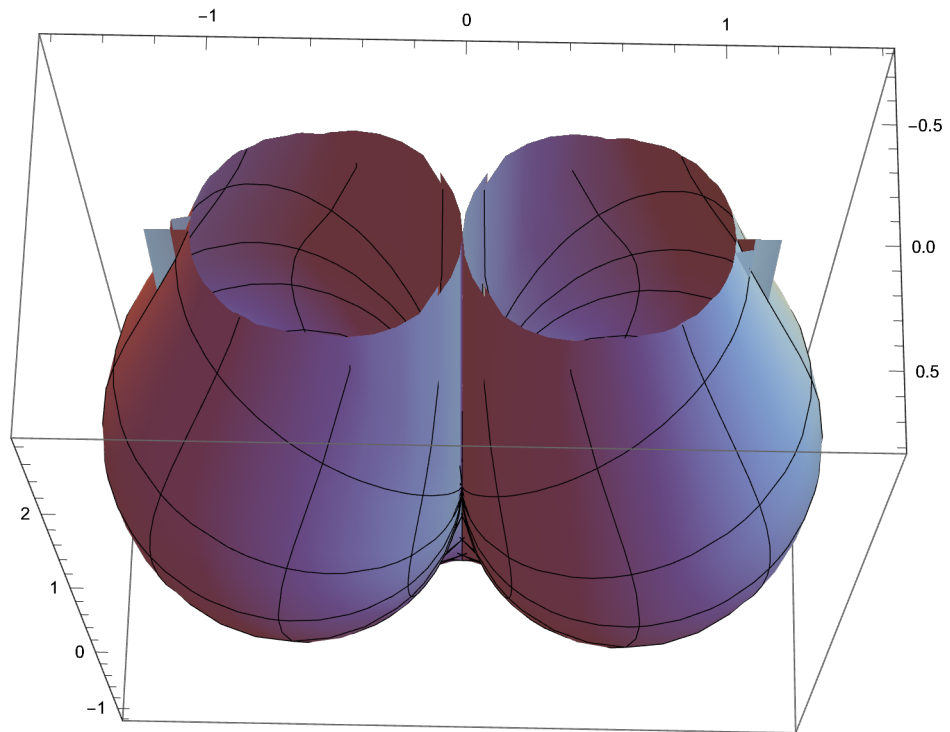
$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{4 \pi^2 \sin[\beta]}{(4 \pi - \theta) \theta}\right\}, \left\{r \rightarrow \frac{4 \pi^2 \sin[\beta]}{(4 \pi - \theta) \theta}\right\}\right\}$$

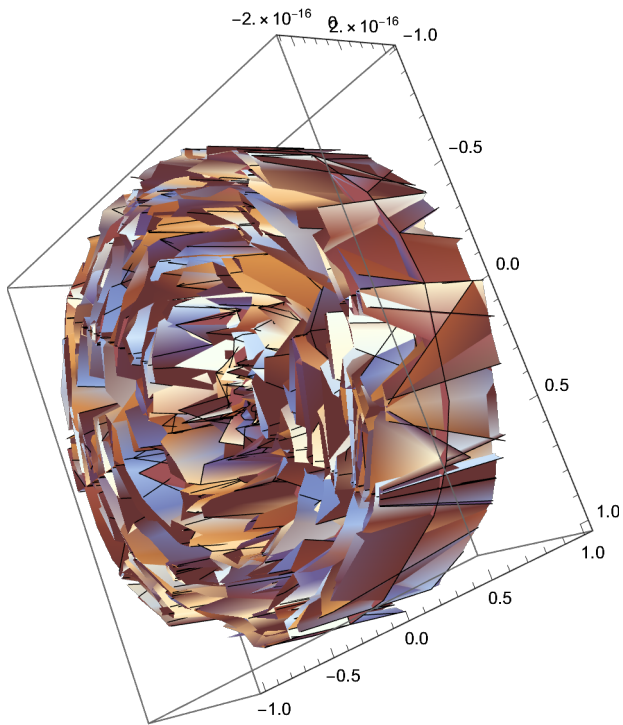
$\text{SphericalPlot3D}\left[\frac{4 \pi^2 \sin[\beta]}{(4 \pi - \theta) \theta}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$



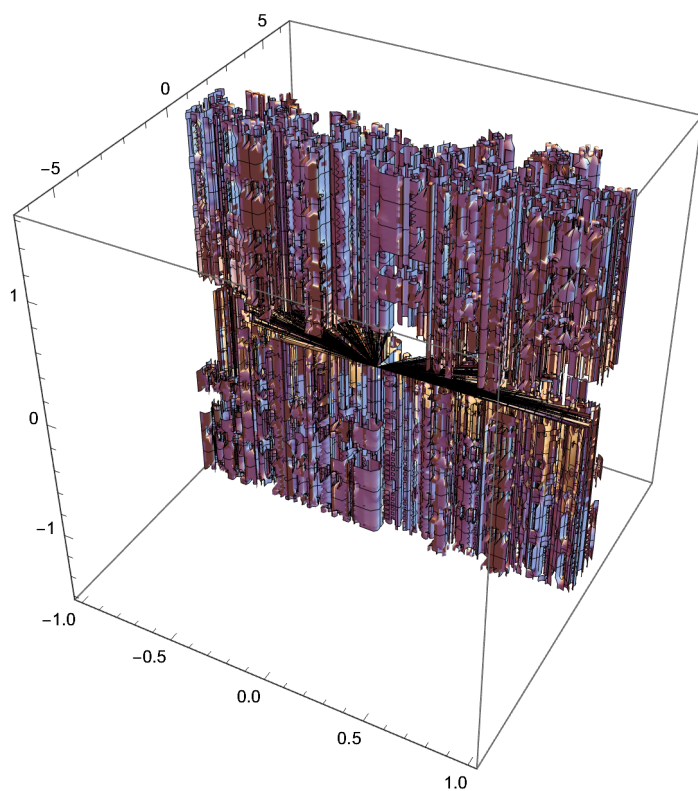
$\text{SphericalPlot3D}\left[\frac{\sqrt{4 \pi \left(\frac{4 \pi^2 \sin[\beta]}{(4 \pi - \theta) \theta}\right)^2 \theta - \left(\frac{4 \pi^2 \sin[\beta]}{(4 \pi - \theta) \theta}\right)^2 \theta^2}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$



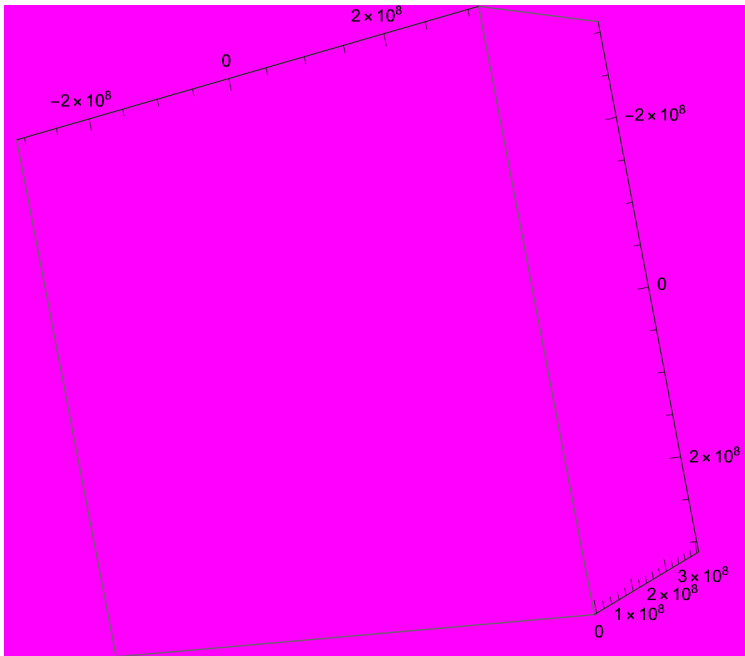
`RevolutionPlot3D` $\left[2\pi r - 2\pi \frac{2\pi r - r\theta}{2\pi} - \theta r, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}\right]$



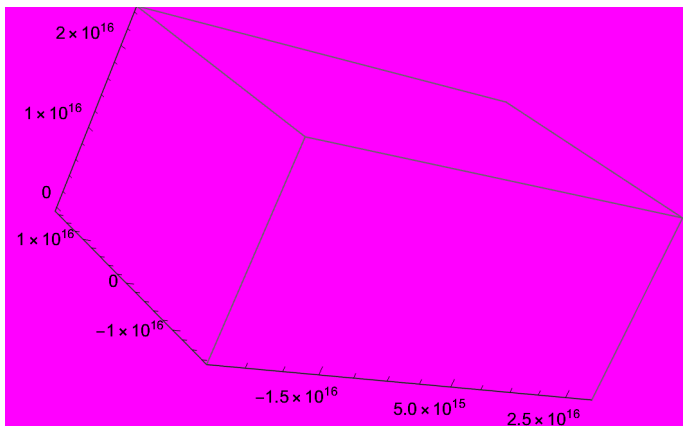
$\text{ContourPlot3D}\left[\frac{\left(2\pi r - 2\pi \frac{2\pi r - r\theta}{2\pi} - \theta r\right)}{\frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}}, \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



```
SphericalPlot3D[
  (
    (
      (
        -1.1294090667581471`*^18  $\frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} + 8.987551787368176`*^16$ 
 $\left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2 + 3.5481432270250993`*^18 \sin[\beta]^2$ 
      ) /
      (
        (
          (
            -12.566370614359172`  $\frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} + \left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2 +$ 
 $39.47841760435743` \sin[\beta]^2$ 
          )
        )
      )
    )
  ],
  { $\beta$ , - $\pi/2$ ,  $\pi/2$ }, { $\theta$ , - $2\pi$ ,  $2\pi$ }, PlotStyle -> Opacity[.75]
]
```



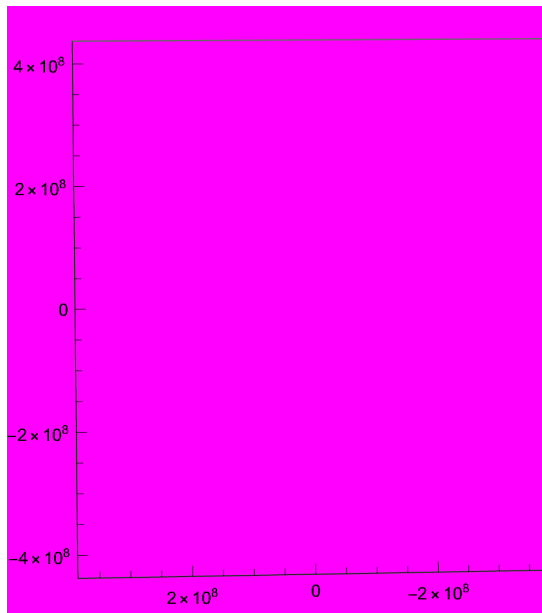
```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18  $\frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} + 8.987551787368176`*^16$ 
      (
         $\left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2 + 3.5481432270250993`*^18 \sin[\beta]^2$ 
      )
    ) /
    (
      Sqrt[
        (-12.566370614359172`  $\frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} + \left( \frac{2 \pi (r^2 + \sqrt{r^4 - r^2 \eta^2})}{r^2} \right)^2 +$ 
        39.47841760435743`  $\sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]^2\right]$ 
      )
    )
  ],
  {β, -π/2, π/2}, {θ, -2π, 2π}, PlotStyle -> Opacity[.75]
```



```

SphericalPlot3D[ $\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} + 8.987551787368176 \cdot 10^{16} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin\left[\arcsin\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2\right)}{\left(\sqrt{\left(-12.566370614359172 \cdot \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} + \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2 + 39.47841760435743 \cdot \sin\left[\arcsin\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2\right)}\right)},$ 
 $\{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}, \text{PlotStyle} \rightarrow \text{Opacity} [.75]$ 

```

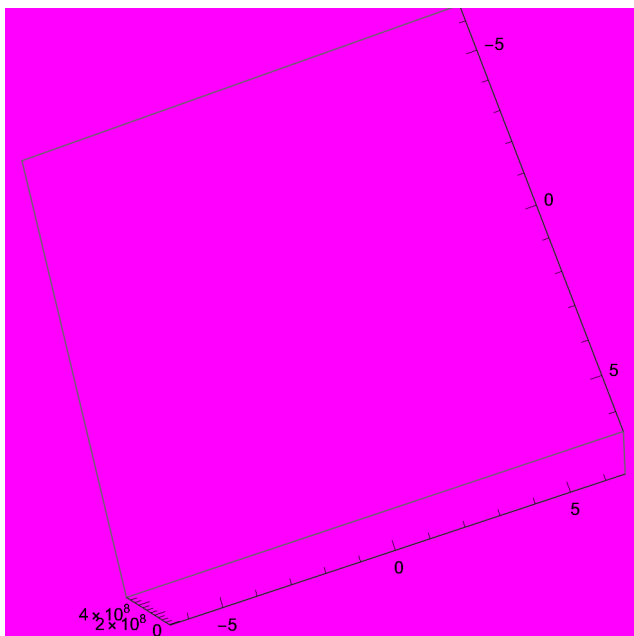




```

RevolutionPlot3D[ $\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2} + 8.987551787368176 \cdot 10^{16} \left(\frac{2 \pi \left(r^2 + \sqrt{r^4 - r^2 \eta^2}\right)}{r^2}\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin\left[\arcsin\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2\right)}{39.47841760435743 \sin\left[\arcsin\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]^2}\right),$ 
{ $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }, PlotStyle  $\rightarrow$  Opacity[.75]]

```

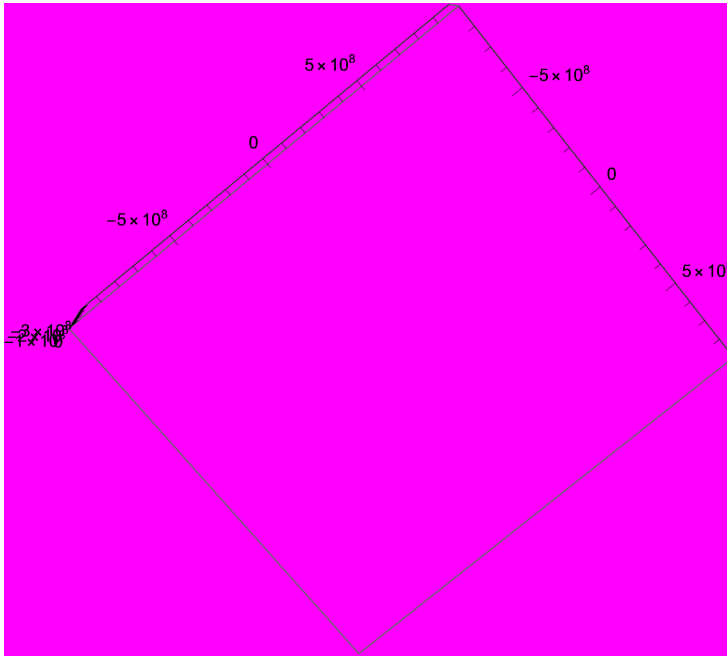


$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$$r := \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta)}$$

$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\text{SphericalPlot3D}\left[-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{-18}-1.1294090667581471\cdot 10^{-18}\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)+8.987551787368176\cdot 10^{-16}\right.\right.\right.\right. \\
\left.\left.\left.\left.\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin\left[\text{ArcSin}\left[\frac{4\pi\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta-\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\theta^2}{4\pi^2}\right]\right)^2\right)\right)\right)^2\right)\right)\right)/ \\
\left(\sqrt{39.47841760435743-12.566370614359172\theta+\theta^2}\right),\{\beta, \\
-\pi/2, \\
\pi/2\}, \\
\{\theta,-2\pi,2\pi\},\text{PlotStyle}\rightarrow\text{Opacity}[.75]\right]$$



$$\text{ArcSin}\left[\frac{\sqrt{-4\pi^2\theta+4\pi\theta^2-\theta^3}}{2\pi\sqrt{-4\pi+\theta}}\right]$$

$$\text{ArcSin}\left[\frac{4\pi r\theta-r\theta^2}{4\pi^2}\right]=\text{ArcSin}\left[\frac{\sqrt{(4\pi-\theta)\theta}}{2\pi}\right]$$

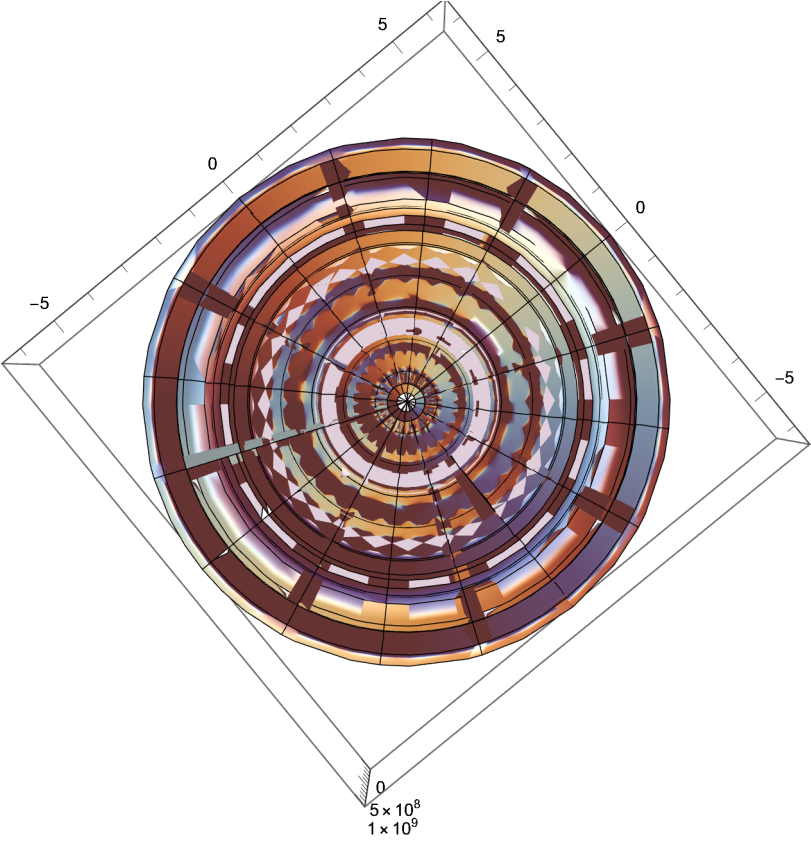
$$\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}$$

$$\begin{aligned}
 & \text{SphericalPlot3D}\left[-\left(1.\sqrt{\left(3.5481432270250993\cdot 10^{-18}-\right.}\right.\right. \\
 & \quad \left.1.1294090667581471\cdot 10^{-18}\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)+8.987551787368176\cdot 10^{-16}\right. \\
 & \quad \left.\left.\left(\left(2\left(\pi+\sqrt{\pi^2-\pi^2\sin\left[\text{ArcSin}\left[\frac{4\pi\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}\theta-\frac{2\pi\sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)}\theta^2}}{4\pi^2}\right]\right)^2\right)\right)\right)^2\right)\right)\right)/ \\
 & \quad \left(\sqrt{39.47841760435743-12.566370614359172\theta+\theta^2}\right),\{\beta, \\
 & \quad -\pi/2, \\
 & \quad \pi/2\}, \\
 & \quad \{\theta,-2\pi,2\pi\},\text{PlotStyle}\rightarrow\text{Opacity}[.75]\left] \right. \\
 & \left(\sqrt{\left(3.5481432270250993\cdot 10^{-18}-\right.}\right. \\
 & \quad \left.1.1294090667581471\cdot 10^{-18}r^2\theta+8.987551787368176\cdot 10^{-16}r^2\theta^2\right)\bigg/ \\
 & \quad \left(\sqrt{39.47841760435743-12.566370614359172r^2\theta+r^2\theta^2}\right)
 \end{aligned}$$

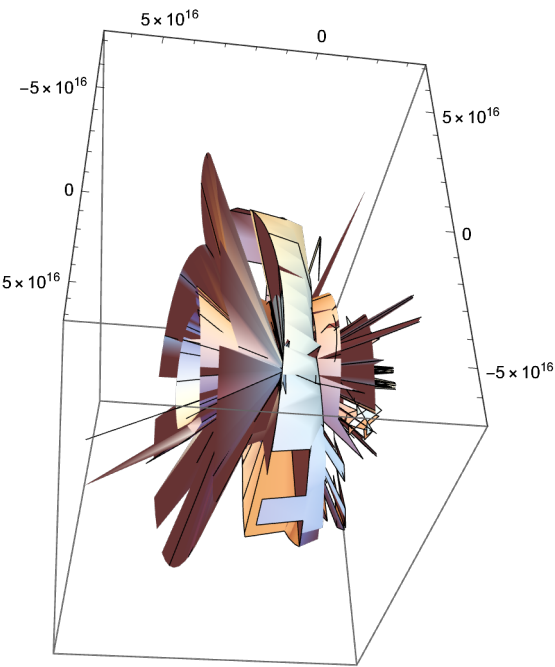
RevolutionPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} \left( \frac{\sqrt{4\pi \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2}}{2\pi} \right)^2 - 1.1294090667581471 \cdot 10^{18} \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta + 8.987551787368176 \cdot 10^{16} \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2 \right)} \right) /$$

$$\left( \sqrt{\left( 39.47841760435743 \cdot \left( \frac{\sqrt{4\pi \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \theta^2 - \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2}}{2\pi} \right)^2 - 12.566370614359172 \cdot \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta + \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2 \right)} \right), \{\theta, -2\pi, 2\pi\}$$

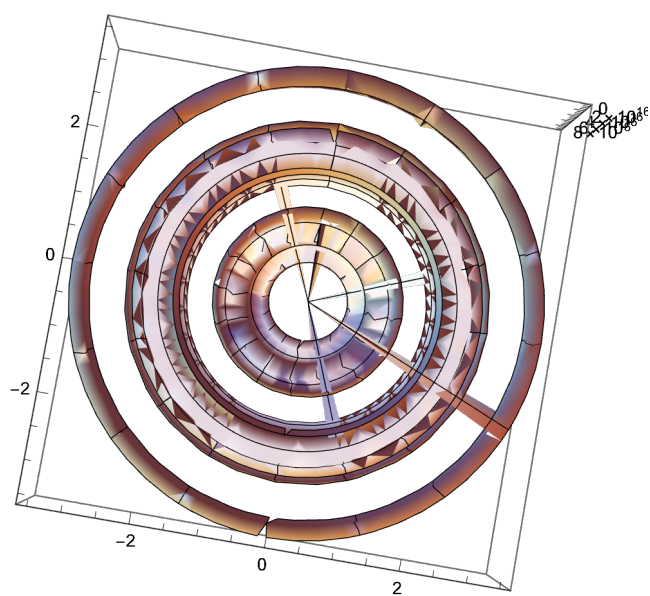


$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} \left( \frac{1}{2\pi} \left( \sqrt{4\pi \left( \frac{1}{(4\pi - \theta)\theta} 2\pi \sqrt{4\pi - \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \sqrt{6(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} + \frac{2}{3}(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} \right) \theta \right)^2 - 1.1294090667581471 \cdot 10^{18} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + 8.987551787368176 \cdot 10^{16} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right) \right) \sqrt{\left( 39.47841760435743 \cdot \frac{\sqrt{4\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}^2}{(4\pi - \theta)\theta} \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}}{2\pi} \right)^2 - 12.566370614359172 \cdot \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\} \right]$$

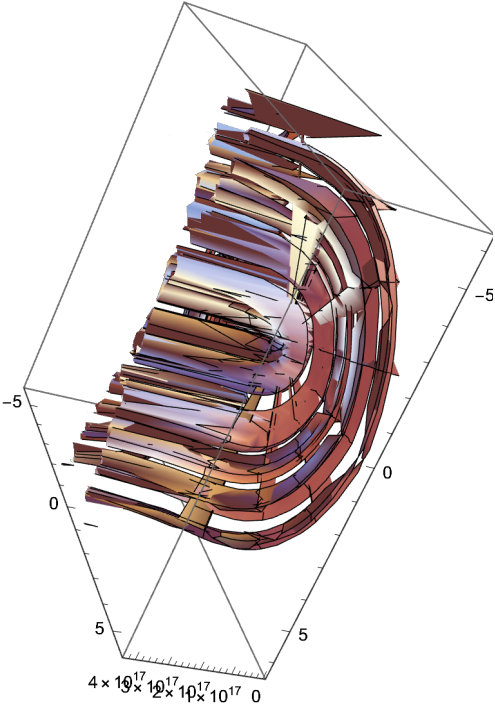








$$\text{RevolutionPlot3D}\left[\left(\sqrt{\frac{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\theta}}{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\theta\right)}\right)^2\theta-\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}\right)^2-\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta+\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}\right)\right]/\left(\sqrt{\left(39.47841760435743\sqrt{\frac{\sqrt{4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\theta}}{\left(4\pi-2\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\theta\right)}\right)^2\theta-\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}\right)^2-12.566370614359172\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta+\left(\frac{2\pi\sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta}\right)^2\theta^2}\right)},\{\theta,-2\pi,2\pi\},\{\beta,-\pi,\pi\}]$$



```
RevolutionPlot3D[| | | 3.5481432270250993`*^18
```

$$\left( \frac{\sqrt{4\pi \left( \frac{2\pi \sqrt{(4\pi-2)(\pi+\sqrt{\pi^2-\pi^2 \sin[\beta]^2})} \theta}{(4\pi-2)(\pi+\sqrt{\pi^2-\pi^2 \sin[\beta]^2})} \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi-\theta)\theta}}{(4\pi-\theta)\theta} \right)^2 \theta^2}}{2\pi} \right)^2 -$$

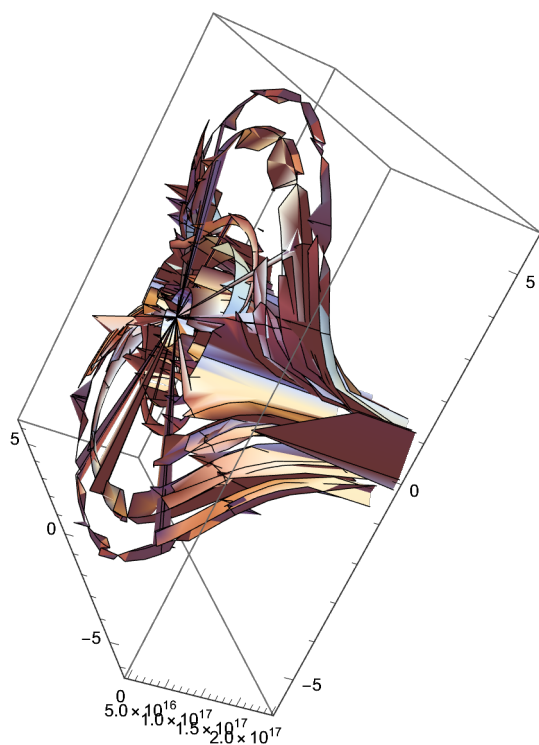
$$1.1294090667581471 \cdot 10^{18} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta +$$

$$8.987551787368176 \cdot 10^{16} \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2 \Bigg) /$$

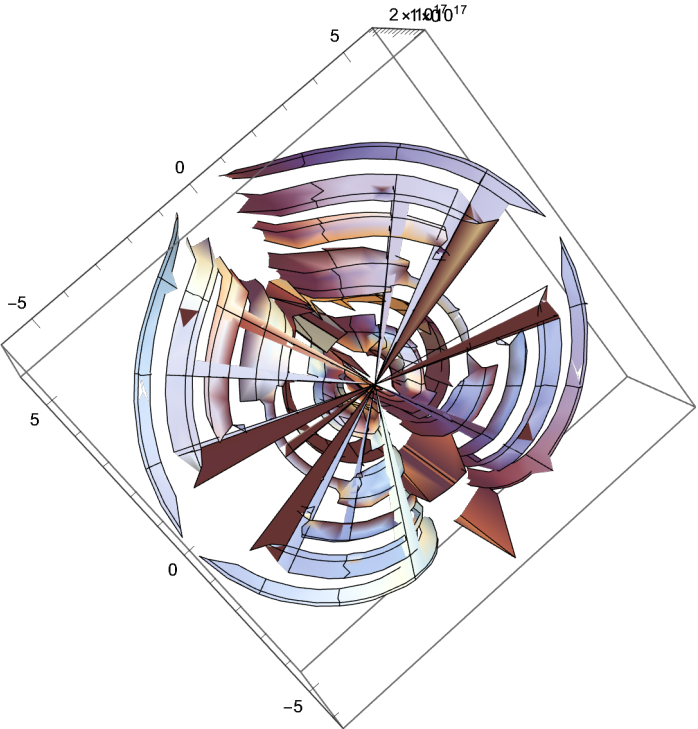
$$\left( \sqrt{39.47841760435743} \cdot \left( \frac{\sqrt{4\pi \frac{2\pi \sqrt{(4\pi-\theta)}\theta^2}{(4\pi-\theta)\theta}} - \left( \frac{2\pi \sqrt{(4\pi-\theta)}\theta}{(4\pi-\theta)\theta} \right)^2 \theta^2}{2\pi} \right)^2 - \right.$$

$$12.566370614359172 \cdot \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta +$$

$$\left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \theta^2 \right) \Bigg], \{ \theta, -2 \pi, 2 \pi \}, \{ \beta, -\pi, \pi \} \Big]$$



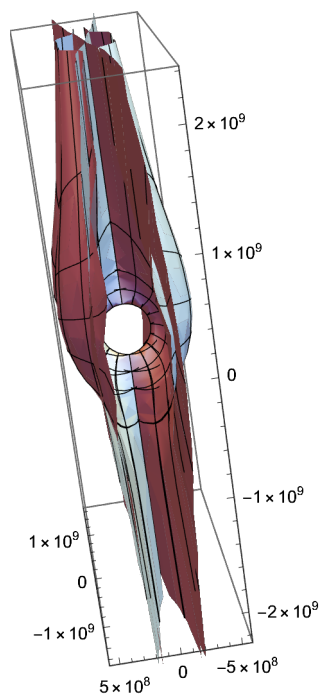




SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot \pi^{18} \left( \frac{1}{2\pi} \left[ \sqrt{4\pi \left( 2\pi \sqrt{\left( 4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \right)} \right)^2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \right) / \left( 4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \right)^2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right)^2 - 1.1294090667581471 \cdot \pi^{18} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + 8.987551787368176 \cdot \pi^{16} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \left( 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) \right)^2 \right) / \left( \sqrt{\left( 39.47841760435743 \cdot \left( \frac{\sqrt{4\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta}}^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}}{2\pi} \right)^2 - 12.566370614359172 \cdot \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta) 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \right)^2 \theta + \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right)}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\} \right]$$





SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} \left( \frac{1}{2\pi} \sqrt{4\pi \left( \left( 2\pi \sqrt{\left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right) 2 \right.} \right.} \right.} \right.} \right.} \right.} \right.} \right.} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) \Big/ \left( \left( 4\pi - 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) 2 \right. \\ \left. \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta} \right)^2 \theta^2 \right) \Bigg)^2 -$$

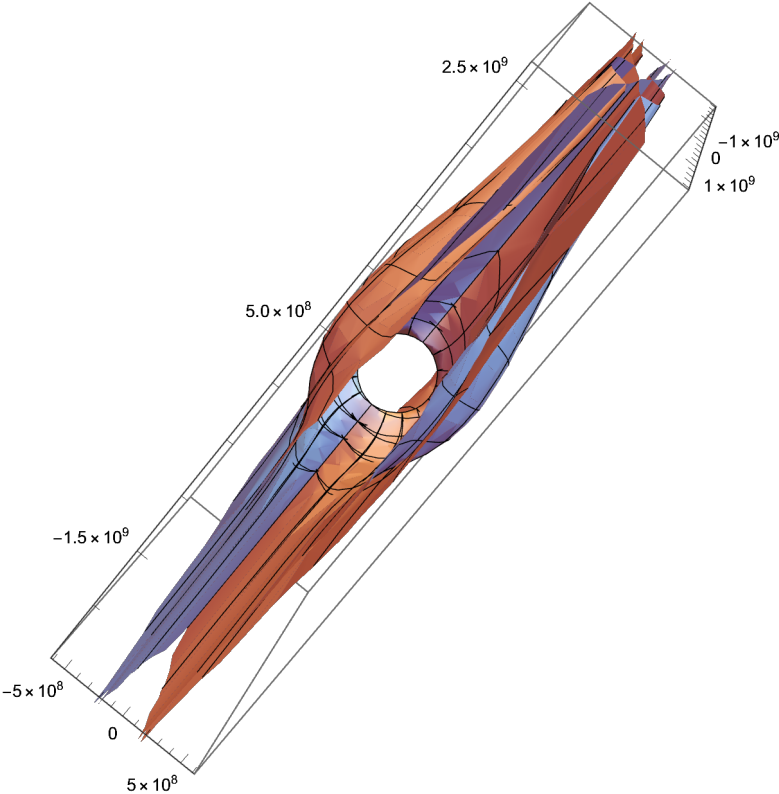
$$1.1294090667581471 \cdot 10^{18} \left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta} \right)^2 \theta + 8.987551787368176 \cdot 10^{16}$$

$$\left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta} \right)^2 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \Bigg) \Bigg/$$

$$\left( \sqrt{\left( 39.47841760435743 \cdot \frac{\sqrt{4\pi \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta}} \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta} \right)^2 \theta^2}{2\pi} \right)^2 -$$

$$12.566370614359172 \cdot \left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right)^2 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) +$$

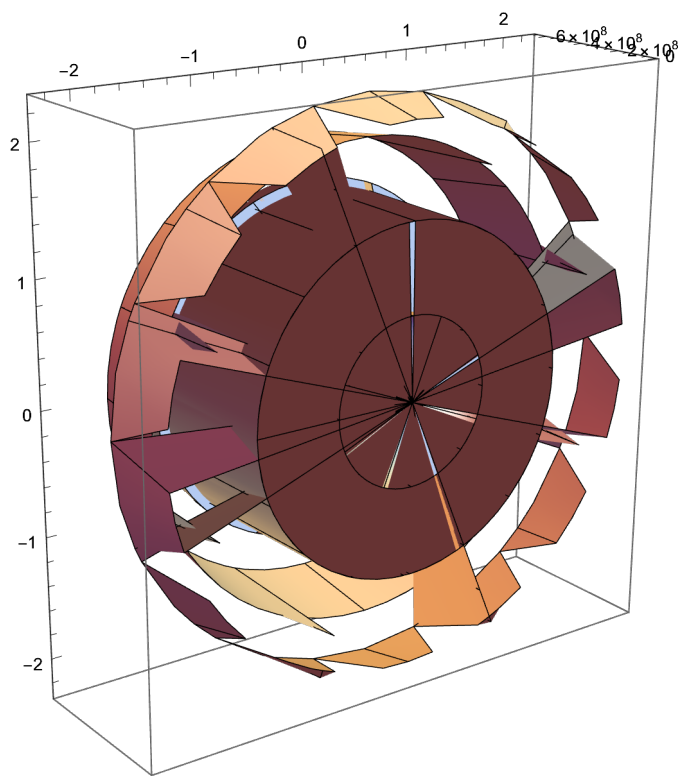
$$\left( \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta} \right)^2 \theta^2 \Bigg), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}]$$



$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right)$$

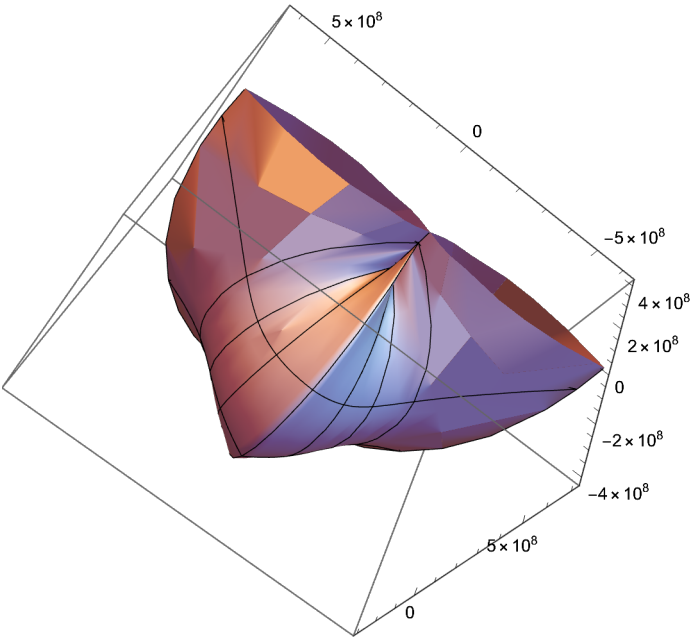
`RevolutionPlot3D[`

[illegible]



SphericalPlot3D[

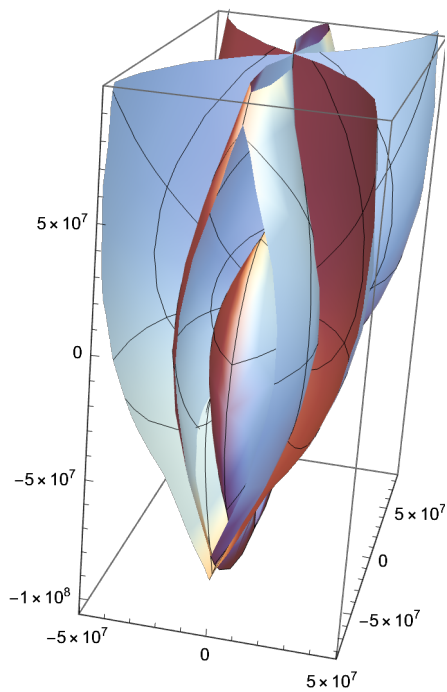
$$\left( \sqrt{\left( 3.5481432270250993 \cdot \pi^{18} \left( \frac{1}{2\pi} \left( \sqrt{4\pi \left( \frac{1}{(4\pi - \theta)\theta} 2\pi \sqrt{4\pi - \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \theta \right)^2 \right.} \right. \\ \left. \left. \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right)^2 - 1.1294090667581471 \cdot \pi^{18} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + 8.987551787368176 \cdot \pi^{16} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) / \left( \sqrt{39.47841760435743} \cdot \left( \frac{\sqrt{4\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}^2}{(4\pi - \theta)\theta} 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2}}{2\pi} \right)^2 - 12.566370614359172 \cdot \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}]$$



SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot \pi^{18} \left( \frac{1}{2\pi} \left( \sqrt{\left( 4\pi \left( \frac{1}{(4\pi - \theta)\theta} 2\pi \sqrt{\left( 4\pi - \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right) \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right)^2 - 1.1294090667581471 \cdot \pi^{18} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + 8.987551787368176 \cdot \pi^{16} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right) \right) / \left( \sqrt{\left( 39.47841760435743 \cdot \left( \frac{1}{2\pi} \left( \sqrt{\left( 4\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})} \right) \theta} 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}) - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right) \right) \right) - 12.566370614359172 \cdot \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right) \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\} \right]$$

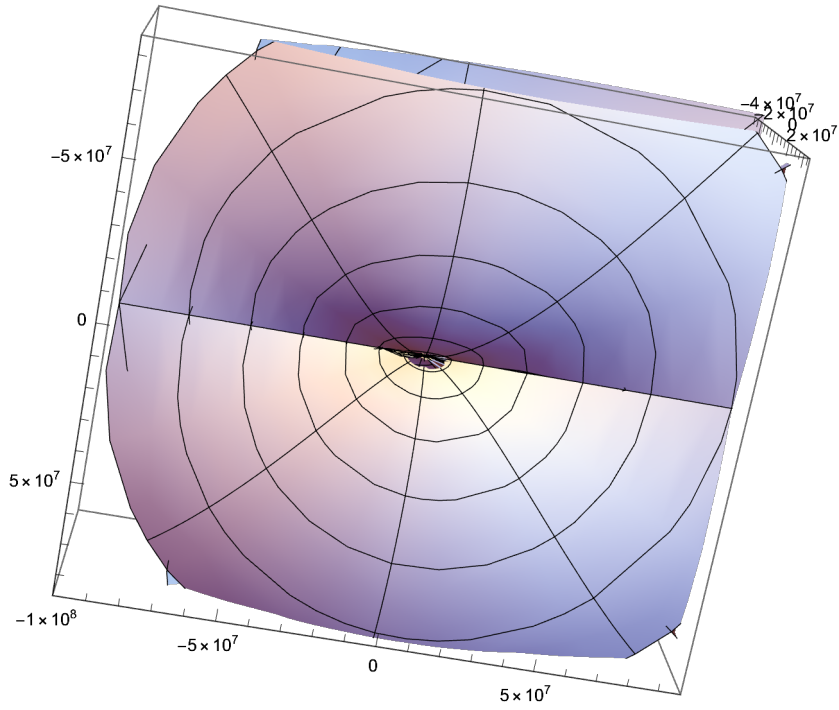




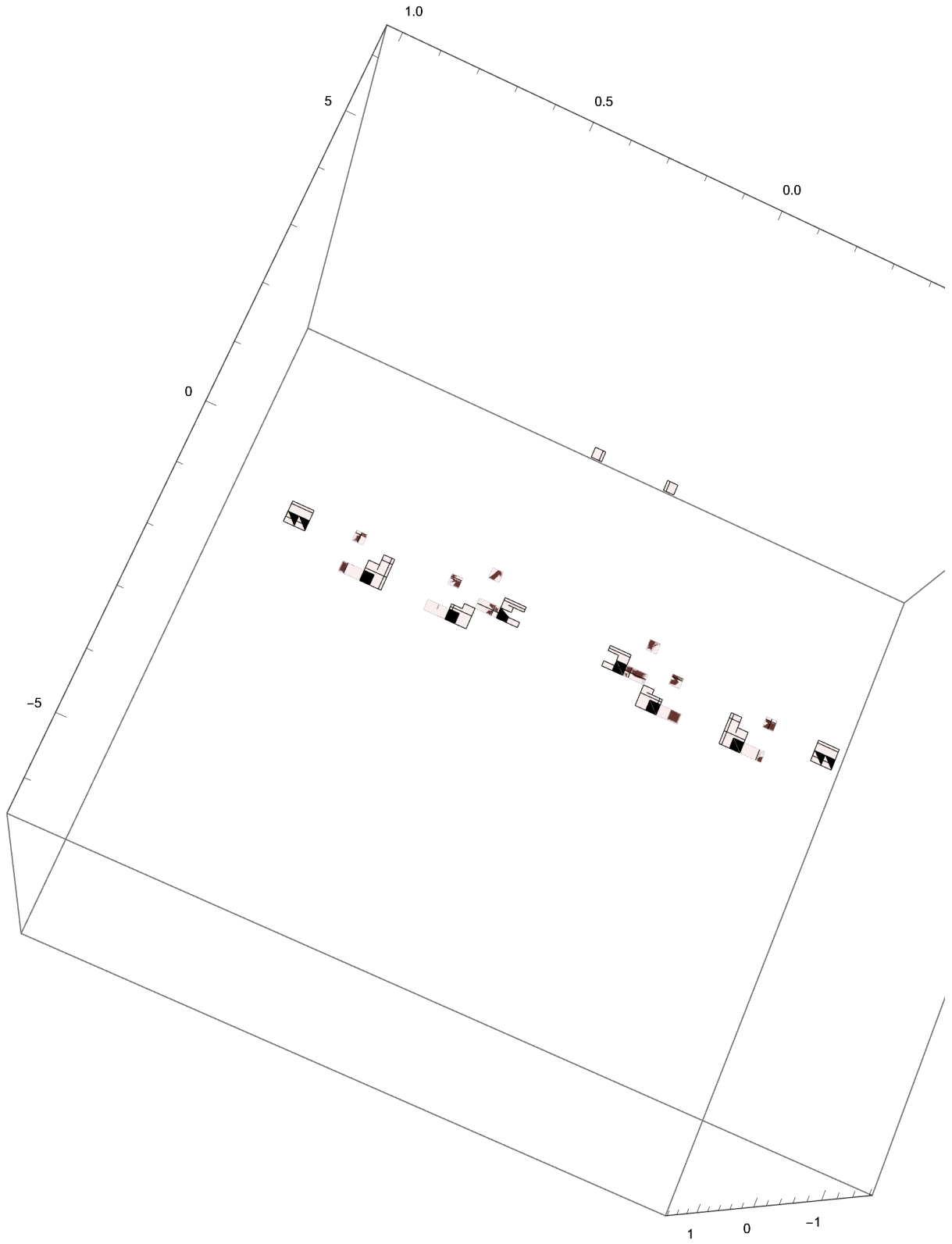
SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} \left( \frac{1}{2\pi} \left( \sqrt{\left( 4\pi \left( \frac{1}{(4\pi - \theta)\theta} 2\pi \sqrt{\left( 4\pi - \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) \right) \right) \right) \right) \right) \right) \right) \right) \right) \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \theta \right)^2 \theta - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right)^2 - 1.1294090667581471 \cdot 10^{18} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta + 8.987551787368176 \cdot 10^{16} \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right) \right) /$$

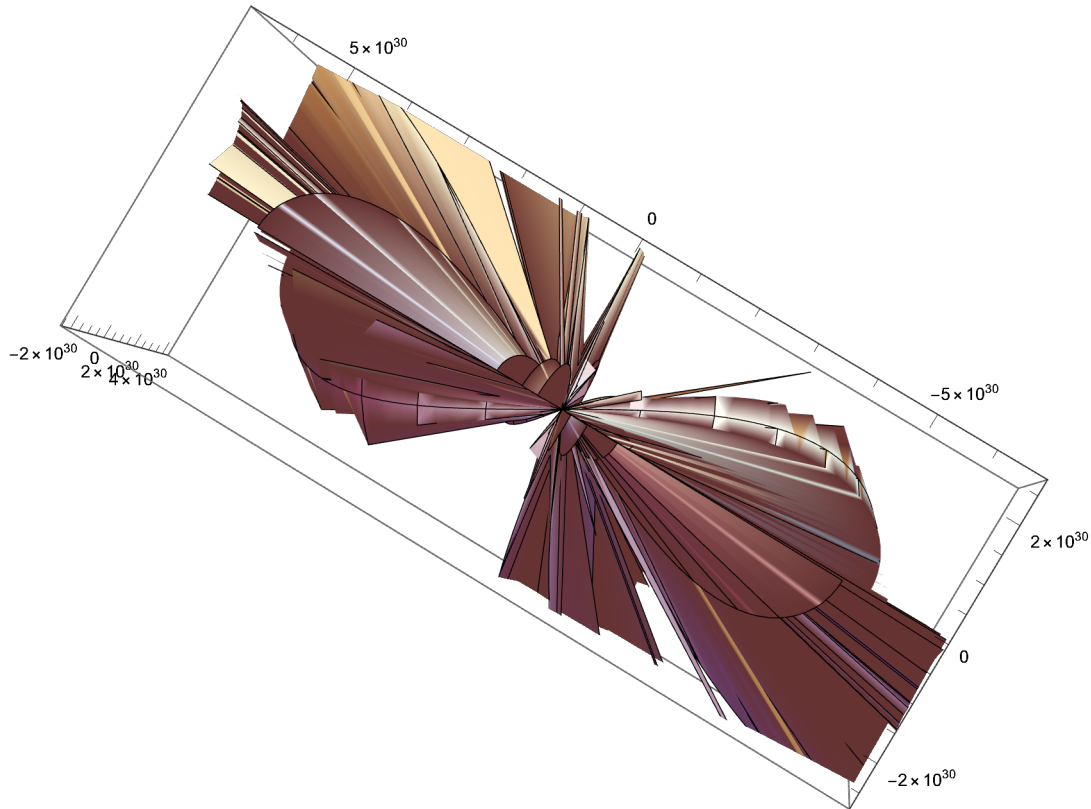
$$\begin{aligned}
& \left( \sqrt{39.47841760435743} \cdot \left( \frac{1}{2\pi} \left( \sqrt{4\pi \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - 2(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})\theta} \right)^2 \left( \pi + \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) - \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \theta^2 \right) \right)^2 - 12.566370614359172 \cdot \right. \\
& \quad \left( \frac{1}{(4\pi - \theta)\theta} 2\pi \sqrt{\left( \left( 4\pi - \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + \right. \right. \right. \right. \\
& \quad \left. \left. \left. 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + \right. \right. \\
& \quad \left. \left. 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \theta \right)^2 \theta + \\
& \quad \left( \frac{2\pi \sqrt{(4\pi - \theta)\theta}}{(4\pi - \theta)\theta} \right)^2 \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + \right. \right. \right. \\
& \quad \left. \left. \left. 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \right. \\
& \quad \left. \left. \left. \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 \right) \right) \right), \\
& \{ \theta, -2\pi, 2\pi \}, \{ \beta, -\pi / \\
& \quad 2, \\
& \quad \pi / \\
& \quad 2 \} ]
\end{aligned}$$



`ContourPlot3D` $\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left(\left(2 \pi r - 2 \pi \left(r - \frac{r \theta}{2 \pi}\right) - \theta r\right)^2\right),\right.$   
 $\left.\{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



$$\text{SphericalPlot3D}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \frac{\theta}{2 \pi} \right) - \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} \right]$$



$$\theta := \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}$$

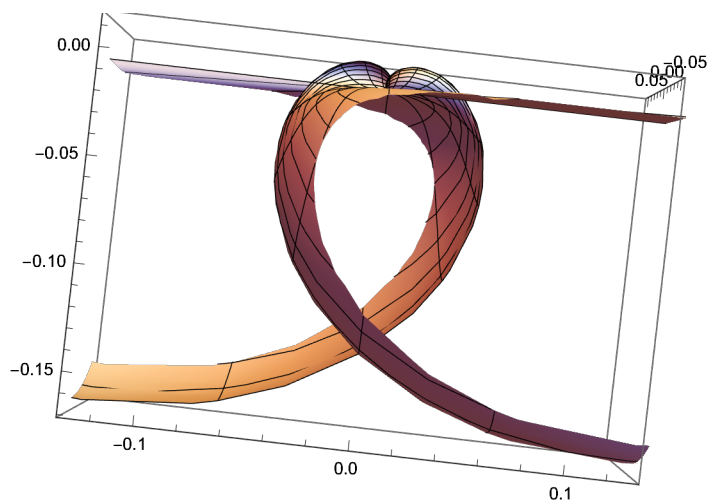
$$\beta := \text{ArcSin}\left[\frac{\sqrt{-4 \pi^2 \theta + 4 \pi \theta^2 - \theta^3}}{2 \pi \sqrt{-4 \pi + \theta}}\right]$$

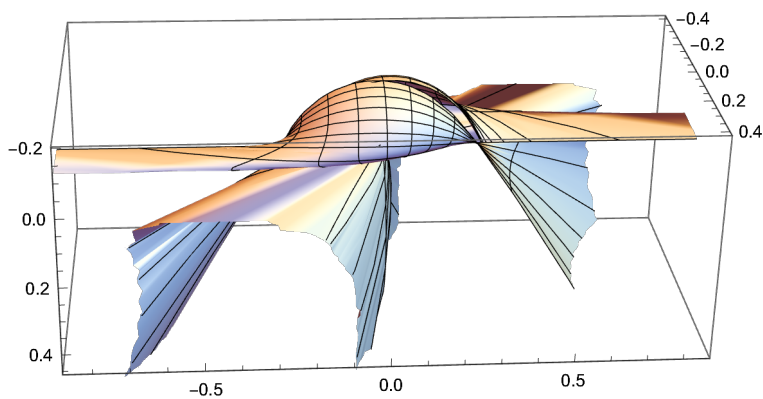
$$\text{SphericalPlot3D}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \right) - \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\} \right]$$

$$\text{SphericalPlot3D}\left[\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} / \left( \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} \right) - \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \right), \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\} \right]$$

{}

$$\text{SphericalPlot3D}\left[\frac{(2 \pi \sin[\beta])}{(\sqrt{4 \pi \theta - \theta^2})} \left/ \left( \left( 2 \pi \frac{1}{(4 \pi - \theta) \theta} 2 \pi \sqrt{\left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)} \right) \right) \right. \right. \\ \left. \left. 2 \pi \left( \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - \frac{\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta}{2 \pi} - \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^2 \right), \right. \\ \left. \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi/2, \pi/2\} \right]$$







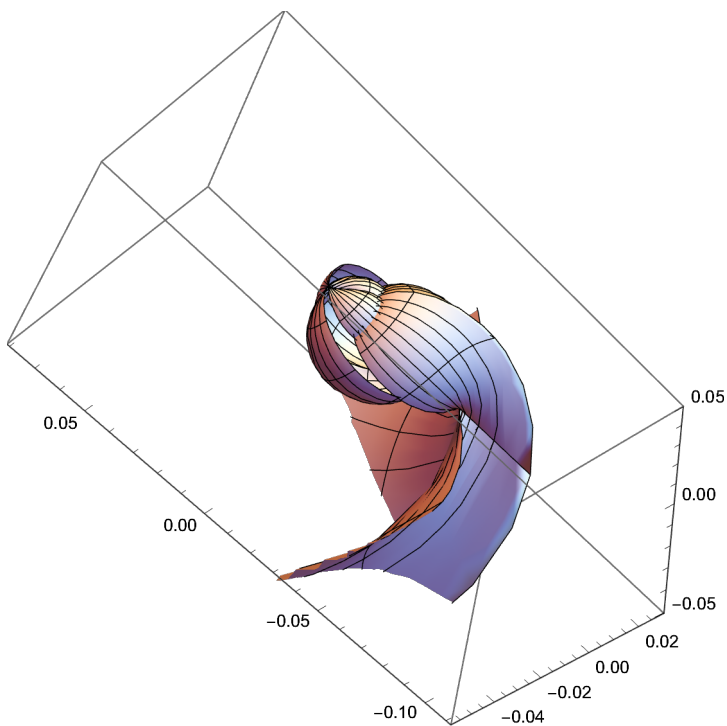
$$\text{SphericalPlot3D}\left[\frac{2 \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{4 \pi \theta - \theta^2}}\right] /$$

$$\left(\left(2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \left(2 \pi \sqrt{(4 \pi - \theta) \theta}\right) / \left((4 \pi - \theta) \left(\frac{4 \pi}{3} -\right.\right.\right.\right.$$

$$\left.\left.\left.\frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}}\right.\right.\right.$$

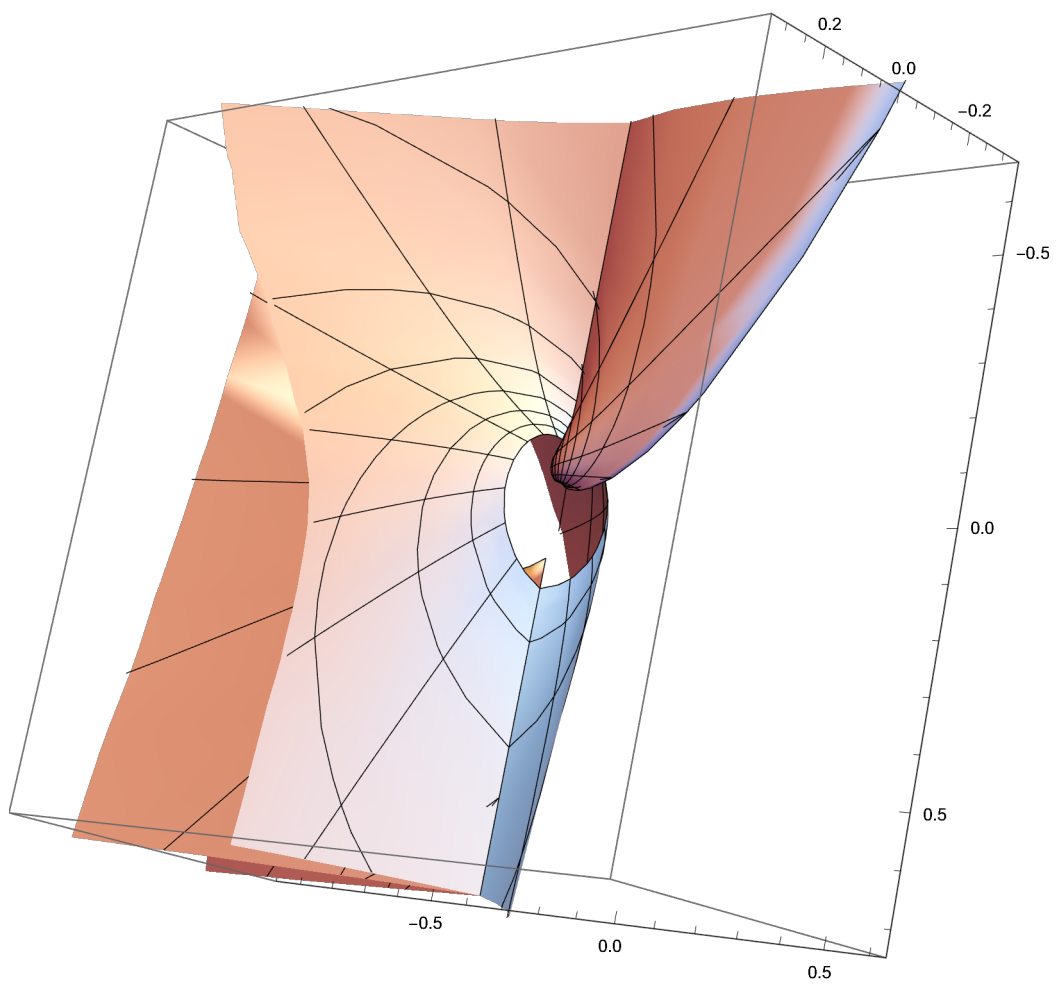
$$\left.\left.\left.+ \frac{2}{3} \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right)\right) - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta -\right.$$

$$\left.\theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}\right)^{1/2}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

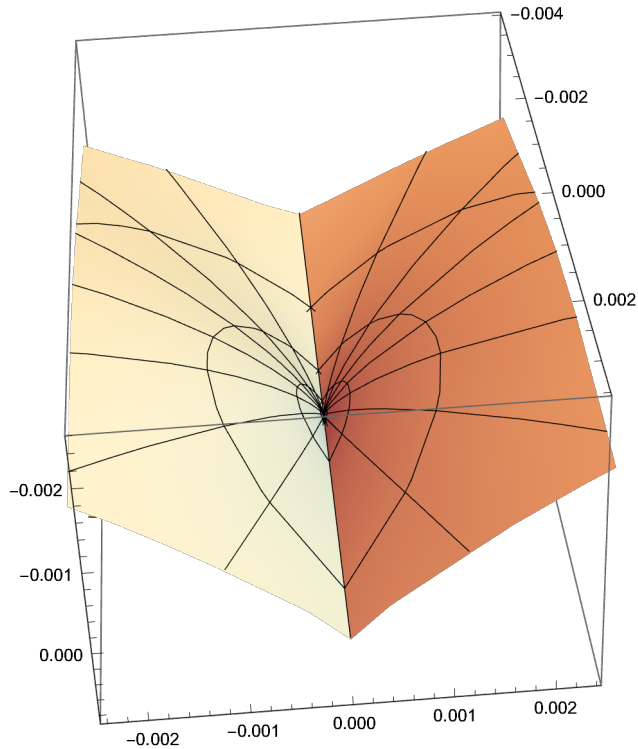


$$\begin{aligned}
& \text{SphericalPlot3D}\left[\frac{2 \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{4 \pi \theta - \theta^2}} / \right. \\
& \left. \left( \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) \theta} \right) / \left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) \right) - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta \right) - \\
& \left. \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^{\wedge 2}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} \Big]
\end{aligned}$$

$$\begin{aligned}
& \text{SphericalPlot3D}\left[\frac{2 \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{4 \pi \theta - \theta^2}} / \right. \\
& \left. \left( \left( 2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} - 2 \pi \left( 2 \pi \sqrt{(4 \pi - \theta) 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right) / \left( (4 \pi - \theta) \left( \frac{4 \pi}{3} - \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right) \right) \right) - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta \right) - \\
& \left. \theta \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \right)^{\wedge 2}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\} \Big]
\end{aligned}$$



$$\text{SphericalPlot3D}\left[\frac{2 \pi \sin\left[\text{ArcSin}\left[\frac{\sqrt{(4 \pi - \theta) \theta}}{2 \pi}\right]\right]}{\sqrt{4 \pi \theta - \theta^2}}\right] / \left(\left(2 \pi \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})) \theta} - \right.\right. \\ \left.2 \pi \left(\left(2 \pi \sqrt{(4 \pi - \theta) 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})}\right) / \left((4 \pi - \theta) \left(\frac{4 \pi}{3} - \right.\right.\right. \\ \left.\left.\left.\frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}} \right.\right.\right. \\ \left.\left.\left. + \frac{2}{3} (-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6})^{1/3}\right)\right) - \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} \theta\right) - \\ \left.\theta \frac{2 \pi \sqrt{(4 \pi - 2 (\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2})) \theta}}{(4 \pi - \theta) \theta}\right)^{1/2}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$

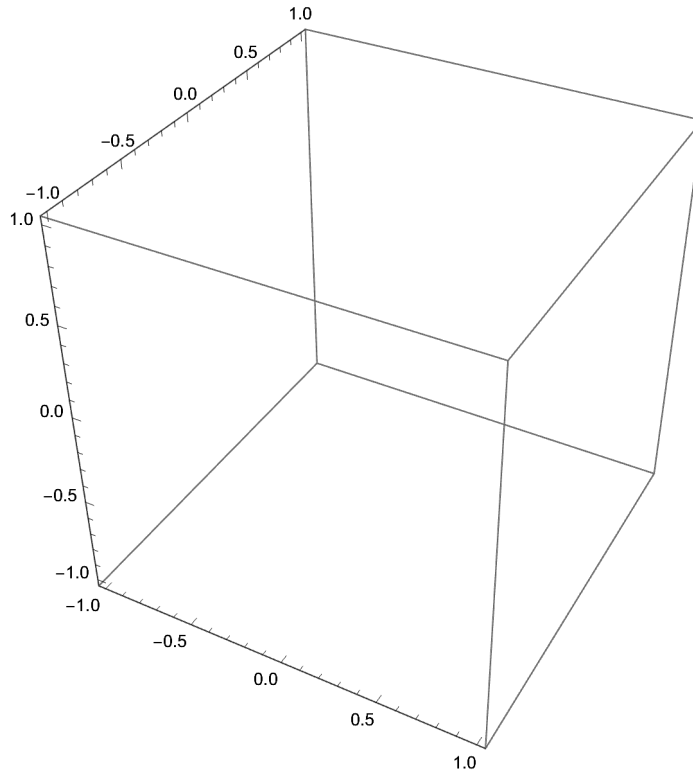


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SphericalPlot3D[
  (

$$\sqrt{\left(3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right) + 8.987551787368176 \cdot 10^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right)^2\right)} \right) /$$


$$\left(\sqrt{\left(39.47841760435743 - 12.566370614359172 \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right)\right) + (\theta)^2\right)}\right),$$

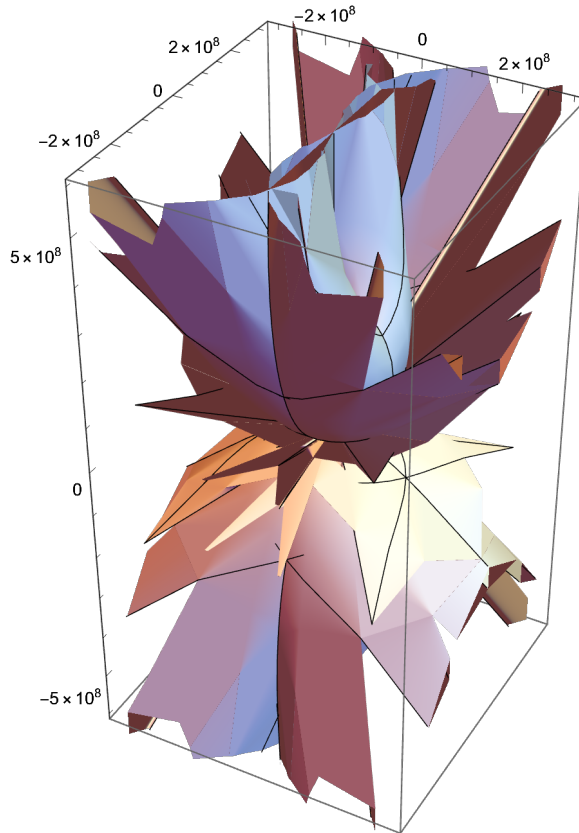
  {\beta, -\pi/2, \pi/2}, {\theta, -2\pi, 2\pi}]
```



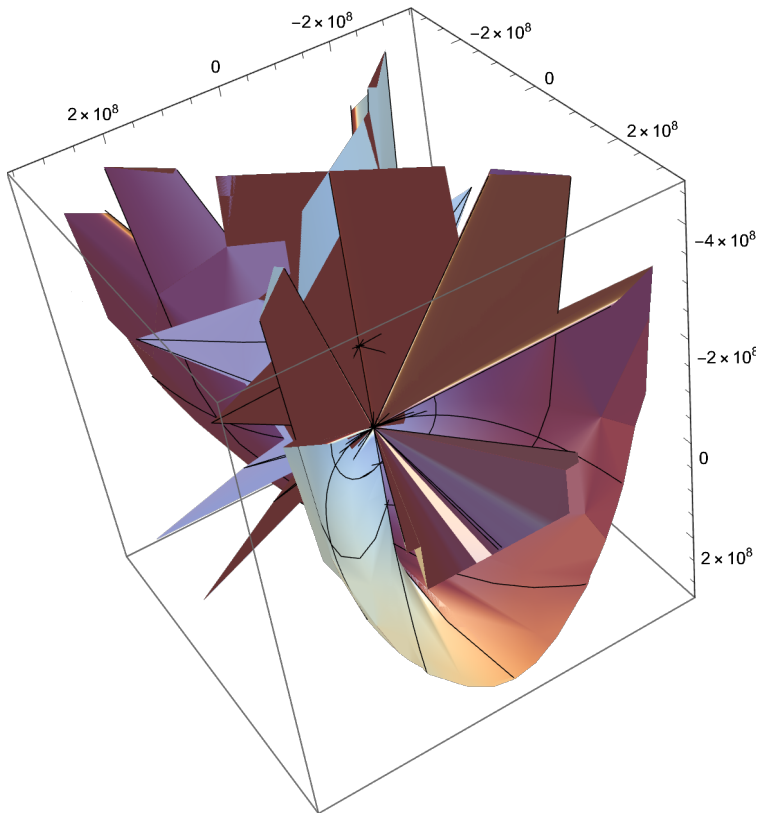
SphericalPlot3D[

$$\left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right) + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 \right)} \right) / \left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right) + (\theta)^2 \right)} \right),$$

{ $\beta$ ,  $-\pi$ ,  $\pi$ }, { $\theta$ ,  $-4\pi$ ,  $4\pi$ }]



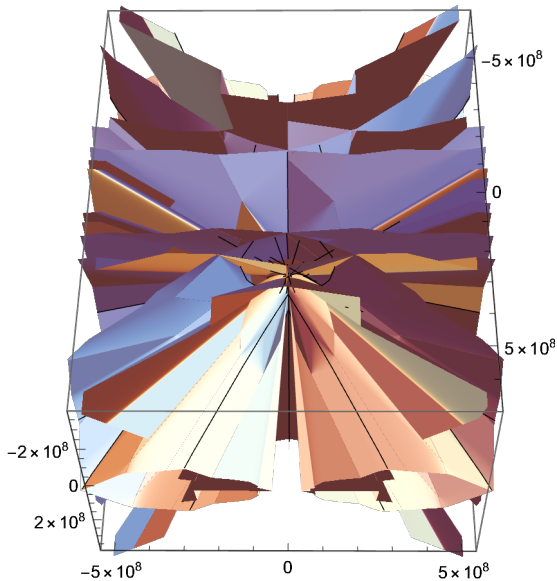
```
SphericalPlot3D[
  (
    Sqrt[
      (
        3.5481432270250993`*^18 - 1.1294090667581471`*^18 (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])) +
        8.987551787368176`*^16 (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])^2)
      )
    ] /
    (
      Sqrt[
        (
          39.47841760435743` - 12.566370614359172` (2 (pi + Sqrt[pi^2 - pi^2 Sin[beta]^2])) + (theta)^2
        )
      )
    ],
  {theta, -4 pi, 4 pi}, {beta, -pi, pi}]
```



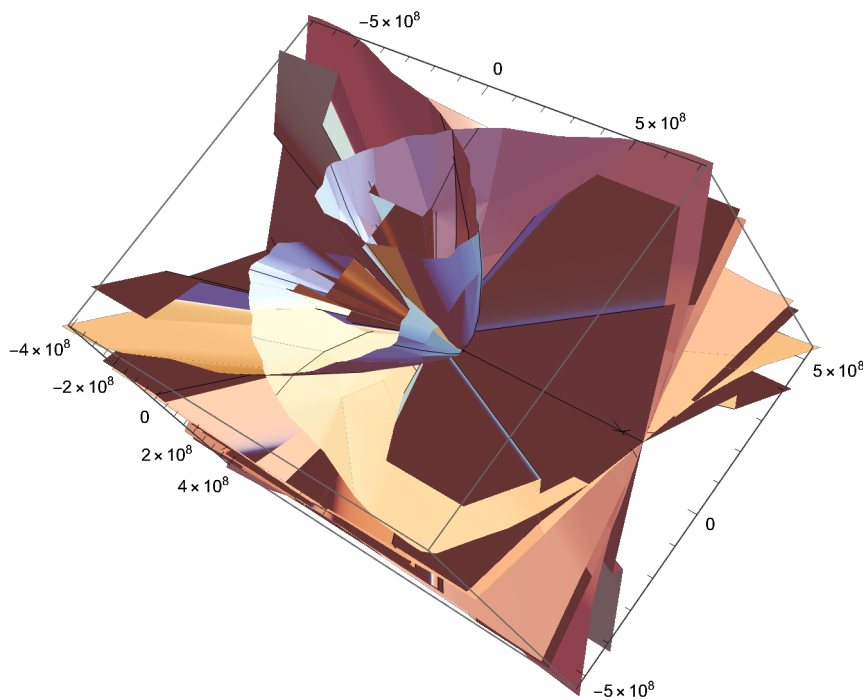
$$\begin{aligned}
& D \left[ \left( \sqrt{\left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right.} \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \right) \right] / \\
& \quad \left( \sqrt{\left( 39.47841760435743 - 12.566370614359172 \cdot \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + (\theta)^2 \right) \right)}, \theta, \beta \right] \\
& - \left( \theta \left( \frac{2.22936 \times 10^{19} \cos[\beta] \sin[\beta]}{\sqrt{\pi^2 - \pi^2 \sin[\beta]^2}} - \frac{7.09629 \times 10^{18} \cos[\beta] \sin[\beta] \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}{\sqrt{\pi^2 - \pi^2 \sin[\beta]^2}} \right) \right) / \\
& \quad \left( 2 \left( 39.4784 + \theta^2 - 25.1327 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2} \sqrt{\left( 3.54814 \times 10^{18} - \right.} \right. \\
& \quad \left. \left. 2.25882 \times 10^{18} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 3.59502 \times 10^{17} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 \right) \right) + \\
& \quad \left( 372.075 \theta \cos[\beta] \sin[\beta] \sqrt{\left( 3.54814 \times 10^{18} - 2.25882 \times 10^{18} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \right.} \right. \\
& \quad \left. \left. 3.59502 \times 10^{17} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 \right) \right) \right) / \\
& \quad \left( \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \left( 39.4784 + \theta^2 - 25.1327 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{5/2} \right)
\end{aligned}$$



$$\text{SphericalPlot3D}\left[-\left(\theta\left(\frac{2.2293641391812866\cdot^{19}\cos[\beta]\sin[\beta]}{\sqrt{\pi^2-\pi^2\sin[\beta]^2}}-\frac{7.096286454050199\cdot^{18}\cos[\beta]\sin[\beta]\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)}{\sqrt{\pi^2-\pi^2\sin[\beta]^2}}\right)\right)/\right. \\ \left.2\left(39.47841760435743\cdot+\theta^2-25.132741228718345\cdot\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)\right)^{3/2}\right. \\ \left.\sqrt{\left(3.5481432270250993\cdot^{18}-2.2588181335162941\cdot^{18}\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)+\right.}\right. \\ \left.3.5950207149472704\cdot^{17}\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^2\right)\right)+ \\ \left(372.0753201635978\cdot\theta\cos[\beta]\sin[\beta]\sqrt{\left(3.5481432270250993\cdot^{18}-\right.}\right. \\ \left.2.2588181335162941\cdot^{18}\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)+\right. \\ \left.3.5950207149472704\cdot^{17}\left(\pi+\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^2\right)\right)/\left(\sqrt{\pi^2-\pi^2\sin[\beta]^2}\right)^{5/2}\right), \\ \{\beta,-\pi,\pi\},\{\theta,-4\pi,4\pi\}]$$

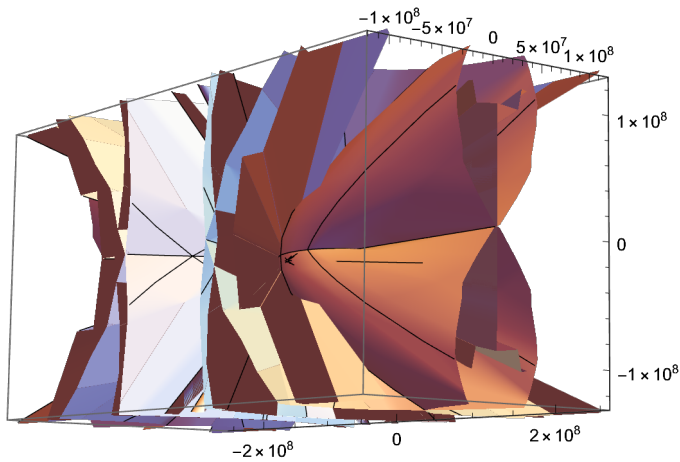


$$\begin{aligned}
& \text{SphericalPlot3D}\left[-\left(\theta\left(\frac{2.2293641391812866 \cdot 10^{19} \cos[\beta] \sin[\beta]}{\sqrt{\pi^2 - \pi^2 \sin[\beta]^2}} - \right.\right.\right. \\
& \quad \left.\left.\frac{7.096286454050199 \cdot 10^{18} \cos[\beta] \sin[\beta] \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)}{\sqrt{\pi^2 - \pi^2 \sin[\beta]^2}}\right)\right) / \\
& \quad \left(2 \left(39.47841760435743 + \theta^2 - 25.132741228718345 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{3/2} \right. \\
& \quad \left. \sqrt{\left(3.5481432270250993 \cdot 10^{18} - 2.2588181335162941 \cdot 10^{18} \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + \right.\right. \\
& \quad \left.\left.3.5950207149472704 \cdot 10^{17} \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)^2\right)}\right) + \\
& \quad \left(372.0753201635978 \theta \cos[\beta] \sin[\beta] \sqrt{\left(3.5481432270250993 \cdot 10^{18} - \right.\right. \\
& \quad \left.\left.2.2588181335162941 \cdot 10^{18} \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + \right.\right. \\
& \quad \left.\left.3.5950207149472704 \cdot 10^{17} \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)^2\right)}\right) / \left(\sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)^2 \\
& \quad \left.\left(39.47841760435743 + \theta^2 - 25.132741228718345 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^{5/2}\right), \\
& \quad \{\theta, -4 \pi, 4 \pi\}, \{\beta, -\pi, \pi\}]
\end{aligned}$$



$$\begin{aligned}
 & D \left[ \left( \sqrt{ \left( 3.5481432270250993 \cdot 10^{18} - 1.1294090667581471 \cdot 10^{18} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + \right. \right. \right. \\
 & \quad \left. \left. \left. 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 \right) \right) \right] / \\
 & \quad \left( \sqrt{ \left( 39.47841760435743 - 12.566370614359172 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right) + (\theta)^2 \right) \right), \theta ] \\
 & - \left( \theta \sqrt{ \left( 3.54814 \times 10^{18} - \right. \right. \\
 & \quad \left. \left. 2.25882 \times 10^{18} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 3.59502 \times 10^{17} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 \right) \right) / \\
 & \quad \left( 39.4784 + \theta^2 - 25.1327 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}
 \end{aligned}$$

$$\begin{aligned}
 & \text{SphericalPlot3D} \left[ \right. \\
 & \quad - \left( \theta \sqrt{ \left( 3.5481432270250993 \cdot 10^{18} - 2.2588181335162941 \cdot 10^{18} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \right. \right. \\
 & \quad \left. \left. 3.5950207149472704 \cdot 10^{17} \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)^2 \right) \right) / \\
 & \quad \left( 39.47841760435743 + \theta^2 - 25.132741228718345 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^{3/2}, \\
 & \quad \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\} \left. \right]
 \end{aligned}$$

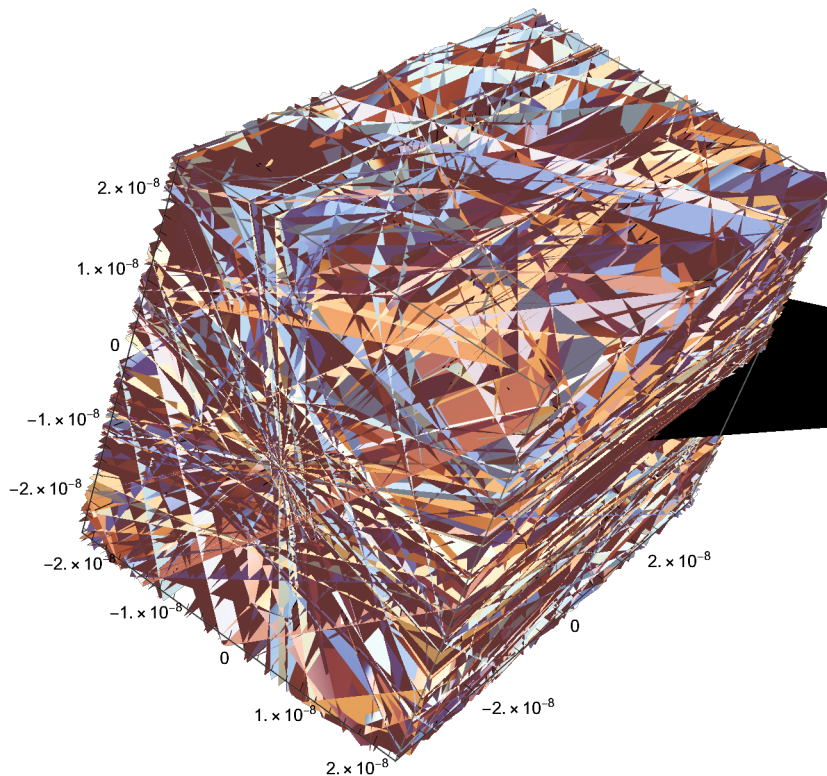


$$\begin{aligned}
& D \left[ \left( \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right. \right. \\
& \quad \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2) \right) \right] / \\
& \left( \sqrt{-12.566370614359172 \cdot 10^0 \theta + \theta^2 + 39.47841760435743 \cdot 10^0 \sin[\beta]^2} \right), \theta, \beta \Big] \\
& - \left( 1.77407 \times 10^{18} (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta] \right) / \\
& \left( \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \right. \\
& \quad \left. (-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2)^{3/2} \right) - \\
& \left( 1.77407 \times 10^{18} (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] \right) / \left( (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^{3/2} \right. \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) - \\
& \left( 19.7392 (-1.12941 \times 10^{18} + 1.79751 \times 10^{17} \theta) \cos[\beta] \sin[\beta] \right) / \\
& \left( (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^{3/2} \right. \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) + \\
& \left( 59.2176 (-12.5664 + 2 \theta) \cos[\beta] \sin[\beta] \right. \\
& \quad \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) / \\
& \left( -12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2 \right)^{5/2}
\end{aligned}$$

```

SphericalPlot3D[
- (1.7740716135125496`*^18 (-1.1294090667581471`*^18 + 1.7975103574736352`*^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( \sqrt{-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2} \right.$ 
   $\left. \left( -1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 + \right.$ 
   $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2 \right)^{3/2} \right) -$ 
(1.7740716135125496`*^18 (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]) /
 $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)^{3/2} \right.$ 
 $\left. \sqrt{(-1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 + \right.$ 
 $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2) \right) -$ 
(19.739208802178716` (-1.1294090667581471`*^18 + 1.7975103574736352`*^17  $\theta$ )
  Cos[ $\beta$ ] Sin[ $\beta$ ]) /  $\left( (-12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2)^{3/2} \right.$ 
 $\left. \sqrt{(-1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 + \right.$ 
 $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2) \right) +$ 
(59.21762640653615` (-12.566370614359172` + 2  $\theta$ ) Cos[ $\beta$ ] Sin[ $\beta$ ]
 $\sqrt{(-1.1294090667581471`*^18 \theta + 8.987551787368176`*^16 \theta^2 + \right.$ 
 $\left. 3.5481432270250993`*^18 \text{Sin}[\beta]^2) \right) /$ 
 $\left( -12.566370614359172` \theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2 \right)^{5/2}, \{\theta, -2$ 
 $\pi, 2\pi\}, \{\beta, -\pi, \pi\}$ 

```



SphericalPlot3D[  

$$\left\{ \left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)} \right) / \right.$$
  

$$\left( \sqrt{-12.566370614359172 \cdot 10^{18} \theta + 39.47841760435743 \cdot 10^{18} \sin[\beta]^2} \right),$$
  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right.$$
  

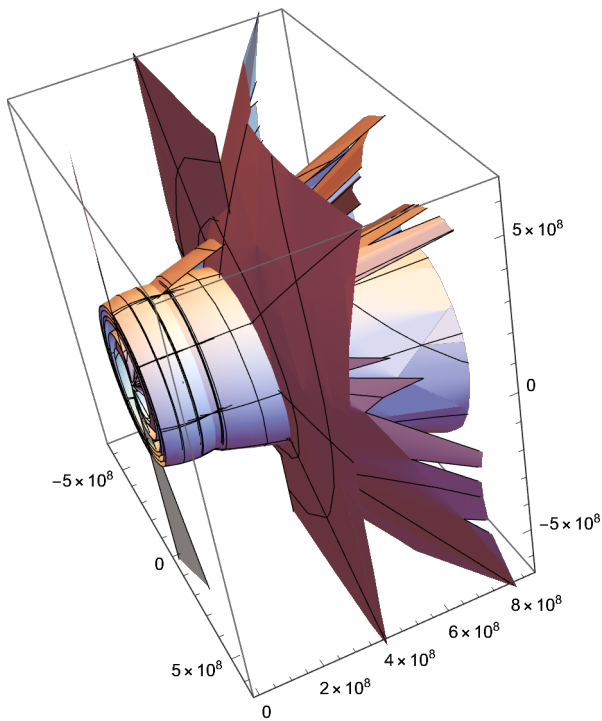
$$\left. \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) /$$
  

$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{18} \theta + \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right) / \right.} \right.$$
  

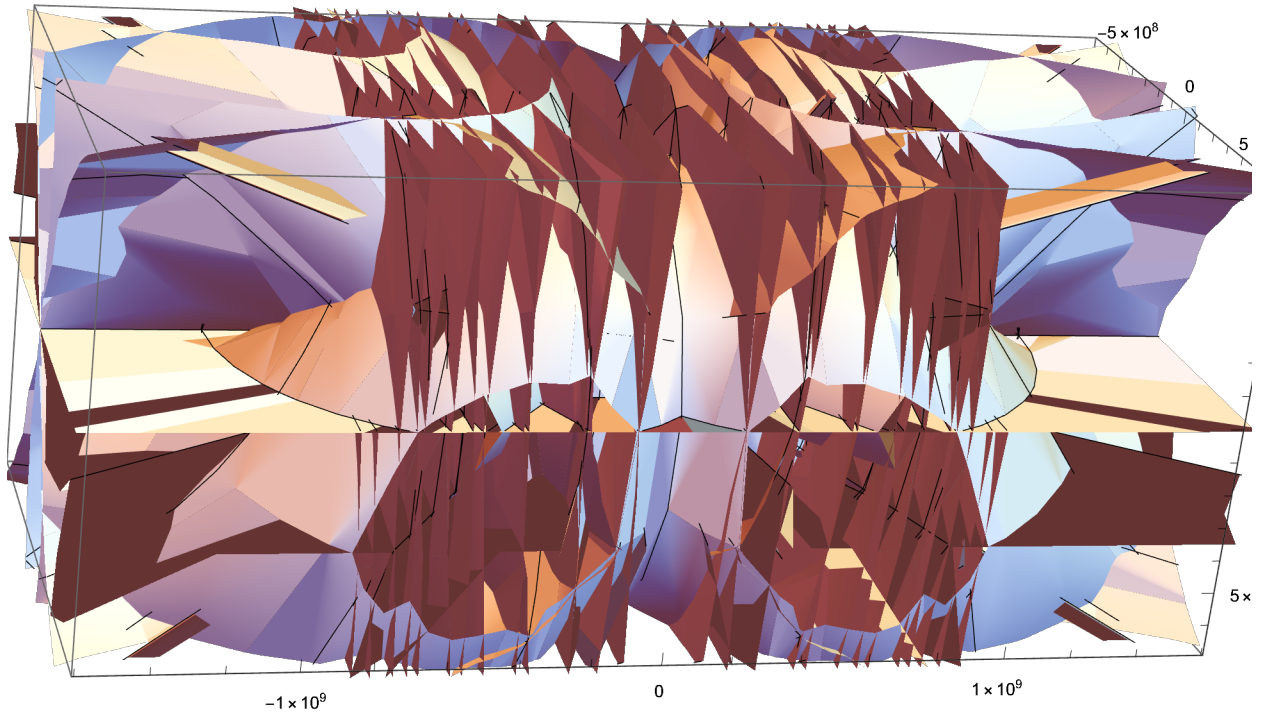
$$\left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) +$$
  

$$\left. \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)^2 +$$
  

$$\left. \left. 39.47841760435743 \cdot 10^{18} \sin[\beta]^2 \right) \right\}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}]$$



$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left\{\sqrt{\left(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + \right.}\right.\right. \\
& \quad \left.8.987551787368176 \cdot \theta^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)\bigg)^2\bigg)\bigg) / \\
& \quad \left(\sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2}\right), \\
& \quad \left(\sqrt{\left(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \right.}\right. \\
& \quad \left.8.987551787368176 \cdot \theta^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)\bigg)^2\bigg)\bigg) / \\
& \quad \left(\sqrt{\left(39.47841760435743 - 12.566370614359172 \cdot \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + (\theta)^2\right)}\right), \\
& \quad - \left(1. \cdot \sqrt{\left(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + \right.}\right. \\
& \quad \left.8.987551787368176 \cdot \theta^{16} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)\bigg)^2\bigg)\bigg) / \\
& \quad \left(\sqrt{\left(39.47841760435743 - 12.566370614359172 \cdot \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \right.}\right. \\
& \quad \left.\left.2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)\bigg)^2\bigg)\bigg), \\
& \quad - \left(1. \cdot \sqrt{\left(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + \right.}\right. \\
& \quad \left.8.987551787368176 \cdot \theta^{16} (\theta)^2\right)\bigg)\bigg) / \\
& \quad \left(\sqrt{\left(39.47841760435743 - 12.566370614359172 \cdot \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \right.}\right. \\
& \quad \left.\left.2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)\bigg)^2\bigg)\bigg), \\
& \quad - \left(1. \cdot \sqrt{\left(3.5481432270250993 \cdot \theta^{18} - 1.1294090667581471 \cdot \theta^{18} + \right.}\right. \\
& \quad \left.8.987551787368176 \cdot \theta^{16} (\theta)^2\right)\bigg)\bigg) / \\
& \quad \left(\sqrt{\left(39.47841760435743 - 12.566370614359172 \cdot (\theta) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2\right)}\right), \\
& \quad - \left(1. \cdot \sqrt{\left(3.5481432270250993 \cdot \theta^{18} - \right.}\right. \\
& \quad \left.1.1294090667581471 \cdot \theta^{18} \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right) + \right. \\
& \quad \left.8.987551787368176 \cdot \theta^{16} \left(\left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)\right)^2\right)\bigg)^2\bigg)\bigg) / \\
& \quad \left.\left(\sqrt{39.47841760435743 - 12.566370614359172 \cdot \theta + \theta^2}\right)\right\}, \{\beta, -\pi, \pi\}, \{\theta, -4\pi, 4\pi\}]
\end{aligned}$$



$$\text{Solve}\left[\eta_1 == \frac{\frac{2\pi r - r\theta}{2\pi} \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi}, \theta_1\right]$$

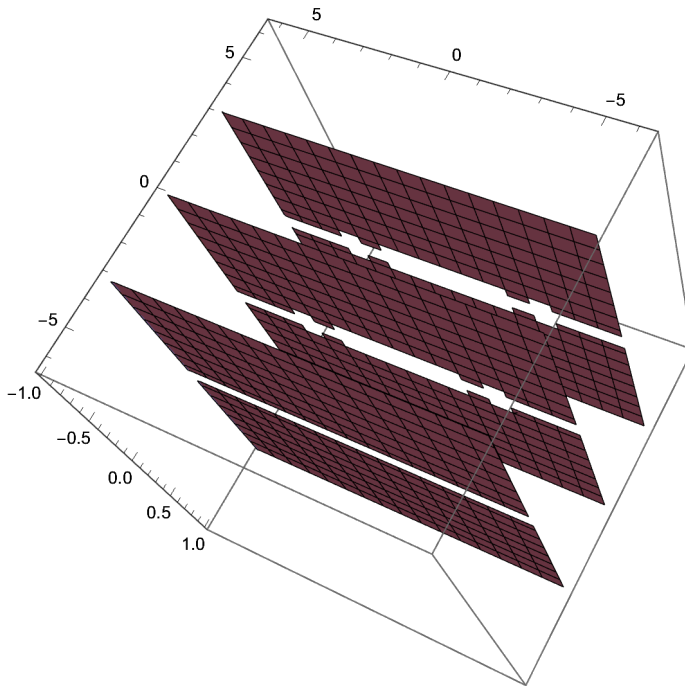
$$\left\{\left\{\theta_1 \rightarrow \left(-\pi r^2 \left(-16\pi^2 + 16\pi\theta - 4\theta^2\right) - \sqrt{\pi^2 r^4 \left(-16\pi^2 + 16\pi\theta - 4\theta^2\right)^2 - 64\pi^4 r^2 \left(4\pi^2 - 4\pi\theta + \theta^2\right) \eta_1^2}\right) / \left(2r^2 \left(4\pi^2 - 4\pi\theta + \theta^2\right)\right)\right\}, \left\{\theta_1 \rightarrow \left(-\pi r^2 \left(-16\pi^2 + 16\pi\theta - 4\theta^2\right) + \sqrt{\pi^2 r^4 \left(-16\pi^2 + 16\pi\theta - 4\theta^2\right)^2 - 64\pi^4 r^2 \left(4\pi^2 - 4\pi\theta + \theta^2\right) \eta_1^2}\right) / \left(2r^2 \left(4\pi^2 - 4\pi\theta + \theta^2\right)\right)\right\}\right\}$$

$$\frac{r_1 \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi}$$



$$\left( -\pi r^2 (-16\pi^2 + 16\pi\theta - 4\theta^2) - \sqrt{\pi^2 r^4 (-16\pi^2 + 16\pi\theta - 4\theta^2)^2 - 64\pi^4 r^2 (4\pi^2 - 4\pi\theta + \theta^2) \frac{r_1 \sqrt{4\pi - \theta_1} \sqrt{\theta_1}}{2\pi}^2} \right) / (2 r^2 (4\pi^2 - 4\pi\theta + \theta^2)) \left( -\pi r^2 (-16\pi^2 + 16\pi\theta - 4\theta^2) - \sqrt{\pi^2 r^4 (-16\pi^2 + 16\pi\theta - 4\theta^2)^2 - 16\pi^2 r^2 (4\pi^2 - 4\pi\theta + \theta^2) r_1^2 (4\pi - \theta_1) \theta_1} \right)$$

$$\text{ContourPlot3D}\left[ \frac{1}{2 r^2 (4\pi^2 - 4\pi\theta + \theta^2)} \left( -\pi r^2 (-16\pi^2 + 16\pi\theta - 4\theta^2) - \sqrt{\pi^2 r^4 (-16\pi^2 + 16\pi\theta - 4\theta^2)^2 - 16\pi^2 r^2 (4\pi^2 - 4\pi\theta + \theta^2) \left( \left( \frac{2\pi r - r\theta}{2\pi} \right)^2 (4\pi - \theta_1) \theta_1 \right)} \right), \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}, \{\theta_1, -2\pi, 2\pi\} \right]$$



$$r := \frac{2\pi \sqrt{(4\pi - \theta) \theta}}{(4\pi - \theta) \theta}$$

$$\text{Solve}\left[\frac{1}{2 r^2 (4 \pi^2 - 4 \pi \theta + \theta^2)} \left( -\pi r^2 (-16 \pi^2 + 16 \pi \theta - 4 \theta^2) - \sqrt{\left( \pi^2 r^4 (-16 \pi^2 + 16 \pi \theta - 4 \theta^2)^2 - 16 \pi^2 r^2 \right.} \right. \right. \\ \left. \left. \left( 4 \pi^2 - 4 \pi 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) + \theta^2 \right) \left( \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^2 (4 \pi - \theta_1) \theta_1 \right) \right) = \theta_1, \theta_1 \right]$$

$$\{\{\theta_1 \rightarrow 0\}, \{\theta_1 \rightarrow 4 \pi\}\}$$

$$\text{Solve}\left[\frac{1}{2 r^2 (4 \pi^2 - 4 \pi \theta + \theta^2)} \left( -\pi r^2 (-16 \pi^2 + 16 \pi \theta - 4 \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) \right)^2) - \right. \right. \\ \left. \left. \sqrt{\left( \pi^2 r^4 (-16 \pi^2 + 16 \pi \theta - 4 \theta^2)^2 - 16 \pi^2 r^2 \left( 4 \pi^2 - 4 \pi 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \text{Sin}[\beta]^2} \right) + \theta^2 \right) \right.} \right. \right. \\ \left. \left. \left( \left( \frac{2 \pi r - r \theta}{2 \pi} \right)^2 (4 \pi - \theta_1) \theta_1 \right) \right) = \theta_1, \theta_1 \right]$$

$$\{\{\theta_1 \rightarrow$$

$$\frac{1}{2 (-4 \pi^2 + 4 \pi \theta - \theta^2)} \left( -24 \pi^3 + 20 \pi^2 \theta - 2 \pi \theta^2 - \theta^3 - 8 \pi^3 \sqrt{1 - \text{Sin}[\beta]^2} + 8 \pi^2 \theta \sqrt{1 - \text{Sin}[\beta]^2} - \right. \\ \left. 2 \pi \theta^2 \sqrt{1 - \text{Sin}[\beta]^2} - \sqrt{\left( (24 \pi^3 - 20 \pi^2 \theta + 2 \pi \theta^2 + \theta^3 + 8 \pi^3 \sqrt{1 - \text{Sin}[\beta]^2} - \right.} \right. \\ \left. \left. 8 \pi^2 \theta \sqrt{1 - \text{Sin}[\beta]^2} + 2 \pi \theta^2 \sqrt{1 - \text{Sin}[\beta]^2} \right)^2 - 4 (-4 \pi^2 + 4 \pi \theta - \theta^2)} \right. \\ \left. (-48 \pi^4 + 6 \pi^2 \theta^2 - \pi \theta^3 + 24 \pi^4 \text{Sin}[\beta]^2 + 4 \pi^3 \theta \text{Sin}[\beta]^2 - 48 \pi^4 \sqrt{1 - \text{Sin}[\beta]^2} + \right. \\ \left. 8 \pi^3 \theta \sqrt{1 - \text{Sin}[\beta]^2} - 2 \pi^2 \theta^2 \sqrt{1 - \text{Sin}[\beta]^2} + 8 \pi^4 \text{Sin}[\beta]^2 \sqrt{1 - \text{Sin}[\beta]^2} \right) \left. \right) \left. \right\},$$

$$\left\{ \theta_1 \rightarrow \frac{1}{2 (-4 \pi^2 + 4 \pi \theta - \theta^2)} \left( -24 \pi^3 + 20 \pi^2 \theta - 2 \pi \theta^2 - \theta^3 - 8 \pi^3 \sqrt{1 - \text{Sin}[\beta]^2} + \right. \right. \\ \left. \left. 8 \pi^2 \theta \sqrt{1 - \text{Sin}[\beta]^2} - 2 \pi \theta^2 \sqrt{1 - \text{Sin}[\beta]^2} + \right. \right. \\ \left. \left. \sqrt{\left( (24 \pi^3 - 20 \pi^2 \theta + 2 \pi \theta^2 + \theta^3 + 8 \pi^3 \sqrt{1 - \text{Sin}[\beta]^2} - \right.} \right. \right. \\ \left. \left. \left. 8 \pi^2 \theta \sqrt{1 - \text{Sin}[\beta]^2} + 2 \pi \theta^2 \sqrt{1 - \text{Sin}[\beta]^2} \right)^2 - 4 (-4 \pi^2 + 4 \pi \theta - \theta^2)} \right. \right. \\ \left. \left. (-48 \pi^4 + 6 \pi^2 \theta^2 - \pi \theta^3 + 24 \pi^4 \text{Sin}[\beta]^2 + 4 \pi^3 \theta \text{Sin}[\beta]^2 - 48 \pi^4 \sqrt{1 - \text{Sin}[\beta]^2} + \right. \right. \\ \left. \left. 8 \pi^3 \theta \sqrt{1 - \text{Sin}[\beta]^2} - 2 \pi^2 \theta^2 \sqrt{1 - \text{Sin}[\beta]^2} + 8 \pi^4 \text{Sin}[\beta]^2 \sqrt{1 - \text{Sin}[\beta]^2} \right) \right. \left. \right) \left. \right\}$$

SphericalPlot3D[  

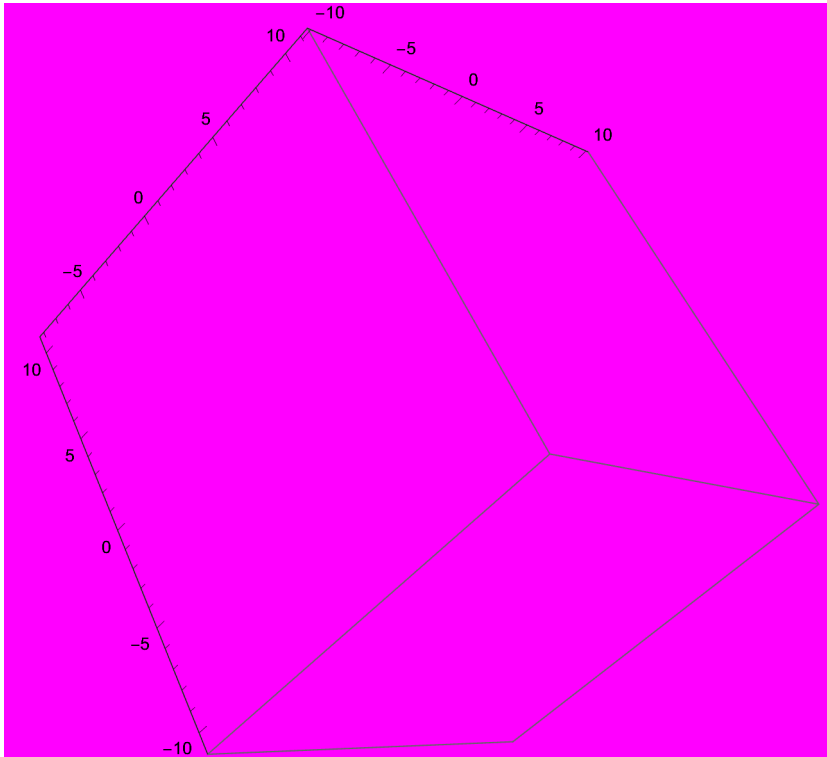
$$\frac{1}{2(-4\pi^2 + 4\pi\theta - \theta^2)} \left( -24\pi^3 + 20\pi^2\theta - 2\pi\theta^2 - \theta^3 - 8\pi^3\sqrt{1 - \sin[\beta]^2} + 8\pi^2\theta\sqrt{1 - \sin[\beta]^2} - \right.$$

$$2\pi\theta^2\sqrt{1 - \sin[\beta]^2} + \sqrt{\left( (24\pi^3 - 20\pi^2\theta + 2\pi\theta^2 + \theta^3 + 8\pi^3\sqrt{1 - \sin[\beta]^2} - \right.$$

$$8\pi^2\theta\sqrt{1 - \sin[\beta]^2} + 2\pi\theta^2\sqrt{1 - \sin[\beta]^2})^2 - 4(-4\pi^2 + 4\pi\theta - \theta^2)}$$

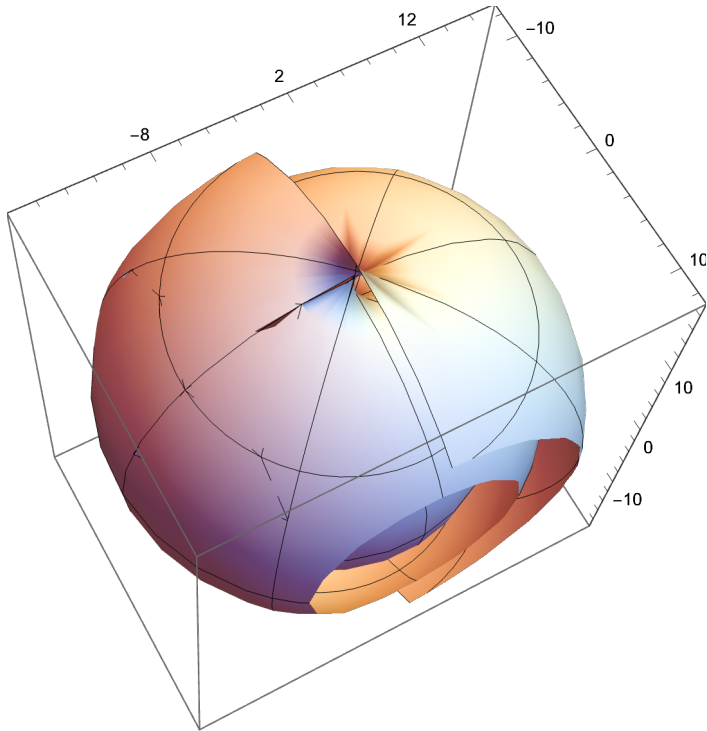
$$\left( -48\pi^4 + 6\pi^2\theta^2 - \pi\theta^3 + 24\pi^4\sin[\beta]^2 + 4\pi^3\theta\sin[\beta]^2 - 48\pi^4\sqrt{1 - \sin[\beta]^2} + \right.$$

$$8\pi^3\theta\sqrt{1 - \sin[\beta]^2} - 2\pi^2\theta^2\sqrt{1 - \sin[\beta]^2} + 8\pi^4\sin[\beta]^2\sqrt{1 - \sin[\beta]^2} \left. \right) \left. \right)},$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi, \pi\}, \text{PlotStyle} \rightarrow \text{Opacity}[\.5]$

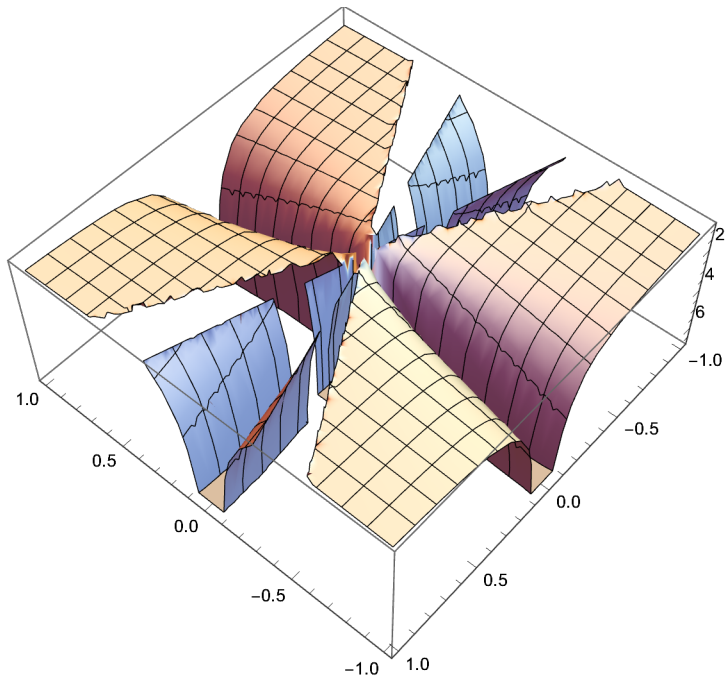


$$2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)$$

$\text{SphericalPlot3D}\left[\frac{1}{2 r^2 (4 \pi^2 - 4 \pi \theta + \theta^2)}\right.$   
 $\left.(-\pi r^2 (-16 \pi^2 + 16 \pi \theta - 4 \theta^2) - \sqrt{\left(\pi^2 r^4 (-16 \pi^2 + 16 \pi \theta - 4 \theta^2)^2 - 16 \pi^2 r^2 (4 \pi^2 - 4 \pi \theta + \theta^2)\right.}\right.$   
 $\left.\left.\left(\left(\frac{2 \pi r - r \theta}{2 \pi}\right)^2\right) (4 \pi - \theta_1) \theta_1\right)\right], \{\theta, -2 \pi, 2 \pi\}, \{\theta_1, -2 \pi, 2 \pi\}]$



$$\begin{aligned}
& \text{Plot3D}\left[1/\left(\left(4\pi - \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} - \right.\right. \\
& \quad \left.\left.\frac{2\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}\right)\right) \\
& \quad \left(\frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} - \right. \\
& \quad \left.\frac{2\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}\right) \times 2\pi \\
& \quad \sqrt{\left(\left(4\pi - \frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} - \right.\right. \\
& \quad \left.\left.\frac{2\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}\right)\right) \\
& \quad \left(\frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} - \right. \\
& \quad \left.\frac{2\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}\right) \Bigg], \{r, -1, 1\}, \{\eta, -1, 1\}]
\end{aligned}$$



SphericalPlot3D[1/

$$\left( 4 \pi - \left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right. \right.$$

$$\left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right)$$

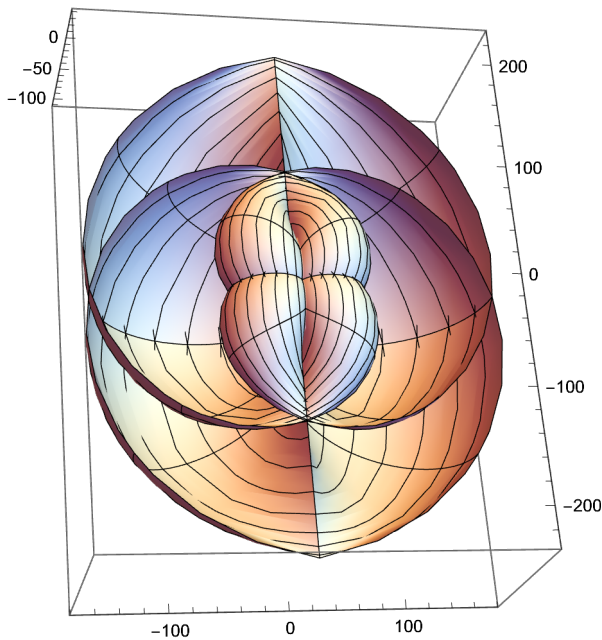
$$\left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right.$$

$$\left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) 2 \pi \sqrt{\left( 4 \pi - \right.$$

$$\left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right.$$

$$\left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)$$

( $\theta$ ), { $\theta$ ,  $-2 \pi$ ,  $2 \pi$ }, { $\beta$ ,  $-\pi / 2$ ,  $\pi / 2$ }]



RevolutionPlot3D[1/

$$\left( 4 \pi - \left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right)$$

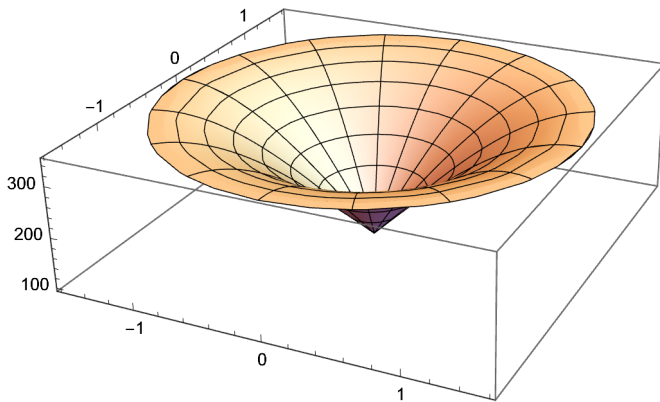
$$\left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) 2 \pi \sqrt{\left( 4 \pi - \left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right)}$$

$$\left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)$$

$$\left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right)$$

$$\left( \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right), \{\beta, -\pi /$$

$$2, \pi / 2\}$$





$$\begin{aligned}
 & 1 / \left( \left( 4 \pi - \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right. \right. \\
 & \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \frac{4 \pi}{3} - \right. \\
 & \quad \left. \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right. \\
 & \quad \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \times 2 \pi \\
 & \sqrt{\left( \left( 4 \pi - \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \right. \right. \\
 & \quad \left. \left. \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \theta \right)}
 \end{aligned}$$

$$r \rightarrow \frac{2 \pi \sqrt{(4 \pi - 2 \pi) 2 \pi}}{(4 \pi - 2 \pi) 2 \pi}$$

$$\text{Solve}\left[\frac{\left(1 + \frac{3}{\frac{2 \pi \sqrt{(4 \pi - (2/3) \pi) (2/3) \pi}}{(4 \pi - (2/3) \pi) (2/3) \pi}}}\right)}{2} == \phi, x\right]$$

{}

$$\frac{\left(1 + \frac{3}{\frac{2 \pi \sqrt{(4 \pi - (2/3) \pi) (2/3) \pi}}{(4 \pi - (2/3) \pi) (2/3) \pi}}}\right)}{2} = \phi$$

$$\frac{1}{2} (1 + \sqrt{5})$$

$$r = \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} == \frac{3}{\sqrt{5}} \text{ at } \theta = (2/3) \pi, \text{ therefore,}$$

$$\text{in the case of } \frac{(1 + \sqrt{5})}{2}, \sqrt{5} == \frac{3}{\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}}$$

$$\frac{3}{\sqrt{5}} = \frac{2 \pi \sqrt{(4 \pi - (2/3) \pi) (2/3) \pi}}{(4 \pi - (2/3) \pi) (2/3) \pi}$$

$$\sqrt{5} = \frac{3}{\frac{2\pi \sqrt{(4\pi - (2/3)\pi) (2/3)\pi}}{(4\pi - (2/3)\pi) (2/3)\pi}} = \frac{3}{r}$$

$$\frac{(1 + \sqrt{5})}{2} == \frac{\left(\frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{3}{r}\right)}{2}$$

$$\text{Solve}\left[y == \frac{3}{\frac{2\pi \sqrt{(4x - (2/3)x) (2/3)x}}{(4\pi - (2/3)x) (2/3)x}}, x\right]$$

$$\{\{x \rightarrow 6\pi - \sqrt{5}\pi y\}, \{x \rightarrow 6\pi + \sqrt{5}\pi y\}\}$$

$$\pi = 6\pi + \sqrt{5}\pi\sqrt{5}$$

$$\text{Solve}\left[y == \frac{3}{\frac{2x \sqrt{(4x - (2/3)x) (2/3)x}}{(4x - (2/3)x) (2/3)x}}, x\right]$$

$$\{\}$$

$$\text{Solve}\left[\sqrt{5} == \frac{3}{\frac{2\pi \sqrt{(4x - (2/3)x) (2/3)x}}{(4\pi - (2/3)x) (2/3)x}}, x\right]$$

$$\{\{x \rightarrow \pi\}\}$$

$$\frac{(1 + \sqrt{5})}{2} == \pi \left(3 + \sqrt{9 - \pi^2}\right)$$

$$\text{N}\left[\pi \left(3 + \sqrt{9 - \pi^2}\right)\right]$$

$$9.42478 + 2.92962 i$$

$$\text{Solve}\left[\frac{(1 + \sqrt{5})}{2} == \frac{\left(\frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{3}{r}\right)}{2 \frac{2\pi r \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\sqrt{\frac{3}{2\pi}} ((4\pi - \theta)\theta)^{1/4} \sqrt{\text{Csc}[\beta]}}{5^{1/4}}\right\}, \left\{r \rightarrow \frac{\sqrt{\frac{3}{2\pi}} ((4\pi - \theta)\theta)^{1/4} \sqrt{\text{Csc}[\beta]}}{5^{1/4}}\right\}\right\}$$

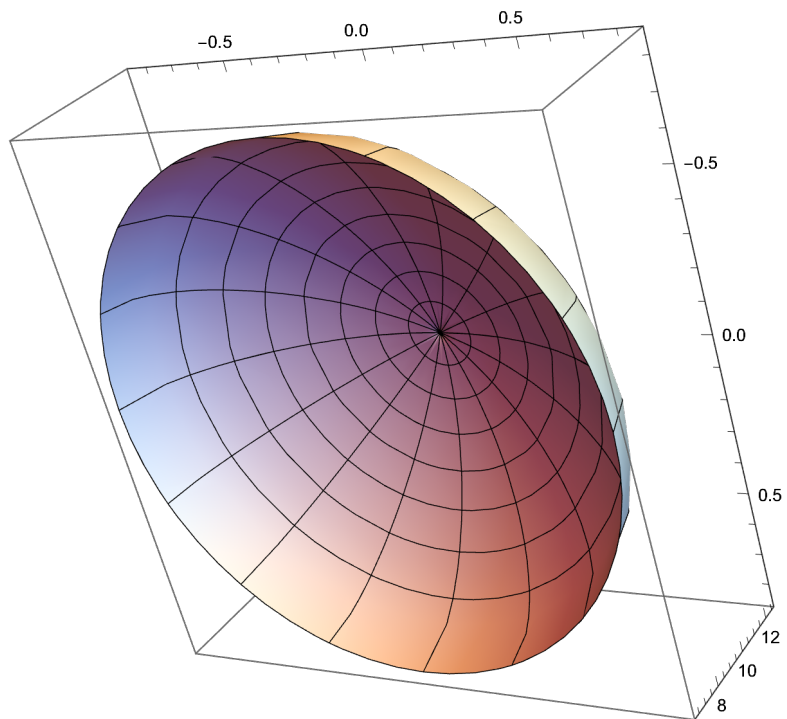
$$\text{Solve}\left[\frac{\sqrt{\frac{3}{2\pi}} ((4\pi - \theta)\theta)^{1/4} \sqrt{\text{Csc}[\beta]}}{5^{1/4}} == \frac{2\pi \sqrt{(4\pi - (2/3)\pi) (2/3)\pi}}{(4\pi - (2/3)\pi) (2/3)\pi}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2}{5} \left(5\pi - \sqrt{5} \sqrt{5\pi^2 - 9\pi^2 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow \frac{2}{5} \left(5\pi + \sqrt{5} \sqrt{5\pi^2 - 9\pi^2 \sin[\beta]^2}\right)\right\}\right\}$$

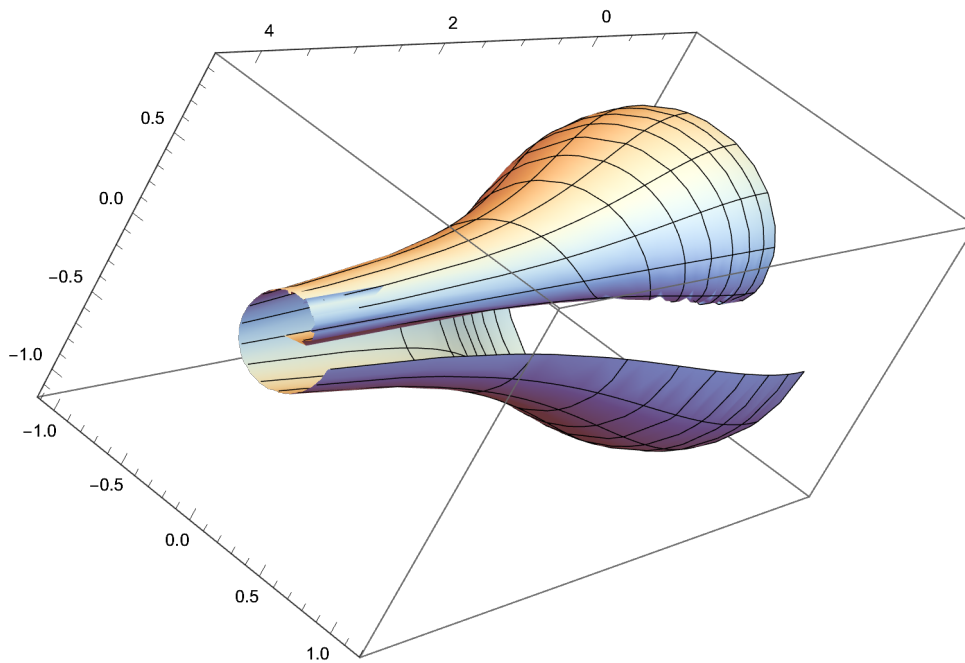
$$\text{Solve}\left[2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) == \frac{2}{5} \left(5\pi + \sqrt{5} \sqrt{5\pi^2 - 9\pi^2 \sin[\beta]^2}\right), \beta\right]$$

$$\{\{\beta \rightarrow 0\}\}$$

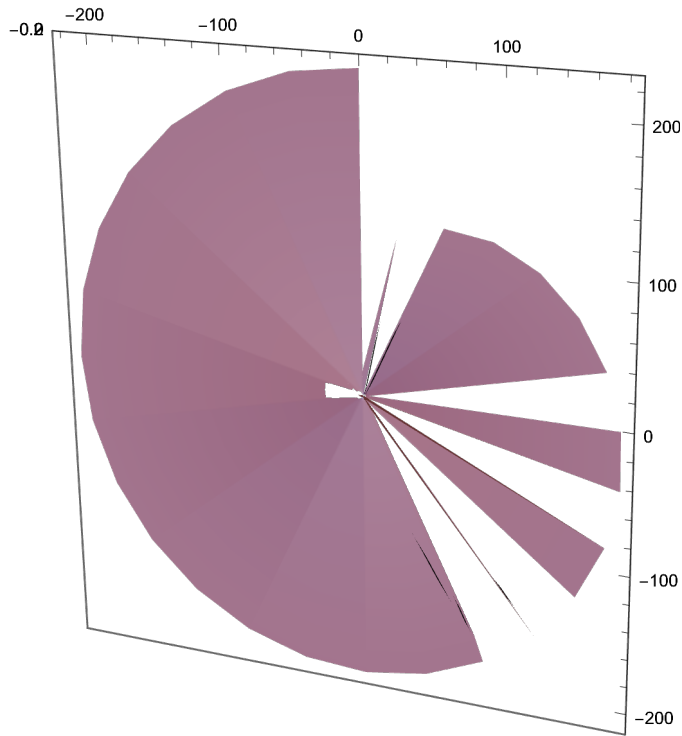
$\text{RevolutionPlot3D}\left[\frac{2}{5}\left(5\pi + \sqrt{5}\sqrt{5\pi^2 - 9\pi^2\sin[\beta]^2}\right), \{\beta, -\pi/2, \pi/2\}\right]$



$\text{SphericalPlot3D}\left[\frac{\sqrt{\frac{3}{2\pi}}((4\pi - \theta)\theta)^{1/4}\sqrt{\text{Csc}[\beta]}}{5^{1/4}}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



$$\text{SphericalPlot3D}\left[\frac{\sqrt{\frac{3}{2\pi}} ((4\pi - \theta)\theta)^{1/4} \sqrt{\text{Csc}[\beta]}}{5^{1/4}}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$$

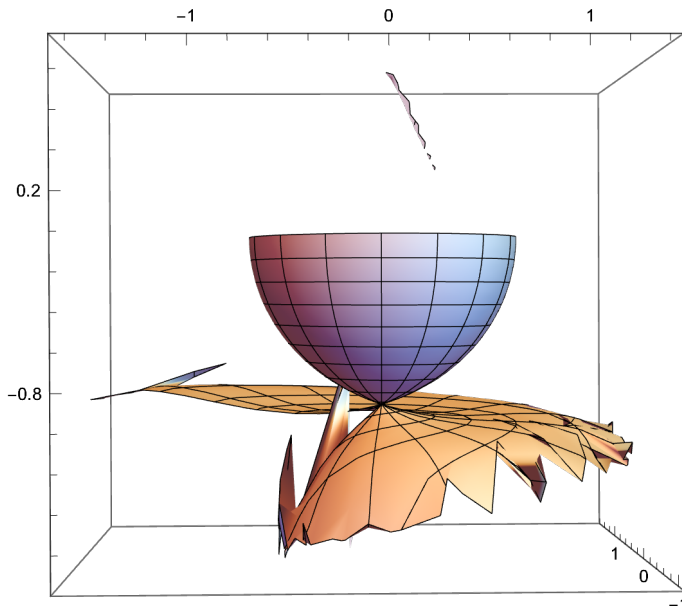


$$\text{Solve}\left[\frac{(1 + \sqrt{5})}{2} = \frac{\left(\frac{2\pi r \text{Sin}[\beta]}{\sqrt{4\pi\theta - \theta^2}} + \frac{3}{r}\right)}{2}, r\right]$$

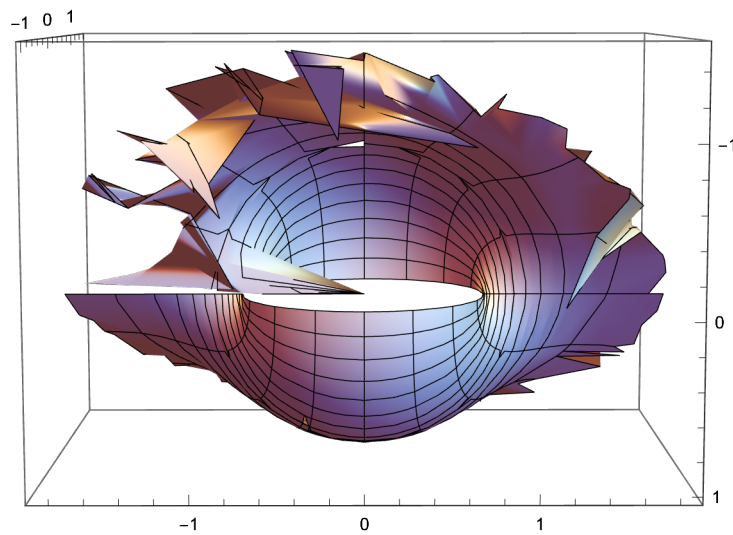
$$\left\{\left\{r \rightarrow -\frac{1}{4\pi} \text{Csc}[\beta] \left(-\sqrt{(4\pi - \theta)\theta} - \sqrt{5} \sqrt{(4\pi - \theta)\theta} - \sqrt{6(4\pi - \theta)\theta + 2\sqrt{5}(4\pi - \theta)\theta - 24\pi\sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]}\right)\right\}, \right.$$

$$\left.\left\{r \rightarrow -\frac{1}{4\pi} \text{Csc}[\beta] \left(-\sqrt{(4\pi - \theta)\theta} - \sqrt{5} \sqrt{(4\pi - \theta)\theta} + \sqrt{6(4\pi - \theta)\theta + 2\sqrt{5}(4\pi - \theta)\theta - 24\pi\sqrt{(4\pi - \theta)\theta} \text{Sin}[\beta]}\right)\right\}\right\}$$

SphericalPlot3D $\left[\frac{1}{4\pi}\text{Csc}[\beta]\left(-\sqrt{(4\pi-\theta)\theta}-\sqrt{5}\sqrt{(4\pi-\theta)\theta}+\sqrt{6(4\pi-\theta)\theta+2\sqrt{5}(4\pi-\theta)\theta-24\pi\sqrt{(4\pi-\theta)\theta}\text{Sin}[\beta]}\right),\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$



SphericalPlot3D $\left[\frac{1}{4\pi}\text{Csc}[\beta]\left(-\sqrt{(4\pi-\theta)\theta}-\sqrt{5}\sqrt{(4\pi-\theta)\theta}+\sqrt{6(4\pi-\theta)\theta+2\sqrt{5}(4\pi-\theta)\theta-24\pi\sqrt{(4\pi-\theta)\theta}\text{Sin}[\beta]}\right),\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$



$$\text{Solve}\left[\frac{(1 + \sqrt{5})}{2} == \frac{\left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} + \frac{3}{r}\right)}{2 \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow \text{ArcCsc}\left[\frac{2 \sqrt{5} \pi r^2 \sqrt{(4 \pi - \theta) \theta}}{3 (4 \pi \theta - \theta^2)}\right]\right\}\right\}$$

$$\text{Solve}\left[\frac{(1 + \sqrt{5})}{2} == \frac{\left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} + \frac{3}{r}\right)}{2}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow \text{ArcSin}\left[\frac{-\frac{3 \sqrt{(4 \pi - \theta) \theta}}{r^2} + \frac{\sqrt{(4 \pi - \theta) \theta}}{r} + \frac{\sqrt{5} \sqrt{(4 \pi - \theta) \theta}}{r}}{2 \pi}\right]\right\}\right\}$$

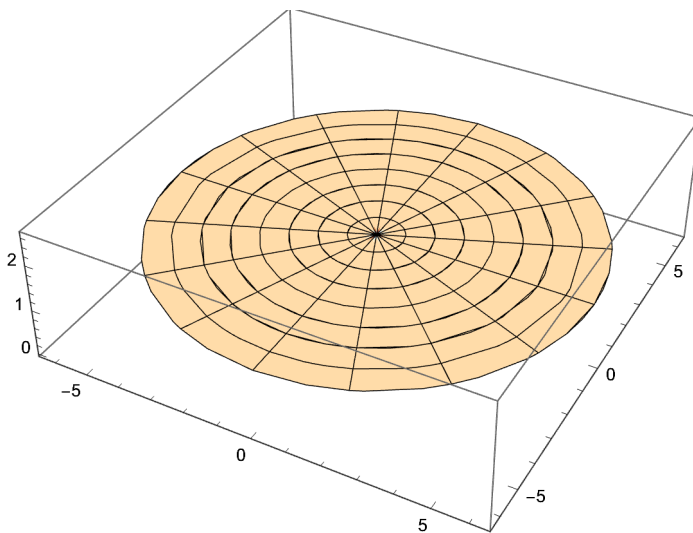
$$\text{Solve}\left[\text{ArcCsc}\left[\frac{2 \sqrt{5} \pi r^2 \sqrt{(4 \pi - \theta) \theta}}{3 (4 \pi \theta - \theta^2)}\right] == \text{ArcSin}\left[\frac{-\frac{3 \sqrt{(4 \pi - \theta) \theta}}{r^2} + \frac{\sqrt{(4 \pi - \theta) \theta}}{r} + \frac{\sqrt{5} \sqrt{(4 \pi - \theta) \theta}}{r}}{2 \pi}\right], r\right]$$

$$\left\{\left\{r \rightarrow -\frac{12 \pi}{\sqrt{5} (-4 \pi + \theta)} + \frac{3 \theta}{\sqrt{5} (-4 \pi + \theta)}\right\}\right\}$$

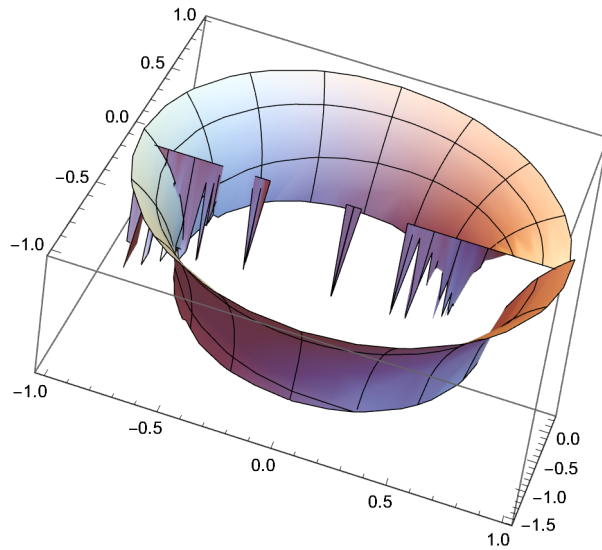
$$\text{Solve}\left[\frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta} == -\frac{12 \pi}{\sqrt{5} (-4 \pi + \theta)} + \frac{3 \theta}{\sqrt{5} (-4 \pi + \theta)}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2 \pi}{3}\right\}, \left\{\theta \rightarrow \frac{10 \pi}{3}\right\}\right\}$$

$$\text{RevolutionPlot3D}\left[-\frac{12 \pi}{\sqrt{5} (-4 \pi + \theta)} + \frac{3 \theta}{\sqrt{5} (-4 \pi + \theta)}, \{\theta, -2 \pi, 2 \pi\}\right]$$



RevolutionPlot3D[  
ArcSin[ $\frac{-\frac{3\sqrt{(4\pi-\theta)\theta}}{r^2} + \frac{\sqrt{(4\pi-\theta)\theta}}{r} + \frac{\sqrt{5}\sqrt{(4\pi-\theta)\theta}}{r}}{2\pi}$ ], {r, -1, 1}, {θ, -2π, 2π}]



Solve[ $\frac{2\pi\sqrt{(4\pi-(2/3)x)(2/3)x}}{(4\pi-(2/3)x)(2/3)x} == \frac{3}{\sqrt{5}}, x]$

{{x → π}, {x → 5π}}

$$\frac{2\pi\sqrt{(4\pi-\pi)\pi}}{(4\pi-\pi)\pi}$$

$$\frac{2}{\sqrt{3}}$$

$$\frac{2\pi\sqrt{(4\pi-(3/2)\pi)(3/2)\pi}}{(4\pi-(3/2)\pi)(3/2)\pi}$$

$$\frac{4}{\sqrt{15}}$$

$$\frac{2\pi\sqrt{(4\pi-2\pi)2\pi}}{(4\pi-2\pi)2\pi}$$

1

$$\frac{2\pi\sqrt{(4\pi-4\pi)4\pi}}{(4\pi-4\pi)4\pi}$$

Indeterminate

$$\frac{2 \pi \sqrt{(4 \pi - 5 \pi) 5 \pi}}{(4 \pi - 5 \pi) 5 \pi}$$

$$-\frac{2 i}{\sqrt{5}}$$

$$r \rightarrow \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$r \rightarrow$$

$$r \rightarrow \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$r \rightarrow \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$r \rightarrow \frac{2 \pi \sqrt{(4 \pi - \theta) \theta}}{(4 \pi - \theta) \theta}$$

$$2 \pi$$

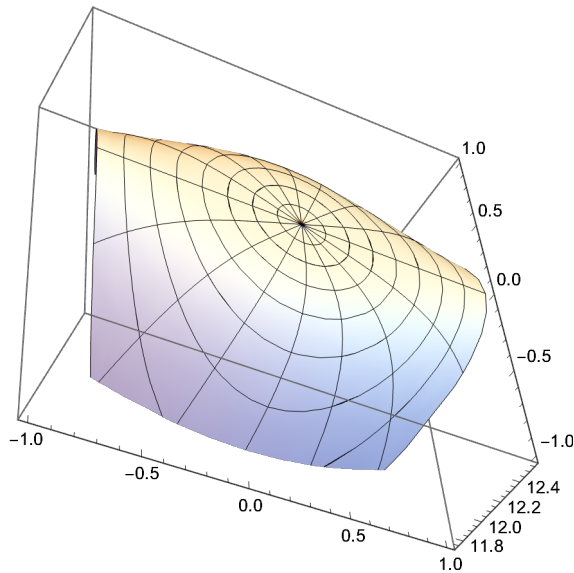
$$\text{Solve}\left[\frac{(1 + \sqrt{5})}{2} = \frac{\left(\frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}} + \frac{3}{r}\right)}{2 \frac{2 \pi r \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \frac{2}{3} \left(3 \pi - \sqrt{9 \pi^2 - 5 \pi^2 r^4 \sin[\beta]^2}\right)\right\}, \left\{\theta \rightarrow \frac{2}{3} \left(3 \pi + \sqrt{9 \pi^2 - 5 \pi^2 r^4 \sin[\beta]^2}\right)\right\}\right\}$$

$$\frac{2}{3} \left(3 \pi + \sqrt{9 \pi^2 - 5 \pi^2 r^4 \sin[\beta]^2}\right) ==$$



RevolutionPlot3D $\left[\frac{2}{3} \left(3 \pi + \sqrt{9 \pi^2 - 5 \pi^2 r^4 \sin[\beta]^2}\right), \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$



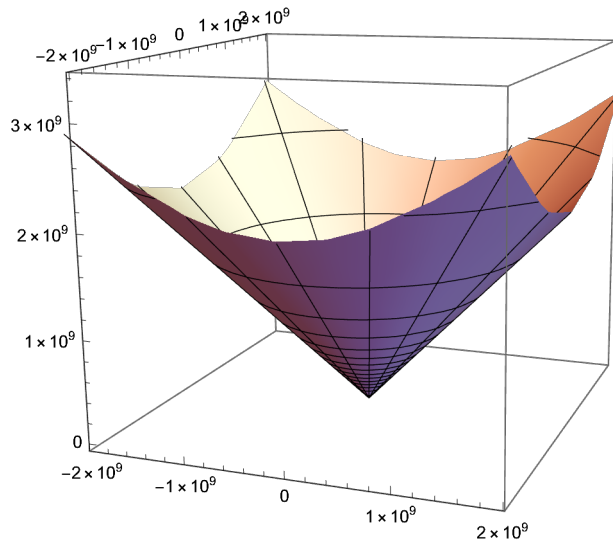
Solve $\left[\left(\sqrt{-1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \theta^{16} + 3.5481432270250993 \cdot \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r\right]$

$\left\{\left\{r \rightarrow -\frac{1. \sqrt{6.91664 \times 10^{33} - 5.50409 \times 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.41771 \times 10^{17} - 7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2}}\right\}, \left\{r \rightarrow \frac{\sqrt{6.91664 \times 10^{33} - 5.50409 \times 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.41771 \times 10^{17} - 7.6958 \times 10^{16} \theta + 6.12412 \times 10^{15} \theta^2}}\right\}\right\}$

RevolutionPlot3D[  

$$\left\{ -\frac{1. \sqrt{6.916640561054567 \cdot 10^{33} - 5.504087674408674 \cdot 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.4177070339300032 \cdot 10^{17} - 7.695800507960096 \cdot 10^{16} \theta + 6.124123459454841 \cdot 10^{15} \theta^2}}, \right.$$
  

$$\left. \frac{\sqrt{6.916640561054567 \cdot 10^{33} - 5.504087674408674 \cdot 10^{32} \theta} \sqrt{\theta}}{\sqrt{2.4177070339300032 \cdot 10^{17} - 7.695800507960096 \cdot 10^{16} \theta + 6.124123459454841 \cdot 10^{15} \theta^2}} \right\},$$
  
 $\{\theta, -2\pi, 2\pi\}]$



Solve[  

$$\left( \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2} \right) /$$
  

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) ==$$
  

$$\frac{4\pi r^2 - 2r^2 \theta}{2\sqrt{4\pi r^2 \theta - r^2 \theta^2}}, \beta]$$
  

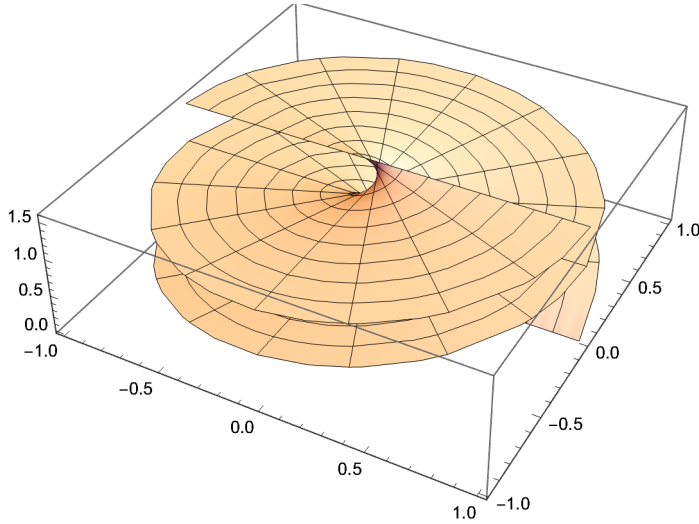
$$\left\{ \left\{ \beta \rightarrow -1. \text{ArcSin} \left[ \frac{\left( \sqrt{\theta} \sqrt{1.08487 \times 10^{33} r^2 - 3.10363 \times 10^{49} \theta - 4.31657 \times 10^{32} r^2 \theta + 4.93958 \times 10^{48} \theta^2 + 5.49602 \times 10^{31} r^2 \theta^2 - 1.9654 \times 10^{47} \theta^3 - 2.1868 \times 10^{30} r^2 \theta^3} \right)}{\left( \sqrt{3.40822 \times 10^{33} r^2 - 9.75034 \times 10^{49} \theta - 1.08487 \times 10^{33} r^2 \theta + 7.75907 \times 10^{48} \theta^2 + 8.63313 \times 10^{31} r^2 \theta^2} \right)} \right] \right\},$$
  

$$\left\{ \beta \rightarrow \text{ArcSin} \left[ \frac{\left( \sqrt{\theta} \sqrt{1.08487 \times 10^{33} r^2 - 3.10363 \times 10^{49} \theta - 4.31657 \times 10^{32} r^2 \theta + 4.93958 \times 10^{48} \theta^2 + 5.49602 \times 10^{31} r^2 \theta^2 - 1.9654 \times 10^{47} \theta^3 - 2.1868 \times 10^{30} r^2 \theta^3} \right)}{\left( \sqrt{3.40822 \times 10^{33} r^2 - 9.75034 \times 10^{49} \theta - 1.08487 \times 10^{33} r^2 \theta + 7.75907 \times 10^{48} \theta^2 + 8.63313 \times 10^{31} r^2 \theta^2} \right)} \right] \right\} \right\}$$

```

RevolutionPlot3D[ArcSin[( $\sqrt{\theta} \sqrt{(1.0848712769677502 \cdot r^2 - 3.10362859208832 \cdot \theta - 4.3165656586958524 \cdot r^2 \theta + 4.9395783195219584 \cdot \theta^2 + 5.496022094097345 \cdot r^2 \theta^2 - 1.965395765853693 \cdot \theta^3 - 2.186797709044656 \cdot r^2 \theta^3)}$ )] /
( $\sqrt{(3.4082236338124617 \cdot r^2 - 9.7503367843759 \cdot \theta - 1.0848712769677502 \cdot r^2 \theta + 7.7590714802208 \cdot \theta^2 + 8.633131317391704 \cdot r^2 \theta^2)}$ )], {r, -1, 1}, { $\theta$ , -2  $\pi$ , 2  $\pi$ }]

```

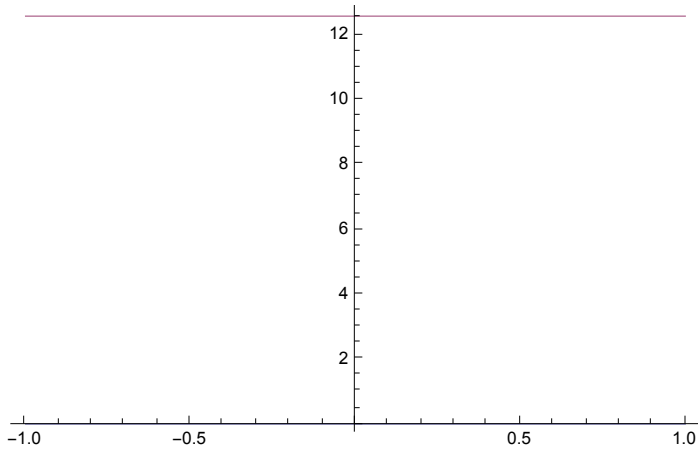


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Solve[( $\sqrt{(-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)}$ )] /
( $\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}$ ) ==
 $\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, \theta]$ 
{ $\theta \rightarrow \frac{0.5 (6.91664 \times 10^{33} + 7.6958 \times 10^{16} r^2 - 2.30714 \times 10^{25} \sqrt{8.98755 \times 10^{16} + 1. r^2})}{5.50409 \times 10^{32} + 6.12412 \times 10^{15} r^2}$ },
{ $\theta \rightarrow \frac{0.5 (6.91664 \times 10^{33} + 7.6958 \times 10^{16} r^2 + 2.30714 \times 10^{25} \sqrt{8.98755 \times 10^{16} + 1. r^2})}{5.50409 \times 10^{32} + 6.12412 \times 10^{15} r^2}$ }}

```

$\text{Plot}\left[\left\{\left(0.5 \cdot \left(6.916640561054567 \cdot r^{33} + 7.695800507960096 \cdot r^{16} - \right.\right.\right.$   
 $\left.\left.2.3071429505590057 \cdot r^{25} \sqrt{8.987551787368176 \cdot r^{16} + 1. \cdot r^2}\right)\right) /$   
 $\left(5.504087674408674 \cdot r^{32} + 6.124123459454841 \cdot r^{15}\right),$   
 $\left(0.5 \cdot \left(6.916640561054567 \cdot r^{33} + 7.695800507960096 \cdot r^{16} + \right.\right.$   
 $\left.\left.2.3071429505590057 \cdot r^{25} \sqrt{8.987551787368176 \cdot r^{16} + 1. \cdot r^2}\right)\right) /$   
 $\left(5.504087674408674 \cdot r^{32} + 6.124123459454841 \cdot r^{15}\right)\}, \{r, -1, 1\}]$

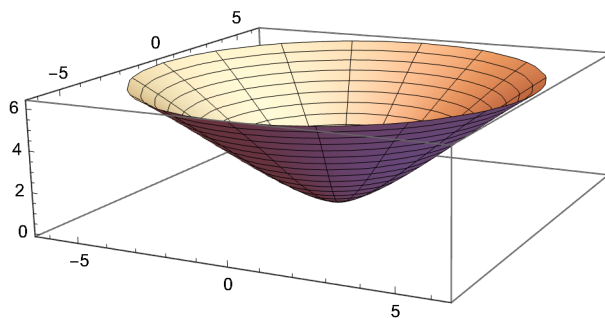


$D\left[\left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right) / (\theta / (2 \pi))\right], \theta] = D[v, v]$

$\text{Solve}\left[1 == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \theta \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{\theta^2}, r\right]$

$\left\{\left\{r \rightarrow -\frac{\sqrt{4 \pi \theta^3 - \theta^4}}{2 \pi}\right\}, \left\{r \rightarrow \frac{\sqrt{4 \pi \theta^3 - \theta^4}}{2 \pi}\right\}\right\}$

$\text{RevolutionPlot3D}\left[\frac{\sqrt{4 \pi \theta^3 - \theta^4}}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\text{Solve}\left[1 == \frac{4 \pi r^2 - 2 r^2 \theta}{2 \theta \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} - \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{\theta^2}, \theta\right]$$

$$\left\{\left\{\theta \rightarrow \pi - \frac{1}{\sqrt{2}}\right.\right.$$

$$\left.\left(\left|\left(2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}\right)\right|\right) - \right.$$

$$\frac{1}{2} \sqrt{\left(8 \pi^2 - \frac{4 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} - 2 \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3} - \right.$$

$$\left.\left.\left(8 \sqrt{2} \pi^3\right) / \left(\left|\left(2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \right.\right.\right.\right.$$

$$\left.\left.\left.\left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}\right)\right|\right)\right\}, \left\{\theta \rightarrow \pi - \frac{1}{\sqrt{2}}\right.$$

$$\left.\left(\left|\left(2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}\right)\right|\right) + \right.$$

$$\frac{1}{2} \sqrt{\left(8 \pi^2 - \frac{4 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} - 2 \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3} - \right.$$

$$\left.\left.\left(8 \sqrt{2} \pi^3\right) / \left(\left|\left(2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \right.\right.\right.\right.$$

$$\left.\left.\left.\left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}\right)\right|\right)\right\}, \left\{\theta \rightarrow \pi + \frac{1}{\sqrt{2}}\right.$$

$$\left.\left(\left|\left(2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}\right)\right|\right) - \right.$$

$$\frac{1}{2} \sqrt{\left(8 \pi^2 - \frac{4 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} - 2 \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3} + \right.$$

$$\begin{aligned}
& (8 \sqrt{2} \pi^3) / \left( \sqrt[3]{2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} +} \right. \\
& \left. \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3} \right) \Bigg\}, \left\{ \theta \rightarrow \pi + \frac{1}{\sqrt{2}} \right. \\
& \left. \left( \sqrt[3]{2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} \right) + \right. \\
& \left. \frac{1}{2} \sqrt[3]{8 \pi^2 - \frac{4 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} - 2 \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} + \right. \\
& \left. (8 \sqrt{2} \pi^3) / \left( \sqrt[3]{2 \pi^2 + \frac{2 \left(\frac{2}{3}\right)^{1/3} \pi r^2}{\left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3}} +} \right. \right. \\
& \left. \left. \left(\frac{2}{3}\right)^{2/3} \pi \left(9 \pi r^2 + \sqrt{3} \sqrt{27 \pi^2 r^4 - 4 r^6}\right)^{1/3} \right) \right) \Bigg\} \Bigg\}
\end{aligned}$$

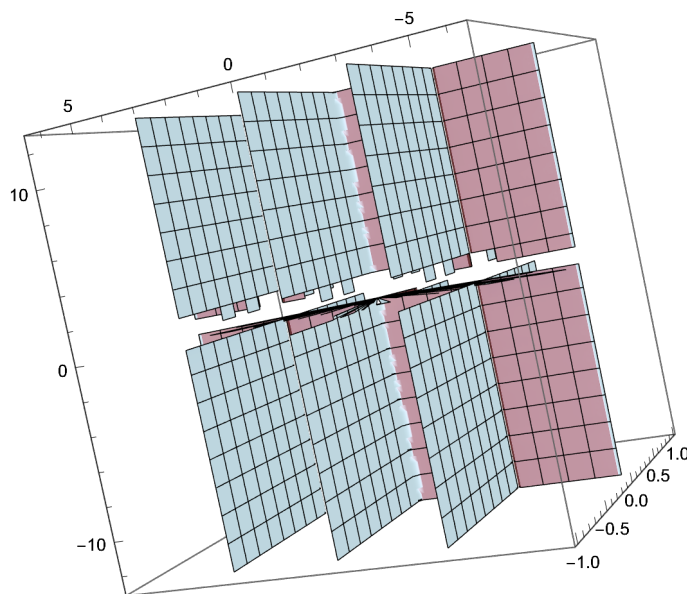
$$D\left[\left(\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}\right) / (\theta / (2 \pi))\right], \theta] = D[(r \sin[\beta]) / (\theta / (2 \pi))], \theta] = D[v, v]$$

$$D[(r \sin[\beta]) / (\theta / (2 \pi))], \theta]$$

$$-\frac{2 \pi r \sin[\beta]}{\theta^2}$$

$$-\frac{2 \pi r \sin[\beta]}{\theta^2} = 1$$

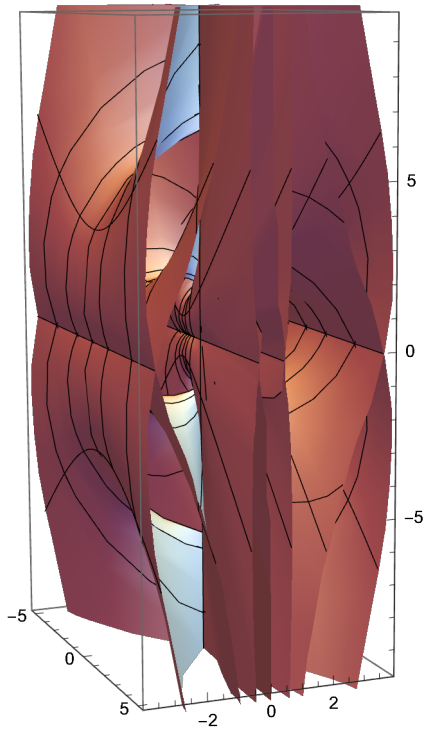
$$\text{ContourPlot3D}\left[-\frac{2 \pi r \sin[\beta]}{\theta^2}, \{r, -1, 1\}, \{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}\right]$$



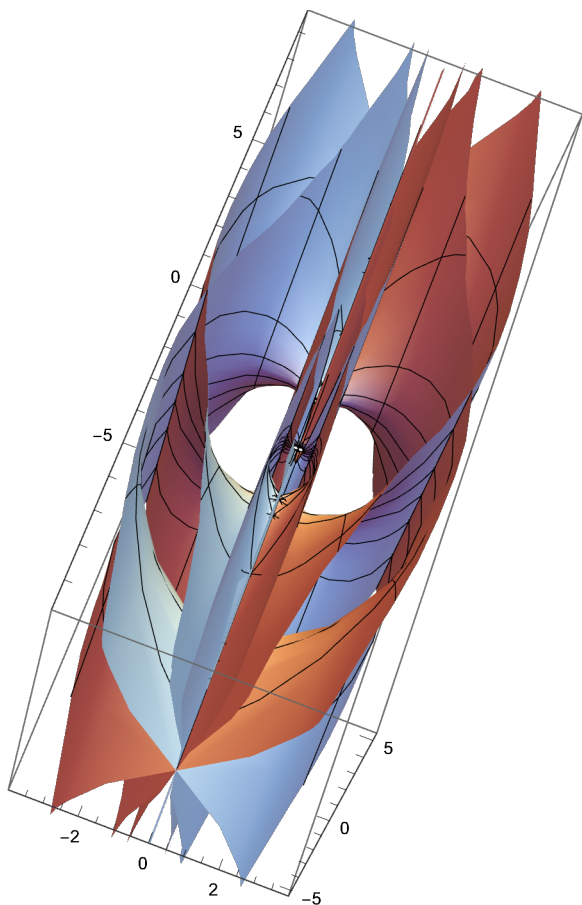
$$\text{Solve}\left[1 == -\frac{2 \pi r \sin[\beta]}{\theta^2}, r\right]$$

$$\left\{\left\{r \rightarrow -\frac{\theta^2 \csc[\beta]}{2 \pi}\right\}\right\}$$

`SphericalPlot3D` $\left[-\frac{\theta^2 \operatorname{Csc}[\beta]}{2 \pi}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi, \pi\}\right]$



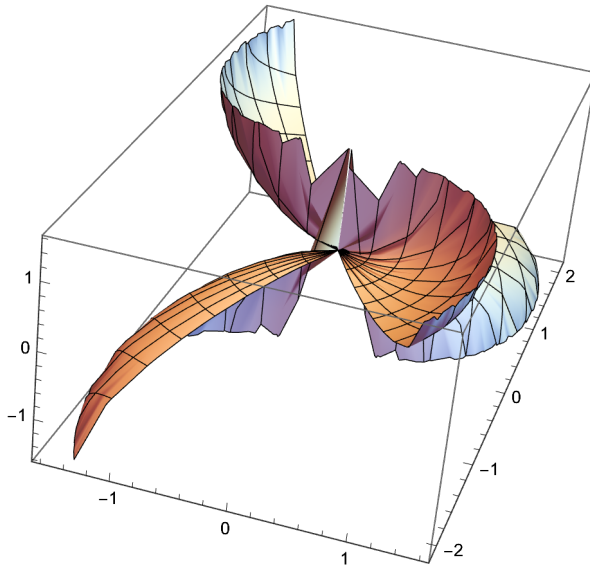




$$\text{Solve}\left[1 == -\frac{2 \pi r \sin[\beta]}{\theta^2}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\theta^2}{2 \pi r}\right]\right\}\right\}$$

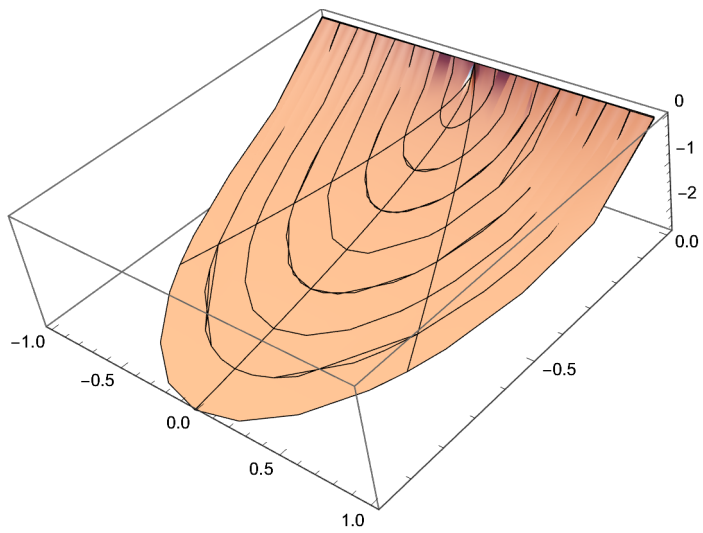
```
RevolutionPlot3D[-ArcSin[ $\frac{\theta^2}{2\pi r}$ ], { $\theta$ , -4  $\pi$ , 4  $\pi$ }, { $r$ , -1, 1}]
```



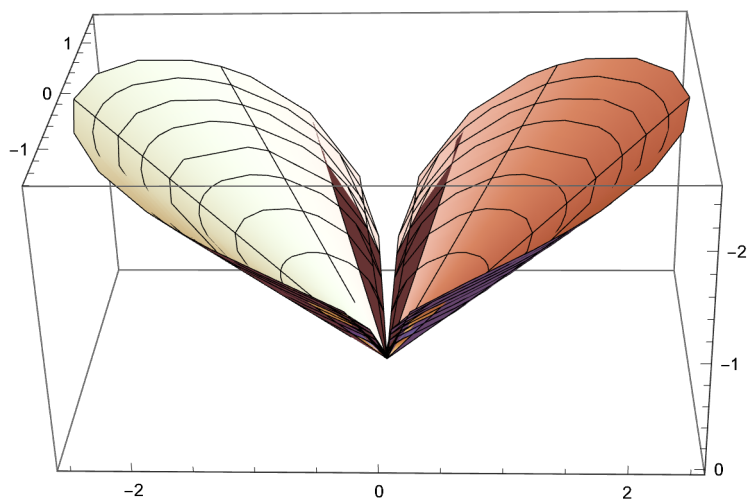
```
Solve[1 == - $\frac{2\pi r \text{Sin}[\beta]}{\theta^2}$ ,  $\theta$ ]
```

```
{ $\{\theta \rightarrow -\sqrt{2\pi} \sqrt{r} \sqrt{\text{Sin}[\beta]}\}$ ,  $\{\theta \rightarrow \sqrt{2\pi} \sqrt{r} \sqrt{\text{Sin}[\beta]}\}$ }
```

```
RevolutionPlot3D[ $\sqrt{2\pi} \sqrt{r} \sqrt{\text{Sin}[\beta]}$ , { $r$ , -1, 1}, { $\beta$ , -2  $\pi$ , 2  $\pi$ }]
```

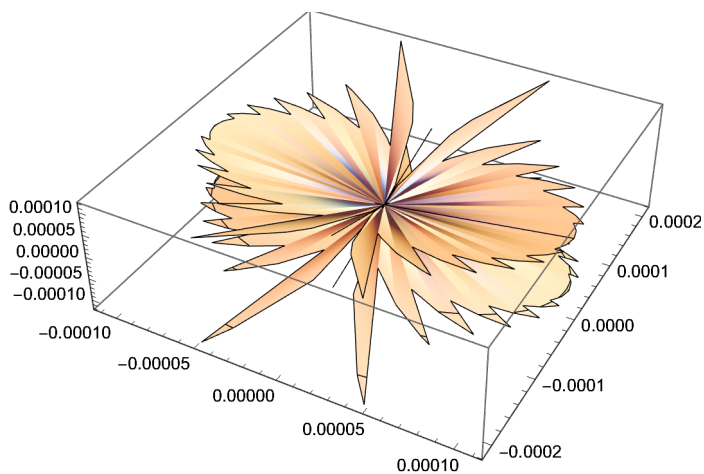


```
RevolutionPlot3D[
  {-I Sqrt[2 Pi] Sqrt[r] Sqrt[Sin[beta]], I Sqrt[2 Pi] Sqrt[r] Sqrt[Sin[beta]]}, {r, -1, 1}, {beta, -2 Pi, 2 Pi}]
```

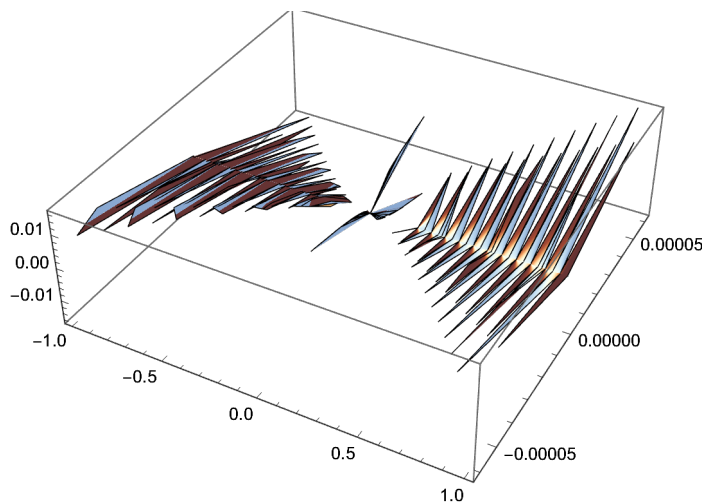


$$e^{i\theta} = i \sin[\theta] + \cos[\theta]$$

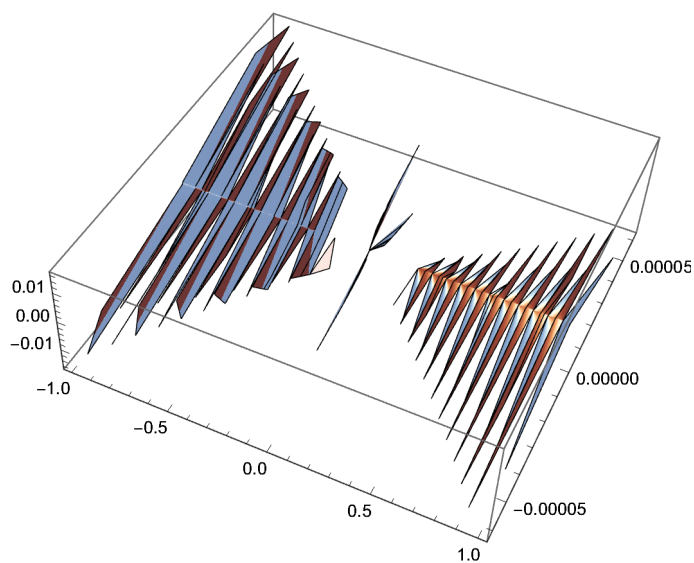
```
RevolutionPlot3D[e^i theta, {theta, -2 Pi, 2 Pi}]
```



```
RevolutionPlot3D[E^I I (-I Sqrt[2] Pi Sqrt[r] Sqrt[Sin[beta]]), {r, -1, 1}, {beta, -Pi, Pi}]
```



```
RevolutionPlot3D[E^I I (I Sqrt[2] Pi Sqrt[r] Sqrt[Sin[beta]]), {r, -1, 1}, {beta, -Pi, Pi}]
```



$$4 \pi r^2 - 4 \pi ((r_1)^2) = 4 \pi \eta^2$$

$$4 \pi r^2 - 4 \pi ((r_1)^2) =$$

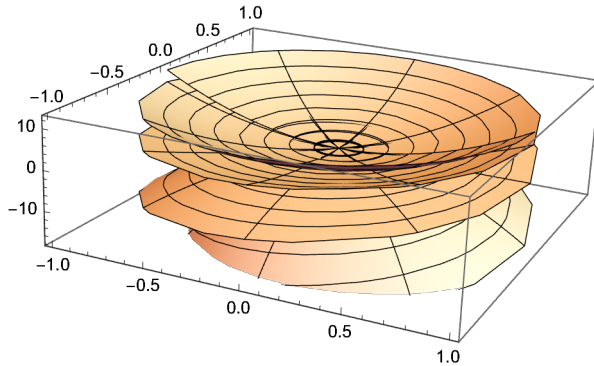
$$4 \pi r^2 - 4 \pi \left( \left( \sqrt{(r^2 - \eta^2)} \right)^2 \right) = 4 \pi \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2 = 4 \pi (r \sin[\beta])^2$$

$$\text{Solve}\left[4 \pi r^2 - 4 \pi \left( \left( \sqrt{(r^2 - (r \sin[\beta])^2)} \right)^2 \right) == 4 \pi (\eta)^2, \beta\right]$$

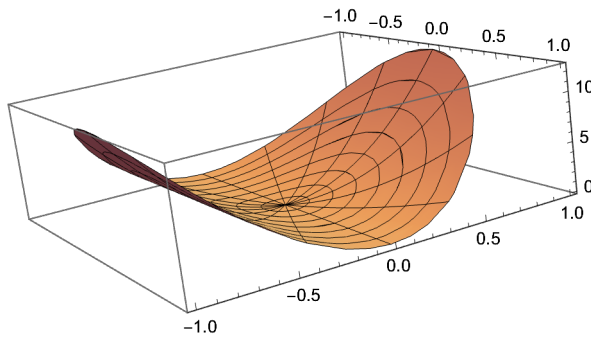
$$\left\{ \left\{ \beta \rightarrow -\text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right] \right\}, \left\{ \beta \rightarrow \text{ArcSin}\left[\sqrt{\frac{\eta^2}{r^2}}\right] \right\} \right\}$$

RevolutionPlot3D[

$$4 \pi r^2 - 4 \pi \left( \left( \sqrt{r^2 - \left( \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)^2} \right)^2 \right), \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]$$



RevolutionPlot3D[ $4 \pi r^2 - 4 \pi \left( \left( \sqrt{r^2 - (r \sin[\beta])^2} \right)^2 \right)$ , {r, -1, 1}, {β, -π, π}]



$$\begin{aligned} & \frac{4 \pi}{3} - \frac{-4 \pi^2 + 12 \pi^2 \sin[\beta]^2}{6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3}} + \\ & \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \\ & \frac{4 \pi}{3} + \left( \left( 1 + i \sqrt{3} \right) \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) \right) / \\ & \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \\ & \frac{1}{3} \left( 1 - i \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \\ & \frac{4 \pi}{3} + \left( \left( 1 - i \sqrt{3} \right) \left( -4 \pi^2 + 12 \pi^2 \sin[\beta]^2 \right) \right) / \\ & \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \\ & \frac{1}{3} \left( 1 + i \sqrt{3} \right) \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \} \end{aligned}$$

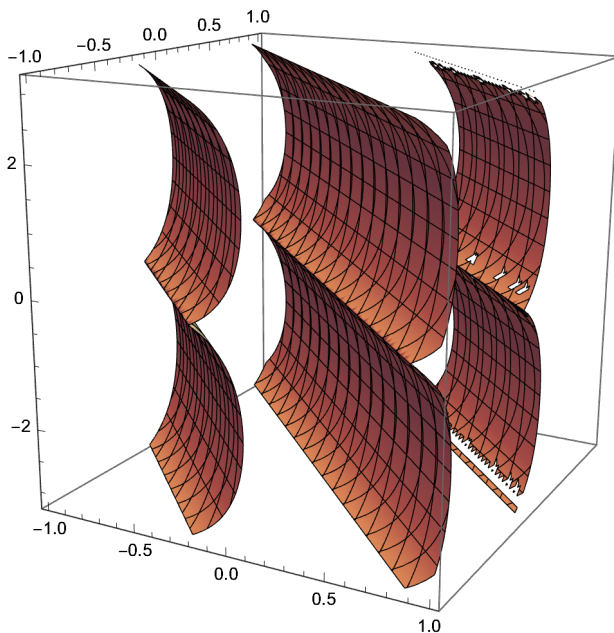
$$(e^{i\pi}) + 1 = 0$$

$$(e^{((i+j+k)\pi/\sqrt{3})}) + 1 = 0$$

if  $\theta = 0$ , then

$$\begin{aligned} \text{Solve}\left[\left(e^{((i+j+k)\pi/\sqrt{3})}\right) + 1 == \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right. \\ \left. \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \\ \left. \frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}, i\right] \\ \left\{\left\{i \rightarrow -\frac{1}{\sqrt{3}\pi}\left(\sqrt{3}j\pi + \sqrt{3}k\pi - 3\text{Log}\left[-1 + \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right. \right. \right. \right. \\ \left. \left. \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \right. \right. \\ \left. \left. \frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right] \right\}\right\} \end{aligned}$$

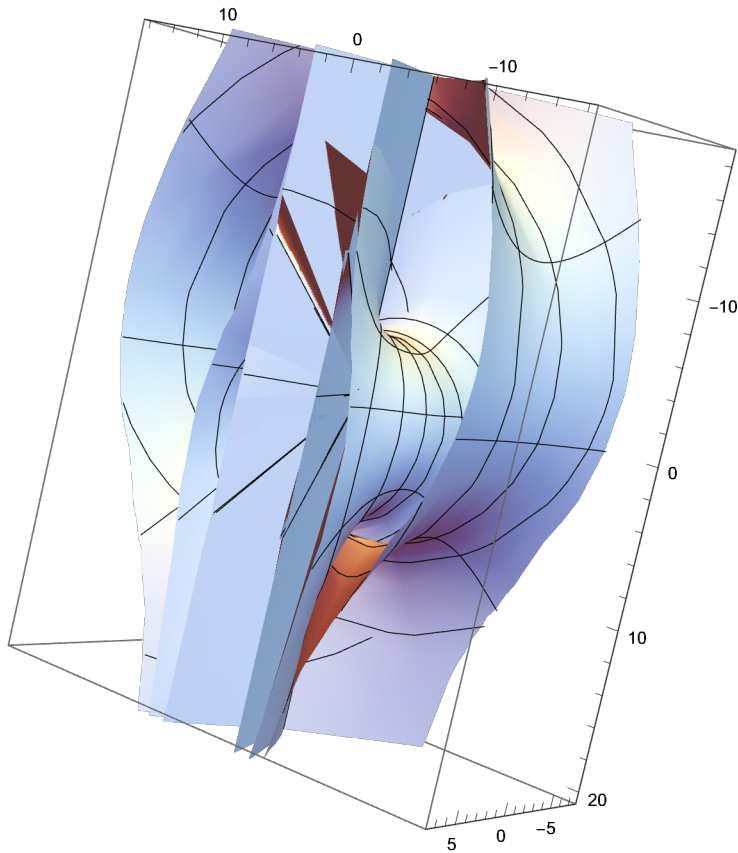
$$\begin{aligned} \text{ContourPlot3D}\left[-\frac{1}{\sqrt{3}\pi}\left(\sqrt{3}j\pi + \sqrt{3}k\pi - 3\text{Log}\left[-1 + \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right. \right. \right. \\ \left. \left. \left(6\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) + \right. \right. \right. \\ \left. \left. \frac{2}{3}\left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3}\sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right] \right), \\ \{k, -1, 1\}, \{j, -1, 1\}, \{\beta, -\pi, \pi\} \end{aligned}$$



$$\begin{aligned}
& \text{Solve}\left[\frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \Big/ \right. \\
& \quad \left(6 \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3 \times \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left(-\pi^3 + 18\pi^3 \sin[\beta]^2 + 3 \times \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3} == \theta, x\right] \\
& \left\{ \left\{ x \rightarrow \left( 36\pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - 36\pi\theta^2 \right. \right. \right. \\
& \quad \left. \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + 9\theta^3 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \\
& \quad 144\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 36\pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad \left. \sqrt{\left( -4 \left( 12\pi^2 \theta - 12\pi\theta^2 + 3\theta^3 - 24\pi^3 \sin[\beta]^2 - 204\pi^2 \theta \sin[\beta]^2 + 216\pi\theta^2 \sin[\beta]^2 - 54\theta^3 \right. \right. \right. \\
& \quad \left. \left. \sin[\beta]^2 + 600\pi^3 \sin[\beta]^4 - 216\pi^2 \theta \sin[\beta]^4 - 24\pi^3 \sin[\beta]^6 \right) \left( -8\pi^3 \sin[\beta]^2 + \right. \right. \\
& \quad \left. \left. 88\pi^3 \sin[\beta]^4 + 8\pi^3 \sin[\beta]^6 \right) + \left( -36\pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \\
& \quad \left. \left. 36\pi\theta^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \\
& \quad \left. \left. 9\theta^3 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \right. \right. \\
& \quad \left. \left. 144\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \\
& \quad \left. \left. 36\pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^2 \right) \Big/ \right. \\
& \quad \left. \left( 2 \left( -8\pi^3 \sin[\beta]^2 + 88\pi^3 \sin[\beta]^4 + 8\pi^3 \sin[\beta]^6 \right) \right) \right\}, \\
& \left\{ x \rightarrow \left( 36\pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \\
& \quad 36\pi\theta^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 9\theta^3 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 144\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 36\pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad \left. \sqrt{\left( -4 \left( 12\pi^2 \theta - 12\pi\theta^2 + 3\theta^3 - 24\pi^3 \sin[\beta]^2 - 204\pi^2 \theta \sin[\beta]^2 + 216\pi\theta^2 \sin[\beta]^2 - \right. \right. \right. \\
& \quad \left. \left. 54\theta^3 \sin[\beta]^2 + 600\pi^3 \sin[\beta]^4 - 216\pi^2 \theta \sin[\beta]^4 - 24\pi^3 \sin[\beta]^6 \right) \left( -8\pi^3 \sin[\beta]^2 + \right. \right. \\
& \quad \left. \left. 88\pi^3 \sin[\beta]^4 + 8\pi^3 \sin[\beta]^6 \right) + \left( -36\pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \right. \right. \\
& \quad \left. \left. 36\pi\theta^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \\
& \quad \left. \left. 9\theta^3 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} + \right. \right. \\
& \quad \left. \left. 144\pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} - \right. \right. \\
& \quad \left. \left. 36\pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11\sin[\beta]^2 + \sin[\beta]^4)} \right)^2 \right) \Big/ \right. \\
& \quad \left. \left( 2 \left( -8\pi^3 \sin[\beta]^2 + 88\pi^3 \sin[\beta]^4 + 8\pi^3 \sin[\beta]^6 \right) \right) \right\} \Big\}
\end{aligned}$$

$$\begin{aligned}
& \text{SphericalPlot3D}\left[\left(36 \pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 36 \pi \theta^2 \right. \right. \\
& \quad \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \theta^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 144 \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 36 \pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad \sqrt{\left(-4 (12 \pi^2 \theta - 12 \pi \theta^2 + 3 \theta^3 - 24 \pi^3 \sin[\beta]^2 - 204 \pi^2 \theta \sin[\beta]^2 + 216 \pi \theta^2 \sin[\beta]^2 - \right. \\
& \quad 54 \theta^3 \sin[\beta]^2 + 600 \pi^3 \sin[\beta]^4 - 216 \pi^2 \theta \sin[\beta]^4 - 24 \pi^3 \sin[\beta]^6) (-8 \pi^3 \sin[\beta]^2 + \\
& \quad 88 \pi^3 \sin[\beta]^4 + 8 \pi^3 \sin[\beta]^6) + (-36 \pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 36 \pi \theta^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad 9 \theta^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& \quad 144 \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \quad \left. \left. 36 \pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)}\right)^2\right)\right] / \\
& \quad (2 (-8 \pi^3 \sin[\beta]^2 + 88 \pi^3 \sin[\beta]^4 + 8 \pi^3 \sin[\beta]^6)), \{\theta, \\
& \quad -2 \\
& \quad \pi, 2 \\
& \quad \pi\}, \{\beta, -\pi, \pi\}]
\end{aligned}$$

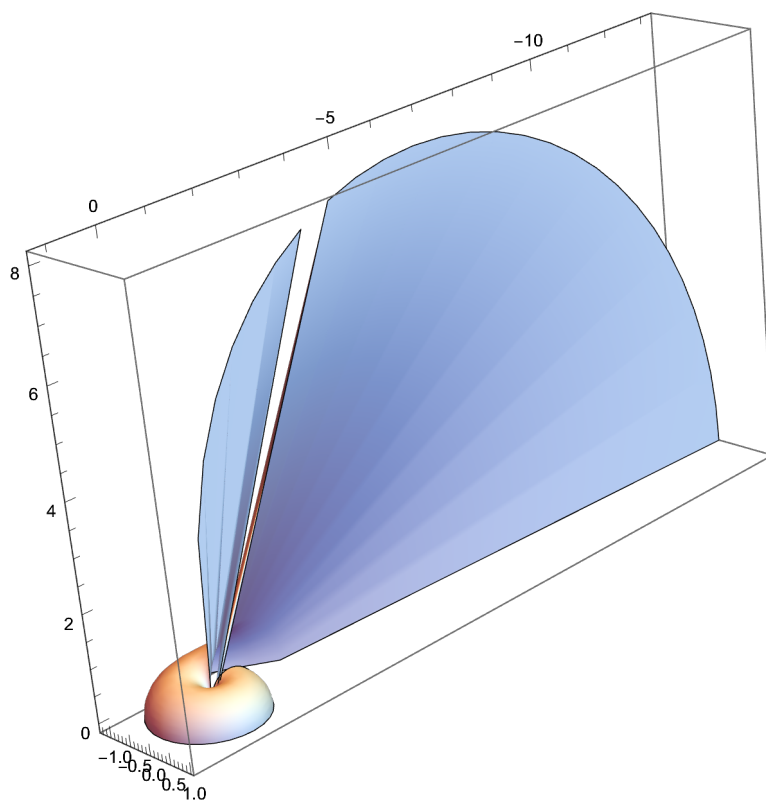


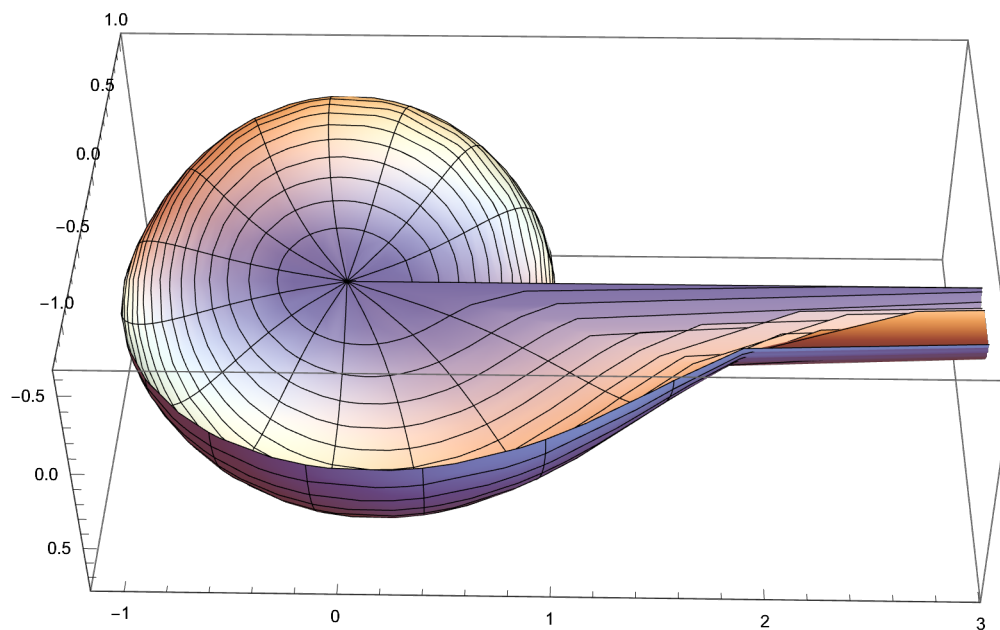


`Solve[(e^((i + j + k) π) / x)) + 1 == 0, x]`

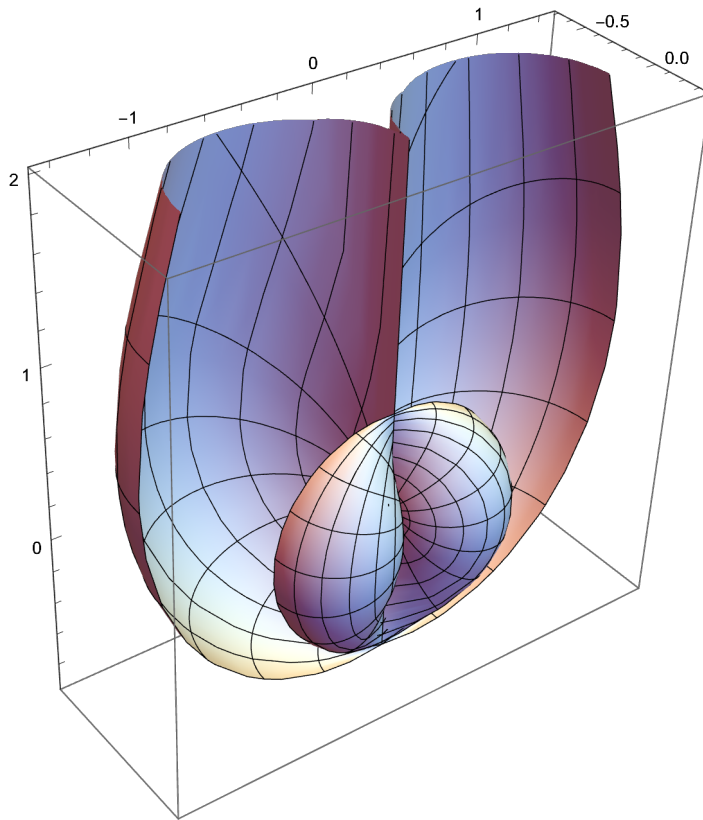
`{{x → -i (i + j + k)}}`

$$\begin{aligned}
\text{Solve}\left[-\frac{1}{2}(\mathbf{i} + \mathbf{j} + \mathbf{k}) == \right. & \left( 36 \pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - 36 \pi \theta^2 \right. \\
& \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + 9 \theta^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 144 \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 36 \pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \left. \sqrt{\left( -4 \left( 12 \pi^2 \theta - 12 \pi \theta^2 + 3 \theta^3 - 24 \pi^3 \sin[\beta]^2 - 204 \pi^2 \theta \sin[\beta]^2 + 216 \pi \theta^2 \sin[\beta]^2 - \right. \right. \right. \\
& 54 \theta^3 \sin[\beta]^2 + 600 \pi^3 \sin[\beta]^4 - 216 \pi^2 \theta \sin[\beta]^4 - 24 \pi^3 \sin[\beta]^6 \left. \right) \left( -8 \pi^3 \sin[\beta]^2 + \right. \\
& 88 \pi^3 \sin[\beta]^4 + 8 \pi^3 \sin[\beta]^6 \left. \right) + \left( -36 \pi^2 \theta \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \right. \\
& 36 \pi \theta^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& 9 \theta^3 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} + \\
& 144 \pi^3 \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} - \\
& \left. \left. \left. 36 \pi^2 \theta \sin[\beta]^2 \sqrt{\sin[\beta]^2 (-1 + 11 \sin[\beta]^2 + \sin[\beta]^4)} \right)^2 \right) \right) \Bigg] / \\
& \left( 2 \left( -8 \pi^3 \sin[\beta]^2 + 88 \pi^3 \sin[\beta]^4 + 8 \pi^3 \sin[\beta]^6 \right) \right), \beta \Big]
\end{aligned}$$

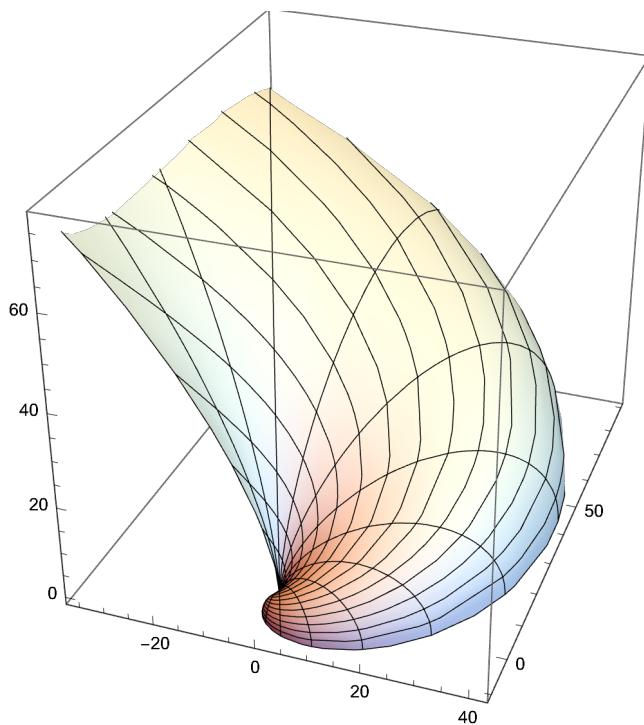
$$\text{SphericalPlot3D}\left[\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}},\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi\}\right]$$


$$\text{SphericalPlot3D}\left[\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}},\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$$


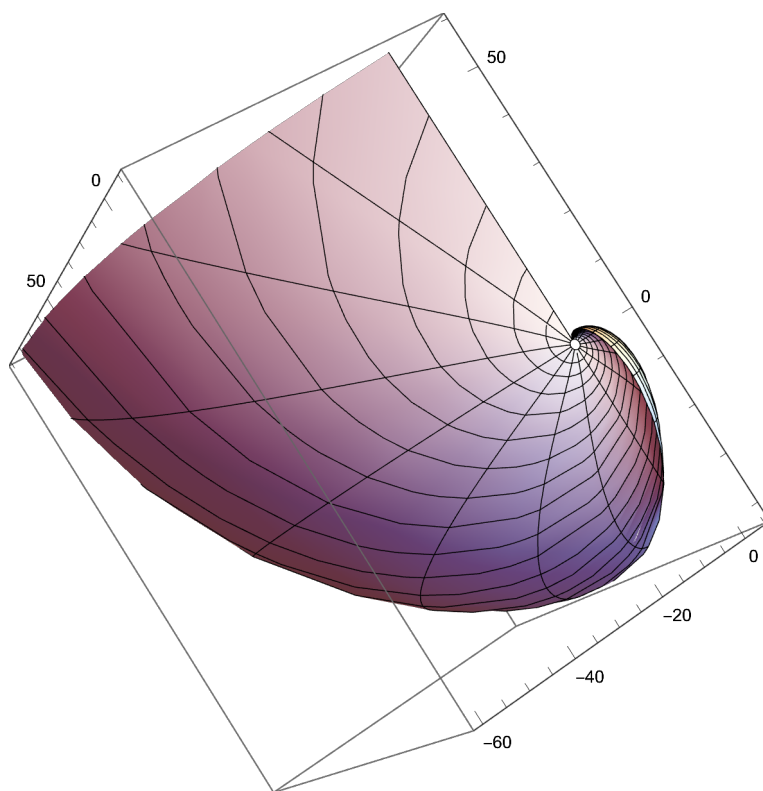
`SphericalPlot3D` $\left[\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}\sqrt{\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}},\{\theta,-2\pi,2\pi\},\{\beta,-\pi/2,\pi/2\}\right]$



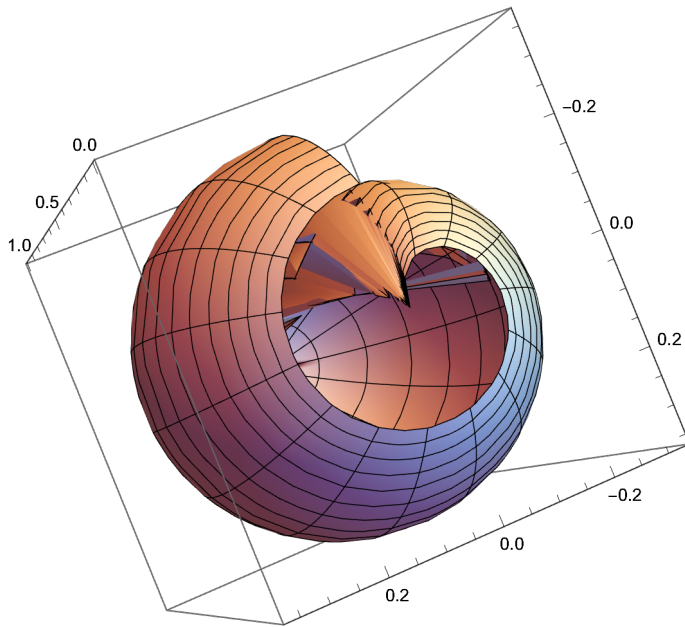
`SphericalPlot3D` $\left[e^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}\theta}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



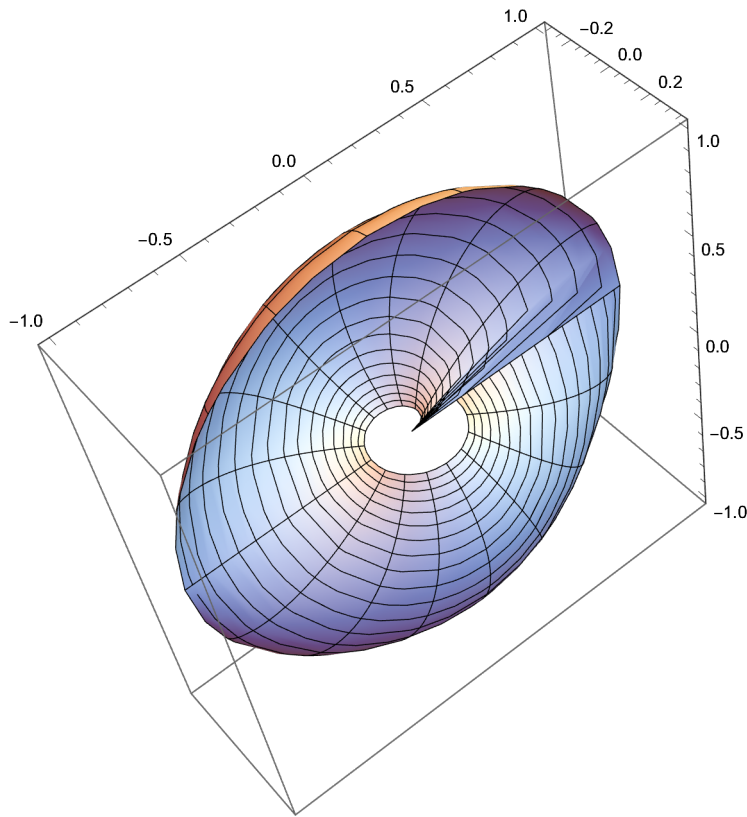
`SphericalPlot3D` $\left[e^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}\theta}, \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}\right]$



`SphericalPlot3D` $\left[e^{\sqrt{-\frac{2\pi\sin[\beta]}{\sqrt{4\pi\theta-\theta^2}}}}\beta, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2\pi, 2\pi\}\right]$



SphericalPlot3D $\left[e^{\sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \beta, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}\right]$



$$e^{\sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \beta$$

$$e^{\sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \beta$$

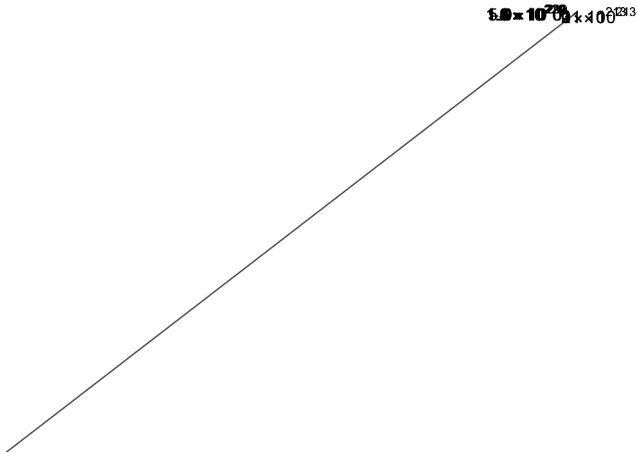
$$\text{Solve}\left[e^{\sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \theta == e^{\sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \beta, \theta\right]$$

$$\{\{\theta \rightarrow \beta\}\}$$

$$\text{SphericalPlot3D}\left[\cos\left[\frac{4 \pi}{3} + \left(1 + \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \sqrt{3}\right) (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2)\right] / \left(12 \left(-\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6}\right)^{1/3}\right) - \frac{1}{3} \left(1 - \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}}} \sqrt{3}\right)\right]$$

$$\begin{aligned}
& \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \Bigg] + \\
& \mathfrak{i} \sin \left[ \left( \frac{4 \pi}{3} + \left( \left( 1 + \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}} \sqrt{3} \right) (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \left. \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \right. \\
& \left. \left( 1 - \mathfrak{i} \sqrt{3} \right) \right. \\
& \left. \left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right] \Bigg] \\
& \left( \cos \left[ \left( \frac{4 \pi}{3} + \left( \left( 1 - \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}} \sqrt{3} \right) (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \right. \\
& \left. \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \right. \\
& \left. \left( 1 + \mathfrak{i} \sqrt{3} \right) \right. \\
& \left. \left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right] + \\
& \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}} \sin \left[ \left( \frac{4 \pi}{3} + \left( \left( 1 - \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}} \sqrt{3} \right) (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right) / \right. \right. \\
& \left. \left( 12 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) - \frac{1}{3} \right. \\
& \left. \left( 1 + \sqrt{-\frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}} \sqrt{3} \right) \right. \\
& \left. \left. \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right] \Bigg], \\
& \{\beta, -\pi, \pi\}, \{\theta, -4 \pi, 4 \pi\} \Big]
\end{aligned}$$





## Purely Geometric Mass from Kinetic Energy

$$\text{Kinetic Energy} = \frac{1}{2} m v^2$$

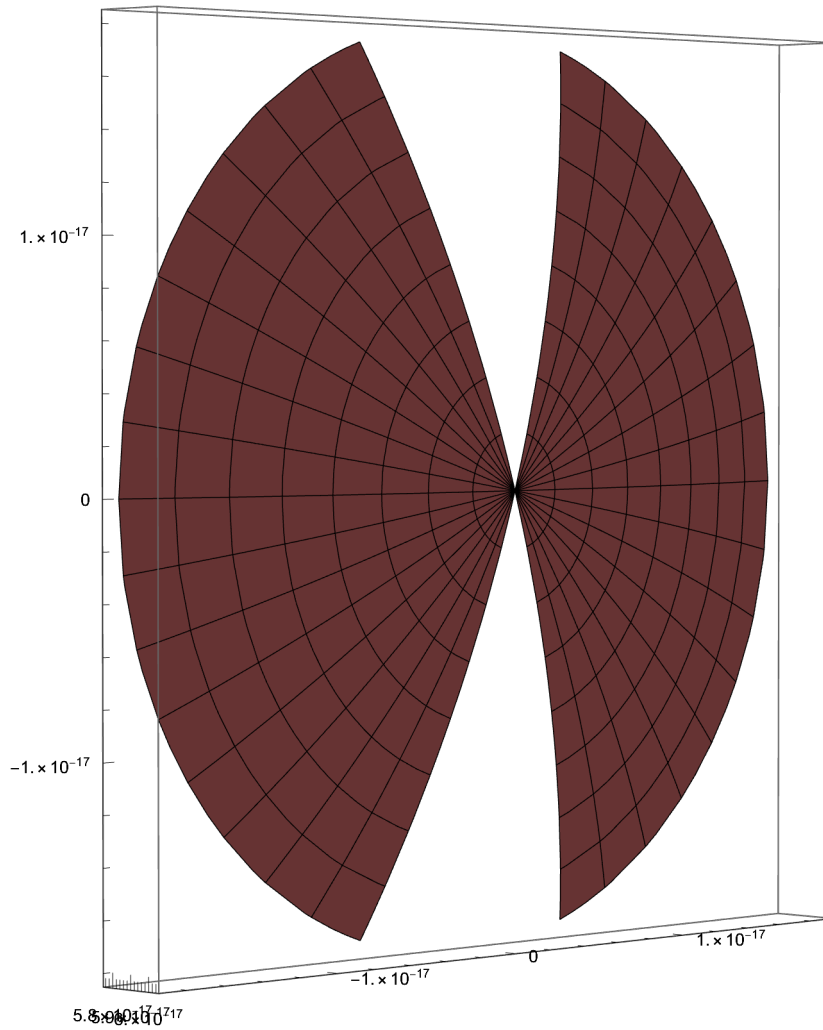
$$\left\{ v \rightarrow \frac{\sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right\}$$

$$\text{Solve}\left[\text{KE} == \frac{1}{2} m \left( \sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right)^2, m\right]$$

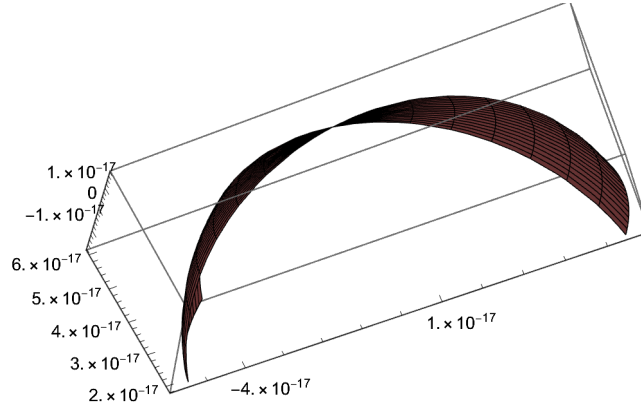
$$\left\{ \left\{ m \rightarrow \frac{2 \cdot \text{KE} (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)}{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right\} \right\}$$

$$\text{ContourPlot3D}\left[\left(2 \cdot \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) / \left( \sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2} \right), \{\beta, -.1 \pi, .1 \pi\}, \{\theta, -.4 \pi, .4 \pi\}, \{E, -1, 1\}\right]$$

```
SphericalPlot3D[
  (5.43656365691809` (-12.566370614359172`  $\theta + \theta^2 + 39.47841760435743` \text{Sin}[\beta]^2$ )) /
  (-1.1294090667581471`  $\theta^{18} + 8.987551787368176` \theta^{16} +$ 
  3.5481432270250993`  $\text{Sin}[\beta]^2$ ), { $\beta$ , -.1  $\pi$ , .1  $\pi$ }, { $\theta$ , -.4  $\pi$ , .4  $\pi$ }]
```



```
SphericalPlot3D[
  (5.43656365691809` (-12.566370614359172`  $\theta$  +  $\theta^2$  + 39.47841760435743` Sin[ $\beta$ ]2)) /
  (-1.1294090667581471` *18  $\theta$  + 8.987551787368176` *16  $\theta^2$  +
  3.5481432270250993` *18 Sin[ $\beta$ ]2), { $\theta$ , -.4  $\pi$ , .4  $\pi$ }, { $\beta$ , -.1  $\pi$ , .1  $\pi$ }]
```



# Theory on the Process of Tachyon Emulsion

In this paper, I will outline a few of the possibilities for transferring information contained within light via frequency, patterns, and digital signals to tachyons traveling faster than light. First, we set up the equation for the energy of a tachyon.

The term emulsion is used to describe this, because it is similar to the mixing of two things that are unblendable. Light energy cannot travel faster than light, and tachyon energy must always travel faster than light. We are trying to imprint the information of the energy of light into the information in the energy of a tachyon, which is traveling faster than light. Information, traveling at the speed of light, impresses itself onto the tachyon, and then the tachyon transfers that information at faster than light speed.

$E = (z c^2) / \sqrt{(u^2 / c^2) - 1}$ , where  $E$  is energy,  $z$  is imaginary mass,  $c$  is the speed of light, and  $u$  is the velocity of the mass.

Then, we note that  $z$  is imaginary mass, defining it to be :

Non - tachyon, or regular energy is equal to

$$E = (m c^2) / \sqrt{1 - v^2 / c^2}$$

$$(z c^2) / \sqrt{(u^2 / c^2) - 1} = (m c^2) / \sqrt{1 - v^2 / c^2} = h \nu$$

$$c := (2.99792458 * 10^8)$$

$$h := 6.626068 \times 10^{-34}$$

$$z := i \, m$$

We then set up a relativistic equation where we can solve for the intrinsic velocity of a wavelength of light.

From a difference in circumferences applied to the Pythagorean Theorem it can

$$\text{be shown that : Solve} \left[ \frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4 \pi r - r \theta}}{2 \pi} = r \sin[\beta], v \right]$$

$$\left\{ \left\{ v \rightarrow - \left( 1. \sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \right\}, \right.$$

$$\left. \left\{ v \rightarrow \left( \sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) \right\} \right\}$$

because the equation rearranges to :

$$\text{Solve} \left[ r \left( 1 - \frac{(v)^2}{c^2} \right) \theta 4 \pi r = (2 \pi r \sin[\beta])^2 + r \theta \sqrt{1 - \frac{(v)^2}{c^2}}, v \right],$$

yielding even more solutions.

We will use the mathematica generated positive solution,

$$v := \left( \sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right)$$

$$E = m c^2 = h \nu$$

$$\nu = \lambda \nu = \eta \nu$$

We solve for the

$$\text{Solve} \left[ \left( \sqrt{-1.1294090667581471 \times 10^{18} \theta + 8.987551787368176 \times 10^{16} \theta^2 + 3.5481432270250993 \times 10^{18} \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) = \eta \nu, v \right]$$

$$\left\{ \left\{ v \rightarrow \frac{1. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}}{\eta \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}} \right\} \right\}$$

$v =$

$$\text{Solve}\left[\left(1 / (\theta / 2 \pi)\right) == \left(1. \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) / \left(\eta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \eta\right]$$

$$v = \left(\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) / \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) = \eta v = \eta (1 / (\theta / (2 \pi)))$$

So, I pull together the equation for Energy of a photon from the geometry of a transformation of a circle into a cone, and then I set that equal to the energy of of the tachyon, because the geometry necessitates that something traveling at constant velocity (light) is at the thirty - sixty - ninety triangle position within the cone formed by the Pythagorean theorem applied to the change in circumferences of two circles, however positions below the 30 - 60 - 90 triangle exist, but necessitate acceleration. The geometry of time, or cyclicity, defines the velocity through the aforementioned transformation for positions above and below the 30 - 60 - 90 position of the cone. The innate geometry of the ontology of spacetime specifies both positive and negative solutions to the time element.

$$E = h (1 / (\theta / 2 \pi))$$

$$E = m c^2 = h v = (z c^2) / \sqrt{(u^2 / c^2) - 1} \text{ where } z = i m$$

$$h v = h \left(1. \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) / \left(\eta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right) = h (1 / (\theta / 2 \pi)) = (z c^2) / \sqrt{(u^2 / c^2) - 1}$$

$$\begin{aligned}
& \text{Solve}\left[h\left(1.\sqrt{-1.1294090667581471\cdot 10^{18}\theta + 8.987551787368176\cdot 10^{16}\theta^2 + 3.5481432270250993\cdot 10^{18}\sin[\beta]^2}\right)\right. \\
& \quad \left.\left(\eta\sqrt{-12.566370614359172\cdot\theta + \theta^2 + 39.47841760435743\cdot\sin[\beta]^2}\right) == \right. \\
& \quad \left.(z c^2) / \sqrt{(u^2 / c^2) - 1}, u\right] \\
& \left\{\left\{u \rightarrow -4.76445 \times 10^{-8} \sqrt{\left(3.95928 \times 10^{31} + 8.10486 \times 10^{114} z^2 \eta^2 - \frac{5.07954 \times 10^{16} \theta}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2} + \frac{1.0261 \times 10^{99} z^2 \eta^2 \theta}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2} + \frac{3.23424 \times 10^{15} \theta^2}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2} - \frac{6.59759 \times 10^{97} z^2 \eta^2 \theta^2}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2}\right)}\right\}, \\
& \left\{u \rightarrow 4.76445 \times 10^{-8} \sqrt{\left(3.95928 \times 10^{31} + 8.10486 \times 10^{114} z^2 \eta^2 - \frac{5.07954 \times 10^{16} \theta}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2} + \frac{1.0261 \times 10^{99} z^2 \eta^2 \theta}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2} + \frac{3.23424 \times 10^{15} \theta^2}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2} - \frac{6.59759 \times 10^{97} z^2 \eta^2 \theta^2}{12.5664 \theta - 1. \theta^2 - 39.4784 \sin[\beta]^2}\right)}\right\}
\end{aligned}$$

To get rid of  $z$  and have  $m$  in terms of the velocity, we solve the equation :

$$E = (m c^2) / \sqrt{1 - v^2 / c^2} = h \nu, \text{ where } v \text{ has been shown to equal :}$$

$$\begin{aligned}
v = & \left(\sqrt{-1.1294090667581471\cdot 10^{18}\theta + 8.987551787368176\cdot 10^{16}\theta^2 + 3.5481432270250993\cdot 10^{18}\sin[\beta]^2}\right) / \\
& \left(\sqrt{-12.566370614359172\cdot\theta + \theta^2 + 39.47841760435743\cdot\sin[\beta]^2}\right)
\end{aligned}$$

and  $\nu =$

$$\begin{aligned}
& (1 / (\theta / 2 \pi)) \left\{\left\{v \rightarrow \left(1.\sqrt{-1.1294090667581471\cdot 10^{18}\theta + 8.987551787368176\cdot 10^{16}\theta^2 + 3.5481432270250993\cdot 10^{18}\sin[\beta]^2}\right) / \right. \right. \\
& \quad \left. \left(\eta\sqrt{-12.566370614359172\cdot\theta + \theta^2 + 39.47841760435743\cdot\sin[\beta]^2}\right)\right\}\right\}
\end{aligned}$$

Thus, we set up the equation :

$$\begin{aligned} & (m c^2) / \sqrt{\left(1 - \left(\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right)\right)} / \\ & \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)^2 / c^2 = \\ & h(1 / (\theta / 2 \pi)) = h\left(1 \cdot \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) / \\ & \left(\eta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), \text{ and solve for } m \end{aligned}$$

$$\begin{aligned} & \text{Solve}\left[(m c^2) / \sqrt{\left(1 - \left(\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right)\right)} / \right. \\ & \left. \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)^2 / c^2\right] == \\ & h\left(1 \cdot \sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right) / \\ & \left(\eta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right), m] \\ & \left\{\left\{m \rightarrow \left(7.37249 \times 10^{-51} \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \sqrt{\left(1 - \left(1.11265 \times 10^{-17} \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2}\right)\right)} / \left(-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2\right)\right)} / \left(\eta \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2}\right)\right\}\right\} \end{aligned}$$

$$\begin{aligned} & \text{Solve}\left[(m c^2) / \sqrt{\left(1 - \left(\sqrt{-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2}\right)\right)} / \right. \\ & \left. \left(\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}\right)^2 / c^2\right] == h(1 / (\theta / 2 \pi)), m] \\ & \left\{\left\{m \rightarrow \frac{0.63662 h \sqrt{1 - \frac{1 \cdot \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} (12.5664 - 1 \cdot \theta) \theta + 8.98755 \times 10^{16} \theta^2}}{c^2 (-12.5664 \theta + 1 \cdot (12.5664 - 1 \cdot \theta) \theta + \theta^2)}}}{c^2 \theta}\right\}\right\} \end{aligned}$$

$$c := (2.99792458 \cdot 10^8)$$

$$h := (6.626068 \cdot 10^{-34})$$

We are now ready to return to the Tachyon energy expression that equals the energy of a photon.

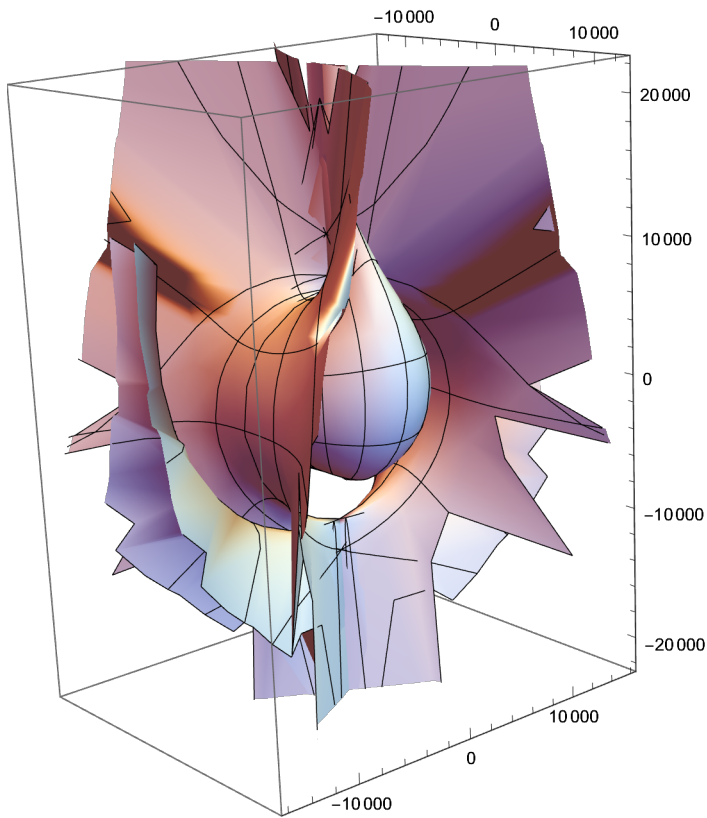
$$\begin{aligned}
h v &= h \left( 1. \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) / \\
&\quad \left( \eta \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) = \\
&\quad (i m c^2) / \sqrt{(u^2 / c^2) - 1} \\
&\quad (i m c^2) / \sqrt{(u^2 / c^2) - 1} = \\
&\quad \left( i \left( 7.372494931615088 \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) \right. \\
&\quad \left. \sqrt{1. - (1.1126500560536185 \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) / } \\
&\quad \left. (-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2) \right) / \\
&\quad \left( \eta \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) c^2 \\
&\quad \left. \right) / \sqrt{(u^2 / c^2) - 1} = \\
&\quad h \left( 1. \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) / \\
&\quad \left( \eta \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) = h v
\end{aligned}$$

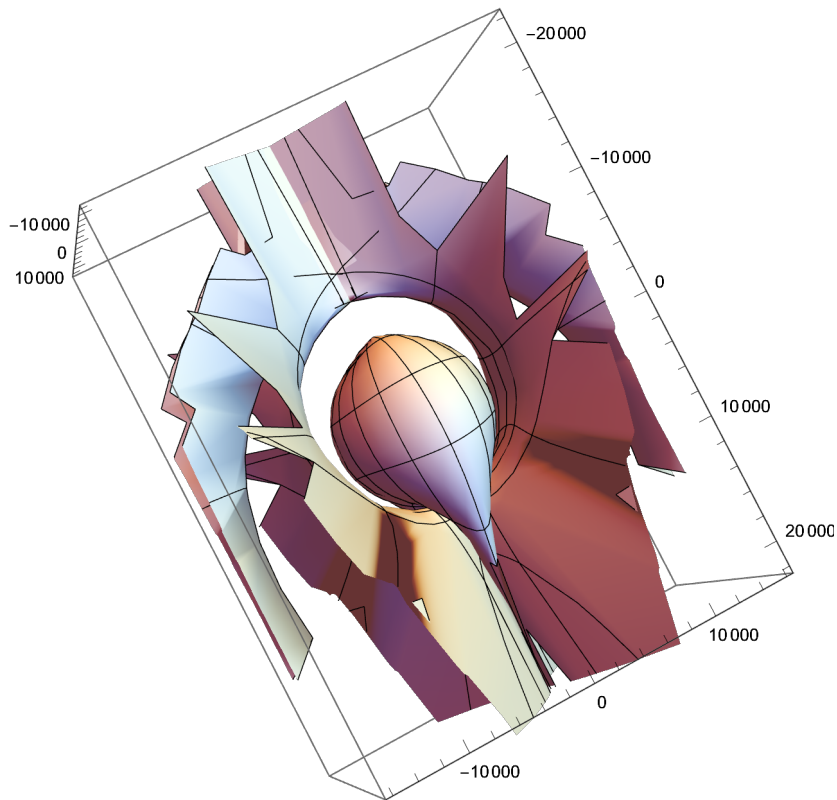
$$\begin{aligned}
\text{Solve} &\left[ h \left( 1. \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) / \right. \\
&\quad \left. \left( \eta \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) = \right. \\
&\quad \left. \left( i \left( 7.372494931615088 \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) \right. \right. \\
&\quad \left. \left. \sqrt{1. - (1.1126500560536185 \sqrt{-1.1294090667581471 \theta + 8.987551787368176 \theta^2 + 3.5481432270250993 \sin[\beta]^2} \right) / } \right. \\
&\quad \left. \left. (-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2) \right) \right) / \\
&\quad \left( \eta \sqrt{-12.566370614359172 \theta + \theta^2 + 39.47841760435743 \sin[\beta]^2} \right) c^2 \\
&\quad \left. \right) / \sqrt{(u^2 / c^2) - 1}, u]
\end{aligned}$$

$$\begin{aligned}
&\left\{ \left\{ u \rightarrow - \frac{3.4921 \times 10^{23} (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^{1/4}}{\sqrt{-5.11167 \times 10^{39} \theta + 4.06774 \times 10^{38} \theta^2 + 1.60588 \times 10^{40} \sin[\beta]^2}} \right\}, \right. \\
&\left. \left\{ u \rightarrow \frac{3.4921 \times 10^{23} (-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2)^{1/4}}{\sqrt{-5.11167 \times 10^{39} \theta + 4.06774 \times 10^{38} \theta^2 + 1.60588 \times 10^{40} \sin[\beta]^2}} \right\} \right\}
\end{aligned}$$



```
SphericalPlot3D[(3.492100110115638`*^23
  (-12.566370614359172` $\theta$  +  $\theta^2$  + 39.47841760435743`Sin[ $\beta$ ]^2)^{1/4}) /
  (\sqrt{(-5.1116667405465595`*^39  $\theta$  + 4.067735145982109`*^38  $\theta^2$  +
    1.6058774679700357`*^40 Sin[ $\beta$ ]^2)}), { $\theta$ , -2  $\pi$ , 2  $\pi$ }, { $\beta$ , - $\pi$ ,  $\pi$ }]
```





This is a single expression of the information contained through tachyon emulsion, and I hope people can develop this into a technological process in the future. Please note that you found the methods at this source.

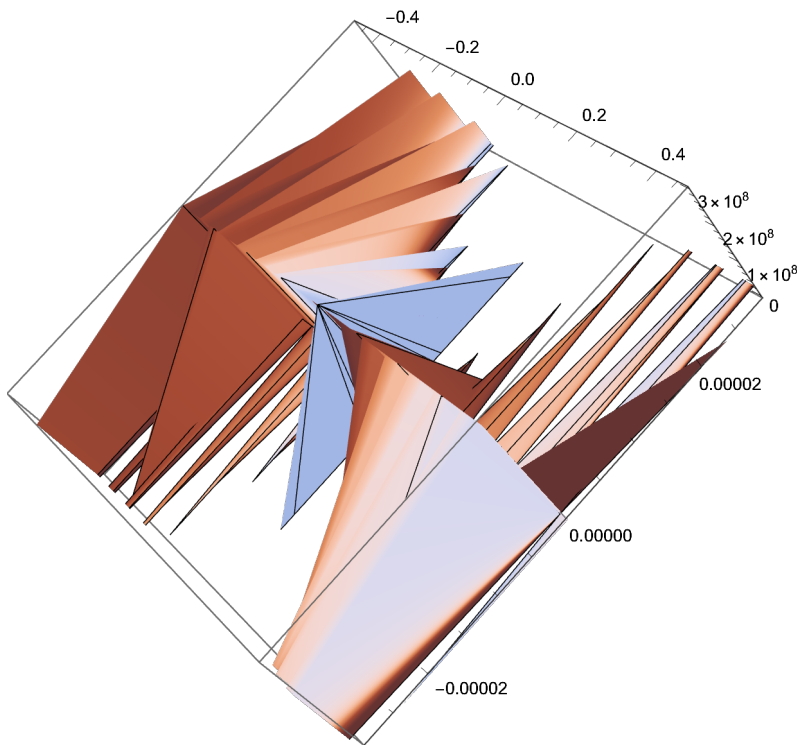
$$\text{Solve}\left[h \left(1 / (\theta / 2 \pi)\right) == (z c^2) / \sqrt{(u^2 / c^2) - 1}, z\right]$$

$$\left\{\left\{z \rightarrow \frac{2 h \sqrt{-1 + \frac{u^2}{c^2}}}{c^2 \pi \theta}\right\}\right\}$$

$$\text{Solve}\left[h \left(1 / (\theta / 2 \pi)\right) == (z c^2) / \sqrt{(u^2 / c^2) - 1}, u\right]$$

$$\left\{\left\{u \rightarrow -\frac{1}{2} c \sqrt{4 + \frac{c^4 \pi^2 z^2 \theta^2}{h^2}}\right\}, \left\{u \rightarrow \frac{1}{2} c \sqrt{4 + \frac{c^4 \pi^2 z^2 \theta^2}{h^2}}\right\}\right\}$$

RevolutionPlot3D $\left[\frac{1}{2} c \sqrt{4 + \frac{c^4 \pi^2 (\mathbf{i} m)^2 \theta^2}{h^2}}, \{m, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}\right]$



Solve $\left[h (1 / (\theta / 2 \pi)) == (z c^2) / \sqrt{(u^2 / c^2) - 1}, \theta\right]$

$$\left\{\left\{\theta \rightarrow \frac{2 h \sqrt{-1 + \frac{u^2}{c^2}}}{c^2 \pi z}\right\}\right\}$$

$$v = \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} =$$

$$\frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} = \lambda v = \eta v$$

$$v = \left( \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) / \eta =$$

$$\left( \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) / (r \sin[\beta]) = \left( \frac{4 \pi r^2 - 2 r^2 \theta}{2 \sqrt{4 \pi r^2 \theta - r^2 \theta^2}} \right) / \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$$

$$\text{Solve}\left[\frac{\sqrt{r}\sqrt{1-\frac{(v)^2}{c^2}}\sqrt{\frac{\theta}{\sqrt{1-\frac{(v)^2}{c^2}}}}\sqrt{4\pi r-r\theta}}{2\pi}=r\sin[\beta],v\right]$$

$$\left\{\left\{v\rightarrow-\frac{1.\sqrt{-1.12941\times 10^{18}\theta+8.98755\times 10^{16}\theta^2+3.54814\times 10^{18}\sin[\beta]^2}}{\sqrt{-12.5664\theta+\theta^2+39.4784\sin[\beta]^2}}\right\},\right.$$

$$\left.\left\{v\rightarrow\frac{\sqrt{-1.12941\times 10^{18}\theta+8.98755\times 10^{16}\theta^2+3.54814\times 10^{18}\sin[\beta]^2}}{\sqrt{-12.5664\theta+\theta^2+39.4784\sin[\beta]^2}}\right\}\right\}$$

$$E=mc^2=hv=h\left(\frac{4\pi r^2-2r^2\theta}{2\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)/\eta=$$

$$h\left(\frac{4\pi r^2-2r^2\theta}{2\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)/(r\sin[\beta])=h\left(\frac{4\pi r^2-2r^2\theta}{2\sqrt{4\pi r^2\theta-r^2\theta^2}}\right)/\frac{\sqrt{4\pi r^2\theta-r^2\theta^2}}{2\pi}$$

$$\text{Plot3D}\left[\frac{2h\sqrt{-1+\frac{u^2}{c^2}}}{c^2\pi z},\{m,-1,1\},\{u,c,c\}\right]$$

$$\text{Plot3D}\left[\frac{2h\sqrt{-1+\frac{u^2}{c^2}}}{c^2\pi(\text{im})},\{m,-1,1\},\{u,c,c\}\right]$$

$$c:=(2.99792458*10^8)$$

$$h:=6.626068*10^{-34}$$

$$(zc^2)/\sqrt{(u^2/c^2)-1}=(mc^2)/\sqrt{1-v^2/c^2}=hv$$

$$(zc^2)/\sqrt{(u^2/c^2)-1}=$$

$$\left(\left(\left(7.372494931615088*10^{-51}\sqrt{(-1.1294090667581471*10^{18}\theta+8.987551787368176*10^{16}\theta^2+3.5481432270250993*10^{18}\sin[\beta]^2)}\right.\right.\right.$$

$$\left.\left.\sqrt{(1.-\left(1.1126500560536185*10^{-17}\sqrt{(-1.1294090667581471*10^{18}\theta+8.987551787368176*10^{16}\theta^2+3.5481432270250993*10^{18}\sin[\beta]^2)}\right))}\right.\right.$$

$$\left.\left.(-12.566370614359172\theta+\theta^2+39.47841760435743\sin[\beta]^2)\right)\right)/$$

$$\left(\eta\sqrt{-12.566370614359172\theta+\theta^2+39.47841760435743\sin[\beta]^2}\right)c^2$$

$$\left.\right)/\sqrt{1-v^2/c^2}$$

We can also solve for z alone :

m =

$$\begin{aligned} & \left( 7.372494931615088 \cdot 10^{-51} \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + \right. \\ & \quad \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right. \\ & \quad \sqrt{\left( 1. - \left( 1.1126500560536185 \cdot 10^{-17} \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right. \right. \\ & \quad \left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2)} \right) \right) / \\ & \quad \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right) \Bigg) / \\ & \quad \left( \eta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \end{aligned}$$

$$(m c^2) / \sqrt{1 - v^2 / c^2} =$$

$$\begin{aligned} & (z c^2) / \sqrt{\left( \left( 3.492100110115638 \cdot 10^{23} (-12.566370614359172 \cdot \theta + \right. \right. \\ & \quad \left. \left. \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2)^{1/4} \right) \right) / \\ & \quad \left( \sqrt{(-5.1116667405465595 \cdot 10^{39} \theta + 4.067735145982109 \cdot 10^{38} \theta^2 + \right.} \\ & \quad \left. 1.6058774679700357 \cdot 10^{40} \sin[\beta]^2)} \right) \Bigg)^2 / c^2 - 1 \end{aligned}$$

$$\text{Solve}\left[h \left( 1. - \sqrt{(-1.1294090667581471 \cdot 10^{18} \theta + \right.} \right.$$

$$\left. \left. 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) /$$

$$\left( \eta \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) ==$$

$$(z c^2) / \sqrt{(u^2 / c^2) - 1}, z]$$

$$\left\{ \left\{ z \rightarrow \left( 7.37249 \times 10^{-51} \sqrt{-1. + 1.11265 \times 10^{-17} u^2} \right. \right. \right.$$

$$\left. \left. \sqrt{-1.12941 \times 10^{18} \theta + 8.98755 \times 10^{16} \theta^2 + 3.54814 \times 10^{18} \sin[\beta]^2} \right) \right) /$$

$$\left( \eta \sqrt{-12.5664 \theta + \theta^2 + 39.4784 \sin[\beta]^2} \right) \Bigg\} \Bigg\}$$

z := i m

$$u = \left( 3.492100110115638 \cdot 10^{23} \right.$$

$$\left. \left( -12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2 \right)^{1/4} \right) /$$

$$\left( \sqrt{(-5.1116667405465595 \cdot 10^{39} \theta + 4.067735145982109 \cdot 10^{38} \theta^2 + \right.} \\ \left. 1.6058774679700357 \cdot 10^{40} \sin[\beta]^2)} \right)$$

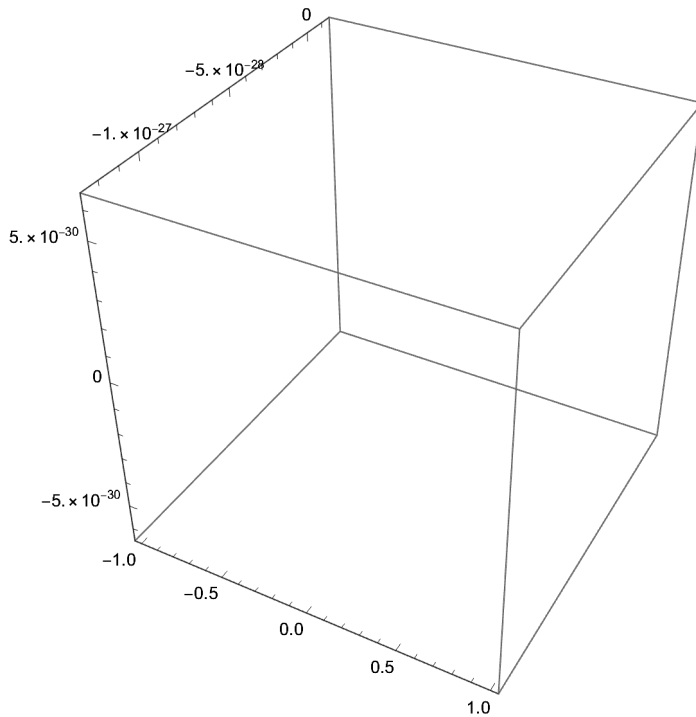
$$\eta := \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} = r \sin[\beta]$$

$$\sqrt{\left( r \sin[\beta] \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} \right)} = \pm \eta$$

```

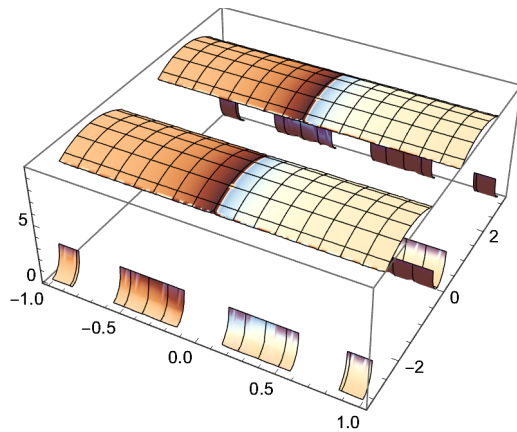
ContourPlot3D[ (7.372494931615088`*^-51
  Sqrt[(-1.` + 1.1126500560536185`*^-17 ((3.492100110115638`*^23
    (-12.566370614359172`  $\theta$  +  $\theta^2$  + 39.47841760435743` Sin[ $\beta$ ]2)1/4) /
    (Sqrt[(-5.1116667405465595`*^39  $\theta$  + 4.067735145982109`*^38  $\theta^2$  +
      1.6058774679700357`*^40 Sin[ $\beta$ ]2)))]2)
  Sqrt[(-1.1294090667581471`*^18  $\theta$  + 8.987551787368176`*^16  $\theta^2$  +
    3.5481432270250993`*^18 Sin[ $\beta$ ]2))] / (Sqrt[ (r Sin[ $\beta$ ]  $\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}$ ) ]
  Sqrt[-12.566370614359172`  $\theta$  +  $\theta^2$  + 39.47841760435743` Sin[ $\beta$ ]2],
  {r, -1, 1}, { $\theta$ , -.00000000000000000000000000000004
     $\pi$ ,
    .00000000000000000000000000000000000000000004
     $\pi$ },
  { $\beta$ , -.0000000000000000000000000000000000000000002
     $\pi$ ,
    .000000000000000000000000000000000000000002  $\pi$ } ]

```

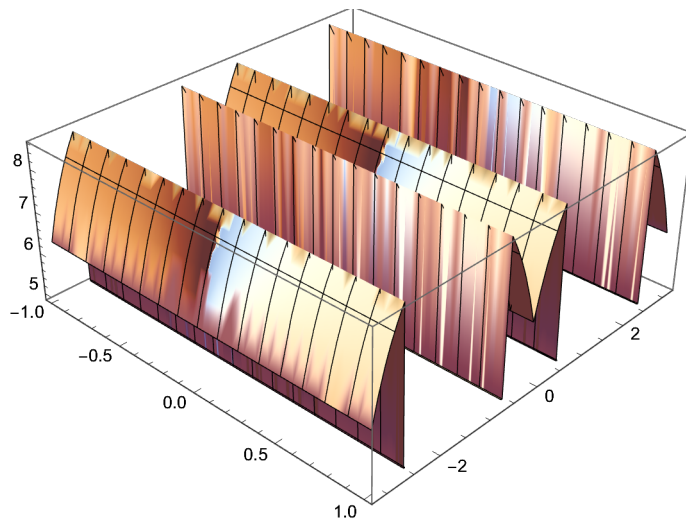


$\eta := r \sin[\beta]$

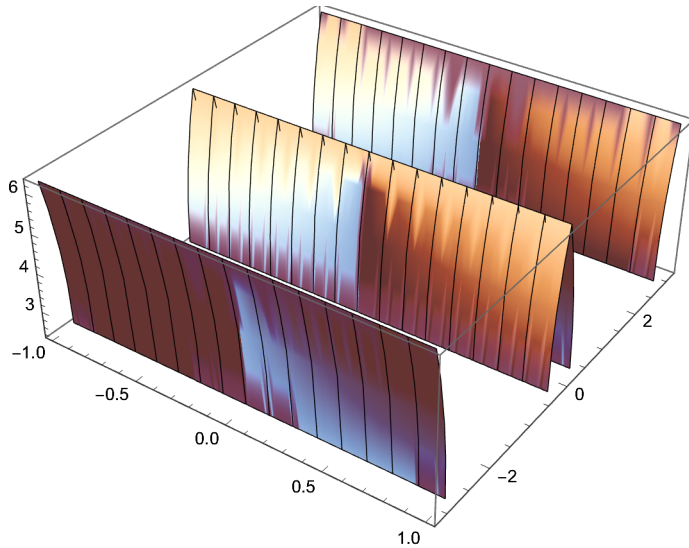
$$\text{Plot3D}\left[\frac{4\pi}{3} + \frac{-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2}{6\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} - \frac{2\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$$



$$\text{Plot3D}\left[\frac{4\pi}{3} - \frac{(1 + i\sqrt{3})(-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2)}{12\pi r^2 \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}} + \frac{(1 - i\sqrt{3})\pi \left(r^6 - 18r^4 \eta^2 + 3\sqrt{3}\sqrt{-r^{10}\eta^2 + 11r^8\eta^4 + r^6\eta^6}\right)^{1/3}}{3r^2}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$$



$$\text{Plot3D}\left[\frac{4\pi}{3} - \frac{(1 - \sqrt{3}) (-4\pi^2 r^4 + 12\pi^2 r^2 \eta^2)}{12\pi r^2 (r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6})^{1/3}} + \frac{(1 + \sqrt{3}) \pi (r^6 - 18r^4 \eta^2 + 3\sqrt{3} \sqrt{-r^{10} \eta^2 + 11r^8 \eta^4 + r^6 \eta^6})^{1/3}}{3r^2}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}\right]$$



$$\frac{\sqrt{r} \sqrt{1 - \frac{(v)^2}{c^2}} \sqrt{\frac{\theta}{\sqrt{1 - \frac{(v)^2}{c^2}}}} \sqrt{4\pi r - r\theta}}{2\pi} = r \sin[\beta]$$

$$t / 1.00 = .10$$

$$x / 1.00 \rightarrow \text{user1} = \text{ref \#}$$

$$y / 1.00 \rightarrow \text{user2}$$

$$x + y + z \dots b \leq 1.00$$

$$t / m = .10 = \text{blogband}$$

$$x / m \rightarrow \text{user1} = \text{ref \#1}$$

$$y / m \rightarrow \text{user2} = \text{ref \#2}$$

$$x + y + z \dots b \leq 1.00$$

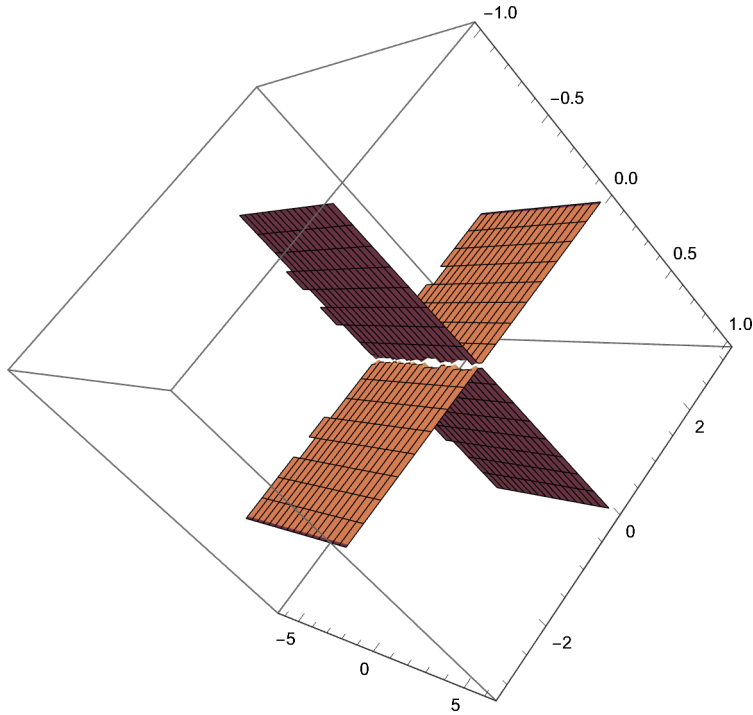
$$t, x, y \dots = \theta$$

$$\theta := 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right), \text{ because } 1 = \frac{2\pi \sin[\beta]}{\sqrt{4\pi\theta - \theta^2}}$$

$$\eta := \frac{\sqrt{4\pi r^2 \theta - r^2 \theta^2}}{2\pi} = r \sin[\beta]$$



ContourPlot3D $\left[r \frac{2 \pi \sin[\beta]}{\sqrt{4 \pi \theta - \theta^2}}, \{r, -1, 1\}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



**Form :** Circumference of a circle with radius of the height of the base cone minus circumference of another circle equals a hypothetical arc length.

$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \delta = \epsilon r, r\right]$$

$$\left\{\left\{r \rightarrow \frac{2 \pi \left(-\delta \epsilon - \sqrt{4 \pi \delta^2 \theta - \delta^2 \theta^2}\right)}{\epsilon^2 - 4 \pi \theta + \theta^2}\right\}, \left\{r \rightarrow \frac{2 \pi \left(-\delta \epsilon + \sqrt{4 \pi \delta^2 \theta - \delta^2 \theta^2}\right)}{\epsilon^2 - 4 \pi \theta + \theta^2}\right\}\right\}$$

$$\text{Solve}\left[2 \pi \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} - 2 \pi \delta = \theta r, r\right]$$

$$\left\{\left\{r \rightarrow \frac{\pi \left(-\delta \theta - \sqrt{4 \pi \delta^2 \theta - \delta^2 \theta^2}\right)}{-2 \pi \theta + \theta^2}\right\}, \left\{r \rightarrow \frac{\pi \left(-\delta \theta + \sqrt{4 \pi \delta^2 \theta - \delta^2 \theta^2}\right)}{-2 \pi \theta + \theta^2}\right\}\right\}$$

$$\text{Solve}\left[2\pi \frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi} - 2\pi \sqrt{\frac{\sqrt{4\pi r^2\theta - r^2\theta^2}}{2\pi}}^2 - \xi^2 = \theta r, r\right]$$

$$\left\{\left\{r \rightarrow -2 \sqrt{-\frac{\pi^2 \xi^2 \theta^2}{-16\pi\theta^3 + 5\theta^4} - \frac{2\pi^2 \sqrt{\xi^4(4\pi - \theta)\theta^3}}{-16\pi\theta^3 + 5\theta^4}}\right\},\right.$$

$$\left\{r \rightarrow 2 \sqrt{-\frac{\pi^2 \xi^2 \theta^2}{-16\pi\theta^3 + 5\theta^4} - \frac{2\pi^2 \sqrt{\xi^4(4\pi - \theta)\theta^3}}{-16\pi\theta^3 + 5\theta^4}}\right\},$$

$$\left\{r \rightarrow -2 \sqrt{-\frac{\pi^2 \xi^2 \theta^2}{-16\pi\theta^3 + 5\theta^4} + \frac{2\pi^2 \sqrt{\xi^4(4\pi - \theta)\theta^3}}{-16\pi\theta^3 + 5\theta^4}}\right\},$$

$$\left\{r \rightarrow 2 \sqrt{-\frac{\pi^2 \xi^2 \theta^2}{-16\pi\theta^3 + 5\theta^4} + \frac{2\pi^2 \sqrt{\xi^4(4\pi - \theta)\theta^3}}{-16\pi\theta^3 + 5\theta^4}}\right\}\}$$

$$2\pi x - 2\pi l = \theta x$$

$$2\pi \left(r - \frac{r\theta}{2\pi}\right) - 2\pi l = \theta x$$

$$-2l\pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = x\theta$$

$$-2l\pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = x\theta$$

$$-2l\pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = x\theta$$

$$-2l\pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = \left(r - \frac{r\theta}{2\pi}\right)\theta$$

$$-2l\pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = \theta \left(r - \frac{r\theta}{2\pi}\right)$$

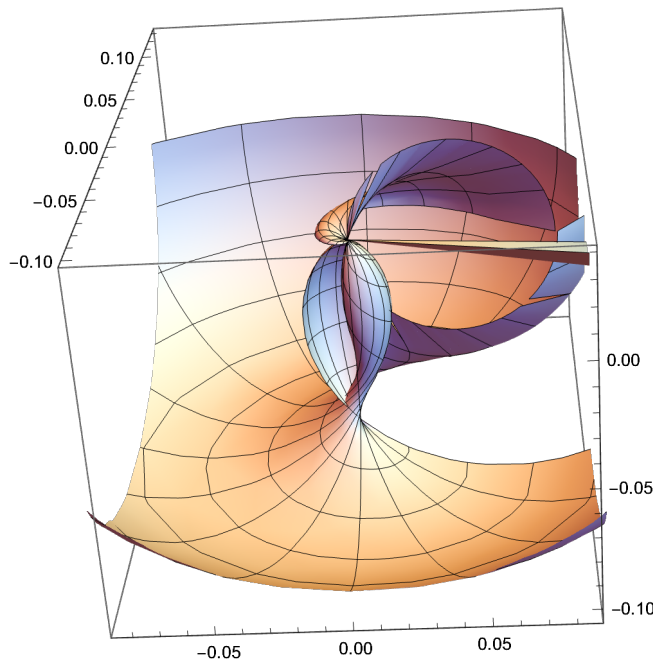
$$-2 \sqrt{\left(r - \frac{r\theta}{2\pi}\right)^2 - y^2} \pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = \theta \left(r - \frac{r\theta}{2\pi}\right)$$

$$\text{Solve}\left[-2 \sqrt{\left(r - \frac{r\theta}{2\pi}\right)^2 - y^2} \pi + 2\pi \left(r - \frac{r\theta}{2\pi}\right) = \theta \left(r - \frac{r\theta}{2\pi}\right), y\right]$$

$$\left\{\left\{y \rightarrow -\frac{r\sqrt{\theta}\sqrt{16\pi^3 - 20\pi^2\theta + 8\pi\theta^2 - \theta^3}}{4\pi^2}\right\}, \left\{y \rightarrow \frac{r\sqrt{\theta}\sqrt{16\pi^3 - 20\pi^2\theta + 8\pi\theta^2 - \theta^3}}{4\pi^2}\right\}\right\}$$

$$r := \left(-4\pi\theta + \theta^2 + 2\pi\sqrt{(4\pi - \theta)\theta}\sin[\beta] + 4\pi^2\sin[\beta]^2 - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{4\pi - \theta} - \frac{2\pi^2\sqrt{(4\pi - \theta)\theta}\sin[\beta]^3}{\theta}\right) / (16\pi^2\theta - 12\pi\theta^2 + 2\theta^3 - 16\pi^3\sin[\beta]^2 + 8\pi^2\theta\sin[\beta]^2)$$

SphericalPlot3D $\left[\frac{r \sqrt{\theta} \sqrt{16 \pi^3 - 20 \pi^2 \theta + 8 \pi \theta^2 - \theta^3}}{4 \pi^2}, \{\beta, -\pi/2, \pi/2\}, \{\theta, -2 \pi, 2 \pi\}\right]$

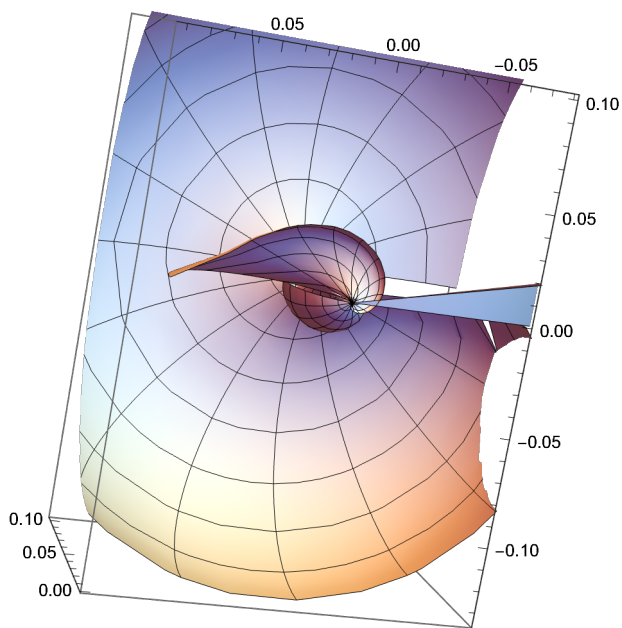


$$\frac{\sqrt{4 \pi \left(r - \frac{r \theta}{2 \pi}\right)^2 \theta - \left(r - \frac{r \theta}{2 \pi}\right)^2 \theta^2}}{2 \pi}$$

$$\left( \left( -4 \pi \theta + \theta^2 + 2 \pi \sqrt{(4 \pi - \theta) \theta} \sin[\beta] + 4 \pi^2 \sin[\beta]^2 - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{4 \pi - \theta} - \frac{2 \pi^2 \sqrt{(4 \pi - \theta) \theta} \sin[\beta]^3}{\theta} \right) / (16 \pi^2 \theta - 12 \pi \theta^2 + 2 \theta^3 - 16 \pi^3 \sin[\beta]^2 + 8 \pi^2 \theta \sin[\beta]^2) \right)$$

SphericalPlot3D $\left[\frac{1}{2\pi}\right.$

$$\left(\sqrt{\left(4\pi\left(\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)\right)/\left(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2\right)\right)-\frac{1}{2\pi}\left(\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)\right)/\left(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2\right)\right)\right)^2\theta-\left(\left(\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)\right)/\left(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2\right)\right)-\frac{1}{2\pi}\left(\left(\left(-4\pi\theta+\theta^2+2\pi\sqrt{(4\pi-\theta)\theta}\sin[\beta]+4\pi^2\sin[\beta]^2-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{4\pi-\theta}-\frac{2\pi^2\sqrt{(4\pi-\theta)\theta}\sin[\beta]^3}{\theta}\right)\right)/\left(16\pi^2\theta-12\pi\theta^2+2\theta^3-16\pi^3\sin[\beta]^2+8\pi^2\theta\sin[\beta]^2\right)\right)\right)^2\theta^2\right)\right),\{\beta,-\pi/2,\pi/2\},\{\theta,-2\pi,2\pi}\right]$$



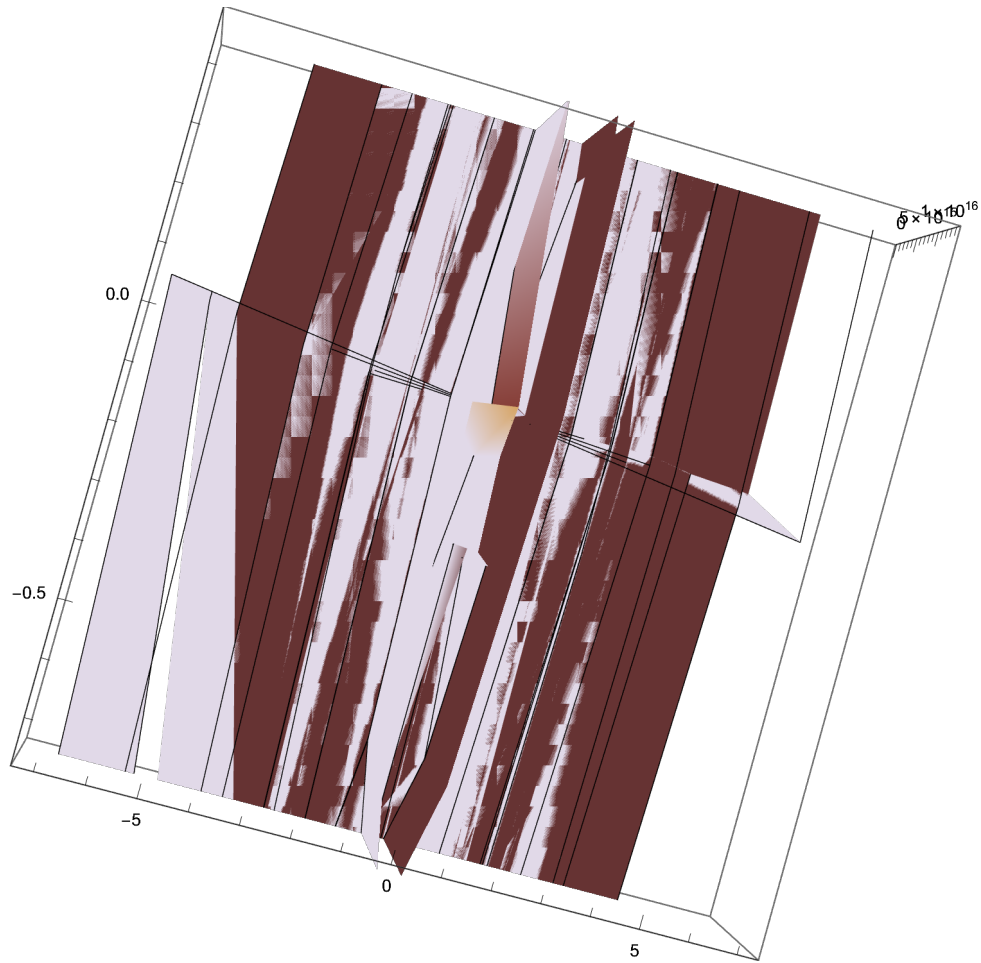
$$\text{Solve}\left[\frac{r \sqrt{\theta} \sqrt{16 \pi^3 - 20 \pi^2 \theta + 8 \pi \theta^2 - \theta^3}}{4 \pi^2} == \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\{\{\theta \rightarrow 0\}, \{\theta \rightarrow 4 \pi\}\}$$

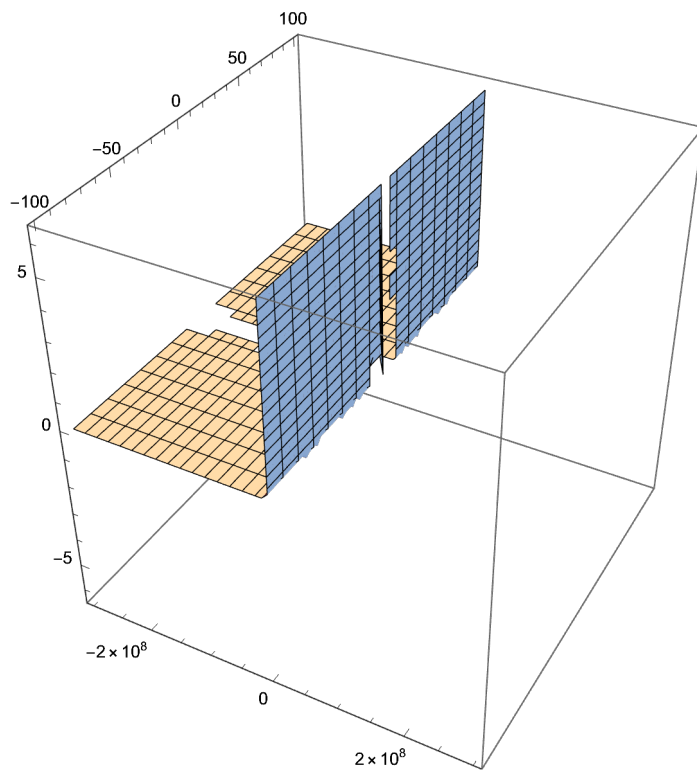
$$\text{Solve}\left[\frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi} == c(\theta / (k)), r\right]$$

$$\left\{\left\{r \rightarrow -\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right\}, \left\{r \rightarrow \frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}\right\}\right\}$$

$\text{RevolutionPlot3D}\left[\frac{2 \, c \, \pi \, \sqrt{\theta}}{\sqrt{4 \, k^2 \, \pi - k^2 \, \theta}}, \{k, -100, 100\}, \{\theta, -200 \, \pi, 200 \, \pi\}\right]$



```
ContourPlot3D[ $\frac{2 c \pi \sqrt{\theta}}{\sqrt{4 k^2 \pi - k^2 \theta}}$ ,
{c, -(2.99792458 * 10^8), (2.99792458 * 10^8)}, {k, -100, 100}, {\theta, -2 \pi, 2 \pi}]
```

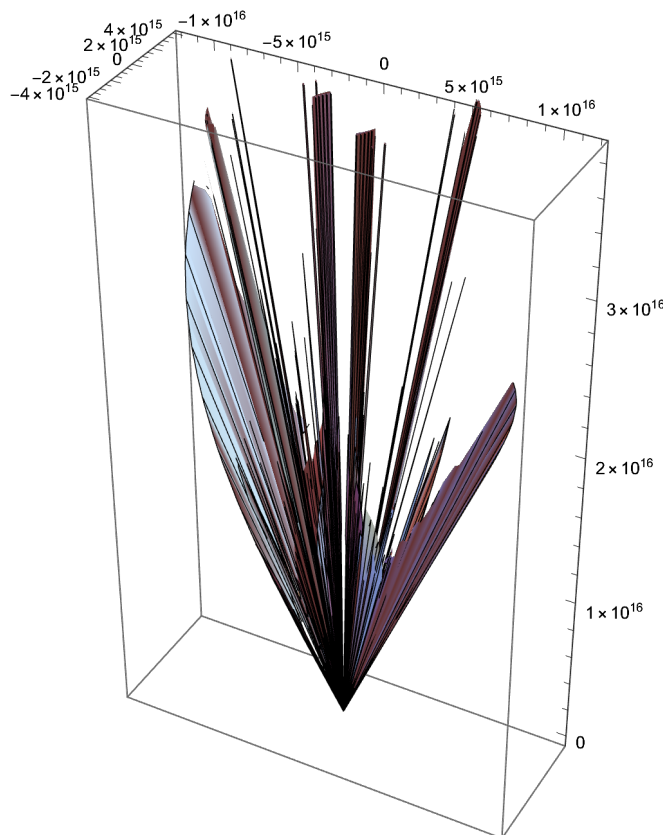


```
c := (2.99792458 * 10^8)
```

SphericalPlot3D[

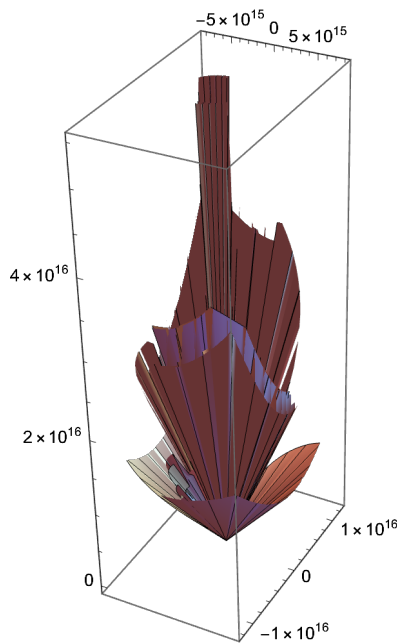
$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{16} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot 10^{16} \sin[\beta]^2 \right)} \right), \{\beta, -.125 \pi, .125 \pi\}, \{\theta, -.25 \pi, .25 \pi\}]$$





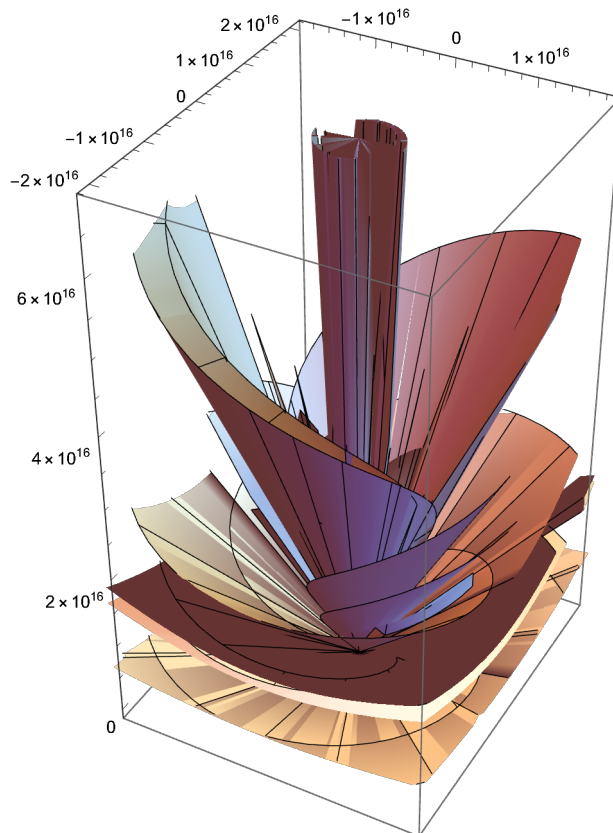
```
SphericalPlot3D[
  (Sqrt[(-1.1294090667581471`*^18 theta + 8.987551787368176`*^16 (2 (pi - Sqrt[pi^2 - pi^2 Sin[beta]^2]))^2 +
    3.5481432270250993`*^18 Sin[beta]^2)))/
  (Sqrt[(-12.566370614359172`* 2 (pi - Sqrt[pi^2 - pi^2 Sin[beta]^2]) + (2 (pi - Sqrt[pi^2 - pi^2 Sin[beta]^2]))^2 +
    39.47841760435743` Sin[beta]^2)]), {beta, -.25 pi, .25 pi}, {theta, -.5 pi, .5 pi}]
```



SphericalPlot3D[

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$

$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{16} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot 10^{16} \sin[\beta]^2 \right)} \right), \{\beta, -.5 \pi, .5 \pi\}, \{\theta, -\pi, \pi\}]$$



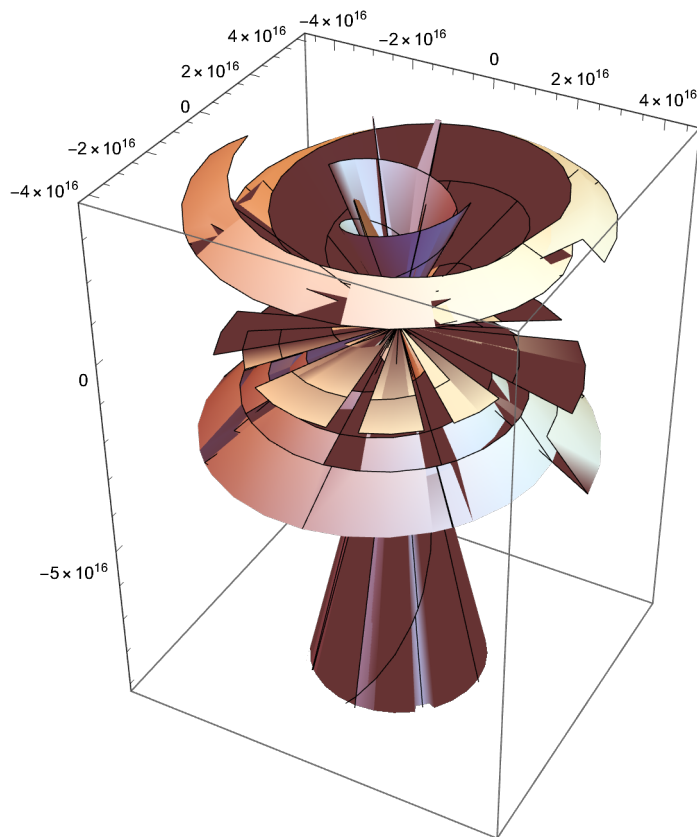
SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 + \right.} \right.$$
  

$$\left. \left. 3.5481432270250993 \cdot 10^{18} \sin^2[\beta] \right) \right) /$$
  

$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{16} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 + \right.} \right.$$
  

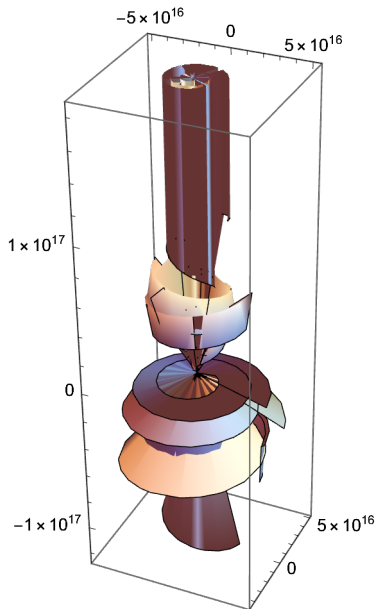
$$\left. \left. 39.47841760435743 \cdot 10^{16} \sin^2[\beta] \right) \right), \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\
\left. \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) /$$
  

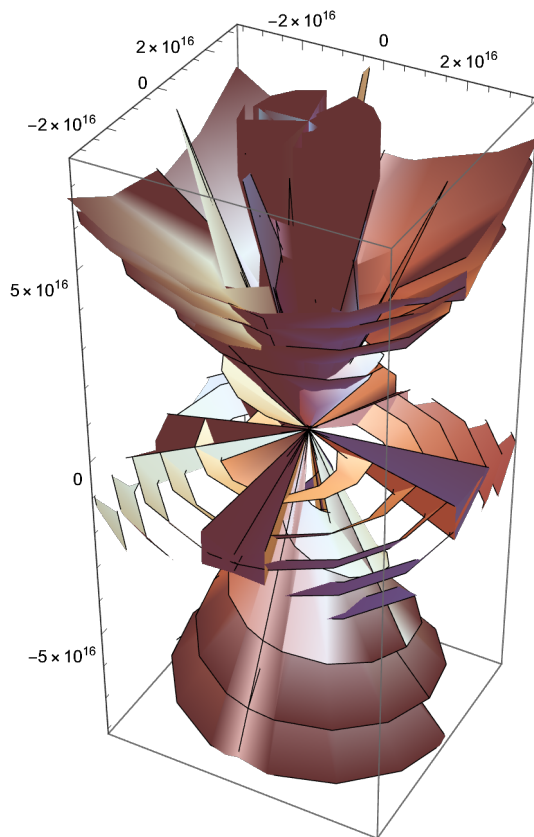
$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{17} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\
\left. \left. 39.47841760435743 \cdot 10^{17} \sin[\beta]^2 \right) \right), \{\beta, -1.5 \pi, 1.5 \pi\}, \{\theta, -3 \pi, 3 \pi\}]$$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\
\left. \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) /$$
  

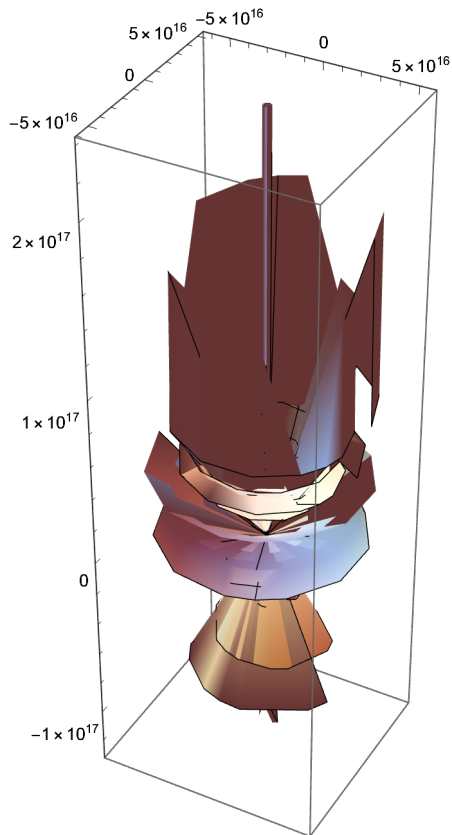
$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{16} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\
\left. \left. 39.47841760435743 \cdot 10^{16} \sin[\beta]^2 \right) \right), \{\beta, -2 \pi, 2 \pi\}, \{\theta, -4 \pi, 4 \pi\}]$$



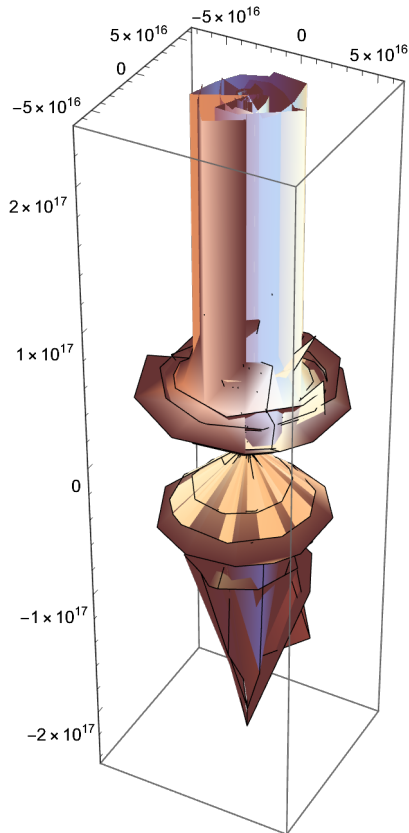
SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\
\left. \left. 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right) \right) /$$
  

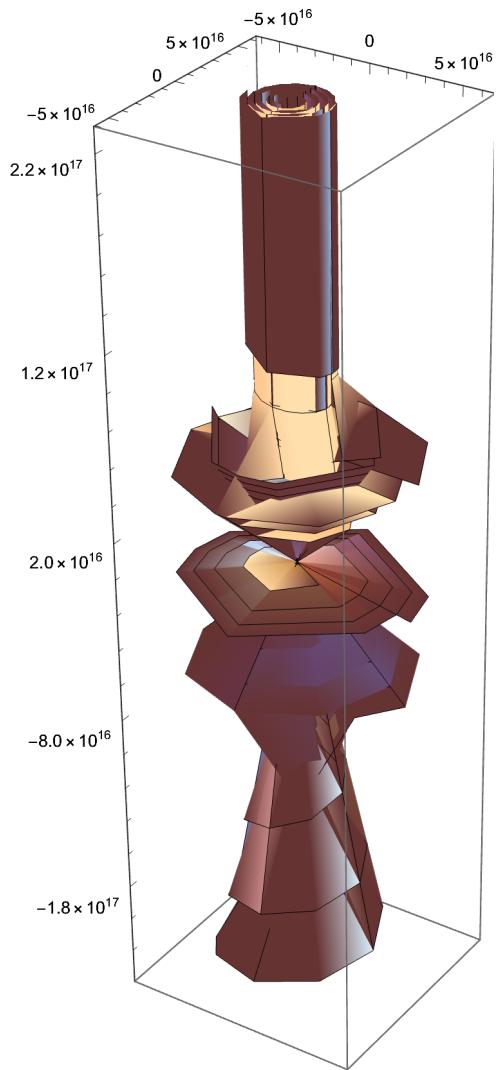
$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{17} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + \right.} \right. \\
\left. \left. 39.47841760435743 \cdot 10^{17} \sin[\beta]^2 \right) \right), \{\beta, -2.5 \pi, 2.5 \pi\}, \{\theta, -5 \pi, 5 \pi\}]$$



```
SphericalPlot3D[
  (Sqrt[(-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 (2 (π - Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
    3.5481432270250993`*^18 Sin[β]^2)))/
  (Sqrt[(-12.566370614359172` × 2 (π - Sqrt[π^2 - π^2 Sin[β]^2]) + (2 (π - Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
    39.47841760435743` Sin[β]^2)]), {β, -3 π, 3 π}, {θ, -6 π, 6 π}]
```

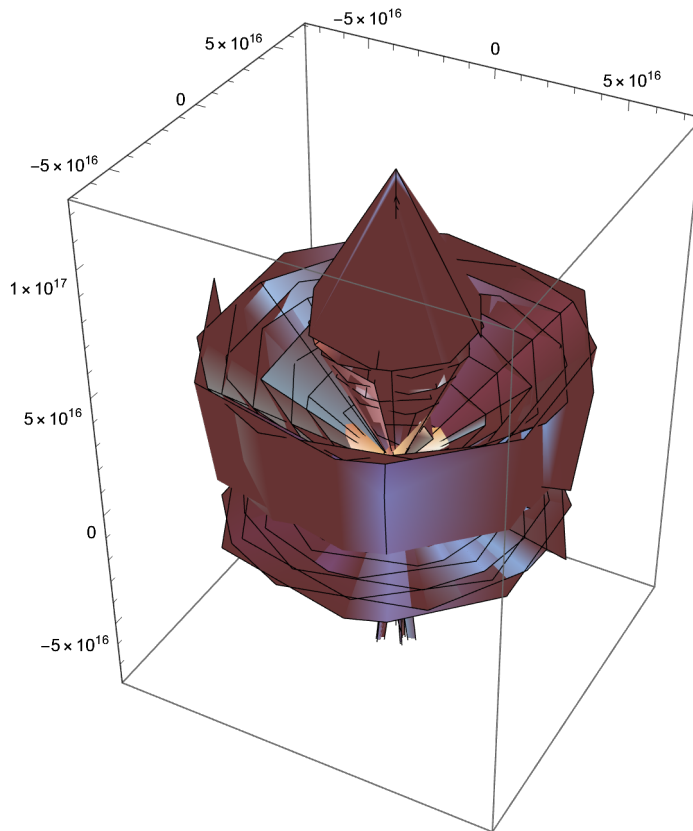


```
SphericalPlot3D[
  (Sqrt[(-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 (2 (π - Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
    3.5481432270250993`*^18 Sin[β]^2)))/
  (Sqrt[(-12.566370614359172` × 2 (π - Sqrt[π^2 - π^2 Sin[β]^2]) + (2 (π - Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
    39.47841760435743` Sin[β]^2)]), {β, -3.5 π, 3.5 π}, {θ, -7 π, 7 π}]
```





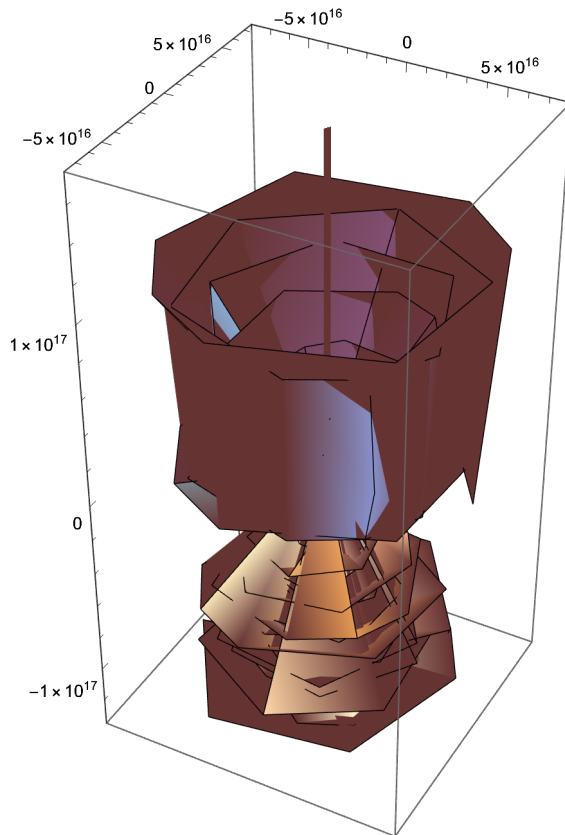
```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 (2 (π - Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
        3.5481432270250993`*^18 Sin[β]^2)
    ] /
    (
      Sqrt[
        (-12.566370614359172` × 2 (π - Sqrt[π^2 - π^2 Sin[β]^2]) + (2 (π - Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
          39.47841760435743` Sin[β]^2)
      ]
    ), {β, -4 π, 4 π}, {θ, -8 π, 8 π}]
```



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$
  

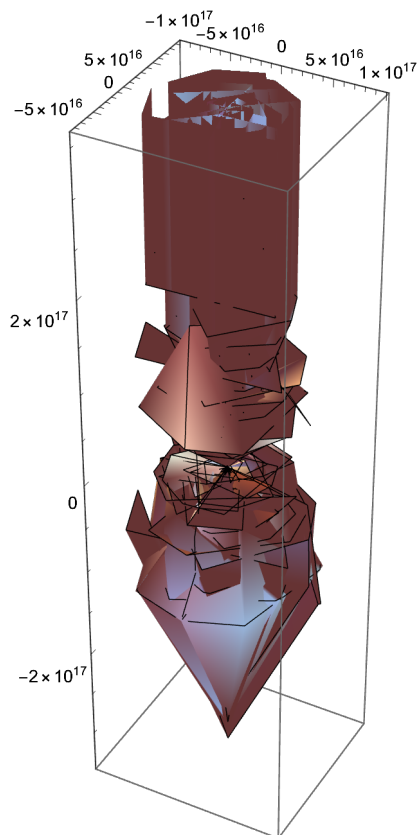
$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{17} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot 10^{17} \sin[\beta]^2 \right)} \right), \{\beta, -5 \pi, 5 \pi\}, \{\theta, -10 \pi, 10 \pi\}]$$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$
  

$$\left( \sqrt{\left( -12.566370614359172 \cdot 10^{17} \times 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + \left( 2 \left( \pi - \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) \right)^2 + 39.47841760435743 \cdot 10^{17} \sin[\beta]^2 \right)} \right), \{\beta, -6\pi, 6\pi\}, \{\theta, -12\pi, 12\pi\}]$$

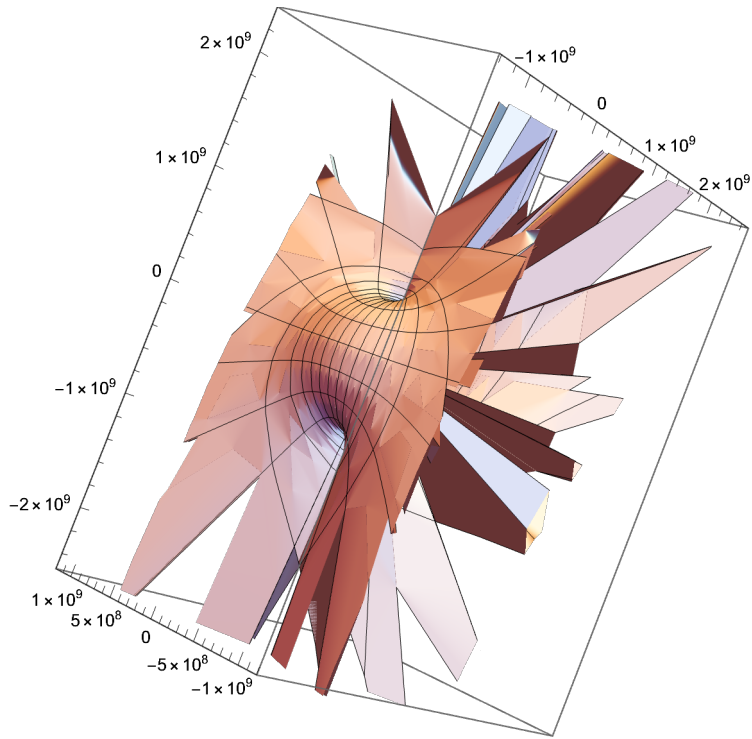


Velocity graphs

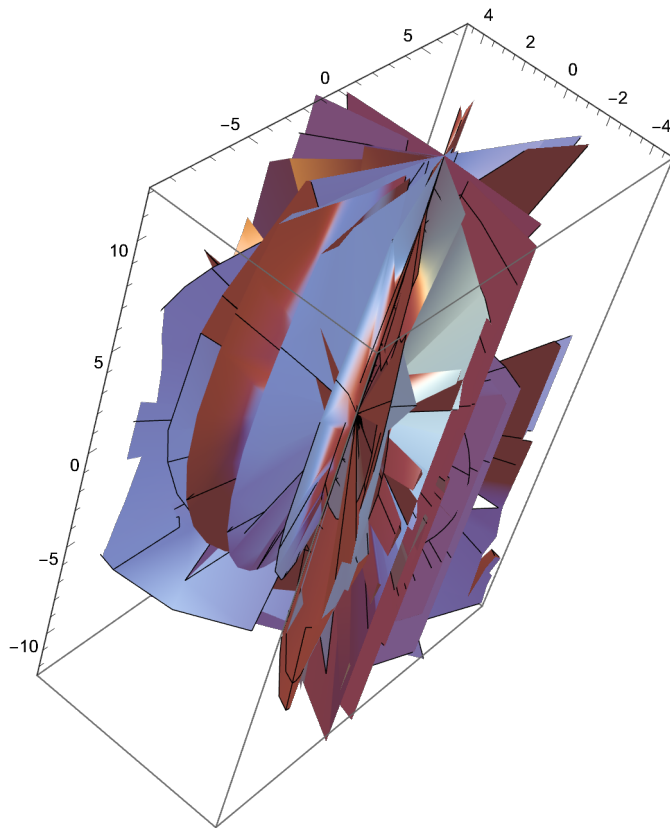
SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2 \right)} \right) /$$
  

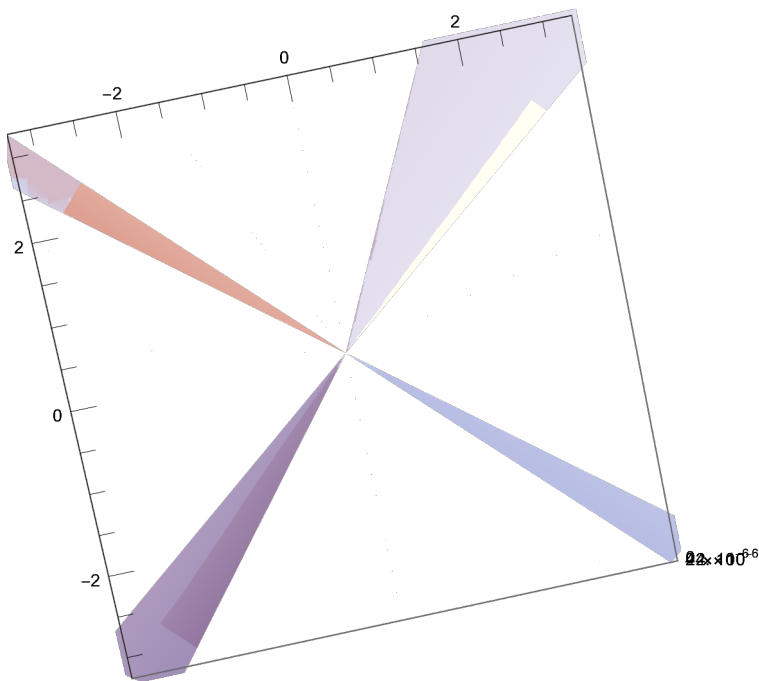
$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right),$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$



```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18 * 2 (
        pi + Sqrt[pi^2 - pi^2 Sin[beta]^2]
      ) + 8.987551787368176`*^16
      (
        2 (
          pi + Sqrt[pi^2 - pi^2 Sin[beta]^2]
        )
      )^2 + 3.5481432270250993`*^18 Sin[beta]^2
    )
  ) /
  (
    Sqrt[-12.566370614359172` theta + theta^2 + 39.47841760435743` Sin[beta]^2]
  ),
  {theta, -2 pi, 2 pi}, {beta, -pi/2, pi/2}]
```



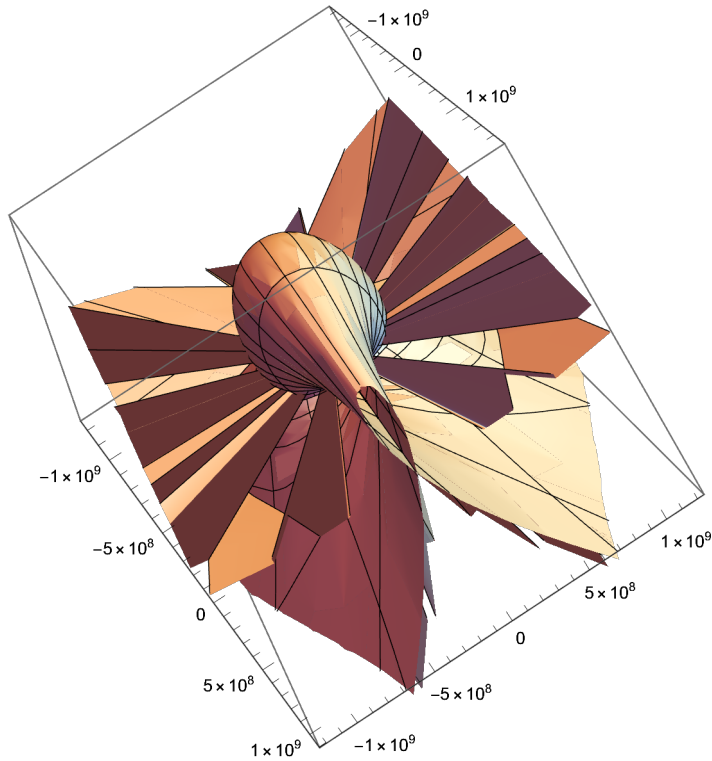
```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18 * 2 (
        Pi + Sqrt[Pi^2 - Pi^2 Sin[Beta]^2]
      ) + 8.987551787368176`*^16
      (
        2 (
          Pi + Sqrt[Pi^2 - Pi^2 Sin[Beta]^2]
        )^2 + 3.5481432270250993`*^18 Sin[Beta]^2
        )
      )
    ) /
    (
      Sqrt[
        (-12.566370614359172` (
          2 (
            Pi + Sqrt[Pi^2 - Pi^2 Sin[Beta]^2]
          )
        ) + theta^2 +
        39.47841760435743` Sin[Beta]^2
      )
    ), {theta, -2 Pi, 2 Pi}, {beta, -Pi/2, Pi/2}]
```



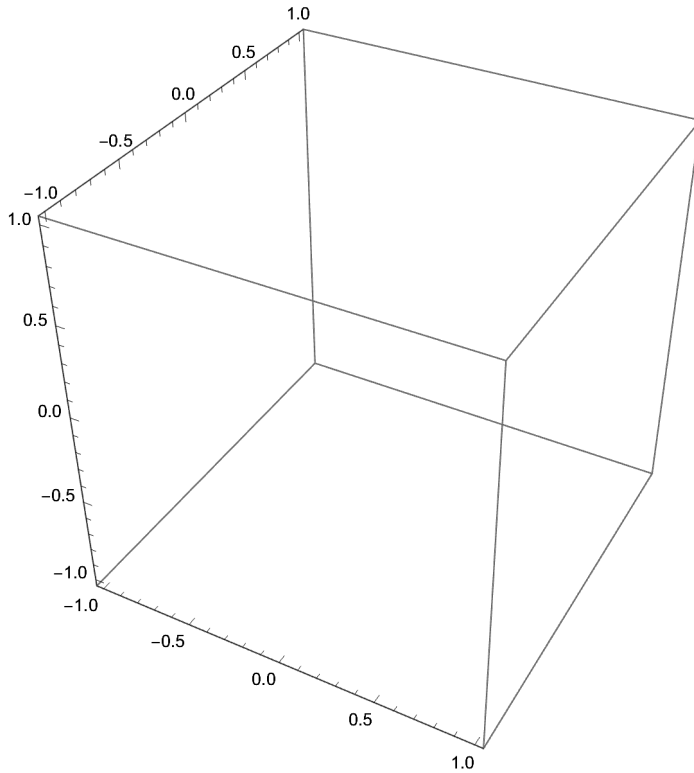
SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot \theta^{18} + 8.987551787368176 \cdot \sin^{16} \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 + 3.5481432270250993 \cdot \sin^{18}[\beta] \right)} \right) /$$
  

$$\left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin^2[\beta]} \right),$$
  
 $\{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}$ ]



```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 (2 (π + Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
        3.5481432270250993`*^18 Sin[β]^2)
    ] /
    (
      Sqrt[
        (-12.566370614359172` × 2 (π + Sqrt[π^2 - π^2 Sin[β]^2]) + θ^2 +
          39.47841760435743` Sin[β]^2)
      ], {θ, -2 π, 2 π}, {β, -π / 2, π / 2}
    ]
  ]
```





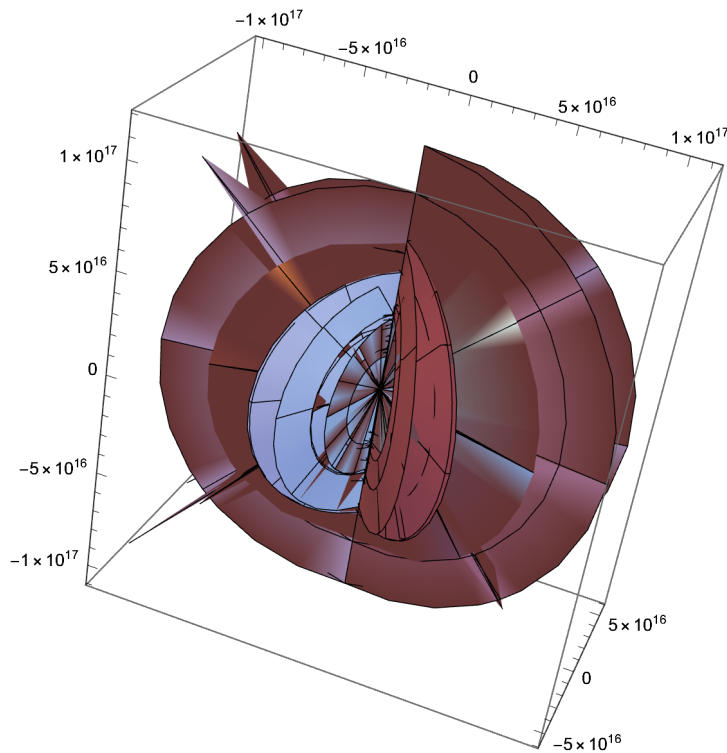
```
SphericalPlot3D[
  (
    Sqrt[
      (-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 (2 (π + Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
        3.5481432270250993`*^18 Sin[β]^2)
    ] /
    (
      Sqrt[
        (-12.566370614359172` × 2 (π + Sqrt[π^2 - π^2 Sin[β]^2]) + (2 (π + Sqrt[π^2 - π^2 Sin[β]^2]))^2 +
          39.47841760435743` Sin[β]^2)
      ]
    ), {θ, -2 π, 2 π}, {β, -π / 2, π / 2}]
```

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

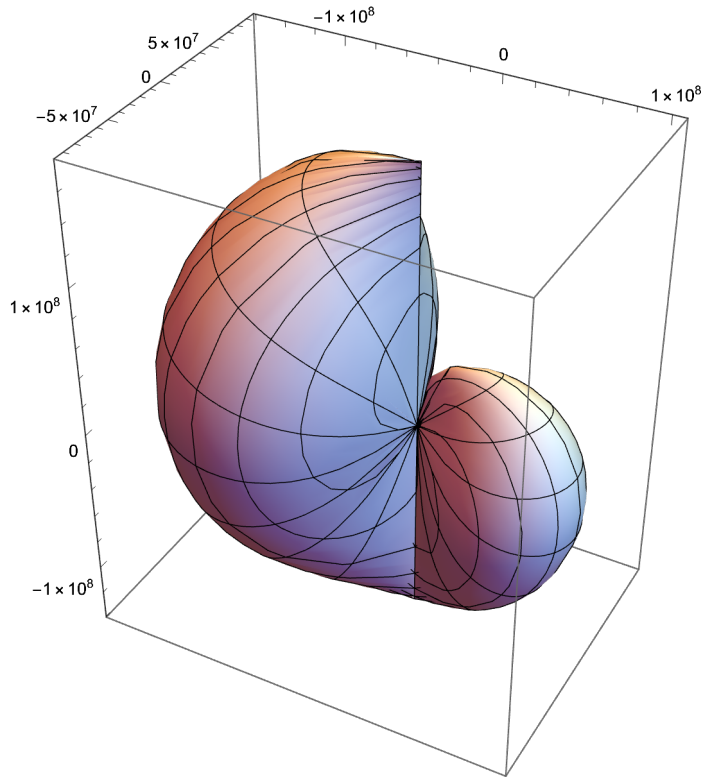
Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>



SphericalPlot3D $\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot 10^2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + \theta^2 + 39.47841760435743 \sin[\beta]^2\right)}\right)\right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$

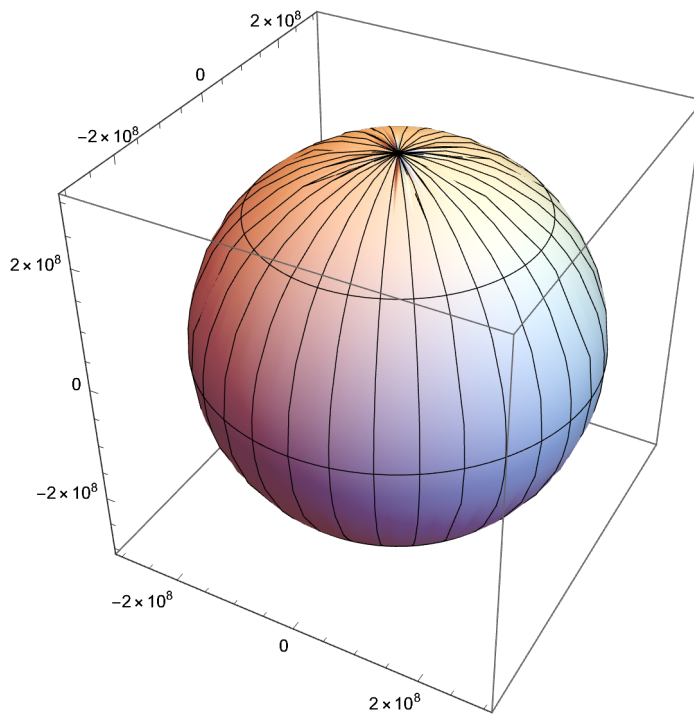


```
SphericalPlot3D[
  (

$$\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right) + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin^2[\beta]\right)} \Bigg) /$$


$$\left(\sqrt{\left(-12.566370614359172 \cdot 10^{18} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]}\right) + \theta^2 + 39.47841760435743 \cdot 10^{18} \sin^2[\beta]\right)}\right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$


```



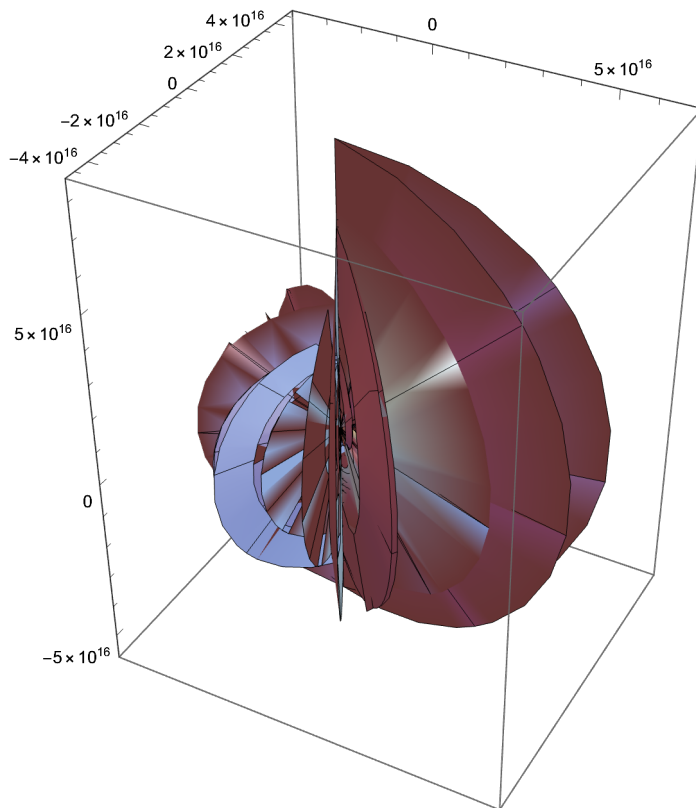
`SphericalPlot3D` $\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot 10^{16} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 39.47841760435743 \cdot \sin[\beta]^2\right)}\right)\right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

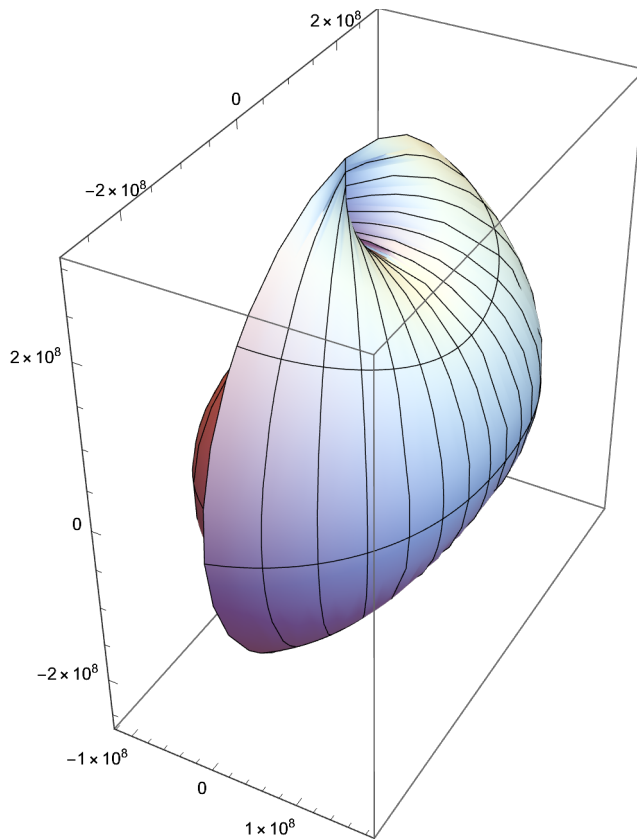
Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

Power::infy : Infinite expression  $\frac{1}{0.}$  encountered. >>

General::stop : Further output of Power::infy will be suppressed during this calculation. >>



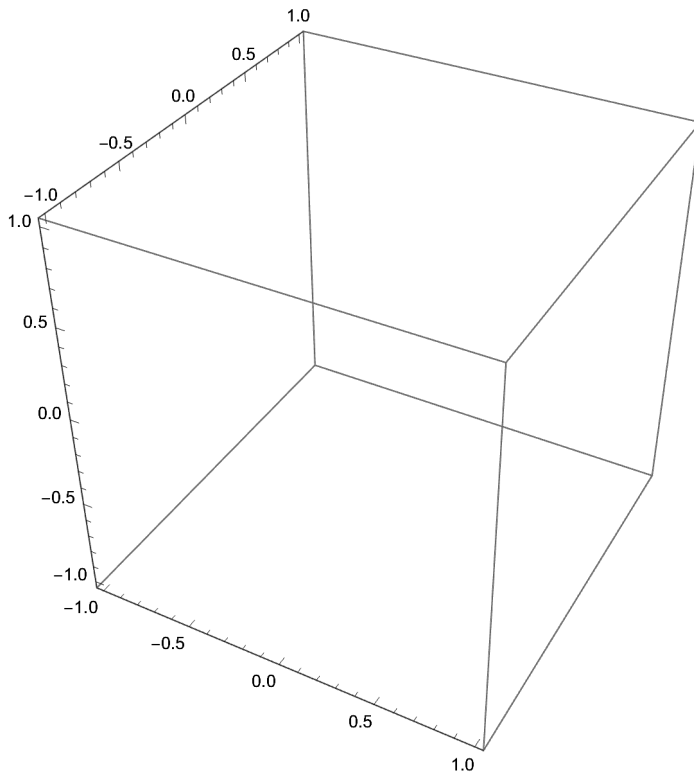
SphericalPlot3D $\left[\left(\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \theta + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)}\right) / \left(\sqrt{\left(-12.566370614359172 \cdot 10^{18} \theta + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 39.47841760435743 \cdot 10^{18} \sin[\beta]^2\right)}\right)\right], \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$



SphericalPlot3D[  

$$\left( \sqrt{\left( -1.1294090667581471 \cdot 10^{18} \times 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) + 8.987551787368176 \cdot 10^{16} \theta^2 + 3.5481432270250993 \cdot 10^{18} \sin^2[\beta] \right)} \right) /$$
  

$$\left( \sqrt{\left( -12.566370614359172 \cdot \theta + \left( 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin^2[\beta]} \right) \right)^2 + 39.47841760435743 \cdot \sin^2[\beta] \right)} \right), \{\theta, -2\pi, 2\pi\}, \{\beta, -\pi/2, \pi/2\}]$$



```
SphericalPlot3D[
  (

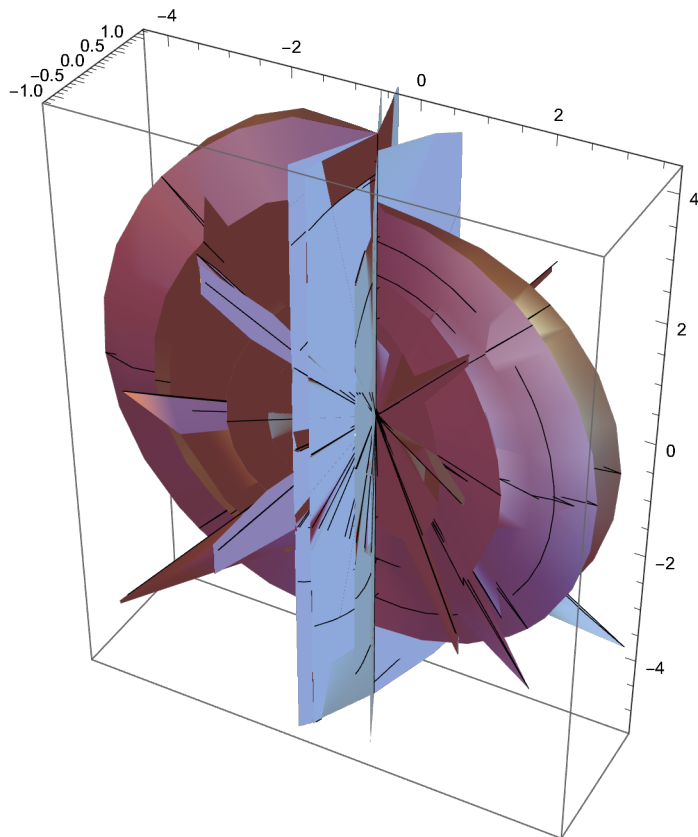
$$\sqrt{\left(-1.1294090667581471 \cdot 10^{18} \times 2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right) + 8.987551787368176 \cdot 10^{16}\right.}$$


$$\left.\left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 + 3.5481432270250993 \cdot 10^{18} \sin[\beta]^2\right)} /$$

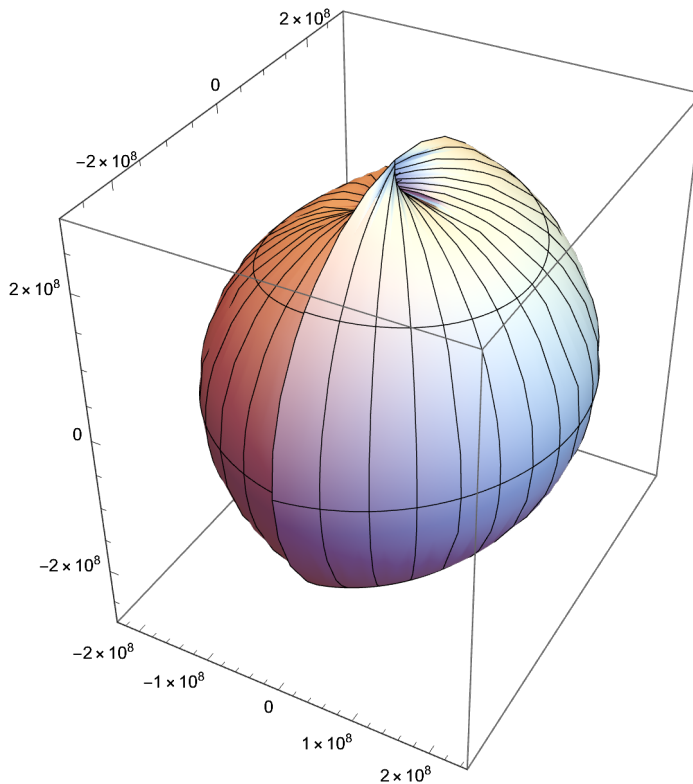

$$\sqrt{\left(-12.566370614359172 \cdot \theta + \left(2 \left(\pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2}\right)\right)^2 +\right.}$$


$$\left.39.47841760435743 \cdot \sin[\beta]^2\right)}, \{\theta, -2 \pi, 2 \pi\}, \{\beta, -\pi / 2, \pi / 2\}]$$


```



```
SphericalPlot3D[
  (Sqrt[(-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 × 2 (π + √(π² - π² Sin[β]²))² +
    3.5481432270250993`*^18 Sin[β]²)))/
  (Sqrt[(-12.566370614359172` θ + (2 (π + √(π² - π² Sin[β]²))² +
    39.47841760435743` Sin[β]²))], {θ, -2 π, 2 π}, {β, -π / 2, π / 2}]
```



```
SphericalPlot3D[
  (Sqrt[(-1.1294090667581471`*^18 θ + 8.987551787368176`*^16 × 2 (π + √(π² - π² Sin[β]²))² +
    3.5481432270250993`*^18 Sin[β]²)))/
  (Sqrt[(-12.566370614359172` θ + (2 (π + √(π² - π² Sin[β]²))² +
    39.47841760435743` Sin[β]²))], {θ, -2 π, 2 π}, {β, -π / 2, π / 2}]
```



$$D\left[k \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{k (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}$$

$$\mathbf{r} := \left( \sqrt{1 - \frac{v^2}{(c)^2}} \right) \boldsymbol{\xi}$$

$$\theta := k(t)$$

$$\text{Solve}\left[\frac{2\pi\left(2\pi r-2\pi\sqrt{r^2-(\eta)^2}\right)}{\theta^2}==\frac{4\pi r^2-2r^2\theta}{2\sqrt{4\pi r^2\theta-r^2\theta^2}},v\right]$$

$$\frac{2 \pi \frac{(2 \pi r - 2 \pi r_1)}{\theta}}{\theta}$$

$$D\left[k \frac{\sqrt{4 \pi r^2 \theta - r^2 \theta^2}}{2 \pi}, \theta\right]$$

$$\frac{k(4\pi r^2 - 2r^2\theta)}{4\pi\sqrt{4\pi r^2\theta - r^2\theta^2}}$$

$$k \frac{\left( 2 \pi r \left( \sqrt{1 - \frac{v^2}{(c)^2}} \right) - 2 \pi x \right)}{\theta}$$

$$\text{Solve} \left[ \frac{\frac{\theta}{\sqrt{1 - \frac{v^2}{(c)^2}}}}{\sqrt{1 - \frac{v^2}{(c)^2}}} == \frac{k (4 \pi r^2 - 2 r^2 \theta)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v \right]$$

$$\left\{ \left\{ v \rightarrow \text{Root} \left[ -4.216470103348157002649971815393 \times 10^{131} + \frac{8.432940206696313101045715680419 \times 10^{130} x^2}{r^2} + 4.238858080243061632839516848970 \times 10^{132} / \right. \right.$$
$$\left. \left( 12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \theta \right) - 2.684288237388216155696380581377 \times 10^{130} \theta - 2.136088708318827900033959336776 \times 10^{129} \theta^2 - 1.69204412431095 \times 10^{112} \theta^3 - 5.4107759072974008435227506871481 \times 10^{127} \theta^4 + \frac{1}{r^2} 2.684288237388215879568552148305 \times 10^{130} \right.$$
$$\left. \times \sqrt{\left( 12.566370614359172953850573533118 r^2 \theta - 1.00000000000000000000000000000000 r^2 \theta^2 \right)} - \left( 3.373176082678525587410749174984 \times 10^{131} x \right. \right.$$
$$\left. \sqrt{\left( 12.566370614359172953850573533118 r^2 \theta - \right.} \right.$$





$$\begin{aligned}
& 4.238858080243061632839516848970 \times 10^{132} / \\
& (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \theta) - \\
& 2.684288237388216155696380581377 \times 10^{130} \theta - \\
& 2.136088708318827900033959336776 \times 10^{129} \theta^2 - \\
& 1.69204412431095 \times 10^{112} \theta^3 - \\
& 5.4107759072974008435227506871481 \times 10^{127} \theta^4 + \\
& \frac{1}{r^2} 2.684288237388215879568552148305 \times 10^{130} \\
& \times \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) - \\
& (3.373176082678525587410749174984 \times 10^{131} \times \\
& \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) ) / \\
& (r^2 (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \theta) ) + \frac{1}{r^2} 4.2721774166376552542825626603082 \times 10^{129} \\
& \times \theta \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) + \\
& (2.8148734181032390479027151232292 \times 10^{114} - \\
& \frac{1.8765822787354933772571250979976 \times 10^{114} x^2}{r^2} - \\
& \frac{1}{r^2} 2.986673457794067498599348047634 \times 10^{113} \times \\
& \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) + \\
& (3.753164557470987140595433494997 \times 10^{114} \times \\
& \sqrt{(12.566370614359172953850573533118 r^2 \\
& \theta - 1.00000000000000000000000000000000 r^2 \theta^2) ) / (r^2 \\
& (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \theta) ) - \frac{1}{r^2} 4.7534384420928906688467313657196 \times 10^{112} \\
& \times \theta \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) ) \\
& \mp 1^2 + \left( -3.1319690664364097084714540587558 \times 10^{97} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{1.0439896888121370251787709015348 \times 10^{97} x^2}{r^2} \right) \mp 1^4 + \\
& 1.1615951857762235174602622821929 \times 10^{80} \mp 1^6 \&, 3 \Big] \Big\}, \\
& \left\{ v \rightarrow \text{Root} \left[ -4.216470103348157002649971815393 \times 10^{131} + \right. \right. \\
& \quad \left. \frac{8.432940206696313101045715680419 \times 10^{130} x^2}{r^2} + \right. \\
& 4.238858080243061632839516848970 \times 10^{132} / \\
& \quad (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \theta) - \\
& 2.684288237388216155696380581377 \times 10^{130} \theta - \\
& 2.136088708318827900033959336776 \times 10^{129} \theta^2 - \\
& 1.69204412431095 \times 10^{112} \theta^3 - \\
& 5.4107759072974008435227506871481 \times 10^{127} \theta^4 + \\
& \frac{1}{r^2} 2.684288237388215879568552148305 \times 10^{130} \\
& \quad \times \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) -} \\
& (3.373176082678525587410749174984 \times 10^{131} x \\
& \quad \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2)}) / \\
& (r^2 (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \quad \theta) + \frac{1}{r^2} 4.2721774166376552542825626603082 \times 10^{129} \\
& \quad \times \theta \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) +} \\
& \left( 2.8148734181032390479027151232292 \times 10^{114} - \right. \\
& \quad \left. \frac{1.8765822787354933772571250979976 \times 10^{114} x^2}{r^2} - \right. \\
& \frac{1}{r^2} 2.986673457794067498599348047634 \times 10^{113} x \\
& \quad \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) +} \\
& (3.753164557470987140595433494997 \times 10^{114} x \\
& \quad \sqrt{(12.566370614359172953850573533118 r^2 \\
& \quad \theta - 1.00000000000000000000000000000000 r^2 \theta^2)}) / (r^2 \\
& (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \quad \theta) - \frac{1}{r^2} 4.7534384420928906688467313657196 \times 10^{112}
\end{aligned}$$





$$x := r - \frac{r \theta}{2 \pi}$$

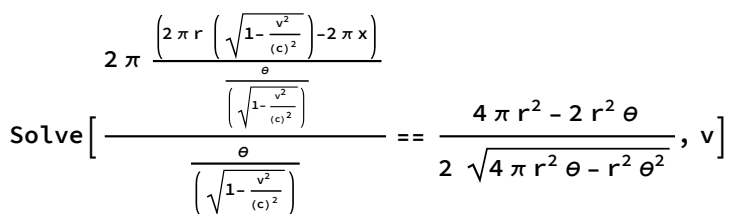
$$\text{RevolutionPlot3D}[\text{Root}[$$

$$\begin{aligned}
& -4.21647010334815700264997181539348253021191869093890165`31.039947820651026*^{131} \\
& + \frac{1}{r^2} \\
& 8.43294020669631310104571568041853996480888272572410532`31.90917954038201*^{130} \\
& x^2 + \\
& 4.2388580802430616328395168489698310541847495871681420192`30.653907035278717*^{132} / \\
& (12.5663706143591729538505735331180115367886775975004232838998`31.90917954038201 - 1.`31.90917954038201 \theta) - \\
& 2.68428823738821615569638058137698794428193150015282769`30.653907035278717*^{130} \\
& \theta - \\
& 2.1360887083188279000339593367755863975675677421987276`30.678730619003755*^{129} \\
& \theta^2 - 1.6920441243109525639694280607586791`14.828000558248899*^{112} \theta^3 - \\
& 5.410775907297400843522750687148061274448586061633469676696799341148595`31.90917954038201*^{127} \theta^4 + \frac{1}{r^2}
\end{aligned}$$



$$\begin{aligned}
& 2.68428823738821587956855214830523396329791317421630874`31.210209536046005* \\
& \quad ^{130} \\
& \times \\
& \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998`31.90917954\right. \\
& \quad \left.038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2\right) -} \\
& \left(3.37317608267852558741074917498380056731522153667370724`31.13102828999839*^{1\right. \\
& \quad \left.31 \times\right. \\
& \quad \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998`31.909179\right. \\
& \quad \left.54038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2\right)} / \left(r^2\right. \\
& \quad \left.(12.5663706143591729538505735331180115367886775975004232838998`31.9091795\right. \\
& \quad \left.4038201 - 1.`31.90917954038201 \theta)\right) + \frac{1}{r^2} \\
& 4.2721774166376552542825626603081738764587872286506608`31.90917954038201*^{1\right. \\
& \quad \left.29\right. \\
& \times \\
& \theta \\
& \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998`31.90917954\right. \\
& \quad \left.038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2\right) +} \\
& \left(2.81487341810323904790271512322916459769206163016662605819`31.90917954038201\right. \\
& \quad \left.*^{114} - \frac{1}{r^2}\right. \\
& \quad 1.87658227873549337725712509799758878149376167997057124208`31.9091795403\right. \\
& \quad \left.82027*^{114} x^2 - \frac{1}{r^2}\right. \\
& \quad 2.9866734577940674985993480476343925829853057792073646239`31.21020953604\right. \\
& \quad \left.6023*^{113} \times\right. \\
& \quad \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998`31.9091\right. \\
& \quad \left.7954038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2\right) +} \\
& \quad \left(3.75316455747098714059543349499700426760740839308096603667`31.1310282899\right. \\
& \quad \left.9839*^{114} \times\right. \\
& \quad \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998`31.90\right. \\
& \quad \left.917954038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2\right)} / \left(r^2\right. \\
& \quad \left.(12.5663706143591729538505735331180115367886775975004232838998`31.9091\right. \\
& \quad \left.7954038201 - 1.`31.90917954038201 \theta)\right) - \frac{1}{r^2} \\
& \quad 4.753438442092890668846731365719623771383697652080416222`31.909179540382\right. \\
& \quad \left.01*^{112} \times \theta\right. \\
& \quad \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998`31.9091\right. \\
& \quad \left.7954038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2\right)} \#1^2 +
\end{aligned}$$

$$8201*^{80} \#1^6 \&, 6], \{r, -1, 1\}, \{\theta, -2\pi, 2\pi\}]$$



$$\left\{ \left\{ v \rightarrow \text{Root} \left[ -4.216470103348157002649971815393 \times 10^{131} + \frac{8.432940206696313101045715680419 \times 10^{130} x^2}{r^2} + 4.238858080243061632839516848970 \times 10^{132} / (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \theta) - 2.684288237388216155696380581377 \times 10^{130} \theta - 2.136088708318827900033959336776 \times 10^{129} \theta^2 - 1.69204412431095 \times 10^{112} \theta^3 - 5.4107759072974008435227506871481 \times 10^{127} \theta^4 + \right. \right.$$



$$\begin{aligned}
& 4.238858080243061632839516848970 \times 10^{132} / \\
& (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \theta) - \\
& 2.684288237388216155696380581377 \times 10^{130} \theta - \\
& 2.136088708318827900033959336776 \times 10^{129} \theta^2 - \\
& 1.69204412431095 \times 10^{112} \theta^3 - \\
& 5.4107759072974008435227506871481 \times 10^{127} \theta^4 + \\
& \frac{1}{r^2} 2.684288237388215879568552148305 \times 10^{130} \\
& \times \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) - \\
& (3.373176082678525587410749174984 \times 10^{131} \times \\
& \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2)}) / \\
& (r^2 (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \theta) + \frac{1}{r^2} 4.2721774166376552542825626603082 \times 10^{129} \\
& \times \theta \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) + \\
& (2.8148734181032390479027151232292 \times 10^{114} - \\
& \frac{1.8765822787354933772571250979976 \times 10^{114} x^2}{r^2} - \\
& \frac{1}{r^2} 2.986673457794067498599348047634 \times 10^{113} \times \\
& \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2) + \\
& (3.753164557470987140595433494997 \times 10^{114} \times \\
& \sqrt{(12.566370614359172953850573533118 r^2 \\
& \theta - 1.00000000000000000000000000000000 r^2 \theta^2)}) / (r^2 \\
& (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \theta) - \frac{1}{r^2} 4.7534384420928906688467313657196 \times 10^{112} \\
& \times \theta \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& 1.00000000000000000000000000000000 r^2 \theta^2)}) \\
& \mp 1^2 + \left( -3.1319690664364097084714540587558 \times 10^{97} + \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{1.0439896888121370251787709015348 \times 10^{97} x^2}{r^2} \right) \mp 1^4 + \\
& 1.1615951857762235174602622821929 \times 10^{80} \mp 1^6 \&, 2 \Big] \Big\}, \\
& \left\{ v \rightarrow \text{Root} \left[ -4.216470103348157002649971815393 \times 10^{131} + \right. \right. \\
& \quad \left. \frac{8.432940206696313101045715680419 \times 10^{130} x^2}{r^2} + \right. \\
& 4.238858080243061632839516848970 \times 10^{132} / \\
& \quad (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \theta) - \\
& 2.684288237388216155696380581377 \times 10^{130} \theta - \\
& 2.136088708318827900033959336776 \times 10^{129} \theta^2 - \\
& 1.69204412431095 \times 10^{112} \theta^3 - \\
& 5.4107759072974008435227506871481 \times 10^{127} \theta^4 + \\
& \frac{1}{r^2} 2.684288237388215879568552148305 \times 10^{130} \\
& \quad \times \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) -} \\
& (3.373176082678525587410749174984 \times 10^{131} x \\
& \quad \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) \Big) \Big/ \\
& (r^2 (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \quad \theta) + \frac{1}{r^2} 4.2721774166376552542825626603082 \times 10^{129} \\
& \quad \times \theta \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) +} \\
& \left( 2.8148734181032390479027151232292 \times 10^{114} - \right. \\
& \quad \left. \frac{1.8765822787354933772571250979976 \times 10^{114} x^2}{r^2} - \right. \\
& \frac{1}{r^2} 2.986673457794067498599348047634 \times 10^{113} x \\
& \quad \sqrt{(12.566370614359172953850573533118 r^2 \theta - \\
& \quad 1.00000000000000000000000000000000 r^2 \theta^2) +} \\
& (3.753164557470987140595433494997 \times 10^{114} x \\
& \quad \sqrt{(12.566370614359172953850573533118 r^2 \\
& \quad \theta - 1.00000000000000000000000000000000 r^2 \theta^2) \Big) \Big/ (r^2 \\
& (12.566370614359172953850573533118 - 1.00000000000000000000000000000000 \\
& \quad \theta) - \frac{1}{r^2} 4.7534384420928906688467313657196 \times 10^{112}
\end{aligned}$$









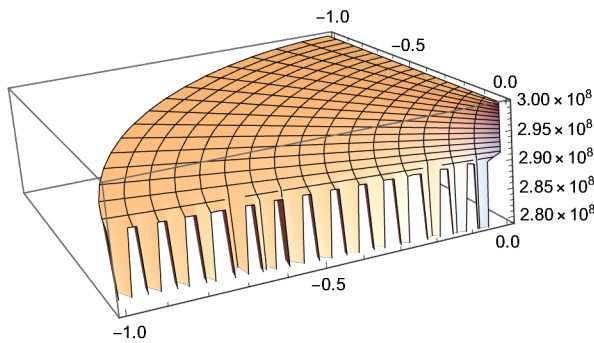
[illegible]

$$X :=$$
`RevolutionPlot3D[Root[`

$$\begin{aligned}
& -4.21647010334815700264997181539348253021191869093890165`31.039947820651026*^131 \\
& + \frac{1}{r^2} \\
& 8.43294020669631310104571568041853996480888272572410532`31.90917954038201*^130 \\
& x^2 + \\
& 4.2388580802430616328395168489698310541847495871681420192`30.653907035278717*^132 / \\
& (12.5663706143591729538505735331180115367886775975004232838998`31.90917954038201 - 1.`31.90917954038201 \theta) - \\
& 2.68428823738821615569638058137698794428193150015282769`30.653907035278717*^130 \\
& \theta -
\end{aligned}$$

$$\begin{aligned}
& 2.1360887083188279000339593367755863975675677421987276`30.678730619003755*^129 \\
& \quad \theta^2 - 1.6920441243109525639694280607586791`14.828000558248899*^112 \theta^3 - \\
& 5.410775907297400843522750687148061274448586061633469676696799341148595`31.90\backslash \\
& \quad 917954038201*^127 \theta^4 + \frac{1}{r^2} \\
& 2.68428823738821587956855214830523396329791317421630874`31.210209536046005*\backslash \\
& \quad ^{130} \\
& x \\
& \sqrt{(12.5663706143591729538505735331180115367886775975004232838998`31.90917954\backslash \\
& \quad 038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2) - \\
& (3.37317608267852558741074917498380056731522153667370724`31.13102828999839*^1\backslash \\
& \quad 31 x \\
& \sqrt{(12.5663706143591729538505735331180115367886775975004232838998`31.909179\backslash \\
& \quad 54038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2)) / (r^2 \\
& (12.5663706143591729538505735331180115367886775975004232838998`31.9091795\backslash \\
& \quad 4038201 - 1.`31.90917954038201 \theta)) + \frac{1}{r^2} \\
& 4.2721774166376552542825626603081738764587872286506608`31.90917954038201*^1\backslash \\
& \quad 29 \\
& x \\
& \theta \\
& \sqrt{(12.5663706143591729538505735331180115367886775975004232838998`31.90917954\backslash \\
& \quad 038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2) + \\
& (2.81487341810323904790271512322916459769206163016662605819`31.90917954038201\backslash \\
& \quad *^114 - \frac{1}{r^2} \\
& 1.87658227873549337725712509799758878149376167997057124208`31.9091795403\backslash \\
& \quad 82027*^114 x^2 - \frac{1}{r^2} \\
& 2.9866734577940674985993480476343925829853057792073646239`31.21020953604\backslash \\
& \quad 6023*^113 x \\
& \sqrt{(12.5663706143591729538505735331180115367886775975004232838998`31.9091\backslash \\
& \quad 7954038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2) + \\
& (3.75316455747098714059543349499700426760740839308096603667`31.1310282899\backslash \\
& \quad 9839*^114 x \\
& \sqrt{(12.5663706143591729538505735331180115367886775975004232838998`31.90\backslash \\
& \quad 917954038201 r^2 \theta - 1.`31.90917954038201 r^2 \theta^2)) / (r^2 \\
& (12.5663706143591729538505735331180115367886775975004232838998`31.9091\backslash \\
& \quad 7954038201 - 1.`31.90917954038201 \theta)) - \frac{1}{r^2} \\
& 4.753438442092890668846731365719623771383697652080416222`31.909179540382\backslash
\end{aligned}$$

$$\begin{aligned}
 & 01 \cdot 112 \times \theta \\
 & \sqrt{\left(12.5663706143591729538505735331180115367886775975004232838998 \cdot 31.9091 \cdot \right. \\
 & \quad \left. 7954038201 r^2 \theta - 1. \cdot 31.90917954038201 r^2 \theta^2\right) \cdot 1^2 +} \\
 & \left(-3.131969066436409708471454058755800746752224921710902726416 \cdot 31.90917954038 \cdot \right. \\
 & \quad \left. 201 \cdot 1^97 + \frac{1}{r^2}\right. \\
 & \quad \left.1.0439896888121370251787709015348424061239037863640419974924 \cdot 31.90917954 \cdot \right. \\
 & \quad \left.038201 \cdot 1^97 x^2\right) \cdot 1^4 + \\
 & 1.1615951857762235174602622821929494233422786880592713061219311 \cdot 31.9091795403 \cdot \\
 & 8201 \cdot 1^80 \cdot 1^6 \&, 6], \{r, -1, 1\}, \{\theta, -2 \pi, 2 \pi\}]
 \end{aligned}$$



$$x := r - \frac{r \theta}{2 \pi}$$

$$\text{Solve}\left[\frac{k \left(2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2}\right)}{\theta^2} == \frac{k \left(4 \pi r^2 - 2 r r \left(\sqrt{1 - \frac{v^2}{(c)^2}}\right) k \left(\theta / \sqrt{1 - \frac{v^2}{(c)^2}}\right)\right)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, v\right]$$

{{}}

$$\begin{aligned}
 & \text{Solve}\left[\frac{k \left(2 \pi r - 2 \pi \sqrt{r^2 - (\eta)^2}\right)}{\theta^2} == \right. \\
 & \quad \left. \frac{k \left(4 \pi r^2 - 2 r r \left(\sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}\right) k \left(\theta / \sqrt{1 - \frac{v^2}{(c \text{ (meters/second)})^2}}\right)\right)}{4 \pi \sqrt{4 \pi r^2 \theta - r^2 \theta^2}}, r\right]
 \end{aligned}$$

[illegible]

$$E = h \nu = \frac{h (c^2 + r^2)}{2 r^2} = \frac{h \left( c^2 + \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{\theta}}{\sqrt{4 \pi - \theta}} \right)^2} = \frac{h \left( c^2 + \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2}$$

$$\nu = \frac{1}{\theta} = \frac{1}{\left( \frac{4 \pi r^2}{c^2 + r^2} \right)}$$

$$\frac{h \left( c^2 + \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2} =$$

$$\frac{h \left( c^2 + \left( \frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4 \pi + \theta}} \right)^2 \right)}{2 \left( \frac{c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)}}{\sqrt{4 \pi - \theta}} \right)^2} = \left( h \left( c^2 + \left( \frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4 \pi + \theta}} \right)^2 \right) \right) / \left( \left( c - \left( \sqrt{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2} \right) \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \right)$$

$$\left( c + \left( \sqrt{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2} \right) / \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \right) / \left( \sqrt{-4 \pi + \theta} \right)^2 \right) /$$

$$\left( 2 \left( \left( c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right) / \left( \sqrt{4 \pi - \left( \frac{4 \pi}{3} - (-4 \pi^2 + 12 \pi^2 \sin[\beta]^2) \right)} \right) \right) \right)$$

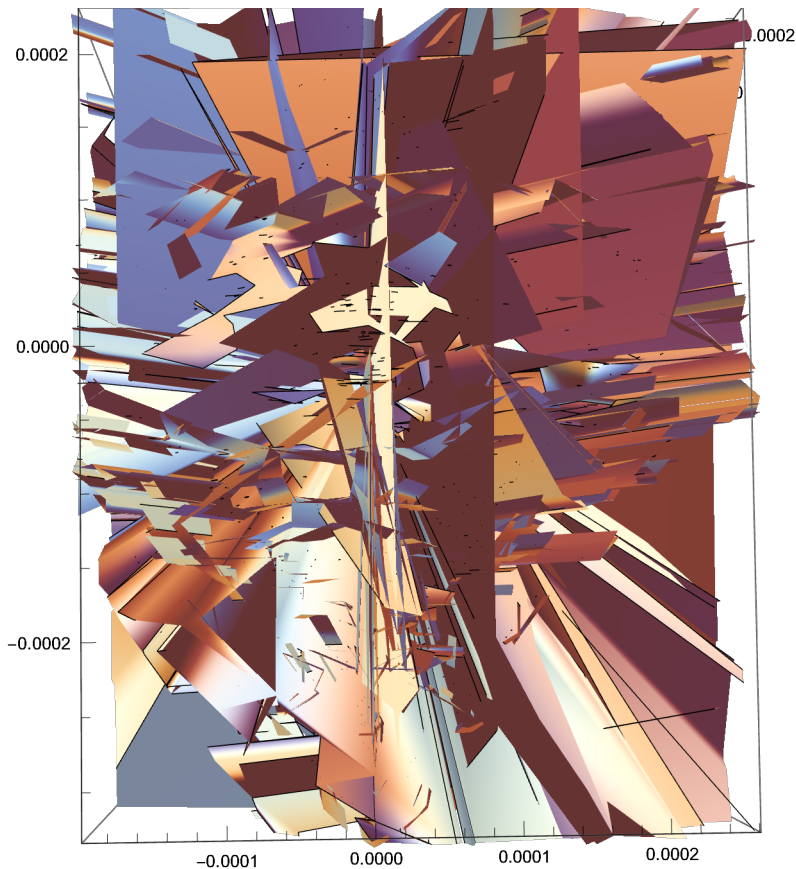
$$\left( 6 \left( -\pi^3 + 18 \pi^3 \sin[\beta]^2 + 3 \sqrt{3} \right. \right.$$

$$\left. \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} + \frac{2}{3} \left( -\pi^3 + 18 \pi^3 \right.$$

$$\left. \sin[\beta]^2 + 3 \sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11 \pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \left. \right) \left. \right) \left. \right) \left. \right)^2$$

SphericalPlot3D[  

$$\left( h \left( c^2 + \left( i c^3 \sqrt{\theta} \right) / \left( (c - (\sqrt{-1.1294090667581471} \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)) / (\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2})) \right. \right. \right. \\
\left. \left( c + (\sqrt{-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2}) / (\sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2}) \right) \sqrt{-4\pi + \theta} \right)^2 \right) / \\
\left( 2 \left( \left( c \sqrt{2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right)} \right) / \left( \sqrt{4\pi - \left( \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) \right)} \right. \right. \right. \\
\left. \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) \right)^2 \right) \right), \\
\{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}]$$



$$\begin{aligned}
r &= \frac{i c^3 \sqrt{\theta}}{(c-v)(c+v) \sqrt{-4\pi + \theta}} = \\
&\left( i c^3 \sqrt{\theta} \right) / \left( \left( c - \left( \sqrt{(-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) \right) / \right. \\
&\quad \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \Big) \\
&\quad \left( c + \left( \sqrt{(-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) \right) / \\
&\quad \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \Big) \sqrt{-4\pi + \theta} \\
v &= \left( \sqrt{(-1.1294090667581471 \cdot \theta + 8.987551787368176 \cdot \theta^2 + 3.5481432270250993 \cdot \sin[\beta]^2)} \right) / \\
&\quad \left( \sqrt{-12.566370614359172 \cdot \theta + \theta^2 + 39.47841760435743 \cdot \sin[\beta]^2} \right) \\
\theta &= 2 \left( \pi + \sqrt{\pi^2 - \pi^2 \sin[\beta]^2} \right) = \frac{4\pi}{3} - (-4\pi^2 + 12\pi^2 \sin[\beta]^2) / \\
&\quad \left( 6 \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \right) + \\
&\quad \frac{2}{3} \left( -\pi^3 + 18\pi^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\pi^6 \sin[\beta]^2 + 11\pi^6 \sin[\beta]^4 + \pi^6 \sin[\beta]^6} \right)^{1/3} \\
&\text{30 - 60 - 90 relativistic says hold.} \\
h &:= (6.62606896 * 10^{\wedge} - 34)
\end{aligned}$$

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Shrinivasa Ramanujan' s Melody combined with a few solutions for pi and then visualized.

What does this look like in terms of the ratio between beta and

$$\text{theta} \left( \frac{\sqrt{5}}{1 + \sqrt[5]{(5^{\wedge} (3/4))} \left( \left( \frac{\sqrt{5}-1}{2} \right)^{\wedge} (5/2) \right)} - \left( \frac{\sqrt{5}+1}{2} \right) \right) e^{\wedge} \left( (2\pi) / \sqrt{5} \right) ?$$

$$\text{Solve}\left[\theta == \frac{4\alpha}{3} - (-4\alpha^2 + 12\alpha^2 \sin[\beta]^2) / \left(6 \left(-\alpha^3 + 18\alpha^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\alpha^6 \sin[\beta]^2 + 11\alpha^6 \sin[\beta]^4 + \alpha^6 \sin[\beta]^6}\right)^{1/3}\right) + \frac{2}{3} \left(-\alpha^3 + 18\alpha^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\alpha^6 \sin[\beta]^2 + 11\alpha^6 \sin[\beta]^4 + \alpha^6 \sin[\beta]^6}\right)^{1/3}, \beta\right]$$

$$\left\{\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{1}{\sqrt{3}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{1}{\sqrt{3}}\right]\right\}, \right.$$

$$\left.\left\{\beta \rightarrow -\text{ArcSin}\left[\frac{\sqrt{4\alpha^2\theta - 4\alpha\theta^2 + \theta^3}}{\sqrt{16\alpha^3 - 4\alpha^2\theta}}\right]\right\}, \left\{\beta \rightarrow \text{ArcSin}\left[\frac{\sqrt{4\alpha^2\theta - 4\alpha\theta^2 + \theta^3}}{\sqrt{16\alpha^3 - 4\alpha^2\theta}}\right]\right\}\right\}$$

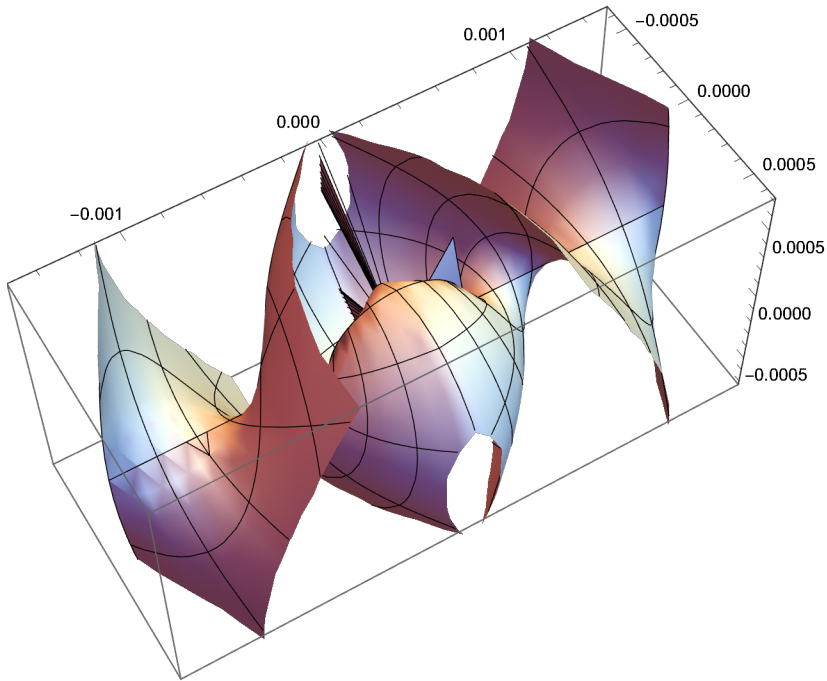
$$\text{Solve}\left[\beta == \text{ArcSin}\left[\frac{\sqrt{4\alpha^2\theta - 4\alpha\theta^2 + \theta^3}}{\sqrt{16\alpha^3 - 4\alpha^2\theta}}\right], \alpha\right]$$

$$\left\{\left\{\alpha \rightarrow \frac{1}{12} \theta \csc[\beta]^2 (1 + \sin[\beta]^2) - \left(\csc[\beta]^2 (192\theta^2 \sin[\beta]^2 - 16\theta^2 (1 + \sin[\beta]^2)^2)\right) / \left(192 (\theta^3 - 15\theta^3 \sin[\beta]^2 + 39\theta^3 \sin[\beta]^4 + \theta^3 \sin[\beta]^6 + 6\sqrt{3} \sqrt{-\theta^6 \sin[\beta]^6 + 11\theta^6 \sin[\beta]^8 + \theta^6 \sin[\beta]^{10}})^{1/3}\right) + \frac{1}{12} \csc[\beta]^2 (\theta^3 - 15\theta^3 \sin[\beta]^2 + 39\theta^3 \sin[\beta]^4 + \theta^3 \sin[\beta]^6 + 6\sqrt{3} \sqrt{-\theta^6 \sin[\beta]^6 + 11\theta^6 \sin[\beta]^8 + \theta^6 \sin[\beta]^{10}})^{1/3}\right\}, \left\{\alpha \rightarrow \frac{1}{12} \theta \csc[\beta]^2 (1 + \sin[\beta]^2) + \left((1 + i\sqrt{3}) \csc[\beta]^2 (192\theta^2 \sin[\beta]^2 - 16\theta^2 (1 + \sin[\beta]^2)^2)\right) / \left(384 (\theta^3 - 15\theta^3 \sin[\beta]^2 + 39\theta^3 \sin[\beta]^4 + \theta^3 \sin[\beta]^6 + 6\sqrt{3} \sqrt{-\theta^6 \sin[\beta]^6 + 11\theta^6 \sin[\beta]^8 + \theta^6 \sin[\beta]^{10}})^{1/3}\right) - \frac{1}{24} (1 - i\sqrt{3}) \csc[\beta]^2 (\theta^3 - 15\theta^3 \sin[\beta]^2 + 39\theta^3 \sin[\beta]^4 + \theta^3 \sin[\beta]^6 + 6\sqrt{3} \sqrt{-\theta^6 \sin[\beta]^6 + 11\theta^6 \sin[\beta]^8 + \theta^6 \sin[\beta]^{10}})^{1/3}\right\}, \left\{\alpha \rightarrow \frac{1}{12} \theta \csc[\beta]^2 (1 + \sin[\beta]^2) + \left((1 - i\sqrt{3}) \csc[\beta]^2 (192\theta^2 \sin[\beta]^2 - 16\theta^2 (1 + \sin[\beta]^2)^2)\right) / \left(384 (\theta^3 - 15\theta^3 \sin[\beta]^2 + 39\theta^3 \sin[\beta]^4 + \theta^3 \sin[\beta]^6 + 6\sqrt{3} \sqrt{-\theta^6 \sin[\beta]^6 + 11\theta^6 \sin[\beta]^8 + \theta^6 \sin[\beta]^{10}})^{1/3}\right) - \frac{1}{24} (1 + i\sqrt{3}) \csc[\beta]^2 (\theta^3 - 15\theta^3 \sin[\beta]^2 + 39\theta^3 \sin[\beta]^4 + \theta^3 \sin[\beta]^6 + 6\sqrt{3} \sqrt{-\theta^6 \sin[\beta]^6 + 11\theta^6 \sin[\beta]^8 + \theta^6 \sin[\beta]^{10}})^{1/3}\right\}\right\}$$



$$\begin{aligned}
& \text{Solve}\left[\theta == \frac{4\alpha}{3} - (-4\alpha^2 + 12\alpha^2 \sin[\beta]^2) / \right. \\
& \quad \left(6 \left(-\alpha^3 + 18\alpha^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\alpha^6 \sin[\beta]^2 + 11\alpha^6 \sin[\beta]^4 + \alpha^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left(-\alpha^3 + 18\alpha^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\alpha^6 \sin[\beta]^2 + 11\alpha^6 \sin[\beta]^4 + \alpha^6 \sin[\beta]^6}\right)^{1/3}, \alpha\right] \\
& \text{Solve}\left[2 \left(\alpha + \sqrt{\alpha^2 - \alpha^2 \sin[\beta]^2}\right) == \frac{4\pi}{3} - (-4\alpha^2 + 12\alpha^2 \sin[\beta]^2) / \right. \\
& \quad \left(6 \left(-\alpha^3 + 18\alpha^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\alpha^6 \sin[\beta]^2 + 11\alpha^6 \sin[\beta]^4 + \alpha^6 \sin[\beta]^6}\right)^{1/3} \right) + \\
& \quad \left. \frac{2}{3} \left(-\alpha^3 + 18\alpha^3 \sin[\beta]^2 + 3\sqrt{3} \sqrt{-\alpha^6 \sin[\beta]^2 + 11\alpha^6 \sin[\beta]^4 + \alpha^6 \sin[\beta]^6}\right)^{1/3}, \alpha\right] \\
& \text{Solve}\left[2 \left(\alpha + \sqrt{\alpha^2 - \alpha^2 \sin[\beta]^2}\right) == \theta, \alpha\right] \\
& \left\{\left\{\alpha \rightarrow \frac{1}{8} \csc[\beta]^2 \left(4\theta - 4\sqrt{\theta^2 - \theta^2 \sin[\beta]^2}\right)\right\}, \left\{\alpha \rightarrow \frac{1}{2} \left(\theta \csc[\beta]^2 + \csc[\beta]^2 \sqrt{\theta^2 - \theta^2 \sin[\beta]^2}\right)\right\}\right\} \\
& \text{SphericalPlot3D}\left[\left(\frac{\sqrt{5}}{1 + \sqrt[3]{(5 \wedge (3/4))} \left(\left(\frac{\sqrt{5}-1}{2}\right) \wedge (5/2)\right)} - \left(\frac{\sqrt{5}+1}{2}\right)\right) e^{\left(2 \times \right.} \right. \\
& \quad \left.\left.\left(\frac{1}{2} \left(\theta \csc[\beta]^2 + \csc[\beta]^2 \sqrt{\theta^2 - \theta^2 \sin[\beta]^2}\right) / \sqrt{5}\right)\right), \{\beta, -\pi, \pi\}, \{\theta, -2\pi, 2\pi\}\right]
\end{aligned}$$

$\text{SphericalPlot3D}\left[\left(\frac{\sqrt{5}}{1 + \sqrt[5]{(5 \wedge (3/4)) \left(\left(\frac{\sqrt{5}-1}{2}\right) \wedge (5/2)\right)} - \left(\frac{\sqrt{5}+1}{2}\right)}\right) e^{\left(2 \times \left(\frac{1}{8} \text{Csc}[\beta]^2 \left(4 \theta - 4 \sqrt{\theta^2 - \theta^2 \text{Sin}[\beta]^2}\right)\right)}\right) / \sqrt{5}}, \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$



$$\text{SphericalPlot3D}\left[\left(\frac{\sqrt{5}}{1 + \sqrt[5]{(5^{\wedge}(3/4)) \left(\left(\frac{\sqrt{5}-1}{2}\right)^{\wedge}(5/2)\right)}} - \left(\frac{\sqrt{5}+1}{2}\right)\right) e^{\wedge}\left(2 \times\right.\right. \\ \left.\left.\left(\frac{1}{2} \left(\theta \text{Csc}[\beta]^2 + \text{Csc}[\beta]^2 \sqrt{\theta^2 - \theta^2 \text{Sin}[\beta]^2}\right) / \sqrt{5}\right)\right), \{\beta, -\pi, \pi\}, \{\theta, -2 \pi, 2 \pi\}\right]$$